

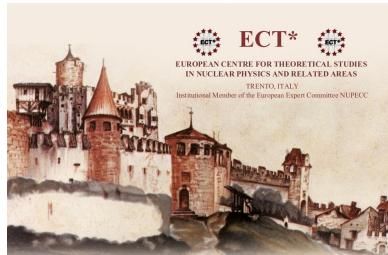
# Investigation of the low-energy $K^-$ hadronic interaction with nucleons by AMADEUS

Raffaele Del Grande<sup>1,2\*</sup>

<sup>1</sup> INFN Laboratori Nazionali di Frascati, Frascati, Italy

<sup>2</sup> CENTRO FERMI - Museo Storico della Fisica e Centro Studi e Ricerche “Enrico Fermi”, Roma, Italy

*On the behalf of the AMADEUS collaboration*



**STRANEX: Recent progress and perspectives in  
STRANGE EXotic atoms studies and related topics**

21-25 October 2019

ECT\*, Trento, Italy

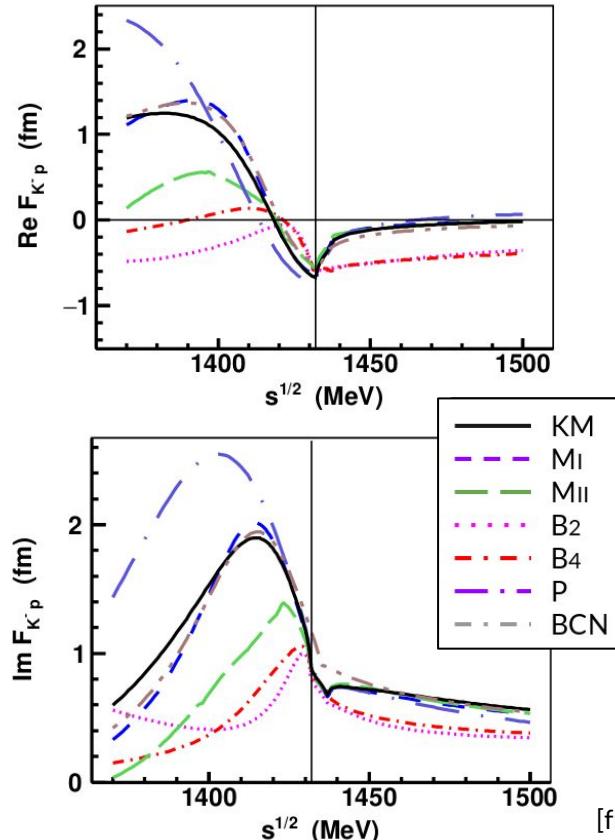
\*raffaele.delgrande@lnf.infn.it

# Motivation

**AMADEUS** (Antikaonic Matter At DAΦNE: an Experiment with Unravelling Spectroscopy )  
investigates **low-energy  $K^-$  absorption in nuclei** with the aim to extract information on:

- $K^-N$  interaction above and below threshold
  - $\Lambda(1405)$  nature
  - kaonic bound states
- $K^-NN$ ,  $K^-NNN$ ,  $K^-NNNN$  (multi-nucleon) interactions
  - essential for the determination of  $K^-$ -nuclei optical potential
- In medium modification of the KbarN interaction
  - partial restoration of chiral symmetry → hadrons mass origin
  - Equation of State of Neutron Stars
  - modification of  $\Lambda(1405)$  and  $\Sigma(1385)$  properties in nuclear medium

# $K^- p$ scattering amplitude



## $K^- p$ scattering amplitude with Chiral models

- Kyoto-Munich (KM)

Y. Ikeda, T. Hyodo, W. Weise, Nucl. Phys. A 881 (2012) 98

- Murcia (MI , MII )

Z. H. Guo, J. A. Oller, Phys. Rev. C 87 (2013) 035202

- Bonn (B2 , B4 )

M. Mai, U.-G. Meißner - Eur. Phys. J. A 51 (2015) 30

- Prague (P)

A. C., J. Smejkal, Nucl. Phys. A 881 (2012) 115

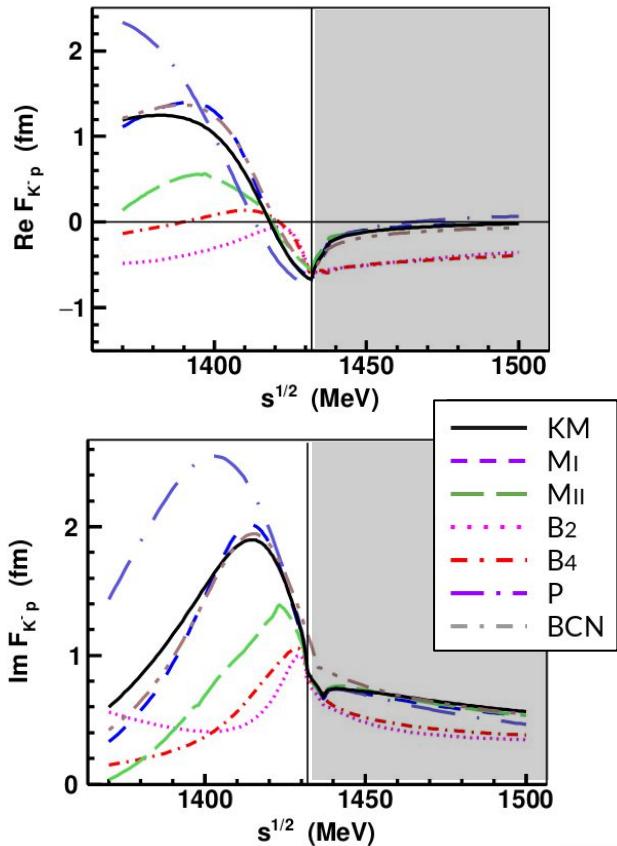
- Barcelona (BCN)

A. Feijoo, V. Magas, À. Ramos, Phys. Rev. C 99 (2019) 035211

**Large discrepancies in the region below threshold!**

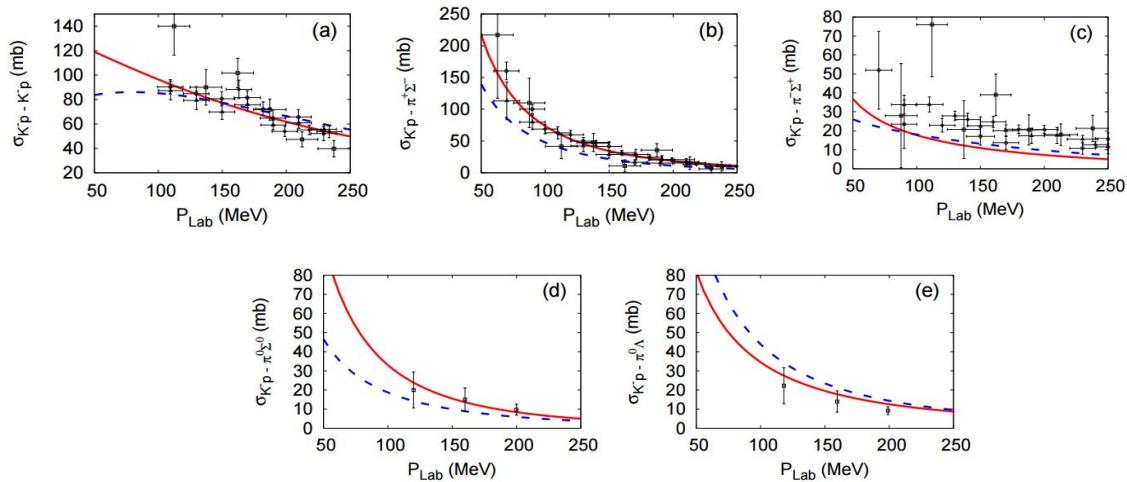
[from A. Cieply talk at MENU2019 conference]

# Experimental constraints above threshold

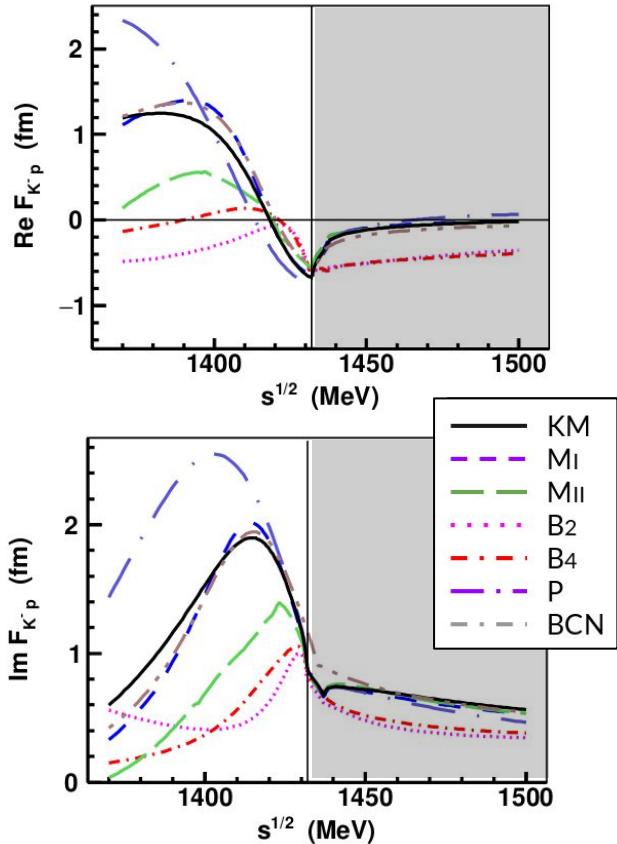


## K-p elastic and inelastic low-energy cross sections

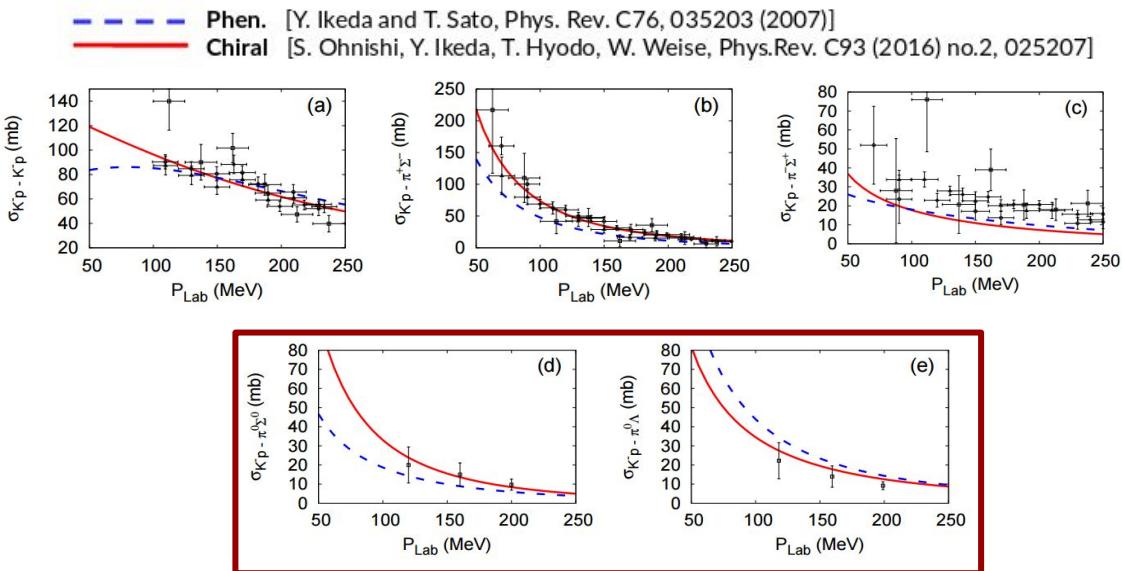
Phen. [Y. Ikeda and T. Sato, Phys. Rev. C76, 035203 (2007)]  
Chiral [S. Ohnishi, Y. Ikeda, T. Hyodo, W. Weise, Phys. Rev. C93 (2016) no.2, 025207]



# Experimental constraints above threshold

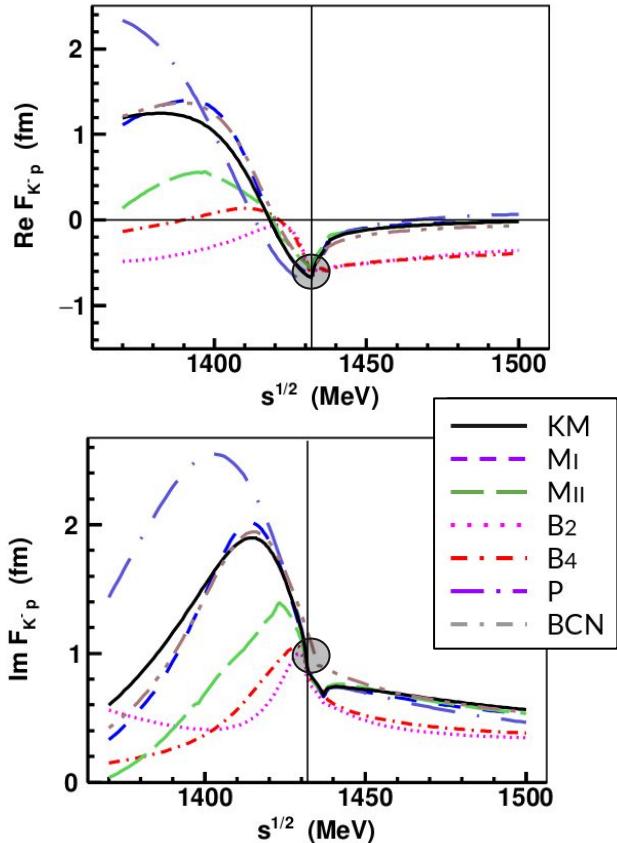


## K-p elastic and inelastic low-energy cross sections

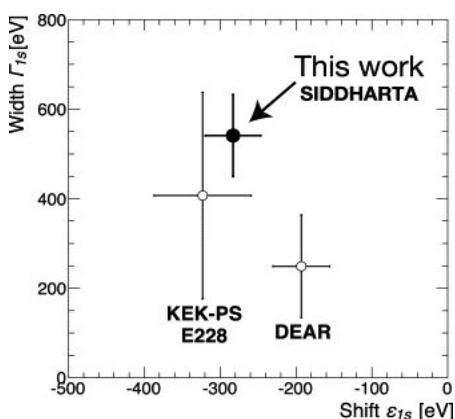


no data for  $p_K < 100 \text{ MeV}/c$

# Experimental constraints at threshold



Precise SIDDHARTA measurement of kaonic hydrogen 1s level shift and width

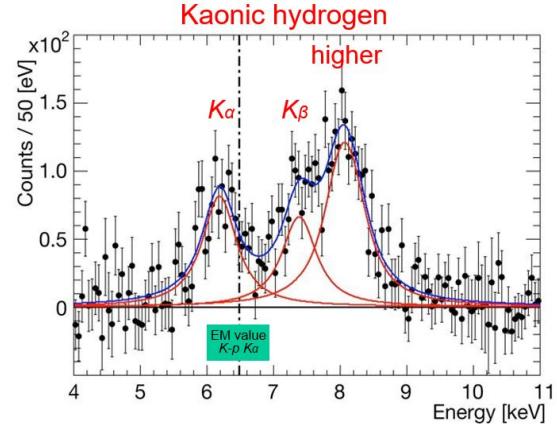


M. Bazzi et al. 2011. (SIDDHARTA Coll.), Phys. Lett. B704, 113

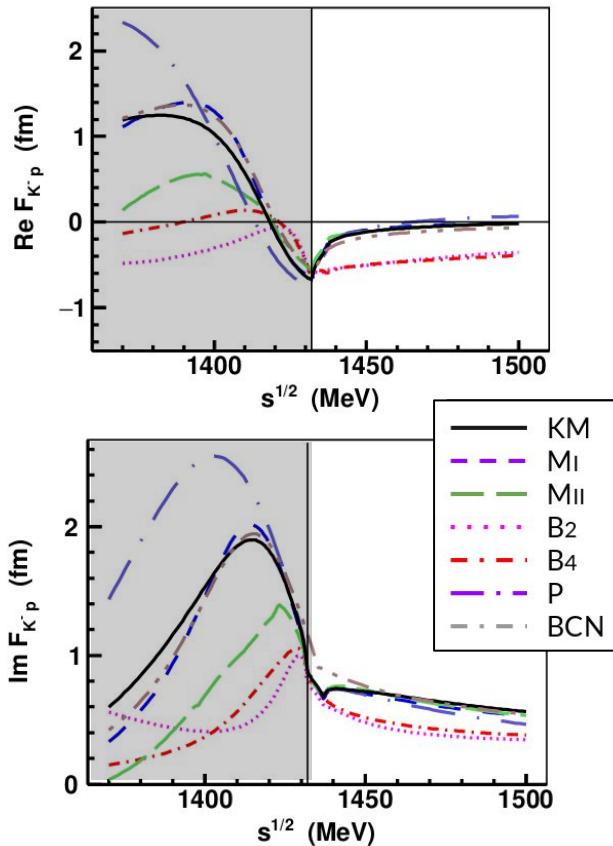
$$\Delta E_N(1s) = 283 \pm 36(\text{stat.}) \pm 6(\text{syst.}) \text{ eV}$$

$$\Gamma(1s) = 541 \pm 89(\text{stat.}) \pm 22(\text{syst.}) \text{ eV}$$

$$\varepsilon + \frac{i\Gamma}{2} = 2\alpha^3 \mu^2 a_{K^-p} = 412 \frac{\text{eV}}{\text{fm}} a_{K^-p}$$



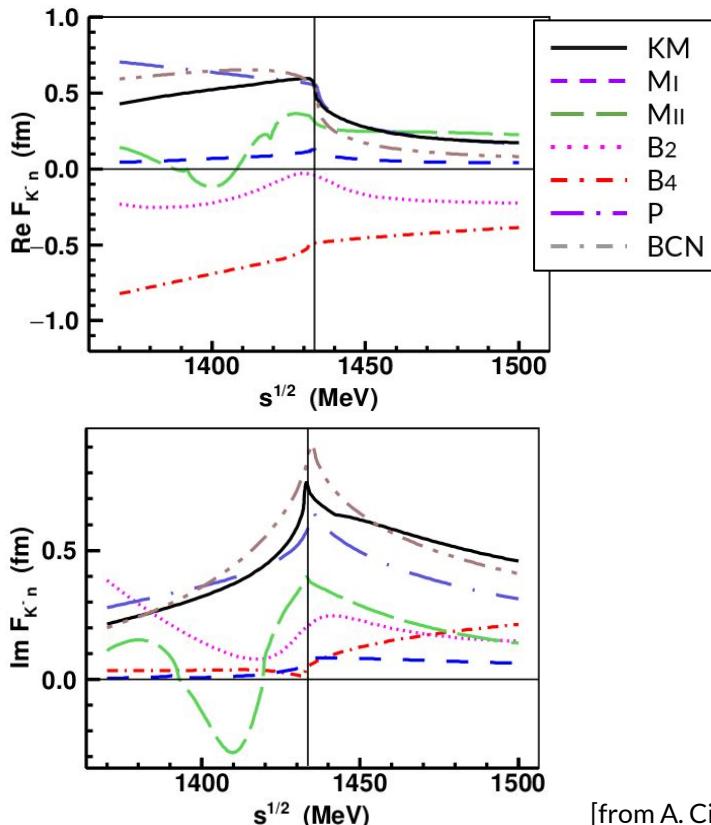
# Below threshold



No data below threshold

**NEW EXPERIMENTAL  
CONSTRAINTS ARE  
STRONGLY NEEDED!!**

# $K^-n$ scattering amplitude



$K^-n$  scattering amplitude with Chiral models

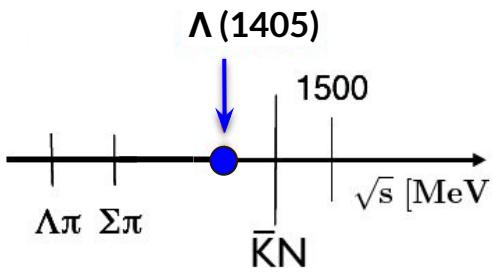
Large spread in  $|l|=1$  channel

Experimental information is totally missing:

- SIDDHARTA-2 → first experimental constraint at threshold
- AMADEUS → first experimental constraint below threshold

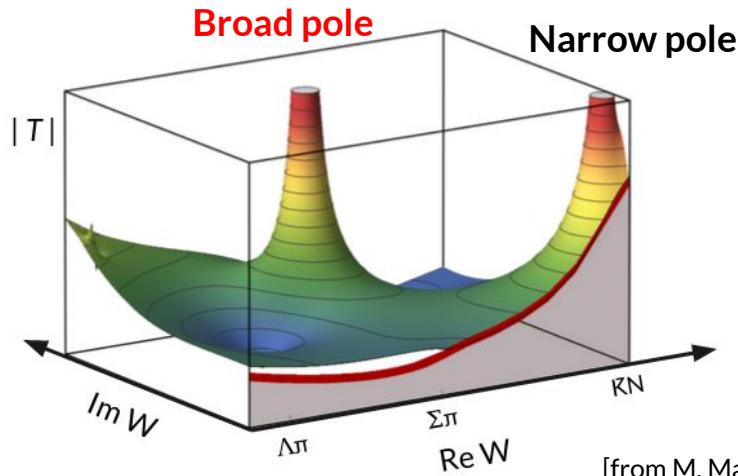
[from A. Cieply talk at MENU2019 conference]

# Impact on $\Lambda(1405)$ nature

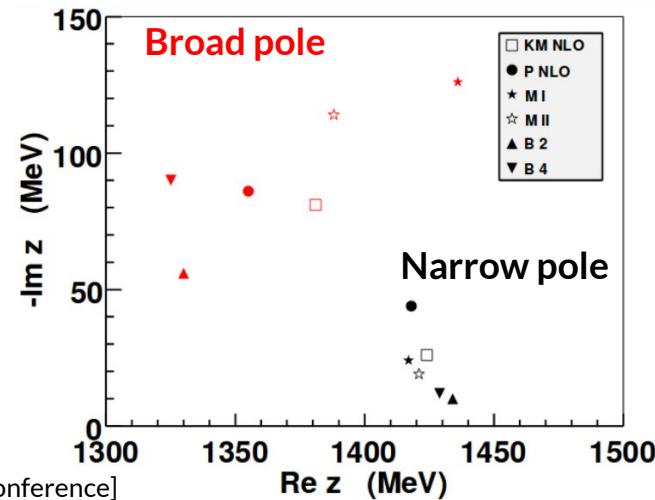


The  $\Lambda(1405)$  state does not fit with the simple three quarks model ( $uds$ ) and it is commonly accepted to be **partially, a  $\bar{K}N$  bound state**.

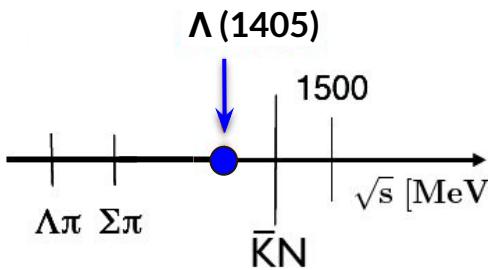
**Chiral models:** dynamical origin. Two poles of the scattering amplitude  $\rightarrow$  pole positions is model dependent (relative contributions not measured experimentally)



[from M. Mai talk at NSTAR19 conference]

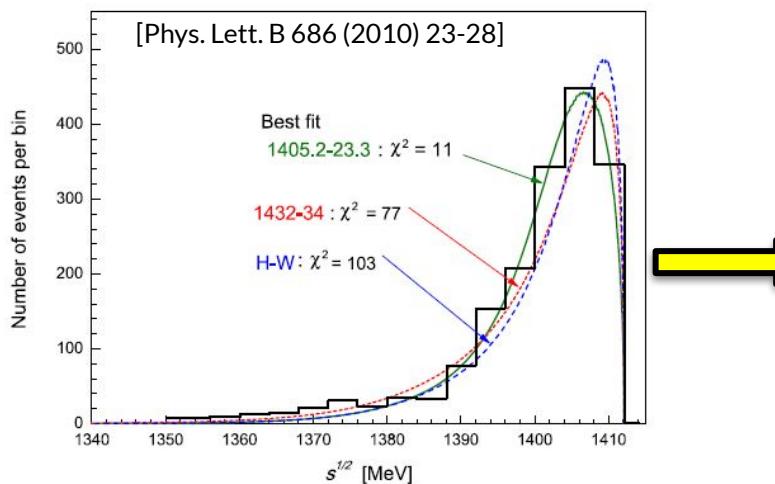


# Impact on $\Lambda(1405)$ nature

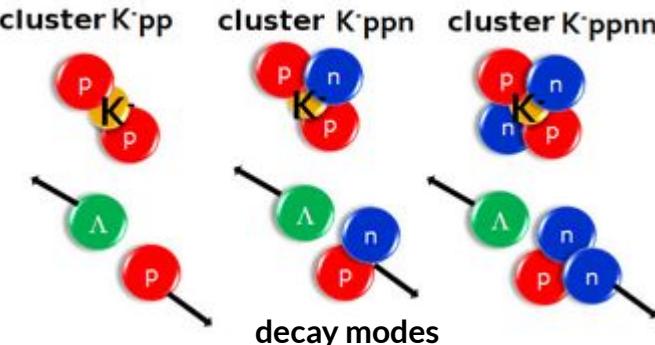


The  $\Lambda(1405)$  state does not fit with the simple three quarks model ( $uds$ ) and it is commonly accepted to be **partially, a  $\bar{K}N$  bound state**.

**Single pole ansatz (Esmaili-Akaishi-Yamazaki phenomenological potentials model):** Very strongly attractive  $\bar{K}N$  interaction → existence of deeply bound kaonic bound states

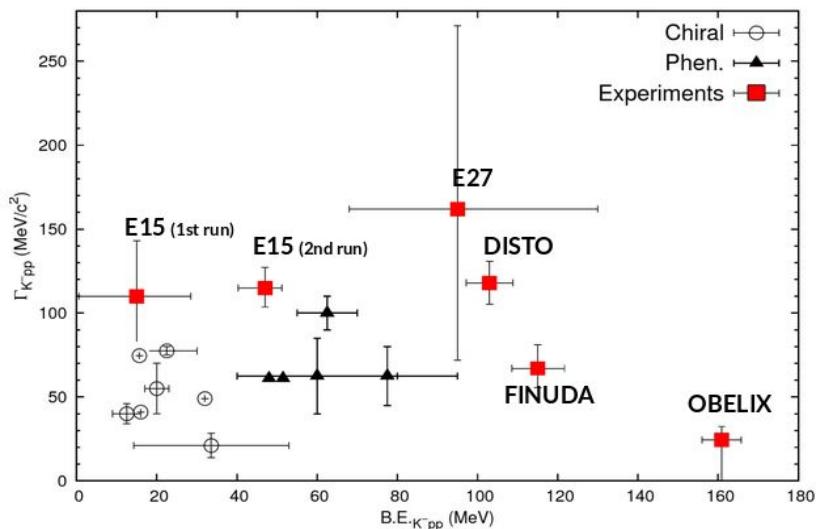


## Kaonic Bound States



# $K^-pp$ bound state

- KN input model is critical for the theoretical interpretation
- different bound state production mechanisms are experimentally investigated
- E15 → **first clear evidence** in  $K^-$  induced reactions (theoretical interpretation by Sekihara, Oset, Ramos)



	BE (MeV)	$\Gamma$ (MeV)	Reference
Dote, Hyodo, Weise	17-23	40-70	Phys.Rev.C79 (2009) 014003
Akaishi, Yamazaki	48	61	Phys.Rev.C65 (2002) 044005
Barnea, Gal, Liverts	16	41	Phys.Lett.B712 (2012) 132-137
Ikeda, Sato	60-95	45-80	Phys.Rev.C76 (2007) 035203
Ikeda, Kamano, Sato	9-16	34-46	Prog.Theor.Phys. (2010) 124(3): 533
Shevchenko, Gal, Mares	55-70	90-110	Phys.Rev.Lett.98 (2007) 082301
Revai, Shevchenko	32	49	Phys.Rev.C90 (2014) no.3, 034004
Maeda, Akaishi, Yamazaki	51.5	61	Proc.Jpn.Acad.B 89, (2013) 418
Bicudo	14.2-53	13.8-28.3	Phys.Rev.D76 (2007) 031502
Bayar, Oset	15-30	75-80	Nucl.Phys.A914 (2013) 349
Wycech, Green	40-80	40-85	Phys.Rev.C79 (2009) 014001
Sekihara, Oset, Ramos	16	72	Prog.Theor.Phys. (2016) no.12, 123D03
Sekihara, Oset, Ramos	20	80	E. Oset talk at UJ Symposium 2019

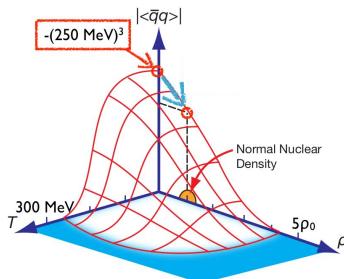
Experiment	BE (MeV)	$\Gamma$ (MeV)	Reference
FINUDA	$115^{+6}_{-5}$ (stat.) $^{+3}_{-4}$ (syst.)	$67^{+14}_{-11}$ (stat.) $^{+2}_{-3}$ (syst.)	PRL 94 (2005), 212303
OBELIX	$160.9 \pm 4.9$	$< 24.4 \pm 8.0$	NPA 789 (2007), 222
E549	-	-	MPLA 23 (2008), 2520
DISTO	$103 \pm 3$ (stat.) $\pm 5$ (syst.)	$118 \pm 8$ (stat.) $\pm 10$ (syst.)	PRL 104 (2010), 132502
LEPS/SPring-8	Upper Limit		PLB 728 (2014), 616
HADES	Upper Limit		PLB 742 (2015), 242
E27	$95^{+18}_{-17}$ (stat.) $^{+30}_{-21}$ (syst.)	$162^{+87}_{-45}$ (stat.) $^{+66}_{-78}$ (syst.)	PTEP (2015), 021D01
AMADEUS	Upper Limit		PLB 758 (2016), 134
E15	$15^{+6}_{-8}$ (stat.) $\pm 12$ (syst.)	$110^{+19}_{-17}$ (stat.) $\pm 27$ (syst.)	PTEP (2016), 051D01
E15 (2 <sup>nd</sup> run)	$47 \pm 3$ (stat.) $^{+3}_{-4}$ (syst.)	$115 \pm 7$ (stat.) $^{+10}_{-20}$ (syst.)	PLB 789 (2019), 620

Experiments

Theory

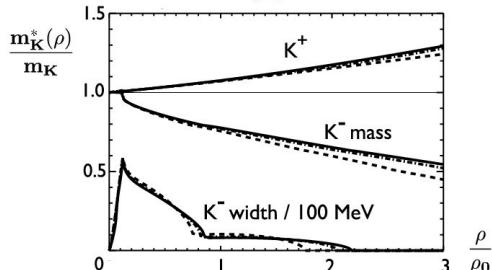
# Impact on in-medium KN interaction

- Partial restoration of chiral symmetry in medium

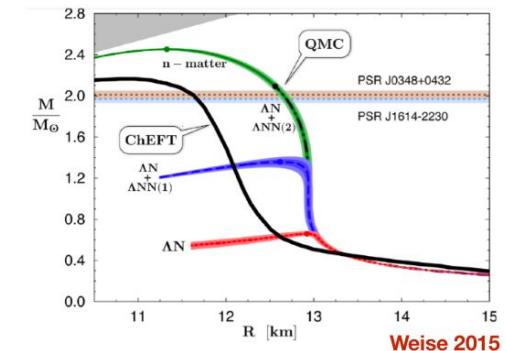
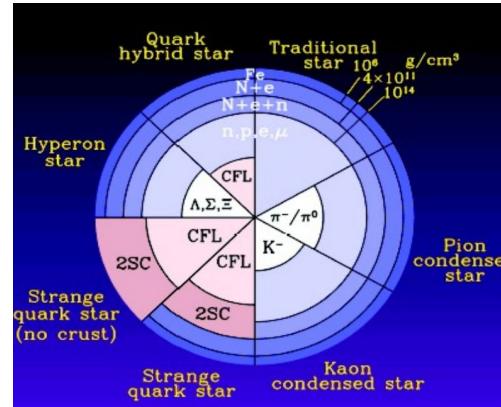


kaon mass modification:

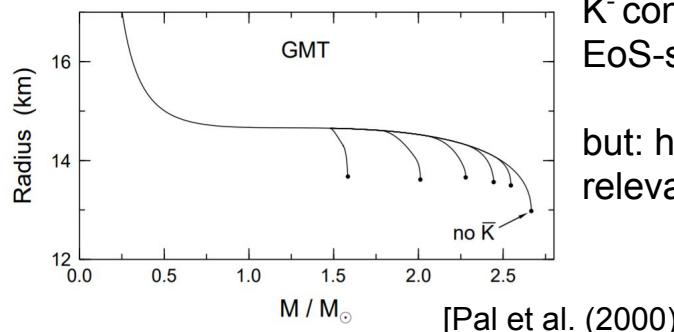
$$m_K^{*2} = m_K^2 - \frac{\Sigma_{\text{KN}}}{f_\pi^2} \rho + \mathcal{O}(k_F^4)$$



- Impact on Equation of State (EoS) of Neutron Stars:



$K^-$  condensate can change EoS-stiffness



but: hyperons become more relevant at higher densities  
[Gal et al. (2016)]

# Goals of AMADEUS

Unprecedented studies of the **low-energy charged kaons interactions in nuclear matter**: solid and gaseous targets ( $\text{H}$ ,  ${}^4\text{He}$ ,  ${}^8\text{Be}$ ,  ${}^{12}\text{C}$  ...) in order to obtain unique quality information about:

1. Controversial nature of the  $\Lambda(1405)$  and  $\bar{K}N$  amplitude below threshold



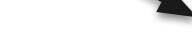
**YJ CORRELATION STUDIES**

(i.e.  $\Lambda\pi$  and  $\Sigma\pi$  and final states)

2. Low-energy charged kaon **cross sections** for momenta of 100 MeV/c



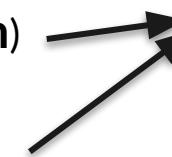
3. a) Interaction of  $K^-$  with one and more nucleons  
**(single and multi-nucleon  $K^-$  absorption)**



**YN CORRELATION STUDIES**

(i.e.  $\Lambda p$ ,  $\Sigma^0 p$ , and  $\Lambda t$  final states)

3. b) possible existence of **kaonic bound states**

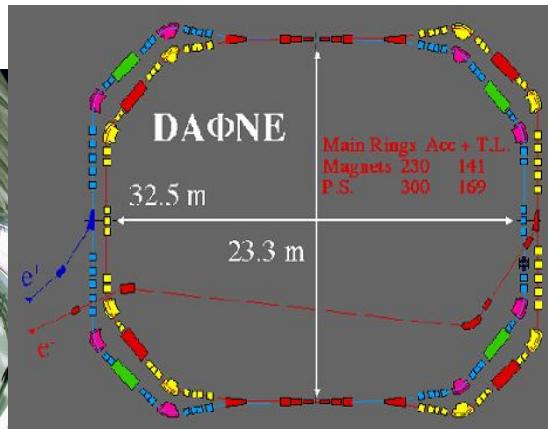
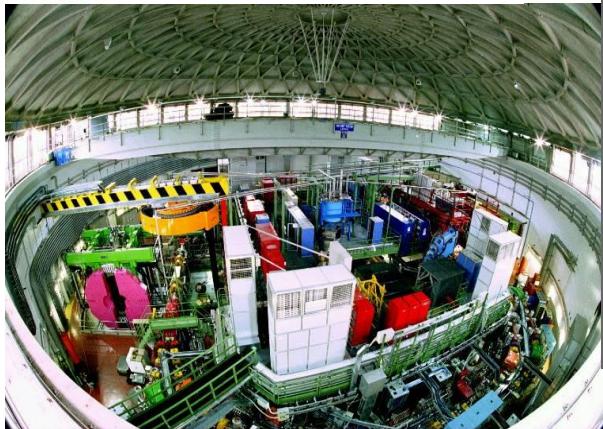


4. **YN scattering** → extremely poor experimental information from scattering data  
(helpful to understand the EoS of Neutron Stars)

# DAΦNE the $\Phi$ factory



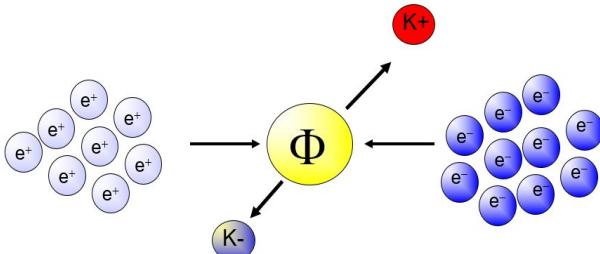
Istituto Nazionale di Fisica Nucleare  
LABORATORI NAZIONALI DI FRASCATI



- $e^+ e^-$  at 510 MeV
- $\Phi$  resonance decays at 49.2 % in  $K^+$
- $K^-$  back to back pair
- Very low momentum ( $\approx 127$  MeV)  $K^-$  beam
- Flux of produced kaons: about 1000/second

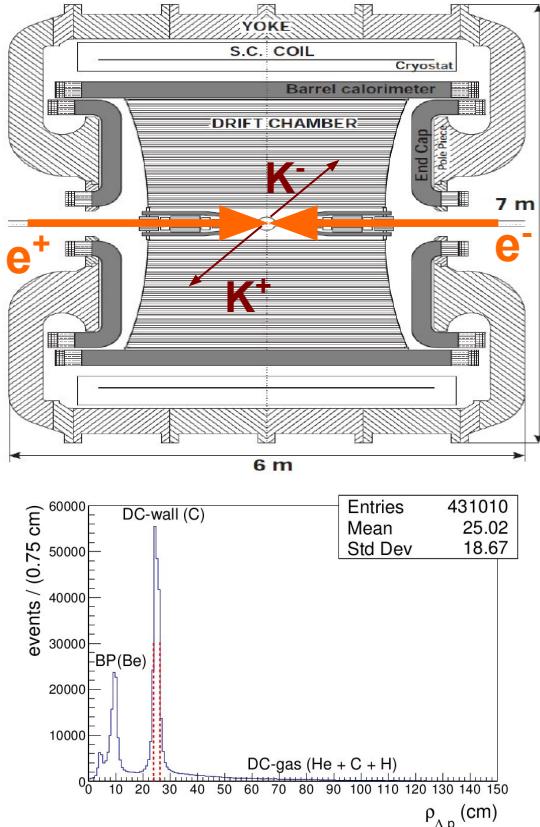


Best low momentum  $K^-$  factory in the world



Suitable for low-energy kaon physics:  
→ **Kaonic atoms (SIDDHARTA-2)**  
→ **Kaon-nucleons/nuclei interaction studies (AMADEUS)**

# AMADEUS step 0



## The KLOE detector

- Cylindrical drift chamber with a  **$4\pi$  geometry** and electromagnetic calorimeter
- **96% acceptance**
- optimized in the energy range of all **charged particles** involved
- **good performance** in detecting **photons and neutrons** checked by kloNe group  
[M. Anelli et al., Nucl Inst. Meth. A 581, 368 (2007)]

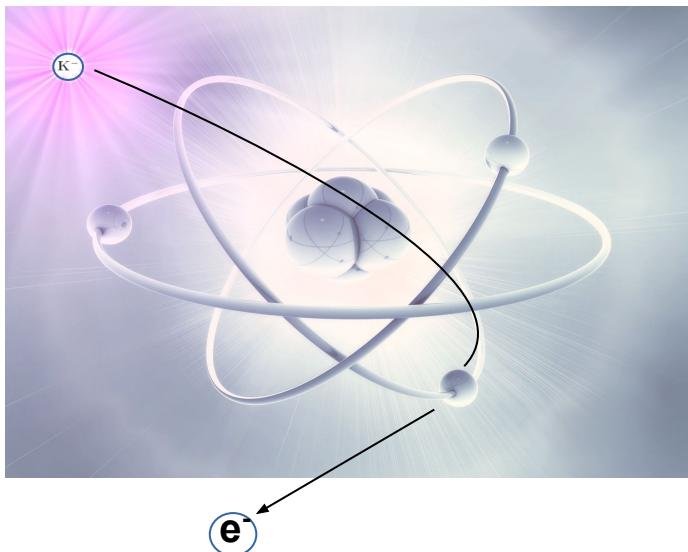
Possibility to use KLOE materials as an **active target**

- DC wall ( $750 \mu\text{m}$  C foil,  $150 \mu\text{m}$  Al foil);
- DC gas (90% He, 10%  $\text{C}_4\text{H}_{10}$ ).

# $K^-$ absorptions at-rest and in-flight

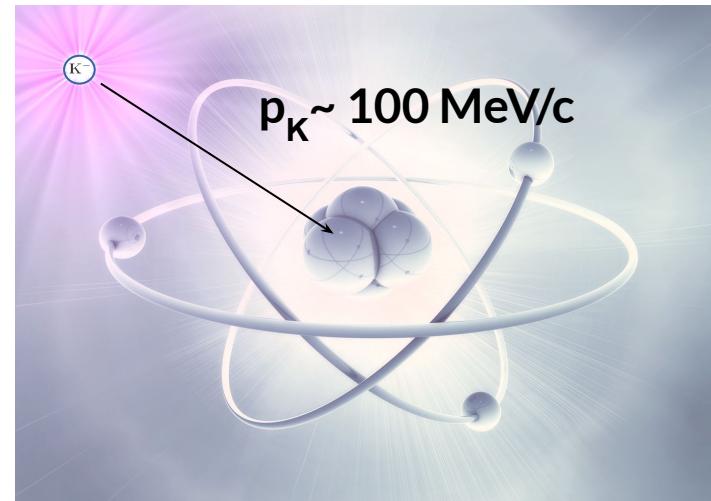
## AT-REST

$K^-$  absorbed from atomic orbitals  
( $p_K \sim 0 \text{ MeV}/c$ )

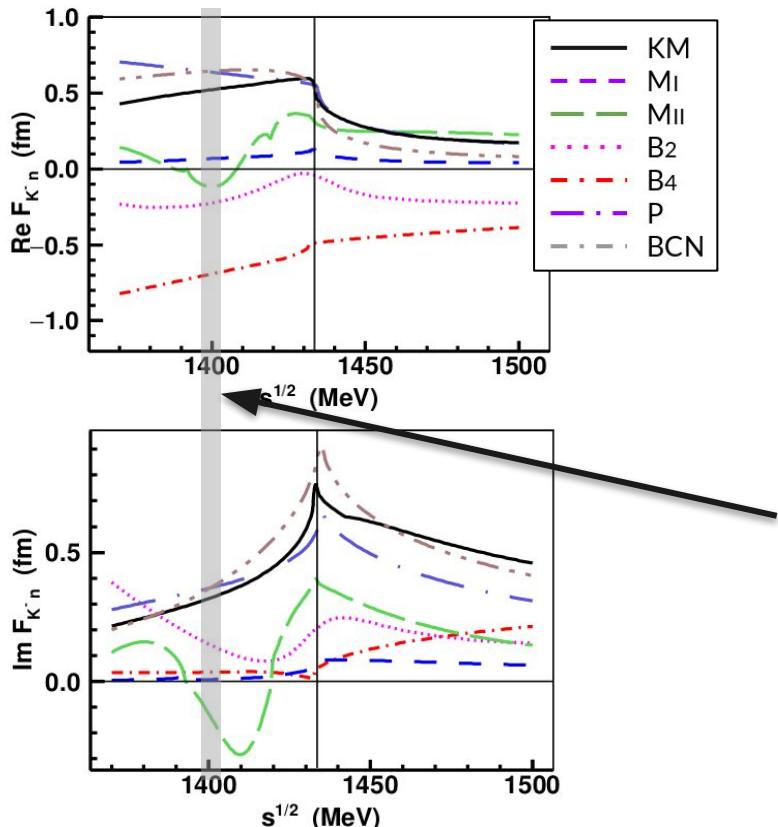


## IN-FLIGHT

( $p_K \sim 100 \text{ MeV}/c$ )



# Experimental constraints at threshold



$K^-n$  scattering amplitude with Chiral models

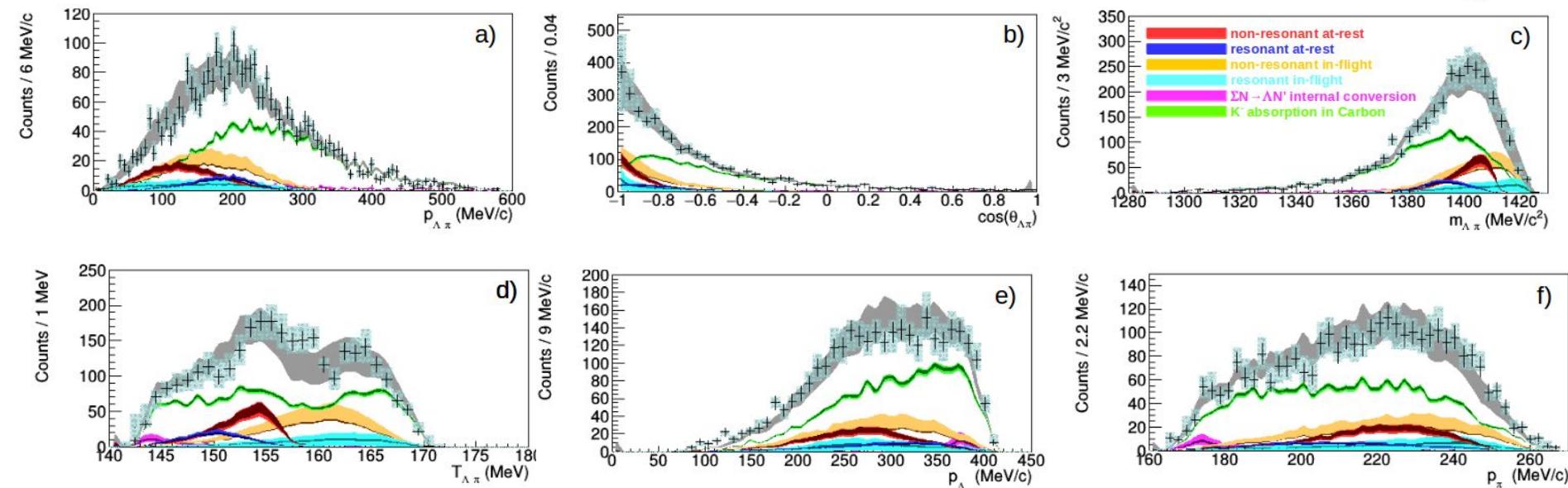
Large spread in  $l=1$  channel

Experimental information is totally missing:

- SIDDHARTA-2 → first experimental constraint at threshold
- AMADEUS → First determination of the non-resonant transition amplitude below threshold  
Investigated using:  
 $K^- "n" \rightarrow \Lambda\pi^-$  to extract  $|f^{N-R}_{\Lambda\pi}(l=1)|$  below threshold

# Simultaneous fit : $p_{\Lambda\pi^-}$ - $m_{\Lambda\pi^-}$ - $\cos\theta_{\Lambda\pi^-}$

Investigated using:  $K^-$  “n”  $^3He \rightarrow \Lambda\pi^-$   $^3He$

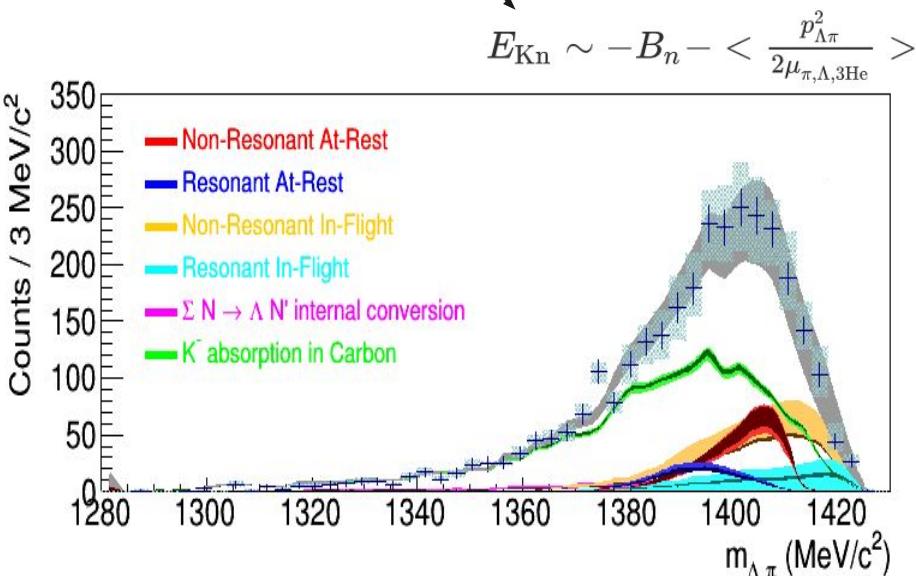


[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]

[K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

# Outcome of the measurement

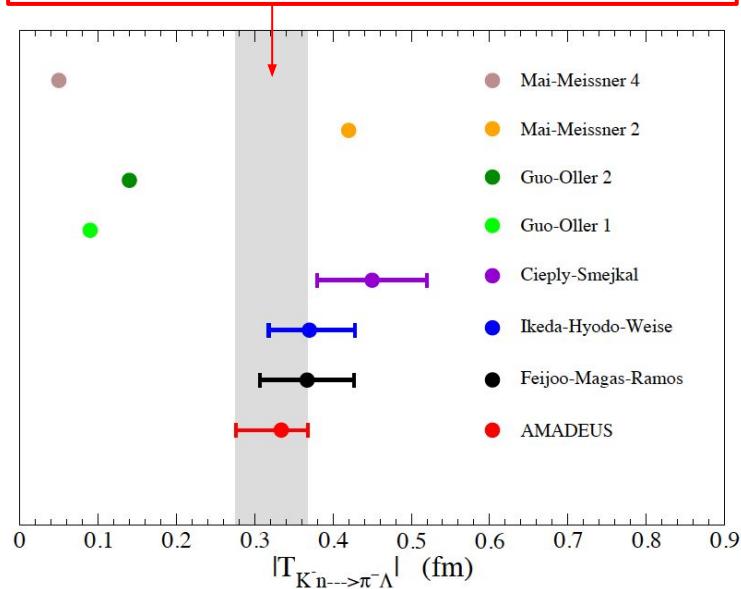
Investigated using:  $K^- "n" ^3He \rightarrow \Lambda \pi^- ^3He$



[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]

[K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

$$|f_{ar}^s| = (0.334 \pm 0.018 \text{ stat}^{+0.034}_{-0.058} \text{ syst}) \text{ fm}.$$



# $K^- p \rightarrow \Sigma^0 \pi^0$ cross section

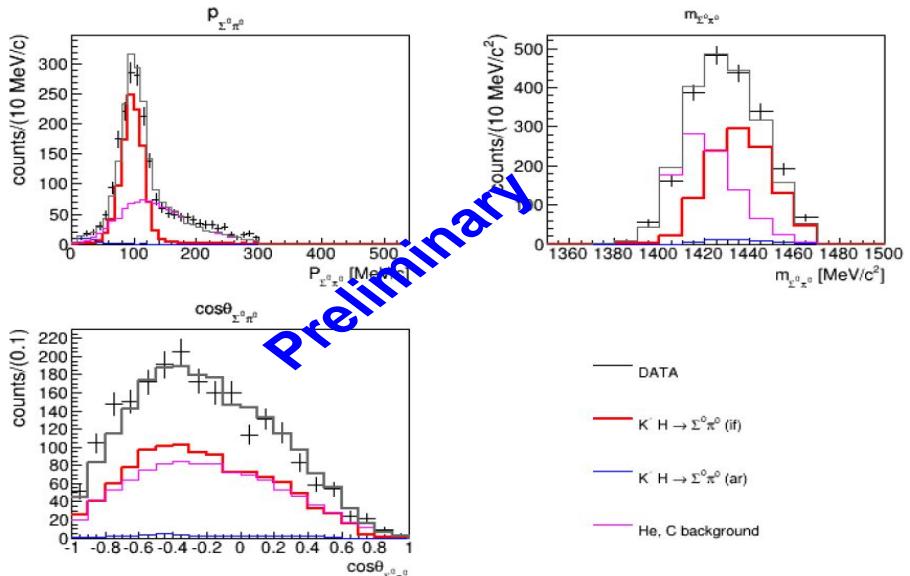
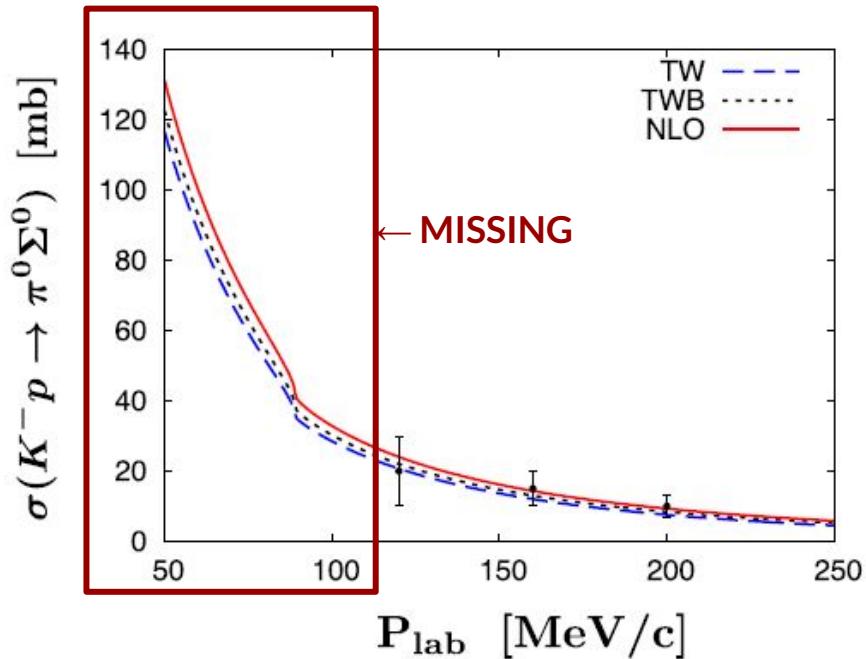


Figure 14.  $K^- p \rightarrow \Sigma^0 \pi^0$  cross section as function of  $K^-$  laboratory momentum. The black points represent the experimental data from [15, 16], the corresponding uncertainty on the kaon momentum is not shown in this figure. The solid red curve with the shaded uncertainty band represents the theoretical calculation in Ref. [12]. The blue point is the measurement of this work.

- [15] W. E. Humphrey and R. R. Ross, Phys. Rev. 127 (1962) 1305
- [16] J. K. Kim, Columbia University Report No. NEVIS-149 (1966)
- [12] Y. Ikeda, T. Hyodo, W. Weise, Nucl. Phys. A 881 (2012) 98

# $K^-$ multi-nucleon absorptions

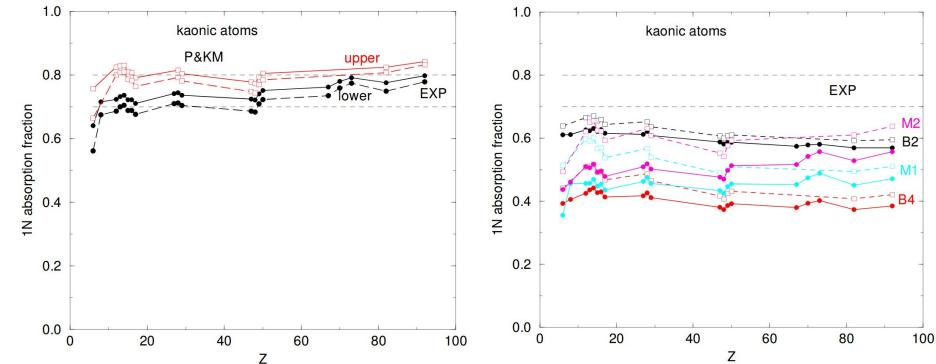
In  $K^-$ -nuclei optical potential a  $K^-$  multi-nucleon absorption term is necessary to fit the kaonic atoms data:

$$V_{K^-}(\rho) = V_{K^-}^{(1)}(\rho) + V_{K^-}^{(2)}(\rho) \rightarrow \text{multi-nucleon term}$$

[E. Friedman, A. Gal, Nucl. Phys. A 959, 66 (2017)]

[Hrtáková, J. & Mareš, J. Phys. Rev. C96, 015205 (2017)]

single nucleon term from chiral models



- Single nucleon absorption (**1NA**):
- Two nucleon absorption (**2NA**):
- Three nucleon absorption (**3NA**):
- Four nucleon absorption (**4NA**):

$K^- "N" \rightarrow Y \pi$   $\longrightarrow$  pionic processes

$K^- "NN" \rightarrow Y N$

$K^- "NNN" \rightarrow Y (NN)$

$K^- "NNNN" \rightarrow Y (NNN)$

+ non-pionic processes

bound nucleons = “N”, “NN”, “NNN”, “NNNN”

bound or unbound nucleons = (NN), (NNN)

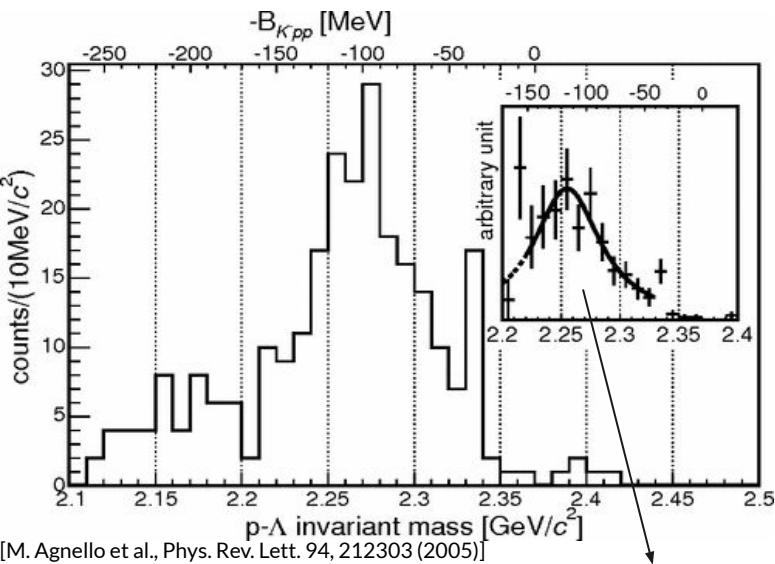
$Y = \Lambda, \Sigma$

# Experimental search in $K^-$ induced reactions

FINUDA at DAΦNE:  $K^-_{\text{stop}} + X \rightarrow \Lambda + p + X'$

only back-to-back  $\Lambda p$  pairs ( $\cos\theta_{\Lambda p} < -0.8$ )

detected particles



[M. Agnello et al., Phys. Rev. Lett. 94, 212303 (2005)]

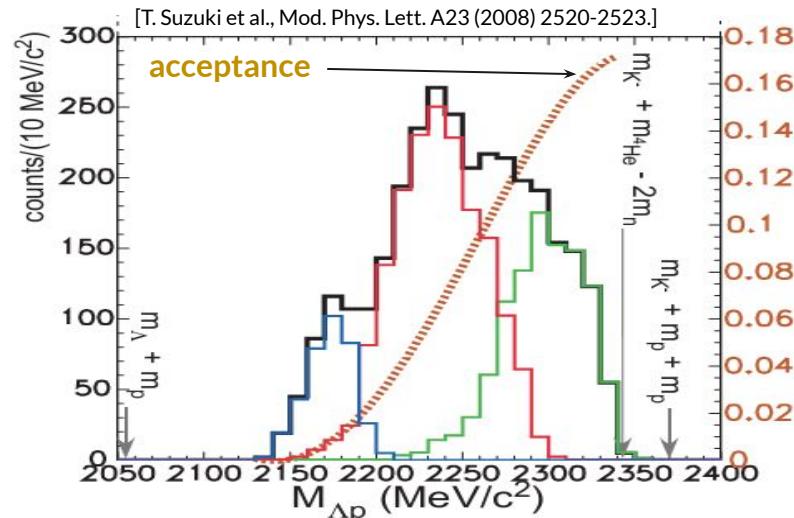
Interpreted as the signal of:  
**extracted parameters:**  $K^- pp \rightarrow \Lambda + p$

$$BE = (115^{+6}_{-5} \text{ (stat.)}^{+3}_{-4} \text{ (syst.)}) \text{ MeV}$$

$$\Gamma = (67^{+14}_{-11} \text{ (stat.)}^{+2}_{-3} \text{ (syst.)}) \text{ MeV}/c^2$$

E549 at KEK:  $K^-_{\text{stop}} + {}^4\text{He} \rightarrow \Lambda + p + X'$

detected particles



Using the missing mass information, three components to the invariant mass spectrum are found:

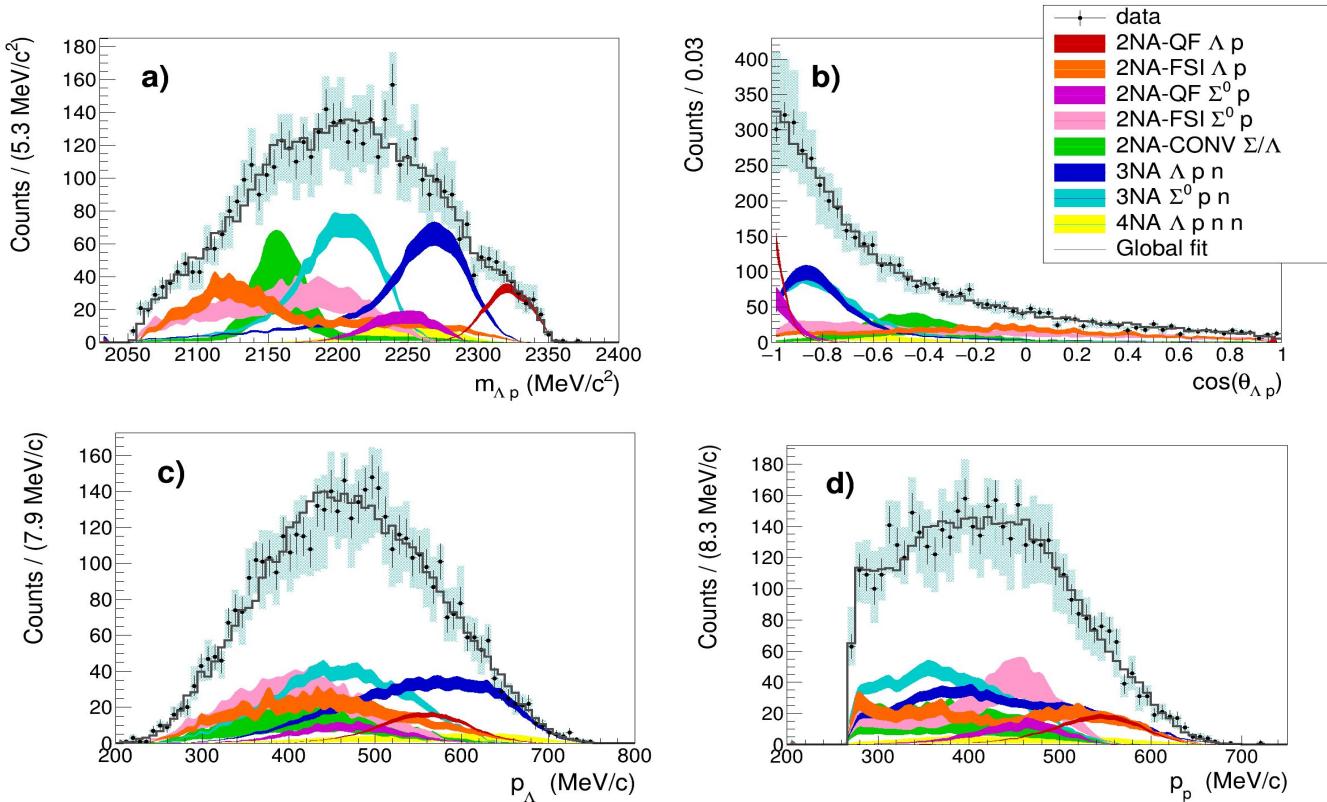
- **1NA:**  $K^-$  single nucleon absorption
- **2NA:**  $K^-$  two nucleon absorption
- **2NA + conversion, multi-nucleon, or Bound State?**

# $\Lambda p$ analysis: $K^- + {}^{12}C \rightarrow \Lambda + p + R$

Simultaneous fit of:

- $\Lambda p$  invariant mass;
- angular correlation;
- proton momentum;
- $\Lambda$  momentum.

Total reduced  $\chi^2$ :  $\chi^2/dof = 0.94$



[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]  
[R. Del Grande, K. Piscicchia, S. Wycech, Acta Phys. Pol. B 48 (2017) 1881]

# $\Lambda p$ analysis: $K^-$ multi-nucleon absorption BRs and $\sigma$

[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]

Process	Branching Ratio (%)	$\sigma$ (mb)	@	$p_K$ (MeV/c)
2NA-QF $\Lambda p$	$0.25 \pm 0.02$ (stat.) $^{+0.01}_{-0.02}$ (syst.)	$2.8 \pm 0.3$ (stat.) $^{+0.1}_{-0.2}$ (syst.)	@	$128 \pm 29$
2NA-FSI $\Lambda p$	$6.2 \pm 1.4$ (stat.) $^{+0.5}_{-0.6}$ (syst.)	$69 \pm 15$ (stat.) $\pm 6$ (syst.)	@	$128 \pm 29$
2NA-QF $\Sigma^0 p$	$0.35 \pm 0.09$ (stat.) $^{+0.13}_{-0.06}$ (syst.)	$3.9 \pm 1.0$ (stat.) $^{+1.4}_{-0.7}$ (syst.)	@	$128 \pm 29$
2NA-FSI $\Sigma^0 p$	$7.2 \pm 2.2$ (stat.) $^{+4.2}_{-5.4}$ (syst.)	$80 \pm 25$ (stat.) $^{+46}_{-60}$ (syst.)	@	$128 \pm 29$
2NA-CONV $\Sigma/\Lambda$	$2.1 \pm 1.2$ (stat.) $^{+0.9}_{-0.5}$ (syst.)	-		
3NA $\Lambda p n$	$1.4 \pm 0.2$ (stat.) $^{+0.1}_{-0.2}$ (syst.)	$15 \pm 2$ (stat.) $\pm 2$ (syst.)	@	$117 \pm 23$
3NA $\Sigma^0 p n$	$3.7 \pm 0.4$ (stat.) $^{+0.2}_{-0.4}$ (syst.)	$41 \pm 4$ (stat.) $^{+2}_{-5}$ (syst.)	@	$117 \pm 23$
4NA $\Lambda p n n$	$0.13 \pm 0.09$ (stat.) $^{+0.08}_{-0.07}$ (syst.)	-		
Global $\Lambda(\Sigma^0)p$	$21 \pm 3$ (stat.) $^{+5}_{-6}$ (syst.)	-		

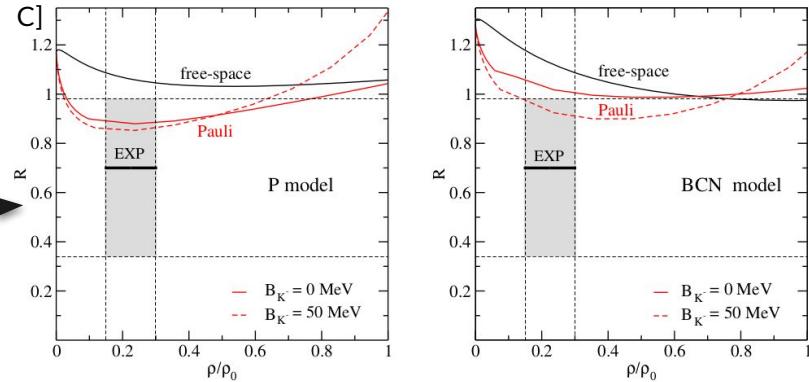
The ratio between the branching ratios of the 2NA-QF in the  $\Lambda p$  channel and in the  $\Sigma^0 p$  is measured to be:

$$\mathcal{R} = \frac{BR(K^- pp \rightarrow \Lambda p)}{BR(K^- pp \rightarrow \Sigma^0 p)} = 0.7 \pm 0.2 \text{ (stat.)} ^{+0.2}_{-0.3} \text{ (syst.)}$$

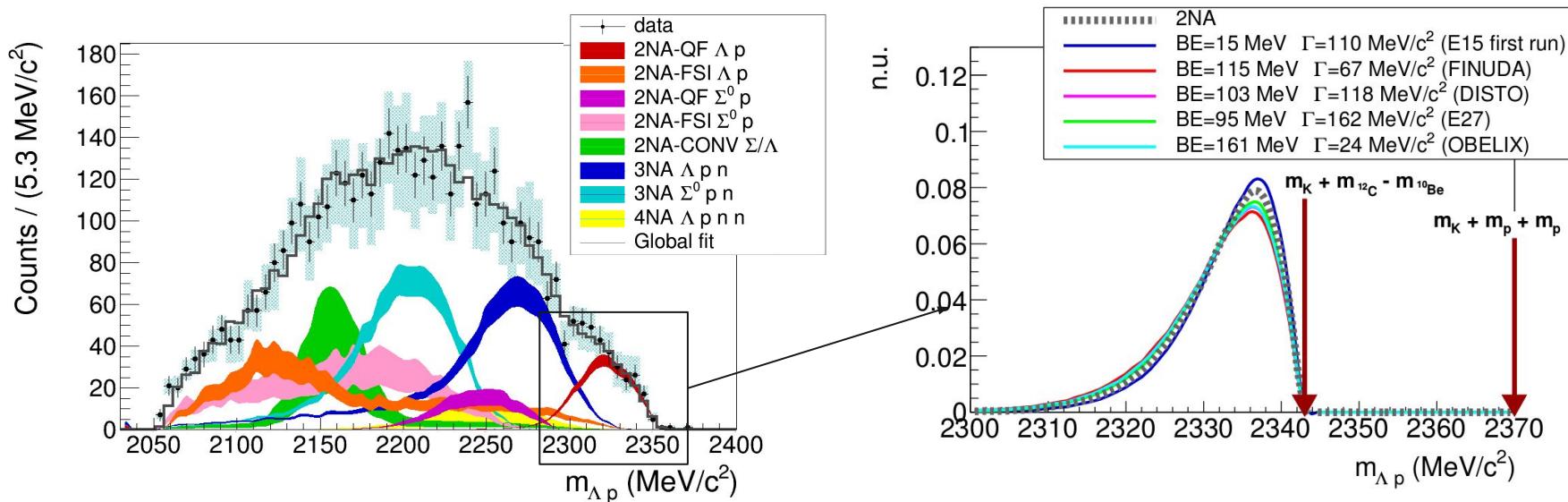
and the ratio between the corresponding phase spaces is  $\mathcal{R}' \simeq 1.22$ .

## Information on the in-medium dynamics

[J. Hrtáková, A. Ramos, arXiv:1910.01336, submitted to Phys. Rev. C]



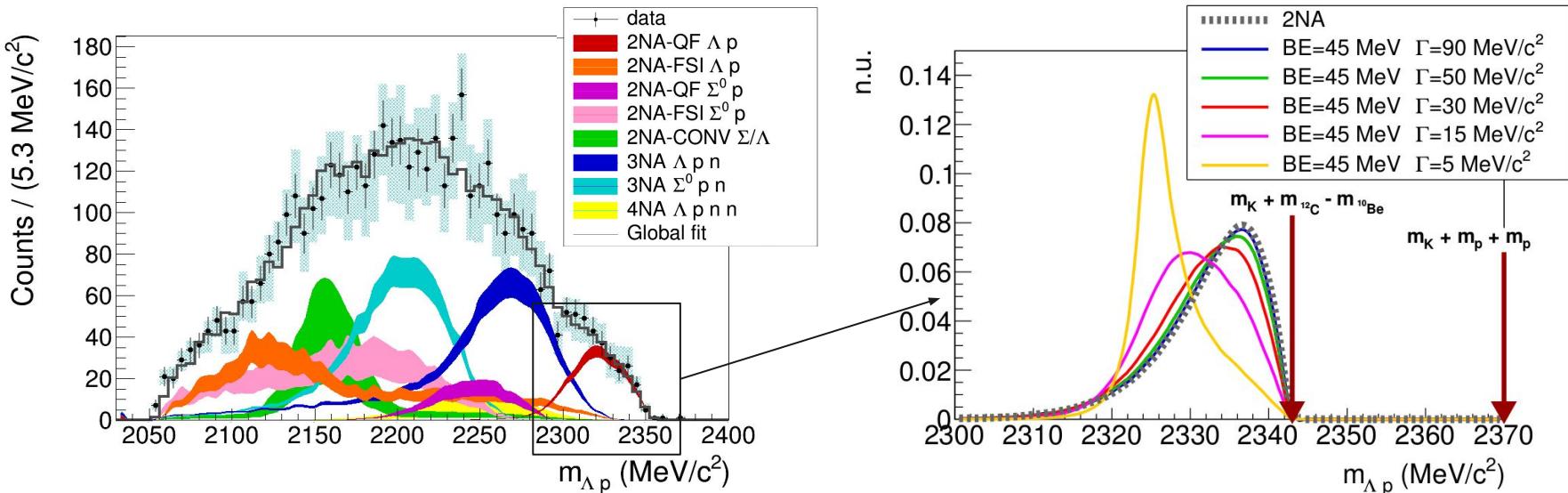
# $\Lambda p$ analysis: $K^- pp$ bound state



$K^- pp$  bound state contribution completely overlaps with the  $K^- 2NA$

[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]  
 [R. Del Grande, K. Piscicchia, S. Wycech, Acta Phys. Pol. B 48 (2017) 1881]

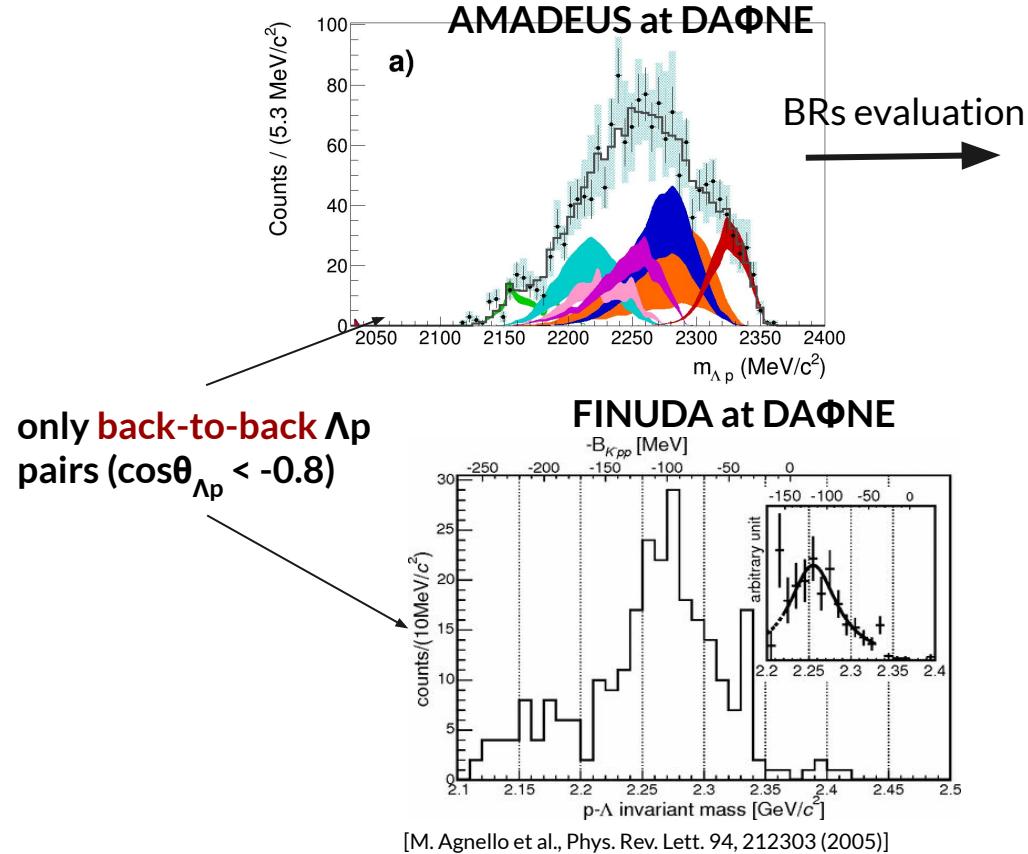
# $\Lambda p$ analysis: $K^- pp$ bound state



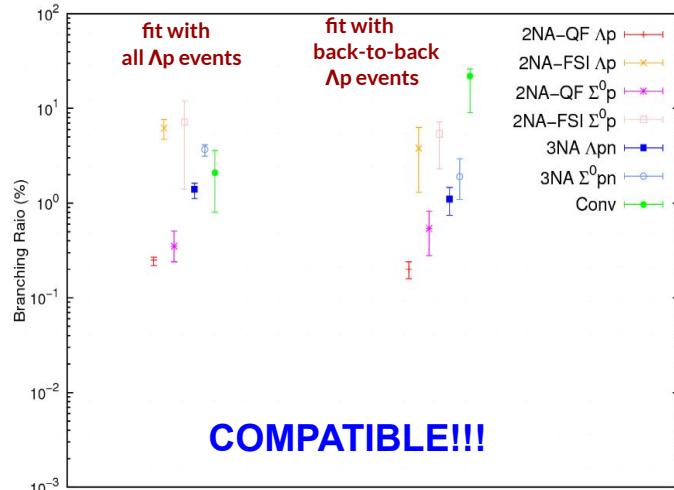
$K^- pp$  bound state contribution completely overlaps with the  $K^- 2NA$

[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]  
 [R. Del Grande, K. Piscicchia, S. Wycech, Acta Phys. Pol. B 48 (2017) 1881]

# $\Lambda p$ analysis: $K^- pp$ bound state search



Process	Branching Ratio (%)
2NA-QF $\Lambda p$	$0.20 \pm 0.04(\text{stat.}) \pm 0.02(\text{syst.})$
2NA-FSI $\Lambda p$	$3.8 \pm 2.3(\text{stat.}) \pm 1.1(\text{syst.})$
2NA-QF $\Sigma^0 p$	$0.54 \pm 0.20(\text{stat.})^{+0.20}_{-0.16}(\text{syst.})$
2NA-FSI $\Sigma^0 p$	$5.4 \pm 1.5(\text{stat.})^{+1.0}_{-2.7}(\text{syst.})$
2NA-CONV $\Sigma/\Lambda$	$22 \pm 4(\text{stat.})^{+1}_{-12}(\text{syst.})$
3NA $\Lambda p n$	$1.1 \pm 0.3(\text{stat.}) \pm 0.2(\text{syst.})$
3NA $\Sigma^0 p n$	$1.9 \pm 0.7(\text{stat.})^{+0.8}_{-0.4}(\text{syst.})$



# $\Lambda t$ analysis: Cross section and BR for 4NA

GOLDEN CHANNEL to extrapolate the  $K^- 4NA$



Previous data:

- in  ${}^4\text{He}$ : bubble chamber experiment

/M. Roosen, J. H. Wickens, Il Nuovo Cimento 66, 101 (1981)/

only 3 events compatible with  $\Lambda t$  kinematics found

$$\text{BR}(K^- {}^4\text{He} \rightarrow \Lambda t) = (3 \pm 2) \times 10^{-4} / K_{\text{stop}} \rightarrow \text{global, no 4NA}$$

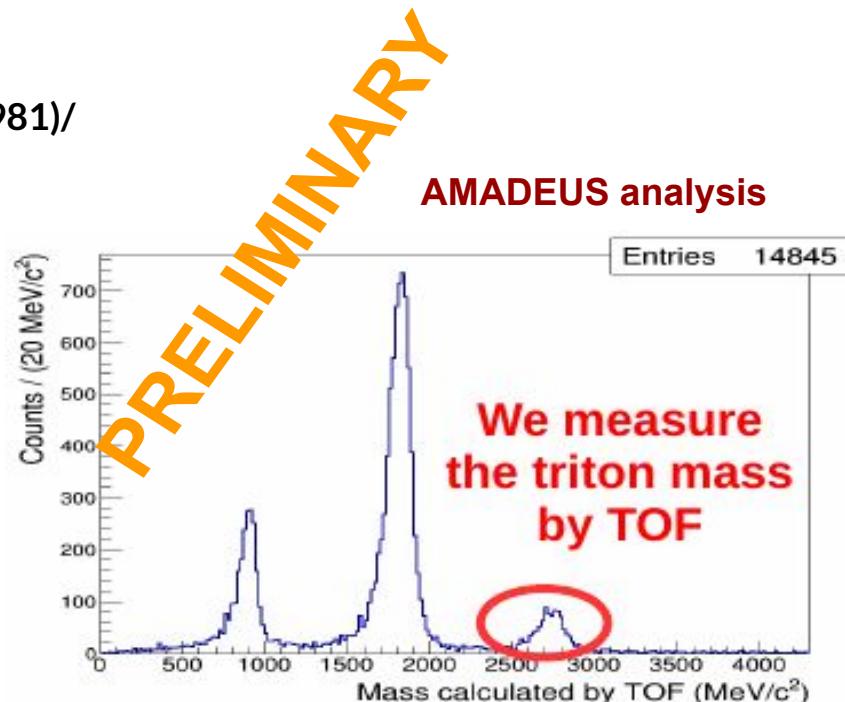
- in solid targets:  ${}^{6,7}\text{Li}$ ,  ${}^9\text{Be}$  (FINUDA)

/Phys. Lett. B, 229 (2008)/

40 events, only back-to-back data

$$\Lambda t \text{ emission yield} \rightarrow 10^{-3} - 10^{-4} / K_{\text{stop}}$$

$\rightarrow$  global, no 4NA



# $\Lambda t$ analysis: Cross section and BR for 4NA in $K^- {}^4He \rightarrow \Lambda t$ process

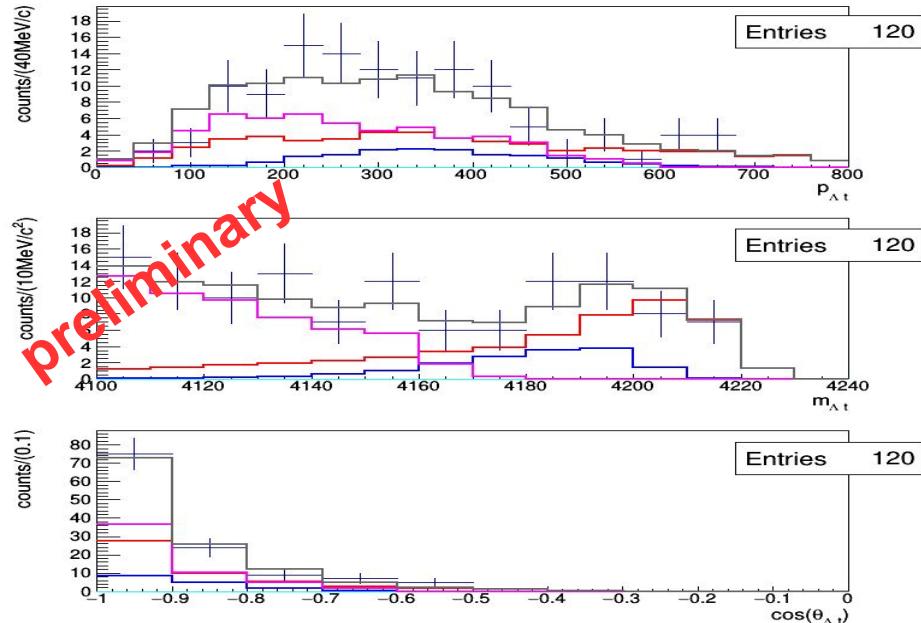
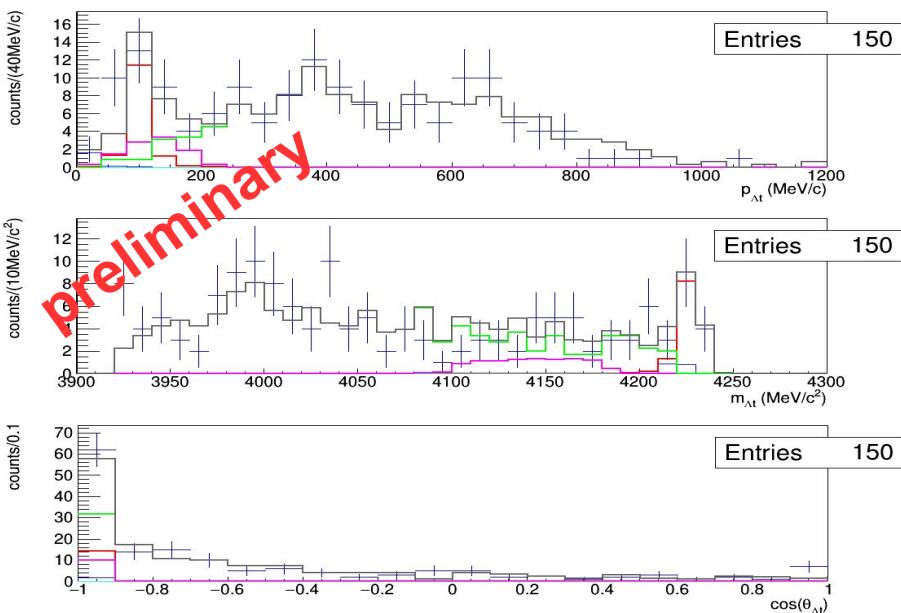
$$BR(K^- {}^4He(4NA) \rightarrow \Lambda t) < 2.0 \times 10^{-4} / K_{stop} \text{ (95% c. l.)}$$

$$\sigma(100 \pm 19 \text{ MeV/c}) (K^- {}^4He(4NA) \rightarrow \Lambda t) = \\ = (0.81 \pm 0.21 \text{ (stat)} {}^{+0.03}_{-0.04} \text{ (syst)}) \text{ mb}$$

$$BR(K^- {}^{12}C(4NA) \rightarrow \Lambda t {}^8Be) = 1.5 \pm 0.5 \times 10^{-4} \text{ (stat)} / K_{stop}$$

$$\sigma(K^- {}^{12}C(4NA) \rightarrow \Lambda t {}^8Be) = 0.58 \pm 0.11 \text{ (stat)} \text{ mb}$$

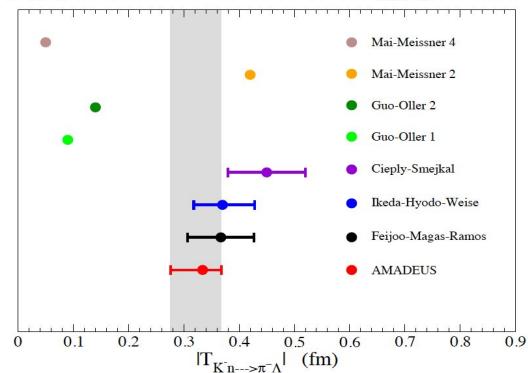
$$\sigma(K^- {}^{12}C(4NA) \rightarrow \Sigma^0 t {}^8Be) = 1.88 \pm 0.35 \text{ (stat)} \text{ mb}$$



# Summary

## K<sup>-</sup>n amplitude below threshold

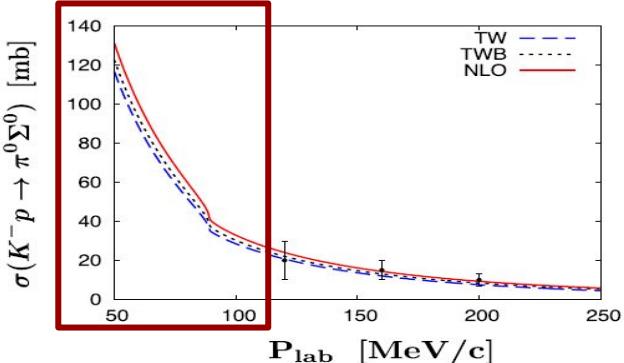
$$|f_{\text{ar}}^s| = (0.334 \pm 0.018 \text{ stat}^{+0.034}_{-0.058} \text{ syst}) \text{ fm}.$$



## $\Lambda$ p channel: 2NA, 3NA and 4NA BRs and $\sigma$

Process	Branching Ratio (%)	$\sigma$ (mb)	@	$p_K$ (MeV/c)
2NA-QF $\Lambda p$	$0.25 \pm 0.02 \text{ (stat.)} {}^{+0.01}_{-0.02} \text{ (syst.)}$	$2.8 \pm 0.3 \text{ (stat.)} {}^{+0.1}_{-0.2} \text{ (syst.)}$	@	$128 \pm 29$
2NA-FSI $\Lambda p$	$6.2 \pm 1.4 \text{ (stat.)} {}^{+0.5}_{-0.6} \text{ (syst.)}$	$69 \pm 15 \text{ (stat.)} \pm 6 \text{ (syst.)}$	@	$128 \pm 29$
2NA-QF $\Sigma^0 p$	$0.35 \pm 0.09 \text{ (stat.)} {}^{+0.13}_{-0.06} \text{ (syst.)}$	$3.9 \pm 1.0 \text{ (stat.)} {}^{+1.4}_{-0.7} \text{ (syst.)}$	@	$128 \pm 29$
2NA-FSI $\Sigma^0 p$	$7.2 \pm 2.2 \text{ (stat.)} {}^{+4.2}_{-5.4} \text{ (syst.)}$	$80 \pm 25 \text{ (stat.)} {}^{+46}_{-60} \text{ (syst.)}$	@	$128 \pm 29$
2NA-CONV $\Sigma/\Lambda$	$2.1 \pm 1.2 \text{ (stat.)} {}^{+0.9}_{-0.5} \text{ (syst.)}$	-		
3NA $\Lambda pn$	$1.4 \pm 0.2 \text{ (stat.)} {}^{+0.1}_{-0.2} \text{ (syst.)}$	$15 \pm 2 \text{ (stat.)} \pm 2 \text{ (syst.)}$	@	$117 \pm 23$
3NA $\Sigma^0 pn$	$3.7 \pm 0.4 \text{ (stat.)} {}^{+0.2}_{-0.4} \text{ (syst.)}$	$41 \pm 4 \text{ (stat.)} {}^{+2}_{-5} \text{ (syst.)}$	@	$117 \pm 23$
4NA $\Lambda pnn$	$0.13 \pm 0.09 \text{ (stat.)} {}^{+0.08}_{-0.07} \text{ (syst.)}$	-		
Global $\Lambda(\Sigma^0)p$	$21 \pm 3 \text{ (stat.)} {}^{+5}_{-6} \text{ (syst.)}$	-		

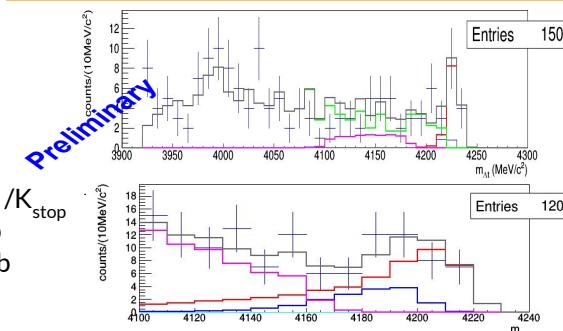
## K<sup>-</sup>p $\rightarrow \Sigma^0 \pi^0$ cross section



## $\Lambda$ t channel: 4NA BRs and $\sigma$

$$\begin{aligned} \text{BR}(K^-{}^4\text{He(4NA)} \rightarrow \Lambda t) &< 2.0 \times 10^{-4} / K_{\text{stop}} \quad (95\% \text{ c. l.}) \\ \sigma(100 \pm 19 \text{ MeV/c}) (K^-{}^4\text{He(4NA)} \rightarrow \Lambda t) &= \\ &= (0.81 \pm 0.21 \text{ (stat)} {}^{+0.03}_{-0.04} \text{ (syst)}) \text{ mb} \end{aligned}$$

$$\begin{aligned} \text{BR}(K^-{}^{12}\text{C(4NA)} \rightarrow \Lambda t {}^8\text{Be}) &= 1.5 \pm 0.5 \times 10^{-4} \text{ (stat) / } K_{\text{stop}} \\ \sigma(K^-{}^{12}\text{C(4NA)} \rightarrow \Lambda t {}^8\text{Be}) &= 0.58 \pm 0.11 \text{ (stat) mb} \\ \sigma(K^-{}^{12}\text{C(4NA)} \rightarrow \Sigma^0 t {}^8\text{Be}) &= 1.88 \pm 0.35 \text{ (stat) mb} \end{aligned}$$



# Thank You