

# Top-quark production at NNLO using $q_T$ subtraction

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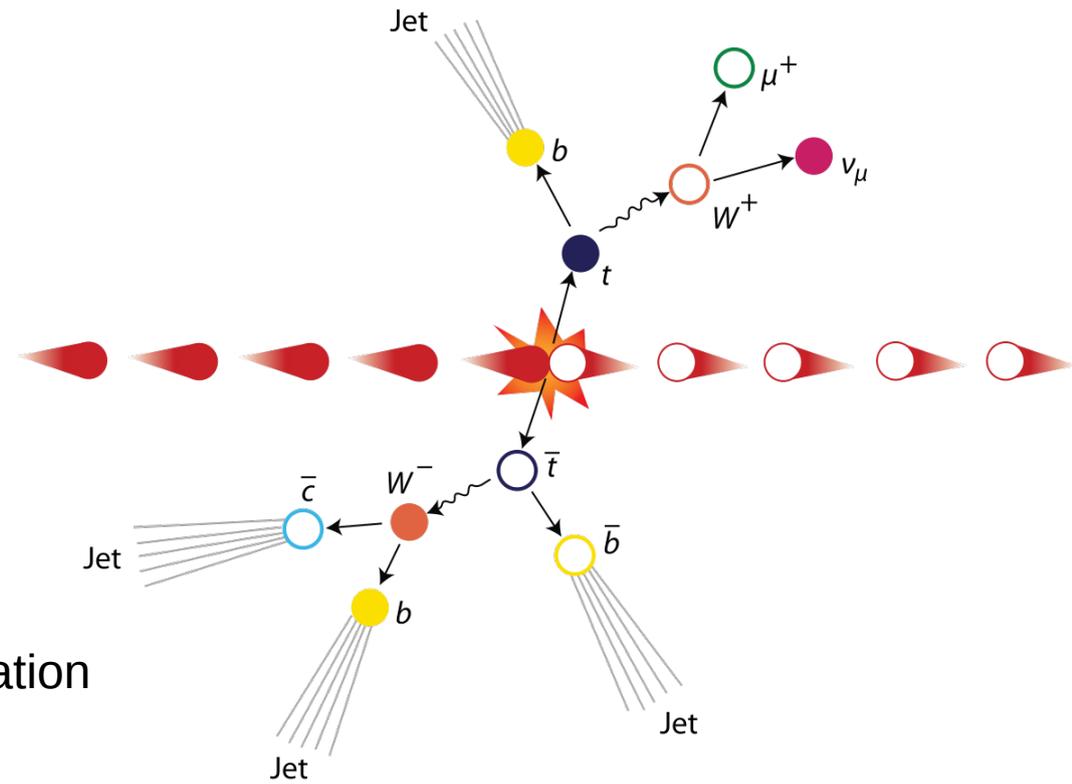
In collaboration with S. Catani, S. Devoto, M. Grazzini, S. Kallweit, H. Sargsyan

# Outline

- **Introduction**
- **NNLO corrections with  $q_T$  subtraction**
- **Extension to heavy quark production**
- **Results and comparison with data**
- **Conclusions and outlook**

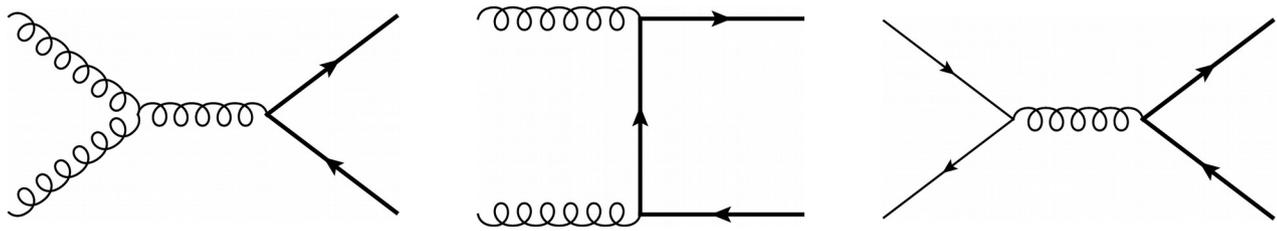
# The top quark

- Heaviest particle in the SM
- Strongest coupling to Higgs boson
- Only quark that decays before hadronization
- Possible window to new physics
- Important background in many searches
- Standard candle at the LHC (triggering, tracking, b-tagging, energy and jet calibration)

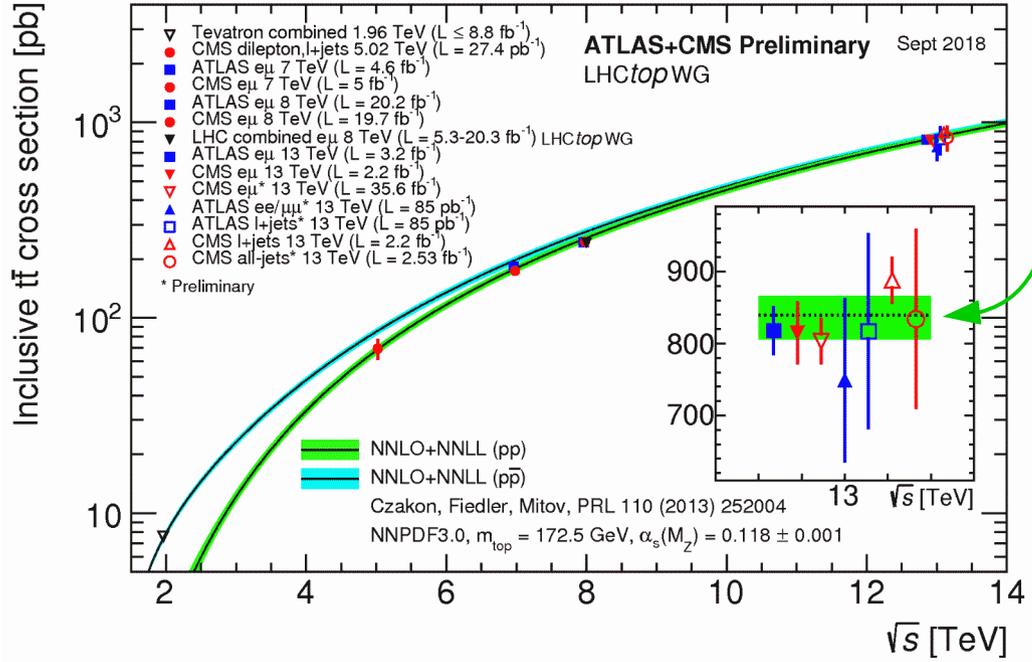


# Top-quark pair production

Main production mechanism of top quarks at hadron colliders



- Approx. 3 times larger than single-top production
- About **15  $t\bar{t}$**  pairs produced **per second** at the LHC!



Impressive experimental precision

(see talk by D. Melini)

Very precise theoretical predictions are needed

Cross section known at NNLO QCD + NLO EW + resummation

(see talk by D. Scott)

Why a new NNLO QCD calculation?

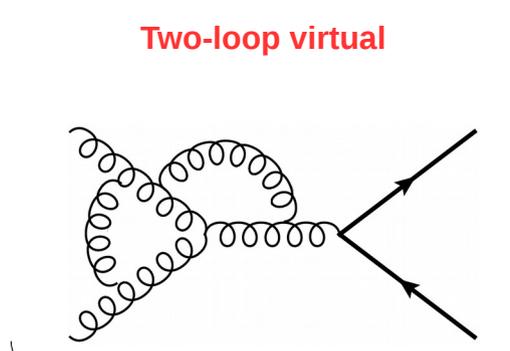
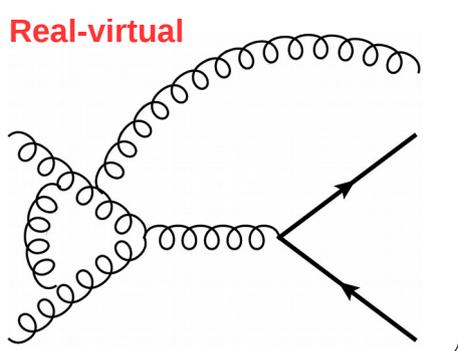
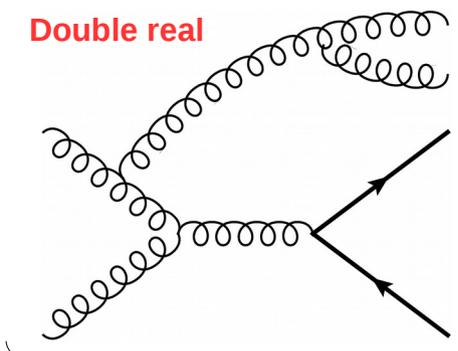


- Very difficult calculation: only one group able to complete it until now
- Independent check is always useful!
- No publicly available tool to produce NNLO distributions yet

Bärnreuther, Czakon, Mitov (2012)  
Czakon, Mitov (2012)  
Czakon, Fiedler, Mitov (2013)  
Czakon, Fiedler, Heymes, Mitov (2015,2016)

# $t\bar{t}$ production at NNLO

We need the scattering amplitudes:



Fast and stable evaluation with OpenLoops2

Cascioli et al. (2012), Buccioni et al. (2018)

Available numerically

Czakon (2008)  
Barnreuther, Czakon, and Fiedler (2013)

... but we also need to handle their divergencies:

$$\Delta\sigma_{\text{NNLO}} = \int_{F+2} d\sigma_{\text{RR}} + \int_{F+1} d\sigma_{\text{RV}} + \int_F d\sigma_{\text{VV}}$$

No  $\epsilon$  poles, singular in (double) unresolved limit
Explicit  $1/\epsilon^2$  poles, singular in unresolved limit
Explicit  $1/\epsilon^4$  poles, no further PS singularities

↓ Finite
 ↓ Individually divergent contributions

We need **subtraction methods** that allow us to perform these calculations numerically

# Subtraction methods

**NLO:** solved, Dipole subtraction, FKS, ...

**NNLO:**

- Antenna [Gehrmann-de Ridder, Gehrmann, Glover '05, ...]
- CoLoRFulNNLO [Somogyi, Trócsányi, Del Duca '05, ...]
- $q_T$  subtraction [Catani, Grazzini '07, ...]
- STRIPPER [Czakon '10, '11]
- Projection-to-Born [Cacciari et al. '15]
- N-jettiness [Gaunt et al. '15; Boughezal et al. '15, ...]
- Nested soft-collinear [Caola, Melnikov, Roentsch '17]
- Geometric [Herzog '18]
- Local analytic sector [Magnea et al. '18]

# $q_T$ subtraction

Originally developed for the hadroproduction of **colourless** final states Catani, Grazzini (2007)

Slicing method, slicing parameter:  $q_T$  (transverse momentum of final state  $F$ )

## Master formula:

$$d\sigma_{\text{NNLO}}^F = \mathcal{H}_{\text{NNLO}}^F \otimes d\sigma_{\text{LO}}^F + \left[ d\sigma_{\text{NLO}}^{F+\text{jet}} - d\sigma_{\text{NNLO}}^{\text{CT}} \right]$$

Process dependent hard-collinear function

Restores correct normalization, includes the 2-loop corrections

NLO  $F$ +jet cross section (using dipole subtraction)

Universal counterterm to cancel  $q_T \rightarrow 0$  divergencies

Based on known low  $q_T$  behaviour from resummation

Difference computed with a cut on  $r = q_T/M$

General form of hard-collinear function known at NNLO for colourless  $F$

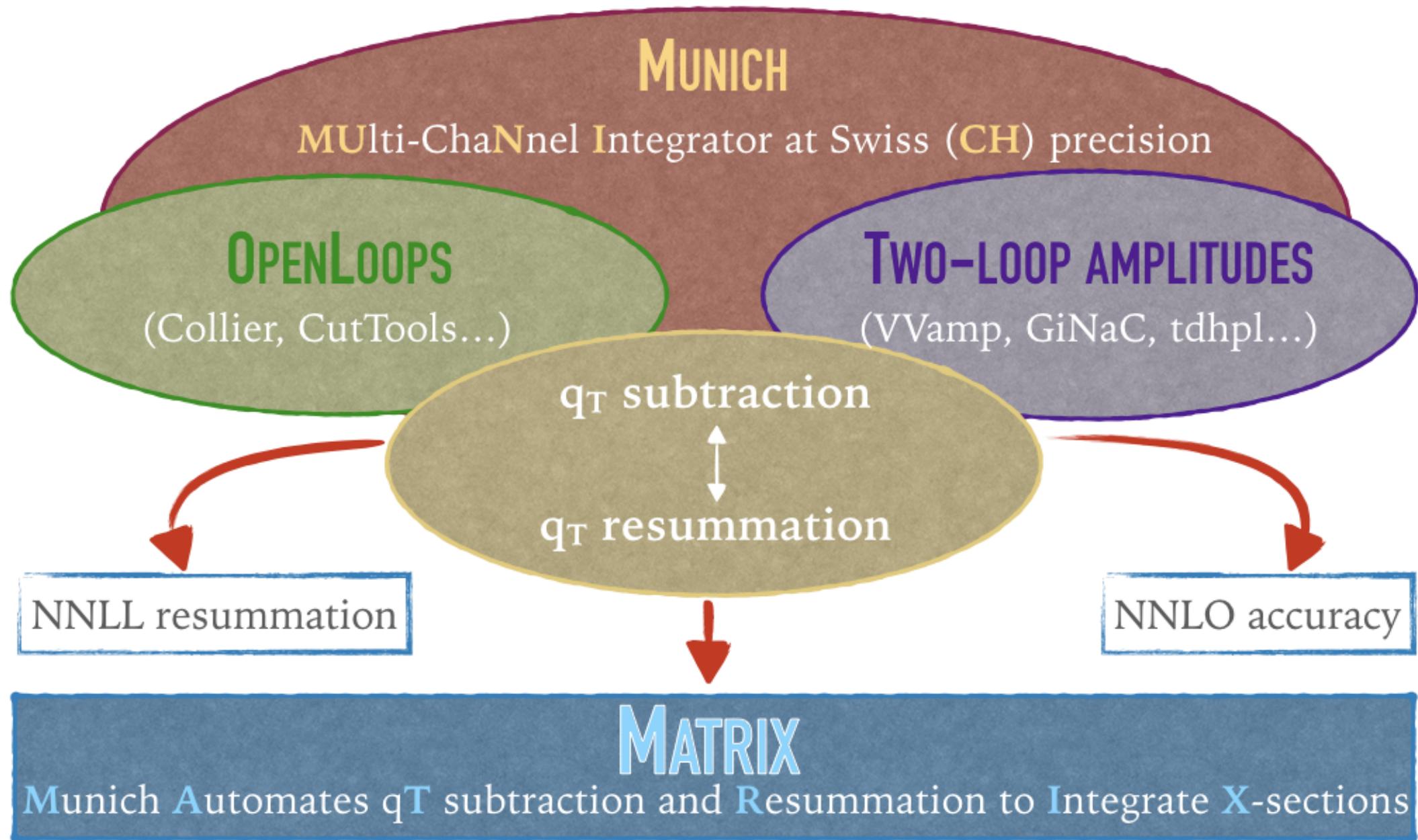
Implies knowledge of **correct** subtraction operator for virtual corrections

$$H \sim \langle \tilde{\mathcal{M}} | \tilde{\mathcal{M}} \rangle \quad \text{with} \quad |\tilde{\mathcal{M}}\rangle = \left( 1 - \tilde{I} \right) |\mathcal{M}\rangle$$

Method can be applied to the production of arbitrary colour singlets at NNLO once the relevant amplitudes are available

**MATRIX**  
Grazzini, Kallweit, Wieseemann (2017)

# The MATRIX project



# The MATRIX project

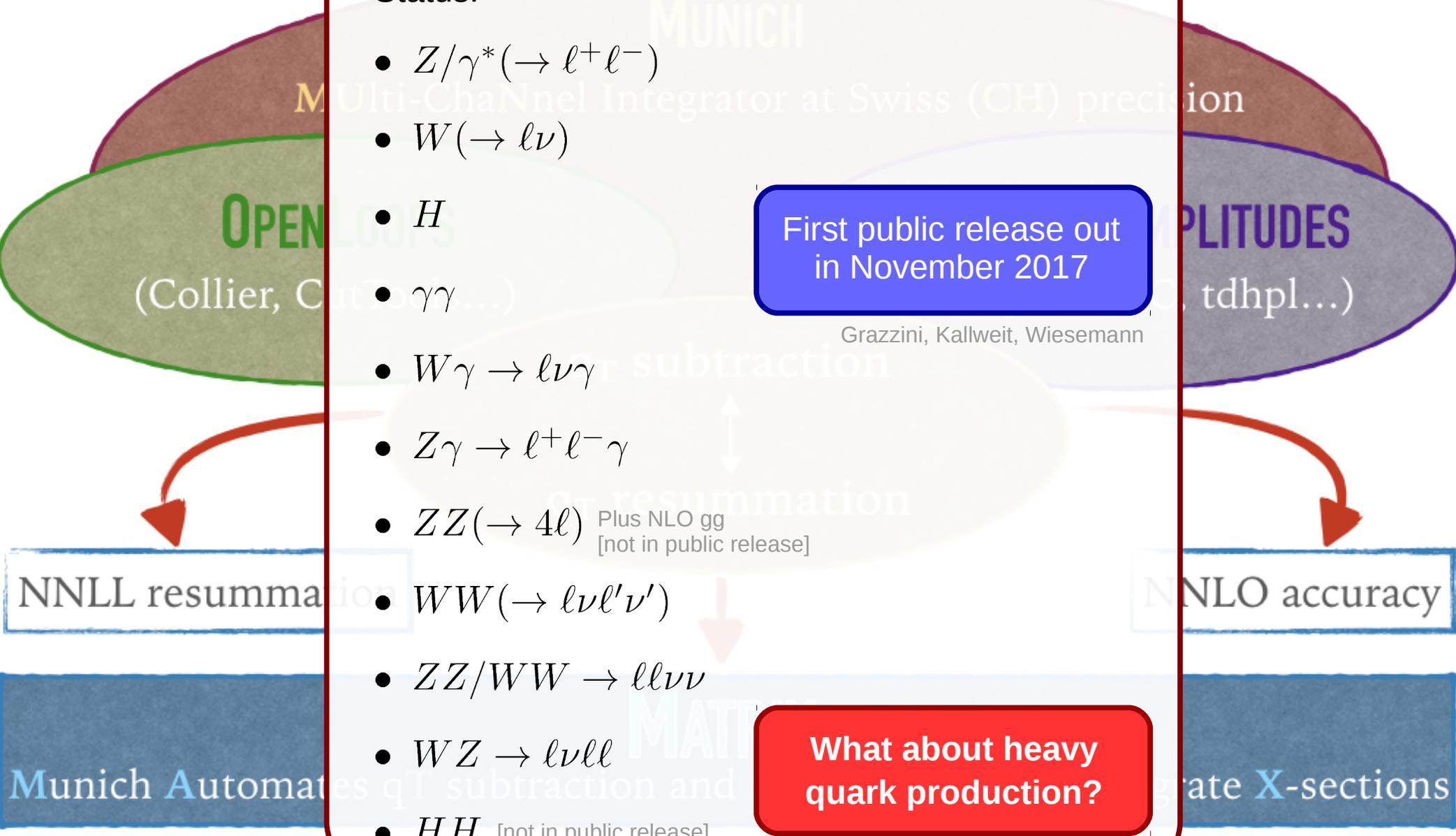
Status:

- $Z/\gamma^*(\rightarrow l^+l^-)$
- $W(\rightarrow l\nu)$
- $H$
- $\gamma\gamma$  ...
- $W\gamma \rightarrow l\nu\gamma$
- $Z\gamma \rightarrow l^+l^-\gamma$
- $ZZ(\rightarrow 4l)$  Plus NLO gg [not in public release]
- $WW(\rightarrow l\nu l'\nu')$
- $ZZ/WW \rightarrow ll\nu\nu$
- $WZ \rightarrow l\nu ll$
- $HH$  [not in public release]

First public release out in November 2017

Grazzini, Kallweit, Wiesemann

What about heavy quark production?

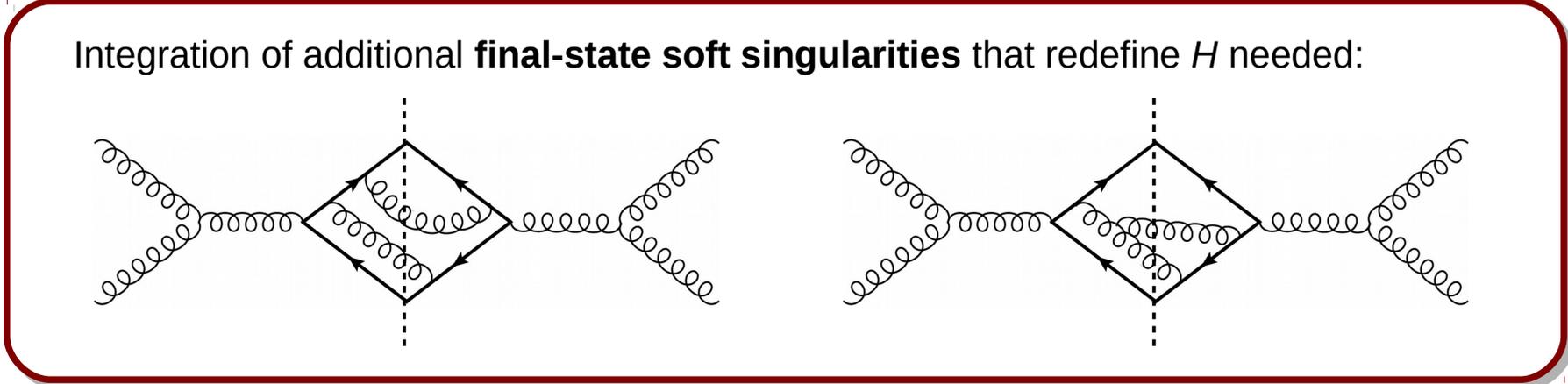


# Extension to heavy-quark production

Analogous formula, but with new contributions coming from **final state radiation**

$$d\sigma_{\text{NNLO}}^{t\bar{t}} = \mathcal{H}_{\text{NNLO}}^{t\bar{t}} \otimes d\sigma_{\text{LO}}^{t\bar{t}} + \left[ d\sigma_{\text{NLO}}^{t\bar{t}+\text{jet}} - d\sigma_{\text{NNLO}}^{t\bar{t},\text{CT}} \right]$$

- Modified subtraction counterterm fully known (ingredient: NNLO soft anomalous dimension  $\Gamma_{\downarrow}$ )
- The structure of the hard-collinear function  $H$  also changes:



$$H \sim \langle \tilde{\mathcal{M}} | \tilde{\mathcal{M}} \rangle \longrightarrow (\mathbf{H}\Delta) \sim \langle \tilde{\mathcal{M}} | \Delta | \tilde{\mathcal{M}} \rangle \quad \left( \begin{array}{l} \text{Equivalent to:} \\ \tilde{\mathbf{I}} \longrightarrow \tilde{\mathbf{I}} \end{array} \right)$$

Additional radiative soft factor  $\Delta$  which includes **colour** correlations

# Extension to heavy-quark production

- Specifically, we have to compute  $d\sigma/d^2q_T$
- Only new soft singularities → integrate the (subtracted) **soft current**

E.g. at NLO:

$$- \mathbf{J}(k)^2|_{\text{sub}} = \sum_{J=3,4} \left[ \frac{p_J^2}{(p_J \cdot k)^2} \mathbf{T}_J^2 + \sum_{i=1,2} \left( \frac{p_i \cdot p_J}{p_J \cdot k} - \frac{p_1 \cdot p_2}{(p_1 + p_2) \cdot k} \right) \frac{2 \mathbf{T}_i \cdot \mathbf{T}_J}{p_i \cdot k} \right] + \frac{2p_3 \cdot p_4}{(p_3 \cdot k)(p_4 \cdot k)} \mathbf{T}_3 \cdot \mathbf{T}_4$$

- After integration the following NLO subtraction operator can be obtained:

[Catani, Grazzini, Torre; 1408.4564]

$$\tilde{\mathbf{I}}_{c\bar{c} \rightarrow Q\bar{Q}}^{(1)} \left( \epsilon, \frac{M^2}{\mu_R^2} \right) = -\frac{1}{2} \left( \frac{M^2}{\mu_R^2} \right)^{-\epsilon} \left\{ \underbrace{\left( \frac{1}{\epsilon^2} + i\pi \frac{1}{\epsilon} - \frac{\pi^2}{12} \right) (\mathbf{T}_1^2 + \mathbf{T}_2^2) + \frac{2}{\epsilon} \gamma_c}_{\text{Purely initial-state}} - \underbrace{\frac{4}{\epsilon} \Gamma_t^{(1)}(y_{34}) + \mathbf{F}_t^{(1)}(y_{34})}_{\text{New soft contributions}} \right\}$$

↓ Pole structure agrees with studies on one-loop amplitudes  
 [Catani, Dittmaier, Trocsanyi, 0011222]

↓ Finite piece: only from direct computation

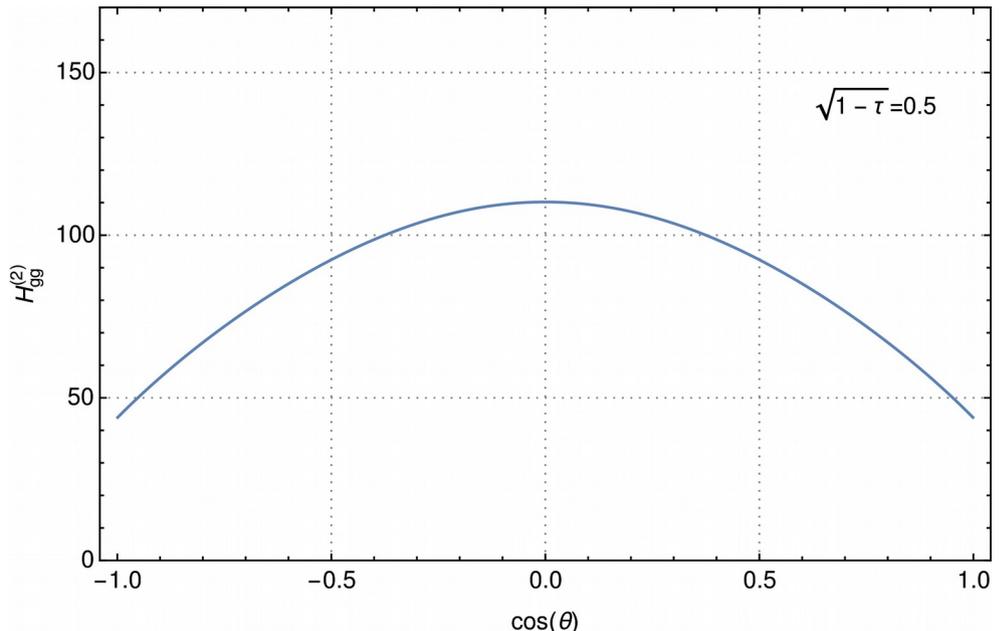
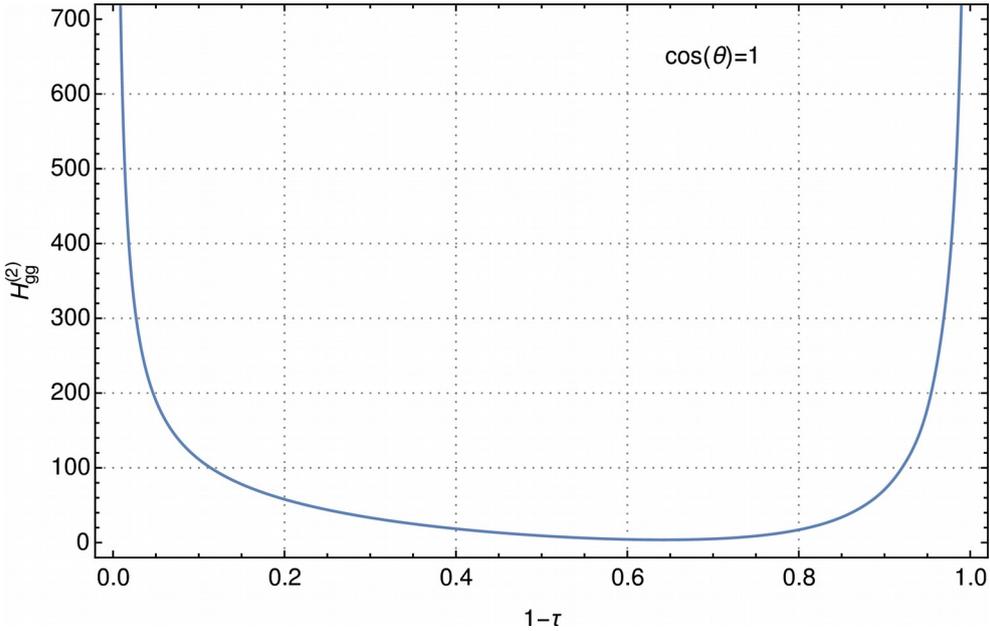
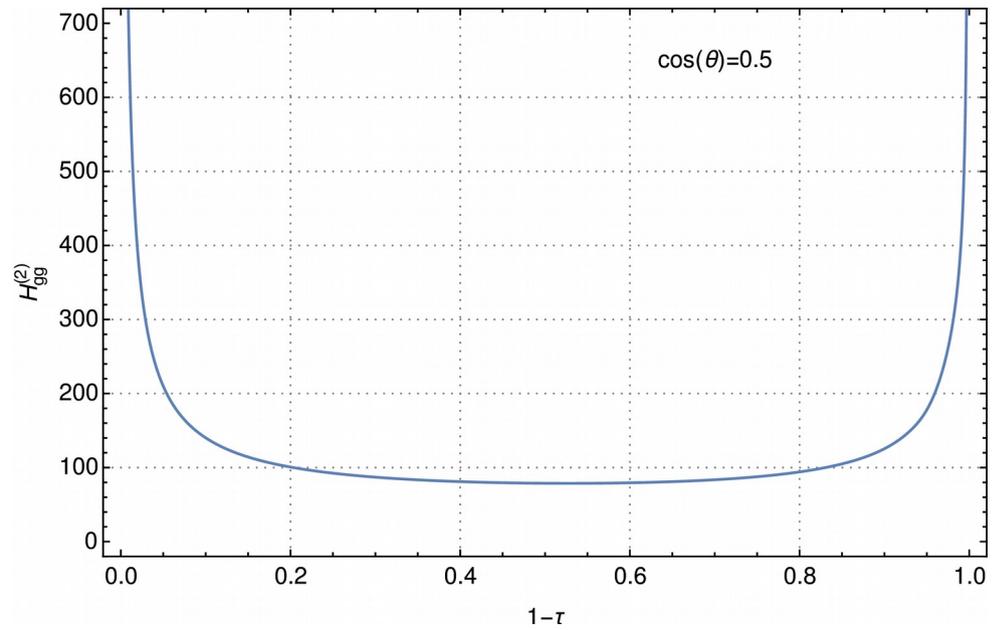
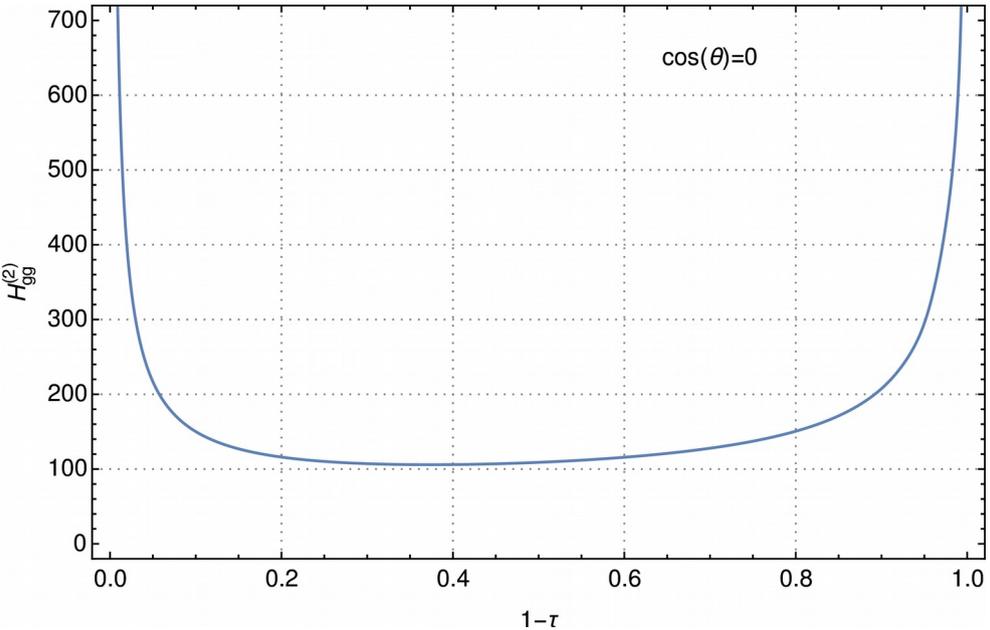
- We had to **extend** the above results to **NNLO**

# Final result - $H^{(2)}$

$\tau = 4m^2/s$ ,  $\cos\theta$  scattering angle

Catani, Devoto, Grazzini, JM (to appear)  
See also Angeles-Martinez, Czakon, Sapeta (2018)

- We have recently finished their computation
- Results mostly analytical, numerical integration for some pieces

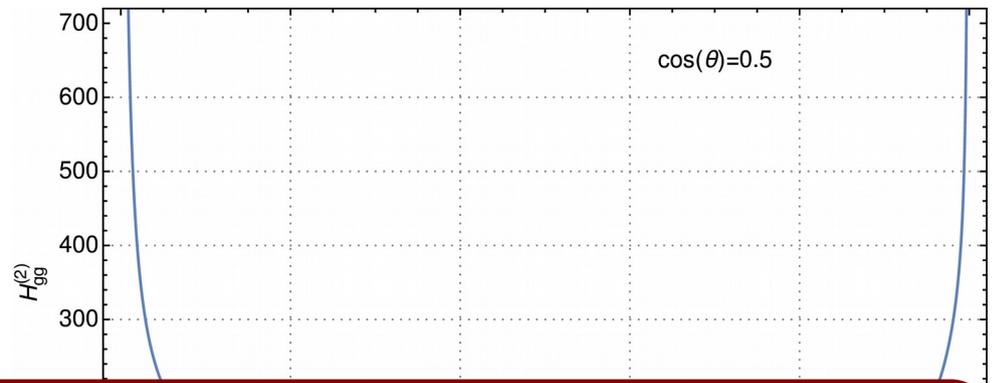
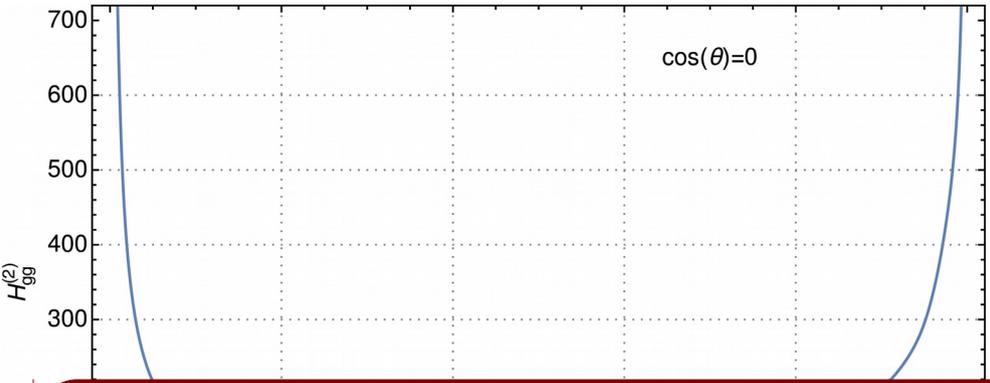


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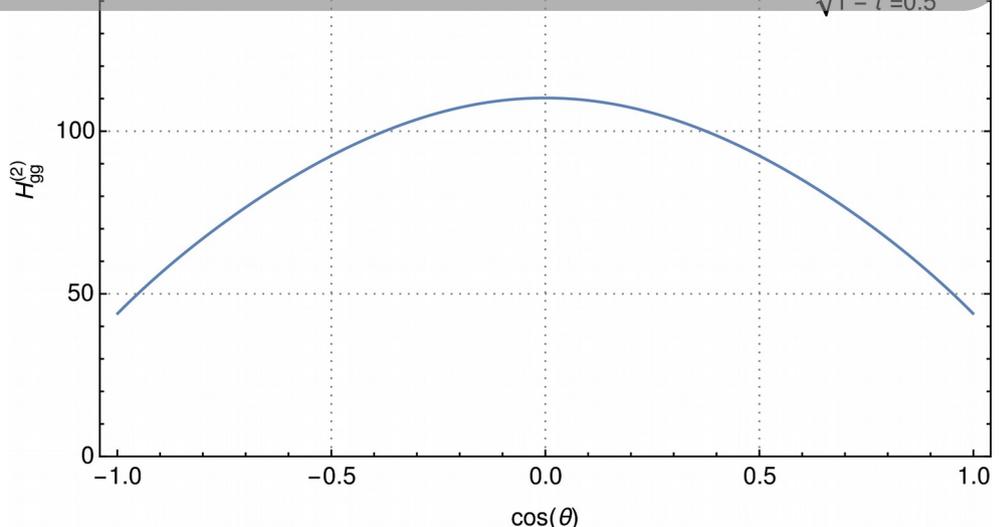
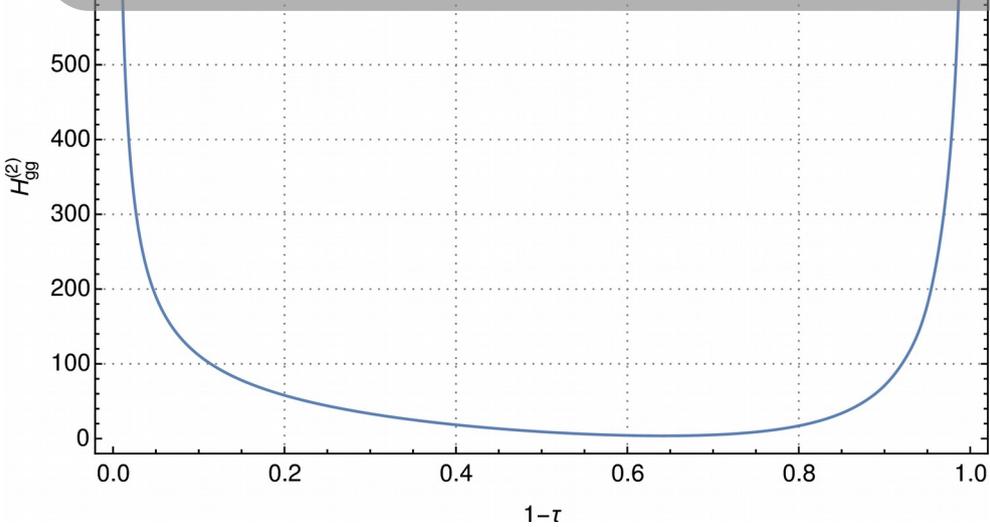


Thanks to these results,  **$q_T$  subtraction** can now deal with  **$Q\bar{Q}$  production**

Our calculation is implemented within the MATRIX framework

First inclusive and differential results recently published, presented in the following slides

Catani, Devoto, Grazzini, Kallweit, JM, Sargsyan (2019); Catani, Devoto, Grazzini, Kallweit, JM (2019)



# Inclusive cross section

Excellent agreement with Top++

$\sigma_{\text{NNLO}}$ [pb]	MATRIX	TOP++
8 TeV	$238.5(2)^{+3.9\%}_{-6.3\%}$	$238.6^{+4.0\%}_{-6.3\%}$
13 TeV	$794.0(8)^{+3.5\%}_{-5.7\%}$	$794.0^{+3.5\%}_{-5.7\%}$
100 TeV	$35215(74)^{+2.8\%}_{-4.7\%}$	$35216^{+2.9\%}_{-4.8\%}$

Statistical+systematic  
uncertainties

Scale  
uncertainties

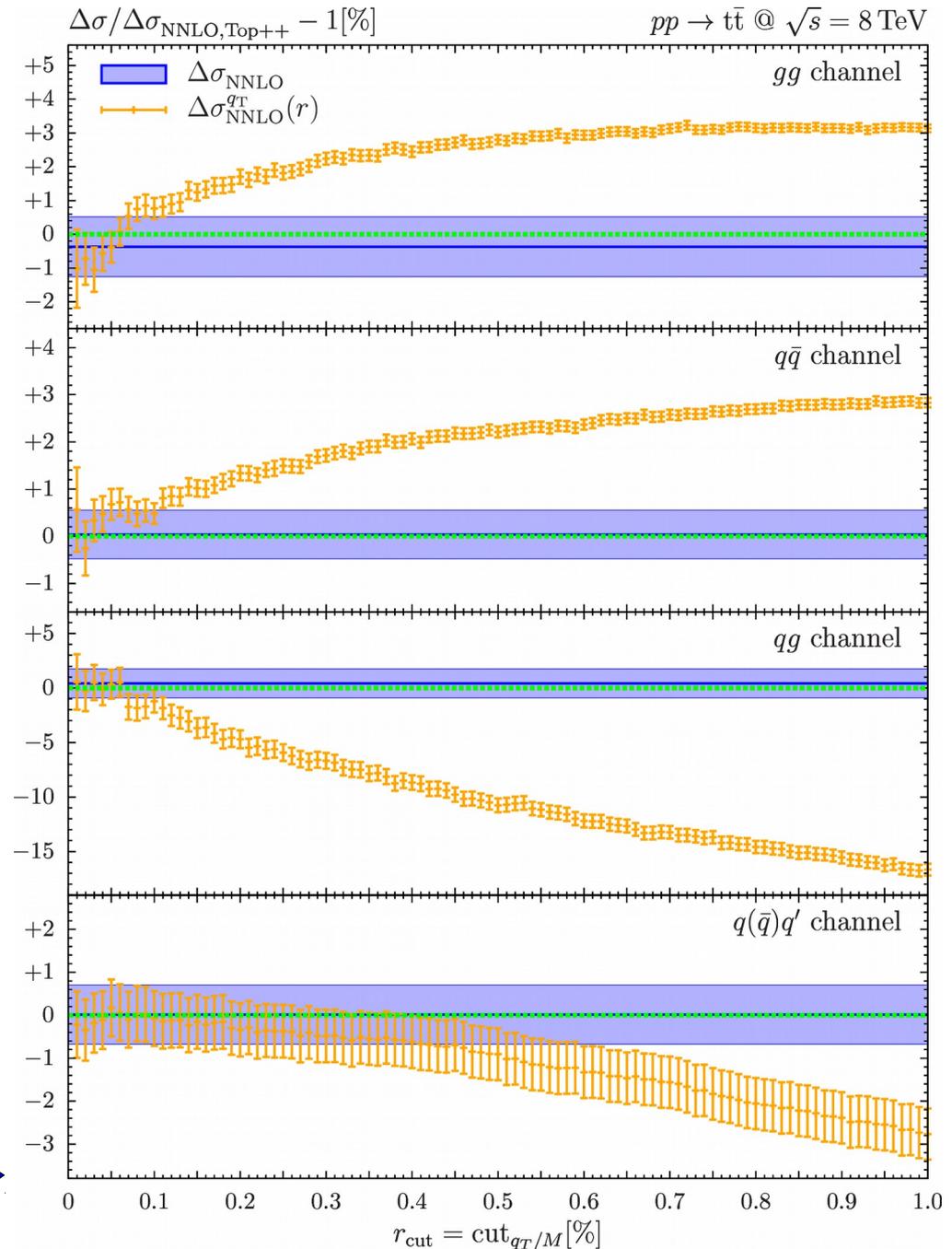
NNPDF31 sets,  $m_t=173.3\text{GeV}$

Scale uncertainties:  $\mu_0=m_t$

$\mu_0 < \mu_F, \mu_R < 2\mu_0$      $0.5 < \mu_F/\mu_R < 2$

Per-mille accuracy in  $\sim 1000\text{CPU days}$

Quality of the  $q_T \rightarrow 0$  extrapolation can be understood looking at the  $r_{\text{cut}}$  dependence



# Differential results

We compute single and double differential distributions

We compare our results with recent measurements from CMS in the lepton+jets channel [CMS-TOP-17-002]

CMS measurements are extrapolated to parton level in the inclusive phase space

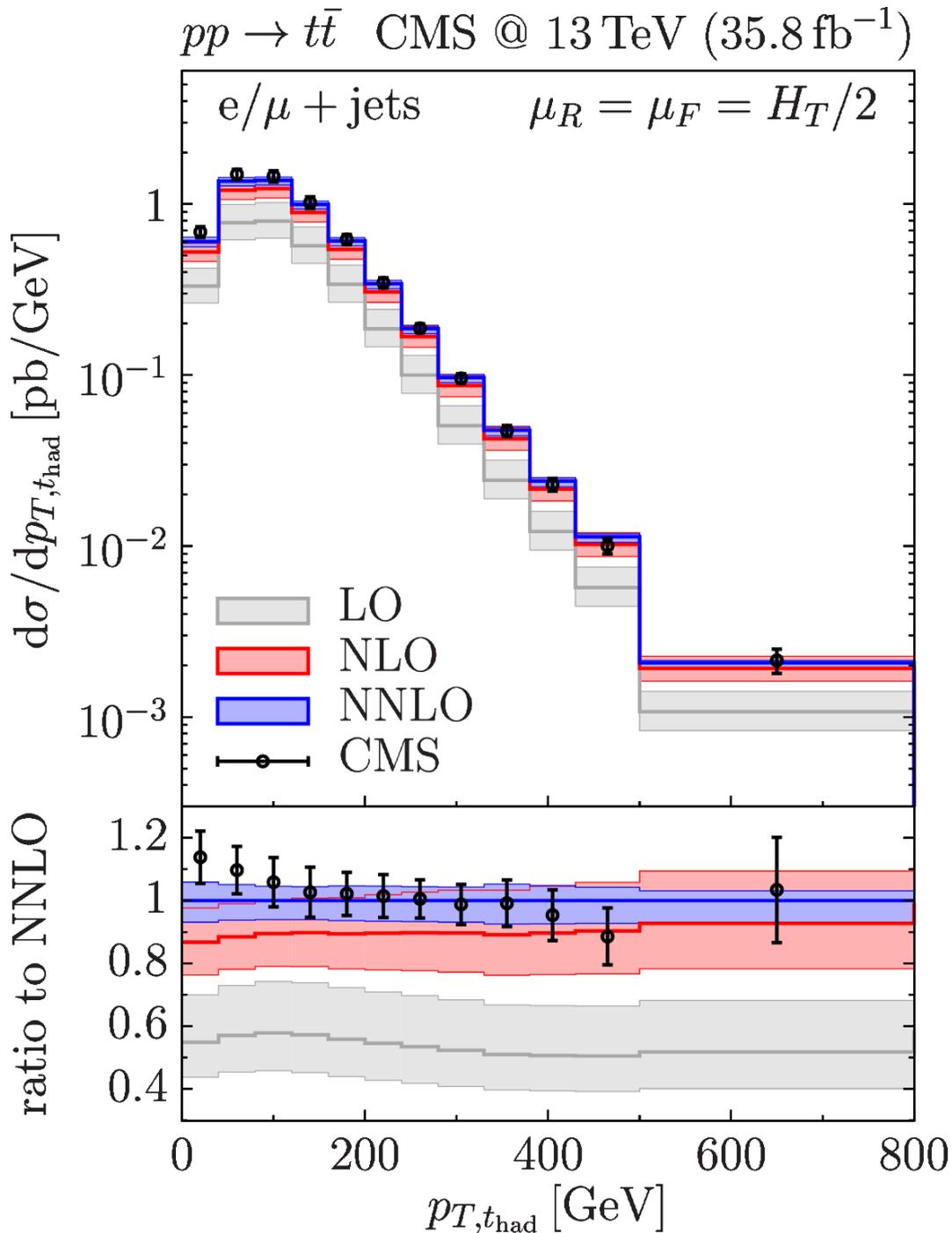
 we carry out our calculation without cuts

Perturbative results depend on the choice of scales  $\mu_F$ ,  $\mu_R$  which should be chosen of the order of the characteristic hard scale

- Total cross section and rapidity distribution:  $m_t$
- Invariant mass distribution:  $m_{t\bar{t}}$
- Transverse momentum distribution:  $m_T$

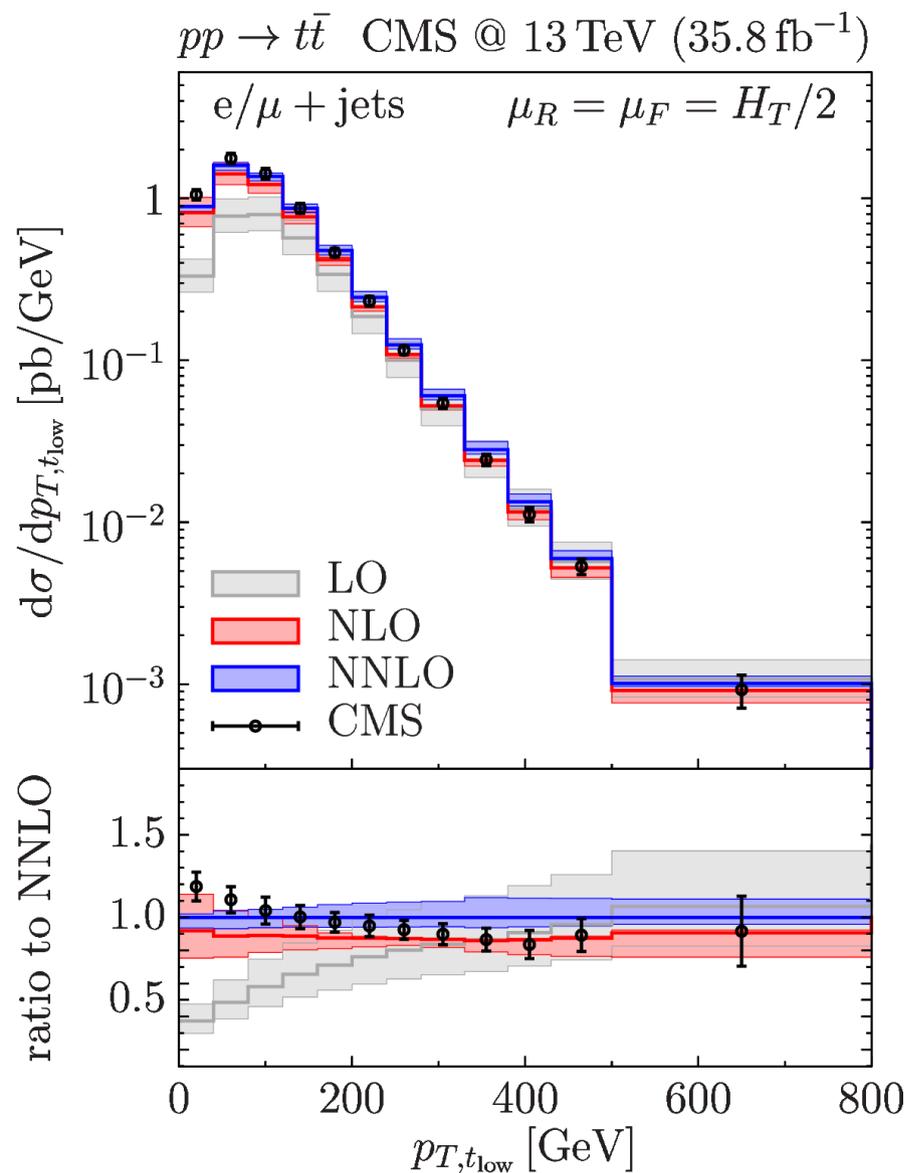
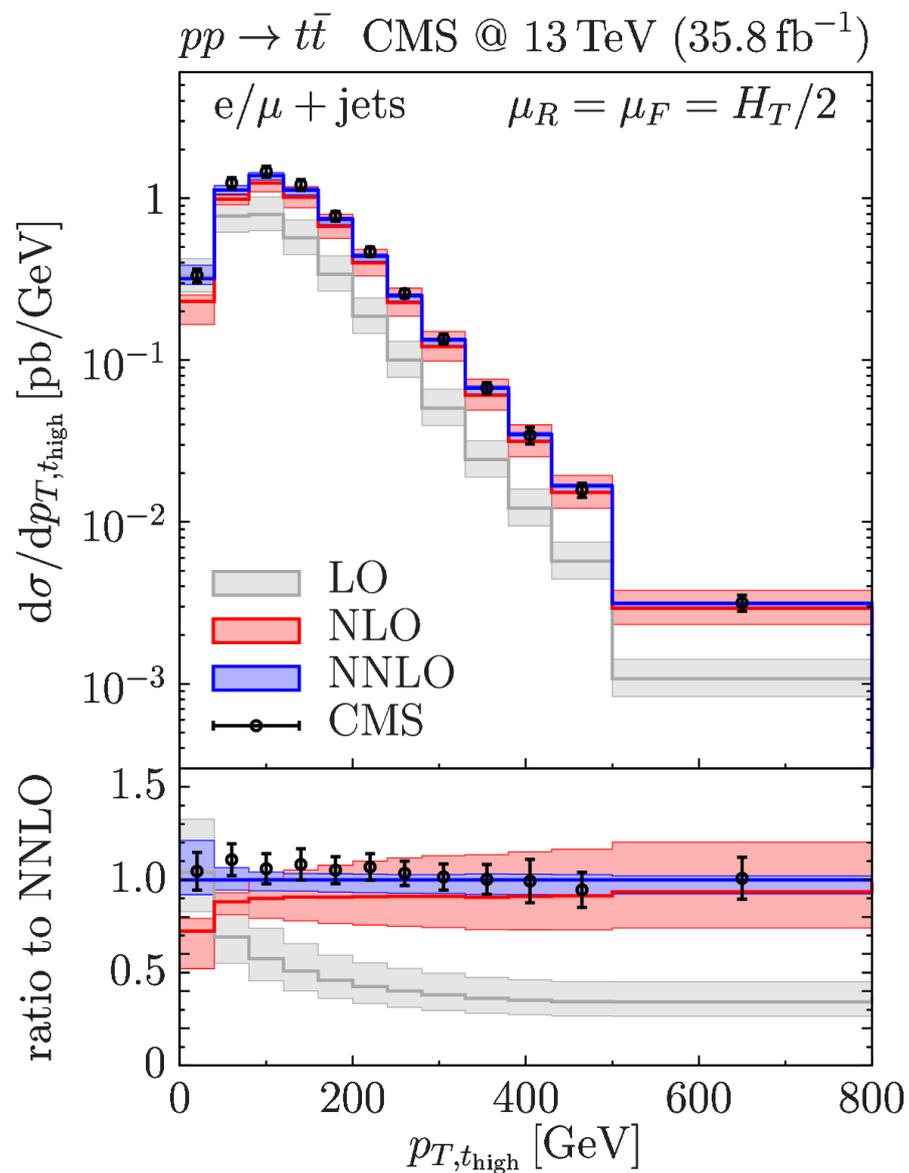
The dynamical scale  $\mu_0 = H_T/2 = (m_{T,t} + m_{T,\bar{t}})/2$  is a good approximation to all these scales

# Single-differential distributions



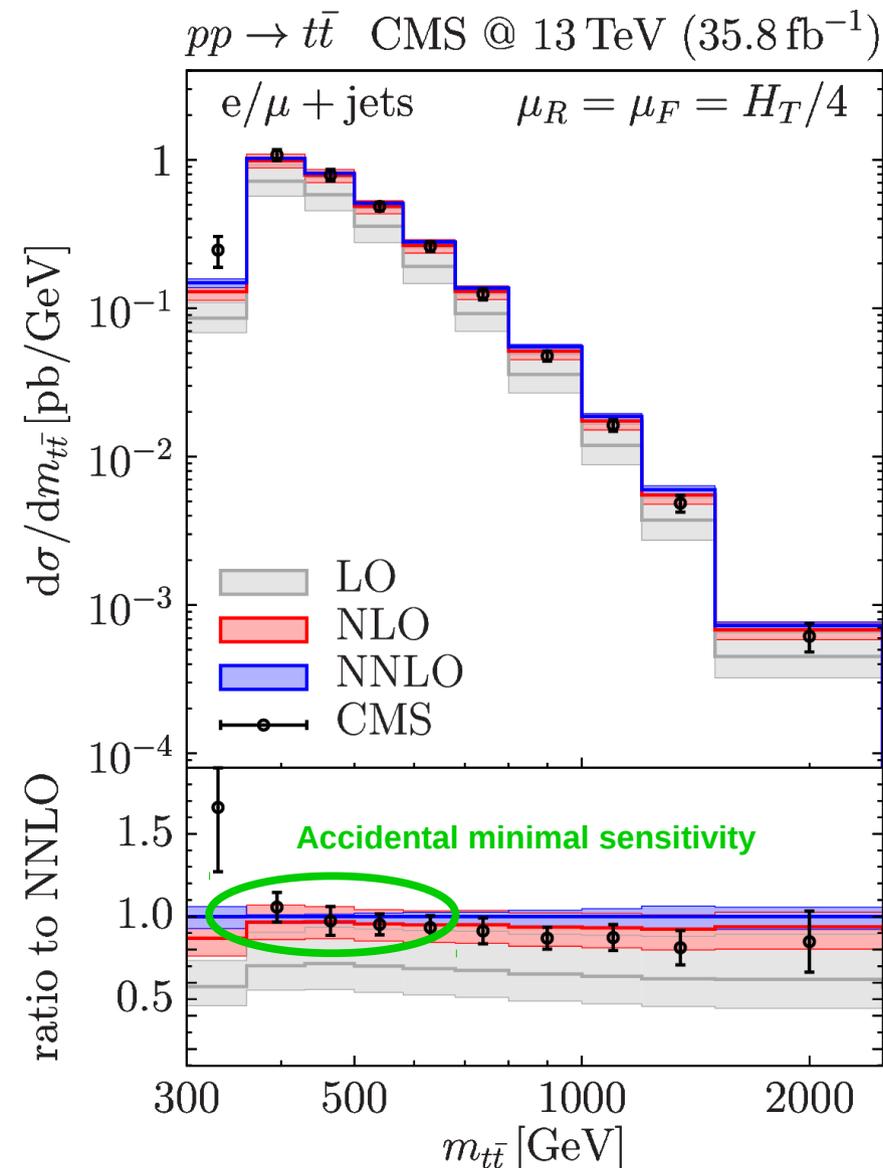
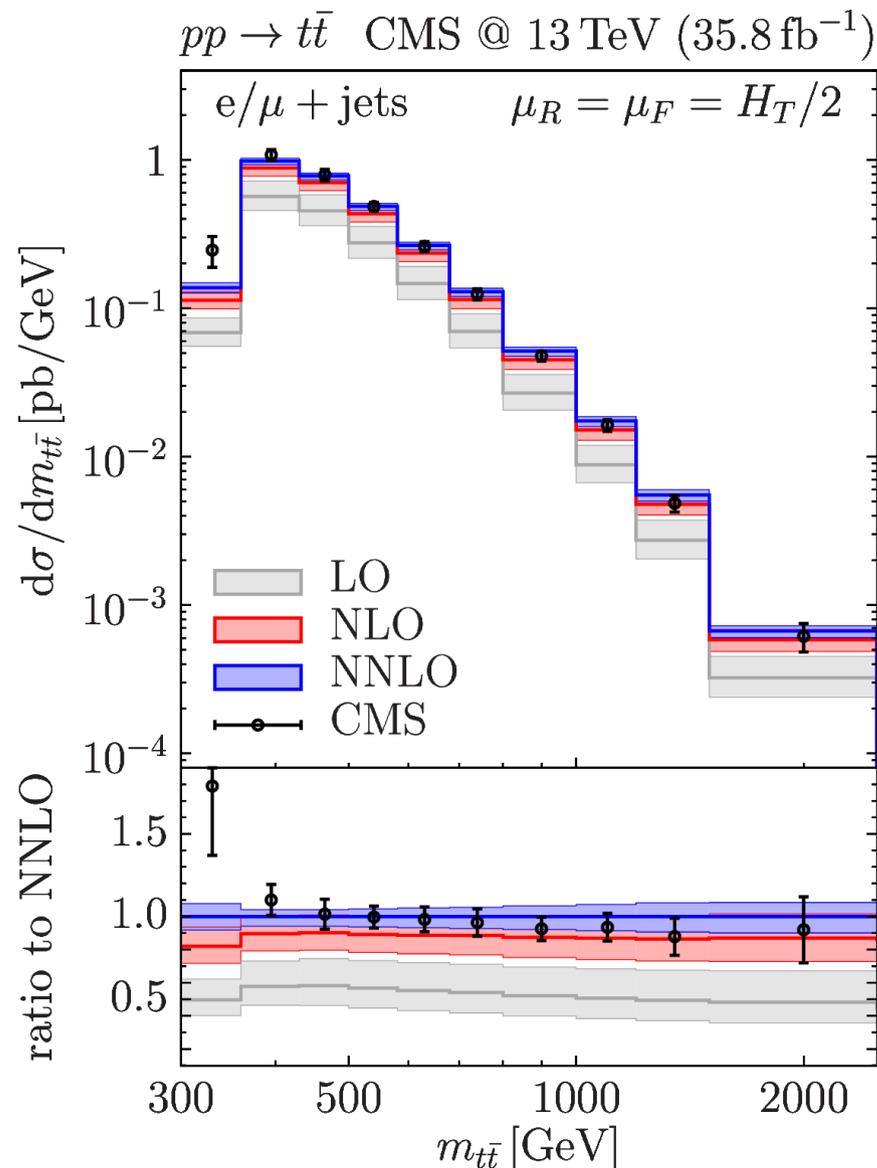
- Good perturbative behaviour, large overlap between NLO and NNLO bands
- As noted in previous analysis the measured  $p_T$  is slightly softer than the NNLO prediction
- Data and theory consistent within uncertainties

# Single-differential distributions



- Higher order corrections have a larger effect on the shape
- Low  $p_T(t_{\text{high}})$  region: FO instabilities associated with low  $p_T(t\bar{t})$
- Good agreement with data

# Single-differential distributions

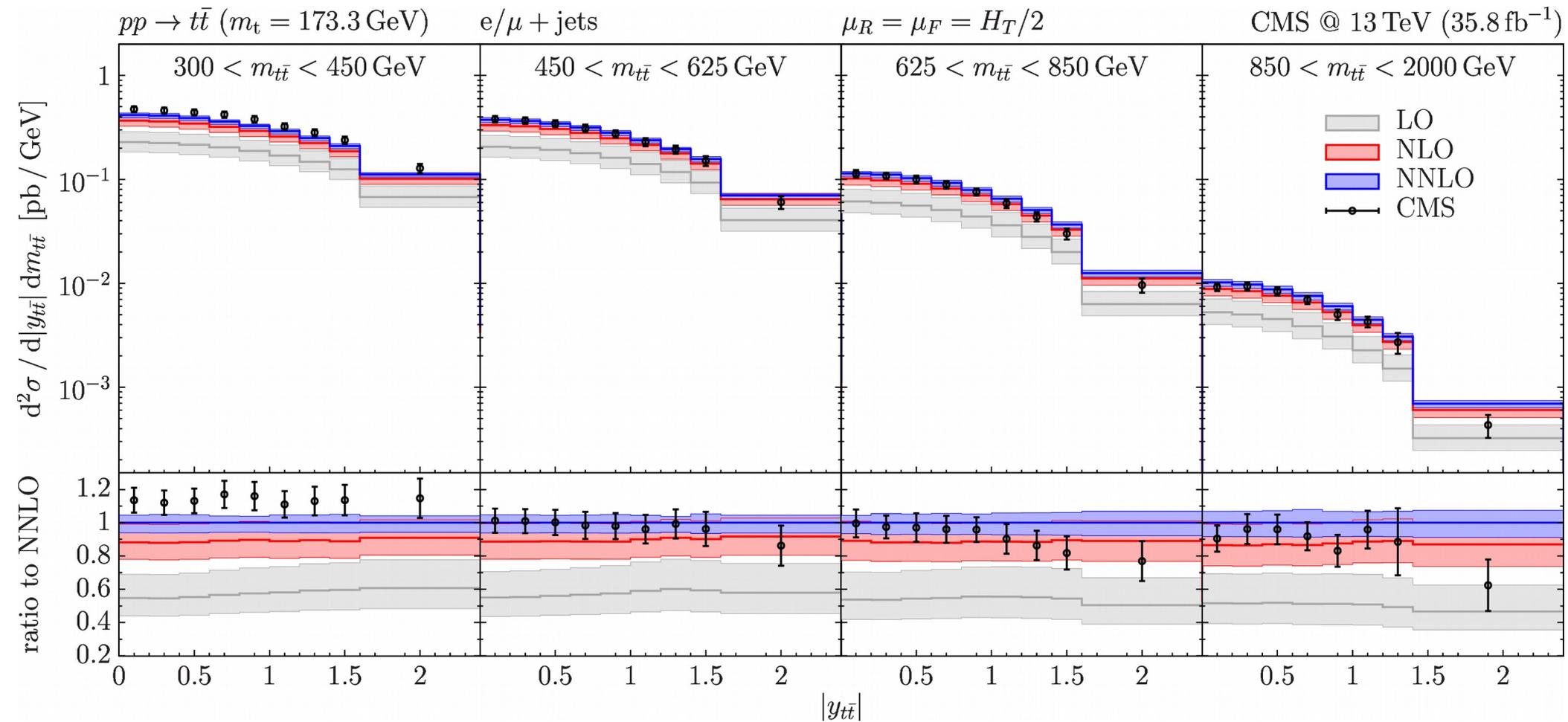


- Lower scale  $H_T/4$  (usually used as a benchmark) seems to lead to underestimation of perturbative uncertainties in certain  $m_{t\bar{t}}$  regions

- Good description of data except for first bin ( $m_{t\bar{t}} < 360 \text{ GeV}$ )

Issues in extrapolation? Smaller  $m_t$ ? CMS-TOP-18-004: leptonic channel, fit  $m_t = 170.81 \pm 0.68 \text{ GeV}$

# Double-differential distributions

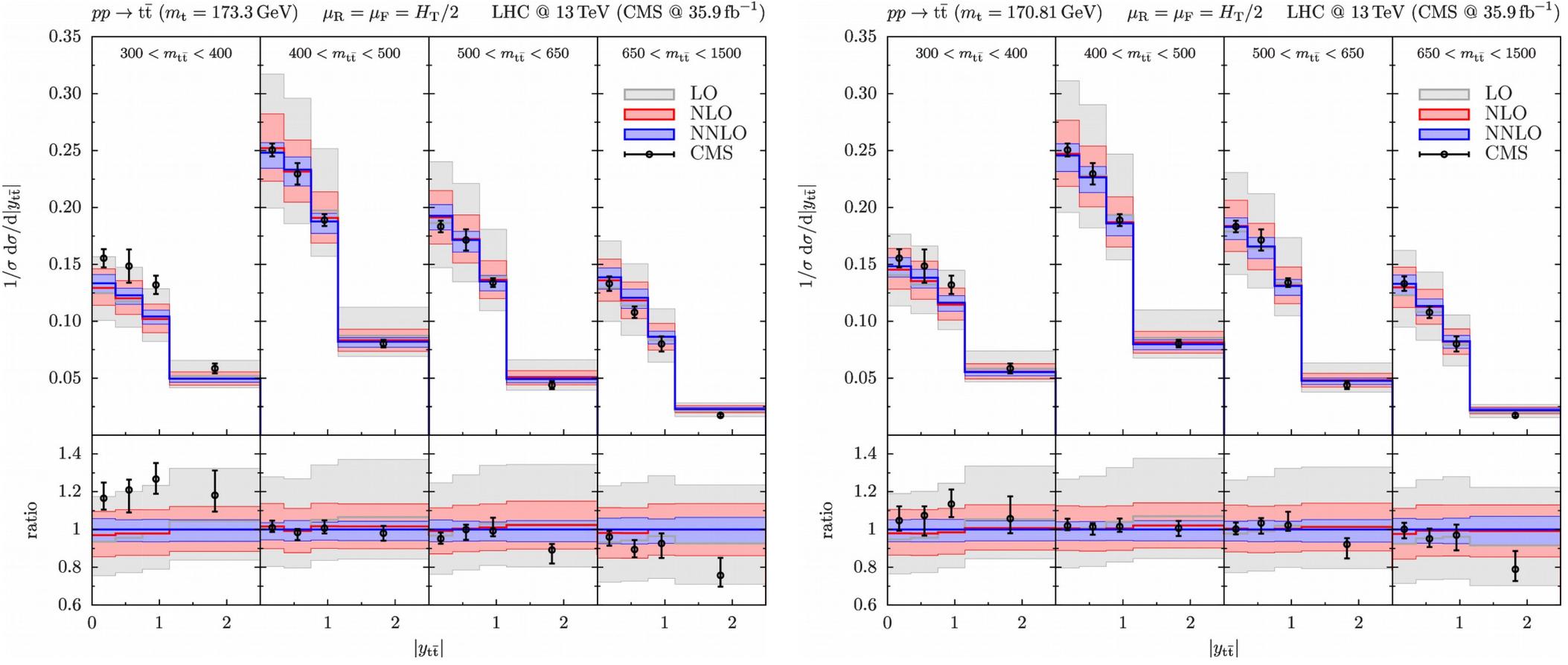


- Again some discrepancy in the low  $m_{t\bar{t}}$  region, smaller effect due to larger bin size
- Impact of radiative corrections relatively uniform in both variables

# Double-differential distributions

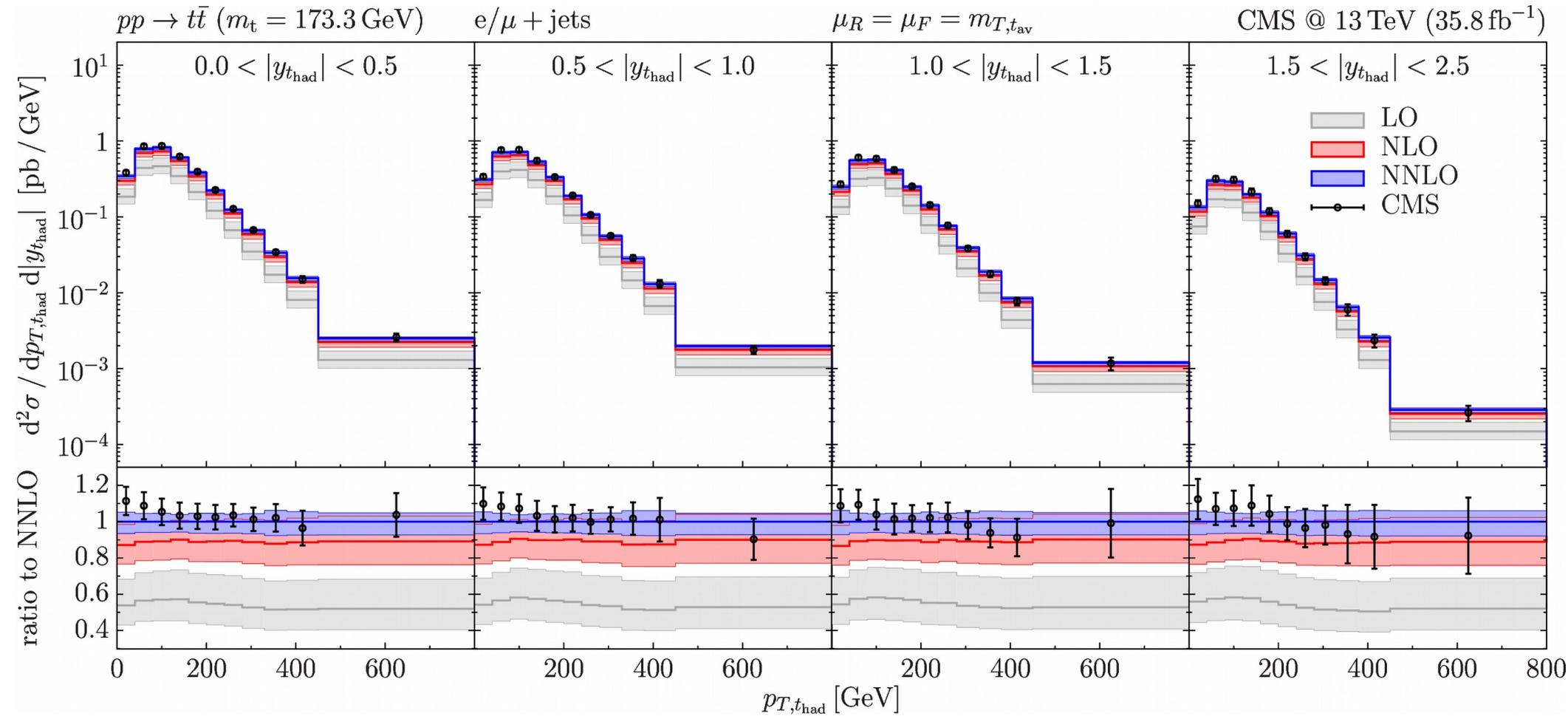
**New:** predictions for parton level CMS measurements using fully leptonic final state

[CMS-TOP-18-004]



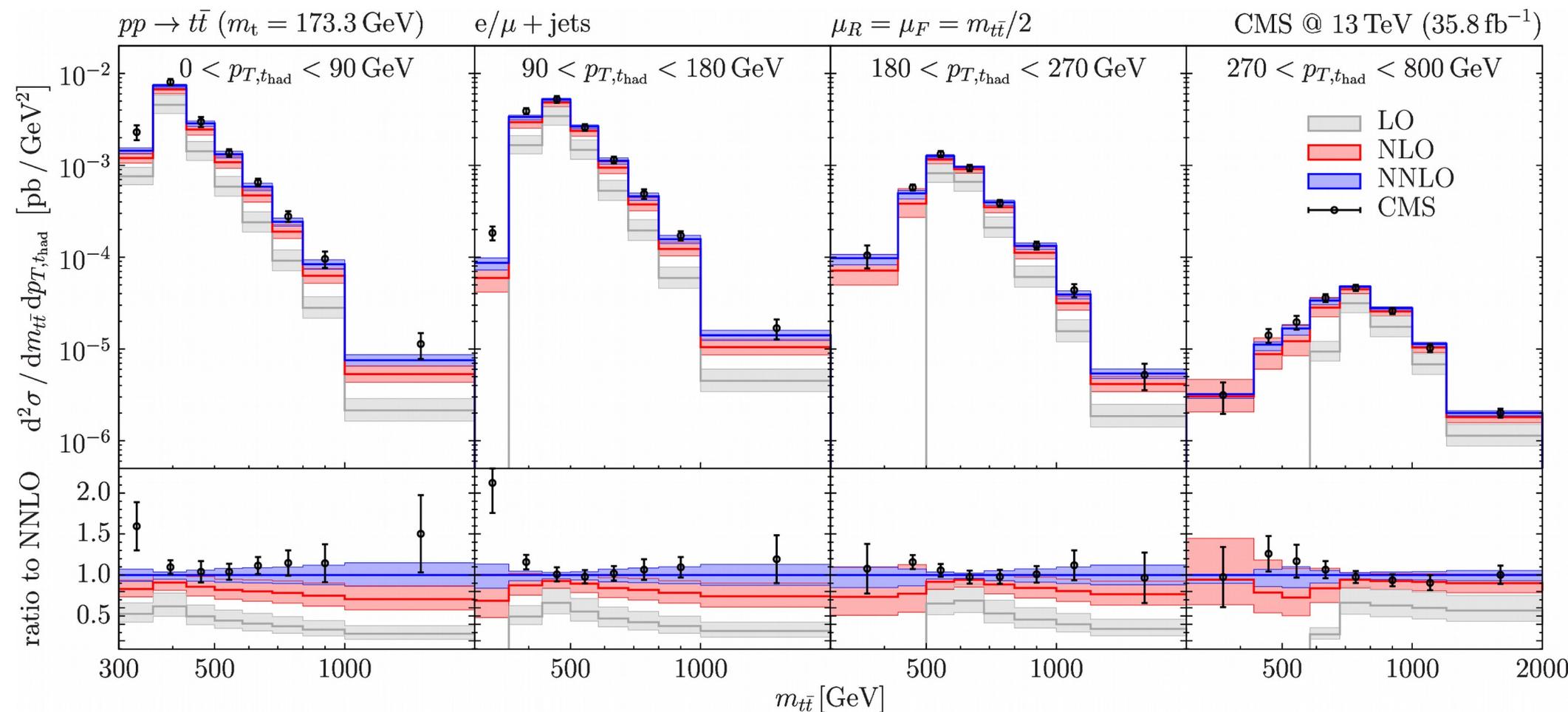
- Similar features in this decay channel (note these are normalized distributions)
- Using fitted top mass by CMS (170.81GeV) leads to a better agreement with data

# Double-differential distributions



- As for single differential distribution,  $p_T$  data softer than NNLO
- This feature holds in all the rapidity intervals

# Double-differential distributions



- Kinematical boundary at LO:  $m_{t\bar{t}} > 2 m_{T,\text{min}}$
- NLO (NNLO) is effectively LO (NLO) below that threshold  $\rightarrow$  larger uncertainties
- NNLO nicely describes the data (except only close to the physical  $m_{t\bar{t}}$  threshold)

# Summary and outlook

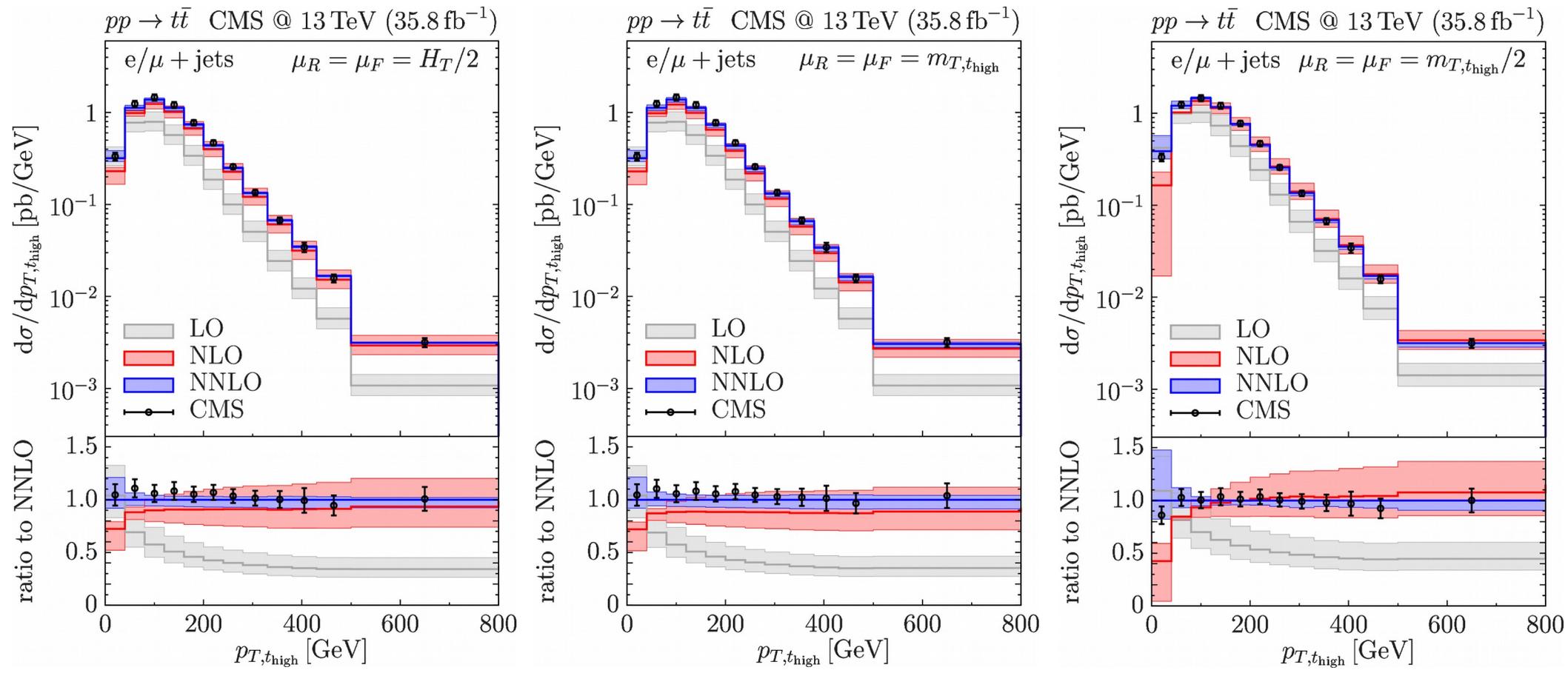
- We have presented a new computation of **top-quark pair** production at **NNLO**
- First complete application of  **$q_T$  subtraction** to colourful final states at NNLO
- Calculation fully implemented within the **MATRIX** framework
- We are able to evaluate arbitrary IR safe observables for stable top quarks
  - multi-differential distributions
  - cross sections with cuts in the top quarks and jets kinematics
- NNLO differential distributions in 1000-2000 CPU days
- Nice description of parton level CMS data
  
- **Outlook:**
  - inclusion of EW corrections
  - inclusion of top-quark decays

**Thanks!**

**Backup slides**

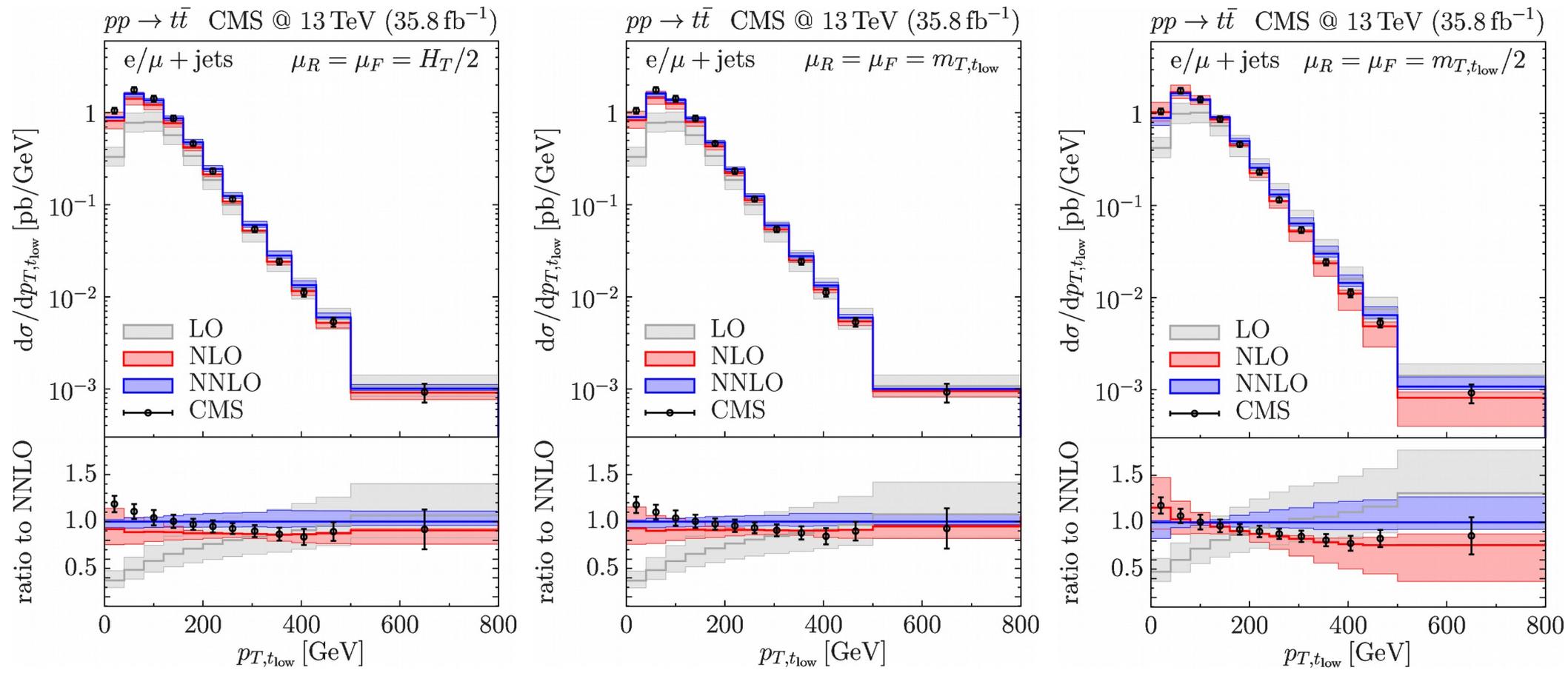
# Other scale choices

$p_T(t_{\text{high}})$



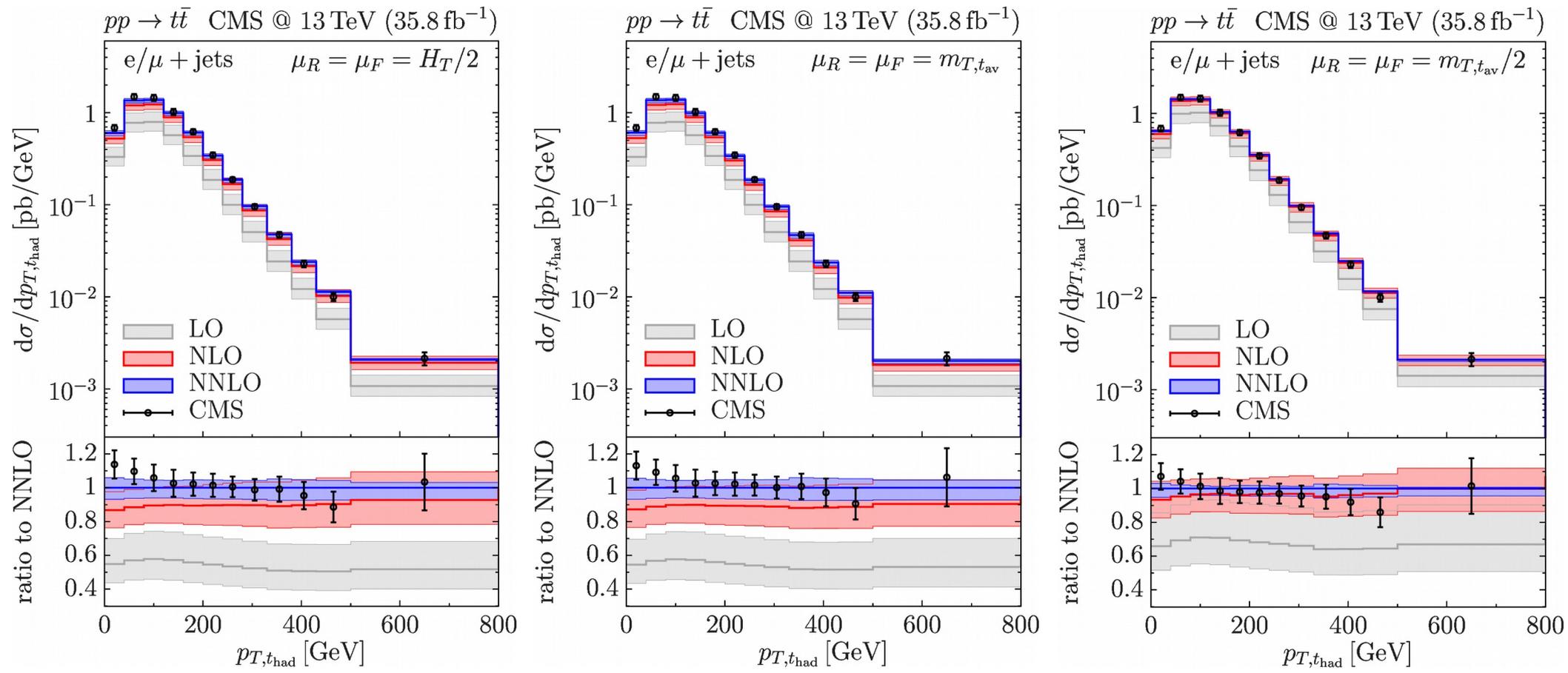
# Other scale choices

$p_{T,t_{\text{low}}}$



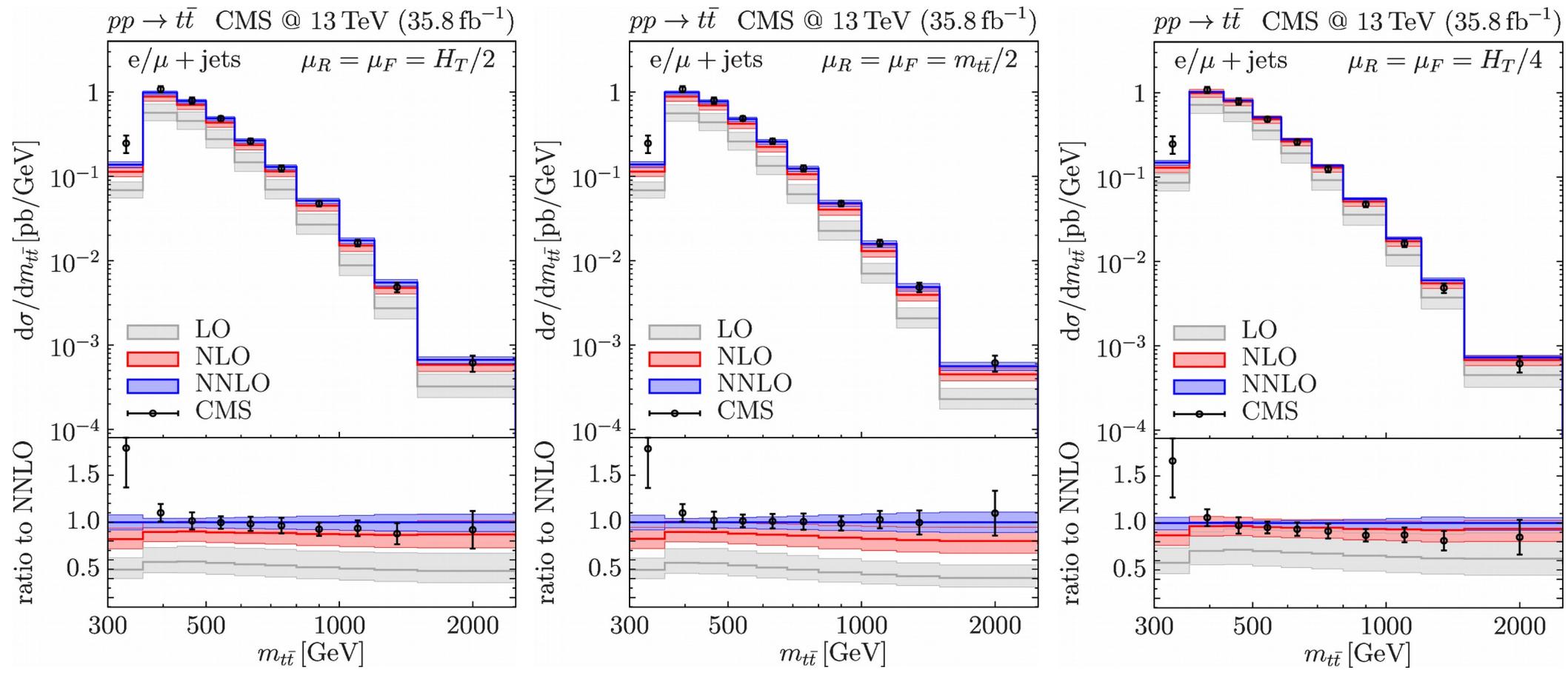
# Other scale choices

$p_T(t_{\text{had}})$



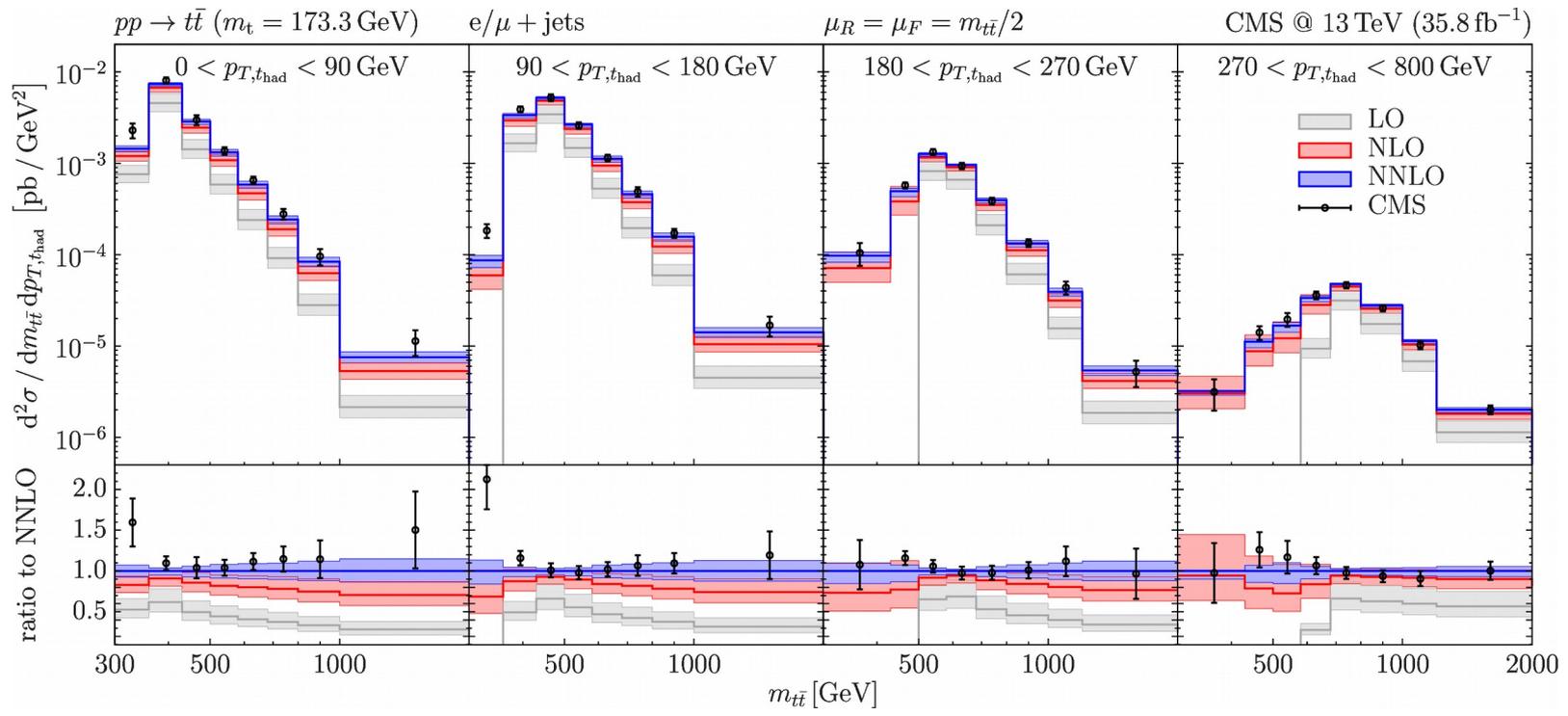
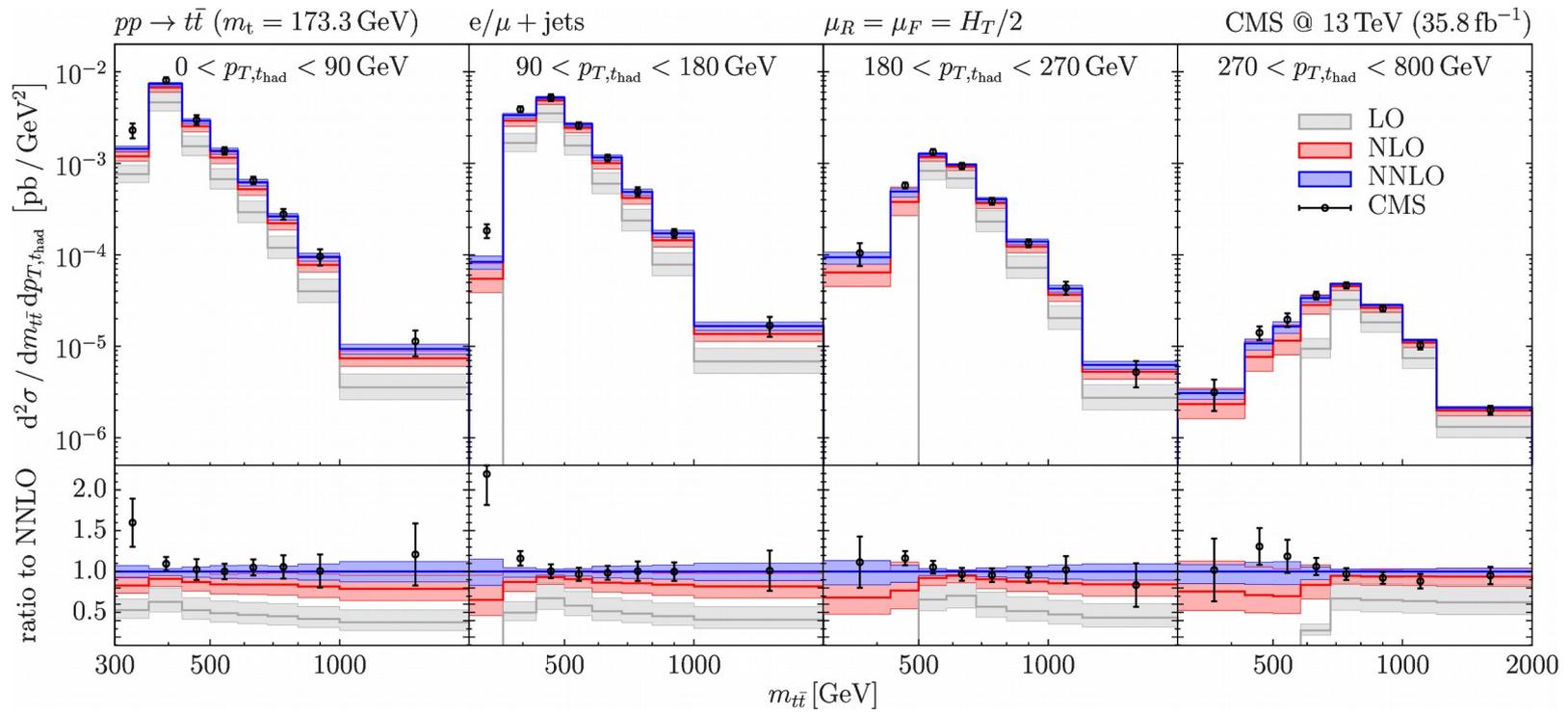
# Other scale choices

$m_{t\bar{t}}$



# Other scale choices

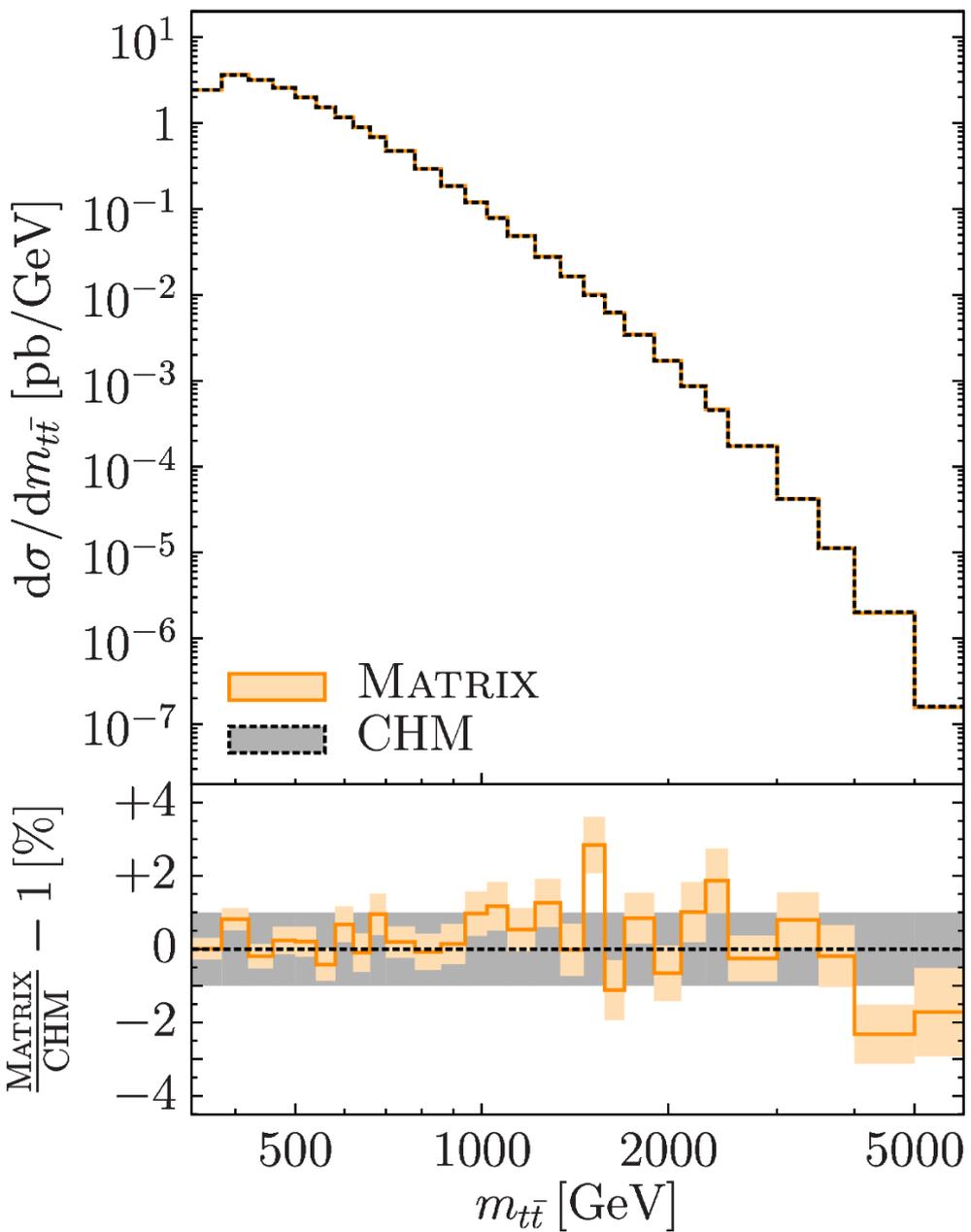
$m_{t\bar{t}}$  vs  $p_T(t_{\text{had}})$



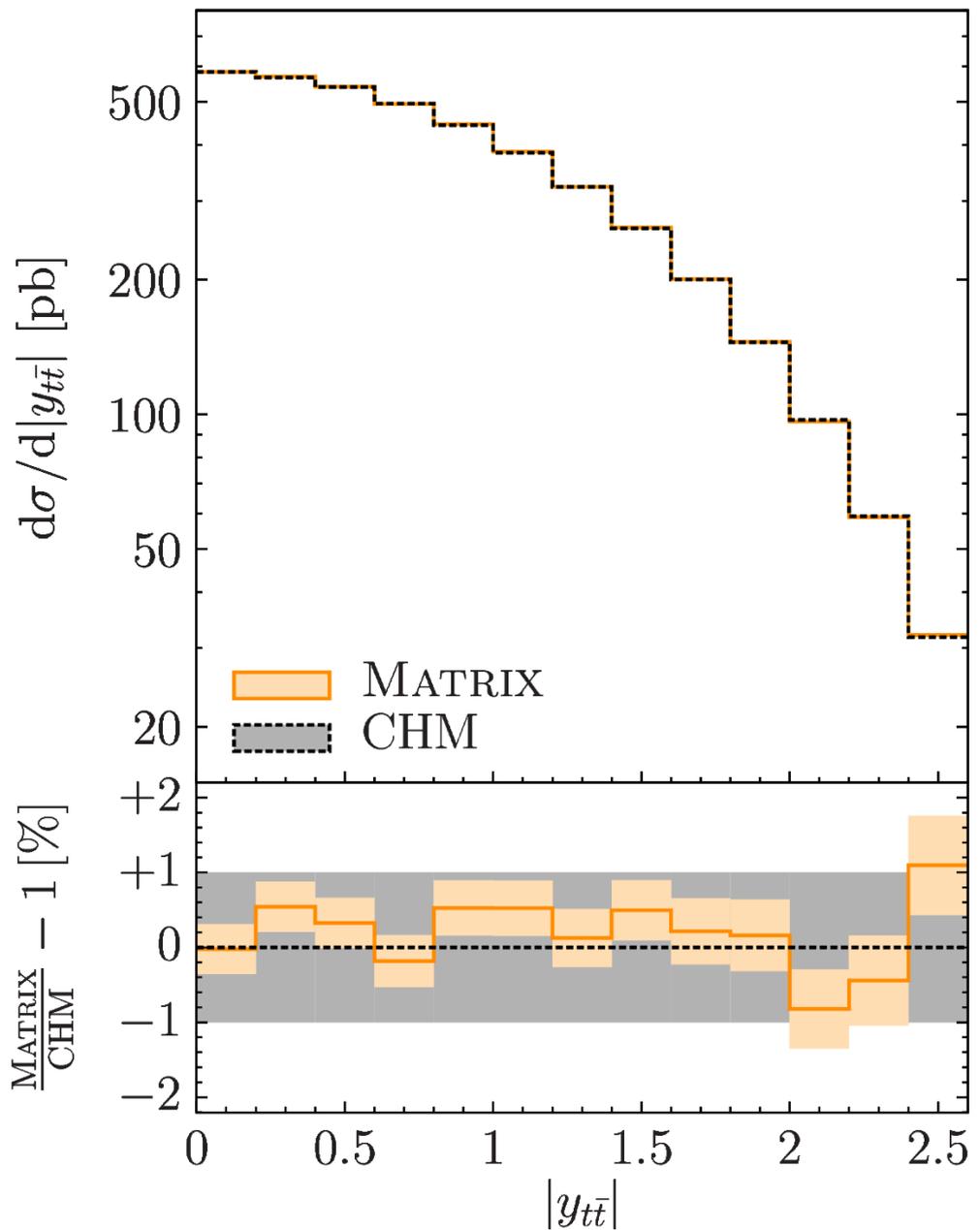
# Comparison to existing results

CHM = [Czakon, Heymes, Mitov, 1606.03350]

$pp \rightarrow t\bar{t}$  LHC @ 13 TeV



$pp \rightarrow t\bar{t}$  LHC @ 13 TeV

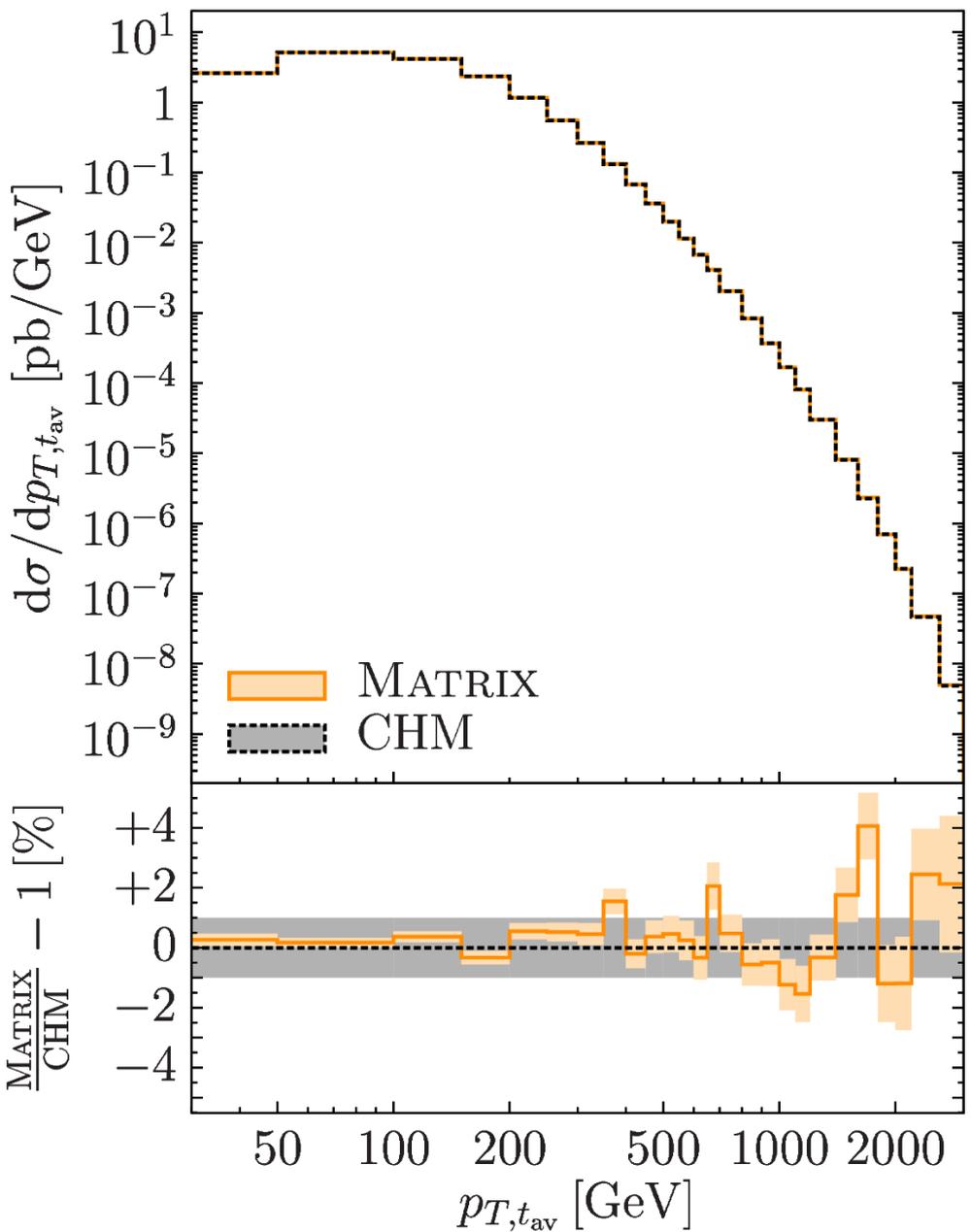


Excellent agreement even in extreme kinematical regions

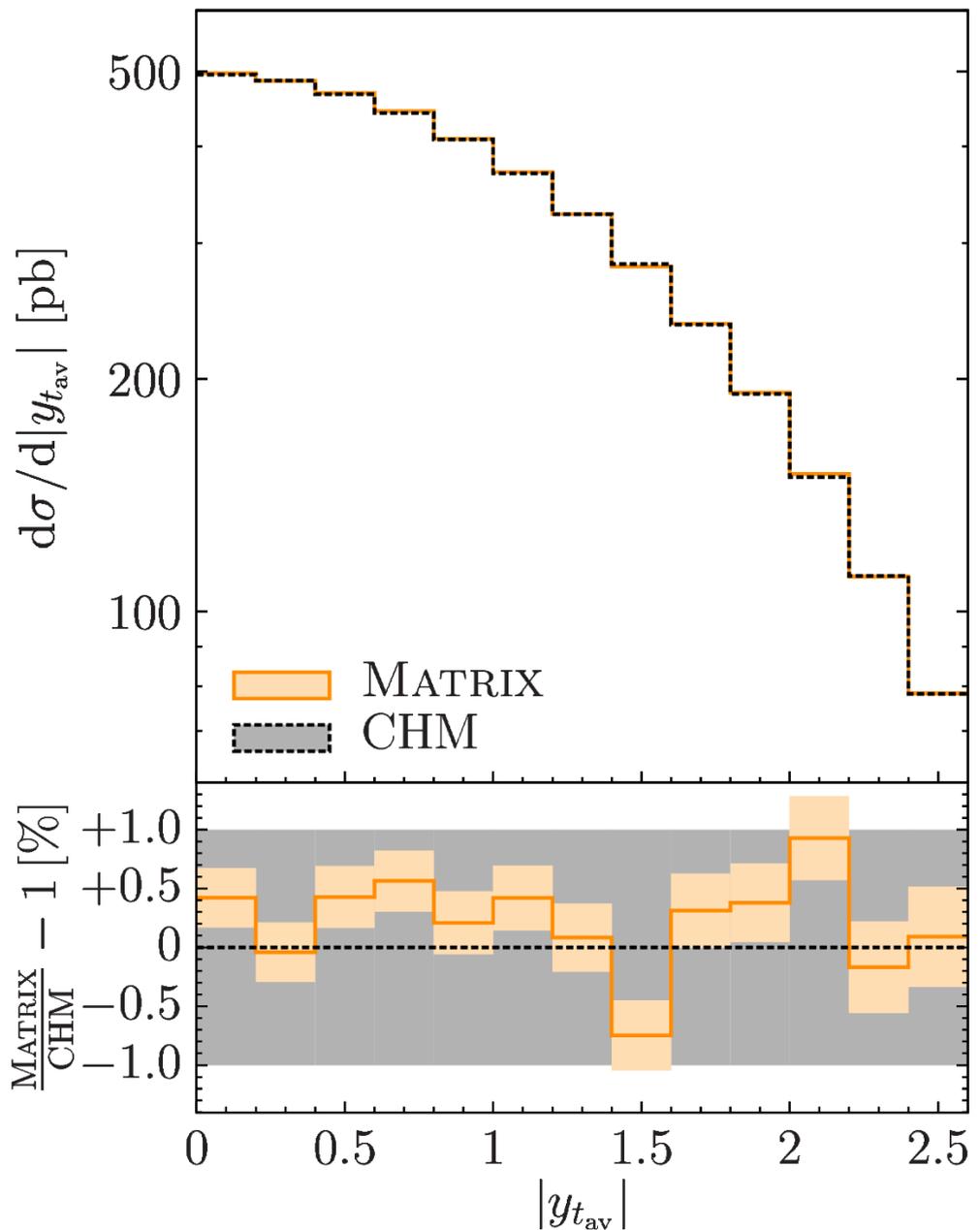
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Excellent agreement even in extreme kinematical regions