



华南理工大学
South China University of Technology

Particle production and hypernucleus formation in heavy-ion collisions

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Outline

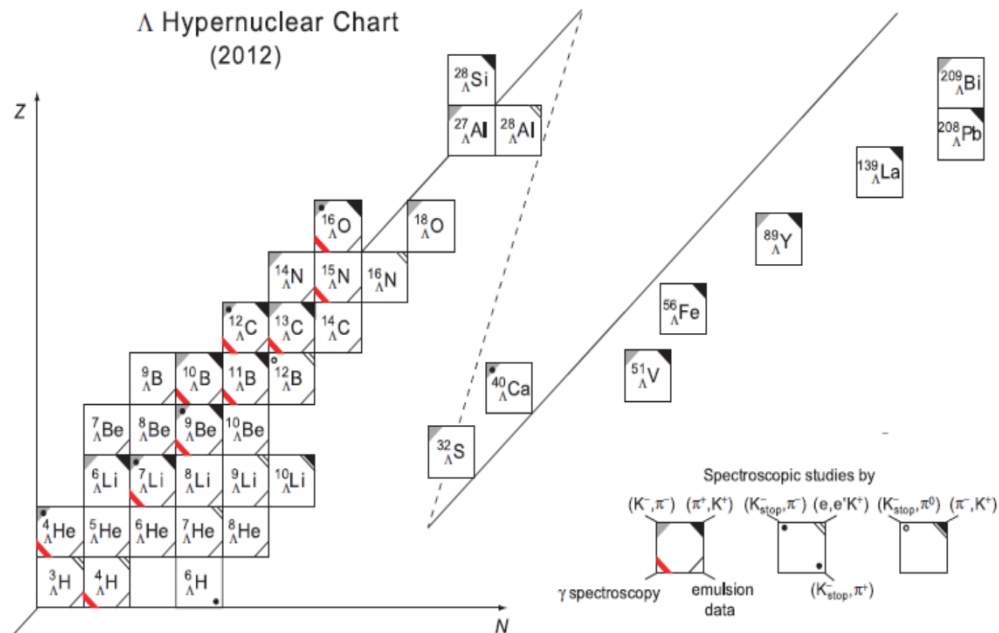


- Introduction
- Particle production in heavy-ion collisions and in hadron induced reactions near threshold energies
- In-medium and isospin effects on particle production (π , η , K , Λ , Σ , Ξ)
- Hypernuclear formation
- Summary

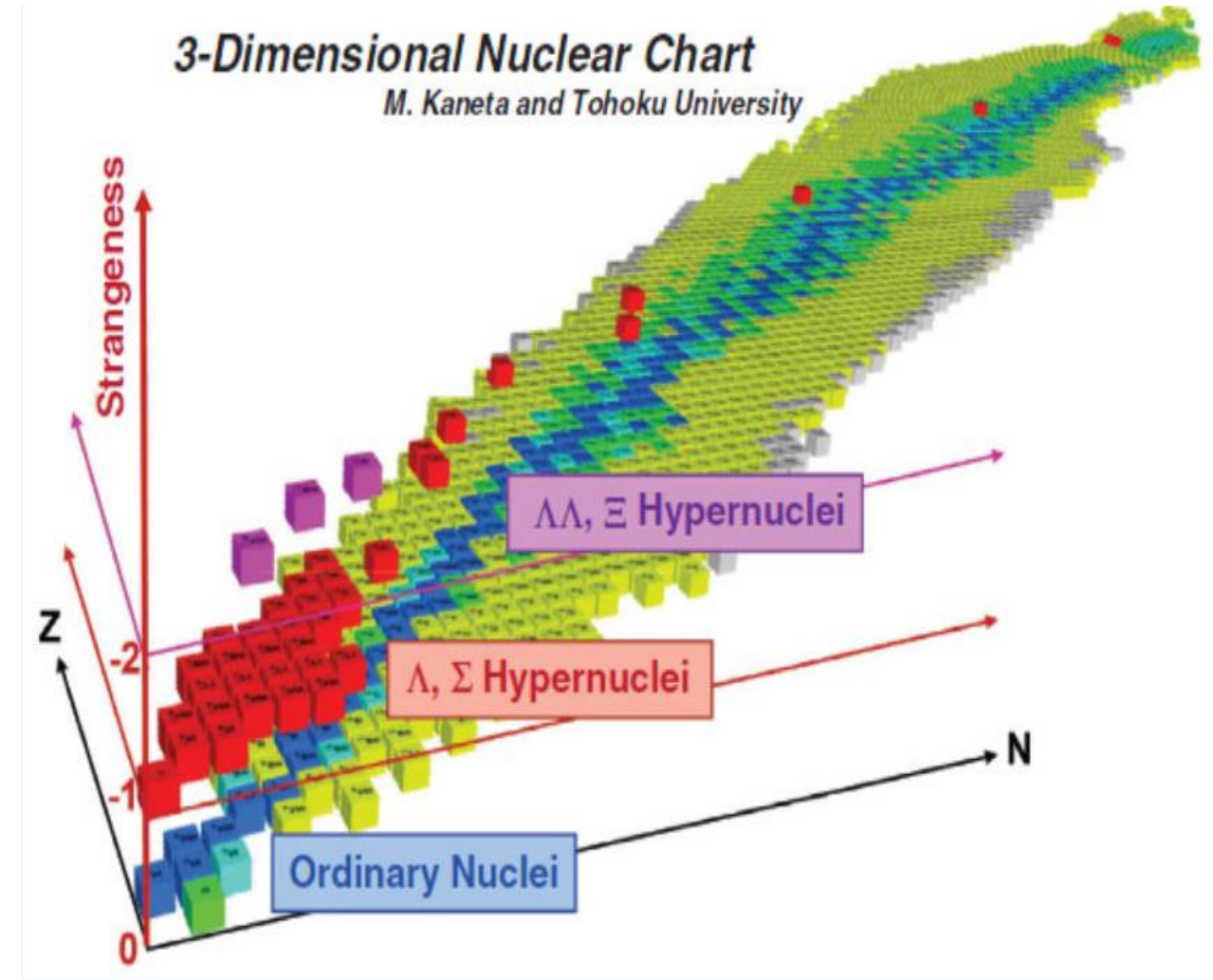
I. Introduction

Advantages of heavy-ion collisions on hypernucleus production

1. Neutron-rich/proton-rich hypernuclear isotopes
2. Hypernucleus with $s=-2$ by capturing $\Xi^{-,0}$ by nucleonic fragments
3. Λ - Λ correlation in dense nuclear matter



H. Tamura, *Prog. Theor. Exp. Phys.* (2012) 02B012

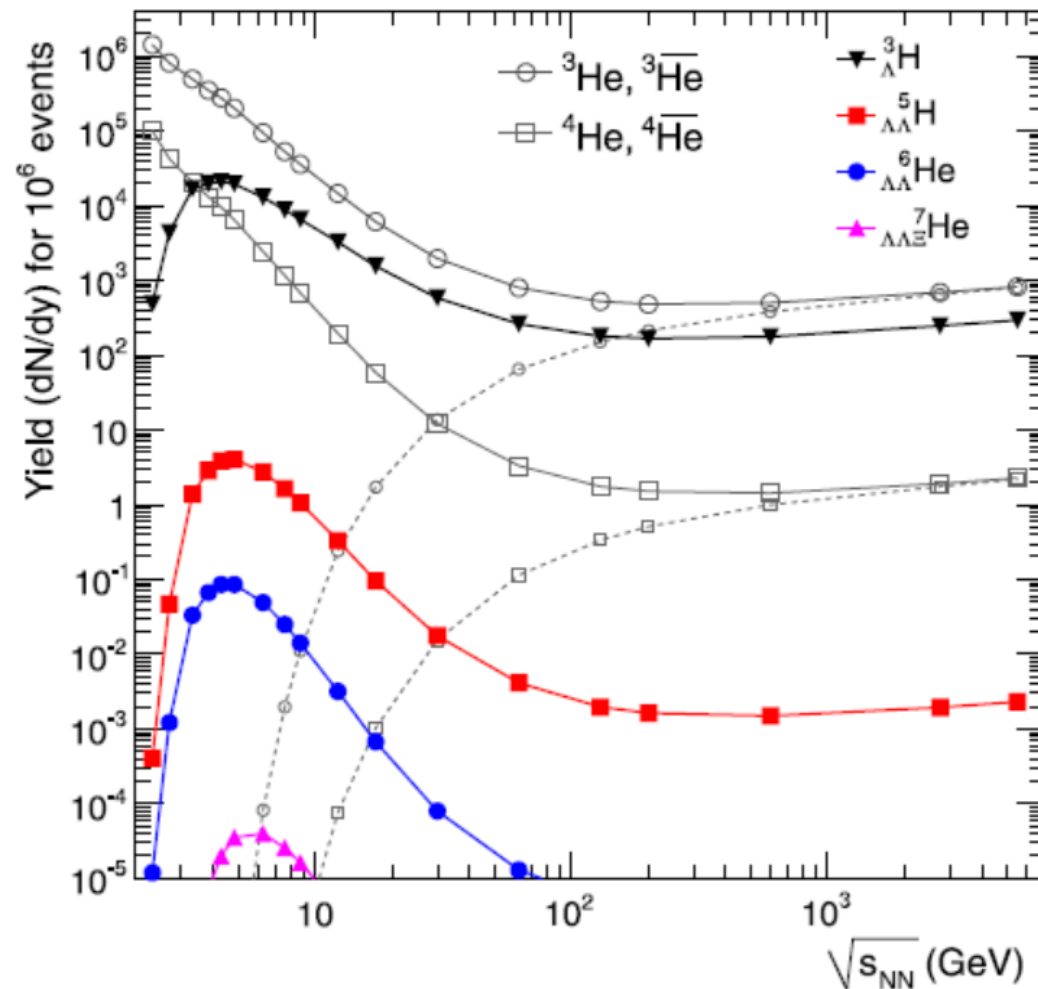


A. Andronic, P. Braun-Munzinger, J. Stachel, H. Stöcker,
Physics Letters B 697 (2011) 203–207

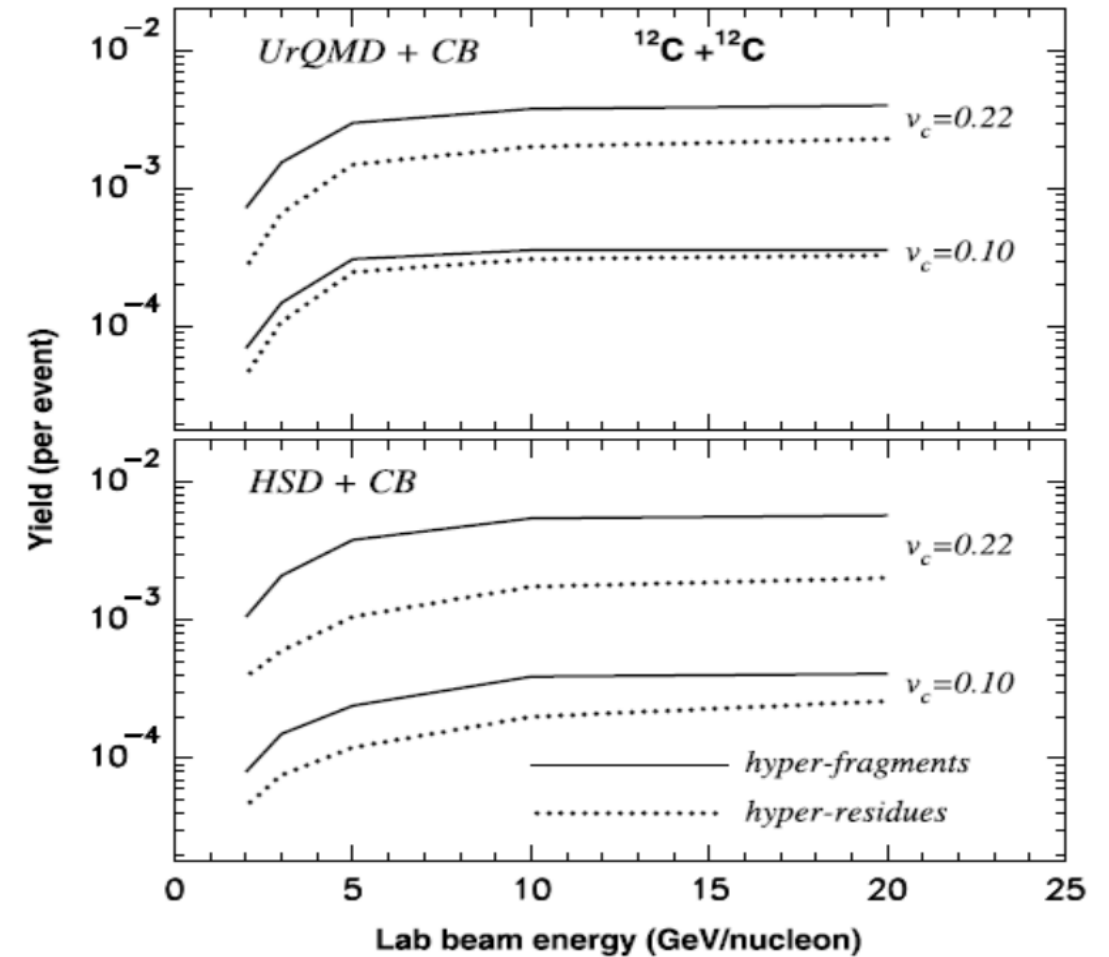
A.S.Botvina, J.Steinheimer, E.Bratkovskaya,
M.Bleicher, J.Pochodzalla, Physics Letters B 742
(2015)7–14

Pb+Pb

statistical model



transport model+coalescence approach



home.cern/about/accelerators/low-energy-antiproton-ring

Low Energy Antiproton Ring at CERN (1982-1996)

Proton Synchrotron (PS), Antiproton Collector (AC), Antiproton Accumulator (AA)

Physics: highly excited nucleus, delayed fission process, cold QGP, hadrons in-medium

...

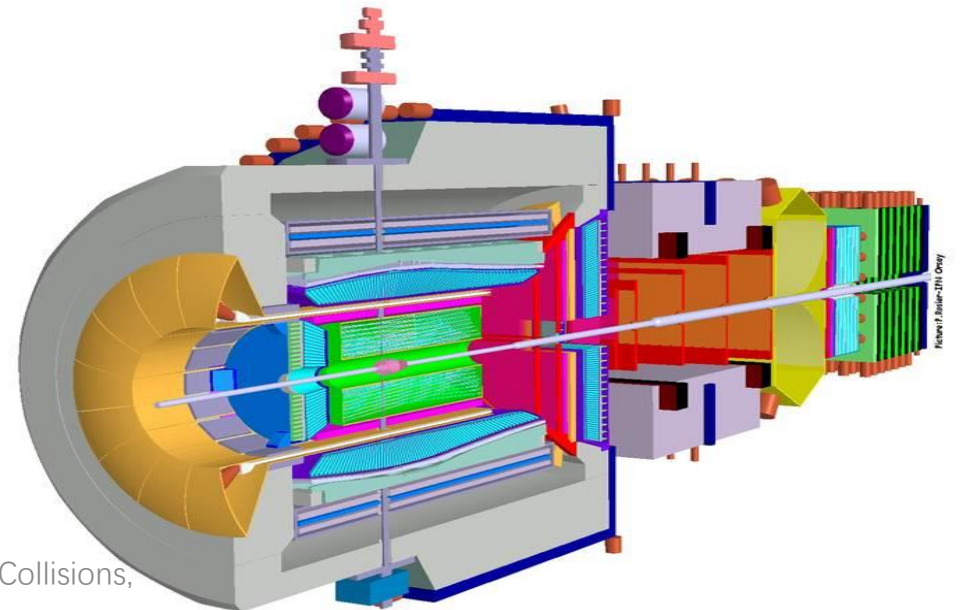


[PANDA detector from http://www-panda.gsi.de/](http://www-panda.gsi.de/)

PANDA(antiProton ANnihilation at Darmstadt)

Physics purpose:

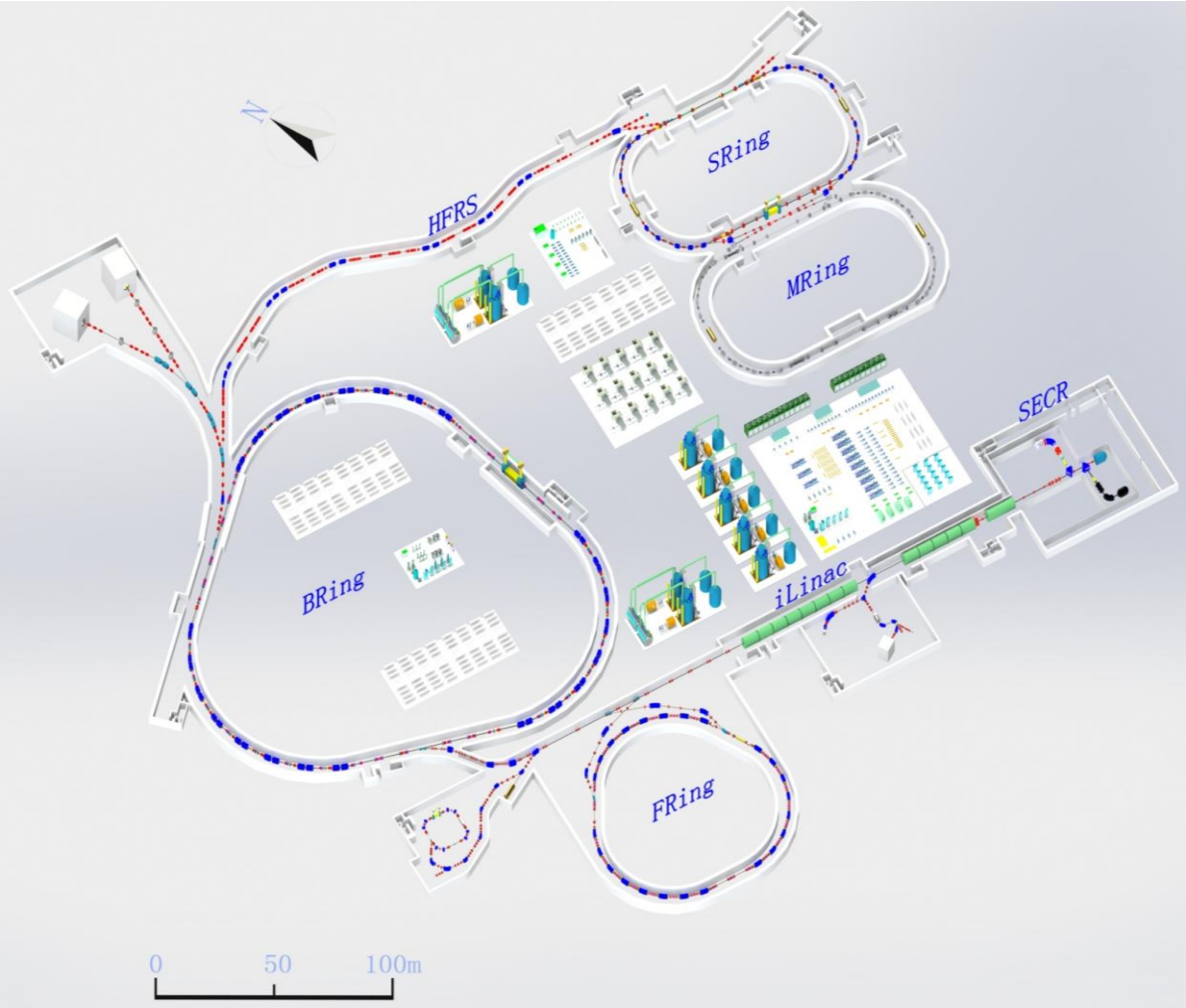
**Hadron Spectroscopy, Nucleon Structure,
Hadron in Baryonic Matter, Hypernucleus**



HIAF

(*High-Intensity Heavy Ion Accelerator Facility*)

Provided by Jian-Cheng Yang



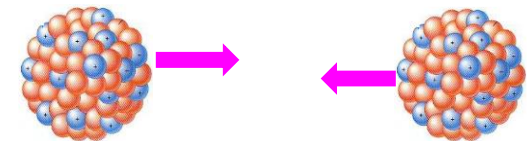
	Ions	Energy	Intensity
SECR	$^{238}\text{U}^{35+}$	14 keV/u	0.05- 0.1 pmA
iLinac	$^{238}\text{U}^{35+}$	17 MeV/u	0.028-0.05 pmA
FRing	$^{238}\text{U}^{35+}$	0.35 GeV/u	$\sim 2.0 \times 10^{11}$ ppp
BRing	$^{238}\text{U}^{35+}$	1.0 GeV/u	$\sim 1.0 \times 10^{12}$ ppp
	$^{238}\text{U}^{92+}$	3.8 GeV/u	$\sim 5.0 \times 10^{11}$ ppp
SRing	RIBs: neutron-rich, proton-rich	0.84 GeV/u ($A/q=3$)	$\sim 10^{9-10}$ ppp
	Fully stripped heavy ions H-like, He-like heavy ions	0.8 GeV/u ($^{238}\text{U}^{92+}$)	$\sim 10^{11-12}$ ppp

II. Model description

Lanzhou Quantum Molecular Dynamics (LQMD) transport model

Nuclear dynamics from 15 MeV/nucleon – 5 GeV/nucleon for HICs, antiproton (proton, π , K, etc)

- **Dynamics of low-energy heavy-ion collisions** (dynamical interaction potential, barrier distribution, neck dynamics, fusion/caption excitation functions etc)
- **Isospin physics at intermediate energies** (constraining nuclear **symmetry energy** at sub- and supra-saturation densities in HICs and probing isospin splitting of nucleon effective mass from HICs)
- **In-medium properties of hadrons in dense nuclear matter from heavy-ion collisions** (extracting optical potentials, i.e., $\Delta(1232)$, $N^*(1440)$, $N^*(1535)$), hyperons ($\Lambda, \Sigma, \Xi, \Omega$) and mesons ($\pi, K, \eta, \rho, \omega, \phi \dots$), hypernucleus dynamics)
- **Hadron (antiproton, proton, π^\pm , K^\pm) induced reactions** (hypernucleus production, e.g., $\Lambda(\Sigma)X$, $\Lambda\Lambda X$, ΞX , $\bar{\Lambda}X(S=1)$, in-medium modifications of hadrons, cold QGP)



Density, isospin and momentum-dependent single-nucleon potential in LQMD

$$U_{\tau}(\rho, \delta, \mathbf{p}) = \alpha \frac{\rho}{\rho_0} + \beta \frac{\rho^{\gamma}}{\rho_0^{\gamma}} + E_{\text{sym}}^{\text{loc}}(\rho) \delta^2 + \frac{\partial E_{\text{sym}}^{\text{loc}}(\rho)}{\partial \rho} \rho \delta^2 + E_{\text{sym}}^{\text{loc}}(\rho) \rho \frac{\partial \delta^2}{\partial \rho_{\tau}}$$

$$+ \frac{1}{\rho_0} C_{\tau, \tau} \int d\mathbf{p}' f_{\tau}(\mathbf{r}, \mathbf{p}) [\ln(\epsilon(\mathbf{p} - \mathbf{p}')^2 + 1)]^2$$

$$+ \frac{1}{\rho_0} C_{\tau, \tau'} \int d\mathbf{p}' f_{\tau'}(\mathbf{r}, \mathbf{p}) [\ln(\epsilon(\mathbf{p} - \mathbf{p}')^2 + 1)]^2.$$

$$C_{\tau, \tau} = C_{\text{mom}}(1 + x), \quad C_{\tau, \tau'} = C_{\text{mom}}(1 - x) \quad (\tau \neq \tau')$$

ZQF, Phys. Rev. C 84 (2011) 024610

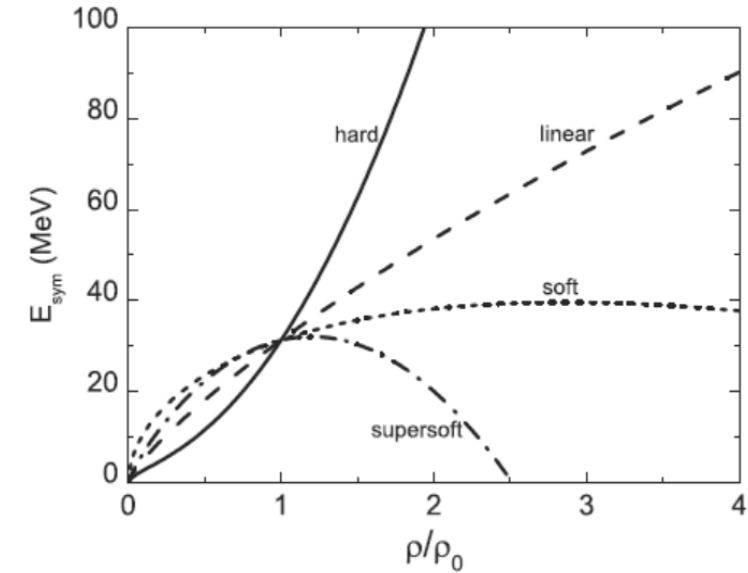


Table 1: The parameters and properties of isospin symmetric EoS used in the LQMD model at the density of 0.16 fm^{-3} .

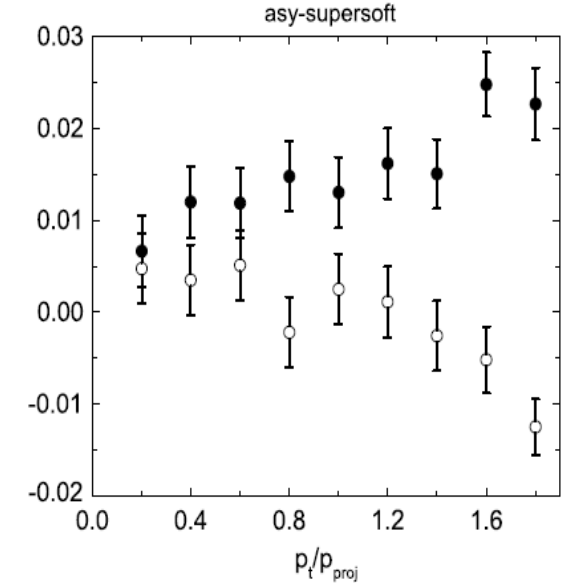
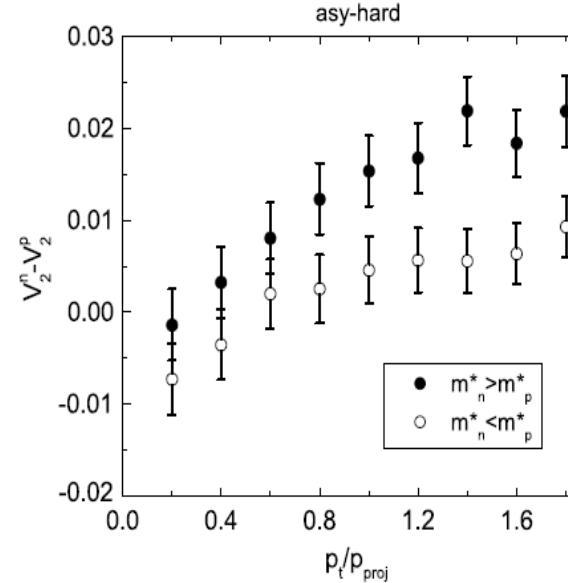
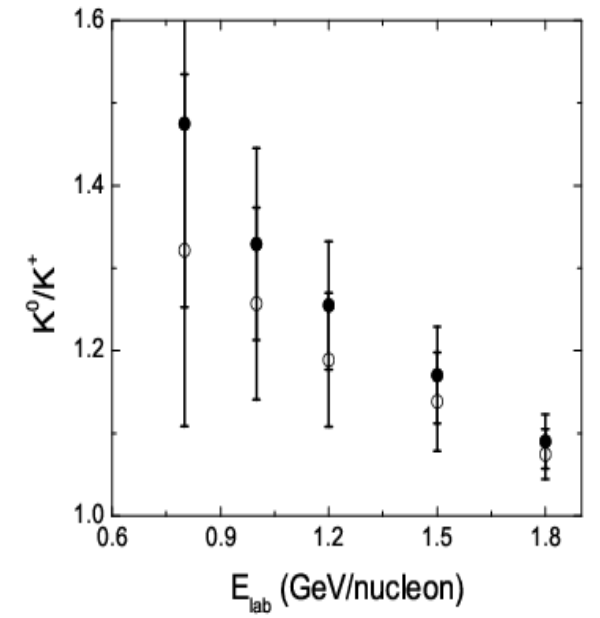
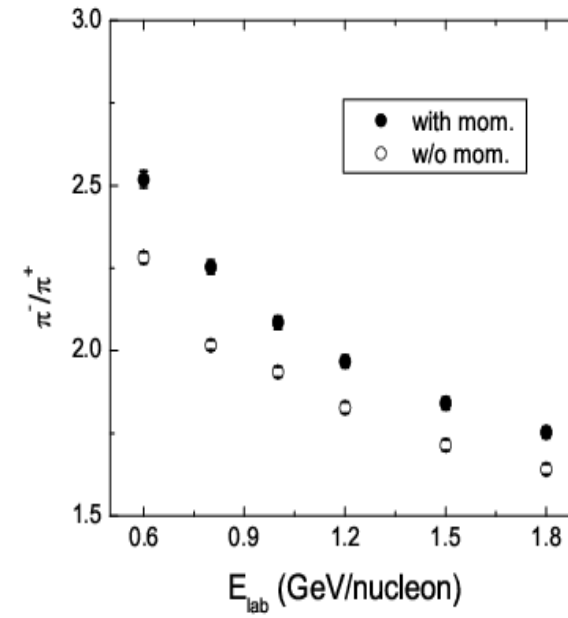
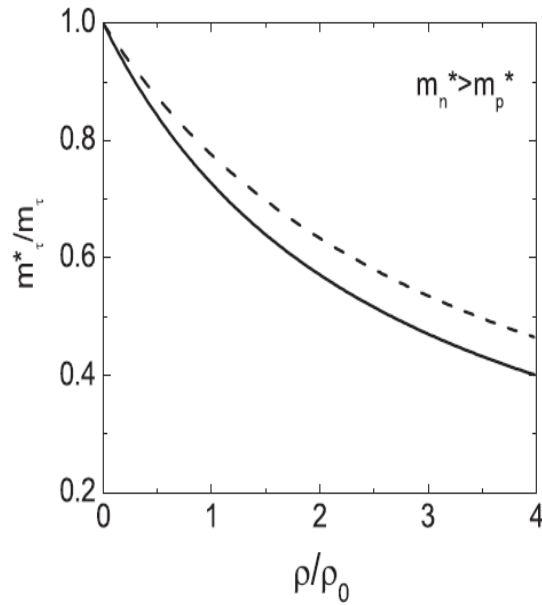
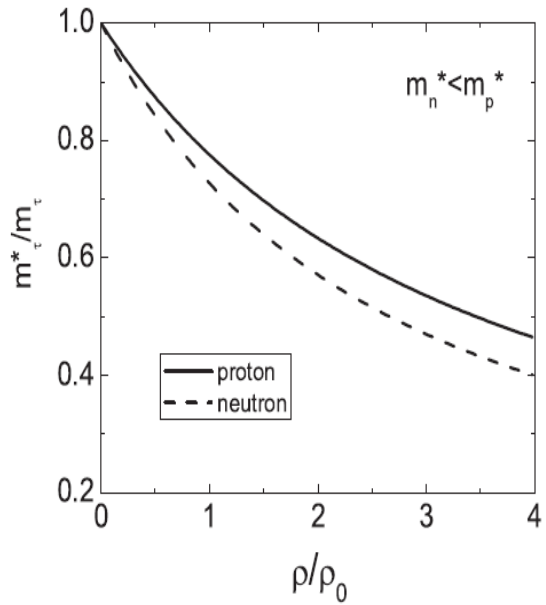
Parameters	α (MeV)	β (MeV)	γ	C_{mom} (MeV)	ϵ (c^2/MeV^2)	m_{∞}^*/m	K_{∞} (MeV)
PAR1	-215.7	142.4	1.322	1.76	5×10^{-4}	0.75	230
PAR2	-226.5	173.7	1.309	0.	0.	1.	230

Isospin splitting of nucleon effective mass on

isospin emissions in heavy-ion collisions

(Nucl. Phys. A 878 (2012) 3)

$$\frac{m_{\tau}^*}{m} = \left[1 + \frac{m}{\hbar^2 k} \frac{\partial U_{\tau}}{\partial k} \right]^{-1}$$



Particle production channels in the LQMD model

π and resonances ($\Delta(1232)$, $N^*(1440)$, $N^*(1535)$, ...) production:

$$NN \leftrightarrow N\Delta, \quad NN \leftrightarrow NN^*, \quad NN \leftrightarrow \Delta\Delta, \quad \Delta \leftrightarrow N\pi, \\ N^* \leftrightarrow N\pi, \quad NN \leftrightarrow NN\pi(s - \text{state}), \quad N^*(1535) \leftrightarrow N\eta$$

Collisions between resonances,

$$NN^* \leftrightarrow N\Delta, \quad NN^* \leftrightarrow NN^*$$

Strangeness channels:

$$BB \rightarrow BYK, \quad BB \rightarrow BBK\bar{K}, \quad B\pi \rightarrow YK, \\ B\pi \rightarrow NK\bar{K}, \quad Y\pi \rightarrow N\bar{K}, \quad N\bar{K} \rightarrow Y\pi, \quad YN \rightarrow \bar{K}NN$$

Reaction channels with antiproton:

$$\bar{p}N \rightarrow \bar{N}N, \quad \boxed{\bar{N}N \rightarrow \bar{N}N, \bar{N}N \rightarrow \bar{B}B, \bar{N}N \rightarrow \bar{Y}Y} \\ \boxed{\bar{N}N \rightarrow \text{annihilation}(\pi, \eta, \rho, \omega, K, \bar{K}, K^*, \bar{K}^*, \phi)}$$

Statistical model with SU(3)

symmetry for annihilation

(E.S. Golubeva et al., Nucl. Phys. A 537, 393 (1992))

The **PYTHIA** and **FRITIOF** code are used for baryon(meson)-baryon and antibaryon-baryon collisions at high invariant energies

Mean-field potentials for resonances, hyperons and mesons

1. Mean-field potentials for resonances ($\Delta(1232)$, $N^*(1440)$, ...) are considered based on nucleon potentials, but distinguishing isospin effect.

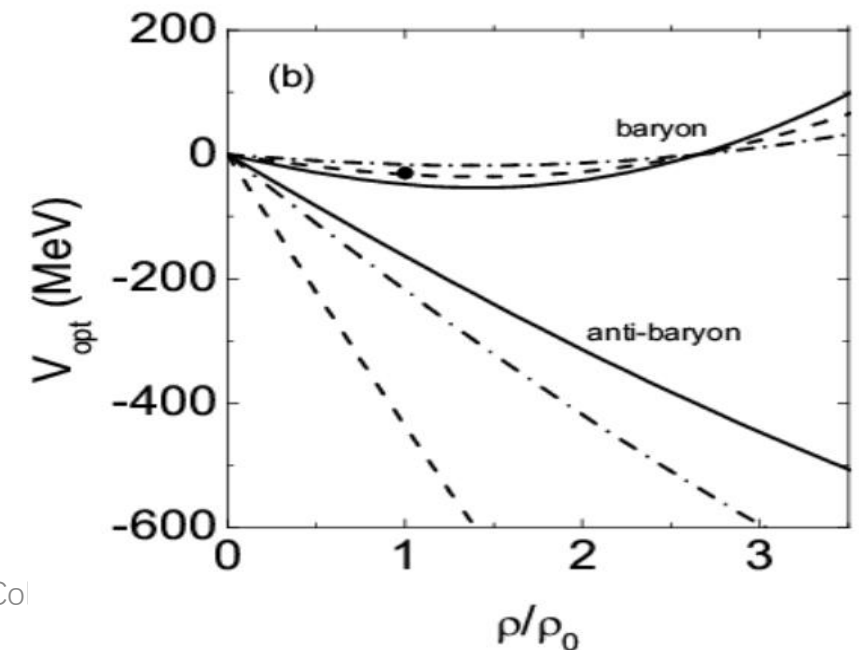
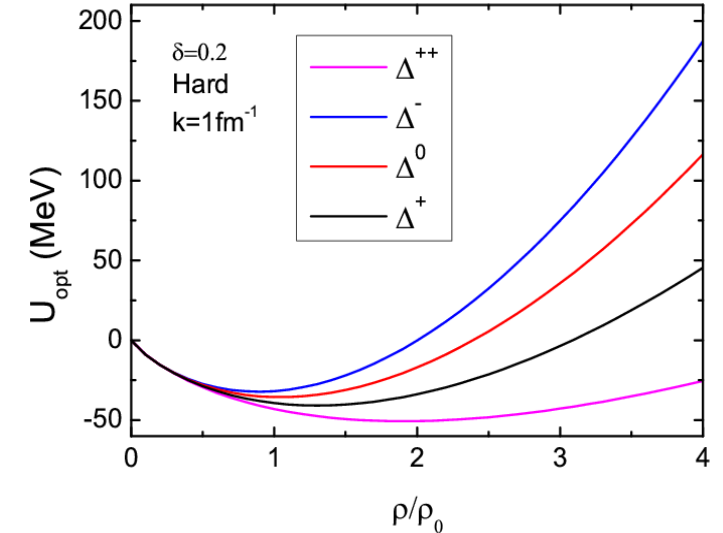
$$U_{\Delta^{++}} = U_p(\rho, \mathbf{p}), U_{\Delta^+} = 2U_p(\rho, \mathbf{p})/3 + U_n(\rho, \mathbf{p})/3, U_{\Delta^0} = U_p(\rho, \mathbf{p})/3 + 2U_n(\rho, \mathbf{p})/3, U_{\Delta^-} = U_n(\rho, \mathbf{p})$$

2. Mean-field potentials for hyperons and antiprotons in nuclear medium

$$H_M = \sum_{i=1}^{N_M} (V_i^{\text{Coul}} + \omega(\mathbf{p}_i, \rho_i))$$

$$\omega(\mathbf{p}_i, \rho_i) = \sqrt{(m_H + \Sigma_S^H)^2 + \mathbf{p}_i^2} + \Sigma_V^H$$

$$V_{opt}(\mathbf{p}, \rho) = \omega(\mathbf{p}, \rho) - \sqrt{\mathbf{p}^2 + m^2}$$



3. Mean-field potentials for pion dynamics

ZQF et al, PRC92, 044604 (2015)

$$\omega_{\tau_z}(\rho, \vec{p}) = \omega_{isoscalar}(\rho, \vec{p}) + C_{iso}^{\pi} \tau_z \delta \left(\frac{\rho}{\rho_0} \right)^{\gamma_{\pi}}$$

$\tau_z=1, 0, -1$ for π^- , π^0 and π^+

$$\omega_{isoscalar}(\mathbf{p}_i, \rho_i) = S_{\pi}(\mathbf{p}_i, \rho_i) \omega_{\pi\text{-like}}(\mathbf{p}_i, \rho_i) + S_{\Delta}(\mathbf{p}_i, \rho_i) \omega_{\Delta\text{-like}}(\mathbf{p}_i, \rho_i)$$

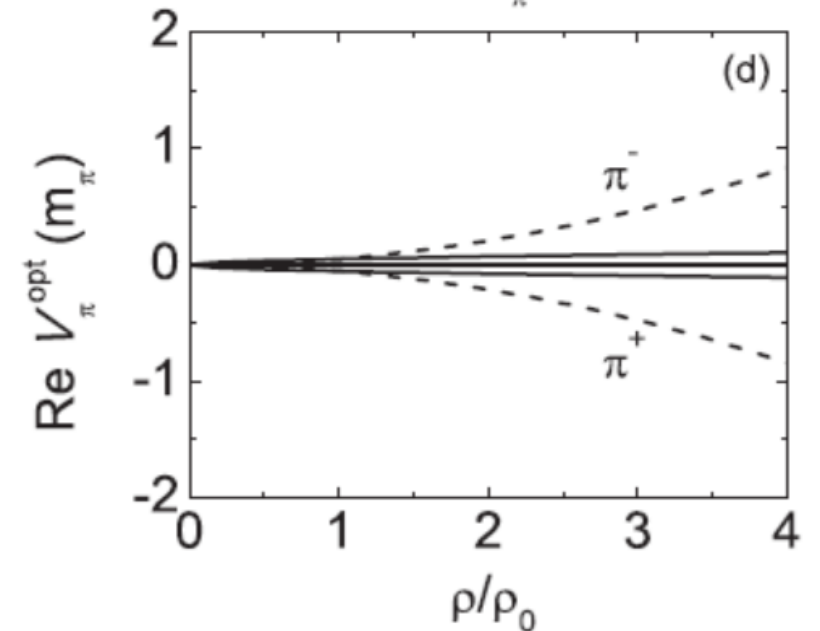
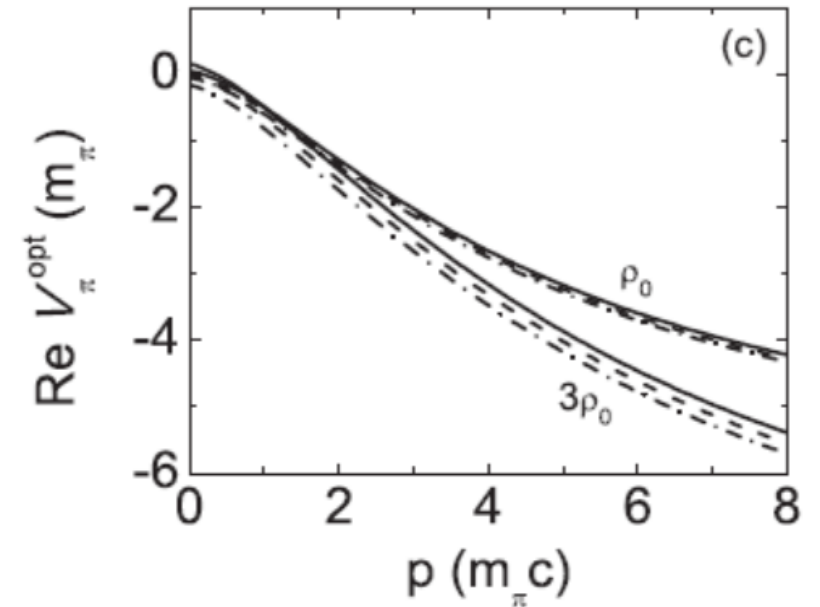
$$S_{\pi}(\mathbf{p}_i, \rho_i) + S_{\Delta}(\mathbf{p}_i, \rho_i) = 1$$

$$S(\mathbf{p}_i, \rho_i) = \frac{1}{1 - \partial \Pi(\omega) / \partial \omega^2}$$

Details in PRC47 (1993) 788, 55 (1997) 411

The energy balance in the decay of resonance

$$\sqrt{m_R^2 + \mathbf{p}_R^2} = \sqrt{m_N^2 + (\mathbf{p}_R - \mathbf{p}_{\pi})^2} + \omega_{\pi}(\mathbf{p}_{\pi}, \rho)$$

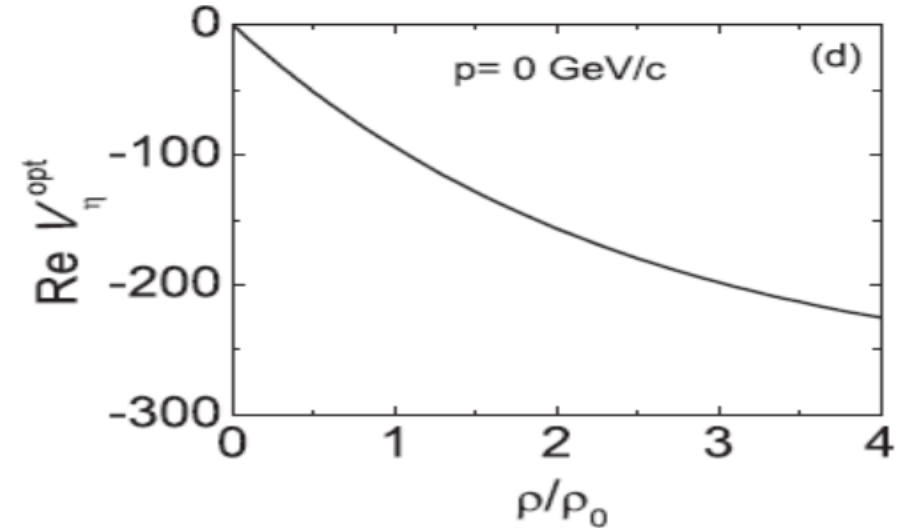
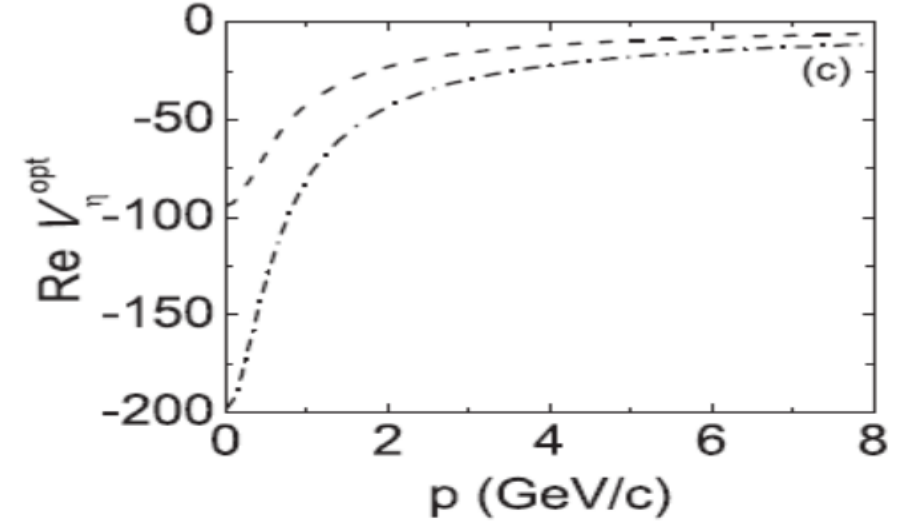
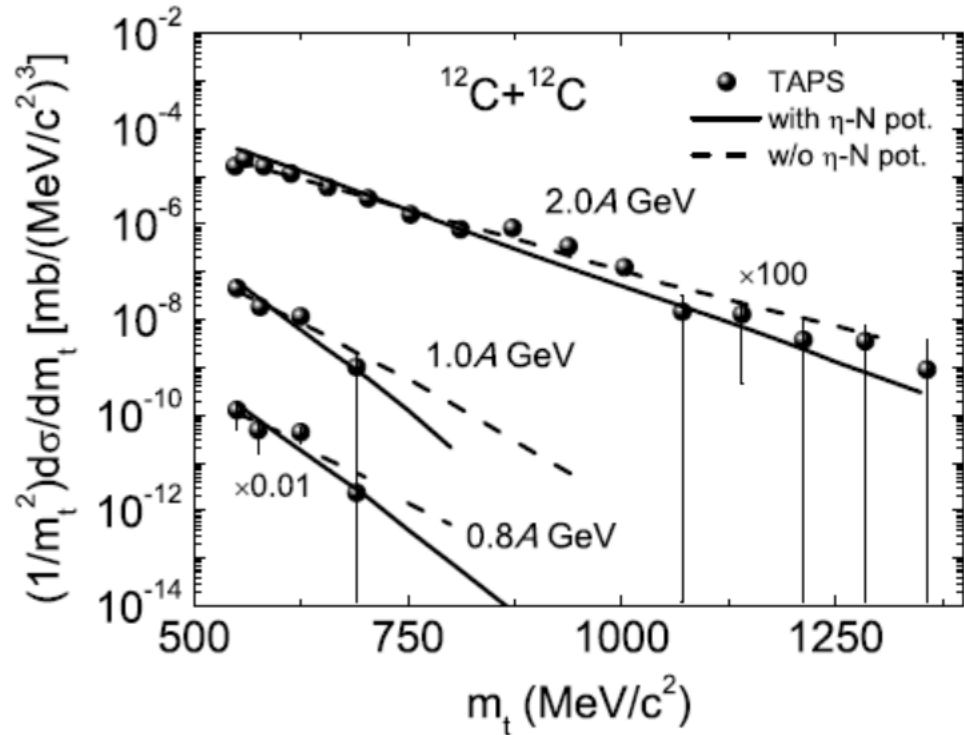


4. Mean-field potentials for η transport (J. Chen, Z. Q. Feng et al., Eur. Phys. J. A (2017) 53: 128)

$$\omega_\eta = \sqrt{\left(m_\eta^2 - \frac{\Sigma_{\eta N}}{f^2} \rho_s\right) \left(1 + \frac{\kappa}{f^2} \rho_s\right)^{-1} + p^2}$$

$$V_\eta^{\text{opt}} = \omega_\eta^*(\mathbf{p}_i, \rho_i) - \omega_\eta(\mathbf{p}_i, \rho_i)$$

$$= \sqrt{(m_\eta^*)^2 + \mathbf{p}_i^2} - \sqrt{m_\eta^2 + \mathbf{p}_i^2}$$



5. Mean-field potentials for kaons and antikaons

J.Schaffner-Bielich et al., Nucl. Phys. A 625 (1997) 325, Z. Q. Feng, Nucl. Phys. A 919 (2013) 32-45

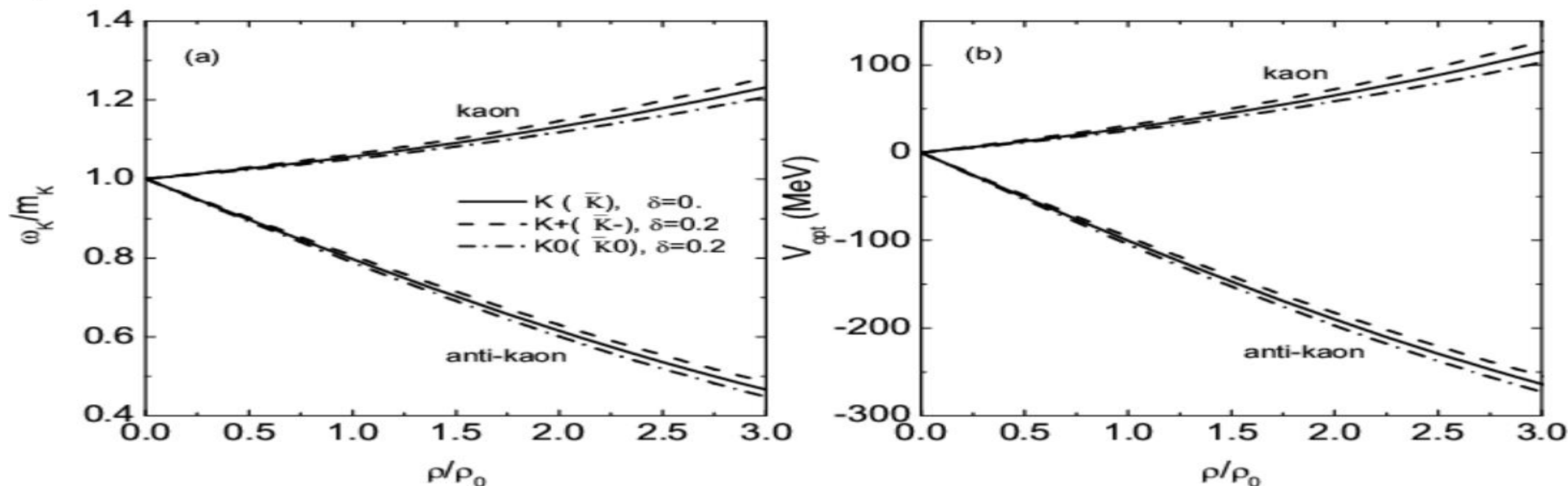
$$\omega_K(\mathbf{p}_i, \rho_i) = \left[m_K^2 + \mathbf{p}_i^2 - a_K \rho_i^S - \tau_3 c_K \rho_{i3}^S + (b_K \rho_i + \tau_3 d_K \rho_{i3})^2 \right]^{1/2} + b_K \rho_i + \tau_3 d_K \rho_{i3}$$

$$\omega_{\bar{K}}(\mathbf{p}_i, \rho_i) = \left[m_{\bar{K}}^2 + \mathbf{p}_i^2 - a_{\bar{K}} \rho_i^S - \tau_3 c_K \rho_{i3}^S + (b_K \rho_i + \tau_3 d_K \rho_{i3})^2 \right]^{1/2} - b_K \rho_i - \tau_3 d_K \rho_{i3}$$

$b_K = 3/(8f_\pi^{*2}) \approx 0.333 \text{ GeV fm}^3$ with assuming $f_\pi^* = f_\pi$, the a_K and $a_{\bar{K}}$ are $0.18 \text{ GeV}^2 \text{ fm}^3$ and $0.31 \text{ GeV}^2 \text{ fm}^3$, respectively,

The parameters $c_K = 0.0298 \text{ GeV}^2 \text{ fm}^3$ and $d_K = 0.111 \text{ GeV fm}^3$

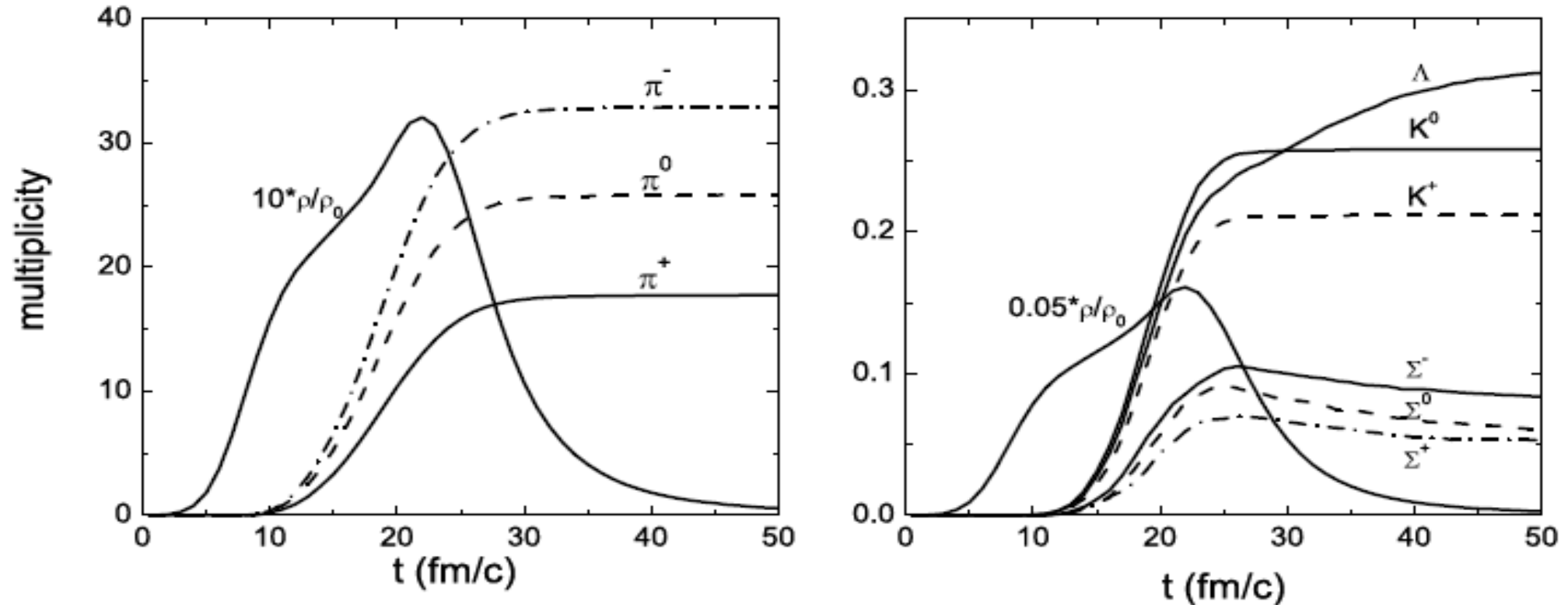
$$\frac{d\mathbf{p}_i}{dt} = -\frac{\partial V_i^{\text{Coul}}}{\partial \mathbf{r}_i} - \frac{\partial \omega_{K(\bar{K})}(\mathbf{p}_i, \rho_i)}{\partial \mathbf{r}_i} \pm \mathbf{v}_i \frac{\partial \mathbf{V}_i}{\partial \mathbf{r}_i}$$



$$V_{K^+}(\rho_0) = 28 \text{ MeV}, \quad V_{K^-}(\rho_0) = -100 \text{ MeV}$$

III. (1) Particle production in HICs

Particle production π , K, Λ and Σ in the reaction $^{197}\text{Au}+^{197}\text{Au}$ at 1.5A GeV (Phys. Rev. C 82 (2010) 057901)



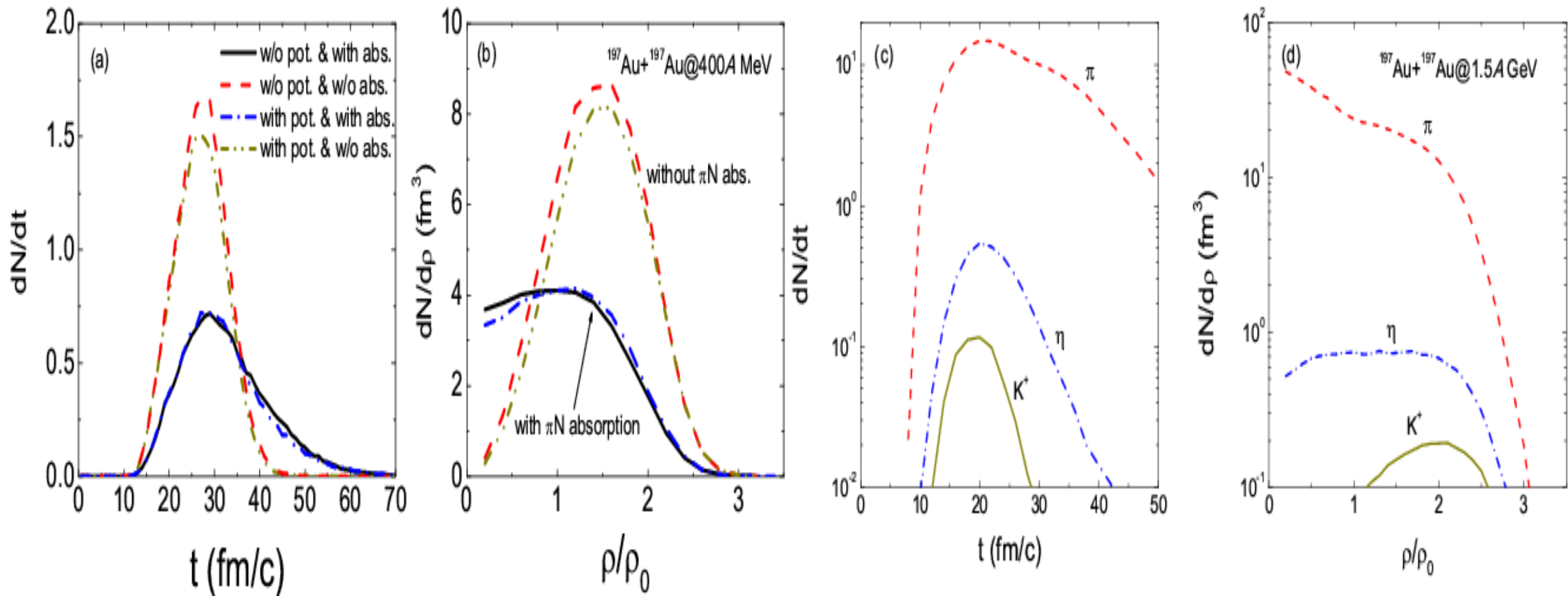
In-medium modifications on elementary cross section via effective mass, e.g., $\pi N \rightarrow KY$

$$\sqrt{s_{th}} = m_Y^* + m_K^*$$

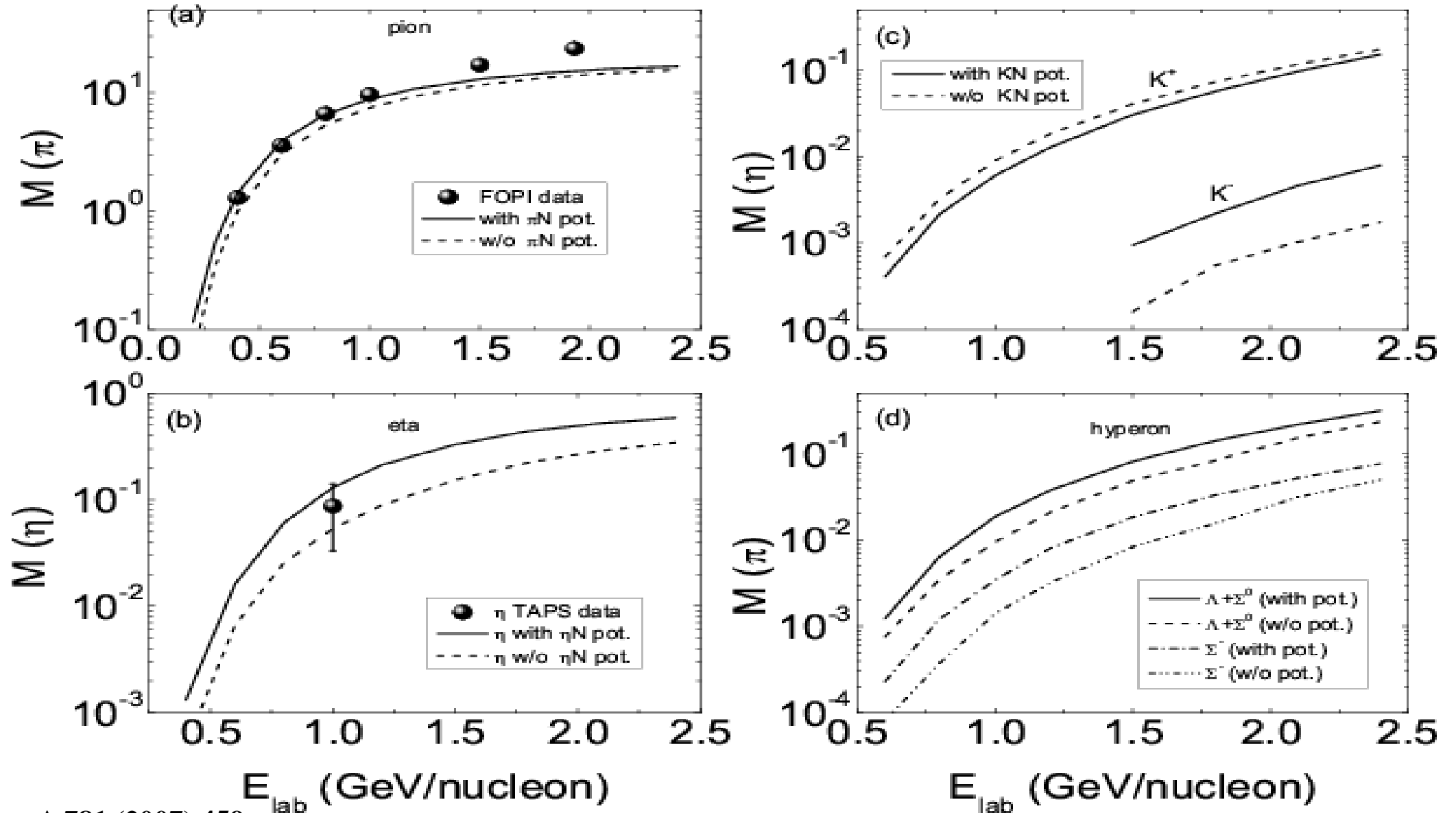
Threshold energies for $E_{th}(\pi^0) = 0.28$ GeV, $E_{th}(\eta) = 1.25$ GeV, $E_{th}(K^+) = 1.58$ GeV, $E_{th}(K^-) = 2.5$ GeV

Temporal evolution of production rate and density profiles of particles in collisions of $^{197}\text{Au}+^{197}\text{Au}$

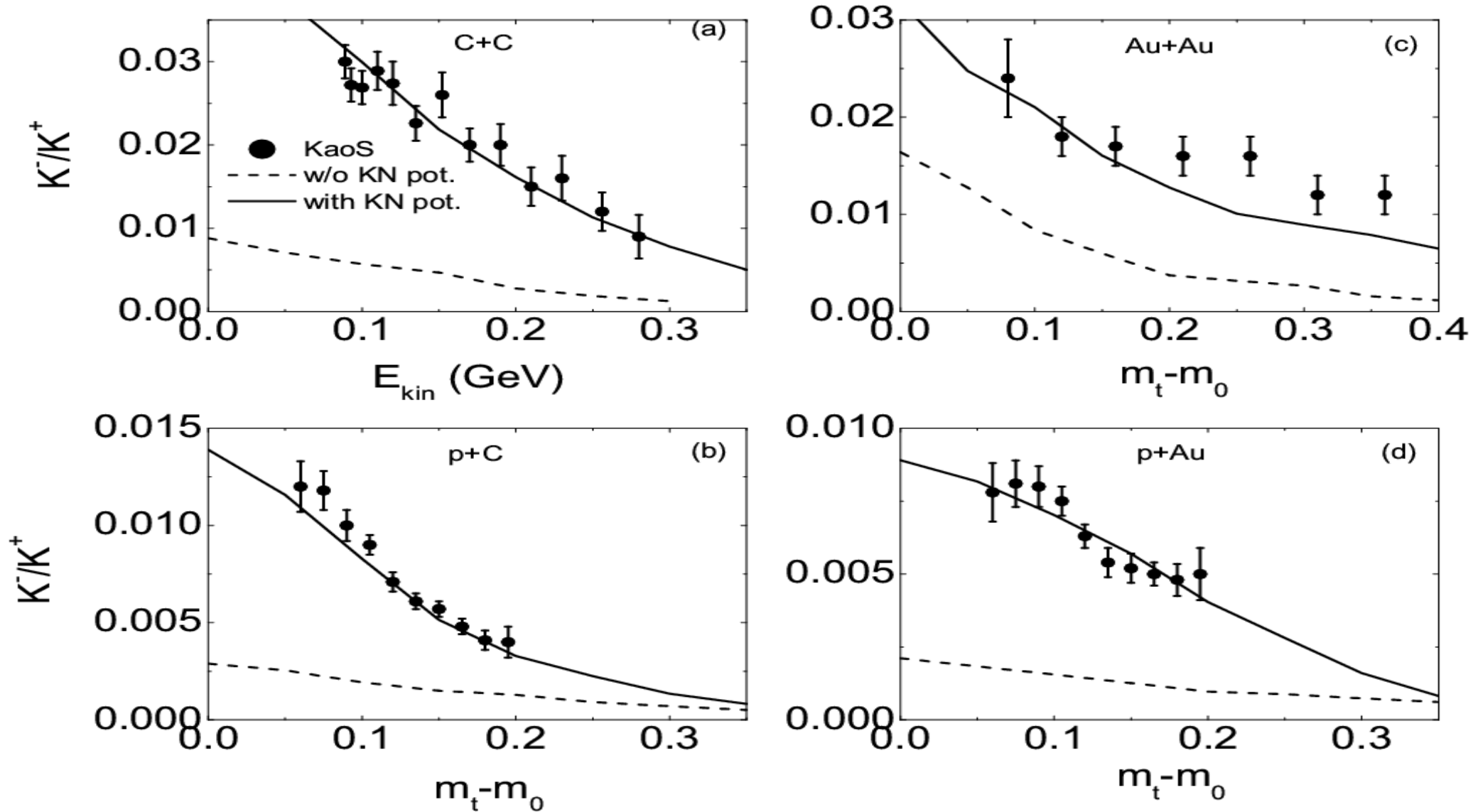
Nucl. Sci. Tech. 29, 40 (2018)



Production of neutral particles in central $^{40}\text{Ca} + ^{40}\text{Ca}$ collisions



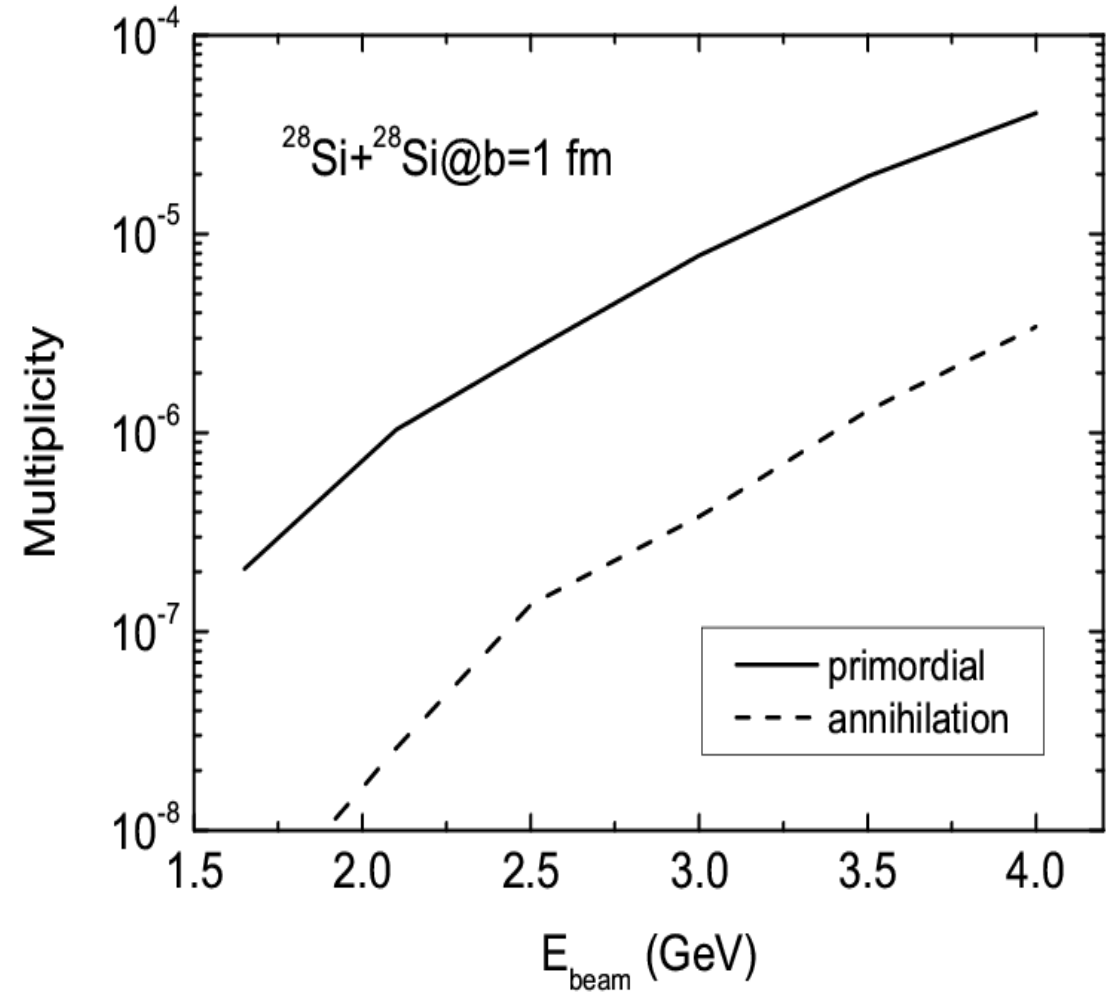
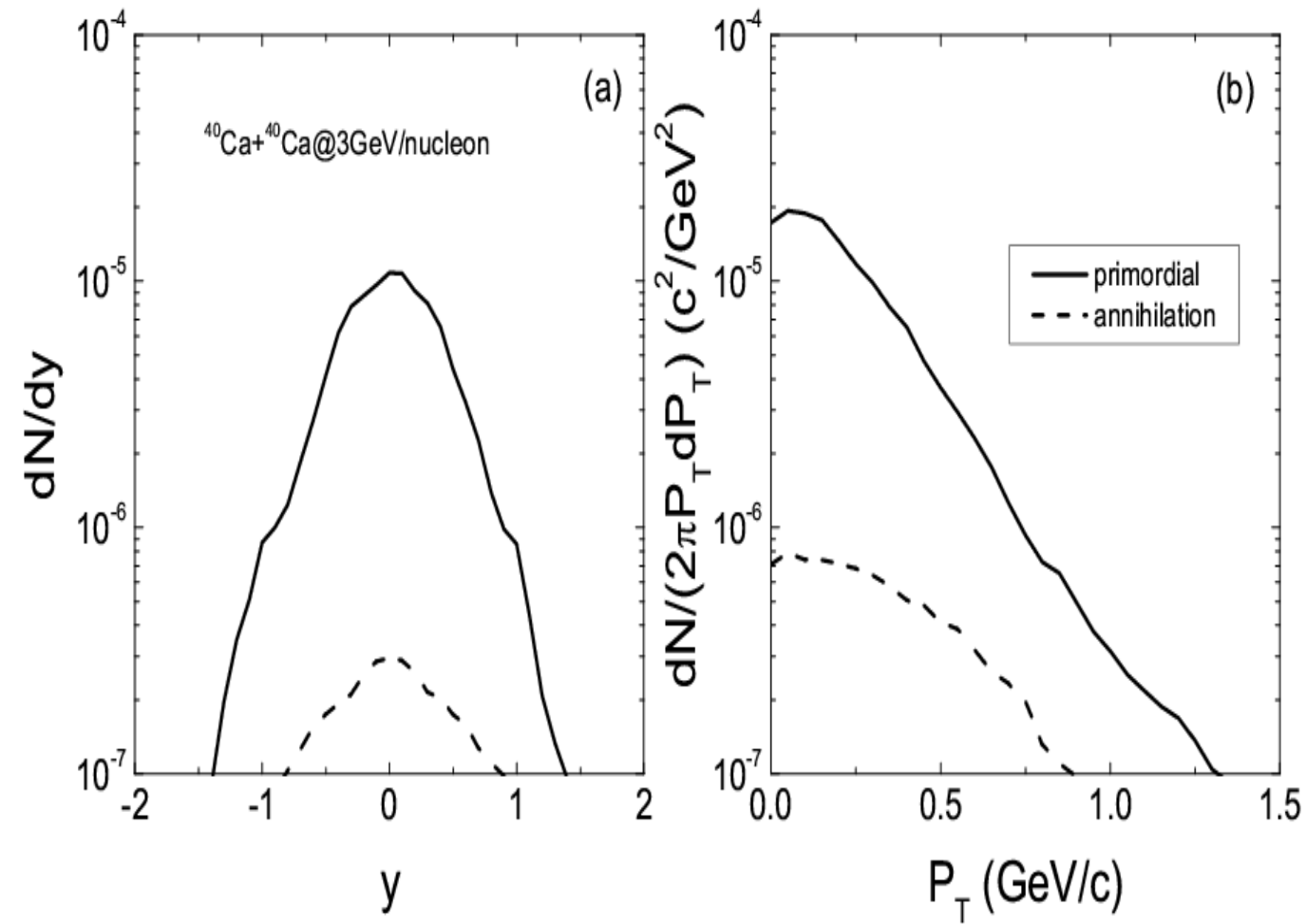
The ratio of K^-/K^+ as a function of transverse mass (kinetic energy) in collisions of $^{12}\text{C} + ^{12}\text{C}$ and protons on ^{12}C and ^{197}Au at the beam energies of 1.8A GeV and 2.5 GeV, respectively.



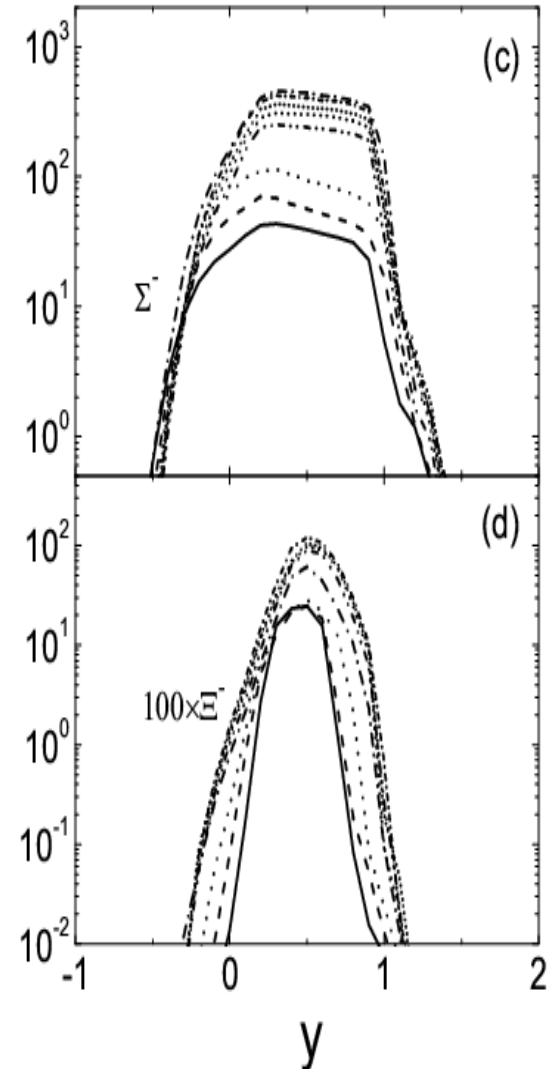
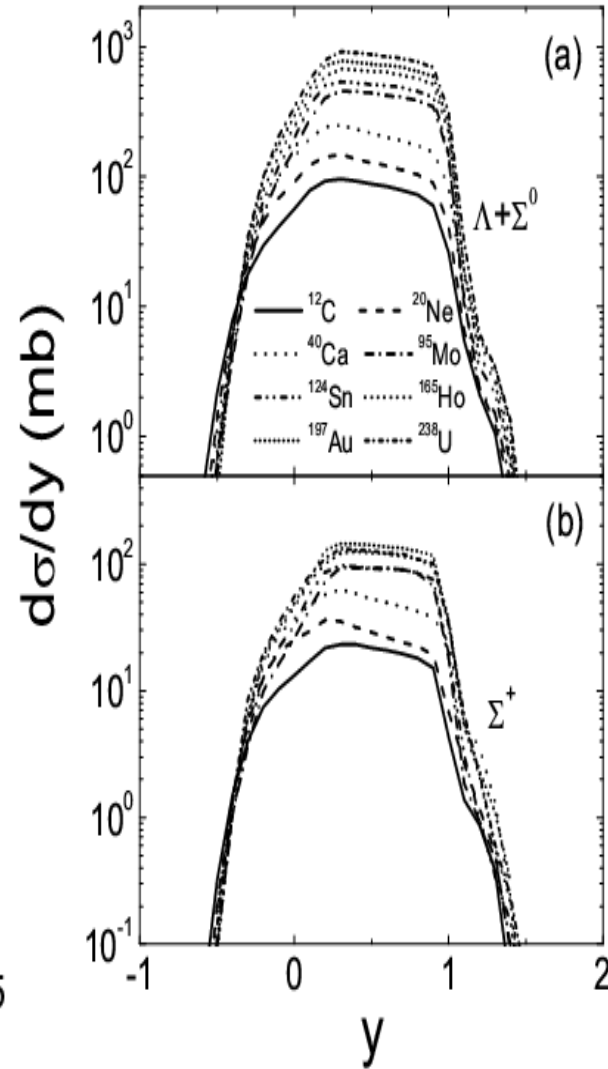
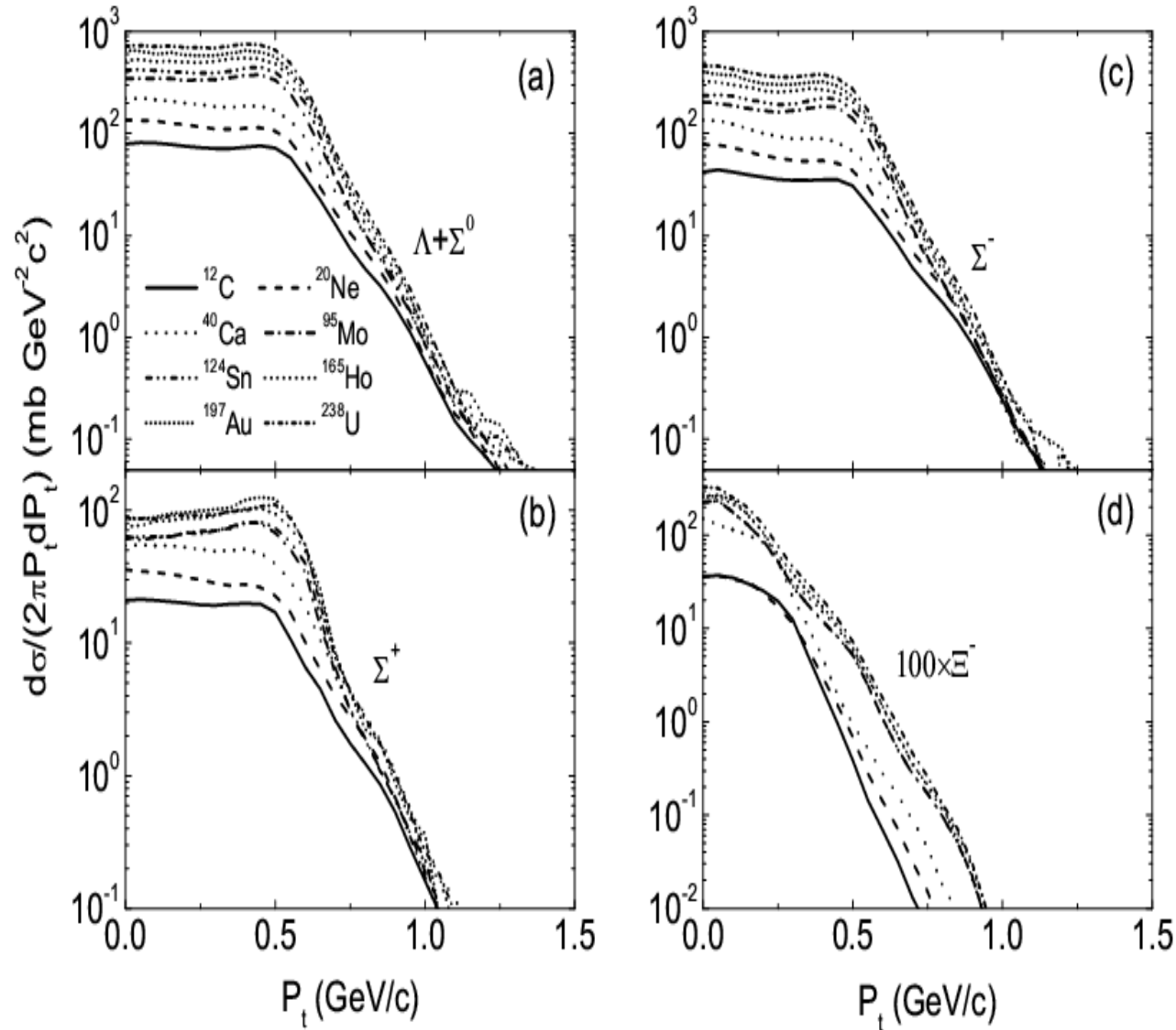
$$V_{K^+}(\rho_0) = 28 \text{ MeV}, \quad V_{K^-}(\rho_0) = -100 \text{ MeV}$$

Antiproton production in HICs

$$E_{\text{th}}(\bar{p}) = 5.62 \text{ GeV}$$

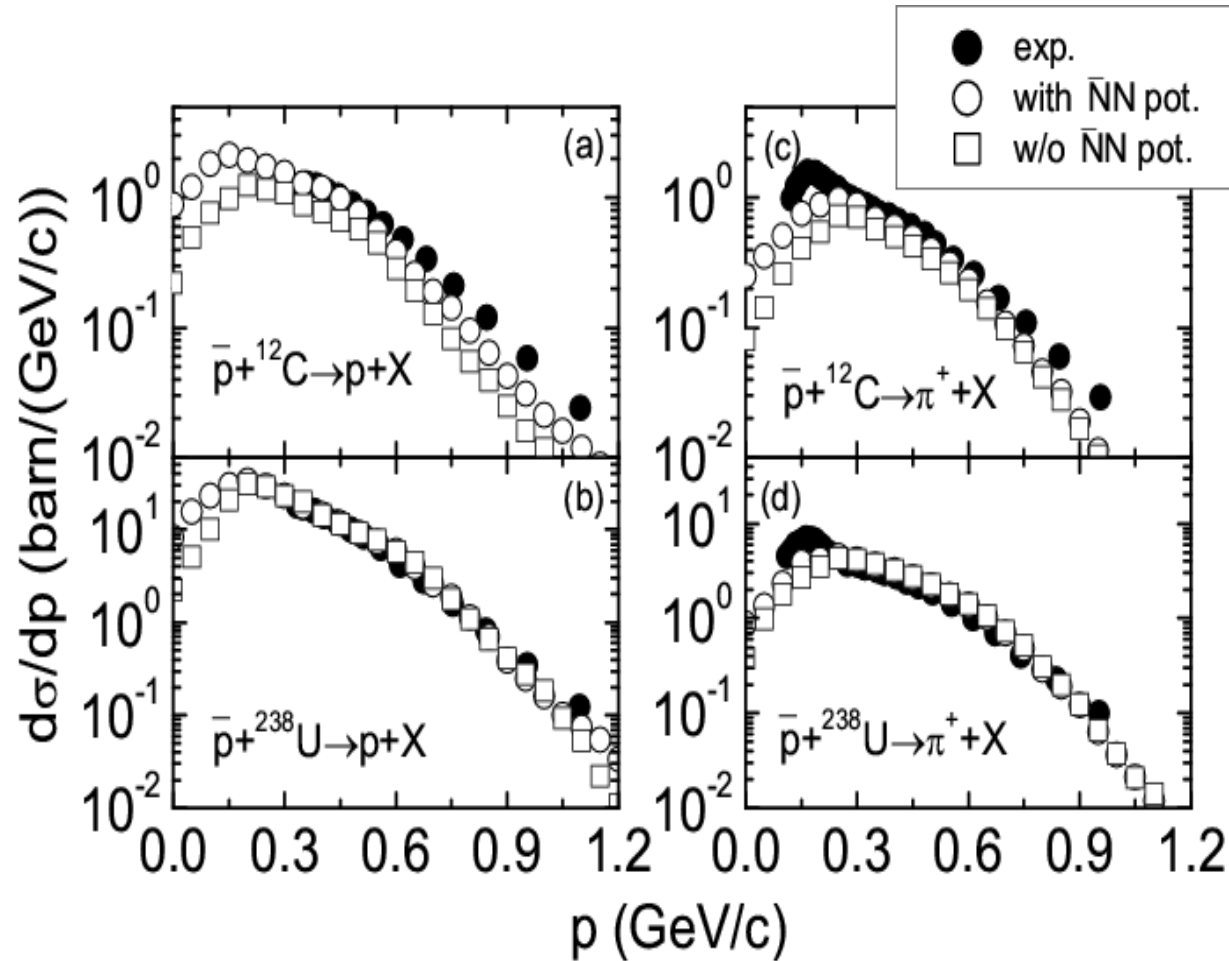


III. (2) K⁻ induced nuclear reactions

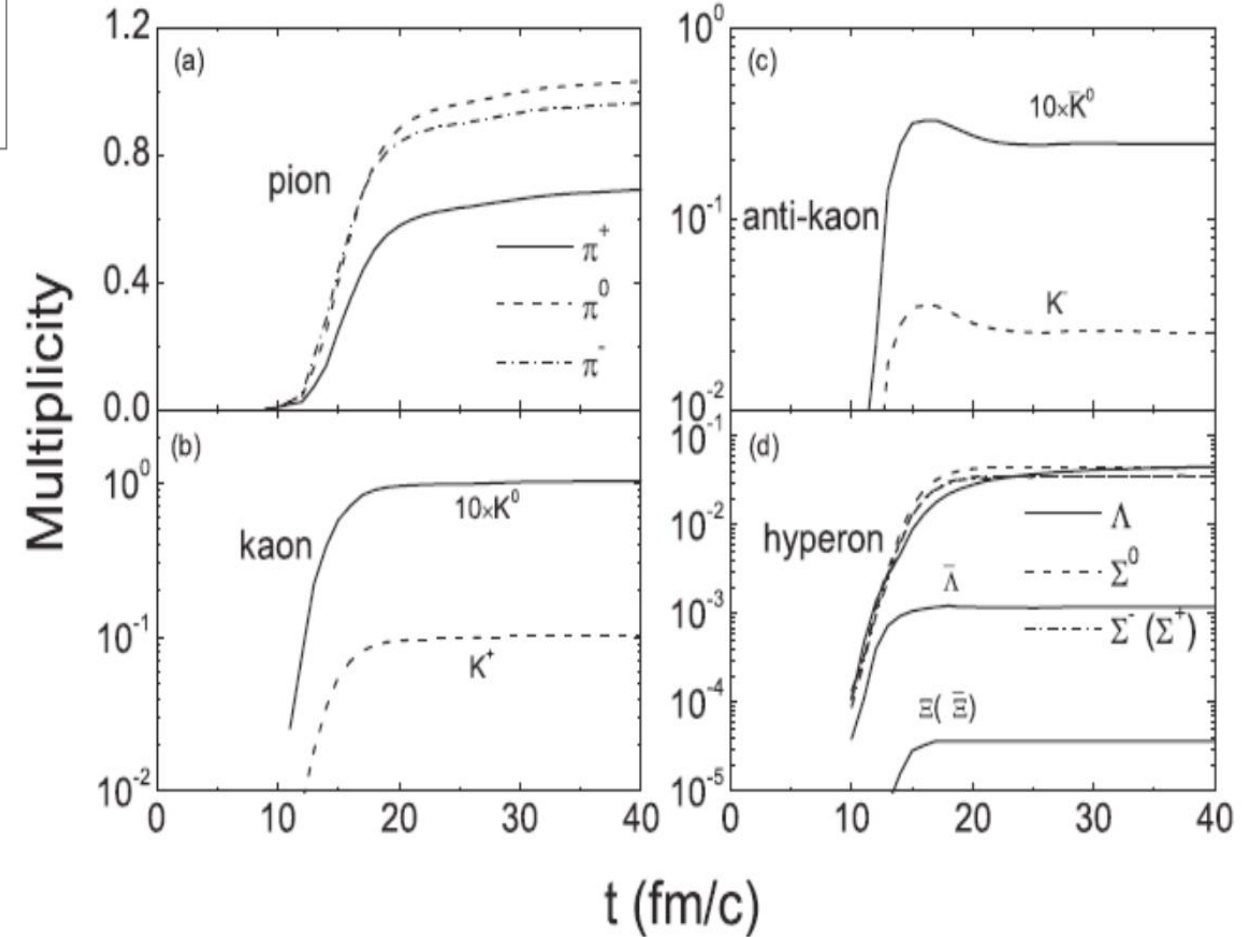


III. (3) antiproton induced reactions

Z. Q. Feng and H. Lenske, Phys. Rev. C 89, 044617 (2014)



$\bar{p} + {}^{40}\text{Ca}, 4 \text{ GeV/c}$

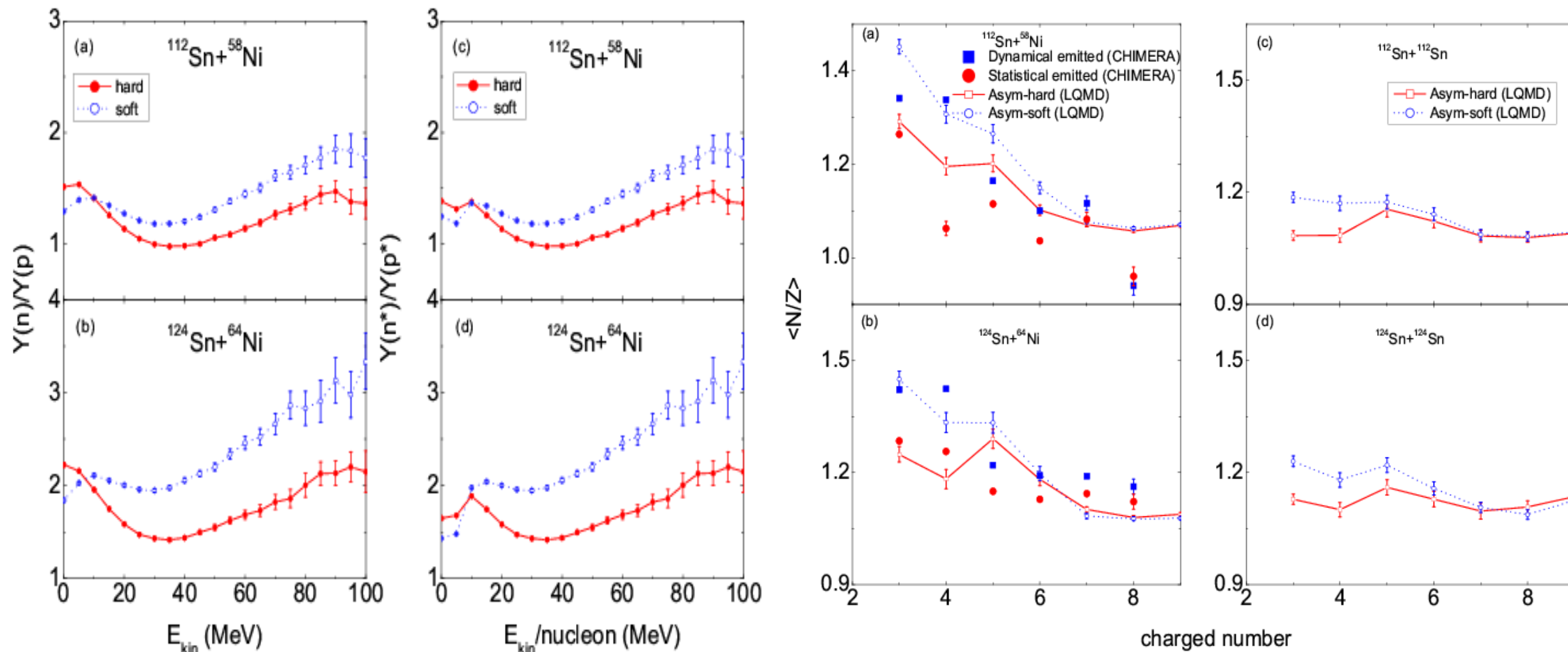


LEAR (Low-Energy Antiproton Ring) at CERN (P. L. McGaughey et al., Phys. Rev. Lett. 56, 2156 (1986))

III. (4) Isospin effects in HICs

Zhao-Qing Feng, Phys. Rev. C 94, 014609 (2016)

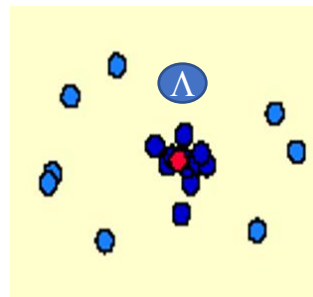
The yields of free nucleons and 'gas-phase' nucleons (nucleons, hydrogen and helium isotopes) from the neck fragmentations at the fermi energy of 35 MeV/nucleon within the collision centralities of 6-8 fm



III. (5) Hypernuclear formation in HICs

Classical coalescence approach

The rapidity and kinetic energy distributions of nucleonic fragments, Λ -hypernucleide fragments and free hyperons

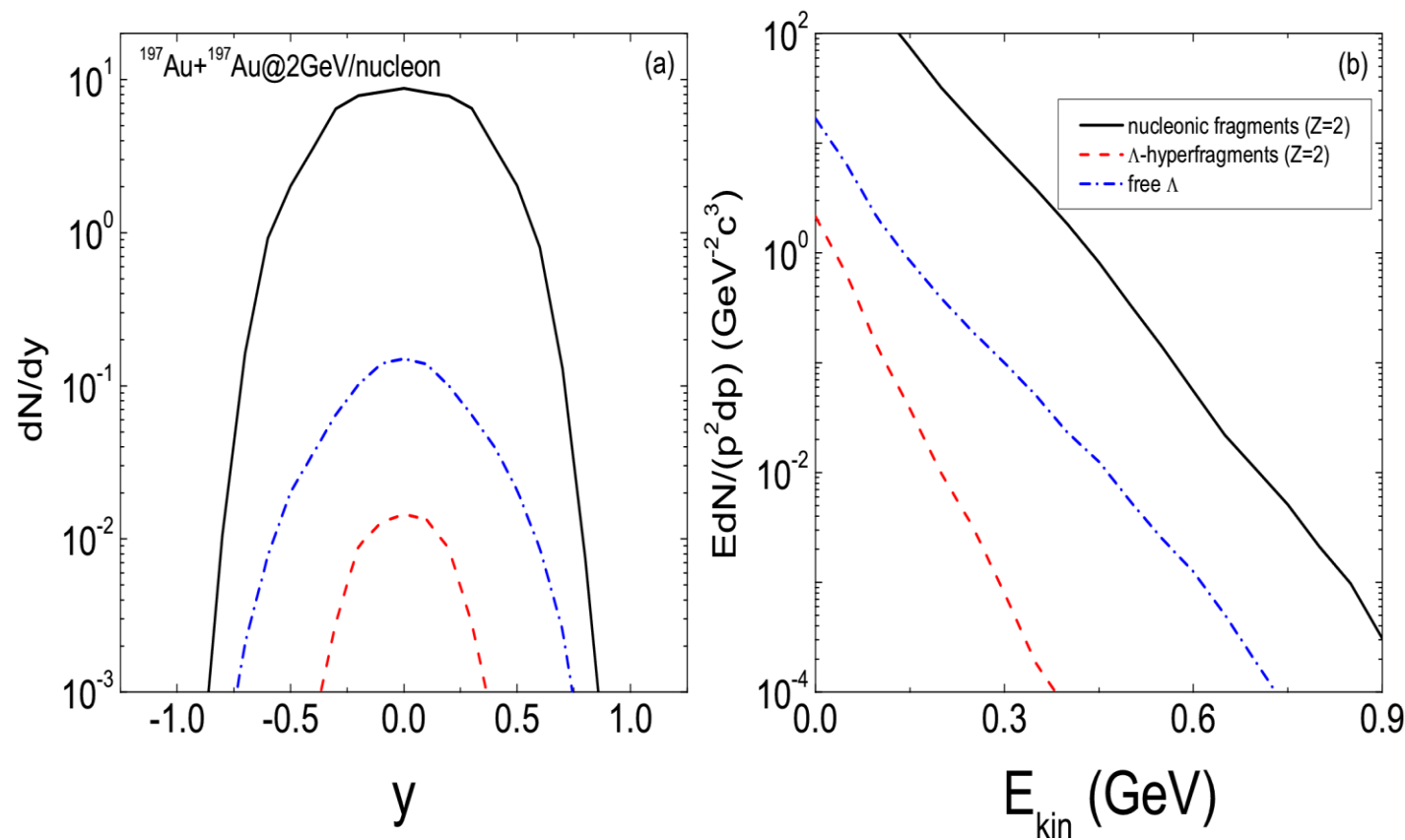
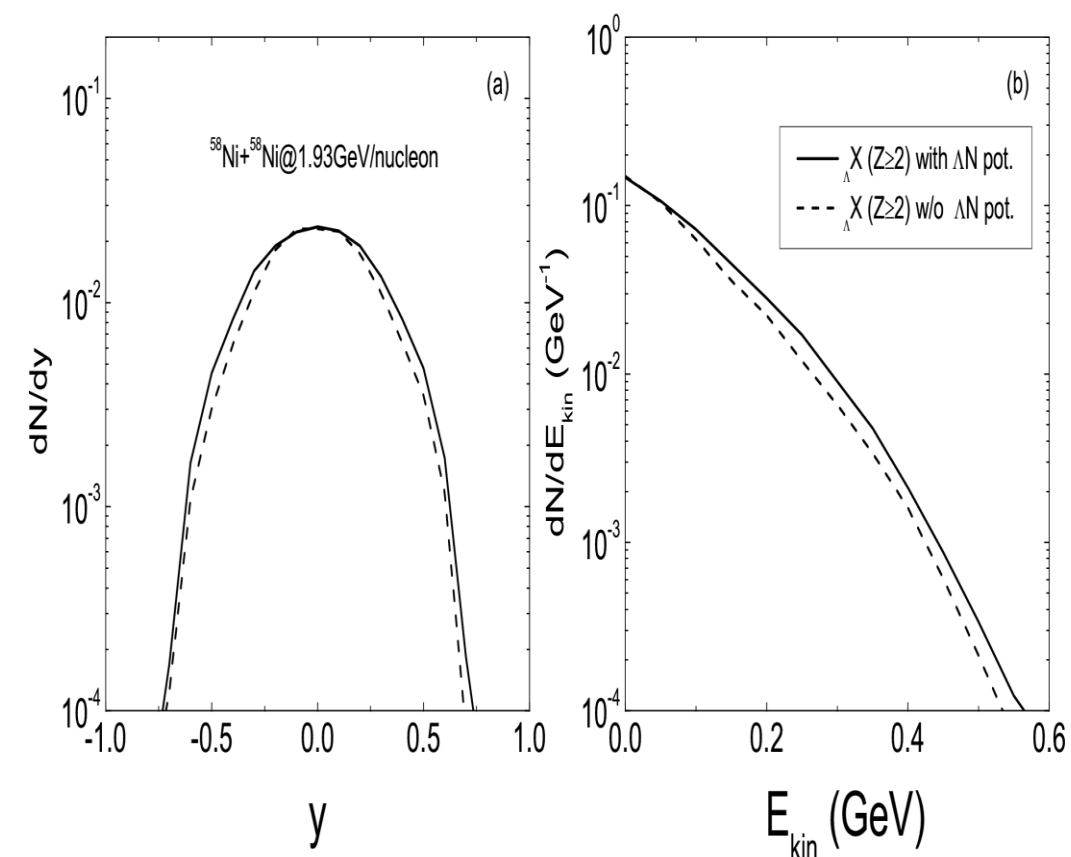


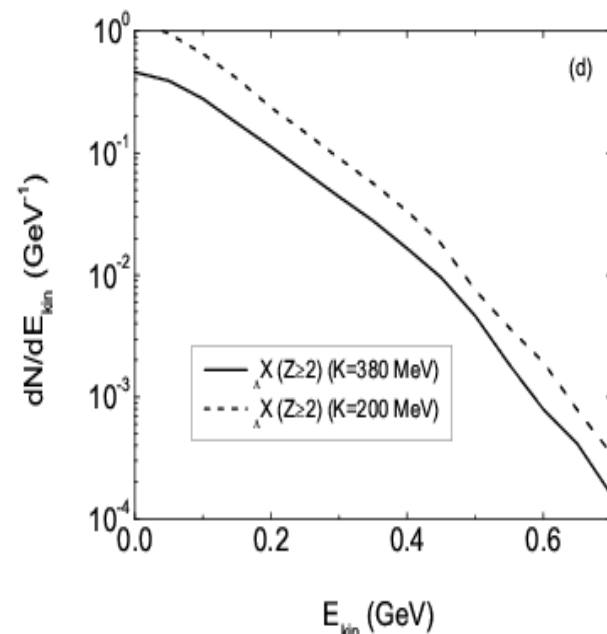
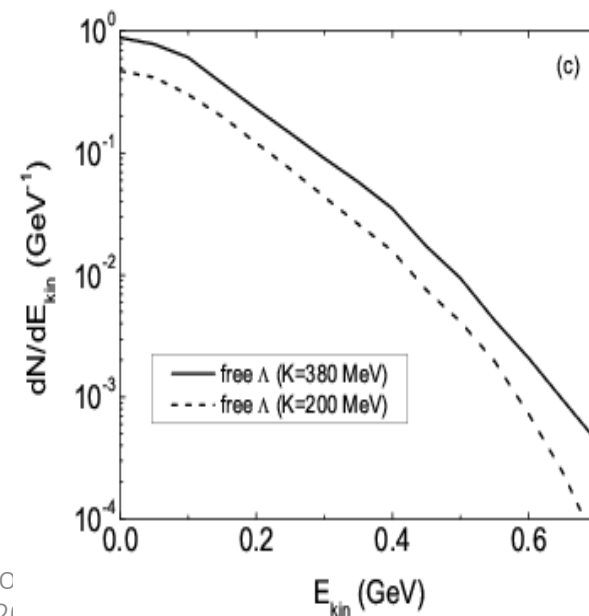
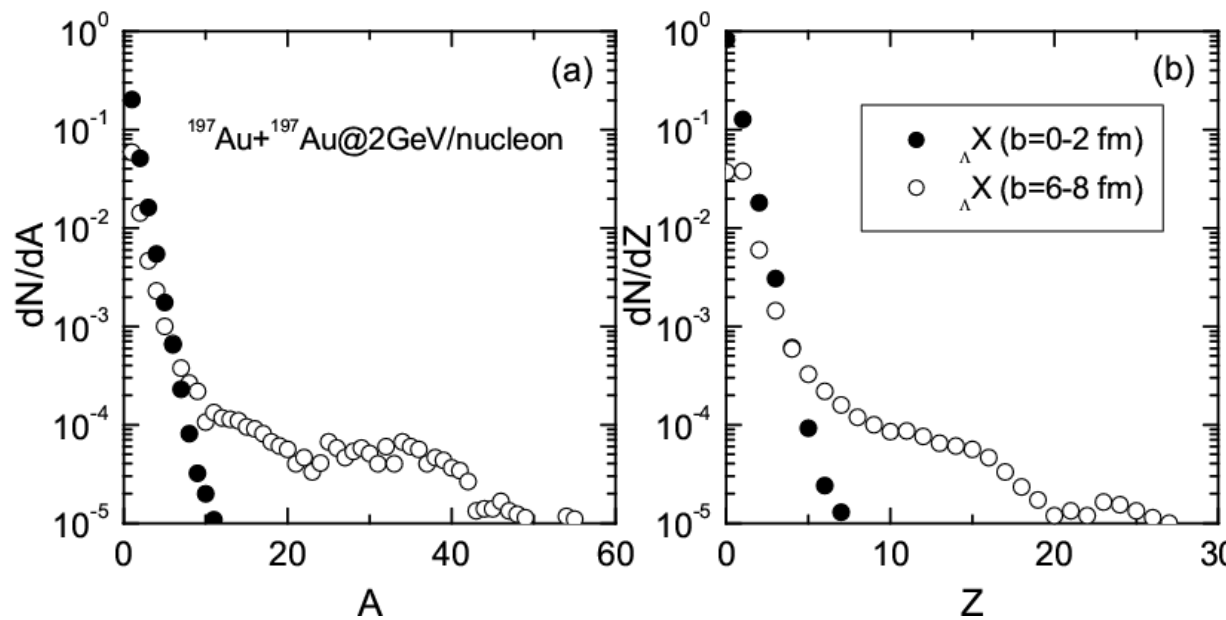
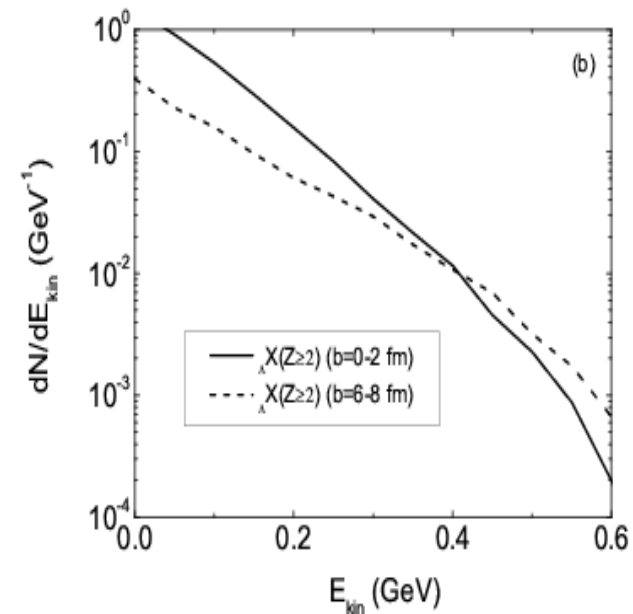
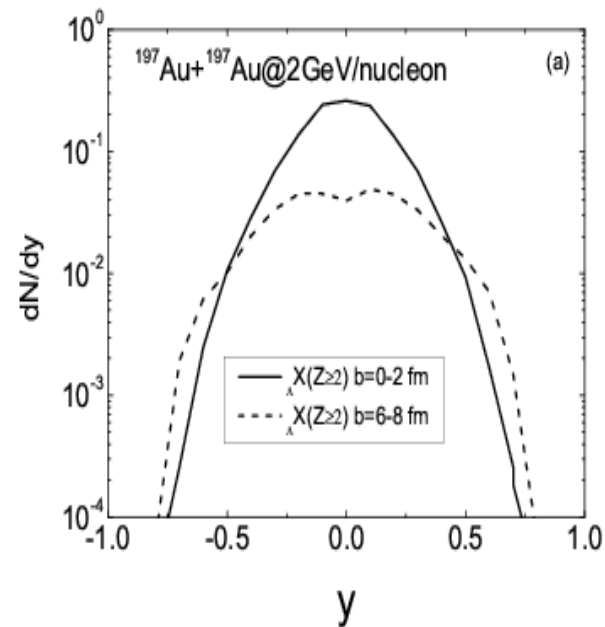
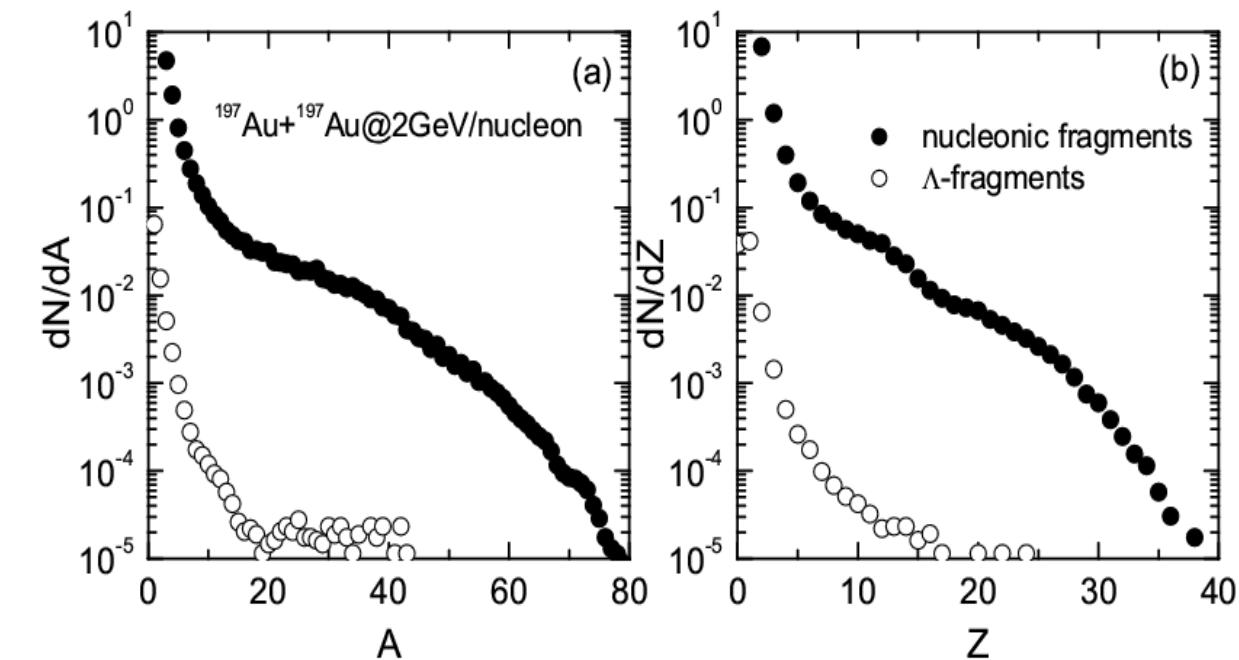
中高能重离子碰撞中奇异粒子产生和超核形成机制

冯兆庆

中国科学院近代物理研究所, 兰州 730000

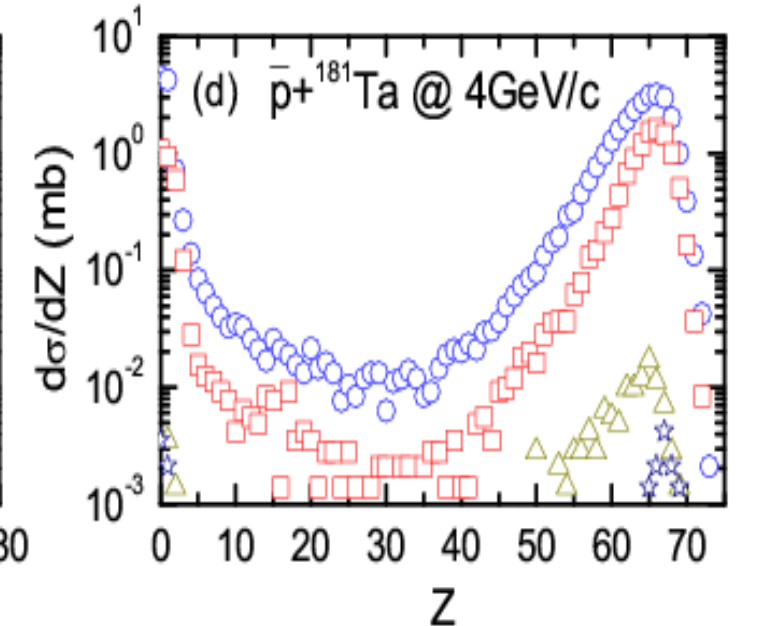
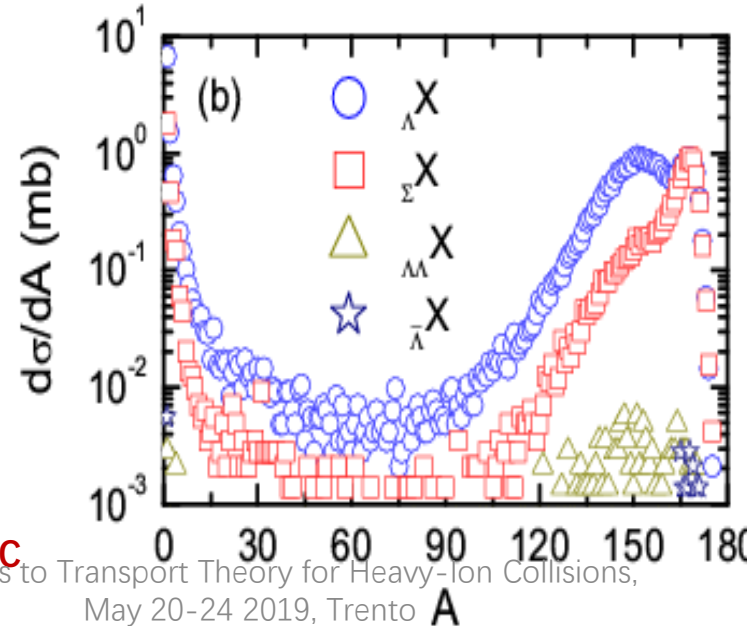
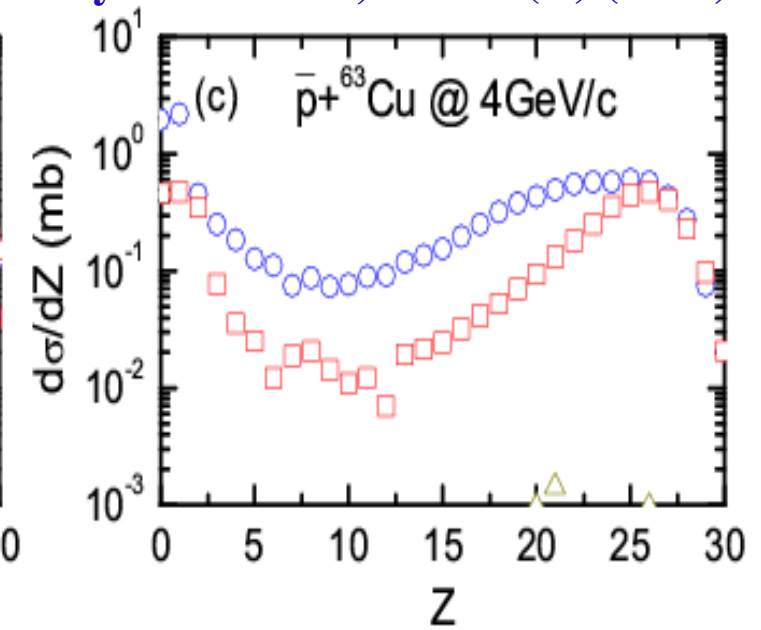
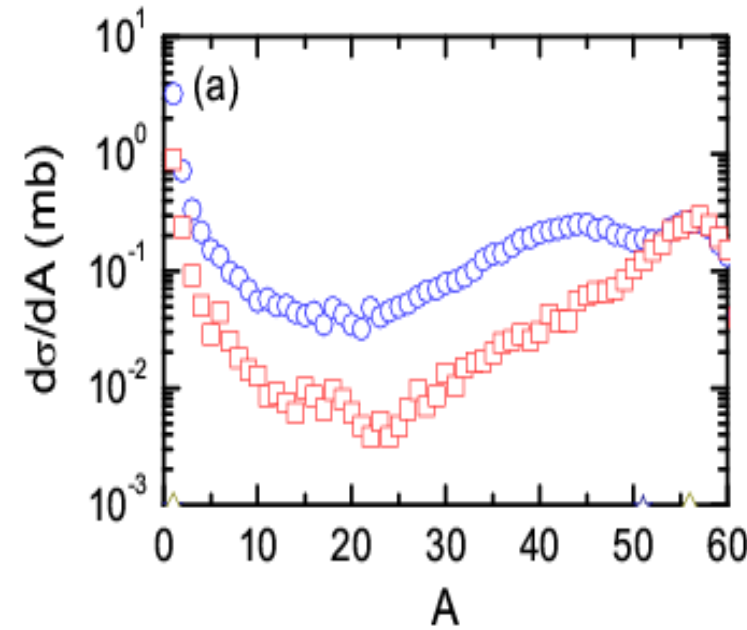
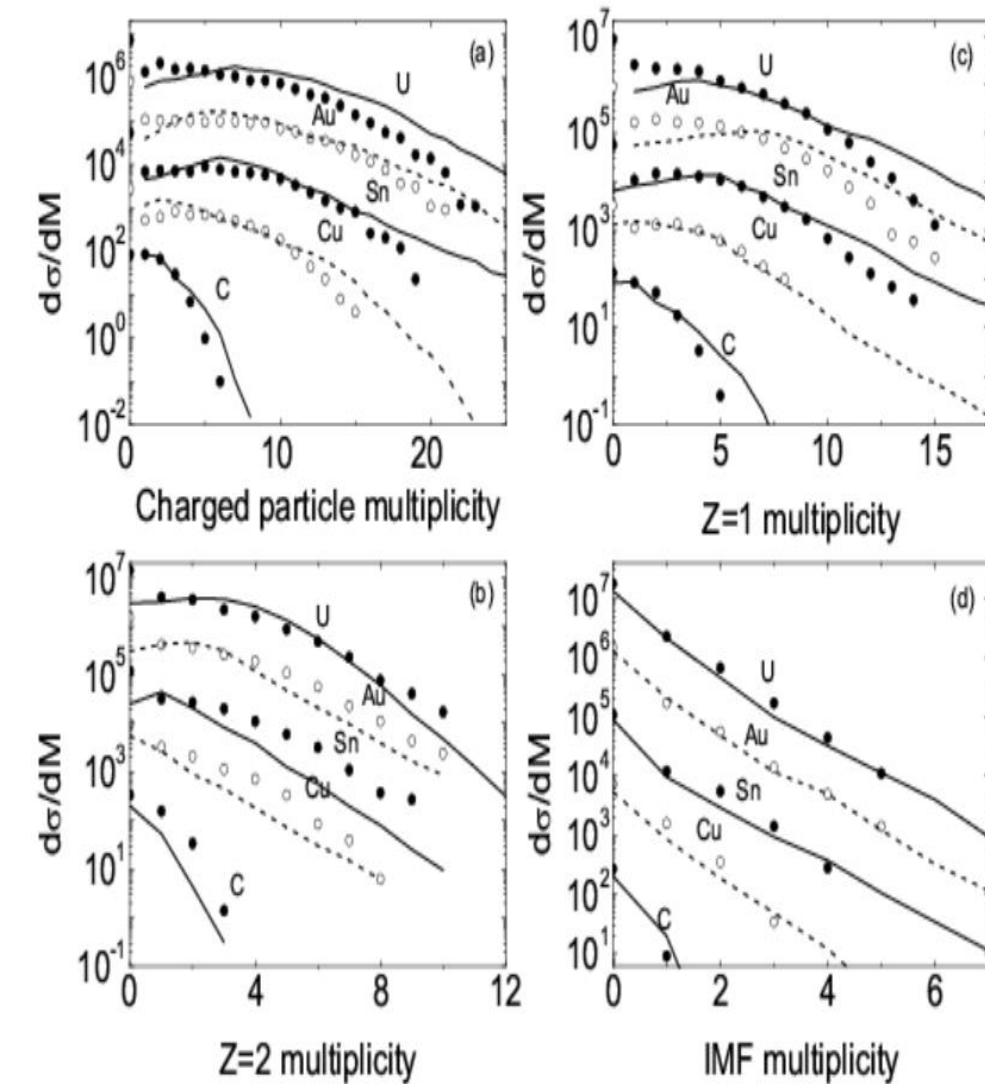
E-mail: fengzhq@impcas.ac.cn





III. (6) Hypernuclear formation in antiproton induced reactions

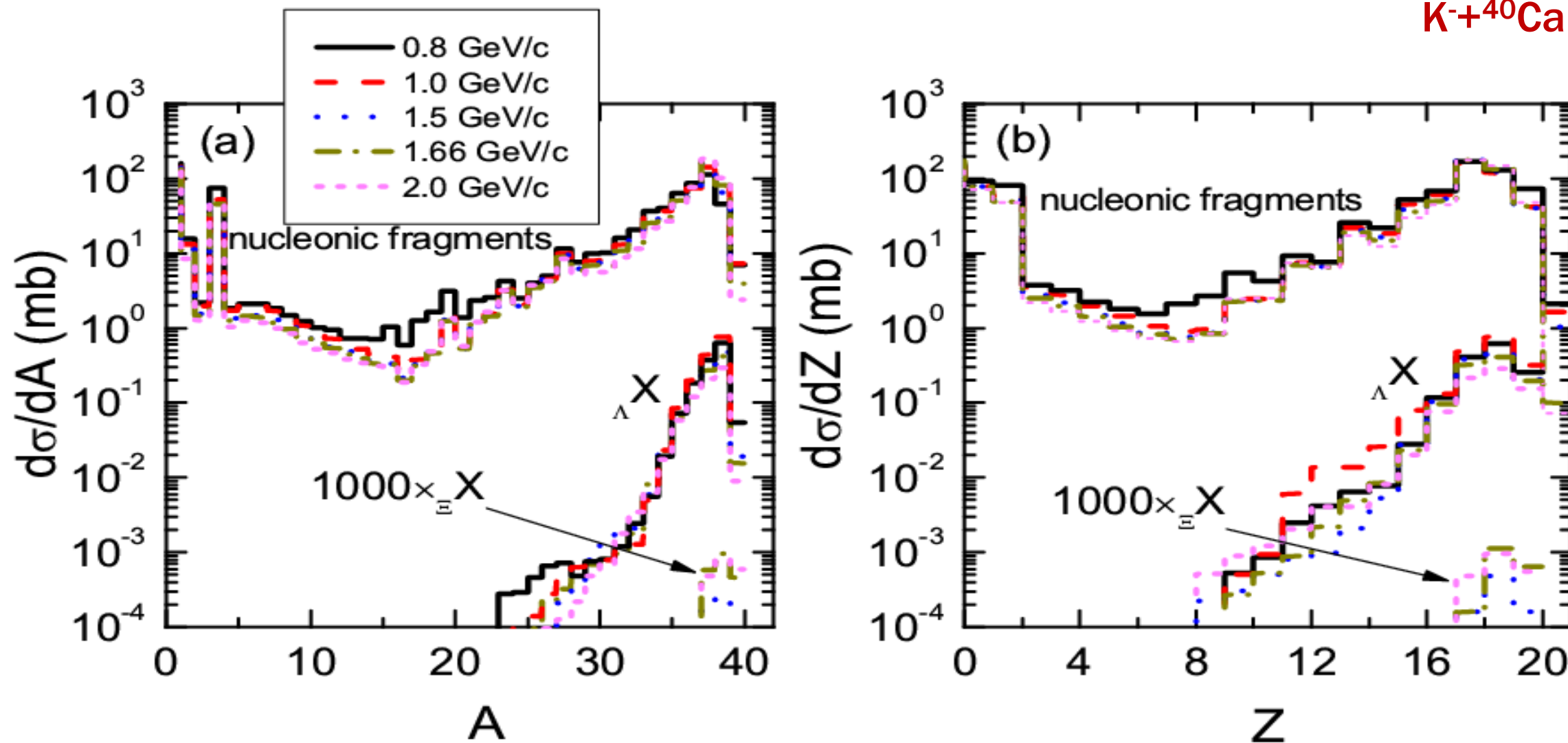
Phys. Rev. C 93, 041601(R) (2016)



Experimental data: LEAR at CERN, B. Lott *et al.*, Phys. Rev. C 63, 034616 (2001) with 1.22 GeV antiproton

III. (7) Hypernuclear formation in K⁻-induced reactions

K⁻+⁴⁰Ca



VI. Summary

- Dynamics of strange particles and hypernuclear formation in heavy-ion collisions near threshold energies have been investigated by using the LQMD transport model.
- The mean-field potentials and in-medium modifications on elementary cross sections are of importance on particle emission in phase space. The available experimental data can be well understood within inclusion of the mean-field potentials.
- Dynamics of hypernuclide formed in heavy-ion collisions and in antiproton (K-) induced reactions is discussed and proposed in the future experiments.

Thank you for your attention!