

Low-energy interactions of heavy quarkonium with matter: pentaquarks, tetraquarks, and chromoelectric polarizabilities*

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Outline

- **motivation**
 - quarkonium bound in light hadron: hadrocharmonium
- **effective interaction of quarkonia with hadrons**
 - chromoelectric polarizabilities
 - chromoelectric field strength
- **hadrocharmonia**
 - pentaquarks and tetraquarks
 - predictions and tests
- **lattice QCD**
 - $\alpha(1S)$ and $\alpha(2S)$
 - possibility of pentaquarks
- **EIC**
 - what can we study?
 - building bridges

* supported by NSF

Motivation

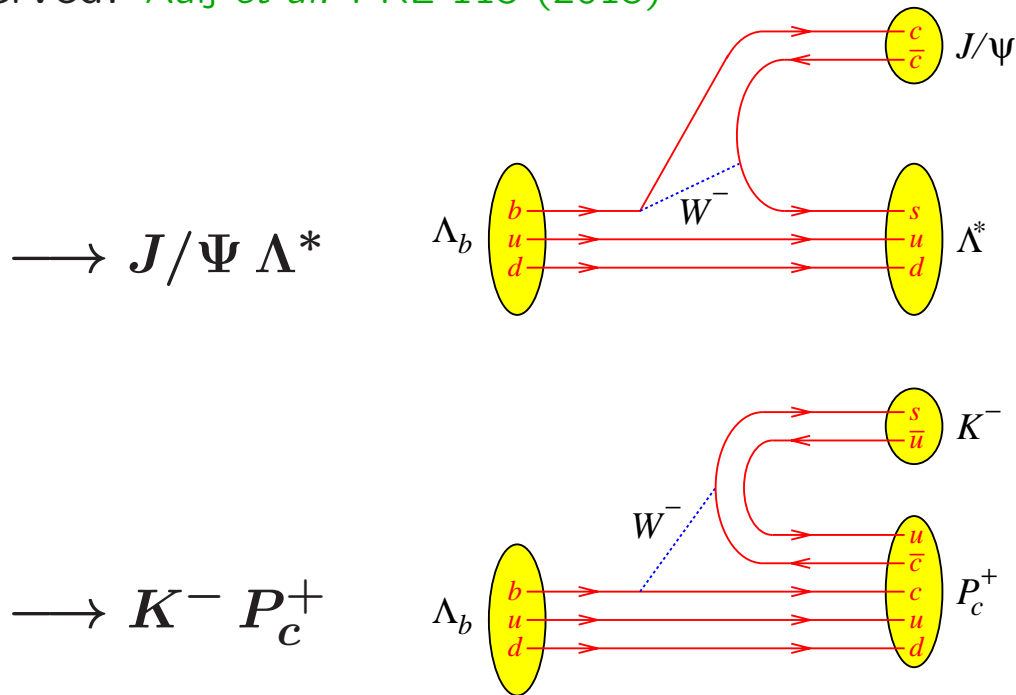
- hypothetical process:
 - capture of (small-size) quarkonium in (large-size) light hadron or nucleus
- in principle remote(!) analogy to:
 - “muon capture” in muonic atoms
- if this was possible(?) for charmonia:
opportunity to study slow charmonia in matter!
- in practice the life time of J/ψ with 7×10^{-21} s short for:
 - producing charmonium (typically at high energies)
 - slowing down charmonium in nuclear matter
 - waiting for bound state to form
- more promising: take advantage of weak decays
 - e.g. $\Lambda_b^0 \rightarrow J/\Psi p K^-$ branching ratio $(3.2_{-0.5}^{+0.6}) \times 10^{-4}$
 - explore configurations of $J/\psi p$ with low relative momentum
 - done at LHCb

hidden-charm pentaquarks in $\Lambda_b^0 \longrightarrow J/\psi p K^-$ at LHCb

- “kinematical configuration” possible
where $\bar{c}c$ slow with respect to nucleon
 \Rightarrow “enough time” to form resonance

Λ_b^0 $m = 5.6$ GeV, $\tau = 1.5$ ps
 J/ψ $m = 3.1$ GeV, $\Gamma = 93$ keV, $\Gamma_{\mu^+\mu^-} = 6\%$
 Λ^* $m \geq 1.4$ GeV, subsequently $\Lambda^* \rightarrow K^- p$

- observed! [Aaij et al. PRL 115 \(2015\)](#)



state	m [MeV]	Γ [MeV]	Γ_{rel}	mode	J^P
$P_c^+(4380)$	$4380 \pm 8 \pm 29$	$205 \pm 18 \pm 86$	$(4.1 \pm 0.5 \pm 1.1)\%$	$J/\psi p$	$\frac{3}{2}^-$ or $\frac{5}{2}^+$
$P_c^+(4450)$	$4450 \pm 2 \pm 3$	$39 \pm 5 \pm 19$	$(8.4 \pm 0.7 \pm 4.2)\%$	$J/\psi p$	$\frac{5}{2}^\pm$ or $\frac{3}{2}^-$

observation of resonances in J/ψ -nucleon-spectrum

- resonances in J/ψ p -spectrum in decay mode $\Lambda_b^0 \rightarrow J/\psi p K^-$ at LHCb
[Aaij et al. PRL 115, 072001 \(2015\)](#)
- $p K^-$ -resonant or nonresonant contributions cannot explain it [Aaij et al. PRL 117, 082002 \(2016\)](#)
- analysis of $\Lambda_b \rightarrow J/\psi p \pi^-$ decay mode provides support for existence of pentaquark states
[Aaij et al. PRL 117, 082003 \(2016\)](#)
- preparing independent confirmation e.g. in photoproduction at JLab, Hall-C proposal [Meziani et al, PR12-16-007, arXiv:1609.00676 \[hep-ex\]](#)
 πp collisions in J-PARC charm spectroscopy program [S.H.Kim, H.C.Kim, A.Hosaka, PLB763 \(2016\) 358](#)

theoretical approaches (non-exhaustive list)

- loosely bound (“molecular”) charmed baryon-meson states: [Chen, Liu, Li, Zhu, PRL 115, 132002 \(2015\)](#);
[Chen, Chen, Liu, Steele, Zhu, PRL 115, 172001 \(2015\)](#); [Roca, Nieves, Oset, PRD 92, 094003 \(2015\)](#);
[J.He, PLB 753, 547 \(2016\)](#), [Yamaguchi, Santopinto PRD96 \(2017\) 014018](#)
- bound states of light and heavy diquarks including c -quarks: [Maiani, Polosa, Riquer, PLB 749, 289 \(2015\)](#);
[Anisovich, Matveev, Nyiri, Sarantsev, Semenova, arXiv:1507.07652](#); [Lebed, PLB 749, 454 \(2015\)](#);
[Li, He, He, J. High Energy Phys. 12 \(2015\) 128](#)
- possibility of open-color bound states explored:
[Mironov, Morozov, JETP Lett. 102, 271 \(2015\)](#)
- credible explanation for broader $P_c(4380)$: threshold cusp effect [Meißner, Oller, PLB 751, 59 \(2015\)](#);
[Mikhasenko, arXiv:1507.06552](#); [Guo, Meißner, Wang, Yang, PRD D 92, 071502 \(2015\)](#)
- appealing approach to $P_c(4450) = \text{hadrocharmonium}$ [Eides, Petrov, Polyakov, PRD 93, 054039 \(2016\)](#);
[Perevalova, Polyakov, Schweitzer, PRD 94, 054024 \(2016\)](#); [Eides, Petrov, Polyakov, EPJ C78, 36 \(2018\)](#)

hadrocharmonia

- effective interaction

$\bar{c}c$ -system small in heavy quark limit $\ll R_{\text{nucleon}}$

\Rightarrow non-relativistic multipole expansion [Gottfried, PRL 40 \(1978\) 598](#)

baryon-quarkonium interaction dominated by emission of
2 virtual chromoelectric dipole gluons in a color singlet state

$$V_{\text{eff}} = -\frac{1}{2} \alpha \vec{E}^2 \quad \text{Voloshin, Yad. Fiz. 36, 247 (1982)}$$

- ingredients:

α = chromoelectric polarizability property of quarkonium

\vec{E}^2 = chromoelectric field strength in nucleon

chromoelectric polarizability α

- describes effective interaction of a hadron with soft gluonic fields
 - in principle, property of each hadron (immersed in a gluonic back ground field)
- analogous to electric polarizability of neutral atom in electric field
 - induced dipole moments
 - van der Waals interactions
 - exact result: $\alpha_{\text{H-atom}} = \frac{9}{2} R_{\text{Bohr}}^3$
- practical importance for quarkonia
 - $R_{\text{quarkonium}} \rightarrow 0$ in heavy quark limit $m_Q \rightarrow \infty$
- plays important role for many applications
 - hadrocharmonia
 - interaction of slow charmonia with nuclear medium
 - hadronic transitions between charmonium resonances
 - photo/hadro-production of charmonia, charmed hadrons

- perturbative QCD calculation for α of quarkonia

- heavy quark + large N_c limit (Coulomb system): $\alpha(nS)_{\text{pert}} = \frac{16\pi n^2 c_n}{3g_c^2 N_c^2} a_0^3$, $a_0 = \frac{16\pi}{g_c^2 N_c m_Q}$
 $c_1 = 7/4$, $c_2 = 251/8$, $c_n = (5/16)n^2(7n^2 - 3)$ for $n \geq 3$

Peskin, Bhanot & Peskin (1979)

- practical estimates for charmonia can vary (depending how one evaluates):

$$\begin{array}{lll} \alpha(1S)_{\text{pert}} \approx 0.2 \text{ GeV}^{-3} & \alpha(2S)_{\text{pert}} \approx 14 \text{ GeV}^{-3} & \text{Eides, Petrov, Polyakov, PRD 93 (2016)} \\ \alpha(1S)_{\text{pert}} \approx 4.1 \text{ GeV}^{-3} & \alpha(2S)_{\text{pert}} \approx 296 \text{ GeV}^{-3} & \text{J. Ferretti, Phys.Lett.B782 (2018) 702} \end{array}$$

discrepancy: estimate "Bohr radius" $a_0 =$ size of a hadron in perturbative QCD(?)

- use transitional polarizability to "test" perturbative calculation:

$$\alpha(2S \rightarrow 1S)_{\text{pert}} = - \frac{51200\sqrt{2}\pi}{1287g_c^2 N_c^2} \text{ perturbative calculation Peskin (1979)}$$

$$\alpha(2S \rightarrow 1S)_{\text{pert}} \approx -0.6 \text{ GeV}^{-3} \text{ from Eides, Petrov, Polyakov, PRD 93 (2016)}$$

$$|\alpha(2S \rightarrow 1S)|_{\text{pheno}} \approx 2 \text{ GeV}^{-3} \text{ analysis of } \psi' \rightarrow J/\psi \pi \pi \text{ decays Voloshin (2008)}$$

- perturbative QCD results: rough guideline (to be used with caution)

chromoelectric field strength \vec{E}^2

- explore trace anomaly

$$\vec{E}^2 = g_c^2 \left(\frac{8\pi^2}{bg_s^2} T^\mu{}_\mu + T_{00}^G \right)$$

$b = \frac{11}{3} N_c - \frac{2}{3} N_F$ leading coeff. of β -function

g_s strong coupling at low (nucleon) scale $\lesssim 1$ GeV

$g_c =$ strong coupling at scale of heavy quark ($g_c \neq g_s$)

$T_{00}^G = \xi T_{00}$ with $\xi =$ fraction of gluon contribution to M_N

$T^\mu{}_\mu = T^{00} + T^{ii}$, stress tensor $T^{ij} = \left(\frac{r^i r^j}{r^2} - \frac{1}{3} \delta^{ij} \right) s(r) + \delta^{ij} p(r)$

- universal effective potential

$$V_{\text{eff}} = -\frac{1}{2} \alpha \frac{8\pi^2}{b} \frac{g_c^2}{g_s^2} \left[\nu T_{00}(r) + 3p(r) \right], \quad \nu = 1 + \xi_s \frac{b g_s^2}{8\pi^2}$$

$\nu \approx 1.5$ estimate by Eides et al, op. cit.
Novikov, Shifman, Z.Phys.C8, 43 (1981)
X. D. Ji, Phys.Rev.Lett. **74**, 1071 (1995)

- nonperturbative nucleon properties:

$T_{00}(r)$ energy density: $\int d^3r T_{00}(r) = M_N$

$p(r)$ pressure distribution: $\int dr r^2 p(r) = 0$

densities of energy-momentum tensor

Polyakov, PLB 555, 57 (2003)

for a review see Polyakov and Schweitzer,

Int.J.Mod.Phys.A 33 (2018) 1830025

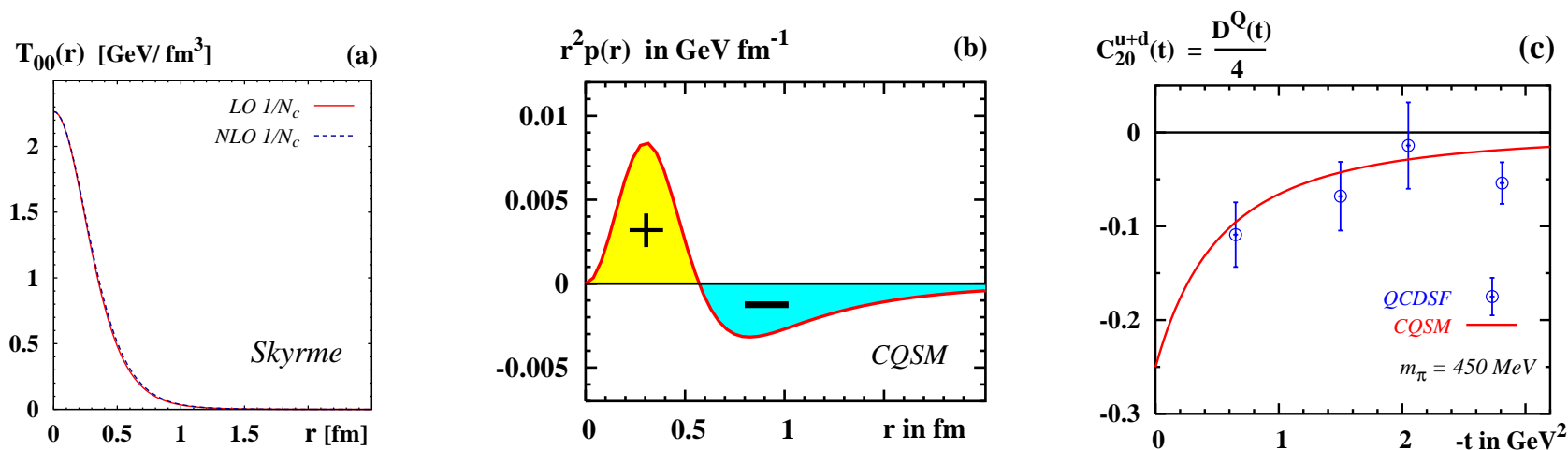
- for $T_{00}(r)$, $p(r)$ needed: non-perturbative computations or experiment

chiral quark soliton model [Goeke et al, PRD 75, 094021 \(2007\)](#)

Skyrme model [Cebulla et al, NPA 794, 87 \(2007\)](#)

lattice [Hägler et al PRD 68, 034505 \(2003\)](#);

[Shanahan, Detmold, arXiv:1810.07589](#)



future: EMT form factors from hard exclusive reactions

via generalized parton distribution functions (GPDs)

very first insights from phenomenology/experiment:

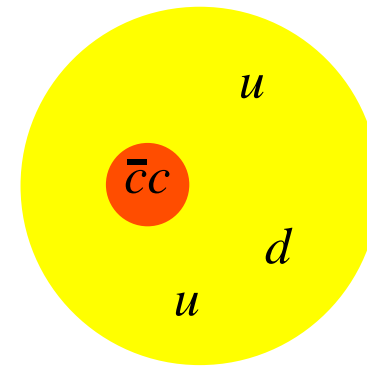
[Kresimir Kumerički, Dieter Müller, arXiv:1512.09014](#);

[Burkert, Elouadrhiri, Girod, Nature 557 \(2018\) 396](#).

- compute quarkonium-nucleon bound state

$$\text{solve } \left(-\frac{\vec{\nabla}^2}{2\mu} + V_{\text{eff}}(r) \right) \psi = E_{\text{bind}} \psi$$

$\mu =$ reduced quarkonium-baryon mass



- results:

nucleon and J/ψ form no bound state

nucleon and $\psi(2S)$ form 2 bound states

for $\alpha(2S) \approx 17 \text{ GeV}^{-3}$

nearly degenerate masses around 4450 MeV

$L = 0$ channel, $J^P = \frac{1}{2}^-, \frac{3}{2}^-$ compatible with LHCb

mass-splitting $\mathcal{O}(10) \text{ MeV}$ (suppressed in heavy quark limit)

decay: width of $\psi(2S)$ ca. 200keV (practically stable)

“wait” for $2S \rightarrow 1S$ transition in background gluon field

governed by V_{eff} with $|\alpha(2S \rightarrow 1S)| \sim 2 \text{ GeV}^{-3} \ll \alpha(2S) \approx 17 \text{ GeV}^{-3} \Rightarrow$ “takes” time!

narrow width $\Gamma = |\alpha(2S \rightarrow 1S)|^2 \times \dots =$ few tens of MeV \Rightarrow compatible with LHCb

narrow $P_c(4450) = \psi(2S)$ -nucleon bound state, broad $P_c(4380)$ not

- approach can be tested

predictions for bound states of $\psi(2S)$ with Δ

Perevalova, Polyakov, Schweitzer, PRD 94, 054024 (2016)

predictions for bound states of $\psi(2S)$ with hyperons

Eides, Petrov, Polyakov, EPJ C78, 36 (2018)

$X(4274)$ resonance in $J/\psi \phi$ system Aaij et al, PRD 95 (2017) 012002

candidate for $\psi(2S)$ - ϕ hadrocharmonium (tetraquark $\bar{c}c\bar{s}s$)

concluded despite knowing nothing about ϕ -meson EMT densities

characteristic relation of mass-width in hadrocharmonium picture

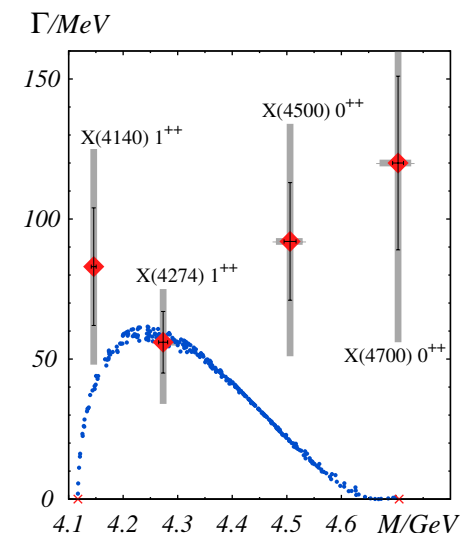
Panteleeva, Perevalova, Polyakov, Schweitzer, arXiv:1802.09029

- so far:

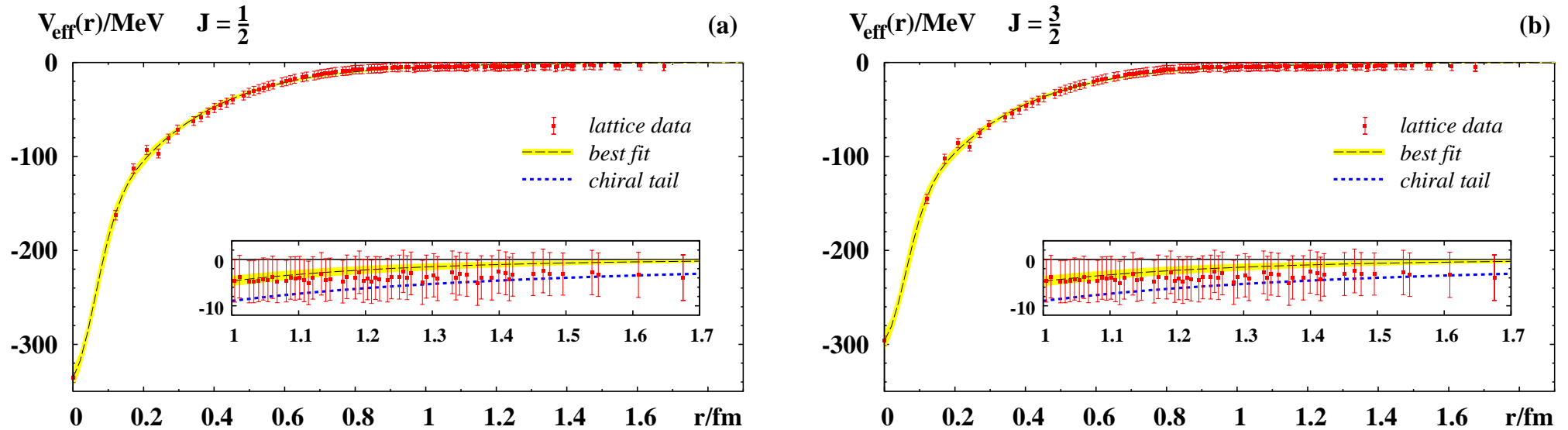
compatible with experiment

compatible with lattice study

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lattice study of nucleon J/ψ potential



lattice: 2+1 light Wilson clover quarks, $16^3 \times 32$, $a = 0.1209\text{fm}$, $m_\pi = 875\text{ MeV}$

T.Sugiura, Y.Ikeda, N.Ishii, arXiv:1711.11219 [hep-lat]

- $J = \frac{1}{2}$ and $\frac{3}{2}$ channels agree (except for 1 bin at $r = 0$) \Rightarrow $1/m_Q$ corrections small

- normalization $\int d^3r V_{\text{eff}}(r) = -\alpha(1S) \frac{4\pi^2}{b} \frac{g_c^2}{g_s^2} \nu M_N$

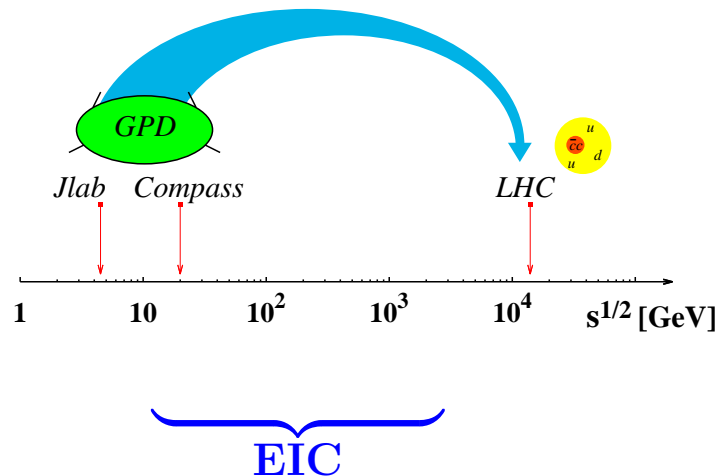
- **nonperturbative determination of $\alpha(1S) = (1.6 \pm 0.8) \text{ GeV}^{-3}$**

- $P_c(4450) = \psi(2S)$ -nucleon bound state for $\frac{\alpha(2S)}{\alpha(1S)} = (15 \pm 1)$
Polyakov, Schweitzer PRD98 (2018) 034030

- similar values can be estimated from J/ψ -nucleon scattering wave-lengths
Ferretti, Santopinto arXiv:1806.02489

what can EIC contribute?

- measurements of hard-exclusive reactions
generalized parton distributions (GPDs) \rightarrow EMT densities
- interaction of slow J/ψ , $\psi(2S)$ with nuclear matter
cross section determined by $\alpha(1S)$, $\alpha(2S)$
- direct production of pentaquarks $P_c(4450)$
test hadrocharmonium picture



Thank you!