

Constraining the $N-\Lambda \leftrightarrow N-\Sigma$ coupled-system using femtoscopy at the LHC

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STRANU: HOT TOPICS IN STRANGENESS NUCLEAR AND ATOMIC PHYSICS

24 May 2021 — 28 May 2021



Dimensions

$R \sim 10 - 15 \text{ km}$

$M \sim 1.5 - 2 M_{\odot}$

Outer Crust

Ions, electron gas,
Neutrons

Inner Core

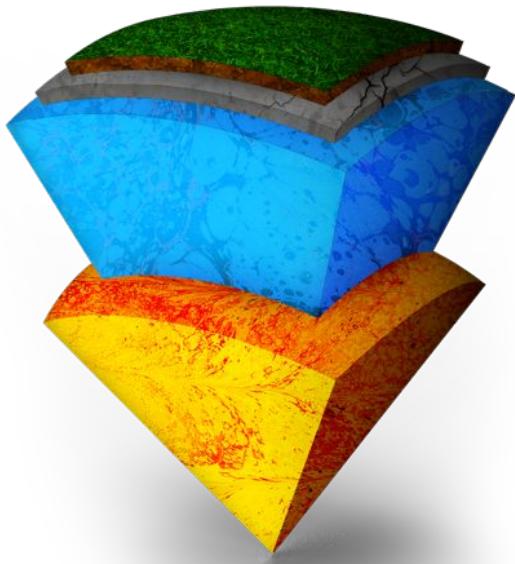
Neutrons?

Protons?

Hyperons?

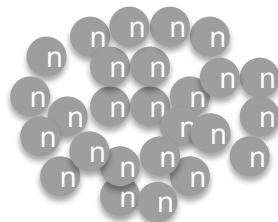
Kaon condensate?

Quark Matter?



Determination of the EoS challenging

- Particle composition of NS?
- Interaction among constituents?



Dimensions

$R \sim 10 - 15 \text{ km}$

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Outer Crust

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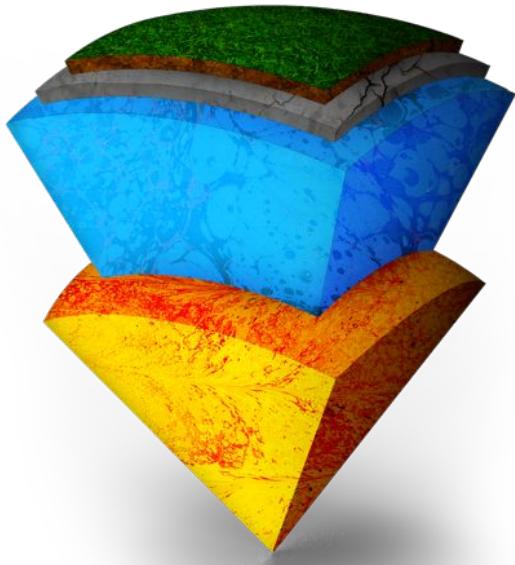
Neutrons?

Protons?

Hyperons?

Kaon condensate?

Quark Matter?

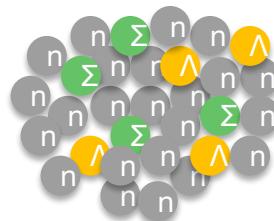


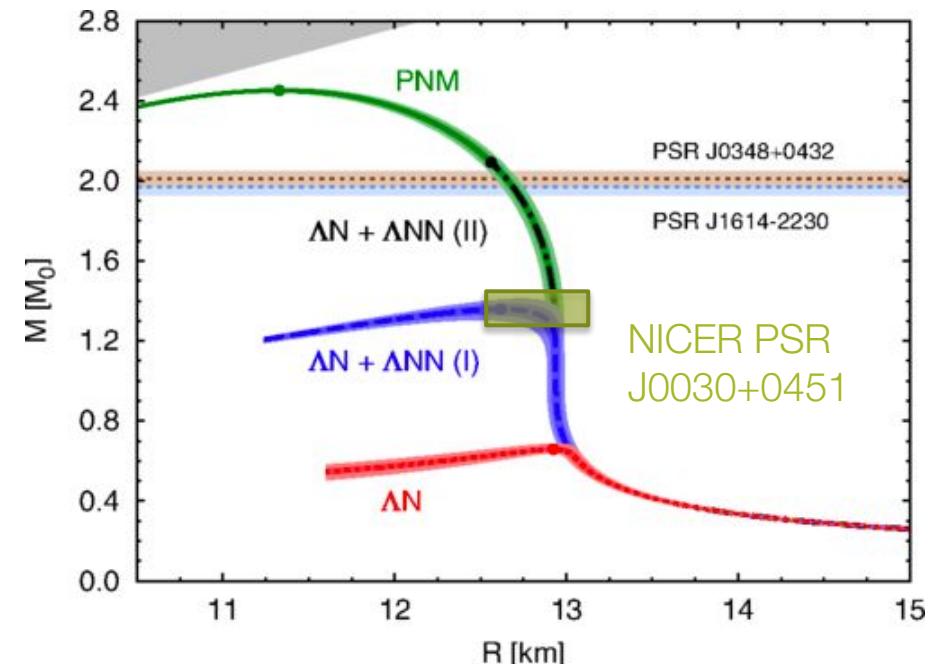
Determination of the EoS challenging

- Particle composition of NS?
- Interaction among constituents?

Considering energetically favourable scenarios

- Naively introduce Λ and other hyperons





Lonardoni et al. Phys. Rev. Lett 114, 092301 (2015)

'Hyperon-Puzzle'

- Hyperonic EoS in compatible with observations

Potential solutions

- Procure high precision measurements of N-Y interaction
- Provide constraints for genuine NNY-forces

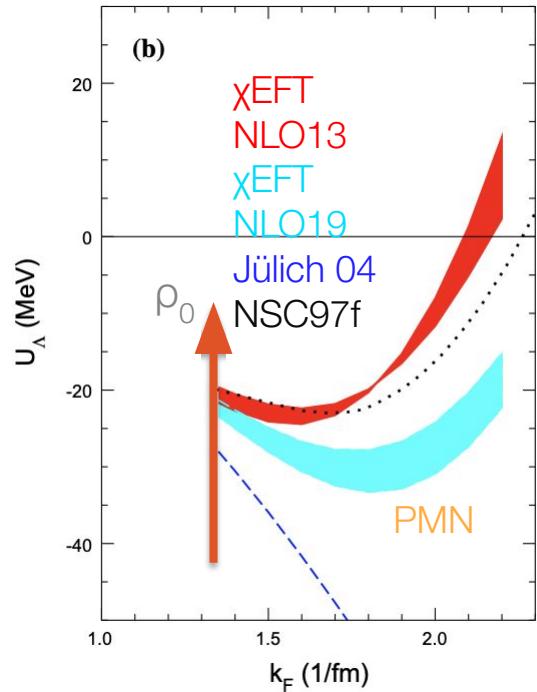
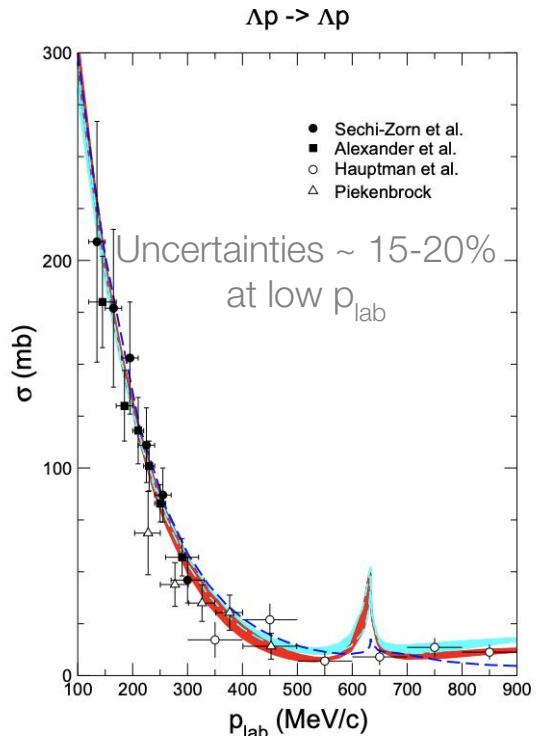


Experimental efforts

- Large uncertainties for low momenta
- No observation of predicted cusp from N- Λ \leftrightarrow N- Σ

Theory efforts

- N- Λ \leftrightarrow N- Σ affects Λ behaviour at finite density
- Implications for Λ NN(*)

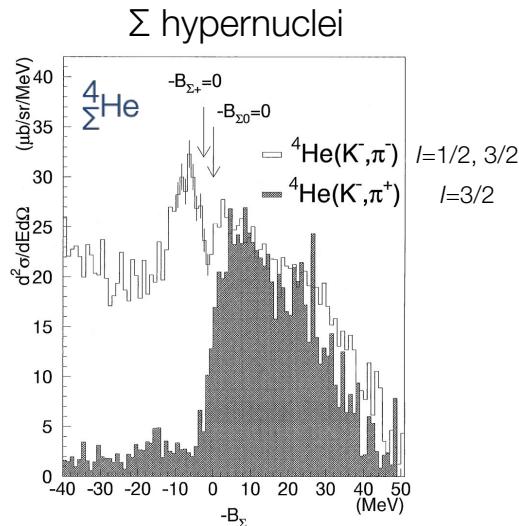


NLO13: J.Haidenbauer, N.Kaiser et al., NPA 915, 24 (2013)

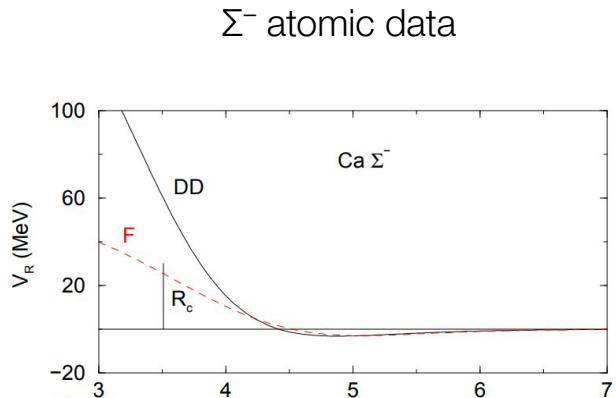
NLO19: J.Haidenbauer, U. Meißner, Eur.Phys.J.A 56 (2020)

(*)D. Gerstung et al. Eur.Phys.J.A 56 (2020) 6, 175





T. Nagae et al., *Phys. Rev. Lett.* 80 (1998) 1605.



G. Backenstoss et al., *Phys. Lett.* B33 (1970) 230.
E. Friedman and A. Gal, *Phys. Rept.* 452 (2007) 89.

Theory predictions

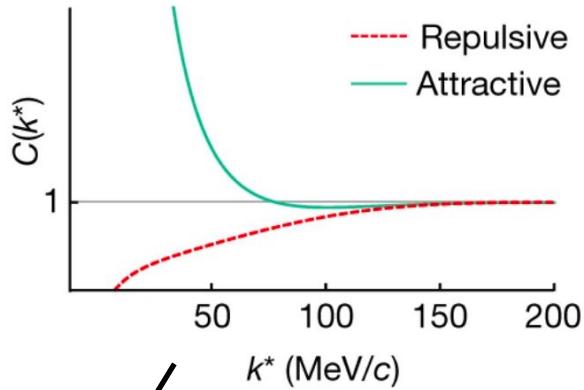
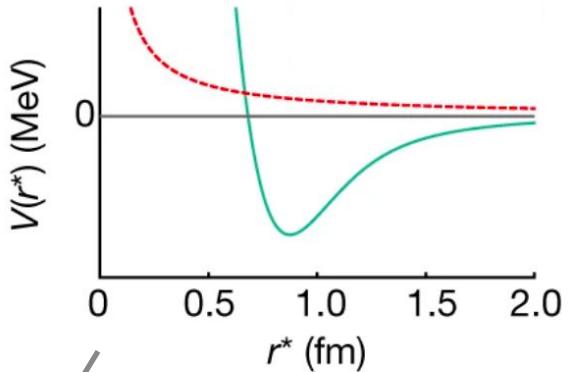
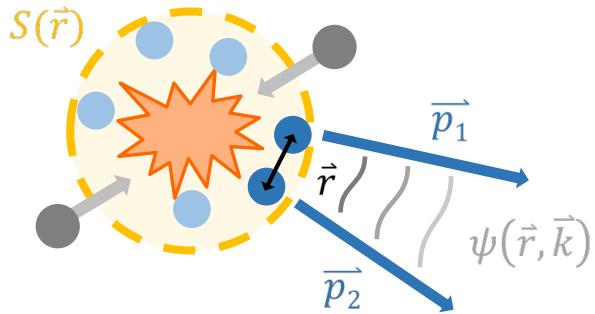
Model	U_Σ (MeV)
NSC97f	-16.1
ESC16	-3.3
fss2	7.5
HAL QCD	14.6
χ EFT (NLO)	17.1

T. Rijken et al., *Phys. Rev.* C59 (1999) 21.
M. Nagels et al., *Phys. Rev.* C99 (2019) 044003.
Y. Fujiwara et al., *Prog. Part. Nucl. Phys.* 58 (2007) 439.
HAL QCD Collab., *AIP Conf. Proc.* 2130 (2019) 020002.
J. Haidenbauer et al., *Nucl. Phys.* A915 (2013) 24.

Inventory of theoretical models

- Strongly isospin dependent interaction
- Different scattering parameters predicted by different models





Schrödinger Equation for
relative Wavefunction

$$C(k^*) = \int S(\vec{r}^*) |\psi(\vec{k}^*, \vec{r}^*)|^2 d^3\vec{r}^* = \mathcal{N} \frac{N_{same}(k^*)}{N_{mixed}(k^*)} \xrightarrow{k^* \rightarrow \infty} 1$$



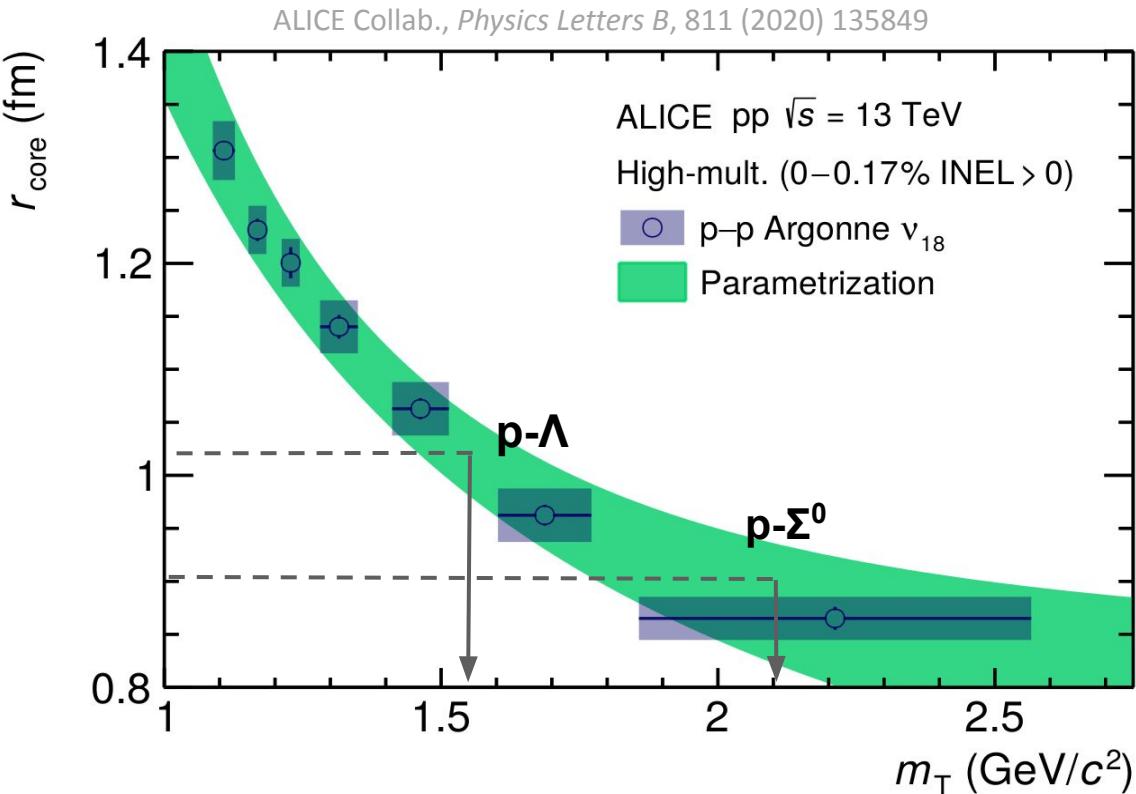
Relative momentum $k^* = \frac{1}{2} | \vec{p}_1^* - \vec{p}_2^* |$ and $\vec{p}_1^* + \vec{p}_2^* = 0$
Relative distance $\vec{r}^* = \vec{r}_1^* - \vec{r}_2^*$

Universal source model

- r_{core} fixed for each pair based on $\langle m_T \rangle$
- Particle-specific resonances are added to the core

Core radii

- $r_{\text{core}}(\text{p}\Lambda) = 1.02$, $r_{\text{eff}}(\text{p}\Lambda) = 1.23$
- $r_{\text{core}}(\text{p}\Sigma^0) = 0.91$, $r_{\text{eff}}(\text{p}\Sigma^0) = 1.25$



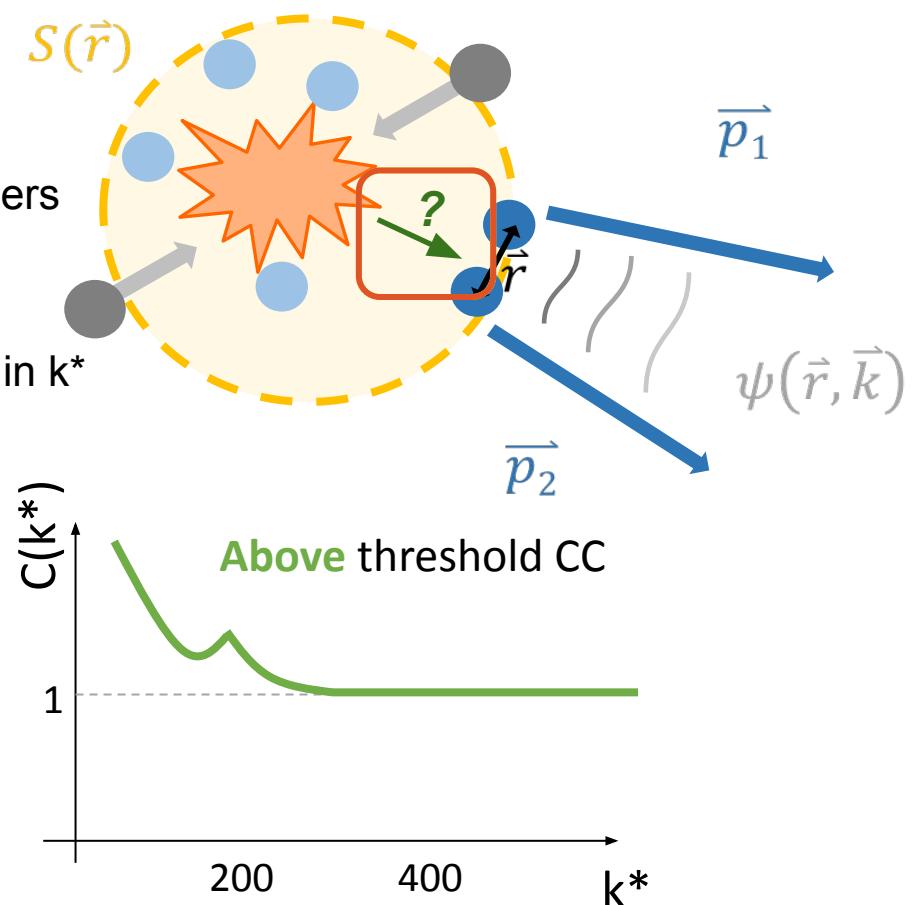
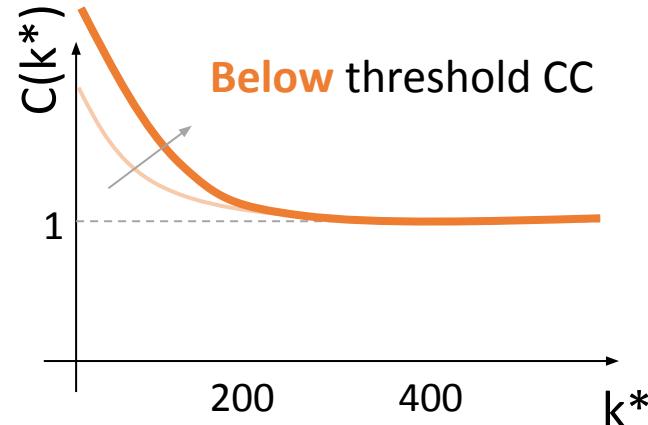
'Coupled-Channels'

- Different pair with matching quantum numbers

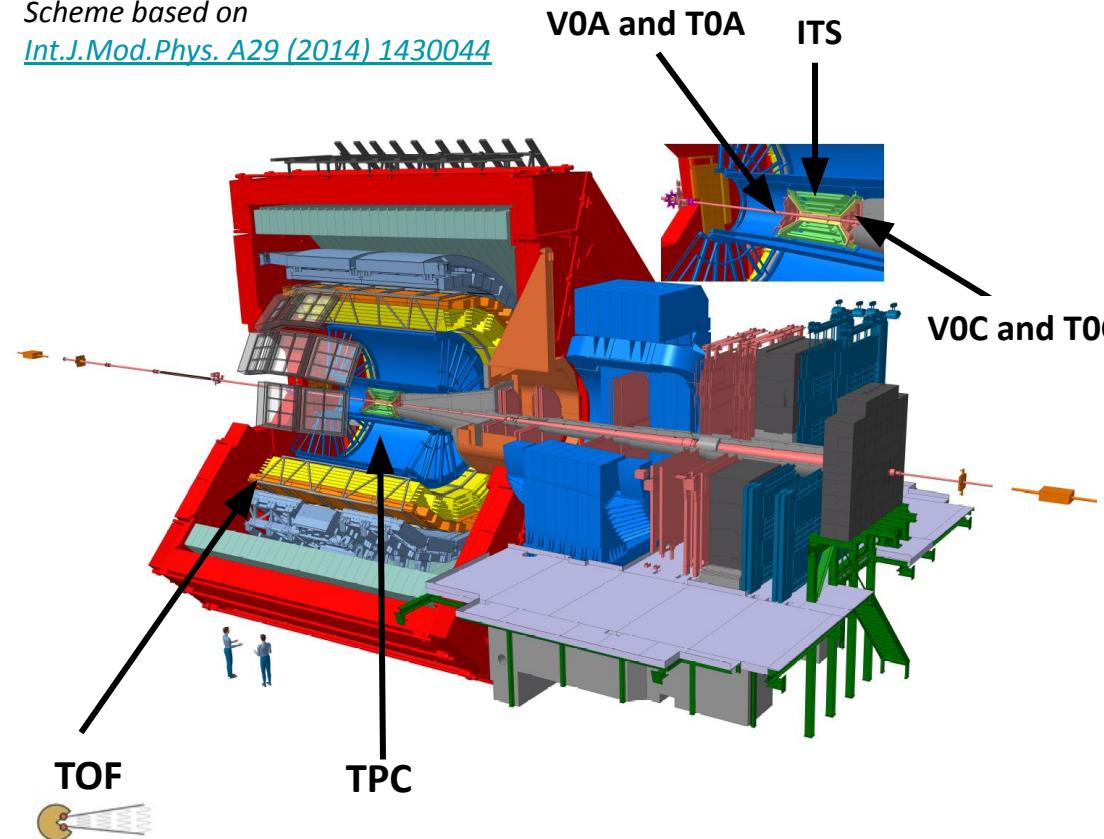
J. Haidenbauer, Nucl.Phys.A 981 (2019) 1
Y. Kamiya et al., Phys.Rev.Lett. 124 (2020) 13

Emerging threshold effects

- Above**: Cusp-structure at channel opening in k^*
- Below**: Enhanced of CF at small k^*



Scheme based on
[Int.J.Mod.Phys. A29 \(2014\) 1430044](https://doi.org/10.1142/S0217751X1430044)



Data analysis

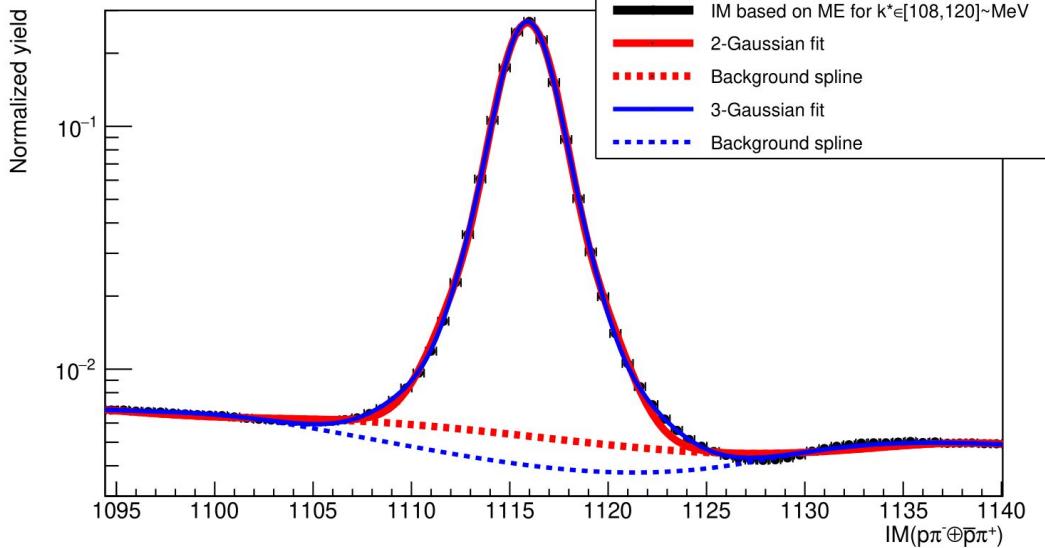
- Data set pp 13 TeV (1000 M high multipl. events)
- Direct detection of charged particles (protons, kaons, pions)
- Reconstruction of hyperons:

$$\Sigma^0 \rightarrow \gamma \Lambda \quad (\text{B.R.: } \sim 100\%)$$

$$\Lambda \rightarrow p \pi^- \quad (\text{B.R.: } \sim 64\%)$$

- # of pairs for $k^* < 200$ MeV/c:
 - $p-\Sigma^0 \sim 1120$
 - $p-\Lambda \sim 13 \times 10^5$

$$C_{exp}(k^*) = \textcircled{P_\Lambda} C_{corrected}(k^*) + (1 - \textcircled{P_\Lambda}) C_{p\tilde{\Lambda}}(k^*)$$



Explanation

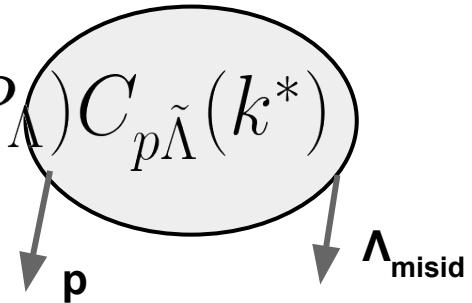
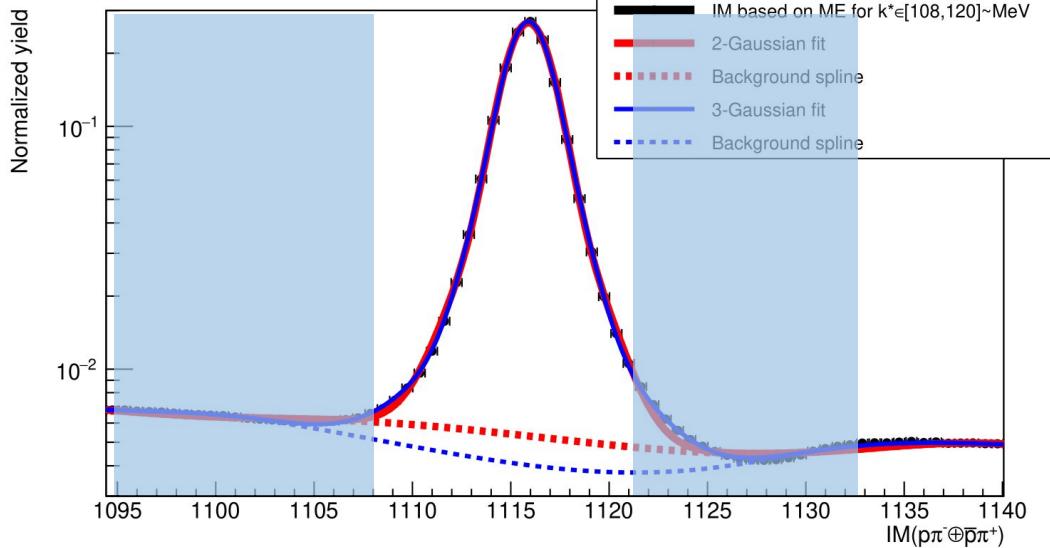
- Purity of the reconstructed Λ

Derivation

- Double gaussian fit to invariant mass spectrum yields
 $P(\Lambda) = 95.3\% \quad [P(p) = 99.4\%]$



$$C_{exp}(k^*) = P_\Lambda C_{corrected}(k^*) + (1 - P_\Lambda) C_{p\tilde{\Lambda}}(k^*)$$



Explanation

- CF obtained from a '**sideband analysis**'

Derivation

- Pair p with Λ of a mass which is outside $3-8\sigma$ -band away of nominal mass



$$C_{exp}(k^*) = P_\Lambda C_{corrected}(k^*) + (1 - P_\Lambda) C_{p\tilde{\Lambda}}(k^*)$$

$$b(k^*) [\lambda_{p\Lambda} C_{p\Lambda}(k^*) + \lambda_{p(\Sigma^0)} C_{p(\Sigma^0)}(k^*) + \lambda_{p(\Xi)} C_{p(\Xi)}(k^*) + \lambda_{ff} + \lambda_{\tilde{p}\Lambda}]$$

Explanation

- In order to quantify each single contribution use the formalism of λ parameters

Derivation

- Purity as before
- Fractions determined data driven (CPA template fits)

$$\lambda_{ij} = f_i p_i f_j p_j$$

fraction

purity



$$C_{exp}(k^*) = P_\Lambda C_{corrected}(k^*) + (1 - P_\Lambda) C_{p\tilde{\Lambda}}(k^*)$$



$$b(k^*) [\lambda_{p\Lambda} C_{p\Lambda}(k^*) + \lambda_{p(\Sigma^0)} C_{p(\Sigma^0)}(k^*) + \lambda_{p(\Xi)} C_{p(\Xi)}(k^*) + \lambda_{ff} + \lambda_{\tilde{p}\Lambda}]$$

47.1%	15.7%	19.0%	17.6%	0.6%
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Explanation

- In order to quantify each single contribution use the formalism of λ parameters

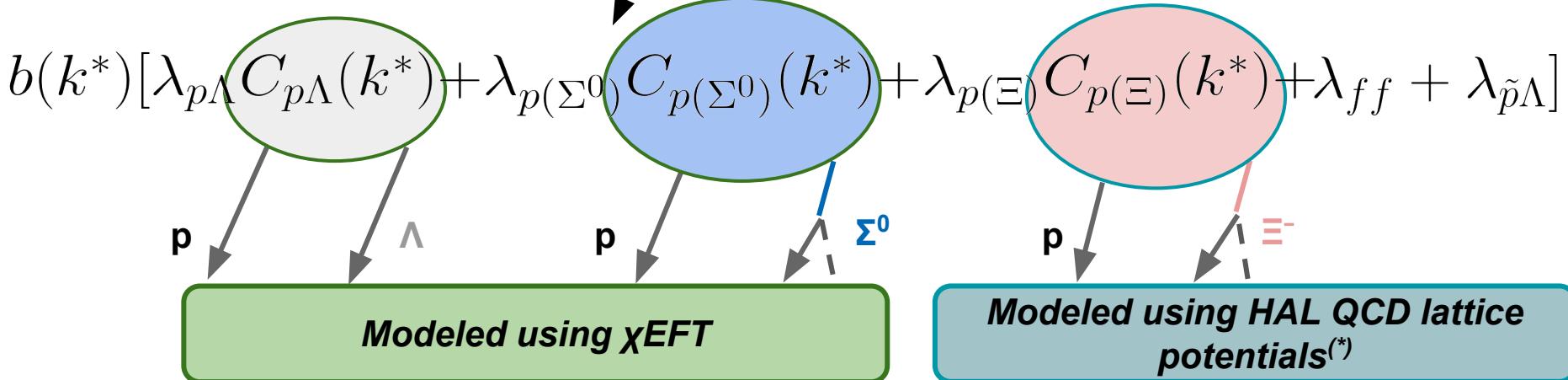
Derivation

- Purity as before
- Fractions determined data driven (CPA template fits)



Pair	λ (%)
p- Λ	47.1
p- Σ^0	15.7
p- Ξ	19.0
Flat-feeddown	17.6
p~ Λ	0.6

$$C_{exp}(k^*) = P_\Lambda C_{corrected}(k^*) + (1 - P_\Lambda) C_{p\tilde{\Lambda}}(k^*)$$



Note

- $p\text{-}\Sigma^0$: Not well known
- $p\text{-}\Xi^-$: Known from femtoscopic measurements^(**)

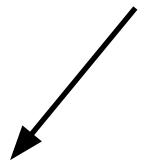
(*) T. Hatsuda Front. Phys. 13(6), 132105 (2018))

(**) ALICE Coll. Phys. Rev. Lett 123, (2019) 112002

ALICE Coll. Nature 588, 232–238 (2020)



$$C_{exp}(k^*) = P_\Lambda C_{corrected}(k^*) + (1 - P_\Lambda) C_{p\tilde{\Lambda}}(k^*)$$



$$b(k^*) [\lambda_{p\Lambda} C_{p\Lambda}(k^*) + \lambda_{p(\Sigma^0)} C_{p(\Sigma^0)}(k^*) + \lambda_{p(\Xi)} C_{p(\Xi)}(k^*) + \lambda_{ff} + \lambda_{\tilde{p}\Lambda}]$$

Explanation

- Non-femtoscopic background

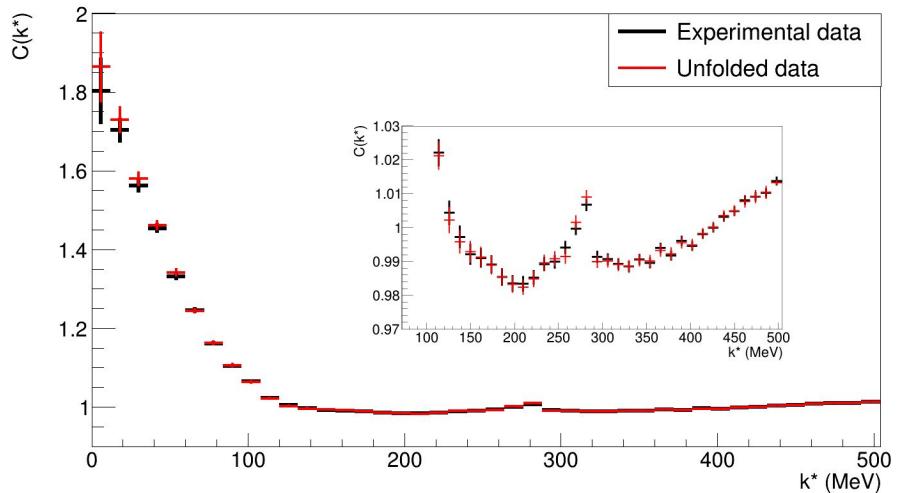


$$C_{exp}(k^*) = P_\Lambda C_{corrected}(k^*) + (1 - P_\Lambda) C_{p\tilde{\Lambda}}(k^*)$$

CF used in fits

- Signal of interest corrected for residual mis-identifications and **unfolded** for momentum resolution
 - Effect most pronounced at $k^* < 60 \text{ MeV}/c \rightarrow$ changes up to 2%

$$C_{corrected}(k^*) = \frac{C_{exp}(k^*) + (1 - P_\Lambda) C_{p\tilde{\Lambda}}(k^*)}{P_\Lambda}$$



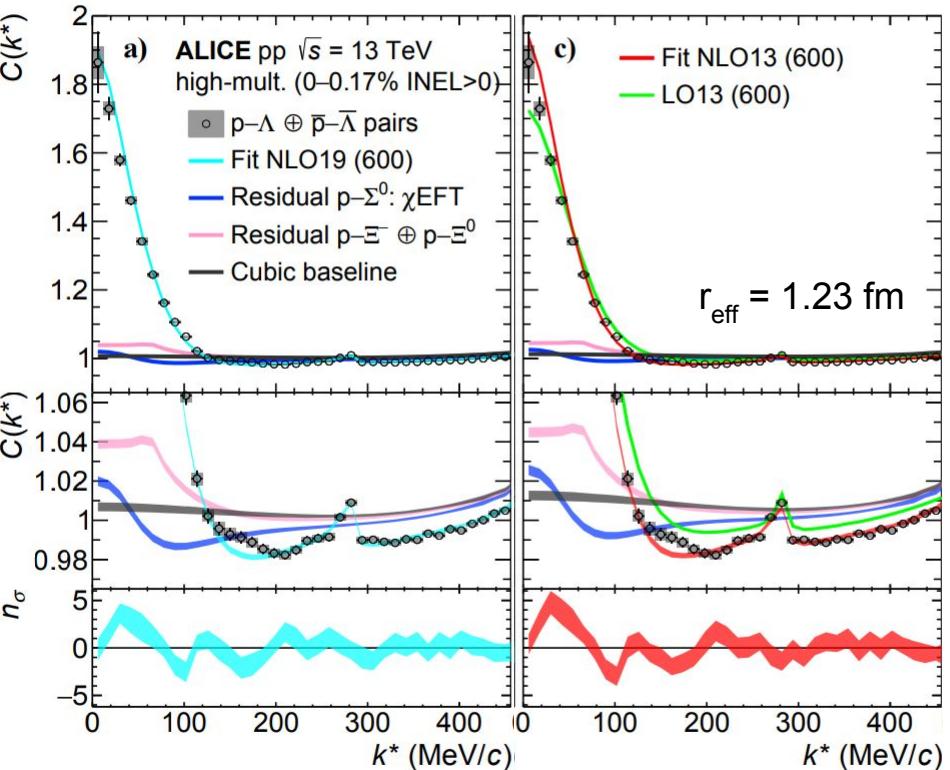
ALICE collab., arXiv:2104.04427 submitted to PRL

New Results

- First observation of cusp from $N-\Lambda \leftrightarrow N-\Sigma$
- High precision data down to low k^*

Discussion

- NLO19 (600) preferred
 - less (enhanced) attractive Λ interaction in vacuum (at high densities)
 - requires more repulsive NN Λ
 - deviations $> 3\sigma$



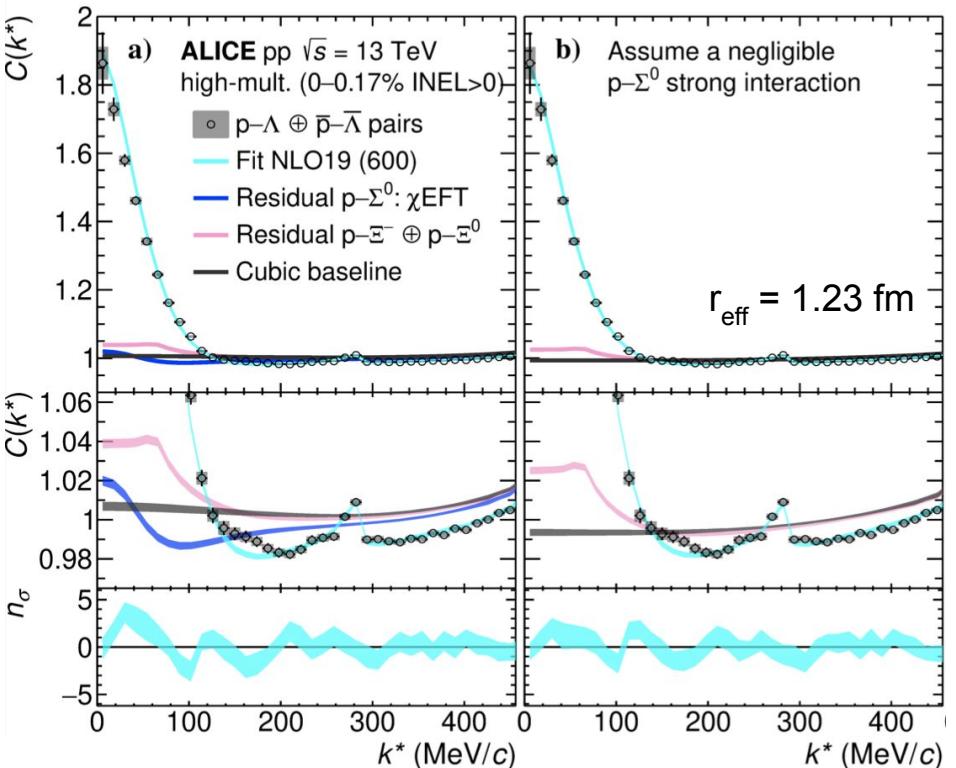
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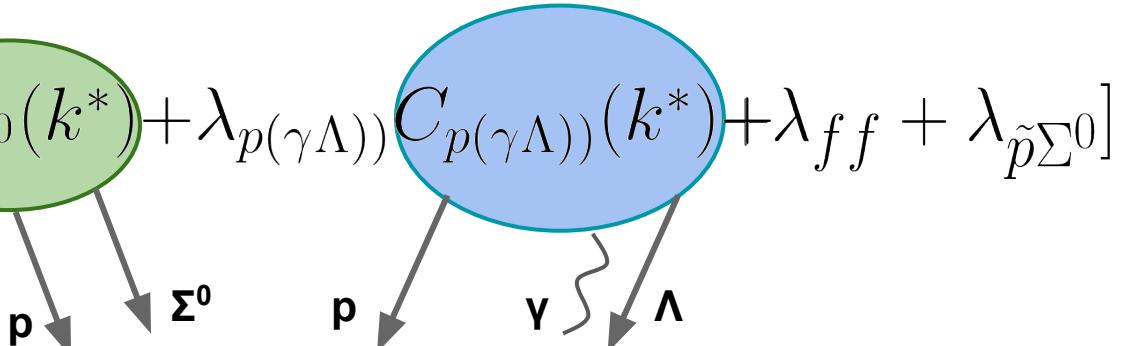
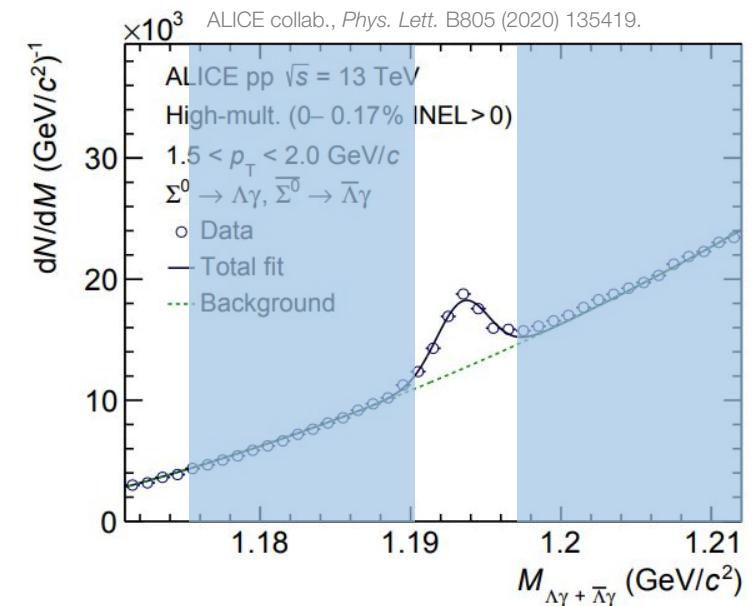
- First observation of cusp from $N-\Lambda \leftrightarrow N-\Sigma$
- High precision data down to low k^*

Discussion

- Negligible interaction for $p-\Sigma^0$ is favoured



$$C_{exp}(k^*) = b(k^*)[\lambda_{p\Sigma^0} C_{p\Sigma^0}(k^*) + \lambda_{p(\gamma\Lambda)} C_{p(\gamma\Lambda)}(k^*) + \lambda_{ff} + \lambda_{\tilde{p}\Sigma^0}]$$



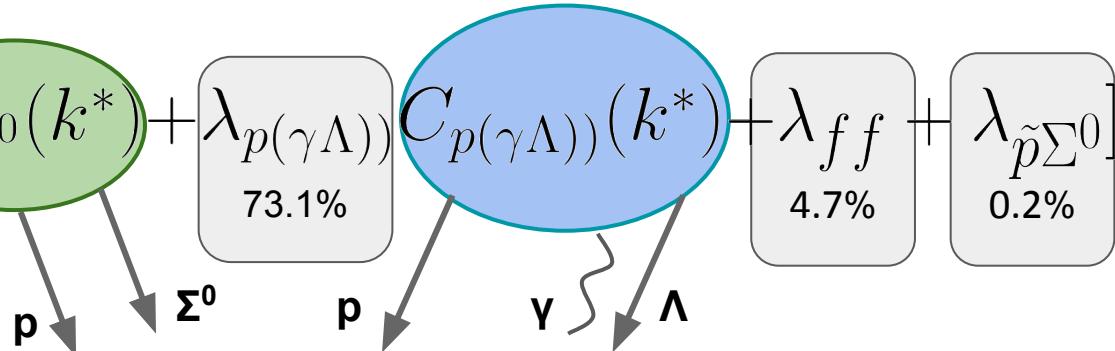
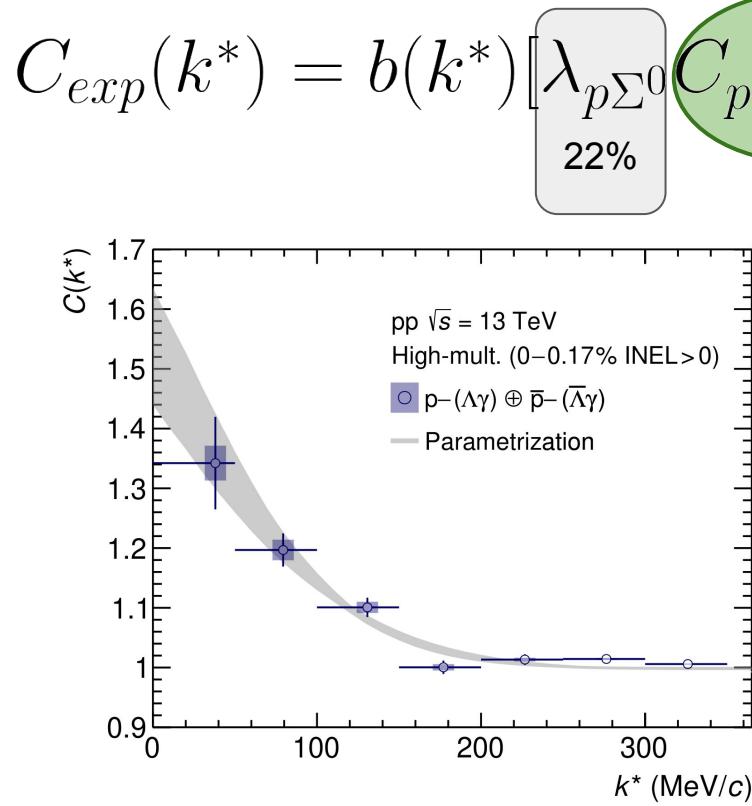
Explanation

- **Genuine** CF
- CF obtained from a '**sideband analysis**'

Derivation

- Pair p with Σ^0 of a mass which is outside $3-8\sigma$ -band away of nominal mass





'sideband analysis'

- CF is dominated by contributions from the sidebands
- Modeled by Gaussian distribution

Note

- The CF obtained from sidebands is the 'reference' in this study

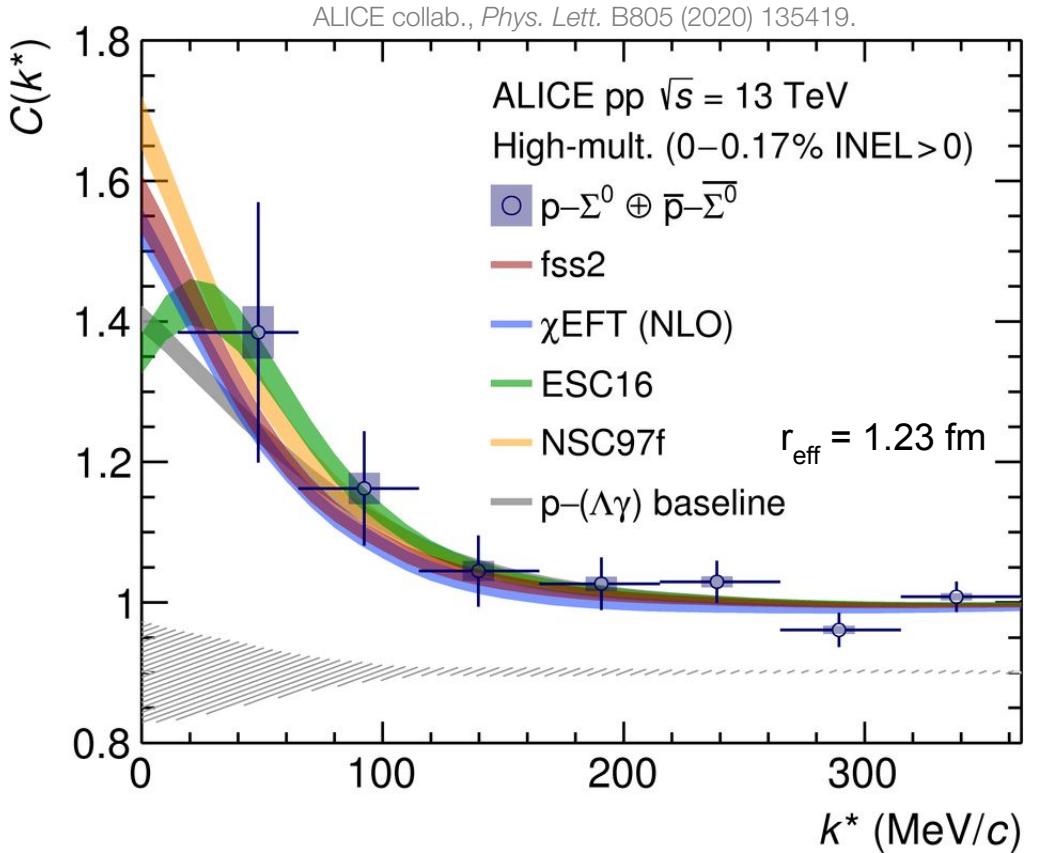


New Results

- First observation of N- Σ interaction

Discussion

- CF consistent with reference baseline obtained from sidebands
 - shallow attractive interaction of p- Σ
 - indicates positive sign for potential



High precision measurement of p- Λ

- High resolution of cusp structure $N-\Lambda \leftrightarrow N-\Sigma$
 - Favours NLO19 (600):
 - less (enhanced) attractive Λ interaction in vacuum (at high densities)
 - necessitates more repulsive $NN\Lambda$
- => High quality data available for model tuning
- => Probing the genuine 3-body forces with high precision femtoscopy in RUN3

First successful observation of p- Σ

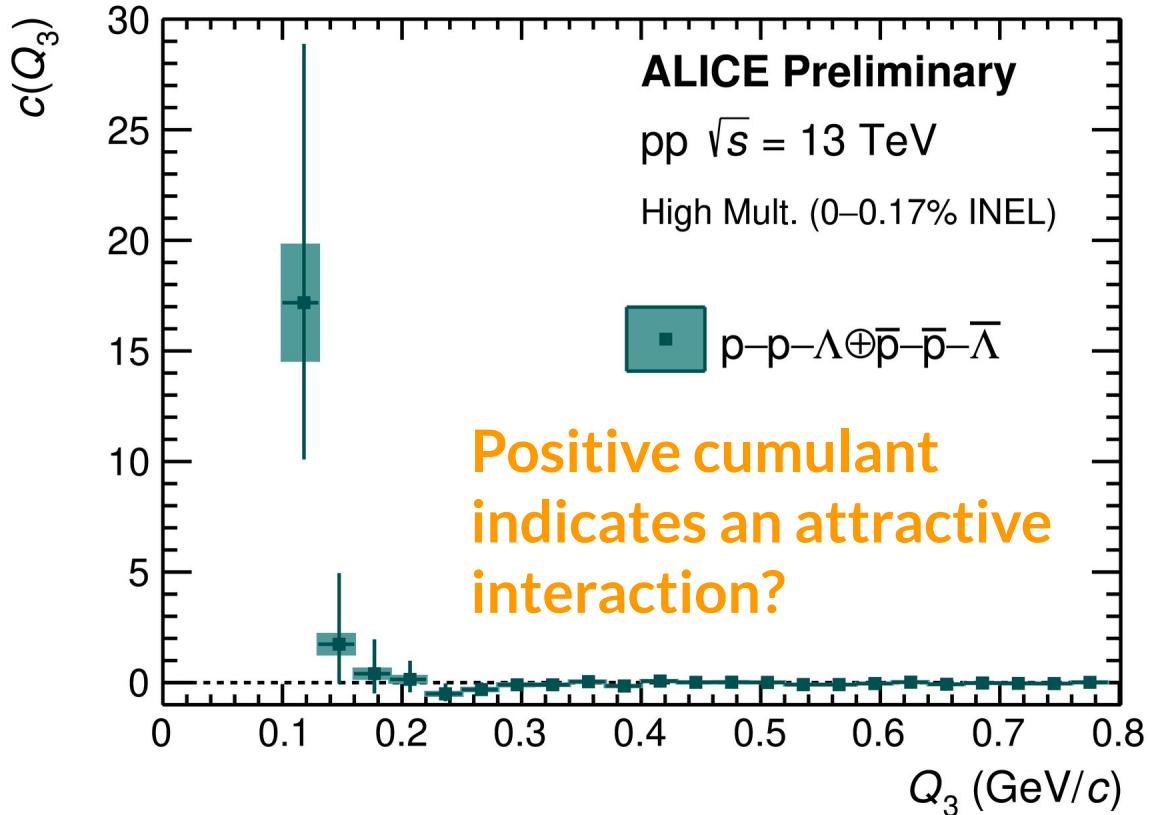
- In favour of shallow strong interaction
 - Indicates positive sign for single particle potential
- => Clarification of the role of Σ within reach with RUN3 data



- High r_s
- High r_s
 - Fave

=> High
=> Prc

- First sign
- In favor
 - Indicative
- => Class



Back-up

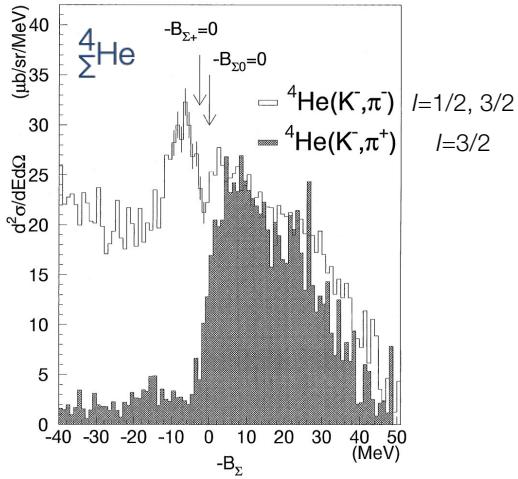
Back-up

- $N\Sigma$ additional slides with comments about exp.data till now
- Femtoscopy: Information about the source
- Reconstruction of Σ^0 with ALICE
- Reconstruction of Λ with ALICE
- CC-modified Koonin-Pratt eqn.
- Details on the unfolding procedure

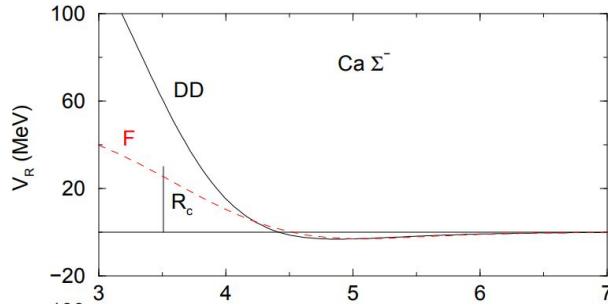


Knowledge about N- Σ

Σ hypernuclei



Σ^- atomic data



G. Backenstoss *et al.*, *Phys. Lett.* B33 (1970) 230.
E. Friedman and A. Gal, *Phys. Rept.* 452 (2007) 89.

T. Nagae *et al.*, *Phys. Rev. Lett.* 80 (1998) 1605.

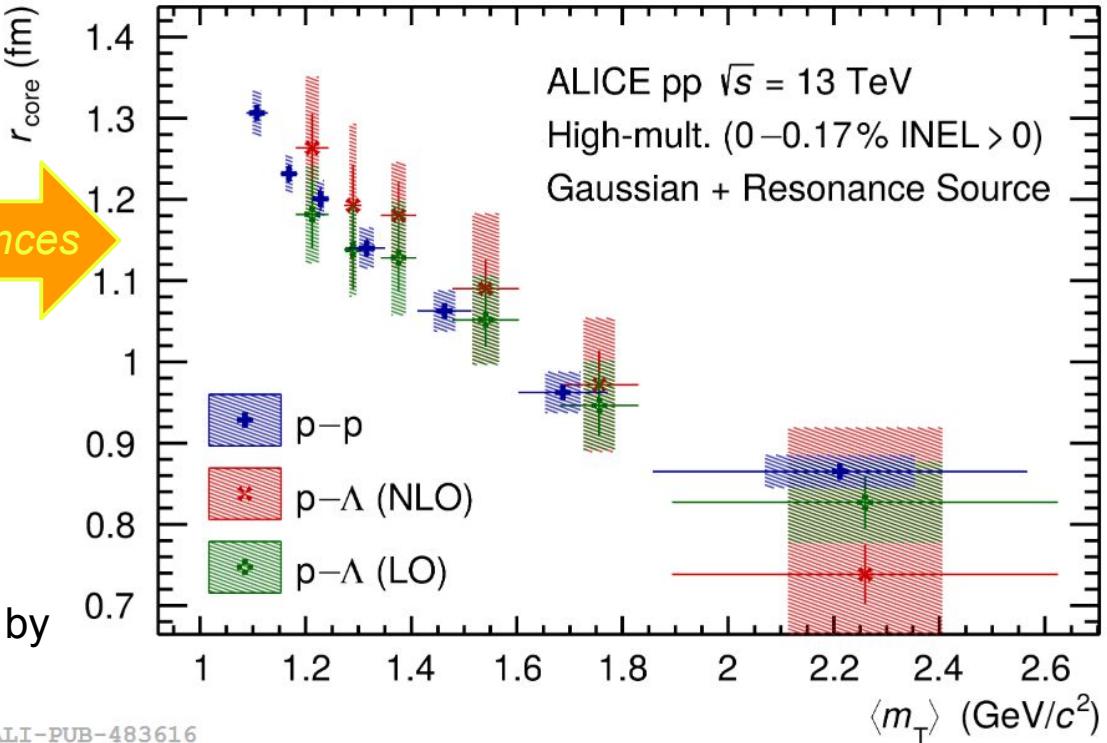
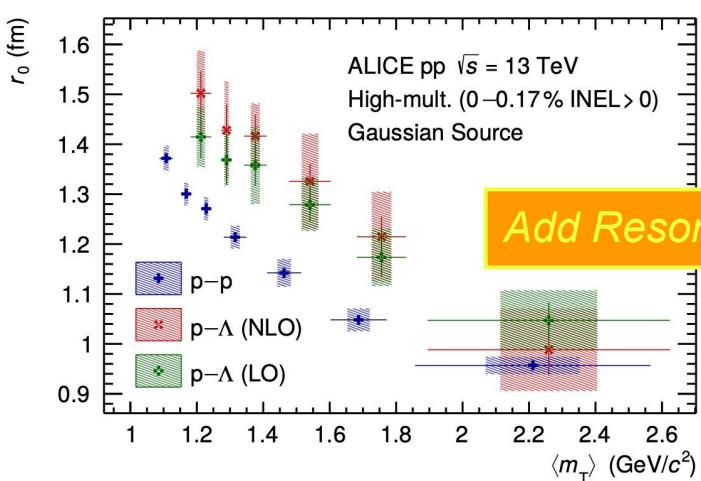
Inventory of experimental data

- Few events of hypernuclei
- Optical potential derived from atomic data



Femtoscopy: Source

ALICE Collab., Physics Letters B, 811 (2020) 135849



Source modifications

- Increase in apparent source size by short lived strongly-decaying resonances (e.g. Δ)

ALI-PUB-483616



Femtoscopy: Source

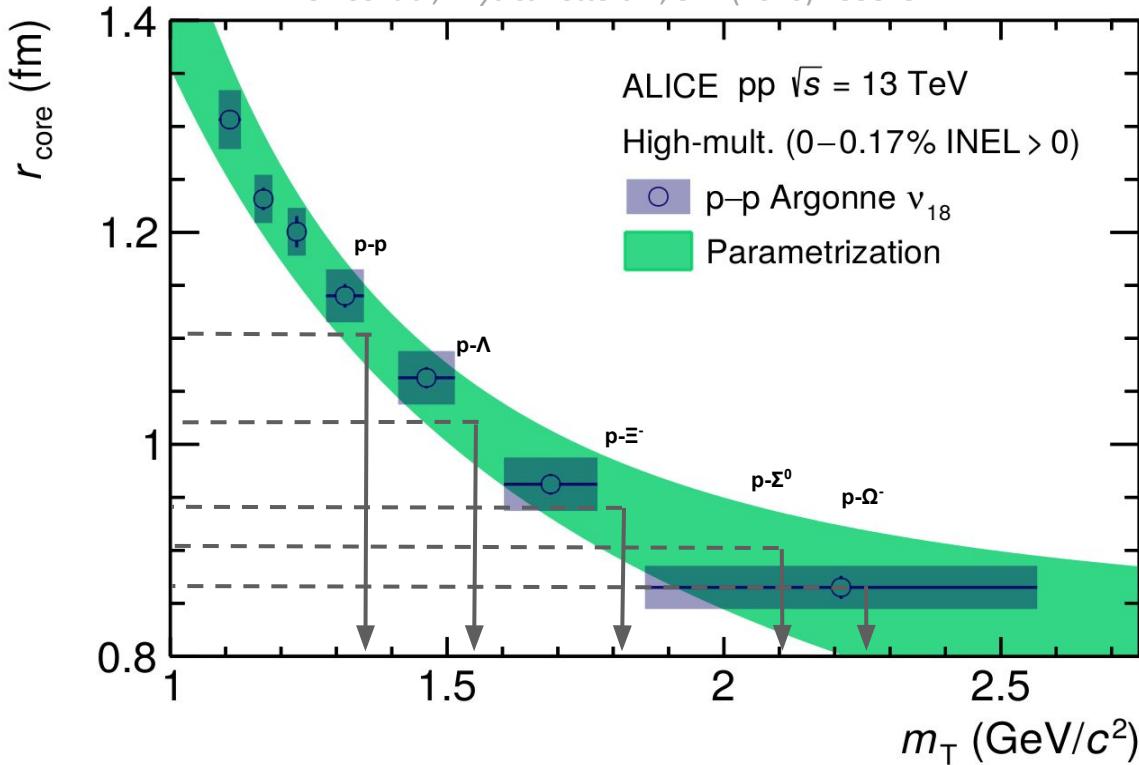
ALICE Collab., Physics Letters B, 811 (2020) 135849

Universal source model

- r_{core} fixed for each pair based on $\langle m_T \rangle$
- Particle-specific resonances are added to the core

Notice

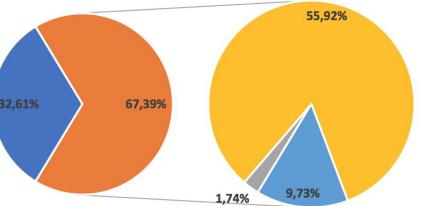
- Small radii probe large densities



Femtoscopy: Source Resonances

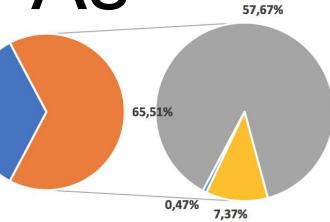
Protons

- Primordial
- From resonances
- $\text{ct} > 2 \text{ fm}$
- $1 < \text{ct} < 2 \text{ fm}$
- $\text{ct} < 1 \text{ fm}$



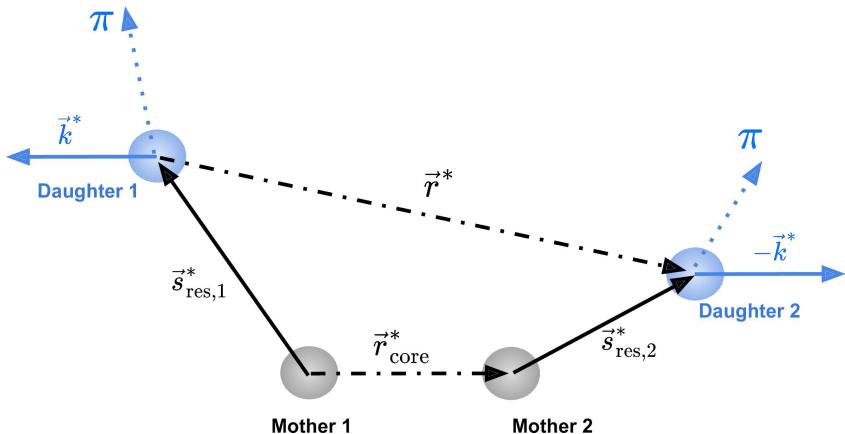
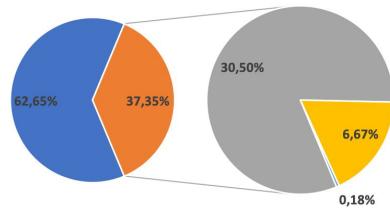
Λ s

- Primordial
- From resonances
- $\text{ct} > 2 \text{ fm}$
- $1 < \text{ct} < 2 \text{ fm}$
- $\text{ct} < 1 \text{ fm}$



Σ^0 s

- Primordial
- From resonances
- $\text{ct} > 2 \text{ fm}$
- $1 < \text{ct} < 2 \text{ fm}$
- $\text{ct} < 1 \text{ fm}$



$$s = \beta \gamma \tau_{\text{res}} = \frac{p_{\text{res}}}{M_{\text{res}}} \tau_{\text{res}}$$

$$E(r, M_{\text{res}}, \tau_{\text{res}}, p_{\text{res}}) = \frac{1}{s} \exp\left(-\frac{r}{s}\right)$$

Particle	M_{res} [MeV]	τ_{res} [fm]
p	1361.52	1.65
Λ	1462.93	4.69
Σ^0	1581.73	4.28



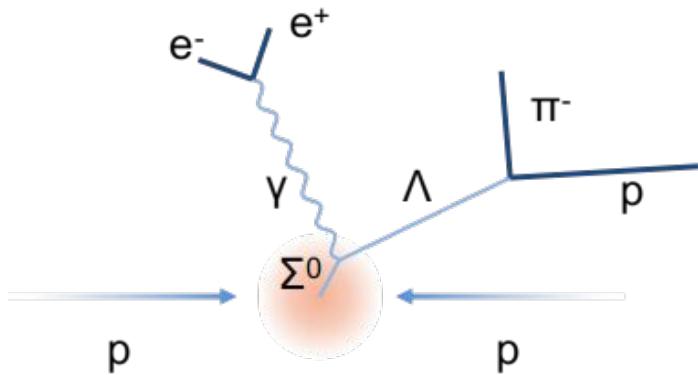
Reconstruction of Σ

Reconstruction

- Target channel $\gamma\Lambda$ (B.R. 100%)
 - Λ identification subsequent decay into $p\pi^-$ (B.R 64%)
 - γ measurement via pair conversion (prob. 8% in ALICE central barrel)

Dataset

- ALICE Run 2 data
- High-multiplicity pp collisions at $\sqrt{s} = 13$ TeV



Reconstruction of Λ

Reconstruction

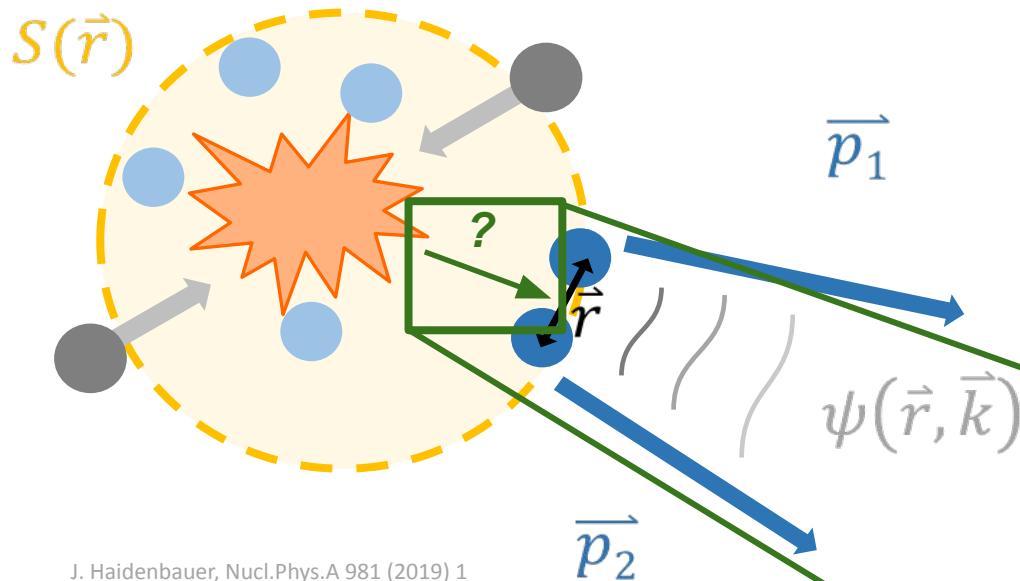
- Target channel $p\pi^-$ (B.R 64%)

Dataset

- ALICE Run 2 data
- High-multiplicity pp collisions at $\sqrt{s} = 13$ TeV



Femtoscopy: Overview Coupled-Channels (CC)



J. Haidenbauer, Nucl.Phys.A 981 (2019) 1
Y. Kamiya et al., Phys.Rev.Lett. 124 (2020) 13

'Coupled-Channels' (cc)

- Different pair with matching quantum numbers
- $\mathbf{N}-\Lambda \leftrightarrow \mathbf{N}-\Sigma$
- $\omega = 0.33$ (Iso-spin symmetry)

$$C(k^*) = \int S(\vec{r}^*) |\psi(\vec{k}^*, \vec{r}^*)| d^3\vec{r}^* + \sum_{cc} \omega_{cc} \int S_{cc}(\vec{r}^*) |\psi_{cc}(\vec{k}^*, \vec{r}^*)| d^3\vec{r}^*$$

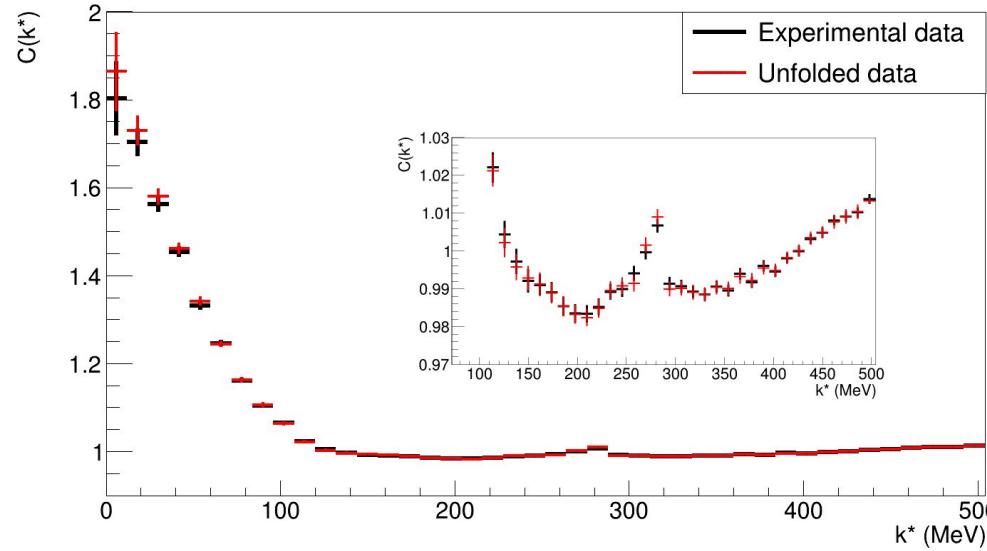


Unfolding for momentum resolution

- Motivation: more convenient representation for theorists to test their models.
- Method: **brute force**.

Each fitted correlation function (45 fit x 2 purity x 2 sideband variations, 180 in total) is unfolded by:

- Fitting the experimental correlation, by applying the smearing on the theoretical curve.
- The theory curve providing the best χ^2 is used as an initial guess for the unfolded correlation.
- The unfolded correlation is bootstrapped and folded to the exp. data, until a better χ^2 is found.
- Repeated until obtaining a $\chi^2/\text{DataPoints} < 0.2$.



Formula up-keep

$$\lambda_{\text{gen}} C_{\{\text{th,gen}(k^*)} + \lambda_{\{p\}\Sigma^0} C_{\{\text{th,p}\}\Sigma^0}(k^*) + \lambda_{\{p\}\Xi^-} C_{\{\text{th,p}\}\Xi^-}(k^*) + \dots + \lambda_{\{\text{misid}\}} C_{\{\text{th,misid}\}}(k^*) +$$
$$b(k^*)[\lambda_{\{p\}\lambda} C_{\{\text{th,p}\}\lambda}(k^*) + \lambda_{\{p\}\Sigma^0} C_{\{\text{th,p}\}\Sigma^0}(k^*) + \lambda_{\{p\}\Xi^-} C_{\{\text{th,p}\}\Xi^-}(k^*) + \lambda_{\{ff\}} + \lambda_{\{\tilde{p}\}\Lambda}]$$
$$C_{\{\text{exp}\}}(k^*) =$$
$$b(k^*)[\lambda_{\{p\}\Sigma^0} C_{\{p\}\Sigma^0}(k^*) + \lambda_{\{p\}\gamma\Lambda} C_{\{p\}\gamma\Lambda}(k^*) + \lambda_{\{ff\}} + \lambda_{\{\tilde{p}\}\Sigma^0}]$$
