

# The Borromean Picture of Baryons: Diquark Insights

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**Diquark Correlations in Hadron Physics: Origin, Impact and Evidence**

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## Emergence

**Low-level rules producing high-level phenomena with enormous apparent complexity**

Start from the QCD Lagrangian:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_a^{\mu\nu} G_{\mu\nu}^a + \frac{1}{2\xi} (\partial^\mu A_\mu^a)^2 + \partial^\mu \bar{c}^a \partial_\mu c^a + g f^{abc} (\partial^\mu \bar{c}^a) A_\mu^b c^c + \text{quarks}$$



Lattice, DSEs, ...

And obtain:

- ☞ Dynamical generation of fundamental mass scale in pure Yang-Mills (gluon mass).
- ☞ Quark constituent masses and chiral symmetry breaking.
- ☞ Bound state formation: mesons, baryons, glueballs, hybrids, multi-quark systems...
- ☞ Signals of confinement.

**Emergent phenomena** could be associated with dramatic, dynamically driven changes in the analytic structure of QCD's Green functions (propagators and vertices).

Quark propagator:

$$\text{---}\bigcirc\text{---}^{-1} = \text{---}\text{---}^{-1} + \text{---}\bigcirc\text{---}$$

Ghost propagator:

$$\text{---}\bigcirc\text{---}^{-1} = \text{---}\text{---}^{-1} + \text{---}\bigcirc\text{---}$$

Ghost-gluon vertex:

$$\text{---}\bigcirc\text{---} = \text{---}\text{---} + \text{---}\bigcirc\text{---}$$

Gluon propagator:

$$\text{---}\bigcirc\text{---}^{-1} = \text{---}\text{---}^{-1} + \text{---}\bigcirc\text{---} + \text{---}\bigcirc\text{---} + \text{---}\bigcirc\text{---} + \text{---}\bigcirc\text{---} + \text{---}\bigcirc\text{---}$$

Quark-gluon vertex:

$$\text{---}\bigcirc\text{---} = \text{---}\text{---} + \text{---}\bigcirc\text{---} + \text{---}\bigcirc\text{---} + \text{---}\bigcirc\text{---} + \text{---}\bigcirc\text{---} + \text{---}\bigcirc\text{---}$$

## Off-shell Green's (correlation) functions

### Even though they are:

- Gauge dependent.
- Renormalization point and scheme dependent.

### However:

- They capture characteristic features of the underlying dynamics, both perturbative and non-perturbative.
- When appropriately combined they give rise to physical observables.

## Theory tool based on Dyson-Schwinger equations

### Interesting features:

- Inherently non-perturbative but, at the same time, captures the perturbative behavior  $\rightarrow$  accommodates the full range of physical momenta.
- Cover smoothly the full quark mass range, from the chiral limit to the heavy-quark domain.

### Main caveats:

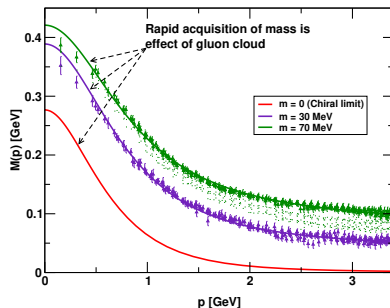
- Truncation of the infinite system of coupled non-linear integral equations that preserves the underlying symmetries of the theory.
- No expansion parameter  $\rightarrow$  no formal way of estimating the size of the omitted terms  $\leftrightarrow$  the projection of higher Green's functions on the lower ones is small.

# Non-perturbative QCD: Dynamical generation of quark and gluon masses

## ☞ Dressed-quark propagator in Landau gauge:

$$S^{-1}(p) = Z_2(i\gamma \cdot p + m) + \Sigma(p) = \left( \frac{Z(p^2)}{i\gamma \cdot p + \mathbf{M}(p^2)} \right)^{-1}$$

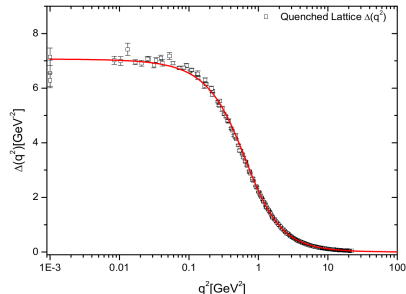
- Mass generated from the interaction of quarks with the gluon-medium.
- Light quarks acquire a **HUGE** constituent mass.
- Responsible of the 98% of proton's mass, the large splitting between parity partners, . . .



## ☞ Dressed-gluon propagator in Landau gauge:

$$i\Delta_{\mu\nu} = -iP_{\mu\nu}\Delta(q^2), \quad P_{\mu\nu} = g_{\mu\nu} - q_\mu q_\nu / q^2$$

- An inflexion point at  $p^2 > 0$ .
- Breaks the axiom of reflexion positivity.
- Gluon mass generation  $\leftrightarrow$  Schwinger mechanism.



# Non-perturbative QCD: Ghost saturation and three-gluon-vertex suppression

## ☞ Dressed-ghost propagator in Landau gauge:

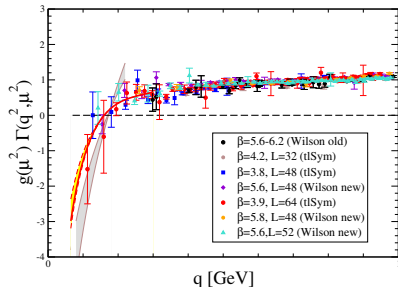
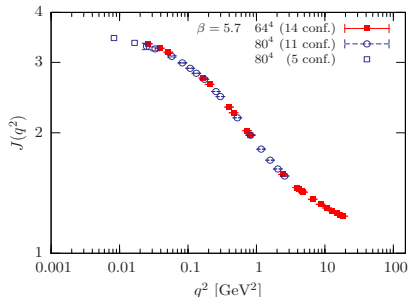
$$G^{ab}(q^2) = \delta^{ab} \frac{J(q^2)}{q^2}$$

- No power-like singular behavior at  $q^2 \rightarrow 0$ .
- Good indication that  $J(q^2)$  reaches a plateau.
- Saturation of ghost's dressing function.

## ☞ Three-gluon vertex form factor in Landau gauge: ( $\propto$ the tree-level tensor structure)

$$\Gamma_{T,R}^{\text{asym}}(q^2) \xrightarrow{q^2 \rightarrow 0} F(0) \left[ \frac{\partial}{\partial q^2} \Delta_R^{-1}(q^2) - C_1(r^2) \right]$$

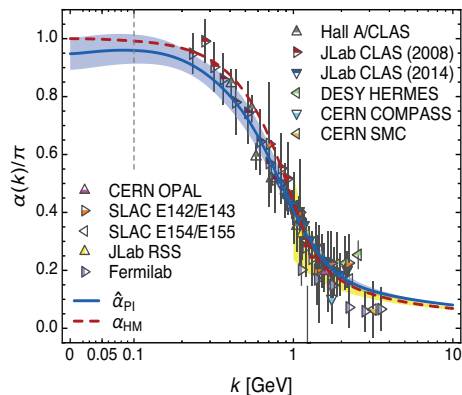
- Appearance of (longitudinally coupled) massless poles.
- Suppression of the form factor in the so-called asymmetric momentum configuration.
- Plausible zero-crossing.



# Non-perturbative QCD: Saturation at IR of process-independent effective-charge

D. Binosi *et al.*, Phys. Rev. D96 (2017) 054026.

A. Deur *et al.*, Prog. Part. Nucl. Phys. 90 (2016) 1-74.



⚡ Perturbative regime:

$$\alpha_{g1}(k^2) = \alpha_{\overline{\text{MS}}}(k^2) \left[ 1 + 1.14\alpha_{\overline{\text{MS}}}(k^2) + \dots \right]$$

$$\hat{\alpha}_{\text{PI}}(k^2) = \alpha_{\overline{\text{MS}}}(k^2) \left[ 1 + 1.09\alpha_{\overline{\text{MS}}}(k^2) + \dots \right]$$

⚡ Data = running coupling defined from the Bjorken sum-rule.

$$\int_0^1 dx \left[ g_1^p(x, k^2) - g_1^n(x, k^2) \right] = \frac{g_A}{6} \left[ 1 - \frac{1}{\pi} \alpha_{g1}(k^2) \right]$$

⚡ Curve determined from combined continuum and lattice analysis of QCD's gauge sector (massless ghost and massive gluon).

⚡ The curve is a running coupling that does NOT depend on the choice of observable.

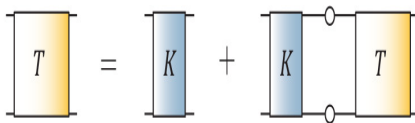
- No parameters.
- No matching condition.
- No extrapolation.

⚡ It predicts and unifies an enormous body of empirical data via the matter-sector bound-state equations.

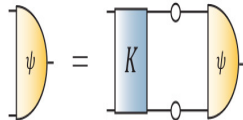
# The bound-state problem in quantum field theory

*Extraction of hadron properties from poles in  $q\bar{q}$ ,  $qqq$ ,  $qq\bar{q}\bar{q}$ ... scattering matrices*

Use **scattering equation** (inhomogeneous BSE) to obtain  $T$  in the first place:  $T = K + KG_0 T$

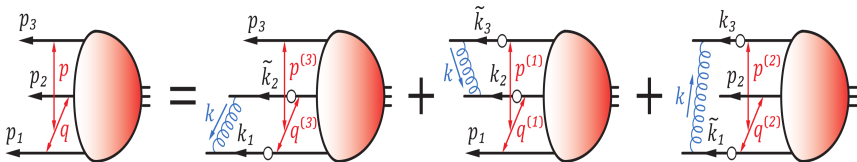


Homogeneous BSE for **BS amplitude**:



🔍 **Baryons.** A 3-body bound state problem in quantum field theory:

Faddeev equation in rainbow-ladder truncation



**Faddeev equation:** Sums all possible quantum field theoretical exchanges and interactions that can take place between the three dressed-quarks that define its valence quark content.

non-relativistic

Mesons:  $P = (-1)^{L+1}$

S	L	$J^{PC}$
0	0	$0^{-+}$
1	0	$1^{--}$
0	1	$1^{+-}$
1	1	$0^{++}$



relativistic

~~$$P = (-1)^{L+1}$$~~

Bethe, Salpeter, Llewellyn-Smith 1950ies

$$\Gamma_\pi(P, p) = \gamma_5 \left[ F_1(P, p) \quad \text{s-wave} \right. \\ \left. + F_2(P, p) i \not{P} \right. \\ \left. + F_3(P, p) p \not{P} i \not{p} \quad \text{p-wave} \right. \\ \left. + F_4(P, p) [\not{p}, \not{P}] \right]$$

Baryons:  $P = (-1)^L$

S	L	$J^P$
1/2	0	$1/2^+$
3/2	2	

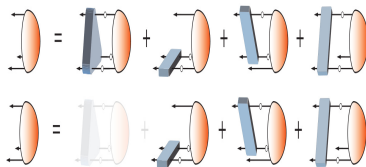
~~$$P = (-1)^L$$~~

$J^P$	total				
		s-wave	p-wave	d-wave	f-wave
$1/2^+$	64	8	36	20	
$3/2^+$	128	4	36	60	28

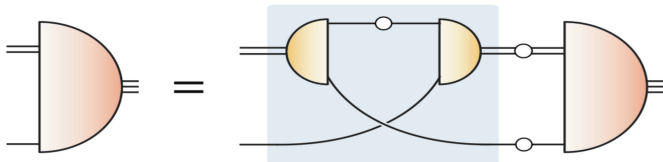
*The attractive nature of quark-antiquark correlations in a colour-singlet meson is also attractive for  $\bar{3}_c$  quark-quark correlations within a colour-singlet baryon*

## 👉 Diquark correlations:

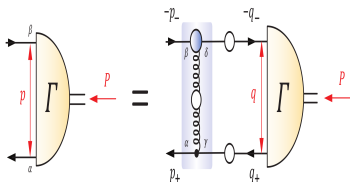
- A tractable truncation of the Faddeev equation.
- In  $N_c = 2$  QCD: diquarks can form colour singlets and are the baryons of the theory.
- In our approach: Non-pointlike colour-antitriplet and fully interacting.



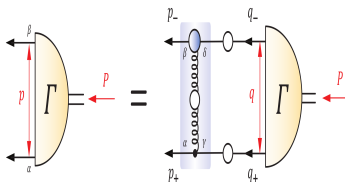
## Diquark-quark approximation:



Meson BSE



Diquark BSE



☞ Owing to properties of charge-conjugation, a diquark with spin-parity  $J^P$  may be viewed as a partner to the analogous  $J^{-P}$  meson:

$$\Gamma_{q\bar{q}}(p; P) = - \int \frac{d^4 q}{(2\pi)^4} g^2 D_{\mu\nu}(p-q) \frac{\lambda^a}{2} \gamma_\mu S(q+P) \Gamma_{q\bar{q}}(q; P) S(q) \frac{\lambda^a}{2} \gamma_\nu$$

$$\Gamma_{qq}(p; P) C^\dagger = - \frac{1}{2} \int \frac{d^4 q}{(2\pi)^4} g^2 D_{\mu\nu}(p-q) \frac{\lambda^a}{2} \gamma_\mu S(q+P) \Gamma_{qq}(q; P) C^\dagger S(q) \frac{\lambda^a}{2} \gamma_\nu$$

☞ Whilst no pole-mass exists, the following mass-scales express the strength and range of the correlation:

$$m_{[ud]_{0+}} = 0.7 - 0.8 \text{ GeV}, \quad m_{\{uu\}_{1+}} = 0.9 - 1.1 \text{ GeV}, \quad m_{\{dd\}_{1+}} = m_{\{ud\}_{1+}} = m_{\{uu\}_{1+}}$$

☞ Diquark correlations are soft, they possess an electromagnetic size:

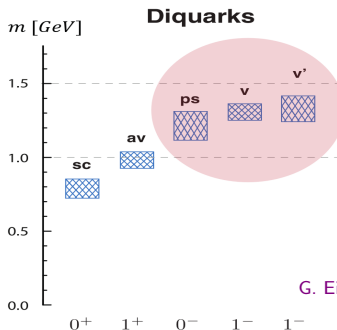
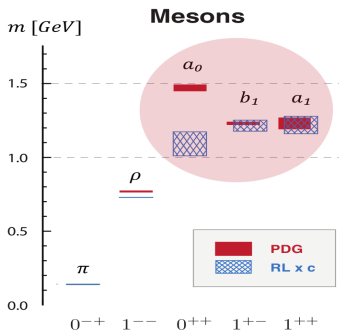
$$r_{[ud]_{0+}} \gtrsim r_\pi, \quad r_{\{uu\}_{1+}} \gtrsim r_\rho, \quad r_{\{uu\}_{1+}} > r_{[ud]_{0+}}$$

## Octet and decuplet baryons

	[nn]	{nn}	[ns]	{ns}	{ss}
$N$	●	●			
$\Delta$		●			
$\Lambda$	●		●	●	
$\Sigma$		●	●	●	
$\Xi$			●	●	●
$\Omega$					●

## Other baryons as parity partners

- ☞  $[I = 0, J^P = 0^+]$ : Isoscalar-scalar.
- ☞  $[I = 1, J^P = 1^+]$ : Isovector-pseudovector.
- ☞  $[I = 0, J^P = 0^-]$ : Isoscalar-pseudoscalar.
- ☞  $[I = 0, J^P = 1^-]$ : Isoscalar-vector.
- ☞  $[I = 1, J^P = 1^-]$ : Isovector-vector.



G. Eichmann et al.

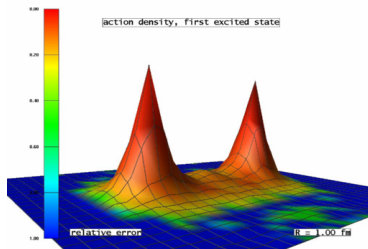
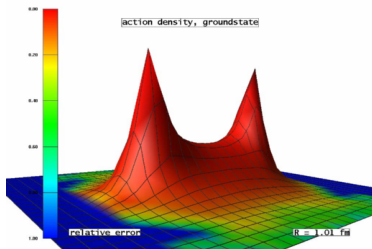
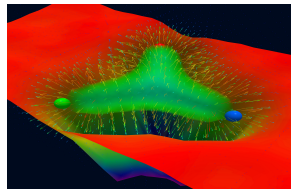
# Remark about the 3-gluon vertex

☞ A Y-junction flux-tube picture of nucleon structure is produced in **quenched** lattice QCD simulations that use **static sources** to represent the proton's valence-quarks.

*F. Bissey et al. PRD 76 (2007) 114512.*

☞ This might be viewed as originating in the 3-gluon vertex which signals the non-Abelian character of QCD.

☞ These suggest a key role for the three-gluon vertex in nucleon structure if they were equally valid in real-world QCD: **finite quark masses and light dynamical/sea quarks.**

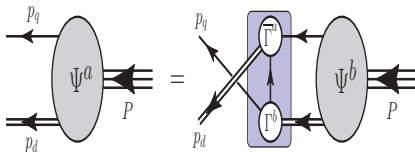


*G.S. Bali, PRD 71 (2005) 114513.*

*The dominant effect of non-Abelian multi-gluon vertices is expressed in the formation of diquark correlations through Dynamical Chiral Symmetry Breaking.*

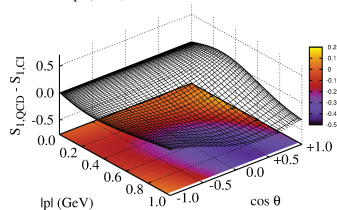
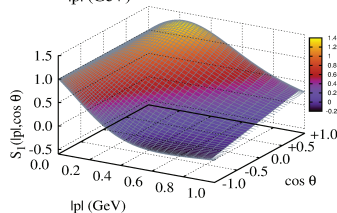
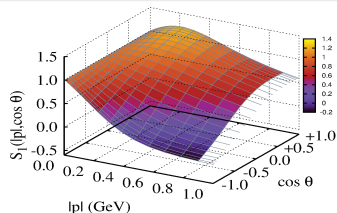
# The quark+diquark structure of the nucleon

## Faddeev equation in the quark-diquark picture



Dominant piece in nucleon's eight-component Poincaré-covariant Faddeev amplitude:  $s_1(|p|, \cos \theta)$

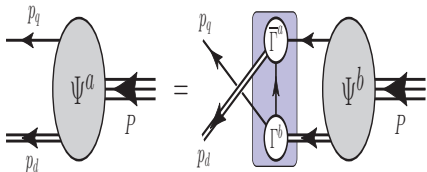
- There is strong variation with respect to both arguments in the quark+scalar-diquark relative momentum correlation.
- Support is concentrated in the forward direction,  $\cos \theta > 0$ . Alignment of  $p$  and  $P$  is favoured.
- Amplitude peaks at  $(|p| \sim M_N/6, \cos \theta = 1)$ , whereat  $p_q \sim p_d \sim P/2$  and hence the *natural* relative momentum is zero.
- In the anti-parallel direction,  $\cos \theta < 0$ , support is concentrated at  $|p| = 0$ , i.e.  $p_q \sim P/3$ ,  $p_d \sim 2P/3$ .



# The quark+diquark structure of any baryon

A baryon can be viewed as a **Borromean bound-state**, the binding within which has two contributions:

- Formation of tight diquark correlations.
- Quark exchange depicted in the shaded area.



The exchange ensures that diquark correlations within the baryon are **fully dynamical**: no quark holds a special place.

The rearrangement of the quarks guarantees that the baryon's wave function complies with **Pauli statistics**.

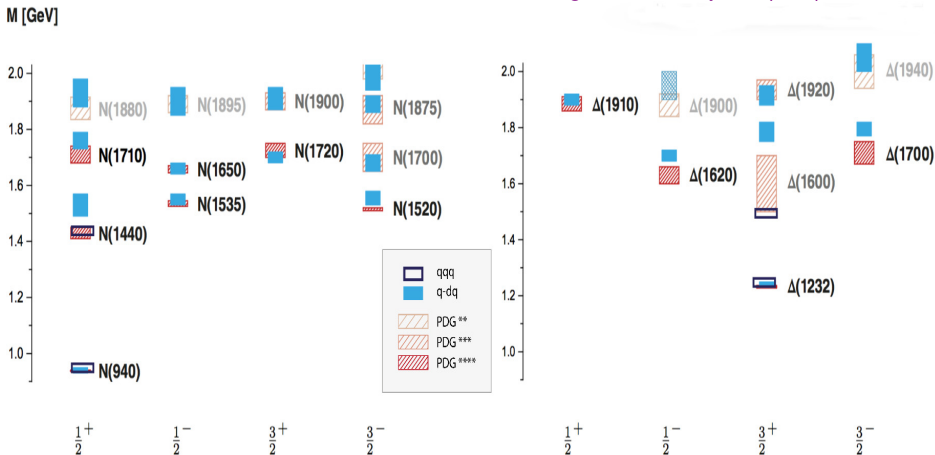
Modern diquarks are **different from the old static, point-like diquarks** which featured in early attempts to explain the so-called missing resonance problem.

The number of states in the **spectrum of baryons obtained is similar** to that found in the three-constituent quark model, just as it is in today's LQCD calculations.

Modern diquarks enforce certain **distinct interaction patterns** for the singly- and doubly-represented valence-quarks within the baryon.

# Three-quark cf. quark-diquark

G. Eichmann *et al.*, Phys. Rev. D94 (2016) 094033;  
 Few Body Syst. 58 (2017) 81;  
 Prog. Part. Nucl.Phys. 91 (2016) 1-100



- ☞ Spectrum in one to one agreement with experiment.
- ☞ Correct level ordering (without coupled-channels effects).
- ☞ Three-body agrees with quark-diquark where applicable.

## One-loop diagrams

## Two-loop diagrams

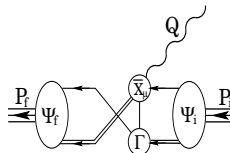
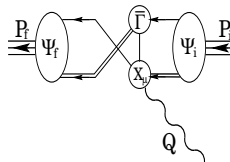
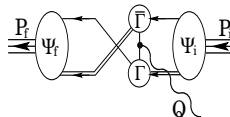
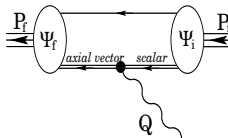
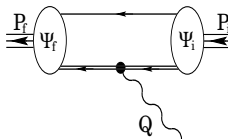
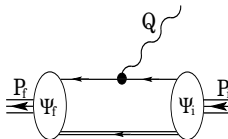
One must specify how the photon couples to baryon's constituents



Six contributions to the current in the quark-diquark picture



- Coupling of the photon to the dressed quark.
- Coupling of the photon to the dressed diquark:
  - ➡ Elastic transition.
  - ➡ Induced transition.
- Exchange and seagull terms.



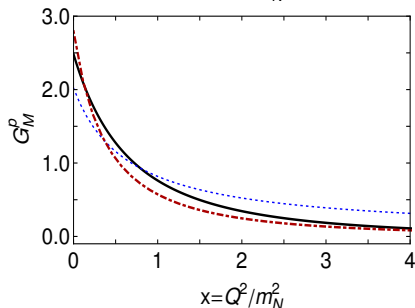
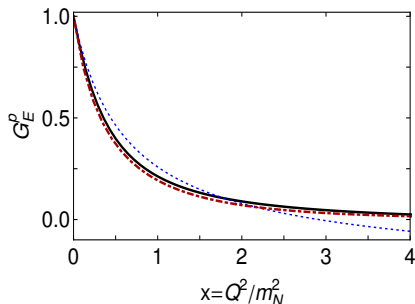
$$\gamma^* N(940)\frac{1}{2}^+ \rightarrow N(940)\frac{1}{2}^+$$

Based on:

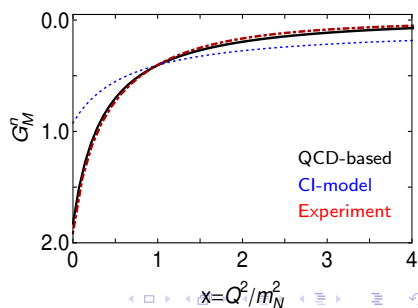
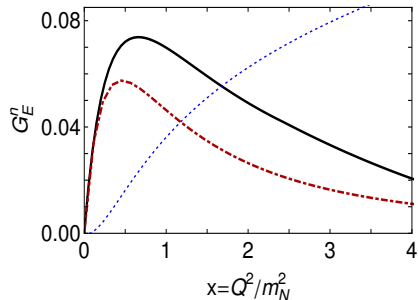
- **PDAs: Revealing correlations within the proton and Roper**  
C. Mezrag, J. Segovia, L. Chang and C.D. Roberts  
Phys. Lett. B783 (2018) 263-267, arXiv:nucl-th/1711.09101
- **Contact-interaction Faddeev equation and, inter alia, proton tensor charges**  
S.-S. Xu, C. Chen, I.C. Cloët, C.D. Roberts, J. Segovia and H.-S. Zong  
Phys. Rev. D92 (2015) 114034, arXiv:nucl-th/1509.03311
- **Understanding the nucleon as a borromean bound-state**  
J. Segovia, C.D. Roberts and S.M. Schmidt  
Phys. Lett. B750 (2015) 100-106, arXiv:nucl-th/1506.05112
- **Nucleon and Delta elastic and transition form factors**  
J. Segovia, I.C. Cloët, C.D. Roberts and S.M. Schmidt  
Few-Body Syst. 55 (2014) 1185-1222, arXiv:nucl-th/1408.2919

# Nucleon's electric and magnetic (Sachs) form factors

Q<sup>2</sup>-dependence of **proton** form factors:

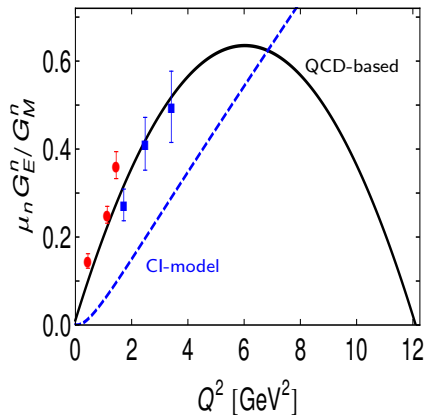
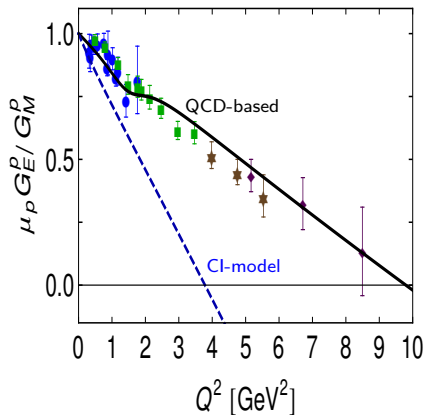


Q<sup>2</sup>-dependence of **neutron** form factors:



# Unit-normalized ratio of Sachs electric and magnetic form factors (I)

*Both CI and QCD-kindred frameworks predict a zero crossing in  $\mu_p G_E^p / G_M^p$*

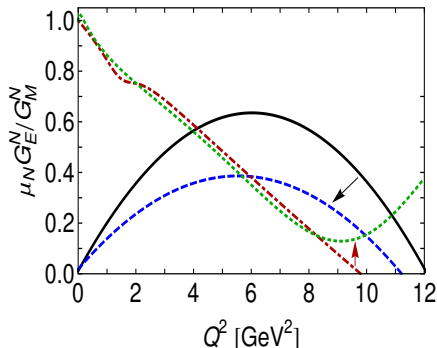
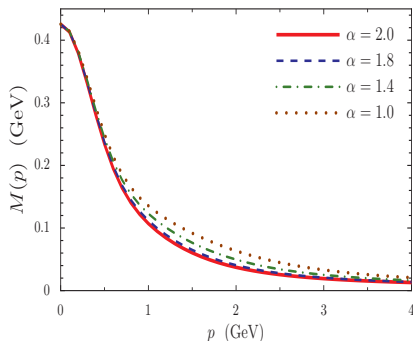


The possible existence and location of the zero in  $\mu_p G_E^p / G_M^p$  is a fairly direct measure of the nature of the quark-quark interaction

# Unit-normalized ratio of Sachs electric and magnetic form factors (II)

I. Cloët *et al.*, Phys.Rev.Lett. 111 (2013) 101803.

J. Segovia *et al.*, Few Body Syst. 55 (2014) 1185-1222.

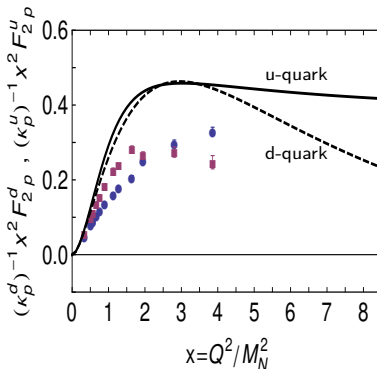
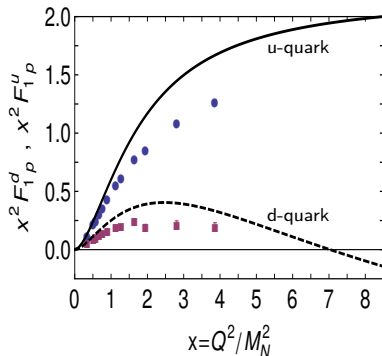


🔍 Black-solid and red-dot-dashed curves:

⇒ Unit-normalized ratio of Sachs electric and magnetic form factors of the neutron and proton, respectively.

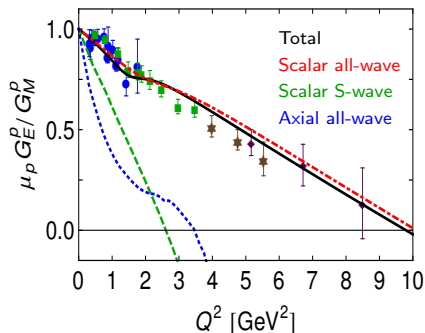
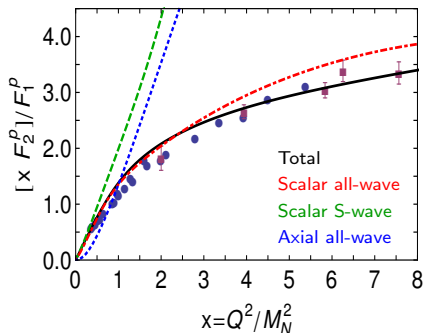
🔍 Blue-dashed and green-dotted curves:

⇒ The same but using a momentum-dependent quark dressing with an accelerated rate of transition from dressed-quark → parton.



## Observations:

- $F_{1p}^d$  is suppressed with respect  $F_{1p}^u$  in the whole range of momentum transfer.
- The location of the zero in  $F_{1p}^d$  depends on the relative probability of finding  $1^+$  and  $0^+$  diquarks in the proton.
- $F_{2p}^d$  is suppressed with respect  $F_{2p}^u$  but only at large momentum transfer.
- There are contributions playing an important role in  $F_2$ , like the anomalous magnetic moment of dressed-quarks or meson-baryon final-state interactions.



## Observations:

- Axial-vector diquark contribution is not enough in order to explain the proton's electromagnetic ratios.
- Scalar diquark contribution is dominant and responsible of the  $Q^2$ -behaviour of the the proton's electromagnetic ratios.
- Higher quark-diquark orbital angular momentum components of the nucleon are critical in explaining the data.

*The presence of higher orbital angular momentum components in the nucleon is an inescapable consequence of solving a realistic Poincaré-covariant Faddeev equation*

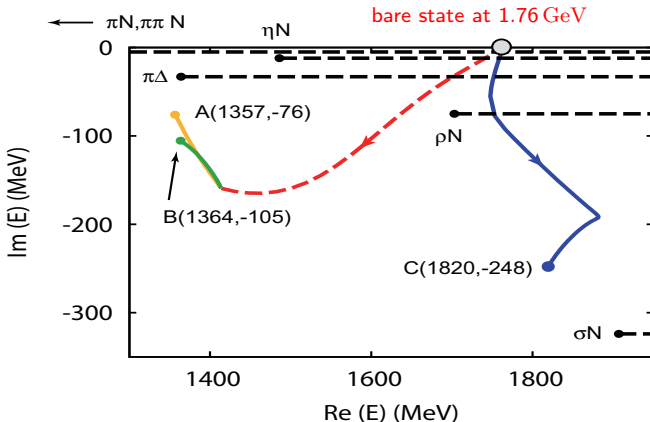
$$\gamma^* N(940)\frac{1}{2}^+ \rightarrow N(1440)\frac{1}{2}^+$$

Based on:

- **Nucleon-to-Roper electromagnetic transition form factors at large  $Q^2$**   
C. Chen, Y. Lu, D. Binosi, C.D. Roberts, J. Rodríguez-Quintero, and J. Segovia  
Phys. Rev. D99 (2019) 034013, arXiv:nucl-th/1811.08440
- **Structure of the nucleon's low-lying excitations**  
C. Chen, B. El-Benich, C.D. Roberts, S.M. Schmidt, J. Segovia and S. Wan  
Phys. Rev. D97 (2018) 034016, arXiv:nucl-th/1711.03142
- **Dissecting nucleon transition electromagnetic form factors**  
J. Segovia and C.D. Roberts  
Phys. Rev. C94 (2016) 042201(R), arXiv:nucl-th/1607.04405
- **Completing the picture of the Roper resonance**  
J. Segovia, B. El-Bennich, E. Rojas, I.C. Cloët, C.D. Roberts, S.-S. Xu and H.-S. Zong  
Phys. Rev. Lett. 115 (2015) 171801, arXiv:nucl-th/1504.04386

# Disentangling the Dynamical Origin of $P_{11}$ Nucleon Resonances

N. Suzuki,<sup>1,2</sup> B. Juliá-Díaz,<sup>3,2</sup> H. Kamano,<sup>2</sup> T.-S. H. Lee,<sup>2,4</sup> A. Matsuyama,<sup>5,2</sup> and T. Sato<sup>1,2</sup>



**The Roper is the proton's first radial excitation. Its unexpectedly low mass arise from a dressed-quark core that is shielded by a meson-cloud which acts to diminish its mass.**

# Nucleon's first radial excitation in DSEs

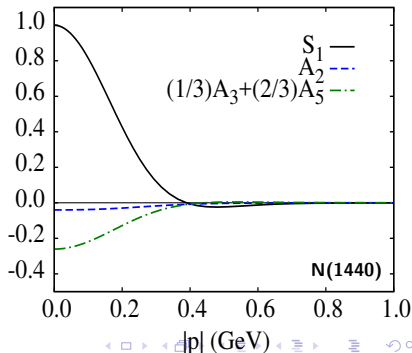
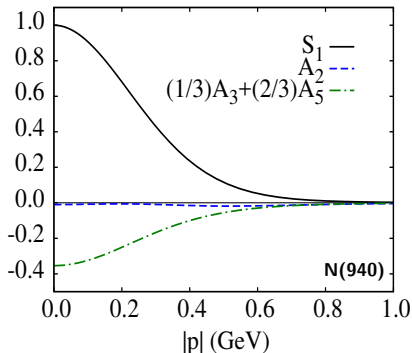
*Bare-states of nucleon resonances correspond to hadron structure calculations which exclude the coupling with the meson-baryon final-state interactions*

$$M_{Roper}^{DSE} = 1.73 \text{ GeV} \quad M_{Roper}^{EBAC} = 1.76 \text{ GeV}$$

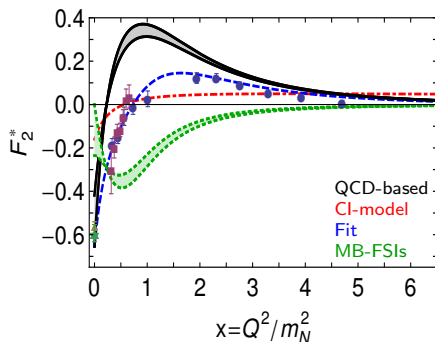
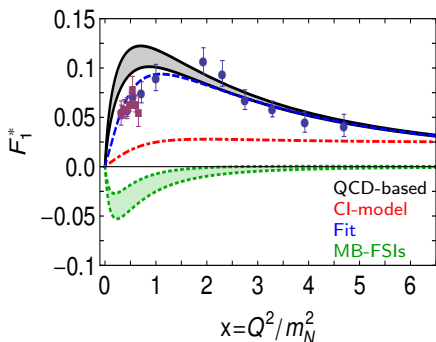
## Observations:

- Meson-Baryon final state interactions reduce dressed-quark core mass by 20%.
- Roper and Nucleon have very similar wave functions and diquark content.
- A single zero in S-wave components of the wave function  $\Rightarrow$  A radial excitation.

0th Chebyshev moment of the S-wave components



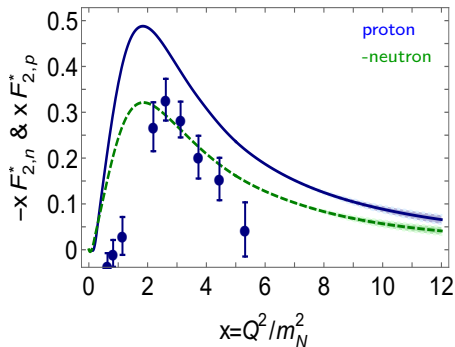
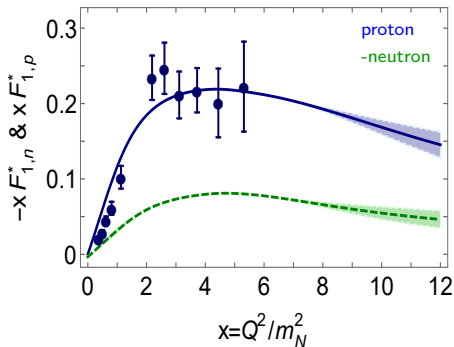
*Nucleon-to-Roper transition form factors at high virtual photon momenta penetrate the meson-cloud and thereby illuminate the dressed-quark core*



## Observations:

- Our calculation agrees quantitatively in magnitude and qualitatively in trend with the data on  $x \gtrsim 2$ .
- The mismatch between our prediction and the data on  $x \lesssim 2$  is due to meson cloud contribution.
- The dotted-green curve is an inferred form of meson cloud contribution from the fit to the data.

CLAS12 detector at JLab will deliver data on the Roper-resonance electroproduction form factors out to  $Q^2 \sim 12m_N^2$  in both the charged and neutral channels



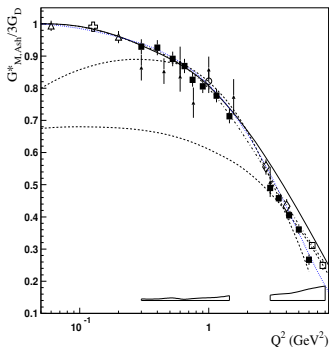
## Observations:

- On the domain depicted, there is no indication of the scaling behavior expected of the transition form factors:  $F_1^* \sim 1/x^2$ ,  $F_2^* \sim 1/x^3$ .
- Since each dressed-quark in the baryons must roughly share the momentum,  $Q$ , we expect that such behaviour will only become evident on  $x \gtrsim 20$ .

$$\gamma^* N(940)\frac{1}{2}^+ \rightarrow \Delta(1232)\frac{3}{2}^+$$

Based on:

- **Dissecting nucleon transition electromagnetic form factors**  
J. Segovia and C.D. Roberts  
Phys. Rev. C94 (2016) 042201(R), arXiv:nucl-th/1607.04405
- **Nucleon and Delta elastic and transition form factors**  
J. Segovia, I.C. Cloët, C.D. Roberts and S.M. Schmidt  
Few-Body Syst. 55 (2014) 1185-1222, arXiv:nucl-th/1408.2919
- **Elastic and transition form factors of the  $\Delta(1232)$**   
J. Segovia, C. Chen, I.C. Cloët, C.D. Roberts, S.M. Schmidt and S. Wan  
Few-Body Syst. 55 (2014) 1-33, arXiv:nucl-th/1308.5225
- **Insights into the  $\gamma^* N \rightarrow \Delta$  transition**  
J. Segovia, C. Chen, C.D. Roberts and S. Wan  
Phys. Rev. C88 (2013) 032201(R), arXiv:nucl-th/1305.0292

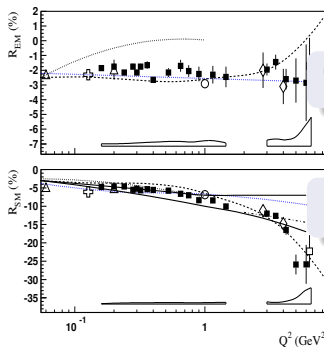


## The $SU(6)$ predictions

(Symmetry considerations of baryon's wave function)

$$\langle p|\mu|\Delta^+ \rangle = \langle n|\mu|\Delta^0 \rangle$$

$$\langle p|\mu|\Delta^+ \rangle = -\sqrt{2} \langle n|\mu|n \rangle$$



The  $R_{EM}$  ratio is measured to be minus a few percent.

The  $R_{SM}$  ratio does not seem to settle to a constant at large  $Q^2$ .

## The CQM predictions

(Without quark orbital angular momentum)

$$R_{EM} = 0$$

$$R_{SM} = 0$$

## The pQCD predictions

(Helicity arguments at very large photon's momenta)

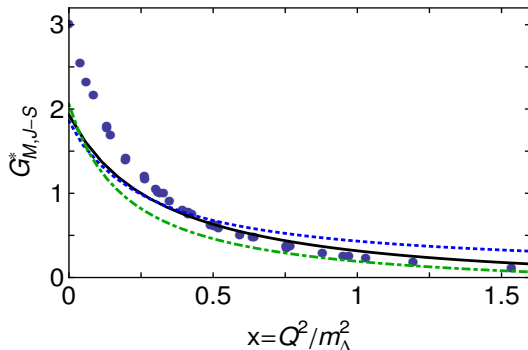
$$G_M^* \rightarrow 1/Q^4$$

$$R_{EM} \rightarrow 1$$

$$R_{SM} \rightarrow \text{constant}$$

Experimental data do not support theoretical predictions

$G_{M,J-S}^*$  cf. *Experimental data and EBAC analysis*



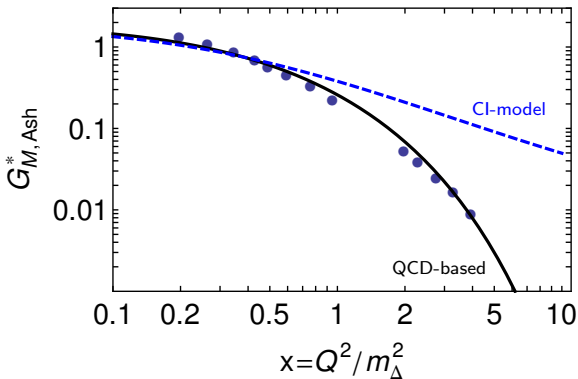
- Solid-black:  
QCD-kindred interaction.
- Dashed-blue:  
Contact interaction.
- Dot-Dashed-green:  
Dynamical + no meson-cloud

## Observations:

- All curves are in marked disagreement at infrared momenta.
- Similarity between Solid-black and Dot-Dashed-green.
- The discrepancy at infrared comes from omission of meson-cloud effects.
- Both curves are consistent with data for  $Q^2 \gtrsim 0.75m_{\Delta}^2 \sim 1.14 \text{ GeV}^2$ .

*Presentations of experimental data typically use the Ash convention*

*–  $G_{M,Ash}^*(Q^2)$  falls faster than a dipole –*



☞ No sound reason to expect:

$$G_{M,Ash}^* / G_M \sim \text{constant}$$

☞ Jones-Scadron must exhibit:

$$G_{M,J-S}^* / G_M \sim \text{constant}$$

☞ Meson-cloud effects

- Up-to 35% for  $Q^2 \lesssim 2.0 m_{\Delta}^2$ .
- Soft  $\rightarrow$  disappear rapidly.

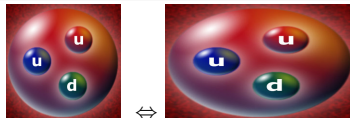
☞  $G_{M,Ash}^*$  vs  $G_{M,J-S}^*$

- A Difference of  $1/\sqrt{Q^2}$ .

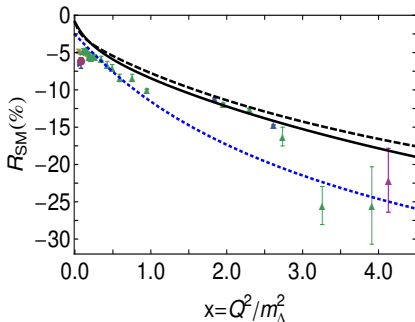
# The electric- and coulomb-quadrupole ratios

☞  $R_{EM} = R_{SM} = 0$  in SU(6)-symmetric CQM.

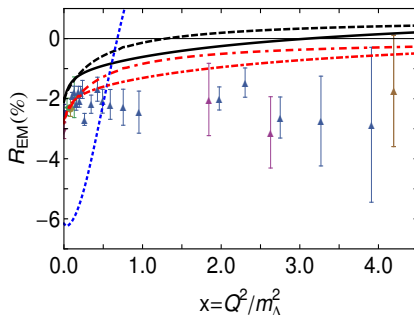
- Deformation of the hadrons involved.
- Modification of the transition current.



☞  $R_{SM}$ : Good description of the rapid fall at large momentum transfer.



☞  $R_{EM}$ : A particularly sensitive measure of orbital angular momentum correlations.



☞ *Zero Crossing in the electric transition form factor:*

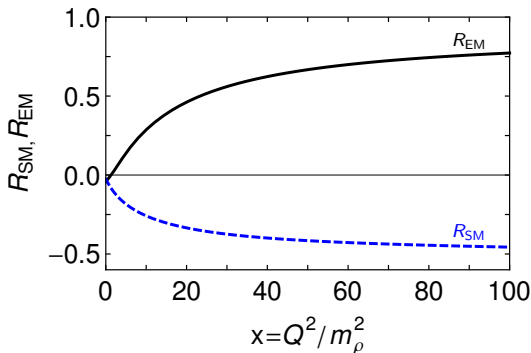
Contact interaction  $\rightarrow Q^2 \sim 0.75m_\Delta^2 \sim 1.14 \text{ GeV}^2$

QCD-kindred interaction  $\rightarrow Q^2 \sim 3.25m_\Delta^2 \sim 4.93 \text{ GeV}^2$

*Helicity conservation arguments in pQCD should apply equally to:*

- *Results obtained within our QCD-kindred framework;*
- *Results produced by a symmetry-preserving treatment of a contact interaction.*

$$R_{EM} \stackrel{Q^2 \rightarrow \infty}{\Rightarrow} 1, \quad R_{SM} \stackrel{Q^2 \rightarrow \infty}{\Rightarrow} \text{constant}.$$



## Observations:

- Truly asymptotic  $Q^2$  is required before predictions are realized.
- $R_{EM} = 0$  at an empirical accessible momentum and then  $R_{EM} \rightarrow 1$ .
- $R_{SM} \rightarrow \text{constant}$ . Curve contains the logarithmic corrections expected in QCD.

$$\gamma^* N(940)\frac{1}{2}^+ \rightarrow \Delta(1600)\frac{3}{2}^+$$

Based on:

- **Transition form factors:  $\gamma + p \rightarrow \Delta(1232), \Delta(1600)$**   
Y. Lu, C. Chen, Z.-F. Cui, C.D. Roberts, S.M. Schmidt, J. Segovia, H.-S. Zong  
Submitted to Phys. Rev. D, [arXiv:nucl-th/1904.03205](#)
- **Spec. and struc. of octet and decuplet and their positive-parity excitations**  
C. Chen, G. Krein, C.D. Roberts, S.M. Schmidt and J. Segovia  
Submitted to Phys. Rev. D, [arXiv:nucl-th/1901.04305](#)
- **Parity partners in the baryon resonance spectrum**  
Y. Lu, C. Chen, C.D. Roberts, J. Segovia, S.-S. Xu and H.-S. Zong  
Phys. Rev. C96 (2017) 015208, [arXiv:nucl-th/1705.03988](#)

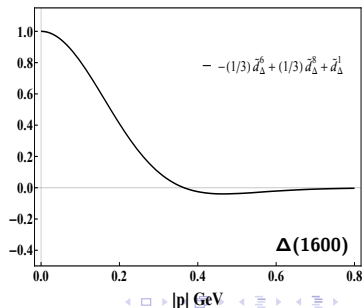
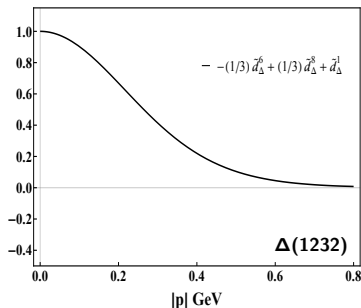
*Bound-state kernels which omit meson-cloud corrections produce masses for hadrons that are larger than the empirical values (in GeV):*

$$\begin{aligned} m_N &= 1.19 \pm 0.13, & m_\Delta &= 1.35 \pm 0.12, \\ m_{N'} &= 1.73 \pm 0.10, & m_{\Delta'} &= 1.79 \pm 0.12. \end{aligned}$$

## Observations:

- Meson-Baryon final state interactions reduce bare mass by 10 – 20%.
- The cloud's impact depends on the state's quantum numbers.
- A single zero in S-wave components of the wave function  $\Rightarrow$  A radial excitation.

0th Chebyshev moment of the S-wave component



# Wave function decomposition: $N(1440)$ cf. $\Delta(1600)$

	$N(940)$	$N(1440)$	$\Delta(1232)$	$\Delta(1600)$
scalar	62%	62%	—	—
pseudovector	29%	29%	100%	100%
mixed	9%	9%	—	—
$S$ -wave	0.76	0.85	0.61	0.30
$P$ -wave	0.23	0.14	0.22	0.15
$D$ -wave	0.01	0.01	0.17	0.52
$F$ -wave	—	—	$\sim 0$	0.02

$N(1440)$

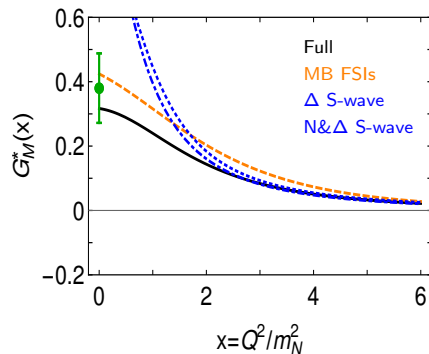
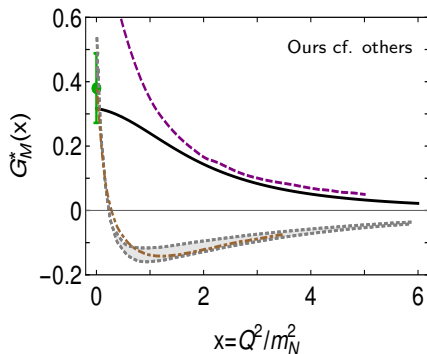
- Roper's diquark content are almost identical to the nucleon's one.
- It has an orbital angular momentum composition which is very similar to the one observed in the nucleon.

$\Delta(1600)$

- $\Delta(1600)$ 's diquark content are almost identical to the  $\Delta(1232)$ 's one.
- It shows a dominant  $\ell = 2$  angular momentum component with its  $S$ -wave term being a factor 2 smaller.

**The presence of all angular momentum components compatible with the baryon's total spin and parity is an inescapable consequence of solving a realistic Poincaré-covariant Faddeev equation**

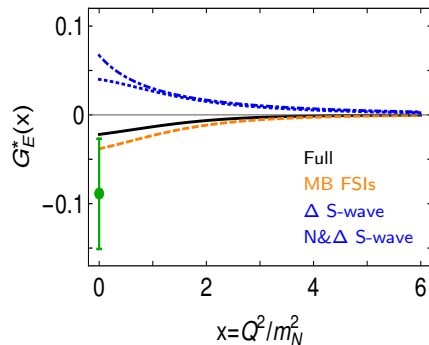
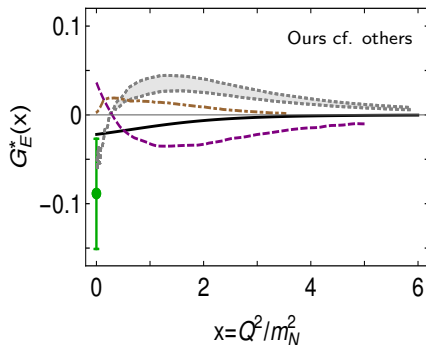
# Transition form factors (I)



## Observations:

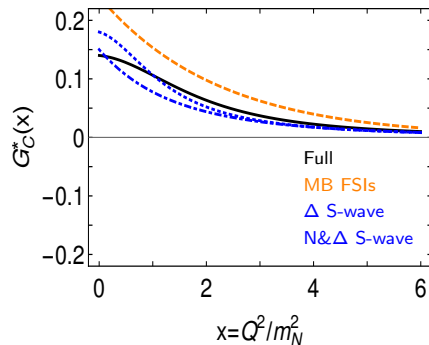
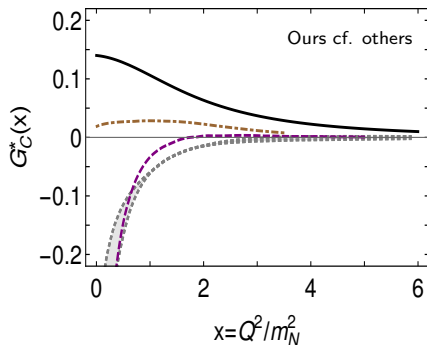
- It is positive defined in the whole range of photon momentum and decreases smoothly with larger  $Q^2$ -values.
- The mismatch with the empirical result are comparable with that in the  $\Delta(1232)$  case, suggesting that MB FSIs are of similar importance in both channels.
- Higher partial-waves have a visible impact on  $G_M^*$ : They bring the magnetic dipole moment to lower values which could be compatible with experiment.

# Transition form factors (II)



## Observations:

- It is negative defined in the whole range of photon momentum and decreases smoothly with larger  $Q^2$ -values.
- The mismatch with the empirical result could be due to meson cloud contributions.
- Higher partial-waves have a visible impact on  $G_E^*$ : They produce a change in sign which is crucial to get agreement with experiment at the real photon point.



## Observations:

- It is positive defined in the whole range of photon momentum and decreases smoothly with larger  $Q^2$ -values.
- Quark model results for all form factors are very sensitive to the wave functions employed for the initial and final states.
- MB FSI's could be important: a factor of two is observed for  $G_C^*$  at the real photon point. Moreover, higher partial-waves have a visible impact on  $G_C^*$ .

*We insist on our purpose of getting an unified study of EM elastic and transition form factors of nucleon resonances using QCD-based kernels and interaction vertices*

## ☞ The $\gamma^*N \rightarrow \text{Nucleon} [\equiv N(940)]$ reaction:

- Proton's and neutron's electromagnetic ratios are sensible observables to disentangle fundamental quantities of QCD.
- The presence of strong diquark correlations within the nucleon is sufficient to understand empirical extractions of the flavor-separated form factors.
- Scalar diquark dominance and the presence of higher orbital angular momentum components are responsible of the  $Q^2$ -behaviour of  $G_E^p/G_M^p$  and  $F_2^p/F_1^p$ .

## ☞ The $\gamma^*N \rightarrow \text{Nucleon}' [\equiv N(1440)]$ reaction:

- The Roper is the proton's first radial excitation. It consists on a dressed-quark core augmented by a meson cloud that reduces its mass by approximately 20%.
- Our calculation agrees quantitatively in magnitude and qualitatively in trend with the data on  $x \gtrsim 2$ . The mismatch on  $x \lesssim 2$  is due to meson-cloud contribution.
- CLAS12@JLab will test our predictions for the charged and neutral channels in a range of momentum transfer larger than  $4.5 \text{ GeV}^2$ .

## ☞ The $\gamma^*N \rightarrow \text{Delta} [\equiv \Delta(1232)]$ reaction:

- $G_{M,J-S}^{*P}$  falls asymptotically at the same rate as  $G_M^P$ . This is compatible with isospin symmetry and pQCD predictions.
- Data do not fall unexpectedly rapid once the kinematic relation between Jones-Scadron and Ash conventions is properly account for.
- Limits of pQCD,  $R_{EM} \rightarrow 1$  and  $R_{SM} \rightarrow \text{constant}$ , are apparent in our calculation but truly asymptotic  $Q^2$  is required before the predictions are realized.

## ☞ The $\gamma^*N \rightarrow \text{Delta}' [\equiv \Delta(1600)]$ reaction:

- $G_M^*$  and  $R_{EM}$  are consistent with the empirical values at the real photon point, but we expect inclusion of MB FSI to improve the agreement on  $Q^2 \sim 0$
- $R_{EM}$  is markedly different for  $\Delta(1600)$  than for  $\Delta(1232)$ , highlighting the sensitivity of  $G_E^*$  to the degree of deformation of the  $\Delta$ -baryons.
- $R_{SM}$  is qualitatively similar for both  $\gamma^*N \rightarrow \Delta(1600)$  and  $\gamma^*N \rightarrow \Delta(1232)$  transitions, still larger (in absolute value) for the  $\Delta(1600)$  case.