

# Search for a stable six-quark state in $\Upsilon$ decays at *BABAR*



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# Outline

- Introduction and motivations
  - Multi-quark configurations
  - Six-quark configurations and lattice QCD expectations
  - Dark matter candidates and implications
- Analysis approach in *BABAR*
  - Pre-selections
  - Efficiencies and systematic uncertainties
- Results
  - Signal region and sidebands
  - Upper limits
- Conclusions

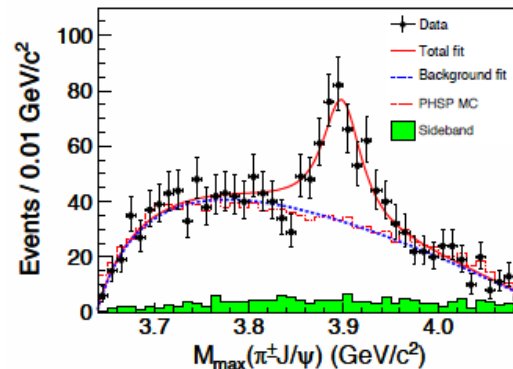


# Multiquark configurations

- Multiquark states allowed by QCD
- Recent observations of many-quark systems :

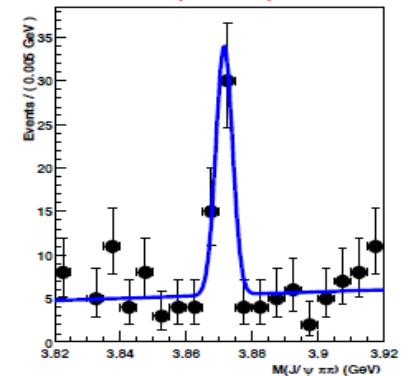
## – Tetraquarks

- Belle:
  - $X(3872)$ ,  $J^{PC} = 1^{++}$ , observed in  $B \rightarrow K \pi^+ \pi^- J/\psi$
  - $Z_c(4430)^+$
- BESIII:  $Z_c(3900)^\pm$ , observed in  $\pi^\pm J/\psi$



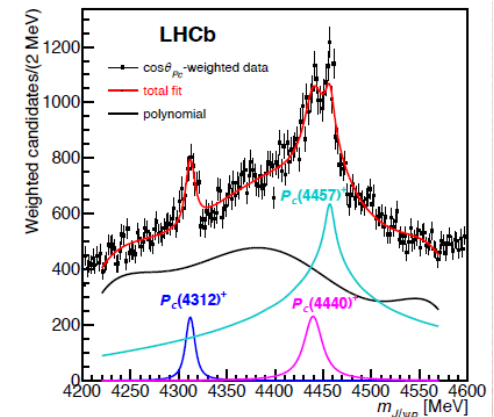
BESIII Coll., PRL110, 252100 (2013)

Belle Coll., PRL91, 262001 (2003)



## – Pentaquarks:

- LHCb:  $P_c(4312)$ ,  $P_c(4440)$ ,  $P_c(4457)$ , observed in  $J/\psi p$



LHCb Coll., PRL122, 072002 (2019)

## – What about 6-quark states?

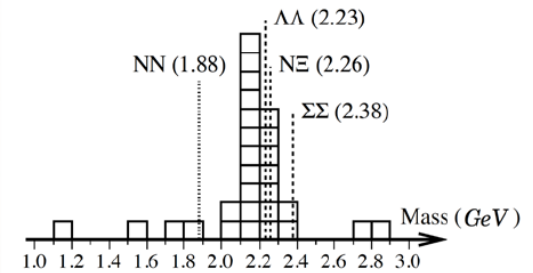


# Six-quark states

- First proposed by R. Jaffe in 1977:

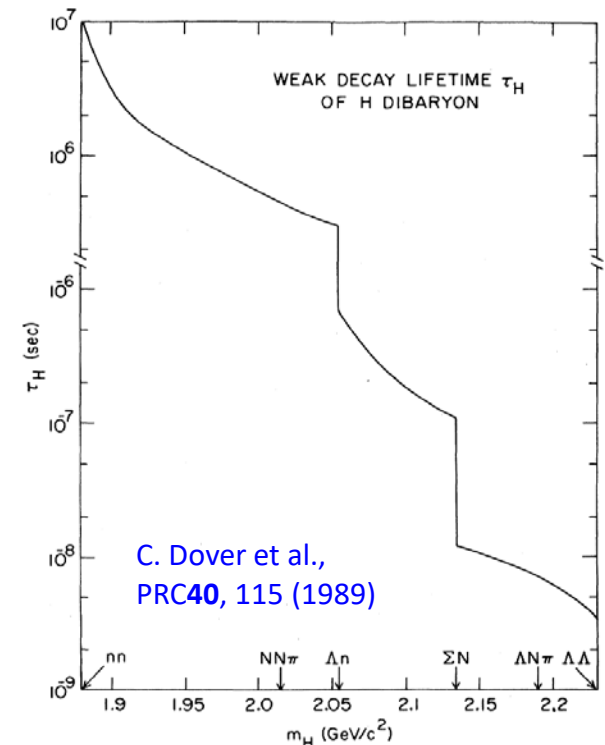
## H dibaryon

- Flavor singlet state  $|udsuds\rangle$
- Loosely bound  $\Lambda\Lambda$  state**
- Bag model prediction:  $m_H \sim 2150 \text{ MeV}$
- Decay modes: if  $m_H < 2m_\Lambda$  (2230 MeV)
  - Strong decay forbidden
  - Weak decay allowed, lifetime  $\sim 10^{-10} \text{ s}$**
  - Wide expected range depending on the binding energy:
    - $B.E. \sim 180 \text{ MeV}$ : days/months
    - $B.E. > 350 \text{ MeV}$ : stable object
- Many searches over the years in several channels, all unsuccessful
  - Main channel: one-nucleon absorption of kaons on deuterons +  $\Xi$  absorption
  - Double  $\Lambda$  hypernuclei observations set limits to mass/B.E. ( ${}_{\Lambda\Lambda}^6\text{He}$ )

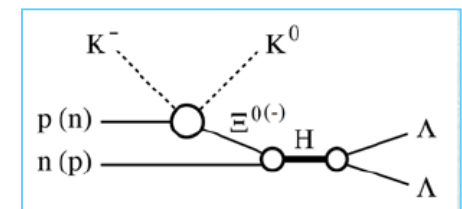


R. Jaffe et al., PRL**38**, 195 (1977)

S. Bashinsky et al., NPA**625**, 167 (1997)



C. Dover et al.,  
PRC**40**, 115 (1989)



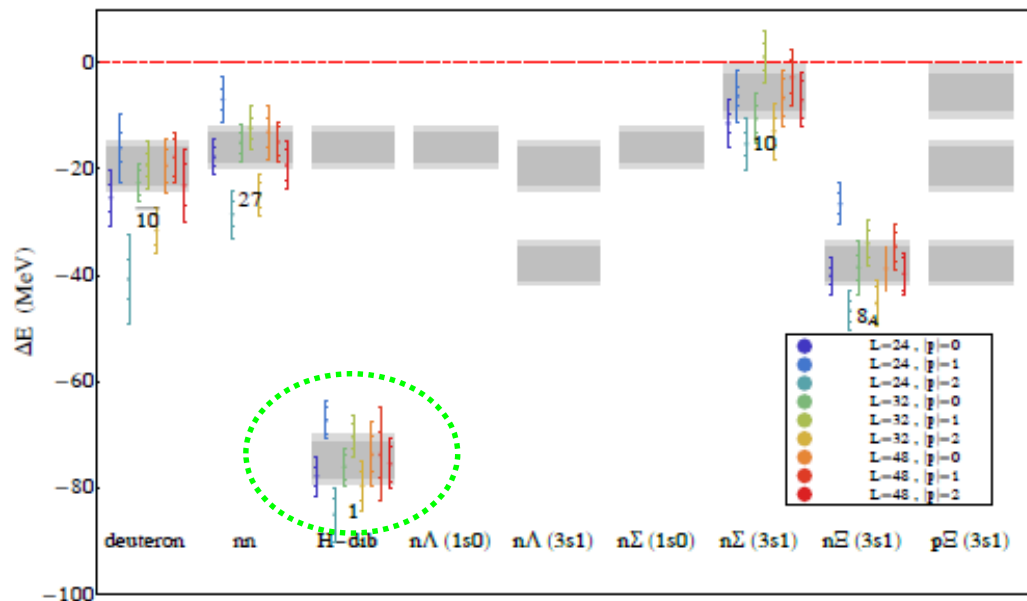


# A light H dibaryon: the $S$ six-quark state

- Proposed by G. Farrar in 2017 as possible Dark Matter candidate  
(arXiv: 1708.08951)
- Tightly bound** six-quark combination, doubly strange
  - $S \sim |uuddss\rangle$ ,  $Q = 0$ ,  $B = 2$ ,  $S = -2$
  - Completely symmetric spatial wave function
  - Flavor singlet: very small coupling to  $\gamma$ ,  $\pi$ ,  $\rho$ , ...
  - Very compact object:  $r \sim 0.1\text{-}0.4\text{ fm}$  ( $< r_N/4$ )**
  - Large binding energy, smaller mass:  $m_S < 2.05\text{ GeV}$** 
    - new stable hadron,  $\Lambda\Lambda$  bound state
    - If  $m_S < m_\Lambda + m_p + m_e = 2.05\text{ GeV}$ : only doubly-weak decays allowed, cosmologically stable
    - Lower bound on mass can be fixed by non-observation of  $nn \rightarrow S\pi^0$  in nuclei:
      - $m_S \geq 2m_n - m_\pi \sim 1.7\text{ GeV}$
- SN interaction suppressed by tiny wavefunction overlap ( $\sigma \sim 10^{-30}\text{ cm}^2$ )
  - It does not bind to nuclei (no exotic isotopes)
- Not excluded so far by experiments



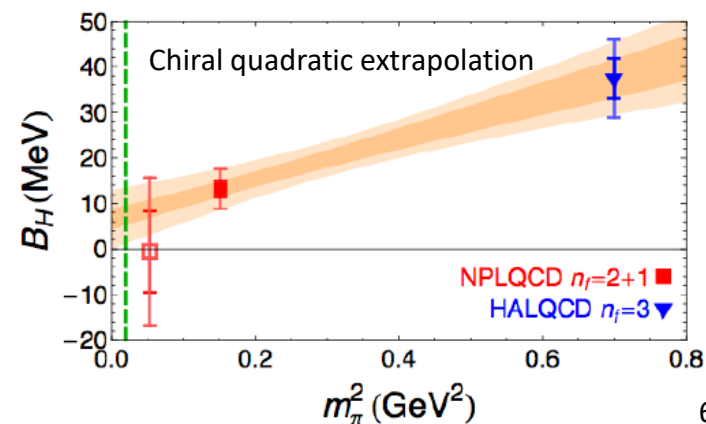
# Dibaryons on the lattice



NPLQCD Coll.,  
S. Beane et al., PRD**87**, 034506 (2013)

- LQCD calculations in the limit of SU(3) flavor symmetry, with  $m_\pi = m_K \approx 800$  MeV
  - Pion mass still (too) unphysical
  - Quarks are non-relativistic at this mass scale (not realistic)
  - Several bound baryon-baryon systems foreseen
  - **Most tightly bound: singlet state**
    - H: B.E.  $\sim 90$  MeV
  - Lower binding energies expected in earlier calculations, with lower  $m_\pi$  mass

HALQCD, Prog. Theor. Phys. **124**, 591 (2010)  
NPLQCD, PRL**106**, 162001 (2011)



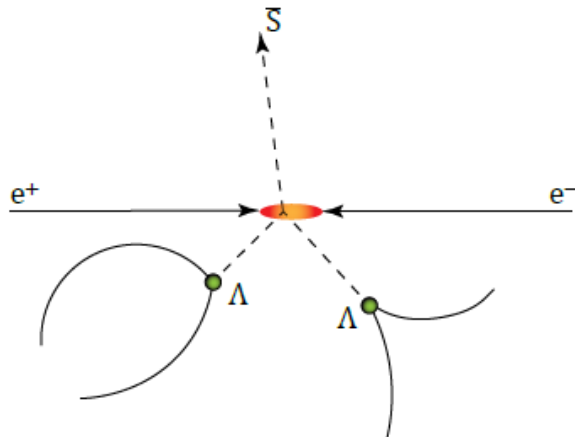
# Hexa-quarks as Dark Matter candidates

- Hypothesis (G. Farrar, [arXiv:1805.03723](#)): **DM formed by an equal amount of  $u$ ,  $d$ ,  $s$  quarks**
  - Formation rate driven by QGP transition to the hadronic phase
  - DM models include hexa-quarks/quark nuggets/many-quark aggregates
    - negligible coupling to photons
- Hexa-quarks with mass 1860-1880 MeV can reproduce the ratio of densities within 15%:  $\Omega_{DM}/\Omega_B \sim 5$ 
  - The total baryon asymmetry in the Universe, including Dark Matter, would be close to the observed value: asymmetric DM models
- Not excluded by current direct searches yet
- Ongoing discussion about the validity of this hypothesis ([Kolb & Turner, PRD99, 063519 \(2019\)](#))
  - Hexa-quarks better candidates as relics, rather than DM constituents



# Search for $S$

- Viable search channels:
  - Fixed target experiments with intense beams (small rates expected)
    - $K^- p \rightarrow \bar{\Lambda} S$
  - $S$  production in hadronic collisions:  $\bar{S}$  annihilation along the beampipe/detector, detection of decay products  $B = -1$ ,  $S = +2$ 
    - $\bar{S} N \rightarrow \Xi^{+,0} X$ ,  $\bar{S} N \rightarrow \bar{\Lambda} K^{+,0} X$
    - $\bar{S} n \rightarrow \bar{\Lambda} K^0_s$ ,  $\bar{S} p \rightarrow \bar{\Lambda} K^+$
  - $\Upsilon$  decays below open-bottom threshold:
    - $\Upsilon(2S, 3S) \rightarrow \text{gluons} \rightarrow S \bar{\Lambda} \bar{\Lambda} + \text{pions} / \gamma$  (+ c.c.)
      - High  $\Lambda$  reconstruction efficiency ( $c\tau \sim 8$  cm)
    - Other discovery avenues:  $\Xi^- p$ , or  $\Lambda$  replaced by  $K^- p$
    - Short distance nature of the gluonic force
    - Expected inclusive branching fractions (based on statistical models):  $\mathbf{O(10^{-7})}$



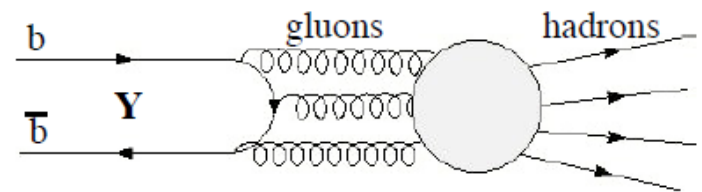
Missing-mass analysis for exclusive decays:  $S$  recoils against a  $\bar{\Lambda} \bar{\Lambda}$  ( $\Lambda \Lambda$ ) system in the  $\Upsilon$  center of mass

$$m_{rec}^2 = (p_Y - p_{\bar{\Lambda}} - p_{\bar{\Lambda}})^2$$



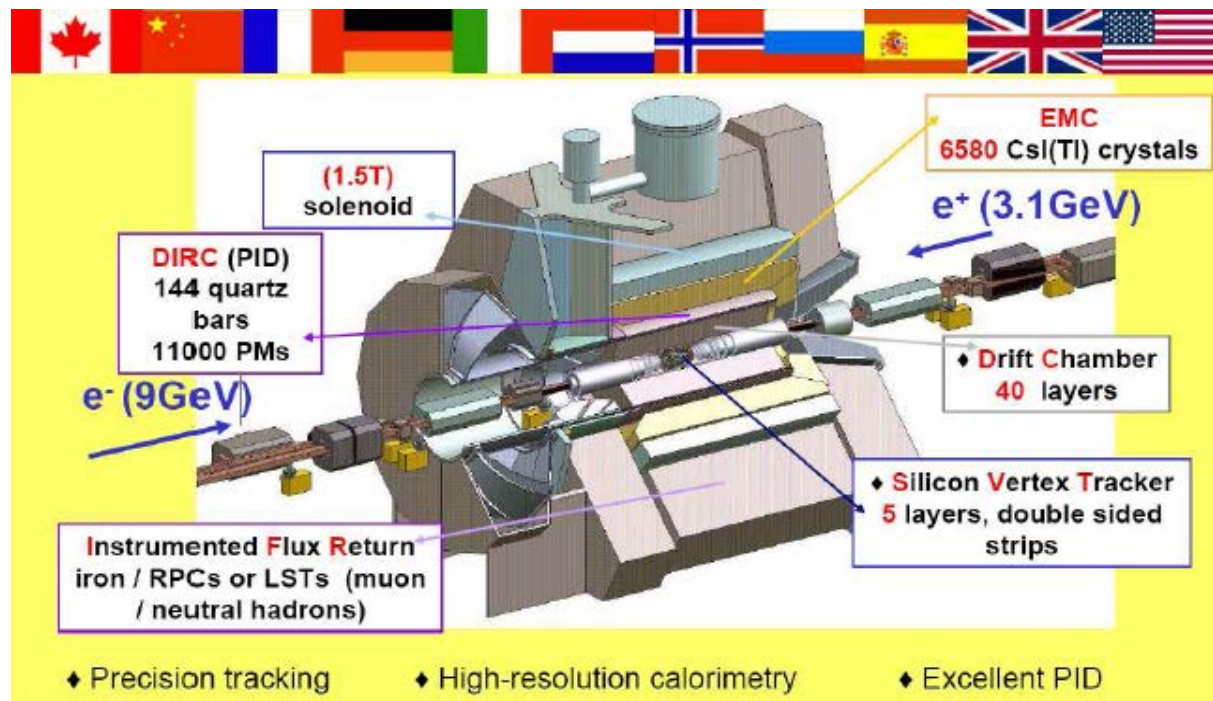
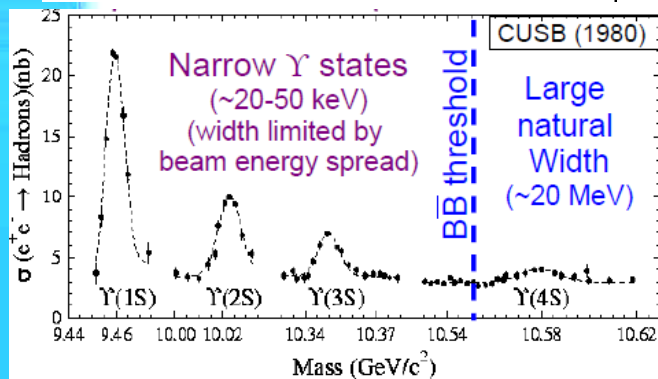
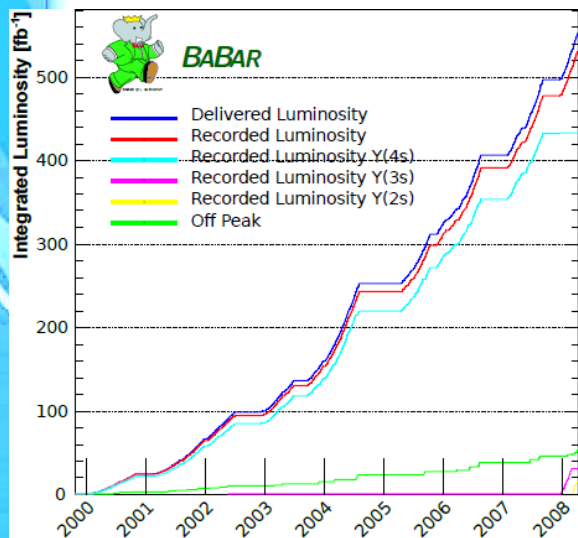


- Annihilation to gluons happens at a scale  $R \sim 1/m_b \sim 0.04$  fm
- Initial gluon density: 40 TeV/fm<sup>3</sup>





# The *BABAR* experiment at PEP-II, SLAC



NIM A479, 1 (2002); NIM A729, 615 (2013)

PEP-II and *BABAR* operated from Oct 1999 to Apr 2008

$\sim 460 \text{ fb}^{-1}$   
integrated  
luminosity

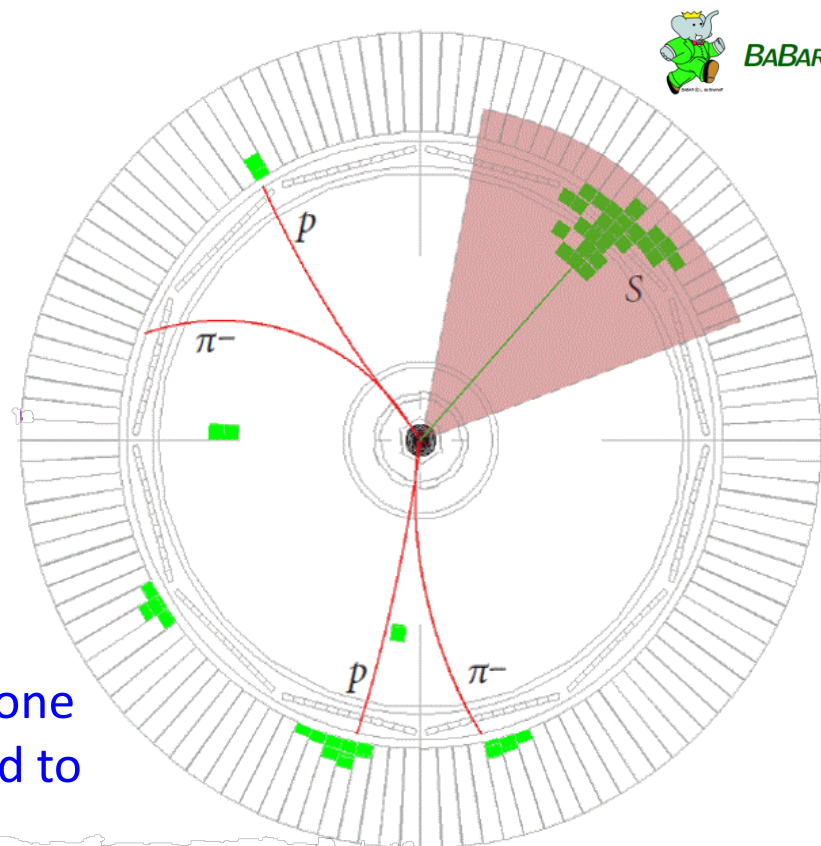
$\sim 470 \times 10^6 \Upsilon(4S)$   
 $\sim 120 \times 10^6 \Upsilon(3S)$  (10x BELLE)  
 $\sim 100 \times 10^6 \Upsilon(2S)$  (10x CLEO)  
 $\sim 18 \times 10^6 \Upsilon(1S)$  from  $\Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$

For this analysis: 90M  $\Upsilon(2S)$  + 110M  $\Upsilon(3S)$



# Search for $\Upsilon(2S, 3S) \rightarrow S\bar{\Lambda}\bar{\Lambda}$ (+ c.c.) in BABAR

- Full reconstruction of 2x $\bar{\Lambda}$  ( $2\Lambda$ ) decays:  $\bar{\Lambda} \rightarrow \bar{p}\pi^+$
- Target: zero background in the signal region
- Selection criteria:
  - Four charged tracks + at most one additional track not from IP
  - Loose PID criteria to select  $\bar{p}$
  - Selection of events with  $2\Lambda$  or  $2\bar{\Lambda}$ 
    - flight significance for each  $\Lambda$ :
$$|\vec{r}_\Lambda| / \sigma_r > 5$$
    - $\Lambda$  pointing back to IP:
$$\cos(\vec{r}_\Lambda, \vec{p}_\Lambda) > 0.9$$
  - Minimal contribution from out of cone events + hits on ECAL not connected to tracks:  $E_{extra} < 0.5$  GeV
  - Blind analysis (MC tuning)

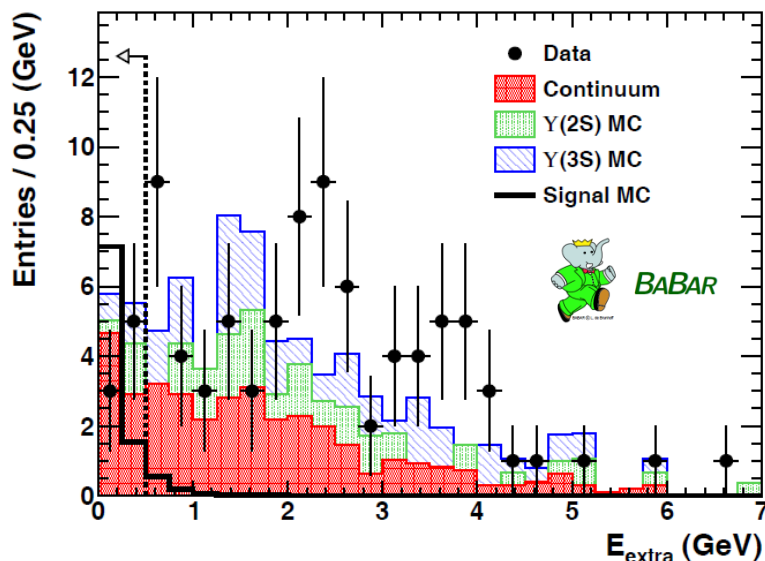




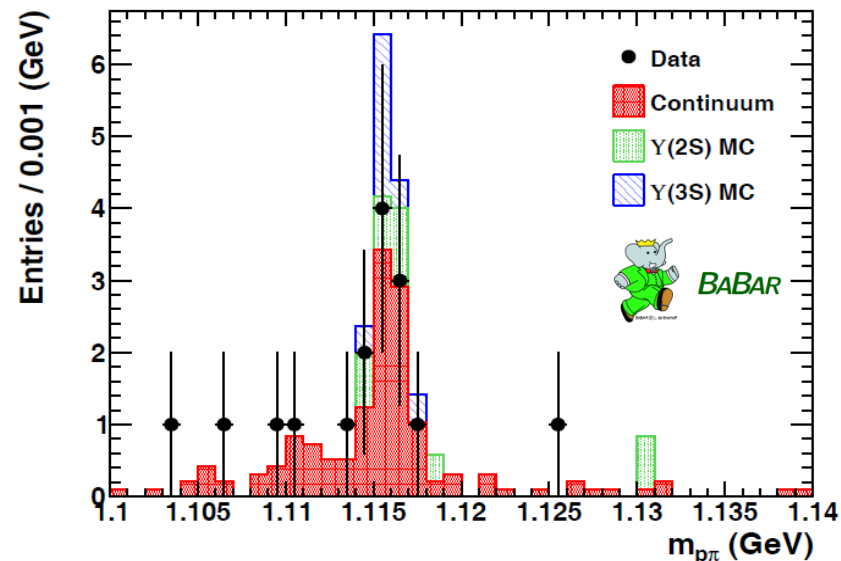
# Event preselection

- $2\Lambda$  candidates, 5 tracks/event at most: **92 events**
- $E_{extra}$  distribution of ECAL hits
  - Signal:  $E_{extra} < 500$  MeV: **8 events** (2 entries/event)
    - True signal in  $(p\pi)$  invariant mass
- Backgrounds: dominated by hadronic events with several strange baryons (typically  $2\Lambda$ ) and additional charged and neutral particles escaping detection

BABAR Coll., PRL122, 072002 (2019)



BABAR Coll., PRL122, 072002 (2019)



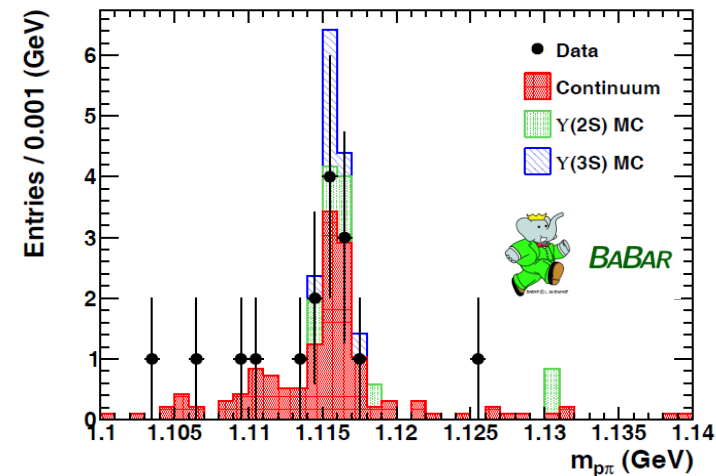
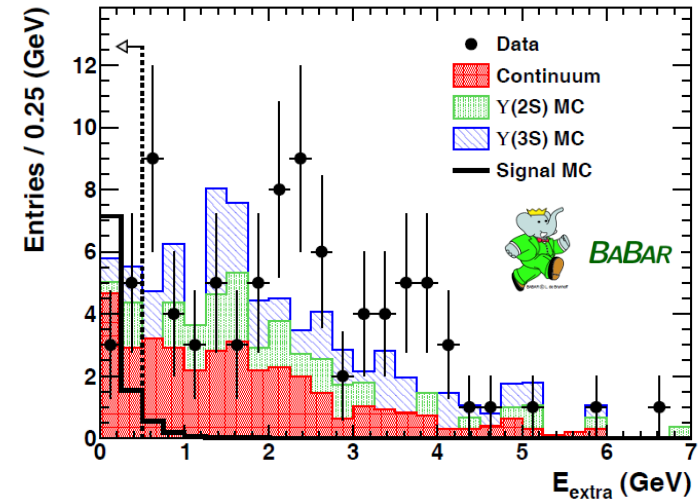
- Last step: kinematic fit imposing mass constraint to each  $\Lambda$  candidate, requiring common origin from beamspot ( $\chi^2 < 25$ ): **4 events**





# Background studies

- MC generation of  $\Upsilon(2S, 3S)$  decays with EVTGEN generator
- Continuum  $e^+e^- \rightarrow q\bar{q}$  from  $\Upsilon(4S)$  data ( $q = u, d, s, c$ )
- Background sample normalization chosen to match the sideband  $E_{extra} > 500$  MeV distribution
- Remaining background (may filter through the  $E_{extra}$  selection):
  - $e^+e^- \rightarrow \Lambda\Lambda\bar{\Lambda}\bar{\Lambda} (X)$  with the two  $\Lambda$ 's decaying in the neutral channel  $\Lambda \rightarrow n\pi^0$





# Efficiencies evaluation

- Necessary for the determination of branching fractions
- The efficiencies have been obtained by simulations of the signal MC based on:
  - different models for decay amplitudes
    1. G. Farrar: effective Lagrangian with constant matrix elements combined in different arrangements according to the relative angular momentum
    2. phase-space flat decays
  - Different interaction patterns of  $S$  with the detector materials
    1. As a neutron
    2. Non interacting (as a neutrino)
- Differences used as systematic uncertainties
- The efficiency is mainly determined by the geometrical acceptance
  - 7.2% at threshold, 8.2% @ 2 GeV
- *Mass resolution* (on recoiling mass) in *BABAR*:  $\sim 100$  MeV



# Systematic uncertainties

- Main sources:
  - MC signal modelling
    - Production amplitude  $\Rightarrow$  different angular distributions
    - $S$  interactions in the detector (neutron? neutrino?)
  - Data/MC differences in the reconstruction, PID

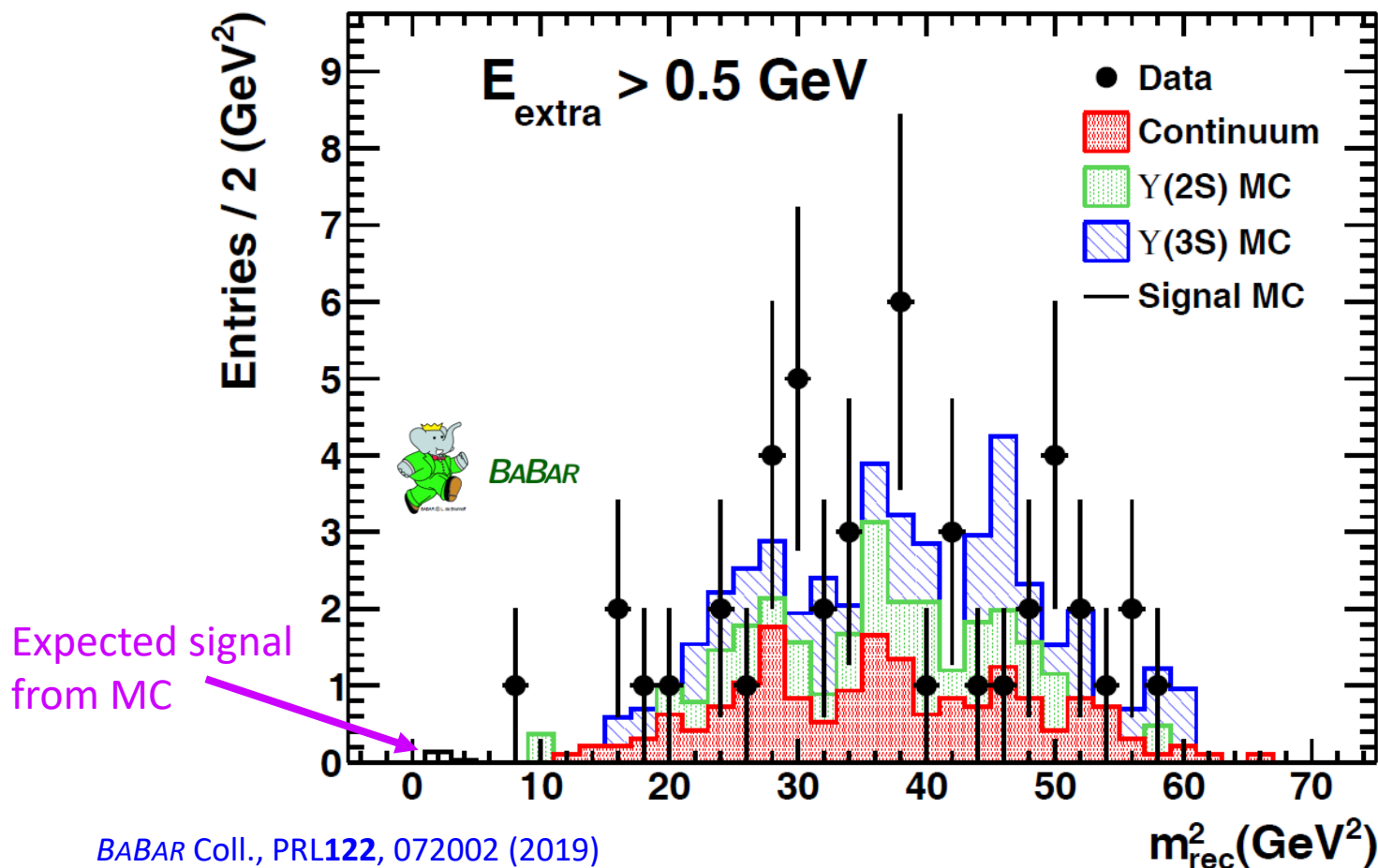
Source	Systematic error
$S$ angular distribution modelling	(4-15)%
$S$ interactions modelling	(8-10)%
$\Lambda$ reconstruction	4%/ $\Lambda$
proton/antiproton PID	1%/ $p$
MC sample size	1.5%
$\Lambda$ branching fraction	1.6%
$Y(2S, 3S)$ counts	0.6%

Total systematic uncertainty: (12.8-16.1)%



# Validation on sideband: $E_{extra} > 0.5$ GeV

- Study of  $m_{rec}^2$  distribution for events in the sideband (combined  $\Upsilon(2S)$  and  $\Upsilon(3S)$  datasets)
  - Zero background event in the **expected signal region (0 - 5 GeV<sup>2</sup>)**
    - Signal region expected to be background free



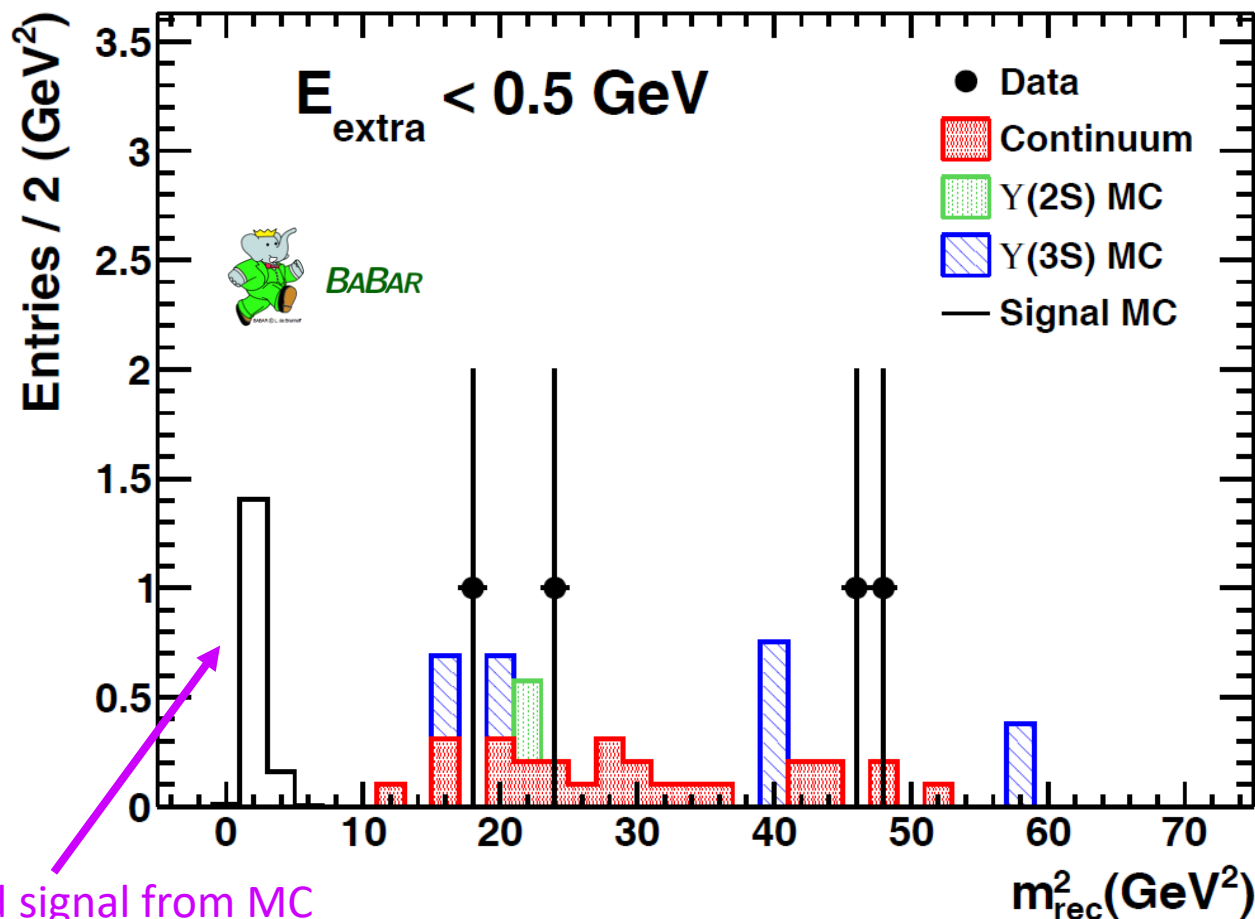




# Signal region: $E_{extra} < 500 \text{ MeV}$

- No event observed in the expected signal region
- MC signal simulated in the hypotheses:
  - $m_S = 1.6 \text{ GeV}$
  - $B(Y(nS) \rightarrow S \bar{A} \bar{A}) = 10^{-7}$

BABAR Coll., PRL122, 072002 (2019)

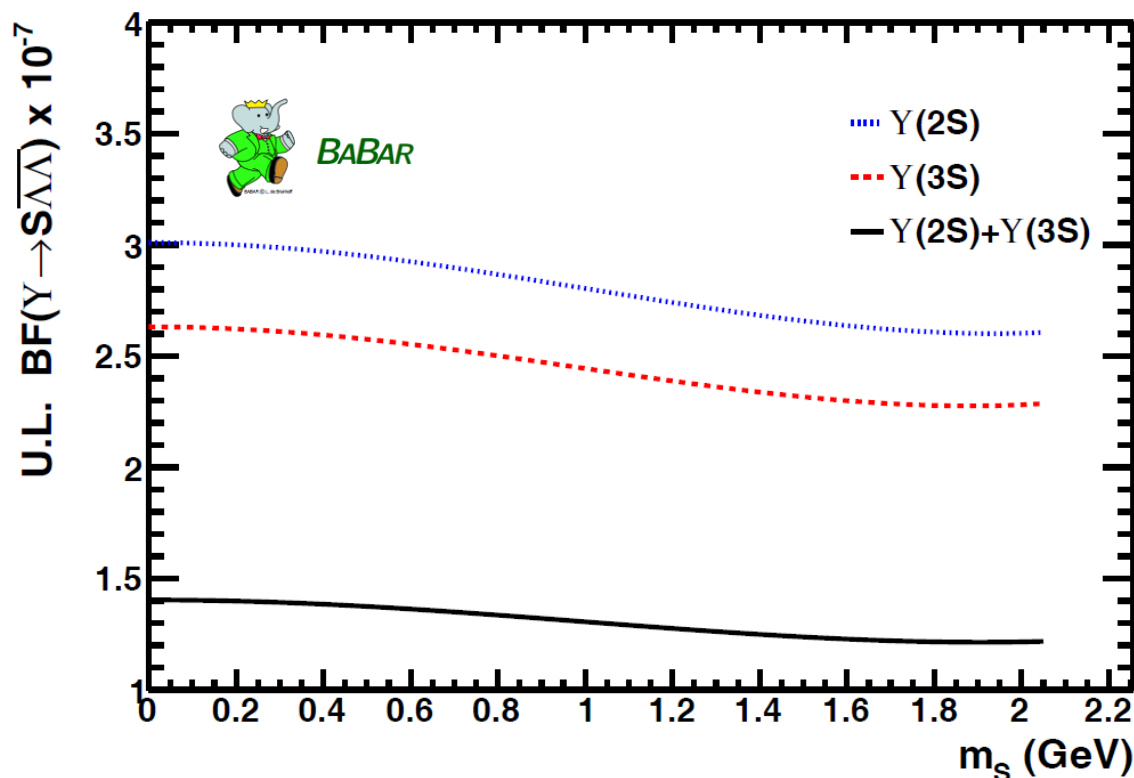




# Upper limits: $B(\Upsilon(nS) \rightarrow S \bar{\Lambda} \bar{\Lambda})$

- Scan on  $S$  masses in the (0 - 2.05) GeV range in 50 MeV steps
- No signal event observed
- Set upper limit at 90% C.L. using profile likelihood method (single event sensitivity: one event, zero bck) including systematic uncertainties

BABAR Coll., PRL**122**, 072002 (2019)



$$B(\Upsilon(nS) \rightarrow S \bar{\Lambda} \bar{\Lambda}) < (1.2 - 1.4) \times 10^{-7} @ 90\% \text{ C.L.}$$



# Conclusions

- Some interest recently revived in the search for stable six-quark states as possible baryonic Dark Matter candidates
- 200 millions  $\Upsilon(2S,3S)$  decay events analysed by *BABAR* to search for signatures of  $S = |uuddss\rangle$  six-quark state recoiling against  $\bar{\Lambda}\bar{\Lambda}(\Lambda\Lambda)$  pairs
- No signal found, no background
- Stringent limit set, at 90% C.L.:
  - **$\mathcal{B}(\Upsilon(2S, 3S) \rightarrow S\bar{\Lambda}\bar{\Lambda}) < (1.2 - 1.4) \times 10^{-7}$**  *BABAR Coll., PRL122, 072002 (2019)*
- This limits add up to a former measurement by Belle for  $S$  production in  $\Upsilon(1S,2S)$  decays, with  $S$  recoiling against  $\Lambda p \pi^-$  or  $\Lambda\Lambda$  :  $(0.8 - 33) \times 10^{-7}$  *Belle Coll., PRL110, 222002 (2013)*
- The exclusive branching fraction could be too small than *BABAR*'s sensitivity
  - Need to look for semi-inclusive decays:  $\Upsilon(nS) \rightarrow S\bar{\Lambda}\bar{\Lambda}X$
  - Analysis ongoing, but probably the available *BABAR* statistics won't be enough





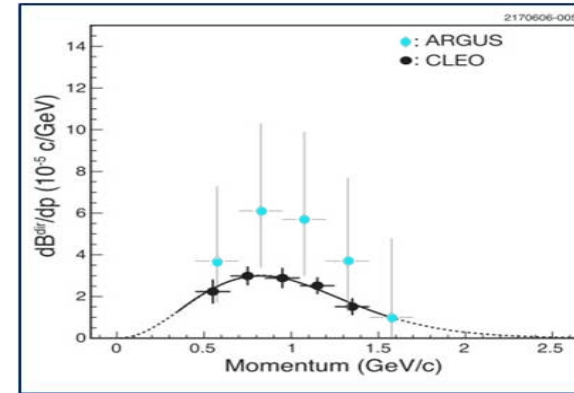
**Backup slides**



# (Anti-)deuteron formation models: fireball and coalescence

- **Fireball spectrum** for C.M.  $d$  ( $\bar{d}$ ) energy: thermal production

$$P(E) = \alpha v^2(E) \exp(-\beta E) = \\ = \alpha \frac{E^2 - m_d^2}{E^2} \exp(-\beta E)$$



maxwellian  
temperature  
 $\beta = 160 \text{ MeV}$   
(CLEO)

PLB98 (1981) 153 - PR131 (1986), 223

- **Coalescence**: production of the bound state expected when  $(pn)(\bar{p}\bar{n})$  are emitted nearby in phase-space
  - The **relative  $p^*$  momentum** is  $\sim$  **deuteron binding energy** (or smaller)
  - The  $d$  ( $\bar{d}$ ) production is related to the **square** of the nucleon  $\sigma_{prod}$
  - **Coalescence volume**  $4\pi p_0^3/3$ : related to the spatial size of  $\bar{d}$  wave function and the size of the fragmentation region (CLEO: 130 MeV/c)
  - No correlation between the momenta of nucleons produced in the same fragmentation



# Inclusive antideuteron production in $\Upsilon$ decays at *BABAR*

Process	Rate
$B(\Upsilon(3S) \rightarrow \bar{d}X)$	$(2.33 \pm 0.15^{+0.31}_{-0.28}) \times 10^{-5}$
$B(\Upsilon(2S) \rightarrow \bar{d}X)$	$(2.64 \pm 0.11^{+0.26}_{-0.21}) \times 10^{-5}$
$B(\Upsilon(1S) \rightarrow \bar{d}X)$	$(2.81 \pm 0.49^{+0.20}_{-0.24}) \times 10^{-5}$
$\sigma(e^+e^- \rightarrow \bar{d}X) [\sqrt{s} \approx 10.58 \text{ GeV}]$	$(9.63 \pm 0.41^{+1.17}_{-1.01}) \text{ fb}$
$\frac{\sigma(e^+e^- \rightarrow \bar{d}X)}{\sigma(e^+e^- \rightarrow \text{Hadrons})}$	$(3.01 \pm 0.13^{+0.37}_{-0.31}) \times 10^{-6}$

*BABAR* Coll., PRD89, 111102(R) (2014)

- Agreement with CLEO  $\Upsilon(1,2S)$  results: fits of the  $\bar{d}$  yields to a fireball spectrum
- Results: integral of the fireball spectrum
- Production of  $\bar{d}$  measured from  $q\bar{q}$  continuum @10.58 GeV and  $\Upsilon(1,2,3S)$  decays
  - First measurements from continuum and  $\Upsilon(3S)$
  - Most precise measurement from  $\Upsilon(2S)$
- Orders of magnitude smaller than ordinary branching fractions
- Decreasing *BF* with c.m. energy
- Suppressed production in  $q\bar{q}$  vs gluons
  - Slightly harder spectrum from continuum

