

# The QCD phase structure at finite density: Facts & Fiction

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Universität Heidelberg & ExtreMe Matter Institute

ECT\* Trento, September 11<sup>th</sup> 2025



[fqcd-collaboration.github.io](https://fqcd-collaboration.github.io)



STRUCTURES  
CLUSTER OF  
EXCELLENCE



UNIVERSITÄT  
HEIDELBERG  
ZUKUNFT  
SEIT 1386





**fqcd-collaboration.github.io**

**Dalian, Beijing, Darmstadt, Heidelberg, Gießen**

**Braun, Chen, Fu, Gao, Geissel, Huang, Ihssen, Lu, Pawłowski, Rennecke,  
Sattler, Schallmo, Tan, Töpfel, Wen, Wessely, Yin, Wang, Zheng, Zorbach**

## **Selected talks**

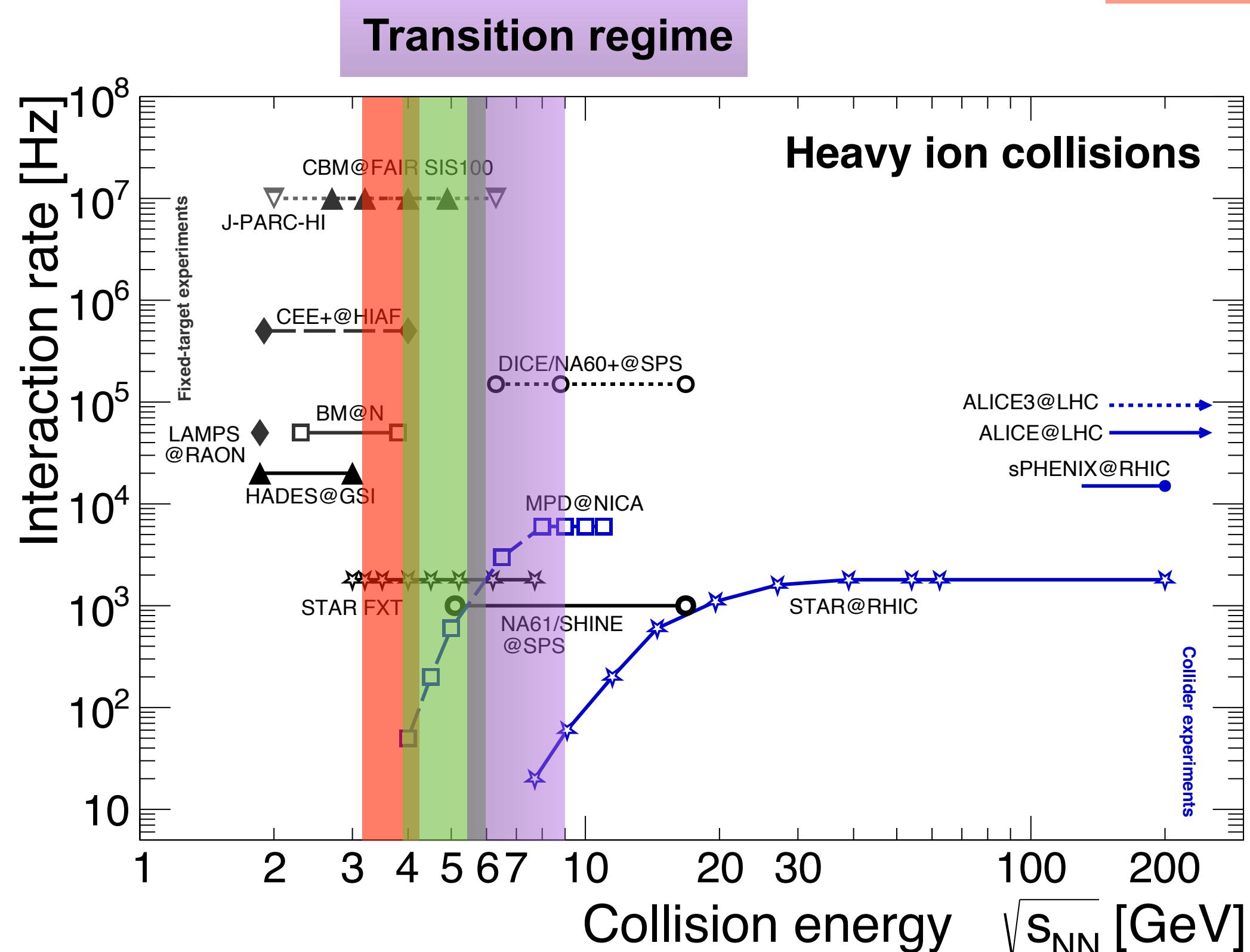
**Workshop Confinement and symmetry from vacuum to QCD phase diagram:  
The QCD phase structure from first principles**

**Satellite meeting Quark Matter 2025: Physics at high net-baryon densities:  
New Insights on the Phase Structure with Functional OCD**

**PhD school xQCD 2024:  
Functional QCD and the QCD phase structure**

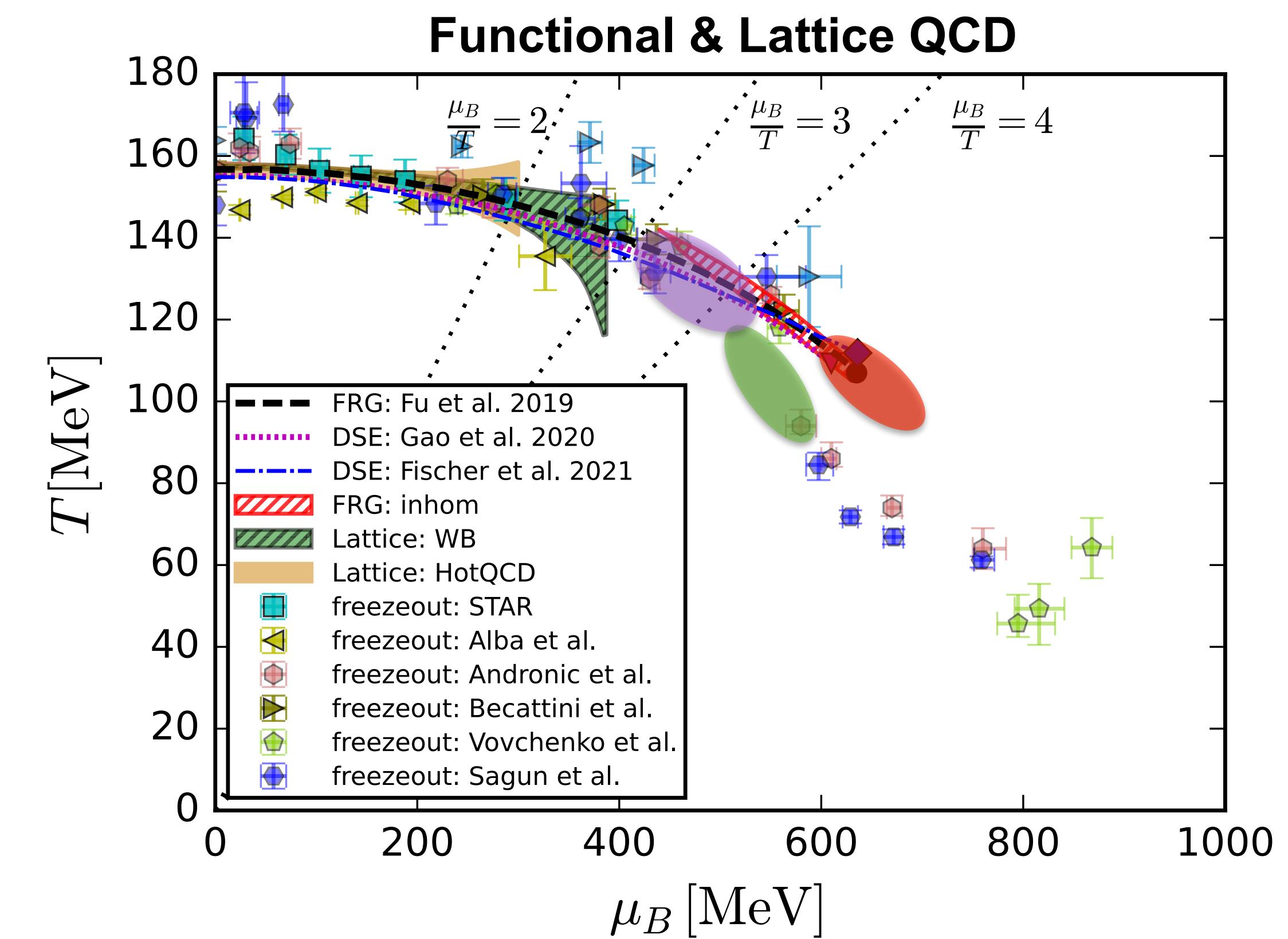
# Experimental & Theoretical Landscape

## Experimental landscape



## Onset of new physics (CEP)

## Theoretical landscape



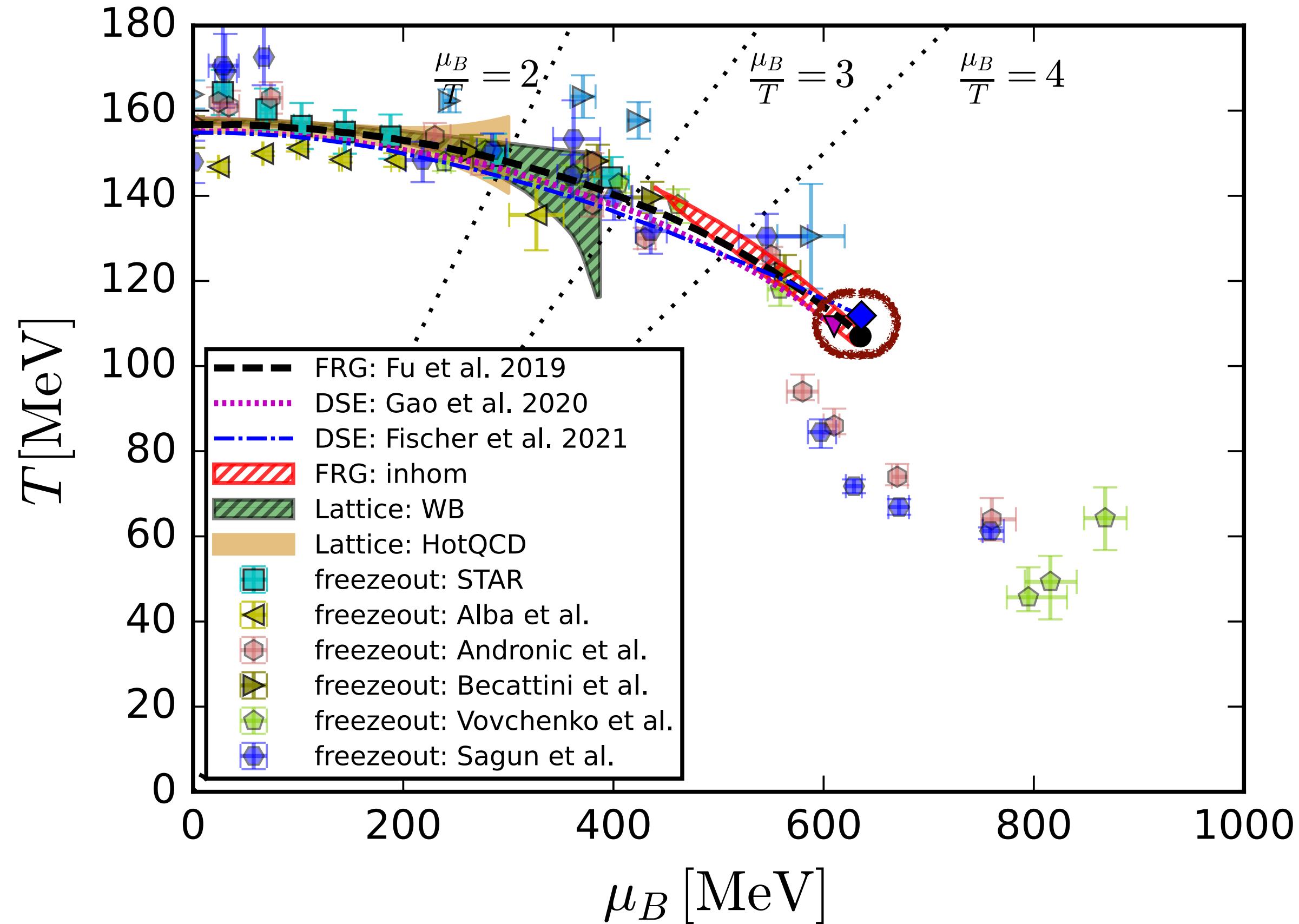
## Peak of kurtosis at the freeze-out line

Galatyuk, A982 (2019) update 2025; CBM, EPJA 53 3 (2017) 60

Fu, JMP, Rennecke, PRD 101 (2020) 054032

Gao, JMP, PLB 820 (2021) 136584

# Comprehensive QCD phase structure



**Functional QCD: CEP estimate**

**fRG:** **Fu, JMP, Rennecke, PRD 101 (2020) 054032**

**DSE:** **Gao, JMP, PLB 820 (2021) 136584**  
**Gunkel, Fischer, PRD 104 (2021) 054022**

$(\mu_B, T)_{\text{CEP}} \sim (600 - 650, 105 - 115) \text{ MeV}$

**Lattice:**

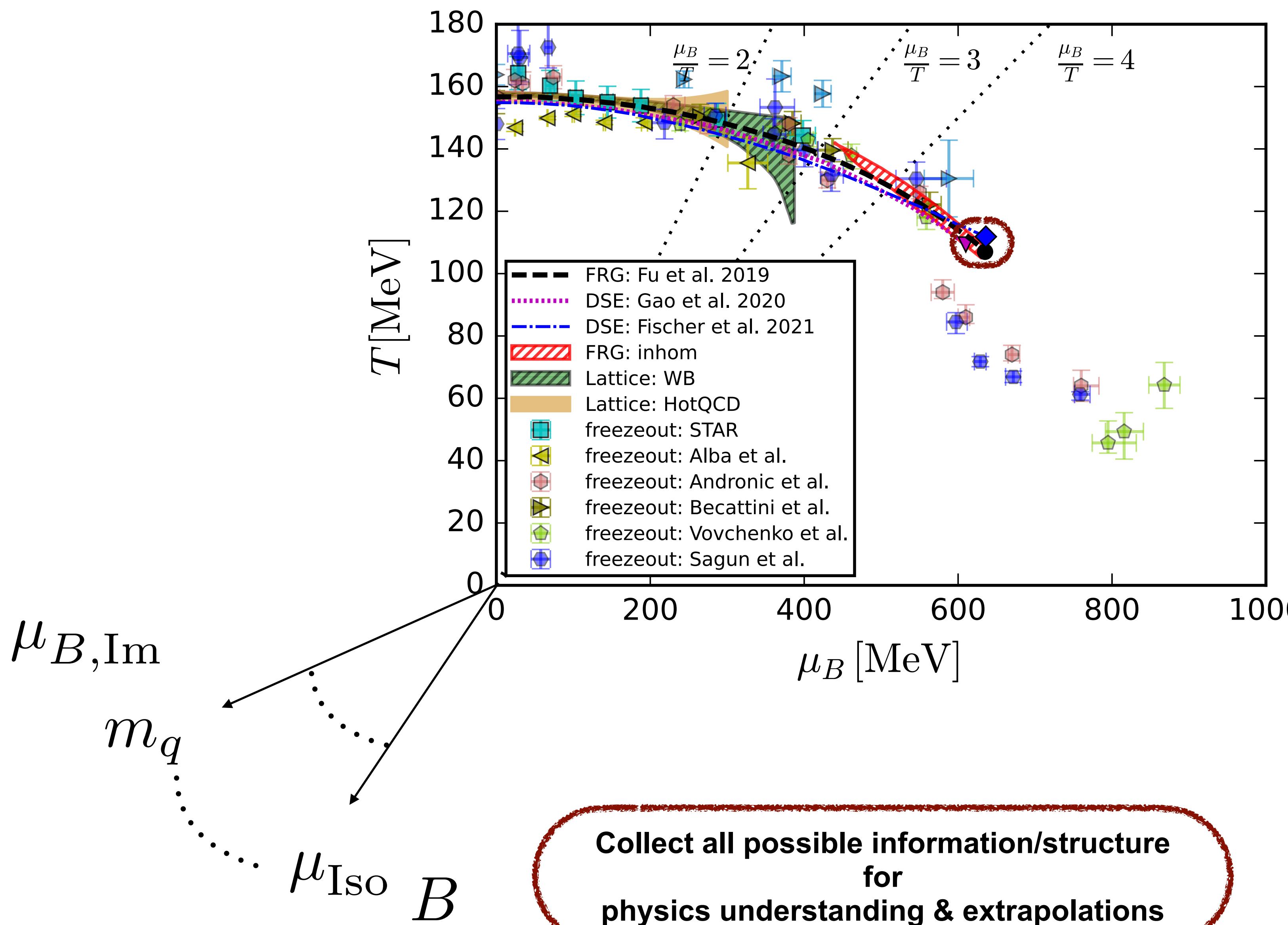
**HotQCD:**

**Bazavov, Ding, Hegde, Kaczmarek, Karsch, Karthik, Laermann, Lahiri, Larsen, Li, Mukherjee, Ohno, Petreczky, Sandmeyer, Schmidt, Sharma, Steinbrecher, PLB 795 (2019)**

**WB:**

**Borsányi, Fodor, Guenther, Kara, Katz, Parotto, Pasztor, Ratti, Szabo, PRL 125 (2020) 052001**

# Comprehensive QCD phase structure



Functional QCD: CEP estimate

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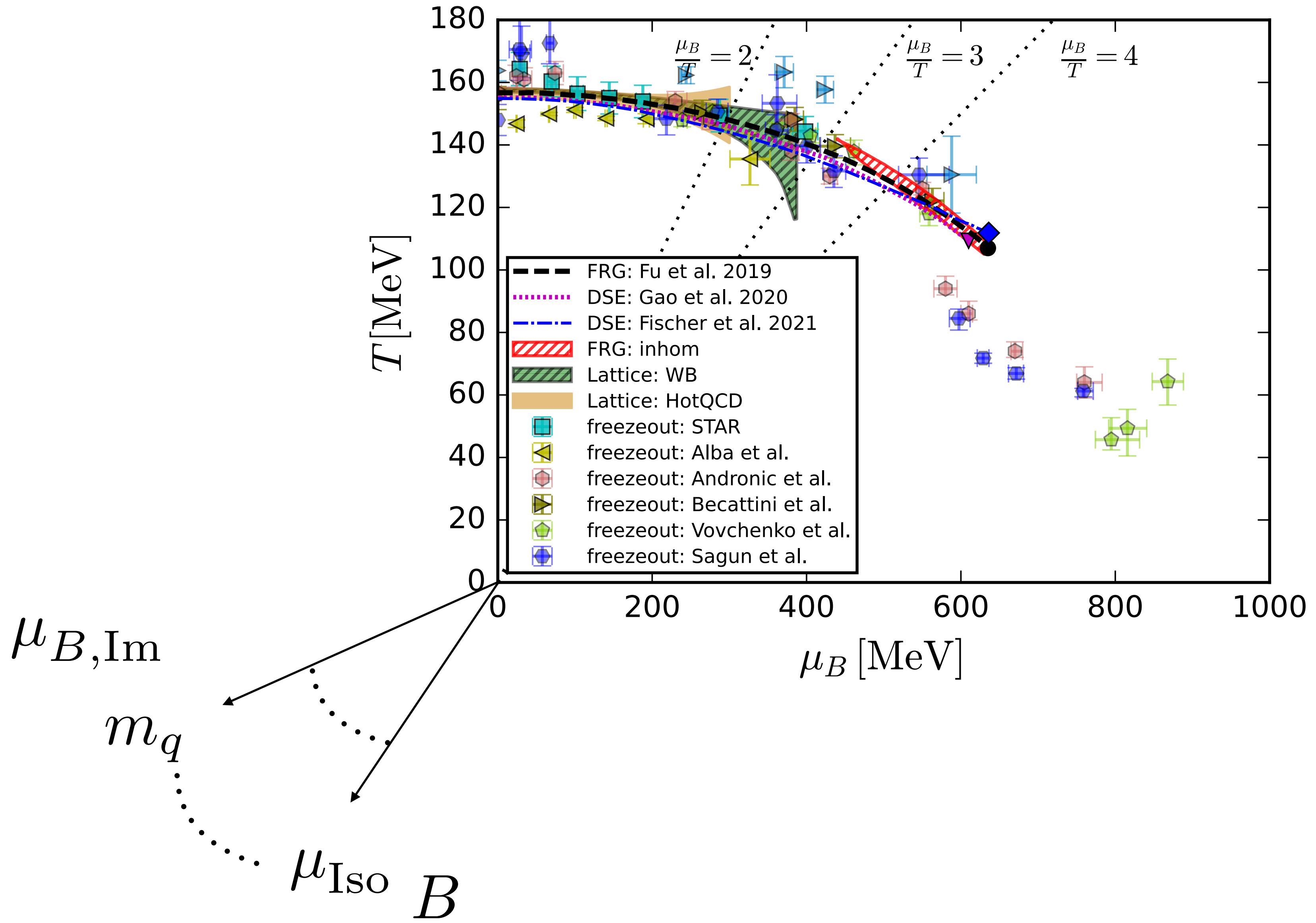
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WB:

Borsányi, Fodor, Guenther, Kara, Katz, Parotto, Pasztor, Ratti, Szabo, PRL 125 (2020) 052001

# Comprehensive QCD phase structure



- What bases work

- Extrapolation limits

:



# Direct computations and the minimal point of view

Those are my interpretations,  
and if you don't like them...  
well, I have others

- Self-consistent truncations to functional relations define analytic functions in  $\mu_B$ , eg:

$$\partial_t \left\langle q(x)\bar{q}(y) \right\rangle(\underline{\mu_B}) = \text{Loop} \left[ \left\langle q(x)\bar{q}(y) \right\rangle(\underline{\mu_B}), \left\langle q(x)A_\mu(y)\bar{q}(z) \right\rangle(\underline{\mu_B}), \dots; \underline{\mu_B} \right]$$

Yang-Lee: see talk of Fei Gao

Extrapolations: See talk of Shi Yin

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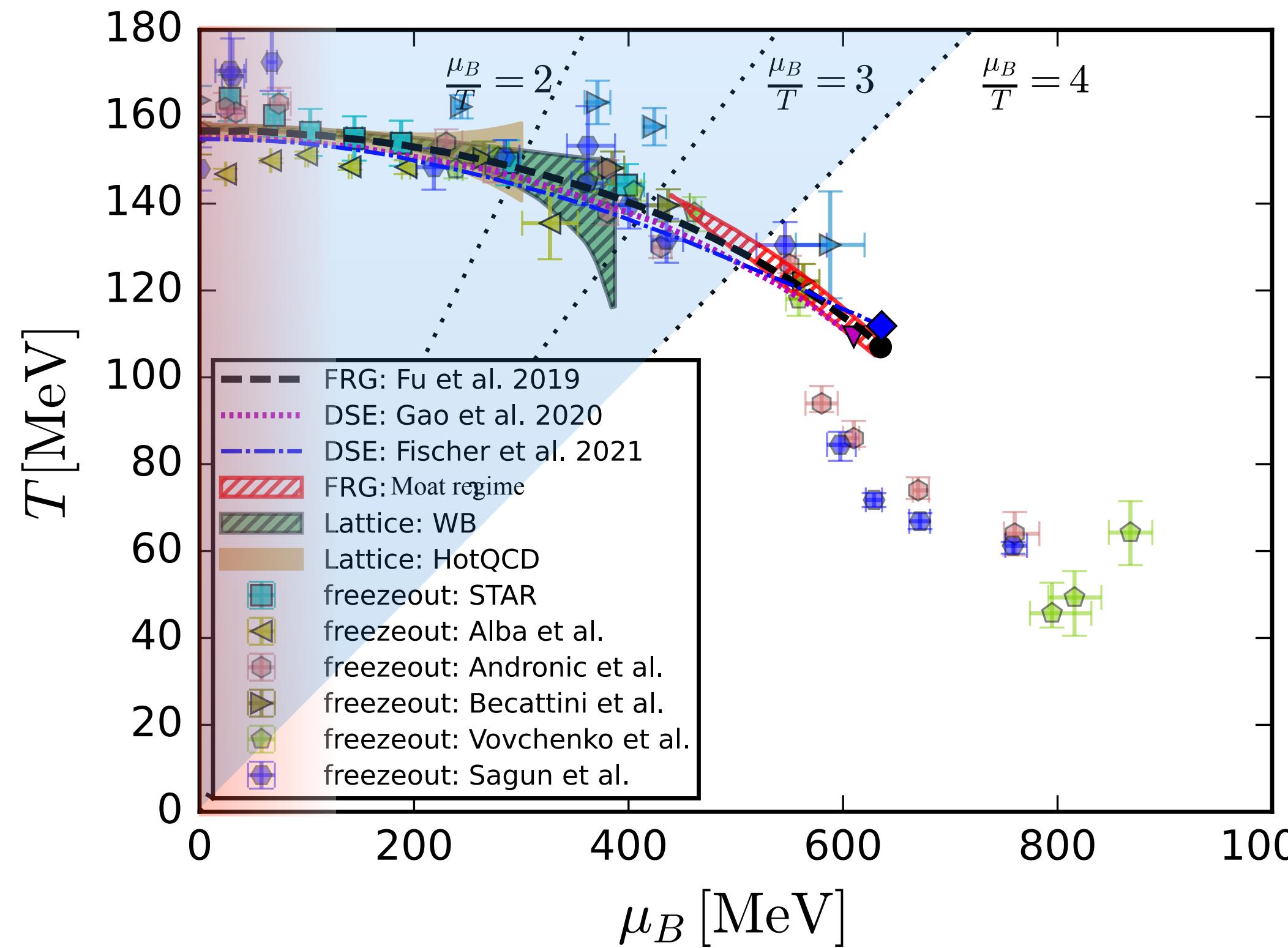
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Yang-Lee: see talk of Fei Gao

- Consequences for functional QCD predictions at finite density

Extrapolations: See talk of Shi Yin



By now the best truncations to functional QCD pass lattice benchmark tests at vanishing and small chemical potential

Regime of quantitative reliability of current best truncation

Unique: QCD-based analytic continuations that satisfy the lattice benchmarks at small chemical potential.

# QCD phase structure at finite density: Facts & Fiction

## Facts

$$\mu_B = 0$$

- Chiral crossover at about

$$T_\chi \approx 155 \text{ MeV}$$

- Strongly correlated phase for temperatures

$$T_\chi \lesssim T \lesssim 2T_\chi$$

$$\mu_B \neq 0$$

- No chiral critical end point for

$$\mu_B \lesssim 600 \text{ MeV}$$

- No chiral crossover for

$$\mu_B \gtrsim 700 \text{ MeV}$$

## Fiction

- Physical QCD is in the chiral scaling regime

Chiral scaling regimes are very small  $m_\pi \lesssim 10 \text{ MeV}$

Soft modes are commonplace

- Confinement crossover is at XXX

$$T_\chi \lesssim T_{\text{conf}} \lesssim 2T_\chi$$

- There is a CEP

Onset of new phases  $600 \text{ MeV} \lesssim \mu_B^{\text{onset}} \lesssim 700 \text{ MeV}$

- Scaling regime (Ising) of the CEP is humongous

No, it is not! Most likely: too small to be measured

# QCD phase structure at finite density: Facts & Fiction

## Facts

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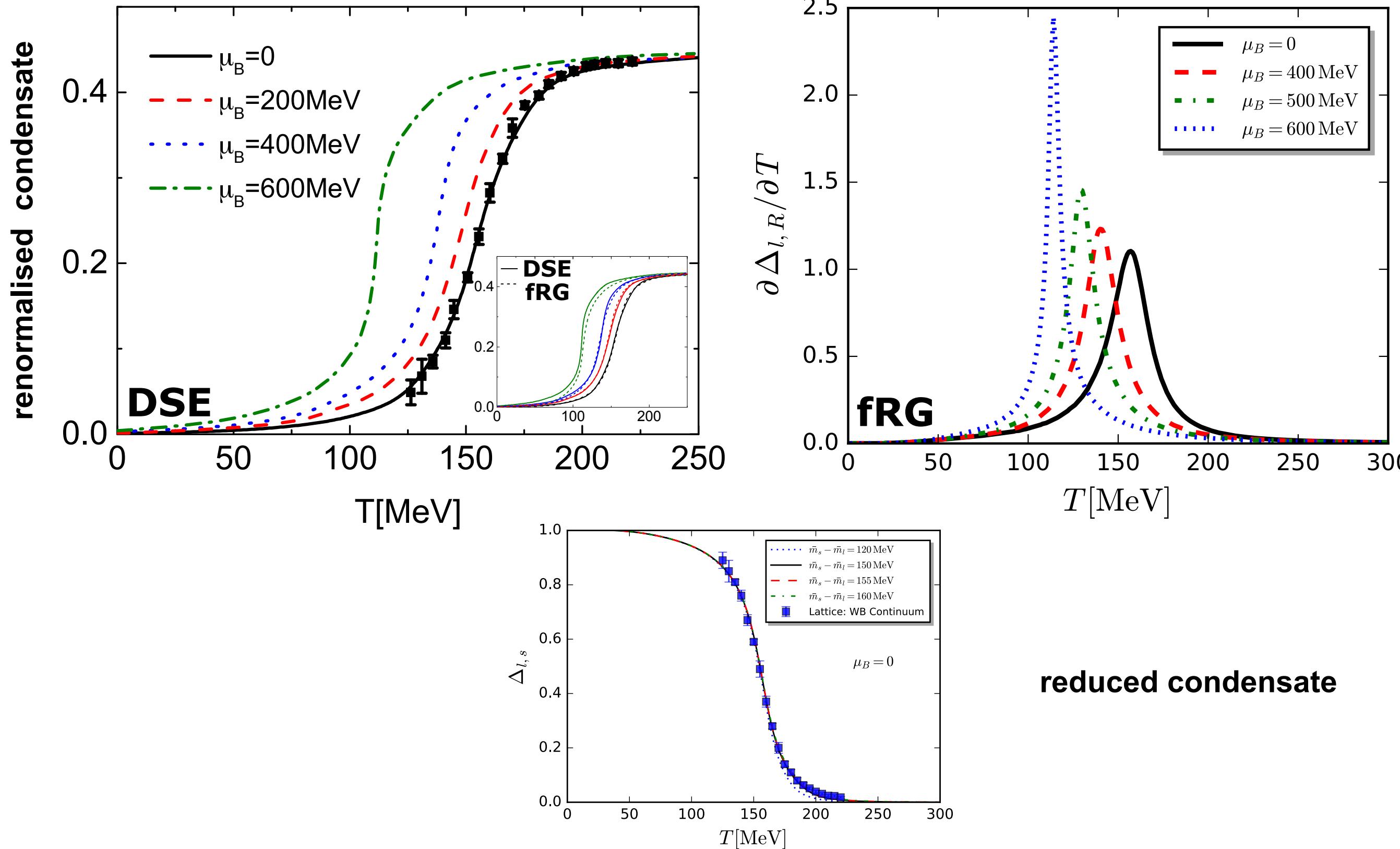
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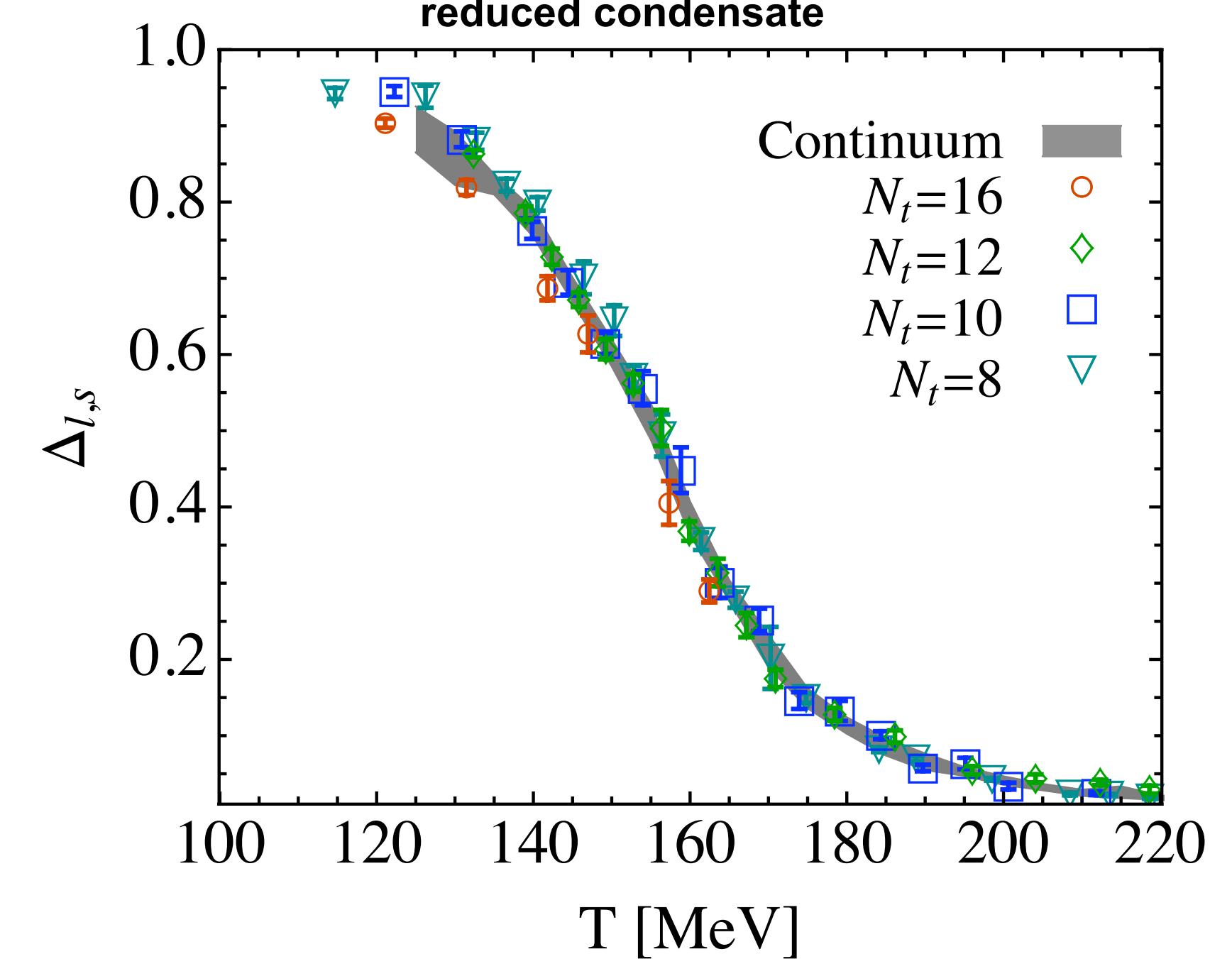
# QCD phase structure at finite density: Facts & Fiction

Chiral crossover at about  $T_\chi \approx 155$  MeV

## Functional QCD



## Lattice QCD



**DSE:** Fischer, Luecker, Welzbacher, PRD 90 (2014) 034022

Gao, JMP, PLB 820 (2021) 136584

Gunkel, Fischer, PRD 104 (2021) 054022

**fRG:** Fu, JMP, Rennecke, PRD 101 (2020) 054032

Borsányi, Fodor, Hoelbling, Katz, Krieg, Ratti, Szabo, JHEP 09, 073 (2010)

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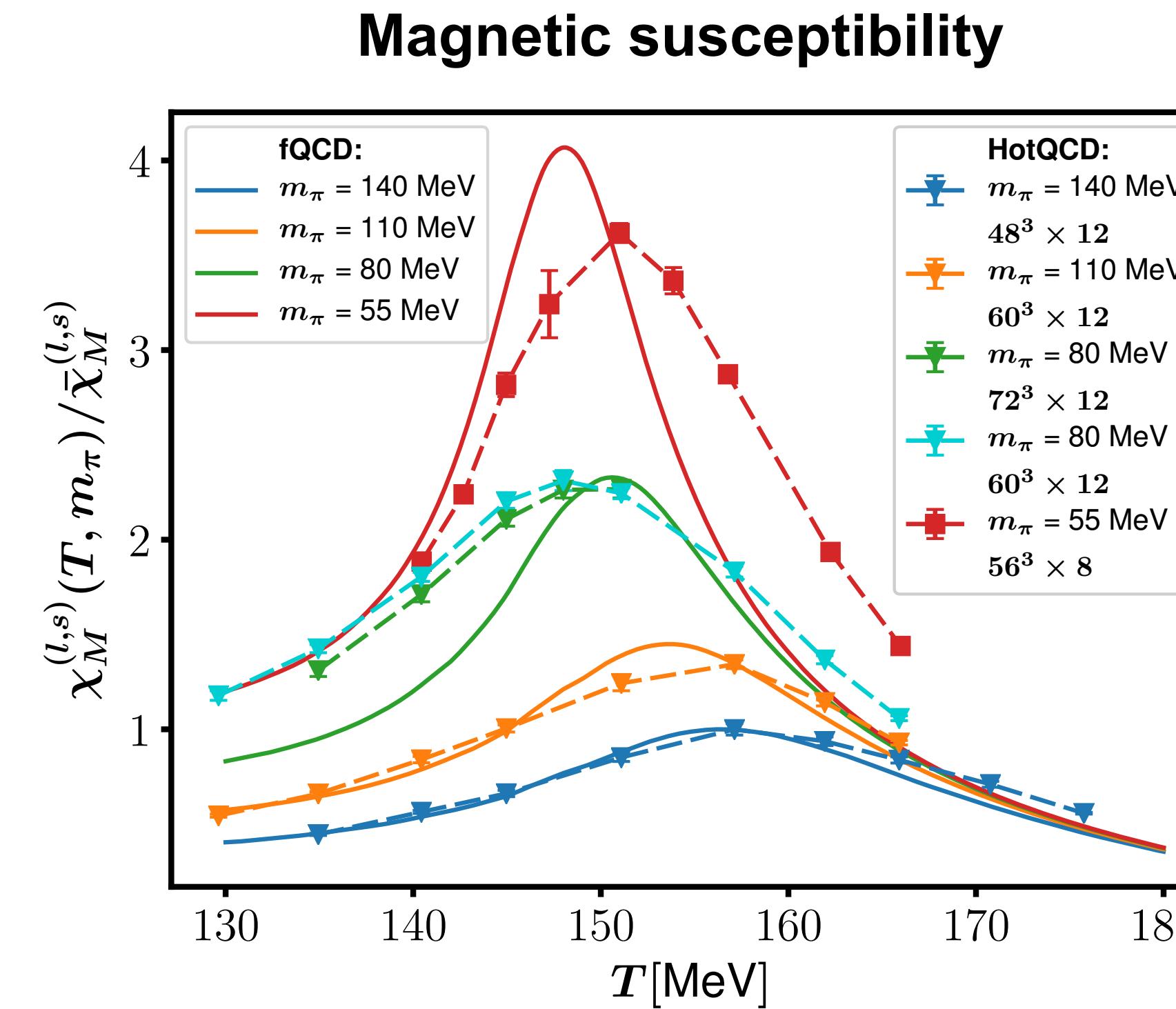
Soft modes are commonplace

# QCD phase structure at finite density: Facts & Fiction

Scaling regime of QCD for  $m_\pi \lesssim 10$  MeV

Functional QCD

Lattice QCD



Gao, JMP, PRD 105 (2022) 094020

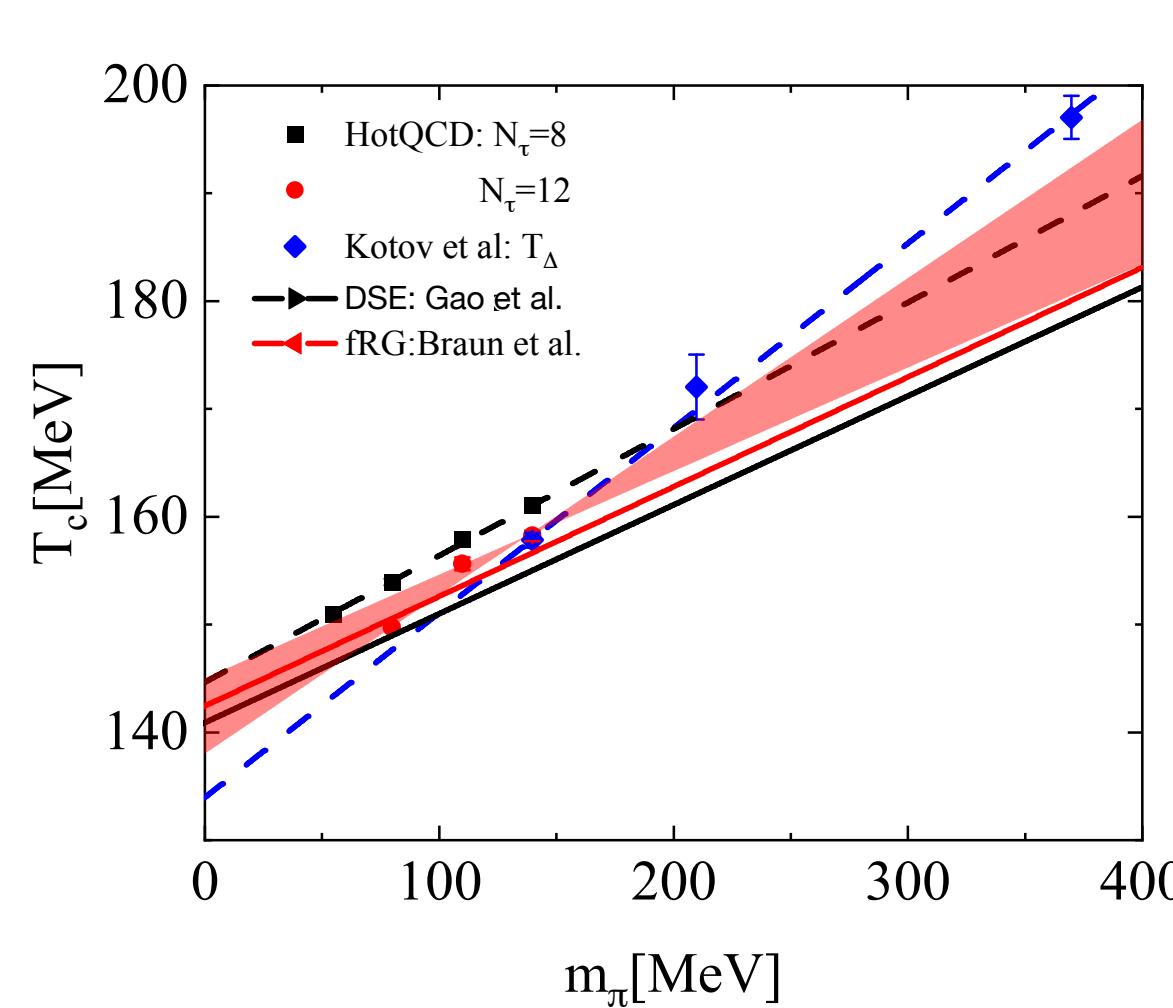
Braun, Chen, Fu, Gao, Huang, Ihssen, JMP, Rennecke,

Sattler, Tan, Wen, Yin, PRD 111 (2025) 094010

Columbia plot: Bernhardt, Fischer, 2507.21680

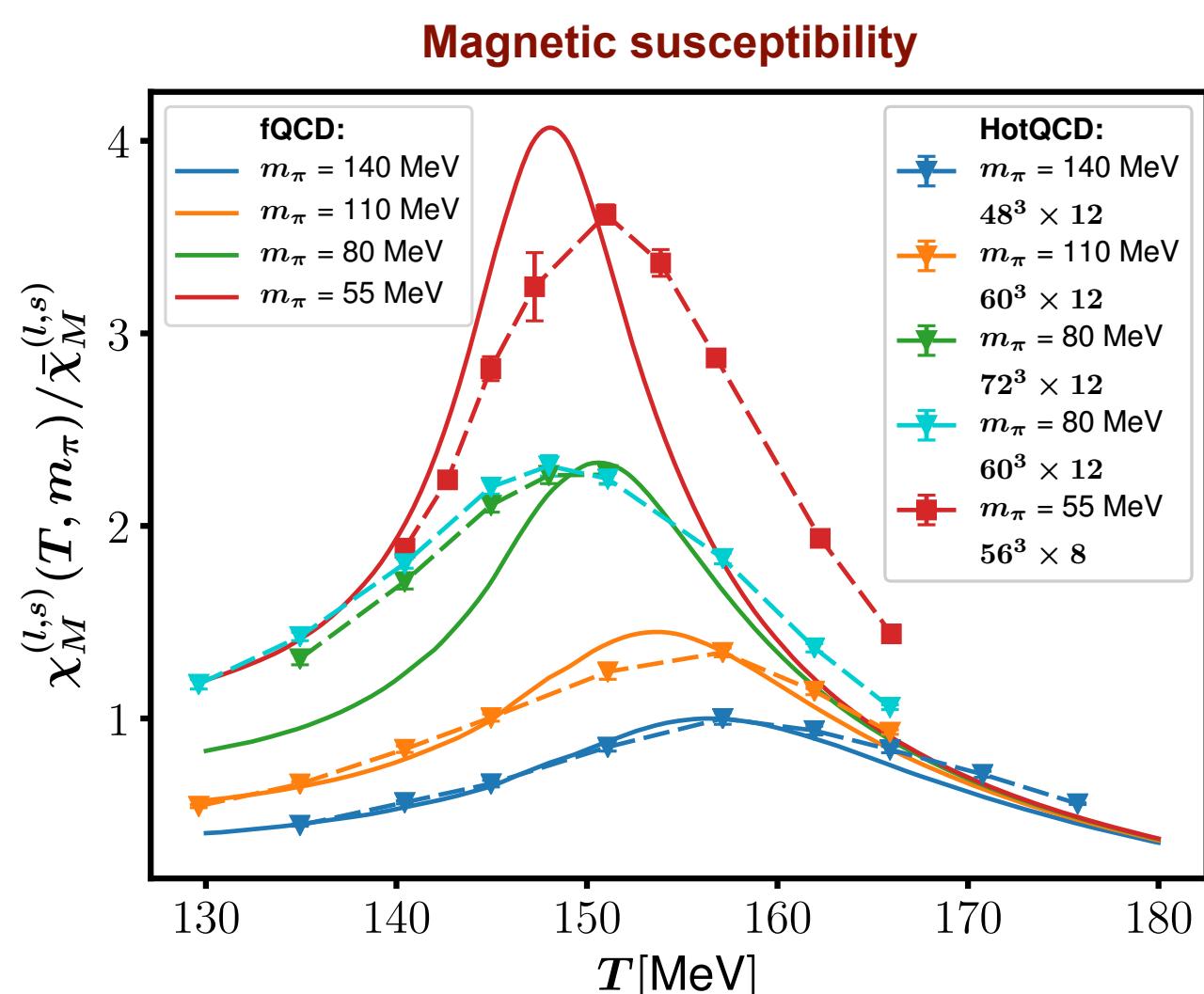
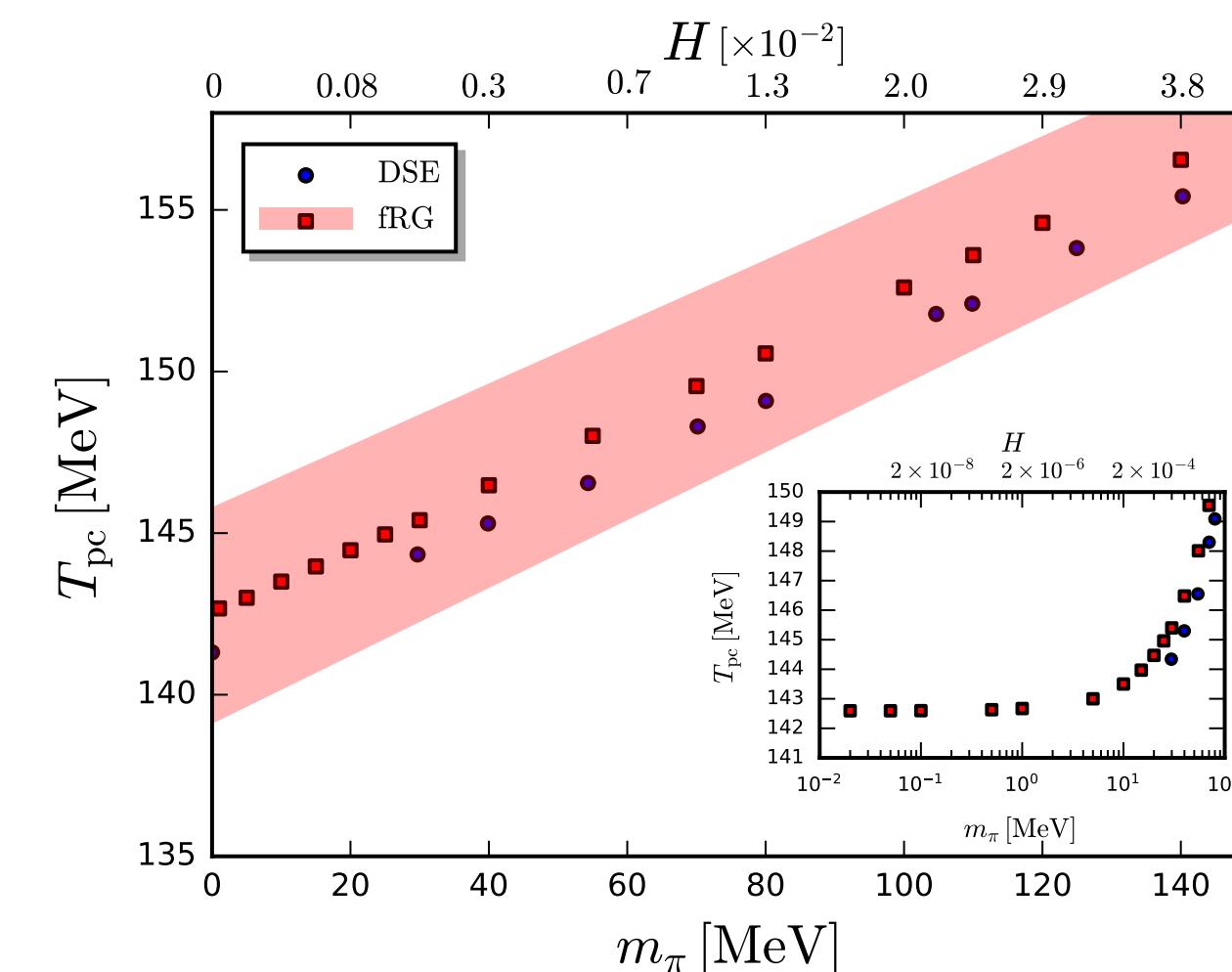
Ding, Hegde, Kaczmarek, Karsch, Lahiri, Li, Mukherjee, Ohno,  
Petreczky Schmidt, Steinbrecher, PRL 123 (2019) 062002

# To be (critical) or not (to be)



Chiral transition temperature

$$H = \frac{m_l}{m_s}$$

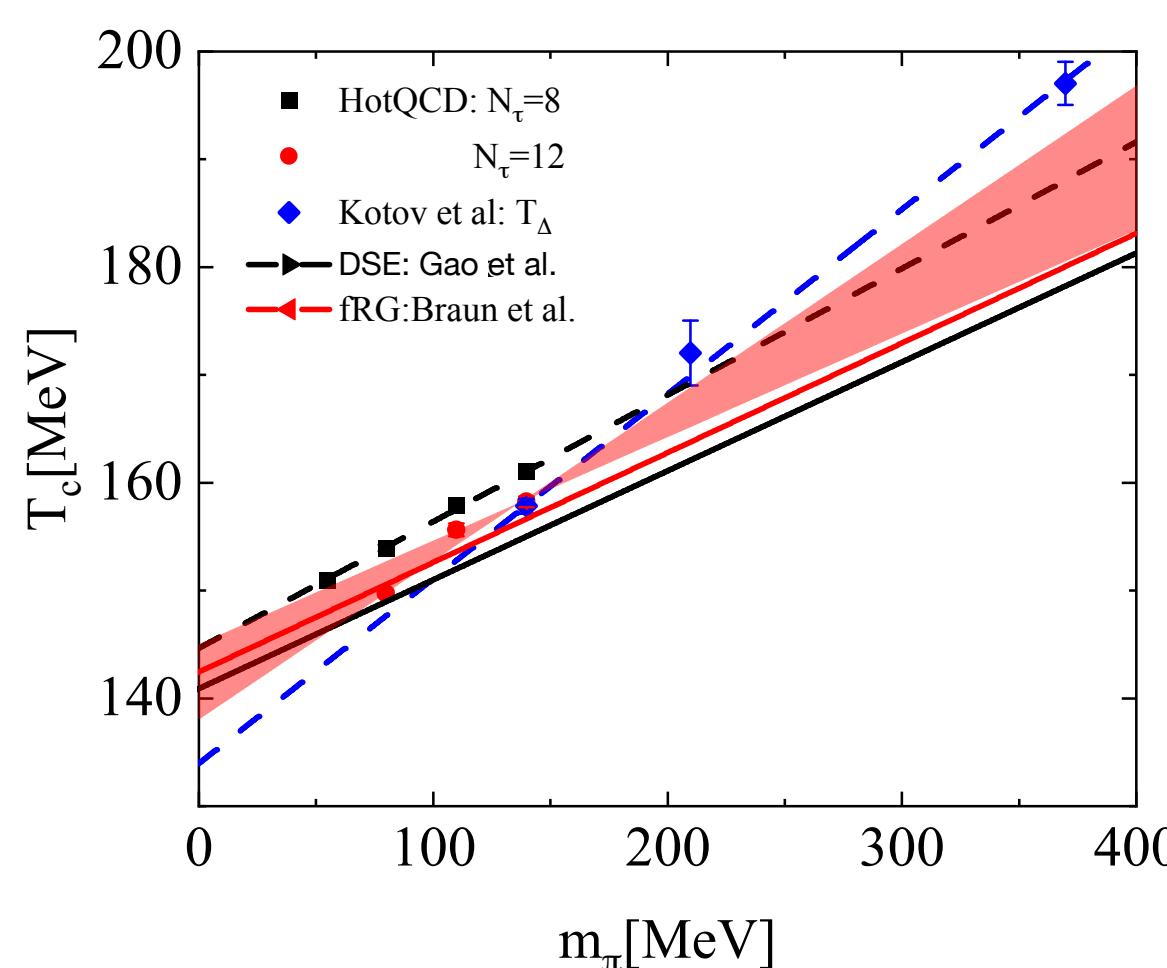


Braun, Fu, JMP, Rennecke, Rosenblüh, Yin, PRD 102 (2020) 056010

Gao, JMP, PRD 105 (2022) 094020

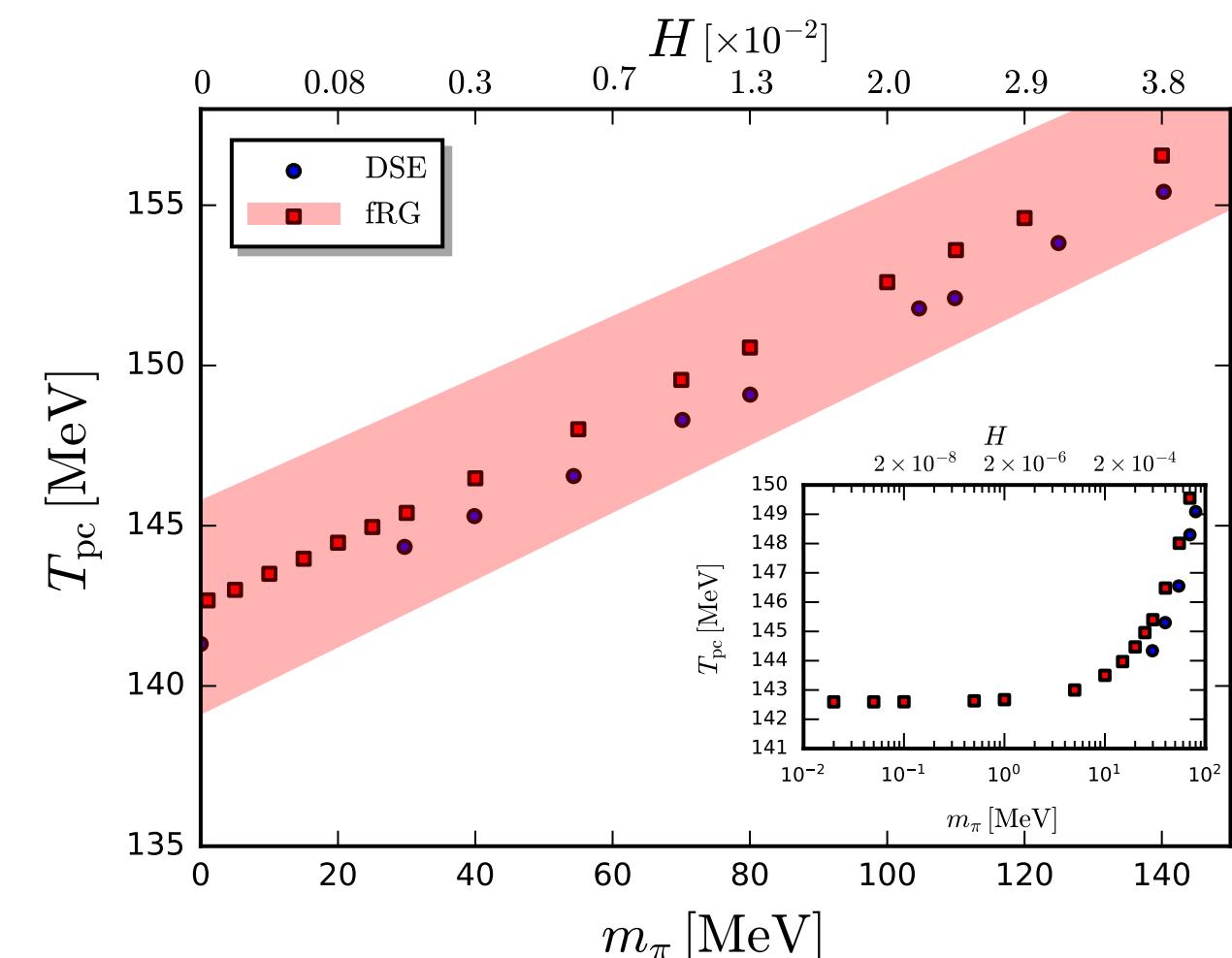
Braun, Chen, Fu, Gao, Huang, Ihssen, JMP, Rennecke, Sattler, Tan, Wen, Yin, PRD 111 (2025) 094010

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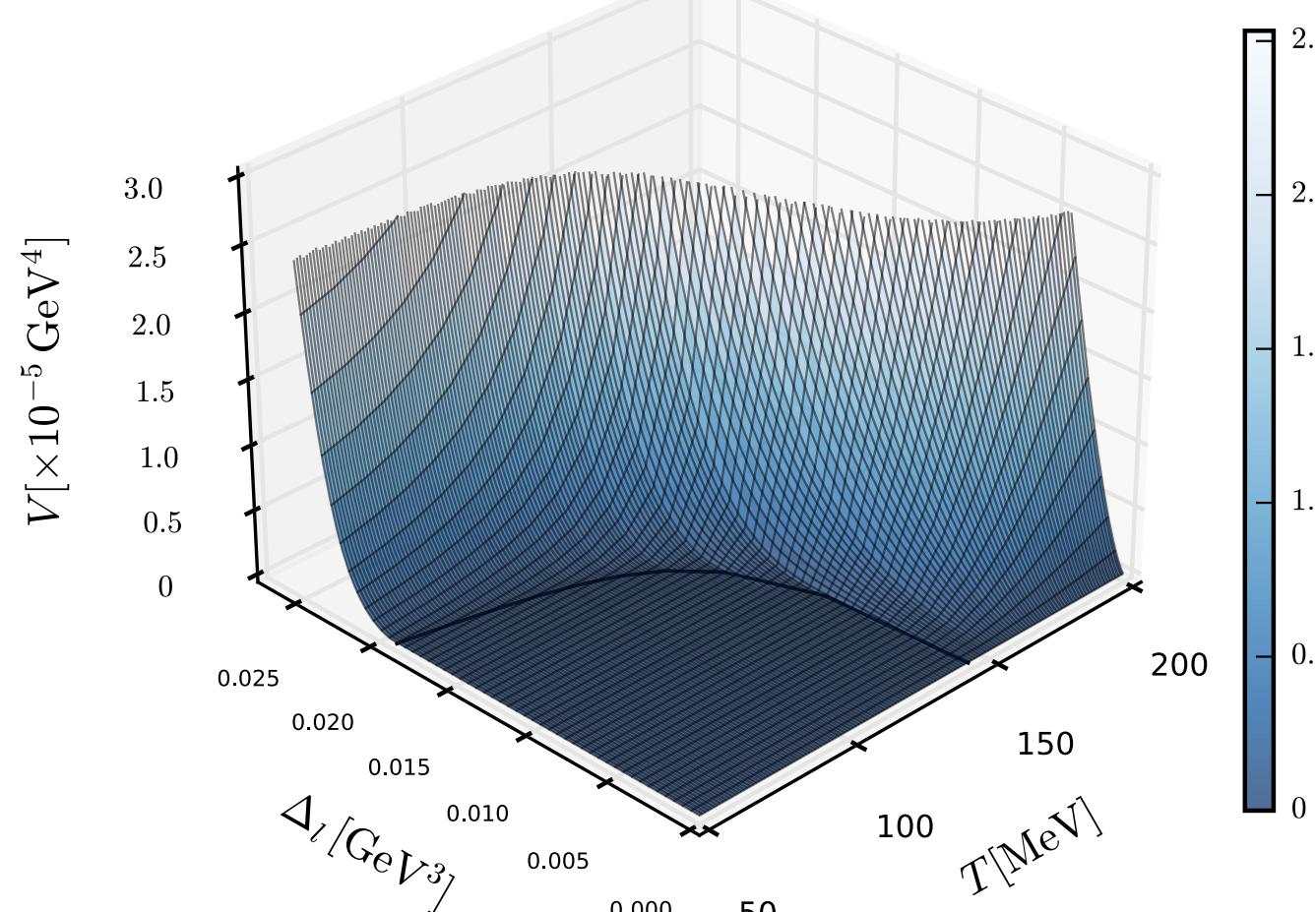
$$H = \frac{m_l}{m_s}$$



Order parameter potential & scaling

$$V_\chi \approx \Delta_l^n \quad \longleftrightarrow \quad \Delta_l(H) \propto H^{\frac{1}{n-1}}$$

$$(\text{Critical}) \text{ exponent: } \frac{1}{\delta} = \frac{1}{n-1}$$



$$V_\chi^{(\text{fRG})} \approx V_\chi^{(\text{DSE})}$$

Braun, Fu, JMP, Rennecke, Rosenblüh, Yin, PRD 102 (2020) 056010

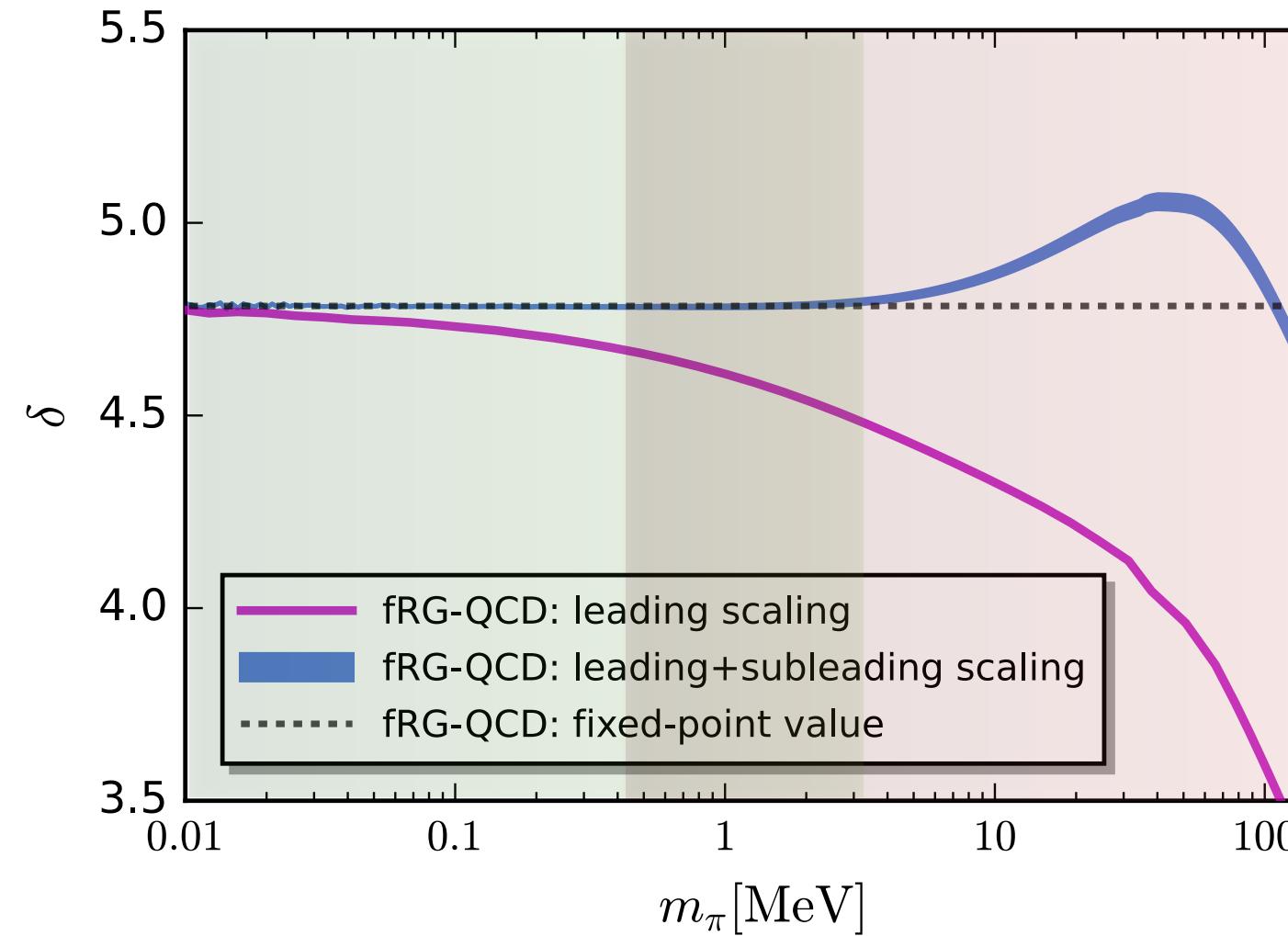
Gao, JMP, PRD 105 (2022) 094020

Braun, Chen, Fu, Gao, Huang, Ihssen, JMP, Rennecke, Sattler, Tan, Wen, Yin, PRD 111 (2025) 094010

# Chiral dynamics & quasi-massless modes

Scaling coefficient as function of the pion mass

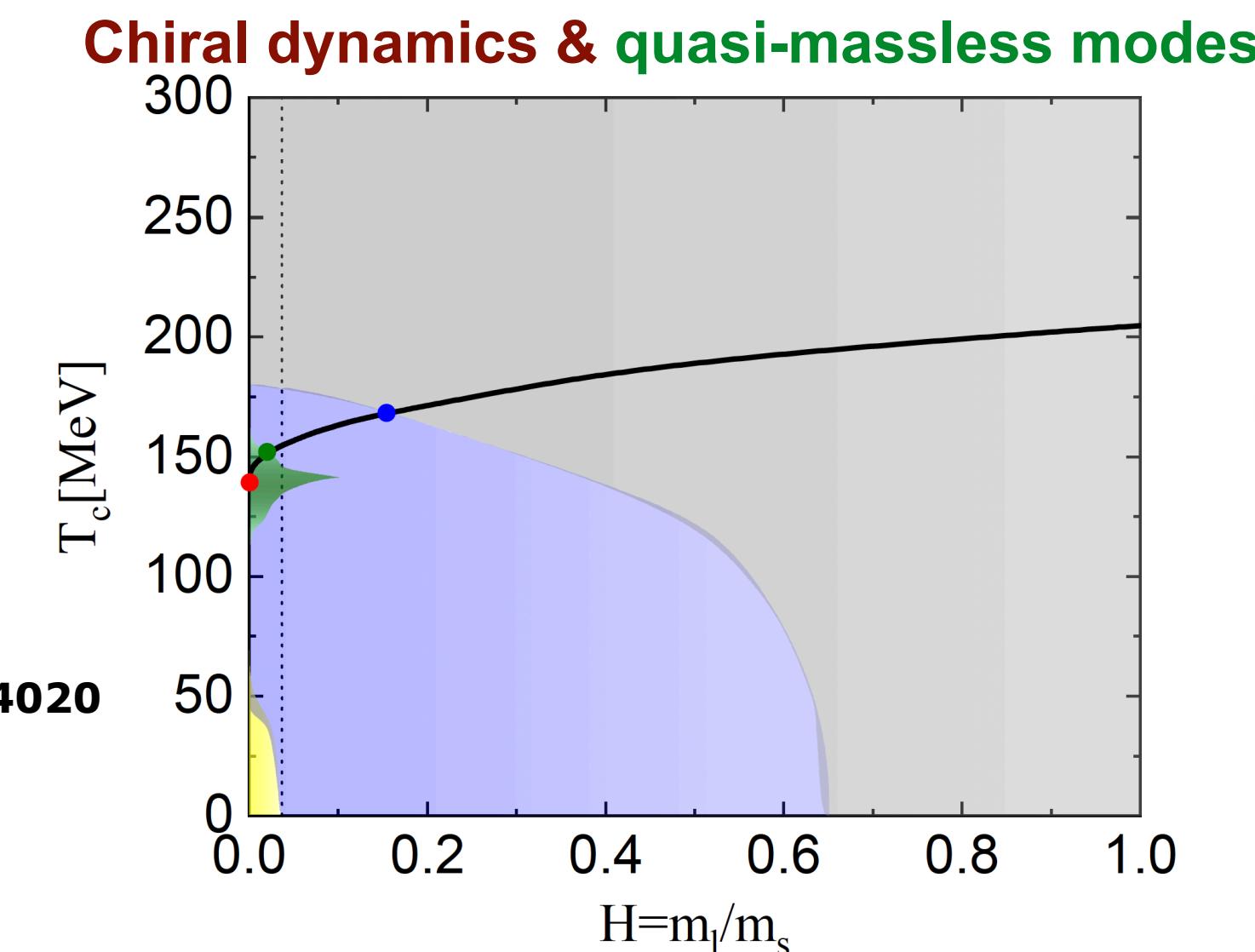
Critical O(4) scaling



Trivial  $\Delta_l^{1+\delta}$  scaling

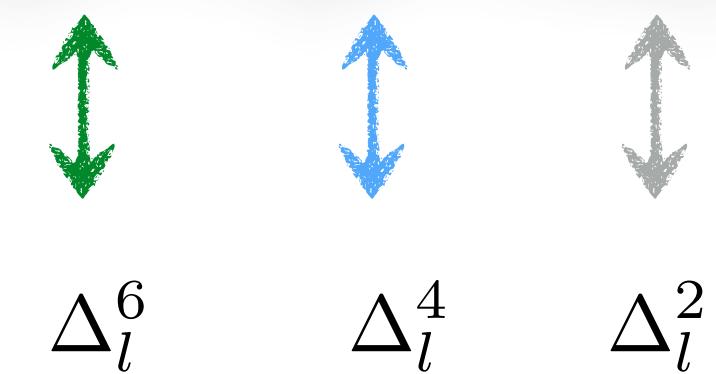
Critical scaling

Gao, JMP, PRD 105 (2022) 094020



Far away from the critical regime for  $m_\pi \gtrsim 1$  MeV

$$\Delta_l(T, H) \approx \Delta_{l,\chi}(0) \left( c_0 + c_{\frac{1}{5}} H^{\frac{1}{5}} + c_{\frac{1}{3}} H^{\frac{1}{3}} + c_1 H \right)$$

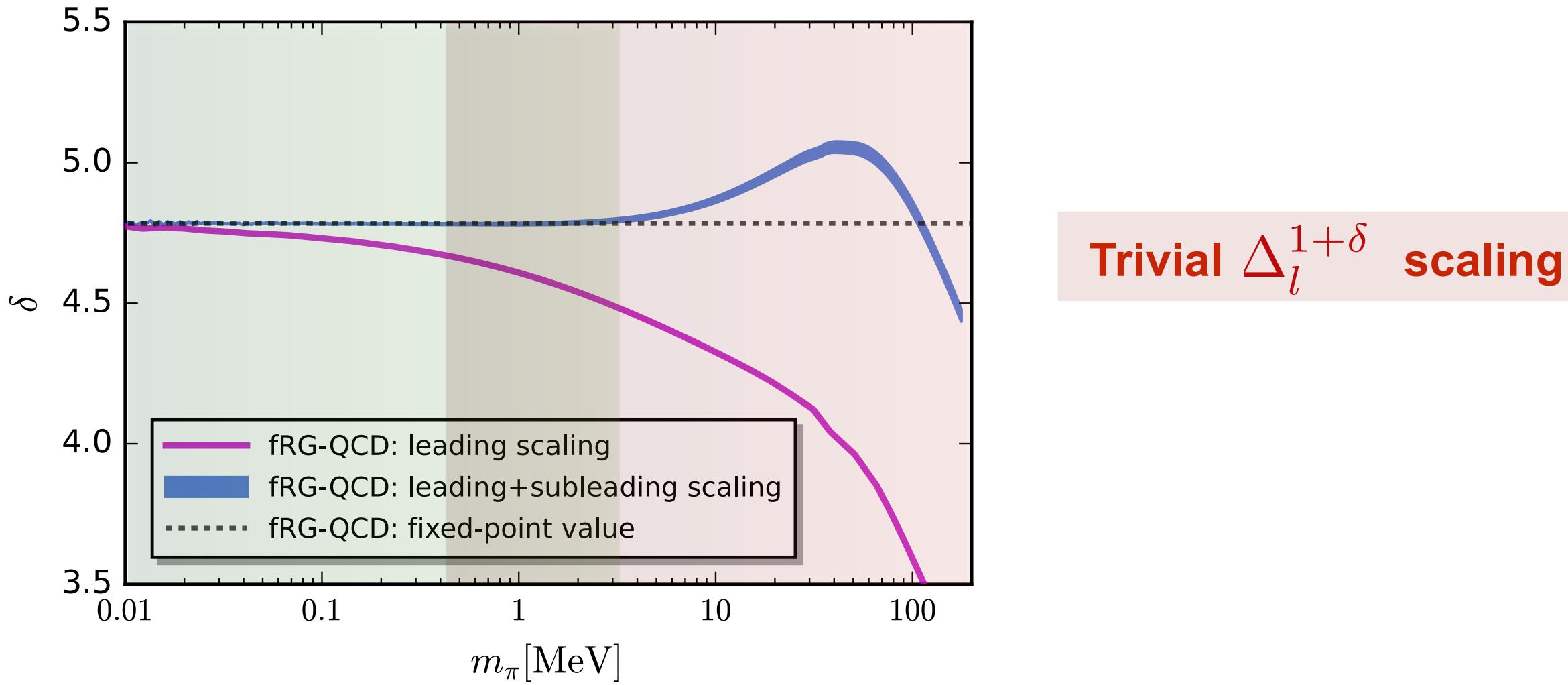


$$V_\chi(\Delta_l) \propto$$

# Chiral dynamics & quasi-massless modes

$$\Delta_l(m_\pi) \propto m_\pi^{2/\delta} [1 + a_m m_\pi^{2\theta_H} + \dots]$$

Scaling coefficient as function of the pion mass

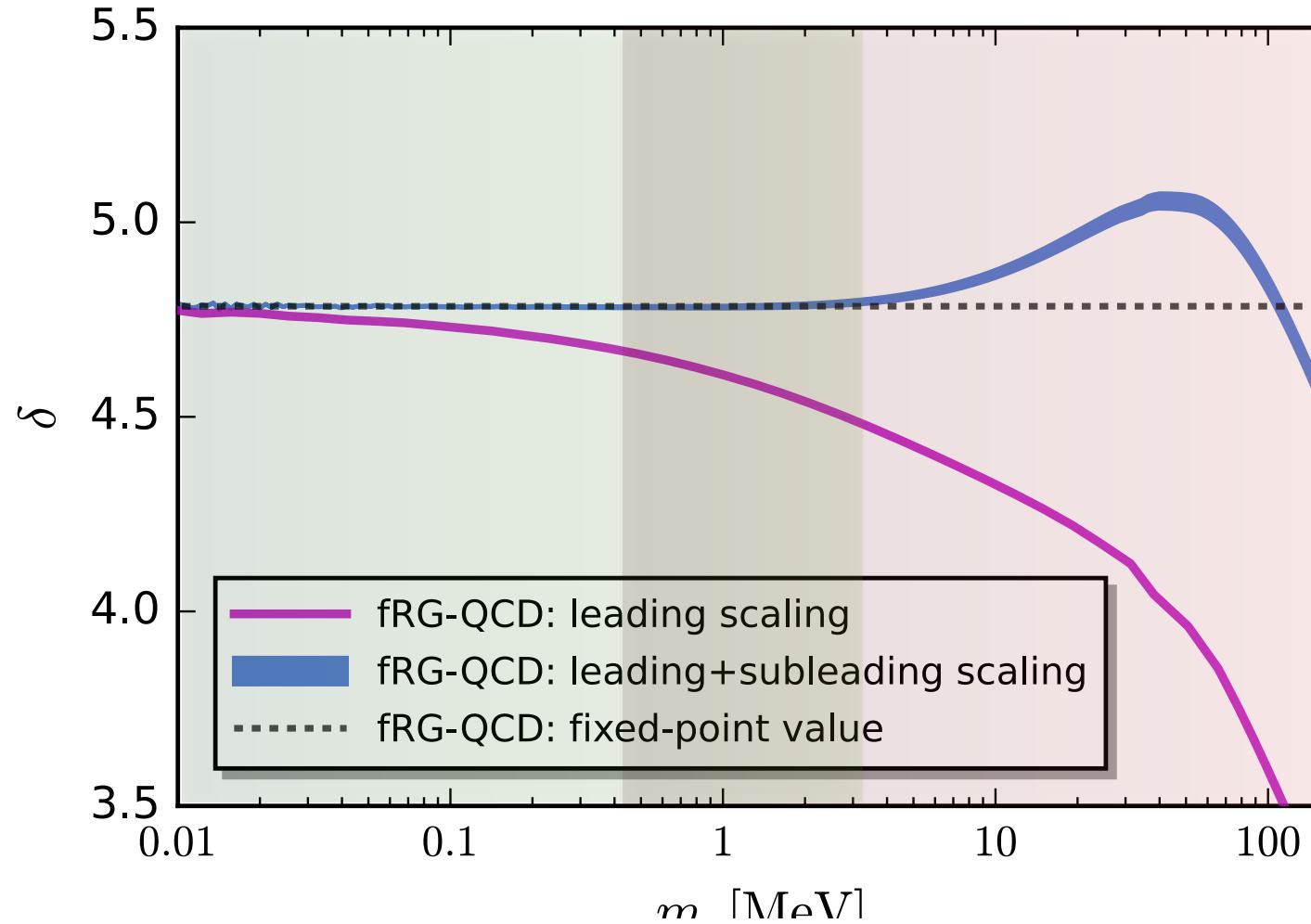


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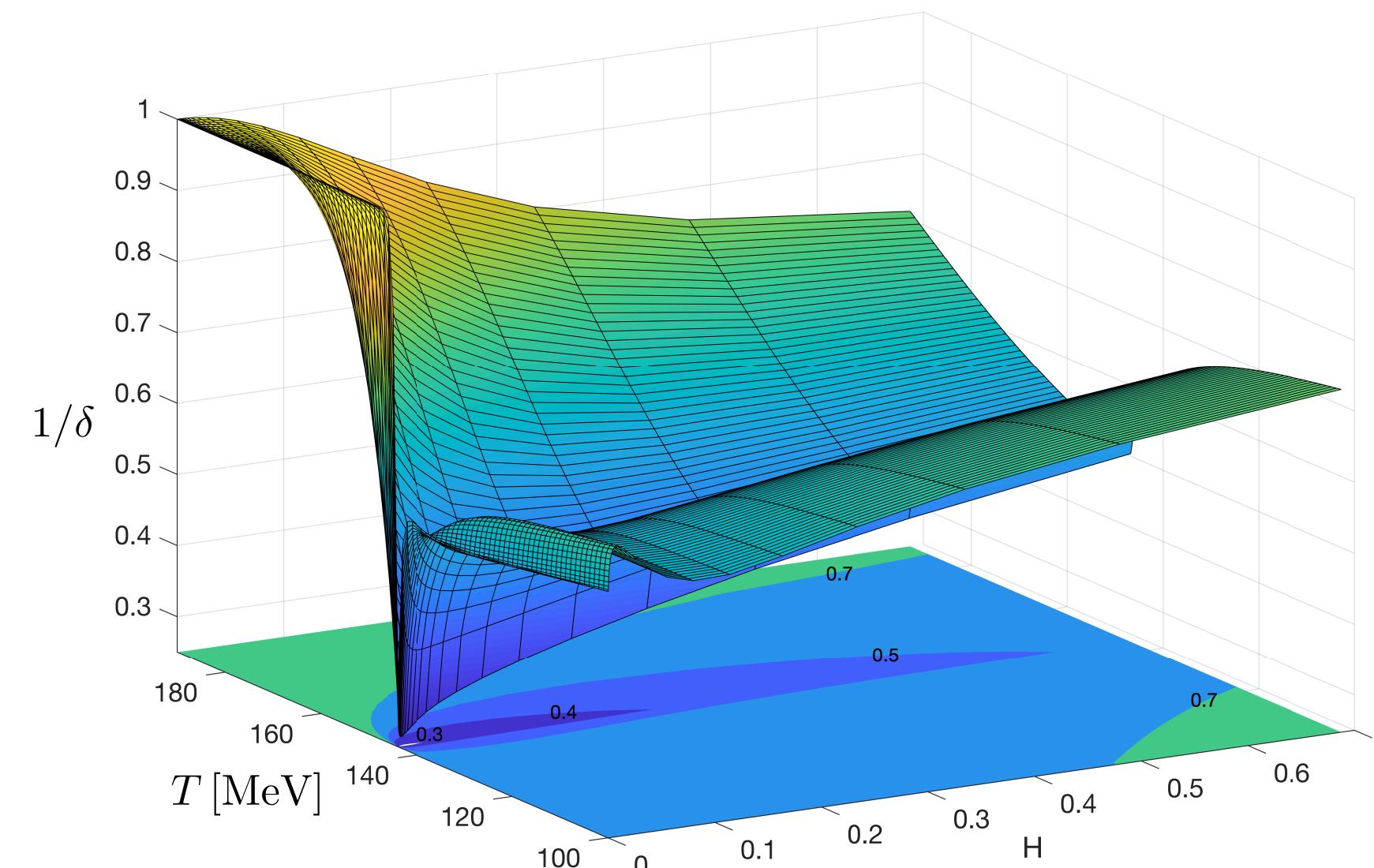
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Small chiral scaling regime

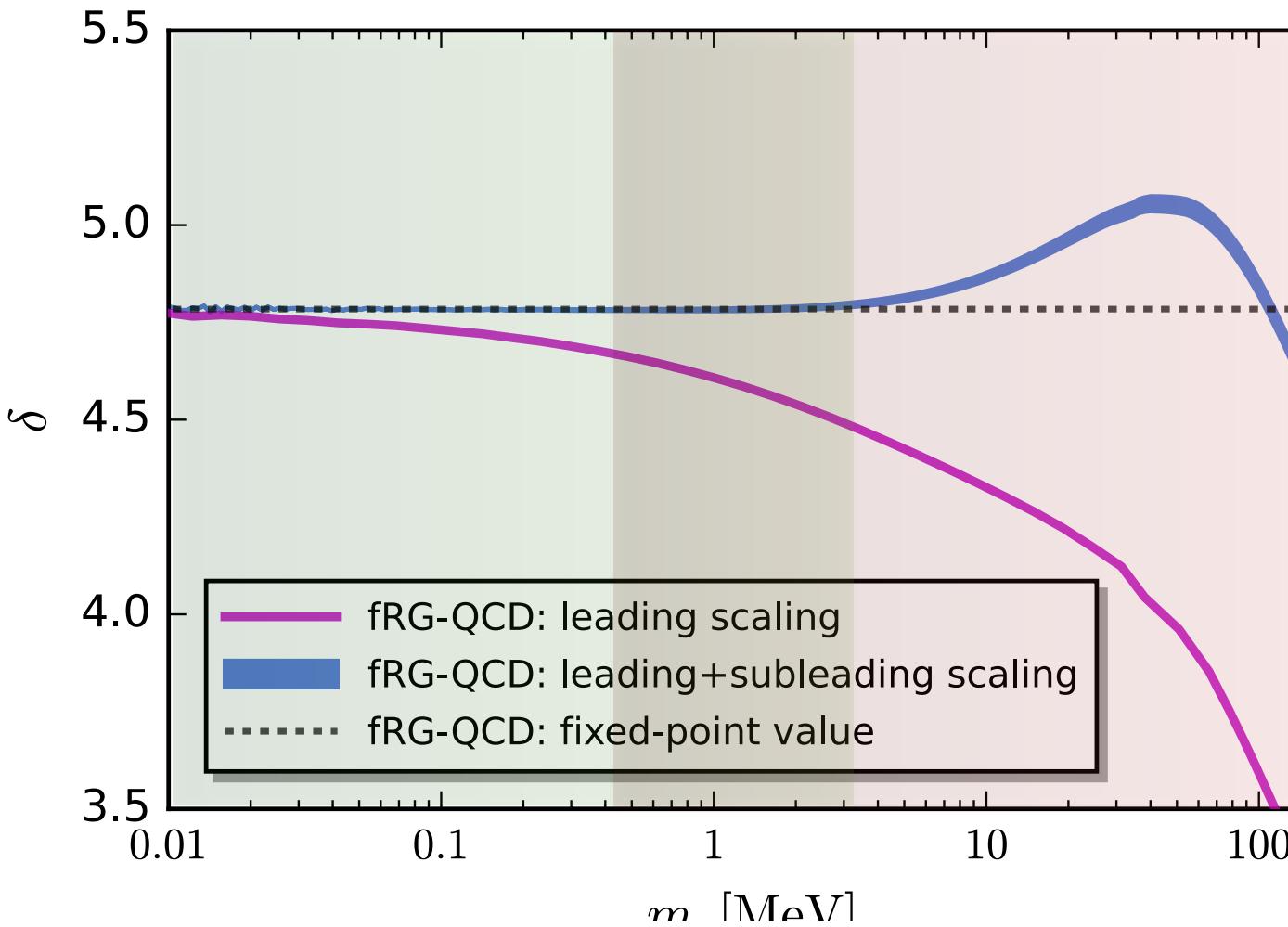


Small critical regime around pot. CEP

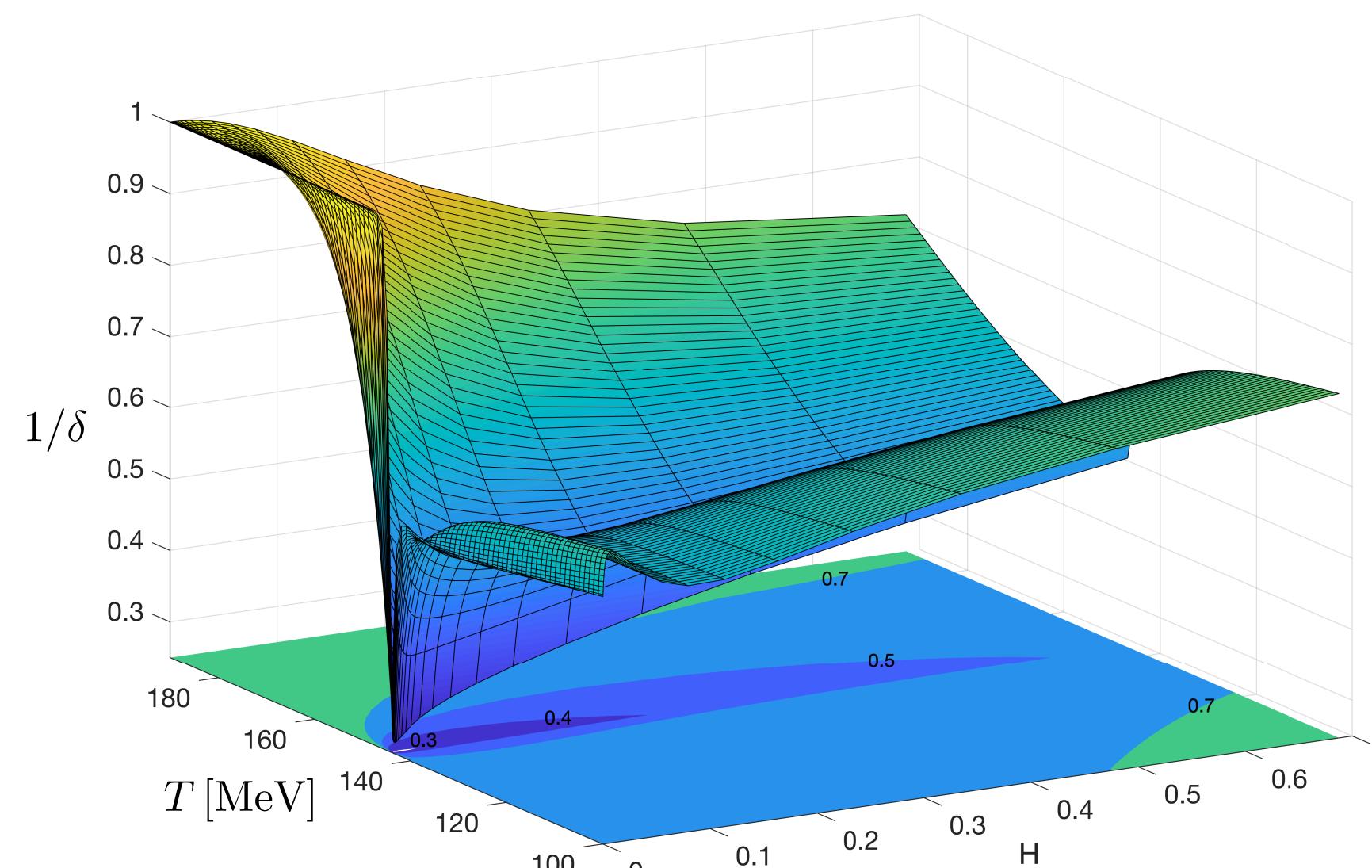
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Small critical regime around pot. CEP

!!Great News!!  
Location of CEP/New phase accessible via combination  
of precision measurements & computations

# QCD phase structure at finite density: Facts & Fiction

## Facts

- Chiral crossover at about

$$T_\chi \approx 155 \text{ MeV}$$

- Strongly correlated phase for temperatures

$$T_\chi \lesssim T \lesssim 2 T_\chi$$

---

$$\mu_B = 0$$

---

- Physical QCD is in the chiral scaling regime

Chiral scaling regimes are very small  $m_\pi \lesssim 10 \text{ MeV}$

Soft modes are commonplace

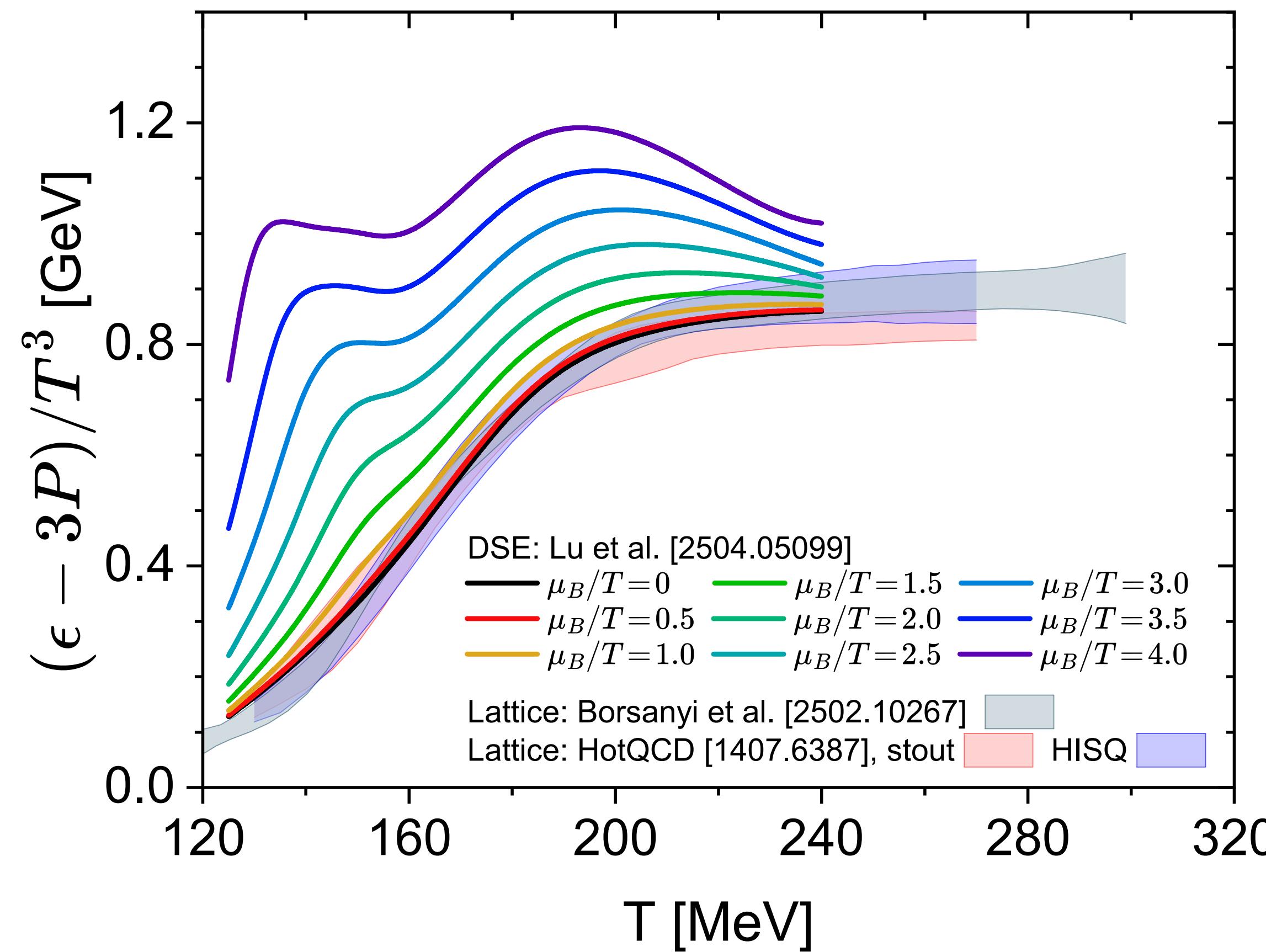
## Fiction

# QCD phase structure at finite density: Facts & Fiction

Strongly correlated phase for temperatures  $T_\chi \lesssim T \lesssim 2T_\chi$

Functional QCD

Lattice QCD



# QCD phase structure at finite density: Facts & Fiction

Spin symmetry for  $T_\chi \lesssim T \lesssim 2T_\chi$

Functional QCD

not yet

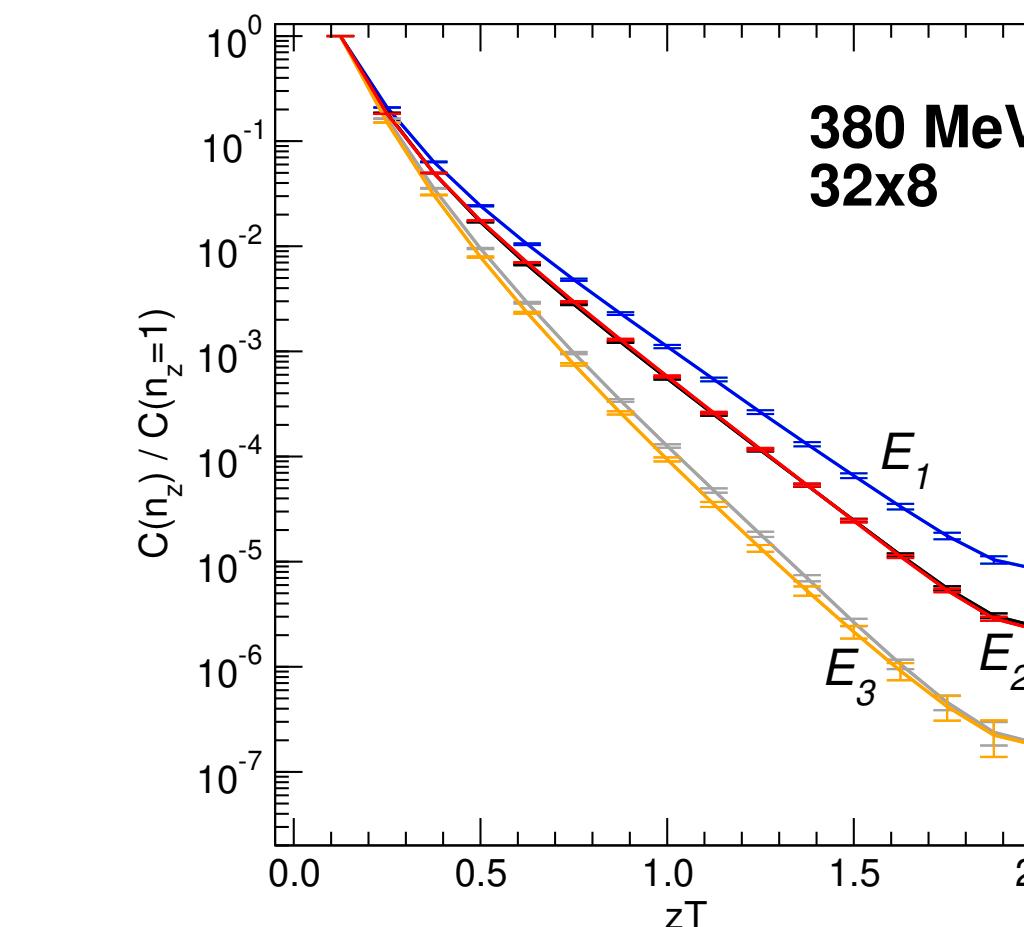
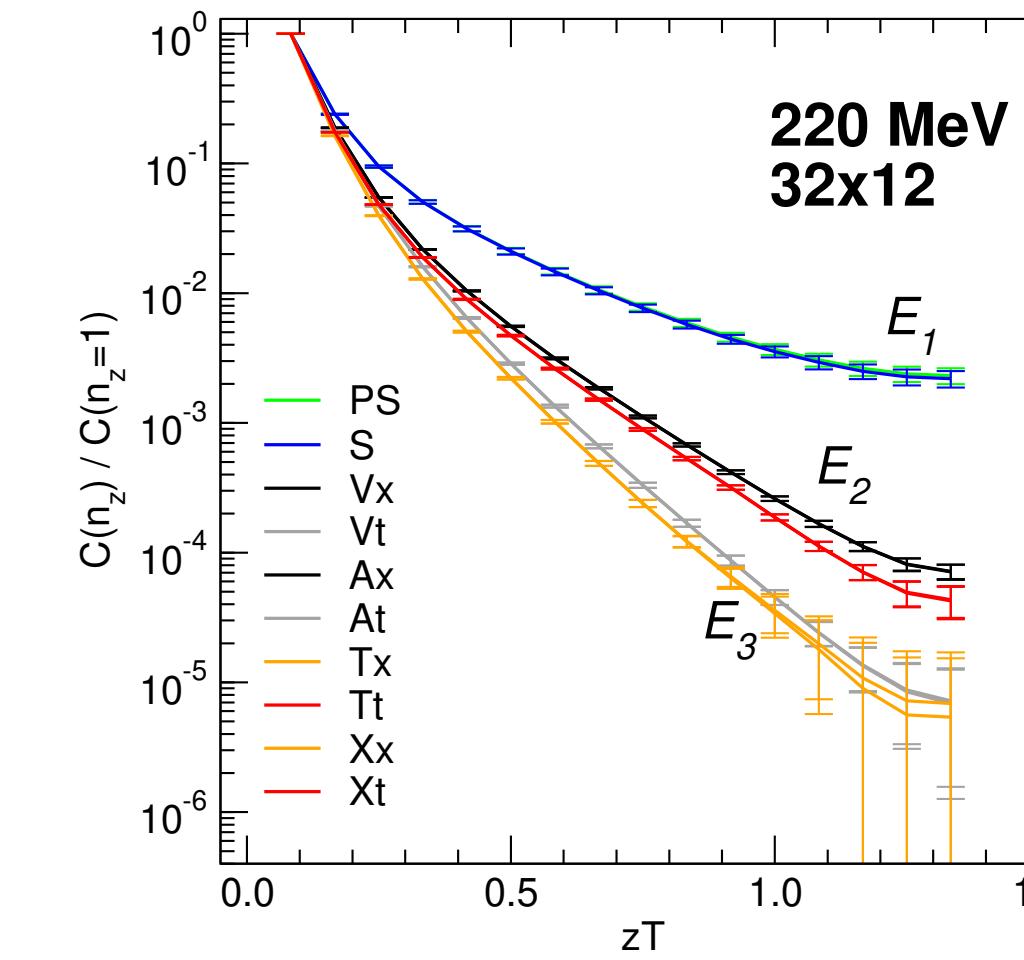
Rohrhofer, Aoki, Cossu, Fukaya, Glozman, Hashimoto,  
Lang, Prelovsek, PRD 96 (2017) 094501

⋮

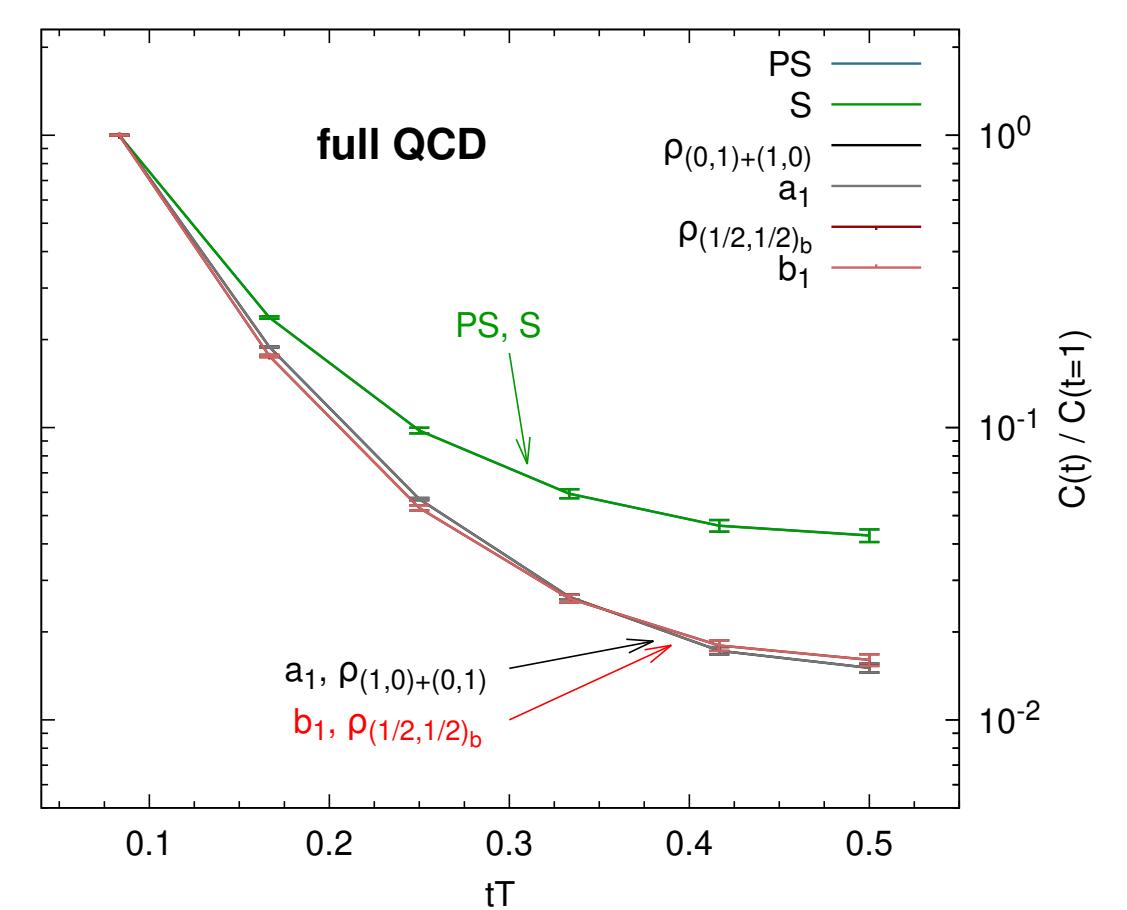
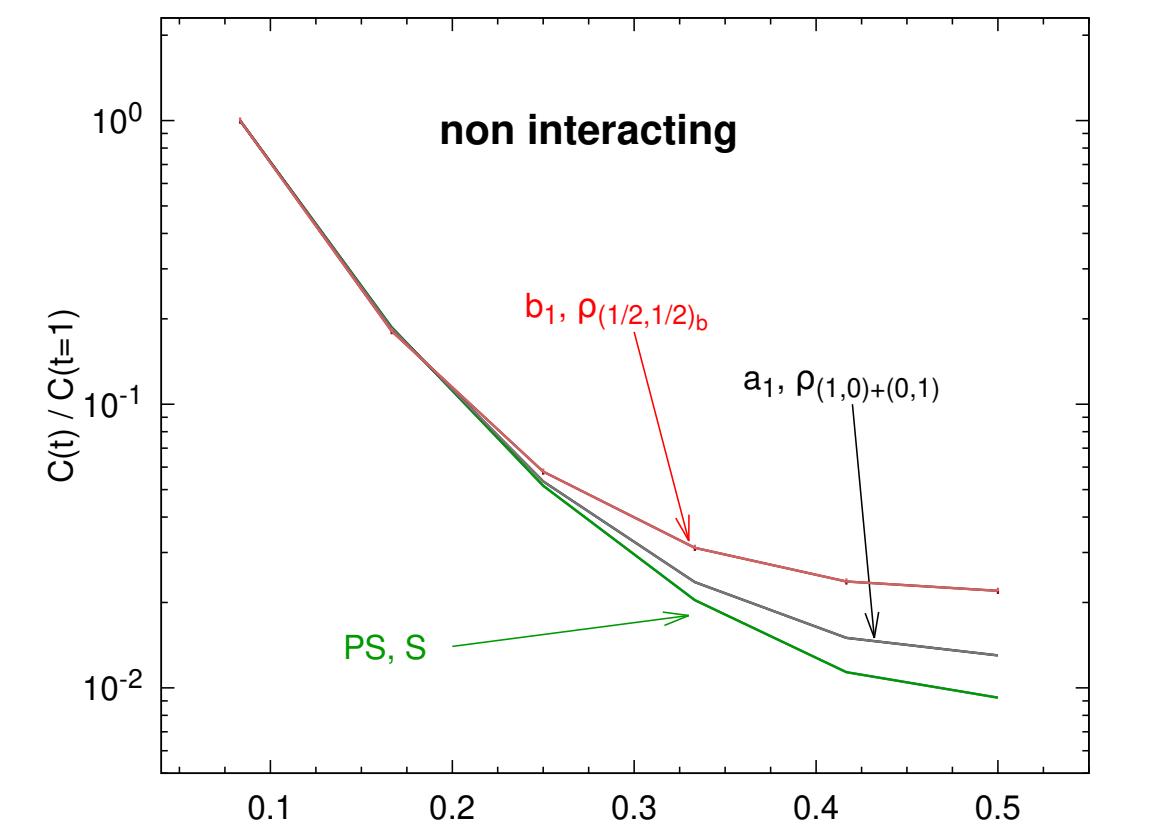
⋮

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Rohrhofer, Aoki, Glozman, Hashimoto, PLB 802 (2020) 135245



Lattice QCD



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# **QCD phase structure at finite density: Facts & Fiction**

**‘Confinement’ related crossovers at  $T_\chi \lesssim T_{\text{conf}} \lesssim 2 T_\chi$**

**Functional QCD**

**Lattice QCD**

**Variants of the  
traced Polyakov loop**

$$P = \frac{1}{N_c} \text{tr } e^{2\pi i \varphi}$$

:

**Braun, Gies, JMP, PLB 684 (2010) 262-267**

:

**Lu, Gao, Liu, JMP, arxiv:2504.05099**

**Borsanyi, Fodor, Hoelbling, Katz, Krieg, Ratti, Szabo, JHEP 09, 073 (2010)**

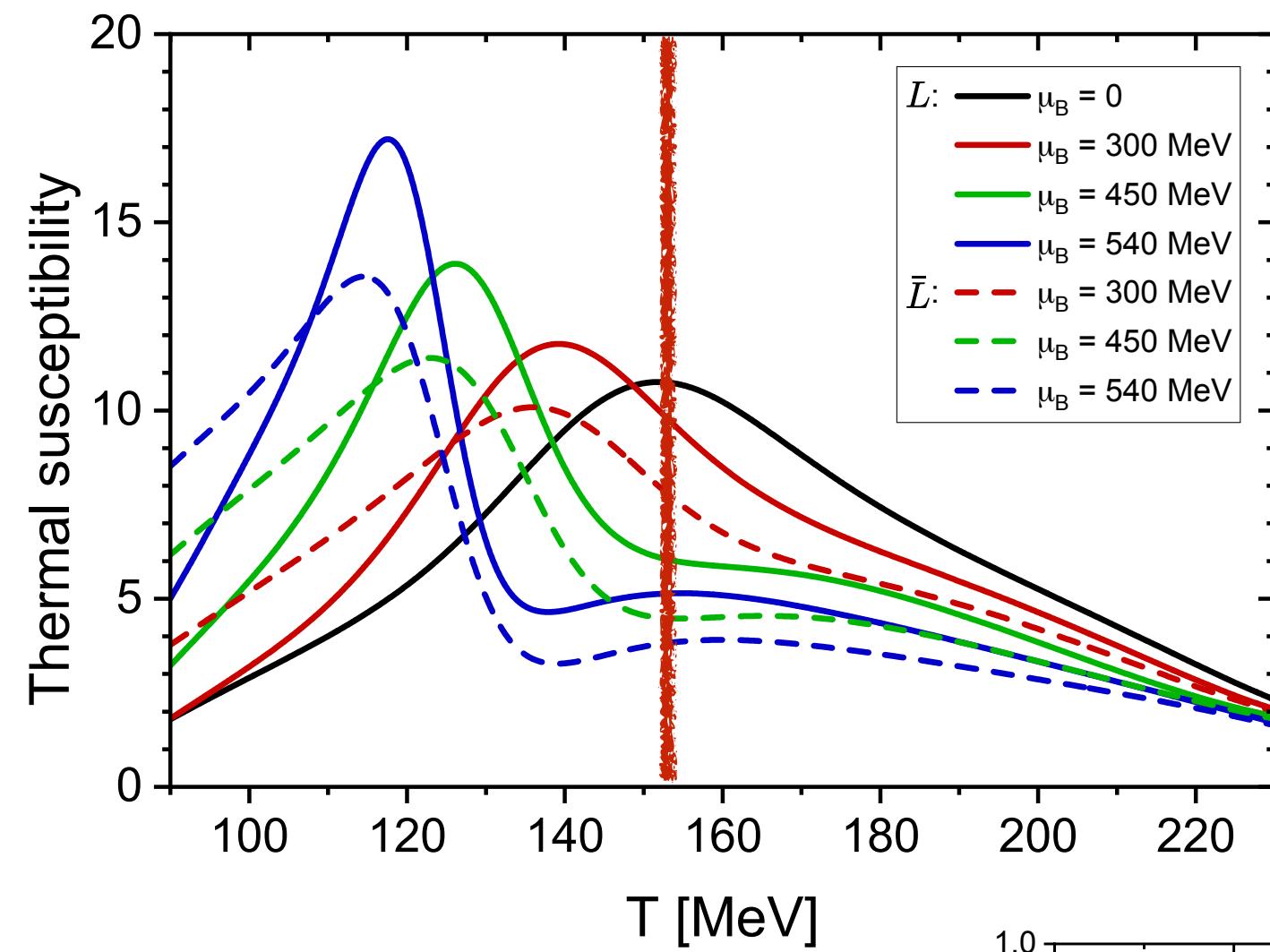
:

**Borsányi, Fodor, Guenther, Kara, Paolo Parotto, Pásztor, Pirelli, Wong, PRD 110 (2024) 114507**

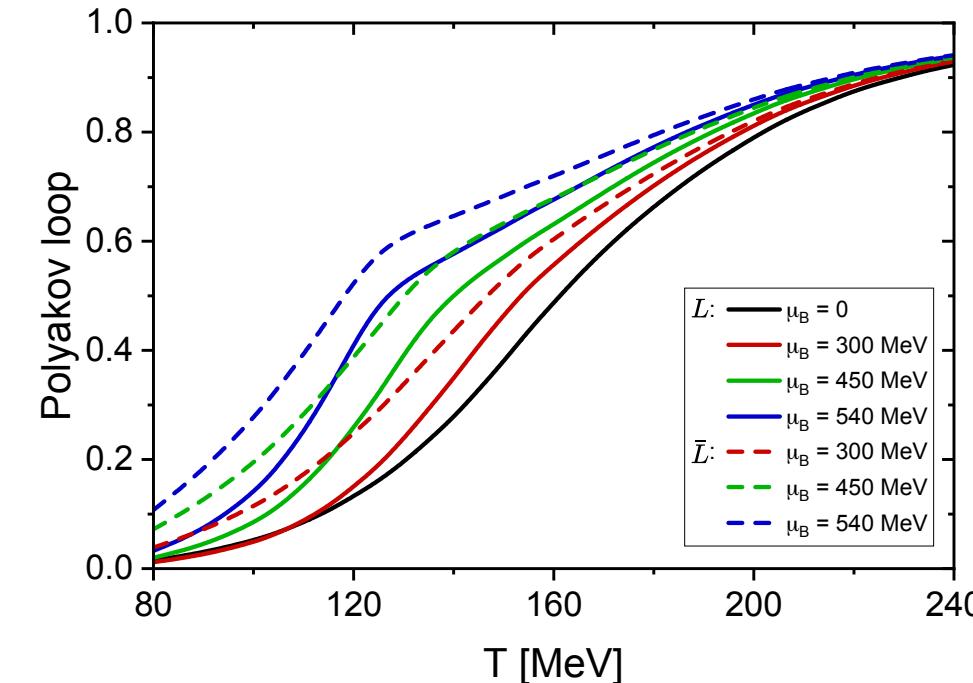
# QCD phase structure at finite density: Facts & Fiction

‘Confinement’ related crossovers at  $T_\chi \lesssim T_{\text{conf}} \lesssim 2T_\chi$

## Functional QCD



$$\propto P(\langle \text{ev}(\varphi) \rangle)$$

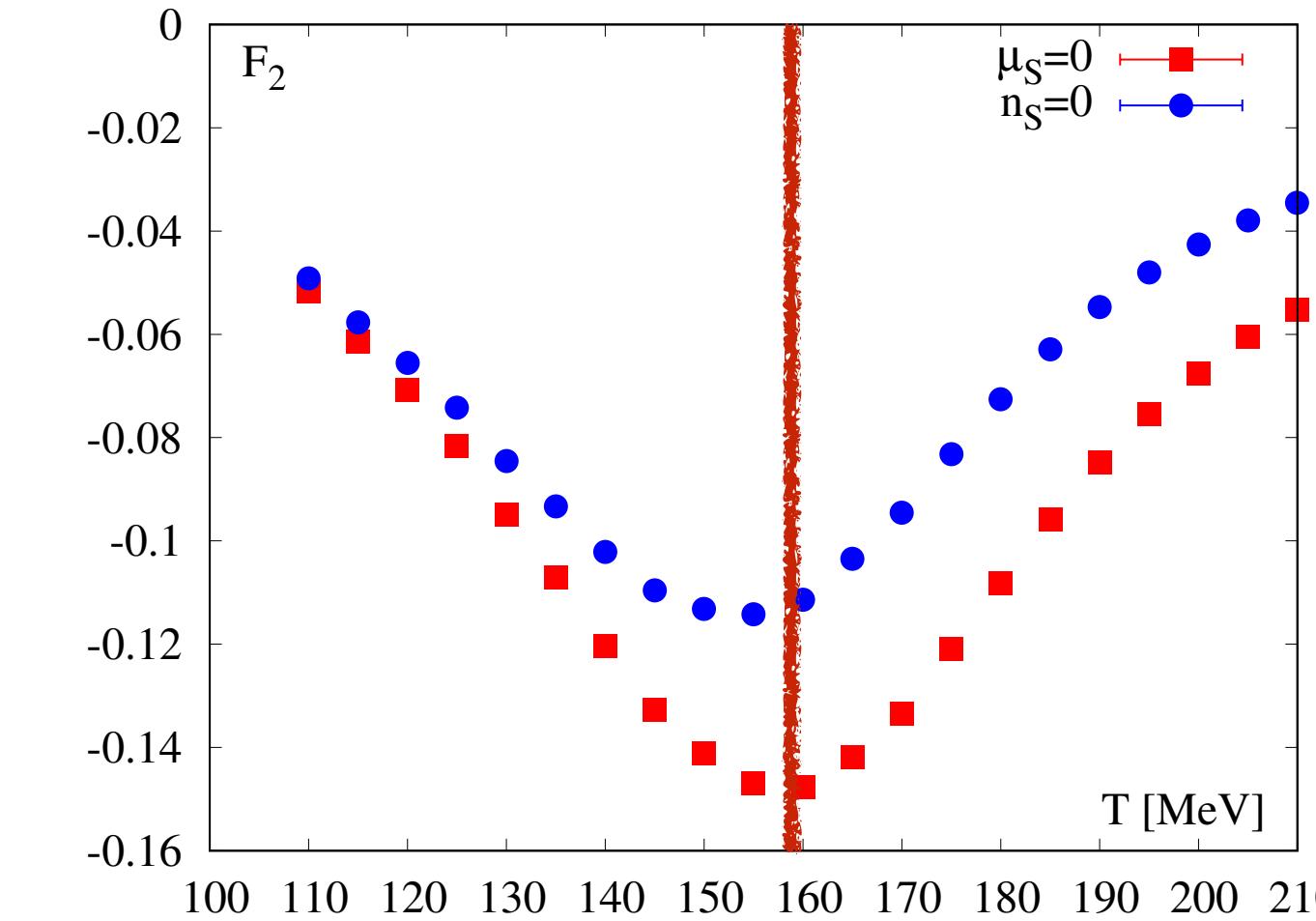


Braun, Gies, JMP, PLB 684 (2010) 262-267

⋮

## Variants of the traced Polyakov loop

$$P = \frac{1}{N_c} \text{tr } e^{2\pi i \varphi}$$



$$\propto T \frac{\partial^2 \log |\langle P \rangle|}{(\partial \mu_B/T)^2}$$

⋮

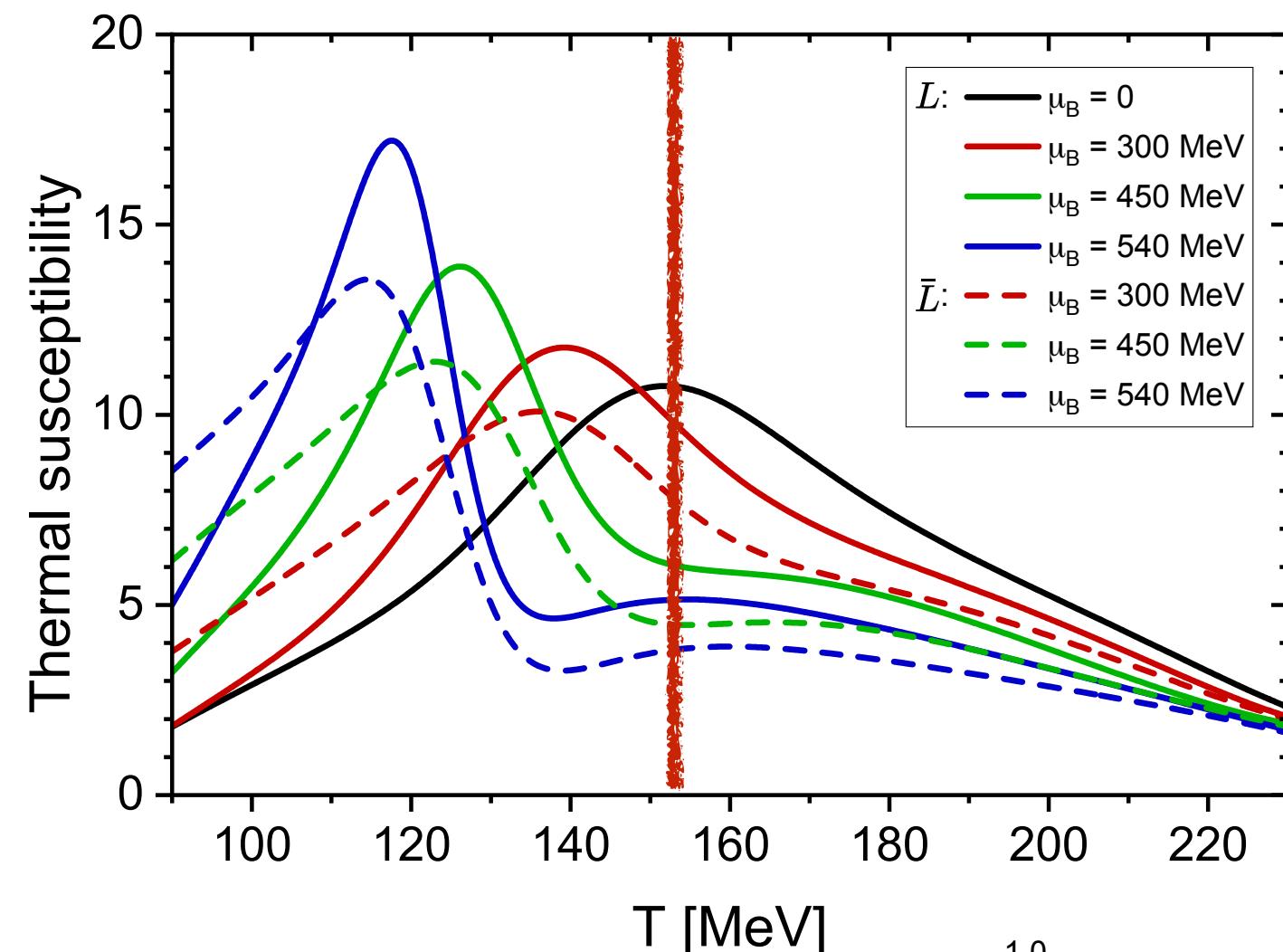
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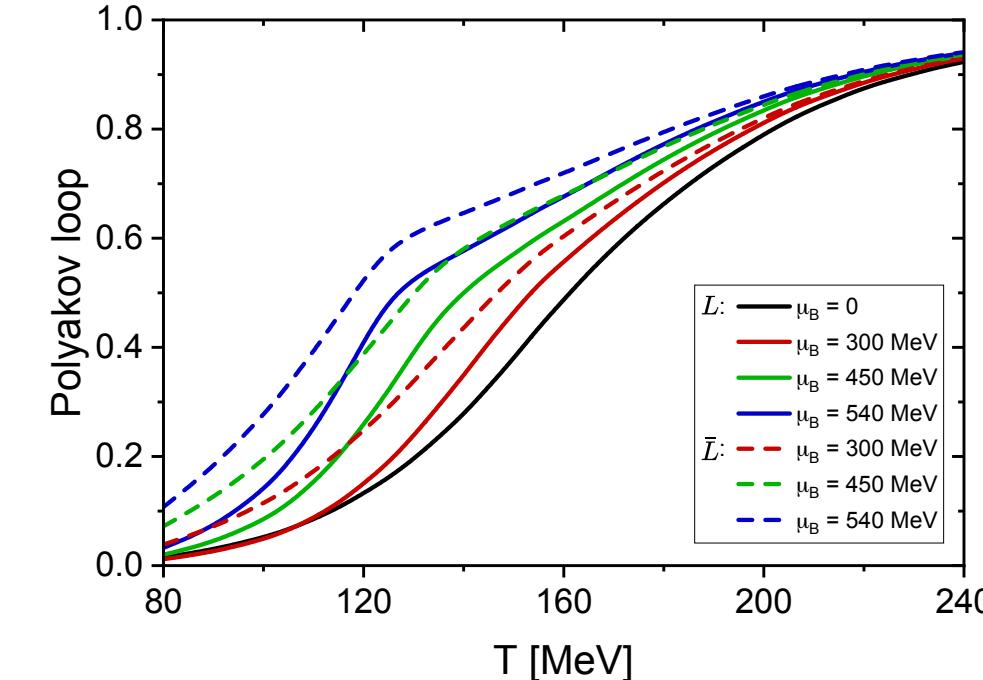
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## Functional QCD



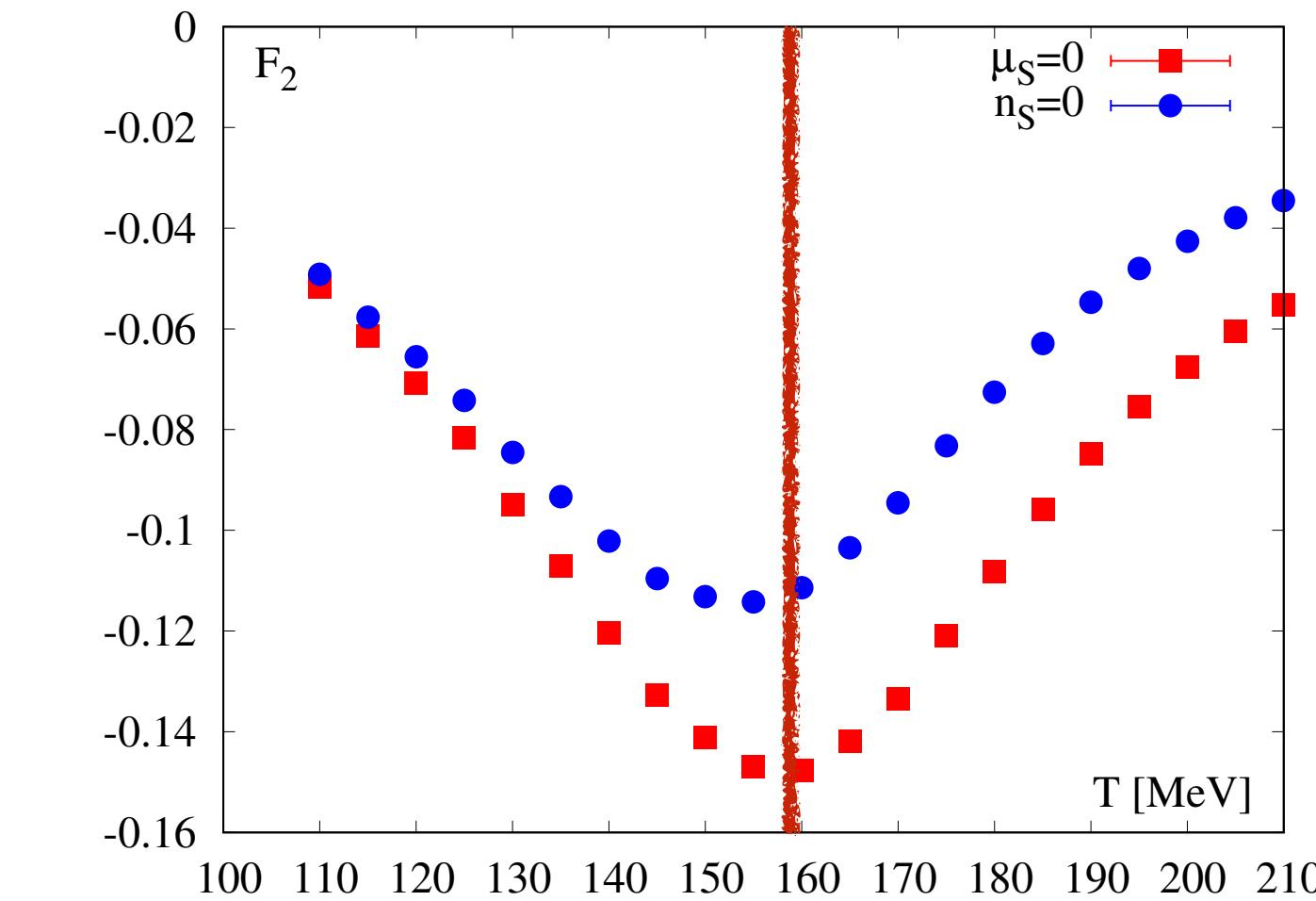
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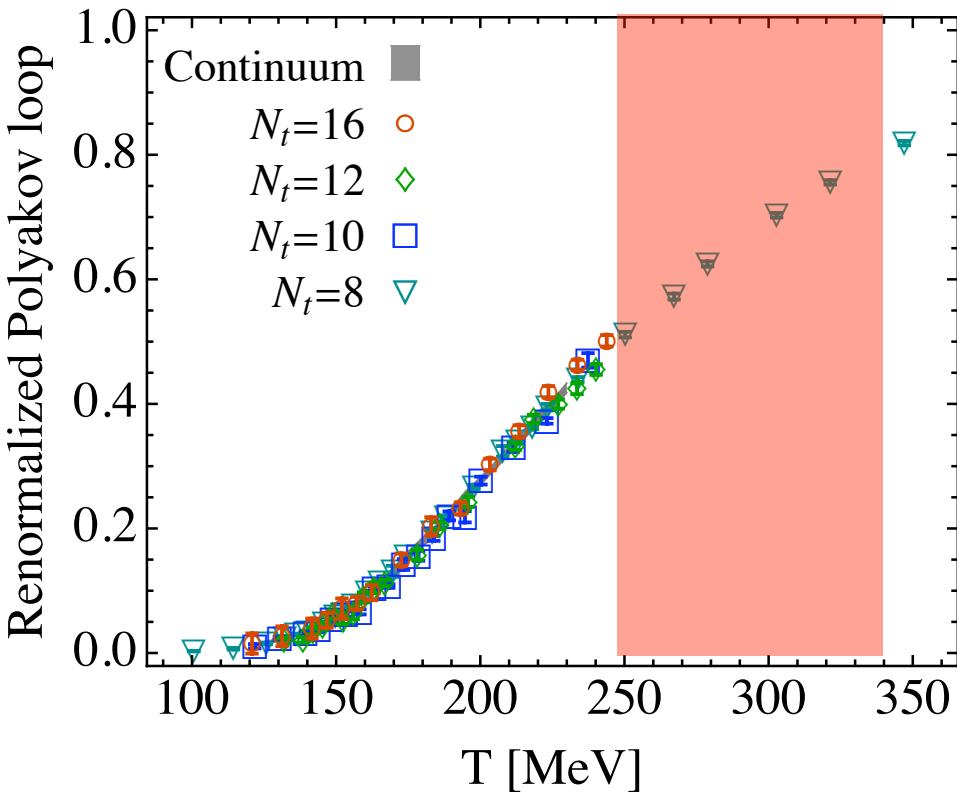
⋮

## Lattice QCD



$$\propto \langle P \rangle$$

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⋮

Borsanyi, Fodor, Hoelbling, Katz, Krieg, Ratti, Szabo, JHEP 09, 073 (2010)

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$$\mu_B \neq 0$$

chiral: driven by scalar-pseudoscalar fluctuations

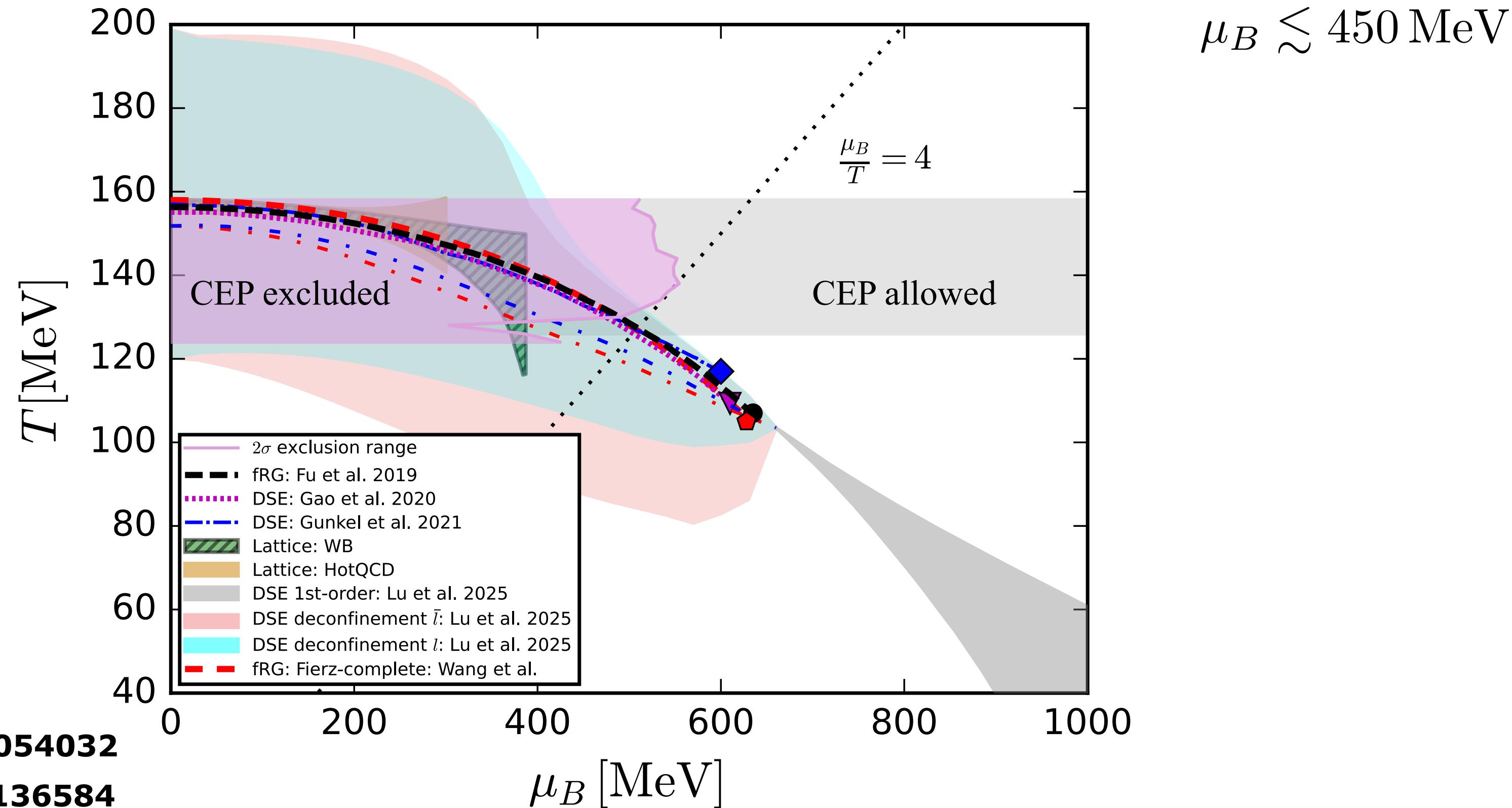
# QCD phase structure at finite density: Facts & Fiction

No chiral critical end point for  $\mu_B \lesssim 600$  MeV

## Functional QCD

## Functional QCD CEP+ lattice QCD exclusion plot

## Lattice QCD



Fu, JMP, Rennecke, PRD 101 (2020) 054032

Gao, JMP, PLB 820 (2021) 136584

Gunkel, Fischer, PRD 104 (2021) 054022

Lu, Gao, Liu, JMP, arXiv:2504.05099

Lu, Gao, Liu, arXiv:2509.02974

Wang et al, in preparation

$\mu_B \lesssim 450$  MeV

Borsanyi, Fodor, Guenther, Parotto, Pasztor,  
Ratti, Vovchenko, Wong, arxiv: 2502.10267

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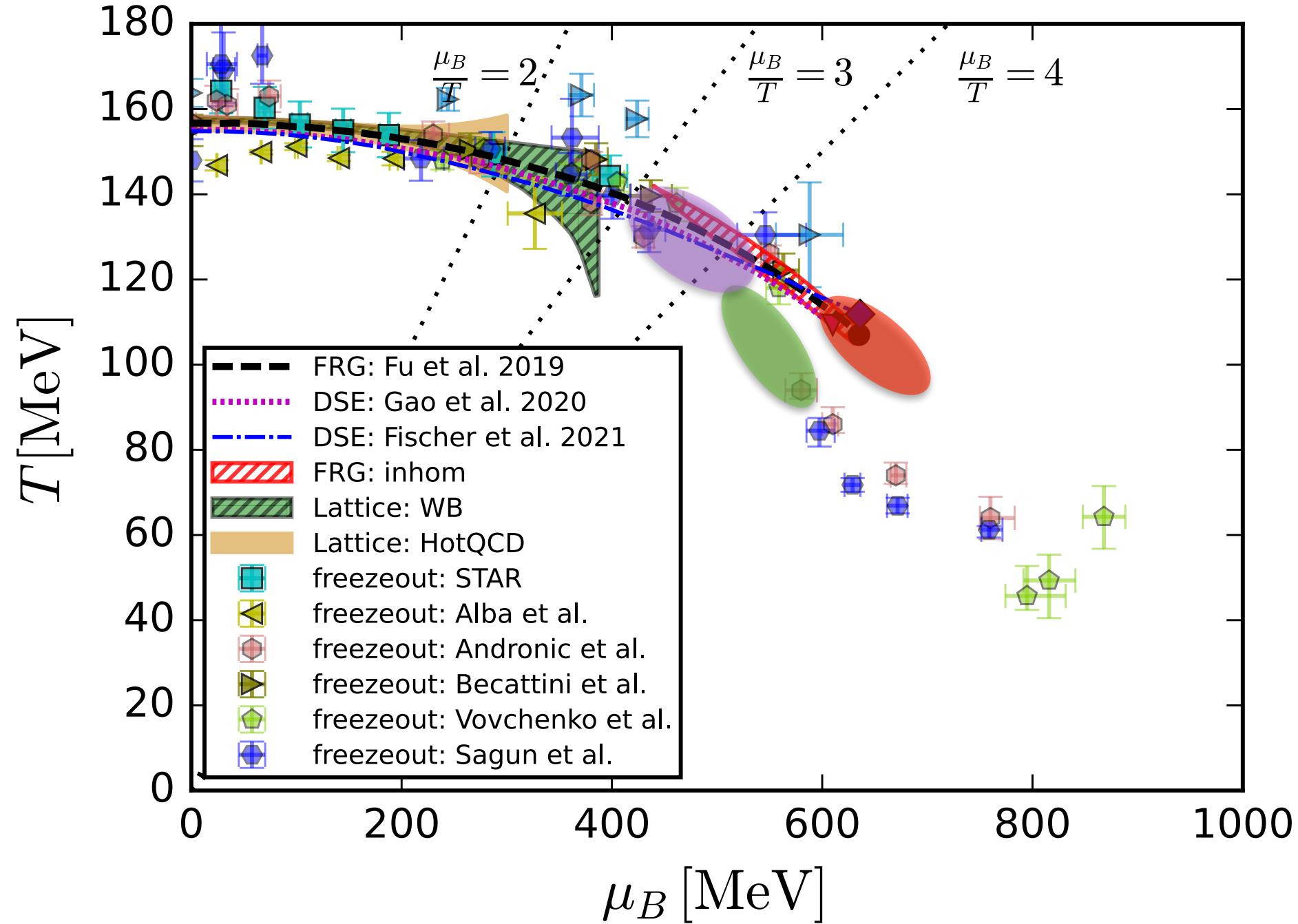
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Functional QCD

Lattice QCD

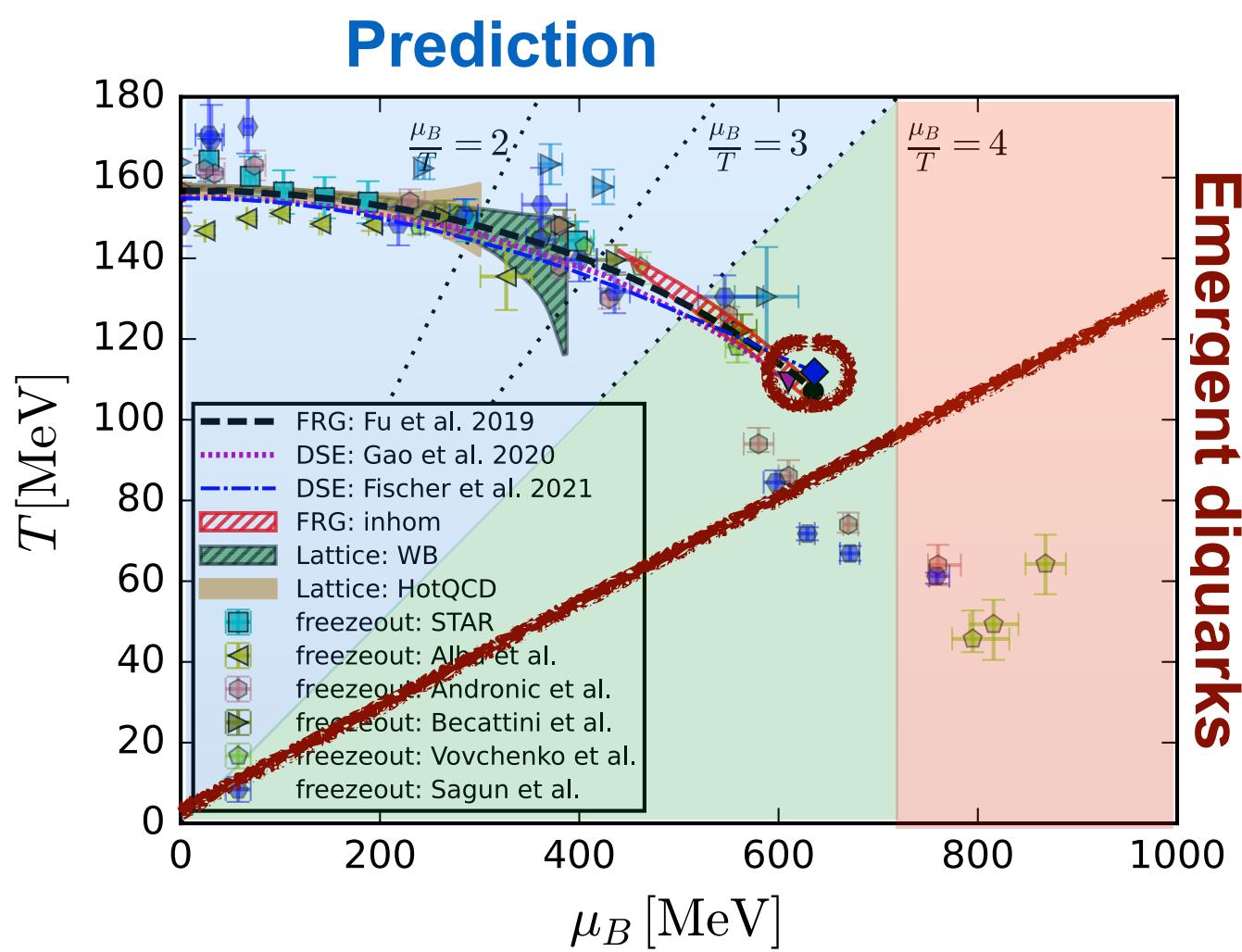
not yet

## High density phase structure from function



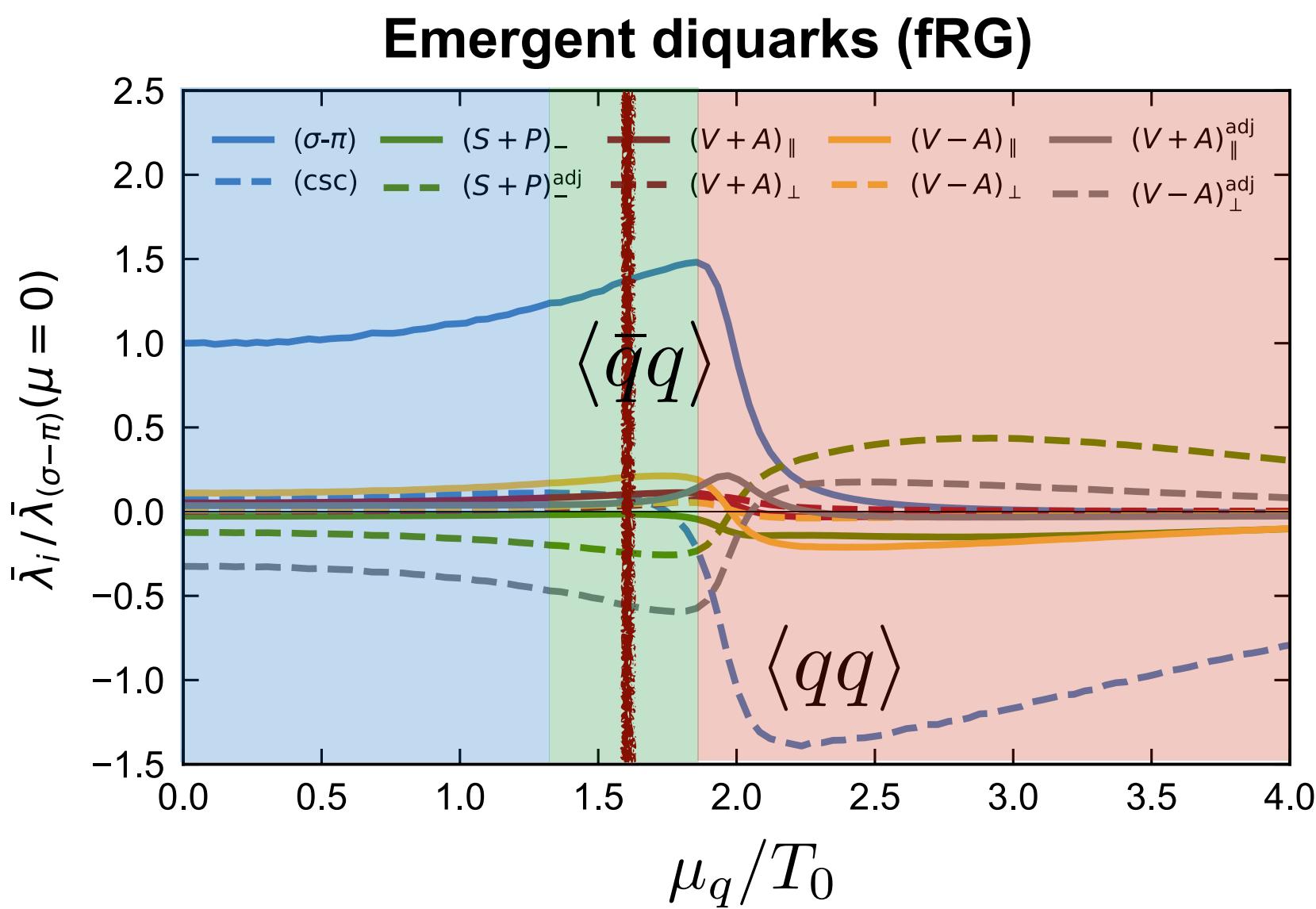
# Predictions & estimates

Emergent diquarks



Emergent diquarks

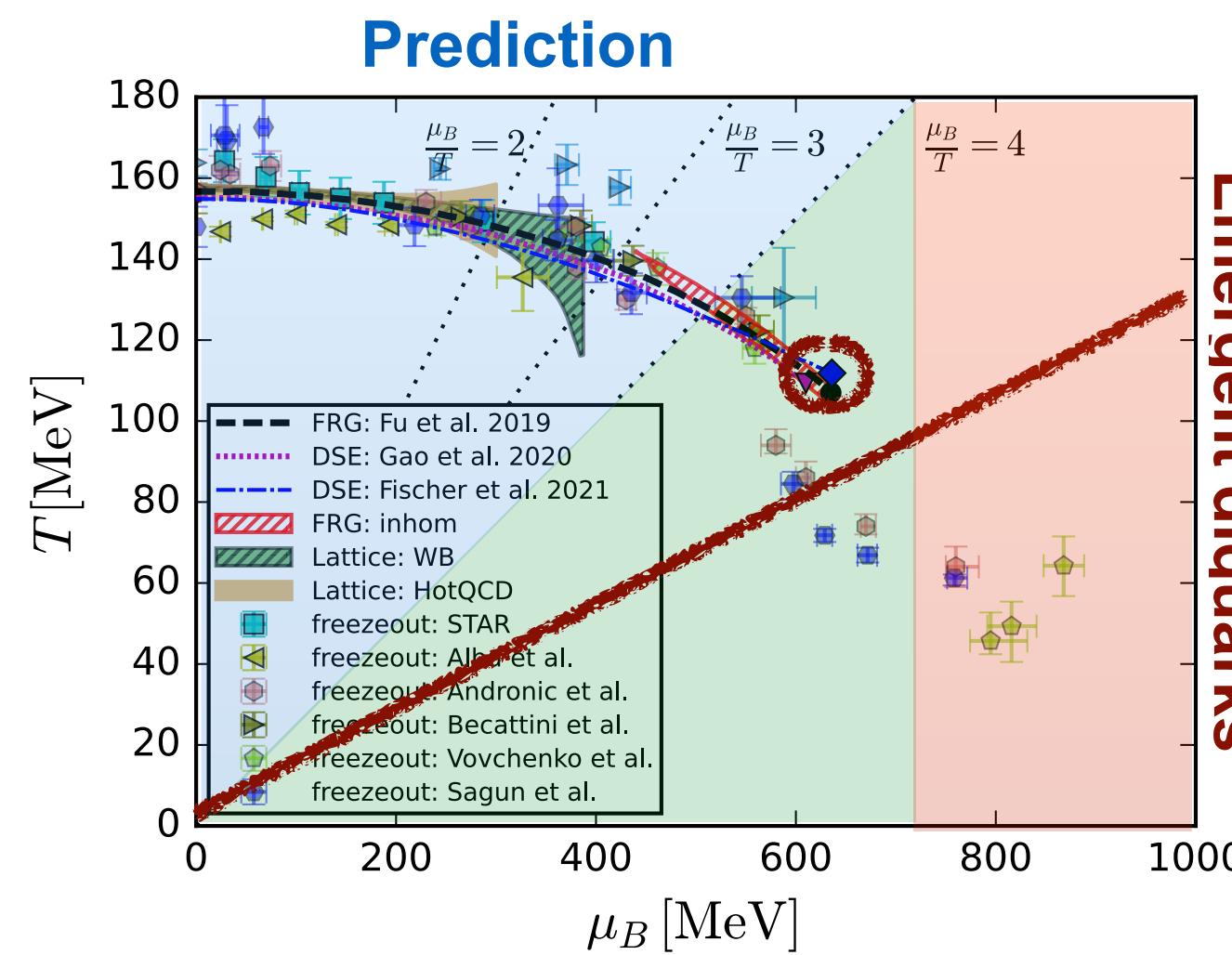
Regime of quantitative reliability  
of  
current best truncation



Estimate

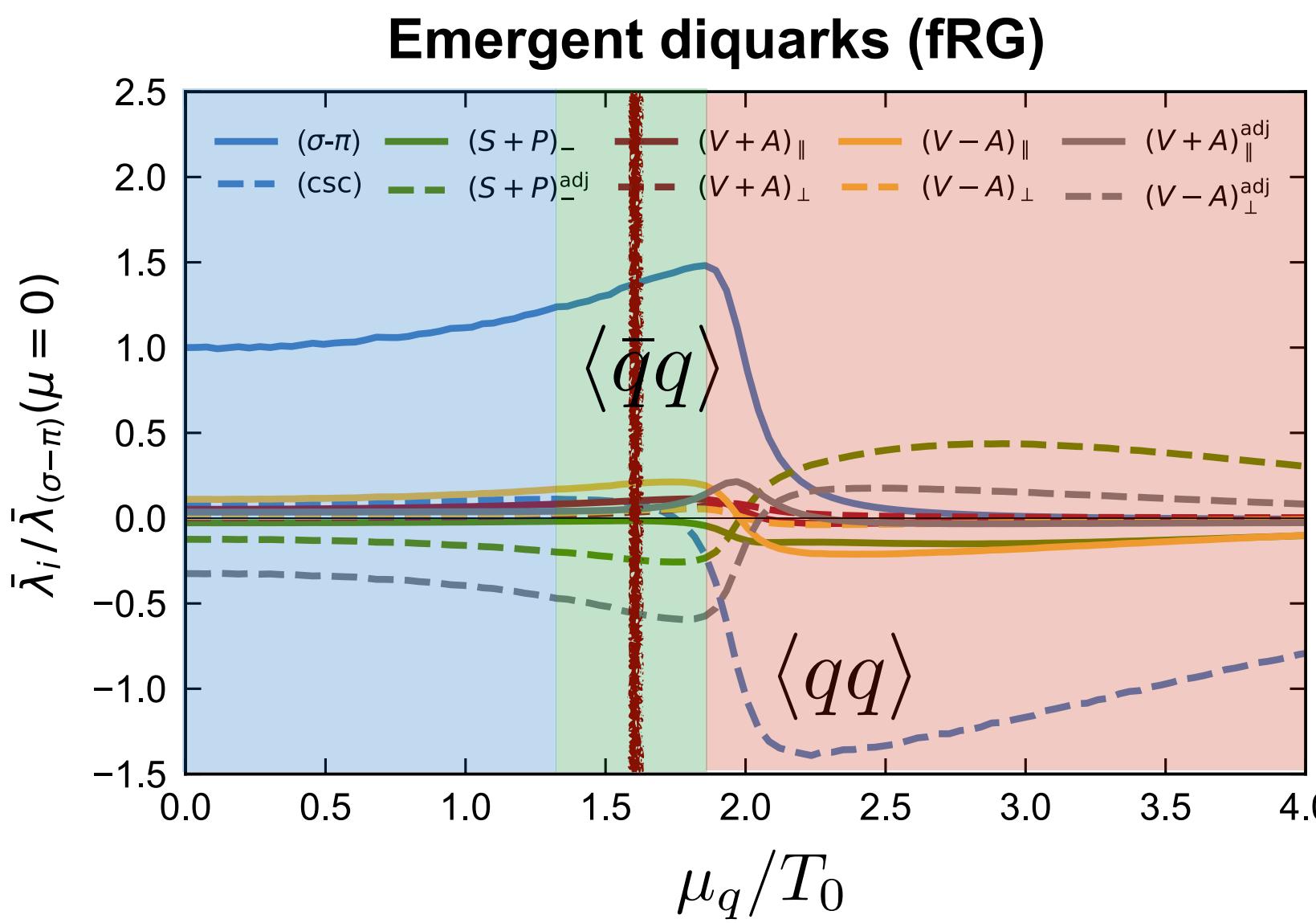
# Predictions & estimates

Emergent diquarks



Emergent diquarks

Regime of quantitative reliability  
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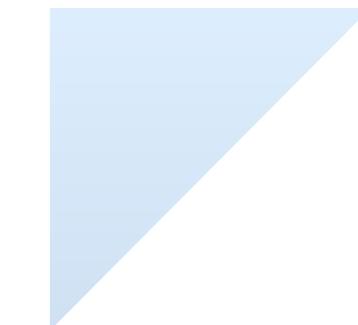
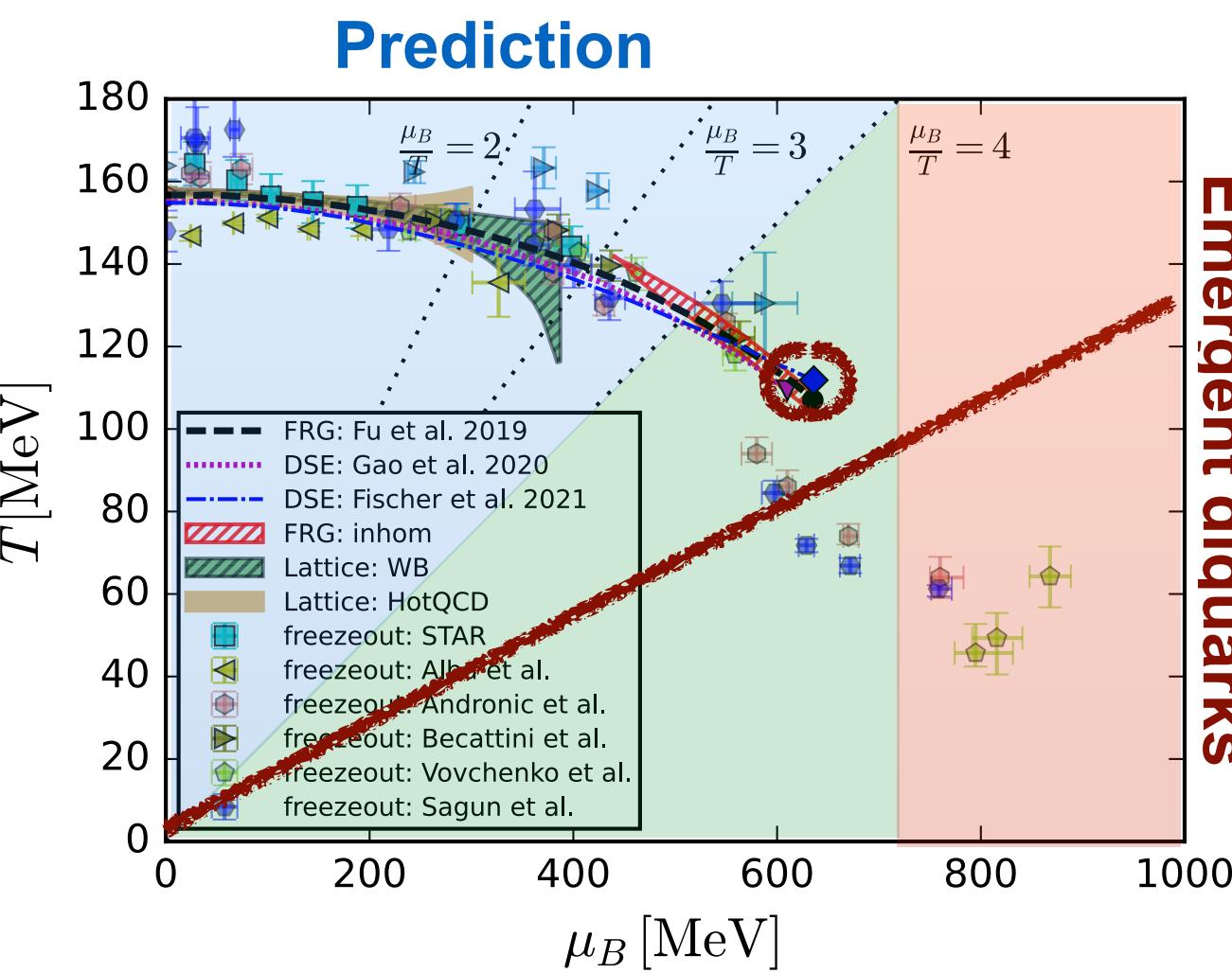


Estimate

Emergent diquarks are not captured  
by extrapolations

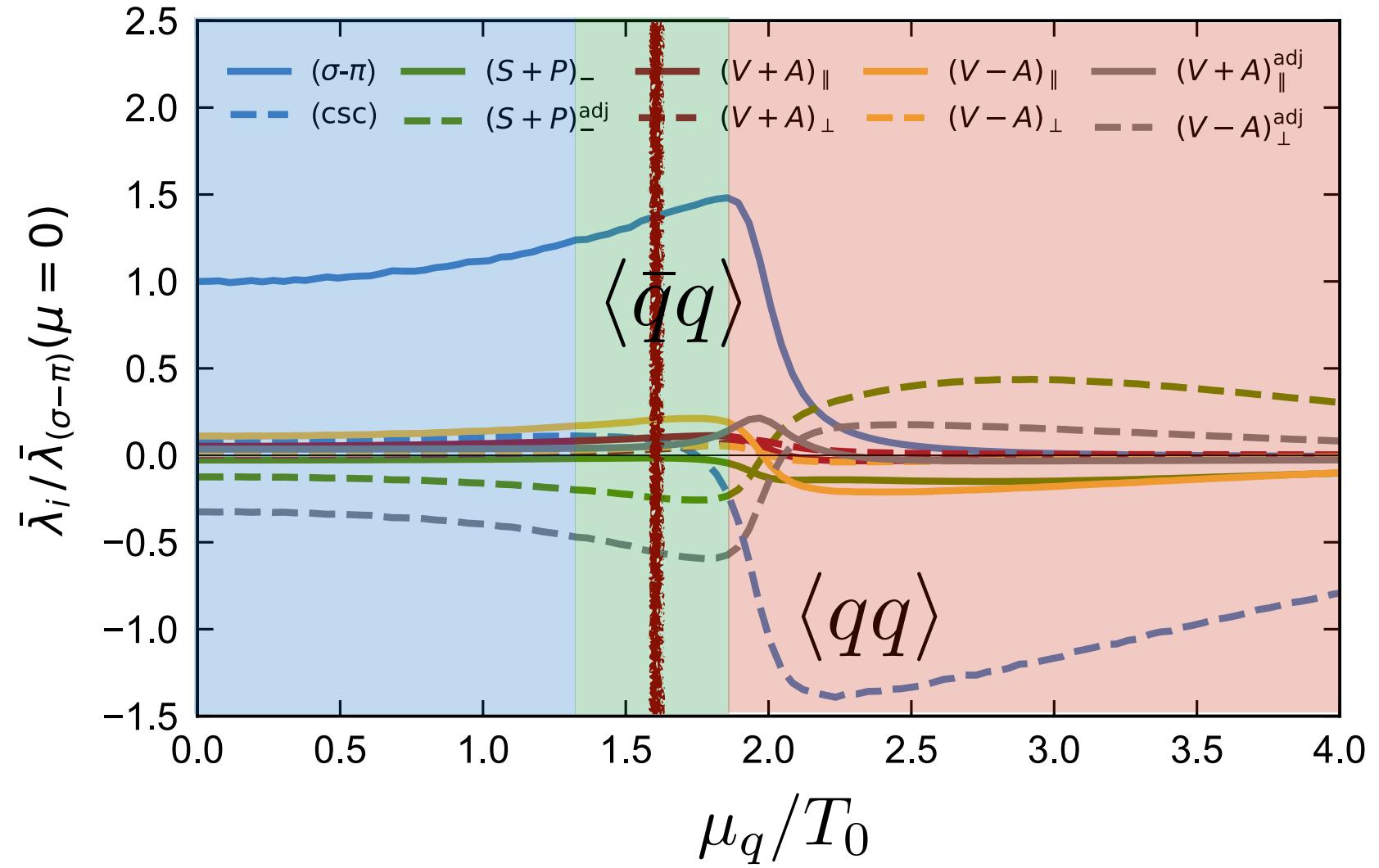
# Predictions & estimates

Emergent diquarks



Regime of quantitative reliability  
of  
current best truncation

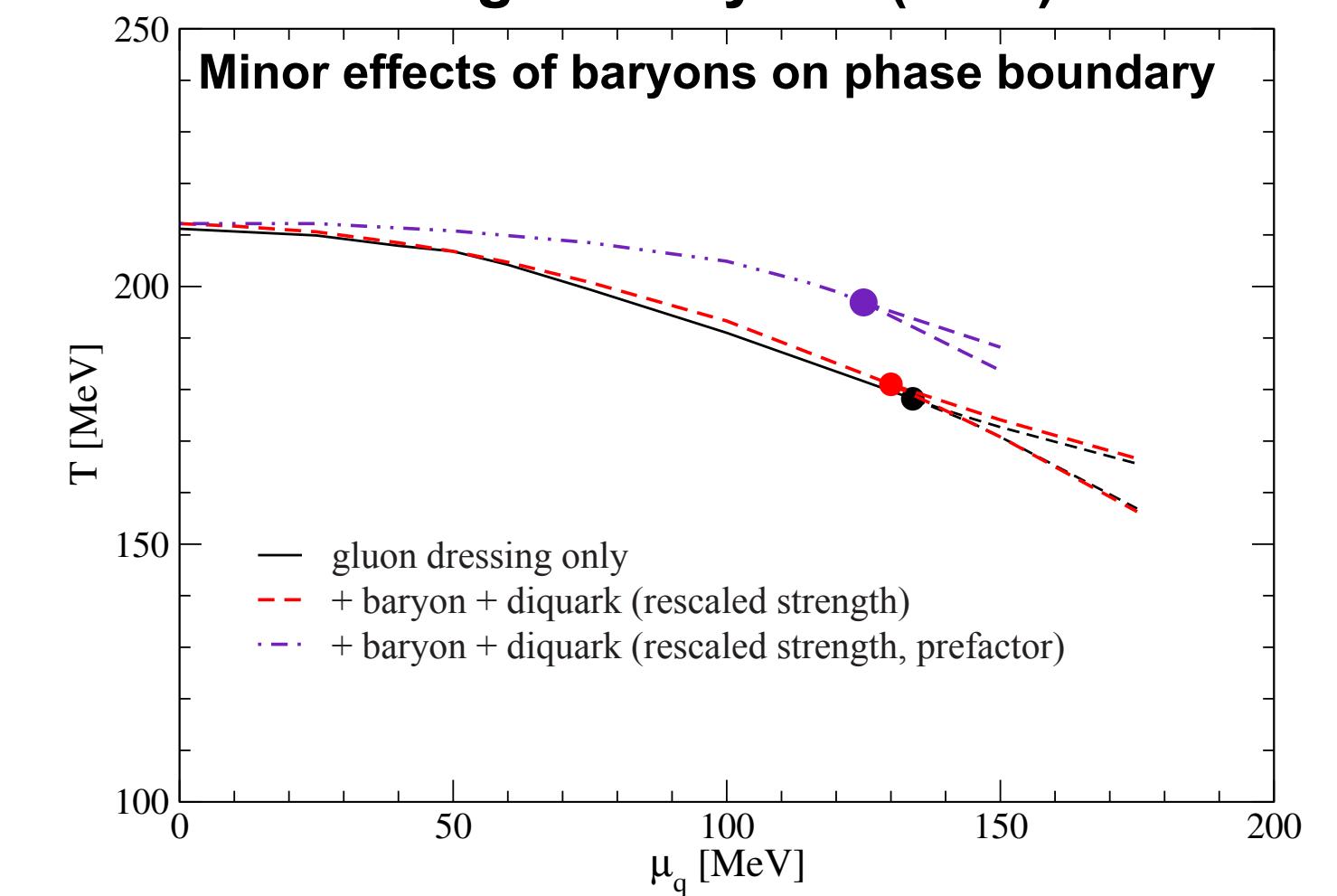
Emergent diquarks (fRG)



Estimate

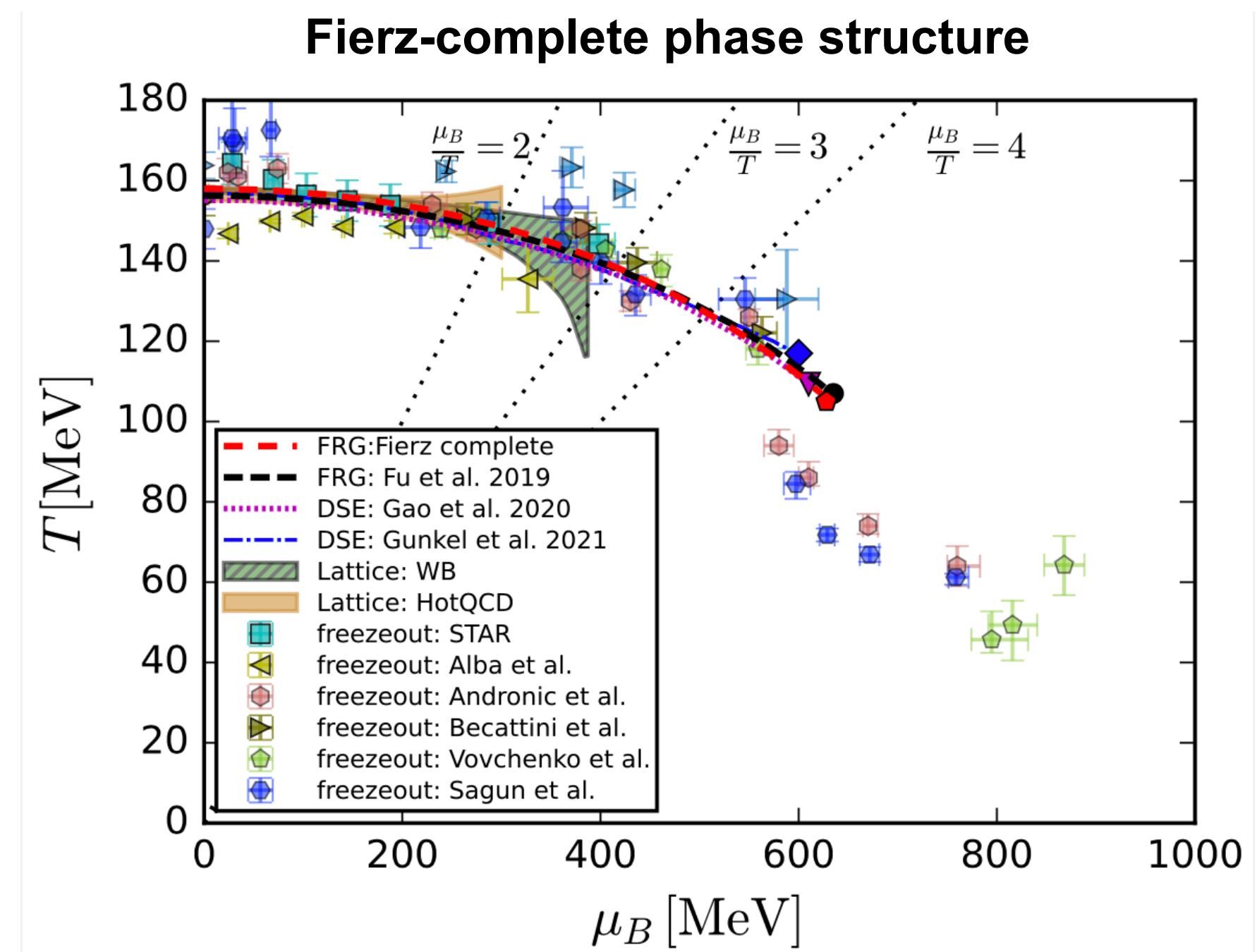
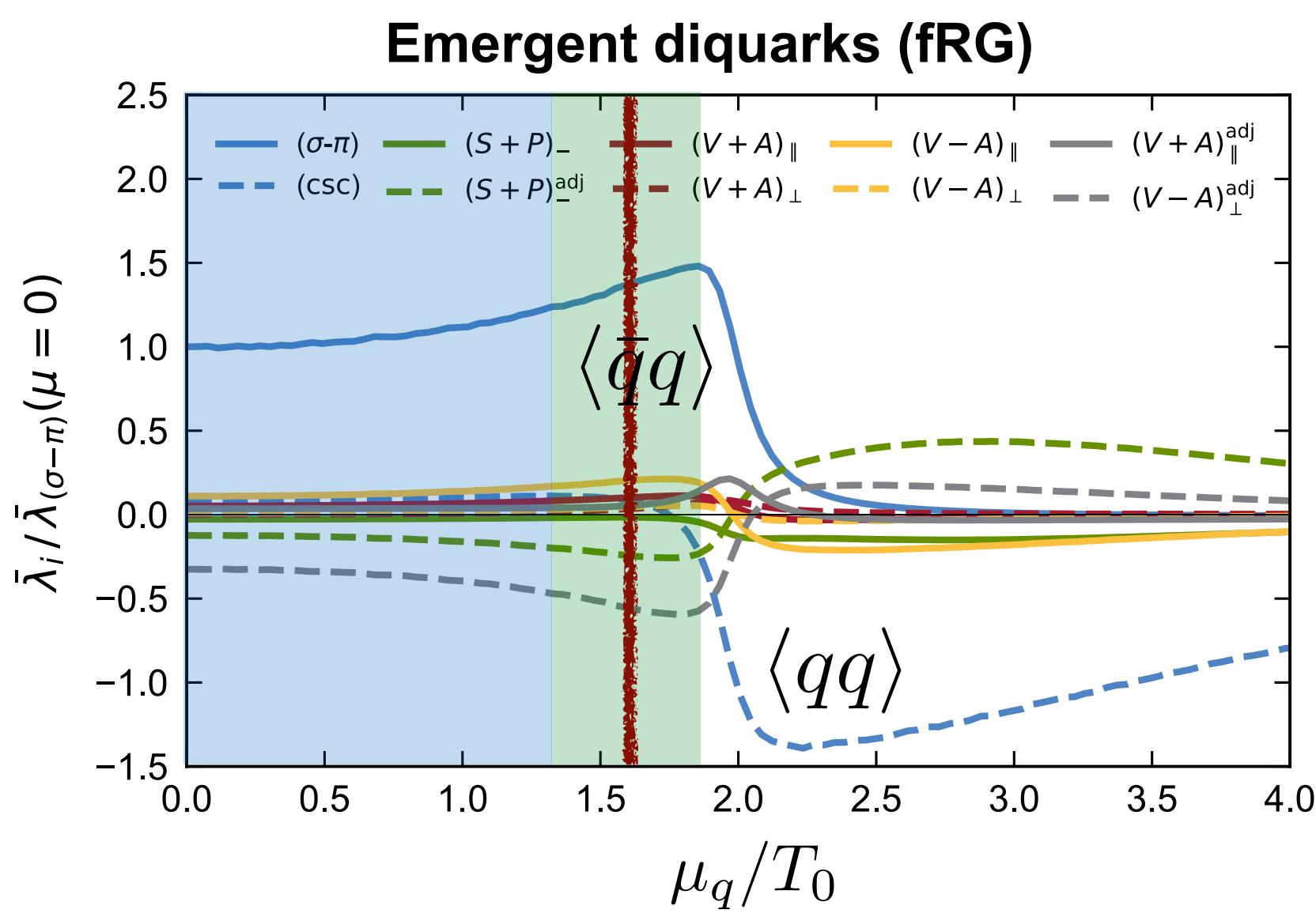
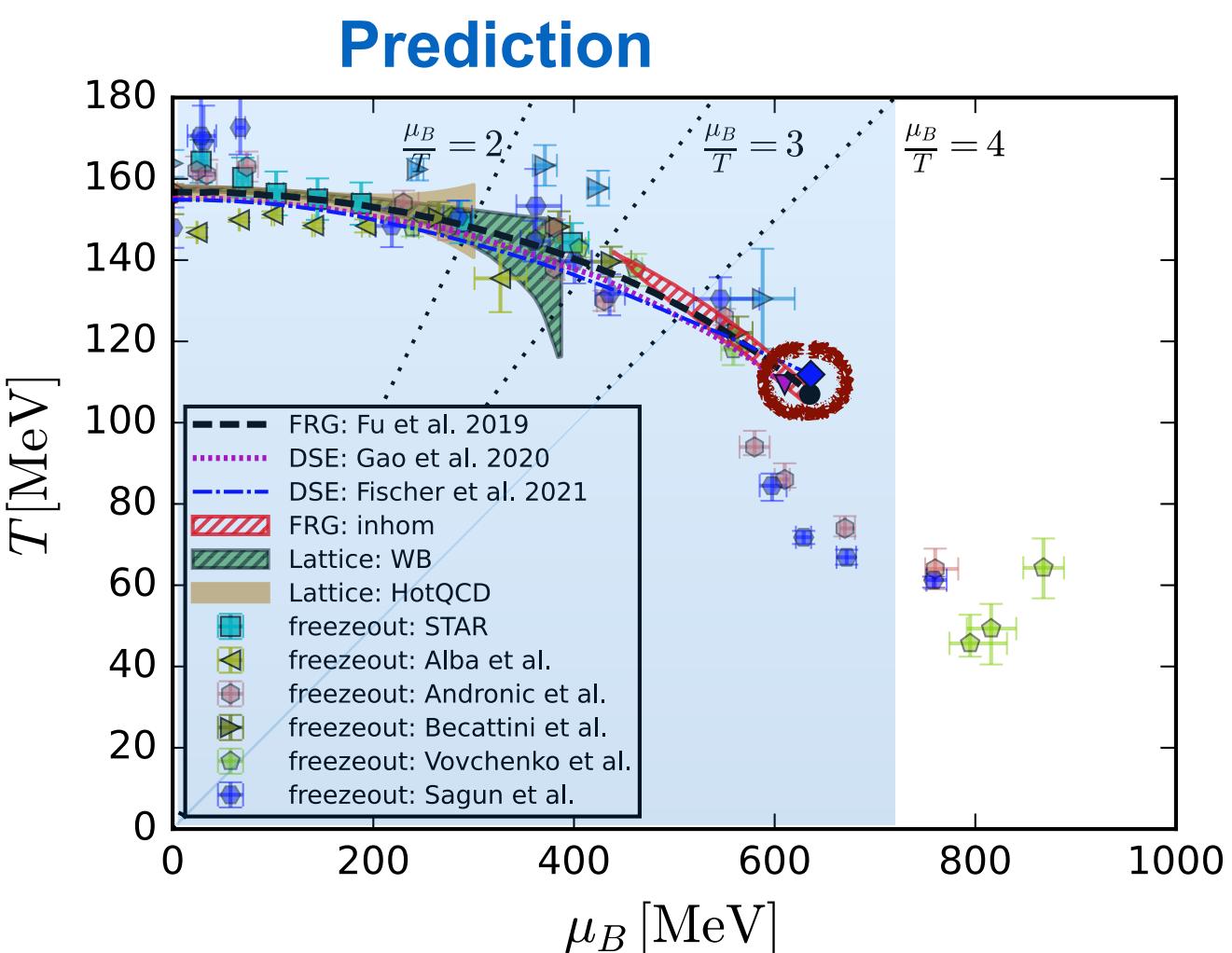


Emergent baryons (DSE)



# Predictions & estimates

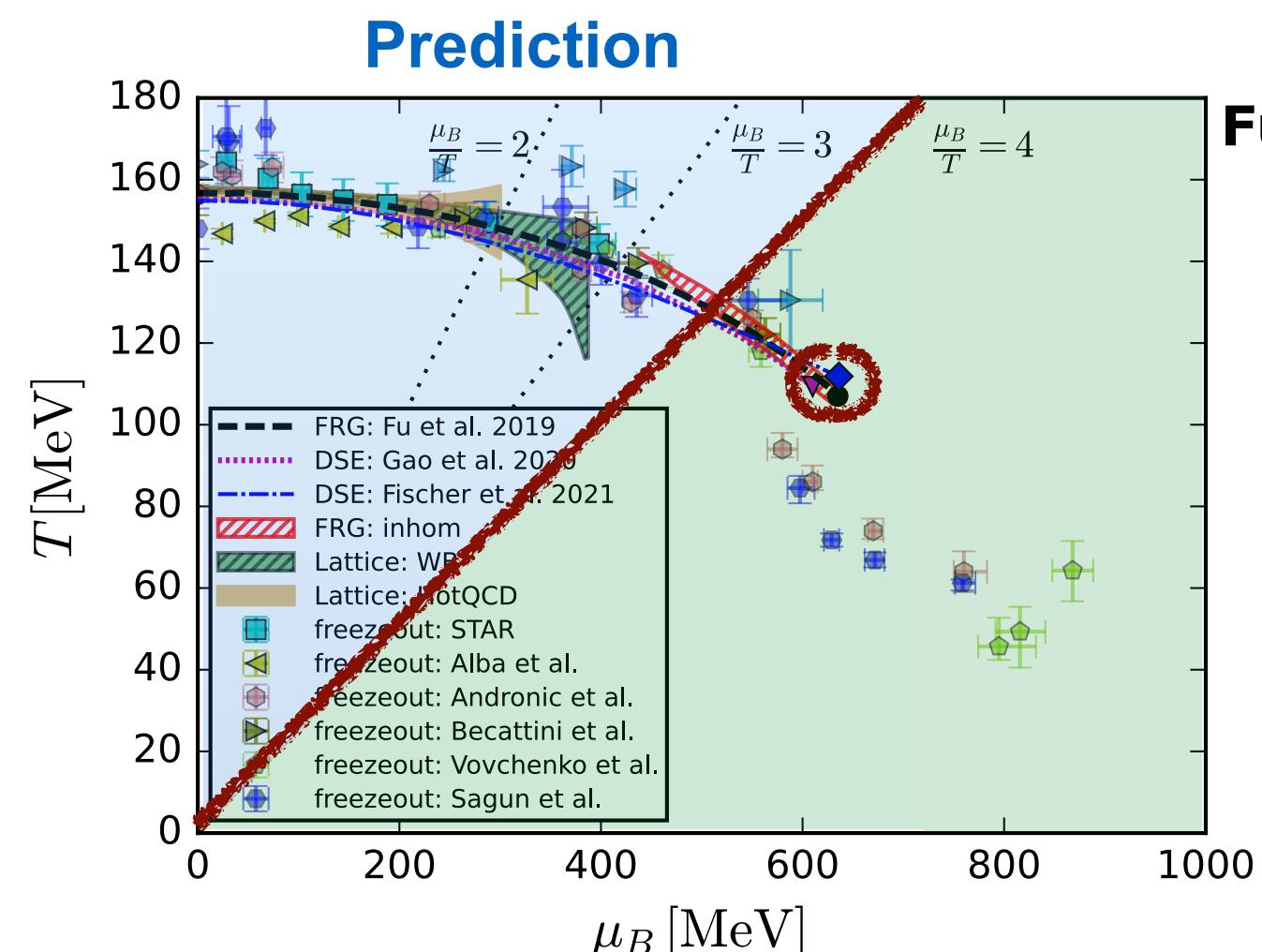
Dominance of scalar-pseudoscalar fluctuations  
Pions & sigma mode



# Predictions & estimates

Moat regime

Pisarski, Rennecke, PRL 127 (2021) 152302

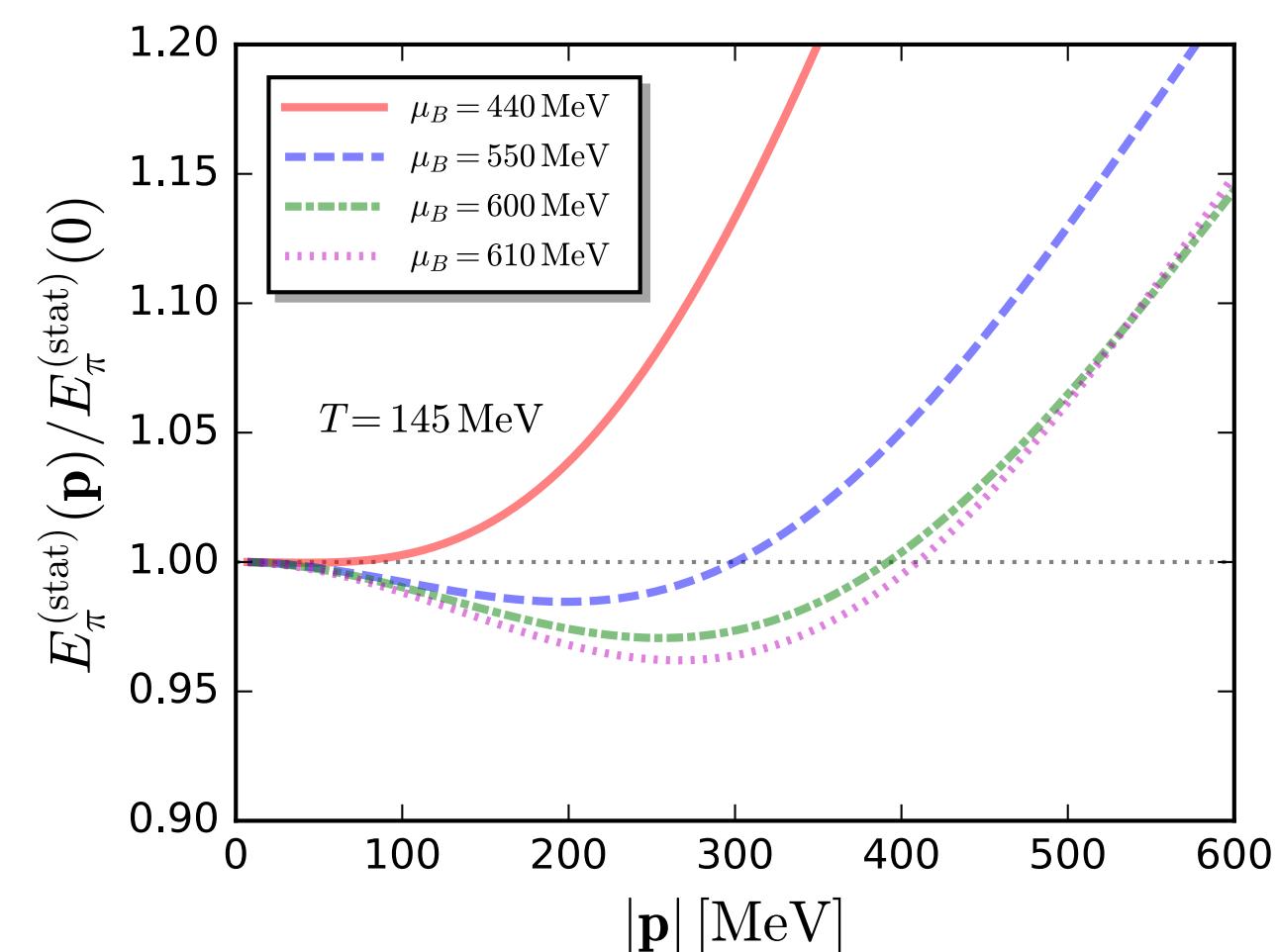


Fu, JMP, Rennecke, PRD 101 (2020) 054032

Regime of quantitative reliability  
of  
current best truncation

Estimate

Moat regime is not captured quantitatively



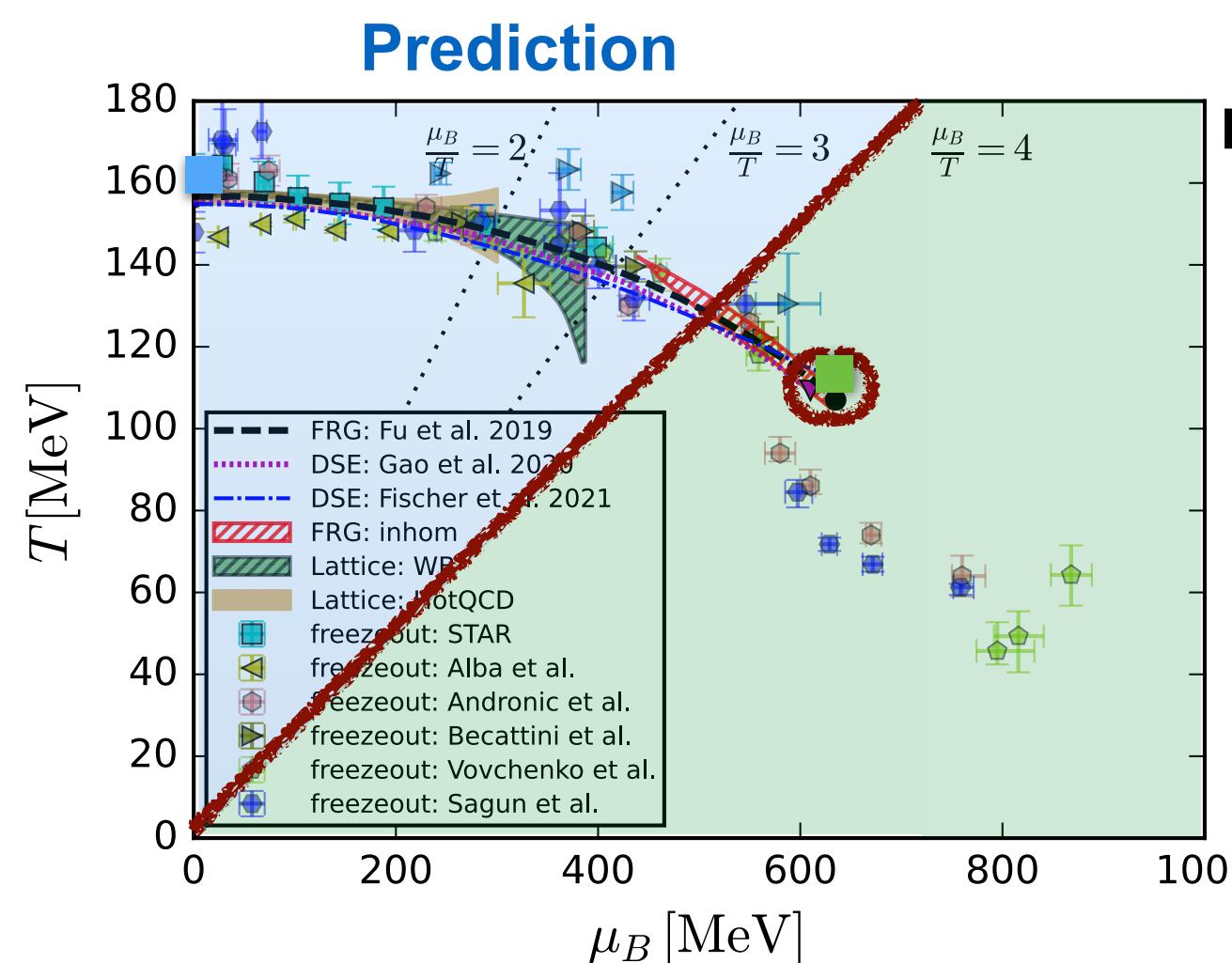
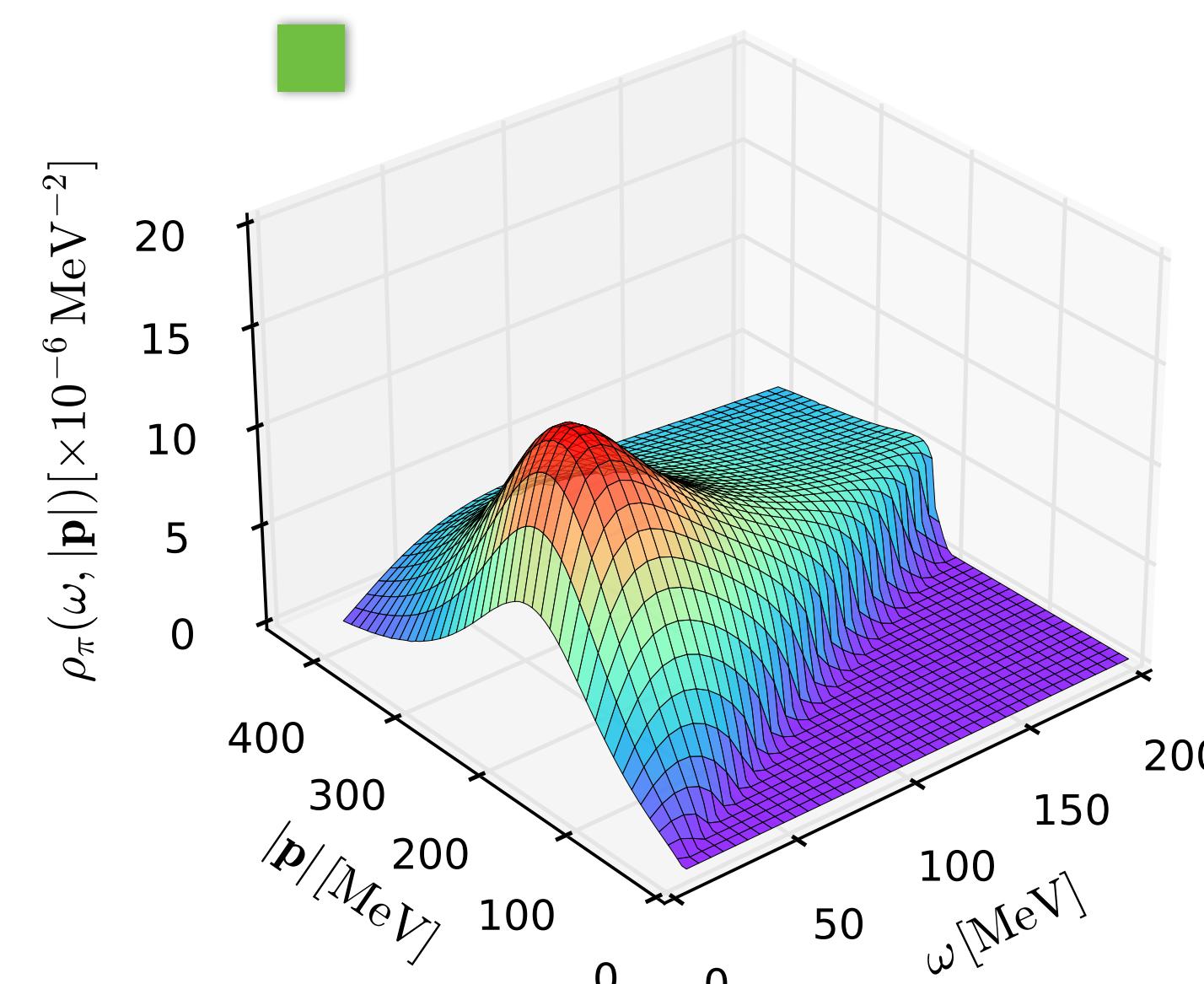
Fu, JMP, Pisarski, Rennecke, Wen, Shi Yin, 2412.15949

# Predictions & estimates

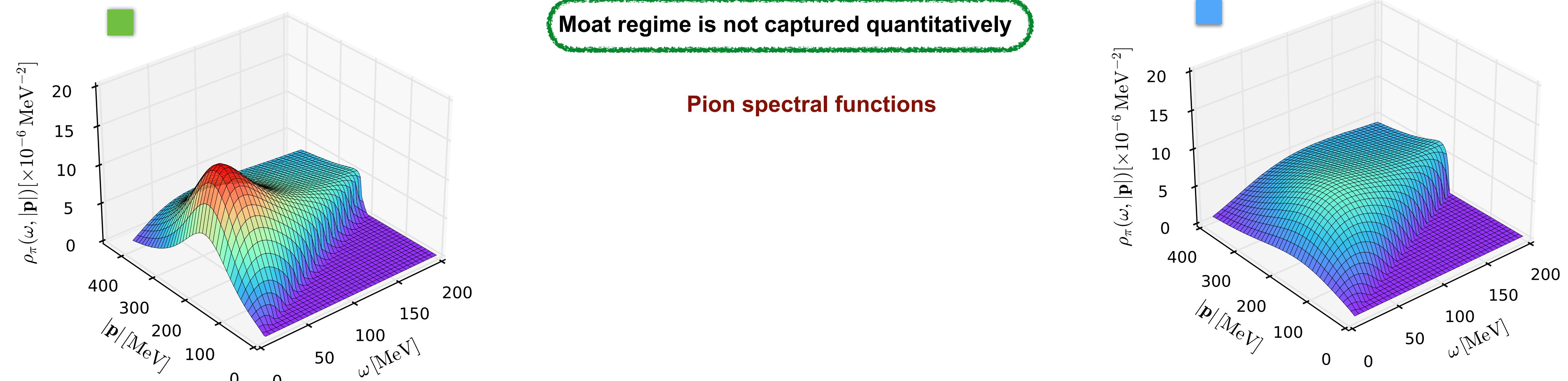
**Moat regime**

Pisarski, Rennecke, PRL 127 (2021) 152302

T=114 MeV &  $\mu_B$ =630 MeV



T=160 MeV &  $\mu_B$ =0 MeV



**Moat regime is not captured quantitatively**

**Pion spectral functions**

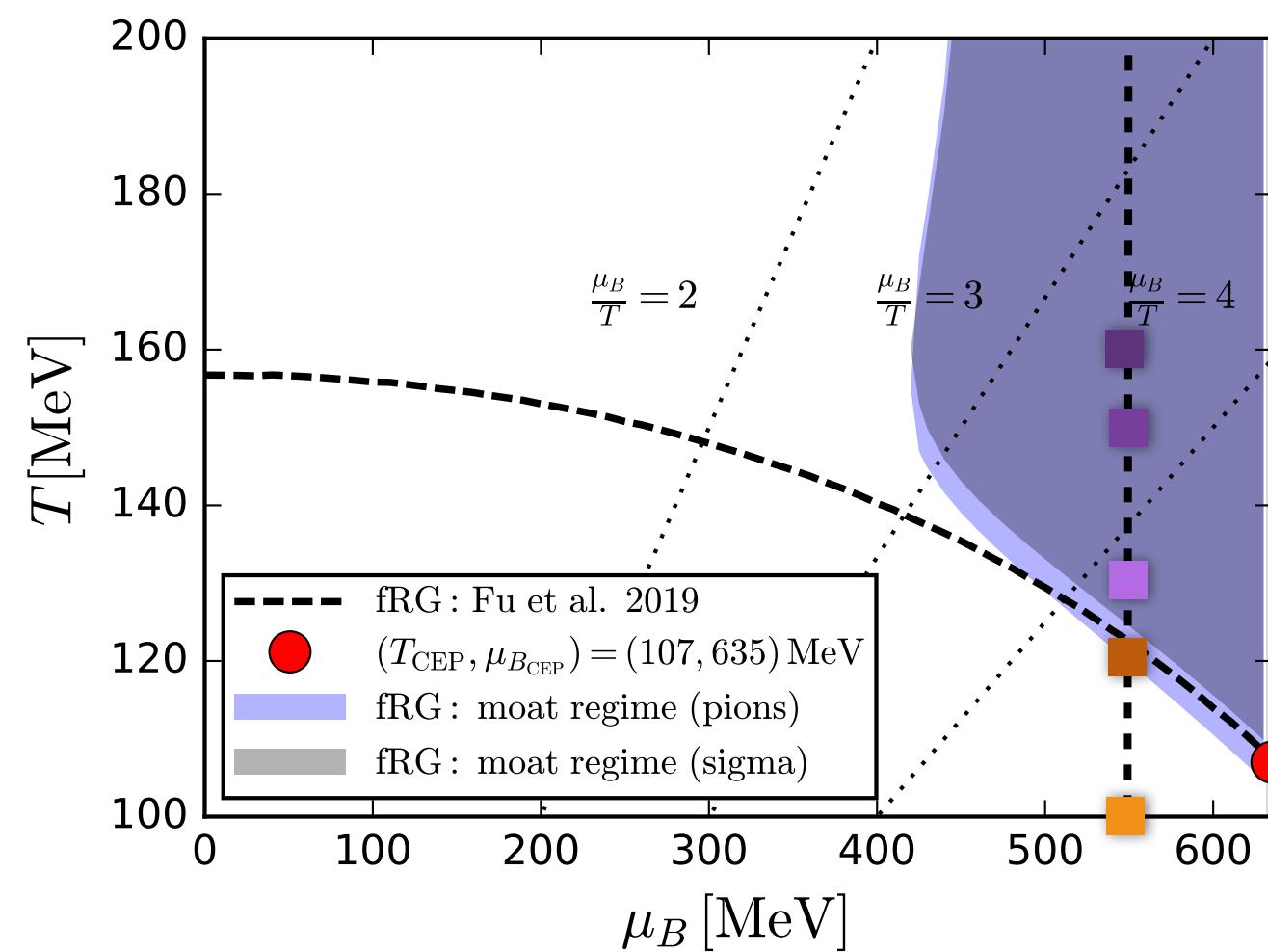
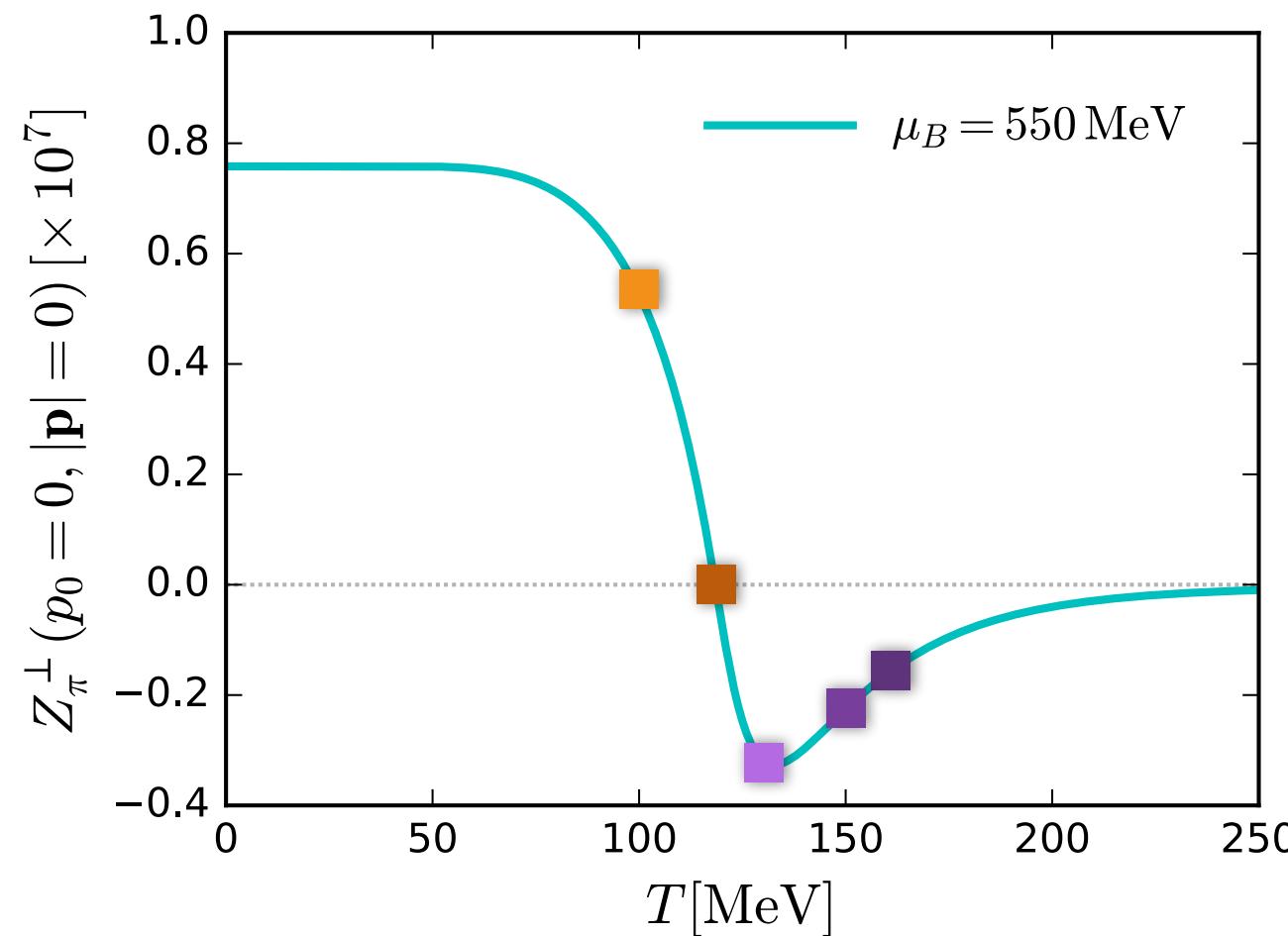
Fu, JMP, Rennecke, PRD 101 (2020) 054032

**Regime of quantitative reliability  
of current best truncation**

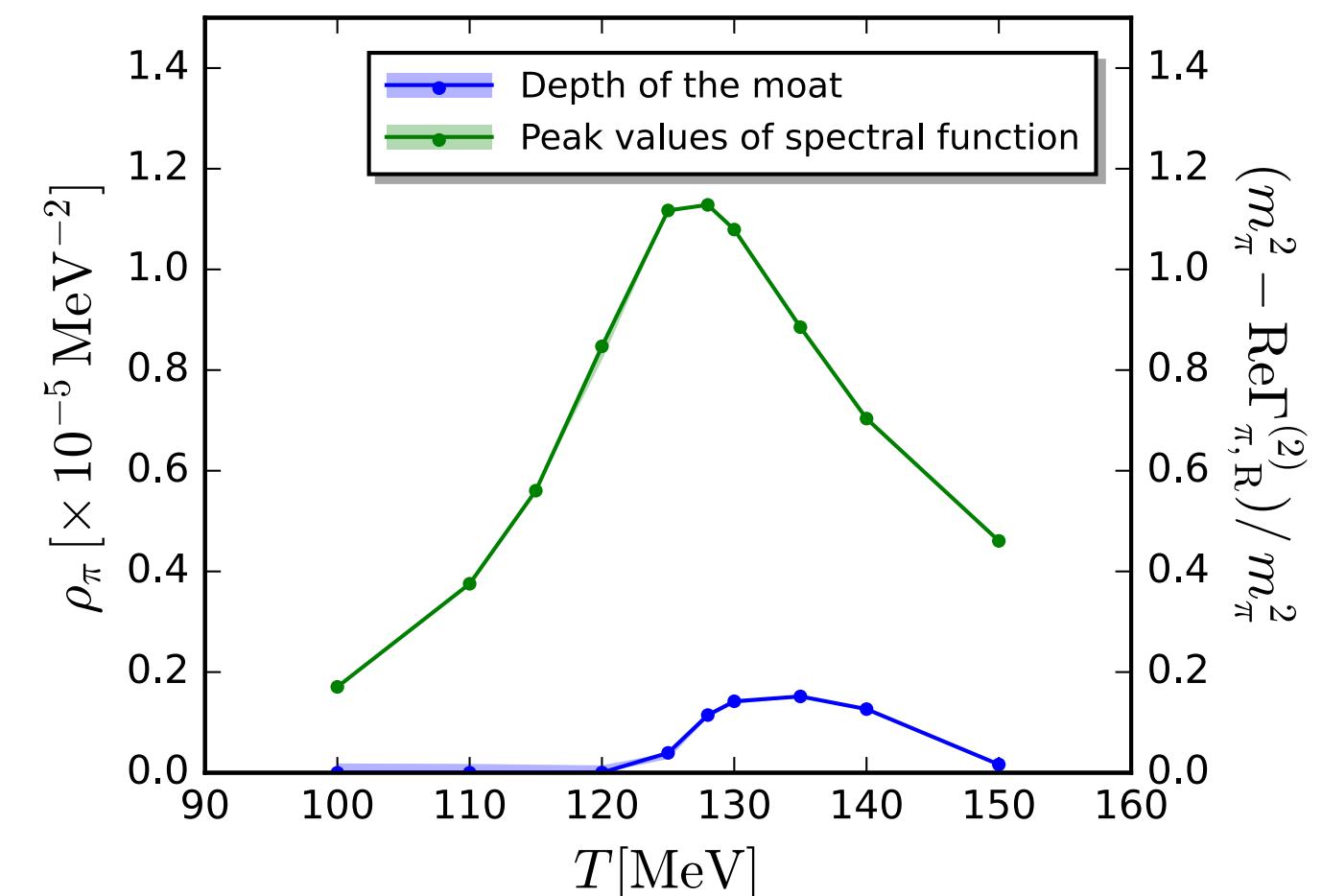


# Predictions & estimates

Spatial wave function of the pion at  $p=0$



Depth of the moat & spectral peak of the pion



Dissecting the moat & the moaton

$\mu_B = 650$  MeV

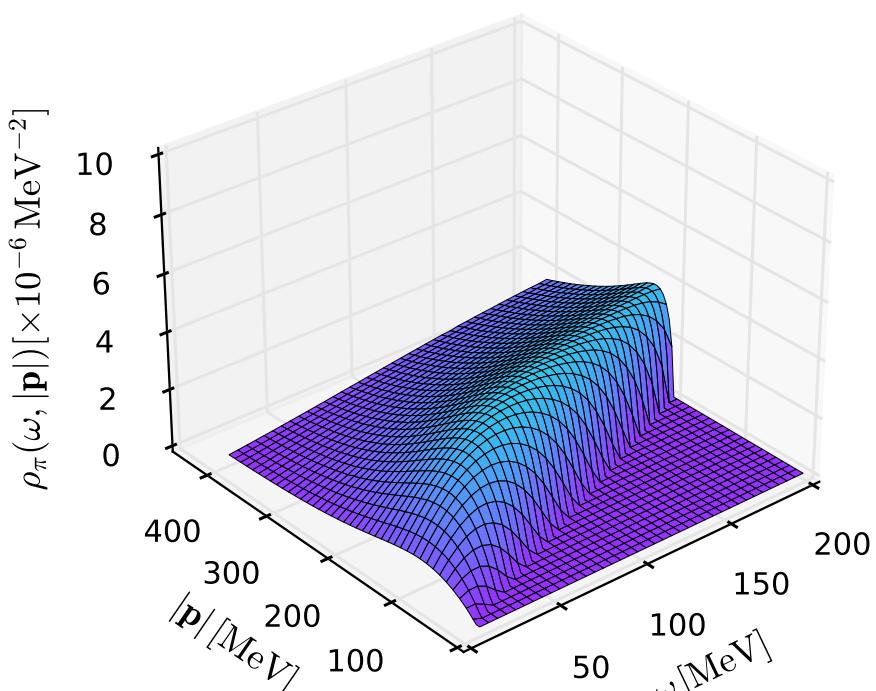
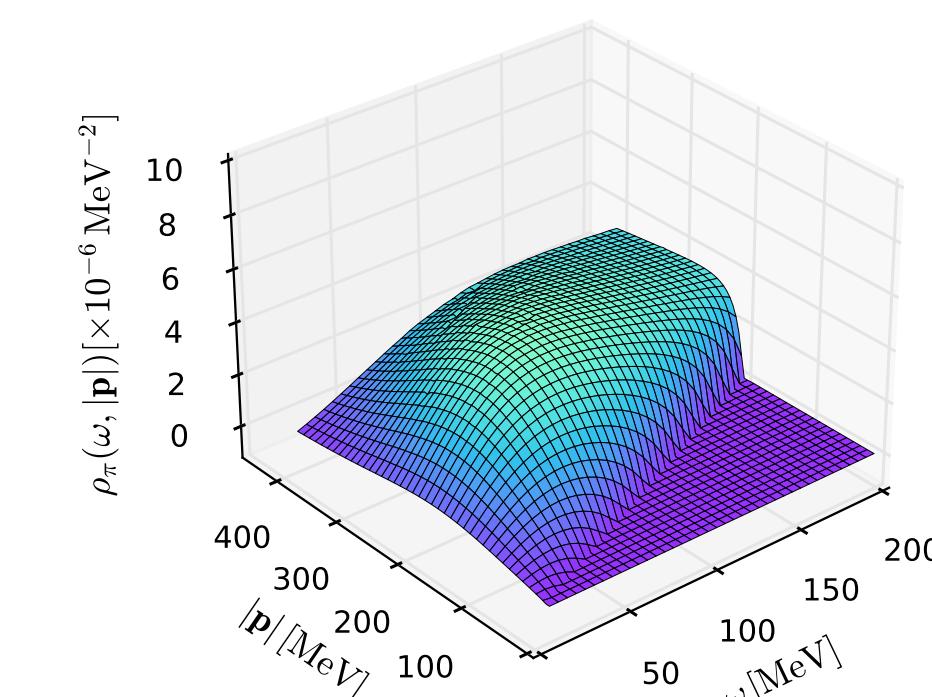
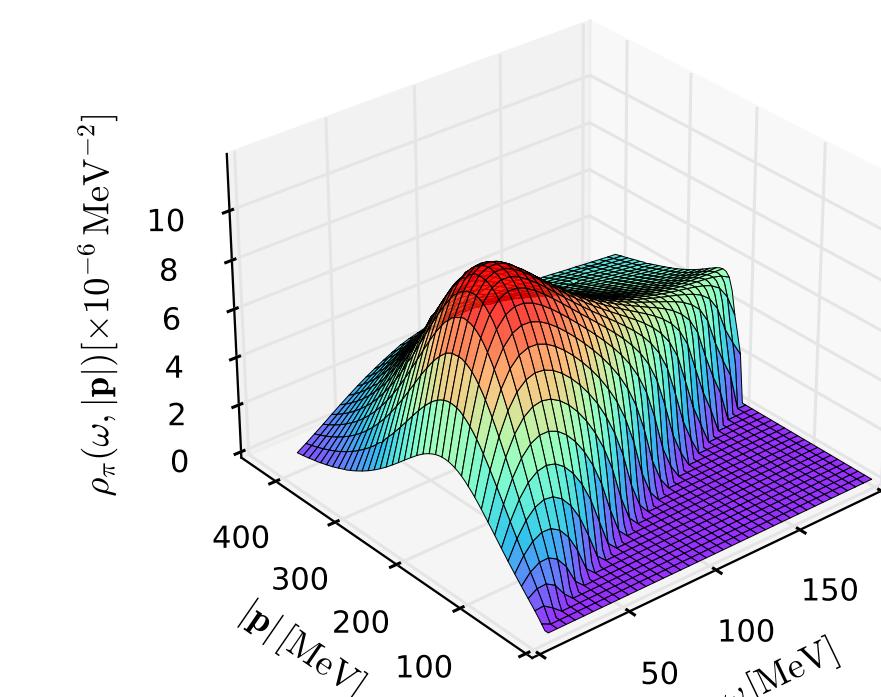
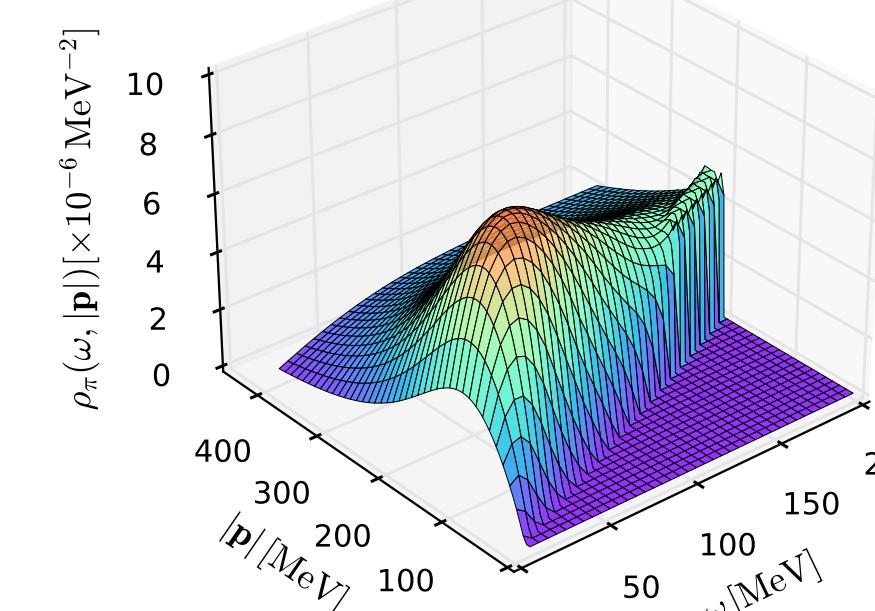
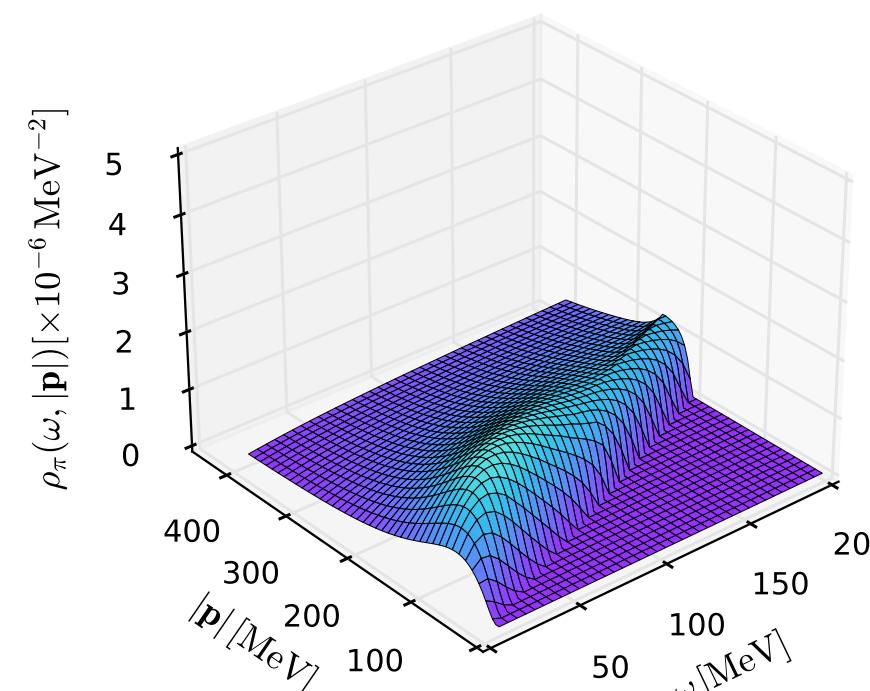
T=100 MeV

T=120 MeV

T=130 MeV

T=150 MeV

T=160 MeV

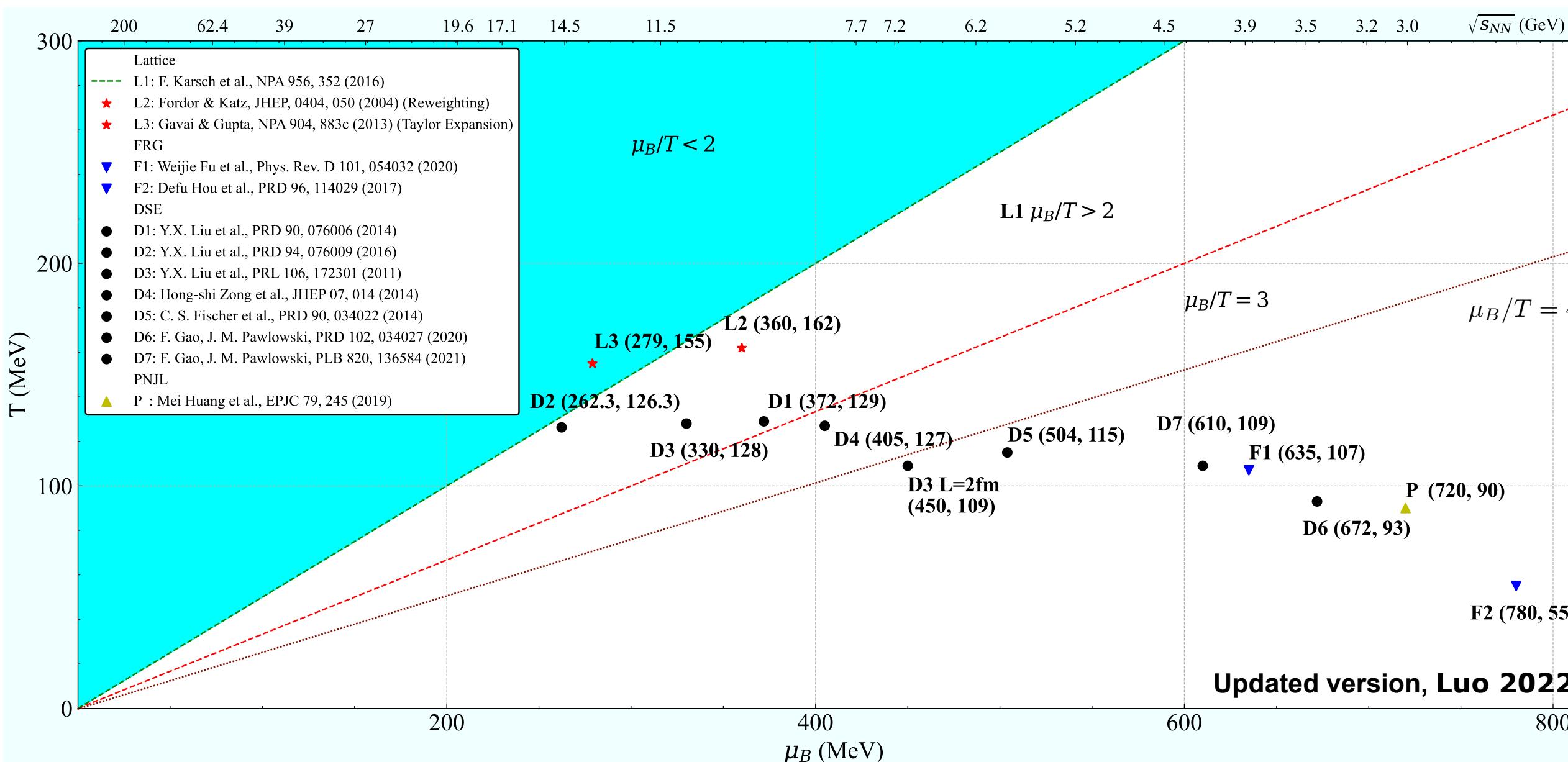


# Predictions, estimates & extrapolations and how to judge them



## Location of CP : Theoretical Prediction

Preliminary collection from Lattice, DSE, FRG and PNJL (2004-2020)



Large uncertainties for the estimation of CP location.

## Disclaimer

Most functional computations (LEFT or QCD) have not been set-up for CEP-predictions!

Lack of predictive power for CEP-predictions is no quality measure!

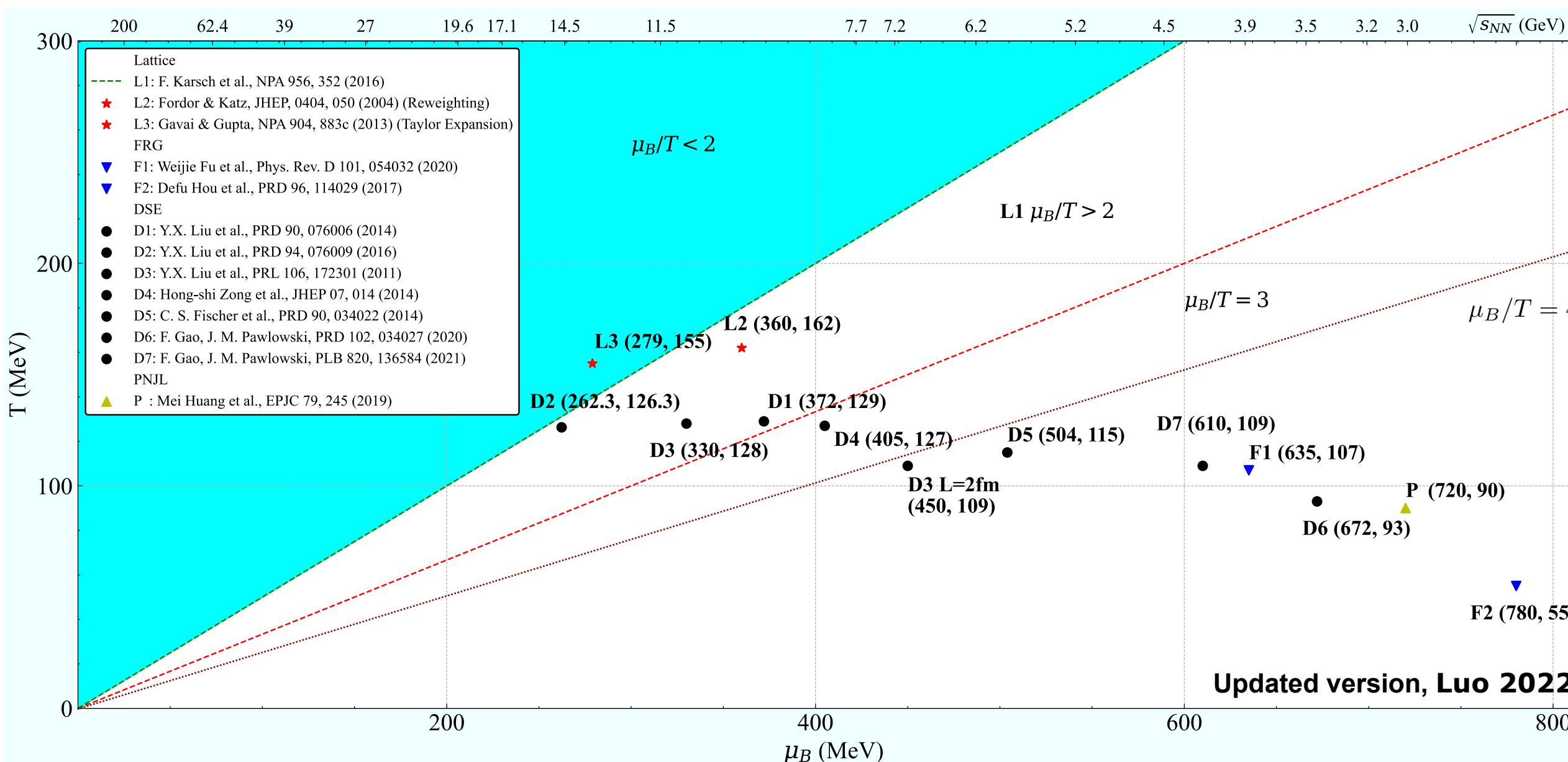
CEP is standing for 'regime with new physics'

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Common folklore  
since ~2004

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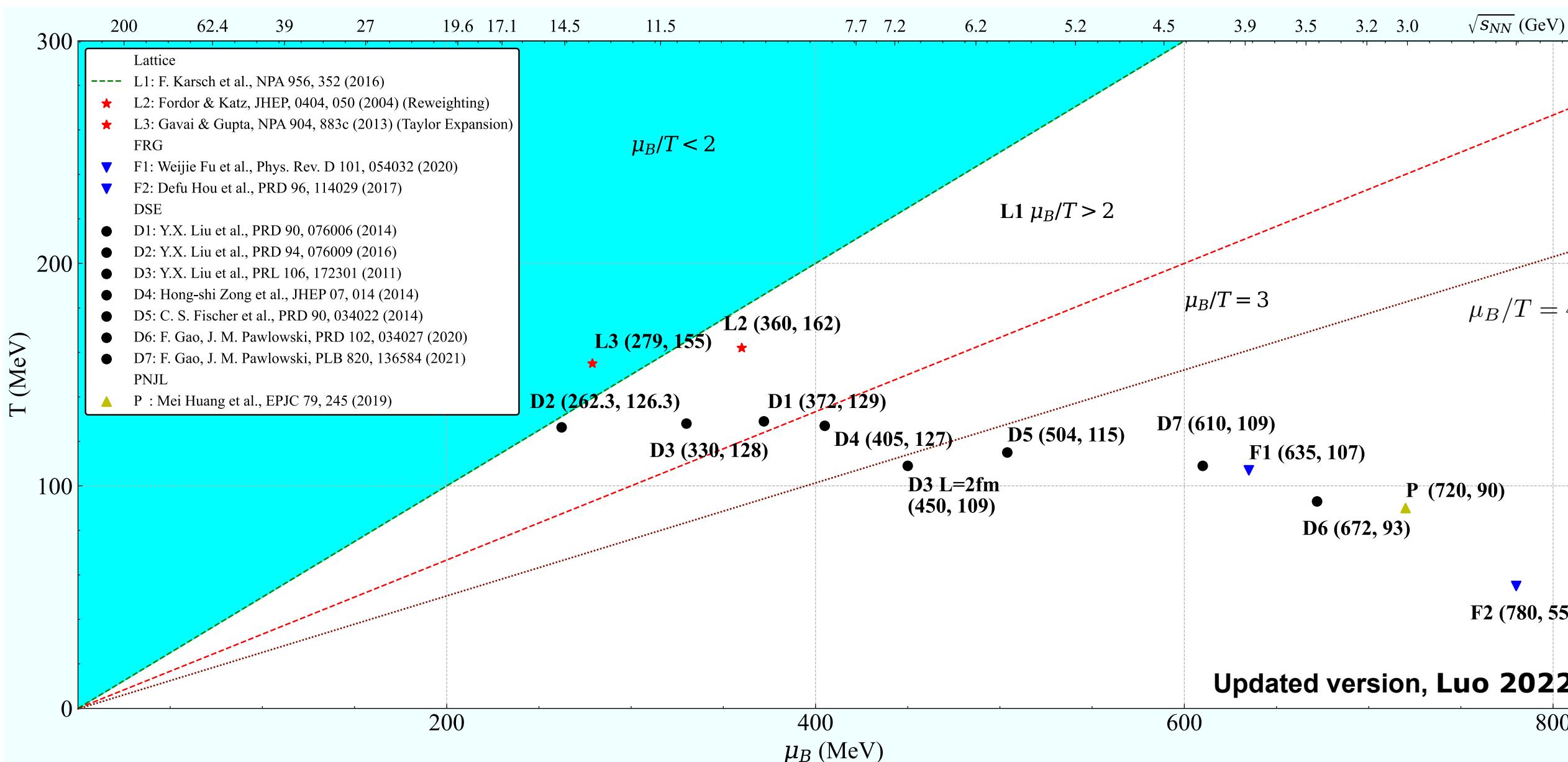
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## Remove CEP-predictions

RHIC-BES Seminar Oct. 6th 2020, Xiaofeng Luo

(i) 'old' CEPs: lattice, Functional QCD approaches, LEFTS (updated computations available)

(ii) LEFTs & Functional Results (qualitative approximations) that miss lattice benchmarks at  $\mu_B = 0$

(iii) LEFTs with CEPs at large density (missing quark-gluon back reaction)

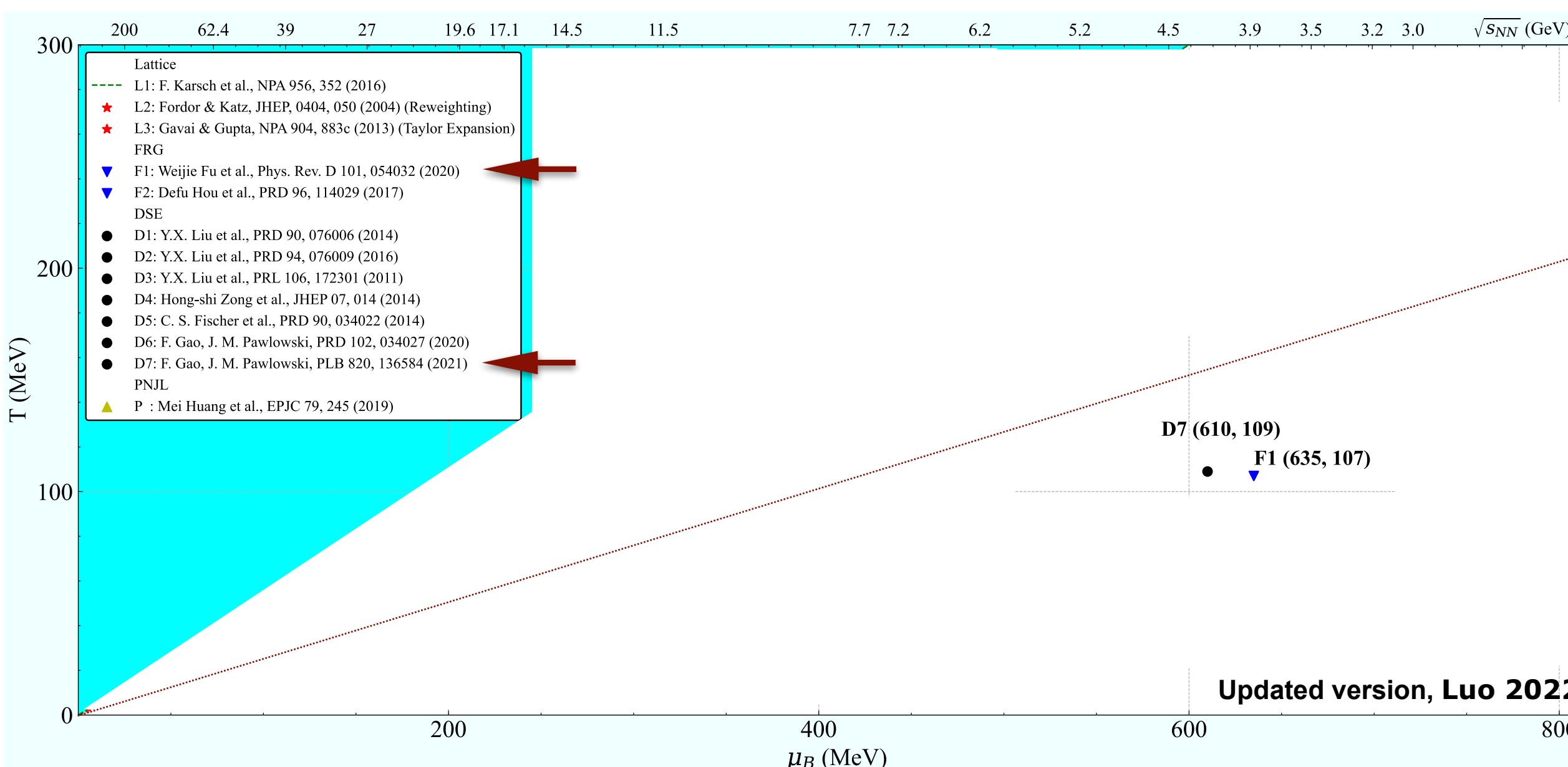
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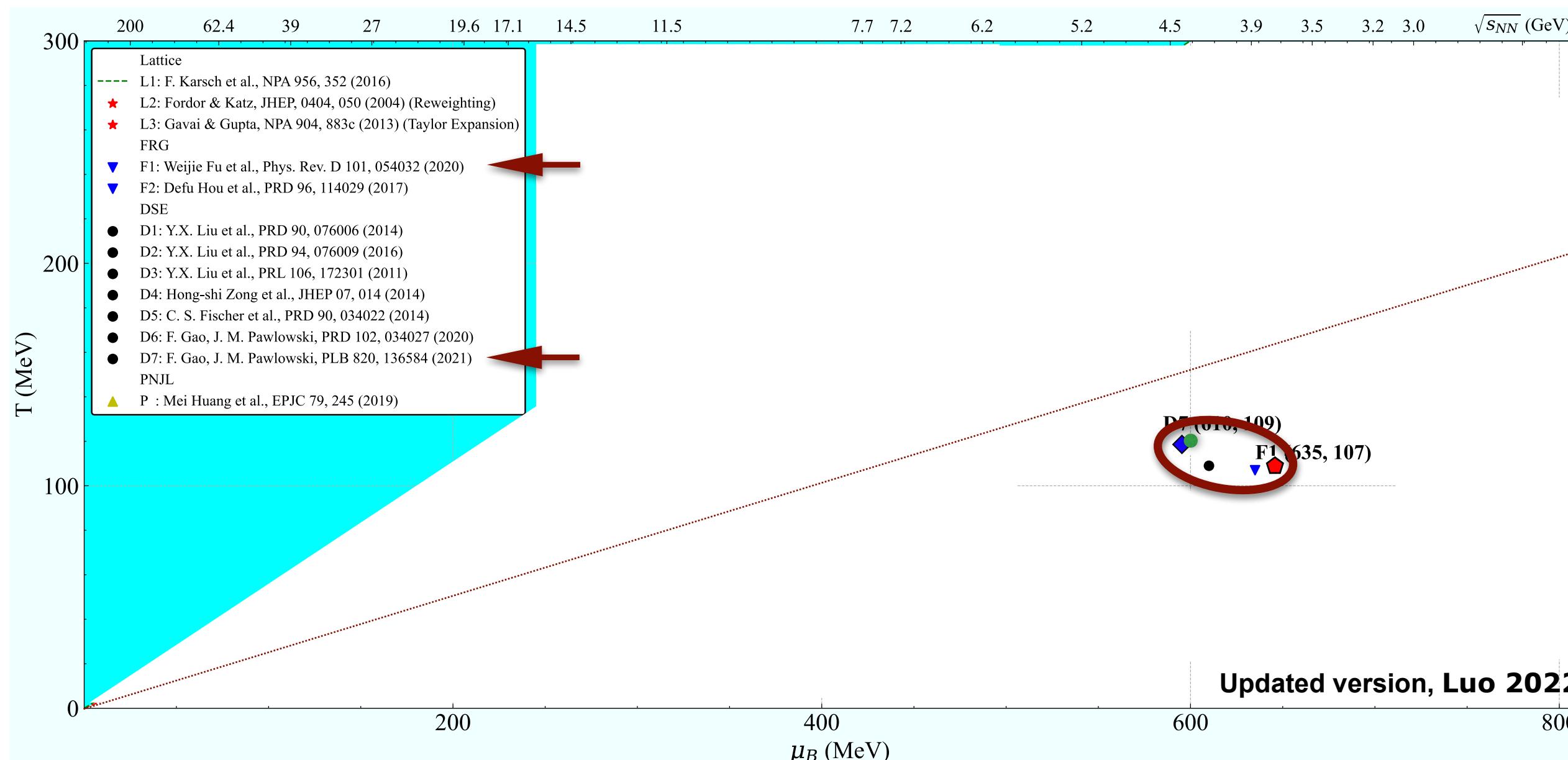


## Location of CP : Theoretical Prediction

Preliminary collection from Lattice, DSE, fRG and PNJL (2004-2023)

### Functional QCD

- ◆ Gao, Lu, JMP, Schneider, in prep (DSE)
- ◆ Fu, JMP, Rennecke, Wen, Yin, in prep (fRG)
- Gunkel, Fischer, PRD 104 (2021) 054022 (DSE)



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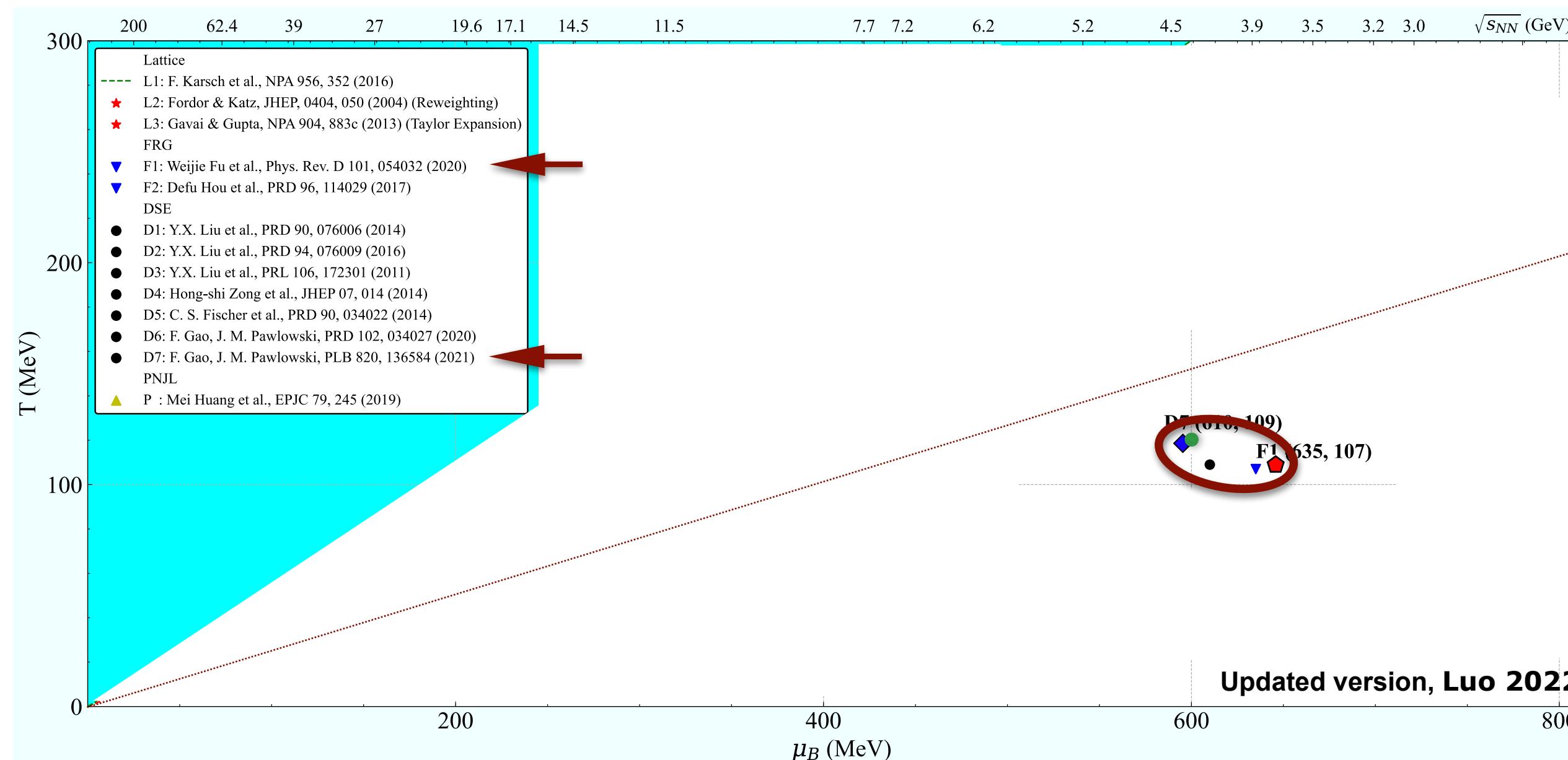


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Still small uncertainties for the estimation of CP location /Onset of new phases

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# Predictions, estimates & extrapolations and how to judge them



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- ◆ Fu, JMP, Rennecke, Wen, Yin, in prep (fRG)
- Gunkel, Fischer, PRD 104 (2021) 054022 (DSE)



### Extrapolations

Lattice extrapolations:

Basar, PRC 110 (2024) 015203

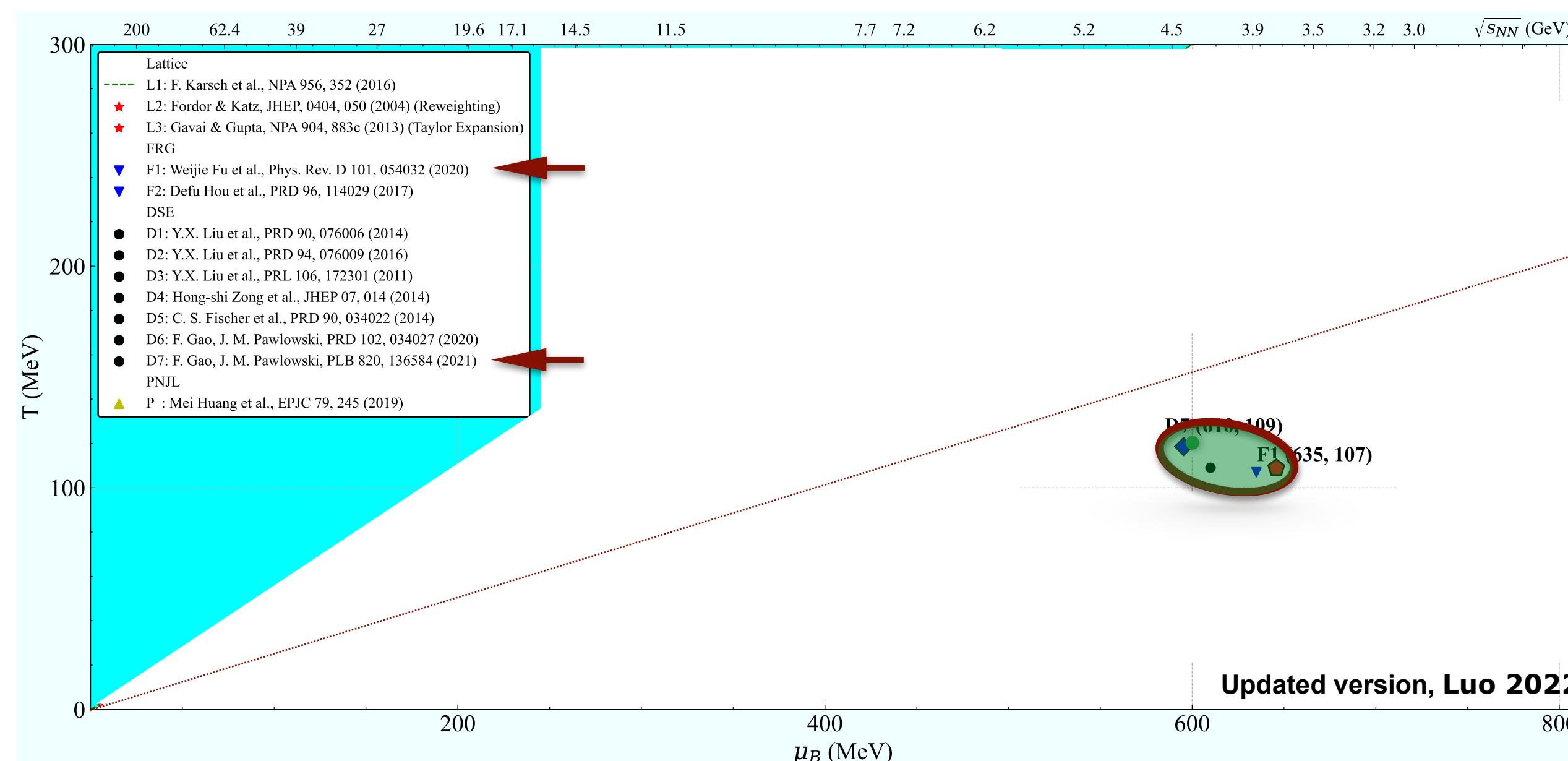
Bielefeld-Parma, arXiv:2405.10196

⋮

Holographic models:

Hippert, Grefa, Manning, Noronha,  
Noronha-Hostler, Portillo Vazquez, Ratti,  
Rougemont, Trujillo, arXiv: 2309.00579

⋮



Still small uncertainties for the estimation of CP location /Onset of new phases

## Remove CEP-predictions

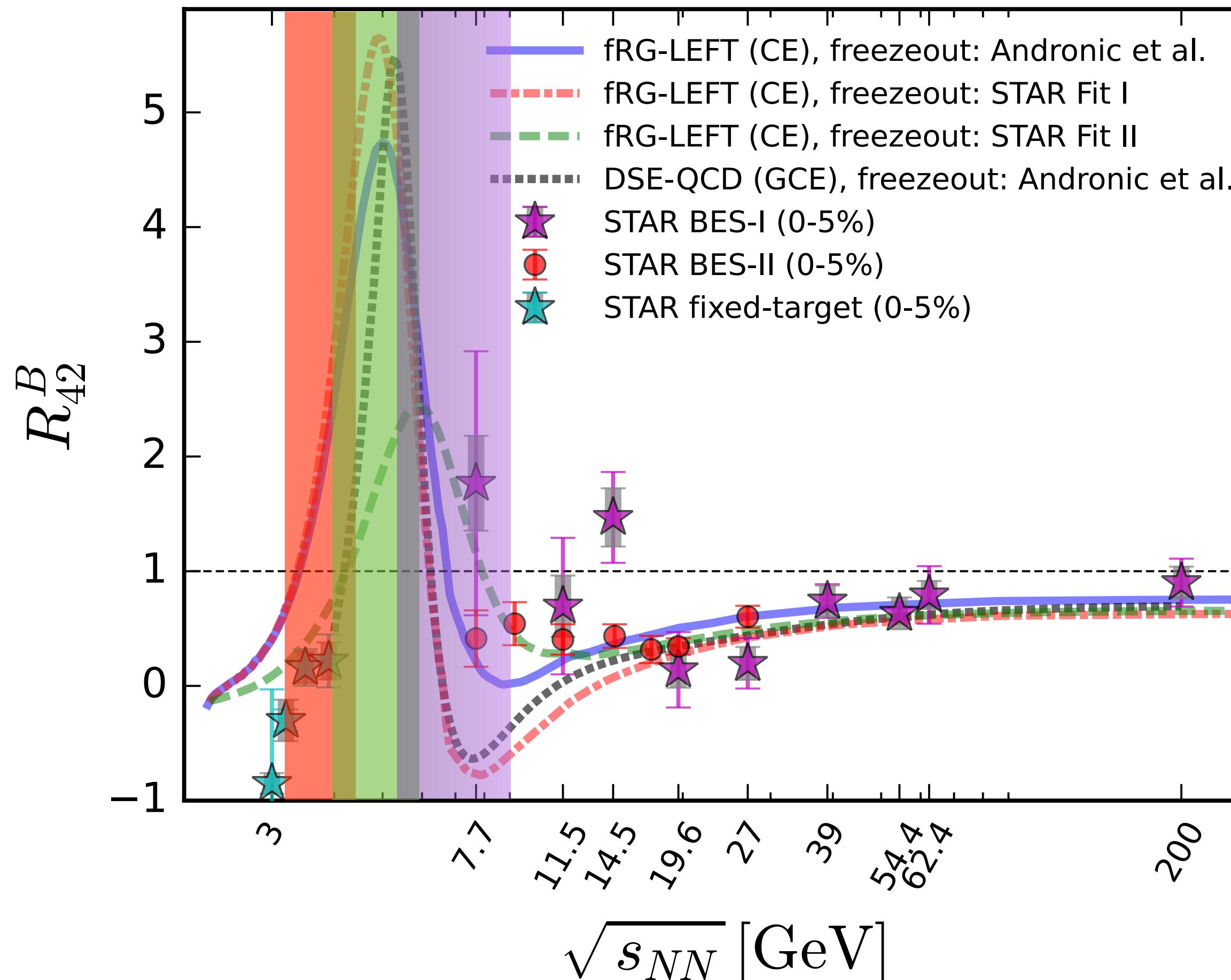
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# Ripples of the critical point

net-baryon fluctuations in QCD vs net-proton fluctuations at STAR



Dominated by non-critical soft modes

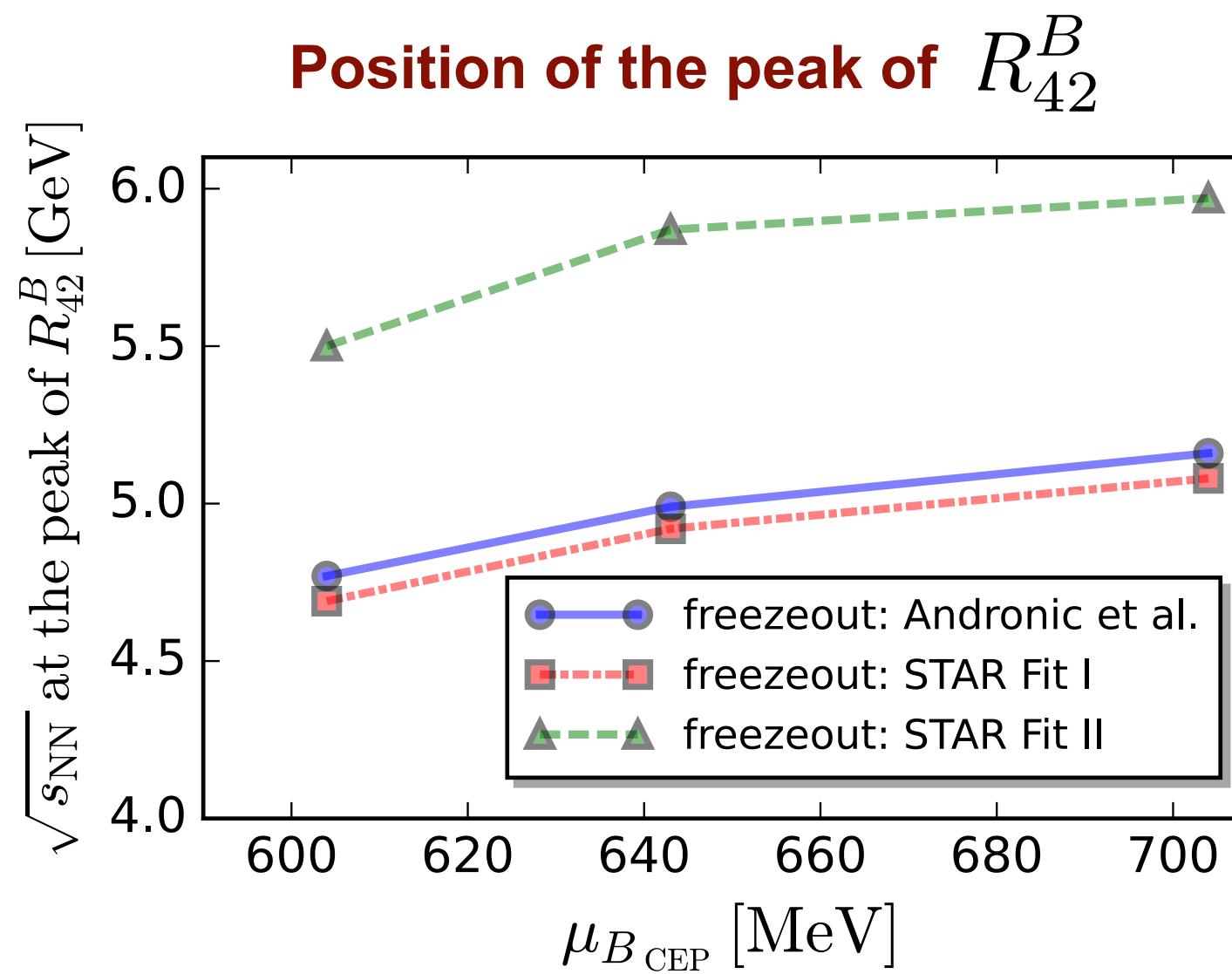
Results:  
1<sup>st</sup> principles functional QCD computations  
& low energy effective theories/extrapolations  
explicit & implicit assumptions

Fu, Luo, JMP, Rennecke, Wen, Yin, PRD 104 (2021) 9

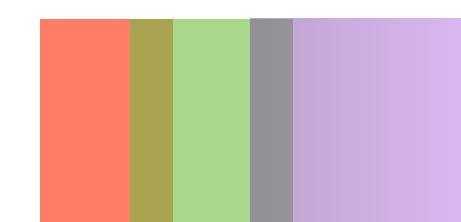
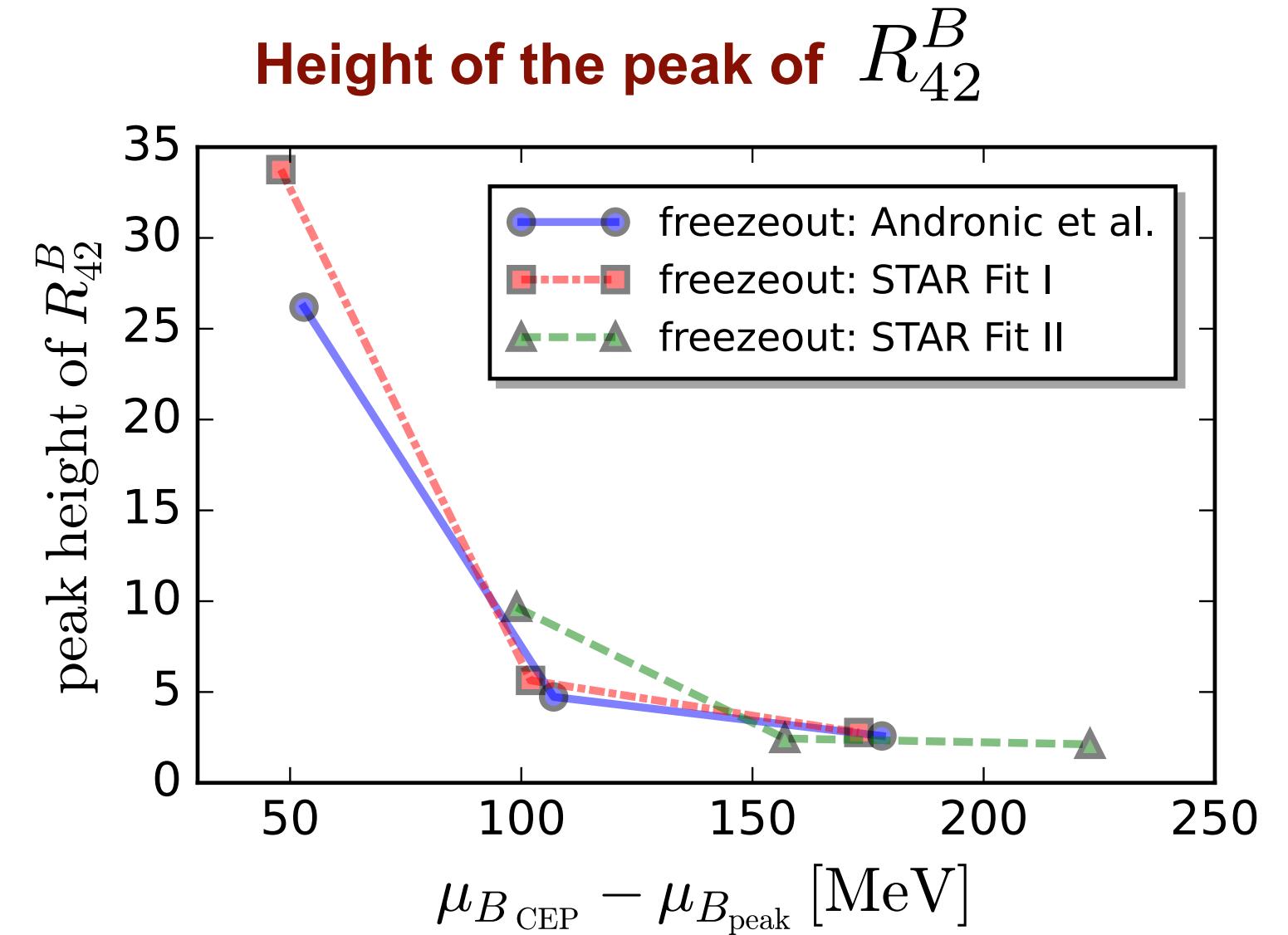
Fu, Luo, JMP, Rennecke, Yin, PRD 111, L031502

Lu, Gao, Liu, JMP, arXiv:2504.05099

# Ripples of the critical point



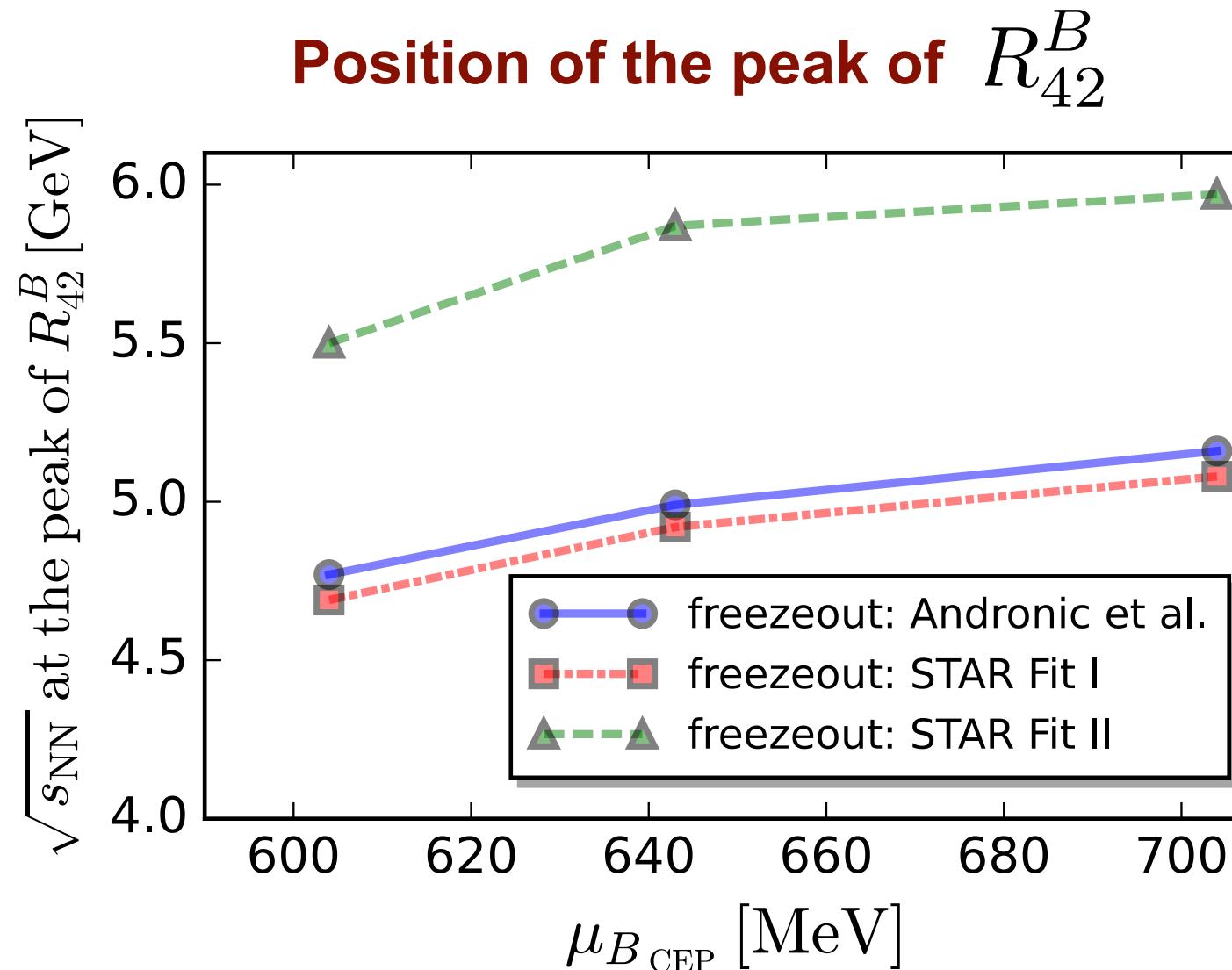
Reconstructing the CEP



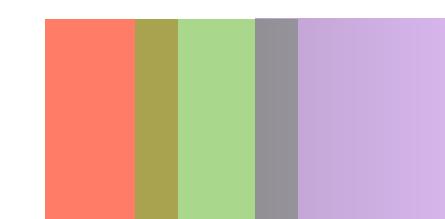
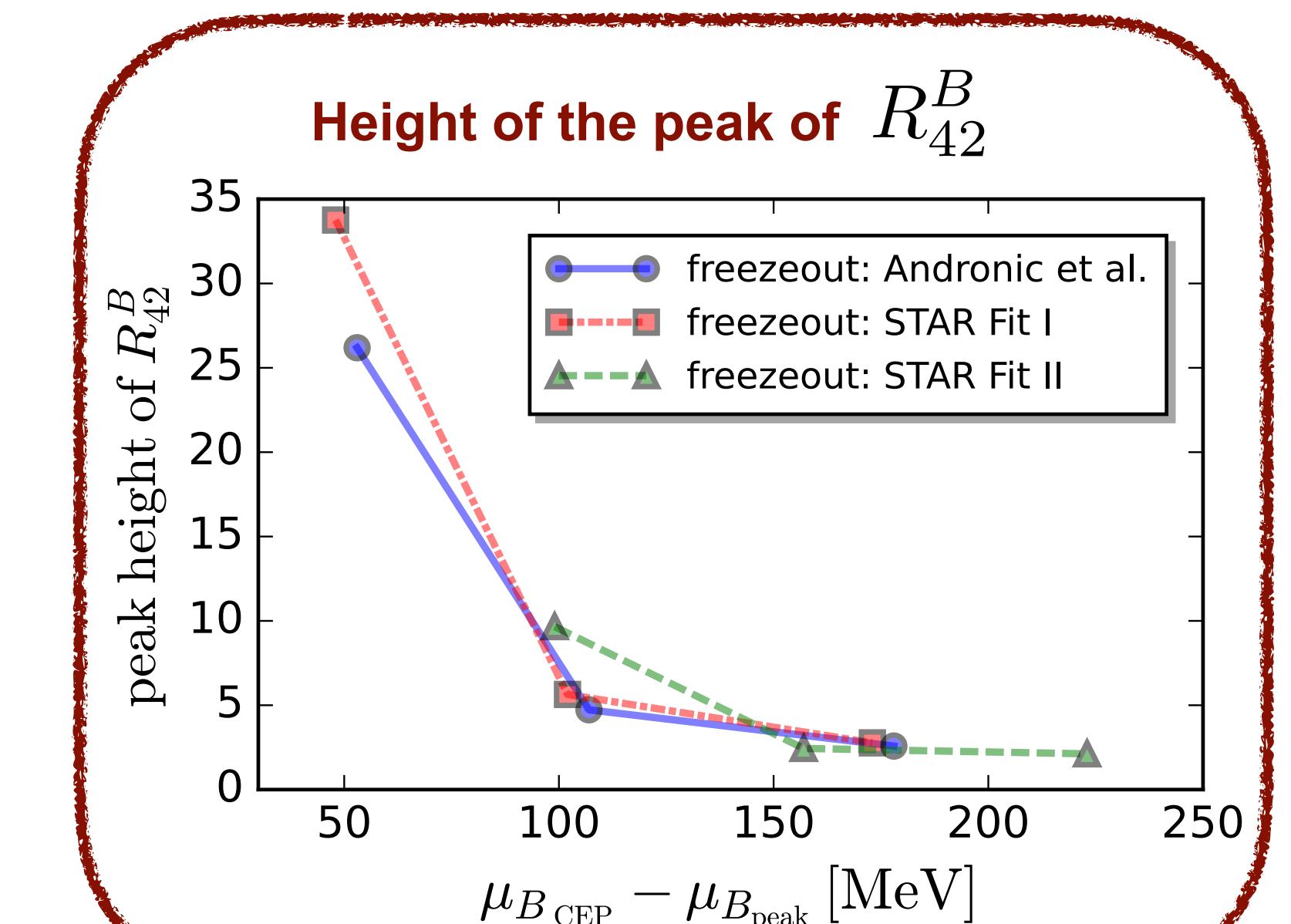
Dominated by non-critical soft modes

**Demand: Precise freeze-out line at high density**

# Ripples of the critical point



Reconstructing the CEP

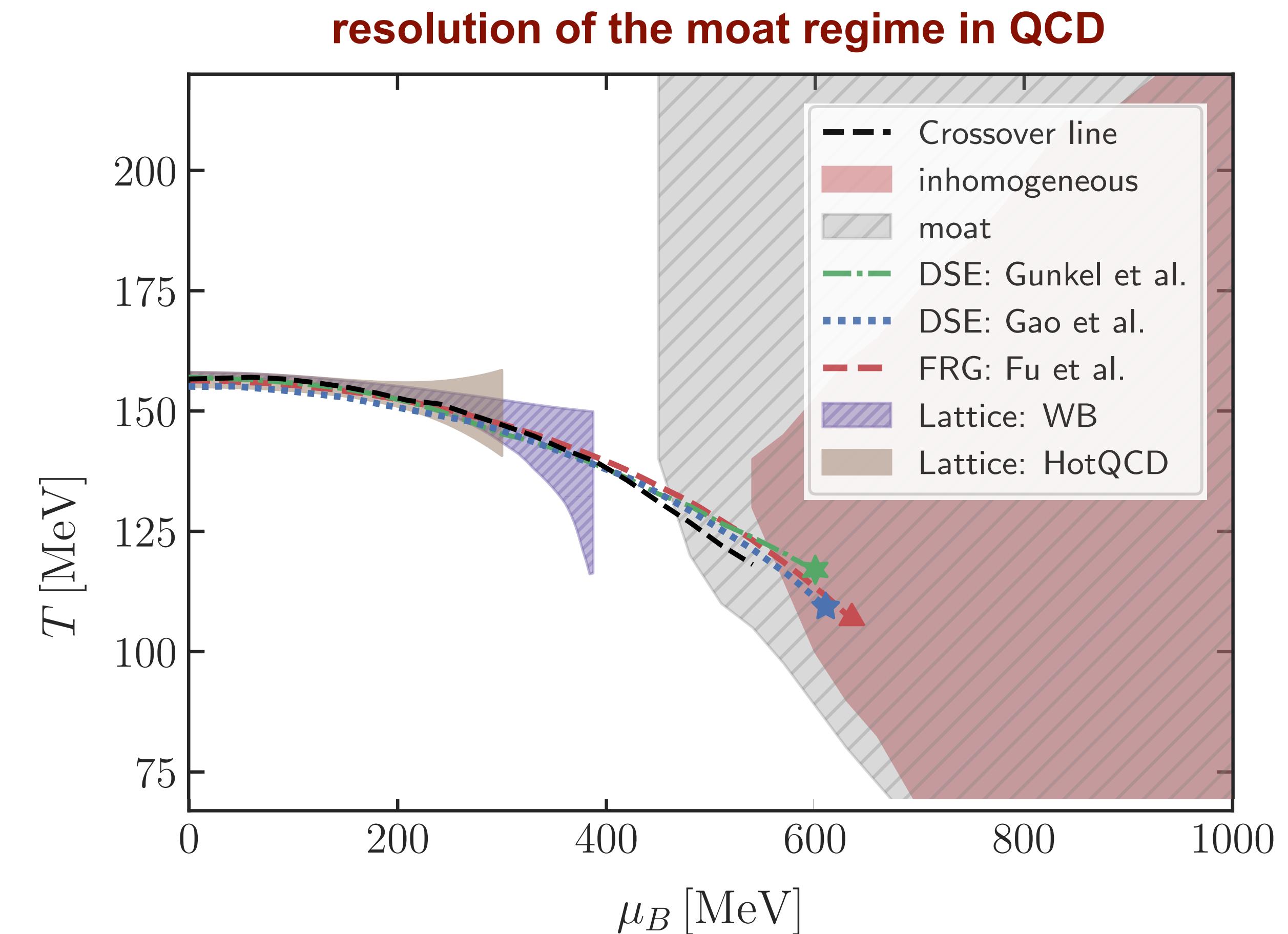
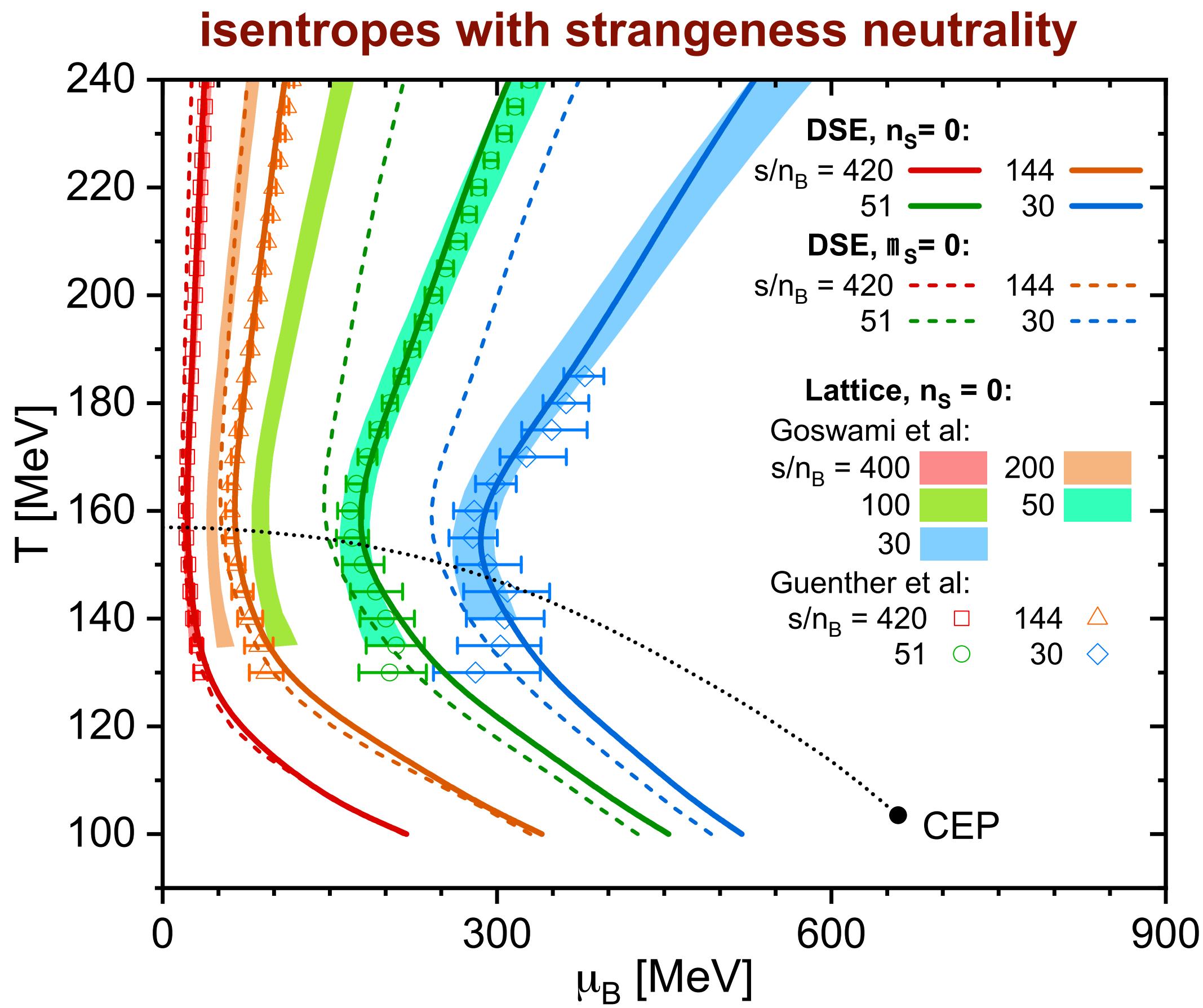


Dominated by non-critical soft modes

Unfolding the high density regime with new phases & physics

Great opportunity for a combined high precision analysis of high density QCD (Exp. data + lattice QCD + functional QCD)

# Ripples of the critical point: Sneak preview



Lu, Gao, Liu, JMP, arXiv:2504.05099 & in preparation

JMP, Rennecke, Sattler, in preparation

# QCD phase structure at finite density: Facts & Fiction

## Facts

- Chiral crossover at about

$$T_\chi \approx 155 \text{ MeV}$$

- Strongly correlated phase for temperatures

$$T_\chi \lesssim T \lesssim 2T_\chi$$

- No chiral critical end point for

$$\mu_B \lesssim 600 \text{ MeV}$$

- No chiral crossover for

$$\mu_B \gtrsim 700 \text{ MeV}$$

$$\mu_B = 0$$

- Physical QCD is in the chiral scaling regime

Chiral scaling regimes are very small  $m_\pi \lesssim 10 \text{ MeV}$

Soft modes are commonplace

- Confinement crossover is at XXX

$$T_\chi \lesssim T_{\text{conf}} \lesssim 2T_\chi$$

$$\mu_B \neq 0$$

- There is a CEP

Onset of new phases  $600 \text{ MeV} \lesssim \mu_B^{\text{onset}} \lesssim 700 \text{ MeV}$

- Scaling regime (Ising) of the CEP is humongous

No, it is not! Most likely: too small to be measured

## Fiction