

On the spectrum of composite resonances

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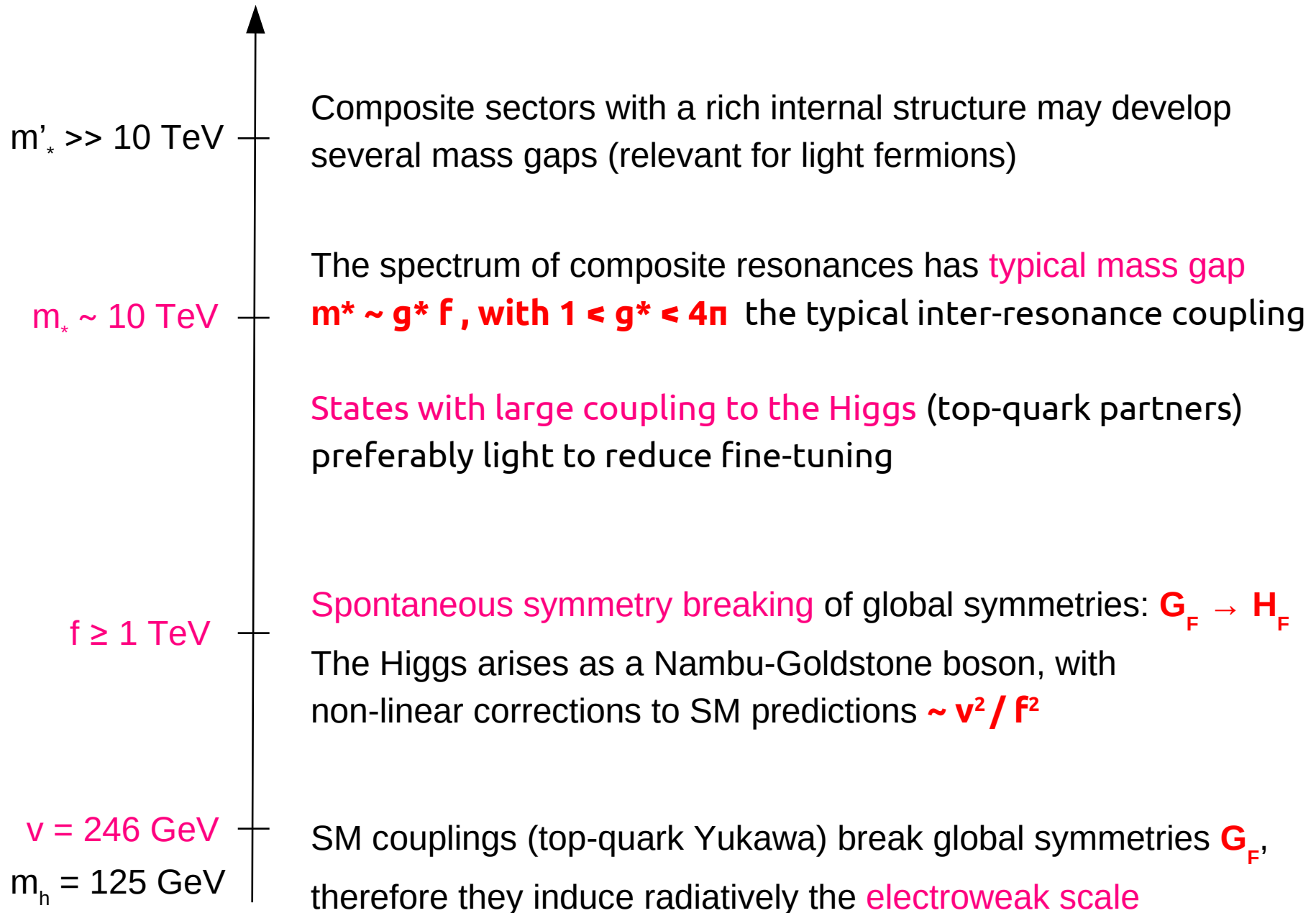
- * **Nicolas Bizot, MF, Marc Knecht, Jean-Loic Kneur** – 1610.09293, PRD95(2017)075006
Non-perturbative analysis of the spectrum of meson resonances in an ultraviolet-complete composite-Higgs model
- * **Daniel Elander, MF, Marc Knecht, Jean-Loic Kneur** – in preparation
Holographic models of composite Higgs in the Veneziano limit

LFC19 @ ECT*, Trento, 9-16 September 2019

Motivations & Outline

- *No new physics signals below the TeV scale: little hierarchy problem for any extension of the Standard Model ($m_h \sim 0.1\text{TeV}$)*
- *Large hierarchy problem (from TeV to Planck scale) still calls for an answer: the Higgs may be a composite object*
- *If the Higgs is composite, how heavy are the other resonances?*
- *Predictions require a definite ultraviolet completion: a new gauge theory of fermions, that confines at the TeV scale*
- *Estimate the spectrum of composite resonances in well-defined approximations: (I) non-perturbative QCD techniques
(II) gauge-gravity duality techniques*

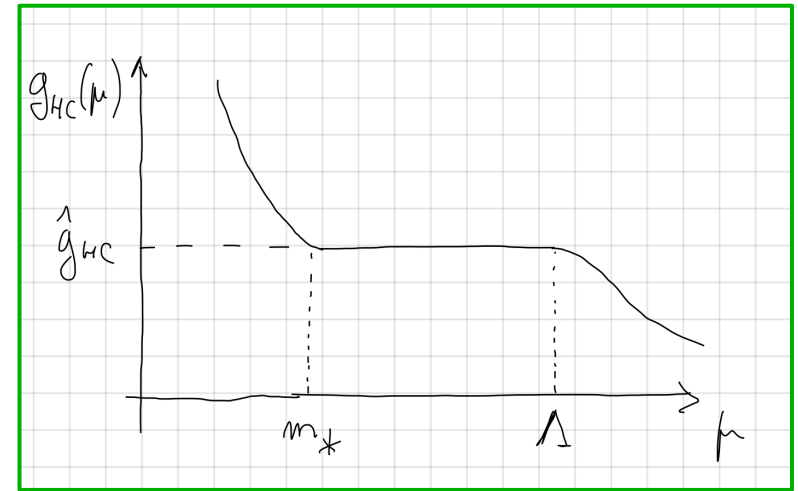
Scales in composite Higgs scenario



review:
Panico
Wulzer
2015

From the UV to the IR

Prototype: **asymptotically-free** gauge theory (hyper-colour), that enters a strongly-coupled, **walking regime** (approximate scale-invariance), and eventually confines and develops a **mass gap**



- **Partial Compositeness**: mixing SM fermions with composite operators may induce **hierarchy at IR scale m_* from anarchy at UV scale Λ**

D.B.Kaplan '91, Contino-Pomarol '04, ++

$$\mathcal{L}_{PC} = \lambda_i f_i \mathcal{O}_i + \dots$$

$$\lambda_i(m_*) \underset{\Delta_i > 5/2}{\simeq} \lambda_i(\Lambda) \left(\frac{m_*}{\Lambda} \right)^{\Delta_i - 5/2} \equiv g^* \epsilon_i$$

- This explains Yukawa hierarchies & suppresses flavour / CP violation
- Large **top-quark Yukawa** requires $3/2 \leq \Delta_t \lesssim 5/2$

Minimal UV-complete composite Higgs

- Hyper-Colour gauge theory: $G_{\text{HC}} = \text{Sp}(2N_c)$
- 4 Weyl fermions ψ^a in the fundamental of G_{HC} : flavour symmetry $G_F = \text{SU}(4)$
- Strong dynamics breaks spontaneously G_F to a subgroup $H_F = \text{Sp}(4) \supset \text{SU}(2)_w$
→ the Higgs emerges as a composite Goldstone
- **Unavoidably, the Higgs is not alone:** e.g. **several fermion-bilinear operators**

	Lorentz	$Sp(2N)$	$SU(4)$	$Sp(4)$
ψ_i^a	$(1/2, 0)$	\square_i	4^a	4
$\bar{\psi}_{ai} \equiv \psi_{aj}^\dagger \Omega_{ji}$	$(0, 1/2)$	\square_i	$\bar{4}_a$	4^*
Spin-0 mesons	$M^{ab} \sim (\psi^a \psi^b)$	1	6^{ab}	$5 + 1$
	$\bar{M}_{ab} \sim (\bar{\psi}_a \bar{\psi}_b)$	1	$\bar{6}_{ab}$	$5 + 1$
Spin-1 mesons	$a^\mu \sim (\bar{\psi}_a \bar{\sigma}^\mu \psi^a)$	1	1	1
	$(V^\mu, A^\mu)_a^b \sim (\bar{\psi}_a \bar{\sigma}^\mu \psi^b)$	$(1/2, 1/2)$	1	15_b^a

Two-point correlators

- The mass spectrum for each composite operator is determined by the poles of the associated two-point function

$$\Pi_V(q^2) \delta^{AB} (q_\mu q_\nu - \eta_{\mu\nu} q^2) = i \int d^4x e^{iq \cdot x} \langle \text{vac} | T \{ \mathcal{J}_\mu^A(x) \mathcal{J}_\nu^B(0) \} | \text{vac} \rangle$$

$$\mathcal{J}_\mu^A = \Omega_{ij} \bar{\psi}_i \bar{\sigma}_\mu T^A \psi_j \quad \Pi_V(q^2) \underset{\text{large } N_C}{\simeq} \sum_n \frac{f_{Vn}^2}{q^2 - m_{Vn}^2}$$

- The symmetry structure determines
 - quantum numbers of the resonances
 - qualitative dependence of masses on symmetry-breaking parameters
 - spectral sum rules relating S-P and V-A masses and decay constant

$$\begin{array}{ll} \text{scalars : } \sigma + S^{\hat{A}} \sim 1 + 5 & \text{pseudoscalars : } \eta' + G^{\hat{A}} \sim 1 + 5 \\ \text{vectors : } V_\mu^A \sim 10 & \text{axialvectors : } a_\mu + A_\mu^{\hat{A}} \sim 1 + 5 \end{array}$$

- To be quantitative, need to model the non-perturbative dynamics

Spectrum of mesons à la NJL

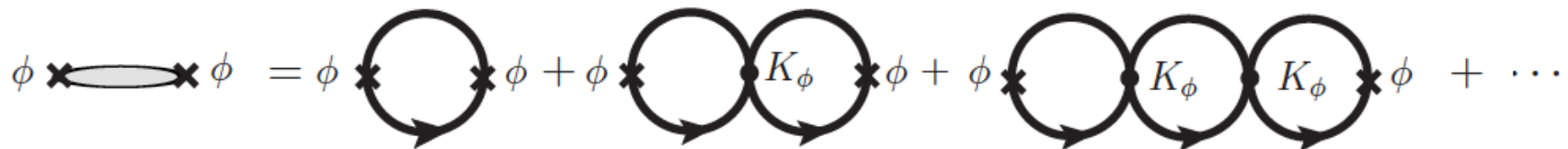
Bizot, Frigerio, Knecht, Kneur '16

- Nambu-Jona Lasinio approximation of strong dynamics: 'decouple' hypergluons to induce effective 4-fermion interactions

$$\mathcal{L}_{scal}^{\psi} = \frac{\kappa_A}{2N} (\psi^a \psi^b) (\bar{\psi}_a \bar{\psi}_b) - \frac{\kappa_B}{8N} [\epsilon_{abcd} (\psi^a \psi^b) (\psi^c \psi^d) + h.c.]$$

Barnard-Gherghetta
-Sankar Ray '13

- A non-zero mass-gap is induced $\langle \psi^a \psi^b \rangle \neq 0 \Rightarrow SU(4) \rightarrow Sp(4)$
- One can resum constituent fermion loops (at leading order in $1/N_c$) that contribute to the two-point correlators



$$\bar{\Pi}_{\phi}(q^2) \equiv \frac{\tilde{\Pi}_{\phi}(q^2)}{1 - 2K_{\phi} \tilde{\Pi}_{\phi}(q^2)}$$

A pole develops, thus defining the meson mass

Meson masses in units of f

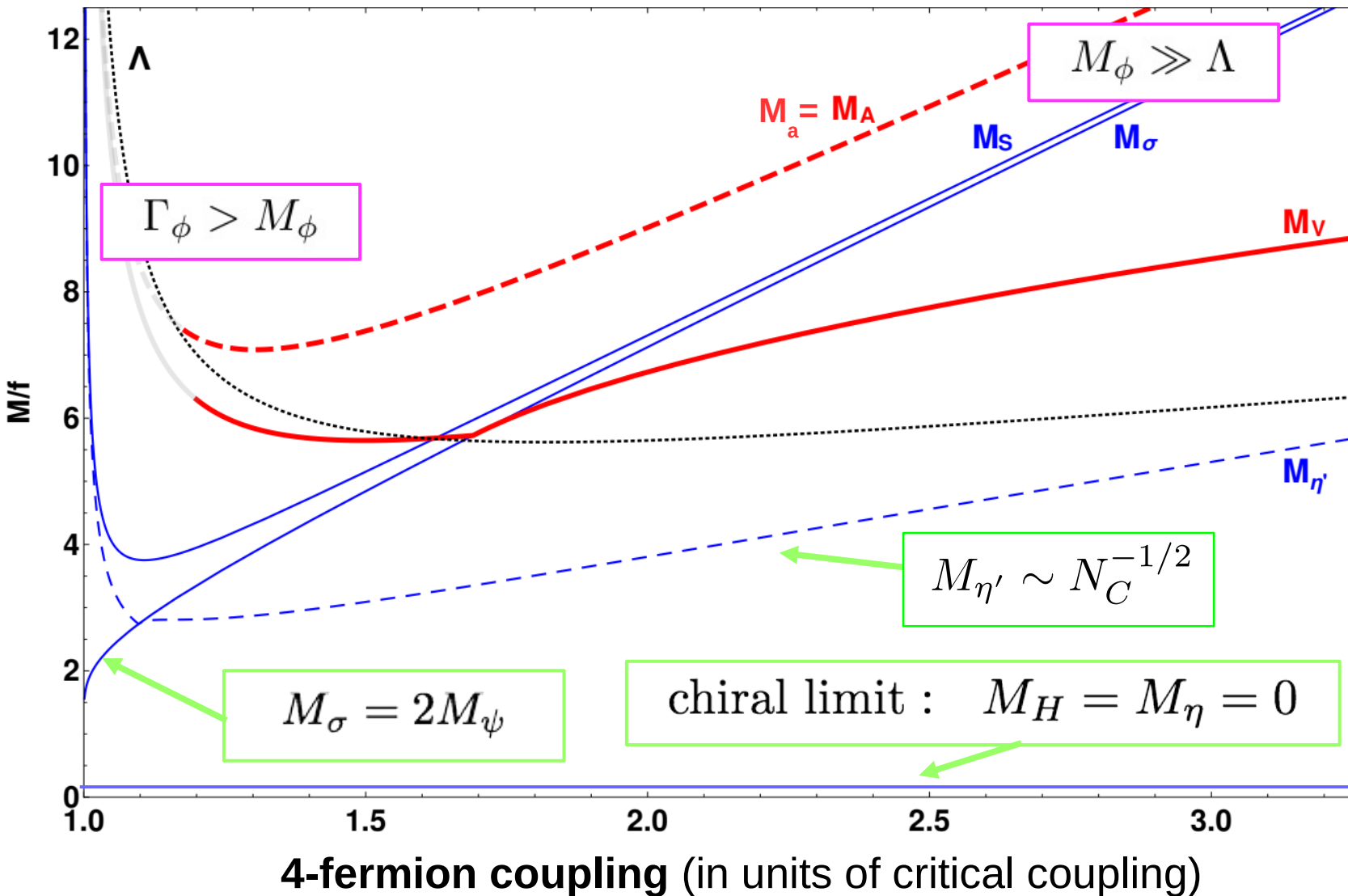
Bizot, Frigerio, Knecht, Kneur '16

spin-0 & spin-1 operators can be related in the NJL approximation

$$f \sim N_C^{1/2}$$

$$M \sim N_C^0$$

Here $N_C = 4$



4-fermion coupling (in units of critical coupling)

Looking for top partners

- Top-quark Partial Compositeness:
need coloured, spin-1/2 composite resonances
- In $Sp(2N_c)$ theories $(\psi_i \psi_j \psi_k)$ cannot be contracted into a hypercolour-singlet (the only invariant tensor is $\Omega_{ij} = -\Omega_{ji}$)
- Need to introduce **new constituent fermions X** to allow for $(\psi \psi X)$

$$X^f \sim \begin{array}{|c|} \hline \square \\ \hline \square \\ \hline \end{array} \quad X_{ij}^f = -X_{ji}^f \quad X_{ij}^f \Omega_{ji} = 0$$

Barnard, Gherghetta,
Sankar Ray, '13

- **Flavour group must also contain colour:**

$$G_F \rightarrow H_F \supset SU(3)_c \times SU(2)_w \times U(1)_y$$

- **Asymptotic freedom** prefers a single X and many flavours for ψ :

$$\psi_i, \quad i = 1, \dots, 2N_F \quad : \quad G_F = SU(2N_F) \rightarrow Sp(2N_F), \quad N_F \geq 4$$

Characterising spin-1/2 resonances

Painful group theory (generalisation of QCD)...

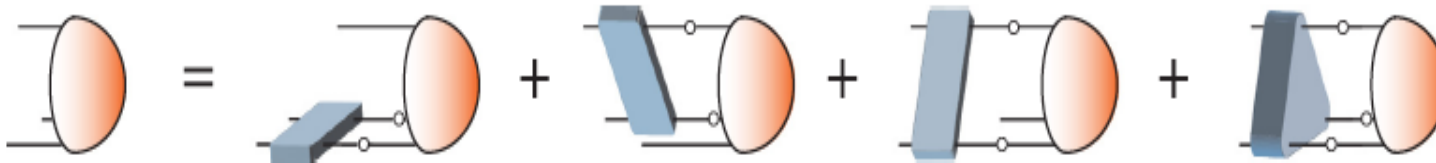
$$\mathcal{B}_1^{ab} = (\psi^a \psi^b X) , \quad \mathcal{B}_2^{ab} = (\psi^a \psi^b \bar{X}) , \quad \mathcal{B}_b^a = (\psi^a \bar{\psi}_b X)$$

Easy to identify flavour-components with the top-quark quantum numbers.

As for mesons, mass spectrum is given by poles of two-point functions:

$$\langle \mathcal{B}(q) \bar{\mathcal{B}}(-q) \rangle$$

Computation of the mass spectrum à la Nambu-Jona Lasinio is possible, via a laborious resummation in two steps: (diquark+quark)

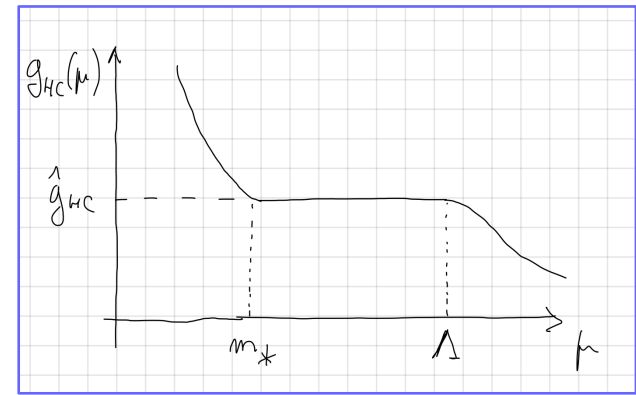


Eichmann et al., PPNP 91 (2016) 1

Preliminary results [Bizot,Kneur] are reasonable,
but several approximations hard to control...

Gauge-gravity duality

à la Daniel Elander



- The HC sector **close to a fixed point** : an approximate CFT
- The CFT (with N_c and $\lambda = g_c^2 N_c$ large) has a **holographic description as gravity in 5-dim AdS** (in the classical & weakly-coupled limit)

Maldacena '97

$$ds^2 = dr^2 + e^{2r} dx_{1,3}^2$$

- **Operator O_ϕ** in given rep of global $G_F \leftrightarrow$
 \leftrightarrow **5-dim field Φ** in same rep of gauged G_F (and also same spin)
- **Bulk scalar $\Phi(r)$ with non-flat profile back-reacts on the metric:**
 CFT loses scale-invariance and may develop a mass gap m_* \leftrightarrow
 \leftrightarrow Gravity loses AdS geometry, acquiring a warp factor $A(r) \neq r$
- **Spontaneous SB** by $\langle O_\phi \rangle \neq 0$: massless dilaton & goldstones
- **Explicit SB** by $\Phi(r \rightarrow \infty) \neq 0$: non-zero β -functions, no light scalars

The role of large N_F

- G_F must contain SM symmetries : need for $N_F \gg 1$
Light resonances require N_C not too large ($f \geq 1$ TeV and $m_*^2 \sim f^2 / N_C$)
- CFT correlators $\leftrightarrow S_{bulk}$ correlators : same scaling with N_C and N_F

$$\begin{aligned} \langle G_{ij} G_{ij} \rangle &\sim N_C^2 & \Leftrightarrow & S_{bulk}[R] \propto N_C^2 \\ \langle \psi_i^a \psi_i^a \rangle &\sim N_C N_F & \Leftrightarrow & S_{bulk}[\text{Tr } \Phi_\psi^{ab}] \propto N_C N_F \end{aligned}$$

- If $x_F = N_F/N_C \sim 1$, one cannot treat the flavour sector as a probe on top of a fixed background (e.g. AdS) :
back-reaction important in the Veneziano limit (large N_C , x_F constant)
- The profile $\sigma(r) = \text{Tr}[\Phi(r)]/N_F$ may relate the two IR scales:
 - the end of geometry r_{IR} corresponds to the mass gap m_*
 - the vev $\langle O_\sigma \rangle$ controls the decay constant f of Goldstones
 Potentially more predictive than AdS models with an IR brane !

Gravity-scalar background

Elander, Frigerio,
Knecht, Kneur,
preliminary

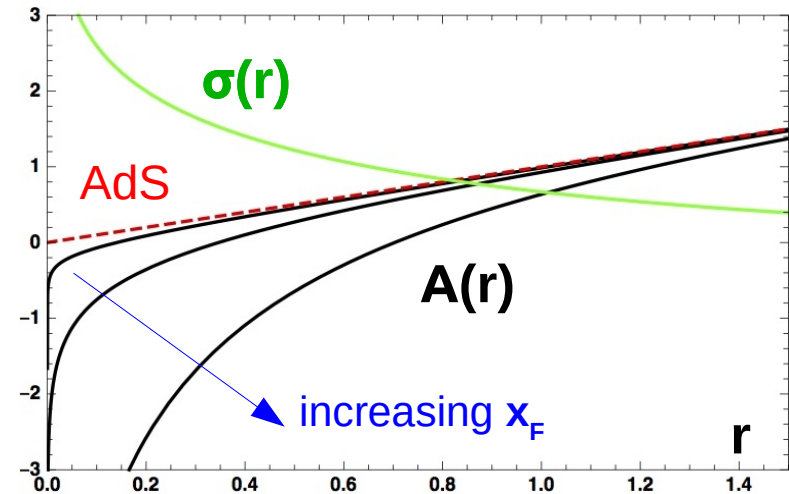
$$ds^2 = g_{MN} dx^M dx^N = dr^2 + e^{2A(r)} dx_{1,3}^2$$

$$S_{bulk} = N_C^2 \int d^5x \sqrt{-g} \left[\frac{R}{4} - \frac{\Lambda}{2} - x_F \left(\frac{1}{2} g^{MN} \partial_M \sigma \partial_N \sigma + V(\sigma) \right) \right]$$

Girardello, Petrini,
Porrati, Zaffaroni '99

Choose a specific form of V
inspired by some top-down models
(relevant for the detailed **behaviour in the IR**)

$$\begin{cases} \sigma(r) = \frac{1}{2} \sqrt{\frac{3}{\Delta}} \log \frac{1 + e^{-\Delta r}}{1 - e^{-\Delta r}} \underset{r \rightarrow \infty}{\sim} \sqrt{\frac{3}{\Delta}} e^{-\Delta r} \\ A(r) = r + \frac{x_F}{2\Delta} \log(1 - e^{-2\Delta r}) \underset{r \rightarrow \infty}{\sim} r \end{cases}$$



The UV behaviour of the scalar controls the deformation of the CFT

$$\sigma(r) \underset{r \rightarrow \infty}{\simeq} (\sigma_- e^{-\Delta_- r} + \sigma_+ e^{-\Delta_+ r})$$

$$\Delta_{\pm} = 2 \pm \sqrt{4 + m_{\sigma}^2}$$

$$V(\sigma) \underset{r \rightarrow \infty}{\simeq} -\frac{1}{2} \Delta(4 - \Delta) \sigma^2 + \dots$$

$0 < \Delta < 2$: ESB by $\Delta \mathcal{L}_{CFT} \sim \mathcal{O}_{\sigma} \sigma_-$
 $2 < \Delta < 4$: SSB by $\langle O_{\sigma} \rangle \sim \sigma_+$

Holography for two-point functions

- Expand S_{bulk} around the background to quadratic order in the field fluctuations, for any bulk field (spin-0, 1/2, 1, 2)
- E.o.m. linear in the fluctuations can be solved, to determine $S_{\text{bulk}}^{\text{on-shell}}$

$$\langle \mathcal{O}_1 \mathcal{O}_2 \rangle \leftrightarrow \lim_{r \rightarrow \infty} \frac{\delta^2 S_{\text{bulk}}^{\text{on-shell}}[\phi_i(r)]}{\delta \phi_1(r) \delta \phi_2(r)}$$

Deformed-CFT: poles of two-point functions are the resonance masses



Fluctuations satisfy appropriate UV boundary conditions only for discrete values of q^2
(equivalently: select KK mode masses)

- The SSB scale f is defined by the residue, at $q^2=0$, of the axial-vector transverse correlator

Elander, Frigerio, Knecht, Kneur, preliminary

$$\langle J^\mu(q) J^\nu(-q) \rangle = - \lim_{r \rightarrow \infty} \frac{\delta^2 S_{\text{bulk}}^{\text{on-shell}}}{\delta A_\mu(-q, r) \delta A_\nu(q, r)} \supset \lim_{r \rightarrow \infty} \left[e^{2A(r)} P^{\mu\nu} \frac{\partial_r A_\rho(q, r)}{A_\rho(q, r)} \right]$$

Spectrum of resonances - Bosons

Elander, Frigerio, Knecht, Kneur, preliminary

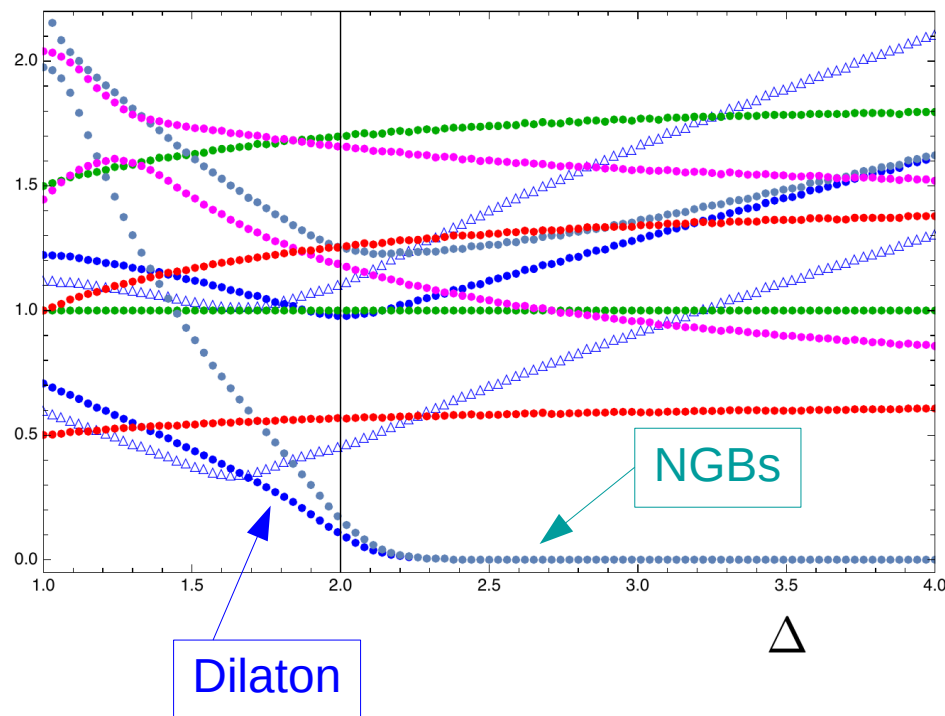
The masses of spin-0,1,2 resonances crucially depend on the operator anomalous dimension Δ

Other parameters are fixed to $g_5 = 5$ [the 5-dim gauge coupling]

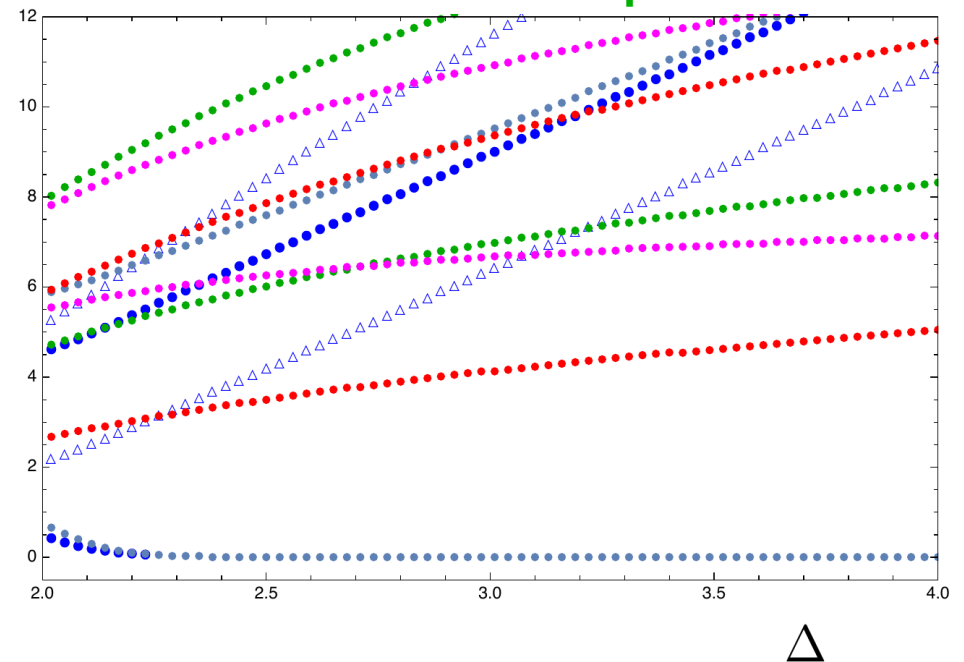
and $x_F = 1$ [number of flavours / number of colours]

Scalars
Pseudo-scalars
Vectors
Axial-vectors
Spin-two

$$m/m_{\text{glueball,spin-2}}^{(1)}$$



$$m/f$$



- **Dilaton mass may be lifted** by flavour-singlet breaking of scale-invariance, e.g. XX operator
- Scaling of f with N_C and N_F known, but **f normalisation** depends on specific top-down model

Spectrum of resonances - Fermions

Elander, Frigerio,
Knecht, Kneur,
preliminary

Fermionic operator B (top partner) \leftrightarrow Dirac fermion Ψ in the bulk

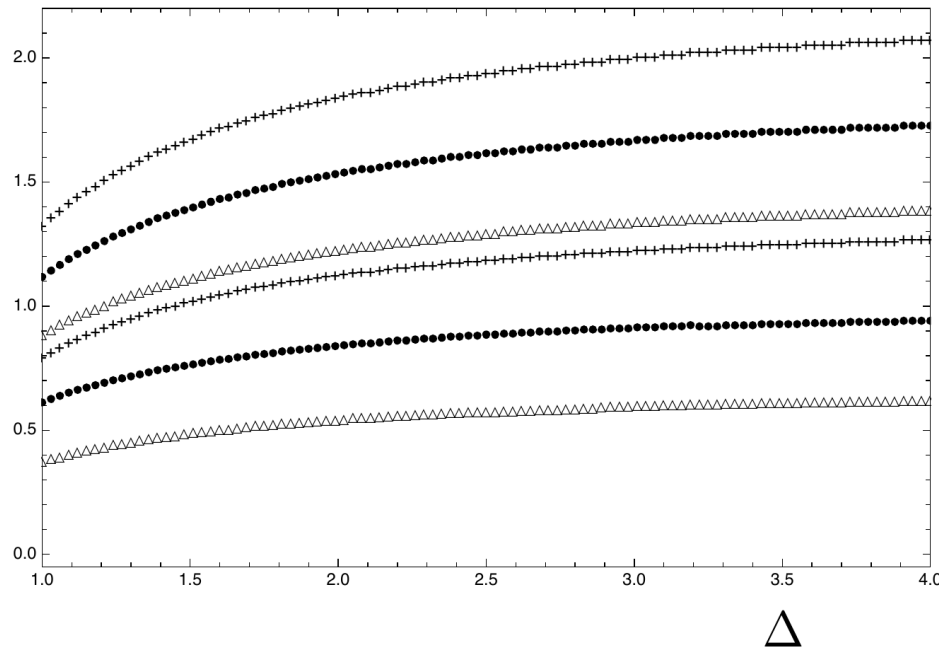
The bulk mass m_ψ is related to the operator scaling dimension Δ_ψ

Large top Yukawa requires marginal / relevant operator: $\Delta_\psi \leq 5/2$

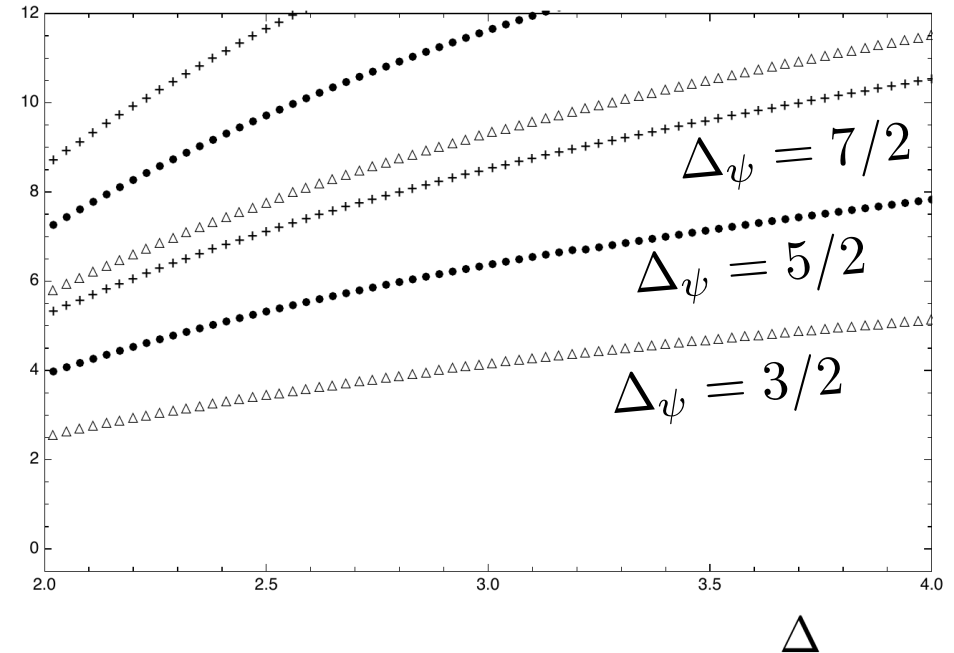
$$\mathcal{L} \supset \lambda_{t_L} \overline{\Psi}_{t_L} \mathcal{B}_{t_L}$$

$$\Delta_{t_L} = \frac{3}{2} + \left| m_{t_L} + \frac{1}{2} \right|$$

$m/m_{\text{glueball, spin-2}}^{(1)}$



m/f



Searching for scenarios with a fermion resonance parametrically light ...

Summary

- A composite Higgs does not come alone
- Higgs & top composite partners may well be within reach
- Modeling non-perturbative dynamics requires radical assumptions, but it appears to be very instructive
- A few rationales for lightness:
 - *SSB scale \gg ESB scale: light Goldstones, dilaton, ...*
 - *Anomaly-matching : light η' , composite chiral fermions, ...*
 - *Others ?*
- Quantitative estimates are model-dependent