

# Charmonia, open charm states, exotica, and deconfinement

**new developments in the framework of the SHMc**  
(SHMc = statistical hadronization model with charm)



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Heavy Flavor Transport in QCD Matter  
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# the multiple-charm hierarchy in the statistical hadronization model

results shown in this talk: A. Andronic, P. Braun-Munzinger, J. Stachel, M. Koehler,  
A. Mazeliauskas, K. Redlich, V. Vislavicius, arXiv:2104.12754

focus on production of open (multi)-charm hadrons at LHC energy  
collision systems: Pb-Pb, Xe-Xe, Kr-Kr, Ar-Ar, O-O  
production yields, rapidity and transverse momentum distributions

# the mechanism for statistical hadronization with charm (SHMc)

[Braun-Munzinger and Stachel, PLB 490 (2000) 196]

[Andronic, Braun-Munzinger and Stachel, NPA 789 (2007) 334]

- ▶ Charm quarks are produced in initial hard scatterings ( $m_{c\bar{c}} \gg T_c$ ) and production can be described by pQCD ( $m_{c\bar{c}} \gg \Lambda_{\text{QCD}}$ )
- ▶ Charm quarks survive and *thermalise* in the QGP
- ▶ Full screening before  $T_{\text{CF}}$
- ▶ Charmonium is formed at phase boundary (together with other hadrons)
- ▶ Thermal model input ( $T_{\text{CF}}, \mu_b \rightarrow n_X^{\text{th}}$ )

$$N_{c\bar{c}}^{\text{dir}} = \underbrace{\frac{1}{2} g_c V \left( \sum_i n_{D_i}^{\text{th}} + n_{\Lambda_i}^{\text{th}} + \dots \right)}_{\text{Open charm}} + \underbrace{g_c^2 V \left( \sum_i n_{\psi_i}^{\text{th}} + n_{\chi_i}^{\text{th}} + \dots \right)}_{\text{Charmonia}}$$

- ▶ Canonical correction is applied to  $n_{\text{oc}}^{\text{th}}$
- ▶ Outcome  $N_{J/\psi}, N_D, \dots$

core-corona picture: treat low density part of nuclear overlap region, where a nucleon undergoes 1 or less collisions as pp collisions, use measured pp cross section scaled by  $T_{\text{AA}}$

# statistical hadronization model for charm (SHMc) including canonical thermodynamics

- selected early references:

1. P. Braun-Munzinger, J. Stachel: Phys. Lett. B 490 (2000) 196-202, nucl-th/0007059
2. M. Gorenstein, A.P. Kostyuk, H. Stoecker, W. Greiner, Phys.Lett.B 524 (2002) 265-272, hep-ph/0104071
3. A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel, Phys. Lett. B 571 (2003) 36-44, nucl-th/0303036
4. F. Becattini, Phys.Rev.Lett. 95 (2005) 022301, hep-ph/0503239
5. A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel, Nucl.Phys.A 789 (2007) 334-356, nucl-th/0611023
6. P. Braun-Munzinger, J. Stachel: Nature 448 (2007) 302-309
7. A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel, Phys.Lett.B 652 (2007) 259-261, nucl-th/0701079
8. P. Braun-Munzinger, J. Stachel: Landolt-Bornstein 23 (2010) 424, 0901.2500

the beginning  
SPS/RHIC  
open/hidden charm  
multi-charm baryons  
detailing the model  
LHC predictions  
rapidity dependence  
deconfined c quarks

- the charm balance eq. developed in 1., 2., and 3. determines the fugacity  $g_c$

$$N_{c\bar{c}} = \frac{1}{2} g_c N_{oc}^{th} \frac{I_1(g_c N_{oc}^{th})}{I_0(g_c N_{oc}^{th})} + g_c^2 N_{c\bar{c}}^{th}$$

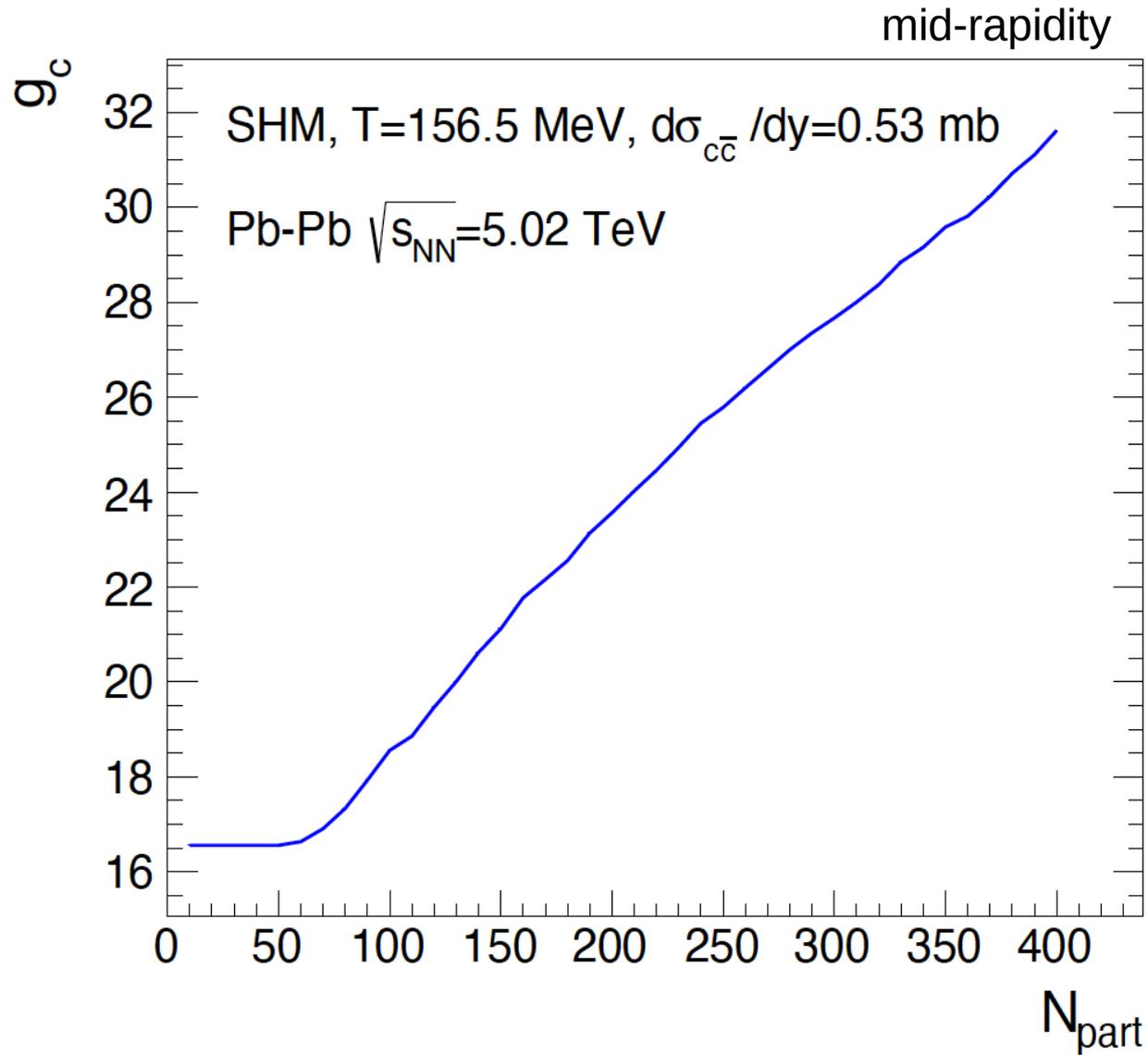
obtained from measured  
open charm cross section

$N_{oc}^{th}$ : # of thermal open charm hadrons

- balance equation with canonical suppression needs to be solved numerically to obtain  $g_c$

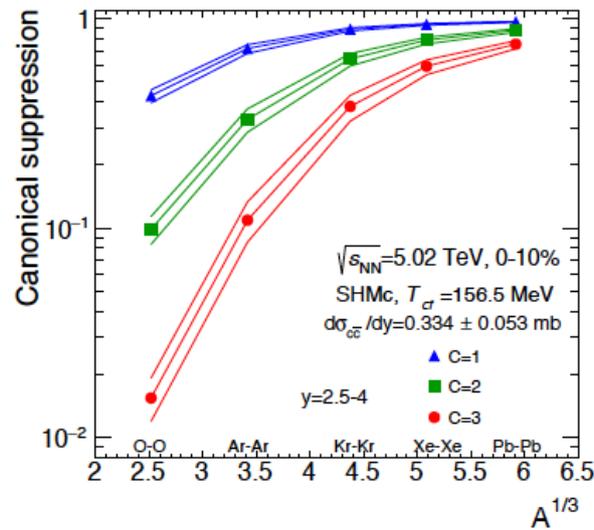
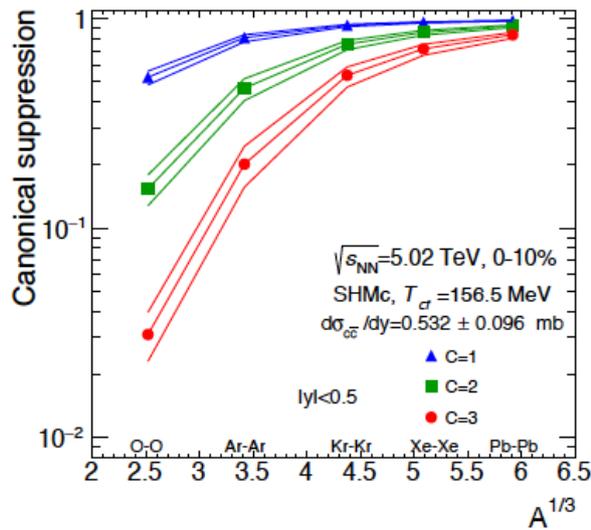
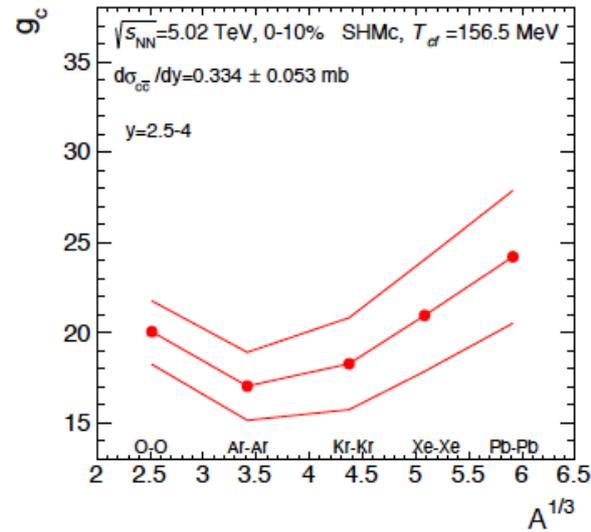
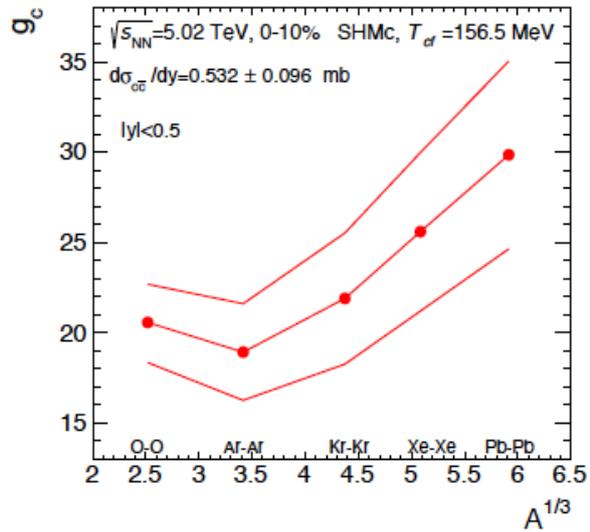
- for yields of charm hadron  $i$  with  $n_c$  charm quarks  $N_{n_c}(i) = g_c^{n_c} N_{n_c}(i)^{th} \frac{I_{n_c}(g_c N_{oc}^{th})}{I_0(g_c N_{oc}^{th})}$

# centrality dependence of charm fugacity $g_c$ at LHC energy



# charm fugacities and canonical suppression factors

different collision systems:



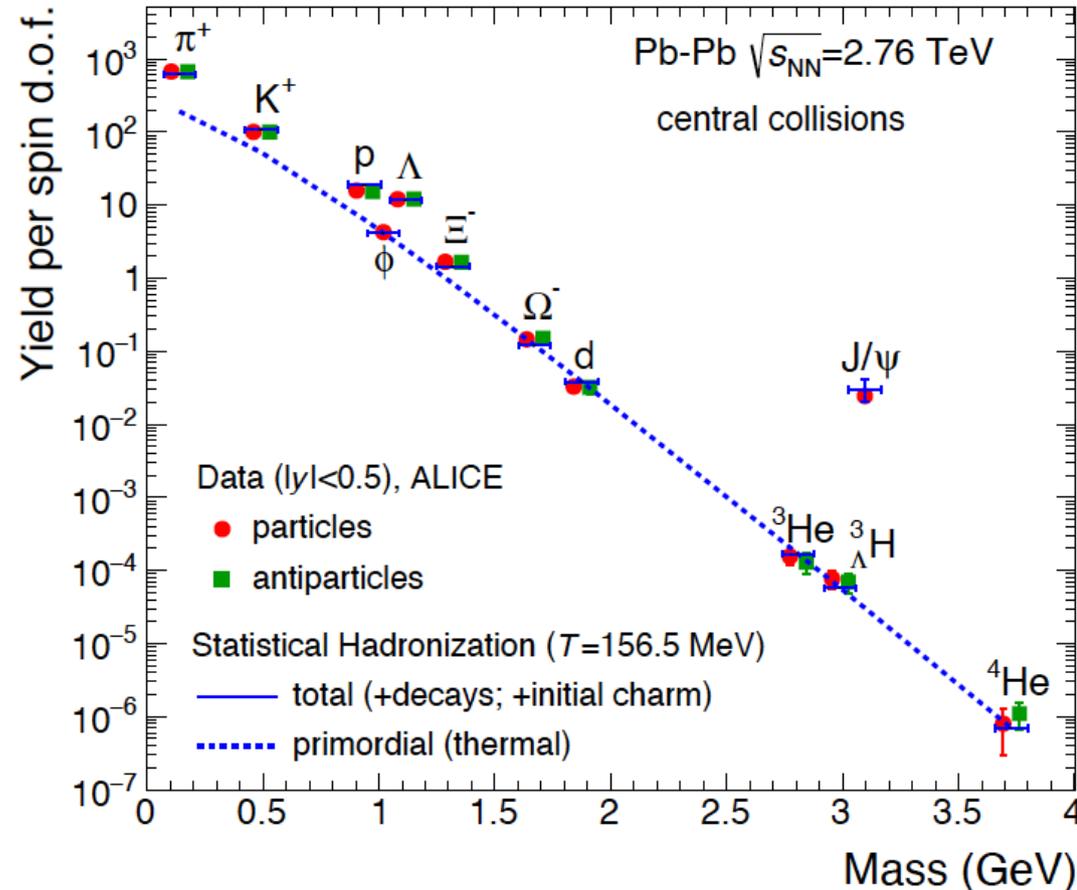
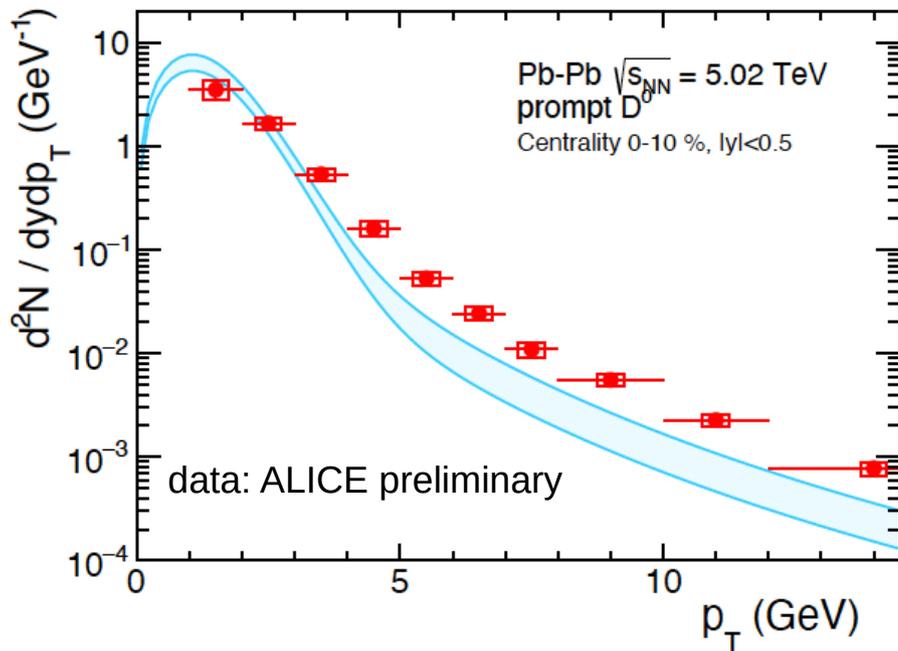
# statistical hadronization for hidden and open charm

J/ψ enhanced compared to other M = 3 GeV hadrons since number of c-quarks is about 30 times larger than expected for pure thermal production at T = 156 MeV due to production in initial hard collisions and subsequent thermalization in the fireball.

production probability scales with  $N_{c\bar{c}}$ <sup>2</sup>

enhancement factor is 900 for J/ψ

enhancement factor is 30 for D<sup>0</sup>



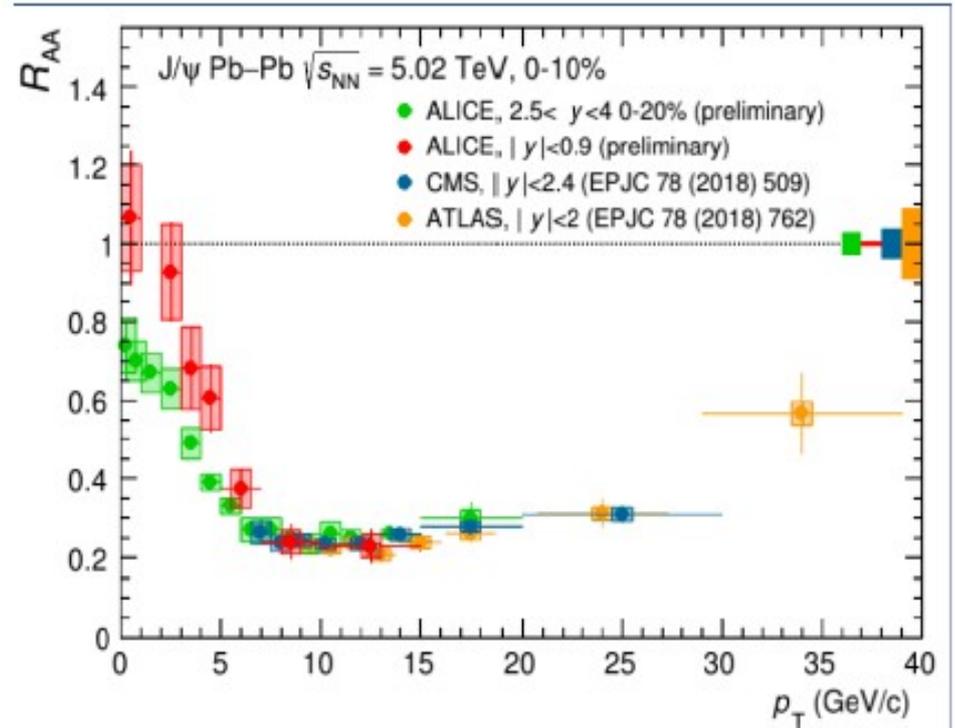
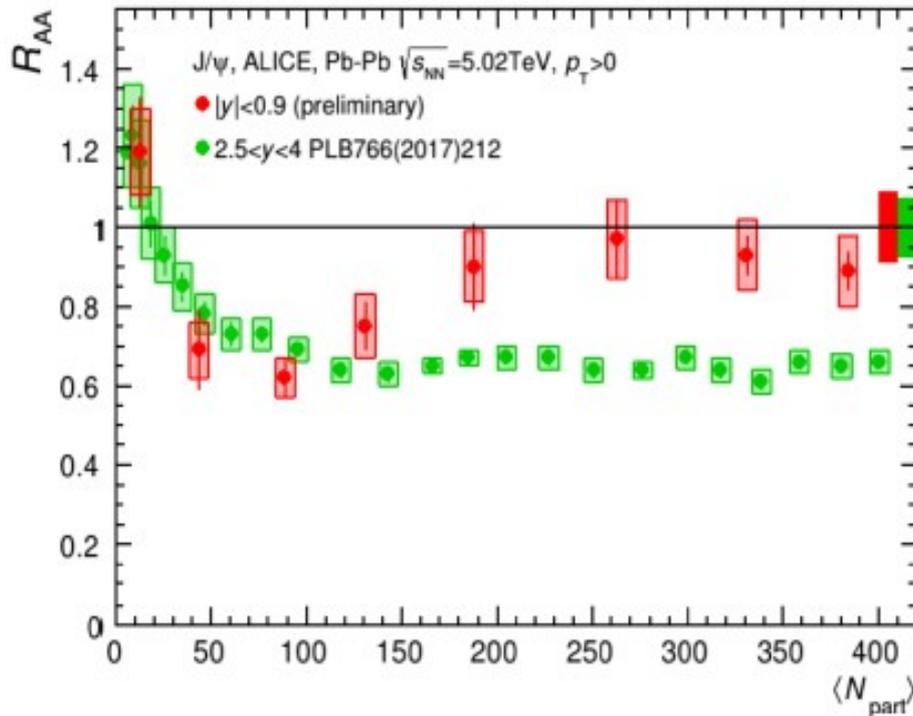
Andronic, Braun-Munzinger, Koehler, Redlich, JS PLB 792 (2019) 304  
 Andronic, Braun-Munzinger, Koehler, Mazeliauskas, Redlich, Stachel,  
 Vislavicius arXiv:2104.12754

quantitative agreement for open and hidden charm hadrons, same mechanism should work for all open and hidden charm hadrons, even for exotica such as  $\Omega_{ccc}$  where enhancement factor is nearly 30000  
 quantitative tests in LHC Run3/Run4

enhancement is defined relative to purely thermal value, not to pp yield

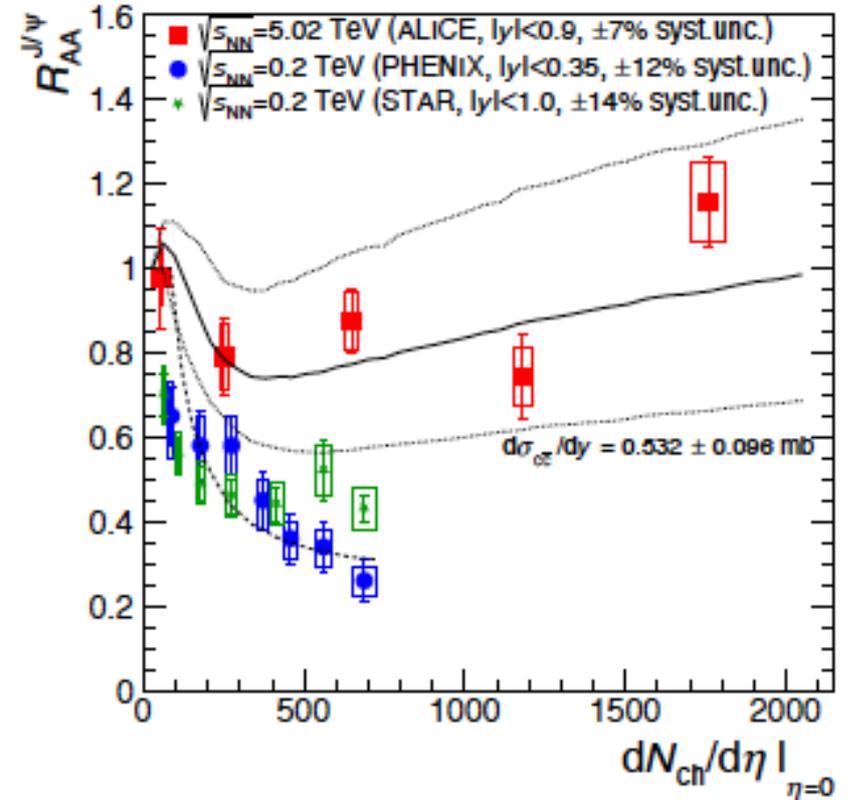
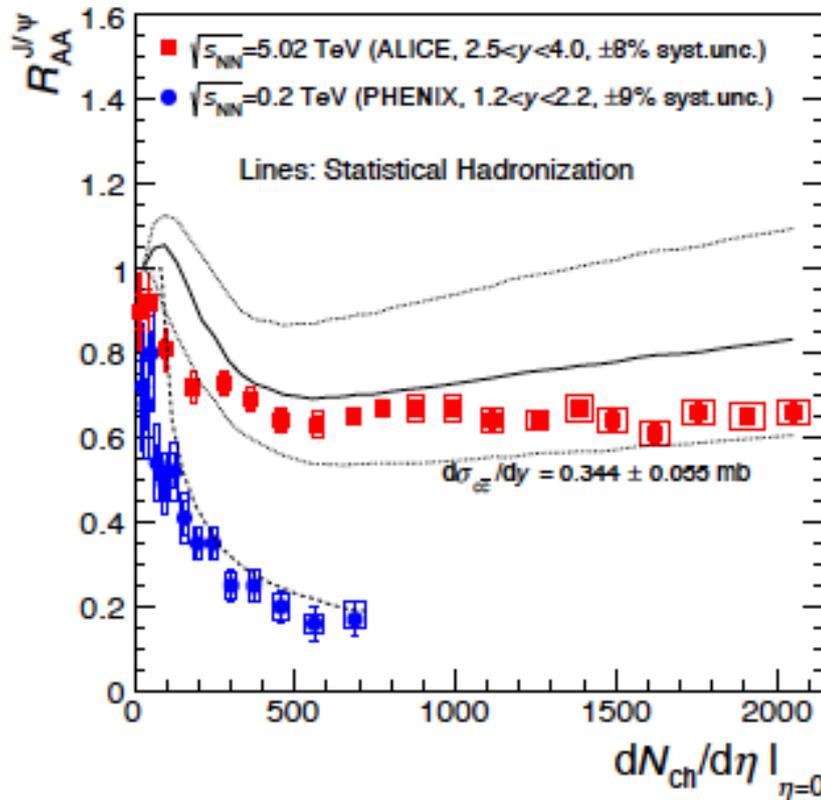
# charmonium at LHC: peaks at mid-y and strong enhancement at low transverse momentum

nuclear modification factor: 
$$R_{AA}(p_T) = \frac{dN^{AA}/dp_T}{\langle N_{\text{coll}} \rangle dN^{\text{PP}}/dp_T}$$



# RHIC and LHC data compared to SHMc predictions

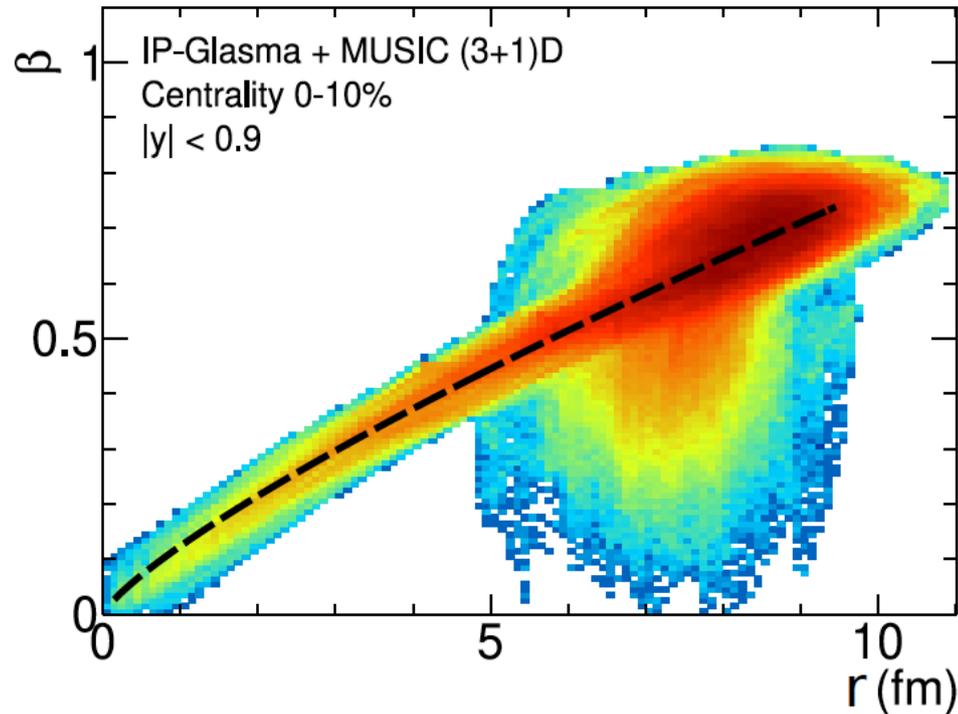
note the energy dependence of the nuclear modification factor  $R_{AA}$



the band with the model predictions at LHC energy is due to the uncertainties in the pp open charm cross section and the necessary shadowing corrections

# beyond yields: transverse momentum distributions

assume thermalization of charm quarks in QGP, charm quarks follow collective flow  
use hydro velocity profile at pseudocritical temperature from MUSIC (3+1) D  
tuned to light flavor observables



$$\beta(r) = \beta_{\max} \frac{r^n}{r_{\max}^n}$$

$$\beta_{\max} = 0.62$$

$$n = 0.85$$

$$V = 2\pi \int_0^{r_{\max}} dr r \tau(r) u^\tau \left[ 1 - \beta(r) \frac{\partial \tau}{\partial r} \right]$$

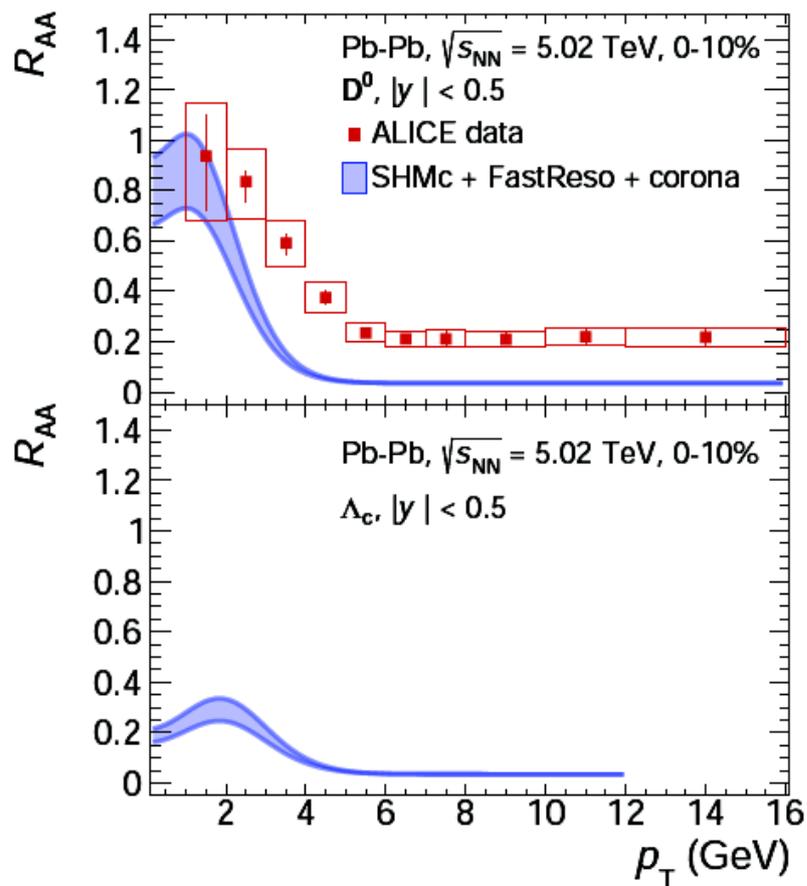
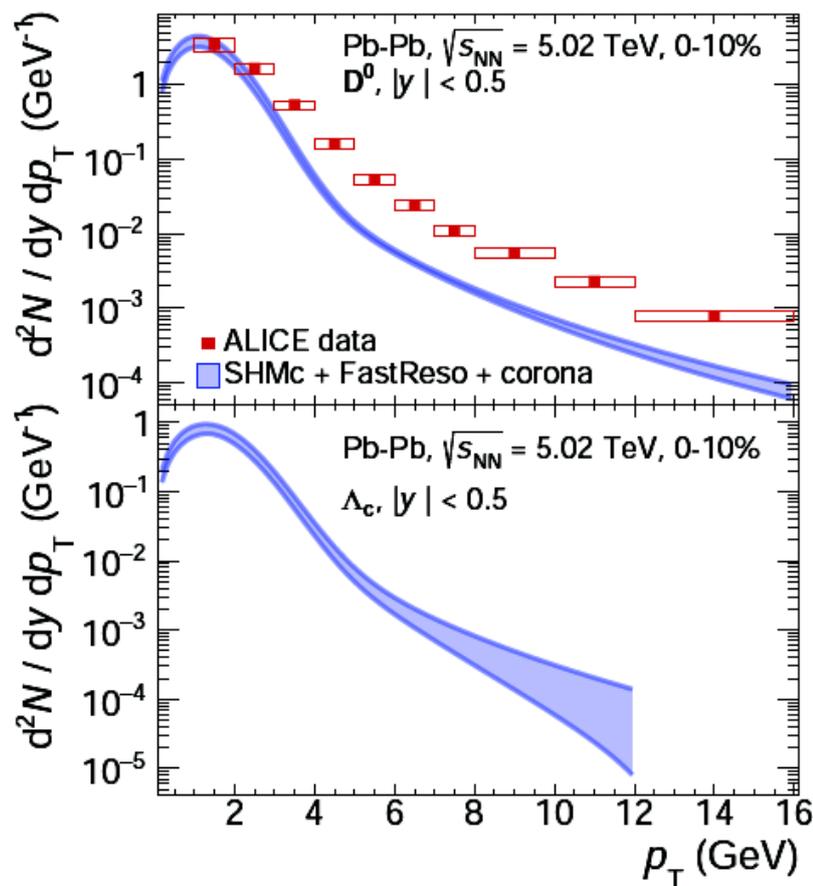
$$V = 4997 \text{ fm}^3$$

and blast wave parametrization of spectral shape with  $T = 156.5 \text{ MeV}$  and  
a fireball volume per unit rapidity for central PbPb collisions  $V = 4997 \text{ fm}^3$   
sensitivity to shape of freeze-out surface: backup

# spectra and $R_{AA}$ of $D^0$ mesons and $\Lambda_c$ baryons

for open heavy flavor hadrons strong contribution from resonance decays

- include all known charm hadron states as of PDG2020 in SHMc
- compute decay spectra with FastReso: 76 2-body and 10 3-body decays  
(A. Mazeliauskas, S. Floerchinger, E. Grossi, D. Teaney, EPJ C79 (2019) 284 arXiv: 1809.11049)



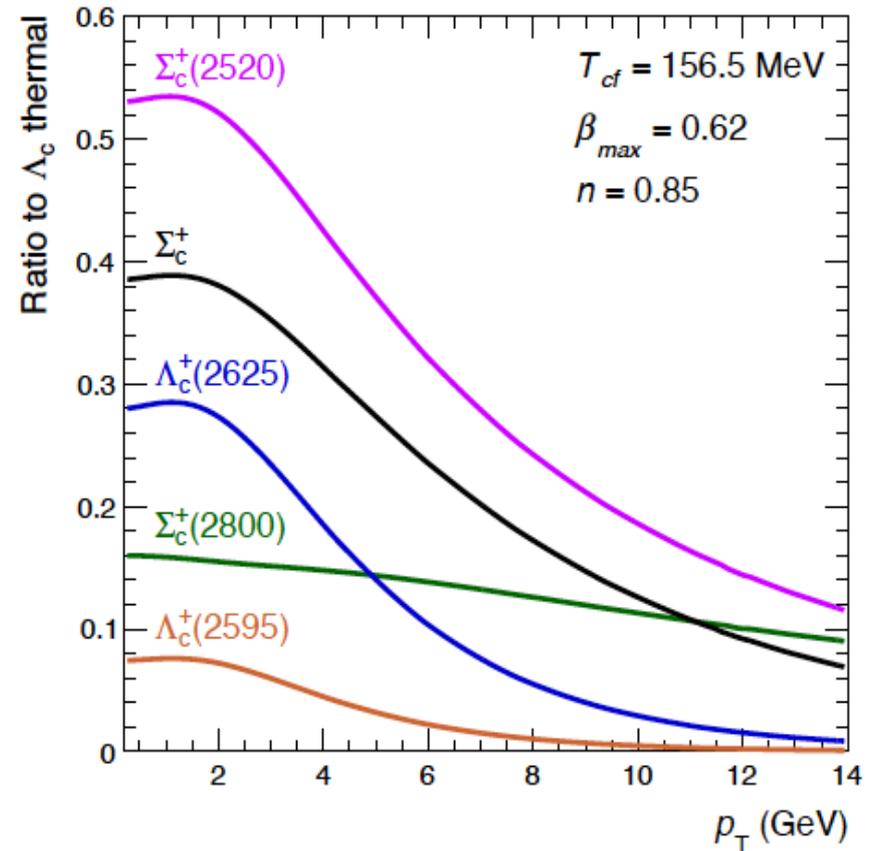
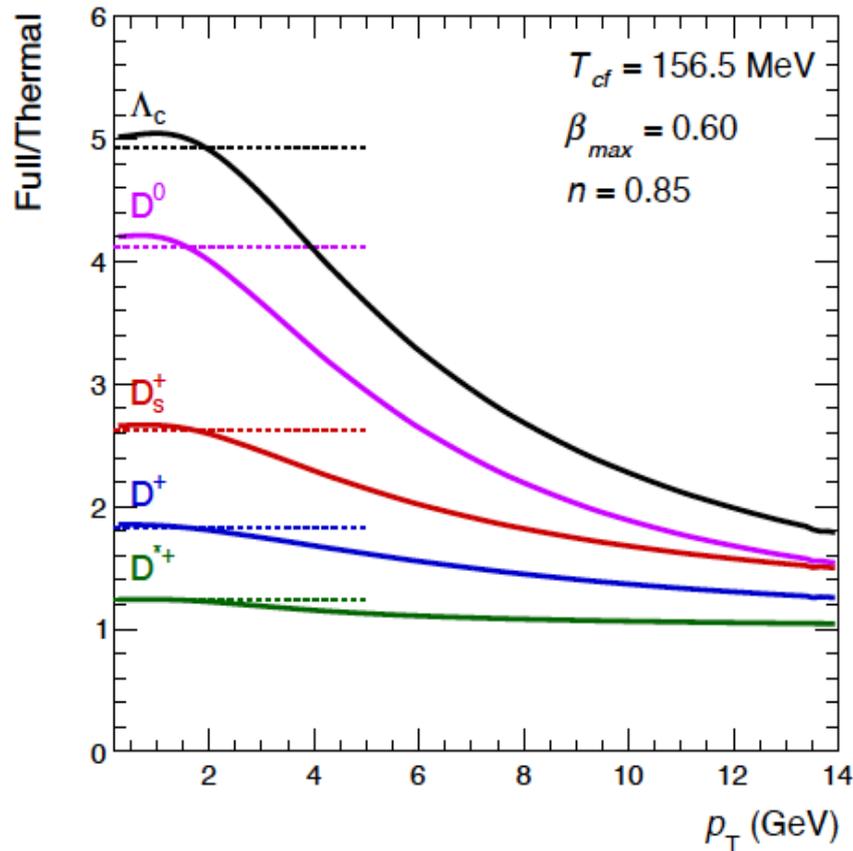
$\Lambda_c$  data exist but are not (yet) cleared by ALICE

# impact of resonance decays

$D_0$  quadrupled by strong decays

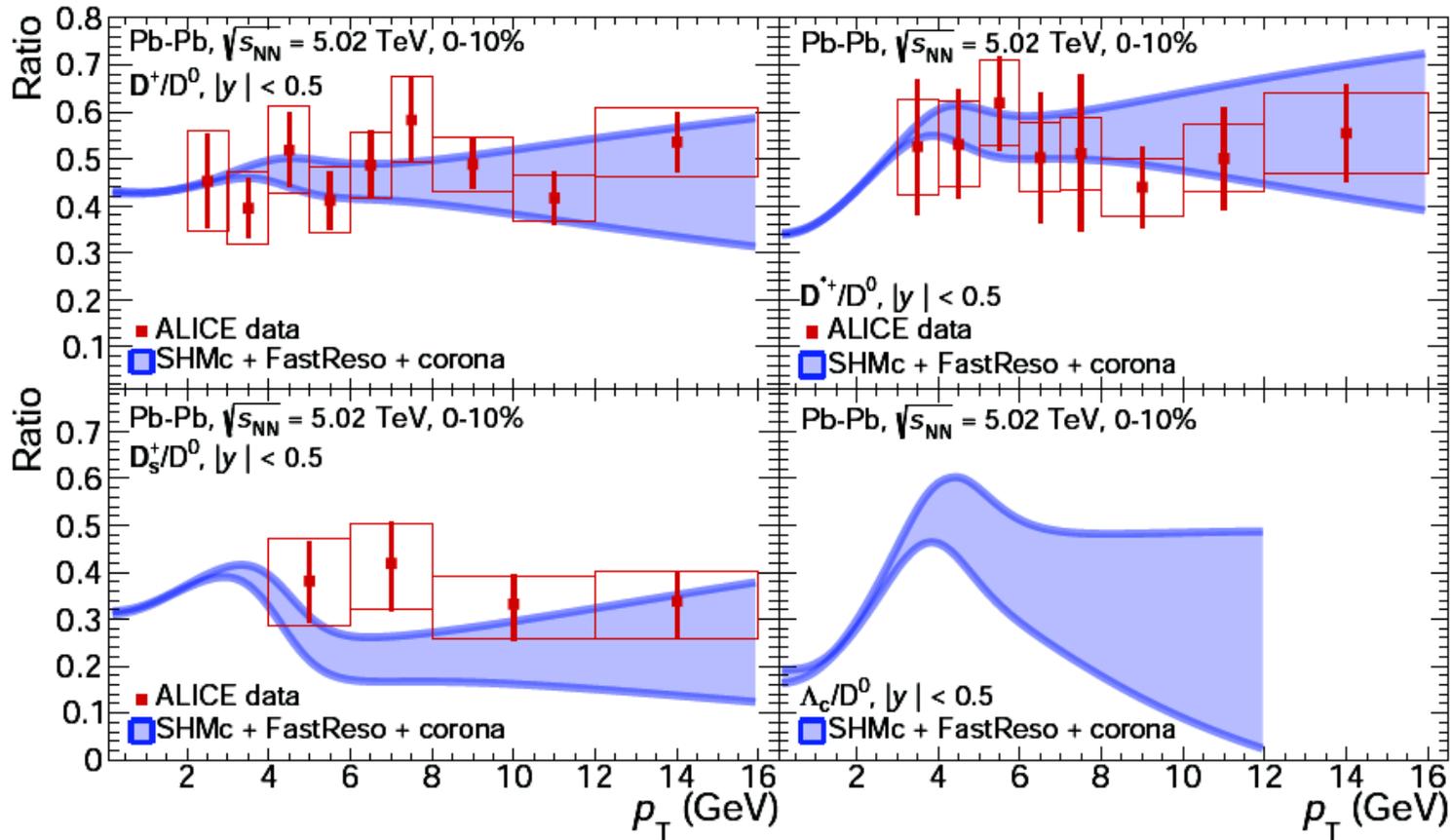
$\Lambda_c$  5 times as many after strong decays

feed-down to  $\Lambda_c$



but: beyond 4 GeV corona dominates, hence change in shape not very visible

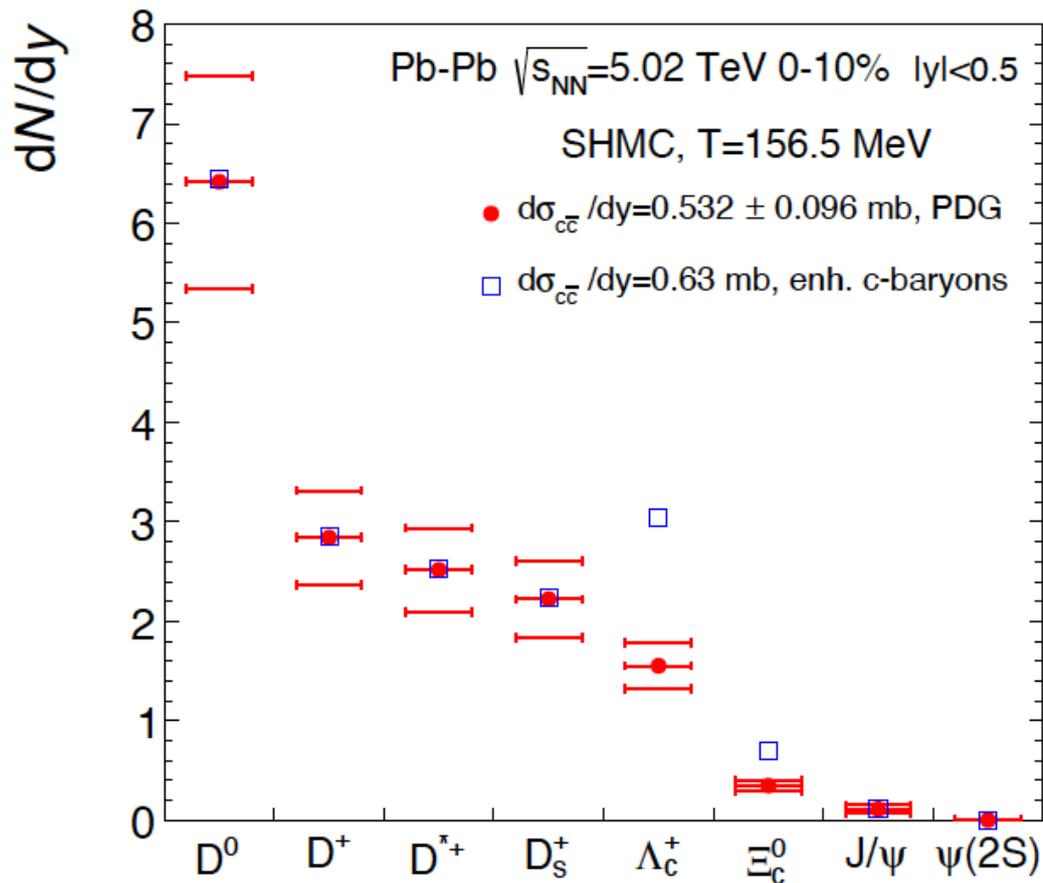
# ratios of charm hadron to $D^0$ spectra



excellent agreement considering that there are NO free parameters

# charm hadron yields with modified charm resonance spectrum

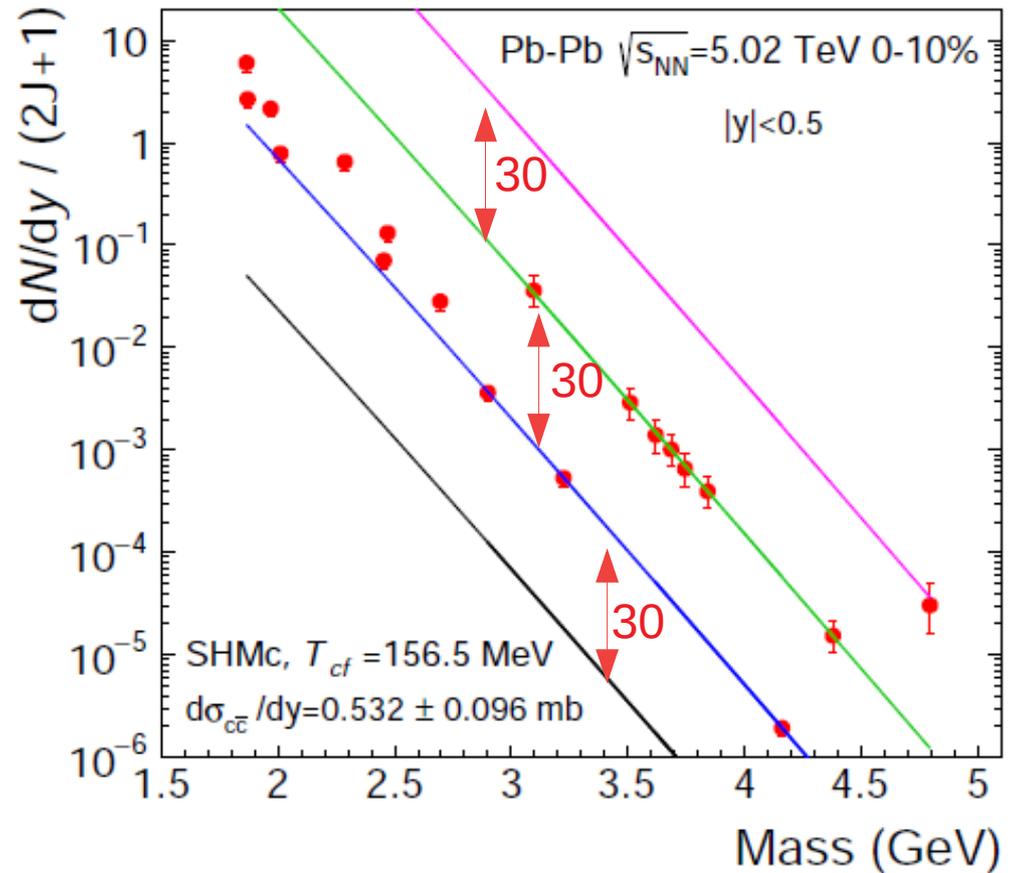
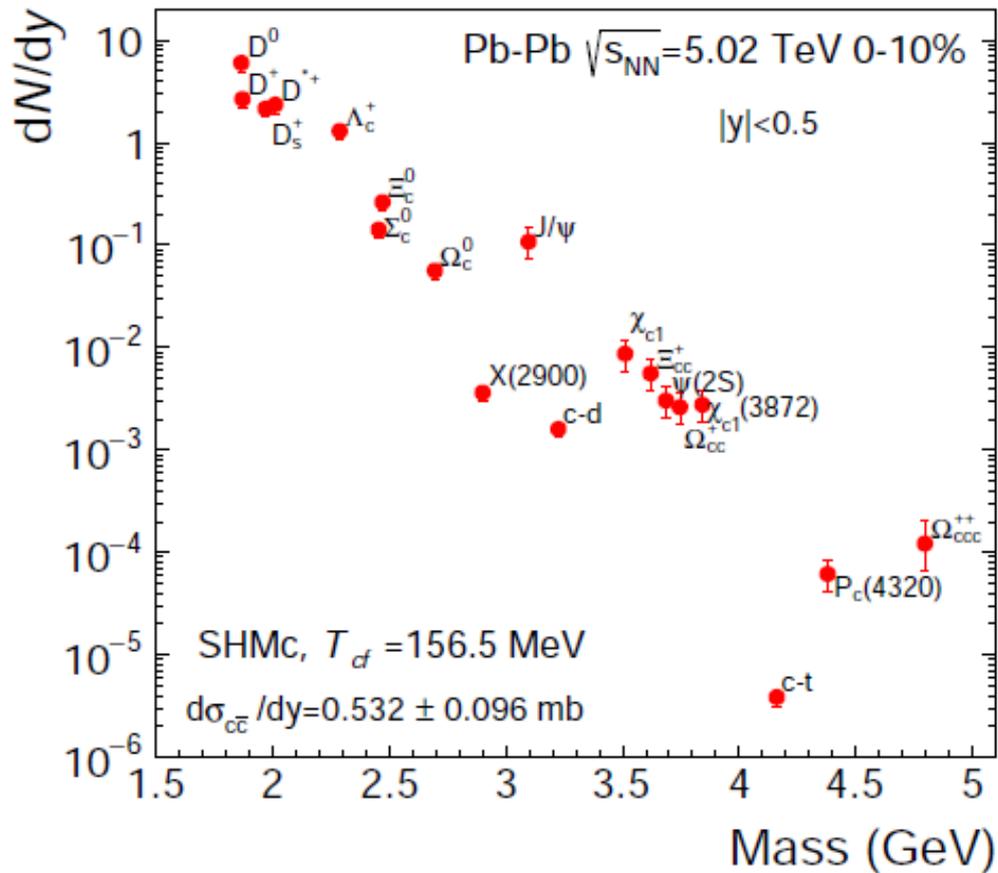
recently a lot of speculation about possibly incomplete charm baryon spectrum  
to test impact, tripled statistical weights of excited charm baryons



charm cross section increases 20%  
yield of charm baryons nearly doubles  
mesons practically unaffected

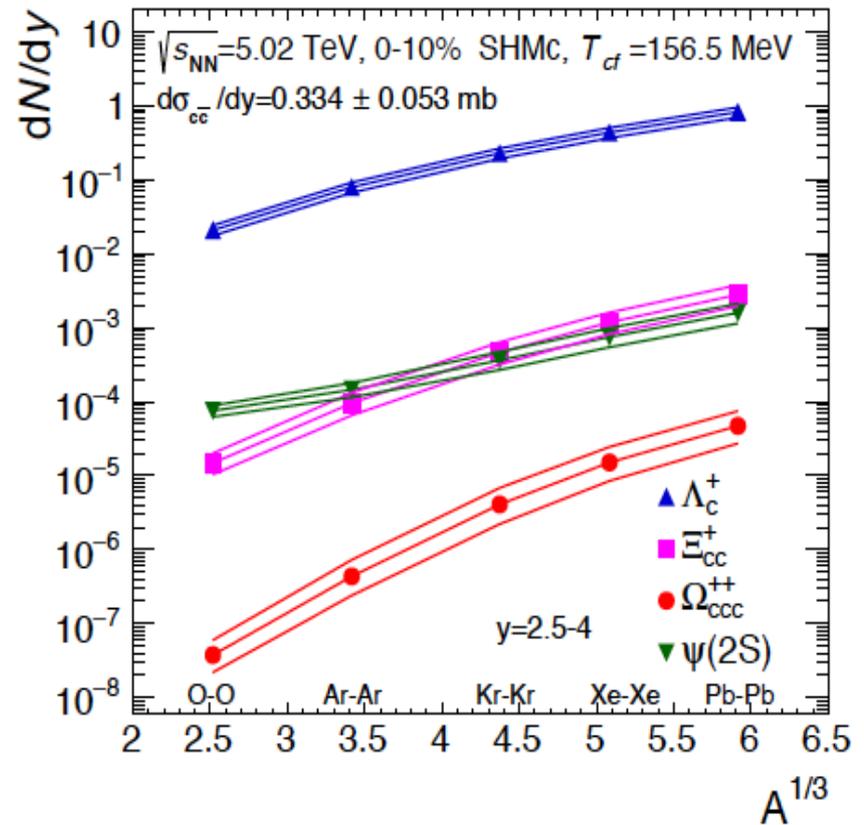
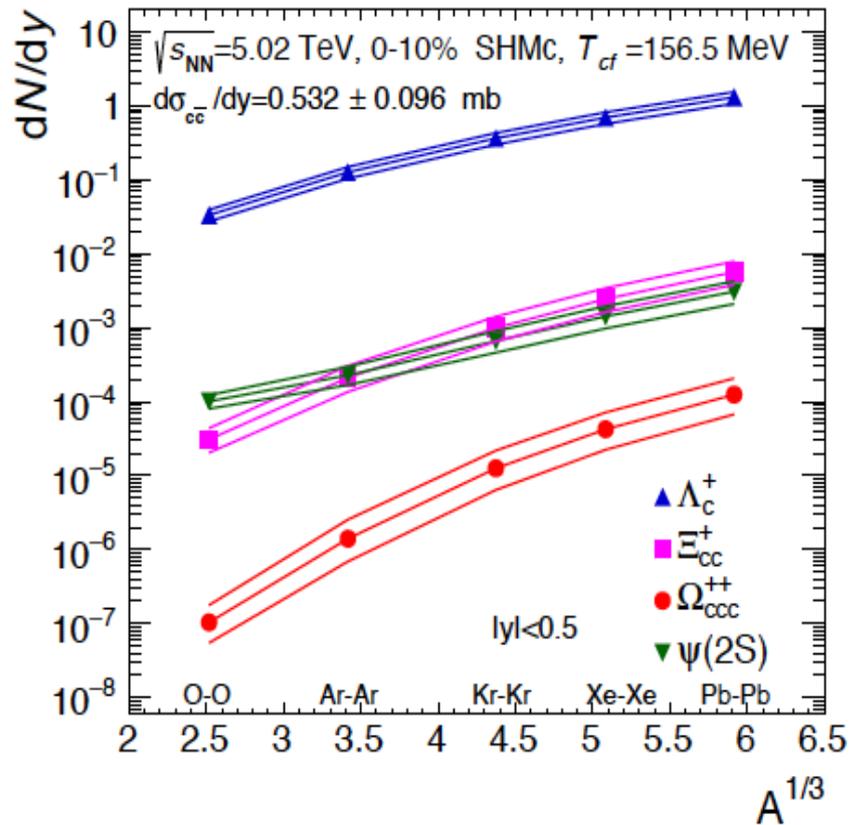
# the multi-charm hierarchy

open and hidden charm hadrons, including exotic objects, such as X-states, c-deuteron, c-triton, pentaquark,  $\Omega_{ccc}$



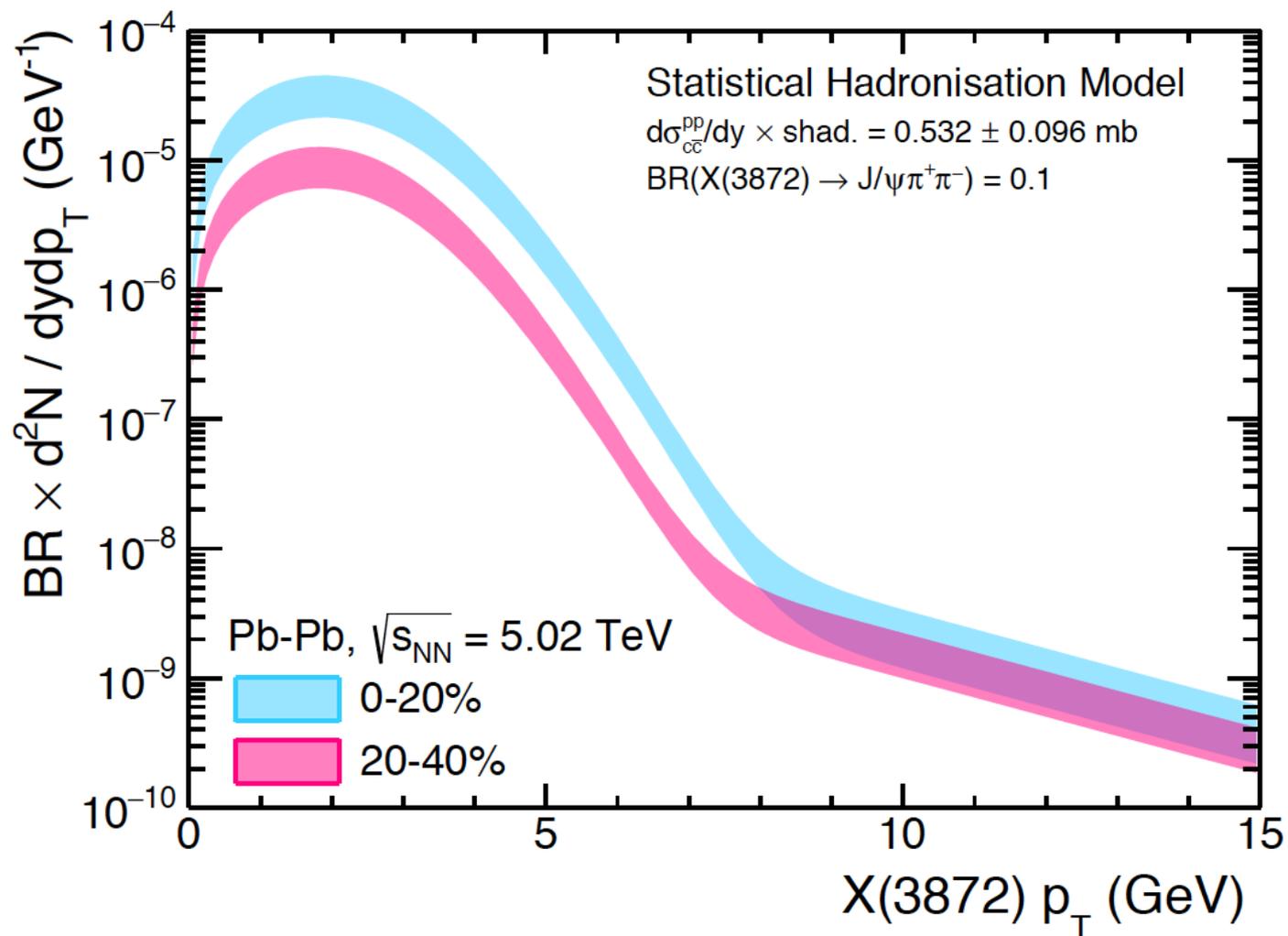
emergence of a unique pattern, due to  $g_c^n$  and mass hierarchy  
 perfect testing ground for deconfinement for LHC Runs3 and beyond

# system size dependence of yields



due to different charm quark content different canonical suppression for multicharm very light collision systems not favored

# transverse momentum spectrum for $\chi_{c1}(3872)$ in the SHMc



note: dramatic enhancement at low  $p_t$  predicted

# summary – charm production

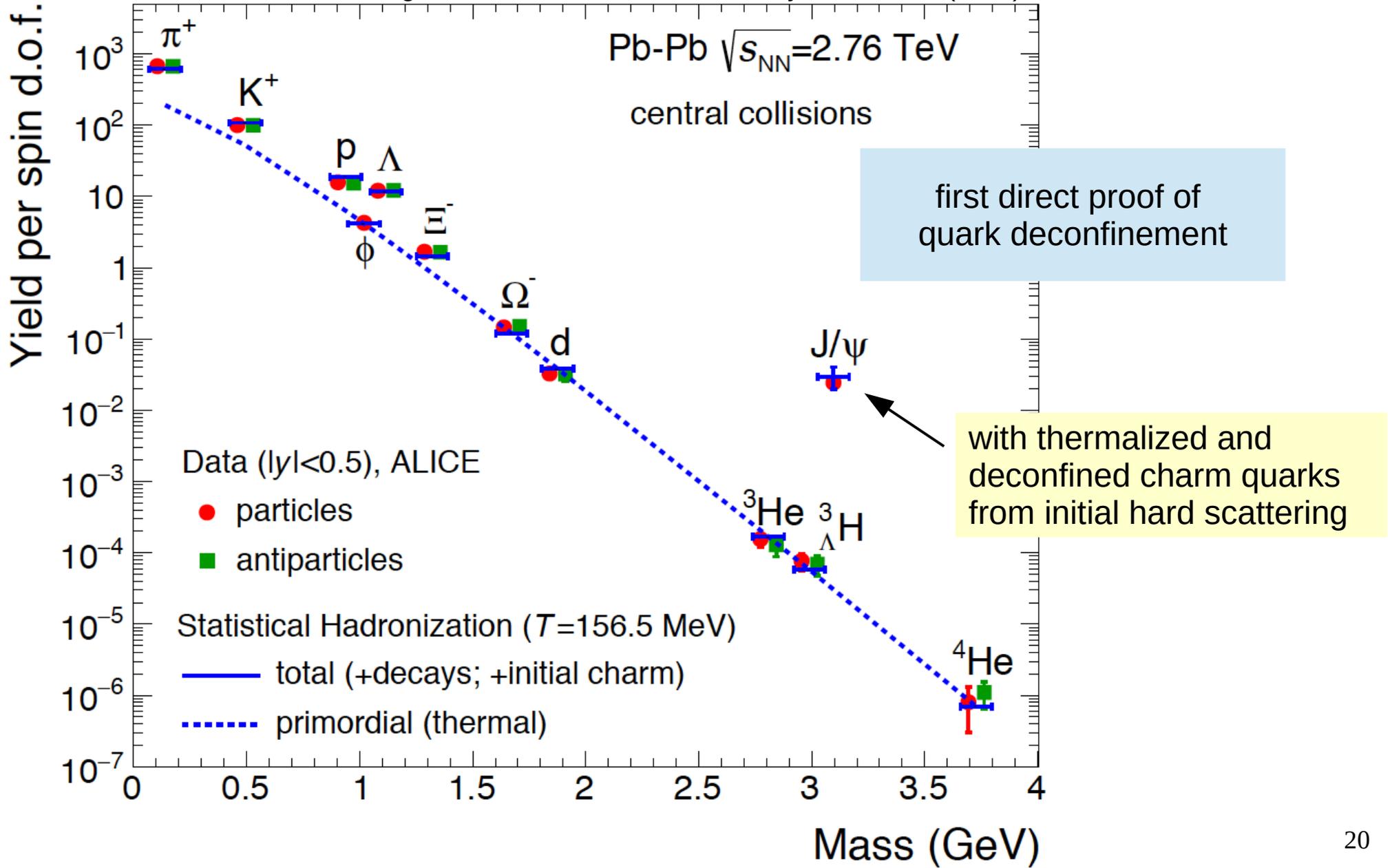
## probing the QCD phase boundary with heavy quarks

- statistical hadronization works quantitatively also for hadrons with charm quarks
  - parameter free, only external input: charm production cross section
  - treatment of open and hidden charm on an equal footing, same mechanism
  - low momentum part of spectra characterized by hydro expansion + temperature  
no fit parameter
- 
- universal hadronization for hadrons with (u,d,s,c) quarks
  - the study of open charm hadron production has just begun
  - predict  $dN/dy$  for hierarchy of multi-charm states, very large ( $> 5000$ ) enhancement expected
  - precision study of such hadrons → further insight into deconfinement and hadronization

backup

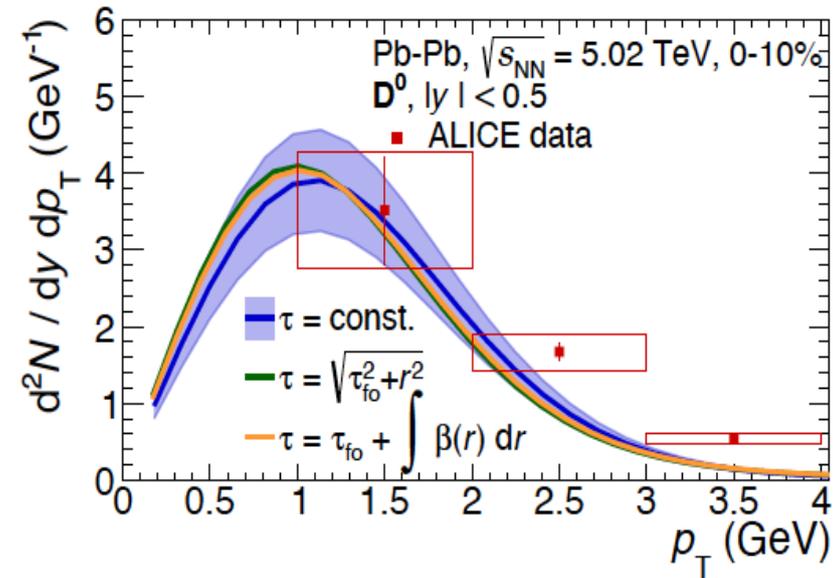
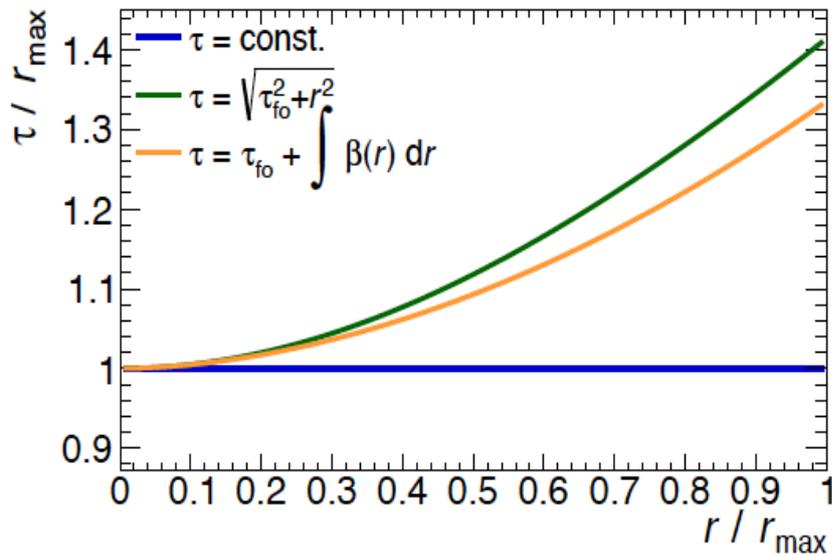
J/ψ enhancement relative to uds hadrons is prediction by SHMc for quadratic scaling in number of charm quarks, they have to travel freely over the size of the fireball of 10 fm, about 10 times the radius of a proton

Andronic, Braun-Munzinger, Koehler, Redlich, Stachel, Phys. Lett B797 (2019) 134836



# blast wave parametrization of transverse momentum spectrum

$$\begin{aligned} \frac{d^2N}{2\pi p_T dp_T dy} &= \frac{2J+1}{(2\pi)^3} \int d\sigma_\mu p^\mu f(p) \\ &= \frac{2J+1}{(2\pi)^3} \int_0^{r_{\max}} dr \tau(r) r \left[ K_1^{\text{eq}}(p_T, u^r) - \frac{\partial \tau}{\partial r} K_2^{\text{eq}}(p_T, u^r) \right] \\ K_1^{\text{eq}}(p_T, u^r) &= 4\pi m_T I_0 \left( \frac{p_T u^r}{T} \right) K_1 \left( \frac{m_T u^\tau}{T} \right) \\ K_2^{\text{eq}}(p_T, u^r) &= 4\pi p_T I_1 \left( \frac{p_T u^r}{T} \right) K_0 \left( \frac{m_T u^\tau}{T} \right) \end{aligned}$$



## mid-rapidity yields for Pb-Pb collisions

Particle	dN/dy core (SHMc)	dN/dy corona	dN/dy total
	0-10%		
$D^0$	$6.02 \pm 1.07$	$0.396 \pm 0.032$	$6.42 \pm 1.07$
$D^+$	$2.67 \pm 0.47$	$0.175 \pm 0.026$	$2.84 \pm 0.47$
$D^{*+}$	$2.36 \pm 0.42$	$0.160 +0.048-0.022$	$2.52 \pm 0.42$
$D_s^+$	$2.15 \pm 0.38$	$0.074 +0.024-0.015$	$2.22 \pm 0.38$
$\Lambda_c^+$	$1.30 \pm 0.23$	$0.250 \pm 0.028$	$1.55 \pm 0.23$
$\Xi_c^0$	$0.263 \pm 0.047$	$0.090 \pm 0.035$	$0.353 \pm 0.058$
$J/\psi$	$0.108 +0.041-0.035$	$(5.08 \pm 0.37) \cdot 10^{-3}$	$0.113 +0.041-0.035$
$\psi(2S)$	$(3.04 +1.2-1.0) \cdot 10^{-3}$	$(7.61 \pm 0.55) \cdot 10^{-4}$	$(3.80 +1.2-1.0) \cdot 10^{-3}$
	30-50%		
$D^0$	$0.857 \pm 0.153$	$0.207 \pm 0.017$	$1.06 \pm 0.154$
$D^+$	$0.379 \pm 0.068$	$0.092 \pm 0.014$	$0.471 \pm 0.069$
$D^{*+}$	$0.335 \pm 0.060$	$0.084 +0.025-0.011$	$0.419 +0.065-0.061$
$D_s^+$	$0.306 \pm 0.055$	$0.039 +0.013-0.008$	$0.344 \pm 0.056$
$\Lambda_c^+$	$0.185 \pm 0.033$	$0.131 \pm 0.015$	$0.316 \pm 0.036$
$\Xi_c^0$	$0.038 \pm 0.007$	$0.047 \pm 0.018$	$0.084 \pm 0.020$
$J/\psi$	$(1.12 +0.37-0.32) \cdot 10^{-2}$	$(2.65 \pm 0.19) \cdot 10^{-3}$	$(1.39 +0.37-0.32) \cdot 10^{-2}$
$\psi(2S)$	$(3.16 +1.04-0.89) \cdot 10^{-4}$	$(3.98 \pm 0.29) \cdot 10^{-4}$	$(7.14 +1.08-0.94) \cdot 10^{-4}$

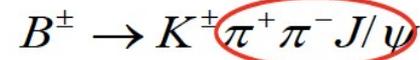
## dependence of $\Omega_{ccc}$ production yields on system size for a run time of $10^6$ s

	O-O	Ar-Ar	Kr-Kr	Xe-Xe	Pb-Pb
$\sigma_{\text{inel}}(10\%)$ mb	140	260	420	580	800
$T_{AA}(0 - 10\%)$ mb <sup>-1</sup>	0.63	2.36	6.80	13.0	24.3
$\mathcal{L}(\text{cm}^{-2}\text{s}^{-1})$	$4.5 \cdot 10^{31}$	$2.4 \cdot 10^{30}$	$1.7 \cdot 10^{29}$	$3.0 \cdot 10^{28}$	$3.8 \cdot 10^{27}$
	$d\sigma_{c\bar{c}}/dy = 0.53$ mb				
$dN_{\Omega_{ccc}}/dy$	$8.38 \cdot 10^{-8}$	$1.29 \cdot 10^{-6}$	$1.23 \cdot 10^{-5}$	$4.17 \cdot 10^{-5}$	$1.25 \cdot 10^{-4}$
$\Omega_{ccc}$ Yield	$5.3 \cdot 10^5$	$8.05 \cdot 10^5$	$8.78 \cdot 10^5$	$7.26 \cdot 10^5$	$3.80 \cdot 10^5$
	$d\sigma_{c\bar{c}}/dy = 0.63$ mb				
$dN_{\Omega_{ccc}}/dy$	$1.44 \cdot 10^{-7}$	$2.33 \cdot 10^{-6}$	$2.14 \cdot 10^{-5}$	$7.03 \cdot 10^{-5}$	$2.07 \cdot 10^{-4}$
$\Omega_{ccc}$ Yield	$9.2 \cdot 10^5$	$1.45 \cdot 10^6$	$1.53 \cdot 10^6$	$1.22 \cdot 10^6$	$6.29 \cdot 10^5$

# example: X(3872)

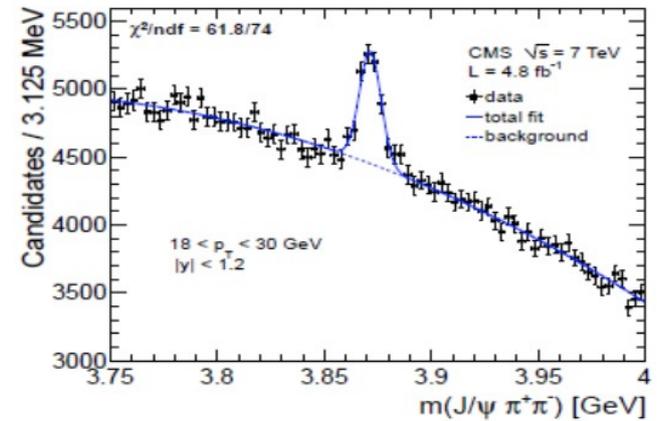
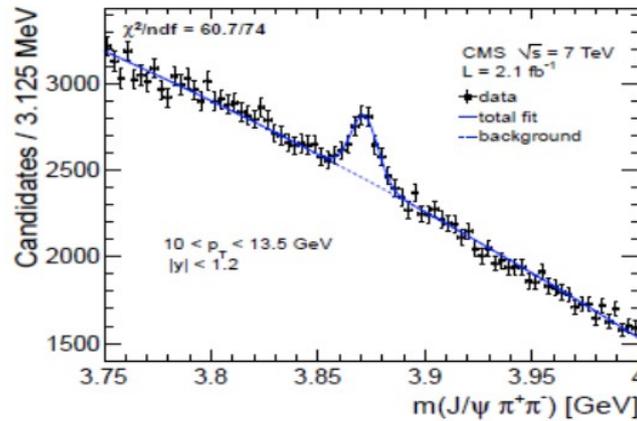
X(3872)

- 2003 -



$$M = 3872.0 \pm 0.6 \pm 0.5 \text{ MeV}$$

- 2013 -



**X(3872)**

$$J^{PC} = 0^+(1^{++})$$

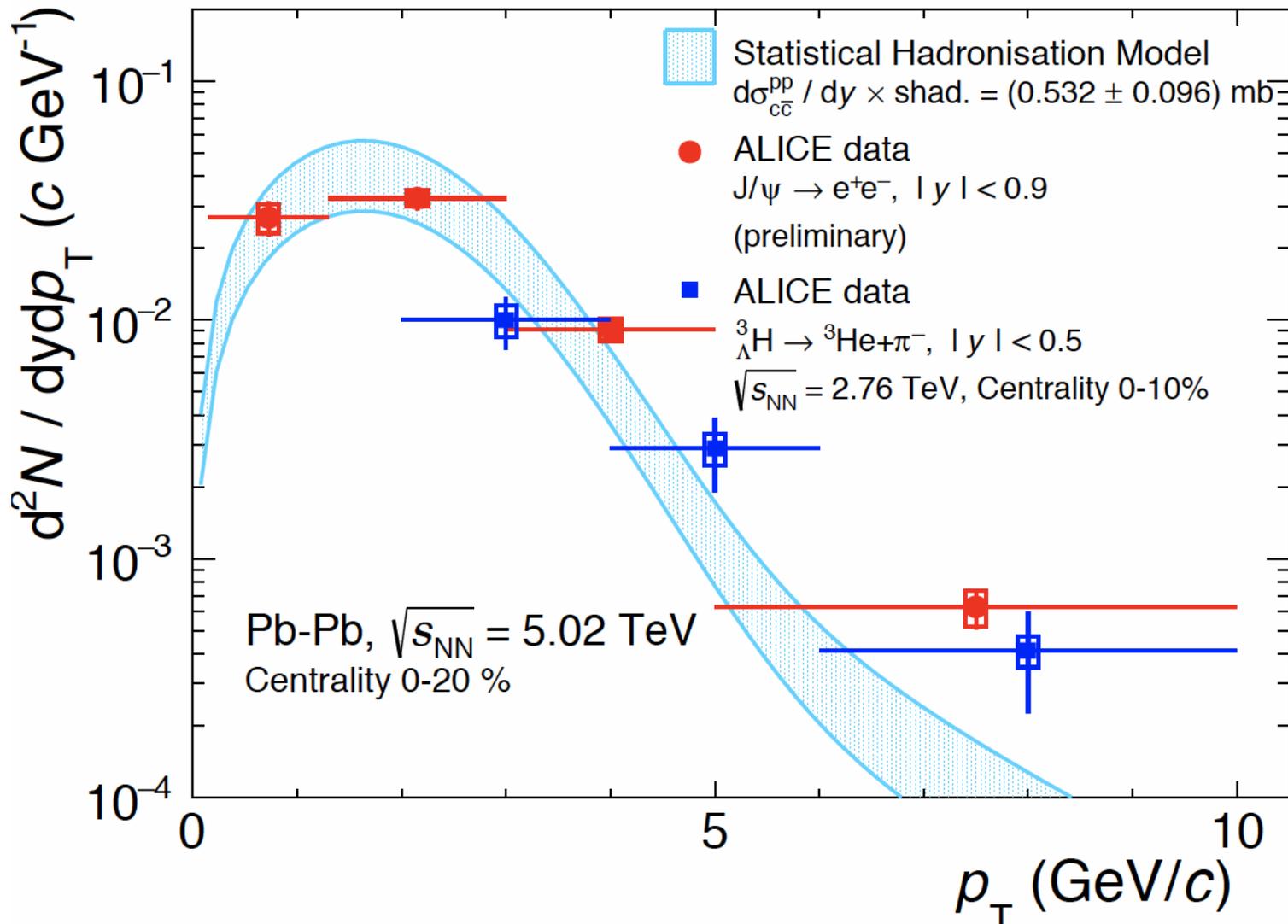
$$\text{Mass } m = 3871.69 \pm 0.17 \text{ MeV}$$

$$m_{X(3872)} - m_{J/\psi} = 775 \pm 4 \text{ MeV}$$

$$m_{X(3872)} - m_{\psi(2S)}$$

$$\text{Full width } \Gamma < 1.2 \text{ MeV, CL} = 90\%$$

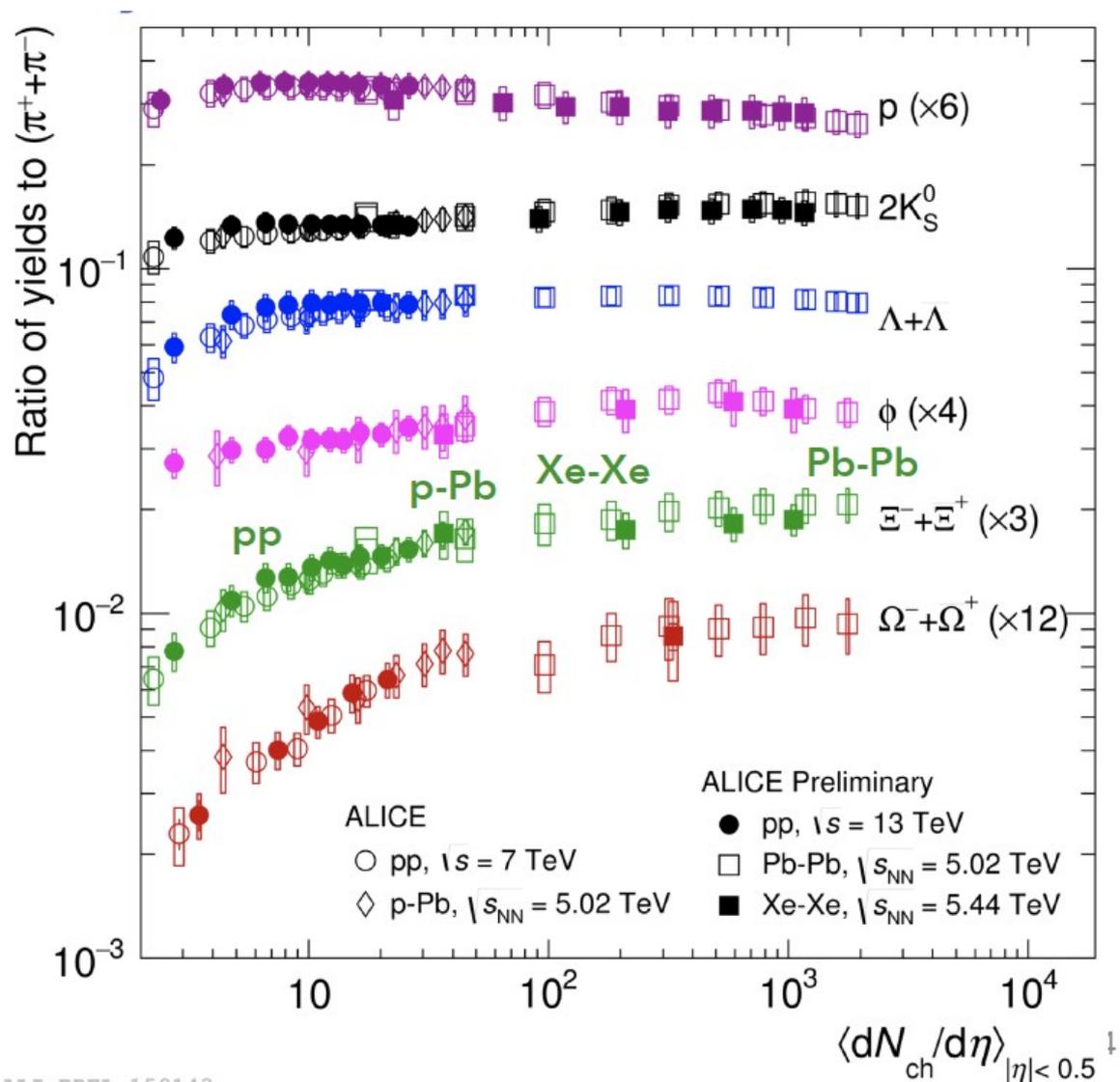
# J/psi and hyper-triton described with the same flow parameters in the statistical hadronization model



binding energies:  
 J/psi 600 MeV  
 hypertriton 2.2 MeV  
 Lambda S.E. 0.2 MeV

from review: hypernuclei and other loosely bound objects produced in nuclear collisions at the LHC,  
 pbm and Benjamin Doenigus,  
 Nucl. Phys. A987 (2019) 144, arXiv:1809.04681

# from pp to Pb-Pb collisions: smooth evolution with system size



ALI-PREL-159143

universal hadronization can be described with few parameters in addition to  $T$  and  $\mu_B$   
 transition from canonical to grand-canonical thermodynamics

## outlook (1)

when statistics and precision of open charm cross section improves one can look into  
hadronization of multi-charm states,  
correlation width in rapidity

coupling to hydro code determines shape of  $p_T$  spectra and flow of charm hadrons

beauty can be treated in similar way but:  
thermalization of b quarks?

it would be interesting to extend the measurements to  
charm/beauty hadrons in jets

can one measure net charm correlations and higher moments?

**we look forward to testing the predictions from SHMc with  
Run3/Run4 and, of course, ALICE3 data**

## outlook (2)

ALICE is currently upgraded:

GEM based read-out chambers for the TPC  
new inner tracker with ultra-thin Si layers  
continuous read of (all) subdetectors

**increase of data rates by factor >50**

focus on rare objects, exotic quarkonia, double and triple charm hadrons to address a number of fundamental questions and issues such as:

- what is the deconfinement radius for charm quarks
- are there colorless bound states in a deconfined medium?
  
- are complex, light nuclei and exotic charmonia (X,Y,Z) produced as compact multi-quark bags?
  
- can fluctuation measurements shed light on critical behavior near the phase boundary?

deciphering QCD in the strongly coupled regime