

Precise QCD measurements from LHC to future colliders

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on behalf of ATLAS, CMS, LHCb

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Precise QCD measurements

- Understanding QCD is critical for physics at hadron colliders
- Focus on precision:
 - Interplay between QCD and electroweak precision measurements
 - Precise QCD measurements leading to determination of α_s(m_z), PDFs
- Topics:
 - QCD measurements of the Drell-Yan process
 - Measurements of α_s(m_z) with jets and top at the LHC, and at future coliders



Drell-Yan QCD measurements

- The Drell-Yan mechanism was proposed and observed in 1970. It was a milestone in the building of QCD as the theory of the strong interation. After 45 years, why is this process still of interest for QCD and what can we learn from it?
- The Drell-Yan process at the LHC provides an extremely clear experimental signature: high resolution in the electron and muon channels, and small background contamination
- Measurements have reached permille level accuracy, QCD predictions are at 3 orders beyond LO → ideal framework for precision tests of QCD
 - do/dpt allows probing of the transverse dynamic of nonperturbative and perturbative QCD
 - $d\sigma/dy$ allows probing of the longitudinal dynamic (PDFs)
 - The angular coefficients allow testing of the QCD and EW helicity structure
- QCD issues in these measurements are tightly connected to precision measurements of m_w and $sin^2\theta_w$



Measurement of Z-boson transverse momentum



- Measurements have reached an accuracy of a few permille in the region below 100 GeV
- QCD predictions at N3LO+N3LL
- Excellent test of perturbative and nonperturbative QCD



Measurement of Z-boson transverse momentum



 Measurements differential in invariant mass, allows disentaglement of perturbative and non perturbative effects, and of different initial flavour compositions

W, Z rapidity cross section measurements

 W asymmetry and Z rapidity measurements at the LHC directly constrain valence and sea PDFs



- These measurements are systematics limited already in Run 1
- New experimental methodology are needed to fully exploit the potential of the full LHC data sample
- With enough statistics, low pile up data can also be used to perform measurements with smaller systematic uncertainties

Fiducial power corrections

- The usage of W asymmetry and Z rapidity measurements to reduce PDF uncertainties is currently limited by symmetric fiducial cuts
- Perturbative calculations are be affected by enhanced logarithms, connected to the linear dependence of acceptance on the boson p_T . When approaching the limit $p_{T,2} \rightarrow p_{T,1}$ they become unreliable
- The effect is larger when p_T is closer m_{II}/2, and at large values of cos(θ), as in the central-forward (CF) kinematic region
- Need to resum fiducial power corrections in order to get a meaningful predictions, either with parton shower or with analytic resummation

Recent studies on this topic with alternative solutions arXiv:2106.08329 Salam, Slade arXiv:2104.02400 Alekhin et al. arXiv:2006.11382 Ebert et al. arXiv:2001.02933 Glazov



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Fiducial power corrections

- Preliminary study, including q_T-resummation with a recoil prescription in PDF fits to ATLAS W,Z rapidity measurements
- Corrections are significant compared to the experimental accuracy, and gives large improvement in χ^2
- Striking example is the Z central-forward configuration, with 10% corrections in the first and last bins



Dataset	CT14 published	CT14 NNLL
ATLAS low mass Z rapidity 2011	11/6	8.7 / 6
ATLAS peak CC Z rapidity 2011	16 / 12 🗛	10 / 12
ATLAS peak CF Z rapidity 2011	10/9	5.6/9
ATLAS high mass CC Z rapidity 2011	6.3 / 6	6.3 / 6
ATLAS high mass CF Z rapidity 2011	5.1/6	5.4 / 6
ATLAS W- lepton rapidity 2011	8.9 / 11	8.8 / 11
ATLAS W+ lepton rapidity 2011	10 / 11	10 / 11
Correlated χ^2	39	35
Log penalty χ^2	-4.11	-3.60
Total χ^2 / dof	103 / 61	86 / 61
χ^2 p-value	0.00	0.02



Z-boson angular coefficients

 The angular coefficients provide a powerful framework to describe asymmetries of the DY cross section as the azimuthal (A2) and the forward-backward (A4). The decomposition holds at all order in QCD

$$\frac{d\sigma}{dpdq} = \frac{d^3\sigma}{dp_T dy dm} \sum_i A_i(y, p_T, m) P_i(\cos\theta, \phi)$$



- Coefficients defined in the Collins-Soper frame
- Percent-level measurements from ATLAS and CMS at 8 TeV, as well as accurate perturbative QCD predictions at $O(\alpha_s^3)$ are available



Z-boson angular coefficients

- Interesting violation of the The Lam-Tung relation A0-A2 = 0 in excess with respect to perturbative QCD predictions
- Tension mildly reduced at $O(\alpha_s^3)$





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Angular coefficients in the non perturbative regime



- cos(2\u03c6) (A2) asymmetries in the non perturbative regime were observed in fixed target Drell-Yan experiments (NA10, E866)
- They are well described by Boer-Mulder TMD functions

- The non-perturbative contribution to A2 at small $q_{_{\rm T}}$ is expected to change sign between γ^* and Z exchange
- Is such an asymmetry expected also in W? The measurement of m_w could be sensitive to such nonperturbative QCD asymmetries, it may be necessary to quantify it precisely for future measurements

CMS W polarisation



arXiv:2008.04174

- New measurement of W helicity fractions, essentially a measurement of forward-backward asymmetry in W
- Together with the standard W charge asymmetry provides an interesting constraint on PDFs



QCD issues in the measurement of m_W at the LHC

- The measurement of m_w at the LHC is extremely sensitive to QCD effects
- They affect all aspects of the measurement: detector calibration, transfer from Z to W, PDF uncertainties, W polarisation, modelling of p_T W
- The measurement of m_w provides a great occasion to understand QCD, recent examples are the ATLAS and LHCb measurements



ATLAS and LHCb results for m_w

ATLAS

 $M_W = 80369.5 \pm 6.8$ (stat) ± 10.6 (exp.syst.) ± 13.6 (model.syst.) MeV

Combined categories	Value [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.	χ^2/dof of Comb.
m_{T} - p_{T}^{ℓ} , W^{\pm} , e - μ	80369.5	6.8	6.6	6.4	2.9	4.5	8.3	5.5	9.2	18.5	29/27

l HCb	Source	Size [MeV]
EIIOS	Parton distribution functions	9
$NA = 000 \Gamma A$	Theory (excl. PDFs) total	17
$M_W = 80354$	Transverse momentum model	11
+ 22 (stat)	Angular coefficients	10
± 23 (Stat)	QED FSR model	7
± 10 (exp)	Additional electroweak corrections	5
	Experimental total	10
± 17 (theory)	Momentum scale and resolution modelling	7
	Muon ID, trigger and tracking efficiency	6
± 9 (PDF)	Isolation efficiency	4
MeV	QCD background	2
	Statistical	23
	Total	32

- The dominant uncertainty is due to the physics modelling (theory)
- The largest contributions are from QCD/PDFs

W mass at the LHC

A proton-proton collider is the most challenging environment to measure m_w , worse compared to e+e- and proton-antiproton



In $p\overline{p}$ collisions W bosons are mostly produced in the same helicity state



In pp collisions they are equally distributed between positive and negative helicity states

Further QCD complications

- Heavy-flavour-initiated processes
- W+, W- and Z are produced by different light flavour fractions
- Larger gluon-induced W production



Large PDF-induced Wpolarisation uncertainty affecting the p_T lepton distribution

PDF uncertainties

- PDF uncertainties are currently the largest uncertainty at the LHC, and they are expected to remain dominant in future measurements
- The main mechanism which gives rise to large PDF uncertainties is: valence/sea \rightarrow W helicity $\rightarrow p_{\tau}$ lepton $\rightarrow m_{w}$



~80% of the PDF uncertainty on m_w is longitudinal-polarisation induced

Physics modelling for m_w

- The physics modelling comprises the theoretical prediction used to extract the W mass from the observed distributions in data, and the way theory uncertainties are addressed.
- The DY cross section can be reorganised by factorising the dynamic of the boson production, and the kinematic of the boson decay:



- This factorization allows building a composite model, and using the most appropriate or accurate model for each term.
- Precise QCD is essential for modelling of do/dy, do/dpt and of the angular coefficients. The physics modelling strategy is based on QCD predictions and auxiliary DY measurements.

Physics modelling – DY ancillary measurements



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• The p_{τ} W modelling is based on precise measurements of p_{τ} Z and accurate predictions of the W/Z p_{τ} ratio



- The $p_T Z$ distribution is measured at permille accuracy
- The WZ p_{T} ratio is currently known with 2-3% uncertainty
- Large spread of W/Z p_T ratio predictions at the level of 5-10%
 - \rightarrow Require great control of:
 - non-perturbative QCD
 - q_{τ} -resummation
 - heavy-flavour-initiated production







- Ongoing effort in the LPCC EW working group to benchmark various different predictions of the W/Z p_{τ} ratio, aimed at
 - Define a common baseline where all predictions agree
 - Allow using the prediction which is best suited to derive each particular correction and/or uncertainty on top of the baseline
- Recently q_T-resummation predictions have reached N3LL' accuracy
- However high-order perturbative accuracy alone is not sufficient for a precise prediction of the W/Z pT ratio





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hep-ph/0509023



 Heavy flavours initiated production with ACOT VFN scheme for Drell-Yan



 SCET-based approach for q_T-resummation with massive quark effects



LHCb mw



LHCb physics modelling



- LHC measurements would greatly benefit from understanding such issues from first principles
- Normalisation of A3 coefficient is left free in the fit

Prospects for m_w at the HL-LHC with low pileup data



ATL-PHYS-PUB-2018-026

- Increased acceptance provided by the new inner detector in ATLAS, (ITk) extends the coverage up to $|\eta| < 4$
- Allows further constraints on PDFs from cross section measurements
- With 1fb⁻¹ of low pileup data (<µ>~2) likely to reach ~ 6 MeV of stat+PDF uncertainty
- LHeC ep collisions would largely reduce PDF uncertainties (< 2 MeV)

W mass at future colliders

σ_{WW} (pb) The ultimate precision on m_w can be achieved at e⁺e⁻ 20-I FP colliders through an energy scan of the WW YFSWW and RacoonW production threshold 10 Near threshold, the WW cross section is proportional to the non-relativistic W velocity $\sigma(WW) \propto \beta_W$ arXiv:1306.6352 200 160 180 Phys.Rept. 532 (2013) 119-244 ILC Giga-Z program Ps (GeV) Energy scan 160 to 170 GeV (qd) (MM)⁶ FCCee W-pair threshold δM_w = 6-7 MeV m_w=80.385 GeV Γ_w=2.085 GeV mw=79.385-81.835 GeV, Γw=2.085 GeV m_w=80.385 GeV, Γ_w=1.085-3.085 GeV FCC-ee WW program δM_w = 0.5 MeV \rightarrow dominated by statistical uncertainty Dominant theory uncertainties Initial state QED corrections Parametrization of cross section near threshold QCD not an issue! 160

Physics at LHC and beyond

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√s (GeV)

170

165

Top quark QCD measurements



- Top quark production cross-section measurements at the LHC have reached percent-level accuracy
- Focus on measurements and QCD analyses leading to the determination of PDFs and $\alpha_s(m_z)$
 - Inclusive top quark production
 - Differential partonic tt cross sections
 - Differential leptonic tt cross sections

Top quark production inclusive cross section



- Inclusive cross section is sensitive to PDFs, a_s(m_z) and top mass
- Allows determination of a_s(m_z) with a NNLO QCD analysis



PDF set	$\alpha_S(m_Z)$
ABMP16	0.1139 ± 0.0023 (fit + PDF) $^{+0.0014}_{-0.0001}$ (scale)
NNPDF3.1	0.1140 ± 0.0033 (fit + PDF) $^{+0.0021}_{-0.0002}$ (scale)
CT14	0.1148 ± 0.0032 (fit + PDF) $^{+0.0018}_{-0.0002}$ (scale)
MMHT14	0.1151 ± 0.0035 (fit + PDF) $^{+0.0020}_{-0.0002}$ (scale)

QCD analysis of top production



• Simultaneous fit of m_{top} , $\alpha_s(m_z)$, PDFs

α_s(m_z)

Leptonic top production cross sections



- Measurements of leptonic differential cross sections in top production at 8 and 13 TeV have reached subpercent accuracy
- Measurement at 8 TeV was used for PDFs and m_{top} determination



Strong-coupling constant from jets measurements



- Measurements with highest experimental sensitivity:
 - ➡ TEEC (ATLAS)
 - Inclusive jet cross sections (CMS)
- Other measurements not discussed here: dijets, 3-jet mass, R₃₂ cross-section ratios

Transverse energy-energy correlations



$$\frac{1}{\sigma} \frac{\mathrm{d}\Sigma}{\mathrm{d}\cos\phi} \equiv \frac{1}{N} \sum_{A=1}^{N} \sum_{ij}^{N} \frac{E_{\mathrm{T}i}^{A} E_{\mathrm{T}j}^{A}}{\left(\sum_{k} E_{\mathrm{T}k}^{A}\right)^{2}} \delta(\cos\phi - \cos\phi_{ij})$$

- Transverse energy-energy correlations (TEECs) are the transverse energy-weighted angular distribution of jet pairs
- TEECs provide a measurement of $\alpha_s(m_z)=0.1162\pm0.0011(exp.)+0.0084-0.0070(theo.)$
- High experimental sensitivity <1%, experimental uncertainties dominated by jet modeling and JES/JER
- Large theory uncertainties dominated by scale variations



CMS inclusive jet production at 2.76, 7 and 8 TeV



sensitivity to PDFs

HERAPDF1.5

300

400 500 Jet p₁ (GeV)

MMHT14

200

0.

0.08

0.06

0.04

0.02

80 100

|y| < 0.5

CMS inclusive jets





- The measurement is used to determine $\alpha_s(m_z)=0.1164\pm0.0015(exp.)$ +0.0058-0.0040(theo.)
- Dominated by scale variations and PDFs
- The running of α_{s} is probed up to 1.5 TeV



Strong-coupling constant from W,Z cross section



- First determination of $\alpha_s(m_z)$ with the DY process
- Result compatible with the PDG world average: $\alpha_s(m_z) = 0.1175+0.0025-0.0028$
- Measurement dominated by PDF and luminosity uncertainties

$\alpha_s(m_z)$ from R_w and at R_z FCC-ee



 Prospects for measuring α_s(m_z) at permille level precision from the hadronic/leptonic Z and W decay ratios (R_z, R_w) at the FCC-ee

- Understanding of QCD is critical for all aspects of the LHC physics program: many analyses limited by PDFs, α_s , and QCD modelling
- QCD is entering a new precision era, with several LHC measurements at percent or permille level precision, and QCD predictions at two and three loops
- Permille level accuracy is expected for tests of QCD at future colliders, and in particular a determination of the strong-coupling constant at 0.1% accuracy

BACKUP

Angular coefficients A_i

 The angular coefficients provide a powerful framework to describe asymmetries of the DY cross section as the azimuthal (A2) and the forward-backward (A4). The decomposition holds at all order in QCD



Precise measurements from ATLAS and CMS as well as accurate perturbative QCD predictions at O(α_s³) are available

Motivation for m_W

The global fit of the electroweak observables is dominated by the measurement of m_{w}



	Measurement	SM Prediction (*)
mн	125.09 ± 0.24	100.6 ± 23.6
m _t	173.1 ± 0.6	176.1 ± 2.2
mw	80.379 ± 0.012	80.360 ± 0.007
		(*) arXiv:1710.05402

The measurements of the Higgs and topquark masses are currently more precise than their indirect determination from the global fit of the electroweak observables

Improving precision will not increase sensitivity to new physics

Indirect determination of m_w (±7 MeV) is more precise than the experimental measurement



Call for $\delta m_w^{exp} \sim 5 \text{ MeV}$

The W mass is nowadays the crucial measurement to improve the sensitivity of the global EW fits to new physics

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Measurements of SM parameters at the LHC

Various SM parameters can be measured at the LHC with a precision competitive with previous determinations

m _H	125.09 ± 0.24 GeV (ATLAS+CMS Run 1) arXiv:1503.07589	Uniquely measured at the LHC	- Higgs
mt	172.69 ± 0.48 GeV (ATLAS) arXiv:1810.01772 172.44 ± 0.49 GeV (CMS) arXiv:1509.04044	Most precise measurements	
α _s (m _z)	0.1164 ± 0.0052 (CMS jets) arXiv:1609.05331 0.1151 ± 0.0028 (CMS tt̄) arXiv:1307.1907 0.1173 ± 0.0046 (ATLAS TEEC) arXiv:1508.01579	Currently dominated by large theory uncertainty (MHO, PDFs)	QCD
m _w	80.370 ± 0.019 GeV (ATLAS) arXiv:1701.07240	Competing with Tevatron precision	
$sin^2 \theta_w$	0.23140 ± 0.00036 (ATLAS) 0.23101 ± 0.00053 (CMS) 0.2314 ± 0.0011 (LHCb) ATLAS-CONF-2018-037 arXiv:1806.00863 arXiv:1509.07645	Not yet competitive with LEP and SLD	Electroweak
Γ_{W}	2144 ± 62 MeV (CMS) arXiv:1107.4789	From W/Z cross section ratio	

Experimental measurements at colliders

The W-boson mass can be measured from:

- Kinematic properties of decay leptons in the final state in pp → W → lv processes (hadron colliders)
- Direct reconstruction from the final state in ee → WW → qqqq/qqlv (e+e- colliders)
- W-pair production at thresholds (e+e- colliders)

 Limited by statistics at LEP, ³/₆
but most precise prospect at future colliders



SPS, Tevatron,

LHC

LEP best

LHC experiments







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W mass at the LHC

$$pp \to W \to \ell \nu$$

- Main signature: final state prompt and isolated charged lepton (electron or muon)
- The neutrino momentum can be reconstructed from momentum imbalance in the transverse plane: p_T^{miss}
- The transverse mass m_T is defined from variables measured in the transverse plane



Observables sensitive to m_w are

Lepton transverse momentum p_T^ℓ	Good detector resolution, pileup robust	Very sensitive to theory uncertainties (PDF, p⊤W)
Transverse mass	Poor detector resolution,	Less sensitive to theory
$m_T = \sqrt{2p_T^\ell p_T^\nu (1 - \cos \Delta \phi(\ell, \nu))}$	sensitive to recoil calibration, degrades at high pileup	uncertainties

W mass – Measurement strategy

 $m_{\scriptscriptstyle W}$ extracted from the $p_{\scriptscriptstyle T}$ lepton and transverse mass (m_{\scriptscriptstyle T}) distributions





 m_T has a Jacobian edge at m_W

Template-fit approach:

- Vary the W-boson mass values in the theory prediction, and predict the p_T lepton and m_T distributions
- Compare to data, and determine the W mass by $\chi^{\rm 2}$ minimization

Challenges:

- Ultra-precise detector calibration ~ 10⁻⁴
- Accurate theory predictions

ATLAS -7 TeV result for m_w

The ATLAS result equals in precision the previous single-experiment best measurement of CDF

$M_W = 80369.5 \pm 18.5 \text{ MeV}$



 $M_w = 80369.5 \pm 6.8$ (stat) ± 10.6 (exp.syst.) ± 13.6 (model.syst.) MeV

The dominant uncertainty is due to the physics modelling



and the largest contributions are from QCD/PDF

$LHCb - Prospects for m_W$

- Run 1 + 2 allows reaching ~10 MeV statistical uncertainty
- LHCb analysis plans to exploit the sensitivity of the p_T lepton distribution to the W mass and to all components of the p_T W uncertainty
- Simultaneous fit to W mass and $\textbf{p}_{_{T}}$ W nuisance parameters





 When the fit range is large enough it is possible to determine all parameters with a relatively small loss in the precision of the W mass

Prospects for future measurements

Two paths for future measurements at ATLAS and CMS

	High pileup	Low pileup	
Most sensitive observable	p _T lepton	m _r	
Theory challenge	W/Z p _r ratio, PDFs	PDFs	
Experimental challenge	p_{τ} lepton calibration	Recoil calibration	
Dominant uncertainties	Physics modelling, PDFs	Recoil, stat, PDFs	
→ Or	nly option at LHCb	Requires ded	icated r

- Can benefit from very high stat of the HL-LHC program
- Provides measurement and data-driven modelling of p_T W
- Orthogonal approaches with different dominant uncertainties
- Should be both pursued, will benefit from the combination

Physics modelling – Summary of QCD uncertainties

W-boson charge		W^+		W^-		Combined	
Kinematic distribution	p_{T}^ℓ m_{T} p_{T}^ℓ m_{T} p_{T}^ℓ		p_{T}^ℓ	m_{T}			
δm_W [MeV]							
Fixed-order PDF uncertainty	13.1	14.9	12.0	14.2	8.0	8.7	
AZ tune	3.0	3.4	3.0	3.4	3.0	3.4	
Charm-quark mass	1.2	1.5	1.2	1.5	1.2	1.5	
Parton shower $\mu_{\rm F}$ with heavy-flavour decorrelation	on 5.0	6.9	5.0	6.9	5.0	6.9	
Parton shower PDF uncertainty	3.6	4.0	2.6	2.4	1.0	1.6	
Angular coefficients	5.8	5.3	5.8	5.3	5.8	5.3	
Total	15.9	18.1	14.8	17.2	11.6	12.9	

- PDFs are the dominant uncertainty, followed by p_T W uncertainty due to heavy-flavour-initiated production
- PDF uncertainties are partially anti-correlated between W+ and W-, and significantly reduced by the combination of these two categories.
- p_T W uncertainties are similar for m_w extracted from p_T lepton and from m_T

Models for $p_T W$

Since the $p_T Z$ distribution is very well measured, the relevant theoretical uncertainties are those which affect the W/Z p_T distribution



Only Herwig, Pythia, and Powheg predict a monotonic falling W/Z pt ratio



MINLO and NNLL analytic resummed predictions as Resbos, Cute, and DyRes are strongly disfavoured by the recoil distribution in data

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- The modelling of p_{τ} W is crucial for the measurement of m_w , especially when using p_{τ} lepton
- ~300 pb⁻¹ already collected at $<\mu>$ = 2 by ATLAS and CMS can provide a new ~1% measurement of p_{τ} W and significantly reduce the associated uncertainty



• The expected resolution at $<\mu>$ = 2 is \sim 5 GeV

Uncertainties in the p_T W modelling

- Heavy-flavour-initiated (HFI) production introduce differences between Z and W production
- HFI production determines a harder boson p_T spectrum, $cc \rightarrow Z$ and $bb \rightarrow Z$ are 6% and 3% of Z production, $cs \rightarrow W$ is ~20% of W production
- HFI addressed with charm-quark mass variations, and by decorrelating the PS μ_F between light and HFI processes



 p_T W theory uncertainties are evaluated as the sum of experimental Z p_T unc. and theory unc. on the W/Z p_T ratio



W mass at the LHC

- A large fraction of W production at the LHC is inititiated by sea quarks
- The W polarisation at the LHC is more influenced by PDF uncertainties, implying larger uncertainties on the lepton p_T distribution
- The valence-sea difference, as well as the amount of sea quarks with u and d flavour, must be known with better precision than needed at the Tevatron



- The effect can be isolated by switching off spin correlations
- O(10-20) MeV effect for m_w extracted from the p_T lepton distribution

 Large reduction of PDF
uncertainties near the Jacobian peak

p_T W uncertainties on p_T lepton and m_T

 p_T W uncertainties are similar for m_W extracted from p_T lepton and from m_T



on m_T are less distinguishable from m_W variations

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