

# On a quasi-bound state in the $K^-np$ system caused by strong interactions

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Interest to antikaon-nucleon systems: quasi-bound state in the  $K^-pp$  system

[*Y.Akaishi, T.Yamazaki, Phys.Rev.C65, 044005 (2002)*]

→ experimental and theoretical efforts with different results

**Our contribution:** series of dynamically exact calculations of three-body antikaon-nucleon systems

- Quasi-bound states in  $\bar{K}NN$ , spin 0 ( $K^-pp/\bar{K}^0np$ ) and  $\bar{K}\bar{K}N$  systems - binding energy and width
- No quasi-bound state in  $\bar{K}NN$ , spin 1 ( $K^-np/\bar{K}^0nn$ ) - proven
- Near-threshold scattering in  $\bar{K}NN$ , spin 1 ( $K^-d$ ) (Faddeev-type AGS equations with coupled  $\bar{K}NN - \pi\Sigma N$  channels)
- 1s level shift and width of kaoninic deuterium (Faddeev-type equations with directly included Coulomb interaction)

[*N. V. S., Three-Body Antikaon-Nucleon Systems, Few Body Syst. 58, 6 (2017)*]

## "Strong" quasi-bound state in $K^-np$ - previous results

No quasi-bound state in  $\bar{K}NN$ , spin 1 ( $K^-np$ ) - proven

$K^-np$  quasi-bound state caused by strong interactions:  $\leftrightarrow$  kaonic deuterium  
(an atom, Coulomb is the main interaction, is known)

### Evidence

Faddeev calculations of the  $K^-d$  scattering length  $a_{K^-d}$  – evidence that a "strong" quasi-bound state in  $K^-np$  could exist:

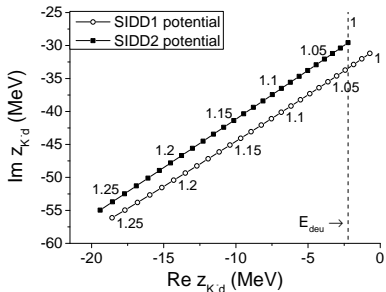
- Analytical continuation of the effective range formula below the  $K^-d$  threshold  $\rightarrow$   $K^-np$  quasi-bound state with binding energy 14.6 – 19.6 MeV, width 15.6 – 22.0 MeV **should exist**
- Systematic search for these states using three-body coupled-channel AGS equations  $\rightarrow$  **no (corresponding) poles** in the complex energy plane

The reason of discrepancy: effective range formula is valid in the vicinity of the corresponding threshold (*expected large binding energy and width - out of the validity region*)

## ”Strong” quasi-bound state in $K^-np$ - previous results

Strength constant of  $V_{\bar{K}N-\pi\Sigma}$  changed by hands:

$$\lambda_{I=0}^{\bar{K}N, \bar{K}N} \rightarrow c \lambda_{I=0}^{\bar{K}N, \bar{K}N}, \quad c = 1.25..1$$



**Fig:** Pole trajectories in the  $K^-np$  system for increasing absolute value of the  $\lambda_{I=0}^{\bar{K}\bar{K}}$  strength constant of the phenomenological  $V_{\bar{K}N-\pi\Sigma}^{1,SIDD}$  and  $V_{\bar{K}N-\pi\Sigma}^{2,SIDD}$  potentials. The numbers along the trajectories indicate the multiplication factors. Quasi-bound states are the poles to the left of the  $K^-d$  threshold.

Next step – **four-body calculations** of the  $\bar{K}NNN$  system using Faddeev-type equations. New  $NN$  potential constructed and used ( $V_{NN}$  by *P. Doleschall* was used before) → **quasi-bound state in the  $K^-np$  subsystem caused by strong interactions** was found

## Two-term Separable New potential (TSN) of nucleon-nucleon interaction

$$V_{NN}^{\text{TSN}}(k, k') = \sum_{m=1}^2 g_m(k) \lambda_m g_m(k'),$$

$$g_m(k) = \sum_{n=1}^3 \frac{\gamma_{mn}}{(\beta_{mn})^2 + k^2}, \quad \text{for } m = 1, 2$$

fitted to Argonne V18 potential [*R.B. Wiringa, V.G.J. Stoks, R. Schiavilla, Phys. Rev. C 51, 38 (1995)*] phase shifts

Triplet and singlet scattering lengths  $a$  and effective ranges  $r_{\text{eff}}$

$$a_{np}^{\text{TSN}} = -5.400 \text{ fm}, \quad r_{\text{eff}, np}^{\text{TSN}} = 1.744 \text{ fm}$$

$$a_{pp}^{\text{TSN}} = 16.325 \text{ fm}, \quad r_{\text{eff}, pp}^{\text{TSN}} = 2.792 \text{ fm},$$

deuteron binding energy  $E_{\text{deu}} = 2.2246 \text{ MeV}$ .

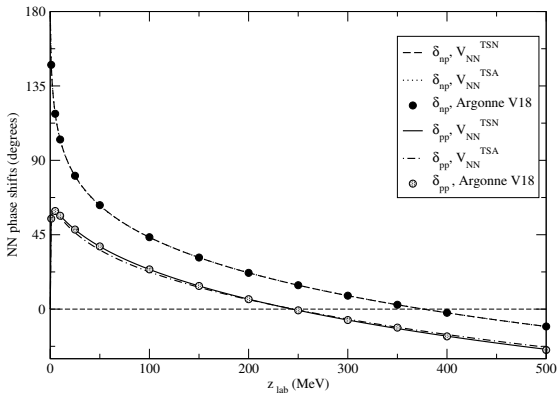


Fig: Phase shifts of  $np$  and  $pp$  scattering calculated using the new  $V_{NN}^{TSN}$  and  $V_{NN}^{TSA-B}$  potentials plus phase shifts of Argonne V18

## Antikaon-nucleon interaction

### Three potentials

- phenomenological  $\bar{K}N - \pi\Sigma$  with **one-pole**  $\Lambda(1405)$  resonance
- phenomenological  $\bar{K}N - \pi\Sigma$  with **two-pole**  $\Lambda(1405)$  resonance
- chirally motivated  $\bar{K}N - \pi\Sigma - \pi\Lambda$  potential, **two-pole**  $\Lambda(1405)$

reproduce (with the same level of accuracy):

- 1s level shift and width of kaonic hydrogen (*SIDDHARTA*)  
**direct inclusion of Coulomb interaction, no Deser-type formula used**
- Cross-sections of  $K^-p \rightarrow K^-p$  and  $K^-p \rightarrow MB$  reactions
- Threshold branching ratios  $\gamma$ ,  $R_c$  and  $R_n$
- $\Lambda(1405)$  resonance (*one- or two-pole structure*)  
 $M_{\Lambda(1405)}^{PDG} = 1405.1_{-1.0}^{+1.3}$  MeV,  $\Gamma_{\Lambda(1405)}^{PDG} = 50.5 \pm 2.0$  MeV [*PDG (2016)*]



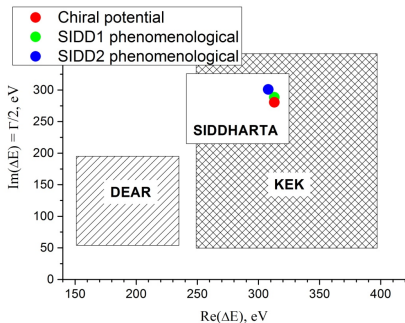


Fig: Experimental and theoretical 1s level shift and width of kaonic hydrogen given by the three  $\bar{K}N$  potentials

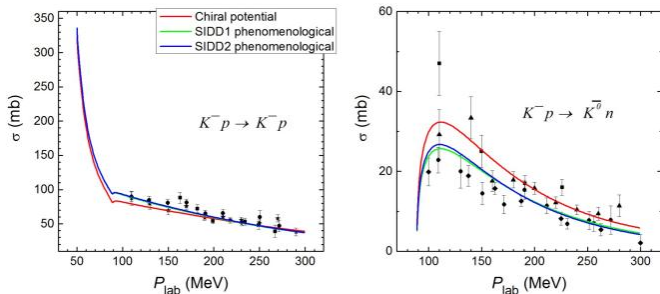
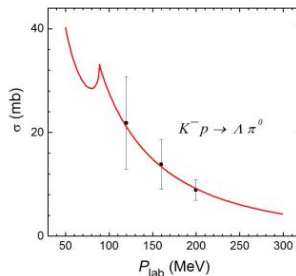
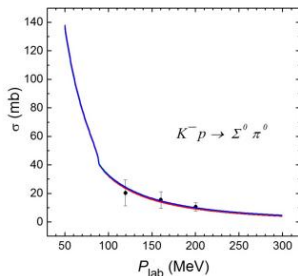
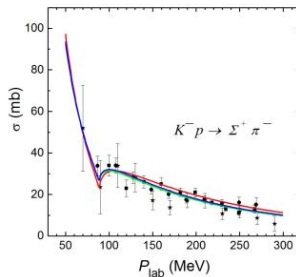
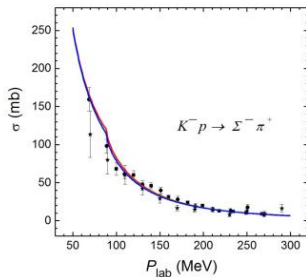


Fig: Comparison with the experimental data on  $K^-p$  cross-sections (phenomenological and chirally motivated potentials)

# $K^-p$ cross-sections: theory vs. experiment



**Table:** Strong poles ( $\Lambda(1405)$ ) given by the three antikaon-nucleon potentials (MeV)

	$z_{\text{pole1}}$	$z_{\text{pole2}}$
$V_{\bar{K}N}^{1,\text{SIDD}}$	$1426 - i 48$	—
$V_{\bar{K}N}^{2,\text{SIDD}}$	$1414 - i 58$	$1386 - i 104$
$V_{\bar{K}N}^{\text{Chiral}}$	$1417 - i 33$	$1406 - i 89$

”Experimental” value:

$$M_{\Lambda(1405)}^{PDG} = 1405.1_{-1.0}^{+1.3} \text{ MeV}, \Gamma_{\Lambda(1405)}^{PDG} = 50.5 \pm 2.0 \text{ MeV}$$

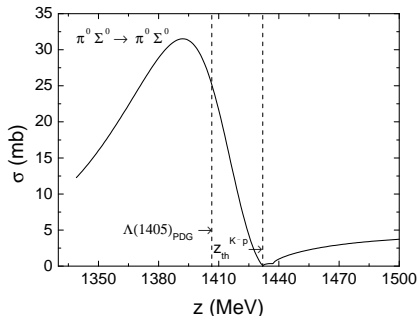


Fig: Elastic  $\pi^0 \Sigma^0$  cross-sections of the chirally motivated potential  $V_{\bar{K}N}^{Chiral}$  –  $\Lambda(1405)$  resonance.

Three-body Faddeev-type Alt-Grassberger-Sandhas equations,  
solved separately

$$U_{ij}^{\alpha\beta} = \delta_{\alpha\beta} (1 - \delta_{ij}) (G_0^\alpha)^{-1} + \sum_{k,\gamma=1}^3 (1 - \delta_{ik}) T_k^{\alpha\gamma} G_0^\gamma U_{kj}^{\gamma\beta}, \quad i, j = 1, 2, 3,$$

particle channels:

$$\alpha = 1 : |\bar{K}_1 N_2 N_3\rangle, \alpha = 2 : |\pi_1 \Sigma_2 N_3\rangle, \alpha = 3 : |\pi_1 N_2 \Sigma_3\rangle$$

Input: two-body  $T$ -matrices, corresponding to  $V_{\bar{K}N-\pi\Sigma(-\pi\Lambda)}$  (three versions),  $V_{NN}^{\text{TSN}}$  (new),  $V_{\Sigma N(-\Lambda N)}$  (isospin-dependent and spin-independent, parameters fitted to experimental cross-sections)

Quantum numbers:

spin  $S = 1$ , orbital momentum  $L = 0$ , isospin  $I = 1/2$ :

- $\bar{K}NN$  system with  $J^\pi = 1^-$  (isospin representation)
- $K^- np / \bar{K}^0 nn$  system (particle representation)

## Results: $K^-np$ quasi-bound state

**Table:** Binding energy  $B_{K^-np}$  (MeV) and width  $\Gamma_{K^-np}$  (MeV) of the quasi-bound state in the  $K^-pn$  system: coupled-channel  $\bar{K}NN - \pi\Sigma N$  calculation and one-channel  $\bar{K}NN$  with exact optical  $V_{\bar{K}N}^{\text{Opt}}$ ;

$$z_{th,K-d} = m_{\bar{K}} + 2m_N + E_{\text{deu}}.$$

	Coupled-channels calculation		With exact optical $\bar{K}N$ potential	
	$B_{K^-np}$	$\Gamma_{K^-np}$	$B_{K^-np}$	$\Gamma_{K^-np}$
$V_{\bar{K}N}^{1,\text{SIDD}}$	—	—	0.8	68.3
$V_{\bar{K}N}^{2,\text{SIDD}}$	0.9	59.4	3.8	63.2
$V_{\bar{K}N}^{\text{Chiral}}$	1.3	41.8	0.9	43.6

[N. V. S., *Few Body Syst.* 61, 27 (2020)]

**Table:** Binding energy  $B_{K^-pp}$  (MeV) and width  $\Gamma_{K^-pp}$  (MeV) of the quasi-bound state in the  $K^-pp$  system: coupled-channel  $\bar{K}NN - \pi\Sigma N$  calculation and one-channel  $\bar{K}NN$  with exact optical  $V_{\bar{K}N}^{\text{Opt}}$ ;

$$z_{th, K^-pp} = m_{\bar{K}} + 2m_N.$$

	Coupled channels calculation		With exact optical $\bar{K}N$ potential		Our previous coupled-channel results	
	$B_{K^-pp}$	$\Gamma_{K^-pp}$	$B_{K^-pp}$	$\Gamma_{K^-pp}$	$B_{K^-pp}$	$\Gamma_{K^-pp}$
$V_{\bar{K}N}^{1,\text{SIDD}}$	52.18	67.1	53.29	63.3	53.29	64.9
$V_{\bar{K}N}^{2,\text{SIDD}}$	46.56	51.2	46.65	47.4	47.45	49.8
$V_{\bar{K}N}^{\text{Chiral}}$	29.43	46.4	30.01	46.6	32.24	48.6



## Summary

- quasi-bound  $K^-np$  state caused by strong interactions was predicted, its binding energy is small (1 – 2 MeV), while the width (40 – 60 MeV) is comparable with the width of the  $K^-pp$  quasi-bound state
- the particular model of  $V_{NN}$  plays a minor role in the  $K^-pp$  system
- the same is true for the  $K^-np$  system, but since the quasi-bound state there is situated so close to the threshold,  $V_{NN}$  can resolve the question of the  $K^-np$  quasi-bound state existence
- the quasi-bound  $K^-np$  state caused by strong interactions is stronger bound and is much broader than kaonic deuterium, therefore, the atomic and the strong quasi-bound states cannot be misidentified