

Measurements of the Λ - Λ , p- Λ and p- Ξ^- interaction via the femtoscopy method

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22.10.2019



150 Jahre
culture of
excellence



SFB 1258

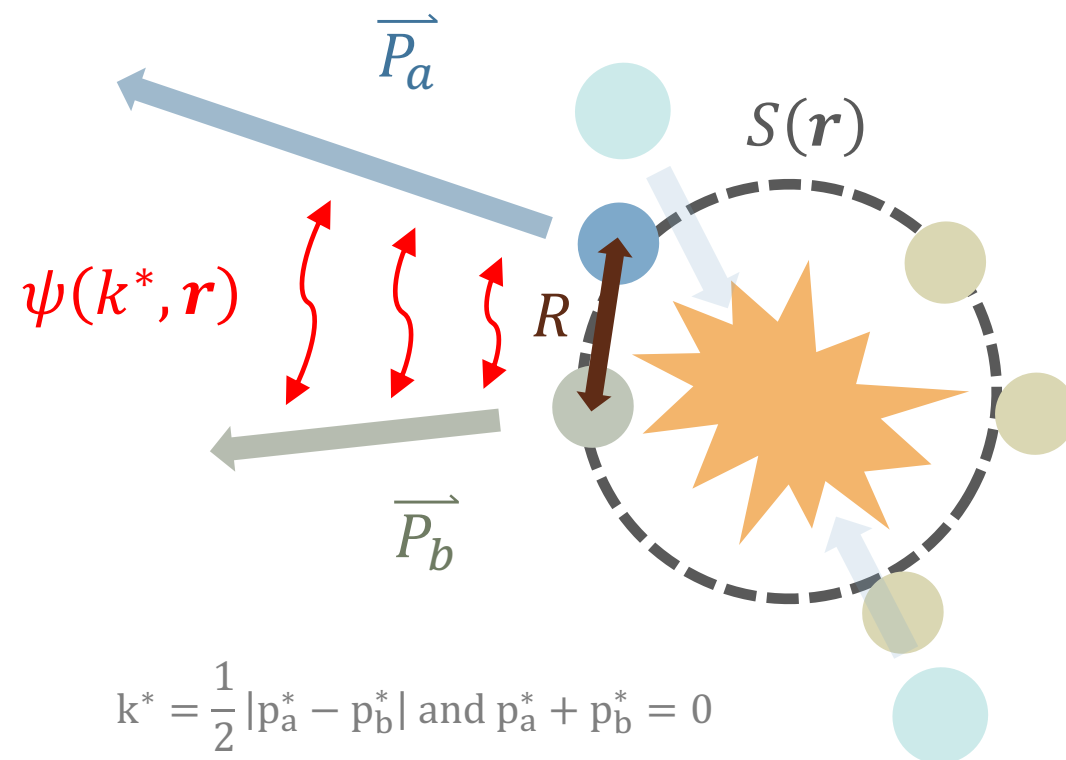
Neutrinos
Dark Matter
Messengers



Femtoscopic measurement

$$C(k^*) = \frac{\mathcal{P}(\vec{p}_a, \vec{p}_b)}{\mathcal{P}(\vec{p}_a)\mathcal{P}(\vec{p}_b)} = \int S(\mathbf{r}) |\psi(k^*, \mathbf{r})| d^3r = \mathcal{N} \frac{N_{same}}{N_{mixed}}$$

- Traditionally used to study the emission source $S(\mathbf{r})$ with particles of known interaction
- Reversing the paradigm: Study interactions
 - All detectable particle species can be studied



$$k^* = \frac{1}{2} |\mathbf{p}_a^* - \mathbf{p}_b^*| \text{ and } \mathbf{p}_a^* + \mathbf{p}_b^* = 0$$

Femtoscopic measurement

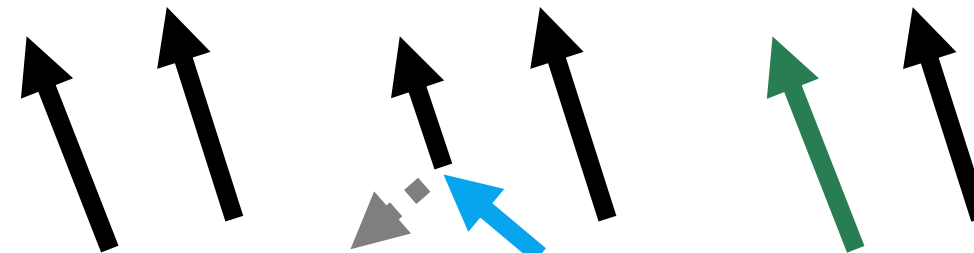
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Evaluation of $C(k^*)$ within the CATS framework

<https://doi.org/10.1140/epjc/s10052-018-5859-0>

- Analytically using the **Lednický model**
R. Lednický and V.L. Lyuboshits, Sov. J. Nucl. Phys. 53, 770 (1982)
 - Modelling of the interaction via scattering length (f_0) and effective range (d_0)
- **Numerically** solving the Schrödinger equation
 - Accounting for any (local) strong interaction potentials, quantum statistics and Coulomb interaction

Residual correlations



$$C_{tot}(k^*) = \lambda_0 C_0 \oplus \lambda_1 C_1 \oplus \lambda_2 C_2 \oplus \dots$$

Contributions from: genuine feed-down misidentifications

$$C(k^*) = 1 + \lambda_{genuine} (C_{genuine}(k^*) - 1) + \sum_{ij} \lambda_{ij} (C_{ij}(k^*) - 1)$$

- Pair contributions quantified by purity ($\mathcal{P}_i$) and feed down fractions (f_i):

$$\lambda_{ij} = \mathcal{P}_{i_1} \cdot f_{i_1} \cdot \mathcal{P}_{j_2} \cdot f_{j_2}$$

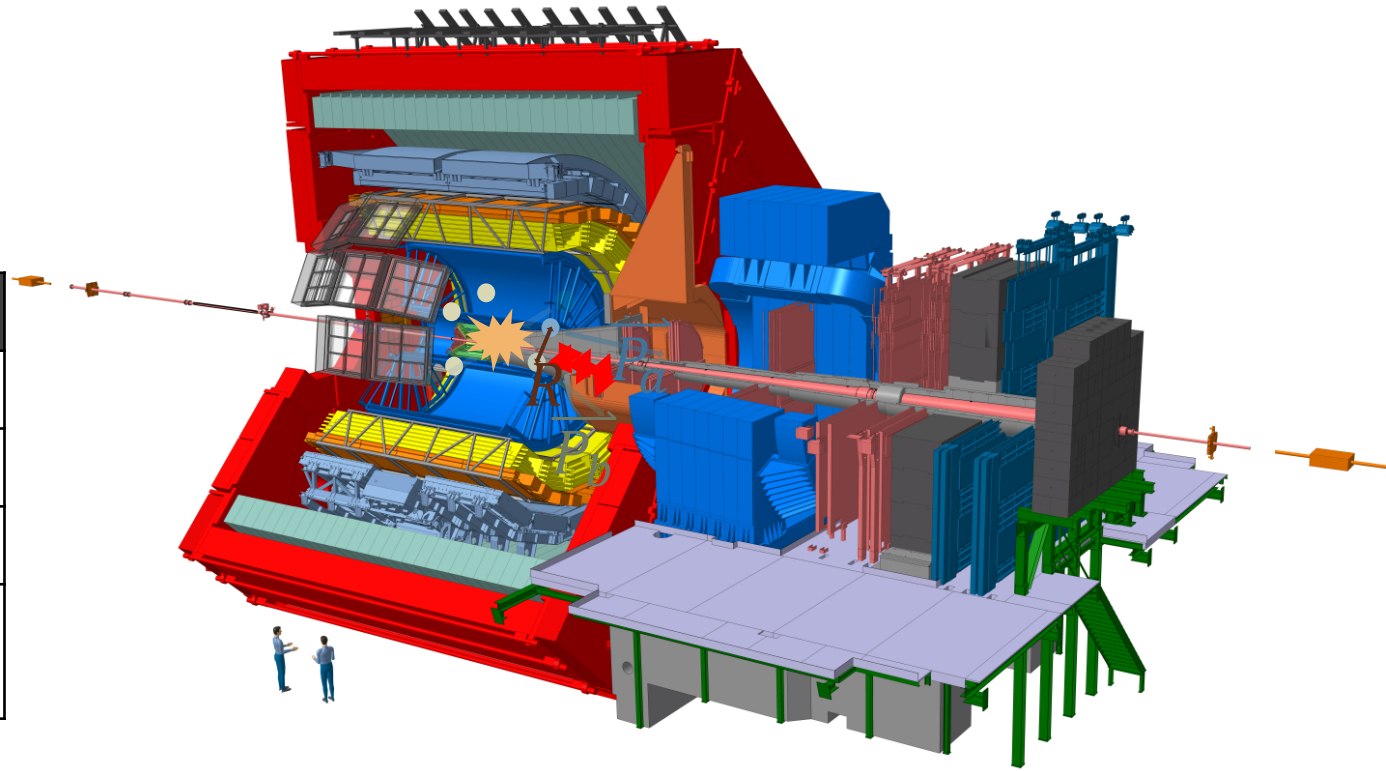
- Smearing for finite momentum resolution of the detector
- Non flat baseline

(Details see Phys. Rev. C 99 (2019), 024001)

The Detector: ALICE

- Particle identification with TPC (dE/dx) and TOF
 - Direct detection of charged particles (p, K, π)
 - Reconstruction of Hyperons:
 $\Lambda \rightarrow p\pi^-$ and $\Xi^- \rightarrow \Lambda\pi^-$
- Datasets:

System	# Events
pp 7 TeV	3.4×10^8 minimum bias
p-Pb 5.02 TeV	6.0×10^8 minimum bias
pp 13 TeV	15×10^8 minimum bias
	10×10^8 high multiplicity (0-0.072% INEL)

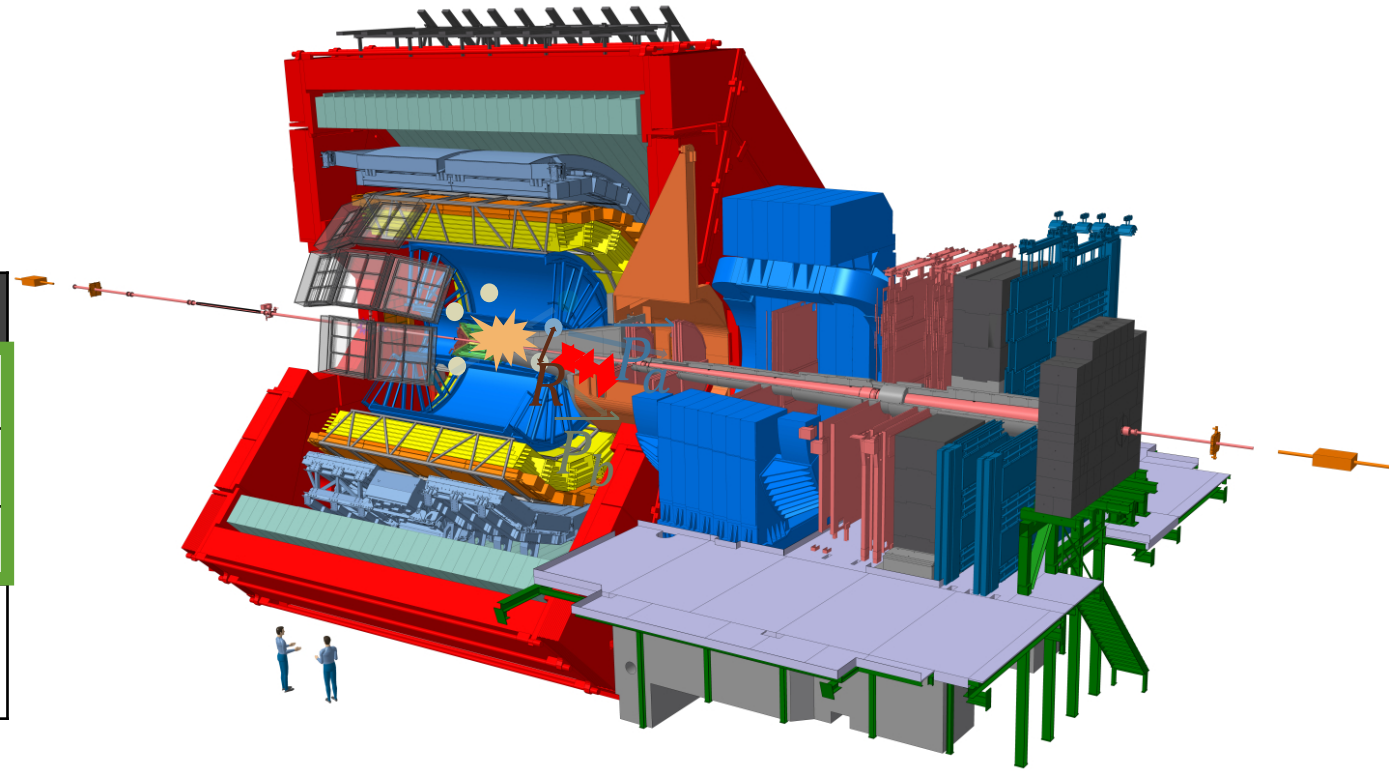


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$\Lambda - \Lambda$



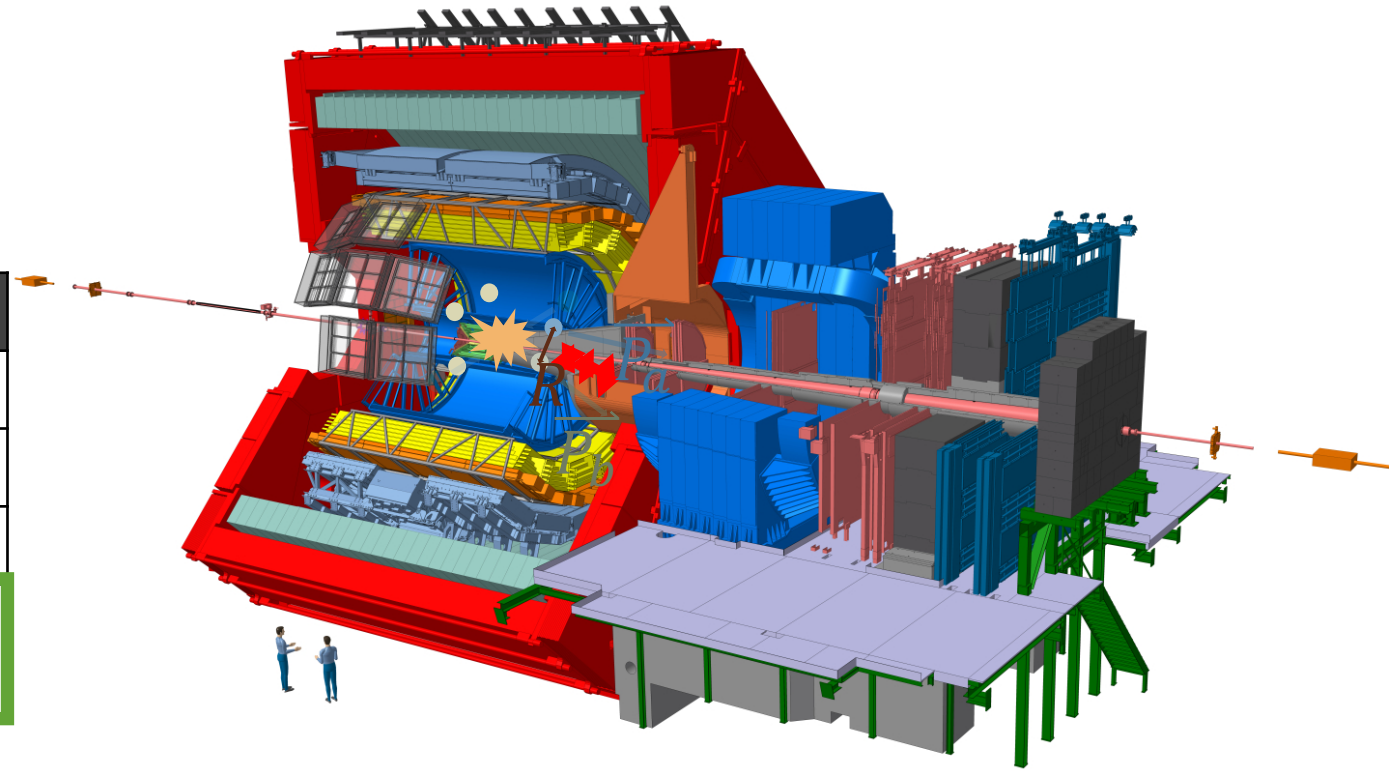
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$p-\Lambda$

$p-\Xi$



Λ – Λ Femtoscopy

Published: ALICE Collaboration, PLB 797, 134822

<https://doi.org/10.1016/j.physletb.2019.134822>

Datasets: Minimum Bias pp 7 & 13 TeV, p-Pb 5.02 TeV



ALICE

Λ - Λ interaction

- No scattering data
- The observed double Λ hyper-nuclei events predict a shallow attraction

H. Takahashi et al., PRL 87 (2001) 212502.

- $B_{\Lambda-\Lambda} = 6.91 \pm 0.16$ MeV
- Femtoscopic analysis in heavy-ion collisions (STAR) extremely inconclusive, due to the unconstrained residual signal

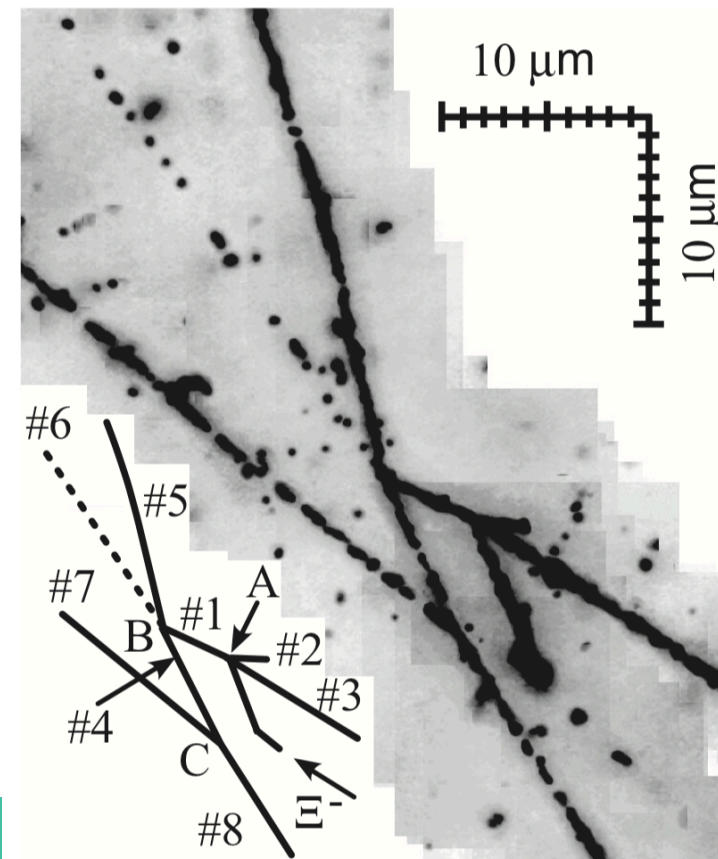
Original analysis by STAR
PRL 114 (2015), 022301.

Repulsive potential?

Reanalysis by Morita *et al.*
PRC 91 (2015), 024916.

Attractive potential?

Small scattering length ($|f_0| \leq 1$ fm)
Large effective range ($d_0 \geq 4$ fm)

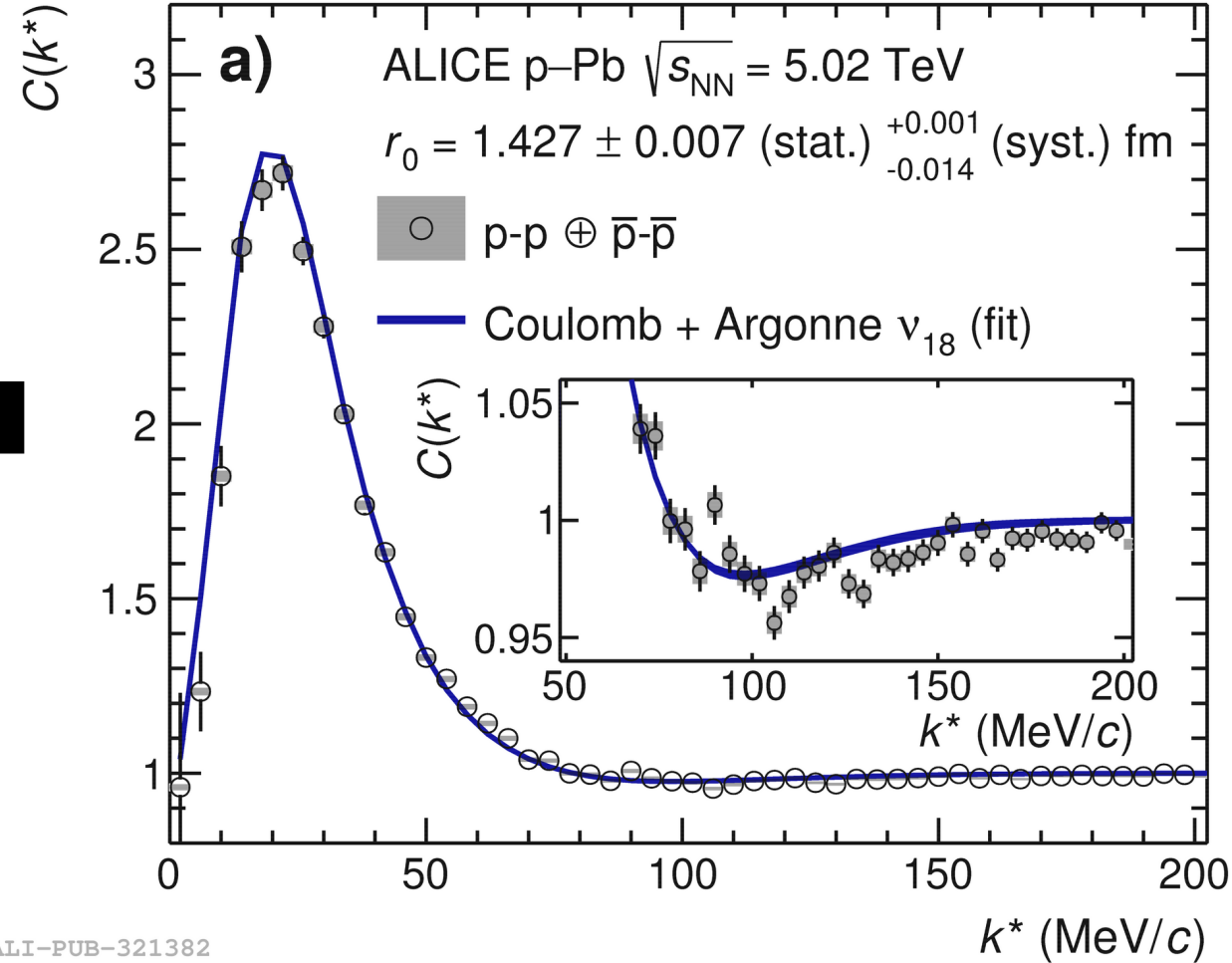


J. K. Ahn *et al.*, PRC 88, 014003 (2013)

Constraining the source

- Assumption: $S(\mathbf{r})$ Gaussian and same for all particle pairs
 - p-p interaction: well known
- Source sizes for the three systems:

System	Radius
pp 7 TeV	$1.125 \pm 0.018 (\text{stat.})^{+0.058}_{-0.035} (\text{syst.}) \text{ fm}$
pp 13 TeV	$1.182 \pm 0.008 (\text{stat.})^{+0.005}_{-0.002} (\text{syst.}) \text{ fm}$
p-Pb 5 TeV	$1.427 \pm 0.007 (\text{stat.})^{+0.001}_{-0.014} (\text{syst.}) \text{ fm}$



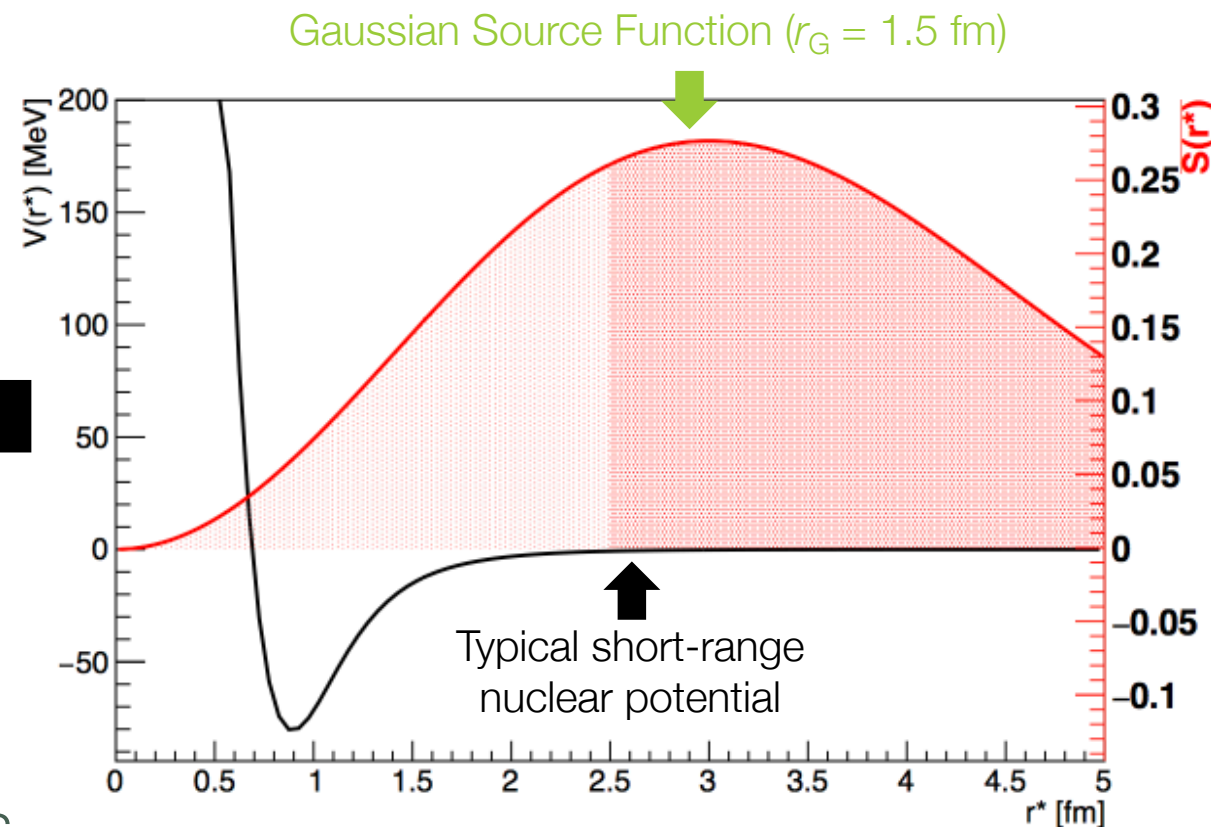
Constraining the source

- Assumption: $S(\mathbf{r})$ Gaussian and same for all particle pairs

- p-p interaction: well known
- Source sizes for the three systems:

System	Radius
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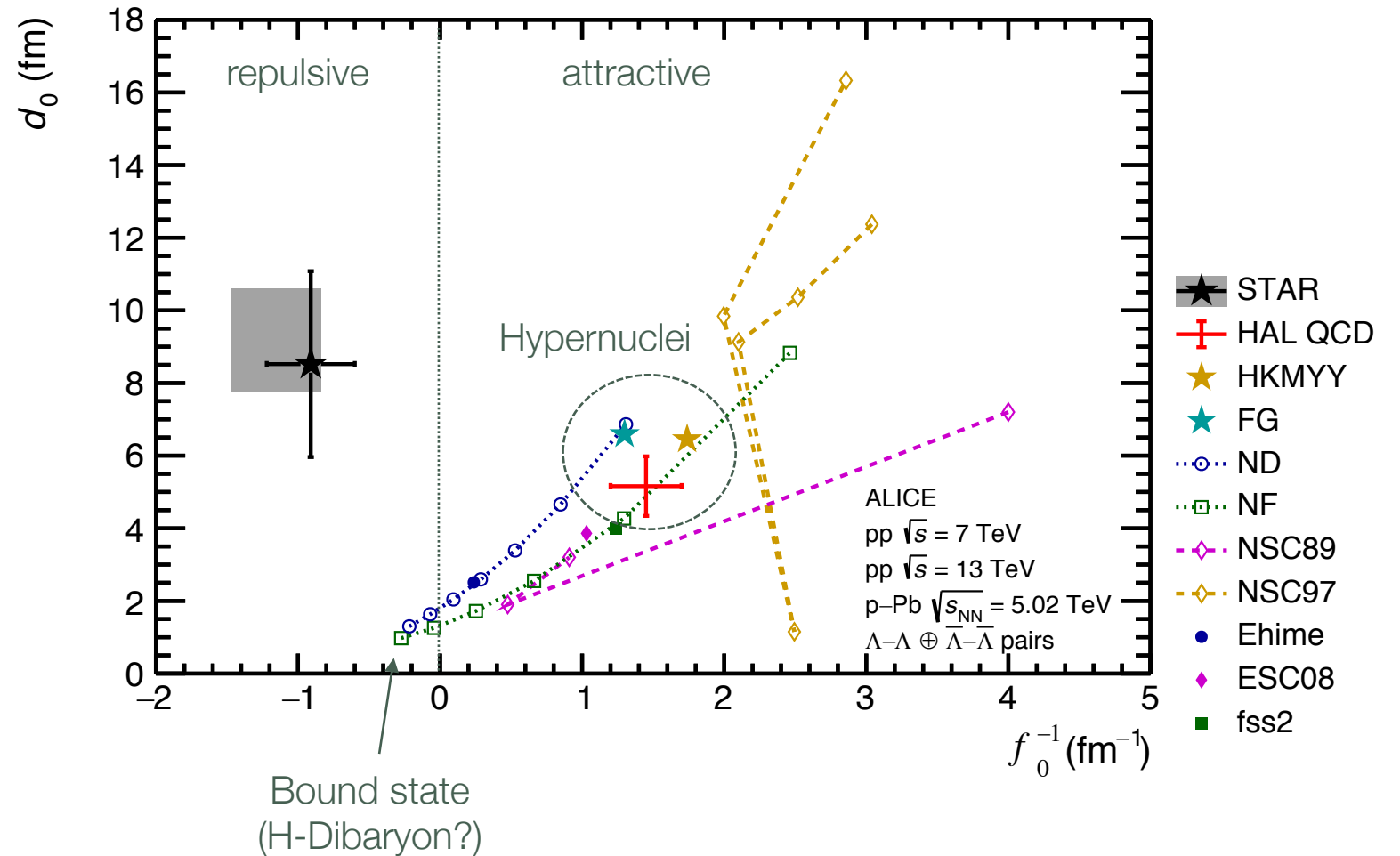
- Source size of the same magnitude as strong interaction potentials



Λ - Λ interaction

- Theoretical models and experimental measurements cover a wide range in the scattering parameter phase space

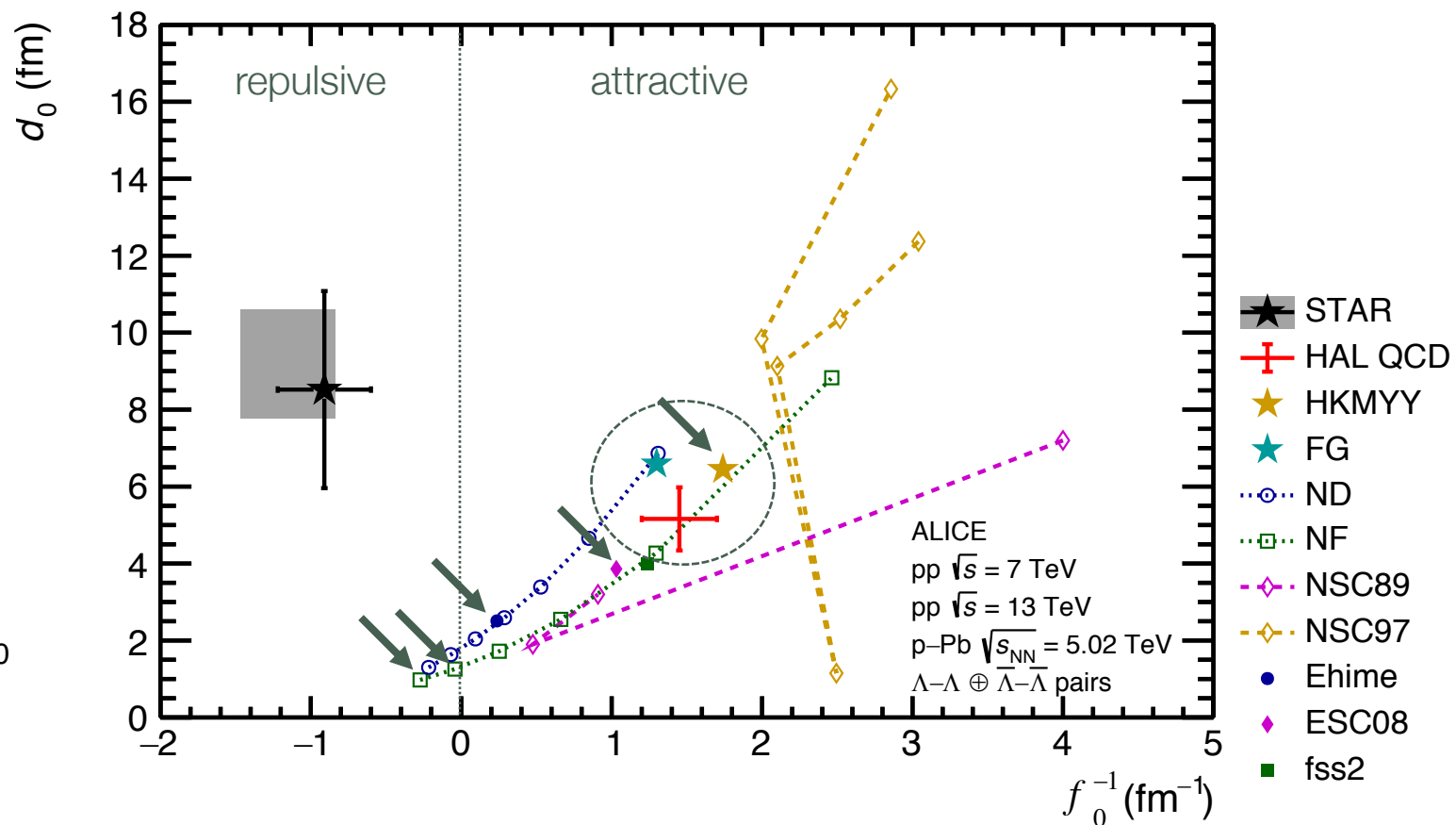
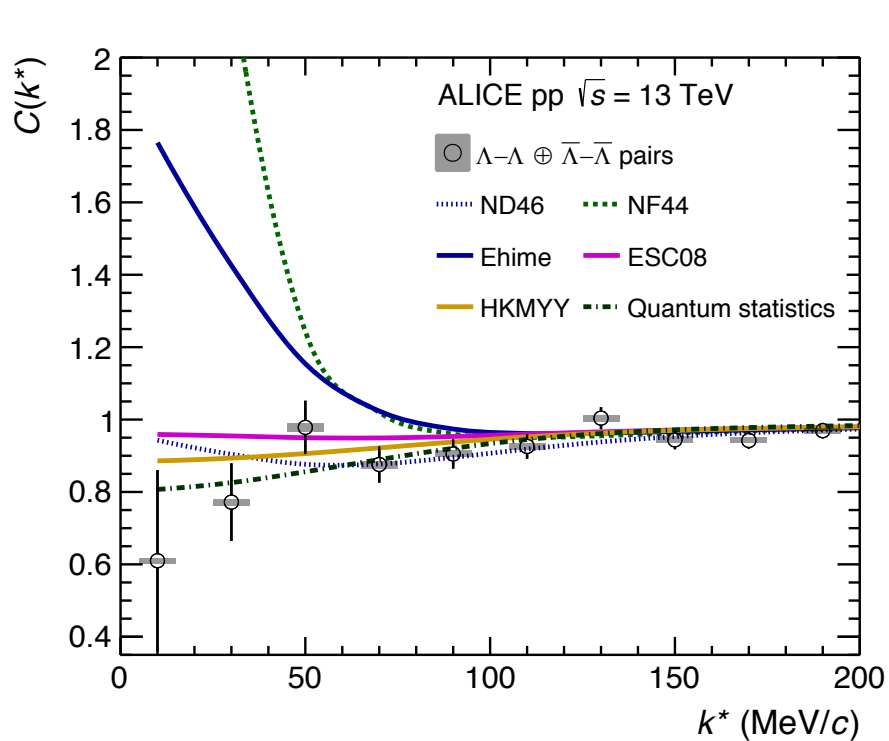
- Measurement: STAR Collab., PRL 114 (2015) 022301.
- Models from K. Morita *et al.*, PRC 91 (2015) 024916.
- HAL QCD: K. Sasaki and T. Hatsuda (HAL QCD Collab.), private communication.





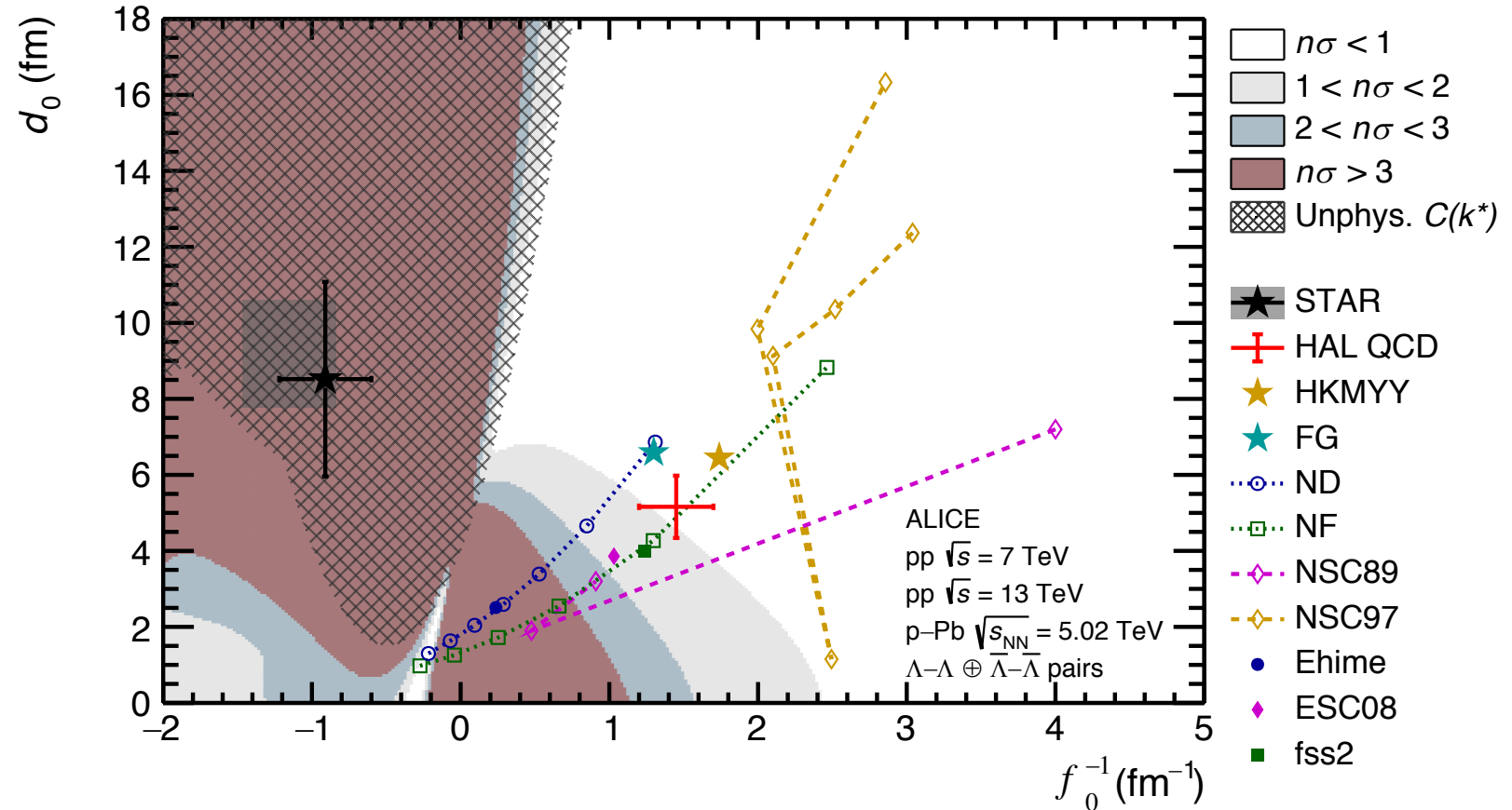
ALICE

Λ - Λ interaction



Λ - Λ femtoscopy

- Combination of all analyzed datasets
 - pp 7 & 13 TeV
 - p-Pb 5.02 TeV
- Test of the agreement between data and the prediction by the Lednický model in $n\sigma$
 - Under the hypothesis of a **common, Gaussian source**
 - Small source size limits the prediction power of the Lednický model



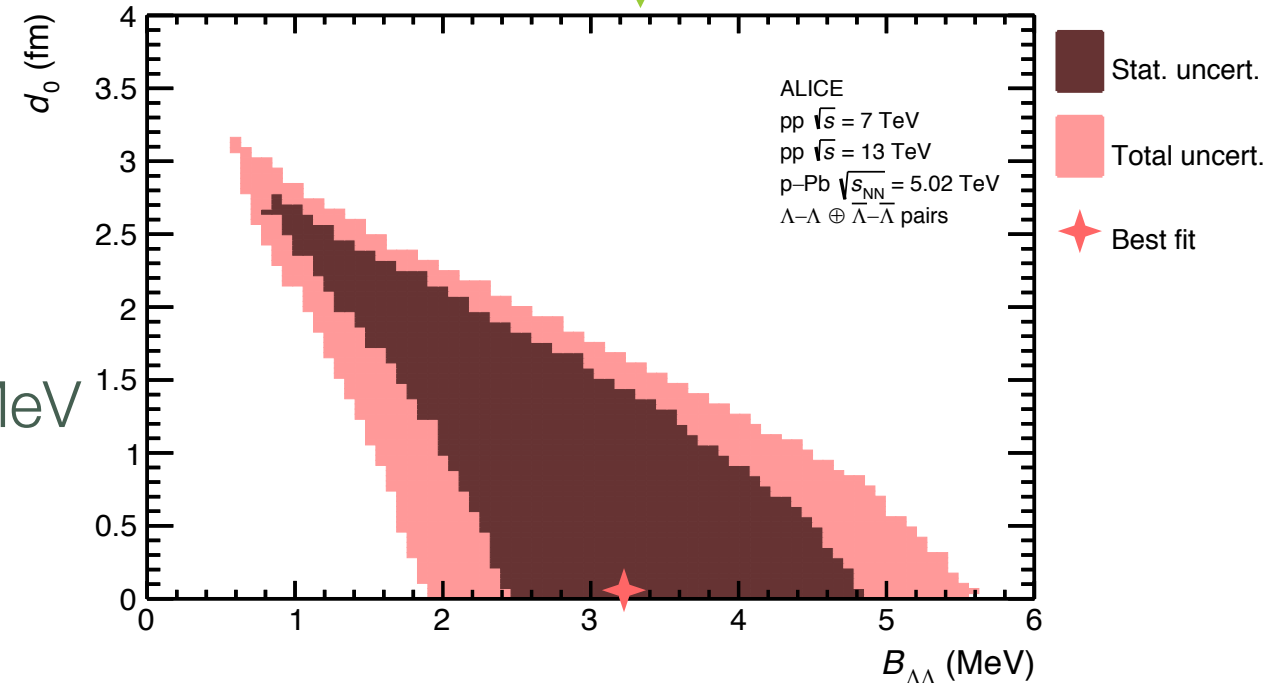
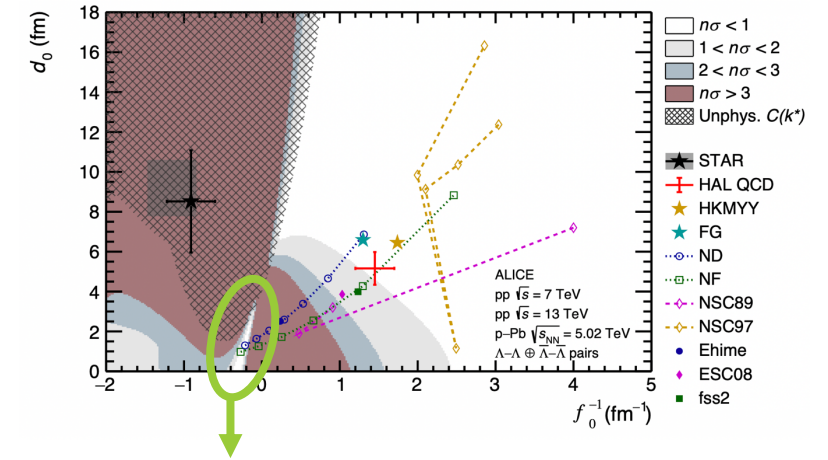
Λ - Λ femtoscopy – H-Dibaryon

$$B_{\Lambda\Lambda} = \frac{1}{m_{\Lambda} d_0^2} \cdot \left(1 - \sqrt{1 + \frac{2d_0}{f_0}} \right)$$

S. Gongyo et al., PRL 120 (2018) 212001.

P. Naidon and S. Endo, Rept. Prog. Phys. 80 (2017) 056001.

- H-Dibaryon: Tight constraints on the allowed binding energy
 - $B_{\Lambda-\Lambda} = 3.2_{-2.4}^{+1.6} \text{ (stat.) }_{-1.0}^{+1.8} \text{ (syst.) MeV}$
 - More stringent than previous measurements





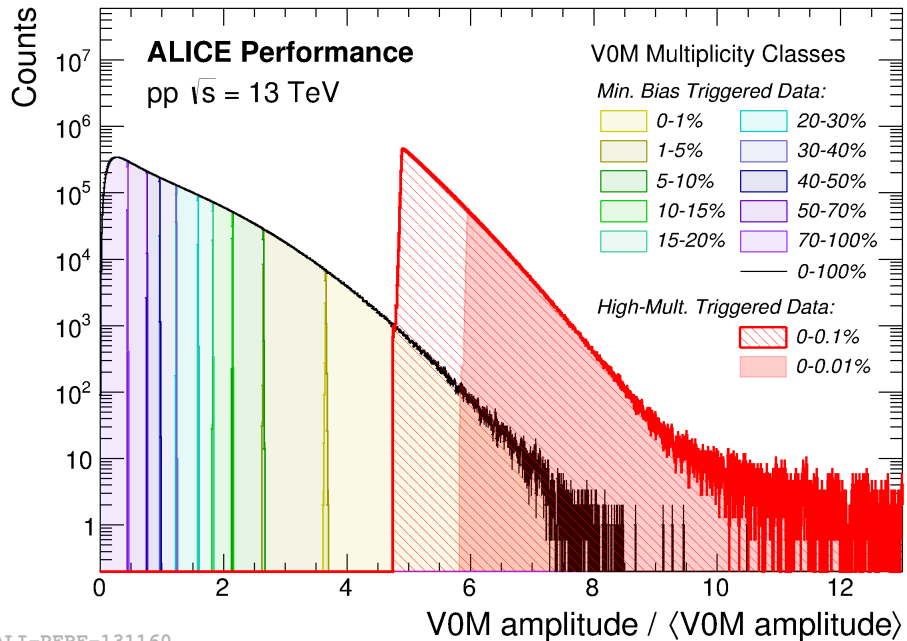
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High multiplicity dataset

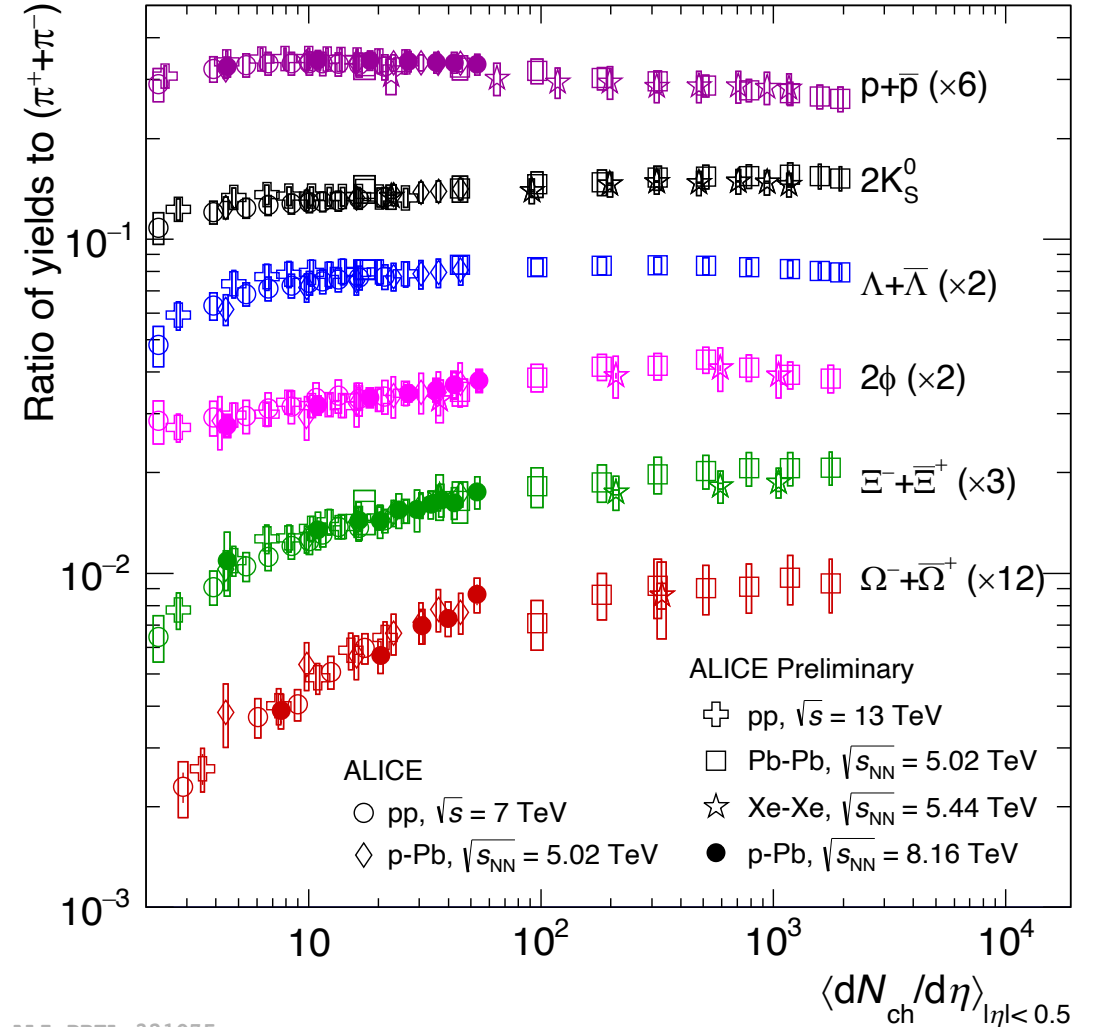
p-p collisions at 13 TeV

High Multiplicity Dataset

- Increased average multiplicity & production of hyperons
 - Significant increase in amount of pairs by a factor of 5-10



ALI-PERF-131160



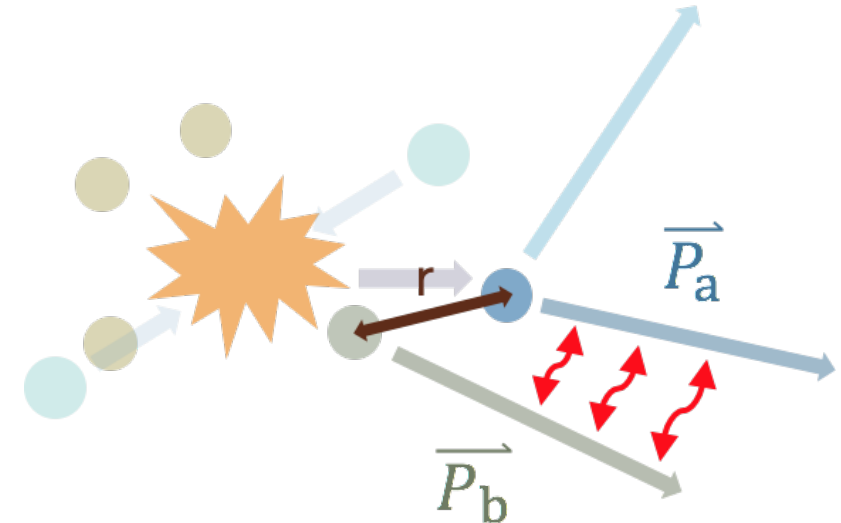
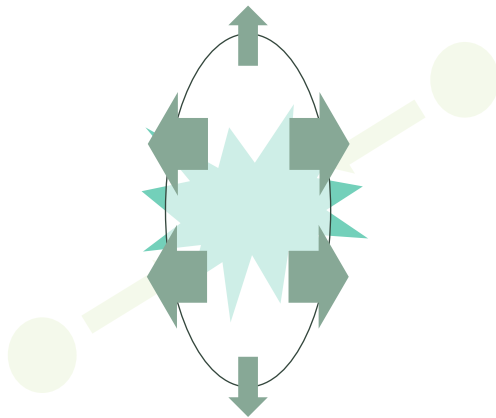
ALI-PREL-321075

Collective effects and strongly decaying resonances

(An)isotropic flow

+

Strongly decaying resonances



- (An) isotropic pressure gradients affect the emission
 - Initial geometric anisotropies introduce a transverse modulation
 - Expanding source with common velocity field
- Affects particles depending on their masses

- Resonances with $ct \sim r_0 \sim 1$ fm (Δ^* , N^* , Σ^*) introduce an exponential tail to the source
- Different for each particle species



ALICE

Collective effects and strongly decaying resonances

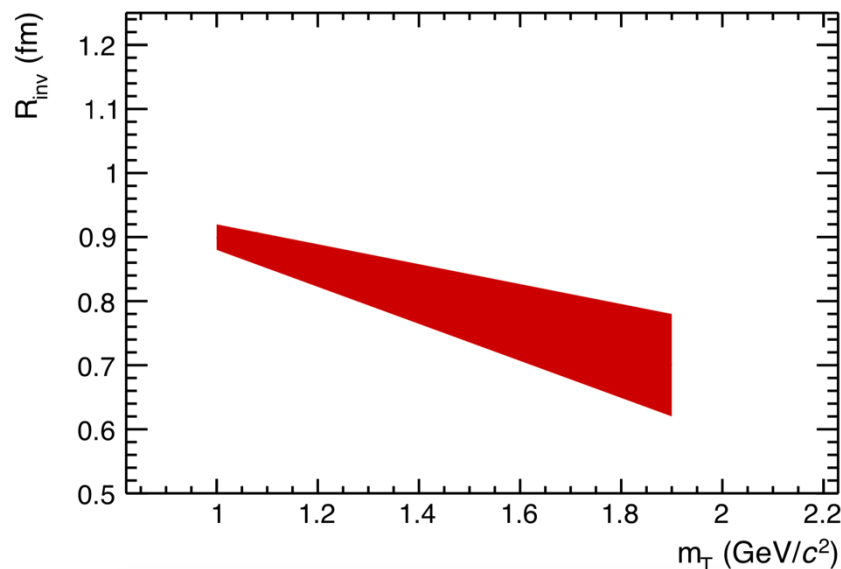
(An)isotropic flow

+ Strongly decaying resonances

Gaussian core

⊗

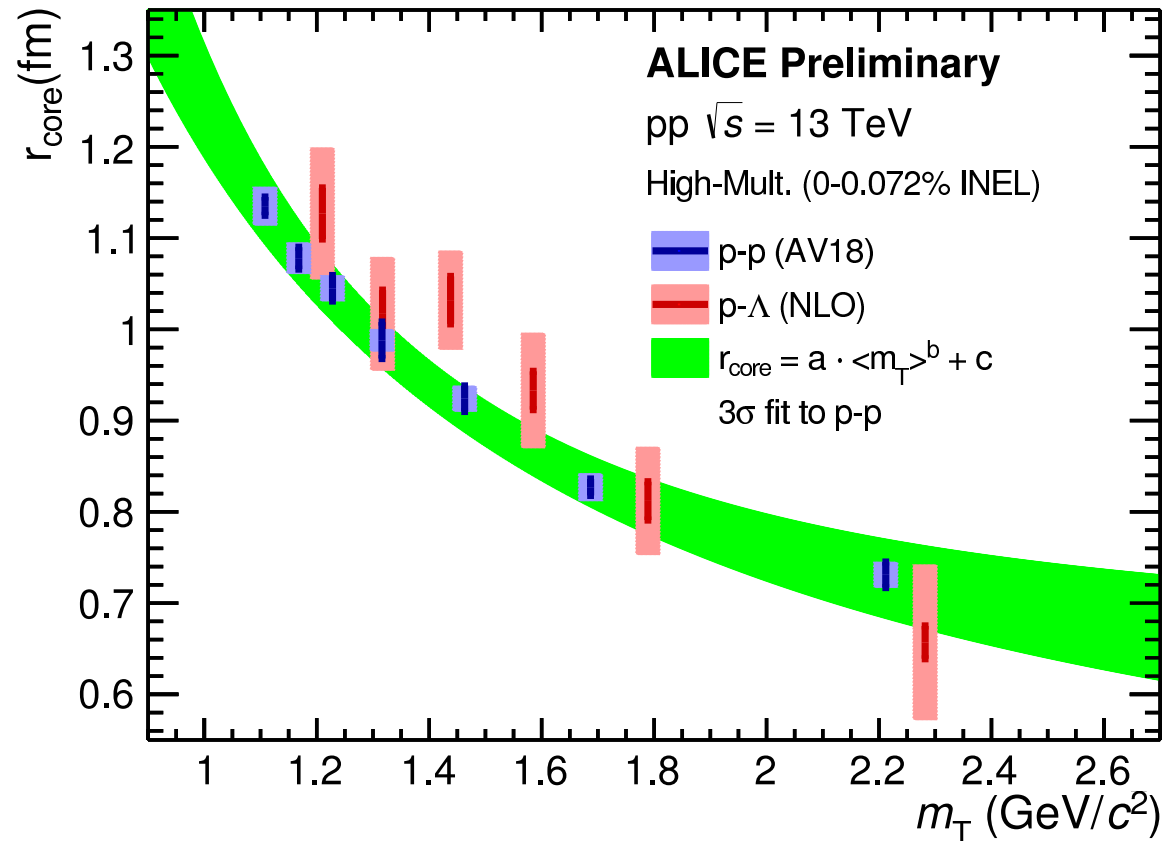
Exponential tail



Particle	Primordial fraction	Resonances	
		$1 < c\tau < 2 \text{ fm}$	$c\tau > 2 \text{ fm}$
Proton	33 %	56 %	2 %
Lambda	35 %	8 %	58 %

- Amount of resonances determined within the Statistical Hadronization Model in the canonical approach
- Priv. Comm. with Prof. F. Becattini
J.Phys. G38 (2011) 025002.

m_T dependence of the Gaussian core radius

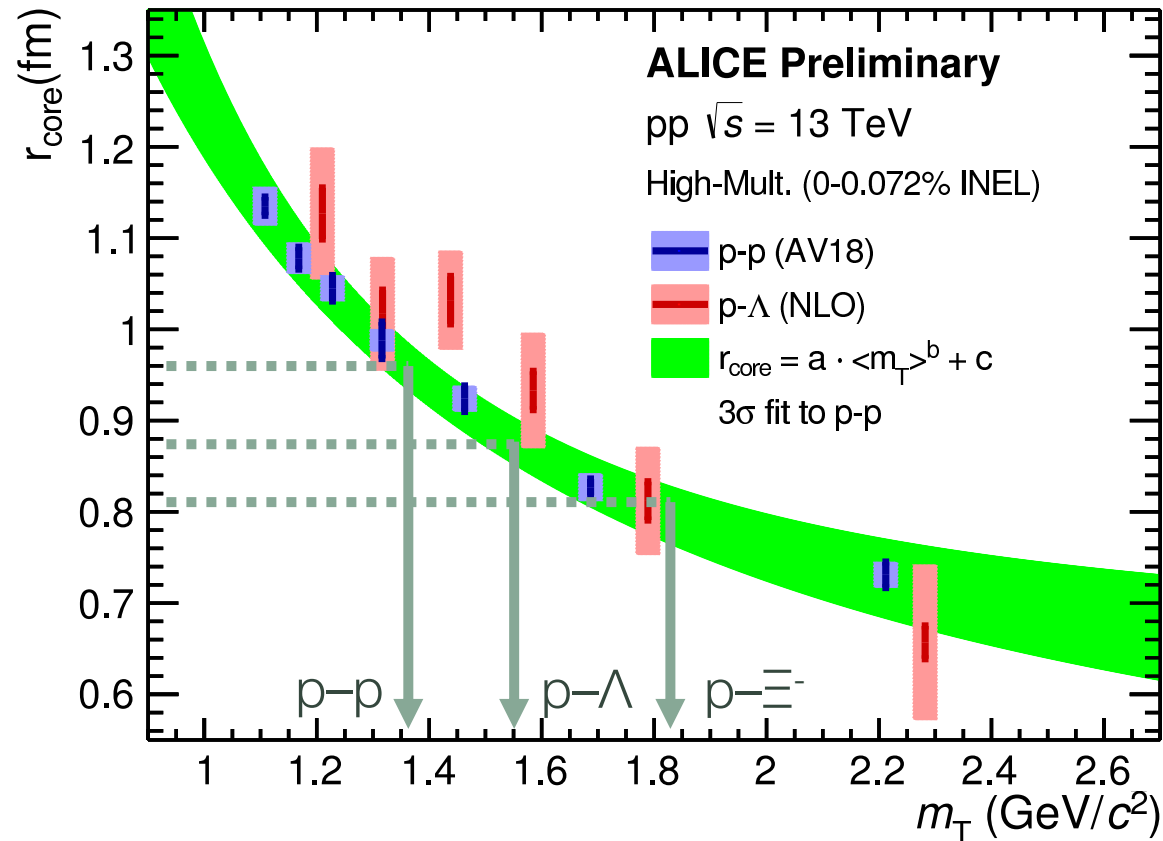


ALI-PREL-315640

- Core radius for p-p and p- Λ in agreement

D. Mihaylov (ALICE)
[WPCF2019](#)

m_T dependence of the Gaussian core radius



ALI-PREL-315640

- Fix the value of r_{Core} of each particle species based on their $\langle m_T \rangle$
 - Add specific resonance contribution to obtain the corresponding pair source

D. Mihaylov (ALICE)
[WPCF2019](#)



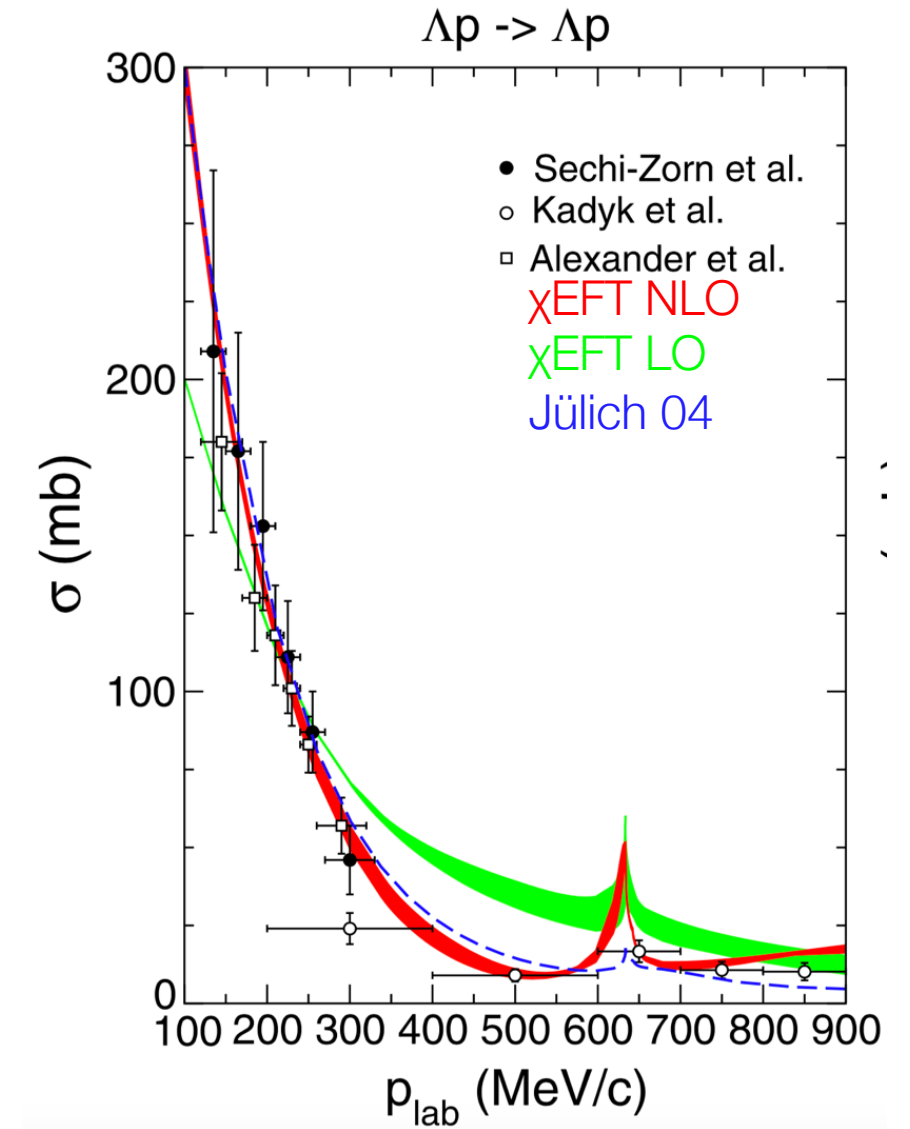
ALICE

p- Λ Femtoscopy

Dataset: High multiplicity pp 13 TeV

Proton Λ interaction

- Indirect measurement via hypernuclei
- Scarce scattering data
 - No constraints at lab momenta below 100 MeV/c
- Theoretical predictions for cusp in Λ -N due to the Σ -N - Λ -N coupling
 - Coupling introduces a repulsive short range component in the p- Λ interaction
 - Not experimentally confirmed so far

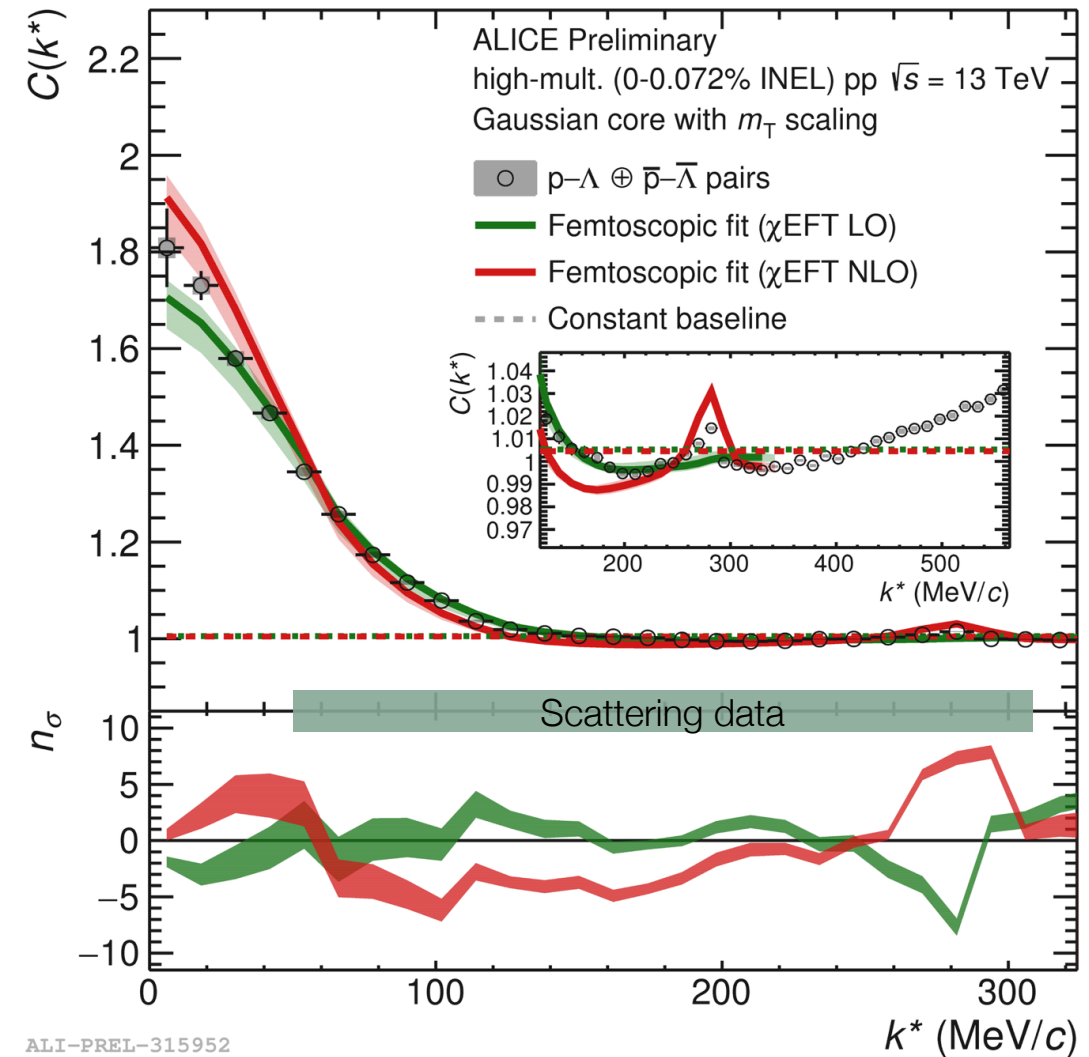


J. Haidenbauer et al., Nucl. Phys. A 915 (2013) 24.



Measurement of the p- Λ correlation function

- Significant extension of the kinematic range
- Clear experimental evidence for the cusp
- Different variations of the baseline
 - Constant, linear & quadratic
 - Best fit for LO: $n_\sigma > 8$
 - Best fit for NLO: $n_\sigma > 10$
- LO and NLO calculations of the interaction within χ EFT fail to reproduce the data
 - Entering a precision era!



p- Ξ - Femtoscropy

Continuation of the analysis in minimum bias p-Pb 5.02 TeV

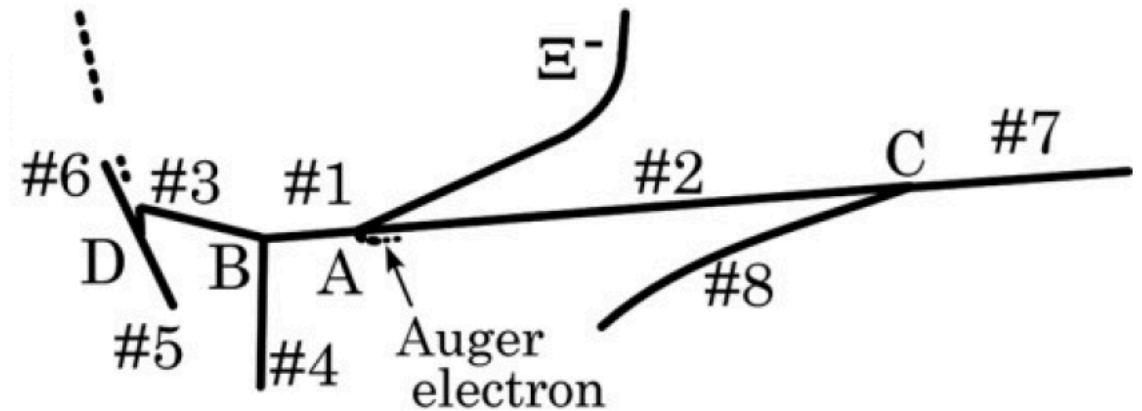
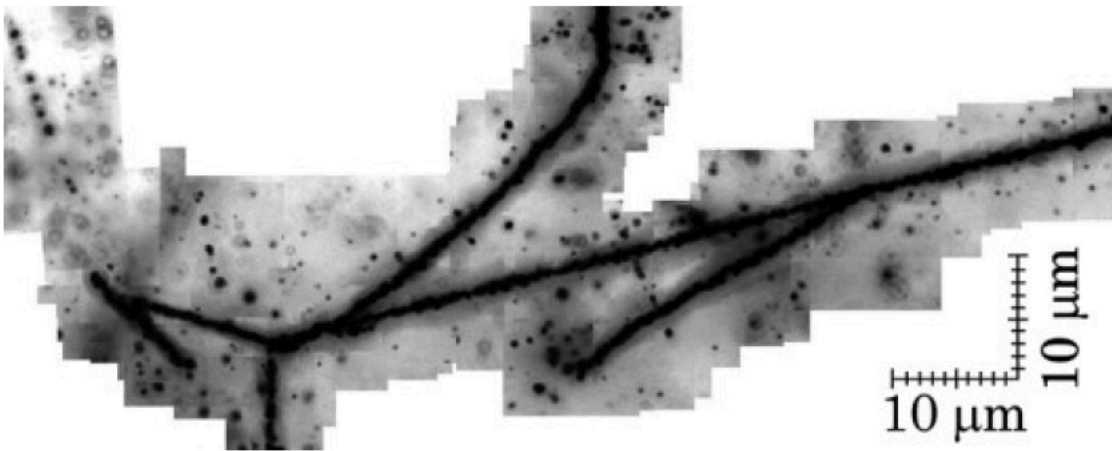
ALICE Collaboration, PRL 123, 112002

<https://doi.org/10.1103/PhysRevLett.123.112002>

Dataset: High multiplicity pp 13 TeV

Data on Ξ interaction

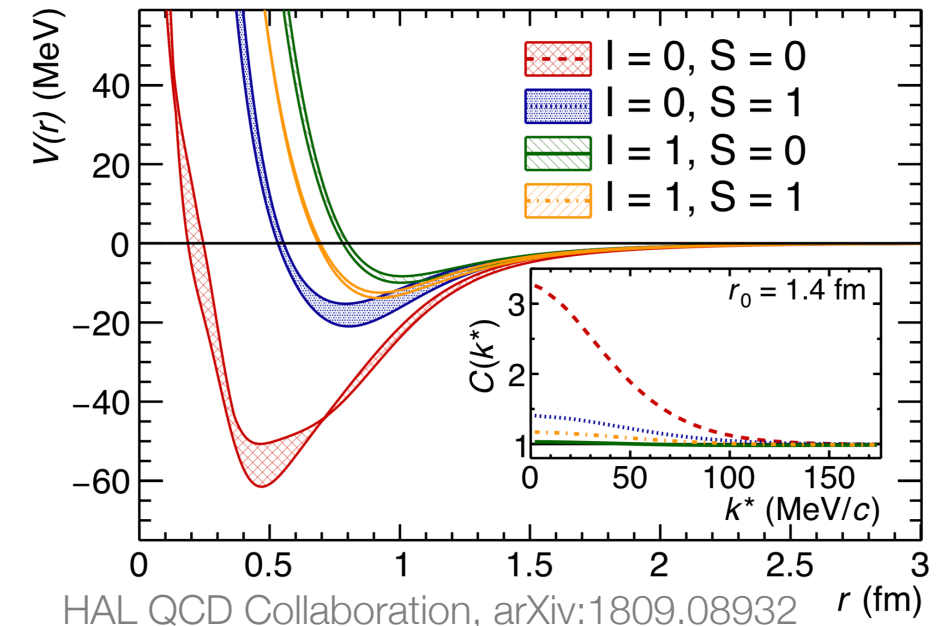
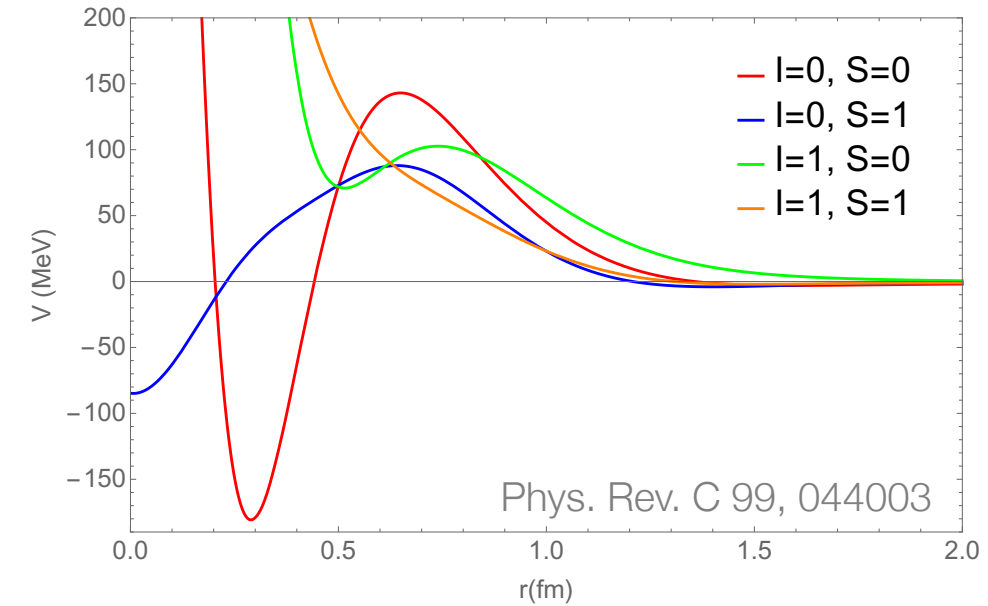
- Kiso and Ibuki Event: Ξ^- hyper nucleus
- Points towards an attractive interaction
 - Hyper nucleus binding energy $B_{\Xi^-} \sim 1$ MeV



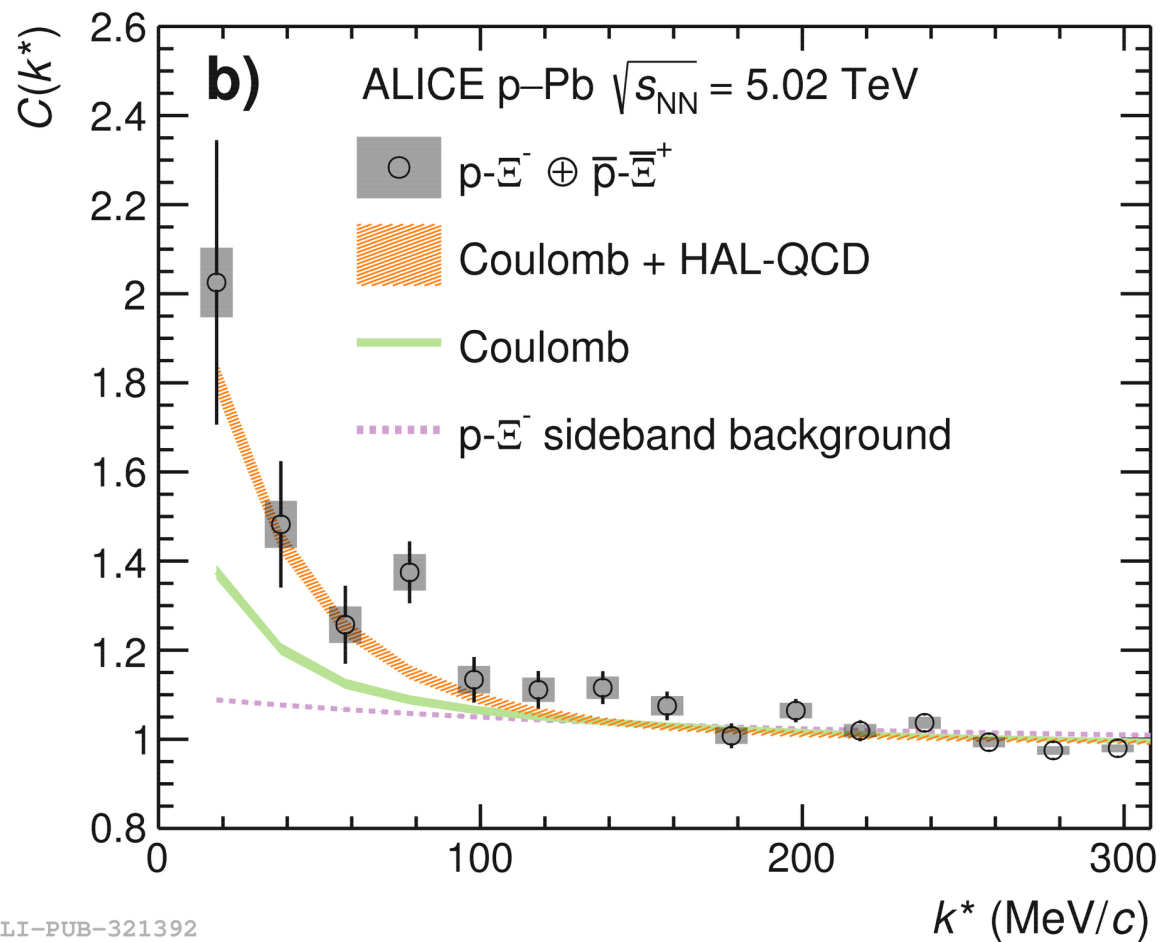
The N- Ξ interaction

	$I = 0$	$I = 1$	Detectable
$n-\Xi^-$	X	✓	No
$p-\Xi^0$	X	✓	Difficult
$p-\Xi^{*+}$	✓	X	Difficult
$p-\Xi^-$	✓	✓	Yes

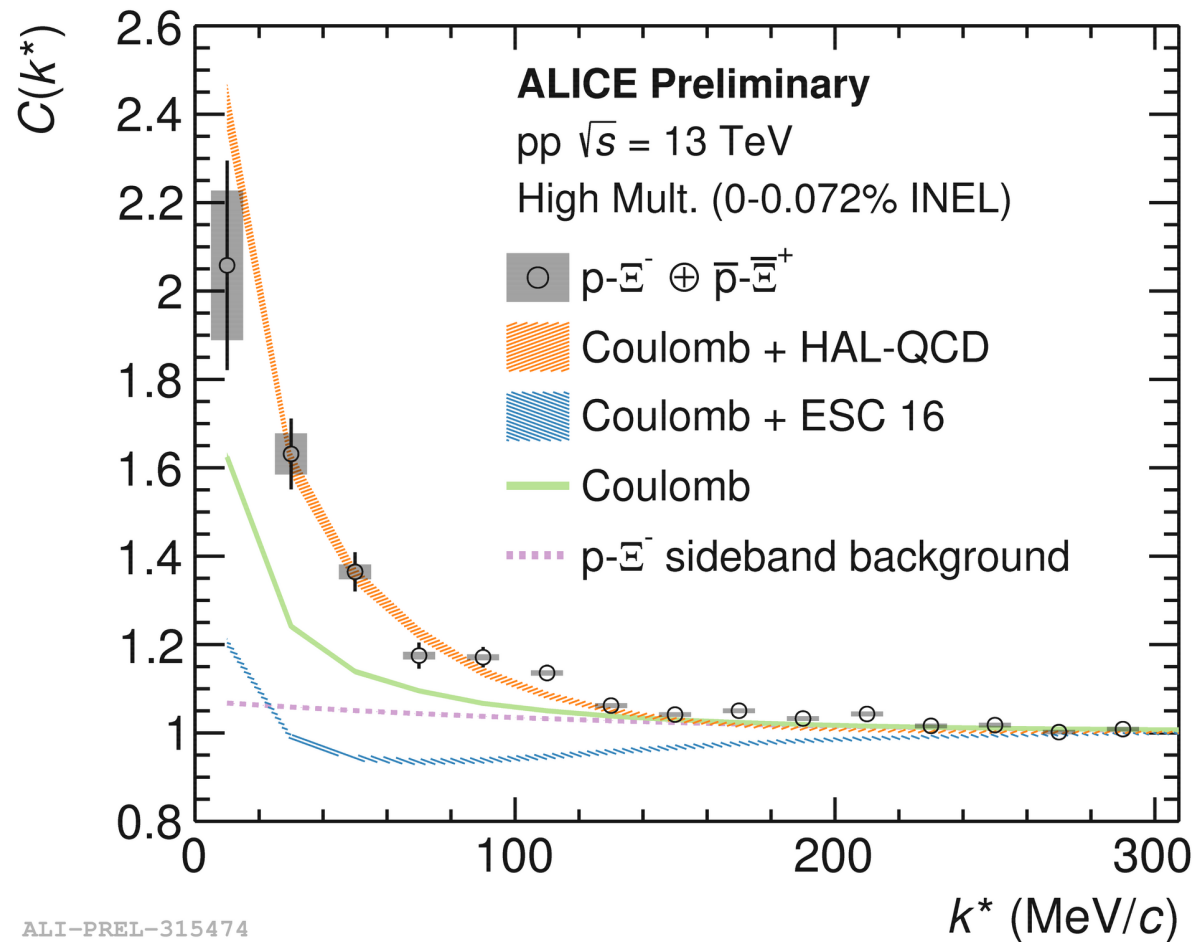
- Null Hypothesis: Coulomb only
- HAL QCD Potential
- NEW: Potential by Nijmegen group



Measurement of the $p\text{-}\Xi^-$ interaction



ALI-PUB-321392

<https://doi.org/10.1103/PhysRevLett.123.112002>


ALI-PREL-315474

Summary and Outlook

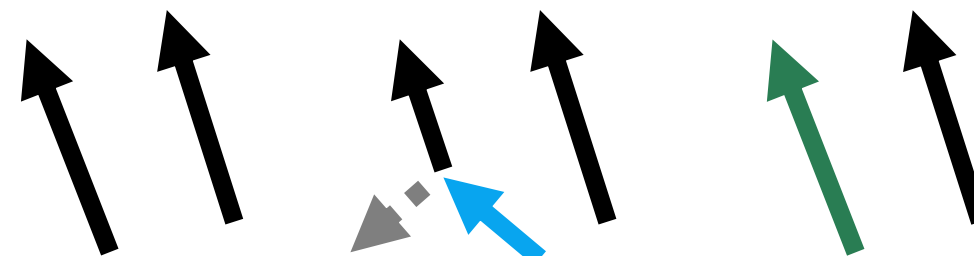
- Λ – Λ correlation function interaction studies
 - Combined analysis of different datasets
 - Analysis of high multiplicity data
 - Constraint on the parameter space
 - Upper limit on the binding energy of a hypothetical Λ – Λ bound state
- p – Λ correlation function interaction studies
 - Experimental confirmation of cusp effects in p – Λ
 - Providing constraints with unprecedented precision for theory
- p – Ξ^- correlation function interaction studies
 - Continuation of the p – Pb analysis
 - Confirms previous results: Observation of attractive strong interaction
 - Test of additional models



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Backup

Decomposition of $C(k^*)$

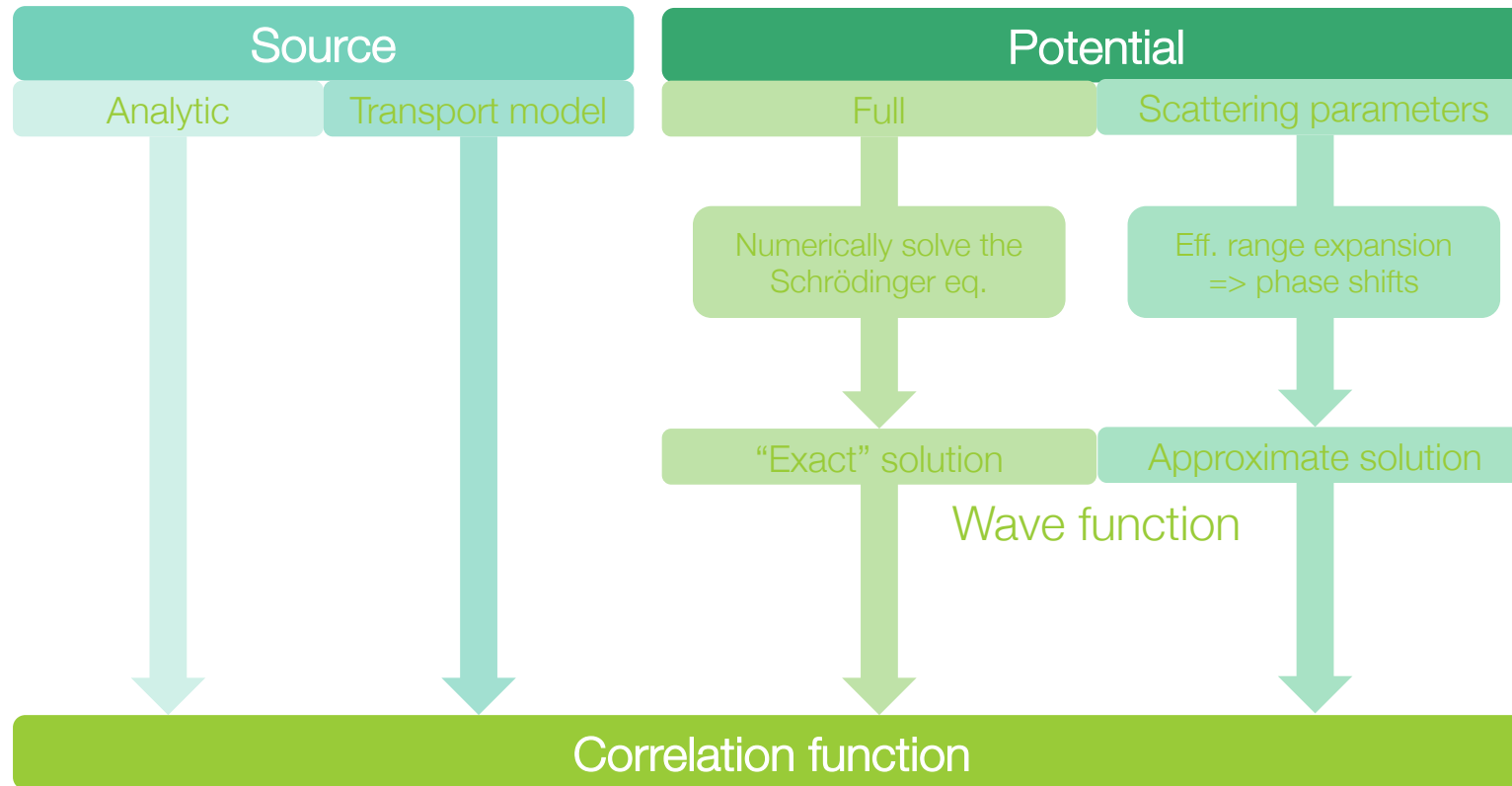


$$C_{tot}(k^*) = \lambda_0 C_0 \oplus \lambda_1 C_1 \oplus \lambda_2 C_2 \oplus \dots$$

Contributions from: genuine feed-down impurities

- Purity ($\mathcal{P}_i$) and Feed down fractions (f_i) yield weight of pair contributions as $\lambda_{ij} = \mathcal{P}_{i_1} \cdot f_{i_1} \cdot \mathcal{P}_{j_2} \cdot f_{j_2}$ (Details see Phys. Rev. C 99 (2019), 024001)
 - Purity: Fits of the Invariant mass and MC truth information
 - Feed down fractions: MC template fits to data
 - For all pairs: Genuine pair contribution dominates

Modelling the correlation function

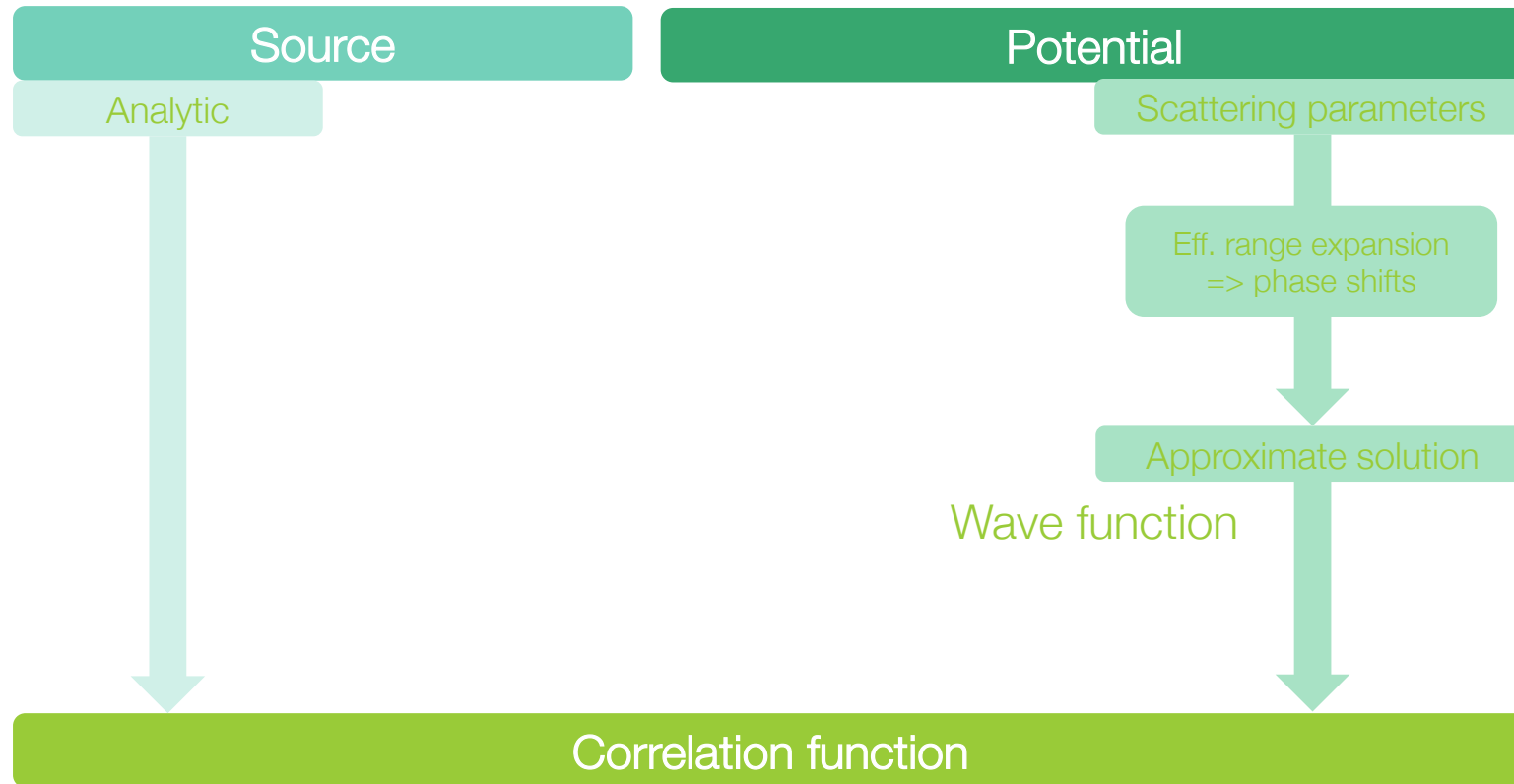


$$C(k^*) = \frac{P(\mathbf{p}_a, \mathbf{p}_b)}{P(\mathbf{p}_a)P(\mathbf{p}_b)} = \mathcal{N} \cdot \frac{N_{\text{same}}}{N_{\text{mixed}}} = \int S(\mathbf{r}) |\Psi(k^*, \vec{r})|^2 d\vec{r}$$

Emission source

Two-particle wave function

Lednicky model



$$C(k) = 1 + \sum_S \rho_S \left[\frac{1}{2} \left| \frac{f^S(k)}{R_G^{\Lambda p}} \right|^2 \left(1 - \frac{d_0^S}{2\sqrt{\pi} R_G^{\Lambda p}} \right) + 2 \frac{\Re f^S(k)}{\sqrt{\pi} R_G^{\Lambda p}} F_1(Q R_G^{\Lambda p}) - \frac{\Im f^S(k)}{R_G^{\Lambda p}} F_2(Q R_G^{\Lambda p}) \right]$$

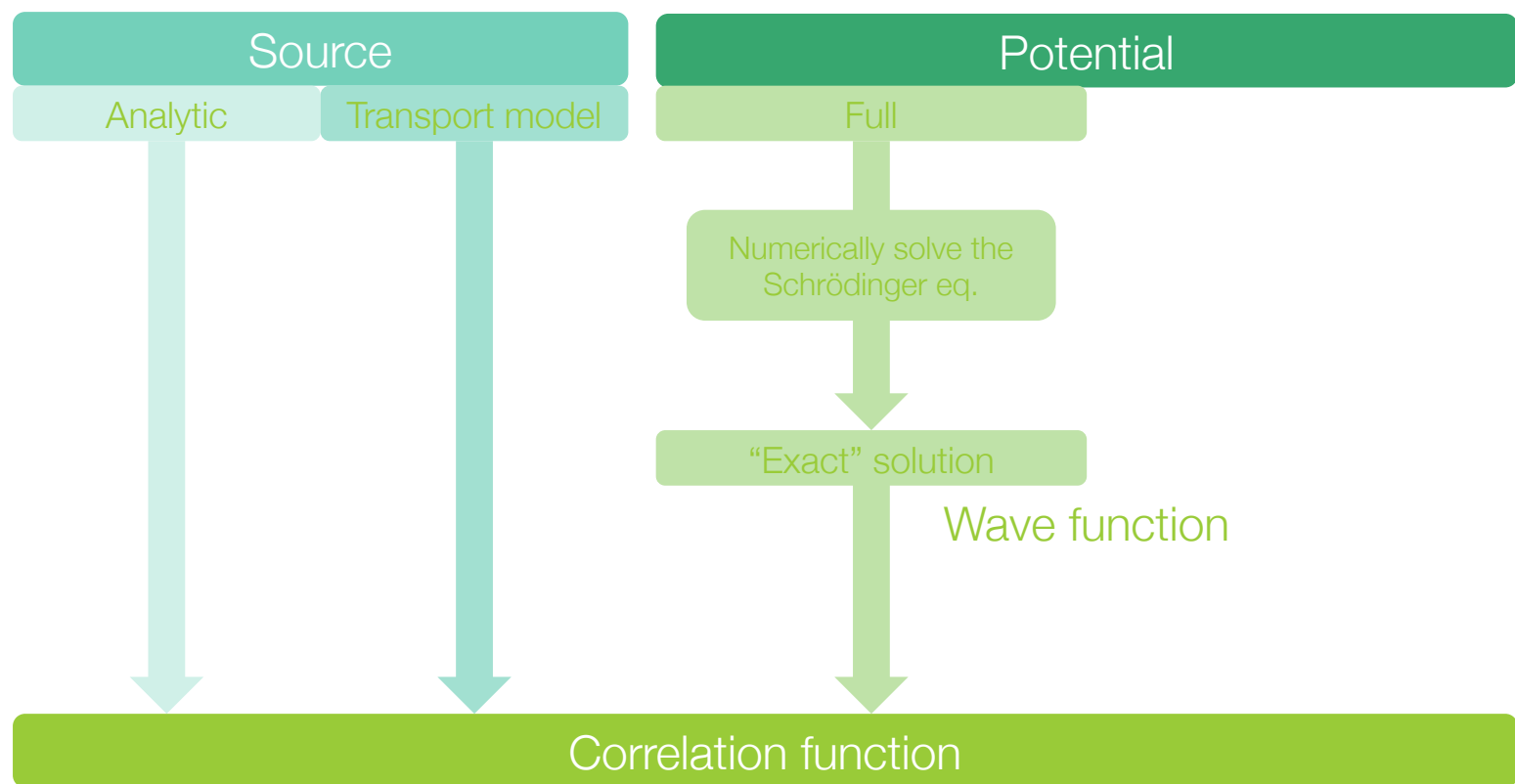
R. Lednicky and V.L. Lyuboshits, Sov. J. Nucl. Phys. 53, 770 (1982)

- Might locally break down for small sources



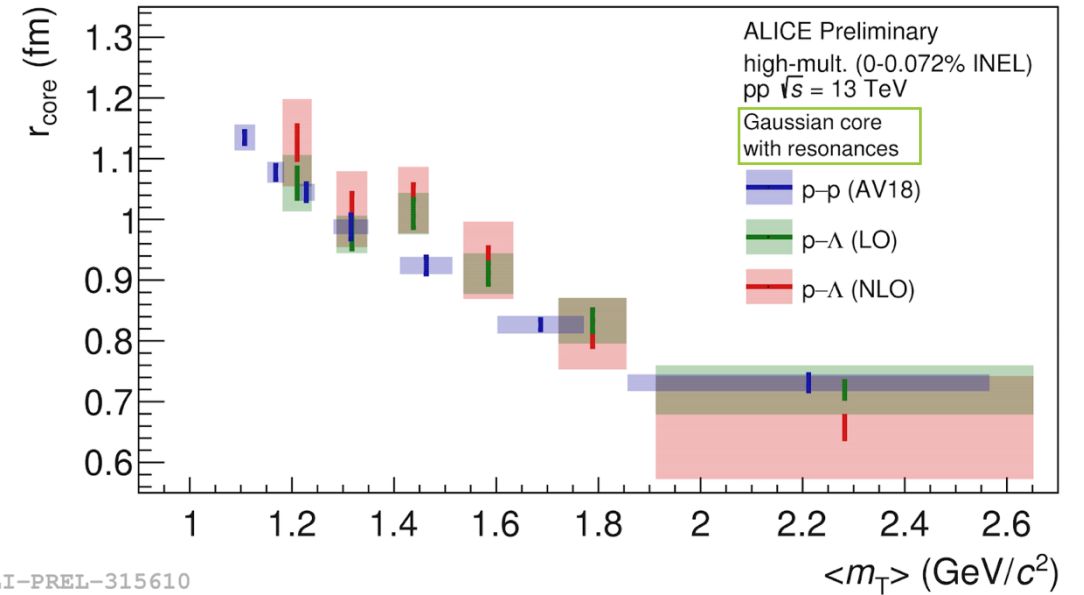
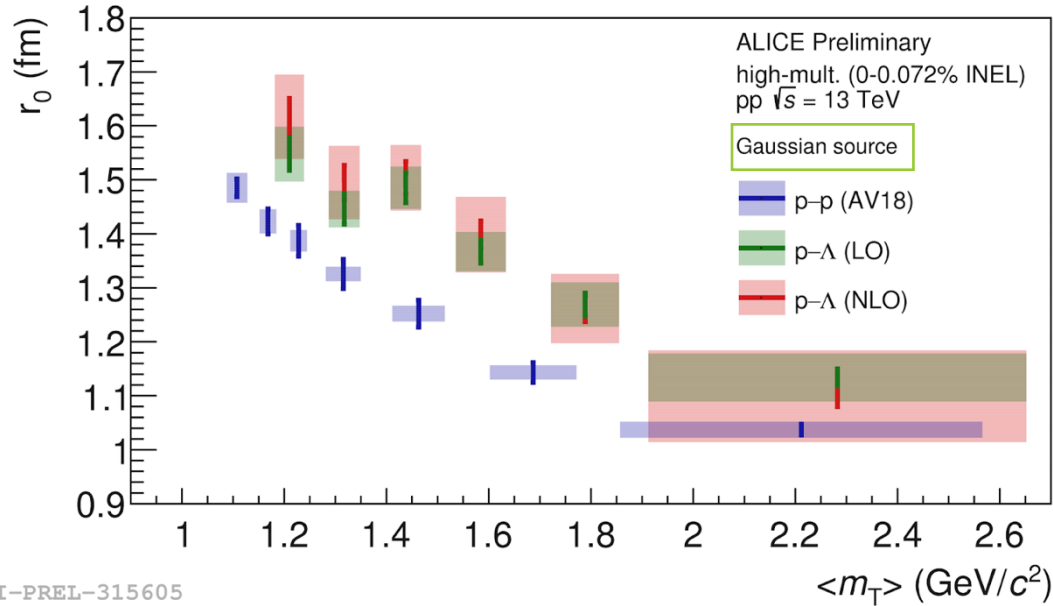
ALICE

CATS



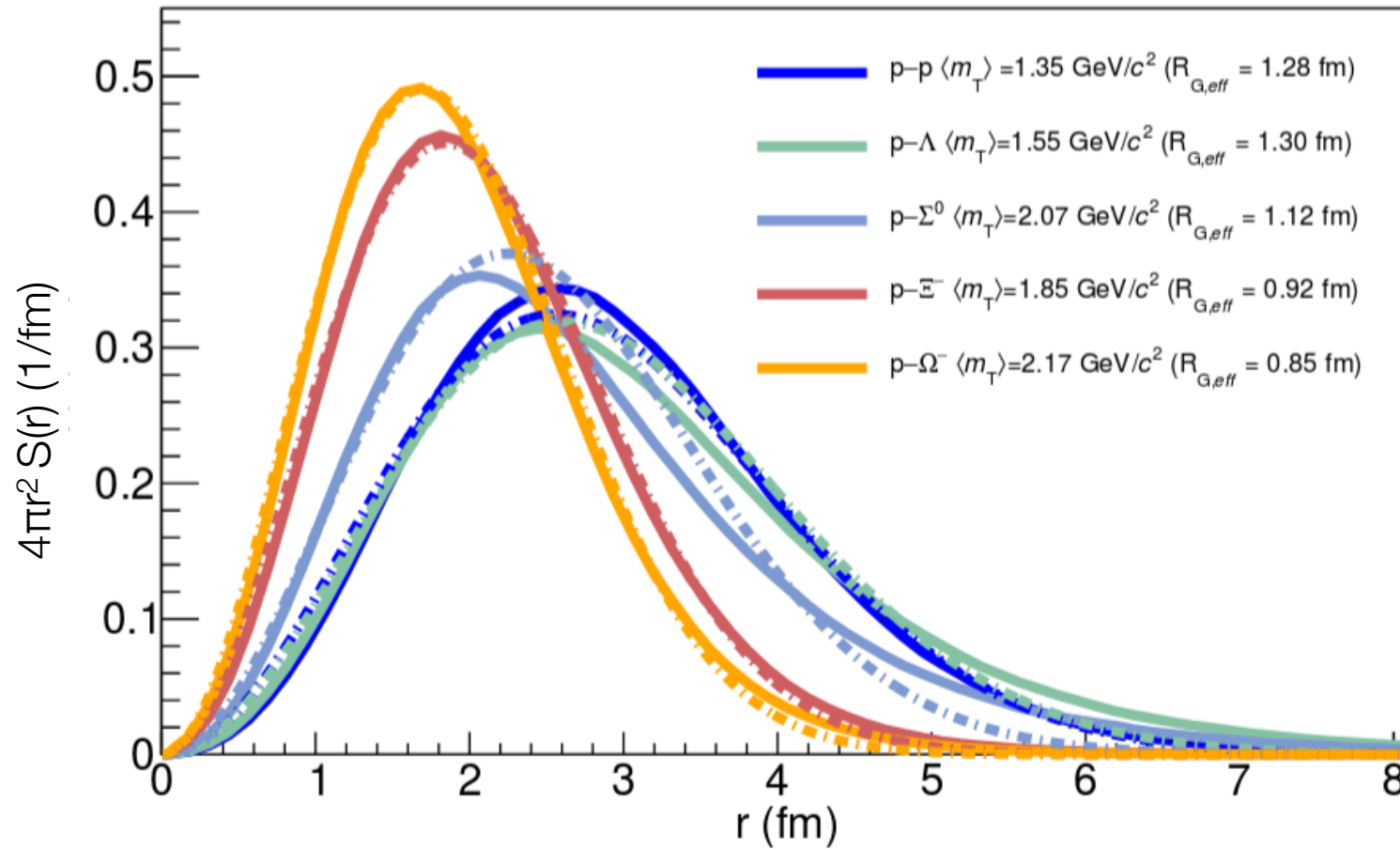
D.L. Mihaylov et al, Eur.Phys.J. C78 (2018) no.5, 394

The source function



- Each $\langle m_T \rangle$ bin fitted independently with the two source models
- The results are compared for p-p and p- Λ correlation
- Our Ansatz: The scaling should be the same.
 - The basic MC model works

Source r_{Core} + resonances





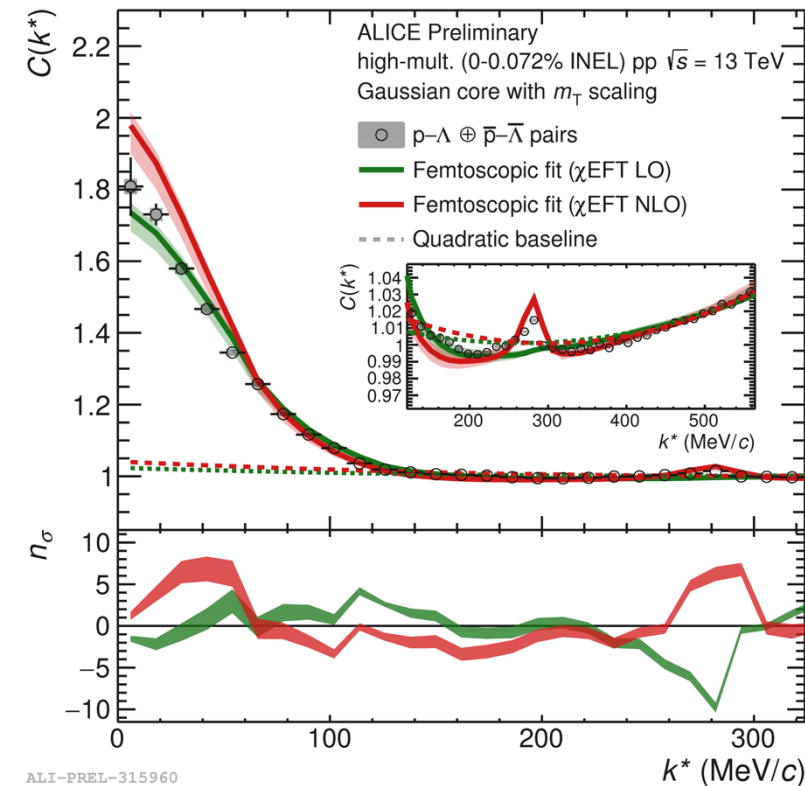
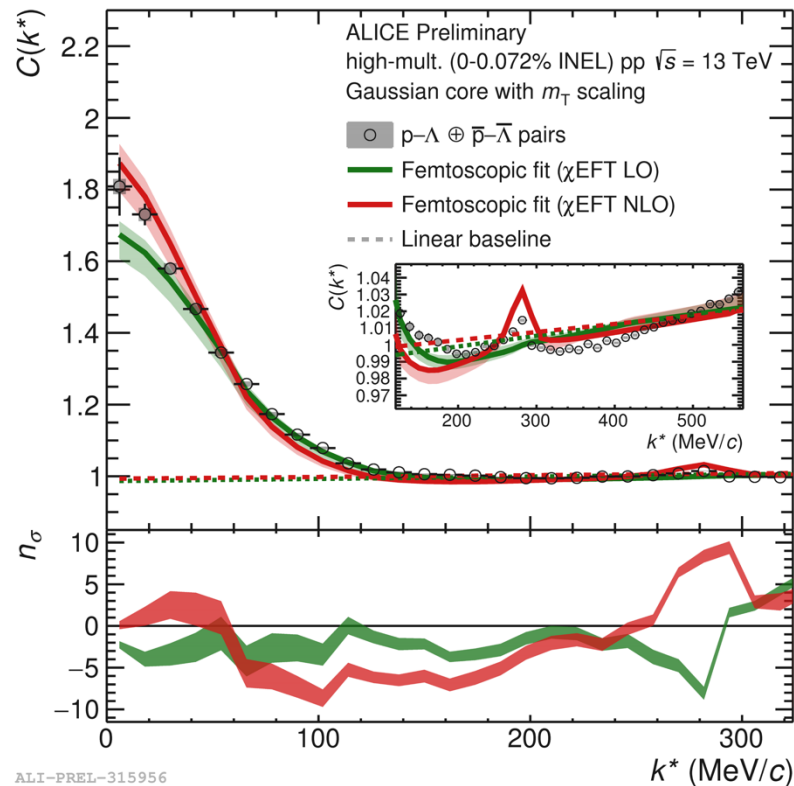
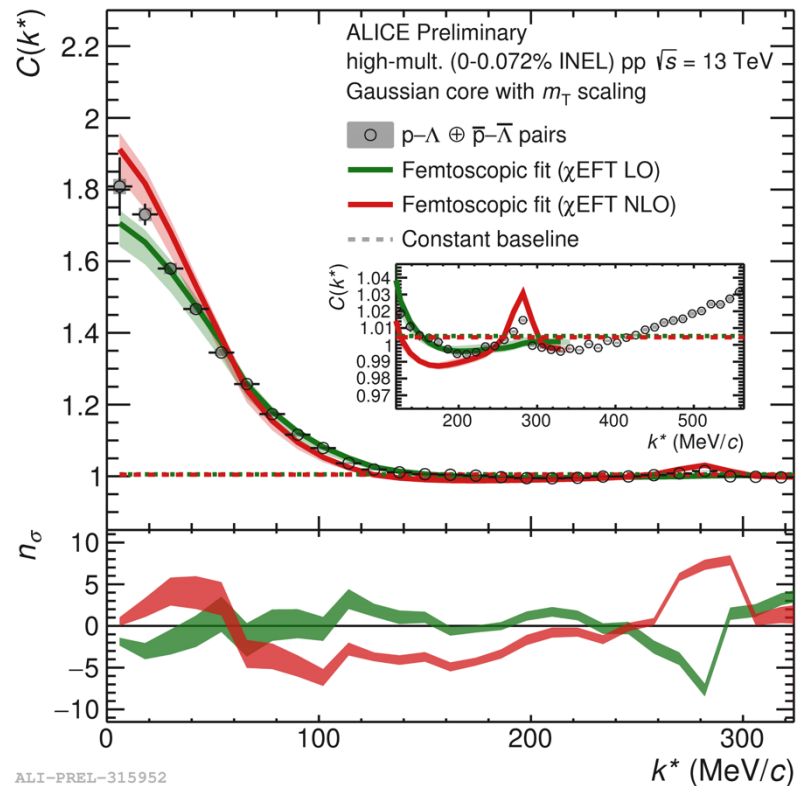
ALICE

p- Λ results in pp 13 TeV (high multiplicity)

Constant baseline

Linear baseline

Quadratic baseline



- Different variations of the baseline: Constant, linear & quadratic
 - Best fit for LO: $n_\sigma > 8$
 - Best fit for NLO: $n_\sigma > 10$

Measurement of the p - Ξ^- interaction

- Identification via $\Xi^- \rightarrow \Lambda \pi^-$
- Treatment of residual correlations
 - Misidentification of Ξ^-
 - Ξ^- Purity ~ 92 %
 $\rightarrow \lambda_{p-\Xi^-}$ pair contribution ~ 8.5 %
 - $C_{p-\Xi^-}(k^*)$ from the **sidebands** of the Ξ^- selection
 - p - $\Xi^-(1530)$
 $\rightarrow \lambda_{p-\Xi^-(1530)}$ pair contribution ~ 8.2 %

