

Direct detection signatures of standard and non-standard WIMPs

Eugenio Del Nobile

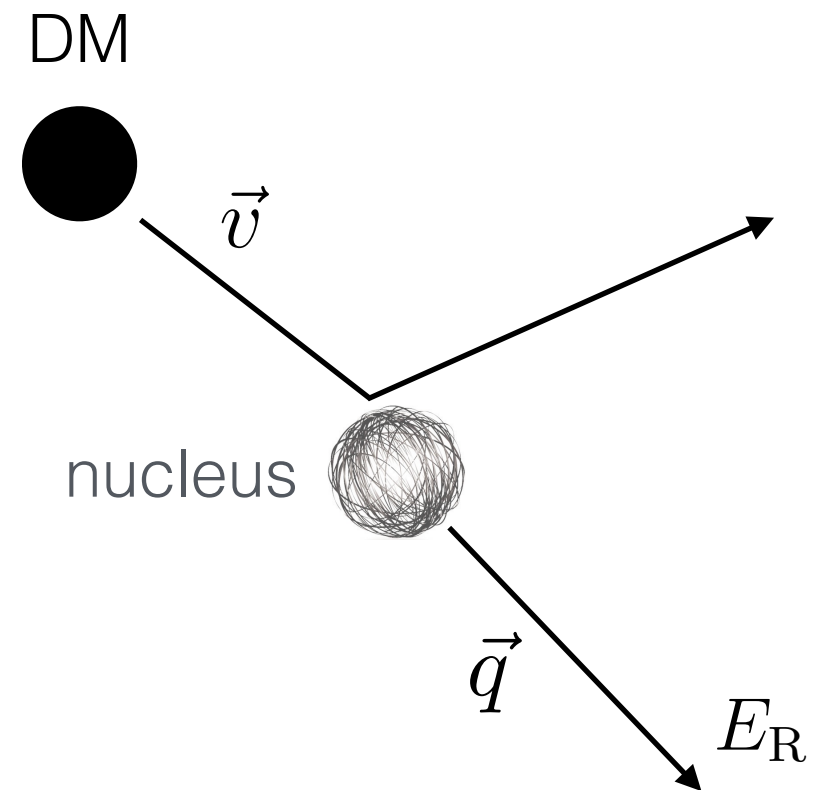
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Basics of direct detection



For halo DM, $v \sim 300 \text{ km/s} \sim 10^{-3} c$

$1/q \sim O(\text{fm})$: the interaction occurs with the whole nucleus

WIMP here = any stable particle detectable with direct searches (mass $\geq \text{GeV}$)

Scattering rate

The basic ingredient is the nuclear recoil rate

$$\frac{dR_T}{dE_R} = \frac{\xi_T}{m_T} \Phi_{\text{DM}}(t) \frac{d\sigma_T}{dE_R}$$

Target density

DM-nucleus
cross section

$$\Phi_{\text{DM}} = \frac{\rho}{m_{\text{DM}}} v f(\vec{v}, t) d^3v$$

DM flux (has an annual modulation due to Earth's rotation around the Sun)

Scattering rate

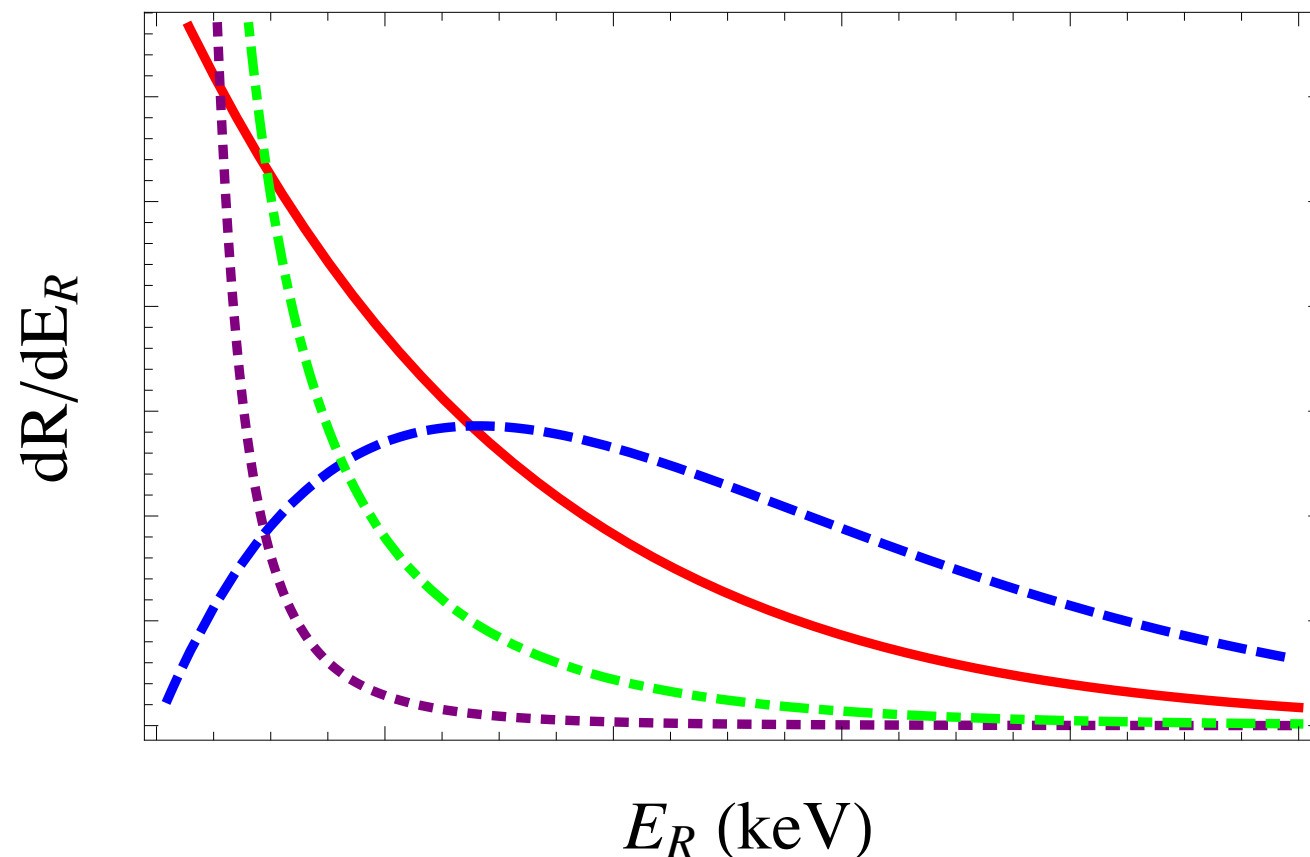
$$\frac{dR_T}{dE_R}(E_R, t) = \frac{\xi_T}{m_T} \frac{\rho}{m_{\text{DM}}} \int_{v \geq v_{\min}(E_R)} d^3v f(\vec{v}, t) v \frac{d\sigma_T}{dE_R}(E_R, \vec{v})$$

ρ DM local density

$f(\vec{v}, t)$ DM velocity distribution

ξ_T target mass fraction

v_{\min} kinematic cutoff



arXiv:1008.1591

Scattering rate

$$\frac{dR_T}{dE_R}(E_R, t) = \frac{\xi_T}{m_T} \frac{\rho}{m_{\text{DM}}} \int_{v \geq v_{\text{min}}(E_R)} d^3v f(\vec{v}, t) v \frac{d\sigma_T}{dE_R}(E_R, \vec{v})$$

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	LHC	Direct Detection
scattering type	deeply inelastic	mostly elastic
mom. transfer q	TeV	MeV
Mandelstam s	integrated (PDF)	integrated (f)
Mandelstam t	observed (p_T)	observed ($E_R \sim q \sim v_{\text{min}}$)

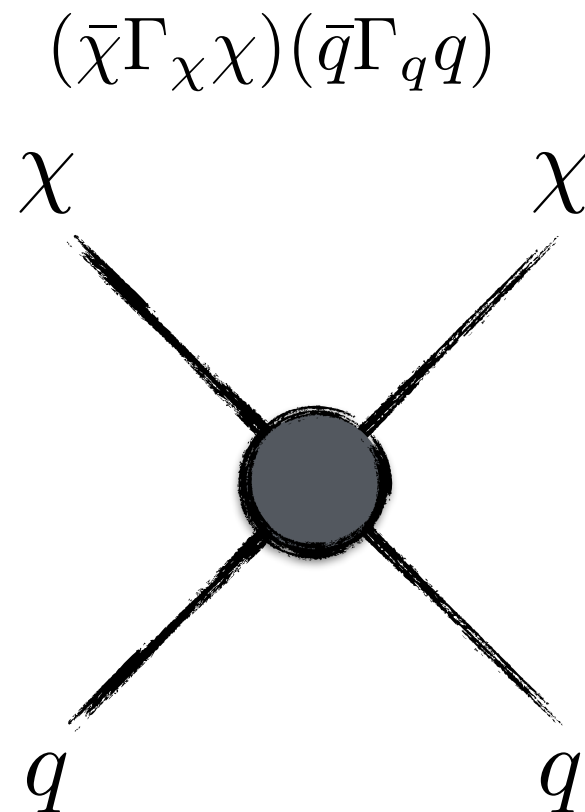
From theory to experiment

1. Write your favorite DM model in terms of interactions with **nucleons**
2. $v \sim 10^{-3} \implies$ **non-relativistic** expansion of the scattering amplitude
3. Compute the **DM-nucleus** cross section (including form factors)

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Example

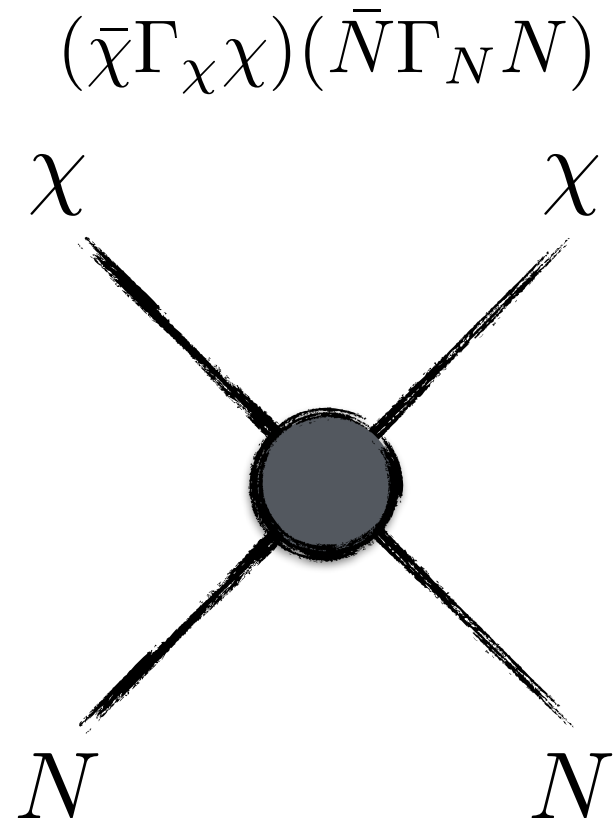


Γ_{χ}	Γ_q
γ^{μ}	γ_{μ}
$\gamma^{\mu}\gamma^5$	γ_{μ}
γ^{μ}	$\gamma_{\mu}\gamma^5$
$\gamma^{\mu}\gamma^5$	$\gamma_{\mu}\gamma^5$

From theory to experiment

1. Write your favorite DM model in terms of interactions with **nucleons**
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Example



Γ_{χ}	Γ_N	non-relativistic limit
γ^{μ}	γ_{μ}	1
$\gamma^{\mu}\gamma^5$	γ_{μ}	$i\mathbf{s}_{\chi} \cdot (\mathbf{s}_N \times \mathbf{q}), \mathbf{s}_{\chi} \cdot \mathbf{v}^{\perp}$
γ^{μ}	$\gamma_{\mu}\gamma^5$	$i\mathbf{s}_{\chi} \cdot (\mathbf{s}_N \times \mathbf{q}), \mathbf{s}_N \cdot \mathbf{v}^{\perp}$
$\gamma^{\mu}\gamma^5$	$\gamma_{\mu}\gamma^5$	$\mathbf{s}_{\chi} \cdot \mathbf{s}_N$
γ^5	γ^5	$(\mathbf{s}_{\chi} \cdot \mathbf{q})(\mathbf{s}_N \cdot \mathbf{q})$

↪ pion exchange

From theory to experiment

1. Write your favorite DM model in terms of interactions with **nucleons**
2. $v \sim 10^{-3} \implies$ **non-relativistic** expansion of the scattering amplitude
3. Compute the **DM-nucleus** cross section (including form factors)

Result

The non-relativistic amplitude is Galilean invariant at leading order

Ingredients

(Galilean invariant, hermitian)

$$i\mathbf{q}, \mathbf{v}^\perp, \mathbf{s}_N, \mathbf{s}_\chi$$

Exercise

Combine the ingredients in all possible rotationally-invariant ways

Non-relativistic theory

spin-0 DM

$$H_N = \sum_i c_i^N(q^2, v^\perp{}^2) O_i$$

$$O_1 \equiv \mathbb{1}$$

$$O_3 \equiv i\mathbf{s}_N \cdot (\mathbf{q} \times \mathbf{v}^\perp)$$

$$O_7 \equiv \mathbf{s}_N \cdot \mathbf{v}^\perp$$

$$O_{10} \equiv i\mathbf{s}_N \cdot \mathbf{q}$$

Non-relativistic theory

spin-1/2 DM

$$H_N = \sum_i c_i^N(q^2, v^\perp{}^2) O_i$$

$$O_1 \equiv \mathbb{1}$$

$$O_3 \equiv i\mathbf{s}_N \cdot (\mathbf{q} \times \mathbf{v}^\perp)$$

$$O_5 \equiv i\mathbf{s}_\chi \cdot (\mathbf{q} \times \mathbf{v}^\perp)$$

$$O_7 \equiv \mathbf{s}_N \cdot \mathbf{v}^\perp$$

$$O_9 \equiv i\mathbf{s}_\chi \cdot (\mathbf{s}_N \times \mathbf{q})$$

$$O_{11} \equiv i\mathbf{s}_\chi \cdot \mathbf{q}$$

$$O_{13} \equiv i(\mathbf{s}_\chi \cdot \mathbf{v}^\perp)(\mathbf{s}_N \cdot \mathbf{q})$$

$$O_{15} \equiv [\mathbf{s}_\chi \cdot (\mathbf{q} \times \mathbf{v}^\perp)](\mathbf{s}_N \cdot \mathbf{q})$$

$$O_{17} \equiv i[\mathbf{s}_\chi \cdot (\mathbf{q} \times \mathbf{v}^\perp)](\mathbf{s}_N \cdot \mathbf{v}^\perp)$$

$$O_4 \equiv \mathbf{s}_\chi \cdot \mathbf{s}_N$$

$$O_6 \equiv (\mathbf{s}_\chi \cdot \mathbf{q})(\mathbf{s}_N \cdot \mathbf{q})$$

$$O_8 \equiv \mathbf{s}_\chi \cdot \mathbf{v}^\perp$$

$$O_{10} \equiv i\mathbf{s}_N \cdot \mathbf{q}$$

$$O_{12} \equiv \mathbf{v}^\perp \cdot (\mathbf{s}_\chi \times \mathbf{s}_N)$$

$$O_{14} \equiv i(\mathbf{s}_\chi \cdot \mathbf{q})(\mathbf{s}_N \cdot \mathbf{v}^\perp)$$

$$O_{16} \equiv (\mathbf{s}_\chi \cdot \mathbf{v}^\perp)(\mathbf{s}_N \cdot \mathbf{v}^\perp)$$

Non-relativistic theory

spin-1 DM

$$H_N = \sum_i c_i^N(q^2, v^\perp{}^2) O_i$$

$$O_1 \equiv \mathbb{1}$$

$$O_3 \equiv i\mathbf{s}_N \cdot (\mathbf{q} \times \mathbf{v}^\perp)$$

$$O_5 \equiv i\mathbf{s}_\chi \cdot (\mathbf{q} \times \mathbf{v}^\perp)$$

$$O_7 \equiv \mathbf{s}_N \cdot \mathbf{v}^\perp$$

$$O_9 \equiv i\mathbf{s}_\chi \cdot (\mathbf{s}_N \times \mathbf{q})$$

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+ others...

Hierarchies I: nuclear spin

$$O_1, O_5, O_8, O_{11}$$

All nucleons interact equal

Spin independent: coherent enhancement $d\sigma_T \sim \mathcal{O}(A^2) \lesssim 10^4$

(however v^\perp factors can imply a coupling to the nuclear spin)

$$O_3, O_4, O_6, O_7, O_9, O_{10}, O_{12}, O_{13}, O_{14}, O_{15}, O_{16}, O_{17}$$

Opposite spins cancel pairwise

Spin dependent: coherent cancellation $d\sigma_T \sim \mathcal{O}(A^0) \sim 1$

Hierarchies II: DM speed

$$\frac{q^2}{4\mu_T^2} = v_{\min}^2 \leq v^2 \sim 10^{-6}$$

$$\frac{d\sigma_T}{dE_R} \sim \frac{|\langle O_i \rangle|^2}{v^2}$$

O_1, O_4	$\sim \mathcal{O}(v^0)$	$d\sigma_T \sim \mathcal{O}(v^{-2})$
$O_7, O_8, O_9, O_{10}, O_{11}, O_{12}$	$\sim \mathcal{O}(v^1)$	$d\sigma_T \sim \mathcal{O}(v^0)$
$O_3, O_5, O_6, O_{13}, O_{14}, O_{16}$	$\sim \mathcal{O}(v^2)$	$d\sigma_T \sim \mathcal{O}(v^2)$
O_{15}, O_{17}	$\sim \mathcal{O}(v^3)$	$d\sigma_T \sim \mathcal{O}(v^4)$

(however $(\mathbf{q} \times \mathbf{s}_\chi) \cdot (\mathbf{q} \times \mathbf{s}_N) = q^2 O_4 - O_6$)

Hierarchies III: EFT cutoff

Some operators appear at tree level at dimension ≤ 6 in the EFT of a singlet Dirac DM. Others...

	Example of EFT operator	dimension
O_3	$-i\varepsilon^{\alpha\mu\nu\rho}[\partial_\rho(\bar{\chi}\gamma_\alpha\chi)][\bar{N}\gamma_\mu\gamma^5\overleftrightarrow{\partial}_\nu N]$	8
O_{13}	$i\bar{\chi}\gamma^\alpha\gamma^5\chi(\bar{N}\gamma^5\overleftrightarrow{\partial}_\alpha N)$	7
O_{14}	$i(\bar{\chi}\gamma^5\overleftrightarrow{\partial}_\mu\chi)\bar{N}\gamma^\mu\gamma^5 N$	7
O_{15}	$\varepsilon^{\alpha\mu\nu\rho}[\partial_\rho(\bar{\chi}\gamma_\alpha\gamma^5\overleftrightarrow{\partial}_\mu\chi)](\bar{N}\gamma^5\overleftrightarrow{\partial}_\nu N)$	9
O_{16}	$-(\bar{\chi}\gamma^\alpha\gamma^5\overleftrightarrow{\partial}_\mu\chi)(\bar{N}\gamma^\mu\gamma^5\overleftrightarrow{\partial}_\alpha N)$	8
O_{17}	$i\varepsilon^{\beta\mu\nu\rho}(\bar{\chi}\sigma_{\alpha\beta}\overleftrightarrow{\partial}_\nu\chi)[(\partial_\alpha\bar{N})\gamma_\mu\overleftrightarrow{\partial}_\rho N - \bar{N}\gamma_\mu\overleftrightarrow{\partial}_\rho(\partial_\alpha N)]$	9

(the dimension can be larger for Majorana DM)

Cross section structure

Type	Lagrangian	NR operators	Nuclear responses	Structure of $\frac{d\sigma_T}{dE_R}$
Spin independent	$\bar{\chi}\chi\bar{N}N$ or $\bar{\chi}\gamma^\mu\chi\bar{N}\gamma_\mu N$	$O_1 = \mathbb{1}$	M	$\frac{[f_n(A-Z) + f_p Z]^2}{v^2}$
Spin dependent	$\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}\gamma_\mu\gamma^5 N$ or $\bar{\chi}\sigma^{\mu\nu}\chi\bar{N}\sigma_{\mu\nu}N$	$O_4 = \mathbf{s}_\chi \cdot \mathbf{s}_N$	$\Sigma' + \Sigma''$	$\frac{(J+1)/J}{v^2}$
Pseudoscalar	$\bar{\chi}\gamma^5\chi\bar{N}\gamma^5 N$	$O_6 = (\mathbf{s}_\chi \cdot \mathbf{q})(\mathbf{s}_N \cdot \mathbf{q})$	Σ''	$q^4 \frac{(J+1)/J}{v^2}$
Millicharge	$Qe\bar{\chi}\gamma^\mu\chi A_\mu$	$O_1 = \mathbb{1}$	M	$\frac{Q^2 Z^2 \alpha^2}{q^4 v^2}$
Electric dipole	$\frac{id}{2}\bar{\chi}\sigma_{\mu\nu}\gamma^5\chi F^{\mu\nu}$	$O_{11} = i\mathbf{s}_\chi \cdot \mathbf{q}$	M	$\frac{d^2 Z^2 \alpha}{q^2 v^2}$
Magnetic dipole	$\frac{\mu}{2}\bar{\chi}\sigma_{\mu\nu}\chi F^{\mu\nu}$	O_1, O_4, O_5, O_6	M, Σ', Δ	$\mu^2 \left[Z^2 \alpha \left(\frac{1}{v_{\min}^2} - \frac{1}{v^2} \right) + \frac{\mu_T^2}{v^2} \right]$
Anapole moment	$\frac{a}{2}\bar{\chi}\gamma^\mu\gamma^5\chi\partial^\nu F_{\mu\nu}$	O_8, O_9	M, Σ', Δ	$E_R a^2 \left[Z^2 \alpha \left(\frac{1}{v_{\min}^2} - \frac{1}{v^2} \right) + \frac{\mu_T^2}{v^2} \right]$

Cross section structure

Majorana DM

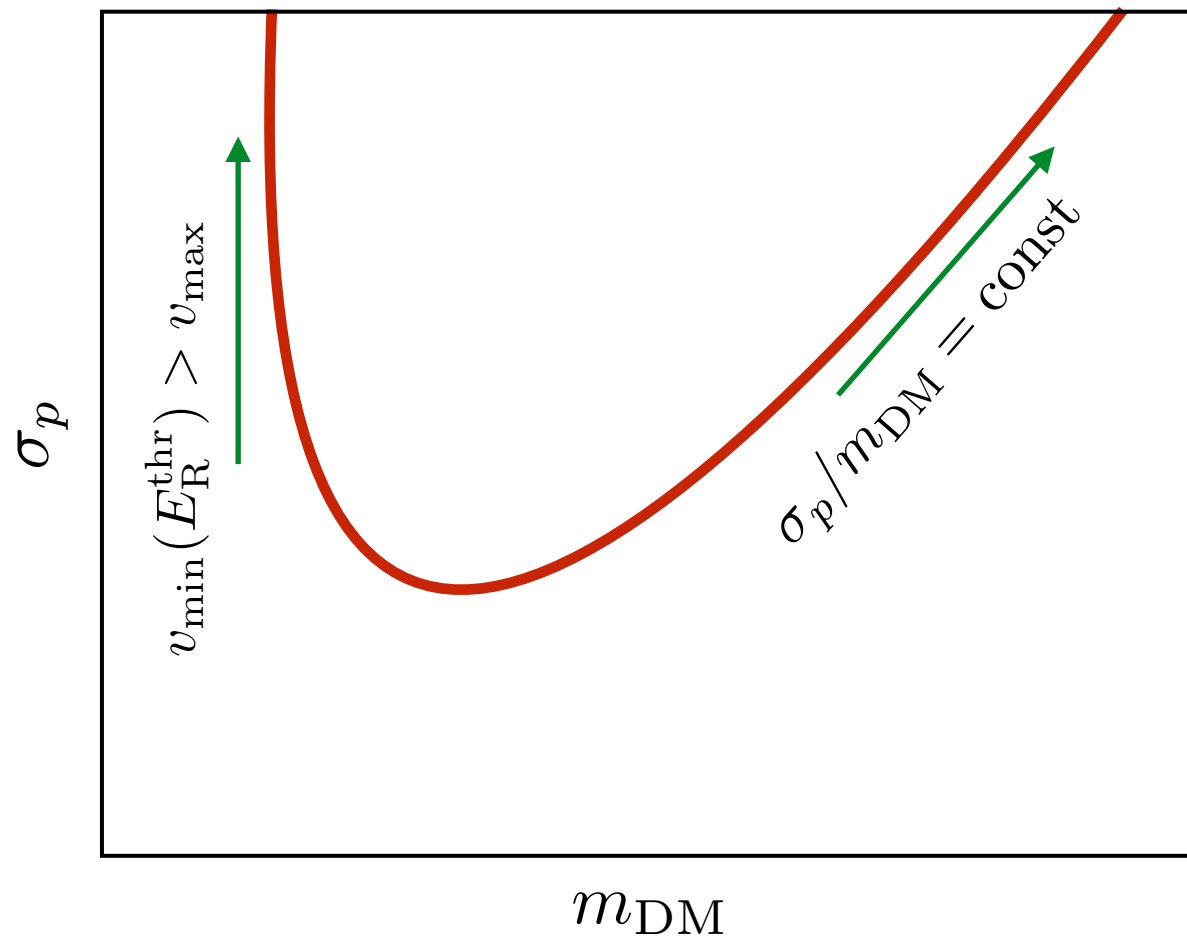
Neutralino

Type	Lagrangian	NR operators	Nuclear responses	Structure of $\frac{d\sigma_T}{dE_R}$
Spin independent	$\bar{\chi}\chi \bar{N}N$ or $\bar{\chi}\gamma^\mu\chi \bar{N}\gamma_\mu N$	$O_1 = \mathbb{1}$	M	$\frac{[f_n(A - Z) + f_p Z]^2}{v^2}$
Spin dependent	$\bar{\chi}\gamma^\mu\gamma^5\chi \bar{N}\gamma_\mu\gamma^5 N$ or $\bar{\chi}\sigma^{\mu\nu}\chi \bar{N}\sigma_{\mu\nu} N$	$O_4 = \mathbf{s}_\chi \cdot \mathbf{s}_N$	$\Sigma' + \Sigma''$	$\frac{(J + 1)/J}{v^2}$
Pseudoscalar	$\bar{\chi}\gamma^5\chi \bar{N}\gamma^5 N$	$O_6 = (\mathbf{s}_\chi \cdot \mathbf{q})(\mathbf{s}_N \cdot \mathbf{q})$	Σ''	$q^4 \frac{(J + 1)/J}{v^2}$
Millicharge	$Qe \bar{\chi}\gamma^\mu\chi A_\mu$	$O_1 = \mathbb{1}$	M	$\frac{Q^2 Z^2 \alpha^2}{q^4 v^2}$
Electric dipole	$\frac{id}{2} \bar{\chi}\sigma_{\mu\nu}\gamma^5\chi F^{\mu\nu}$	$O_{11} = i\mathbf{s}_\chi \cdot \mathbf{q}$	M	$\frac{d^2 Z^2 \alpha}{q^2 v^2}$
Magnetic dipole	$\frac{\mu}{2} \bar{\chi}\sigma_{\mu\nu}\chi F^{\mu\nu}$	O_1, O_4, O_5, O_6	M, Σ', Δ	$\mu^2 \left[Z^2 \alpha \left(\frac{1}{v_{\min}^2} - \frac{1}{v^2} \right) + \frac{\mu_T^2}{v^2} \right]$
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Spin-dependent & spin-independent

$$R \sim \frac{\rho \sigma_p}{m_{\text{DM}}} \int_{E_{\text{R}1}}^{E_{\text{R}2}} \eta_0(v_{\text{min}}(E_{\text{R}})) dE_{\text{R}}$$

$$\eta_0(v_{\text{min}}) \sim \int_{v \geq v_{\text{min}}} \frac{f(\mathbf{v})}{v} d^3v$$



Scattering off Xe in LUX

Spin-dependent vs spin-independent

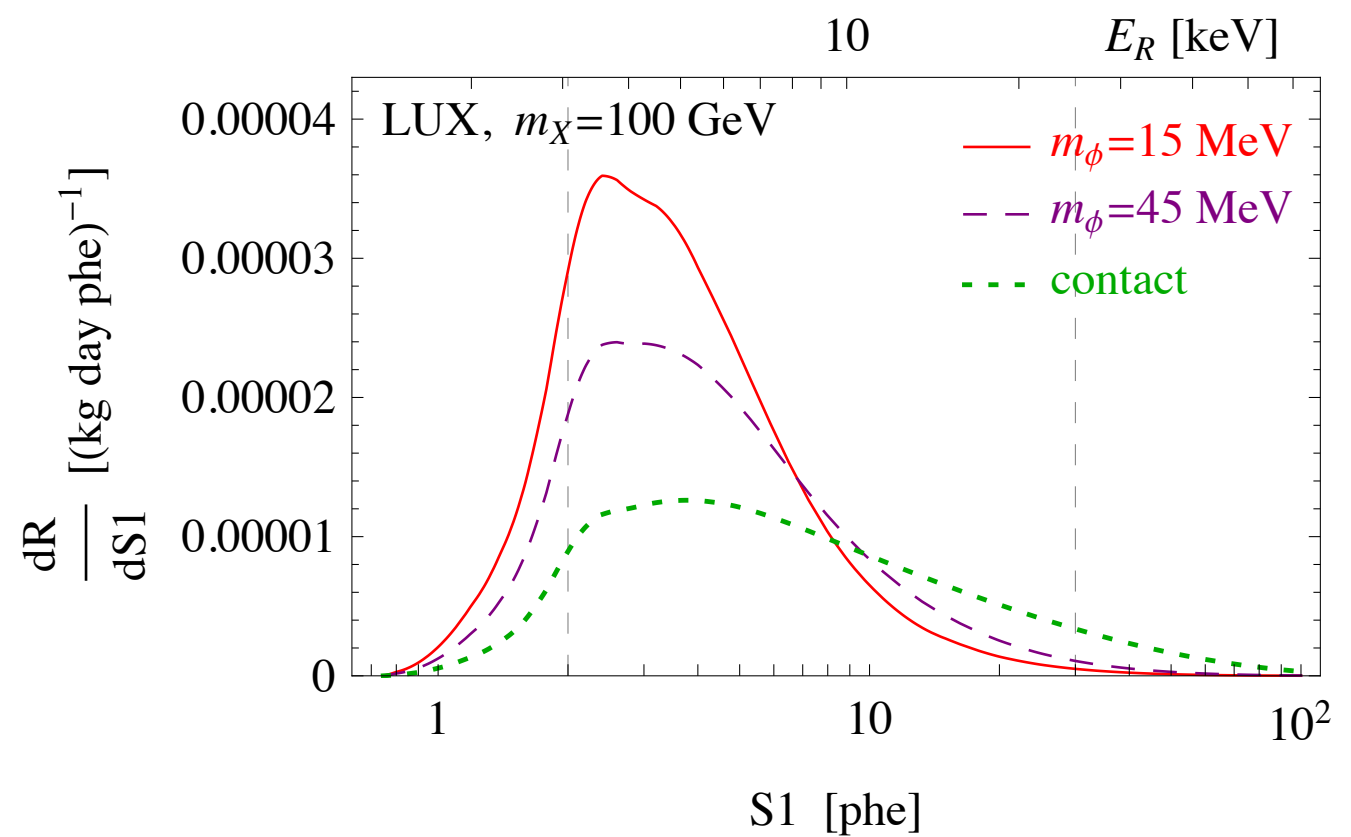
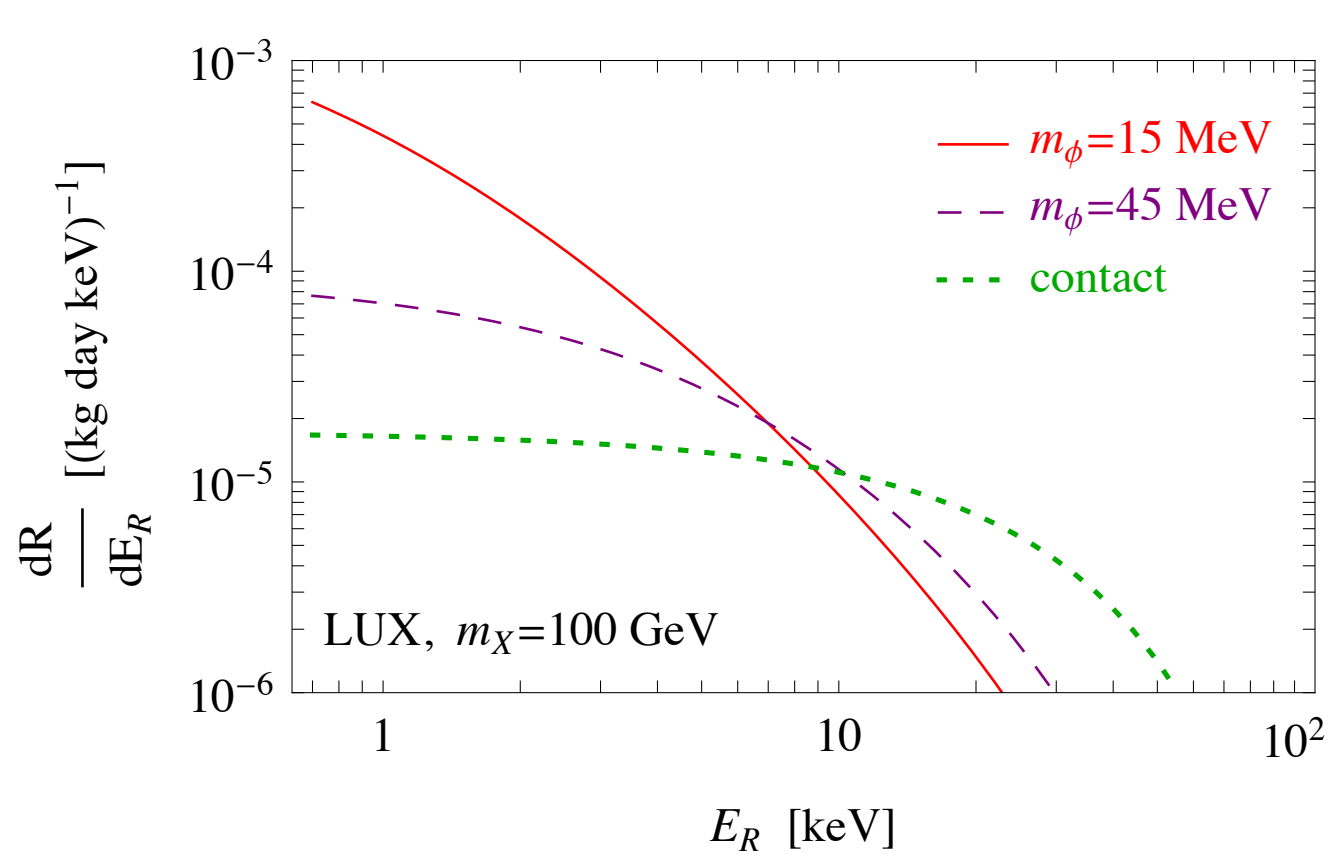
For a given DM mass:

- ✗ Very similar spectrum
- ✗ Identical modulation
- ✓ Different A dependence

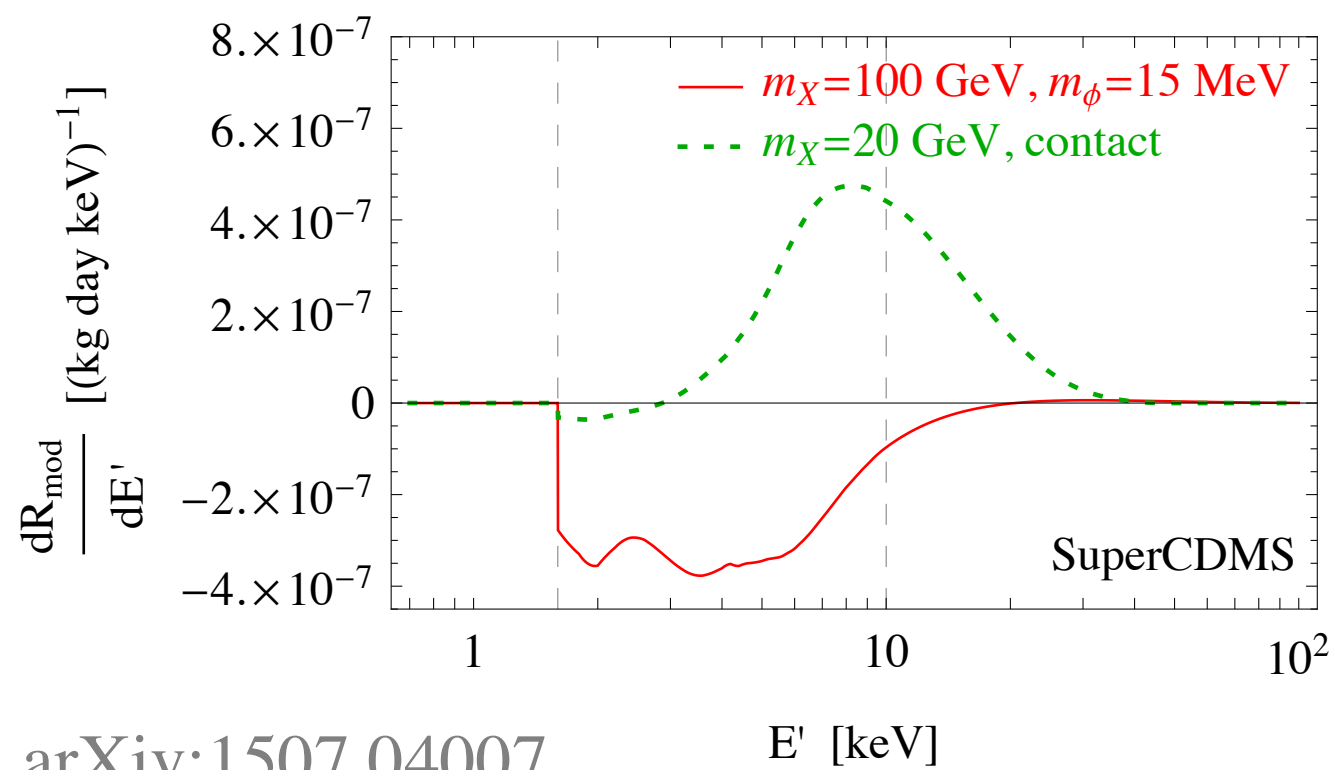
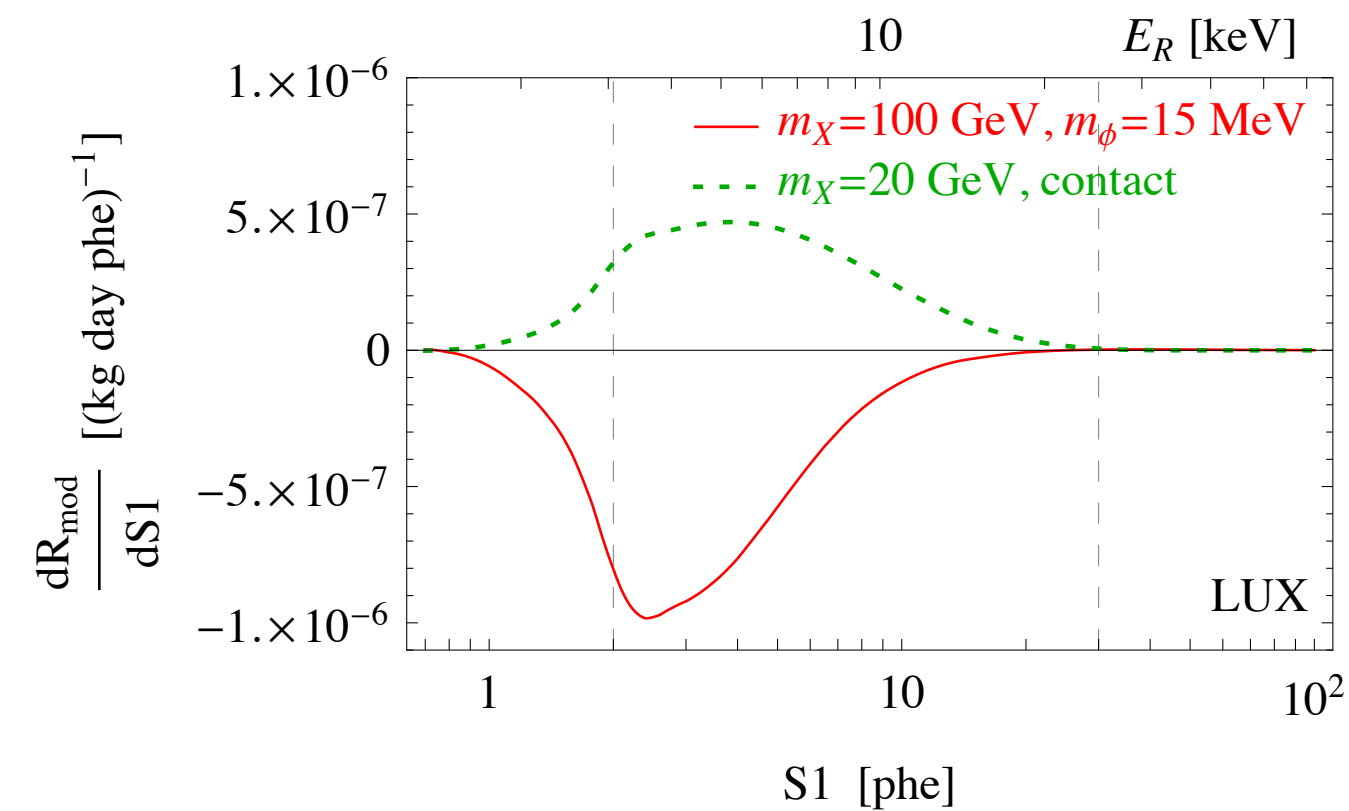
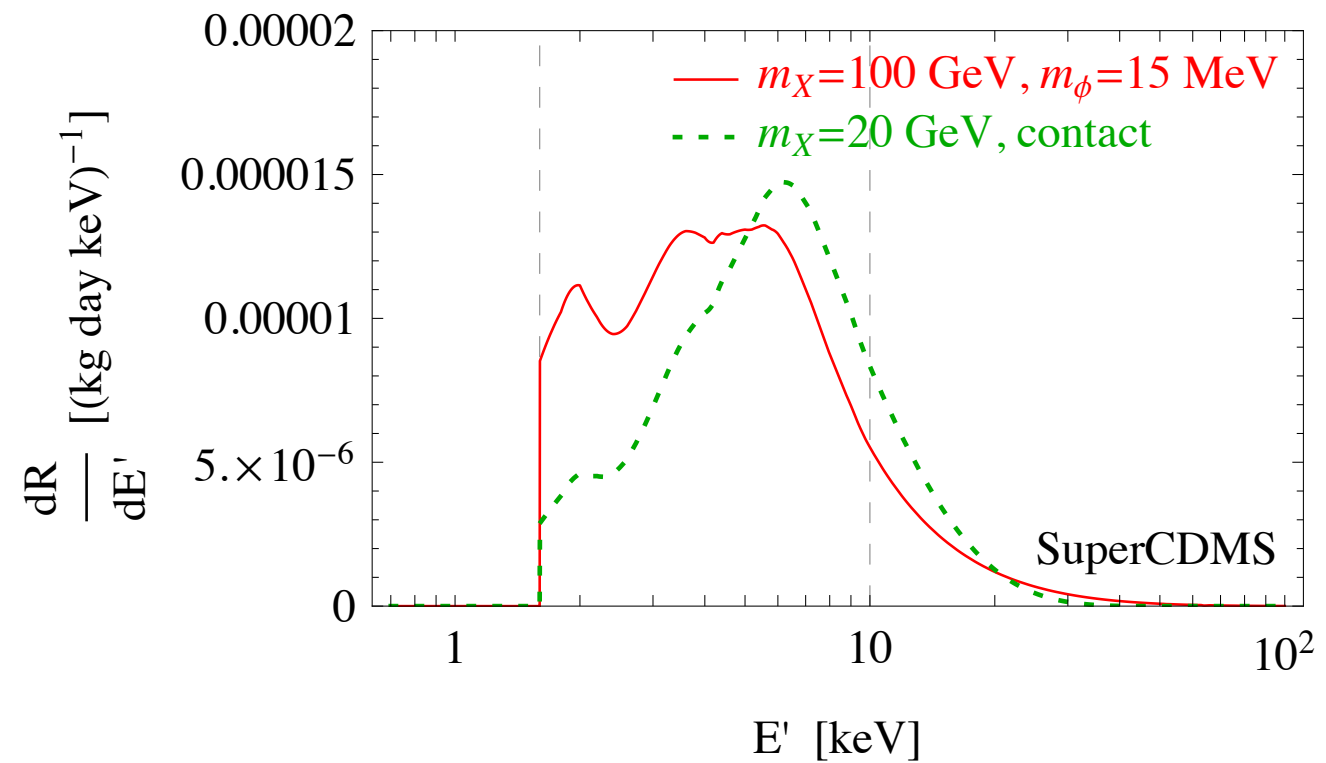
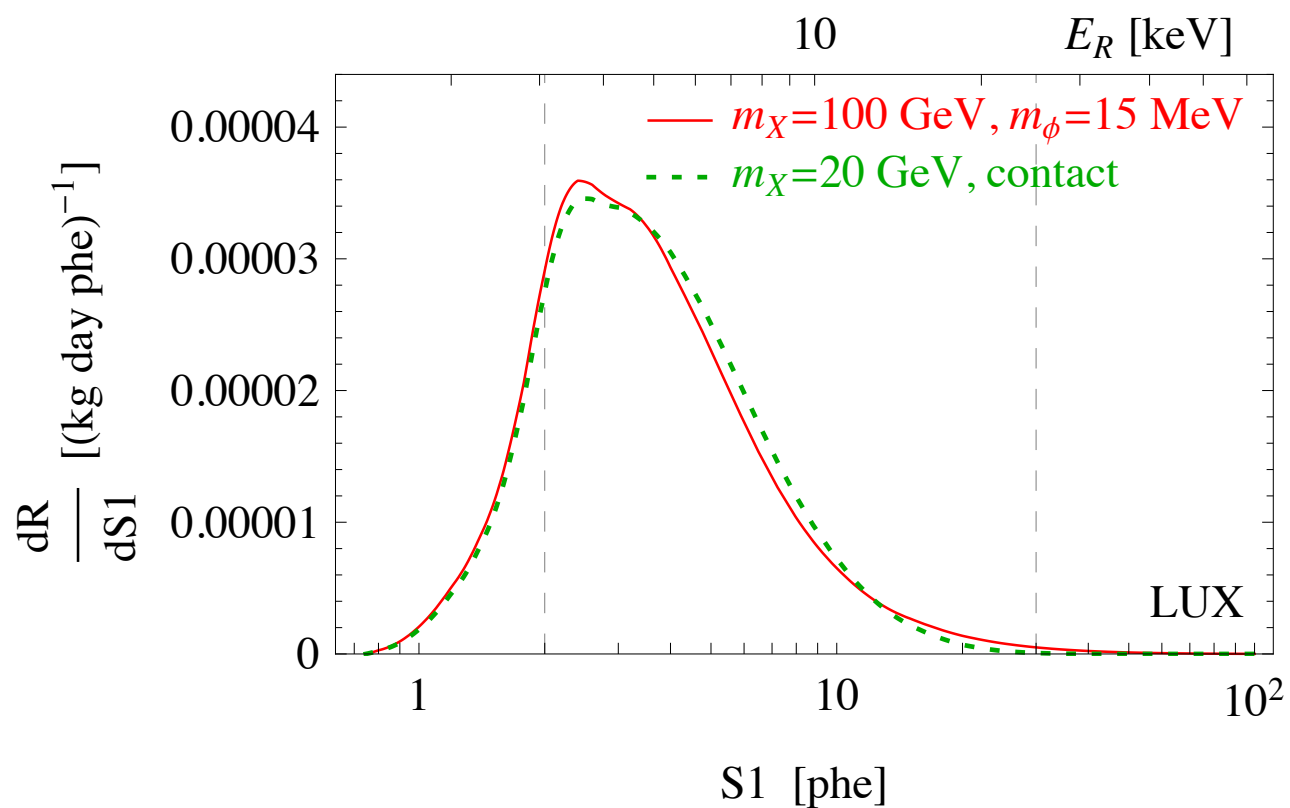
Several experiments employing different targets may be able to fit cross section dependence on A and J

Light mediator

$$\frac{d\sigma_T}{dE_R} \sim \frac{g^2 F^2(E_R)}{(q^2 + m_\phi^2)^2 v^2}$$



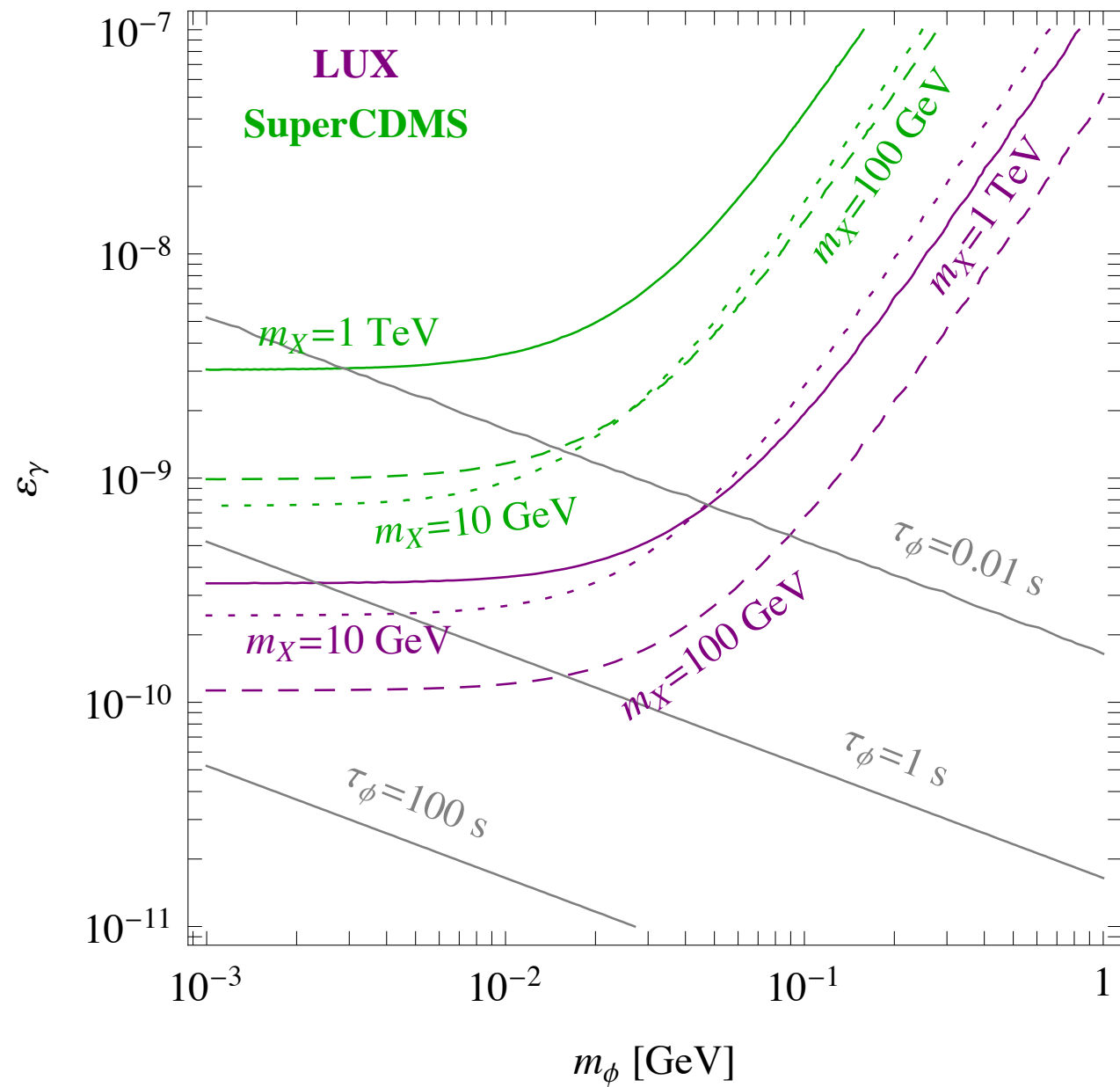
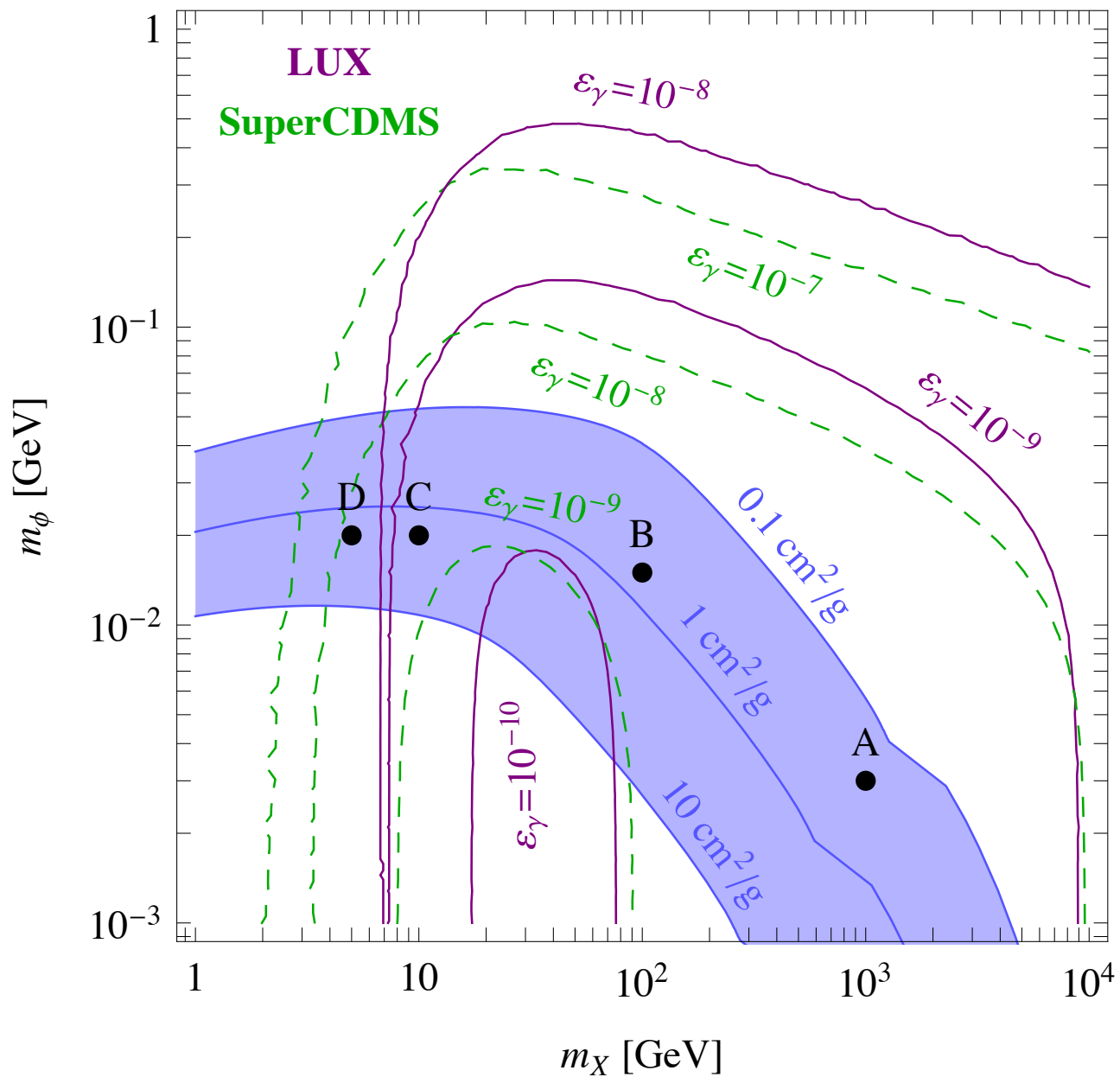
Light mediator



Light mediator

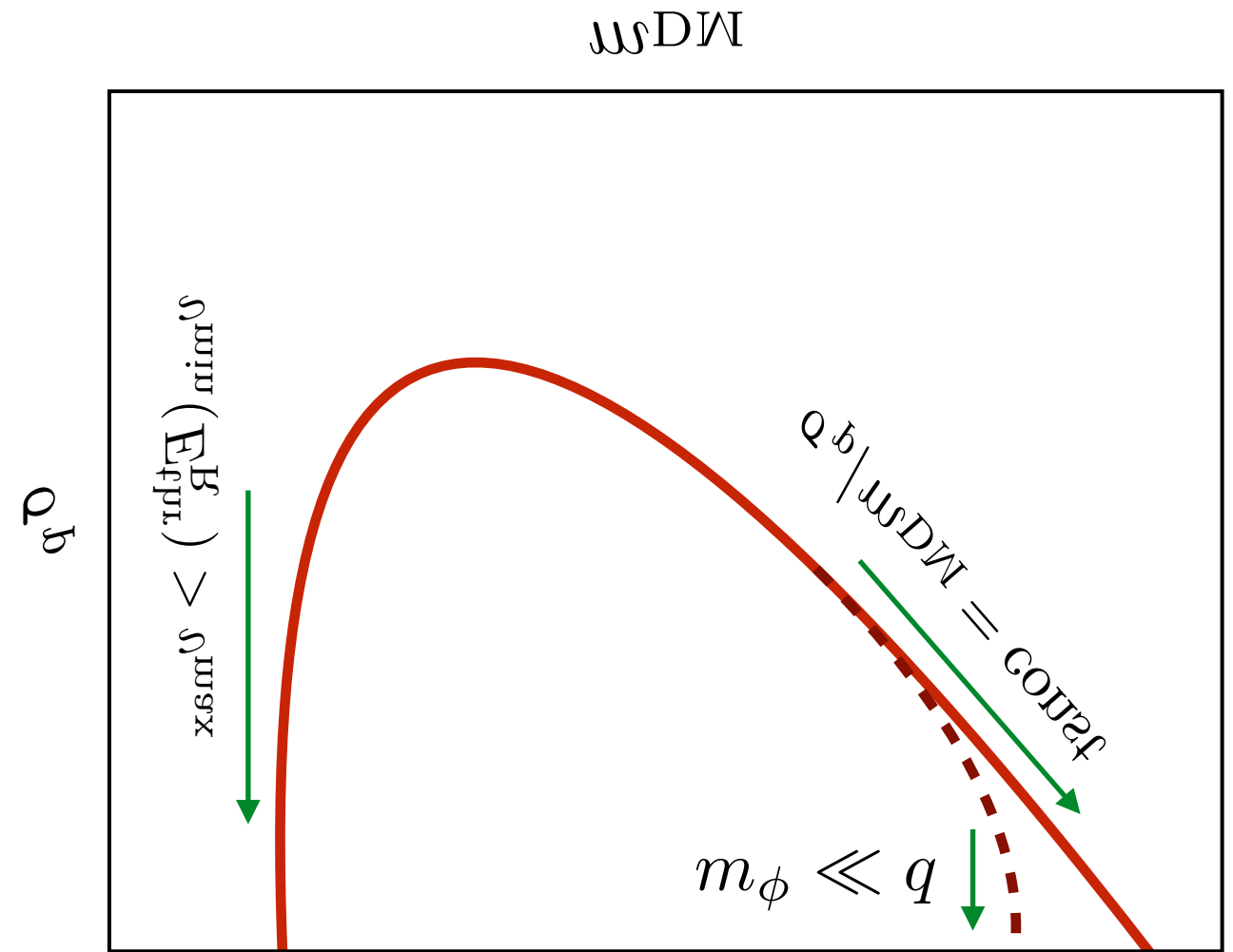
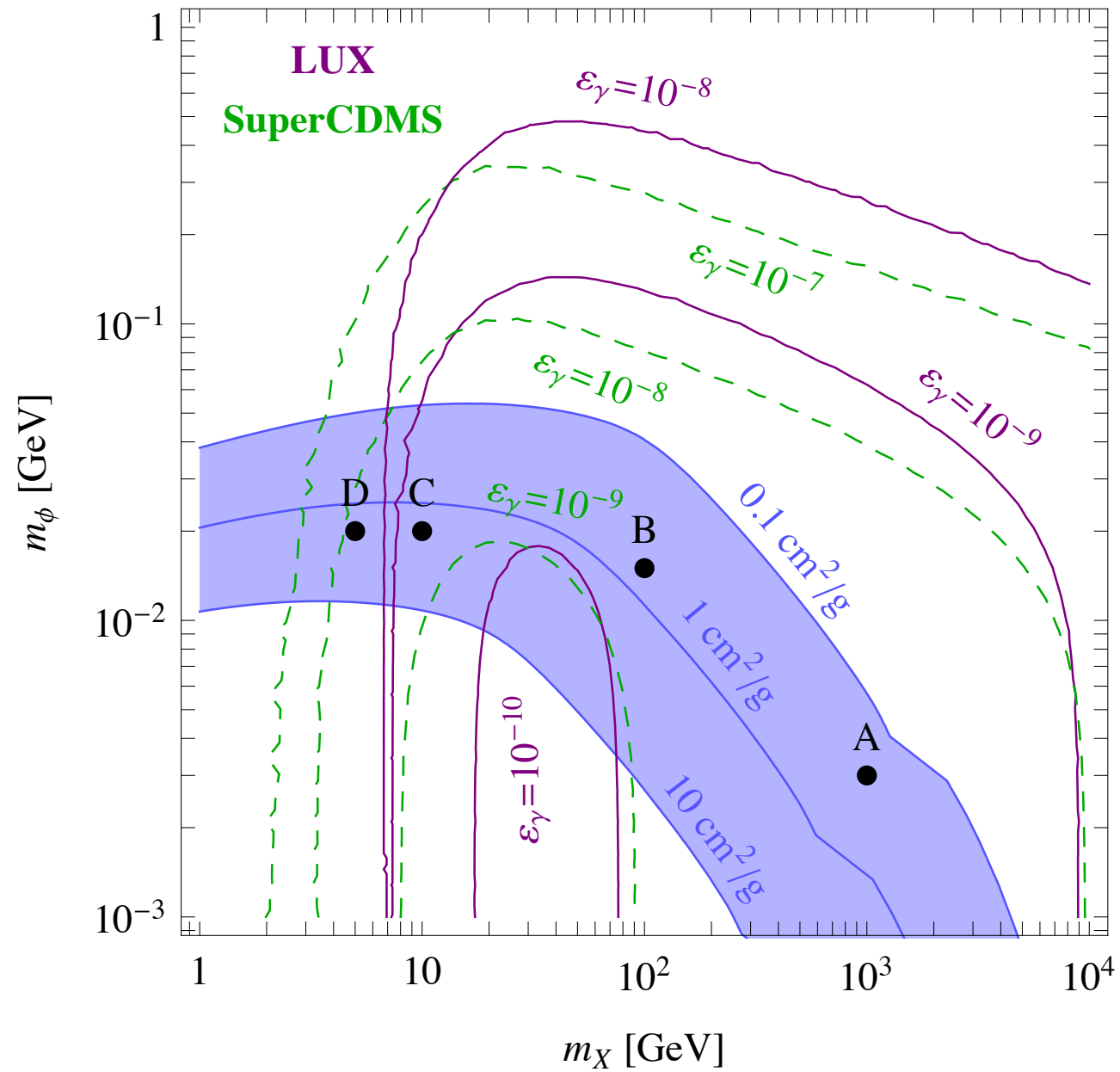
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Light mediator

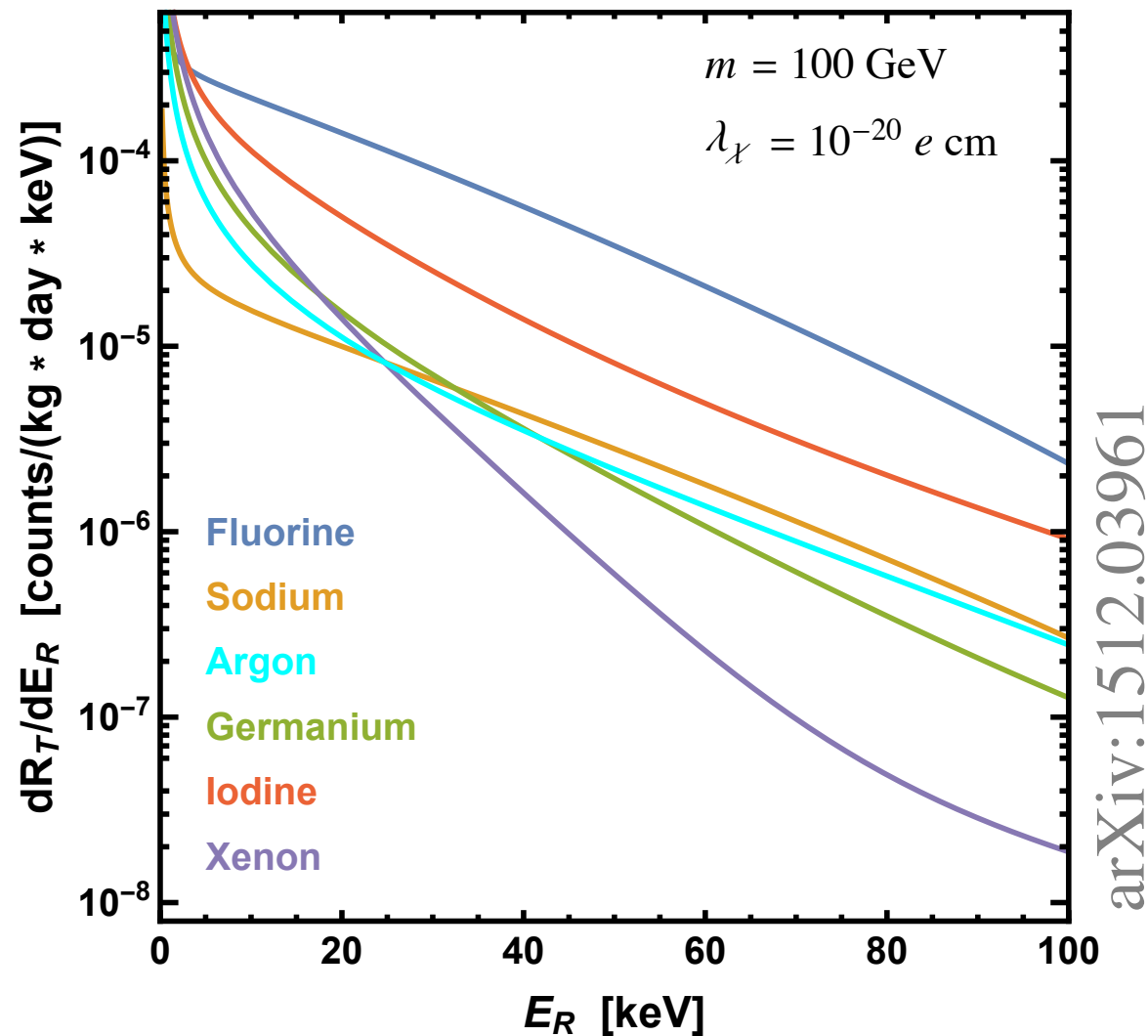
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Dark Matter with magnetic dipole moment

$$\mathcal{L}_M = \frac{\mu}{2} \bar{\chi} \sigma_{\mu\nu} \chi F^{\mu\nu} \quad H_M = -\vec{\mu} \cdot \vec{B}$$

$$\frac{d\sigma_T^M}{dE_R} \sim \left(\frac{1}{E_R} - \frac{\#}{v^2} \right) \mu^2 Z^2 F_C^2(E_R) + \frac{\textcircled{a}}{v^2} \mu^2 \mu_T^2 F_M^2(E_R)$$

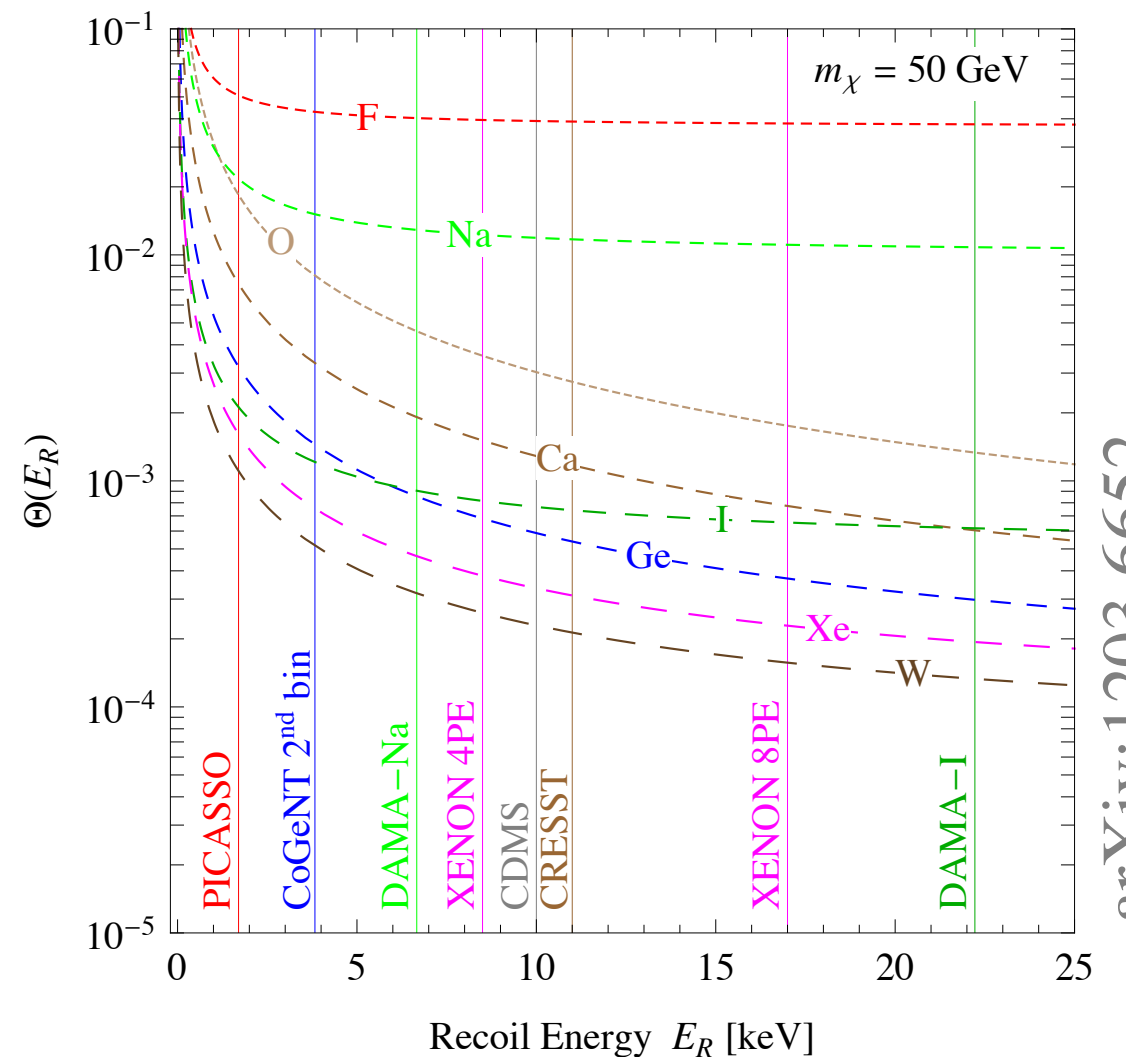
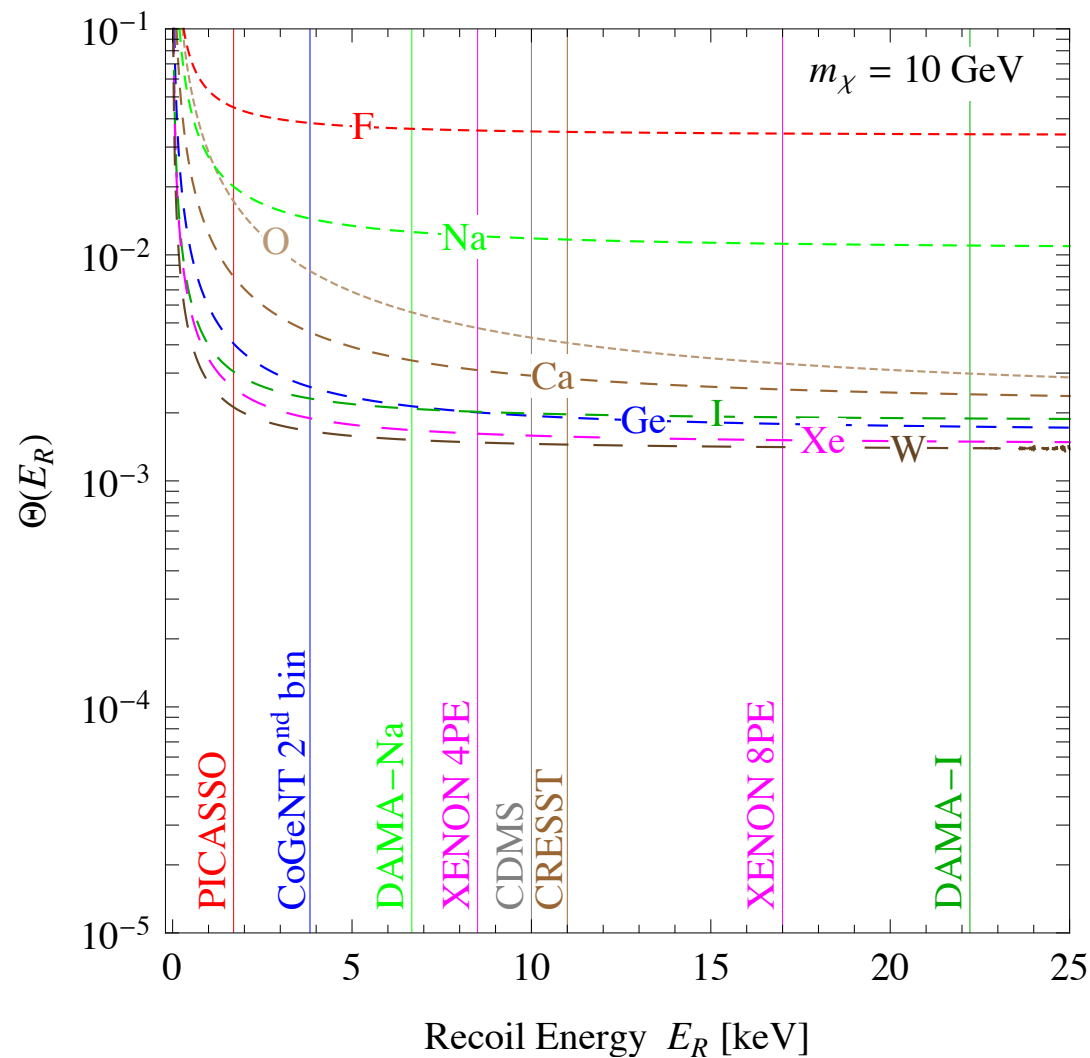


Dark Matter with magnetic dipole moment

$$\mathcal{L}_M = \frac{\mu}{2} \bar{\chi} \sigma_{\mu\nu} \chi F^{\mu\nu}$$

$$H_M = -\vec{\mu} \cdot \vec{B}$$

$$\frac{d\sigma_T^M}{dE_R} \sim \left(\frac{1}{E_R} - \frac{\#}{v^2} \right) \mu^2 Z^2 F_C^2(E_R) + \frac{\textcircled{a}}{v^2} \mu^2 \mu_T^2 F_M^2(E_R)$$

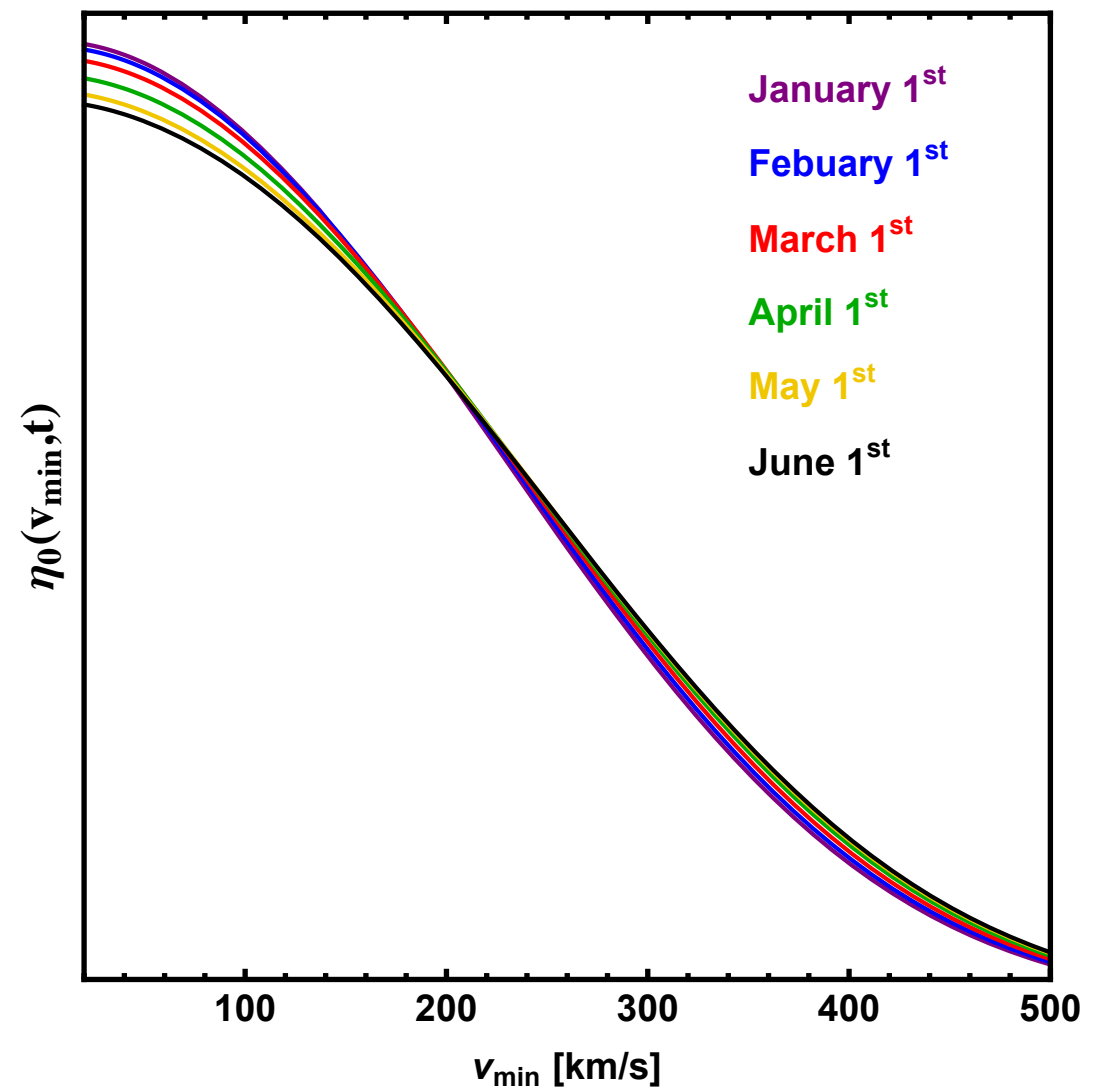
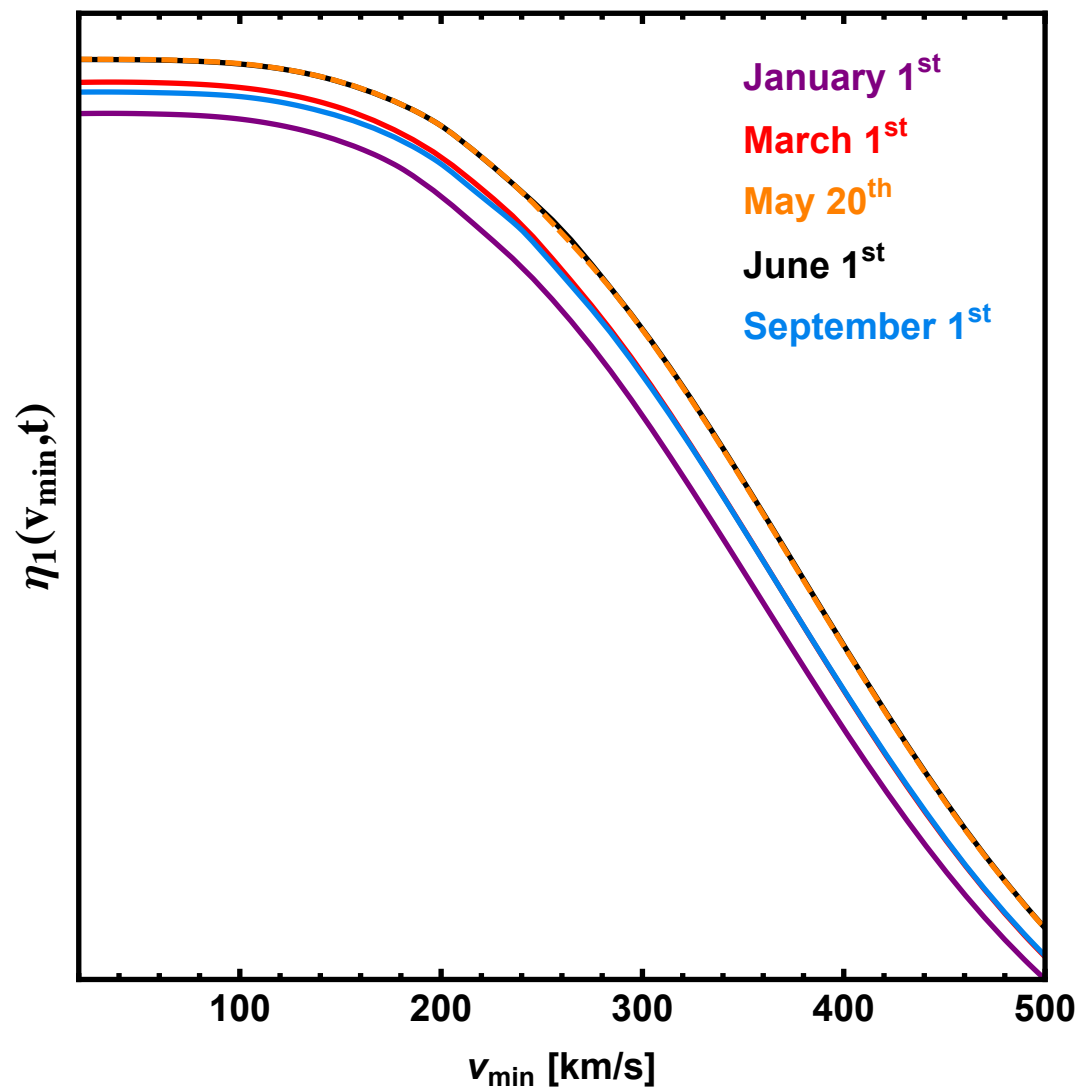


Modulation of magnetic dipole Dark Matter

$$\frac{d\sigma_T^M}{dE_R} \sim \left(\frac{1}{E_R} - \frac{\#}{v^2} \right) \mu^2 Z^2 F_C^2(E_R) + \frac{\textcircled{a}}{v^2} \mu^2 \mu_T^2 F_M^2(E_R)$$

$$\tilde{\eta}(v_{\min}, t) \equiv \int_{v \geq v_{\min}} d^3v v f(\vec{v}, t)$$

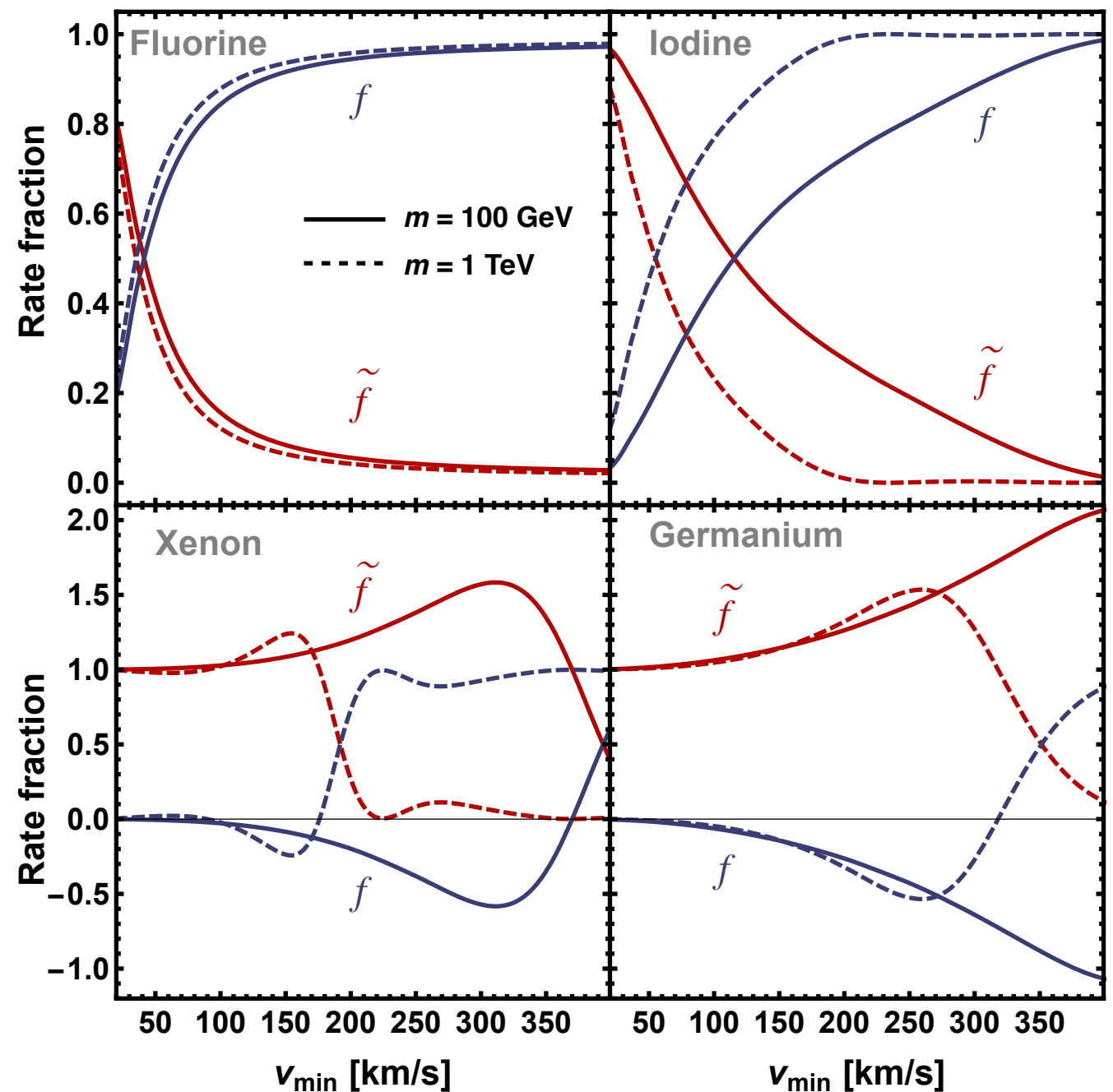
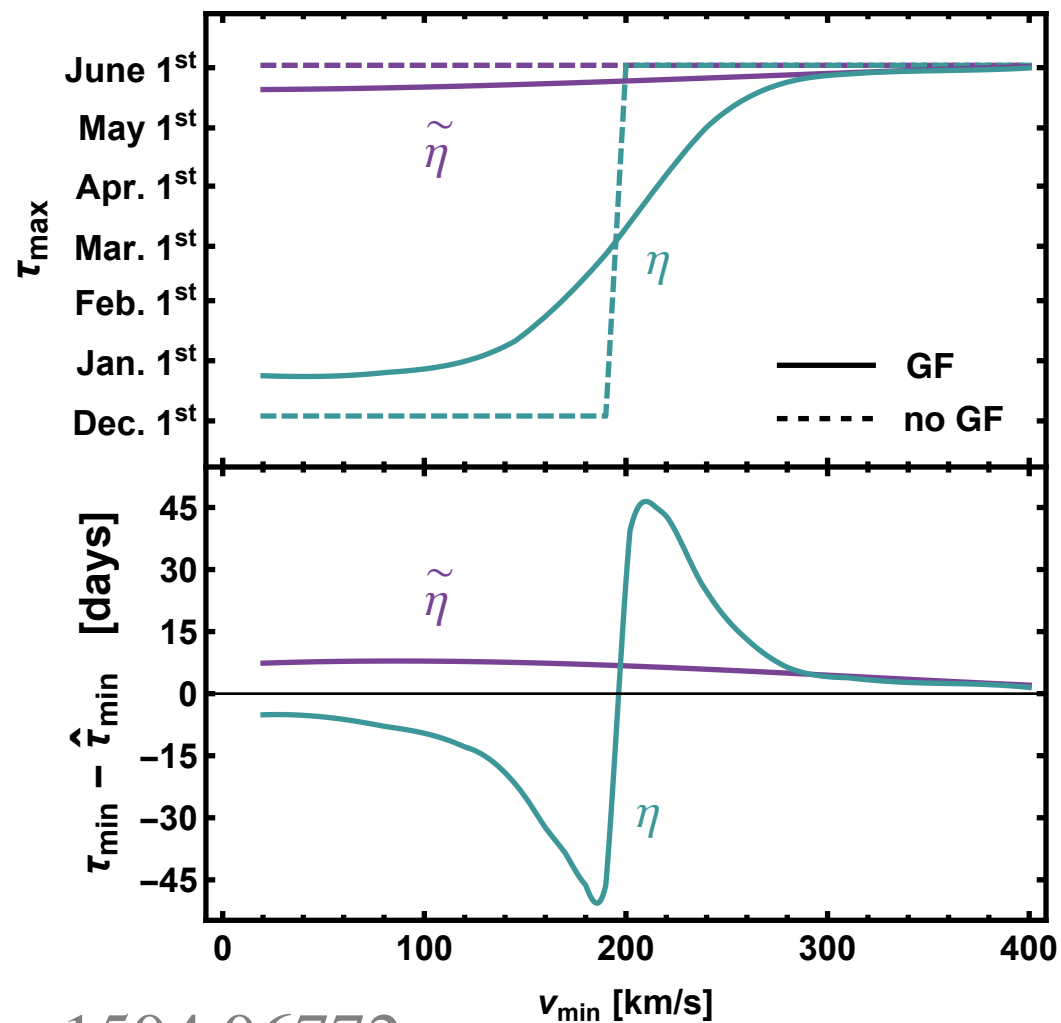
$$\eta(v_{\min}, t) \equiv \int_{v \geq v_{\min}} d^3v \frac{f(\vec{v}, t)}{v}$$



Modulation of magnetic dipole Dark Matter

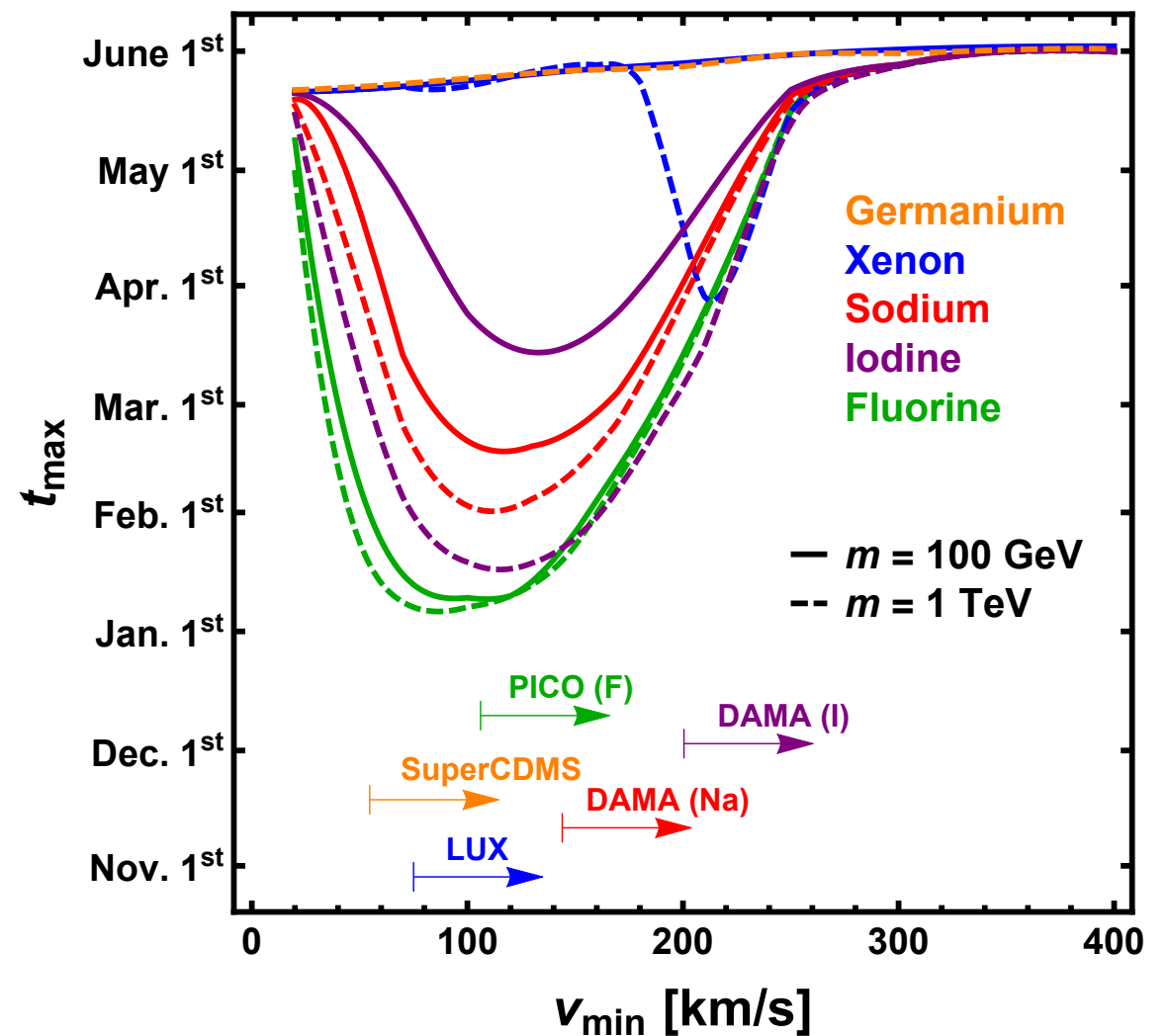
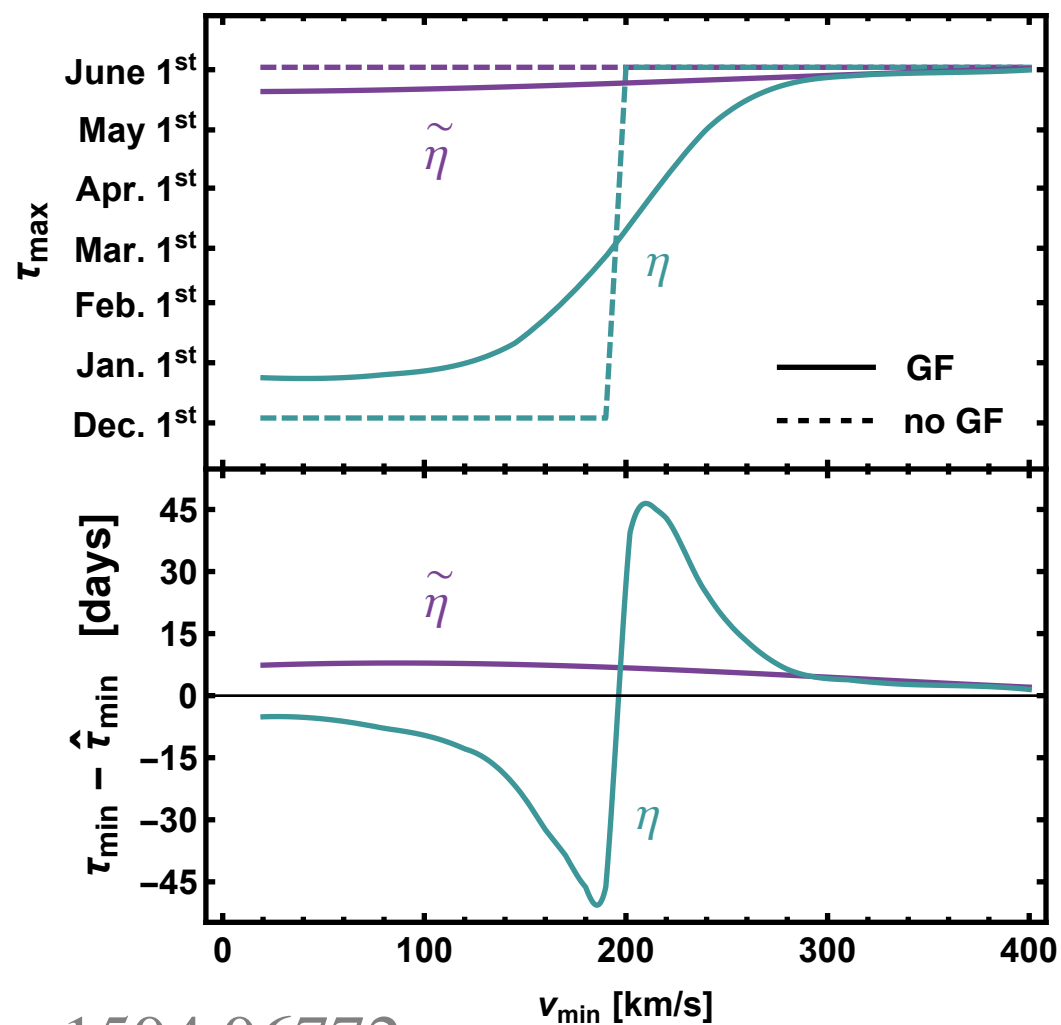
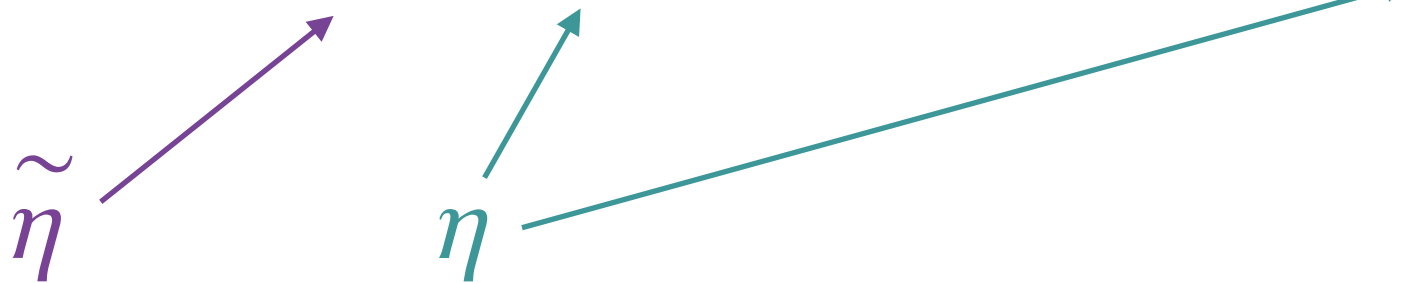
$$\frac{d\sigma_T^M}{dE_R} \sim \left(\frac{1}{E_R} - \frac{\#}{v^2} \right) \mu^2 Z^2 F_C^2(E_R) + \frac{\textcircled{a}}{v^2} \mu^2 \mu_T^2 F_M^2(E_R)$$

$\tilde{\eta}$ η

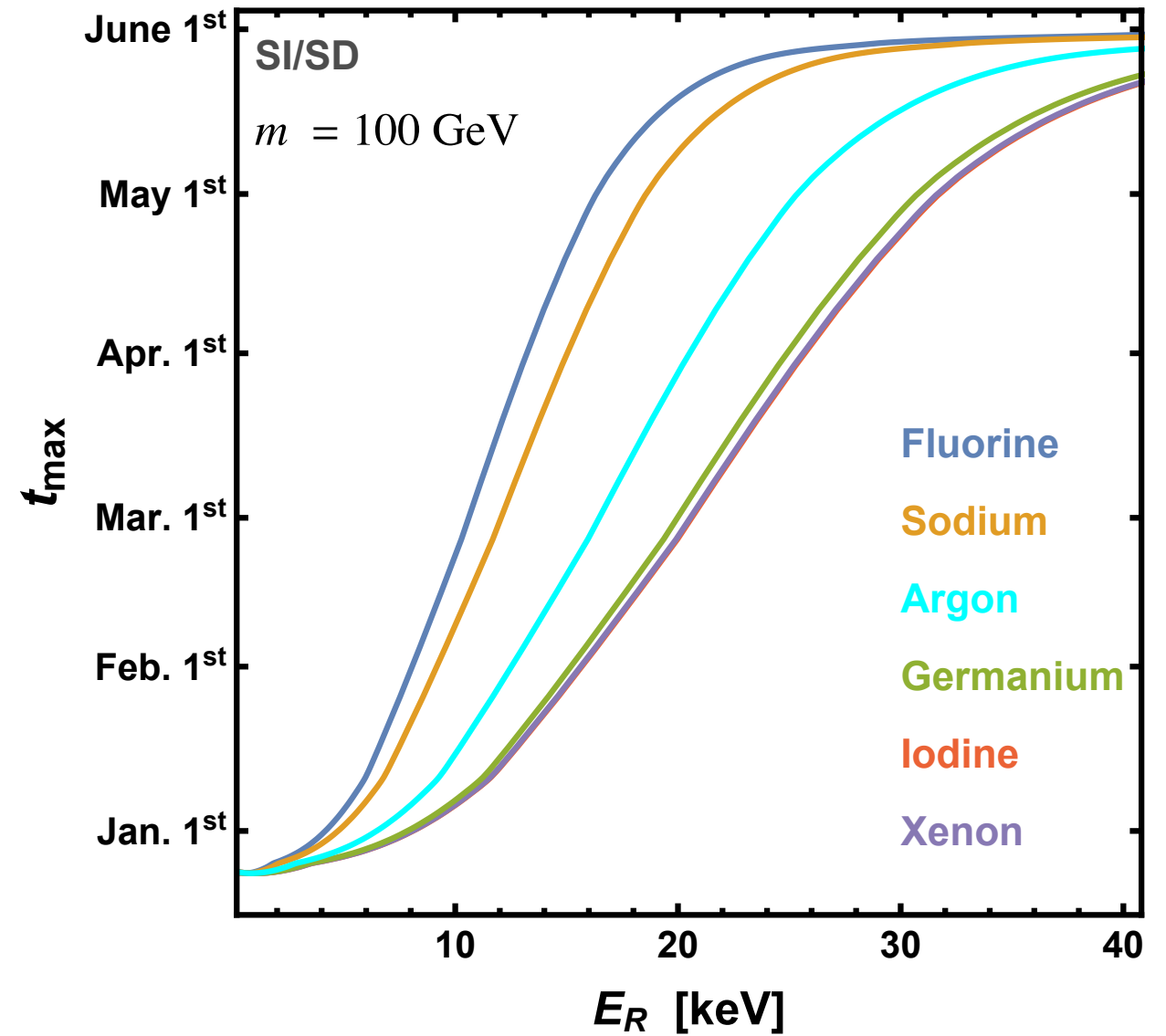
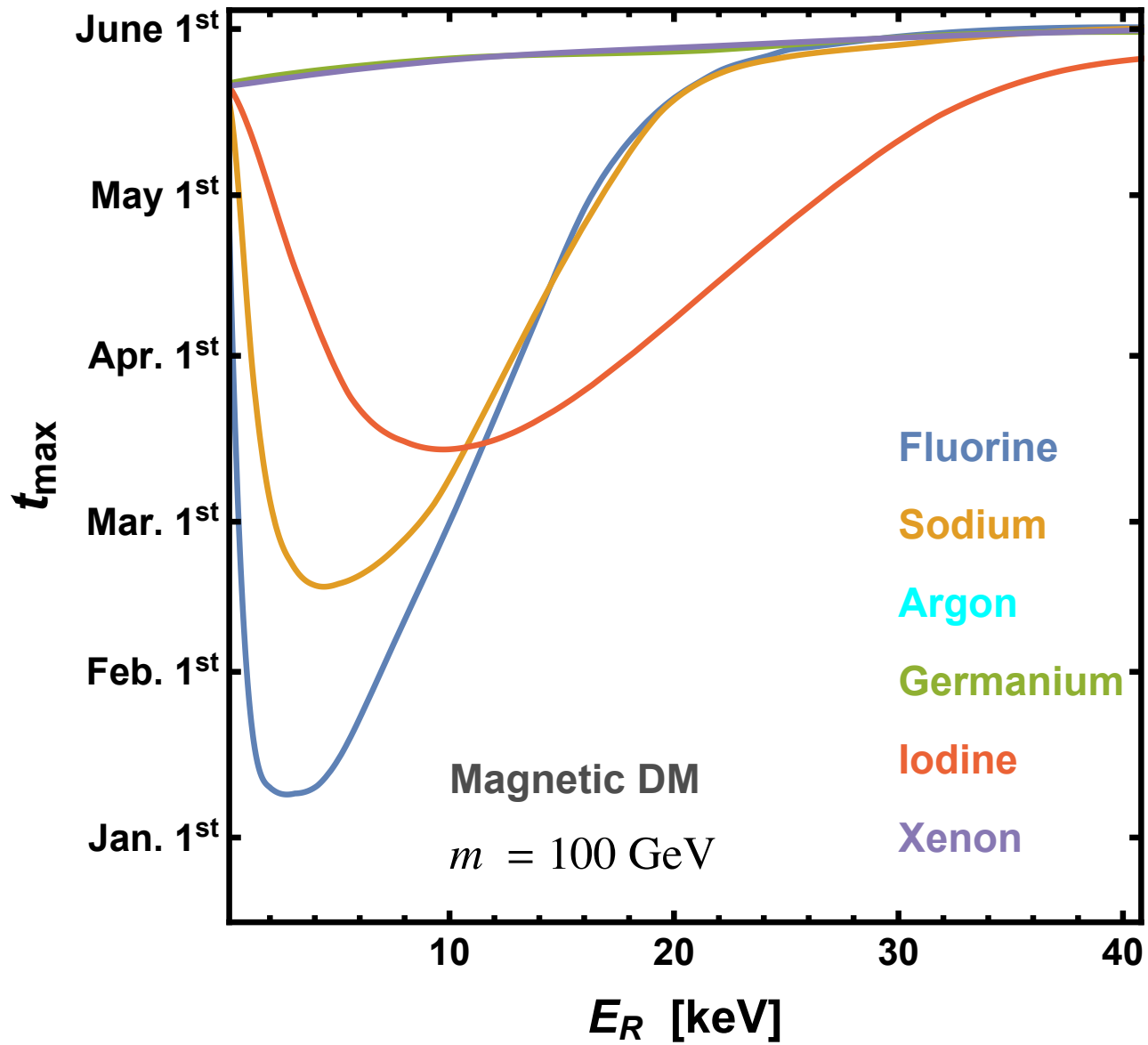


Modulation of magnetic dipole Dark Matter

$$\frac{d\sigma_T^M}{dE_R} \sim \left(\frac{1}{E_R} - \frac{\#}{v^2} \right) \mu^2 Z^2 F_C^2(E_R) + \frac{\textcircled{a}}{v^2} \mu^2 \mu_T^2 F_M^2(E_R)$$



Modulation of magnetic dipole Dark Matter



Conclusions

WIMPs don't need to be standard

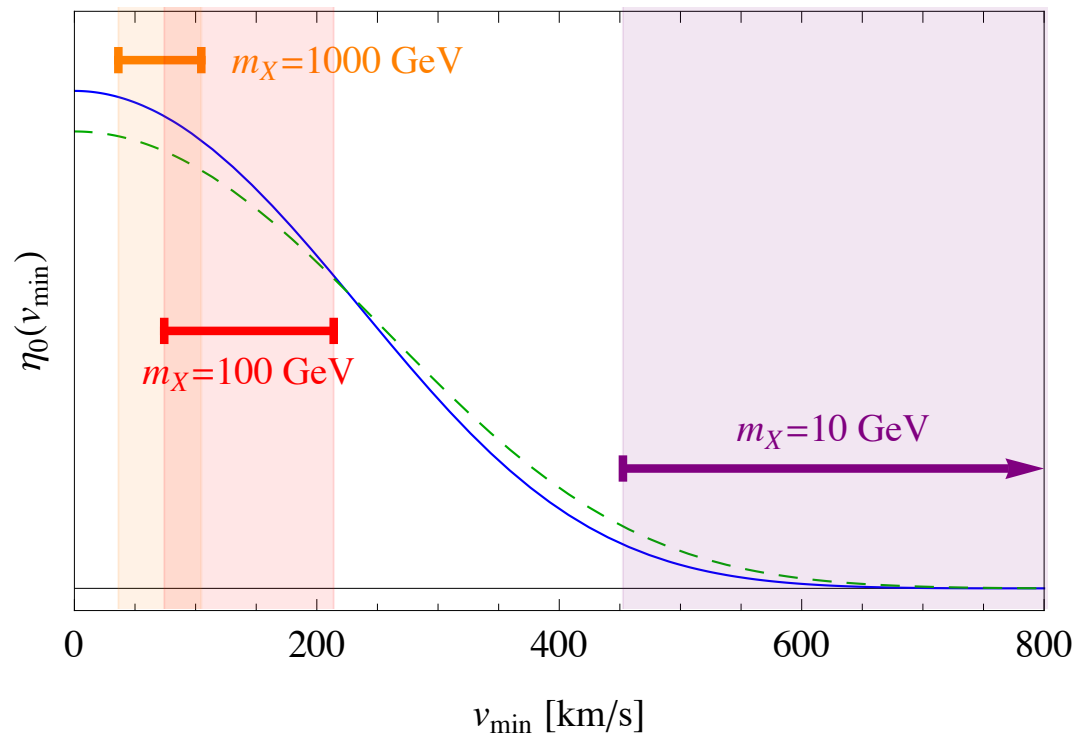
Direct detection can discriminate between different DM candidates (as long as any of them actually exists)

Look at: A dependence, energy spectrum, modulation

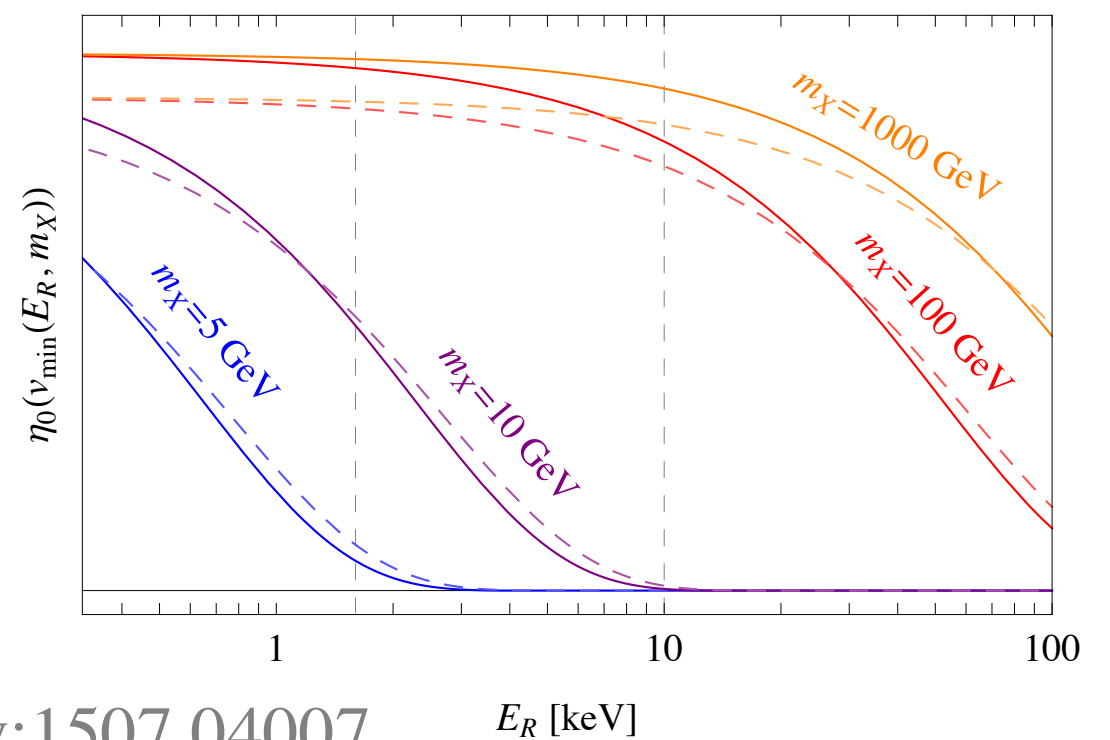
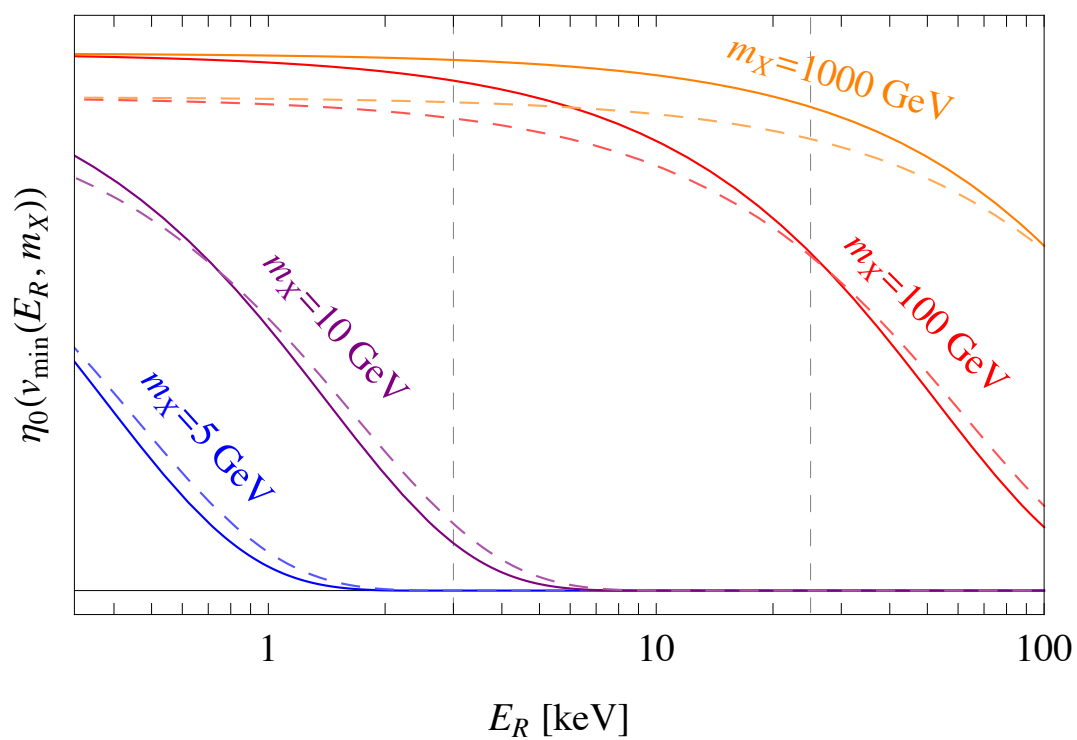
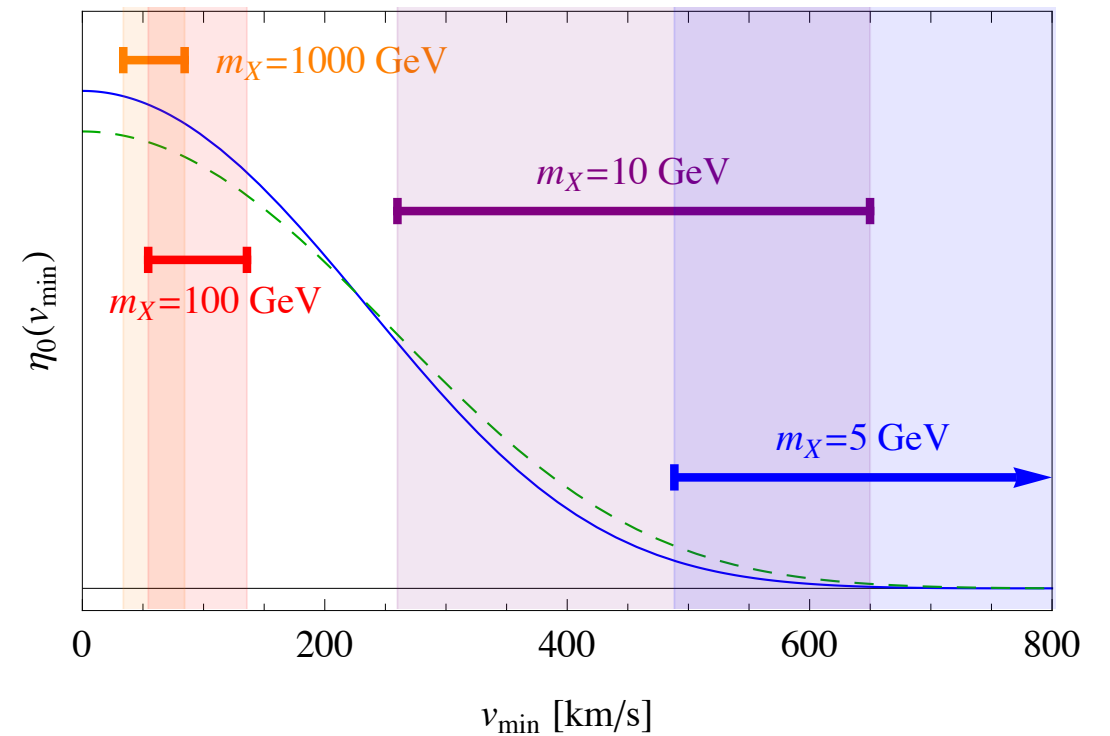
Backups

Velocity integral (time average)

Scattering off Xe in LUX

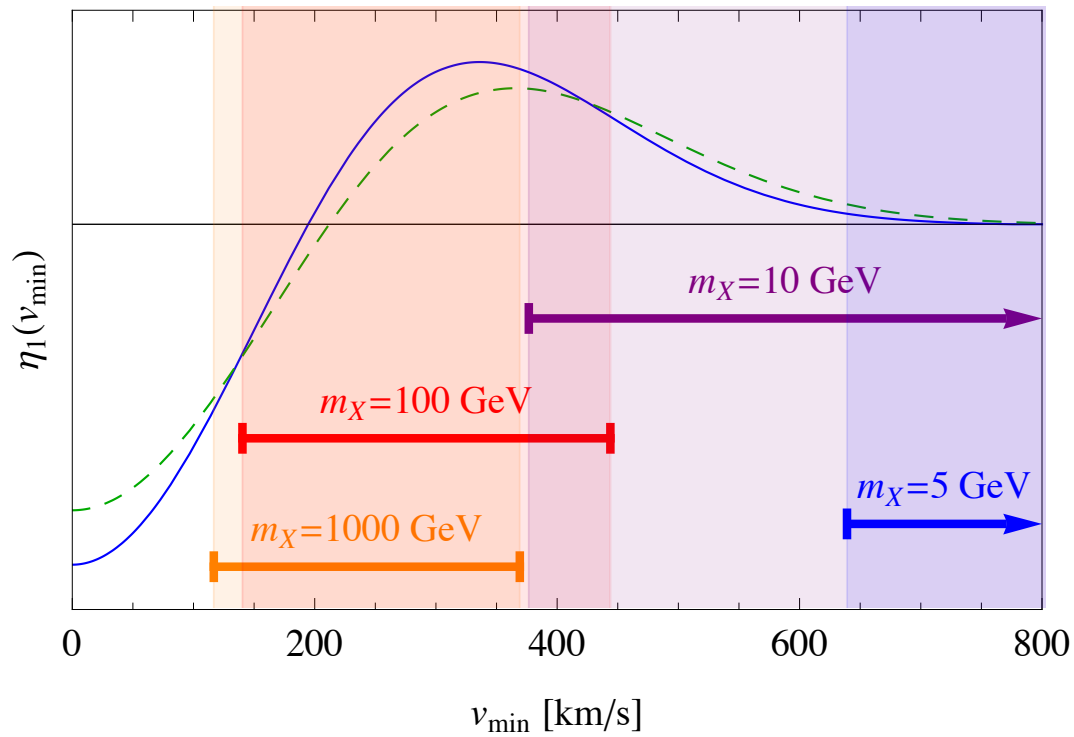


Scattering off Ge in SuperCDMS

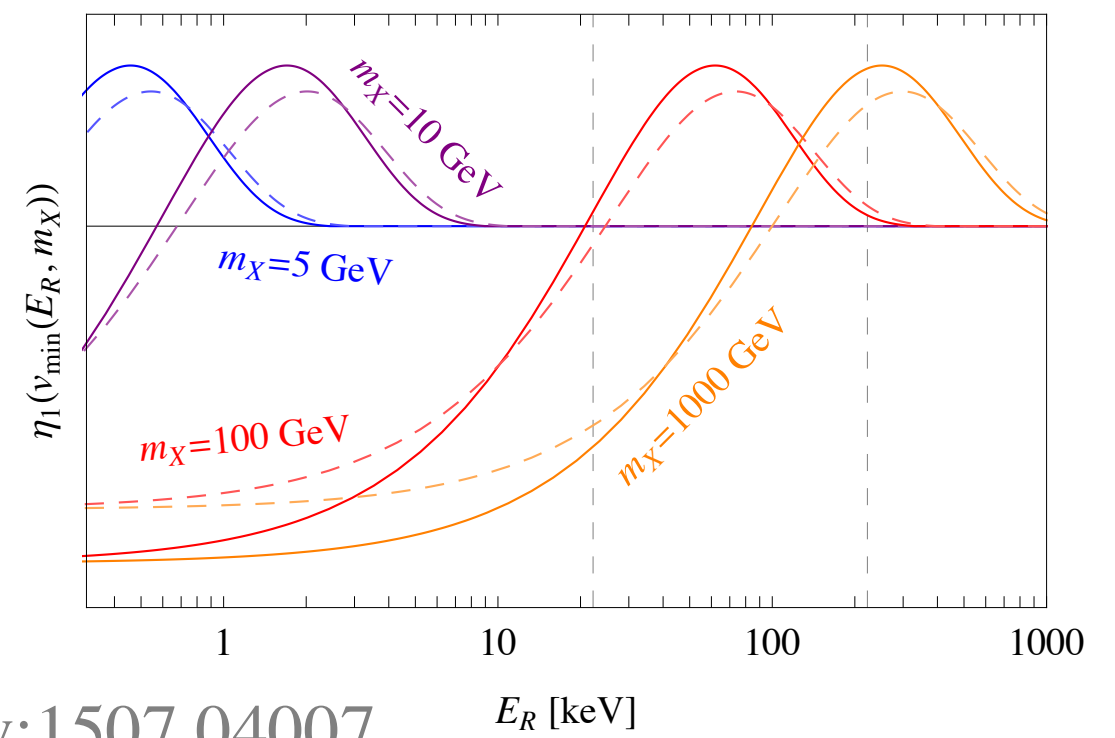
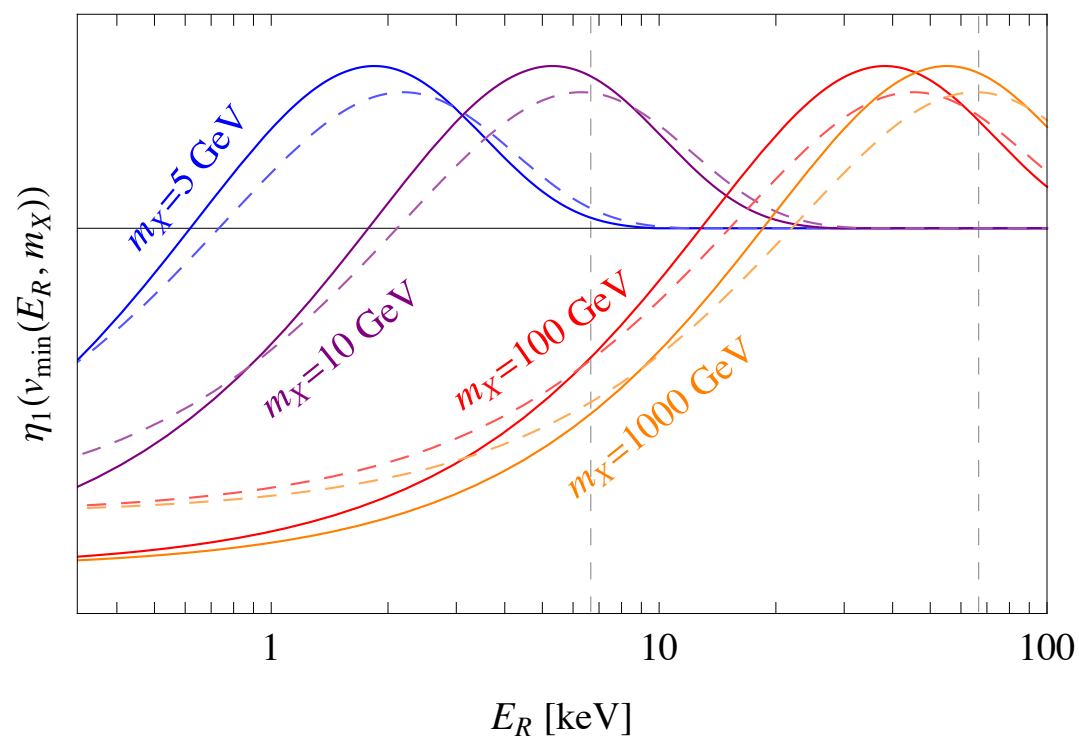
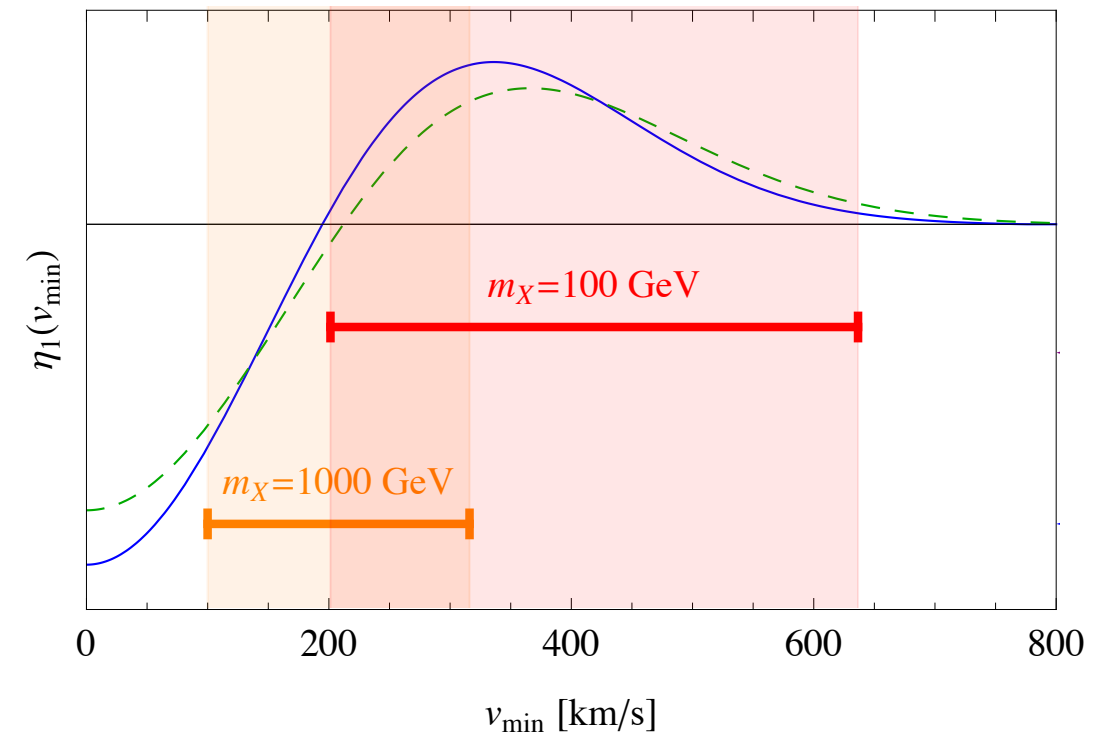


Velocity integral (modulation)

Scattering off Na in DAMA, $Q_{\text{Na}}=0.3$



Scattering off I in DAMA, $Q_I=0.09$



Dark Matter with magnetic/anapole moment

