



MUSEO STORICO DELLA FISICA E CENTRO STUDI E RICERCHE ENRICO FERMI

An insight of the sub-threshold KbarN interaction (a story which instructed and inspired me :)

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STRANU: Hot Topics in STRANgeness NUclear and Atomic Physics

ECT* 24-28 May 2021

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AMADEUS at LNF



TWO SAMPLES OF DATA:

2004-2005 KLOE data (Analyzed luminosity of ~2 fb⁻¹)

K⁻ absorbed in KLOE materials (H, ⁴He, ⁹Be, ¹²C) At-rest + In-flight

Dedicated 2012 run with pure graphite Carbon target inside KLOE (~90 pb⁻¹; analyzed 37 pb⁻¹, x1.5 statistics)

K^{- 12}C absorptions At-rest

DAΦNE the **Φ** factory



- $e^+ e^-$ at 510 MeV
- φ resonance decays at 49.2 % in K⁺
 K⁻ back to back pair
- Very low momentum (≈ 127 MeV) K⁻ beam
- Flux of produced kaons: about 1000/second

Best low momentum K⁻ factory in the world



Suitable for low-energy kaon physics:

 \rightarrow Kaonic atoms (SIDDHARTA-2)

→ Kaon-nucleons/nuclei interaction studies (AMADEUS)

AMADEUS



The KLOE detector

- Cylindrical drift chamber with a 4π geometry and electromagnetic calorimeter
- 96% acceptance
- optimized in the energy range of all charged particles involved
- good performance in detecting photons and neutrons checked by kloNe group [M. Anelli et al., Nucl Inst. Meth. A 581, 368 (2007)]

KLOE as active target

- DC wall (750 µm C fibre , 150 µm Al foil);
- DC gas (90% He, 10% C₄H₁₀).

K⁻ absorptions at-rest and in-flight



(e)





$K^{-}p \rightarrow \Sigma^{0} \pi^{0}$ (bound proton in ¹²C and ⁴He)



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 $\mathbf{p}_{\pi \mathbf{0}}$ resolution: $\sigma \approx 12 \text{ MeV/c}$



difficulty: epoxy resin, contained in the carbon fibre target, contains H

BUT - K⁻H interaction probability, based on K⁻ interaction AT-REST in hydrocarbons mixture data (Lett. Nuovo Cimento, C 1099 (1972)) gives max contribution order of 1% !!!



HYDROGEN contamination \rightarrow from $\Sigma^+ \pi^-$

 $K^-p \rightarrow \Sigma^+\pi^-$ detected via: $(p\pi^0) \pi^-$



measured channel: $K^{-}p \rightarrow \Sigma^{+}\pi^{-}$ (bound proton in ¹²C)

p_{_} resolution about 1MeV \rightarrow K- capture at-rest/in-flight/on H can be distinguished



Figure 3: (Colour online.) $m_{\Sigma\pi}$ invariant mass distributions in-flight (green) and at-rest (violet) in ¹²C. Blue histogram represents the sum of green and violet histograms. The red distribution refers to K^- absorptions on Hydrogen

The non-resonant production is interesting by itself

In $\Lambda\pi^-$ direct production in 4He the isospin I = 1, P-wave amplitude, dominated by the $\Sigma(1385)$ is well known -> the non-resonant I = 1, S -wave amplitude $|f^{N-R}_{\Lambda\pi}(I=1)|$ can be extracted for the first time below threshold.

IDEA - in bubble chamber experiments the reaction K^{-4} He $\rightarrow \Lambda \pi^{-3}$ He

interpreted as direct capture on a neutron with 3He being a spectator. The recoil energy of 3He indicated a low energy component due to S wave KN capture from atomic S state. Atomic experiments confirmed that due to molecular collisions the bulk of capture occurs from the high n, S states of the atom.

K. Bunnell et al., Phys. Rev. D 2, 98 (1970), D. Riley et al., Phys. Rev. D 11, 3065 (1975), J. Uretsky et al. Phys. Rev. D 2, 119 (1970), B. R. Wienke, Phys. Rev. D 1, 2514 (1970), . Suzuki et al., Mod. Phys. Lett. A 23, 2520-2523 (2008),
C. Curceanu et al., Eur. Phys. J. A 31, 537-539 (2007)

The non-resonant production is interesting by itself

IDEA - Bubble chamber experiments discovered also a higher energy component in the recoil energy spectrum, whose origin has not been understood.

$$K^{-}(n+R) \rightarrow \Lambda \pi^{-3}$$
He

(n + R) denotes the initial nucleus with the first struck neutron n singled out. The final nucleus is not assumed to be a spectator. The Λ may be formed directly or indirectly in an inelastic collision of an initially produced Σ .

The direct process may go in two basic ways:

- non-resonant isospin I=1, S-wave reaction
- resonant I=1, P-wave reaction, may be formed in atomic S-wave states as a consequence of its three body structure (K- = 1, n = 2 and R = 3).

- . Bubble chamber experiments exhibit two components:
- Low momentum $\Lambda\pi^{-}$ pair \rightarrow S-wave, I=1, non-resonant transition amplitude.
 - High momentum $\Lambda\pi^-$ pair \rightarrow P-wave resonant formation ?



$K^{-}(s=0)$ ⁴He(s=0) n(s=1/2) Σ^{*-}(s=3/2) → resonance <u>p-wave</u> only

atomic s-state capture:



• $(K^{-4}He \rightarrow \Lambda \pi^{-3}He)$ absorptions from (n s) - atomic states are assumed \rightarrow ⁴He bubble chamber data (Fetkovich, Riley interpreted by Uretsky, Wienke)

• Coordinates recupling enables for P-wave resonance formation



Direct and non-direct $\Lambda \pi^-$ production



K⁻p scattering amplitude



K⁻p scattering amplitude in Chiral calculations

Kyoto-Munich (KM)

Y. Ikeda, T. Hyodo, W. Weise, Nucl. Phys. A 881 (2012) 98

• Murcia (MI, MII)

Z. H. Guo, J. A. Oller, Phys. Rev. C 87 (2013) 035202

• Bonn (B2, B4)

M. Mai, U.-G. Meißner - Eur. Phys. J. A 51 (2015) 30

• Prague (P)

A. Cieply, J. Smejkal, Nucl. Phys. A 881 (2012) 115

• Barcelona (BCN)

A. Feijoo, V. Magas, À. Ramos, Phys. Rev. C 99 (2019) 035211

[from A. Cieply talk at MENU2019 conference]

Experimental constraints at KN threshold



K⁻p scattering amplitude



K⁻p scattering amplitude in Chiral calculations

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Large discrepancies in the region below threshold!

[from A. Cieply talk at MENU2019 conference]

K⁻n scattering amplitude



K⁻n scattering amplitude (s-wave .. non resonant) in chiral calculations

Even larger spread in I=1 channel

Experimental information was missing:

- SIDDHARTA-2 → first experimental constraint at threshold
- AMADEUS → we could already give information below threshold

Experimental constraints below threshold



K⁻n scattering amplitude with Chiral models

Large spread in I=1 channel

Experimental information was missing:

- SIDDHARTA-2 → first experimental constraint at threshold
- AMADEUS \rightarrow First determination of the non-resonant (s-wave) transition amplitude below threshold Investigated using: K^{-} "n" $\rightarrow \Lambda \pi^{-}$ to extract $|f^{N-R}_{\Lambda \pi}(I=1)|$ with bound neutron in ⁴He

The kinetic energy in the K⁻n CM system is: $E_{\rm Kn} \sim -B_n - \boxed{<\frac{p_{\Lambda\pi}^2}{2\mu_{\pi,\Lambda,3\rm He}}>} \qquad \begin{array}{c} {\rm recoil\ energy\ of\ the\ \Lambda\pi^-\ pair\ with} \\ {\rm respect\ to\ the\ residual} \\ \end{array}$ $B_n = 21\ {\rm MeV} \qquad <p_3^2/2\mu_{12,3}>\simeq 12\ {\rm MeV}$

see also

A. Cieply et al., Phys. Lett. B 702 (2011) 402, T. Hoshino et al., Phys. Rev. C 96 (2017) 045204 N. Barnea, E. Friedman, A. Gal, Nucl. Phys. A968 (2017)



so we are testing the interaction about 33 MeV below the KbarN threshold. The interaction is very short range (off shell dependence on relative momenta is neglected)

$$t_{Kn\to\Lambda\pi}(E_{Kn}) \equiv f^s$$

is a free parameter to be extracted by comparison of predicted and measured momentum probability distributions.

- The sub-threshold result can help to better determine the I=1 $\Sigma \pi$ background
- the modulus of the s-wave K⁻n -> Λπ⁻ amplitude below threshold can be used to constraint models of s-wave interaction,
- the subthreshold result is to be compared with the corresponding values extracted from experimental $K^- p \rightarrow \Lambda \pi^0$ cross section measurements above the threshold: J. K. Kim, Phys. Rev. Lett. 19, 1074 (1967).

J. K. Kim, Columbia University report, Nevis, 149 (1966).

Table 1: The $K^-n \to \Lambda \pi^-$, S-Wave amplitude, $|f^s| fm$ extracted from $K^-p \to \Lambda \pi^0$ scattering [18, 19].

E = -33 MeV	$p_{lab} = 120 MeV/c$	160	200	245
to be determined	0.33(11)	0.29(10)	0.24 (6)	0.28(2)

the amplitude is weakly energy dependent and downward extrapolation by 55 MeV is of interest.

Fit of the $p_{\Lambda\pi^-}$ observed distribution ($p_{\Lambda\pi^-}$ resolution about 2 Mev) using calculated distributions :

$$P_s^s(p_{\Lambda\pi}) = |\Psi_N(p_{\Lambda\pi})|^2 |f^s(p_{\Lambda\pi})|^2 \rho$$
 non-resonant

$$\mathsf{P}_{\mathsf{s}}^{\mathsf{p}}(\mathsf{p}_{\Lambda\pi}) = |\Psi_{\mathsf{N}}(\mathsf{p}_{\Lambda\pi})|^2 \mathsf{c}^2 |2\mathsf{f}^{\Sigma^*}(\mathsf{p}_{\Lambda\pi})|^2 \rho/3 (\mathsf{kp}_{\Lambda\pi})^2$$
 resonant

Where $\rho = k p_{\Lambda \pi}^{2}$, $c = M_{\kappa}/(M_{\kappa}+M_{n}) = 0.345$ re-couples the S x S waves to P x P waves

To determine
$$|f^{N-R}_{\Lambda\pi}|$$
 given the fairly well known $|f^{\Sigma^*}_{\Lambda\pi}|$

Calculated $\mathbf{p}_{\Lambda\pi-}$ probability distributions



Λ(1116) identification

<u>1st Step</u>: $\Lambda \rightarrow p + \pi^{-}$ reconstruction (BR = 63.9 ± 0.5 %)



$K^{-4}He \rightarrow \Lambda \pi^{-3}He \dots calculated reactions$

Calculated primary hadronic interactions:



$K^{-4}He \rightarrow \Lambda \pi^{-3}He$ events selection



. CUT based on MC simulations used to select $\Lambda\pi^-$ direct production events

- . At-rest CAN NOT be separated from In-flight \rightarrow global fit performed
- Background sources: $\Lambda\pi^-$ events from $\Sigma p/n \rightarrow \Lambda p/n$ conversion

- $\Lambda\pi^-$ events from K⁻¹²C absorptions in Isobutane

Main Background due to Inelastic FSI :

-

- also Λ can follow a primary Σ^0 decay

 contribution of elastic FSI rescattering of Λ or π⁻ on the residual is found to introduce global 3% correction on the amplitude modulus

All the involved non-direct production processes were calculated and introduced in KLOE MC simulation:



contamination of the $\Lambda \pi^-$ sample due to events from K⁻¹²C absorptions in Isobutane (90% He, 10% C₄H₁₀):

- K^{- 12}C DATA in the KLOE DC wall are used
- estimated contribution:

$$\frac{N_{\mathrm{K}^{-4}\mathrm{He}}}{N_{\mathrm{K}^{-12}\mathrm{C}}} = \frac{n_{^{4}\mathrm{He}}\sigma_{\mathrm{K}^{-4}\mathrm{He}}\mathrm{BR}_{\mathrm{K}^{-4}\mathrm{He}}(\Lambda\pi^{-})}{n_{^{12}\mathrm{C}}\sigma_{\mathrm{K}^{-12}\mathrm{C}}\mathrm{BR}_{\mathrm{K}^{-12}\mathrm{C}}(\Lambda\pi^{-})}$$

$$\%(K^{-12}C) = 0.44 \pm 0.13$$

- Λ and π^- momentum resolutions checked for this sample to be comparable with the the gas sample
- uncertainty introduced by the geometric vertex cut considered in the systematic

Fit of the measured distributions

Strategy of the analysis: compare the measured rate of the resonant over non resonant $\Lambda\pi^{-}$ production to the theoretical prediction, from which to extract the modulus of the non resonant amplitude below threshold, exploiting K- absorption on a bound neutron

K⁻"n" ³He → Λπ^{- 3}He

how much below the threshold?

$$E_{
m Kn} \sim -B_n - < rac{p_{\Lambda\pi}^2}{2\mu_{\pi,\Lambda,3
m He}} > 1$$

 33 ± 6 MeV below threshold

see also

A. Cieply et al., Phys. Lett. B 702 (2011) 402, T. Hoshino et al., Phys. Rev. C 96 (2017) 045204 N. Barnea, E. Friedman, A. Gal, Nucl. Phys. A968 (2017)

Fit of the measured distributions

The $p_{\Lambda\pi}$, $m_{\Lambda\pi}$ and $\cos(\theta_{\Lambda\pi})$ measured spectra are fitted simultaneously with the following contributions:

- non-resonant K⁻ capture at-rest from atomic S states in ⁴He,
- resonant K^- capture at-rest from atomic S states in ⁴He,
- non-resonant K⁻ capture in-flight in ⁴He,
- resonant K⁻ capture in-flight in ⁴He,
- primary $\Sigma \pi^-$ production followed by the $\Sigma N \to \Lambda N'$ conversion process,
- K⁻ capture processes in ¹²C giving rise to $\Lambda\pi^-$ in the final state.

We also confirmed the contribution of the K- captures at-rest from atomic P states to be negligibly small.

Simultaneous fit : $p_{\Lambda\pi^-} - m_{\Lambda\pi^-} - \cos\theta_{\Lambda\pi^-}$



Results of the analysis

/c ²	350	-Non Re	conant At D	oot					81			1
e<	300 <u></u>	- Resona	ant At-Rest	551					Channels	Ratio/yield	$\sigma_{\rm stat}$	$\sigma_{\rm syst}$
Σ	250	-Non-Re	sonant In-Fl	aht			$++^{++}$		RES-ar/NR-ar	0.39	± 0.04	$^{+0.18}_{-0.07}$
10	200	Resona	Int In-Flight					4	RES-if/NR-if	0.23	± 0.03	$^{+0.23}_{-0.22}$
nts	150Ē	$-\!\!-\!\!\!-\Sigma N \to$	Λ N' internal	conversion		4	Ť		NR-ar	12.0 %	± 1.7 %	$^{+2.0}_{-2.8}$ %
no	100	-K abso	rption in Car	bon		+ +++	~		NR-if	19.2 %	± 4.4 %	$^{+5.9}_{-3.3}$ %
0						+			$\Sigma \to \Lambda$ conv.	2.2 %	± 0.3 %	$^{+1.6}_{-0.8}~\%$
	50들				-				K^{-12} C capture	57.0 %	\pm 1.2 $\%$	$^{+2.2}_{-3.2}$ %
	1980	1300	1320	13/0	1360	1380	1/00	1/20				
	1200	1000	1520	1040	1000	1000	m.	(MeV/c^2)				
							··· ^ 7					

Results of the analysis

$$\frac{\mathrm{NR} - \mathrm{ar}}{\mathrm{RES} - \mathrm{ar}} = \frac{\int_{0}^{pmax} P_{ar}^{nr}(p_{\Lambda\pi}) \, dp_{\Lambda\pi}}{\int_{0}^{pmax} P_{ar}^{res}(p_{\Lambda\pi}) \, dp_{\Lambda\pi}} =$$

$$= |f_{ar}^{nr}|^2 \cdot 8.94 \cdot 10^5 \mathrm{MeV^2}$$

 $|f_{ar}^{nr}| = (0.334 \pm 0.018 \operatorname{stat}_{-0.058}^{+0.034} \operatorname{syst}) \operatorname{fm}$

E = -33 MeV	$0.334 \pm 0.018 \mathrm{stat}^{+0.034}_{-0.058} \mathrm{syst}$
$p_{lab} = 120~{\rm MeV}$	0.33 ± 0.11
$p_{lab} = 160~{\rm MeV}$	0.29 ± 0.10
$p_{lab} = 200 \text{ MeV}$	0.24 ± 0.06
$p_{lab}=245~{\rm MeV}$	0.28 ± 0.02

To be compared with the corresponding values extracted from cross section measurements

TABLE II. The S-wave non-resonant amplitude $(|f^{nr}| \text{ fm})$ extracted from $K^-p \rightarrow \Lambda \pi^0$ scattering [34, 35] and from this experiment (E = -33 MeV).

J. K. Kim, Columbia University Report, Nevis 149 (1966) J. K. Kim, Phys. Rev. Lett. 19 (1977) 1074

[K. P., S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345] [K. P., S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

Results of the analysis



Comparison with theoretically predicted real and imaginary parts of the non resonant, coupled channels, $K^-n \rightarrow \Lambda \pi / \Sigma \pi$ scattering amplitudes:

- for each model $|A_{K-n}|$ is calculated at 33 MeV below the KbarN threshold
- $|A_{K-n \to \Lambda \pi^-}|$ is extracted from $|A_{K-n}|$ by calculating the probability ratios:

$$\frac{Prob_{K^-n\to\Lambda\pi^-}}{Prob_{K^-n\to\Sigma^-\pi^0}} = \frac{Ph_{K^-n\to\Lambda\pi^-}}{c_1Ph_{K^-n\to\Sigma^-\pi^0}}$$

$$\frac{Prob_{K^-n\to\Lambda\pi^-}}{Prob_{K^-n\to\Sigma^0\pi^-}} = \frac{Ph_{K^-n\to\Lambda\pi^-}}{c_2Ph_{K^-n\to\Sigma^0\pi^-}}$$

With gratitude,

and the wish this story will continue long



measured channel: $K^{-} p \rightarrow \Sigma^{0} \pi^{0}$ (bound proton in ¹²C)

for the extraction of the $\Lambda(1405)$ shape

Λ(1116) identification

<u>1st Step</u>: $\Lambda \rightarrow p + \pi^{-}$ reconstruction (BR = 63.9 ± 0.5 %)

