

Trento, December 19, 2018

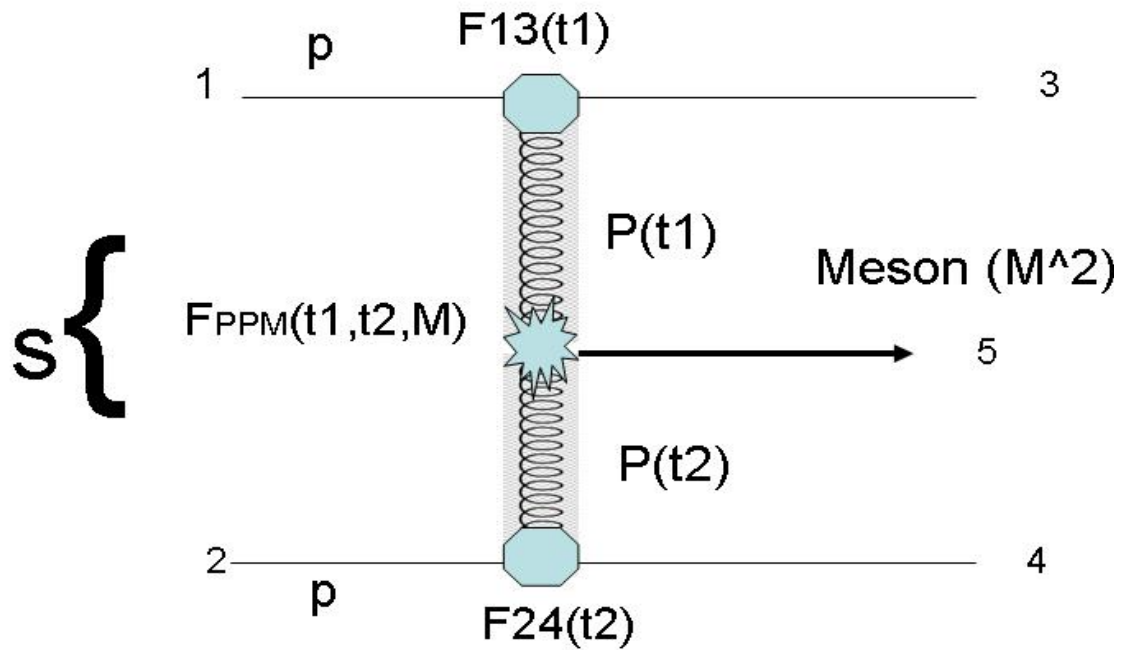
**Glueball spectroscopy.
Central diffractive production**

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Topics

- Resonance-Regge duality, the background, two-component duality;
- The pPX vertex and DIS (HERA), triple Regge limit;
- Duality and FMSR;
- SDD, DDD, CED, factorization relations;
- Pomeron (>95%) domination at the LHC and beyond.

Central diffractive meson production (double Pomeron exchange);



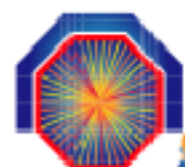
Normalized Counts / (20 MeV/c²)

V0-FMD-SPD-TPC

.....x..... No gap

—○— Double gaps

pp @ $\sqrt{s} = 7$ TeV



ALICE

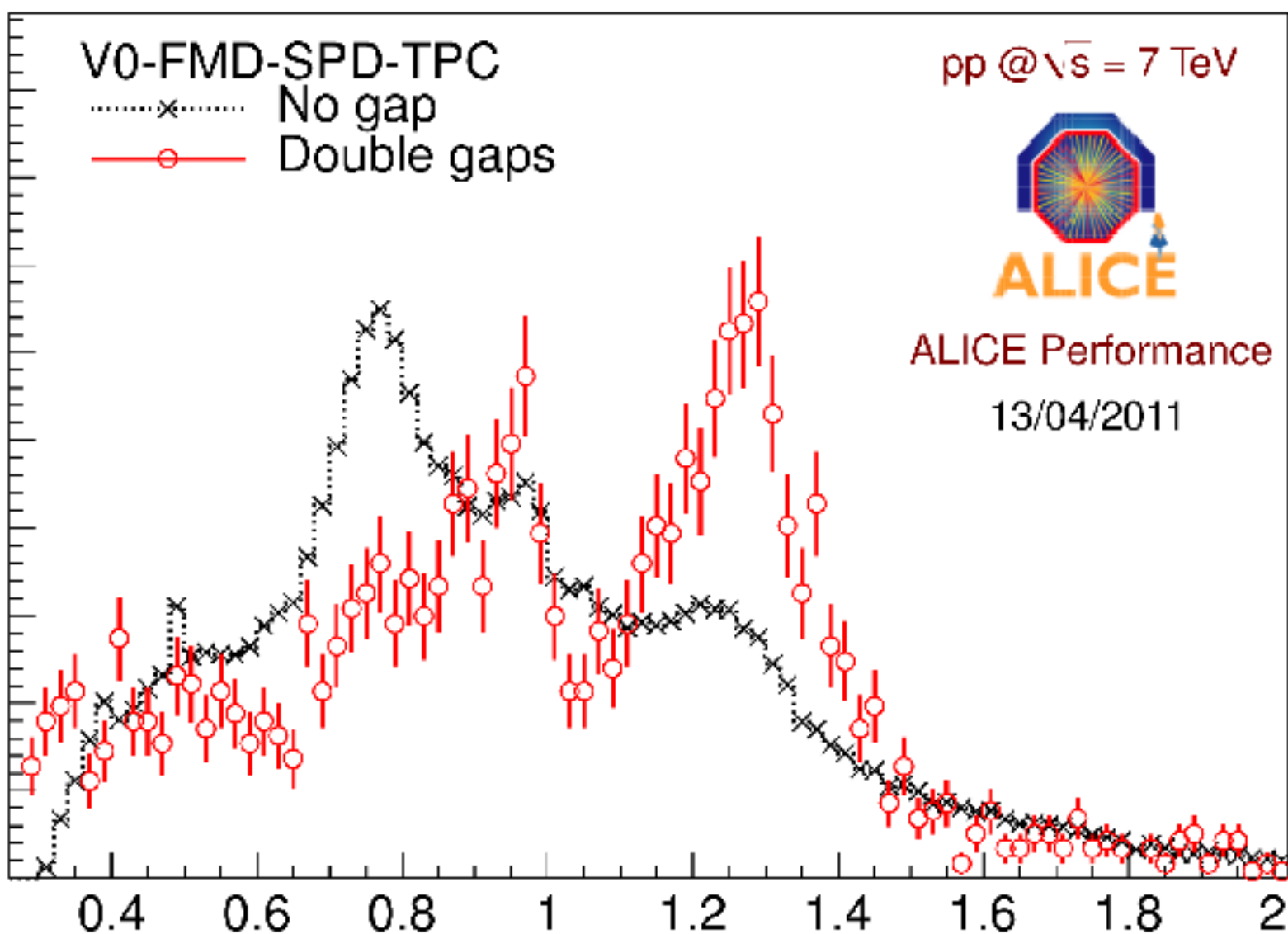
ALICE Performance

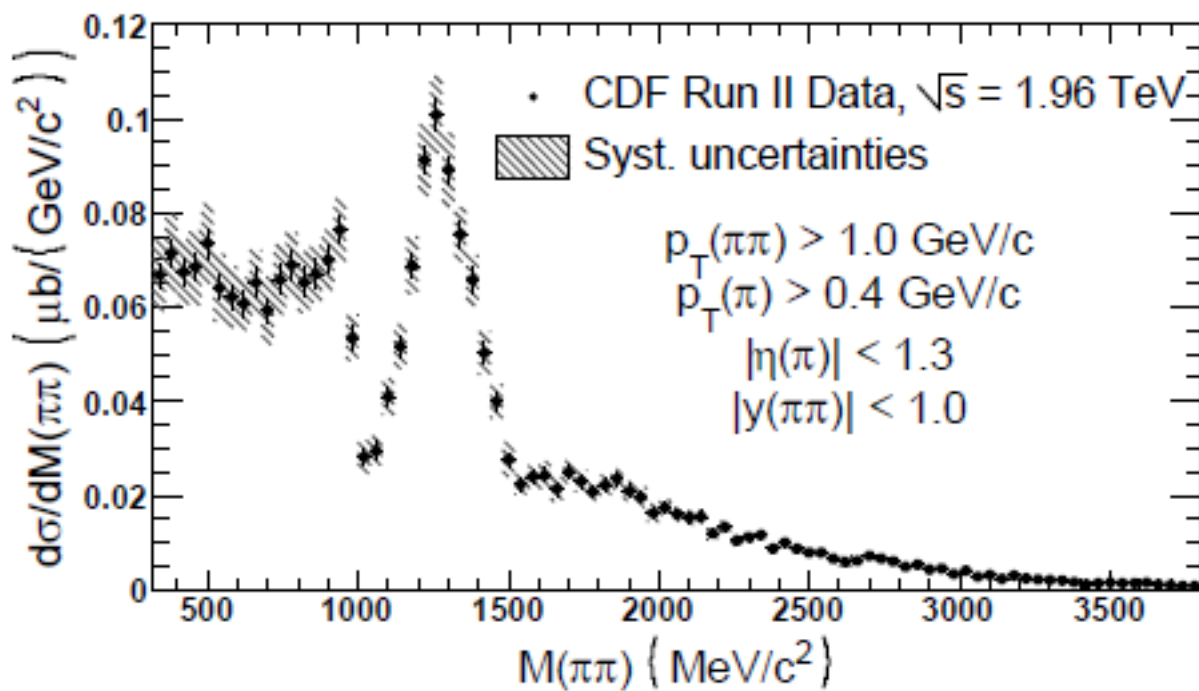
13/04/2011

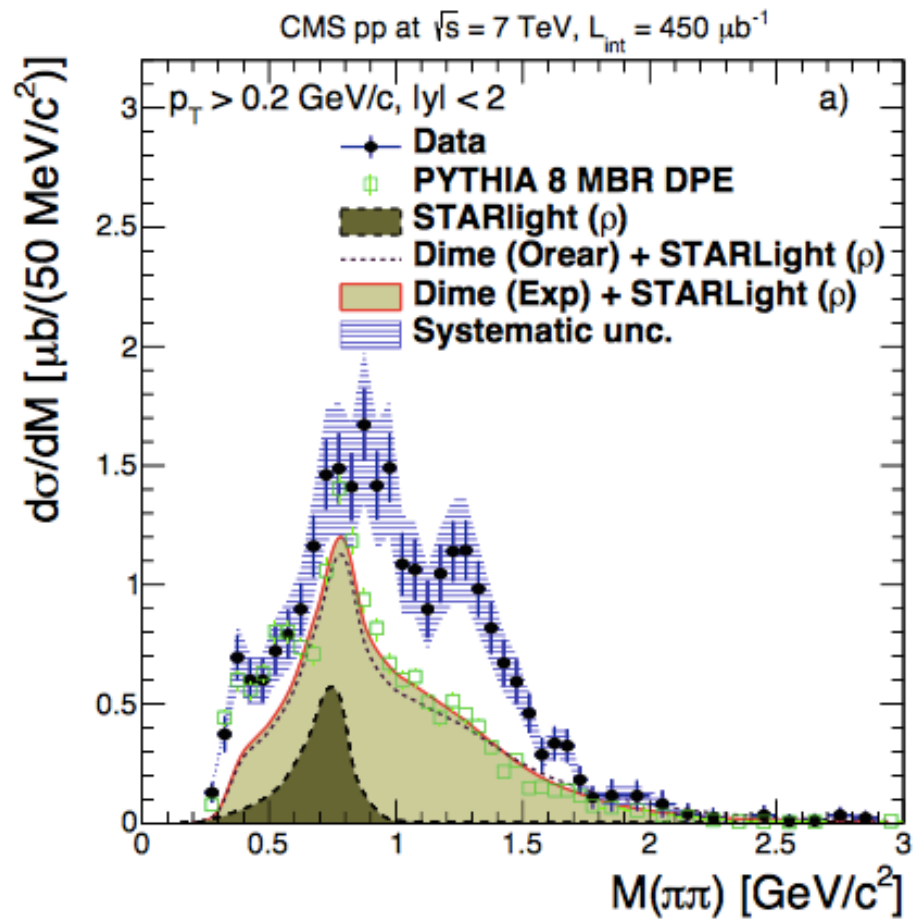
0.045
0.04
0.035
0.03
0.025
0.02
0.015
0.01
0.005
0

0.4 0.6 0.8 1 1.2 1.4 1.6 1.8 2

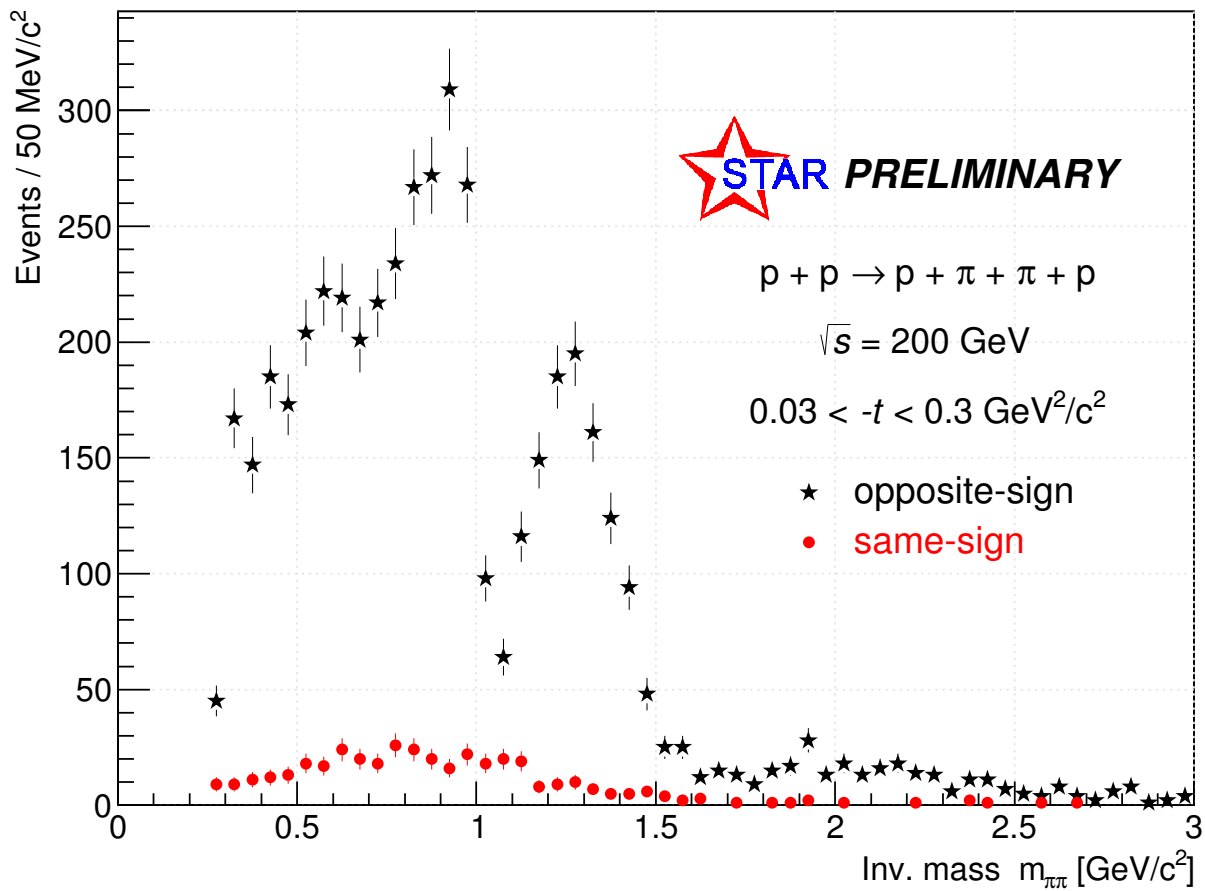
$M(\pi\pi)$ (GeV/c²)

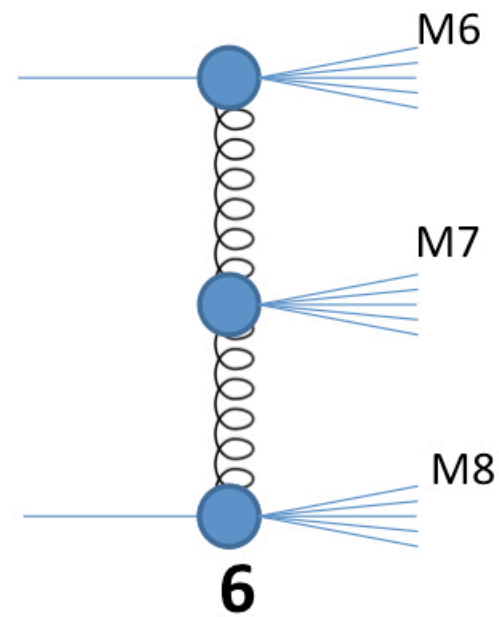
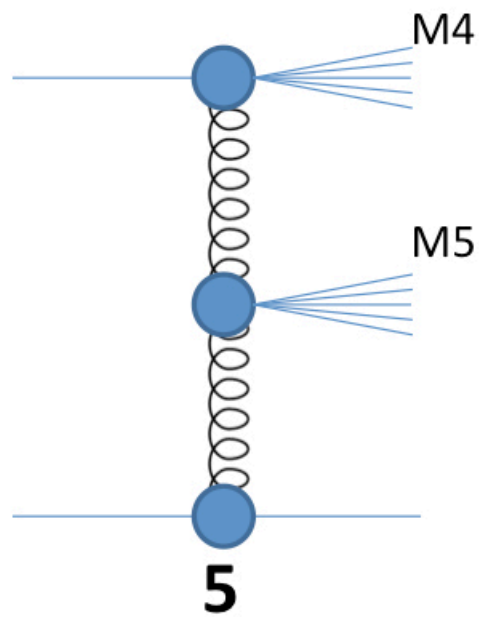
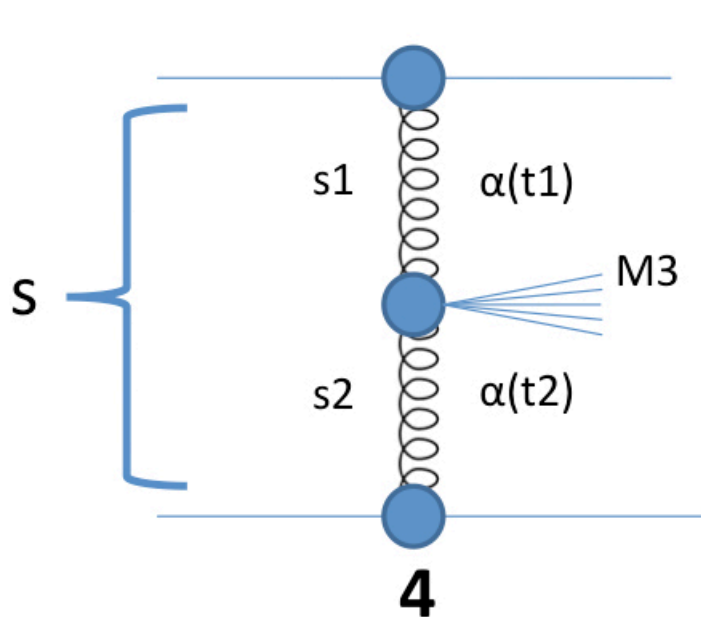
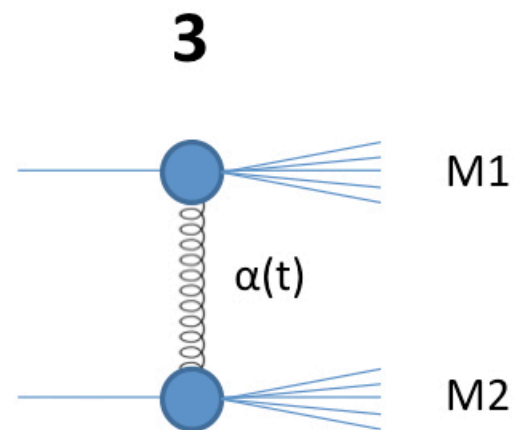
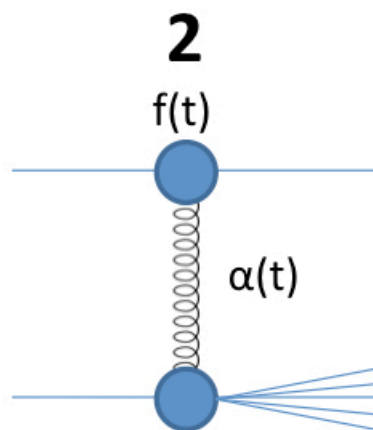
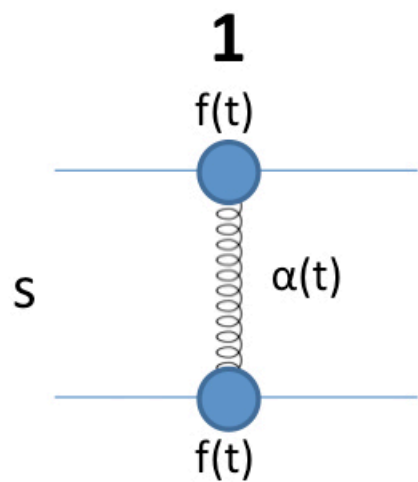


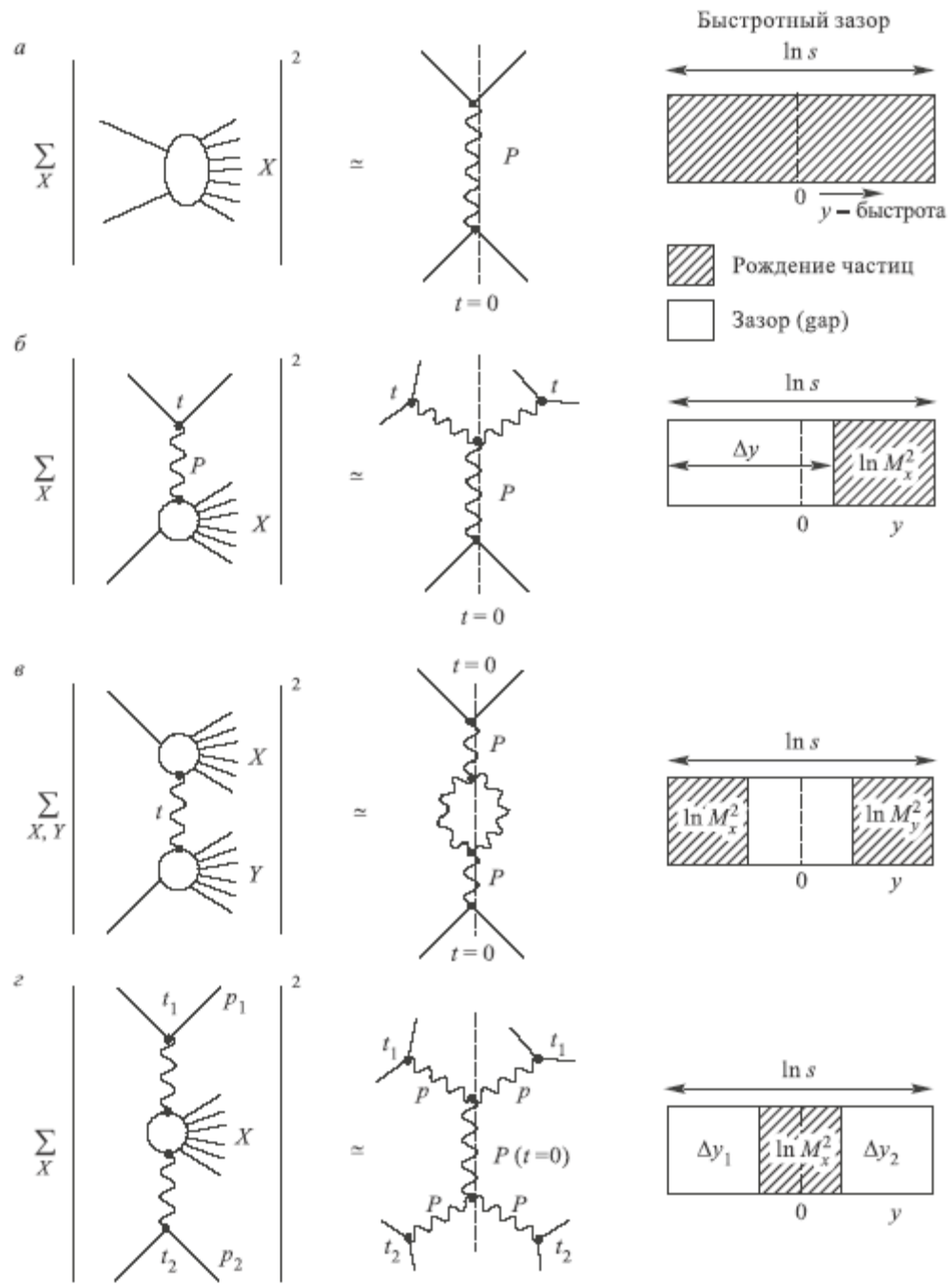




Invariant mass of $\pi\pi$, $p_T^{\text{miss}} < 0.1$ GeV/c, not acceptance-corrected, statistical errors only







Factorization (nearly perfect at the LHC and beyond!)

$$(g_1 g_2)^2 = \frac{(g_1 f_1)^2 (f_1 g_2)^2}{(f_1 f_2)^2}.$$

Hence

$$\frac{d^3 \sigma}{dt dM_1^2 dM_2^2} = \frac{d^2 \sigma_1}{dt dM_1^2} \frac{d^2 \sigma_2}{dt dM_2^2} \frac{d\sigma_{el}}{dt}.$$

Assuming exponential cone, t^{bt} and integrating in t , one gets

$$\frac{d^2 \sigma_{DD}}{dM_1^2 dM_2^2} = k \frac{1}{\sigma_{el}} \frac{d\sigma_1}{dM_1^2} \frac{d\sigma_2}{dM_2^2},$$

where $k = r^2 / (2r - 1)$, $r = b_{SD} / b_{el}$.

Further integration in M^2 yields $\sigma_{DD} = k \frac{\sigma_{SD}^2}{\sigma_{el}}$.

$$\sigma_t(s) = \frac{4\pi}{s} \text{Im}A(s, t=0); \quad \frac{d\sigma}{dt} = \frac{\pi}{s^2} |A(s, t)|^2; \quad n(s);$$

$$\sigma_{el} = \int_{t_{min} \approx -s/2 \approx \infty}^{t_{thr.} \approx 0} \frac{d\sigma}{dt} dt; \quad \sigma_{in} = \sigma_t - \sigma_{el}; \quad B(s, t) = \frac{d}{dt} \ln\left(\frac{d\sigma}{dt}\right);$$

$$A_{pp}^{\bar{p}}(s, t) = P(s, t) \pm O(s, t) + f(s, t) \pm \omega(s, t) \rightarrow_{LHC} \approx P(s, t) \pm O(s, t),$$

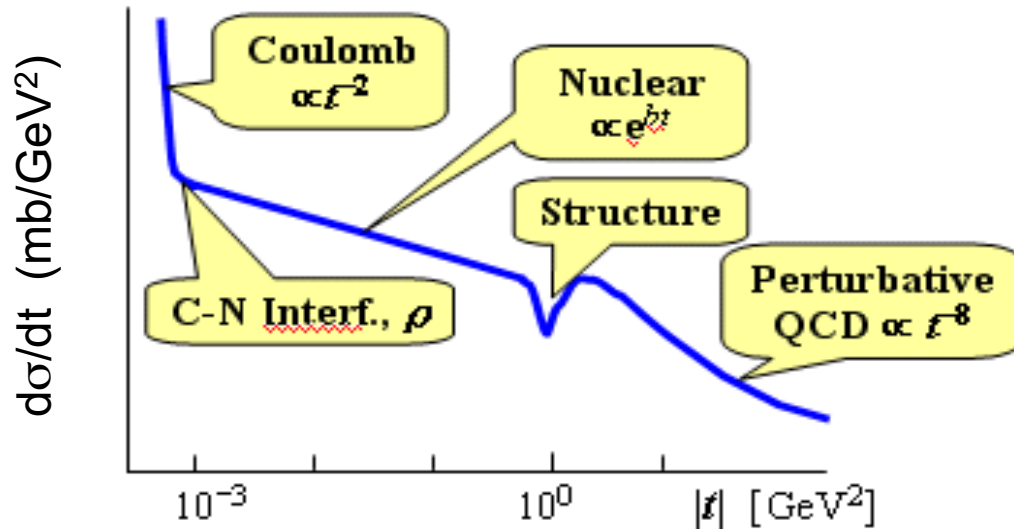
where P , O , f , ω are the Pomeron, odderon and non-leading Reggeon contributions.

$\alpha(0) \setminus C$	+	-
1	P	O
1/2	f	ω

NB: The S-matrix theory (including Regge pole) is applicable to asymptotically free states only (not to quarks and gluons)!

Elastic Scattering

$\sqrt{s} = 14$ TeV prediction of BSW model



momentum transfer $-t \sim (p\theta)^2$
 θ = beam scattering angle
 p = beam momentum

$$\rho = \frac{\text{Re}(f_{el}(t))}{\text{Im}(f_{el}(t))} \Big|_{t \rightarrow 0}$$

$$\left. \frac{dN}{dt} \right|_{t=CNI} = L\pi |f_C + f_N|^2 \approx L\pi \left| -\frac{2\alpha_{EM}}{|t|} + \frac{\sigma_{tot}}{4\pi} (i + \rho) e^{-\frac{b|t|}{2}} \right|^2$$

L , σ_{tot} , b , and ρ
 from FIT in CNI
 region (UA4)

CNI region: $|f_C| \sim |f_N| \rightarrow$ @ LHC: $-t \sim 6.5 \cdot 10^{-4} \text{ GeV}^2$; $\theta_{min} \sim 3.4 \text{ } \mu\text{rad}$

($\theta_{min} \sim 120 \text{ } \mu\text{rad}$ @ SPS)

$$\Gamma(s = M^2) = \frac{2\Im\alpha(s)}{|\alpha'(s)|}$$

$$\sigma_t^{PP} = \frac{\sigma_0 (s/s_0)^\epsilon}{\sqrt{Q_1^2 Q_2^2 \ln(s/s_0)}}.$$

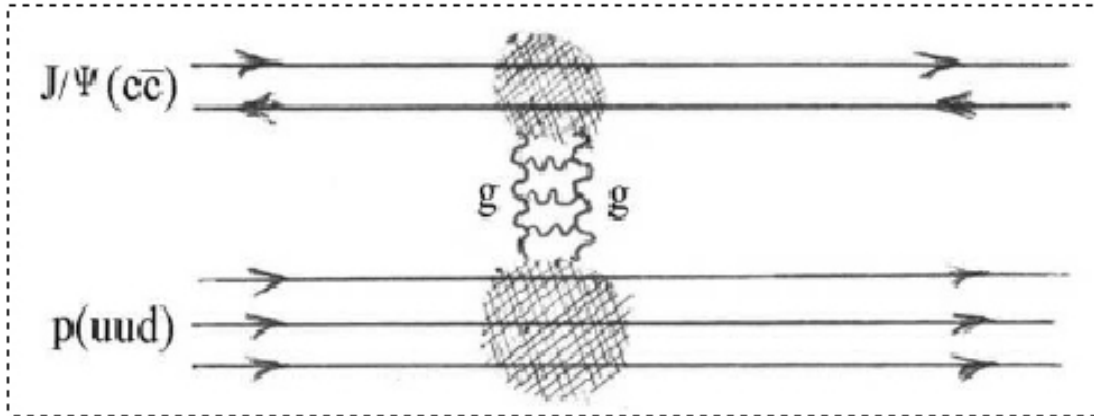
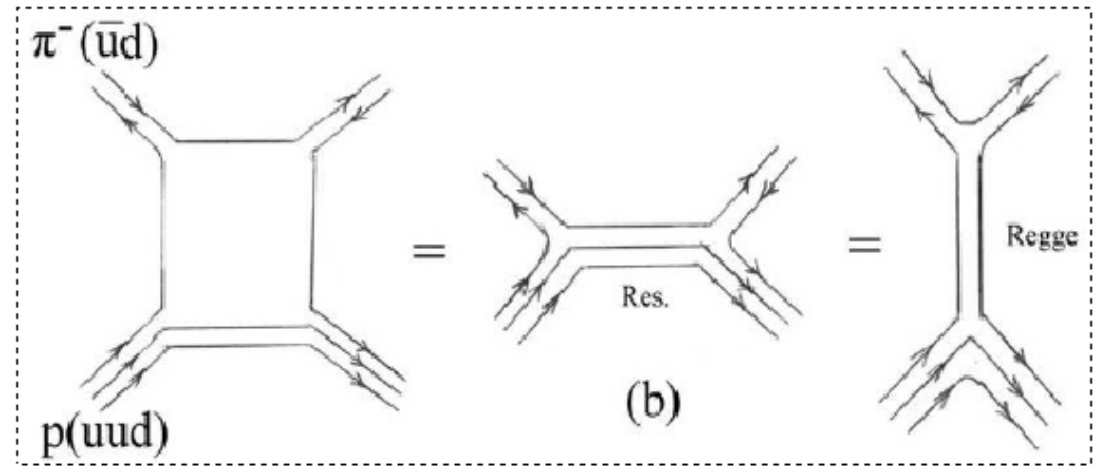
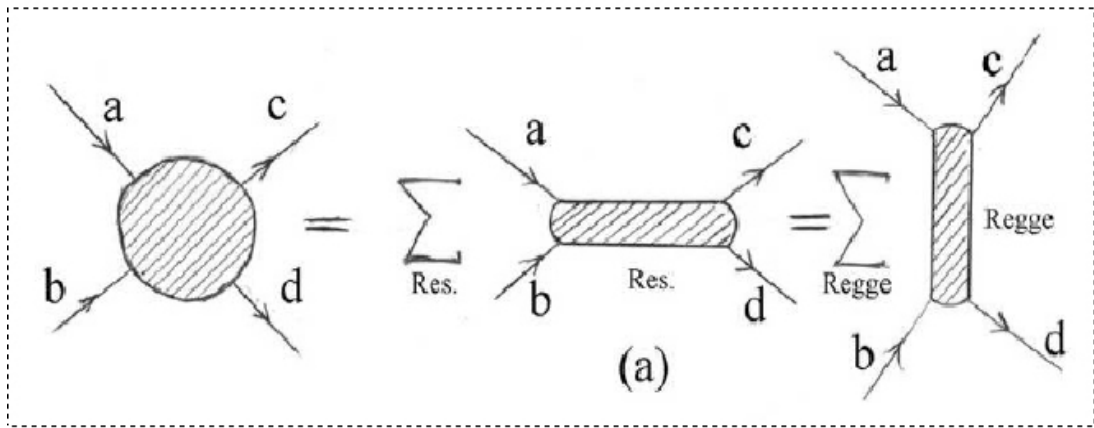


TABLE I: Two-component duality

$\mathcal{I}m A(a + b \rightarrow c + d) =$	R	Pomeron
s -channel	$\sum A_{Res}$	Non-resonant background
t -channel	$\sum A_{Regge}$	Pomeron ($I = S = B = 0; C = +1$)
Duality quark diagram	Fig. 1b	Fig. 2
High energy dependence	$s^{\alpha-1}, \alpha < 1$	$s^{\alpha-1}, \alpha \geq 1$

The (s, t) term of a dual amplitude is

$$D(s, t) = c \int_0^1 dx \left(\frac{x}{g_1}\right)^{-\alpha(s')-1} \left(\frac{1-x}{g_2}\right)^{-\alpha(t')-1},$$

where s and t are the Mandelstam variables, and g_1, g_2 are parameters, $g_1, g_2 > 1$. For simplicity, we set $g_1 = g_2 = g_0$.

1. Regge behavior, $s \rightarrow \infty, t = \text{const} : D(s, t) \sim s^{\alpha(t)-1}$;

2. Threshold behavior, $s \rightarrow s_0 : D(s, t) \sim \sqrt{s_0 - s} [\text{const} + \ln(1 - s_0/s)]$;

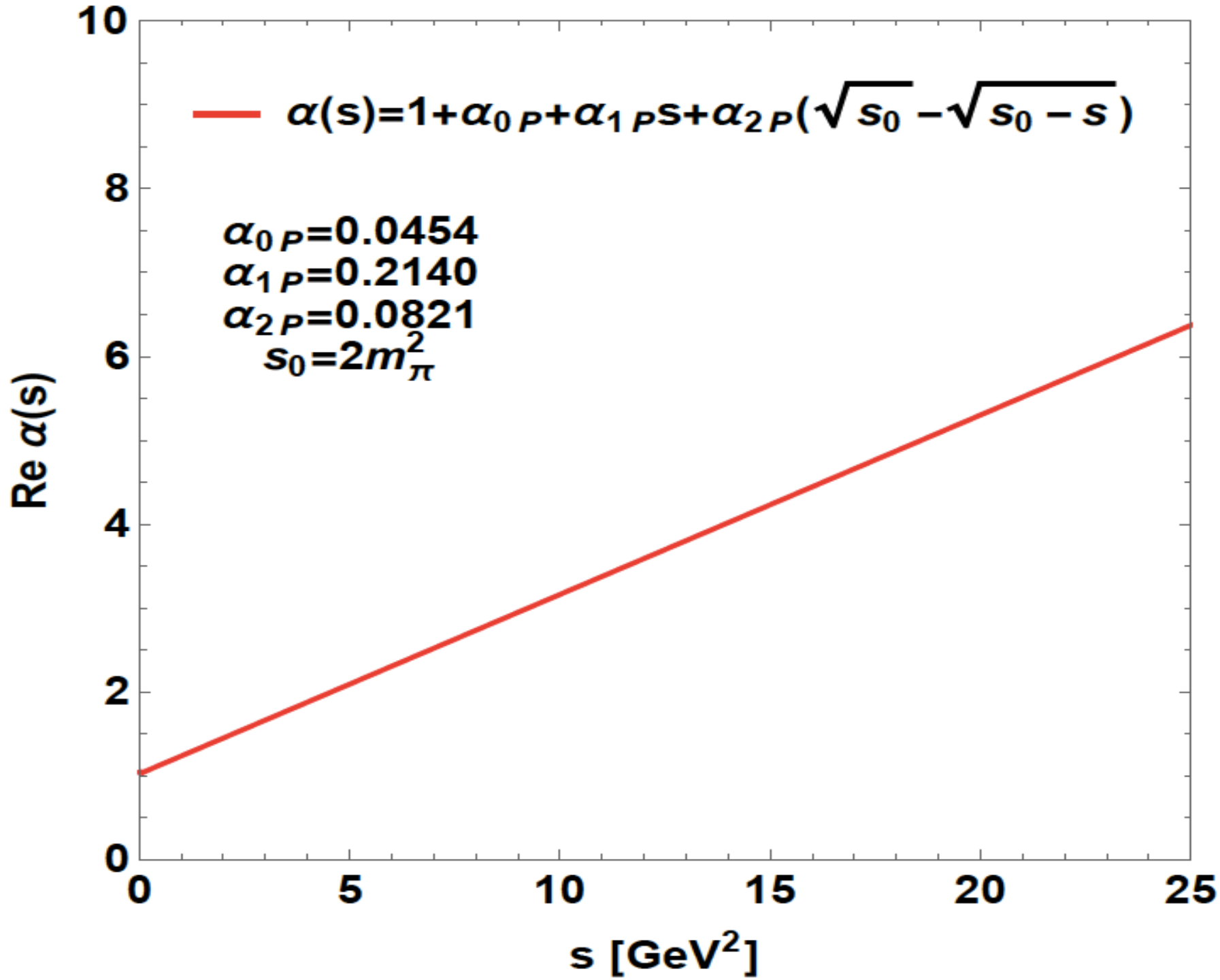
3. Direct-channel poles:

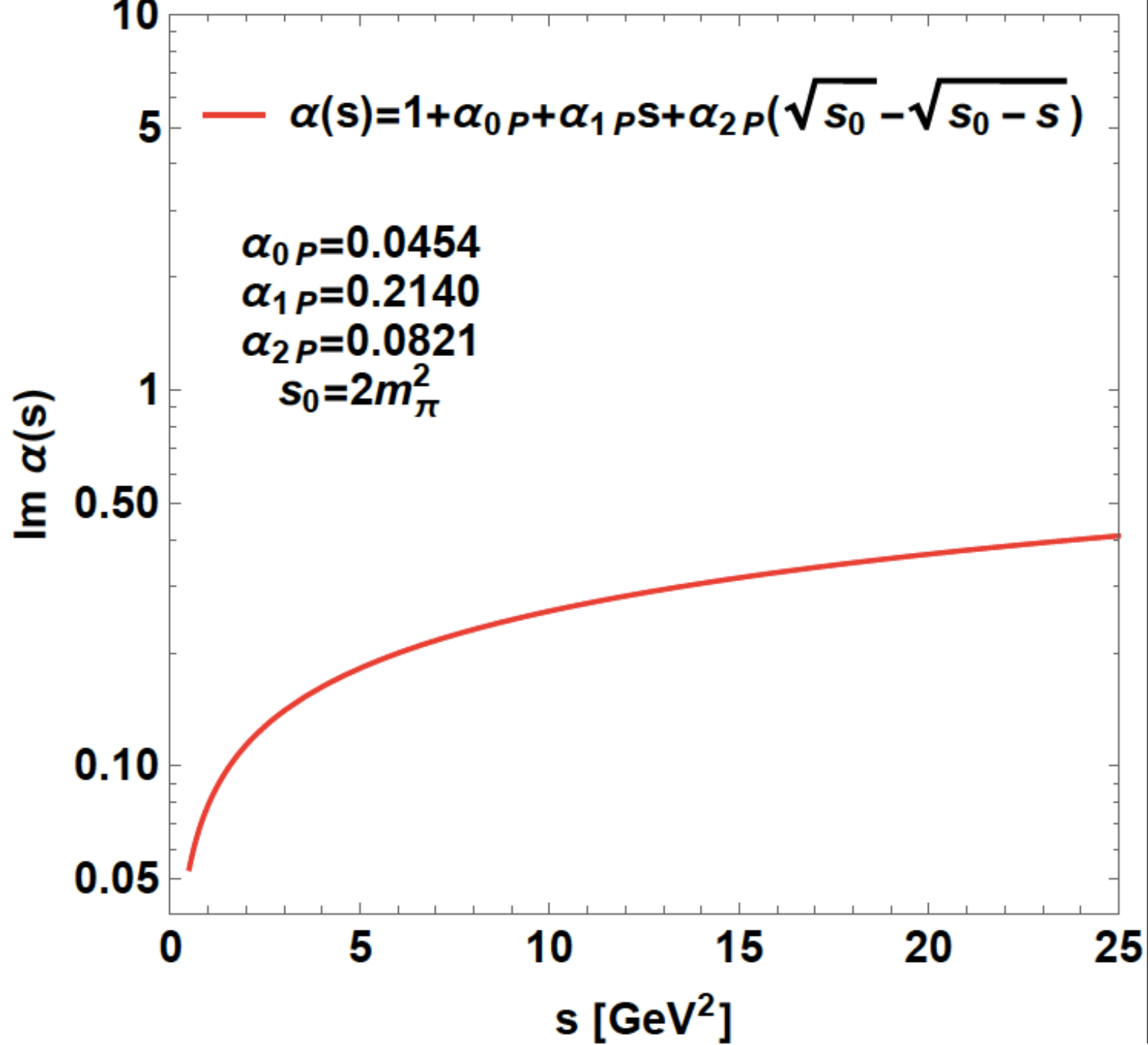
$$D(s, t) = \sum_{n=0}^{\infty} g^{n+1} \sum_{l=0}^n \frac{[-s\alpha'(s)]^l C_{n-l}(t)}{[n - \alpha(s)]^{l+1}}.$$

Exotic direct-channel trajectory: $\alpha(s) = \alpha(0) + \alpha_1(\sqrt{s_0} - \sqrt{s_0 - s})$.

"GOLDEN" diffraction reaction: $J/\Psi p$ - scattering: By VMD, photoproduction is reduced to elastic hadron scattering:

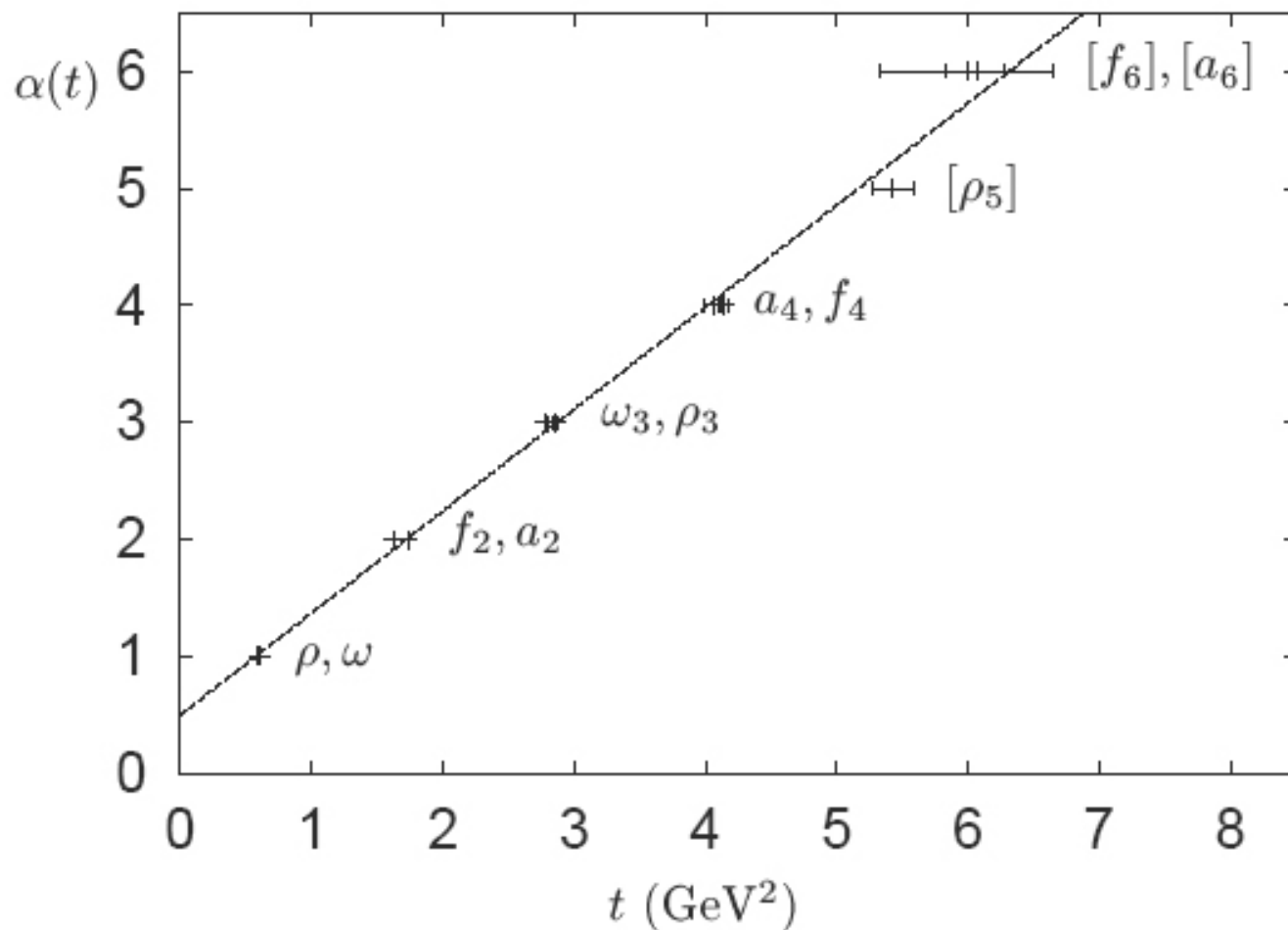
$$D(\gamma p - V p) = \sum \frac{e}{f_V} D(V p - V p).$$

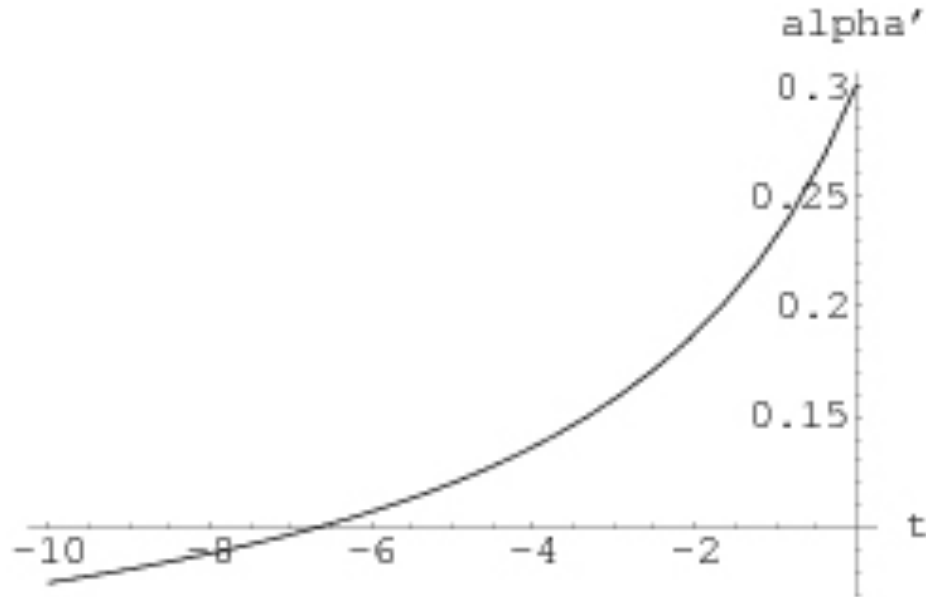




Linear particle trajectories

Plot of spins of families of particles against their squared masses:





The slope of the cone for a single pole is: $B(s, t) \sim \alpha'(t) \ln s$. The Regge residue $e^{b\alpha(t)}$ with a logarithmic trajectory $\alpha(t) = \alpha(0) - \gamma \ln(1 - \beta t)$, is identical to a form factor (geometrical model).

[R. Fiore](#), [L.L. Jenkovszky](#), [V. Magas](#), [F. Paccanoni](#), [A. Papa](#), *Analytic model of Regge trajectories*, Eur.Phys.J. A10 (2001) 217-221;
[arXiv:hep-ph/0011035](#)

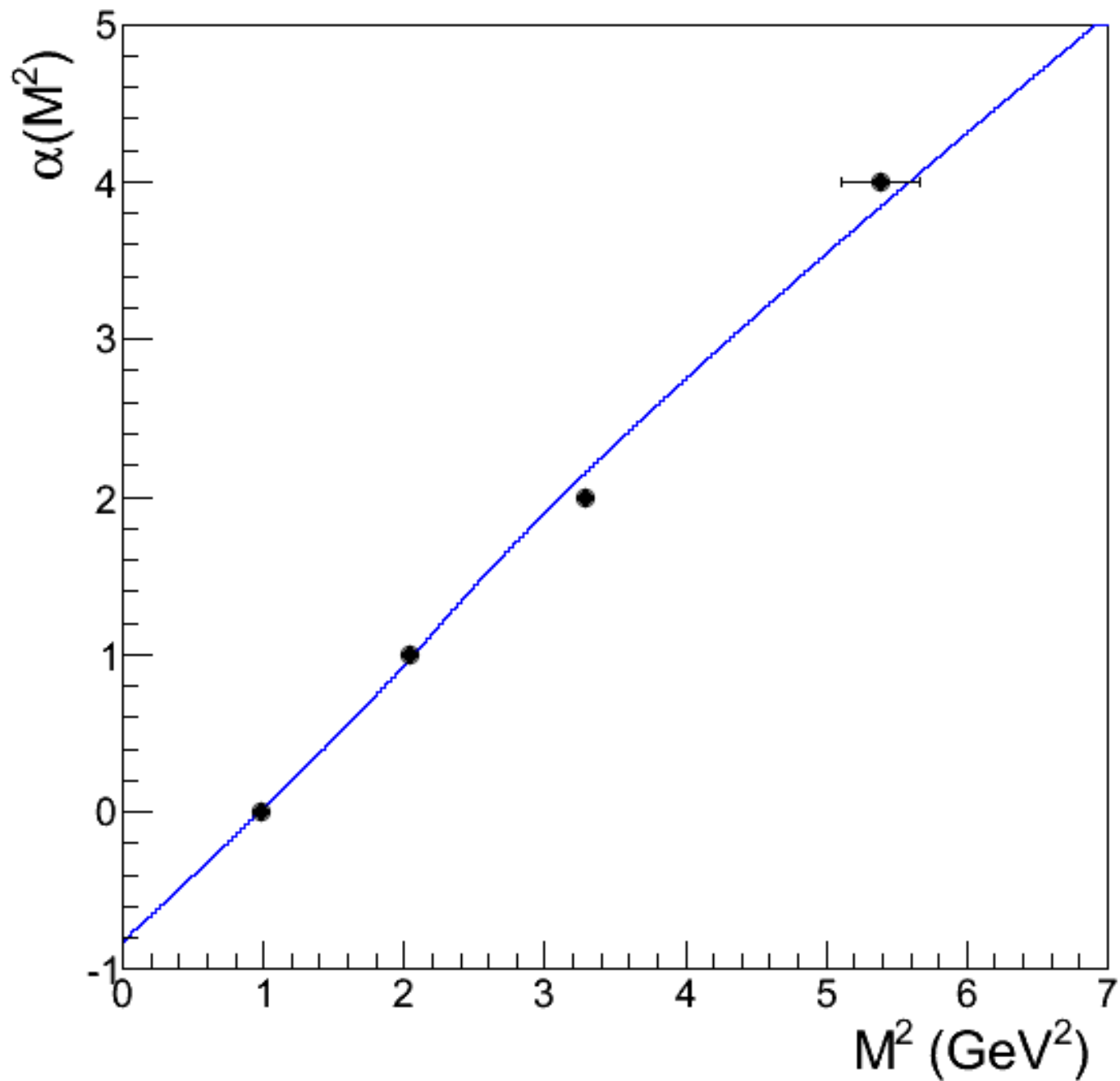
The Pomeron trajectory

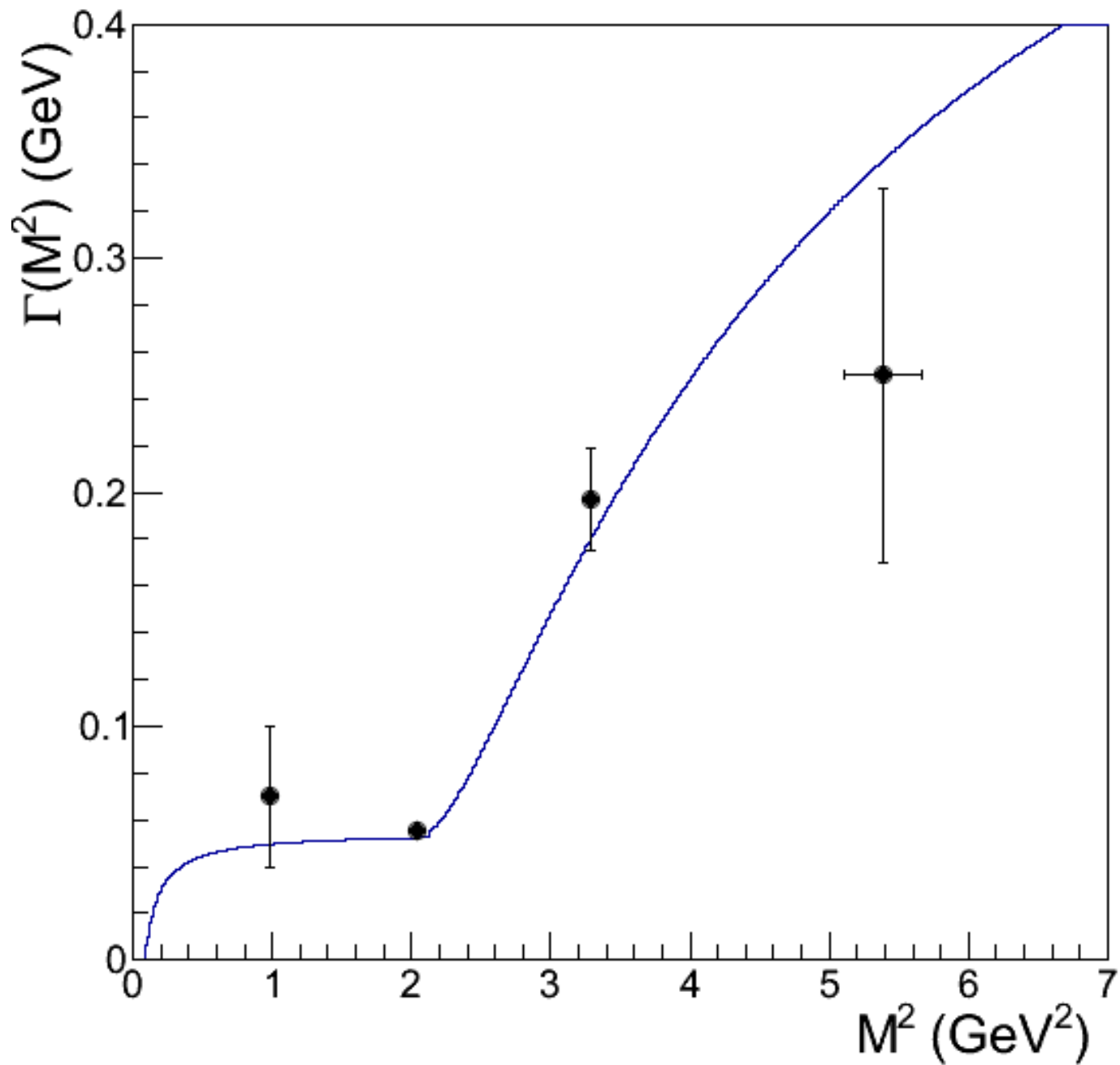
The Pomeron trajectory has threshold singularities, the lowest one being due to the two-pion exchange, required by the t -channel unitarity. There is a constrain (Barut, Zwanziger; Gribov) from the t -channel unitarity, by which

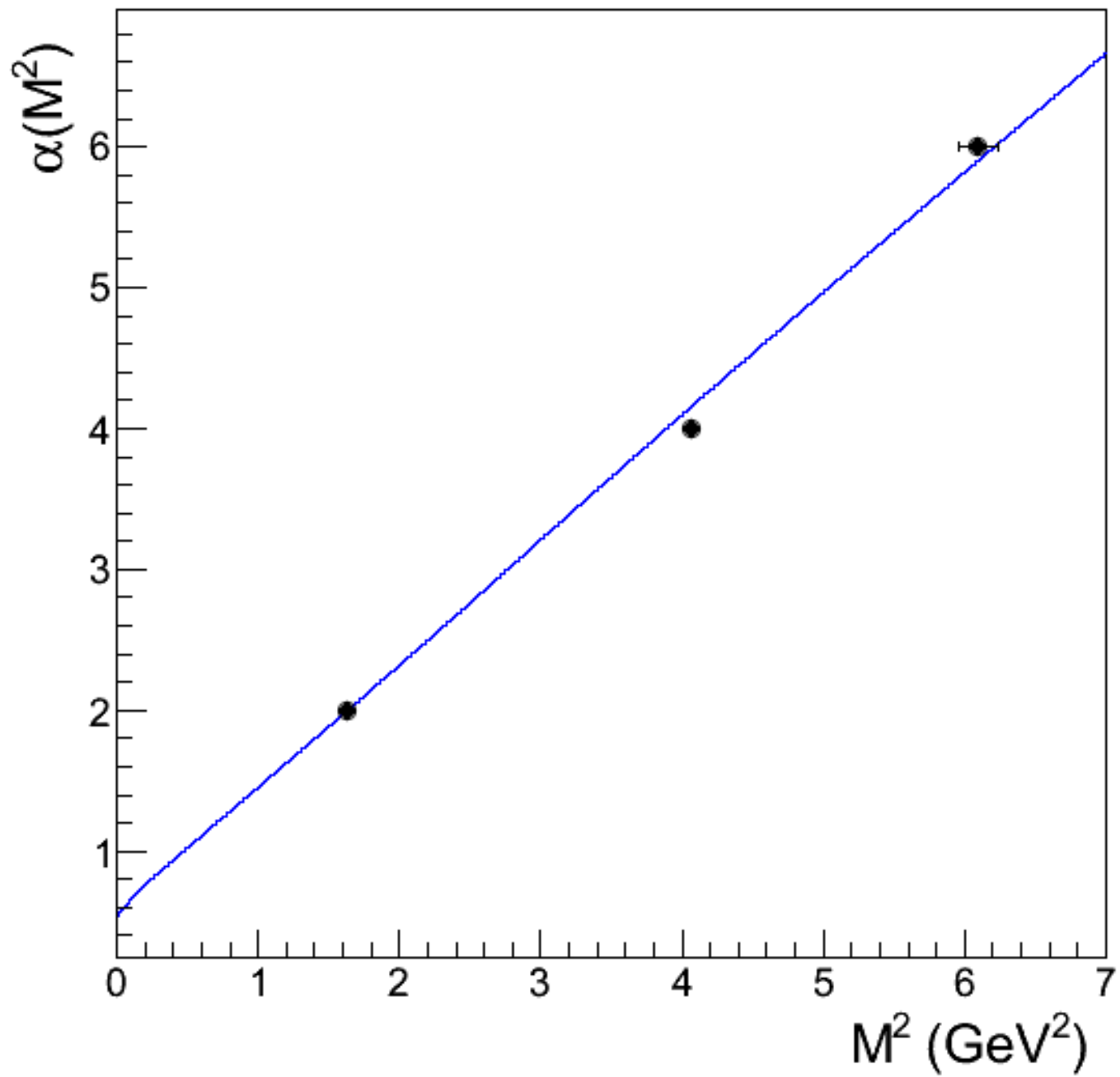
$$\Im\alpha(t) \sim (t - t_0)^{\Re\alpha(t_0)+1/2}, \quad t \rightarrow t_0,$$

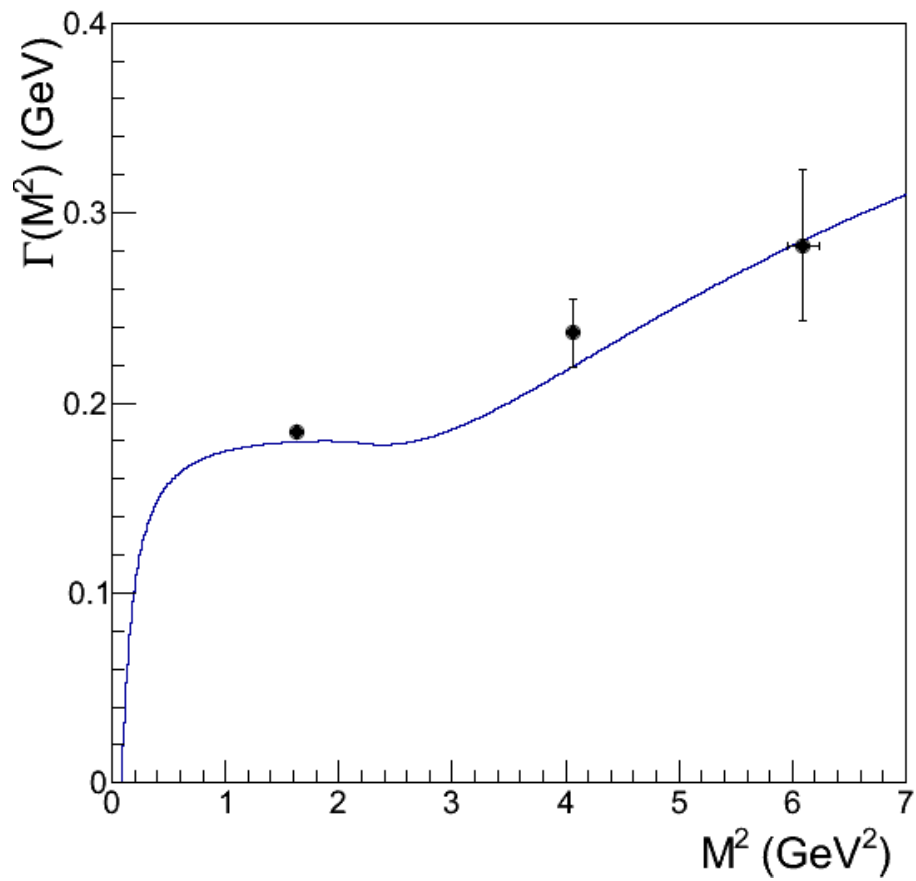
where t_0 is the lightest threshold. For the Pomeron trajectory it is $t_0 = 4m_\pi^2$, and near the threshold:

$$\alpha(t) \sim \sqrt{4m_\pi^2 - t}. \quad (1)$$









“Reggeized (dual) Breit-Wigner” formula:

$$\begin{aligned} \sigma_T^{Pp}(M_x^2, t) &= \text{Im } A(M_x^2, t) = \frac{A_{N^*}}{\sum_n n - \alpha_{N^*}(M_x^2)} + Bg(t, M_x^2) = \\ &= A_n \sum_{n=0,1,\dots} \frac{[f(t)]^{2(n+1)} \text{Im } \alpha(M_x^2)}{(2n + 0.5 - \text{Re } \alpha(M_x^2))^2 + (\text{Im } \alpha(M_x^2))^2} + B_n e^{b_{in}^{bg} t} (M_x^2 - M_{p+\pi}^2)^\epsilon \end{aligned}$$

$$F(x_B, t) = \frac{x_B(1 - x_B)}{(M_x^2 - m_p^2) (1 + 4m_p^2 x_B^2 / (-t))^{3/2}}, \quad x_B = \frac{-t}{M_x^2 - m_p^2 - t}$$

$$F_p(t) = \frac{1}{1 - \frac{t}{0.71}}, \quad f(t) = e^{b_{in} t}$$

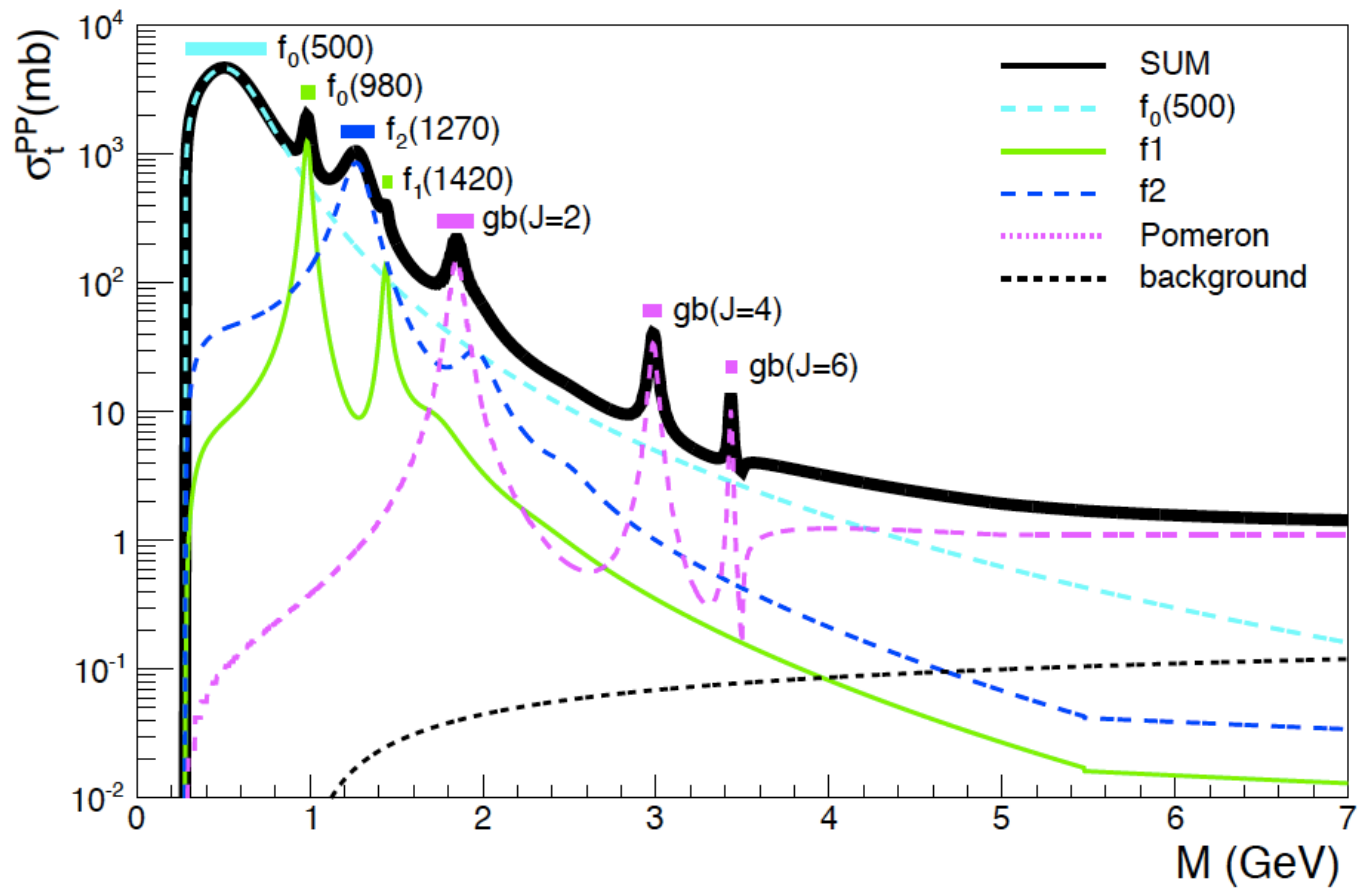
$$\alpha(t) = \alpha(0) + \alpha' t = 1.04 + 0.25t$$

Representative examples of the Pomeron trajectories: 1) Linear; 2) With a square-root threshold, required by t -channel unitarity and accounting for the small- t “break” as well as the possible “Orear”, $e^{\sqrt{-t}}$ behavior in the second cone; and 3) A logarithmic one, anticipating possible “hard effects” at large $|t|$ $|t| < 8 \text{ GeV}^2$.

$$\alpha_P \equiv \alpha_P(t) = 1 + \delta_P + \alpha_{1P}t, \quad (\text{TR.1})$$

$$\alpha_P \equiv \alpha_P(t) = 1 + \delta_P + \alpha_{1P}t - \alpha_{2P} \left(\sqrt{4\alpha_{3P}^2 - t} - 2\alpha_{3P} \right), \quad (\text{TR.2})$$

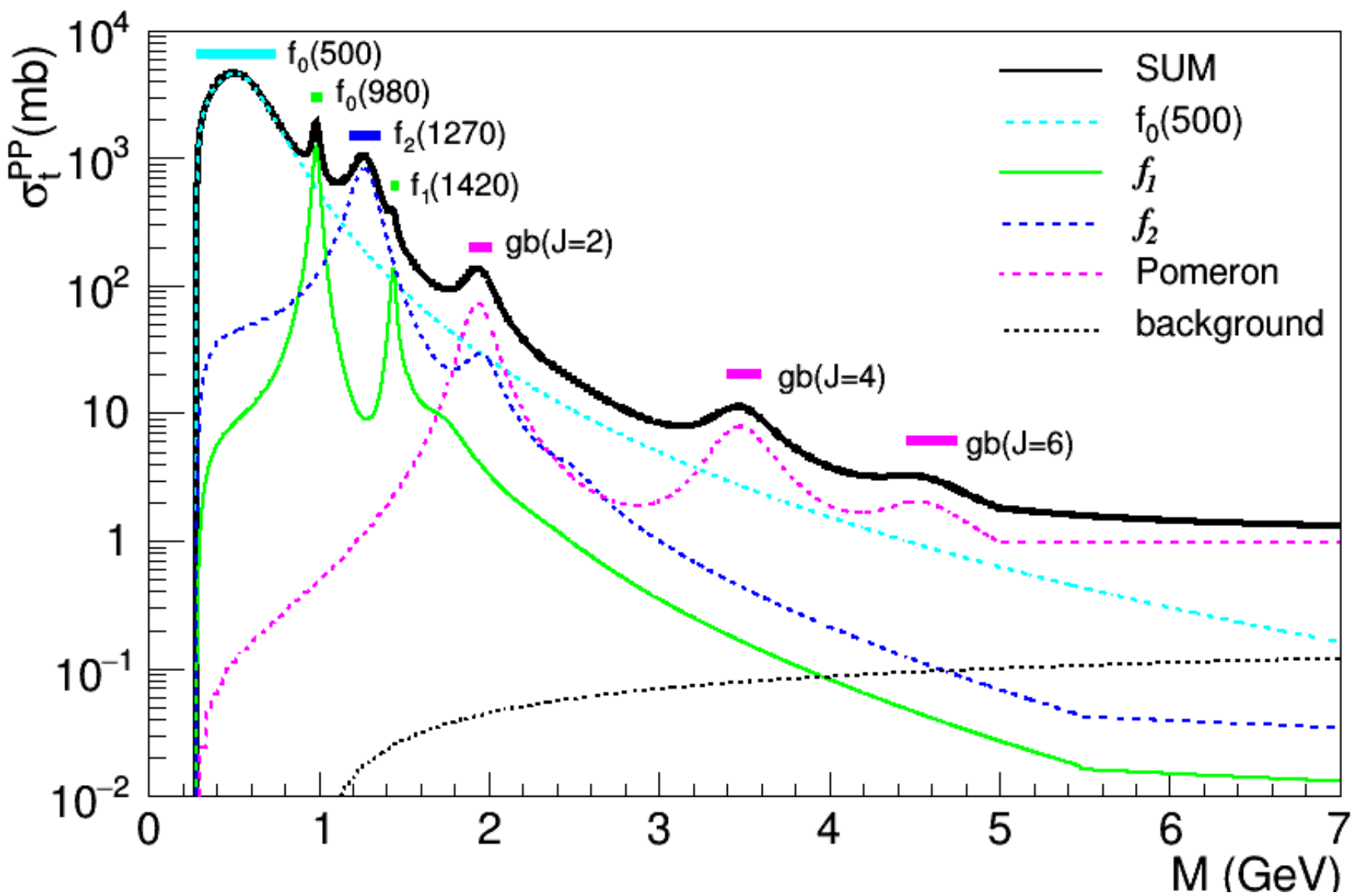
$$\alpha_P \equiv \alpha_P(t) = 1 + \delta_P - \alpha_{1P} \ln(1 - \alpha_{2P}t). \quad (\text{TR.3})$$

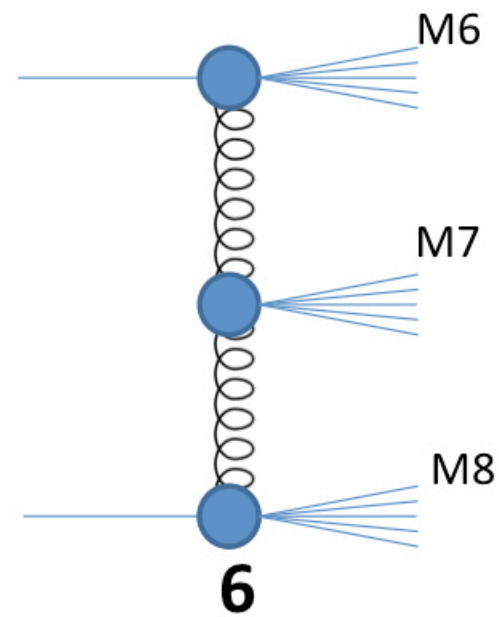
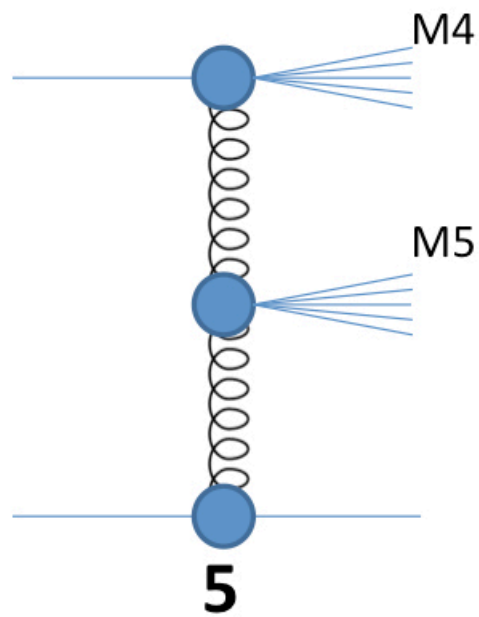
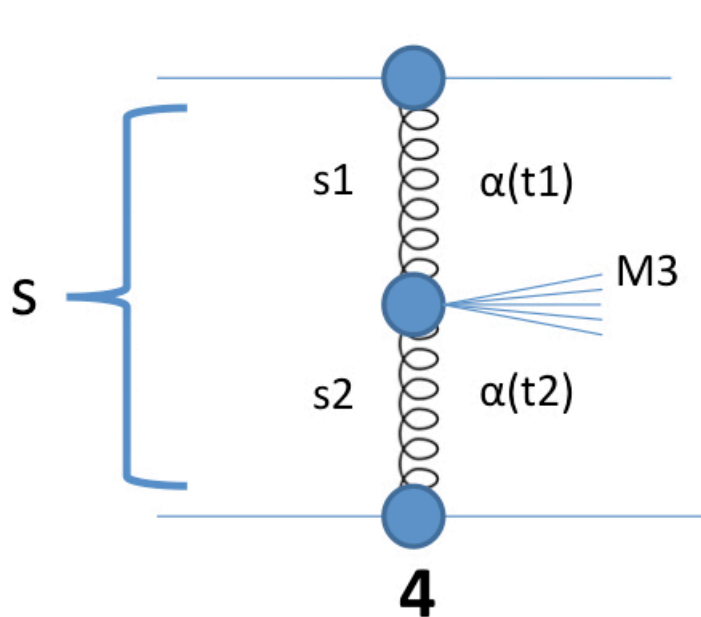
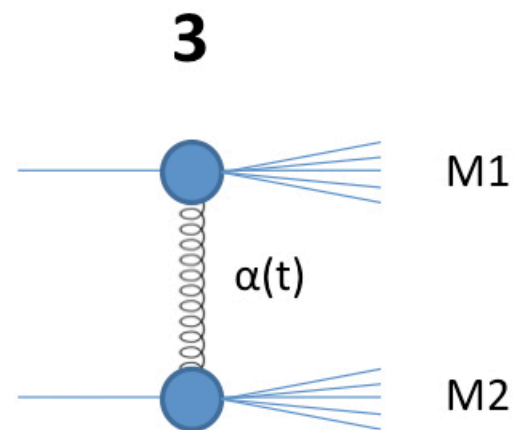
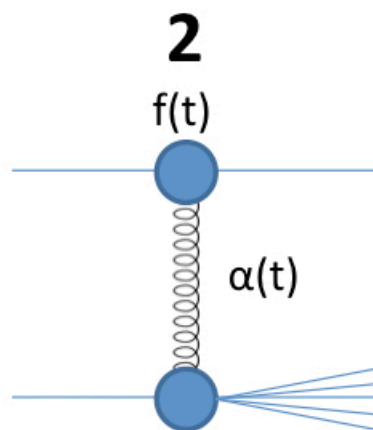
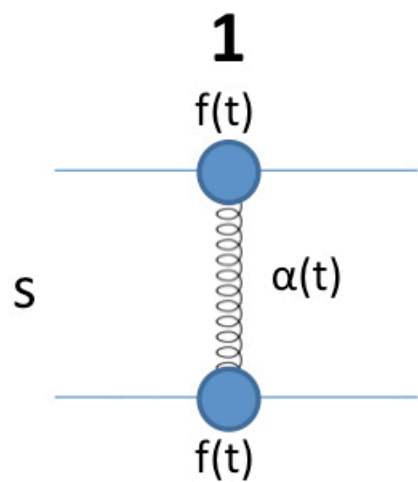


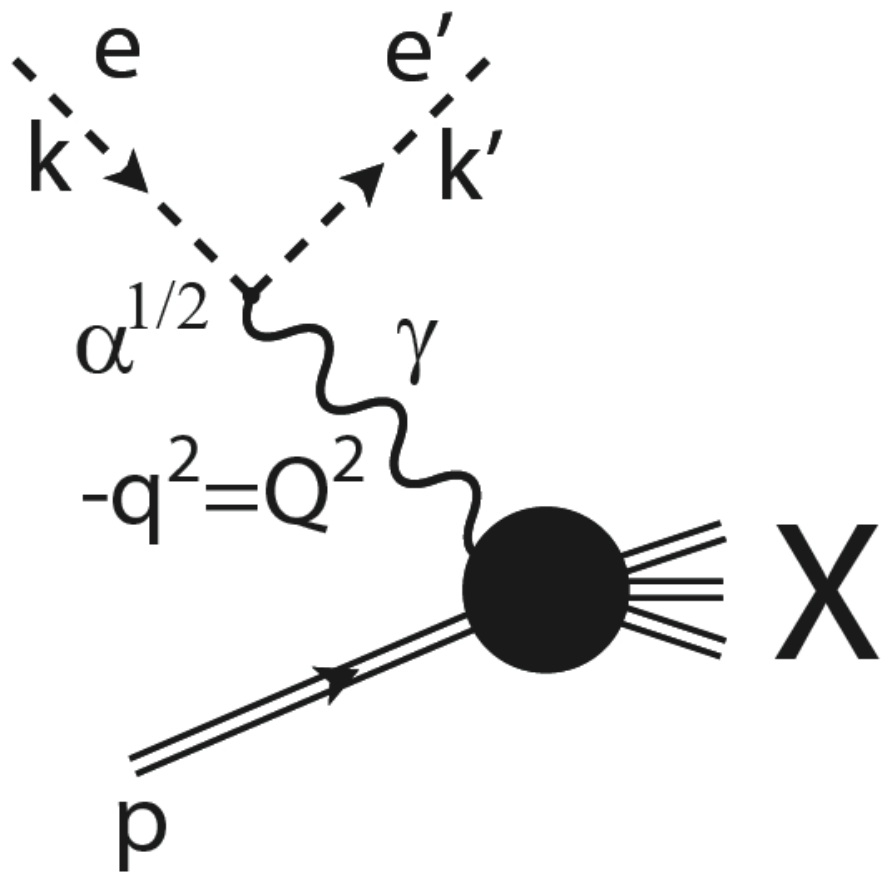
$$\alpha(s) = \alpha_0 + \alpha' s + \alpha_1 \sqrt{s_0 - s};$$

$$\alpha(s) = \alpha_0 + \alpha_2 \sqrt{s_0 - s} + \alpha_3 \sqrt{s_1 - s};$$

$$\alpha(s) = \frac{\alpha_0 + \alpha' s}{1 + \alpha_4 \sqrt{s_0 - s}},$$







$$\left| \begin{array}{c} \text{wavy } q \\ \bullet \\ \text{double } p \\ \text{X} \end{array} \right|^2 = \sum_X \begin{array}{c} \text{wavy } q \\ \bullet \\ \text{double } p \\ \text{X} \end{array} = \begin{array}{c} \text{wavy } q \\ \bullet \\ \text{double } p \\ \text{X} \end{array} \quad \text{Unitarity } t=0 = \sum_R \begin{array}{c} \text{wavy } q \\ \bullet \\ \text{double } p \\ \text{R} \end{array} = \sum_{\text{Res}} \begin{array}{c} \text{wavy } q \\ \bullet \\ \text{double } p \\ \text{Res} \end{array} \quad \text{Veneziano duality}$$

- R. Fiore, A. Flachi, L. Jenkovszky, A. Lengyel, and V. Magas, *A kinematically complete analysis of the CLAS data on the proton structure function F_2 in a Regge-Dual model*, Phys.Rev. D**69** (2004) 014004; arXiv:0308178.
- Wolfgang Schäfer, Photon-Pomeron fusion..., Trento Workshop, March 2017-->
- H. Abramowicz et al. (2007)

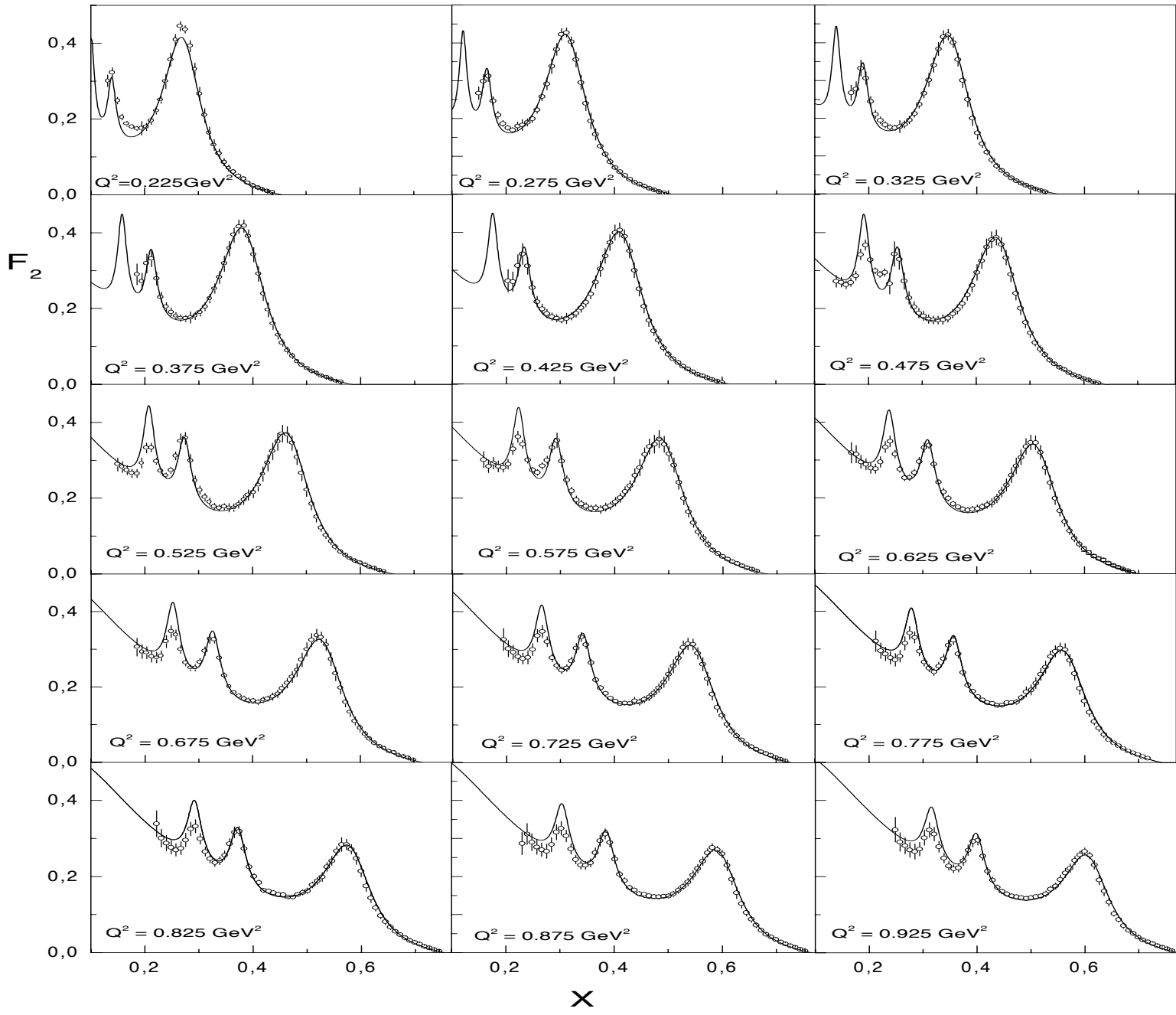
$$F_2(x, Q^2) = \frac{Q^2(1-x)}{4\pi\alpha(1+4m^2x^2/Q^2)} \sigma_t^{\gamma^*p},$$

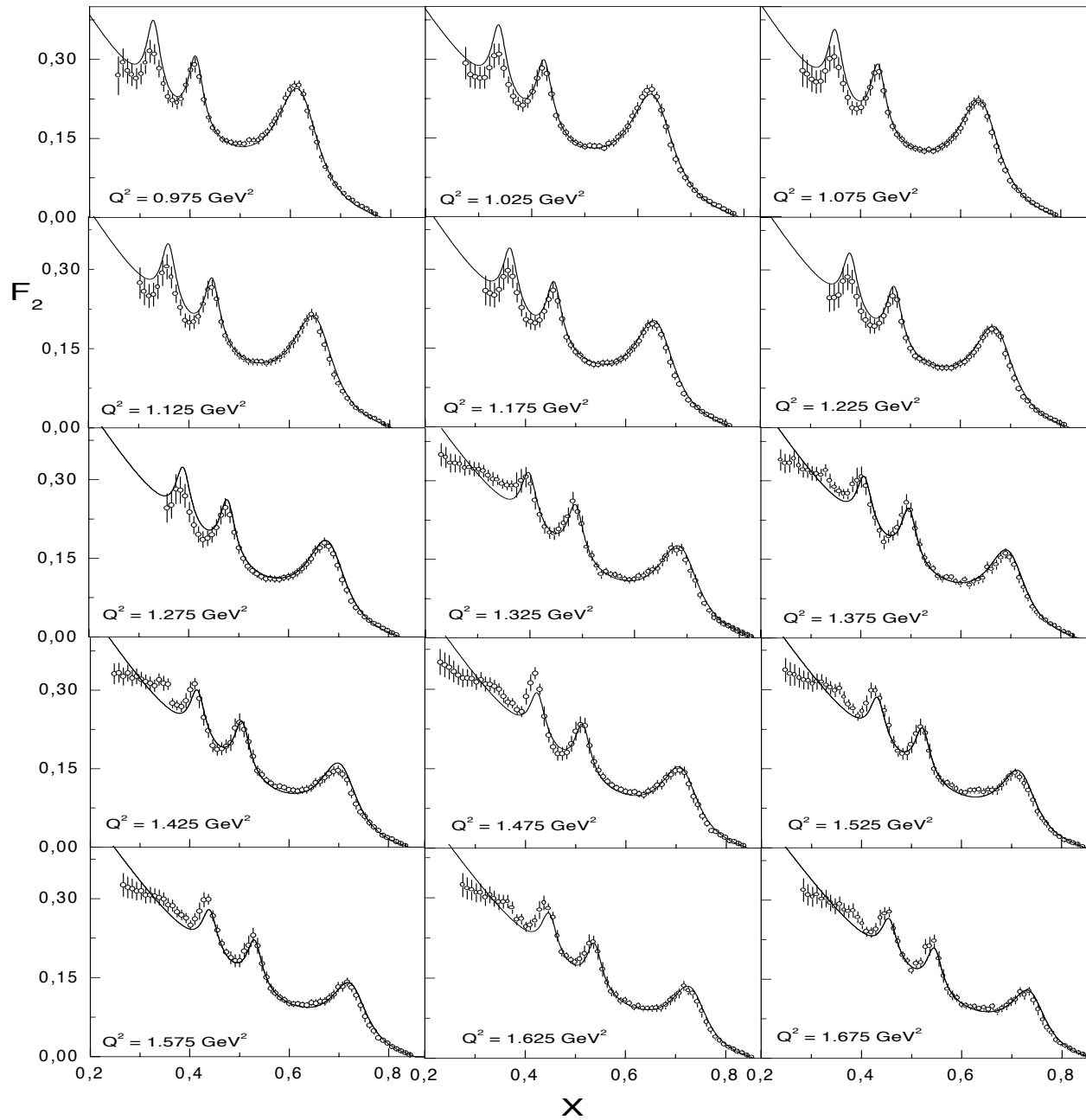
with the norm

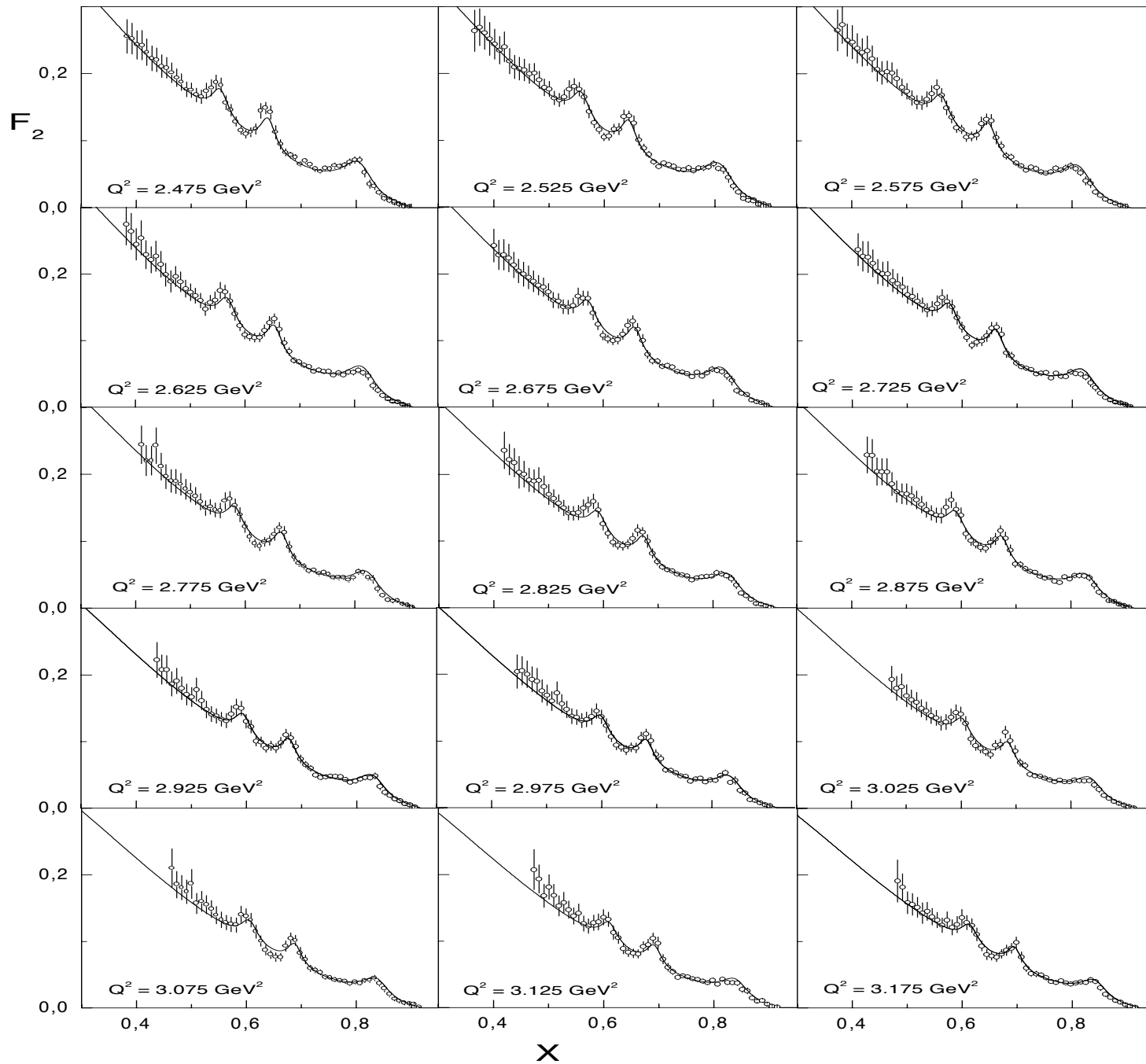
$$\sigma_t^{\gamma^*p}(s) = \text{Im} A(s, Q^2).$$

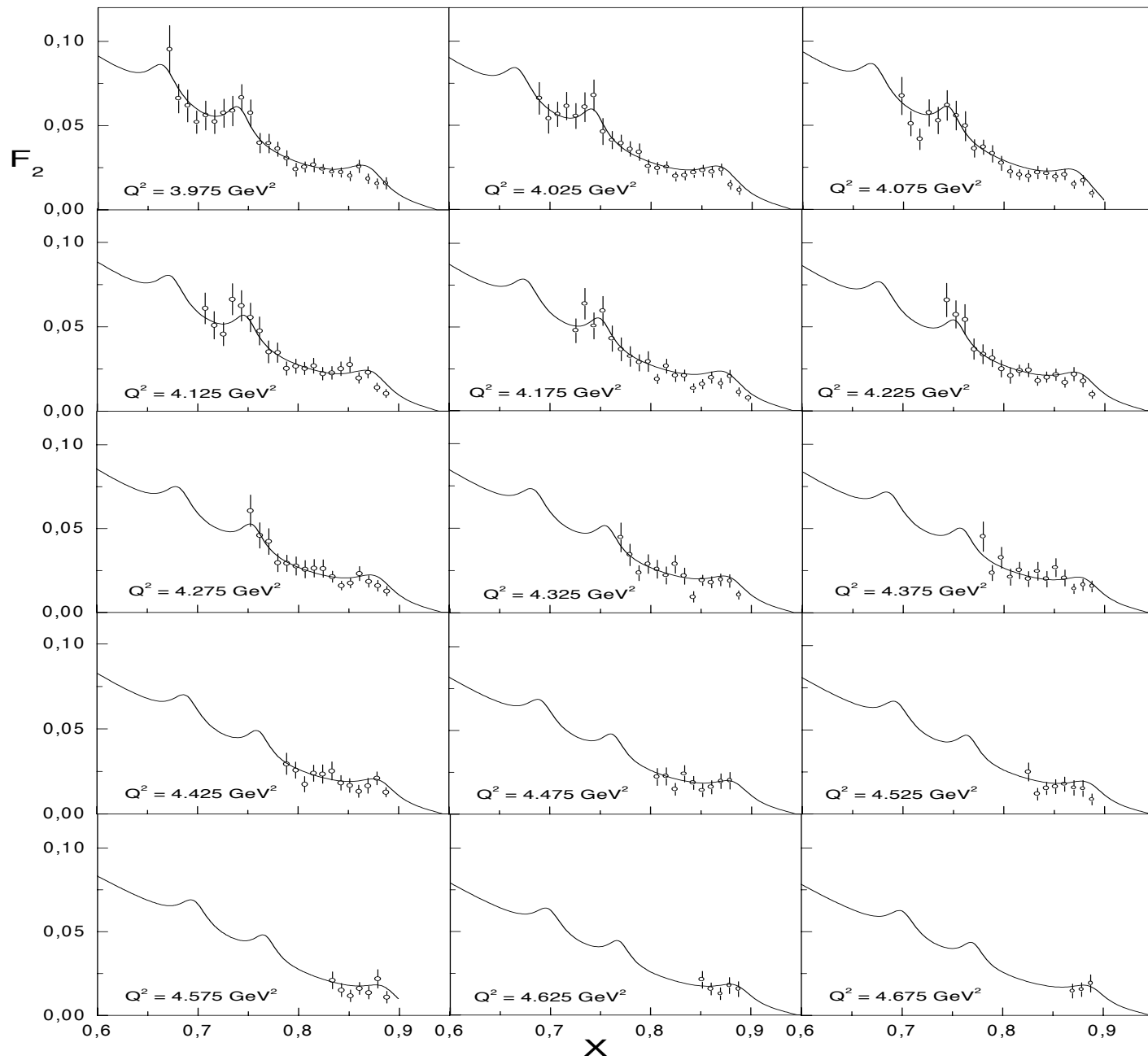
The center of mass energy of the γ^*p system, the negative squared photon virtuality Q^2 and the Bjorken variable x are related by

$$s = W^2 = Q^2(1-x)/x + m^2.$$

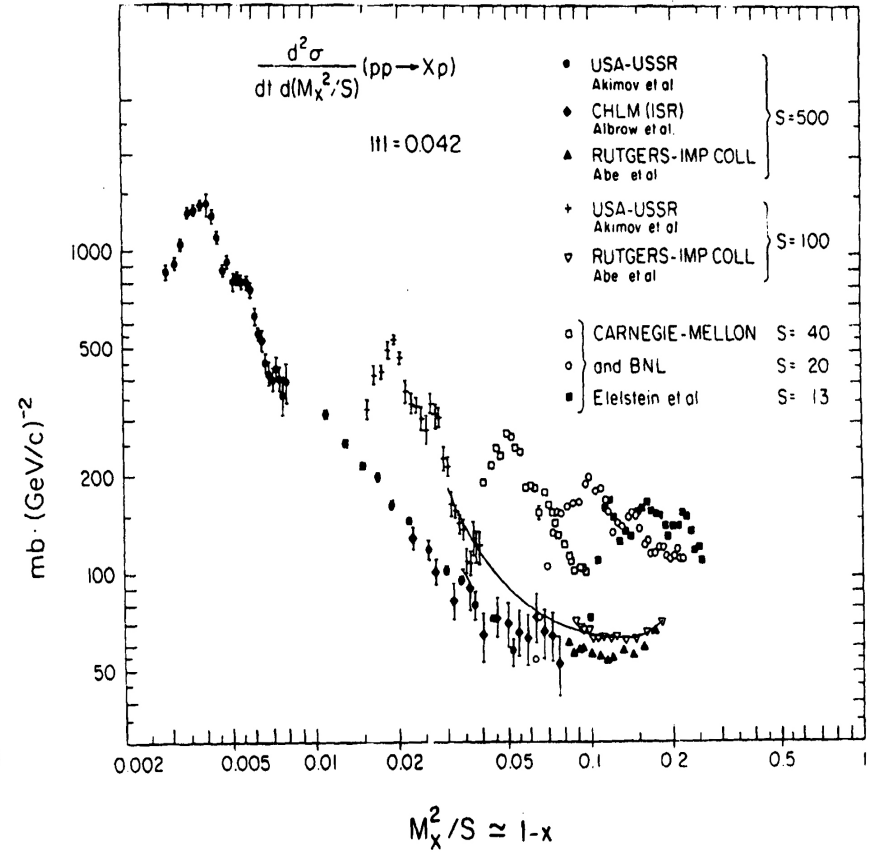
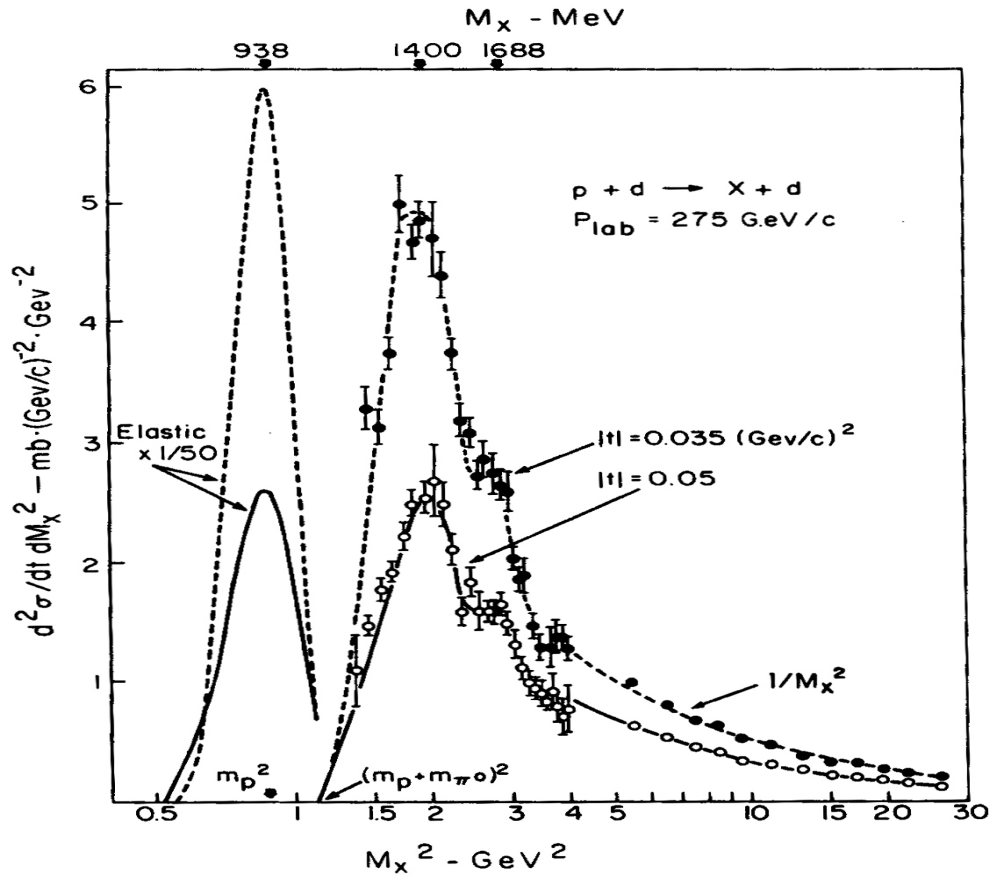


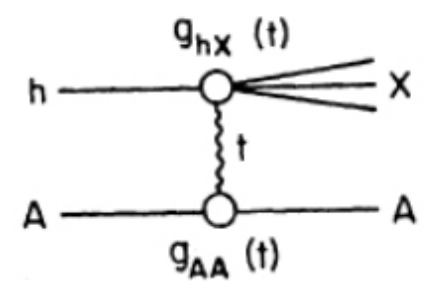
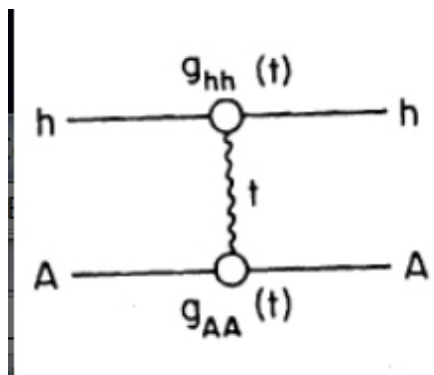






FNAL





$$\frac{d^2\sigma}{dtdx} = \left| \begin{array}{c} h \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ p \end{array} \right|^2 = \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ t \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ p \end{array} = \begin{array}{c} h \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ p \end{array}$$

$$\sigma_{\text{tot}} = \left| \begin{array}{c} h \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ p \end{array} \right|^2 = \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ p \end{array} = \begin{array}{c} h \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ p \end{array}$$

Similar to the case of elastic scattering, the double differential cross section for the SDD reaction, by Regge factorization, can be written as

$$\frac{d^2\sigma}{dt dM_X^2} = \frac{9\beta^4 [F^P(t)]^2}{4\pi \sin^2[\pi\alpha_P(t)/2]} (s/M_X^2)^{2\alpha_P(t)-2} \times \quad (1)$$

$$\left[\frac{W_2}{2m} \left(1 - M_X^2/s\right) - mW_1(t + 2m^2)/s^2 \right],$$

where W_i , $i = 1, 2$ are related to the structure functions of the nucleon and $W_2 \gg W_1$. For high M_X^2 , the $W_{1,2}$ are Regge-behaved, while for small M_X^2 their behavior is dominated by nucleon resonances. The knowledge of the inelastic form factors (or transition amplitudes) is crucial for the calculation of low-mass diffraction dissociation.

The pp scattering amplitude

$$A(s, t)_P = -\beta^2 [f^u(t) + f^d(t)]^2 \left(\frac{s}{s_0}\right)^{\alpha_P(t)-1} \frac{1 + e^{-i\pi\alpha_P(t)}}{\sin \pi\alpha_P(t)}, \quad (1)$$

where $f^u(t)$ and $f^d(t)$ are the amplitudes for the emission of u and d valence quarks by the nucleon, β is the quark-Pomeron coupling, to be determined below; $\alpha_P(t)$ is a vacuum Regge trajectory. It is assumed that the Pomeron couples to the proton via quarks like a scalar photon.

A single-Pomeron exchange is valid at the LHC energies, however at lower energies (e.g. those of the ISR or the SPS) the contribution of non-leading Regge exchanges should be accounted for as well.

Thus, the unpolarized elastic pp differential cross section is

$$\frac{d\sigma}{dt} = \frac{[3\beta F^p(t)]^4}{4\pi \sin^2[\pi\alpha_P(t)/2]} (s/s_0)^{2\alpha_P(t)-2}. \quad (2)$$

The final expression for the double differential cross section reads:

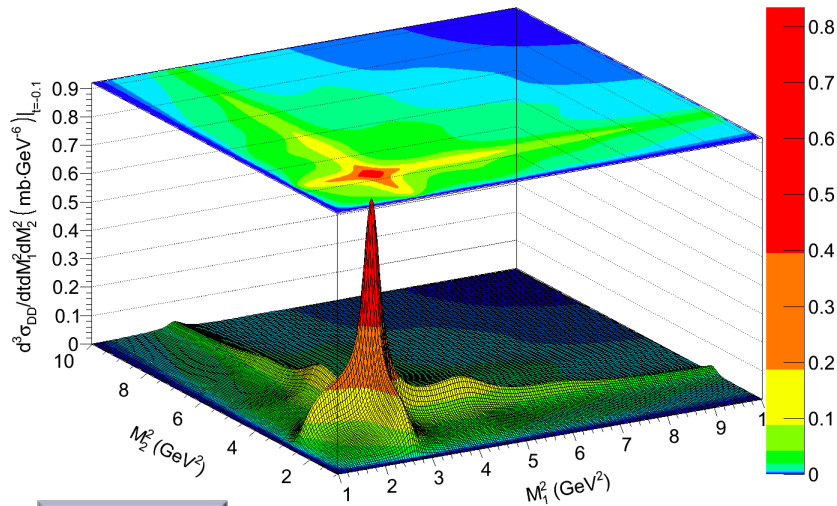
$$\begin{aligned}
 \frac{d^2\sigma}{dt dM_X^2} = & \\
 A_0 \left(\frac{s}{M_X^2} \right)^{2\alpha_P(t)-2} & \frac{x(1-x)^2 [F^p(t)]^2}{(M_x^2 - m^2) \left(1 + \frac{4m^2 x^2}{-t}\right)^{3/2}} \times \\
 \sum_{n=1,3} & \frac{[f(t)]^{2(n+1)} \text{Im } \alpha(M_X^2)}{(2n + 0.5 - \text{Re } \alpha(M_X^2))^2 + (\text{Im } \alpha(M_X^2))^2} .
 \end{aligned} \tag{1}$$

SD and DD cross sections

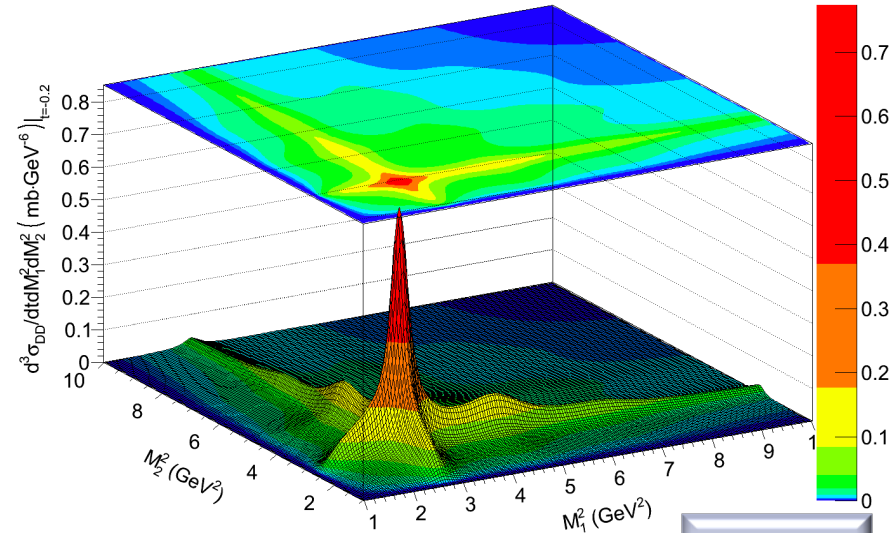
$$\frac{d^2\sigma_{SD}}{dt dM_x^2} = F_p^2(t) F(x_B, t) \frac{\sigma_T^{Pp}(M_x^2, t)}{2m_p} \left(\frac{s}{M_x^2}\right)^{2(\alpha(t)-1)} \ln\left(\frac{s}{M_x^2}\right)$$

$$\begin{aligned} \frac{d^3\sigma_{DD}}{dt dM_1^2 dM_2^2} &= C_n F^2(x_B, t) \frac{\sigma_T^{Pp}(M_1^2, t)}{2m_p} \frac{\sigma_T^{Pp}(M_2^2, t)}{2m_p} \\ &\times \left(\frac{s}{(M_1 + M_2)^2}\right)^{2(\alpha(t)-1)} \ln\left(\frac{s}{(M_1 + M_2)^2}\right) \end{aligned}$$

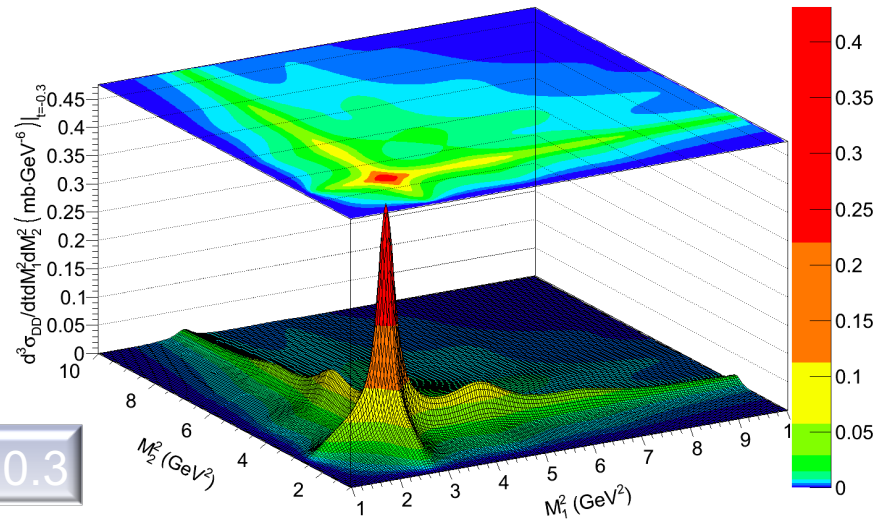
Triple differential DD cross sections



$t = -0.1$

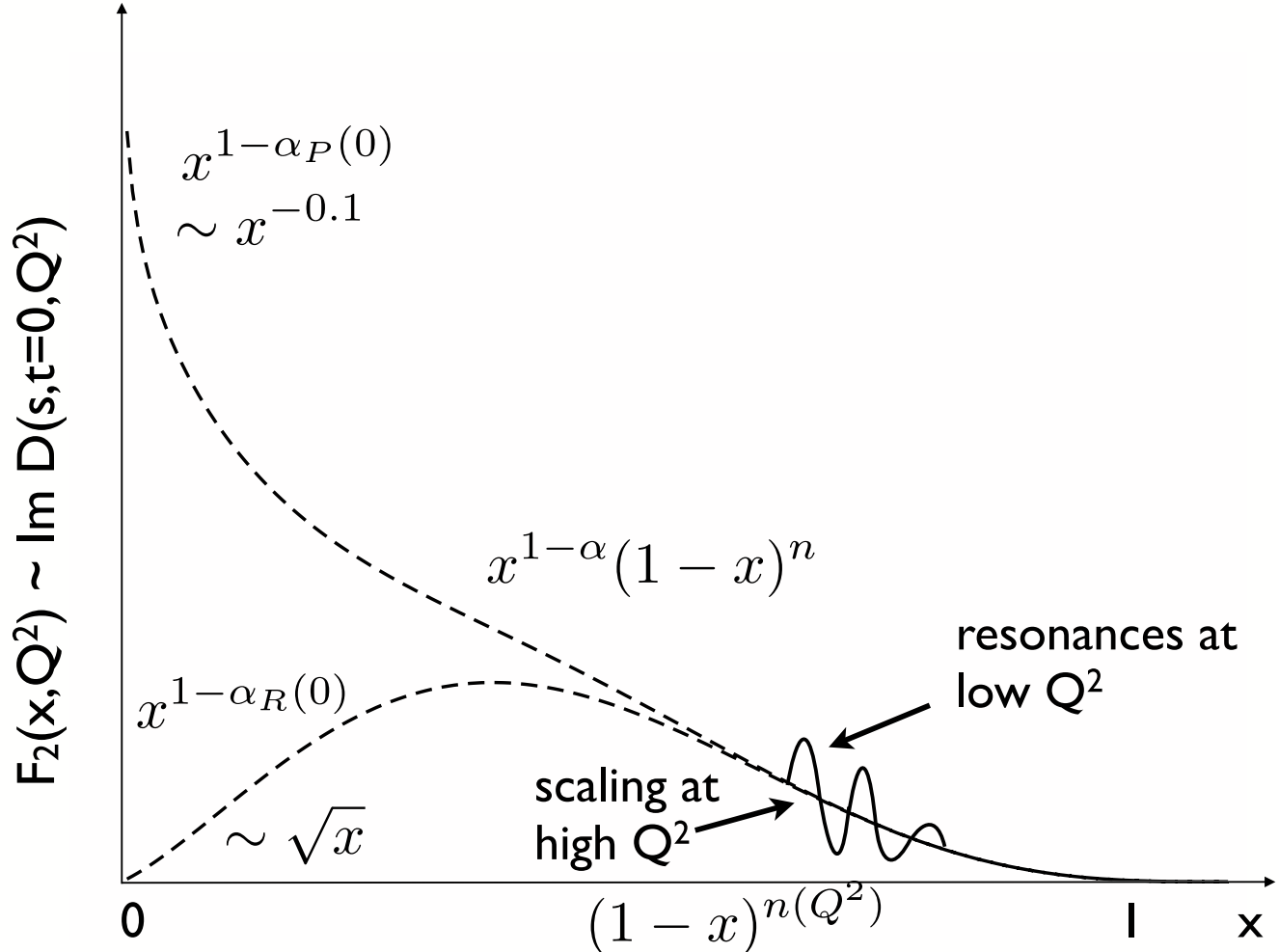


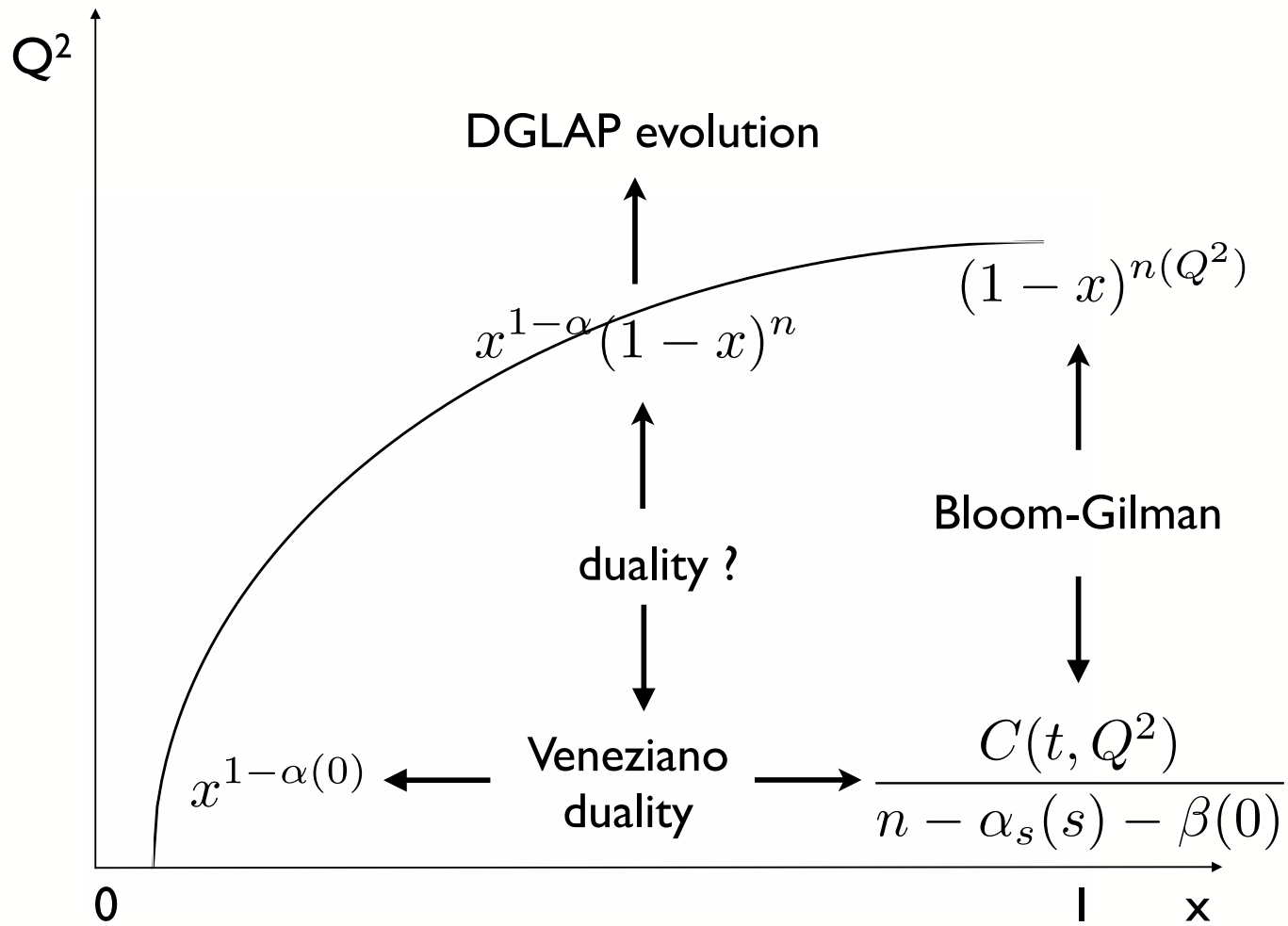
$t = -0.2$



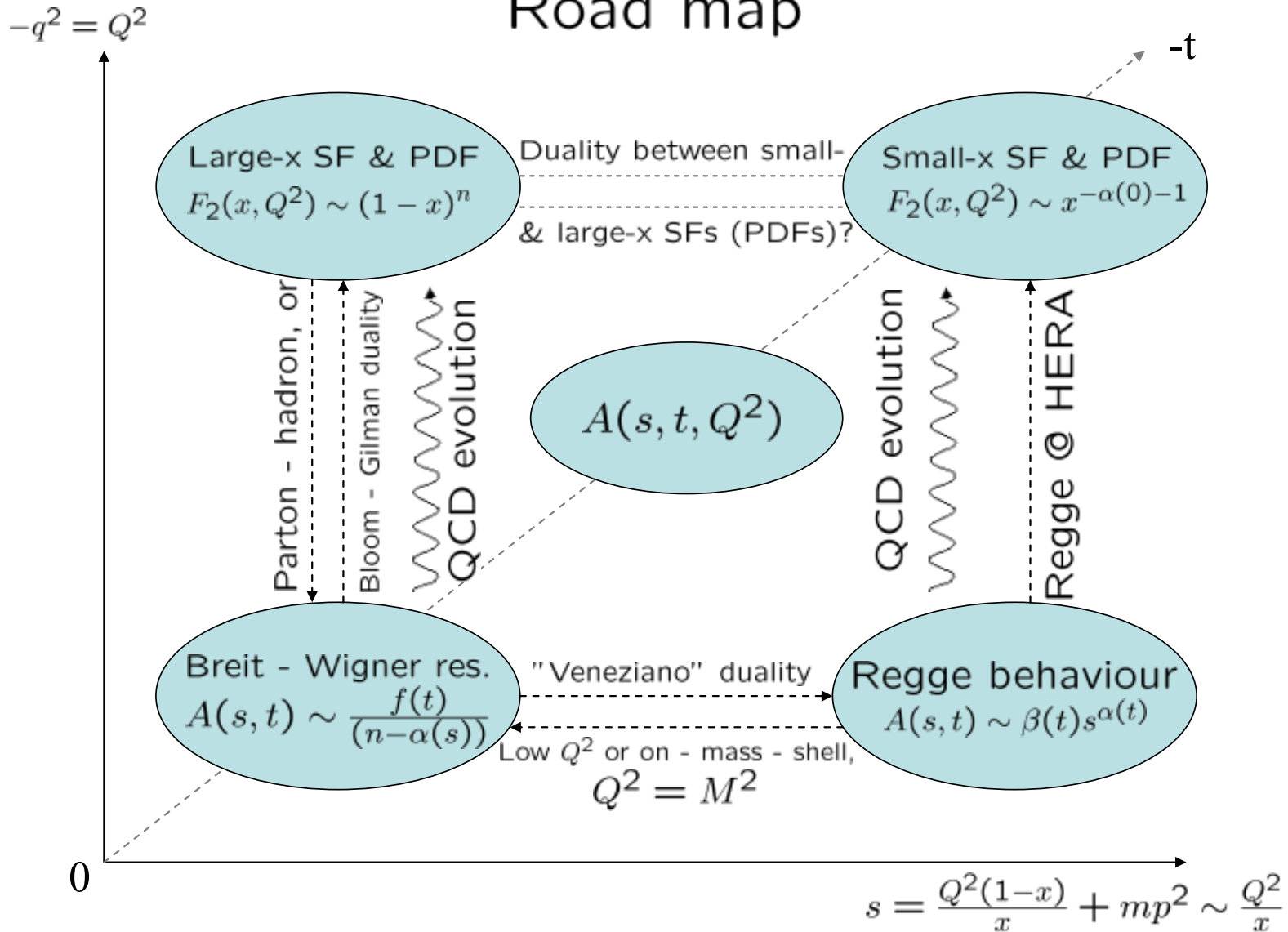
$t = -0.3$

L.L. Jenkovszky, V.K. Magas, J.T. Londergan, A.P. Szczepaniak,
Model Realizing Parton-Hadron Duality,
arXiv:1204.2216





Road map



Thank you!

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