

# Physics interplay between FCC-ee & FCC-hh (with a focus on QCD & Higgs)

LFC21 Strong Interactions from QCD  
to New Strong Dynamics at LHC  
& Future Colliders

ECT\* Trento, Sept 2021



**David d'Enterria (CERN)**

# Open questions in the SM (1)

$$\mathcal{L} = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}tr(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) - \frac{1}{2}tr(\mathbf{G}_{\mu\nu}\mathbf{G}^{\mu\nu}) \quad [\text{Gauge interactions: U(1}_Y, \text{SU(2}_L, \text{SU(3}_c)]$$

$$+(\bar{\nu}_L, \bar{e}_L) \tilde{\sigma}^\mu iD_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} + \bar{e}_R \sigma^\mu iD_\mu e_R + \bar{\nu}_R \sigma^\mu iD_\mu \nu_R + (\text{h.c.}) \quad [\text{Lepton dynamics}]$$

$$-\frac{\sqrt{2}}{v} \left[ (\bar{\nu}_L, \bar{e}_L) \phi M^e e_R + \bar{e}_R \bar{M}^e \bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \right] - \frac{\sqrt{2}}{v} \left[ (-\bar{e}_L, \bar{\nu}_L) \phi^* M^\nu \nu_R + \bar{\nu}_R \bar{M}^\nu \phi^T \begin{pmatrix} -e_L \\ \nu_L \end{pmatrix} \right] \quad [\text{Lepton masses}]$$

$$+(\bar{u}_L, \bar{d}_L) \tilde{\sigma}^\mu iD_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} + \bar{u}_R \sigma^\mu iD_\mu u_R + \bar{d}_R \sigma^\mu iD_\mu d_R + (\text{h.c.}) \quad [\text{Quark dynamics}]$$

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$$+\overline{(D_\mu \phi)} D^\mu \phi - m_h^2 [\bar{\phi} \phi - v^2/2]^2 / 2v^2. \quad [\text{Higgs dynamics \& mass}]$$

✗ Light masses: Higgs Yukawa mechanism for lightest fermions (q,e) unproven  
 Type of Higgs coupling to Dirac/Majorana ν's?

# Open questions in the SM (2)

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$$-\frac{\sqrt{2}}{v} \left[ (\bar{u}_L, \bar{d}_L) \phi M^d d_R + \bar{d}_R \bar{M}^d \bar{\phi} \begin{pmatrix} u_L \\ d_L \end{pmatrix} \right] - \frac{\sqrt{2}}{v} \left[ (-\bar{d}_L, \bar{u}_L) \phi^* M^u u_R + \bar{u}_R \bar{M}^u \phi^T \begin{pmatrix} -d_L \\ u_L \end{pmatrix} \right] \quad [\text{Quark masses}]$$

$$+\overline{(D_\mu \phi)} D^\mu \phi - m_h^2 [\bar{\phi} \phi - v^2/2]^2 / 2v^2. \quad [\text{Higgs dynamics \& mass}]$$

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 & - \frac{\sqrt{2}}{v} \left[ (\bar{\nu}_L, \bar{e}_L) \phi M^e e_R + \bar{e}_R \bar{M}^e \bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \right] - \frac{\sqrt{2}}{v} \left[ (-\bar{e}_L, \bar{\nu}_L) \phi^* M^\nu \nu_R + \bar{\nu}_R \bar{M}^\nu \phi^T \begin{pmatrix} -e_L \\ \nu_L \end{pmatrix} \right] & [\text{Lepton masses}] \\
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 & + \overline{(D_\mu \phi)} D^\mu \phi - m_h^2 [\bar{\phi} \phi - v^2/2]^2 / 2v^2. & [\text{Higgs dynamics & mass}]
 \end{aligned}$$

- ✖ [Light masses](#): Higgs Yukawa mechanism for lightest fermions (q,e) unproven.  
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[Lepton dynamics]

$$-\frac{\sqrt{2}}{v} \left[ (\bar{\nu}_L, \bar{e}_L) \phi M^e e_R + \bar{e}_R \bar{M}^e \bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \right] - \frac{\sqrt{2}}{v} \left[ (-\bar{e}_L, \bar{\nu}_L) \phi^* M^\nu \nu_R + \bar{\nu}_R \bar{M}^\nu \phi^T \begin{pmatrix} -e_L \\ \nu_L \end{pmatrix} \right]$$

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[Quark dynamics]

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[Higgs dyn. & mass] + new particles/symmetries ?

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Higgs should couple to any massive dark world.

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- ✗ Plus many others: Strong CP problem, dark energy, inflation,...

**Some/Most(!?) of these questions will NOT be fully answered at the LHC!**

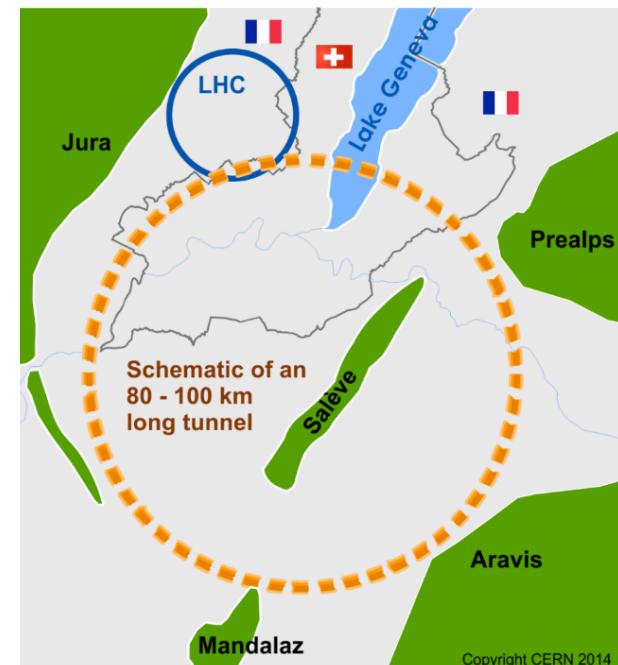
# CERN Future Circular Collider (FCC) project

- Solving those HEP fundamental problems requires new  $e^+e^-$  & pp collider:



- FCC: 100 km ring,  $Nb_3Sn$  16-T magnets, LHC used as injector:

- pp at  $\sqrt{s}=100$  TeV,  $L \sim 2 \times 10^{35}$ ,  $L_{int} = 2 \text{ ab}^{-1}/\text{yr}$   
(also pPb, PbPb at  $\sqrt{s}=39-63$  TeV)
- $e^+e^-$  before pp at  $\sqrt{s}=90-350$  GeV  
 $L_{int} \approx 5 \text{ ab}^{-1}$  Higgs factory  
~1.2 million Higgs in 3+5 years.  
Plus  $10^{12}$  Zs(!),  $10^8$  Ws(!),  $0.5 \cdot 10^6$  tops

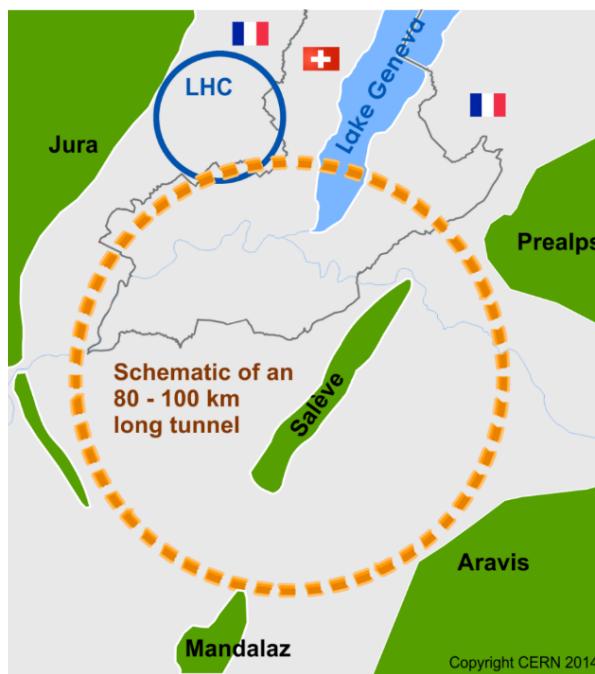
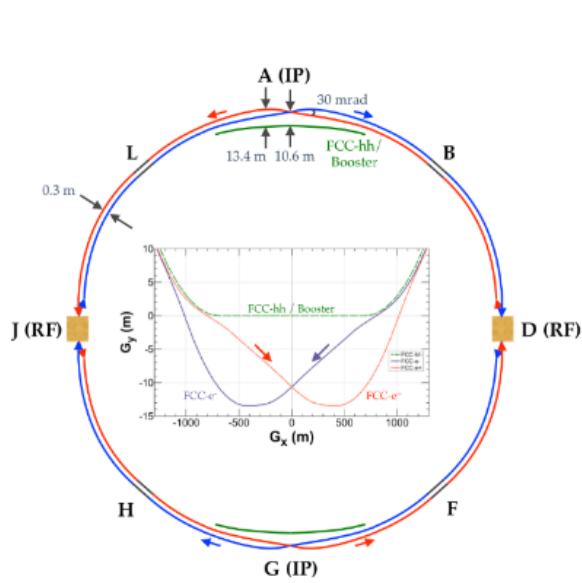


# CERN Future Circular Collider

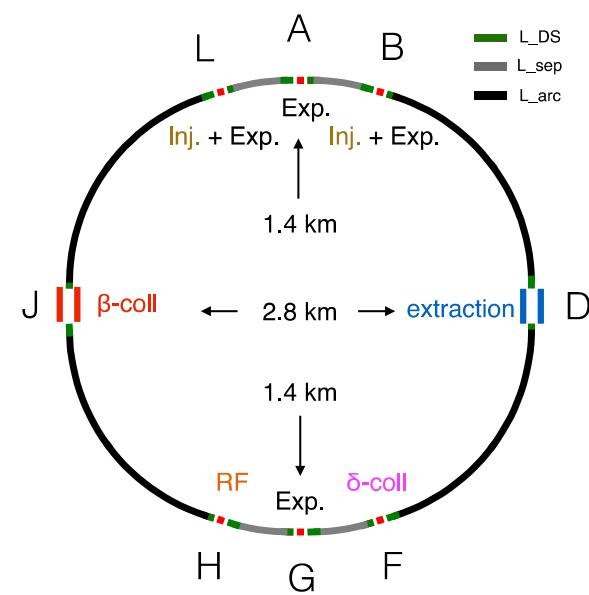
European Strategy for Particle Physics Update (2020) mandate:

*“Europe, together with its international partners, should investigate the technical and financial feasibility of a future hadron collider at CERN with a centre-of-mass energy of at least 100 TeV, and with an electron-positron Higgs and electroweak factory as a possible first stage. Such a feasibility study of the colliders and related infrastructure should be established as a global endeavour and be completed on the timescale of the next Strategy update.”*

FCC-ee



FCC-hh



# CERN Future Circular Collider

June 2021: FCC Feasibility Study (2021-2025) organization approved unanimously by CERN council.

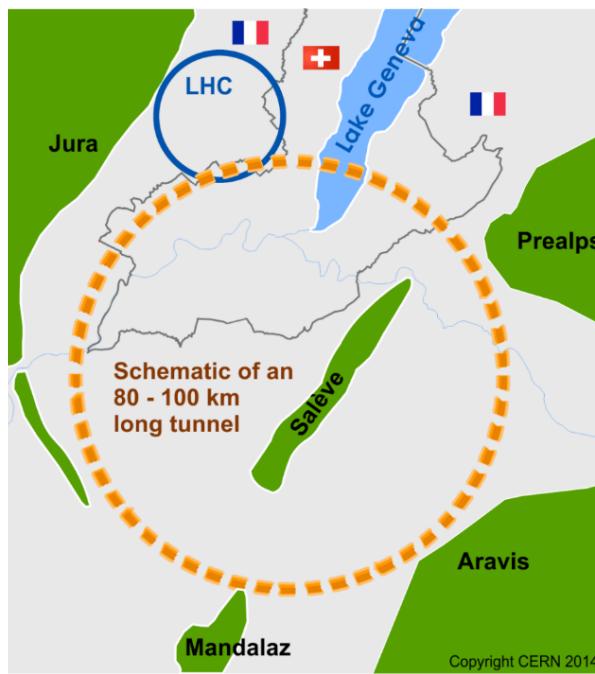
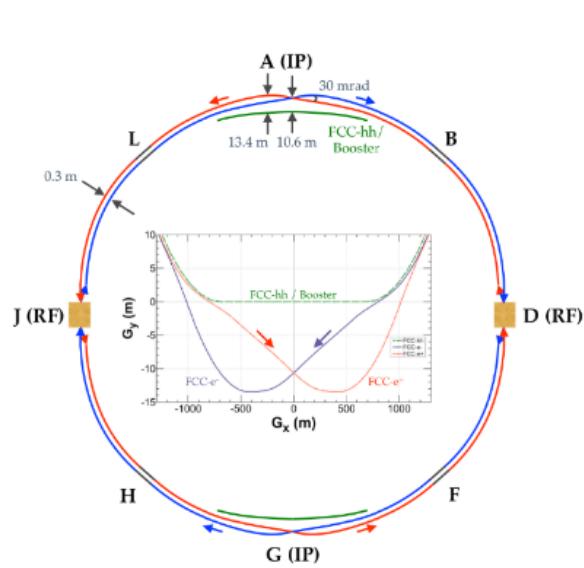
Comprehensive long-term CERN program maximizing physics opportunities:

**Stage 1 (2040–): FCC-ee (Z, W, H, tt)**: Higgs, EWK & top factory with highest luminosities.

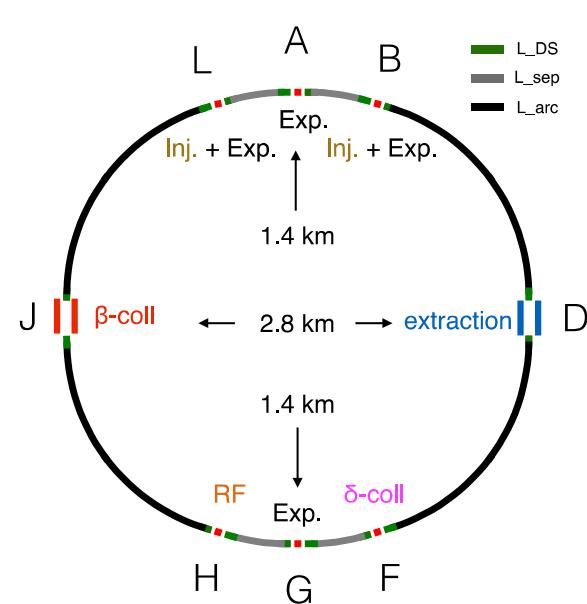
**Stage 2 (2065–): FCC-hh (~100 TeV)**: Energy frontier machine, with ion & e-h options.

- Complementary physics: Searches via **ultraprecise SM tests vs. high mass/ $p_T$  searches**
- FCC builds upon and exploits **CERN's existing lab/infrastructure/know-how**.
- **Common** tunnel, civil engineering and technical infrastructures.
- Integrated project allows **seamless HEP continuation after HL-LHC**

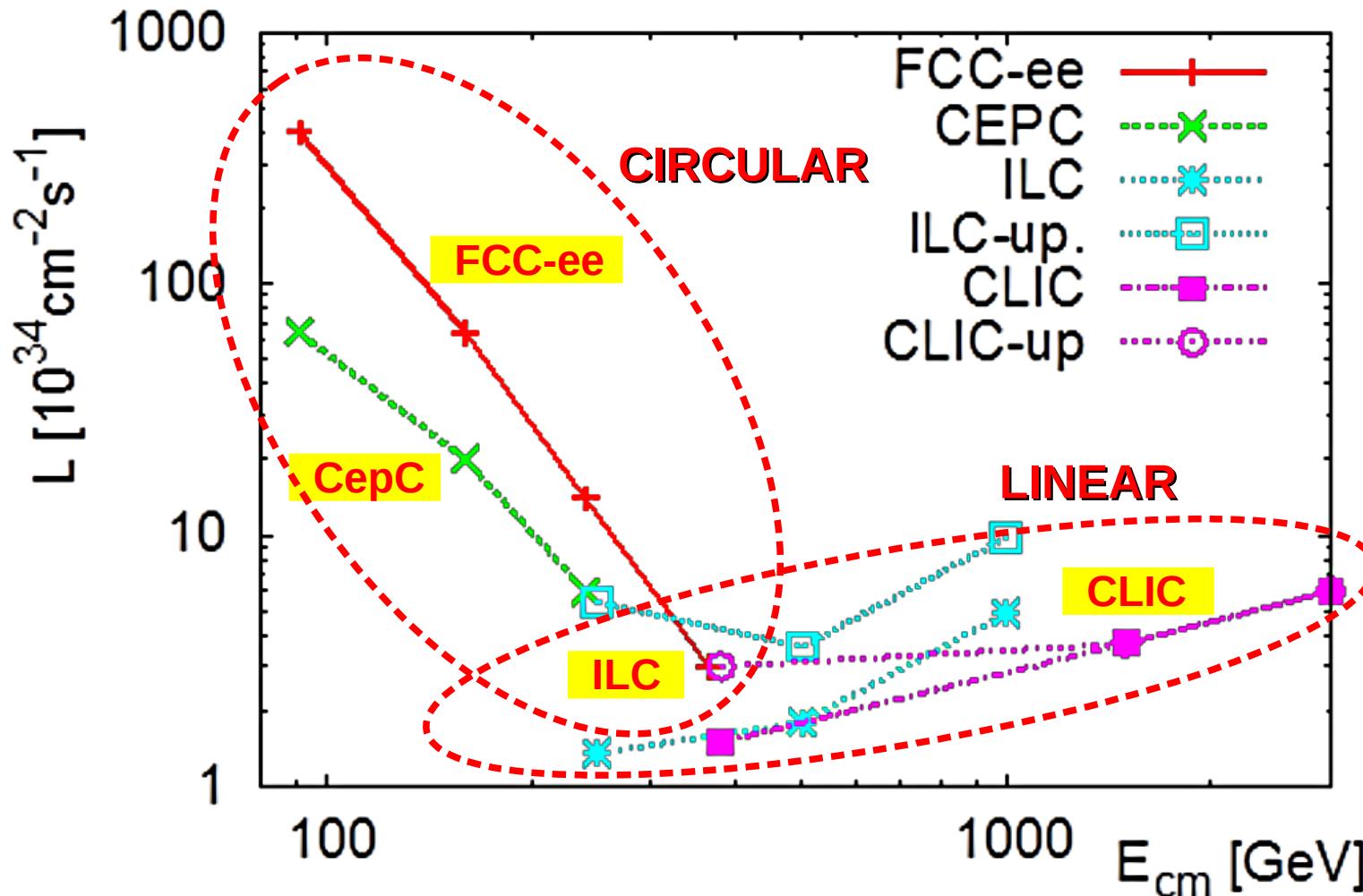
## FCC-ee



## FCC-hh



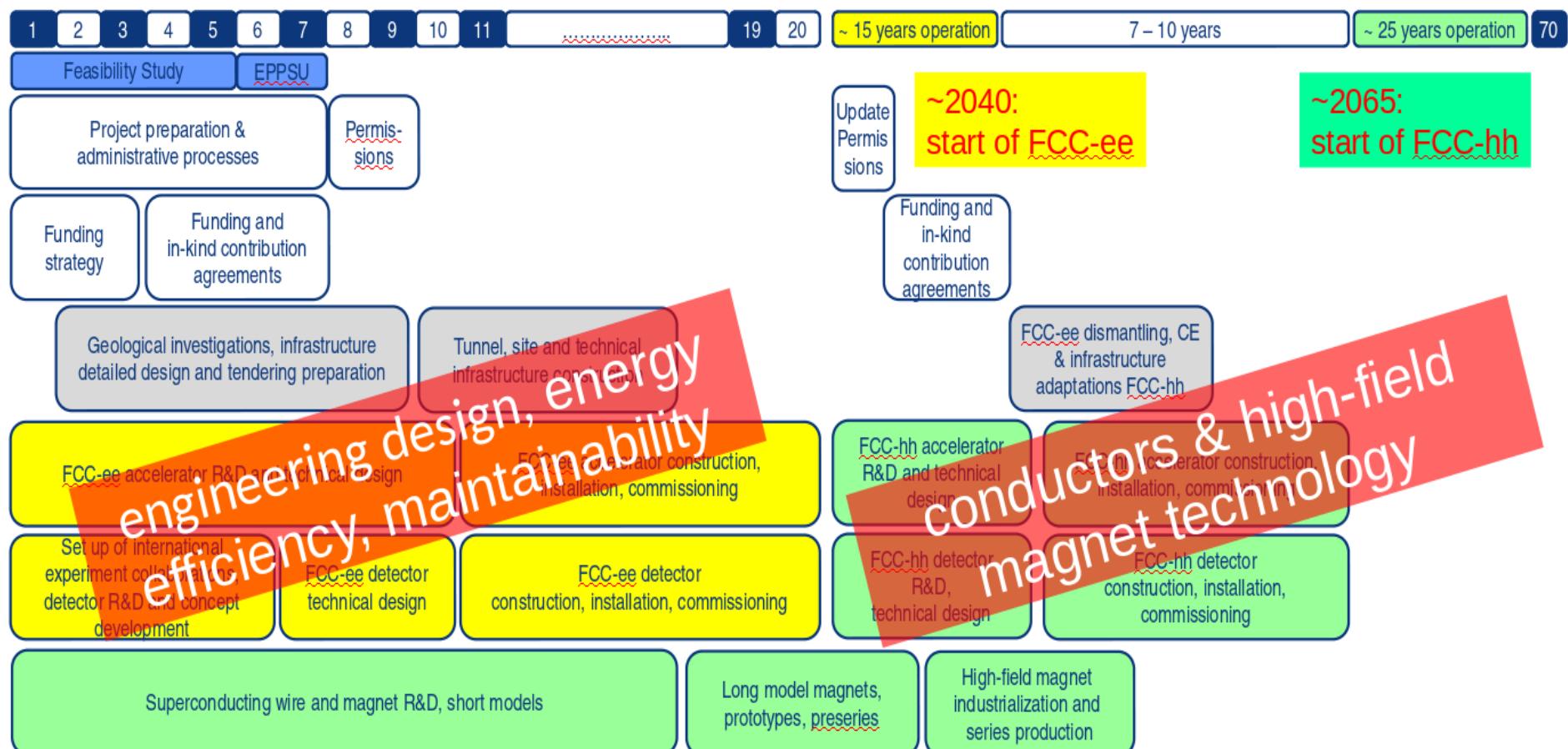
# Future $e^+e^-$ colliders luminosities



- FCC-ee features lumis a few times larger than other machines over 90–300 GeV
- FCC-ee: unparalleled Z, W, jets,  $\tau$ ,... data sets: Negligible stat. uncertainties for SM (Higgs, QCD, EWK, flavour,...) and indirect BSM studies

# CERN Future Circular Collider schedule

## ■ FCC integrated project technical schedule:



# Physics at FCC $e^+e^-$ & $pp$ machines

(1) QCD:  $\alpha_s$  coupling

(2) QCD: Parton Distribution Functions

(3) QCD: Jet substructure & flavour tagging

(4) QCD: Non-perturbative regime

(5) Higgs sector

(6) BSM searches

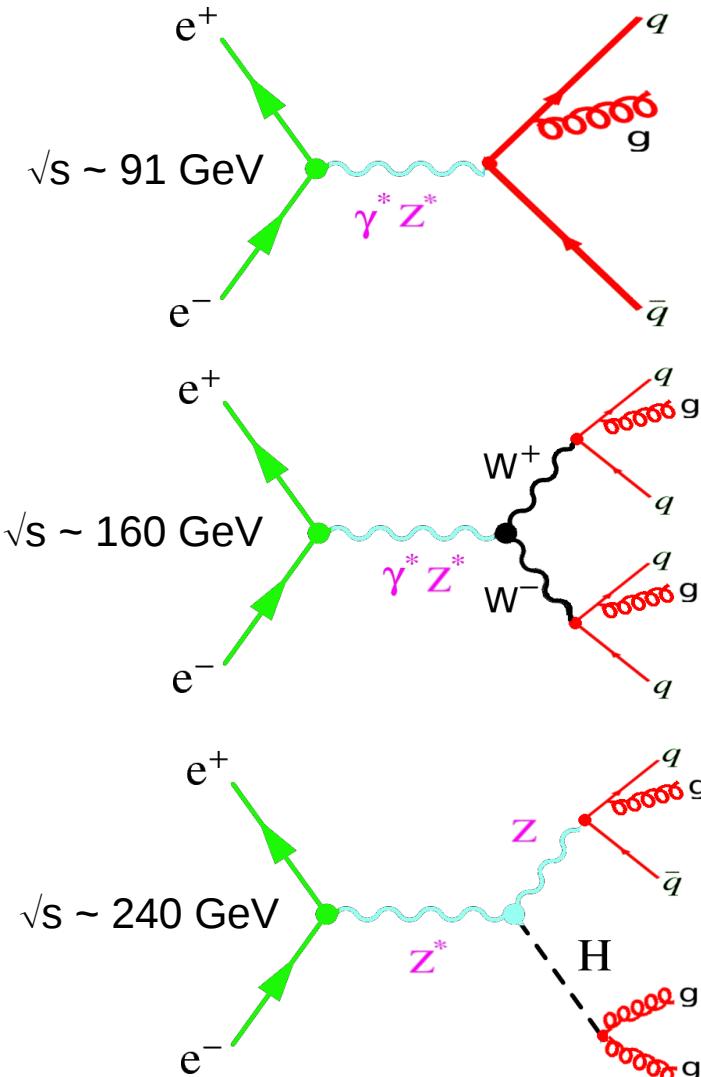
# QCD = Key piece at future ee, pp colliders

► Though QCD is *not per se* the main driving force behind future colliders, QCD is crucial for many pp, ee measurements (signals & backgrounds):

- **High-precision  $\alpha_s$** : Affects all x-sections & decays (esp. Higgs, top, EWPOs).
- **N<sup>n</sup>LO corrs., N<sup>n</sup>LL resummations**: Affects all pQCD x-sections & decays.
- **High-precision PDFs**: Affects all precision W,Z,H (**mid-x**) measurements & all searches (**high-x**) in pp collisions.
- **Heavy-Quark/Quark/Gluon separation** (jet substructure, boosted topologies..):  
Needed for all **precision SM** measurements & **BSM** searches with final jets.
- **Semihard QCD** (**low-x** gluon saturation, **multiple hard parton interactions,...**):  
Leading x-sections at FCC-pp (Note:  $Q_0 \sim 10$  GeV at 100 TeV).
- **Non-perturbative QCD**: Affects final-states with jets: **Colour reconnection**,  $e^+e^- \rightarrow Z, WW, tt\bar{t} \rightarrow 4j, 6j \dots$  ( $m_W, m_{top}$  extractions). **Parton hadronization,...**

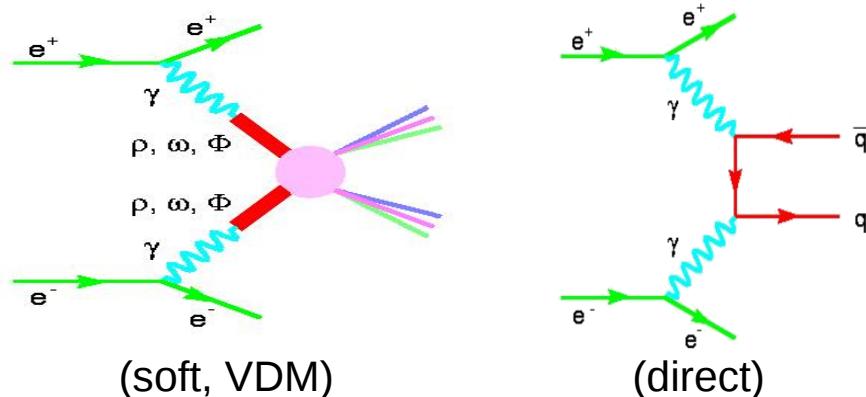
# QCD in $e^+e^-$ collisions

- $e^+e^-$  collisions provide an **extremely clean** environment with fully-controlled initial-state to very precisely probe q,g dynamics:



Advantages compared to p-p collisions:

- QED initial-state with **known kinematics**
  - **Controlled QCD radiation** (only in final-state)
  - Well-defined **heavy-Q, quark, gluon jets**
  - **Smaller non-pQCD uncertainties:**  
no PDFs, no QCD “underlying event”,...
- Direct clean parton fragmentation & hadroniz.
- Plus **QCD physics** in  $\gamma\gamma$  (EPA) collisions:



# Available QCD samples at FCC-ee

- FCC:  $e^+e^-$  at  $\sqrt{s} = 90, (125), 160, 240, 350$  GeV provides huge jets data sets



Working point	Z, years 1-2	Z, later	WW	HZ	$t\bar{t}$	(s-channel H)
$\sqrt{s}$ (GeV)	88, 91, 94		157, 163	240	340-350	365
Lumi/IP ( $10^{34} \text{ cm}^{-2} \text{s}^{-1}$ )	115	230	28	8.5	0.95	1.55
Lumi/year ( $\text{ab}^{-1}$ , 2 IP)	24	48	6	1.7	0.2	0.34
Physics goal ( $\text{ab}^{-1}$ )	150		10	5	0.2	1.5
Run time (year)	2	2	2	3	1	4
Number of events	$5 \times 10^{12}$ Z		$10^8$ WW	$10^6$ HZ + 25k WW $\rightarrow$ H	$10^6 t\bar{t}$ +200k HZ +50k WW $\rightarrow$ H	(6000)

- Approximate number of QCD jets:

# of light-q jets/year:	$\mathcal{O}(10^{12})$	$\mathcal{O}(10^7)$	$\mathcal{O}(10^5)$	-	$\mathcal{O}(10^8)_{\text{bckgds}}$
# of gluon-jets/year:	$\mathcal{O}(10^{11})$	$\mathcal{O}(10^6)$	$\mathcal{O}(10^4)$	$\mathcal{O}(10^3)$	$\mathcal{O}(10^7)_{\text{bckgds}}$
# of heavy-Q jets/yr:	$\mathcal{O}(10^{12})$	$\mathcal{O}(10^7)$	$\mathcal{O}(10^5)$	$\mathcal{O}(10^6)$	$\mathcal{O}(10^8)_{\text{bckgds}}$

# Physics at FCC $e^+e^-$ & $pp$ machines

(1) QCD:  $\alpha_s$  coupling

(2) QCD: Parton Distribution Functions

(3) QCD: Jet substructure & flavour tagging

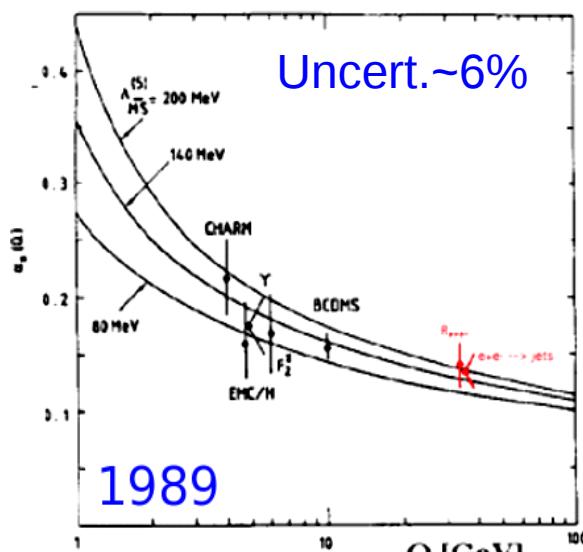
(4) QCD: Non-perturbative regime

(5) Higgs sector

(6) BSM searches

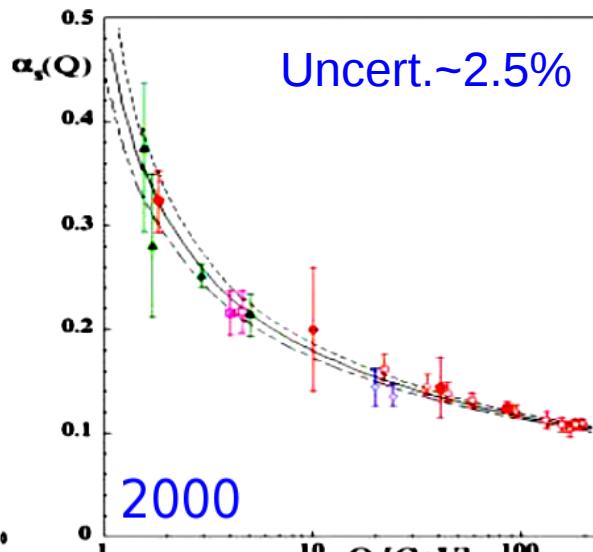
# QCD coupling $\alpha_s$

- Determines **strength of the strong interaction** between quarks & gluons.
- Single free parameter of QCD in the  $m_q \rightarrow 0$  limit.
- Determined at a ref. scale ( $Q=m_Z$ ), decreases as  $\alpha_s \sim \ln(Q^2/\Lambda^2)^{-1}$ ,  $\Lambda \sim 0.2$  GeV



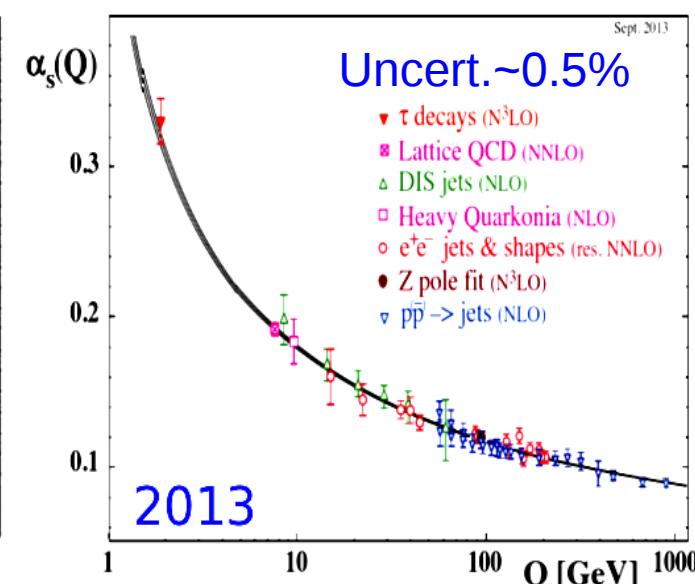
$$\alpha_s(M_Z) = 0.110^{+0.006}_{-0.008} \text{ (NLO)}$$

G. Altarelli, Ann. Rev. Nucl. Part. Sci. 39, 1989



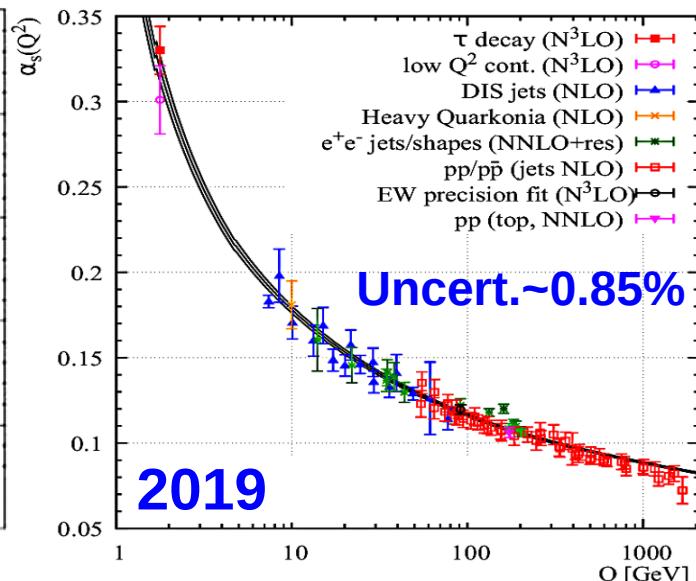
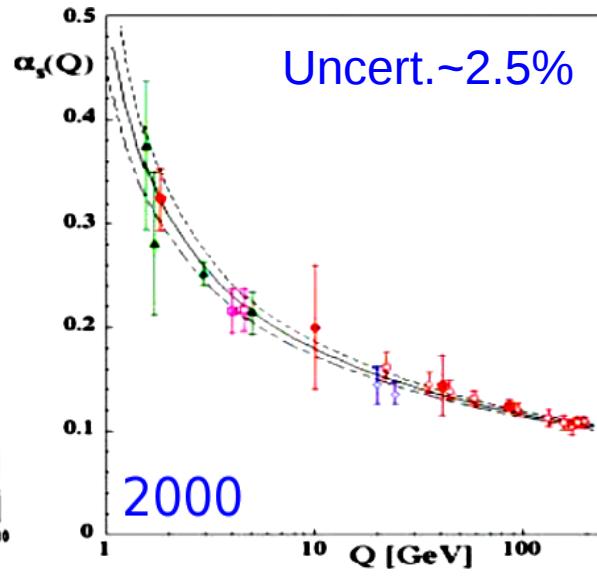
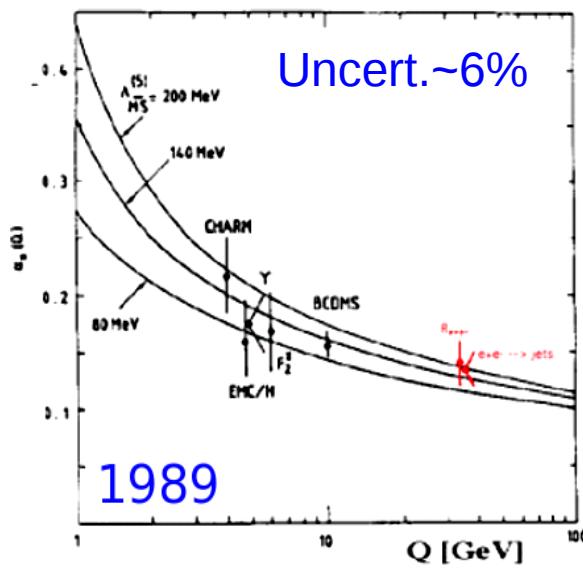
$$\alpha_s(M_Z) = 0.1184 \pm 0.0031 \text{ (NNLO)}$$

S. B., J. Phys. G 26, 2000



# QCD coupling $\alpha_s$

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S. B., J. Phys. G 26, 2000

► Least precisely known of all interaction **couplings** !

$$\delta\alpha \sim 10^{-10} \ll \delta G_F \ll 10^{-7} \ll \delta G \sim 10^{-5} \ll \delta\alpha_s \sim 10^{-3}$$

# Importance of the QCD coupling $\alpha_s$

→ Impacts all QCD x-sections & decays (H), precision top & parametric EWPO:

Process	$\sigma$ (pb)	$\delta\alpha_s$ (%)	PDF + $\alpha_s$ (%)	Scale(%)
ggH	49.87	$\pm 3.7$	-6.2 +7.4	-2.61 + 0.32
tH	0.611	$\pm 3.0$	$\pm 8.9$	-9.3 + 5.9

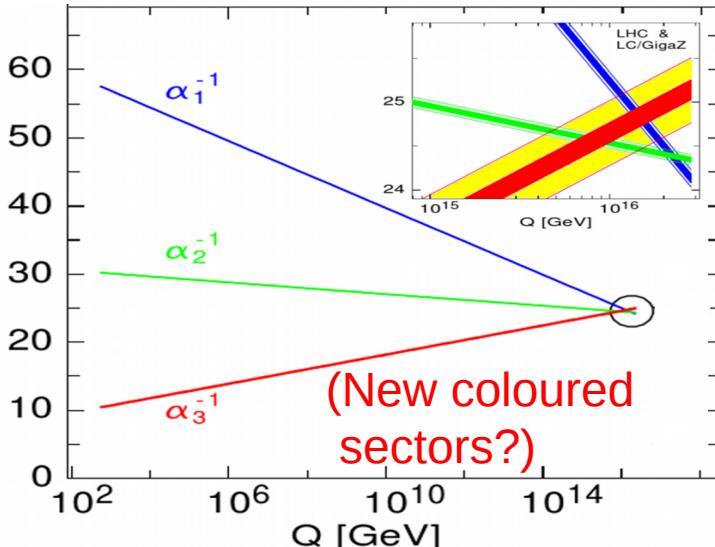
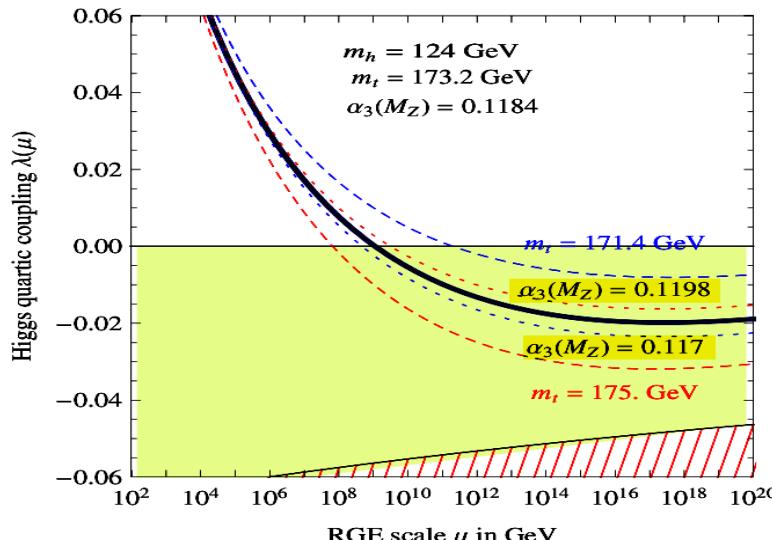
Channel	$M_H$ [GeV]	$\delta\alpha_s$ (%)	$\Delta m_b$	$\Delta m_c$
$H \rightarrow c\bar{c}$	126	$\pm 7.1$	$\pm 0.1\%$	$\pm 2.3\%$
$H \rightarrow gg$	126	$\pm 4.1$	$\pm 0.1\%$	$\pm 0\%$

Msbar mass error budget (from threshold scan)			
$(\delta M_t^{\text{SD-low}})^{\text{exp}}$	$(\delta M_t^{\text{SD-low}})^{\text{theo}}$	$(\delta \bar{m}_t(\bar{m}_t))^{\text{conversion}}$	$(\delta \bar{m}_t(\bar{m}_t))^{\alpha_s}$
40 MeV	50 MeV	7 – 23 MeV	70 MeV
⇒ improvement in $\alpha_s$ crucial			$\delta\alpha_s(M_z) = 0.001$

Quantity	FCC-ee	future param.unc.	Main source
$\Gamma_Z$ [MeV]	0.1	0.1	$\delta\alpha_s$
$R_b$ [ $10^{-5}$ ]	6	< 1	$\delta\alpha_s$
$R_\ell$ [ $10^{-3}$ ]	1	1.3	$\delta\alpha_s$

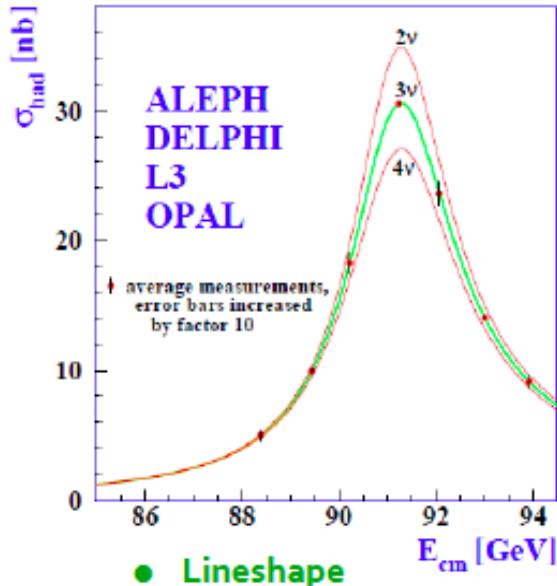
Sven Heinemeyer – 1st FCC physics workshop, CERN, 17.01.2017

→ Impacts physics approaching Planck scale: EW vacuum stability, GUT



# Ultra-precise W, Z, top physics at FCC-ee

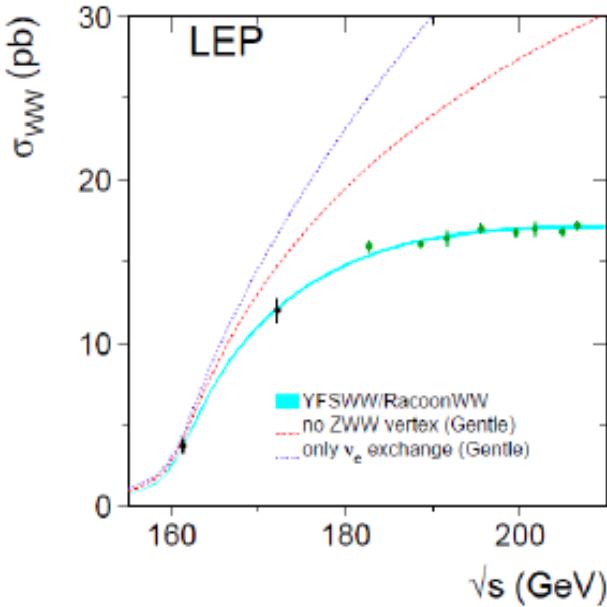
$\sqrt{s}=91 \text{ GeV}, 10^{12} Z's$



- Lineshape
  - Exquisite  $E_{\text{beam}}$  (unique!)
  - $m_Z, \Gamma_Z$  to 10 keV (stat.)
- Asymmetries 100 keV (syst.)
  - $\sin^2\theta_W$  to  $5 \times 10^{-6}$
- Branching ratios,  $R_l, R_{\text{had}}$ 
  - $\alpha_s(m_Z)$  to 0.0002
- Predict  $m_{\text{top}}, m_W$  in SM

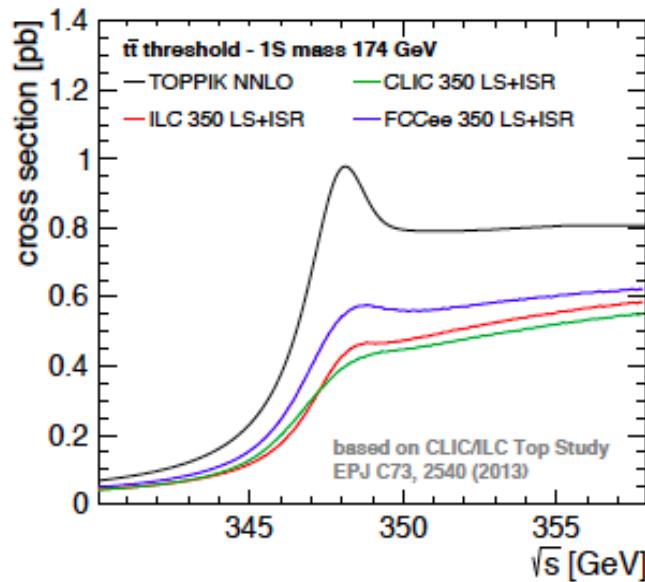
- Unparalleled Z, W, jets,  $\tau, \dots$  data sets: Negligible  $\alpha_s$  stat. uncertainties
- Unparalleled syst. uncert.:  $\delta E_{\text{cm}}(Z, W) \sim 0.1, 0.3 \text{ MeV} \rightarrow$  Very precise  $\Gamma_{W,Z}$

$\sqrt{s}=161 \text{ GeV}, 10^8 W's$



- Threshold scan
  - $m_W$  to 500 keV
- Branching ratios  $R_l, R_{\text{had}}$ 
  - $\alpha_s(m_W)$  to 0.0002
- Radiative returns  $e^+e^- \rightarrow \gamma Z$  ( $Z \rightarrow \nu\nu, \mu^+\mu^-$ )
  - $N_\nu$  to 0.001

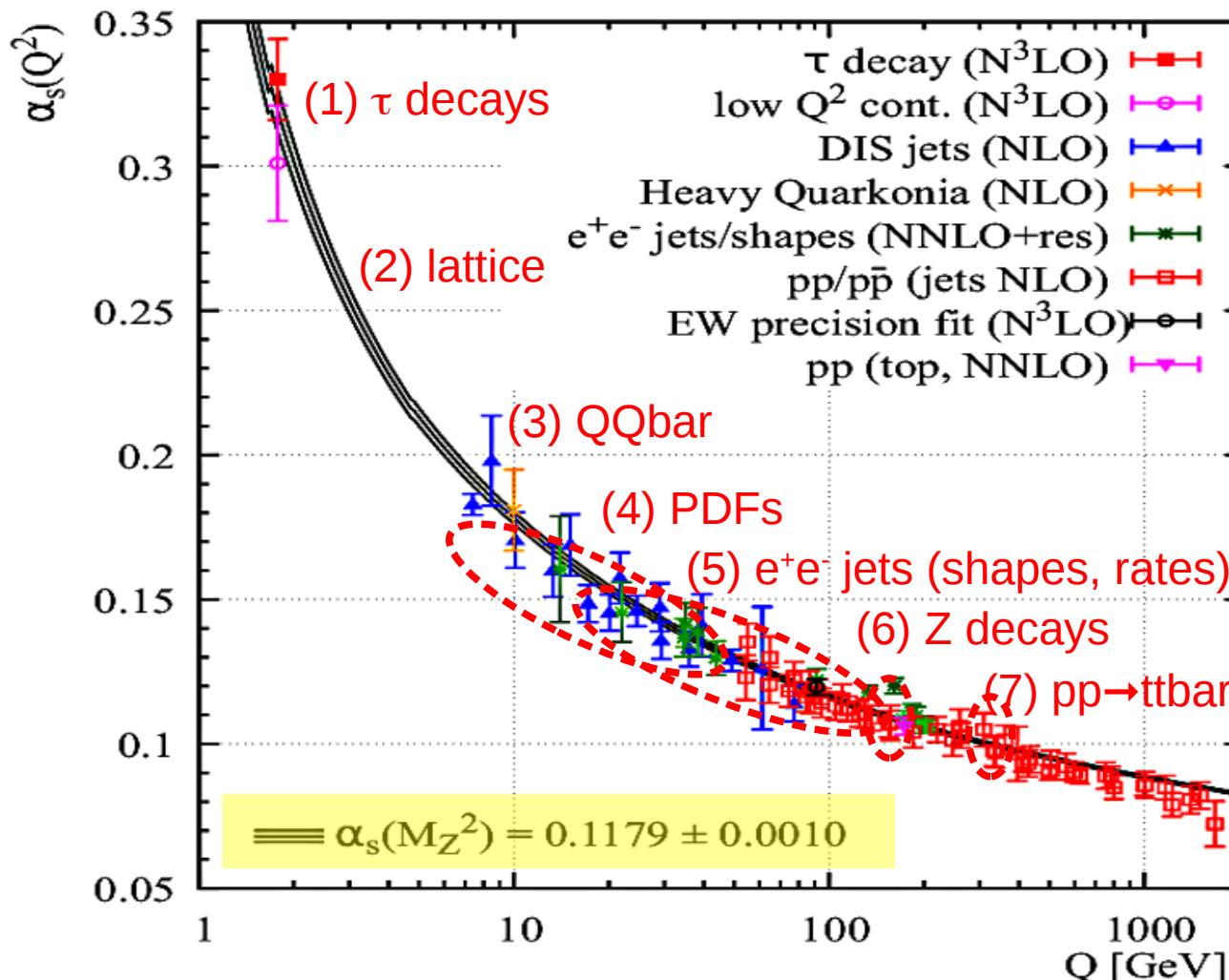
$\sqrt{s}=350 \text{ GeV}, 10^6 \text{ tops}$



- Threshold scan + 4D fit
  - $m_{\text{top}}$  to 10 MeV (stat.)  
40 MeV (th.)
  - $\lambda_{\text{top}}$  to 13%
  - EWK couplings to 1–10%

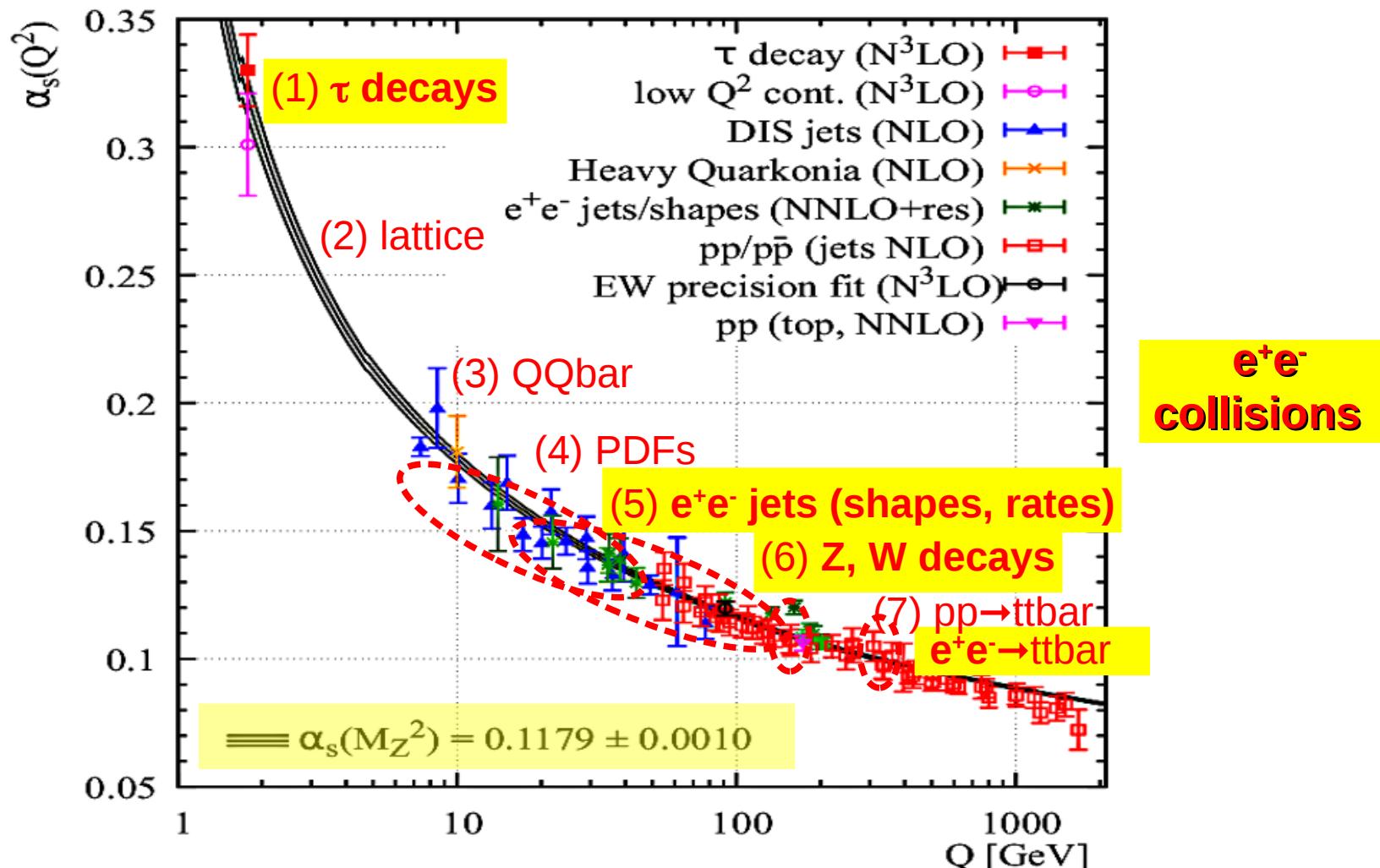
# World $\alpha_s$ determination (PDG 2019)

- Determined today by comparing 7 experimental observables to pQCD NNLO,N<sup>3</sup>LO predictions, plus global average at the Z pole scale:



# World $\alpha_s$ determination (PDG 2019)

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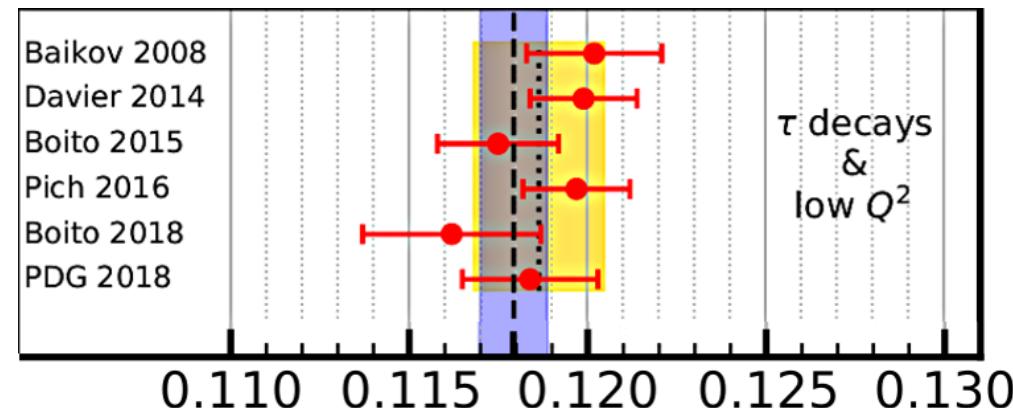


# $\alpha_s$ from hadronic $\tau$ -lepton decays

→ Computed at  $N^3\text{LO}$ :  $R_\tau \equiv \frac{\Gamma(\tau^- \rightarrow \nu_\tau + \text{hadrons})}{\Gamma(\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e)} = S_{\text{EW}} N_C (1 + \sum_{n=1}^4 c_n \left(\frac{\alpha_s}{\pi}\right)^n + \mathcal{O}(\alpha_s^5) + \delta_{\text{np}})$

→ Experimentally:  $R_{\tau, \text{exp}} = 3.4697 \pm 0.0080 (\pm 0.23\%)$

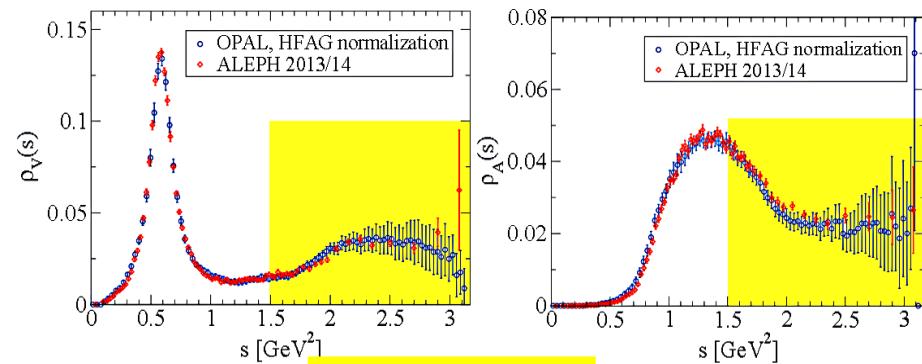
→ Various pQCD approaches (FOPT vs CIPT) & treatment of non-pQCD corrections ( $(\Lambda/m_\tau)^2 \sim 2\%$ , yield different results).



Uncertainty slightly increased:  
2013 ( $\pm 1.3\%$ ) → 2019 ( $\pm 1.5\%$ )

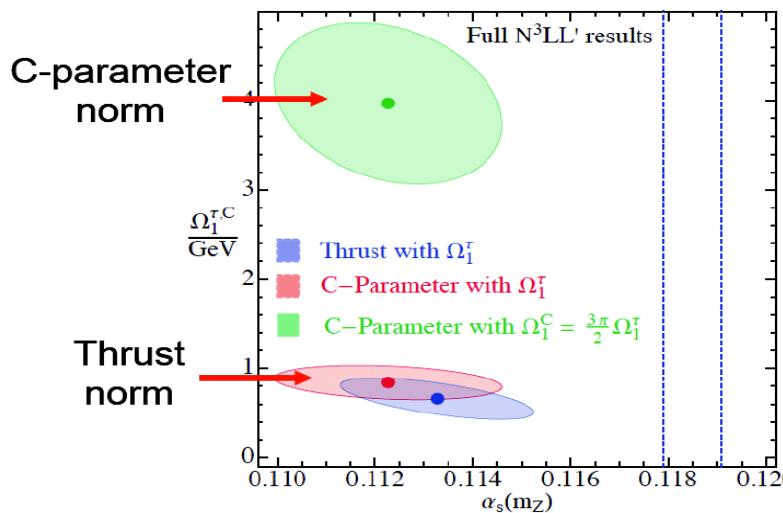
$$\alpha_s(M_Z^2) = 0.1187 \pm 0.0018 (\pm 1.5\%)$$

- Future :
- Understand FOPT vs CIPT diffs.
  - Better spectral functions needed (high stats & better precision): B-factories (BELLE-II)?
  - High-stats:  $\mathcal{O}(10^{11})$  from  $Z \rightarrow \tau\tau$  at FCC-ee(90) :  $\delta\alpha_s \ll 1\%$



# $\alpha_s$ from $e^+e^-$ event shapes & jet rates (today)

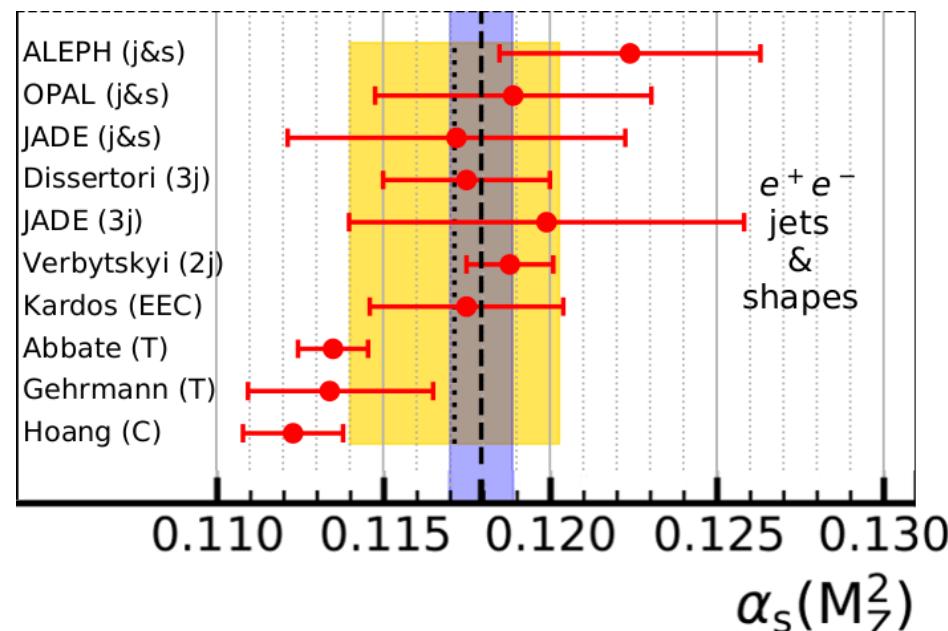
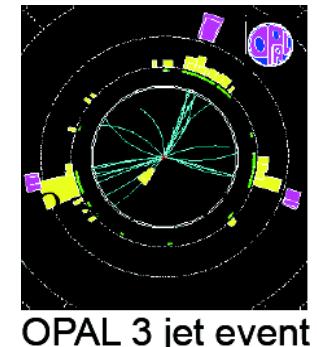
- Computed at  $N^{2,3}\text{LO} + N^{(2)}\text{LL}$  accuracy.
- Experimentally (LEP):
  - Thrust, C-parameter, jet shapes
  - n-jet x-sections
- Results sensitive to non-pQCD (hadronization) accounted for via MCs or analytically:



- Wide span of TH extractions...

$$\tau = 1 - \max_{\hat{n}} \frac{\sum |\vec{p}_i \cdot \hat{n}|}{\sum |\vec{p}_i|}$$

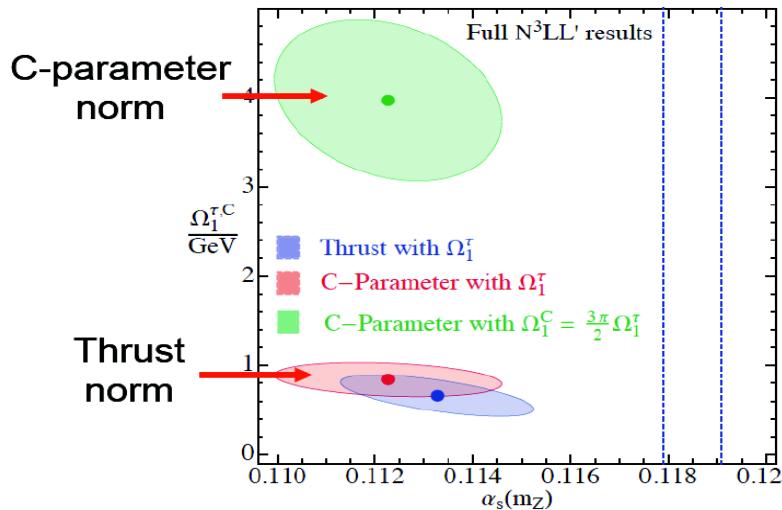
$$C = \frac{3}{2} \frac{\sum_{i,j} |\vec{p}_i| |\vec{p}_j| \sin^2 \theta_{ij}}{\left(\sum_i |\vec{p}_i|\right)^2}$$



$$\alpha_s(M_Z^2) = 0.1171 \pm 0.0031 \quad (\pm 2.6\%)$$

# $\alpha_s$ from $e^+e^-$ event shapes & jet rates (FCC-ee)

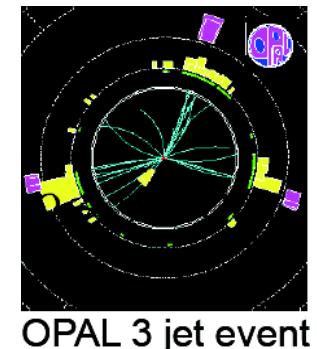
- Computed at  $N^{2,3}\text{LO} + N^{(2)}\text{LL}$  accuracy.
- Experimentally (LEP):
  - Thrust, C-parameter, jet shapes
  - 3-jet x-sections
- Results sensitive to non-pQCD (hadronization) accounted for via MCs or analytically:



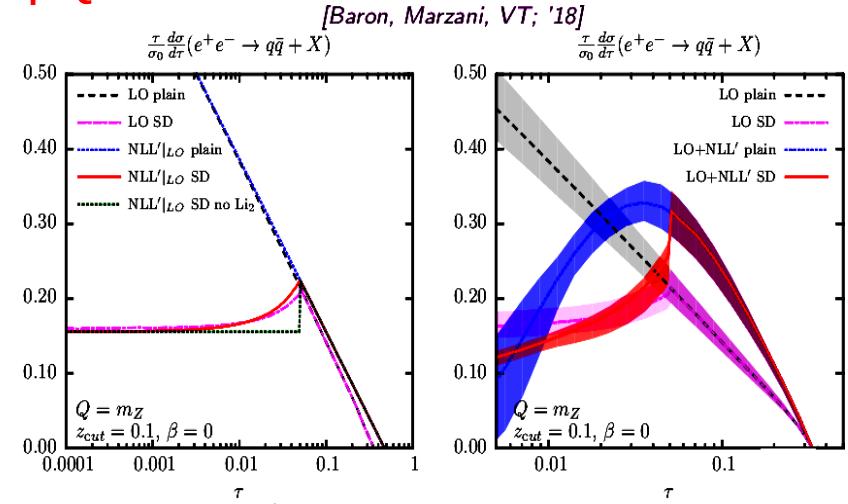
- Future:  $\delta\alpha_s/\alpha_s < 1\%$ 
  - FCC-ee: Lower- $\sqrt{s}$  (ISR) for shapes, higher- $\sqrt{s}$  for jet rates
  - TH: Improved ( $N^{2,3}\text{LL}$ ) resummation for rates, hadronization for shapes

$$\tau = 1 - \max_{\hat{n}} \frac{\sum |\vec{p}_i \cdot \hat{n}|}{\sum |\vec{p}_i|}$$

$$C = \frac{3}{2} \frac{\sum_{i,j} |\vec{p}_i||\vec{p}_j| \sin^2 \theta_{ij}}{\left(\sum_i |\vec{p}_i|\right)^2}$$



- Modern jet substructure techniques:  
“Soft drop” can help reduce non-pQCD corrections for thrust:



# Hadronic Z, W decay pseudo-observables

→ Z & W observables theoretically known at N<sup>3</sup>LO accuracy:

DdE, Jacobsen:  
arXiv:2005.04545

- The W and Z hadronic widths :

$$\Gamma_{W,Z}^{\text{had}}(Q) = \Gamma_{W,Z}^{\text{Born}} \left( 1 + \sum_{i=1}^4 a_i(Q) \left( \frac{\alpha_S(Q)}{\pi} \right)^i + \mathcal{O}(\alpha_S^5) + \delta_{\text{EW}} + \delta_{\text{mix}} + \delta_{\text{np}} \right)$$

TH uncertainties:

( $\alpha^2, \alpha^3$  included for Z):

$\pm 0.015\text{--}0.03\%$  (Z)

$\pm 0.015\text{--}0.04\%$  (W)

- The ratio of W, Z hadronic-to-leptonic widths :

$$R_{W,Z}(Q) = \frac{\Gamma_{W,Z}^{\text{had}}(Q)}{\Gamma_{W,Z}^{\text{lep}}(Q)} = R_{W,Z}^{\text{EW}} \left( 1 + \sum_{i=1}^4 a_i(Q) \left( \frac{\alpha_S(Q)}{\pi} \right)^i + \mathcal{O}(\alpha_S^5) + \delta_{\text{mix}} + \delta_{\text{np}} \right)$$

Param. uncerts.:

( $m_{Z,W}, \alpha, V_{cs,ud}$ ):

- In the Z boson case, the hadronic cross section at the resonance peak in  $e^+e^-$ :

$$\sigma_Z^{\text{had}} = \frac{12\pi}{m_Z} \cdot \frac{\Gamma_Z^e \Gamma_Z^{\text{had}}}{(\Gamma_Z^{\text{tot}})^2}$$

$\pm 0.01\text{--}0.03\%$  (Z)

$\pm 1.1\text{--}1.7\%$  (W)

$\pm 0.03\%$  (W, CKM unit)

→ Measured at LEP with  $\pm 0.1\text{--}0.3\%$  (Z),  $\pm 0.9\text{--}2\%$  (W) exp. uncertainties:

	theory			experiment		
	previous	new (this work)	change	previous [6]	new [20, 21]	change
$\Gamma_Z^{\text{tot}}$ (MeV)	$2494.2 \pm 0.8_{\text{th}}$	$2495.2 \pm 0.6_{\text{par}} \pm 0.4_{\text{th}}$	+0.04%	$2495.2 \pm 2.3$	$2495.5 \pm 2.3$	+0.012%
$R_Z$	$20.733 \pm 0.007_{\text{th}}$	$20.750 \pm 0.006_{\text{par}} \pm 0.006_{\text{th}}$	+0.08%	$20.767 \pm 0.025$	$20.7666 \pm 0.0247$	-0.040%
$\sigma_Z^{\text{had}}$ (pb)	$41\,490 \pm 6_{\text{th}}$	$41\,494 \pm 5_{\text{par}} \pm 6_{\text{th}}$	+0.01%	$41\,540 \pm 37$	$41\,480.2 \pm 32.5$	-0.144%

Recent update of  
LEP luminosity  
bias(\*) change the Z  
values by few permil

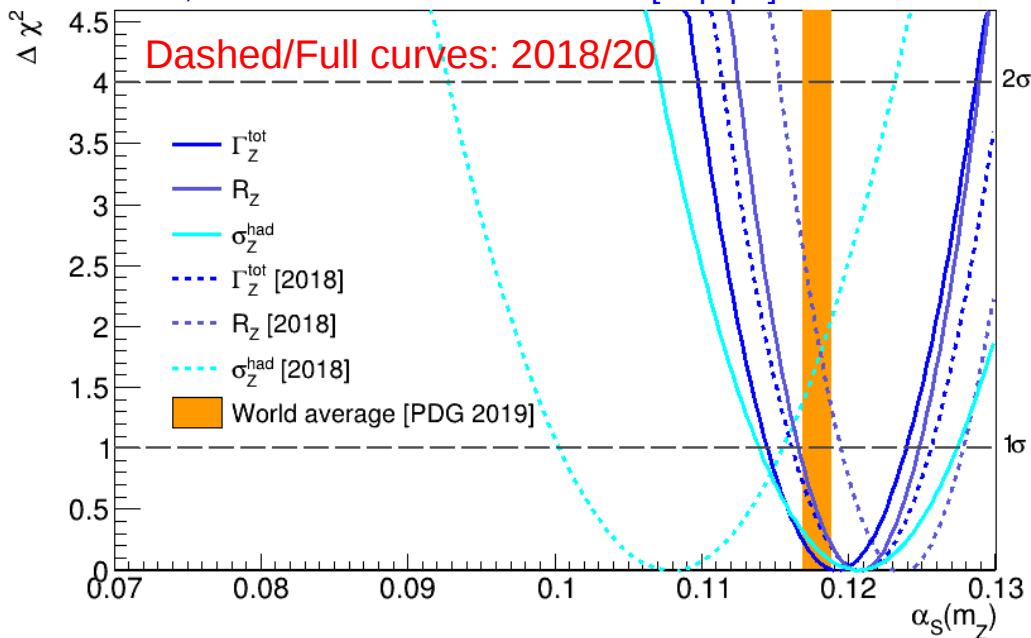
W boson observables	GFITTER 2.2 (NNLO)			this work (N <sup>3</sup> LO)		experiment
	(exp. CKM)			(CKM unit.)		
$\Gamma_W^{\text{had}}$ (MeV)	—			$1440.3 \pm 23.9_{\text{par}} \pm 0.2_{\text{th}}$	$1410.2 \pm 0.8_{\text{par}} \pm 0.2_{\text{th}}$	$1405 \pm 29$
$\Gamma_W^{\text{tot}}$ (MeV)	$2091.8 \pm 1.0_{\text{par}}$			$2117.9 \pm 23.9_{\text{par}} \pm 0.7_{\text{th}}$	$2087.9 \pm 1.0_{\text{par}} \pm 0.7_{\text{th}}$	$2085 \pm 42$
$R_W$	—			$2.1256 \pm 0.0353_{\text{par}} \pm 0.0008_{\text{th}}$	$2.0812 \pm 0.0007_{\text{par}} \pm 0.0008_{\text{th}}$	$2.069 \pm 0.019$

(\*) Voutsinas et al.  
arXiv:1908.01704,  
Janot et al.  
arXiv:1912.02067

# $\alpha_s$ from hadronic Z decays (today)

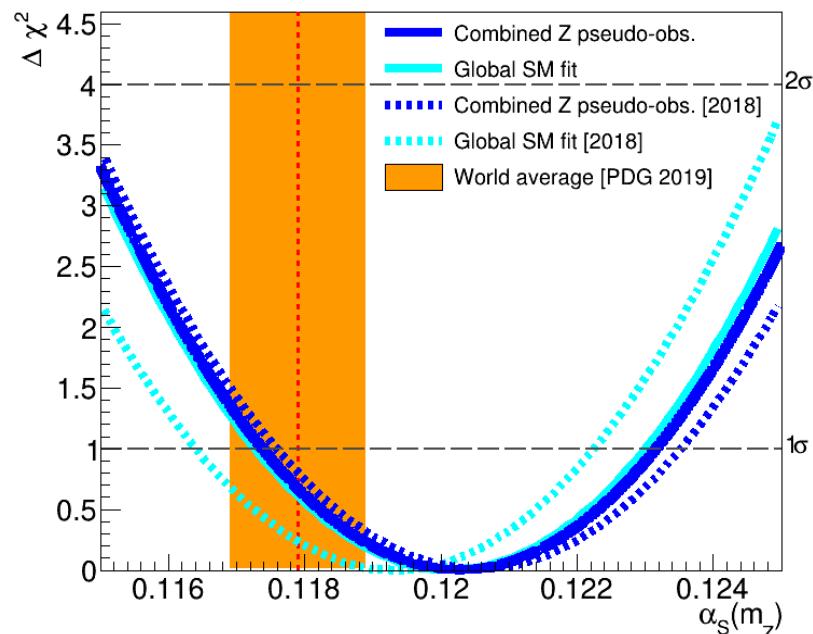
- QCD coupling extracted from:
  - (i) Combined fit of 3 Z pseudo-observ.
  - (ii) Full SM fit (with  $\alpha_s$  free parameter)

DdE, Jacobsen: arXiv:2005.04545 [hep-ph]



- LEP lumi-bias updates lead to much better agreement among  $\Gamma_z$ ,  $R_z$ ,  $\sigma_0$  extractions:
- Improved  $\alpha_s(m_z) = 0.1203 \pm 0.0028$  ( $\pm 2.3\%$ )  
 $PDG'19: \alpha_s(m_z) = 0.1205 \pm 0.0030$  ( $\pm 2.5\%$ )

Z boson observable	$\alpha_s(m_Z)$ extraction	uncertainties		
	exp.	param.	theor.	
$\Gamma_Z^{\text{tot}}$	$0.1192 \pm 0.0047$	$\pm 0.0046$	$\pm 0.0005$	$\pm 0.0008$
$R_Z$	$0.1207 \pm 0.0041$	$\pm 0.0041$	$\pm 0.0001$	$\pm 0.0009$
$\sigma_Z^{\text{had}}$	$0.1206 \pm 0.0068$	$\pm 0.0067$	$\pm 0.0004$	$\pm 0.0012$
All combined	$0.1203 \pm 0.0029$	$\pm 0.0029$	$\pm 0.0002$	$\pm 0.0008$
Global SM fit	$0.1202 \pm 0.0028$	$\pm 0.0028$	$\pm 0.0002$	$\pm 0.0008$



- EXP/TH updates lead to better agreement with full SM fit:
- $\alpha_s(m_z) = 0.1202 \pm 0.0028$   
 $PDG'19: \alpha_s(m_z) = 0.1194 \pm 0.0029$

# $\alpha_s$ from hadronic Z decays (FCC-ee)

→ QCD coupling extracted from:

- (i) Combined fit of 3 Z pseudo-observ:
- (ii) Full SM fit (with  $\alpha_s$  free parameter)

Z boson observable	$\alpha_s(m_Z)$ extraction	uncertainties		
		exp.	param.	theor.
All combined	$0.1203 \pm 0.0029$	$\pm 0.0029$	$\pm 0.0002$	$\pm 0.0008$
Global SM fit	$0.1202 \pm 0.0028$	$\pm 0.0028$	$\pm 0.0002$	$\pm 0.0008$
All combined (FCC-ee)	$0.12030 \pm 0.00026$	$\pm 0.00013$	$\pm 0.00005$	$\pm 0.00022$
Global SM fit (FCC-ee)	$0.12020 \pm 0.00026$	$\pm 0.00013$	$\pm 0.00005$	$\pm 0.00022$

→ FCC-ee:

- Huge Z pole stats. ( $\times 10^5$  LEP):
- Exquisite systematic/parametric precision (stat. uncert. negligible):

$$\Delta R_Z = 10^{-3}, \quad R_Z = 20.7500 \pm 0.0010$$

$$\Delta \Gamma_Z^{\text{tot}} = 0.1 \text{ MeV}, \quad \Gamma_Z^{\text{tot}} = 2495.2 \pm 0.1 \text{ MeV}$$

$$\Delta \sigma_Z^{\text{had}} = 4.0 \text{ pb}, \quad \sigma_Z^{\text{had}} = 41494 \pm 4 \text{ pb}$$

$$\Delta m_Z = 0.1 \text{ MeV}, \quad m_Z = 91.18760 \pm 0.00001 \text{ GeV}$$

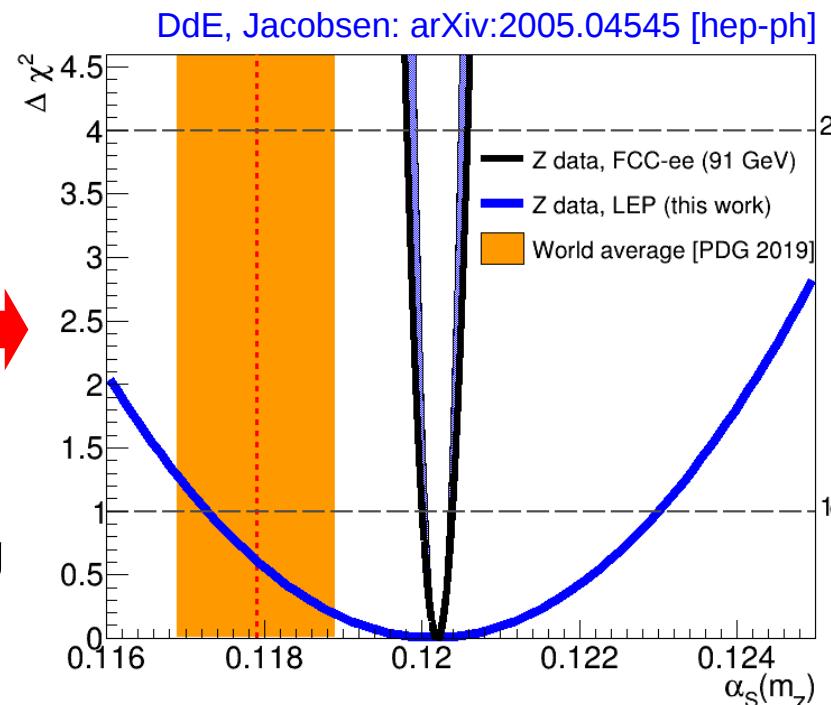
$$\Delta \alpha = 3 \cdot 10^{-5}, \quad \Delta \alpha_{\text{had}}^{(5)}(m_Z) = 0.0275300 \pm 0.0000009$$

- TH uncertainty reduced by  $\times 4$  computing missing  $\alpha_s^5, \alpha^3, \alpha \alpha_s^2, \alpha \alpha_s^2, \alpha^2 \alpha_s$  terms

→ 10 times better precision than today:

$$\delta \alpha_s / \alpha_s \sim \pm 0.2\% \text{ (tot), } \pm 0.1\% \text{ (exp)}$$

Strong (B)SM consistency test.



$$\alpha_s(m_Z) = 0.12030 \pm 0.00028 \quad (\pm 0.2\%)$$

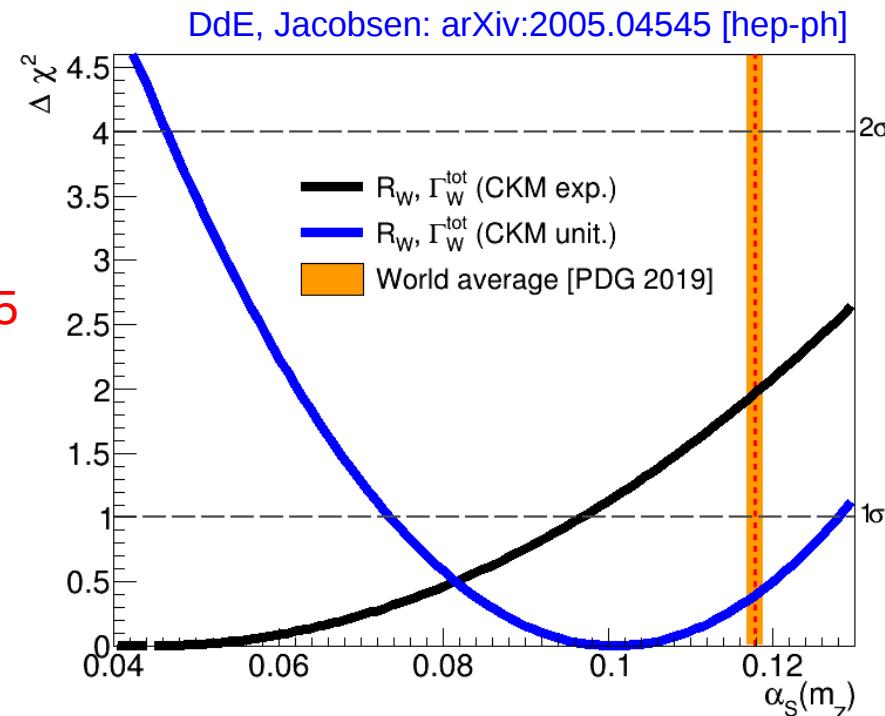
# $\alpha_s$ from hadronic W decays (today)

- QCD coupling extracted from new N<sup>3</sup>LO fit of combined  $\Gamma_w$ ,  $R_w$  pseudo-observ.:

W boson observables	$\alpha_S(m_Z)$ extraction	uncertainties		
		exp.	param.	theor.
$\Gamma_W^{\text{tot}}$ , $R_w$ (exp. CKM)	$0.044 \pm 0.052$	$\pm 0.024$	$\pm 0.047$	( $\pm 0.0014$ )
$\Gamma_W^{\text{tot}}$ , $R_w$ (CKM unit.)	$0.101 \pm 0.027$	$\pm 0.027$	( $\pm 0.0002$ )	( $\pm 0.0016$ )
$\Gamma_W^{\text{tot}}$ , $R_w$ (FCC-ee, CKM unit.)	$0.11790 \pm 0.00023$	$\pm 0.00012$	$\pm 0.00004$	$\pm 0.00019$

► Very imprecise extraction:

- Large propagated parametric uncert. from poor  $V_{cs}$  exp. precision ( $\pm 2\%$ ): QCD coupling unconstrained:  $0.04 \pm 0.05$
- Imposing CKM unitarity: large exp. uncertainties from  $\Gamma_w$ ,  $R_w$  (0.9–2%): QCD extracted with ~27% precision
- Propagated TH uncertainty much smaller today: ~1.5%



$$\alpha_s(m_Z) = 0.101 \pm 0.027 \quad (\pm 27\%)$$

# $\alpha_s$ from hadronic W decays (FCC-ee)

- QCD coupling extracted from new N<sup>3</sup>LO fit of combined  $\Gamma_W$ ,  $R_W$  pseudo-observ.:

W boson observables	$\alpha_S(m_Z)$ extraction	uncertainties		
		exp.	param.	theor.
$\Gamma_W^{\text{tot}}$ , $R_W$ (exp. CKM)	$0.044 \pm 0.052$	$\pm 0.024$	$\pm 0.047$	( $\pm 0.0014$ )
$\Gamma_W^{\text{tot}}$ , $R_W$ (CKM unit.)	$0.101 \pm 0.027$	$\pm 0.027$	( $\pm 0.0002$ )	( $\pm 0.0016$ )
$\Gamma_W^{\text{tot}}$ , $R_W$ (FCC-ee, CKM unit.)	$0.11790 \pm 0.00023$	$\pm 0.00012$	$\pm 0.00004$	$\pm 0.00019$

## FCC-ee extraction:

- Huge W pole stats. ( $\times 10^4$  LEP-2).
- Exquisite syst./parametric precision:

$$\Gamma_W^{\text{tot}} = 2088.0 \pm 1.2 \text{ MeV}$$

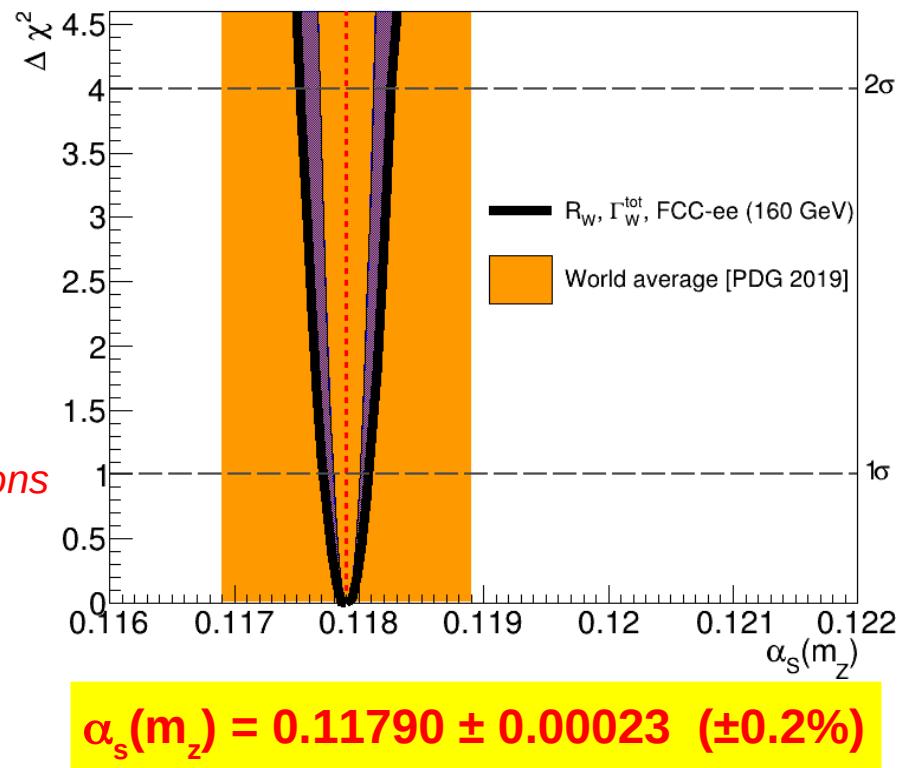
$$R_W = 2.08000 \pm 0.00008$$

$$m_W = 80.3800 \pm 0.0005 \text{ GeV}$$

$$|V_{cs}| = 0.97359 \pm 0.00010 \leftarrow O(10^{12}) D \text{ mesons}$$

- TH uncertainty reduced by  $\times 10$  after computing missing  $\alpha_s^5$ ,  $\alpha^2$ ,  $\alpha^3$ ,  $\alpha\alpha_s^2$ ,  $\alpha\alpha_s^2$ ,  $\alpha^2\alpha_s$  terms

DdE, Jacobsen: arXiv:2005.04545 [hep-ph]



# Partial summary: $\alpha_s$ at FCC-ee

## ■ World-average QCD coupling at N<sup>2,3</sup>LO today:

- Determined from *7 observables* with combined  $\pm 0.85\%$  uncertainty: Least well-known gauge coupling.
- Impacts *all LHC QCD x-sections & decays*.
- Role *beyond SM*: GUT, EWK vacuum stability, New colored sectors?

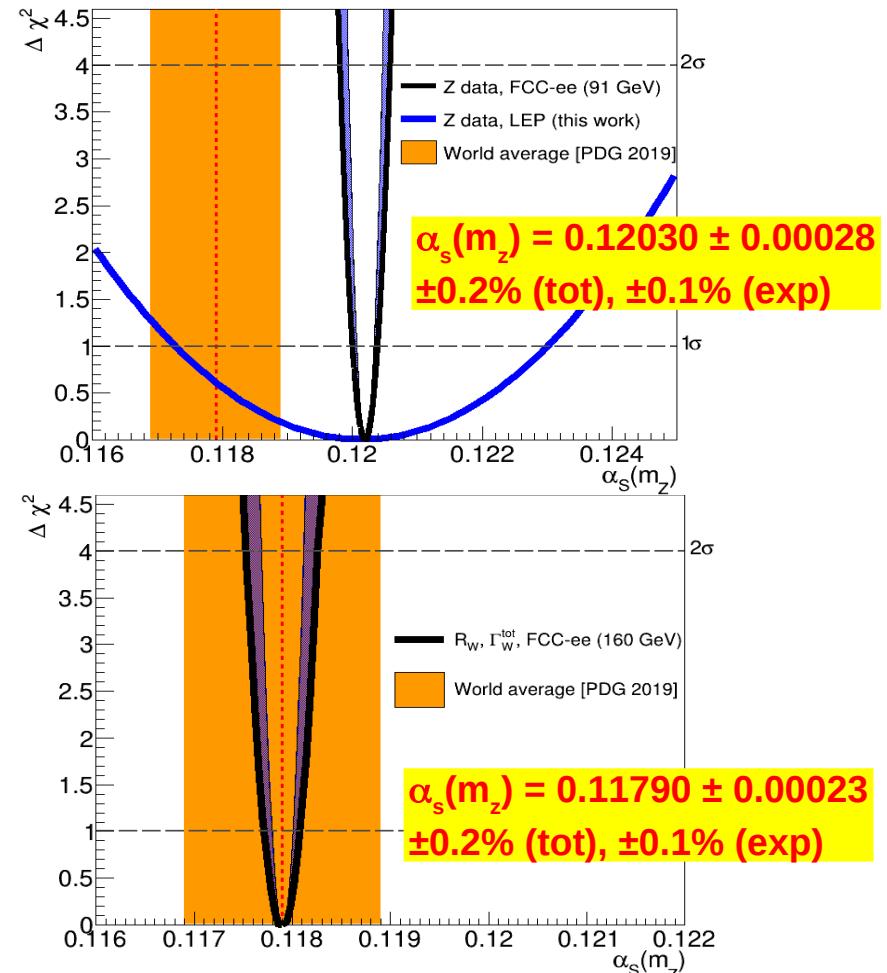
## ■ Uncerts. for e<sup>+</sup>e<sup>-</sup> extractions today:

- $\tau$  decays:  $\pm 1.5\%$  (mostly non-pQCD)
- Shapes, jets:  $\pm 2.6\%$  (mostly non-pQCD)
- Z pseudo-observ.:  $\pm 2.5\%$  (mostly exp.)

## ■ New Z, W extractions:

- Z boson: New fit with high-order EW corrections + updated LEP data:  $\pm 2.3\%, \pm 0.6\%$ , (exp., th.) uncerts.
- W boson: New N<sup>3</sup>LO fit to  $\Gamma_W$ ,  $R_W$   $\sim 47\%, \sim 27\%$  (param., exp.) uncerts.

## ■ 0.1% uncertainty only possible with a machine like FCC-e<sup>+</sup>e<sup>-</sup>



What are the detector design improvements needed to bring propagated syst. uncert. on W,Z pseudo-observ. below 0.1% ?

# $\alpha_s$ running at the multi-TeV scale (FCC-pp)

- Jets from pp collisions above LHC energies provide the only known means to **test asymptotic freedom & new coloured sectors above  $\sim 3$  TeV**:

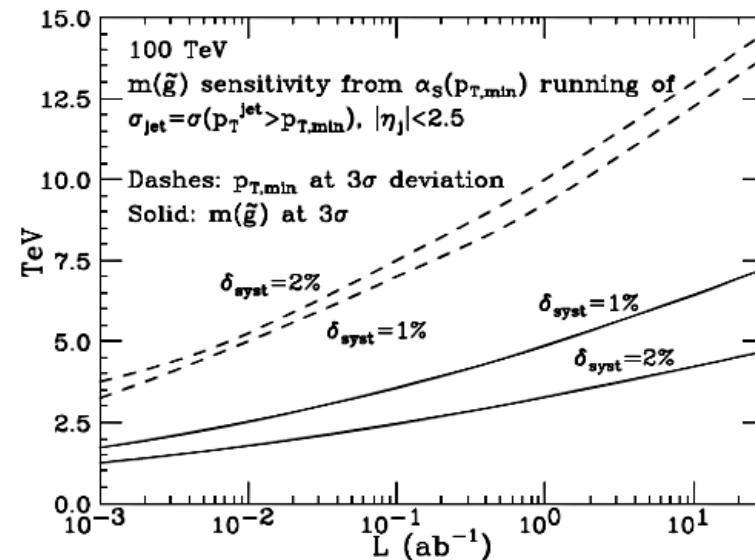
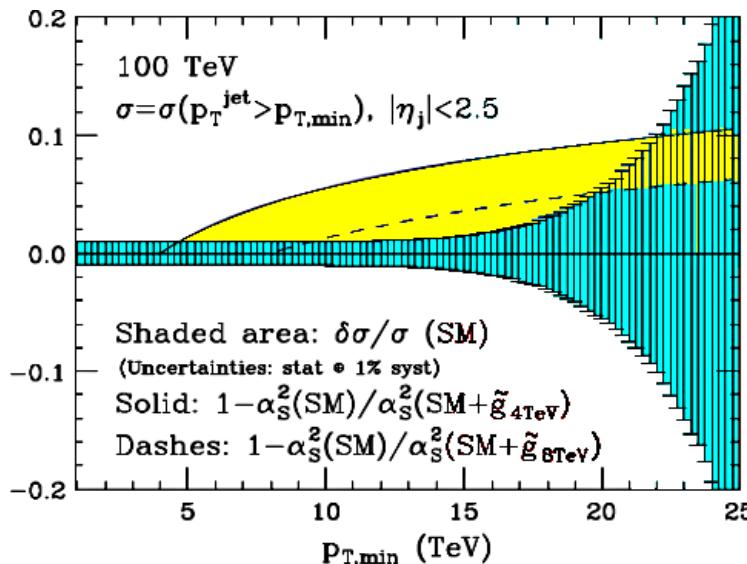


Figure 5.5: Left plot: combined statistical and 1% systematic uncertainties, at  $30 \text{ ab}^{-1}$ , vs  $p_T$  threshold; these are compared to the rate change induced by the presence of 4 or 8 TeV gluinos in the running of  $\alpha_S$ . Right plot: the gluino mass that can be probed with a  $3\sigma$  deviation from the SM jet rate (solid line), and the  $p_T$  scale at which the corresponding deviation is detected.

- FCC-pp:
  - Jet cross sections with <10% stat. uncert. up to  $p_T \sim 25$  TeV
  - Sensitivity to  $m_g = 4-8$  GeV gluinos in  $\alpha_s$  running.

# Physics at FCC e<sup>+</sup>e<sup>-</sup> & pp machines

(1) QCD:  $\alpha_s$  coupling

(2) QCD: Parton Distribution Functions

(3) QCD: Jet substructure & flavour tagging

(4) QCD: Non-perturbative regime

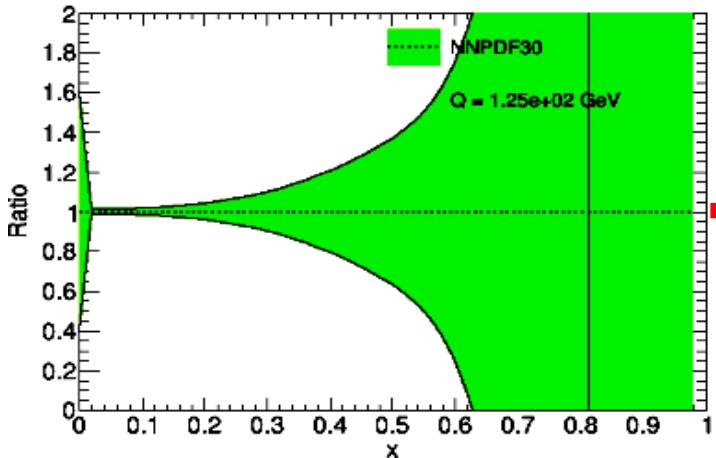
(5) Higgs sector

(6) BSM searches

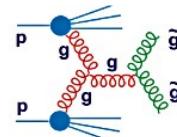
# PDFs impact on new BSM / QCD physics

## New physics at high- $x$ ?

$xg(x,Q)$ , comparison

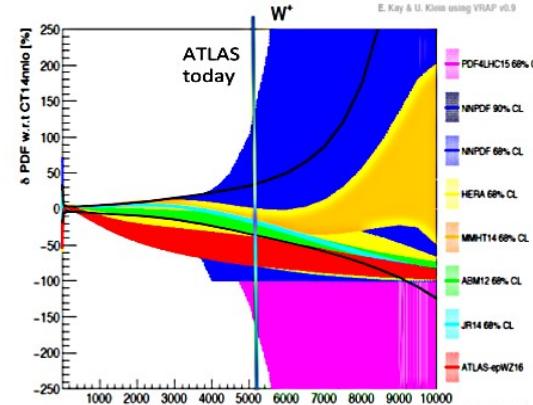
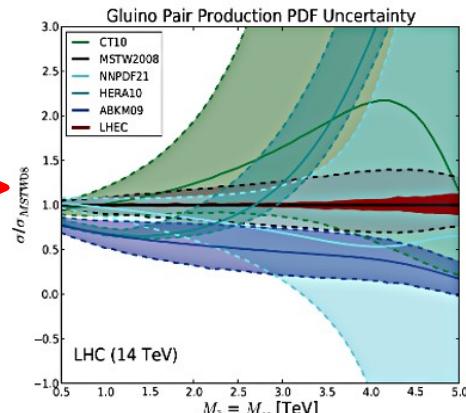


GLUON  
SUSY, RPC, RPV, LQS..



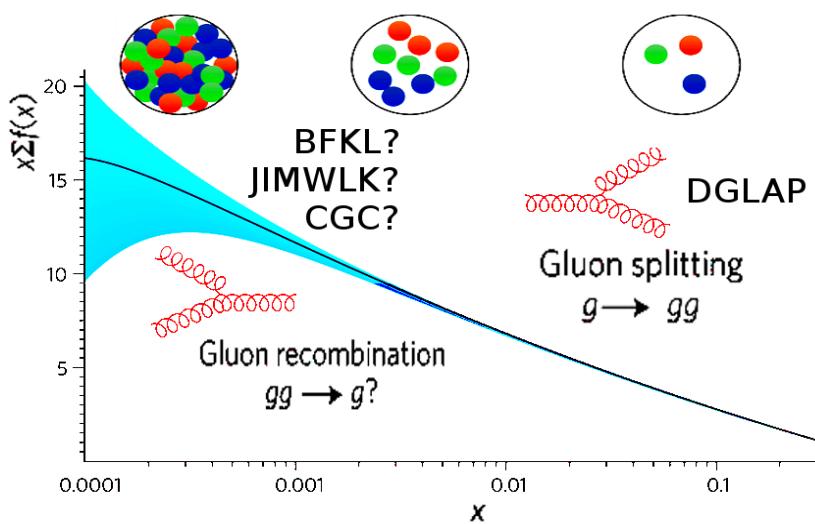
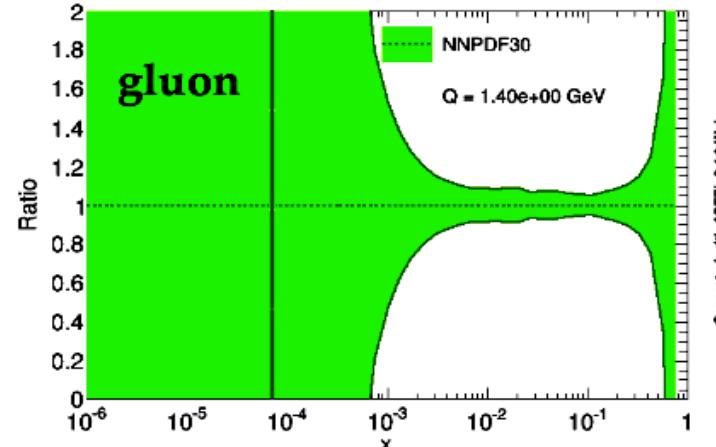
QUARKS

Exotic+ Extra boson searches at high mass



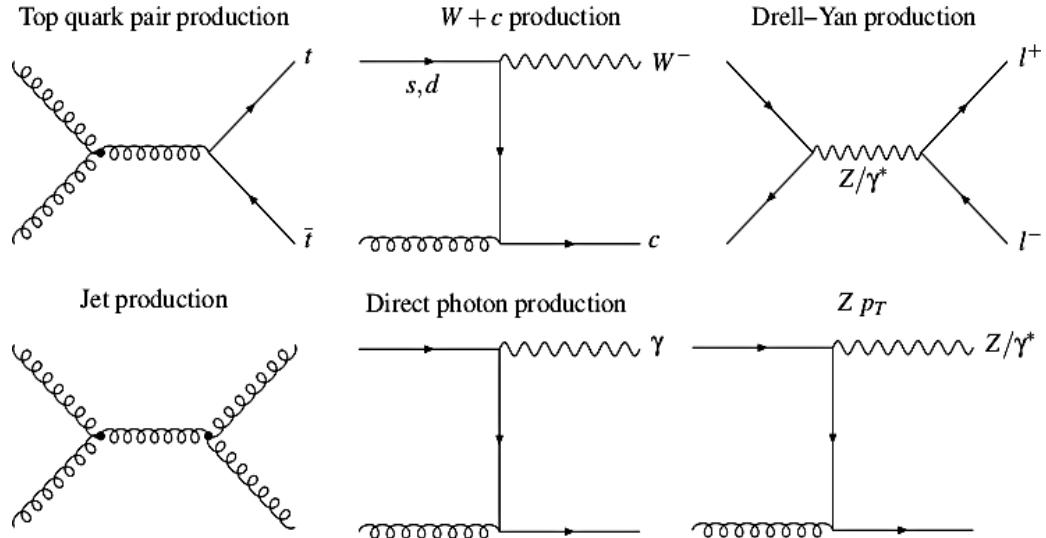
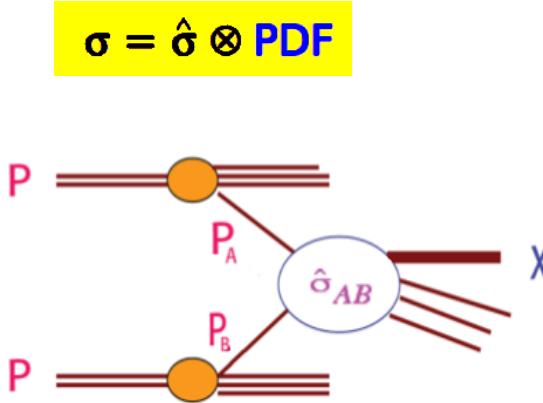
## New QCD evolution at low- $x$ ?

$xg(x,Q)$ , comparison



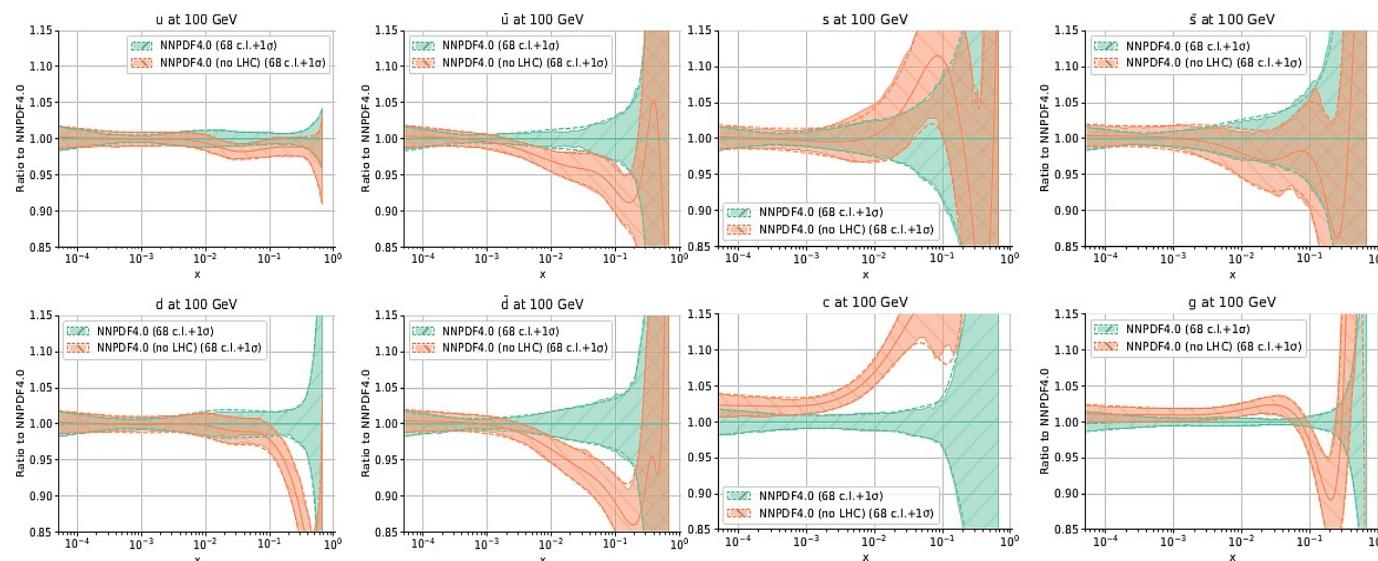
# Improved PDFs with p-p data (today)

- 6 partonic processes in pp at the LHC have provided key PDF constraints:

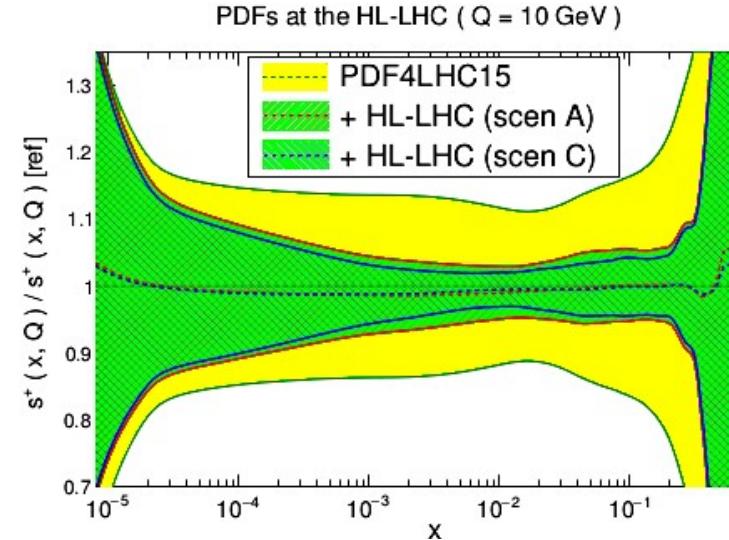
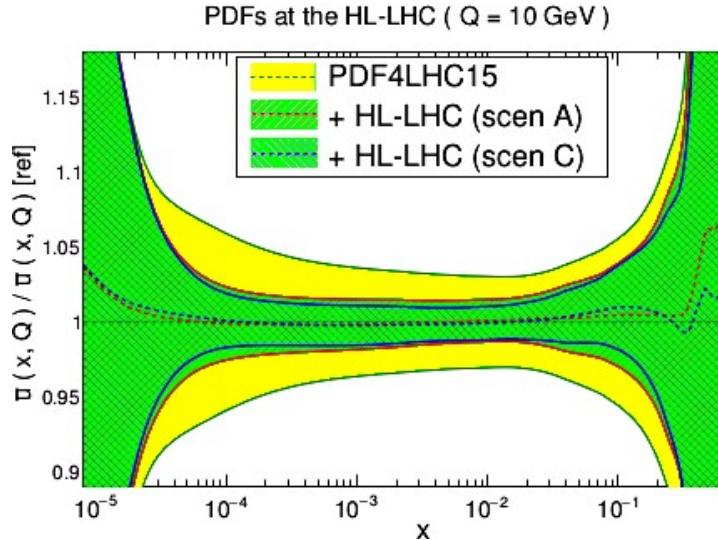
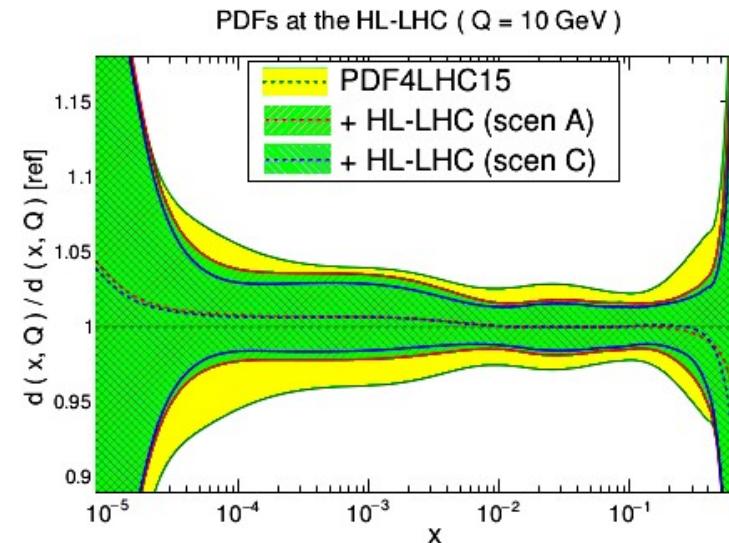
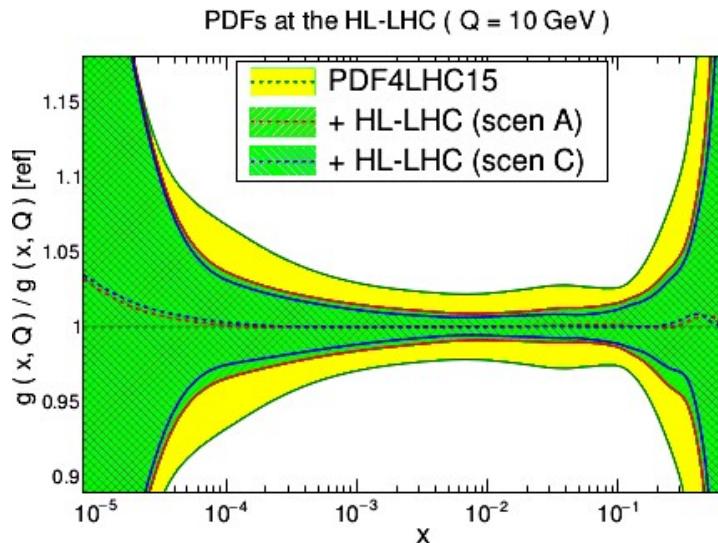


- Updated NNLO PDFs using LHC Run-II data:

At high-x, 10–15% change (plus ~50% reduced uncerts.) for all partons except u-quark



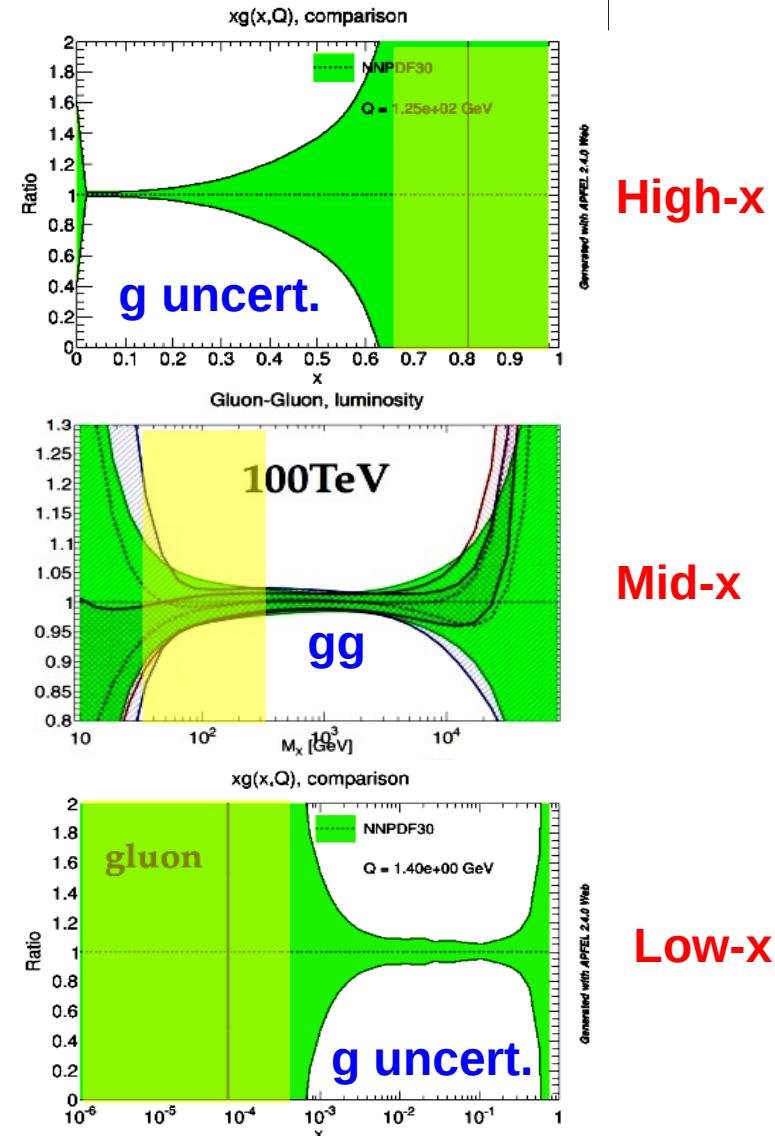
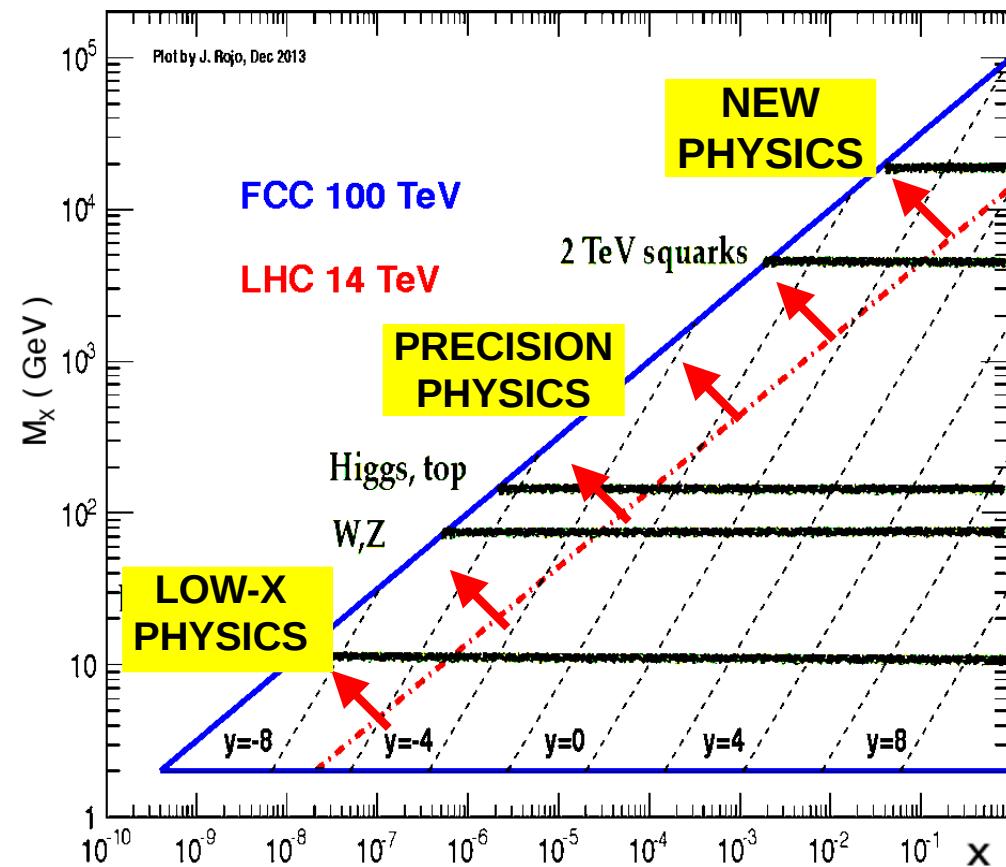
# Improved PDFs with pp data (HL-LHC)



- Significant (factor  $\sim 2$ ) PDF uncertainty reduction (with little dependence on projected systematics). But not at very low-,high- $x$ ...

# PDFs needs for FCC-pp

- Still large PDF uncertainties in pp at 100 TeV in key  $(x, Q^2)$  regions:



- FCC-ep required to reach  $<1\%$  uncertainty for  $\sigma(W, Z, H)$  at FCC-pp, or FCC-pp data themselves will suffice?

# Physics at FCC $e^+e^-$ & $pp$ machines

(1) QCD:  $\alpha_s$  coupling

(2) QCD: Parton Distribution Functions

(3) QCD: Jet substructure & flavour tagging

(4) QCD: Non-perturbative regime

(5) Higgs sector

(6) BSM searches

# Precise jet substructure & flavour tagging

- State-of-the-art jet substructure studies based on **angularities**:

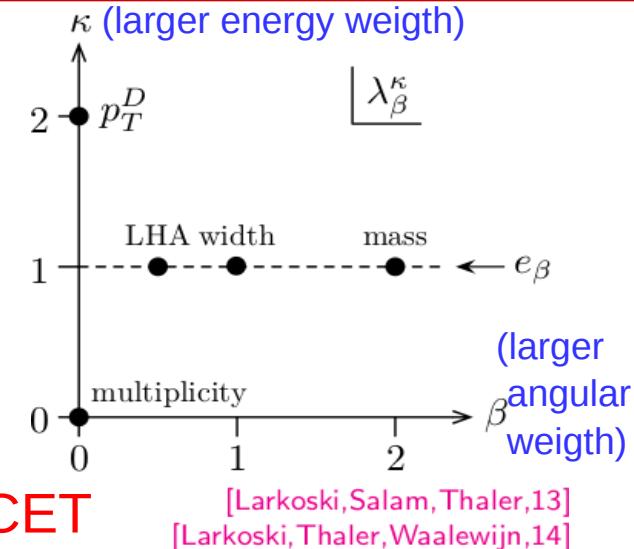
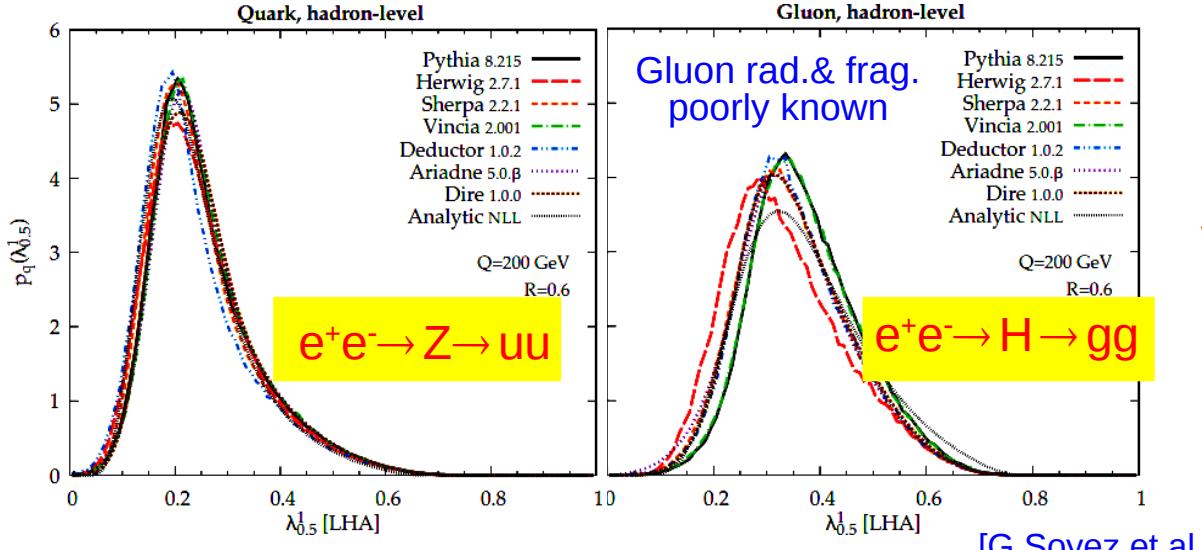
$$\lambda_{\beta}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \theta_i^{\beta},$$

(normalized  $E^n \times \theta^n$  products)

- "Sudakov"-safe variables of **jet constituents**: multiplicity, LHA, width/broadening, mass/thrust, C-parameter,...

- $k=1$ : IRC-safe computable ( $N^n\text{LO}+N^n\text{LL}$ ) via SCET  
(but uncertainties from non-pQCD effects)

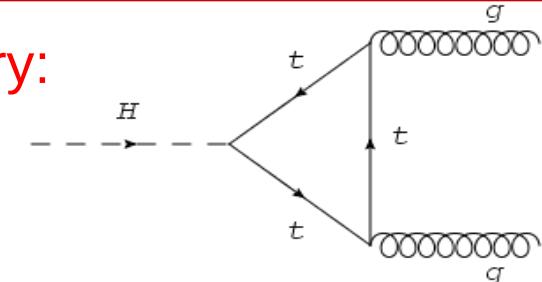
- MC parton showers differ on gluon (less so quark) radiation patterns:



# High-precision gluon & quark jet studies (FCC-ee)

- Exploit FCC-ee  $H(gg)$  as a "pure gluon" factory:

$H \rightarrow gg$  (BR~8% accurately known) provides O(100.000) extra-clean digluon events.



- Multiple handles to study gluon radiation & g-jet properties:

- ▶ Gluon vs. quark via  $H \rightarrow gg$  vs.  $Z \rightarrow qq$

(Profit from excellent g,b separation)

- ▶ Gluon vs. quark via  $Z \rightarrow bbg$  vs.  $Z \rightarrow qq(g)$

(g in one hemisphere recoiling against 2-b-jets in the other).

- ▶ Vary  $E_{jet}$  range via ISR:  $e^+e^- \rightarrow Z^*, \gamma^* \rightarrow jj(\gamma)$

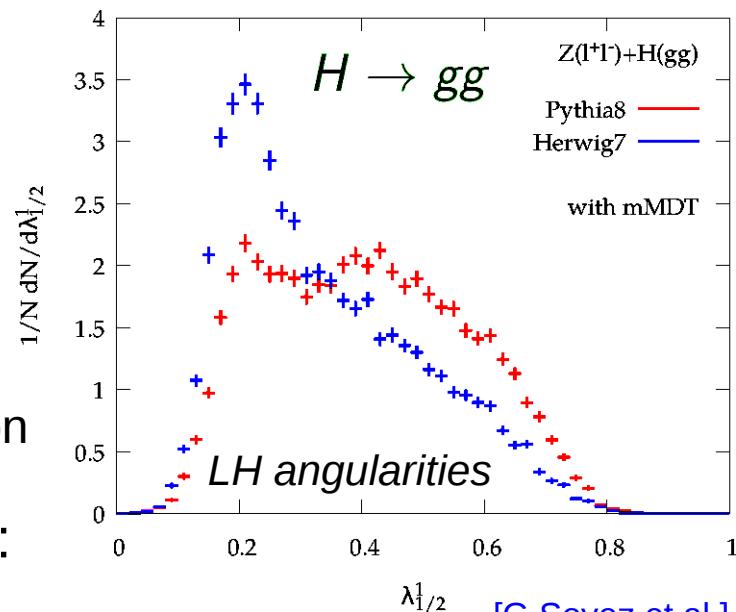
- ▶ Vary jet radius: small-R down to calo resolution

- Multiple high-precision analyses at hand:

- BSM: Improve  $q/g/Q$  discrimination tools

- pQCD: Check  $N^nLO$  antenna functions. High-precision QCD coupling.

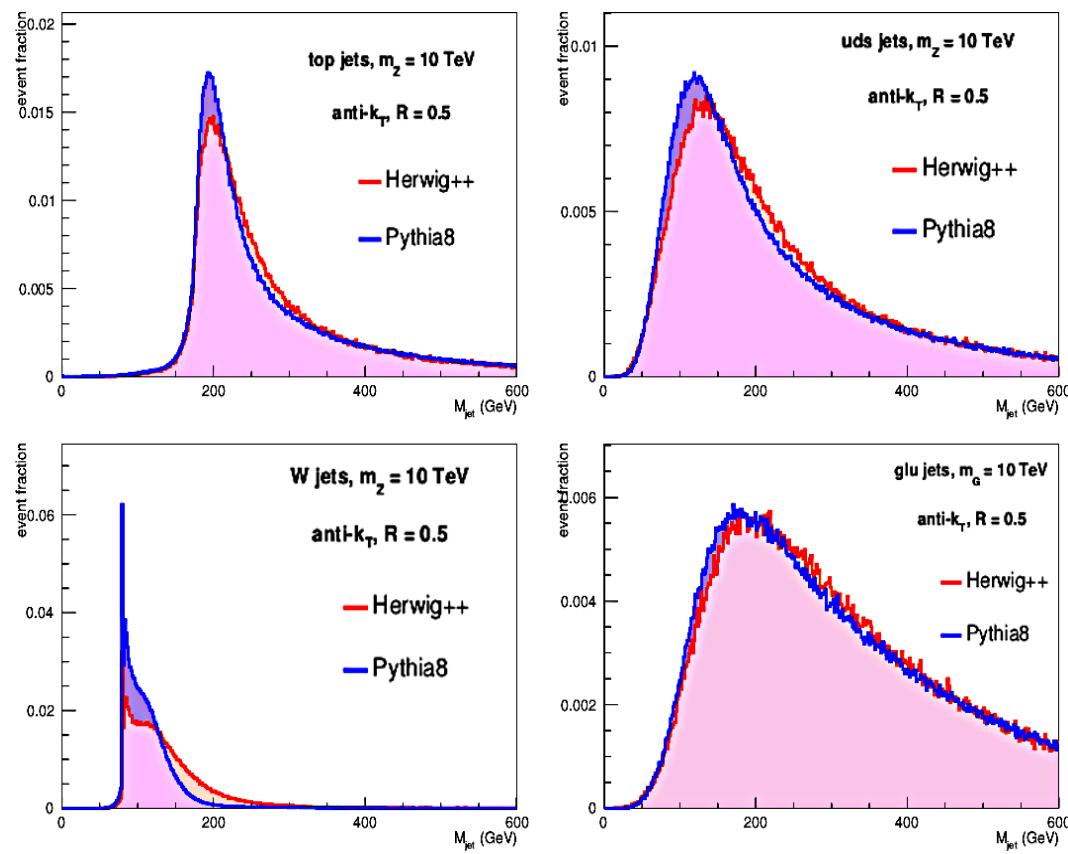
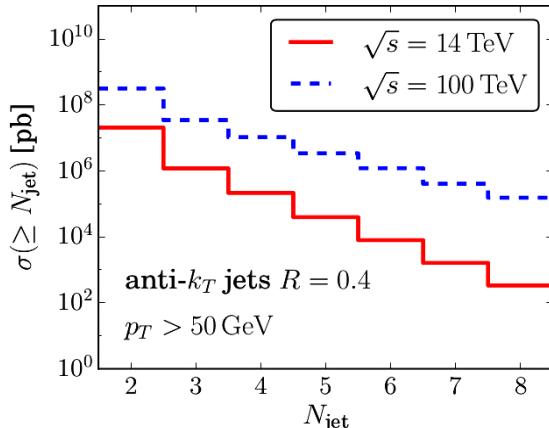
- non-pQCD: Gluon fragmentation: Octet neutralization? (zero-charge gluon jet with rap gaps). Colour reconnection? Glueballs ? Leading  $\eta$ 's,baryons?



# Highly-boosted jets, multijets (FCC-pp)

- Proton-proton collisions at 100 TeV provide **unique conditions** to produce & study **highly-boosted objects**: top, W, Z, H,  $R_{\text{BSM}}(\text{jj})$ ,...  
Resolving **small angular dijet sep.**  $\Delta R \approx 2M(\text{jj})/p_T(\text{j})$ .
- Jet substructure: key to separate **dijets from QCD & (un)coloured resonance decays**, e.g.  
 $R_{10-\text{TeV}} \rightarrow t\bar{t}, q\bar{q}, gg, WW$
- Diffs. in MC generators for **quark vs. gluon jets**  
(& jet radius).
- Also **unique multijet ( $N >> 10$ )**

BSM,  
QCD  
studies



[FCC-pp, arXiv:1607.01831]

# Physics at FCC $e^+e^-$ & $pp$ machines

(1) QCD:  $\alpha_s$  coupling

(2) QCD: Parton Distribution Functions

(3) QCD: Jet substructure & flavour tagging

(4) QCD: Non-perturbative regime

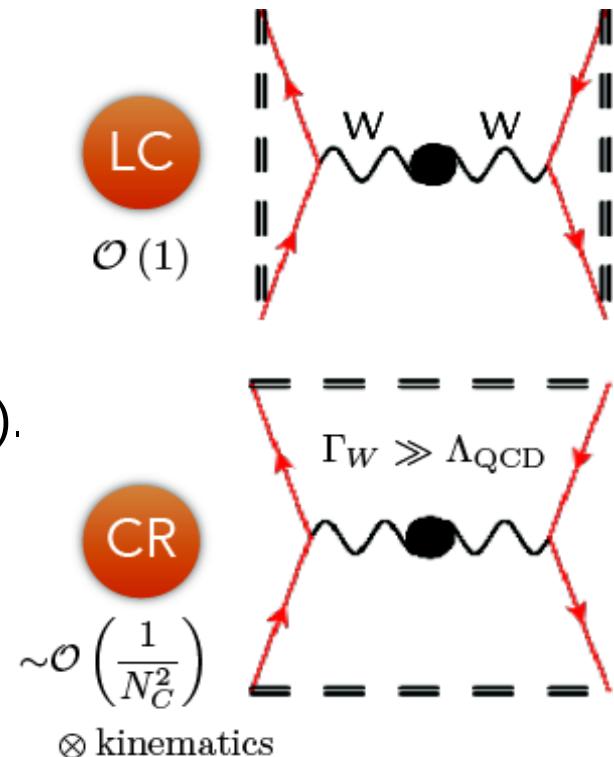
(5) Higgs sector

(6) BSM searches

# Colour reconnection

- Colour reconnection among partons is source of uncertainty in  $m_W$ ,  $m_{top}$ , aGC extractions in multijet final-states. Especially in pp (MPI cross-talk).

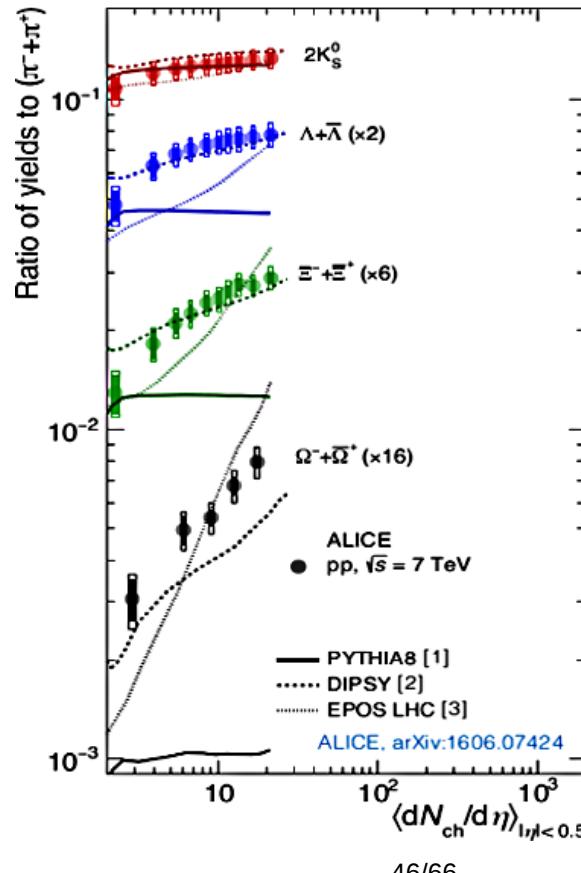
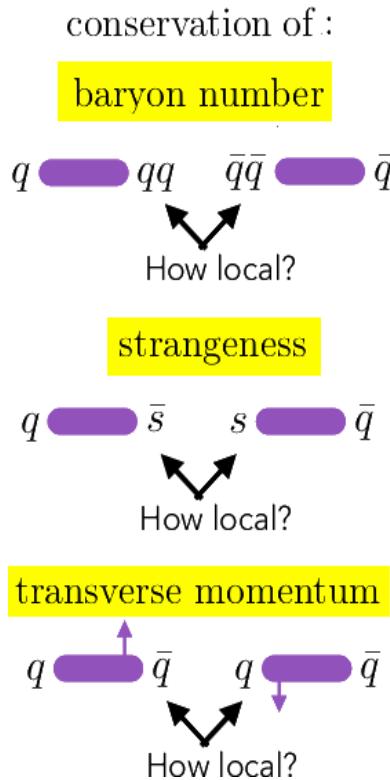
- ▶ CR impacts all FCC-ee multi-jet final-states (potentially shifted angular correlations):
  - $e^+e^- \rightarrow WW(4j)$ ,  $Z(4j)$ , ttbar,
  - H(2j,4j) CP studies,...
  - String-drag effect on W mass  
(Hinted at LEP: No-CR excluded at 99% CL).



- ▶ Exploit huge W stats ( $\times 10^4$  LEP) to “turn the  $m_W$  measurement around”: Determine  $m_W$  leptonically and constrain CR in hadronic WW: Colour reconnection controlled to <1%

# Other non-pQCD phenomena

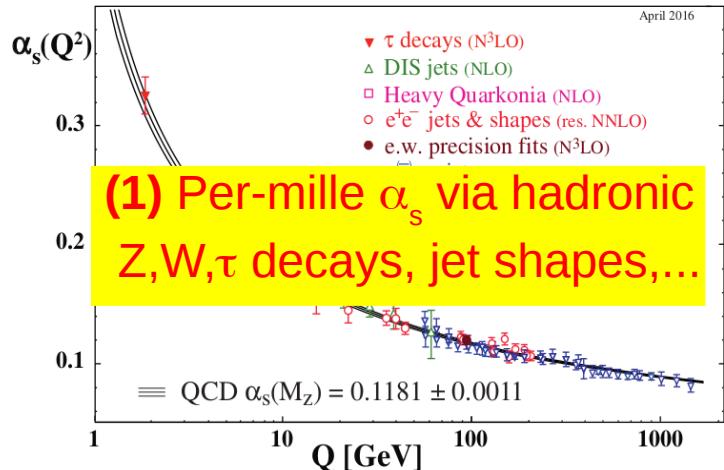
- High-precision low- $p_T$  PID hadrons in  $e^+e^-$ , pp for detailed studies:
  - Baryon & strangeness production. Colour string dynamics.
  - Final-state correlations (spin: BE, FD; momenta; space)
  - Bound state formation: Onia, multi-quark states, glueballs, ...



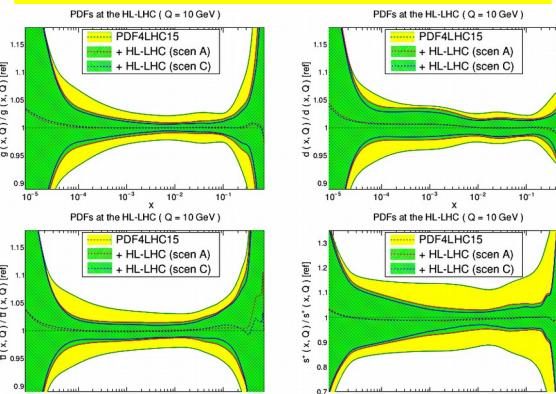
- ▶ Understand breakdown of universality of parton hadronization observed at LHC.
- Baseline vacuum  $e^+e^-$  studies for high-density QCD in small & large systems.

# Partial summary: QCD at FCC-ee & FCC-pp

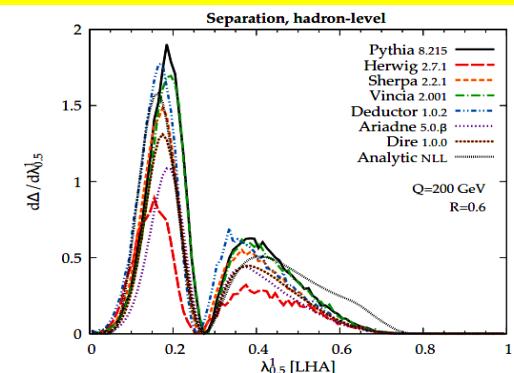
- The precision needed to fully exploit all future ee/pp/ep/eA/AA SM & BSM programs requires exquisite control of pQCD & non-pQCD physics.
- Unique QCD precision studies accessible at FCC-ee, FCC-pp:



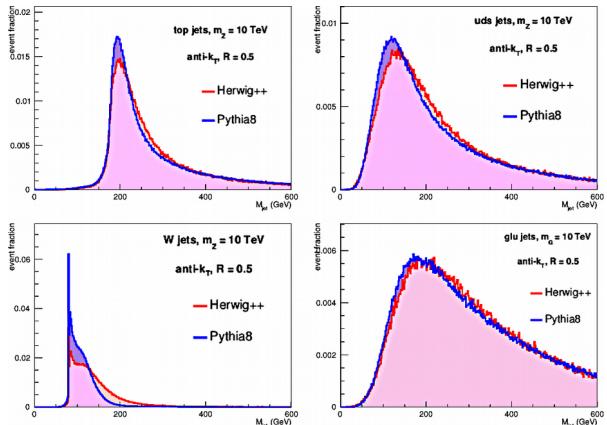
## (2) High-precision PDFs



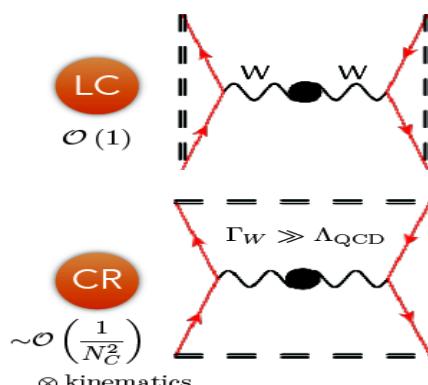
## (3) N<sup>n</sup>LO+N<sup>n</sup>LL jet struct. High g/q/Q discrimination



## (4) Unique studies of highly-boosted dijet & multijets

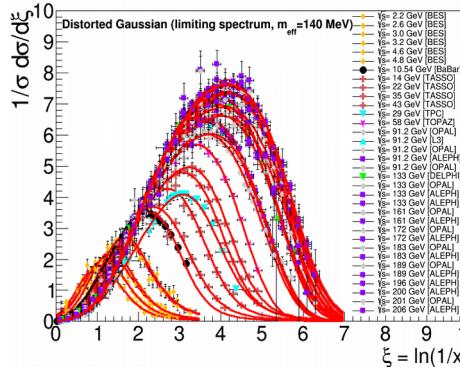
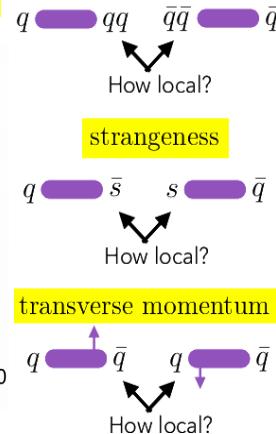


## (5) <1% control of colour reconnection



## (6) High-precision hadronization:

conservation of:  
baryon number



# Physics at FCC e<sup>+</sup>e<sup>-</sup> & pp machines

(1) QCD:  $\alpha_s$  coupling

(2) QCD: Parton Distribution Functions

(3) QCD: Jet substructure & flavour tagging

(4) QCD: Non-perturbative regime

(5) Higgs sector

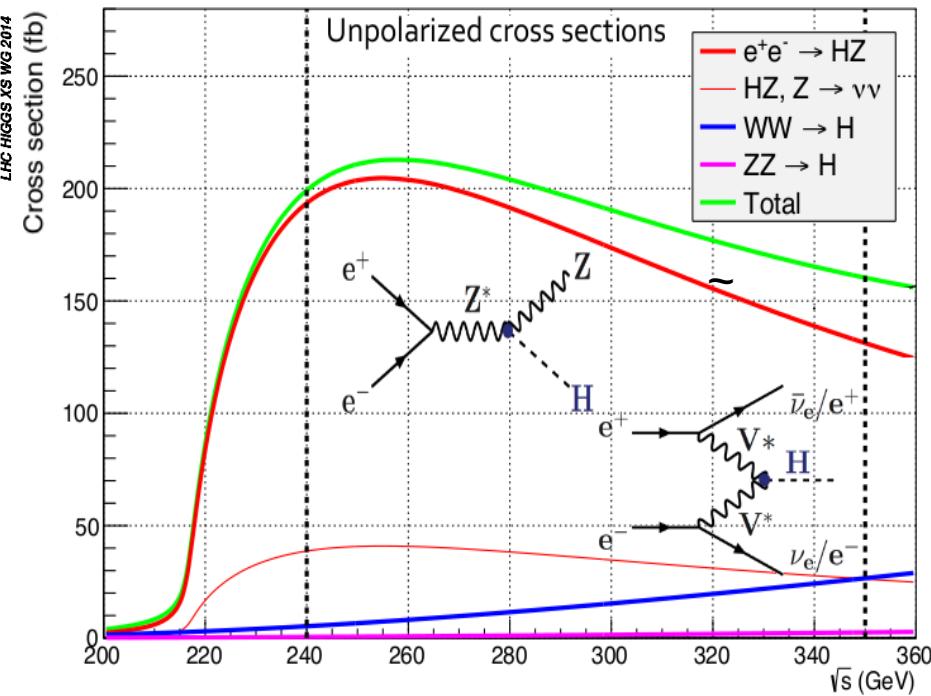
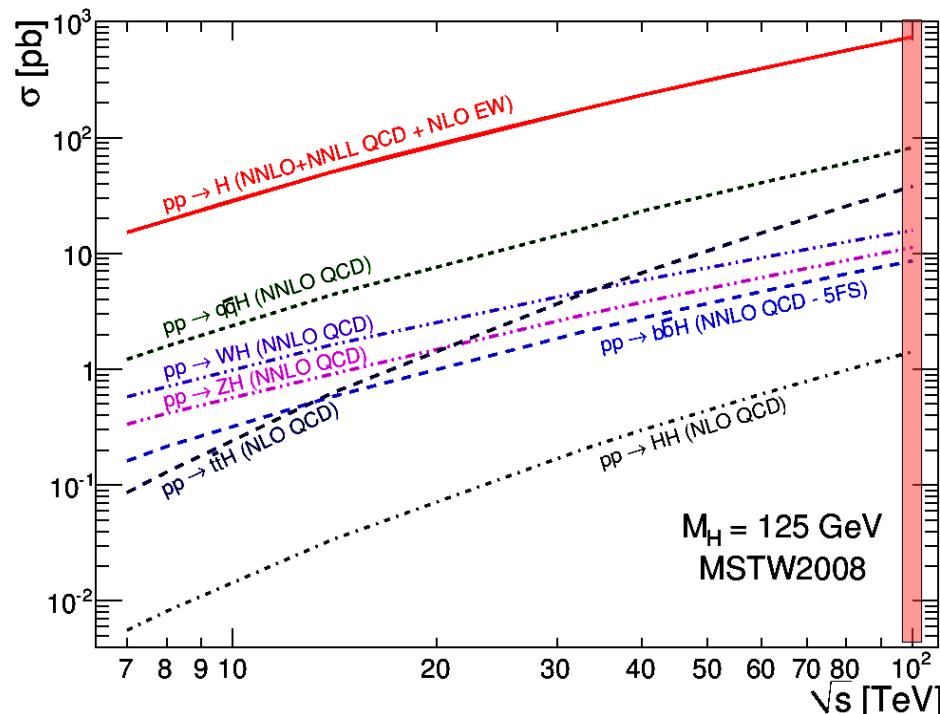
(6) BSM searches

# Higgs physics at FCC-pp & FCC-ee

- Huge number of Higgs expected:  $2 \cdot 10^{10}$  (FCC-pp),  $1.2 \cdot 10^6$  (FCC-ee)

$\sigma(pp \rightarrow H + X) \approx 0.9 \text{ nb}$  (ttH/HH/HHH access)

$\sigma(e^+e^- \rightarrow H + X) \approx 200 \text{ fb}$  (low bckgd, no pileup)



	$gg \rightarrow H$	VBF	$WH$	$ZH$	$ttH$	$HH$
$\sigma_{100}$ [pb]	802	69	16	11	32	1.9
$\sigma_{100}/\sigma_{14}$	x17	x16	x10	x11	x52	x40

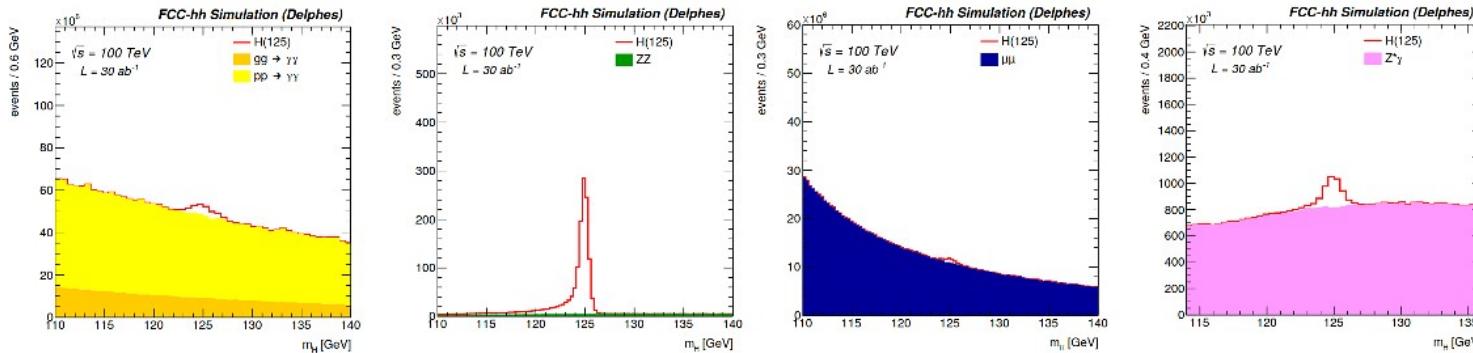
Total Integrated Luminosity (ab $^{-1}$ )	5
Number of Higgs bosons from $e^+e^- \rightarrow HZ$	1,200,000
Number of Higgs bosons from boson fusion	50,000

- H couplings (down to 0.2%), rare & BSM decays, and H self-coupling

# Rare & invisible Higgs decays (FCC-pp)

CERN-ACC-2018-0045

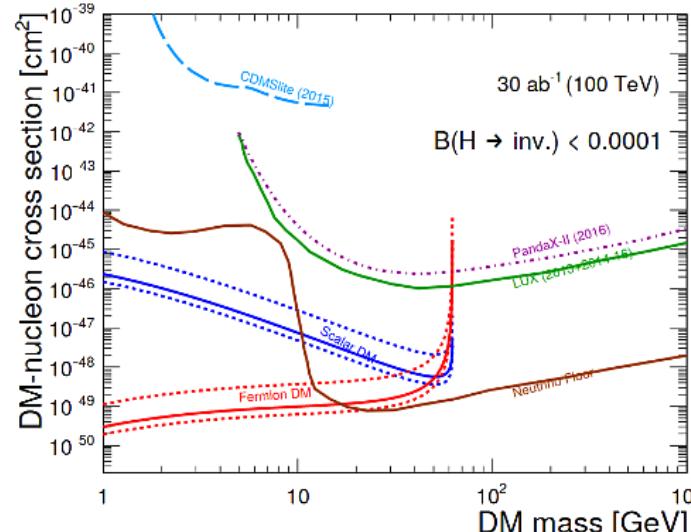
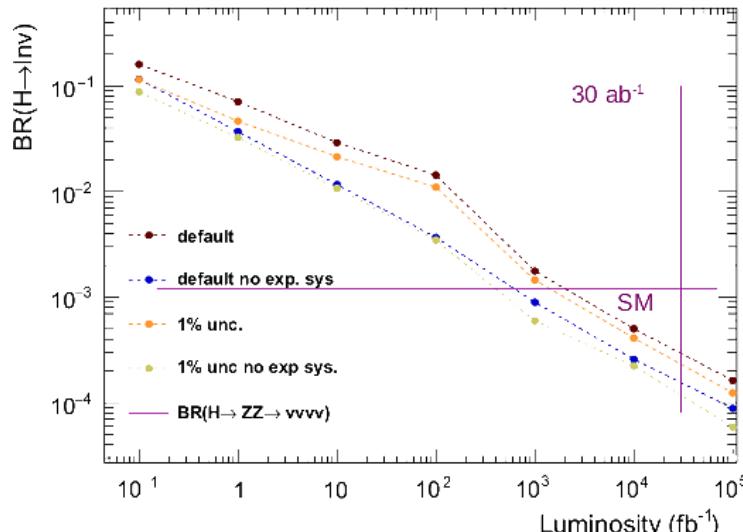
- Complementary measurements of  $H \rightarrow \gamma\gamma$ ,  $H \rightarrow ZZ \rightarrow 4\ell$ ,  $H \rightarrow \mu\mu$ ,  $H \rightarrow Z\gamma \rightarrow \ell\ell\gamma$



BRs  
precision:  
1–2%

- $H + \text{large } E_T^{\text{miss}}$  BR( $H \rightarrow \text{inv}$ ) from precise fit the  $E_T^{\text{miss}}$  spectrum

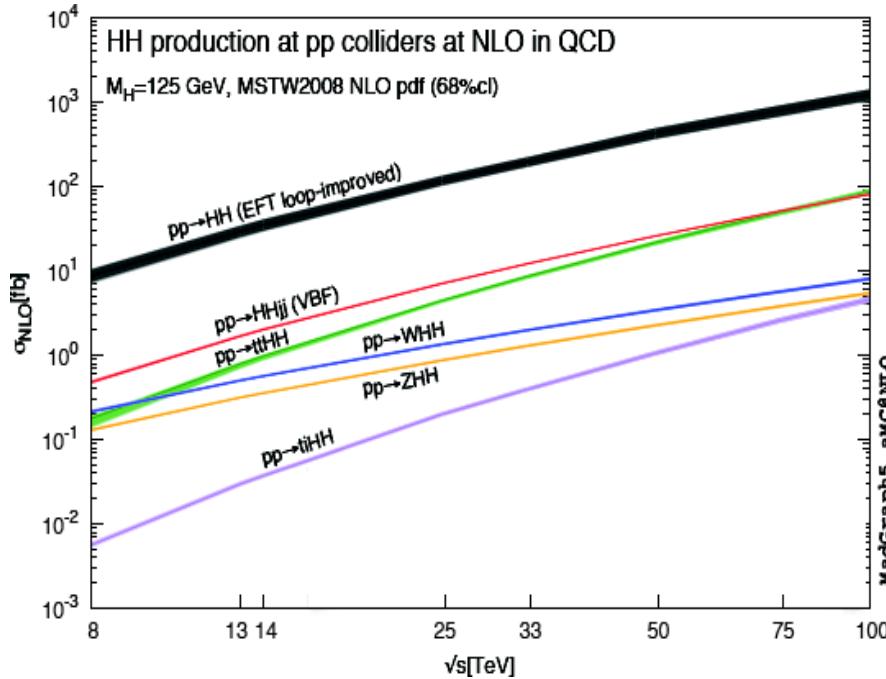
- background  $p_T$  spectrum from  $Z \rightarrow vv$  constrained to the % level
- ultimate precision:  $\text{BR}(H \rightarrow \text{inv}) < 2.5 \cdot 10^{-4}$  • SM ( $\text{BR}(H \rightarrow 4v) = 0.11\%$ ) reached with  $\sim 1 \text{ ab}^{-1}$



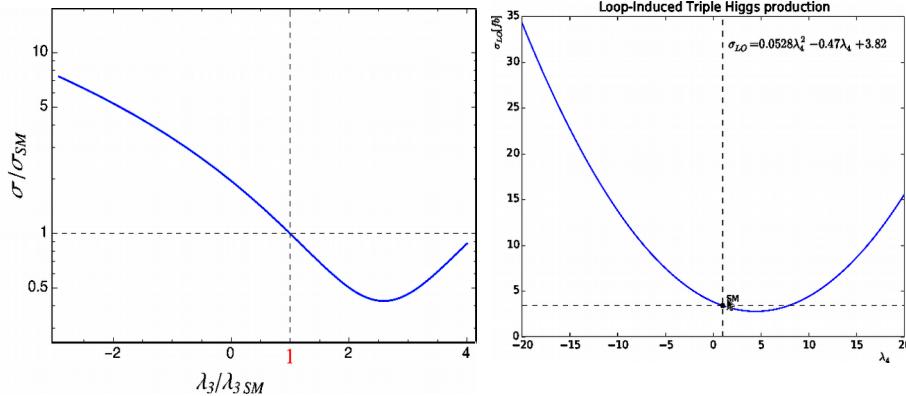
# Higgs self-couplings ( $\lambda_3, \lambda_4$ ) at FCC-pp

■ Double (triple) Higgs cross section  $\approx 1.9 \text{ pb}$  (5 fb)

[R. Contino et al.,  
arXiv:1606.09408]



But various diagrams contribute to  
 $\sigma_{\text{HH}}, \sigma_{\text{HHH}}$ : ~diluted sensitivity to  $\lambda_3, \lambda_4$



■  $b\bar{b}(b\bar{b})\gamma\gamma$  most sensitive channel:  
Critical flavor-tagging performances.

■ Precisions on coupling:  
Trilinear ( $g_{\text{HH}}$ )~3–6%  
Quartic ( $g_{\text{HHH}}$ ) mildly constrained:  $2\sigma$

process	precision on $\sigma_{\text{SM}}$	68% CL interval on Higgs self-couplings
$HH \rightarrow b\bar{b}\gamma\gamma$	3%	$\lambda_3 \in [0.97, 1.03]$
$HH \rightarrow b\bar{b}b\bar{b}$	5%	$\lambda_3 \in [0.9, 1.5]$
$HH \rightarrow b\bar{b}4\ell$	$O(25\%)$	$\lambda_3 \in [0.6, 1.4]$
$HH \rightarrow b\bar{b}\ell^+\ell^-$	$O(15\%)$	$\lambda_3 \in [0.8, 1.2]$
$HH \rightarrow b\bar{b}\ell^+\ell^-\gamma$	—	—
$HHH \rightarrow b\bar{b}b\bar{b}\gamma\gamma$	$O(100\%)$	$\lambda_4 \in [-4, +16]$

# Higgs self-couplings ( $\lambda_3, \lambda_4$ ) at FCC-pp

- 1D maximum likelihood fits of the BDT discriminants

68% CL uncertainty on  $\kappa_\lambda$ :

bb $\gamma\gamma$	bb $\pi\pi$	bbbb	combined
3.5-8.5%	12-13%	24-26%	2.9-5.5%

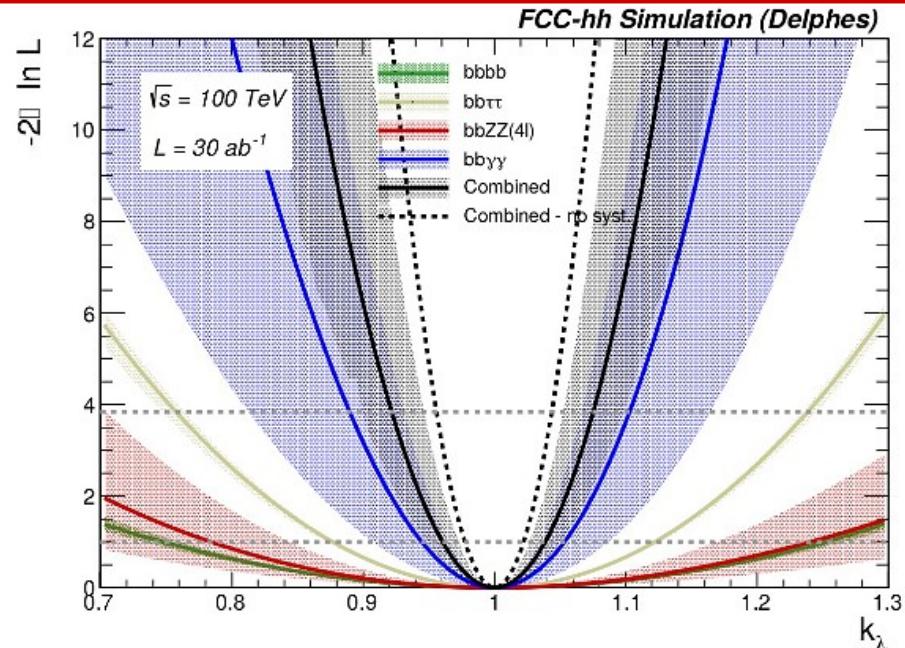
- driven by the bb $\gamma\gamma$  channel, limited by systematics

- A few remarks:

- small impact of (eg QCD) background relies on the fact that the data will help to constrain the normalisations
- precision achievable only if good measurements of other couplings:  
1% uncertainty on  $y_t \Rightarrow$  5% uncertainty on  $\kappa_\lambda$
- uncertainty on  $\sigma_{HH}$ : 0.5%-1.5% (~5% today): needs at least one order beyond NLO with full top-mass dependence, possibly beyond N<sup>3</sup>LO in the infinite top-mass limit

- Evolution with luminosity:

- 10% precision achievable with 3 ab<sup>-1</sup> of data, ie a 3-5 year early run



# Higgs self-coupling ( $\lambda_3$ ) at FCC-ee

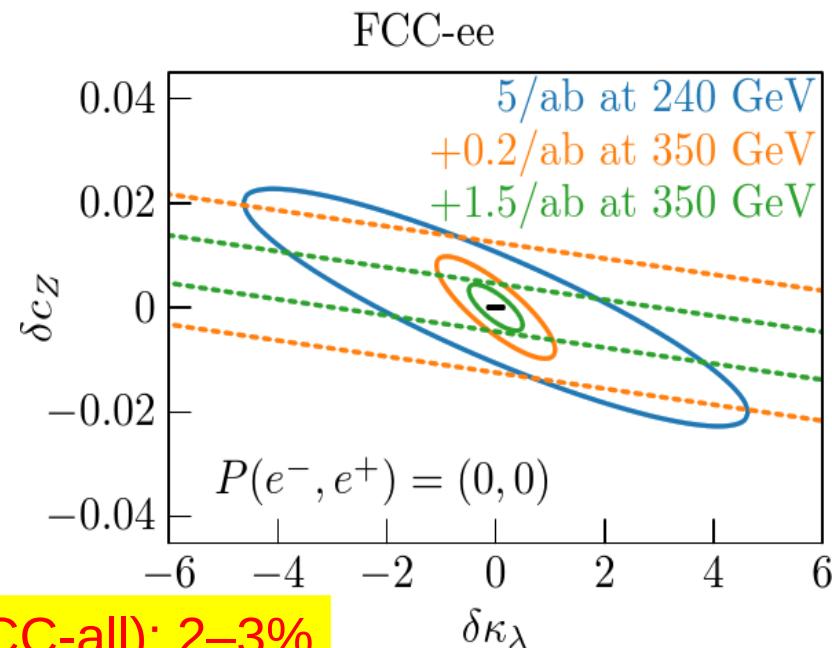
- Higgs trilinear indirectly constrained through loop corrections to  $\sigma(H+Z)$ :

$$\sigma_{Zh} = \left| e \bar{e} \rightarrow Z \rightarrow h \right|^2 + 2 \operatorname{Re} \left[ \delta_Z^{240} = 100 (2\delta_Z + 0.014\delta_h) \% \right]$$

[M. McCullough, 2014]

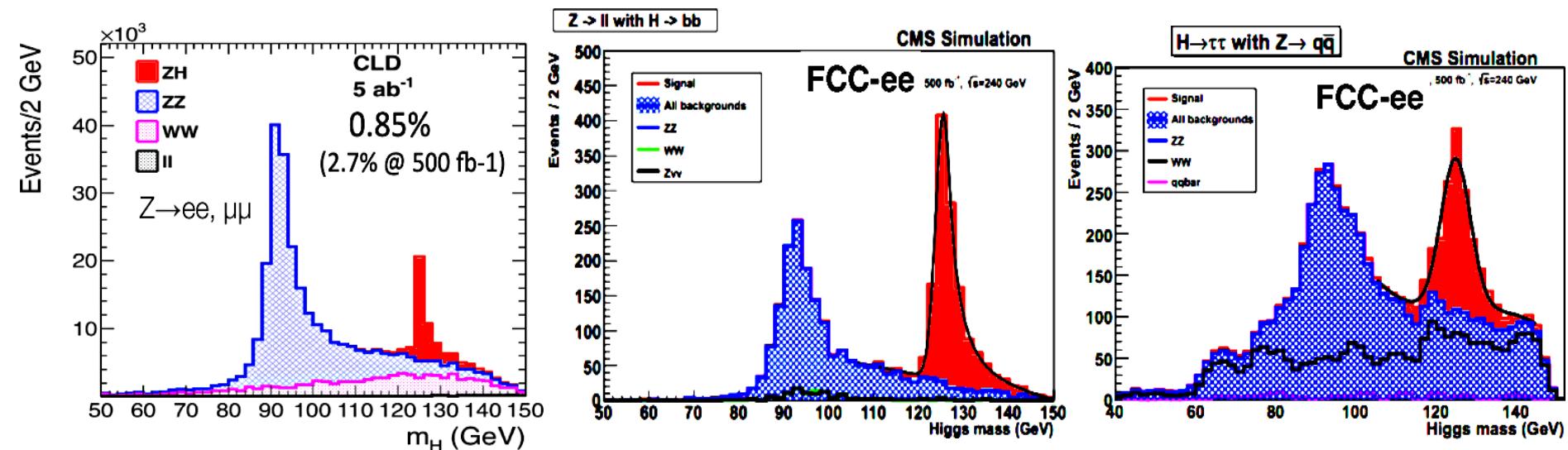
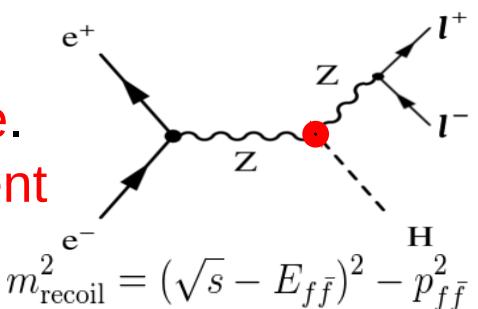
Self-coupling correction  $\delta_h$ : energy-dependent  
 $\delta_z$ : energy-independent (distinguishable).

- Tiny effect, but visible thanks to extreme (0.4%) precision on  $\sigma_{Zh}$  coupling reachable at FCC-ee.
- Indirect limits on trilinear  $\lambda$  coupling at ~40% level combining 240+350GeV
- Final Higgs self-coupling precision (FCC-all): 2–3%



# Precision H couplings, width, mass (FCC-ee)

- Recoil method in  $H-Z(l\bar{l})$  unique to lepton collider: reconstruct  $H$  4-mom. independent of  $H$  decay mode.
- High-precision (0.4%)  $\sigma_{ZH}$  provides model-independent  $g_z$  coupling:  $\sigma(ee \rightarrow ZH) \propto g_z^2$ , with  $\pm 0.2\%$  uncert.



- Total width ( $\Gamma_H$ ) with  $\sim 1\%$  precision by combining  $\sigma(ZH)$  and  $BR(H \rightarrow ZZ)$ :
- $$\sigma(ee \rightarrow ZH) BR(H \rightarrow ZZ) \propto \frac{g_{HZZ}^4}{\Gamma} \Rightarrow \Gamma$$
- Rest of Yukawa from other decays:  $\sigma(ee \rightarrow ZH) BR(H \rightarrow XX) \propto \frac{g_{HZZ}^2 g_{HXX}^2}{\Gamma} \Rightarrow g_{HXX}^2$

# Precision Higgs couplings (FCC-ee,FCC-pp)

- FCC-ee provides **x2–20 improvement** in couplings uncertainties w.r.t. (model-dependent) HL-LHC expectations (2–5%):

Collider	HL-LHC	FCC-ee <sub>240→365</sub>	FCC-INT
Lumi (ab <sup>-1</sup> )	3	5 + 0.2 + 1.5	30
Years	10	3 + 1 + 4	25
$g_{HZZ}$ (%)	1.5	0.18 / 0.17	0.17/0.16
$g_{HWW}$ (%)	1.7	0.44 / 0.41	0.20/0.19
$g_{H\bar{b}b}$ (%)	5.1	0.69 / 0.64	0.48/0.48
$g_{Hcc}$ (%)	SM	1.3 / 1.3	0.96/0.96
$g_{Hgg}$ (%)	2.5	1.0 / 0.89	0.52/0.5
$g_{H\tau\tau}$ (%)	1.9	0.74 / 0.66	0.49/0.46
$g_{H\mu\mu}$ (%)	4.4	8.9 / 3.9	0.43/0.43
$g_{H\gamma\gamma}$ (%)	1.8	3.9 / 1.2	0.32/0.32
$g_{HZ\gamma}$ (%)	11.	– / 10.	0.71/0.7
$g_{Htt}$ (%)	3.4	10. / 3.1	1.0/0.95
$g_{HHH}$ (%)	50.	44./33. 27./24.	2-3 <sup>(*)</sup>
$\Gamma_H$ (%)	SM	1.1	0.91
BR <sub>inv</sub> (%)	1.9	0.19	0.024
BR <sub>EXO</sub> (%)	SM (0.0)	1.1	1

} ee,ep  
} hh  
} ee  
} hh  
} ee

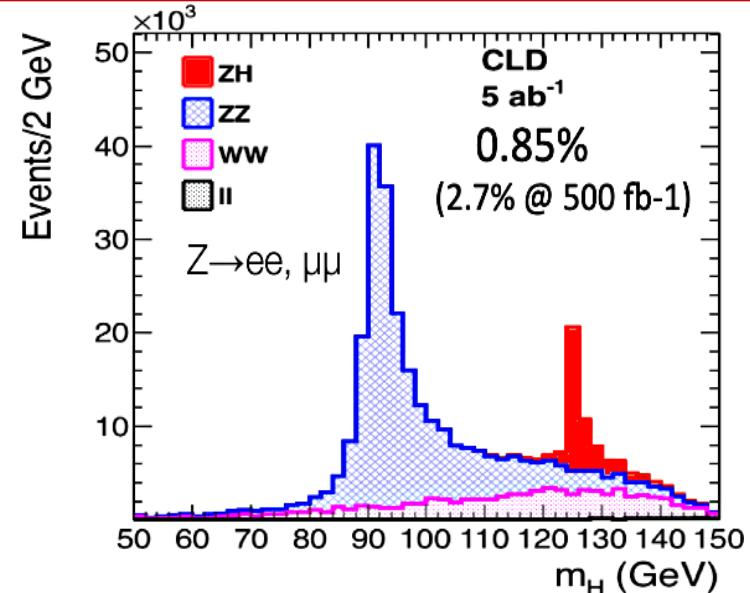
- Most precise  $g_{zz} \approx 0.17\%$  coupling sets limit on new scalar-coupled physics at:  $\Lambda \gtrsim (1 \text{ TeV}) / \sqrt{(\delta g_{HXX}/g_{HXX}^{\text{SM}})/5\%} > 6 \text{ TeV}$

# Few-MeV $m_H$ mass determination (FCC-ee)

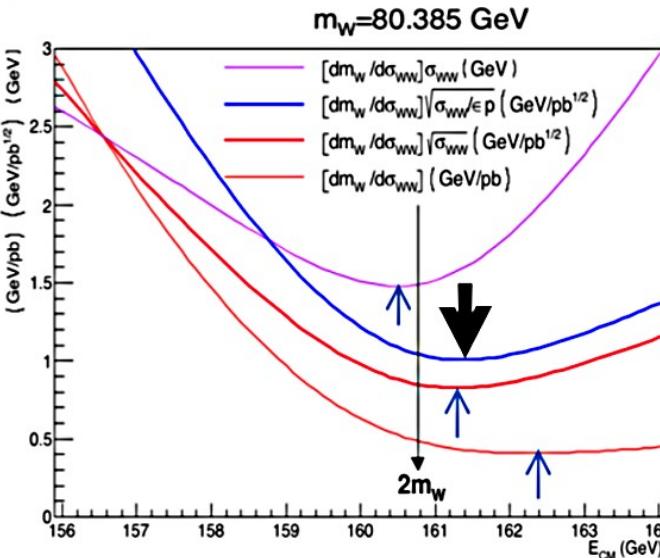
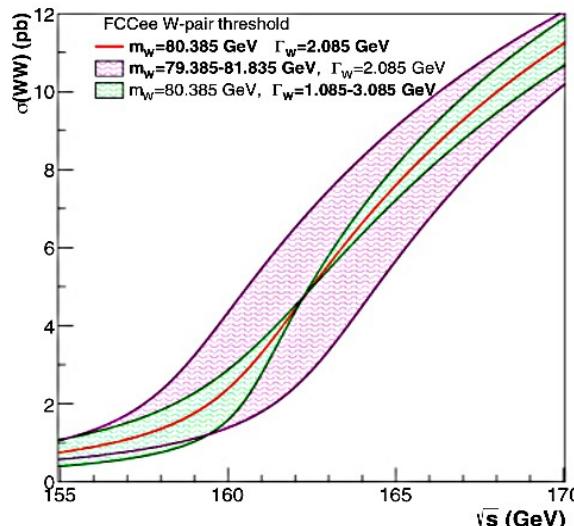
- $e^+e^- \rightarrow H Z(l^+l^-)$  recoil method:  
allows Higgs mass reconstruction  
with  $\delta m_H = 8$  MeV in  $Z \rightarrow \mu^+\mu^-$

$$m_{\text{recoil}}^2 = (\sqrt{s} - E_{f\bar{f}})^2 - p_{f\bar{f}}^2 = s - 2E_{f\bar{f}}\sqrt{s} + m_{f\bar{f}}^2$$

( $\delta m_H = \pm 5$  MeV adding other decays)



- Can  $m_H$  be accurately reconstructed via  $\sigma(HZ)$  line shape scan? Like done for  $m_W$  via  $e^+e^- \rightarrow W^+W^- \dots$



With 7/fb @ 162.6 GeV:  
 $\delta m_W(\text{stat}) = \pm 0.5$  MeV

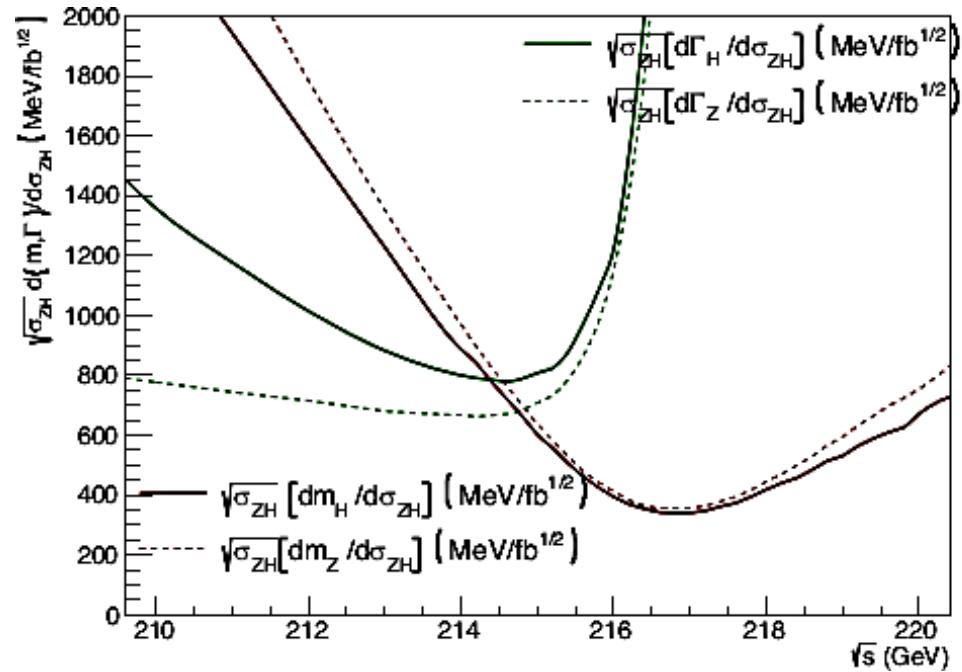
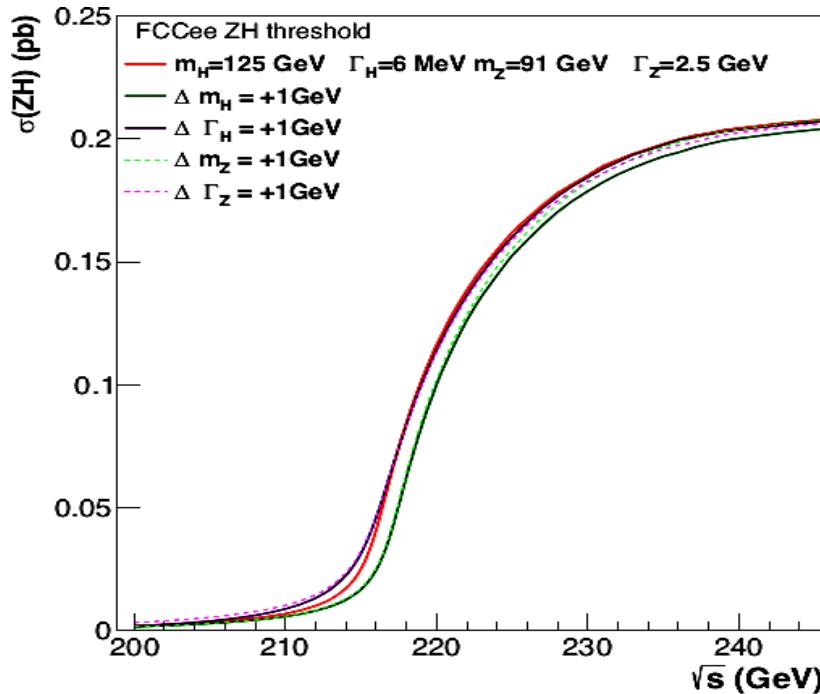
Need systematics control:

- $\delta E_{\text{beam}} < 0.5$  MeV ( $6 \cdot 10^{-6}$ )
- $\delta \varepsilon / \varepsilon, \delta L / L < 2 \cdot 10^{-4}$ )
- $\delta \sigma_B < 1$  fb ( $2 \cdot 10^{-3}$ )

[arXiv:1703.01626  
arXiv:1909.12245]

# Few-MeV $m_H$ mass determination (FCC-ee)

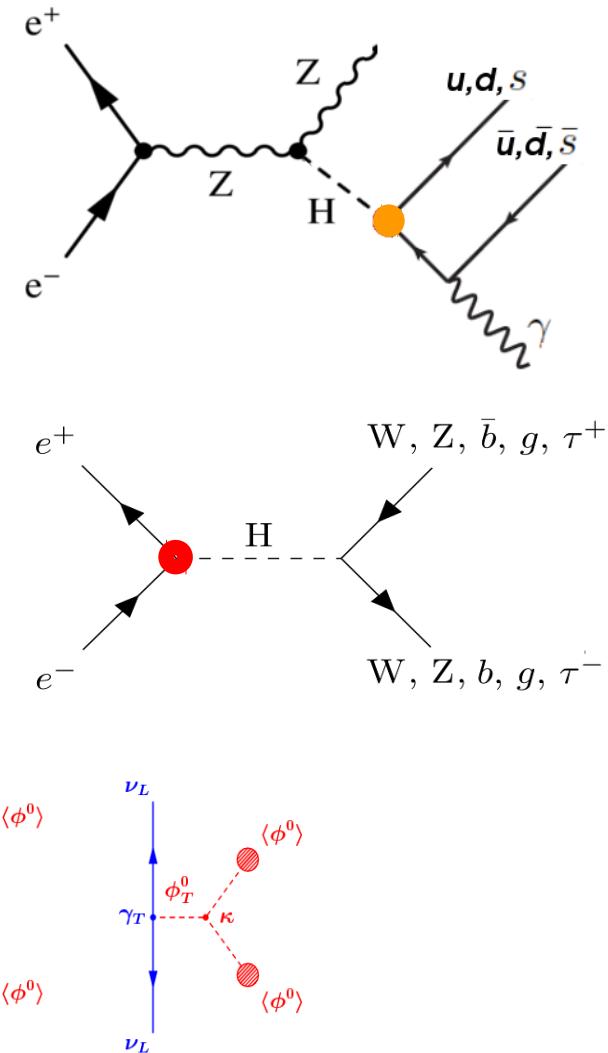
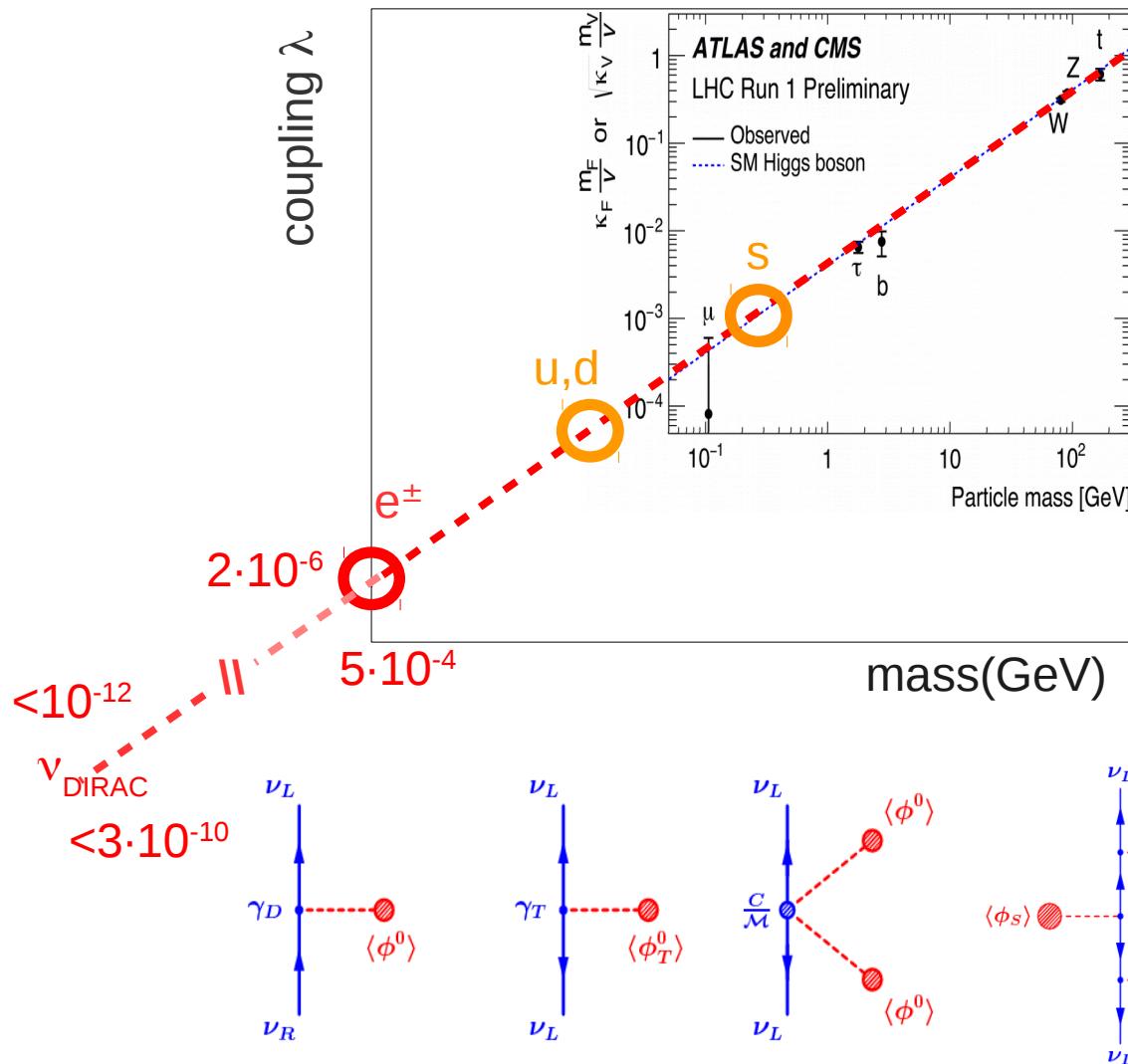
- Can  $m_H$  be accurately reconstructed via  $\sigma(HZ)$  line shape scan?
- Preliminary MG5@NLO studies (Paolo Azzurri):



- Optimal data-taking point for  $\min \Delta m_H(\text{stat})$ :  $\sqrt{s} \simeq m_Z + m_H - 0.2 \simeq 217 \text{ GeV}$
- $\sqrt{\sigma_{ZH}} (dm_H / d\sigma_{ZH})_{\min} = 350 \text{ MeV/vfb}$       With 5/ab @ 217 GeV:  $\delta m_H = \pm 5 \text{ MeV}$
- Need systematics control:  $\delta E_{\text{beam}} < 5 \text{ MeV}$  ( $5 \cdot 10^{-5}$ ),  $\delta \epsilon / \epsilon$ ,  $\delta L / L < 10^{-3}$ ,  $\delta \sigma_B < 0.1 \text{ fb}$  ( $\sim 10^{-3}$ )
- Combining threshold HZ x-section with  $m_{HZ}$ (recoil) should give:  $\delta m_H = \pm 3.5 \text{ MeV}$

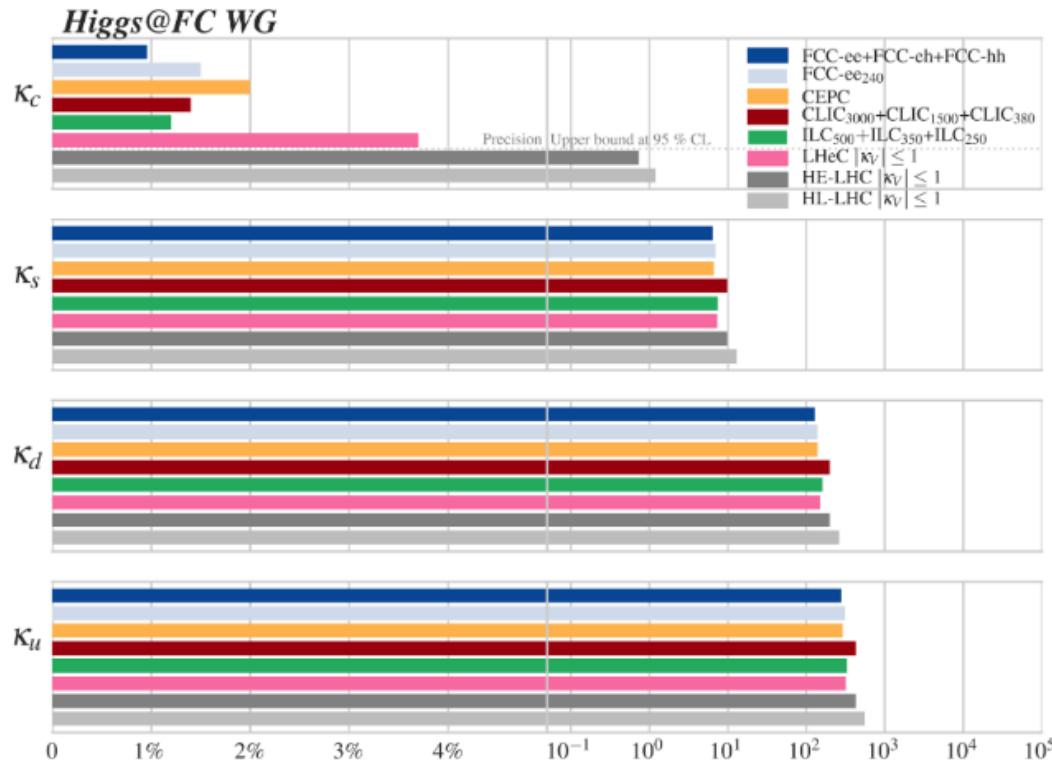
# Generation of lightest fermion (u,d,s,v's) masses?

- LHC can only access 3<sup>rd</sup> (plus few 2<sup>nd</sup>)-gen.Yukawas. What about the rest?



# Light quarks Yukawas (FCC-pp, FCC-ee)

- Constraints on light Yukawa obtained from the upper limits on BR to all untagged particles, using global fits in  $\kappa$  framework



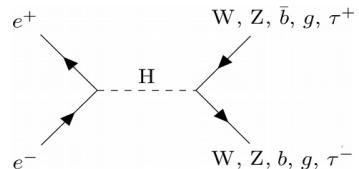
Limits from exclusive  
 $H \rightarrow VM(\rho, \omega\phi) + \gamma$   
decays (BR~ $10^{-6}$ )  
to be studied/added

- FCC-ee+eh+hh:

- first generation: 95% CL limits  $\kappa_u < 280$ ,  $\kappa_d < 130$
- second generation: 95% CL limit  $\kappa_s < 6.4$ ,  $\kappa_c$  measured with precision of  $< 1\%$

# e Yukawa via s-channel $e^+e^- \rightarrow H$ (FCC-ee)

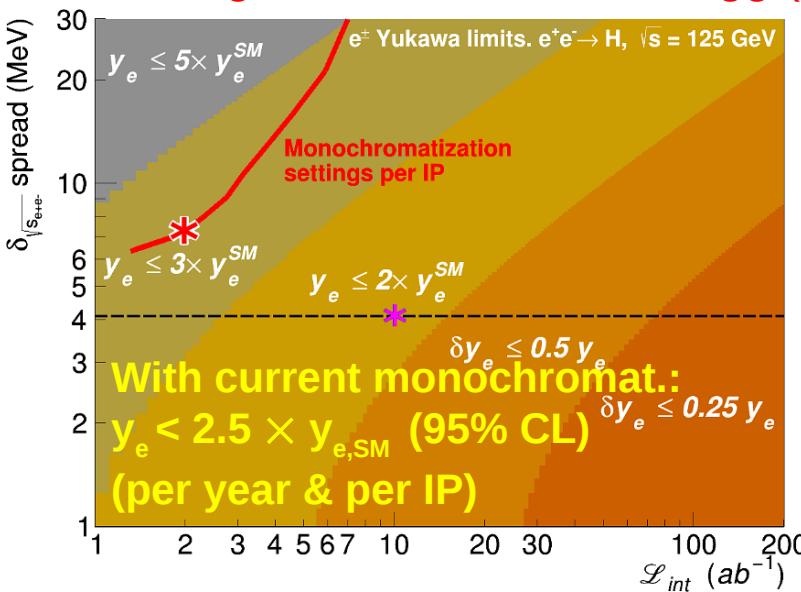
- Resonant s-channel Higgs production at FCC-ee ( $\sqrt{s} = 125.00$  GeV):



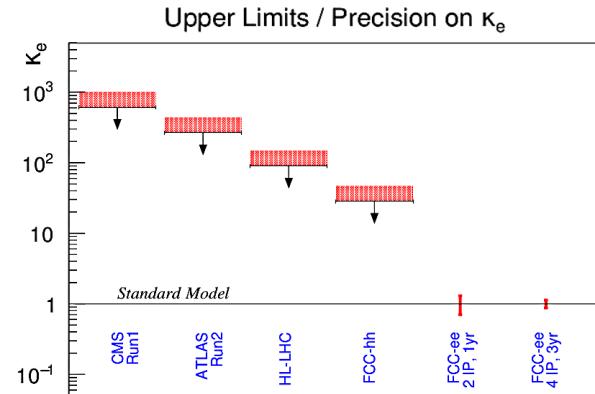
$$\sigma(e^+e^- \rightarrow H)_{B-W} = 1.64 \text{ fb}$$

$$\sigma(e^+e^- \rightarrow H)_{\text{spread}} = 280 \text{ ab} (\text{ISR} + \sqrt{s}_{\text{spread}} = \Gamma_H = 4.2 \text{ MeV})$$

- Prerequisite: Higgs mass extraction  $\delta m_H = O(3 \text{ MeV})$  via HZ @ 240,217 GeV
- Generator-level study for signal + backgrounds for 10 decay channels:  
Most significant channels:  $H \rightarrow gg$  (for light-q mistag  $\sim 1\%$ ),  $H \rightarrow WW^* \rightarrow l+jets$



For  $10 \text{ ab}^{-1}$  &  $\sqrt{s}_{\text{spread}} = \Gamma_H$ : Signif  $\approx 1.3\sigma$



- Monochromatization improvable beyond  $(\sqrt{s}_{\text{spread}}, L_{\text{int}}) \approx (7 \text{ MeV}, 2 \text{ ab}^{-1})$ ?
- Fundamental unique physics accessible:
  - Electron Yukawa coupling: Limits  $\times 100$  ( $\times 30$ ) better than HL-LHC (FCC-hh)
  - BSM scale affecting  $e^\pm$  Yukawa pushed up to  $\Lambda_{\text{BSM}} > 110 \text{ TeV}$

# Physics at FCC $e^+e^-$ & $pp$ machines

(1) QCD:  $\alpha_s$  coupling

(2) QCD: Parton Distribution Functions

(3) QCD: Jet substructure & flavour tagging

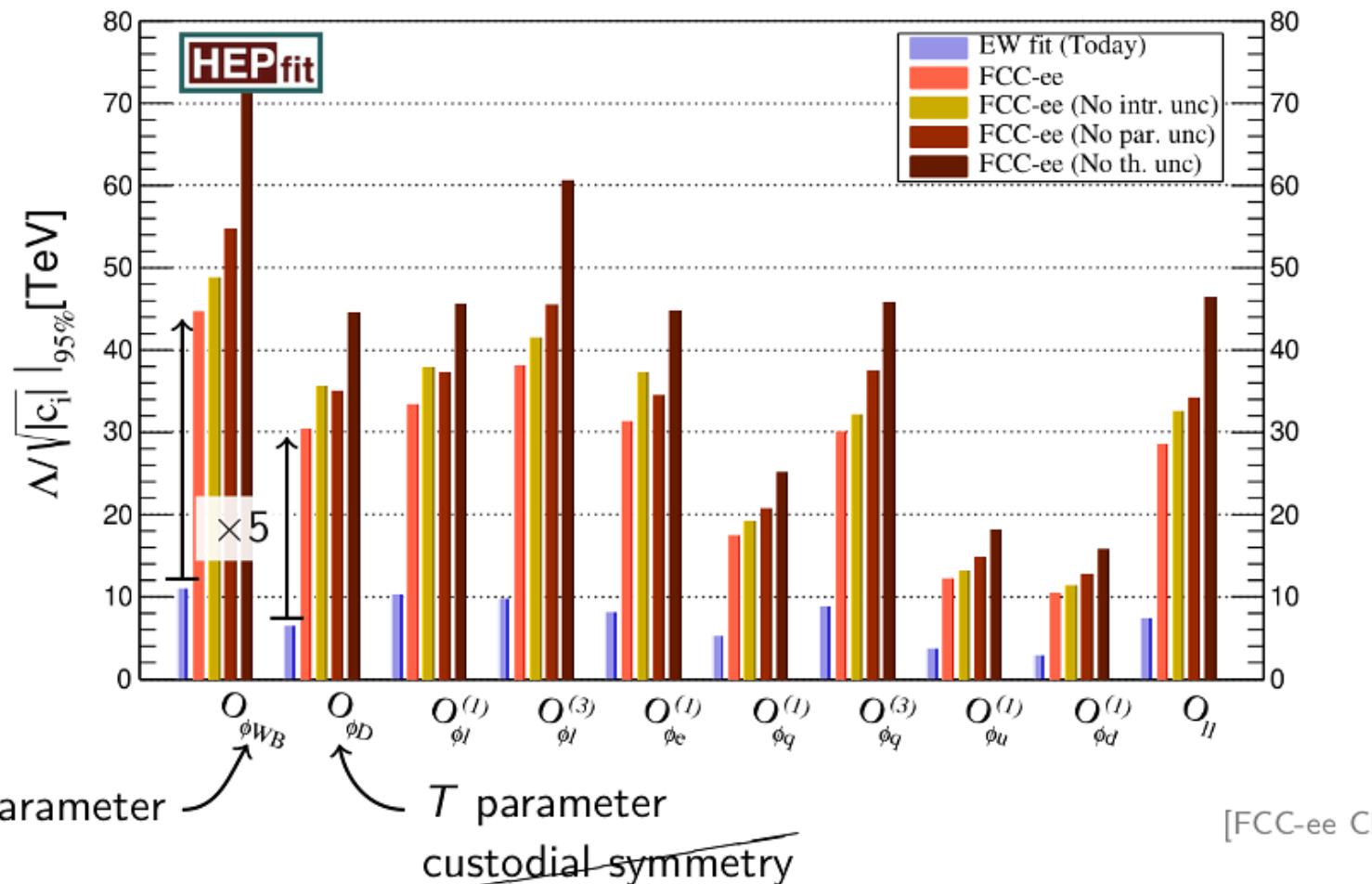
(4) QCD: Non-perturbative regime

(5) Higgs sector

(6) BSM searches

# Indirect BSM searches (EW coupled) at FCC-ee

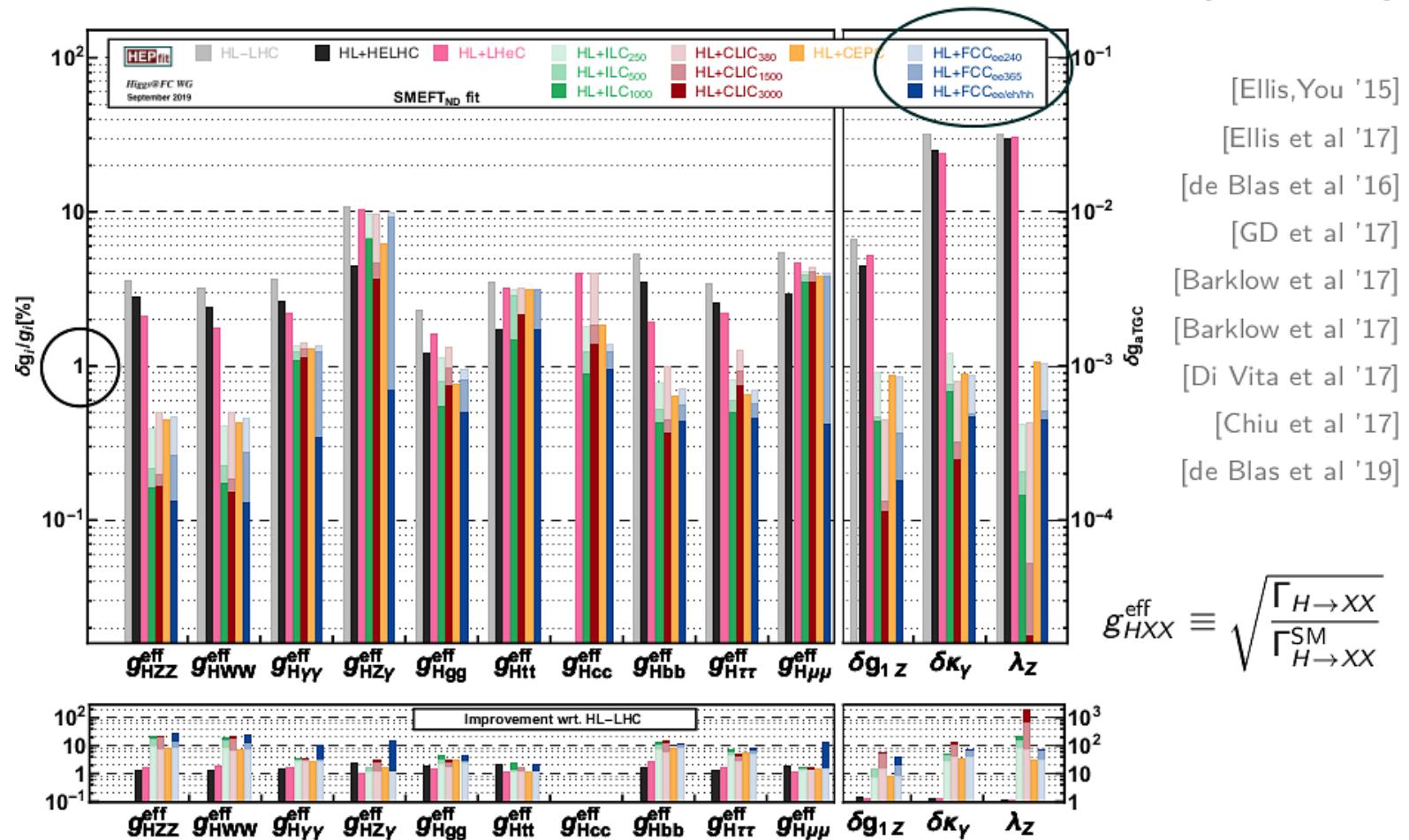
■ Indirect EW-coupled new physics EFT limits pushed up to  $O(50 \text{ TeV})$  thanks to ultraprecise EWPO measurements in  $e^+e^-$  collisions with  $10^{12} Z$ 's and  $10^8 W$ 's:  
 $(m_Z, \Gamma_Z, A_{\text{FB}}, R_x, \alpha(m_Z), m_W, m_t, \text{etc.})$



# Indirect BSM searches (Higgs coupled) at FCC

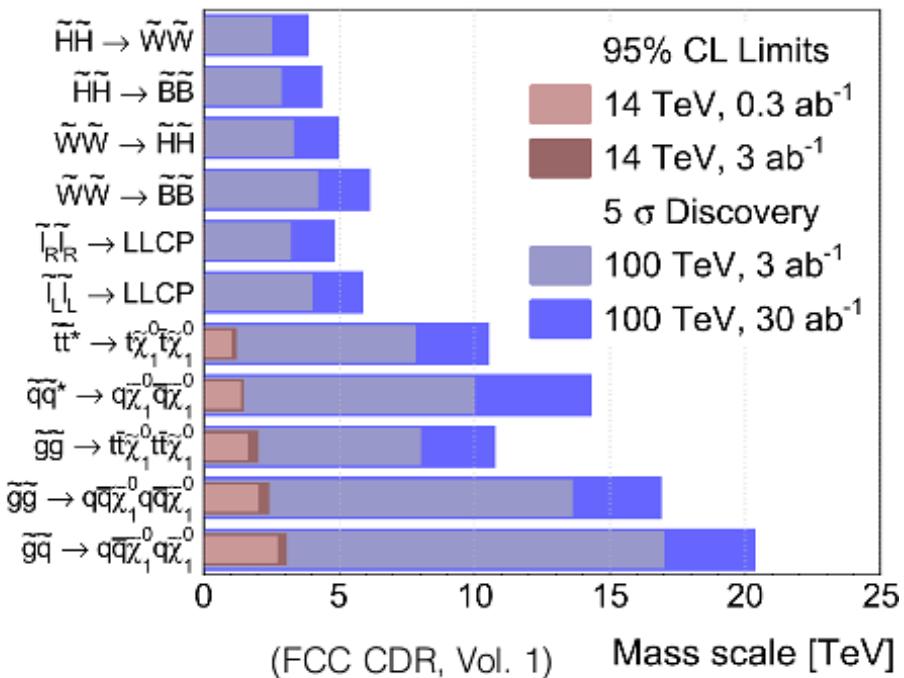
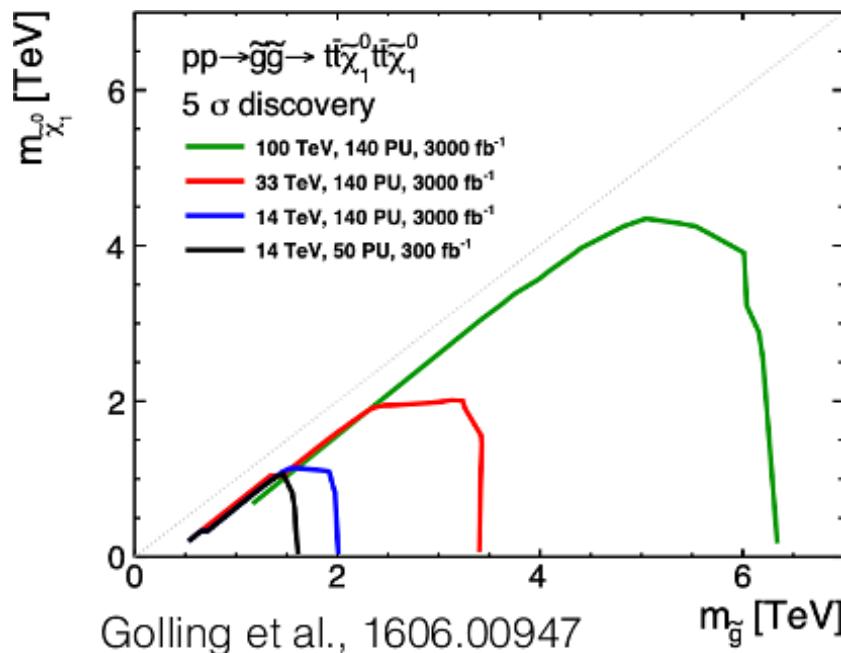
■ Indirect scalar-coupled new physics EFT limits pushed up to  $O(6 \text{ TeV})$  thanks to precision H partial widths down to permil level:

[Higgs@FC '19]



# Direct BSM searches at FCC-hh

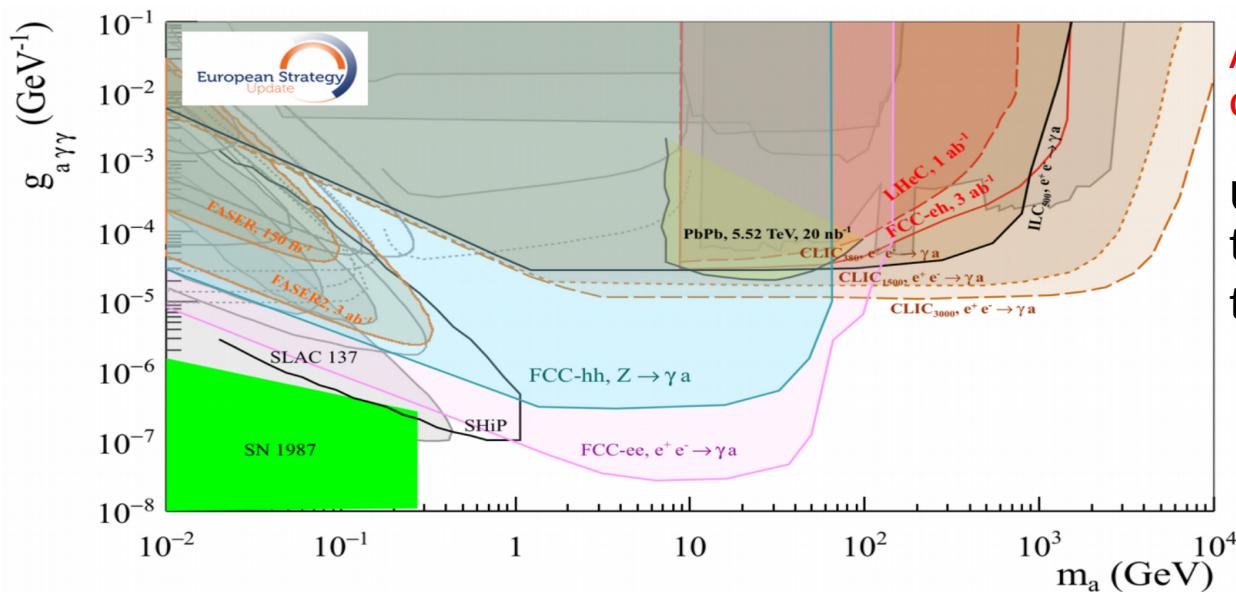
■ Direct heavy-mass reach (e.g. SUSY) in p-p at 100 TeV is  $\times(5\text{-}10)$  times LHC:



$\varepsilon$	High-scale mediation	Low-scale mediation
stop	$5 \times 10^{-5} \left(\frac{10 \text{ TeV}}{m_{\tilde{t}}}\right)^2$	$2 \times 10^{-3} \left(\frac{10 \text{ TeV}}{m_{\tilde{t}}}\right)^2$
gluino	$7 \times 10^{-6} \left(\frac{17 \text{ TeV}}{m_{\tilde{g}}}\right)^2$	$6 \times 10^{-3} \left(\frac{17 \text{ TeV}}{m_{\tilde{g}}}\right)^2$

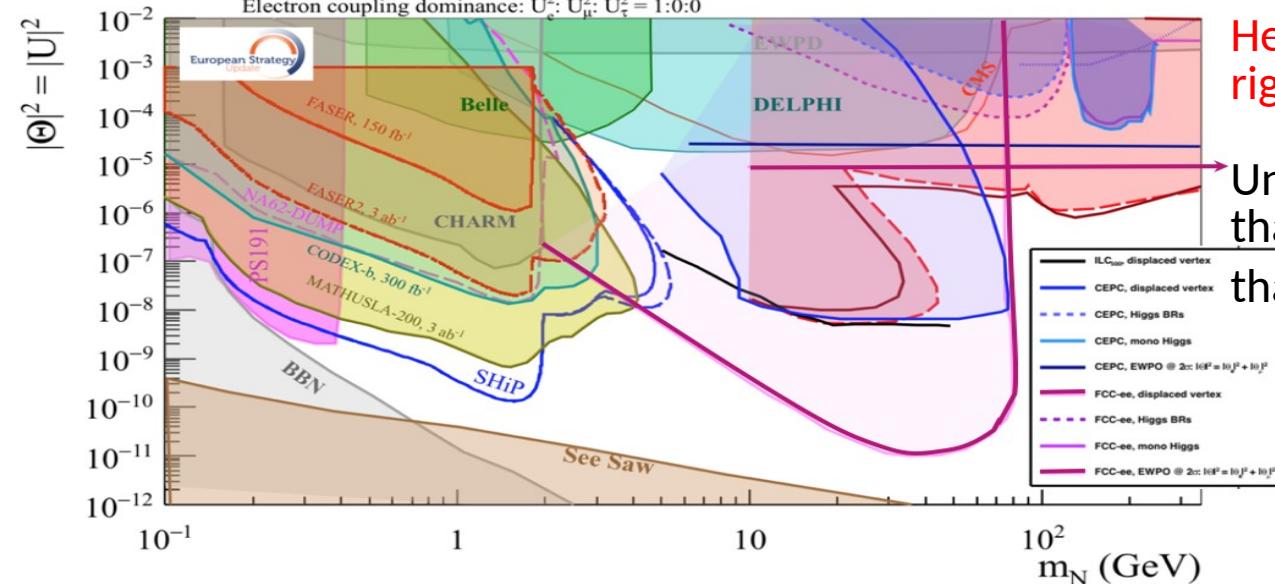
source: European Strategy  
briefing book

# Direct BSM searches at FCC-ee: FIPs



Axion-like particles (ALPs), dilatons,...

Unique limits (up to  $\times 10^3$  better than today) over  $m_a = 1-100$  GeV thanks to  $10^{12}$   $Z$  decays.



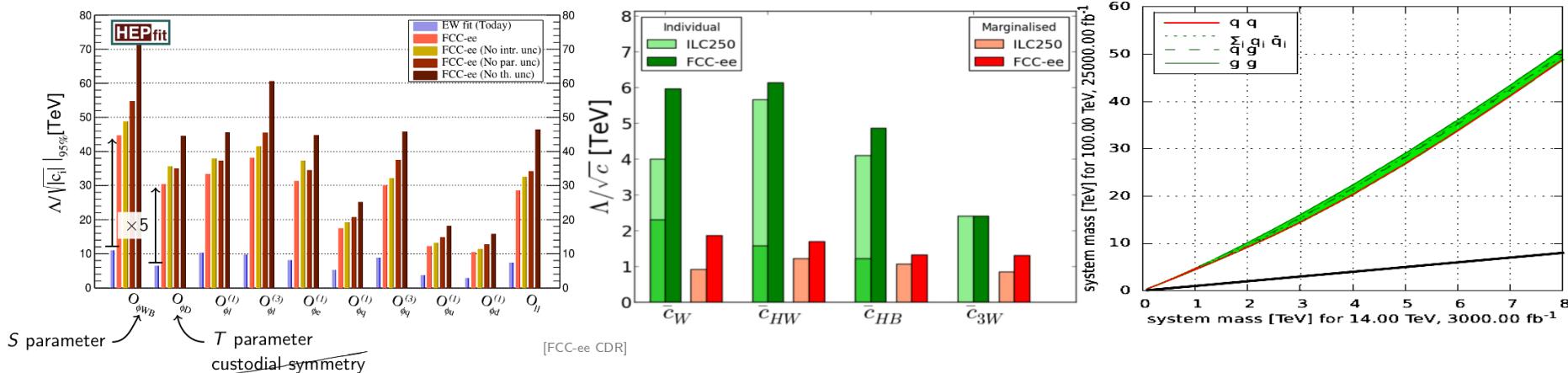
Heavy-neutral leptons (HNLs), right-handed (sterile) neutrinos,...

Unique limits (up to  $\times 10^3$  better than today) over  $m_a = 5-100$  GeV thanks to  $10^{12}$   $Z$  decays.

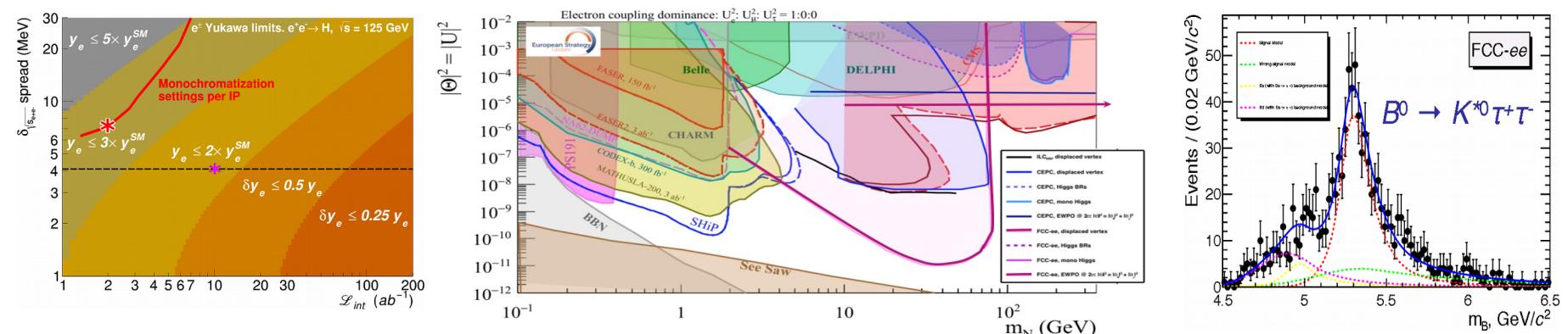
# Summary

- FCC provides unparalleled c.m. energies (100 TeV) & lumis (20, 150 ab<sup>-1</sup>) in p-p and e<sup>+</sup>e<sup>-</sup> colls. to address many HEP fundamental open problems.
- High-precision Z, W, H, top studies (FCC-ee) & high-mass (FCC-pp) allow setting direct/indirect constraints on BSM up to  $\Lambda \gtrsim 50$  TeV

( $m_Z$ ,  $\Gamma_Z$ ,  $A_{FB}$ ,  $R_x$ ,  $\alpha(m_Z)$ ,  $m_W$ ,  $m_t$ , etc.)



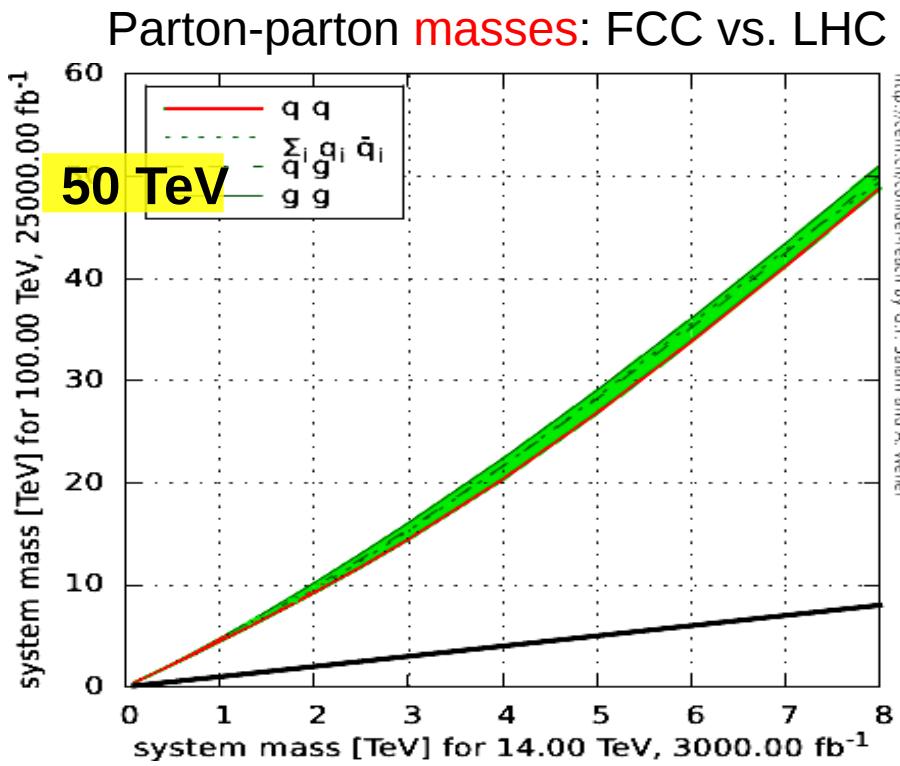
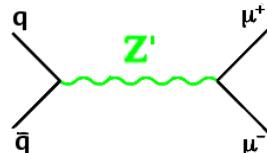
- Plus: 1<sup>st</sup> gen. Yukawas, right-handed ν's, dark matter, QCD, flavour, ...



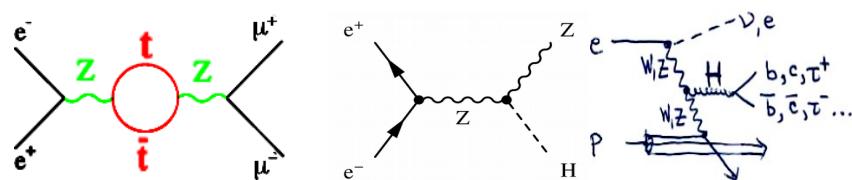
# Backup slides

# BSM physics reach at FCC

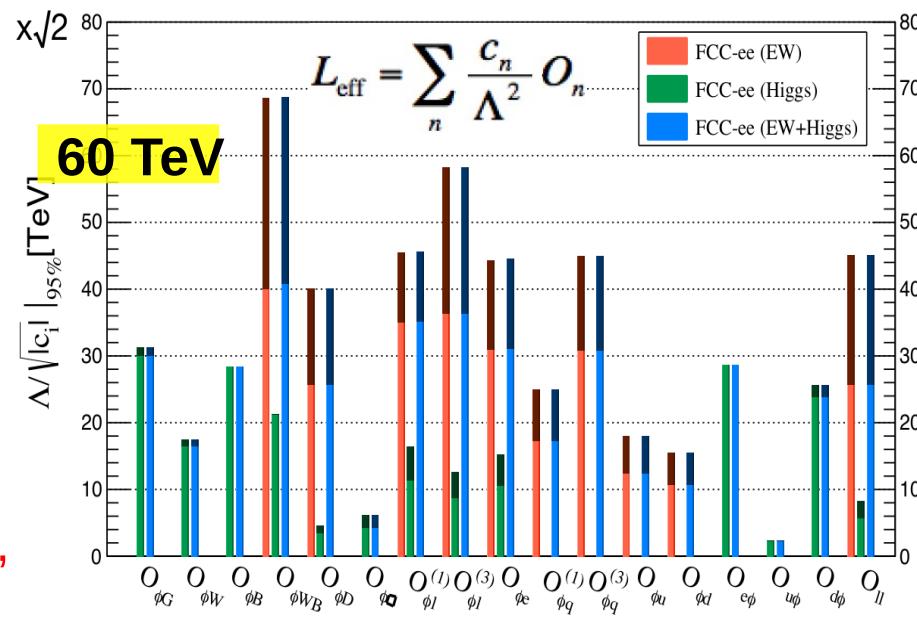
- FCC-pp: Direct production of new heavy particles up to  $\sim 50$  TeV (~8 TeV at LHC):



- FCC-ee,eh: Indirect sensitivity to virtual corrections up to  $\sim 60$  TeV (~3 TeV at LEP for EWK sector):



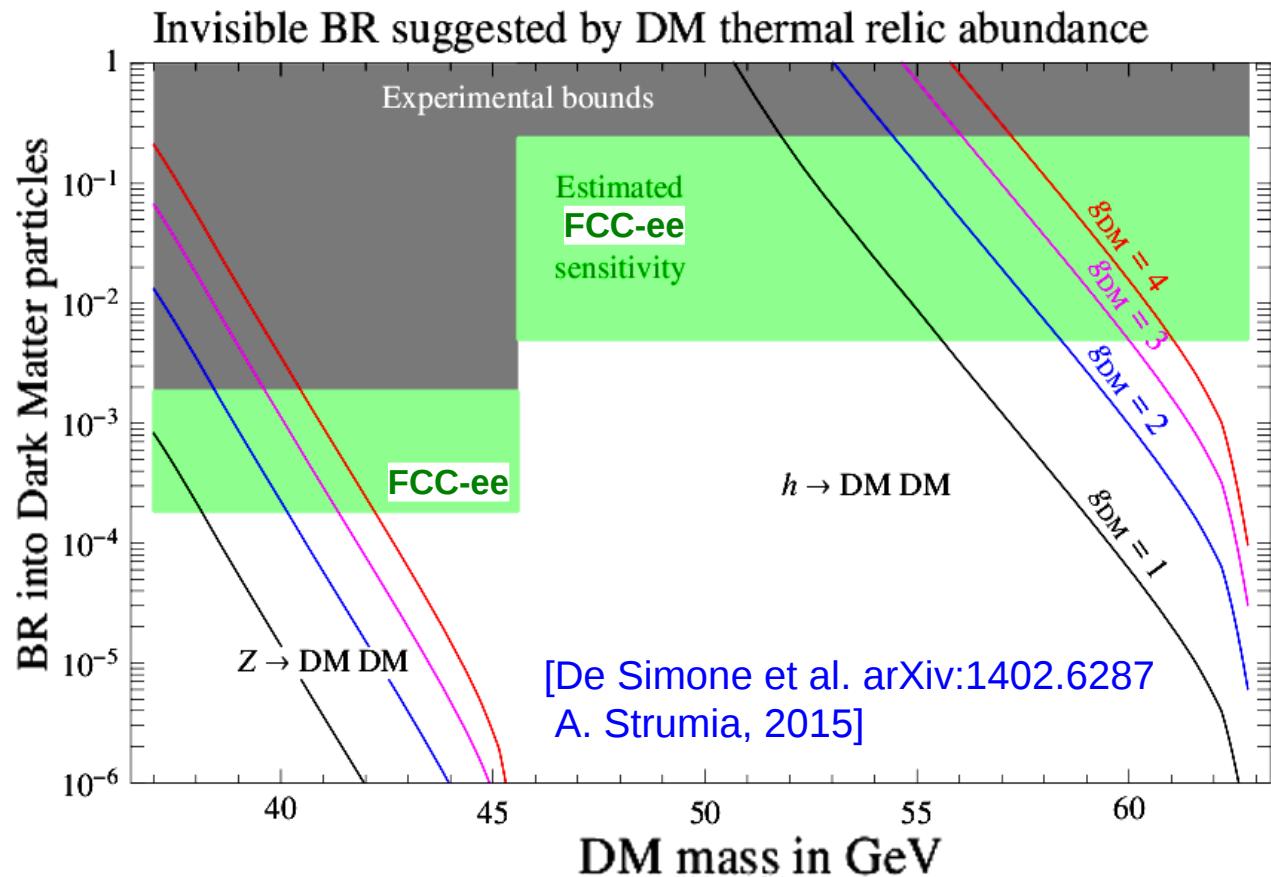
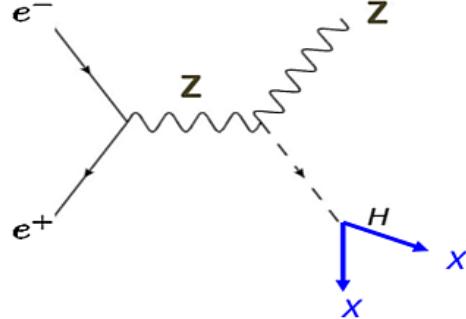
SM-EFT limits from EWK ( $\delta X < 10^{-5}$ ) and Higgs ( $\delta g_H < 1\%$ ) observables uncertainties:



- Plus many more: Higgs self-coupling,  $\text{TeV-}p_T$   $W, Z, H, t$ ;  $WW$  scatt., DM,...

# Direct BSM searches at FCC-ee: DM via H,Z decays

- DM freeze-out fixes  $\sigma v \approx 3 \cdot 10^{-26} \text{ cm}^3/\text{s}$ . If  $m_{\text{DM}}$  is just below  $m_{Z,H}/2$ , DM freeze-out dominated by resonant Z,H exchange, fixing  $\Gamma_{Z,H}$ .



- Precision ( $<10^{-3}$  and  $<10^{-1}$ ) measurements of invisible Z & H widths are best collider option to test any  $m_{\text{DM}} < m_{Z,H}/2$  that couples via SM mediators.

# $\alpha_s$ from photon QCD structure function (NLO)

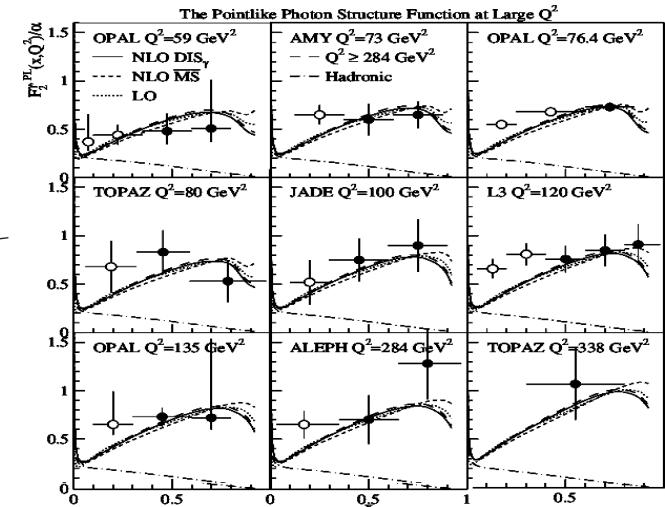
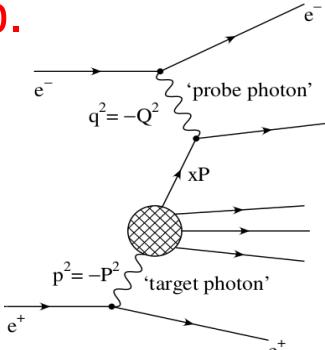
→ Computed at NNLO:  $\int_0^1 dx F_2^\gamma(x, Q^2, P^2) = \frac{\alpha}{4\pi} \frac{1}{2\beta_0} \left\{ \frac{4\pi}{\alpha_s(Q^2)} c_{LO} + c_{NLO} + \frac{\alpha_s(Q^2)}{4\pi} c_{NNLO} + \mathcal{O}(\alpha_s^2) \right\}$

→ Poor  $F_\gamma^2(x, Q^2)$  experimental measurements:

→ Extraction (NLO) with large exp. uncertainties today:

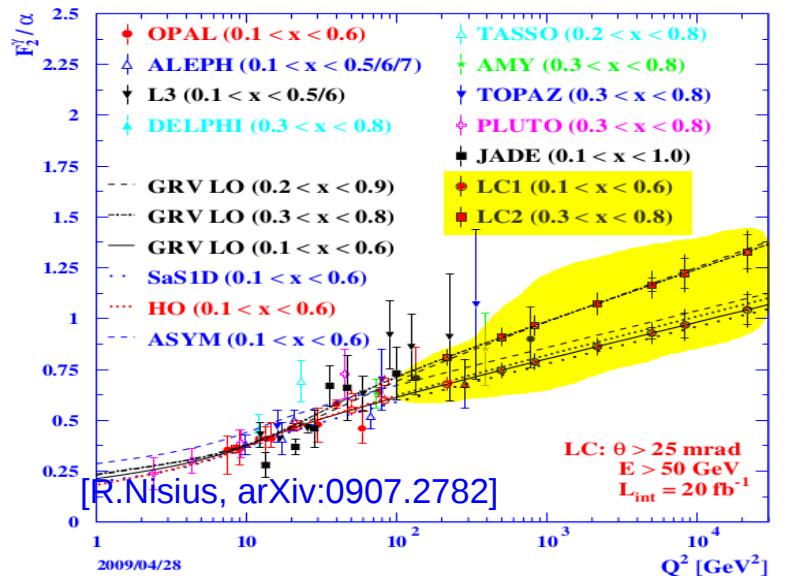
$$\alpha_s(m_z) = 0.1198 \pm 0.0054 \\ (\pm 4.5\%)$$

[M.Klasen et al. PRL89 (2002)122004]



→ Future prospects:

- Fit with NNLO  $F_\gamma^2$  evolution (ongoing)
- Better data badly needed: Belle-II ?
- Dedicated simul. studies at ILC exist:
- Huge  $\gamma\gamma$  (EPA) stats at FCC-ee will lead to:  $\delta\alpha_s/\alpha_s < 1\%$



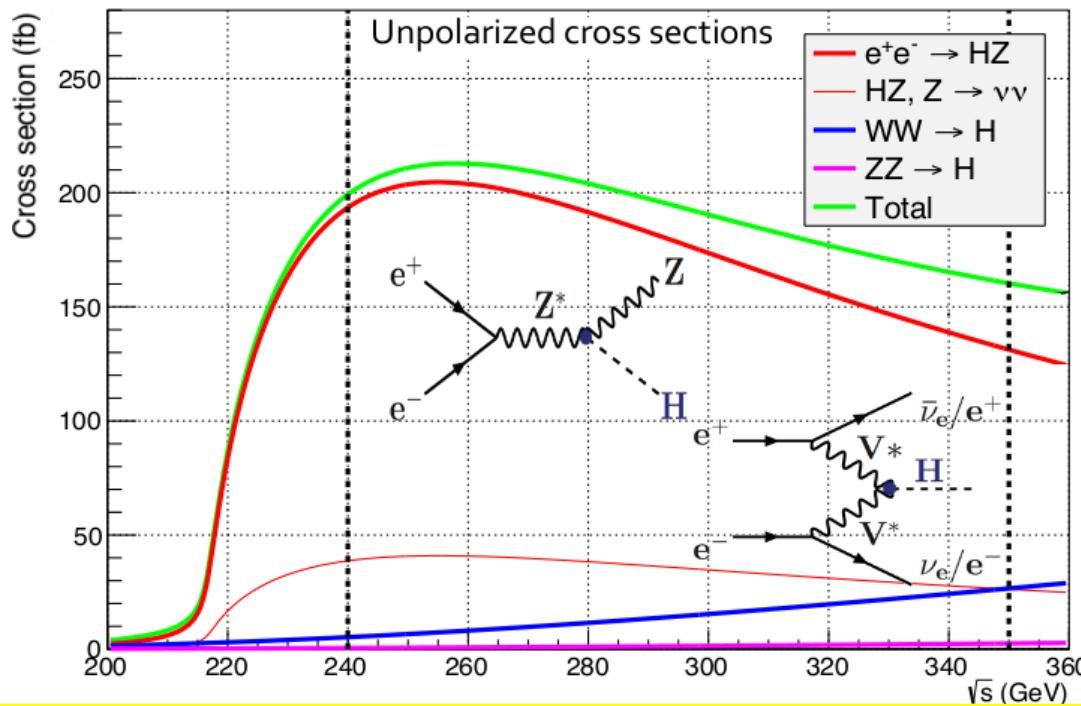
# FCC-ee = Higgs boson factory

■ Higgs cross sections:  $\sigma(e^+e^- \rightarrow H+X) \approx 200 \text{ (HZ)} + 50 \text{ (VBF)} \text{ fb}$

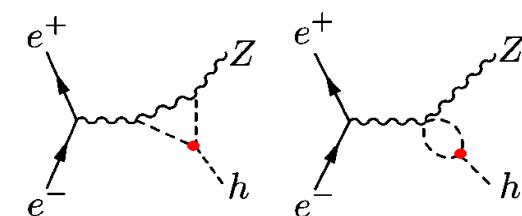
■ 1.2M Higgs bosons produced:

- Small & very well controlled backgrounds (S/B~ $10^{-2}$ – $10^{-3}$ )
- Extra-clean environment w/o pileup:

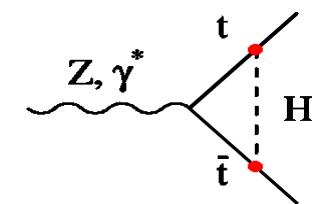
	5/ab @ 240 GeV	0.2/ab @ 350 GeV 1.5/ab @ 365 GeV
# Higgs from HZ	1,000,000	200,000
# Higgs from VBF	25,000	50,000



(sensitivity to self-coupling)



(sensitivity to top  $y_t$ )

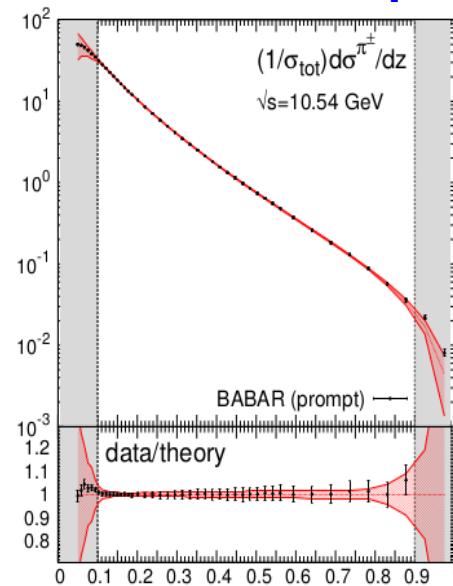
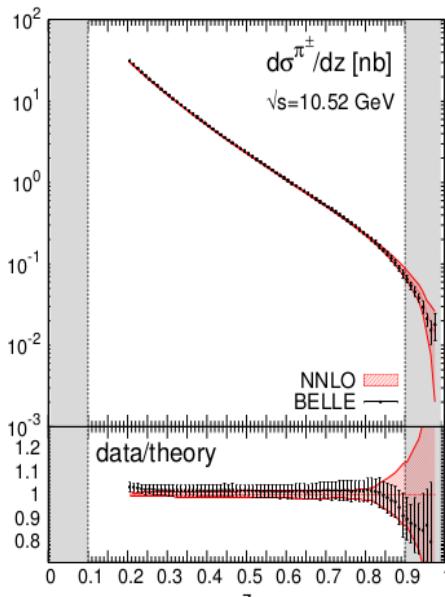


■ Access to precise (down to 0.15%) Higgs couplings & rare & BSM decays

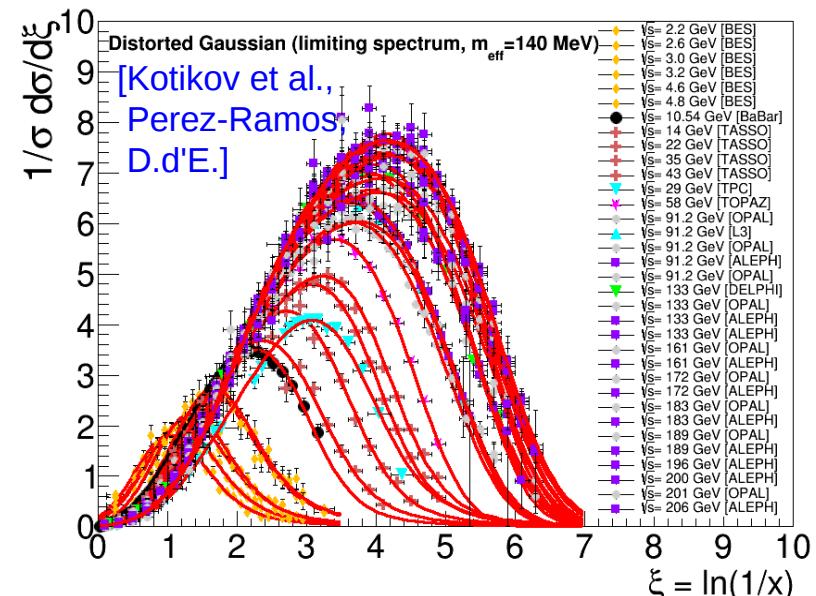
# High-precision parton FFs (FCC-ee)

■ Parton-to-hadron fragment. functions evolution known at NNLO at high-z &

[D.Anderle et al., A.Vossen et al., B.Kniehl et al.,  
V.Bertone et al., N.Sato et al., D.deFlorian et al.,...]



at NNLO\*+NNLL at low-z:



provide additional QCD coupling extractions:

Method	Current $\delta\alpha_s(m_z^2)/\alpha_s(m_z^2)$ uncertainty (theory & experiment state-of-the-art)	Future $\delta\alpha_s(m_z^2)/\alpha_s(m_z^2)$ uncertainty (theory & experiment progress)
soft FFs	$1.8\%_{\text{th}} \oplus 0.7\%_{\text{exp}} \approx 2\%$ (NNLO* only (+NNLL), npQCD small)	$0.7\%_{\text{th}} \oplus 0.7\%_{\text{exp}} \approx 1\%$ ( $\sim 2$ yrs), $< 1\%$ (FCC-ee) (NNLO+NNLL. More precise $e^+e^-$ data: 90–350 GeV)
hard FFs	$1\%_{\text{th}} \oplus 5\%_{\text{exp}} \approx 5\%$ (NLO only. LEP data only)	$0.7\%_{\text{th}} \oplus 2\%_{\text{exp}} \approx 2\%$ (+B-factories), $< 1\%$ (FCC-ee) (NNLO. More precise $e^+e^-$ data)

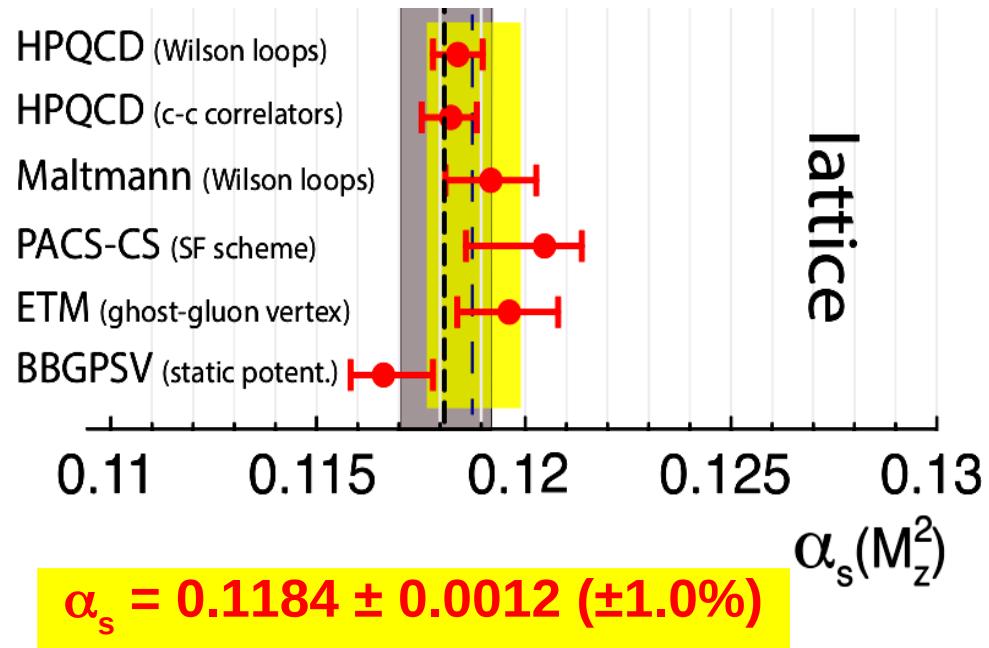
■ FCC-ee (much broader z range) allows for  $\alpha_s$  extraction with  $\delta\alpha_s < 1\%$

# $\alpha_s$ from lattice QCD

- Comparison of short-distance quantities (Wilson loops, q static potential, vacuum polariz,...) computed at NNLO in pQCD, to lattice QCD “data”:

$$K^{\text{NP}} = K^{\text{PT}} = \sum_{i=0}^n c_i \alpha_s^i$$

[FLAG Collab. <http://itpwiki.unibe.ch/flag>]



- Currently, it's extraction with **smallest uncertainties:  $\pm 1\%$**  (lattice spacing & statistics).

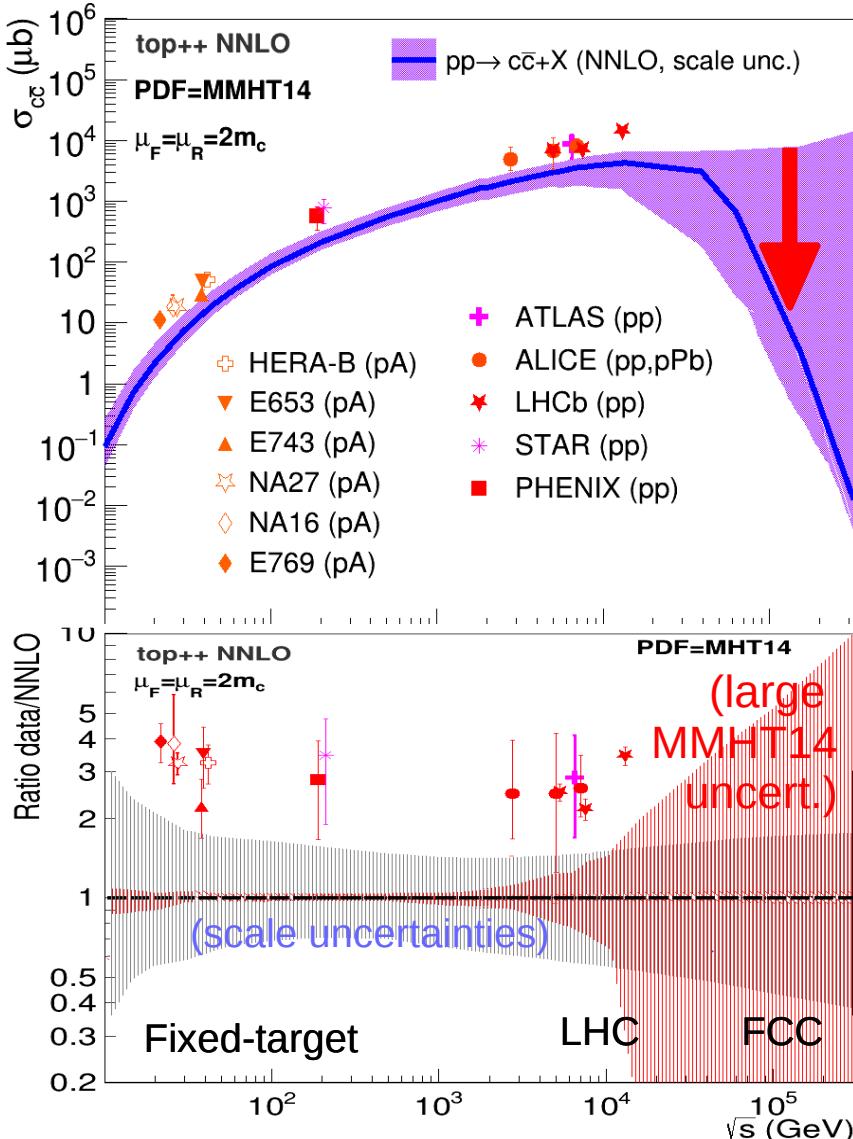
Extracted value depends on observables:

Uncertainty **increased**:  
2013 ( $\pm 0.4\%$ ) → 2017 ( $\pm 1.0\%$ )

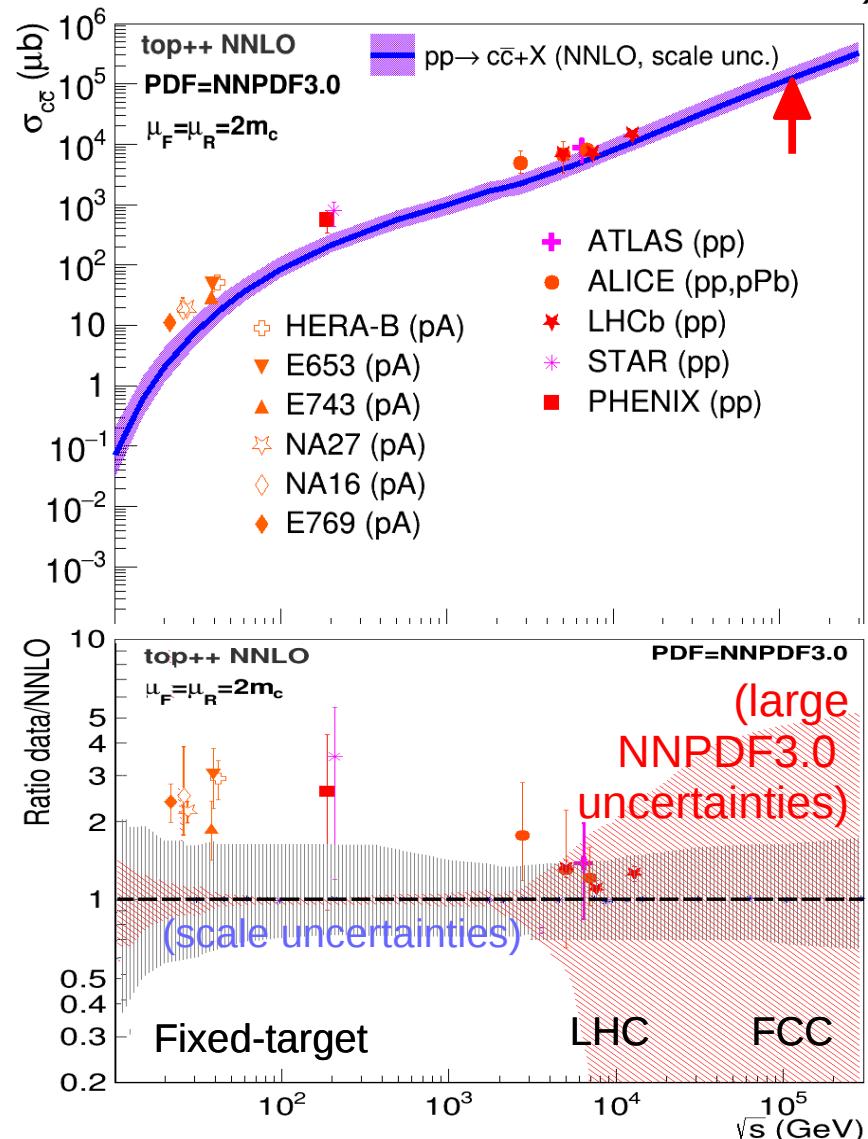
- Future prospects:
- Uncertainty in  $\alpha_s$  could be halved with (much) better numerical data.
- Reaching  $\pm 0.1\%$  requires 4<sup>th</sup>-loop perturbation theory (~10 years?)

# Heavy-quark production (FCC-pp)

■ Charm: Data  $\times 2.5$  theory (negative gluon at very low  $x$ ,  $\sqrt{s} > 30$  TeV)

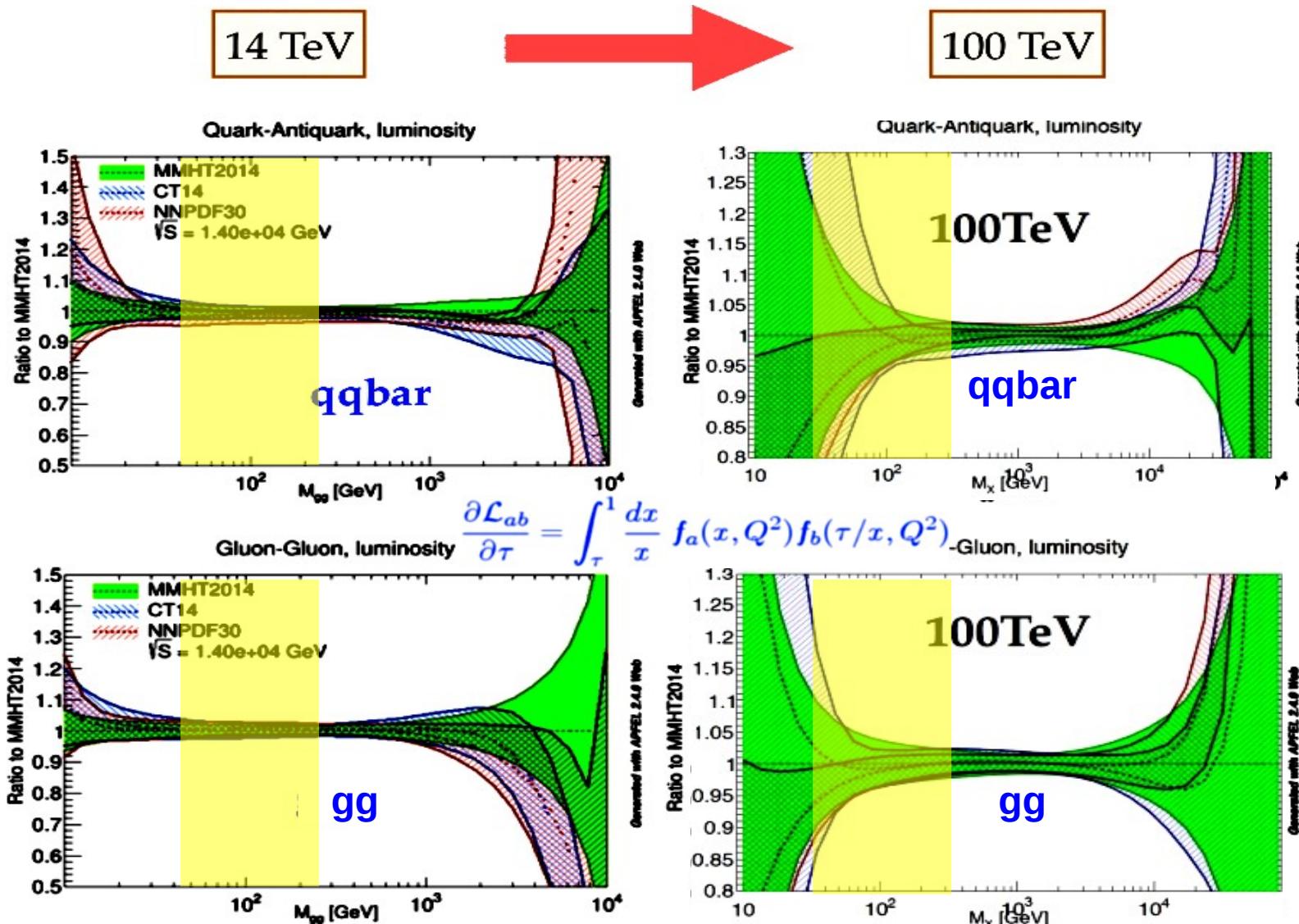


■ Charm: Data  $\times 2$  theory (agreement within uncrt. but “kink” at  $\sqrt{s} > 10$  TeV)

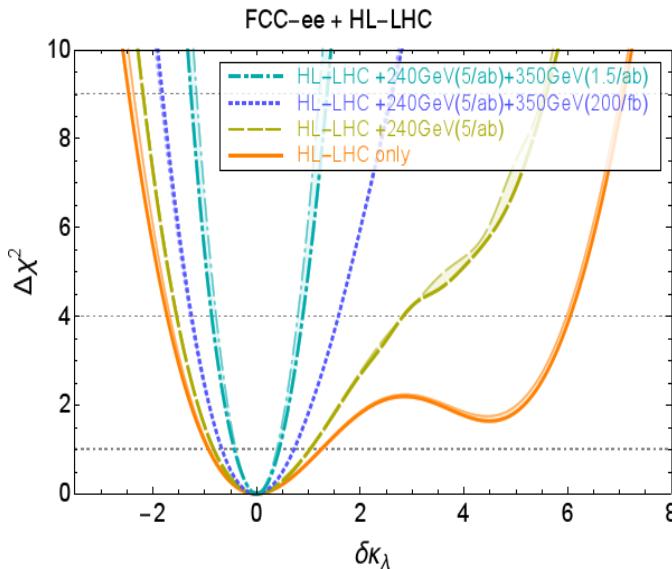


# Parton lumis at FCC “precision” region

- “Precision” region at FCC-pp: 5–7% PDF uncertainty for  $\sigma(W, Z, H)$

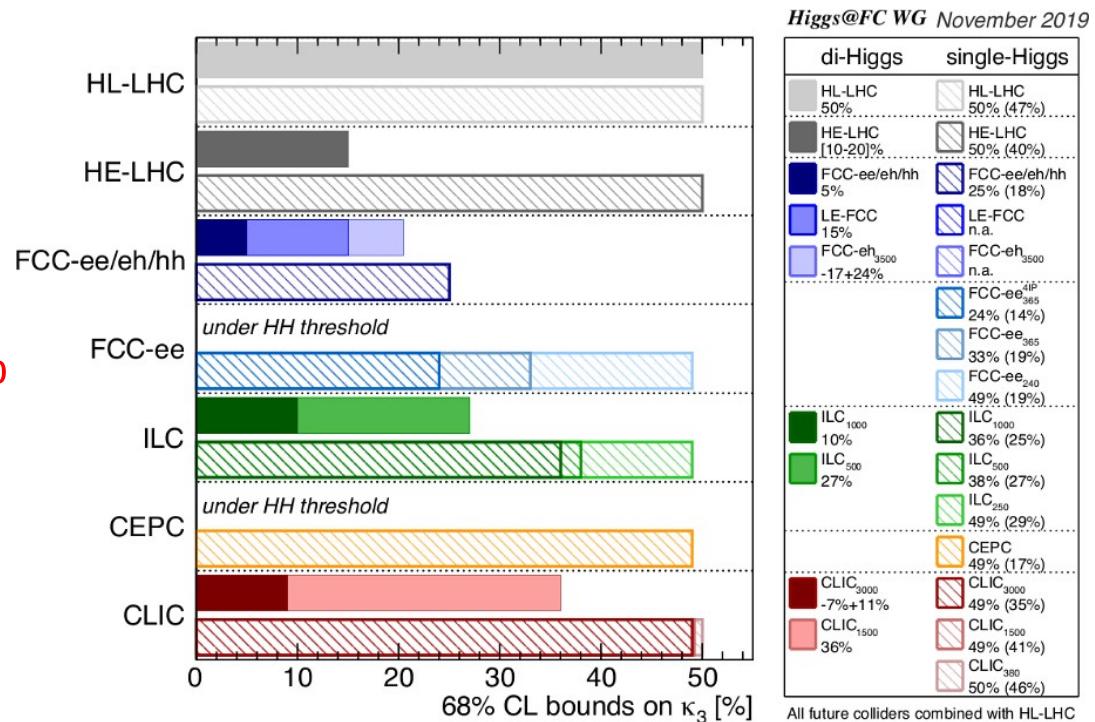


# Higgs self-coupling ( $\lambda_3$ ) at FCC-ee



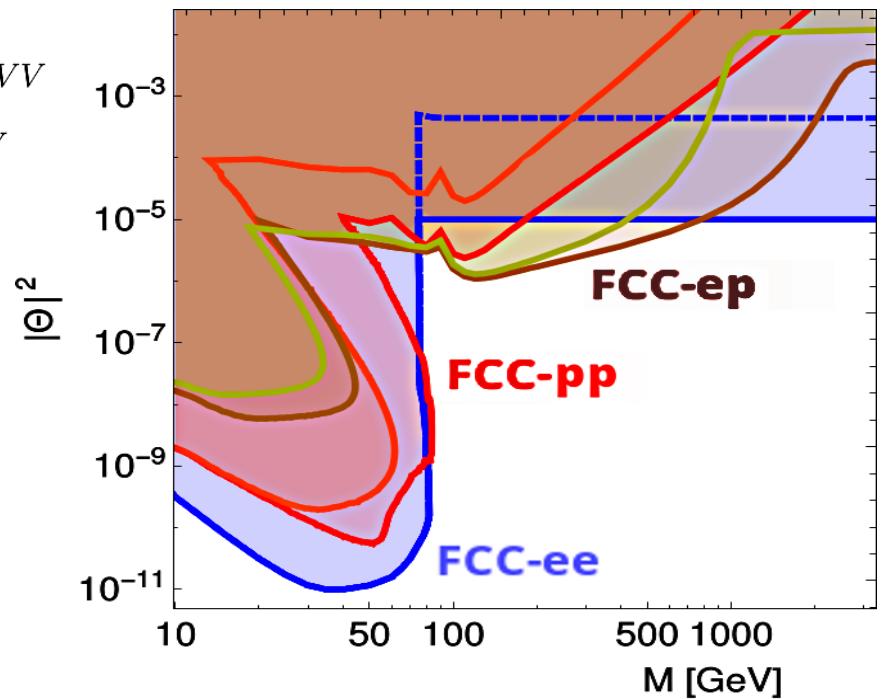
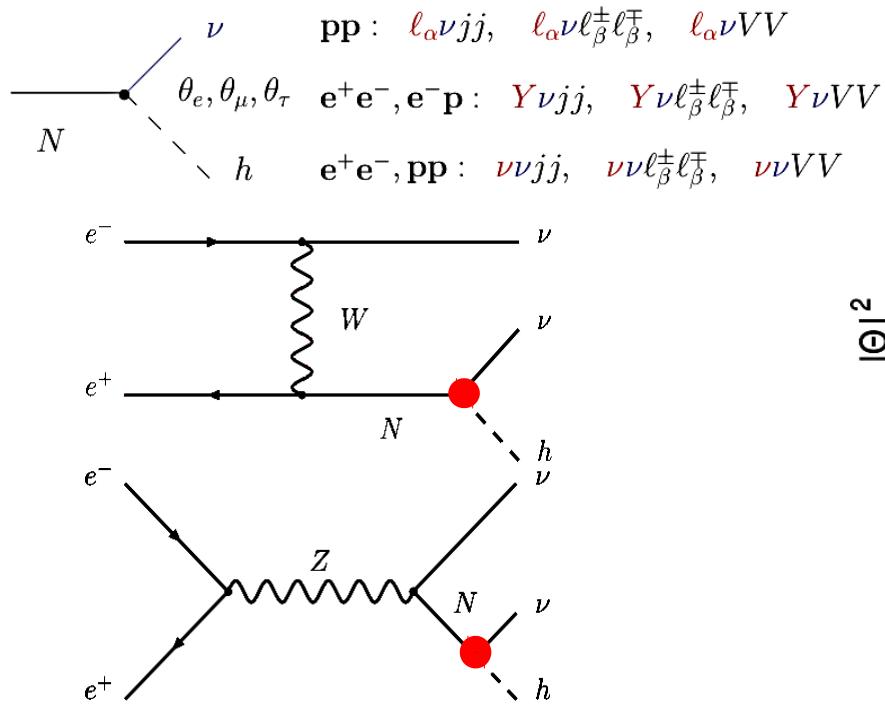
- Final Higgs self-coupling precision (FCC-all): 2–3%

- Higgs self-coupling constrained to within ~40%.
- Addition of FCC-ee 240+350GeV Higgs cross section solves 2<sup>nd</sup> minimum on  $\lambda$  from HL-LHC data alone.



# Higgs coupling to neutrinos (FCC-ee,hh)

- Low-mass seesaw scenario with sterile  $\nu$  ( $N_i$ ) that mix with the SM  $\nu$  with O(1) Yukawa couplings & EW-scale masses.
- $N_i$  decay to Higgs+ $\nu$ . Exp. signature: mono-Higgs(jj+ME).



(Also via invisible  $H \rightarrow N_i \nu$  decays for  $m_N < m_H$ )

[Antusch, Cazzato, Fischer, IJMPA 32 (2017) 1750078]

- With Z (EWPO), sensitivity down to active-sterile mix  $|\Theta|^2 \sim 10^{-11}$  for  $m_N > 10$  GeV