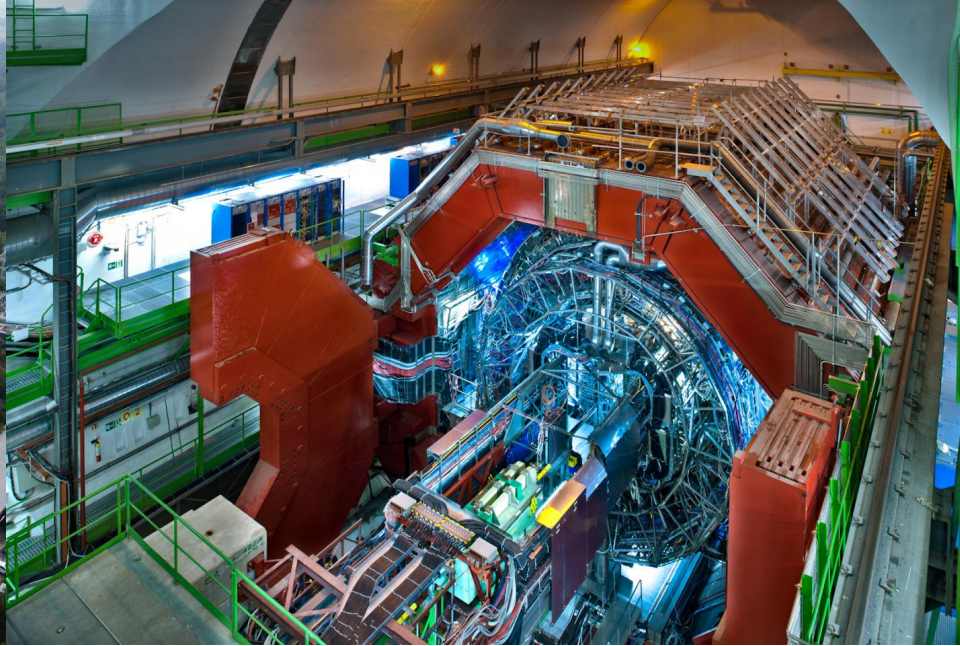




Femtoscscopy for strong interaction studies

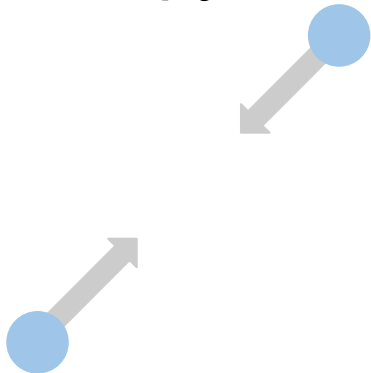
Maximilian Korwieser (TUM)
ECT*PANAM, 17.10.25

Maximilian Korwieser | TUM E62 | max.korwieser@tum.de

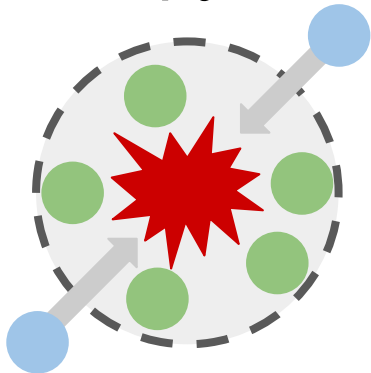


TUM Femtoscopy in a nutshell

[Ann.Rev.Nucl.Part.Sci.55:357-402, 2005](#)

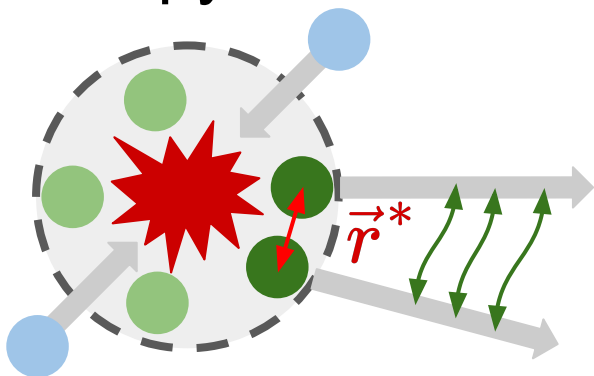


TUM Femtoscopy in a nutshell



[*Ann.Rev.Nucl.Part.Sci.55:357-402, 2005*](#)

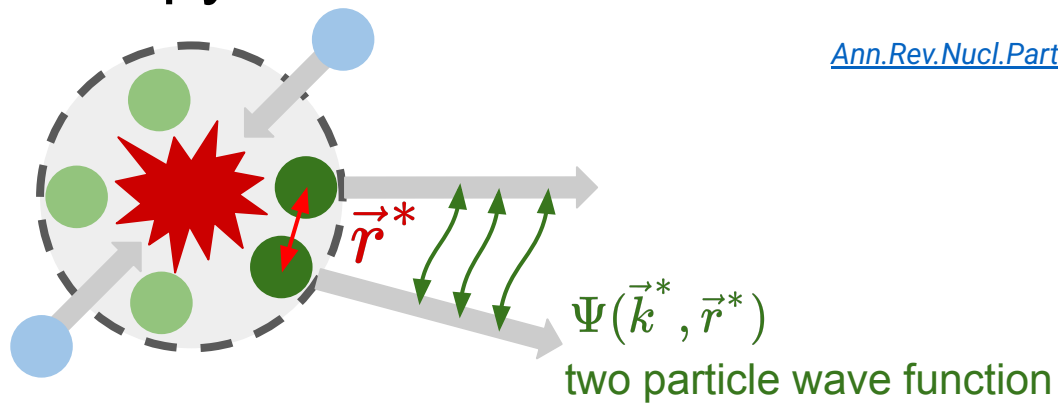
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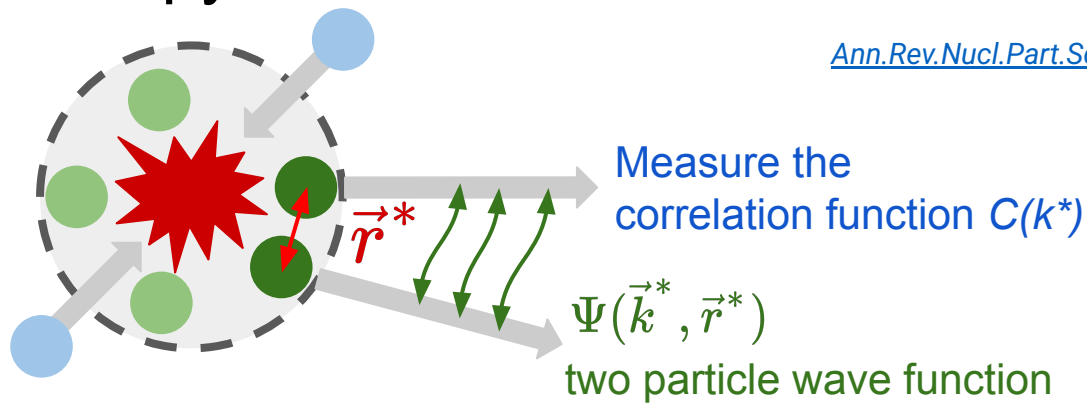
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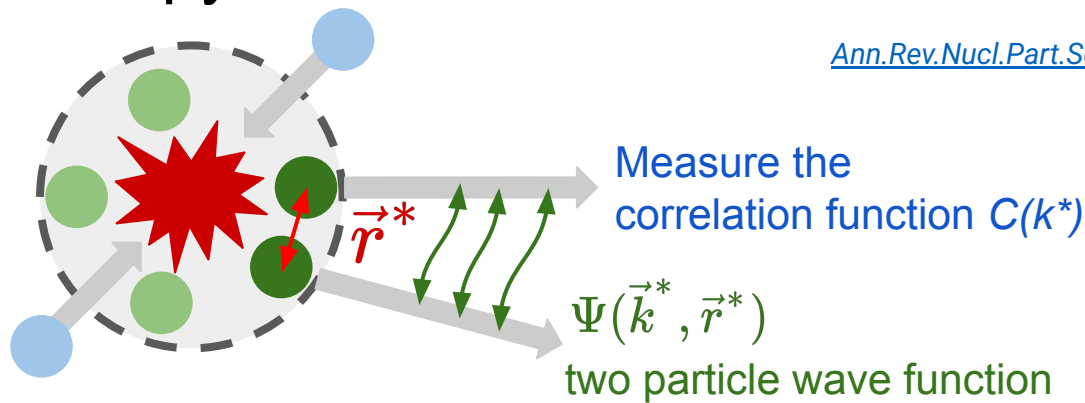
[Ann.Rev.Nucl.Part.Sci.55:357-402, 2005](#)



TUM Femtoscopy in a nutshell

[*Ann.Rev.Nucl.Part.Sci.55:357-402, 2005*](#)

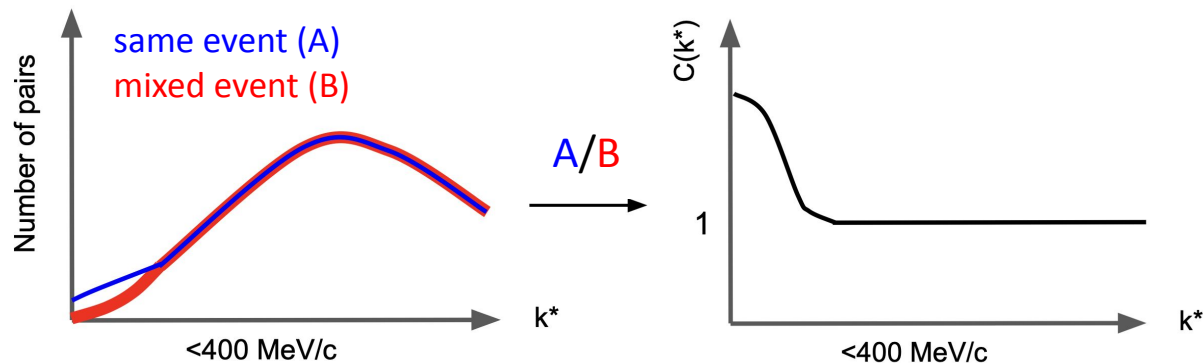
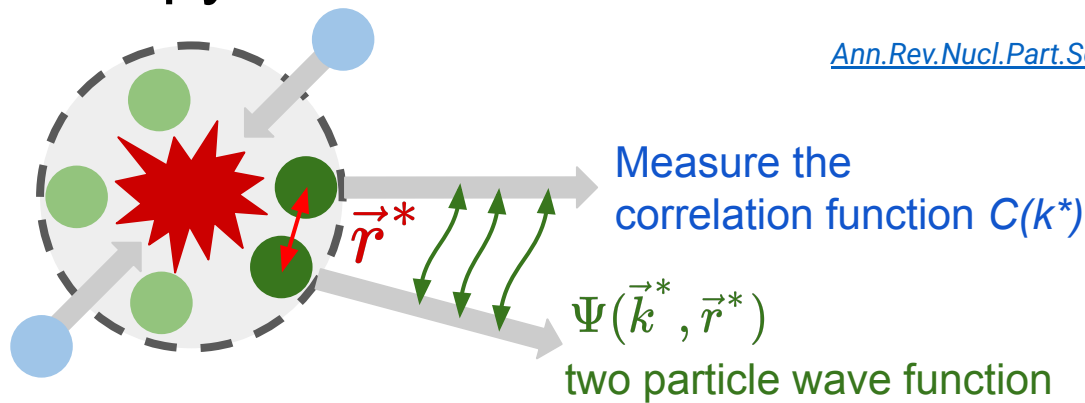




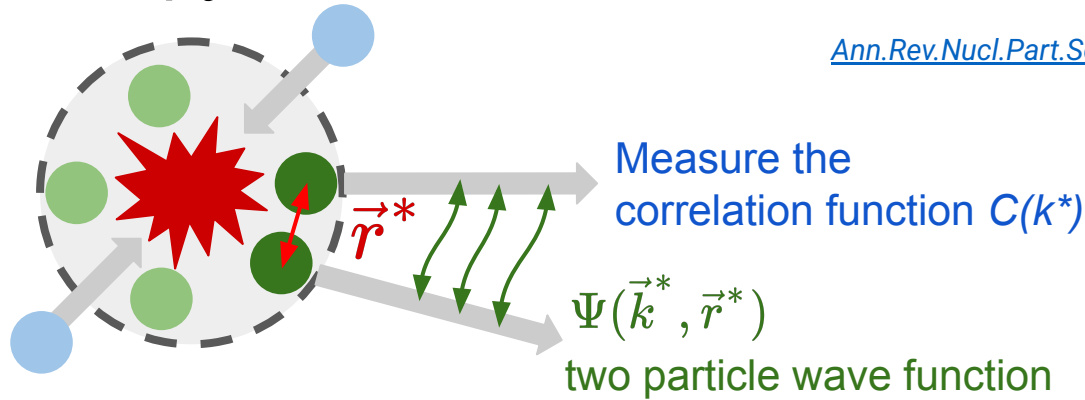
$$C(k^*) = \mathcal{N} \frac{N_{\text{SE}}(k^*)}{N_{\text{ME}}(k^*)}$$

Particle pair observed in the same event

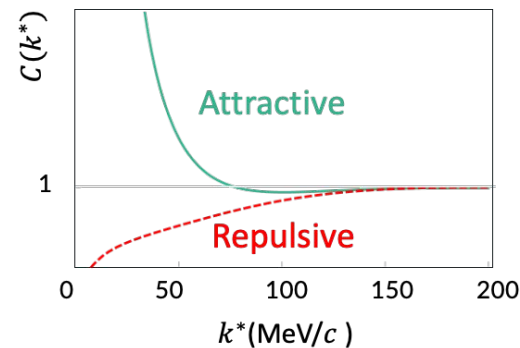
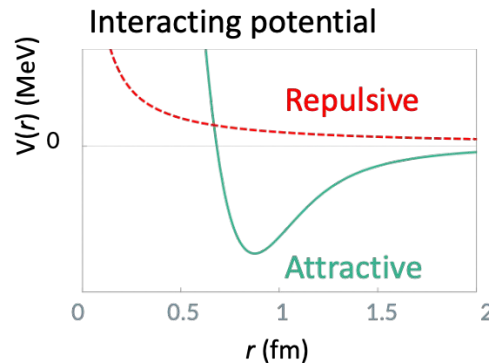
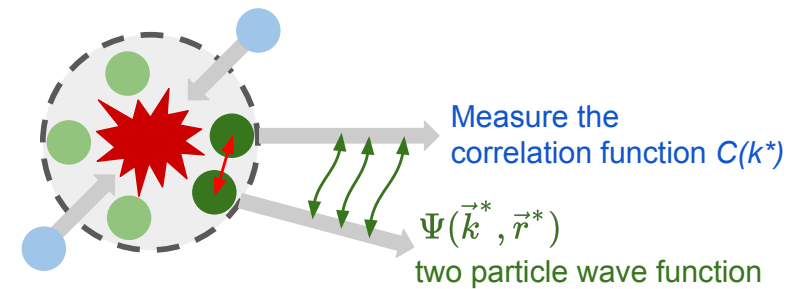
Particle pair constructed from different events



[Ann.Rev.Nucl.Part.Sci.55:357-402, 2005](#)



$$C(k^*) = \int S(r^*) \left| \Psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3 r^* \xrightarrow{k^* \rightarrow \infty} 1$$

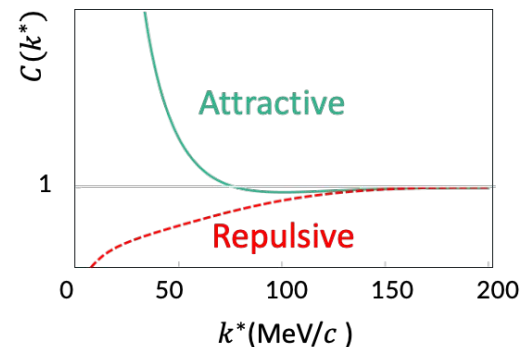
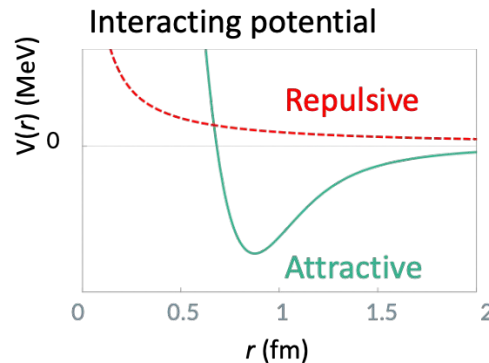
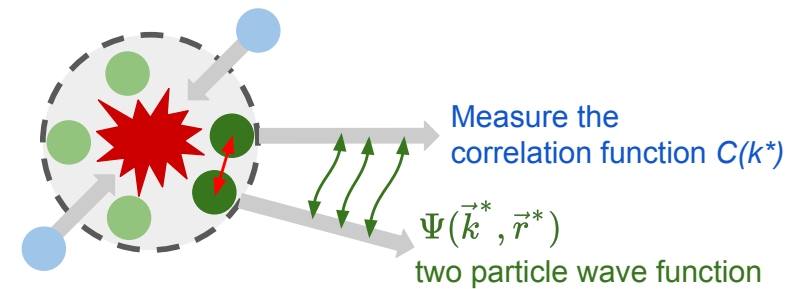


Emission Source $S(r^*)$

Schrödinger equation
Two-particle wave function

Correlation function $C(k^*)$

$$C(k^*) = \int S(r^*) \left| \Psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3 r^* \xrightarrow{k^* \rightarrow \infty} 1$$



Emission Source $S(r^*)$

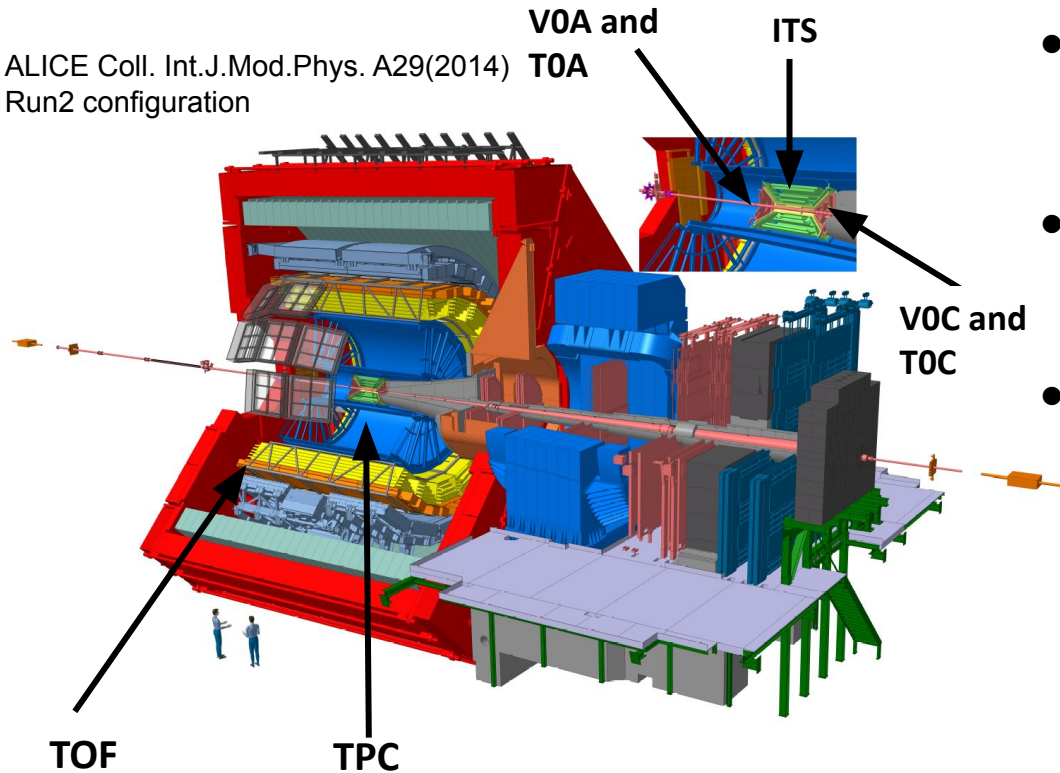
Schrödinger equation
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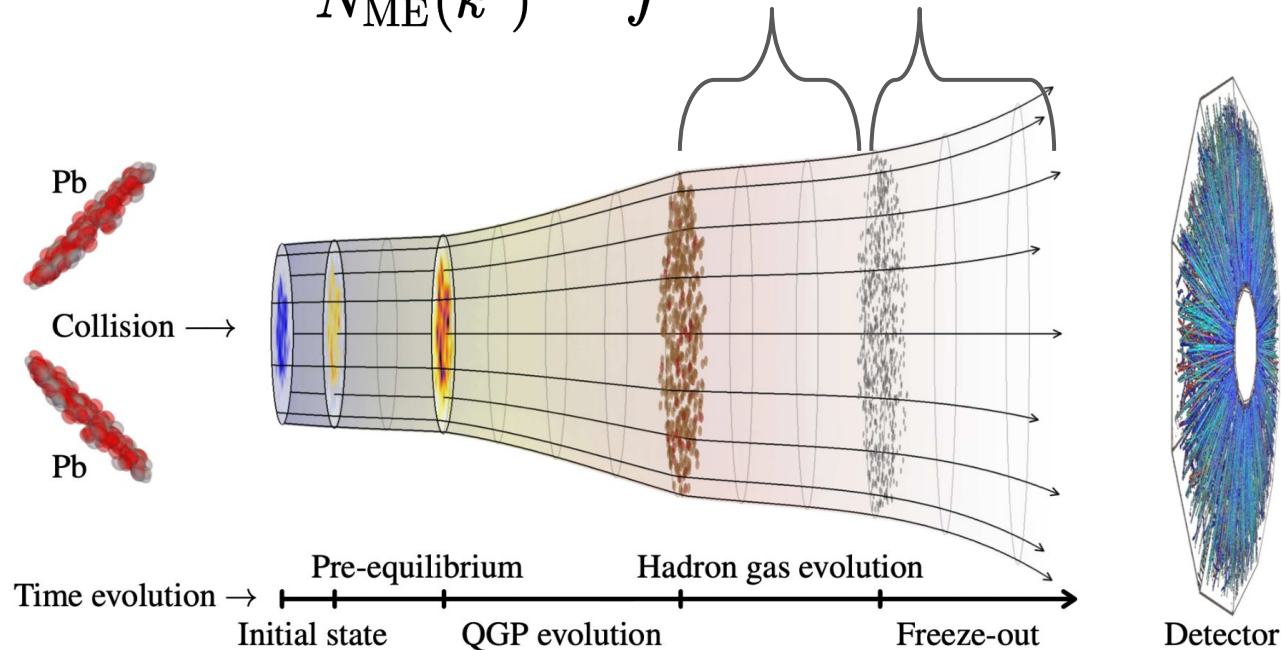
- Measure $C(k^*)$, use well known interaction, study $S(r^*)$
- For evaluation of integral and $S(r^*)$ use CATS framework [Eur.Phys.J.C 78 \(2018\) 5.394](https://arxiv.org/abs/1805.09744)

ALICE Coll. Int.J.Mod.Phys. A29(2014)
Run2 configuration

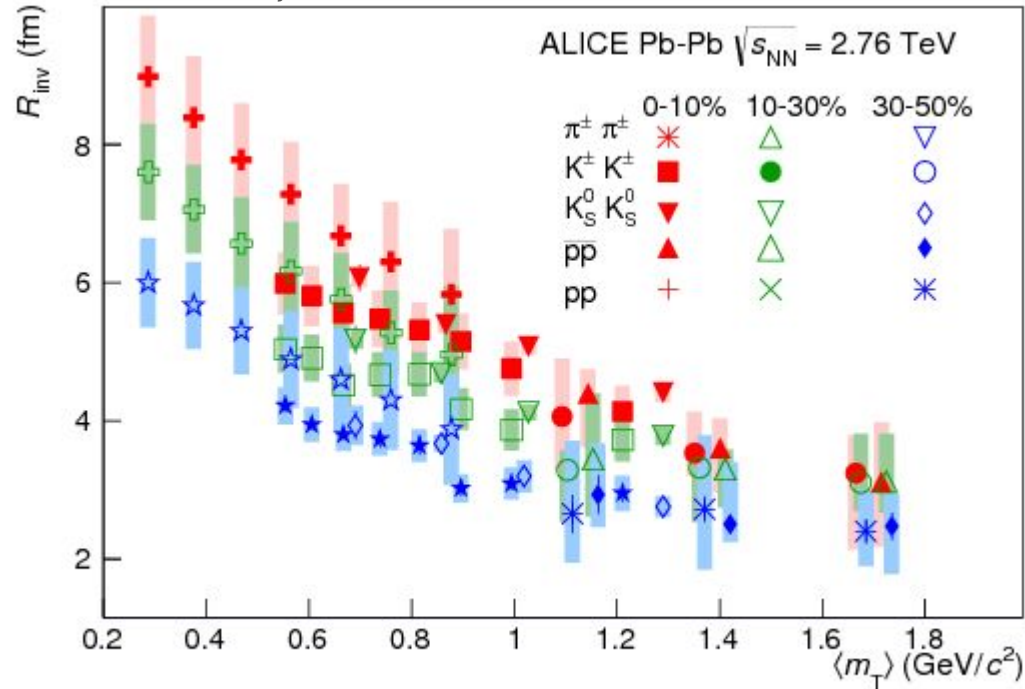


- HM pp collisions @ 13 TeV
 - 1 Billion evts. in Run2
- Direct detection of charged particles (π , K, p) by TPC and TOF
- Particle identification
 - Mean energy loss in TPC
 - Momentum reconstruction by TOF
 - Purity of about 99 % for π , K, p due to excellent PID capabilities

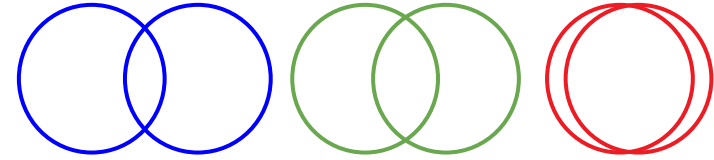
$$C(k^*) = \mathcal{N} \frac{N_{\text{SE}}(k^*)}{N_{\text{ME}}(k^*)} = \int S(r^*) |\Psi(k^*)|^2 d^3 r^* \xrightarrow{k^* \rightarrow \infty} 1$$



ALICE Phys. Rev. C **99**, 064901



- Centrality as a measure of the overlap

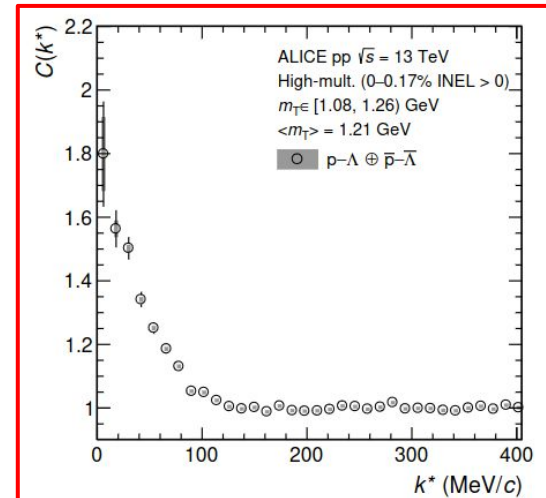
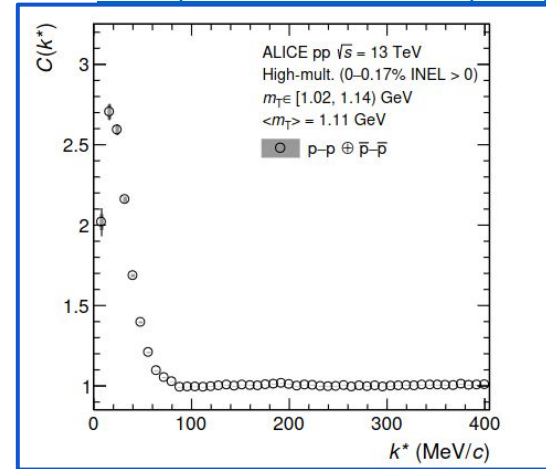


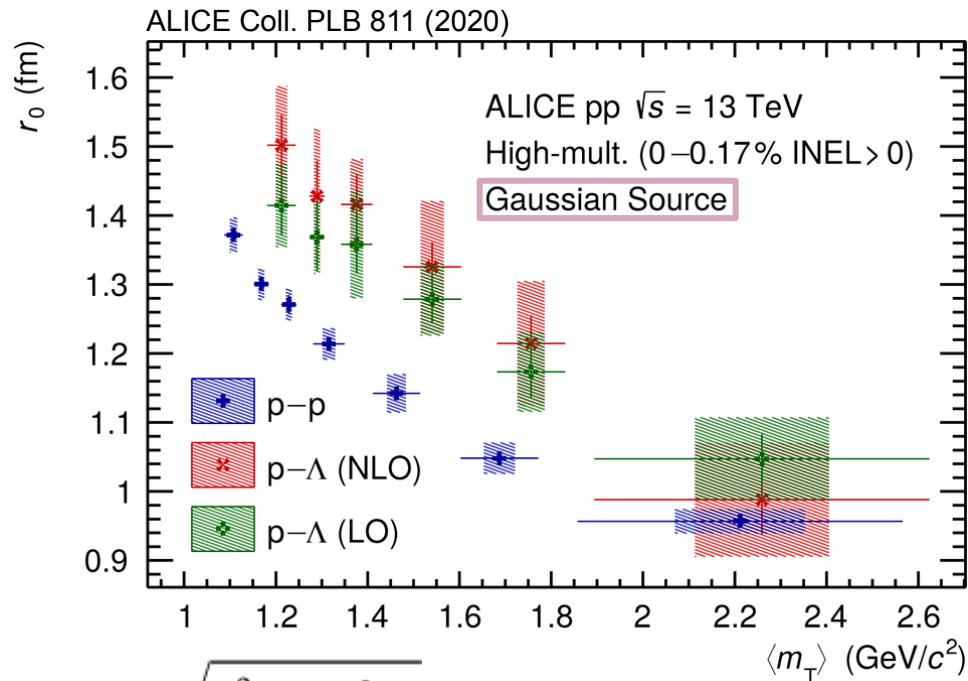
- Most simple ansatz for $S(r^*)$ is a Gaussian
- Scaling in Pb-Pb for identical pairs
- Dependence on centrality/multiplicity and transverse mass (m_T)

- Common source for all produced hadrons in small systems?
- Use $p\text{--}p$ (well known interaction) to constrain the femtoscopic source
- Validate findings with $p\text{--}\Lambda$

$$m_T = \sqrt{k_T^2 + m_{\text{avg}}^2}$$

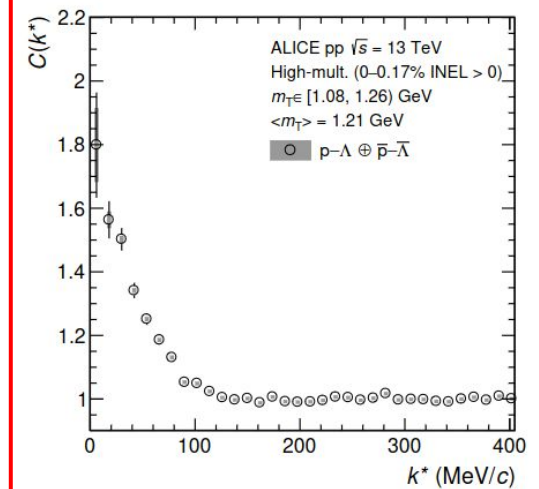
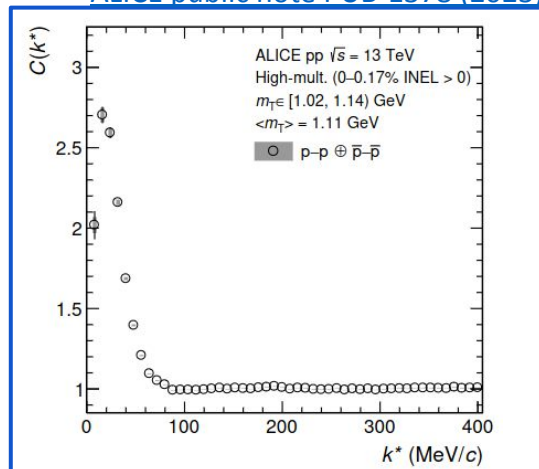
$$k_T = \frac{1}{2} |\vec{p}_{T,1} + \vec{p}_{T,2}|$$

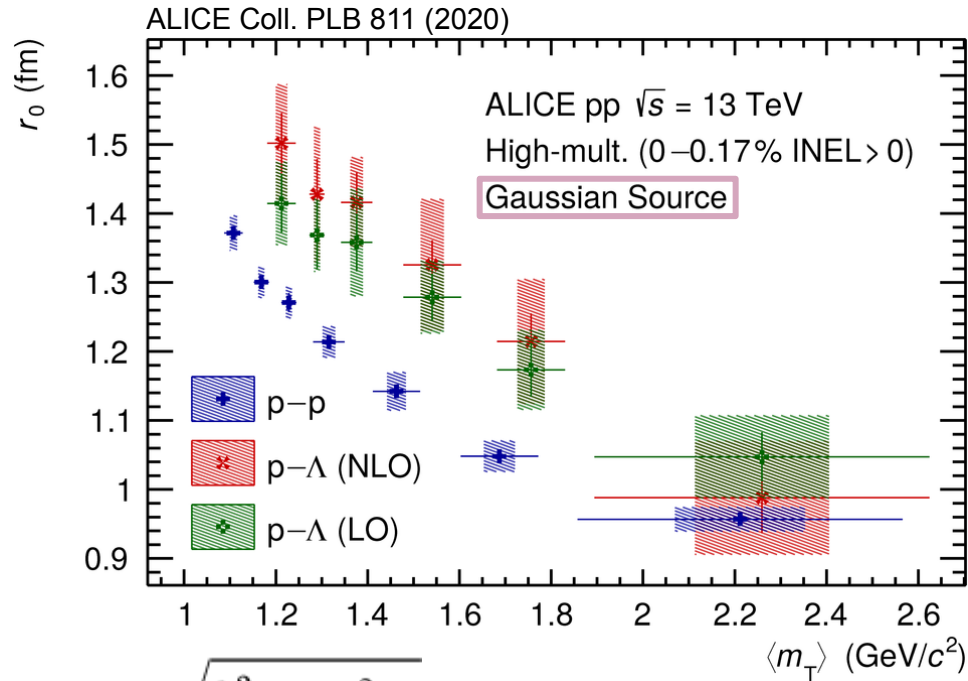




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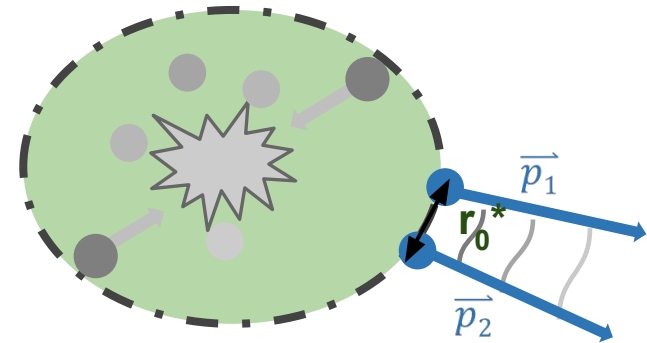




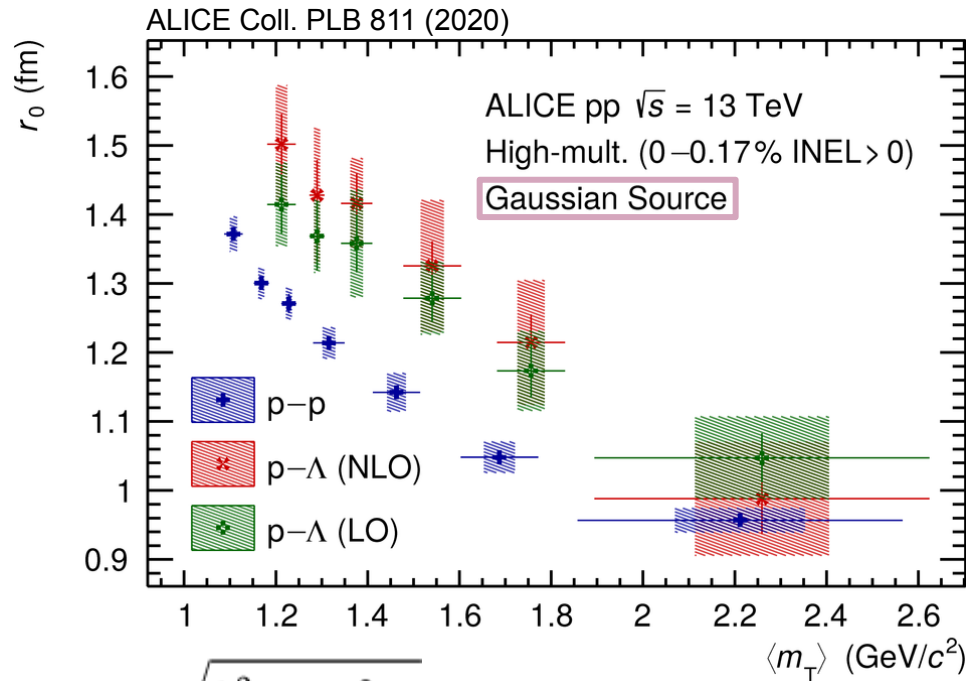
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$$k_T = \frac{1}{2} |\vec{p}_{T,1} + \vec{p}_{T,2}|$$

- Scaling is expected for common radial flow velocity and hadronization time scale



TUM Baryon source in small systems

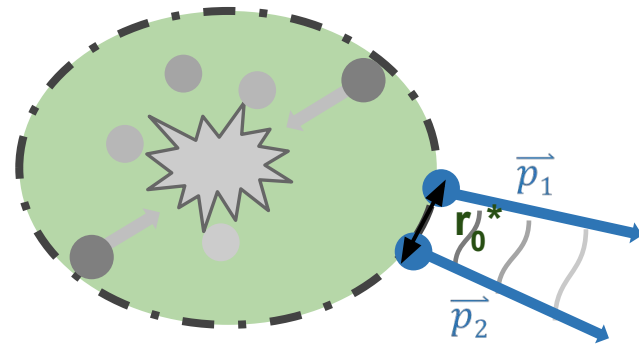


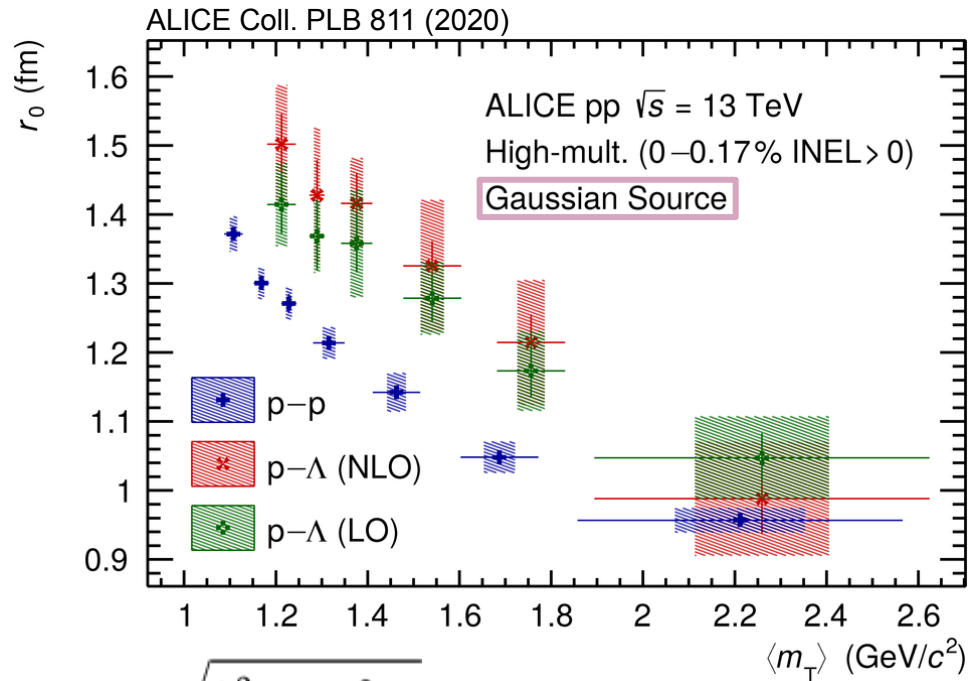
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- [1] Y. Sinyukov et al. NPA 946 (2016)
[2] A. Widemann et al. PRC 865 56 (1997)

- Scaling is expected for common radial flow velocity and hadronization time scale
- Effects influencing the scaling include **non-gaussian** contributions to the source
- **Feed down from resonances** [1,2]





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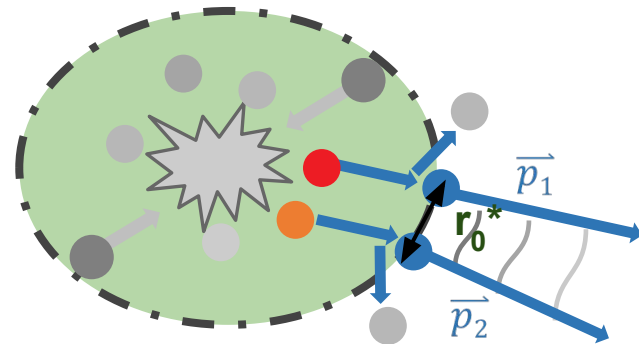
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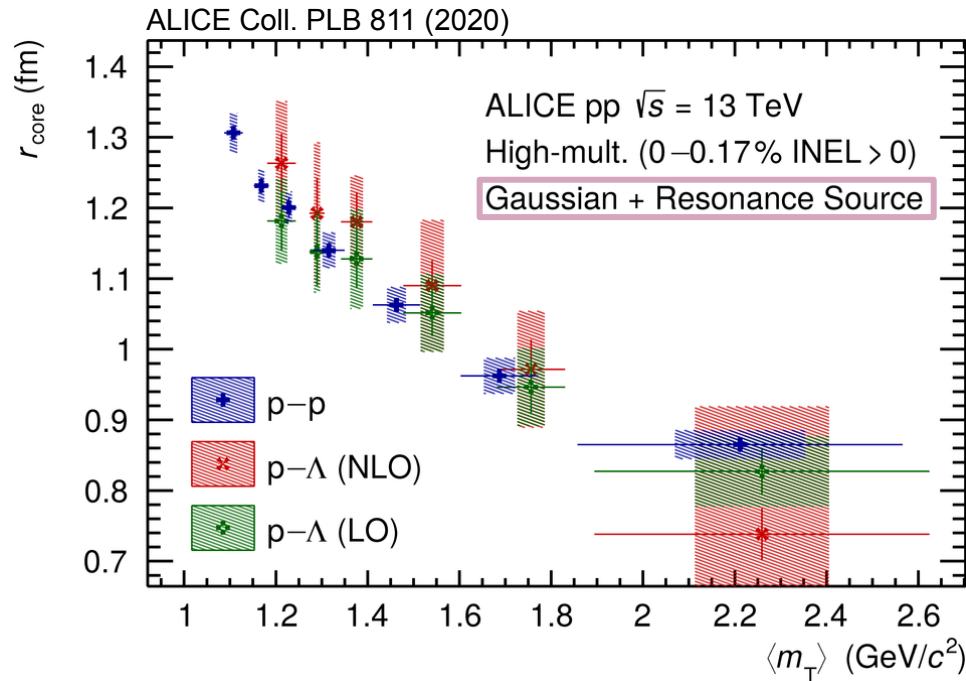
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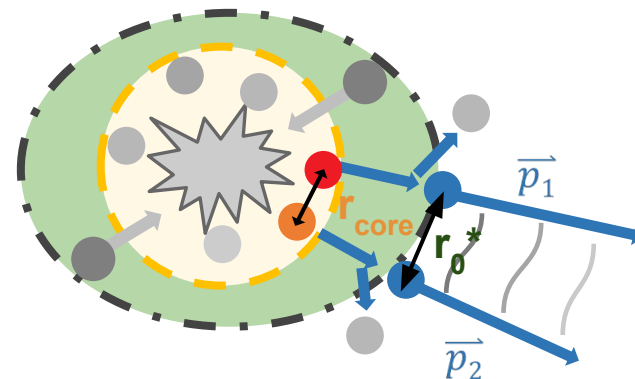
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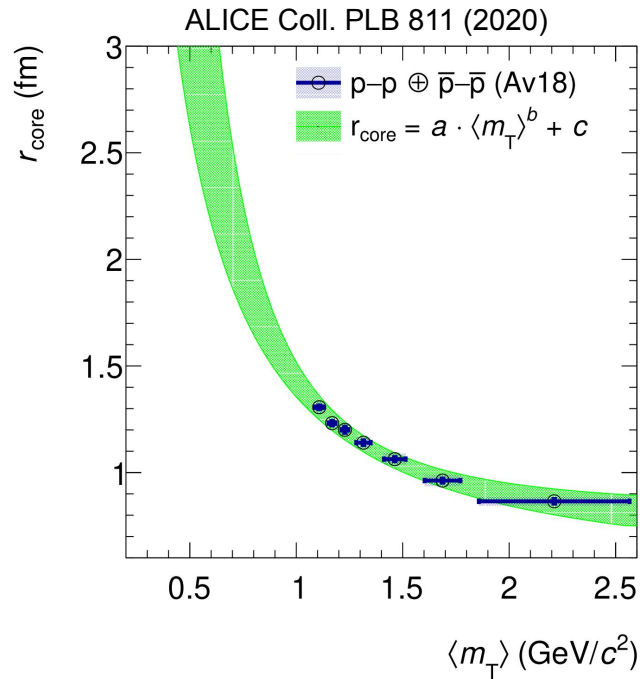




Access smaller m_T by studying π - π and meson-baryon correlations i.e. K^+ -p

- Common scaling is restored by accounting for **non-gaussian** contributions
 - Motivates the assumption of a universal particle source for baryons
- How well does the model perform for mesons? Is the scaling different?

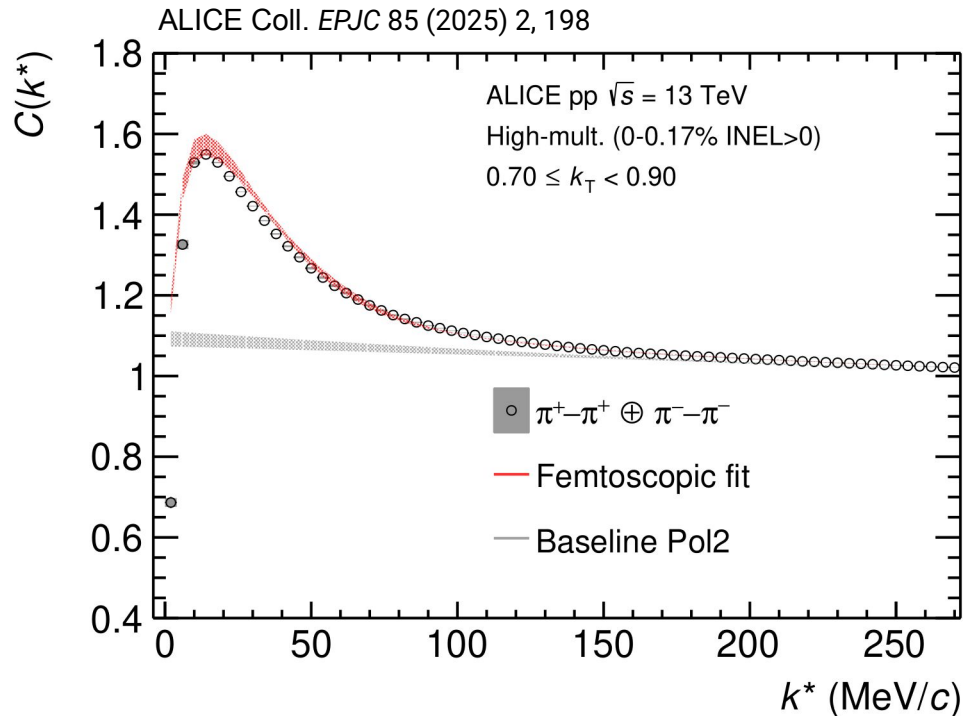




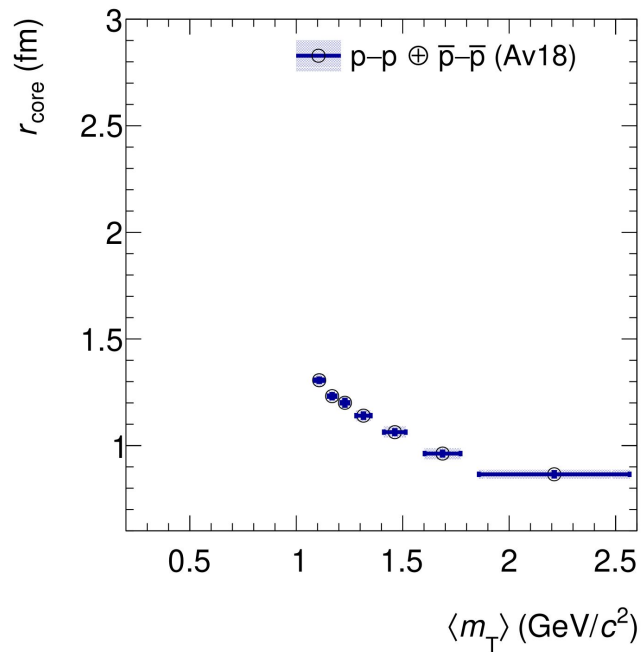
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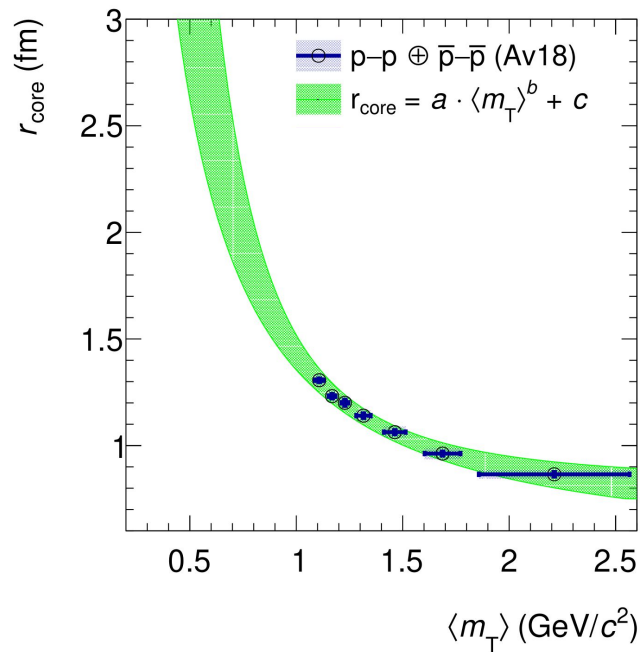
- [1] Y. Sinyukov et al. NPA 946 (2016)
 [2] A. Wiedemann et al. PRC 865 56 (1997)



- Obtained in several m_T bins (# 5)
- Fit with $C^{\pi\pi}(k^*)$ with Pol1 **or** Pol2
 - Polynomial background term to account for residual background
 - Interaction governed by Coulomb interaction and Quantum Statistics

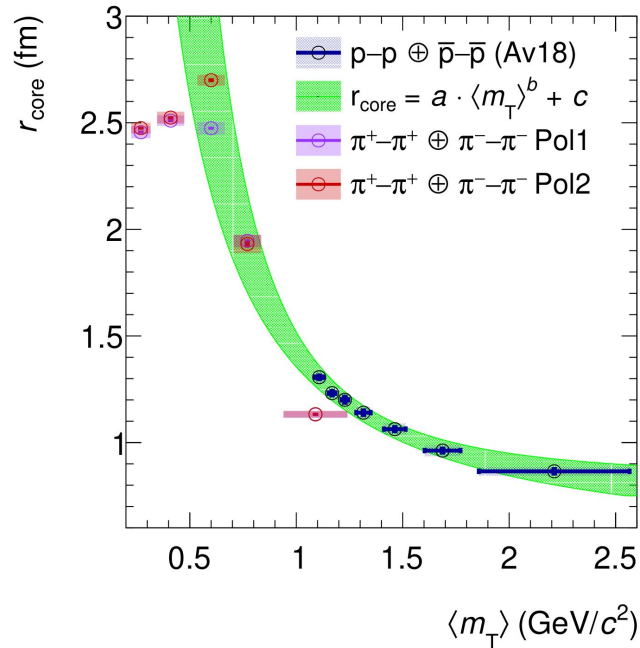


- p-p taken from PLB 811 2020



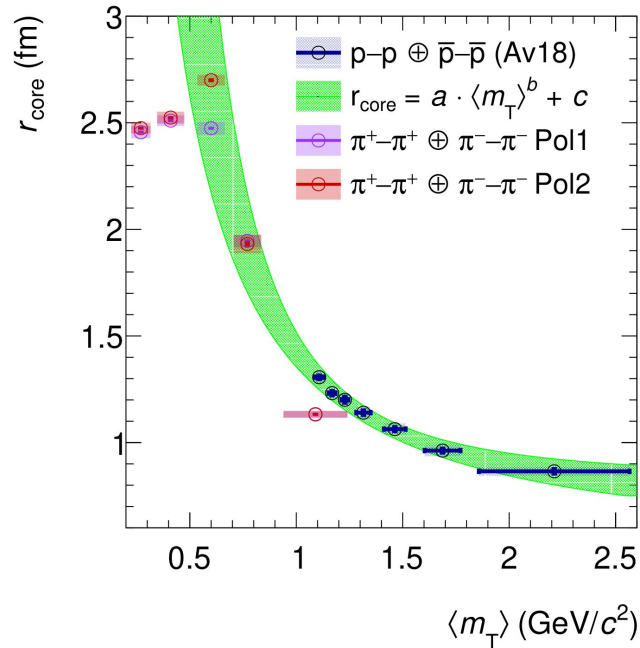
- p-p taken from PLB 811 2020
- Parameterization and extrapolation of the r_{core} dependence

ALICE Coll. *EPJC* 85 (2025) 2, 198



- p-p taken from PLB 811 2020
- Parameterization and extrapolation of the r_{core} dependence
- $\pi\text{-}\pi$ from this analysis (two background assumptions)

ALICE Coll. *EPJC* 85 (2025) 2, 198

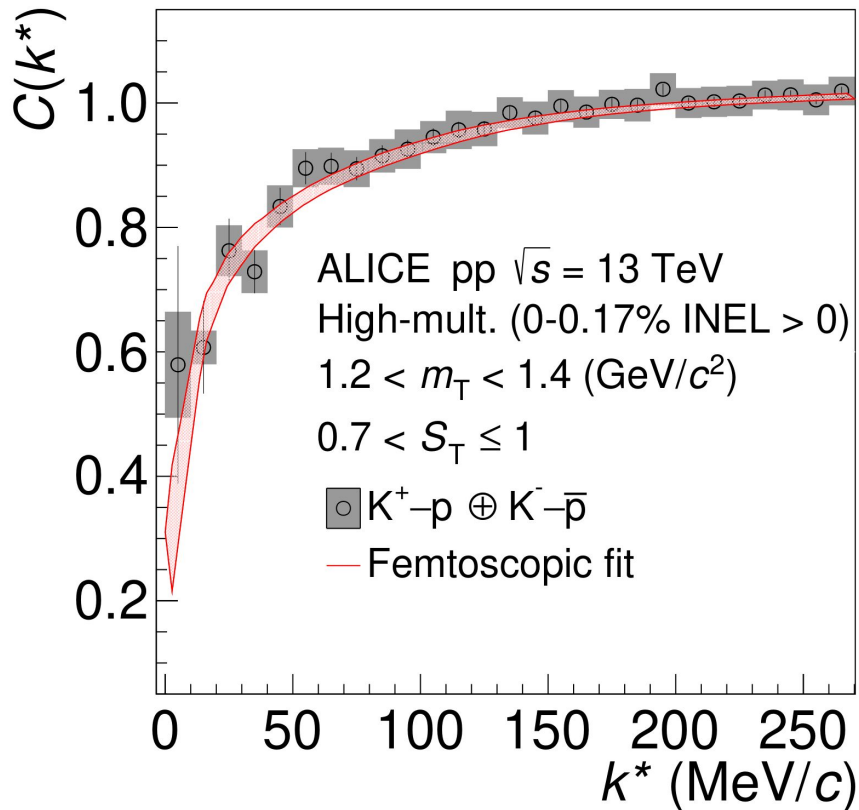


- p-p taken from PLB 811 2020
- Parameterization and extrapolation of the r_{core} dependence
- $\pi^+\pi^-$ from this analysis (two background assumptions)

- For m_T below $0.4 \text{ GeV}/c^2$ good agreement with parametrization
 → Saturation for $\pi^+\pi^-$ radii (**not** predicted by any model)

TUM Measured two-particle correlation

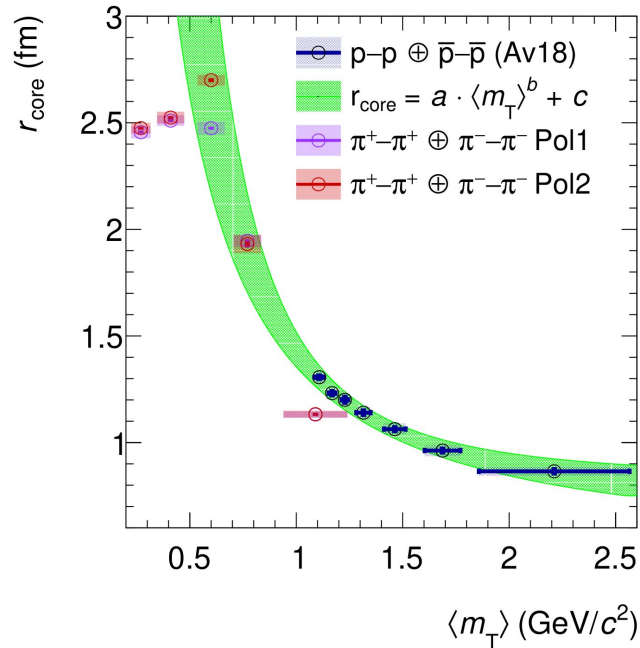
ALICE Coll. *EPJC* 85 (2025) 2, 198



- Obtained in several m_T bins (# 4)
- Interaction is modeled by Coulomb interaction and χ EFT [1]

[1] K. Aoki et al. PTEP 1 (2019)

ALICE Coll. *EPJC* 85 (2025) 2, 198

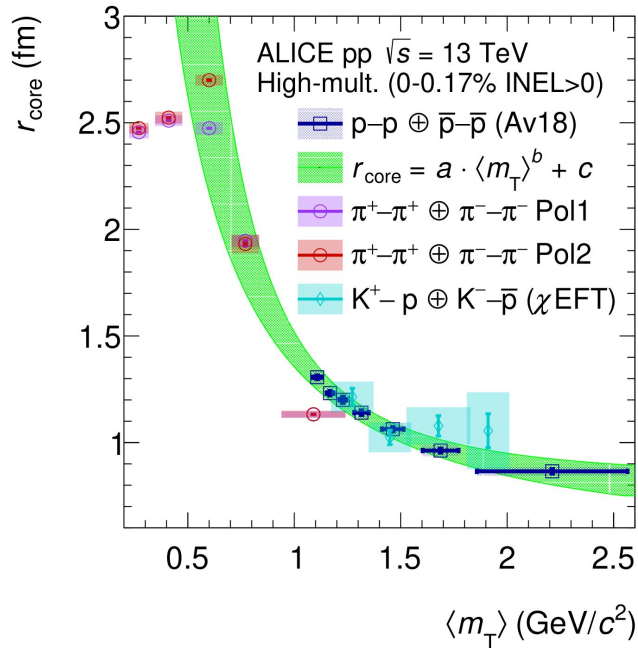


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- Parameterization and extrapolation of the r_{core} dependence
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TUM Core radius compared to previous results

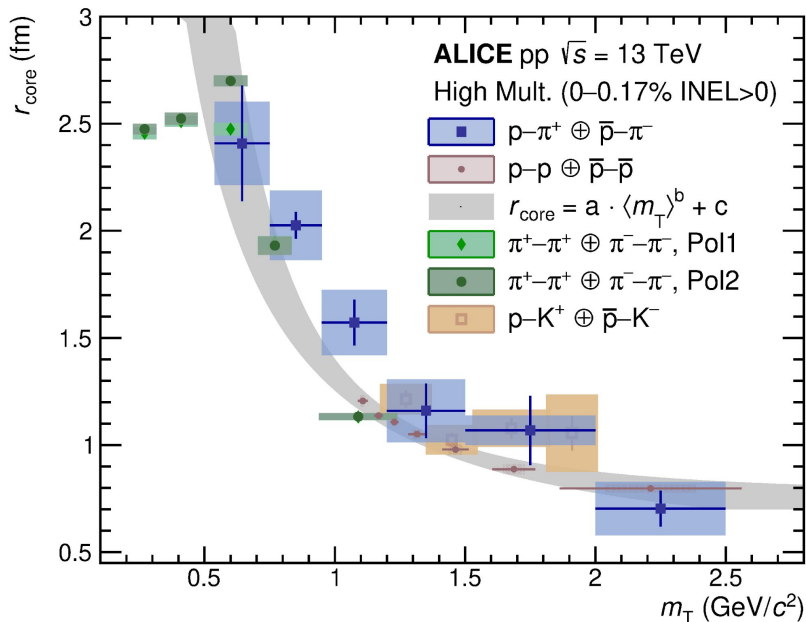
ALICE Coll. EPJC 85 (2025) 2, 198



- p-p taken from PLB 811 2020
- Parameterization and extrapolation of the r_{core} dependence
- π - π from this analysis
- K^+p from this analysis

- For m_T above 0.4 GeV/c² good agreement with parametrization
→ Evidence for a common source for **all** hadrons in pp

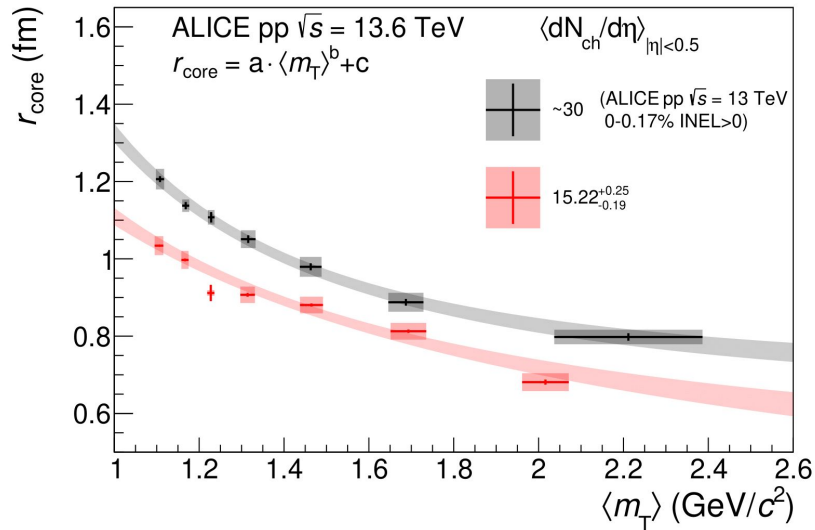
ALICE Coll. *EPJA* 61 (2025) 8, 194



ALI-PUB-594373

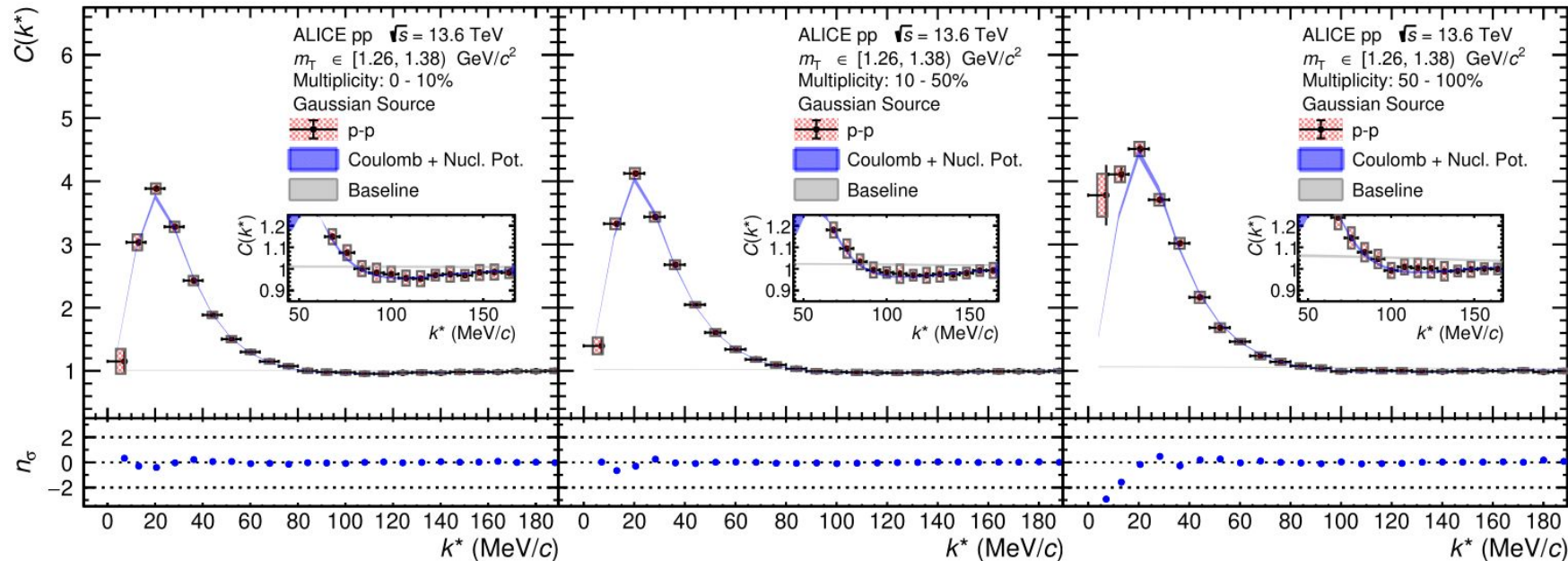
- Adding π - p as second meson-baryon system

Paper in preparation

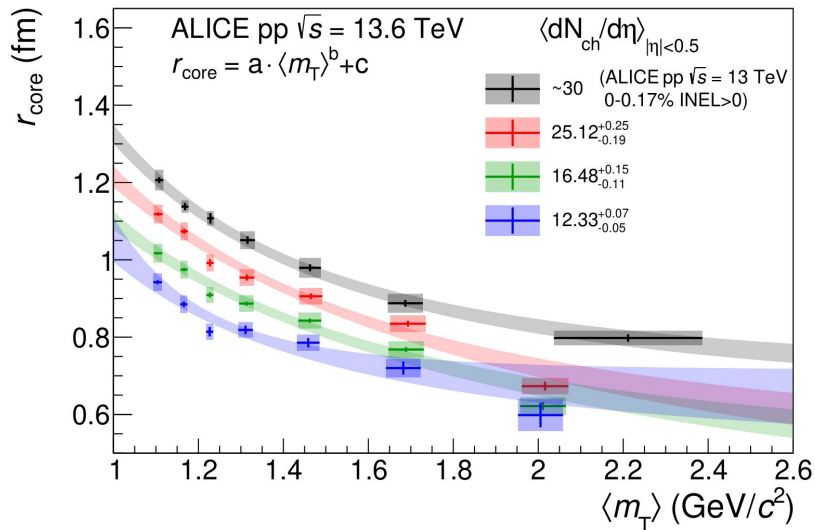


- Adding π -p as second meson-baryon system
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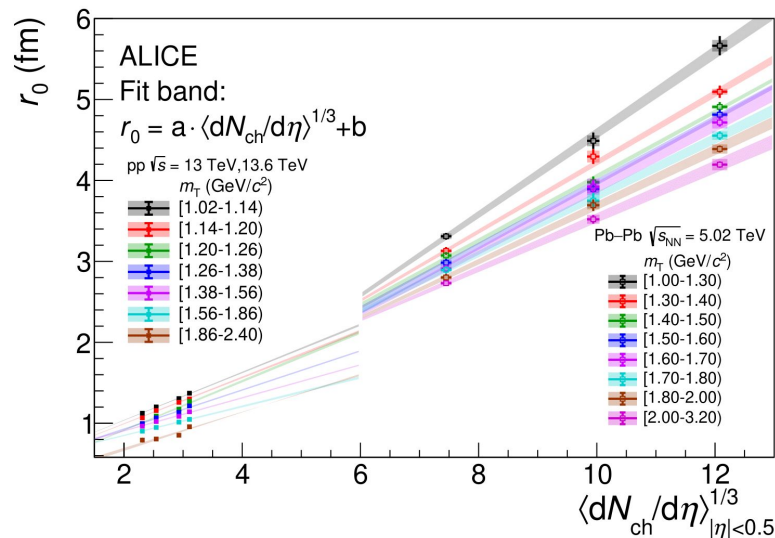


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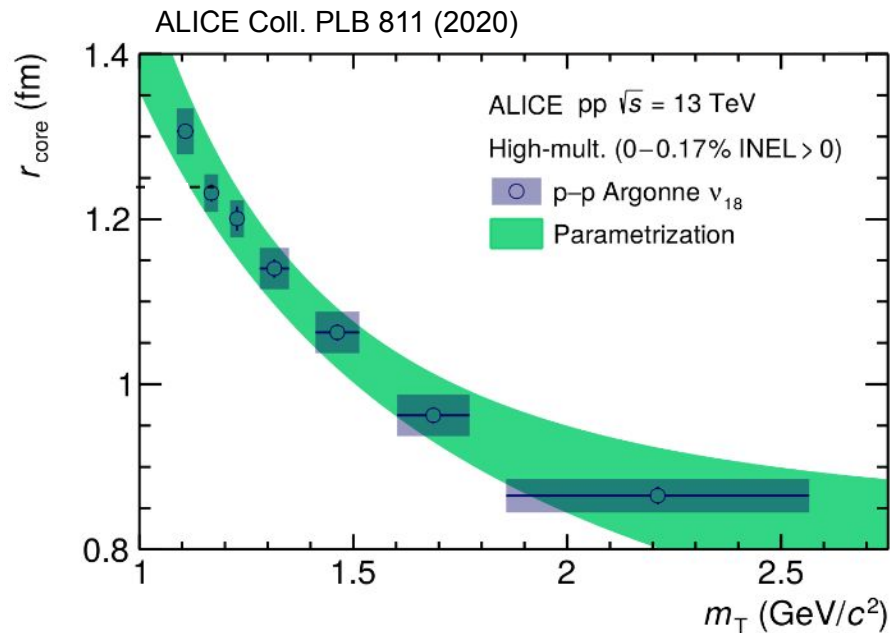


- Adding π -p as second meson-baryon system
- Studying source in Run3 data
 - Multi-differential study

Paper in preparation



- Adding π -p as second meson-baryon system
- Studying source in Run3 data
 - Different trend to PbPb due to QGP?

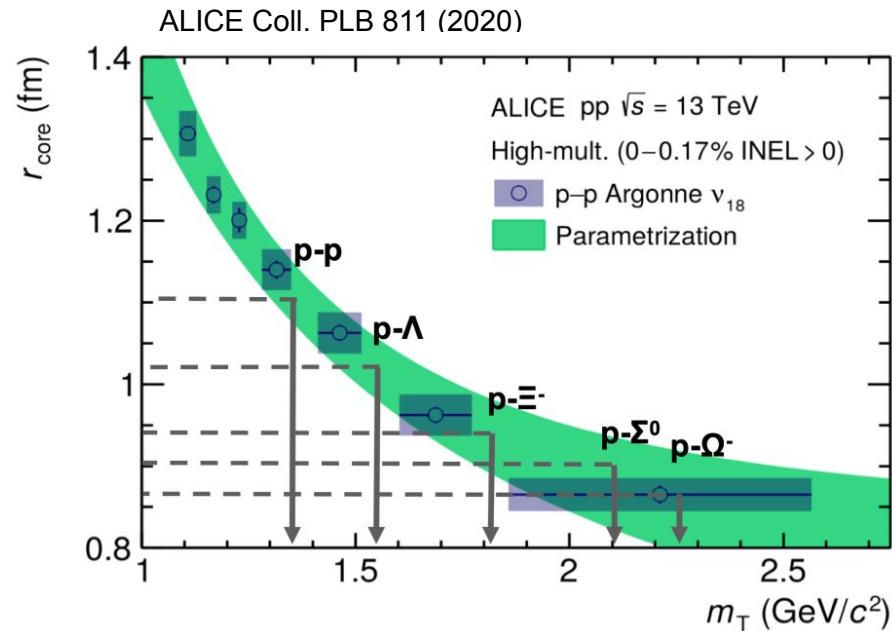


- Centerpiece for high precision FSI studies
 - Enables the construction of $S(r^*)$

[1] Y. Sinyukov et al. NPA 946 (2016)

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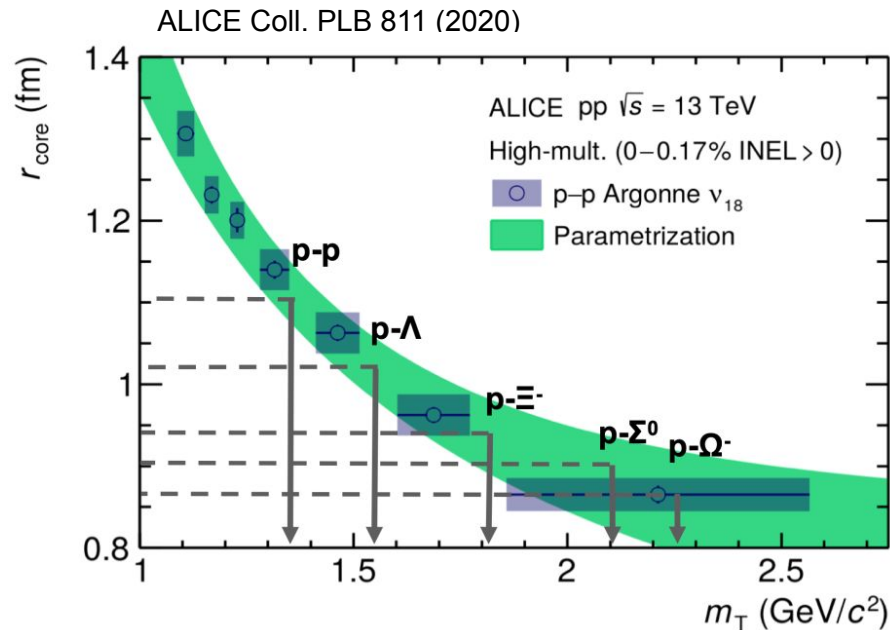
TUM Common baryon source in small systems



- Centerpiece for high precision FSI studies
 - Enables the construction of $S(r^*)$
- Recipe for the source
 - Obtain reference measurement
 - Employ RSM to obtain primordial $S(r^*)$
 - Calculate mean m_T of the pair
 - Employ RSM to add case specific resonances
 - Study final-state interactions

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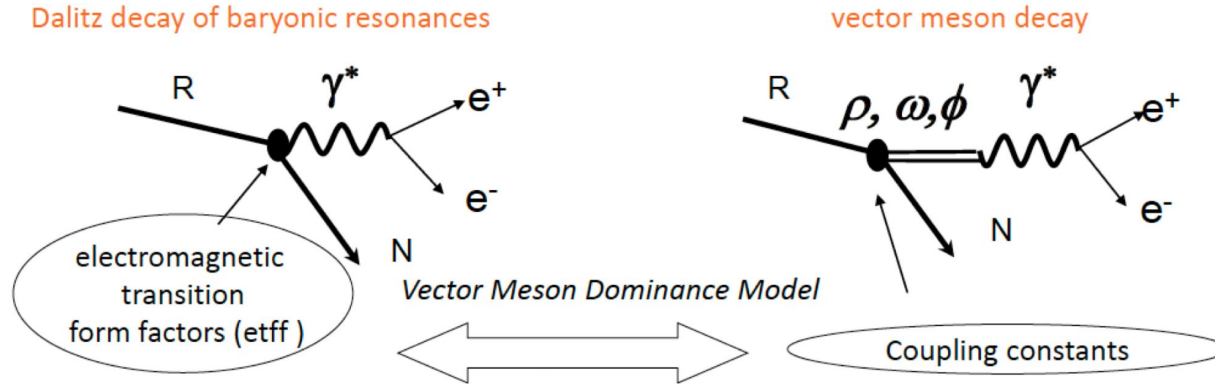
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How to infer on scattering parameters from data?

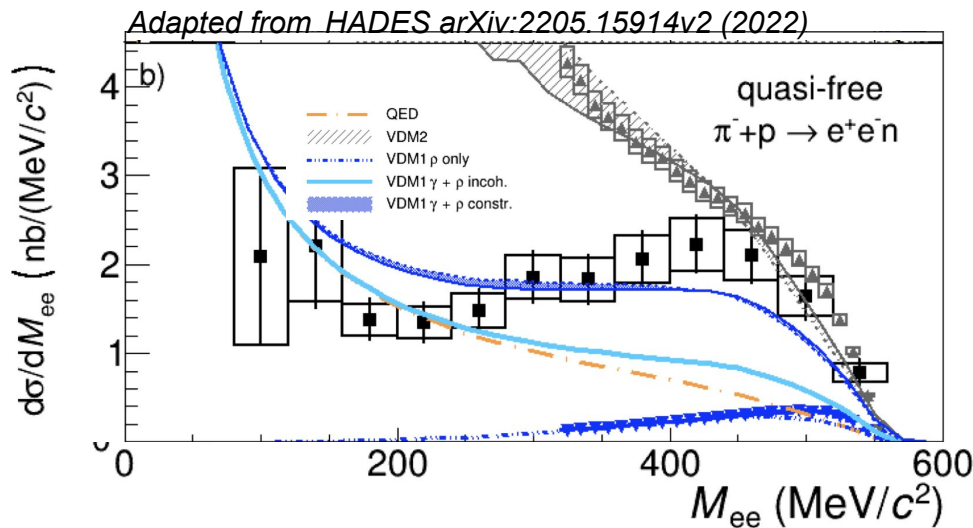
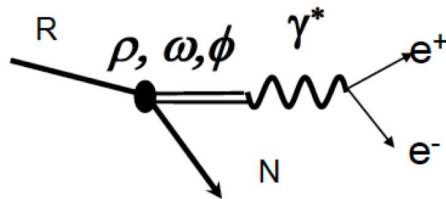
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Vector meson nucleon interaction

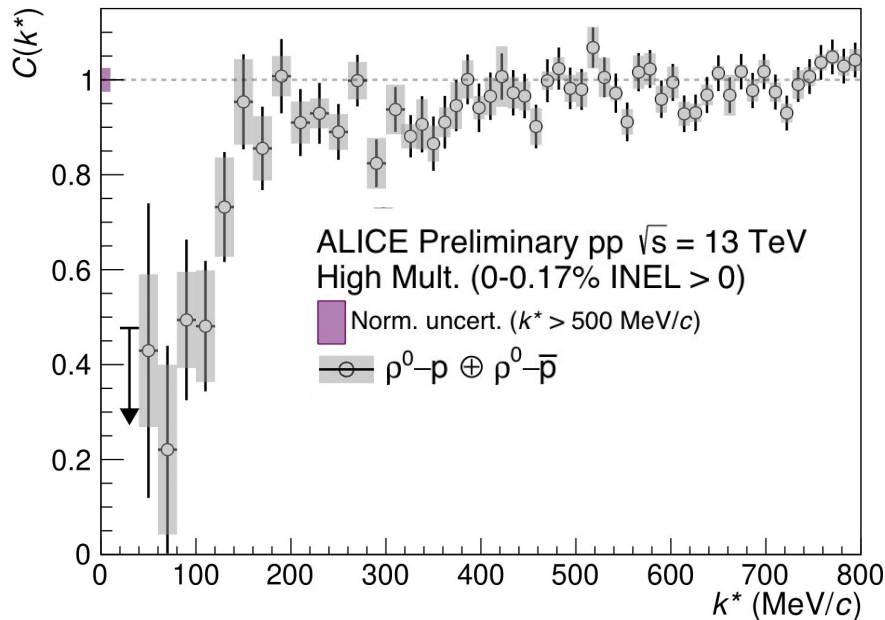


- Usually probed by Vector Meson Dominance (VMD¹) Models
 - 1: J. J. Sakurai, *Phys. Rev. Lett.* 22, 981 (1969)
 - Hadronic contribution to the photon propagator
 - Off-shell vector mesons
- Important to understand...
 - ... in-medium dilepton production
 - ... dynamically generated states N^* and Δ^* (pole positions) from unitarised chiral perturbation theory (UChPT²)
 - 2: N. Kaiser, P. B. Siegel and W. Weise, *Phys. Lett. B* 362, 23 (1995)



- Test of VMD at HADES
 - Low-energy beams (π)
 - M_{ee} excess compared to QED reference
- Excess modeled
 - With low-lying intermediate resonances (R) (N(1440), N(1520), N(1535) in a $R\gamma^*N$ vertex)
- But how can one access the interaction between the ρ^0 and nucleon directly?

First direct observation of the $\rho^0 N$ coupling



1: A. Feijoo, MK, L. Fabbietti PRD 111 (2025) 1, 014009

2: ALICE PRL 127 (2021)

- Prediction obtained within UChPT¹ for S=0
 - Coupled channels: ρ^+n , ωp , ϕp , $K^*\Lambda$, $K^*\Sigma$
 - Includes dynamical states $N^*(1700)$ and $N^*(2000)$
- Additional constraint for ρ^0-p
 - Use $\phi-p$ CF result² for simultaneous fit

Unitarised chiral perturbation theory for ρ^0 -p

Interaction
kernel V

$$T_{ij} = (1 - V_{il}G_l)^{-1} V_{lj}$$

Scattering

Loop-function G

Matrix T from i to j

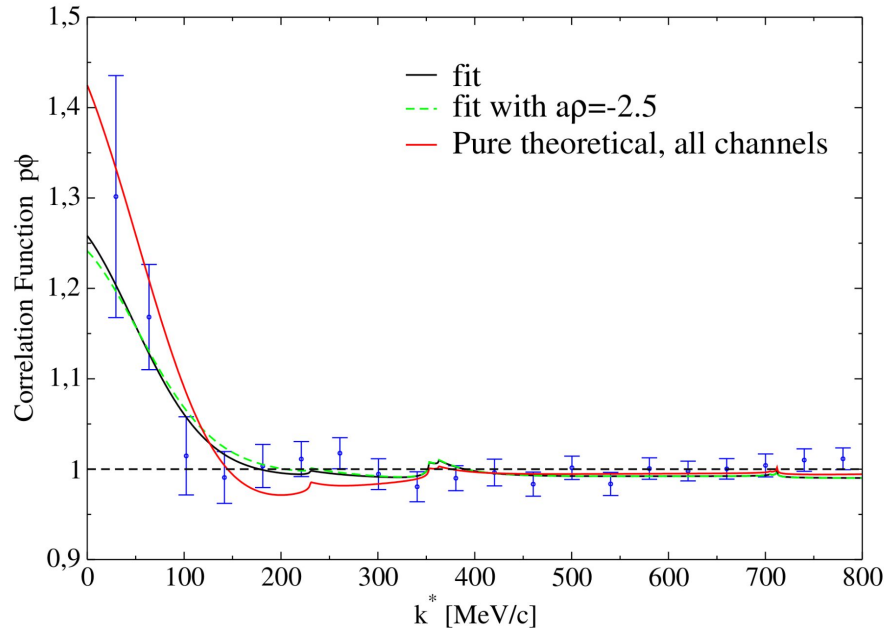
- *Core Idea*
 - Extract LO interaction form
Chiral L + Hidden Gauge Symmetry
 - Solve **Bethe–Salpeter Equation** in **coupled channels** ansatz¹
- *Outcome*
 - Resonances as poles in T -Matrix
 - Extract scattering parameters from wavefunction

$$\psi_{ji}(k^*, r^*) = \delta_{ij} j_0(k^* r^*)$$

$$+ \int_{q \leq q_{\text{cut}}} d^3 q j_0(q r^*) G_j(\sqrt{s}, q) T_{ji}(\sqrt{s}, k^*, q)$$

1: A. Feijoo, MK, L. Fabbietti PRD 111 (2025) 1, 014009

Unitarised chiral perturbation theory for ρ^0 -p

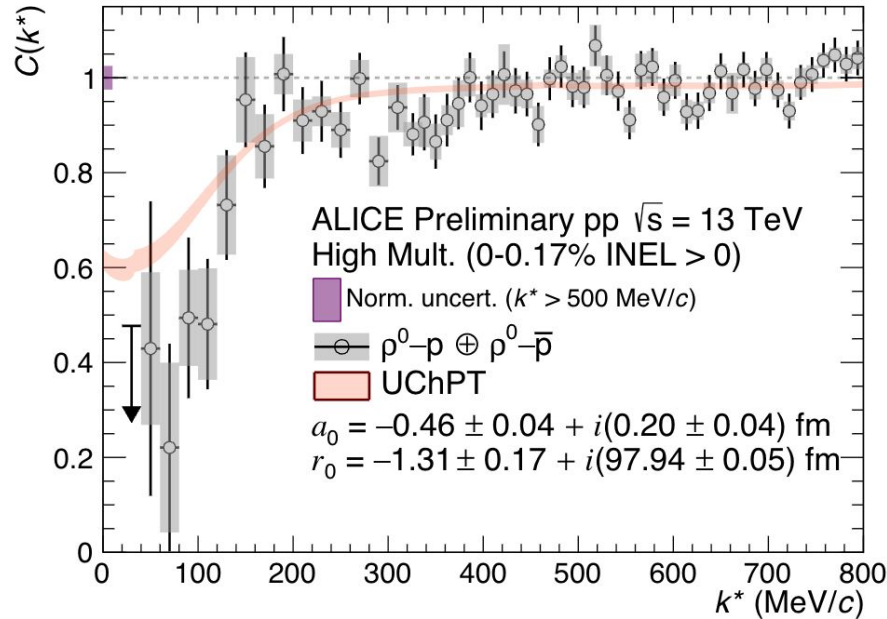


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- *Advantages over VMD*
 - *Naturally* accounts for int. dynamics coupled channels + resonances
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Prediction from UChPT for ρ^0 -p

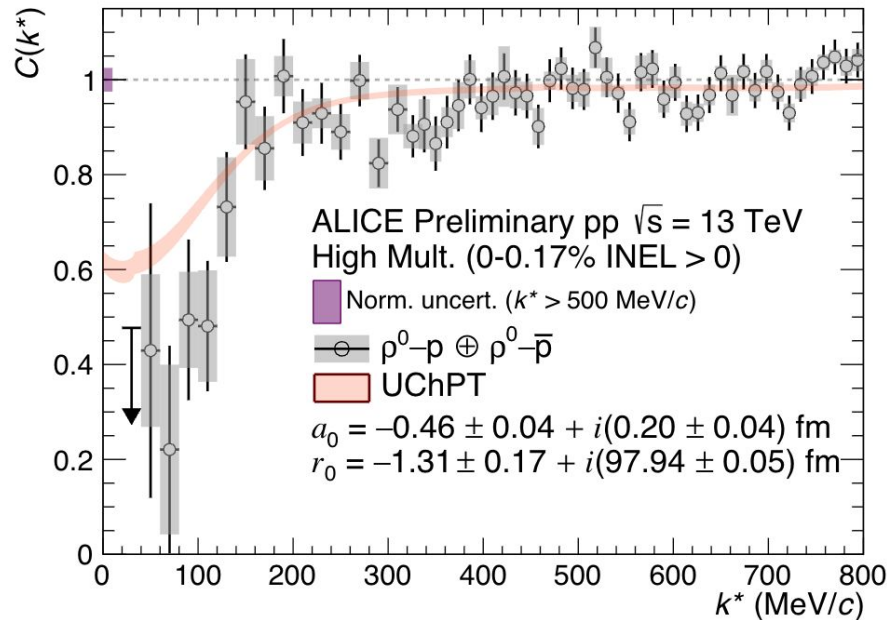


1: A. Feijoo, MK, L. Fabbietti PRD 111 (2025) 1, 014009

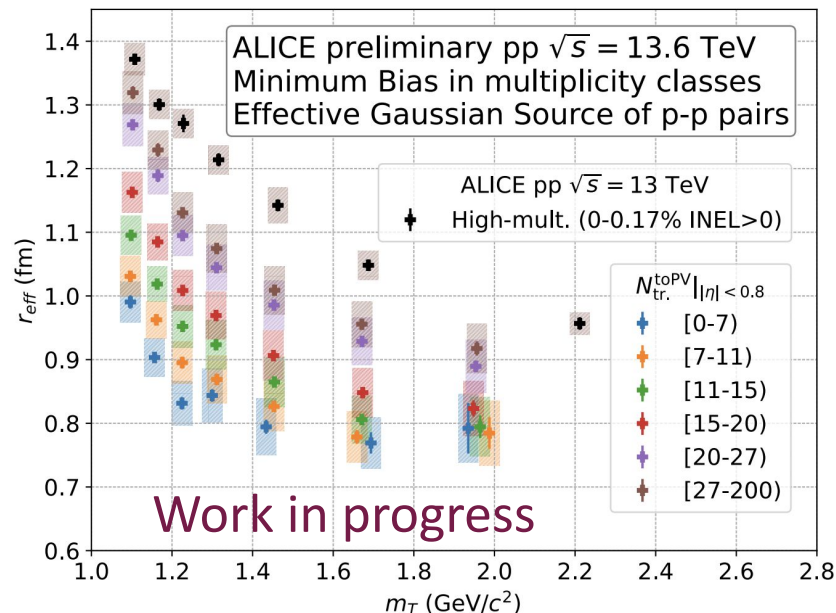
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- Access to the interaction of the shortest-lived QCD state
- First direct measurement of the ρ^0 p interaction with full phase information
- Implications
 - Benchmark VMD implementations
 - Basis for Chiral symmetry restoration studies
 - Collider based insight into QCD spectrum
- Paper submitted to PRL
arXiv:2508.09867



- Adding π -p as second meson-baryon system
- Finalize calibration measurement of **p-p** in Run3
 - Foundation of high precision femtoscopic final state interaction studies

Back-up

Summary

- For the **first time** a quantitative description of the exponential source of pions is presented by **explicitly** considering the influence of short-lived resonances on a Gaussian core (RSM model)
- $K^+ - p$ and same charge $\pi - \pi$ show agreement with the RSM assumption of a **universal** Gaussian core **source** for primordial particles
- Source radii reach saturation for $m_T < 0.4 \text{ GeV}/c$

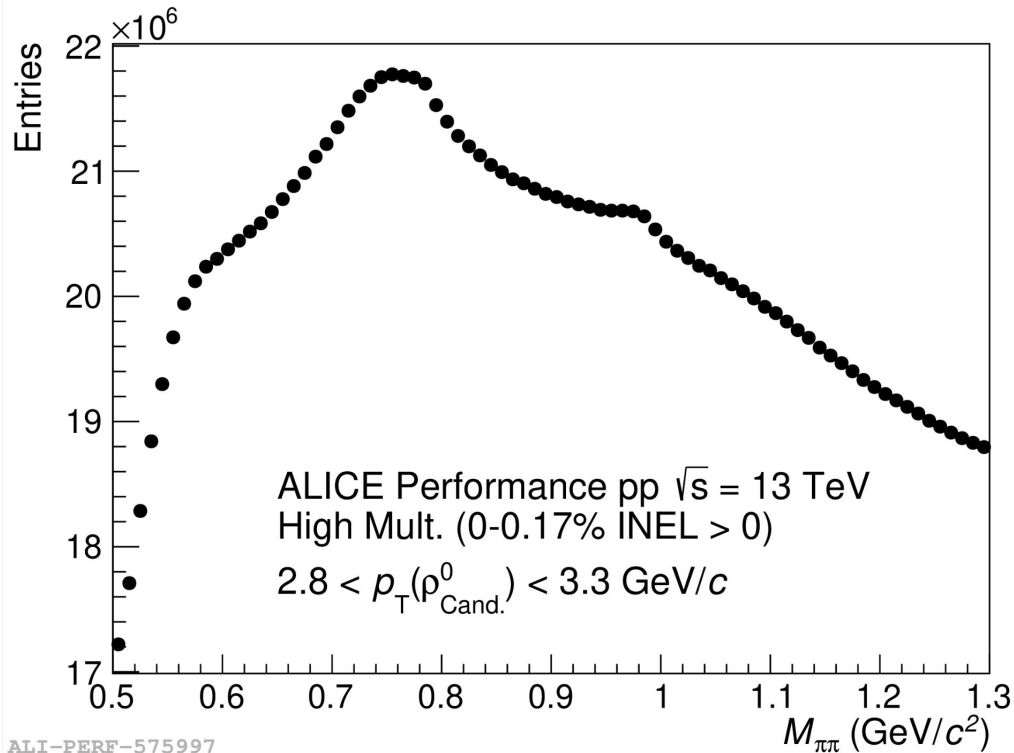
Physics Message

- A scaling behavior with m_T was observed for the extracted radii, **consistent** with previous baryon–baryon findings
- **Saturation** is observed

Outlook

- Available data to tune particle production coordinates in transport models
- Refine source model in order to account for saturation effects (CECA [1])

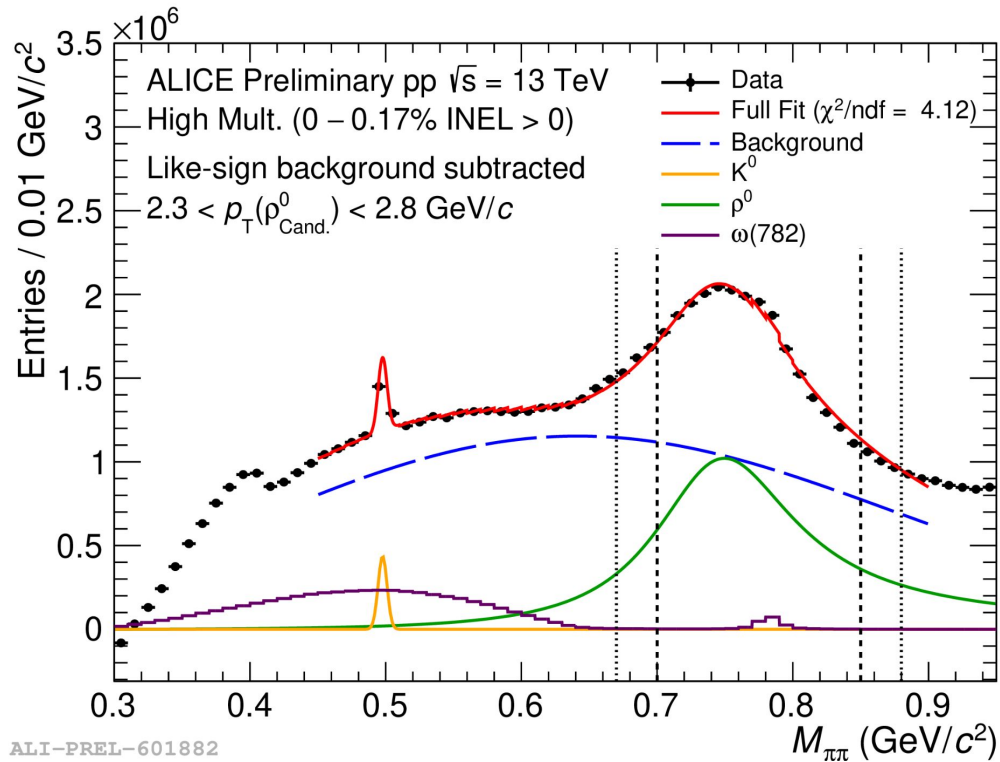
[1] D. Mihaylov et al. arXiv 2305.08441(2023)



ALI-PERF-575997

- Access to ρ^0 ($c\tau = 1.2$ fm/c)
 - Pair all π in an event
 - $\rho^0 \rightarrow \pi^+ \pi^-$ (B.R. $\approx 100\%$)
- Purity of the ρ^0 around **3.26%**
 - Obtained by fit
- Two types of background
 - Combinatorial due to $(\pi\pi)_{\text{Comb.}}$
 - Mini-jet correlations

Model $M_{\pi\pi}$ to access purity of ρ^0



ALI-PREL-601882

Assess purity of ρ^0

- Pair all π in an event
- Record $M_{\pi\pi}$ vs p_T
- Fit projections

Method follows established procedures^{1,2}

- Use LSB subtraction
- Model states with rBW/MC temp.
- Gaussian for K^0
- **Purity 3.26%**

For $p_T > 1.8$ GeV/c ρ^0 -peak is visible

- translates to high m_T pairs
- **$1.64 < m_T < 3.77$ (GeV/c²)**

1: STAR, PRL. 92 (2004) 092301

2: ALICE, PRC 99 (2019) 064901

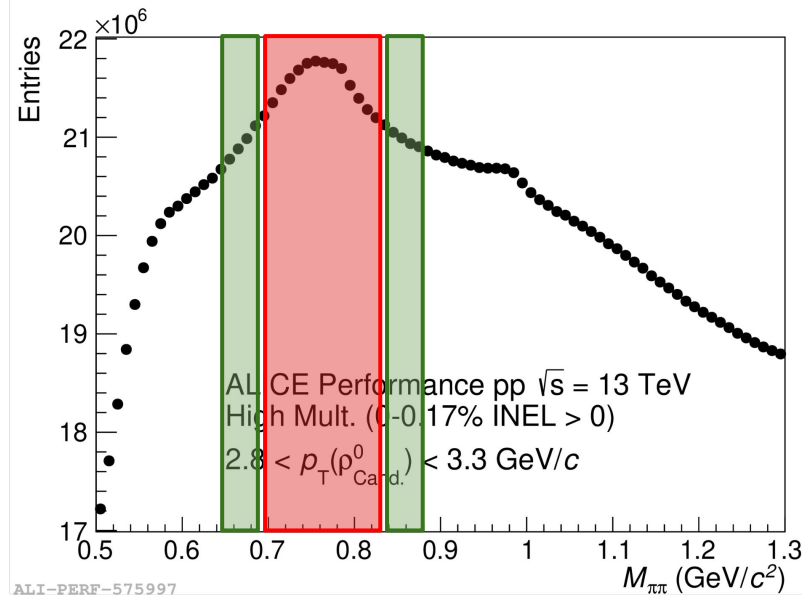
Extraction of the genuine ρ^0 -p correlation

$$C_{\text{measured}}(k^*) = C_{\text{minijet}}(k^*) [\lambda_{\rho^0\text{-p}} \cdot C_{\rho^0\text{-p}}(k^*)] + (1 - \lambda_{\rho^0\text{-p}}) \cdot (\omega_{\text{left}} C_{\text{SB}}^{\text{left}}(k^*) + (1 - \omega_{\text{left}}) C_{\text{SB}}^{\text{right}}(k^*)).$$

Extraction of the genuine ρ^0 -p correlation

$$C_{\text{measured}}(k^*) = C_{\text{mini jet}}(k^*) [\lambda_{\rho^0-p} \cdot C_{\rho^0-p}(k^*)] + (1 - \lambda_{\rho^0-p}) \cdot (\omega_{\text{left}} C_{\text{SB}}^{\text{left}}(k^*) + (1 - \omega_{\text{left}}) C_{\text{SB}}^{\text{right}}(k^*)).$$

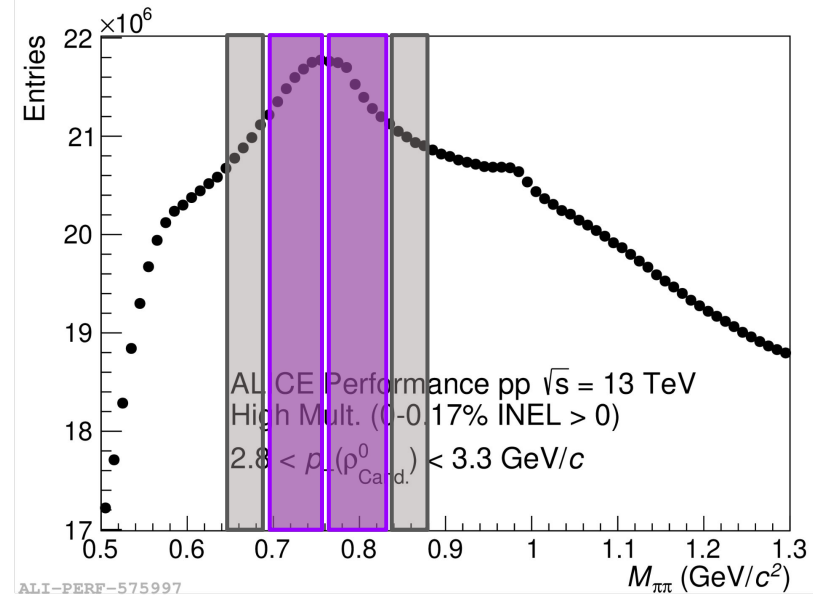
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- Employ sideband (SB) analysis
 - Compute correlation function selecting $\rho^0_{\text{Cand.}}$ from left and right sideband region



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- Account for correlation of $(\pi\pi)_{\text{Comb.}}$ underneath ρ^0 signal
- Employ sideband (SB) analysis
 - Compute correlation function selecting $\rho^0_{\text{Cand.}}$ from left and right sideband region
 - Calculate **weights** by integration
 - Obtain SB correlation by a weighted average



$$C_{\text{measured}}(k^*) = C_{\text{minijet}}(k^*) [\lambda_{\rho^0-p} \cdot C_{\rho^0-p}(k^*)] + (1 - \lambda_{\rho^0-p}) \cdot (\omega_{\text{left}} C_{\text{SB}}^{\text{left}}(k^*) + (1 - \omega_{\text{left}}) C_{\text{SB}}^{\text{right}}(k^*)).$$

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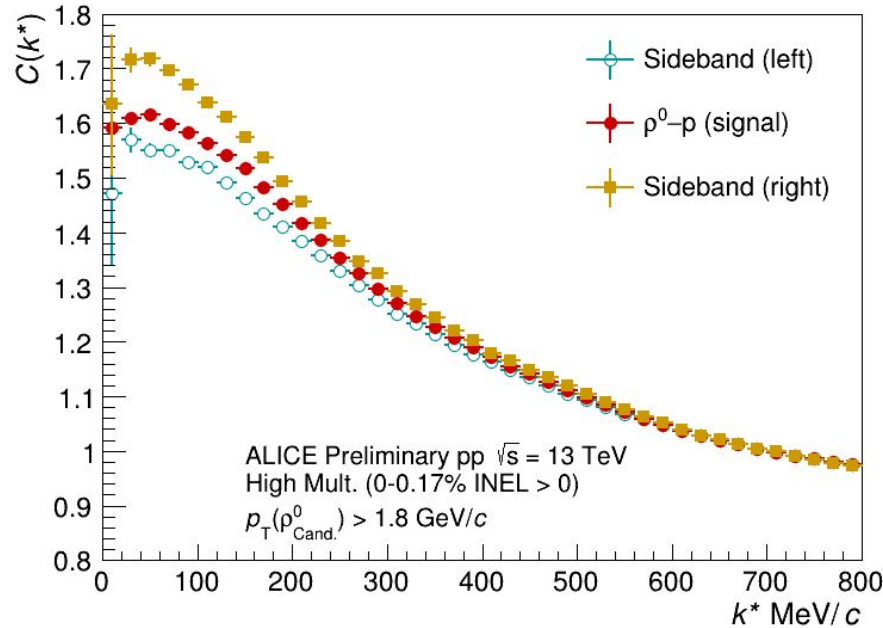
- Account for correlation of ...
 - fake ρ^0 -p by **SB subtraction**
 - SB left and right weighted (ω) with integral under ρ^0 peak
 - Take genuine ρ^0 -p in SB into account
 - **Minijets** in ρ^0 -p by dividing by SB (assume SB is dominated by Minijet)

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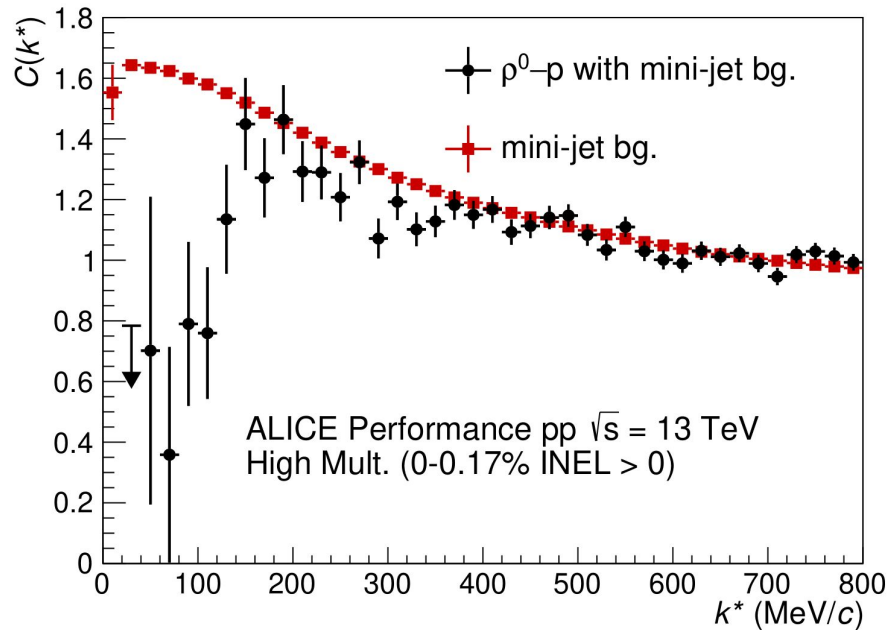
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 - Minijets in ρ^0 -p by dividing by SB (assume SB is dominated by Minijet)
- Properly scaled by the **λ parameter**
 - Depends on the single-particle properties (purity and fractions)
 - dominated by the purity of ρ^0

Correlation function of signal and sidebands



- Normalisation 600 - 800 MeV/c
- Correlation in signal region
 - ρ^0 -p final-state interaction
 - Minijet contribution
 - correlation from SB
- Corrections
 - Take ρ^0 -p in SB into account
 - Subtract λ scaled SB

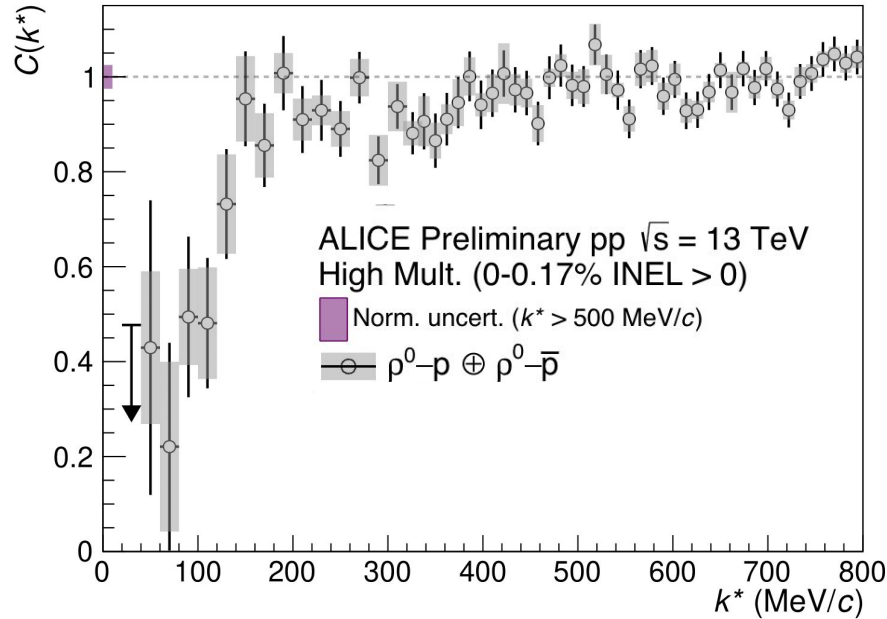
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- Normalization region in 600–800 MeV/c
- $\lambda (= 2.7\%)$ dominated by ρ^0 purity
- Minijet contribution still present
- Corrections
 - Assumption: Minijet equals SB
 - Divide by SB as proxy for Minijet

$$C_{\rho^0-p}(k^*) = \frac{1}{C_{\text{minijet}}} \left\{ \frac{1}{\lambda_{\rho^0-p}} [C_{\text{measured}}(k^*) - (1 - \lambda_{\rho^0-p})C_{\text{SB}}(k^*)] \right\}.$$

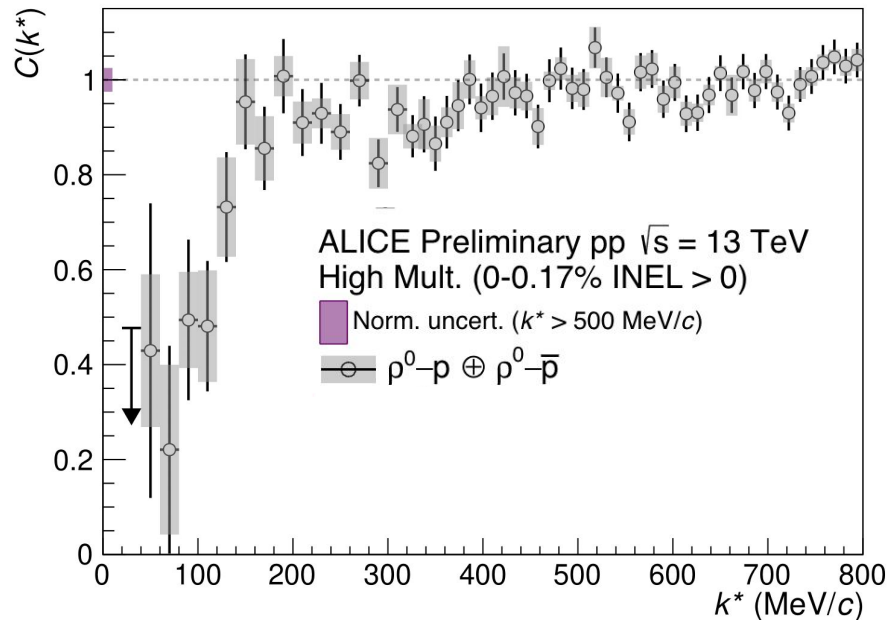
First direct observation of the $\rho^0 N$ coupling



- Systematics obtained by varying selections
- $n\sigma$ values w.r.t to unity (no interaction) for...
 - < 100 MeV/c: 3.6
 - < 120 MeV/c: 4.3
 - < 200 MeV/c: 4.0
- Coupled channels:
 $\rho^+ n, \omega p, \phi p, K^* \Lambda, K^* \Sigma$
- Other N^* and Δ^* states (4* in PDG)
 - $N^*(1700)$ below pN threshold (1713 MeV)

$$C_{\rho^0-p}(k^*) = \frac{1}{C_{\text{minijet}}} \left\{ \frac{1}{\lambda_{\rho^0-p}} [C_{\text{measured}}(k^*) - (1 - \lambda_{\rho^0-p}) C_{\text{SB}}(k^*)] \right\}.$$

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1: A. Feijoo, MK, L. Fabbietti PRD 111 (2025) 1, 014009

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Unitarised chiral perturbation theory for ρ^0 -p

Interaction
kernel V

$$T_{ij} = (1 - V_{il}G_l)^{-1} V_{lj}$$

Scattering

Loop-function G

Matrix T from i to j

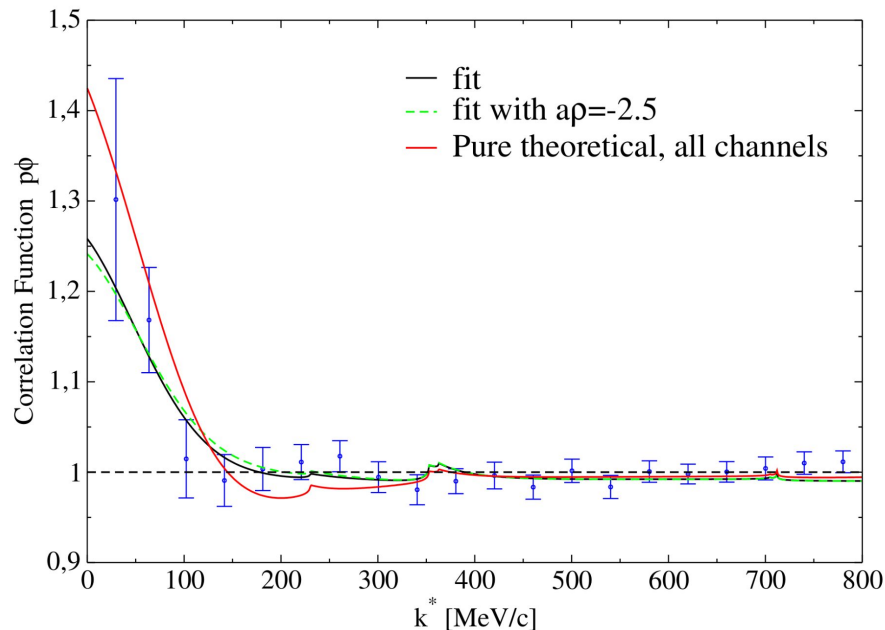
- *Core Idea*
 - Extract LO interaction form
Chiral L + Hidden Gauge Symmetry
 - Solve **Bethe–Salpeter Equation** in **coupled channels** ansatz¹
- *Outcome*
 - Resonances as poles in T -Matrix
 - Extract scattering parameters from wavefunction

$$\psi_{ji}(k^*, r^*) = \delta_{ij} j_0(k^* r^*)$$

$$+ \int_{q \leq q_{\text{cut}}} d^3 q j_0(q r^*) G_j(\sqrt{s}, q) T_{ji}(\sqrt{s}, k^*, q)$$

1: A. Feijoo, MK, L. Fabbietti PRD 111 (2025) 1, 014009

Unitarised chiral perturbation theory for ρ^0 -p

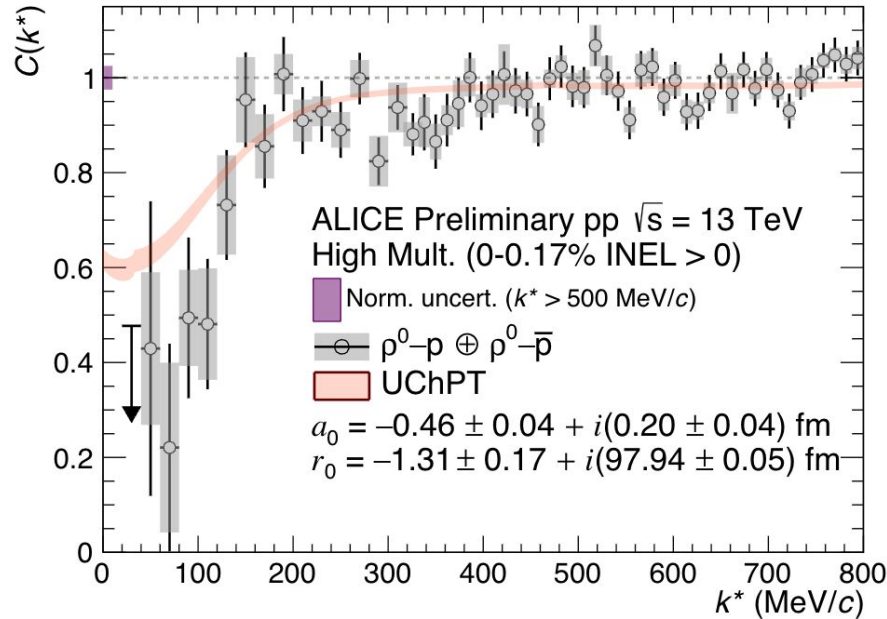


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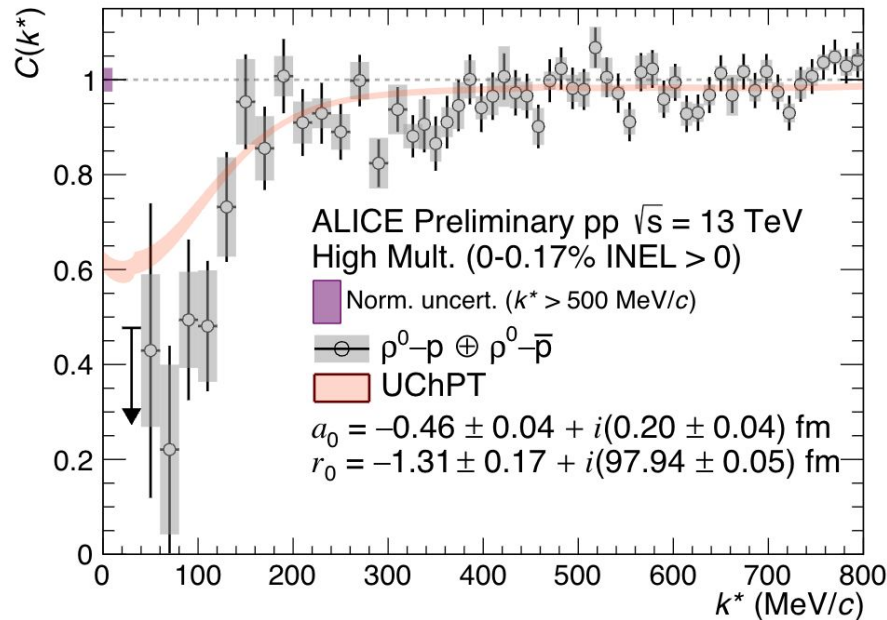


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Summary

- For the **first time** a quantitative description of the exponential source of pions is presented by **explicitly** considering the influence of short-lived resonances on a Gaussian core (RSM model)
- K^+p and K^-p and π^+p and π^-p data are described with the assumption of a **universal** source
- Source radius is extracted

Even more details about the $\pi-\pi$ source were studied: Doubly differential as function of m_T and multiplicity on MB data set!

Same saturation behaviour as in high-mult. data set. Scaling of the radii with multiplicity is observed.

Physics Message

- A scaling of the radii with multiplicity is observed
- **consistent** with the assumption of a universal source
- **Saturation** at is observed

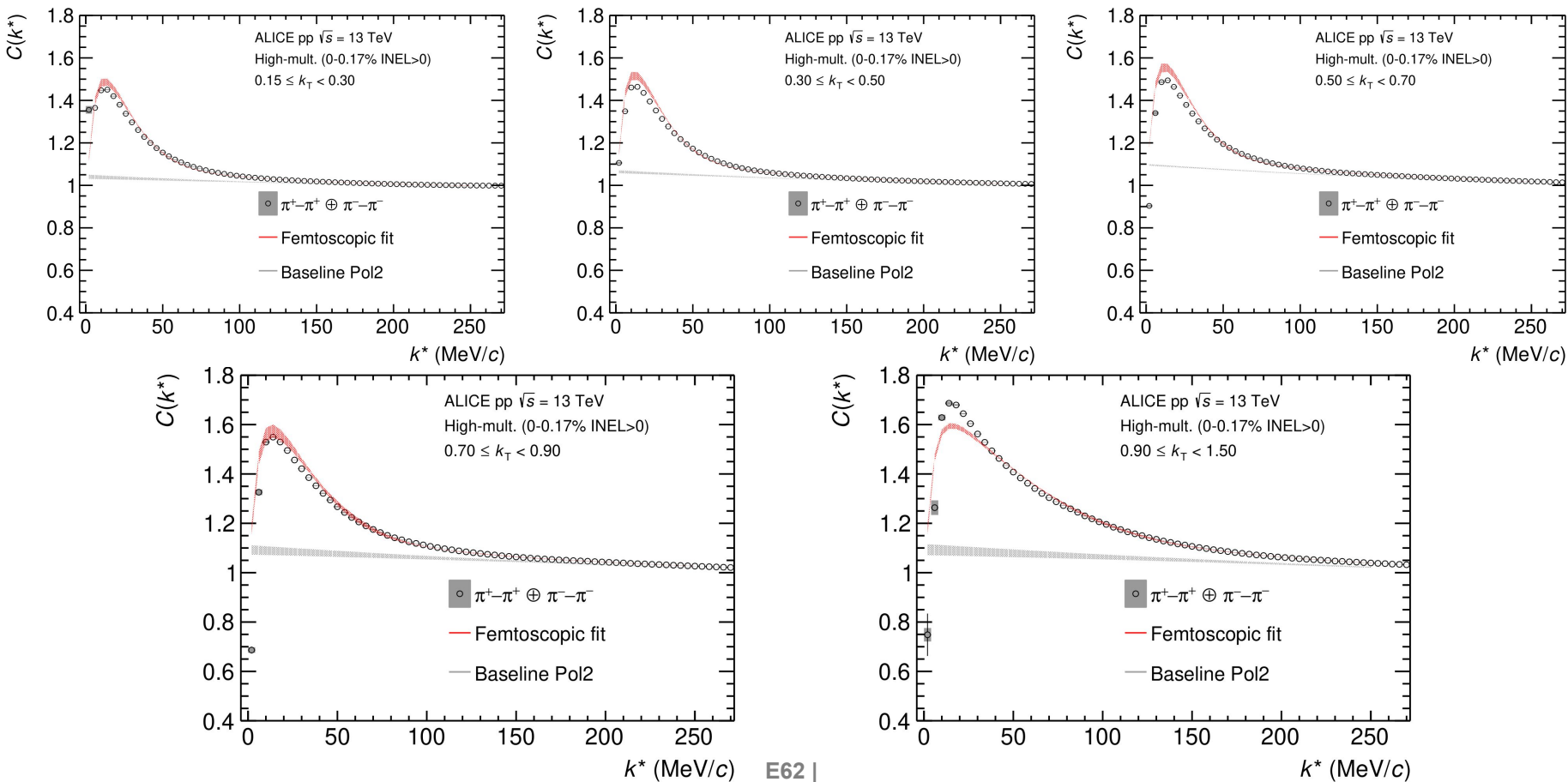
Plots are in the back-up!

Outlook

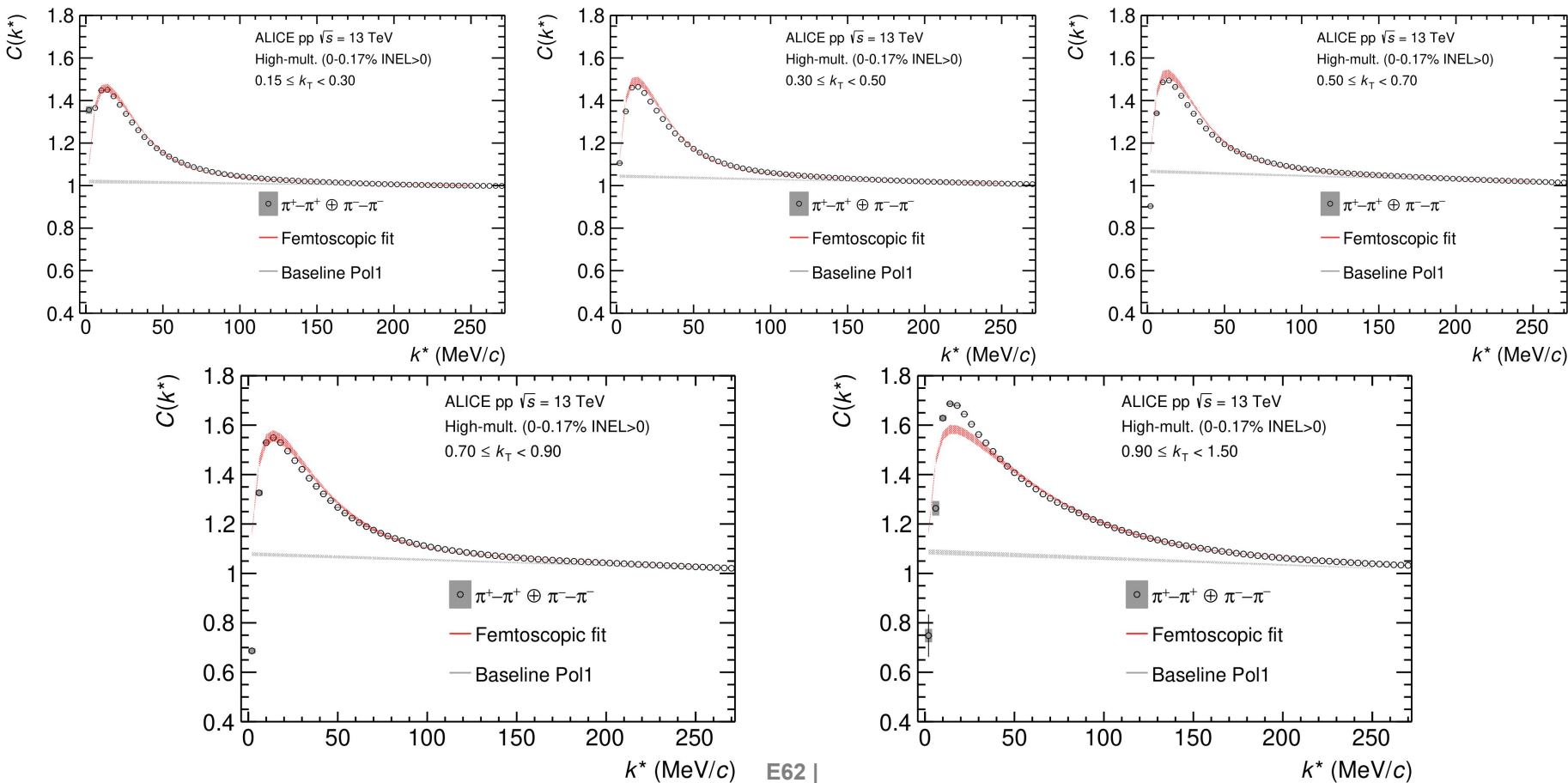
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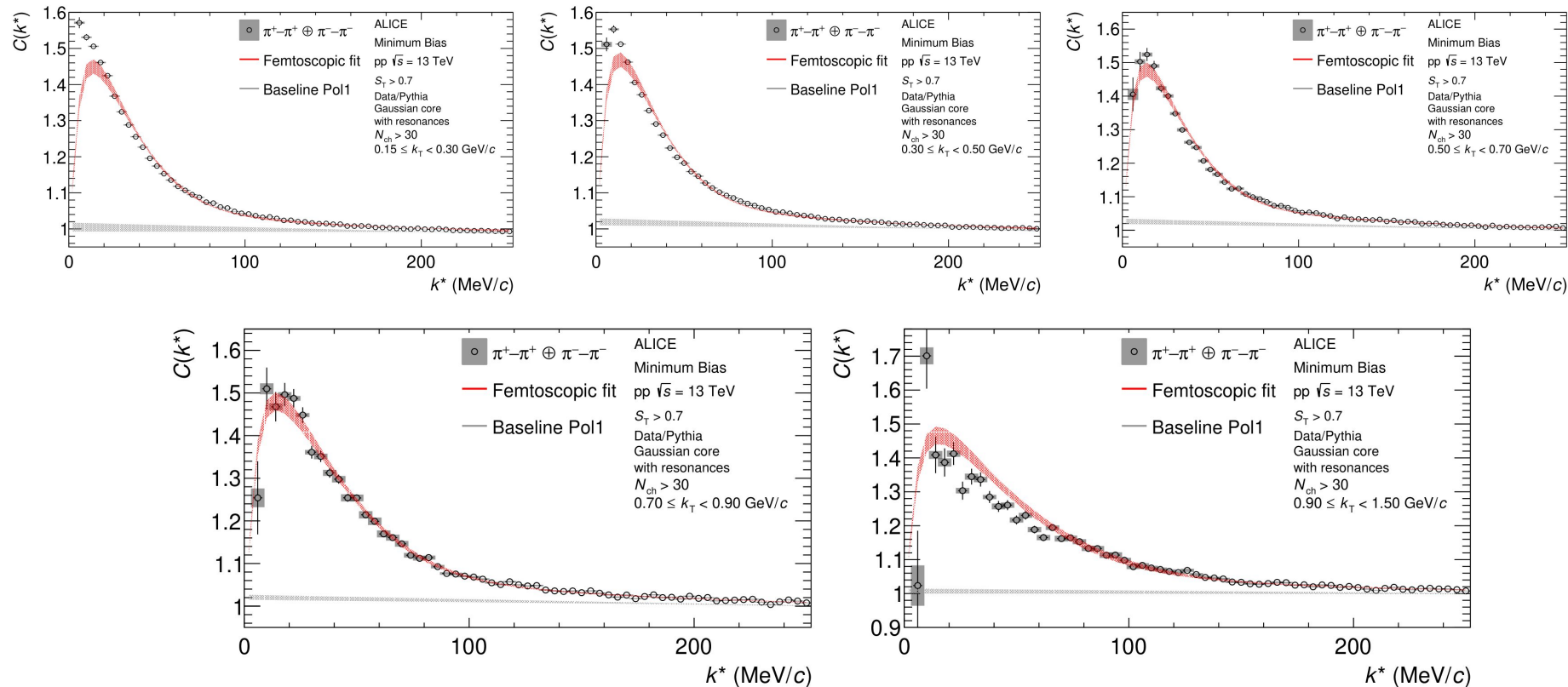
TUM Results for HM $\pi^+\pi^-$ - Pol2



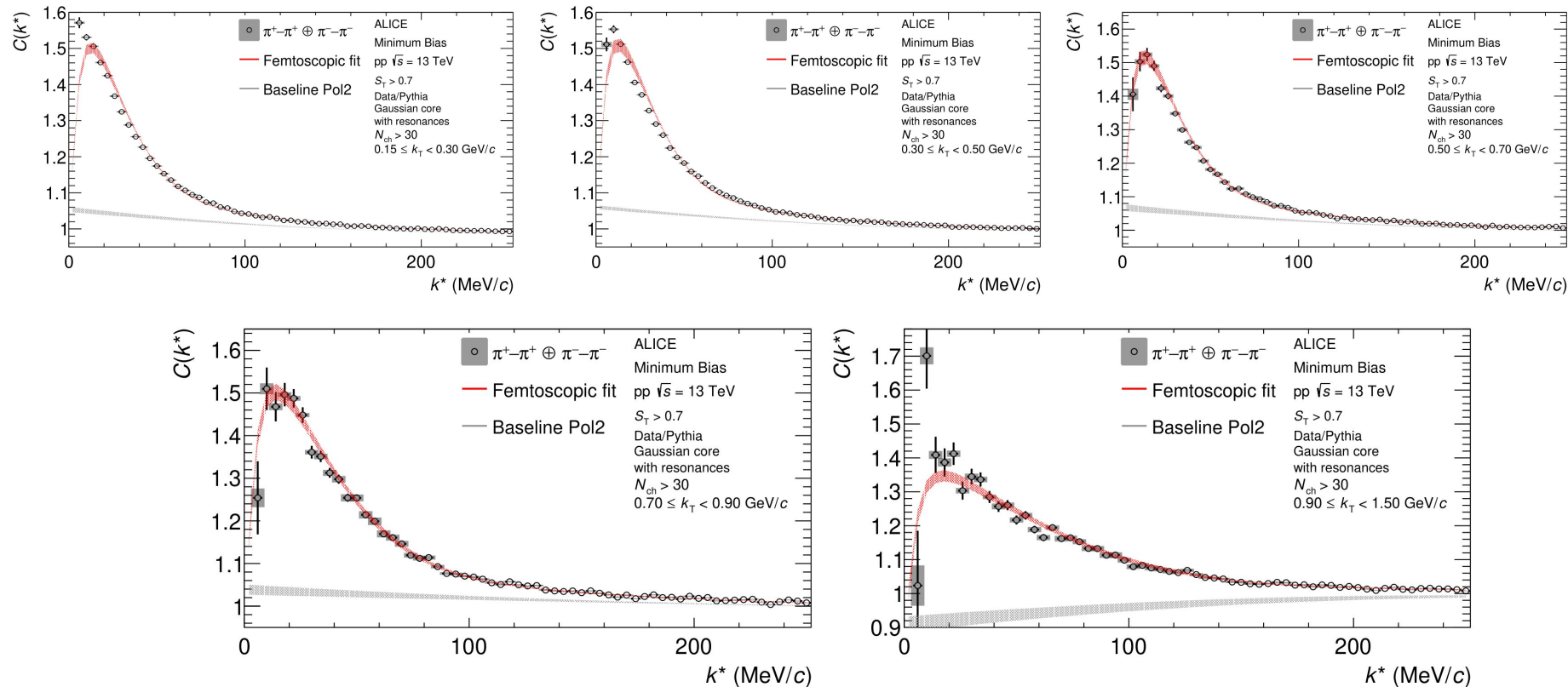
TUM Results for HM $\pi^-\pi^+$ - Pol1



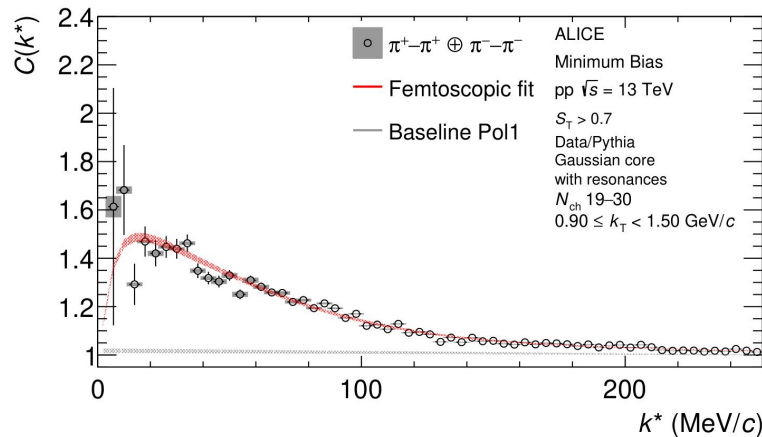
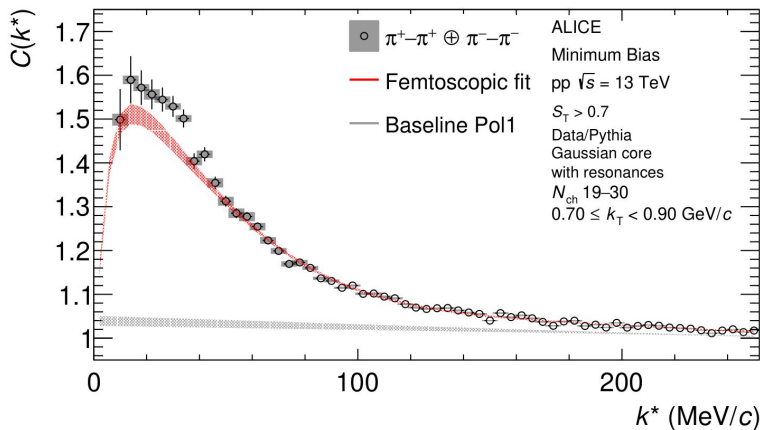
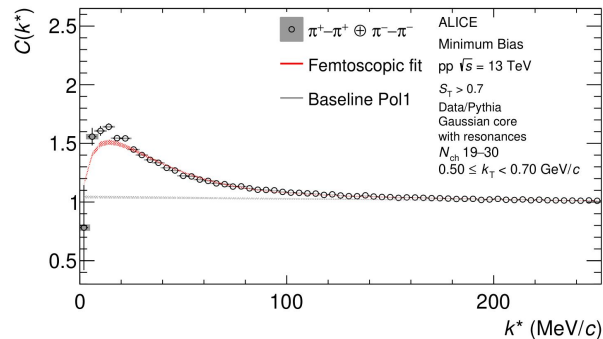
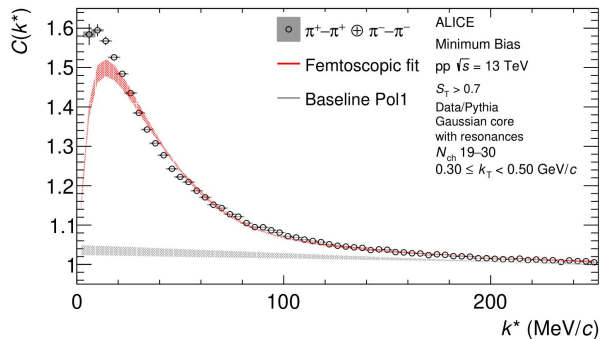
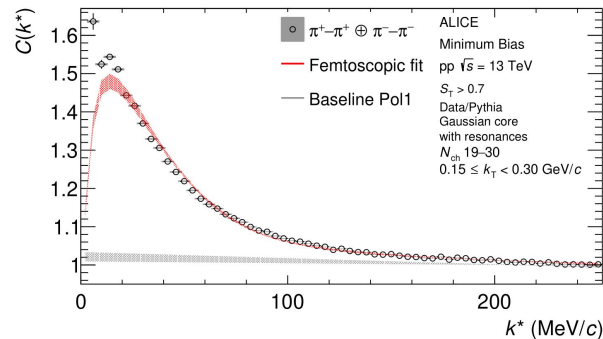
TUM Results for $N_{ch} > 30$ - $\pi^+\pi^-$ - Data/Pythia - Pol1



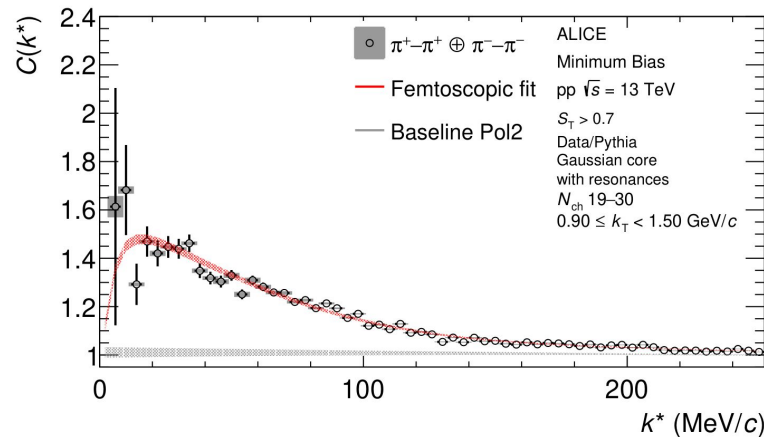
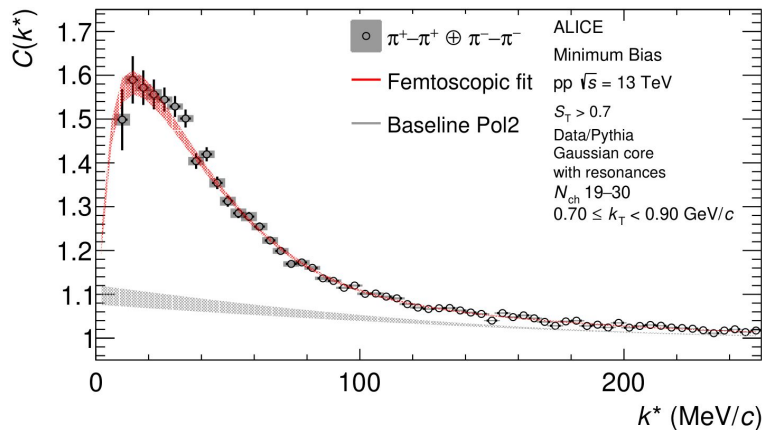
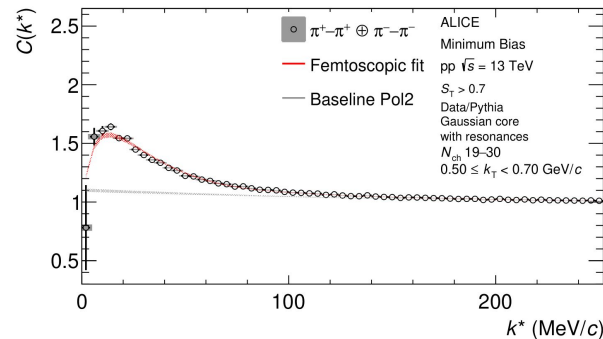
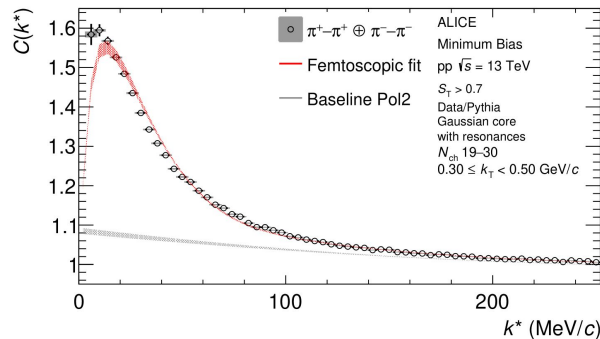
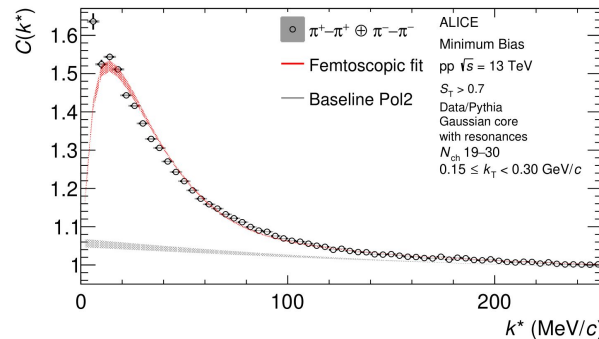
TUM Results for $N_{ch} > 30$ - $\pi^+\pi^-$ - Data/Pythia - Pol2



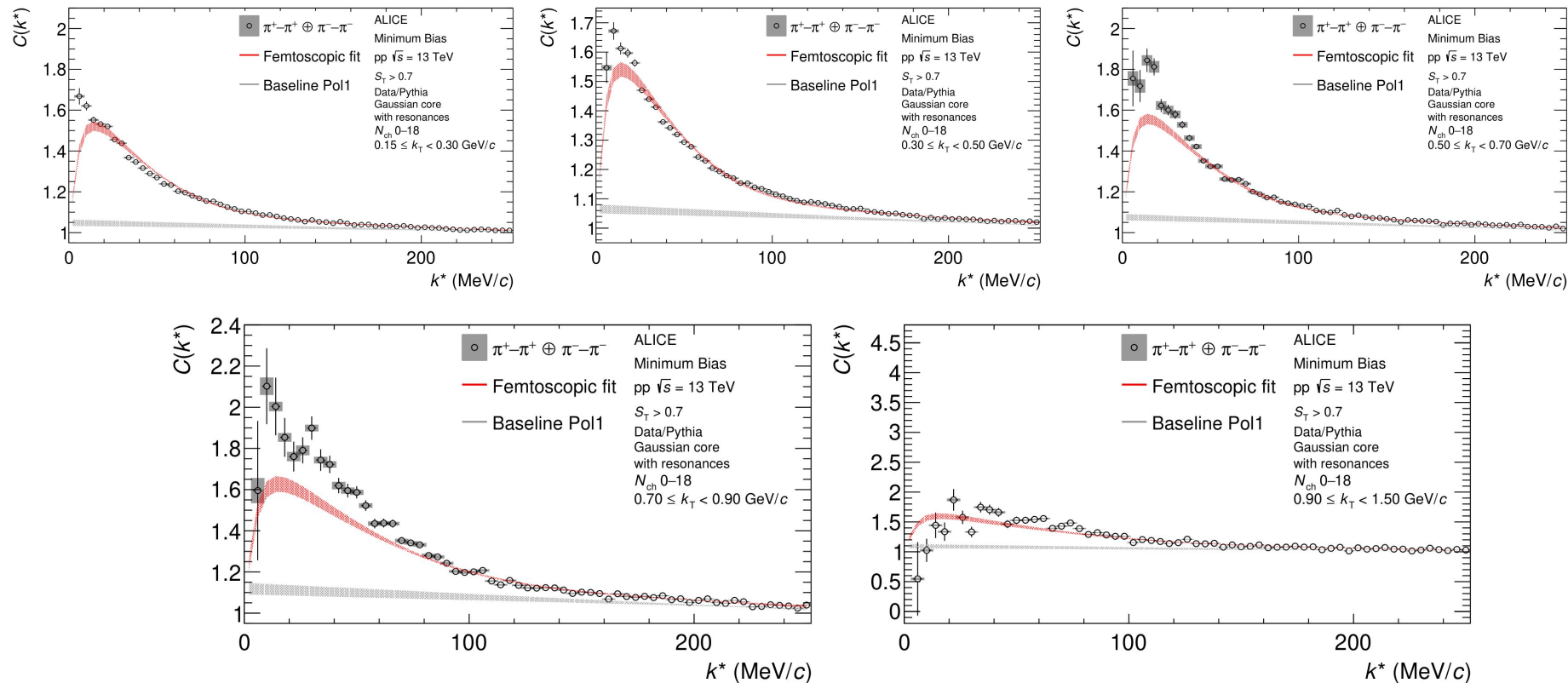
TUM Results for $18 < N_{ch} < 30$ - $\pi^+\pi^-$ - Data/Pythia - Pol1



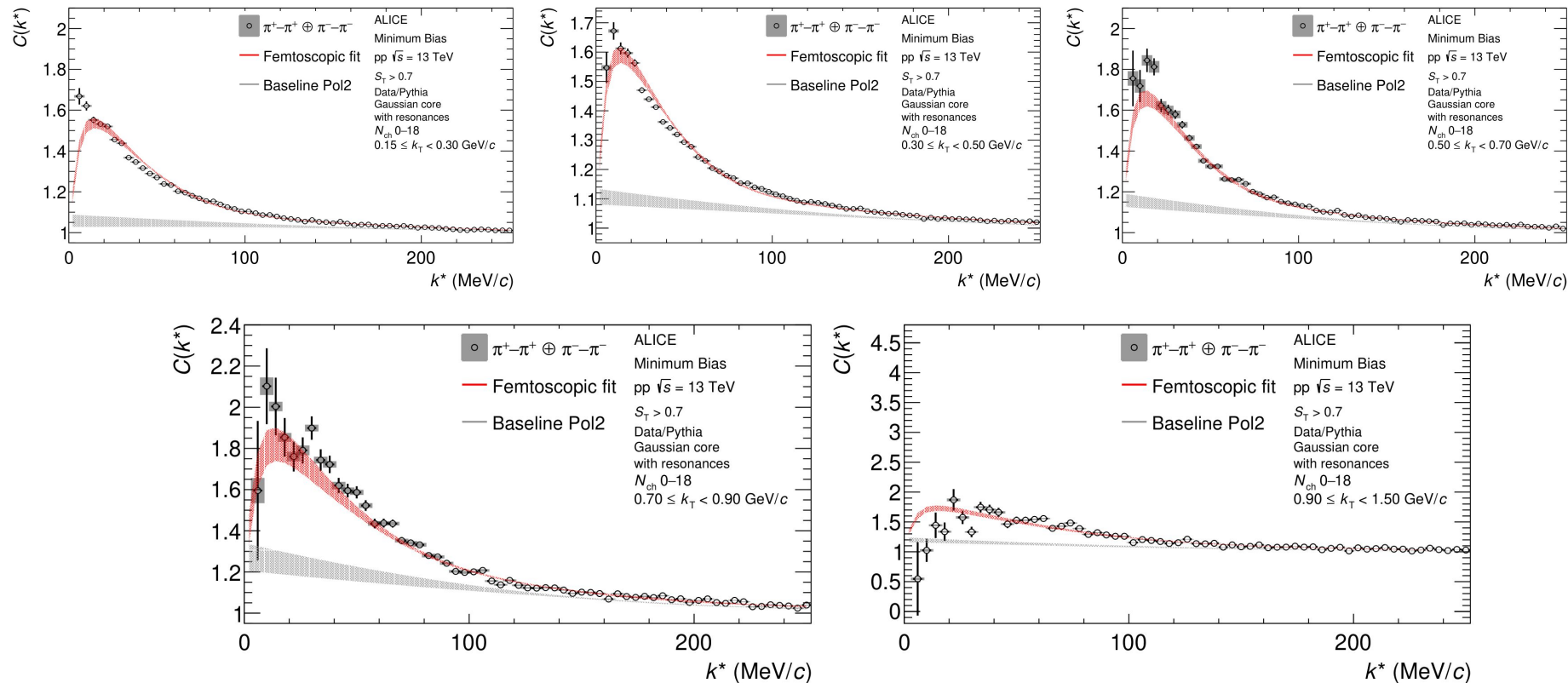
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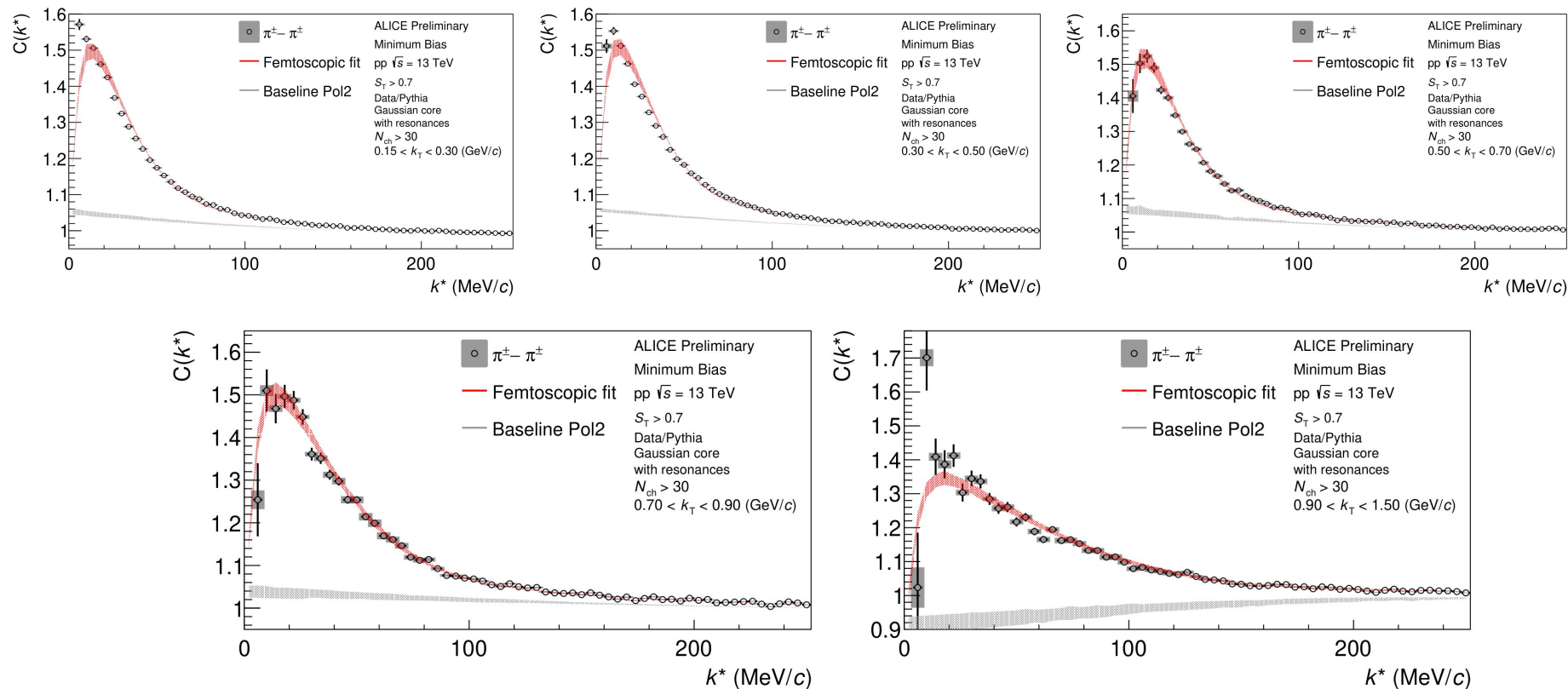
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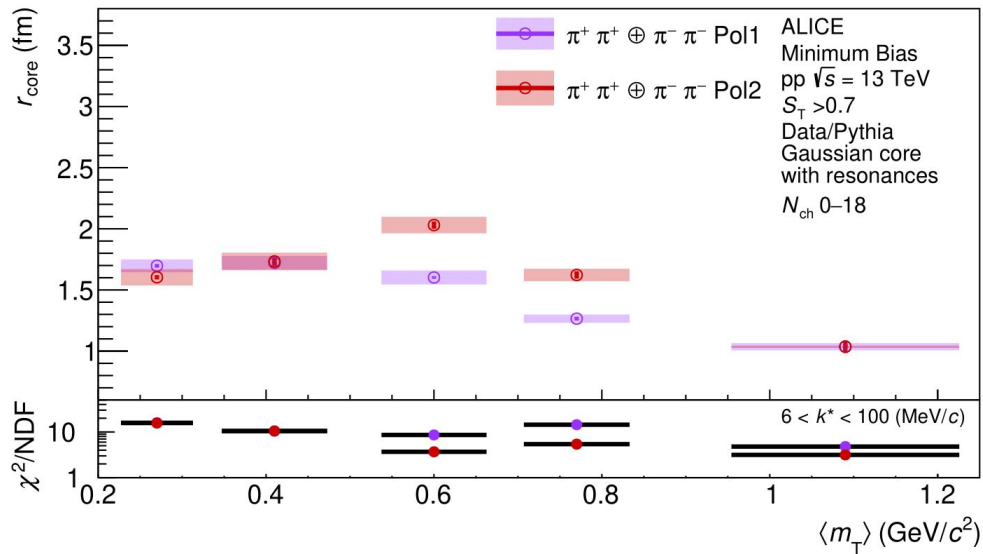


TUM Results for $N_{ch} < 18$ - π - π - Data/Pythia - Pol2

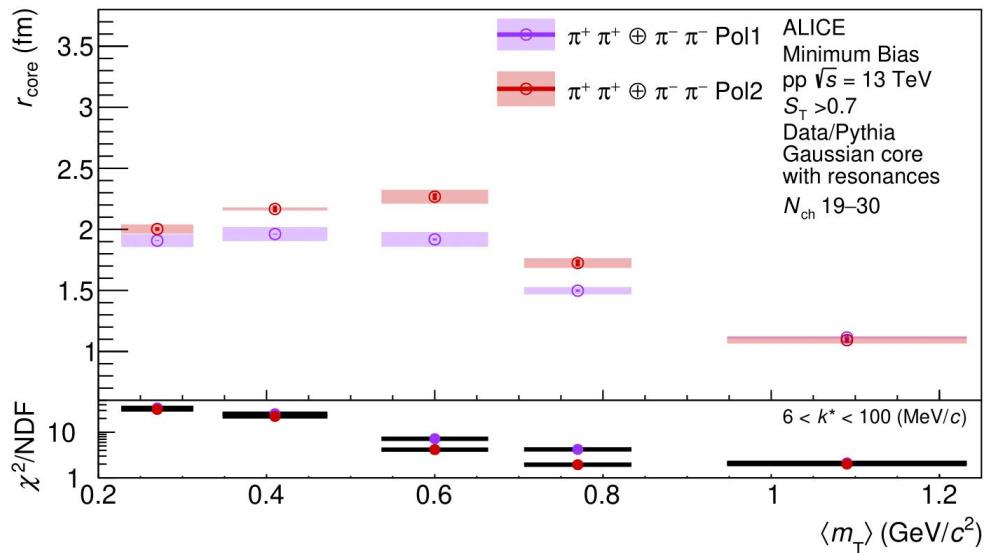


TUM Results for Mult. [> 30] - Data/Pythia - Pol2

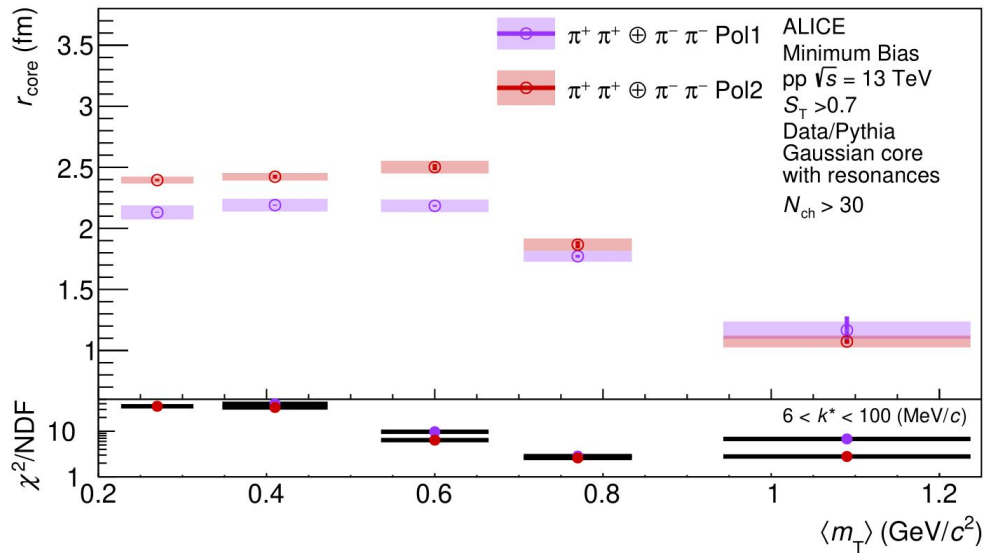




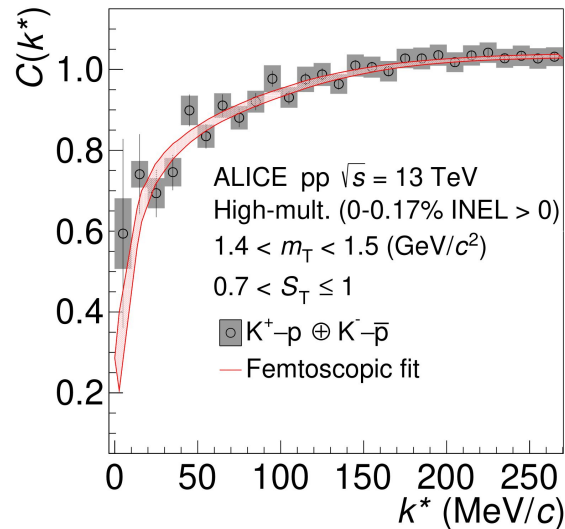
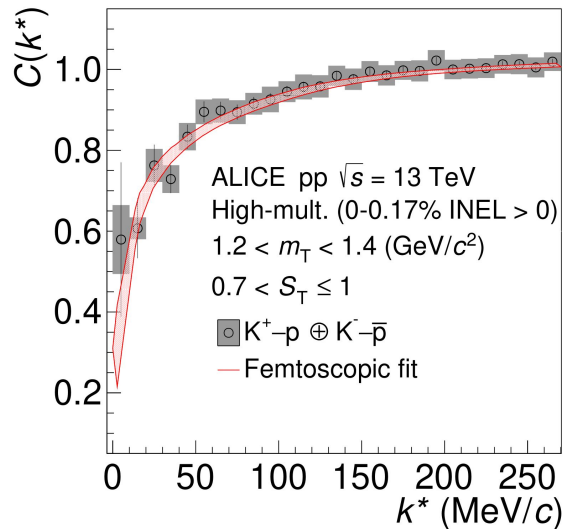
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- The extracted r_{core} radii are increasing with multiplicity



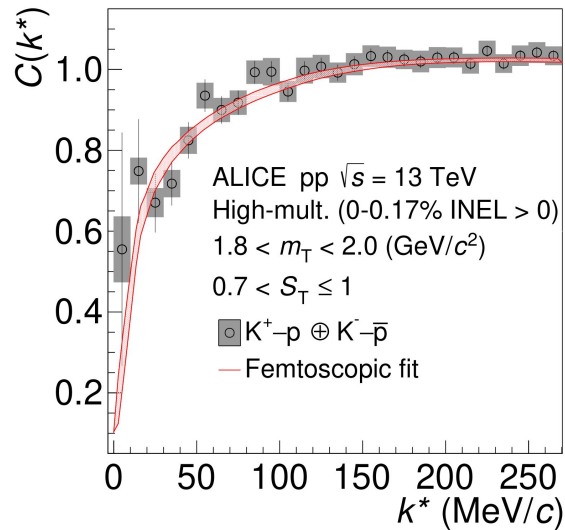
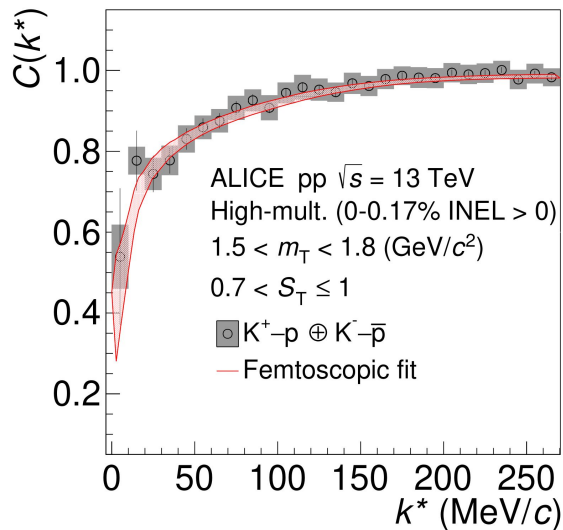
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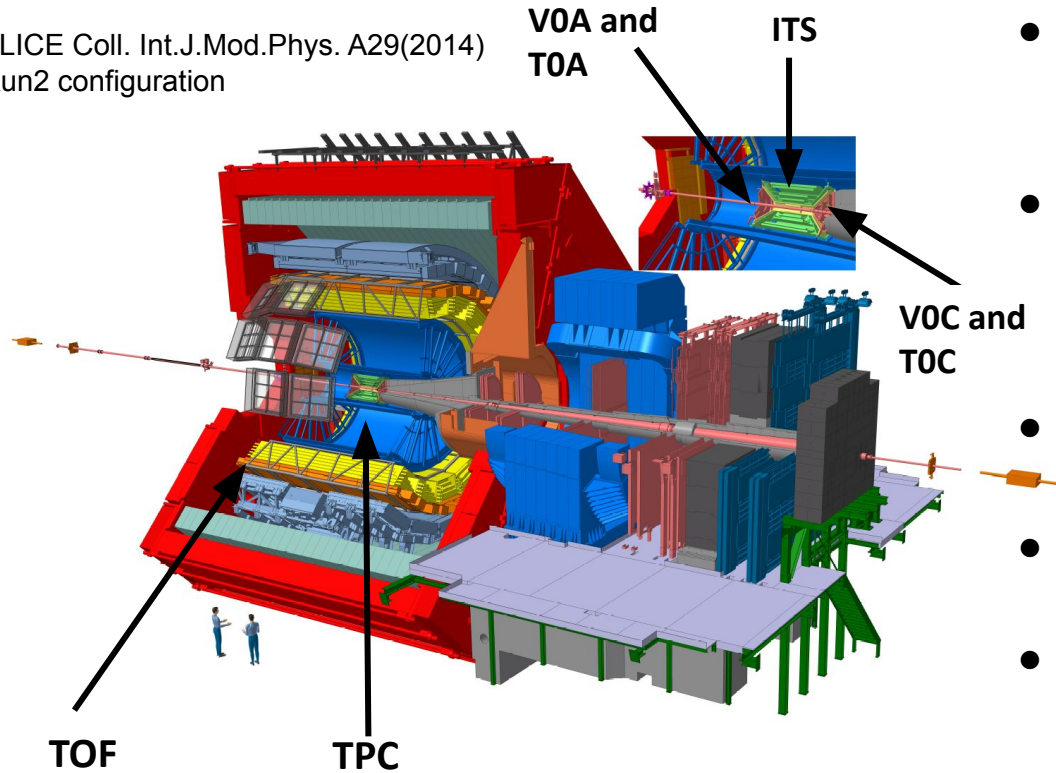


- Strong interaction is modeled by state-of-the-art χ EFT
 [K. Aoki et al. PTEP 1 (2019)]
- Source is modeled with the RSM (as for π) and r_{core} extracted from the fit



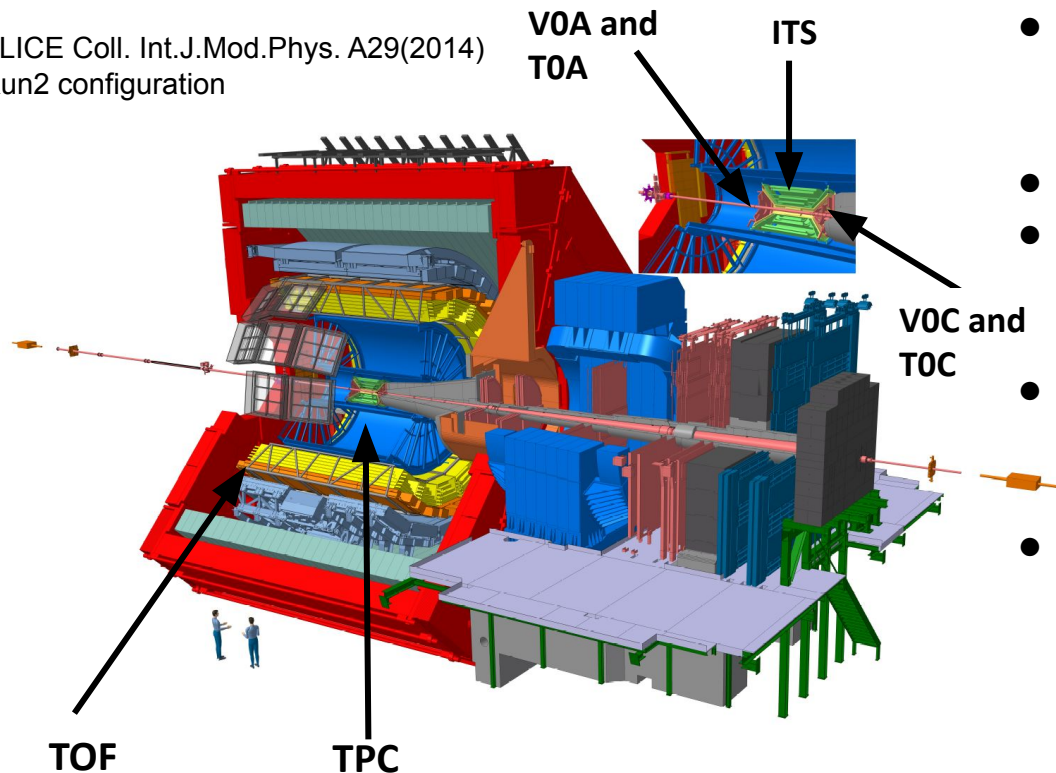
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ALICE Coll. Int.J.Mod.Phys. A29(2014)
Run2 configuration



- Direct detection of charged particles (pions) by TPC and TOF
- Particle identification
 - Mean energy loss in TPC
 - Momentum reconstruction by TOF
- Primary vertex reconstruction by ITS
- Multiplicity estimates by V0
- Reference signal for TOF via T0

ALICE Coll. Int.J.Mod.Phys. A29(2014)
Run2 configuration



- MB pp collisions @ 13 TeV
(1.9×10^9 evts.)
- Mult-Binning: [0-18], [19-30], [>30]
- kT-Binning: (0.15-0.3], (0.3-0.5],
(0.5-0.7], (0.7-0.9], (0.9-1.5]
- General purpose Pythia 8 [1] evts.
filtered by GEANT4 [2] used as MC
- Event cut on transverse sphericity [3]
 $S_{XY} > 0.7$ suppression of mini-jet
background

[1] T. Sjöstrand et al. CPC 191 (2015), [2] S. Agostinelli et al. PRS A 506.3 (2003), [3] ALICE Coll. EPJC 72 (2012)

TUM Estimating the resonance contribution

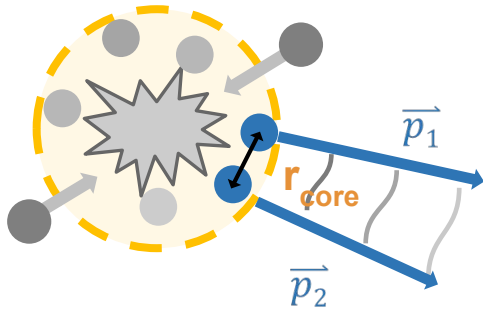
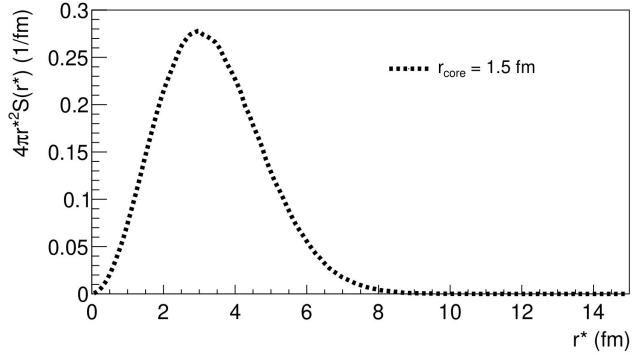
Resonances	$c\tau_{\text{res}}$ (fm)	Fraction (%)
ρ^0	1.3	9.01
ρ^+	1.3	8.71
$\omega(782)$	23.4	7.67
$K^*(892)^+$	3.9	2.29
$\bar{K}^*(892)^0$	3.9	2.25
$b1(1235)^+$	1.4	1.90
$a2(1320)^+$	1.8	1.48
η	150631.3	1.45
$a1(1260)^+$	0.5	1.37
$f2(1270)$	1.1	1.36
$a0(980)^+$	2.6	1.36
$h1(1170)$	0.5	1.18

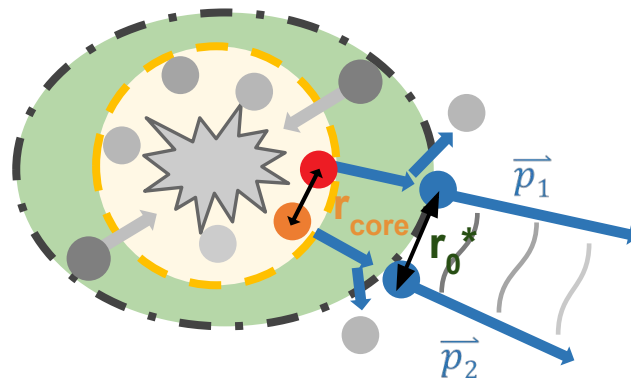
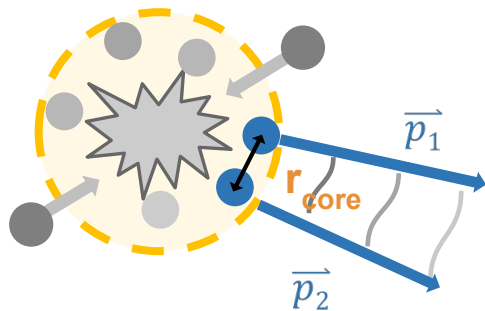
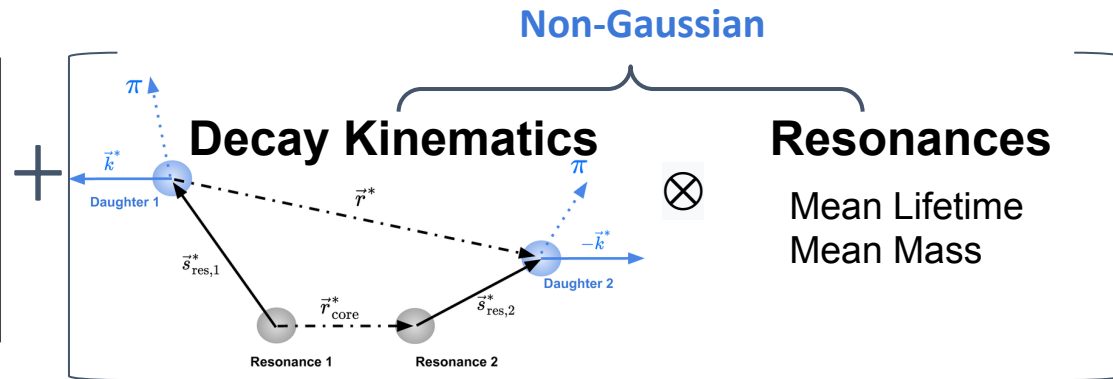
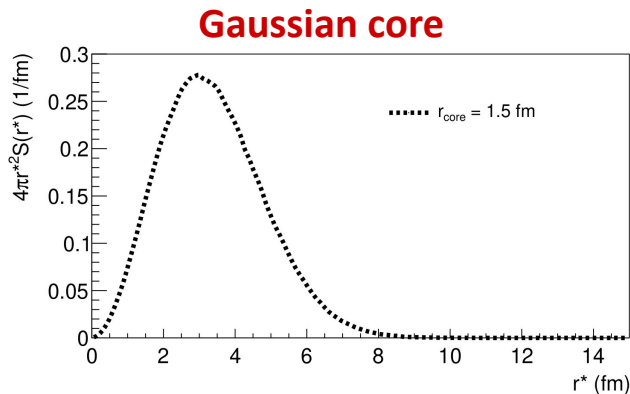
Lifetime $c\tau$ (fm)	Fraction $\mathcal{F}$ (%)	$\langle m_{\text{res}}^{\text{eff}} \rangle$ (GeV/c)
Primordial	28.0	–
$c\tau_{\text{res}} < 1$	14.8	0.308
$1 < c\tau_{\text{res}} < 2$	34.8	0.526
$2 < c\tau_{\text{res}} < 5$	10.2	0.151
$c\tau_{\text{res}} > 5$	12.2	0.146

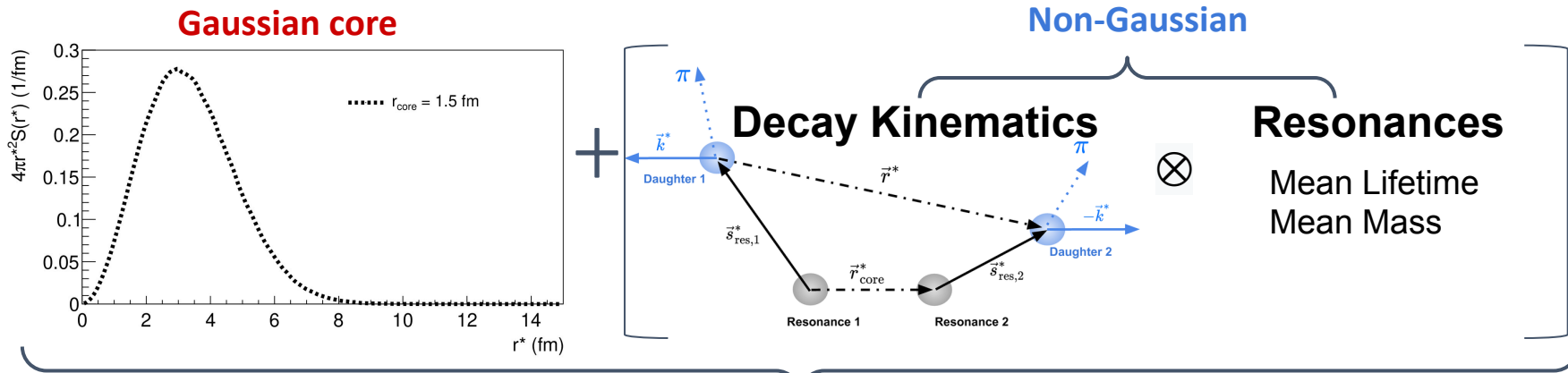
- Employ statistical hadronization model [1]
 - Describe system by statistical ensemble
 - Enforce conservation of quantum numbers
 - Predict yields
- Calculation carried out with Thermal-FIST [2,3]
 - Configure model to pp
 - B.R.s of strong decays fixed to PDG
 - Extract resonances
- Summary parameters for RSM
 - $m_{\text{eff}} = 1124 \text{ GeV}/c^2$
 - $c\tau_{\text{eff}} = 1.5 \text{ fm}$
 - Select resonances cocktail in EPOS [4] for decay kinematics

[1] F. Becattini Z. Phys. C 76 (1997), [2] V. Vovchenko et al. CPC 100 2019,
 [3] V. Vovchenko et al. PRC 100834 (2019), [4] K.Werner et al. PRC 92 (2015)

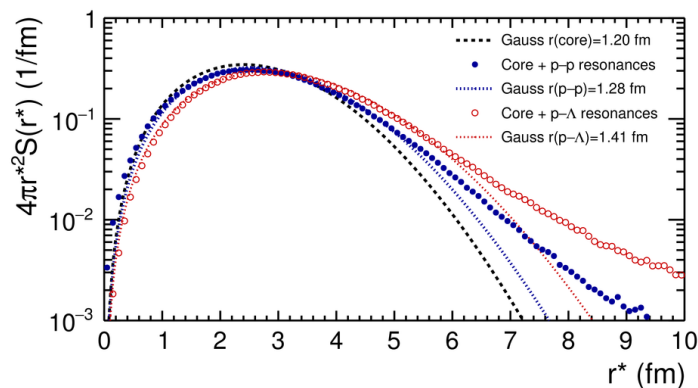
Gaussian core







Source



$$C_{\text{model}}(k^*) =$$

???

But *what* is measured?

- Does purity play a role?
- What about feed-down weak decays?
- Do we have background?

$$C_{\text{model}}(k^*) = 1/C_{\text{MC}}(k^*) \cdot (\lambda_{\text{gen}} C_{\text{gen}}(k^*) + \lambda_{\text{feed}} + \lambda_{\text{misid}})$$

$$C_{\text{model}}(k^*) = 1/C_{\text{MC}}(k^*) \cdot (\lambda_{\text{gen}} C_{\text{gen}}(k^*) + \lambda_{\text{feed}} + \lambda_{\text{misid}})$$

Model for genuine interaction

- Bose-Einstein quantum statistics
- Coulomb interaction

$$C_{\text{model}}(k^*) = 1/C_{\text{MC}}(k^*) \cdot (\lambda_{\text{gen}} C_{\text{gen}}(k^*) + \lambda_{\text{feed}} + \lambda_{\text{misid}})$$

Diagram illustrating the decomposition of the correlation function $C_{\text{model}}(k^*)$ into three components, each with a weight:

- λ_{gen} (66.4 %) - Genuine interaction component
- λ_{feed} (31.6 %) - Feed-down component
- λ_{misid} (2 %) - Misidentified component

Model for **genuine interaction**

- Bose-Einstein quantum statistics
- Coulomb interaction

Introduce **λ -parameter**

- Each component has a weight
- $C(k^*) = 1$, for feed-down and misidentified
- Evaluated by MC studies

$$C_{\text{model}}(k^*) = 1/C_{\text{MC}}(k^*) \cdot (\lambda_{\text{gen}} C_{\text{gen}}(k^*) + \lambda_{\text{feed}} + \lambda_{\text{misid}})$$

The equation is annotated with colored boxes: $C_{\text{MC}}(k^*)$ is in a red box; λ_{gen} is in a green box with "66.4 %" above it; $C_{\text{gen}}(k^*)$ is in a purple box; λ_{feed} is in a green box with "31.6 %" above it; and λ_{misid} is in a green box with "2 %" above it.

Correct for **non-femto effects**

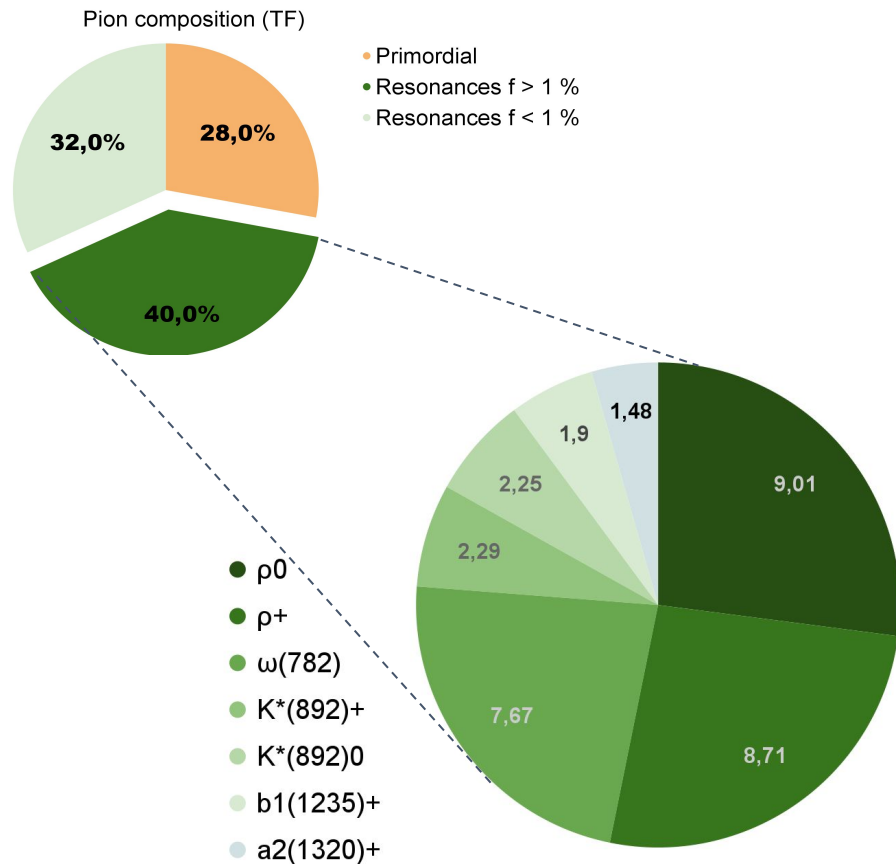
- Divide by $C(k^*)$ obtained from MC
- Collimated production often called 'mini-jet'

Model for **genuine interaction**

- Bose-Einstein quantum statistics
- Coulomb interaction

Introduce **λ -parameter**

- Each component has a weight
- $C(k^*) = 1$, for feed-down and misidentified
- Evaluated by MC studies



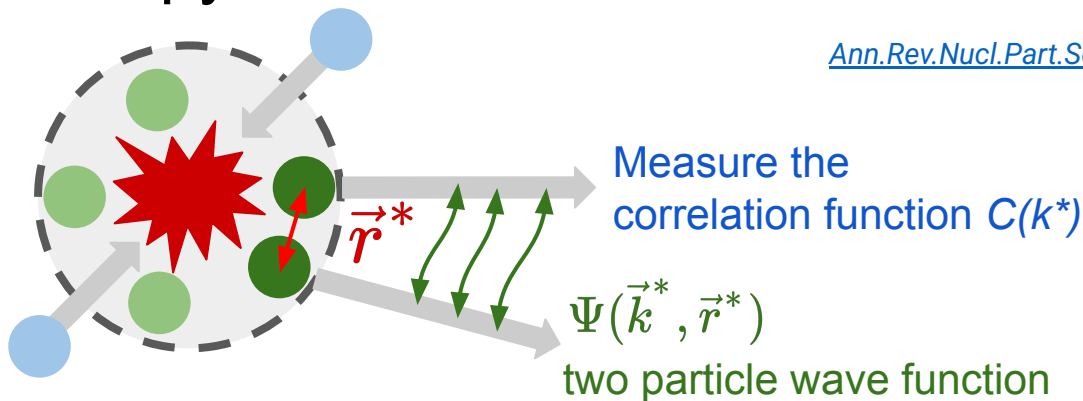
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 - Use statistical hadronization model [3]
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[4] K. Werner et al. PRC 92 (2015)



$$C(k^*) = \int S(r^*) \left| \Psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3 r^* \xrightarrow{k^* \rightarrow \infty} 1$$

- Measure $C(k^*)$, 'fix' interaction, study $S(r^*)$
- For evaluation of integral and $S(r^*)$ use CATS framework [Eur.Phys.J.C 78 \(2018\) 5, 394](#)



- Study final-state interactions of exotic pairs
- Needs **precise** understanding of the source

- Access final state interactions
 - Complementary to scatterings experiments
 - Many measured for the first time

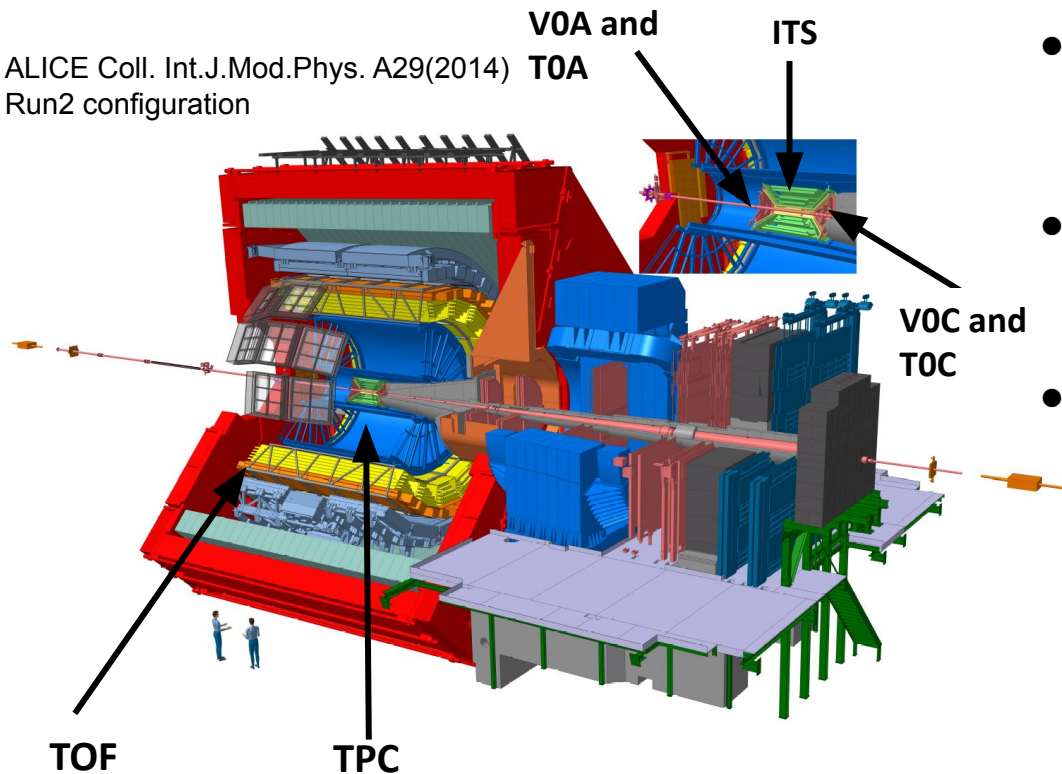
- Valentina Mantovani Sarti (C5):
"Accessing the strong interaction between Λ baryons and kaons with femtoscopy at LHC"
- Wioleta Rzęsa (C5):
"A study of K^-d and K^+d interactions via femtoscopy technique"

- Enables theory comparisons
 - Tests of LQCD
 - χ EFT

- Albert Feijoo (C5):
"Correlation Function constraints on $S=-2$ meson-baryon interaction from UChPT."

TUM Femtoscopy at ALICE in HM pp 13 TeV

ALICE Coll. Int.J.Mod.Phys. A29(2014)
Run2 configuration



- HM pp collisions @ 13 TeV
 - 1 Billion evts. in Run2
- Direct detection of charged particles (π , K, p) by TPC and TOF
- Particle identification
 - Mean energy loss in TPC
 - Momentum reconstruction by TOF
 - Purity of about 99 % for π , K, p due to excellent PID capabilities

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Article | [Published: 09 December 2020](#)

Unveiling the strong interaction among hadrons at the LHC

[ALICE Collaboration](#)[Nature](#) **588**, 232–238(2020) | [Cite this article](#)[Metrics](#)

Abstract

One of the key challenges for nuclear physics today is to understand from first principles the effective interaction between hadrons with different quark content. First successes have been achieved using techniques that solve the dynamics of quarks and gluons on discrete space-time lattices^{1,2}. Experimentally, the dynamics of the strong interaction have been studied by scattering hadrons off each other. Such scattering experiments are difficult or

- Analyses so far...

*ALICE Collaboration**PRC* 99 (2019) 2, 024001*PLB* 797 (2019), 134822*PRL* 123 (2019), 112002*PLB* 805 (2020), 135419*PLB* 811 (2020), 135849***Nature* 588 (2020) 232–238***PRL* 127 (2021), 172301*PLB* 833 (2022), 137272*PLB* 829 (2022), 137060*PRD* 106 (2022) 5, 052010*PLB* (2022), 137223*EPJC* 83 (2023) 4, 340*PLB* 845 (2023), 138145

System

p–p, p– Λ Λ – Λ p– Ξ p– Σ 0p–p, p– Λ p– Ω p– ϕ p– Λ p–(anti)p, p–(anti) Λ , Λ –(anti) Λ

p–D

 Λ – Ξ

K–p

 Λ –K

Not using universal source

PRL 124 (2020), 09230

(anti)K–p

PLB 822 (2021), 136708

(anti)K–p

~~nature~~

- Femtoscopy ...
 - allows to access the final state interaction between 'all kinds of' hadrons
 - is a complementary method to traditional scattering experiments

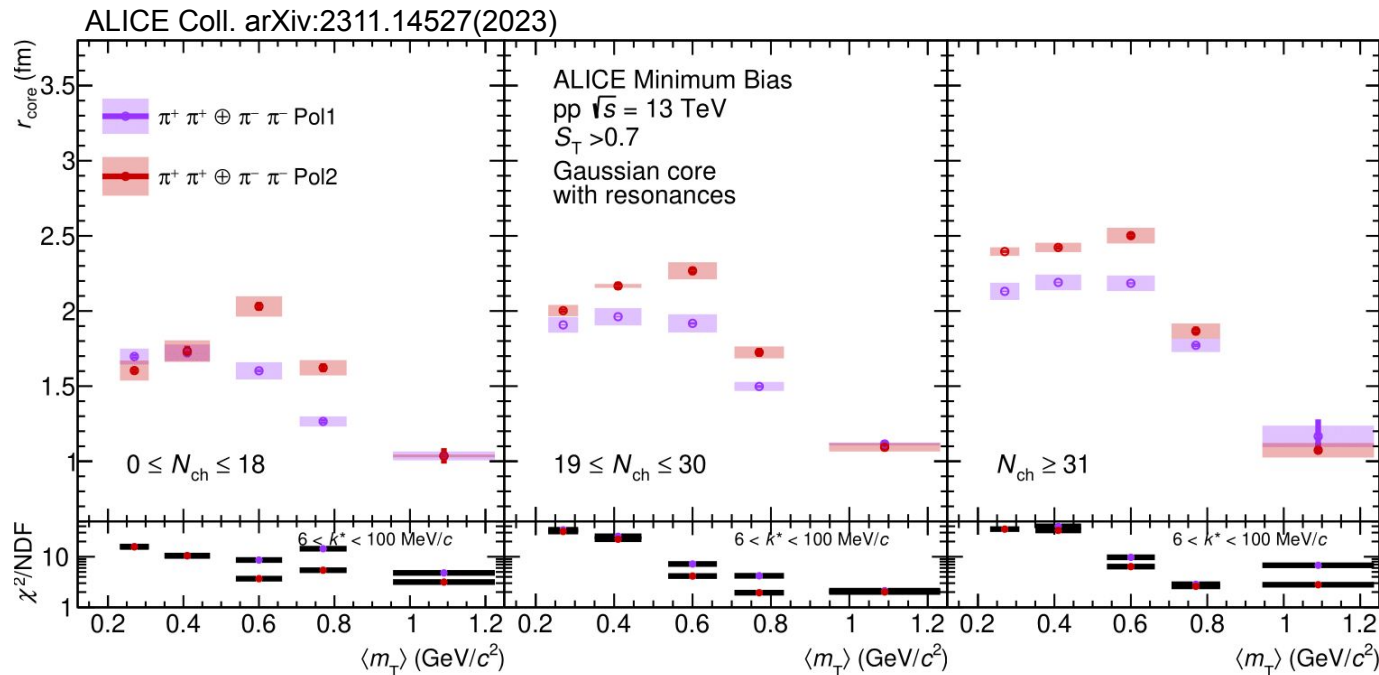
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● Analyses so far...

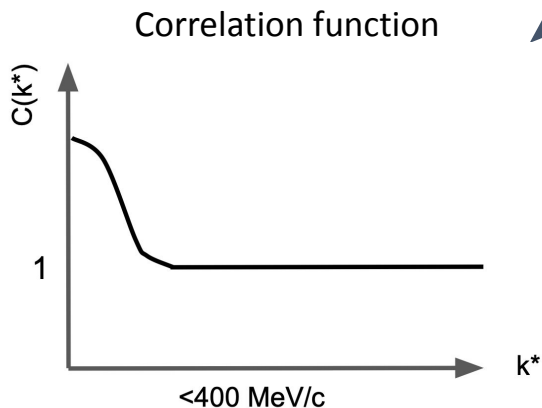
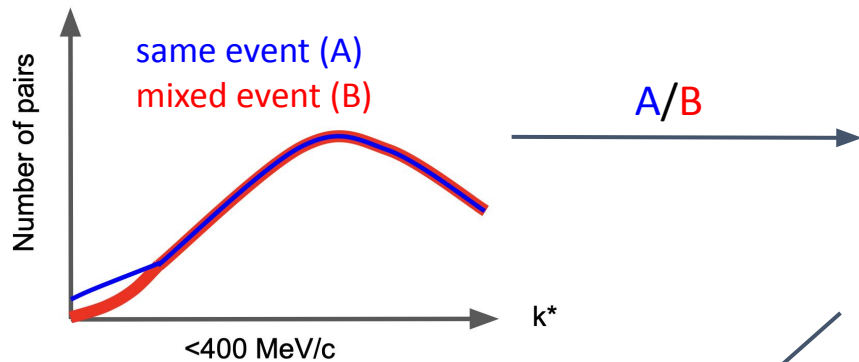
-	ALICE Collaboration	System
	PRC 99 (2019) 2, 024001	p-p, p- Λ
	PLB 797 (2019), 134822	Λ - Λ
	PRL 123 (2019), 112002	p- Ξ
	PLB 805 (2020), 135419	p- $\Sigma 0$
	PLB 811 (2020), 135849	p-p, p- Λ
	Nature 588 (2020) 232-238	p-Ω
	PRL 127 (2021), 172301	p- ϕ
	PLB 833 (2022), 137272	p- Λ
	PLB 829 (2022), 137060	p-(anti)p, p-(anti) Λ , Λ -(anti) Λ
	PRD 106 (2022) 5, 052010	p-D
	PLB (2022), 137223	Λ - Ξ
	EPJC 83 (2023) 4, 340	K-p
	PLB 845 (2023), 138145	Λ -K

Not using universal source

PRL 124 (2020), 09230	(anti)K-p
PLB 822 (2021), 136708	(anti)K-p



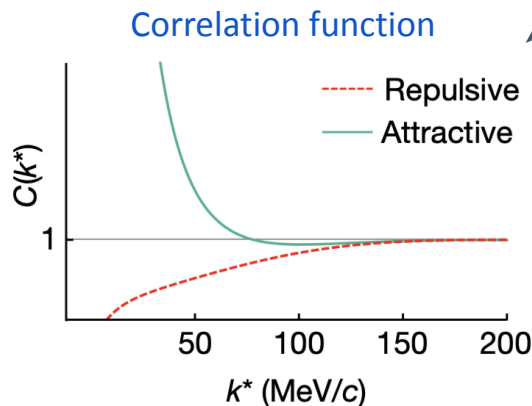
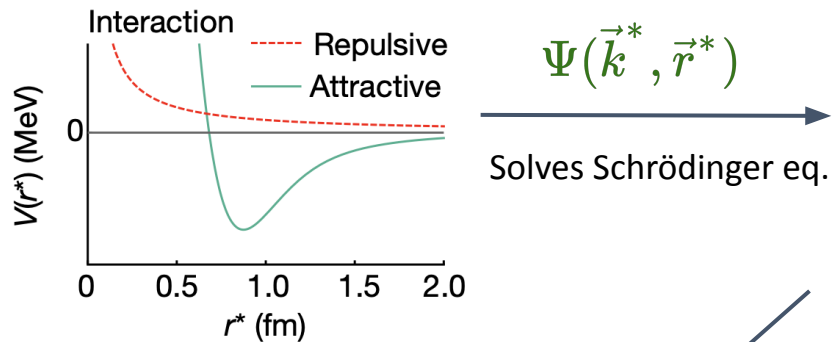
- Studied double differential in multiplicity and m_T
 - Scaling with multiplicity
 - Consistent trend across multiplicities



Experiment

$$C(k^*) = \frac{P(\vec{p}_1, \vec{p}_2)}{P(\vec{p}_1)P(\vec{p}_2)} = \mathcal{N} \frac{A(k^*)}{B(k^*)}$$

- Obtain pairs form
 - same event (A)
 - uncorrelated sample (B)
- Understand data
 - purity, fractions (feed-down)
 - background?



Theory

$$C(k^*) = \int S(r^*) |\Psi(\vec{k}^*, \vec{r}^*)|^2 d^3 r^*$$

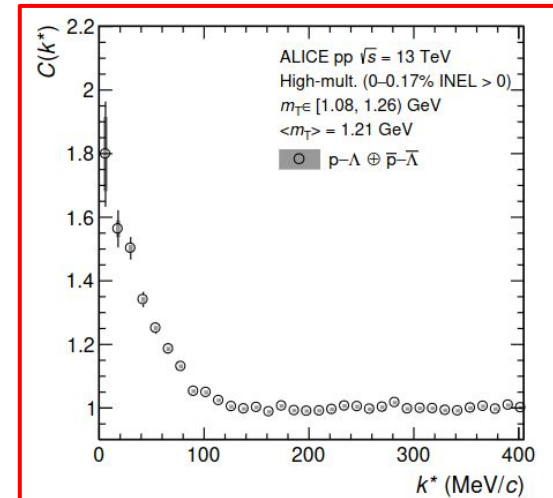
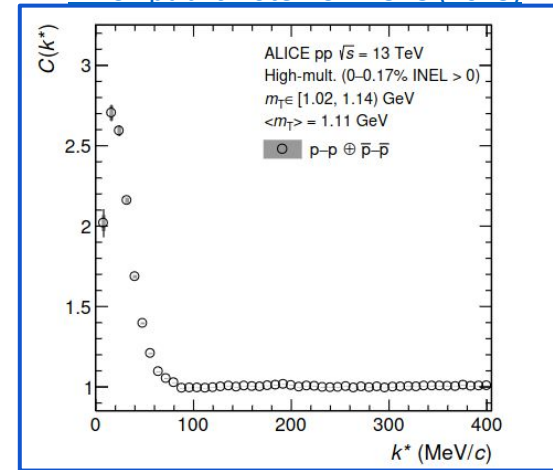
- Calculate $\psi(r^*, k^*)$
 - QS + Coulomb or χ EFT
- **Model $S(r^*)$**
 - Gaussian core
 - Resonance tails
 - Abundances ? (Thermal model)
- CATS framework [1]

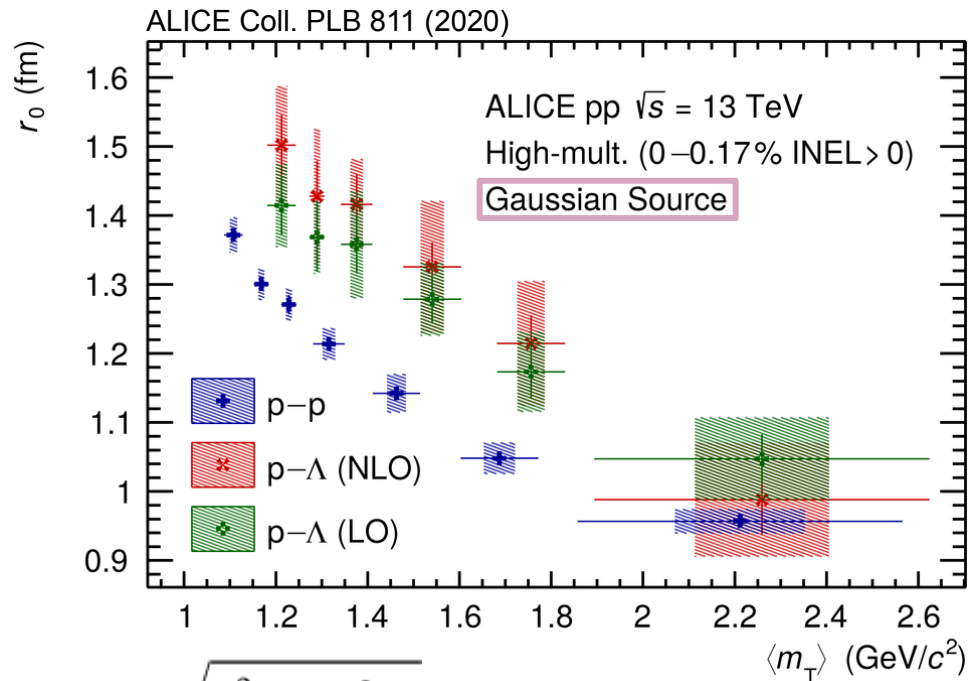
[1] D. Mihaylov et al. EPJC78(2018) 394

- Common source for all produced hadrons in small systems?
- Use $p\text{--}p$ (well known interaction) to constrain the femtoscopic source
- Validate findings with $p\text{--}\Lambda$

$$m_T = \sqrt{k_T^2 + m_{\text{avg}}^2}$$

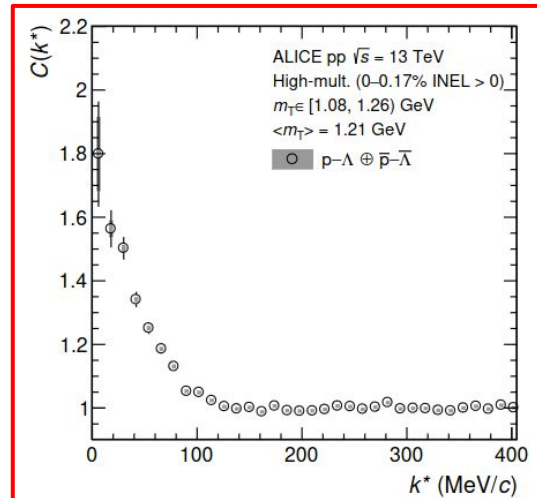
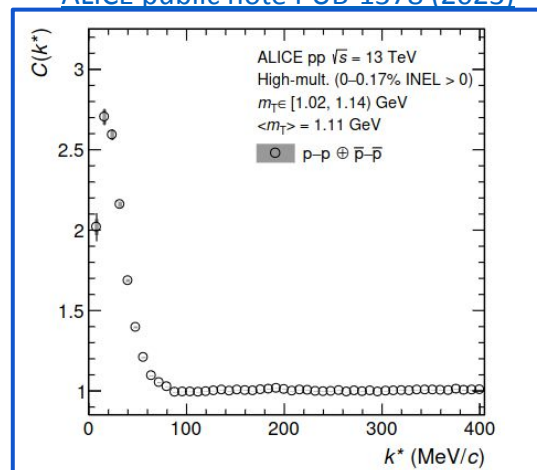
$$k_T = \frac{1}{2} |\vec{p}_{T,1} + \vec{p}_{T,2}|$$

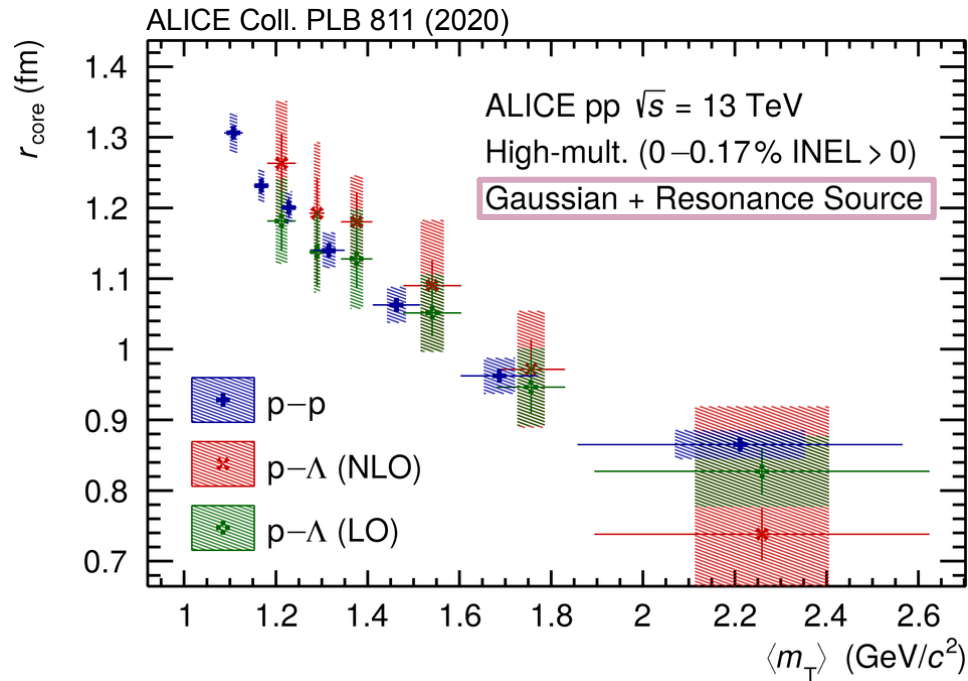




$$m_T = \sqrt{k_T^2 + m_{\text{avg}}^2}$$

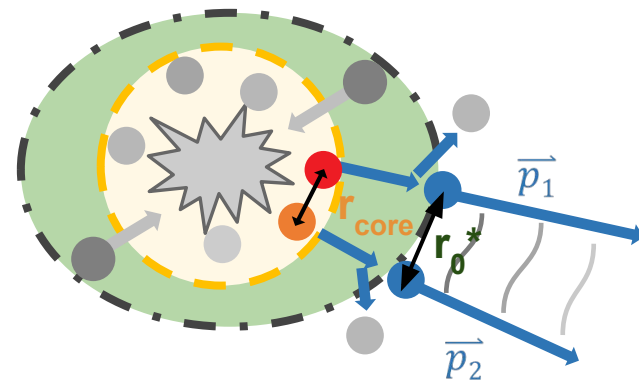
$$k_T = \frac{1}{2} |\vec{p}_{T,1} + \vec{p}_{T,2}|$$





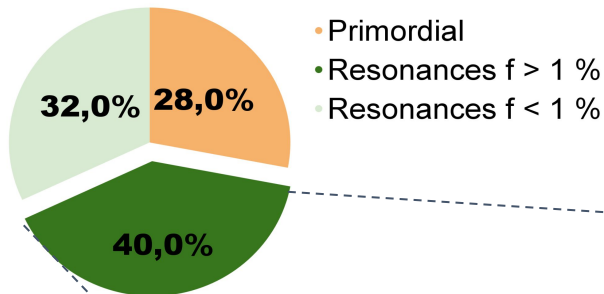
Access smaller m_T by studying π - π and meson-baryon correlations i.e. K^+ -p

- Common scaling is restored by accounting for **non-gaussian** contributions
 - Motivates the assumption of a universal particle source for baryons
- How well does the model perform for mesons? Is the scaling different?



TUM Estimating the resonance contribution (π)

Pion composition (TF)

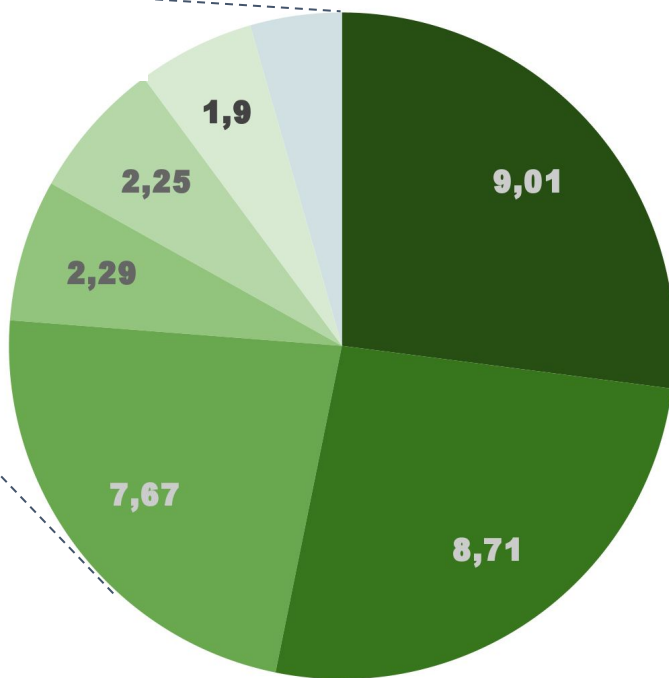


- Calculation carried out with Thermal-FIST [1,2]
 - Use statistical hadronization model [3]
 - **28 % primordial, 72 % resonances**

- Summary parameters for RSM
 - $m_{\text{eff}} = 1124 \text{ GeV}/c^2$
 - $c\tau_{\text{eff}} = 1.5 \text{ fm}$

Resonances $f > 1 \%$

- ρ^0
- ρ^+
- $\omega(782)$
- $K^*(892)^+$
- $K^*(892)^0$
- $b_1(1235)^+$
- $a_2(1320)^+$



- [1] V. Vovchenko et al. PRC 100834 (2019)
 [2] V. Vovchenko et al. CPC 100 (2019)
 [3] F. Becattini Z. Phys. C 76 (1997)

TUM Region of homogeneity and m_T scaling

Region of homogeneity: “size and shape of the phase space cloud of outgoing particles whose velocities have **specific** magnitude and direction.”

A simple case: “For an infinite volume, the size of this region is set by the length one must move, before **collective velocity** overcomes **the thermal velocity**.”

TUM Region of homogeneity and m_T scaling

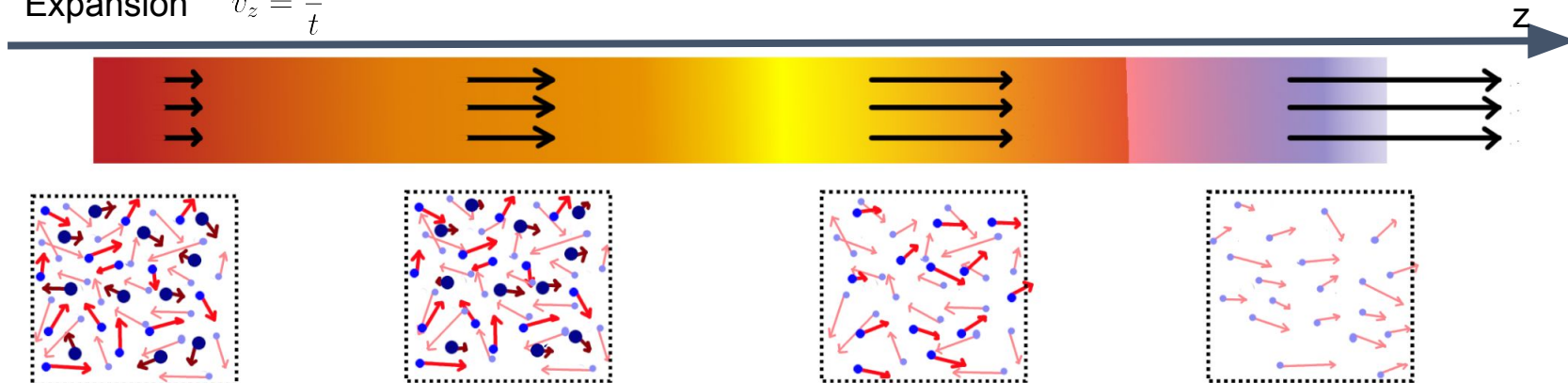
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A simple case: “For an infinite volume, the size of this region is set by the length one must move, before **collective velocity overcomes the thermal velocity.**”

$$\text{homogeneity length} = \frac{\text{thermal velocity}}{\text{fluid velocity gradient}}$$

$$\text{thermal velocity} \sim \sqrt{\frac{T}{m_T}}$$

Expansion $v_z = \frac{z}{t}$



Heavier particles emit sooner

Lighter particles emit later

TUM Region of homogeneity and m_T scaling

Region of homogeneity: “size and shape of the phase space cloud of outgoing particles whose

As it moves • What smallest/largest source size can we achieve?

- We expect a simpler evolution in pp
- How to deal with resonances?

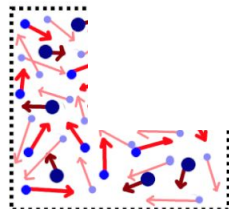
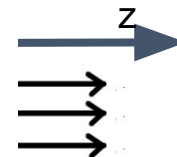
homog

Expa

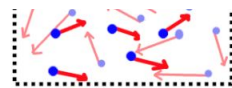
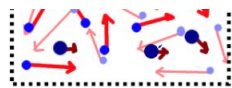
- How does the source evolve in small systems?
 - No scaling at all?
 - Or scaling i.e. a hint of collectivity in small systems?

st

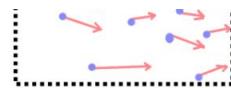
$$\frac{\overline{T}}{m_T}$$

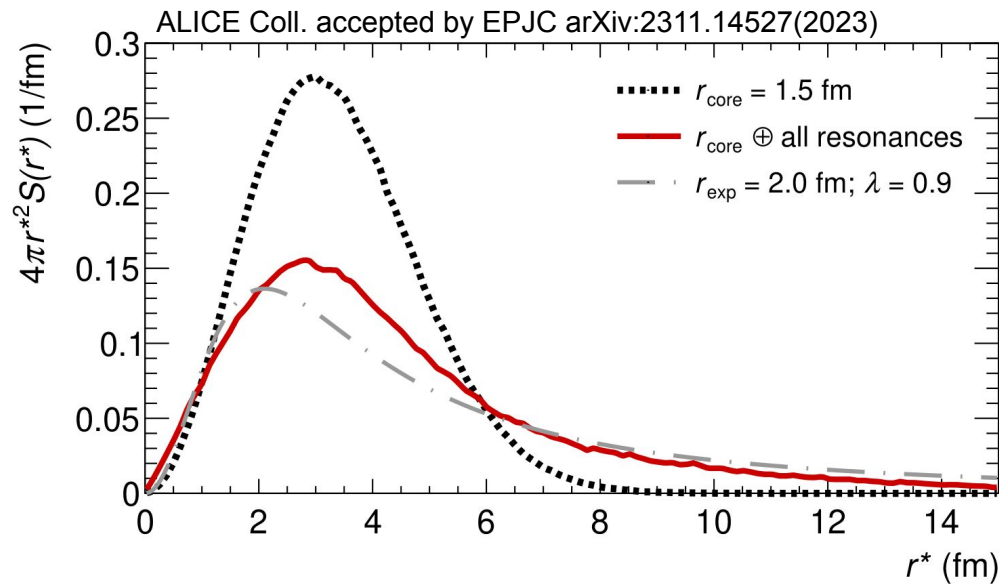


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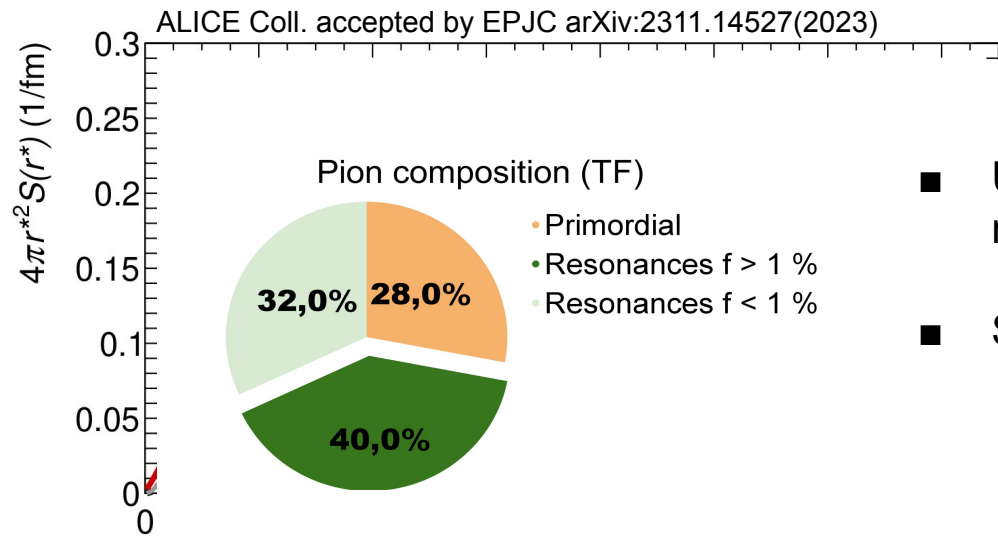




- Example calculation using CATS [1]
- Comparison of exponential source with resonance source model (RSM)
 - Exponential mimics RSM
 - Obtained radii differ
 - RSM provides quantitative insight of resonance contributions
- Resonances explain previous findings of exponential type source for $\pi-\pi$

[1] D. Mihaylov et al. EPJC 78 (2018)

TUM Study the effect of the resonances



- Using statistical hadronisation model [1, 2, 3]

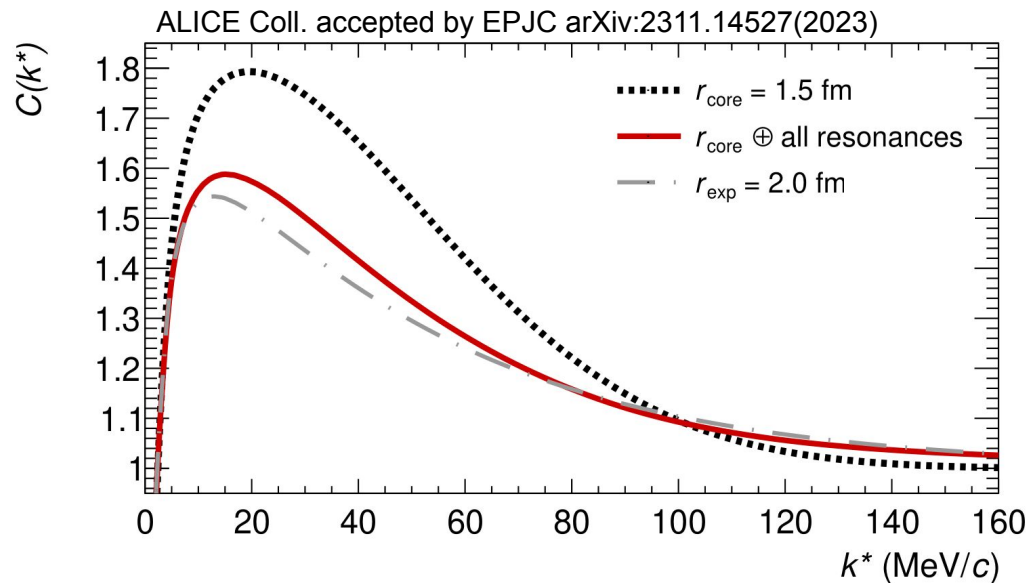
- Summary parameters

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