

Electromagnetic probes from a parton cascade

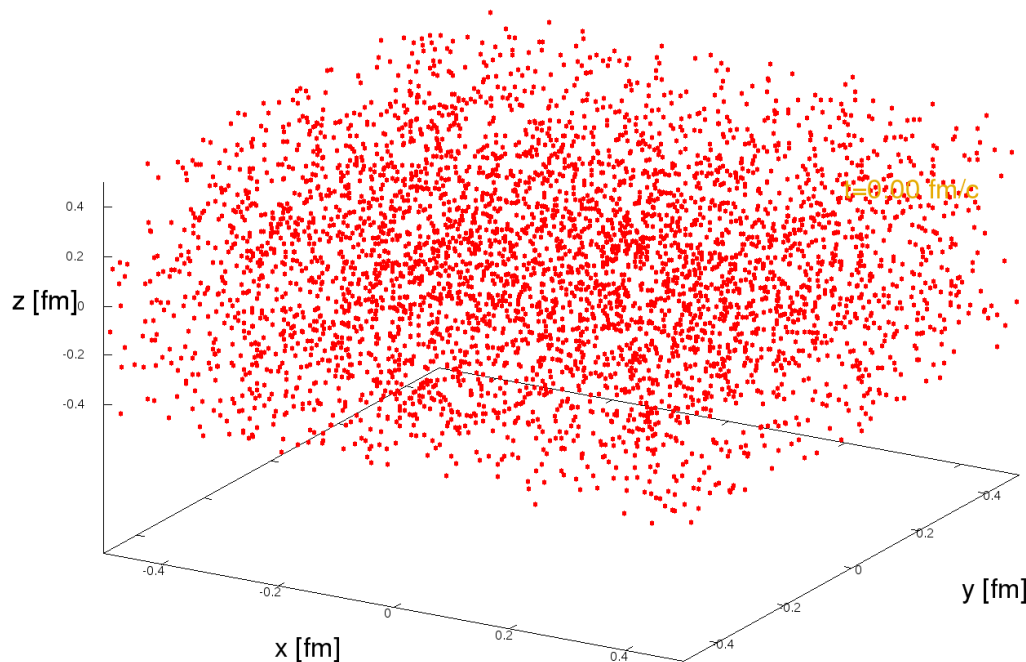
Moritz Greif

in collaboration with
Carsten Greiner, Sören Schlichting,
Florian Senzel, Zhe Xu

Phys.Rev. C95, 054903, 2017

Phys.Rev. C96, 014903, 2017

Parton cascade „BAMPS“



Solves the Boltzmann equation
(numerically exact, Monte Carlo)

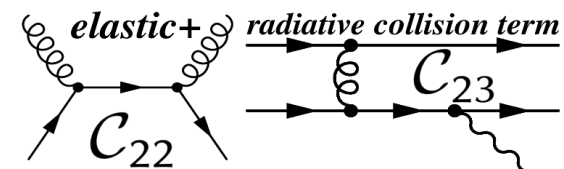
← " $f(x, p)$ "
Single
particle
distribution
function

- Quarks + Gluons
- pQCD cross sections
- Elastic + radiative scattering
- Ideal equation of state

Used as model for heavy-ion collision:
Expanding 3+1d geometry,
Different initial states

BAMPS: Boltzmann Approach to Multi-Parton Scatterings

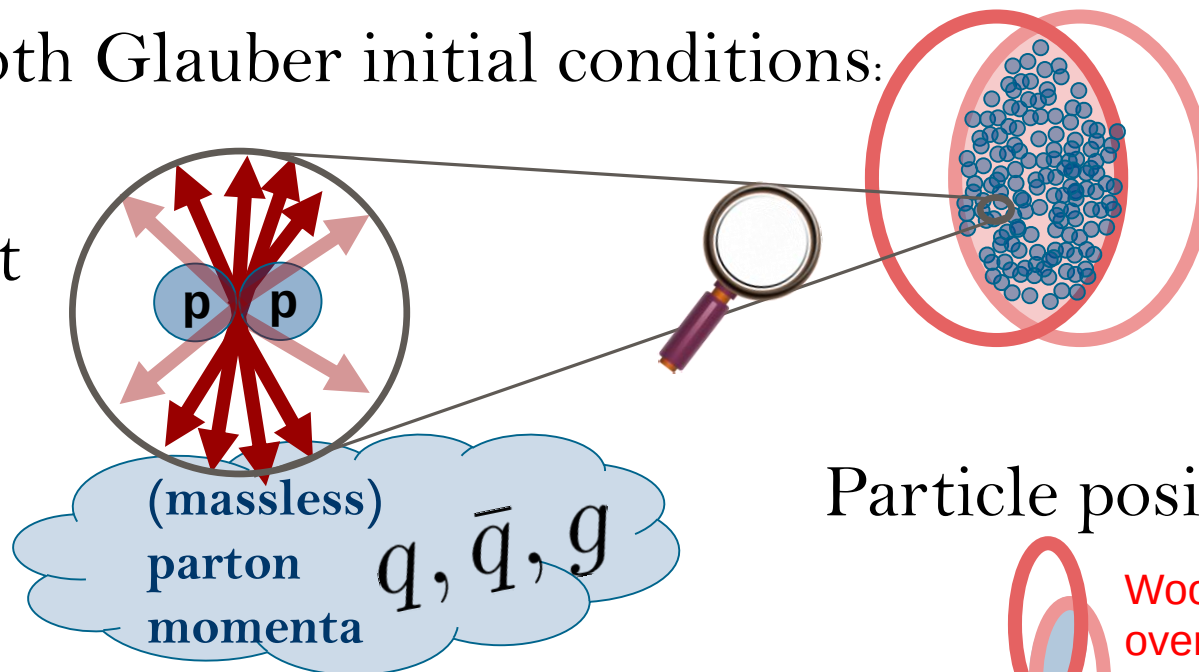
$$p^\mu \partial_\mu f(x, p) = C_{22}[f] + C_{23}[f]$$



Initial state in „BAMPS“

Smooth Glauber initial conditions:

Pythia event
generator:



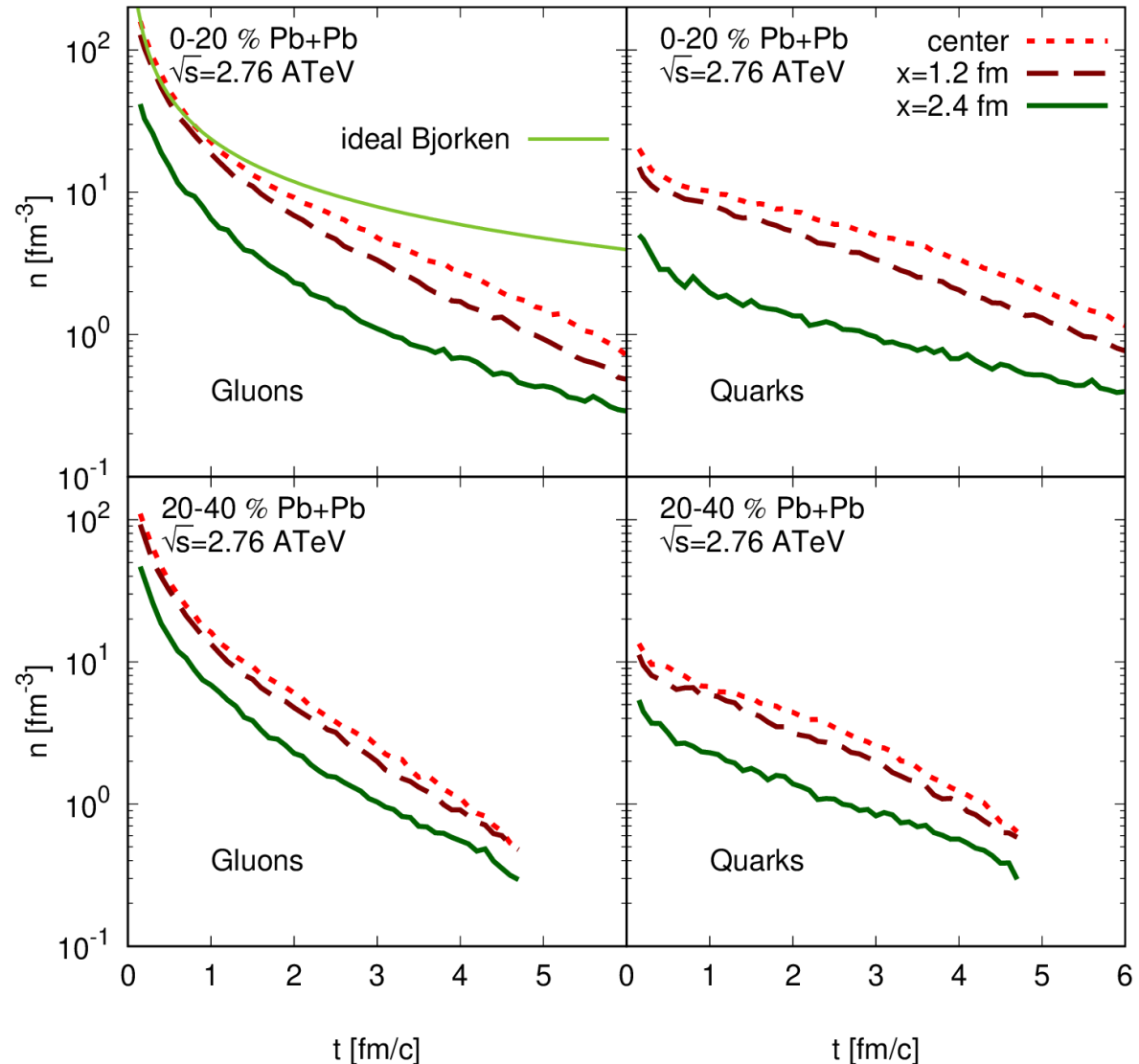
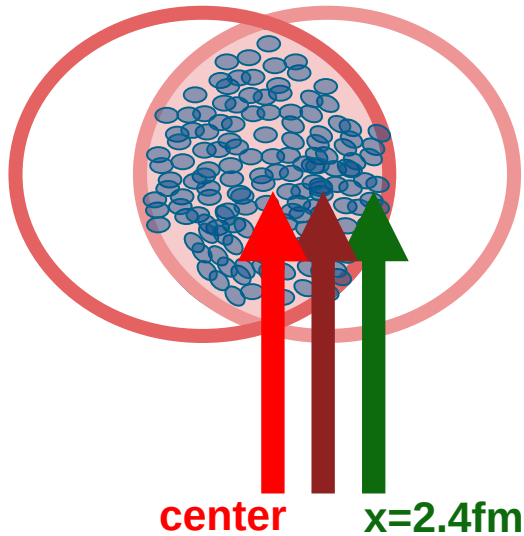
Hard partons scale with N_{binary}

Soft partons scale with $\sim 0.1 N_{binary}$

Formation time: $t_{form} = \frac{1}{p_T} \cosh y$
(only if $t > t_{form}$ interactions allowed)

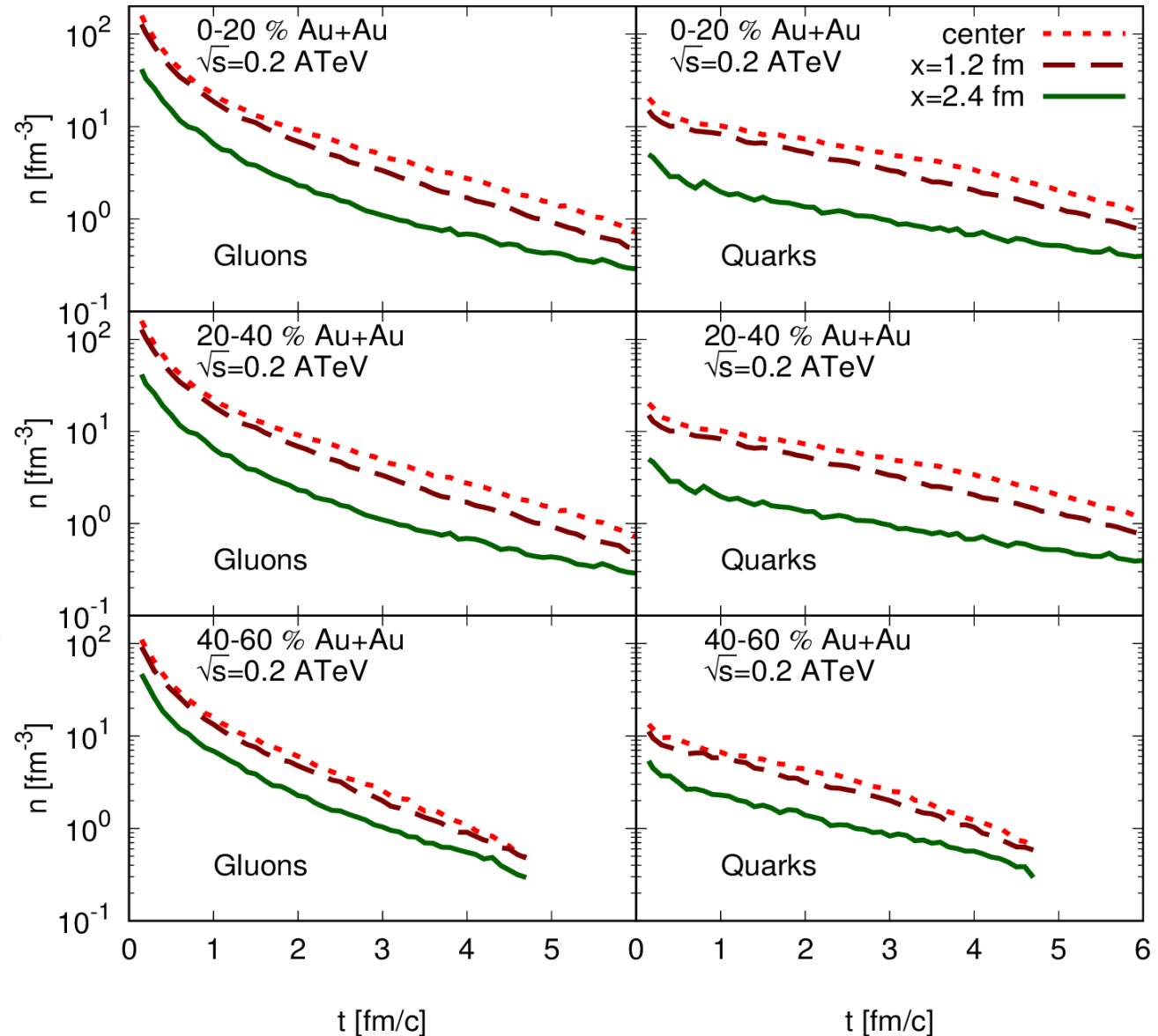
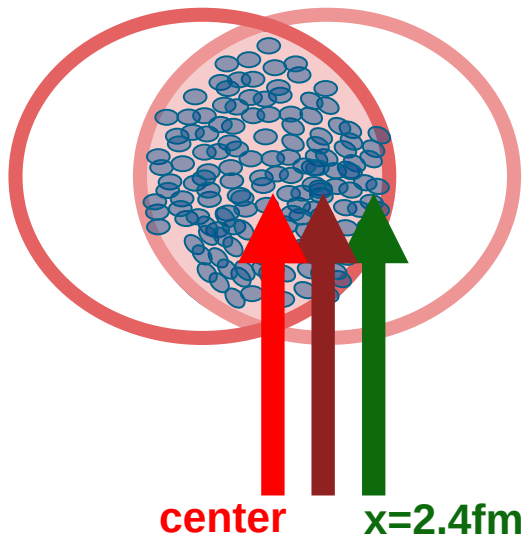
Thermodynamic Evolution

Particle
density n at
midrapidity



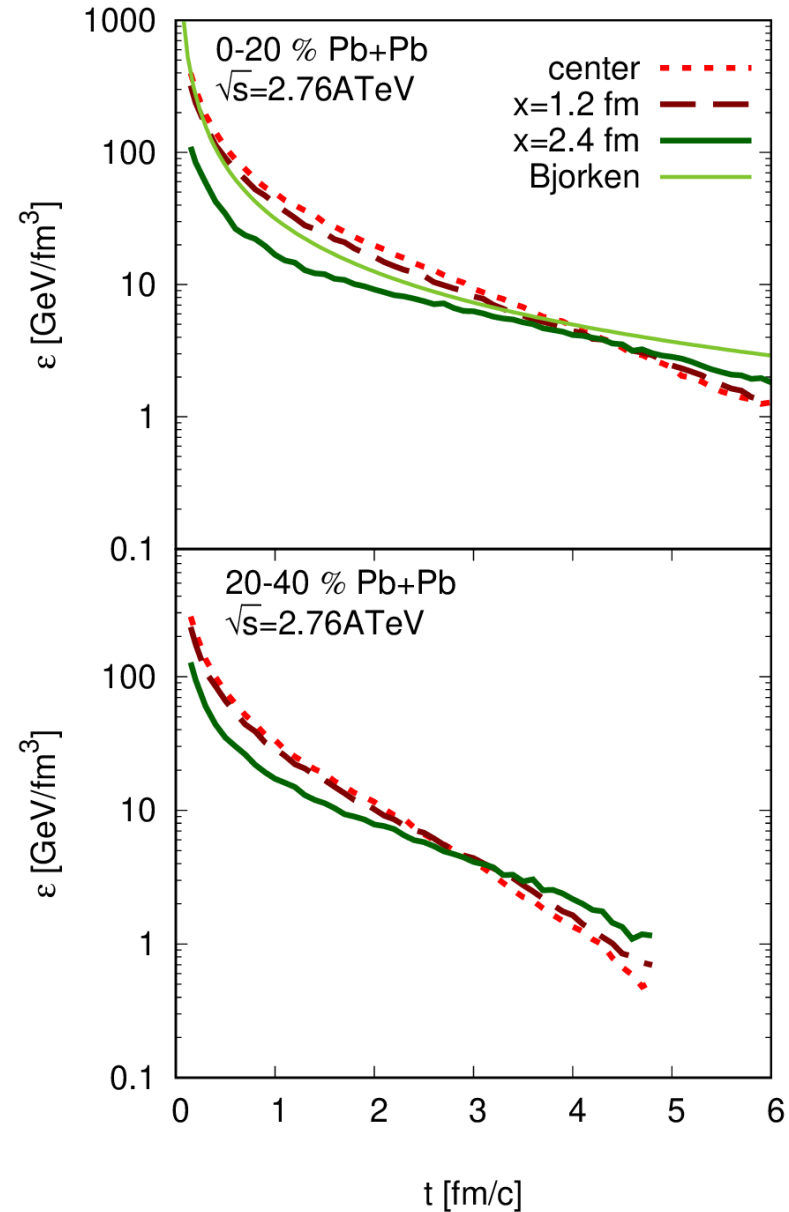
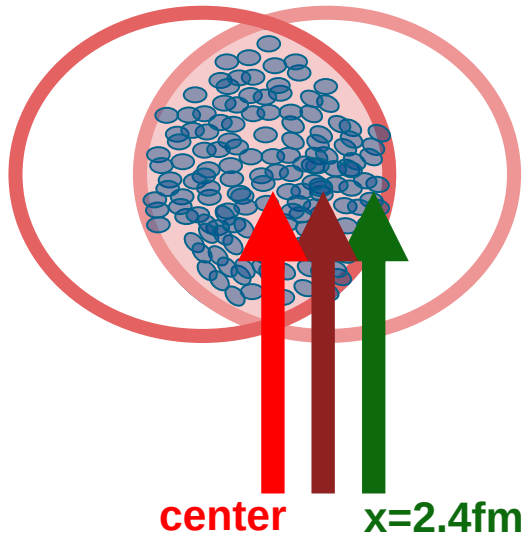
Thermodynamic Evolution

Particle
density n at
midrapidity



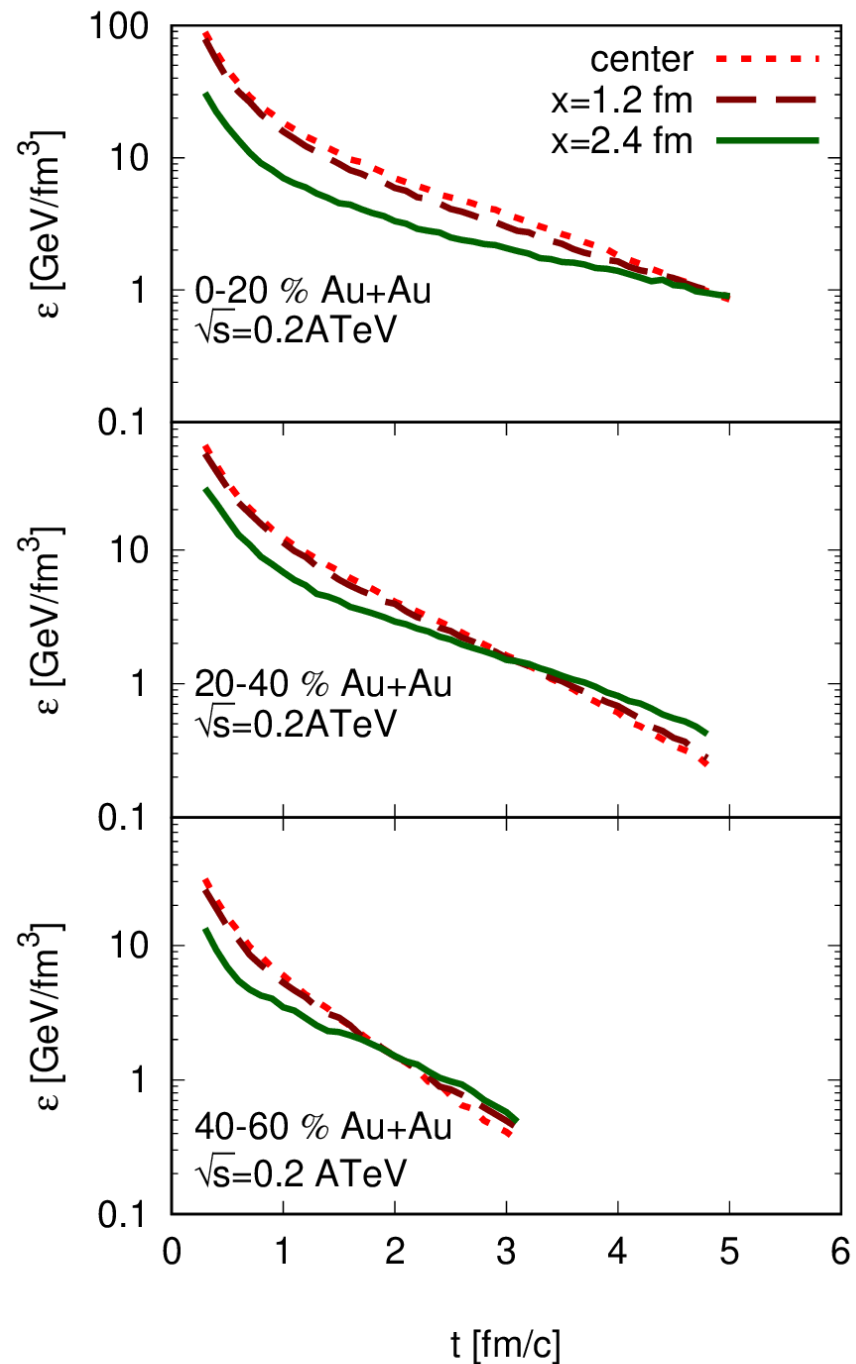
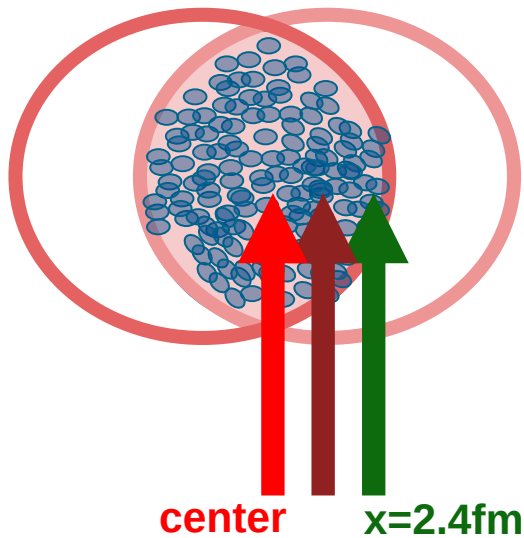
Thermodynamic Evolution

energy
density at
midrapidity



Thermodynamic Evolution

energy
density at
midrapidity



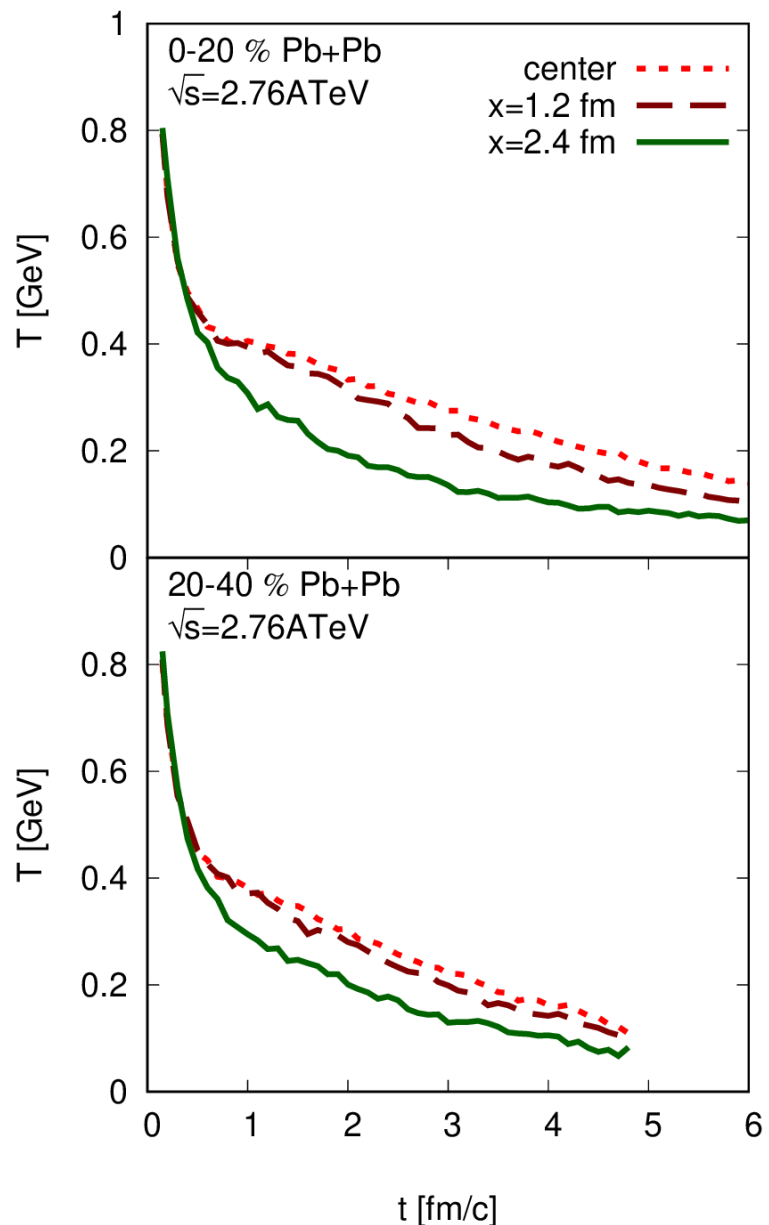
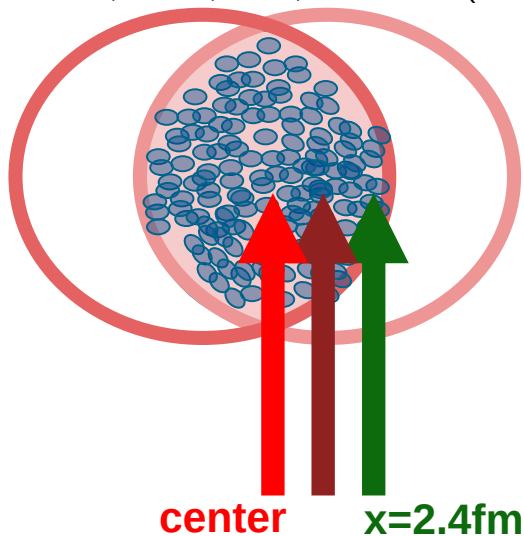
Thermodynamic Evolution

Temperature at midrapidity

$$\mathcal{I} = \frac{1}{2} \int \frac{d^3\vec{p}}{(2\pi)^3 E_p} E_p f \quad \mathcal{J} = \int \frac{d^3\vec{p}}{(2\pi)^3 E_p} f$$

$$T_{\star}^{1st} = \frac{\sum_{\text{species } i} \nu_i \frac{g^2 C_i}{d_A} \mathcal{I}_i}{\sum_{\text{species } i} \nu_i \frac{g^2 C_i}{d_A} \mathcal{J}_i}$$

(cf. Arnold, Moore, Yaffe, JHEP 0301 (2003) 030)

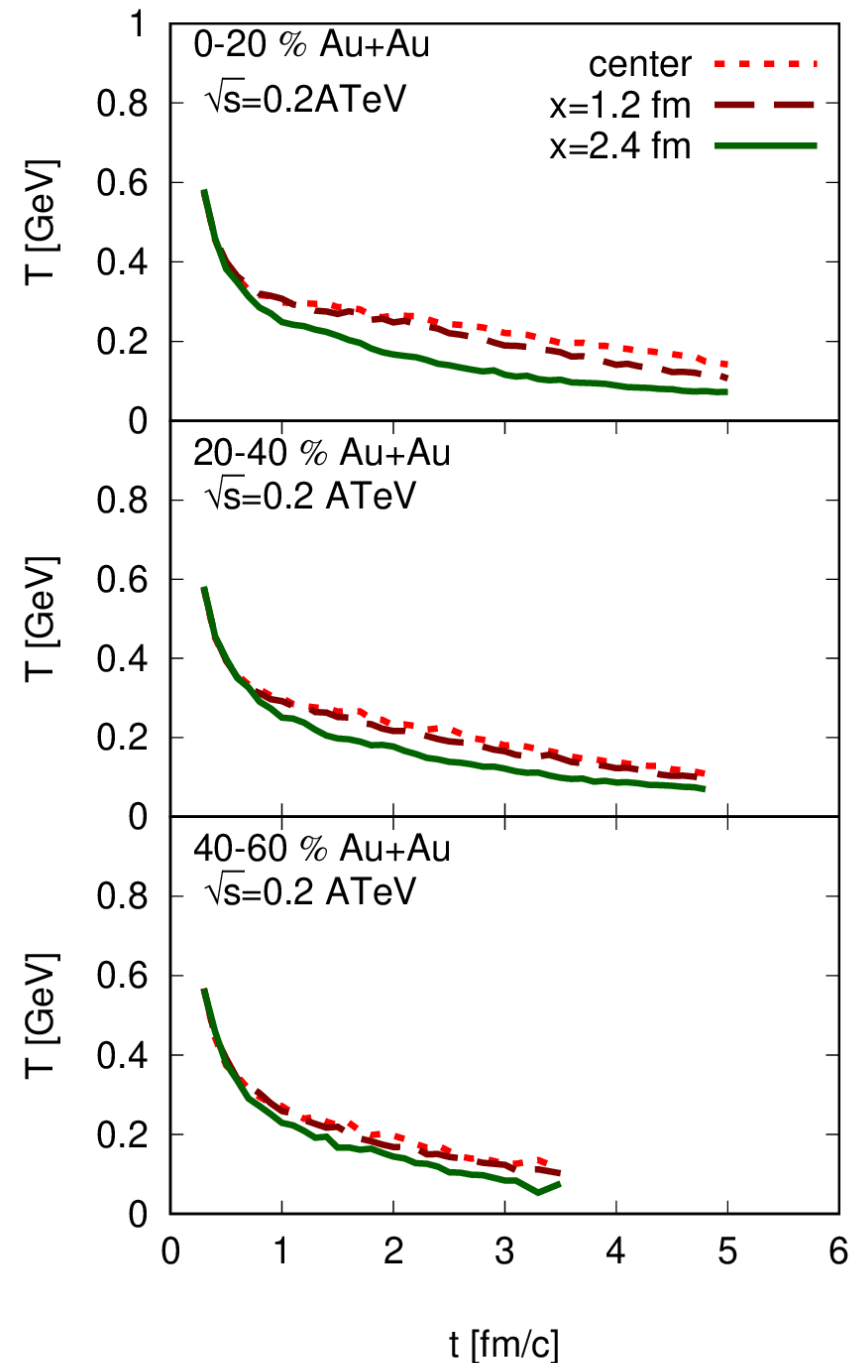
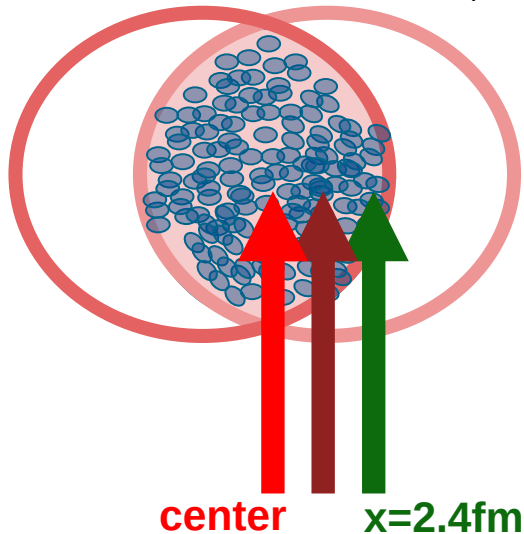


Thermodynamic Evolution

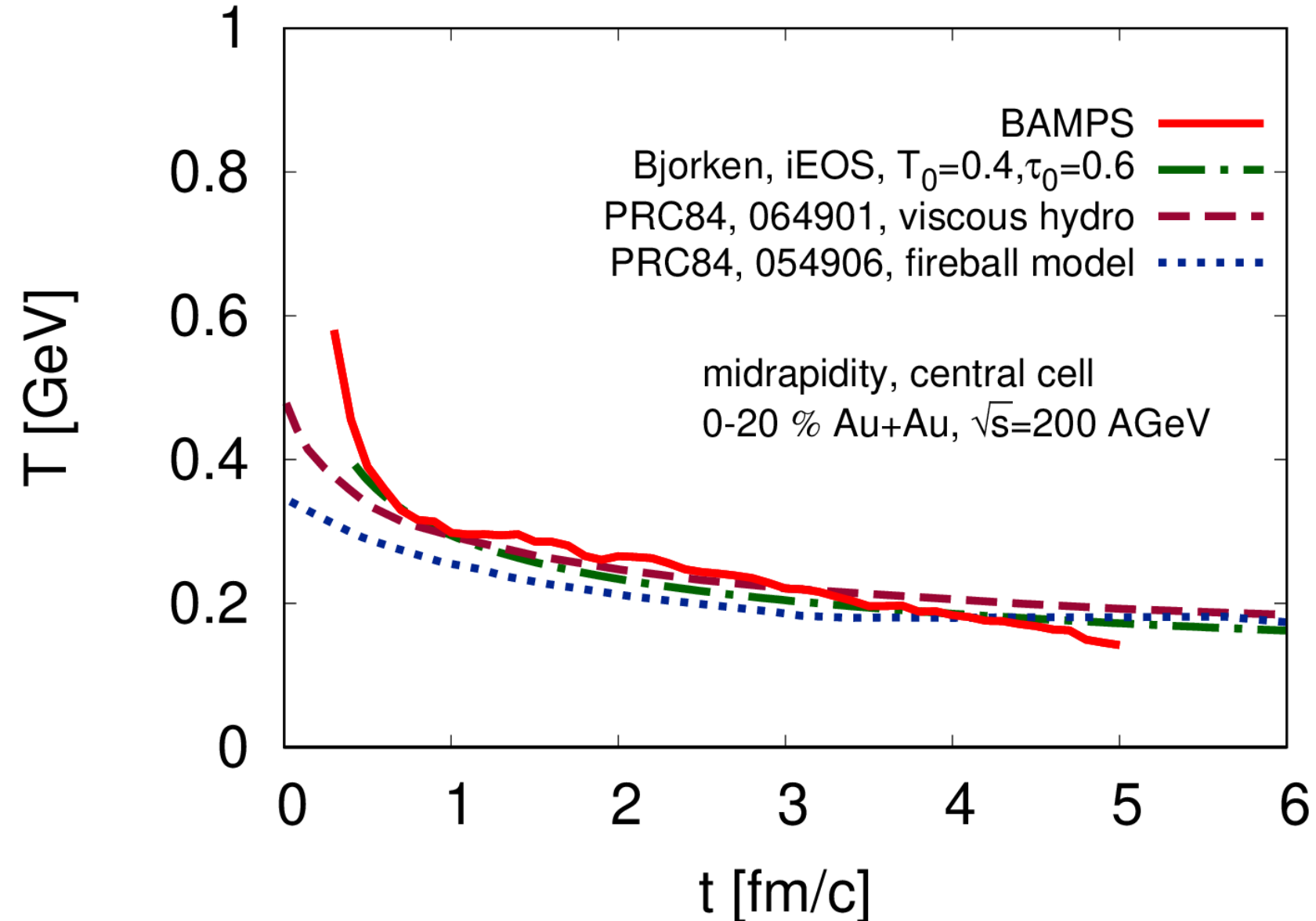
Temperature at midrapidity

$$\mathcal{I} = \frac{1}{2} \int \frac{d^3\vec{p}}{(2\pi)^3 E_p} E_p f \quad \mathcal{J} = \int \frac{d^3\vec{p}}{(2\pi)^3 E_p} f$$
$$T_{\star}^{\text{1st}} = \sum_{\text{species } i} \nu_i \frac{g^2 C_i}{d_A} \mathcal{I}_i \bigg/ \sum_{\text{species } i} \nu_i \frac{g^2 C_i}{d_A} \mathcal{J}_i$$

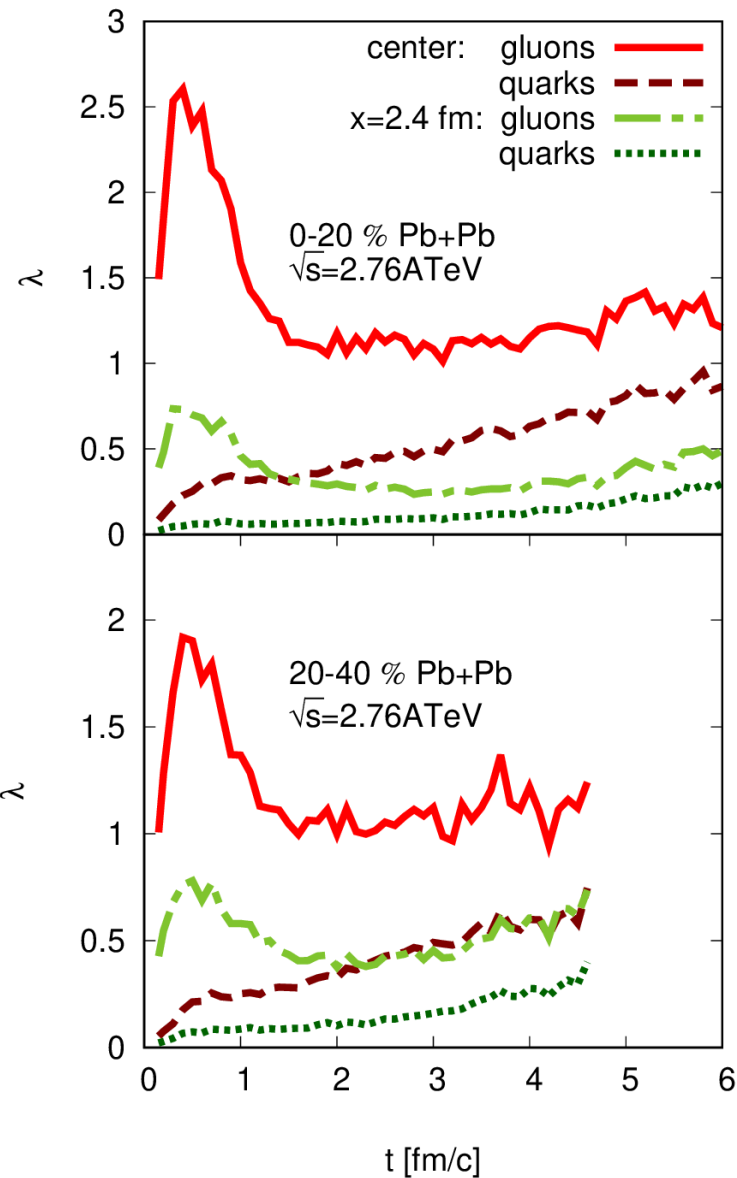
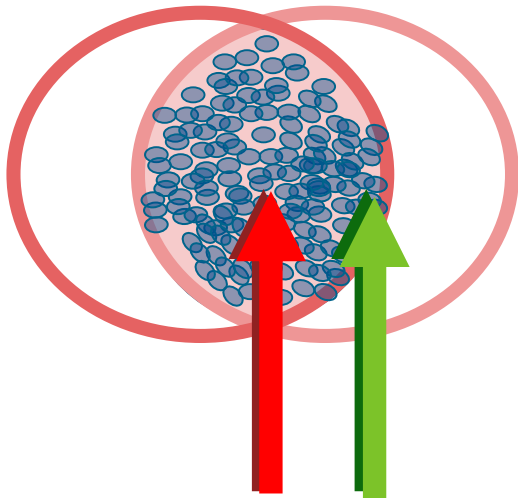
(cf. Arnold, Moore, Yaffe, JHEP 0301 (2003) 030)



Thermodynamic Evolution

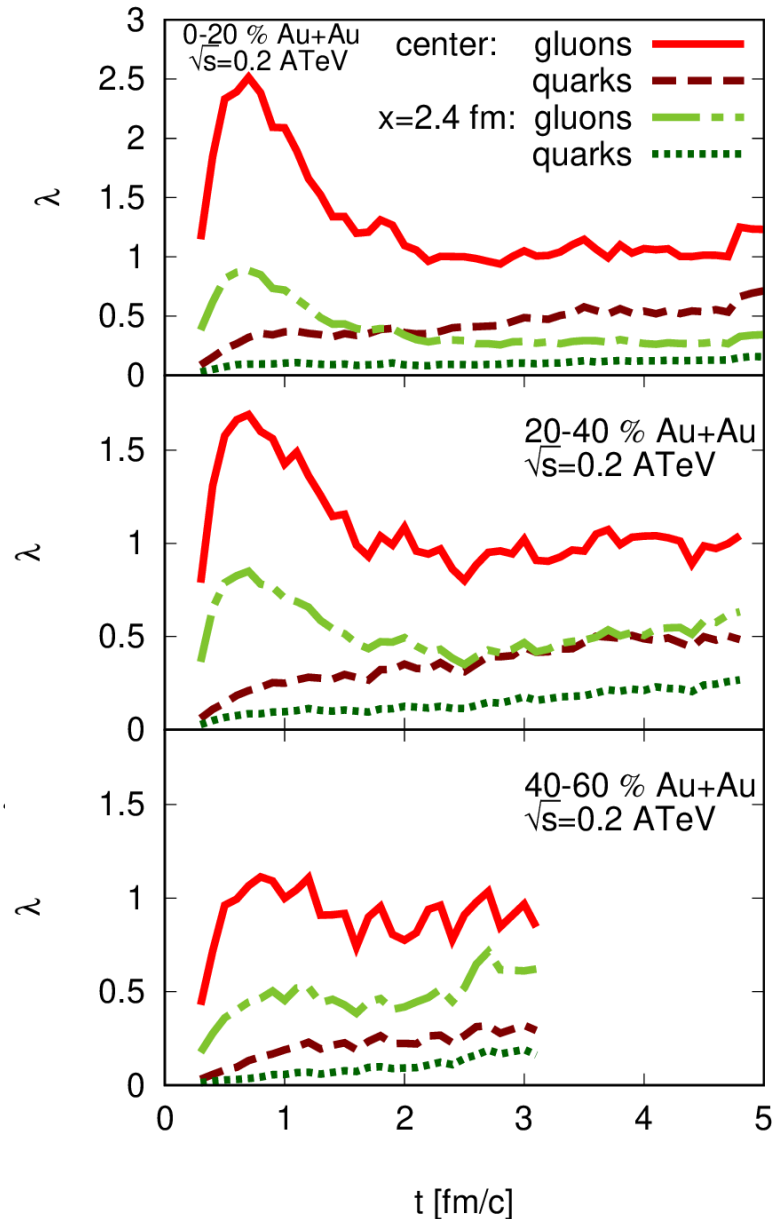
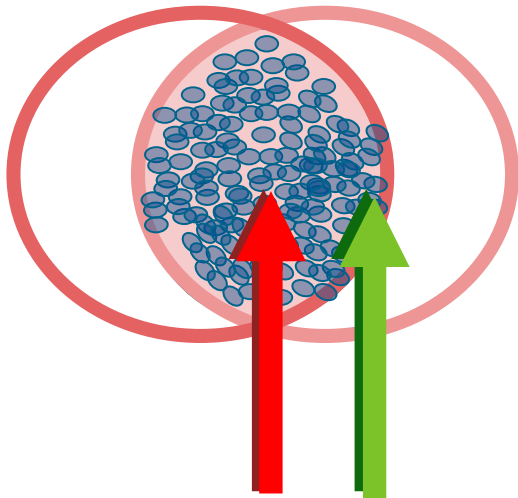


Fugacity $\lambda = n/n_{\text{eq.}}$
at midrapidity

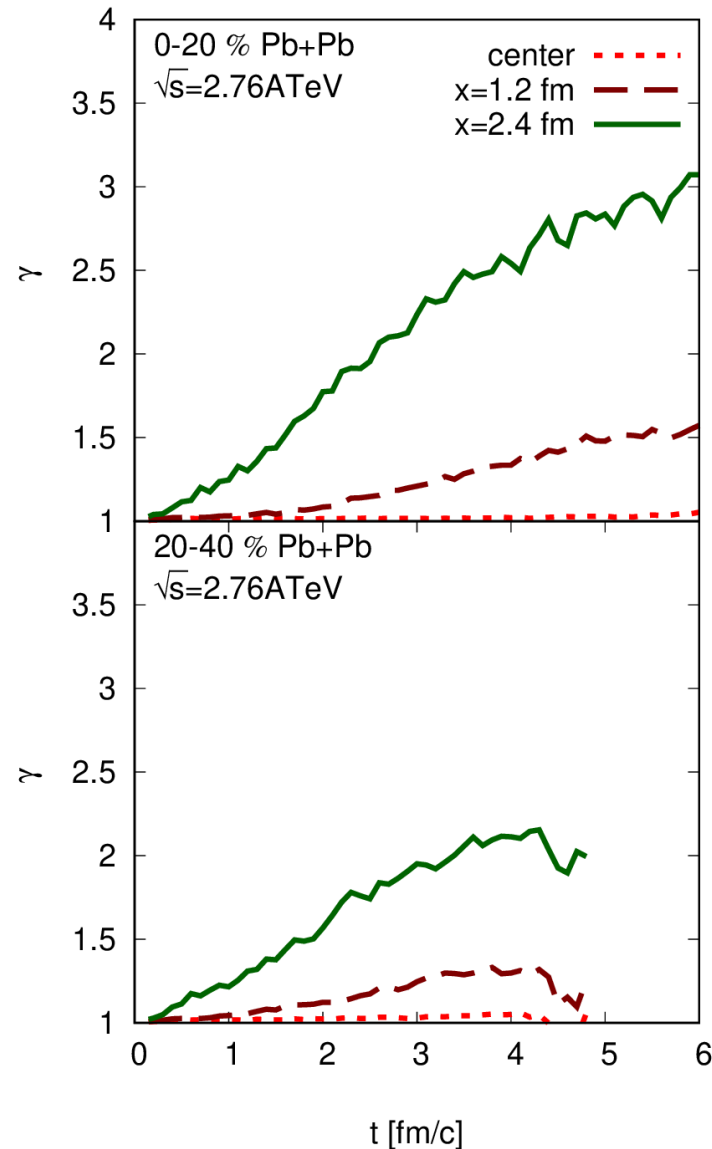
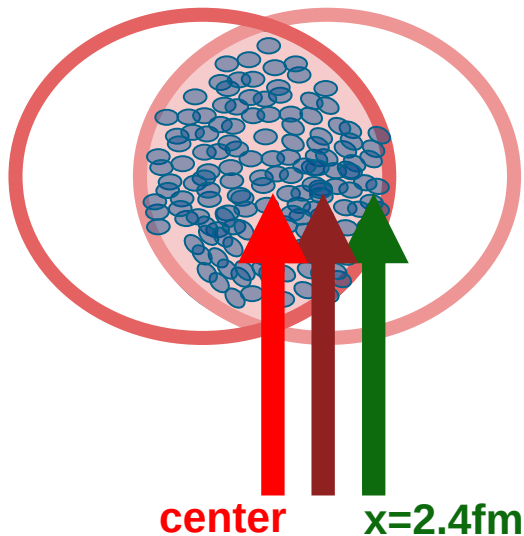


Chemical Evolution

Fugacity $\lambda = n/n_{\text{eq.}}$
at midrapidity

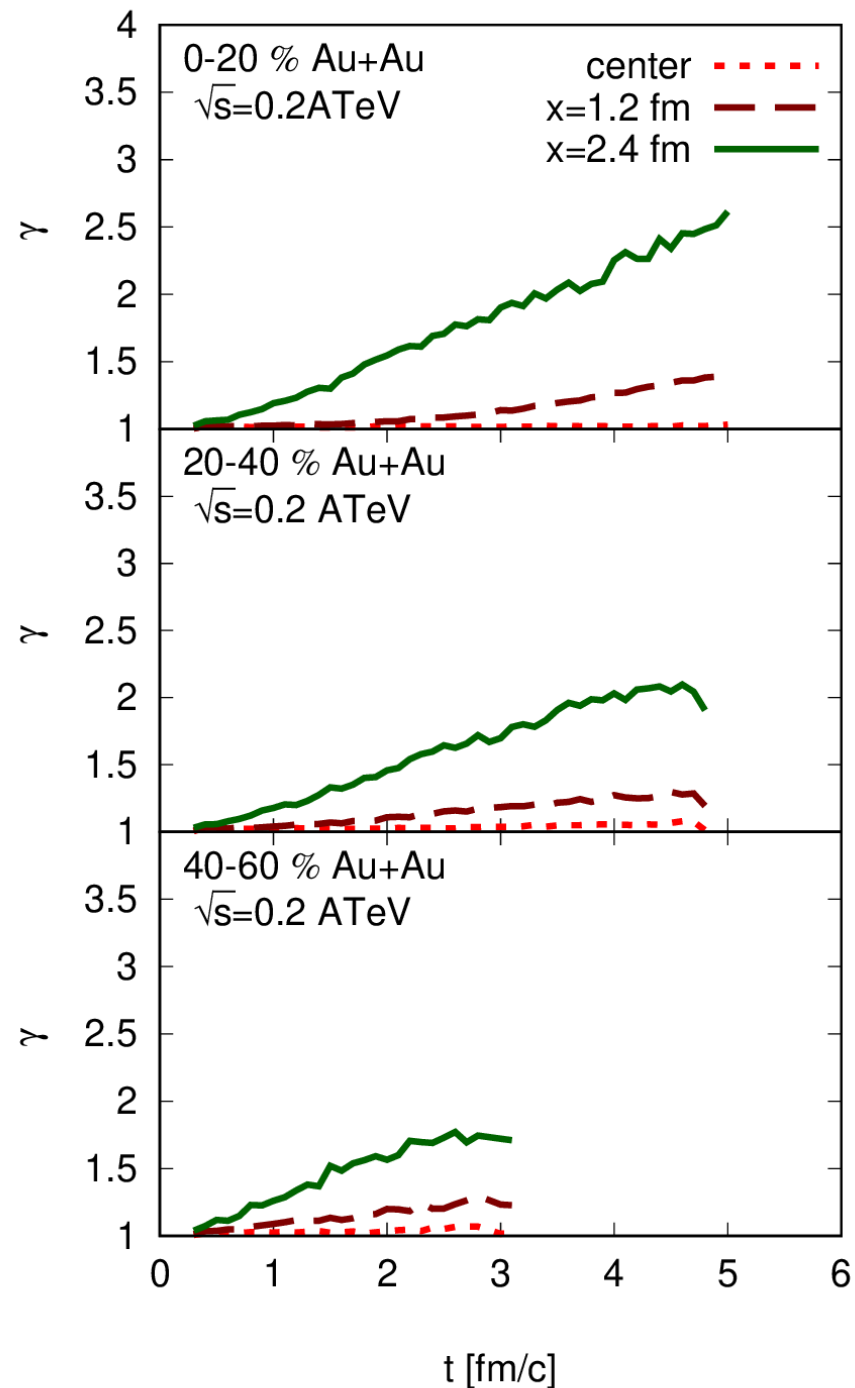
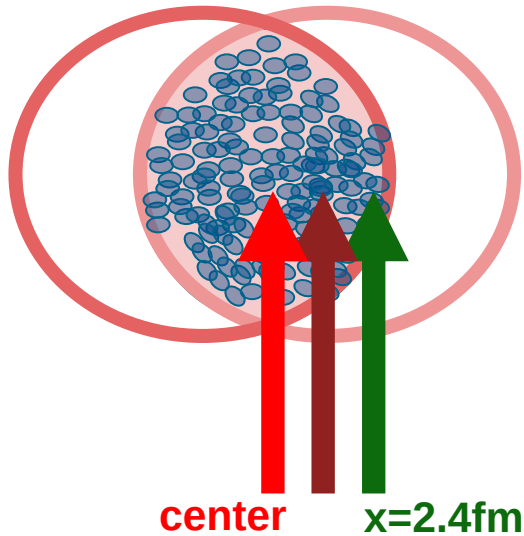


Velocity
(Boost) at
midrapidity



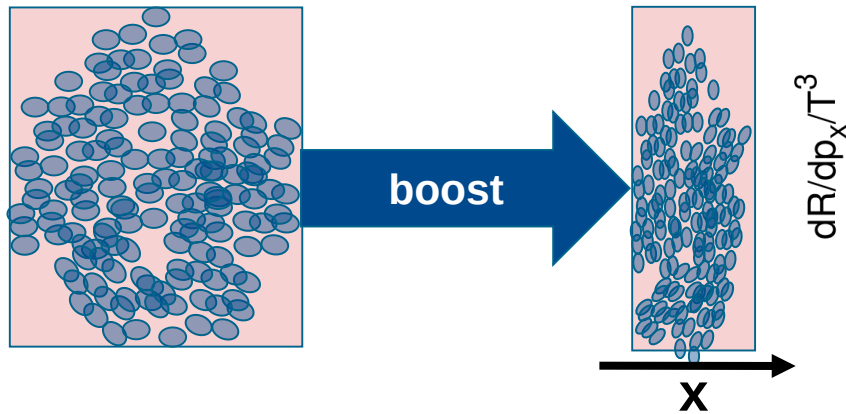
Dynamic Evolution

Velocity
(Boost) at
midrapidity

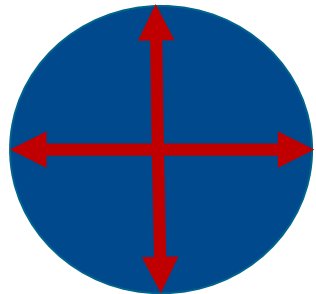


Velocity – Elliptic flow relation

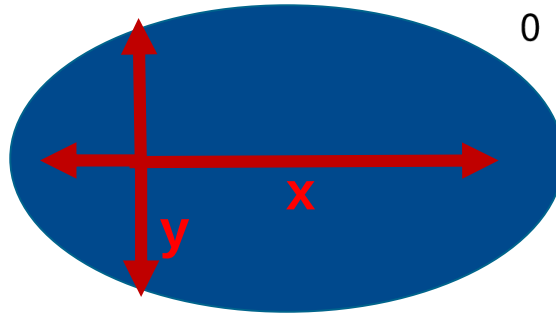
$$v_2 = (p_x^2 - p_y^2) / (p_x^2 + p_y^2)$$



$$dR/dp_x/T^3$$

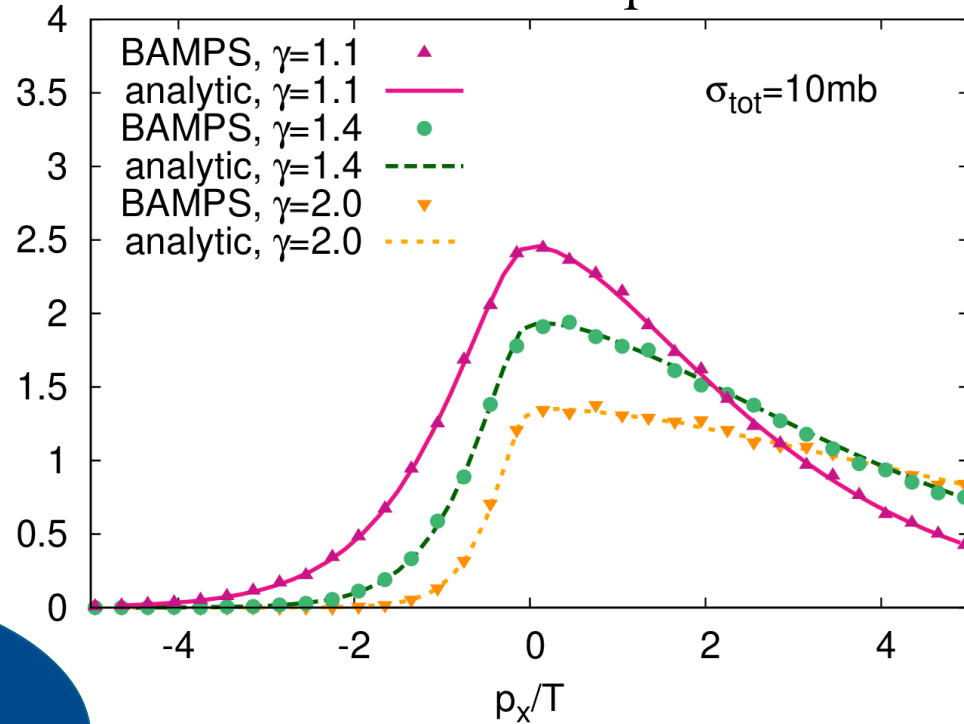


momentum
distribution
isotropic



momentum
distribution
deformed

Production rate of particles



$$\gamma = 2 \rightarrow v_2 \sim 0.5$$

$$\gamma = 1.1 \rightarrow v_2 \sim 0.1$$

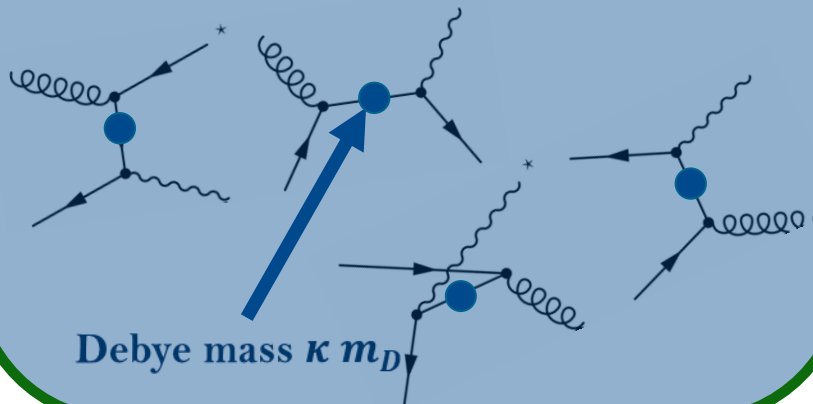
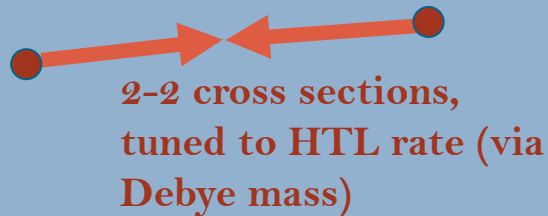
(R=Production rate $dN/dV/dt$ [GeV^4])

Photon production in BAMPS

$2 \leftrightarrow 2$ scattering

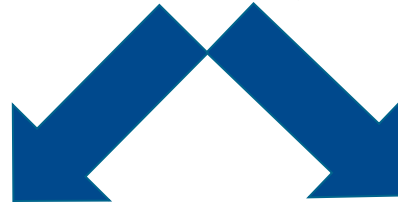


Diagrams, microscopic collisions

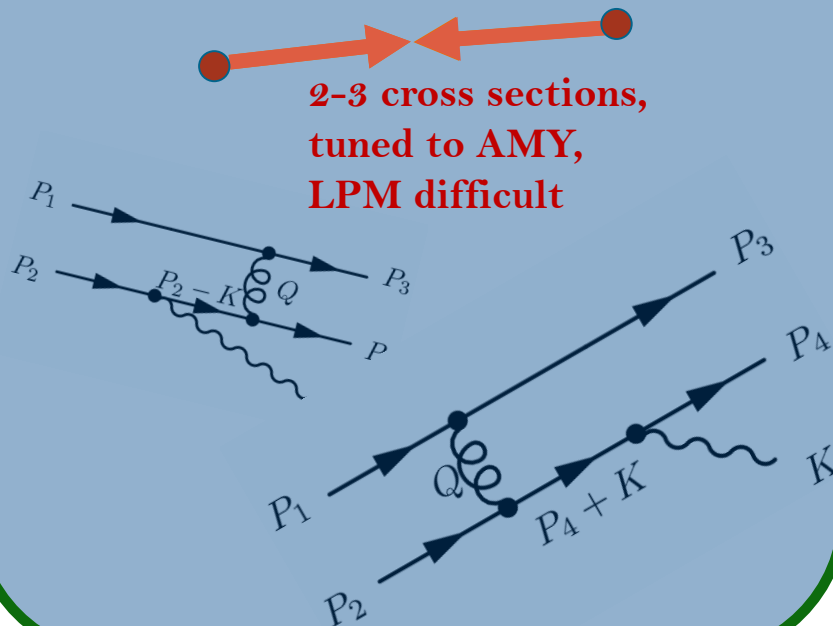


Photon production in BAMPS

$2 \rightarrow 3$ scattering: two independent methods

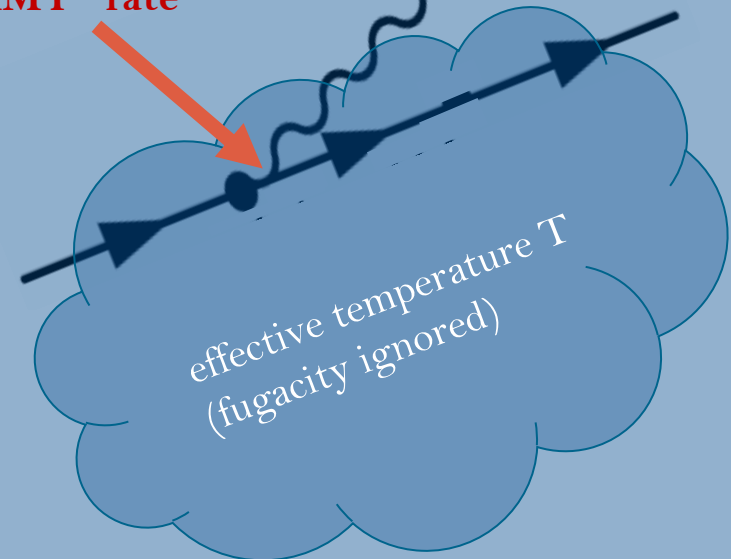


Diagrams, microscopic collisions



Rate approach
„microscopic“ coarse graining

AMY* rate



* Arnold, Moore, Yaffe, JHEP 0112 (2001) 009

22 photoproduction under control

1.) Naive screening with Debye mass:

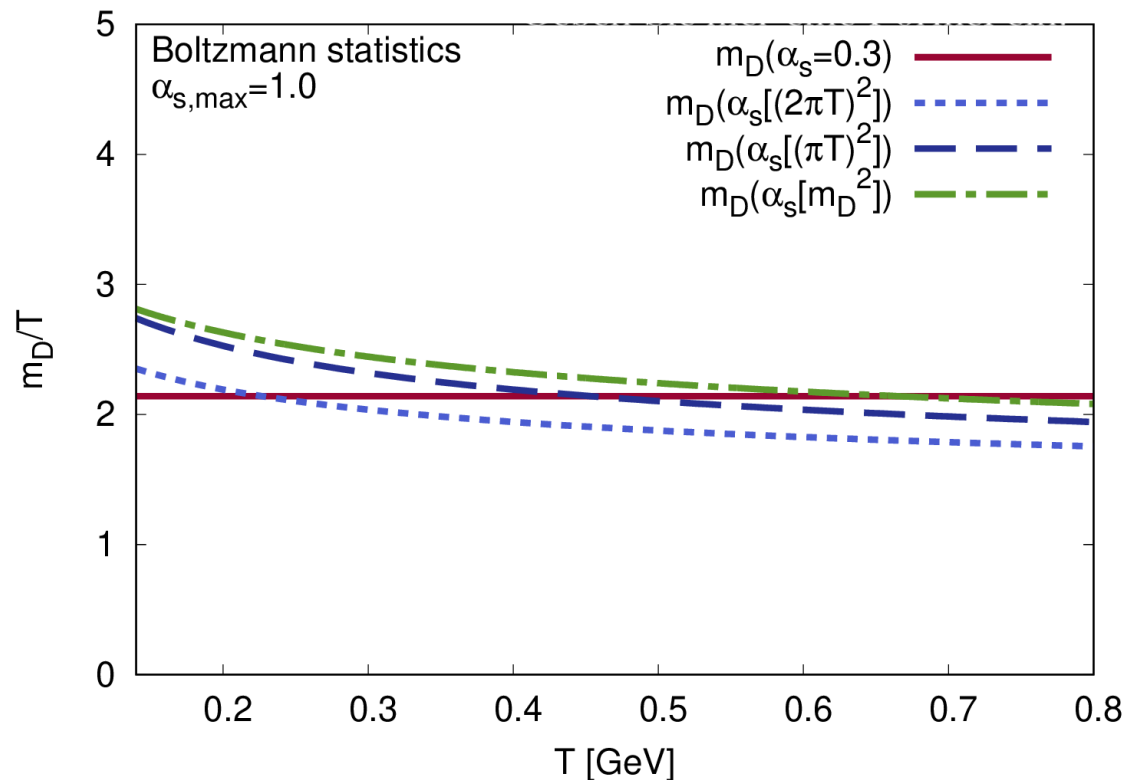
$$\frac{1}{t^2} \rightarrow \frac{1}{(t - m_D^2)^2}$$

2.) tune Debye mass:

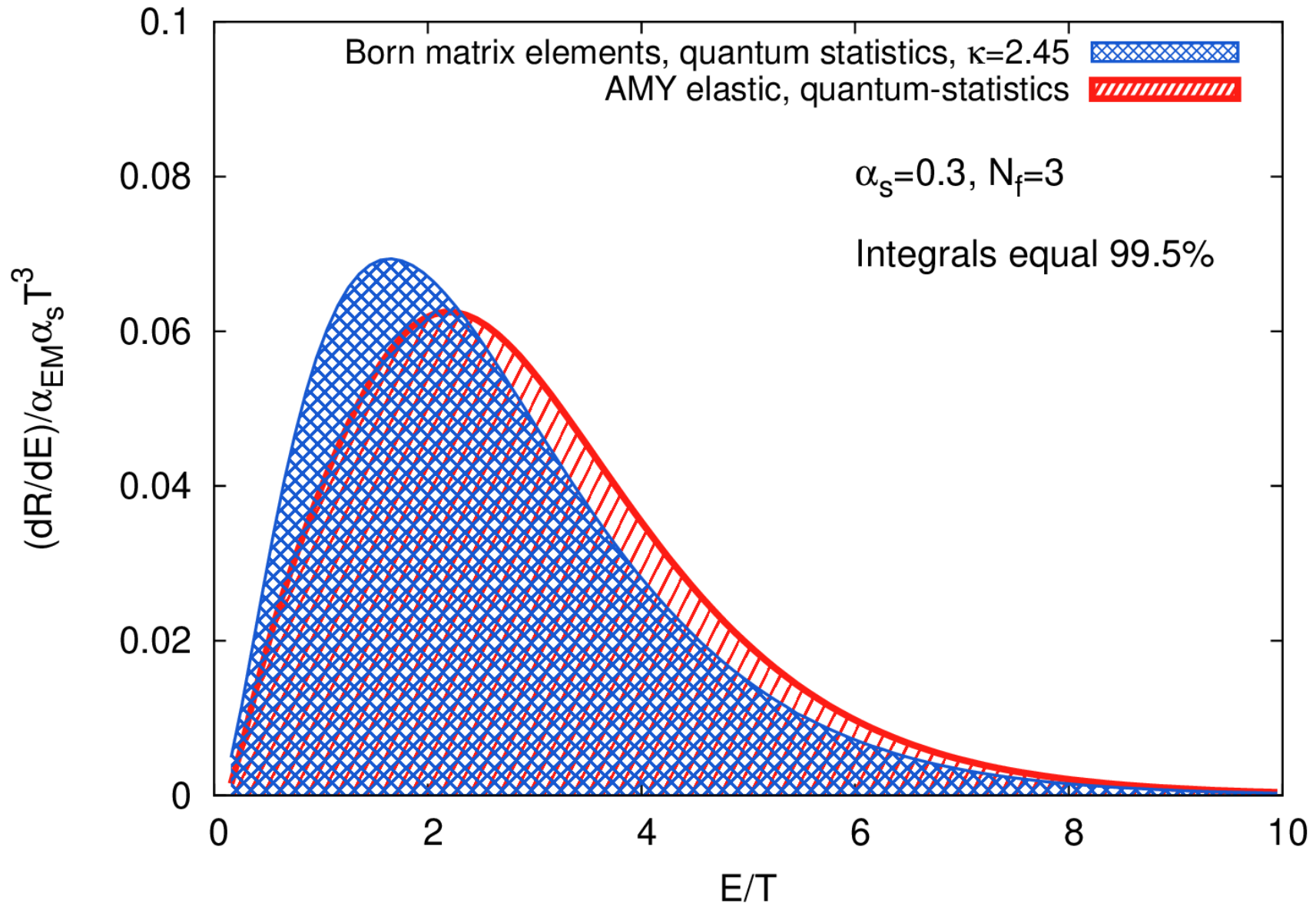
$$m_D^2 \rightarrow \kappa m_D^2$$

3.) tune overall ME
(missing quantum statistics):

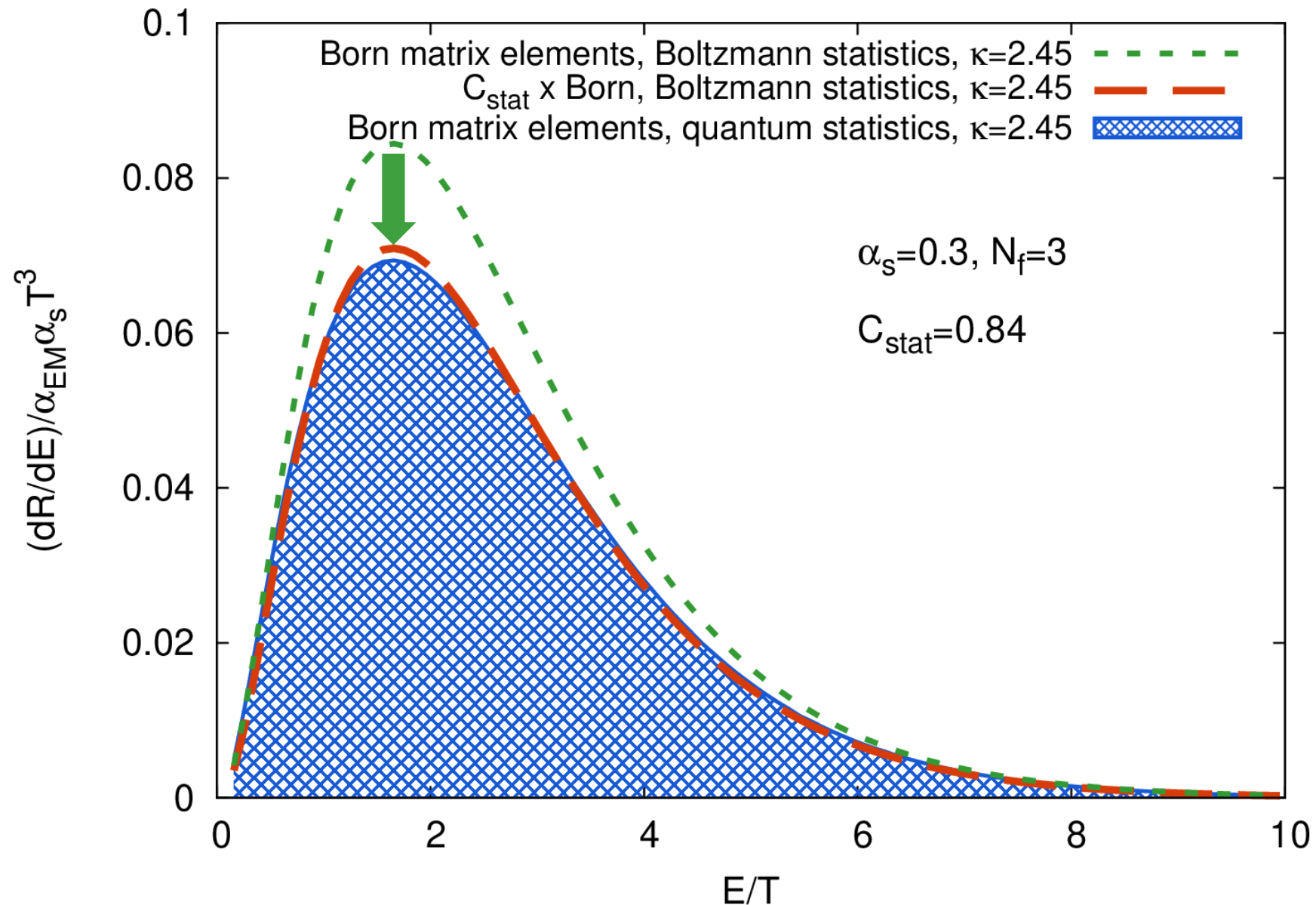
$$|\mathcal{M}|^2 \rightarrow C_{\text{stat}} |\mathcal{M}|^2$$



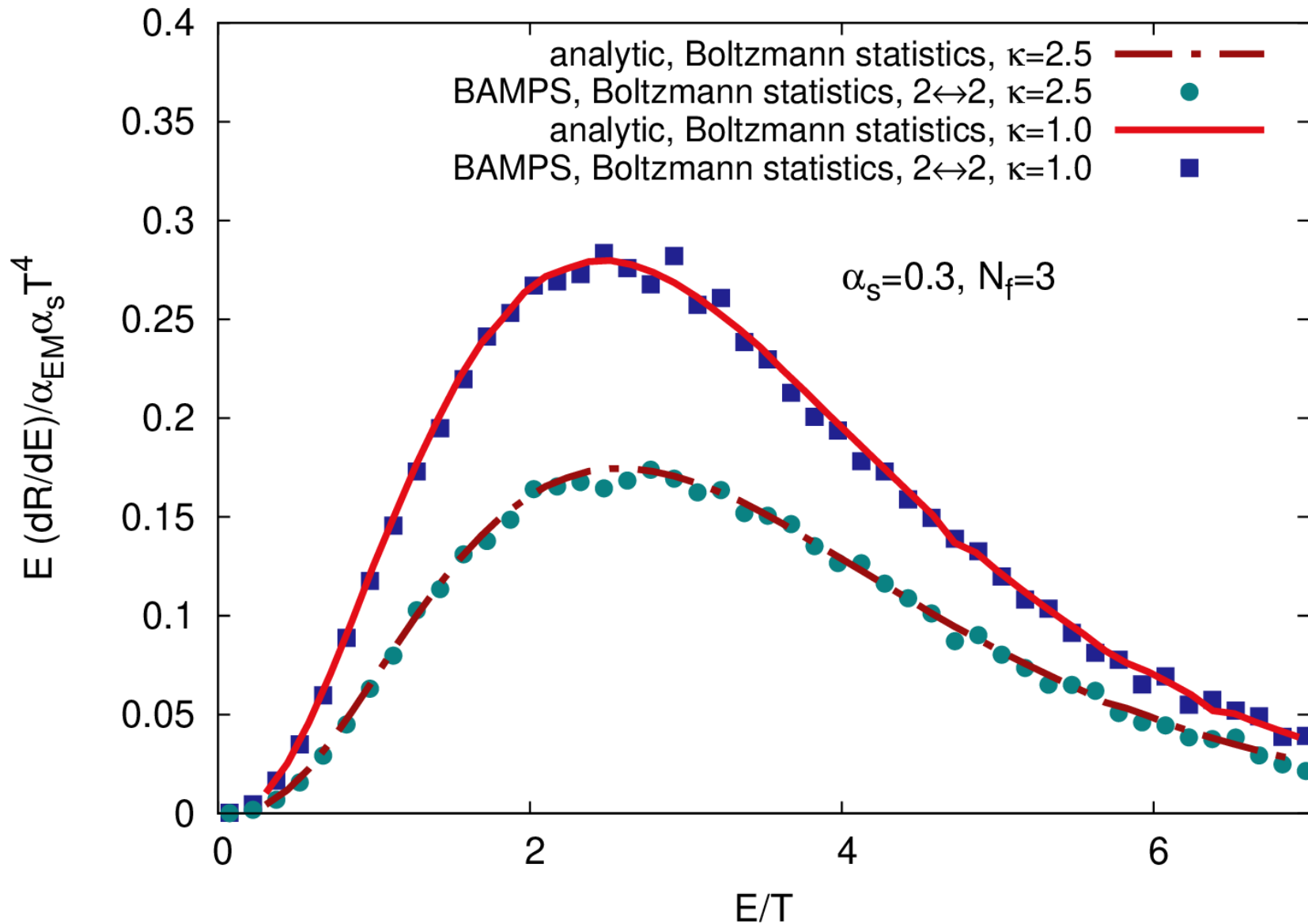
22 photoproduction under control



22 photoproduction under control



22 photoproduction under control

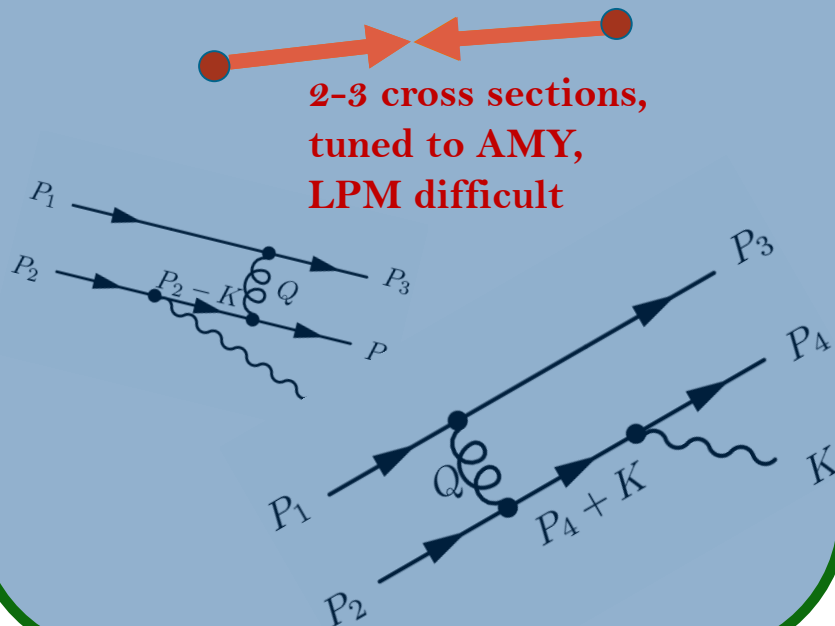


Photon production in BAMPS

$2 \rightarrow 3$ scattering: two independent methods

Method 1

Diagrams, microscopic collisions



Rate approach
“microscopic” coarse graining

AMY* rate

effective temperature T
(fugacity ignored)

* Arnold, Moore, Yaffe, JHEP 0112 (2001) 009

2->3 photoproduction under control

1.) Naive screening with Debye mass:

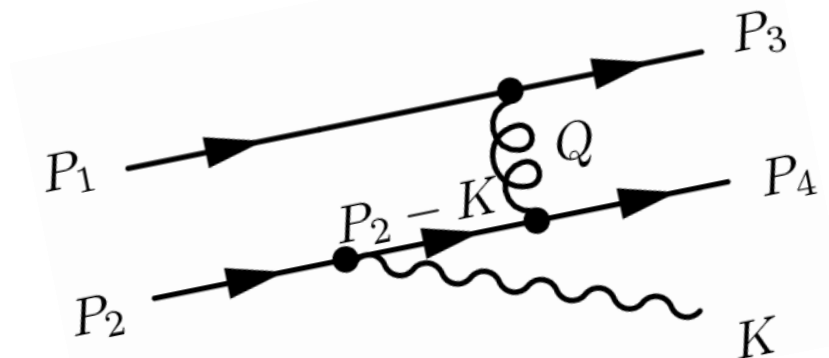
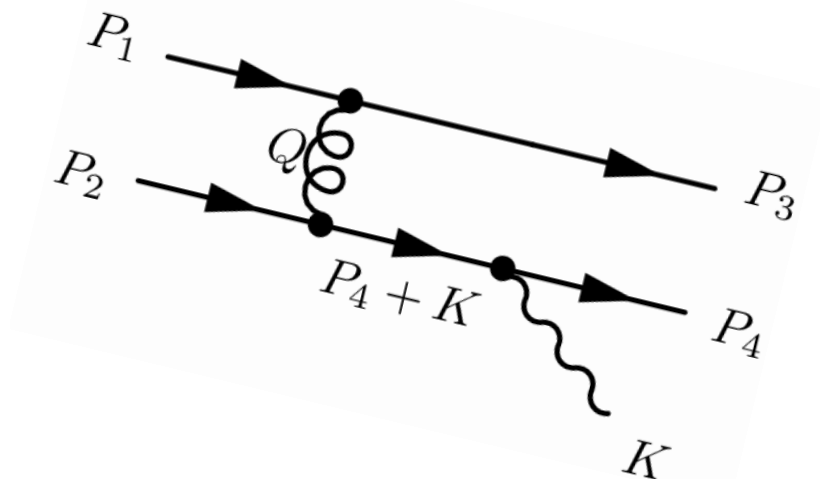
$$\frac{1}{t^2} \rightarrow \frac{1}{(t - m_D^2)^2}$$

2.) simple LPM model:

$$|\mathcal{M}_{2 \rightarrow 3}|^2 \rightarrow \Theta(\lambda - \tau_{\text{form}}) |\mathcal{M}_{2 \rightarrow 3}|^2$$

3.) tune overall Matrix element:

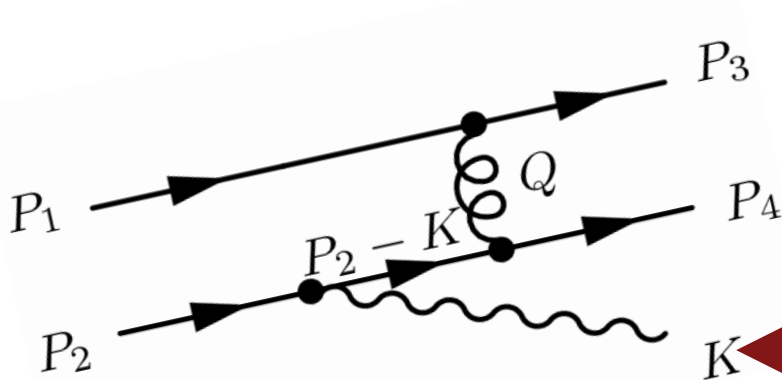
$$|\mathcal{M}_{2 \rightarrow 3}|^2 \rightarrow K_{\text{inel}} |\mathcal{M}_{2 \rightarrow 3}|^2$$



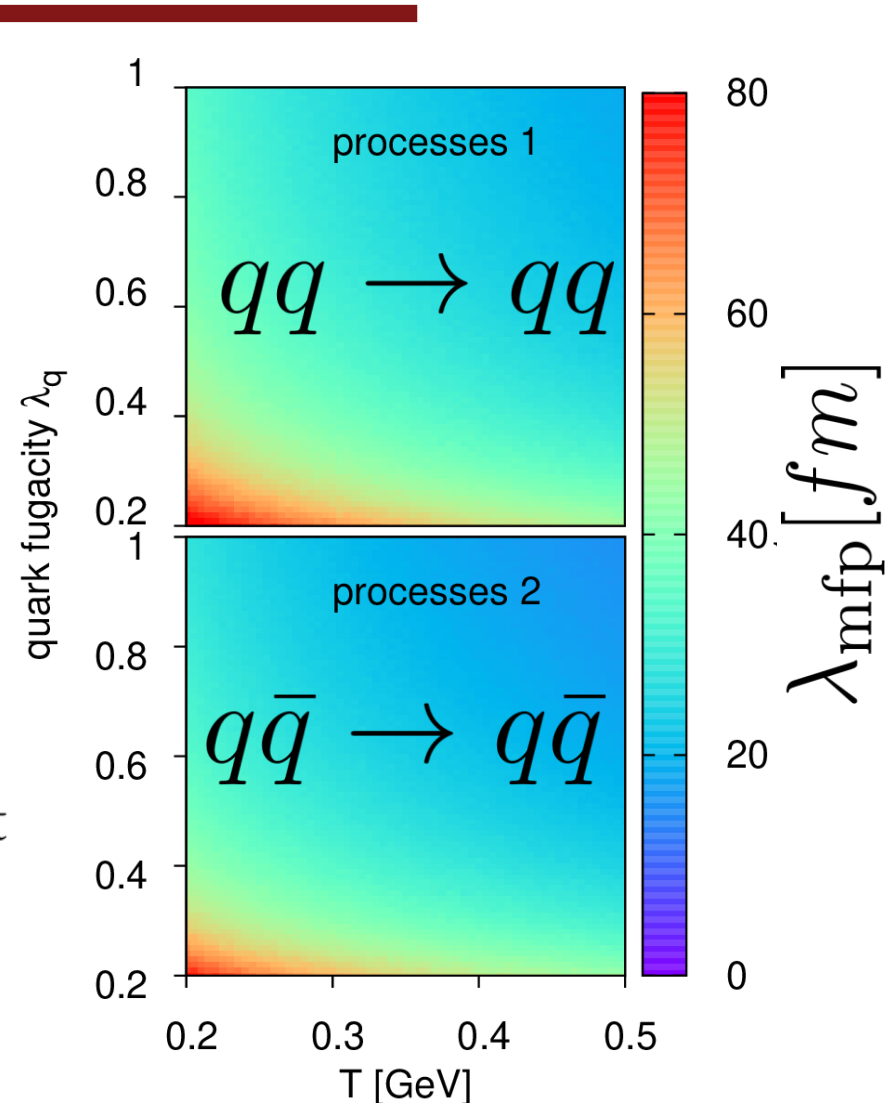
- Numeric integration for total cross section
- Multi-dimensional Metropolis sampling for differential cross section

2->3 photoproduction under control

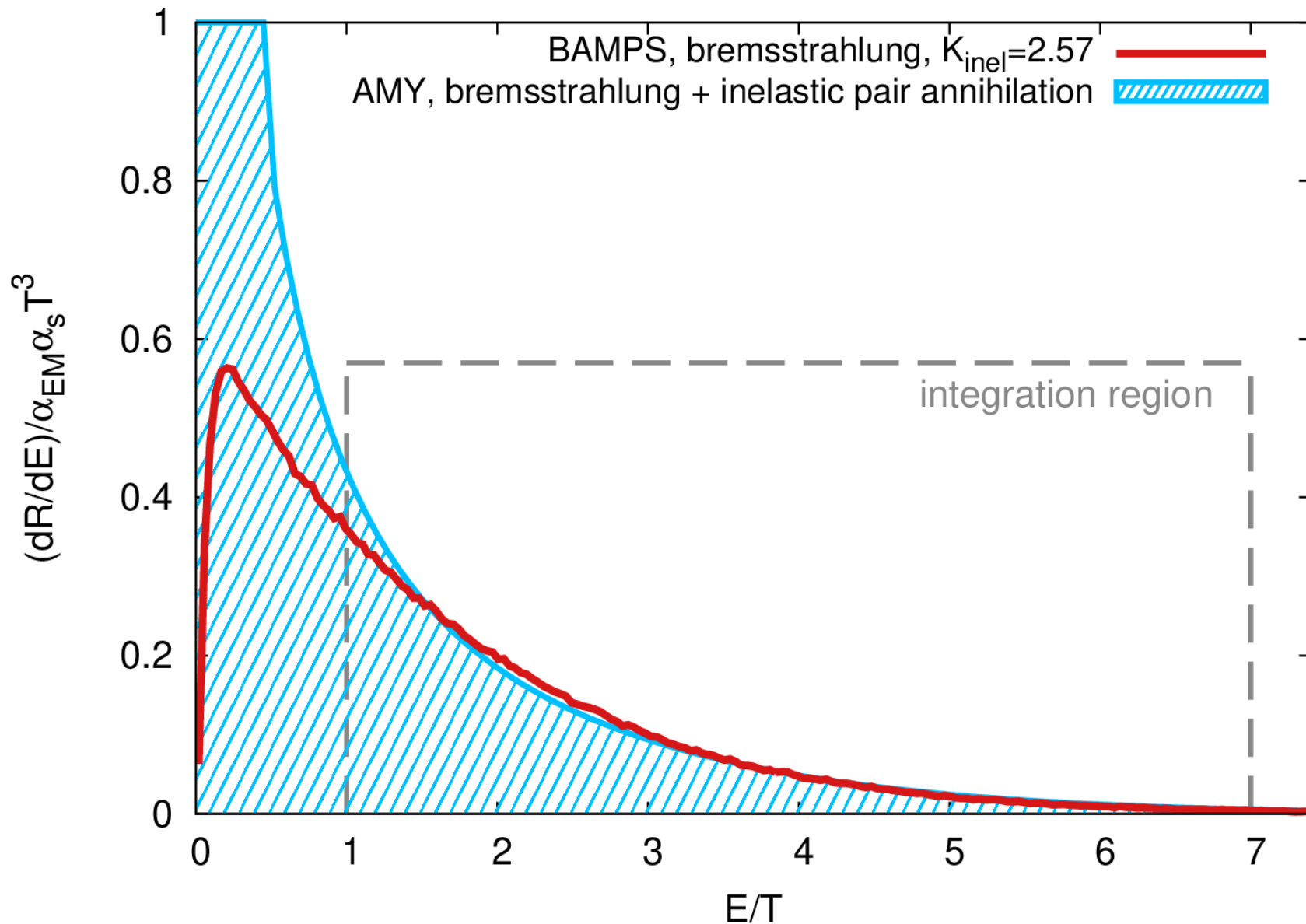
simple LPM model: $|\mathcal{M}_{2 \rightarrow 3}|^2 \rightarrow \Theta(\lambda_{\text{mfp}} - \tau_{\text{form}}) |\mathcal{M}_{2 \rightarrow 3}|^2$



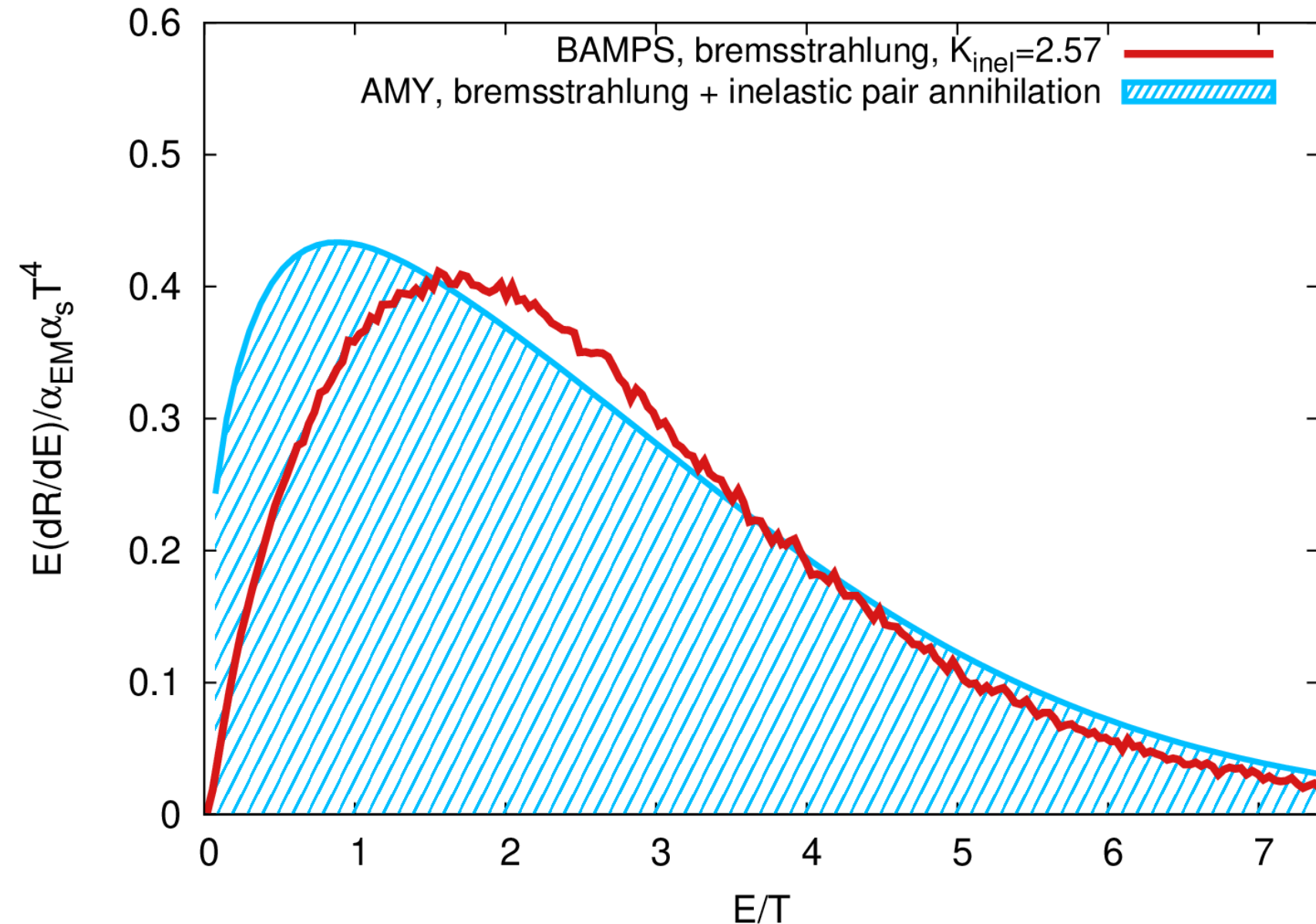
- Formation time of photon $\tau = k_T^{-1}$
- Mean-free path of corresponding processes, T and fugacity dependent



2->3 photoproduction under control



2->3 photoproduction under control

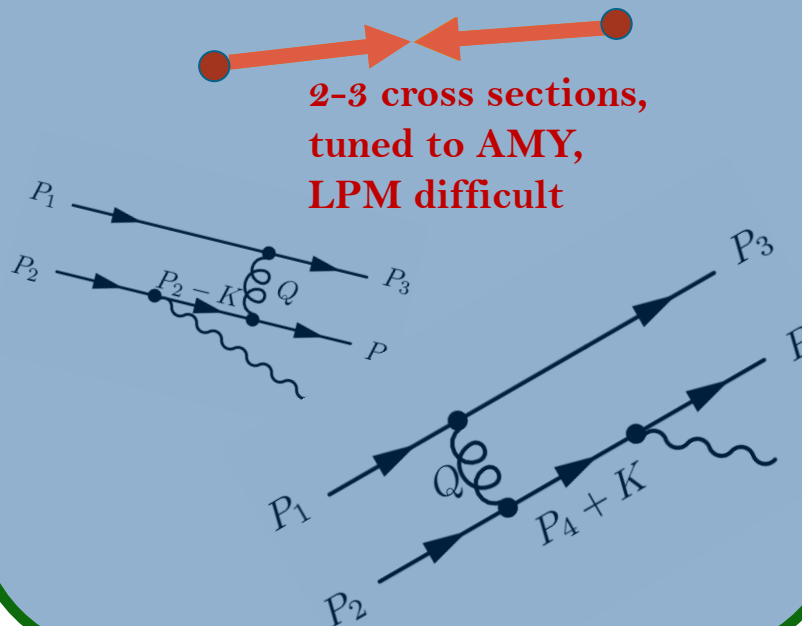


Photon production in BAMPS

$2 \rightarrow 3$ scattering: two independent methods

Method 2

Diagrams, microscopic collisions



Rate approach
„microscopic“ coarse graining

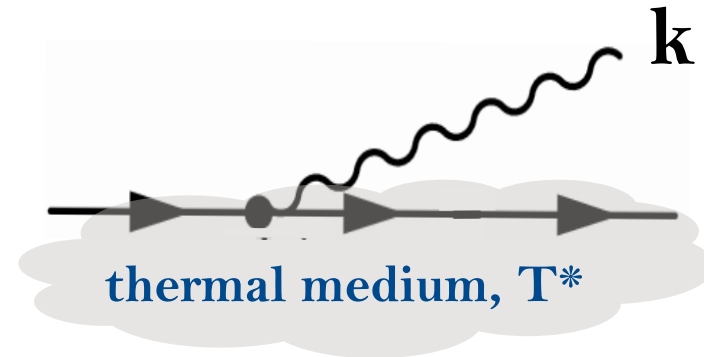
AMY* rate

effective temperature T
(fugacity ignored)

* Arnold, Moore, Yaffe, JHEP 0112 (2001) 009

AMY rate for photon emission of quark

massless quark, momentum P



Rate $dN/dtdk$ for emission, at temperature T :

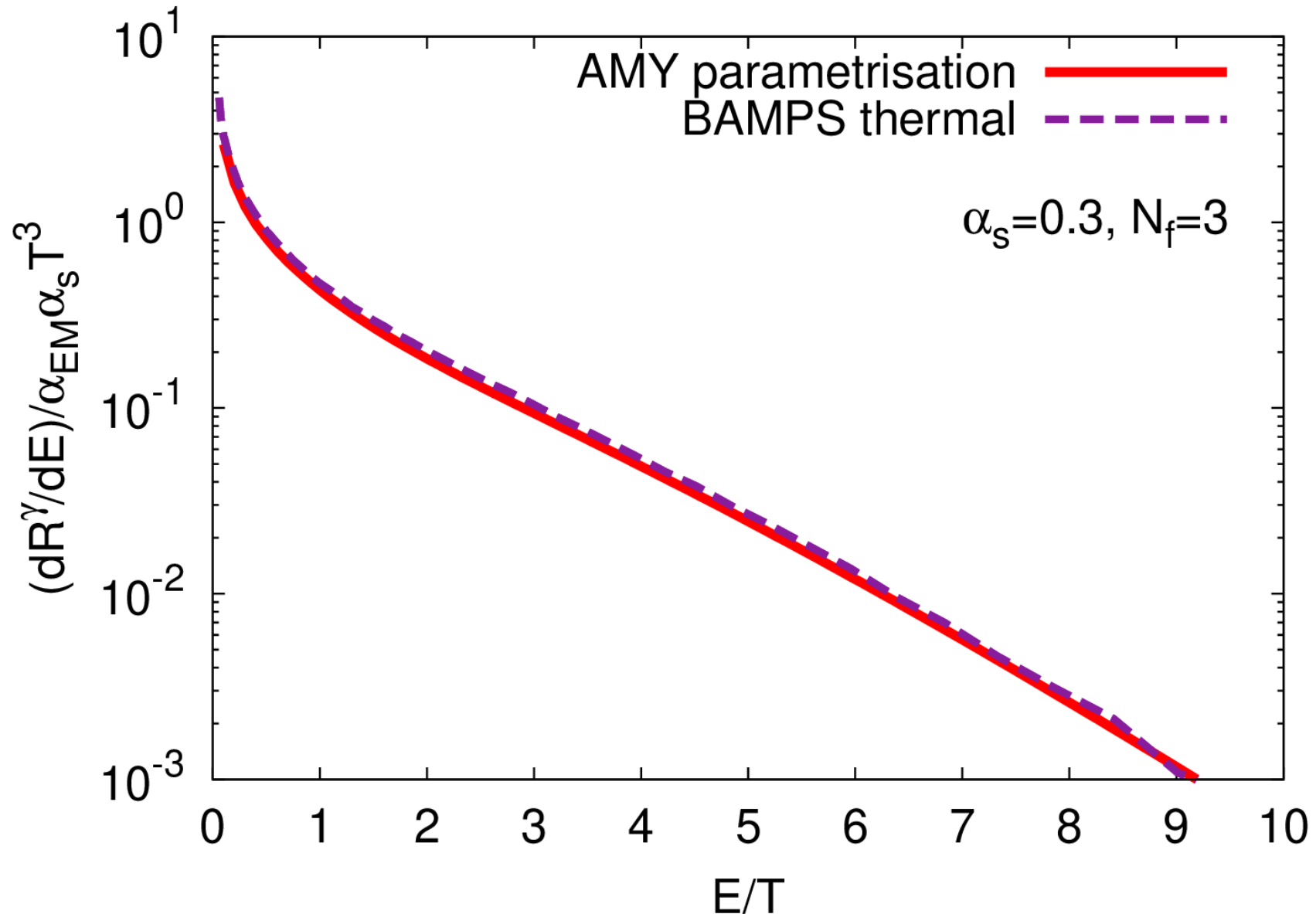
$$\frac{d\Gamma_f^\gamma(p, k, T)}{dk} = \frac{q_f^2}{e^2} \frac{\alpha_{EM} k^4}{4p^7} [1 - f_F(p - k)] \frac{1 + (1 - x)^2}{x^3 (1 - x)^2} \int \frac{d^2 \vec{p}_\perp}{(2\pi)^2} 2\vec{p}_\perp \cdot \text{Re} \vec{f}(\vec{p}_\perp, p, k).$$

AMY Kernel

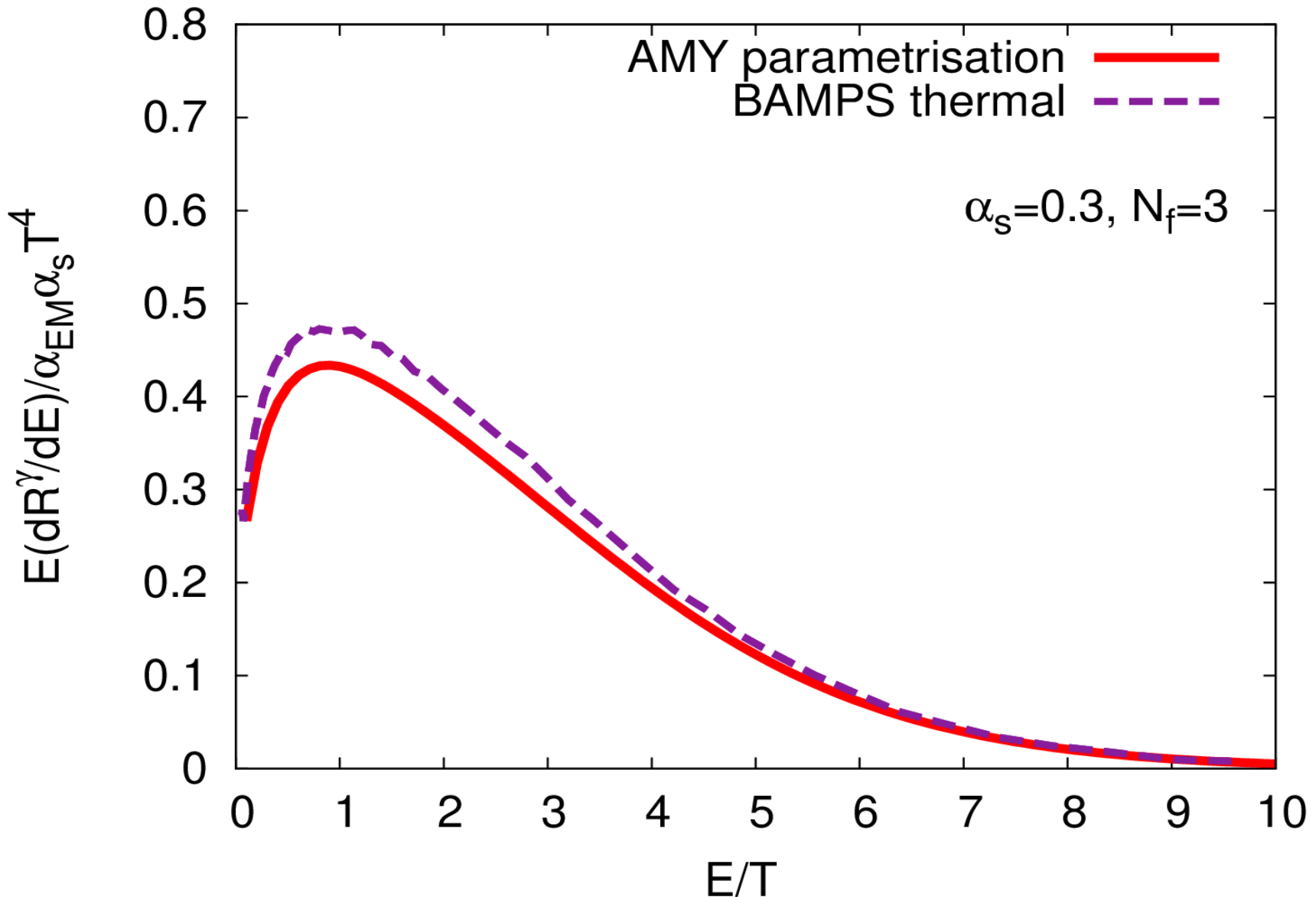
Arnold, Moore, Yaffe, JHEP 0206 (2002) 030

Solved via Differential Equation, cf. e.g. Aurenche,
Gelis, Moore, Zaraket, JHEP 0212 (2002) 006
Courtesy to J.F. Paquet for help.

AMY rate for photon emission off a quark



AMY rate for photon emission off a quark



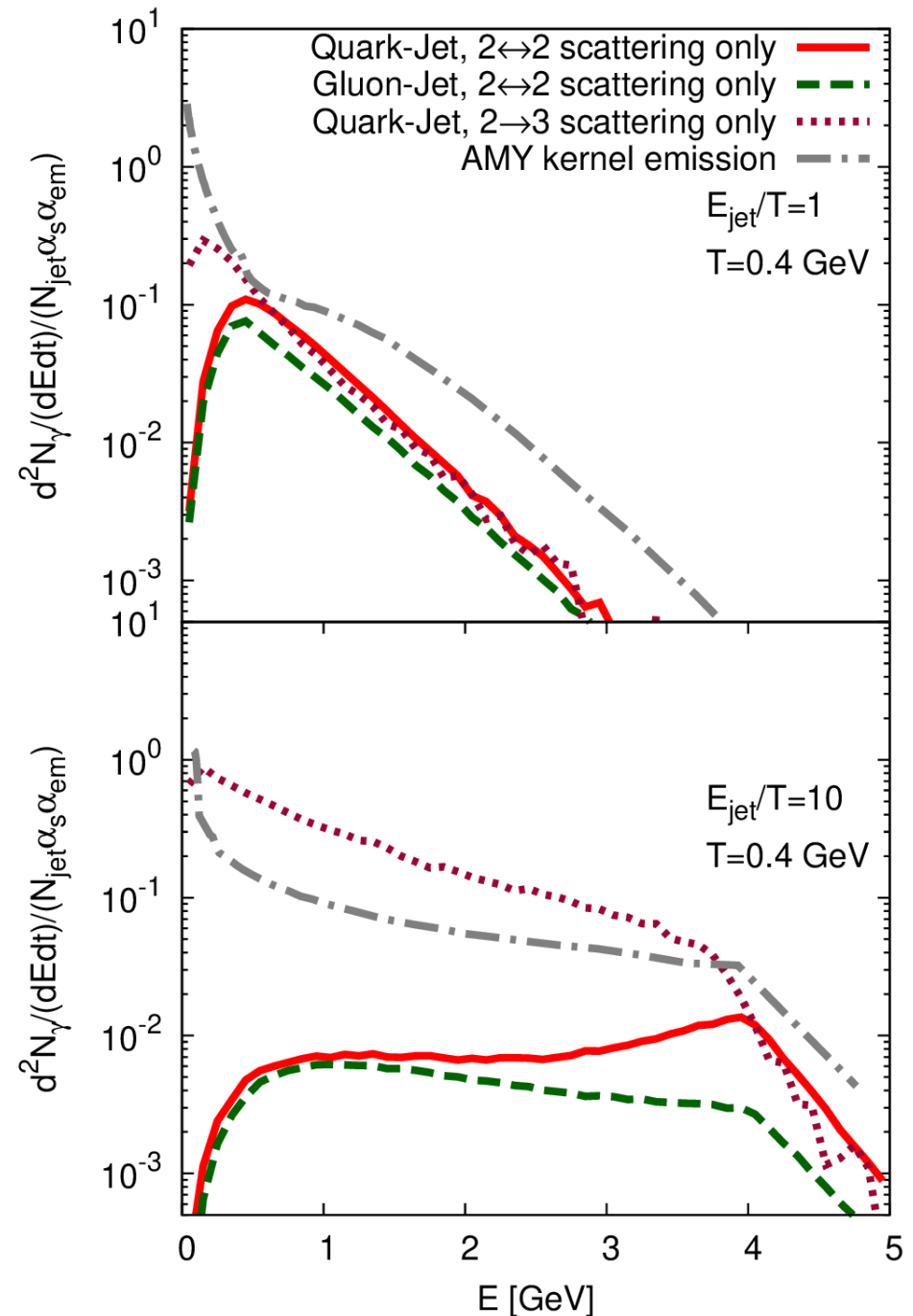
Differential kinematics

„Jet“ = single particle
responsible for emission

Quark-“jet“

vs.

Gluon-“jet“



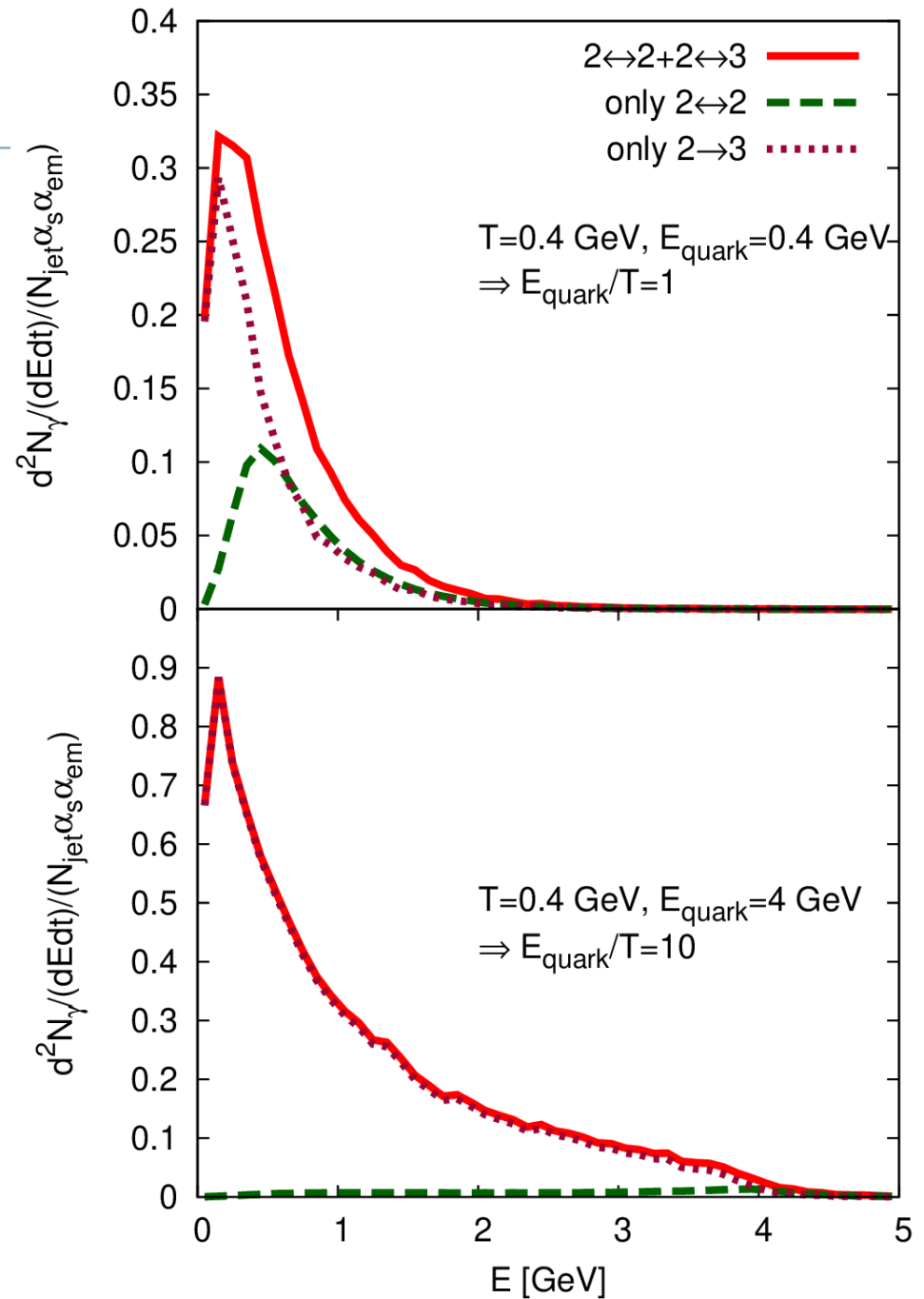
Differential kinematics

„Jet“ = single particle
responsible for emission

$2 \rightarrow 3$

VS.

$2 \rightarrow 2$



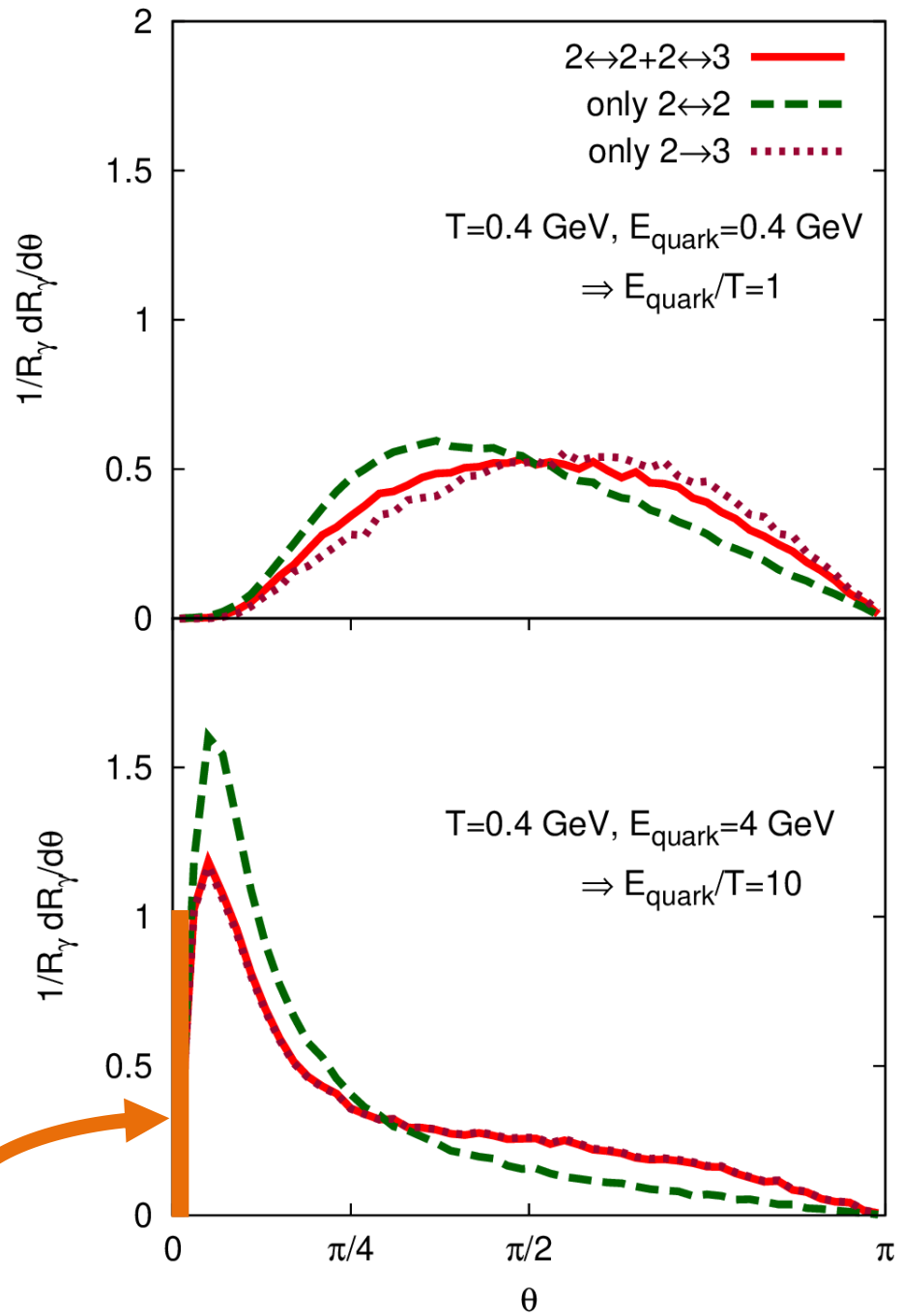
Differential kinematics

Emission
angle
 $2 \rightarrow 3$

vs.

$2 \rightarrow 2$

AMY exactly collinear

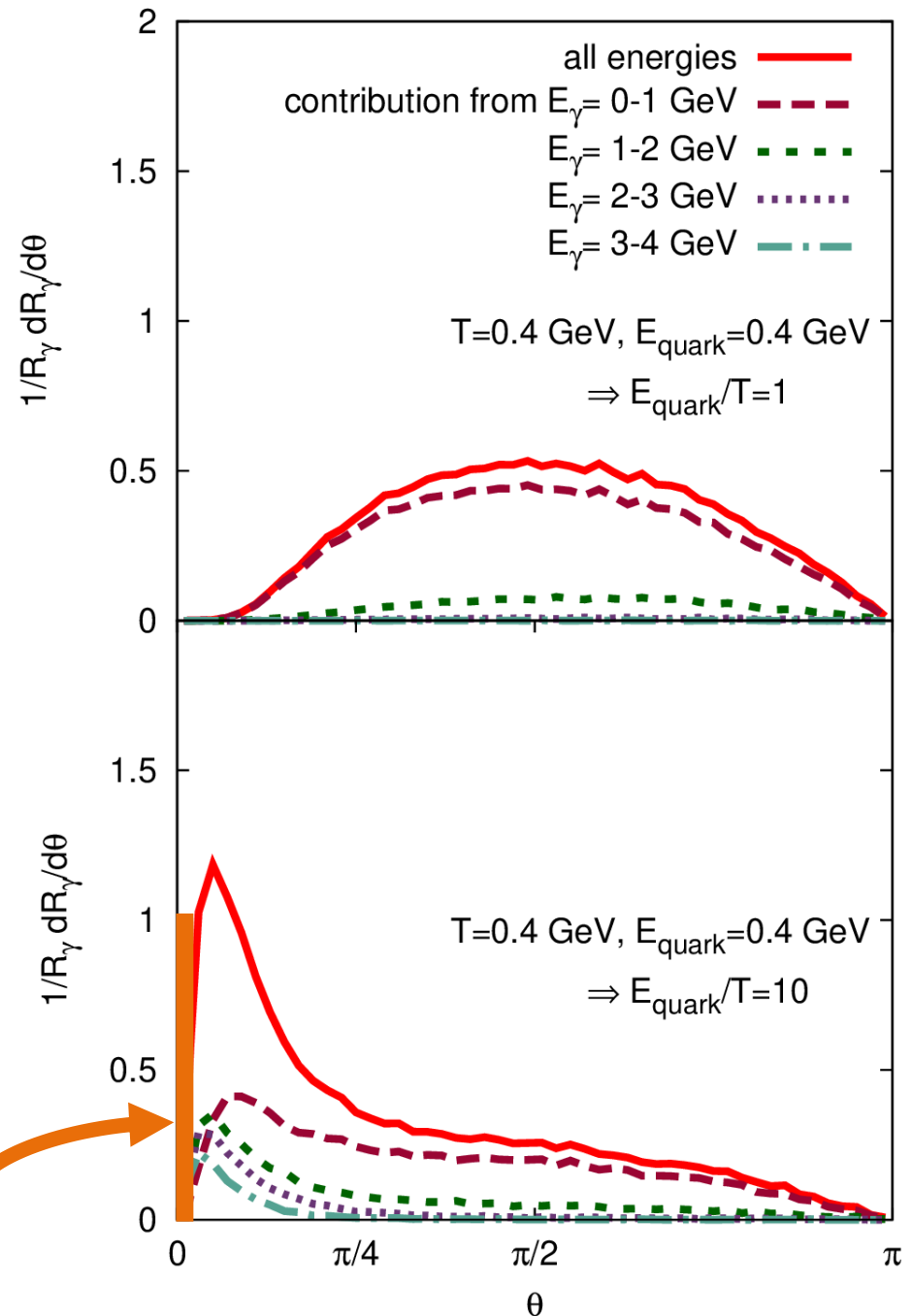


Differential kinematics

Emission angle
@ different
Photon energies

→ Higher photon energy – more collinear

AMY exactly collinear

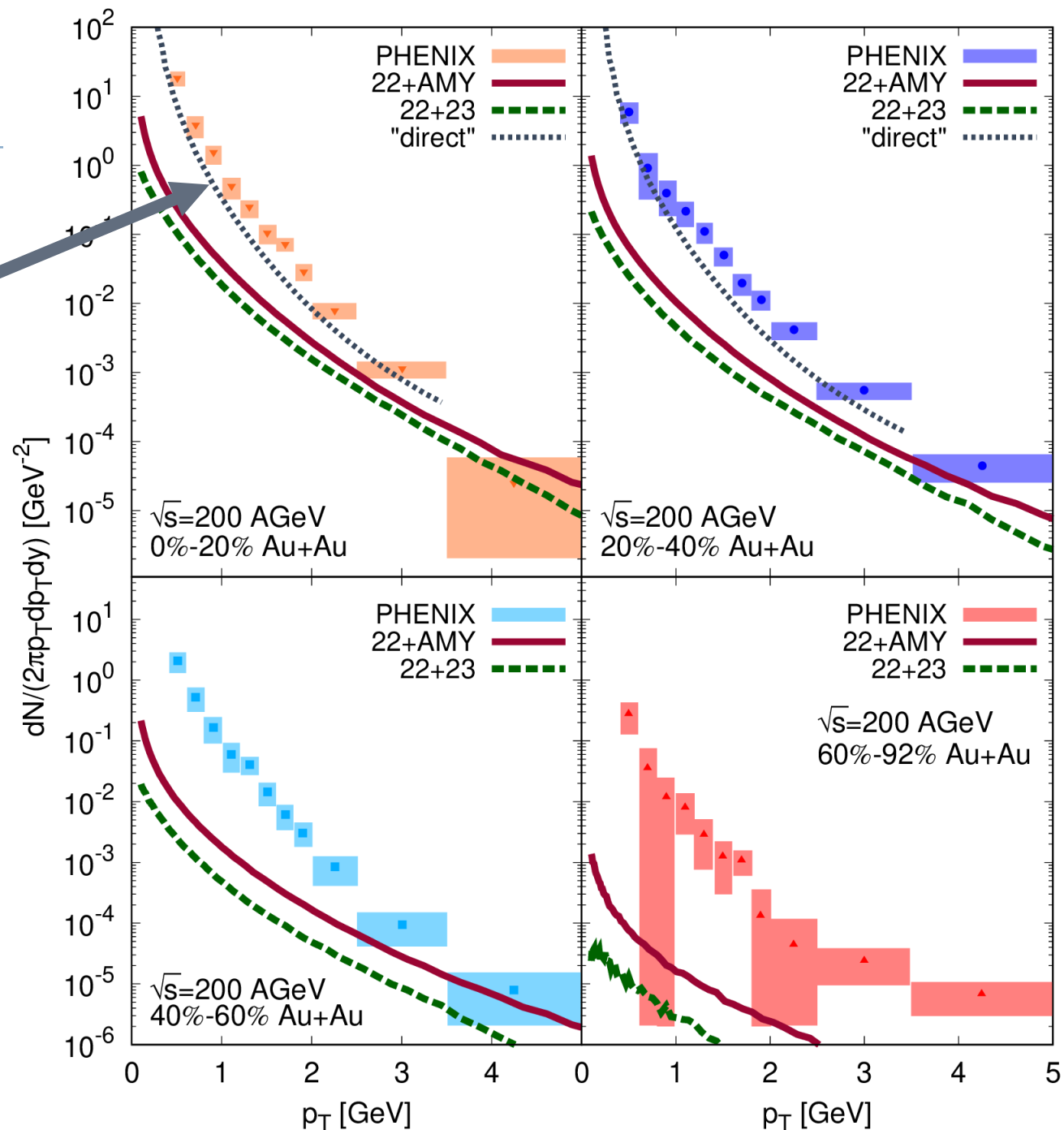


RHIC

„direct“ = prompt +
BAMPS AMY (QGP) +
MUSIC (Hadron gas)

(MUSIC results from Paquet et al.,
Phys.Rev. C93, 044906 (2016))

Heavy-ion
collision



RHIC

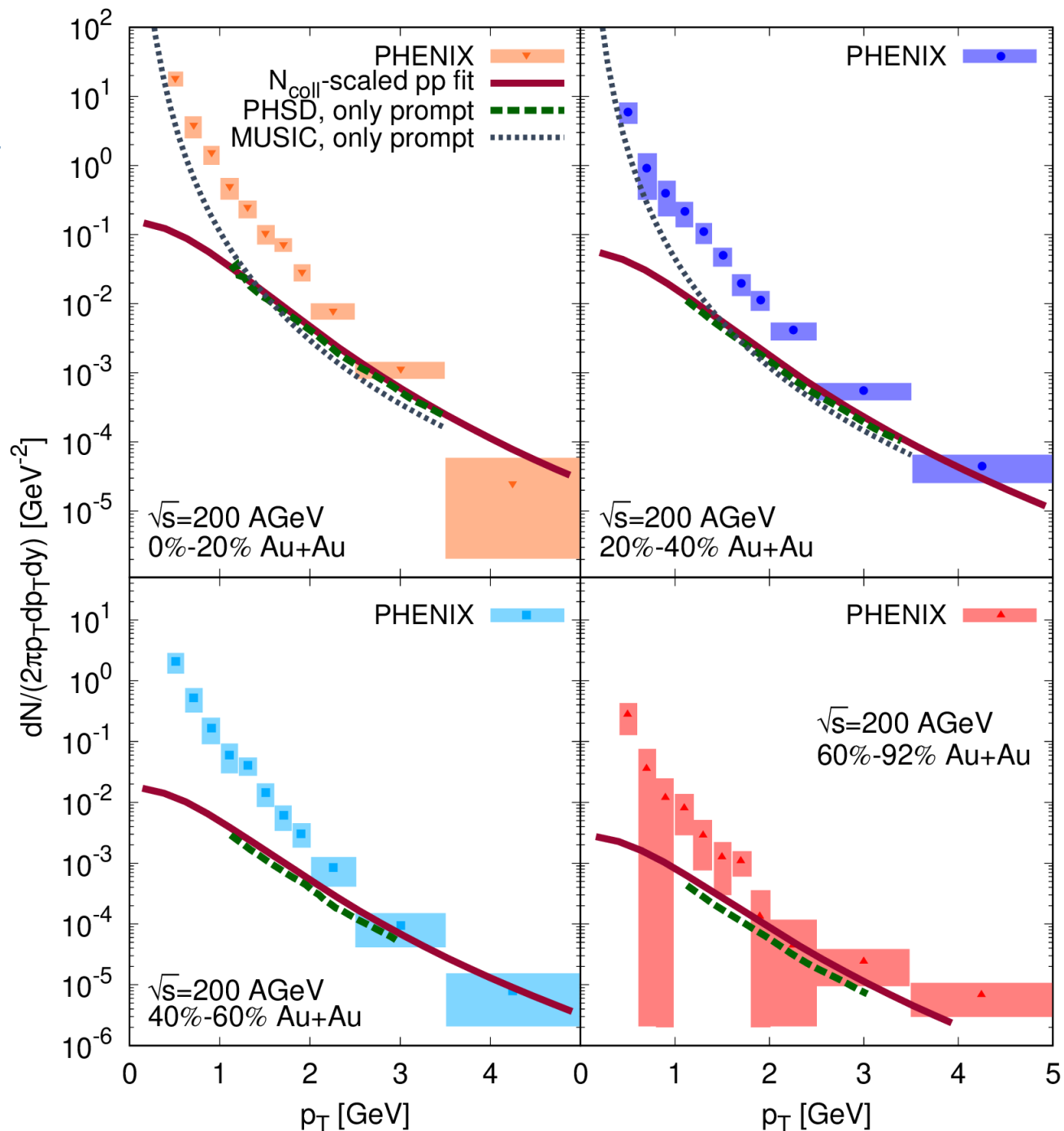
Prompt contribution from literature

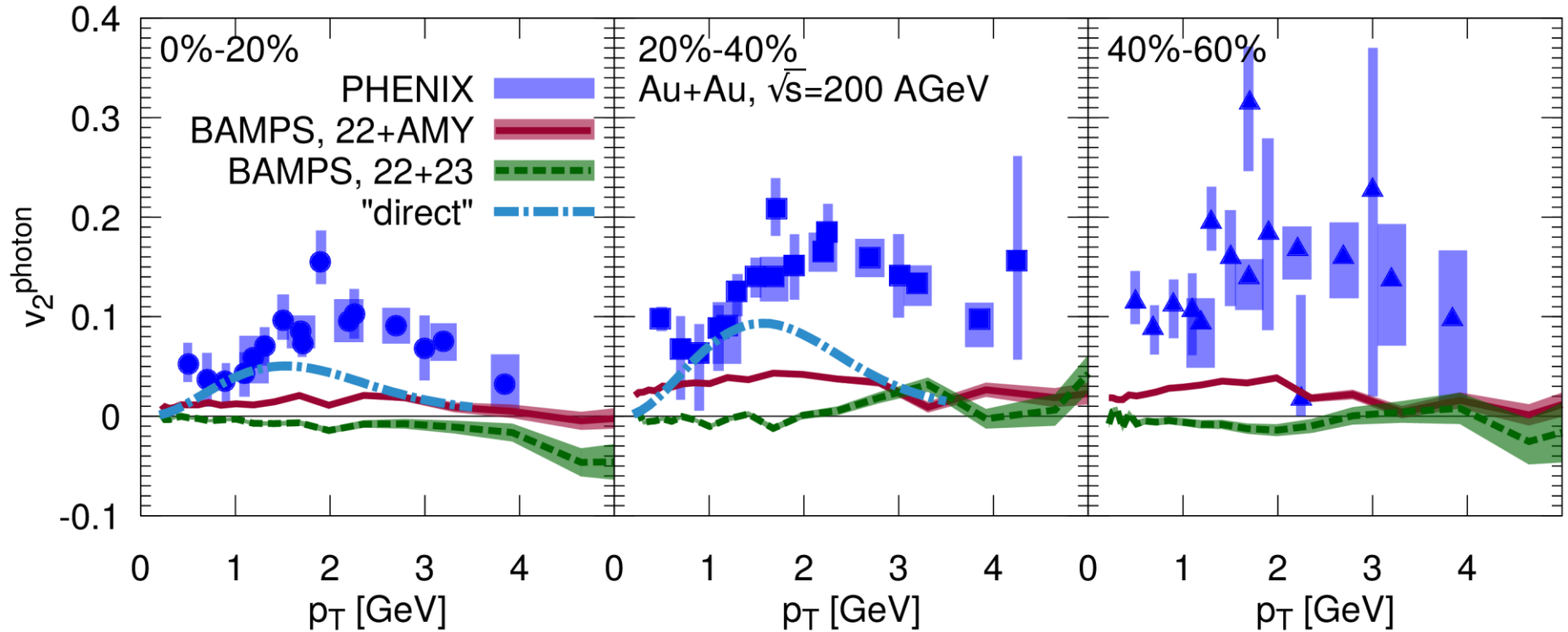
Paquet et al., Phys.Rev. C
93, 044906 (2016)

Linnyk et al., Phys.Rev. C
92, 054914 (2015)

PHENIX, Phys.Rev. C
91, 064904 (2015)

Heavy-ion
collision

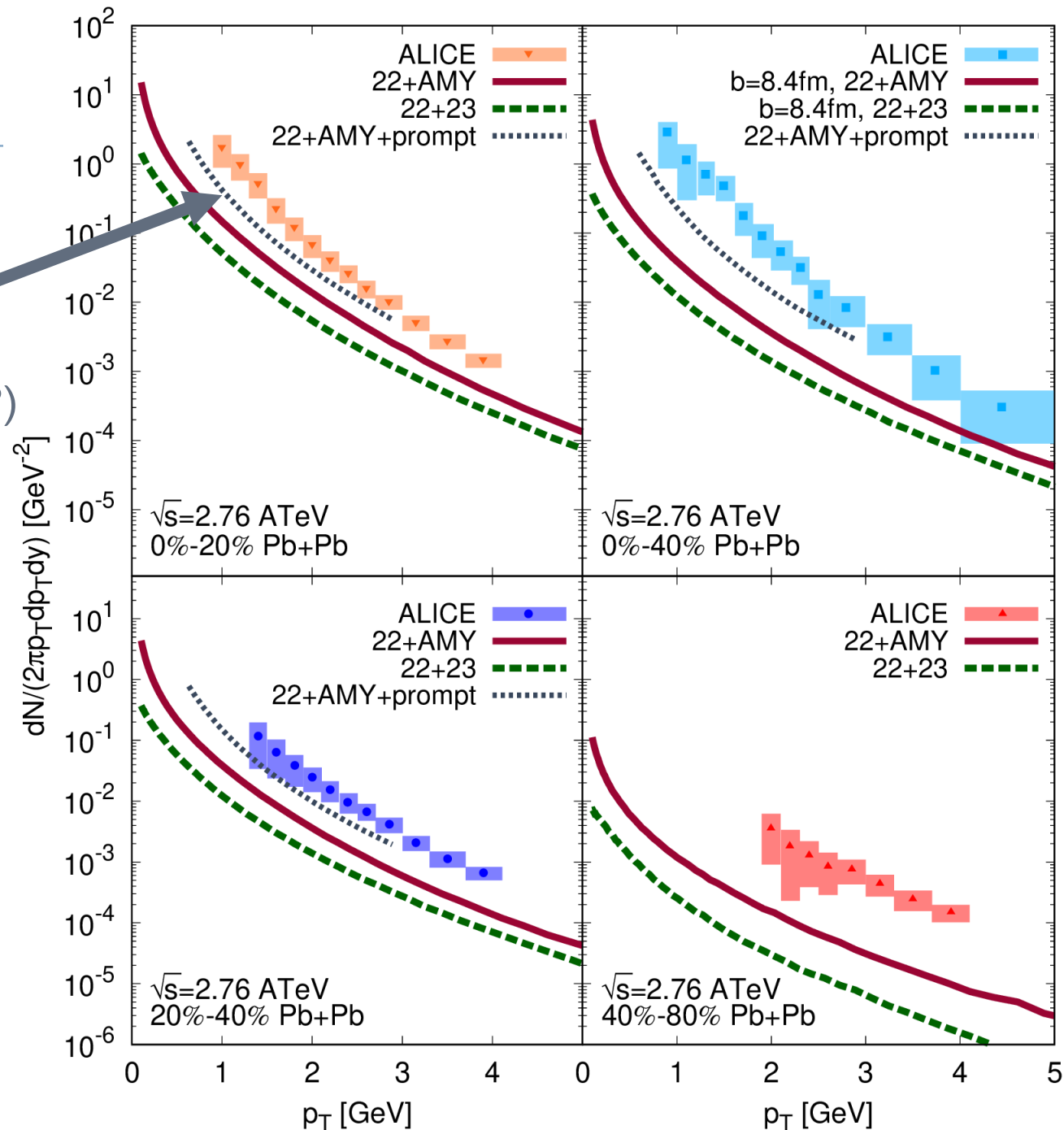


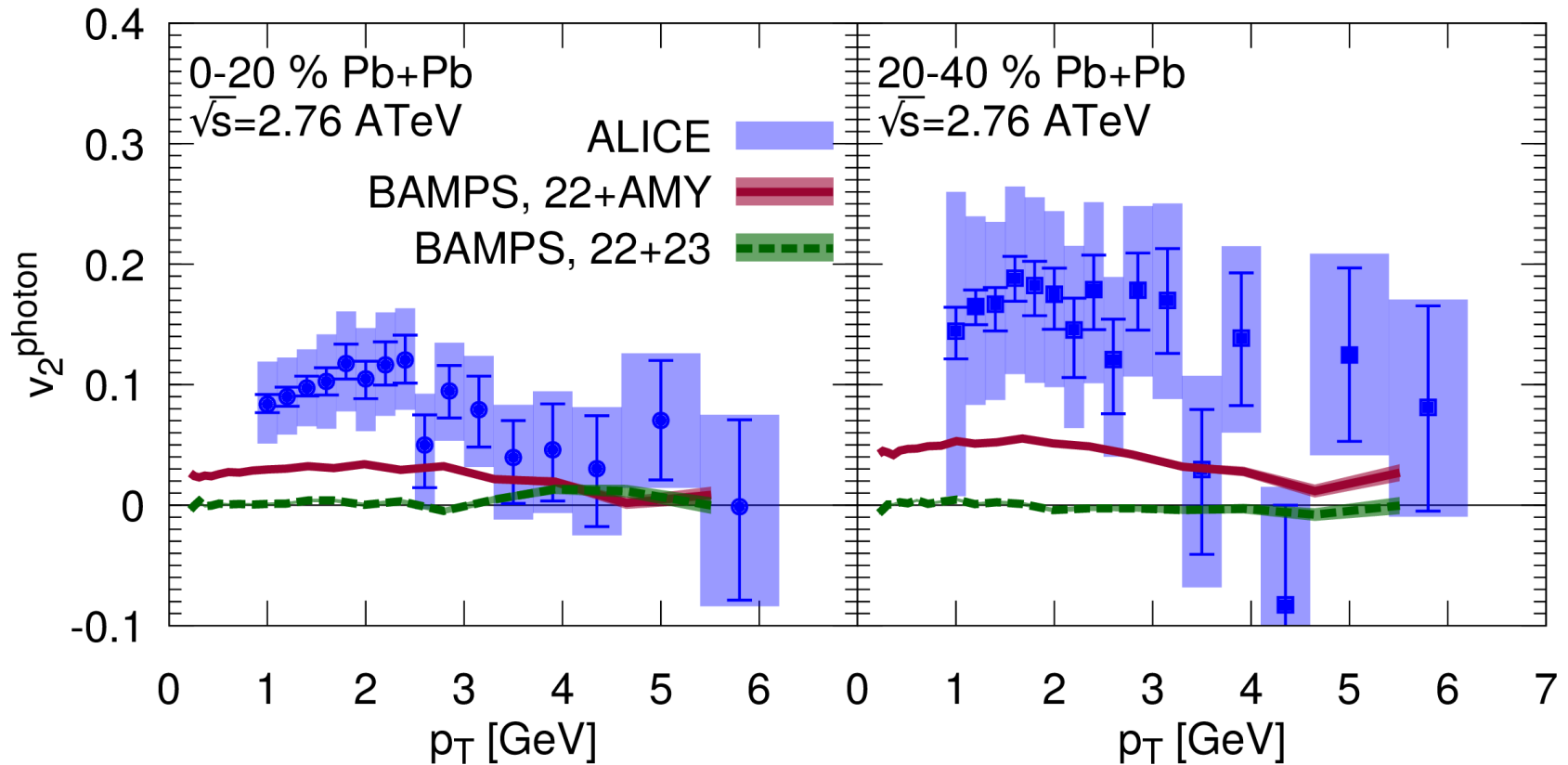


„direct“ = prompt +
BAMPS AMY (QGP) +
MUSIC (Hadron gas)

PHENIX, Phys.Rev. C94 (2016) no.6, 064901

prompt + BAMPS (QGP)
HG missing

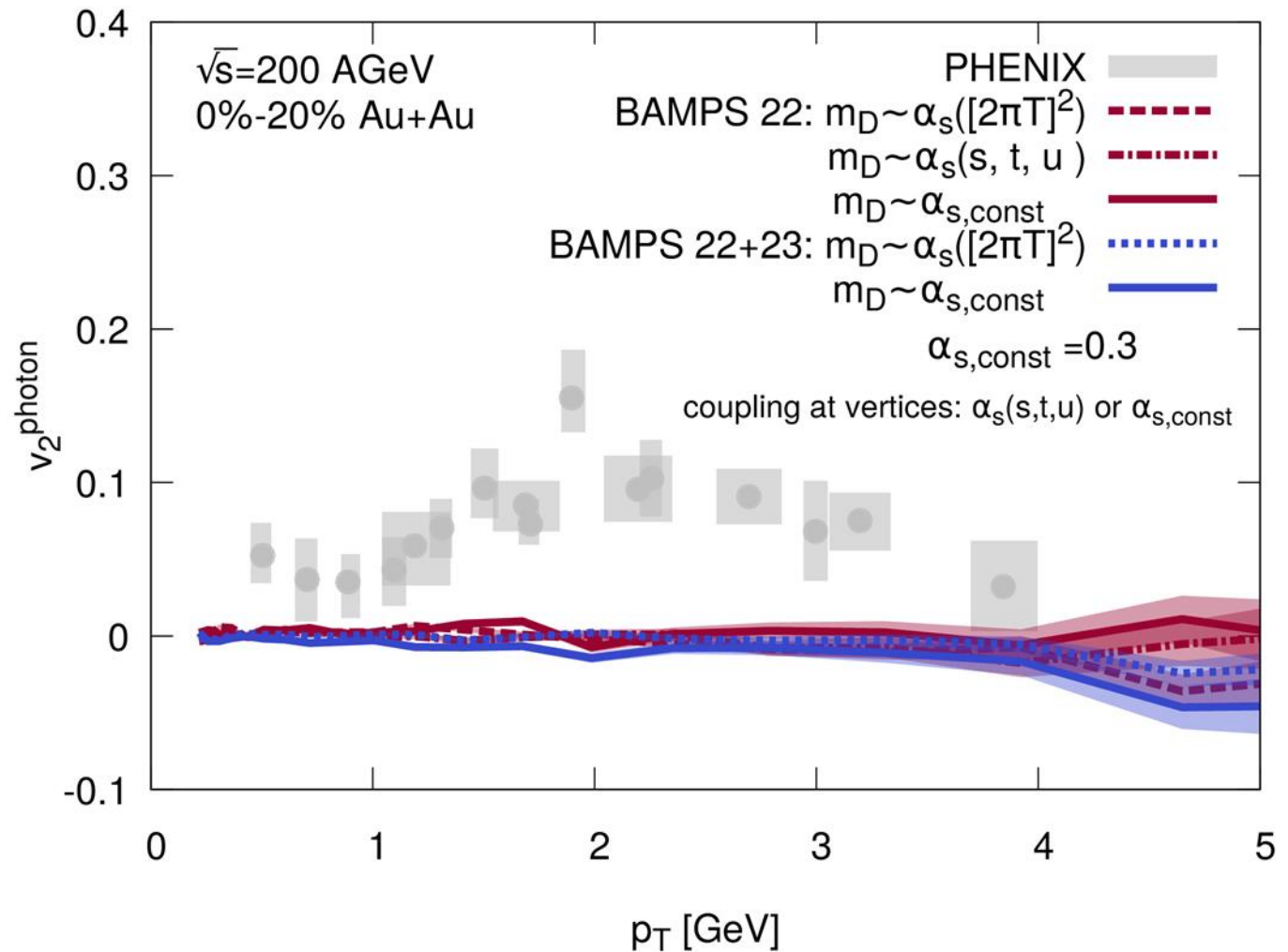




Only BAMPS (QGP)

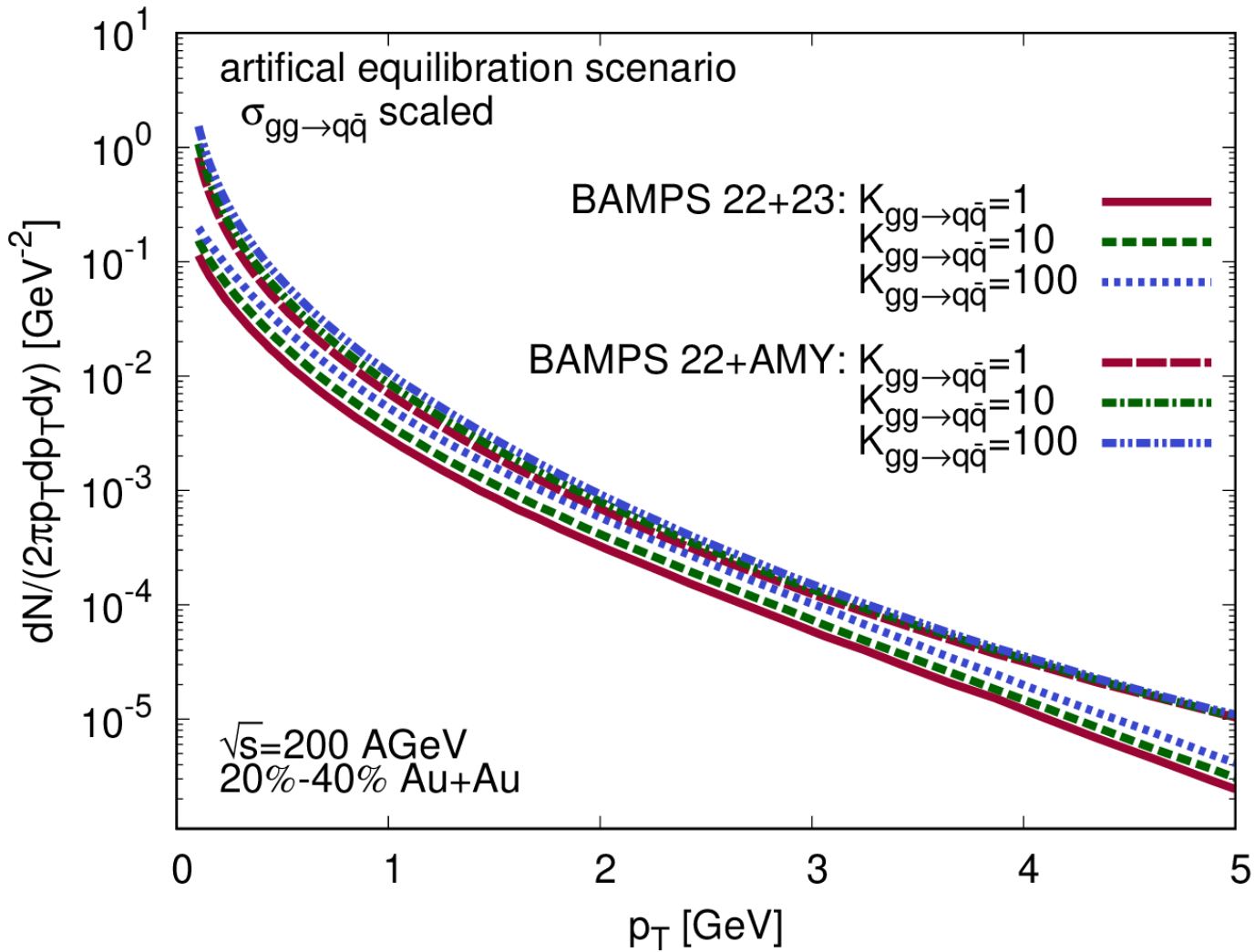
Mike Sas for ALICE, arXiv:1810.03861

Effect of running coupling



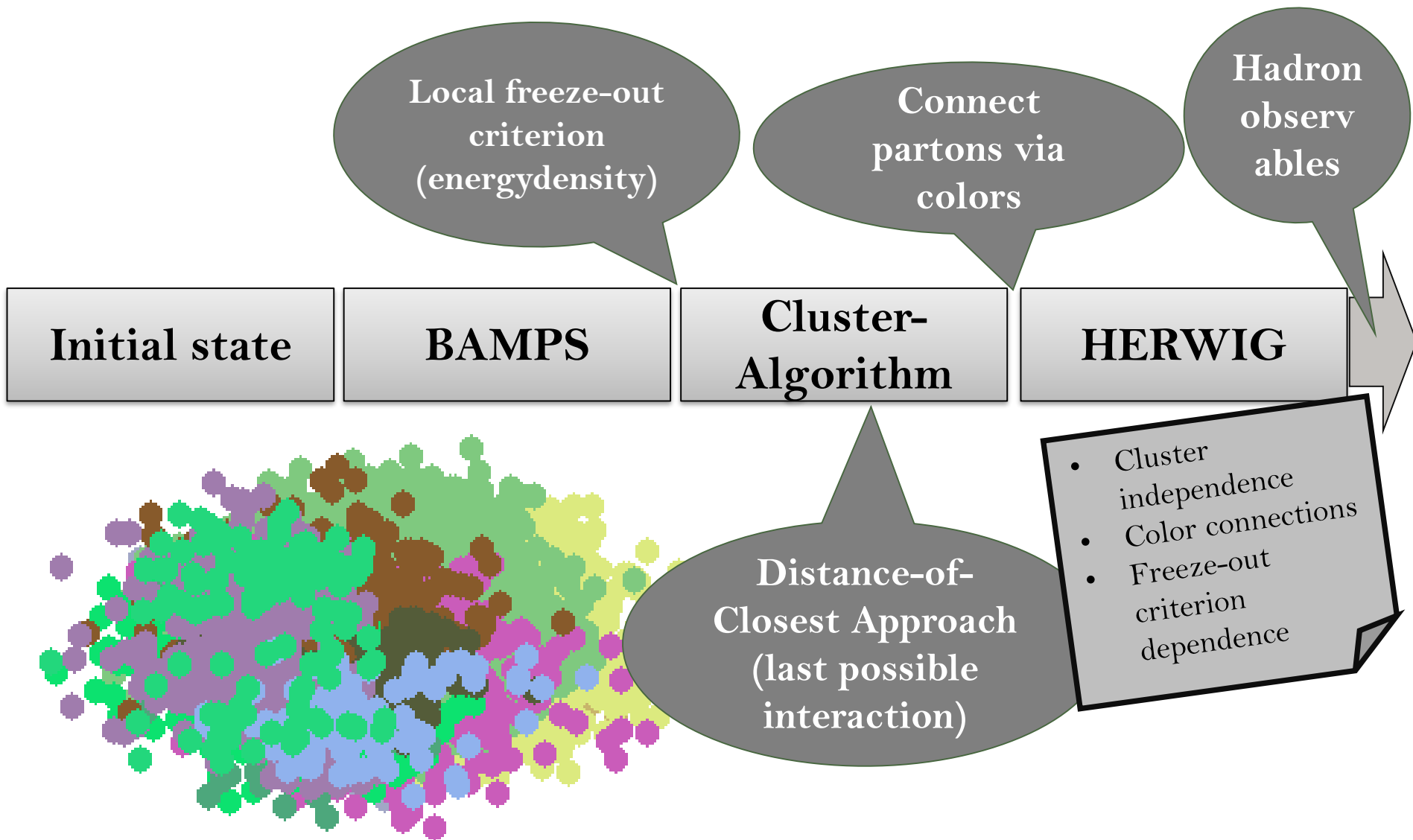
Only BAMPS (QGP)

Artificially fast chem. equilibration



Only BAMPS (QGP)

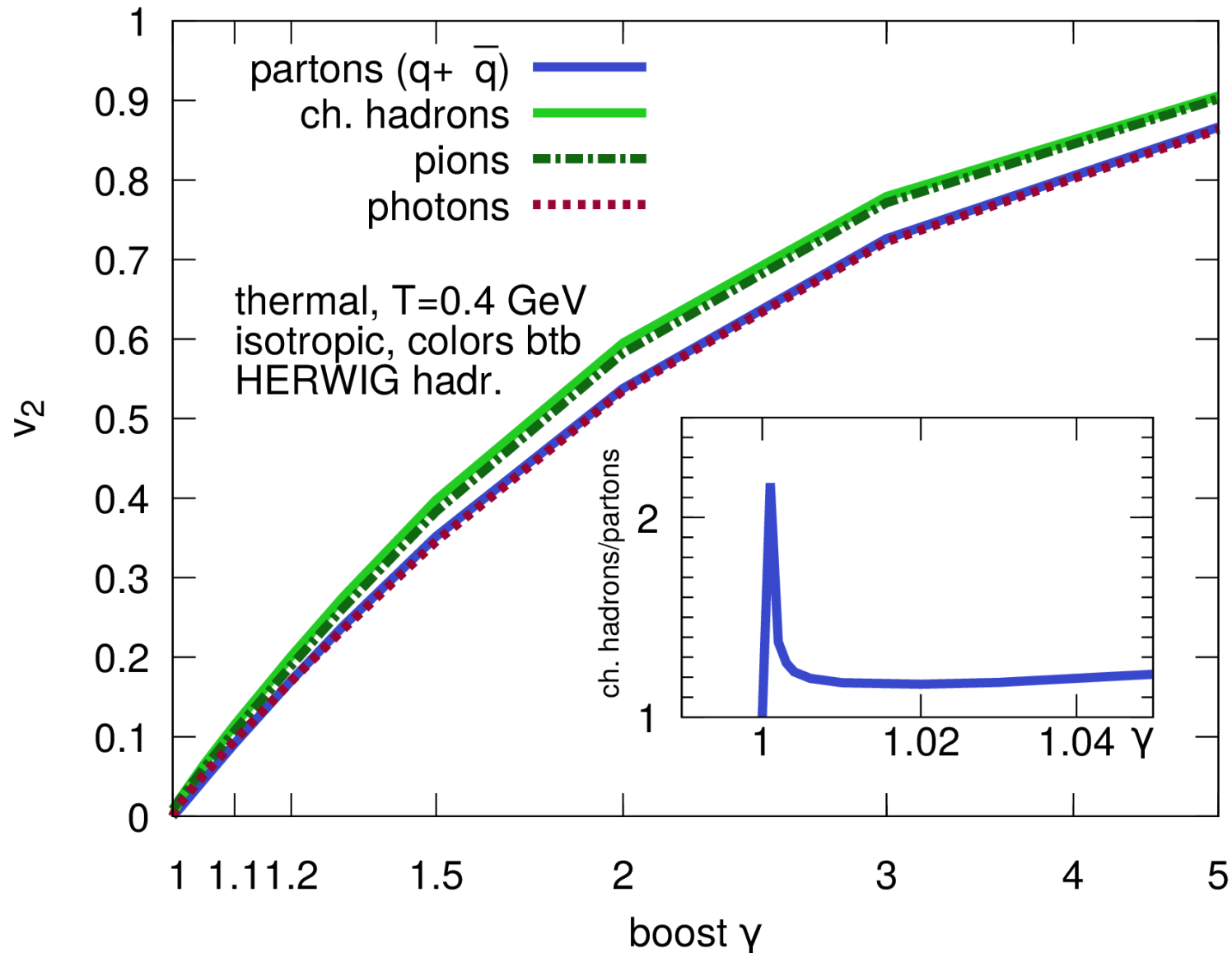
Outlook: Hadronization



See e.g., Bahr et al., HERWIG++, Eur.Phys.J. C58 (2008) 639-707

Courtesy to Simon Plätzer from HERWIG

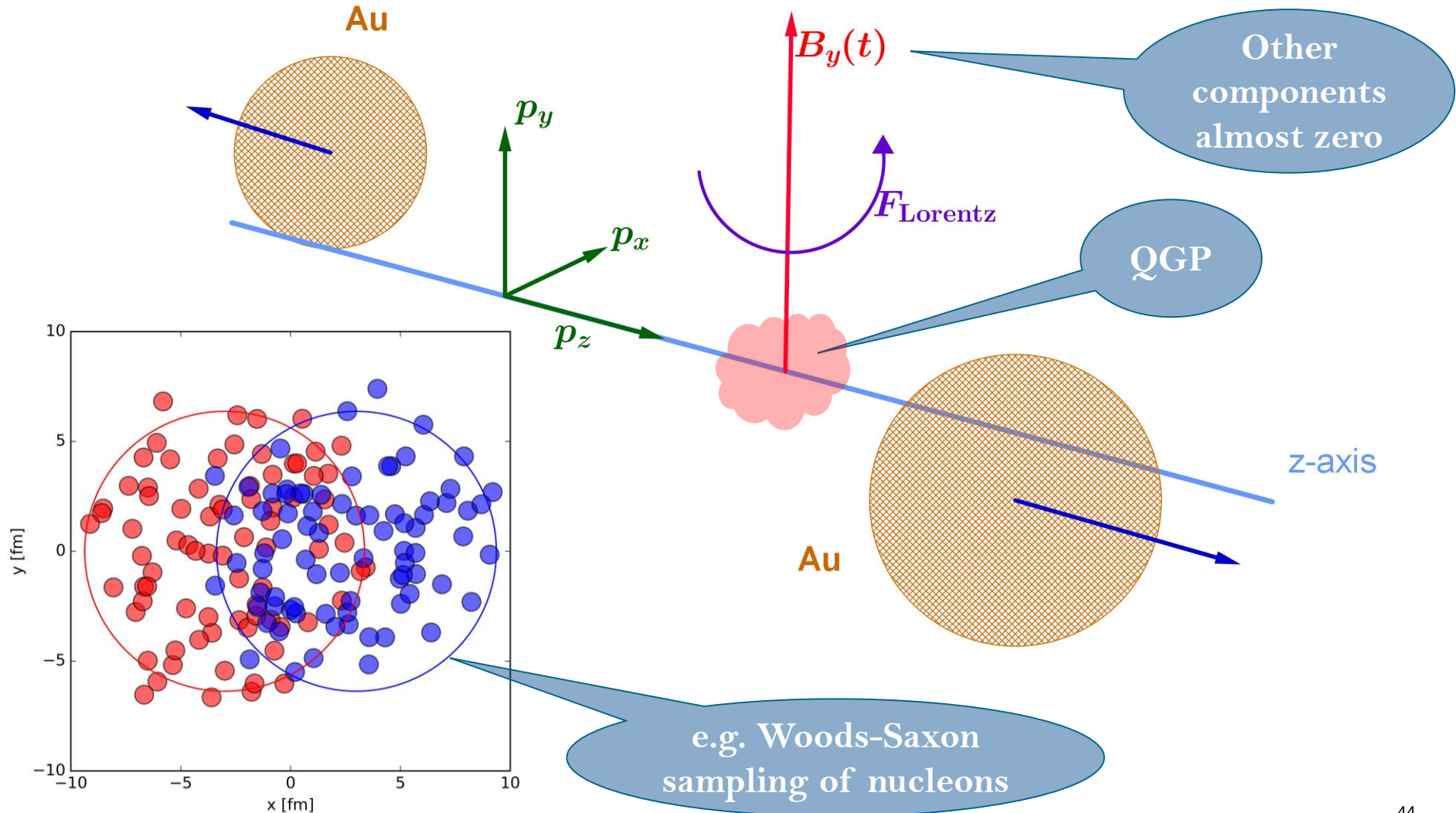
Flow effect from Hadronization?



Initial magnetic fields?

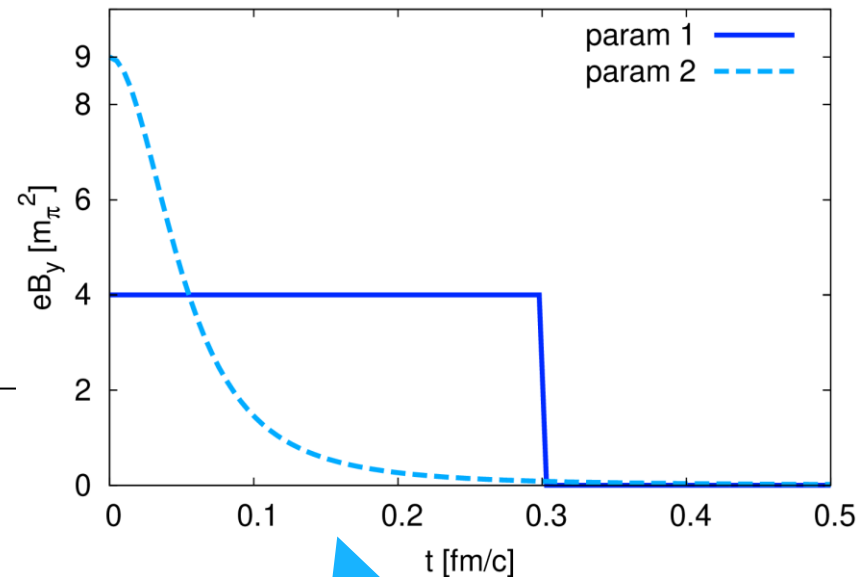
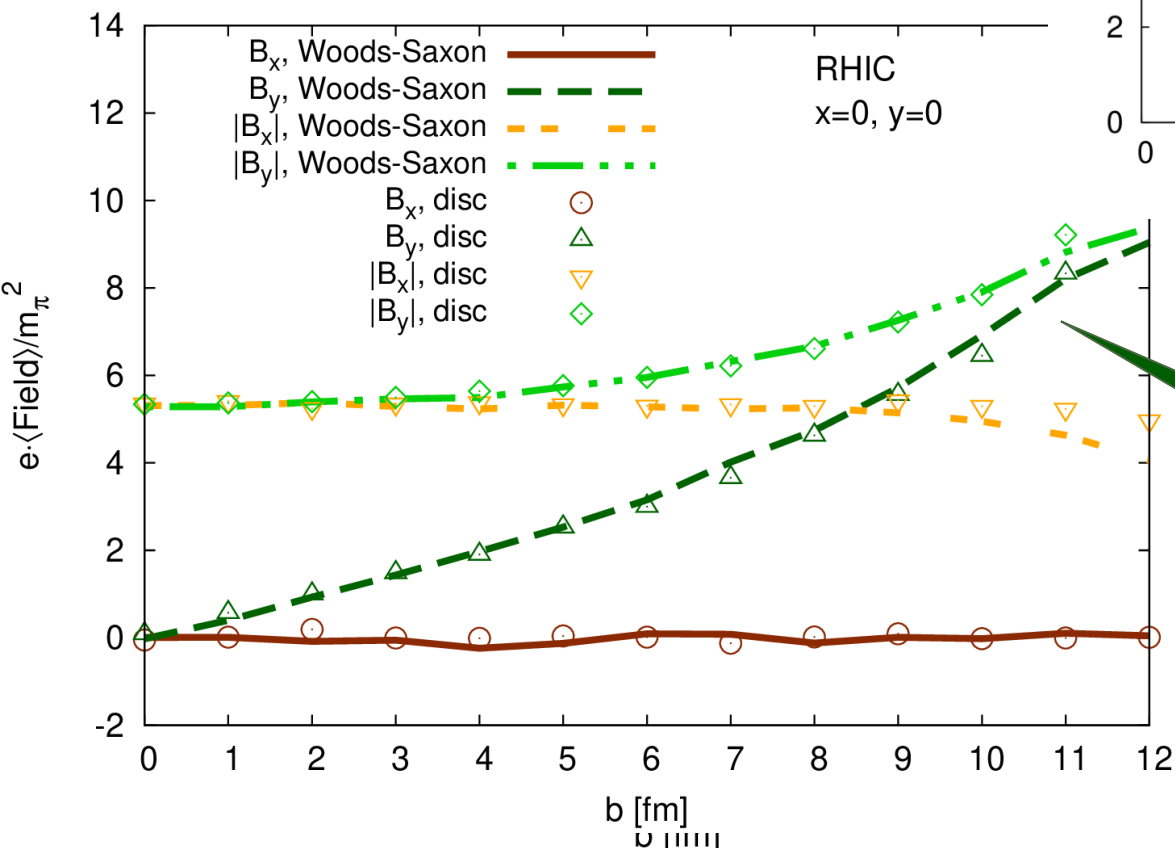
Magnetic field influence on the early time dynamics of heavy-ion collisions

MG, Carsten Greiner, Zhe Xu, Phys.Rev. C96 (2017) no.1, 014903



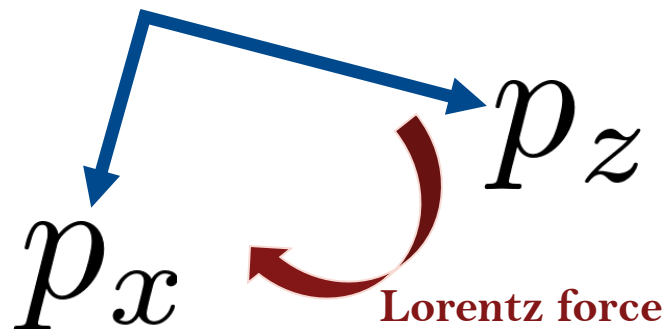
Initial magnetic fields-strong but short

- Simple parameterization
- „induction effect“ ignored
- Initial parton state: simple power law (exponent n), Boost invariant



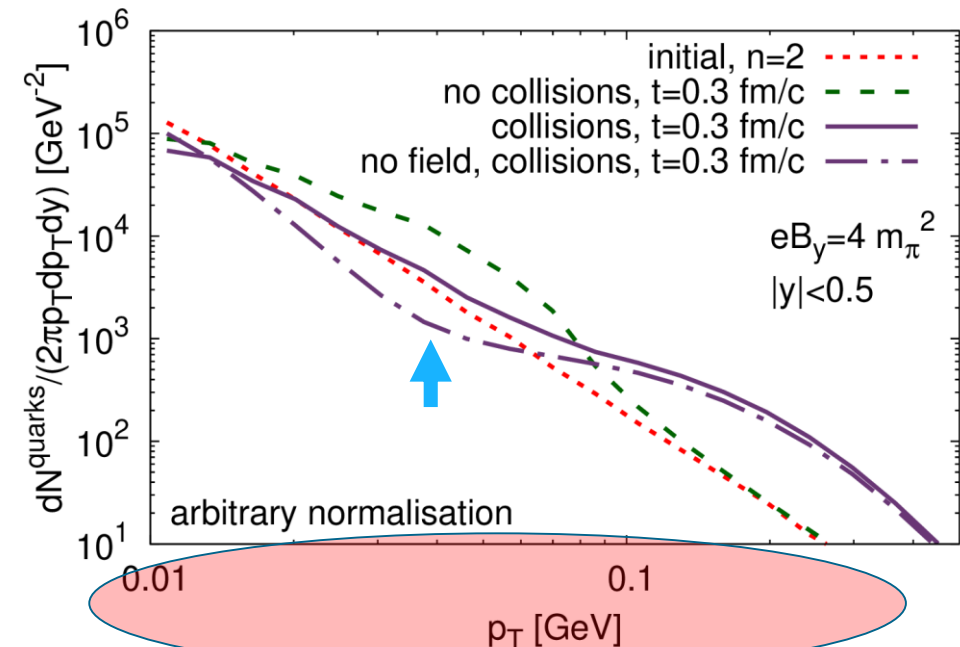
Large field,
but relaxes
fast to zero

Effect on quark spectra and flow?

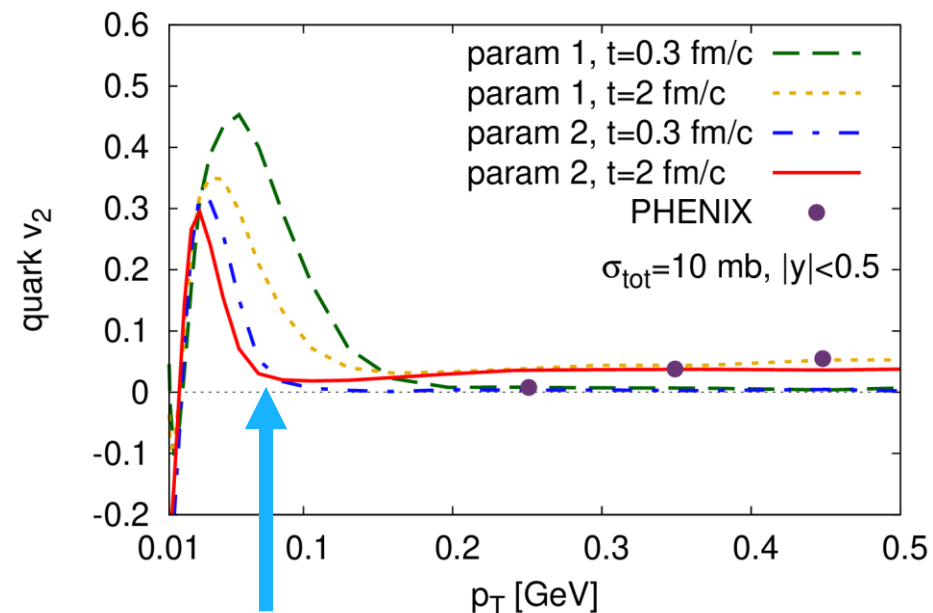


$$v_2 = \frac{p_x^2 - p_y^2}{p_T^2}$$

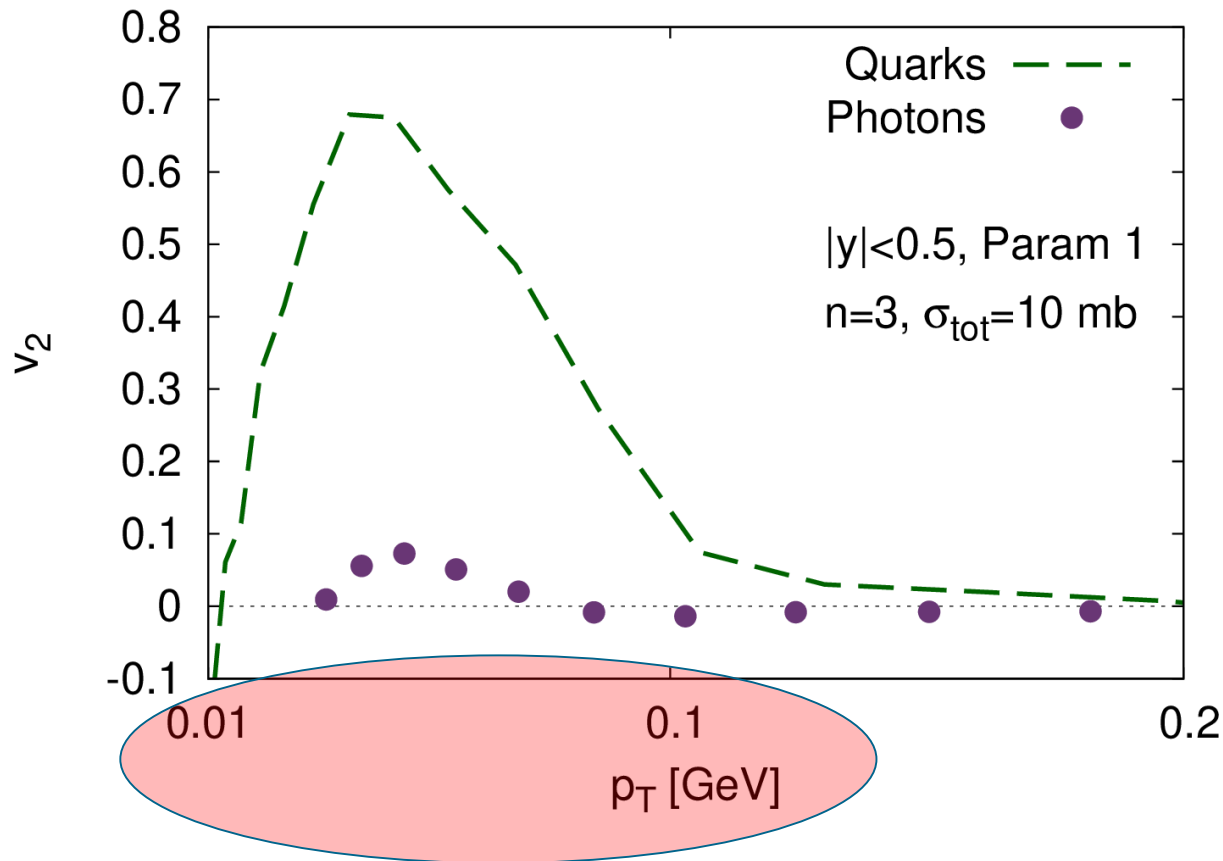
Quark spectrum, w and w/o collisions:



Elliptic flow only at very low p_T



Effect on photons?



- Small effect even with **optimistic** assumptions:
 - Initial quarks (not pure glue, CGC)
 - Magnetic field persistent for some time (parameterization 1)
 - No formation times (quarks immediately affected by field)
- My personal take home message: no effect

Photons from partonic transport

What?

- Microscopic leading order photon production in partonic transport
- Radiative photons using two different methods
- Matrix elements provide angular-differential kinematics

Results:

- Chemical quark undersaturation $\rightarrow$ little photon yield
- Strict collinearity of AMY changes flow $\rightarrow$ still too little
- Running coupling can help
- Magnetic field effect maybe irrelevant

Future possibilities:

- Prompt photons constraints?
- Chemical composition of initial state?
- Hadronization of parton cascade opens new doors