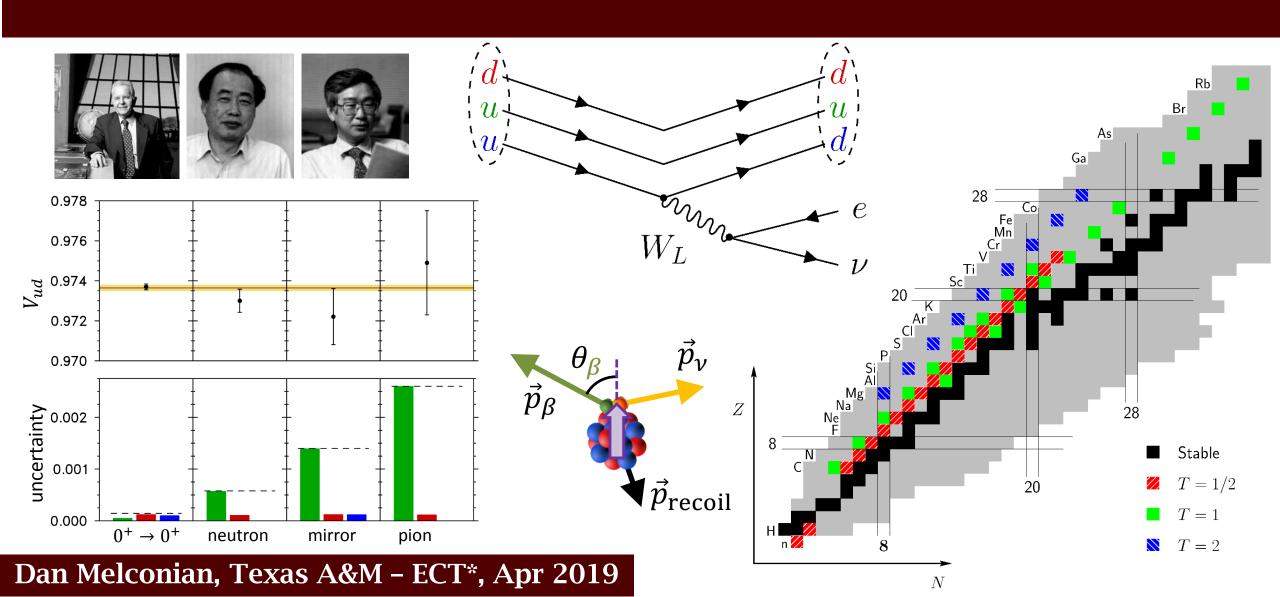
Outlook for the determination of V_{ud}



Outline

- Introduction
 - Stuff you probably already know
- Present status
 - * $0^+ \rightarrow 0^+$ superallowed decays
 - * T = 1/2 transitions
 - Pion decays
 - ***** CKM unitarity
- Looking forward
 - Inner radiative corrections
 - ***** ISB calculations
 - * Experimental efforts on existing and new nuclei
- Summary and outlook

Everyone here knows this, but...

Cabibbo



mass eigenstates ≠ weak eigenstates

$$V_{ud} = G_V/G_F$$

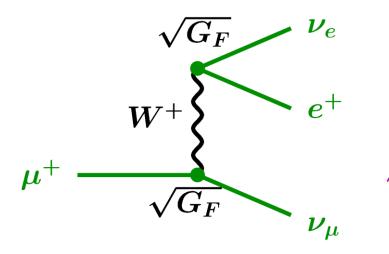
Kobayashi

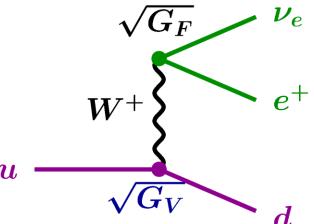


Maskawa



generalized
Cabibbo's theory
to three
generations





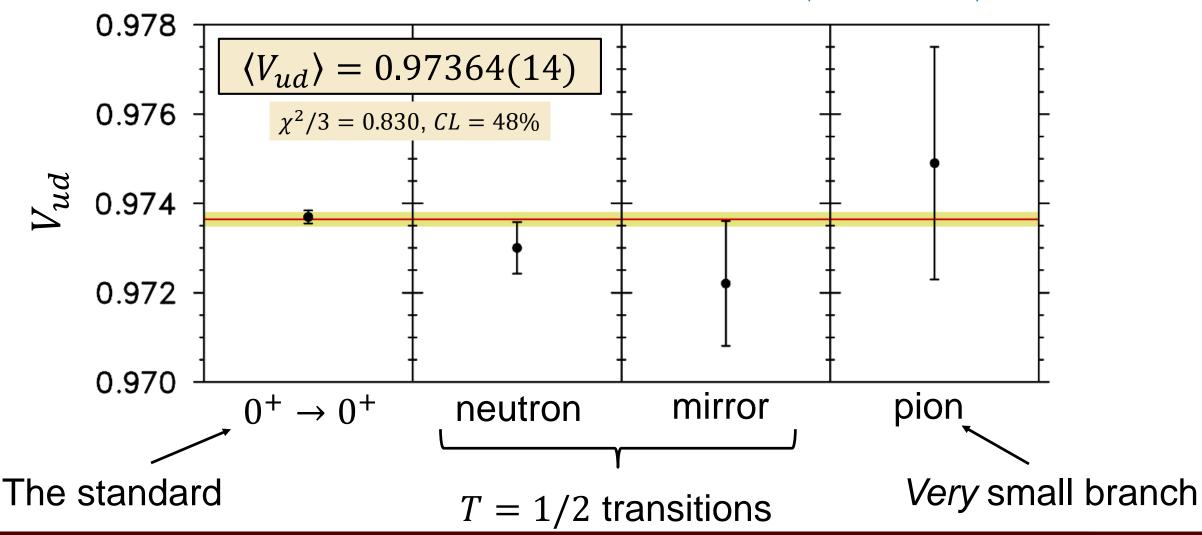
weak mass eigenstates $\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ h \end{pmatrix}$

Unitarity condition: $V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1$

Cabibbo-Kobayashi-Maskawa (CKM) matrix

Cutting to the chase

- * The current status of V_{ud} (using Seng's Δ_R^V and latest PERKEO III result):
 - Seng, Gorchtein, Patel and Ramsey-Musolf, PRL 121, 241084 (2018)
 - Markisch, et al., arXiv:1812.04666 (submitted to PRL)



$0^+ \rightarrow 0^+$ Transitions

These purely Fermi transitions are theoretically well-understood within the Standard Model

(phase) (partial) half life) =
$$ft \approx \frac{K/G_F^2}{V_{ud}^2(M_F^2 + M_{GT}^2)}$$

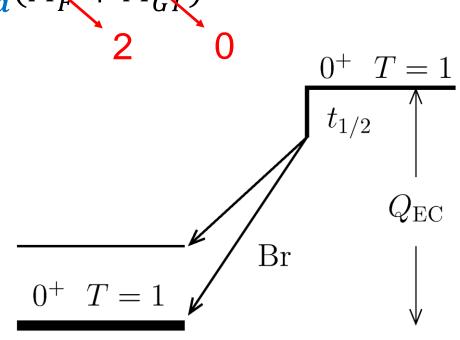
where

$$f(Z, Q_{EC}) = \int F(Z, E)S(E) pE(E - E_0)^2 dE$$

$$\sim Q_{EC}^5$$

is the phase space factor and

$$t(t_{1/2}, Br) = \frac{t_{1/2}}{Br}(1 + P_{EC})$$
 is the partial half life

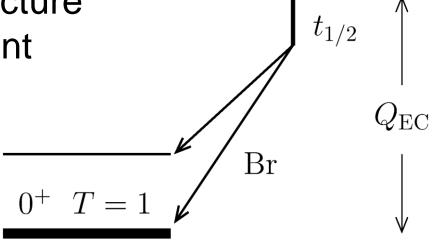


As we know, it's not quite that simple

One must include small radiative and isospin-symmetry breaking corrections

- δ_R' : radiative correction, depends on Z and Q_{EC}
- * δ_C : isospin-symmetry-breaking correction
- δ_{NS} : radiative correction
- \bullet Δ_R^V : radiative correction common to any extraction of V_{ud}

nuclear structure dependent

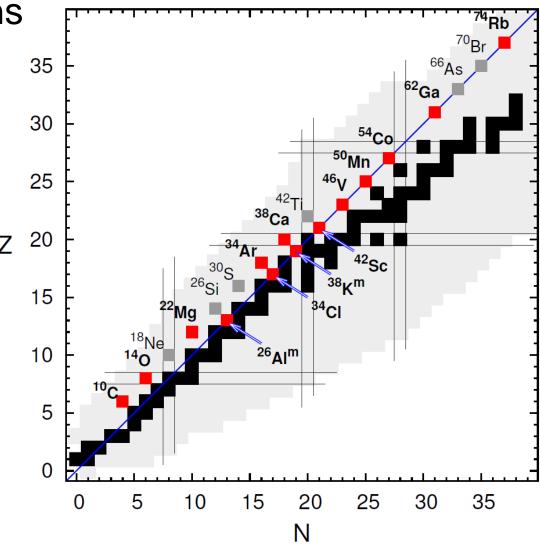


 $\sim 2.4\%$

Theoretical uncertainties: 0.05 + 0.10%

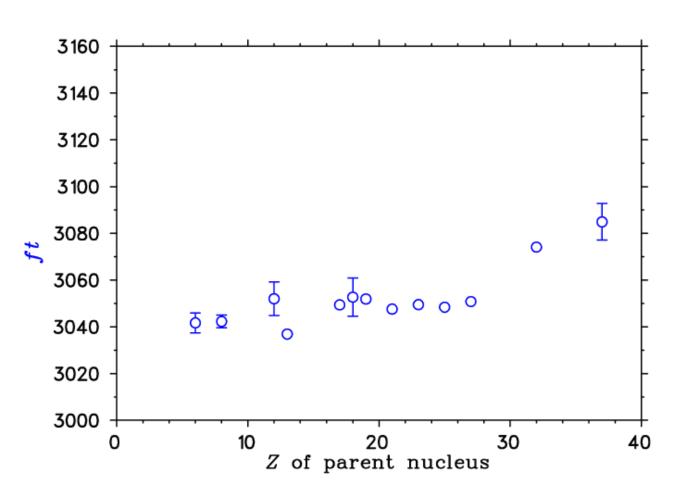
1. Experimentally determine the $\mathcal{F}t$ value by measuring Q_{EC} , $t_{1/2}$ and the branching ratio, and applying corrections

 $\mathcal{F}t = ft(1 + \frac{\delta_R'}{\delta_R})[1 - (\frac{\delta_C}{\delta_C} - \frac{\delta_{NS}}{\delta_{NS}})]$



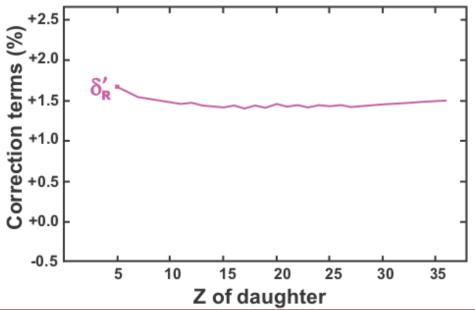
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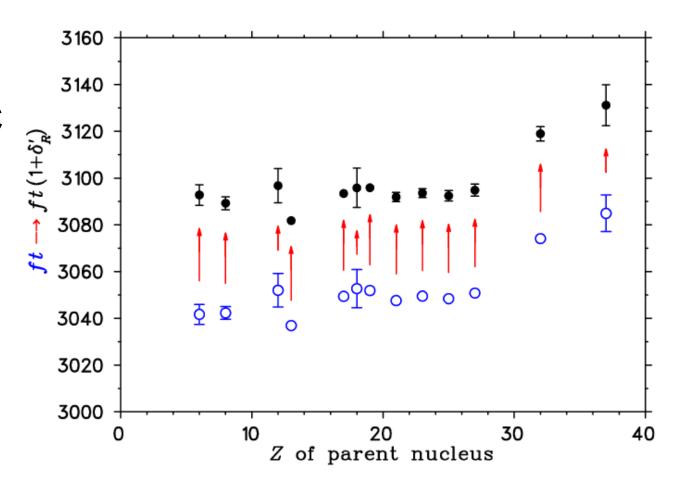
$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})]$$



1. Experimentally determine the $\mathcal{F}t$ value by measuring Q_{EC} , $t_{1/2}$ and the branching ratio, and applying corrections

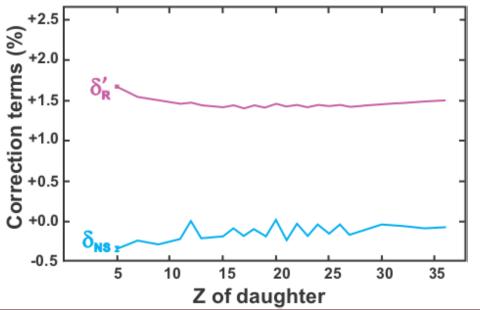
$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})]$$

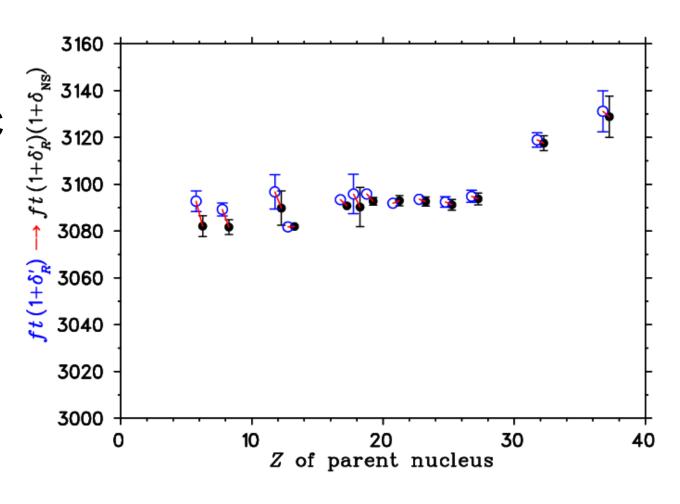




1. Experimentally determine the $\mathcal{F}t$ value by measuring Q_{EC} , $t_{1/2}$ and the branching ratio, and applying corrections

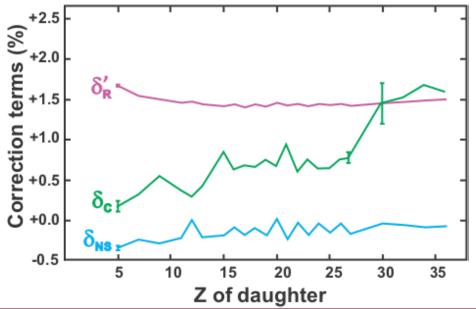
$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})]$$

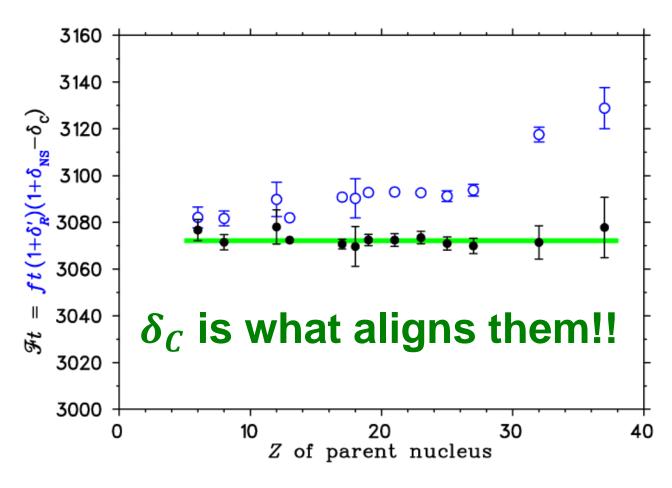




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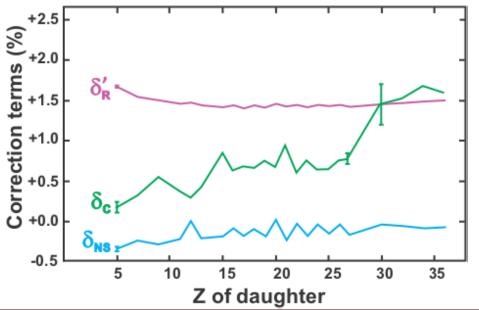
$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C' - \delta_{NS})]$$

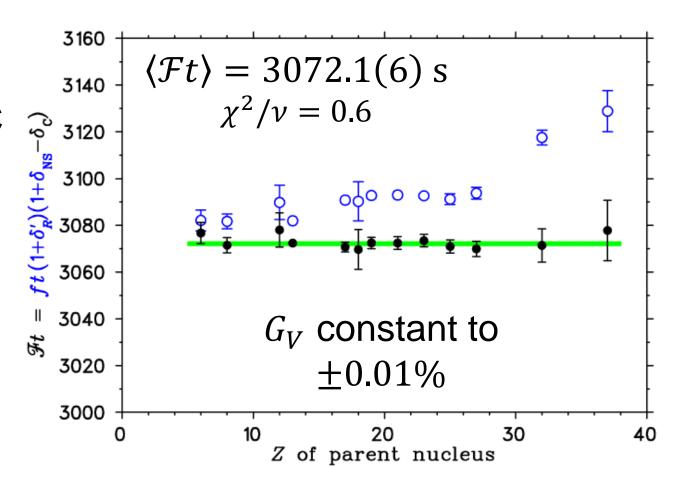




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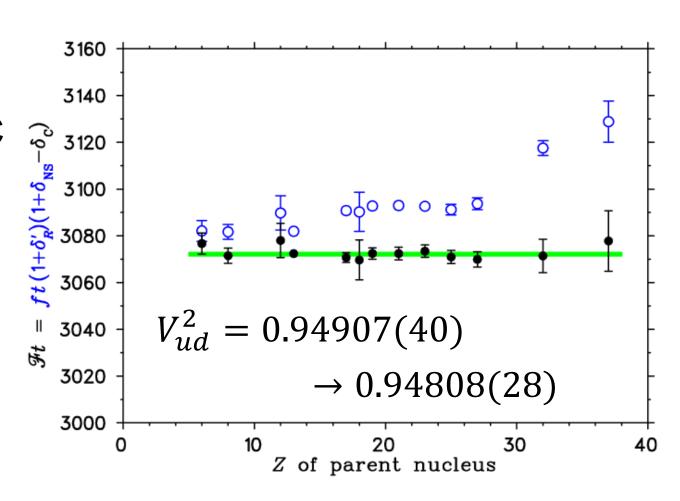




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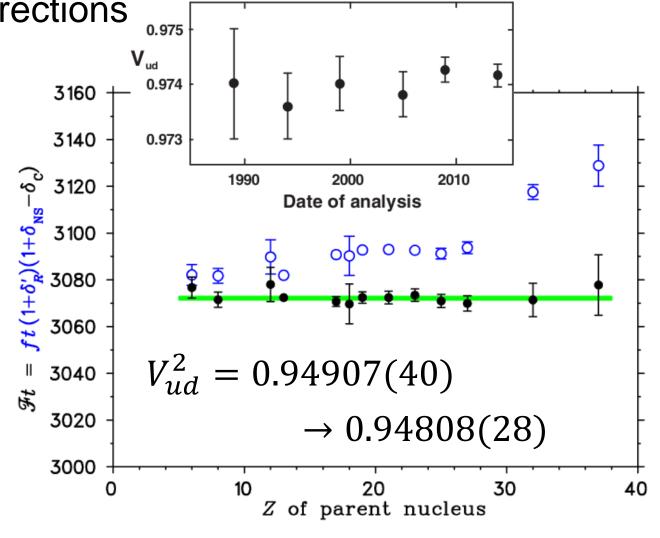
- 2. From many transitions, test CVC and the correction terms
- 3. With CVC verified, determine $\langle \mathcal{F}t \rangle$ and $V_{ud}^2 = \frac{K/G_F^2}{2\langle \mathcal{F}t \rangle (1 + \Lambda_F^V)}$



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$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})]$$

- 2. From many transitions, test CVC and the correction terms
- 3. With CVC verified, determine $\langle \mathcal{F}t \rangle$ and $V_{ud}^2 = \frac{K/G_F^2}{2/\mathcal{F}t \setminus (1 + \Lambda^V)}$



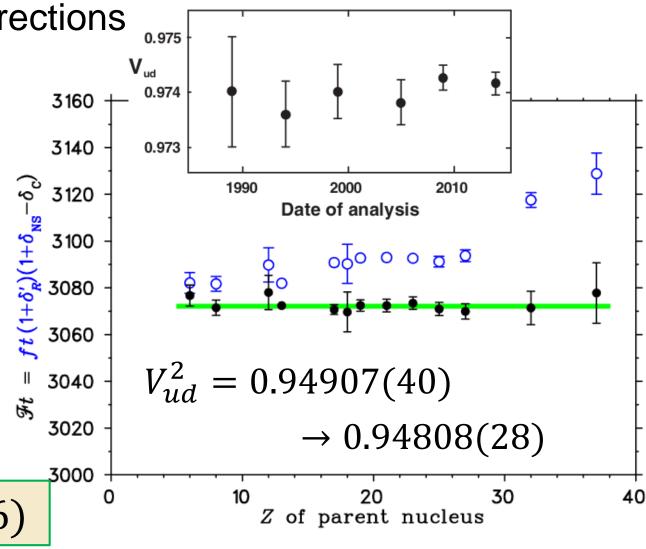
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branching ratio, and applying corrections

$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})]$$

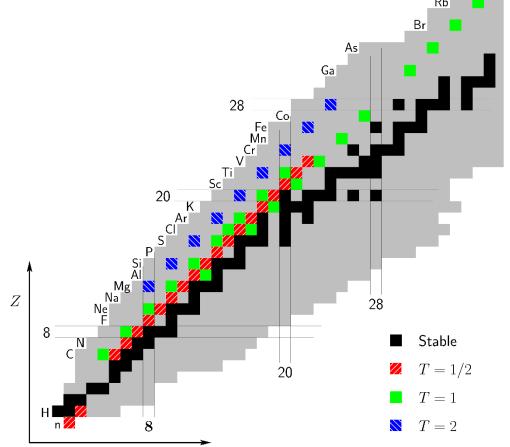
- 2. From many transitions, test CVC and the correction terms
- 3. With CVC verified, determine $\langle \mathcal{F}t \rangle$ and $V_{ud}^2 = \frac{K/G_F^2}{2\langle \mathcal{F}t \rangle (1 + \Delta_P^V)}$
- 4. Test CKM unitarity

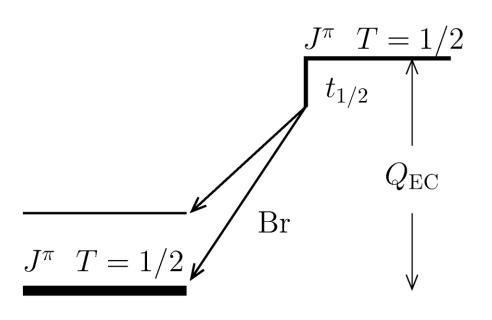
$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.99841(36)$$



These isobaric analogue decays are also theoretically tractable, but experimentally more difficult (mirrors) and/or limited (only one neutron)

$$\mathcal{F}t = ft(1 + \frac{\delta_R'}{\delta_R})[1 - (\frac{\delta_C}{\delta_C} - \frac{\delta_{NS}}{\delta_N})] = \frac{K/G_F^2}{V_{ud}^2(1 + \frac{\Delta_R^V}{\delta_R})(M_F^2 + (G_A/G_F)^2 M_{GT}^2)}$$

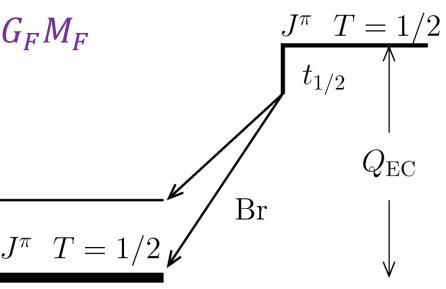




These isobaric analogue decays are also theoretically tractable, but experimentally more difficult (mirrors) and/or limited (only one neutron)

$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})] = \frac{K/G_F^2}{V_{ud}^2(1 + \Delta_R^V)(M_F^2 + (G_A)G_F)^2(M_{GT}^2)}$$

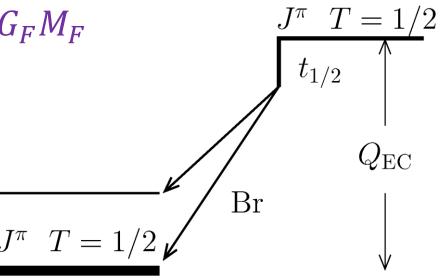
- The neutron: $M_{GT} = \sqrt{3}$, but must measure $\lambda = G_A/G_F$
- Mirror transitions: must measure $\rho = G_A M_{GT}/G_F M_F$



These isobaric analogue decays are also theoretically tractable, but experimentally more difficult (mirrors) and/or limited (only one neutron)

$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})] = \frac{K/G_F^2}{V_{ud}^2(1 + \Delta_R^V)(M_F^2 + (G_A)G_F)^2(M_{GT}^2)}$$

- The neutron: $M_{GT} = \sqrt{3}$, but must measure $\lambda = G_A/G_F$
- Mirror transitions: must measure $\rho = G_A M_{GT}/G_F M_F$
 - \Rightarrow must additionally measure a correlation parameter, e.g. A_{β} , and/or $a_{\beta\nu}$, and/or ...

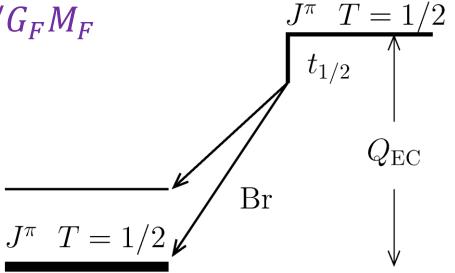


+ correlation parameter(s)

These isobaric analogue decays are also theoretically tractable, but experimentally more difficult (mirrors) and/or limited (only one neutron)

$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})] = \frac{K/G_F^2}{V_{ud}^2(1 + \Delta_R^V)(M_F^2 + (G_A)G_F)^2 M_{GT}^2}$$

- The neutron: $M_{GT} = \sqrt{3}$, but must measure $\lambda = G_A/G_F$
- Mirror transitions: must measure $\rho = G_A M_{GT}/G_F M_F$
 - \Rightarrow must additionally measure a correlation parameter, e.g. A_{β} , and/or $a_{\beta\nu}$, and/or ...
- * Significant plus: **no** δ_C or δ_{NS} corrections for the neutron!



+ correlation parameter(s)

D. Melconian ECT* April 2019

Summary of neutron decay

No time to talk about recent efforts (but see Albert Young's talk from last

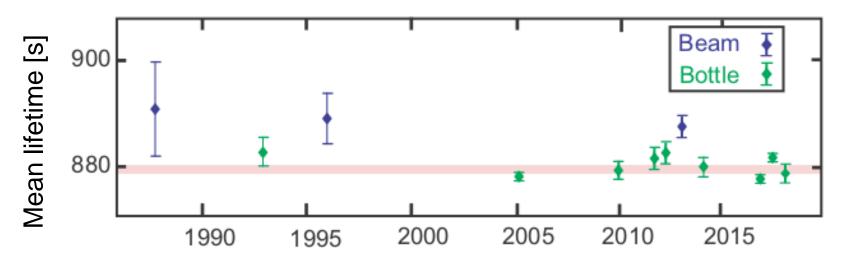
week!)

$$\tau = 879.7(8) \text{ s}$$

 $\chi^2/\nu = 3.8$

Beam: $888.1 \pm 2.0 \text{ s}$

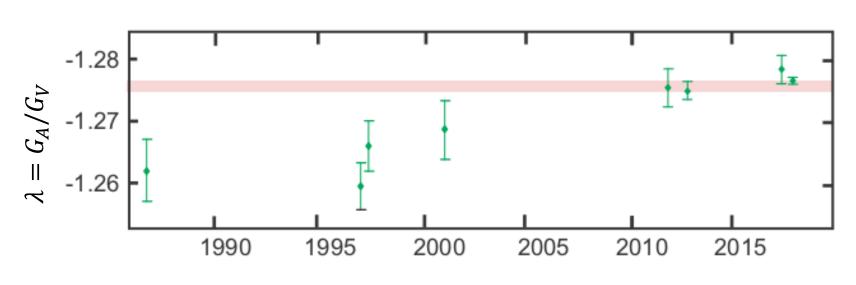
Bottle: $879.4 \pm 0.6 \text{ s}$



$$\lambda = -1.2764(6)$$
 (PERKEO III result arXiv:1812.04666)

$$V_{ud} = 0.9730(6)$$

(lots of activity here)

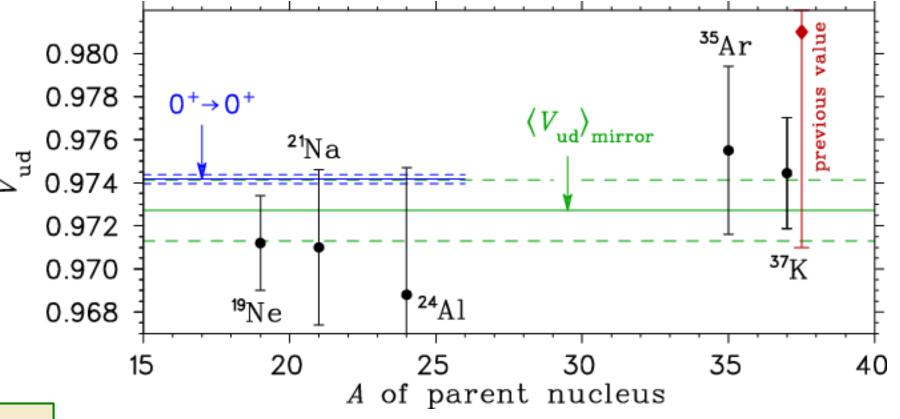


Summary of mirror transitions

And Albert talked about ¹⁹Ne[†], but a few other cases have been measured as well:

* All uncertainties dominated by their correlation measurement(s)

* Tough to imagine these will be truly competitive with $0^+ \rightarrow 0^+$ decays...



$$V_{ud} = 0.9722(14)$$

[†]Or at least I thought he was...

And there's the decay of the pion

• Like the neutron, theoretically clean with no δ_C nor δ_{NS} corrections

$$\pi^+ \rightarrow \pi^0 + e^+ + \nu_e$$

Masses and lifetime known precisely enough, but

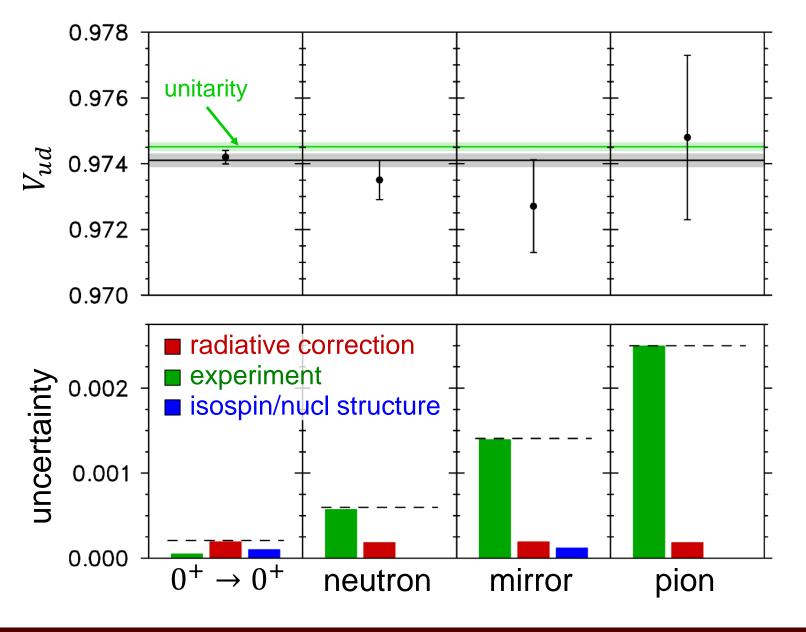
$$Br = 1.036(7) \times 10^{-8}$$

is a *really* small branch!

$$V_{ud} = 0.9743(25)$$

No (ambitious) plan to improve the branching ratio, not likely this will get more precise in the near future.

Summary of current status of V_{ud}



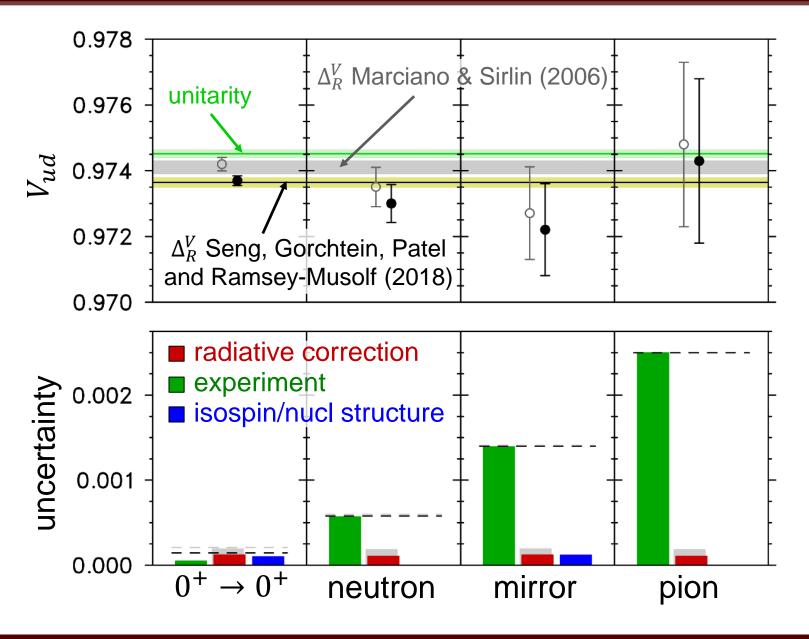
 $0^+ \to 0^+$: $V_{ud} = 0.9742(2)$

The neutron $V_{ud} = 0.9735(6)$

• Mirror transitions $V_{ud} = 0.9727(14)$

* The pion $V_{ud} = 0.9748(25)$

Summary of current status of V_{ud}



$$v_{ud}$$
 0 + → 0 +:
 v_{ud} = 0.9742(2)
→ 0.9737(1)

The neutron

$$V_{ud} = 0.9735(6)$$

 $\rightarrow 0.9730(6)$

Mirror transitions

$$V_{ud} = 0.9727(14)$$

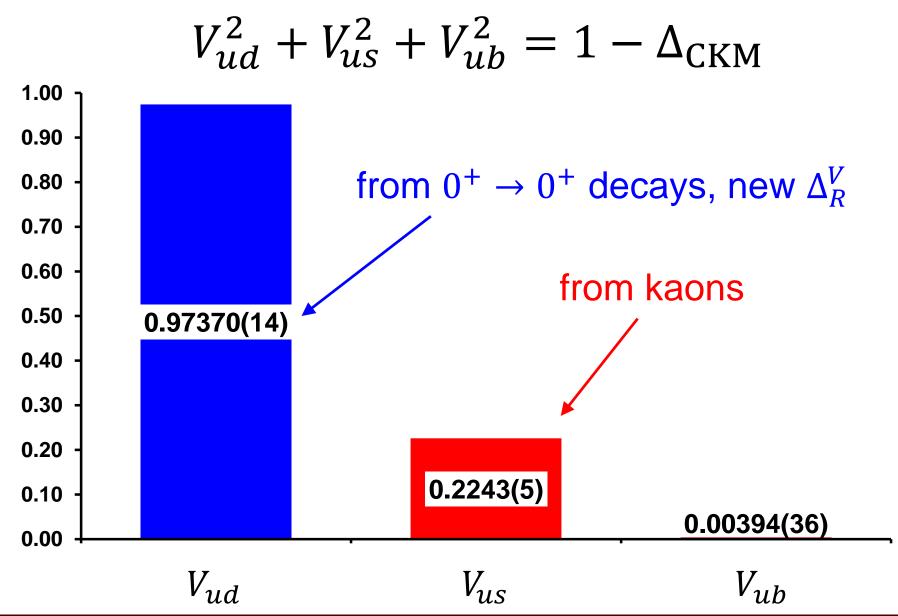
 $\rightarrow 0.9722(14)$

The pion

$$V_{ud} = 0.9748(25)$$

 $\rightarrow 0.9743(25)$

Summary of current status of CKM unitarity



Summary of current status of CKM unitarity

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1 - \Delta_{\text{CKM}}$$

- $V_{ud}^2 = 0.94798(27)$
 - from nuclear, neutron and π^+ decays; Δ_R^V from Seng et al., PRL **121**, 241804 (2018)
- $V_{us}^2 = 0.05031(22)$ from kaon decays (PDG)
- $V_{ub}^2 = 0.00002$ from B decays (negligible)

$$\Rightarrow \Delta_{\text{CKM}} = 1.69(35) \times 10^{-5}$$

is **still** dominated by $\Delta_R^V = 2.467(22)\%$ (though kaons barely behind now)

If the uncertainty in Δ_R^V is further reduced by $3 \times :$ \Rightarrow uncertainty in $V_{ud}^2 \rightarrow 0.00020$ and uncertainty in $\Delta_{\rm CKM} \rightarrow 0.00030$

- JCH

Looking ahead

- "What is the inner radiative correction, Δ_R ?"
 - * Currently the most important and impactful way to improve the unitarity test
- "How much can we believe the ISB corrections? Can we test them?"
 - * At the moment, HF shell model the only one to truly satisfy CVC
- "Can we improve existing cases with $\Delta \mathcal{F}t \lesssim 0.25\%$?"
 - * Maybe, but with ~220 measurements going into 15 ft values...it ain't easy to make a dent
- "Can we add new $0^+ \rightarrow 0^+$ transitions with $\Delta \mathcal{F}t \lesssim 0.25\%$?"
 - * Yes, but will require theoretical progress in heavier nuclei
- * "How much progress can be made with T = 1/2 transitions?"
 - * The neutron still has problems (beam vs bottle), but is only $4 \times$ less precise than $0^+ \rightarrow 0^+$, and there is a lot of experiments in progress and planned
 - * Determining $\rho = G_A M_{GT}/G_V M_F$ is very hard...(but ¹⁹Ne and ³⁷K, at least, have potential)
- "Can V_{ud} from the pion be improved?"
 - * Not in the forseeable future...

"What is the inner radiative correction, Δ_R ?"

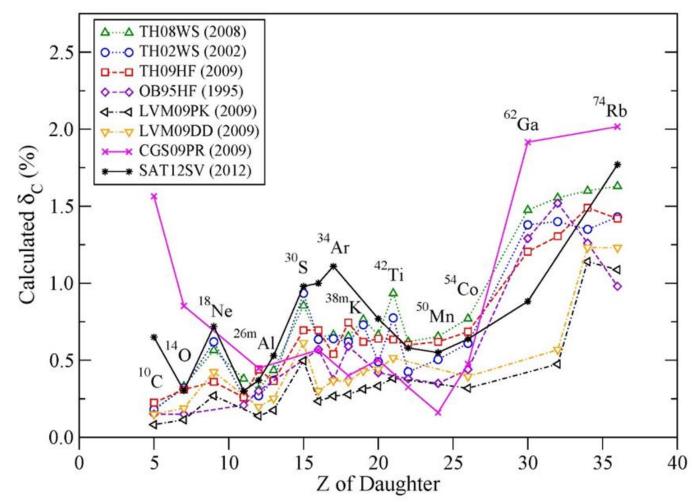
- Marciano & Sirlin made a huge stride in 2006: $\Delta_R^V = 2.361(38)\%$
 - * 0.38% uncertainty in Δ_R^V still dominated unitarity test
- Even more ground-breaking: Seng, Gorchtein, Patel and Ramsey-Musolf, PRL 121, 241804 (2018)
 - * Reduces the uncertainty by a nearly a factor of 2: $\Delta_R^V = 2.467(22)\%$
- If correct and no double-counting, leads to $\Delta_{\text{CKM}} = 16(4) \times 10^{-4}$
 - * Uncertainty in Δ_R^V still dominates unitarity test, and now there is tension with unitarity!

Is there really a 4σ effect?

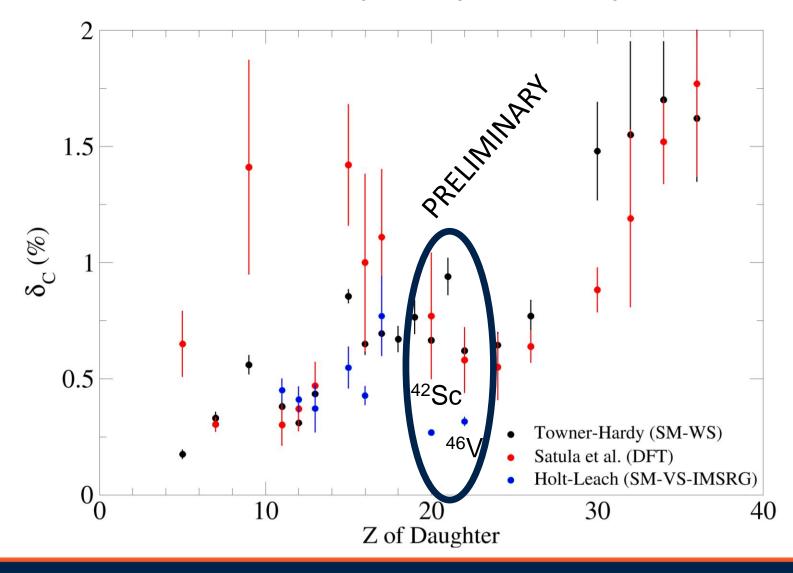
Exciting times (again)!

"How much can we believe the ISB corrections?"

- Flurry of activity circa 2010 to provide complementary calculations
 - * Shell Model
 - * Relativistic Hartree-Fock
 - * Random Phase Approximation
 - Energy Density Functional
- Only the Woods-Saxon shell model [TH] able to confirm CVC
- DFT indicates absolute scale of WS SM
- Newest kids on the block: Holt and Leach
- Reliable theoretical uncertainties?



Nuclear Isospin Symmetry Breaking (ISB) Calculations



- Using χ -EFT + VS-IMSRG now extends *abinitio* shell-model techniques up to the *pf*-shell and beyond
- Can calculate M_F directly to extract δ_C

$$\delta_C = 1 - \frac{|M_F|^2}{|M_F^0|^2}$$

$$=1-\frac{|M_F|^2}{2}$$

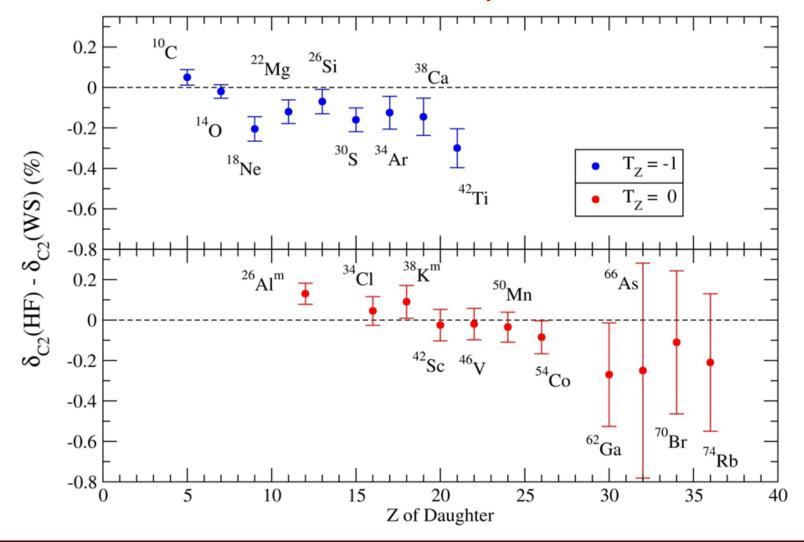
J.C. Hardy and I.S. Towner, Phys. Rev. C 91, 025501 (2015)
 W. Satula et al., Phys. Rev. C 86, 054316 (2012)
 J.D. Holt and K.G. Leach, in progress (2018)





"How much can we believe the ISB corrections?"

Hartree-Fock vs Woods-Saxon (just theory vs theory) radial overlap corrections: there is a Z-dependence



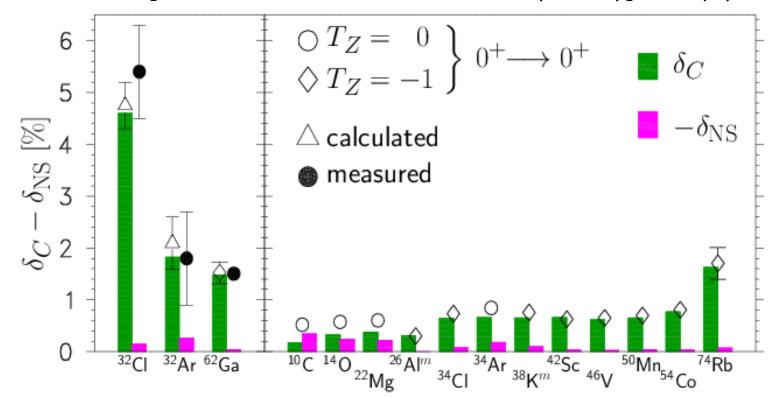
"...it would be nice to have our theory colleagues dig into [this] and explain."

- C.Svennson

Courtesy of C. Svennson

"Can we test calculations of ISB corrections?"

- Yes! We've been trying to for years, actually...
 - * 62Ga [Hyland et al, PRL **97** (2006)]: 1.42(11)% vs 1.38%
 - * 32Ar [Bhattacharya et al., PRC **77** (2008)]: 2.1(8)% → 1.8(8)% vs 2.0%
 - ** 32Cl [Melconian et al., PRL **107** (2011)]: 5.3(9)% vs 4.6%

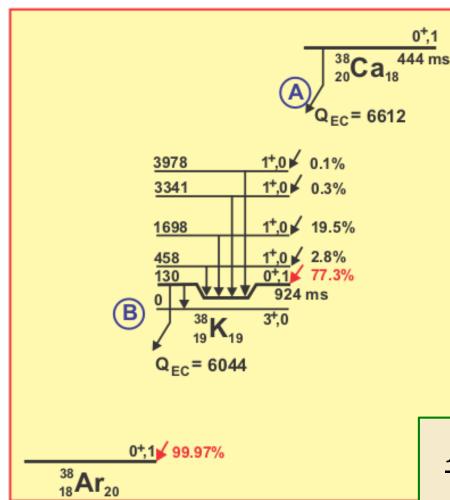


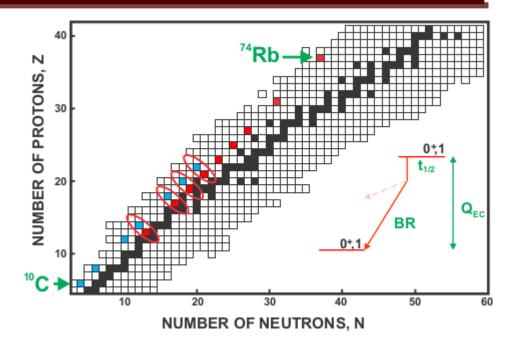
$$\mathcal{F}t = ft(1 + \delta_R')[1 - (\delta_C - \delta_{NS})]$$

$$\Leftrightarrow \quad \delta_{\mathcal{C}} = 1 + \delta_{\text{NS}} - \frac{\mathcal{F}t^{\text{others}}}{ft^{\text{exp}}(1 + \delta_{R}')}$$

WS vs HF: Mirror $0^+ \rightarrow 0^+$ transition pairs

* Ratio of $0^+ \rightarrow 0^+$ pairs less sensitive to theoretical uncertainties:





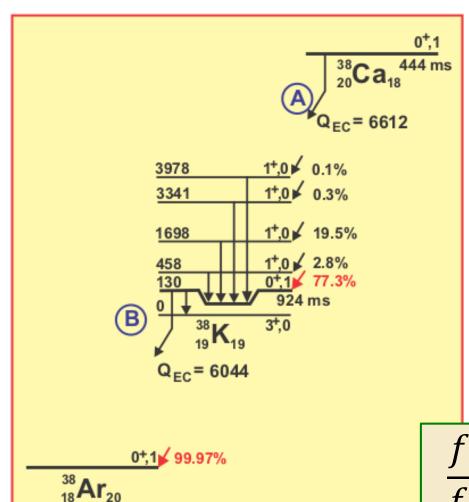
$$\frac{\mathcal{F}t_{A}}{\mathcal{F}t_{B}} = 1 = \frac{ft_{A}(1+\delta_{R}^{\prime A})[1-(\delta_{C}^{A}-\delta_{NS}^{A})]}{ft_{B}(1+\delta_{R}^{\prime B})[1-(\delta_{C}^{B}-\delta_{NS}^{B})]}$$

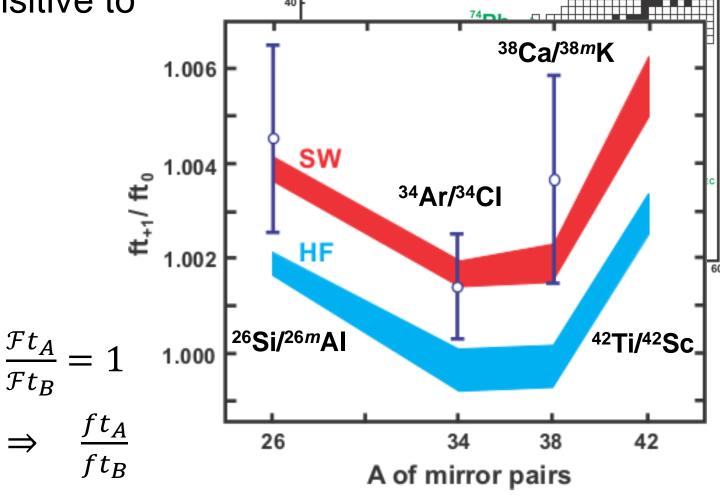
$$\Rightarrow \frac{ft_{A}}{ft_{B}} = \frac{(1+\delta_{R}^{\prime B})[1-(\delta_{C}^{B}-\delta_{NS}^{B})]}{(1+\delta_{R}^{\prime A})[1-(\delta_{C}^{A}-\delta_{NS}^{A})]}$$

$$\frac{ft_A}{ft_B} \approx 1 + \left(\delta_R^{\prime B} - \delta_R^{\prime A}\right) + \left(\delta_{NS}^B - \delta_{NS}^A\right) + \left(\delta_C^B - \delta_C^A\right)$$

WS vs HF: Mirror $0^+ \rightarrow 0^+$ transition pairs

Ratio of 0⁺ → 0⁺ pairs less sensitive to theoretical uncertainties:





$$\frac{ft_A}{ft_B} \approx 1 + \left(\delta_R^{\prime B} - \delta_R^{\prime A}\right) + \left(\delta_{NS}^B - \delta_{NS}^A\right) + \left(\delta_C^B - \delta_C^A\right)$$
ECT* April 2019

"Can we improve existing cases with $\Delta \mathcal{F}t \lesssim 0.25\%$?"

There is already so many precision experiments, significant improvements **Beta Activity**

is not practical in most cases

Cases being investigated:

* ²²Mg – BR @ GRIFFIN/TRIUMF [Svensson] and BR, τ and Q_{EC} @ TITAN [Leach]

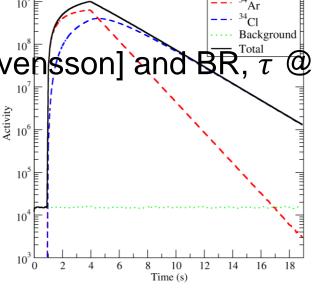
★ 26Si[†] – BR @ TAMU [Hardy]

* 30S - BR @ GANIL/LISE3 [Blank]

* 34Ar[†] – BR, τ @ TAMU and @ GRIFFIN

***** 42Ti[†] − BR @ TAMU

* 62Ga – check 0⁺ exc state in 62Zn @ GRIFFIN

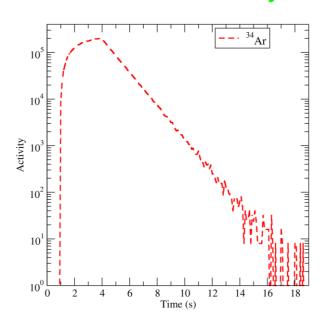


Gate on γ -ray transitions in the ³⁴Cl daughter

β-counting suffers from a large covariance between the 34Ar and ³⁴Cl lifetimes

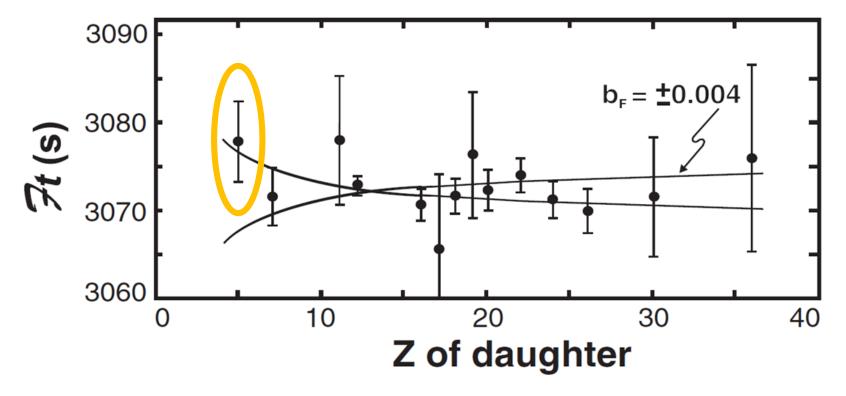
ISOLDE [Blank]

Gamma Activity



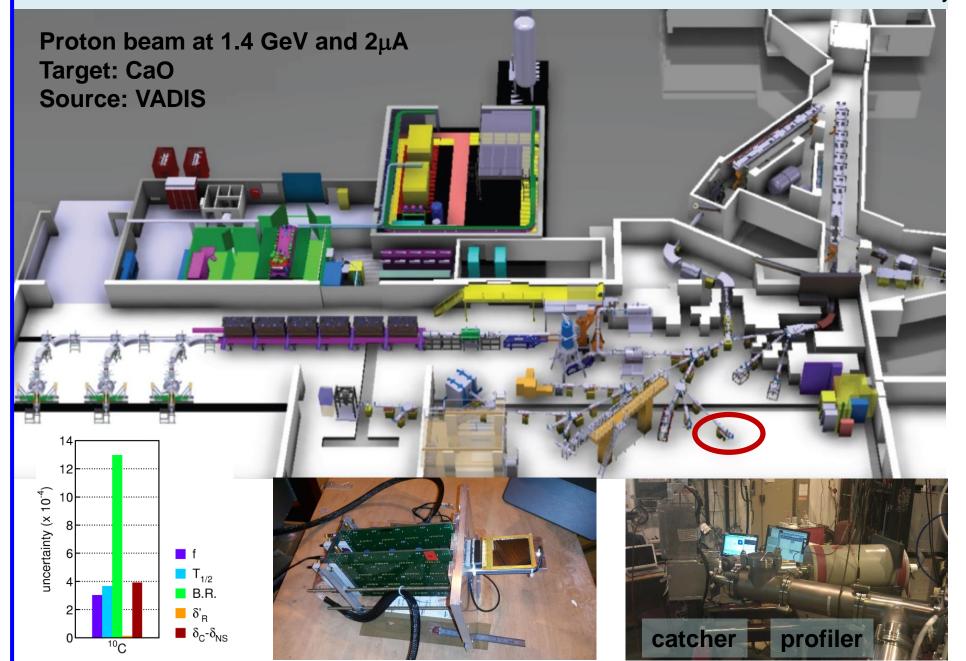
[†]mirror $0^+ \rightarrow 0^+$

Perhaps the most interesting (even if not for V_{ud} ...)

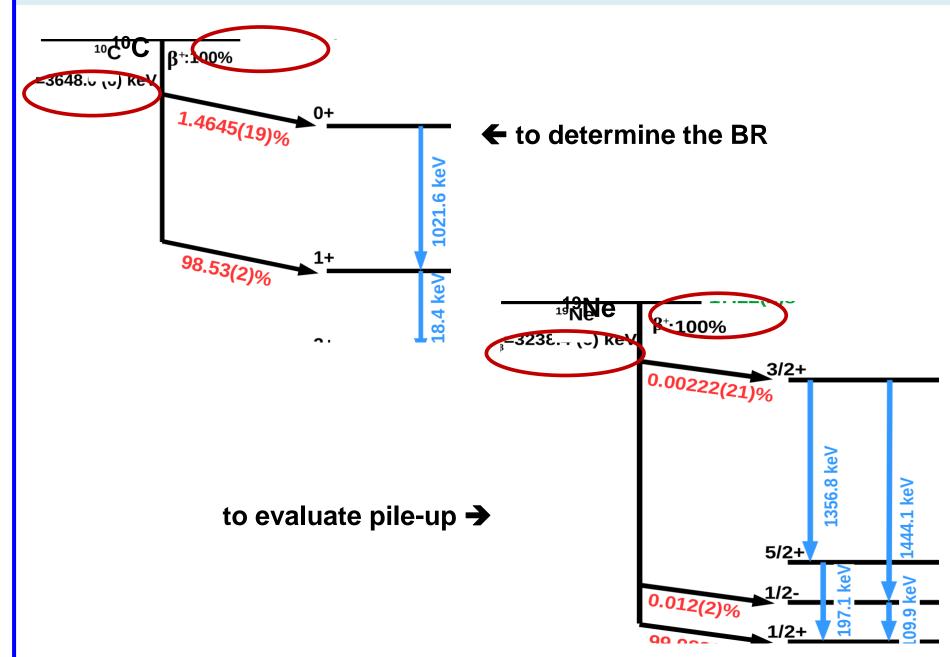


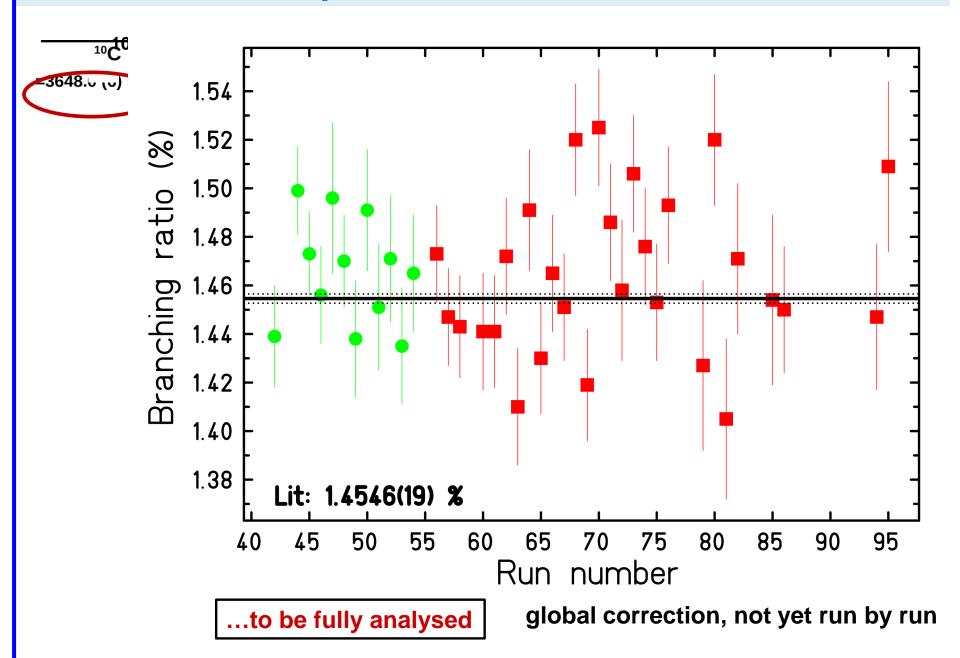
- Eronen & Hardy @ TAMU: BR analysis in progress
- Blank @ ISOLDE: BR analysis in progress
- Svensson @ TRIUMF: τ recently improved

• • ¹0C measurement at ISOLDE



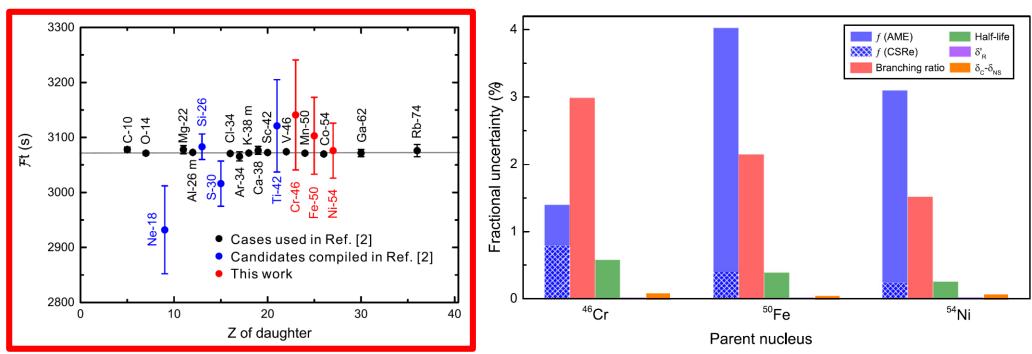
• • • ¹0C/¹9Ne decay scheme





"Can we add new $0^+ \rightarrow 0^+$ transitions with $\Delta \mathcal{F}t \lesssim 0.25\%$?"

- Yes, maybe? Cases I'm aware of:
 - ** 46 Cr BR, τ , Q_{EC} @ EURISOL-DF (Eronen)
 - * 50 Fe BR, τ , Q_{EC} @ EURISOL-DF (Eronen) and TITAN (Leach)
 - * 54 Ni BR, τ , Q_{EC} @ EURISOL-DF (Eronen)

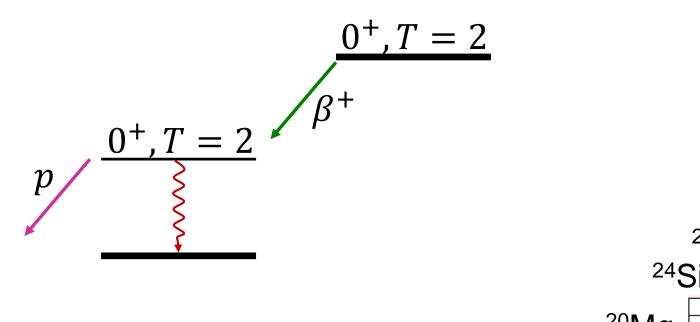


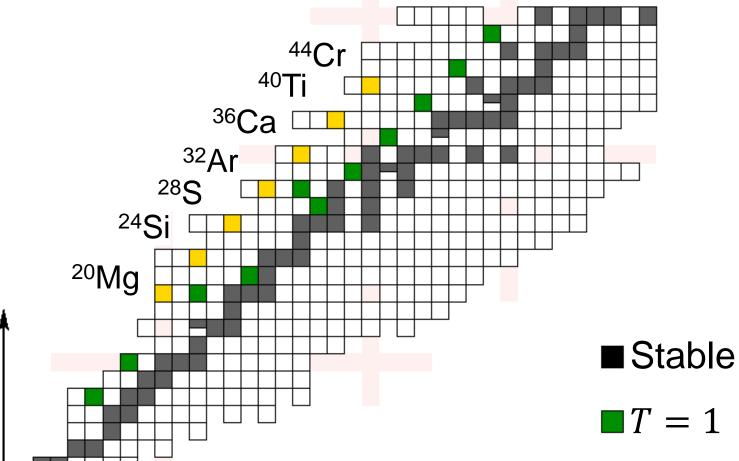
Courtesy of T. Eronen, who points out "These will never compete in precision with lower-A cases. Important for (isospin symmetry breaking) corrections"

"Can we add new $0^+ \rightarrow 0^+$ transitions with $\Delta \mathcal{F}t \lesssim 0.25\%$?"

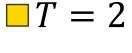
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 - * 50 Fe BR, τ , Q_{EC} @ EURISOL-DF (Eronen) and TITAN (Leach)
 - * 54 Ni BR, τ , Q_{EC} @ EURISOL-DF (Eronen)
- Heavier cases:
 - ***** 58Zn − BR, τ @ BigRIPS/RIKEN (Blank)
 - * 66 As $-Q_{EC}$ @ TITAN/TRIUMF (Leach)
 - * 70 Br Q_{EC} @ TITAN/TRIUMF (Leach)
 - * 74 Rb Q_{EC} @ TITAN/TRIUMF (Leach)
- The problem: shell model is not as well characterized above A = 56
 - * "Who's going to give beamtime and funding for boring spectroscopy?" JCH

More cases that may help with ISB corrections

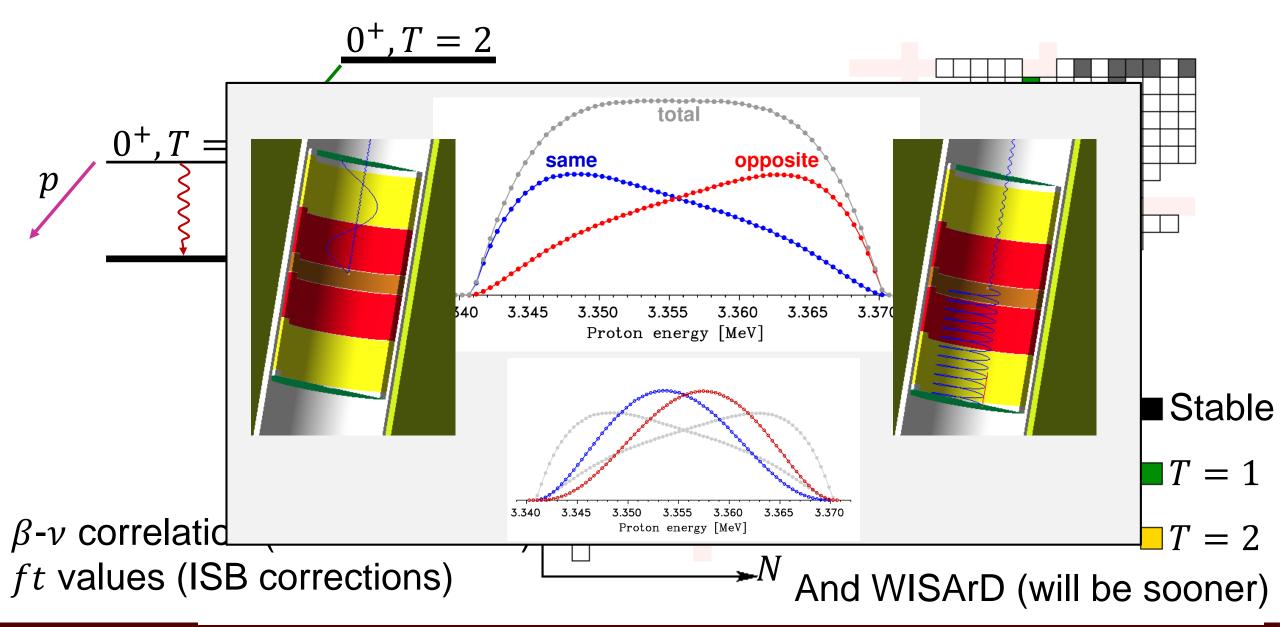




 β - ν correlation (scalar currents) ft values (ISB corrections)

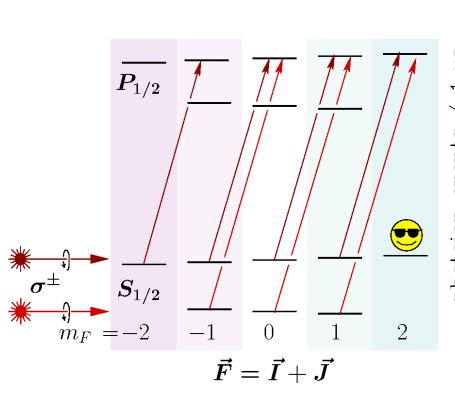


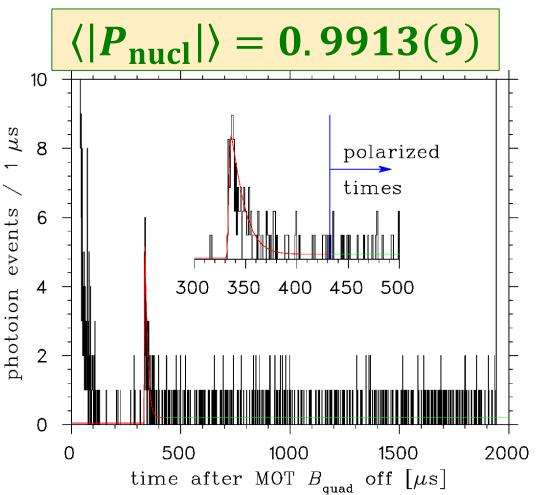
More cases that may help with ISB corrections



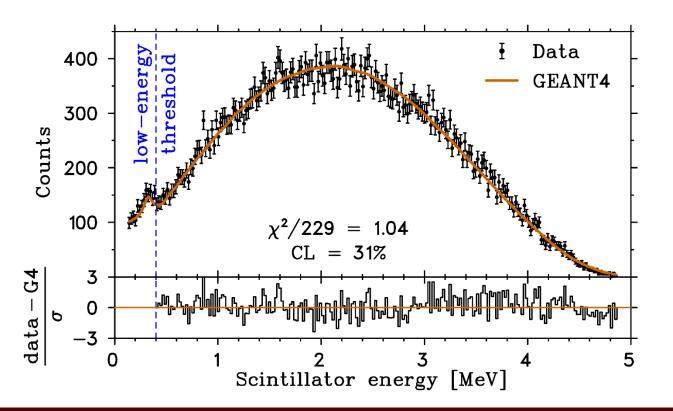
- Albert covered the neutron and ¹⁹Ne
- 37K @ TRINAT/TRIUMF [Melconian & Behr]

* High nuclear polarization: 99.13(9)%

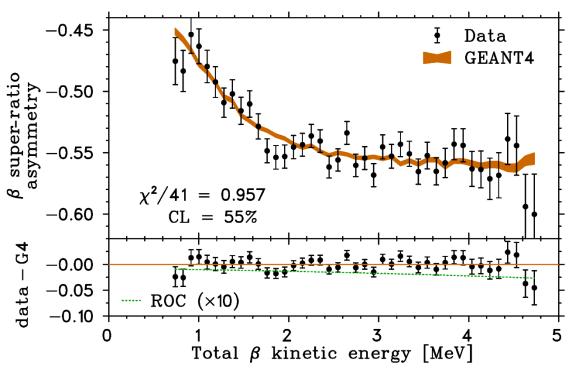




- Albert covered the neutron and ¹⁹Ne
- 37K @ TRINAT/TRIUMF [Melconian & Behr]
 - ★ High nuclear polarization: 99.13(9)%
 - ** Recent A_{β} to 0.3%; \leq 0.1% in sight

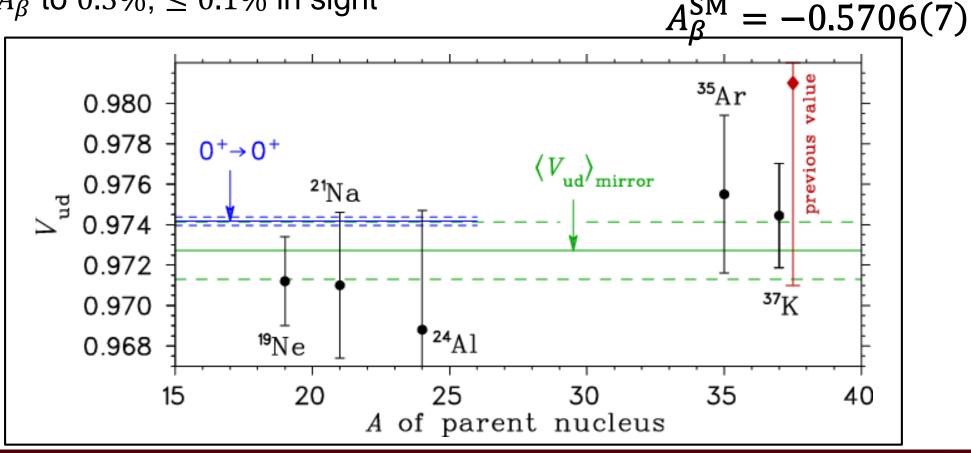


Fenker PRL 120 062502 (2018) $A_{\beta}^{\text{meas}} = -0.5707(19)$ vs $A_{R}^{\text{SM}} = -0.5706(7)$



- Albert covered the neutron and ¹⁹Ne
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Fenker PRL 120 062502 (2018) $A_{\beta}^{\rm meas} = -0.5707(19)$ VS

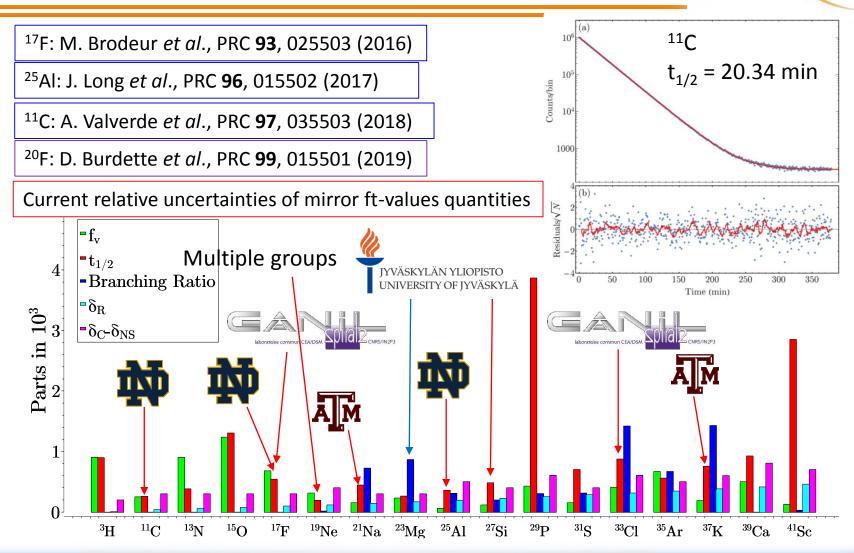


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- St. Benedict @ TwinSol $a_{\beta\nu}$ using a Paul trap



Half-lives measured @ ND





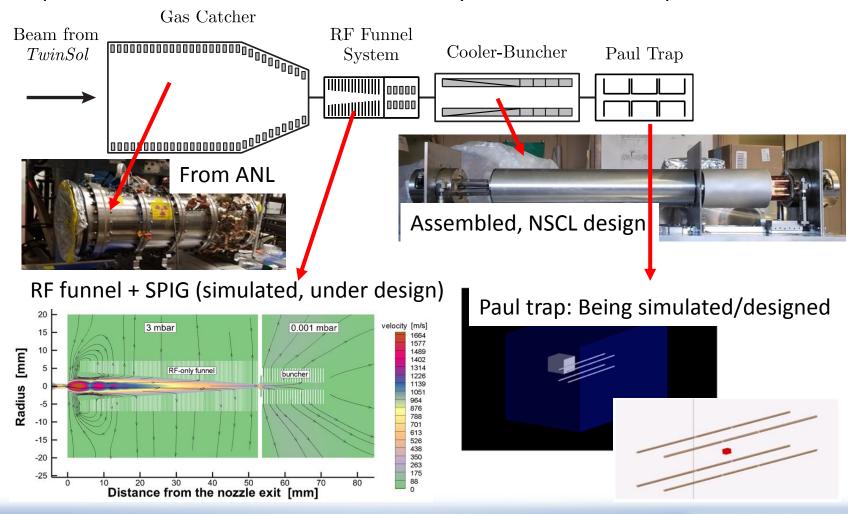




St. Benedict status



Superallowed Transitions Beta Neutrino Decay Ion Coincidance Trap



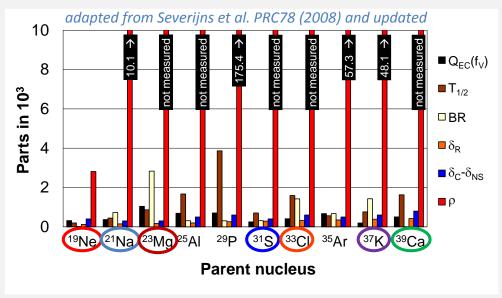


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CVC, V_{ud} & CKM: ft values measurements

Subject discussed in details in the next talk (Bertram Blank)

Nuclear mirrors





M: Mukherjee et al. EPJA35 (2008)
 T_{1/2}: Grinyer et al. PRC91 (2015)

²³Mg M: Saastamoinen et al. PRC80 (2009)

T_{1/2}, BR: *Magron et al. EPJA53 (2017)*

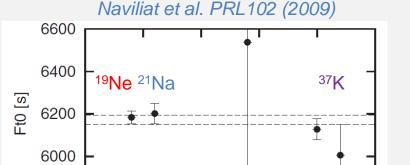
³¹S M: *Kankainen et al. PRC82 (2010)*

 $T_{1/2}$: Bacquias et al. EPJA48 (2012)

³³Cl $T_{1/2}$: *Grinyer et al. PRC92 (2015)*

³⁷K T_{1/2}: Shidling et al. PRC90 (2014) ³⁹Ca T_{1/2}: Blank et al. EPJA44 (2010)





25

Mass number A

30

35

40

The scientific community involved in this field... BUT

5800

15

20

$$V_{ud}$$
 (2009) = 0.9719 (17)
 \downarrow
 V_{ud} (2017) = 0.9721 (17) !!

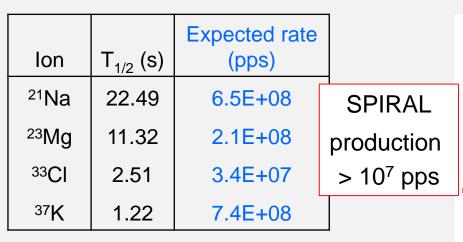
For V_{ud} determination, ρ improvements are necessary ...

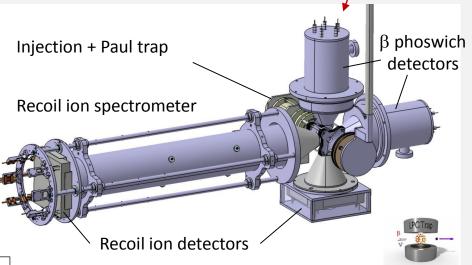
CVC, V_{ud} & CKM: ft values measurements

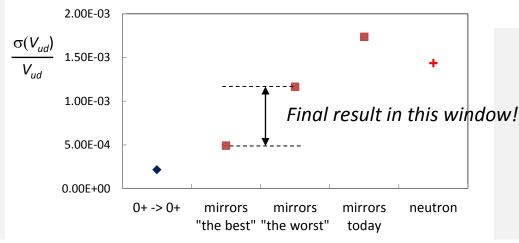
Subject discussed in details in the next talk (Bertram Blank)

Nuclear mirrors

Perspectives @ GANIL: Measurement of a in several mirror decays using LPCTrap2







In any case, a significant improvement on V_{ud} is reachable

@ LIRAT and DESIR

- Albert covered the neutron and ¹⁹Ne
- 37K @ TRINAT/TRIUMF [Melconian & Behr]
 - * High nuclear polarization: 99.13(9)%
 - * Recent A_{β} to 0.3%; 0.1% in sight
- St. Benedict @ TwinSol $a_{\beta\nu}$ using a Paul trap
- LPCTrap2 @ GANIL -- $a_{\beta\nu}$ using a Paul trap

Progress is slow, and it will be hard to compete directly with the precision of $0^+ \rightarrow 0^+$ decays

More cases for models to provide ISB corrections, perhaps make CVC test more stringent

Summary and outlook

After decades of work, it is getting hard to improve the CKM unitarity test

- Greatest progress to be made is through theoretical improvements
 - * Δ_R^V of course
 - * Improved modelling of heavy nuclei
 - * New approaches to complement WS shell model
- Experimentally:
 - * Mirror $0^+ \rightarrow 0^+$ promise a sensitive test of theoretical corrections
 - * 10°C is hard, but better BR will improve already impressive search for scalar currents
 - * The neutron is slowly approaching the precision of $0^+ \to 0^+$, and ultimately does not have $\delta_C \delta_{NS}$ corrections

But probably the best way to conclude:

SUMMARY AND OUTLOOK

- 1. Analysis of superallowed $0^+ \rightarrow 0^+$ nuclear β decay confirms CVC to $\pm 0.011\%$ and thus yields $V_{ud} = 0.97420(21)$.
- 2. The three other experimental methods for determining V_{ud} yield consistent results; the neutron-decay result is only a factor of 4 less precise and agrees completely.
- 3. The current value for V_{ud} , when combined with the PDG values for V_{us} and V_{ub} , satisfies CKM unitarity to ±0.05%.
- 4. The largest contribution to V_{ud} uncertainty is from the inner radiative correction, Δ_R . Very little reduction in V_{ud} uncertainty is possible without improved calculation of Δ_R .
- 5. Transition-dependent corrections have been tested by requiring consistency among the 14 known transitions (CVC), and agreement with mirror-transition pairs.
- 6. Improved and new correction terms are appearing. They will need to be tested for compatibility with CVC.

Thanks to many who gave me slides and comments, particularly:

- John Hardy
- * Carl Svensson
- ***** Bertram Blank
- * Tommi Eronen
- Kyle Leach
- * Etienne Lienard
- * Maxime Brodeur

