

The phase diagram at finite T and μ_B (and μ_I)

Massimo Mannarelli INFN-LNGS

massimo@lngs.infn.it

Exploring high-µ_B matter with rare probes ECT* 11 Oct 2021

Outline

A first approach to the QCD phase diagram

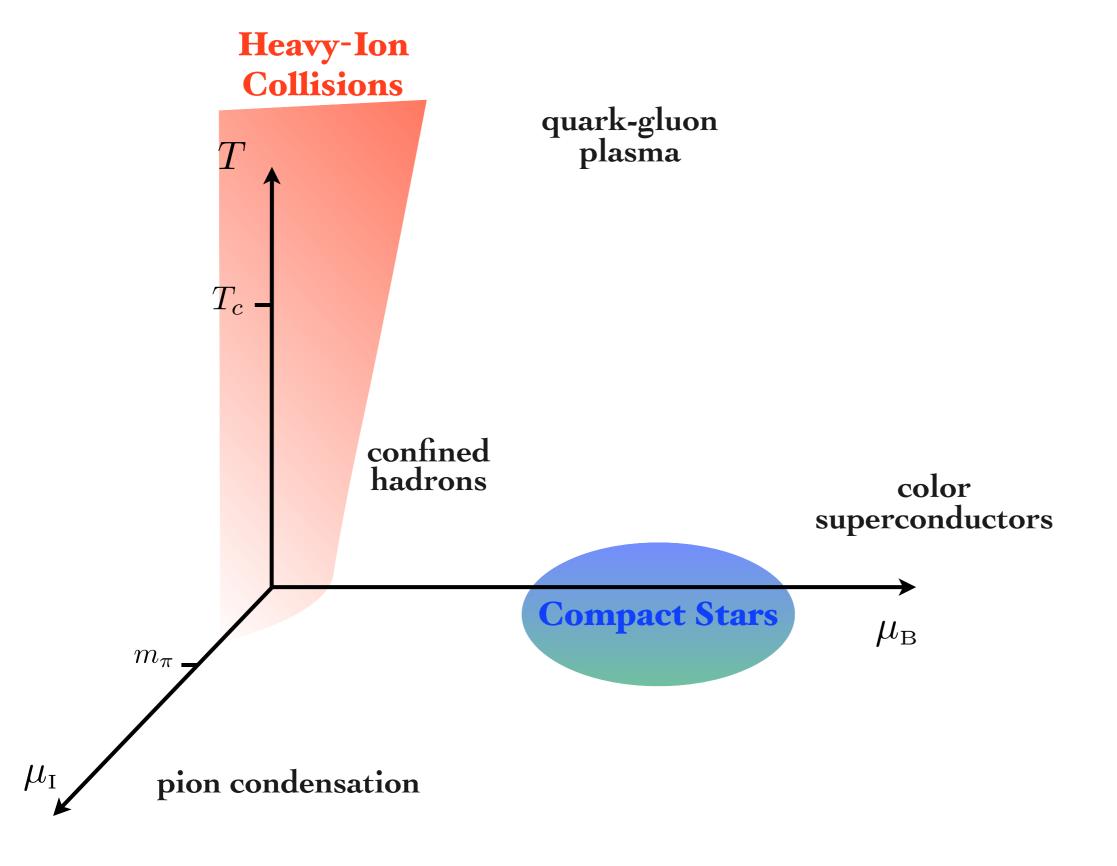
Natural labs

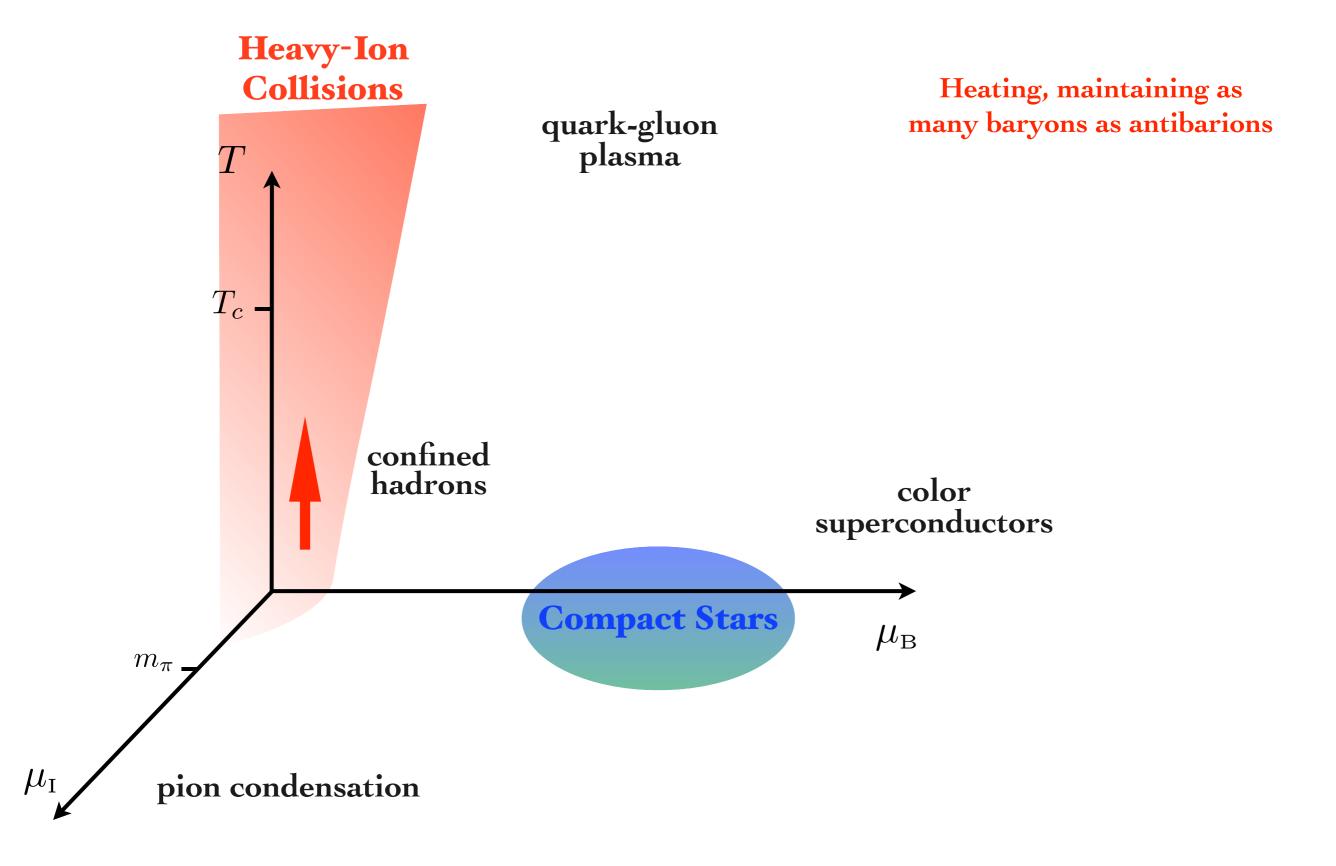
Richness of phases

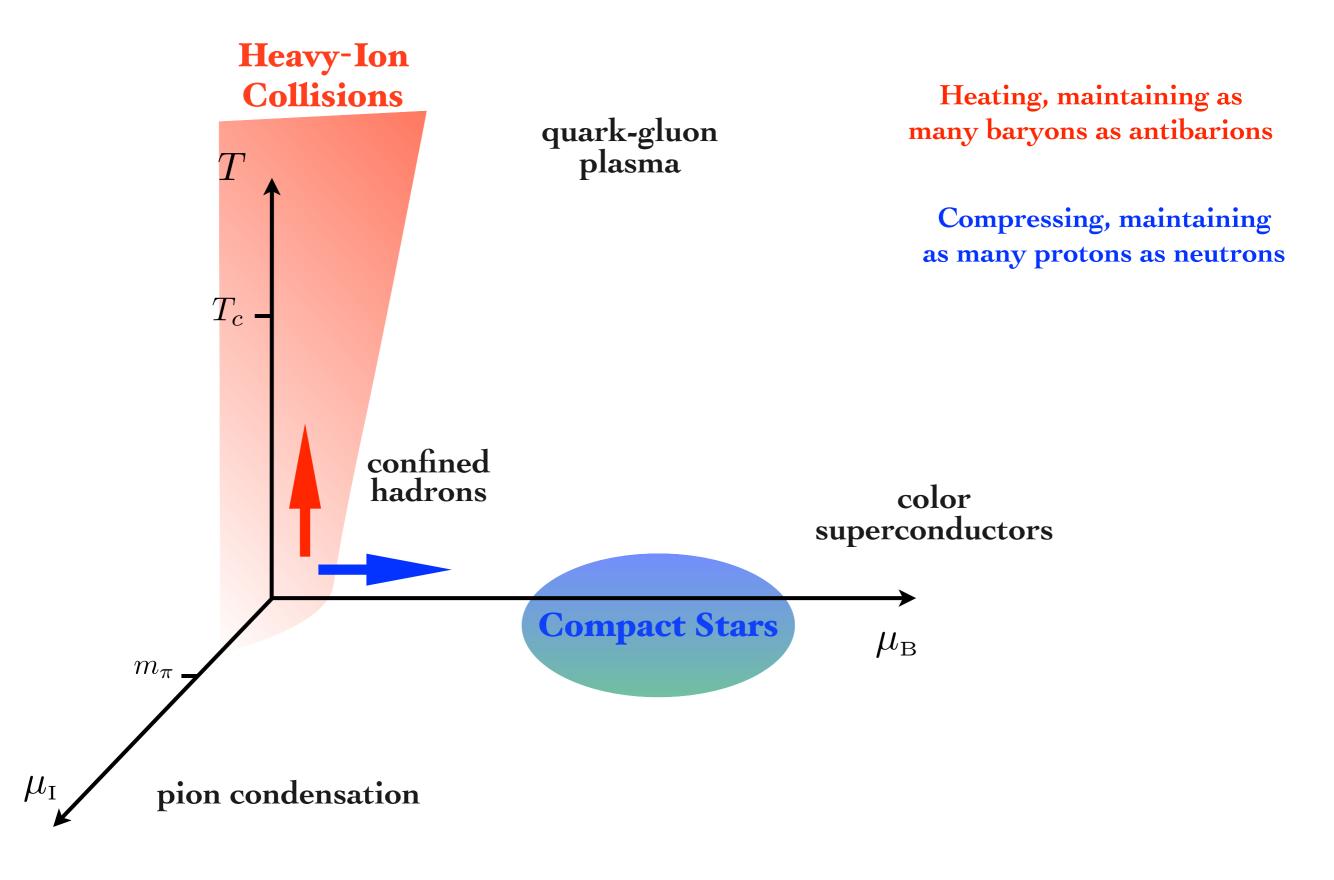
A second view of the QCD phase diagram

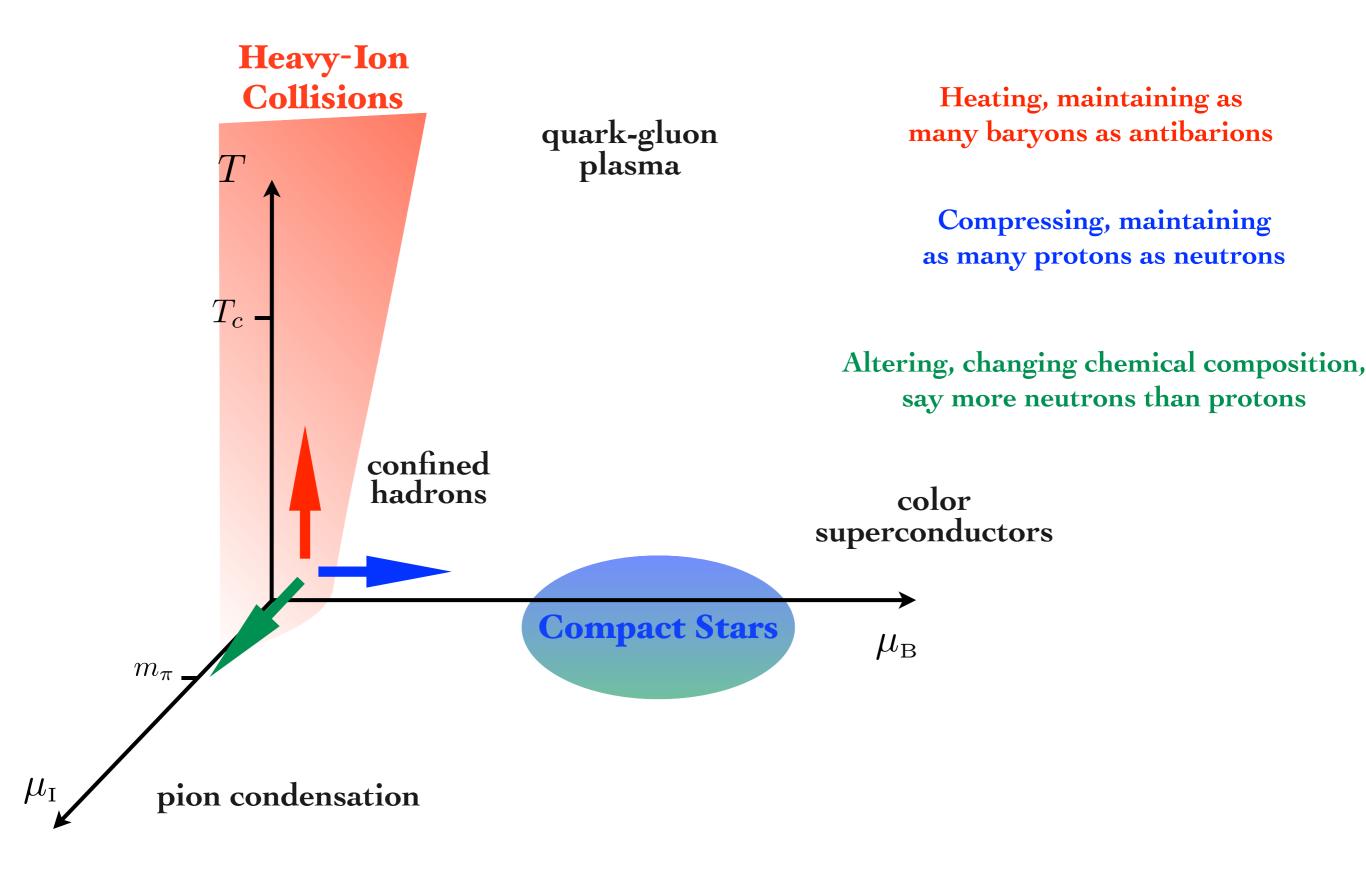
Conclusions

The phase diagram What we know... what we would like to know









A thermodynamic description of hadronic matter should include the possible hadrons

A thermodynamic description of hadronic matter should include the possible hadrons

$\int J$	Particles (mass in MeV)
0	π^0 (135), π^{\pm} (140), η (547), η' (958), K^{\pm} (494), K^0 , \bar{K}^0 (498)
1	$\rho^{\pm,0}$ (771), ω (783), $K^{*\pm}, K^{*0}, \bar{K}^{*0}$ (892), Φ (1020)
$\frac{1}{2}$	p (938), n (939), Λ (1116), $\Sigma^{\pm,0}$ (1193), $\Xi^{0,-}$ (1318)
$\frac{\overline{3}}{2}$	$\Delta^{++}, \Delta^{+}, \Delta^{-}, \Delta^{0}$ (1232), $\Sigma^{*\pm,0}$ (1385), $\Xi^{*\pm,0}$ (1318), Ω^{-} (1672)

A thermodynamic description of hadronic matter should include the possible hadrons

$\int J$	Particles (mass in MeV)
0	π^0 (135), π^{\pm} (140), η (547), η' (958), K^{\pm} (494), K^0 , \bar{K}^0 (498)
1	$\rho^{\pm,0}$ (771), ω (783), $K^{*\pm}, K^{*0}, \bar{K}^{*0}$ (892), Φ (1020)
$\frac{1}{2}$	p (938), n (939), Λ (1116), $\Sigma^{\pm,0}$ (1193), $\Xi^{0,-}$ (1318)
$\frac{3}{2}$	$\Delta^{++}, \Delta^{+}, \Delta^{-}, \Delta^{0}$ (1232), $\Sigma^{*\pm,0}$ (1385), $\Xi^{*\pm,0}$ (1318), Ω^{-} (1672)

R. Hagedorn (1964/65) "statistical bootstrap" idea: the exponential growth of states implies a limiting temperature, T_c , for hadronic matter.

Roughly: close to T_c , putting energy into the system increases the number of particles, not the temperature.

A thermodynamic description of hadronic matter should include the possible hadrons

$\int J$	Particles (mass in MeV)
0	π^0 (135), π^{\pm} (140), η (547), η' (958), K^{\pm} (494), K^0 , \bar{K}^0 (498)
1	$\rho^{\pm,0}$ (771), ω (783), $K^{*\pm}, K^{*0}, \bar{K}^{*0}$ (892), Φ (1020)
$\frac{1}{2}$	p (938), n (939), Λ (1116), $\Sigma^{\pm,0}$ (1193), $\Xi^{0,-}$ (1318)
$\frac{3}{2}$	$\Delta^{++}, \Delta^{+}, \Delta^{-}, \Delta^{0}$ (1232), $\Sigma^{*\pm,0}$ (1385), $\Xi^{*\pm,0}$ (1318), Ω^{-} (1672)

R. Hagedorn (1964/65) "statistical bootstrap" idea: the exponential growth of states implies a limiting temperature, T_c , for hadronic matter.

Roughly: close to T_c , putting energy into the system $\,$ increases the number of particles, not the temperature.

One of the caveats: particles were assumed to be point-like objects.

I.Ya. Pomeranchuk (1951) already noted that a crucial feature of hadrons: their size. A hadron must have its own volume to exist.

Quark liberation

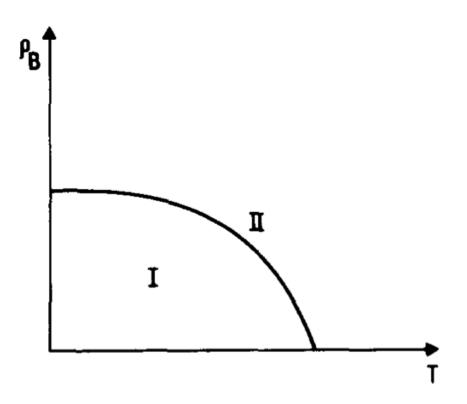
N. Cabibbo and G.Parisi PLB 59, Issue 1, 13 October 1975

"We suggest that the "observed" exponential spectrum is connected to the existence of a different phase of the vacuum in which quarks are not confined."

Quark liberation

N. Cabibbo and G.Parisi PLB 59, Issue 1, 13 October 1975

"We suggest that the "observed" exponential spectrum is connected to the existence of a different phase of the vacuum in which quarks are not confined."



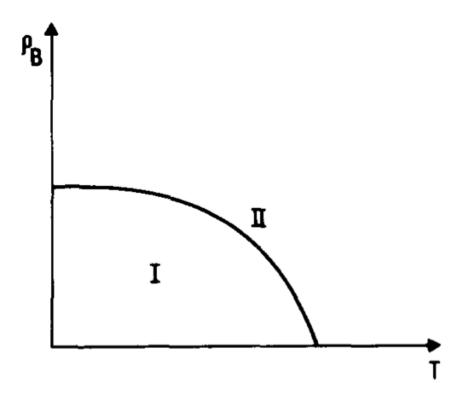
In the $V \to \infty$ limit the exponential spectrum is typical of second order phase transitions

Fig. 1. Schematic phase diagram of hadronic matter. ρ_B is the density of baryonic number. Quarks are confined in phase I and unconfined in phase II.

Quark liberation

N. Cabibbo and G.Parisi PLB 59, Issue 1, 13 October 1975

"We suggest that the "observed" exponential spectrum is connected to the existence of a different phase of the vacuum in which quarks are not confined."



In the $V \to \infty$ limit the exponential spectrum is typical of second order phase transitions

Fig. 1. Schematic phase diagram of hadronic matter. ρ_B is the density of baryonic number. Quarks are confined in phase I and unconfined in phase II.

The behavior of matter close to the phase transition is characterized by a kind of "critical opalescence" of hadrons

Important lesson:

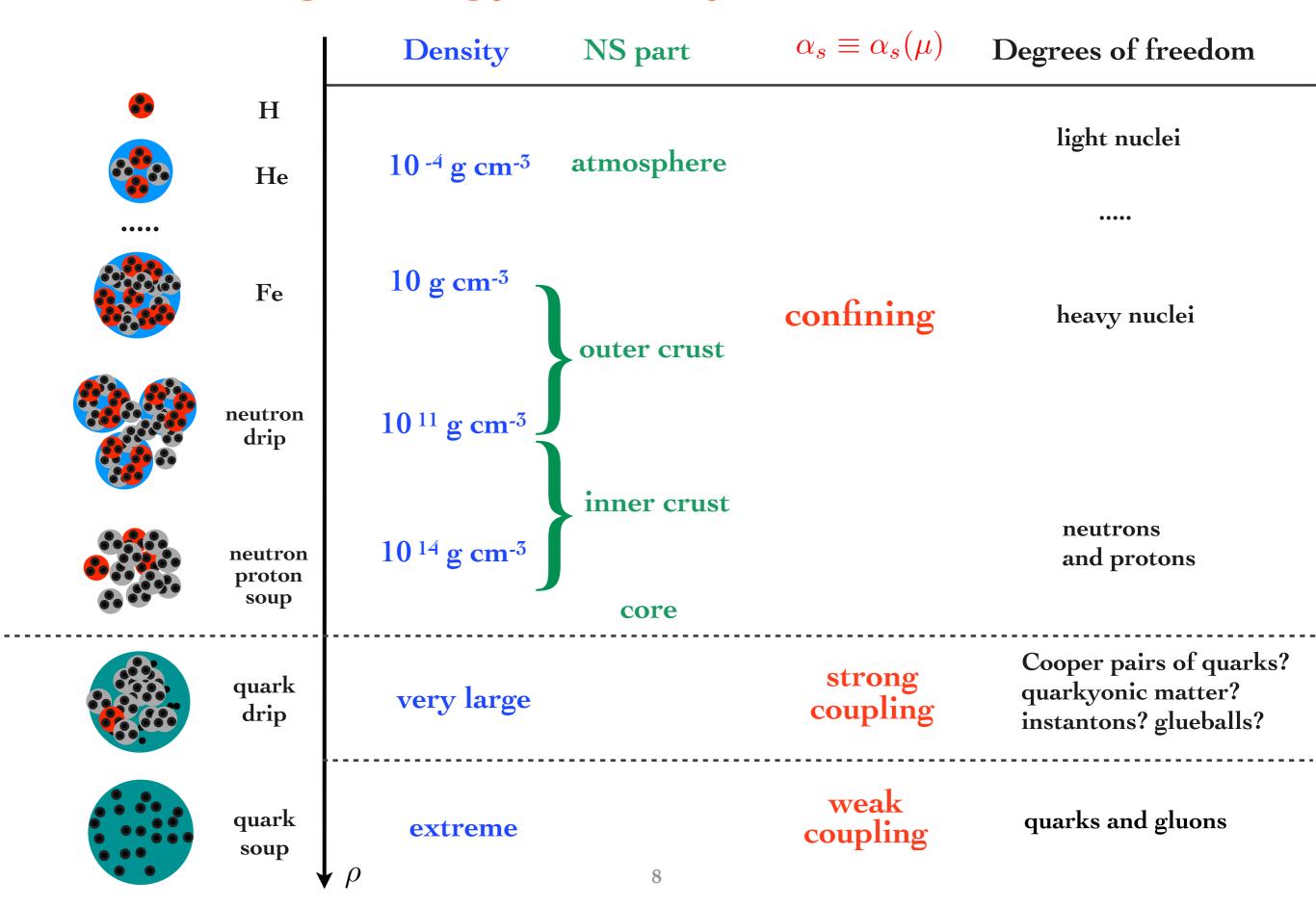
- 1) Close to T_c hadronic resonances play a crucial role
- 2) There exists a limiting temperature, T_c, for hadronic matter. If we insist to describe hadronic matter in terms of baryons and mesons at increasing temperature, the description becomes inconsistent.
- 3) The critical temperature is of order m_{π}
- 4) The pressure of the bootstrap statistical model is in agreement with LQCD calculation below $T_{\rm c}$

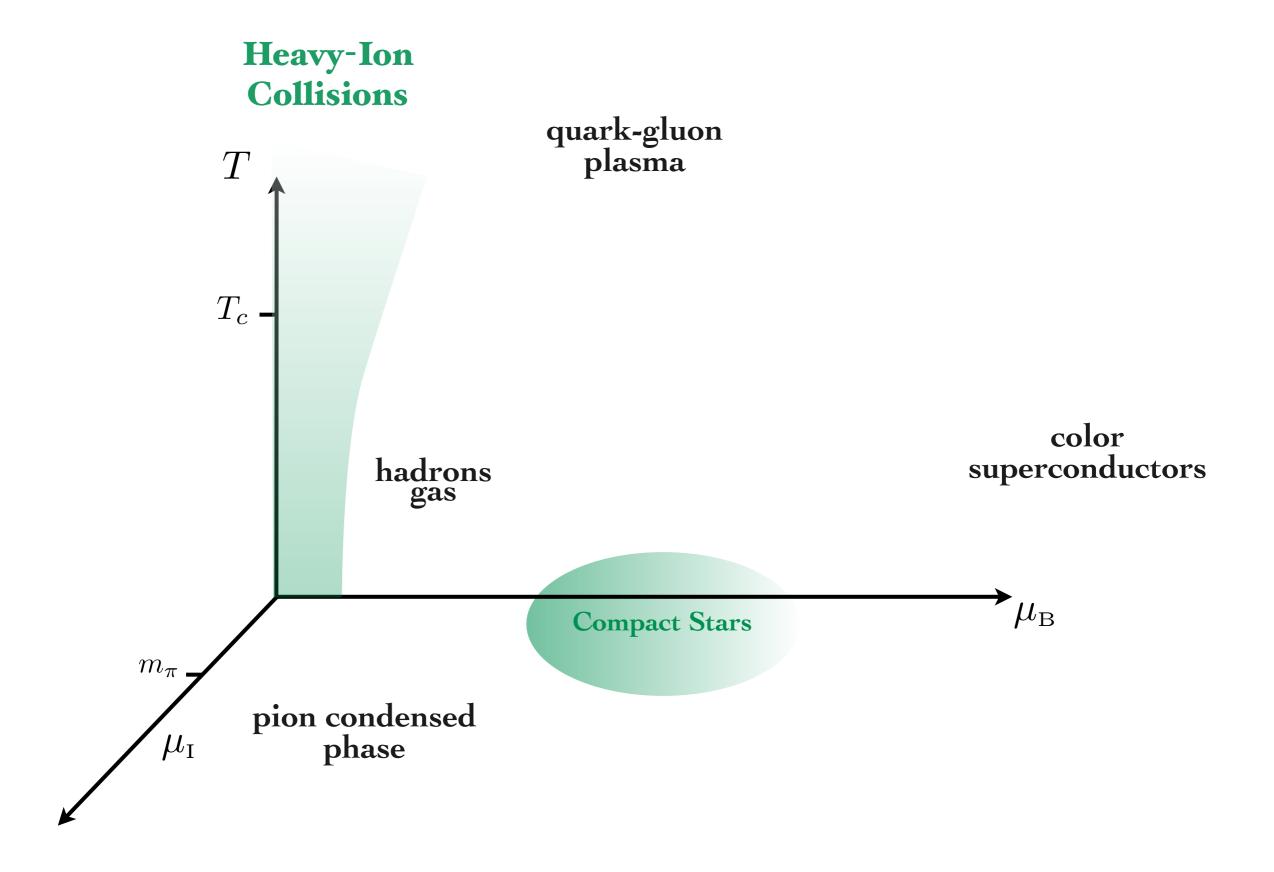
Important lesson:

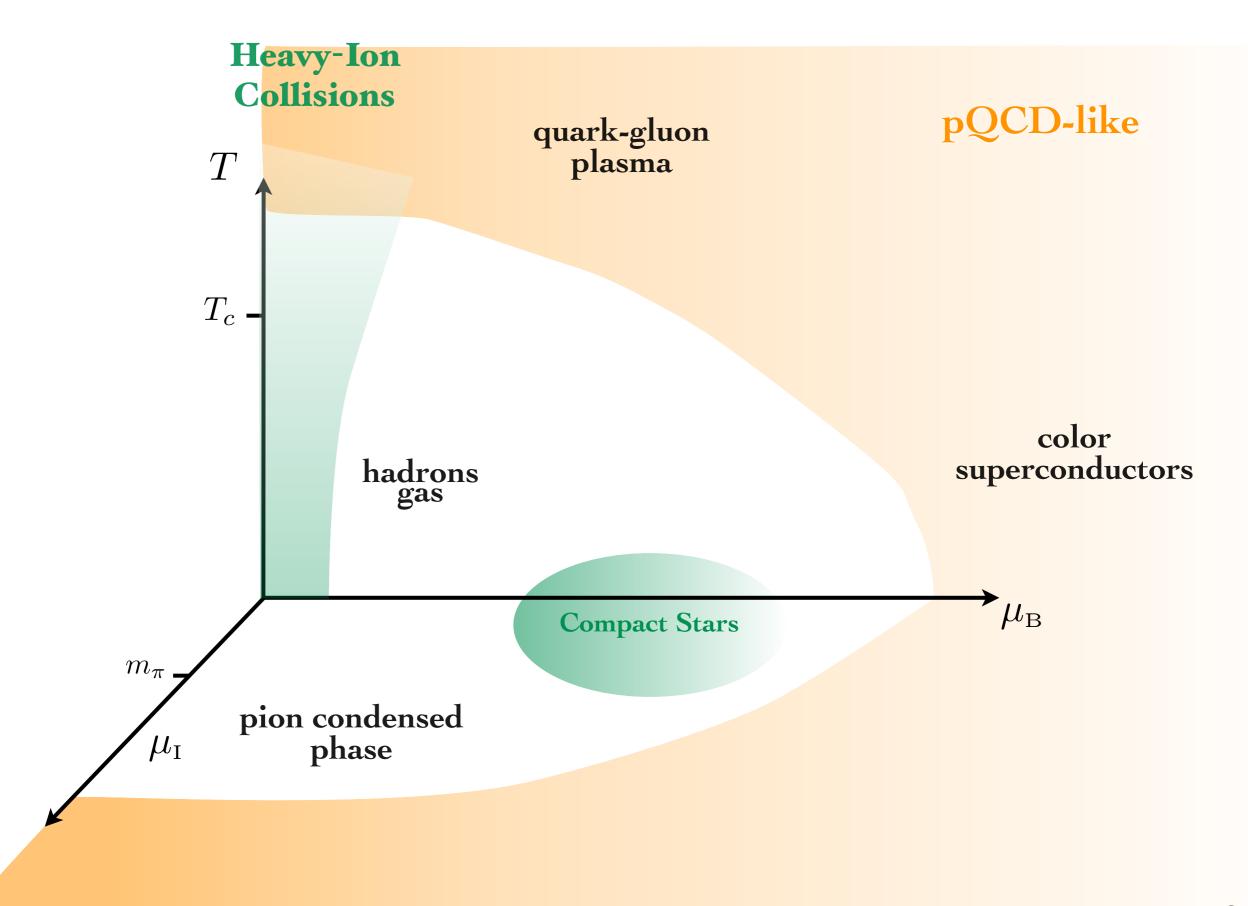
- 1) Close to T_c hadronic resonances play a crucial role
- 2) There exists a limiting temperature, T_c, for hadronic matter. If we insist to describe hadronic matter in terms of baryons and mesons at increasing temperature, the description becomes inconsistent.
- 3) The critical temperature is of order m_{π}
- 4) The pressure of the bootstrap statistical model is in agreement with LQCD calculation below $T_{\rm c}$

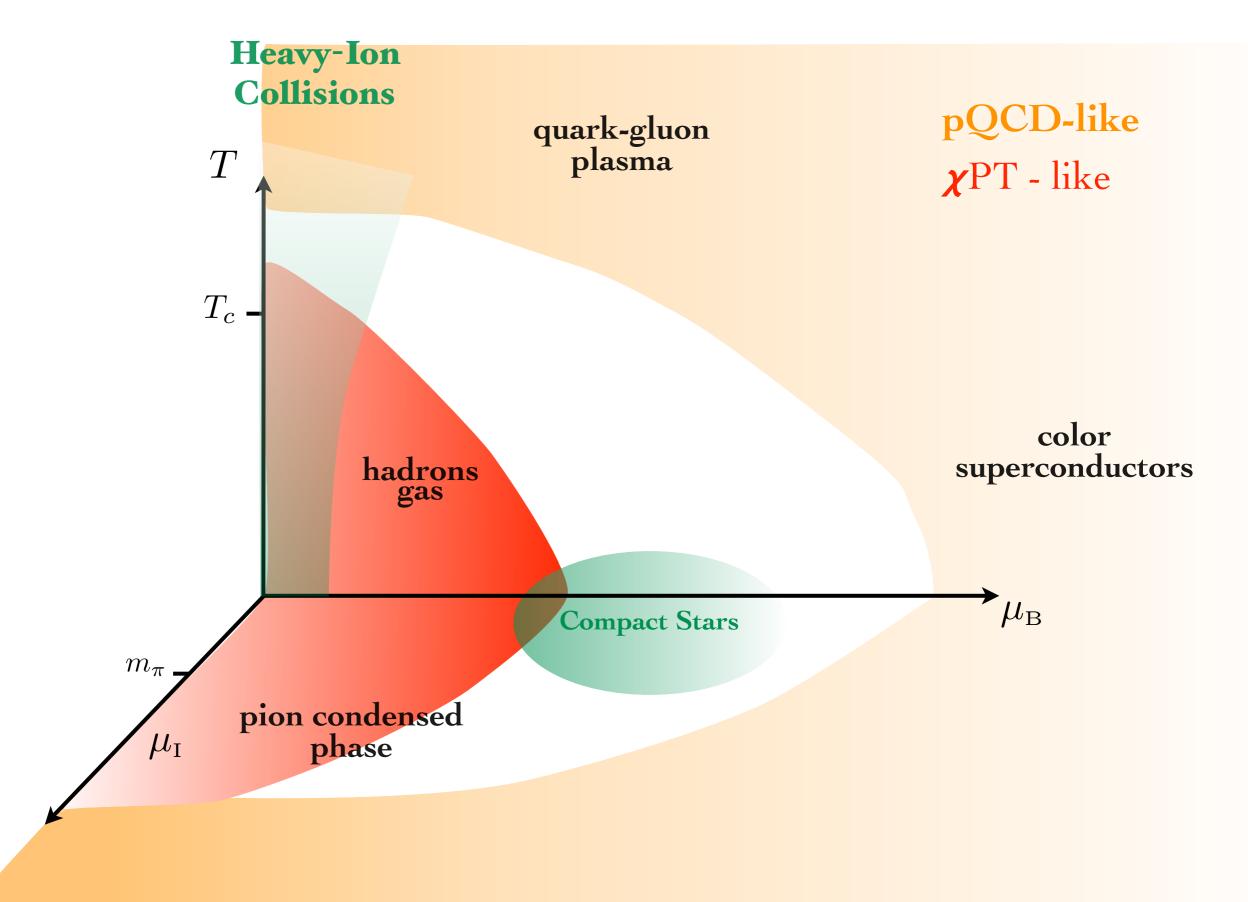
See Redlich and Satz, e-Print: 1501.07523 [hep-ph] for more on Hagedorn's work.

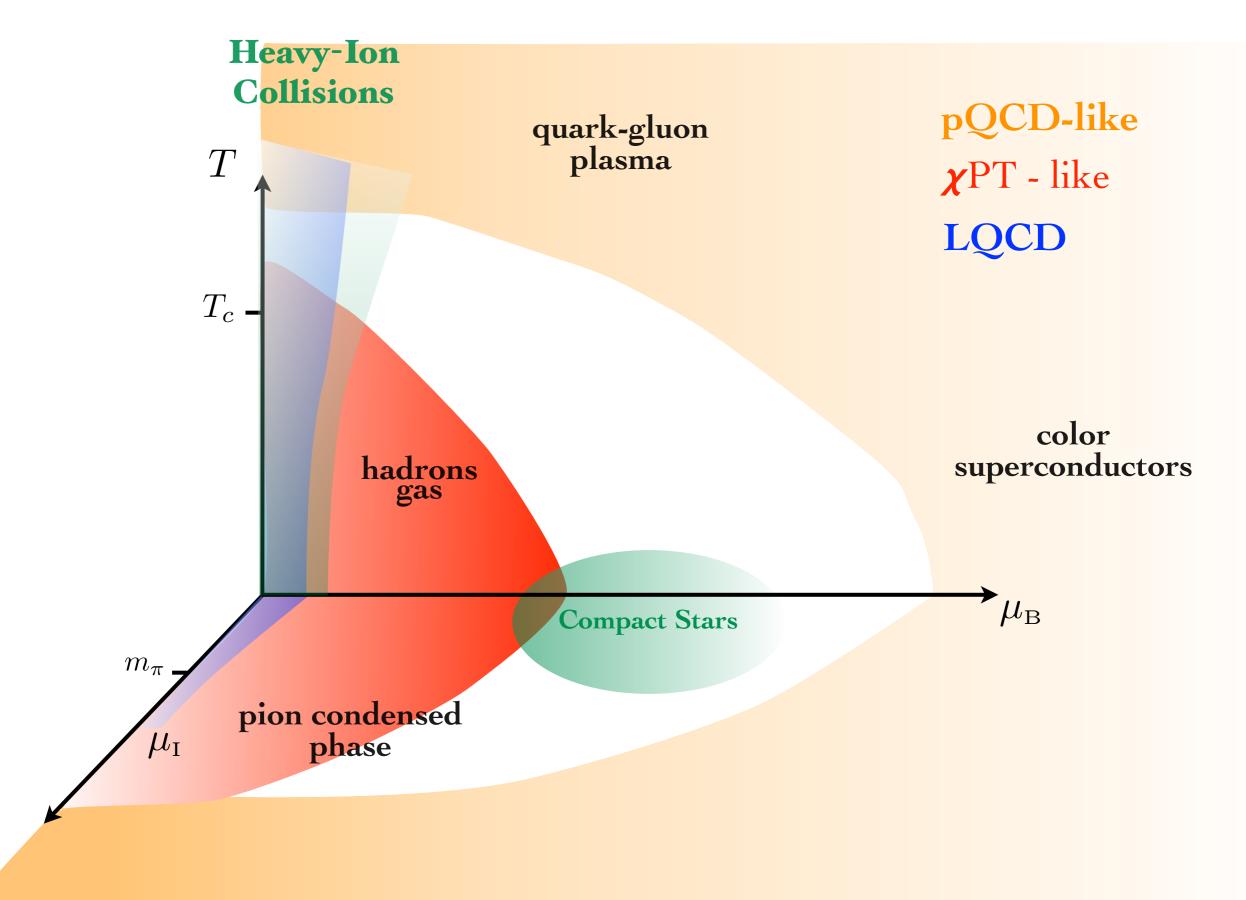
Increasing energy density

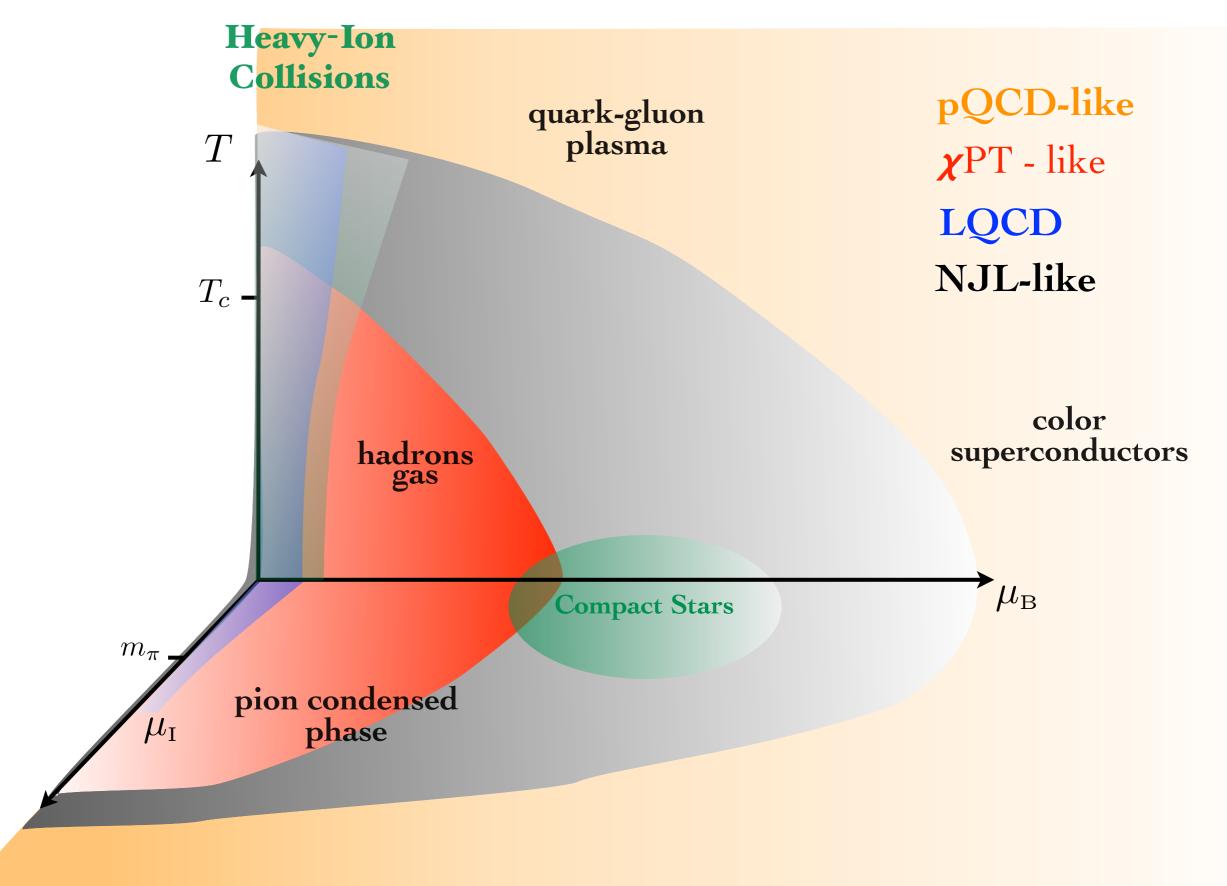


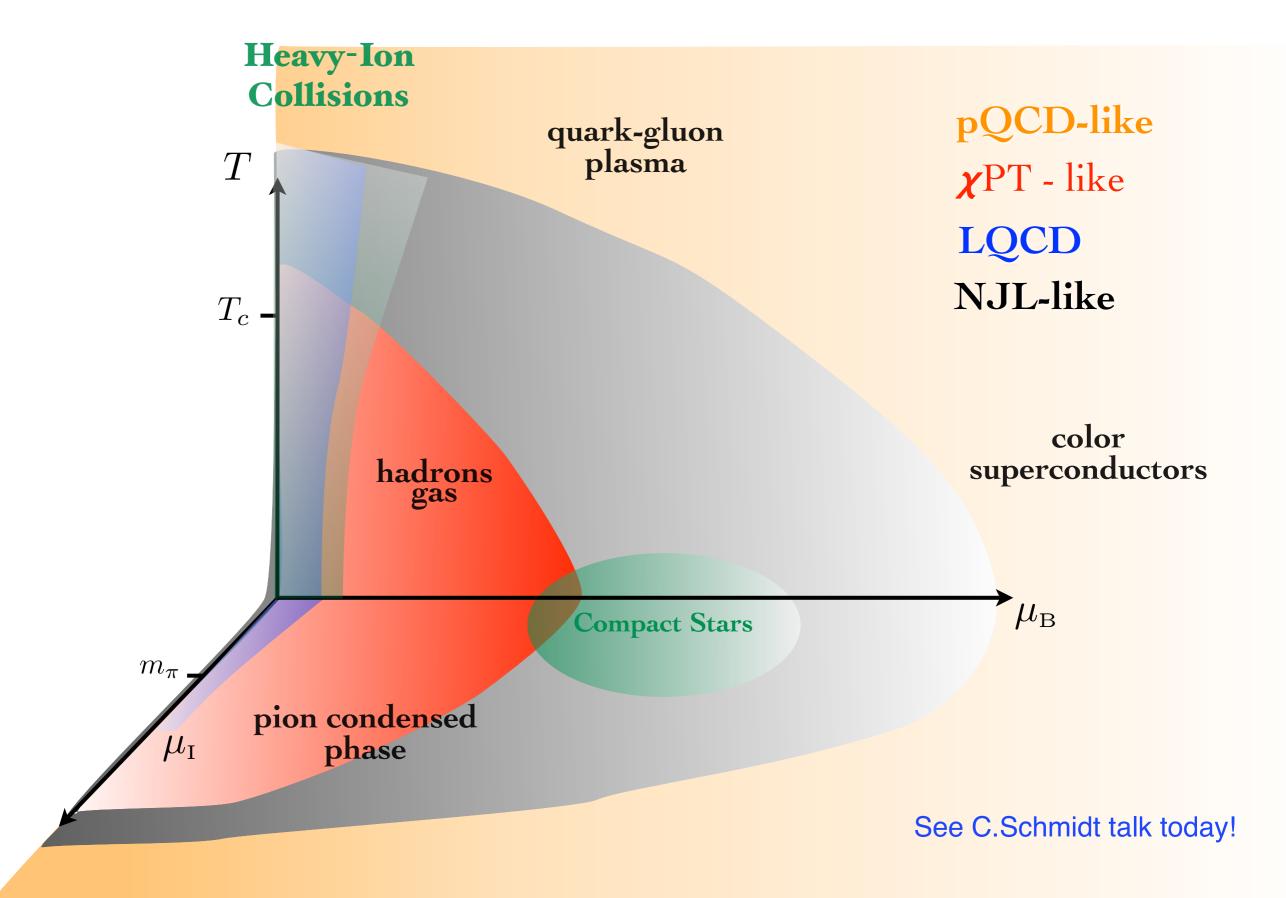


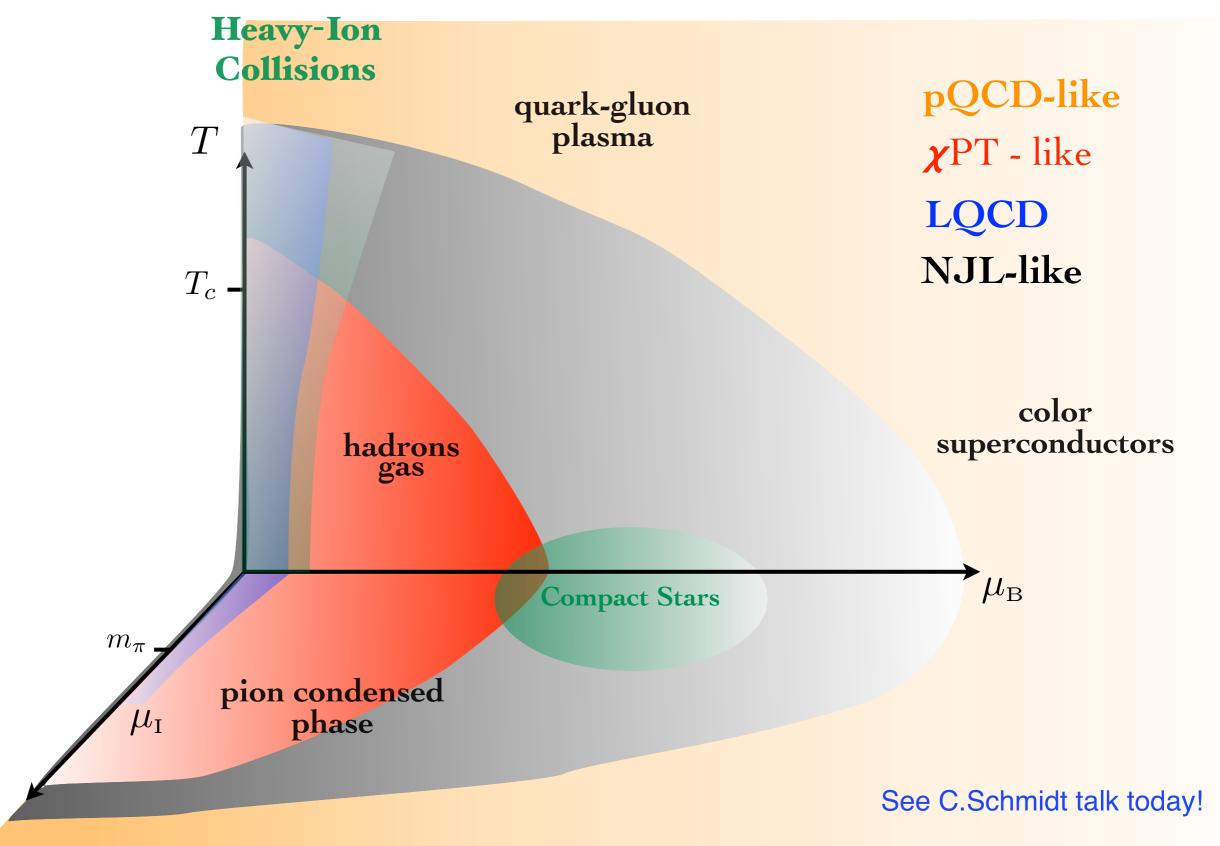












Various approaches use results from LQCD simulation in effective field theories.

Effective field theory: two perspectives

Schematically, two approaches to matter in extreme conditions

- 1) Understanding the (astro)physical phenomena related to high chemical potential and temperature
- 2) Understanding QCD in a region in which the correct degrees of freedom ar quarks and gluons

Effective field theory: two perspectives

Schematically, two approaches to matter in extreme conditions

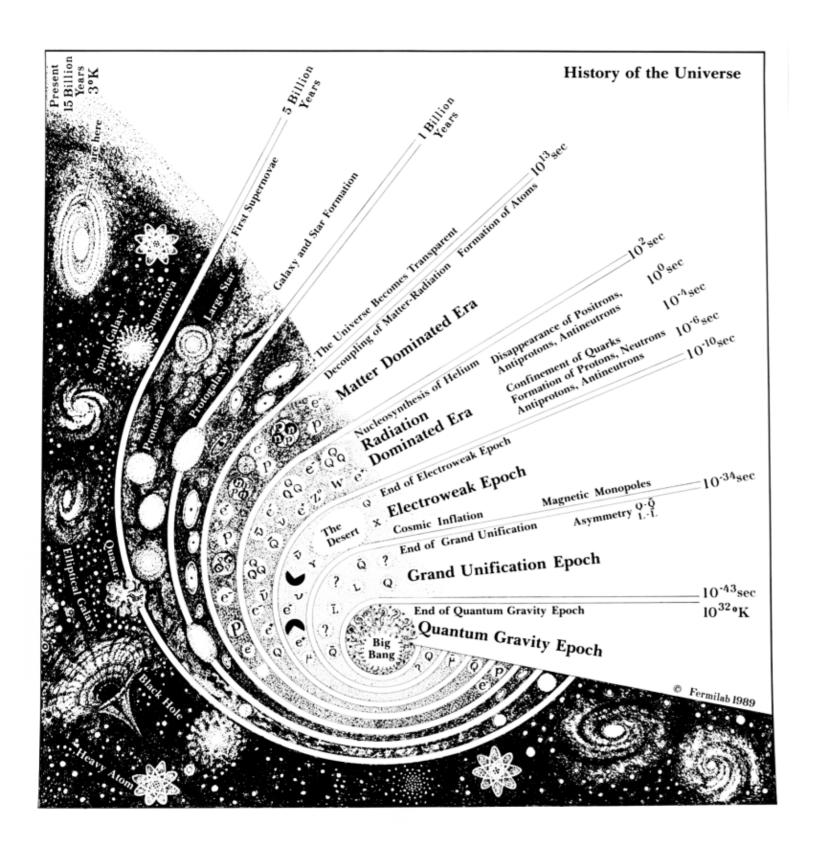
- 1) Understanding the (astro)physical phenomena related to high chemical potential and temperature
- 2) Understanding QCD in a region in which the correct degrees of freedom ar quarks and gluons

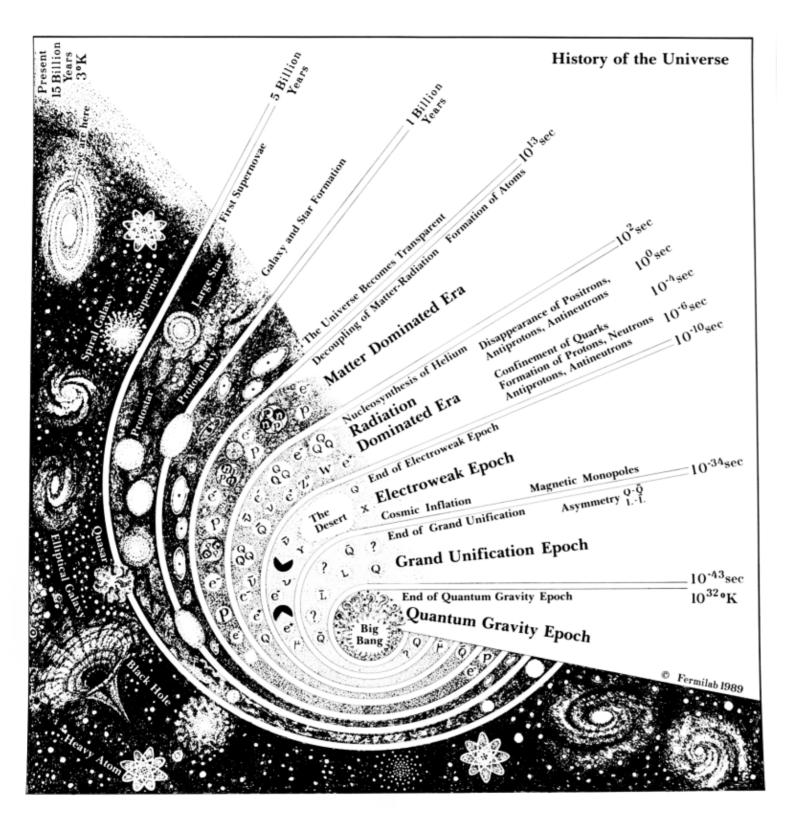
The two perspectives are not mutually exclusive.

However, for those who are interested in (astro)physical phenomena, it is enough to have an effective theory which mimics/reproduces the strong interaction in a sufficiently accurate way.

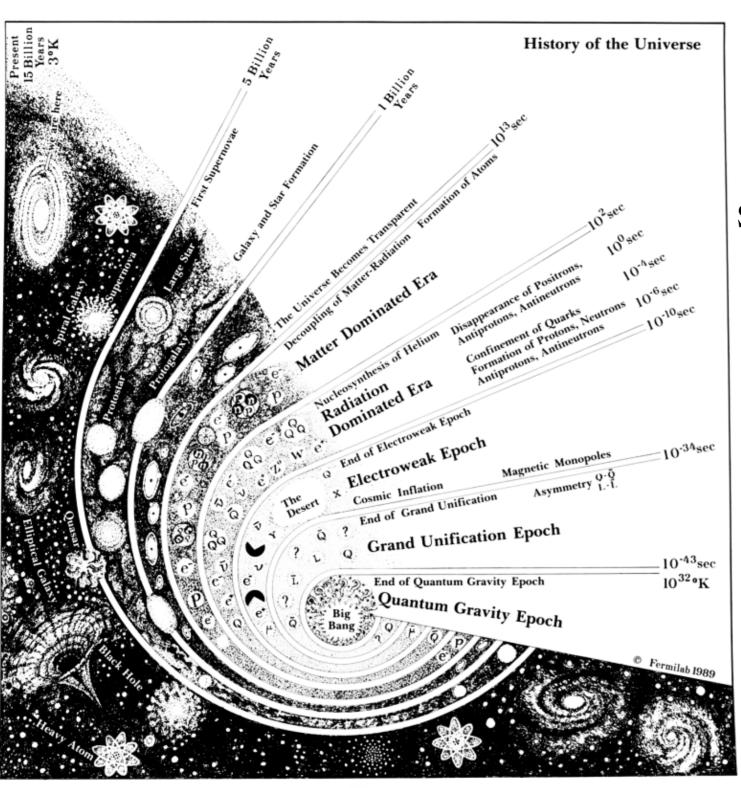
Who is interested to understand QCD wants an effective theory that in a well defined limit is QCD

Natural labs





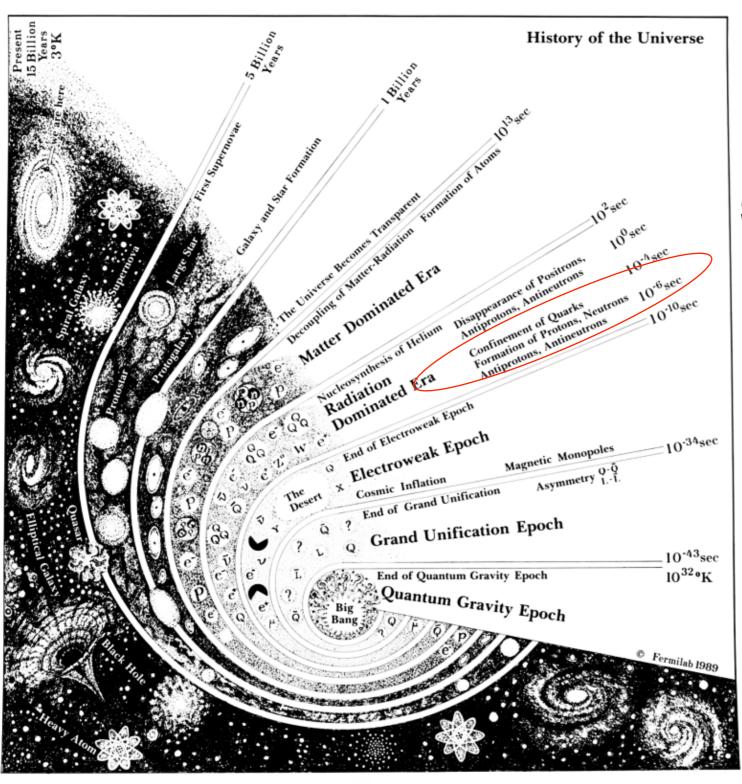
1) The expansion of the Universe is determined by gravity (FLRW cosmology)



1) The expansion of the Universe is determined by gravity (FLRW cosmology)

Scale variation by Friedmann's equation

$$\frac{\ddot{a}}{a} = -\frac{4\pi G_N}{3} (\epsilon + 3p)$$

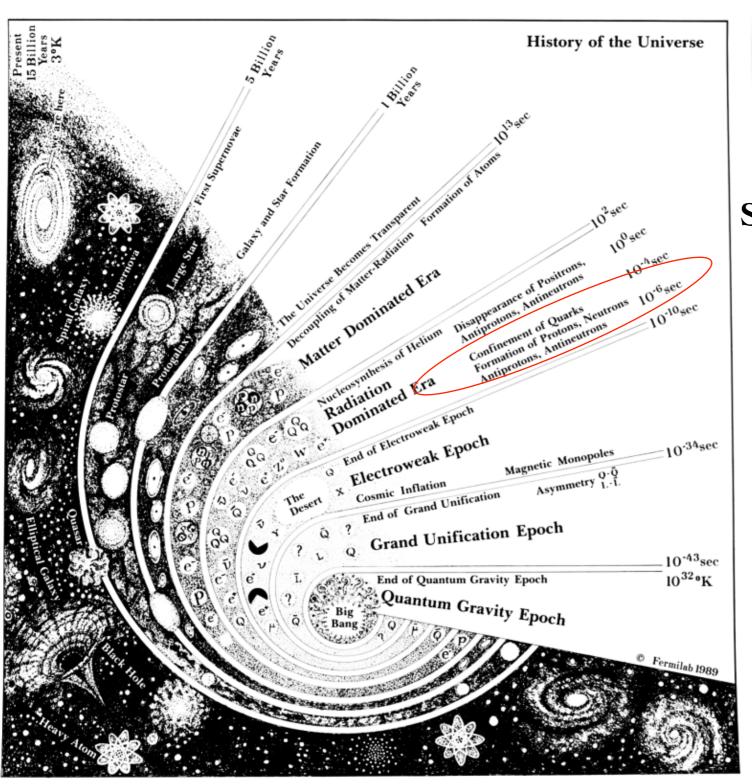


1) The expansion of the Universe is determined by gravity (FLRW cosmology)

Scale variation by Friedmann's equation

$$\frac{\ddot{a}}{a} = -\frac{4\pi G_N}{3} (\epsilon + 3p)$$

2) The quark epoch about 10^{-6} s
The QGP lasts 10^{-23} s



1) The expansion of the Universe is determined by gravity (FLRW cosmology)

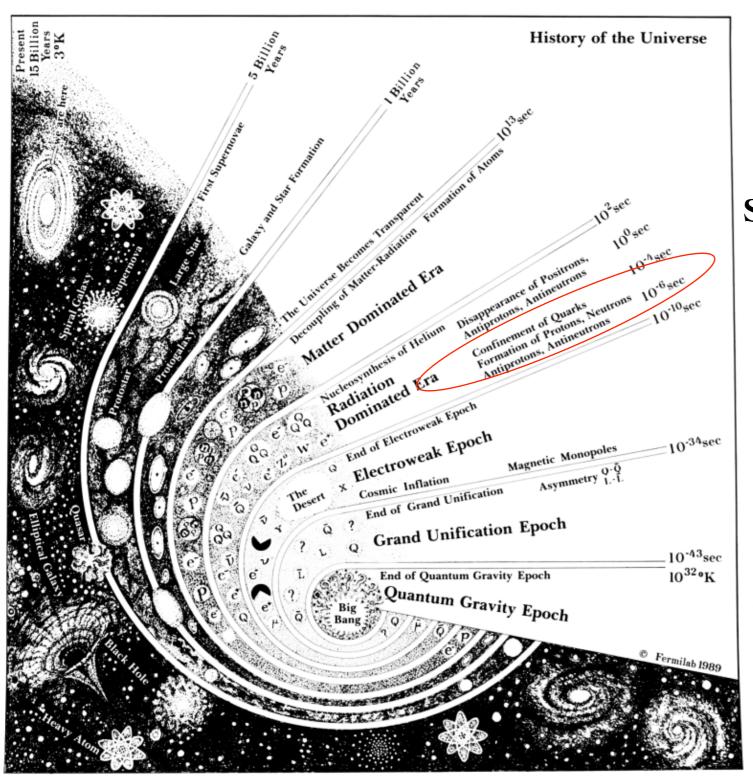
Scale variation by Friedmann's equation

$$\frac{\ddot{a}}{a} = -\frac{4\pi G_N}{3} (\epsilon + 3p)$$

2) The quark epoch about 10^{-6} s The QGP lasts 10^{-23} s

The Universe is quite homogeneous ΔT

For instance in the CMB
$$\frac{\Delta T}{T} \sim 10^{-3}$$



1) The expansion of the Universe is determined by gravity (FLRW cosmology)

Scale variation by Friedmann's equation

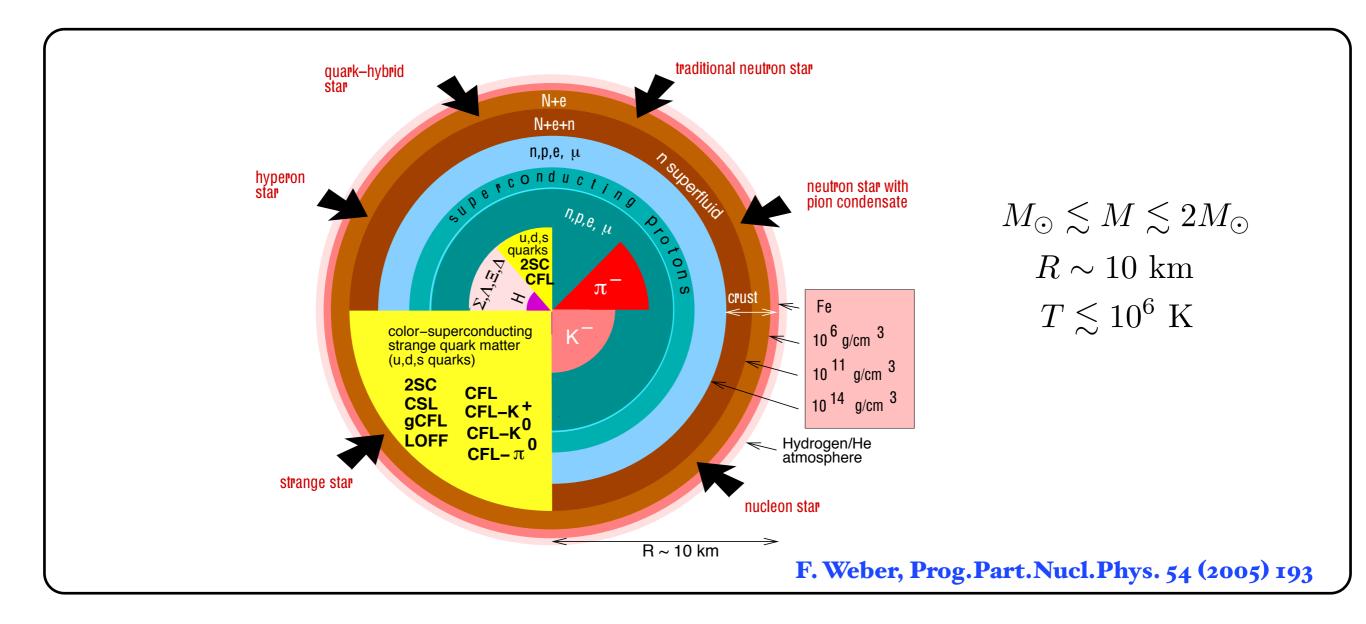
$$\frac{\ddot{a}}{a} = -\frac{4\pi G_N}{3} (\epsilon + 3p)$$

2) The quark epoch about 10^{-6} s The QGP lasts 10^{-23} s

The Universe is quite homogeneous

For instance in the CMB
$$\frac{\Delta T}{T} \sim 10^{-3}$$

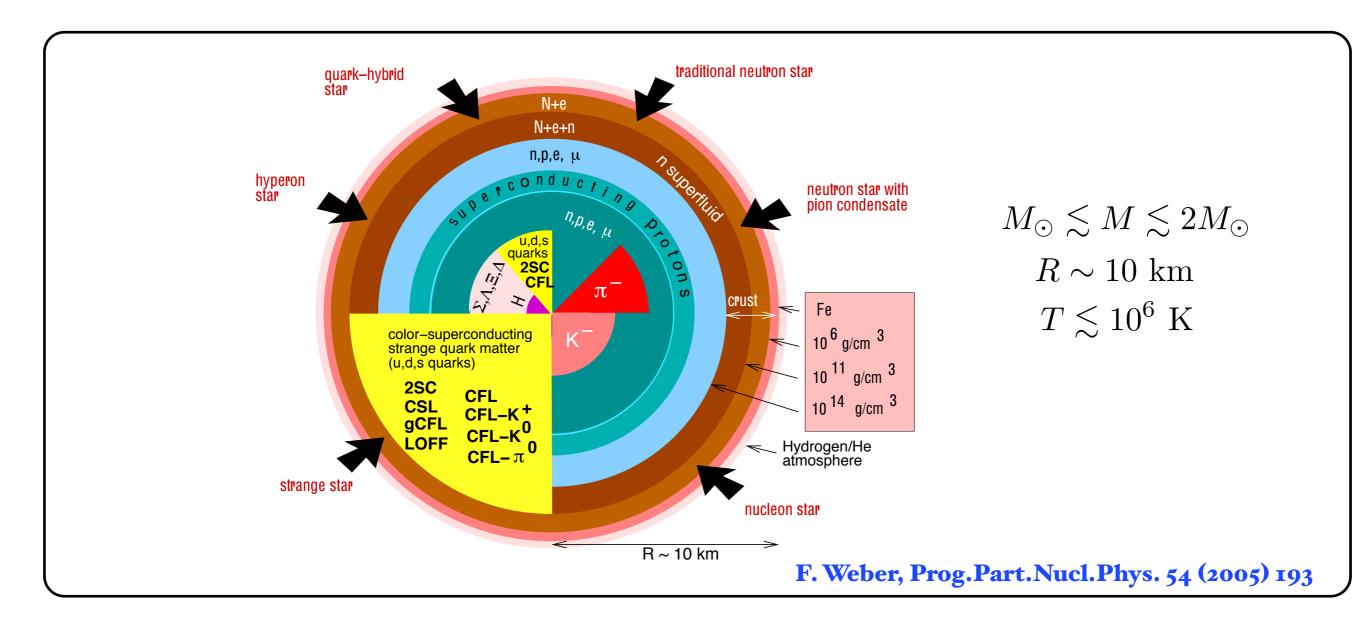
High baryonic density: Compact stars



Possible deconfined phases of matter

Geometrical argument: for central densities $\rho_c > \rho_0$ the distance between nucleons is smaller than their radius: nucleons overlap, "quark drip"

High baryonic density: Compact stars



Possible deconfined phases of matter

Geometrical argument: for central densities $\rho_c > \rho_0$ the distance between nucleons is smaller than their radius: nucleons overlap, "quark drip"

Experimentally access in labs on Earth? Need to produce neutron rich matter.

Compressing cold matter

Neutron rich

matter

Differently from the "lab case", weak equilibrium in Neutron Stars has all the time to work. Favored isotopes in the NS crust

Isotope	\mathbb{Z}/A	$ ho_t(\mathrm{g/cm^3})$	$\mu_e \; ({\rm MeV})$
56 Fe	0.464	7.96×10^{6}	0.95
$^{62}\mathrm{Ni}$	$\sqrt{0.452}$	2.71×10^{8}	2.61
$^{64}\mathrm{Ni}$	0.437	1.3×10^{9}	4.31
⁶⁶ Ni	0.424	1.48×10^{9}	4.45
$^{86}\mathrm{Kr}$	0.419	3.12×10^9	5.66
⁸⁴ Se	0.405	1.10×10^{10}	8.49
$^{82}\mathrm{Ge}$	0.390	2.80×10^{10}	11.4
$^{80}\mathrm{Zn}$	0.375	5.44×10^{10}	14.1
$\sqrt{^{78}\mathrm{Ni}}$	0.359	9.64×10^{10}	16.8
¹²⁶ Ru →	0.350	1.29×10^{11}	18.3
124Mo	0.339	1.88×10^{11}	20.6
$^{122}\mathrm{Zr}$	0.328	2.67×10^{11}	22.9
$120 \mathrm{Sr}$	$\sqrt{0.317}$	3.79×10^{11}	25.4
$^{118}\mathrm{Kr}$	$\sqrt{0.305}$	4.31×10^{11}	26.2

Haensel and Pichon Astron. Astrophys. 283 (1994) 313

Compressing cold matter

Neutron rich

matter

Differently from the "lab case", weak equilibrium in Neutron Stars has all the time to work. Favored isotopes in the NS crust

Isotope	Z/A	$\rho_t(\mathrm{g/cm^3})$	$\mu_e \; ({ m MeV})$
⁵⁶ Fe	0.464	7.96×10^{6}	0.95
⁶² Ni	0.452	2.71×10^{8}	2.61
$^{64}\mathrm{Ni}$	0.437	1.3×10^{9}	4.31
$^{66}\mathrm{Ni}$	0.424	1.48×10^{9}	4.45
$^{86}\mathrm{Kr}$	0.419	3.12×10^{9}	5.66
⁸⁴ Se	0.405	1.10×10^{10}	8.49
$^{82}\mathrm{Ge}$	0.390	2.80×10^{10}	11.4
$^{80}\mathrm{Zn}$	0.375	5.44×10^{10}	14.1
⁷⁸ Ni	0.359	9.64×10^{10}	16.8
¹²⁶ Ru →	0.350	1.29×10^{11}	18.3
$^{124}\mathrm{Mo}$	0.339	1.88×10^{11}	20.6
$^{122}\mathrm{Zr}$	0.328	2.67×10^{11}	22.9
$^{120}\mathrm{Sr}$	0.317	3.79×10^{11}	25.4
$^{118}\mathrm{Kr}$	0.305	4.31×10^{11}	26.2

Haensel and Pichon Astron. Astrophys. 283 (1994) 313

Compressing cold matter

Differently from the "lab case", weak equilibrium in Neutron Stars has all the time to work. Favored isotopes in the NS crust

Isotope	\mathbb{Z}/A	$\rho_t({ m g/cm^3})$	$\mu_e \; ({\rm MeV})$
⁵⁶ Fe	0.464	7.96×10^{6}	0.95
$^{62}\mathrm{Ni}$	$\sqrt{0.452}$	2.71×10^{8}	2.61
$^{64}\mathrm{Ni}$	0.437	1.3×10^{9}	4.31
⁶⁶ Ni	0.424	1.48×10^{9}	4.45
$^{86}{ m Kr}$	0.419	3.12×10^{9}	5.66
⁸⁴ Se	0.405	1.10×10^{10}	8.49
82 Ge	0.390	2.80×10^{10}	11.4
$^{80}\mathrm{Zn}$	0.375	5.44×10^{10}	14.1
√ ⁷⁸ Ni	0.359	9.64×10^{10}	16.8
¹²⁶ Ru →	0.350	1.29×10^{11}	18.3
$^{124}\mathrm{Mo}$	0.339	1.88×10^{11}	20.6
$^{122}\mathrm{Zr}$	$\sqrt{0.328}$	2.67×10^{11}	22.9
$^{120}\mathrm{Sr}$	$\sqrt{0.317}$	3.79×10^{11}	25.4
$^{118}\mathrm{Kr}$	$\sqrt{0.305}$	4.31×10^{11}	26.2

Haensel and Pichon Astron. Astrophys. 283 (1994) 313

neutron drip

Then there are many unbound neutrons $Z/A \sim 0.1$

Neutron rich

matter

Compressing cold matter

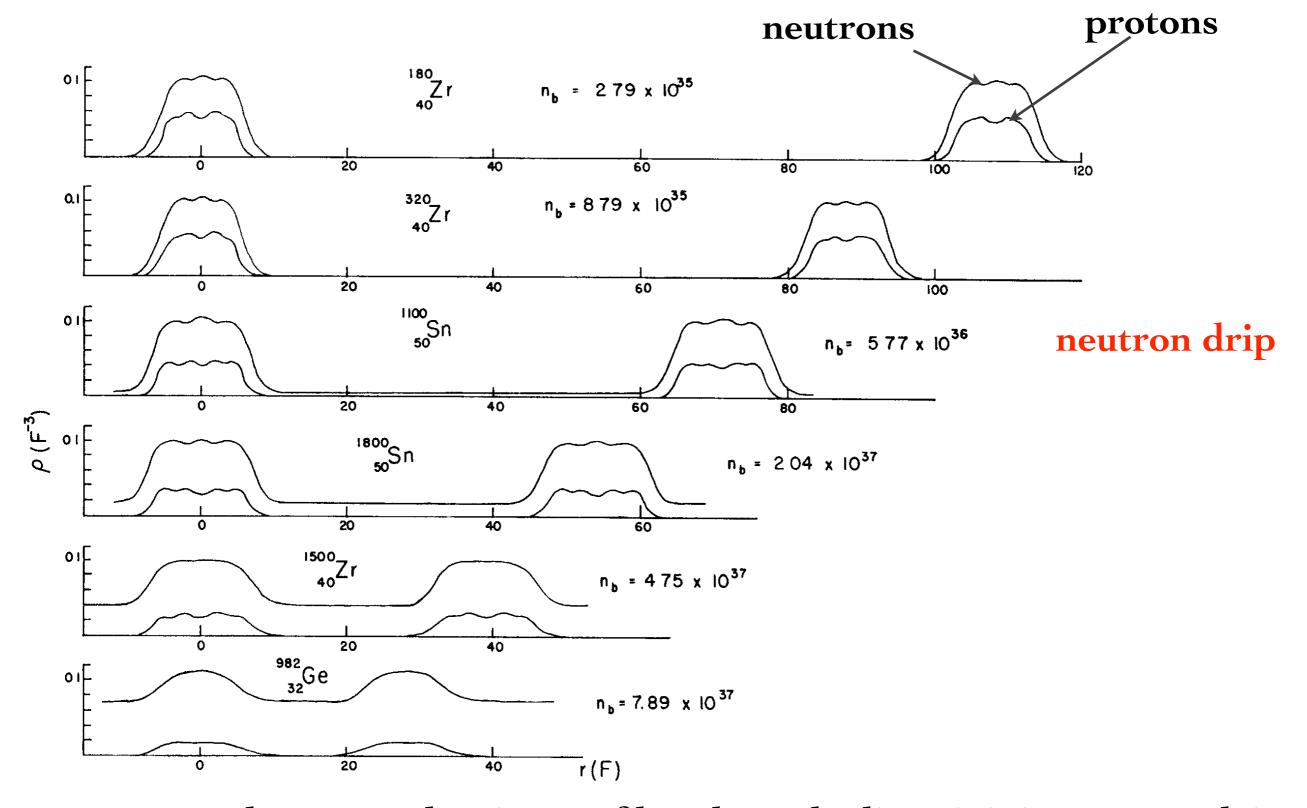
Differently from the "lab case", weak equilibrium in Neutron Stars has all the time to work. Favored isotopes in the NS crust

	Isotope	\mathbb{Z}/A	$ ho_t(\mathrm{g/cm^3})$	μ_{e} (MeV)	
	⁵⁶ Fe	$\sqrt{0.464}$	7.96×10^{6}	0.95	
	⁶² Ni	$\sqrt{0.452}$	2.71×10^{8}	2.61	
	⁶⁴ Ni	0.437	1.3×10^{9}	4.31	
	⁶⁶ Ni	0.424	1.48×10^{9}	4.45	
	⁸⁶ Kr	0.419	3.12×10^{9}	5.66	
Neutron rich	⁸⁴ Se	0.405	1.10×10^{10}	8.49	
Neutron fich	⁸² Ge	0.390	2.80×10^{10}	11.4	
matter	⁸⁰ Zn	0.375	5.44×10^{10}	14.1	
	$\overline{^{78}\mathrm{Ni}}$	0.359	9.64×10^{10}	16.8	many electrons
	¹²⁶ Ru→	0.350	1.29×10^{11}	18.3	
	$\overline{^{124}\mathrm{Mo}}$	0.339	1.88×10^{11}	20.6	
	$^{122}\mathrm{Zr}$	0.328	2.67×10^{11}	22.9	
	$^{120}\mathrm{Sr}$	$\sqrt{0.317}$	3.79×10^{11}	25.4	
	118Kr	$\sqrt{0.305}$	4.31×10^{11}	26.2 / ←	—— neutron drip
				Haense	el and Pichon

Haensel and Pichon Astron. Astrophys. 283 (1994) 313

Then there are many unbound neutrons $Z/A \sim 0.1$

Inner crust $10^{11} \text{ g cm}^{-3} < \rho < 10^{14} \text{ g cm}^{-3}$



Proton and neutron density profiles along the lines joining two nuclei

Quantum chromoynamics

$$\mathcal{L}_{QCD} = \bar{\psi}(i\gamma^{\mu}D_{\mu} + \mu\gamma_0 - M)\psi - \frac{1}{4}F_a^{\mu\nu}F_{\mu\nu}^a$$

quark fields: $\psi_{\alpha,i}$

gluon gauge fields: A

 $\alpha, \beta = 1, 2, 3$ color indices

 $a = 1, \dots, 8$ adjoint color index

 $i, j = 1, \dots, 6$ flavor indices

QCD non-Abelian gauge theory, non-perturbative at energy scales below $\Lambda_{\rm QCD} \sim 200~{
m MeV}$

$$\mathcal{L}_{QCD} = \bar{\psi}(i\gamma^{\mu}D_{\mu} + \mu\gamma_0 - M)\psi - \frac{1}{4}F_a^{\mu\nu}F_{\mu\nu}^a$$

quark fields: $\psi_{\alpha,i}$

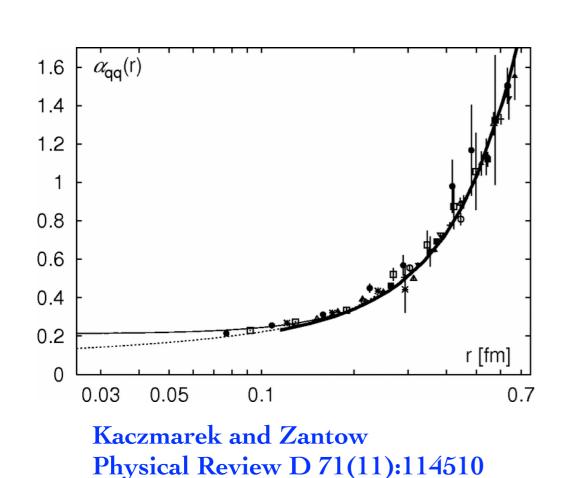
 $\alpha, \beta = 1, 2, 3$ color indices

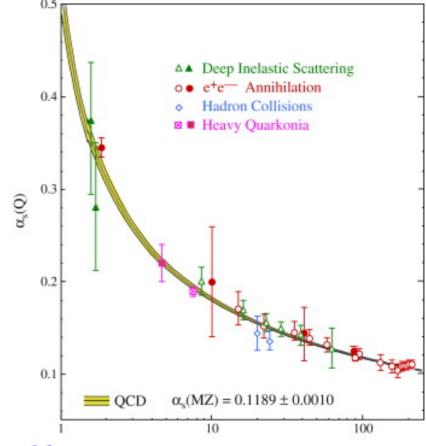
 $i, j = 1, \dots, 6$ flavor indices

gluon gauge fields: A

 $a = 1, \dots, 8$ adjoint color index

QCD non-Abelian gauge theory, non-perturbative at energy scales below $\Lambda_{\rm QCD} \sim 200~{
m MeV}$





S. Bethke, Q[GeV]
Prog.Part.Nucl.Phys. 58 (2007) 351-386

$$\mathcal{L}_{\text{QCD}} = \bar{\psi}(i\gamma^{\mu}D_{\mu} + \mu\gamma_0 - M)\psi - \frac{1}{4}F_a^{\mu\nu}F_{\mu\nu}^a$$

quark fields: $\psi_{\alpha,i}$

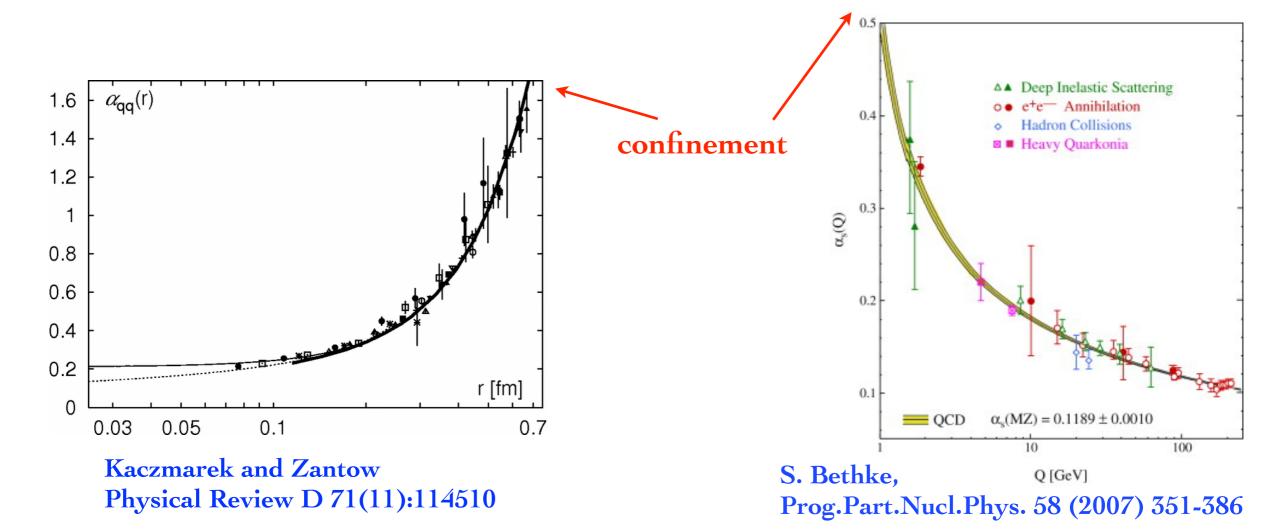
 $\alpha, \beta = 1, 2, 3$ color indices

 $i, j = 1, \dots, 6$ flavor indices

gluon gauge fields: A^a

 $a = 1, \dots, 8$ adjoint color index

QCD non-Abelian gauge theory, non-perturbative at energy scales below $\Lambda_{\rm QCD} \sim 200~{
m MeV}$



$$\mathcal{L}_{QCD} = \bar{\psi}(i\gamma^{\mu}D_{\mu} + \mu\gamma_0 - M)\psi - \frac{1}{4}F_a^{\mu\nu}F_{\mu\nu}^a$$

quark fields: $\psi_{\alpha,i}$

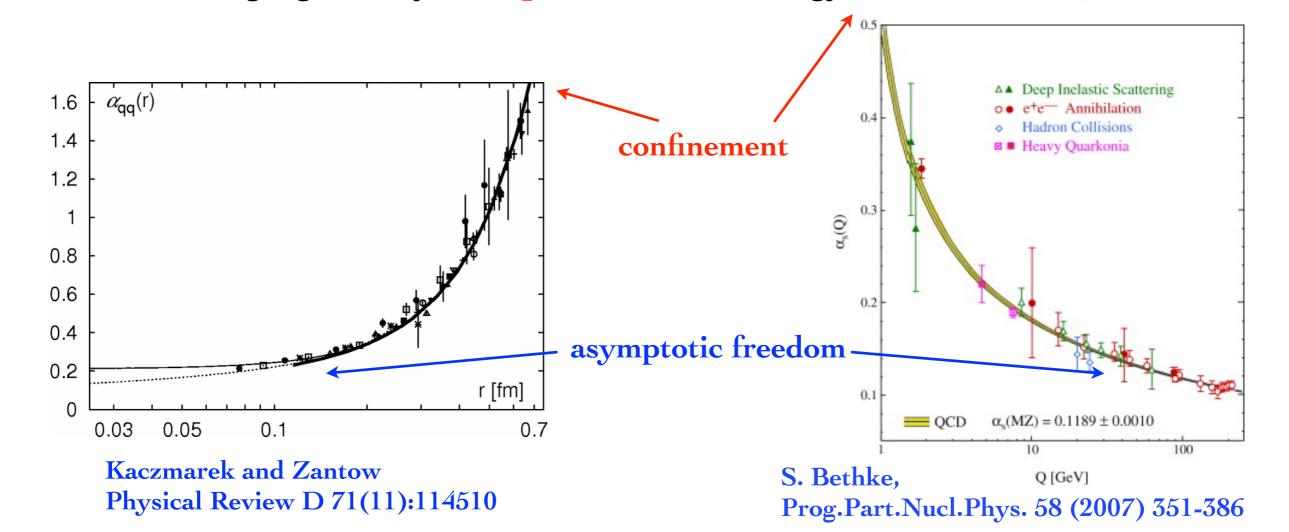
 $\alpha, \beta = 1, 2, 3$ color indices

 $i, j = 1, \dots, 6$ flavor indices

gluon gauge fields: A^a

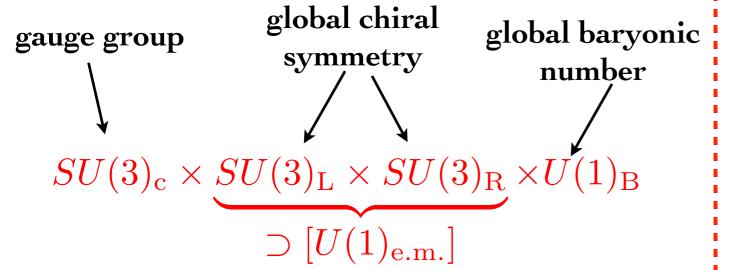
 $a = 1, \dots, 8$ adjoint color index

QCD non-Abelian gauge theory, non-perturbative at energy scales below $\Lambda_{\rm QCD} \sim 200~{
m MeV}$



$$m = 0$$

Three flavor massless quark matter



$$m \to \infty$$

Quenched QCD (pure Yang-Mills)

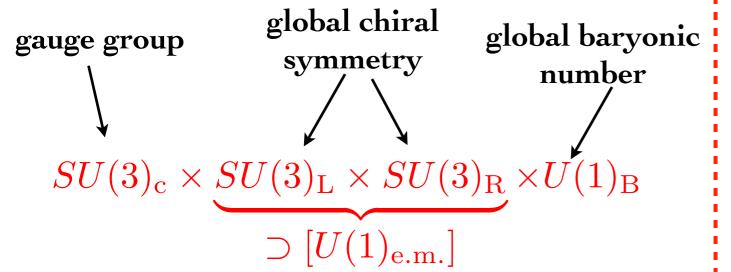
Polyakov loop

$$L = \mathcal{P} \exp \left[i \int_0^\beta dx_4 A_4 \right]$$

remarkably $e^{-\beta F_q} = \langle L \rangle$

$$m = 0$$

Three flavor massless quark matter



Chiral symmetry amounts to rotate independently the left- and right-handed quark fields

$$m \to \infty$$

Quenched QCD (pure Yang-Mills)

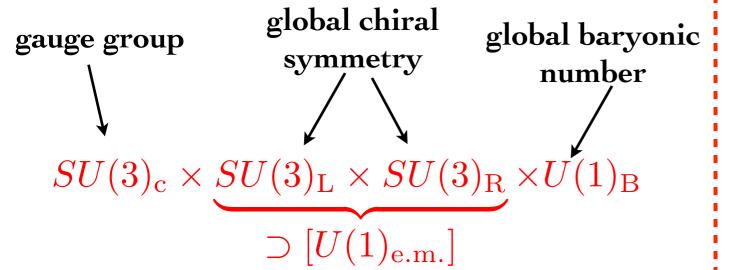
Polyakov loop

$$L = \mathcal{P} \exp\left[i \int_0^\beta dx_4 A_4\right]$$

remarkably $e^{-\beta F_q} = \langle L \rangle$

$$m = 0$$

Three flavor massless quark matter



Chiral symmetry amounts to rotate independently the left- and right-handed quark fields

These rotations can be locked by the $\langle \bar{\psi} \psi \rangle$ condensate

$$m \to \infty$$

Quenched QCD (pure Yang-Mills)

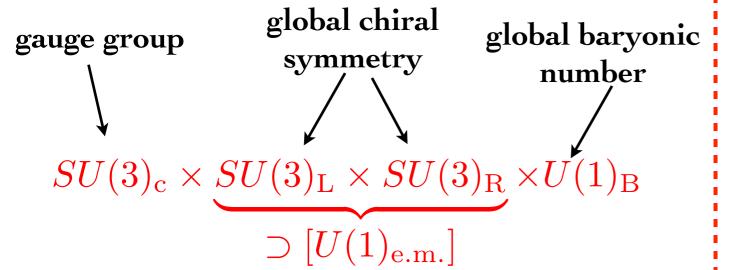
Polyakov loop

$$L = \mathcal{P} \exp\left[i \int_0^\beta dx_4 A_4\right]$$

remarkably $e^{-\beta F_q} = \langle L \rangle$

$$m = 0$$

Three flavor massless quark matter



Chiral symmetry amounts to rotate independently the left- and right-handed quark fields

These rotations can be locked by the $\langle \bar{\psi}\psi \rangle$ condensate

$$m \to \infty$$

Quenched QCD (pure Yang-Mills)

Polyakov loop

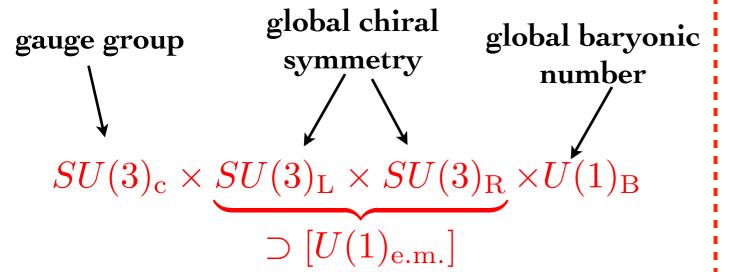
$$L = \mathcal{P} \exp \left[i \int_0^\beta dx_4 A_4 \right]$$

remarkably $e^{-\beta F_q} = \langle L \rangle$

Gauge invariant, but sensitive to the center symmetry:

$$m = 0$$

Three flavor massless quark matter



Chiral symmetry amounts to rotate independently the left- and right-handed quark fields

These rotations can be locked by the $\langle \bar{\psi} \psi \rangle$ condensate

$$m \to \infty$$

Quenched QCD (pure Yang-Mills)

Polyakov loop

$$L = \mathcal{P} \exp\left[i \int_0^\beta dx_4 A_4\right]$$

remarkably $e^{-\beta F_q} = \langle L \rangle$

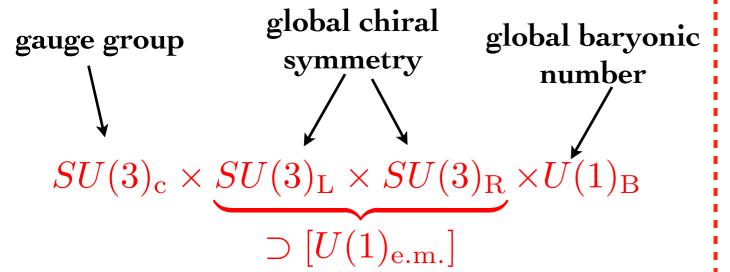
Gauge invariant, but sensitive to the center symmetry:

$$L \to L' = z_k L$$

with
$$z_k = e^{2\pi i k/N_c}$$

$$m = 0$$

Three flavor massless quark matter



Chiral symmetry amounts to rotate independently the left- and right-handed quark fields

These rotations can be locked by the $\langle \bar{\psi} \psi \rangle$ condensate

Low T: chiral symmetry broken $\langle \bar{\psi}\psi \rangle \neq 0$

High T: chiral symmetry holds $\langle \bar{\psi}\psi \rangle = 0$

$$m \to \infty$$

Quenched QCD (pure Yang-Mills)

Polyakov loop

$$L = \mathcal{P} \exp\left[i \int_0^\beta dx_4 A_4\right]$$

remarkably $e^{-\beta F_q} = \langle L \rangle$

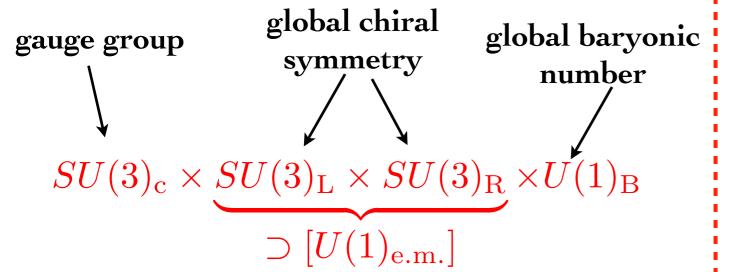
Gauge invariant, but sensitive to the center symmetry:

$$L \to L' = z_k L$$

with
$$z_k = e^{2\pi i k/N_c}$$

$$m = 0$$

Three flavor massless quark matter



Chiral symmetry amounts to rotate independently the left- and right-handed quark fields

These rotations can be locked by the $\langle \bar{\psi} \psi \rangle$ condensate

Low T: chiral symmetry broken $\langle \bar{\psi}\psi \rangle \neq 0$

High T: chiral symmetry holds $\langle \bar{\psi}\psi \rangle = 0$

$$m \to \infty$$

Quenched QCD (pure Yang-Mills)

Polyakov loop

$$L = \mathcal{P} \exp \left[i \int_0^\beta dx_4 A_4 \right]$$

remarkably $e^{-\beta F_q} = \langle L \rangle$

Gauge invariant, but sensitive to the center symmetry:

$$L \to L' = z_k L$$

with
$$z_k = e^{2\pi i k/N_c}$$

Low T: the center symmetry holds

$$\langle L \rangle = 0$$

High T: The center symmetry is broken

$$\langle L \rangle \neq 0$$

Deconfinement and chiral symmetry breaking

m: mass of quark fields

m

Quenched QCD (pure Yang-Mills) $m \to \infty$

Center symmetry: $Z(N_c)$, broken at T_D (first order phase transition)

Order parameter for deconfinement: <Polyakov loop>

Chiral limit m=0

Center symmetry: $SU(N_F)_L \times SU(N_F)_R$, broken at T_{χ}

Order parameter for chiral symmetry breaking: chiral condensate $\langle \bar{\psi} \psi \rangle$

Deconfinement and chiral symmetry breaking

m: mass of quark fields

m

Quenched QCD (pure Yang-Mills) $m \to \infty$

Center symmetry: $Z(N_c)$, broken at T_D (first order phase transition)

Order parameter for deconfinement: <Polyakov loop>

QCD T_D and T_{χ} are pseudo-critical temperatures

Chiral limit m=0

Center symmetry: $SU(N_F)_L \times SU(N_F)_R$, broken at T_{χ}

Order parameter for chiral symmetry breaking: chiral condensate $\langle \bar{\psi} \psi \rangle$

To keep in mind

1) The Polyakov loop is related to quark confinement, not to gluon confinement.

Weird thing: In a theory with no dynamical quarks, the <Polyakov loop> is related to the confinement of quarks.

To keep in mind

1) The Polyakov loop is related to quark confinement, not to gluon confinement.

Weird thing: In a theory with no dynamical quarks, the <Polyakov loop> is related to the confinement of quarks.

2) There is no fundamental reason why T_D and T_χ should be the same. However, QCD has only one scale, and it is natural to expect that these pseudo-critical temperatures are similar

To keep in mind

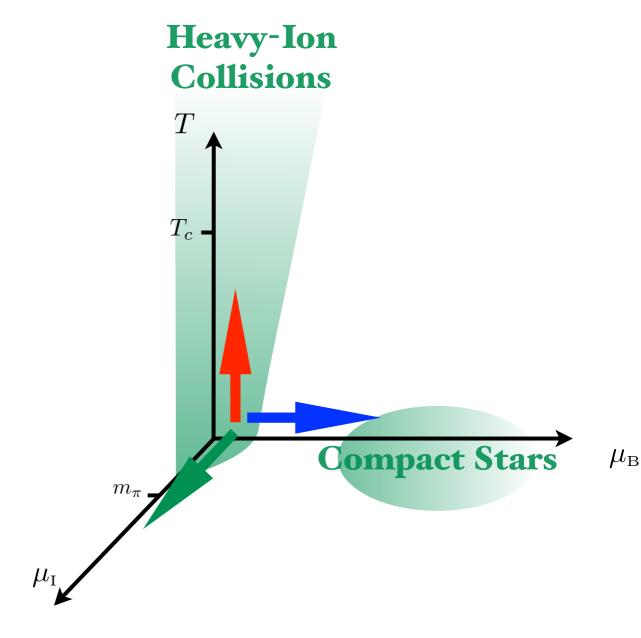
1) The Polyakov loop is related to quark confinement, not to gluon confinement.

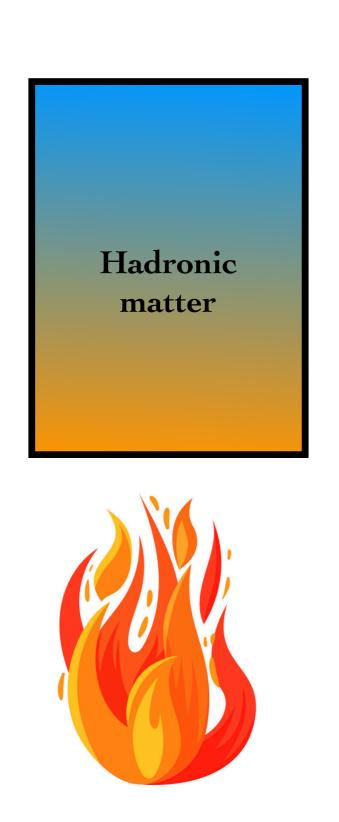
Weird thing: In a theory with no dynamical quarks, the <Polyakov loop> is related to the confinement of quarks.

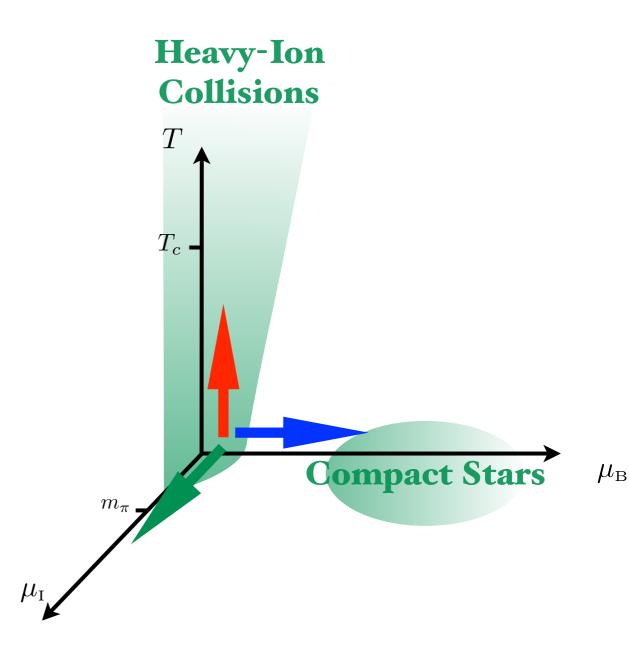
2) There is no fundamental reason why T_D and T_χ should be the same. However, QCD has only one scale, and it is natural to expect that these pseudo-critical temperatures are similar

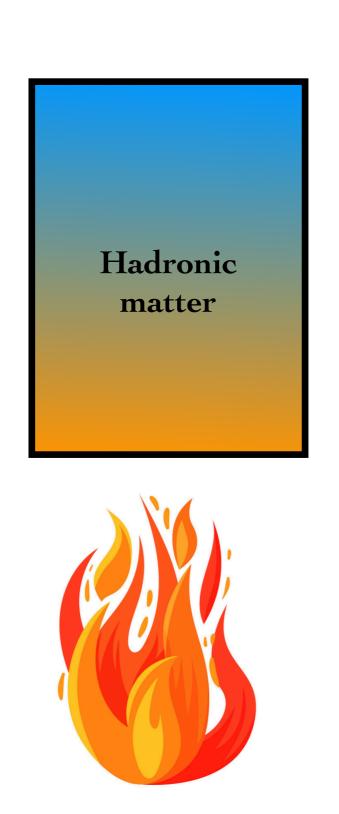
3) Apart from these theory group arguments, it is important to have a phenomenological description of confinement (and chiral symmetry breaking) as associated to a change of degrees of freedom.

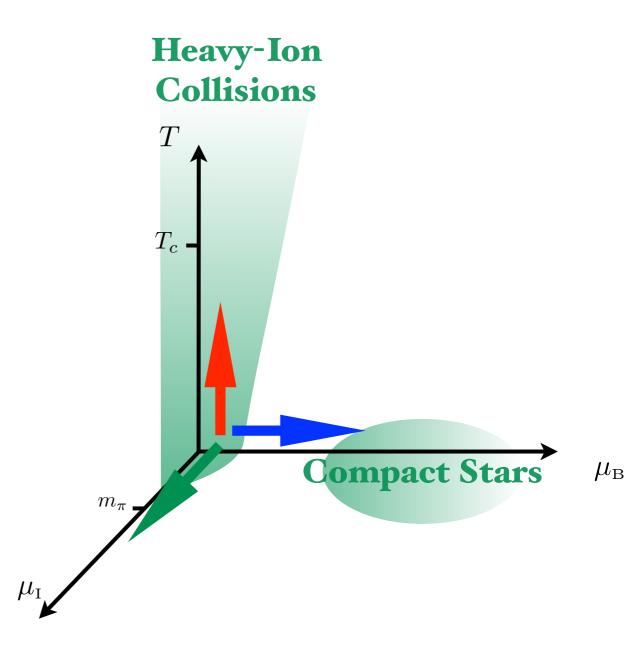


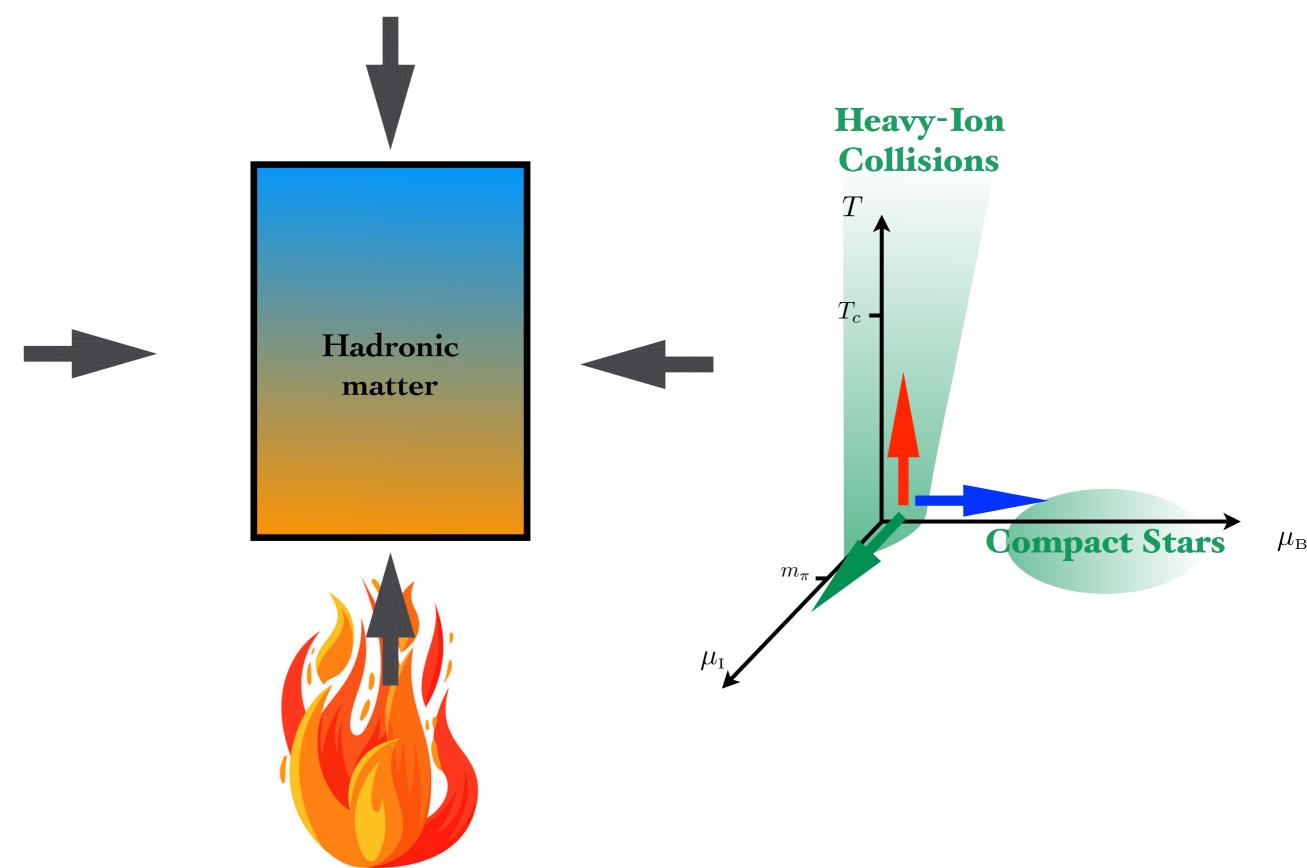


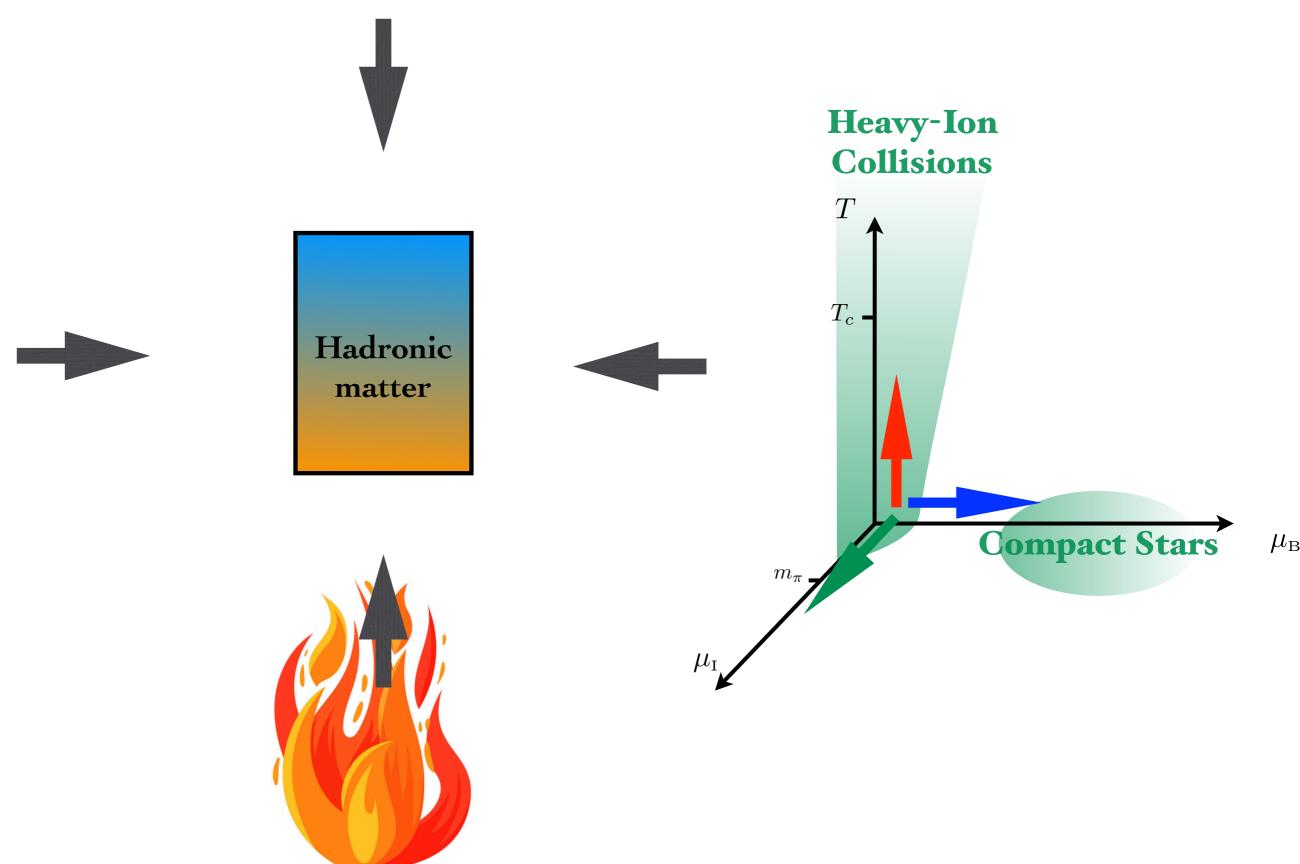


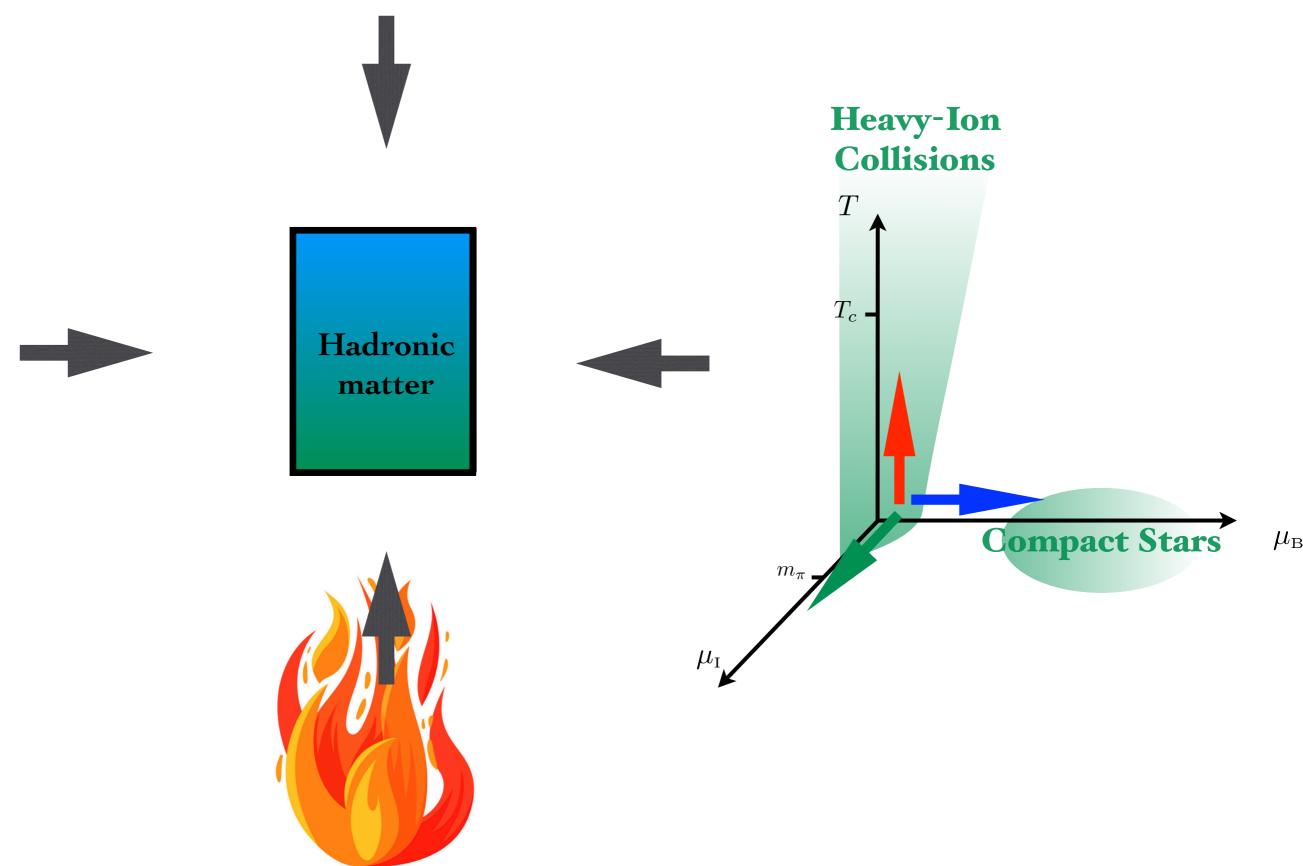










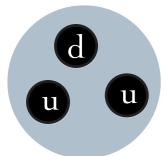


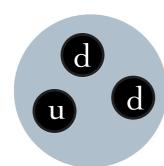
CONFINED HADRONS

BARYONS

proton

neutron



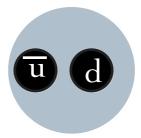


$$m_n \sim 1 \text{GeV} \gg m_{u,d}$$

 $r_n \sim 1 \text{fm} = 10^{-15} \text{m}$

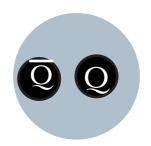
MESONS

pions



$$m_\pi \sim 135 \,\, {
m MeV} \gg m_{u,d}$$
 $r_\pi \sim 0.7 {
m fm} \qquad m_u = m_d
eq 0$ C. Patrignani et al. (PDG)

Heavy mesons

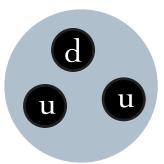


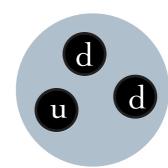
CONFINED HADRONS

BARYONS

proton

neutron





••••

$$m_n \sim 1 \text{GeV} \gg m_{u,d}$$

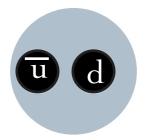
 $r_n \sim 1 \text{fm} = 10^{-15} \text{m}$

In the infrared baryons are blob of gluons with 3 valence quarks.

Not a "bound state" of quarks, rather a soliton or in any case a nonperturbative object.

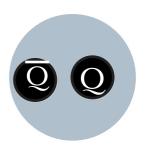
MESONS

pions



$$m_\pi \sim 135 \,\, {
m MeV} \gg m_{u,d}$$
 $r_\pi \sim 0.7 {
m fm}$ $m_u = m_d
eq 0$ C. Patrignani et al. (PDG)

Heavy mesons

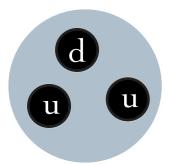


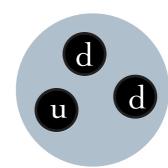
CONFINED HADRONS

BARYONS

proton

neutron





• • • •

$$m_n \sim 1 \text{GeV} \gg m_{u,d}$$

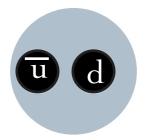
 $r_n \sim 1 \text{fm} = 10^{-15} \text{m}$

In the infrared baryons are blob of gluons with 3 valence quarks.

Not a "bound state" of quarks, rather a soliton or in any case a nonperturbative object.

MESONS

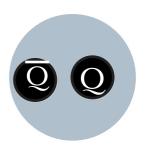
pions



$$m_\pi \sim 135 \,\, {
m MeV} \gg m_{u,d}$$
 $r_\pi \sim 0.7 {
m fm}$ $m_u = m_d
eq 0$ C. Patrignani et al. (PDG)

(pseudo) Nambu-Goldstone bosons

Heavy mesons

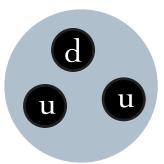


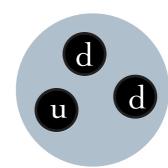
CONFINED HADRONS

BARYONS

proton

neutron





••••

$$m_n \sim 1 \text{GeV} \gg m_{u,d}$$

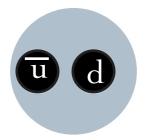
 $r_n \sim 1 \text{fm} = 10^{-15} \text{m}$

In the infrared baryons are blob of gluons with 3 valence quarks.

Not a "bound state" of quarks, rather a soliton or in any case a nonperturbative object.

MESONS

pions



$$m_{\pi} \sim 135 \,\, \mathrm{MeV} \gg m_{u,d}$$
 $r_{\pi} \sim 0.7 \mathrm{fm}$ $m_{u} = m_{d} \neq 0$ C. Patrignani et al. (PDG)

(pseudo) Nambu-Goldstone bosons

Heavy mesons



Nonrelativistic object

The double role of mesons

Pions can be associated with the spontaneous chiral symmetry breaking

$$SU(2)_L \times SU(2)_R \times U(1)_B$$

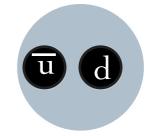
$$\supset [U(1)_{\text{e.m.}}]$$

$$\langle \bar{\psi}\psi \rangle \neq 0$$

$$SU(2)_V \times U(1)_B$$

$$\supset [U(1)_{\text{e.m.}}]$$

pions



$$m_{\pi} \sim 135 \text{ MeV} \gg m_{u,d}$$
 $r_{\pi} \sim 0.7 \text{fm}$

3 (pseudo) Nambu-Goldstone bosons (NGBs)

The double role of mesons

Pions can be associated with the spontaneous chiral symmetry breaking

$$SU(2)_{L} \times SU(2)_{R} \times U(1)_{B}$$

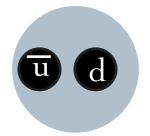
$$\supset [U(1)_{\text{e.m.}}]$$

$$\langle \bar{\psi}\psi \rangle \neq 0$$

$$SU(2)_{V} \times U(1)_{B}$$

$$\supset [U(1)_{\text{e.m.}}]$$

pions



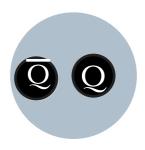
 $m_{\pi} \sim 135 \text{ MeV} \gg m_{u,d}$ $r_{\pi} \sim 0.7 \text{fm}$

3 (pseudo) Nambu-Goldstone bosons (NGBs)

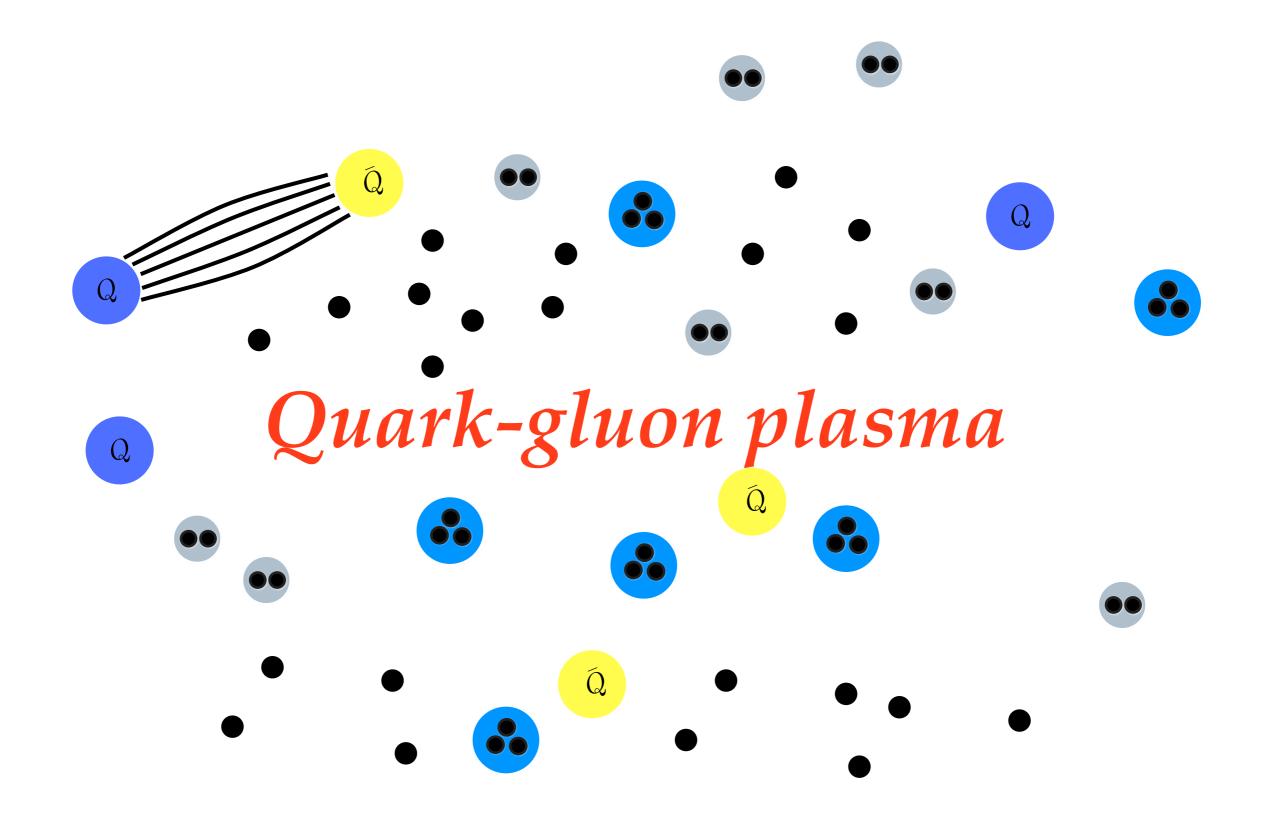
Heavy mesons can be thought as bound states of heavy quarks:
The mass of a heavy meson is smaller than the mass of its constituents.

Good for probing confinement

Heavy mesons



Nonrelativistic models



Deconfinement by increasing temperature

Mesons

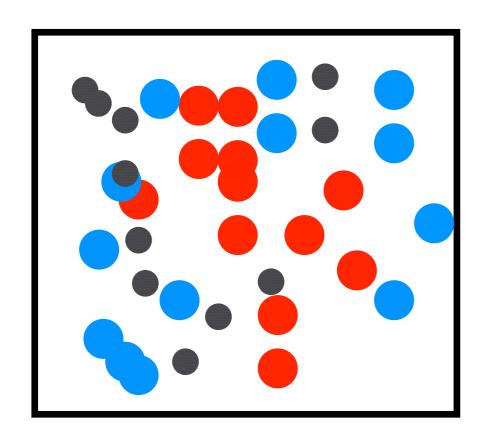
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

At a critical temperature there is saturation: the nucleons lose their identity and start to overlap. Quarks and gluons are liberated

Mesons

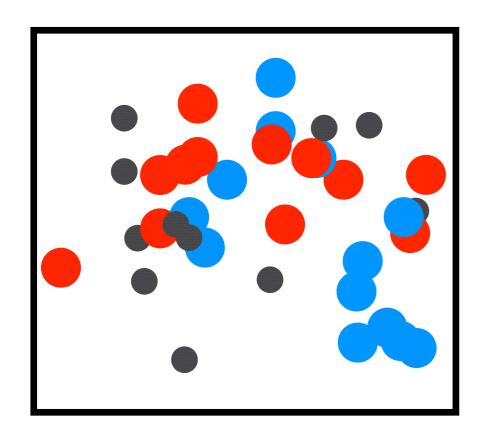
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

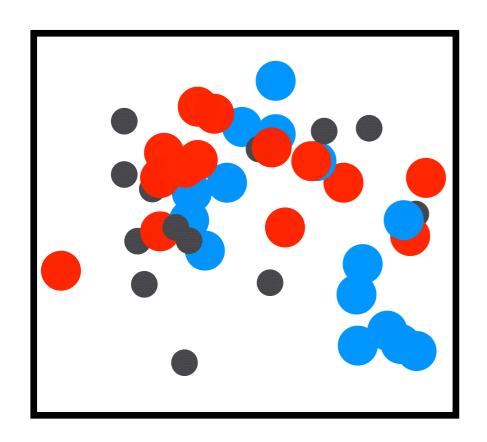
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

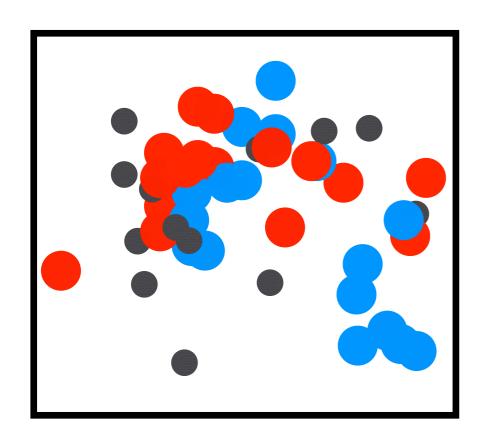
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

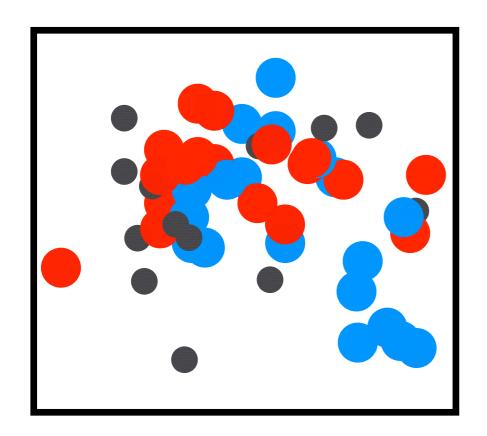
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

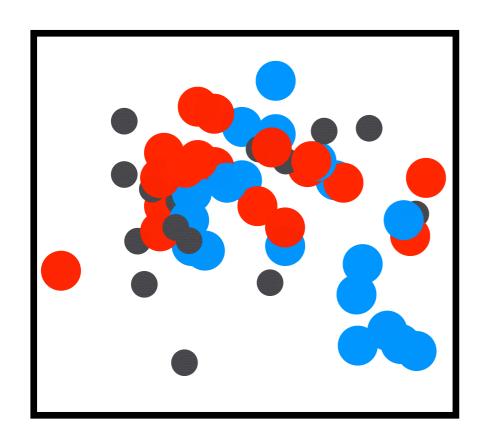
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

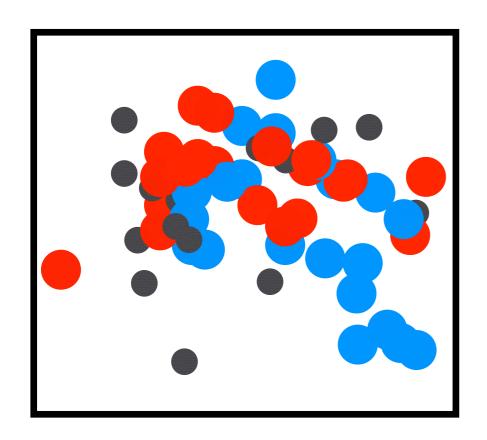
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

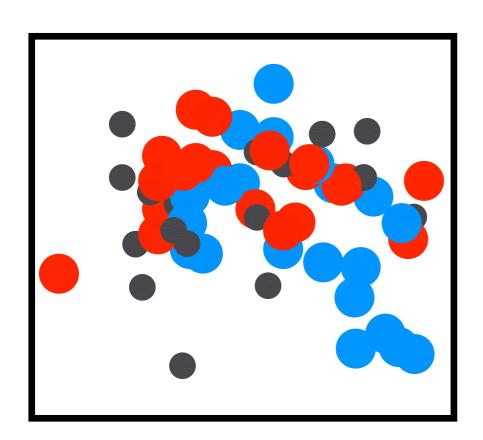
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

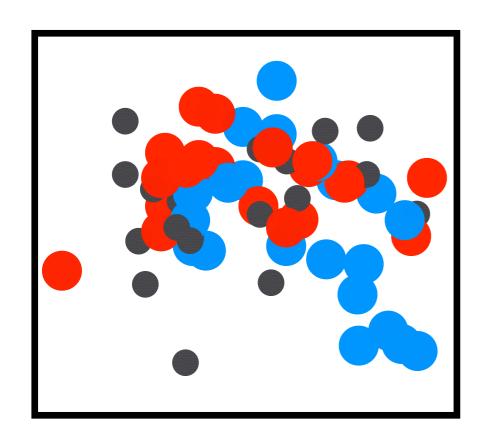
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

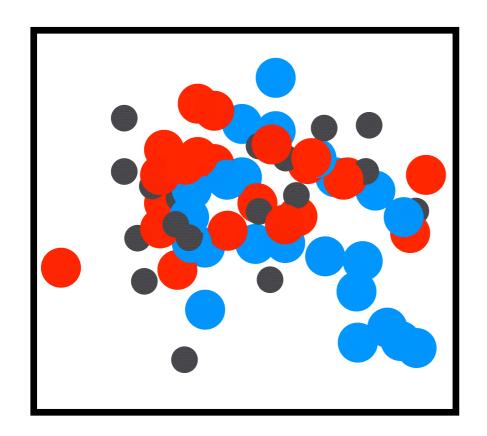
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

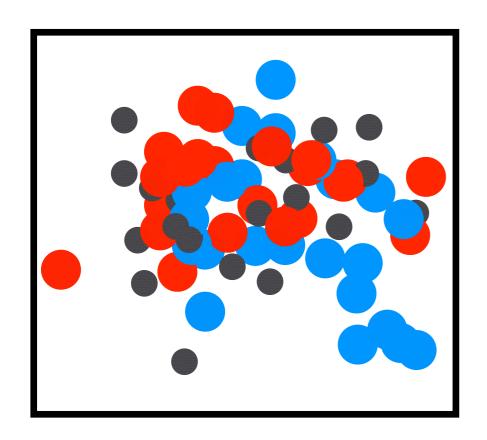
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

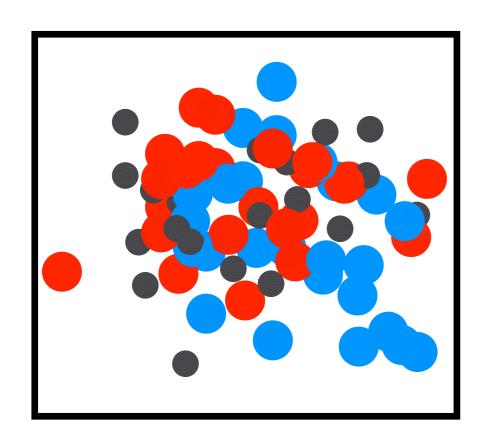
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

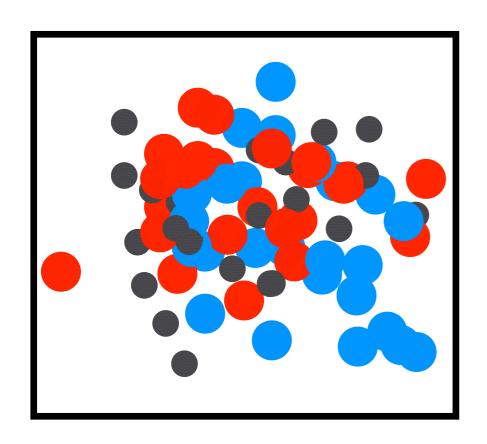
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

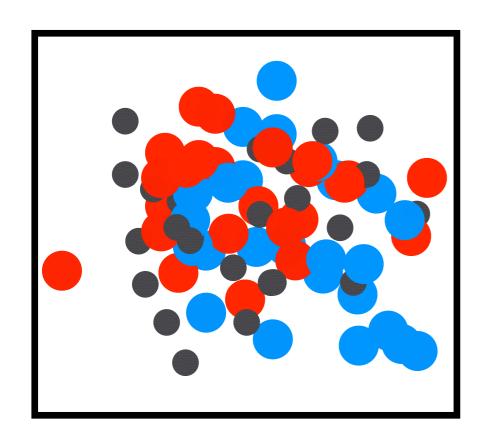
Baryons



Anti Baryons



Increasing T Fixed low μ_B



At high energies, matter interact so strongly to produce a large number of mesons and baryons

Mesons

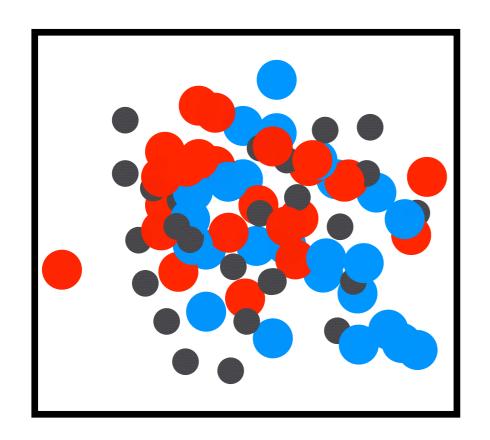
Baryons



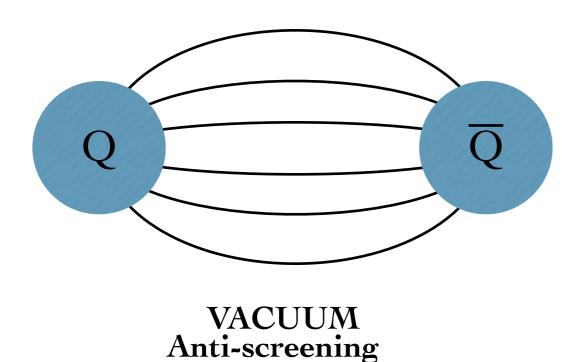
Anti Baryons



Increasing T Fixed low μ_B

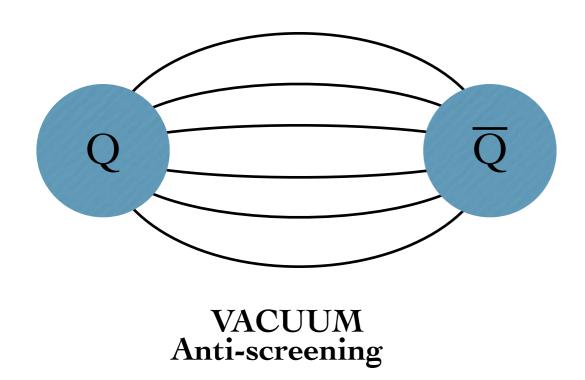


At high energies, matter interact so strongly to produce a large number of mesons and baryons



- 1) Dual superconductor
- 2) It is a bound state
- 3) Strong decay is OZI suppressed
- 4) Potential models can be used

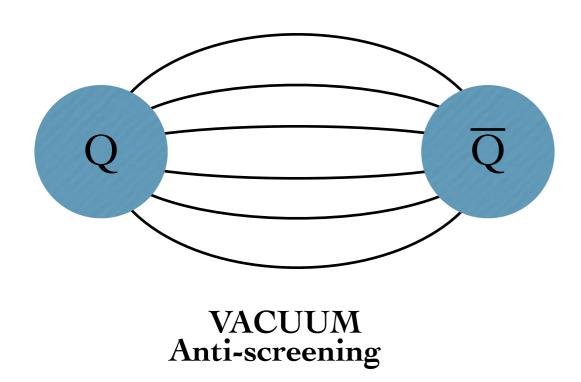
$$V(r) \sim \sigma r - \frac{\alpha}{r}$$



- 1) Dual superconductor
- 2) It is a bound state
- 3) Strong decay is OZI suppressed
- 4) Potential models can be used

$$V(r) \sim \sigma r - \frac{\alpha}{r}$$

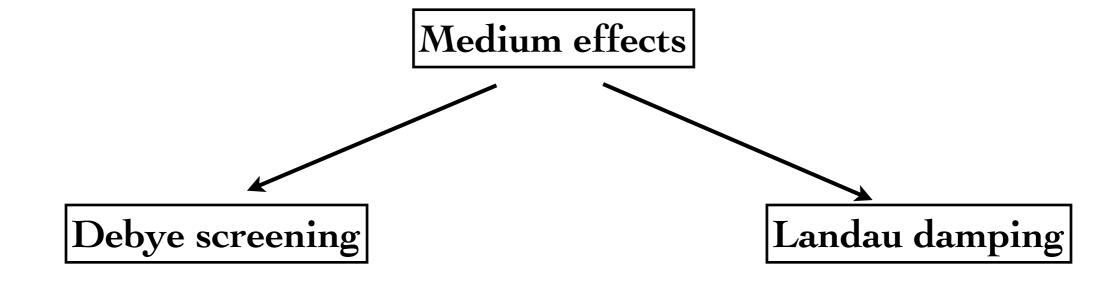
Increasing T and/or μ_B HQ can dissociate by the combination of different effects

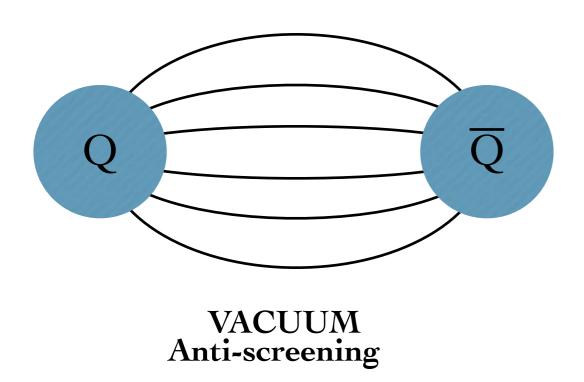


- 1) Dual superconductor
- 2) It is a bound state
- 3) Strong decay is OZI suppressed
- 4) Potential models can be used

$$V(r) \sim \sigma r - \frac{\alpha}{r}$$

Increasing T and/or μ_B HQ can dissociate by the combination of different effects

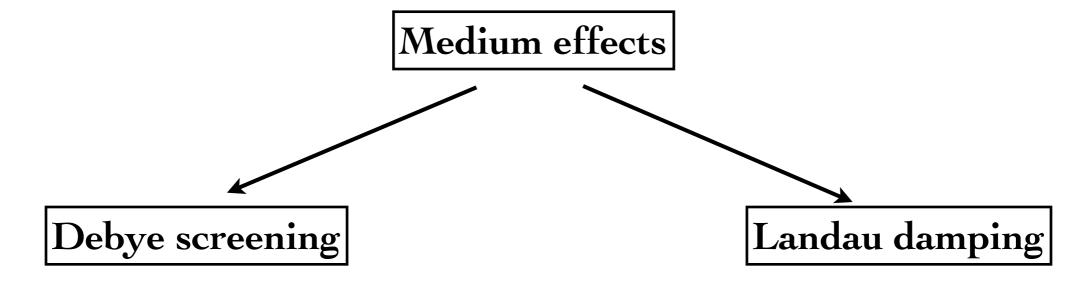


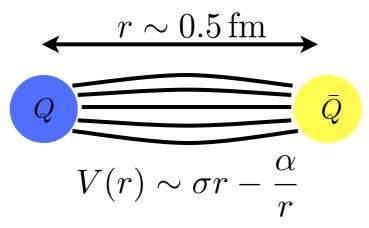


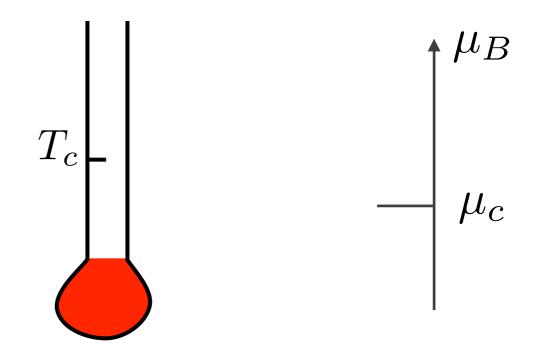
- 1) Dual superconductor
- 2) It is a bound state
- 3) Strong decay is OZI suppressed
- 4) Potential models can be used

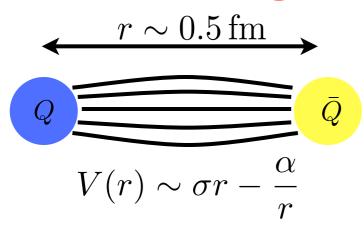
$$V(r) \sim \sigma r - \frac{\alpha}{r}$$

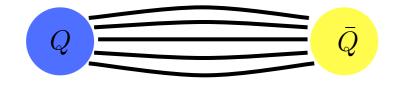
Increasing T and/or μ_B HQ can dissociate by the combination of different effects

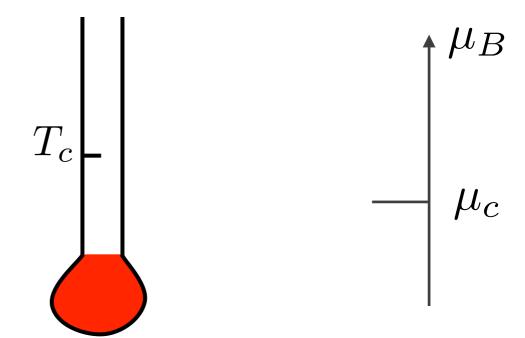


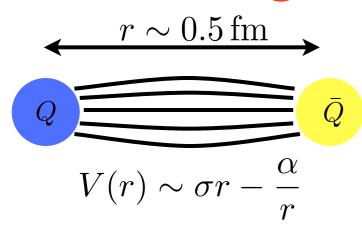


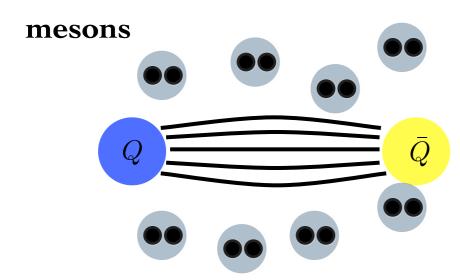


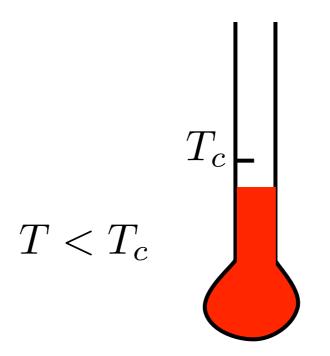


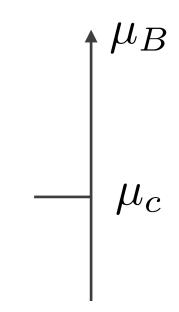


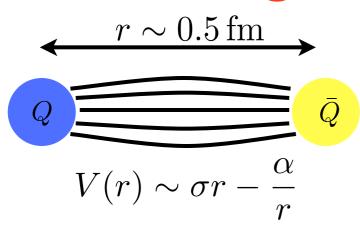


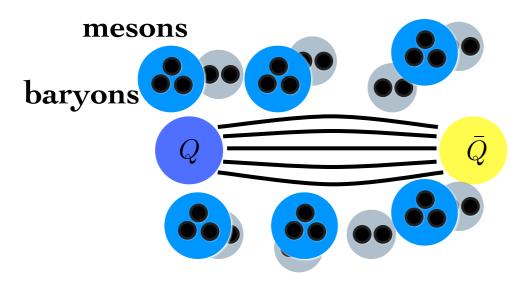


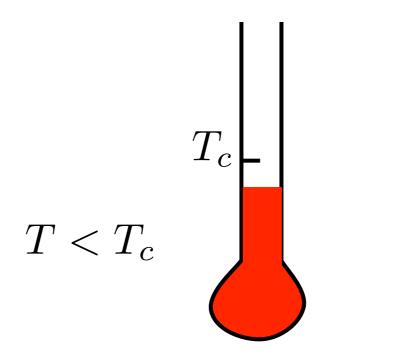


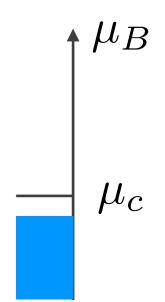


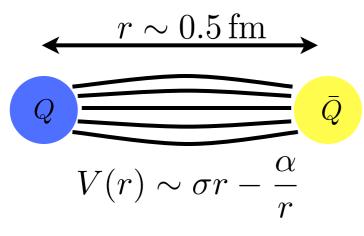


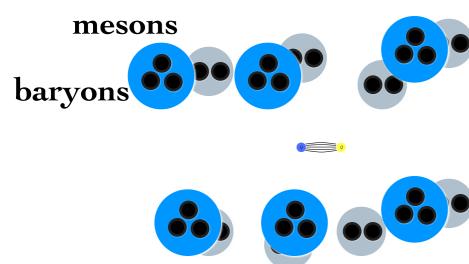


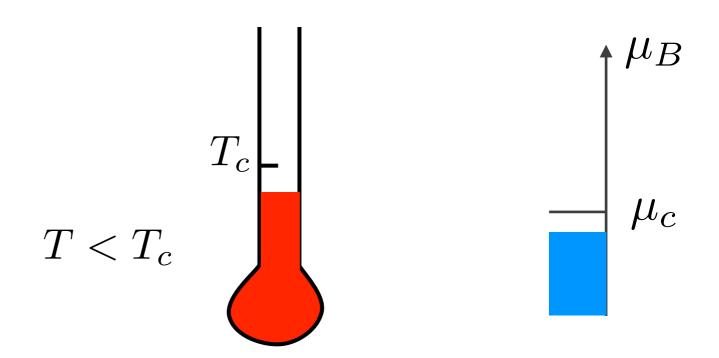


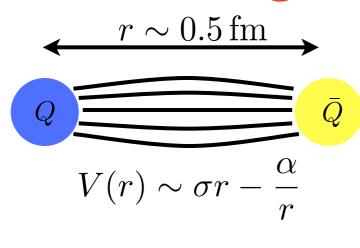


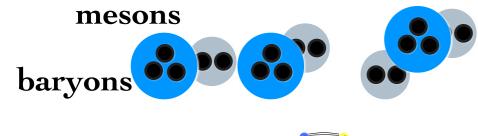




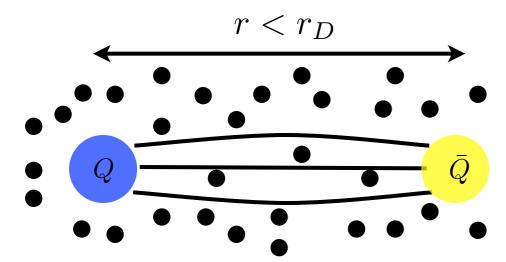


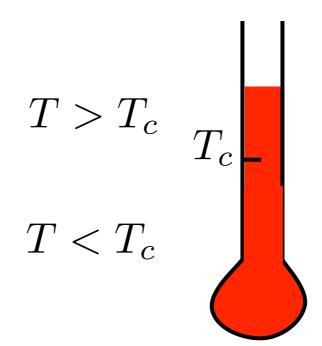


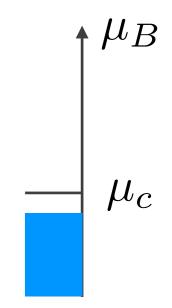


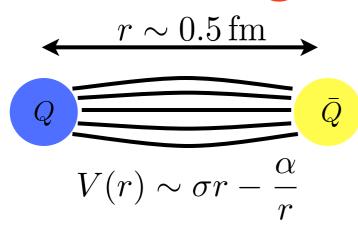


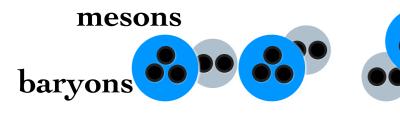


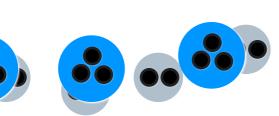


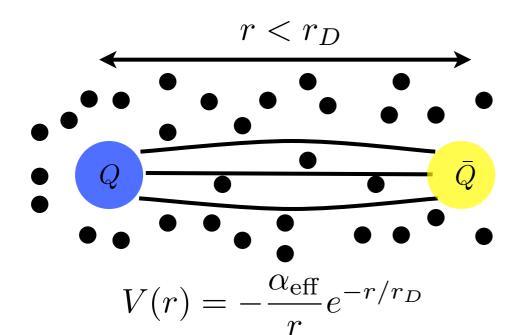


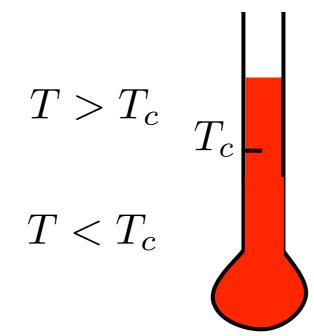


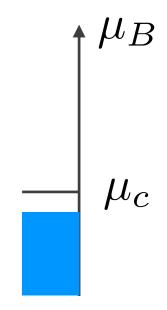


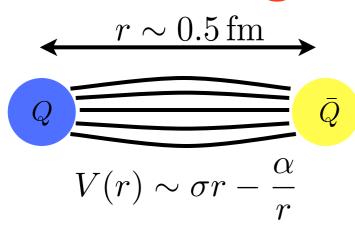


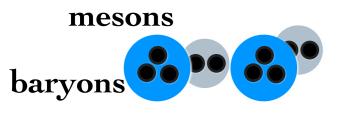




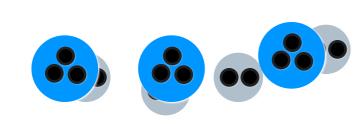


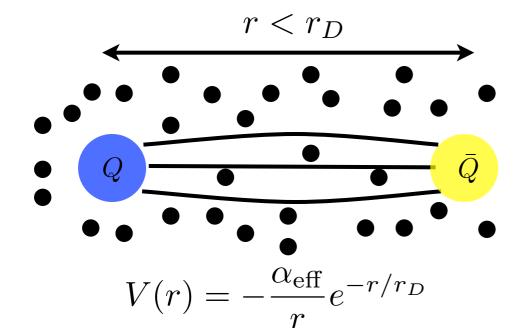




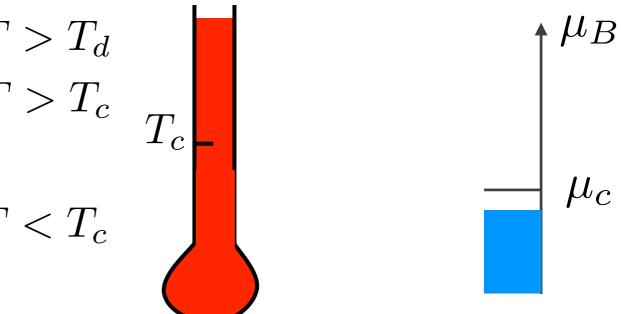


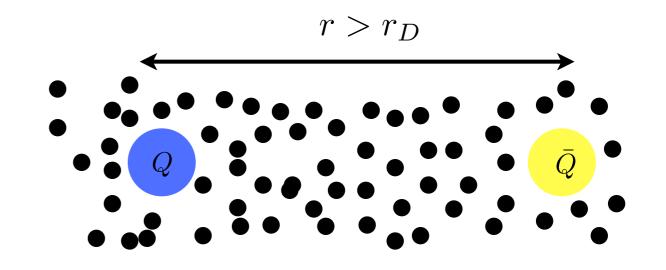


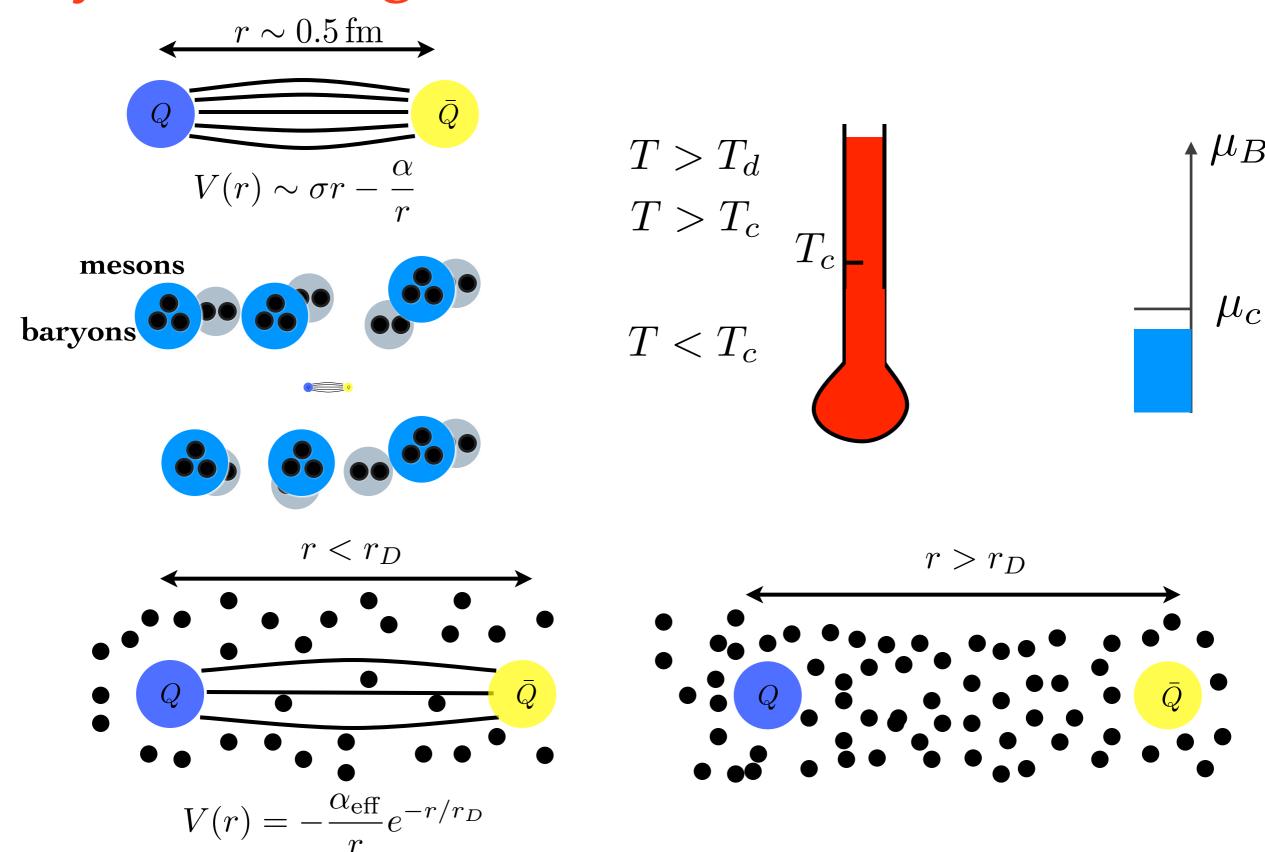




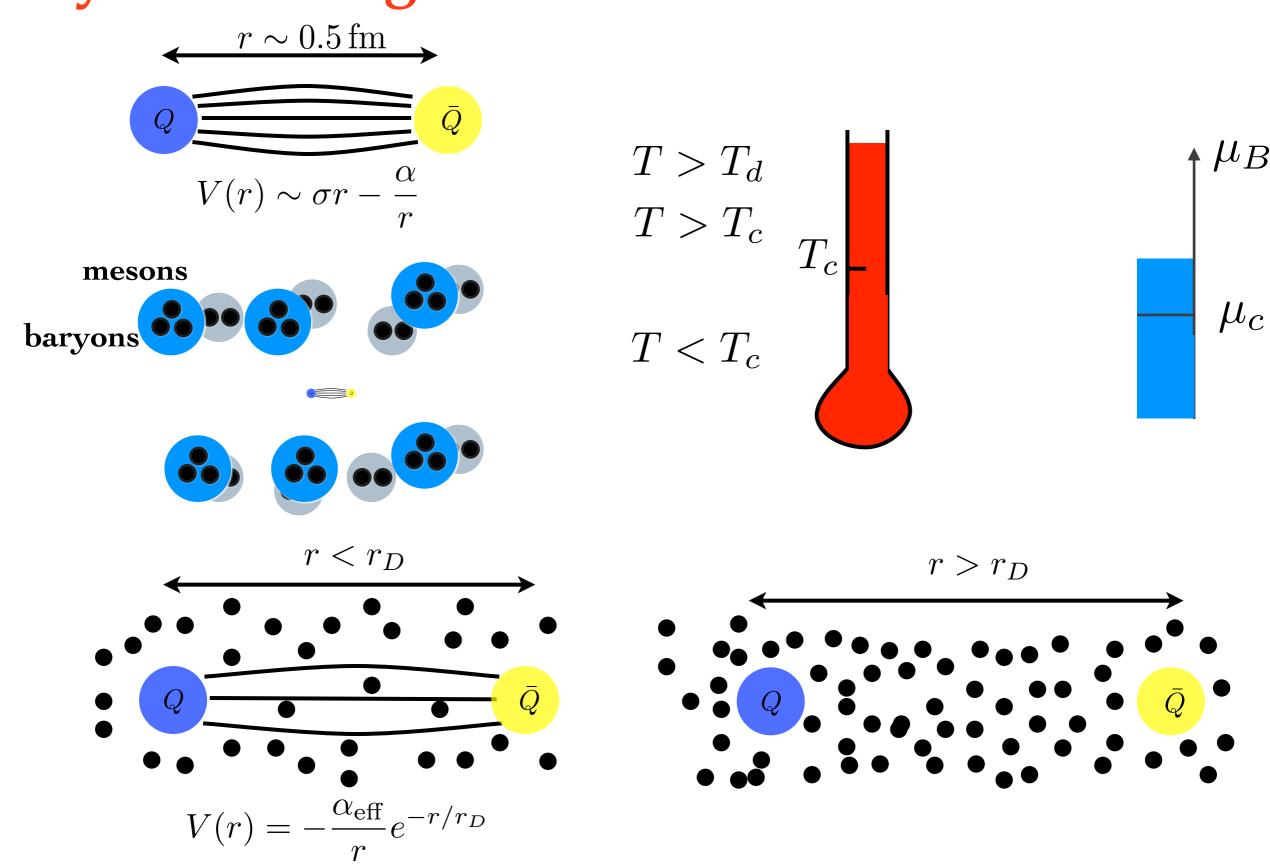
$$T > T_d$$
 $T > T_c$
 T_c
 $T < T_c$







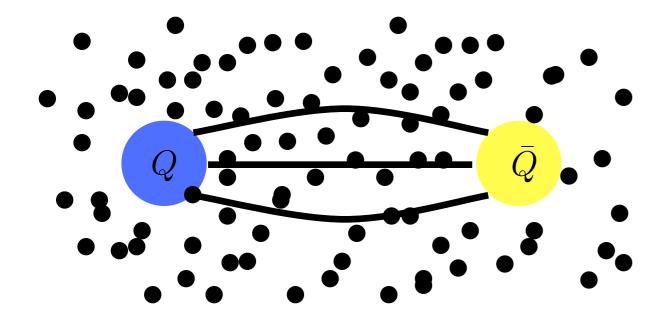
The plasma screens chromo-electric fields: thermal unbinding Matsui and Satz, (1986).



The plasma screens chromo-electric fields: thermal unbinding Matsui and Satz, (1986). Expect similar effect by μ_B : Kakade and Patra, (2015), Carignano and Soto, (2020).

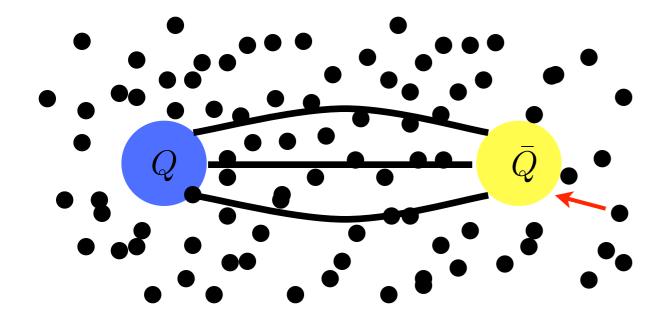
In a thermal medium, no strictly stationary bound state exists.

Interactions with the particles of the medium imply a finite lifetime for all states.



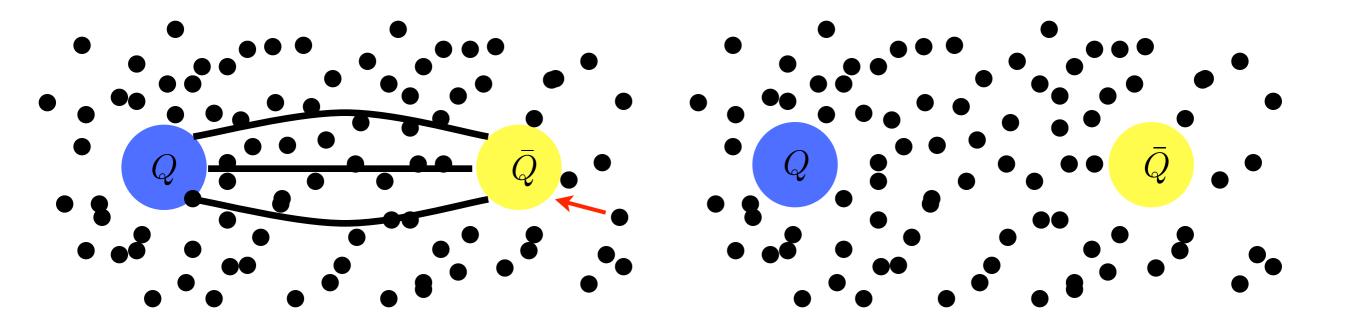
In a thermal medium, no strictly stationary bound state exists.

Interactions with the particles of the medium imply a finite lifetime for all states.



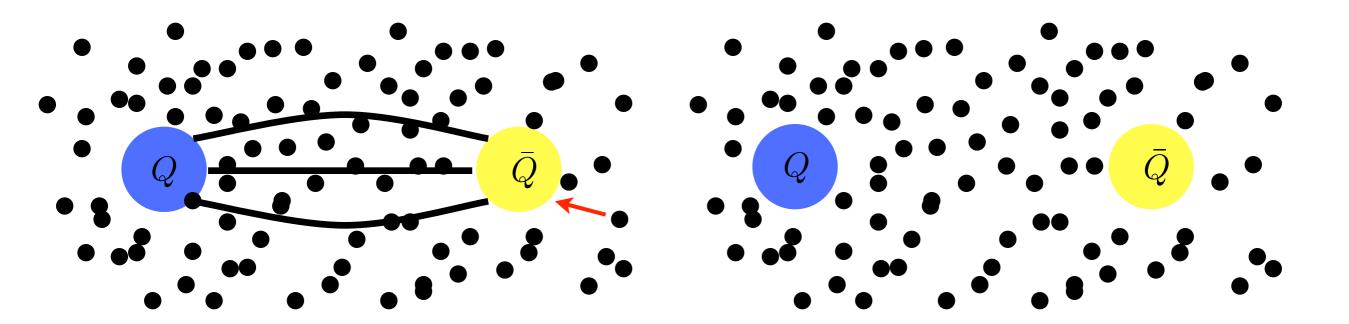
In a thermal medium, no strictly stationary bound state exists.

Interactions with the particles of the medium imply a finite lifetime for all states.



In a thermal medium, no strictly stationary bound state exists.

Interactions with the particles of the medium imply a finite lifetime for all states.

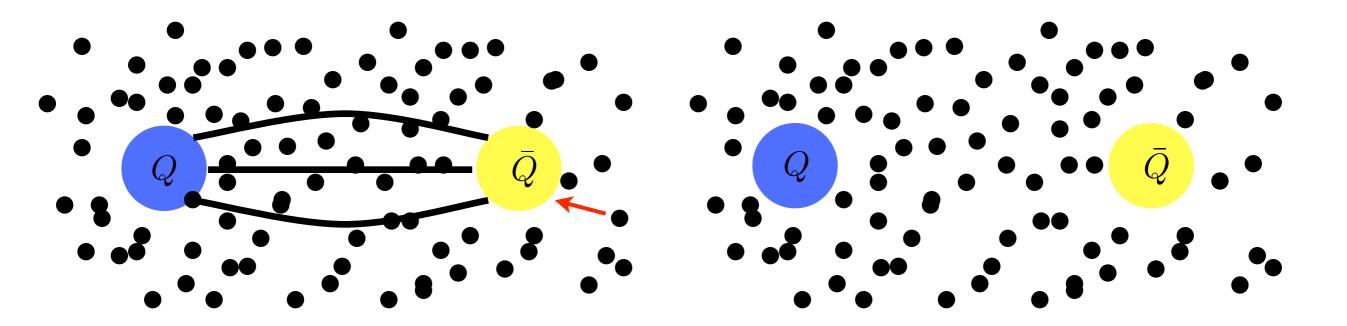


Broadening of the energy levels ↔ imaginary part of the energy eigenvalues. In a Schroedinger equation this corresponds to an imaginary part of the potential.

M. Laine et al. JHEP 0703, 054 (2007)

In a thermal medium, no strictly stationary bound state exists.

Interactions with the particles of the medium imply a finite lifetime for all states.



Broadening of the energy levels ↔ imaginary part of the energy eigenvalues. In a Schroedinger equation this corresponds to an imaginary part of the potential.

M. Laine et al. JHEP 0703, 054 (2007)

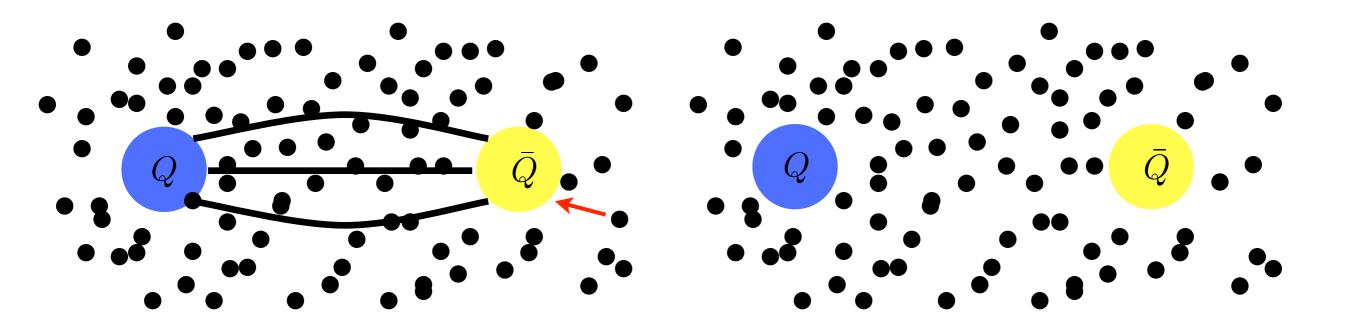
Analogous to photodissociation of molecules like

$$O_2 + \gamma \rightarrow 2O$$

in a heat bath.

In a thermal medium, no strictly stationary bound state exists.

Interactions with the particles of the medium imply a finite lifetime for all states.



Broadening of the energy levels ↔ imaginary part of the energy eigenvalues. In a Schroedinger equation this corresponds to an imaginary part of the potential.

M. Laine et al. JHEP 0703, 054 (2007)

Analogous to photodissociation of molecules like

$$O_2 + \gamma \rightarrow 2O$$

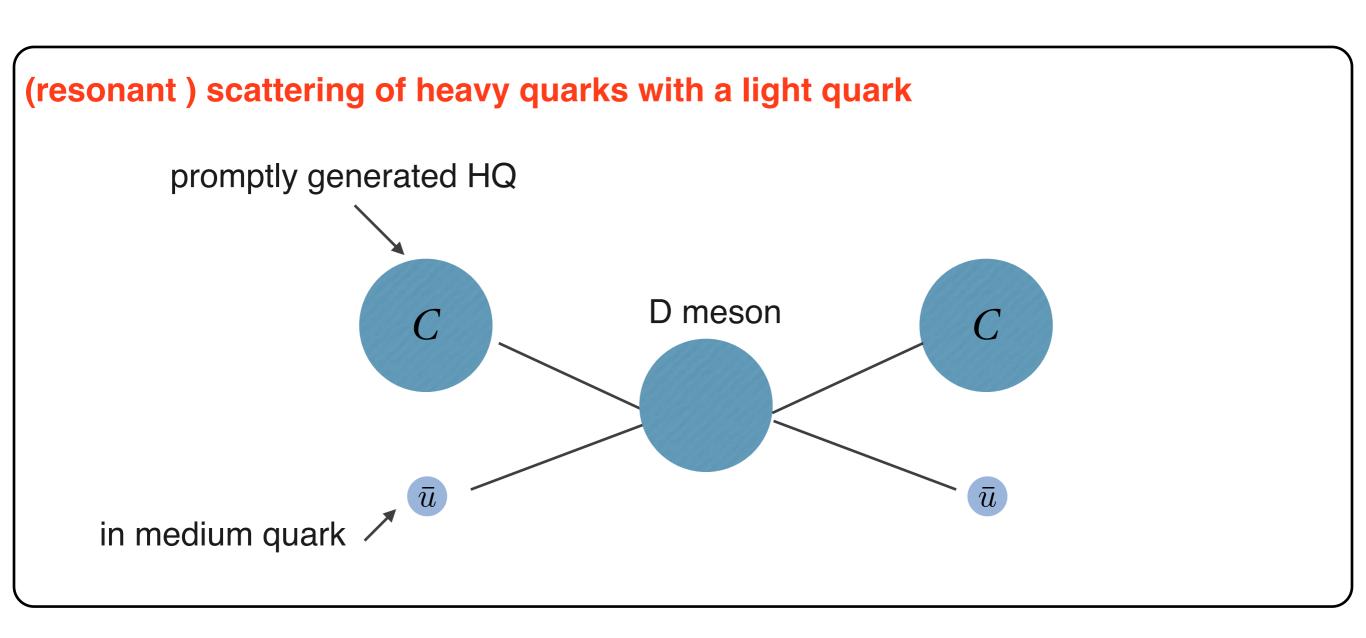
in a heat bath.

In medium heavy quarks

"Brownian motion" of Heavy Quarks (HQs) in the QGP While propagating in the QGP heavy quarks interact with in-medium quarks and gluons

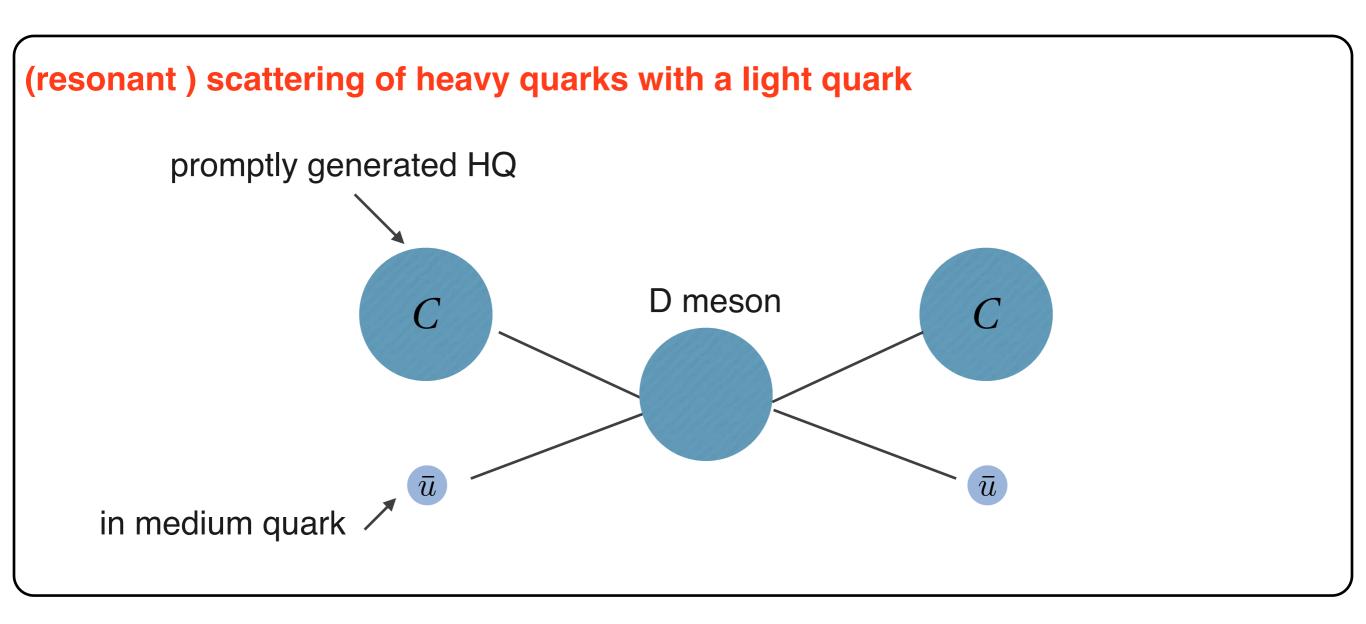
In medium heavy quarks

"Brownian motion" of Heavy Quarks (HQs) in the QGP While propagating in the QGP heavy quarks interact with in-medium quarks and gluons



In medium heavy quarks

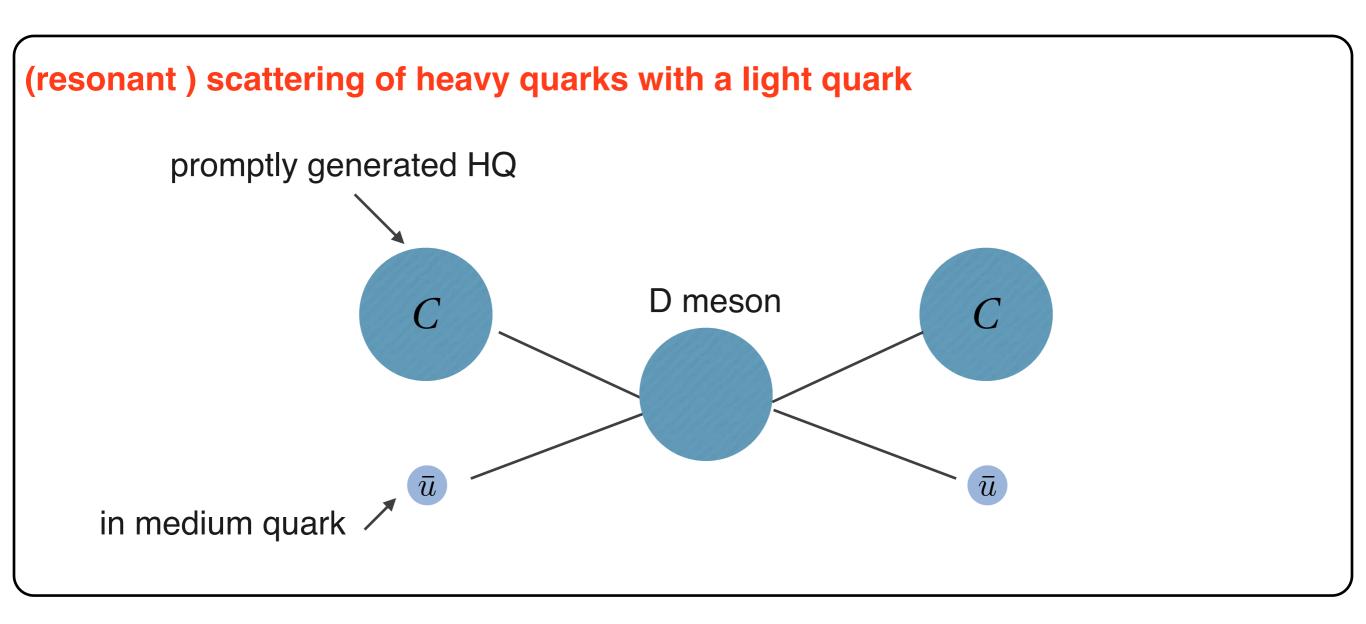
"Brownian motion" of Heavy Quarks (HQs) in the QGP While propagating in the QGP heavy quarks interact with in-medium quarks and gluons



Replacing the light quark with a heavy quark, one has quarkonia generation Thews et al. (2001)

In medium heavy quarks

"Brownian motion" of Heavy Quarks (HQs) in the QGP While propagating in the QGP heavy quarks interact with in-medium quarks and gluons

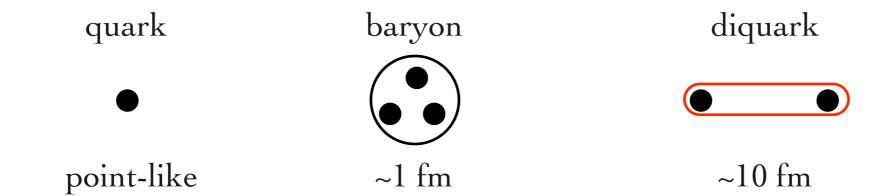


Replacing the light quark with a heavy quark, one has quarkonia generation Thews et al. (2001)

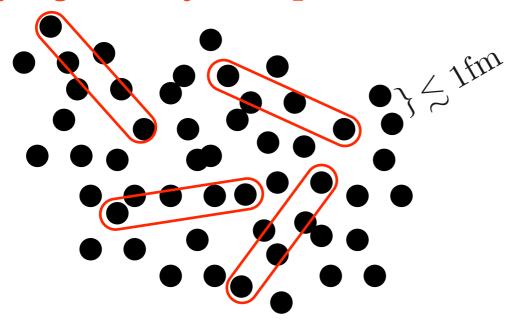
Color superconductor

Deconfinement by baryonic density increase

Deconfinement by baryonic density increase

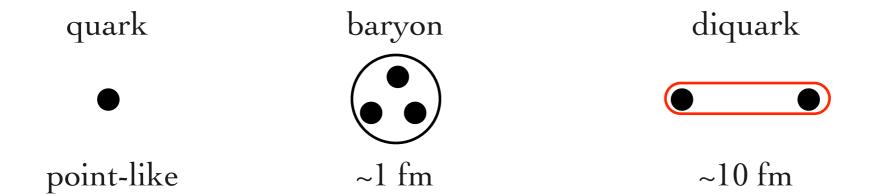


Very high density (Compact Star inner core)

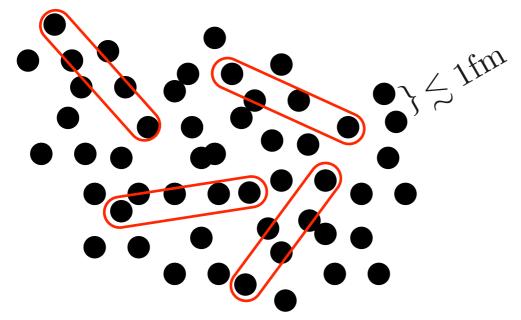


Liquid of quarks with correlated diquarks

Deconfinement by baryonic density increase



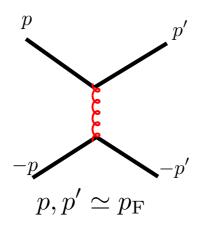
Very high density (Compact Star inner core)



Liquid of quarks with correlated diquarks

Attractive interaction (perturbative)

$$3 \times 3 = \overline{3}_A + 6_S$$
attractive channel



The interaction model

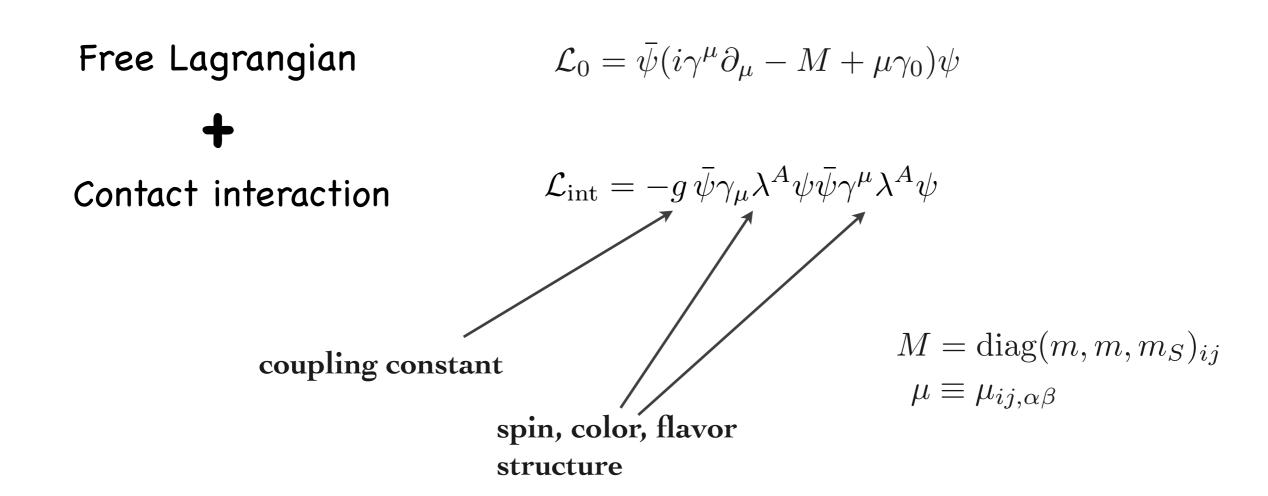
We have to use a model for QCD at densities reachable in compact stars.

One possibility is a NJL-like model with the same global symmetries of QCD

The interaction model

We have to use a model for QCD at densities reachable in compact stars.

One possibility is a NJL-like model with the same global symmetries of QCD



Diquark Condensate

Quark fields
$$\psi_{lpha i}$$

$$\alpha, \beta = 1, 2, 3$$
 color indices

$$i, j = 1, 2, 3$$
 flavor indices

Mixture of 9 different fermions. Six of them are relativistic, three are non relativistic

Diquark Condensate

Quark fields
$$\psi_{lpha i}$$

$$\alpha, \beta = 1, 2, 3$$
 color indices

$$i, j = 1, 2, 3$$
 flavor indices

gap parameters

Mixture of 9 different fermions. Six of them are relativistic, three are non relativistic

General color superconducting condensate

color structure $\langle \psi_{\alpha i} C \gamma_5 \psi_{\beta j} \rangle \propto \sum_{I=1}^3 \Delta_{\rm I} \varepsilon^{\alpha \beta I} \epsilon_{ijI} \qquad \text{flavor structure}$

It has a color charge

It has a flavor charge

It has a baryonic charge

The corresponding symmetries are broken, locked or mixed

Color Flavor Locked phase

Condensate

$$\langle \psi_{\alpha i} C \gamma_5 \psi_{\beta j} \rangle \sim \Delta_{\text{CFL}} \, \epsilon_{I\alpha\beta} \epsilon_{Iij}$$

Pairing of quarks of all flavors and colors

Alford, Rajagopal, Wilczek Nucl. Phys. B537 (1999) 443

Symmetry breaking
$$SU(3)_c \times SU(3)_L \times SU(3)_R \times U(1)_B \to SU(3)_{c+L+R} \times Z_2$$

$$\supset U(1)_{\mathbb{Q}}$$

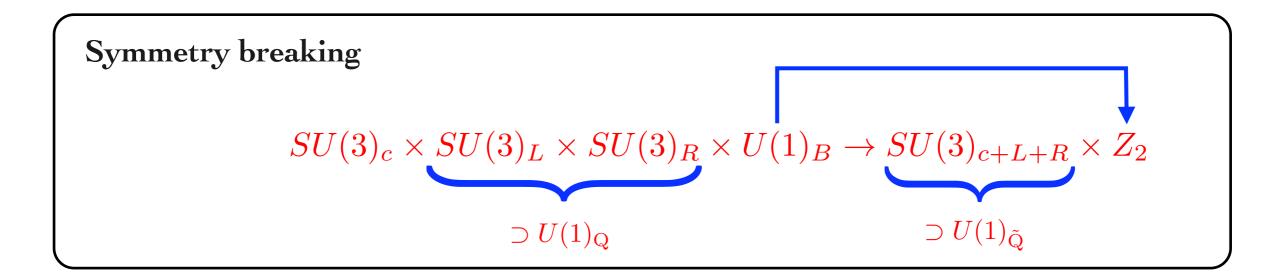
Color Flavor Locked phase

Condensate

 $\langle \psi_{\alpha i} C \gamma_5 \psi_{\beta j} \rangle \sim \Delta_{\text{CFL}} \, \epsilon_{I\alpha\beta} \epsilon_{Iij}$

Pairing of quarks of all flavors and colors

Alford, Rajagopal, Wilczek Nucl. Phys. B537 (1999) 443



- Breaking of SU(3)_c: 8 gauge bosons become massive. It is like having 8 (interacting) photons with a Meissner mass.
- χSB: 8 (pseudo) Nambu-Goldstone bosons (NGBs) as in the hadronic phase!
- U(1)_B breaking: 1 NGB. This is a genuine superfluid mode.

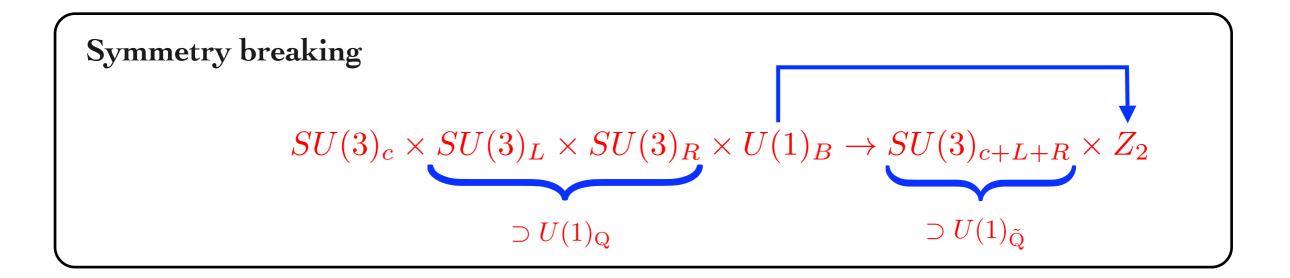
Color Flavor Locked phase

Condensate

 $\langle \psi_{\alpha i} C \gamma_5 \psi_{\beta j} \rangle \sim \Delta_{\text{CFL}} \, \epsilon_{I\alpha\beta} \epsilon_{Iij}$

Pairing of quarks of all flavors and colors

Alford, Rajagopal, Wilczek Nucl. Phys. B537 (1999) 443



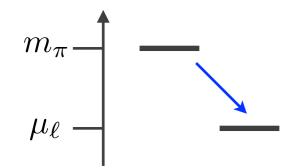
- Breaking of SU(3)_c: 8 gauge bosons become massive. It is like having 8 (interacting) photons with a Meissner mass.
- χSB: 8 (pseudo) Nambu-Goldstone bosons (NGBs) as in the hadronic phase!
- U(1)_B breaking: 1 NGB. This is a genuine superfluid mode.

The system is at the same time a (color) superconductor and a (baryonic) superfluid

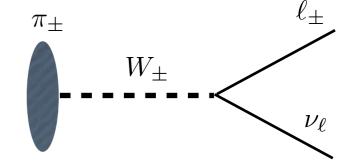
Meson condensation

Stabilization

The pion decay can be Pauli blocked for a large lepton chemical potential



pion decay in vacuum



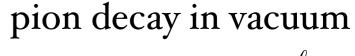
lepton density

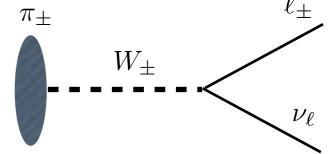
Stabilization pion decay in vacuum The pion decay can be Pauli blocked for a large lepton chemical potential $\begin{array}{c} \tau_{\pm} \\ W_{\pm} \\ \nu_{\ell} \end{array}$

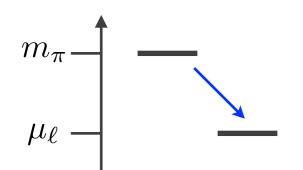
lepton density

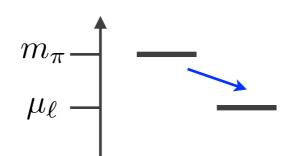
Stabilization

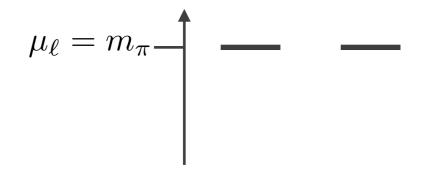
The pion decay can be Pauli blocked for a large lepton chemical potential









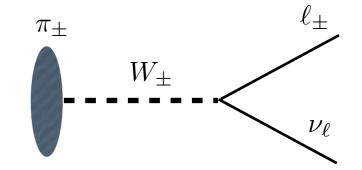


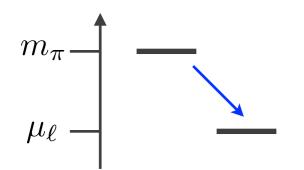
lepton density

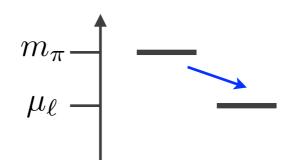
Stabilization

The pion decay can be Pauli blocked for a large lepton chemical potential

pion decay in vacuum







$$\mu_{\ell} = m_{\pi} - \frac{1}{m_{\pi}} - \frac{1}{m_{\pi}}$$

lepton density

Energy spectrum splitting Stark-like effect

$$E_{\pi^0} = \sqrt{m_{\pi}^2 + p^2}$$

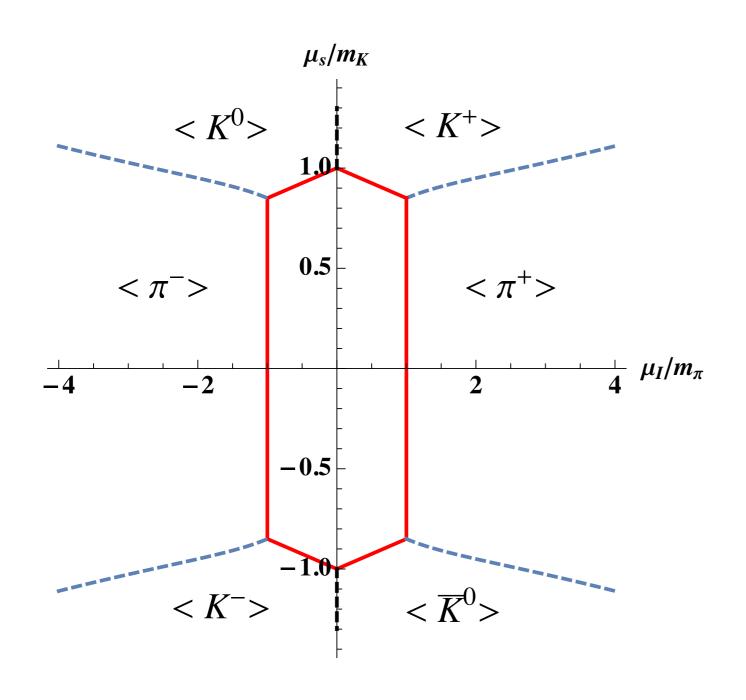
$$E_{\pi^-} = +\mu_I + \sqrt{m_{\pi}^2 + p^2}$$

$$E_{\pi^+} = -\mu_I + \sqrt{m_{\pi}^2 + p^2}$$

$$m_{\pi^+}^{\text{eff}} = m_{\pi} - \mu_I$$

At $\mu_I=m_\pi$ a massless mode appears: pion condensation $\langle \bar{\psi}\sigma_2\gamma_5\psi\rangle$

Phases of meson condensates



Dashed: first order

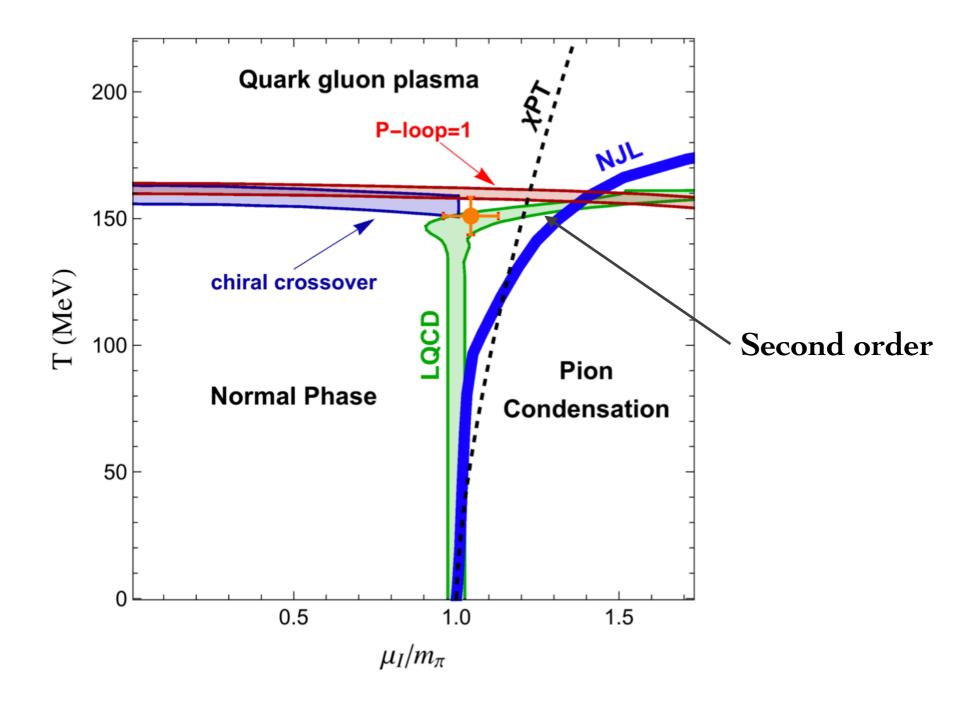
Solid: second order

Kogut and Toublan PhysRevD.64.034007

MM, Particles 2, no.3, 411-443 (2019)

At asymptotic μ_I and/or μ_S matter should be deconfined in a rather unusual way

$T-\mu_I$ phase diagram



Combination of LQCD by Brandt et al, PRD 97, 054514 (2018) with effective field methods.

The phase diagram

In each phase different quark condensates are realized

In each phase different quark condensates are realized

Hadron gas chiral condensate $\langle \bar{\psi}\psi \rangle$

In each phase different quark condensates are realized

Hadron gas chiral condensate $\langle \bar{\psi} \psi
angle$

Color superconductors diquark condensate $\langle \psi C \gamma_5 \psi \rangle$

In each phase different quark condensates are realized

Hadron gas chiral condensate $\langle \bar{\psi}\psi \rangle$

Color superconductors diquark condensate $\langle \psi C \gamma_5 \psi \rangle$

Meson superfluid pion condensate $\langle \bar{\psi}\sigma_2\gamma_5\psi\rangle$

In each phase different quark condensates are realized

Hadron gas chiral condensate

 $\langle \bar{\psi}\psi \rangle$

Color superconductors diquark condensate

 $\langle \psi C \gamma_5 \psi \rangle$

Meson superfluid

pion condensate

 $\langle \bar{\psi} \sigma_2 \gamma_5 \psi \rangle$

Quark-gluon plasma

no condensate

In each phase different quark condensates are realized

Hadron gas chiral condensate

 $\langle \bar{\psi}\psi
angle$

Color superconductors diquark condensate

 $\langle \psi C \gamma_5 \psi \rangle$

Meson superfluid pion condensate

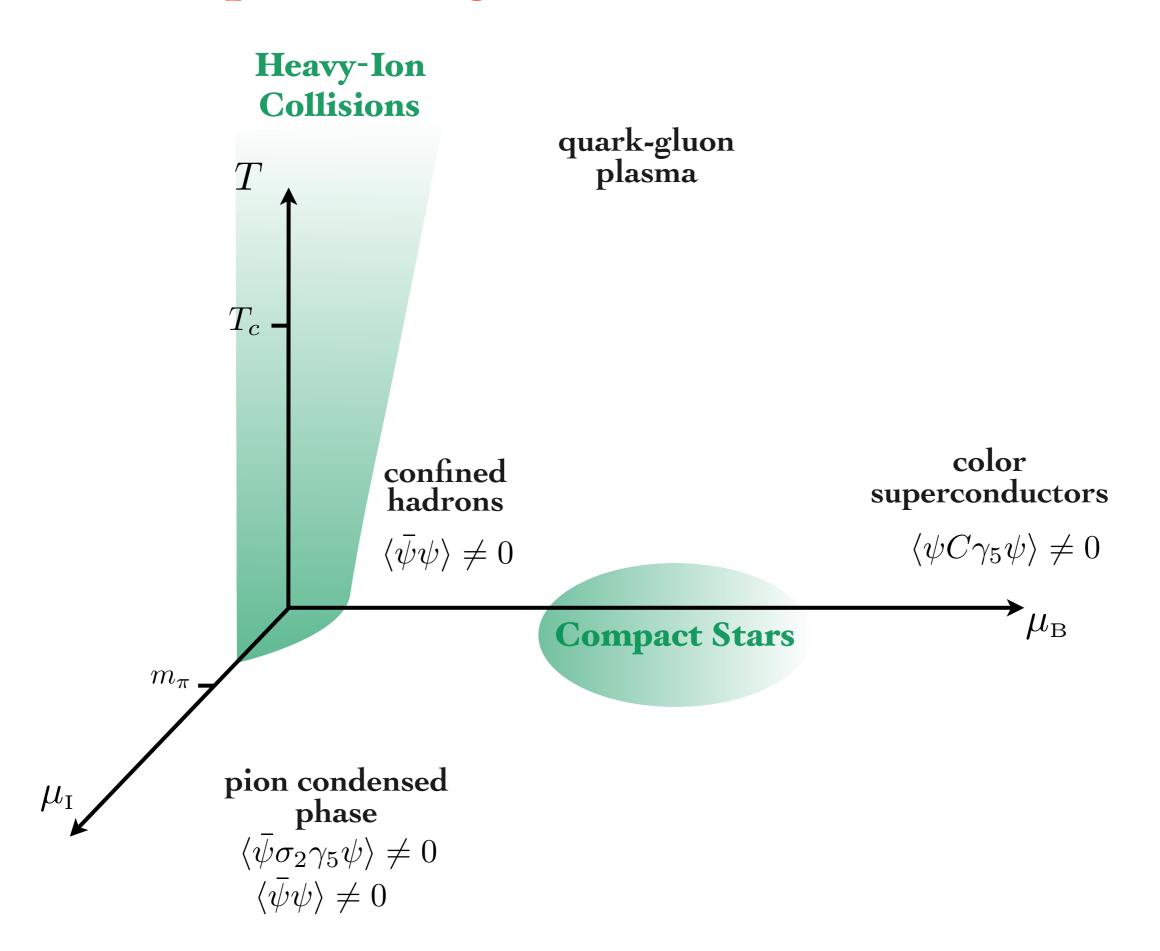
 $\langle \bar{\psi} \sigma_2 \gamma_5 \psi \rangle$

Quark-gluon plasma

no condensate

Each quark condensate **breaks** or **locks** the symmetries of QCD in a different way

The QCD phase diagram



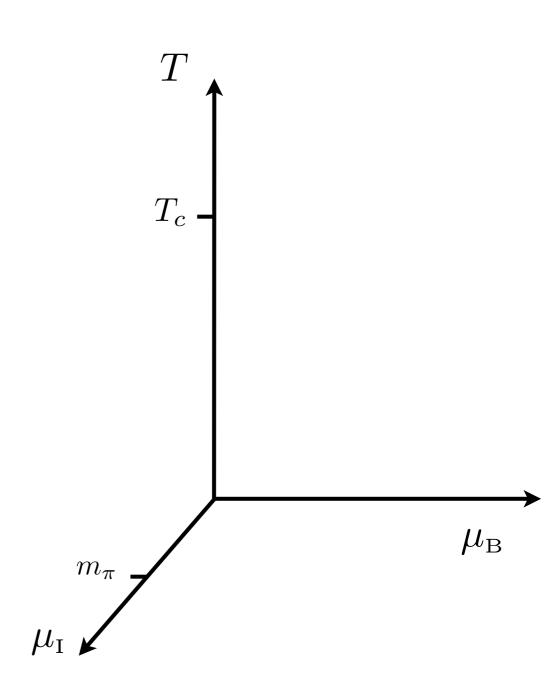
$$\mu_{I} = m_{u,d} = 0$$

$$\psi_{L} \to U_{L} \psi_{L}$$

$$\psi_{R} \to U_{R} \psi_{R}$$

$$SU(2)_{L} \times SU(2)_{R} \times U(1)_{B}$$

$$\supset [U(1)_{\text{e.m.}}]$$



reduce T

 $below \, T_c$

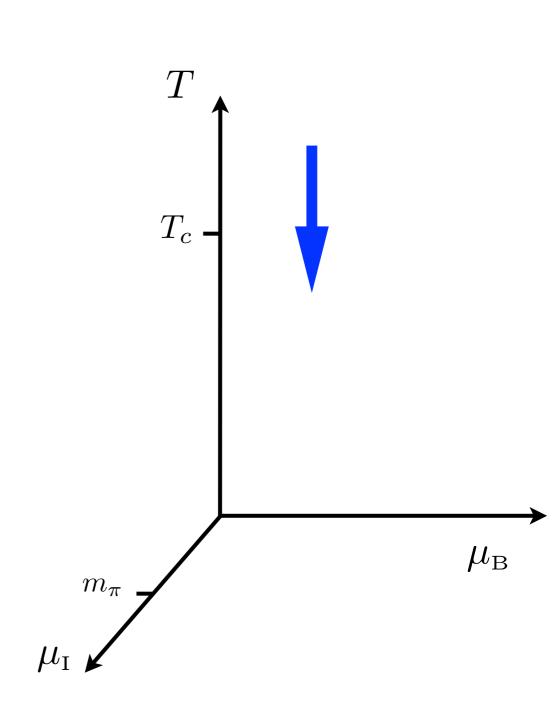
$$\mu_{I} = m_{u,d} = 0$$

$$\psi_{L} \to U_{L} \psi_{L}$$

$$\psi_{R} \to U_{R} \psi_{R}$$

$$SU(2)_{L} \times SU(2)_{R} \times U(1)_{B}$$

$$\supset [U(1)_{\text{e.m.}}]$$



$$\mu_{I} = m_{u,d} = 0$$

$$\psi_{L} \to U_{L} \psi_{L}$$

$$\psi_{R} \to U_{R} \psi_{R}$$

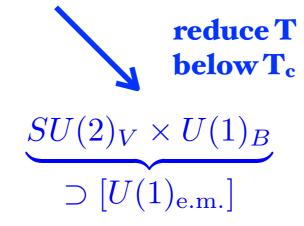
$$SU(2)_{L} \times SU(2)_{R} \times U(1)_{B}$$

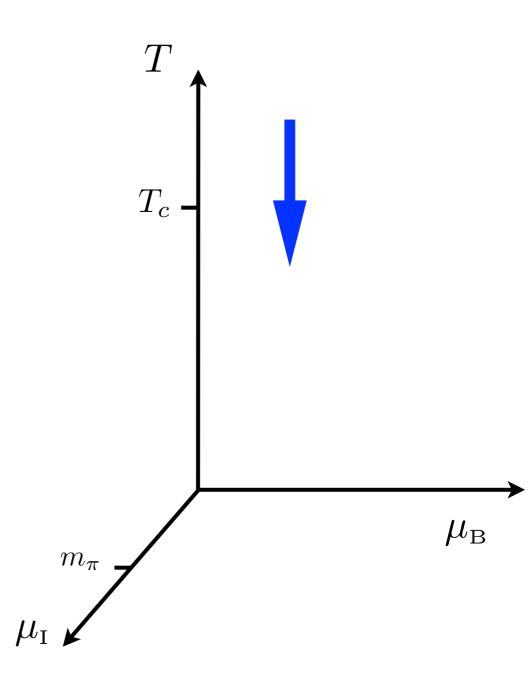
$$\supset [U(1)_{\text{e.m.}}]$$

Spontaneous chiral symmetry breaking $\langle \bar{\psi}\psi \rangle \neq 0$

invariant under $U_L = U_R = e^{i\boldsymbol{\sigma}\cdot\boldsymbol{\theta}}$

Pions are the (pseudo) NGBs





$$\mu_{I} = m_{u,d} = 0$$

$$\psi_{L} \to U_{L} \psi_{L}$$

$$\psi_{R} \to U_{R} \psi_{R}$$

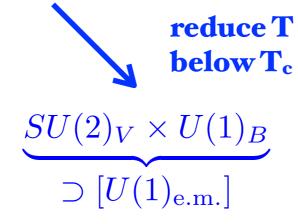
$$SU(2)_{L} \times SU(2)_{R} \times U(1)_{B}$$

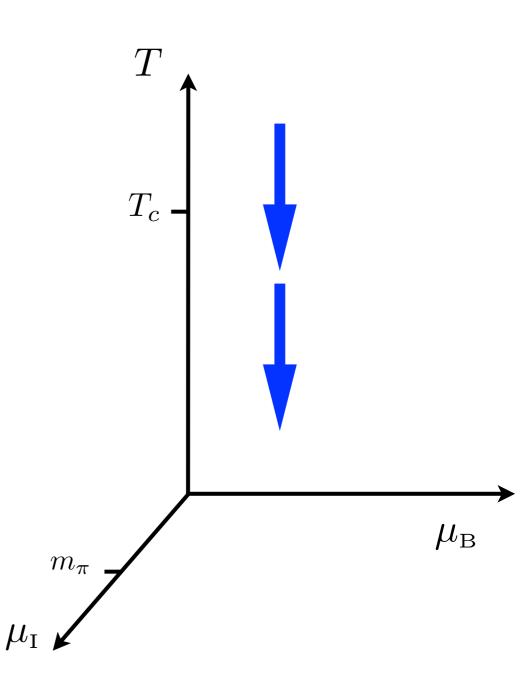
$$\supset [U(1)_{\text{e.m.}}]$$

Spontaneous chiral symmetry breaking $\langle \bar{\psi}\psi \rangle \neq 0$

invariant under $U_L = U_R = e^{i\boldsymbol{\sigma}\cdot\boldsymbol{\theta}}$

Pions are the (pseudo) NGBs





$$\mu_{I} = m_{u,d} = 0$$

$$\psi_{L} \rightarrow U_{L} \psi_{L}$$

$$\psi_{R} \rightarrow U_{R} \psi_{R}$$

$$\sum [U(1)_{c.m.}]$$
Spontaneous chiral symmetry breaking invariant under $U_{L} = U_{R} = e^{i\sigma \cdot \theta}$
Pions are the (pseudo) NGBs
$$U(1) \times U(1)_{B}$$

$$\sum [U(1)_{e.m.}]$$

$$U_{L} = u_{R} = e^{i\sigma \cdot \theta}$$

$$U(1) \times U(1)_{B} = u_{R}$$

$$\mu_{I} = m_{u,d} = 0$$

$$\psi_{L} \rightarrow U_{L}\psi_{L}$$

$$\psi_{R} \rightarrow U_{R}\psi_{R}$$

$$\sum [U(1)_{\text{e.m.}}]$$

$$\text{Spontaneous chiral symmetry breaking invariant under } U_{L} = U_{R} = e^{i\sigma \cdot \theta}$$

$$\text{Pions are the (pseudo) NGBs}$$

$$\mathcal{L} = \mu_{I}(\psi_{L}^{\dagger}\sigma_{3}\psi_{L} + \psi_{R}^{\dagger}\sigma_{3}\psi_{R})$$

$$\text{Increase } \mu_{I}$$

$$\text{Explicit symmetry breaking}$$

$$\text{Increase } \mu_{I}$$

$$\text{Explicit symmetry breaking}$$

$$\text{Pions have effective mass } m_{\pi} \pm \mu_{I}$$

$$D[U(1)_{\text{e.m.}}]$$

$$U(1) \times U(1)_{B}$$

$$D[U(1)_{\text{e.m.}}]$$

$$\mu_{I} = m_{u,d} = 0$$

$$\psi_{L} \rightarrow U_{L}\psi_{L}$$

$$\psi_{R} \rightarrow U_{R}\psi_{R}$$

$$\int [U(1)_{\text{e.m.}}]$$
Spontaneous chiral symmetry breaking invariant under $U_{L} = U_{R} = e^{i\sigma \cdot \theta}$
Pions are the (pseudo) NGBs
$$\mathcal{L} = \mu_{I}(\psi_{L}^{\dagger}\sigma_{3}\psi_{L} + \psi_{R}^{\dagger}\sigma_{3}\psi_{R})$$

$$\text{invariant under } e^{i\sigma_{3} \cdot \theta}$$

$$\text{Pions have effective mass } m_{\pi} \pm \mu_{I}$$

$$Increase \mu_{I}$$

$$\text{Explicit symmetry breaking}$$

$$U(1) \times U(1)_{B}$$

$$D(1)_{\text{e.m.}}$$

$$U(1)_{B}$$

$$D(1)_{B}$$

$$\mu_I = m_{u,d} = 0 \\ \psi_L \to U_L \psi_L \\ \psi_R \to U_R \psi_R \qquad \supset [U(1)_{\mathrm{e.m.}}]$$

$$\mathbf{Spontaneous} \text{ chiral symmetry breaking invariant under } U_L = U_R = e^{i\sigma \cdot \theta} \\ \mathbf{Pions are the (pseudo) NGBs}$$

$$\mathcal{L} = \mu_I (\psi_L^{\dagger} \sigma_3 \psi_L + \psi_R^{\dagger} \sigma_3 \psi_R)$$

$$\mathbf{Increase } \mu_I \\ \mathbf{Explicit} \text{ symmetry breaking invariant under } e^{i\sigma_3 \cdot \theta}$$

$$\mathbf{Pions have effective mass } m_\pi \pm \mu_I \qquad \bigcup [U(1) \times U(1)_B \\ \mathbf{Spontaneous} \\ \mathbf{Symmetry breaking} \\ (meson condensation)$$

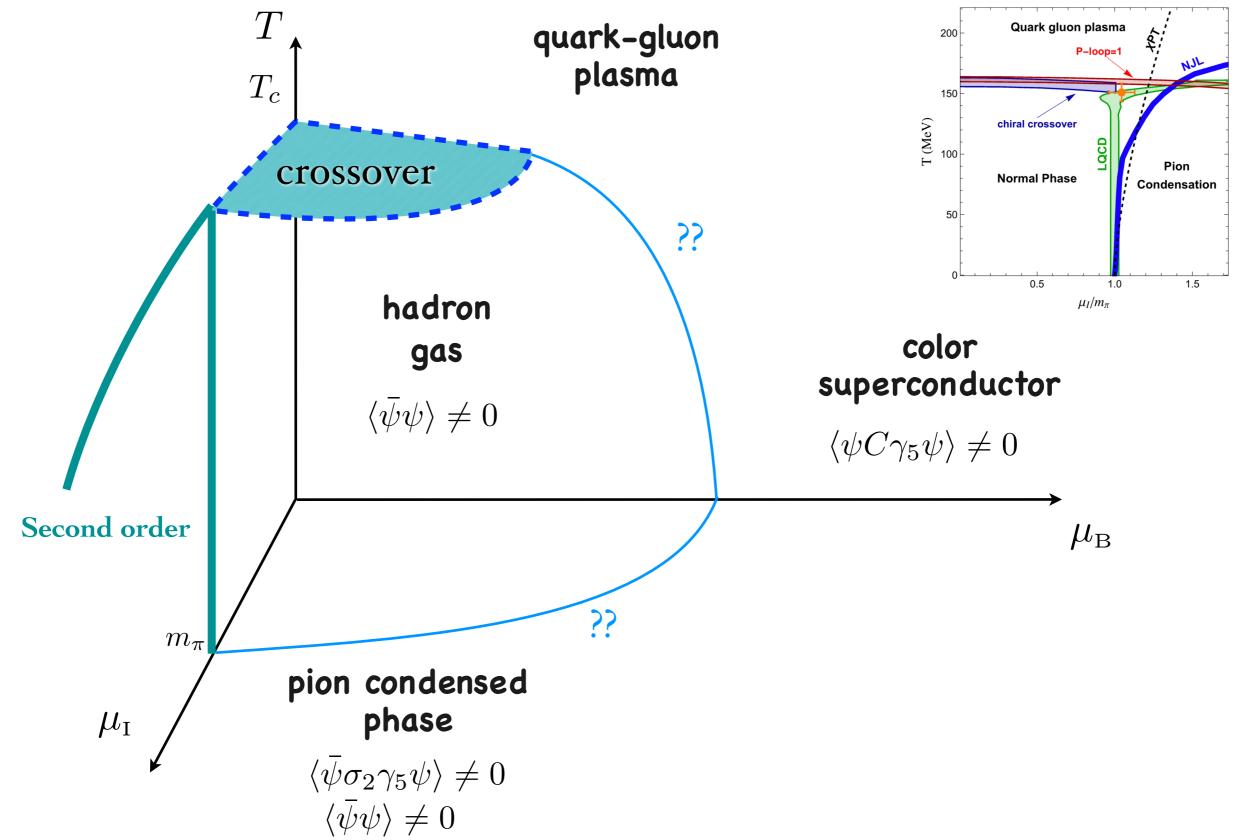
$$\mu_I > m_\pi$$

$$\mu_1$$

$$\mu_1$$

One NGB

Revisiting the QCD phase diagram



Conclusions

Chiral symmetry and quark confinement pertain to two different limits of QCD

They should be approximately realized in real QCD

Any physically sound tool to explore QCD should be used, even going to unphysical parameter space

There is a richness of phases due to a rich particle spectrum

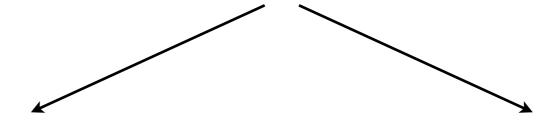
Thanks for your attention!

Back up

Effective field theories

Effective field theories

If we do not use QCD we want theories that preserve (part of) its symmetries and that are capable of describing the symmetry breaking patterns



Lattice QCD

Effective field theories

Discretization on a lattice.

Does not work at large baryonic densities

Describe global symmetries of QCD Lack the gauge field dynamics

Qualitative picture

Any effective theory can be characterized by

- 1) separation scale
- 2) particle content
- 3) matching condition
- 4) method of regularization/cancelation of divergencies

QCD is a renormalizable theory: any divergency can be removed.

This results in a theory which has been very successfully compared to experiments. No UV scale has appeared so far. In other words, if QCD is the low energy EFT of a more fundamental one, we still have not found the breaking scale.

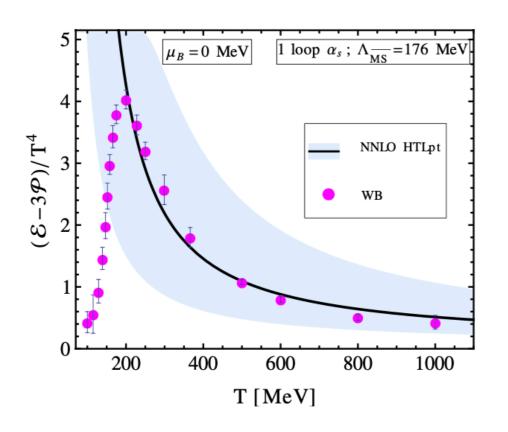
When dealing with EFT of QCD, we always have to keep in mind that there exists a breaking scale. The scale is associated to a change of degrees of freedom or to an internal inconsistency of the EFT.

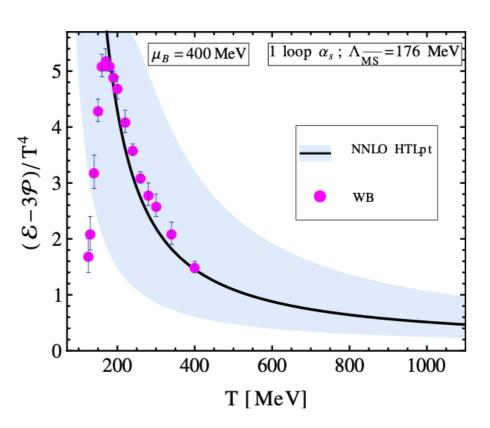
Example: chiral perturbation theory is a low-energy theory with breaking scale

Beyond this point one has to consider the mesonic resonances, baryons and then quarks and gluons. Which means changing the degrees of freedom, of interaction vetc. This is not impossible, it is only extremely hard and does not seem to be simpler than solving QCD itself.

Hard thermal loop (HTL)

Resummed perturbation theory





More on the method

ullet The $\mathcal{O}(p^2)$ Lorentz invariant chiral Lagrangian density for pions

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

• SU(2) variational vev

$$\bar{\Sigma} = e^{i\boldsymbol{\alpha}\cdot\boldsymbol{\sigma}} = \cos\alpha + i\boldsymbol{n}\cdot\boldsymbol{\sigma}\sin\alpha$$

More on the method

• The $\mathcal{O}(p^2)$ Lorentz invariant chiral Lagrangian density for pions

encode medium effects

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

• SU(2) variational vev

$$\bar{\Sigma} = e^{i\boldsymbol{\alpha}\cdot\boldsymbol{\sigma}} = \cos\alpha + i\boldsymbol{n}\cdot\boldsymbol{\sigma}\sin\alpha$$

More on the method

ullet The $\mathcal{O}(p^2)$ Lorentz invariant chiral Lagrangian density for pions

encode medium effects

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

• SU(2) variational vev

$$\bar{\Sigma} = e^{i\boldsymbol{\alpha}\cdot\boldsymbol{\sigma}} = \cos\alpha + i\boldsymbol{n}\cdot\boldsymbol{\sigma}\sin\alpha$$

variational parameters

More on the method

• The $\mathcal{O}(p^2)$ Lorentz invariant chiral Lagrangian density for pions

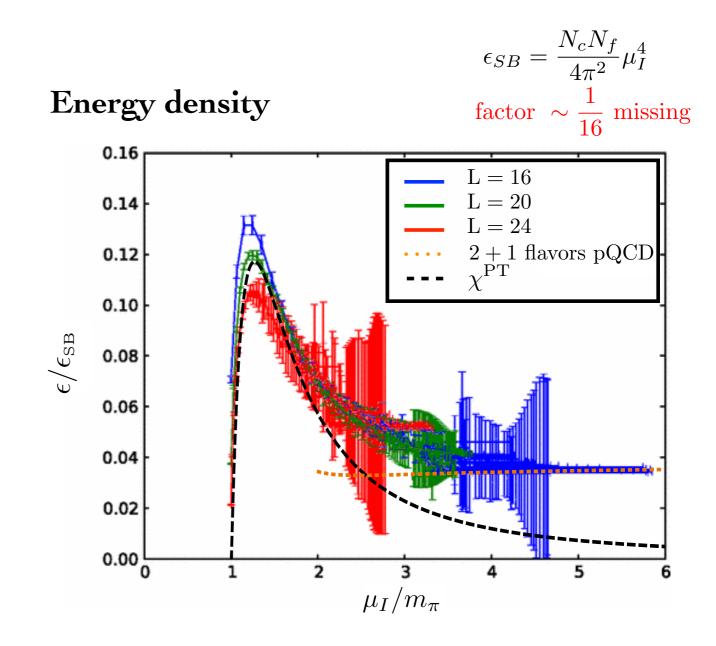
encode medium effects

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

• SU(2) variational vev

$$\bar{\Sigma} = e^{i\boldsymbol{\alpha}\cdot\boldsymbol{\sigma}} = \cos\alpha + i\boldsymbol{n}\cdot\boldsymbol{\sigma}\sin\alpha$$

variational parameters



More on the method

• The $\mathcal{O}(p^2)$ Lorentz invariant chiral Lagrangian density for pions

encode medium effects

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

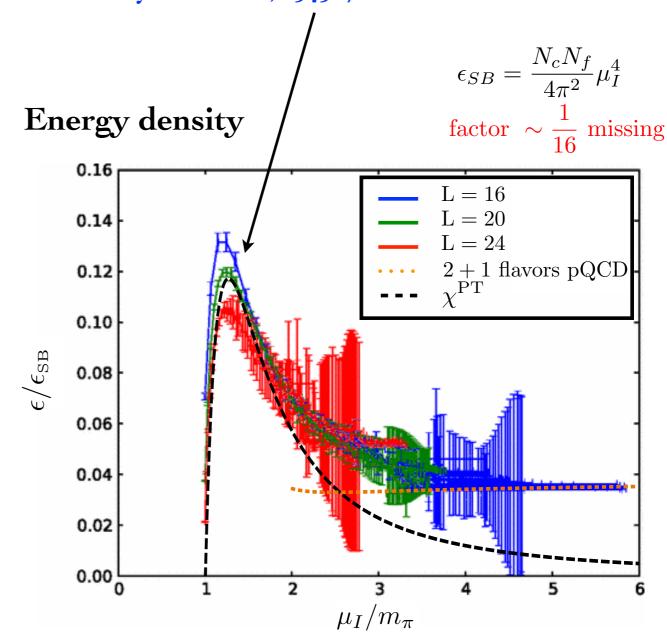
• SU(2) variational vev

$$\bar{\Sigma} = e^{i\boldsymbol{\alpha}\cdot\boldsymbol{\sigma}} = \cos\alpha + i\boldsymbol{n}\cdot\boldsymbol{\sigma}\sin\alpha$$

variational parameters

Lattice QCD simulations

W. Detmold, K. Orginos, and Z. Shi, Phys. Rev. D86, 054507 (2012)



More on the method

• The $\mathcal{O}(p^2)$ Lorentz invariant chiral Lagrangian density for pions

encode medium effects

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

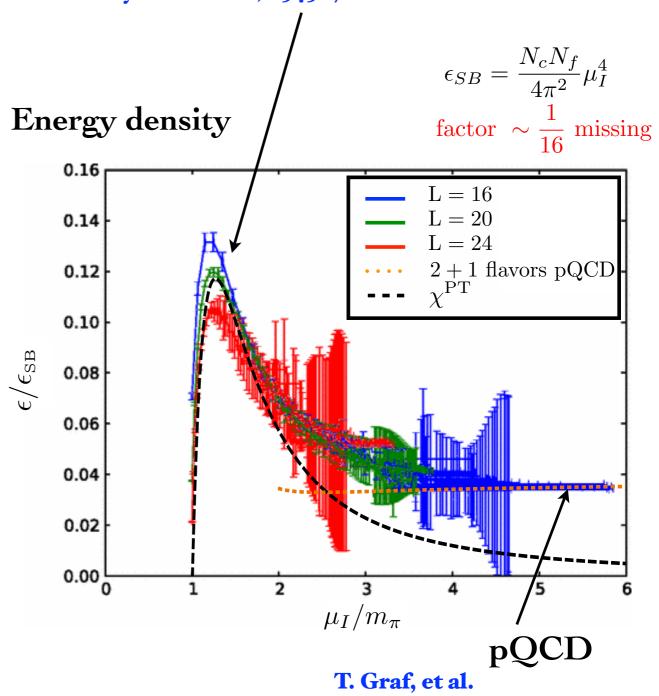
• SU(2) variational vev

$$\bar{\Sigma} = e^{i\boldsymbol{\alpha}\cdot\boldsymbol{\sigma}} = \cos\alpha + i\boldsymbol{n}\cdot\boldsymbol{\sigma}\sin\alpha$$

variational parameters

Lattice QCD simulations

W. Detmold, K. Orginos, and Z. Shi, Phys. Rev. D86, 054507 (2012)



Phys. Rev. D 93, 085030 (2016)

More on the method

• The $\mathcal{O}(p^2)$ Lorentz invariant chiral Lagrangian density for pions

encode medium effects

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

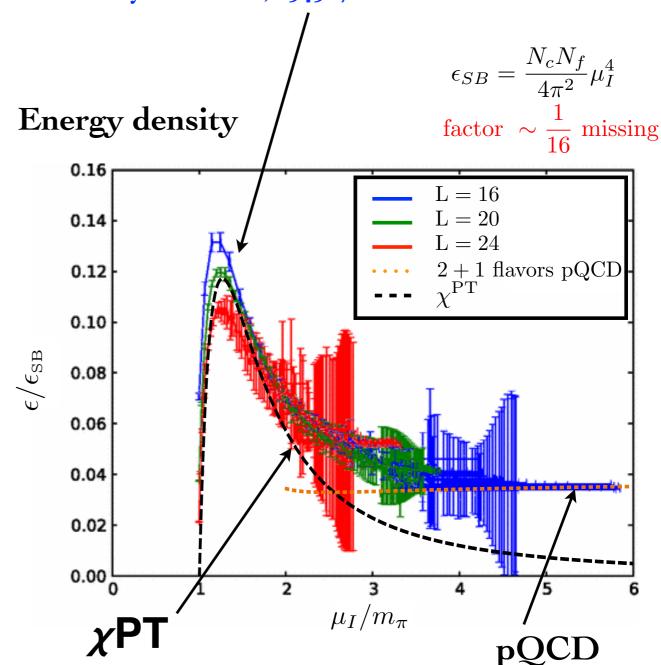
• SU(2) variational vev

$$\bar{\Sigma} = e^{i\boldsymbol{\alpha}\cdot\boldsymbol{\sigma}} = \cos\alpha + i\boldsymbol{n}\cdot\boldsymbol{\sigma}\sin\alpha$$

variational parameters

Lattice QCD simulations

W. Detmold, K. Orginos, and Z. Shi, Phys. Rev. D86, 054507 (2012)



S. Carignano, A. Mammarella, MM Phys.Rev. D93 (2016) no.5, 051503

T. Graf, et al. Phys. Rev. D 93, 085030 (2016)

More on the method

• The $\mathcal{O}(p^2)$ Lorentz invariant chiral Lagrangian density for pions

encode medium effects

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

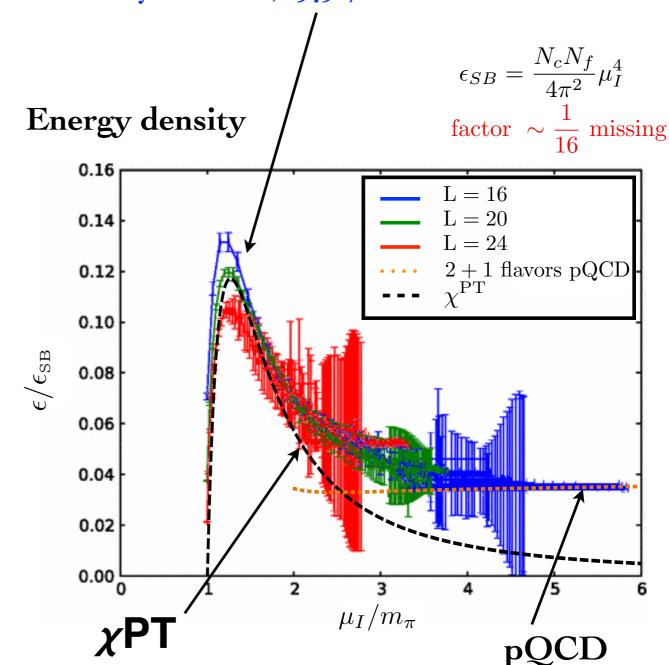
• SU(2) variational vev

$$\bar{\Sigma} = e^{i\boldsymbol{\alpha}\cdot\boldsymbol{\sigma}} = \cos\alpha + i\boldsymbol{n}\cdot\boldsymbol{\sigma}\sin\alpha$$

variational parameters

Lattice QCD simulations

W. Detmold, K. Orginos, and Z. Shi, Phys. Rev. D86, 054507 (2012)



S. Carignano, A. Mammarella, MM Phys.Rev. D93 (2016) no.5, 051503

T. Graf, et al. Phys. Rev. D 93, 085030 (2016)

Our method gives an ANALYTIC expression for the peak

$$\mu_{I, \text{LQCD}}^{\text{peak}} = \{1.20, 1.25, 1.275\} m_{\pi}$$

$$\mu_{I,\text{LQCD}}^{\text{peak}} = \{1.20, 1.25, 1.275\} m_{\pi}$$
 $\mu_{I,\chi\text{PT}}^{\text{peak}} = (\sqrt{13} - 2)^{1/2} m_{\pi} \simeq 1.276 m_{\pi}$

Variational approach

$$\bar{\Sigma} = \mathbf{1}_2 \cos \alpha \pm i \mathbf{n} \cdot \sigma \sin \alpha$$

Static Lagrangian

$$\mathcal{L}_0(\alpha, \mu_I, n_3) = F_0^2 m_\pi^2 \cos \alpha + \frac{F_0^2}{2} \mu_I^2 \sin^2 \alpha (1 - n_3^2)$$

Variational approach

$$\bar{\Sigma} = \mathbf{1}_2 \cos \alpha \pm i \mathbf{n} \cdot \sigma \sin \alpha$$

Static Lagrangian

$$\mathcal{L}_0(\alpha, \mu_I, n_3) = F_0^2 m_\pi^2 \cos \alpha + \frac{F_0^2}{2} \mu_I^2 \sin^2 \alpha (1 - n_3^2)$$

Maximising the Lagrangian

for
$$\mu_I < m_{\pi}$$
 $\cos \alpha = 1$ \mathcal{L}_0 independent of \boldsymbol{n} for $\mu_I > m_{\pi}$ $\cos \alpha_{\pi} = m_{\pi}^2/\mu_I^2$ $n_3 = 0$ residual $O(2)$ symmetry

The vacuum has been tilt in some direction in isospin space

Variational approach

$$\bar{\Sigma} = \mathbf{1}_2 \cos \alpha \pm i \mathbf{n} \cdot \sigma \sin \alpha$$

Static Lagrangian

$$\mathcal{L}_0(\alpha, \mu_I, n_3) = F_0^2 m_\pi^2 \cos \alpha + \frac{F_0^2}{2} \mu_I^2 \sin^2 \alpha (1 - n_3^2)$$

Maximising the Lagrangian

for
$$\mu_I < m_{\pi}$$
 $\cos \alpha = 1$ \mathcal{L}_0 independent of \boldsymbol{n} for $\mu_I > m_{\pi}$ $\cos \alpha_{\pi} = m_{\pi}^2/\mu_I^2$ $n_3 = 0$ residual $O(2)$ symmetry

The vacuum has been tilt in some direction in isospin space

We now look for solutions in which the rotation is local

More about the leading order Lagrangian

The $\mathcal{O}(p^2)$ Lorentz invariant Lagrangian density for pions

$$\mathcal{L} = \frac{F_0^2}{4} \text{Tr}(D_{\nu} \Sigma D^{\nu} \Sigma^{\dagger}) + \frac{F_0^2 m_{\pi}^2}{2} \text{Tr}(\Sigma)$$

Trick for introducing the isospin. We define the covariant derivative

$$D_{\mu}\Sigma = \partial_{\mu}\Sigma - \frac{i}{2}[v_{\mu}, \Sigma]$$

Gasser and Leutwyler, Annals Phys. 158, 142 (1984)

Formally preserving the Lorentz invariance

$$v^{\mu} = \mu_I \, \sigma_3 \, \delta^{\mu 0}$$

BEC of pions!

Rotated condensates

$$\langle \bar{u}u \rangle = \langle \bar{d}d \rangle \propto \cos \alpha$$

 $\langle \bar{d}\gamma_5 u + \text{h.c.} \rangle \propto \sin \alpha$

$$\gamma = \frac{\mu_I}{m_{\pi}}$$

$$P = \frac{f_{\pi}^2 m_{\pi}^2}{2} \gamma^2 \left(1 - \frac{1}{\gamma^2} \right)^2$$

Ground state occupation number

$$n_I = f_\pi^2 m_\pi \gamma \left(1 - \frac{1}{\gamma^4} \right)$$

Pion fluctuations

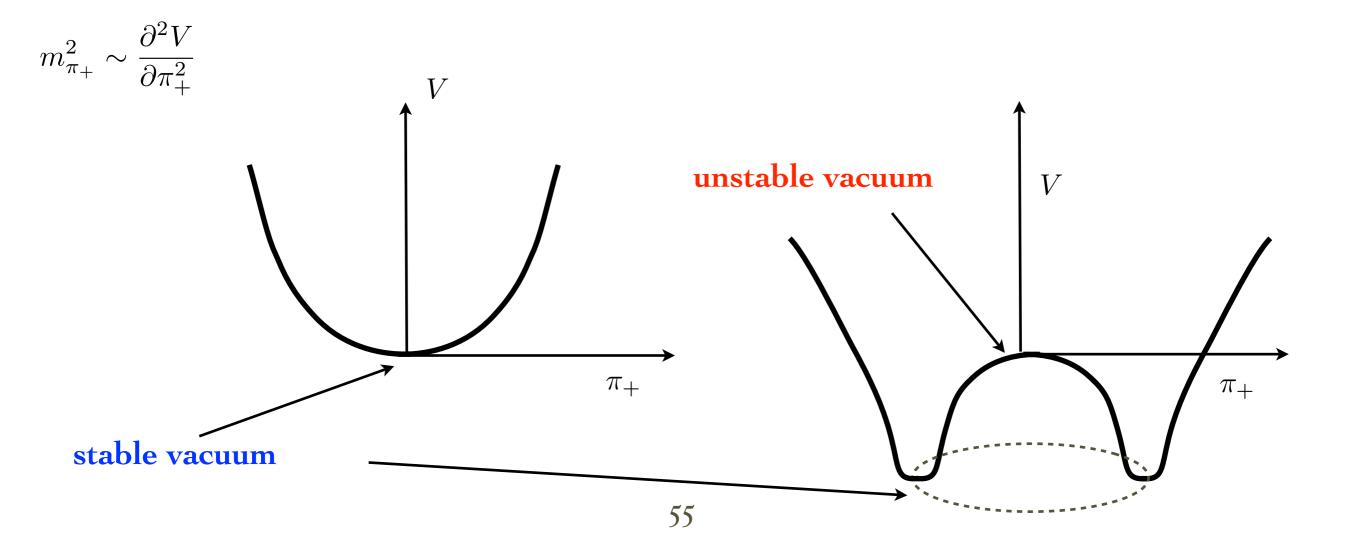
Mass splitting proportional to the isospin charge

$$m_{\pi^0} = m_{\pi}$$

$$m_{\pi^-} = m_{\pi} + \mu_I$$

$$m_{\pi^+} = m_{\pi} - \mu_I$$

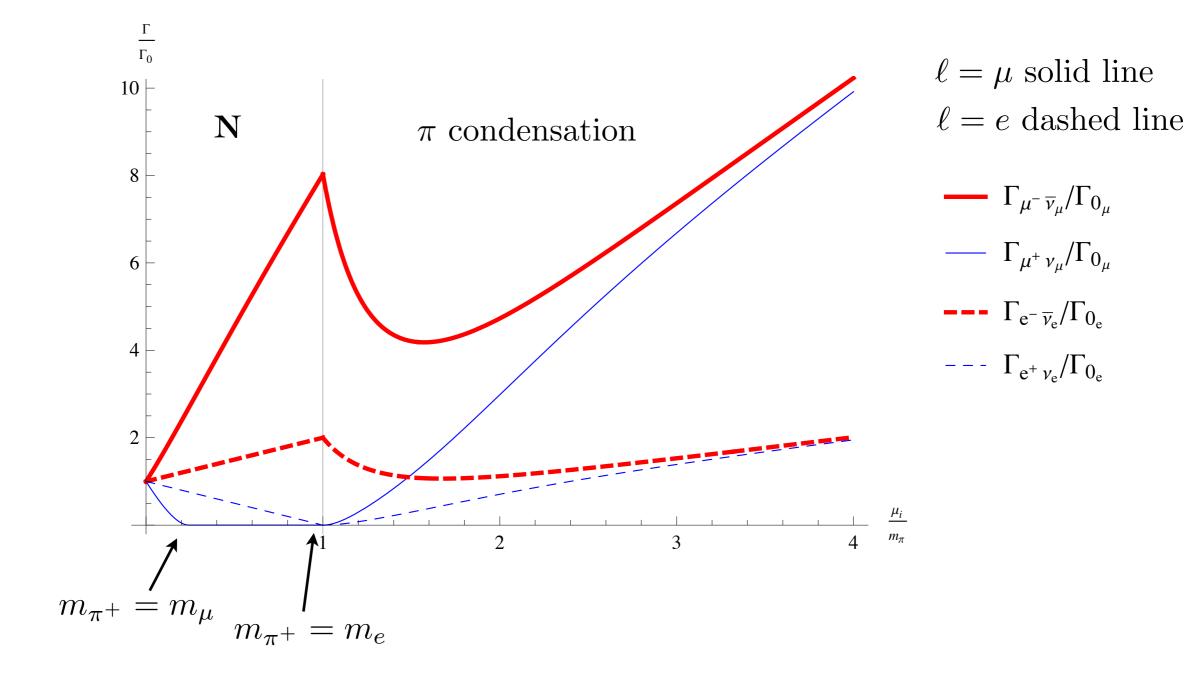
The meson mass vanishes at the phase transition



Leptonic decays

$$ilde{\pi}_-
ightarrow \ell^\pm
u_\ell$$
and

$$\tilde{\pi}_+ \to \ell^{\pm} \nu_{\ell}$$



Pions



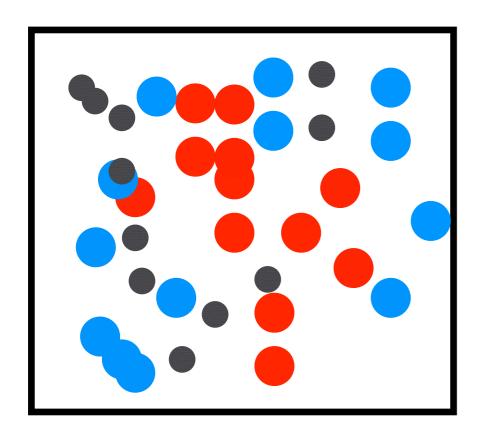
Baryons

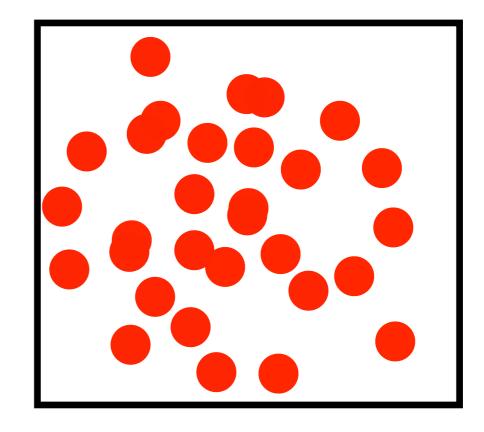


Anti Baryons



Increasing T Fixed low μ_B





Pions

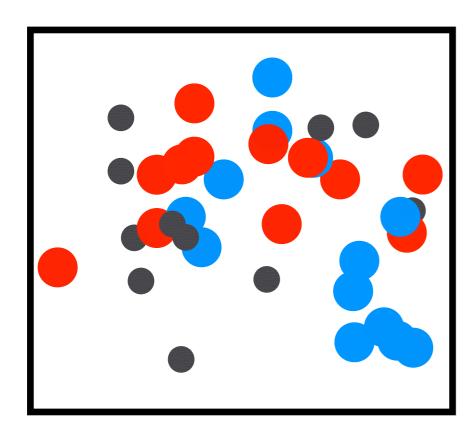


Baryons

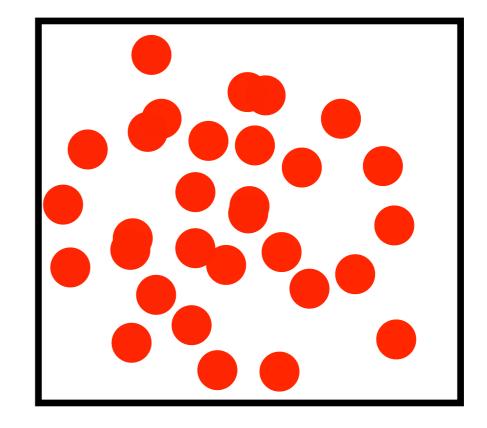




Increasing T Fixed low μ_B



Fixed Low T Increasing μ_B



Pions

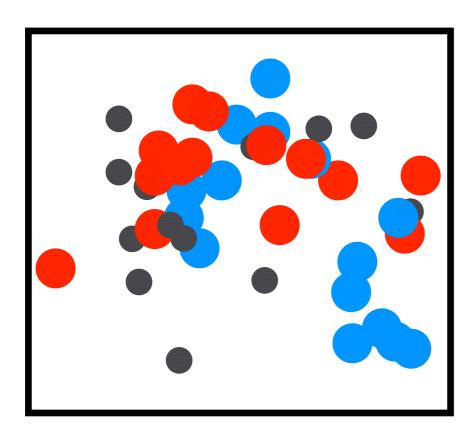


Baryons

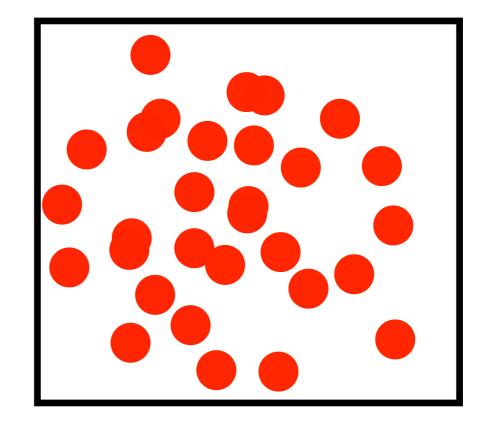




Increasing T Fixed low μ_B



Fixed Low T Increasing μ_B



Pions

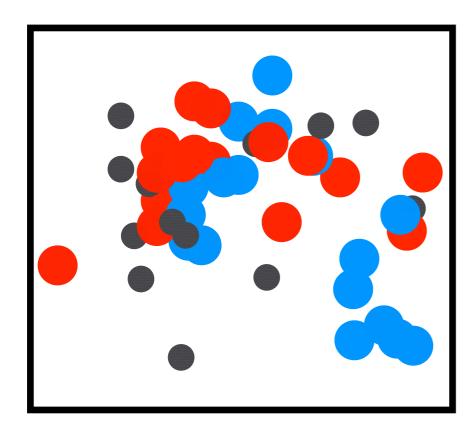


Baryons

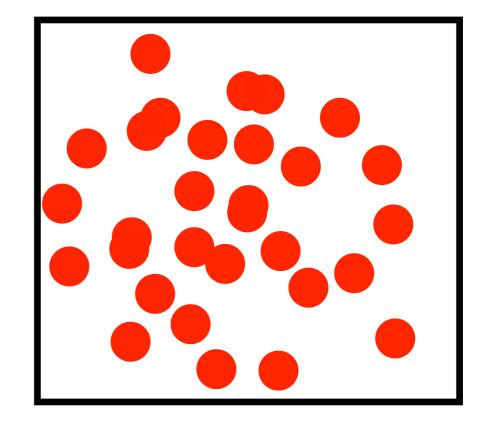




Increasing T Fixed low μ_B



Fixed Low T Increasing μ_B



Pions

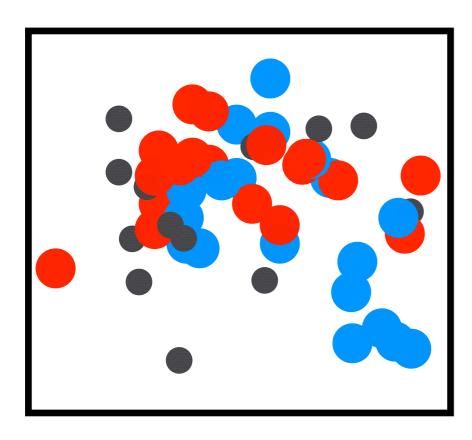


Baryons

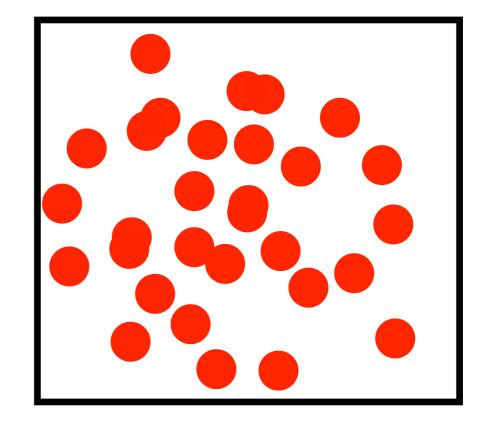




Increasing T Fixed low μ_B



Fixed Low T Increasing μ_B



Pions

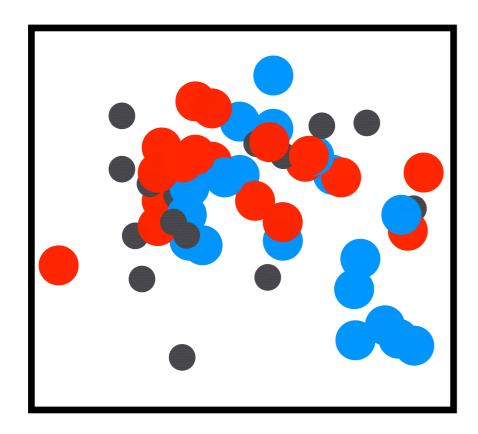


Baryons

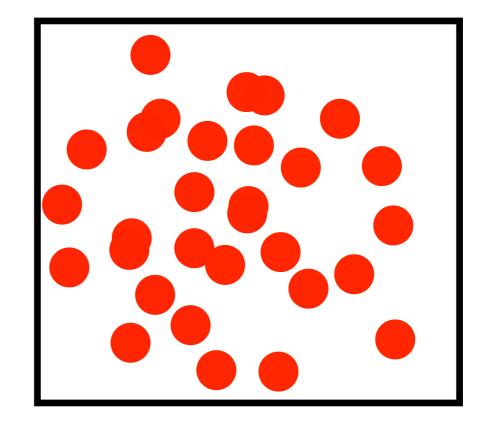




Increasing T Fixed low μ_B



Fixed Low T Increasing μ_B



Pions



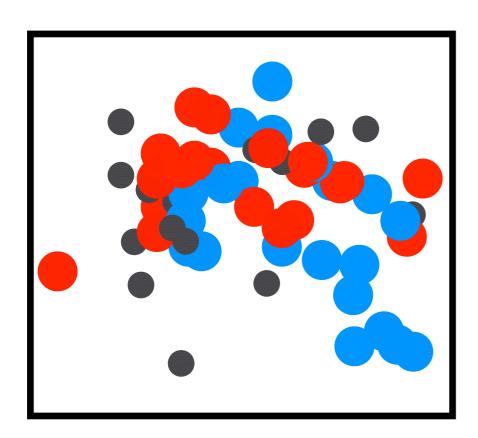
Baryons

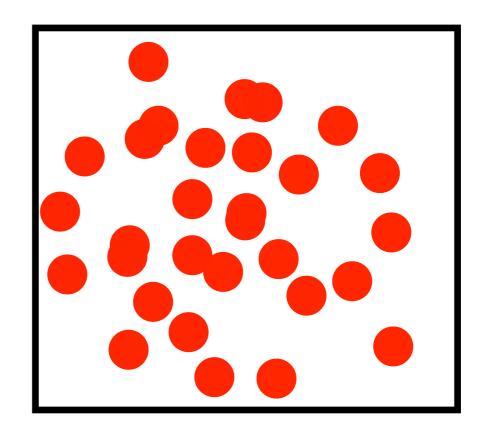


Anti Baryons



Increasing T Fixed low μ_B





Pions



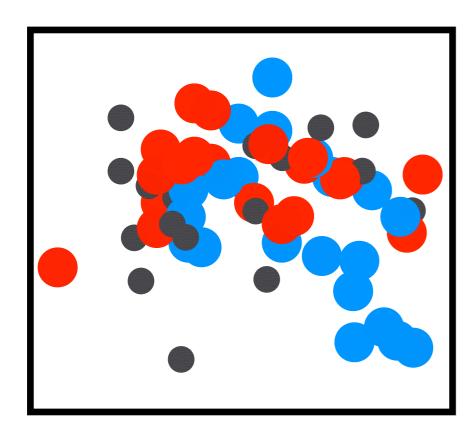
Baryons

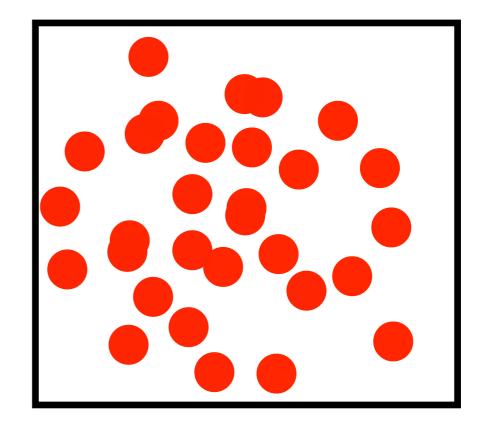


Anti Baryons



Increasing T Fixed low μ_B





Pions



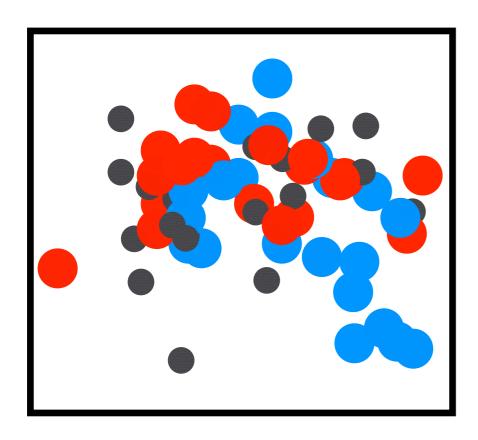
Baryons

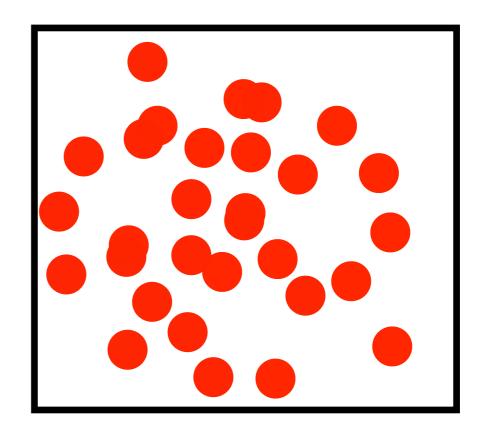


Anti Baryons



Increasing T Fixed low μ_B





Pions



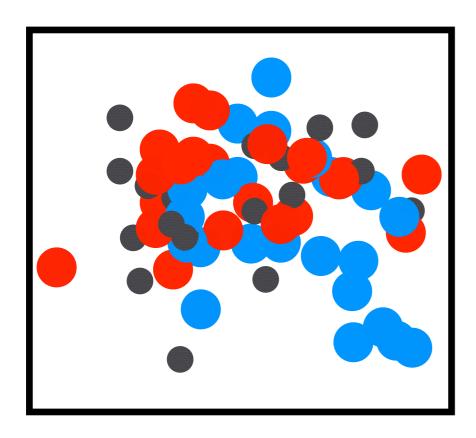
Baryons

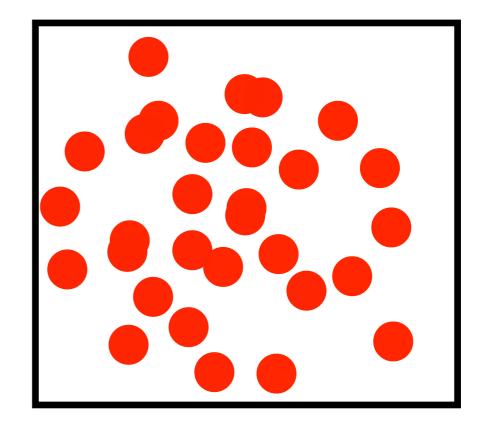


Anti Baryons



Increasing T Fixed low μ_B





Pions



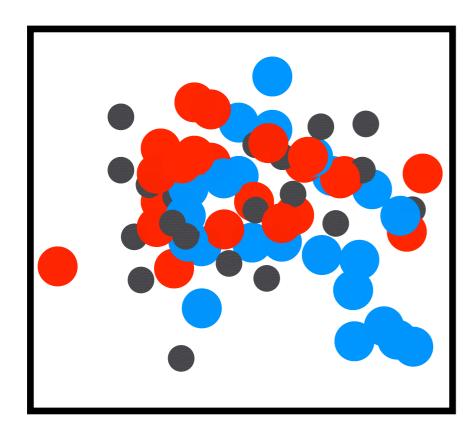
Baryons

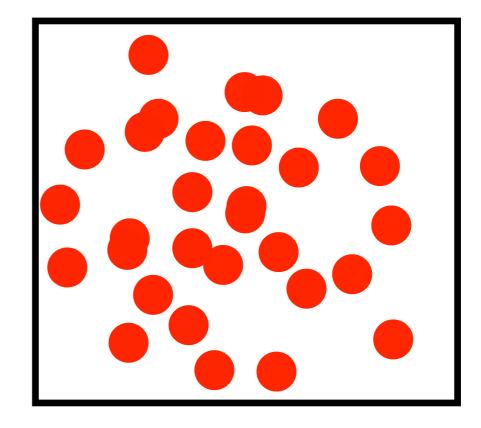


Anti Baryons



Increasing T Fixed low μ_B





Pions



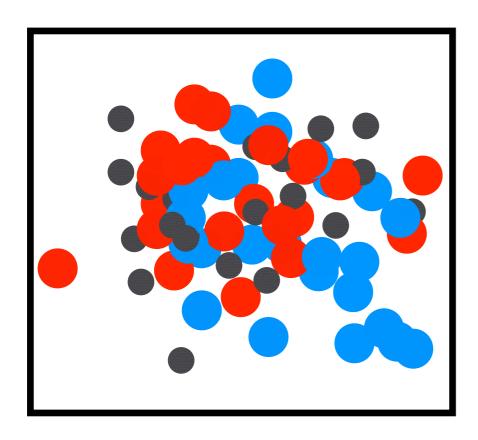
Baryons

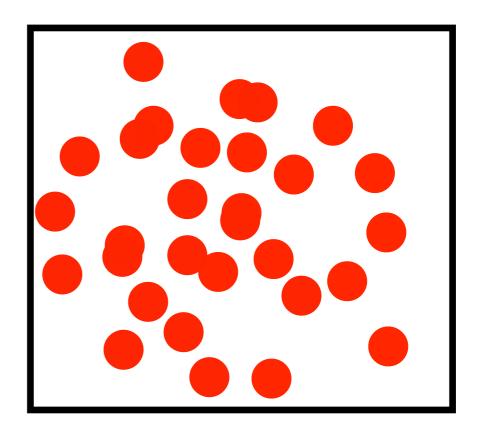


Anti Baryons



Increasing T Fixed low μ_B





Pions



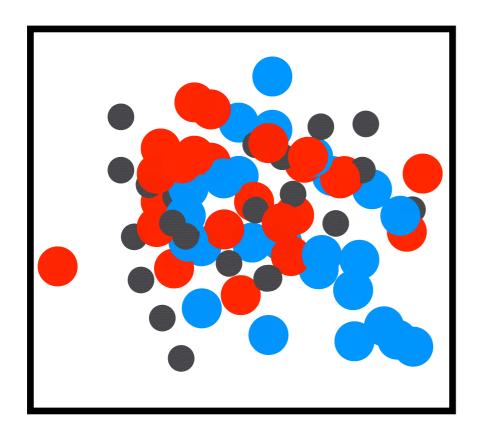
Baryons

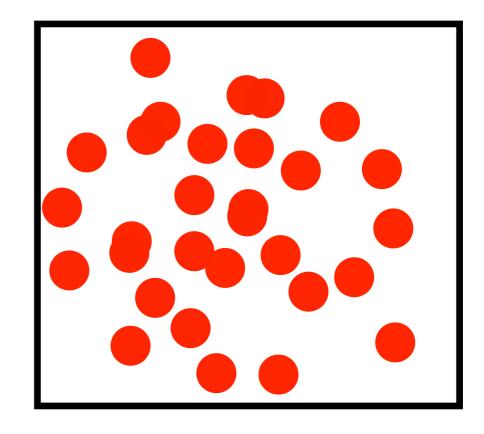


Anti Baryons



Increasing T Fixed low μ_B





Pions



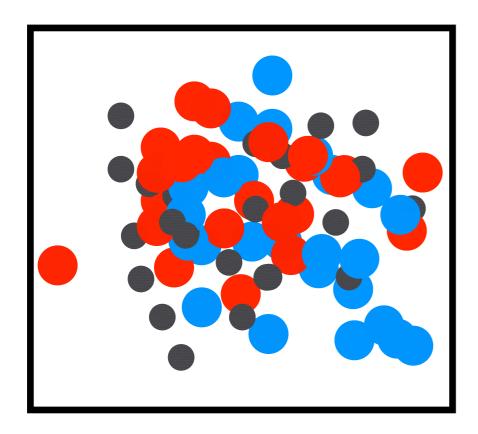
Baryons

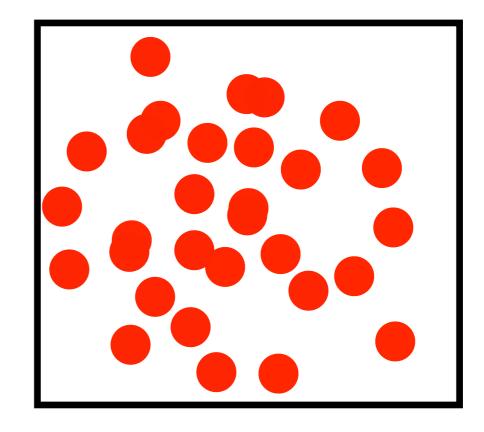


Anti Baryons



Increasing T Fixed low μ_B





Pions

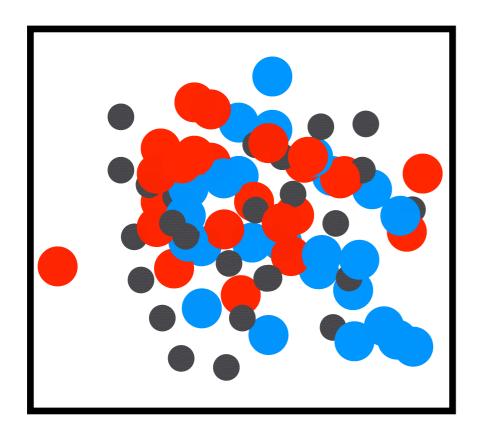
Baryons

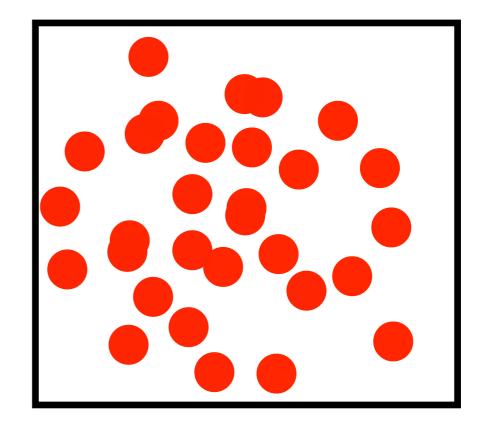


Anti Baryons



Increasing T Fixed low μ_B





Pions



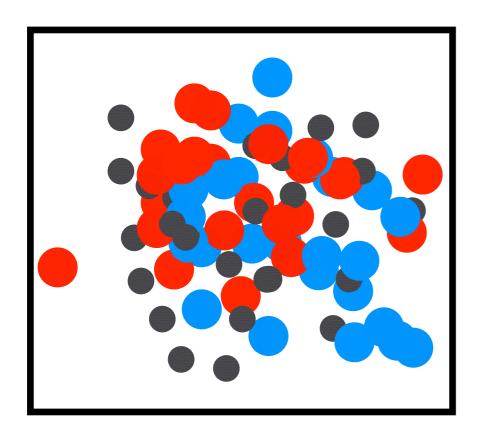
Baryons

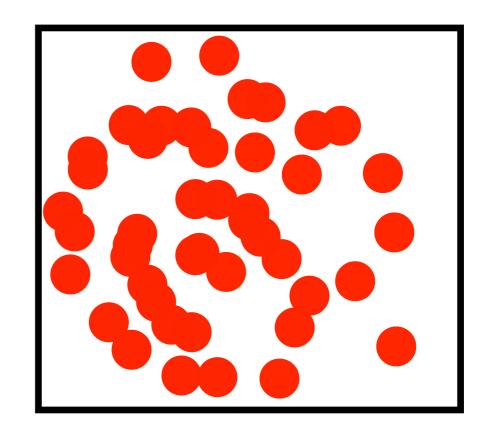


Anti Baryons



Increasing T Fixed low μ_B





Pions



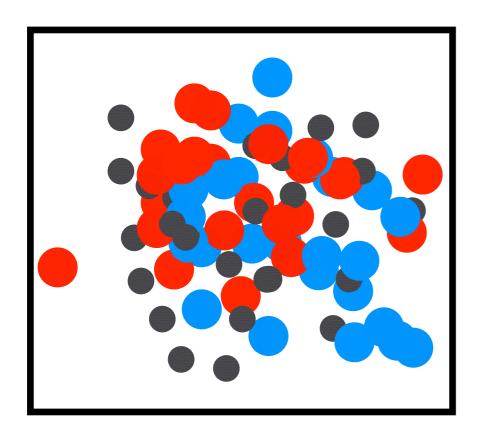
Baryons

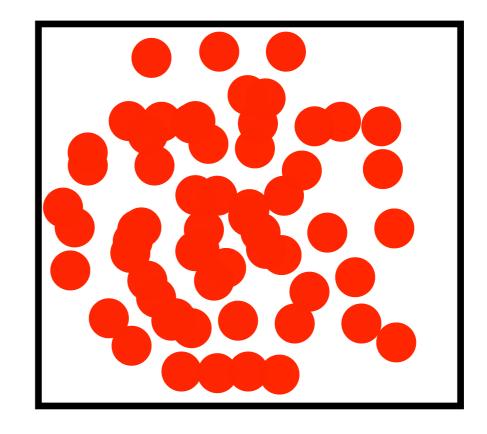


Anti Baryons



Increasing T Fixed low μ_B





Pions



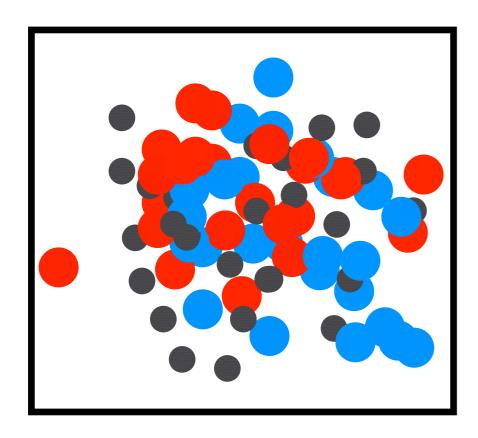
Baryons

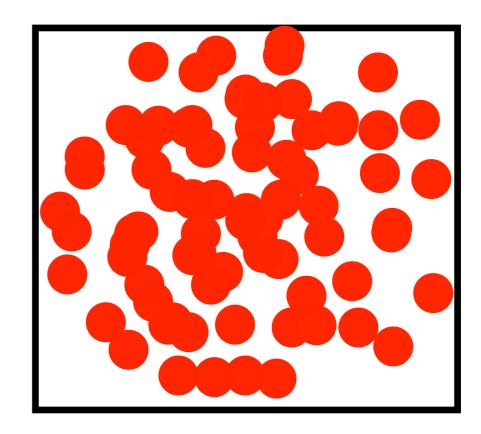


Anti Baryons



Increasing T Fixed low μ_B





Pions



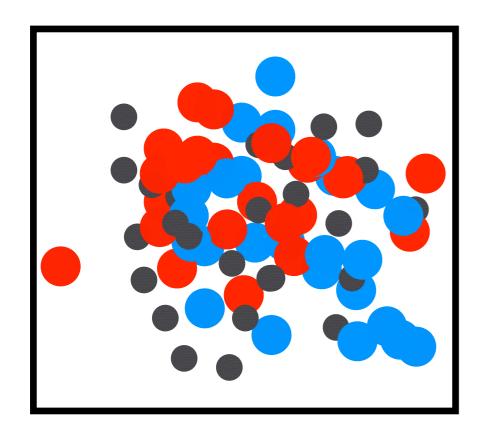
Baryons

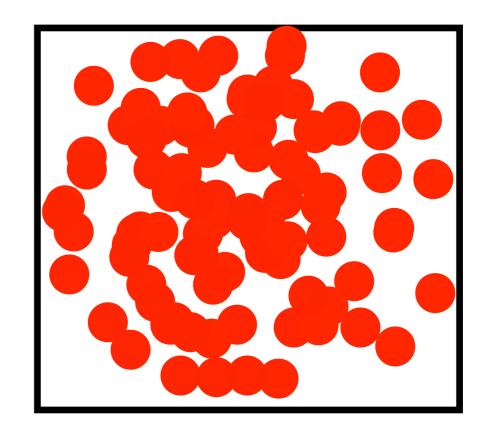


Anti Baryons

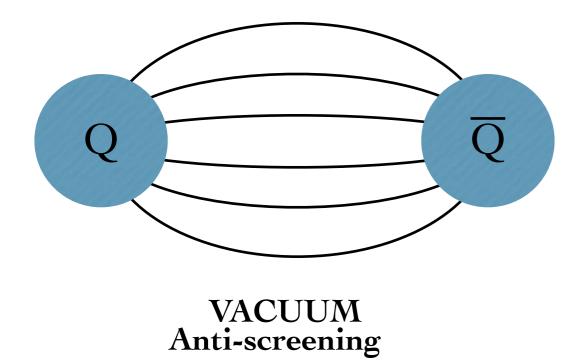


Increasing T Fixed low μ_B



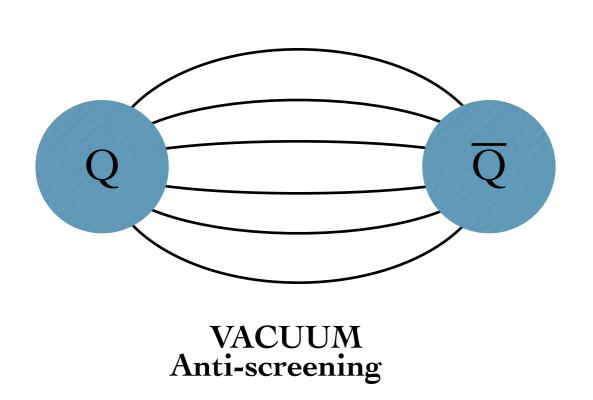


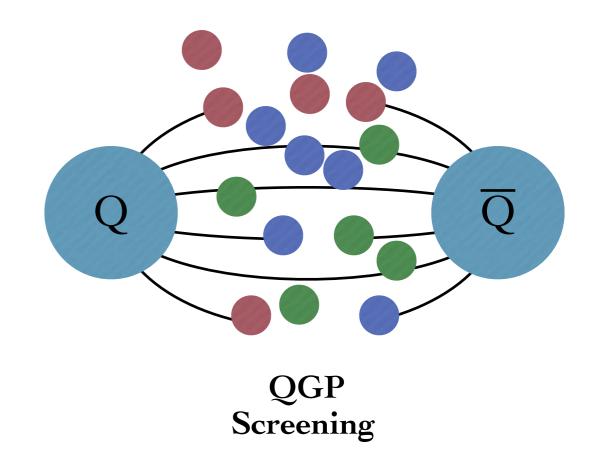
Color screening



M. Laine et al. JHEP 0703, 054 (2007)

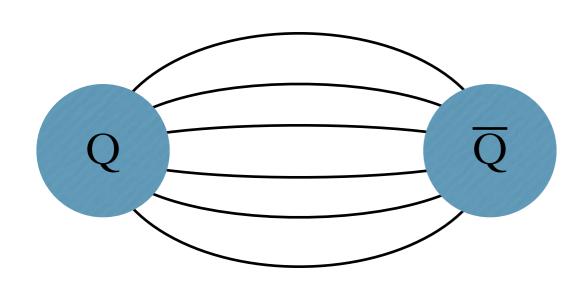
Color screening





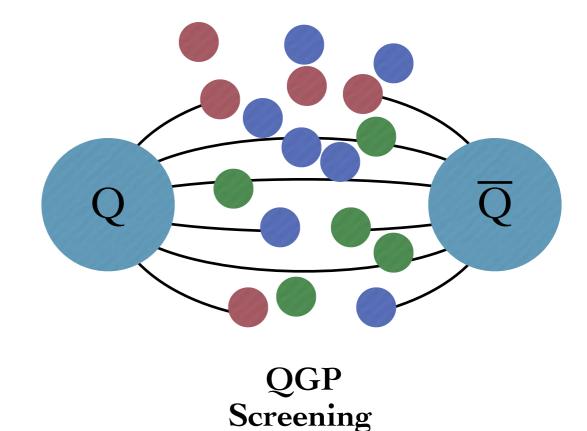
M. Laine et al. JHEP 0703, 054 (2007)

Color screening



VACUUM

Anti-screening



1000 $F_1(r,T)$ [Me \dot{V}] T[MeV] 175 ⊢ 500 186 197 200 0 203 215 226 -500 326 365 424 459 -1000 **RBC-Bielefeld Collaboration** 548 ↦ r [fm]

0.5

0

1.5

2

2.5

Pioneering work by Matsui and Satz Charmonia melting by Debye Screening Phys.Lett. B178 (1986) 416-422

One can use quarkonia melting as a "thermometer" of the QGP temperature

Landau damping is a competitive phenomenon M. Laine et al. JHEP 0703, 054 (2007)