

# Dark Matter EFTs at Colliders

Based on work with:  
Francesco Riva and Alfredo Urbano  
1607.02474  
1607.02475

# Why EFTs at colliders?

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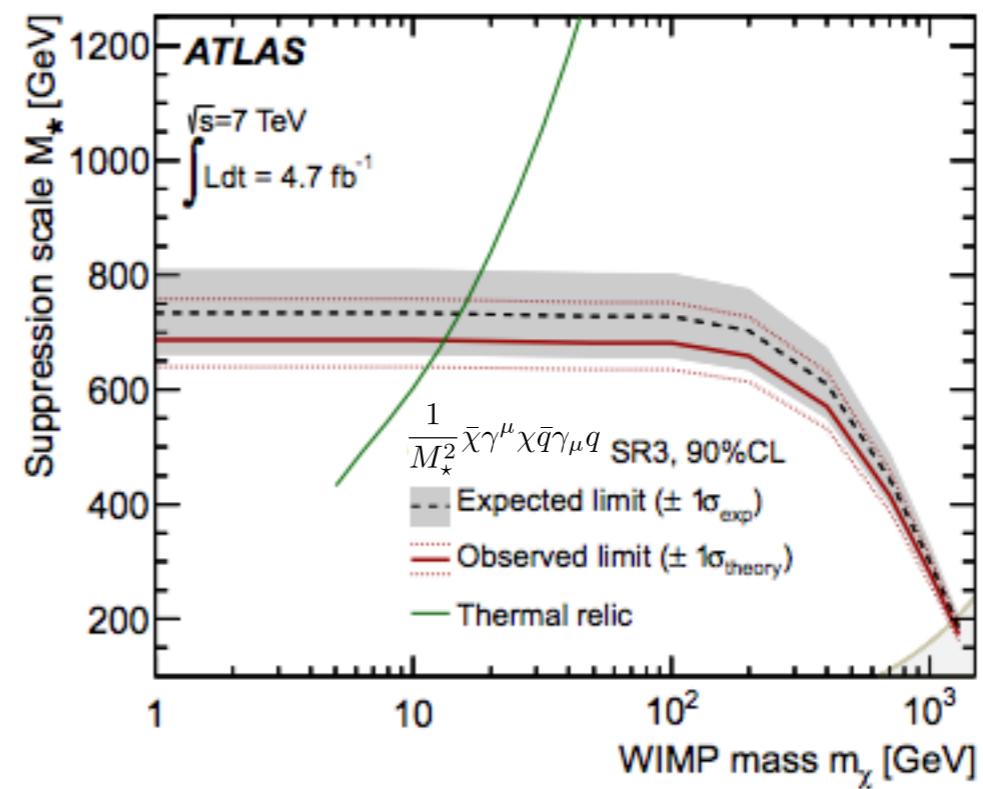


Figure from:  
1210.4491

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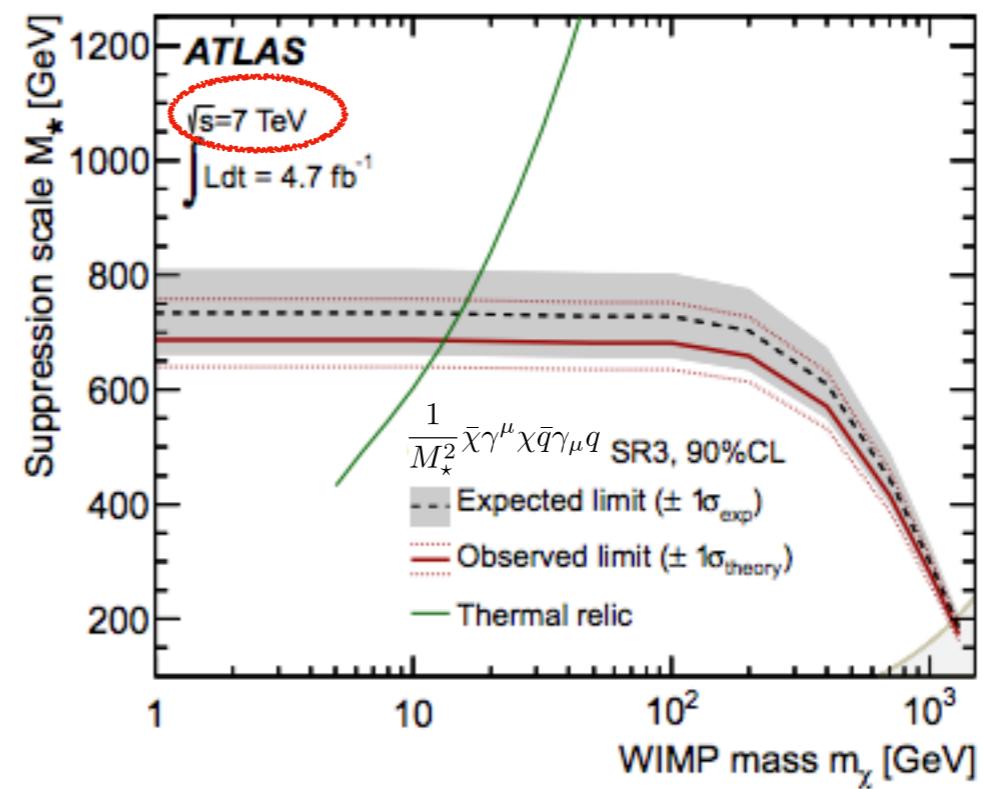


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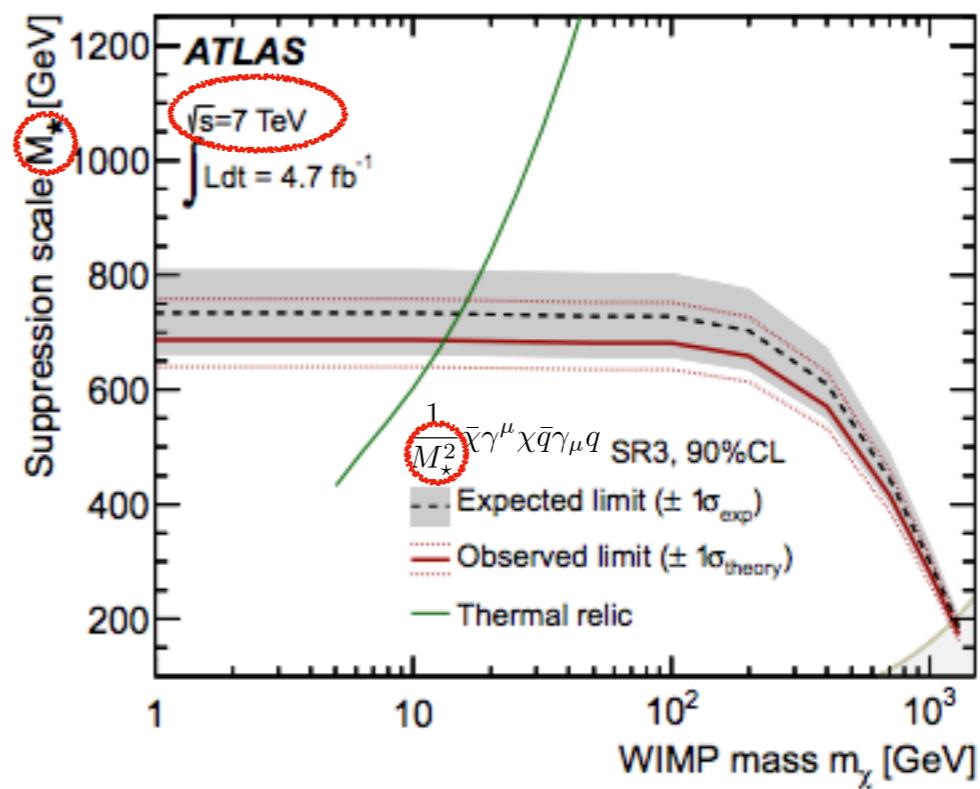


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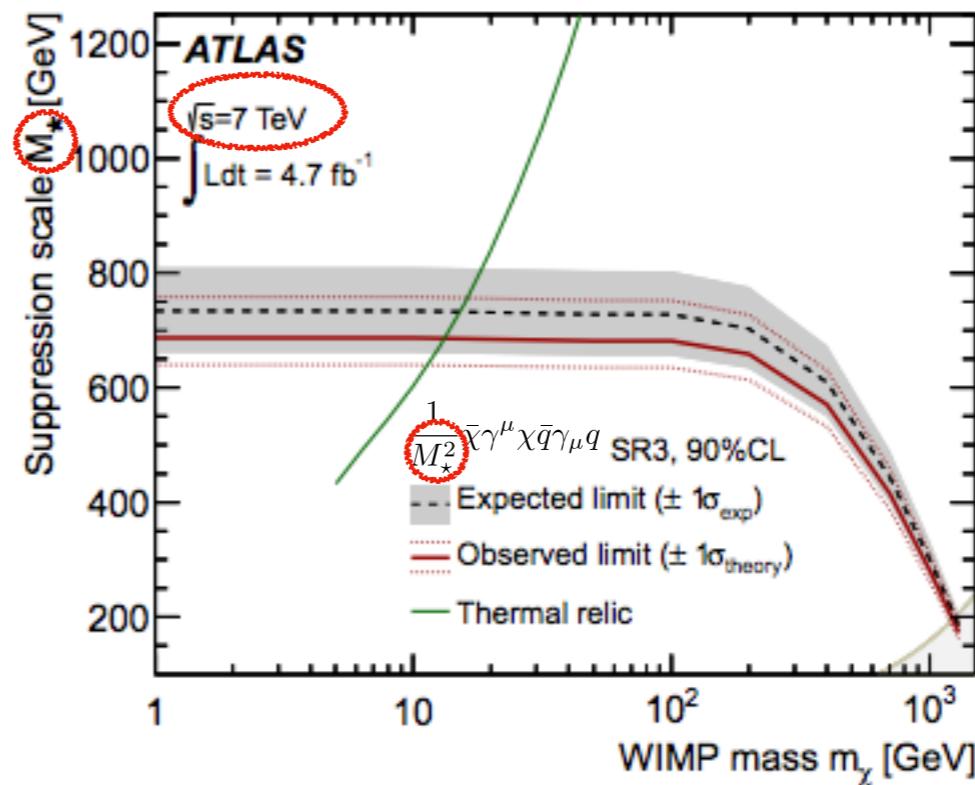


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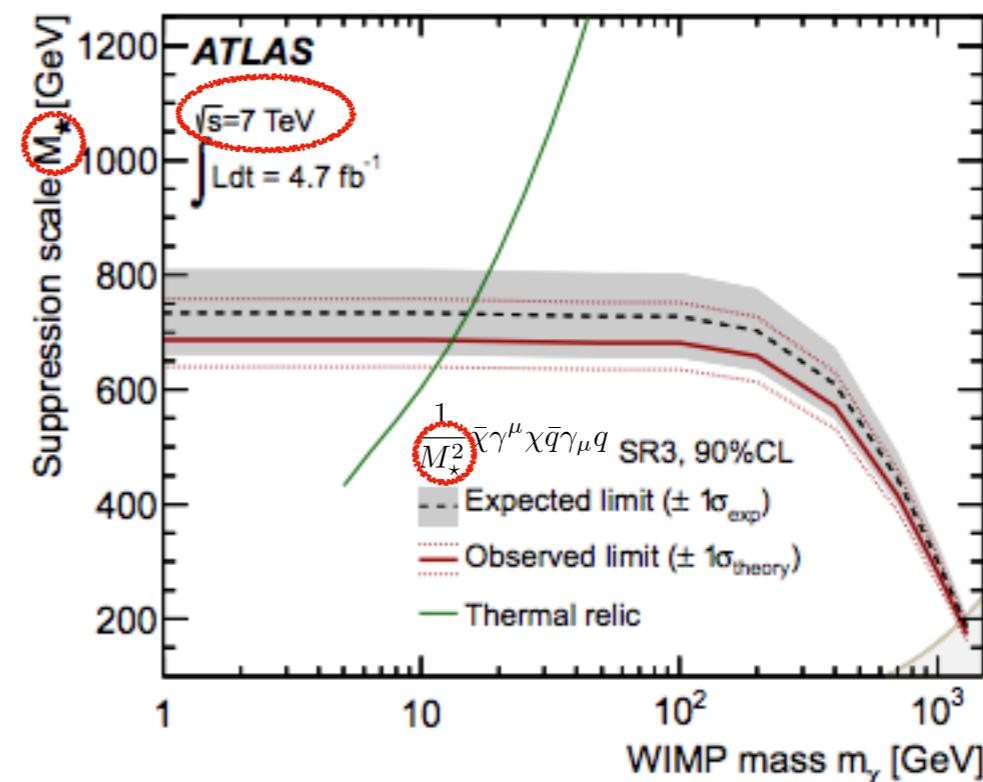


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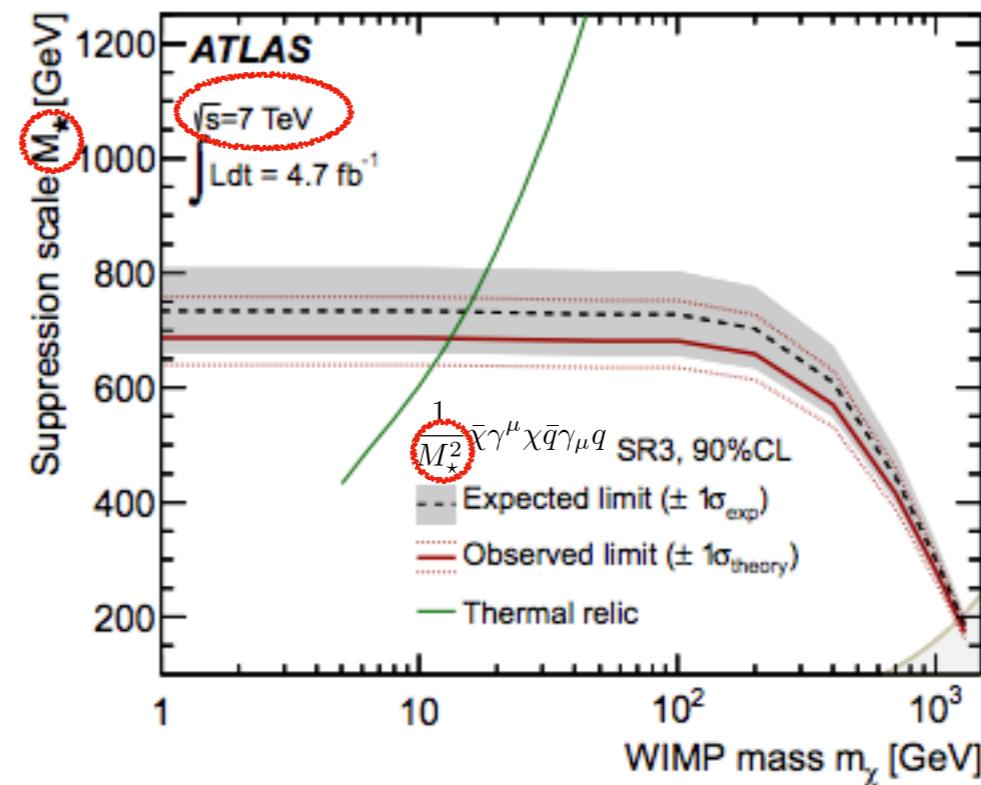


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- What is  $M_*$ ?

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Restoring dimensions in  $\hbar$

Diagram illustrating the suppression scale  $M_*$  as a function of the WIMP mass  $m_\chi$ . The equation  $\frac{1}{M_*^2} \sim c \frac{g_*^2}{M^2}$  is shown, where  $c$  is a Wilson coefficient of order 1. Arrows point from the terms  $\frac{1}{M_*^2}$ ,  $c$ ,  $\frac{g_*^2}{M^2}$ , and  $\hbar$  to the corresponding parts of the equation.

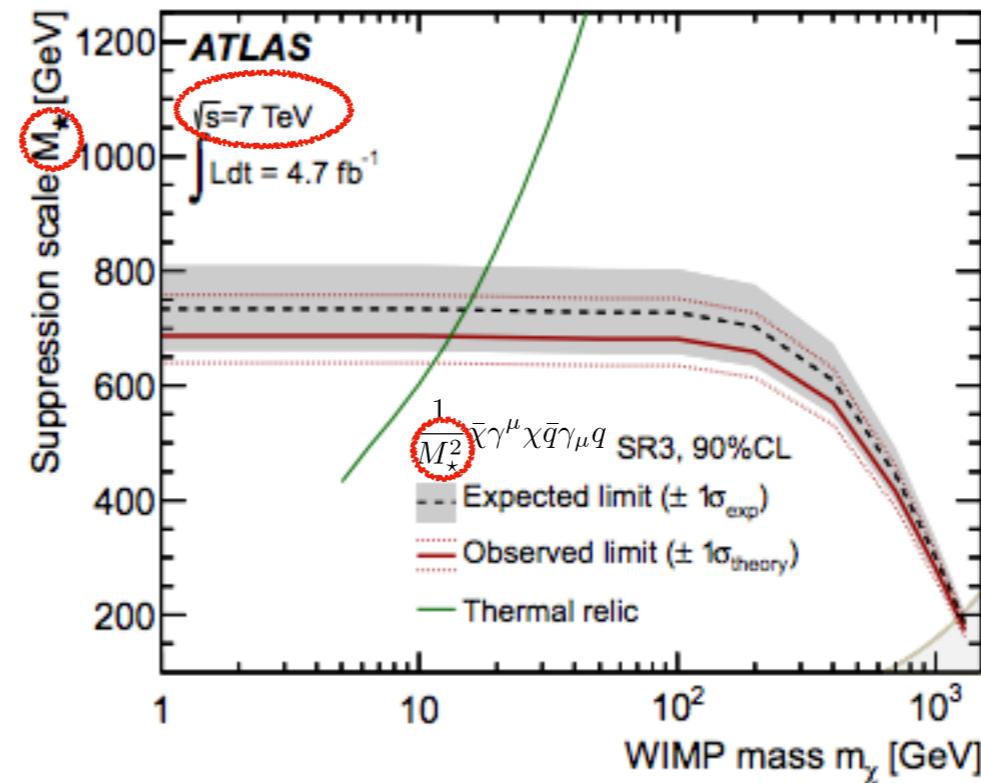


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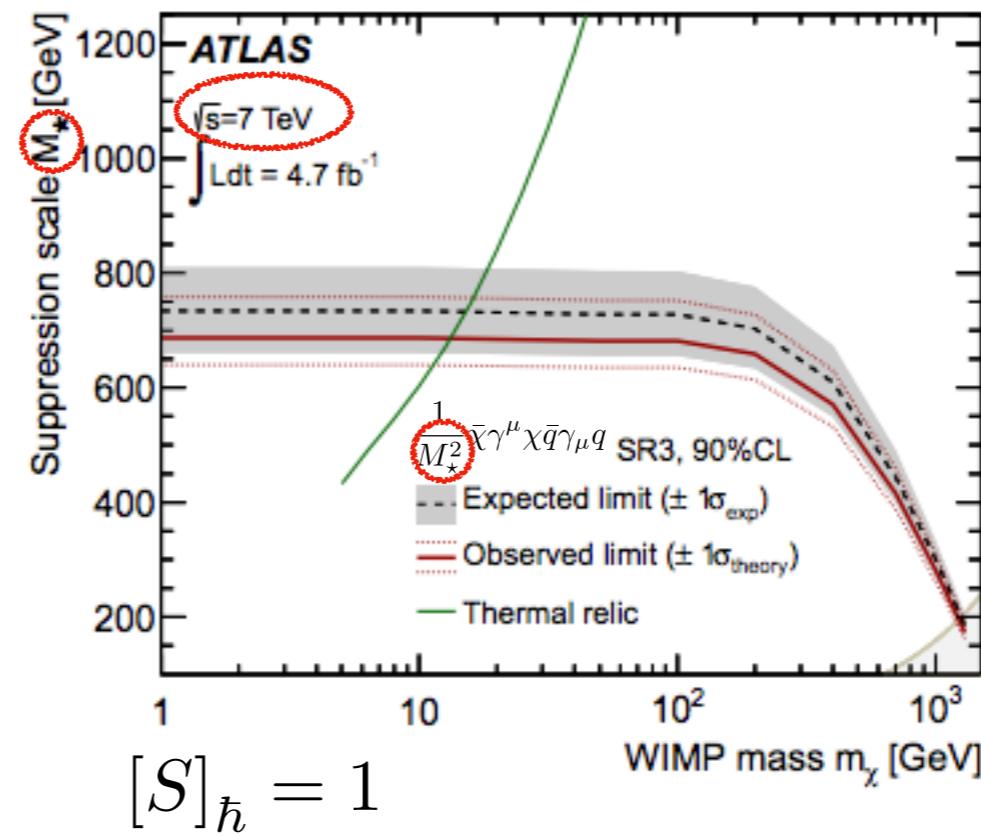


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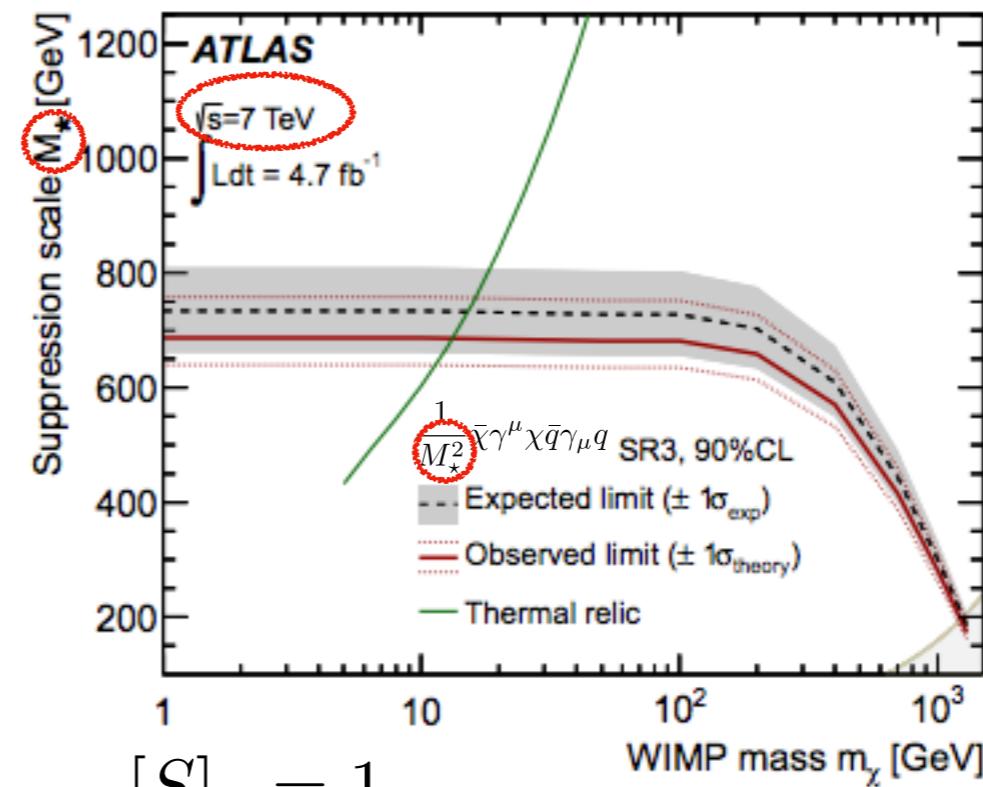
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Restoring dimensions in  $\hbar$



$[\psi]_\hbar = \frac{1}{2}$

Kinetic term

$[\phi]_\hbar = \frac{1}{2}$

Figure from:  
[1210.4491](https://arxiv.org/abs/1210.4491)

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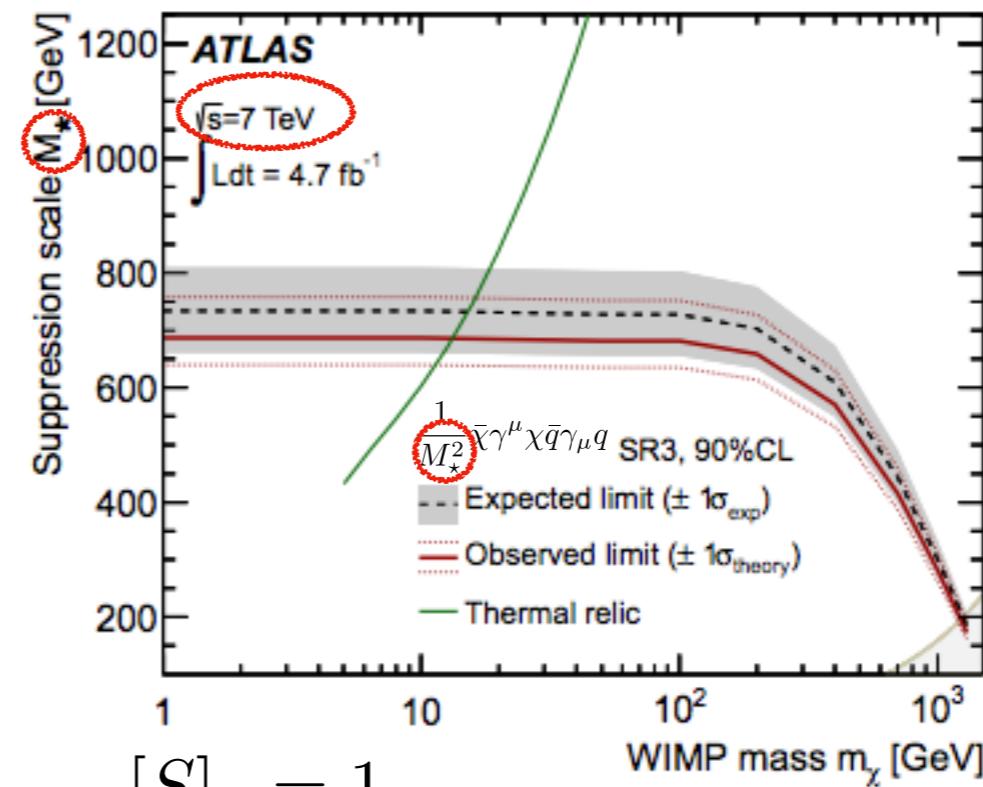


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$$[S]_\hbar = 1$$

$[g]_\hbar = -\frac{1}{2}$  **Interaction term**

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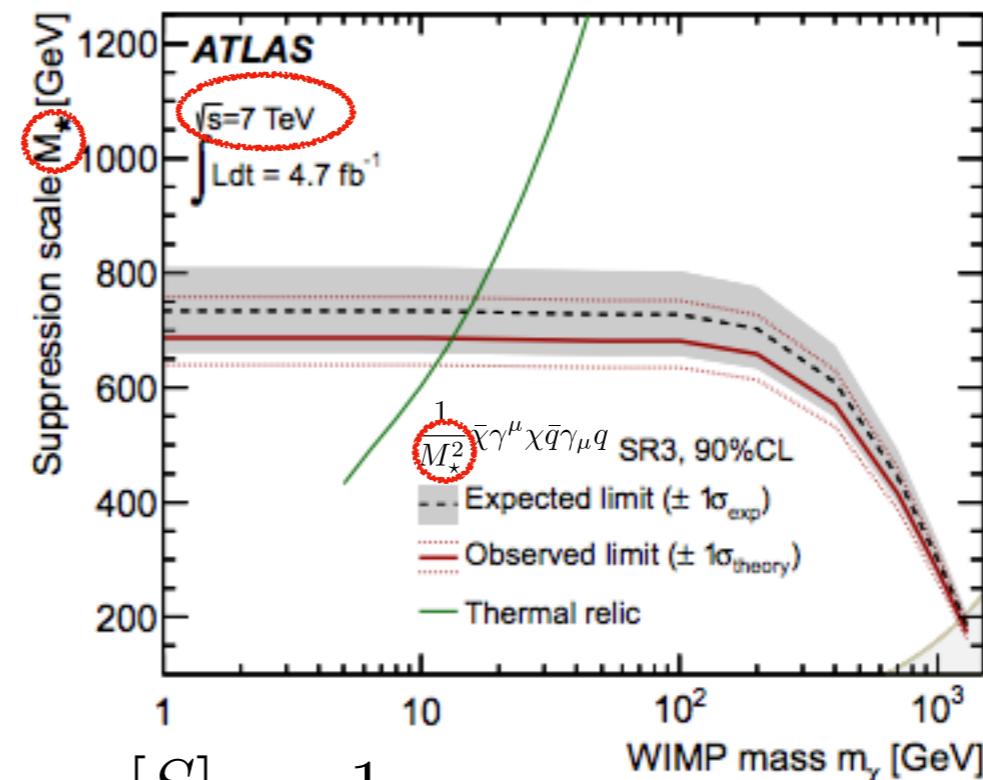
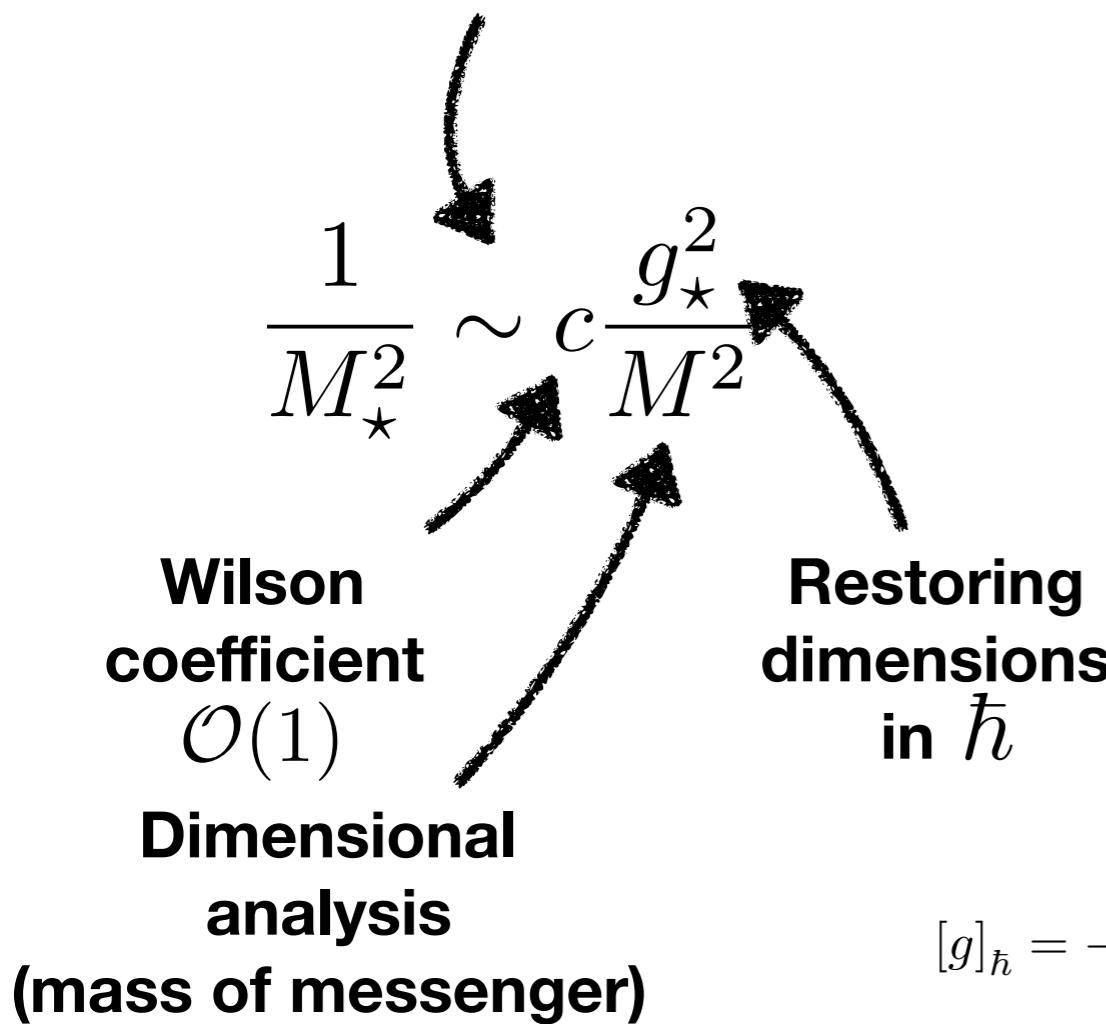


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Interaction term

Kinetic term

 $[g]_\hbar = -\frac{1}{2}$ 
 $[\psi]_\hbar = \frac{1}{2}$ 
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Number of fields in operator

$$\mathcal{L}_{eff} = \sum_{i,d} c_i \frac{\mathcal{O}_i^d}{M^{d-4}} \Rightarrow c_i \sim (\text{coupling})^{n_i - 2}$$

2

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 **Order on factor**

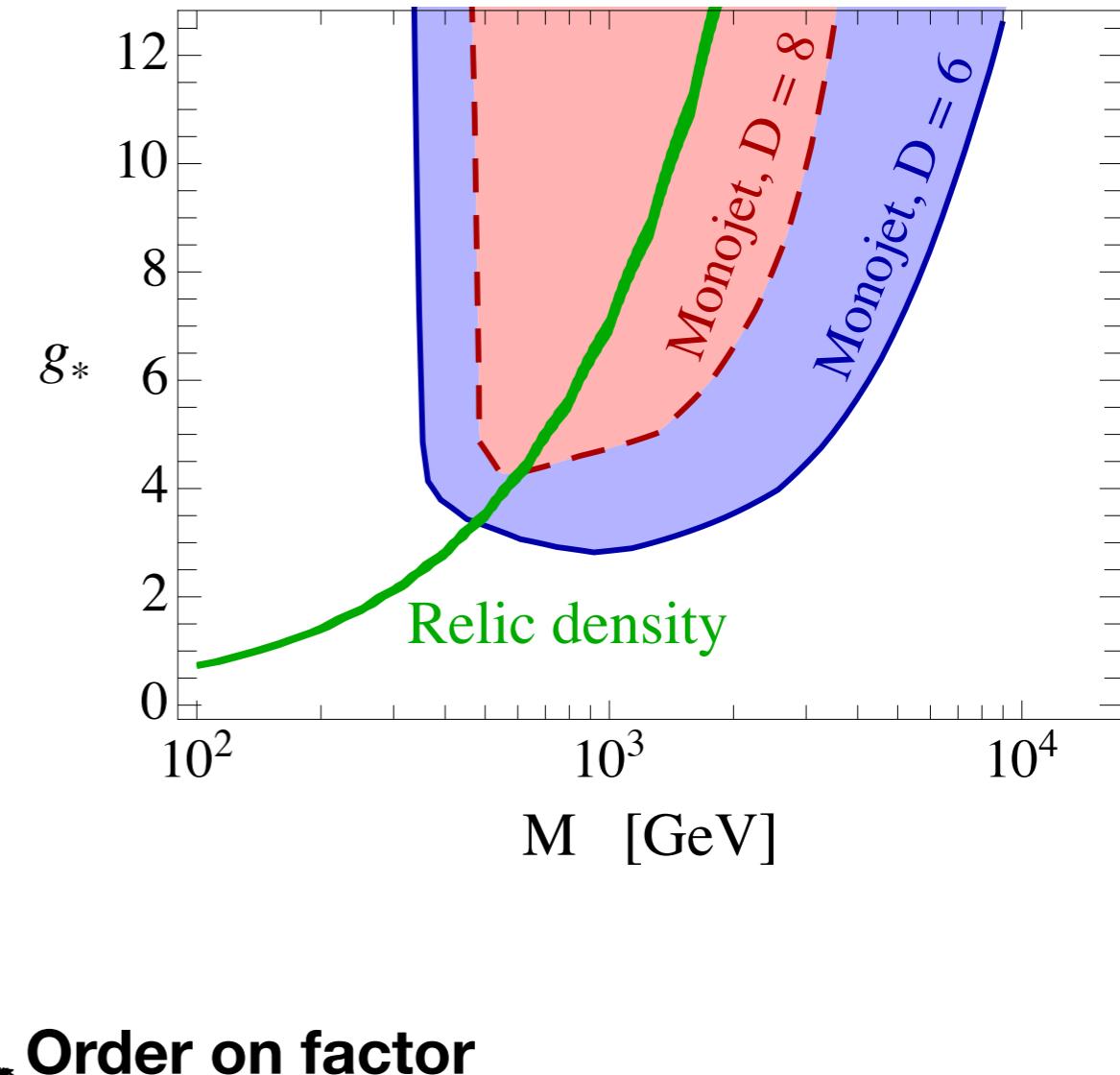
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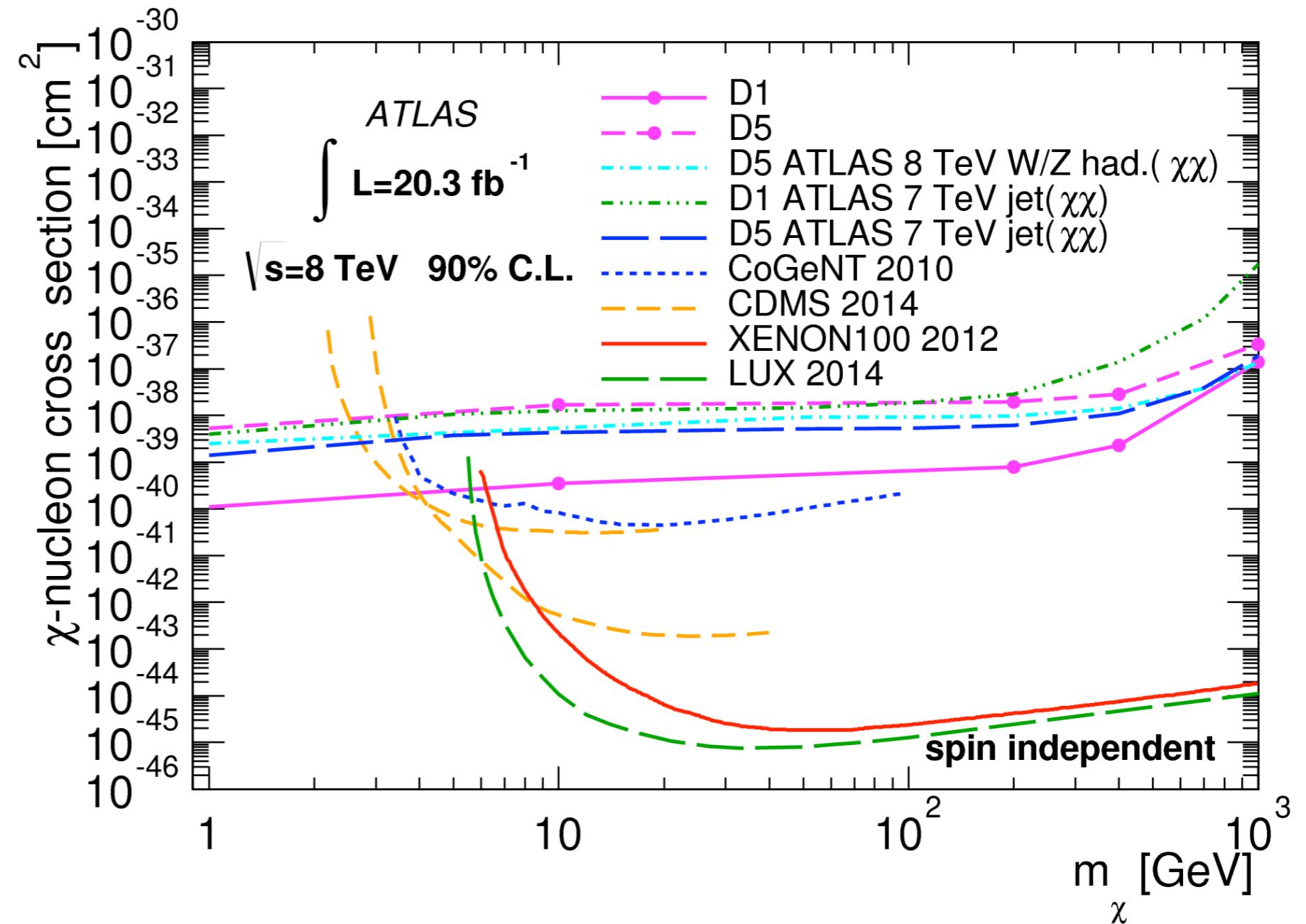
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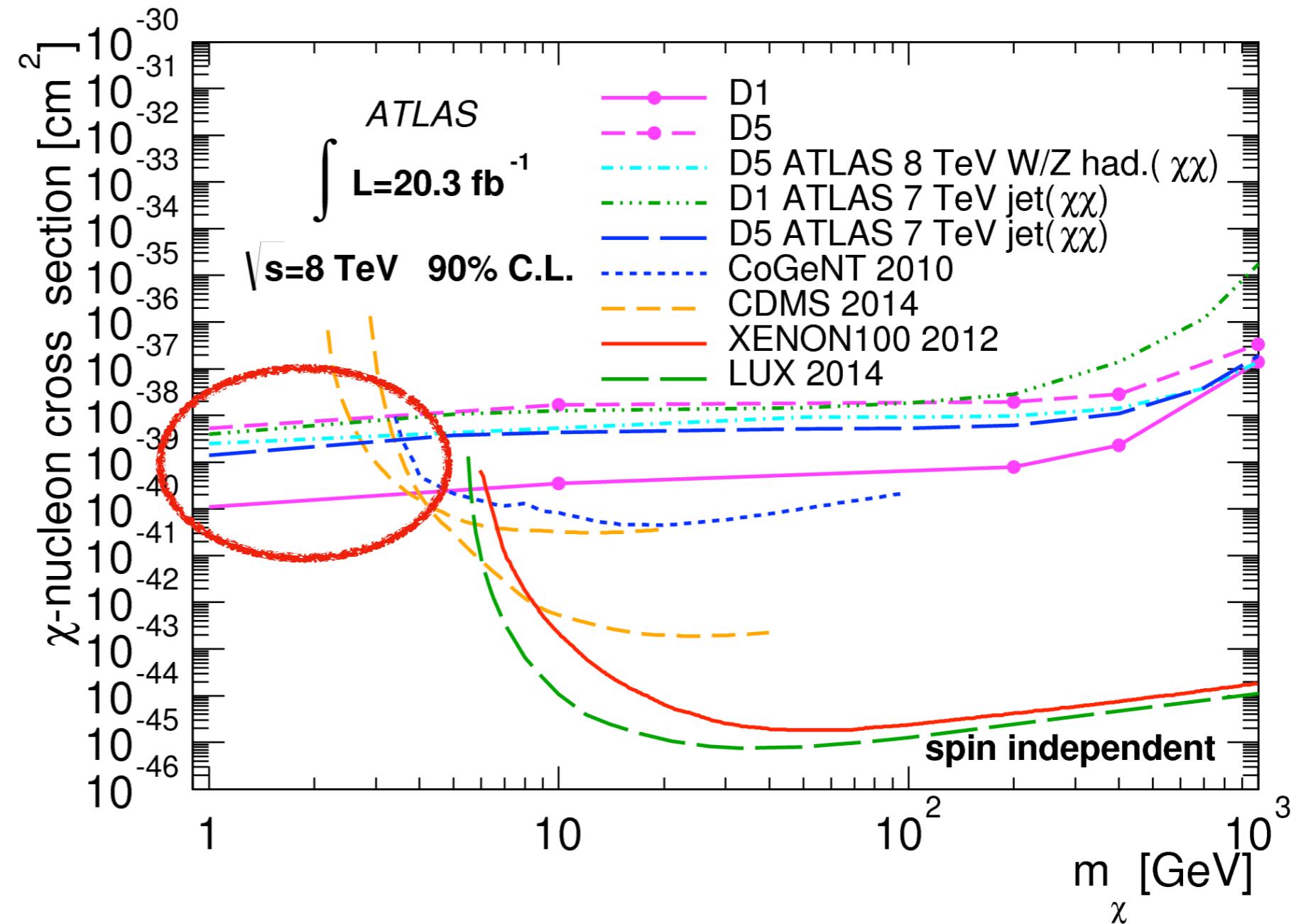
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# Light DM

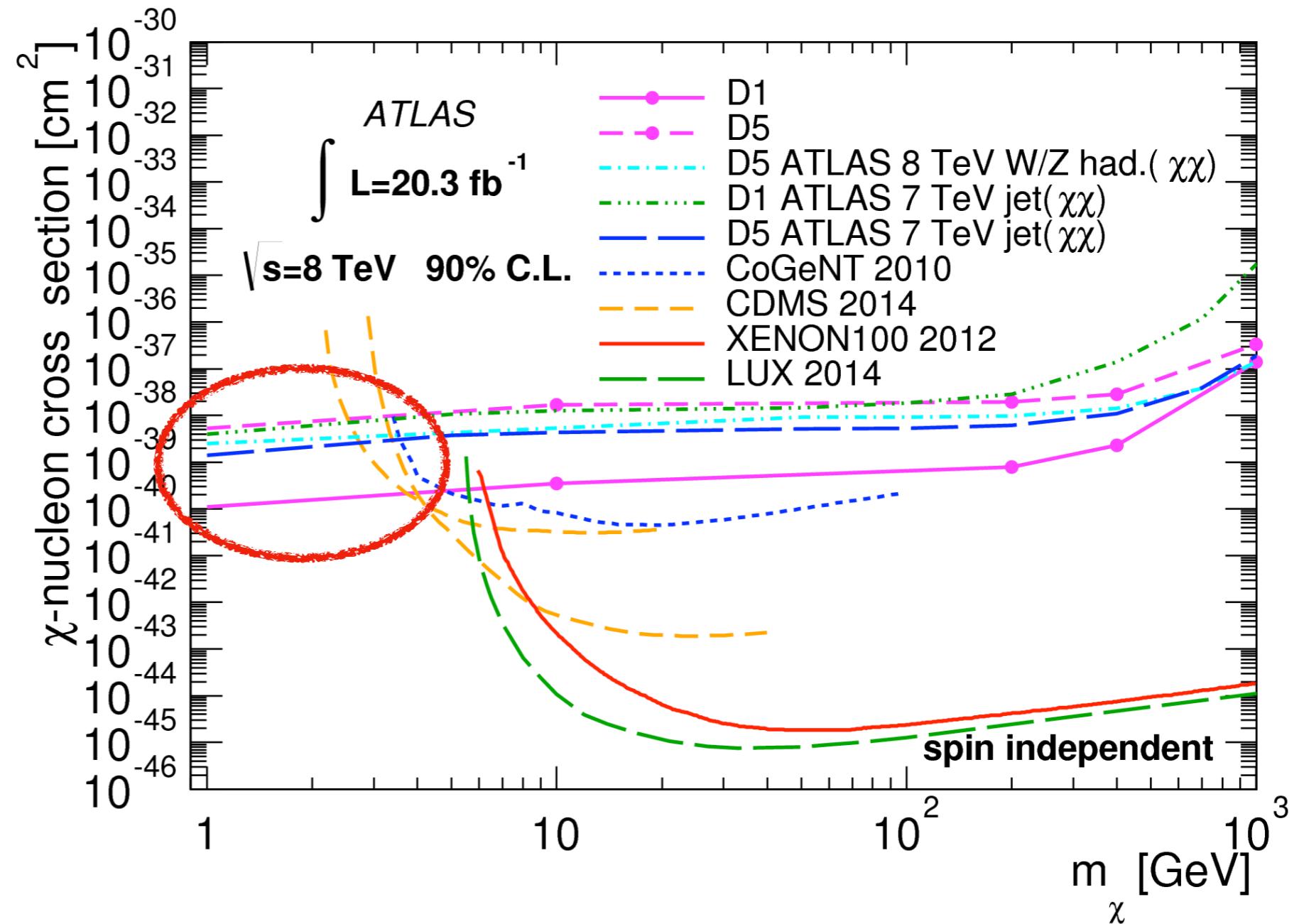


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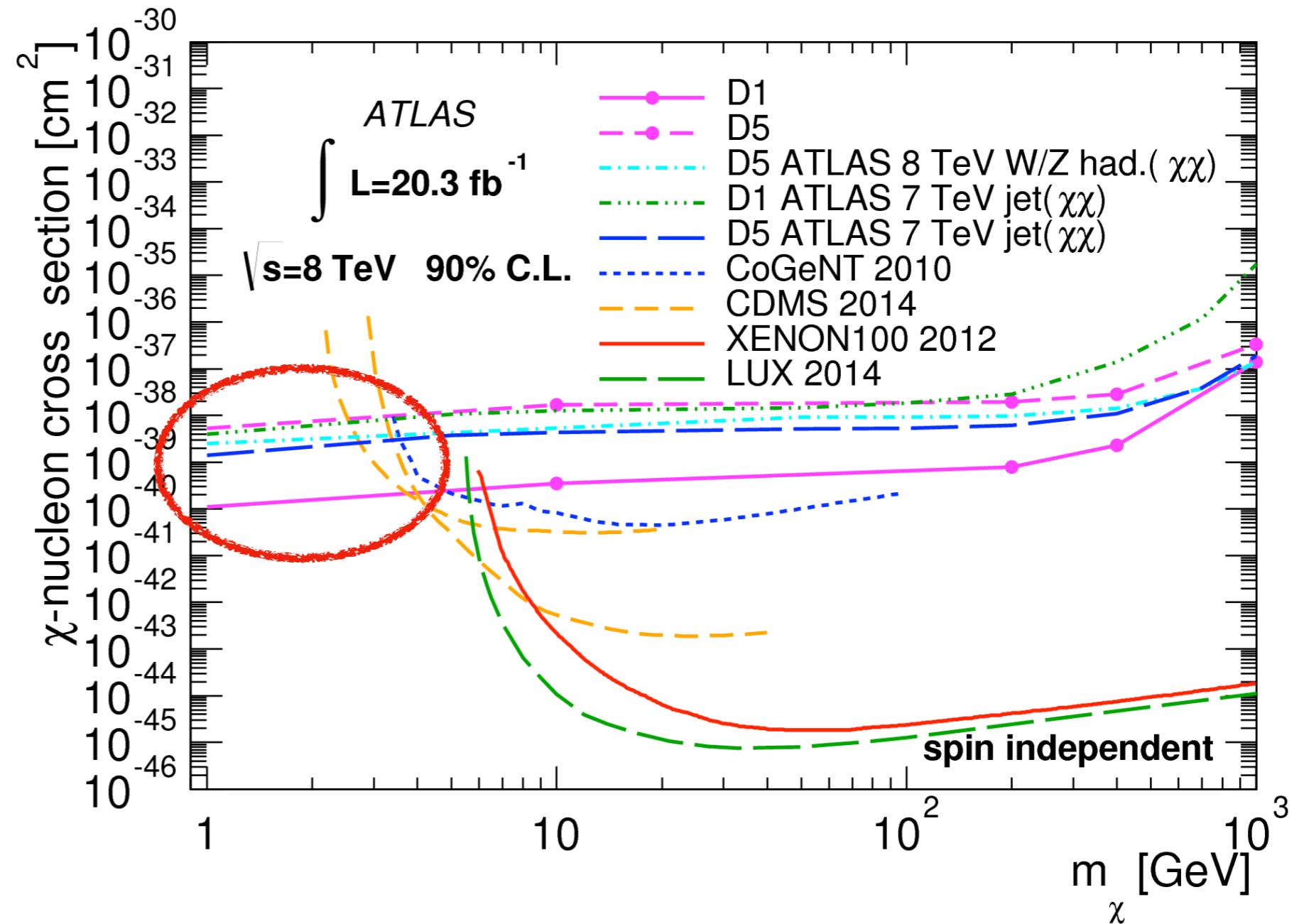
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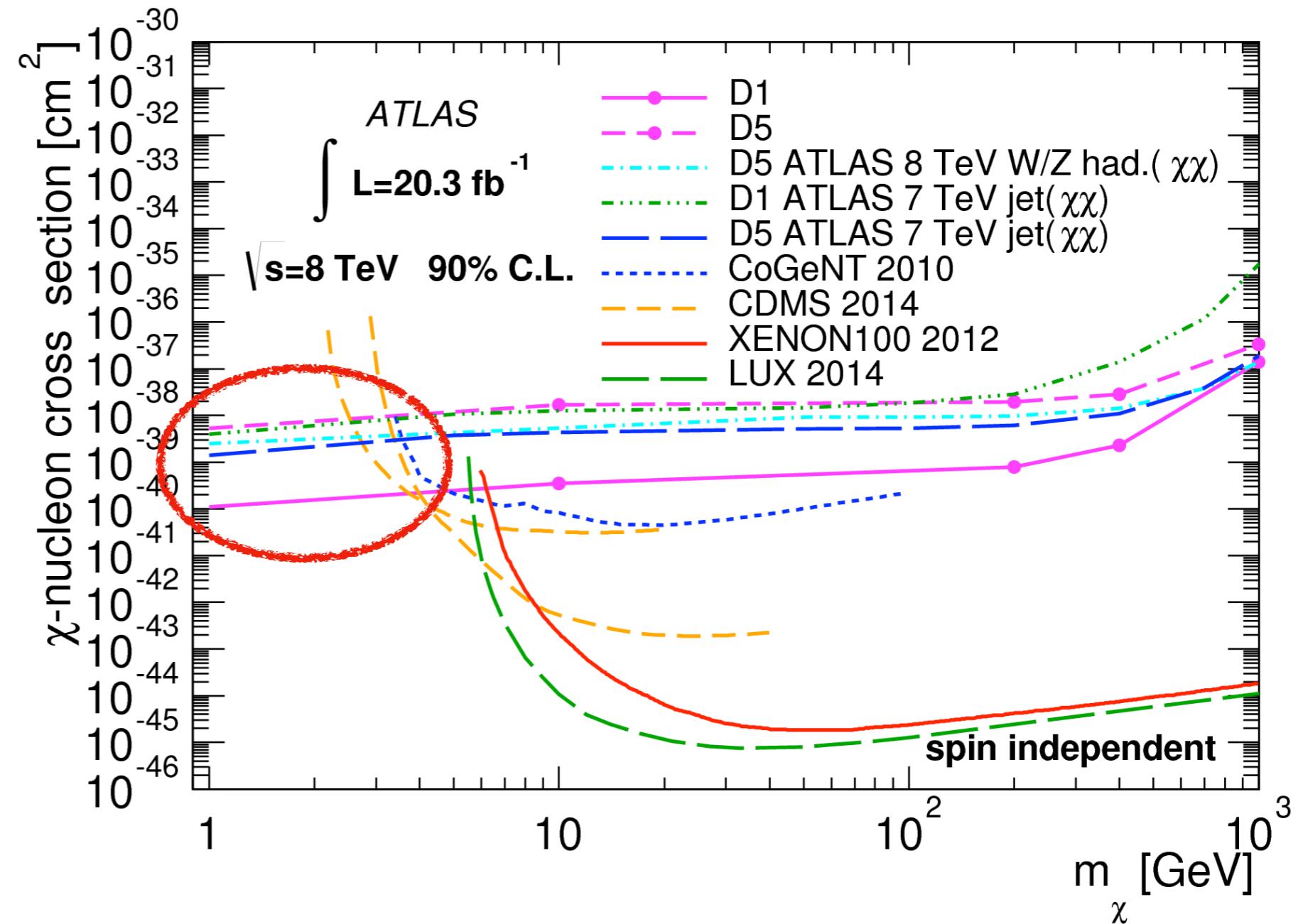


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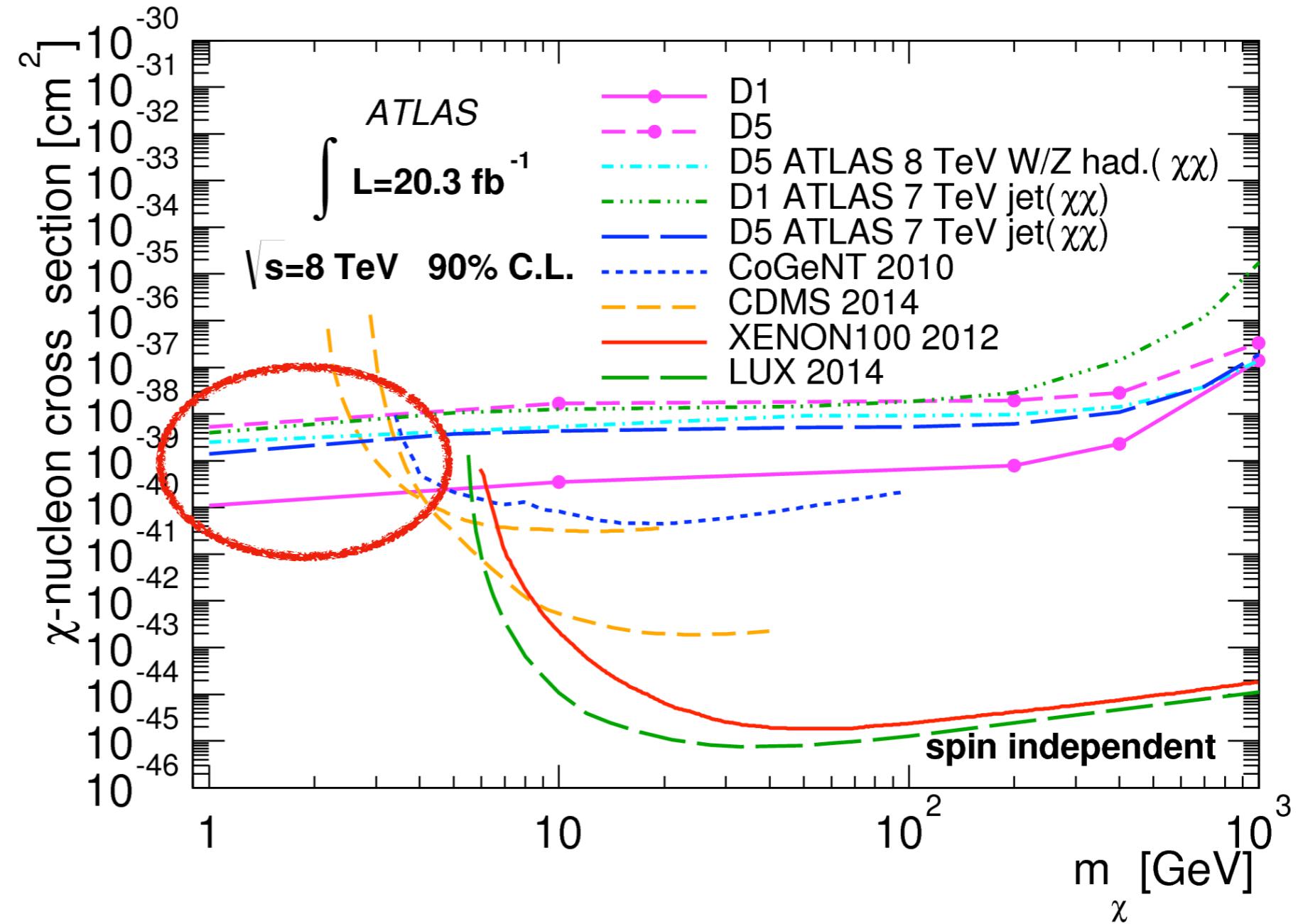
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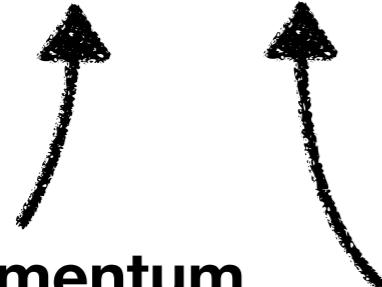
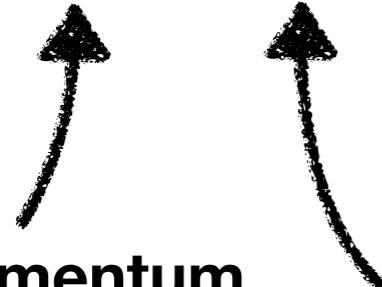
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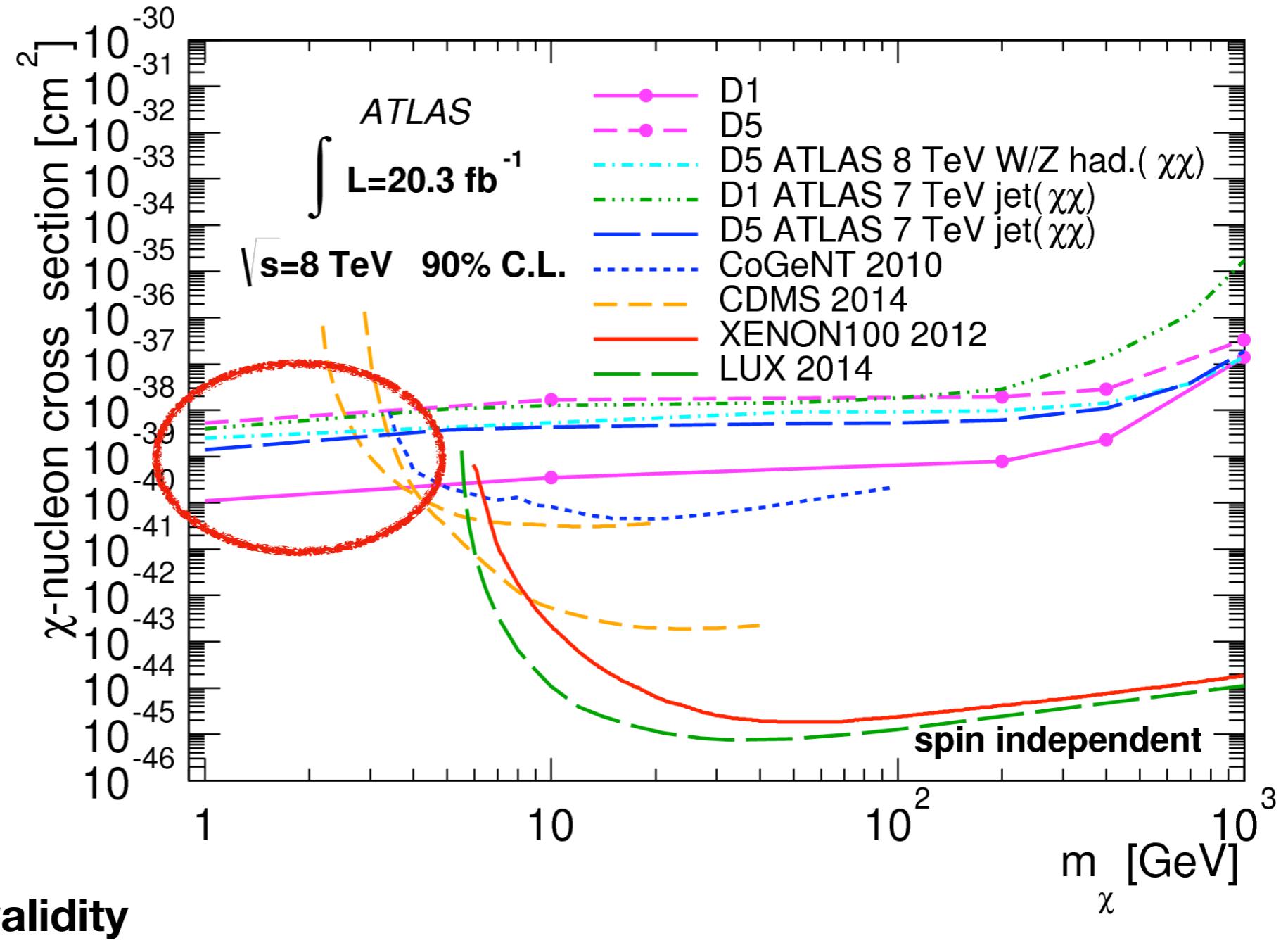
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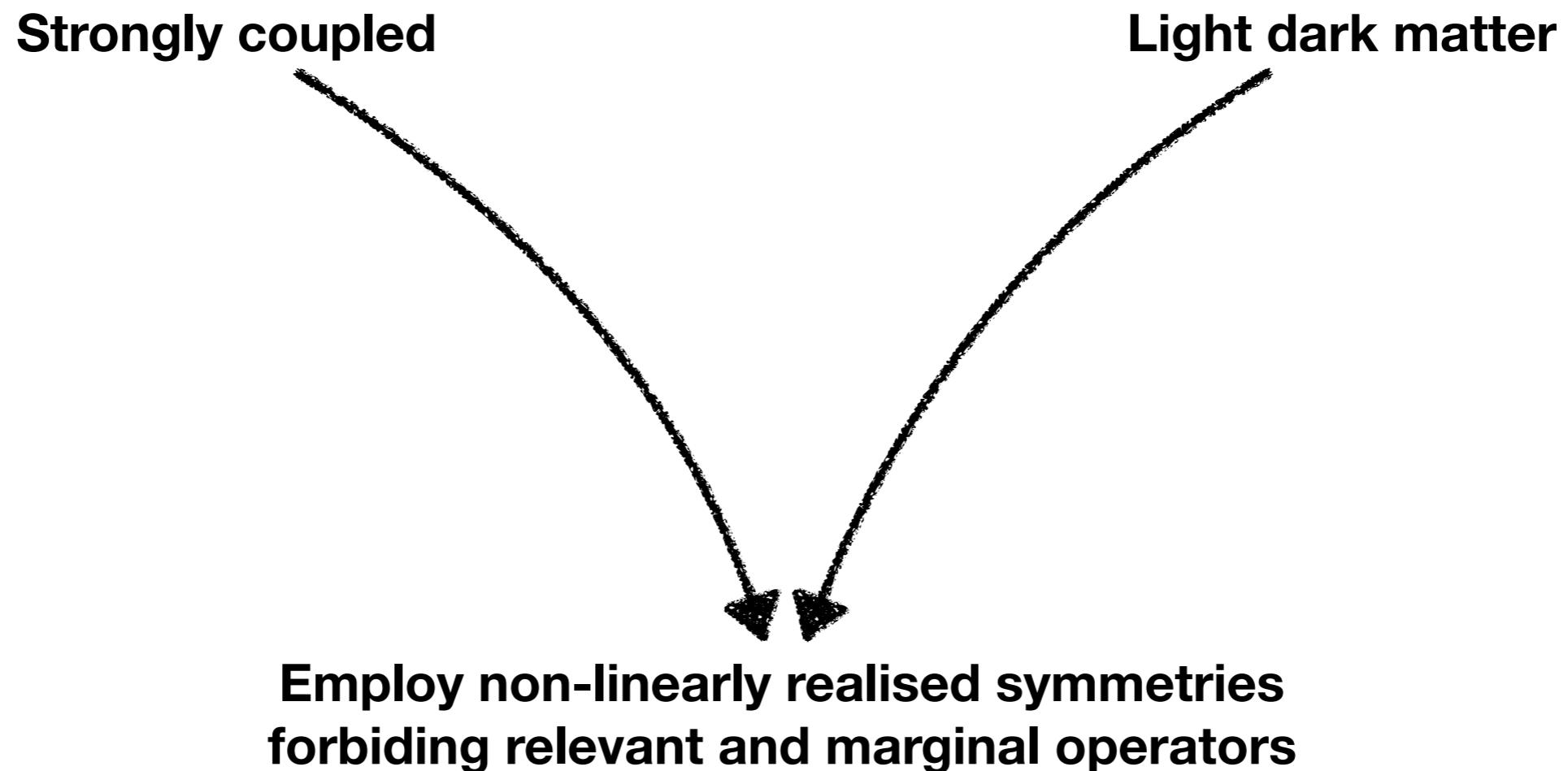
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**Minimal momentum transfer**  
**EFT validity**



# Our paradigm



# The WIMP miracle

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$$\langle \sigma v_{rel} \rangle \sim \left( \frac{\alpha_{DM}}{m_{DM}} \right)^2$$



$$\Omega_{DM} h^2 \approx \frac{10^{-26} cm^3/s}{\langle \sigma v_{rel} \rangle} \approx 0.1 \left( \frac{0.01}{\alpha_{DM}} \right)^2 \left( \frac{m_{DM}}{100 \text{GeV}} \right)^2$$

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$$\alpha_{DM} \sim \frac{g_*^2}{4\pi} \left( \frac{E}{M} \right)^{d-4} \quad E \sim m_{DM}$$

e.g.  $d=6$        $\Omega_{DM} h^2 \approx 0.1 \left( \frac{4\pi}{g_*} \right)^4 \left( \frac{5 \text{GeV}}{m_{DM}} \right)^2 \left( \frac{M}{3 \text{TeV}} \right)^4$

# Consistent Recast

Discard events with  $E > M$

Racco, Wulzer, Zwirner  
1502.04701

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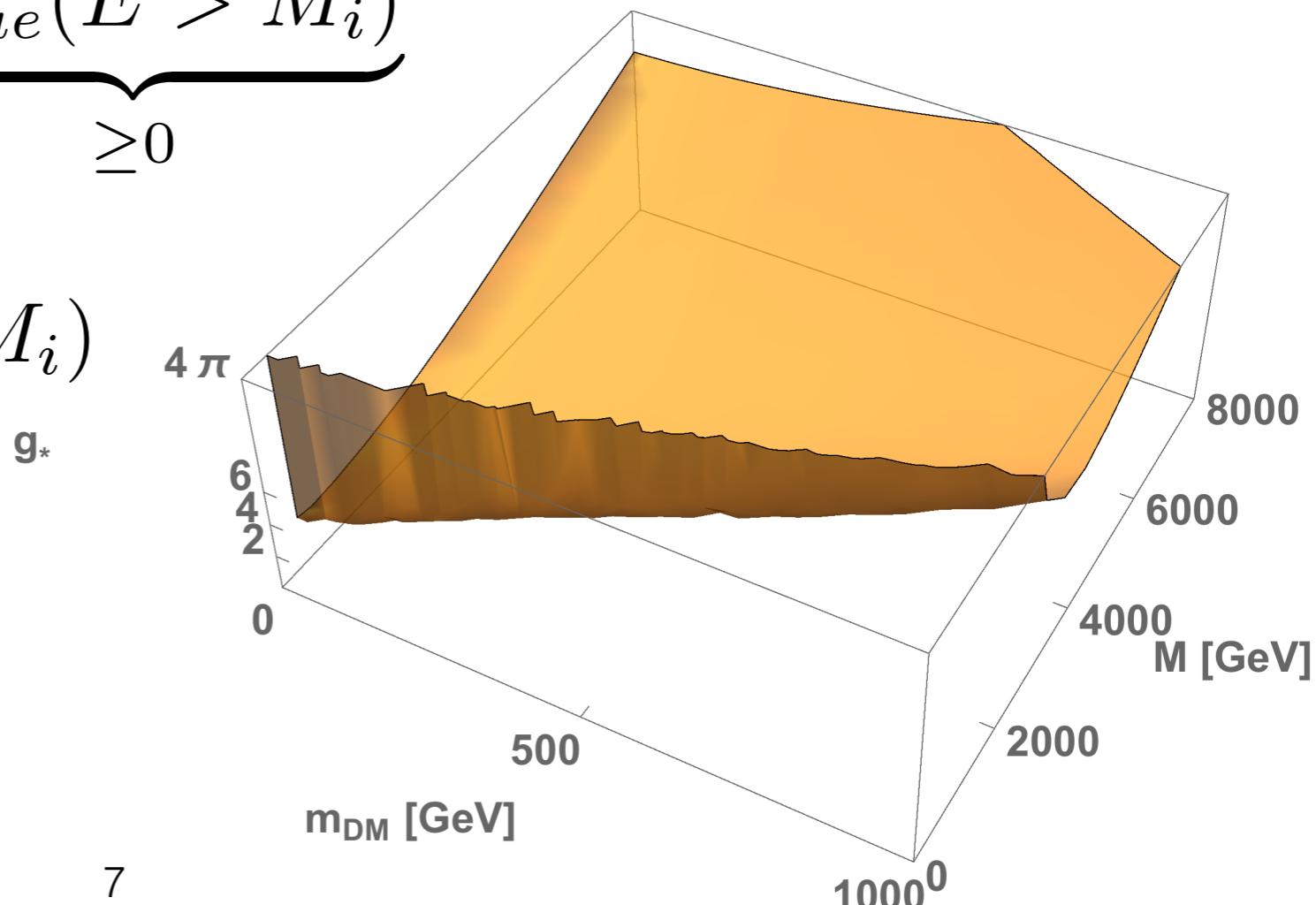
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Recast of '15 ATLAS  
mono-jet search

ATLAS collaboration  
1502.01518



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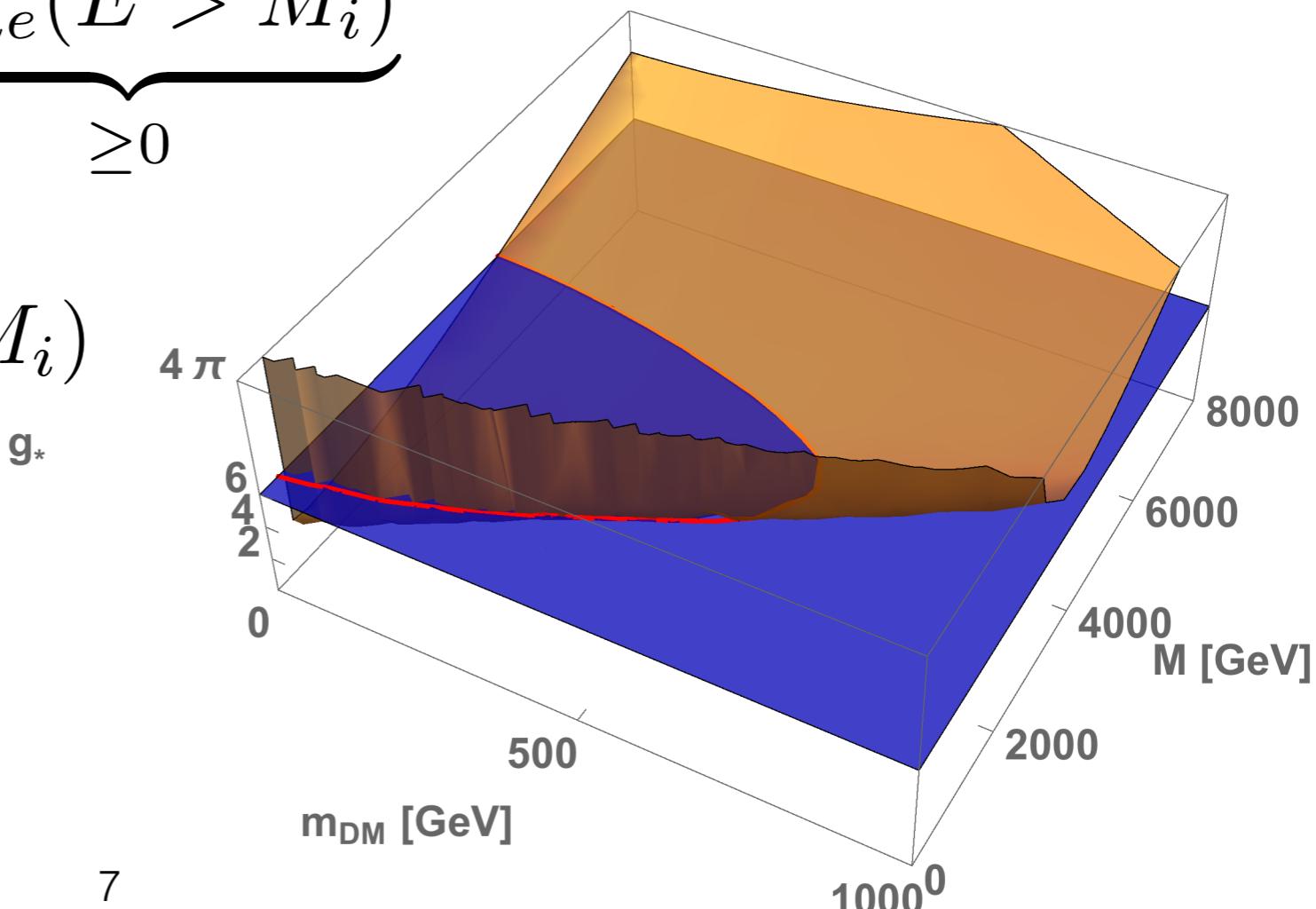
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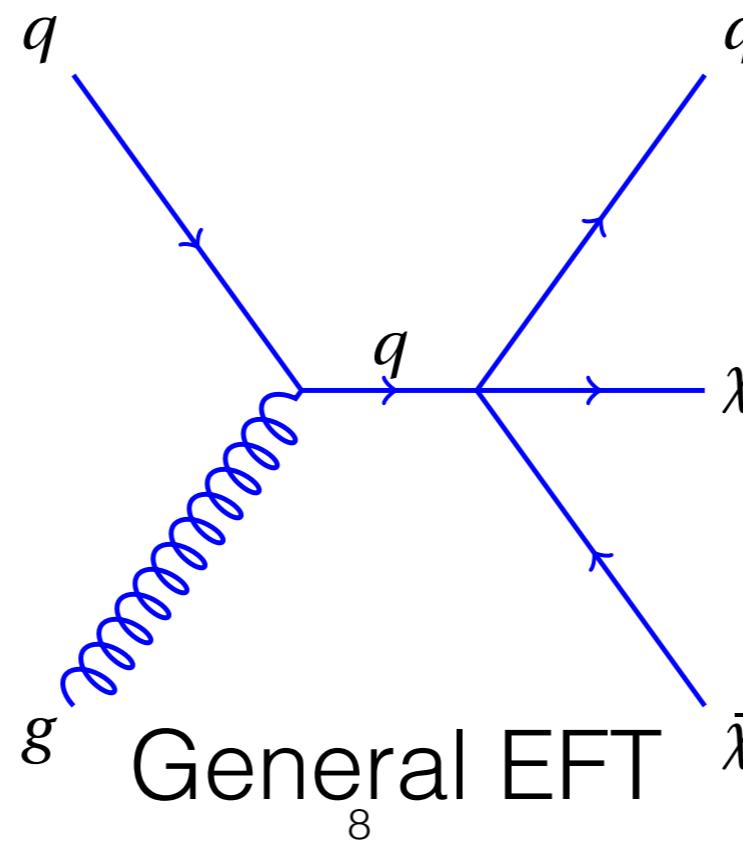
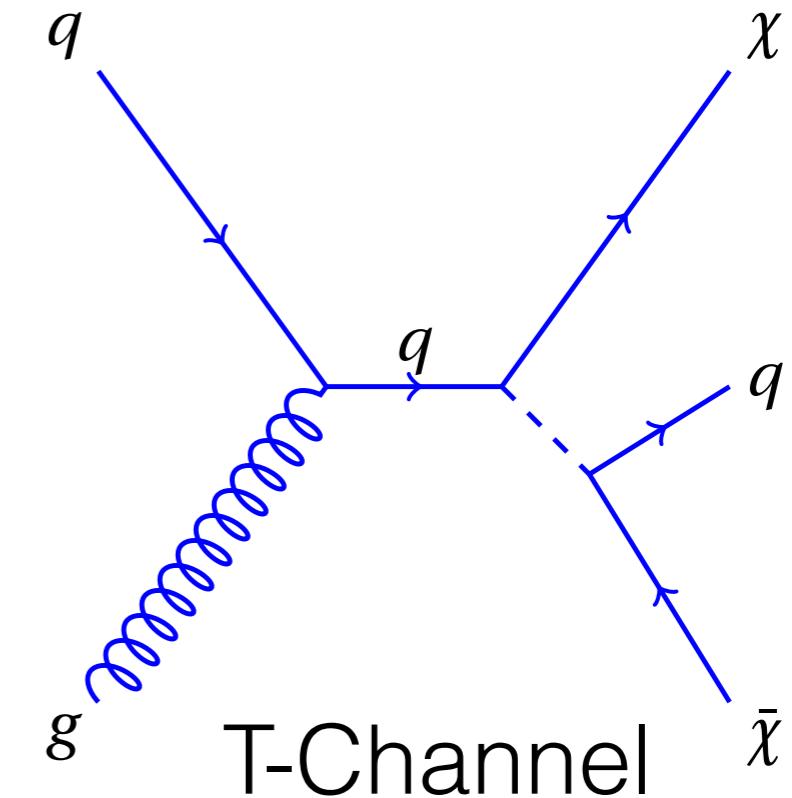
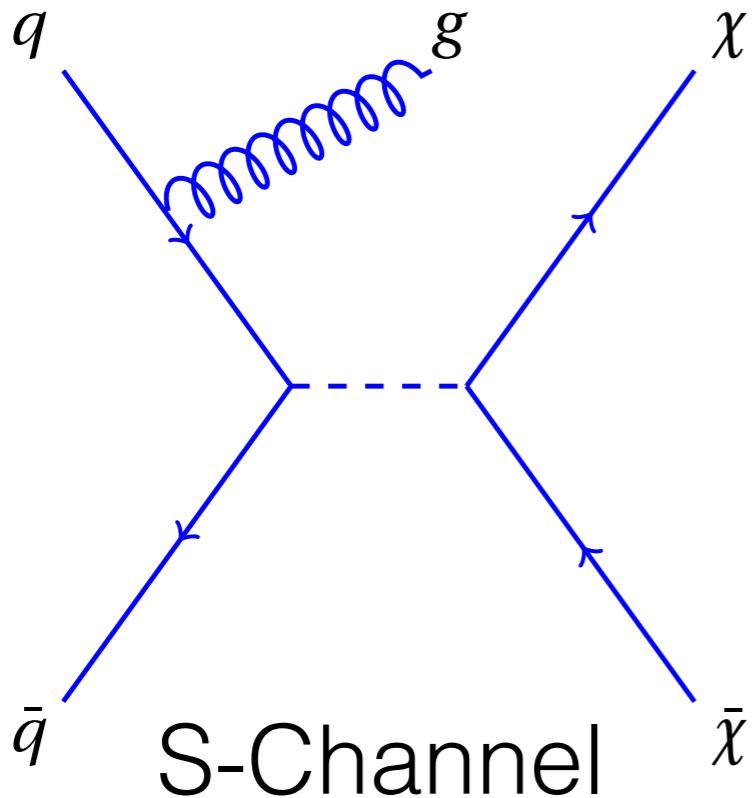
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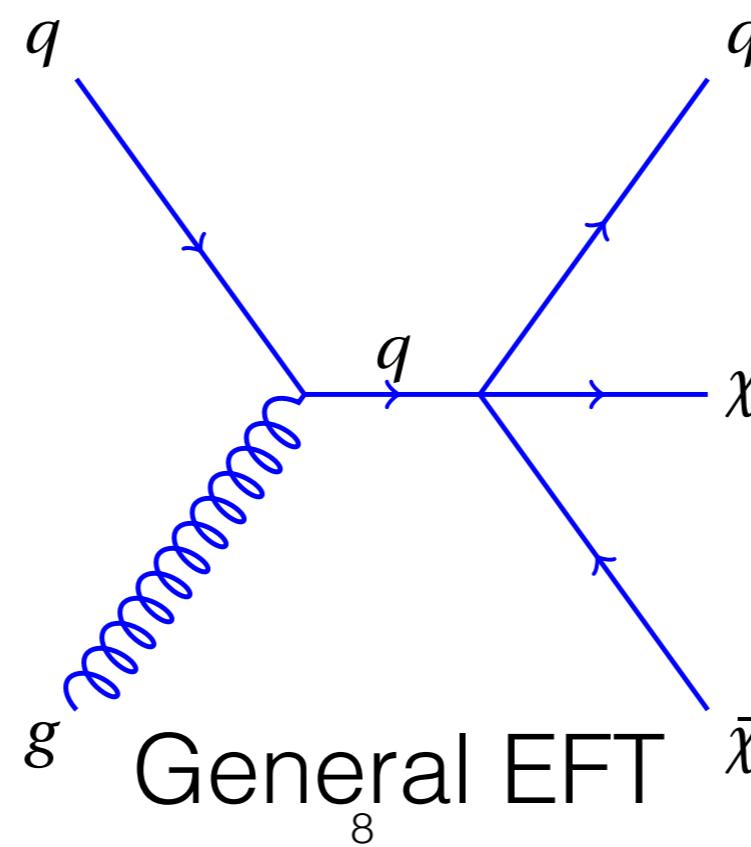
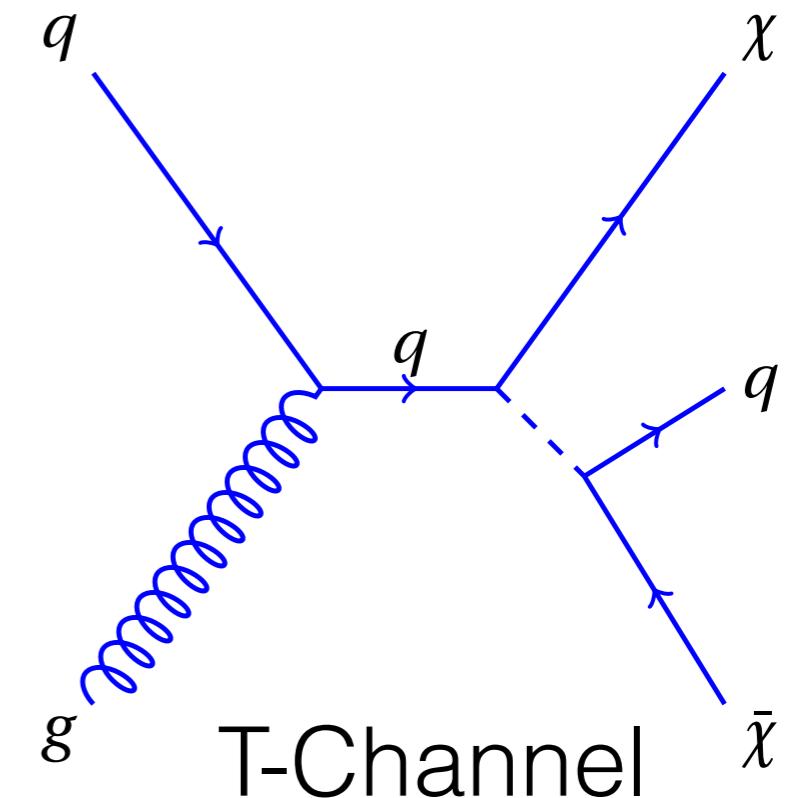
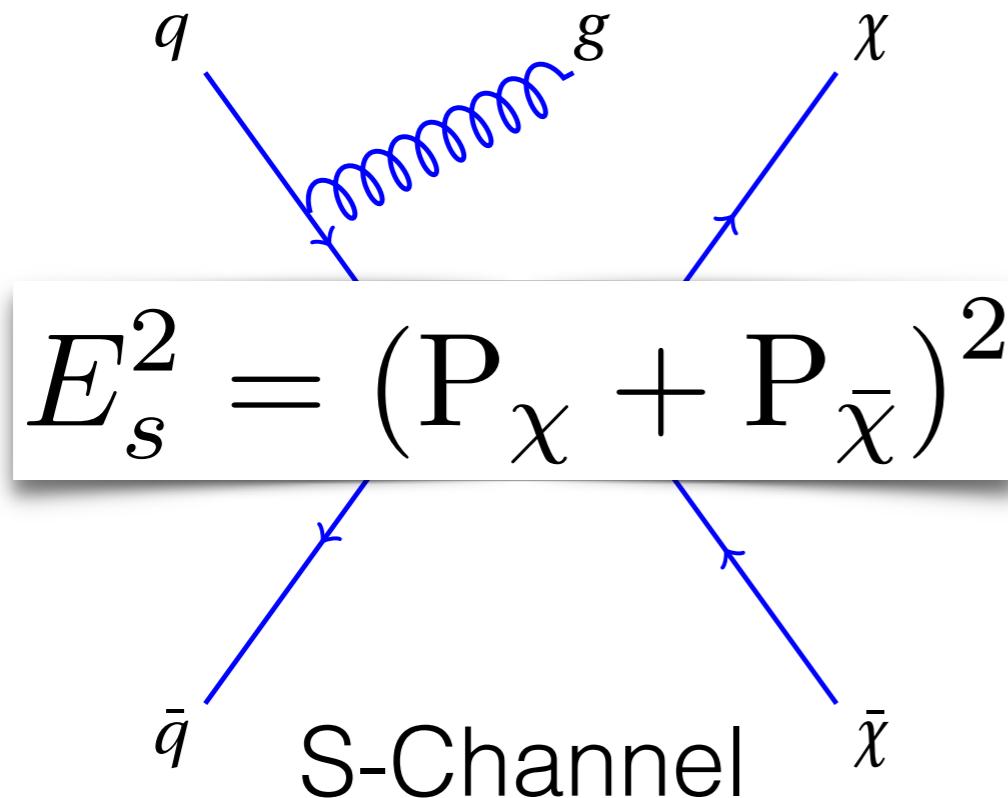
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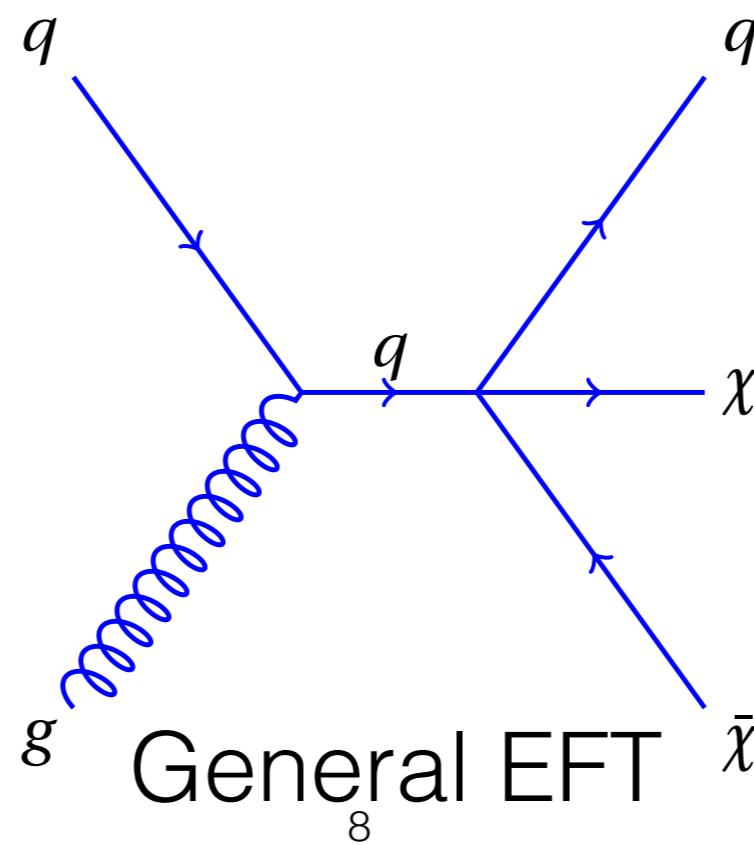
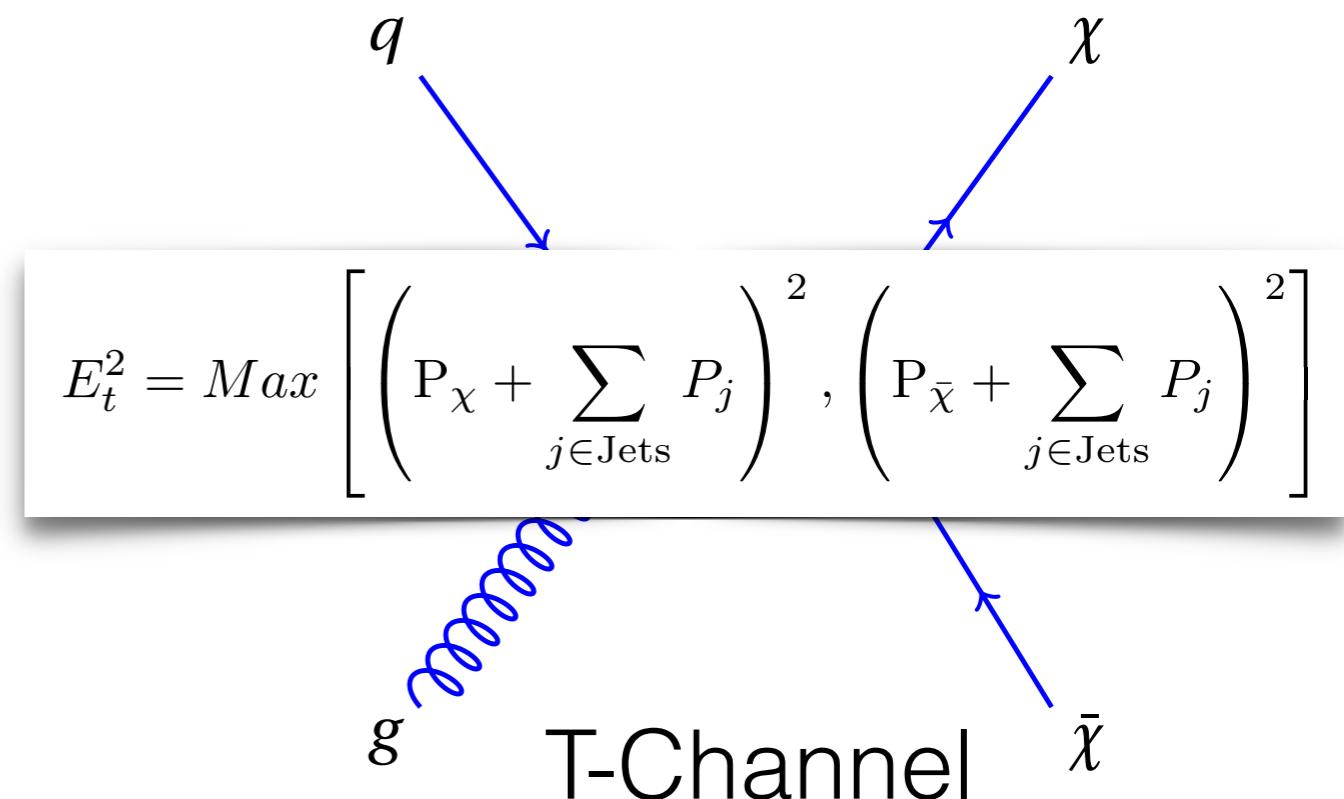
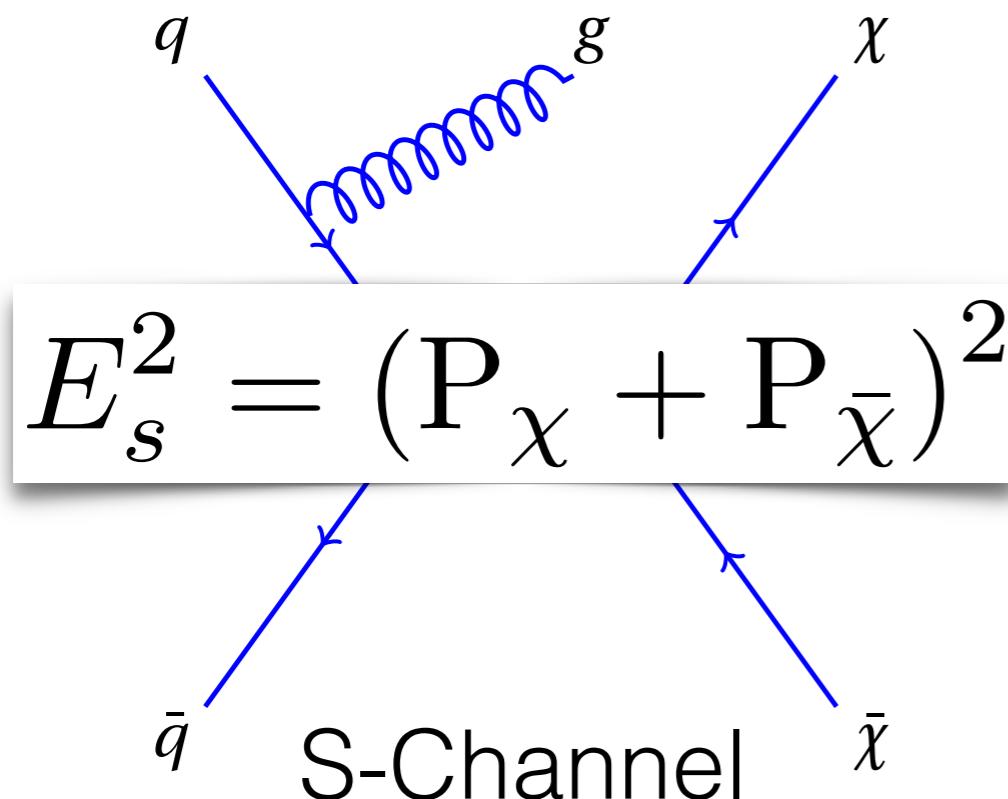
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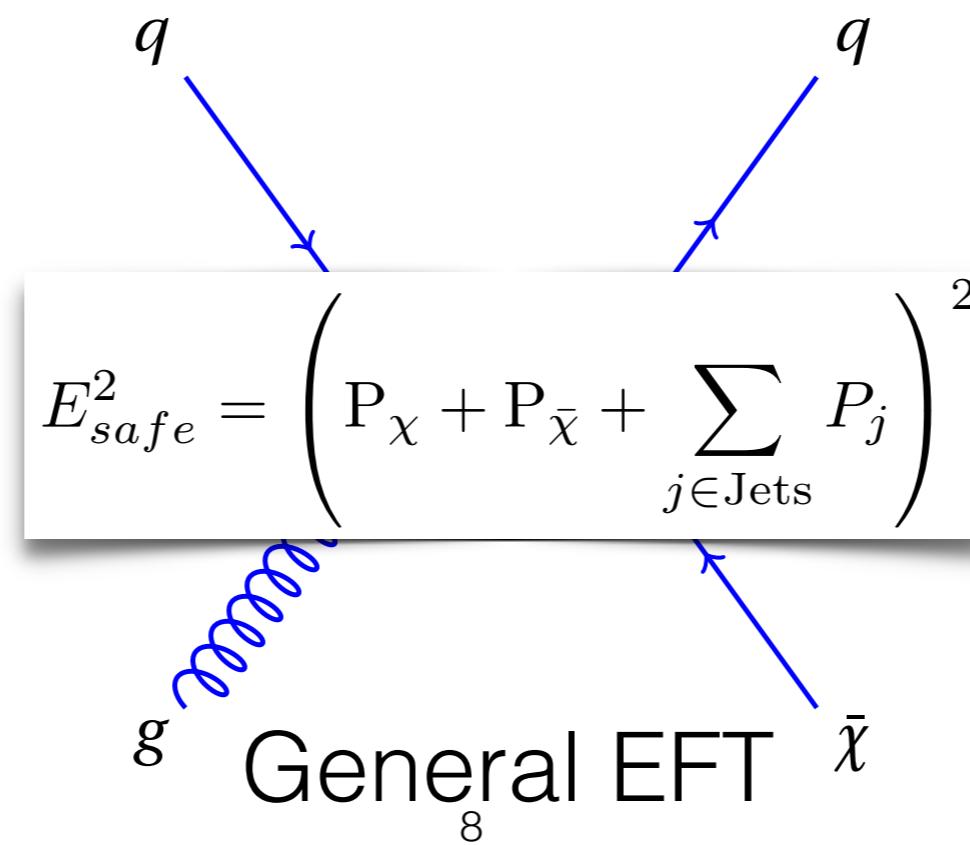
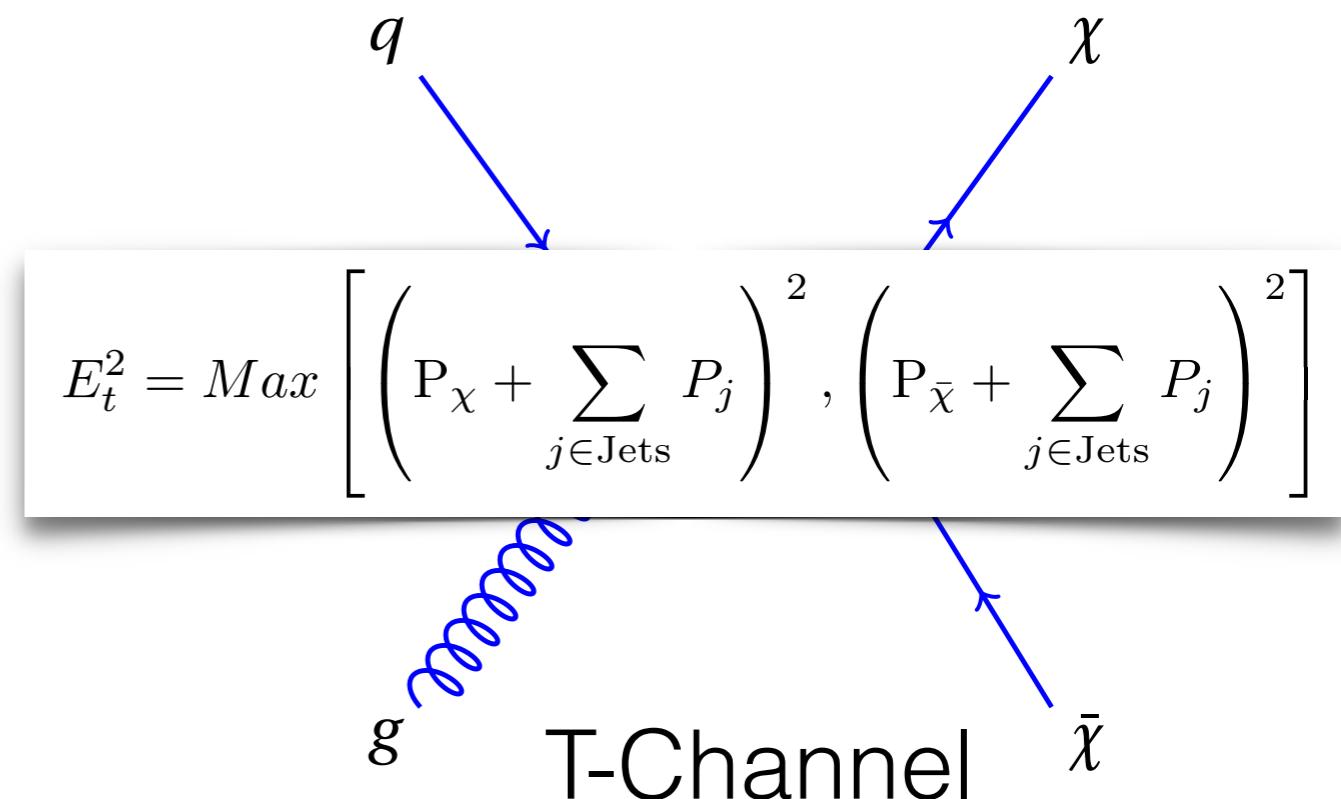
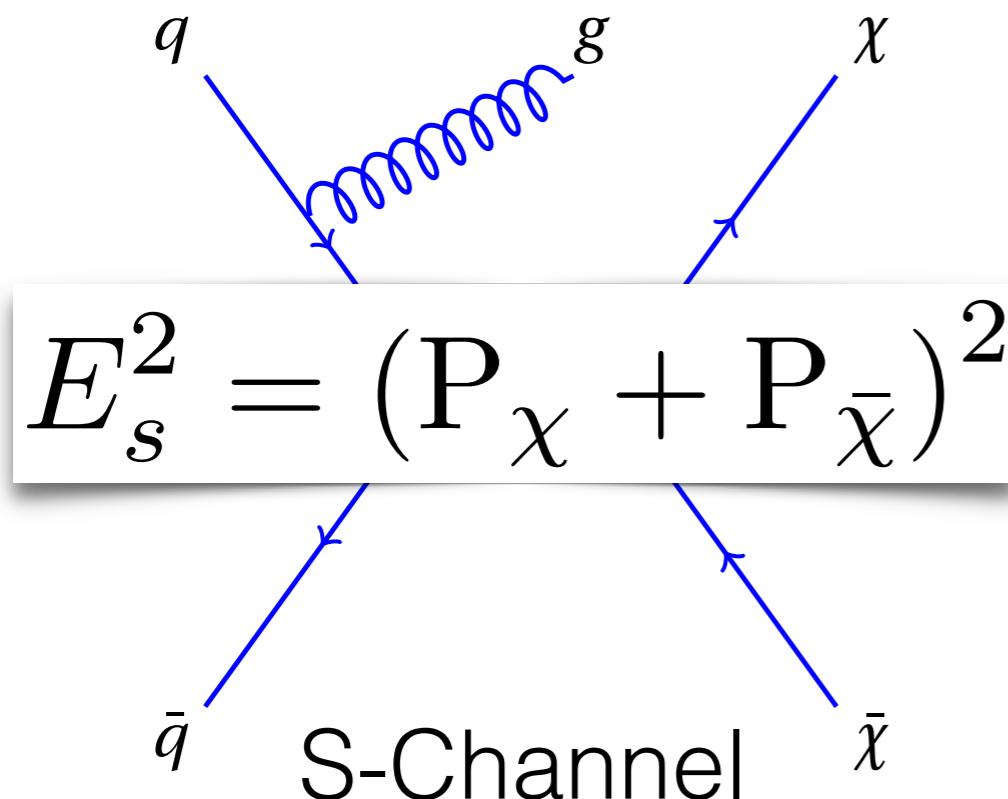
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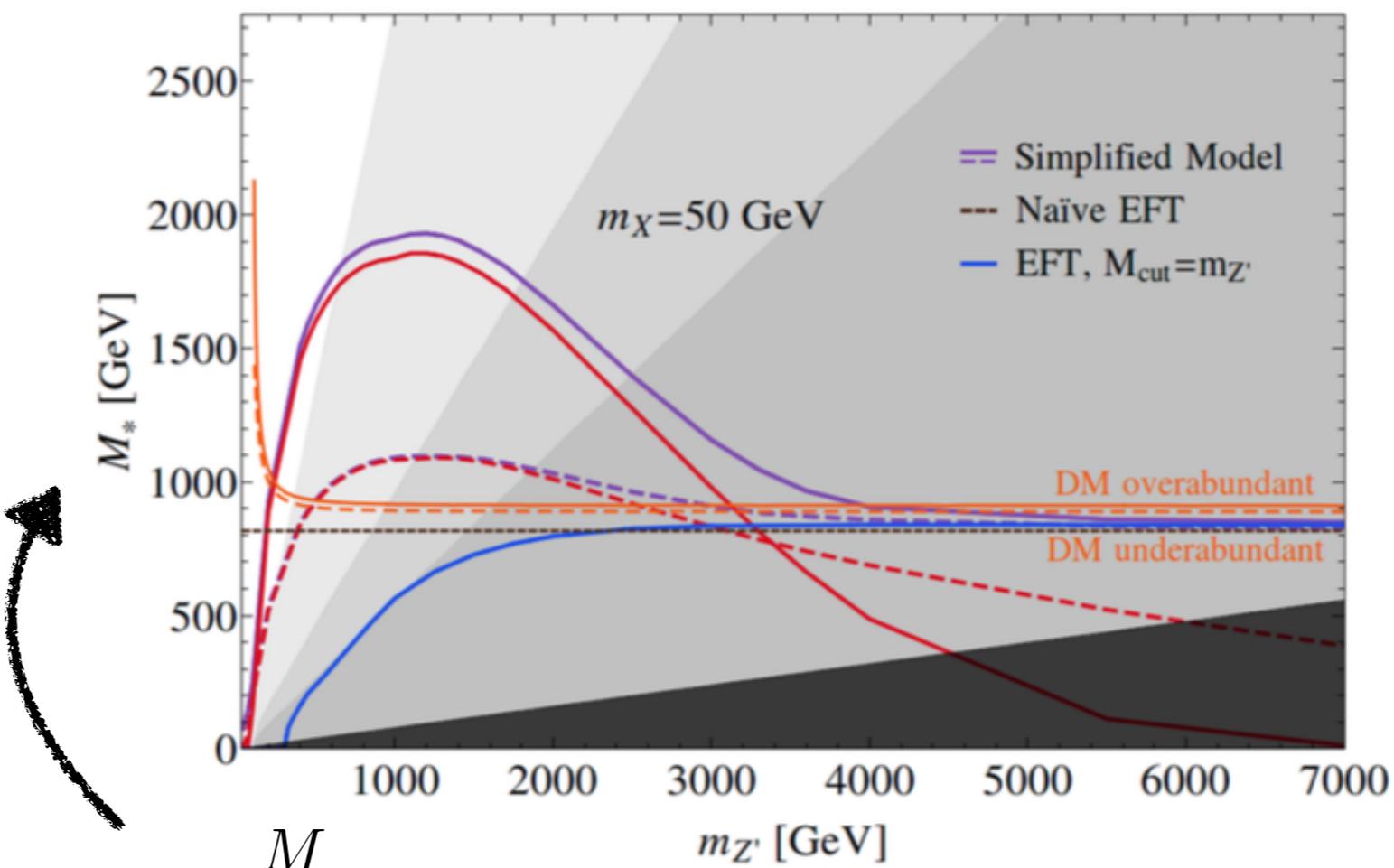
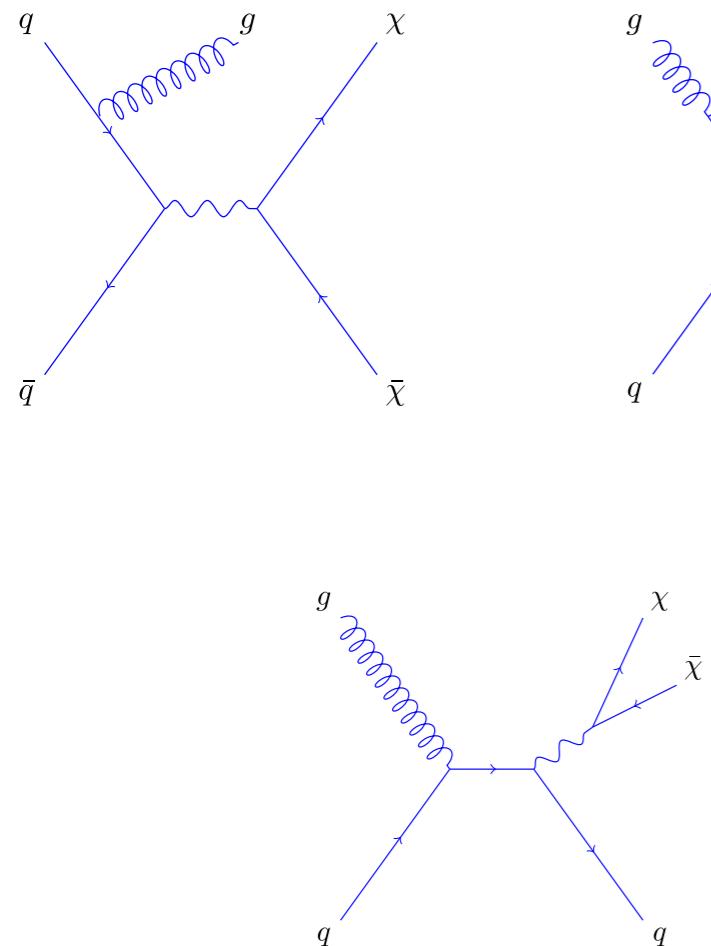


# The right energy scale



# Checking validity

Comparing with Z'  
simplified model:



$$M_* = \frac{M}{g_*}$$

Figure from:  
1502.04701

# Assumptions for EFT

- One coupling one scale
- $2 \rightarrow 2$  processes only
- Only keep lowest order terms and neglect higher order ones.
- Respect all the SM (exact and approximate) symmetries
- Non-linearly realised symmetries protect small DM masses

# Scalar DM

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- Symmetry breaking pattern  $G/H$  dictates degrees of freedom and interactions.
- Write all the interactions compatible with SM symmetries (exact and approximate).
- Weight terms that break  $G/H$  symmetry by breaking factor  $\left(\frac{m_\phi}{M}\right)^2$

# Scalar DM

$D = 6$

$$\begin{aligned} {}_6\mathcal{L}_{\text{eff}}^{DM_\phi} = & c_V^V \frac{g_*^2}{M^2} \phi^\dagger \partial_\mu \phi \psi^\dagger \bar{\sigma}^\mu \psi + c_B^{dip} \frac{g_*}{M^2} \partial_\mu \phi^\dagger \partial_\nu \phi B^{\mu\nu} \\ & + c_H^S \frac{g_*^2}{M^2} |\partial_\mu \phi|^2 |H|^2 + c_H^S \frac{g_*^2 m_{\phi,H}^2}{M^2} |\phi|^2 |H|^2 \\ & + c_\psi^S \frac{g_*^2 y_\psi}{M^2} |\phi|^2 \psi \psi H \end{aligned}$$

$D = 8$

$$\begin{aligned} {}_8\mathcal{L}_{\text{eff}}^{DM} = & C_V^S \frac{g_*^2 m_\phi^2}{M^4} |\phi|^2 V_{\mu\nu}^a V^{a\mu\nu} + C_\psi^S \frac{g_*^2 y_\psi}{M^4} |\partial^\mu \phi|^2 \psi \psi H \\ & + C_V^S \frac{g_*^2}{M^4} |\partial^\mu \phi|^2 V_{\nu\rho}^a V^{a\rho\nu} + C_H^S \frac{g_*^2}{M^4} |\partial^\mu \phi|^2 |D^\nu H|^2 \\ & + C_V^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi V_{\mu\rho}^a V_\nu^{a\rho} + C_H^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi D_{[\mu} H^\dagger D_{\nu]} H \\ & + C_\psi^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi \psi^\dagger \bar{\sigma}_\mu D_\nu \psi, \end{aligned}$$

**Weyl spinors!**

# Scalar DM

SU(2)/U(1), only Monojet relevant

$$D = 6$$

$$\begin{aligned} {}_6\mathcal{L}_{\text{eff}}^{DM_\phi} = & c_V^V \frac{g_*^2}{M^2} \phi^\dagger \partial_\mu \phi \psi^\dagger \bar{\sigma}^\mu \psi + c_B^{dip} \frac{g_*}{M^2} \partial_\mu \phi^\dagger \partial_\nu \phi B^{\mu\nu} \\ & + c_H^S \frac{g_*^2}{M^2} |\partial_\mu \phi|^2 |H|^2 + c_H^S \frac{g_*^2 m_{\phi,H}^2}{M^2} |\phi|^2 |H|^2 \\ & + c_\psi^S \frac{g_*^2 y_\psi}{M^2} |\phi|^2 \psi \psi H \end{aligned}$$

$$D = 8$$

$$\begin{aligned} {}_8\mathcal{L}_{\text{eff}}^{DM} = & C_V^S \frac{g_*^2 m_\phi^2}{M^4} |\phi|^2 V_{\mu\nu}^a V^{a\mu\nu} + C_\psi^S \frac{g_*^2 y_\psi}{M^4} |\partial^\mu \phi|^2 \psi \psi H \\ & + C_V^S \frac{g_*^2}{M^4} |\partial^\mu \phi|^2 V_{\nu\rho}^a V^{a\rho\nu} + C_H^S \frac{g_*^2}{M^4} |\partial^\mu \phi|^2 |D^\nu H|^2 \\ & + C_V^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi V_{\mu\rho}^a V_{\nu}^{a\rho} + C_H^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi D_{[\mu} H^\dagger D_{\nu]} H \\ & + C_\psi^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi \psi^\dagger \bar{\sigma}_\mu D_\nu \psi, \end{aligned}$$

**Weyl spinors!**

# Scalar DM

U(1)/Z<sub>2</sub>, only Monojet relevant

$$D = 6$$

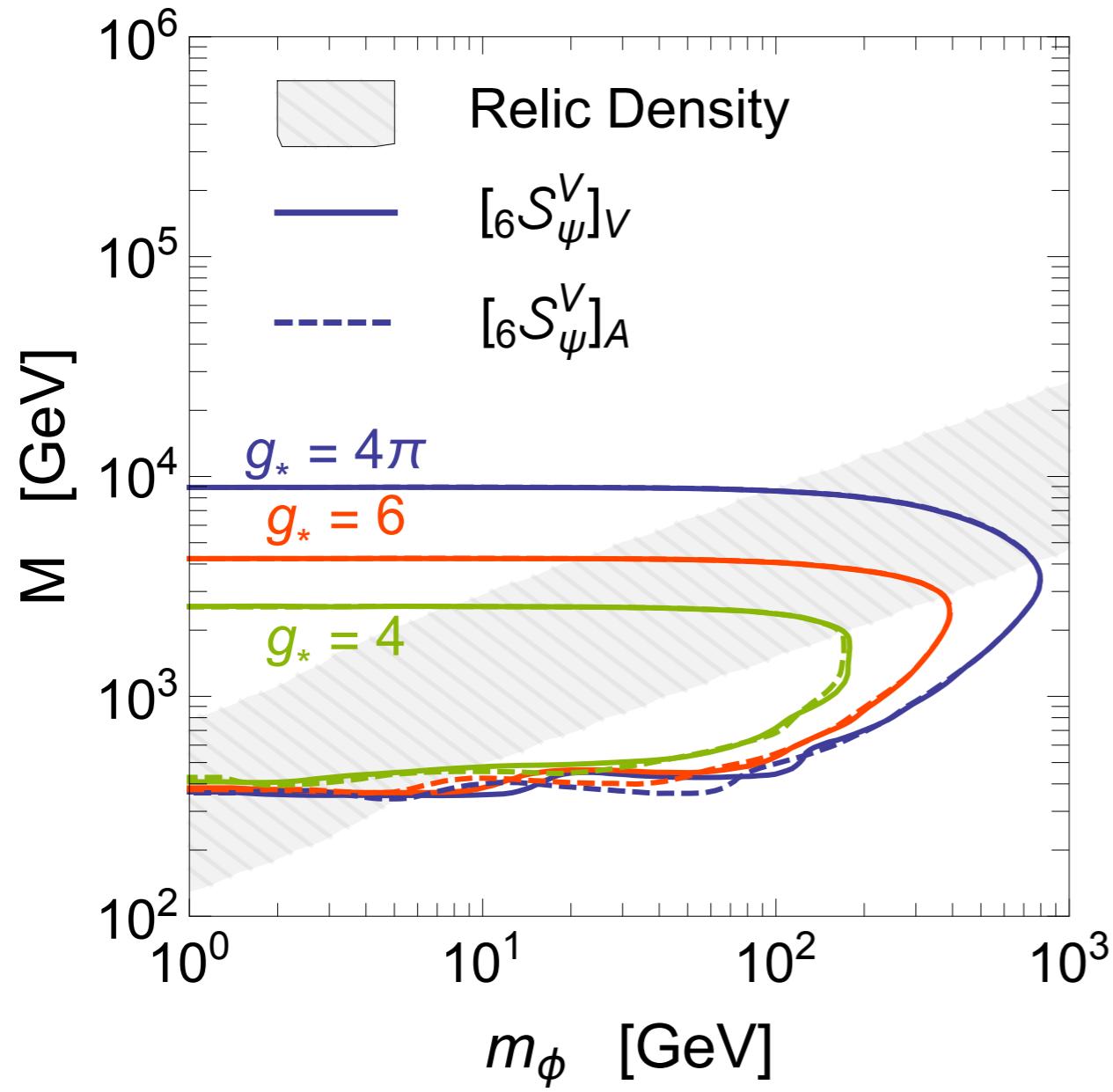
$$\begin{aligned} {}_6\mathcal{L}_{\text{eff}}^{DM_\phi} = & c_V^V \frac{g_*^2}{M^2} \phi^\dagger \partial_\mu \phi \psi^\dagger \bar{\sigma}^\mu \psi + c_B^{dip} \frac{g_*}{M^2} \partial_\mu \phi^\dagger \partial_\nu \phi B^{\mu\nu} \\ & + c_H^S \frac{g_*^2}{M^2} |\partial_\mu \phi|^2 |H|^2 + c_H^S \frac{g_*^2 m_{\phi,H}^2}{M^2} |\phi|^2 |H|^2 \\ & + c_\psi^S \frac{g_*^2 y_\psi}{M^2} |\phi|^2 \psi \psi H \end{aligned}$$

$$D = 8$$

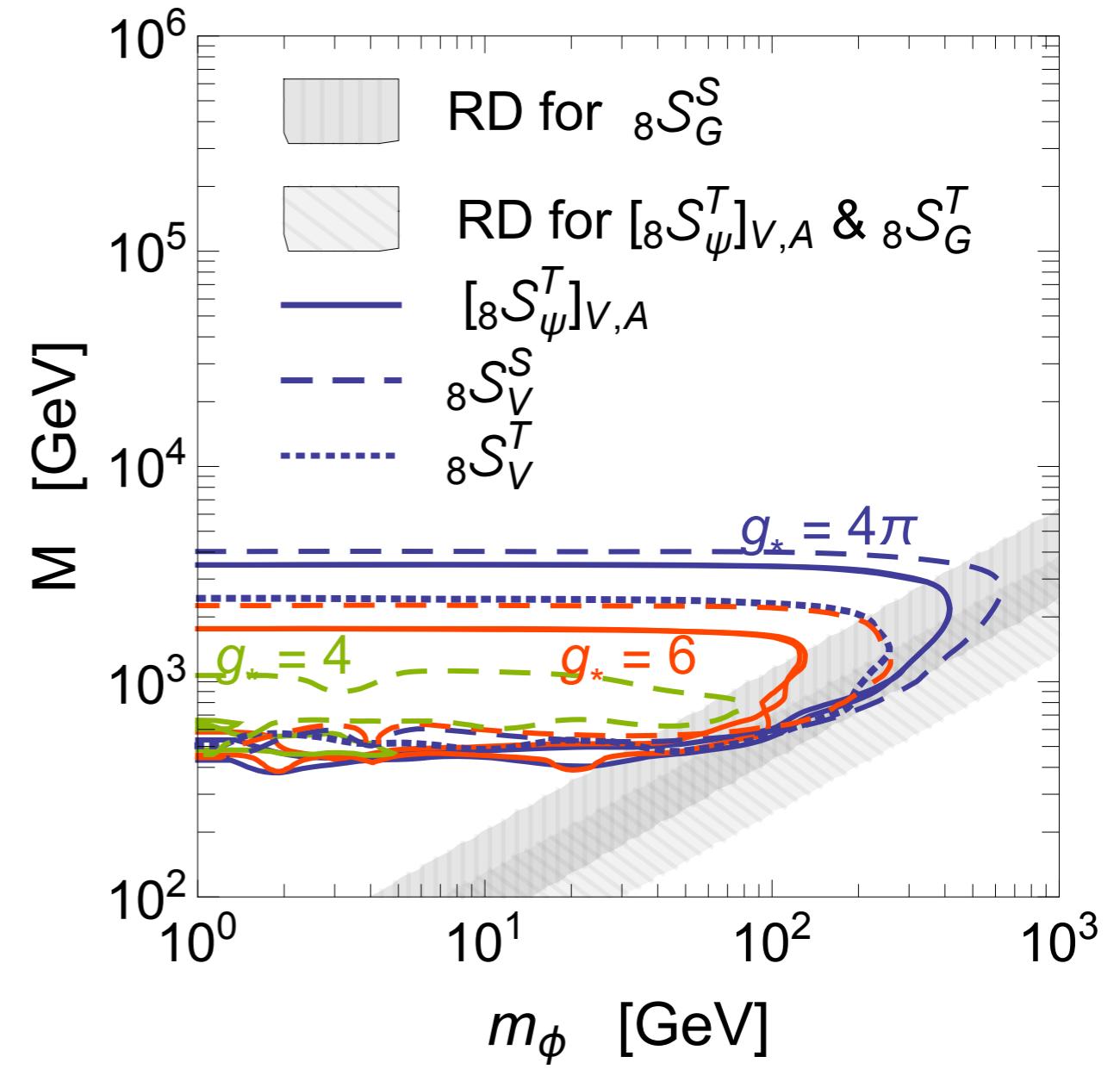
$$\begin{aligned} {}_8\mathcal{L}_{\text{eff}}^{DM} = & C_V^S \frac{g_*^2 m_\phi^2}{M^4} |\phi|^2 V_{\mu\nu}^a V^{a\mu\nu} + C_\psi^S \frac{g_*^2 y_\psi}{M^4} |\partial^\mu \phi|^2 \psi \psi H \\ & + C_V^S \frac{g_*^2}{M^4} |\partial^\mu \phi|^2 V_{\nu\rho}^a V^{a\rho\nu} + C_H^S \frac{g_*^2}{M^4} |\partial^\nu \phi|^2 |D^\nu H|^2 \\ & + C_V^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi V_{\mu\rho}^a V_\nu^{a\rho} + C_H^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi D_{[\mu} H^\dagger D_{\nu]} H \\ & + C_\psi^T \frac{g_*^2}{M^4} \partial^\mu \phi^\dagger \partial^\nu \phi \psi^\dagger \bar{\sigma}_\mu D_\nu \psi, \end{aligned}$$

**Weyl spinors!**

# D=6 > D=8?

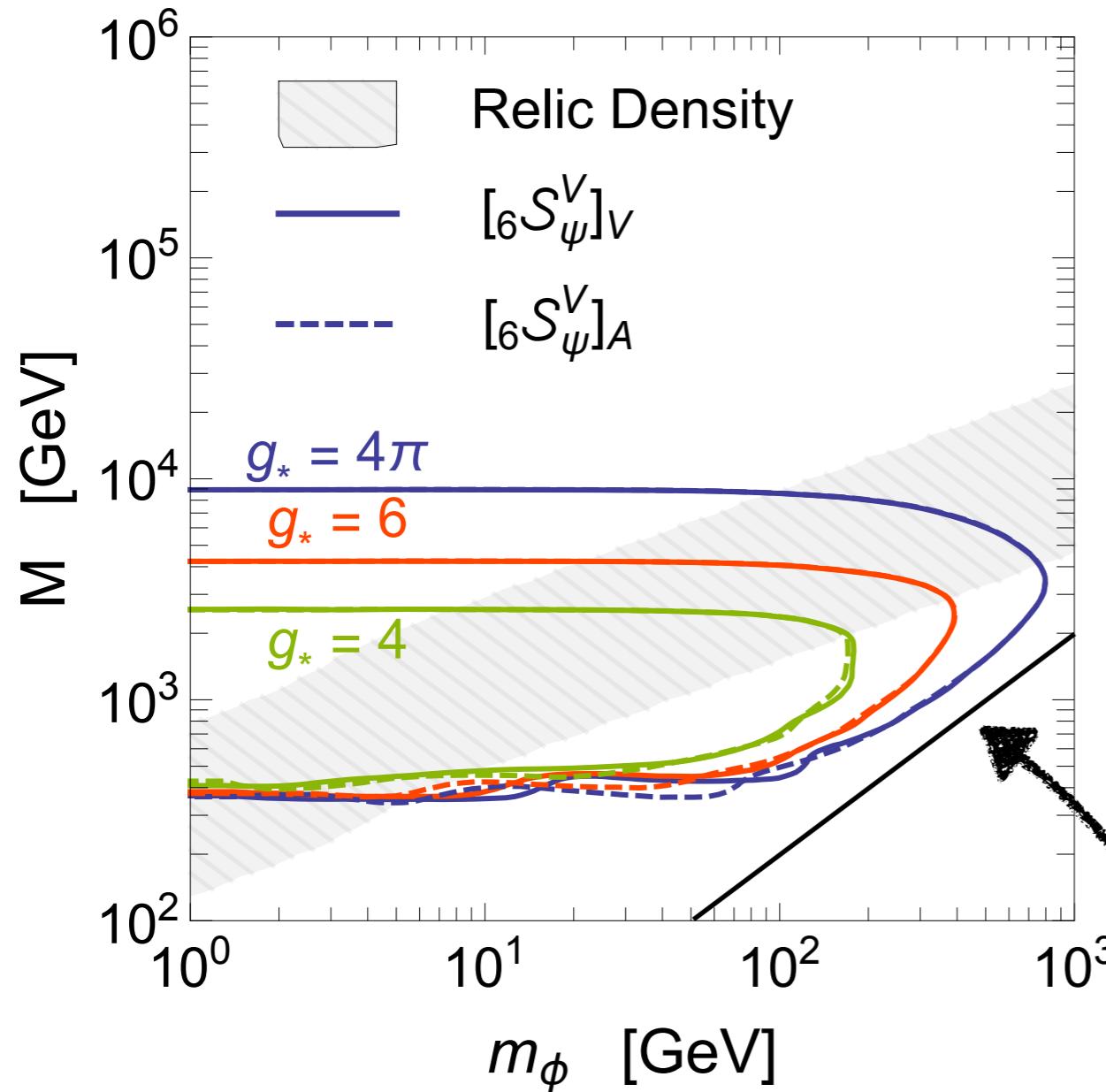


**D=6**



**D=8**

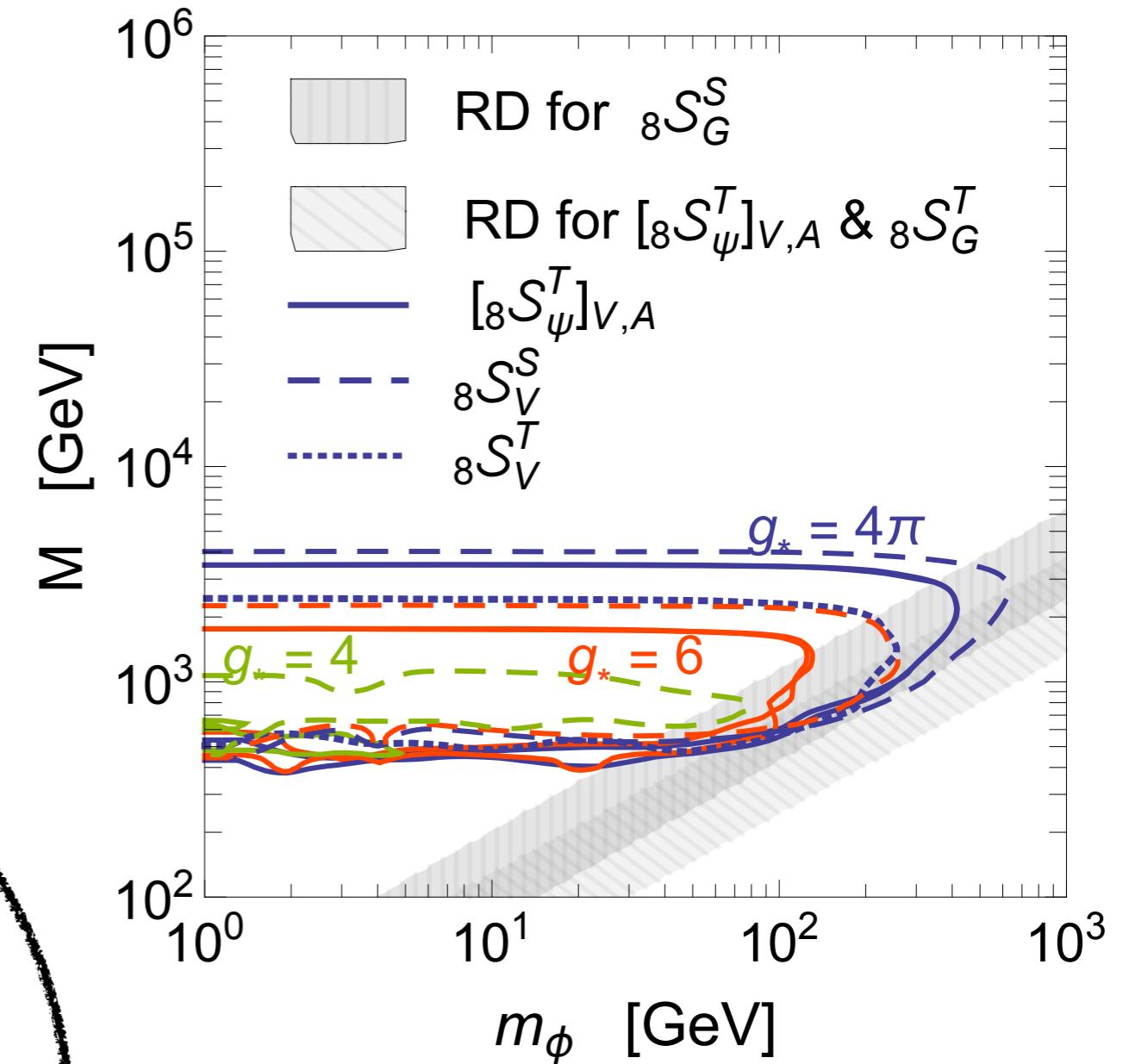
# D=6 > D=8?



$M \sim 2m_{DM}$

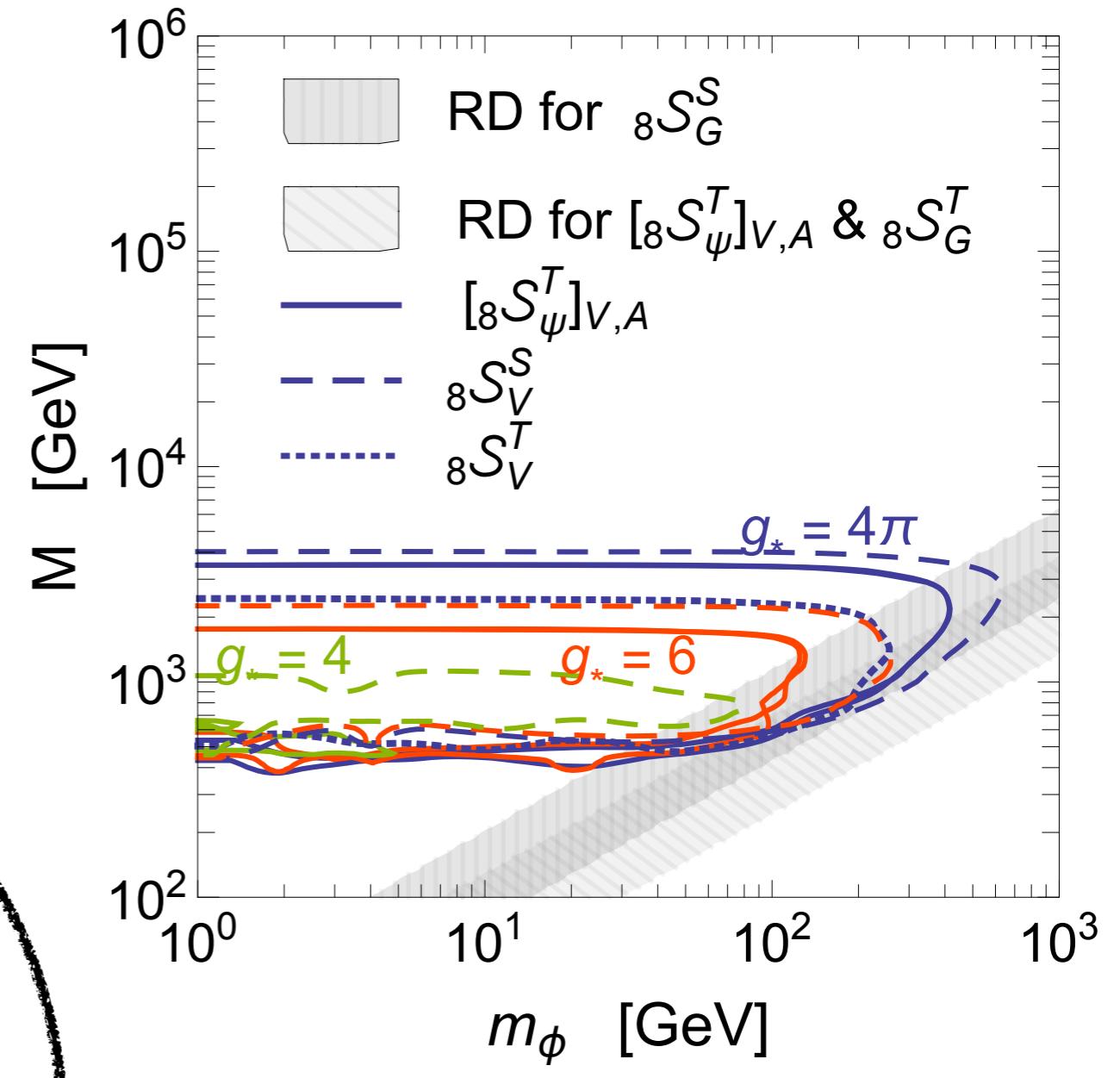
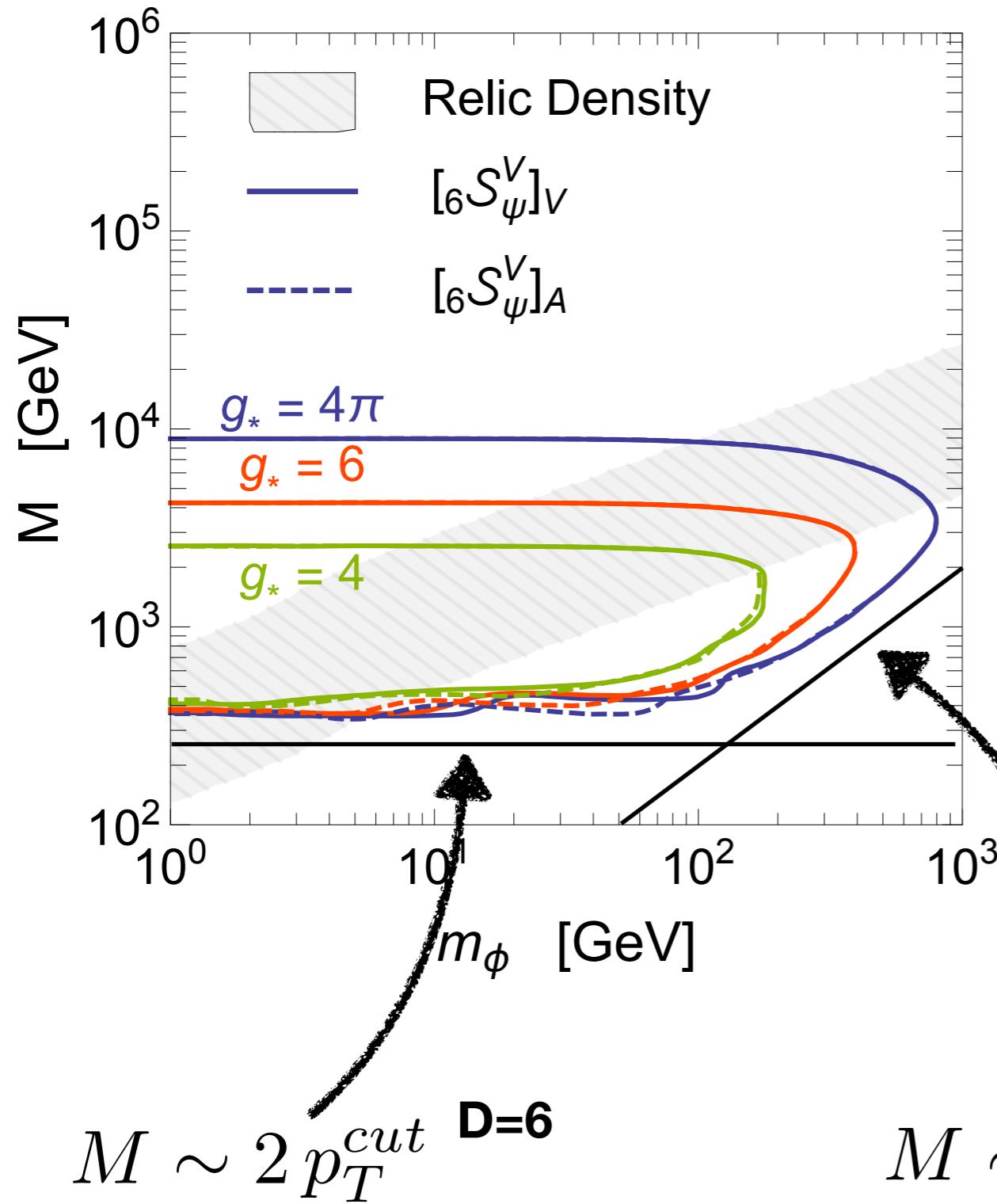
**D=6**

13

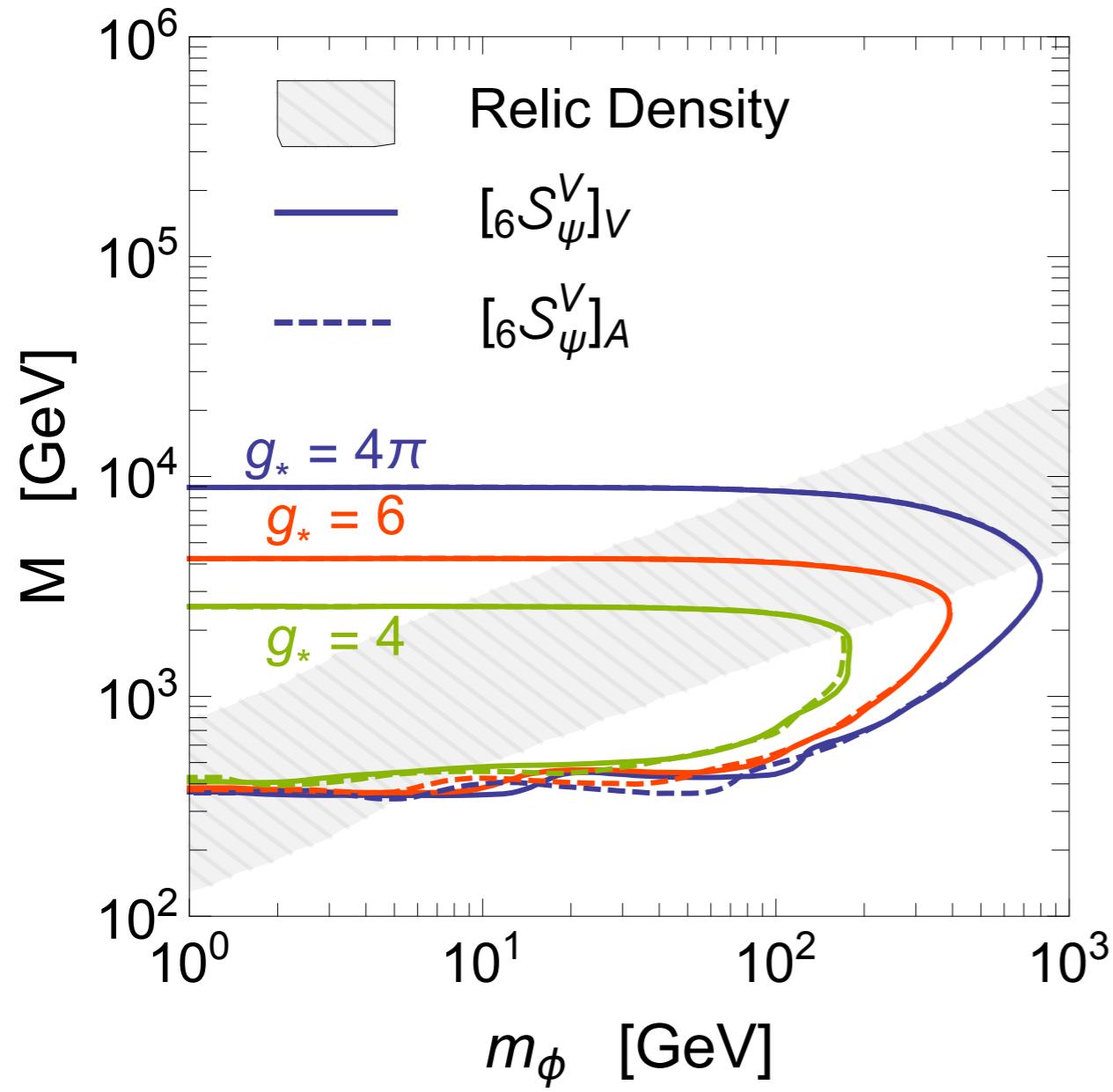


**D=8**

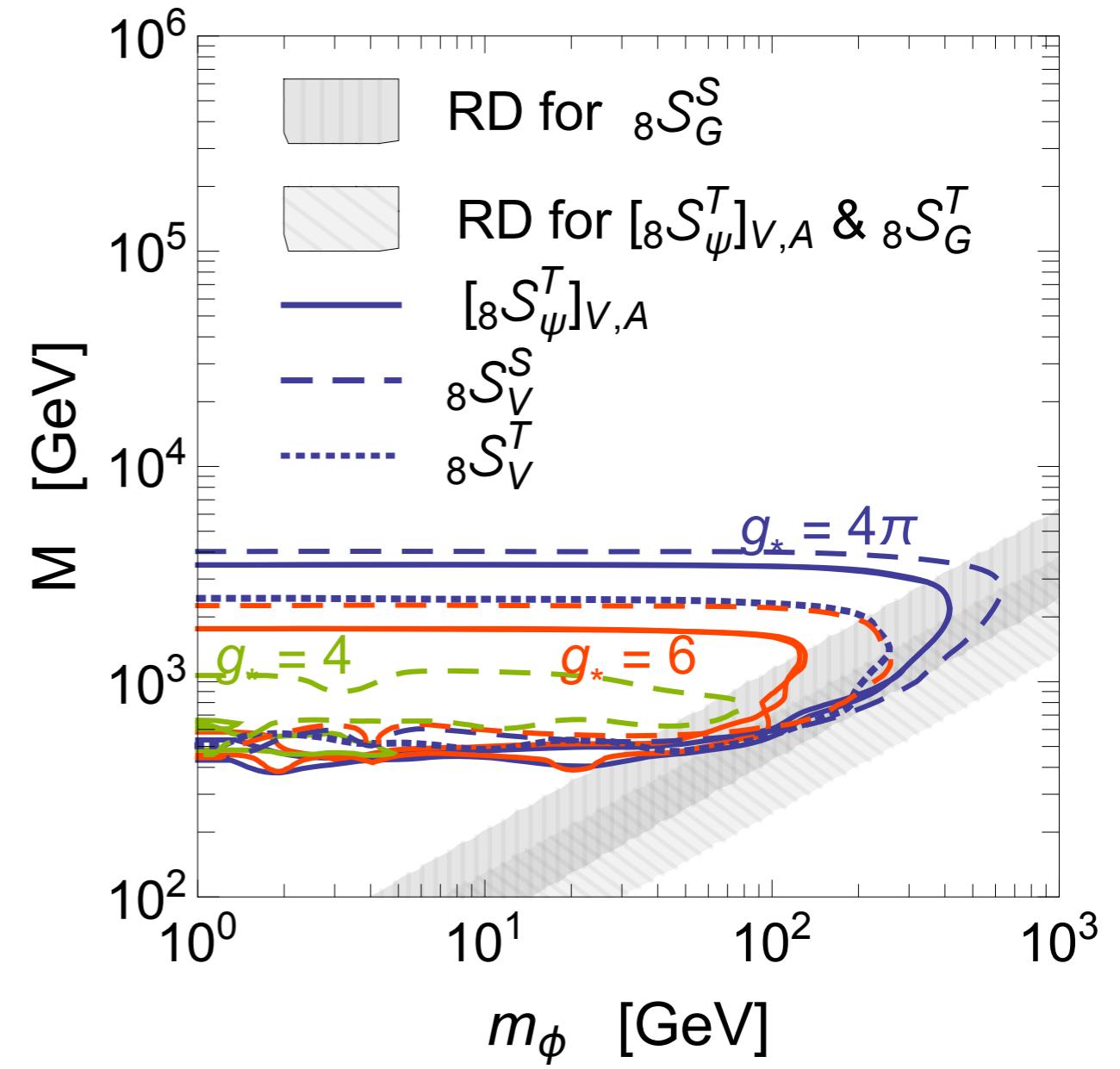
# D=6 > D=8?



# D=6 > D=8?

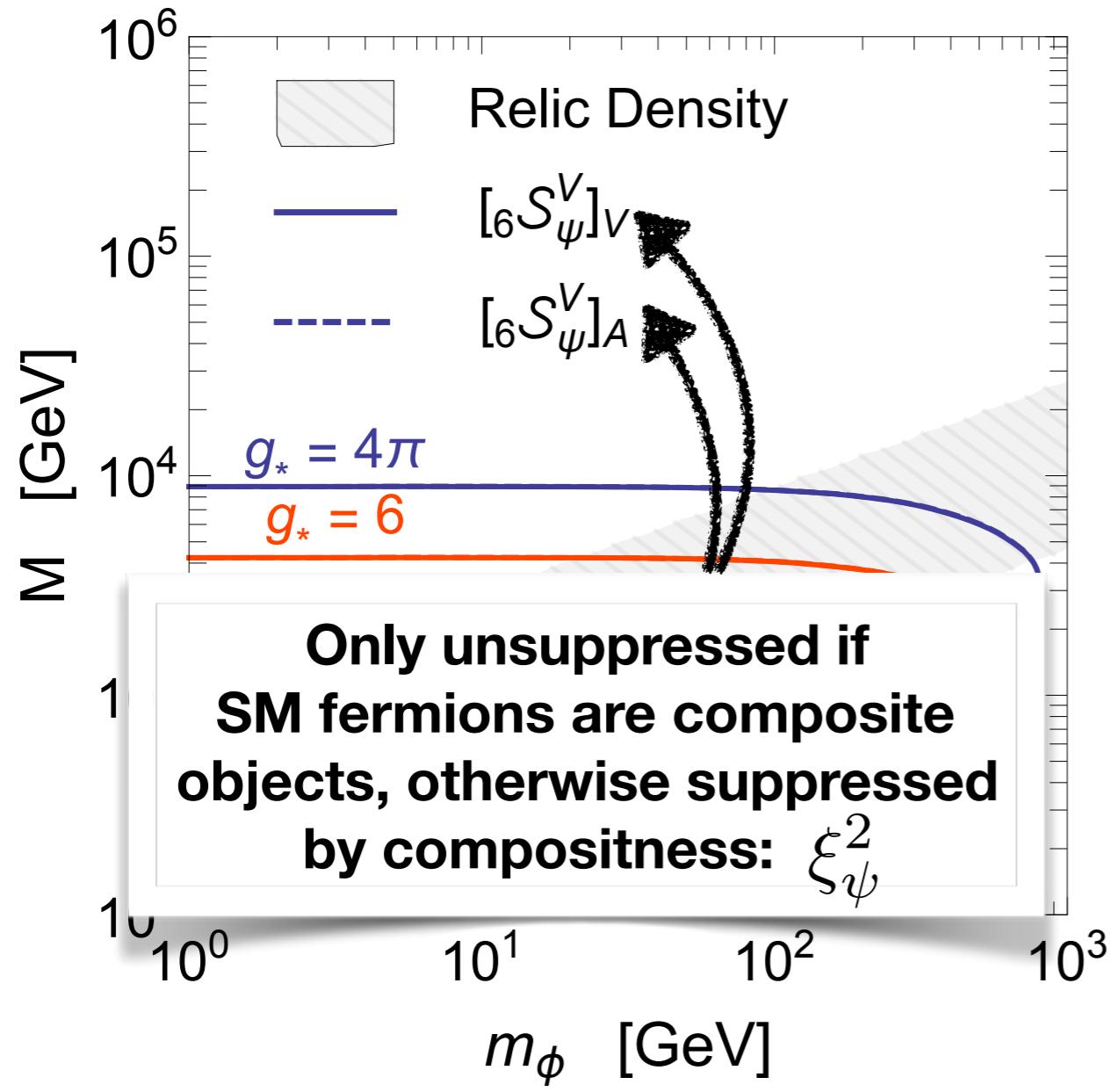


**D=6**

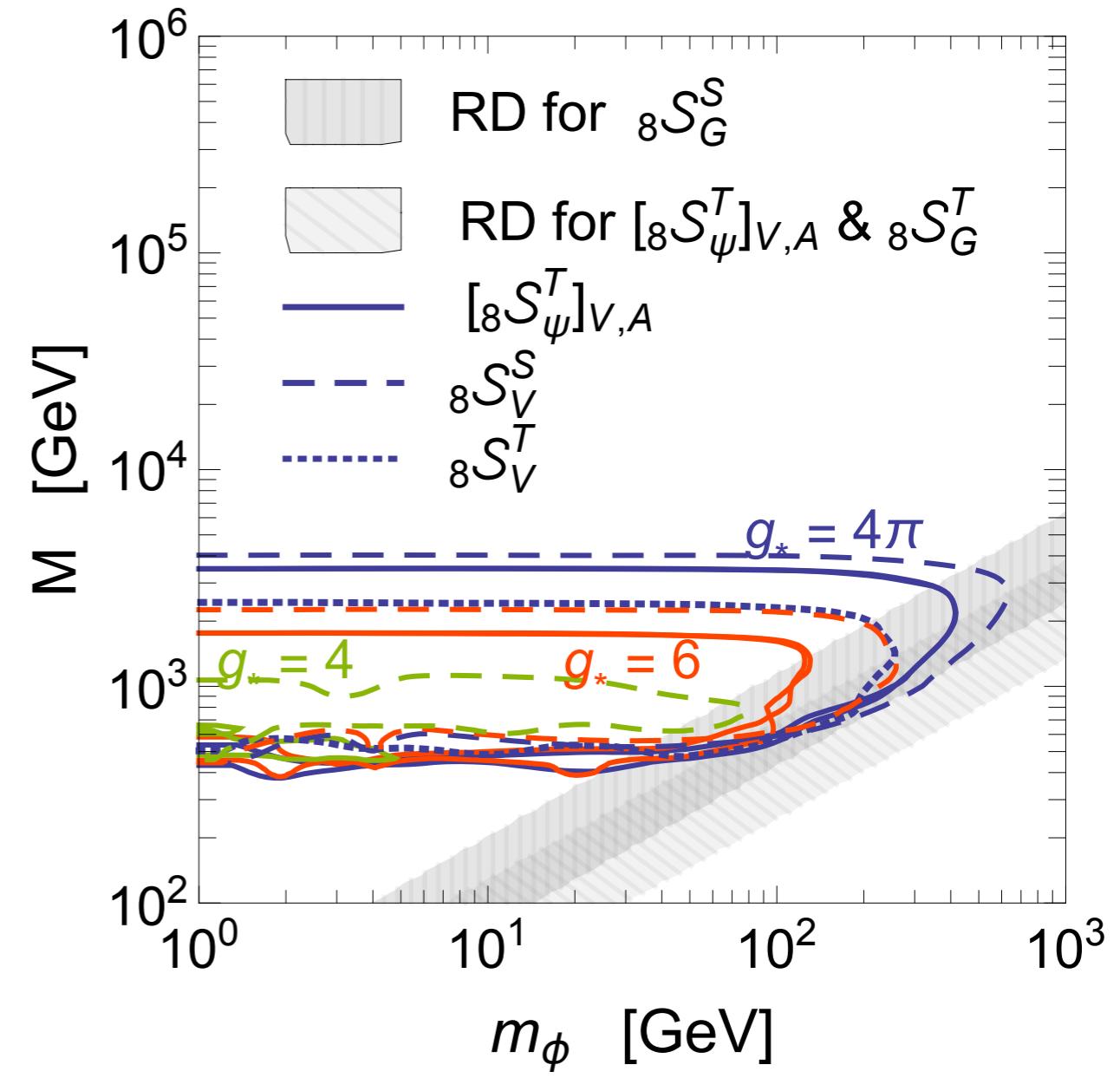


**D=8**

# D=6 > D=8?

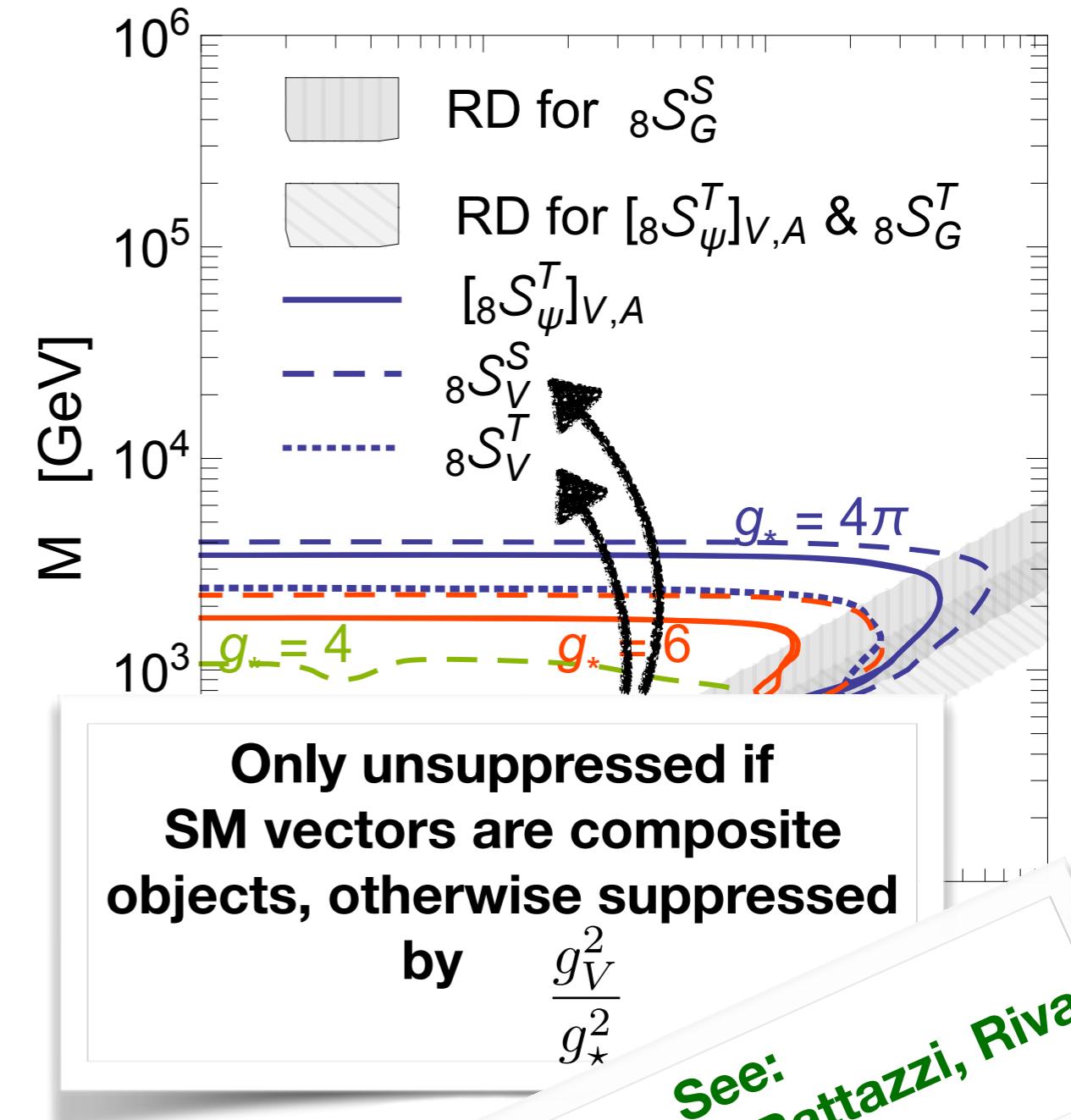
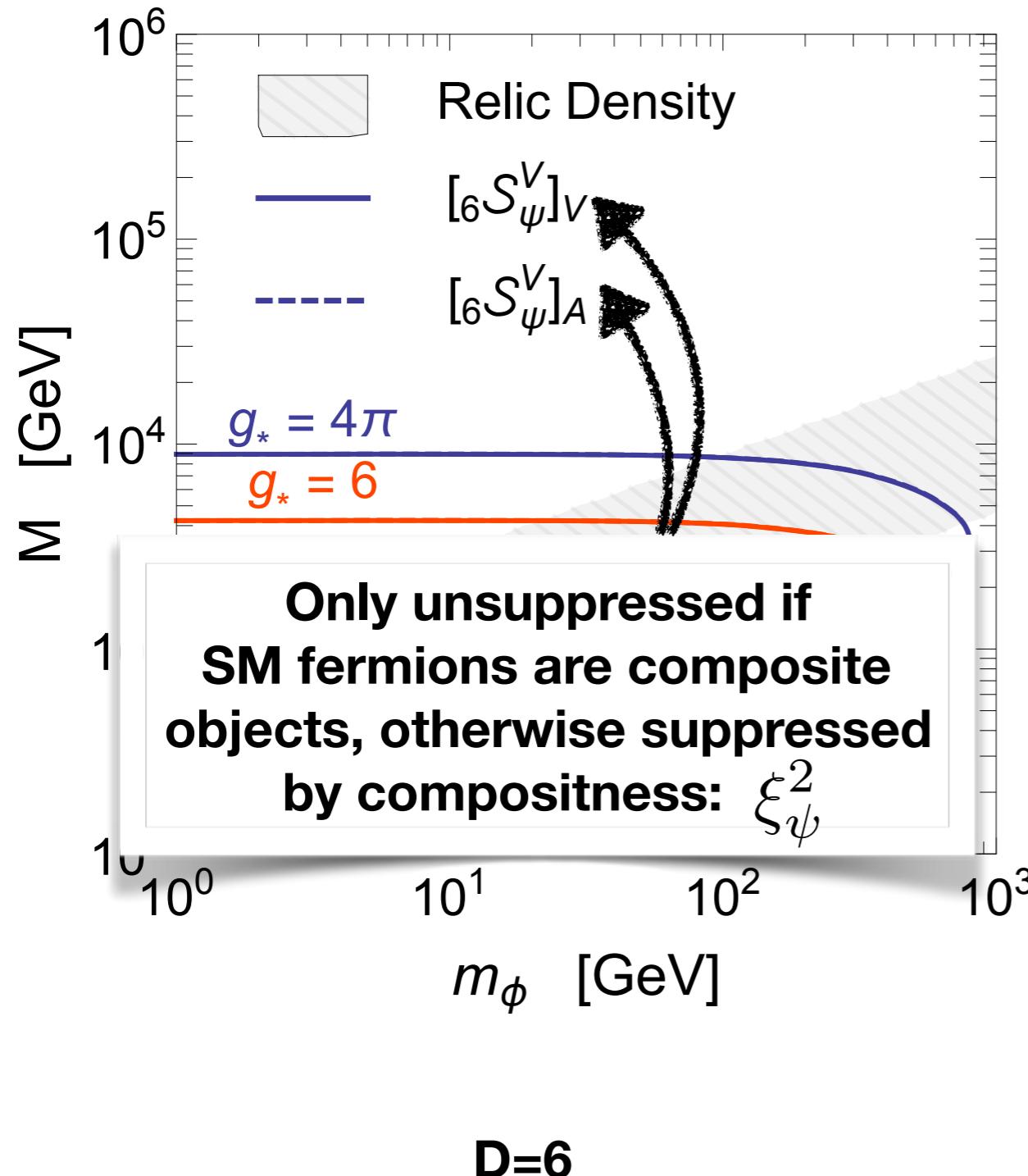


**D=6**



**D=8**

# D=6 > D=8?



See:  
Liu, Pomarol, Rattazzi, Riva  
1603.03064

# What about relict density?

$$D8 \sim \left( \frac{E}{M} \right)^4$$

Suppressed  $D6 \sim \left( \frac{m_\phi}{M} \right)^2 \left( \frac{E}{M} \right)^2$

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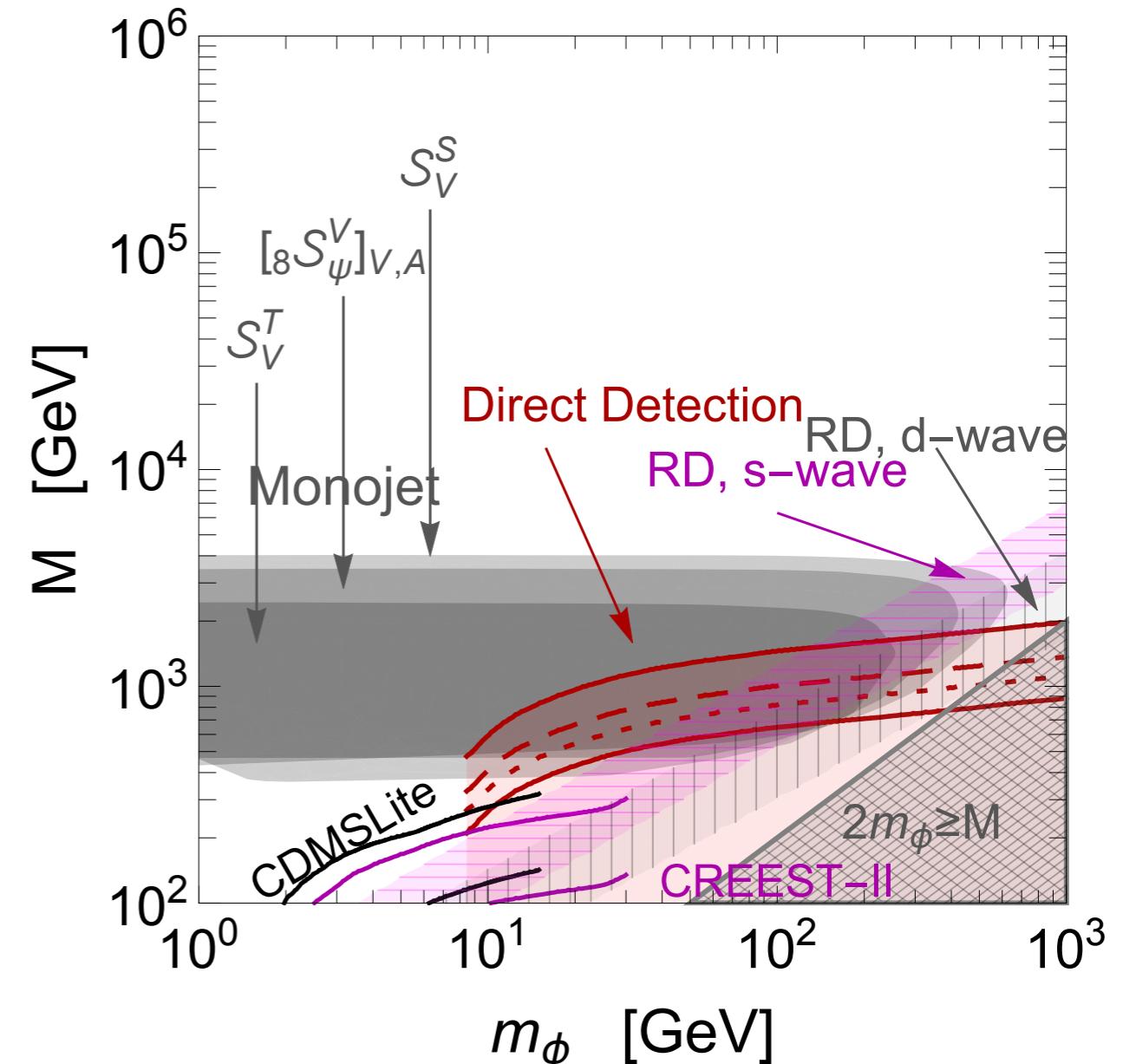
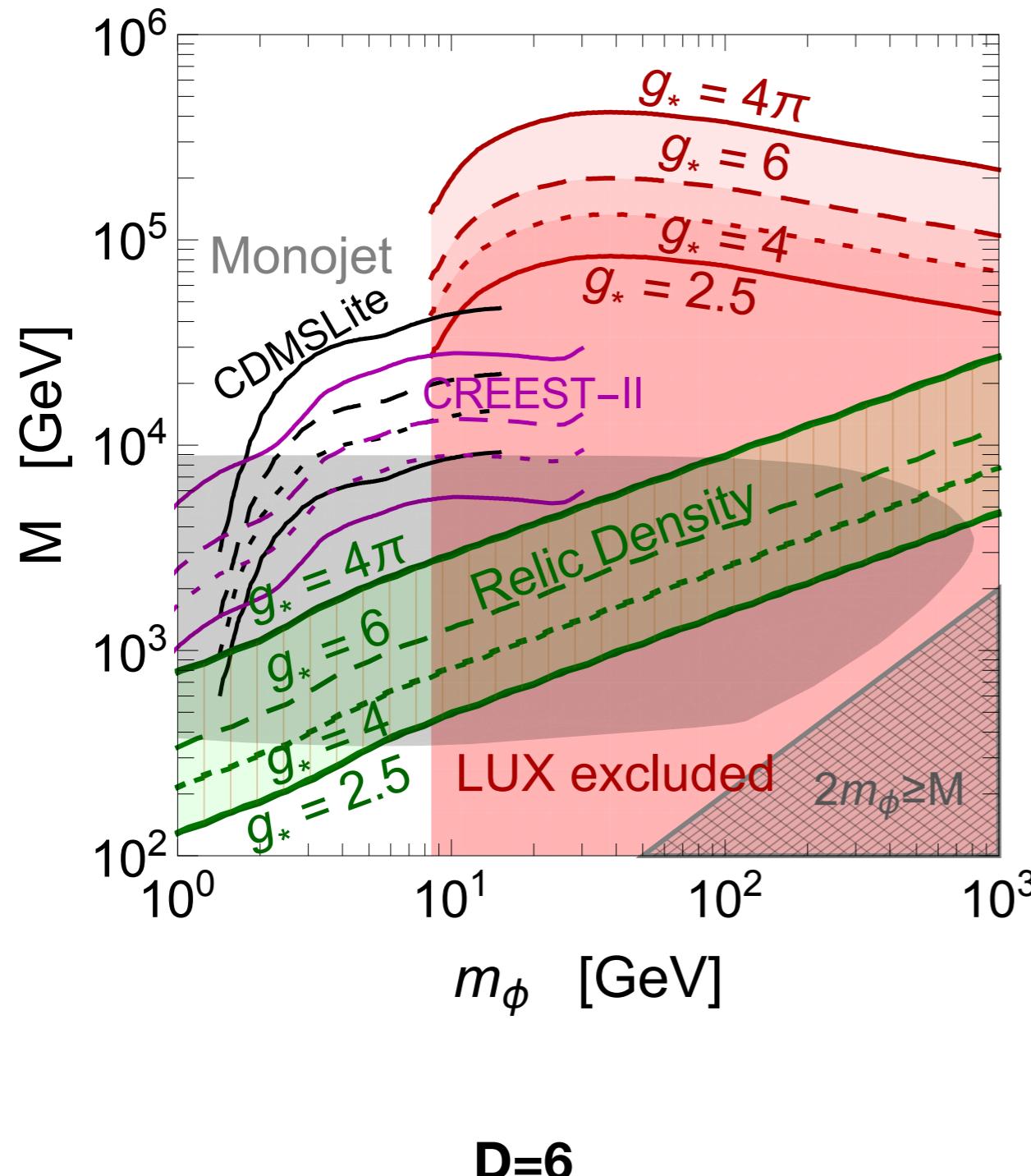
$$\text{Suppressed } D6 \sim \left(\frac{m_\phi}{M}\right)^2 \left(\frac{E}{M}\right)^2$$

At LHC energies  $E \sim M \Rightarrow D8 \gg D6$

At RD & DD energies  $E \sim m_\phi \Rightarrow D8 \sim D6$

$\implies$  Dark Matter complementarity is (partially) lost

# What about relict density?



Comparison only as indication!

# Fermionic DM

Example 2: Fermionic Dark Matter  $\chi$

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Example 2: Fermionic Dark Matter  $\chi$

- Naturally light fermion: Chiral-symmetry-breaking or Goldstino.
- Goldstino  $\rightarrow$  Majorana; Otherwise Dirac.
- Write all the interactions compatible with SM symmetries (exact and approximate).
- Weight terms that break symmetry by  $\frac{m_\chi}{M}$

# Fermionic DM

$$\begin{aligned}
{}_6\mathcal{L}_{eff}^{DM} = & c_\psi^V \frac{g_\star^2}{M^2} \chi^\dagger \bar{\sigma}^\mu \chi \psi^\dagger \bar{\sigma}_\mu \psi + c_H^S \frac{g_{SM}^2 m_\chi}{M^2} \chi^\dagger \chi H^\dagger H \\
& + c_B^{dip} \frac{g_\star m_\chi}{M^2} \chi^\dagger \sigma^{\mu\nu} \chi B_{\mu\nu} \\
{}_8\mathcal{L}_{eff}^{DM} = & C_\psi^{\$} \frac{m_\chi y_\psi g_\star^2}{M^4} \chi^\dagger \chi \psi^\dagger \psi H + C_\psi^{\$'} \frac{m_\chi y_\psi g_\star^2}{M^4} \chi^\dagger \psi^\dagger \psi \chi H \\
& + C_V^{\$} \frac{g_\star^2 m_\chi}{M^4} \chi^\dagger \chi V_{\mu\nu}^a V^{a\mu\nu} + C_V \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi V_{\mu\rho}^a V_\nu^{a\rho} \\
& + C_\psi \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi \psi^\dagger \bar{\sigma}_\mu D_\nu \psi + C'_\psi \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \chi D^\nu \psi^\dagger \bar{\sigma}_\mu D_\nu \psi \\
& + C_H \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi D_\mu H^\dagger D_\nu H
\end{aligned}$$

**Weyl spinors!**

# Fermionic DM

Dirac Fermion, monojet relevant

$$\begin{aligned}
 {}_6\mathcal{L}_{eff}^{DM} = & c_\psi^V \frac{g_\star^2}{M^2} \chi^\dagger \bar{\sigma}^\mu \chi \psi^\dagger \bar{\sigma}_\mu \psi + c_H^S \frac{g_{SM}^2 m_\chi}{M^2} \chi^\dagger \chi H^\dagger H \\
 & + c_B^{dip} \frac{g_\star m_\chi}{M^2} \chi^\dagger \bar{\sigma}^{\mu\nu} \chi B_{\mu\nu} \\
 {}_8\mathcal{L}_{eff}^{DM} = & C_\psi^{\$} \frac{m_\chi y_\psi g_\star^2}{M^4} \chi^\dagger \chi \psi^\dagger \psi H + C_\psi^{\${}'} \frac{m_\chi y_\psi g_\star^2}{M^4} \chi^\dagger \psi^\dagger \psi \chi H \\
 & + C_V^{\$} \frac{g_\star^2 m_\chi}{M^4} \chi^\dagger \chi V_{\mu\nu}^a V^{a\mu\nu} + C_V \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi V_{\mu\rho}^a V_\nu^{a\rho} \\
 & + C_\psi \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi \psi^\dagger \bar{\sigma}_\mu D_\nu \psi + C'_\psi \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \chi D^\nu \psi^\dagger \bar{\sigma}_\mu D_\nu \psi \\
 & + C_H \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi D_\mu H^\dagger D_\nu H
 \end{aligned}$$

**Weyl spinors!**

# Fermionic DM

Majorana (Goldstino) fermion, monojet relevant

$$_6\mathcal{L}_{eff}^{DM} = c_\psi^V \frac{g_\star^2}{M^2} \chi^\dagger \bar{\sigma}^\mu \chi \psi^\dagger \bar{\sigma}_\mu \psi + c_H^S \frac{g_{SM}^2 m_\chi}{M^2} \chi^\dagger \chi H^\dagger H$$

$$+ c_B^{dip} \frac{g_\star m_\chi}{M^2} \chi^\dagger \sigma^{\mu\nu} \chi B_{\mu\nu}$$

$$_8\mathcal{L}_{eff}^{DM} = C_\psi^\$ \frac{m_\chi y_\psi g_\star^2}{M^4} \chi^\dagger \chi \psi^\dagger \psi H + C_\psi^{\$'} \frac{m_\chi y_\psi g_\star^2}{M^4} \chi^\dagger \psi^\dagger \psi \chi H$$

$$+ C_V^\$ \frac{g_\star^2 m_\chi}{M^4} \chi^\dagger \chi V_{\mu\nu}^a V^{a\mu\nu} + C_V \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi V_{\mu\rho}^a V_\nu^{a\rho}$$

$$+ C_\psi \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi \psi^\dagger \bar{\sigma}_\mu D_\nu \psi + C'_\psi \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \chi D^\nu \psi^\dagger \bar{\sigma}_\mu D_\nu \psi$$

$$+ C_H \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi D_\mu H^\dagger D_\nu H$$

**Weyl spinors!**

# Fermionic DM

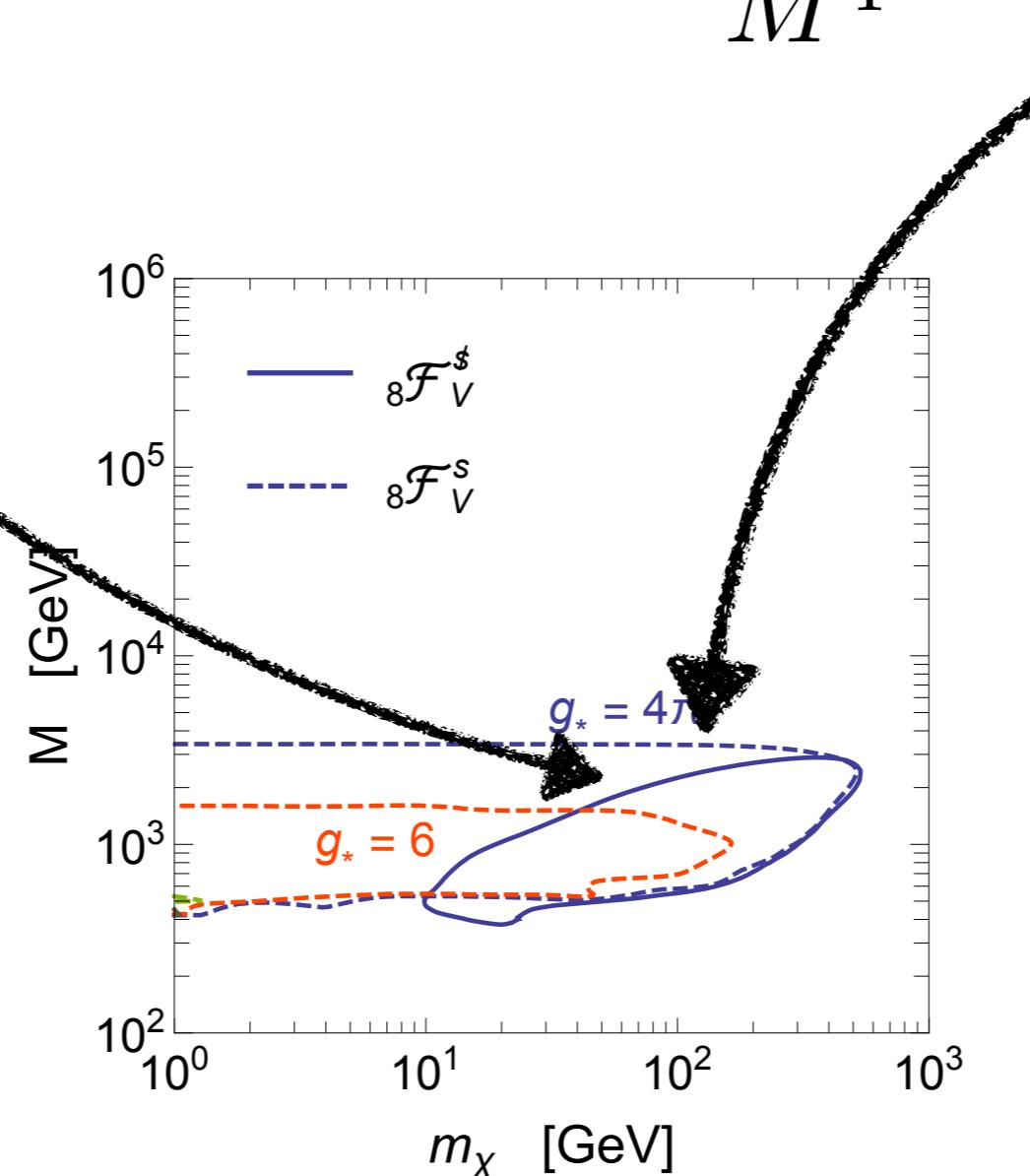
Majorana (Goldstino) fermion, monojet relevant

$$\begin{aligned}
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 & + C_H \frac{g_\star^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi D_\mu H^\dagger D_\nu H
 \end{aligned}$$

**Weyl spinors!**

# Symmetry breaking effects

$$C_V^{\$} \frac{g_*^2 m_\chi}{M^4} \chi^\dagger \chi V_{\mu\nu}^a V^{a\mu\nu} \text{ vs. } C_V \frac{g_*^2}{M^4} \chi^\dagger \bar{\sigma}^\mu \partial^\nu \chi V_{\mu\rho}^a V_\nu^{a\rho}$$

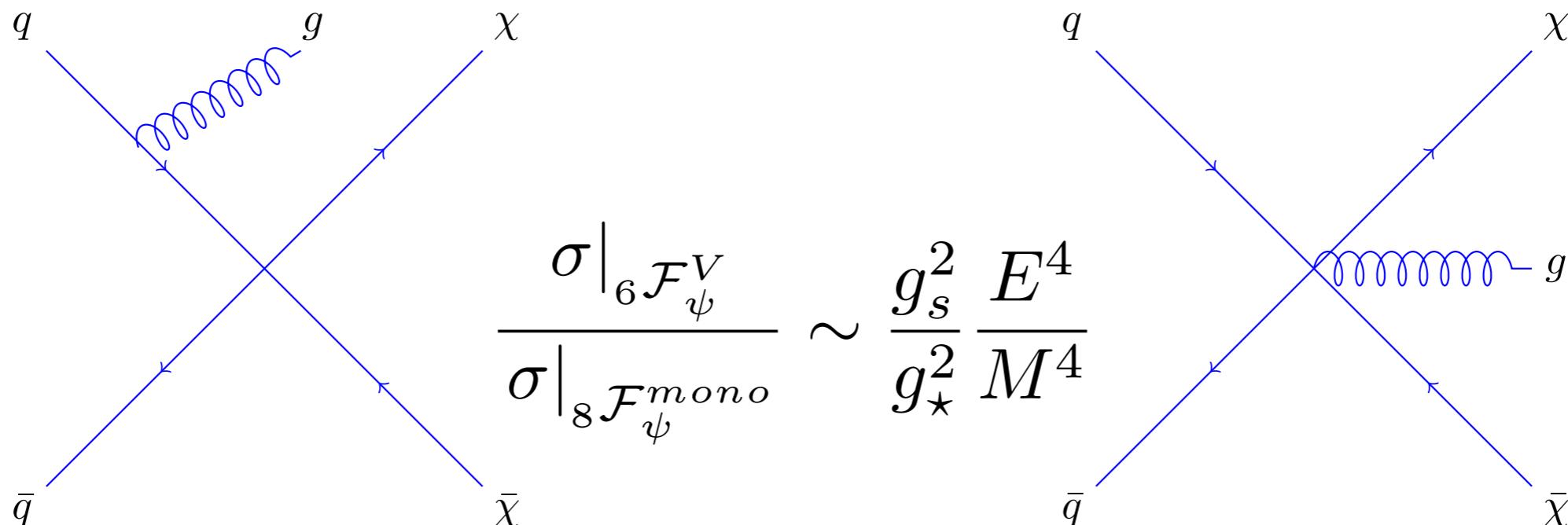


# Composite Vectors

**NEW!**

$$C_{\psi}^{mono} \frac{g_{\star}^3}{M^4} \chi^{\dagger} \bar{\sigma}_{\mu} \chi \psi^{\dagger} \bar{\sigma}_{\nu} T^a \psi V^{a \mu \nu}$$

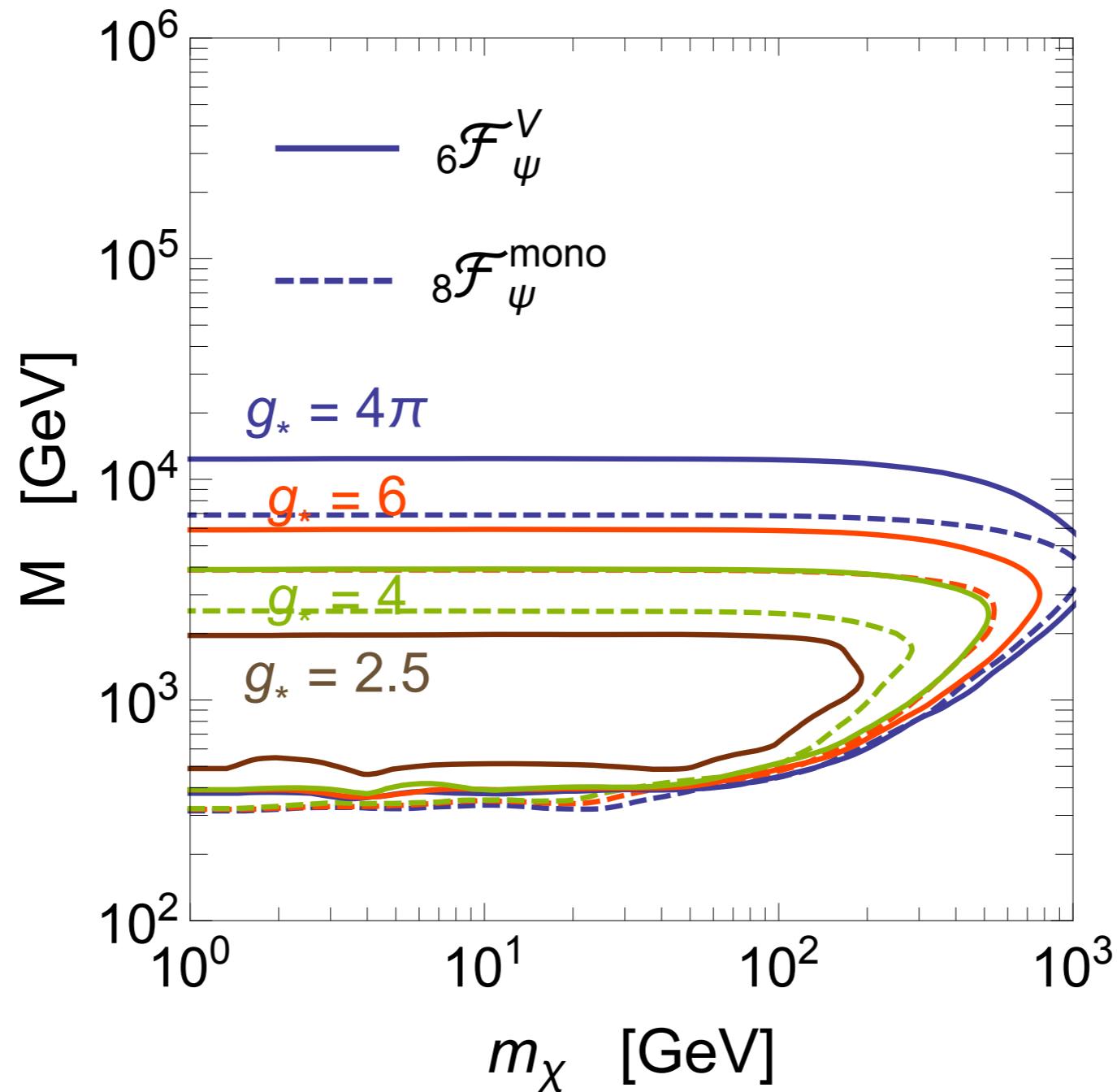
$2 \rightarrow 2 + \text{ISR}$  vs.  $2 \rightarrow 3$



# Composite Vectors

**NEW!**

$$C_{\psi}^{mono} \frac{g_{\star}^3}{M^4} \chi^{\dagger} \bar{\sigma}_{\mu} \chi \psi^{\dagger} \bar{\sigma}_{\nu} T^a \psi V^{a \mu \nu}$$



# Message

- Operators might be more suppressed than expected
- Consistent analysis of data within the framework of EFTs is possible and sometimes needed
- We can test well define hypotheses on UV physics
- Complementarity between collider searches and direct detection is sometimes lost