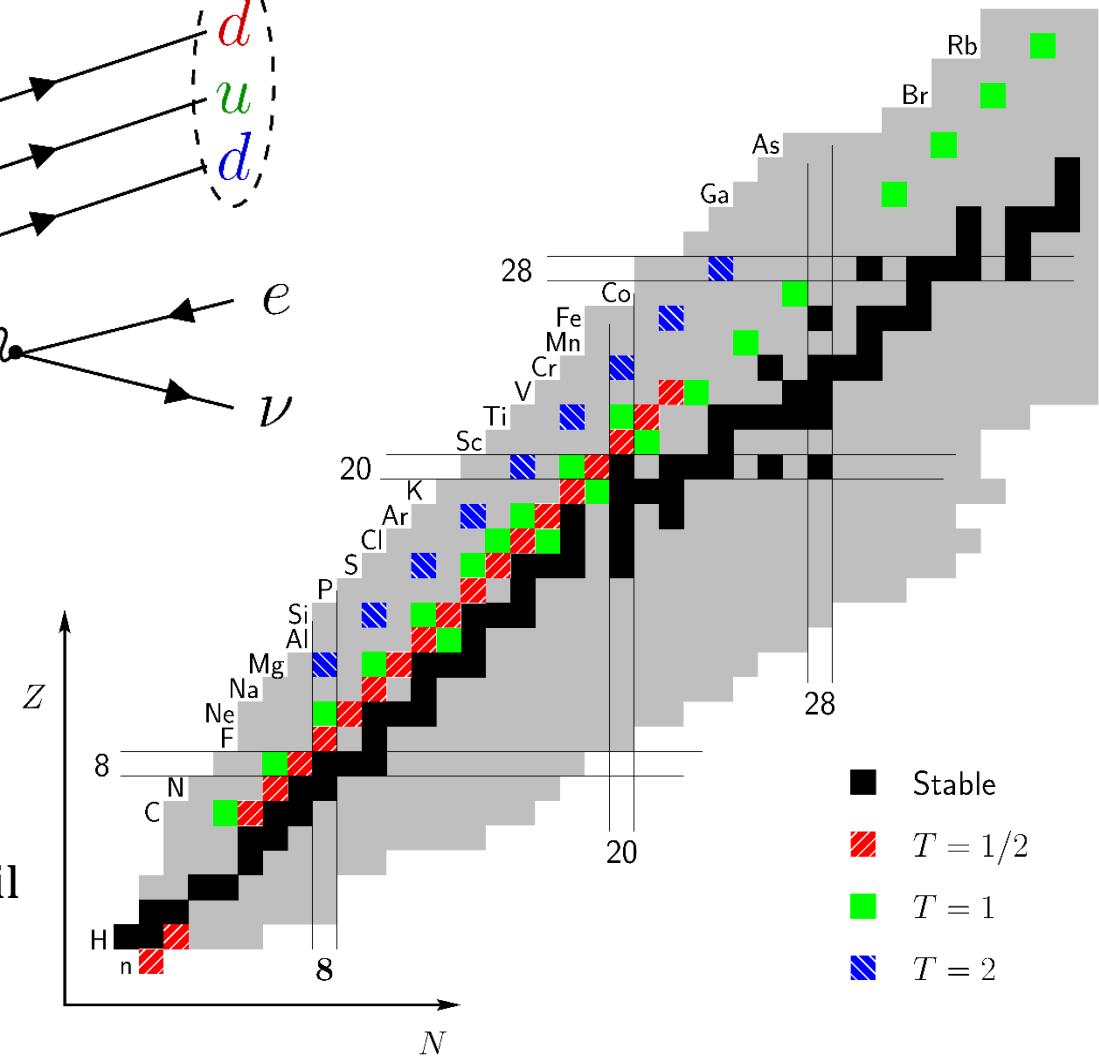
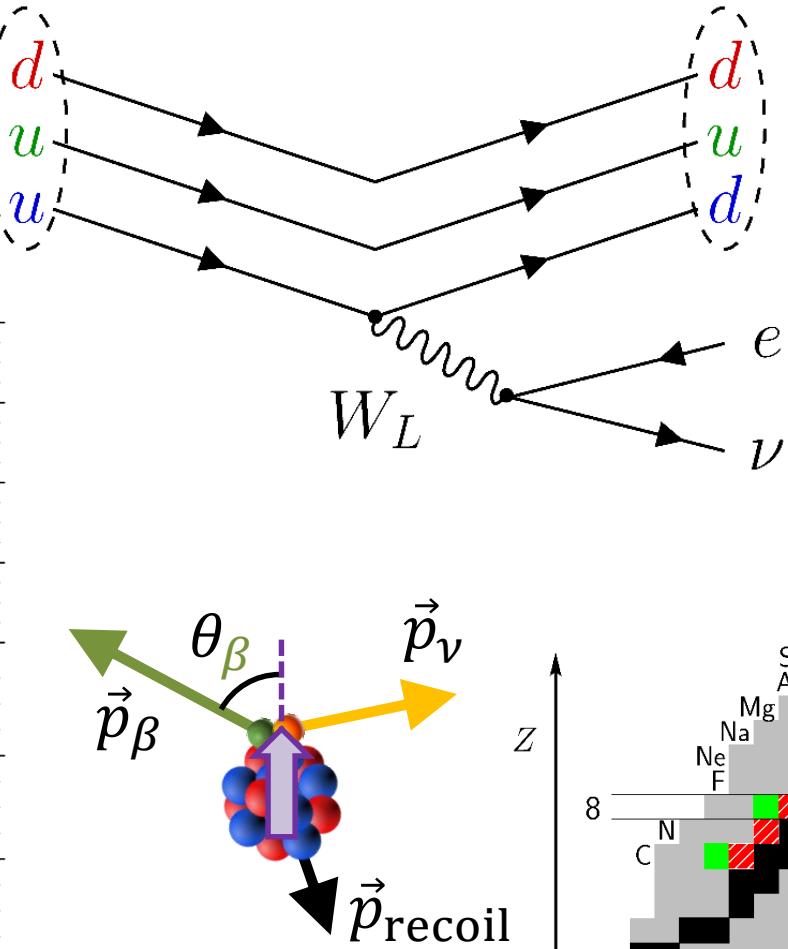
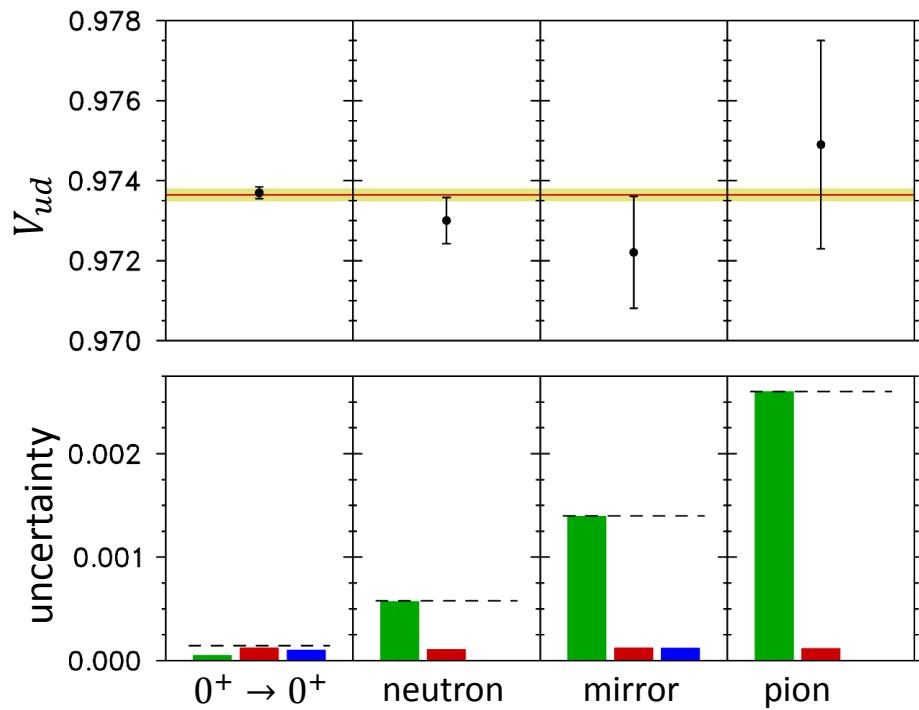


# Outlook for the determination of $V_{ud}$



# Start with an apology 🇨🇦

- ➊ Pretty much the same talk as last week...



# Outline

---

## ● Introduction

- ★ Stuff you probably already know

## ● Present status

- ★  $0^+ \rightarrow 0^+$  superallowed decays
- ★  $T = 1/2$  transitions
- ★ Pion decays
- ★ CKM unitarity

## ● Looking forward

- ★ Inner radiative corrections
- ★ ISB calculations
- ★ Experimental efforts on existing and new nuclei

## ● Summary and outlook

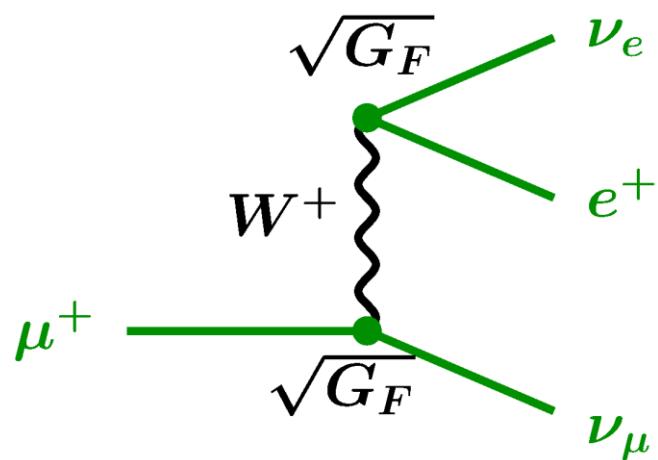
# Everyone here knows this, but...

Cabibbo



mass eigenstates  
≠ weak eigenstates

$$V_{ud} = G_V/G_F$$



$$\text{Unitarity condition: } V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1$$

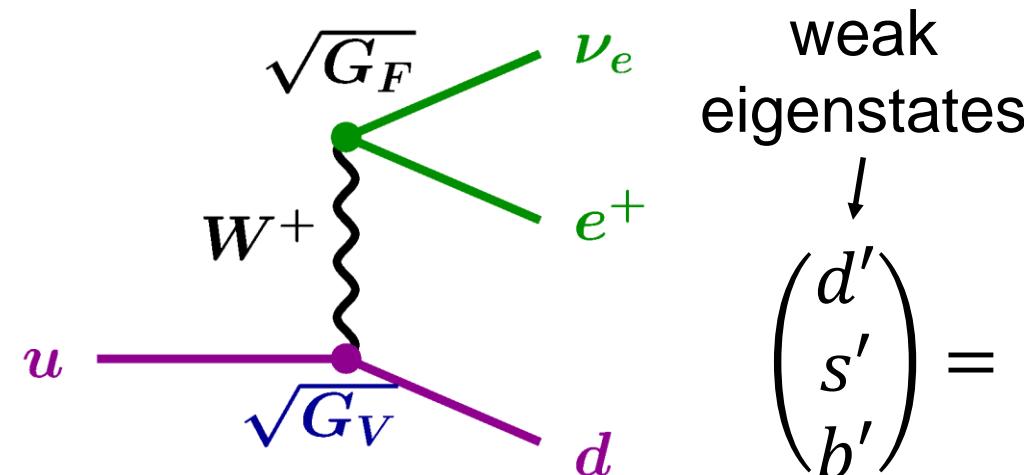
Kobayashi



Maskawa



generalized  
Cabibbo's theory  
to three  
generations



weak  
eigenstates

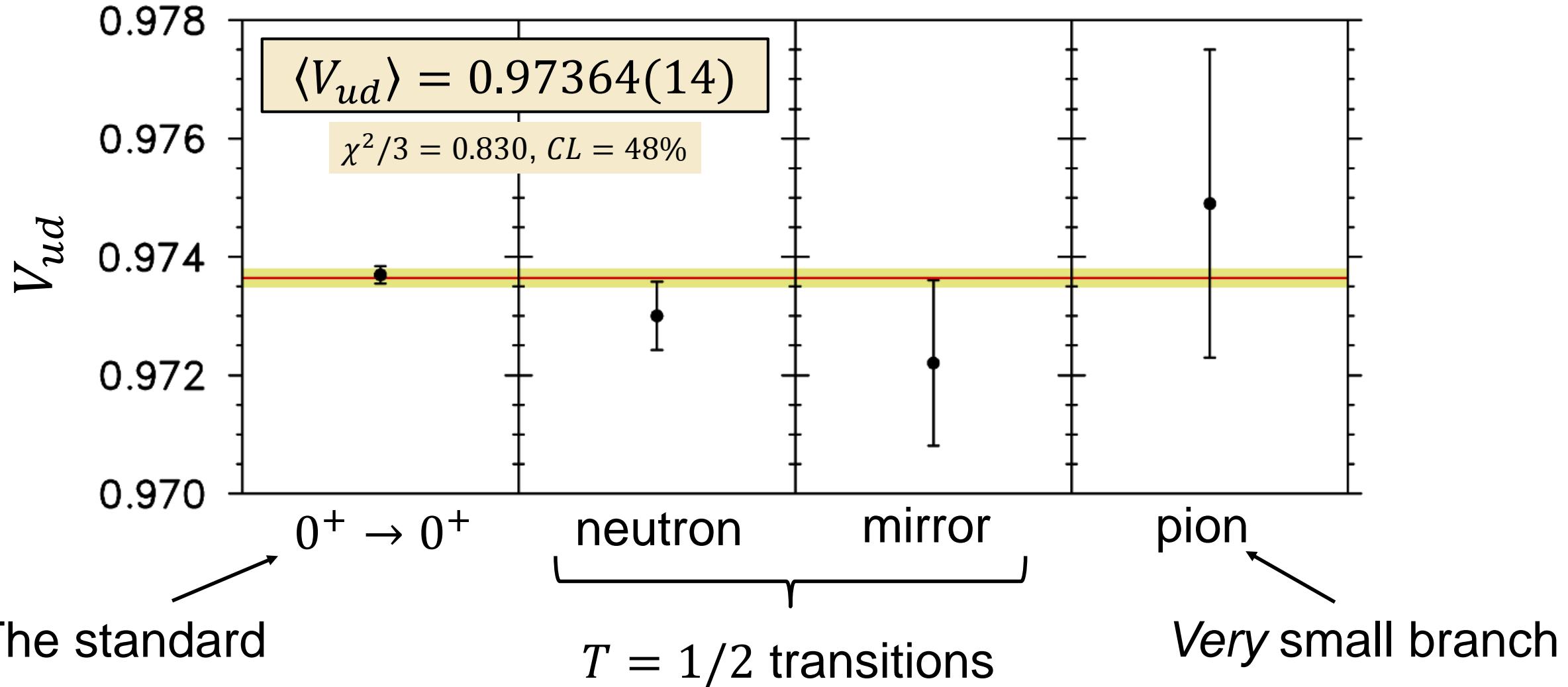
$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Cabibbo-Kobayashi-  
Maskawa (CKM) matrix

# Cutting to the chase

- The current status of  $V_{ud}$  (using Seng's  $\Delta_R^V$  and latest PERKEO III result):

- Seng, Gorchtein, Patel and Ramsey-Musolf, PRL 121, 241084 (2018)
- Markisch, et al., arXiv:1812.04666 (submitted to PRL)



# $0^+ \rightarrow 0^+$ Transitions

- These purely Fermi transitions are theoretically well-understood within the Standard Model

$$\frac{(\text{phase})}{(\text{space})} (\text{partial half life}) = \cancel{ft} \approx \frac{\cancel{K/G_F^2}}{\cancel{V_{ud}^2(M_F^2 + M_{GT}^2)}} \quad 5968.864(6) \text{ s}$$

2            0

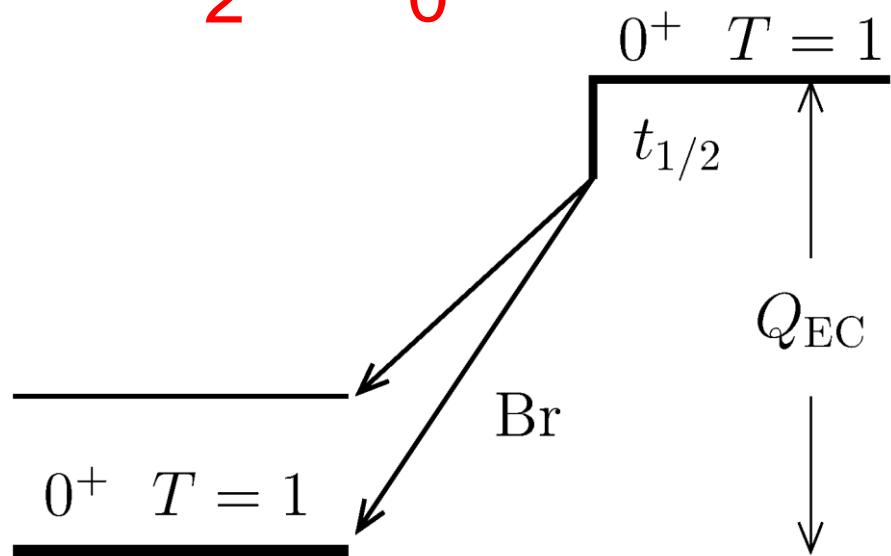
where

$$\cancel{f}(Z, Q_{EC}) = \int F(Z, E) S(E) pE(E - E_0)^2 dE \sim Q_{EC}^5$$

is the phase space factor and

$$\cancel{t}(t_{1/2}, Br) = \frac{t_{1/2}}{Br} (1 + P_{EC})$$

is the partial half life

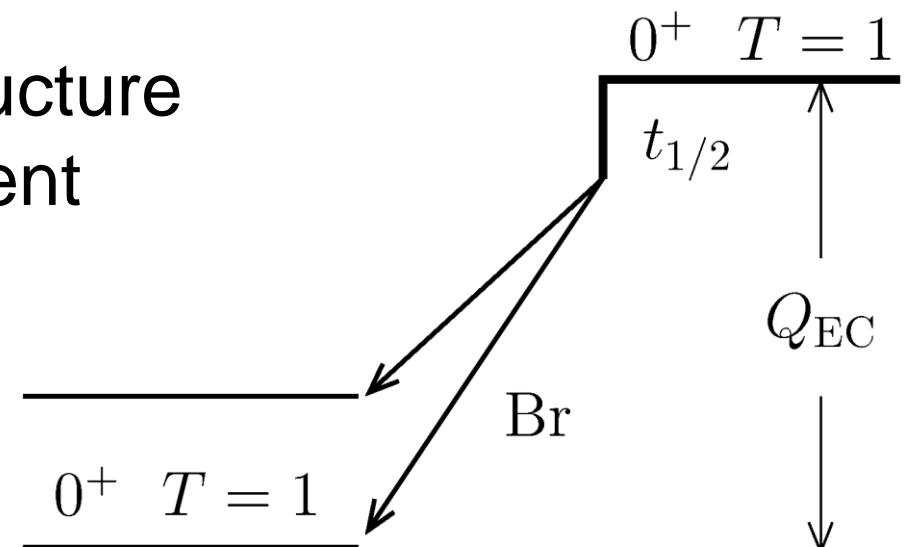


# As we know, it's not *quite* that simple

- One must include small radiative and isospin-symmetry breaking corrections

$$\mathcal{F}t = ft(1 + \delta'_R)[1 - (\delta_C - \delta_{NS})] = \frac{K/G_F^2}{2V_{ud}^2(1 + \Delta_R^V)}$$

- $\delta'_R$ : radiative correction, depends on  $Z$  and  $Q_{EC}$   $\sim 2.4\%$
  - $\delta_C$ : isospin-symmetry-breaking correction
  - $\delta_{NS}$ : radiative correction
  - $\Delta_R^V$ : radiative correction common to any extraction of  $V_{ud}$
- nuclear structure dependent



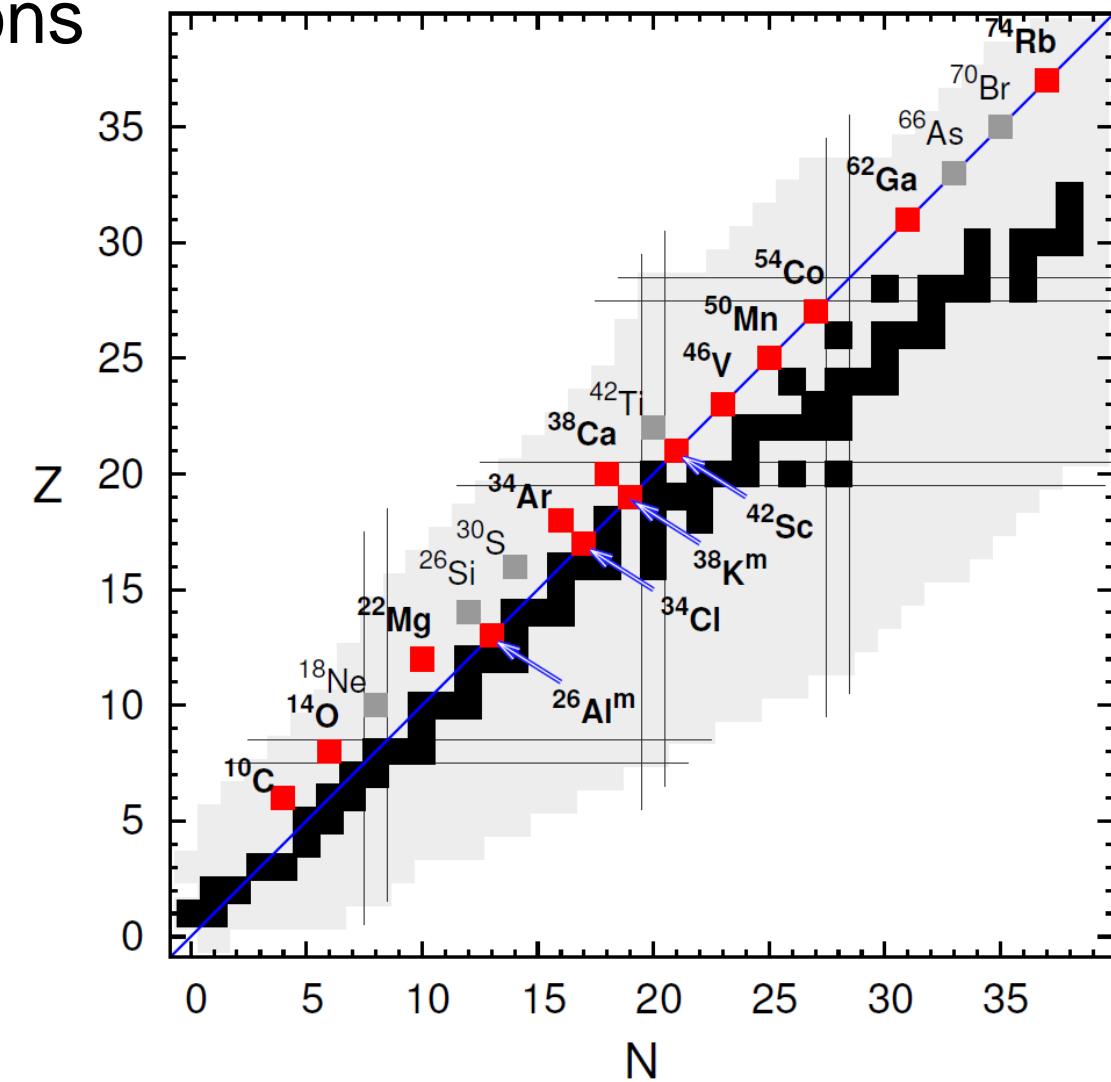
Theoretical uncertainties: 0.05 ?? 0.10%

# Extracting $V_{ud}$ from $0^+ \rightarrow 0^+$ decays

1. Experimentally determine the  $\mathcal{F}t$  value by measuring  $Q_{EC}$ ,  $t_{1/2}$  and the branching ratio, and applying corrections

$$\mathcal{F}t = ft(1 + \delta'_R)[1 - (\delta_C - \delta_{NS})]$$

2. From many transitions, test CVC and the correction terms

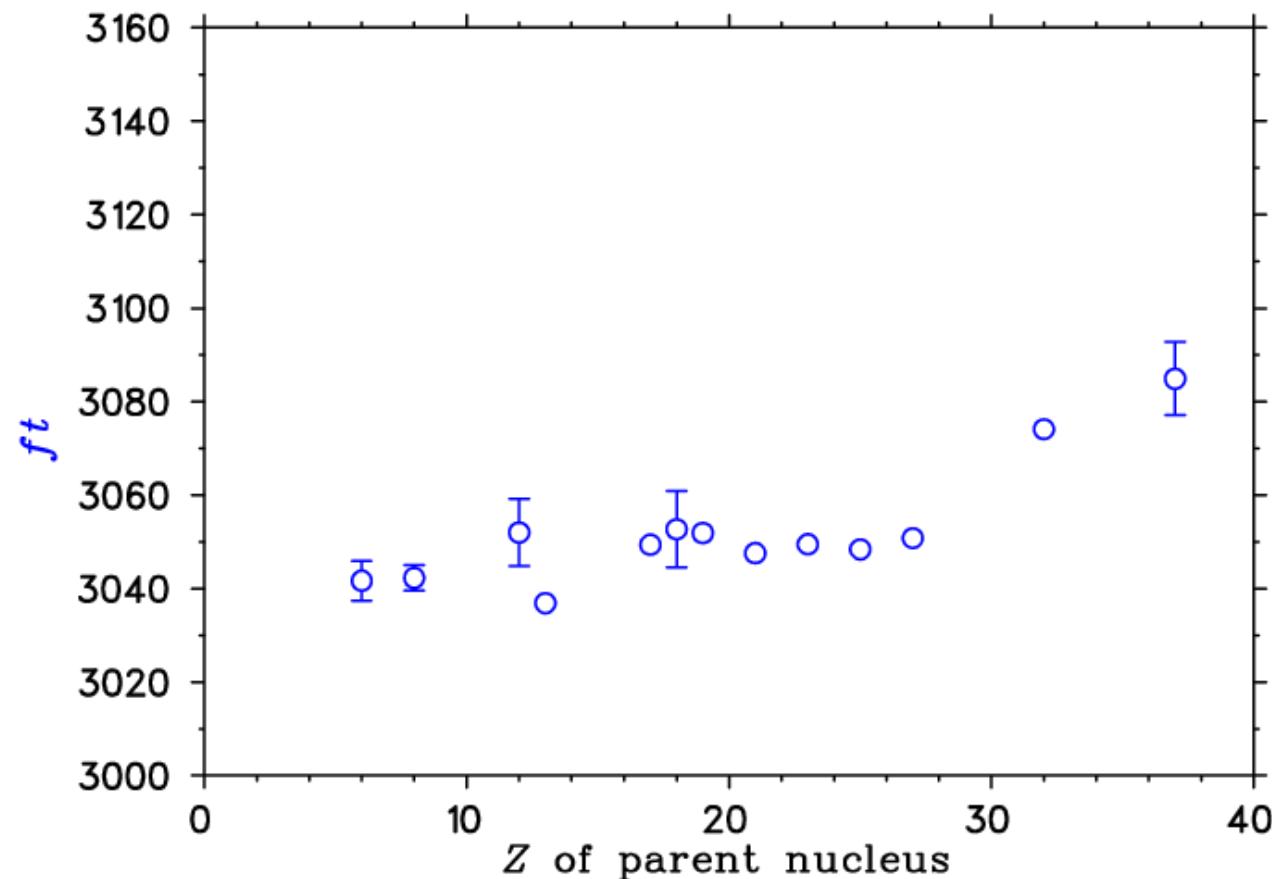


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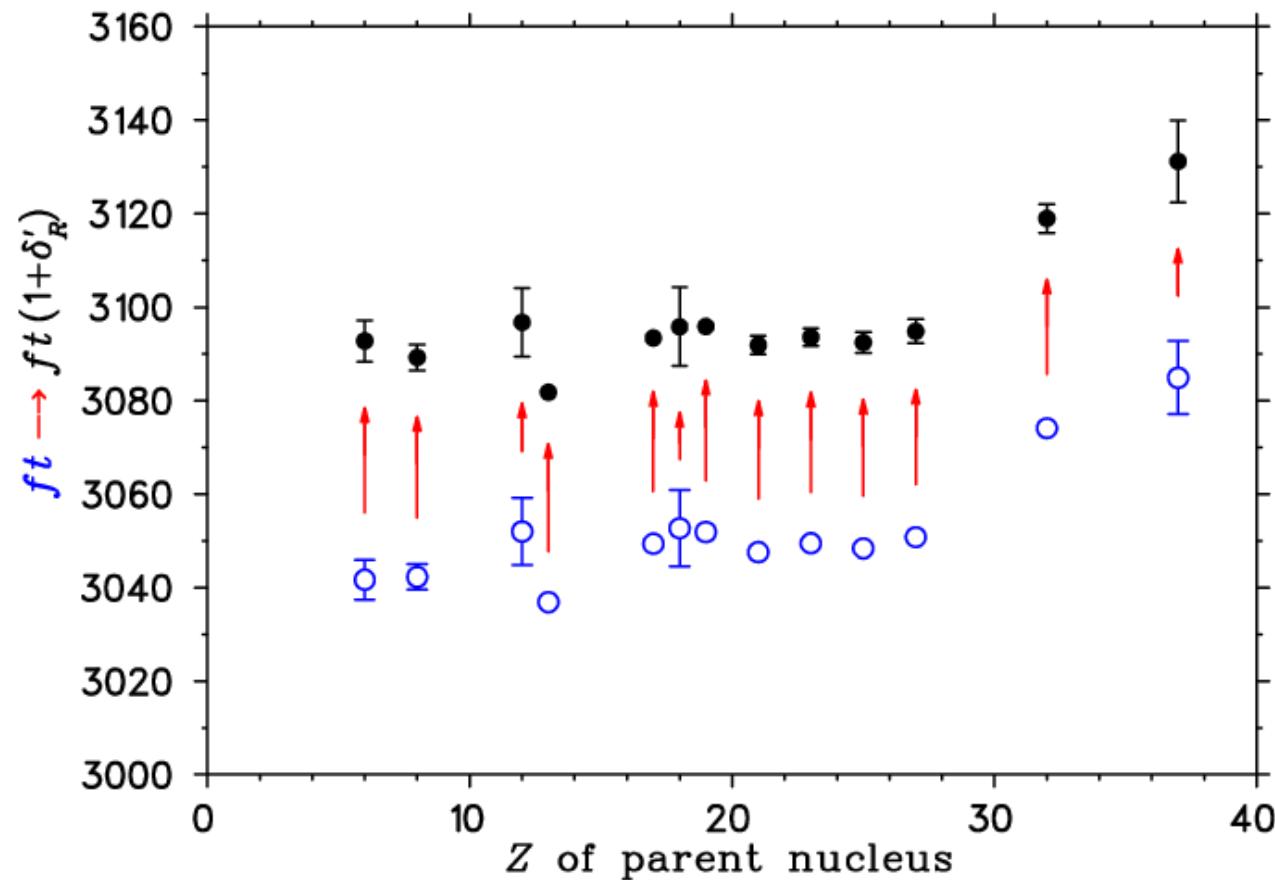
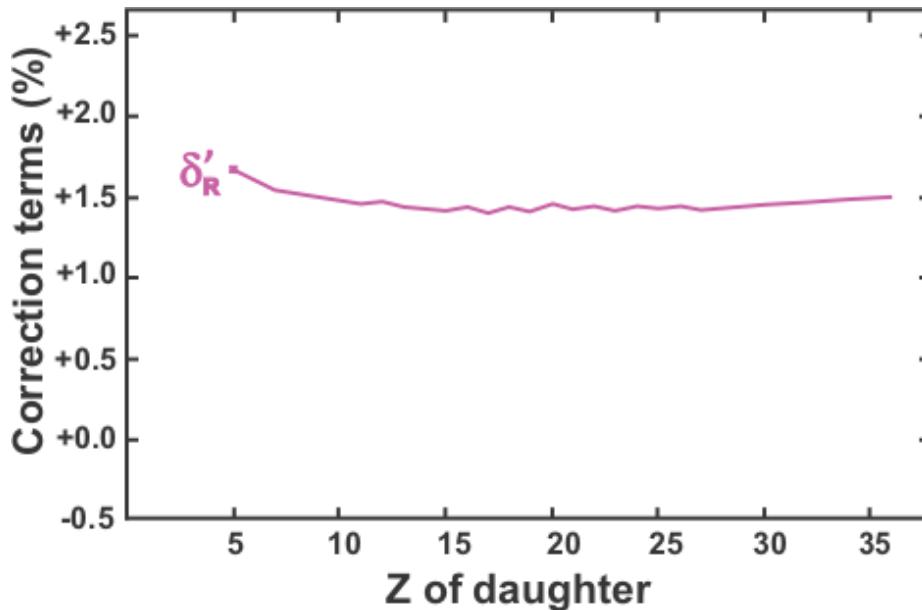


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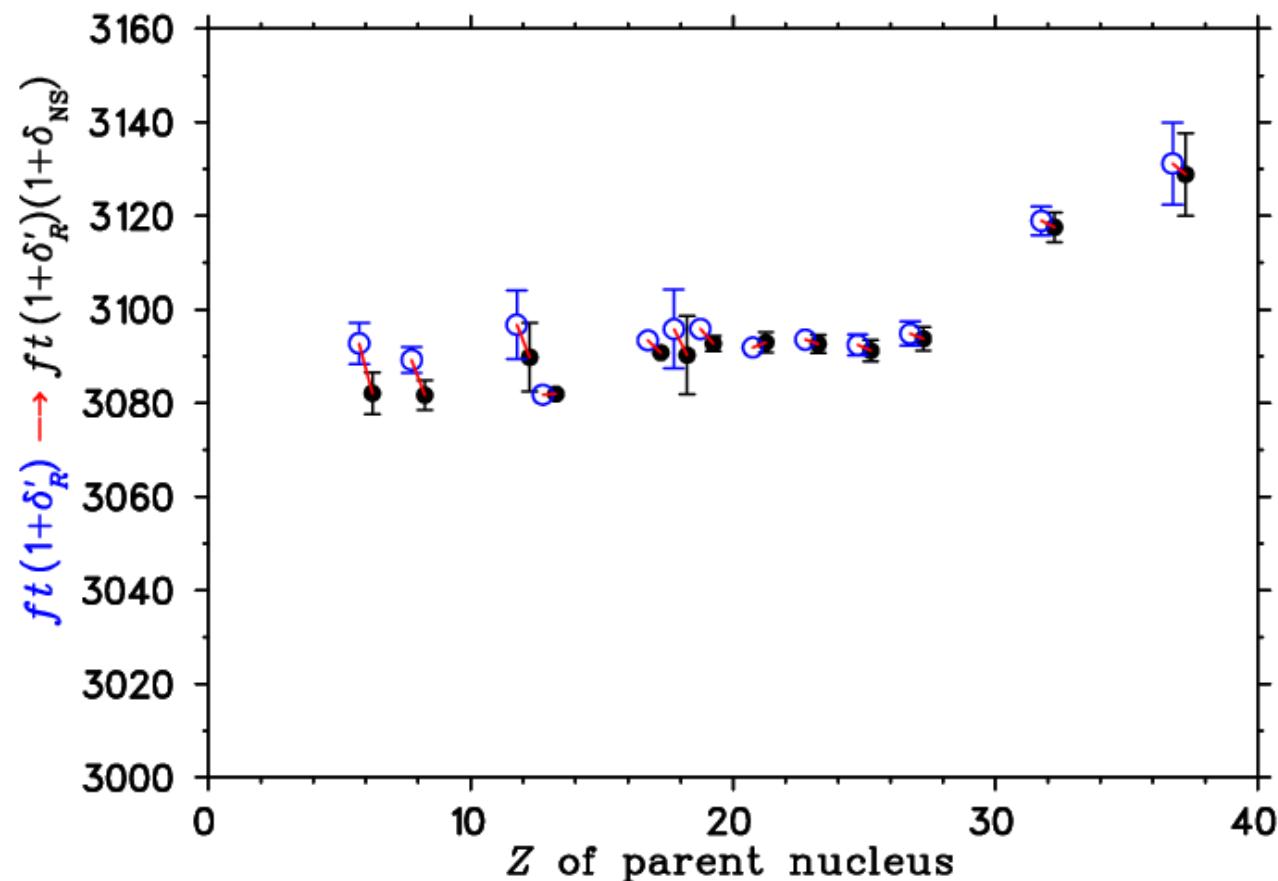
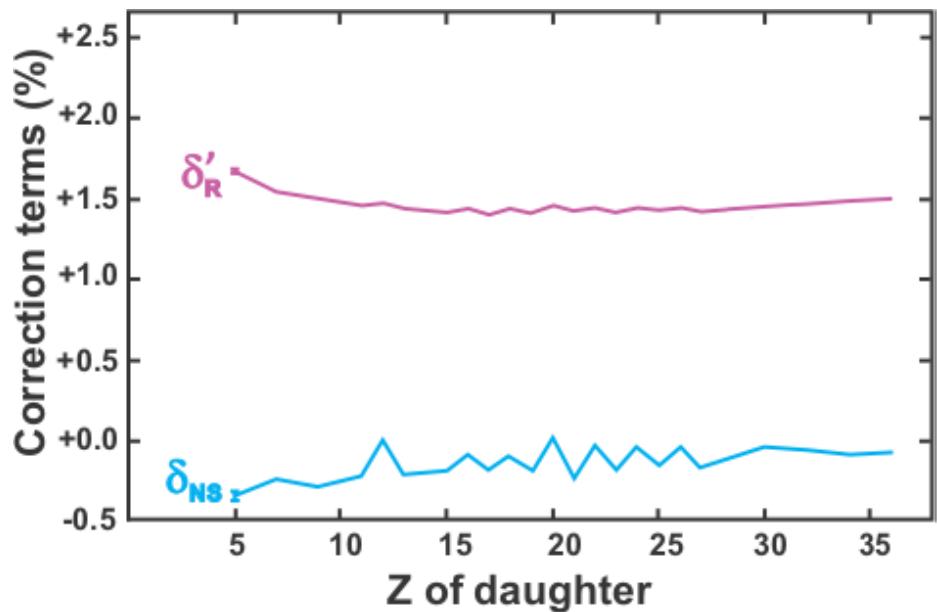


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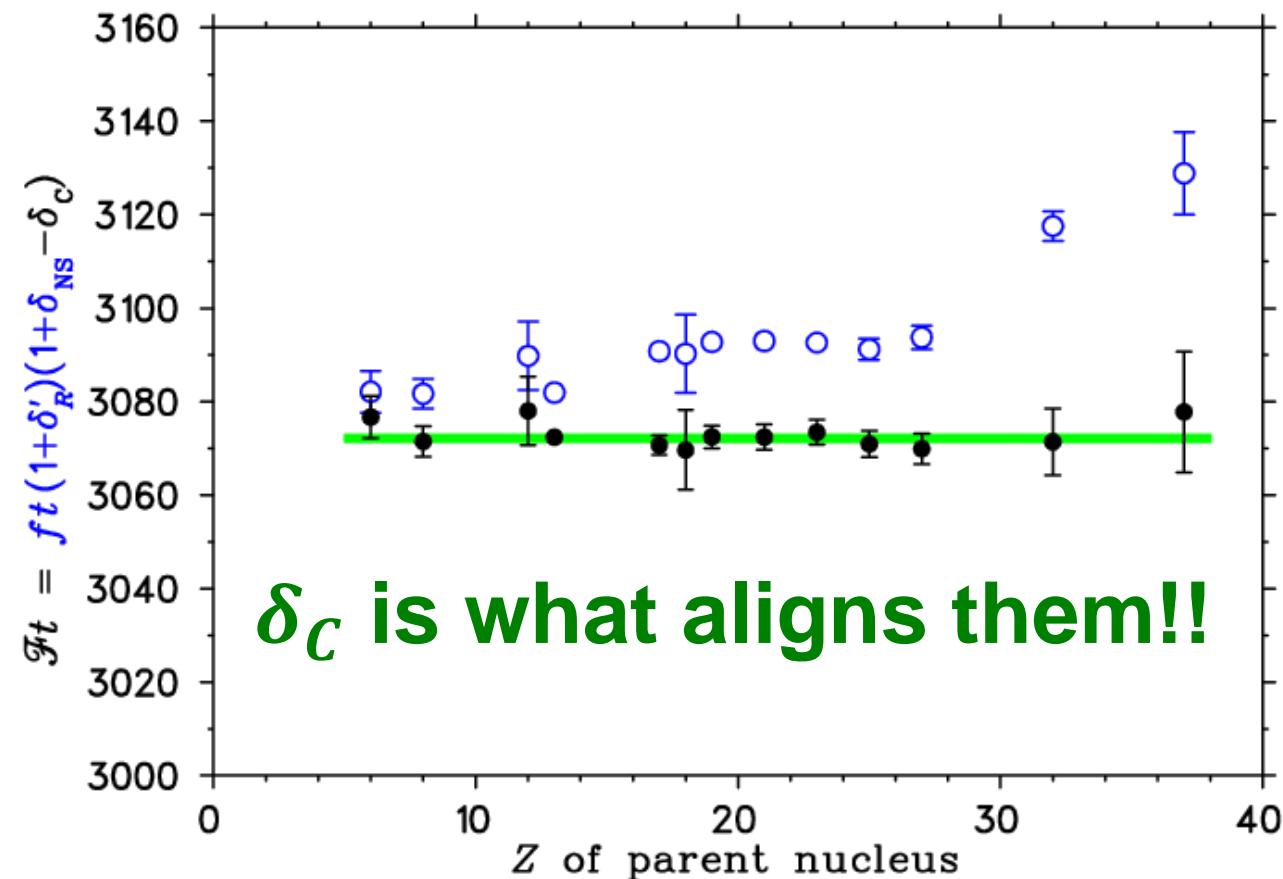
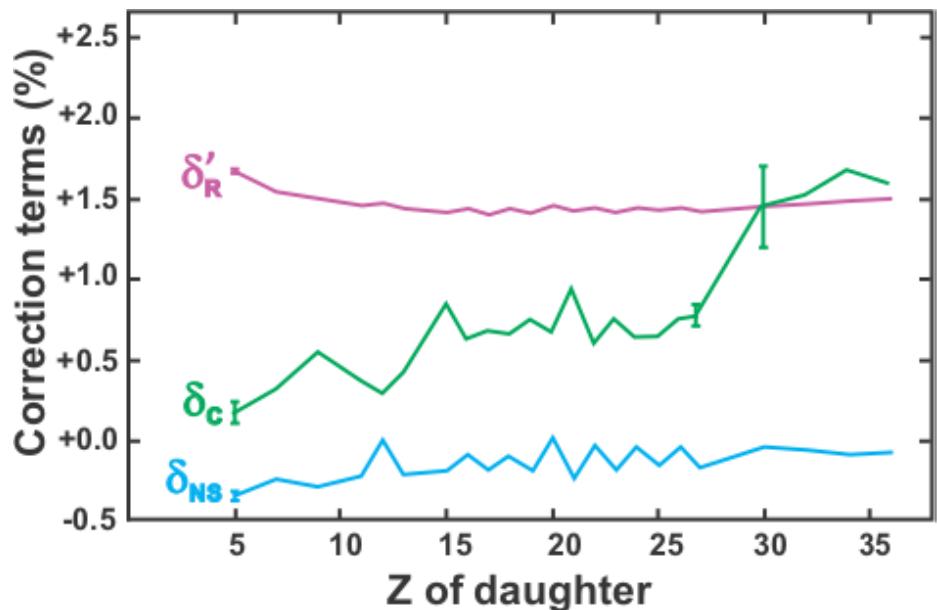


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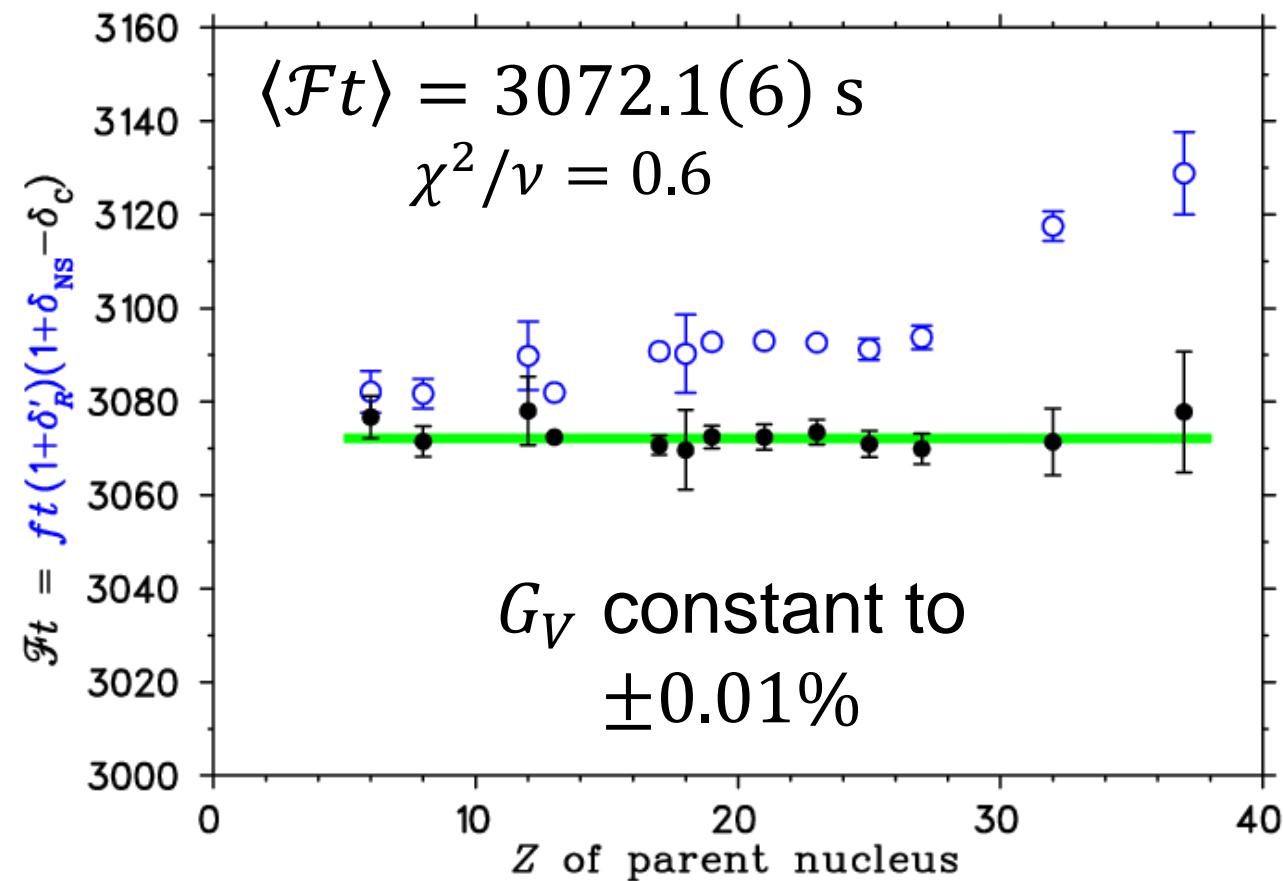
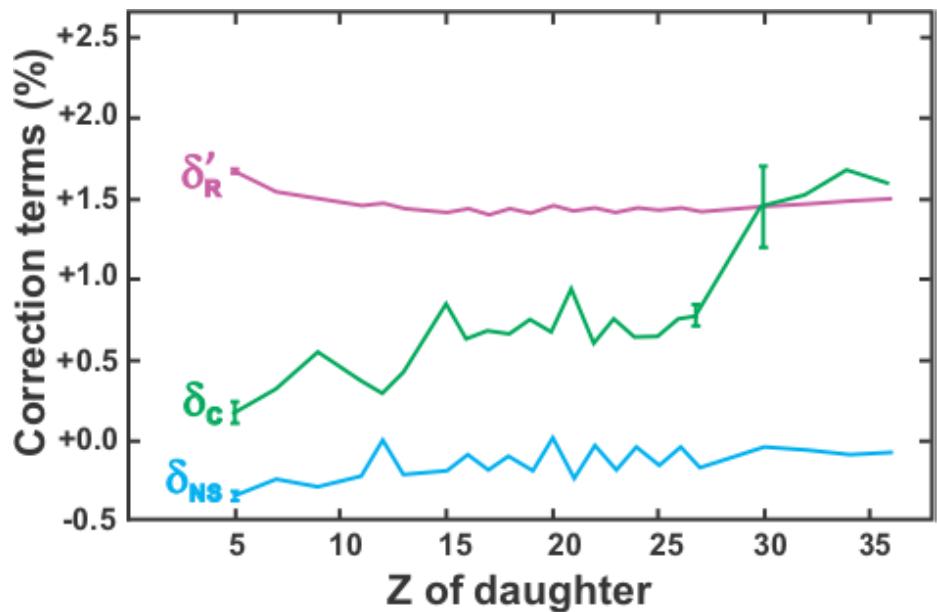


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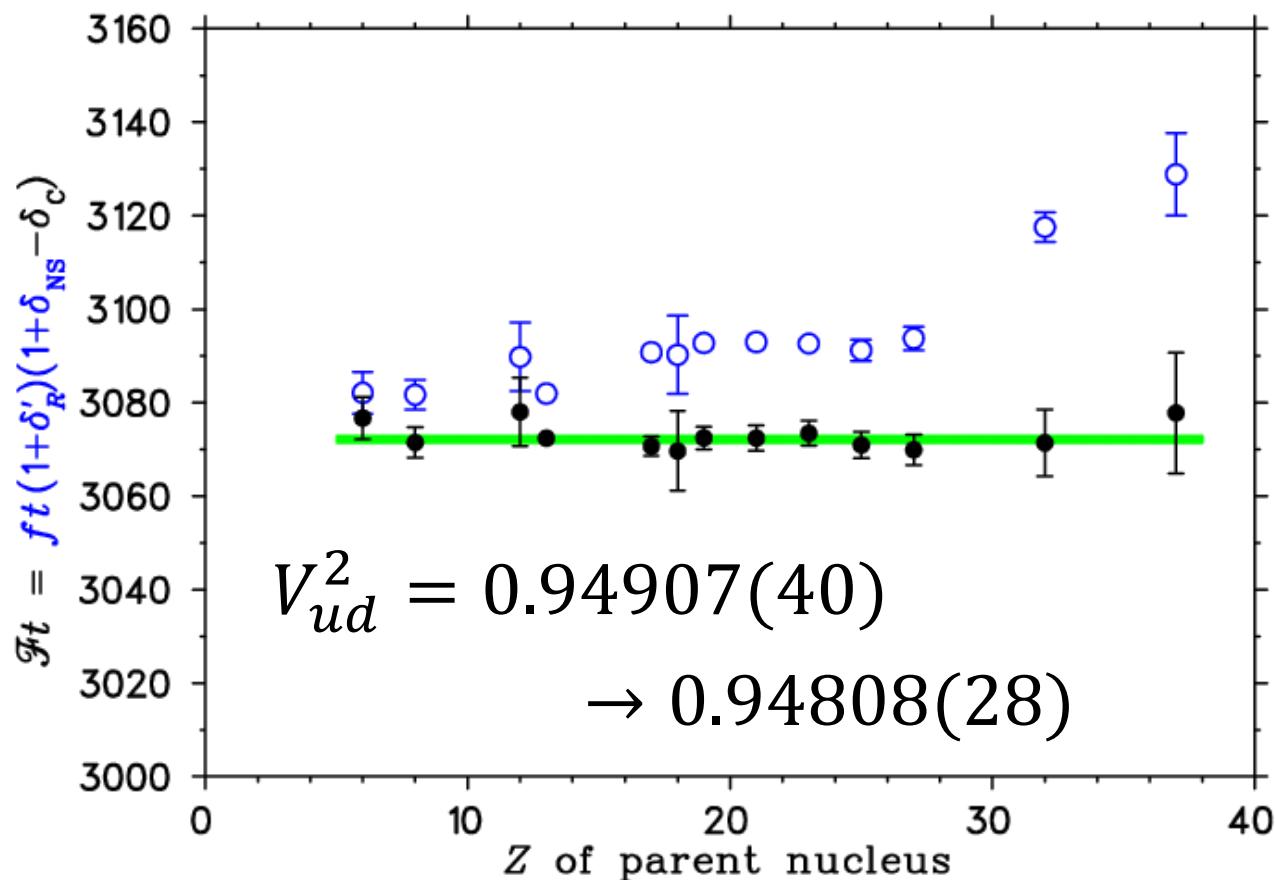
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2. From many transitions, test CVC and the correction terms
3. With CVC verified, determine  $\langle \mathcal{F}t \rangle$  and

$$V_{ud}^2 = \frac{K/G_F^2}{2\langle \mathcal{F}t \rangle(1 + \Delta_R^V)}$$



# Extracting $V_{ud}$ from $0^+ \rightarrow 0^+$ decays

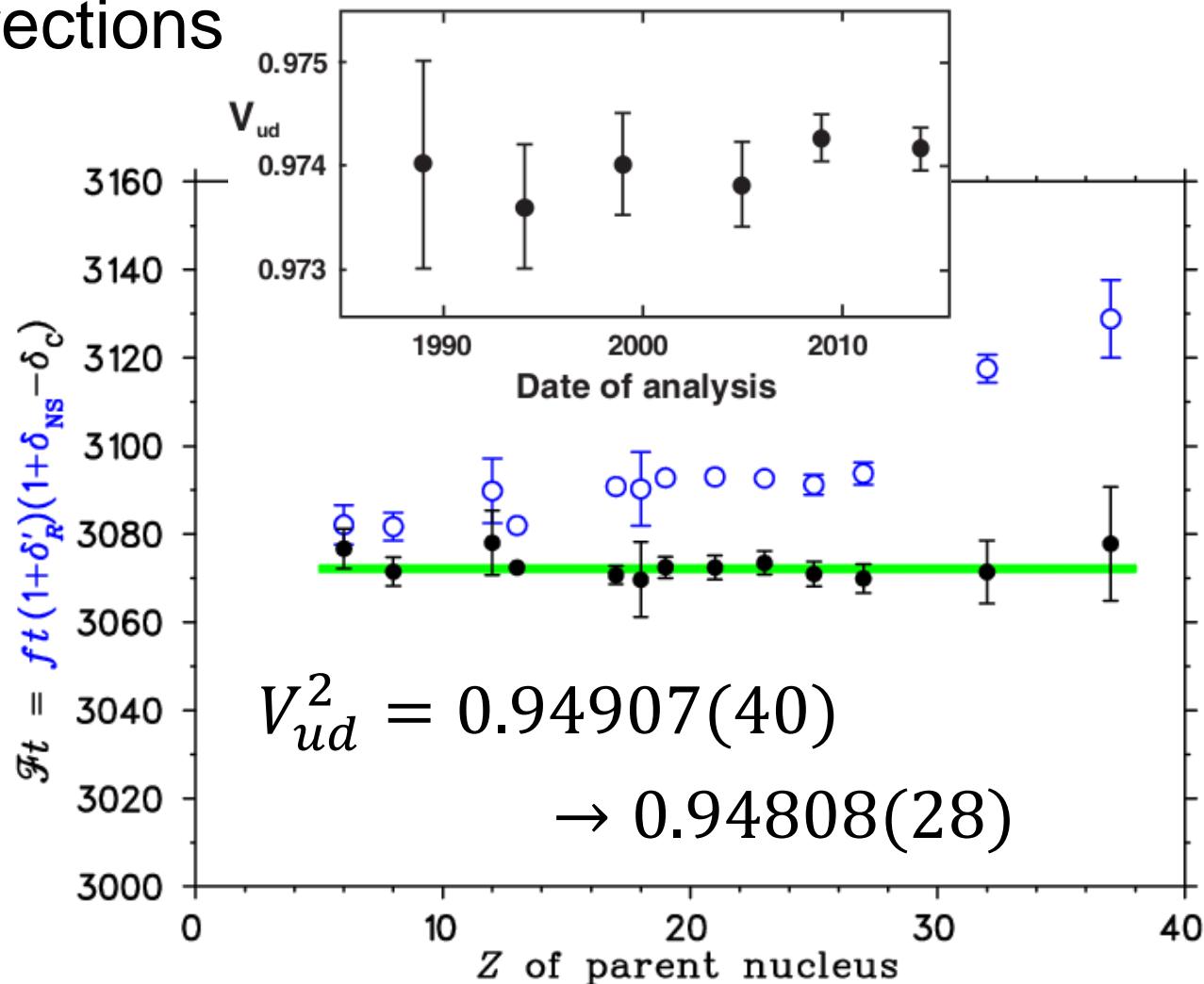
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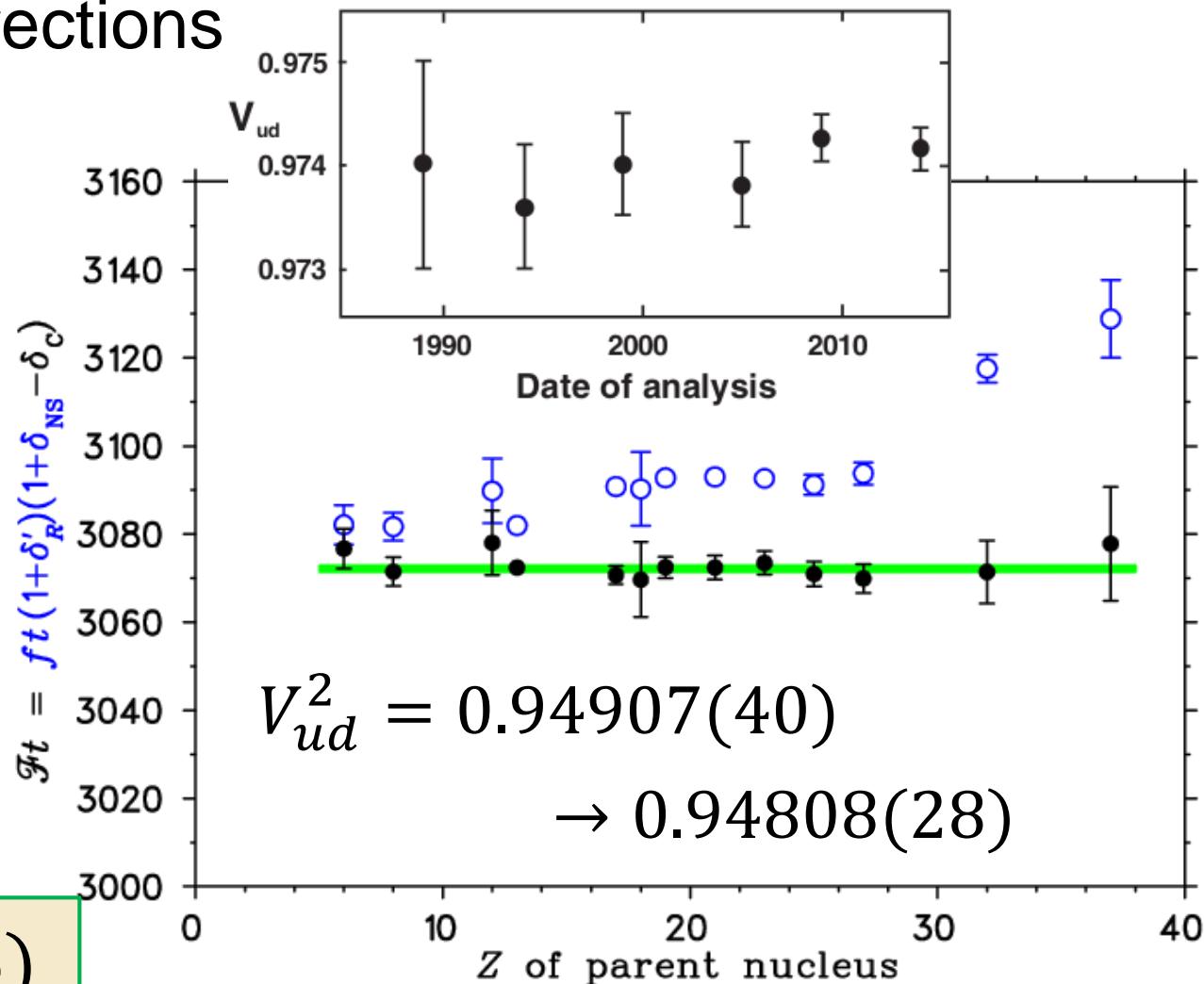
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4. Test CKM unitarity

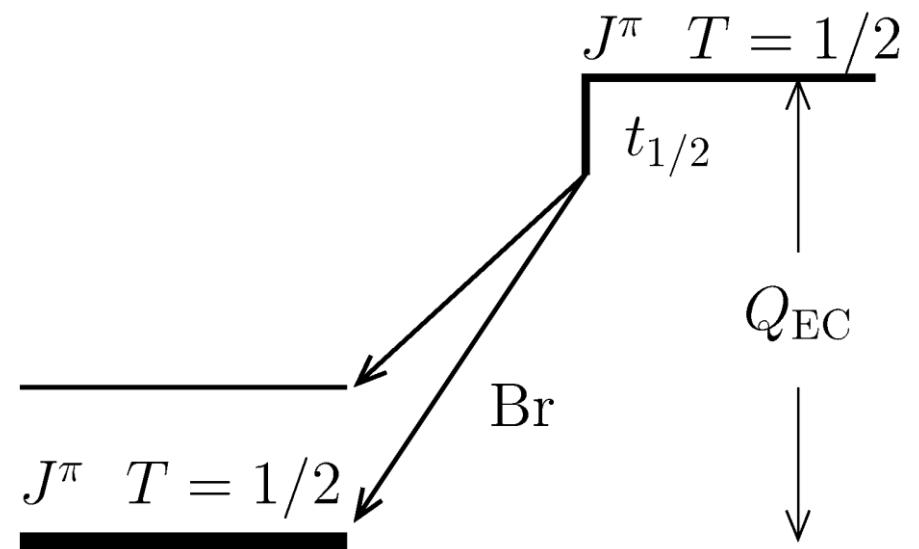
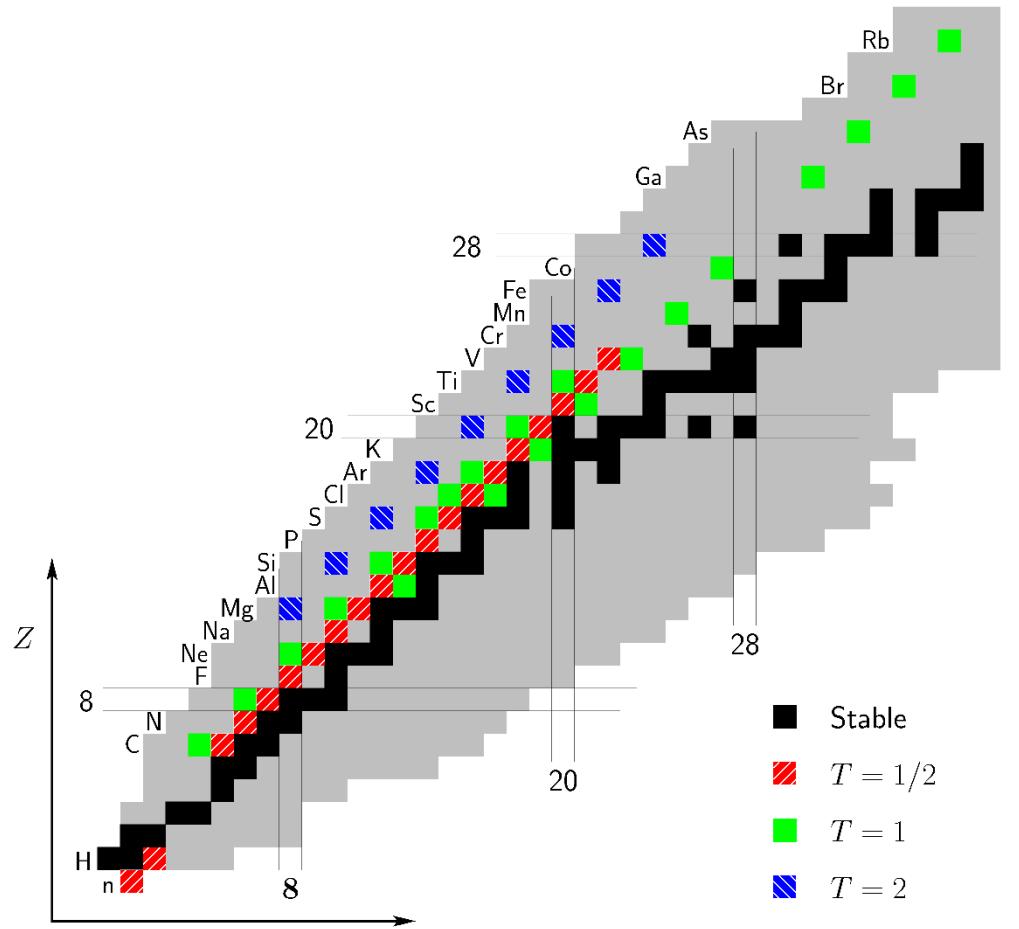
$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.99841(36)$$



# $T = 1/2$ transitions – neutron and mirror decays

- These isobaric analogue decays are also theoretically tractable, but experimentally more difficult (mirrors) and/or limited (only one neutron)

$$\mathcal{F}t = ft(1 + \delta'_R)[1 - (\delta_C - \delta_{NS})] = \frac{K/G_F^2}{V_{ud}^2(1 + \Delta_R^V)(M_F^2 + (G_A/G_F)^2 M_{GT}^2)}$$



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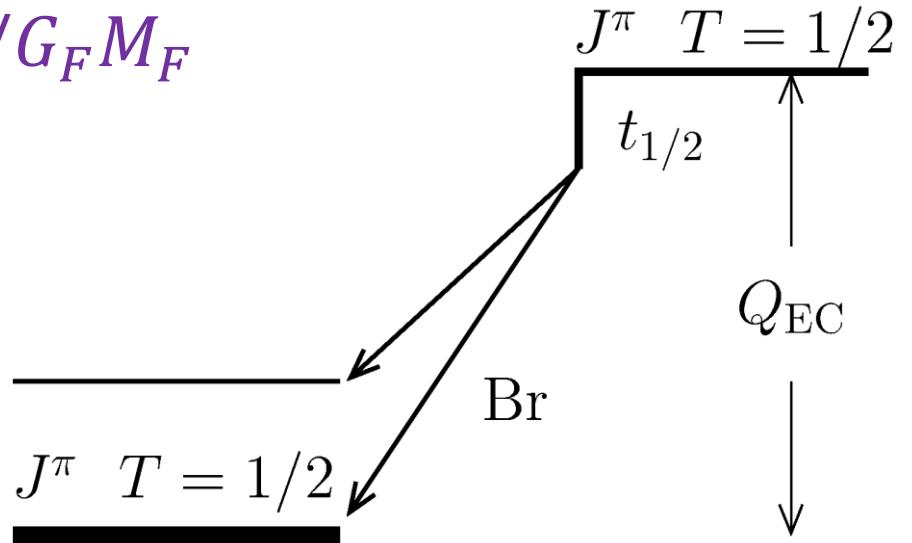
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???

- The neutron:  $M_{GT} = \sqrt{3}$ , but must measure  $\lambda = G_A/G_F$

- Mirror transitions: must measure  $\rho = G_A M_{GT}/G_F M_F$



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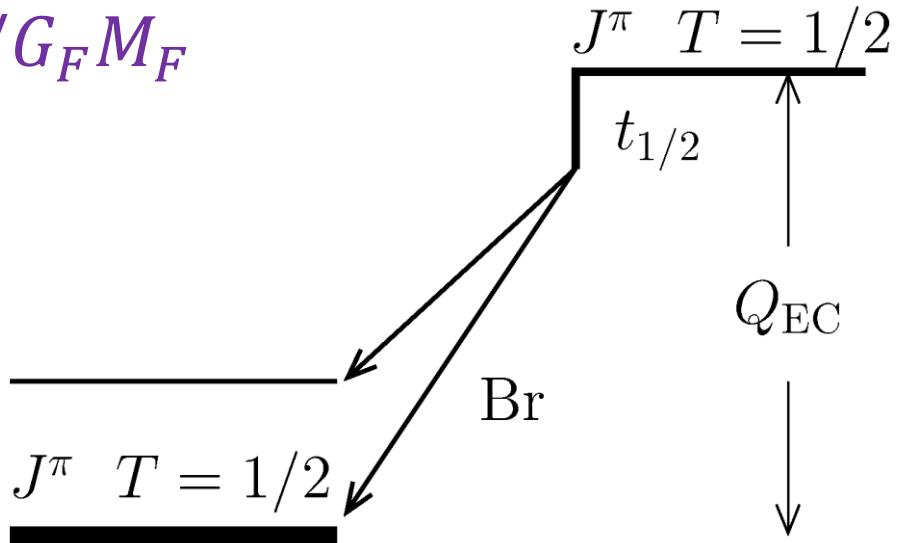
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⇒ must **additionally** measure a correlation parameter, e.g.  $A_\beta$ , and/or  $a_{\beta\nu}$ , and/or ...



+ correlation  
parameter(s)

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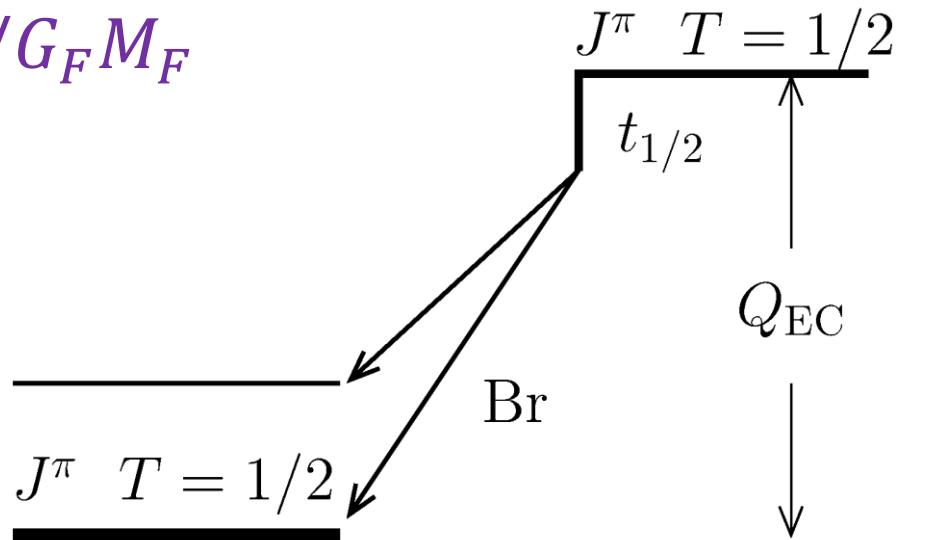
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- Significant plus: **no**  $\delta_C$  or  $\delta_{NS}$  corrections for the neutron!

+ correlation parameter(s)

# Summary of neutron decay

- No time to talk about recent efforts (but see Albert Young's talk from last week!)

$$\tau = 879.7(8) \text{ s}$$

$$\chi^2/\nu = 3.8$$

Beam:  $888.1 \pm 2.0 \text{ s}$

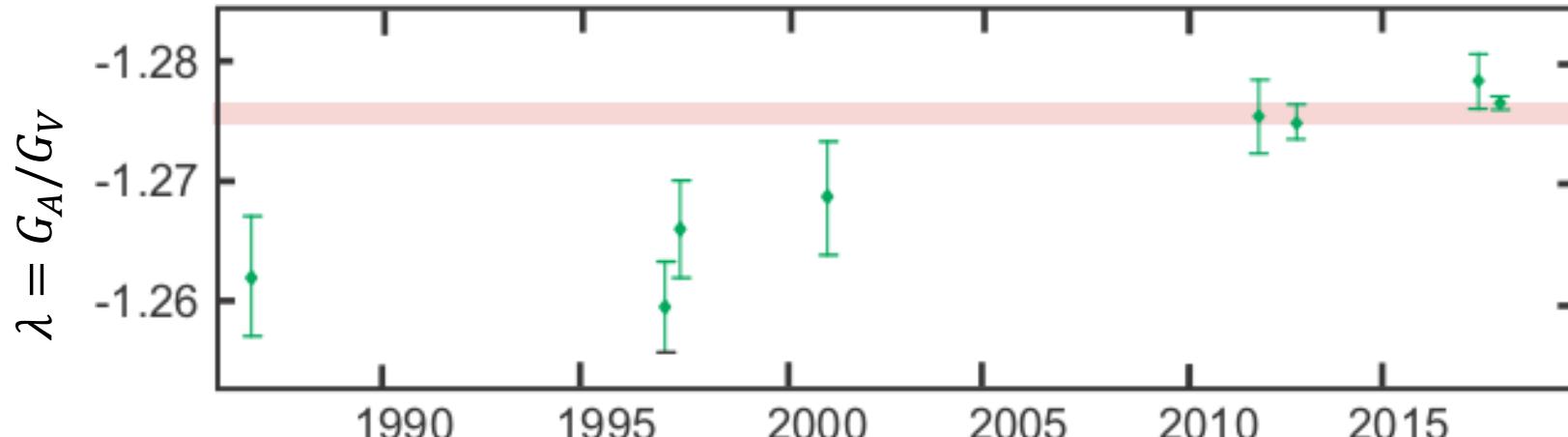
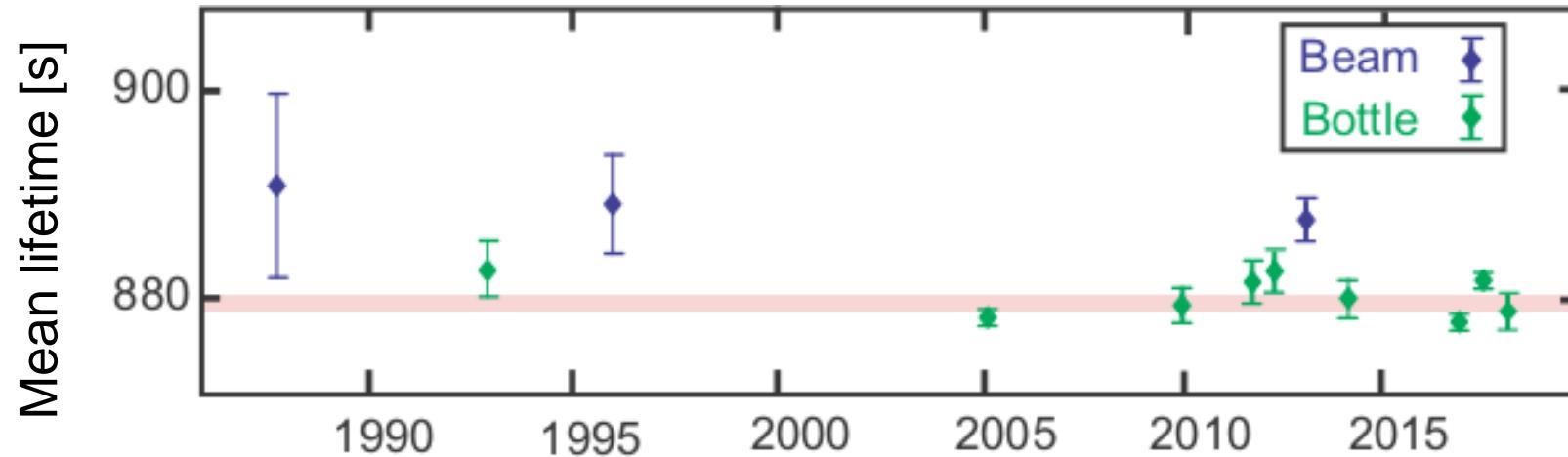
Bottle:  $879.4 \pm 0.6 \text{ s}$

$$\lambda = -1.2764(6)$$

(PERKEO III result  
arXiv:1812.04666)

$$V_{ud} = 0.9730(6)$$

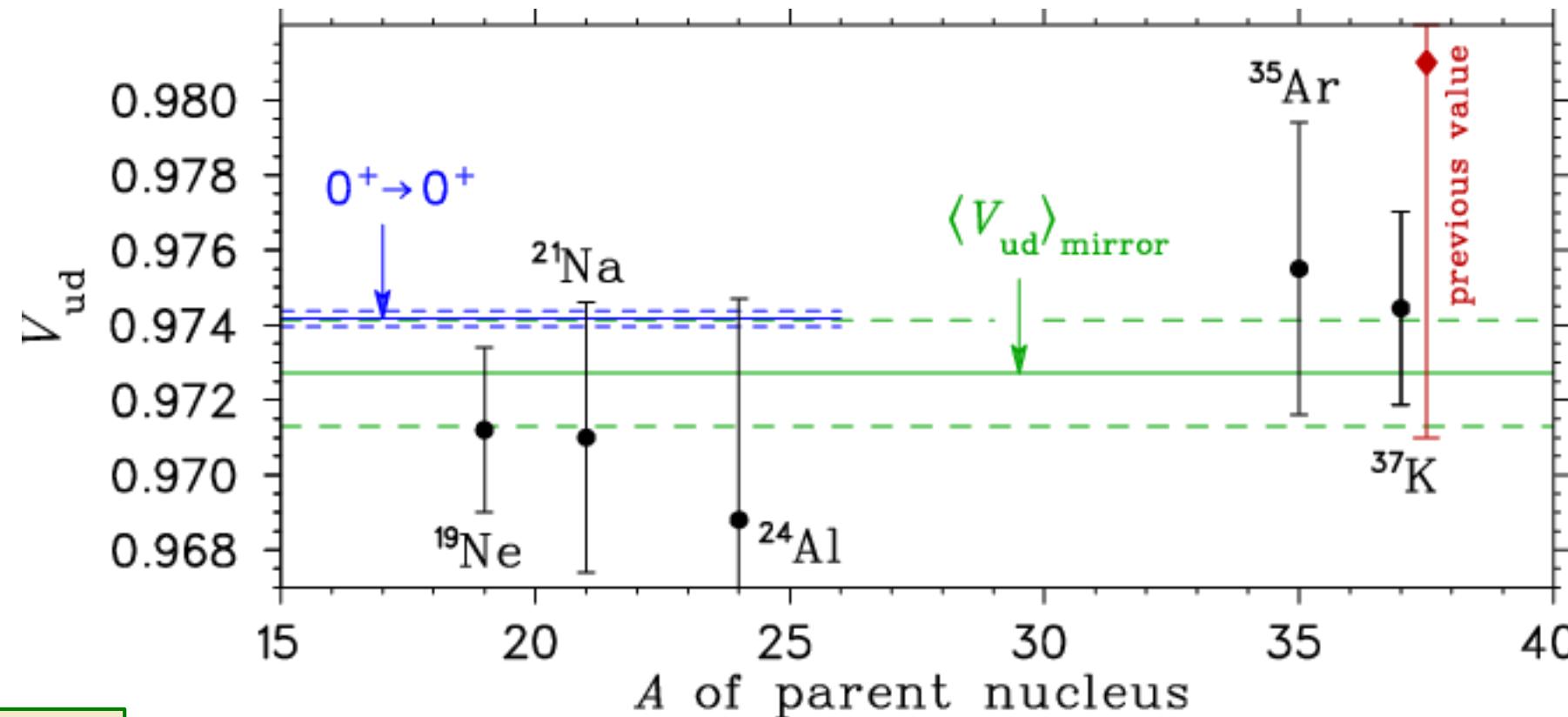
(lots of activity here)



# Summary of mirror transitions

- And Albert talked about  $^{19}\text{Ne}^+$ , but a few other cases have been measured as well:

- All uncertainties dominated by their correlation measurement(s)
- Tough to imagine these will be truly competitive with  $0^+ \rightarrow 0^+$  decays...

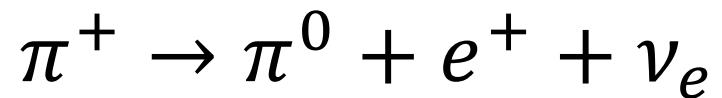


$$V_{ud} = 0.9722(14)$$

<sup>†</sup>Or at least I thought he was...

# And there's the decay of the pion

- Like the neutron, theoretically clean with no  $\delta_C$  nor  $\delta_{NS}$  corrections



- Masses and lifetime known precisely enough, but

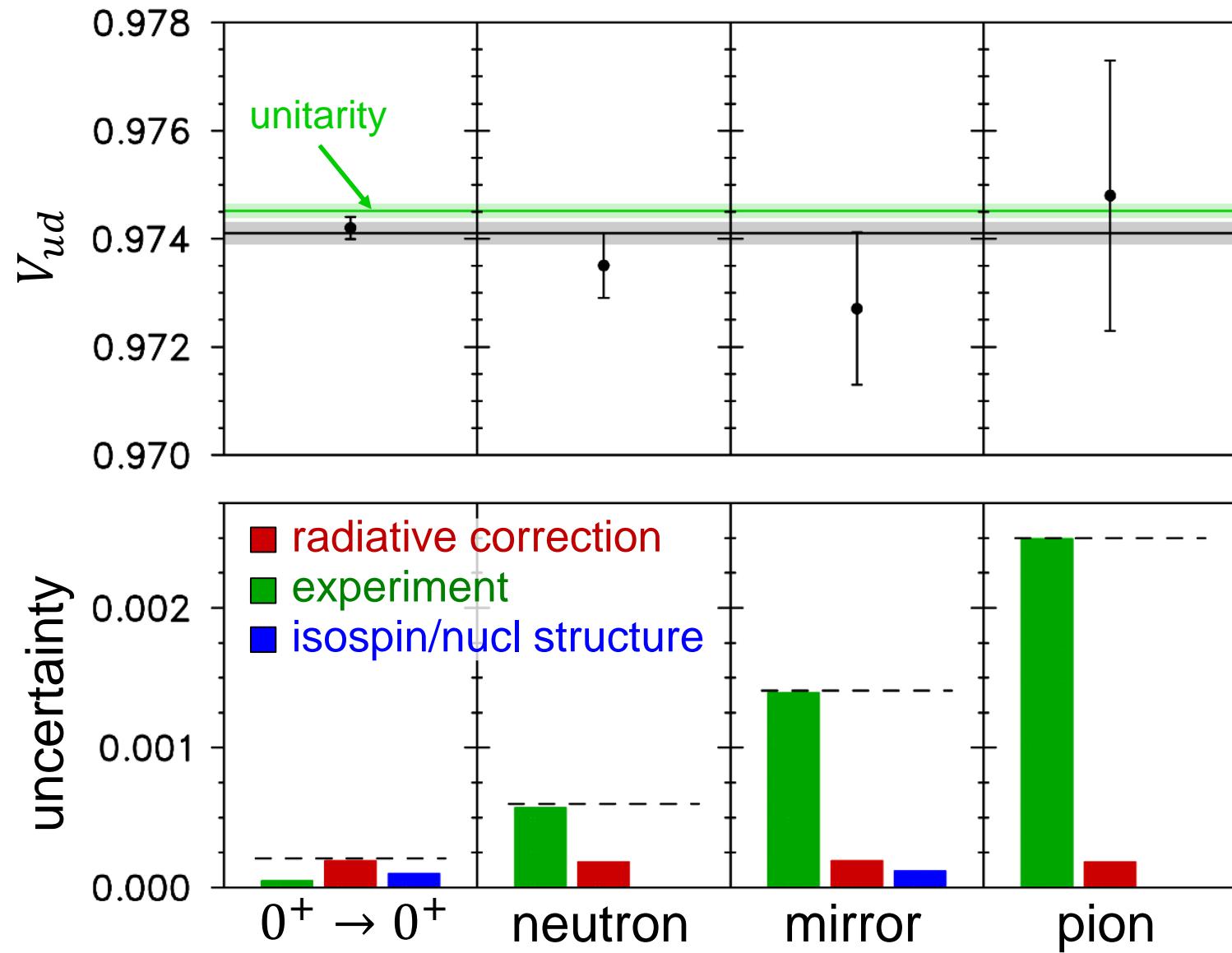
$$\text{Br} = 1.036(7) \times 10^{-8}$$

is a ***really small*** branch!

$$V_{ud} = 0.9743(25)$$

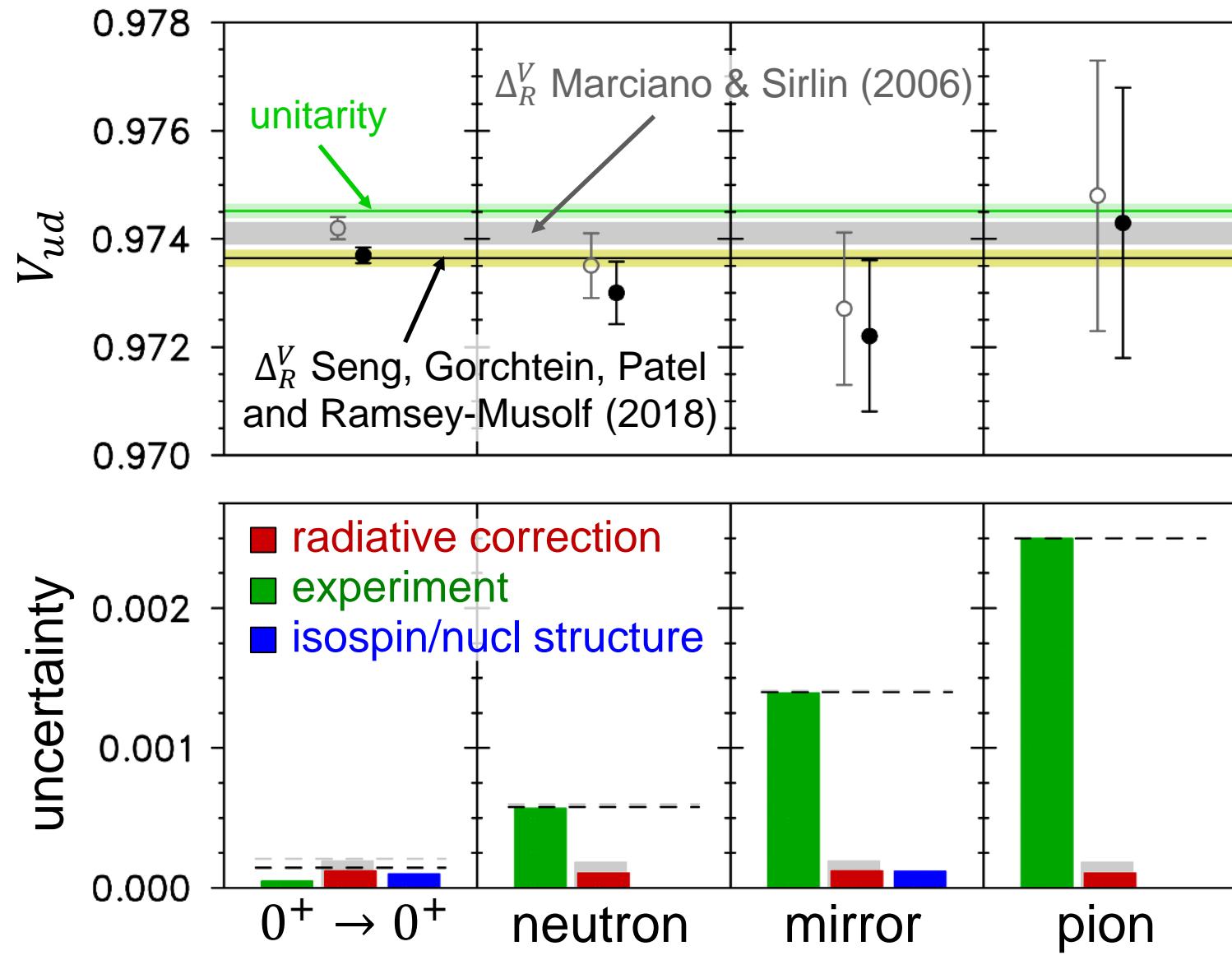
- No (ambitious) plan to improve the branching ratio, not likely this will get more precise in the near future.

# Summary of current status of $V_{ud}$



- $0^+ \rightarrow 0^+$ :  
 $V_{ud} = 0.9742(2)$
- The neutron  
 $V_{ud} = 0.9735(6)$
- Mirror transitions  
 $V_{ud} = 0.9727(14)$
- The pion  
 $V_{ud} = 0.9748(25)$

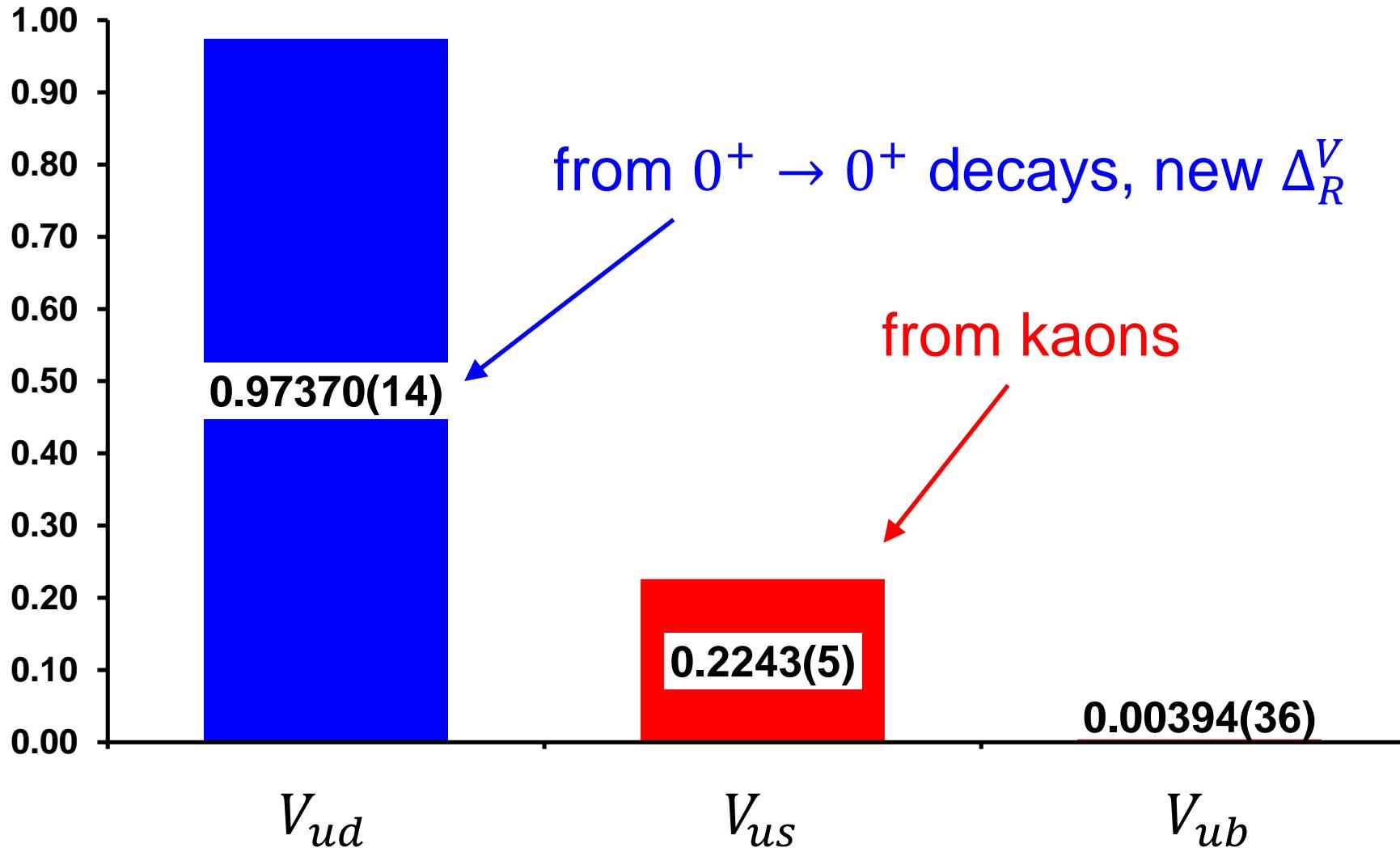
# Summary of current status of $V_{ud}$



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 $\rightarrow 0.9737(1)$
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 $\rightarrow 0.9730(6)$
- Mirror transitions  
 $V_{ud} = 0.9727(14)$   
 $\rightarrow 0.9722(14)$
- The pion  
 $V_{ud} = 0.9748(25)$   
 $\rightarrow 0.9743(25)$

# Summary of current status of CKM unitarity

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1 - \Delta_{\text{CKM}}$$



# Summary of current status of CKM unitarity

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1 - \Delta_{\text{CKM}}$$

•  $V_{ud}^2 = 0.94798(27)$

from nuclear, neutron and  $\pi^+$  decays;  $\Delta_R^V$  from Seng *et al.*, PRL **121**, 241804 (2018)

•  $V_{us}^2 = 0.05031(22)$

from kaon decays (PDG)

$$\Rightarrow \Delta_{\text{CKM}} = 1.69(35) \times 10^{-5}$$

is **still** dominated by  $\Delta_R^V = 2.467(22)\%$   
(though kaons barely behind now)

•  $V_{ub}^2 = 0.00002$

from  $B$  decays (negligible)

If the uncertainty in  $\Delta_R^V$  is further reduced by  $3 \times$ :  
 $\Rightarrow$  uncertainty in  $V_{ud}^2 \rightarrow 0.00020$   
and uncertainty in  $\Delta_{\text{CKM}} \rightarrow 0.00030$

– JCH

# Looking ahead

- “What is the inner radiative correction,  $\Delta_R$ ? ”
  - ★ Currently the most important and impactful way to improve the unitarity test
- “How much can we believe the ISB corrections? Can we test them?”
  - ★ At the moment, HF shell model the only one to truly satisfy CVC
- “Can we improve existing cases with  $\Delta\mathcal{F}t \lesssim 0.25\%$ ? ”
  - ★ Maybe, but with ~220 measurements going into 15 *ft* values...it ain’t easy to make a dent
- “Can we add new  $0^+ \rightarrow 0^+$  transitions with  $\Delta\mathcal{F}t \lesssim 0.25\%$ ? ”
  - ★ Yes, but will require theoretical progress in heavier nuclei
- “How much progress can be made with  $T = 1/2$  transitions?”
  - ★ The neutron still has problems (beam vs bottle), but is only 4× less precise than  $0^+ \rightarrow 0^+$ , and there is a lot of experiments in progress and planned
  - ★ Determining  $\rho = G_A M_{GT}/G_V M_F$  is very hard...(but  $^{19}\text{Ne}$  and  $^{37}\text{K}$ , at least, have potential)
- “Can  $V_{ud}$  from the pion be improved?”
  - ★ Not in the foreseeable future...

# “What is the inner radiative correction, $\Delta_R$ ? ”

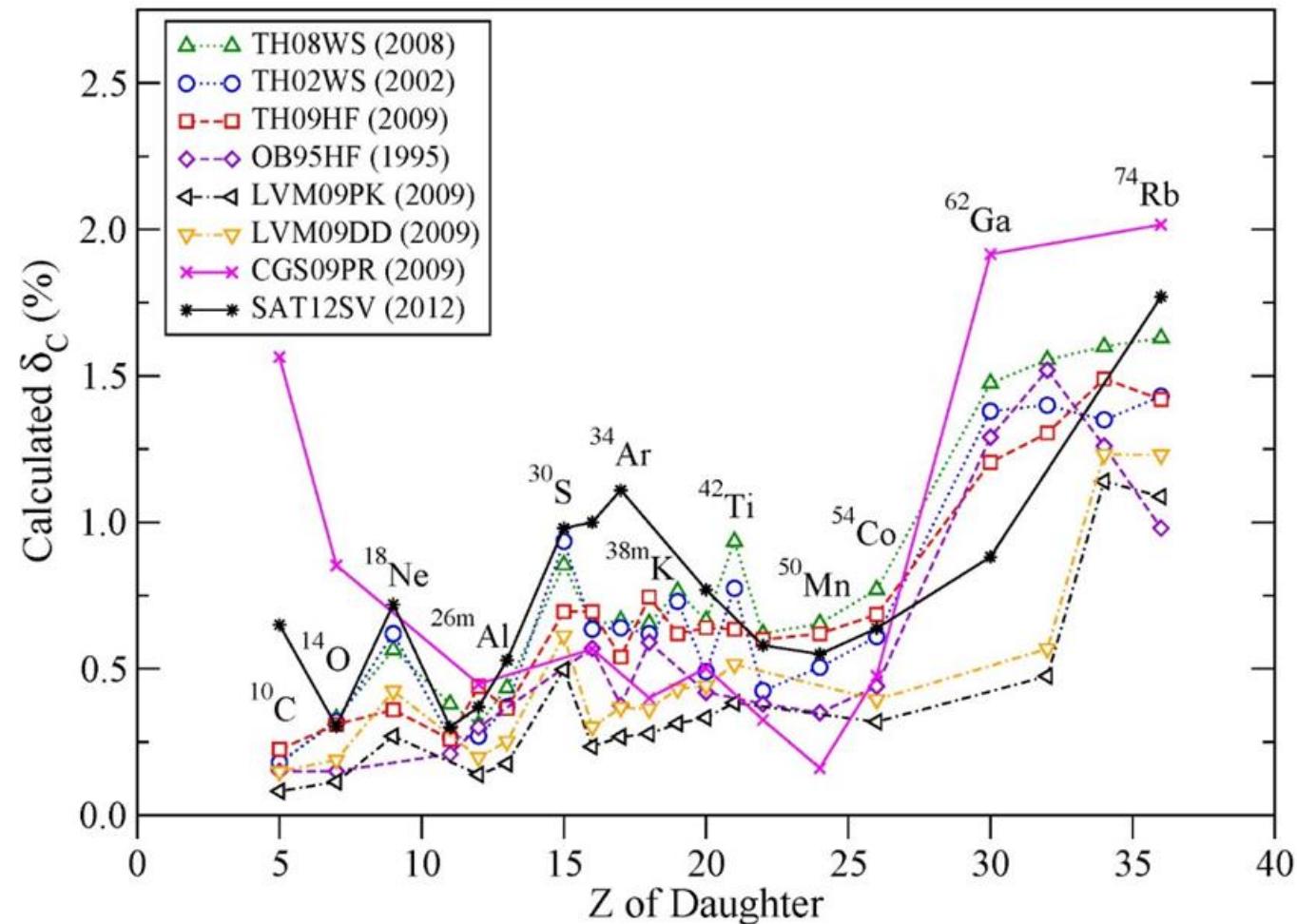
- Marciano & Sirlin made a huge stride in 2006:  $\Delta_R^V = 2.361(38)\%$ 
  - ★ 0.38% uncertainty in  $\Delta_R^V$  still dominated unitarity test
- Even more ground-breaking: Seng, Gorchtein, Patel and Ramsey-Musolf, PRL 121, 241804 (2018)
  - ★ Reduces the uncertainty by a nearly a factor of 2:  $\Delta_R^V = 2.467(22)\%$
- If correct and no double-counting, leads to  $\Delta_{\text{CKM}} = 16(4) \times 10^{-4}$ 
  - ★ Uncertainty in  $\Delta_R^V$  still dominates unitarity test, and now there is tension with unitarity!

Is there really a  $4\sigma$  effect?

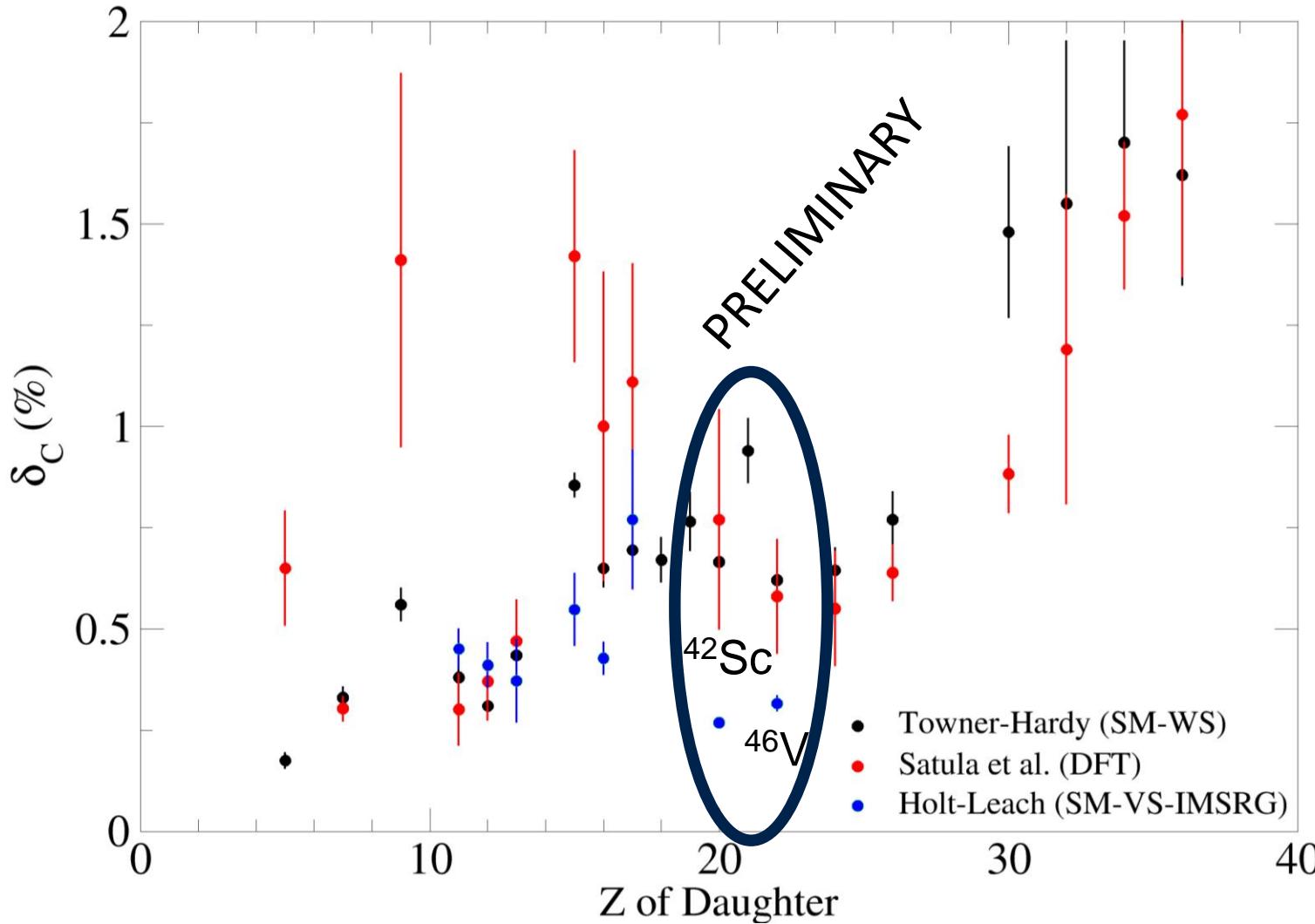
Exciting times (again)!

# **“How much can we believe the ISB corrections?”**

- Flurry of activity circa 2010 to provide complementary calculations
  - Shell Model
  - Relativistic Hartree-Fock
  - Random Phase Approximation
  - Energy Density Functional
- Only the Woods-Saxon shell model [TH] able to confirm CVC
- DFT indicates absolute scale of WS SM
- Newest kids on the block: Holt and Leach
- Reliable theoretical uncertainties?



# Nuclear Isospin Symmetry Breaking (ISB) Calculations



- Using  $\chi$ -EFT + VS-IMSRG now extends *ab initio* shell-model techniques up to the *pf*-shell and beyond
- Can calculate  $M_F$  directly to extract  $\delta_C$

$$\delta_C = 1 - \frac{|M_F|^2}{|M_F^0|^2}$$

$$= 1 - \frac{|M_F|^2}{2}$$

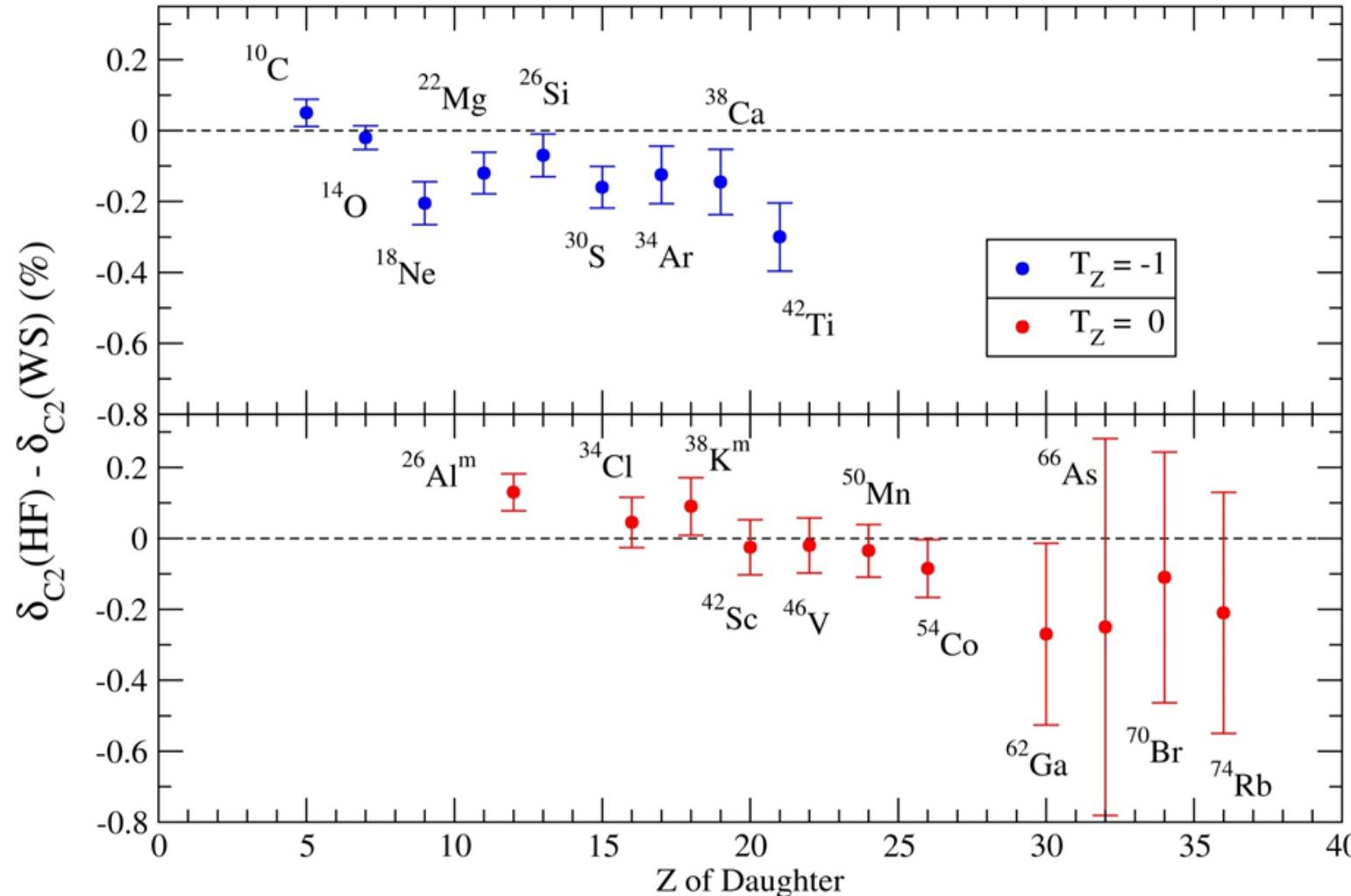
J.C. Hardy and I.S. Towner, Phys. Rev. C **91**, 025501 (2015)

W. Satula et al., Phys. Rev. C **86**, 054316 (2012)

J.D. Holt and K.G. Leach, in progress (2018)

# **“How much can we believe the ISB corrections?”**

- Hartree-Fock vs Woods-Saxon (just theory vs theory) radial overlap corrections: there is a **Z-dependence**



*“...it would be nice to have our theory colleagues dig into [this] and explain.”*

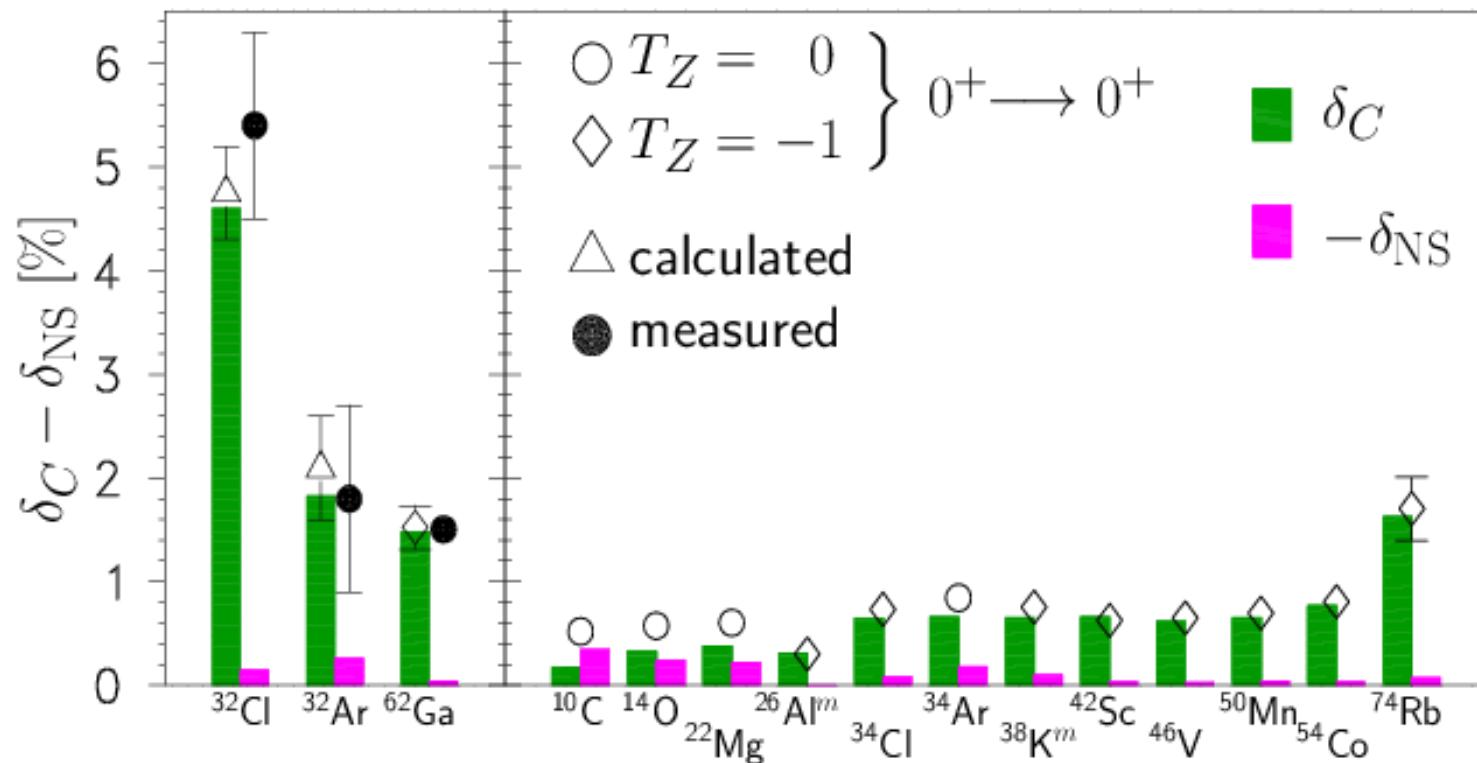
– C. Svennson

Courtesy of C. Svennson

# “Can we test calculations of ISB corrections?”

- Yes! We've been trying to for years, actually...

- 62Ga [Hyland et al, PRL **97** (2006)]: 1.42(11)% vs 1.38%
- 32Ar [Bhattacharya et al., PRC **77** (2008)]: 2.1(8)% → 1.8(8)% vs 2.0%
- 32Cl [Melconian et al., PRL **107** (2011)]: 5.3(9)% vs 4.6%

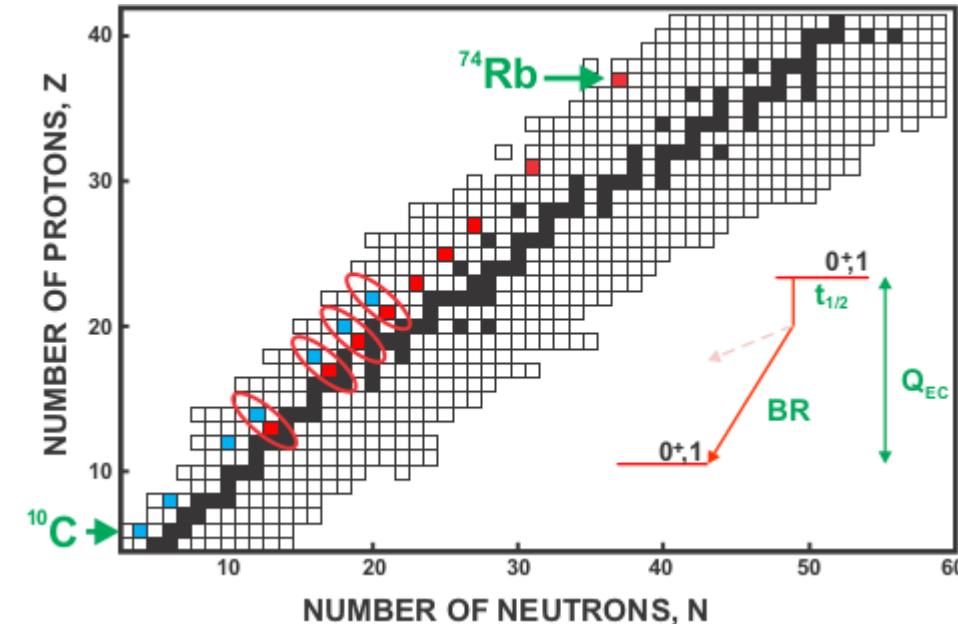
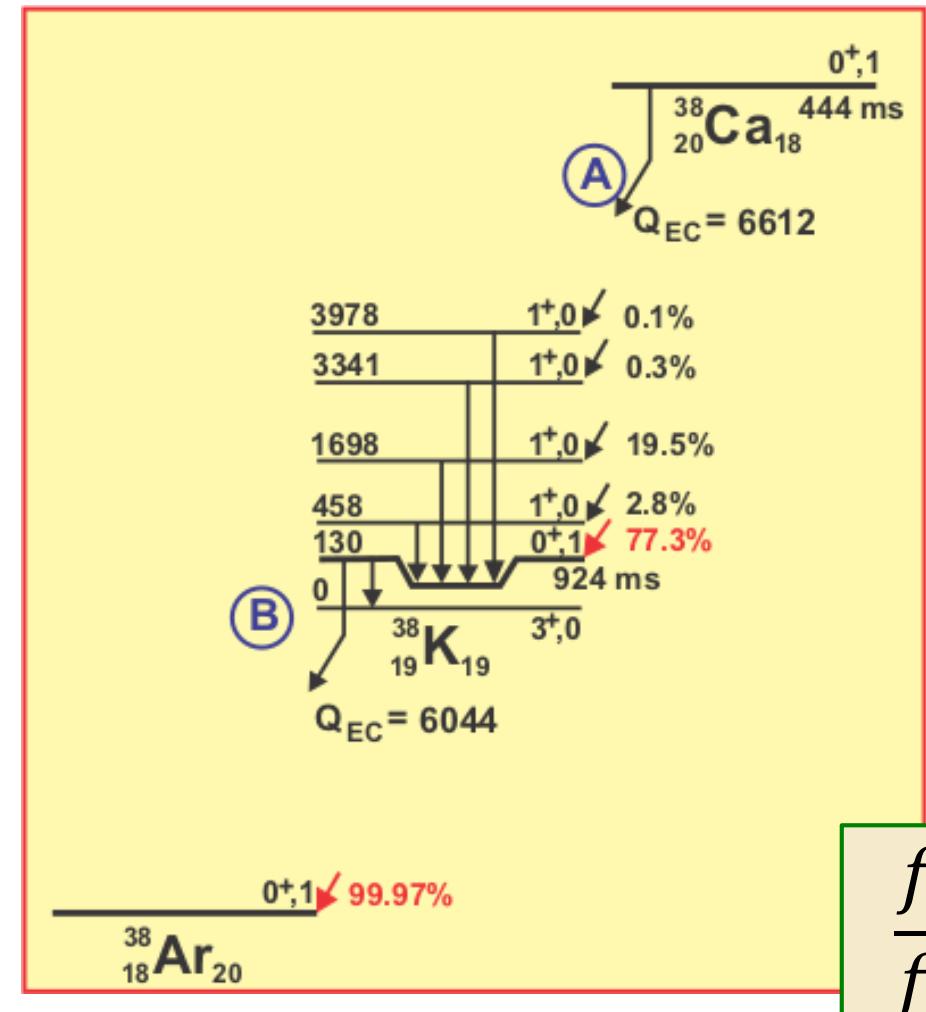


$$\mathcal{F}t = ft(1 + \delta'_R)[1 - (\delta_C - \delta_{NS})]$$

$$\Leftrightarrow \delta_C = 1 + \delta_{NS} - \frac{\mathcal{F}t^{\text{others}}}{ft^{\exp}(1 + \delta'_R)}$$

# WS vs HF: Mirror $0^+ \rightarrow 0^+$ transition pairs

- Ratio of  $0^+ \rightarrow 0^+$  pairs less sensitive to theoretical uncertainties:



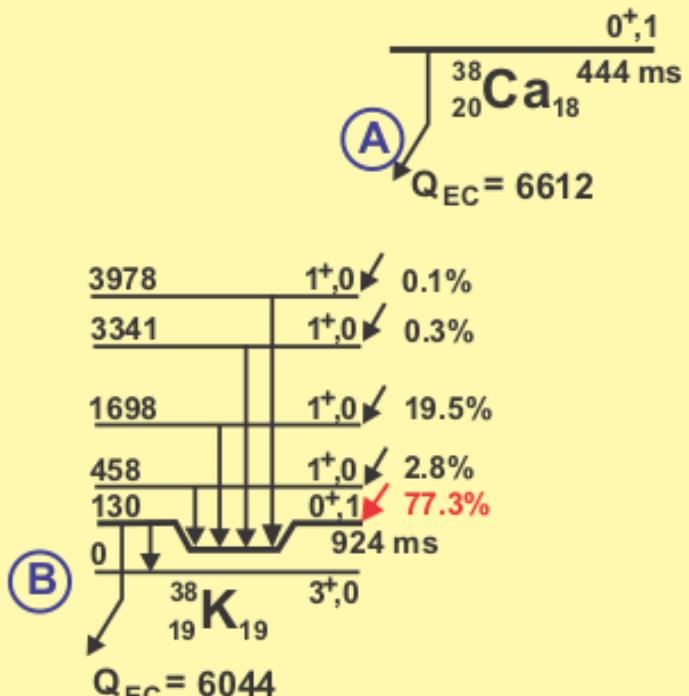
$$\frac{\mathcal{F}t_A}{\mathcal{F}t_B} = 1 = \frac{ft_A(1+\delta'^A_R)[1-(\delta^A_C - \delta^A_{NS})]}{ft_B(1+\delta'^B_R)[1-(\delta^B_C - \delta^B_{NS})]}$$

$$\Rightarrow \frac{ft_A}{ft_B} = \frac{(1+\delta'^B_R)[1-(\delta^B_C - \delta^B_{NS})]}{(1+\delta'^A_R)[1-(\delta^A_C - \delta^A_{NS})]}$$

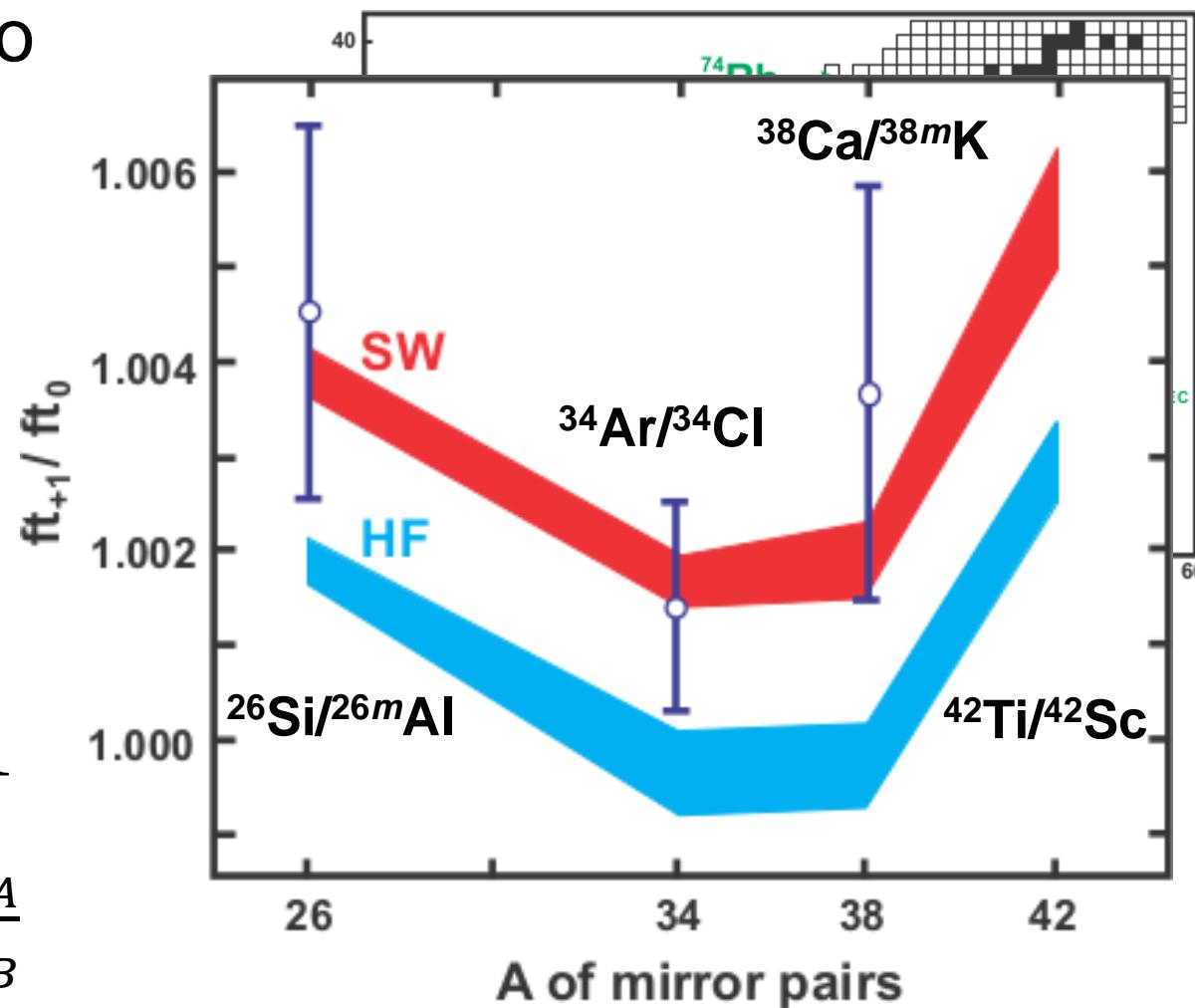
$$\frac{ft_A}{ft_B} \approx 1 + (\delta'^B_R - \delta'^A_R) + (\delta^B_{NS} - \delta^A_{NS}) + (\delta^B_C - \delta^A_C)$$

# WS vs HF: Mirror $0^+ \rightarrow 0^+$ transition pairs

- Ratio of  $0^+ \rightarrow 0^+$  pairs less sensitive to theoretical uncertainties:



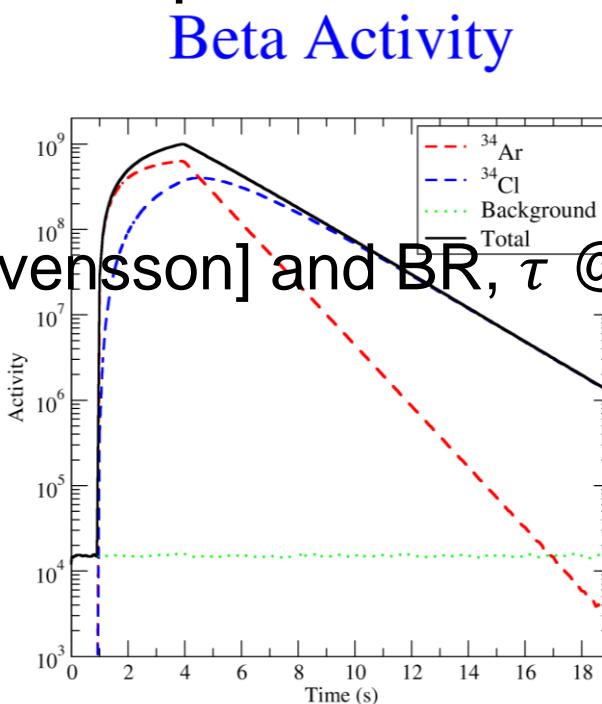
$$\frac{ft_A}{ft_B} \approx 1 + (\delta'^B_R - \delta'^A_R) + (\delta^B_{NS} - \delta^A_{NS}) + (\delta^B_C - \delta^A_C)$$



# “Can we improve existing cases with $\Delta\mathcal{F}t \lesssim 0.25\%$ ?”

- There is already so many precision experiments, significant improvements is not practical in most cases
- Cases being investigated:

- ★  $^{22}\text{Mg}$  – BR @ GRIFFIN/TRIUMF [Svensson] and  $Q_{EC}$  @ TITAN [Leach]
- ★  $^{26}\text{Si}^+$  – BR @ TAMU [Hardy]
- ★  $^{30}\text{S}$  – BR @ GANIL/LISE3 [Blank]
- ★  $^{34}\text{Ar}^+$  – BR,  $\tau$  @ TAMU and @ GRIFFIN
- ★  $^{42}\text{Ti}^+$  – BR @ TAMU
- ★  $^{62}\text{Ga}$  – check  $0^+$  exc state in  $^{62}\text{Zn}$  @ GRIFFIN

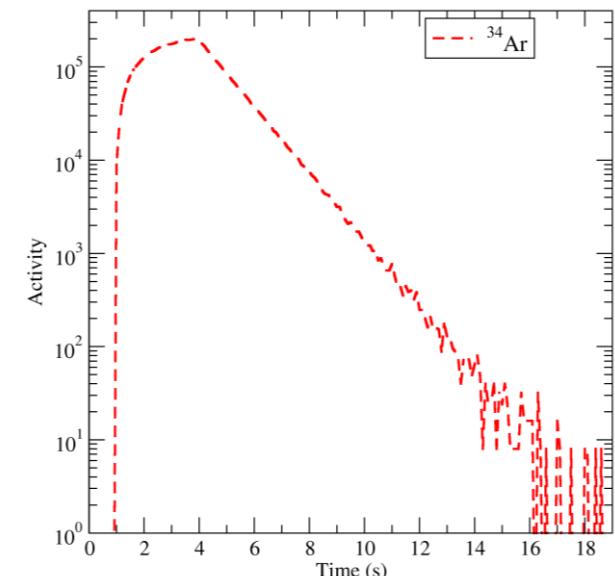


Gate on  $\gamma$ -ray transitions  
in the  $^{34}\text{Cl}$  daughter

$\beta$ -counting suffers from a large covariance between the  $^{34}\text{Ar}$  and  $^{34}\text{Cl}$  lifetimes

ISOLDE [Blank]

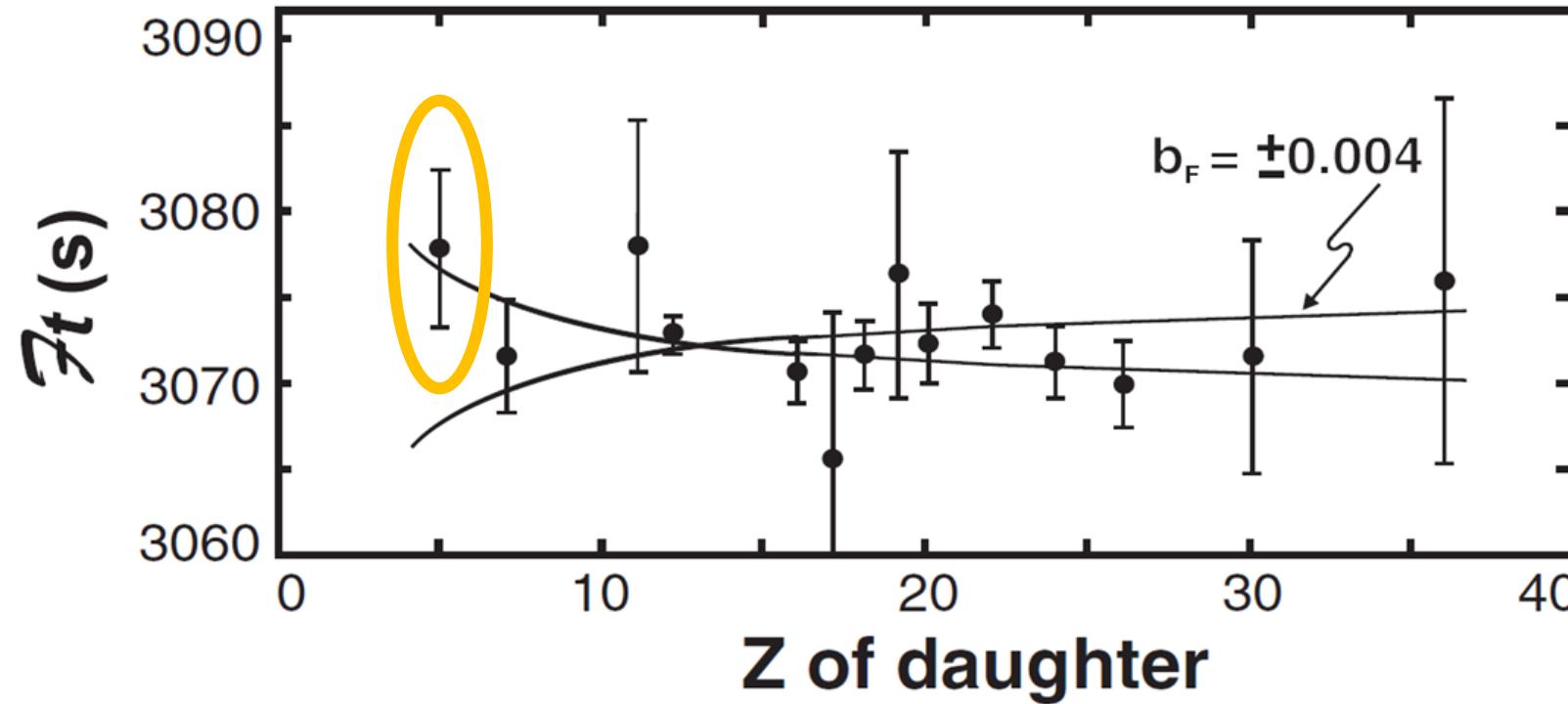
Gamma Activity



$^+$ mirror  $0^+ \rightarrow 0^+$

# Perhaps the most interesting (even if not for $V_{ud}$ ...)

- $^{10}\text{C}$ : lowest  $Z$  of precisely measured superallowed, and so will impact the search for scalar currents



- Eronen & Hardy @ TAMU: BR analysis in progress
- Blank @ ISOLDE: BR analysis in progress
- Svensson @ TRIUMF:  $\tau$  recently improved

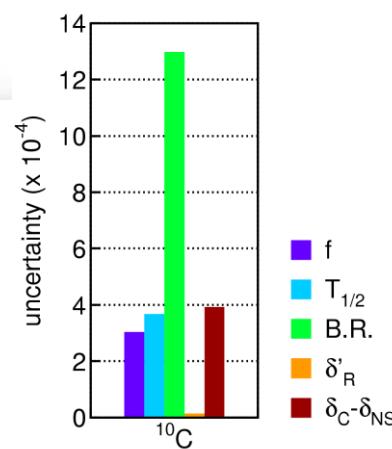
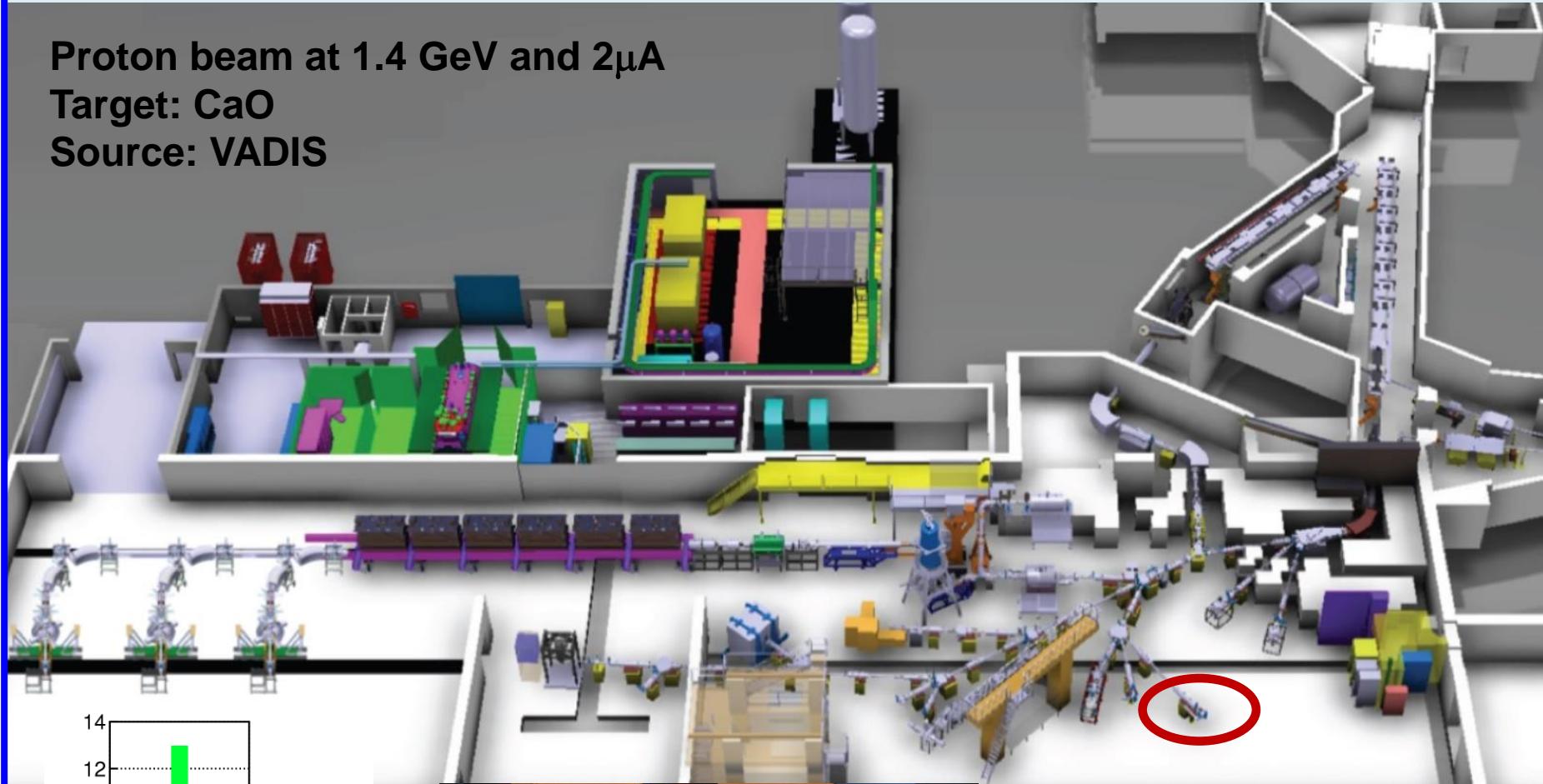
● ● ●  **$^{10}\text{C}$  measurement at ISOLDE**

Courtesy of B. Blank

Proton beam at 1.4 GeV and  $2\mu\text{A}$

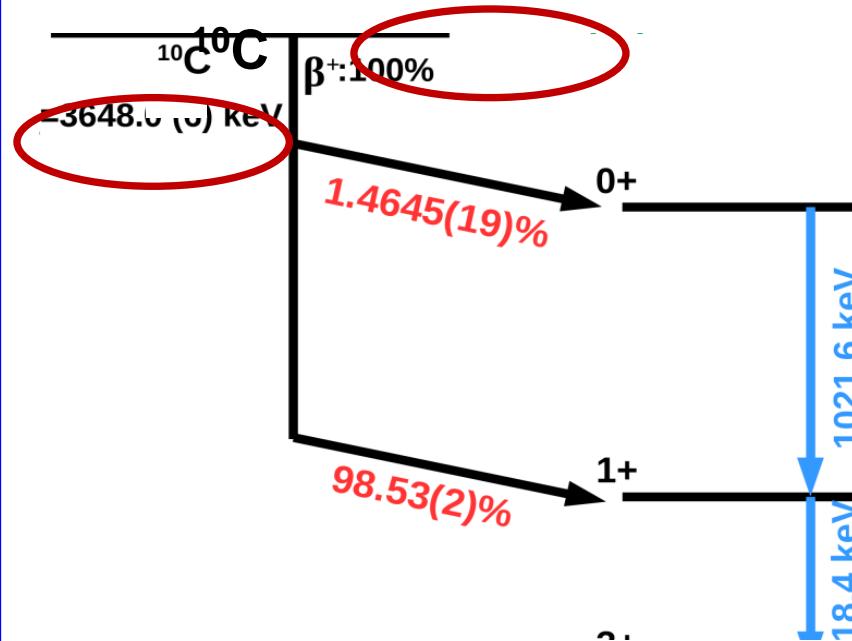
Target: CaO

Source: VADIS

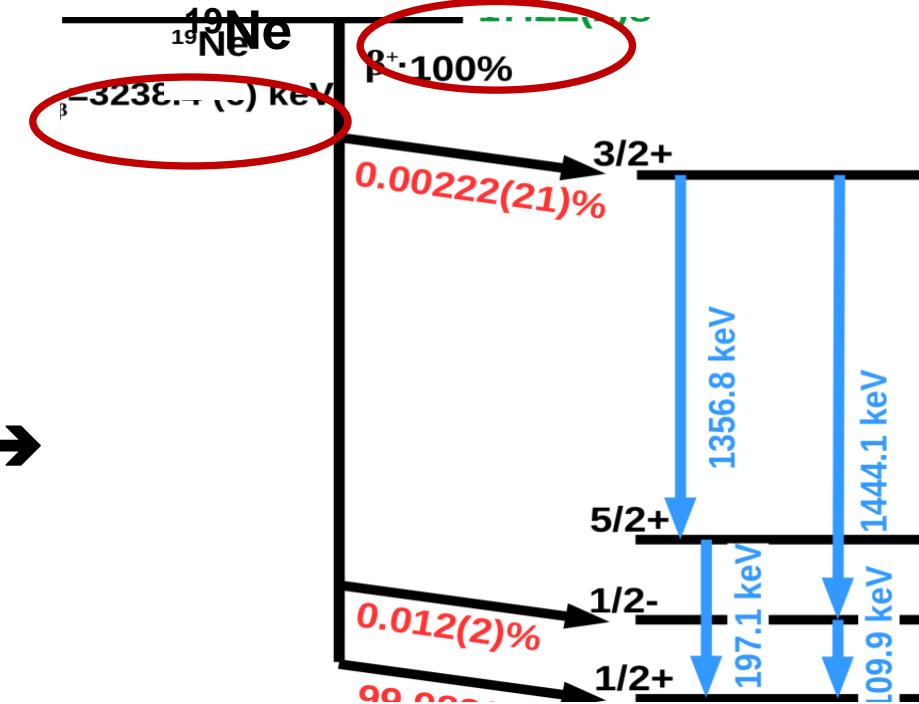


• • •  **$^{10}\text{C}/^{19}\text{Ne}$  decay scheme**

Courtesy of B. Blank



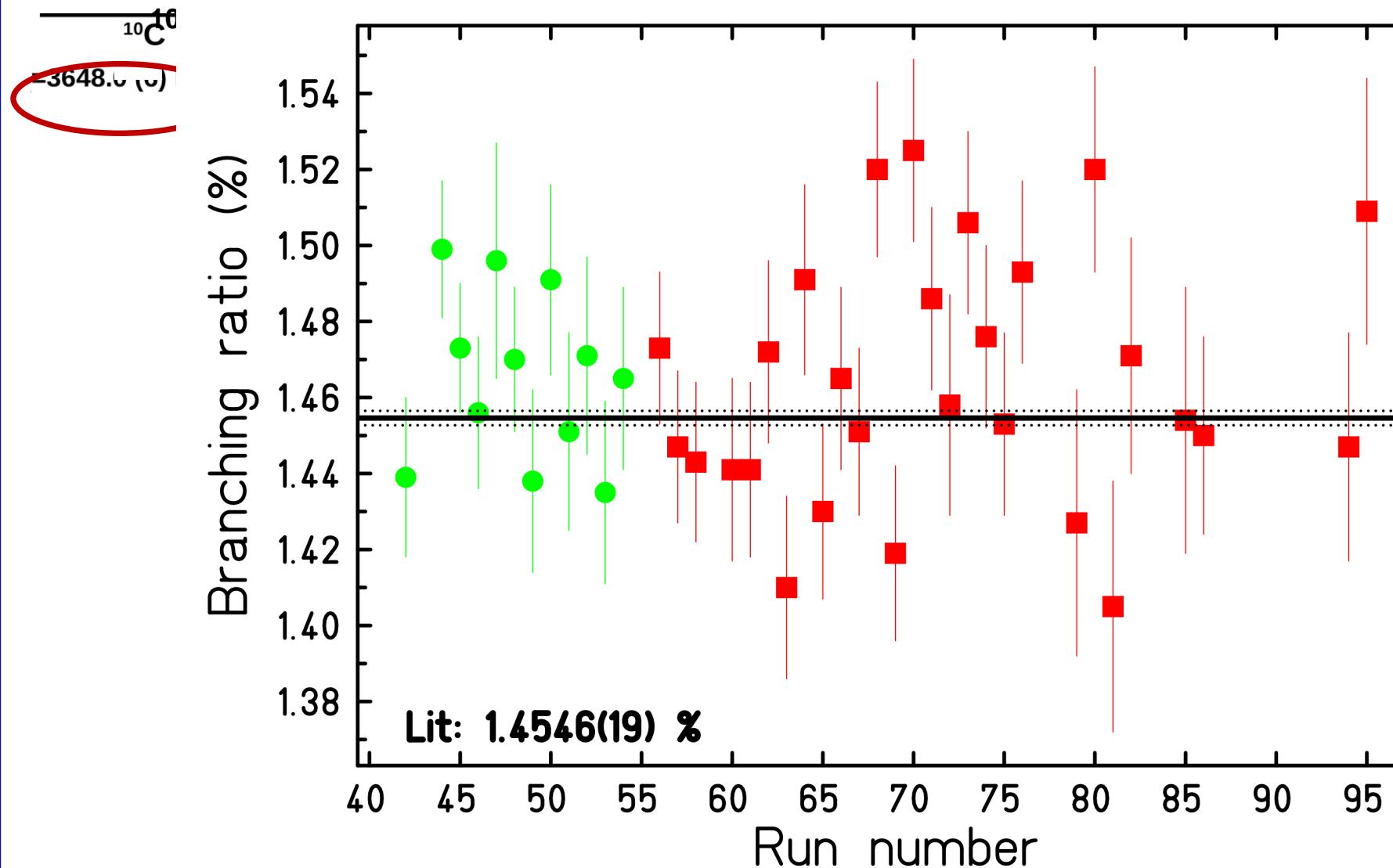
← to determine the BR



to evaluate pile-up →

● ● ●  **$^{10}\text{C}/^{19}\text{Ne}$  decay scheme**

Courtesy of B. Blank



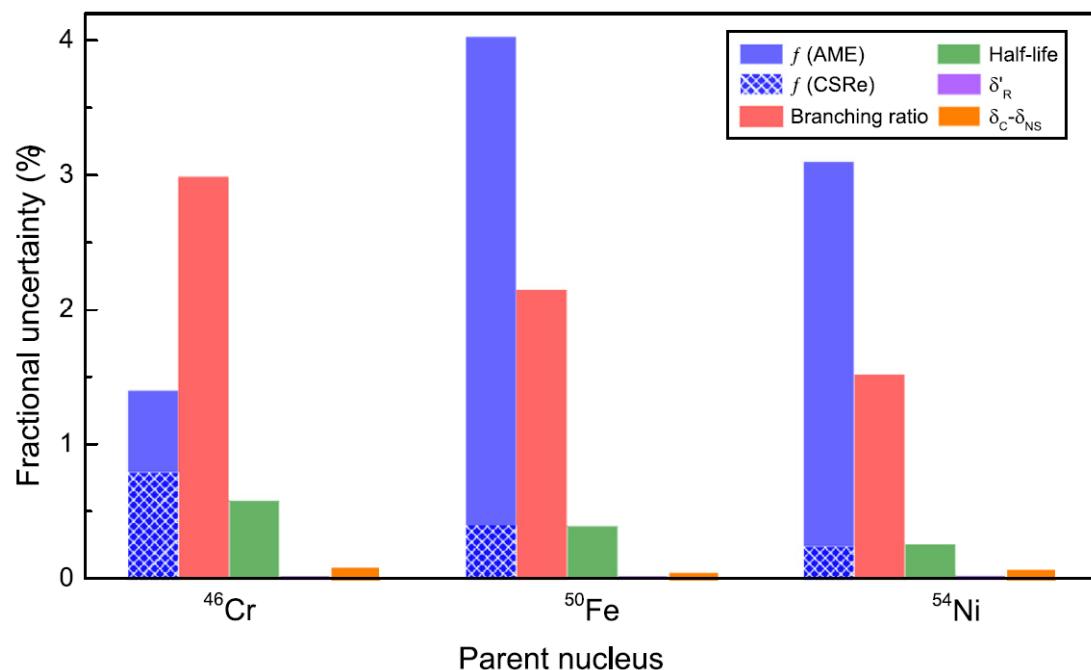
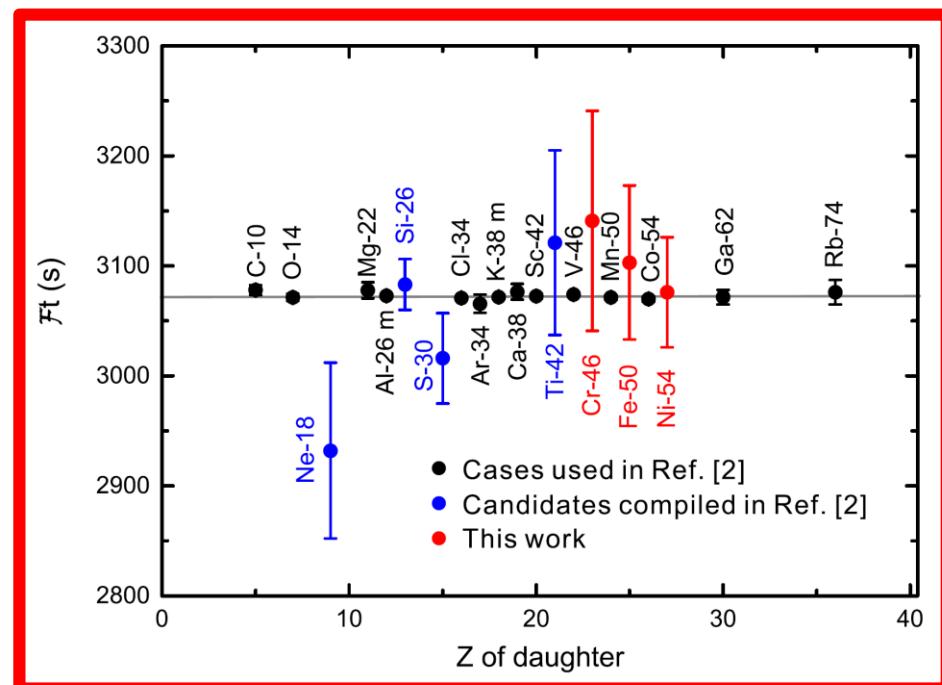
...to be fully analysed

global correction, not yet run by run

# “Can we add new $0^+ \rightarrow 0^+$ transitions with $\Delta\mathcal{F}t \lesssim 0.25\%$ ? ”

- Yes, maybe? Cases I'm aware of:

- $^{46}\text{Cr}$  – BR,  $\tau$ ,  $Q_{EC}$  @ EURISOL-DF (Eronen)
- $^{50}\text{Fe}$  – BR,  $\tau$ ,  $Q_{EC}$  @ EURISOL-DF (Eronen) and TITAN (Leach)
- $^{54}\text{Ni}$  – BR,  $\tau$ ,  $Q_{EC}$  @ EURISOL-DF (Eronen)



Courtesy of T. Eronen, who points out “*These will never compete in precision with lower-A cases. Important for (isospin symmetry breaking) corrections*”

# “Can we add new $0^+ \rightarrow 0^+$ transitions with $\Delta\mathcal{F}t \lesssim 0.25\%$ ? ”

- Yes, maybe? Cases I'm aware of:

- $\text{\color{red}{\tiny \star}}$   $^{46}\text{Cr}$  – BR,  $\tau$ ,  $Q_{EC}$  @ EURISOL-DF (Eronen)
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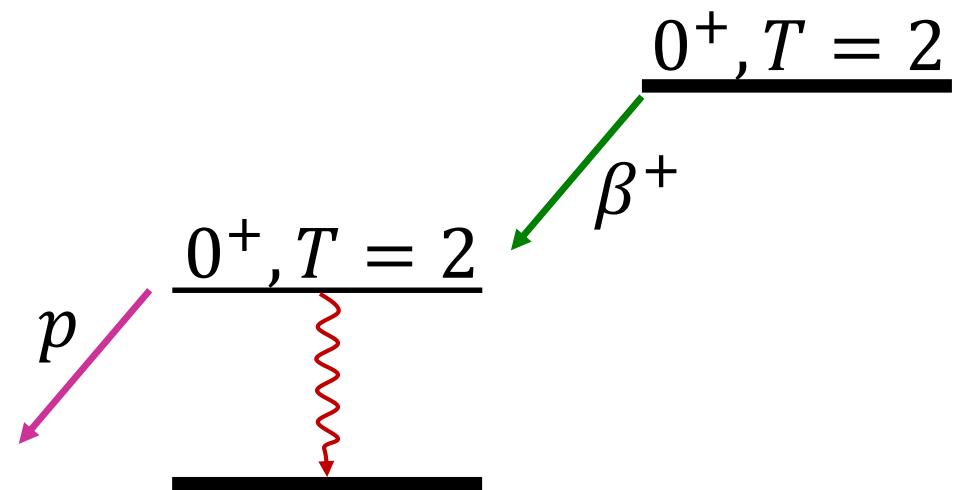
- Heavier cases:

- $\text{\color{red}{\tiny \star}}$   $^{58}\text{Zn}$  – BR,  $\tau$  @ BigRIPS/RIKEN (Blank)
- $\text{\color{red}{\tiny \star}}$   $^{66}\text{As}$  –  $Q_{EC}$  @ TITAN/TRIUMF (Leach)
- $\text{\color{red}{\tiny \star}}$   $^{70}\text{Br}$  –  $Q_{EC}$  @ TITAN/TRIUMF (Leach)
- $\text{\color{red}{\tiny \star}}$   $^{74}\text{Rb}$  –  $Q_{EC}$  @ TITAN/TRIUMF (Leach)

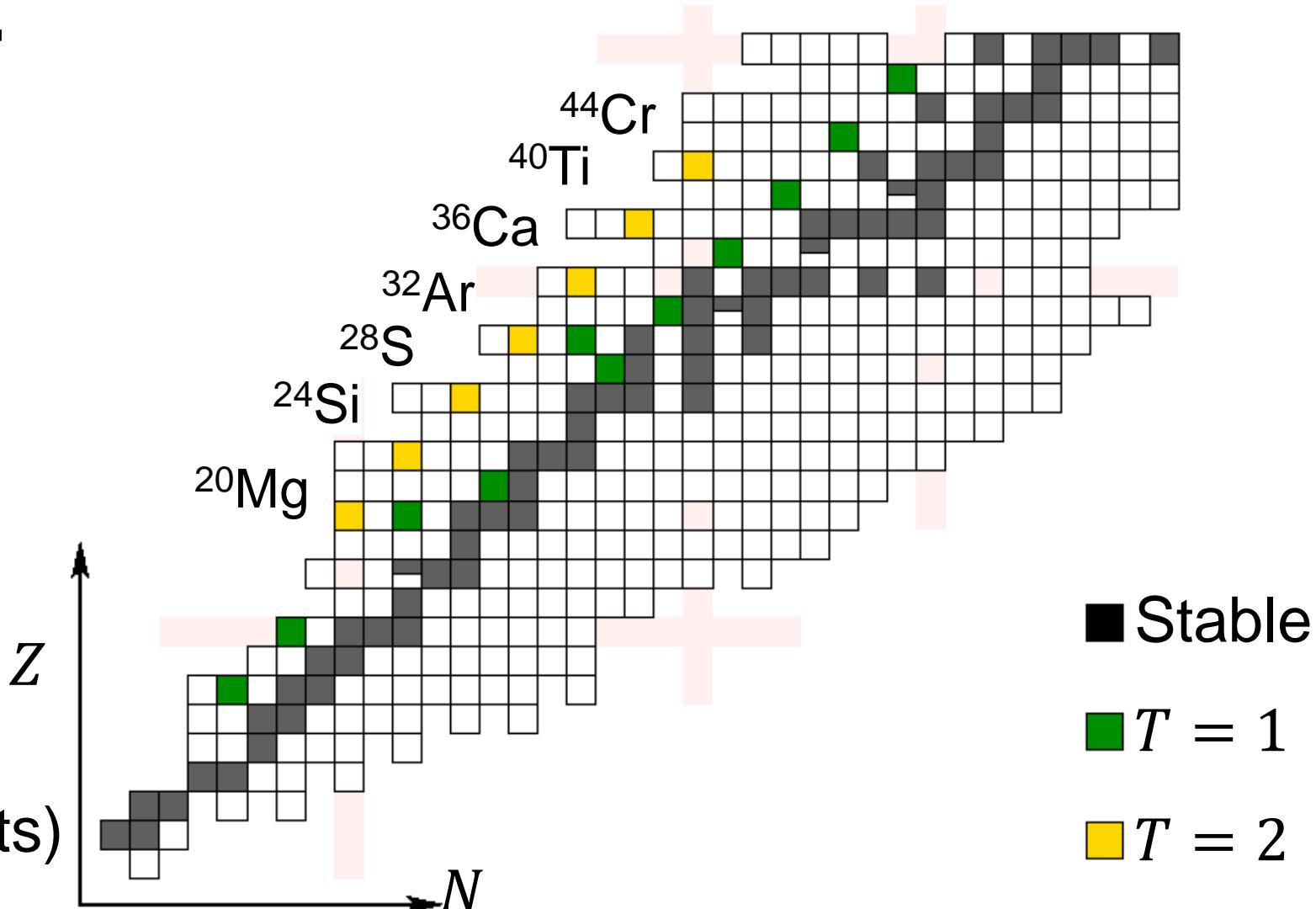
- The problem: shell model is not as well characterized above  $A = 56$

- $\text{\color{red}{\tiny \star}}$  “*Who's going to give beamtime and funding for boring spectroscopy?*” – JCH

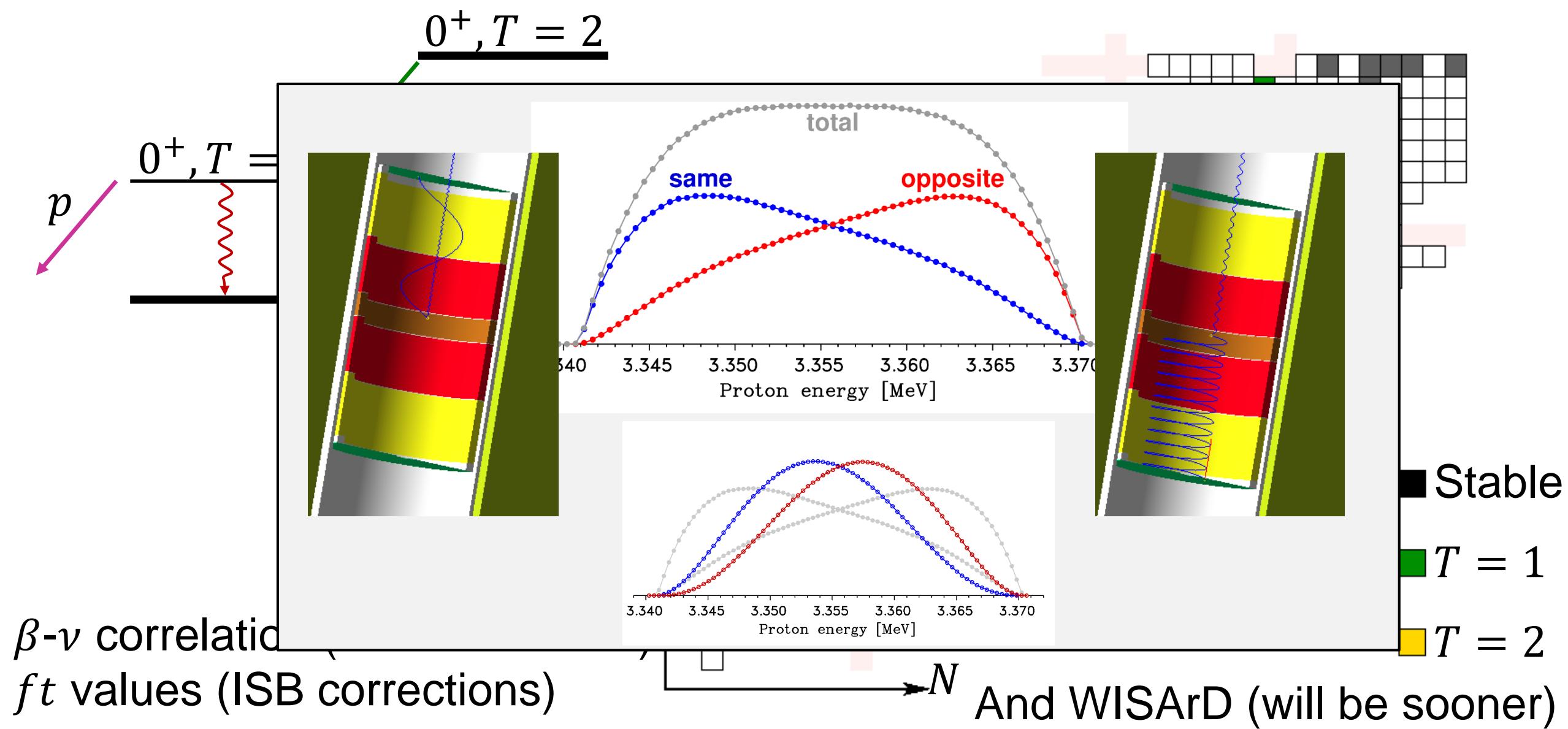
# More cases that may help with ISB corrections



$\beta$ - $\nu$  correlation (scalar currents)  
 $ft$  values (ISB corrections)

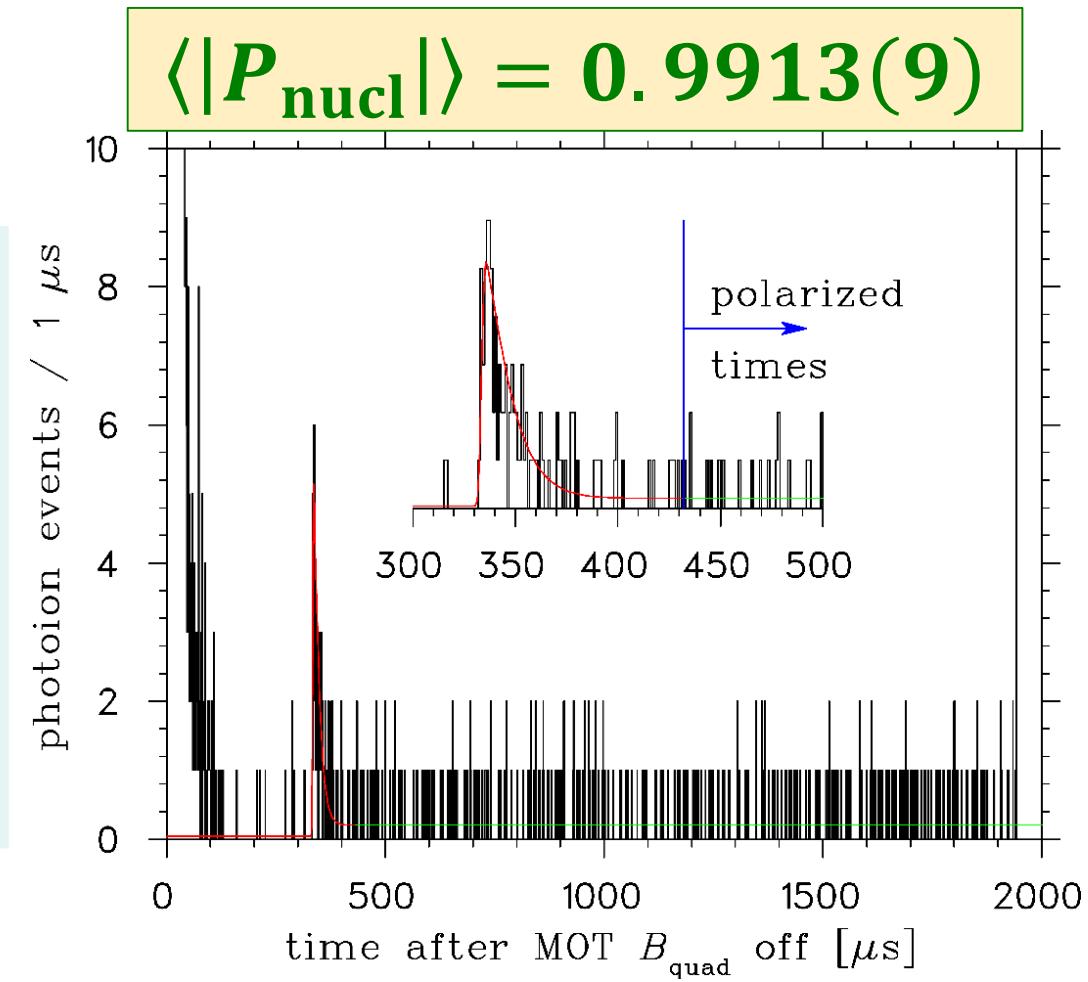
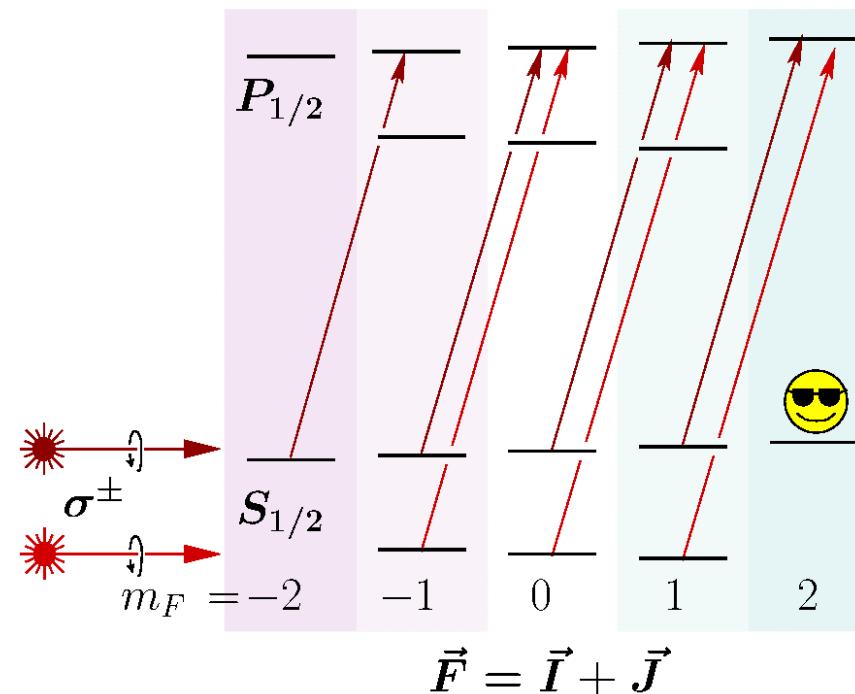


# More cases that may help with ISB corrections



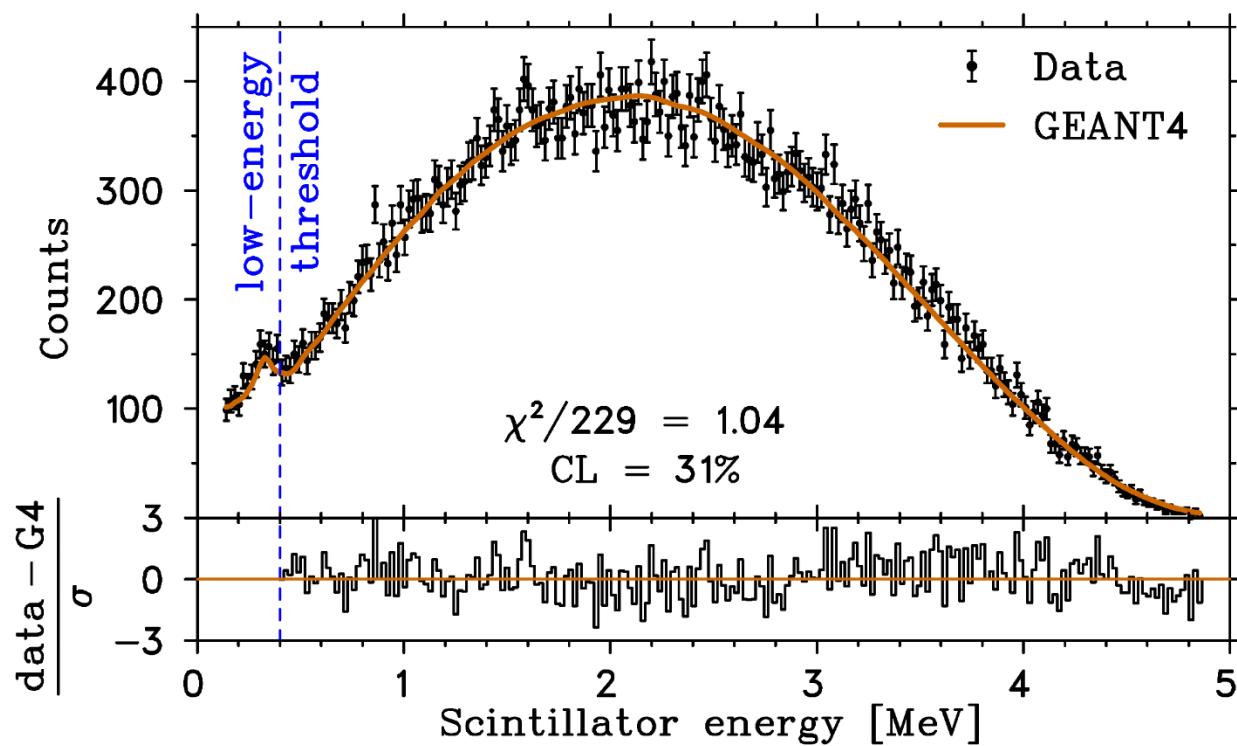
# **“How much progress can be made with $T = 1/2$ transitions?”**

- Albert covered the neutron and  $^{19}\text{Ne}$
- $^{37}\text{K}$  @ TRINAT/TRIUMF [Melconian & Behr]
  - High nuclear polarization: 99.13(9)%

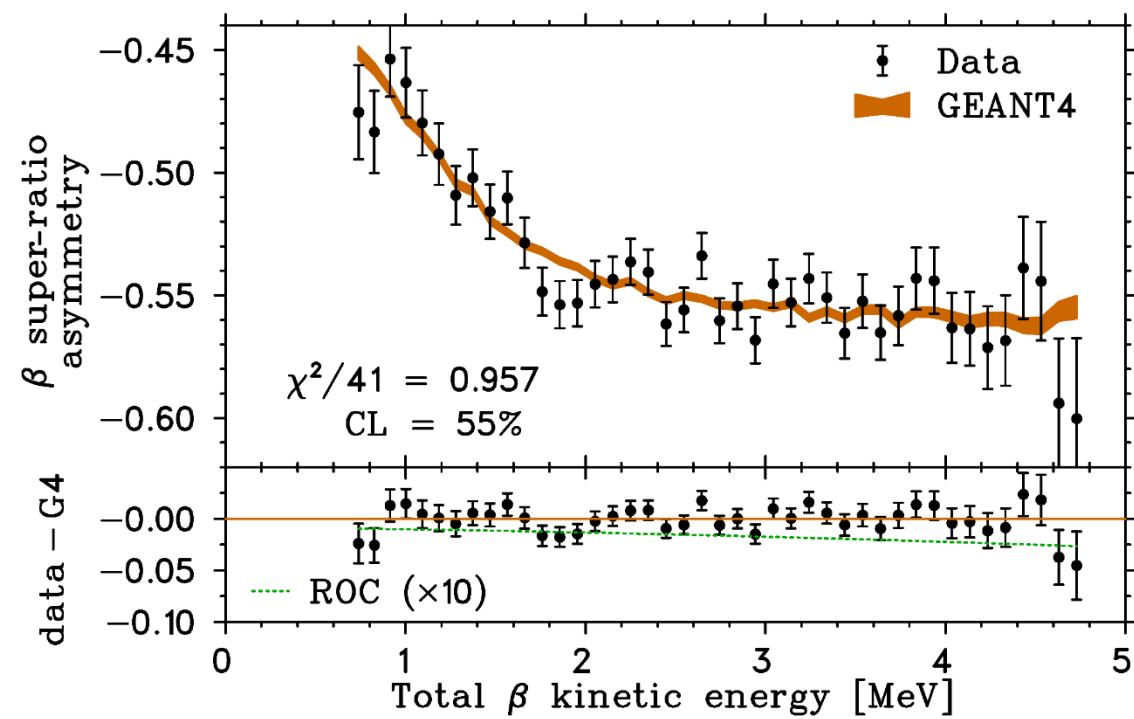


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Fenker PRL 120 062502 (2018)  
 $A_\beta^{\text{meas}} = -0.5707(19)$   
vs  
 $A_\beta^{\text{SM}} = -0.5706(7)$



# “How much progress can be made with $T = 1/2$ transitions?”

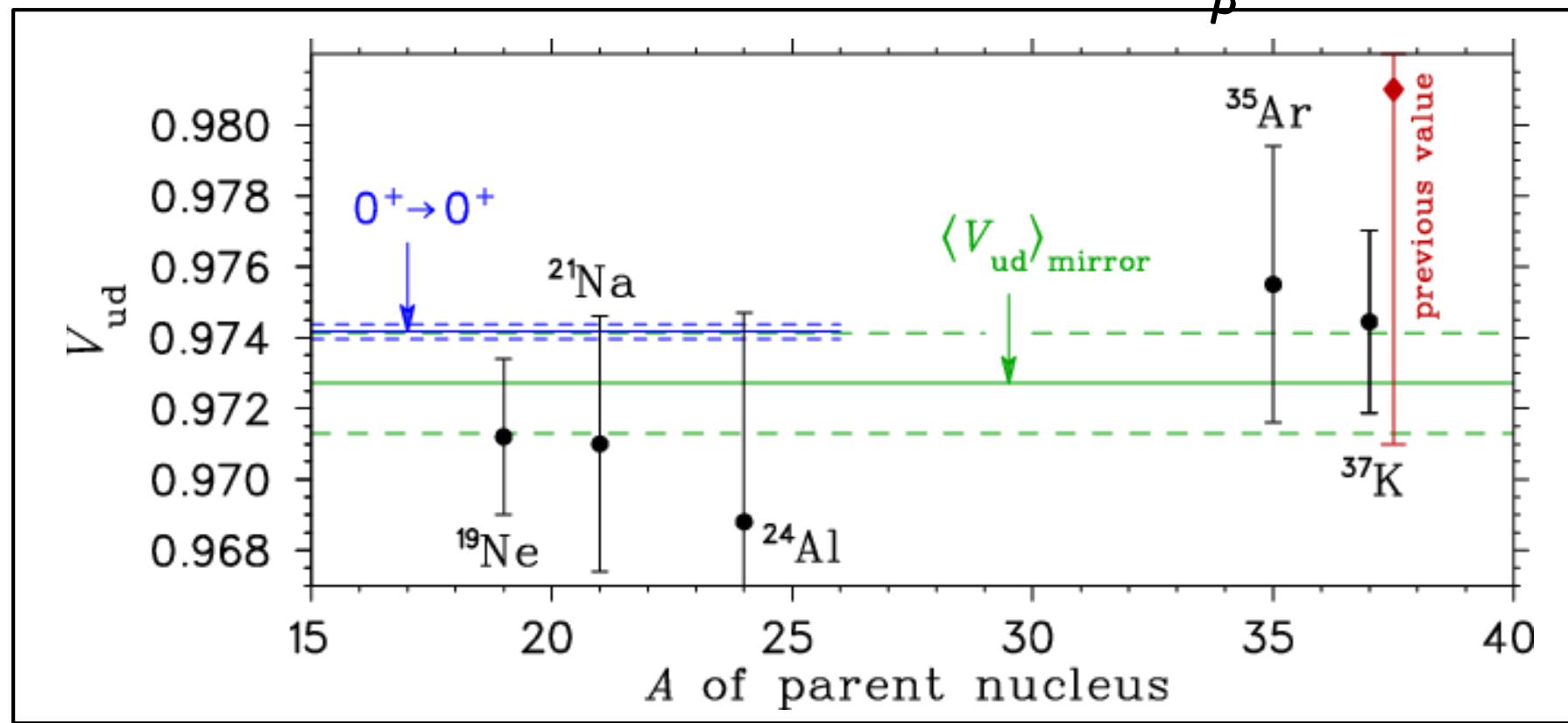
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Fenker PRL 120 062502 (2018)

$$A_\beta^{\text{meas}} = -0.5707(19)$$

vs

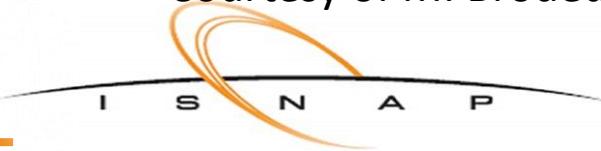
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# **“How much progress can be made with $T = 1/2$ transitions?”**

---

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- St. Benedict @ TwinSol –  $a_{\beta\nu}$  using a Paul trap



# Half-lives measured @ ND

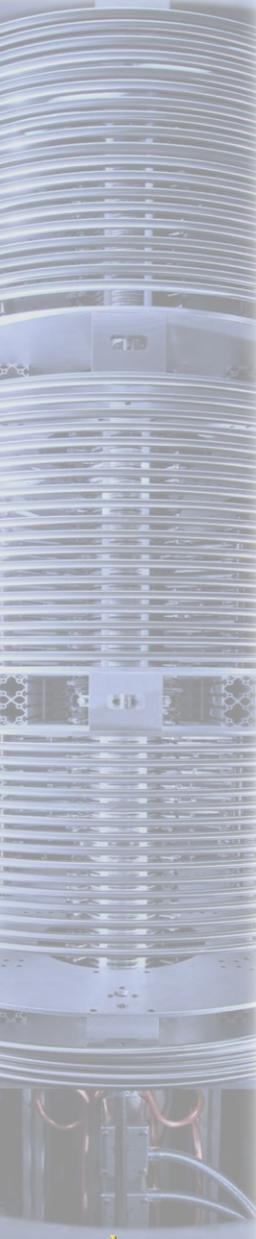
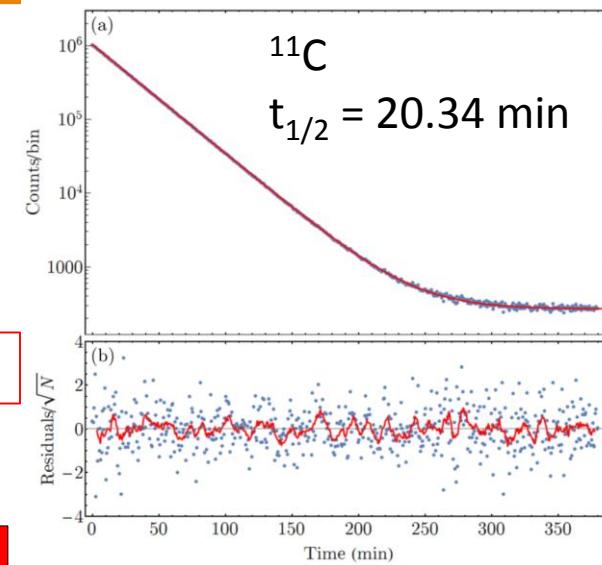
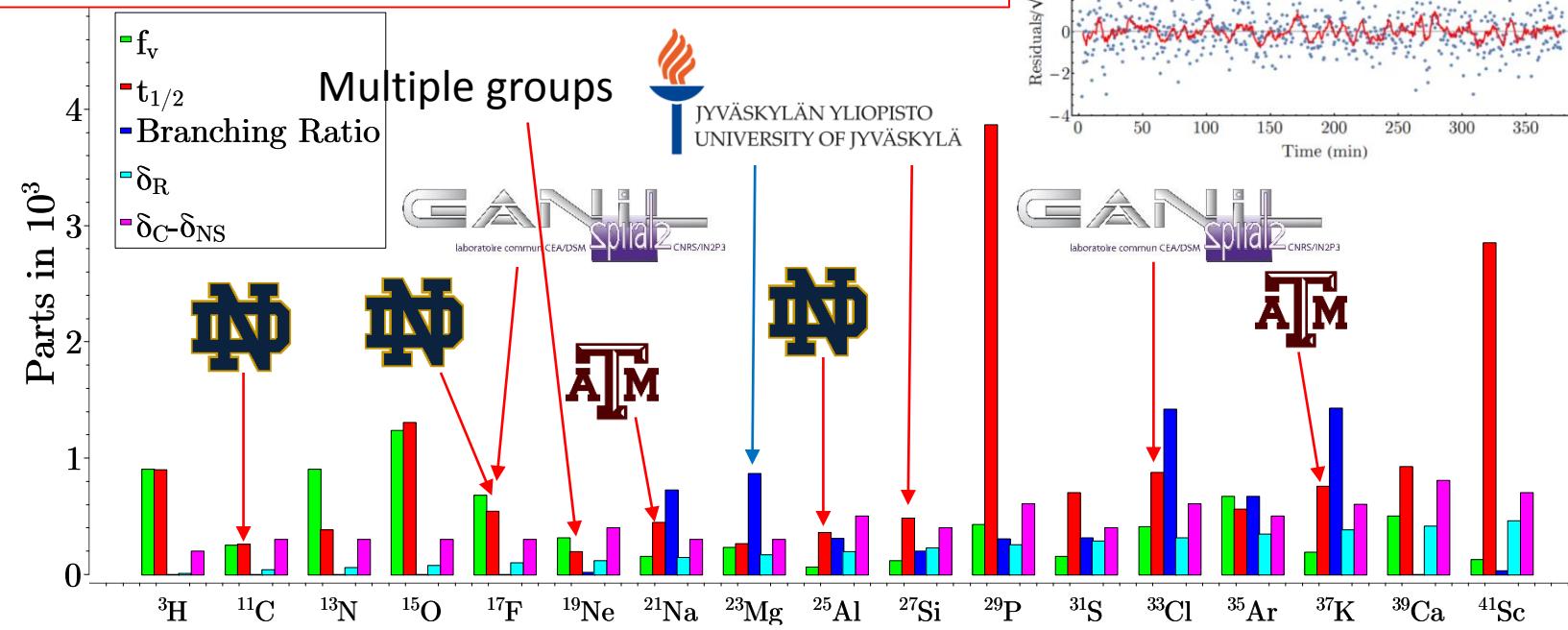
$^{17}\text{F}$ : M. Brodeur *et al.*, PRC **93**, 025503 (2016)

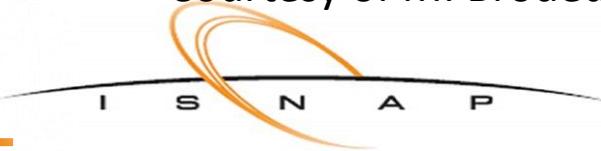
$^{25}\text{Al}$ : J. Long *et al.*, PRC **96**, 015502 (2017)

$^{11}\text{C}$ : A. Valverde *et al.*, PRC **97**, 035503 (2018)

$^{20}\text{F}$ : D. Burdette *et al.*, PRC **99**, 015501 (2019)

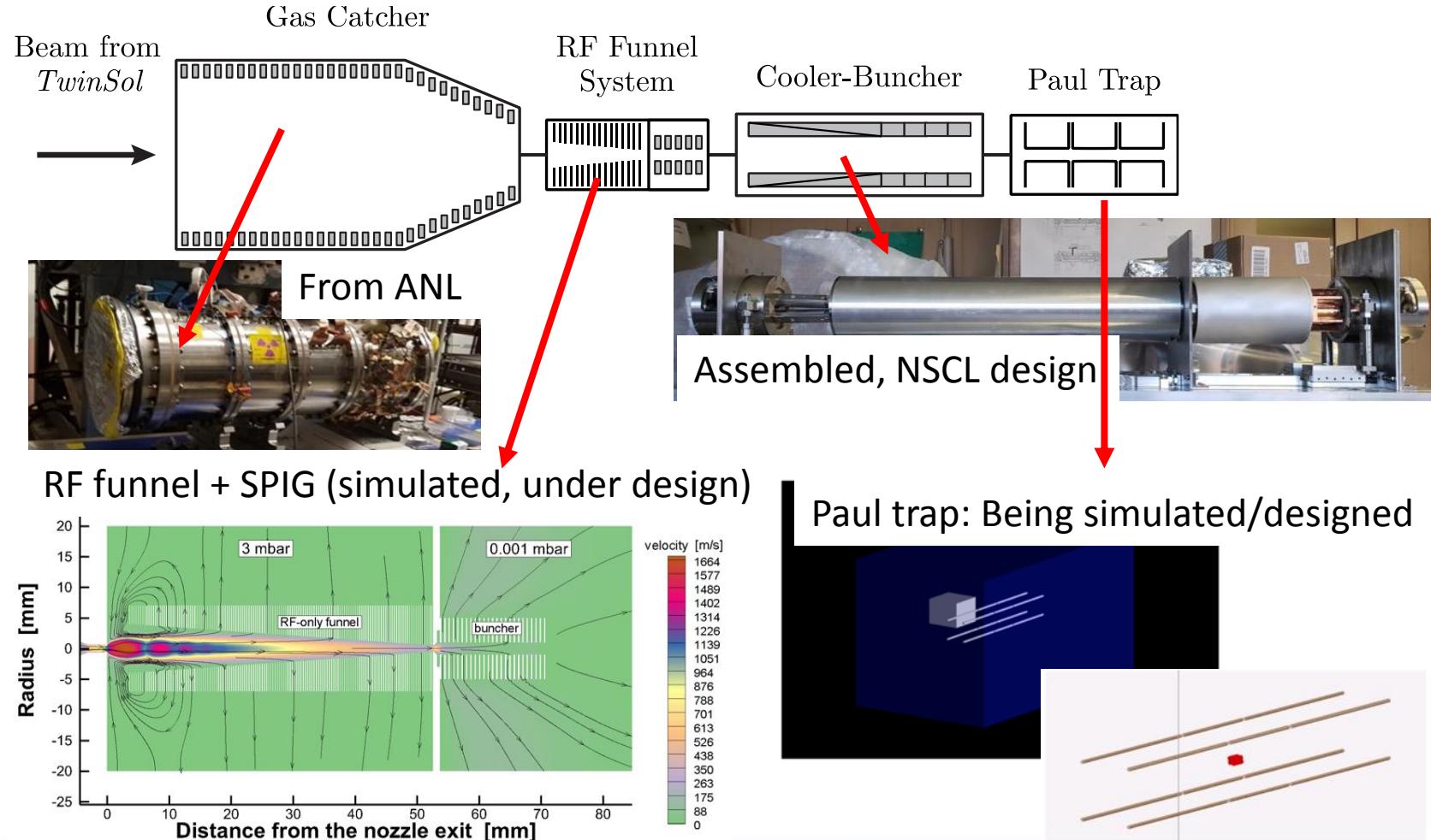
Current relative uncertainties of mirror ft-values quantities





# St. Benedict status

## Superallowed Transitions Beta Neutrino Decay Ion Coincidence Trap



ECT\* workshop, April 9<sup>th</sup>, 2019

# **“How much progress can be made with $T = 1/2$ transitions?”**

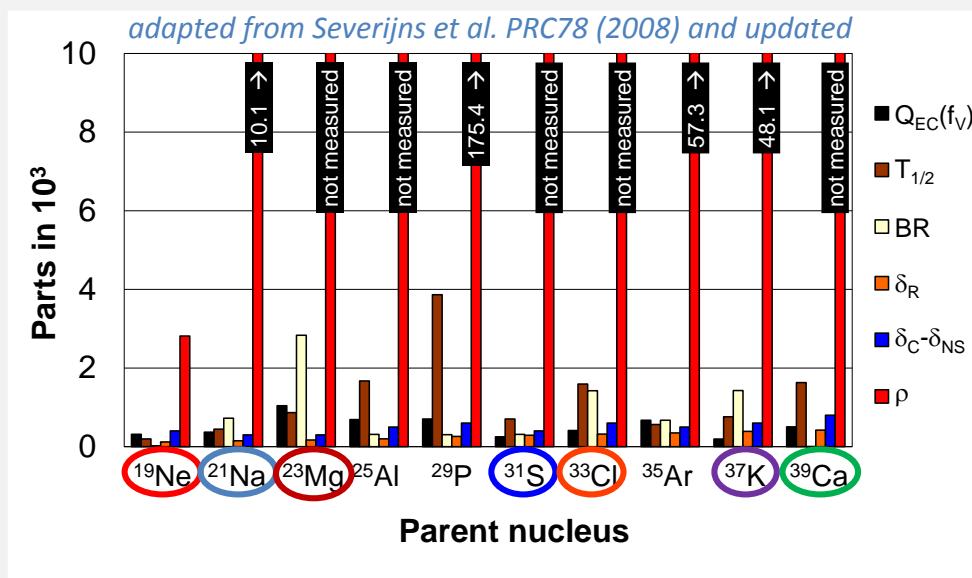
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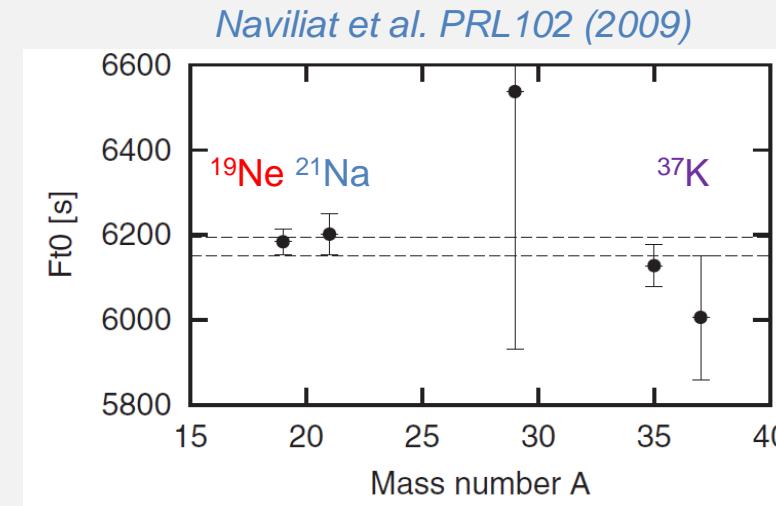
# CVC, $V_{ud}$ & CKM: *ft* values measurements

Subject discussed in details in the next talk (Bertram Blank)

- Nuclear mirrors



- $^{19}\text{Ne}$   $T_{1/2}$ : Broussard et al. PRL112 (2014)
- $^{21}\text{Na}$  M: Mukherjee et al. EPJA35 (2008)  
 $T_{1/2}$ : Grinyer et al. PRC91 (2015)
- $^{23}\text{Mg}$  M: Saastamoinen et al. PRC80 (2009)  
 $T_{1/2}$ , BR: Magron et al. EPJA53 (2017)
- $^{31}\text{S}$  M: Kankainen et al. PRC82 (2010)  
 $T_{1/2}$ : Bacquias et al. EPJA48 (2012)
- $^{33}\text{Cl}$   $T_{1/2}$ : Grinyer et al. PRC92 (2015)
- $^{37}\text{K}$   $T_{1/2}$ : Shidling et al. PRC90 (2014)
- $^{39}\text{Ca}$   $T_{1/2}$ : Blank et al. EPJA44 (2010)



The scientific community involved in this field... BUT

$$V_{ud} (2009) = 0.9719 (17)$$



$$V_{ud} (2017) = 0.9721 (17) !!$$

For  $V_{ud}$  determination,  $\rho$  improvements are necessary ...

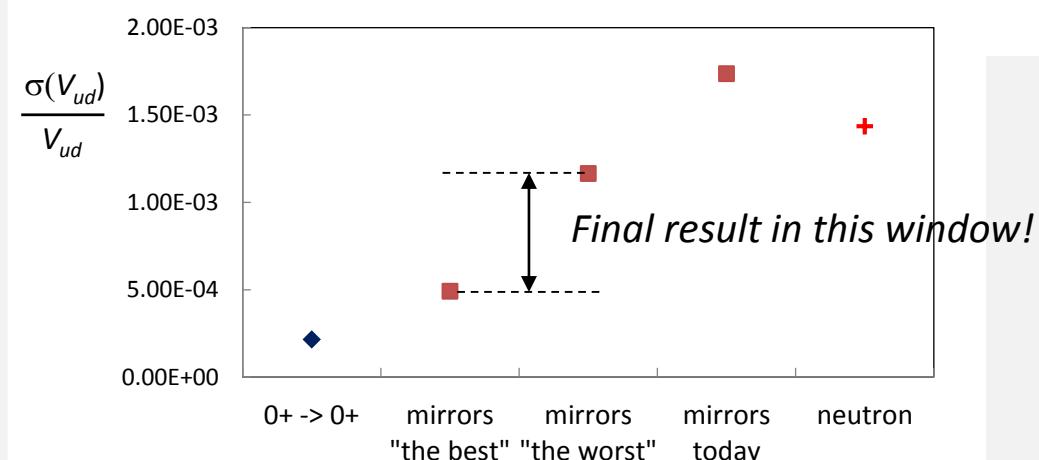
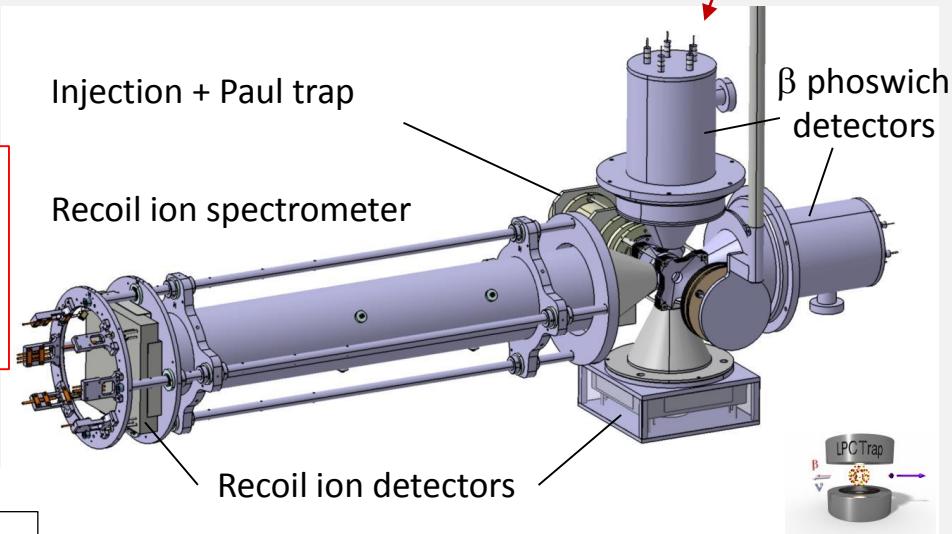
# CVC, $V_{ud}$ & CKM: *ft* values measurements

*Subject discussed in details in the next talk (Bertram Blank)*

- Nuclear mirrors

Perspectives @ GANIL: Measurement of  $a$  in several mirror decays using **LPCTrap2**

Ion	$T_{1/2}$ (s)	Expected rate (pps)	
$^{21}\text{Na}$	22.49	6.5E+08	SPIRAL production $> 10^7$ pps
$^{23}\text{Mg}$	11.32	2.1E+08	
$^{33}\text{Cl}$	2.51	3.4E+07	
$^{37}\text{K}$	1.22	7.4E+08	



*In any case, a significant improvement on  $V_{ud}$  is reachable*

@ LIRAT and DESIR

# **“How much progress can be made with $T = 1/2$ transitions?”**

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Progress is slow, and it will be hard to compete directly with the precision of  $0^+ \rightarrow 0^+$  decays

More cases for models to provide ISB corrections,  
perhaps make CVC test more stringent

# Summary and outlook

---

- After decades of work, it is getting hard to improve the CKM unitarity test
- Greatest progress to be made is through theoretical improvements
  - $\Delta_R^V$  of course
  - Improved modelling of heavy nuclei
  - New approaches to complement WS shell model
- Experimentally:
  - Mirror  $0^+ \rightarrow 0^+$  promise a sensitive test of theoretical corrections
  - $^{10}\text{C}$  is hard, but better BR will improve already impressive search for scalar currents
  - The neutron is slowly approaching the precision of  $0^+ \rightarrow 0^+$ , and ultimately does not have  $\delta_C - \delta_{NS}$  corrections

# But probably the best way to conclude:

## SUMMARY AND OUTLOOK

1. Analysis of superallowed  $0^+ \rightarrow 0^+$  nuclear  $\beta$  decay confirms CVC to  $\pm 0.011\%$  and thus yields  $V_{ud} = 0.97420(21)$ .
2. The three other experimental methods for determining  $V_{ud}$  yield consistent results; the neutron-decay result is only a factor of 4 less precise and agrees completely.
3. The current value for  $V_{ud}$ , when combined with the PDG values for  $V_{us}$  and  $V_{ub}$ , satisfies CKM unitarity to  $\pm 0.05\%$ .

4. The largest contribution to  $V_{ud}$  uncertainty is from the inner radiative correction,  $\Delta_R$ . Very little reduction in  $V_{ud}$  uncertainty is possible without improved calculation of  $\Delta_R$ .
5. Transition-dependent corrections have been tested by requiring consistency among the 14 known transitions (CVC), and agreement with mirror-transition pairs.
6. Improved and new correction terms are appearing. They will need to be tested for compatibility with CVC.

Thanks to many who gave me slides and comments, particularly:

- John Hardy
- Carl Svensson
- Bertram Blank
- Tommi Eronen
- Kyle Leach
- Etienne Lienard
- Maxime Brodeur



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