

Probing **diquark** degrees of freedom using **hadron** **formation dynamics**

William Brooks
Universidad Técnica Federico Santa María

Outline

A **model** that describes meson production in nDIS

The puzzle of nDIS **baryon** production: the link to **diquarks**

Near-future **prospects** for new baryon-diquark studies

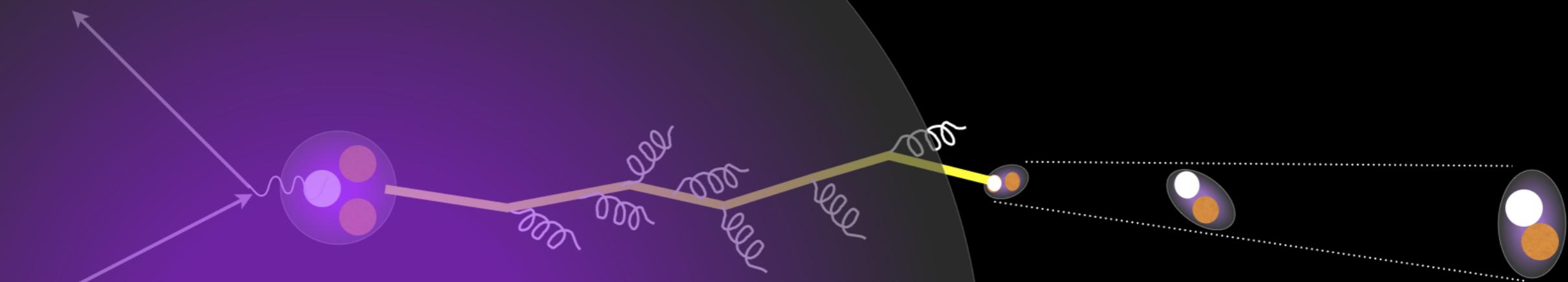
Predictions for future measurements



A model for propagation of **QCD color** through **strongly interacting systems**

The diagram shows a large, semi-transparent grey sphere representing a strongly interacting system. Inside, a yellow path starts from a small red dot on the left and moves towards a larger cluster of four colored dots (red, orange, white, and grey) on the right. The path is composed of several segments connected by wavy lines, representing the propagation of QCD color. Two white arrows point towards the cluster from the right side.

Will Brooks and Jorge López
(UTFSM) (Heidelberg)



About this model

- A **new analysis** of two published HERMES measurements. We isolate the roles of **quark energy loss and pre-hadron formation** in describing the data.
- **Two observables** are analyzed **simultaneously**.
- The primary ingredient is the **well-known density distribution** in nuclei.
- **BDMPS-Z** description needs to be validated by experiment. Important assertions recently challenged: (Zakharov, <https://arxiv.org/abs/1807.09742>).
- These kinds of studies will be important in the **future** at the **Electron Ion Collider**.

Motivations

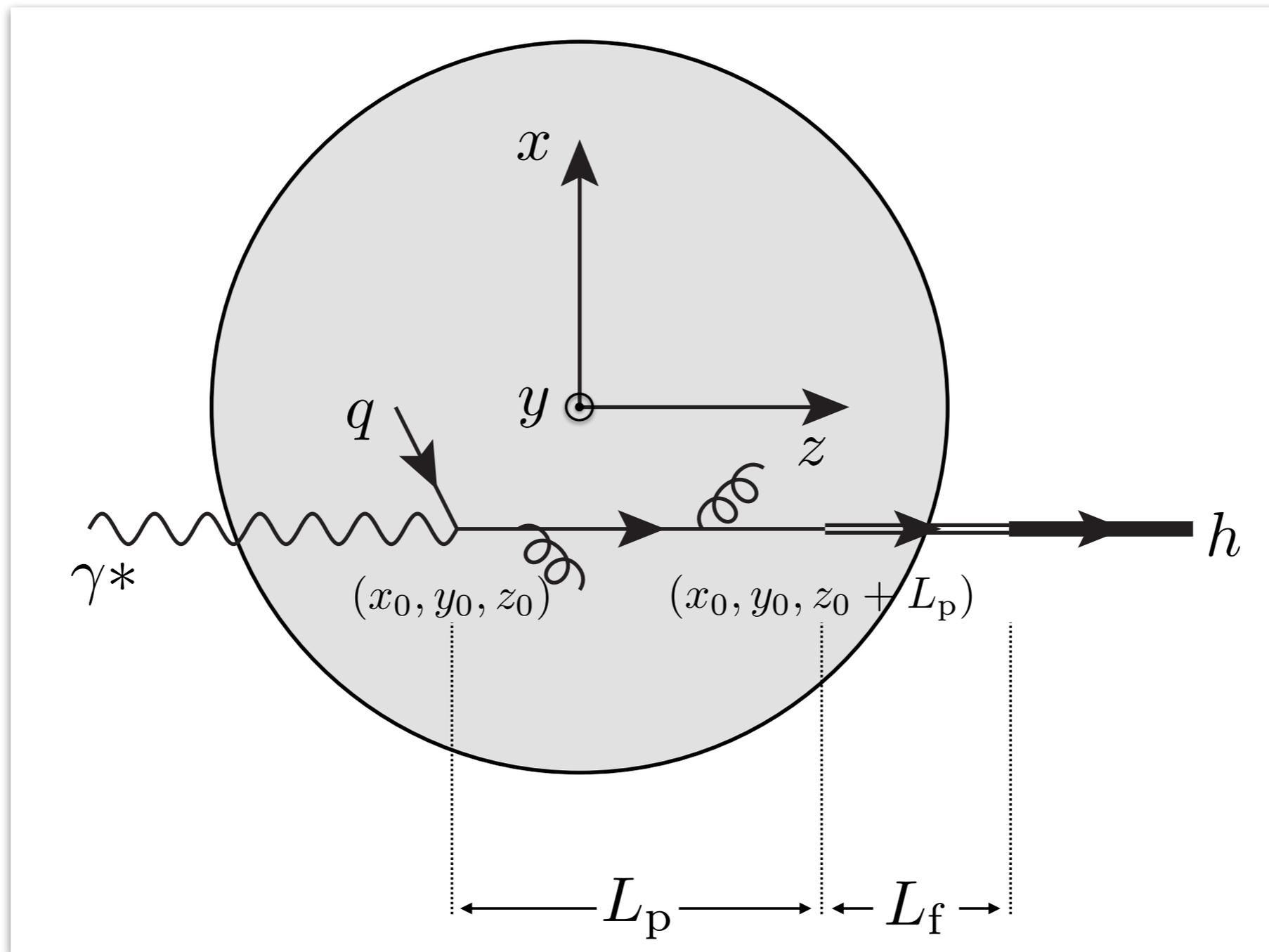
Measure **characteristic lifetimes** for **color propagation** in QCD

Constrain the **functional form** of the **color lifetime** using nuclear medium

Develop **space-time** concepts for **QCD factorization** in ep and eA, possibly pp

Develop **consistent picture** of **quark interactions in nuclei**

Semi-inclusive DIS has unique features for these studies

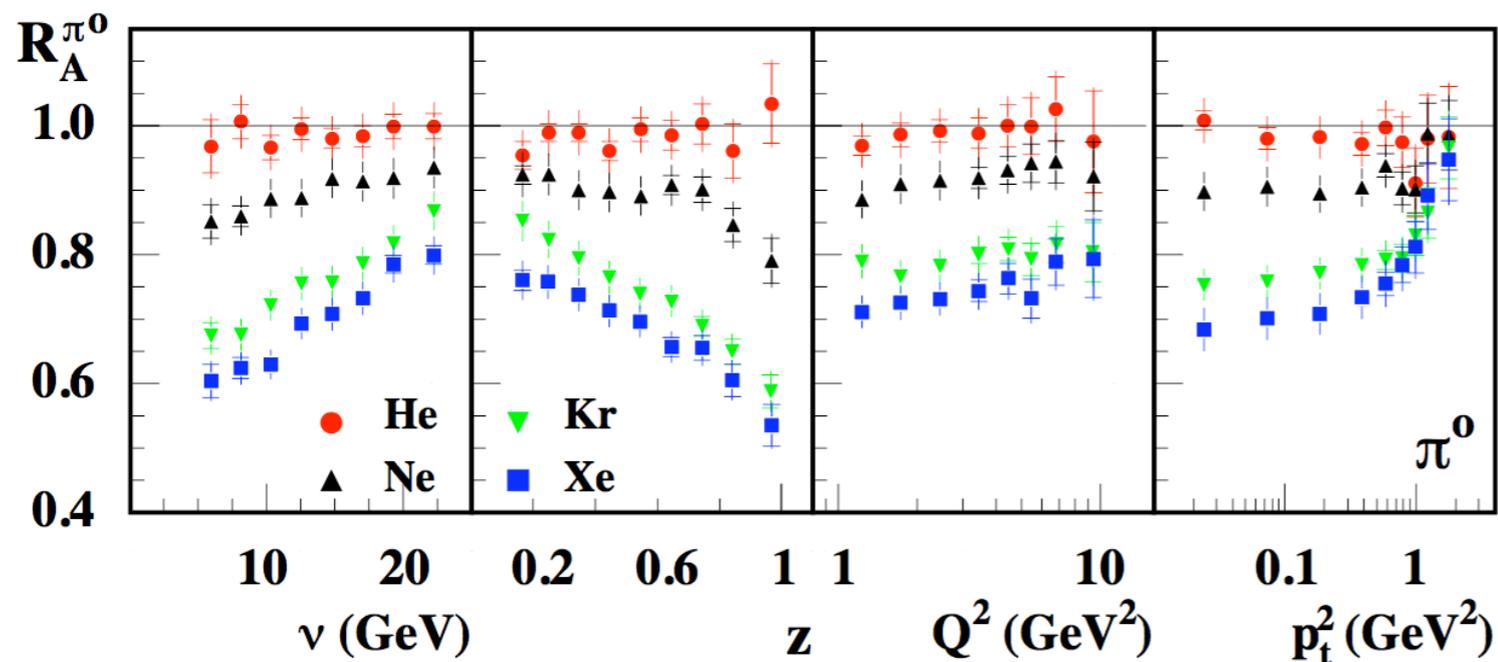
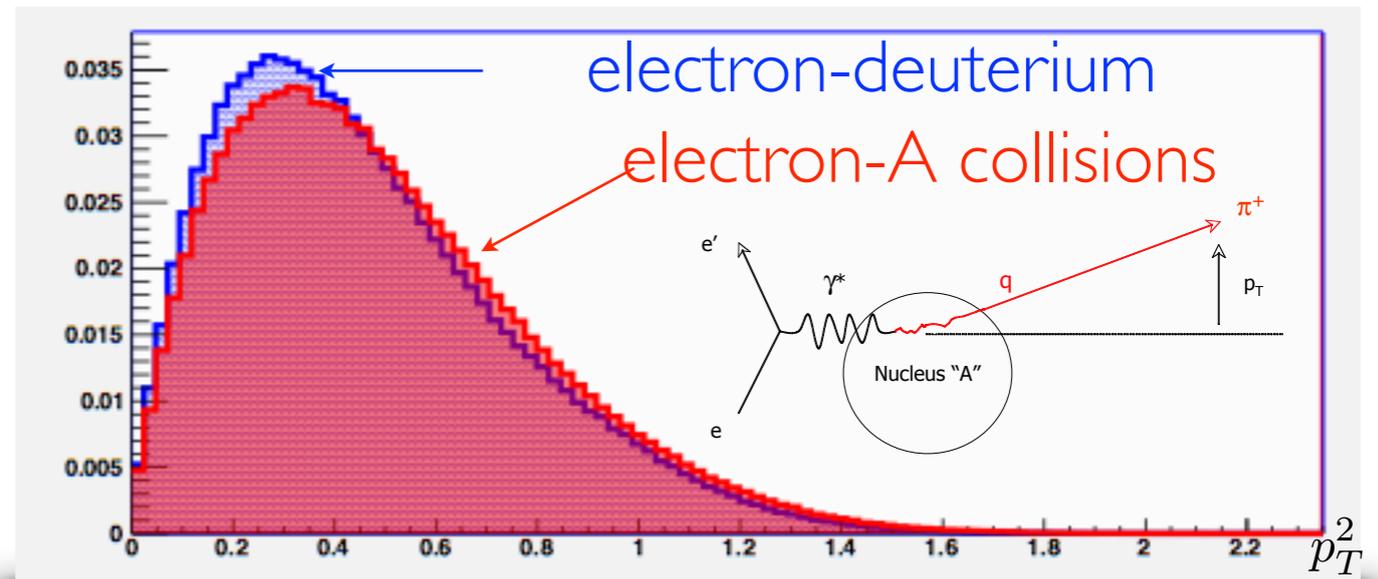


In DIS for $x > 0.1$, we know the **quark initial energy and momentum very precisely**.
There are ~no initial state interactions, only final state interactions.

$$\Delta p_T^2(Q^2, \nu, z_h) \equiv \langle p_T^2(Q^2, \nu, z_h) \rangle |_A - \langle p_T^2(Q^2, \nu, z_h) \rangle |_D$$

Experimental observables

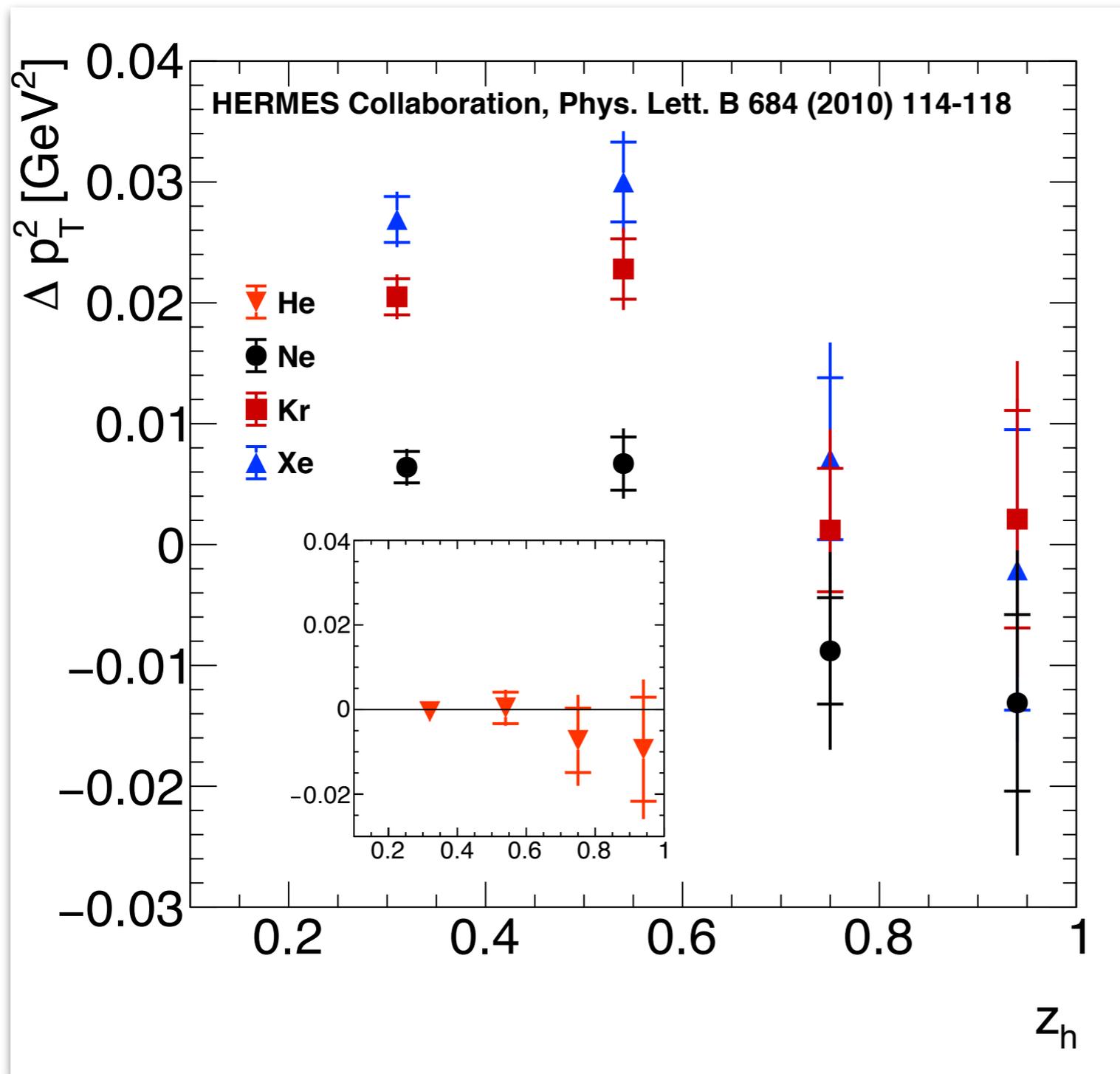
Transverse momentum broadening



Hadronic multiplicity ratio

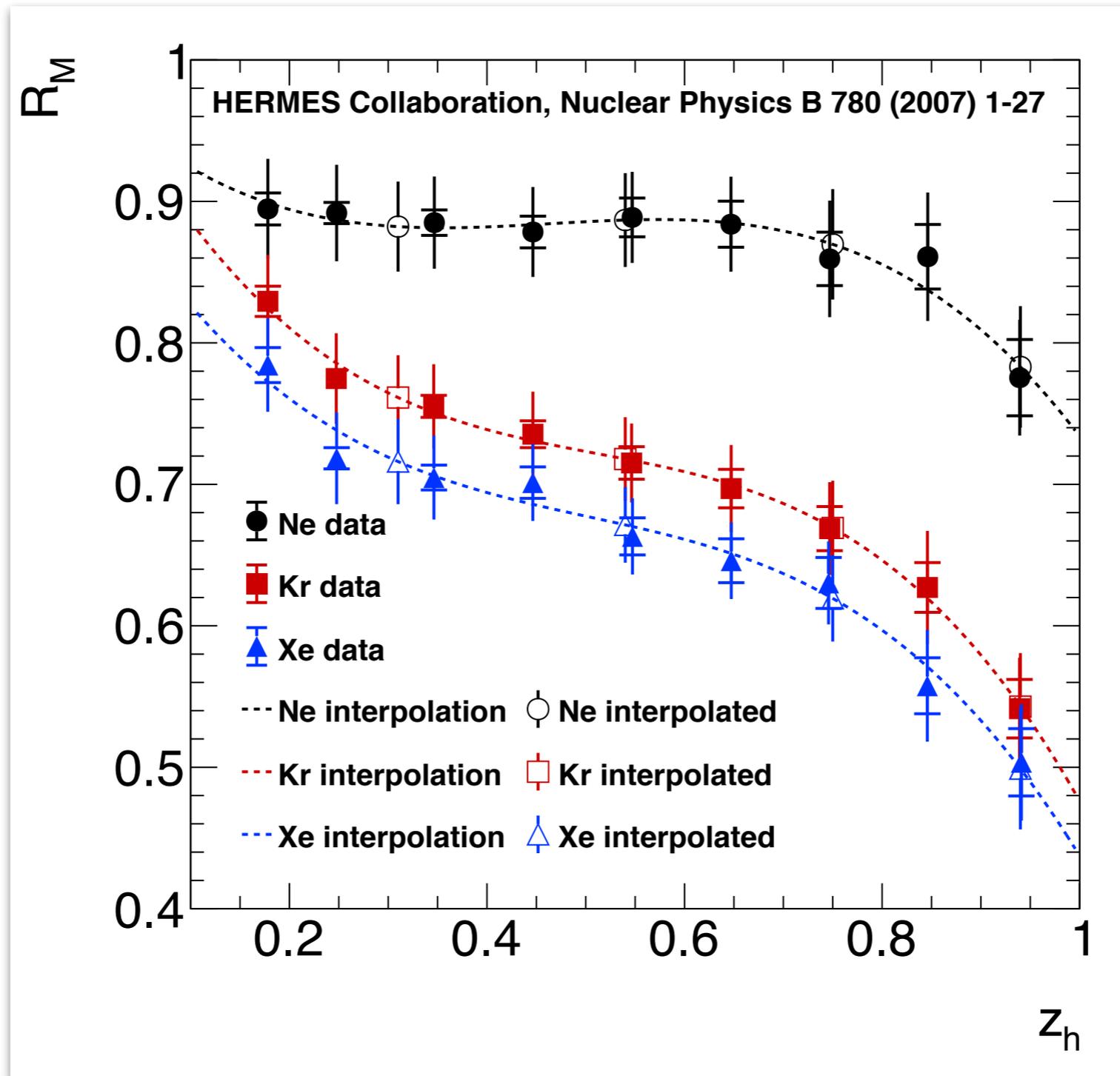
$$R_M^h(Q^2, \nu, z_h, p_T) \equiv \frac{\frac{1}{N_e(Q^2, \nu)} \cdot N_h(Q^2, \nu, z_h, p_T) |_A}{\frac{1}{N_e(Q^2, \nu)} \cdot N_h(Q^2, \nu, z_h, p_T) |_D}$$

Hermes data for p_T broadening vs. $z_h = E/\nu$



Note for later discussion:
maximum is
0.03 GeV^2

Hermes data, hadronic multiplicity ratio vs. $z_h = E/\nu$

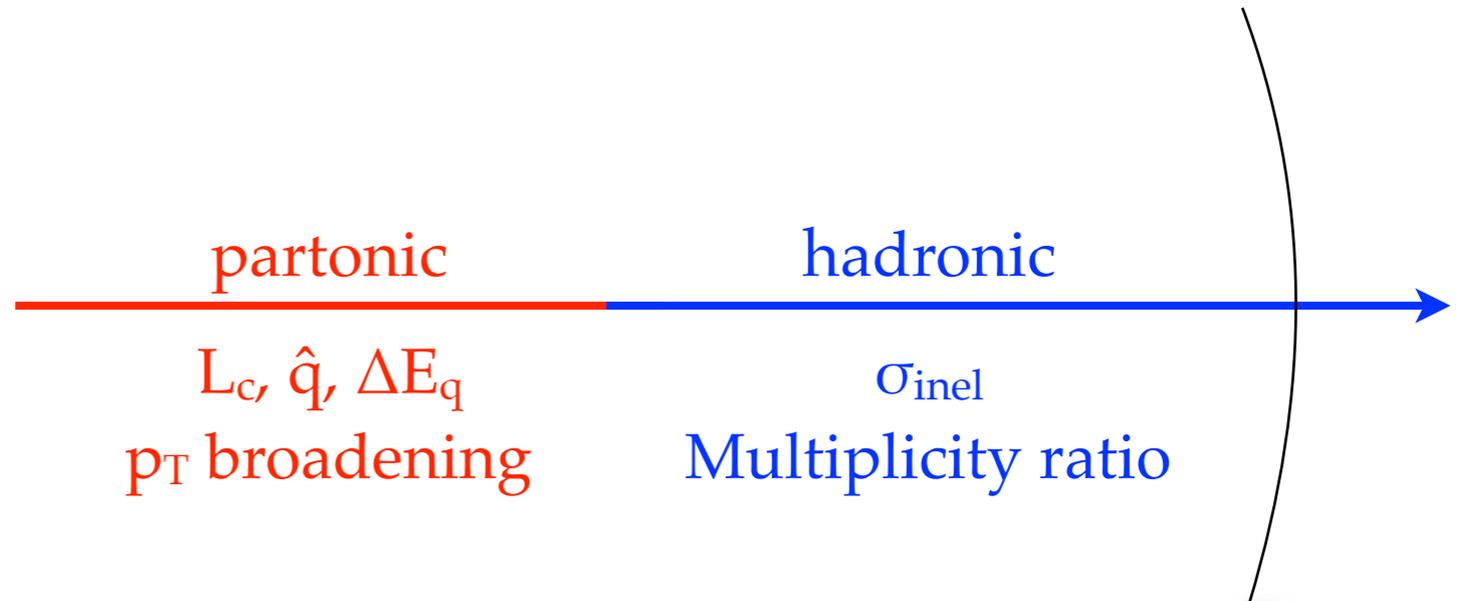


The interpolation is used to match the bins in p_T broadening (in previous slide)

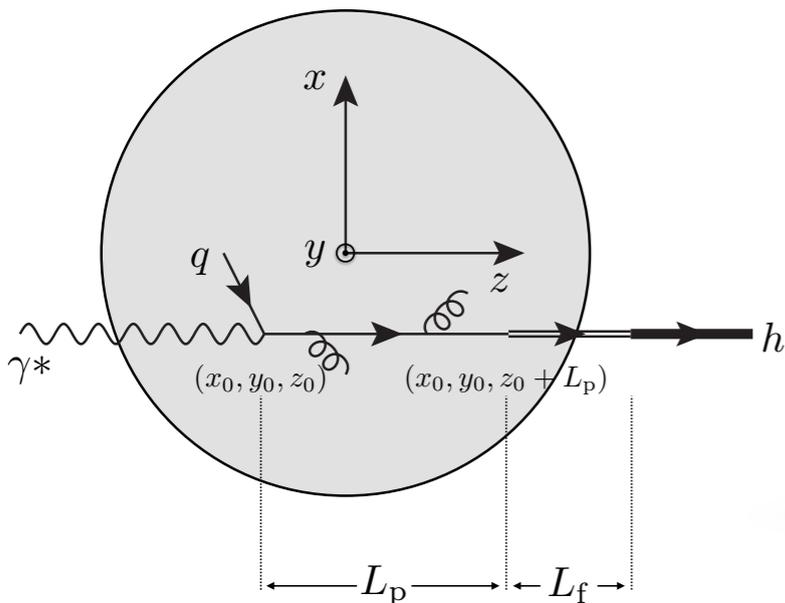
Definition of the model

Division into *partonic* and *hadronic* phases

Path of quark is divided into “*partonic phase*” and “*hadronic phase*”

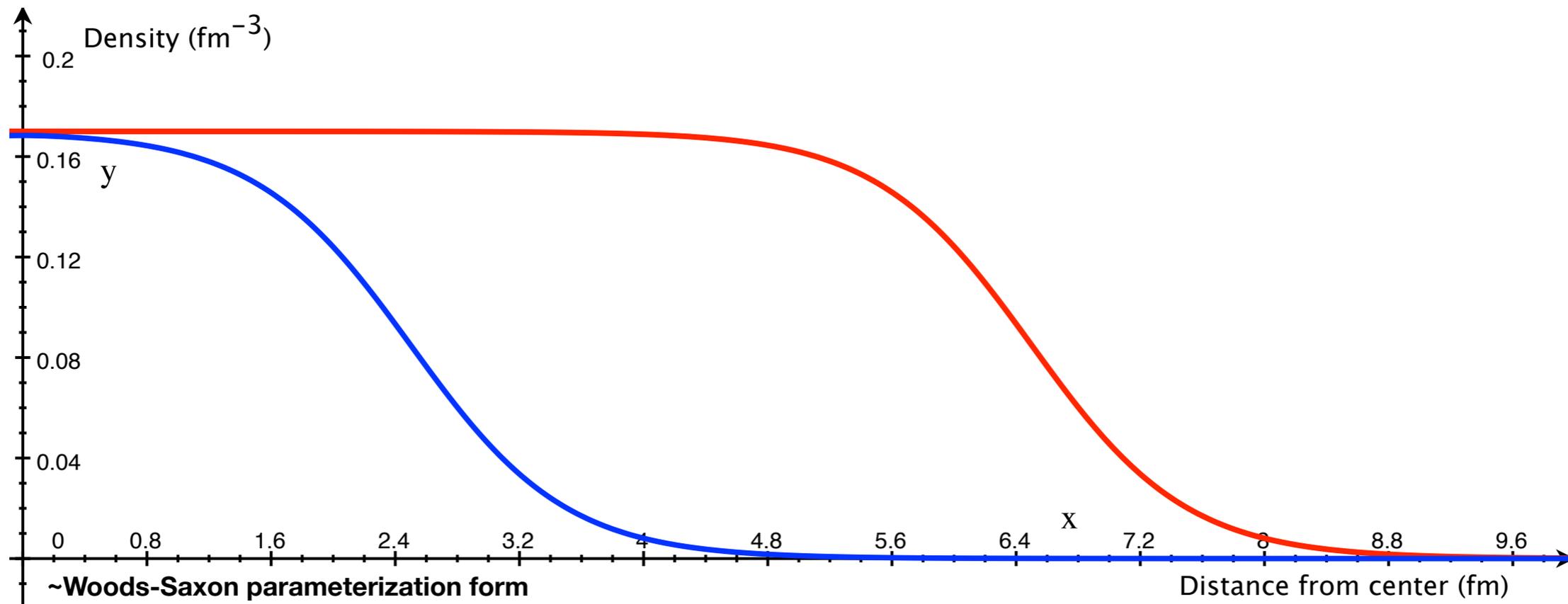


The *partonic phase* persists for a distance L_c , over which p_T broadening via \hat{q} , and partonic energy loss ΔE_q , occur



The *hadronic phase* follows the *partonic phase*, passing through the remainder of the medium, and causing attenuation of hadrons by an *inelastic interaction cross section* σ_{inel}

Density distribution according to H. P. Blok and L. Lapikás,
PHYSICAL REVIEW C 73, 038201 (2006)



Baseline Model Ingredients

p_T broadening is modeled as a line integral over a realistic density in the partonic phase, with 1 unique parameter, averaged over volume and color length L_c

$$\langle \Delta p_T^2 \rangle = \left\langle q_0 \int_{z=z_0}^{z=z_0+L_c^*} \rho(x_0, y_0, z) dz \right\rangle_{x_0, y_0, z_0, L_c}$$

unique parameter

common parameter

Multiplicity ratio is modeled as a line integral over a realistic density in the hadronic phase, with 1 unique parameter, averaged over volume and color length L_c .

$$\langle R_M \rangle = \left\langle \exp\left(-\sigma \int_{z=z_0+L_c}^{z=z_{max}} \rho(x_0, y_0, z) dz\right) \right\rangle_{x_0, y_0, z_0, L_c}$$

unique parameter

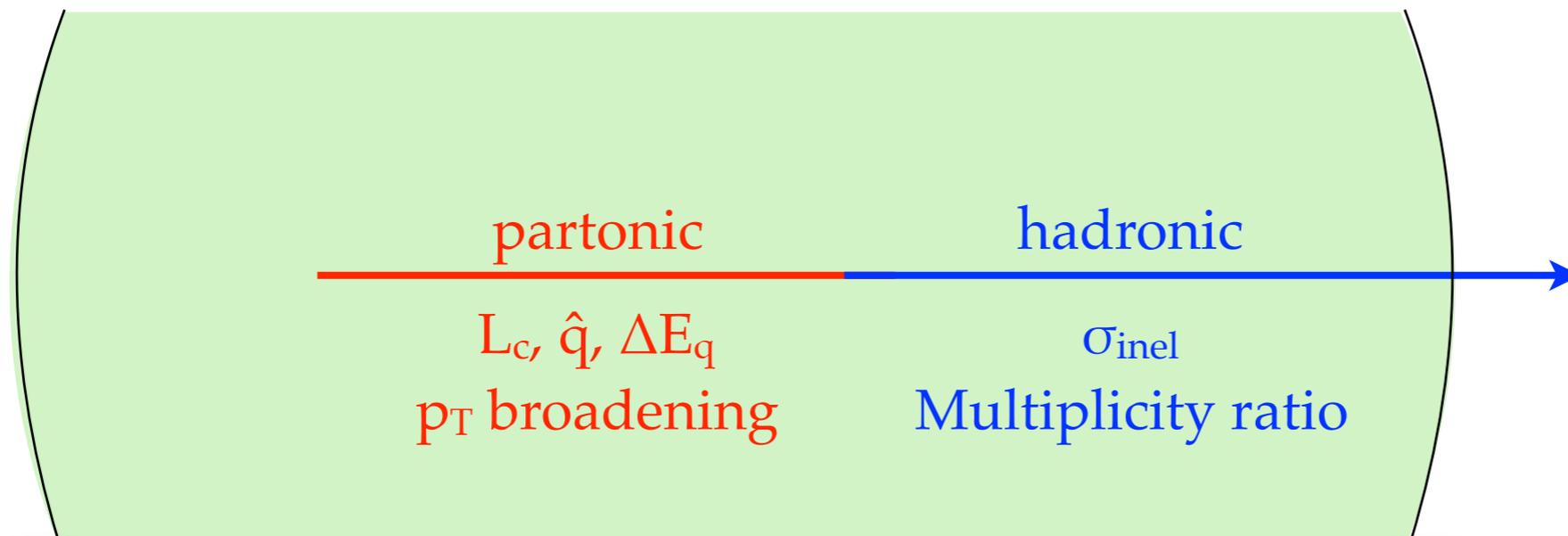
common parameter

Total of 3 parameters in the baseline model. We often fix sigma at 30 or 40 mbarn.

The “common” parameter L_c couples the two observables together.

The coupling of the observables through L_c is the feature of this model that gives it much more discriminating power than the single-observable models used previously.

For example, for fixed q_0 and fixed σ , if L_c is *longer* (**longer partonic phase**) it simultaneously *increases* p_T broadening and *decreases* the multiplicity ratio. The amount of increase and decrease depends on the size of the nucleus and on the size of L_c . Thus the description is highly constrained.



Model Assumptions

- Only **two dynamical processes** are involved - quark energy loss and (pre-)hadron inelastic interactions
- **Straight-line propagation** of the struck quark (soft-gluon assumption)
- **Two stages** of propagation: first, as a color octet system, and second as a color singlet system.
- Non-zero hadron **formation time** (reduced inelastic cross section).
- **Fluctuations** affecting the yield are **neglected** (only average values). Decreasing exponential form for pre-hadron cross section.
- Functional **form** of the color lifetime: either exponential or constant.

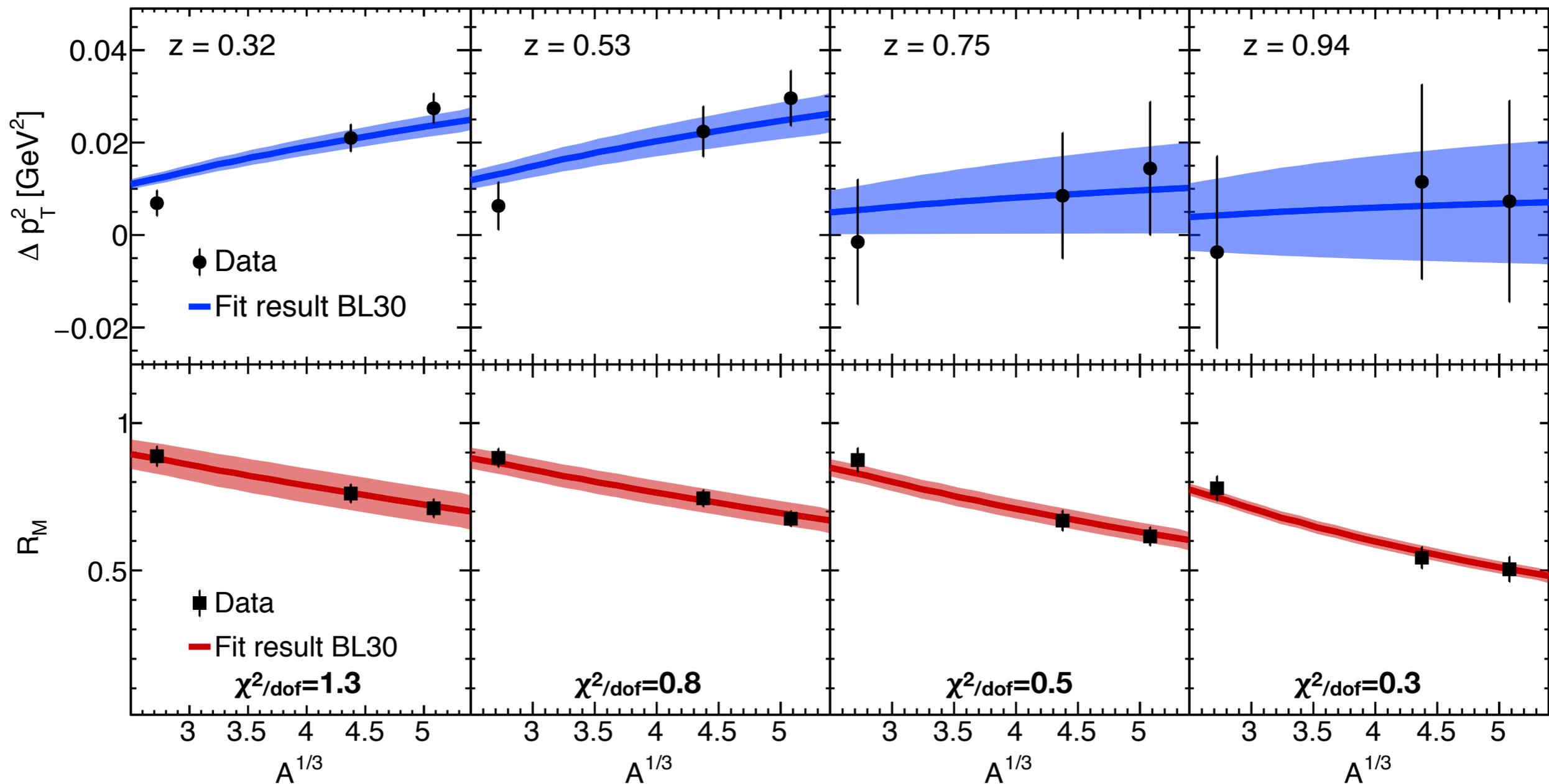
Results of the model fit to two observables from HERMES data

Model fit to HERMES data

Simultaneous fit to 2 observables

3 parameter variant ($q_0, L_c, \sigma_h=30$ mb)

(Baseline model, BL30)

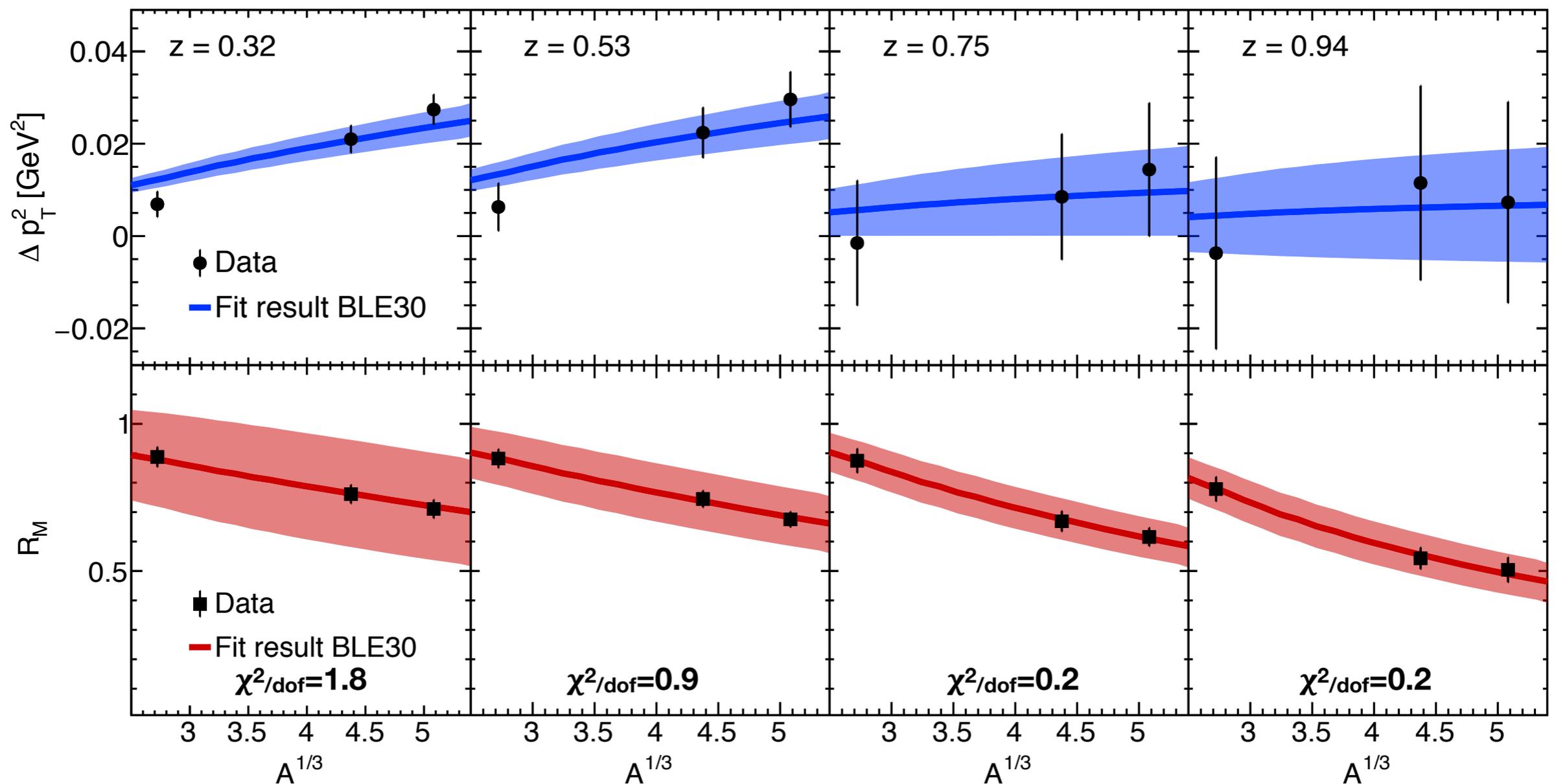


Model fit to HERMES data

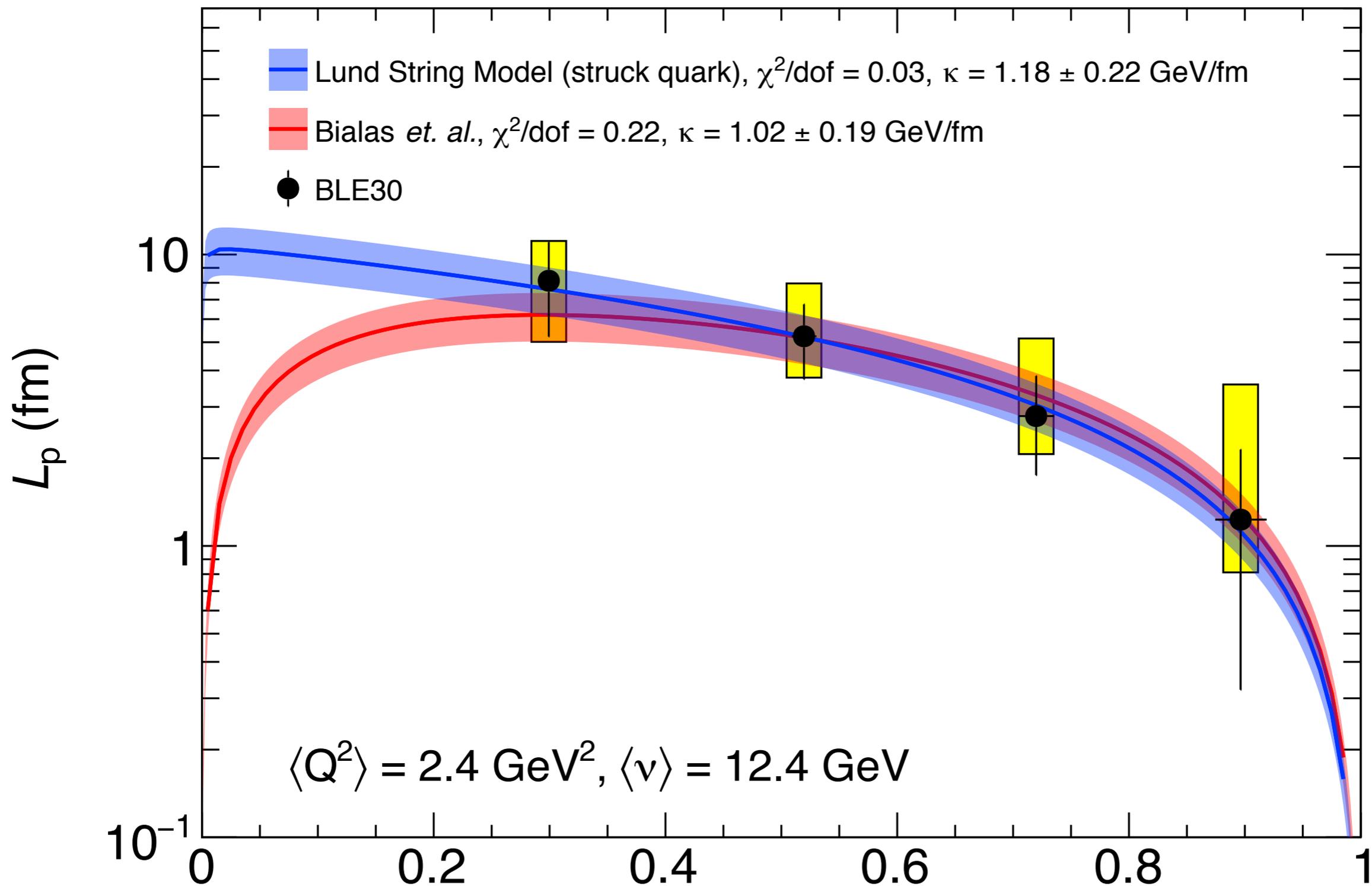
Simultaneous fit to 2 observables

4 parameter variant (q_0 , L_c , ΔE , $\sigma_h=30$ mb)

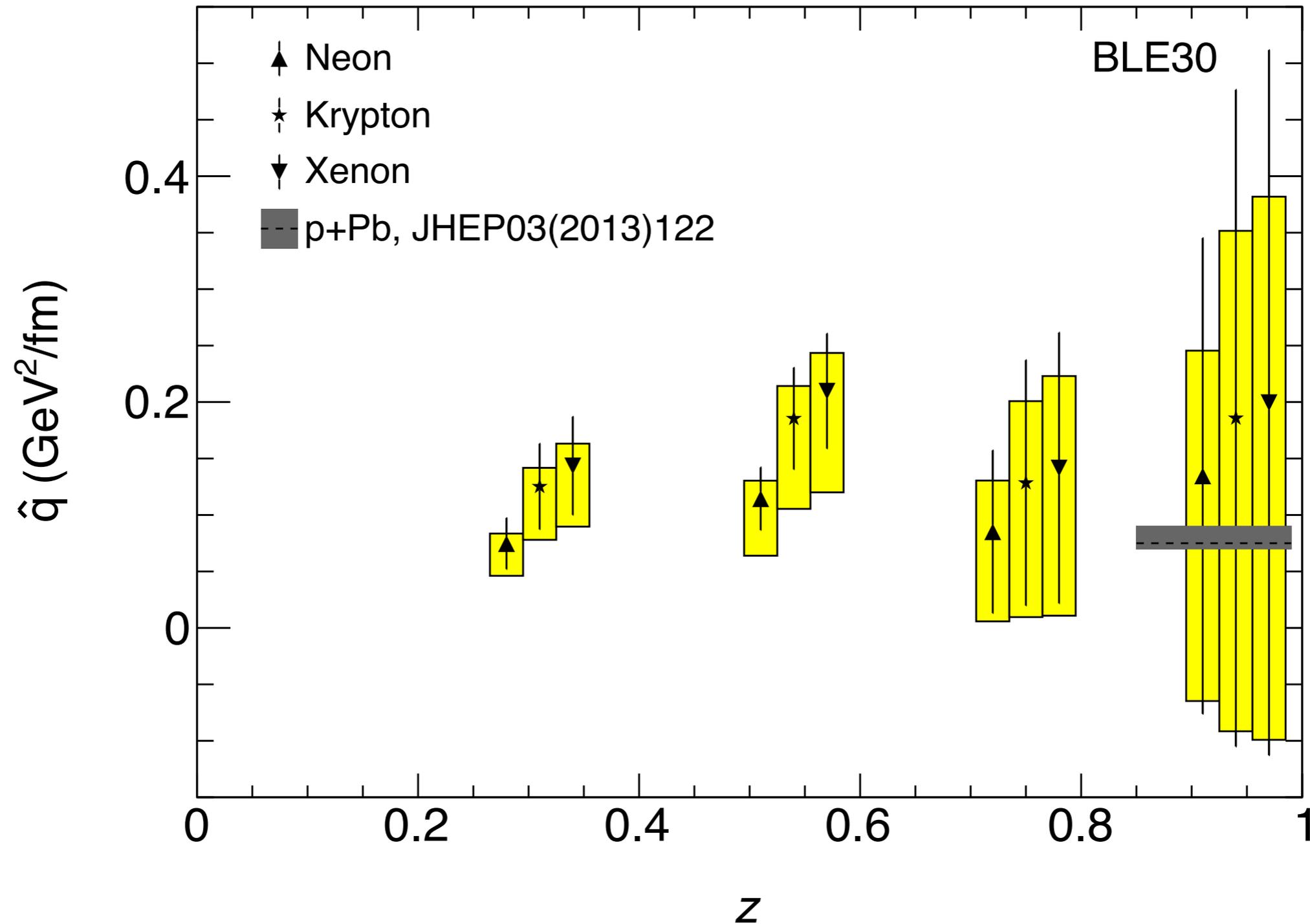
(Baseline model plus quark energy loss, BLE30)



Color lifetime - the main result of the model

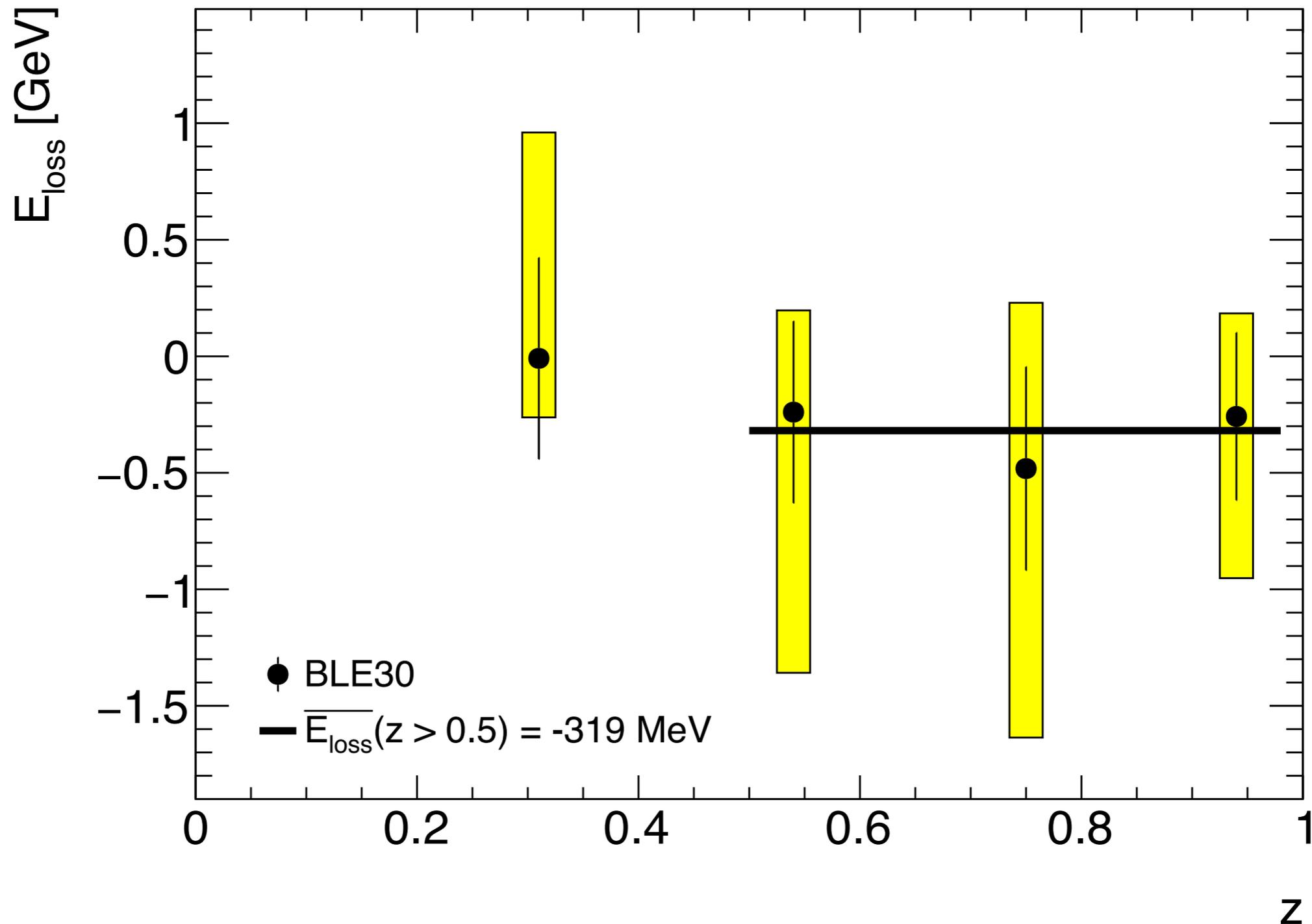


Transport Coefficient \hat{q}



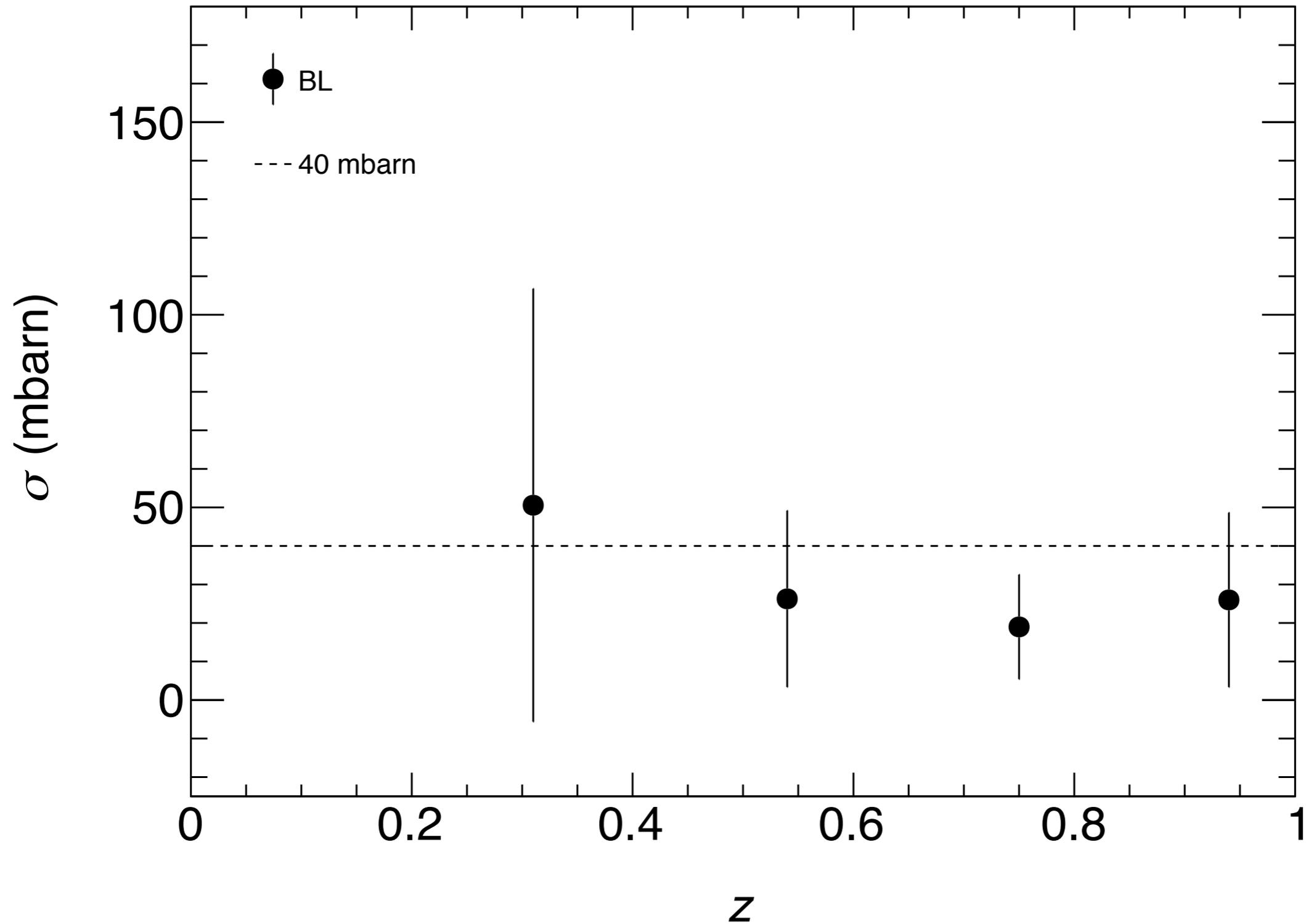
We find a value consistent with other published estimates, $\sim 0.075 \text{ GeV}^2/\text{fm}$.
We find an A-dependence, but with large uncertainties.
We do not see a significant z_h dependence.

Quark energy loss



We get plausible values for the quark energy loss, but with large uncertainties. Values are consistent with other analyses for cold matter. The model fit to the data is essentially of equal quality with and without quark energy loss.

Inelastic pion-nucleon cross section

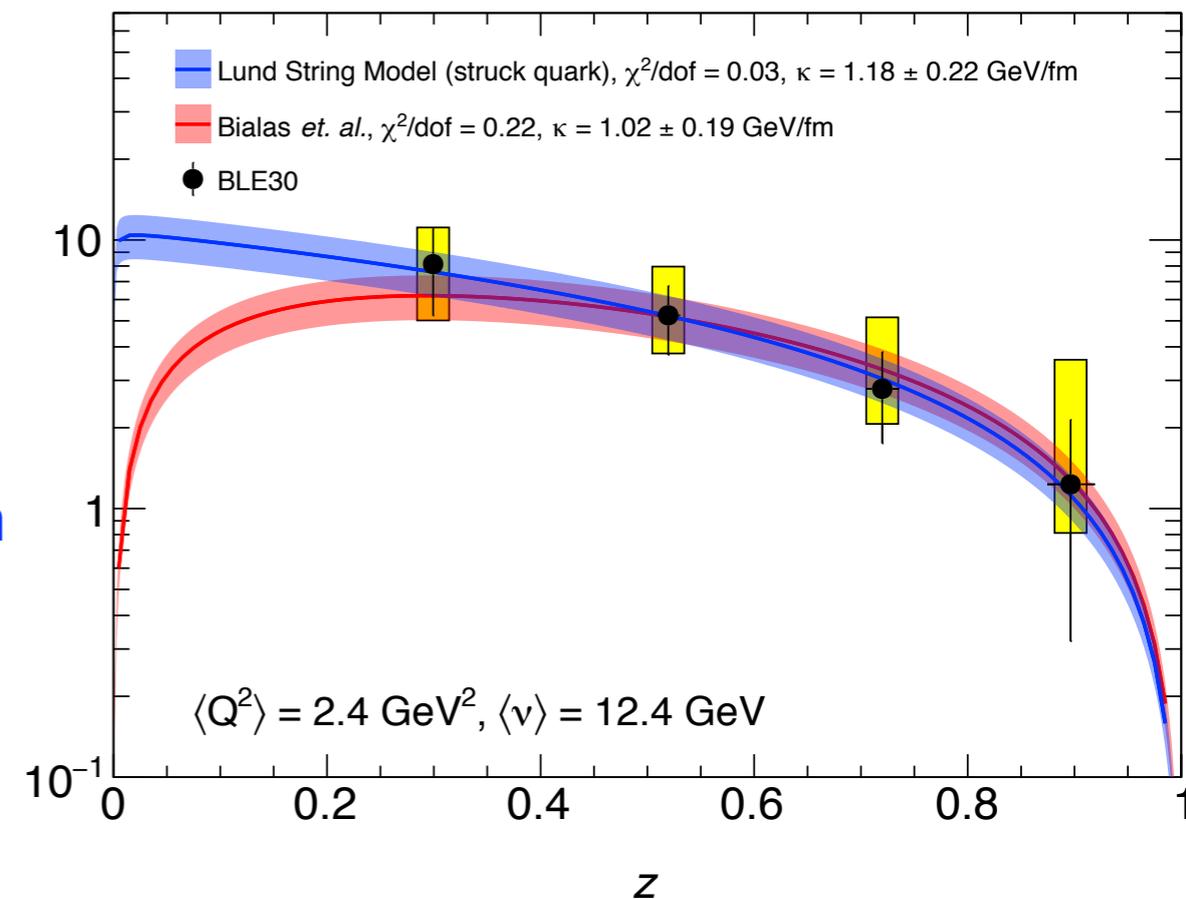


Extracted value consistent with ~ 25 -30 mbarns for $z_h > 0.5$

Color lifetime - the main result of the model

Comments:

- This parameter, L_c , is perfectly **stable** in all model variants
- A fit of our results to the Lund String Model form gives the well-known **string constant** of 1 GeV per fm to 20% accuracy
 - We consider this independent result to be a **strong validation** of our model
- We find a z-dependent color lifetime for HERMES kinematics ranging from **1 to 10 fm**
- As this is a *time interval*, we can boost to different reference frames to obtain the time-dilated color lifetime for **other experiments, such as EIC and JLab.**
- Future experiments can test to see if **time dilation** can be observed, which would further validate our approach.



About this model

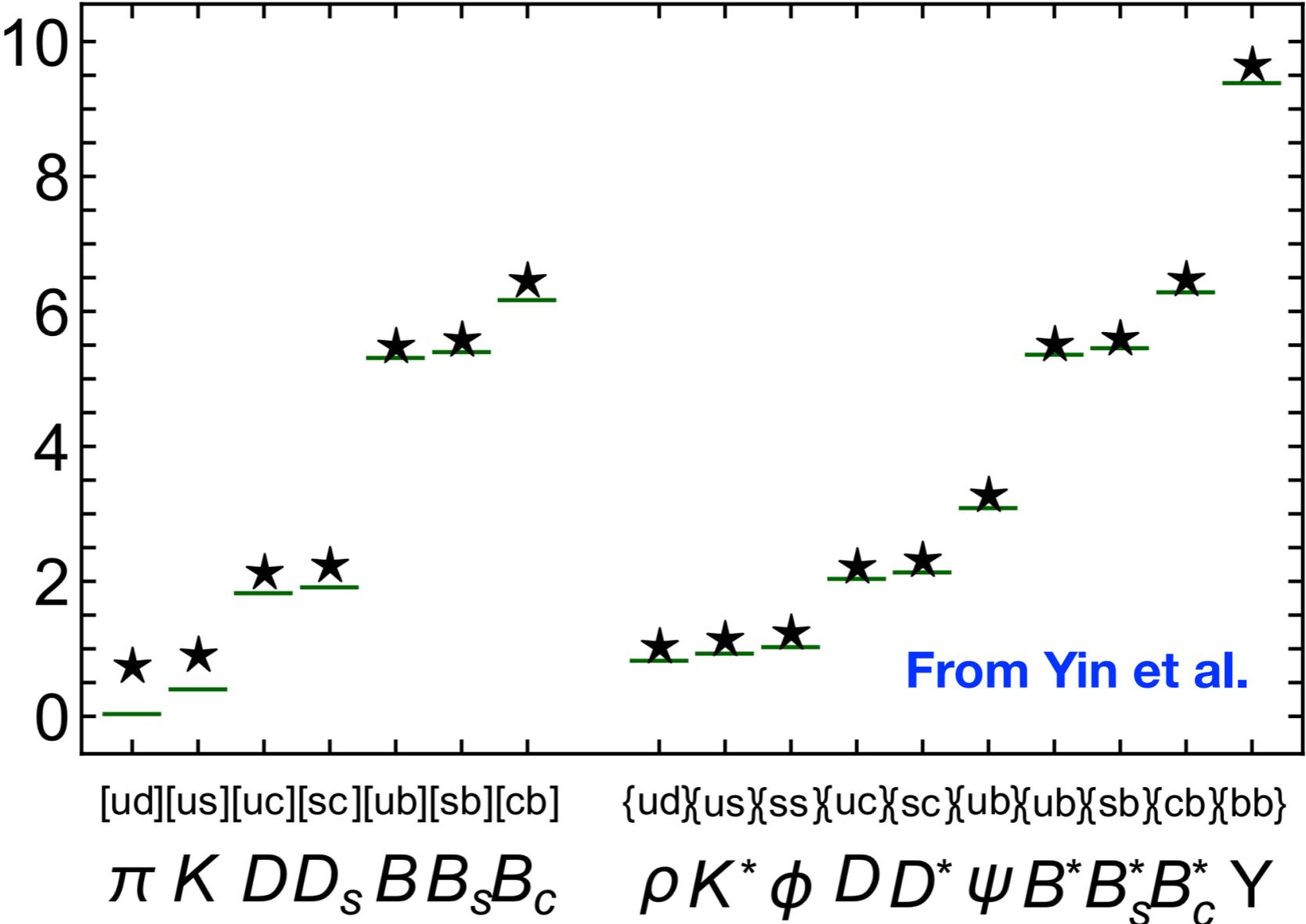
- We have extracted the **color lifetime** from published HERMES data using a **simultaneous fit of two observables**, finding z-dependent values from **1-10 fm/c**.
- The results are perfectly consistent with **Lund String Model** forms for this observable, and **independently** yield a value of the string constant **$\kappa = 1 \text{ GeV/fm}$** , strongly **validating** our approach.
- We also extracted the **\hat{q} transport coefficient**, the **quark energy loss**, and the **reduced inelastic pion-nucleon cross section**, finding values consistent with expectations and other analyses, but with large uncertainties.
- We consider that we “understand” nDIS **meson** production based on these results. New data are needed to prove otherwise.

On to diquarks!

Masses of ground-state mesons and baryons, including those with heavy quarks

Pei-Lin Yin,^{1,*} Chen Chen,^{2,†} Gastão Krein,² Craig D. Roberts,^{3,‡} Jorge Segovia,⁴ and Shu-Sheng Xu¹

arXiv 1903.00160

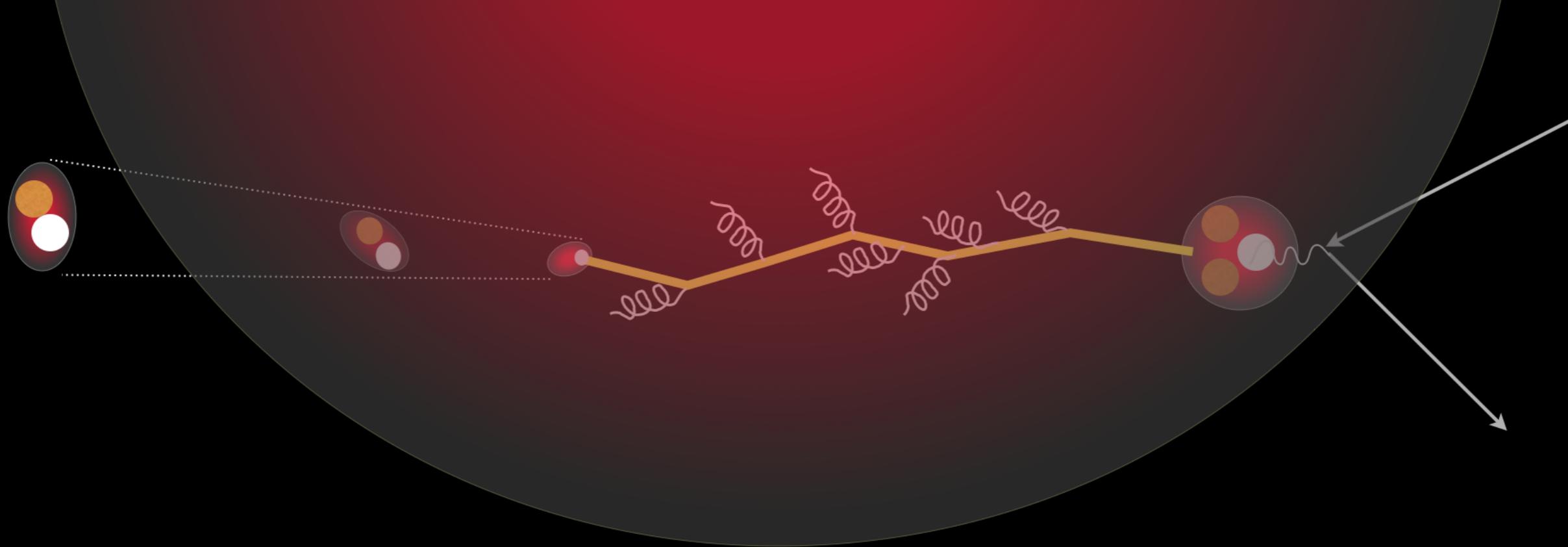


The ud diquarks are heavy. This is very relevant to what follows in this talk.

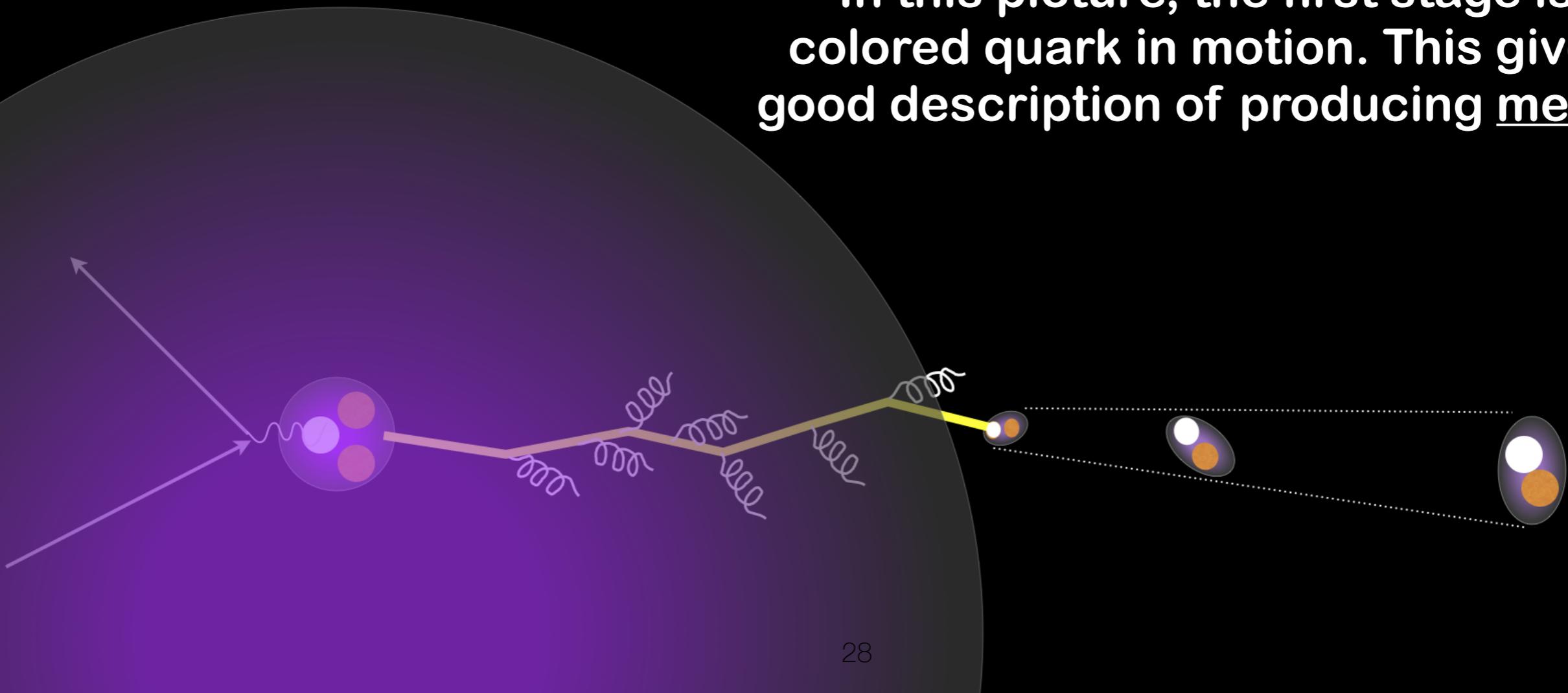
FIG. 2. Comparison between computed masses of diquark correlations and their symmetry-related meson counterparts: diquarks – (black) stars and mesons – (green) bars.

Experimental **evidence** of **diquark scattering** from the HERMES data for SIDIS on nuclear targets

“Multidimensional study of hadronization in nuclei”
arXiv:1107.3496v3 [hep-ex] 13 Sep 2011



In this picture, the first stage is a colored quark in motion. This gives a good description of producing mesons.



Interpreting HERMES Nuclear DIS DATA: MESONS

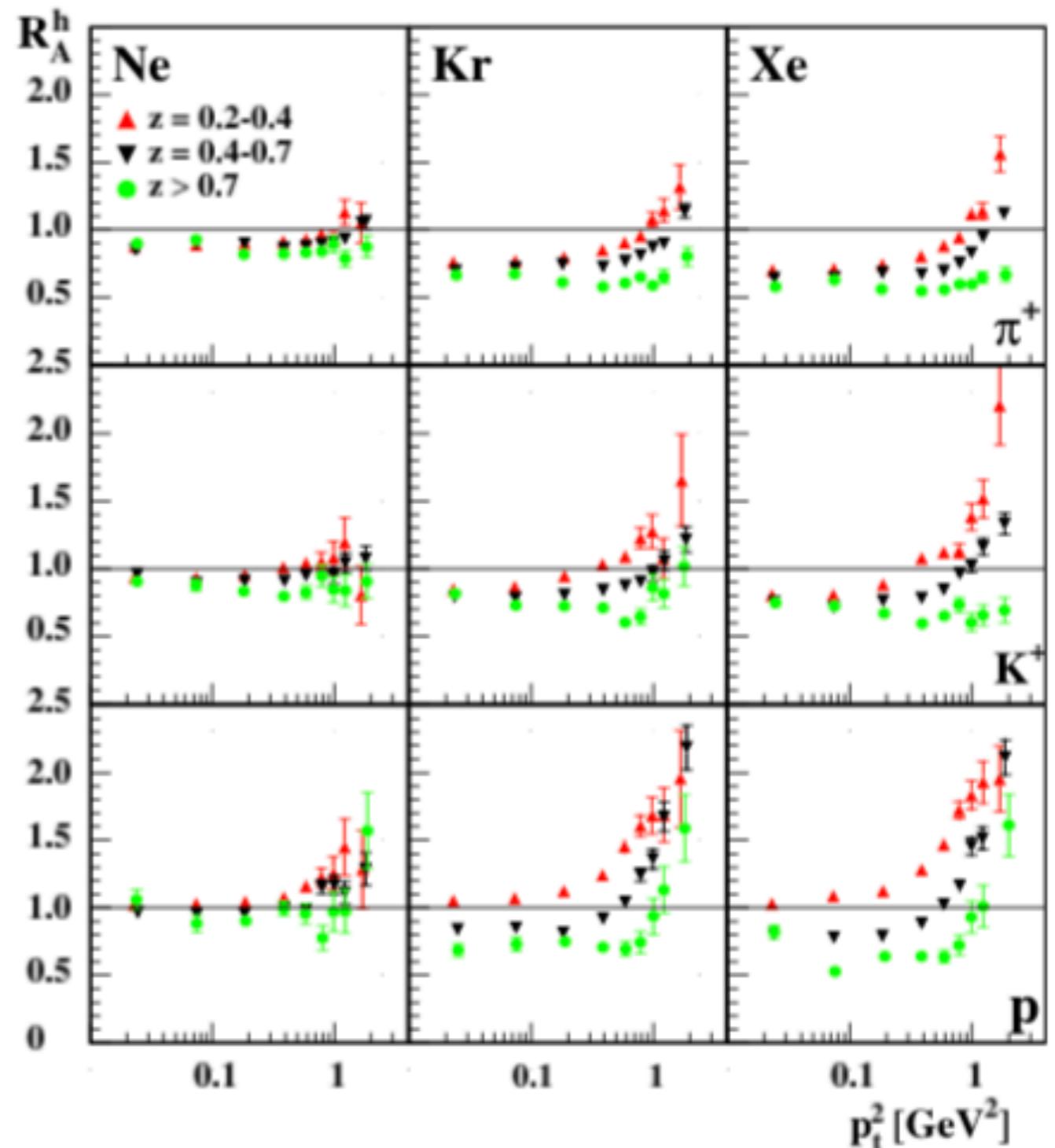
The multiplicity ratio measures effects of the nuclear medium.

“No effects” means $R=1.0$

$$R_A^h(\nu, Q^2, z, p_t^2) = \frac{\left(\frac{N^h(\nu, Q^2, z, p_t^2)}{N^e(\nu, Q^2)} \right)_A}{\left(\frac{N^h(\nu, Q^2, z, p_t^2)}{N^e(\nu, Q^2)} \right)_D}$$

Most basic indicator is pT dependence of multiplicity ratio.

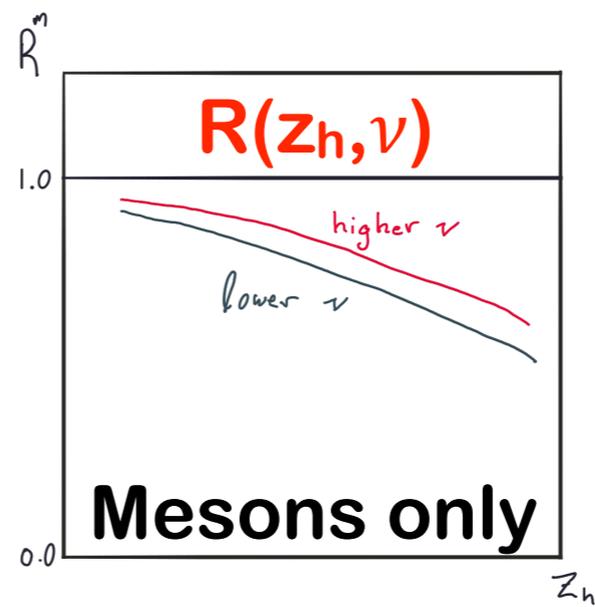
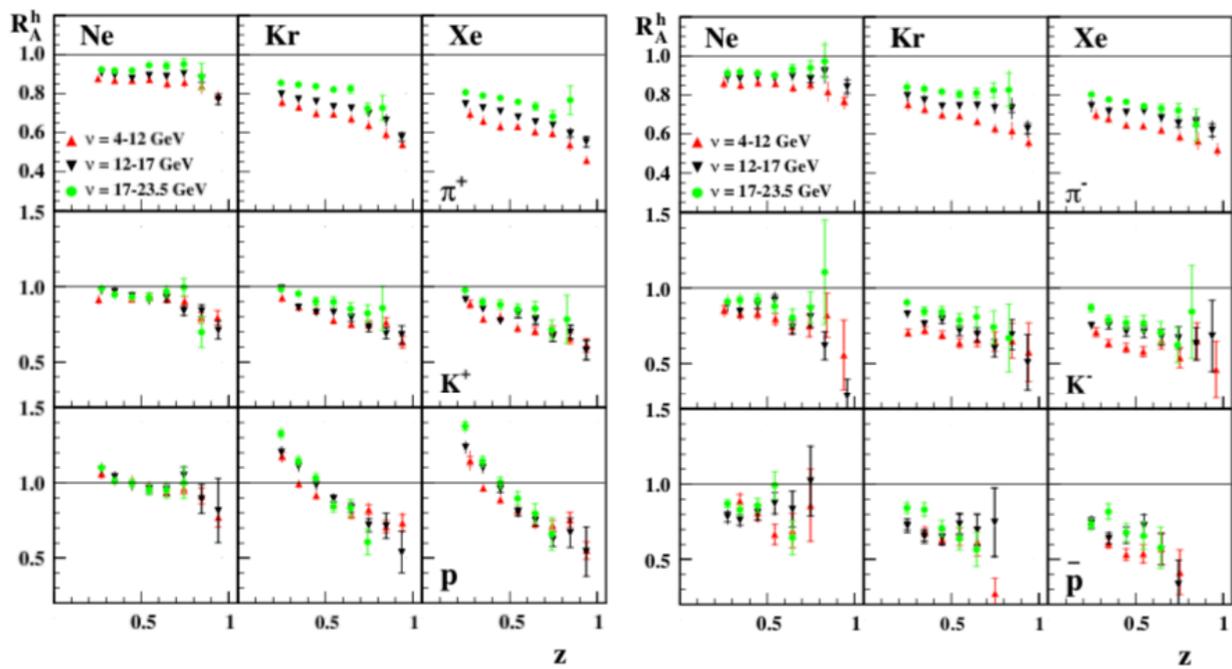
$R > 1$ at high pT because particles that strongly interact with the medium acquire more pT than those that don't interact as much.



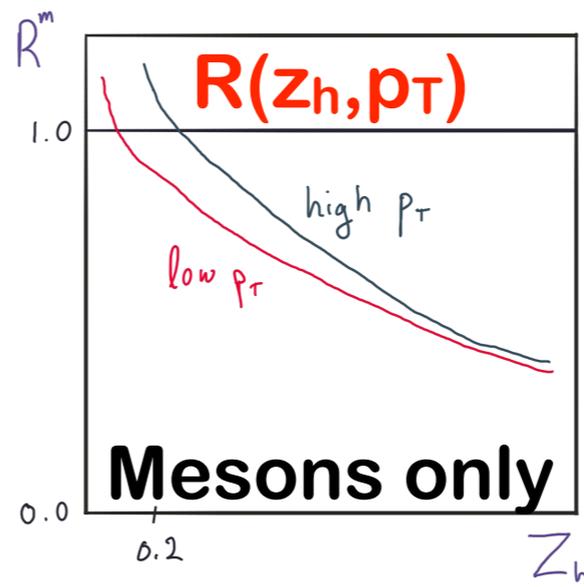
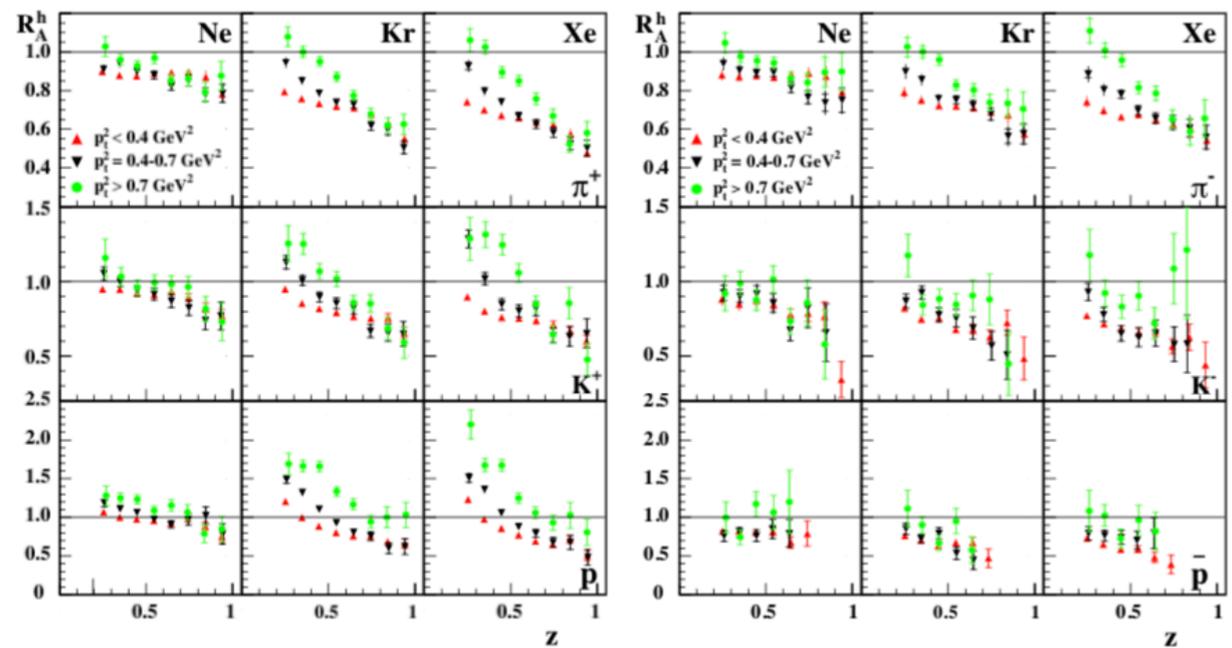
“Interact” = hadronic interaction of forming hadrons, + quark energy loss.

Empirically, from these plots, low-z mesons acquire more pT than high-z.

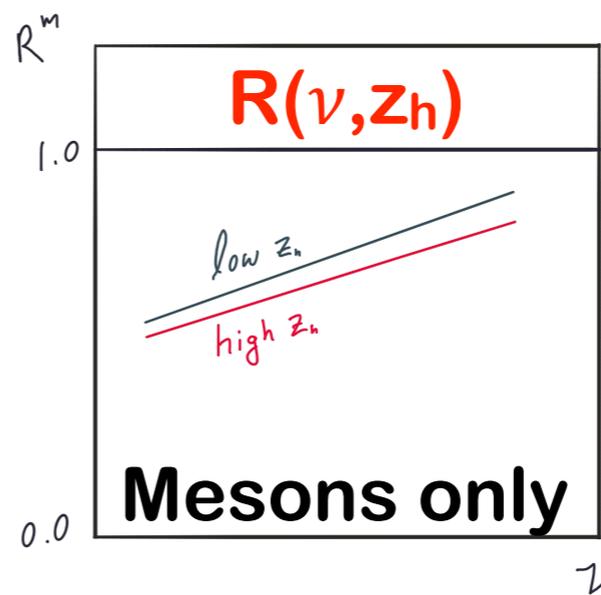
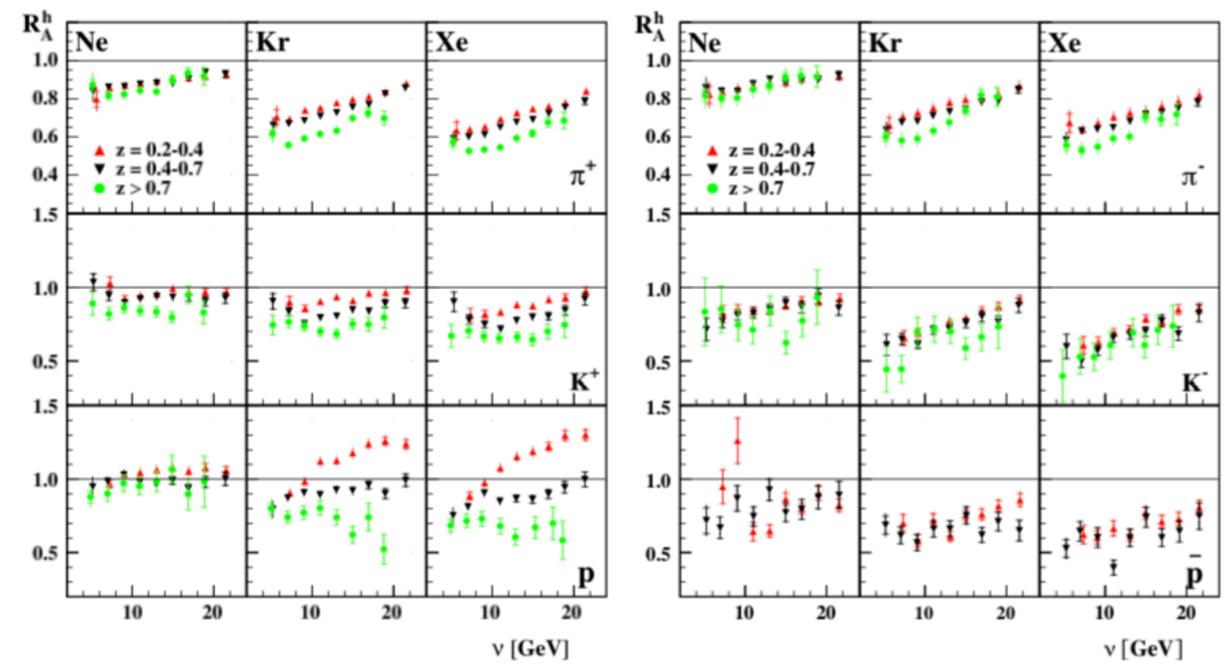
Enhancement at high pT mostly caused by hadronic interactions at low z.



Integrated over p_T ,
so always < 1 .
At higher ν , less
attenuation because
of time dilation of
quark lifetime



Not integrated over
 p_T , so can exceed 1.
Exceeds 1 faster for
higher p_T , so
crossing point is p_T
dependent.



Time dilation is
proportional to ν .
Slow approach to 1.0
at infinite ν . Quark
lifetime goes to zero
at high z , so high z is
attenuated more.

So far, we have a reasonable **qualitative** interpretation for **mesons** that explains multi-dimensional behavior completely.

BUT: mesons don't have diquarks

Let's see if we can understand HERMES **baryon** data

Interpreting HERMES Nuclear DIS DATA: MESONS

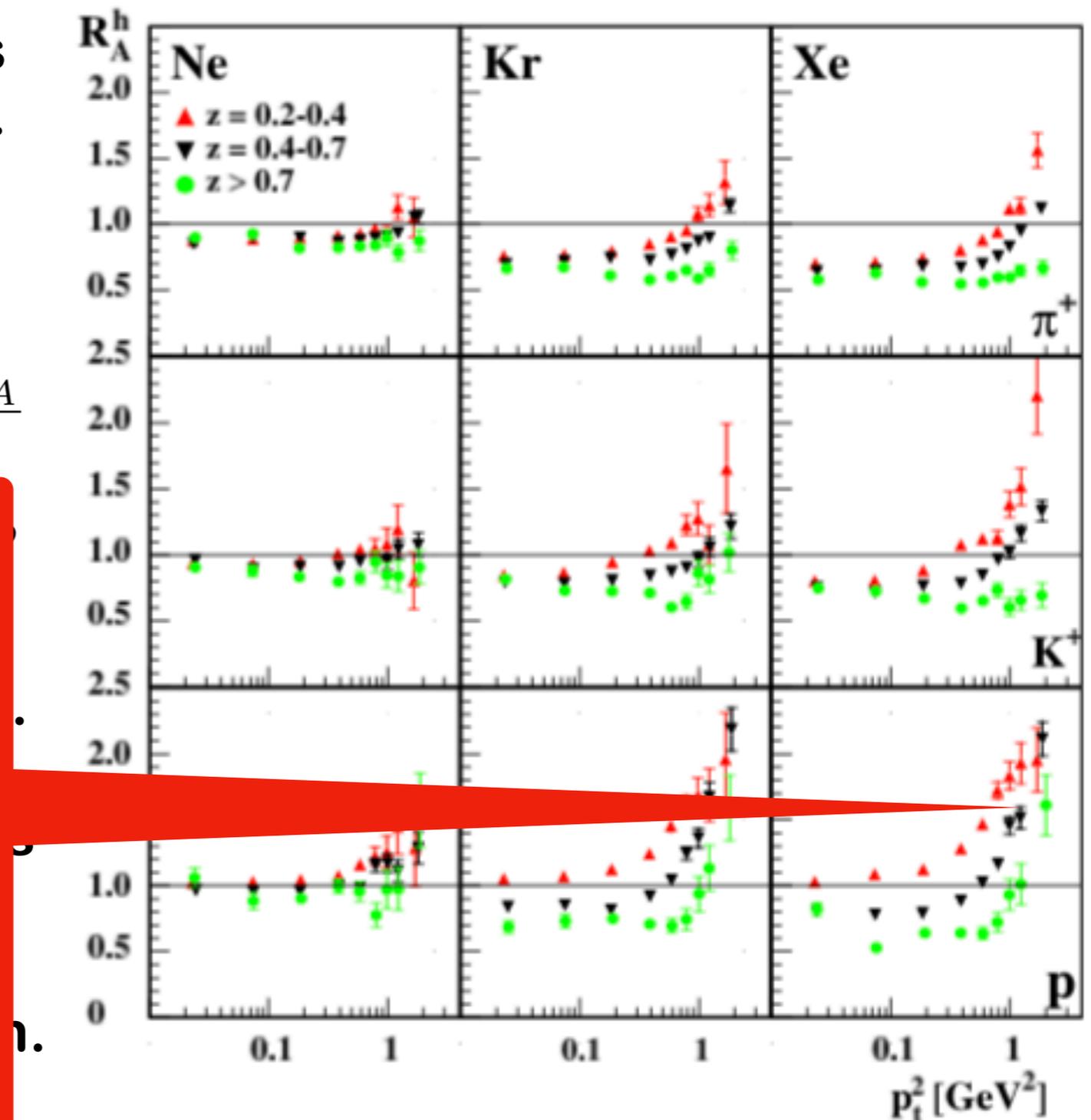
The multiplicity ratio measures effects of the nuclear medium.

“No effects” means $R=1.0$

$$R_A^h(\nu, Q^2, z, p_t^2) = \frac{\left(\frac{N^h(\nu, Q^2, z, p_t^2)}{N^e(\nu, Q^2)} \right)_A}{\left(N^h(\nu, Q^2, z, p_t^2) \right)}$$

The ordering in z seen for mesons disappears at high p_T for protons.

Strong interaction occurs at all values of z .

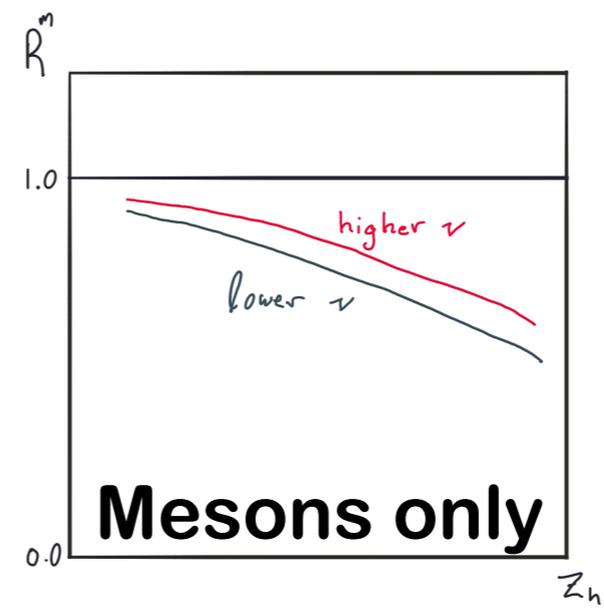
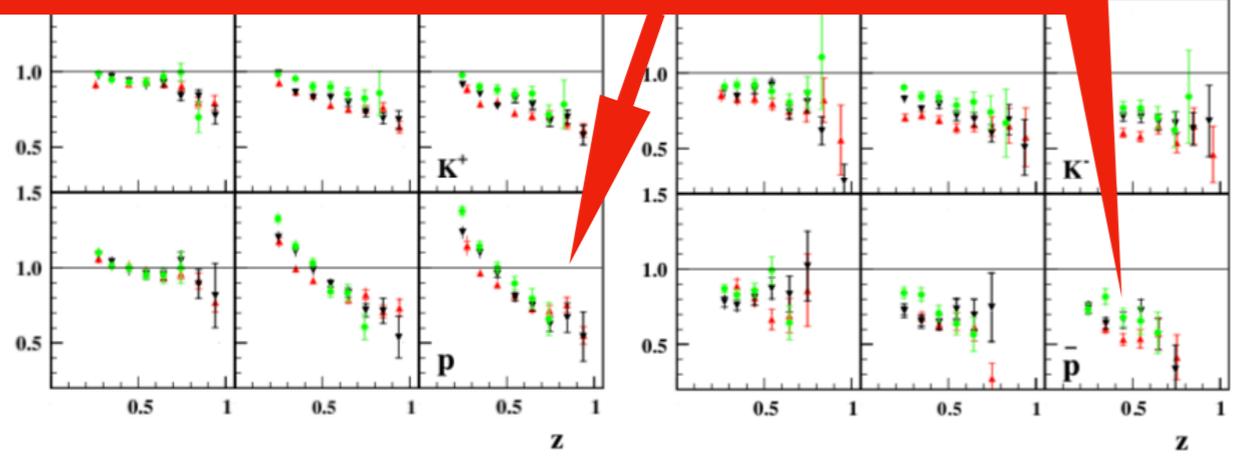


interact hadronic interaction of forming hadrons, + quark energy loss.

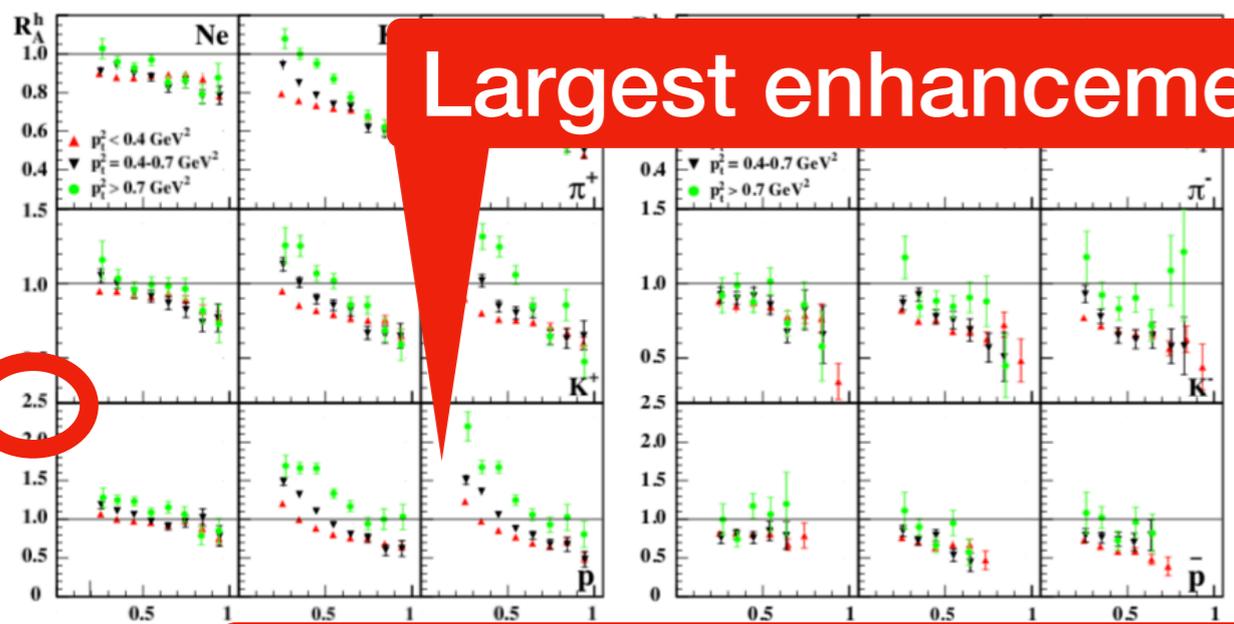
Empirically, from these plots, low- z mesons acquire more p_T than high- z .

Enhancement at high p_T mostly caused by hadronic interactions at low z .

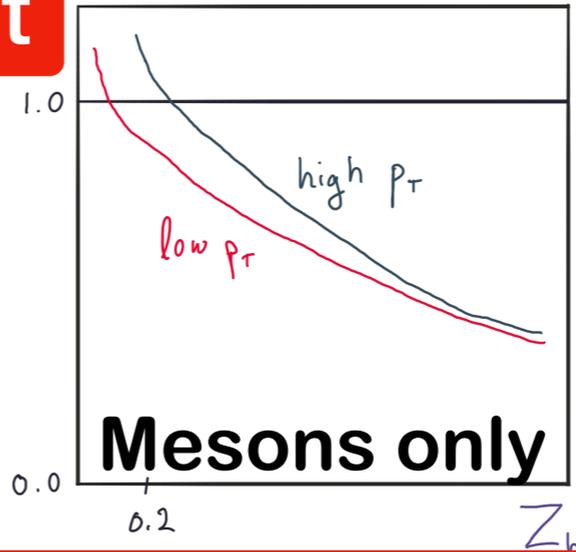
Protons and antiprotons act completely differently



Integrated over p_T , so always < 1 .
At higher ν , less attenuation because of time dilation of quark lifetime

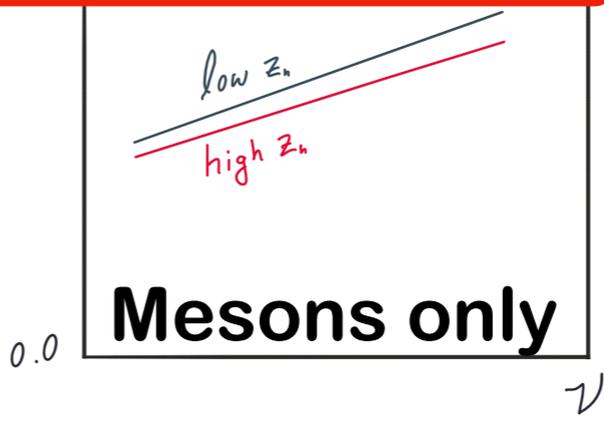
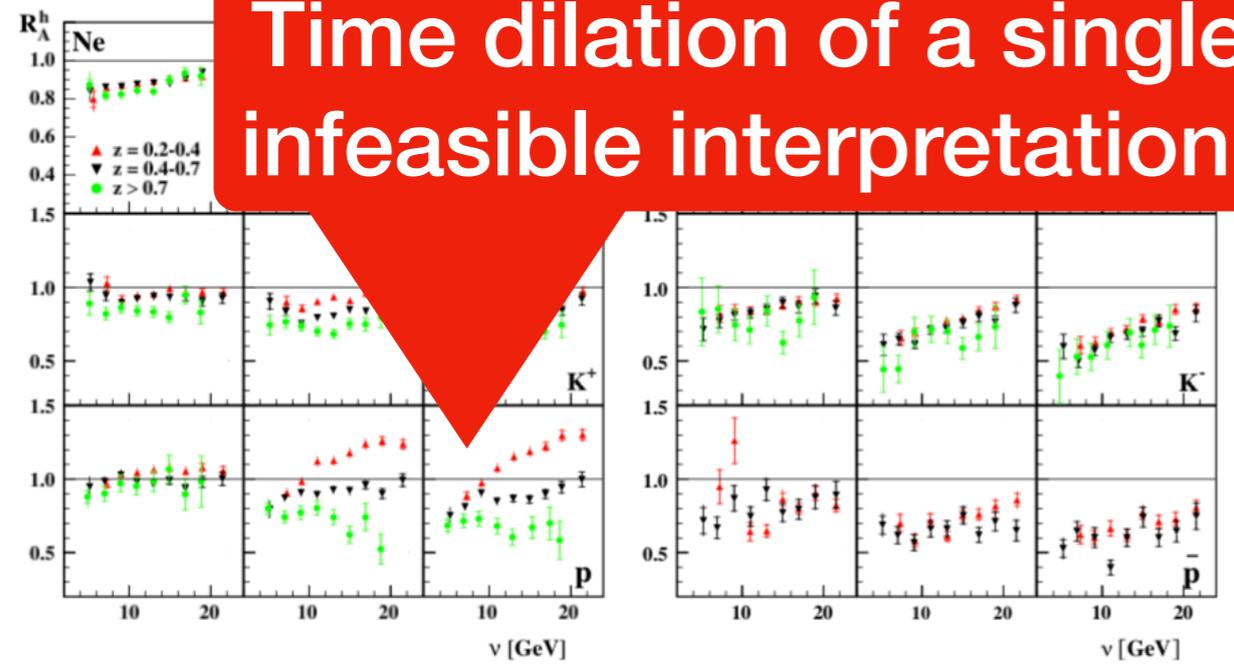


Largest enhancement



Not integrated over p_T , so can exceed 1. Exceeds 1 faster for higher p_T , so crossing point is p_T dependent.

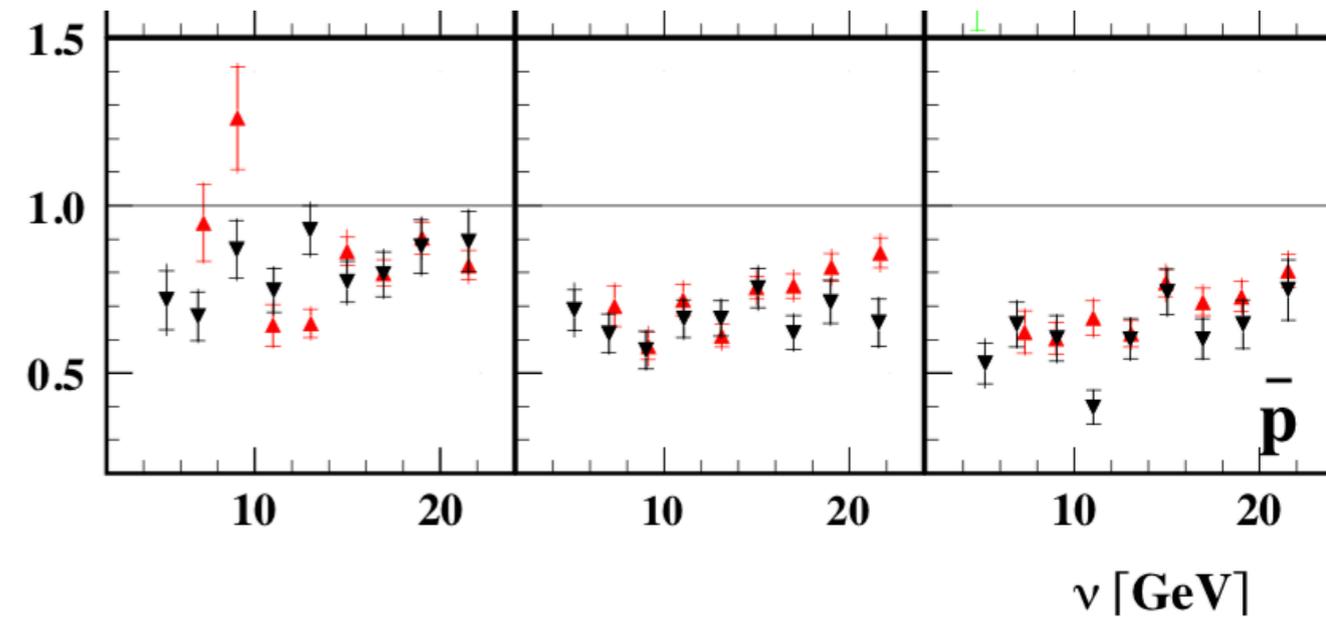
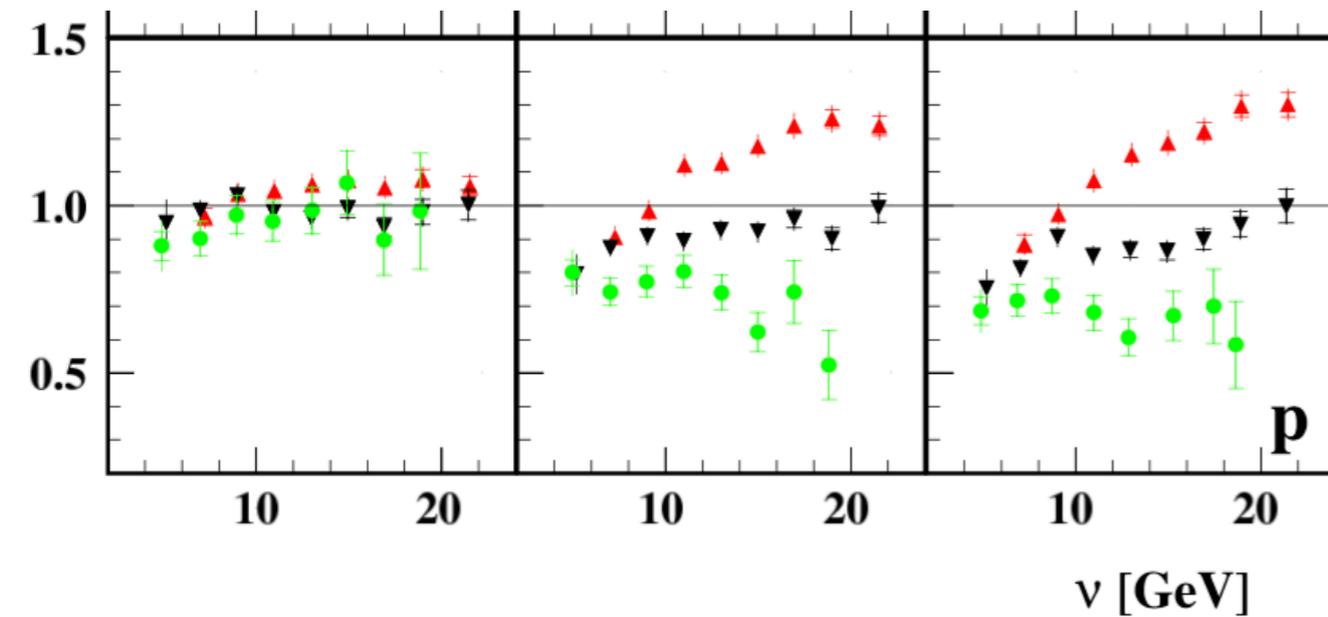
Time dilation of a single quark now an infeasible interpretation: $R \gg 1$ at low z .



Time dilation is proportional to ν . Slow approach to 1.0 at infinite ν . Quark lifetime goes to zero at high z , so high z is attenuated more.

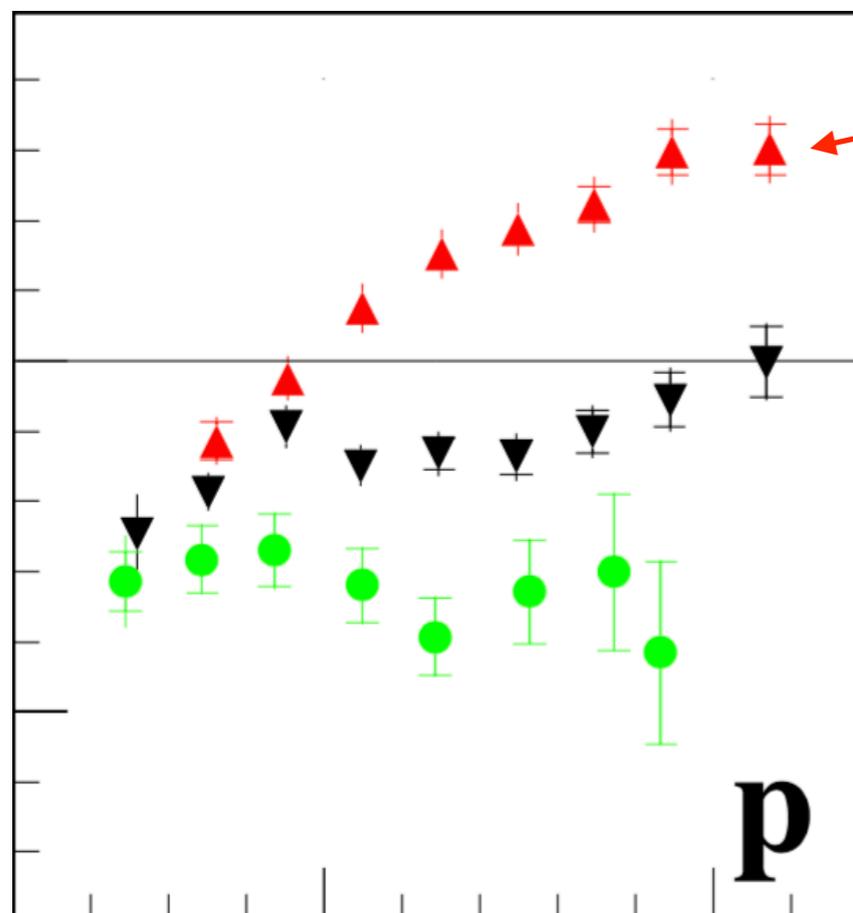
HERMES Proton Multiplicity Ratios

▲ $z = 0.2-0.4$
▼ $z = 0.4-0.7$
● $z > 0.7$



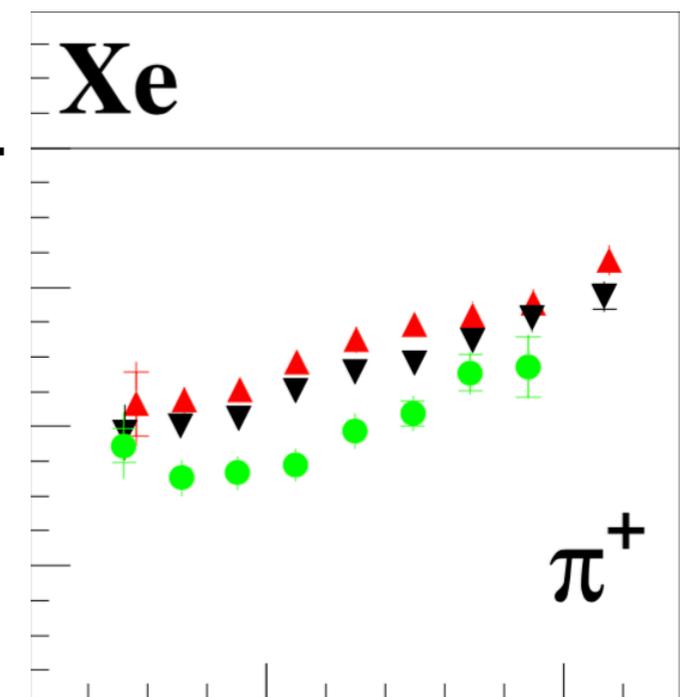
proton (left) and antiproton (right) are totally different

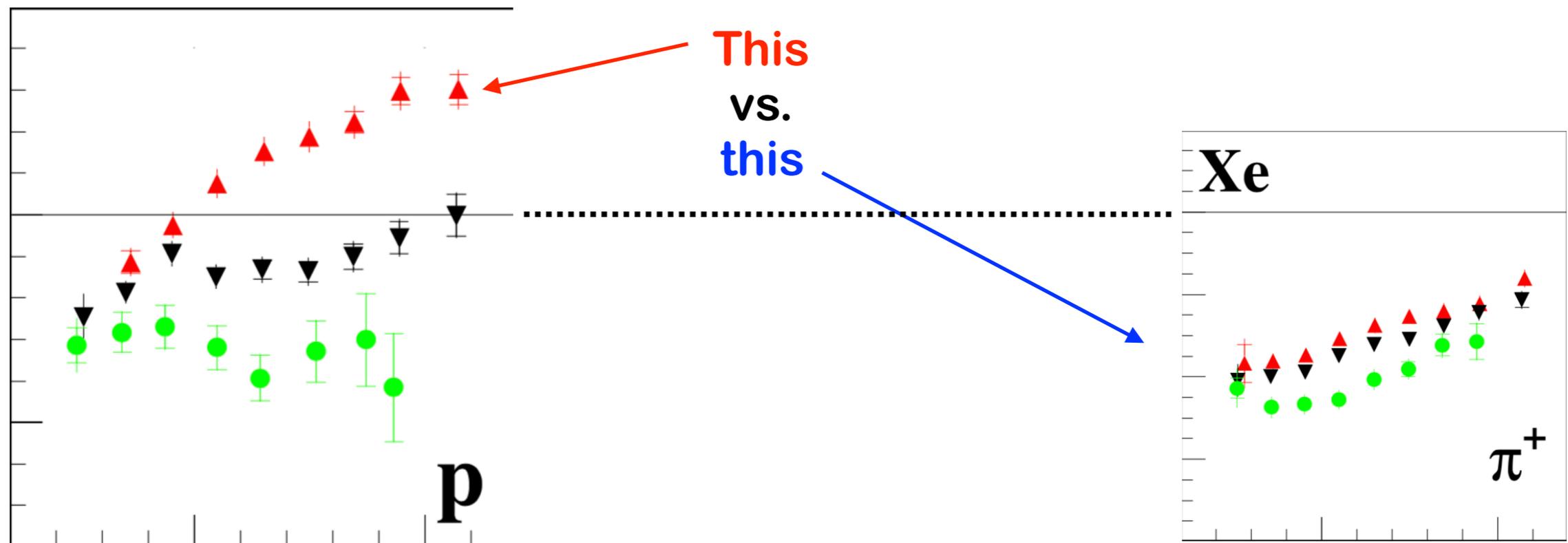
Proton multiplicity ratios qualitatively different from mesons.



This
vs.
this

I will argue that
this behavior is
due to diquarks





HERMES paper explanation: FSI are “knocking out protons.”
Maybe. But, @ high W and Q^2 , = virtual photon strikes **one** quark: need to make a pion in-medium to knock out a proton

But maybe it could be diquarks knocking them out.
 Diquark “size” must be similar to that of a proton (mass is similar to and larger than that of a proton).

= diquark color field much more extended in space

Test this hypothesis: CLAS preliminary nDIS data for Lambda Baryons

**CLAS6 preliminary nDIS data for
Lambda Baryons**

Analysis Team from Mississippi State University:

Prof. Lamiaa El Fassi (Group Leader)

Dr. Latif-ul Kabir

Dr. Taya Chetry

Analysis Contributions from U. Técnica Fed. Santa María:

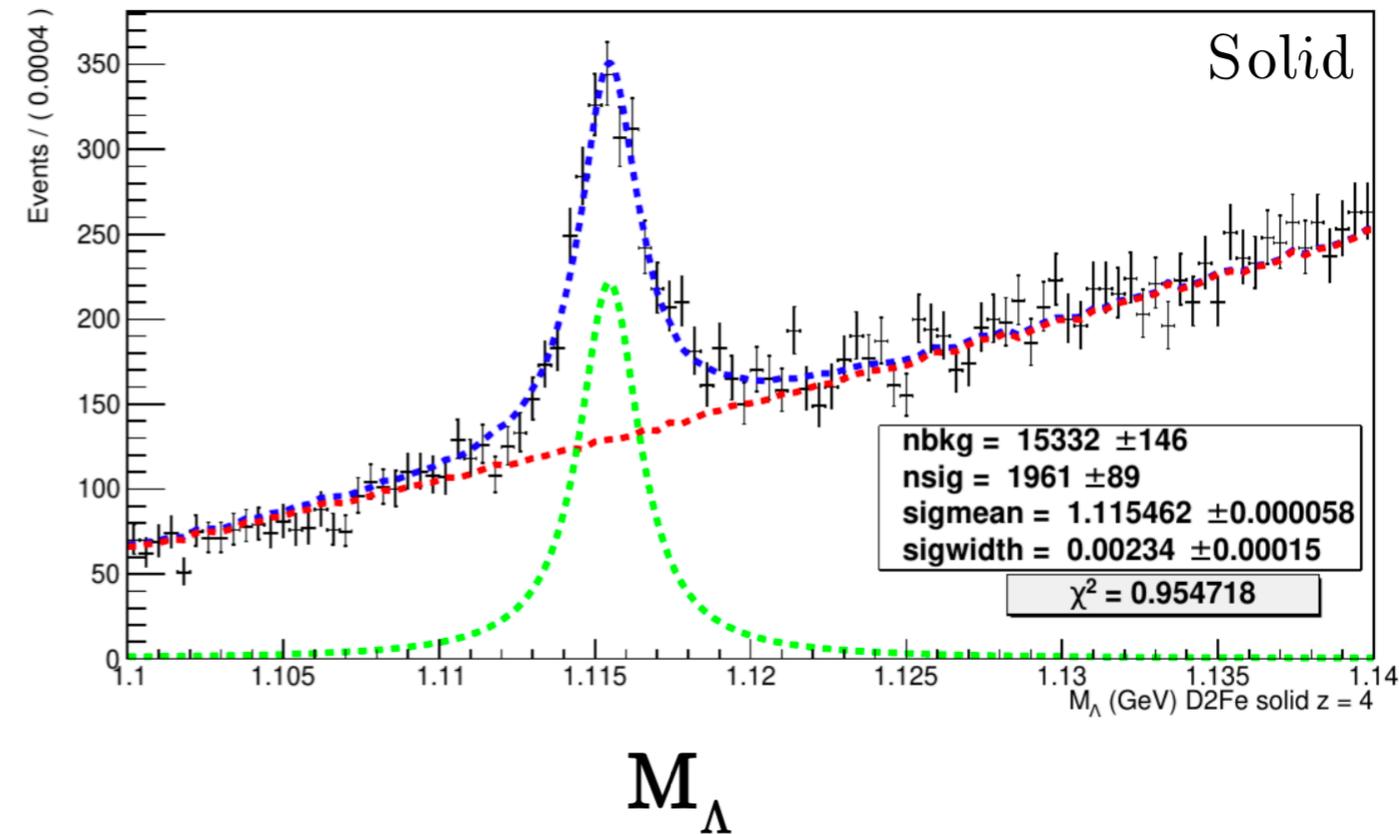
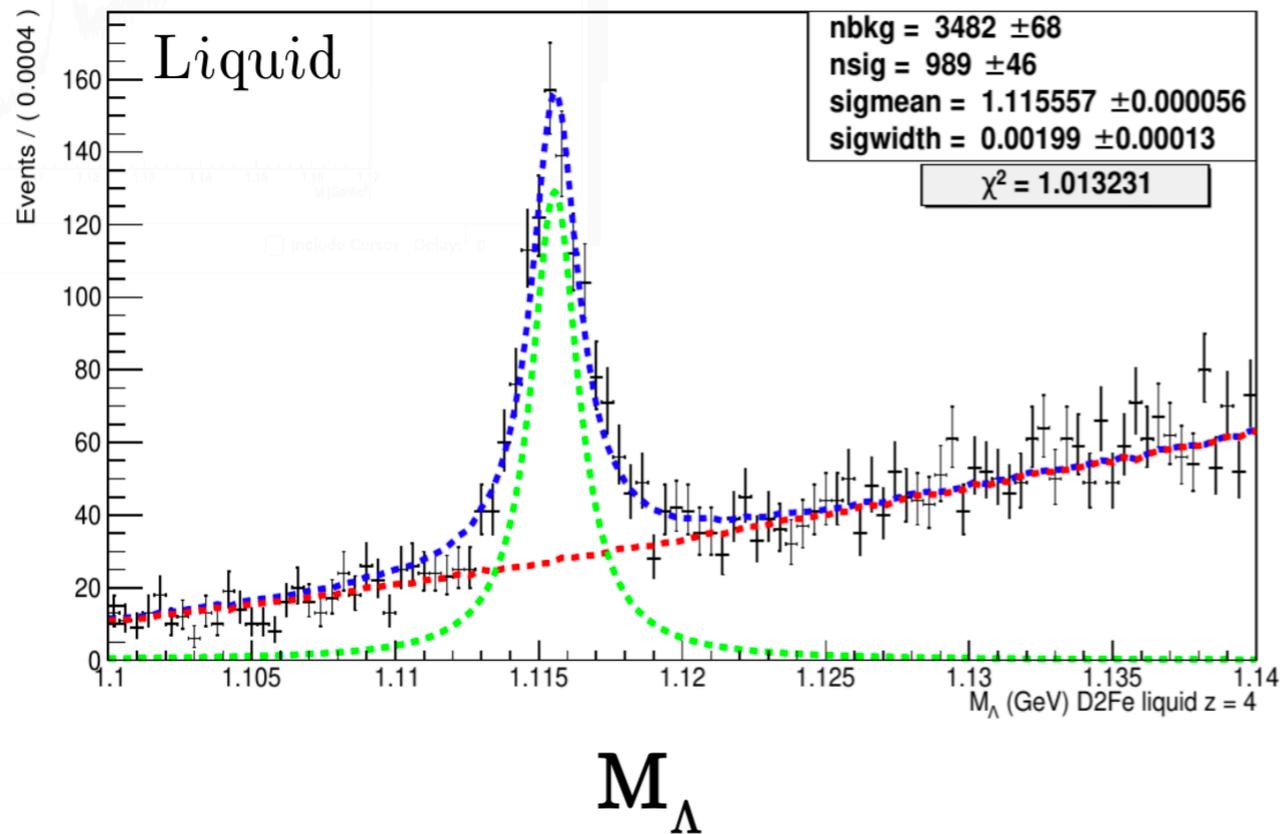
Dr. Ahmed El Alaoui

Some early work performed at ANL.

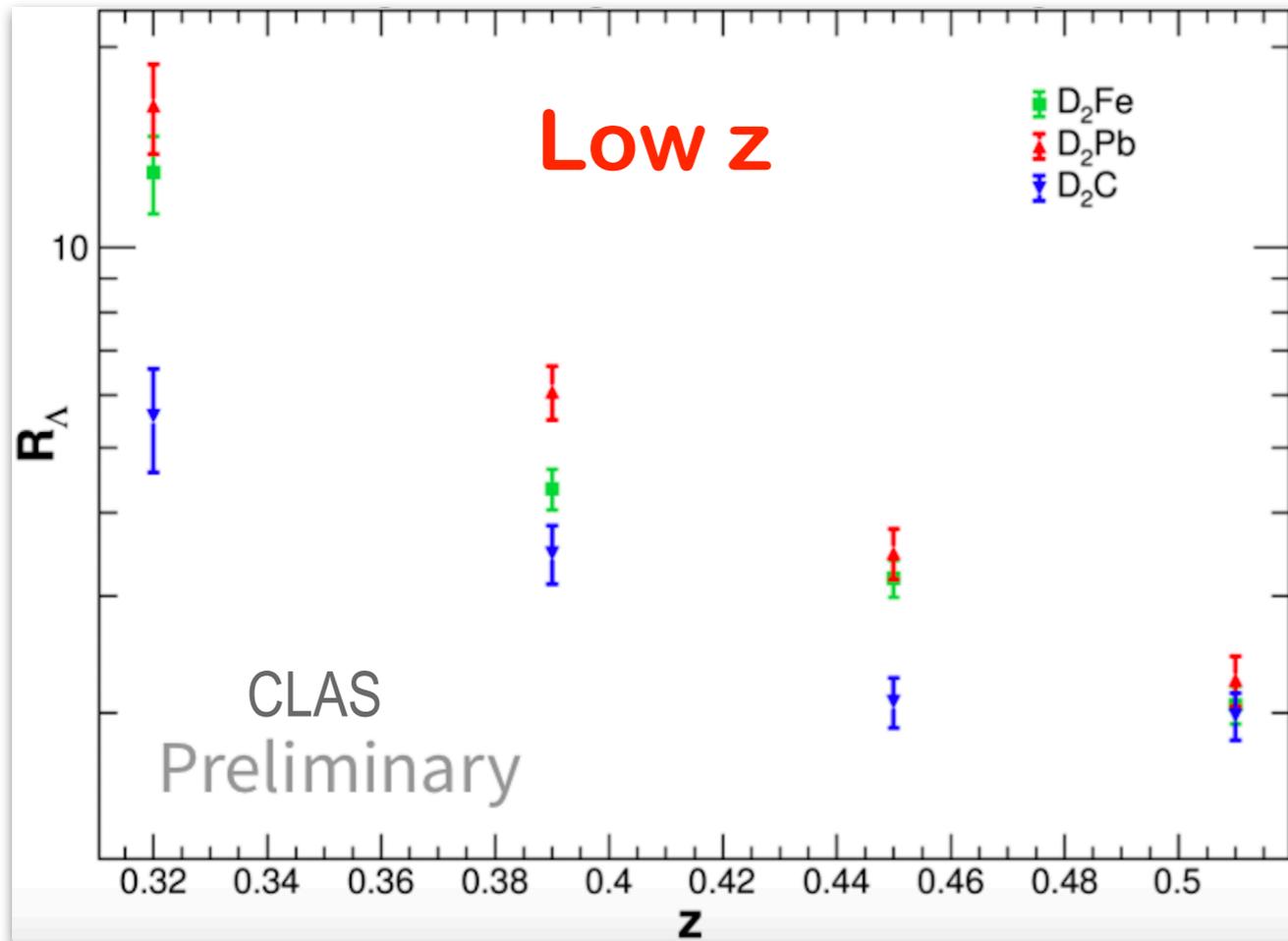
**Uncorrected preliminary results released March 2019 by
Nuclear Physics Working Group of CLAS Collaboration.**

Lambda Baryons are well-identified in π -p channel

$$z = [0.48, 0.54)$$



Backgrounds are under control - three different extraction methods agree

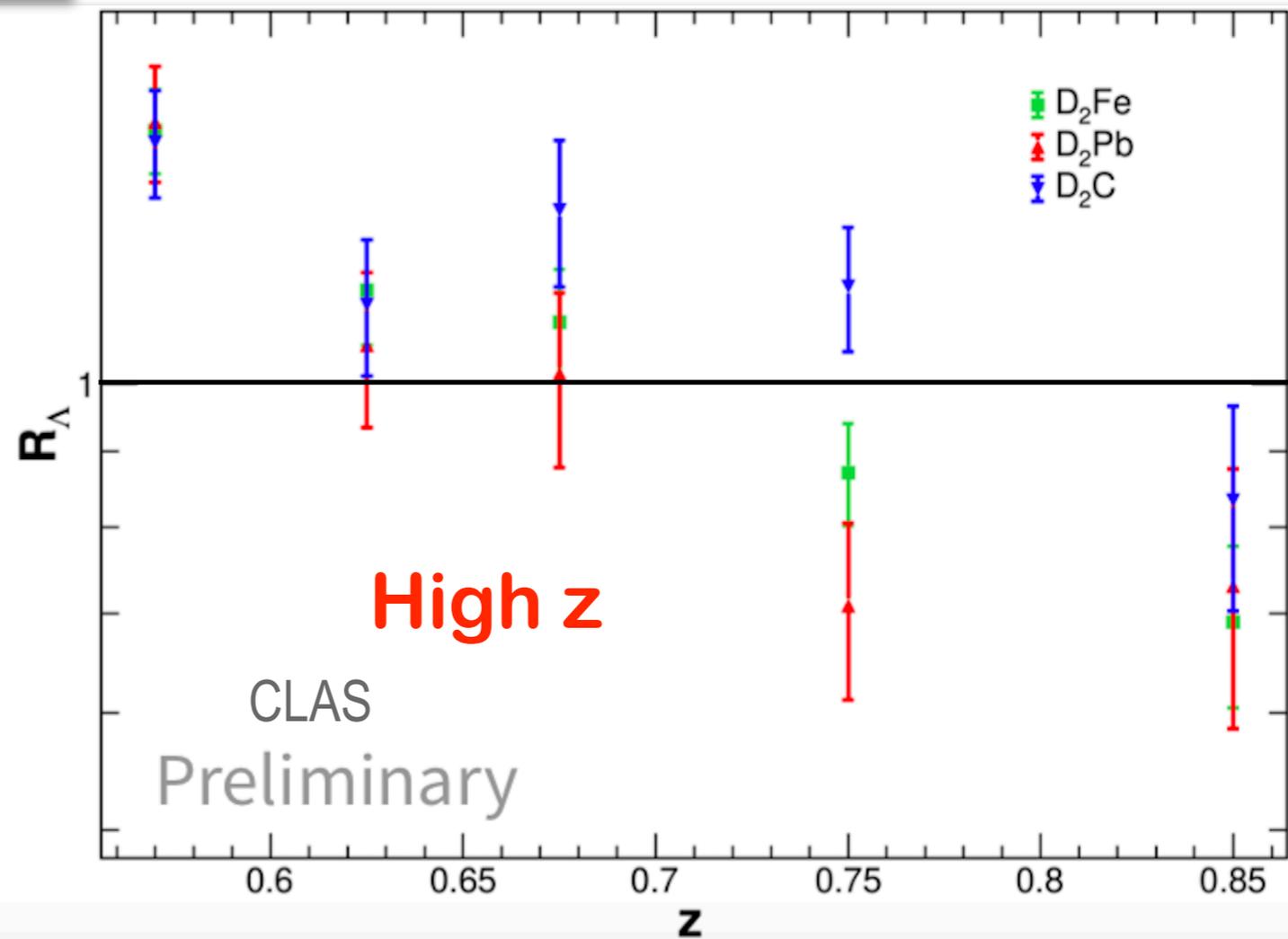


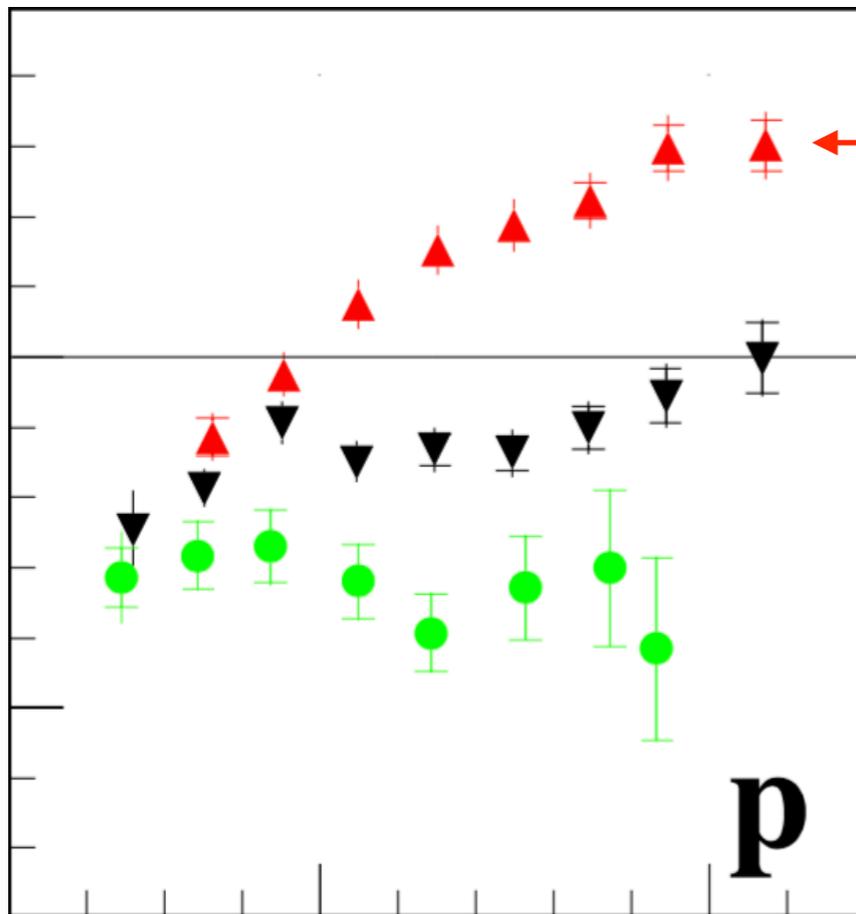
“Pile-up” of events at low z -
huge effect compared to
 pion production

Order inverted as expected:
 heavy-to-light

At higher z, there is
 relatively little
 attenuation.

Order as expected:
 light-to-heavy





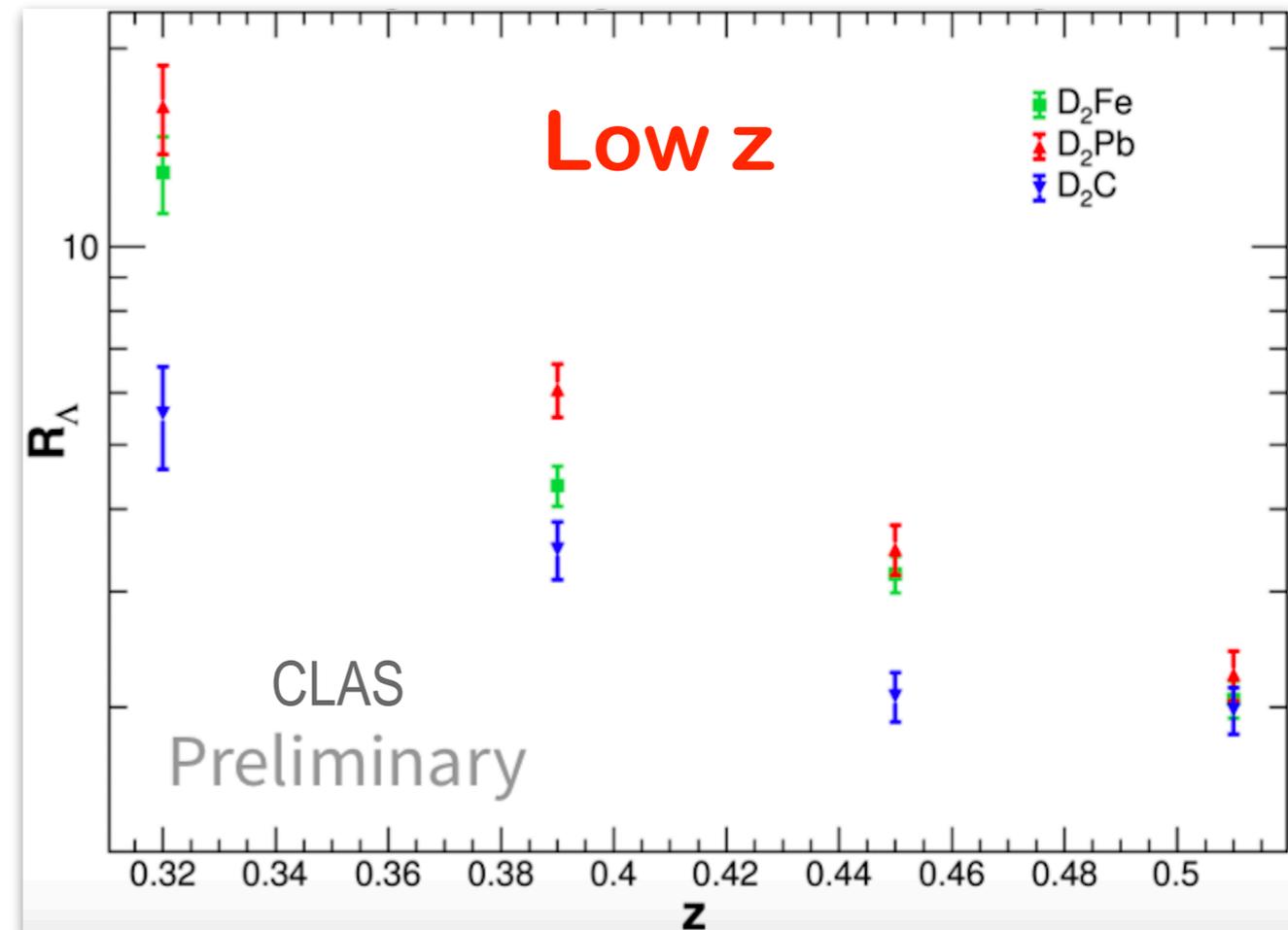
Excess of low-z protons in HERMES data

Explanation: FSI are “knocking out protons”??

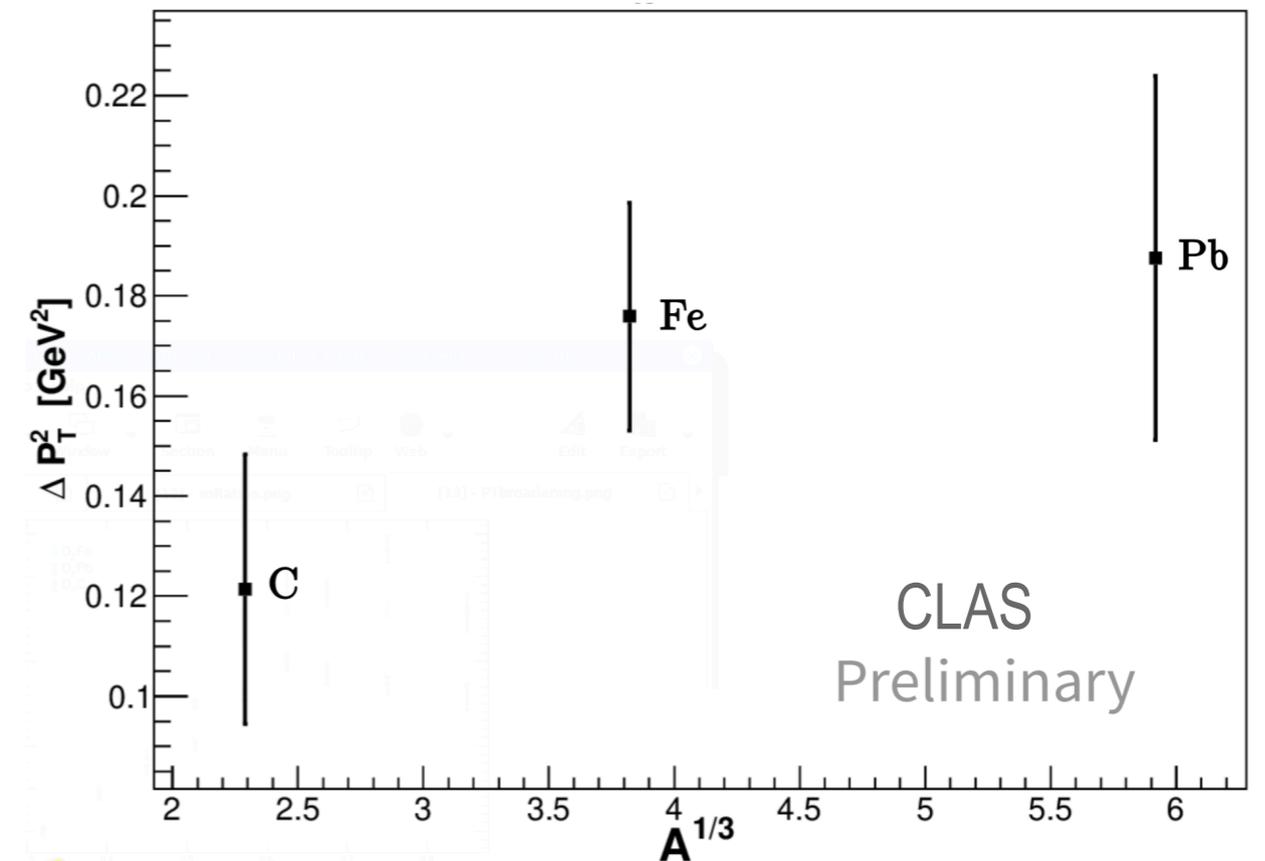
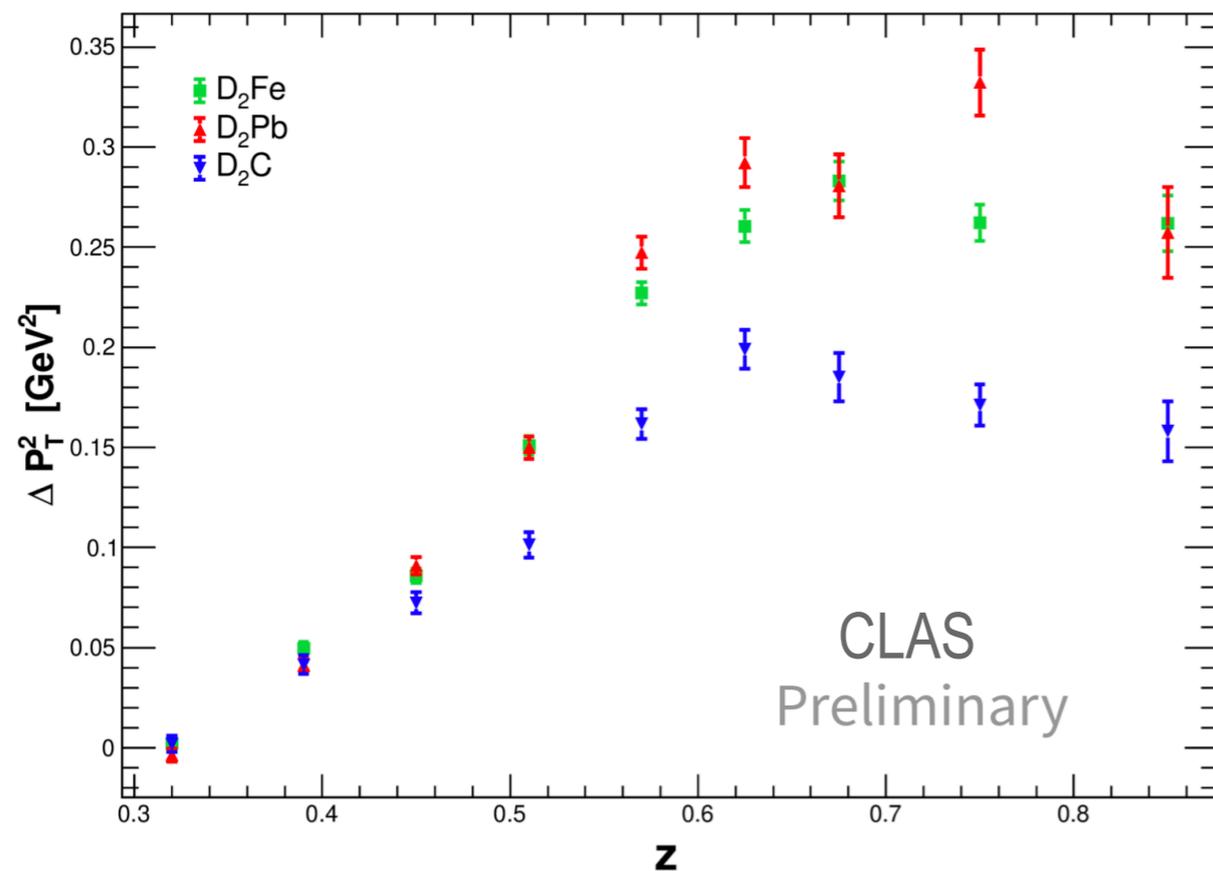
Excess of low-z Lambdas in CLAS data

**Not explained by FSI
“knocking out Lambdas”!!**

I have a better explanation



Transverse Momentum Broadening is **Large**



Maximum is 0.3 GeV²

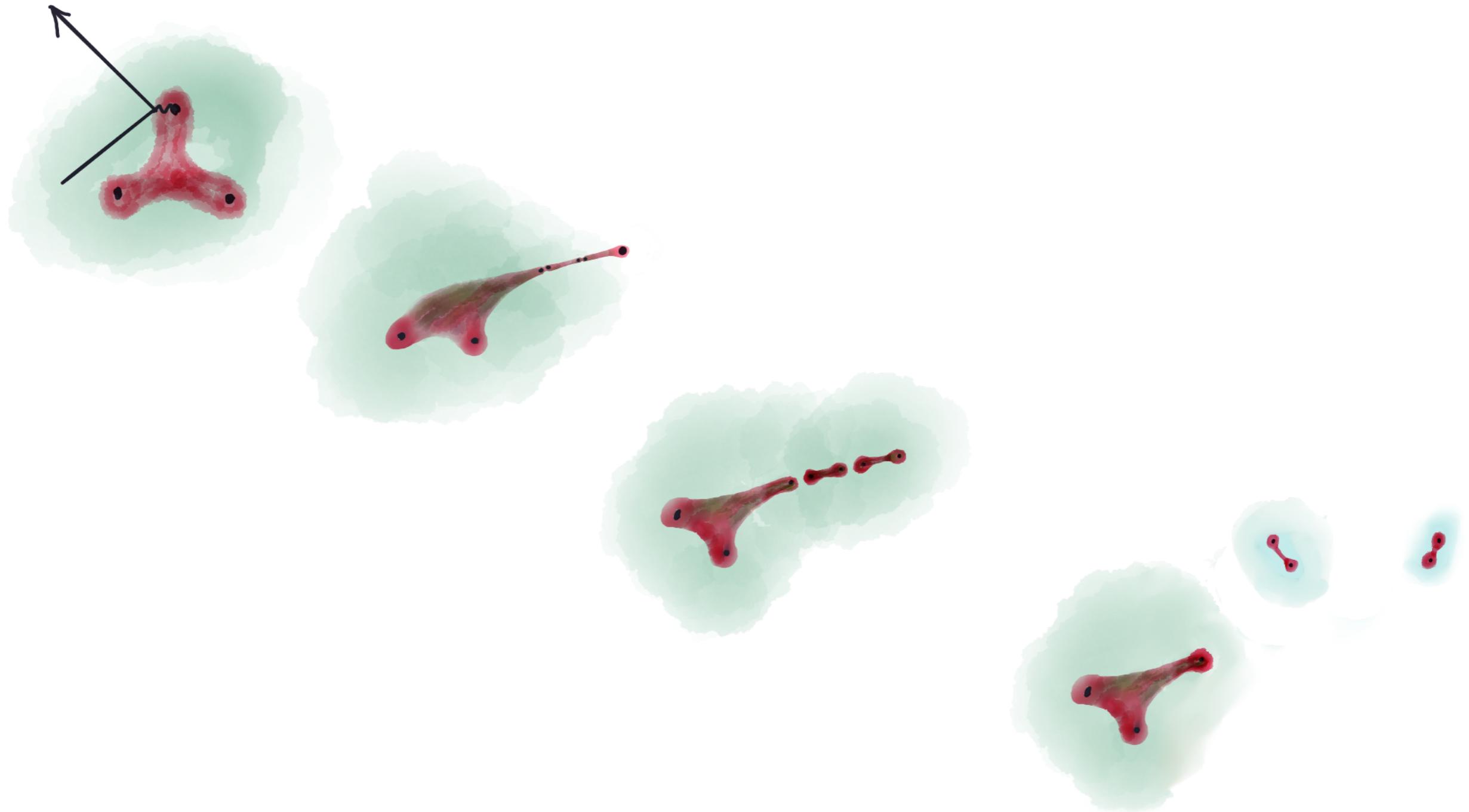
Compare to maximum for pions of 0.03 GeV²!

The **object passing through the medium is disruptive!
E.g., it is “large” (has an extended color field).**

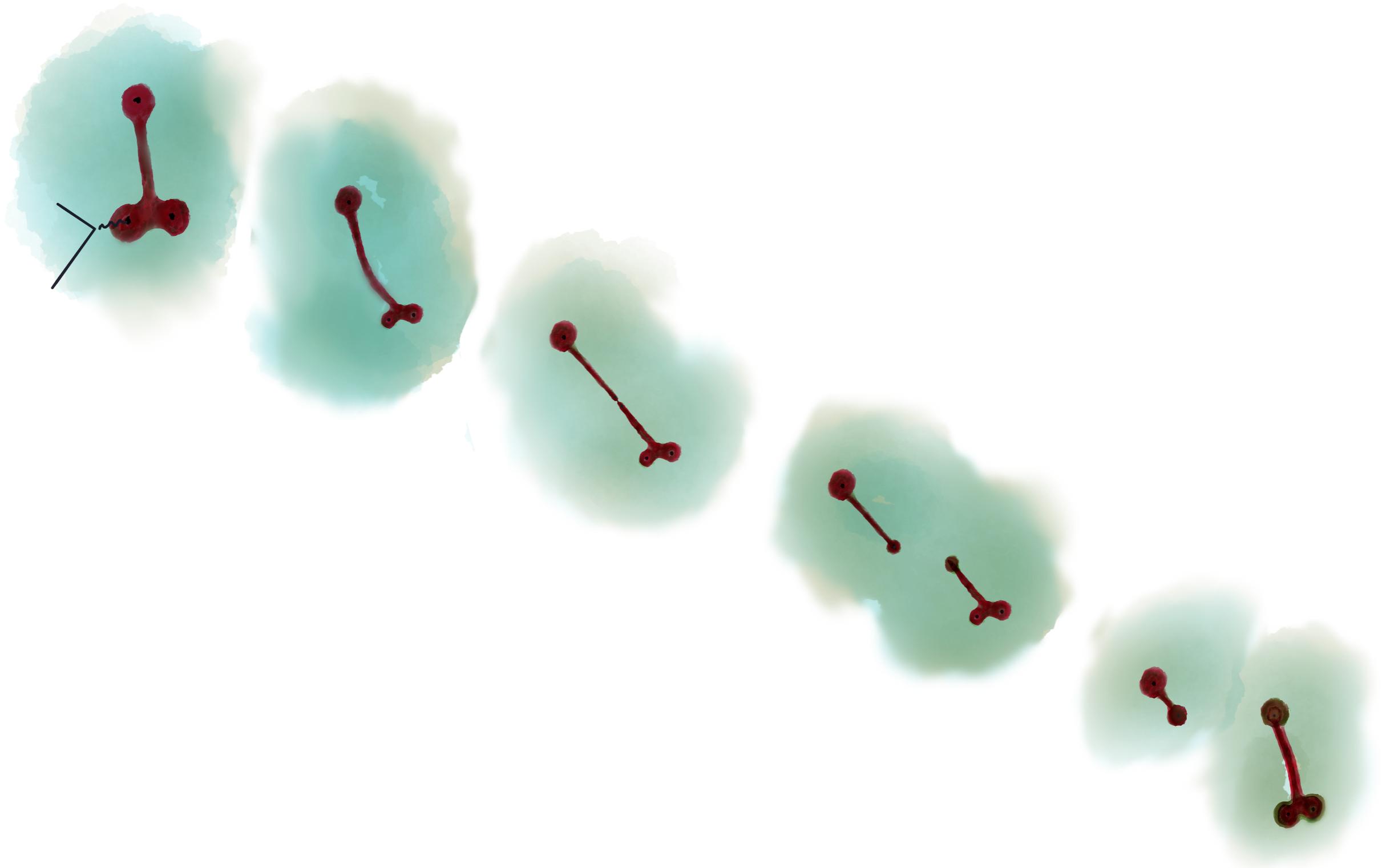
Could it be possible that the **virtual photon is absorbed by a diquark?**

Let's call this **Direct Diquark Scattering (DDS)**

Traditional Lund String Model picture of particle production from proton: Single Quark Scattering



Alternative Lund String Model picture of particle production from proton: Direct Diquark Scattering

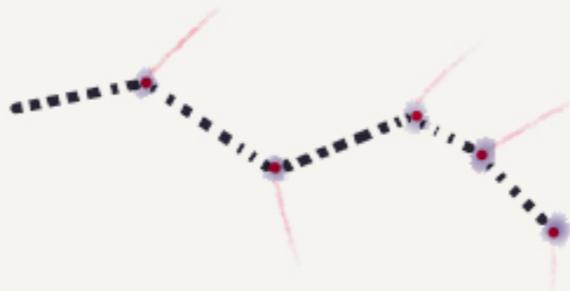
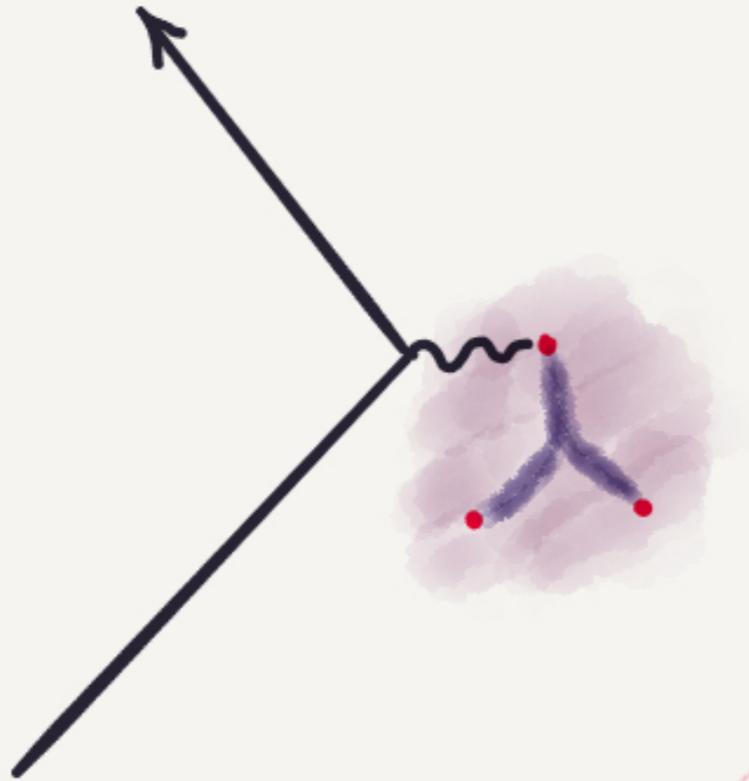


This DDS mechanism makes it a lot easier to form a proton. Making a proton in the Lund String Model is famously problematic.

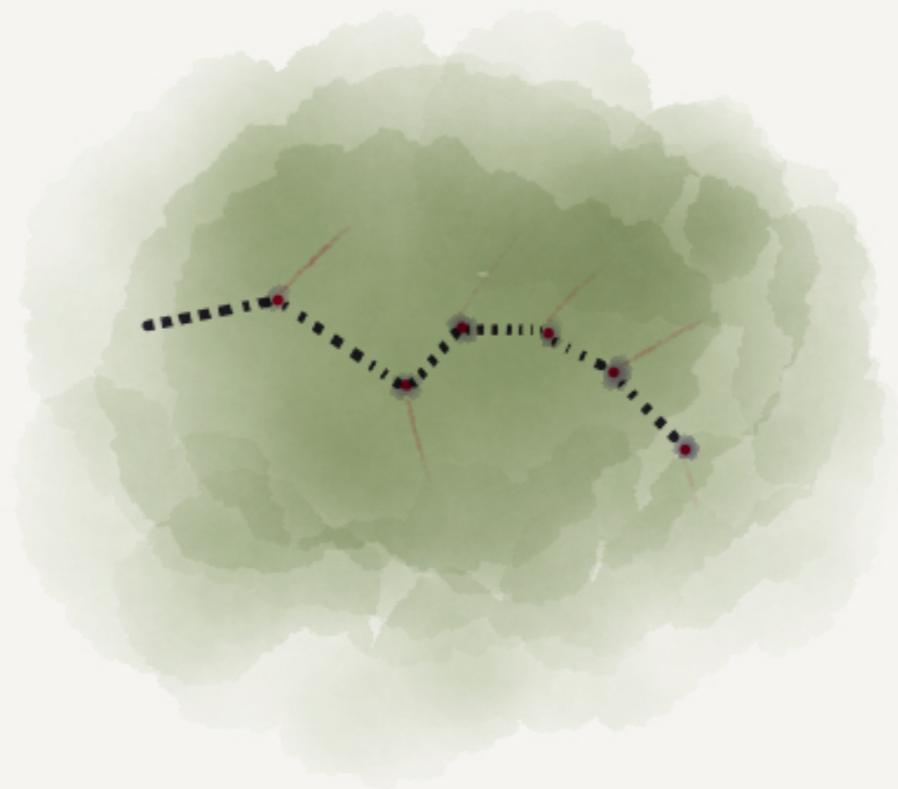
With nDIS baryon production, we will be able to gather a lot of evidence to test this idea.

Multiplicity ratio, p_T broadening, and correlations between hadrons will provide the evidence.

The p_T broadening by a single quark was seen to be at the level of 0.03 GeV^2 by HERMES: not much interaction with the nuclear medium.

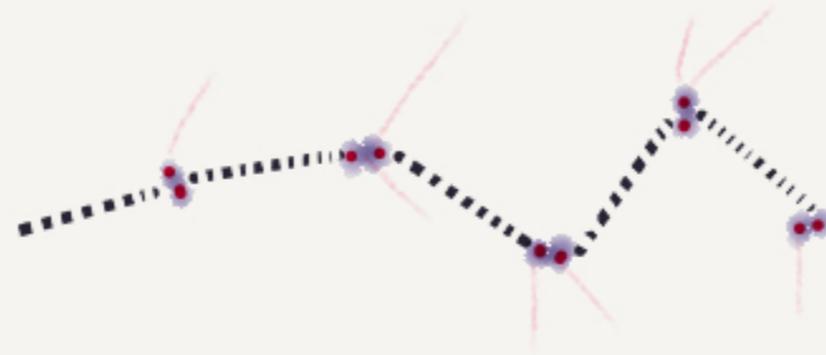
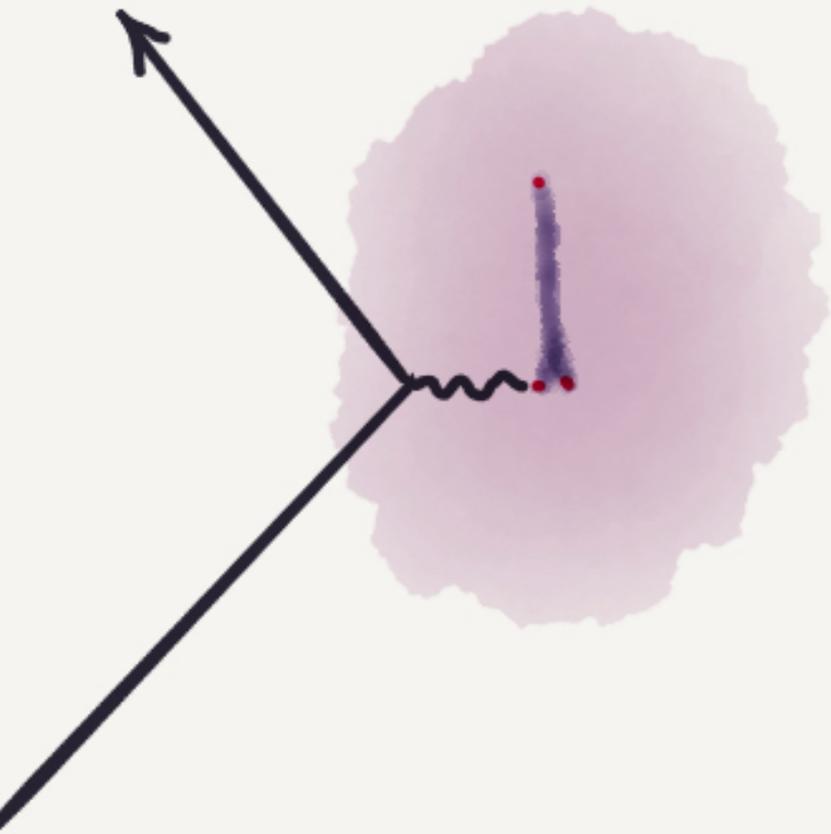


in vacuum

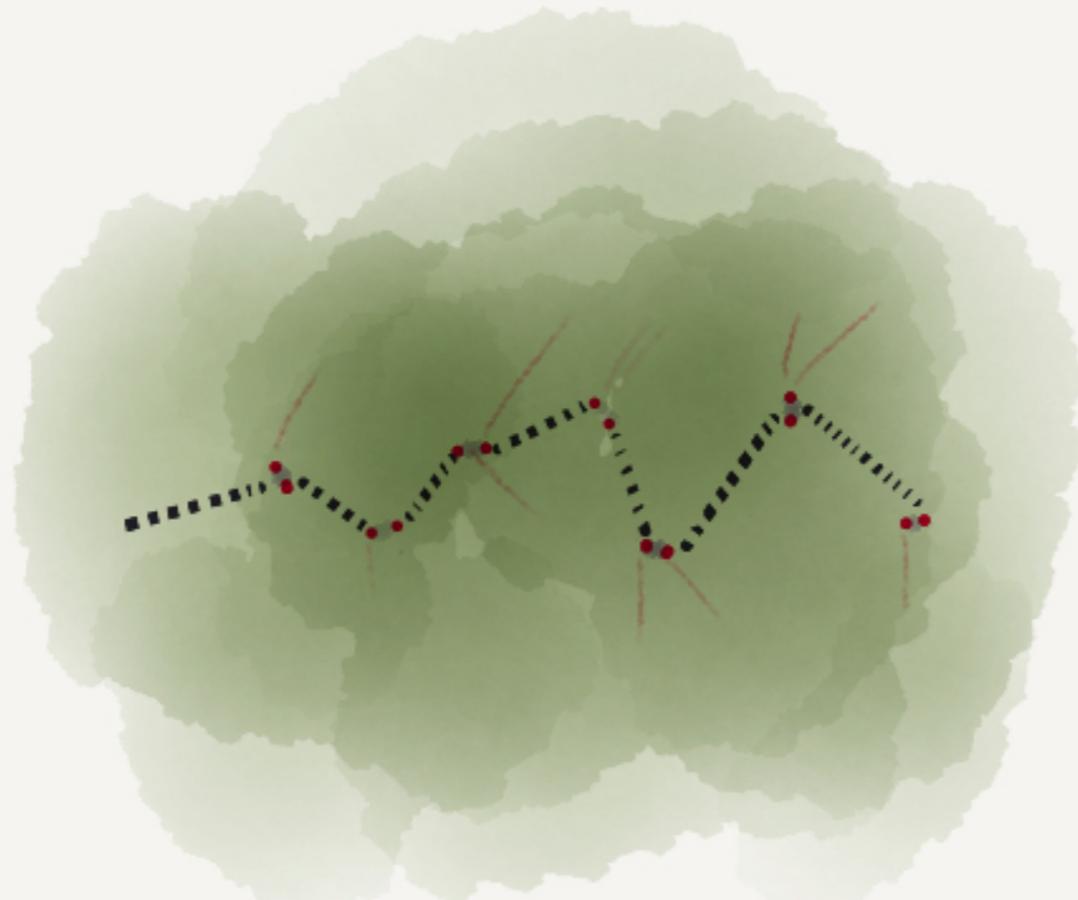


in medium

The p_T broadening by a diquark might be much larger: CLAS lambdas showed up to 0.3 GeV^2 .



in vacuum



in medium

Further tests of the Direct Diquark Scattering hypothesis with CLAS12 nDIS on baryons

Actively underway with existing 5 GeV data

<i>meson</i>	$c\tau$	mass	flavor content	<i>baryon</i>	$c\tau$	mass	flavor content
π^0	25 nm	0.13	$u\bar{u}d\bar{d}$	p	stable	0.94	ud
π^+, π^-	7.8 m	0.14	$u\bar{d}, d\bar{u}$	\bar{p}	stable	0.94	$\bar{u}\bar{d}$
η	170 pm	0.55	$u\bar{u}d\bar{d}s\bar{s}$	Λ	79 mm	1.1	uds
ω	23 fm	0.78	$u\bar{u}d\bar{d}s\bar{s}$	$\Lambda(1520)$	13 fm	1.5	uds
η'	0.98 pm	0.96	$u\bar{u}d\bar{d}s\bar{s}$	Σ^+	24 mm	1.2	us
ϕ	44 fm	1.0	$u\bar{u}d\bar{d}s\bar{s}$	Σ^-	44 mm	1.2	ds
f_1	8 fm	1.3	$u\bar{u}d\bar{d}s\bar{s}$	Σ^0	22 pm	1.2	uds
K^0	27 mm	0.50	$d\bar{s}$	E^0	87 mm	1.3	us
K^+, K^-	3.7 m	0.49	$\bar{u}s, \bar{d}s$	E^-	49 mm	1.3	ds

Baryon	$M^{e/l}$	M^{CI}	s^{r1}	s^{r2}	a_1^{r2}	a_2^{r2}	a_1^{r3}	a_2^{r3}	dom. corr.
p (B.5a)	0.94	0.94	0.89		-0.35	-0.14	0.25	0.098	$[ud]u$
Λ (B.5b)	1.12	1.06	0.67	0.59			-0.42	-0.16	$[ud]s$
Σ (B.5c)	1.19	1.20	0.87		-0.42	0.004	0.25	0.071	$[us]u$
Ξ (B.5d)	1.32	1.24	0.90		-0.29	-0.028	0.31	0.11	$[us]s$
Λ_c (B.5e)	2.29	2.50	0.21	0.86			-0.35	-0.32	$[uc]d - [dc]u$
Σ_c (B.5f)	2.45	2.53	0.48		-0.21	0.84	0.090	0.064	$\{uu\}c$
Ξ_c (B.5g)	2.47	2.66	0.22	0.84			-0.36	-0.34	$[uc]s - [sc]u$
Ξ'_c (B.5h)	2.58	2.68	0.50		-0.22	0.83	0.093	0.061	$\{us\}c$
Ω_c (B.5i)	2.70	2.83	0.51		-0.22	0.82	0.097	0.058	$\{ss\}c$

From Yin et al.

Baryon	$M^{e/l}$	M^{CI}	dom. corr.
p (B.5a)	0.94	0.94	$[ud]u$ ●
Λ (B.5b)	1.12	1.06	$[ud]s$ ●
Σ (B.5c)	1.19	1.20	$[us]u$
Ξ (B.5d)	1.32	1.24	$[us]s$
Λ_c (B.5e)	2.29	2.50	$[uc]d - [dc]u$
Σ_c (B.5f)	2.45	2.53	$\{uu\}c$? almost
Ξ_c (B.5g)	2.47	2.66	$[uc]s - [sc]u$
Ξ'_c (B.5h)	2.58	2.68	$\{us\}c$
Ω_c (B.5i)	2.70	2.83	$\{ss\}c$

**This suggests
a specific behavior
for DDS.**

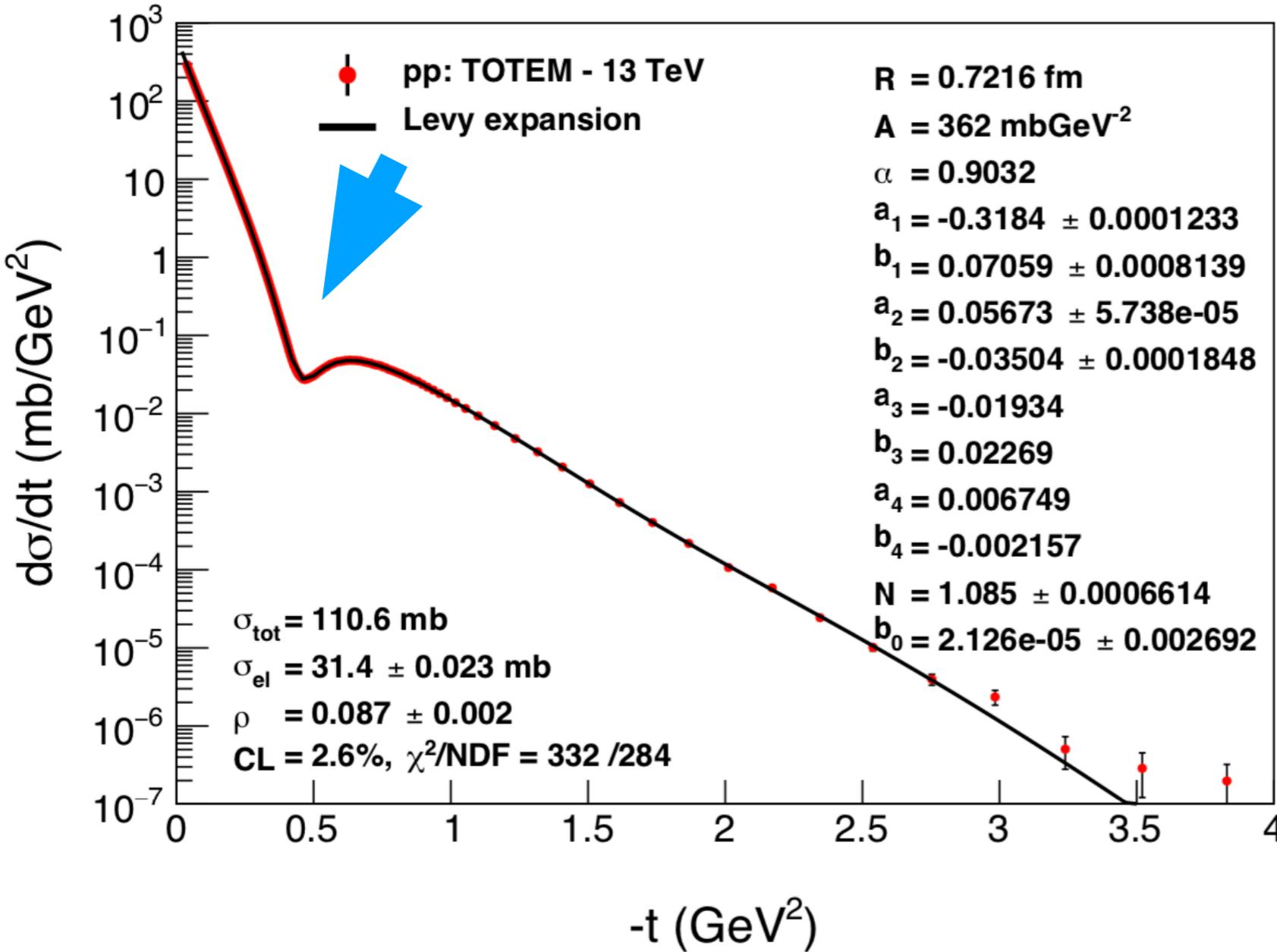
**Only p, n, lambda
can easily be formed
by DDS.**

**Prediction: proton
and lambda will
behave similarly; the
others will be
different.**

Diquarks have been invoked for hadron beam scattering

“Convergence properties of Lévy expansions: implications for Odderon and proton structure,”

T. Csörgő, R. Pasechnik, A. Ster,
<https://arxiv.org/pdf/1903.08235>



Having only one minimum implies there are only two internal substructures, such as quark-diquark.

- <https://arxiv.org/abs/1903.08235>
- <https://arxiv.org/abs/1902.00109>
- <https://arxiv.org/abs/1811.08913>
- <https://arxiv.org/abs/1807.02897>

Diquarks have been invoked for hadron beam scattering

To explain anomalies in proton production!

Breakstone et al. (following 2 slides) 1985 ISR data

<http://cds.cern.ch/record/158001/files/198503162.pdf>



EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

CERN/EP 85-30

5 March 1985

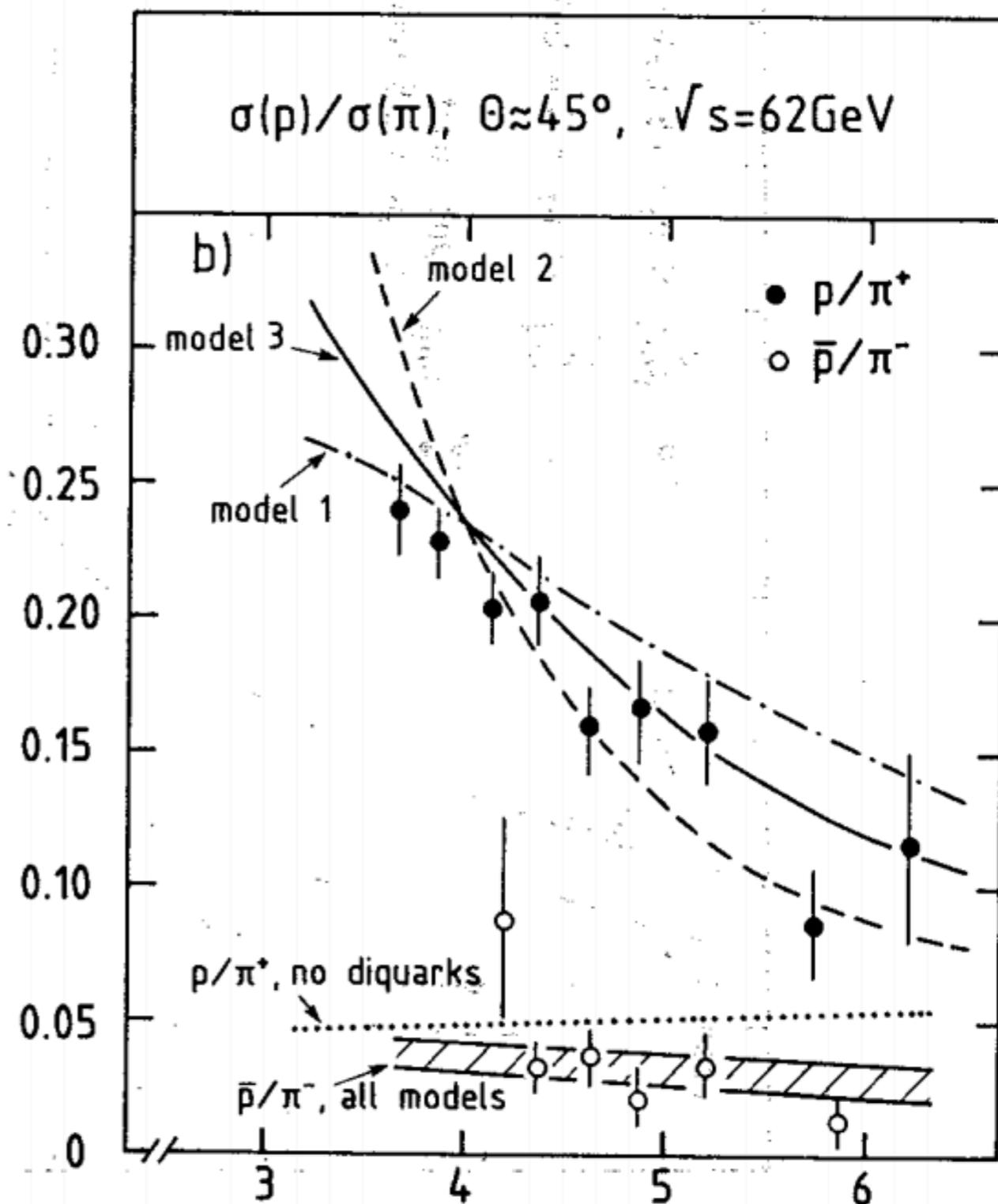
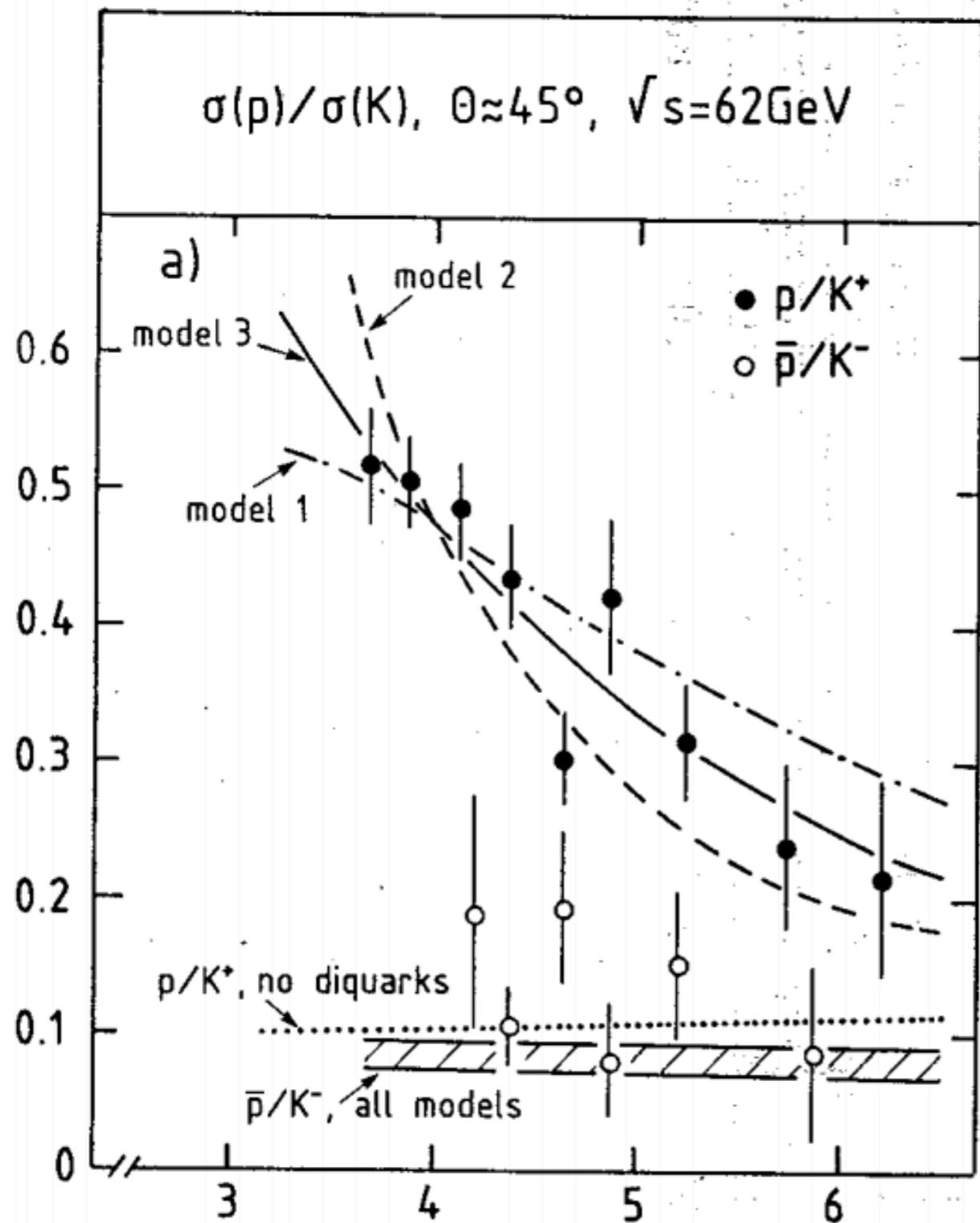
A DIQUARK SCATTERING MODEL FOR HIGH p_T PROTON PRODUCTION IN pp
COLLISIONS AT THE ISR

Ames-Bologna-CERN-Dortmund-Heidelberg-Warsaw Collaboration

A. Breakstone¹⁽⁺⁾, H.B. Crawley¹, G.M. Dallavalle⁵, K. Doroba⁶, D. Drijard³,
F. Fabbri³, A. Firestone¹, H.G. Fischer³, H. Frehse^{3(*)}, W. Geist^{3(**)},
G. Giacomelli², R. Gokieli⁶, M. Gorbics¹, P. Hanke⁵, M. Heiden^{3(**)},
W. Herr⁵, E.E. Kluge⁵, J.W. Lamsa¹, T. Lohse⁴, R. Mankel⁴, W.T. Meyer¹,
T. Nakada^{5(***)}, M. Panter³, A. Putzer⁵, K. Rauschnabel⁴, B. Rensch⁵,
F. Rimondi², M. Schmelling⁴, G. Siroli², R. Sosnowski⁶, M. Szczekowski³,
O. Ullaland³ and D. Wegener⁴

Breakstone et al.

<http://cds.cern.ch/record/158001/files/198503162.pdf>



p_T [GeV/c]

Breakstone et al.

<http://cds.cern.ch/record/158001/files/198503162.pdf>

Fig. 1

Conclusions

- A **very simple model** is able to successfully describe **meson production** in nDIS. In contrast, baryon data from HERMES and CLAS behave **qualitatively differently** from mesons.
- The hypothesis is that **Direct Diquark Scattering** may be the main mechanism for formation of protons and lambdas. **Scattering on nuclei** yields new insights.
- More **theoretical work** is needed to determine the feasibility and plausibility of this interpretation.
- The planned and approved CLAS12 **Color Propagation** program is ideal for testing these ideas: access to production of **nine long-lived baryons**.

Possible objections to the Direct Diquark Scattering hypothesis

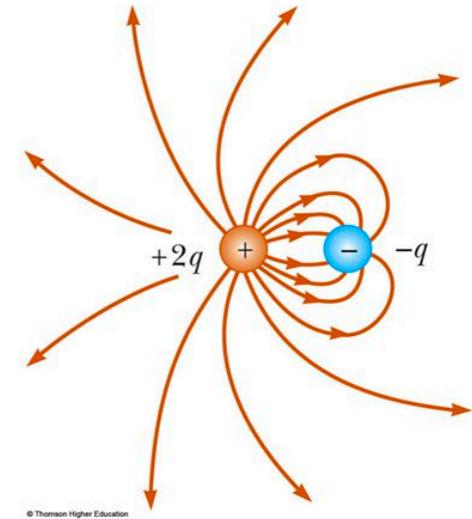
- What about “slingshot” mechanism?
- Hard to reach high z with that. We clearly see large p_T broadening up to high z .

Evidence supporting the Direct Diquark Scattering hypothesis

- **pT broadening of the Lambda is huge compared to that of any meson.**

Problem: how to hit a diquark?

- Scattering off an electric dipole field?
 - The ud system in close proximity presents an asymmetric electric dipole
 - This would leave the u and d without a large momentum imbalance
 - Clearly possible in classical picture; not sure how it translates to quantum picture
- Scattering off one quark in close proximity to another quark
 - Followed by gluon exchanges to keep momentum balance from getting too large
 - Smaller phase space, like LHC MPI's.



Alternative hypotheses

- **Quark recombination**

- Accepted as a mechanism needed to explain aspects of heavy ion collisions, such as J/psi production at low pT.
- Can explain excess hadron production, in principle.
- Detailed calculations are needed to see if it can work for lambda, proton, etc.
- A key feature of producing recombination is elevated temperatures + deconfined system. Unlikely for nDIS.

- **Instant proton/lambda formation**

- Might help to explain proton results, but not excess of Λ .