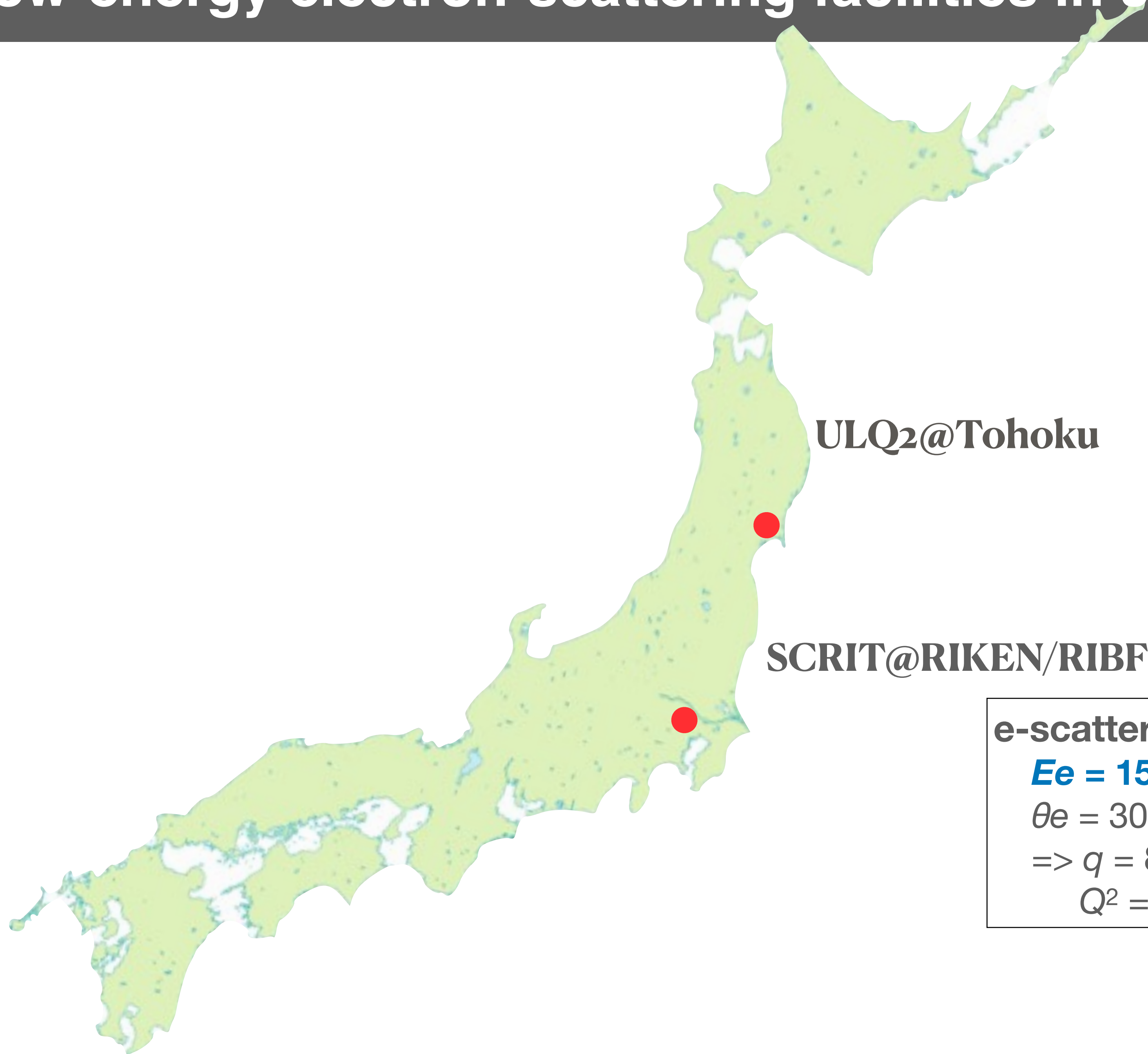


“Low-Energy” Electron Scattering for Exotic Nuclei and Nucleons

Toshimi Suda (RARIS, Tohoku Univ.)
suda@ins.tohoku.ac.jp

for SCRIT and ULQ2 collaboration



ULQ2@Tohoku

Proton Charge Radius

$E_e = 10 - 60 \text{ MeV}$

$\theta_e = 30 - 150 \text{ deg.}$

$\Rightarrow Q^2 = 3 \times 10^{-5} - 0.013 \text{ (GeV/c)}^2$

lowest-ever Q^2 !!

SCRIT@RIKEN/RIBF

e-scattering for exotic nuclei ($\sim 10^8/\text{sec}$)

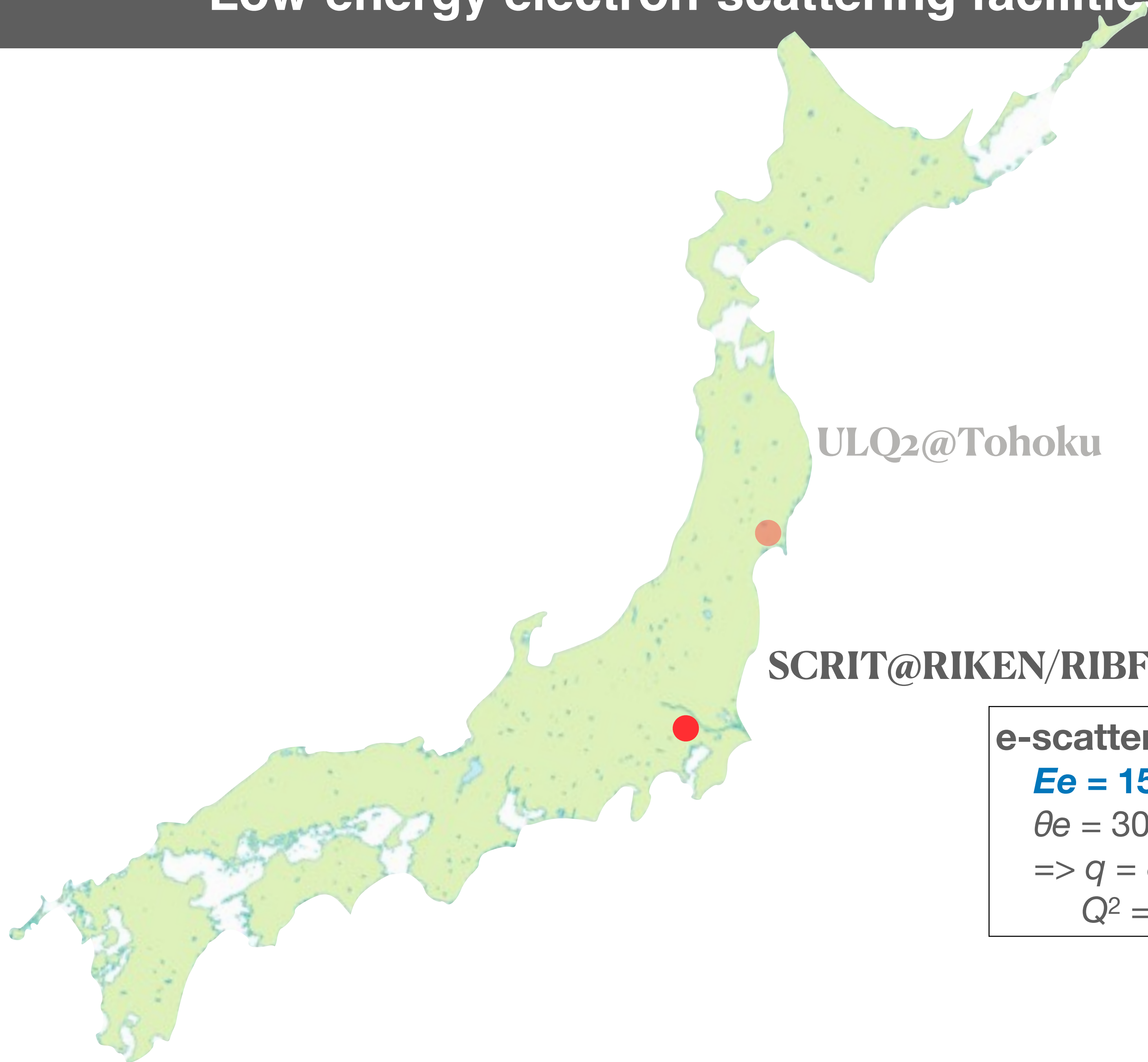
$E_e = 150 - 300 \text{ MeV}$

$\theta_e = 30 - 60 \text{ deg.}$

$\Rightarrow q = 80 - 300 \text{ MeV/c}$

$Q^2 = 0.006 - 0.09 \text{ (GeV/c)}^2$

world's first !!



ULQ2@Tohoku

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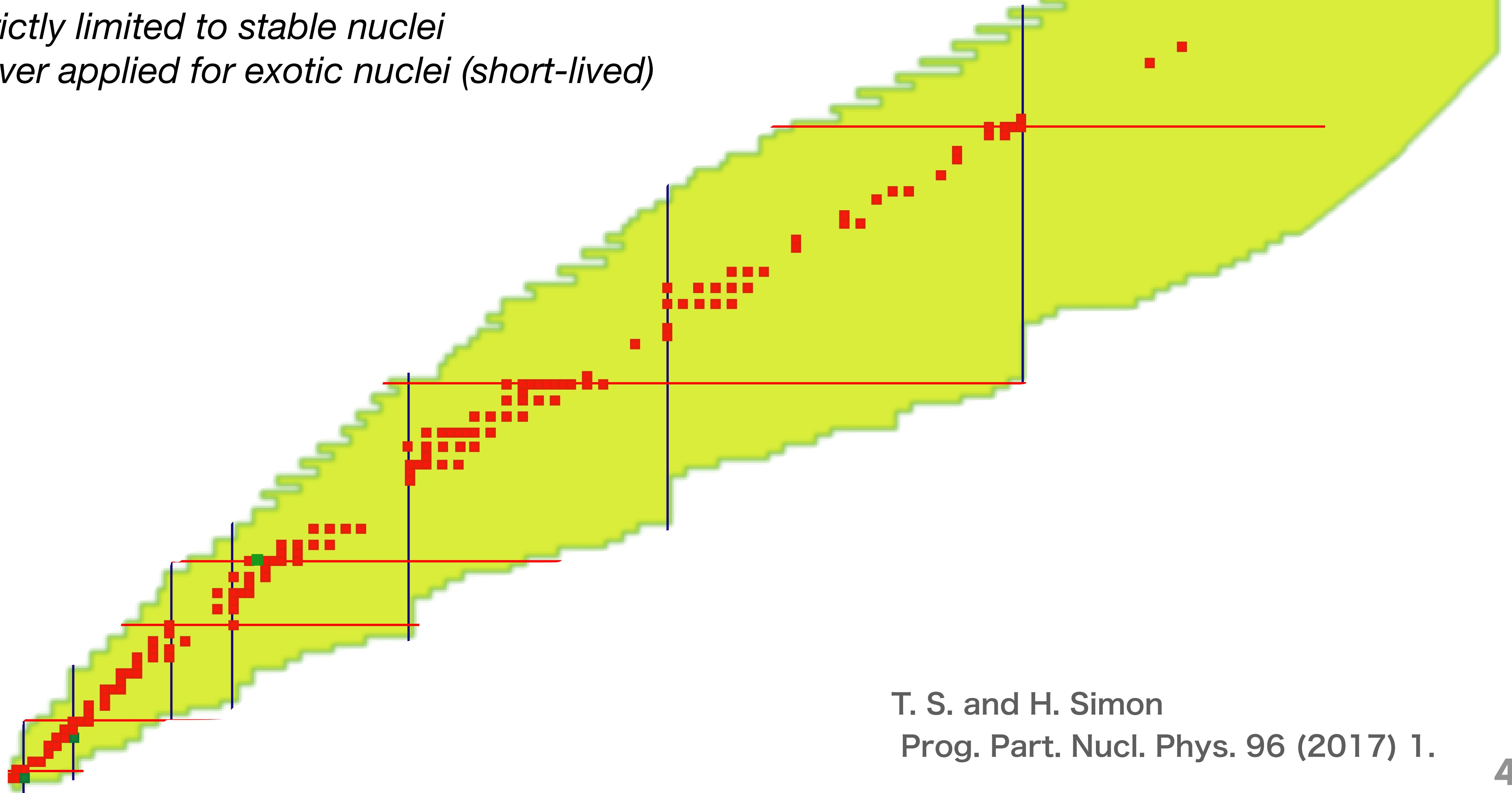
$\Rightarrow q = 80 - 300 \text{ MeV/c}$

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world's first !!

Nuclei ever studied by electron scattering

- *strictly limited to stable nuclei*
- *never applied for exotic nuclei (short-lived)*



T. S. and H. Simon
Prog. Part. Nucl. Phys. 96 (2017) 1.

PHYSICAL REVIEW LETTERS **131**, 092502 (2023)

Editors' Suggestion

Featured in Physics

First Observation of Electron Scattering from Online-Produced Radioactive Target

K. Tsukada^{1,2}, Y. Abe², A. Enokizono^{2,3}, T. Goke⁴, M. Hara², Y. Honda^{2,4}, T. Hori², S. Ichikawa^{2,*},
Y. Ito¹, K. Kurita³, C. Legris⁴, Y. Maehara¹, T. Ohnishi², R. Ogawara^{1,2}, T. Suda^{2,4},
T. Tamae⁴, M. Wakasugi^{1,2}, M. Watanabe², and H. Wauke^{2,4}

¹*Institute for Chemical Research, Kyoto University, Uji, Kyoto 611-0011, Japan*

²*Nishina Center for Accelerator-Based Science, RIKEN, Wako, Saitama 351-0198, Japan*

³*Department of Physics, Rikkyo University, Toshima, Tokyo 171-8501, Japan*

⁴*Research Center for Electron Photon Science, Tohoku University, Sendai, Miyagi 982-0826, Japan*

 (Received 7 March 2023; accepted 21 June 2023; published 30 August 2023)

We successfully performed electron scattering off unstable nuclei which were produced online from the photofission of uranium. The target ^{137}Cs ions were trapped with a new target-forming technique that makes a high-density stationary target from a small number of ions by confining them in an electron storage ring. After ^{137}Cs ions were trapped, the electron beam was turned on and the electron density was increased to $0.9 \times 10^{26} \text{ m}^{-3}$. The electron density of the trapped ^{137}Cs ions was estimated to be $1.5 \times 10^{26} \text{ m}^{-3}$ from the electron density of the scattered electrons is consistent with a calculation. This success marks the realization of the anticipated femtoscope which clarifies the structures of exotic and short-lived unstable nuclei.

Phys. Rev. Lett. 131 (2023) 092502.

Electron scattering provides a long-awaited view of unstable nuclei

Nuclear reactions produce a plethora of short-lived artificial isotopes. Figuring out what they look like has been a challenge.

The cartoon picture of an atomic nucleus looks kind of like the inside of a gumball machine that dispenses only two flavors: protons and neutrons, evenly mixed in a compact, spherical cluster.

That's not generally what real nuclei look like. Neutron-rich lead-208, for example, has a thick skin of neutrons encasing its proton-endowed core (see *Physics Today*, July 2021, page 12). Some nuclei are flattened, and some are elongated. Some are even pear shaped.

The more unstable a nucleus, the

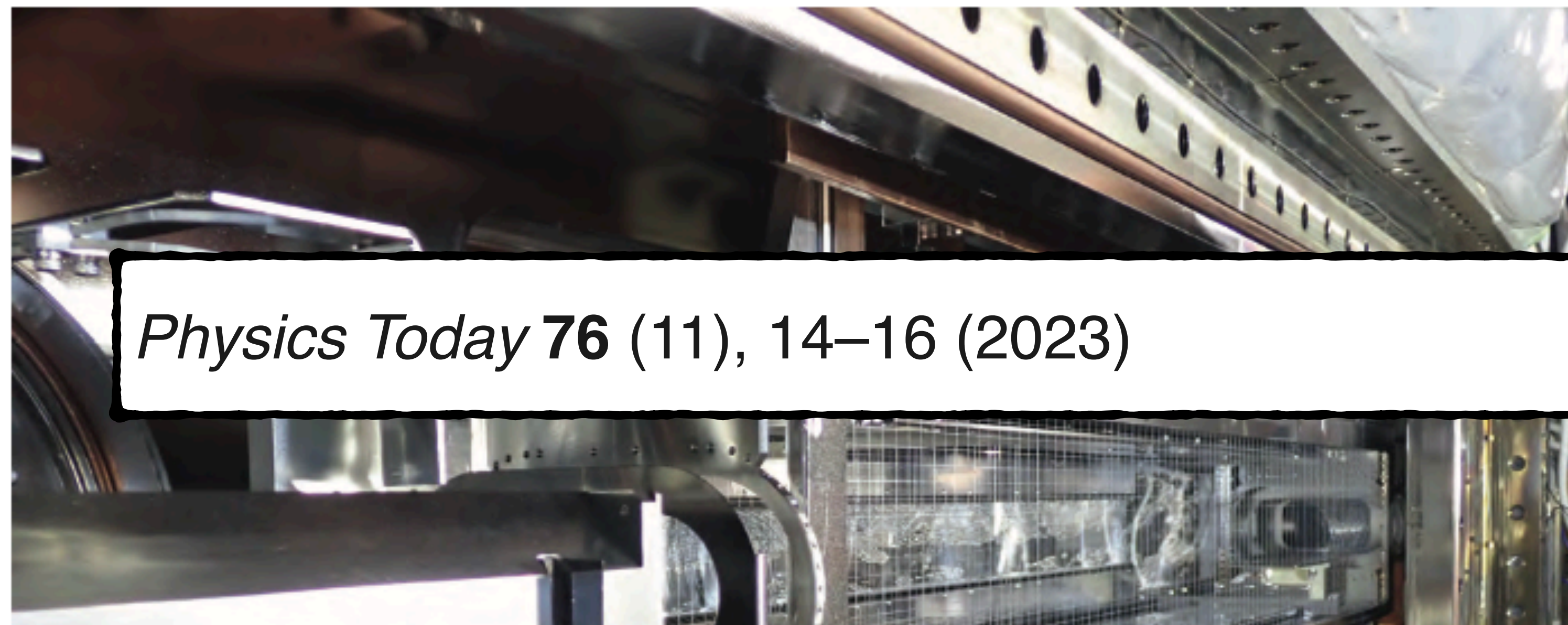
stranger the structures it can adopt. Short-lived nuclei might form bubble structures with depleted central density, or they might have a valence nucleon or two that form a halo around a compact central core. (See the article by Filomena Nunes, *Physics Today*, May 2021, page 34.) Frustratingly, though, those exotic structures are hard to experimentally confirm, because the gold standard for probing nuclear structure—electron scattering—has been off limits to short-lived nuclei.

That could change soon. Kyo Isukada

and colleagues, working at RIKEN's Radioactive Isotope Beam Factory (RIBF) in Wako, Japan, have performed the first electron-scattering experiment on unstable nuclei produced on the fly in a nuclear reaction.¹ Their isotope of choice, cesium-137, has a half-life of 30 years. It's not so exotic that the researchers expected—or found—anything unusual about its structure. But the technique they used is applicable to shorter-lived nuclei, so more experiments are on the way.

Backscatter

Probing nuclei through particle scattering dates back to the discovery of the nucleus itself, in 1911, when Ernest



Physics Today 76 (11), 14–16 (2023)

01 November 2023 22:46:09

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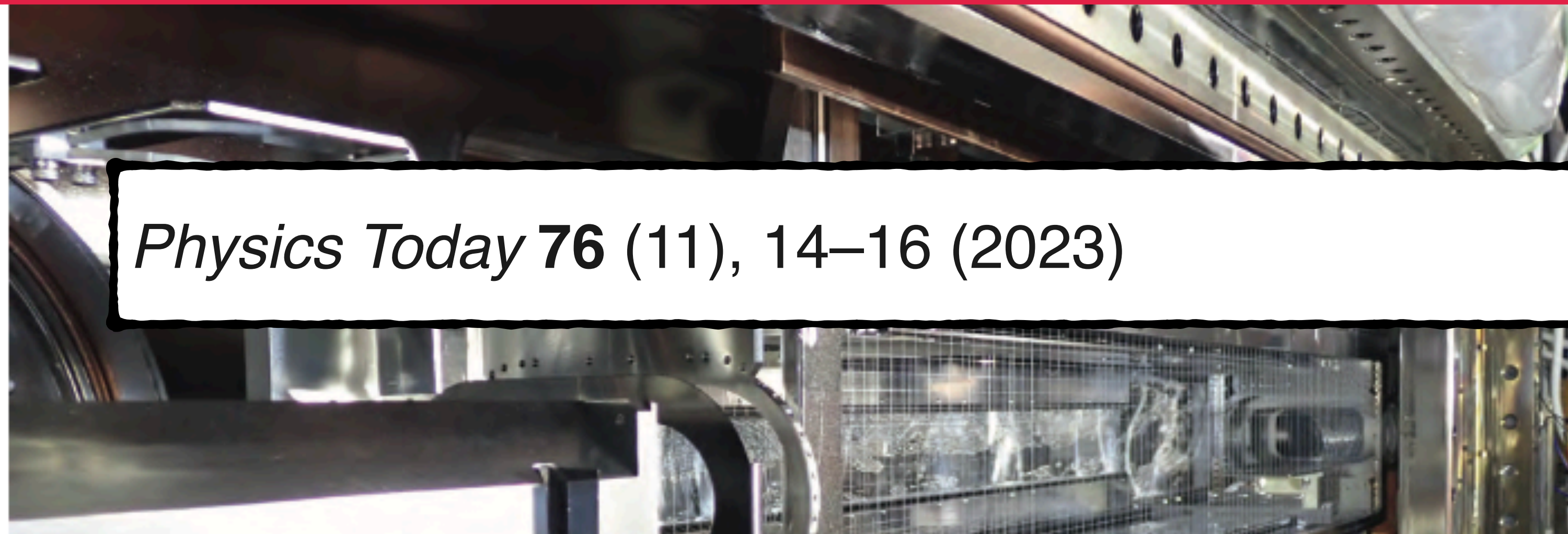
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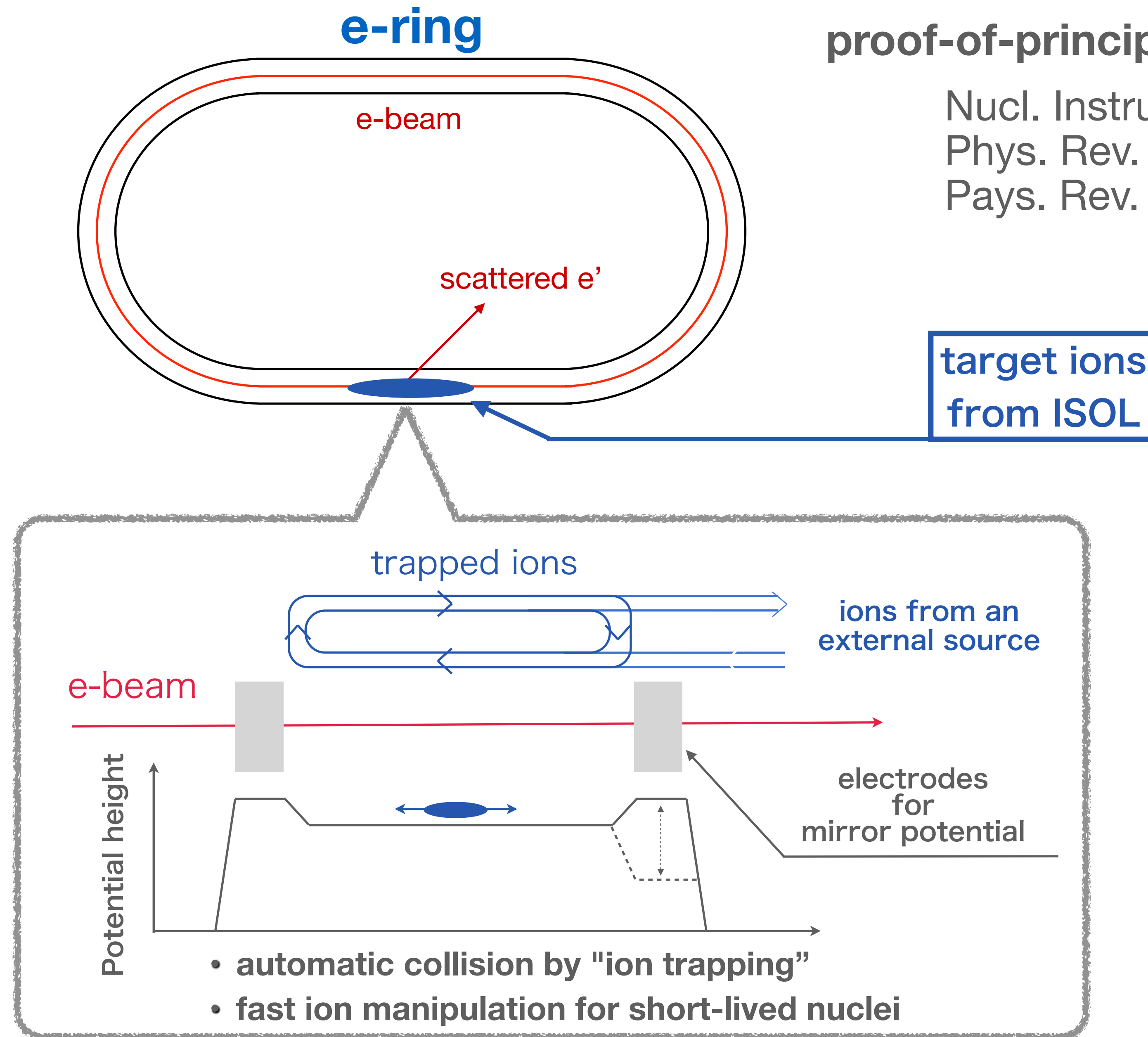
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electron scattering - the gold standard
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Physics Today 76 (11), 14–16 (2023)

01 November 2023 22:46:09



WiSES spectrometer

$\Delta\Omega \sim 90 \text{ mSr}$

$\theta = 30 - 60^\circ$

$\Delta p/p \sim 10^{-3}$

long target accept.

e-RI collisions

FRAC

cooler-buncher
dc-to-pulse conv.

ERIS (ISOL)
photofission of ^{238}U

neutron-rich nuclei
by $\gamma+^{238}\text{U}$

Injector + ISOL driver

150 MeV Microtron

SR2 storage ring

$E_e = 150\text{-}700 \text{ MeV}$

$I_e = 300 \text{ mA}$

$\tau \sim 2 \text{ hours}$

Facility : Nucl. Instrum. and Method B541 (2023) 380-384.

Trapping

Nucl. Instrum. and Method B541 (2023) 90-92

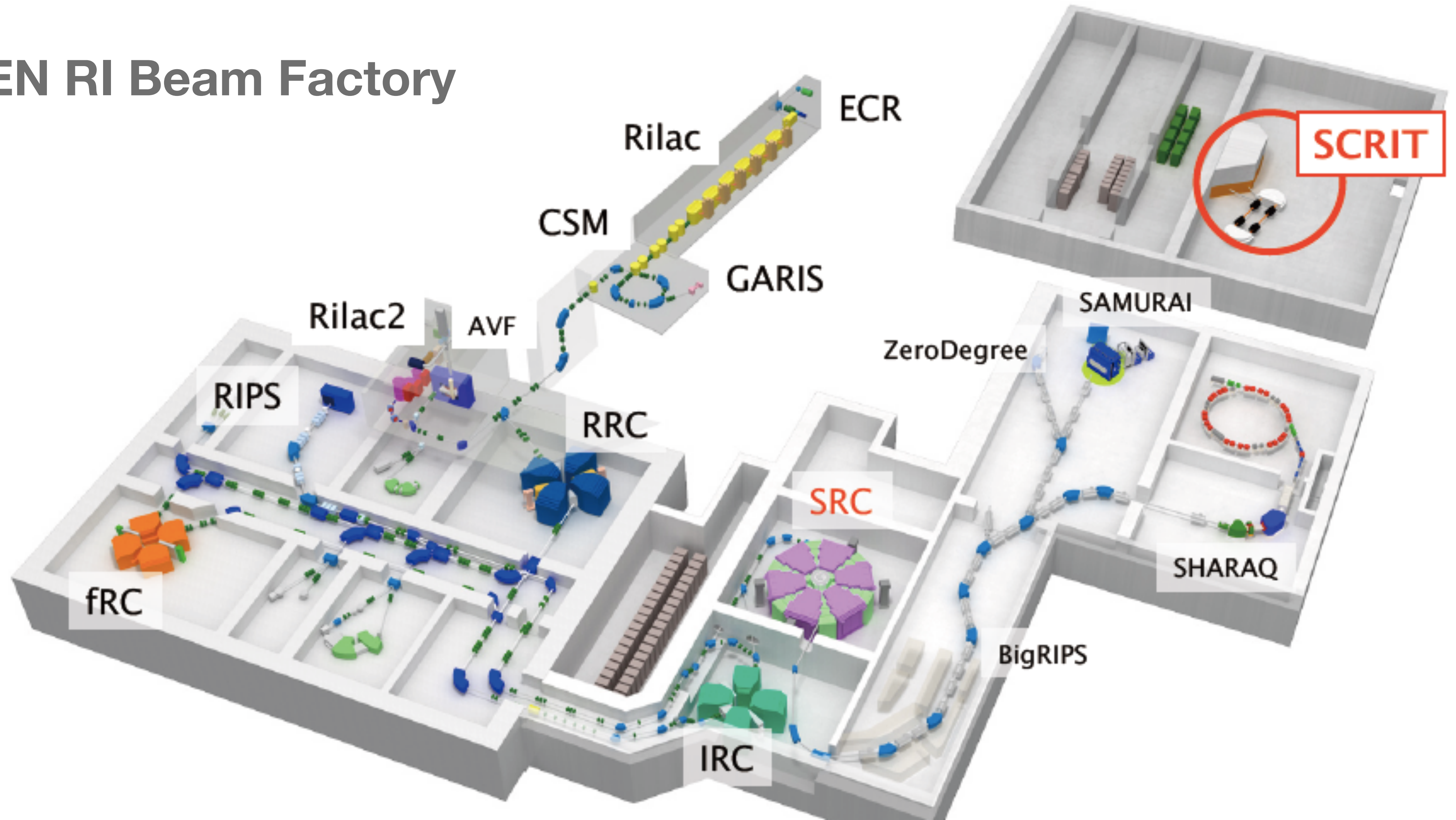
ERIS : Phys. Scr. T 166 (2015) 014071.

Nucl. Instrum. and Method B463 (2020) 290-292.

FRAC : Rev. Sci. Instrum. 89 (2018) 095107.

World's first electron facility dedicated for exotic nuclei

RIKEN RI Beam Factory



RIKEN SCRIT e-scattering facility

ECT*ws

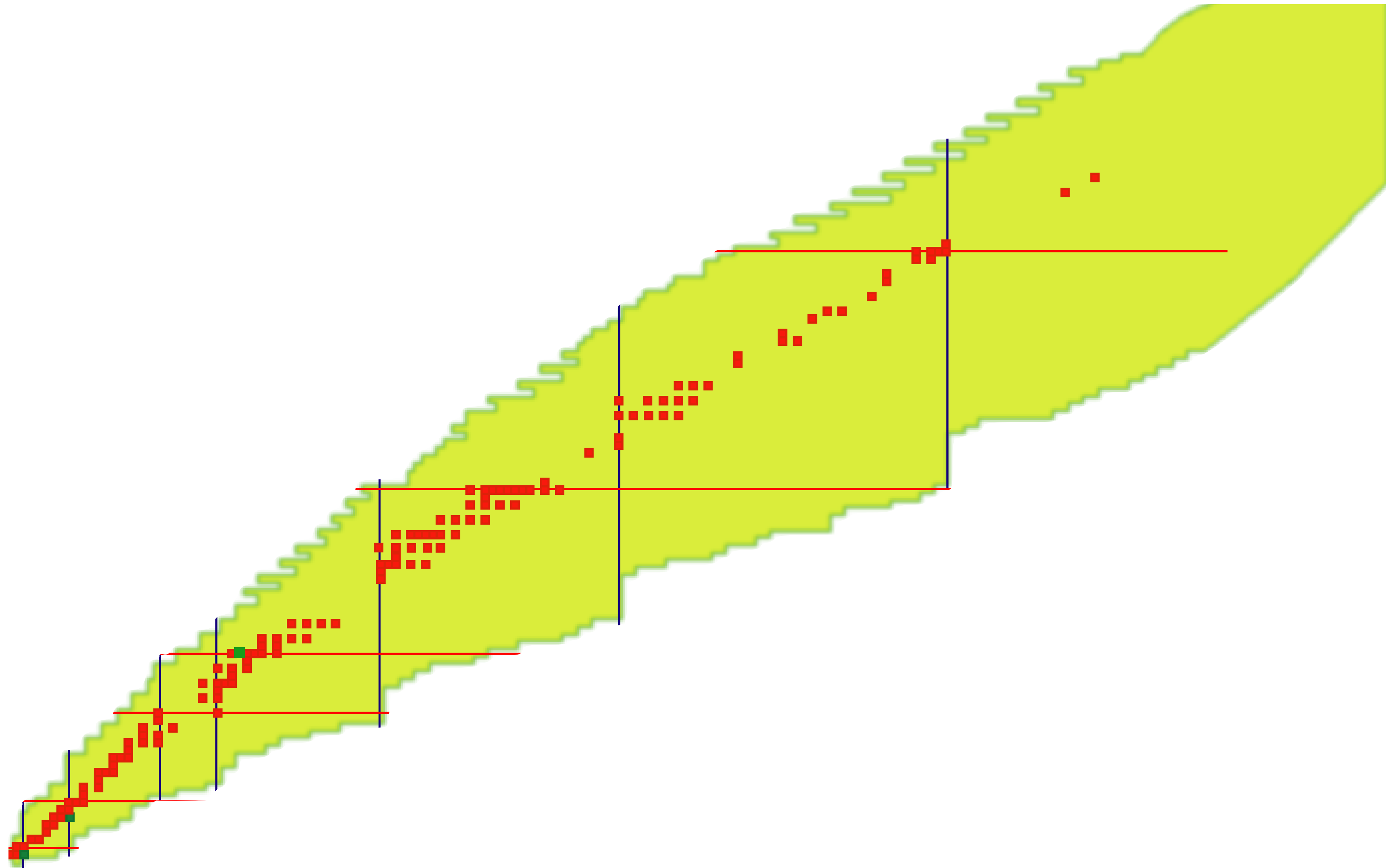
07.14-07.18

Electron Ring
(SCRIT equipped)

WiSES
(Window-frame Spectrometer
for Electron Scattering)

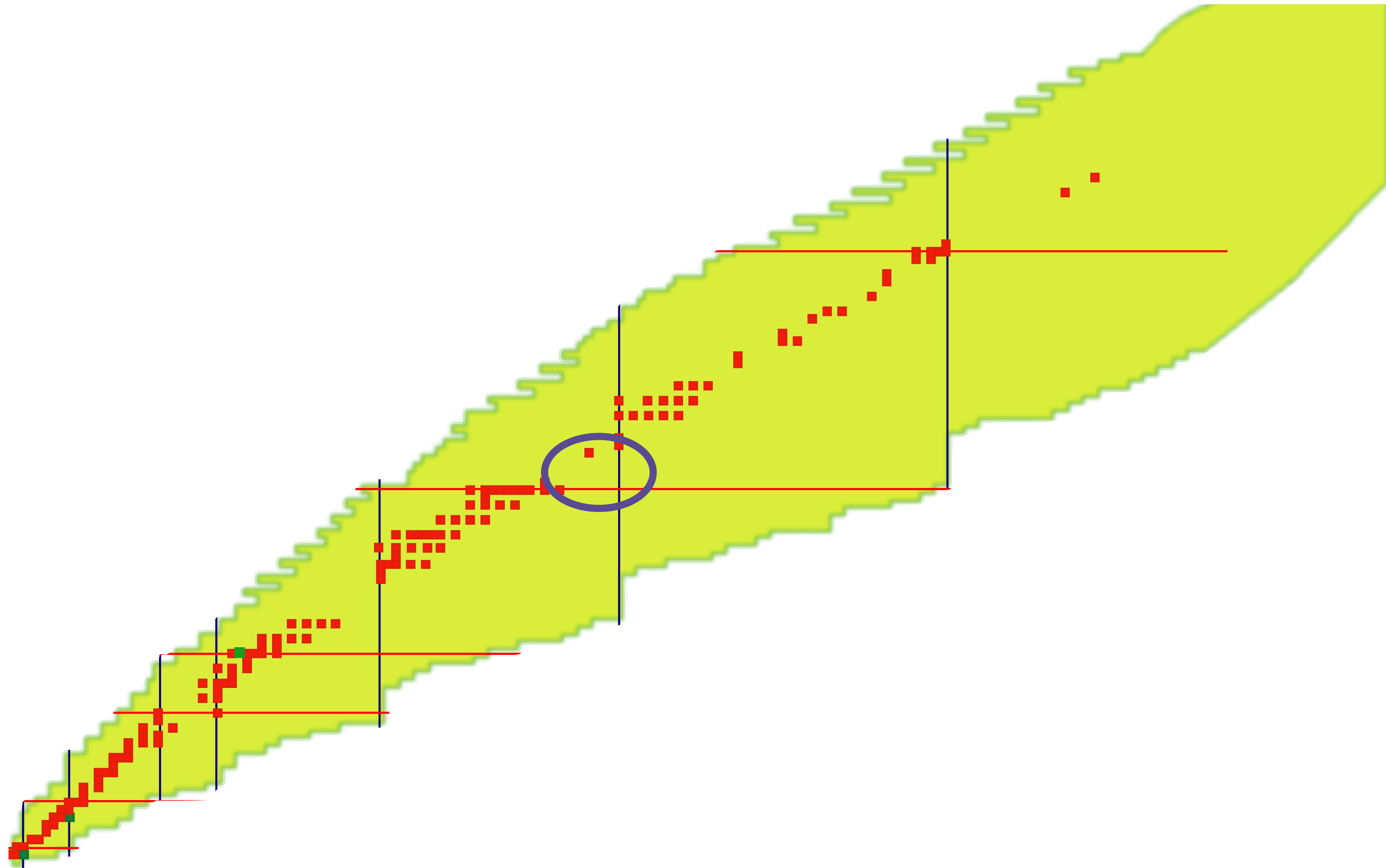
Region of our current studies

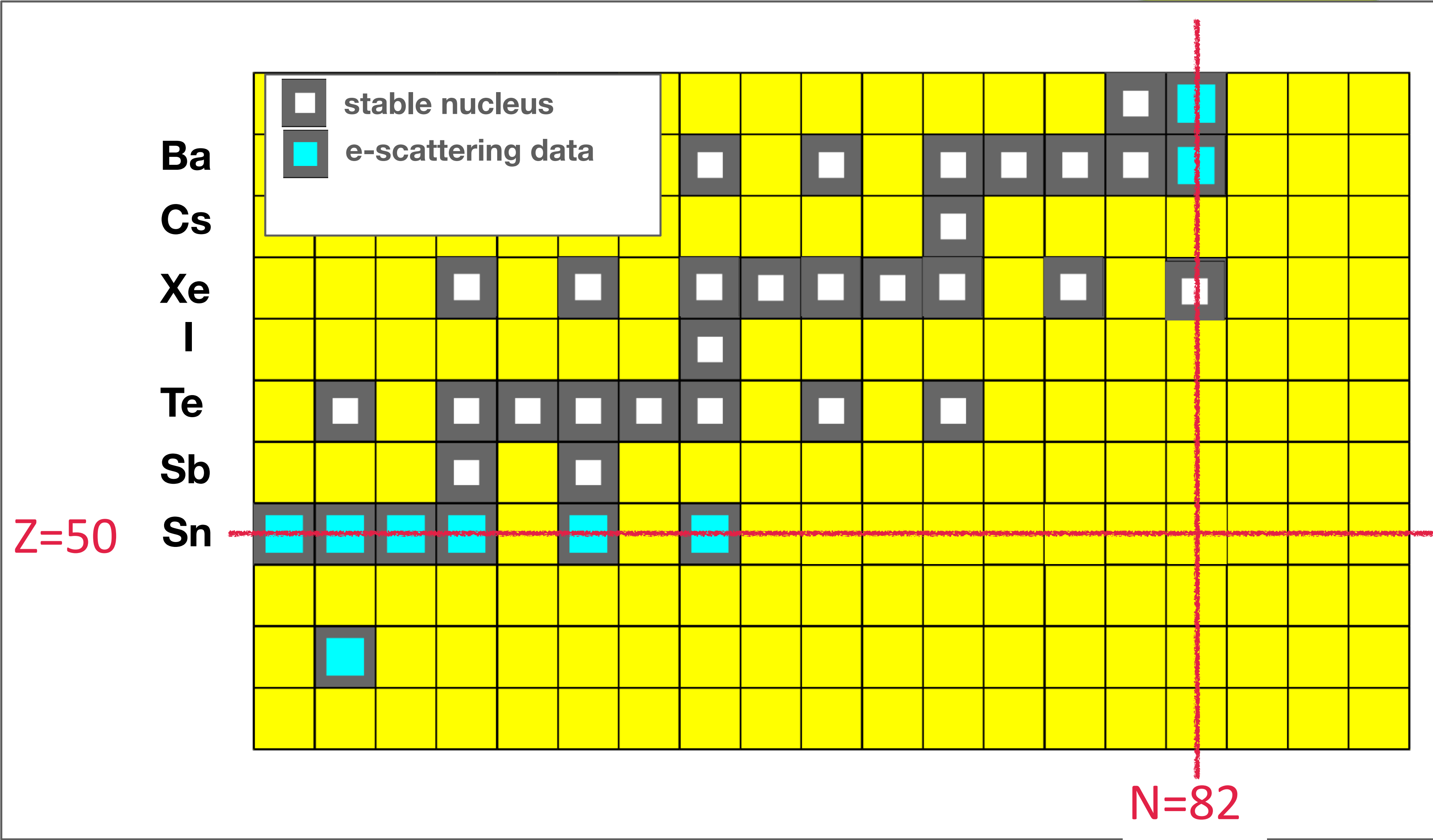
ECT*ws
2025.07.14-07.18



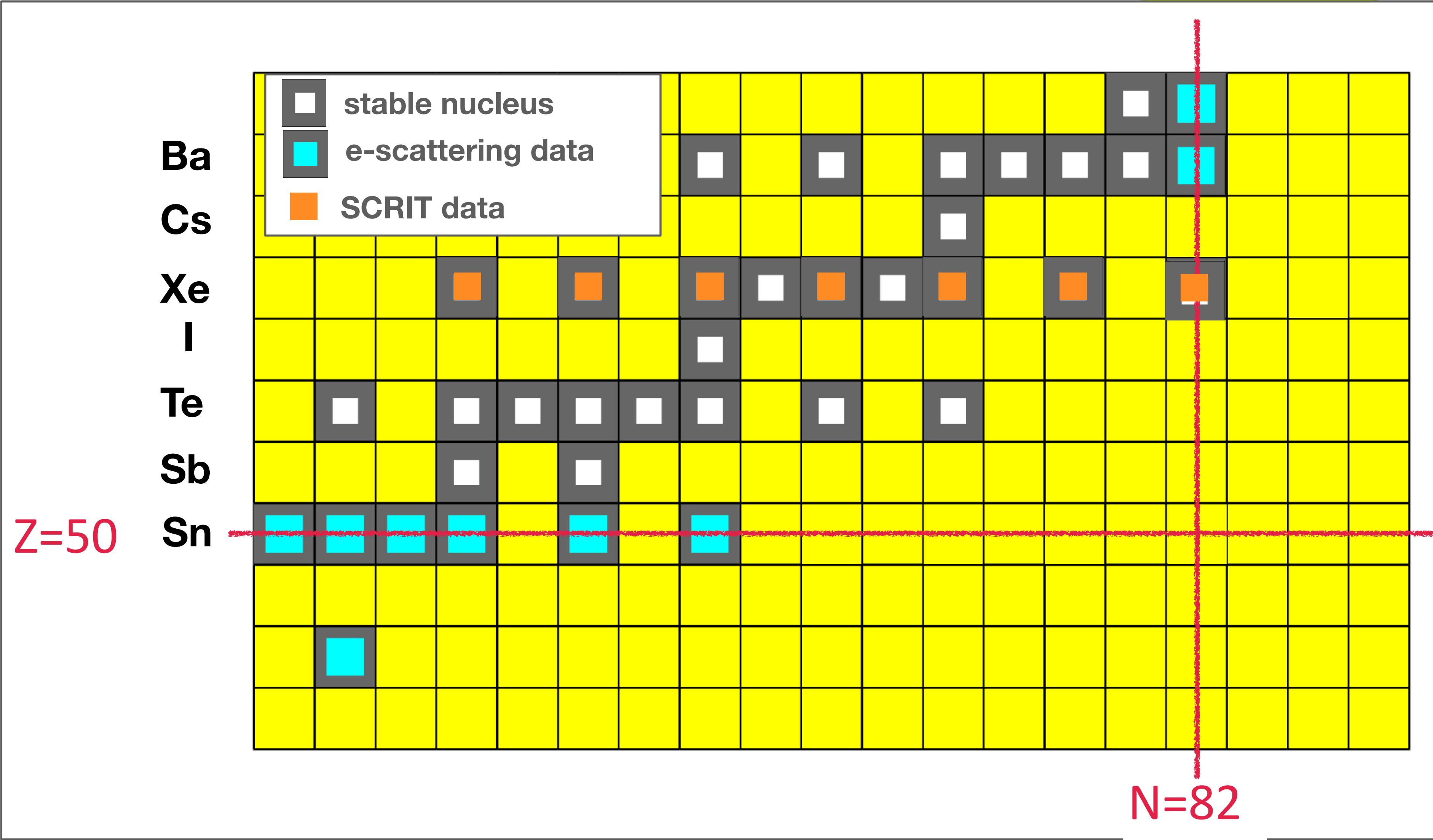
Region of our current studies

ECT*ws
2025.07.14-07.18



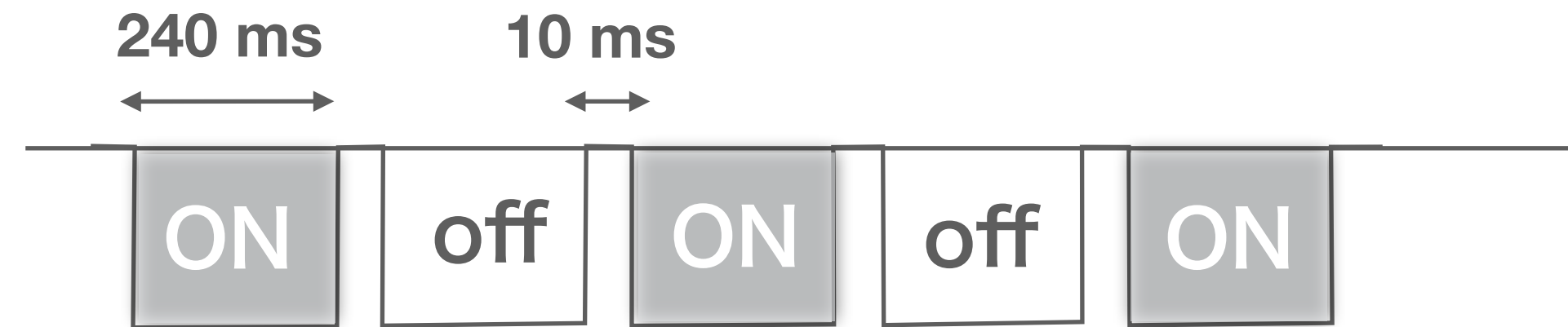


Region of our current studies



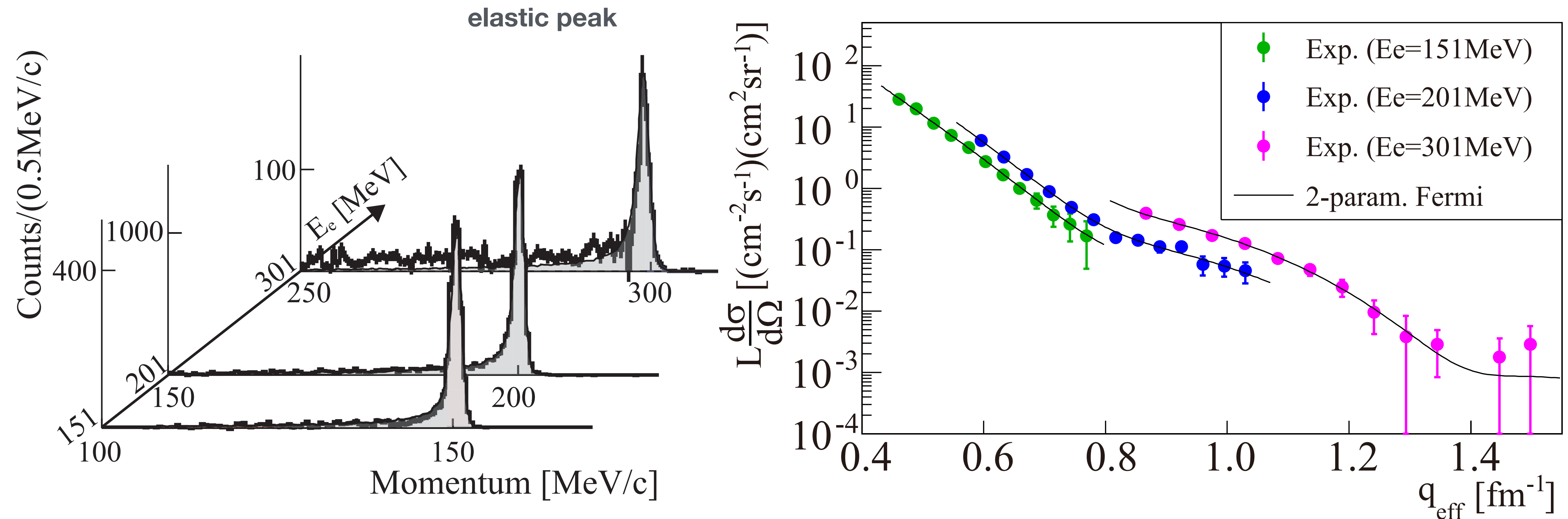
Facility Commissioning with Stable Xe(e,e')

trapping sequence

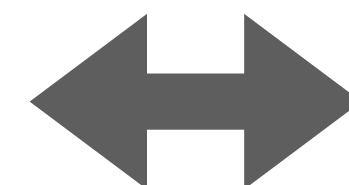


K. Tsukada et al.,
Phys. Rev. Lett. 118 (2017) 262501.

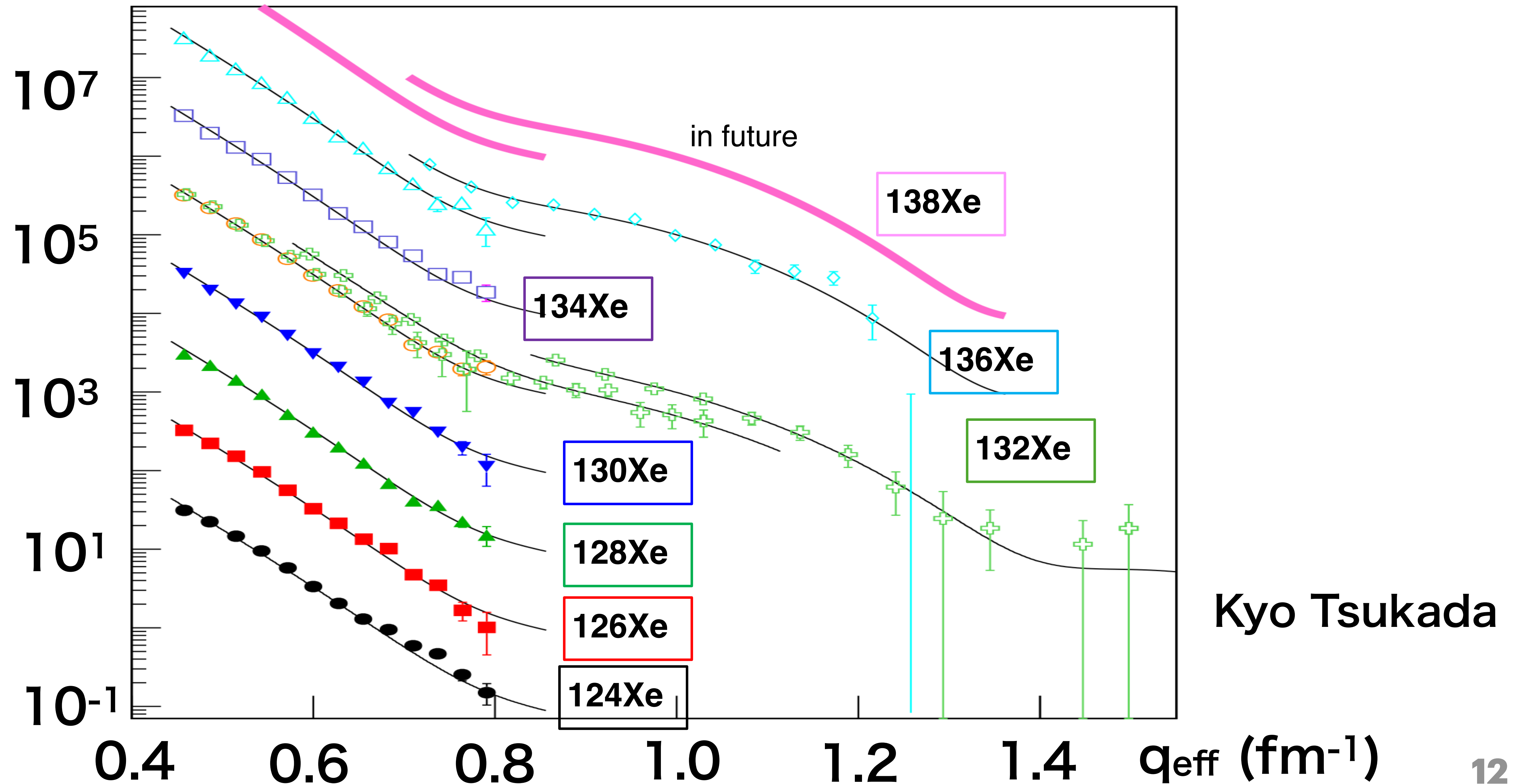
$L \sim 10^{27} \text{ /cm}^2\text{/s}$ with $N_{\text{trapped}} \sim 10^7$



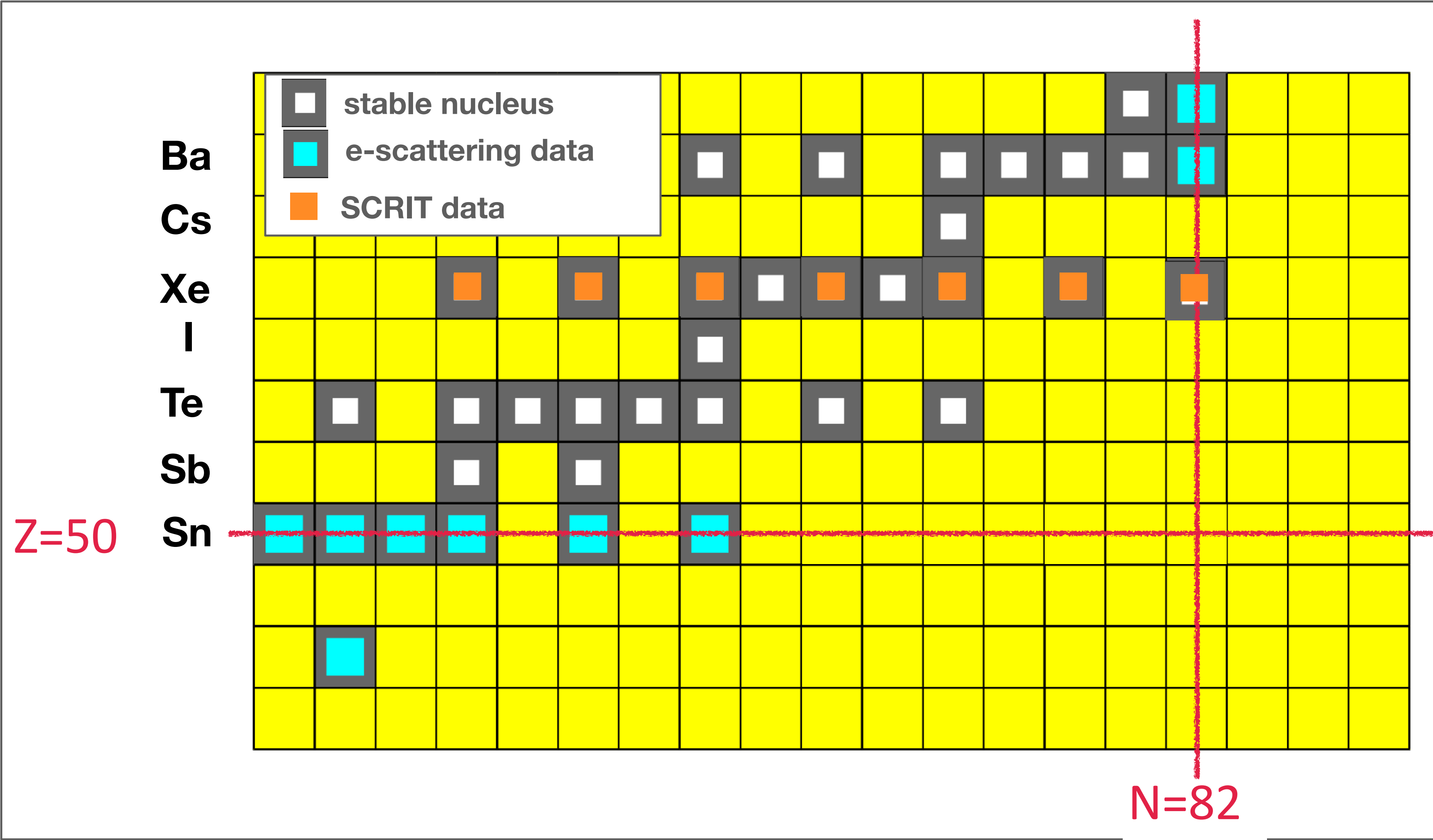
$$\langle r^2 \rangle^{1/2} = 4.789^{+0.12}_{-0.10} \text{ fm}$$



$$\langle r^2 \rangle^{1/2} = 4.787 \text{ fm (}\mu\text{-atom X-rays)}$$



Region of our current studies

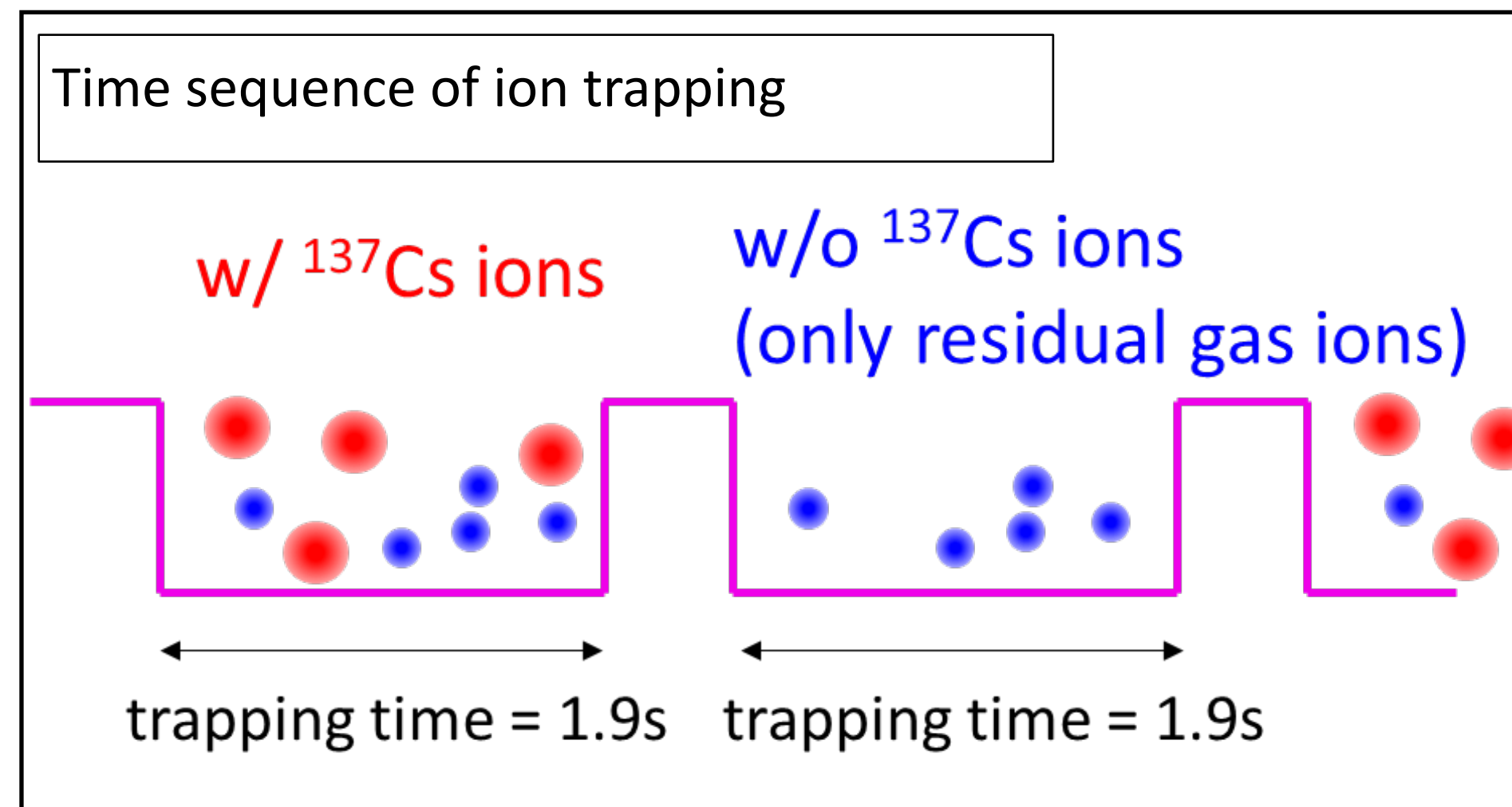


ECT*ws
2025.07.14-07.18



ECT*ws
2025.07.14-07.18





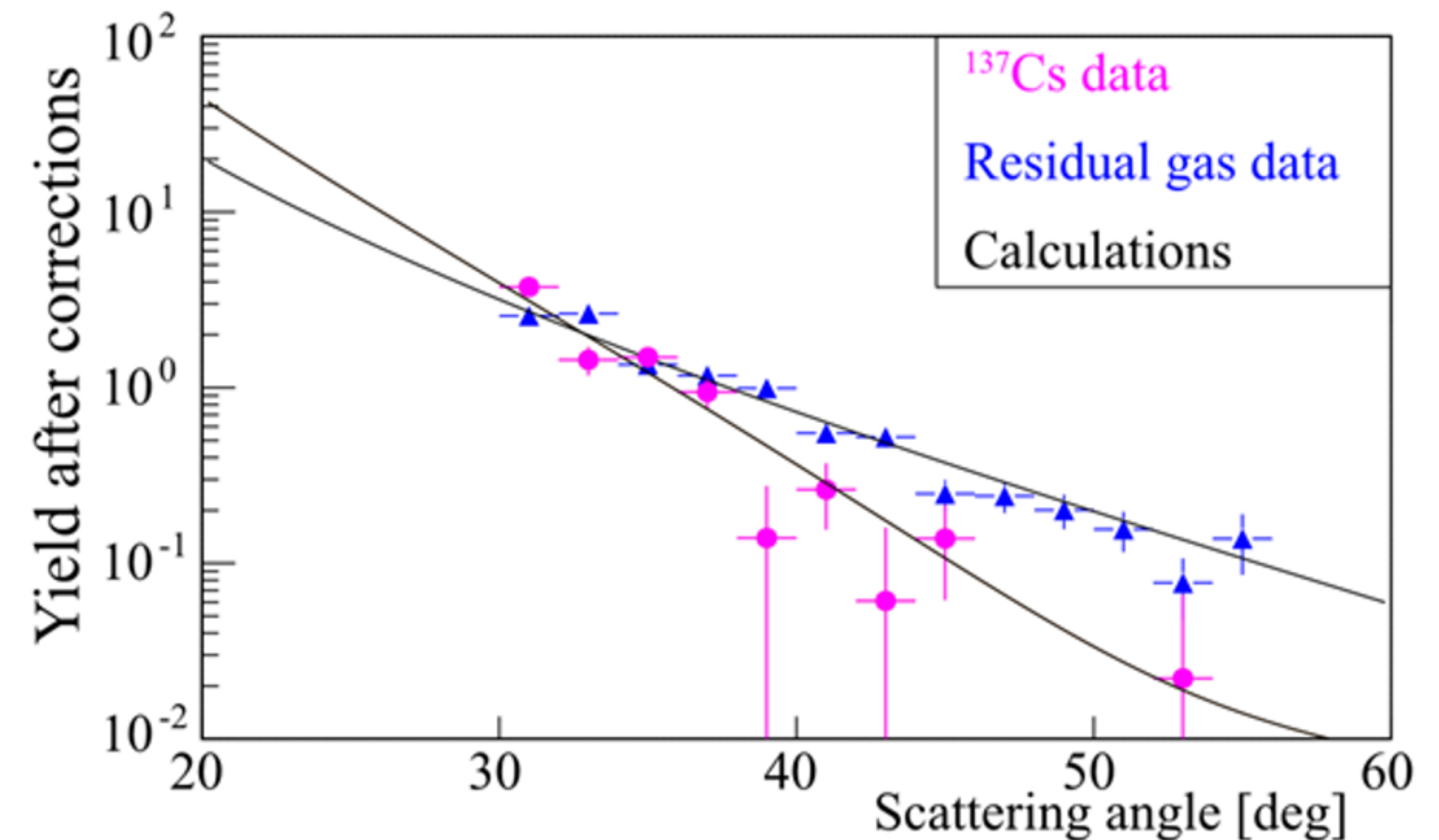
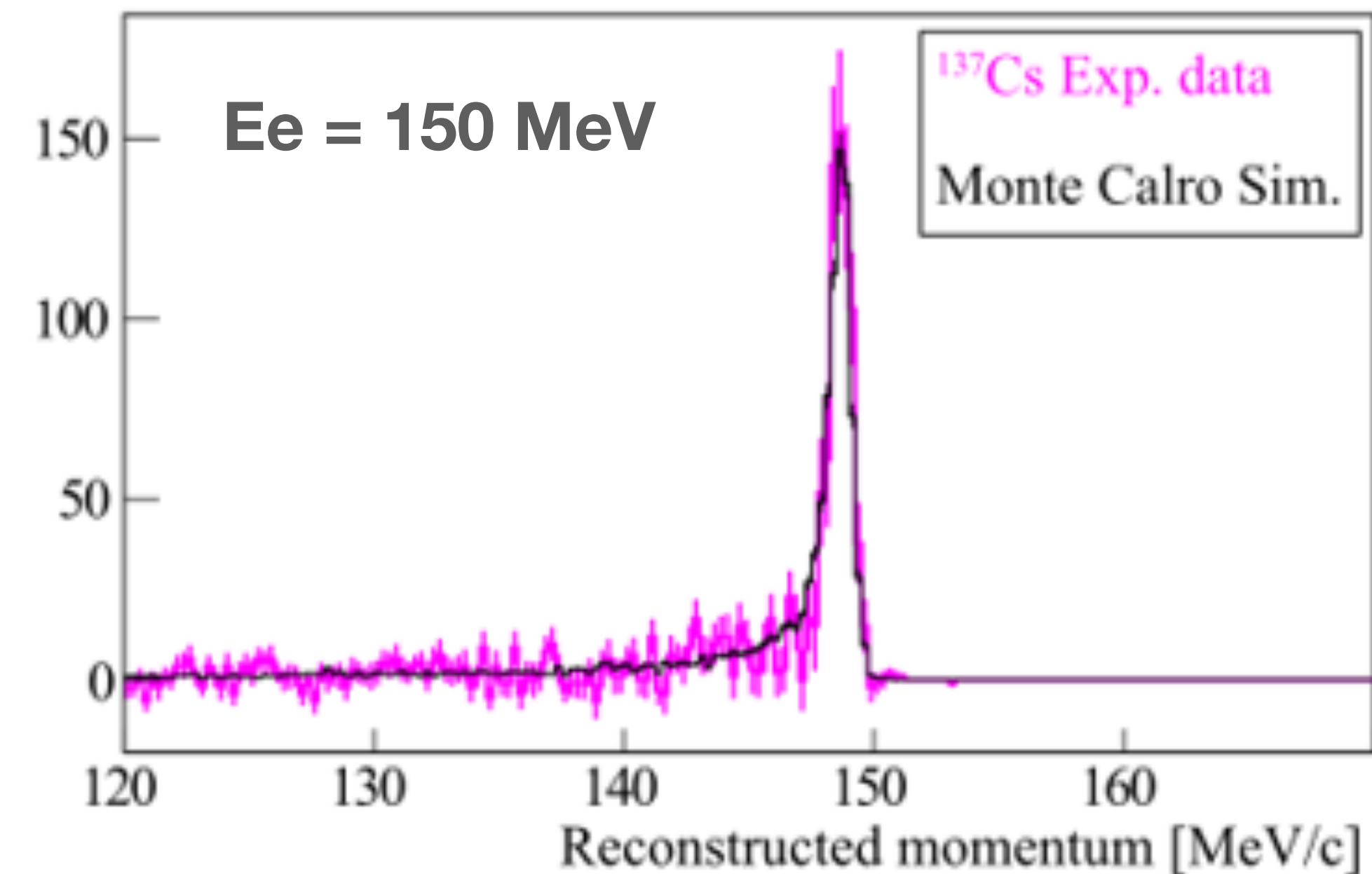
1.9 s trapping

=> mimicking “short-lived” nuclei

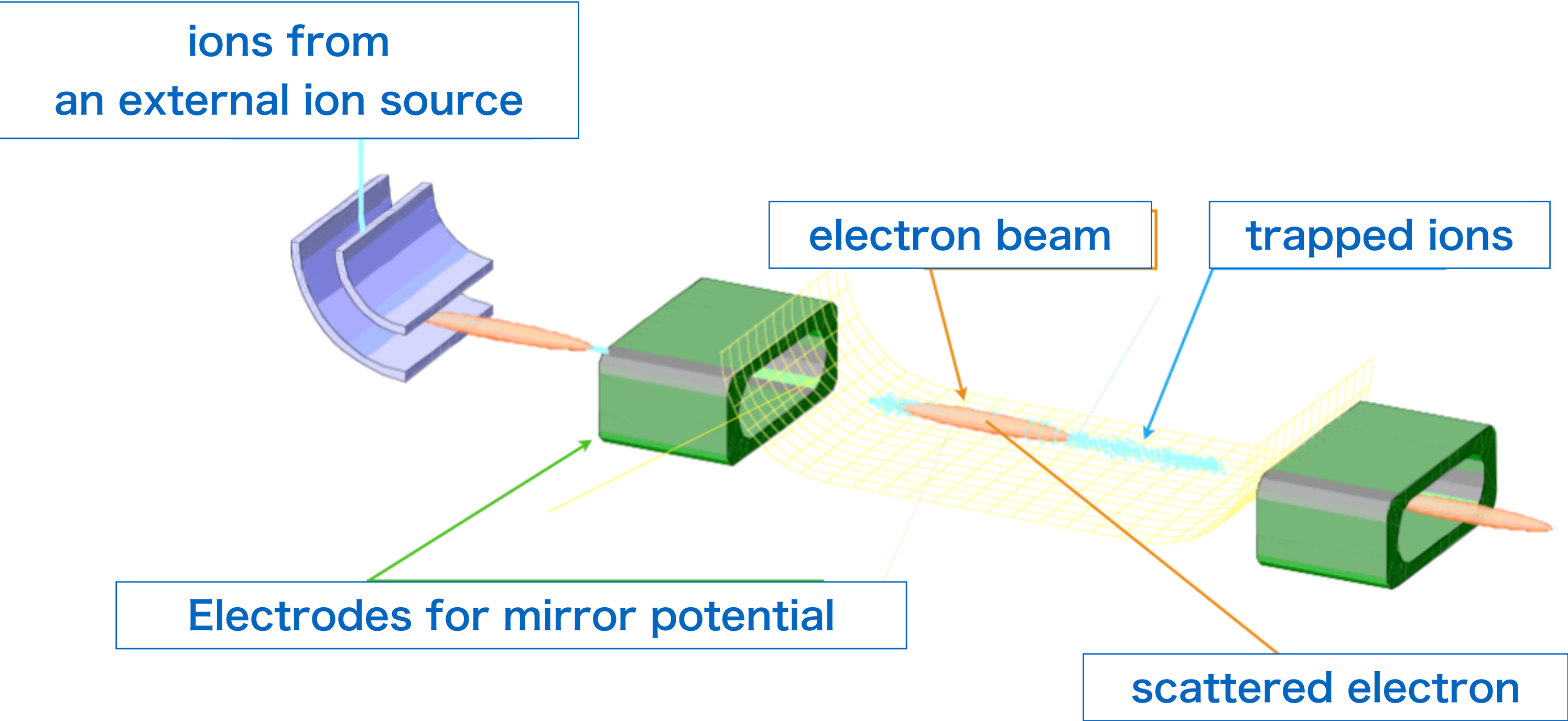
$N_{\text{trapped}} \sim 2 \times 10^7$

=> $L \sim 0.9 \times 10^{26} / \text{cm}^2/\text{s}$

**successful demonstration for
online-produced unstable nuclei**



achieved luminosity with the SCRIT method

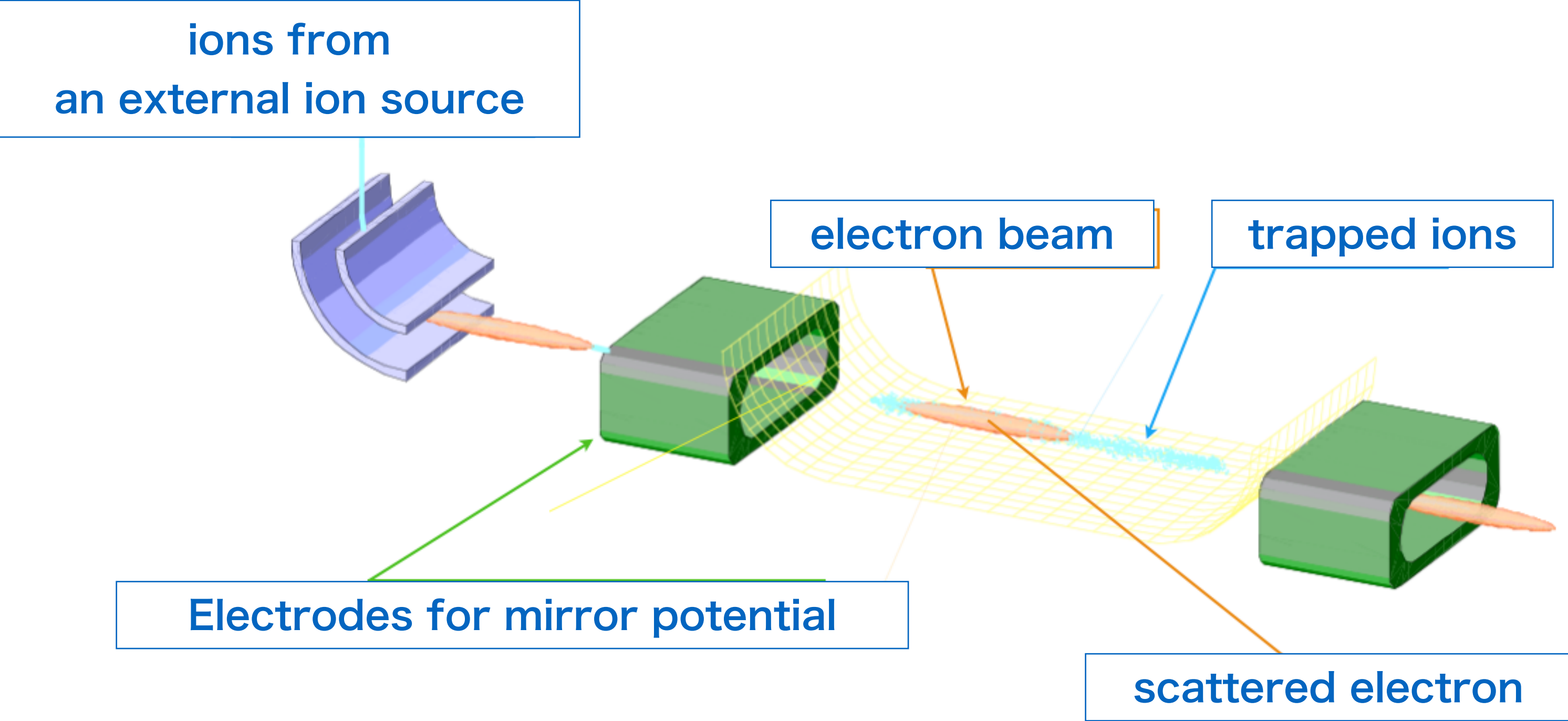


**$\sim 10^7$ ions are trapped
on e-beam ($\sim 1 \text{ mm}^2$)**

$N_t \sim 10^7 / \text{mm}^2 \Rightarrow 10^9 / \text{cm}^2$

	Ee	N _{beam}	$\rho \cdot t$	L
Hofstadter's era (1950s)	150 MeV	$\sim 1 \text{ nA}$ ($\sim 10^9 / \text{s}$)	$\sim 10^{19} / \text{cm}^2$	$\sim 10^{28} / \text{cm}^2 / \text{s}$
JLAB	12 GeV	$\sim 100 \mu\text{A}$ ($\sim 10^{14} / \text{s}$)	$\sim 10^{22} / \text{cm}^2$	$\sim 10^{36} / \text{cm}^2 / \text{s}$
SCRIT	150 - 300 MeV	$\sim 200 \text{ mA}$ ($\sim 10^{18} / \text{s}$)	$\sim 10^9 / \text{cm}^2$	$\sim 10^{27} / \text{cm}^2 / \text{s}$

achieved luminosity with the SCRIT method



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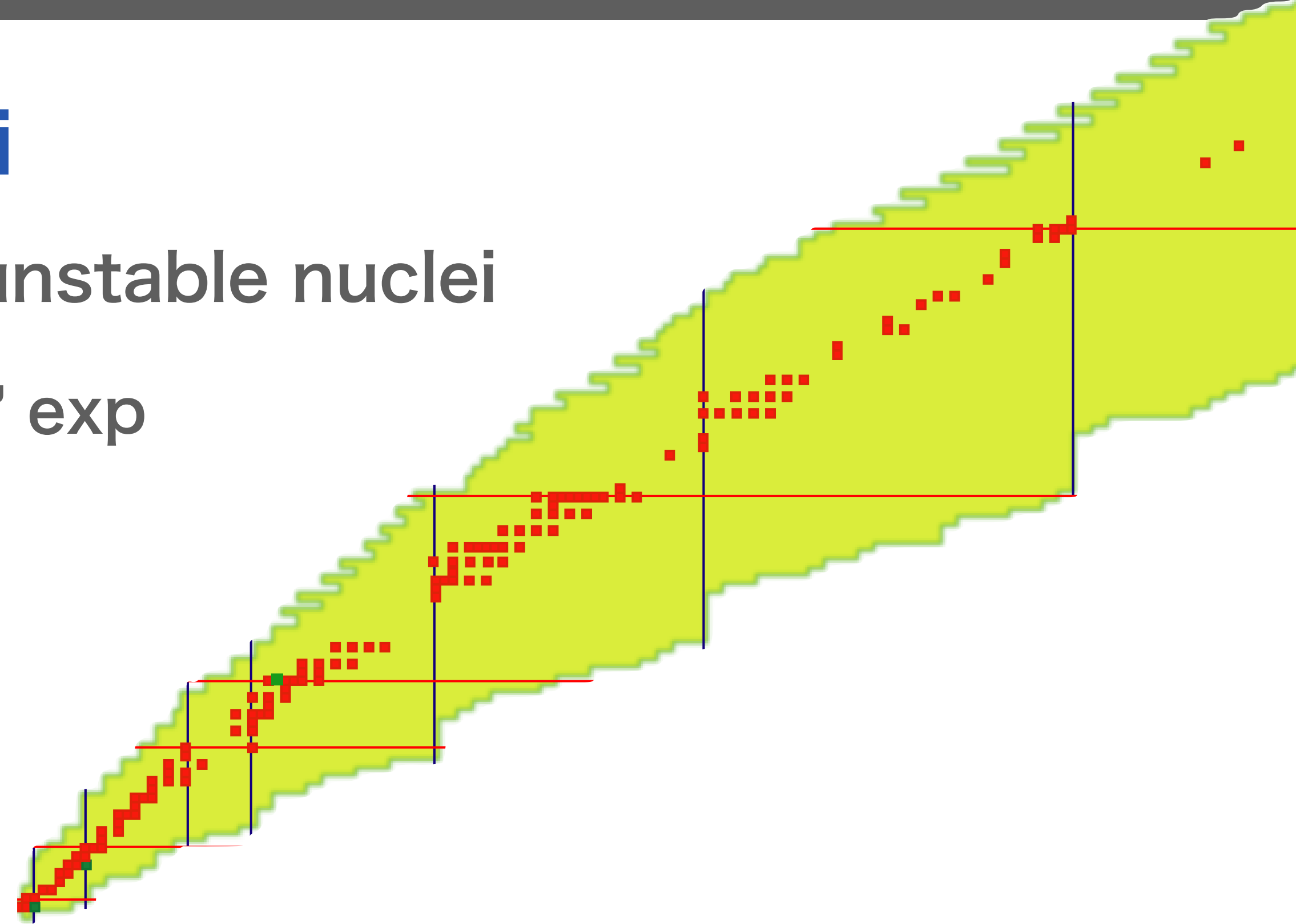
**REQUIRED TARGET
THICKNESS
 10^{-10} !!!**

	Ee	N _{beam}	$\rho \cdot t$	L
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1) charge densities of exotic nuclei

systematic measurements for many unstable nuclei

^{132}Sn : symbolic target for “day-one” exp



ISOL upgrade: towards ^{132}Sn (40s)

ECT*ws
2025.07.14-07.18

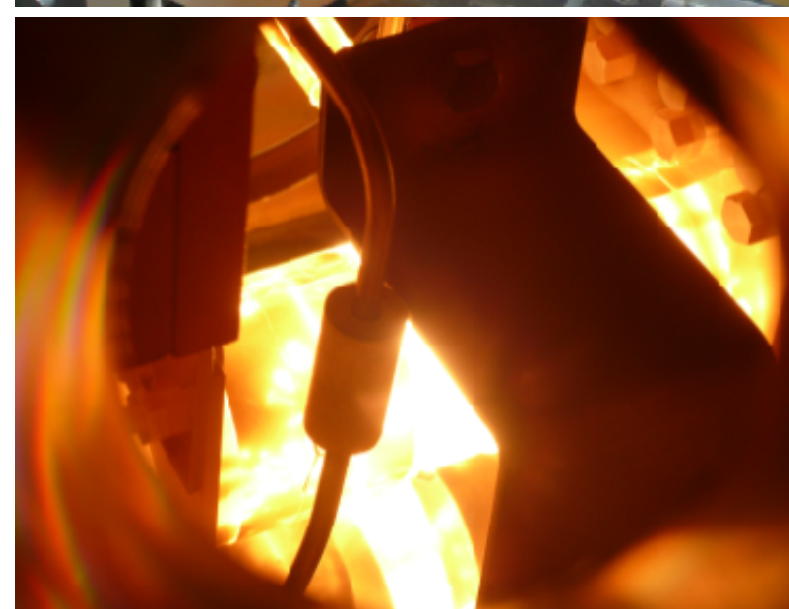
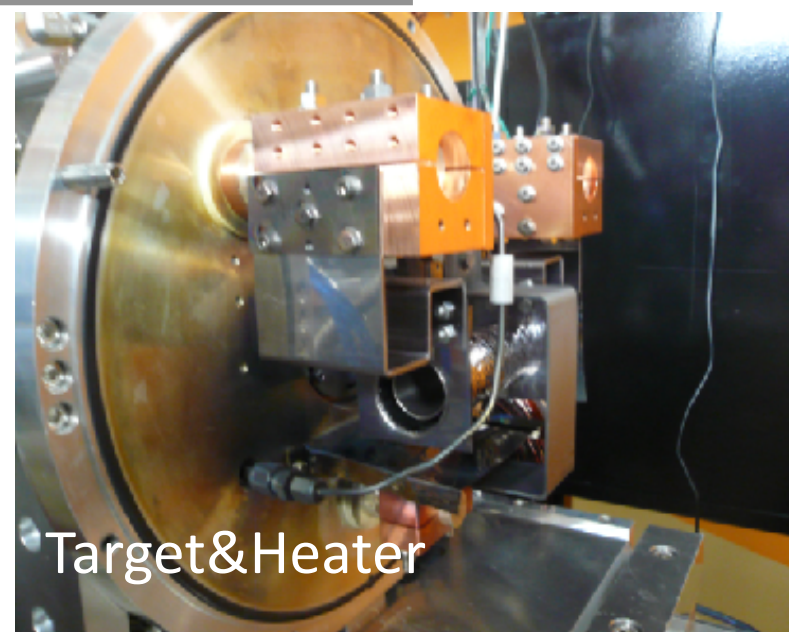
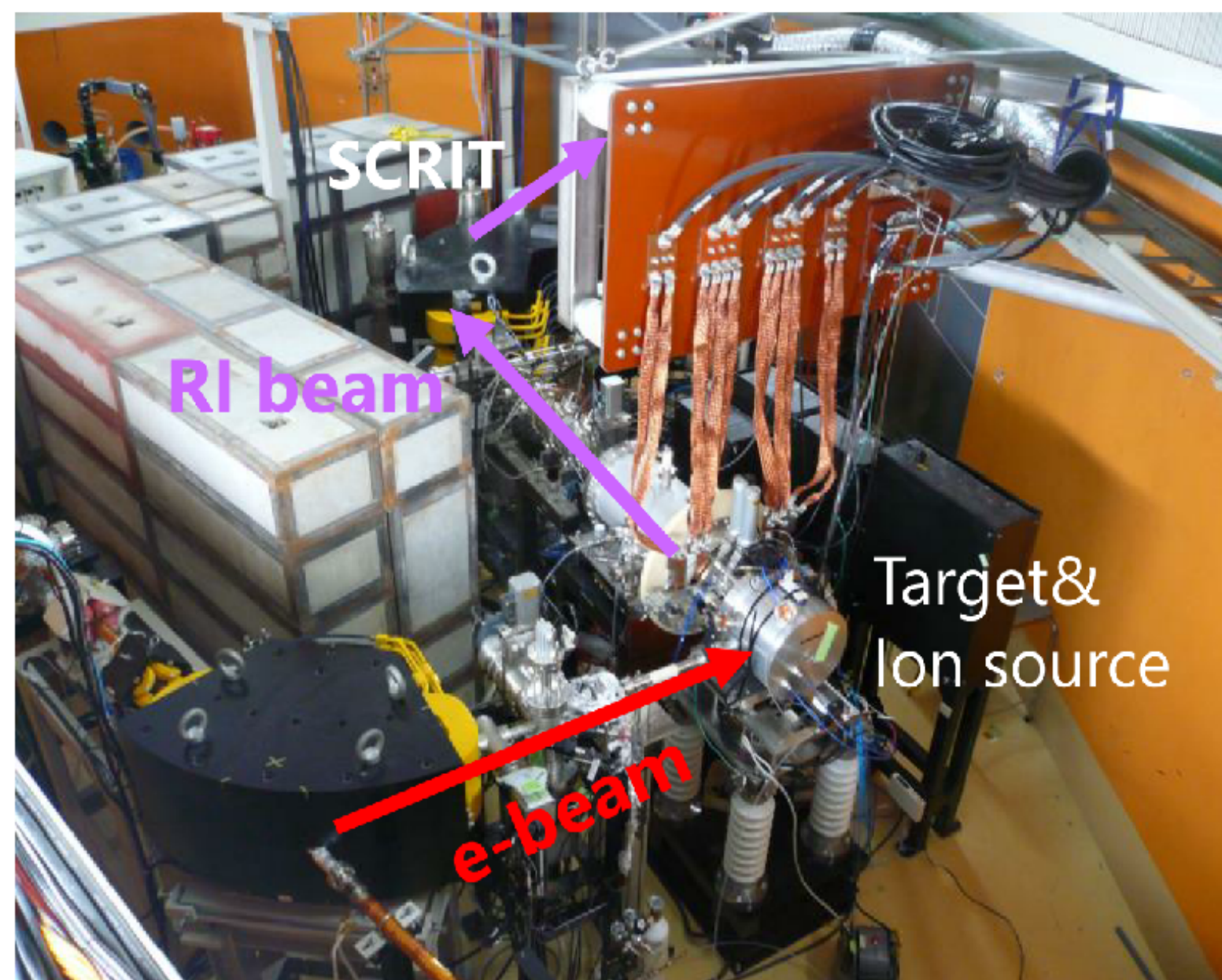
Production Rate

$$N_{\text{fission}} \sim 10^8 \text{ /watt}$$

$$N^{132}\text{Sn} \sim 10^6 \text{ /watt} * 1\% (\epsilon_{\text{trans.}})$$

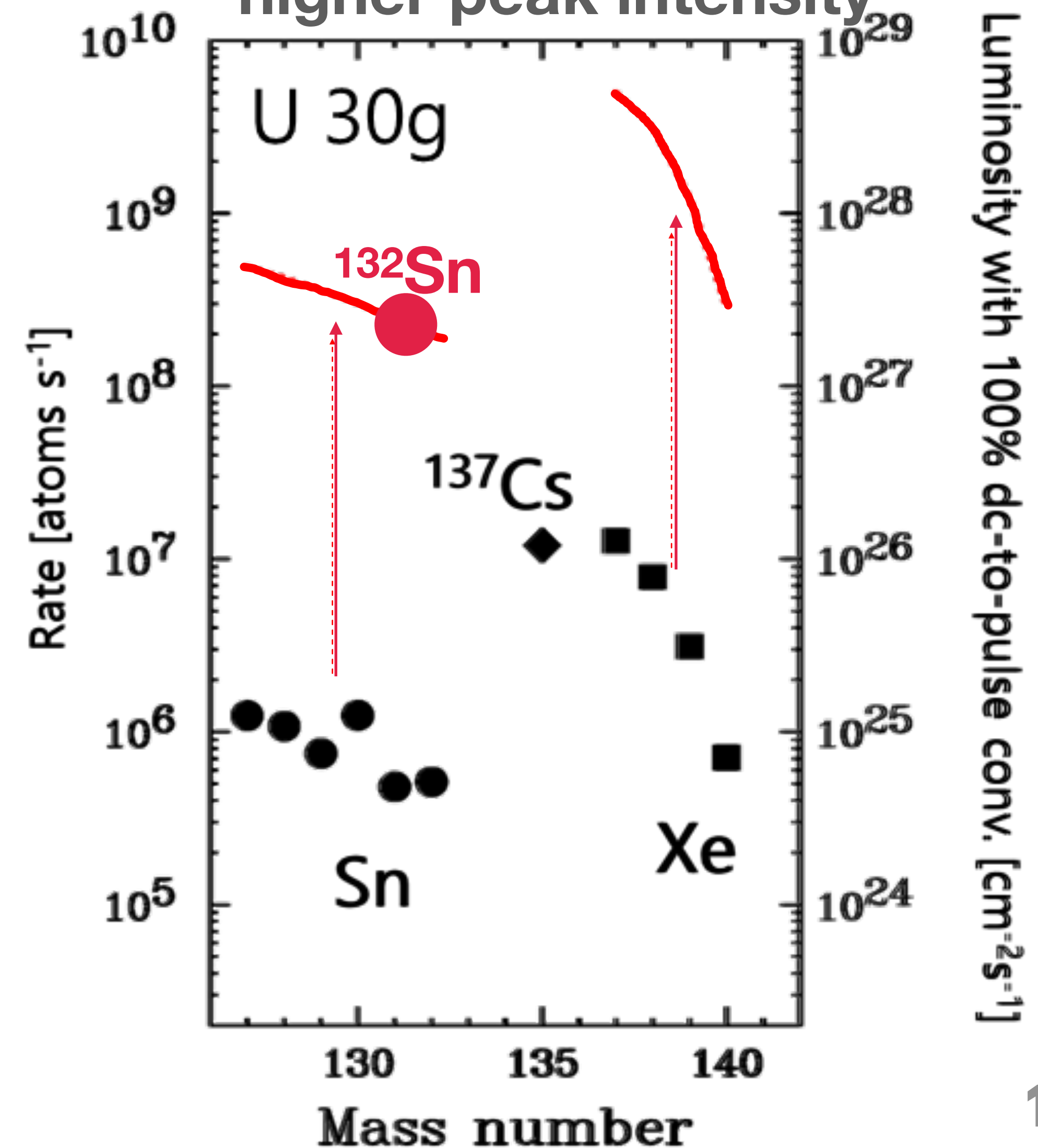
beam power : $\sim 20\text{W}$ (today)

$\sim 2 \text{ kW}$ (underway)



House-made
Uranium carbide (UCx)

towards 2 kW e-beam
higher repetition
higher peak intensity

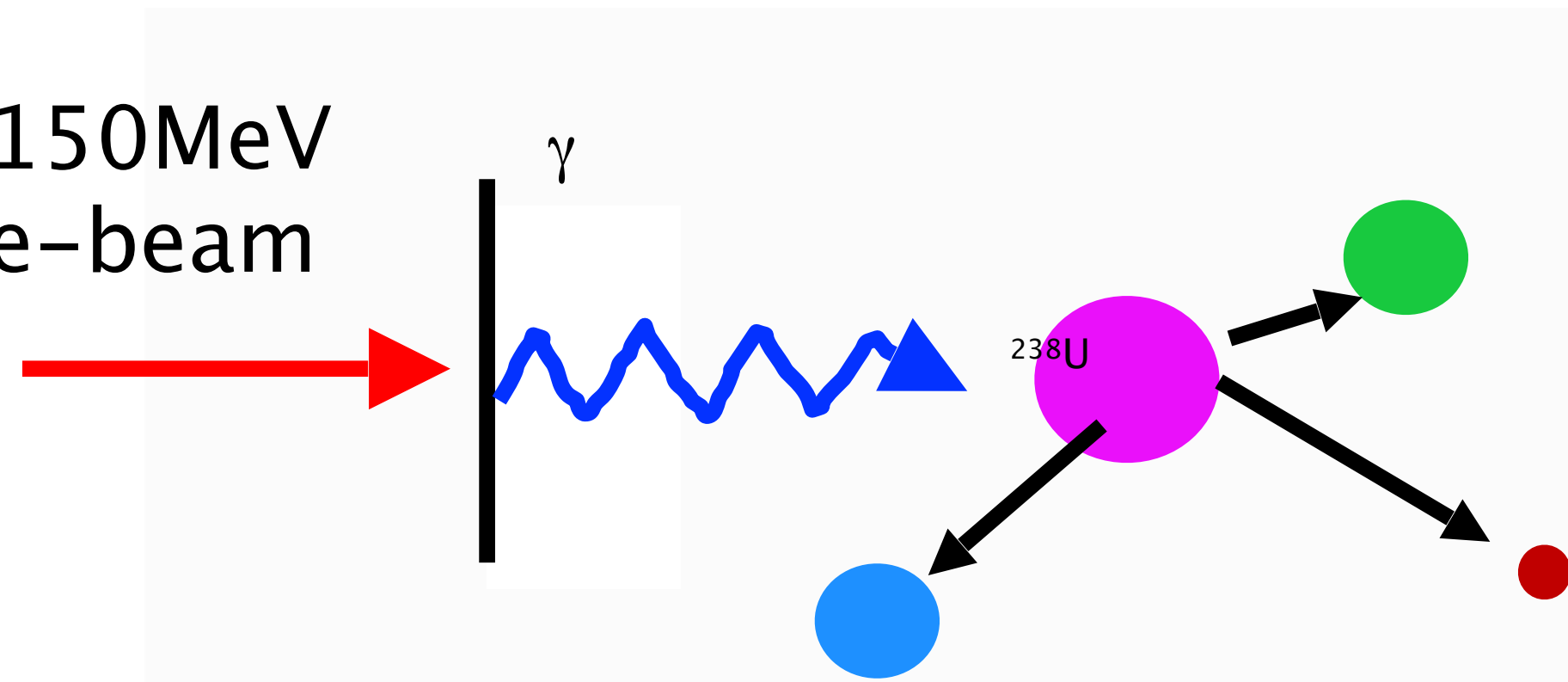


T. Ohnishi *et al.* NIM B317 (2013) 357.

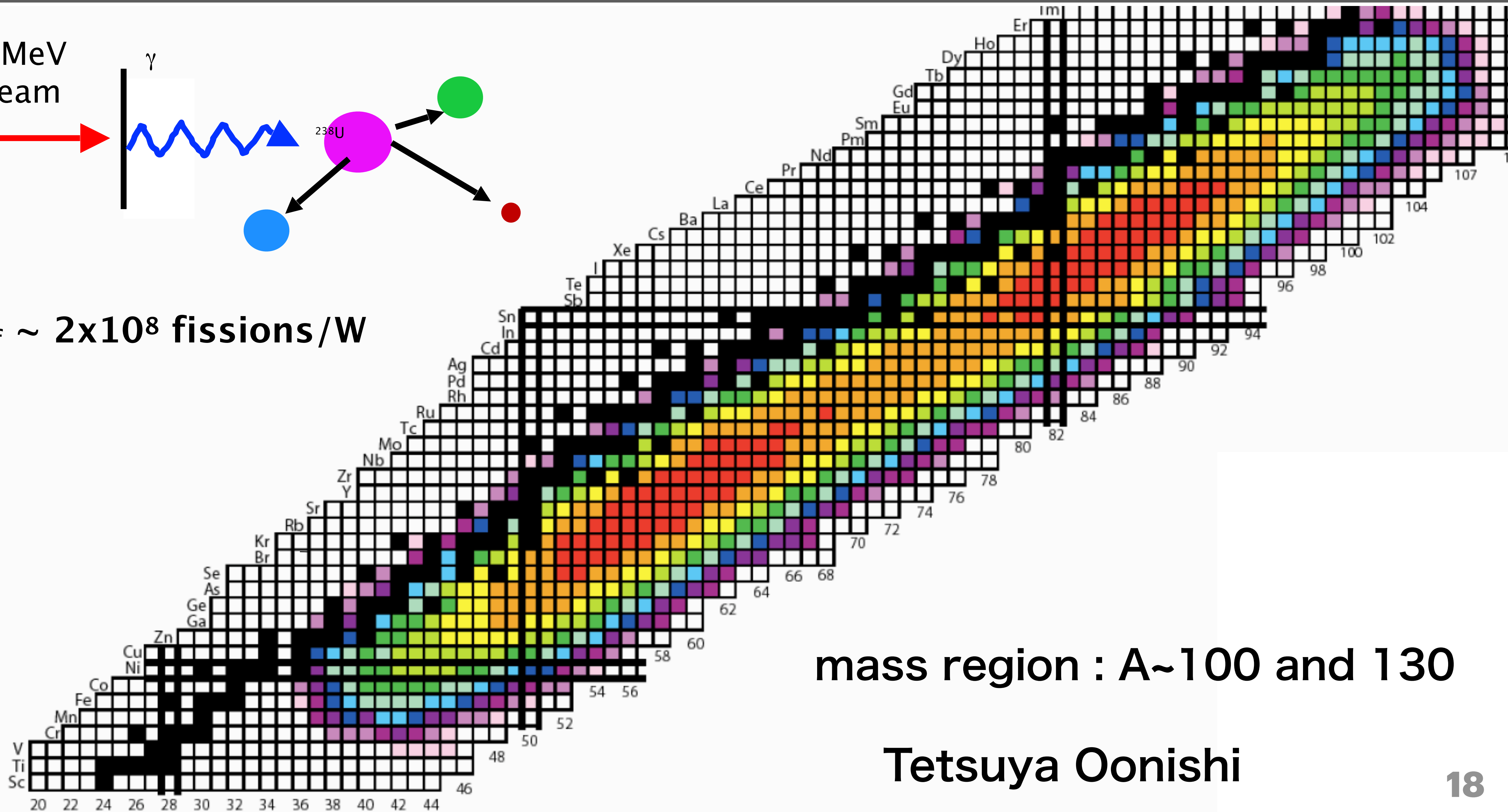
^{238}U photo-fission yields

ECT*ws
2025.07.14-07.18

150MeV
e-beam



$$R_f \sim 2 \times 10^8 \text{ fissions/W}$$



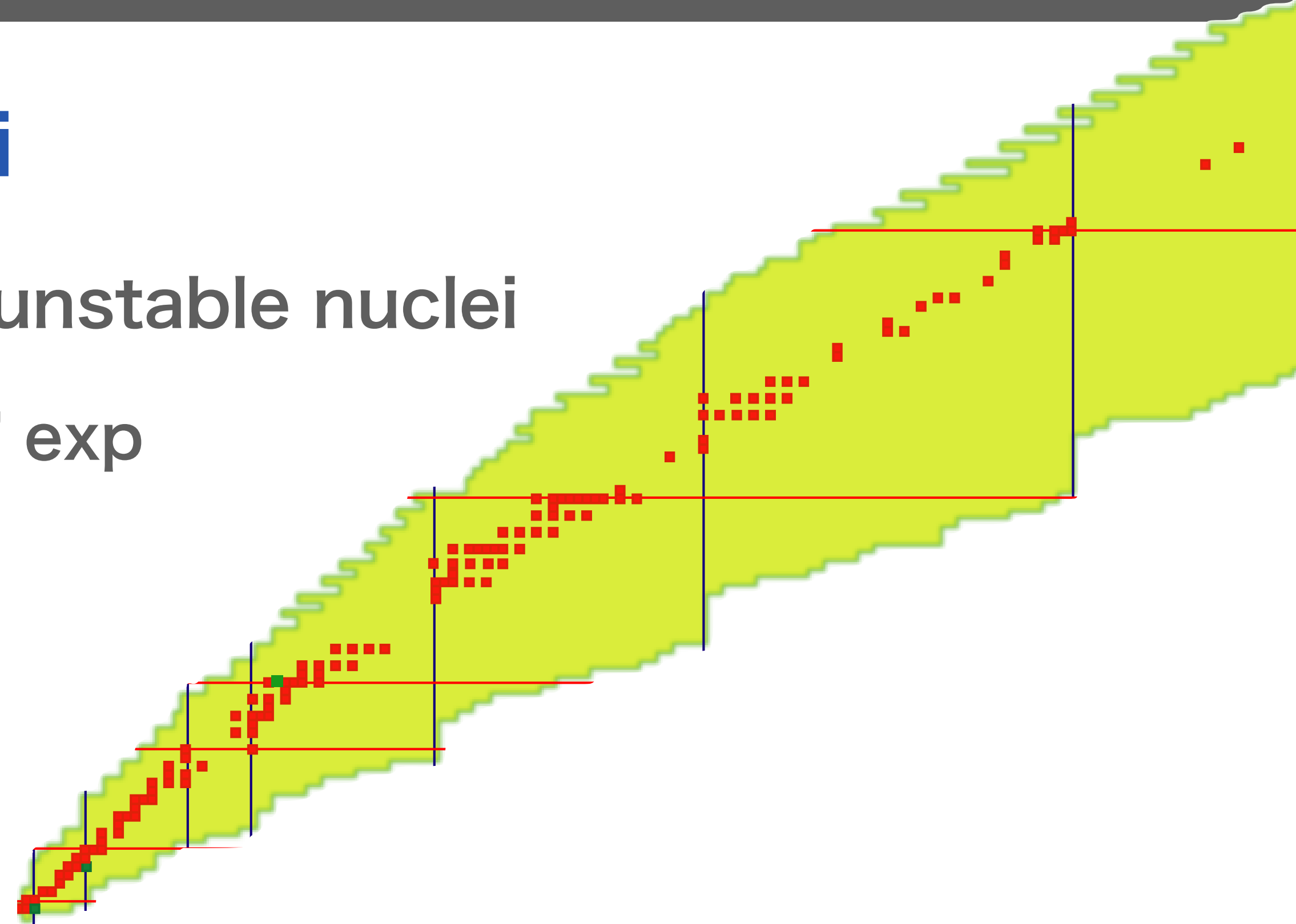
mass region : $A \sim 100$ and 130

Tetsuya Oonishi

1) charge densities of exotic nuclei

systematic measurements for many unstable nuclei

^{132}Sn : symbolic target for “day-one” exp

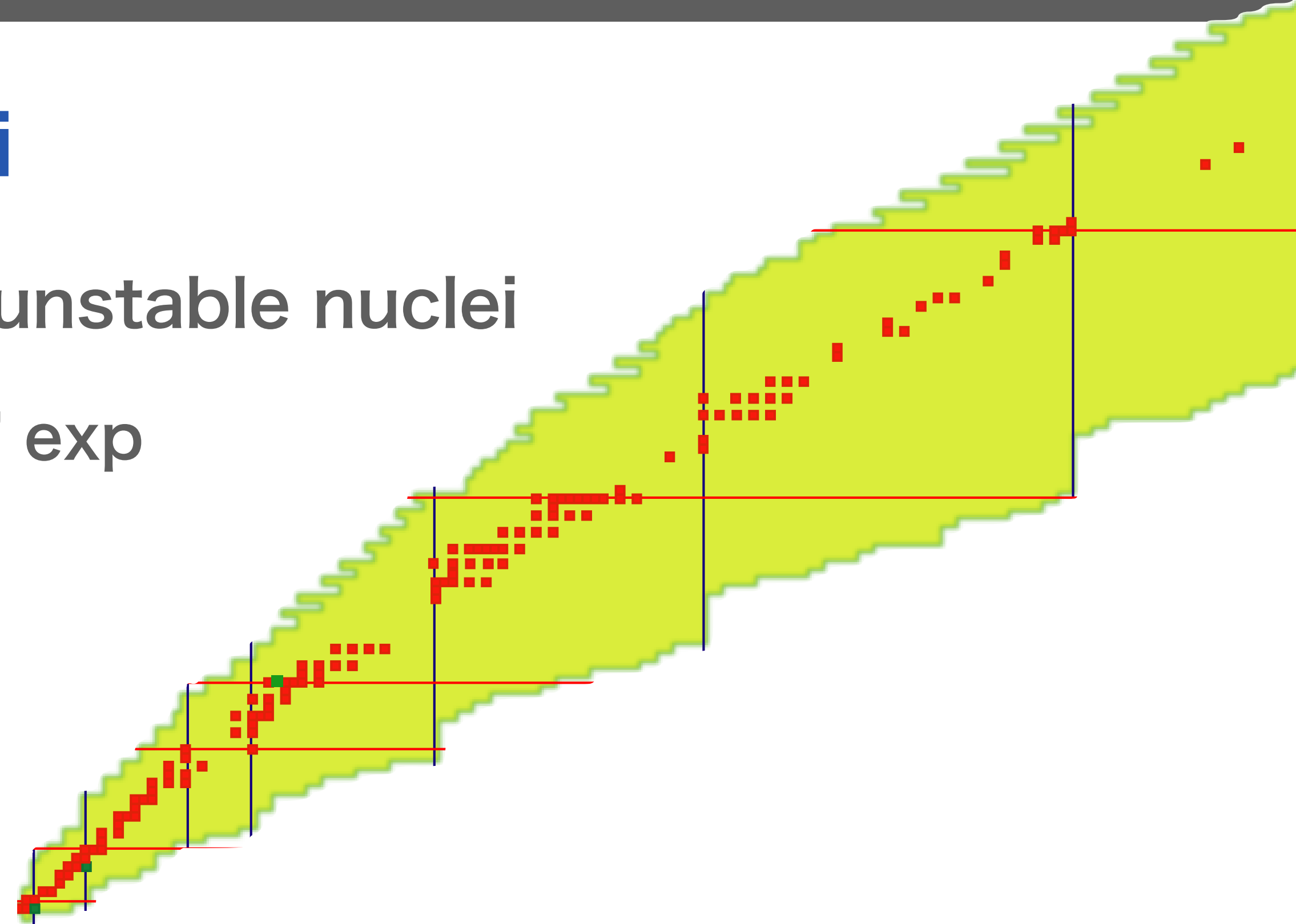


1) charge densities of exotic nuclei

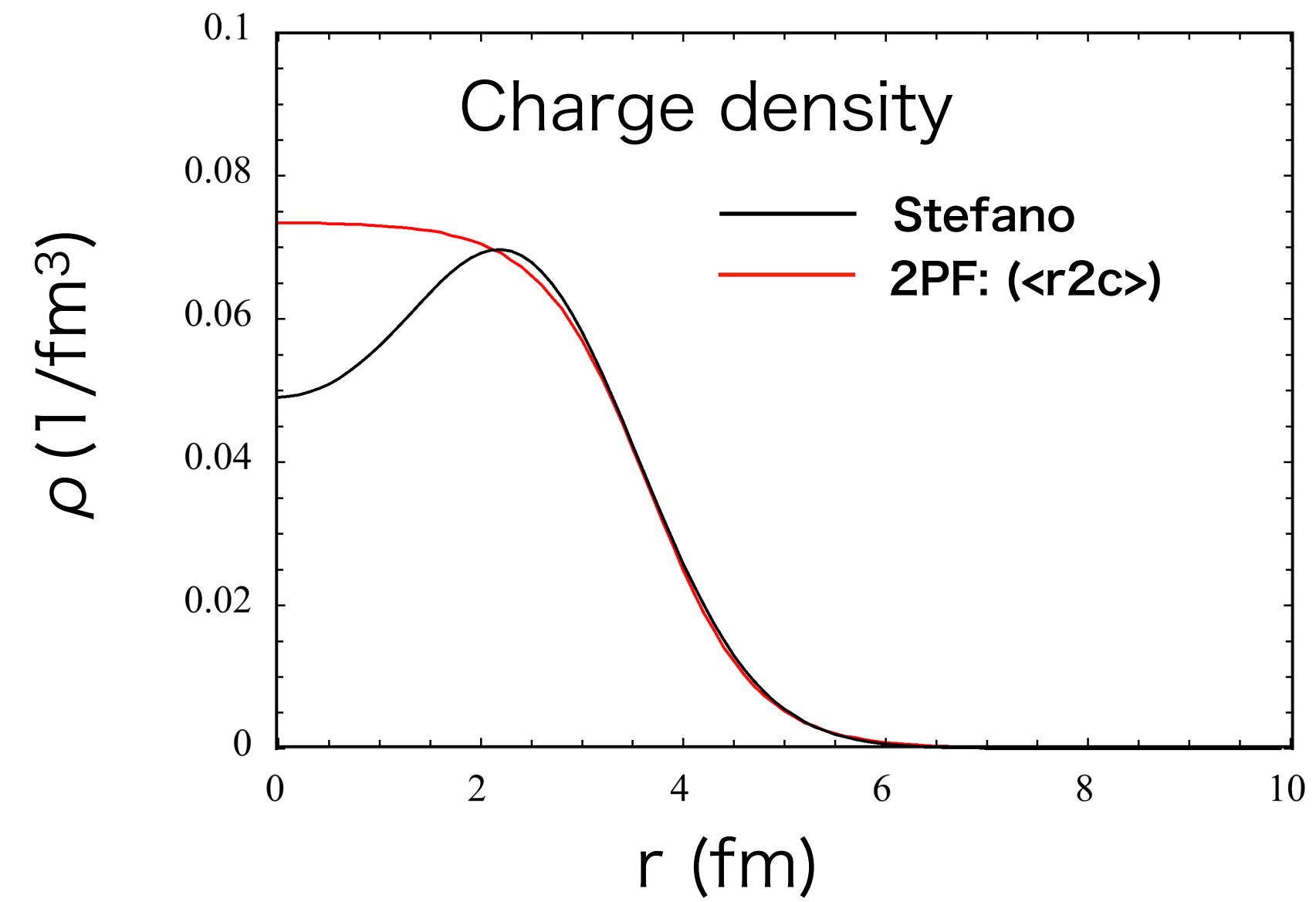
systematic measurements for many unstable nuclei

^{132}Sn : symbolic target for “day-one” exp

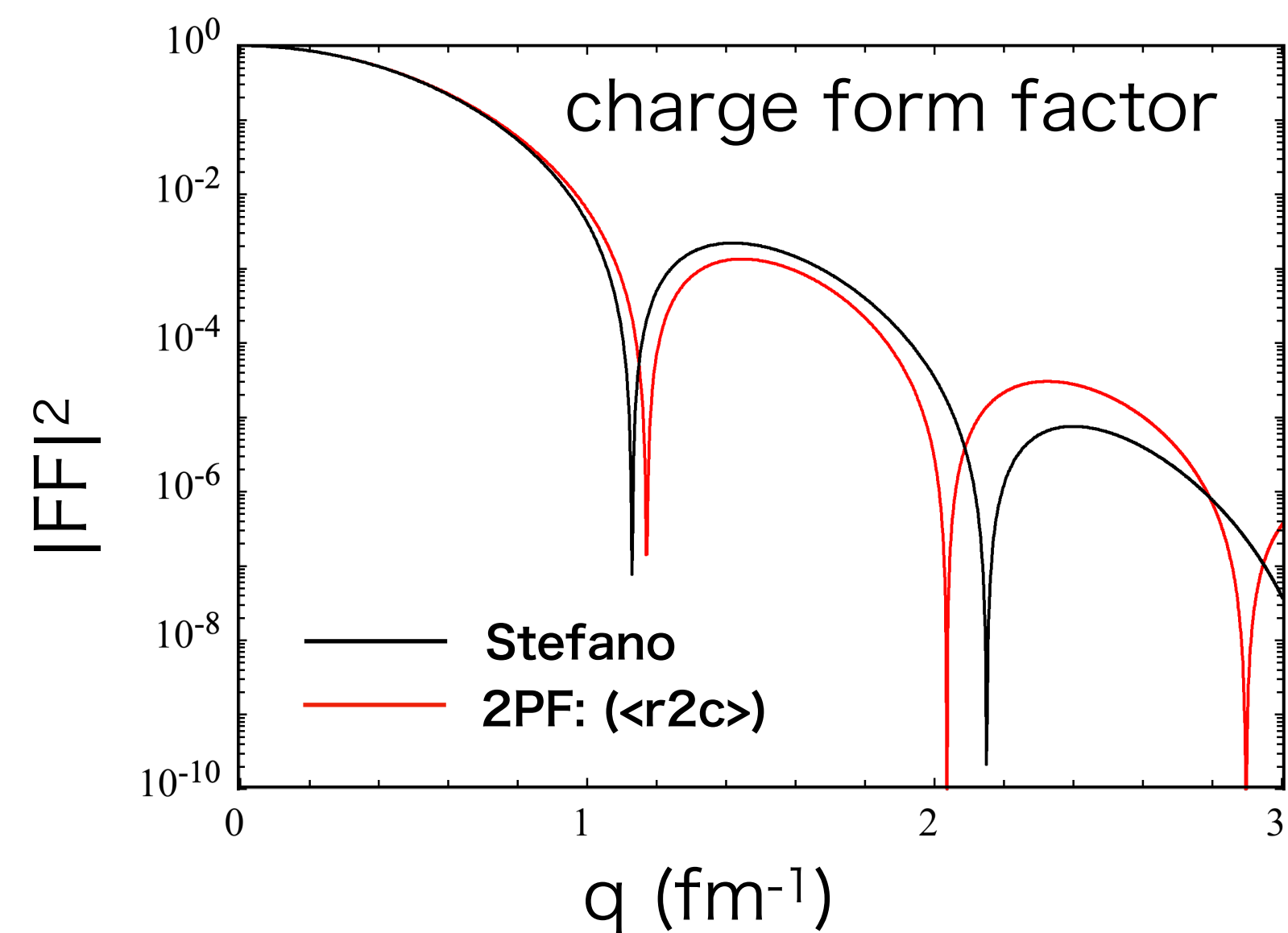
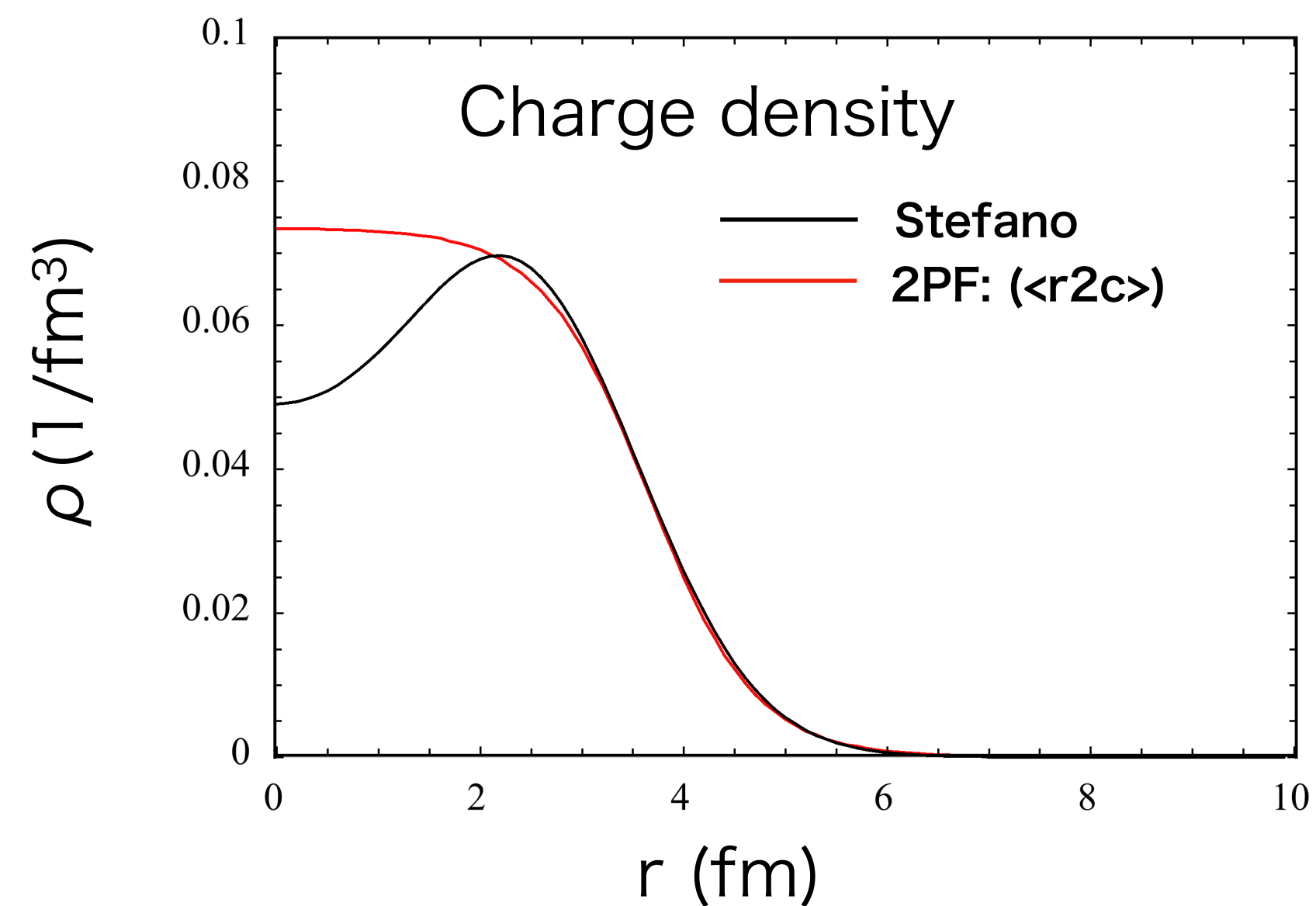
^{46}Ar : Stefano Brolli



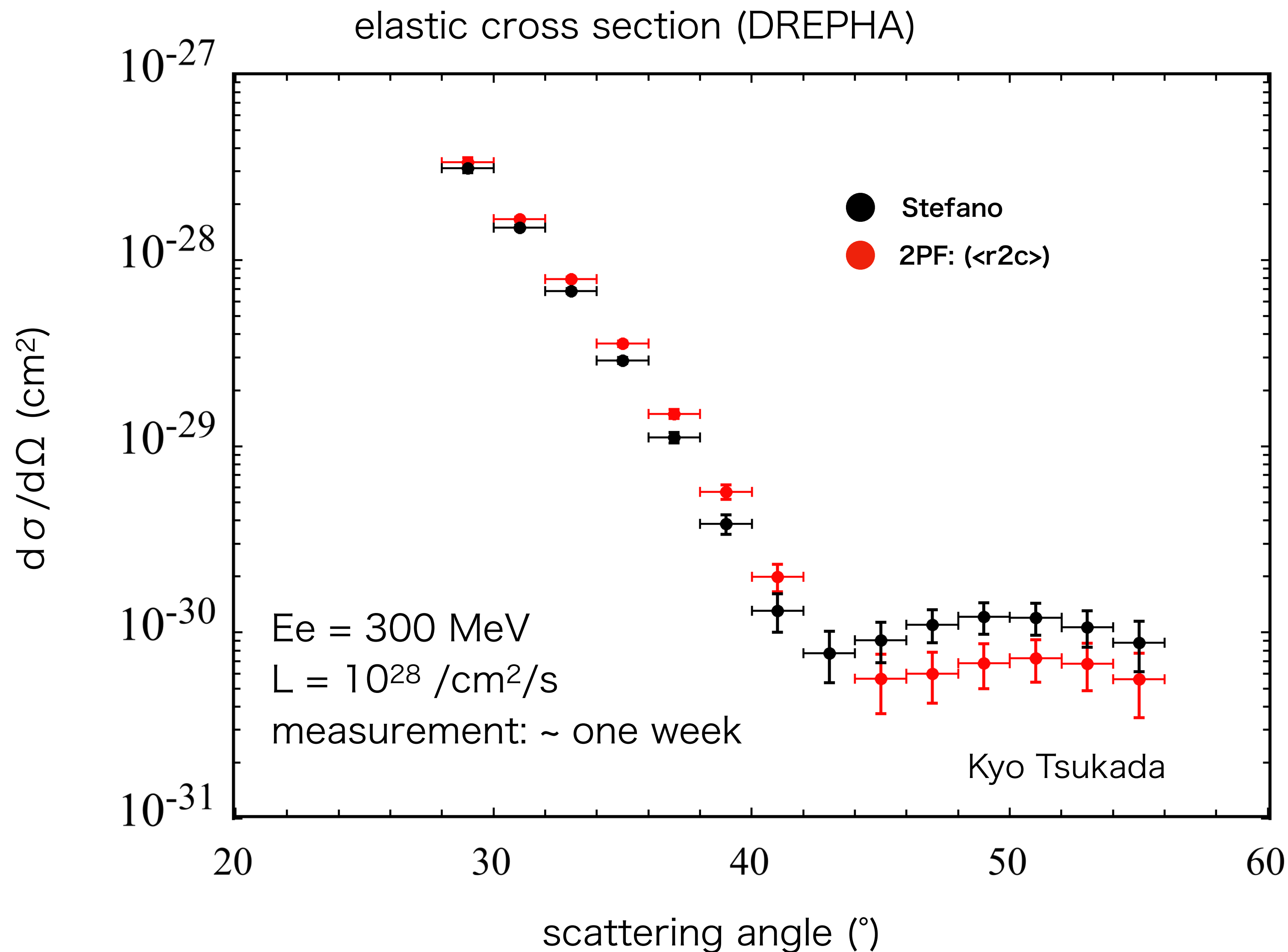
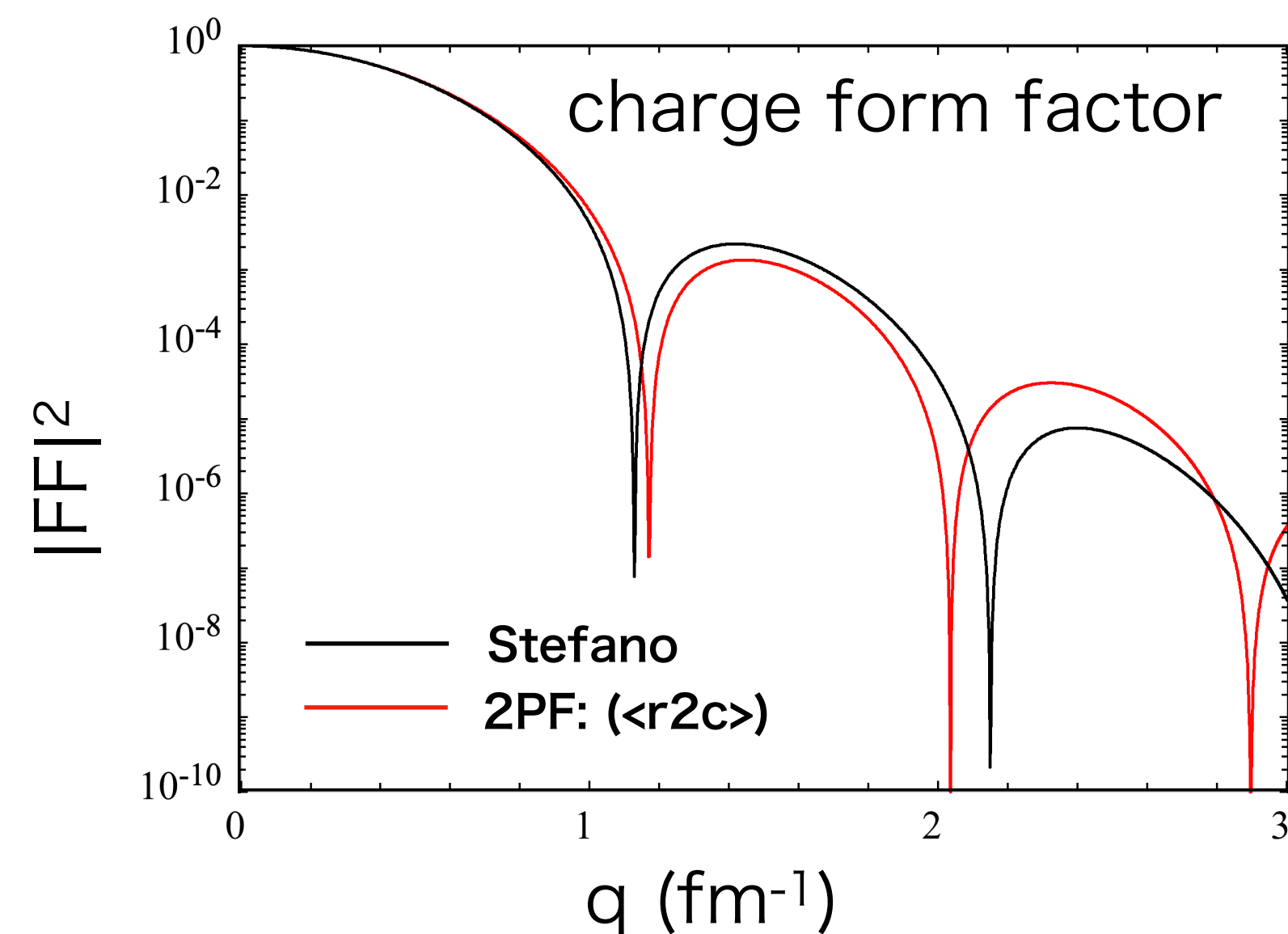
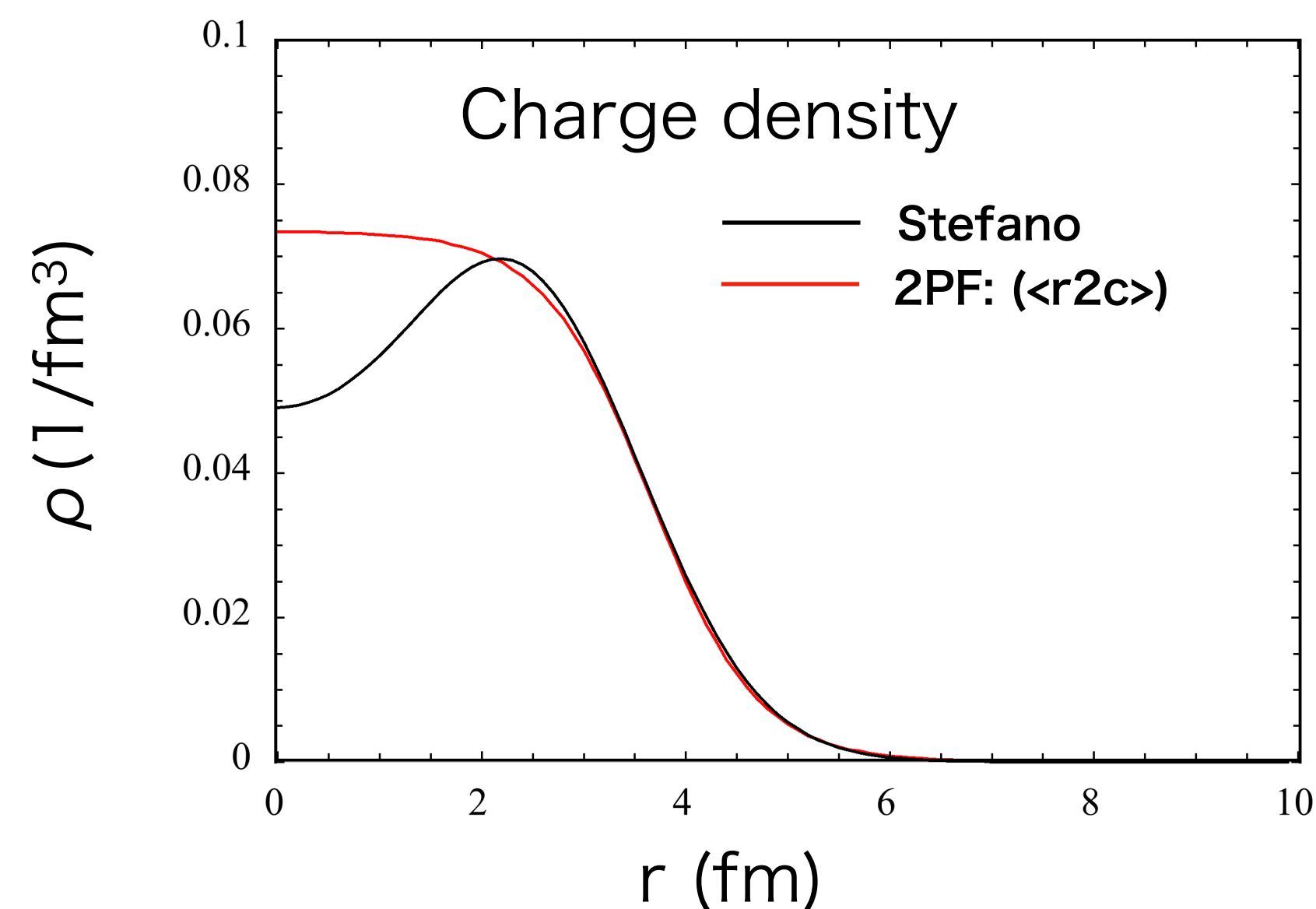
Courtesy: Stefano Brolli



Courtesy: Stefano Brolli



Courtesy: Stefano Brolli



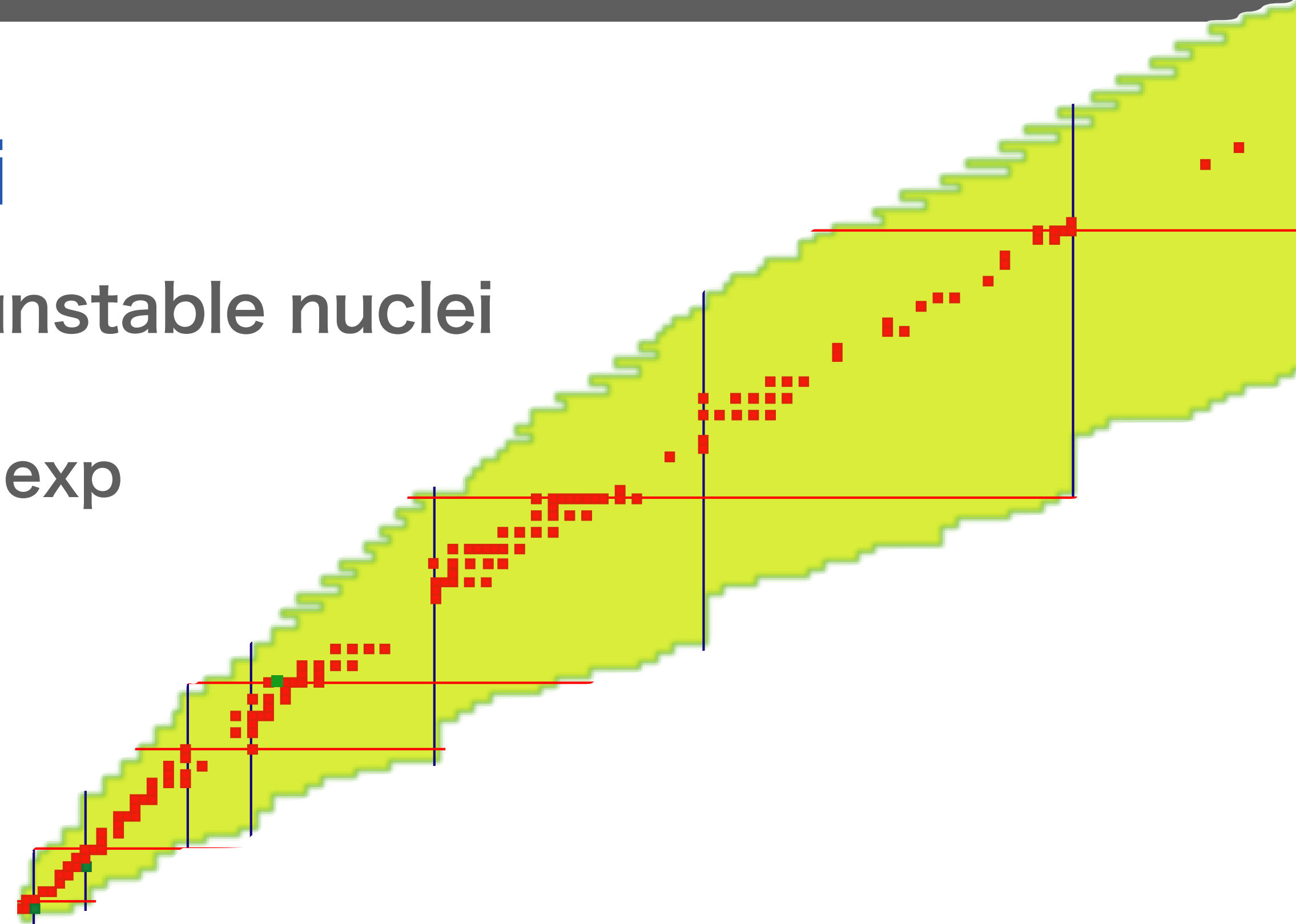
1) charge densities of exotic nuclei

systematic measurements for many unstable nuclei

^{132}Sn : symbolic target for “day-one” exp

^{46}Ar : Stefano Brolli

.....



1) charge densities of exotic nuclei

systematic measurements for many unstable nuclei

^{132}Sn : symbolic target for “day-one” exp

^{46}Ar : Stefano Brolli

.....

2) $\langle r_c^4 \rangle$ and neutron distribution

$$\langle r_c^4 \rangle = \int r^4 \rho_c(r) d^3r$$

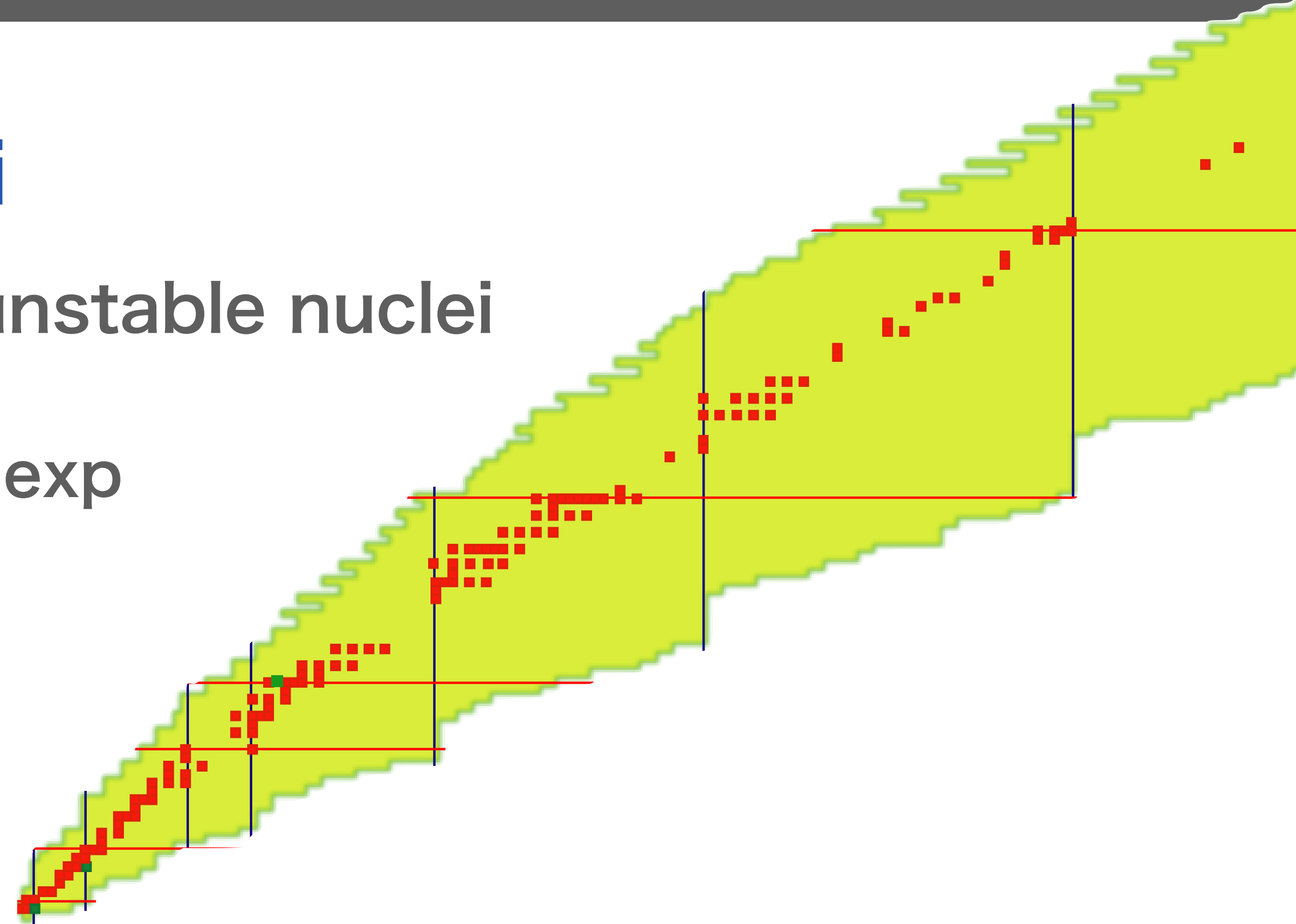
1) H. Kurasawa and T. Suzuki, Prog. Theor. Exp. Phys. 2019, 113D01

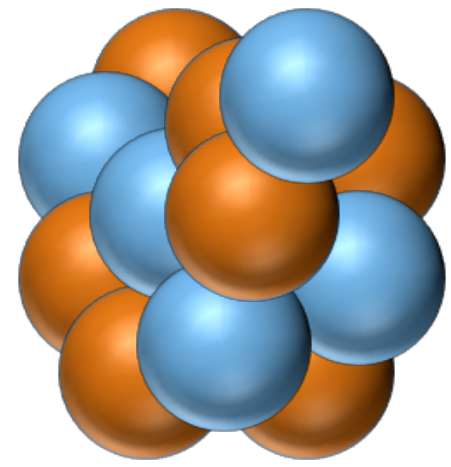
2) H. Kurasawa, T. S. and T. Suzuki, Prog. Theor. Exp. Phys. 2021, 013D02

3) H. Kurasawa and T. Suzuki, Prog. Theor. Exp. Phys. 2022, 023D03

4) T. Suzuki, Prog. Theor. Exp. Phys. 2023, 013D02

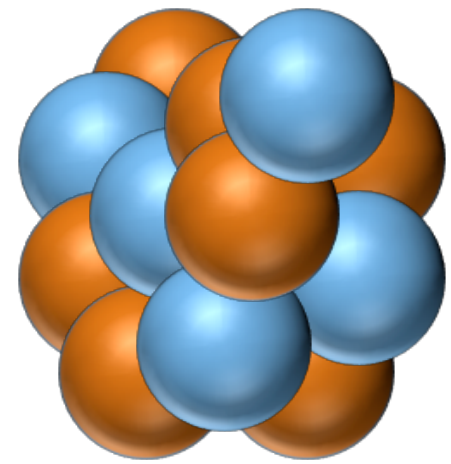
5) T. Suzuki et al., Front. Phys. 13 (2025) 1490337





Proton

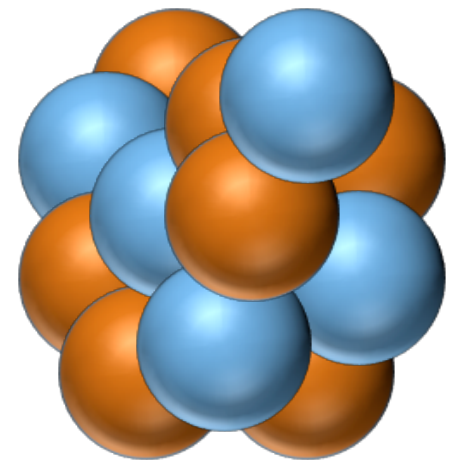
Neutron



Proton

Neutron

$$\rho_c(r) = \rho_c^p(r) + \rho_c^n(r)$$

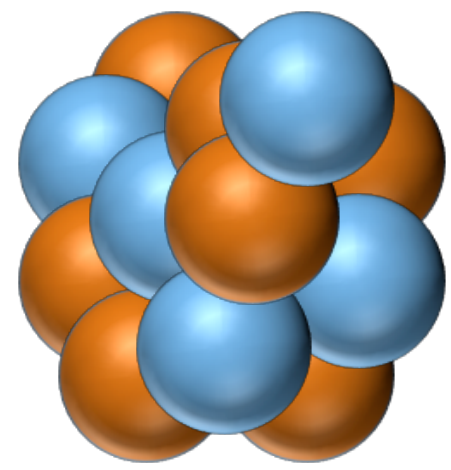


Proton

Neutron

$$\rho_c(r) = \rho_c^p(r) + \rho_c^n(r)$$

$$\rho_c^p(r) = \int \rho_p(r) \rho_{p(point)}(r - r') d^3r'$$
$$\rho_c^n(r) = \int \rho_n(r) \rho_{n(point)}(r - r') d^3r'$$



Proton

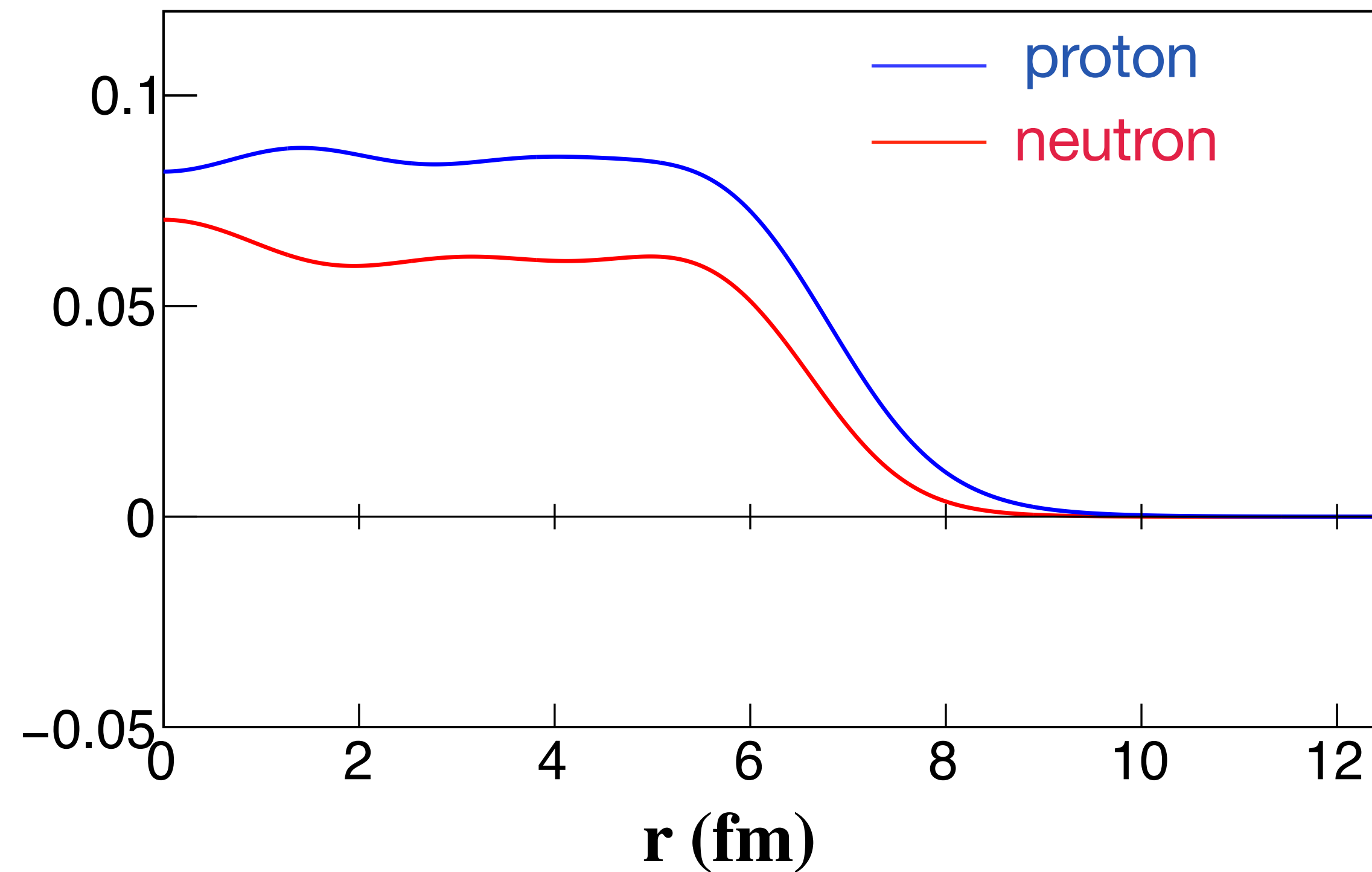
Neutron

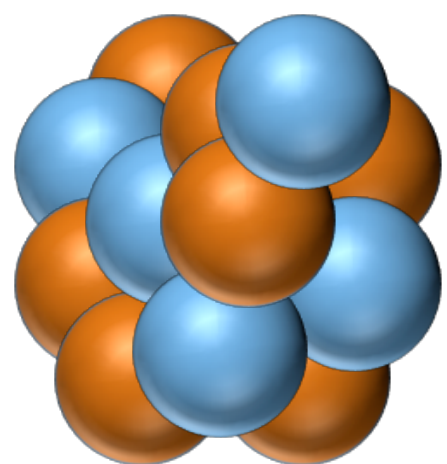
$$\rho_c(r) = \rho_c^p(r) + \rho_c^n(r)$$

$$\rho_c^p(r) = \int \rho_p(r) \rho_{p(point)}(r - r') d^3r'$$
$$\rho_c^n(r) = \int \rho_n(r) \rho_{n(point)}(r - r') d^3r'$$

^{208}Pb

(point) nucleon density





Proton
Neutron

$$\rho_c(r) = \rho_c^p(r) + \rho_c^n(r)$$

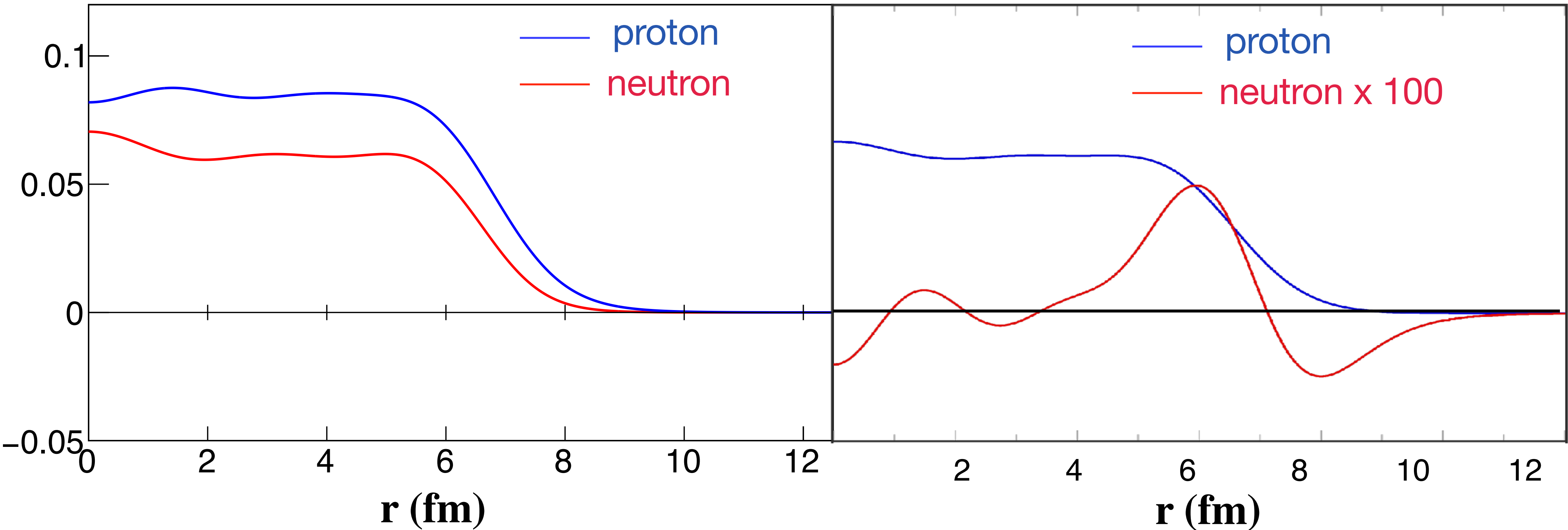
$$\rho_c^p(r) = \int \rho_p(r) \rho_{p(point)}(r - r') d^3r'$$
$$\rho_c^n(r) = \int \rho_n(r) \rho_{n(point)}(r - r') d^3r'$$

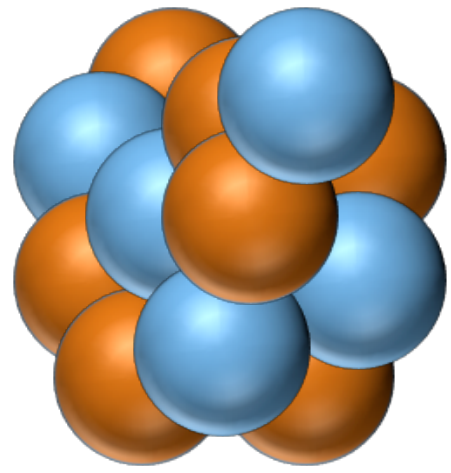
²⁰⁸Pb

(point) nucleon density

charge density distributions

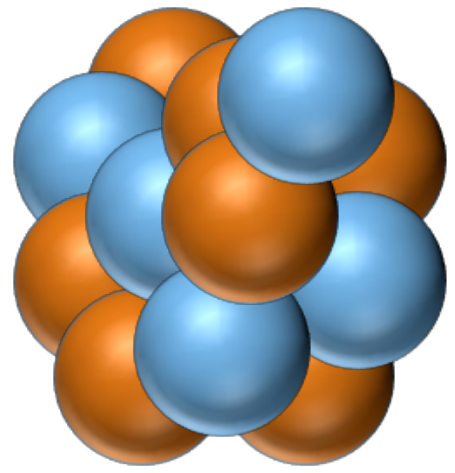
RMF NL3
(H. Kurasawa)





Proton

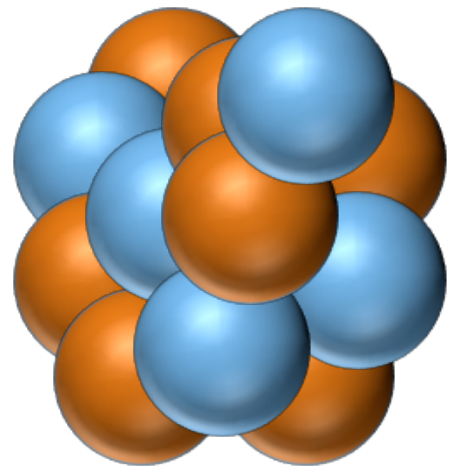
Neutron



Proton

Neutron

$$\langle r_c^2 \rangle = \int r^2 \rho_c(r) d^3r$$

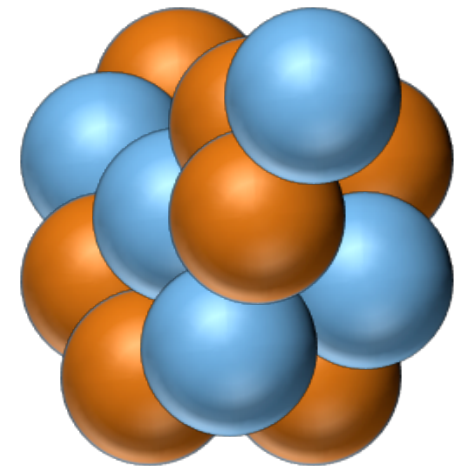


Proton

Neutron

$$\langle r_c^2 \rangle = \int r^2 \rho_c(r) d^3r$$

$$= \langle r_{p(point)}^2 \rangle + \langle r_p^2 \rangle + \langle r_{n(point)}^2 \rangle + \frac{N}{Z} \langle r_n^2 \rangle + \text{rel. corr.}$$

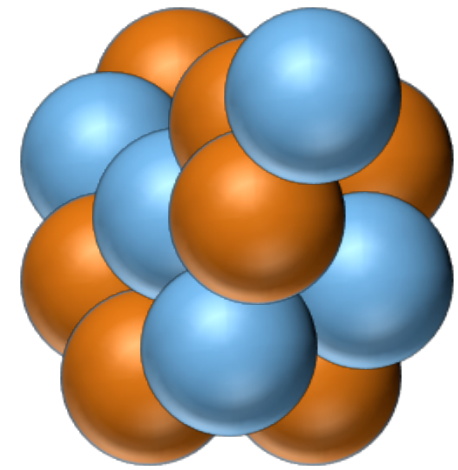


Proton

Neutron

$$\langle r_c^2 \rangle = \int r^2 \rho_c(r) d^3r$$

$$= \langle r_{p(point)}^2 \rangle + \langle r_p^2 \rangle + \overset{e_n = 0}{\cancel{\langle r_{n(point)}^2 \rangle}} + \frac{N}{Z} \langle r_n^2 \rangle + \text{rel. corr.}$$

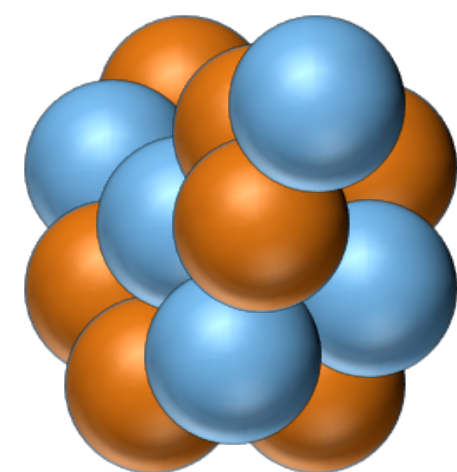


Proton

Neutron

$$\begin{aligned}
 \langle r_c^2 \rangle &= \int r^2 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^2 \rangle + \langle r_p^2 \rangle + \cancel{\langle r_{n(point)}^2 \rangle} + \frac{N}{Z} \langle r_n^2 \rangle + \text{rel. corr.}
 \end{aligned}$$

Proton
 $e_n = 0$
Neutron



Proton

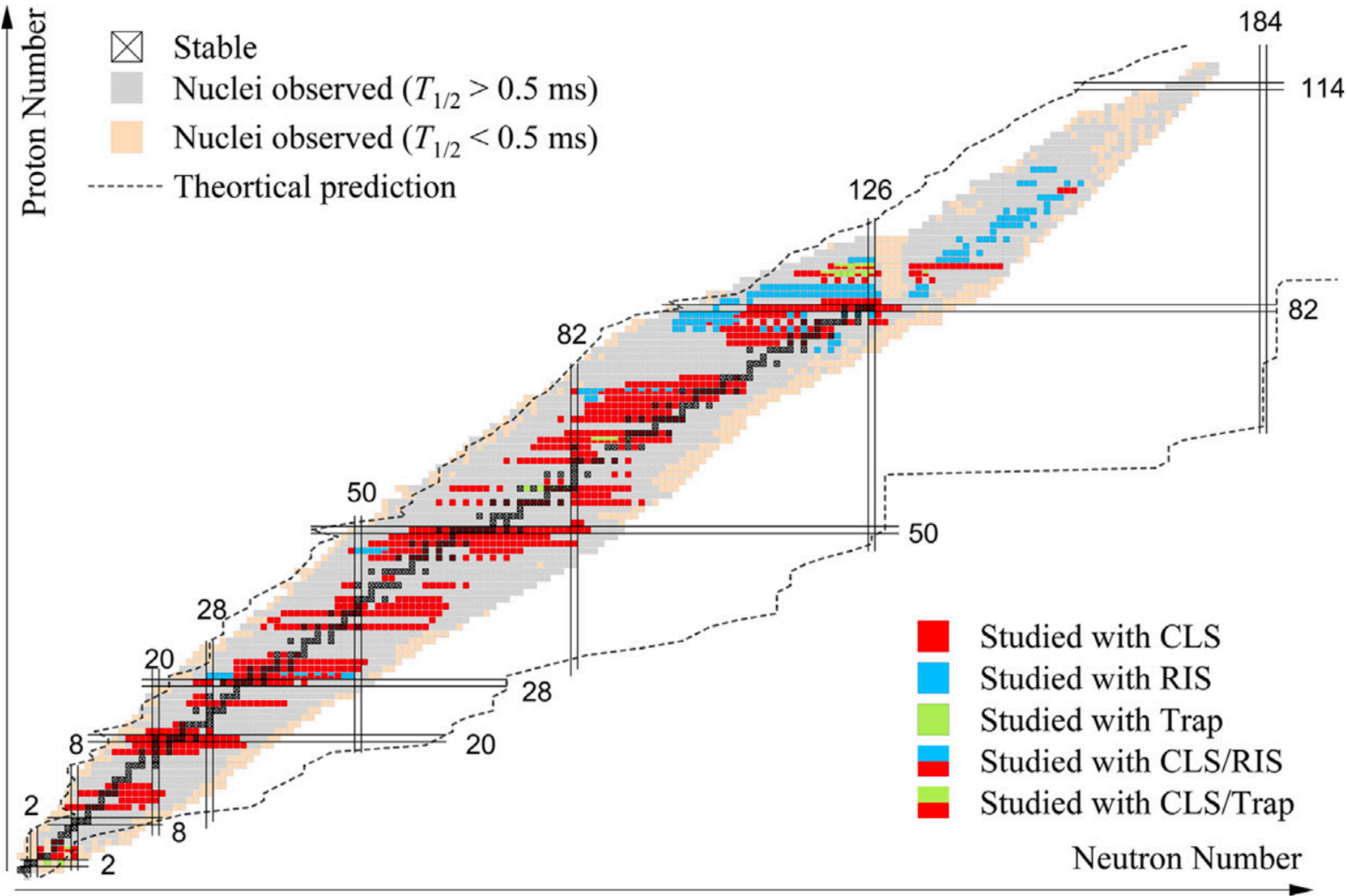
Neutron

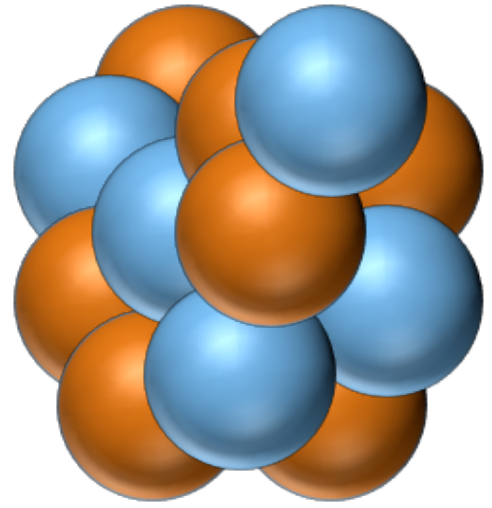
$$\begin{aligned} \langle r_c^2 \rangle &= \int r^2 \rho_c(r) d^3r \\ &= \langle r_{p(point)}^2 \rangle + \langle r_p^2 \rangle + \cancel{\langle r_{n(point)}^2 \rangle} + \frac{N}{Z} \langle r_n^2 \rangle + \text{rel. corr.} \end{aligned}$$

Proton

Neutron

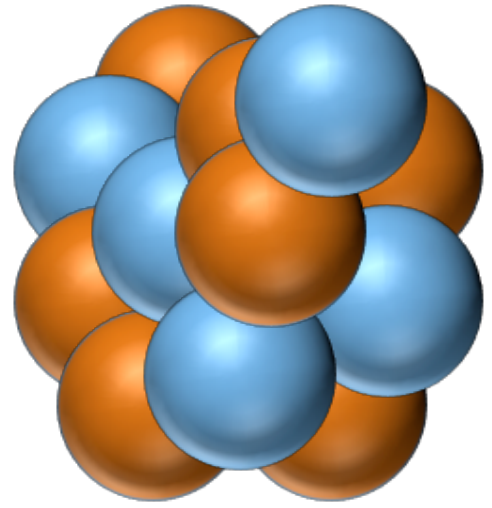
$e_n = 0$





Proton

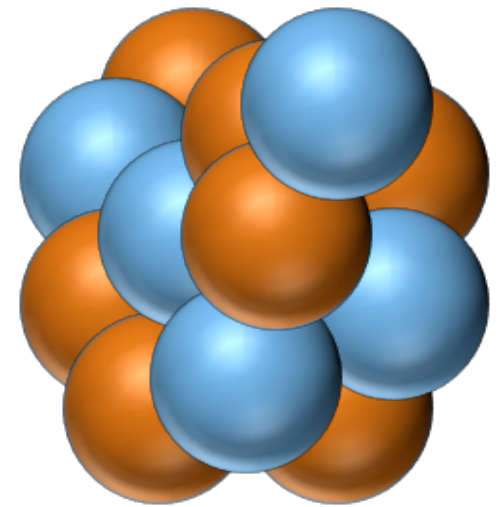
Neutron



Proton

Neutron

$$\langle r_c^4 \rangle = \int r^4 \rho_c(r) d^3r$$

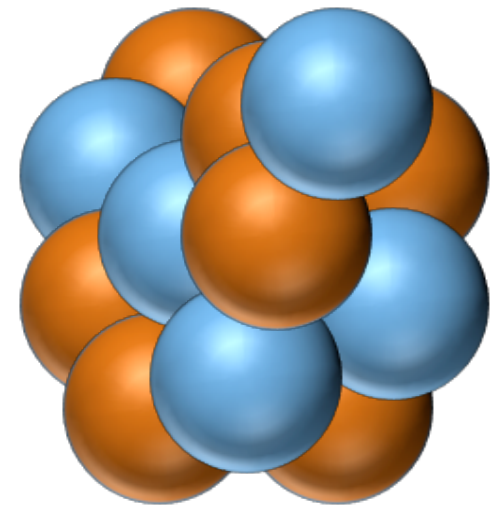


Proton

Neutron

$$\begin{aligned}\langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\ &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\ &\quad + \langle r_{n(point)}^4 \rangle + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}.\end{aligned}$$

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02

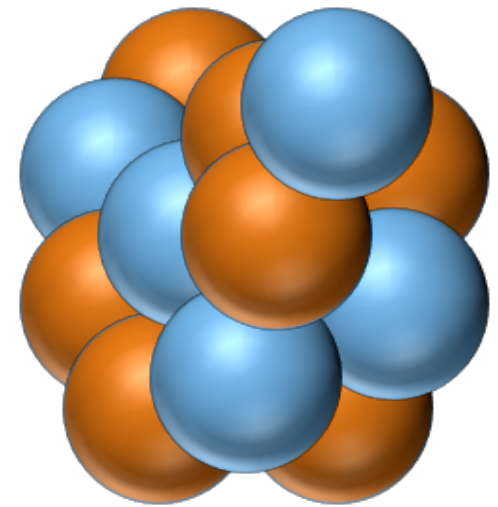


Proton

Neutron

$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 &\quad + \langle r_{n(point)}^4 \rangle + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02

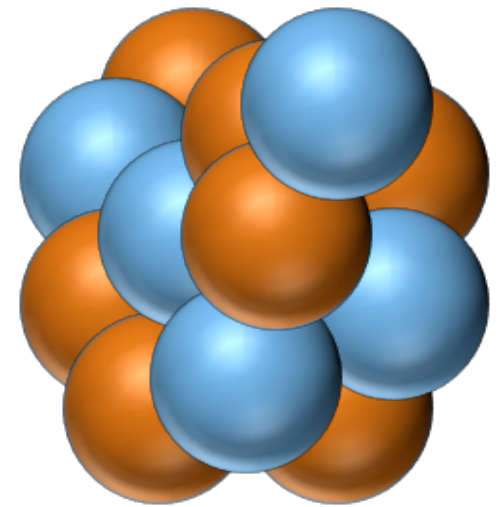


Proton

Neutron

$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 e_n = 0 \quad &+ \cancel{\langle r_{n(point)}^4 \rangle} + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02



Proton

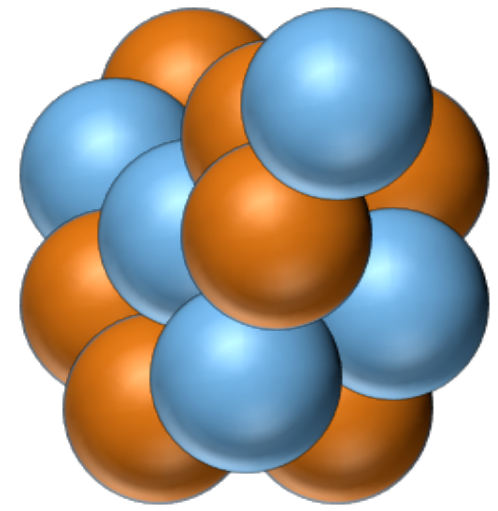
Neutron

$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 &\quad + \cancel{\langle r_{n(point)}^4 \rangle} + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

$e_n = 0$

RMS n-radius

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02



Proton

Neutron

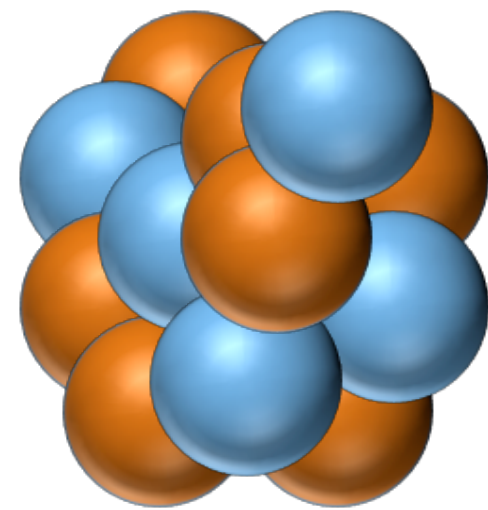
$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 &\quad + \cancel{\langle r_{n(point)}^4 \rangle} + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

e_n = 0

RMS n-radius

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02

$$\langle r_c^4 \rangle = Q_{cp}^4 - Q_{cn}^4$$



Proton

Neutron

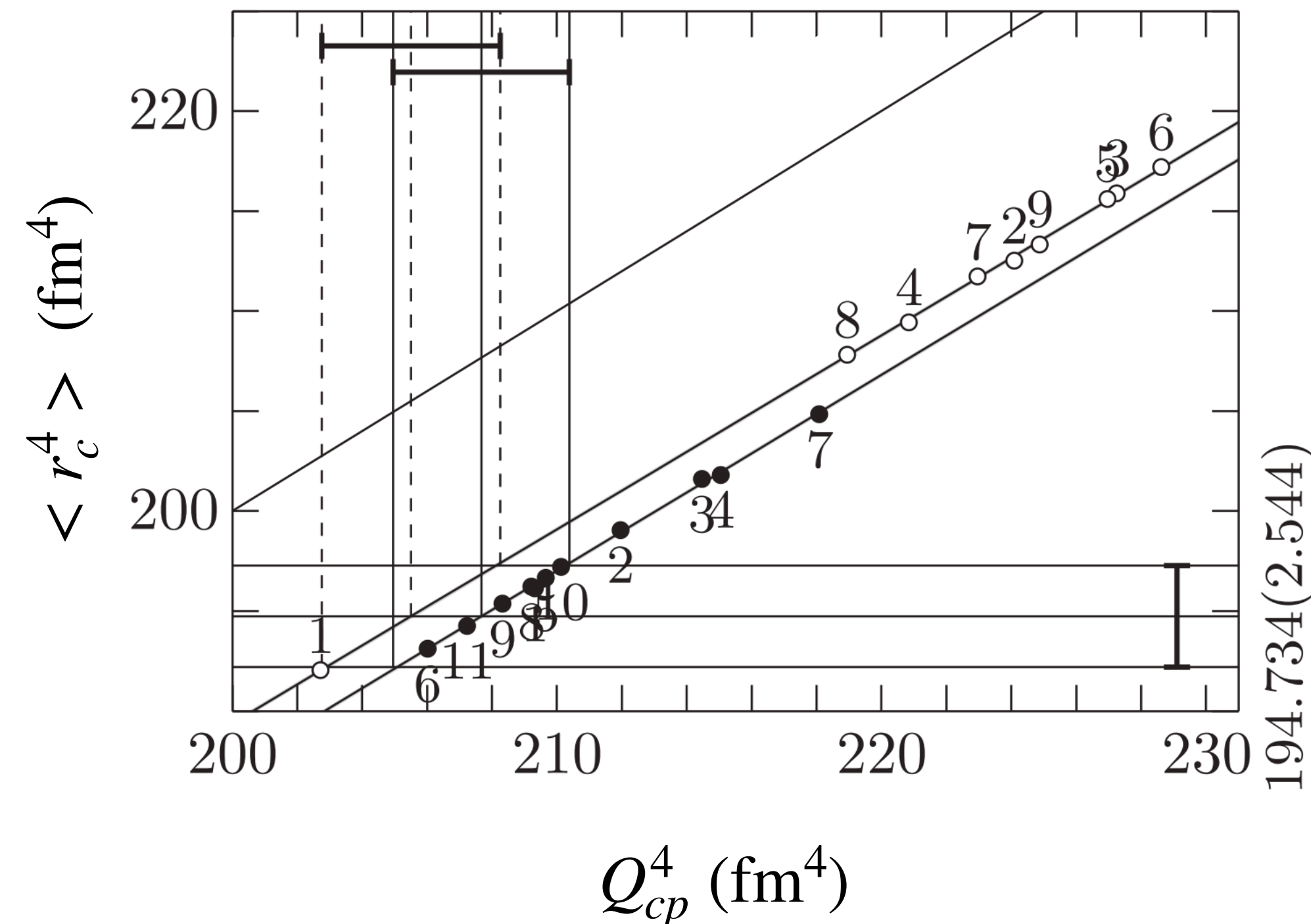
$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 &\quad + \cancel{\langle r_{n(point)}^4 \rangle} + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

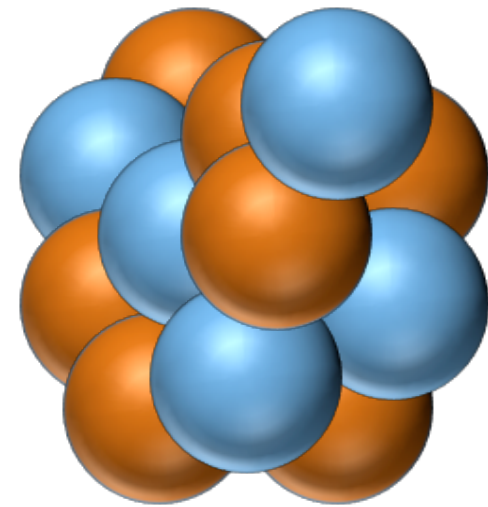
RMS n-radius

$e_n = 0$

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02

$$\langle r_c^4 \rangle = Q_{cp}^4 - Q_{cn}^4$$





Proton

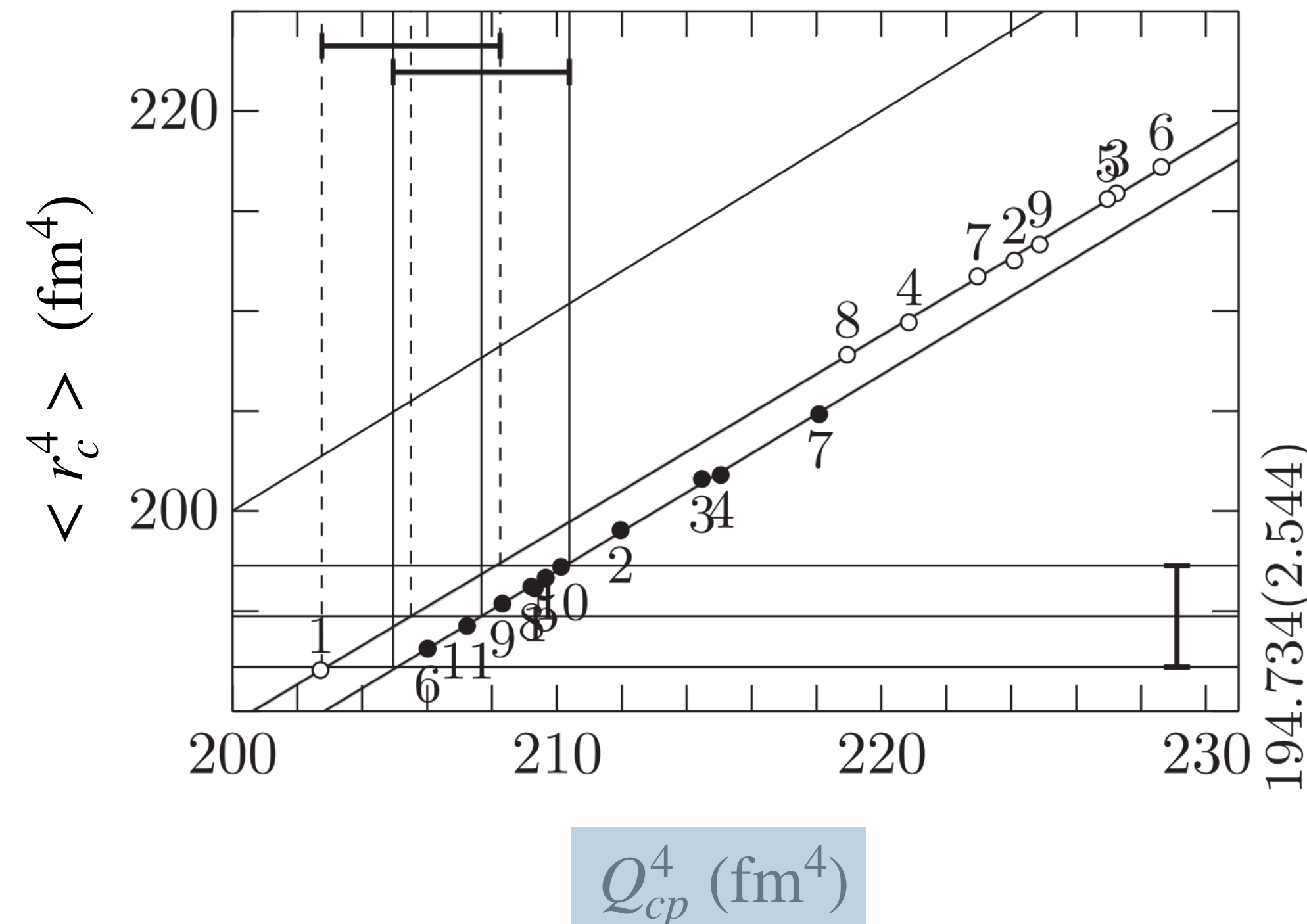
Neutron

$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 &\quad + \cancel{\langle r_{n(point)}^4 \rangle} + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

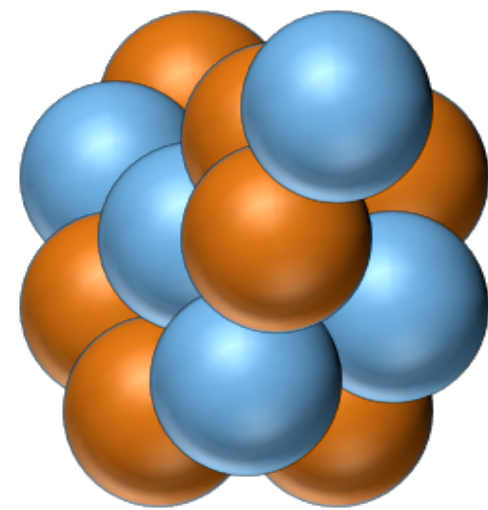
RMS n-radius

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02

$$\langle r_c^4 \rangle = Q_{cp}^4 - Q_{cn}^4$$



- non-rel. MF (SK1, SKI1, SLy4,,,))
- rel. MF (NL2, NL3, NL-SH, FSUGold,,,))



Proton

Neutron

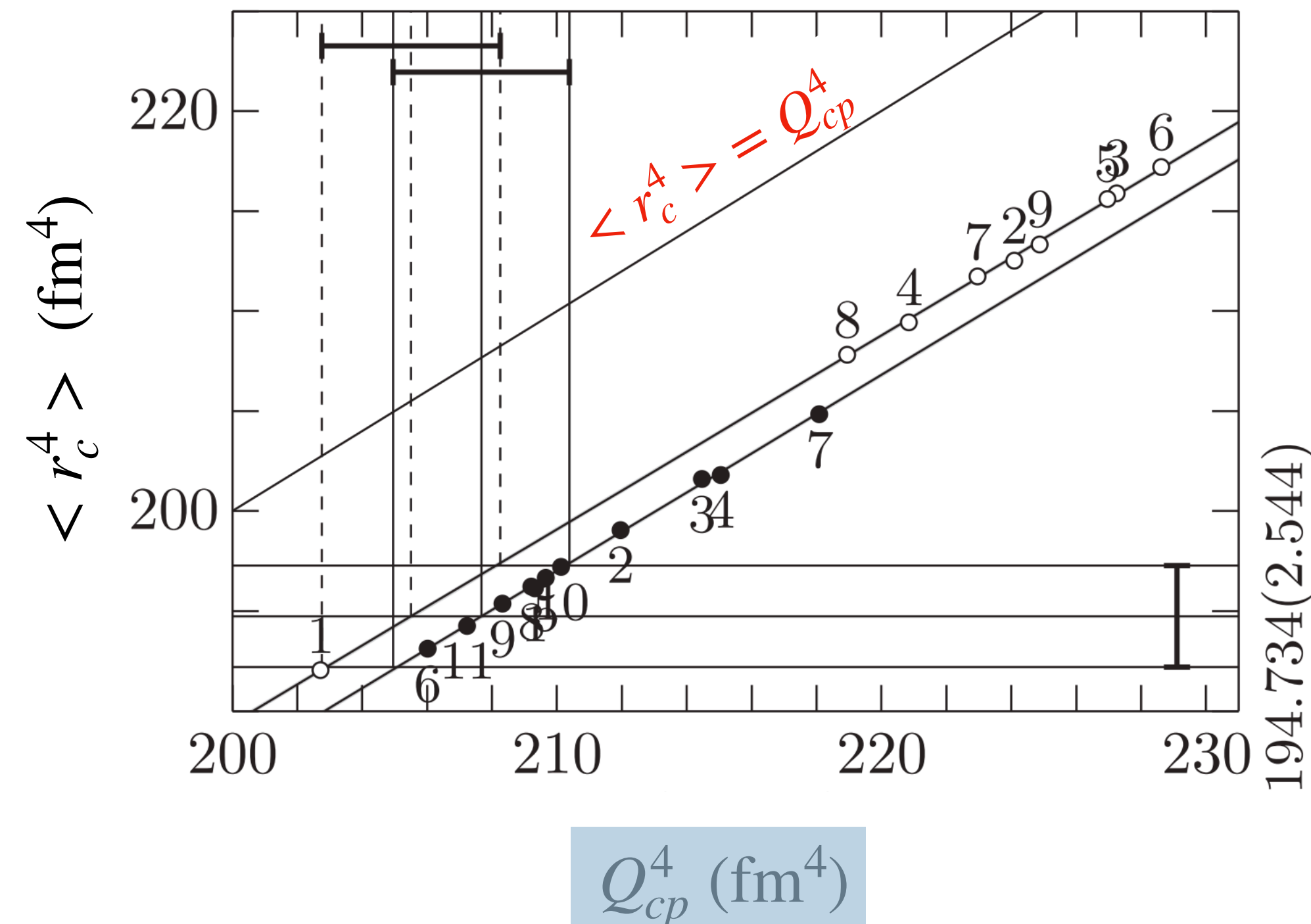
$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 &\quad + \cancel{\langle r_{n(point)}^4 \rangle} + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

RMS n-radius

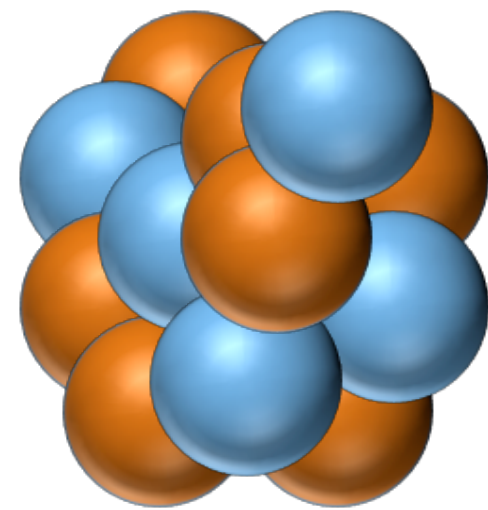
$e_n = 0$

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02

$$\langle r_c^4 \rangle = Q_{cp}^4 - Q_{cn}^4$$



- non-rel. MF (SK1, SKI1, SLy4,,,))
- rel. MF (NL2, NL3, NL-SH, FSUGold,,,))



Proton

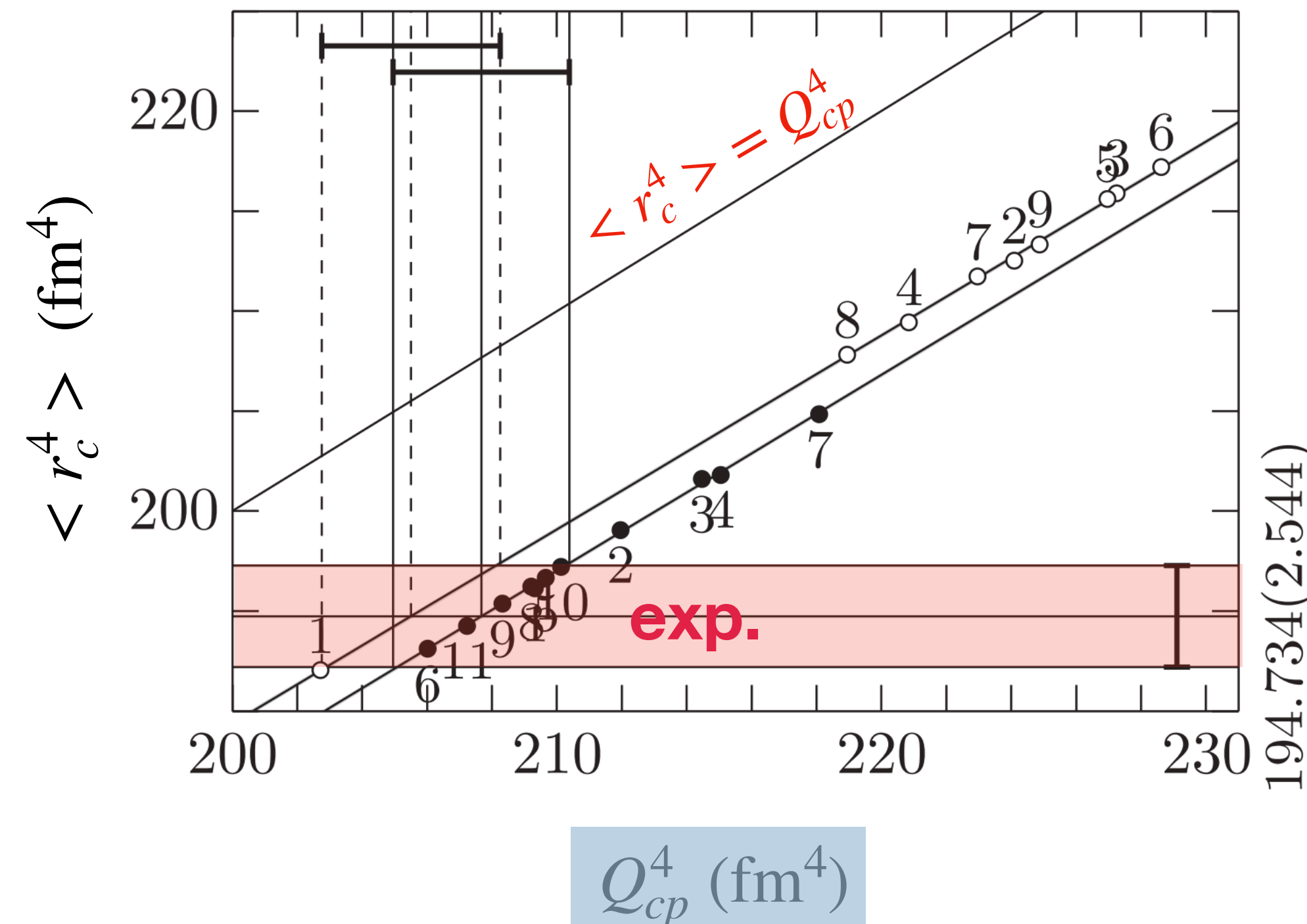
Neutron

$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 &\quad + \cancel{\langle r_{n(point)}^4 \rangle} + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

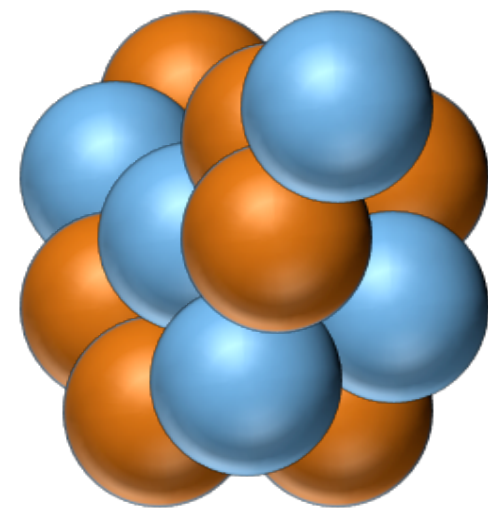
RMS n-radius

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02

$$\langle r_c^4 \rangle = Q_{cp}^4 - Q_{cn}^4$$



- non-rel. MF (SK1, SKI1, SLy4,,,))
- rel. MF (NL2, NL3, NL-SH, FSUGold,,,))



Proton

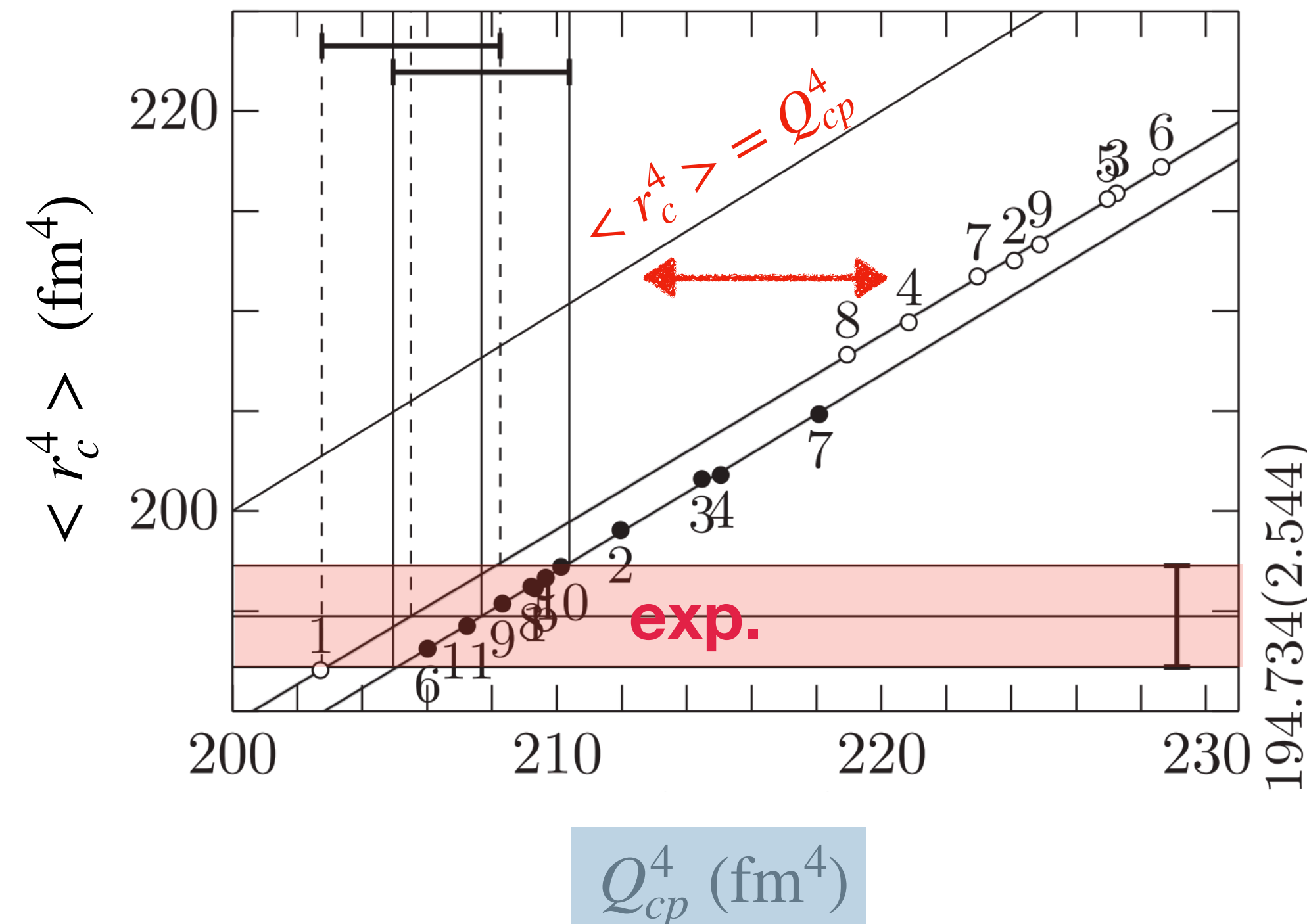
Neutron

$$\begin{aligned}
 \langle r_c^4 \rangle &= \int r^4 \rho_c(r) d^3r \\
 &= \langle r_{p(point)}^4 \rangle + \frac{10}{3} \langle r_{p(point)}^2 \rangle \langle r_p^2 \rangle \\
 &\quad + \cancel{\langle r_{n(point)}^4 \rangle} + \frac{10}{3} \langle r_{n(point)}^2 \rangle \langle r_n^2 \rangle \frac{N}{Z} + \text{rel. corr.}
 \end{aligned}$$

RMS n-radius

H. Kurasawa, T. S. and T. Suzuki,
Prog. Theor. Exp. Phys. 2021, 013D02

$$\langle r_c^4 \rangle = Q_{cp}^4 - Q_{cn}^4$$



There are more than 100 phenomenological models

+ relativistic models

1 L2, 2 NLB, 3 NL1, 4 NL2, 5 NL3,
6 NL-SH, 7 NL-Z, 8 NL-C, 9 NL3II,
10FSUGold.....

**All based on
mean field approximation
accumulated for 50 years !**

Each model has each aim with different parameters .

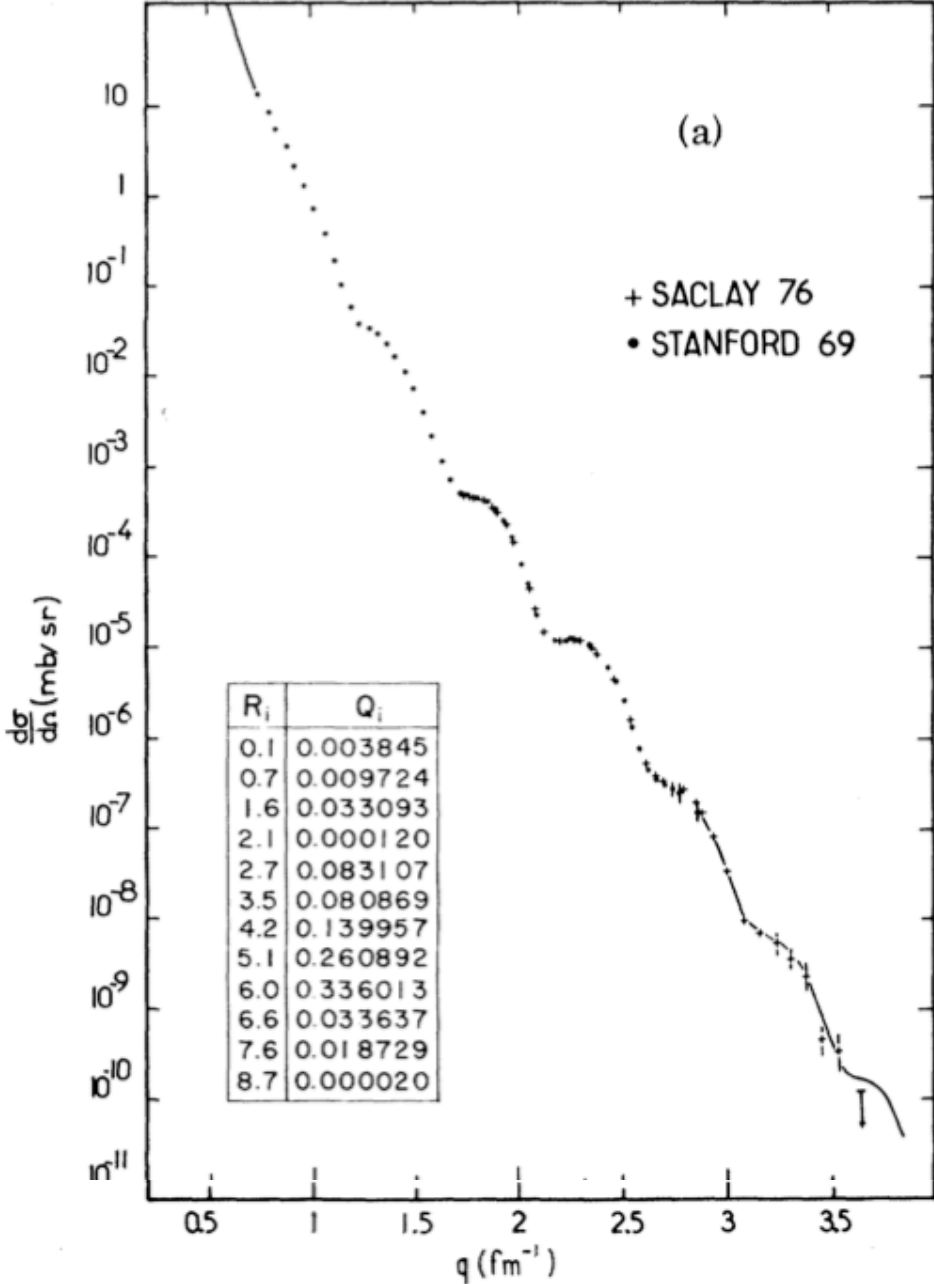
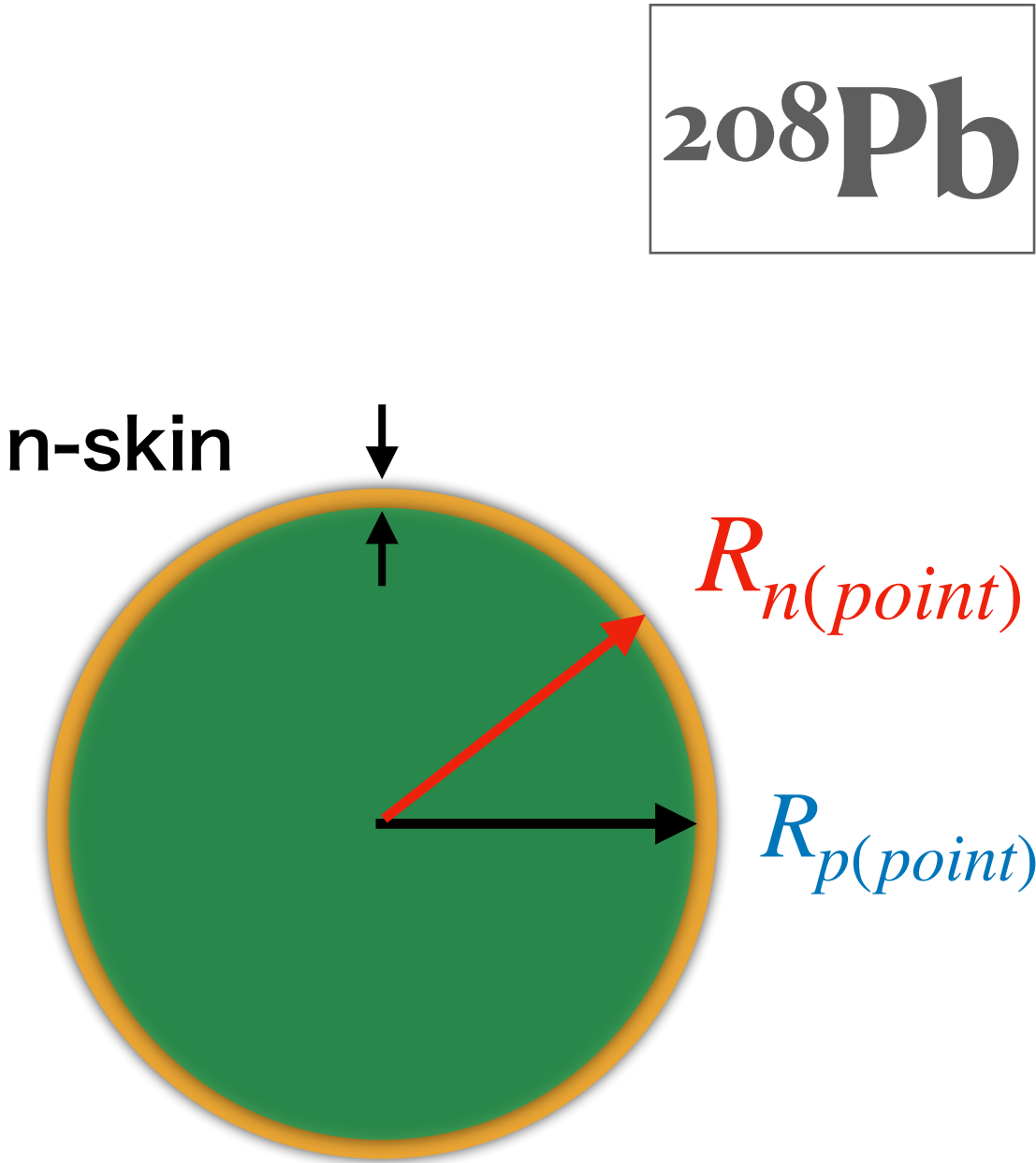
*It is not the best way
to choose
a few models among them.*

STONE, MILLER, KONCEWICZ, STEVENSON, AND STRAYER

PHYSICAL REVIEW C **68**, 034324 (2003)

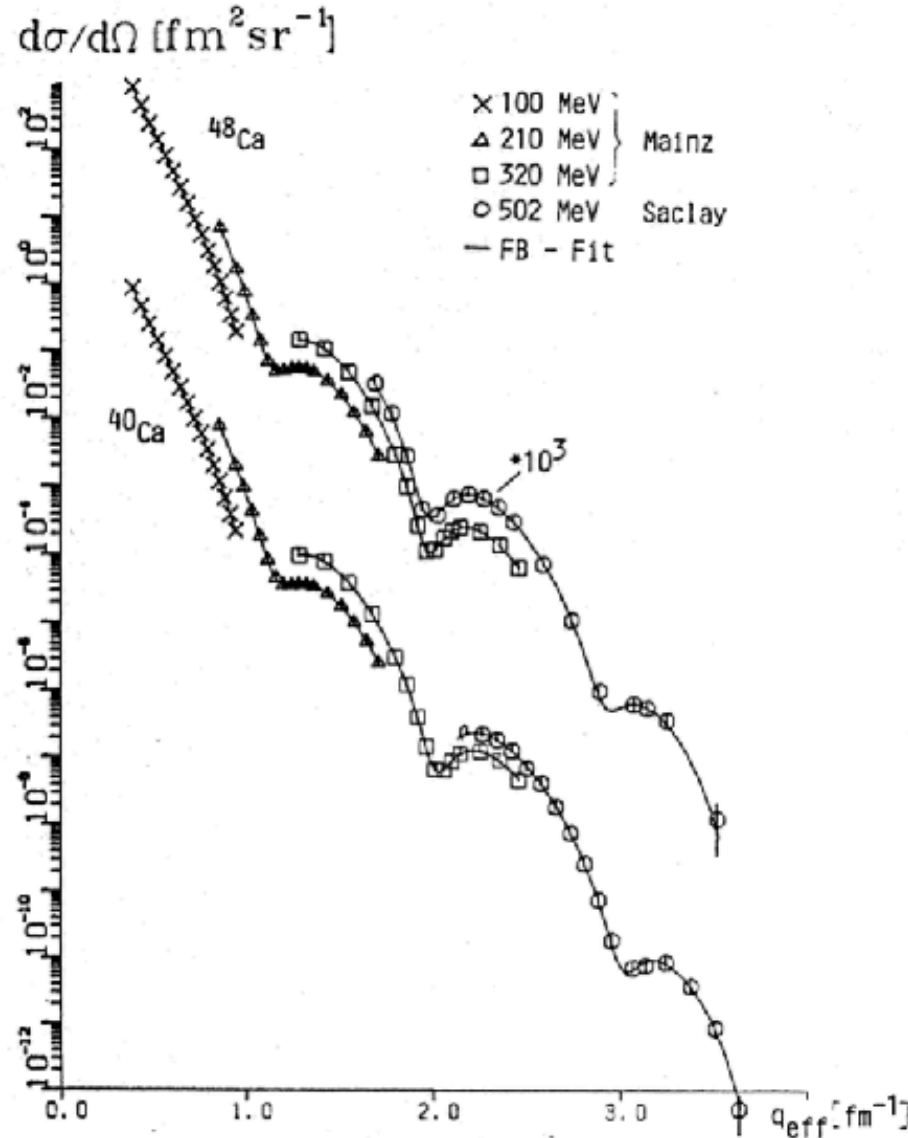
TABLE I. Properties of symmetric nuclear matter at nuclear saturation density n_0 (fm^{-3}) as predicted by different types of Skyrme interaction: Fermi momentum k_F (fm^{-1}), mean distance between adjacent nucleons $r_0 = (9\pi)^{1/3}/2k_F$ (fm), total binding energy per particle $\mathcal{E}$ (MeV), incompressibility modulus K_∞ (MeV), asymmetry coefficient a_s (MeV), speed of sound v_s/c , and the isoscalar effective mass $m_{eff} = m_s^*/m$.

Skyrme	n_0	k_F	r_0	$\mathcal{E}$	a_1	K_∞	v_s	m_{eff}	Skyrme	n_0	k_F	r_0	$\mathcal{E}$	a_1	K_∞	v_s	m_{eff}
SI	0.156	1.320	1.154	-15.99	29.25	372.1	0.212	0.91	SLy0	0.160	1.334	1.142	-15.97	32.03	230.7	0.167	0.70
SII	0.148	1.300	1.172	-15.96	34.15	341.6	0.203	0.58	SLy1	0.161	1.334	1.141	-15.98	32.04	230.8	0.167	0.70
SkT	0.148	1.298	1.174	-15.40	24.90	334.0	0.200	0.60	SLy2	0.161	1.335	1.141	-15.99	32.05	230.9	0.167	0.70
SIII	0.145	1.291	1.180	-15.85	28.17	355.9	0.207	0.76	SLy3	0.161	1.335	1.141	-15.97	32.03	230.9	0.167	0.70
SIV	0.151	1.308	1.165	-15.96	31.24	325.4	0.198	0.47	SLy4	0.160	1.332	1.143	-15.97	32.04	230.9	0.167	0.69
SV	0.155	1.320	1.154	-16.05	32.86	306.8	0.192	0.38	SLy5	0.161	1.335	1.141	-15.98	32.05	230.9	0.167	0.70
SVI	0.144	1.286	1.185	-15.75	26.89	364.0	0.209	0.95	SLy6	0.159	1.331	1.145	-15.92	32.00	230.8	0.167	0.69
SVII	0.143	1.285	1.185	-15.79	26.96	366.9	0.210	1.00	SLy7	0.159	1.329	1.146	-15.90	32.03	230.6	0.167	0.69
SIII*	0.151	1.307	1.165	-16.57	32.67	372.9	0.212	0.79	SLy8	0.161	1.334	1.141	-15.98	32.04	230.9	0.167	0.70
SkM	0.160	1.334	1.142	-15.77	30.77	217.5	0.162	0.79	SLy9	0.151	1.308	1.164	-15.79	32.02	230.3	0.166	0.67
SGI	0.155	1.318	1.156	-15.89	28.35	262.6	0.178	0.61	SLy10	0.156	1.321	1.153	-15.90	32.02	230.4	0.167	0.68
SGII	0.159	1.329	1.146	-15.59	26.85	215.4	0.161	0.79	SkM1	0.160	1.334	1.142	-15.77	25.19	217.5	0.162	0.79
SkM*	0.160	1.334	1.142	-15.77	30.06	217.5	0.162	0.79	Skyrme1'	0.156	1.320	1.154	-15.99	29.37	372.1	0.211	0.91
RATP	0.160	1.333	1.143	-16.05	29.28	240.6	0.170	0.67	SkI6	0.159	1.331	1.144	-15.92	30.13	249.7	0.173	0.64
SkT1	0.161	1.336	1.140	-15.98	32.05	237.2	0.169	1.00	SkXce	0.155	1.322	1.154	-15.86	30.16	269.1	0.180	1.01
SkT2	0.161	1.336	1.140	-15.94	32.03	236.8	0.169	1.00	SkXm	0.159	1.333	1.145	-16.04	31.22	239.1	0.170	0.97
SkT3	0.161	1.336	1.140	-15.94	31.53	236.8	0.169	1.00	SkX	0.156	1.321	1.153	-16.05	31.11	272.0	0.181	0.99
SkT4	0.159	1.331	1.145	-15.95	35.49	236.5	0.169	1.00	MSk1	0.158	1.326	1.148	-15.83	30.02	234.6	0.168	1.00
SkT5	0.164	1.345	1.133	-16.00	37.05	202.7	0.156	1.00	MSk2	0.158	1.326	1.148	-15.83	30.02	232.5	0.167	1.05
SkT6	0.161	1.336	1.140	-15.96	29.99	237.0	0.169	1.00	MSk3	0.158	1.327	1.148	-15.82	28.00	234.4	0.168	1.00
SkT7	0.161	1.335	1.141	-15.94	29.54	236.7	0.169	0.83	MSk4	0.158	1.326	1.148	-15.79	28.01	232.0	0.167	1.05
SkT8	0.161	1.335	1.141	-15.94	29.95	236.8	0.169	0.83	MSk5	0.158	1.326	1.148	-15.79	28.01	232.0	0.167	1.05
SkT9	0.161	1.334	1.142	-15.88	29.78	235.9	0.169	0.83	MSk5*	0.156	1.322	1.152	-15.78	28.01	244.6	0.172	0.80
SkP	0.163	1.341	1.136	-15.95	30.02	201.9	0.156	1.00	MSk6	0.158	1.326	1.148	-15.79	28.01	232.0	0.167	1.05
E	0.159	1.331	1.144	-16.12	27.65	335.3	0.201	0.87	MSk7	0.158	1.326	1.148	-15.79	27.96	232.1	0.167	1.05
Es	0.163	1.341	1.136	-16.02	26.44	249.9	0.173	0.84	SKRA	0.160	1.332	1.144	-15.78	31.35	217.9	0.162	0.75
Z	0.159	1.331	1.145	-15.97	26.81	332.1	0.200	0.84	SKO	0.161	1.335	1.141	-15.83	32.01	224.3	0.164	0.90
Zs	0.163	1.342	1.135	-15.88	26.70	234.5	0.168	0.78	SKO'	0.160	1.334	1.142	-15.75	31.98	223.3	0.164	0.90
Zs*	0.163	1.340	1.136	-15.96	28.82	236.0	0.169	0.77	SLy230a	0.160	1.333	1.142	-15.99	32.04	230.9	0.167	0.70
Rs	0.158	1.327	1.148	-15.59	30.61	238.3	0.169	0.78	v110	0.158	1.326	1.148	-15.79	28.01	232.0	0.167	1.05
Gs	0.158	1.327	1.148	-15.59	31.40	238.1	0.169	0.78	v105	0.158	1.326	1.148	-15.79	28.01	232.0	0.167	1.05
SkMP	0.157	1.325	1.149	-15.56	29.91	231.7	0.167	0.65	v100	0.158	1.326	1.148	-15.79	28.01	232.0	0.167	1.05
SkSC1	0.161	1.335	1.141	-15.85	28.00	235.6	0.168	1.00	v090	0.158	1.326	1.148	-15.79	28.01	232.0	0.167	1.05
SkSC2	0.161	1.335	1.141	-15.90	24.75	236.2	0.169	1.00	v080	0.158	1.326	1.148	-15.79	28.01	232.0	0.167	1.05
SkSC3	0.161	1.335	1.141	-15.83	27.02	235.5	0.168	1.00	v075	0.158	1.326	1.148	-15.80	28.01	232.1	0.167	1.05
SkSC4	0.161	1.335	1.141	-15.86	28.82	235.8	0.168	1.00	v070	0.158	1.326	1.148	-15.80	28.00	232.1	0.167	1.05
SkSC5	0.161	1.335	1.141	-15.85	31.00	235.6	0.168	1.00	BSk1	0.157	1.326	1.149	-15.80	27.82	232.1	0.167	1.05
SkSC6	0.161	1.336	1.141	-15.92	24.59	236.5	0.169	1.00	Skz-1	0.160	1.334	1.142	-16.00	32.02	231.1	0.167	0.70
SkSC10	0.161	1.336	1.141	-15.96	22.84	237.0	0.169	1.00	Skz0	0.160	1.334	1.142	-16.00	32.02	231.1	0.167	0.70
SkI1	0.161	1.335	1.141	-15.95	37.59	243.8	0.171	0.69	Skz1	0.160	1.334	1.142	-16.00	32.03	231.1	0.167	0.70
SkI2	0.158	1.327	1.148	-15.77	33.42	241.9	0.171	0.68	Skz2	0.160	1.334	1.142	-16.00	32.04	231.1	0.167	0.70
SkI3	0.158	1.327	1.148	-15.98	34.89	259.2	0.177	0.58	Skz3	0.160	1.334	1.142	-16.01	32.05	231.1	0.167	0.70
SkI4	0.160	1.334	1.142	-15.94	29.54	249.1	0.173	0.65	Skz4	0.160	1.334	1.142	-16.01	32.05	231.1	0.167	0.70
SkI5	0.156	1.322	1.153	-15.85	36.69	256.7	0.176	0.58									

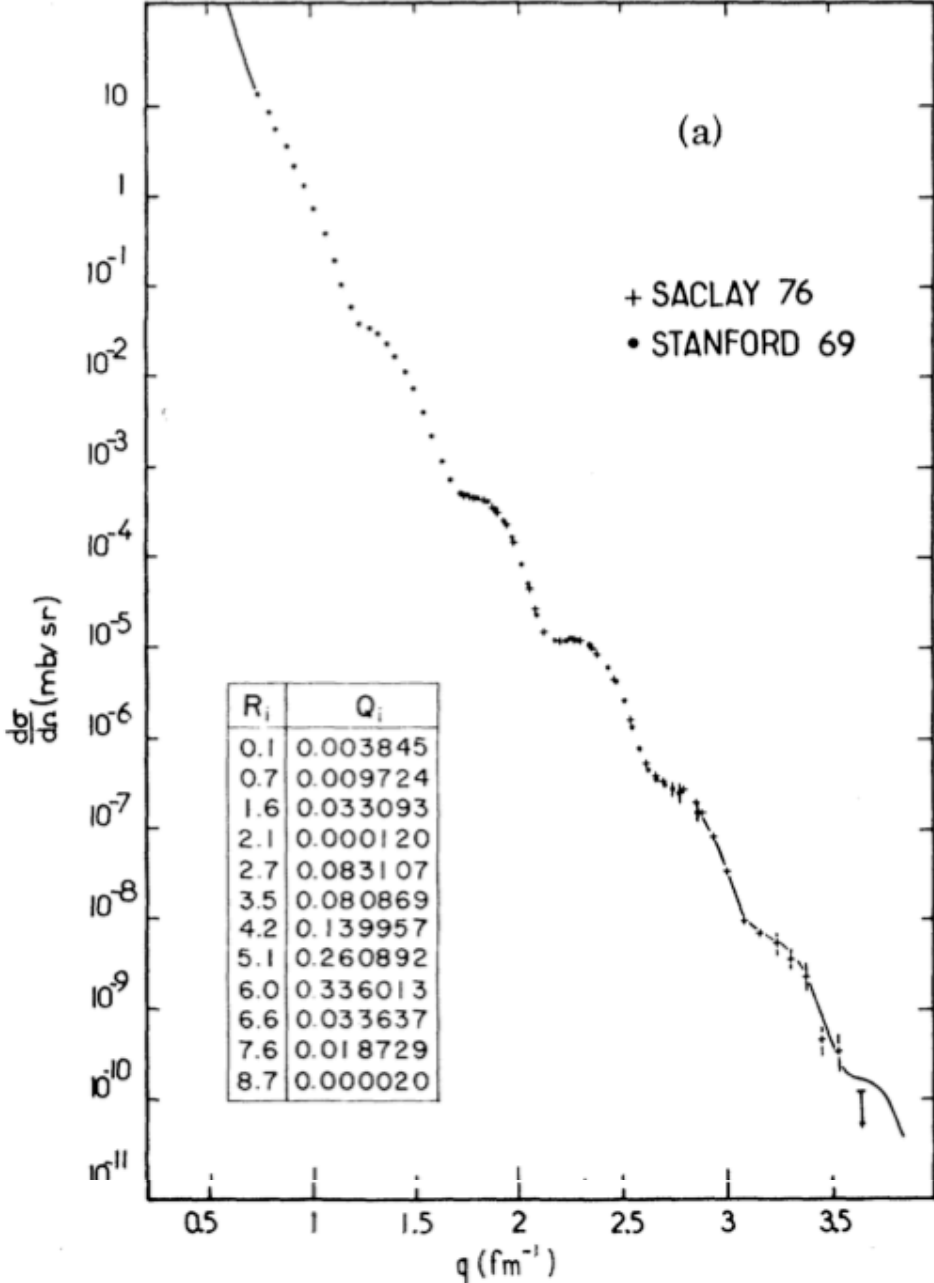
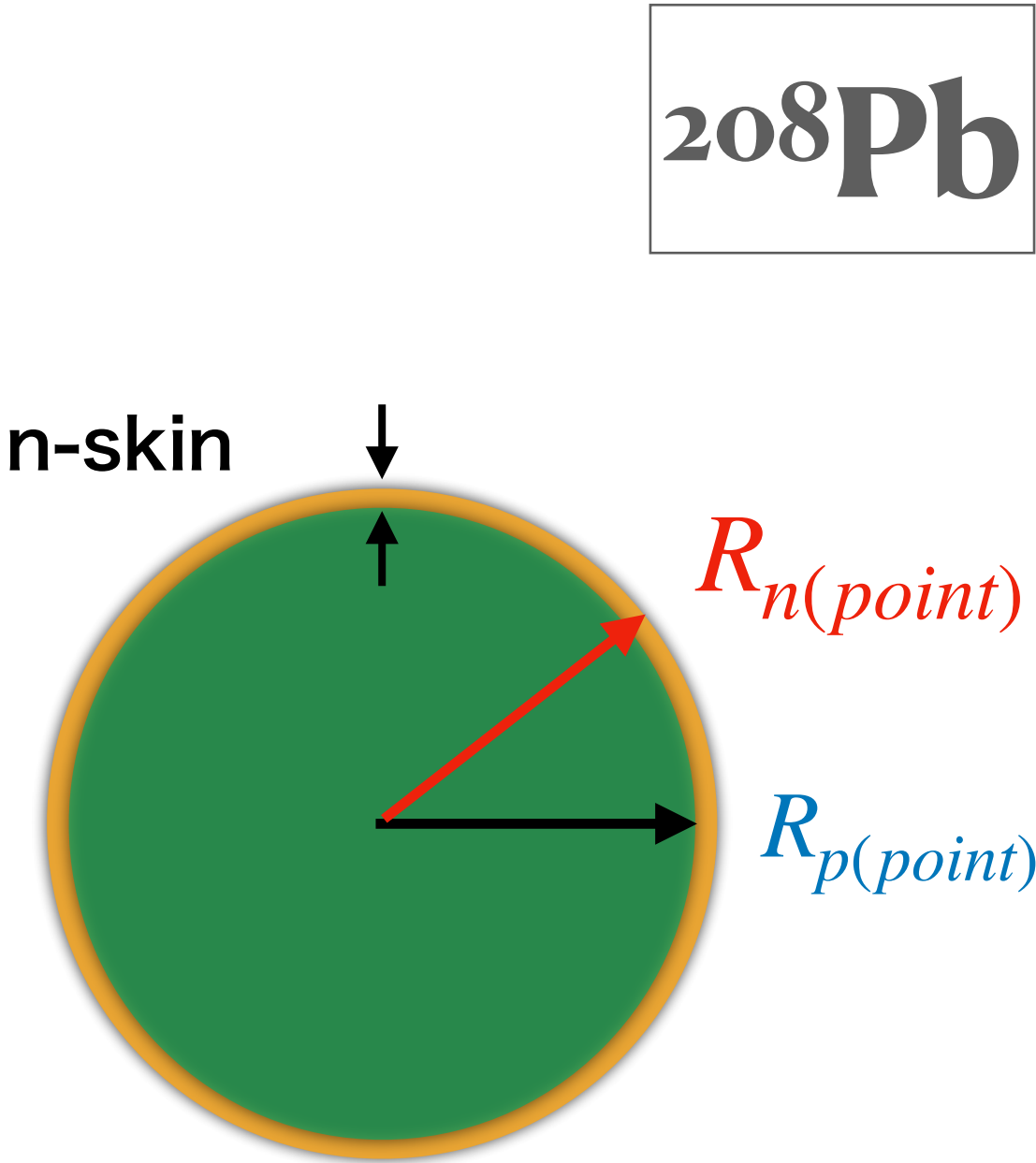


		R_p	R_n	δR
^{208}Pb	Rel.	5.454(0.013)	5.728(0.057)	0.275(0.070)
	Non.	5.447(0.014)	5.609(0.054)	0.162(0.068)
	Exp.	$R_c = 5.503(0.014)$		

48Ca



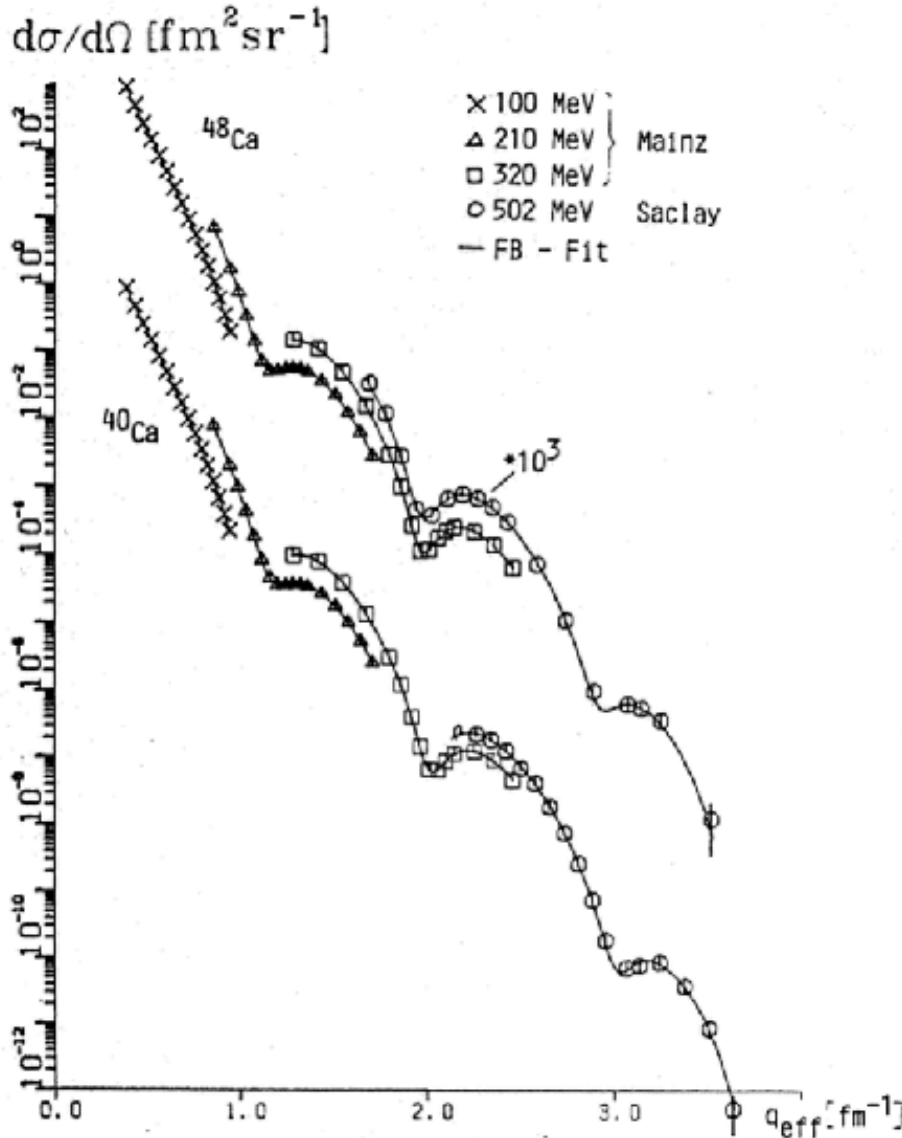
		R_p	R_n	δR
^{48}Ca	Rel.	3.378(0.005)	3.597(0.021)	0.220(0.026)
	Non.	3.372(0.009)	3.492(0.028)	0.121(0.036)
	Exp.	$R_c = 3.451(0.009)$		



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^{208}Pb	Rel.	5.454(0.013)	5.728(0.057)	0.275(0.070)
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JLab : PREX I,II (parity-violating e-scattering)
 $\Delta r_{np} \equiv R_n - R_p = \underline{0.283 \pm 0.071 \text{ fm}}$
PRL 126, 172502 (2021)

48Ca



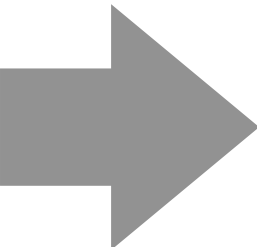
		R_p	R_n	δR
^{48}Ca	Rel.	3.378(0.005)	3.597(0.021)	0.220(0.026)
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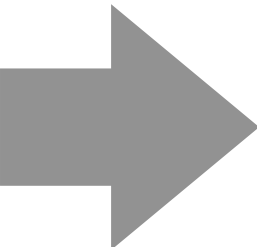
JLab : CREX (parity-violating e-scattering)
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$$\langle r_c^4 \rangle = \int r^4 \rho_c(r) d^3r$$

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$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} |F_c(q)|^2$$


$$\rho_c(r) = \int F_c(q) e^{-iqr} d^3q$$

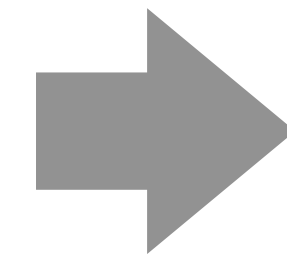
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1) elastic scattering covering upto very high q

ways to access the fourth moment, $\langle r_c^4 \rangle$

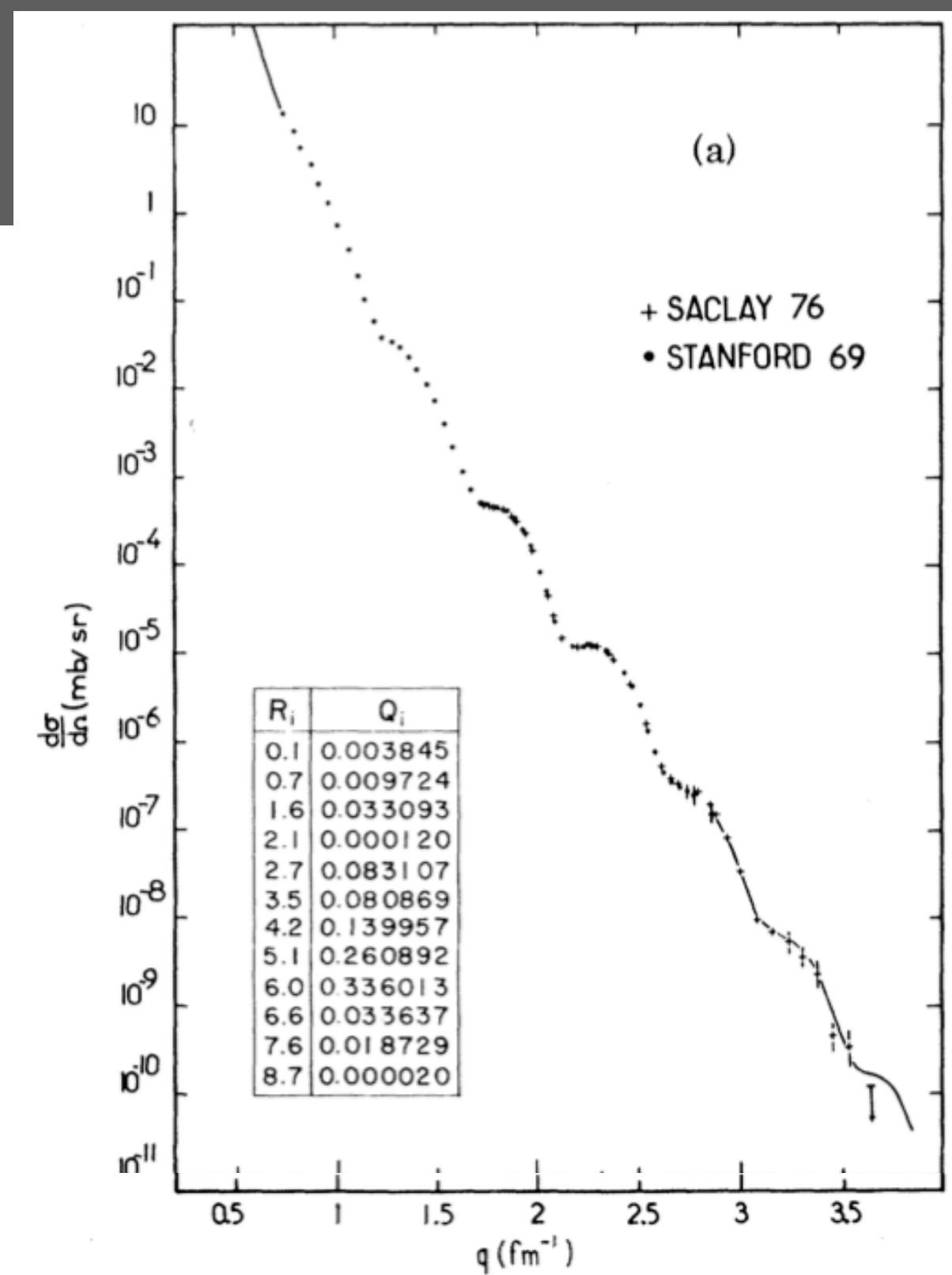
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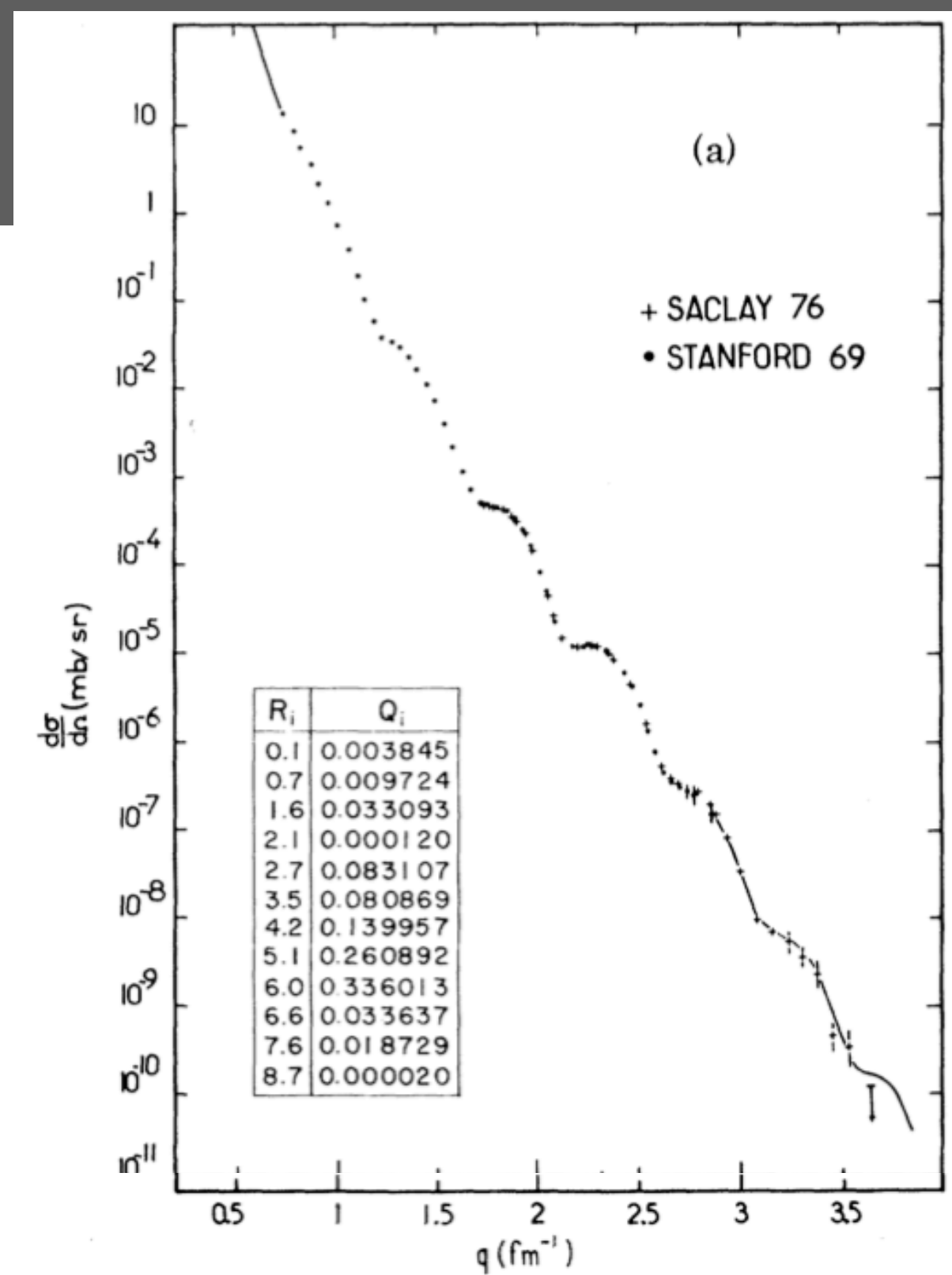
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very high L required

$\Rightarrow$ no chance for low- L e-scattering for exotics



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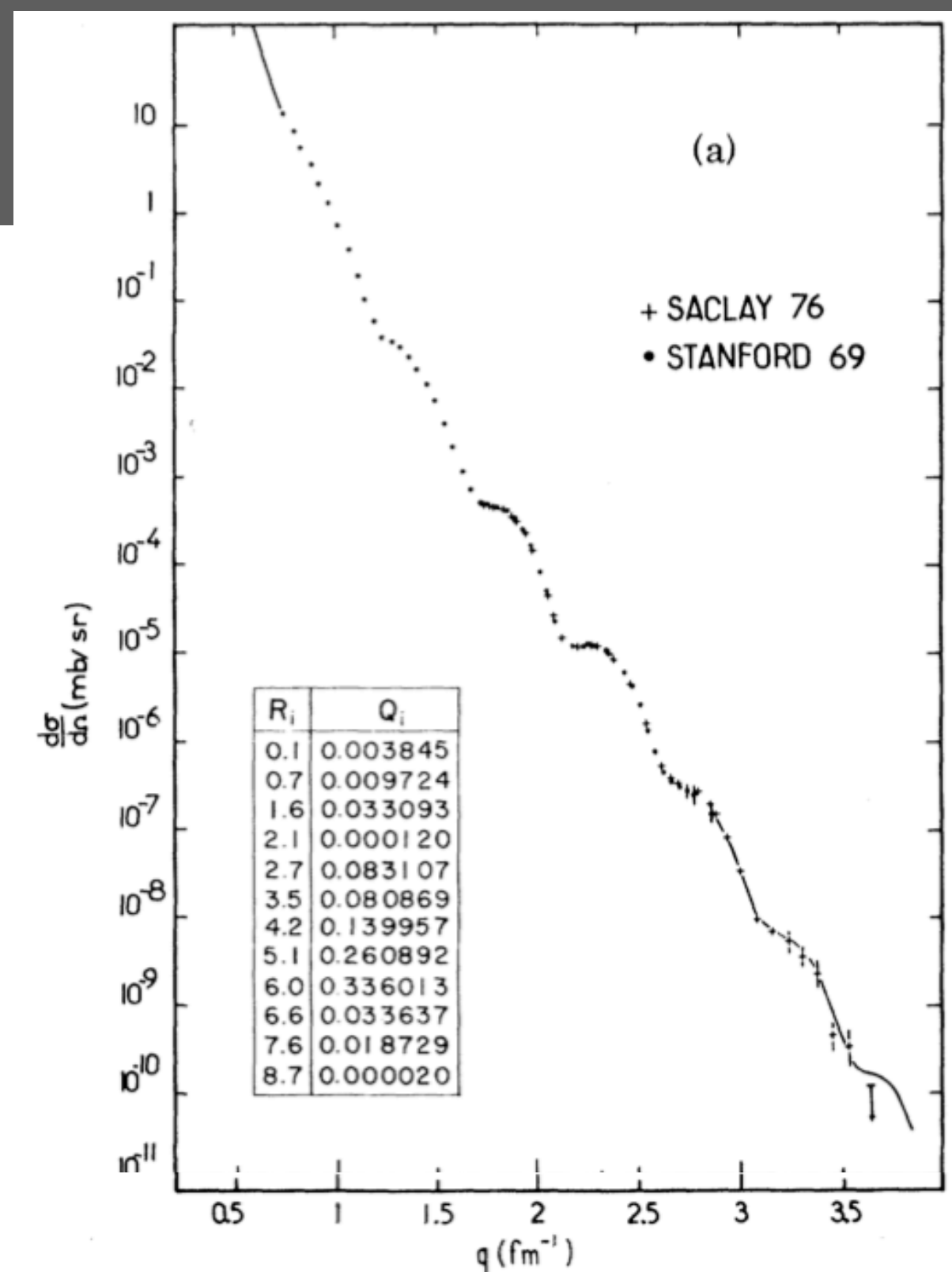
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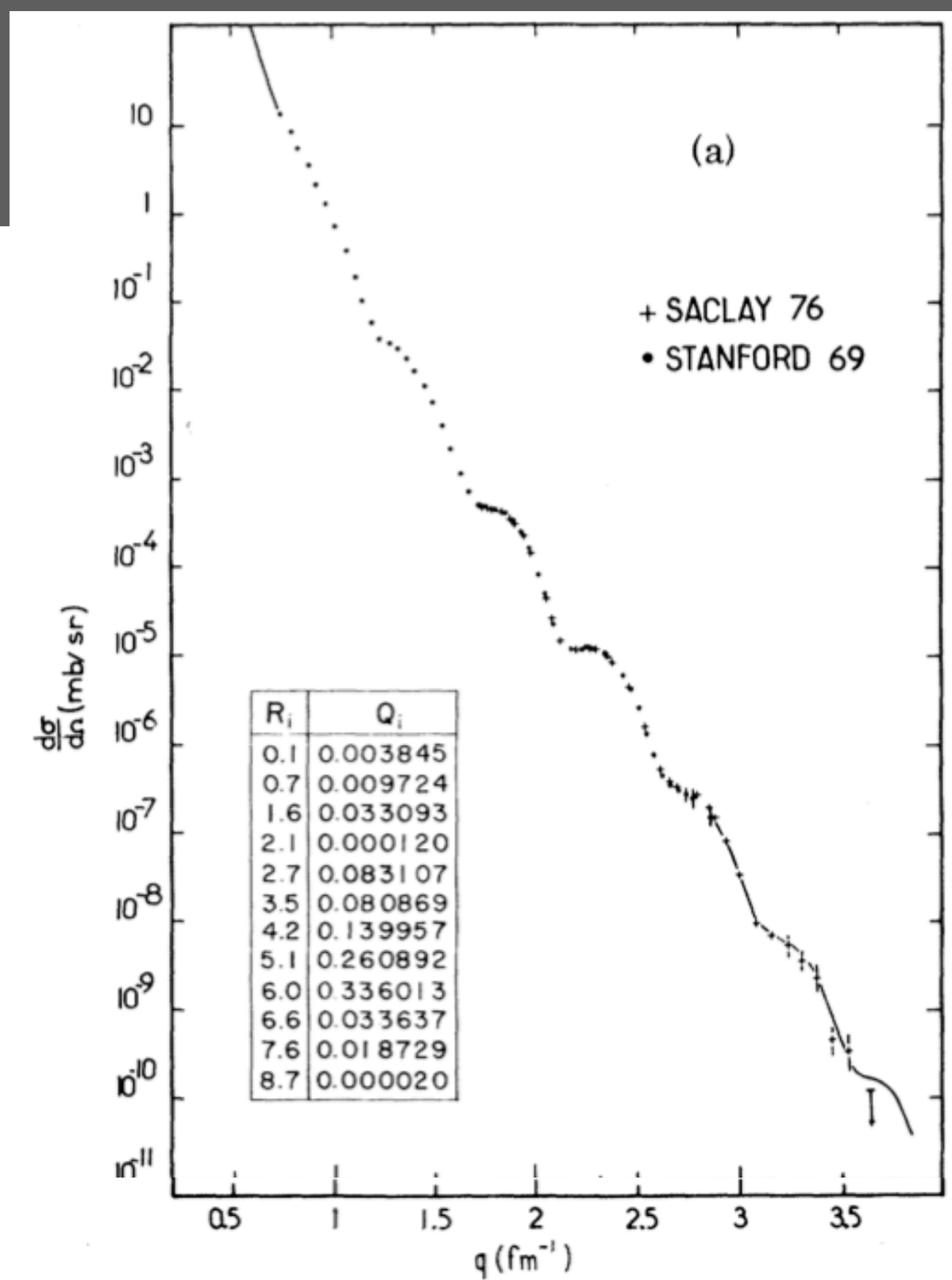
1) elastic scattering covering upto very high q

very high L required

=> no chance for low- L e-scattering for exotics

2) elastic scattering at very low q

$$F_c(q) \sim 1 - \frac{\langle r_c^2 \rangle}{6} q^2 + \frac{\langle r_c^4 \rangle}{120} q^4 + \dots$$



ways to access the fourth moment, $\langle r_c^4 \rangle$

$$\langle r_c^4 \rangle = \int r^4 \rho_c(r) d^3r$$

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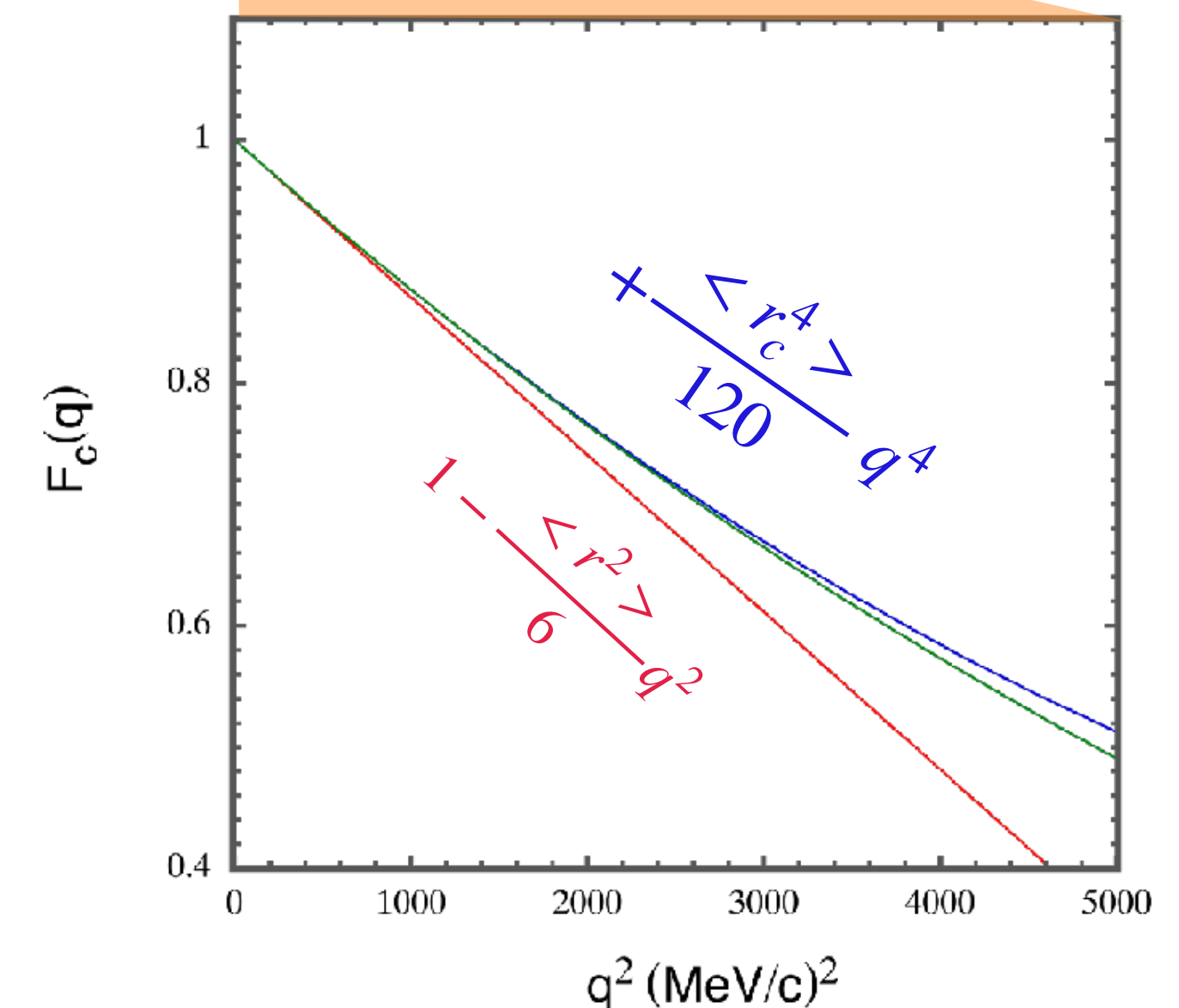
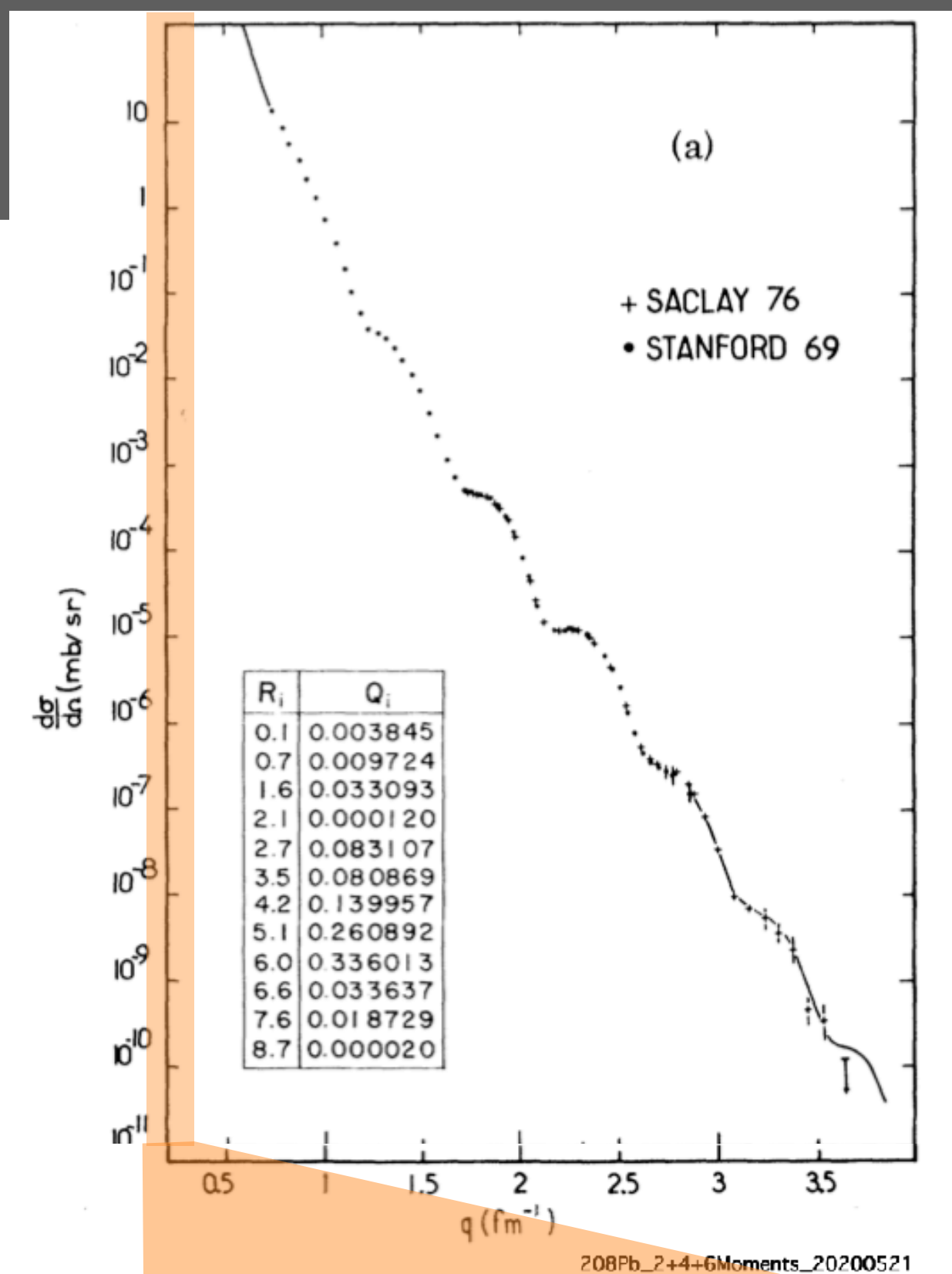
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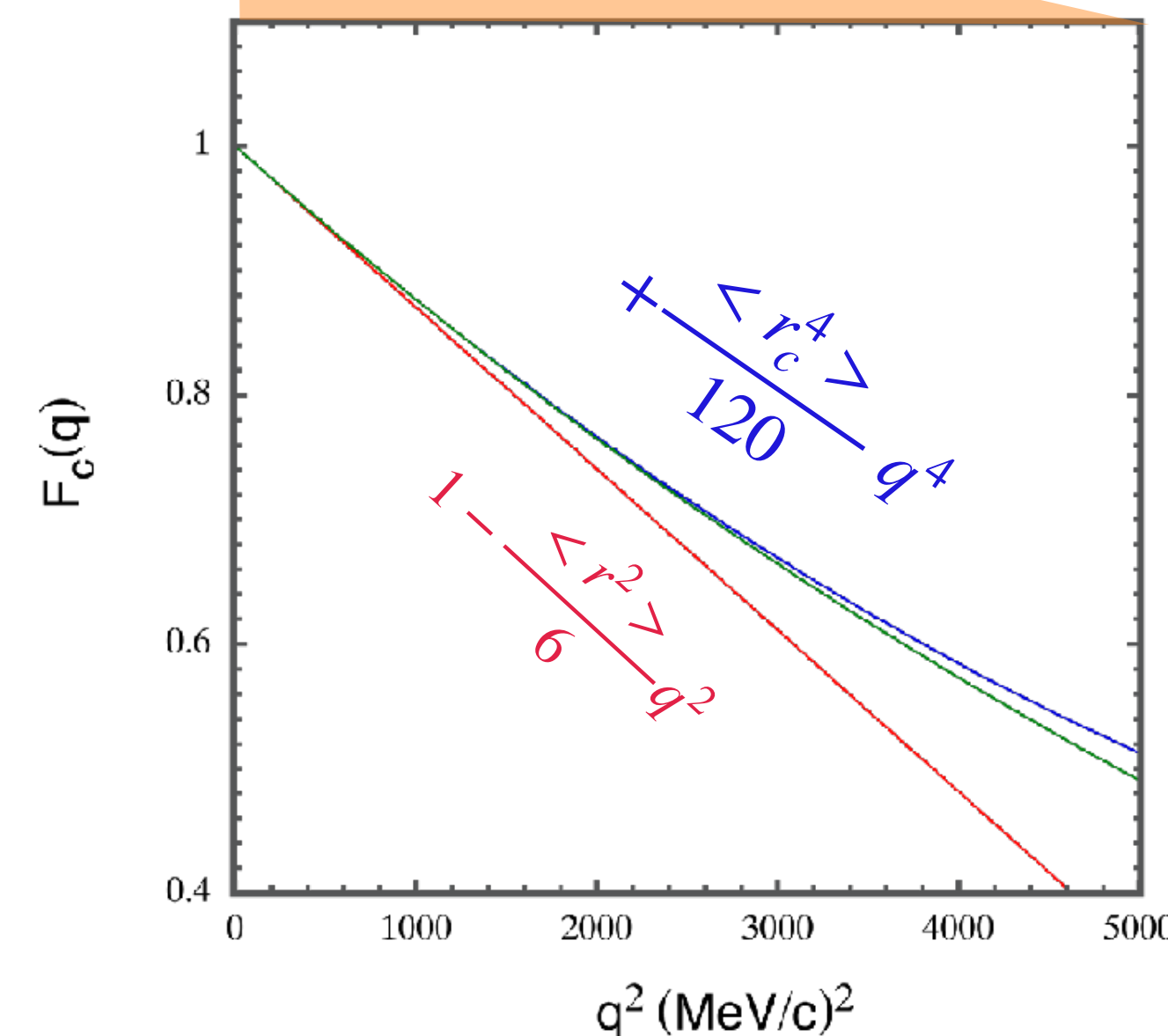
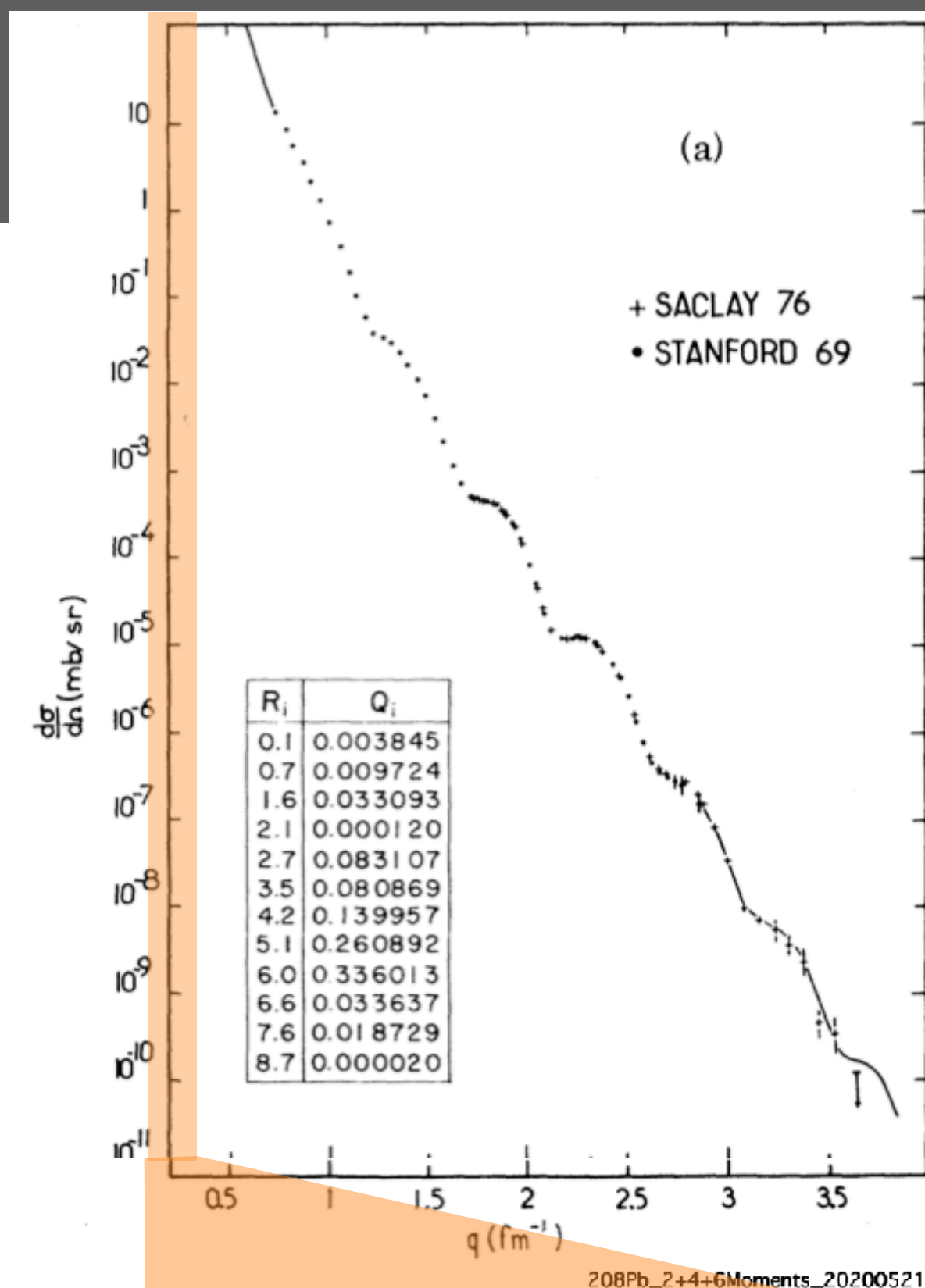
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$$F_c(q) \sim 1 - \frac{\langle r_c^2 \rangle}{6} q^2 + \frac{\langle r_c^4 \rangle}{120} q^4 + \dots$$

$$\frac{d\sigma_{Mott}}{d\Omega} \propto 1/q^4$$

=> low-L SCRIT exp. ??

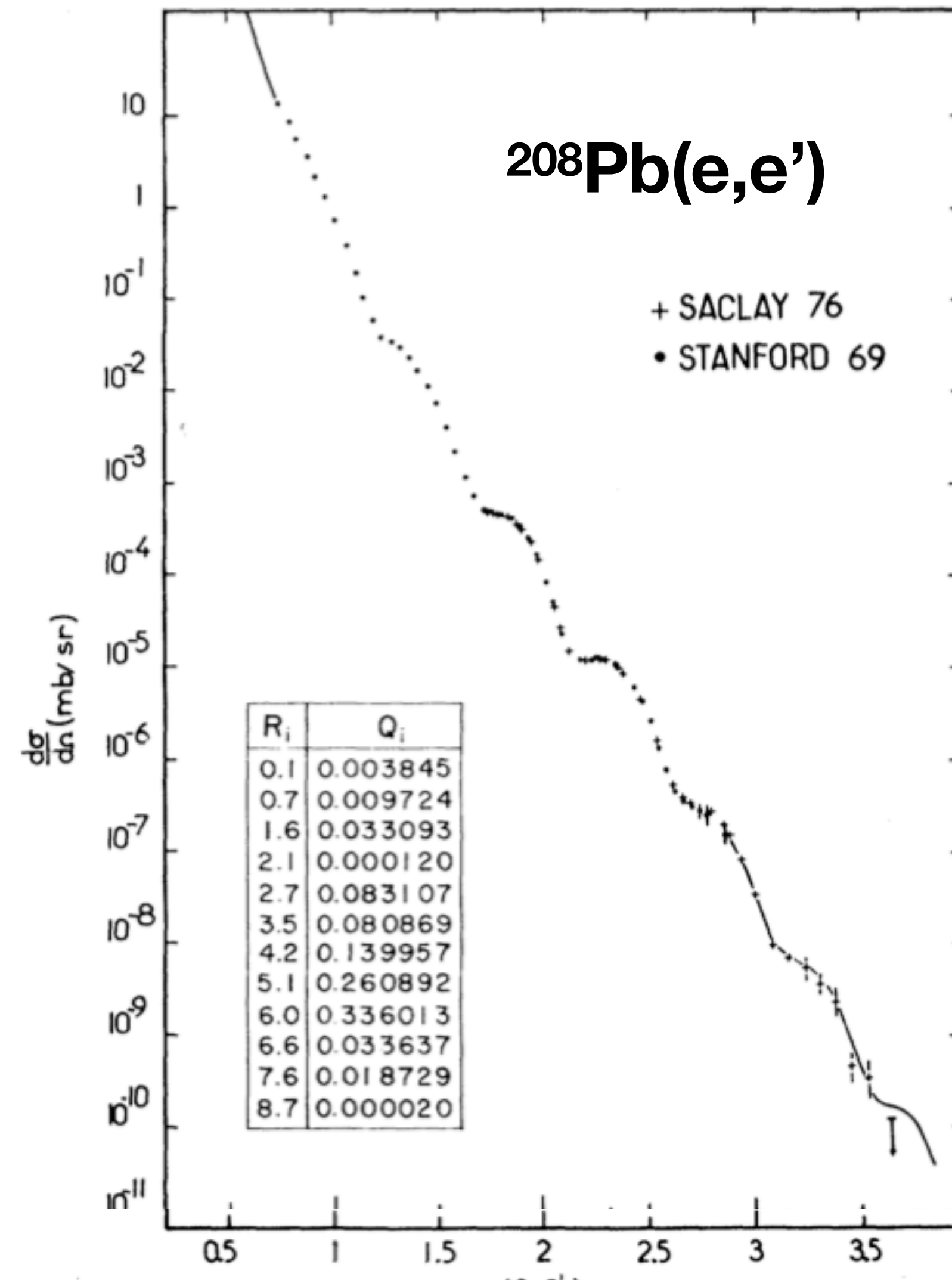
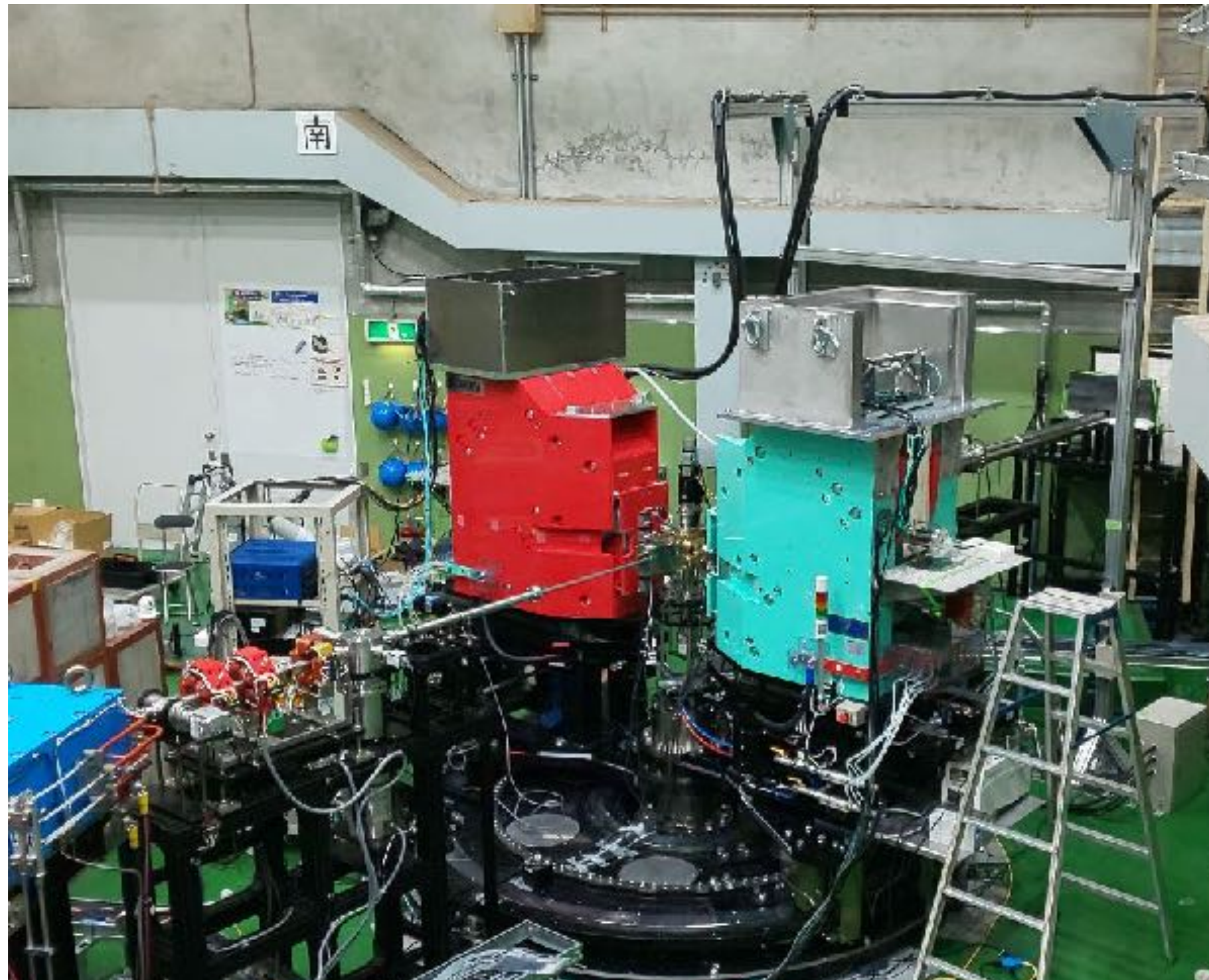


● $^{208}\text{Pb}(e,e')$ at the ULQ2 beam line at Tohoku

$E_e \sim 10 - 50 \text{ MeV}$

$\theta = 30 - 150^\circ$

$q = 5 - 50 \text{ MeV}/c$

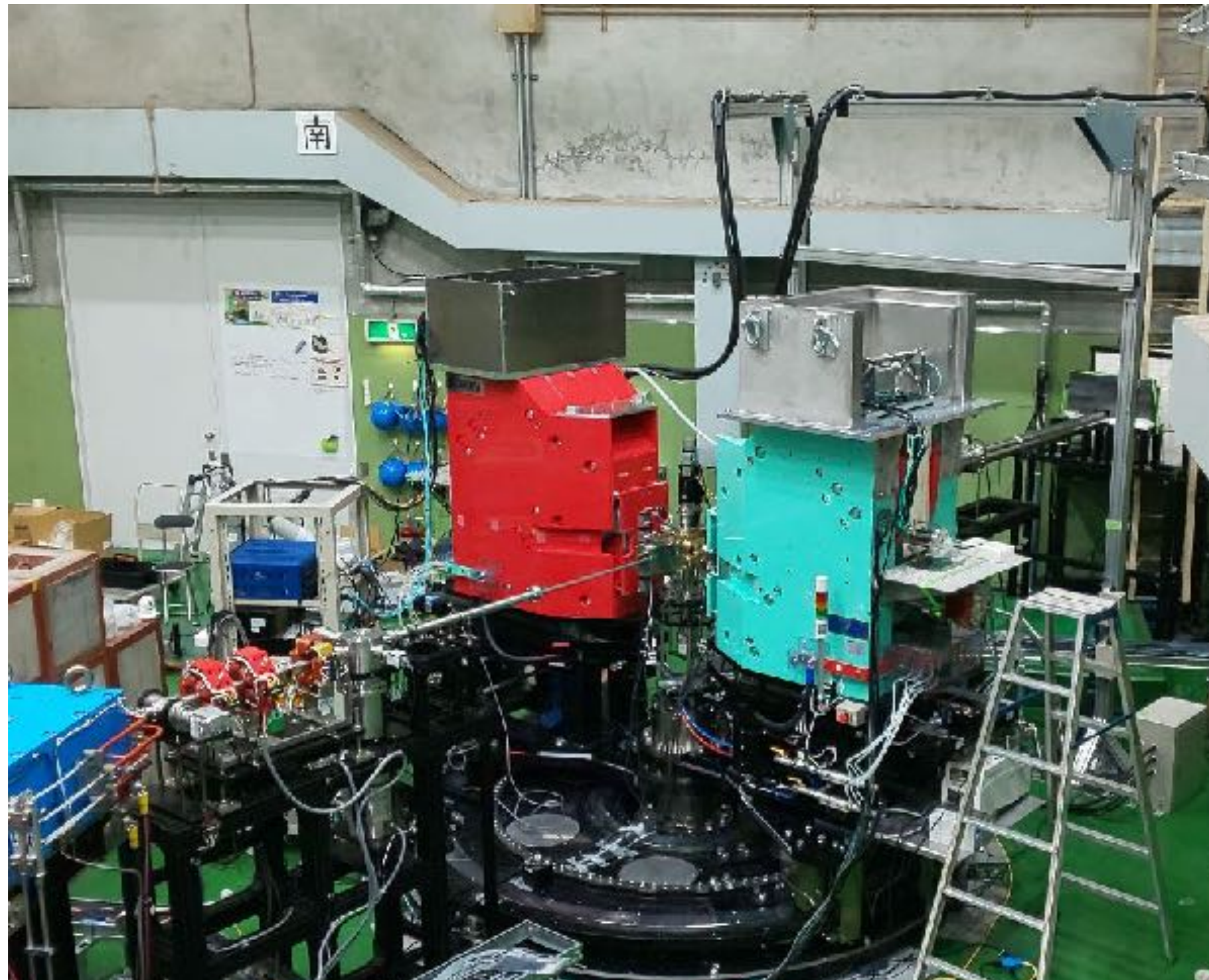


● $^{208}\text{Pb}(e,e')$ at the ULQ2 beam line at Tohoku

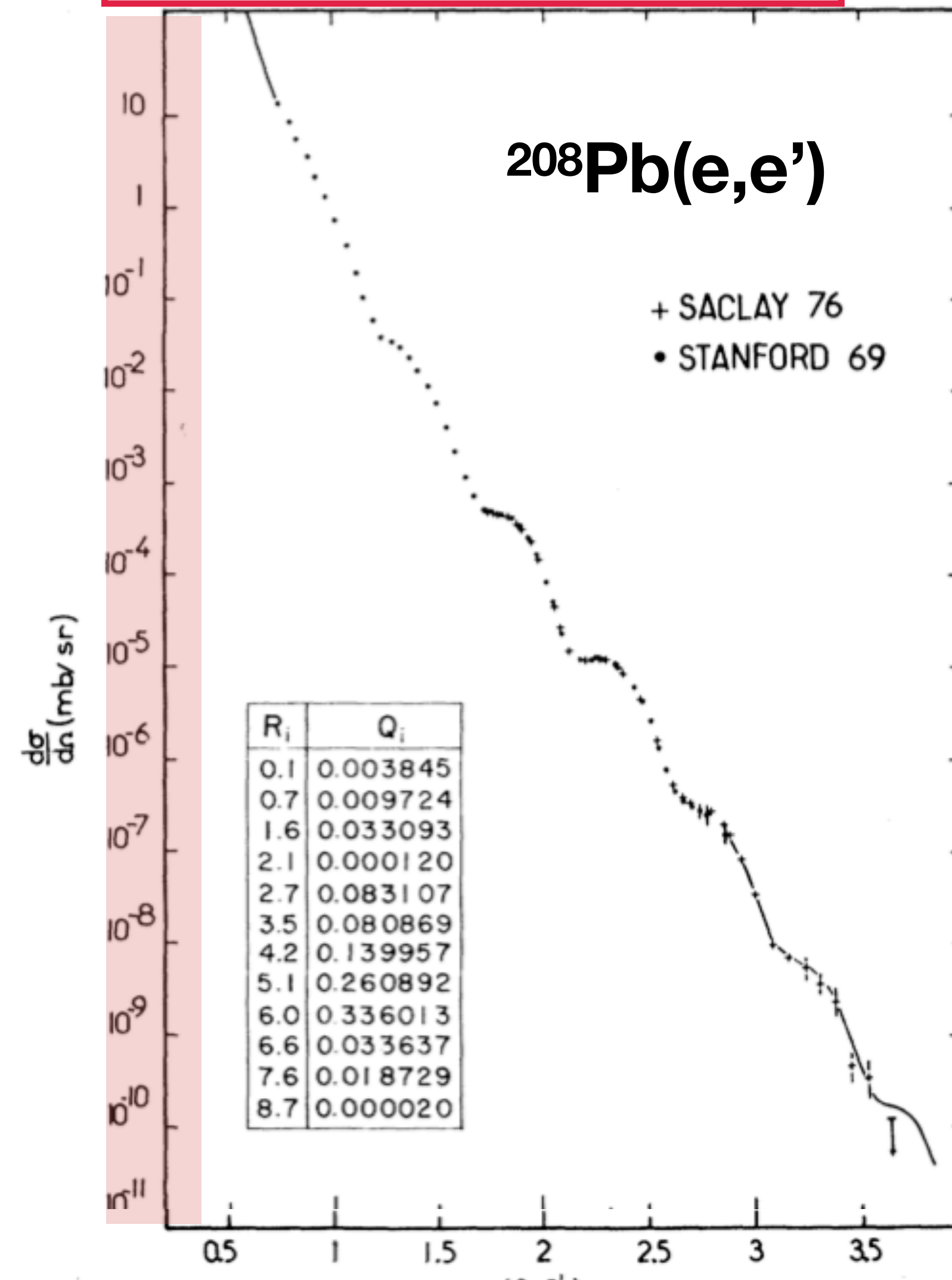
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lowest-ever q region

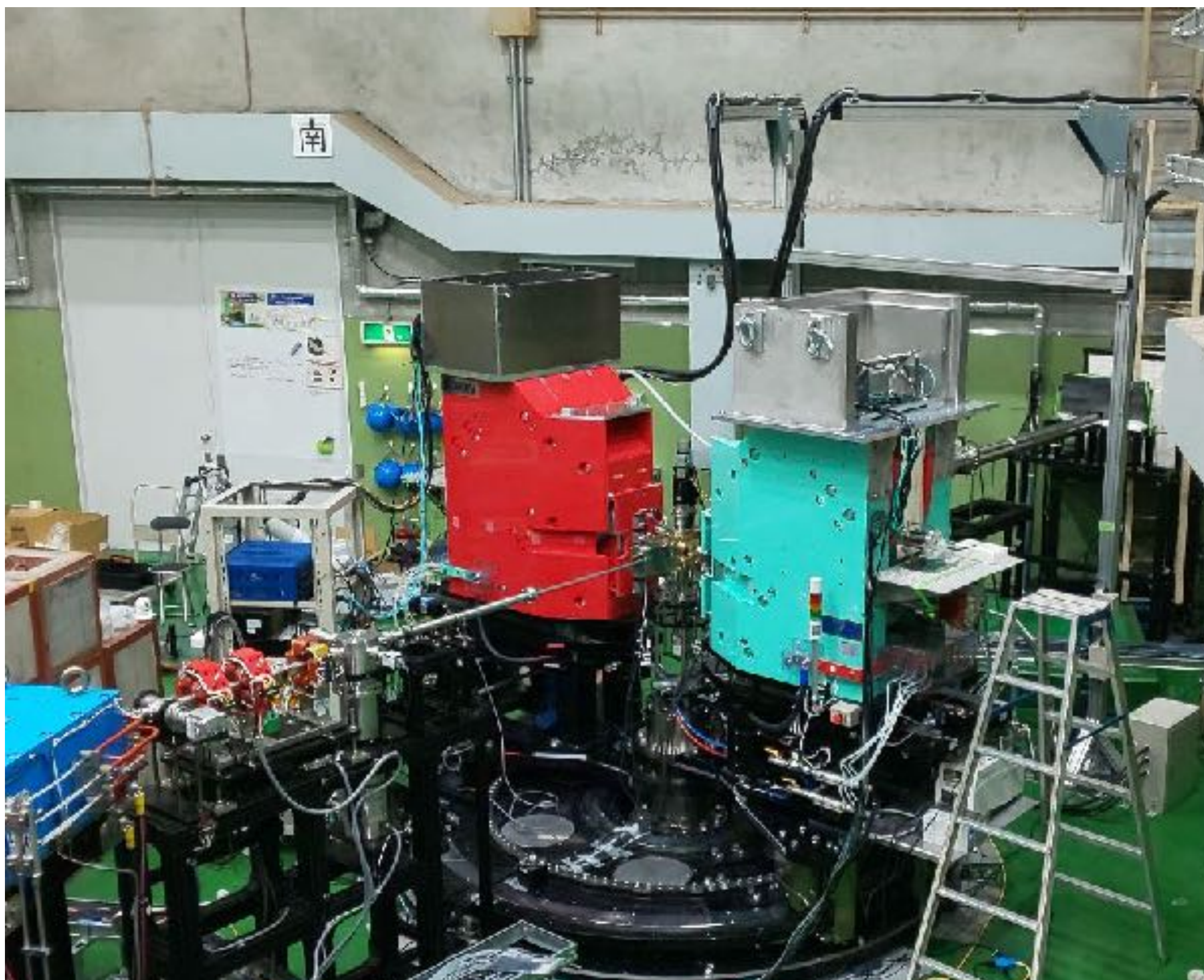


● $^{208}\text{Pb}(e,e')$ at the ULQ2 beam line at Tohoku

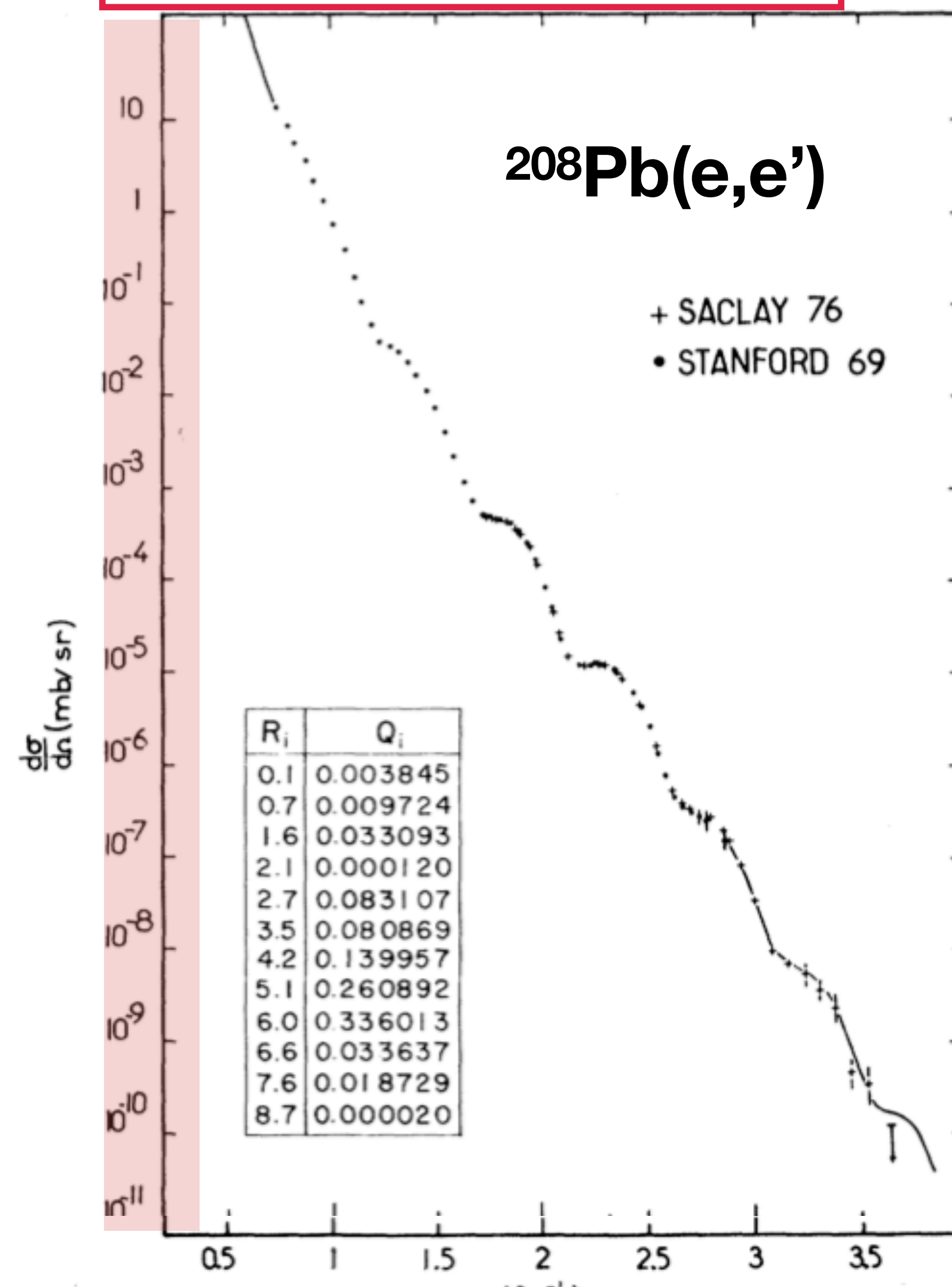
$E_e \sim 10 - 50 \text{ MeV}$

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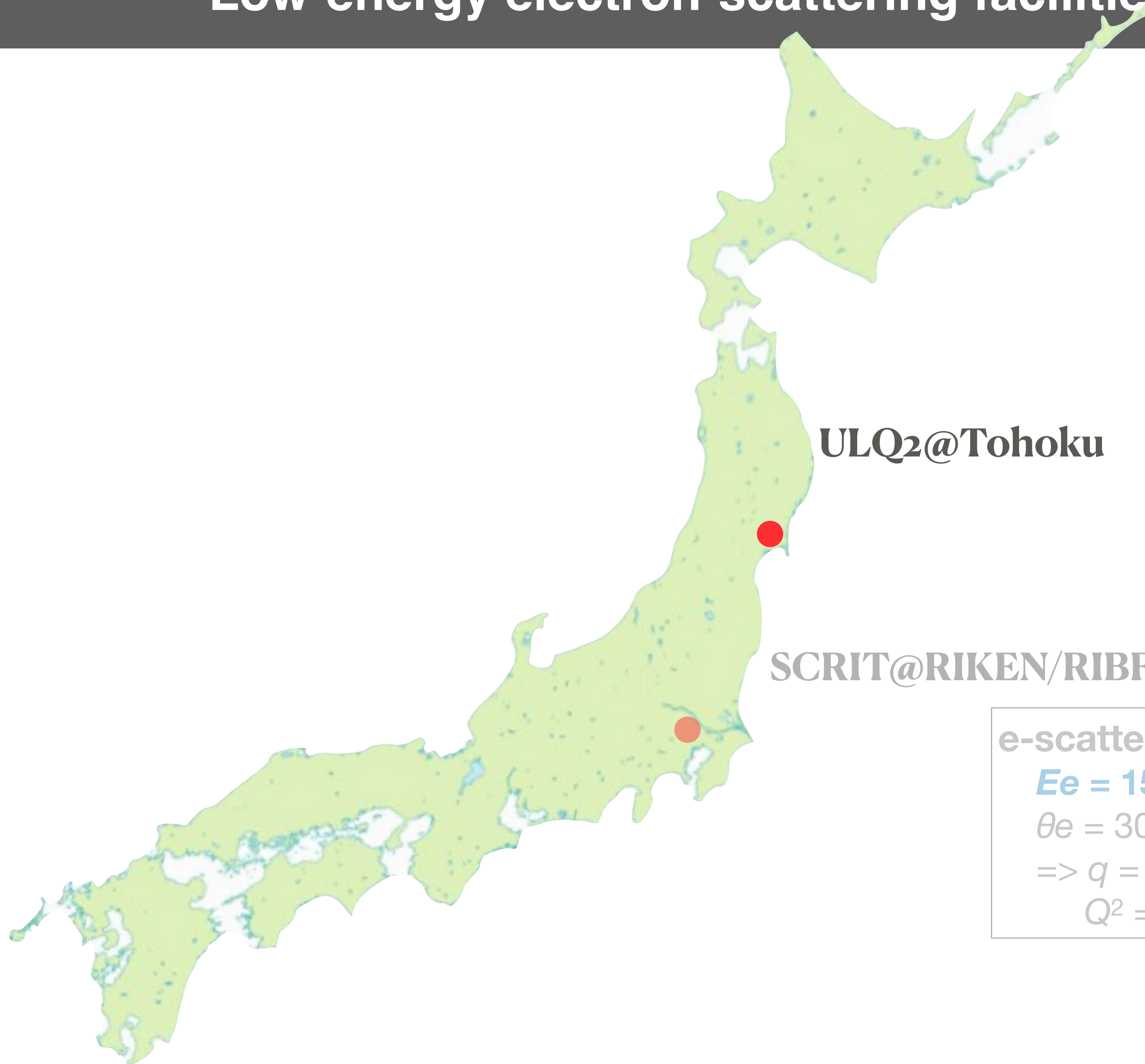
$q = 5 - 50 \text{ MeV}/c$



lowest-ever q region



Rika Danjo



ULQ2@Tohoku

Proton Charge Radius

$E_e = 10 - 60 \text{ MeV}$

$\theta_e = 30 - 150 \text{ deg.}$

$\Rightarrow Q^2 = 3 \times 10^{-5} - 0.013 \text{ (GeV/c)}^2$

lowest-ever Q^2 !!

SCRIT@RIKEN/RIBF

e-scattering for exotic nuclei ($\sim 10^8/\text{sec}$)

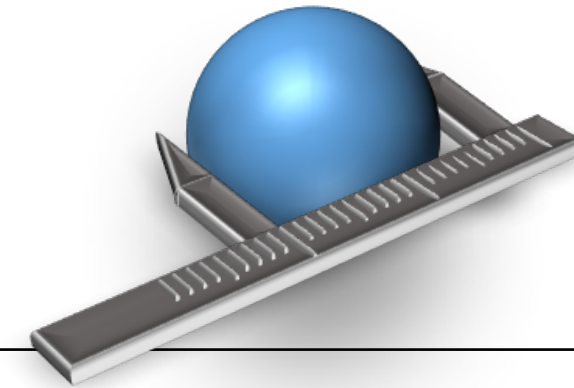
$E_e = 150 - 300 \text{ MeV}$

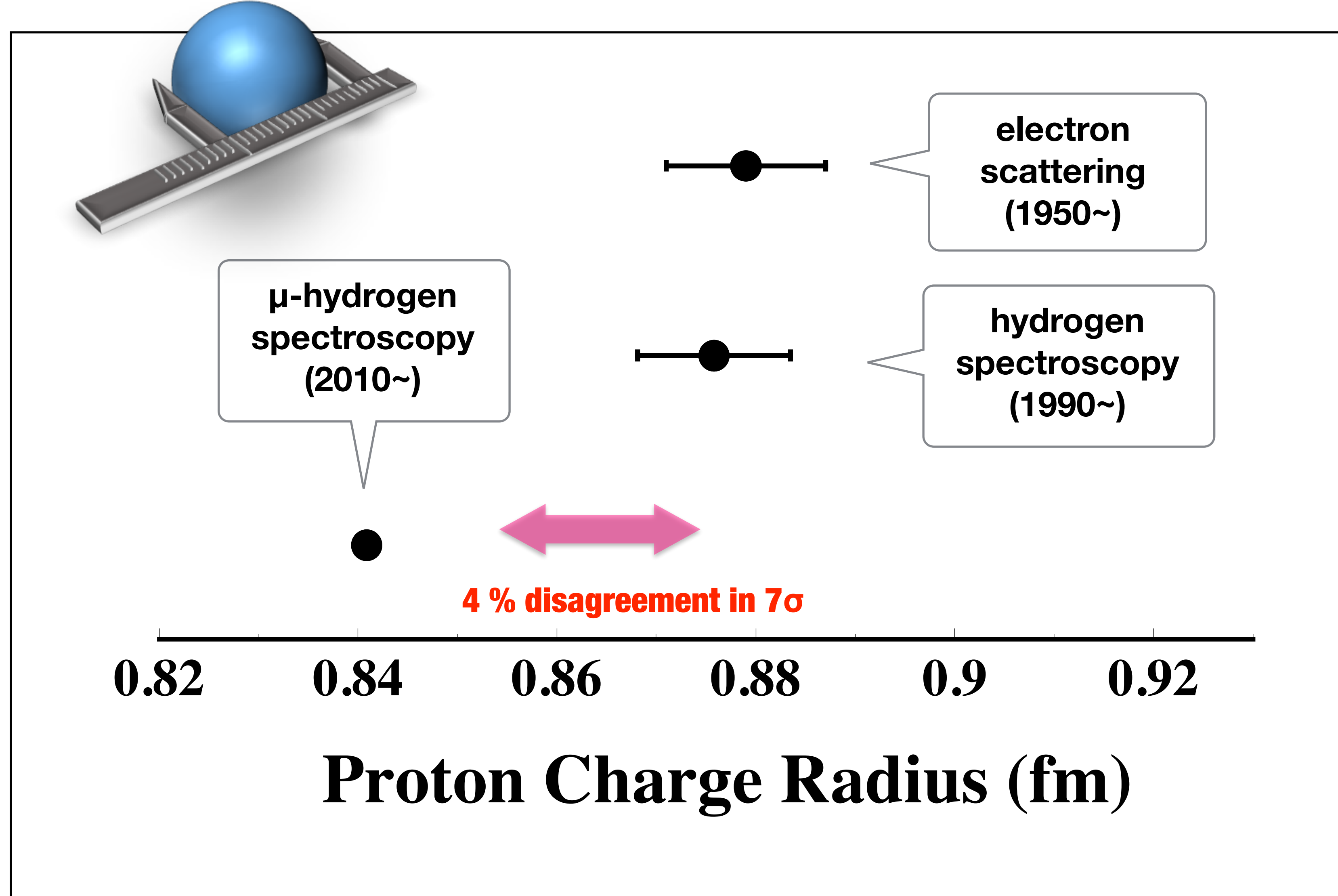
$\theta_e = 30 - 60 \text{ deg.}$

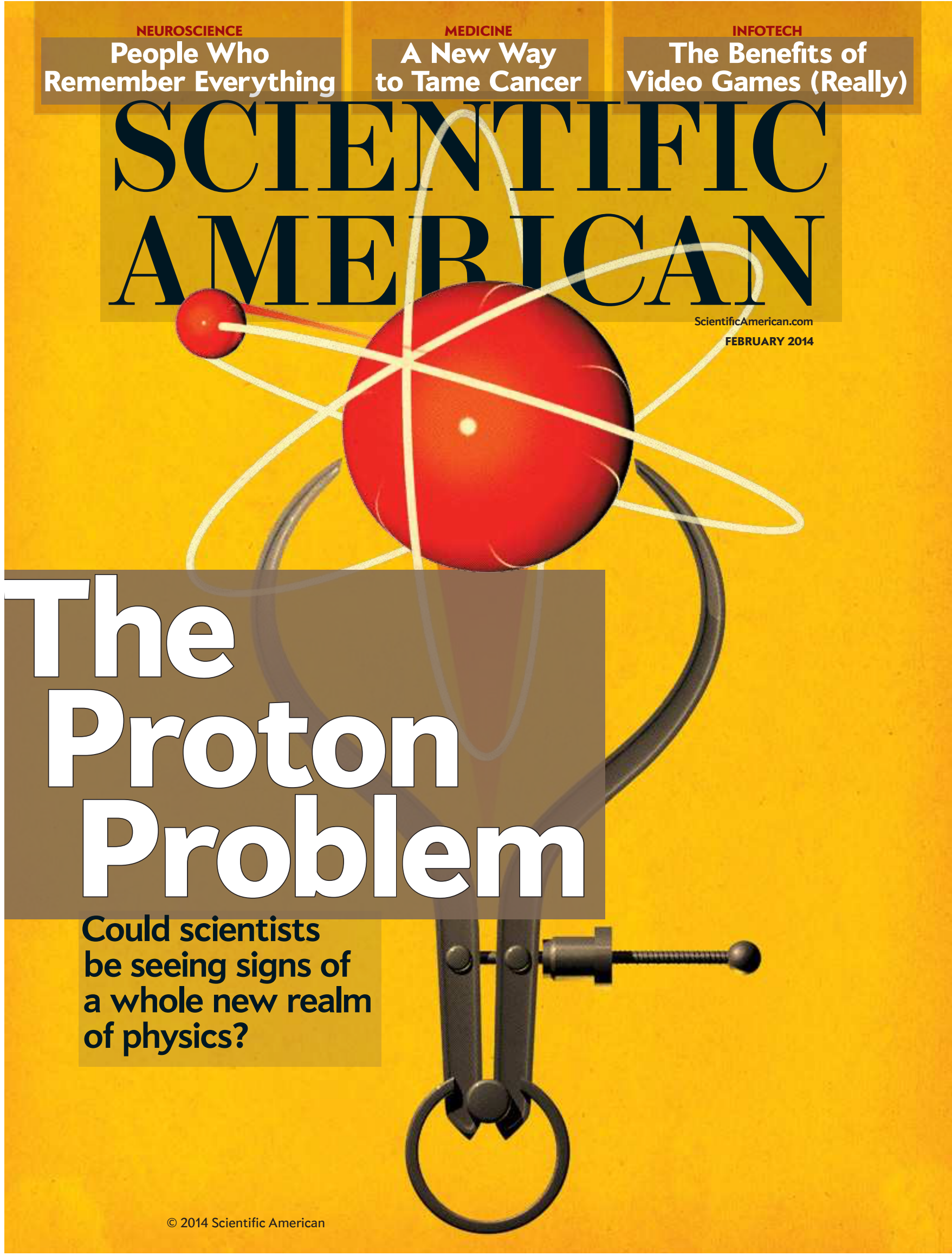
$\Rightarrow q = 80 - 300 \text{ MeV/c}$

$Q^2 = 0.006 - 0.09 \text{ (GeV/c)}^2$

world's first !!

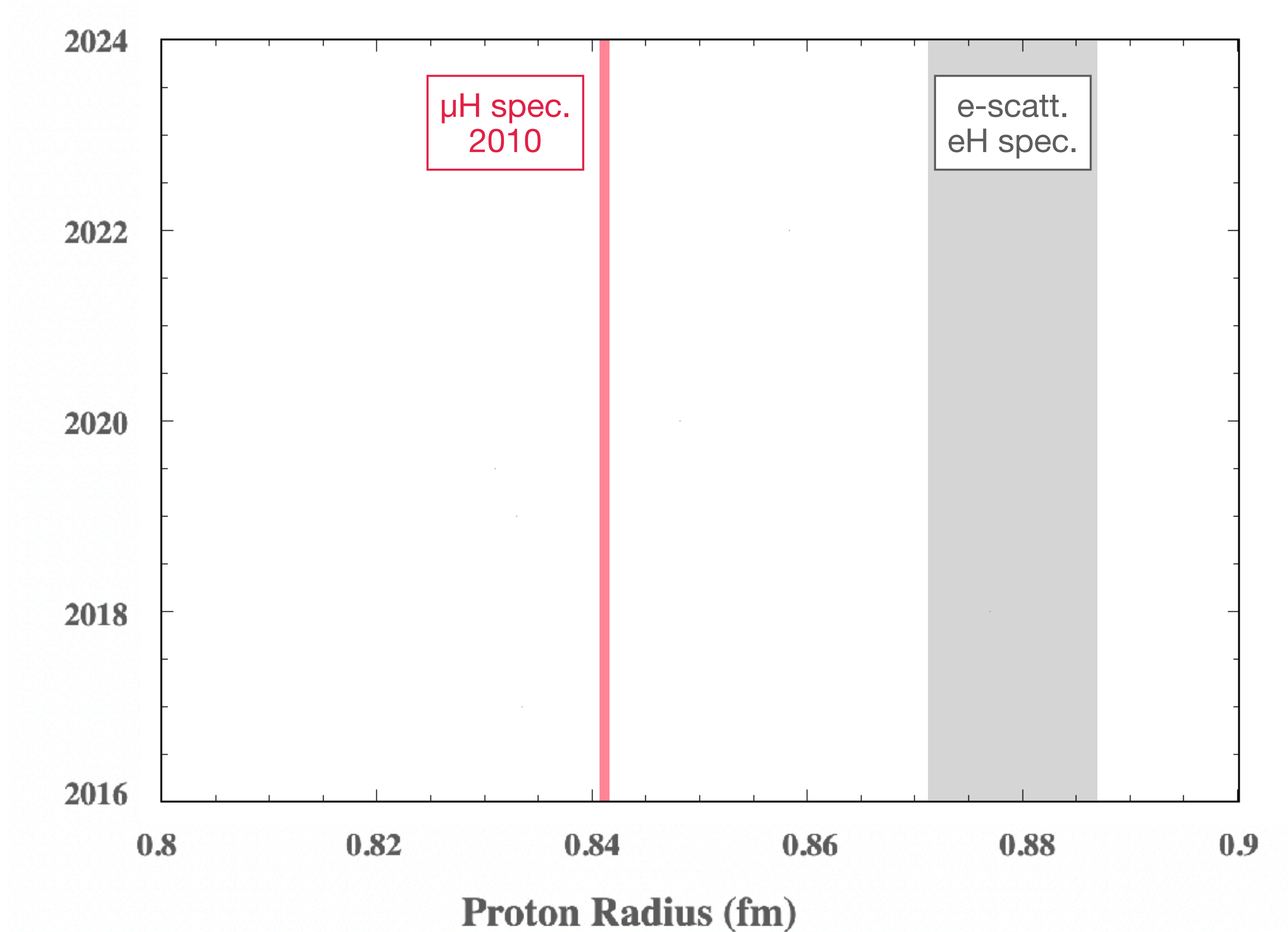




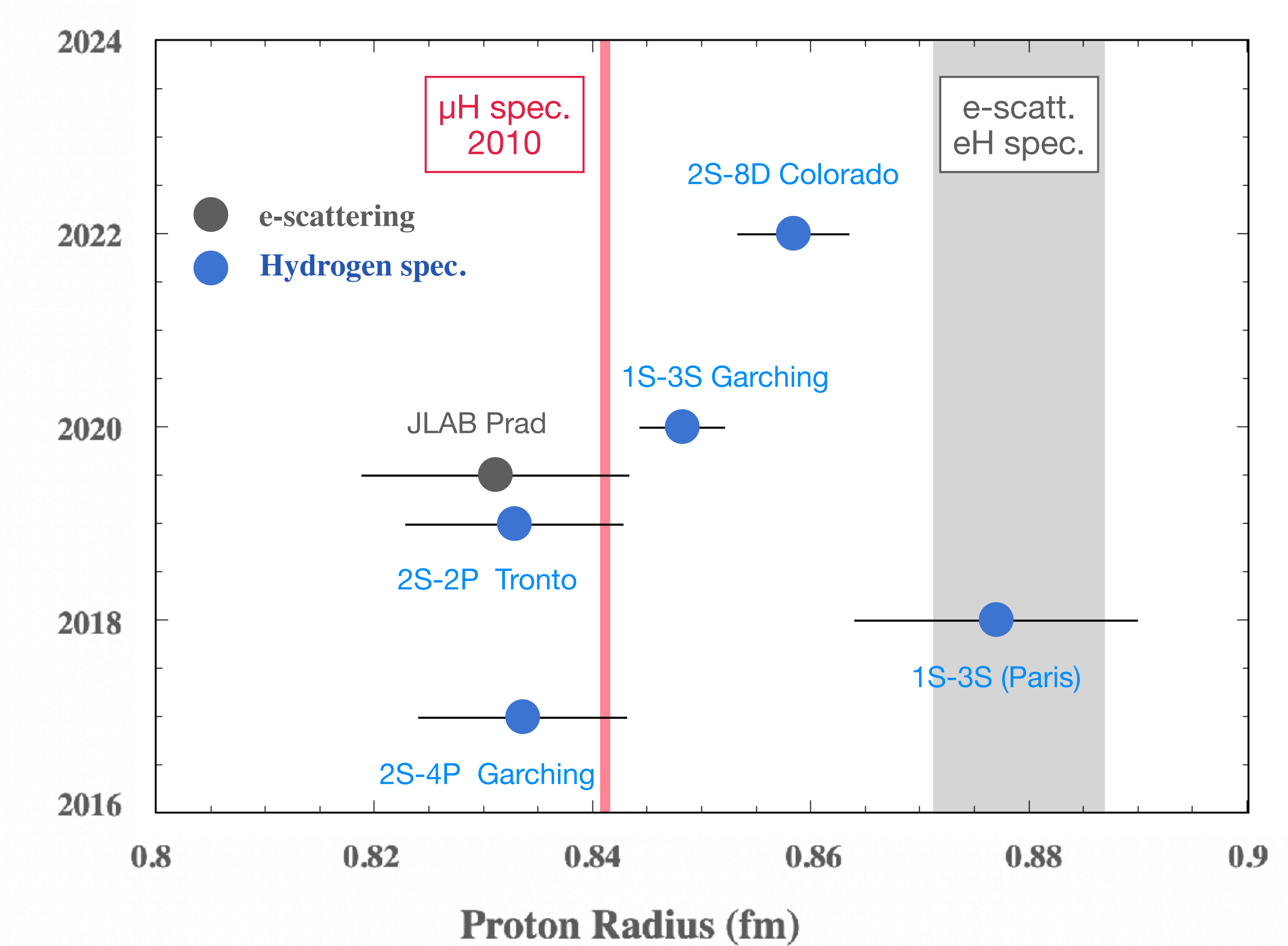


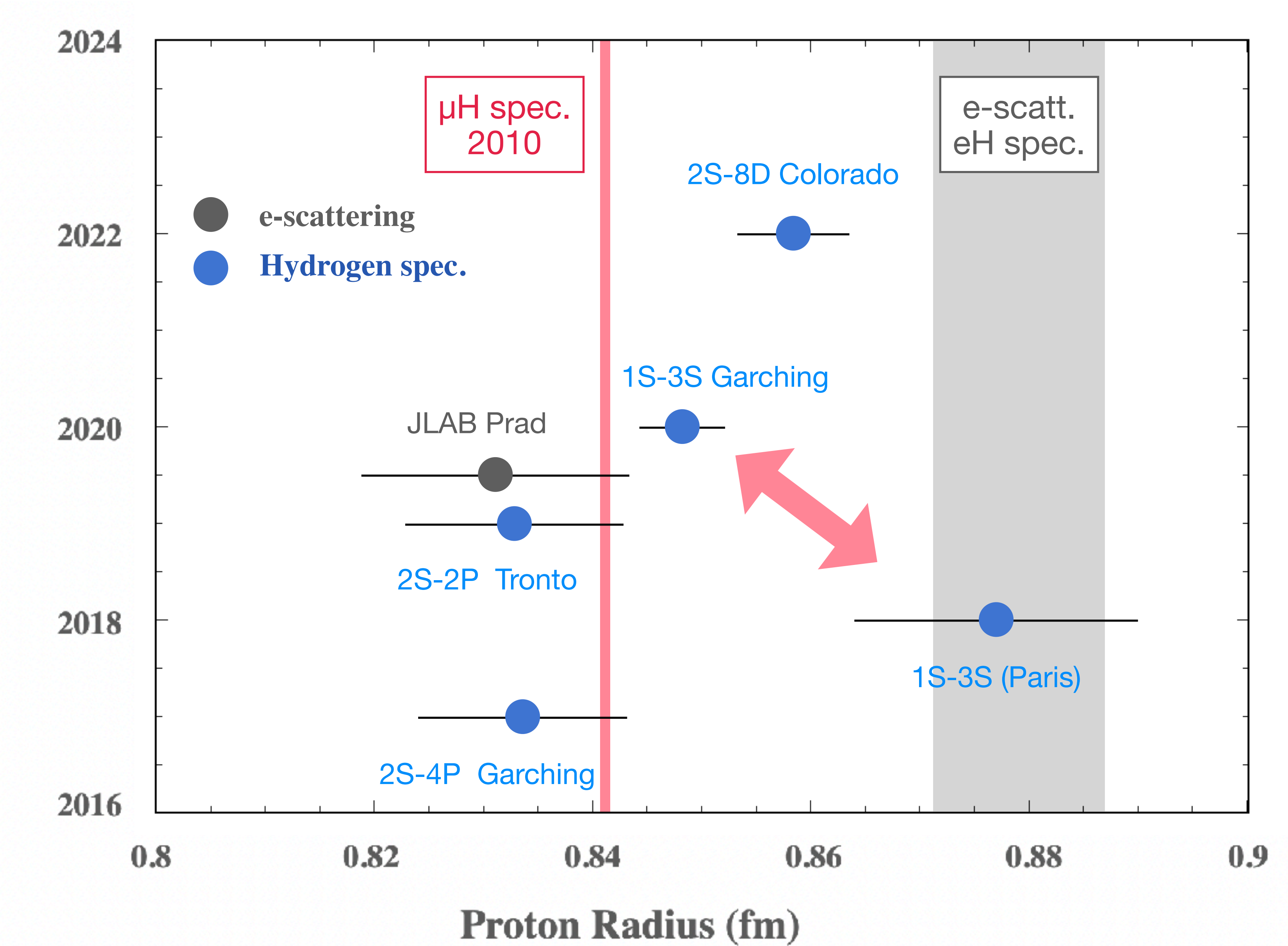
proton charge radius as of today

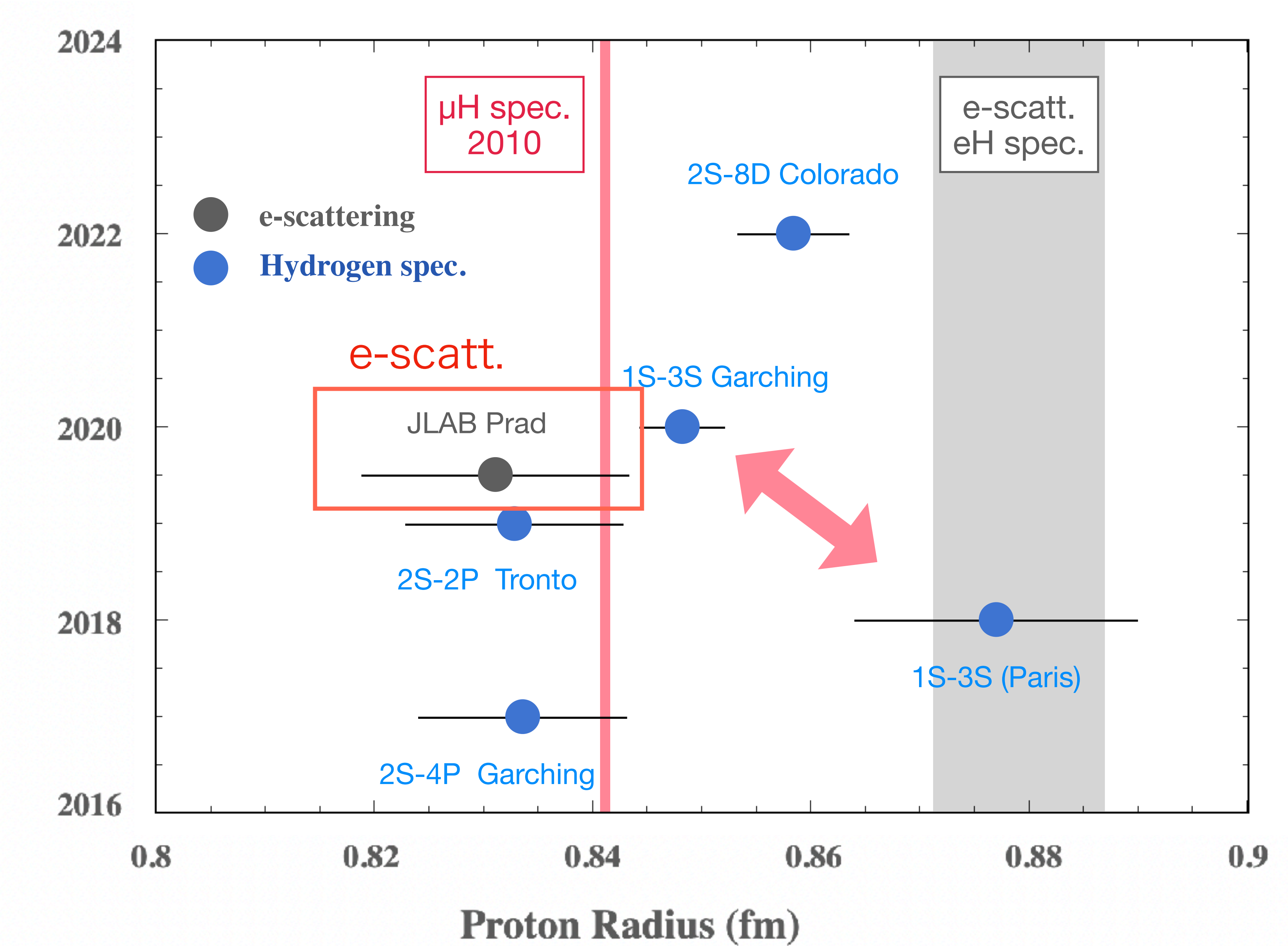
ECT*ws
2025.07.14-07.18

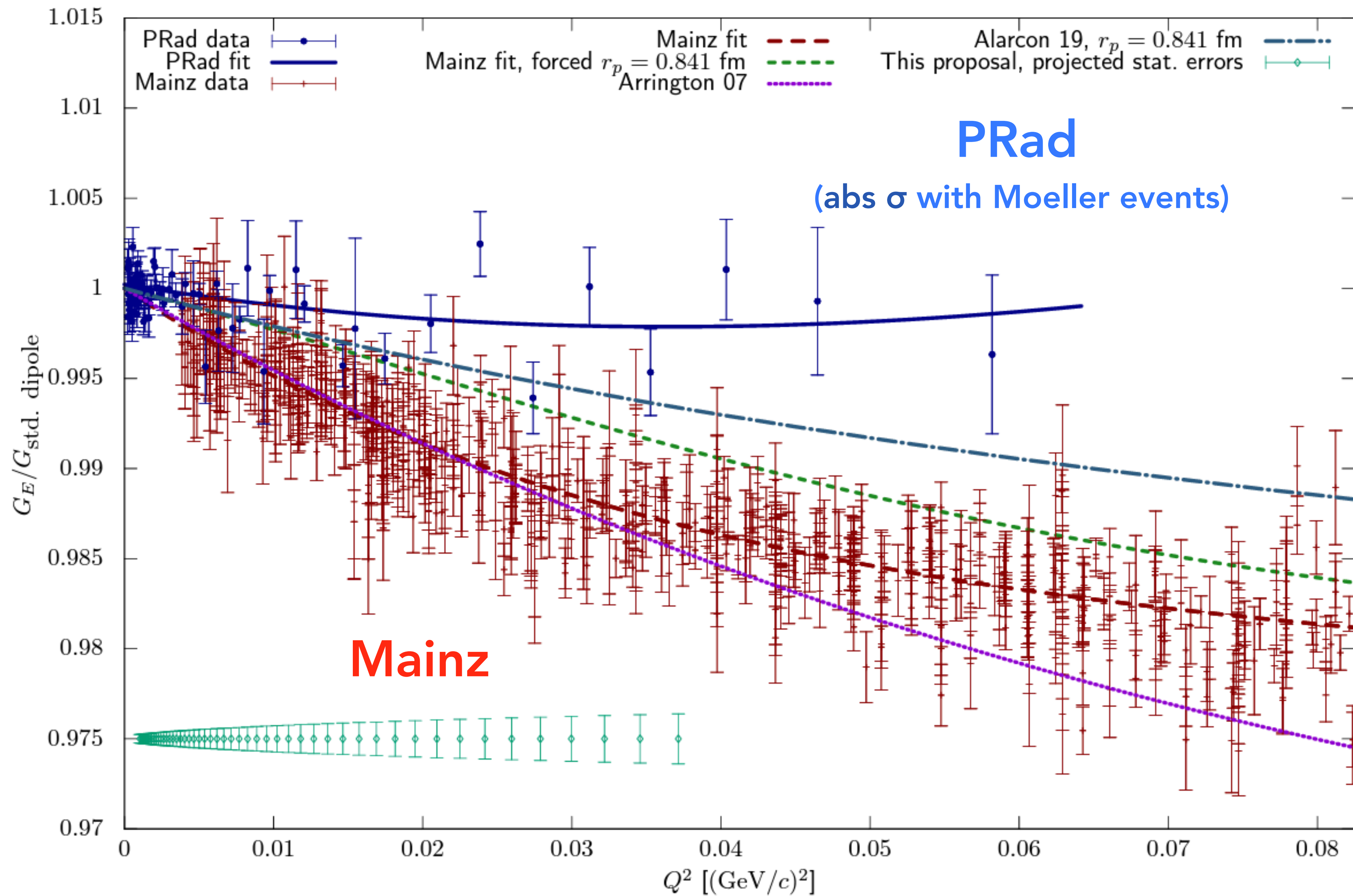


proton charge radius as of today









ULQ2 (Ultra-Low Q^2) at Tohoku, JAPAN since 2016~

ECT*ws
2025.07.14-07.18

“*least model-dependent*” proton charge radius

- 1) **lowest-ever Q^2** by lowest-ever energy e-scattering (**10-60 MeV**)
- 2) **absolute σ** measurements with **10^{-3} accuracy**
- 3) **Rosenbluth-separated $G_E(Q^2)$ and $G_M(Q^2)$**

possible only at Tohoku accel.

60 MeV electron linac (since 1967)

$E_e = 10 - 60 \text{ MeV}$

$\Delta E/E = 0.6 \times 10^{-4}$

beam size $\sim 0.6 \text{ mm}$ on target

duty factor = 10^{-3}

ULQ2 twin-spectrometer setup

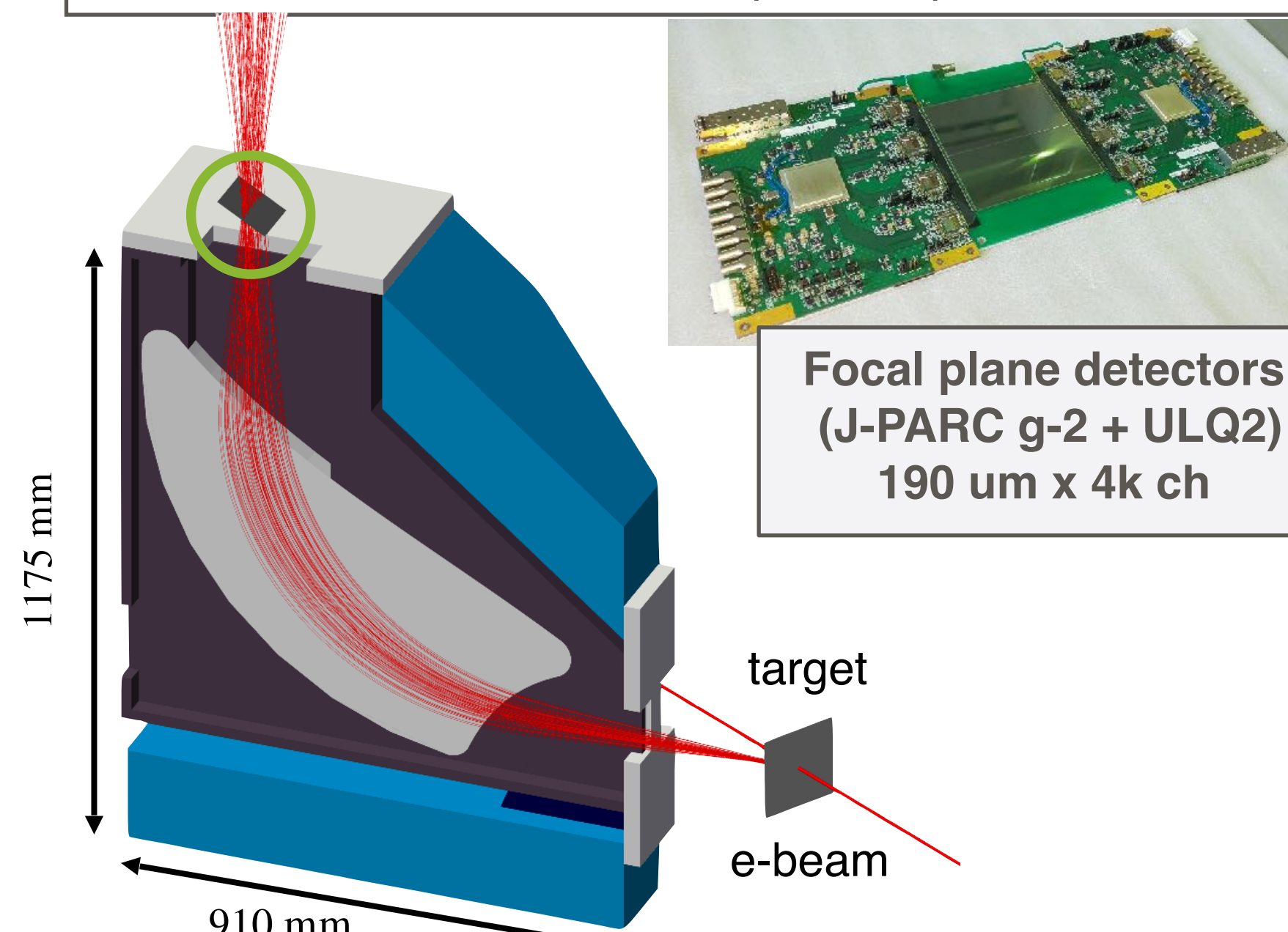
Luminosity monitoring

$\Delta p/p = 5.6 \times 10^{-3}$

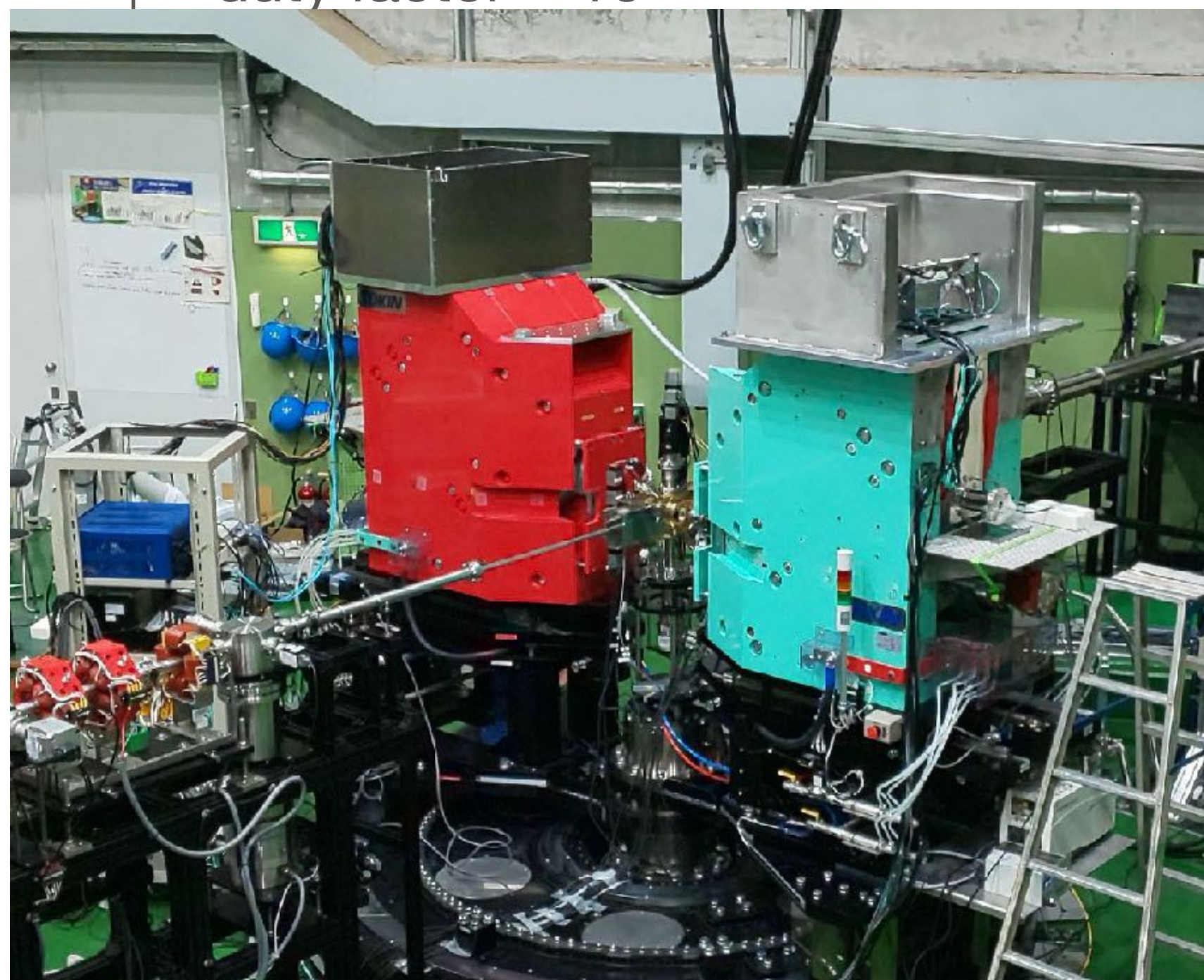
$\Delta\Omega = 6 \text{ mSr}$

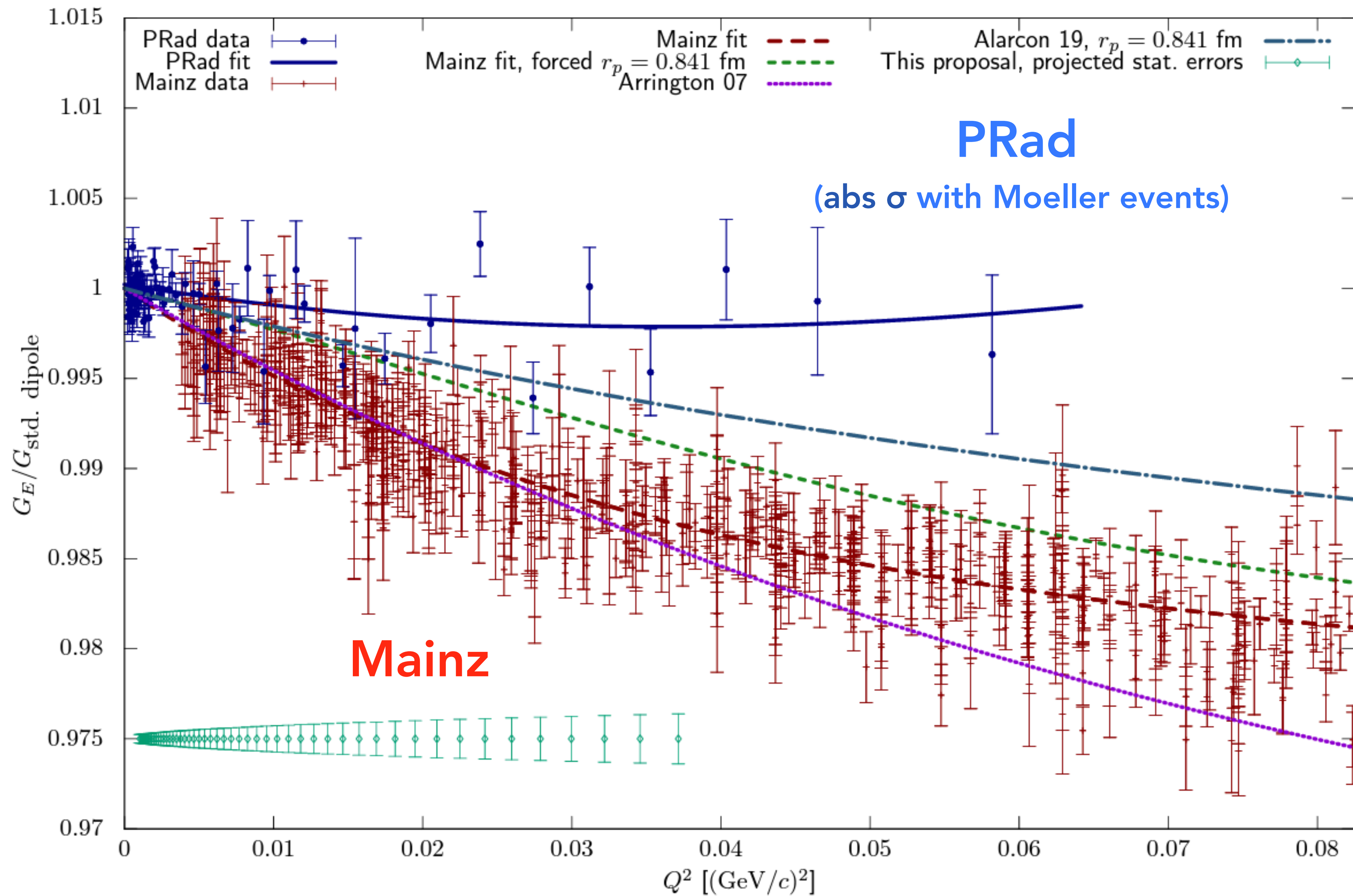
$\theta = 30 - 150 \text{ deg.}$

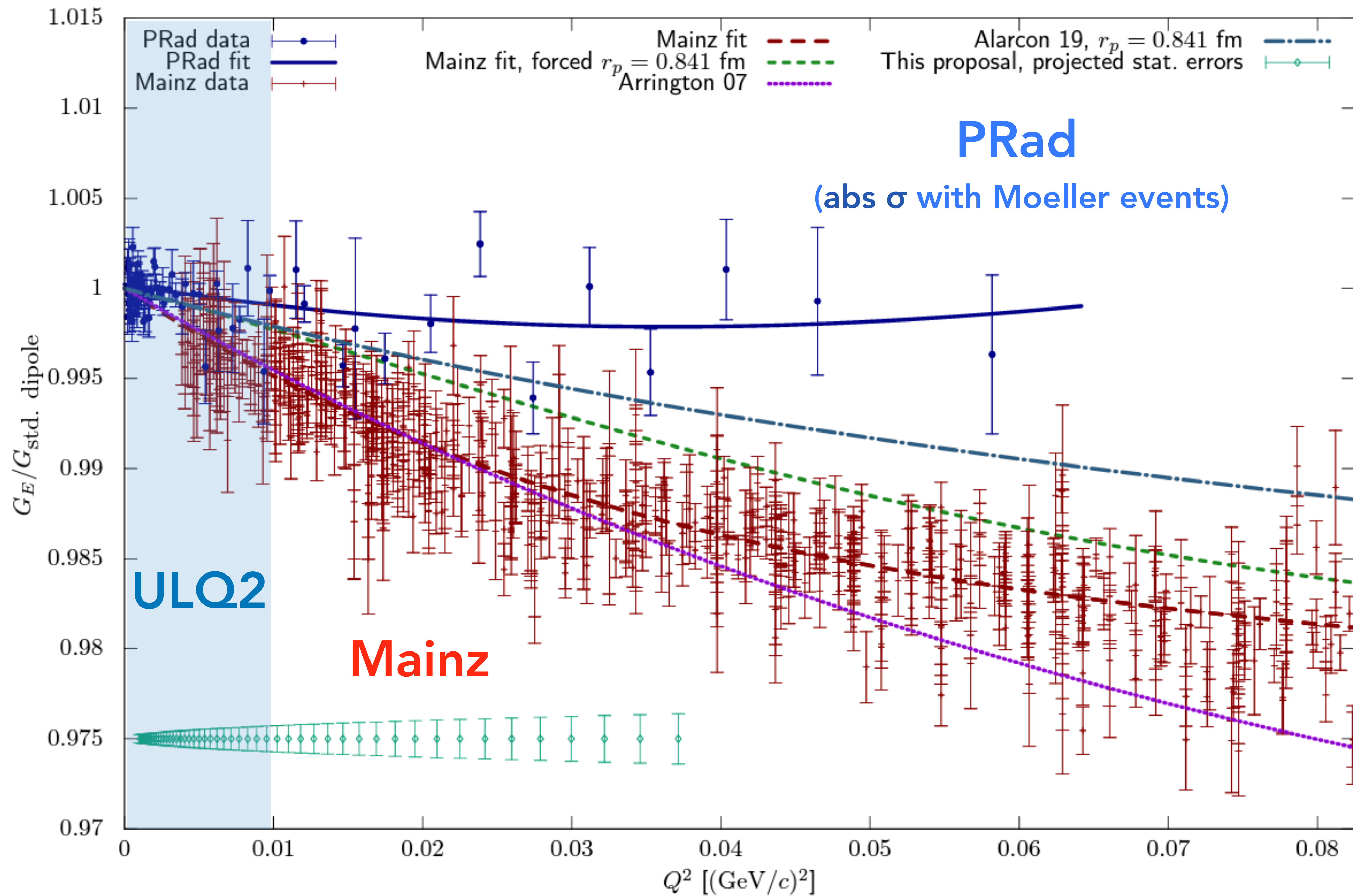
$Q^2 = 3 \times 10^{-5} - 0.013 \text{ (GeV/c)}^2$

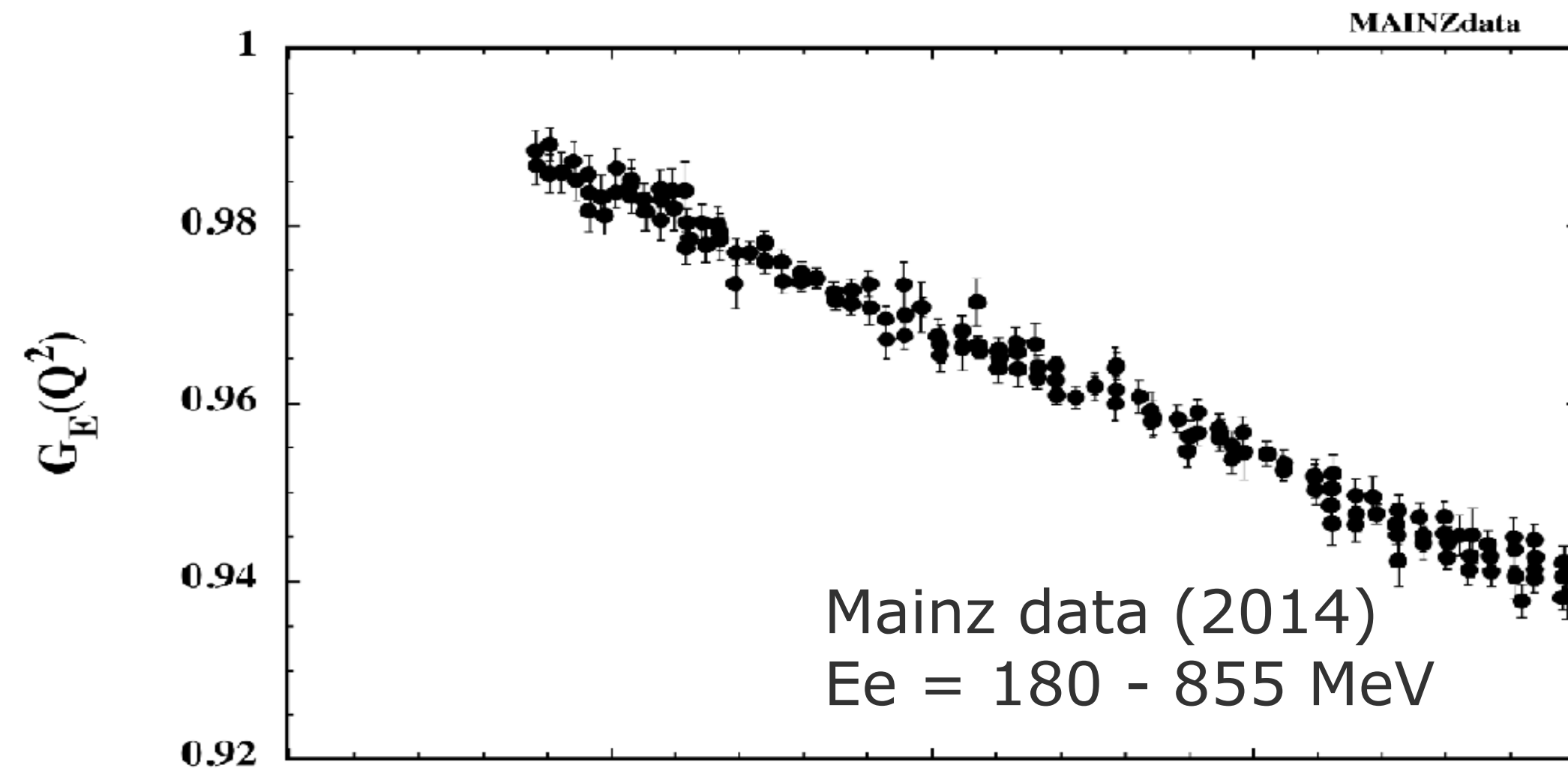


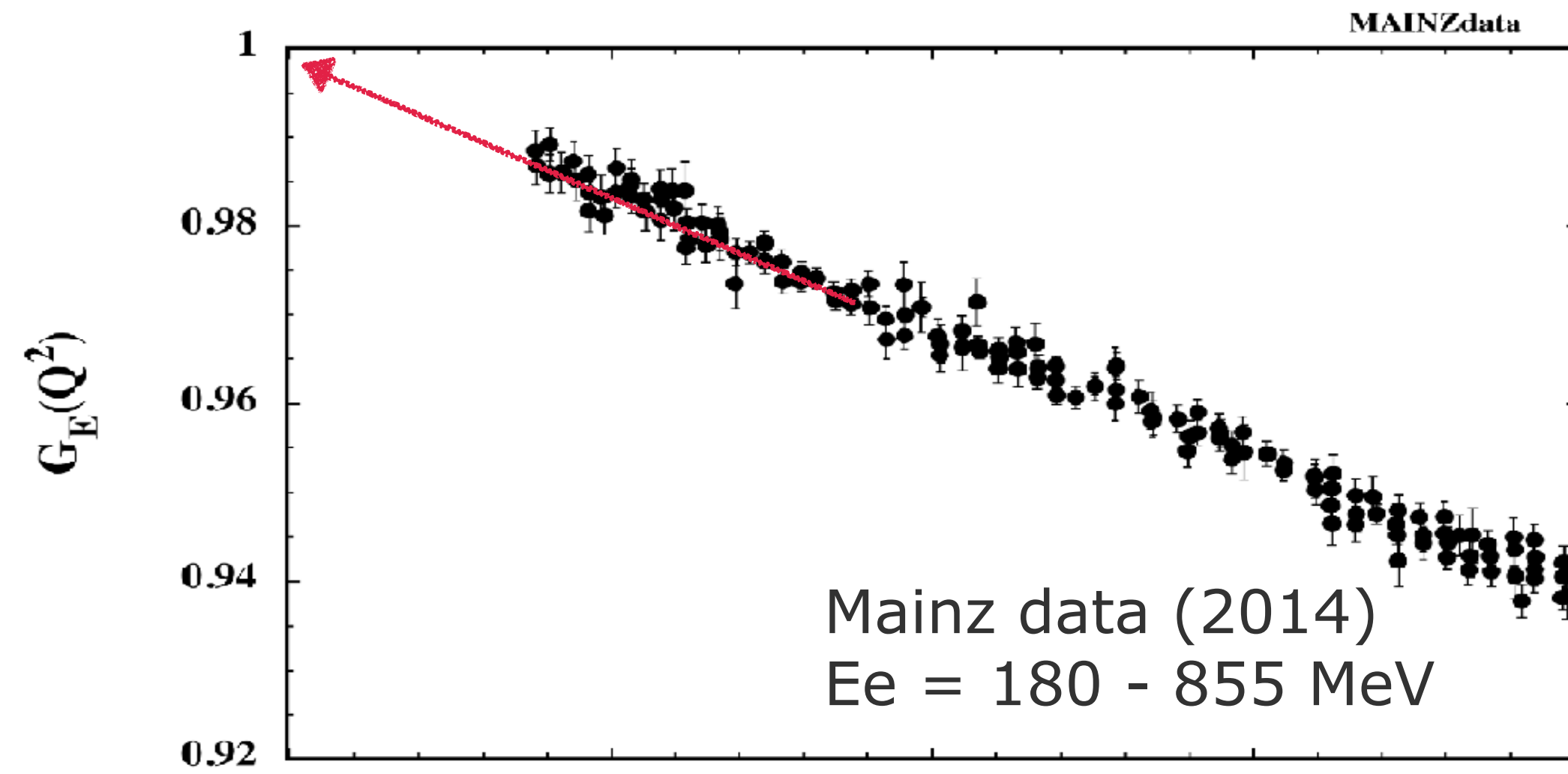
Yuki Honda

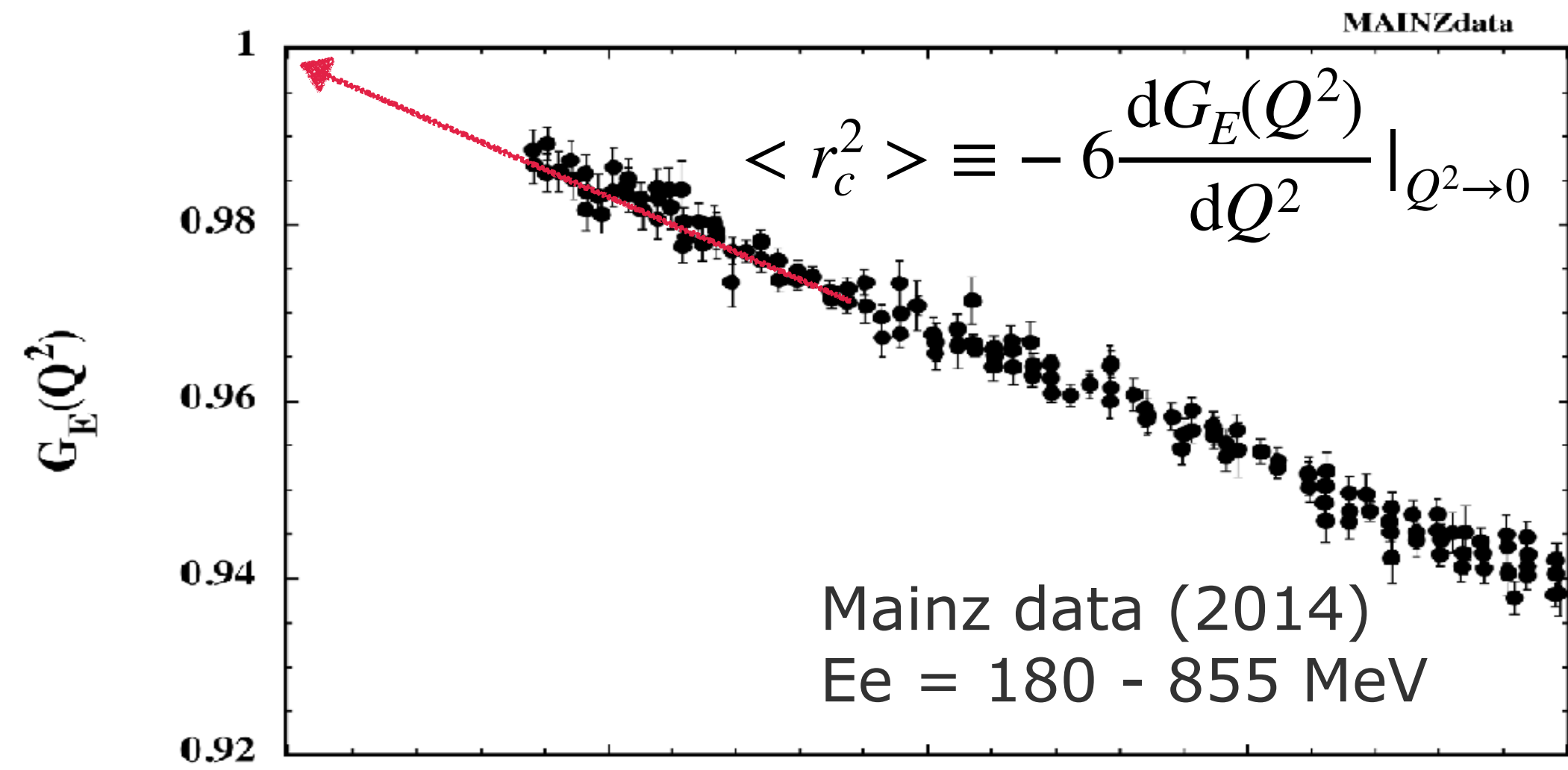


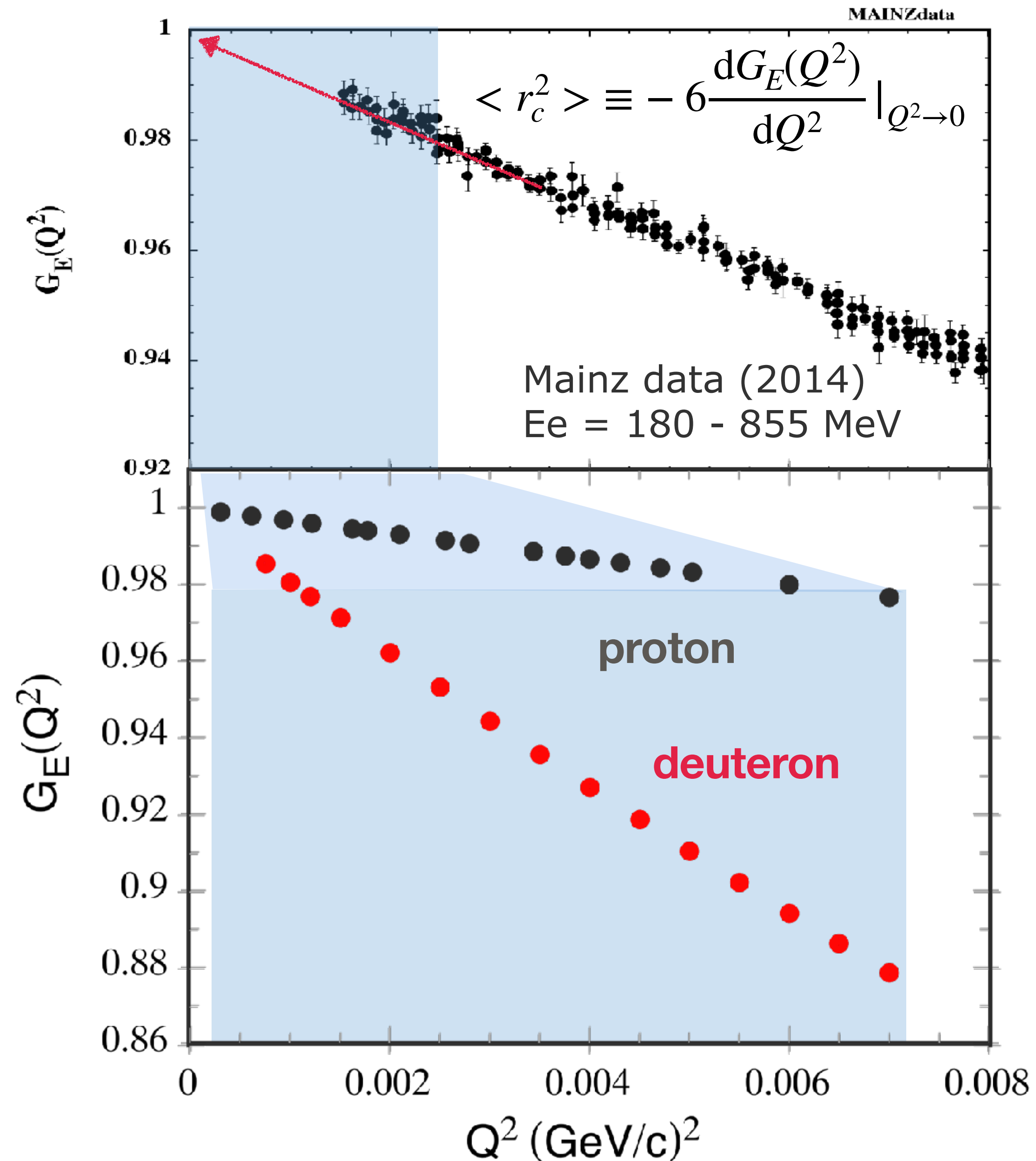


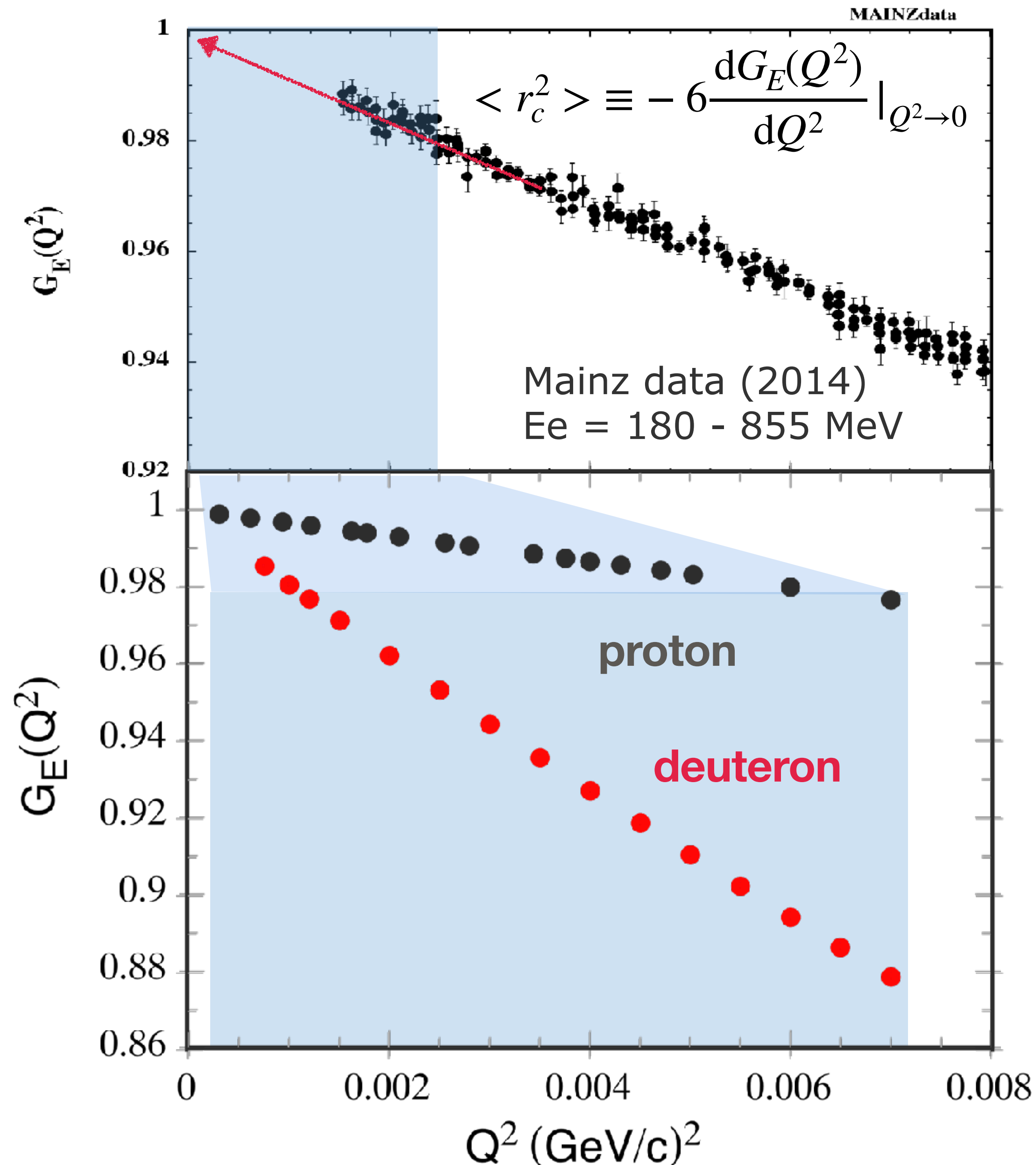










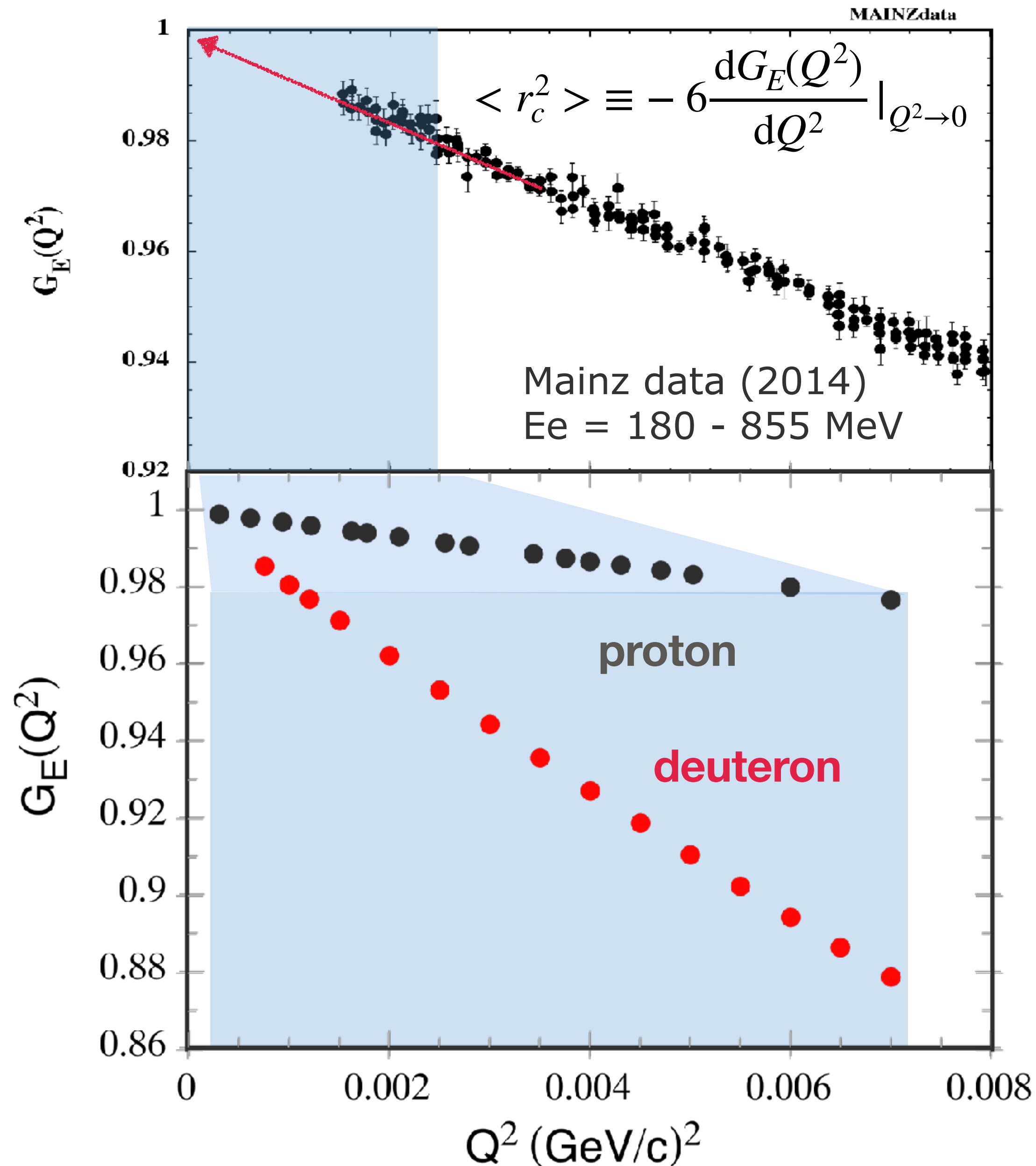


1) **proton** (Clement Legris)
charge radius
magnetic radius (next step)



2) **deuteron** (Taiga Goke)
deuteron charge radius
=> neutron charge radius





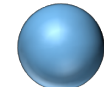
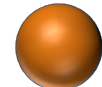
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magnetic radius (next step)



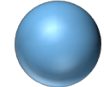
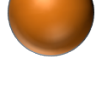
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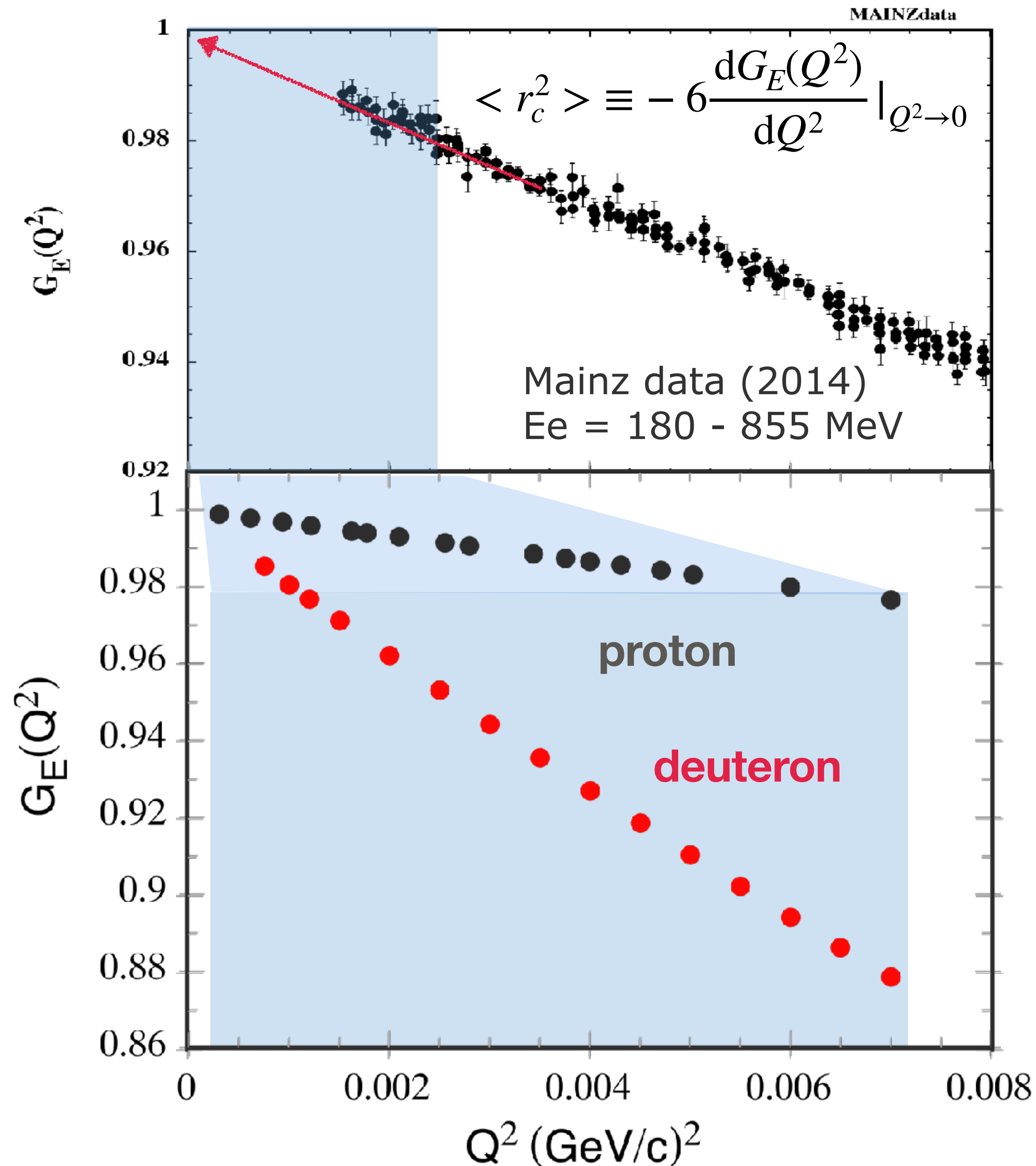


$$\langle r_d^2 \rangle = \langle r_{str}^2 \rangle + \langle r_p^2 \rangle + \langle r_n^2 \rangle + \text{RC}$$

ULQ2 theory  

$$\langle r_d^4 \rangle = \langle r_{str}^4 \rangle + \frac{10}{3} \langle r_{pstr}^2 \rangle (\langle r_p^2 \rangle + \langle r_n^2 \rangle) + O(4) + \text{RC}$$

ULQ2 theory theory  



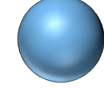
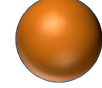
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charge radius
magnetic radius (next step)



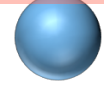
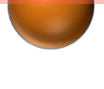
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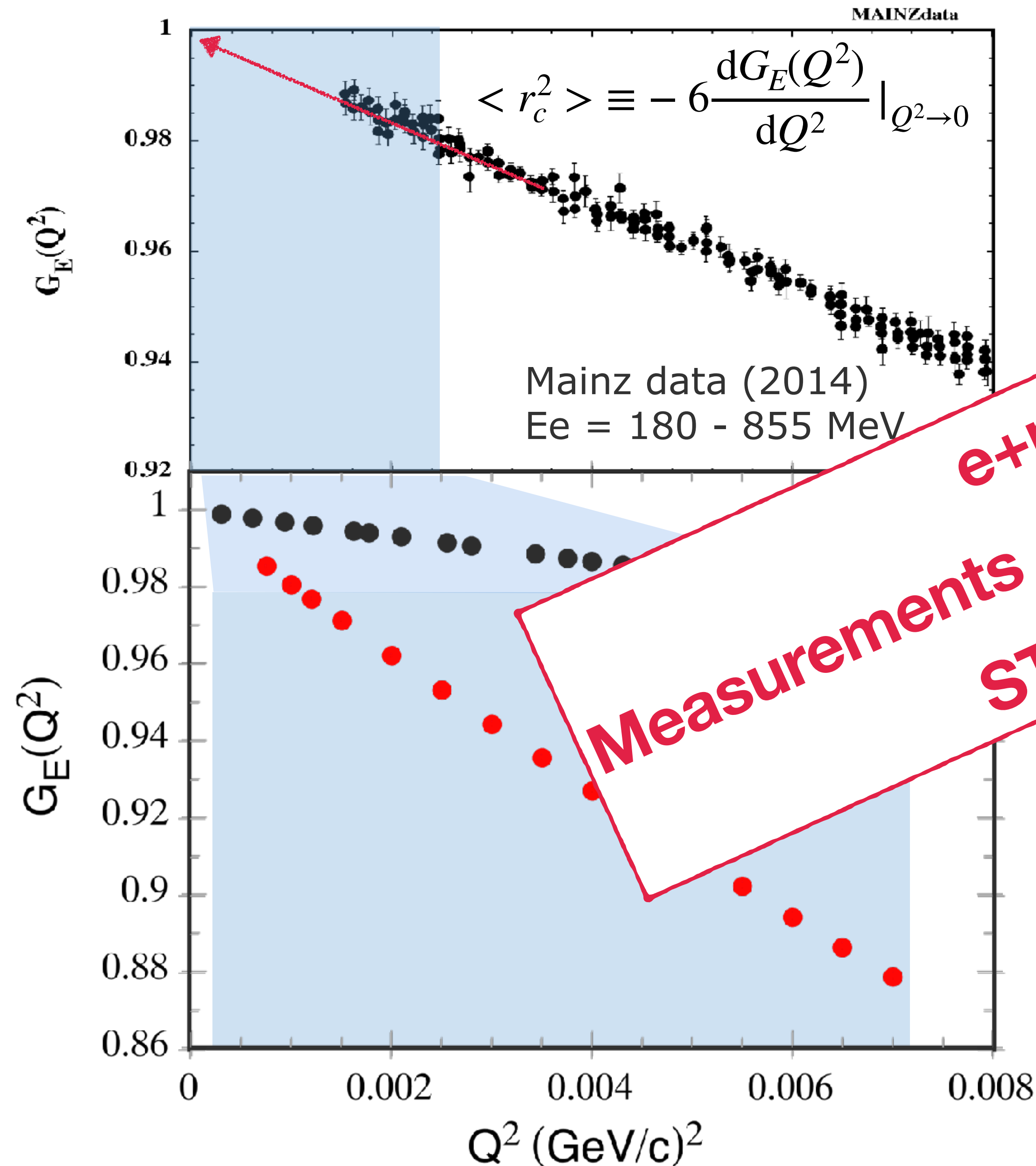


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ULQ2 theory theory  



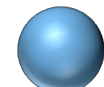
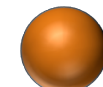
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charge radius
magnetic radius (next step)



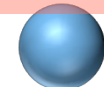
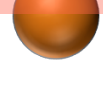
neutron charge radius
neutron charge radius



$$\langle r_d^2 \rangle = \langle r_{str}^2 \rangle + \langle r_p^2 \rangle + \langle r_n^2 \rangle + \text{RC}$$

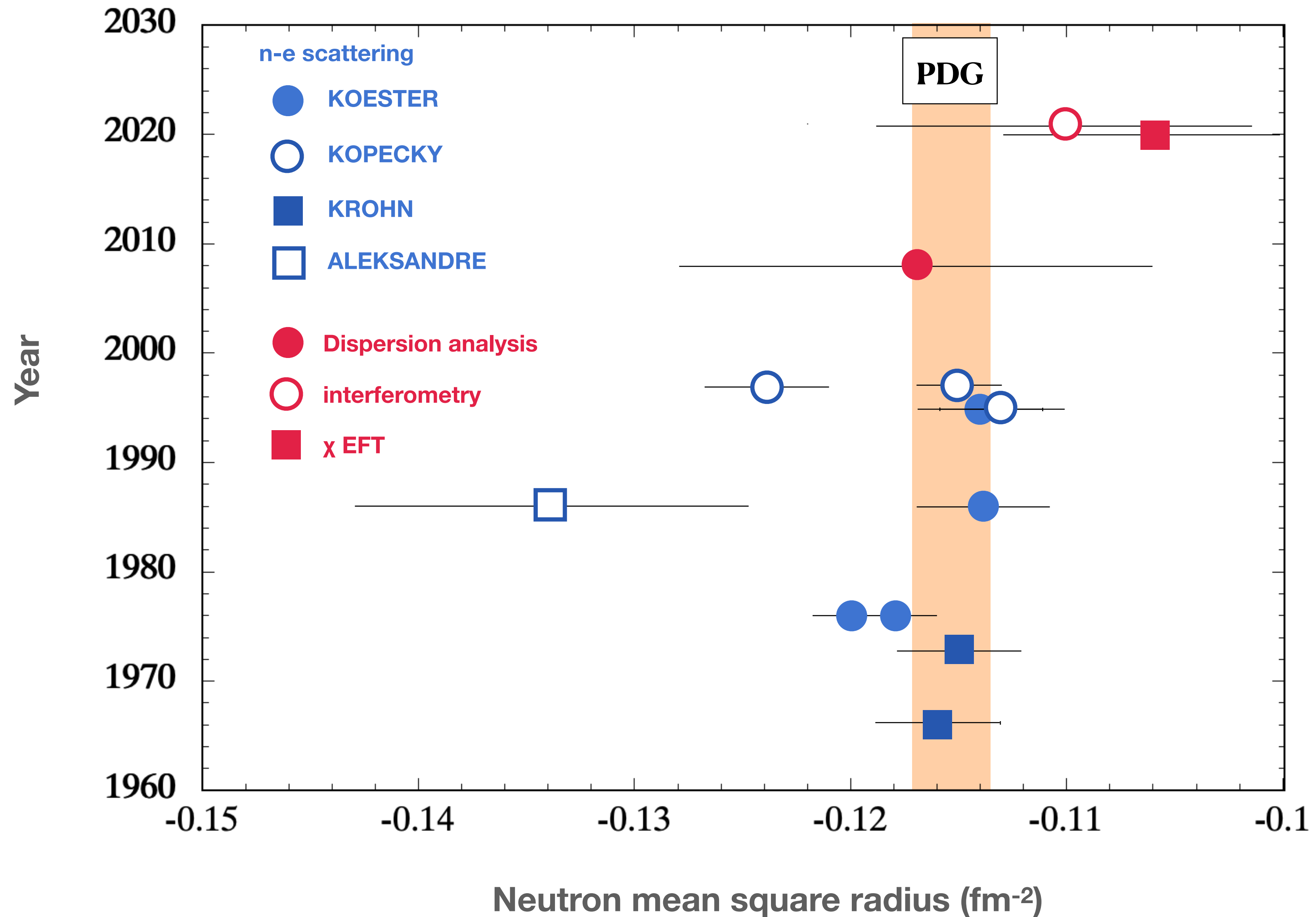
ULQ2 theory  

$$\langle r_d^4 \rangle = \langle r_{str}^4 \rangle + \frac{10}{3} \langle r_{pstr}^2 \rangle (\langle r_p^2 \rangle + \langle r_n^2 \rangle) + O(4) + \text{RC}$$

ULQ2 theory theory  

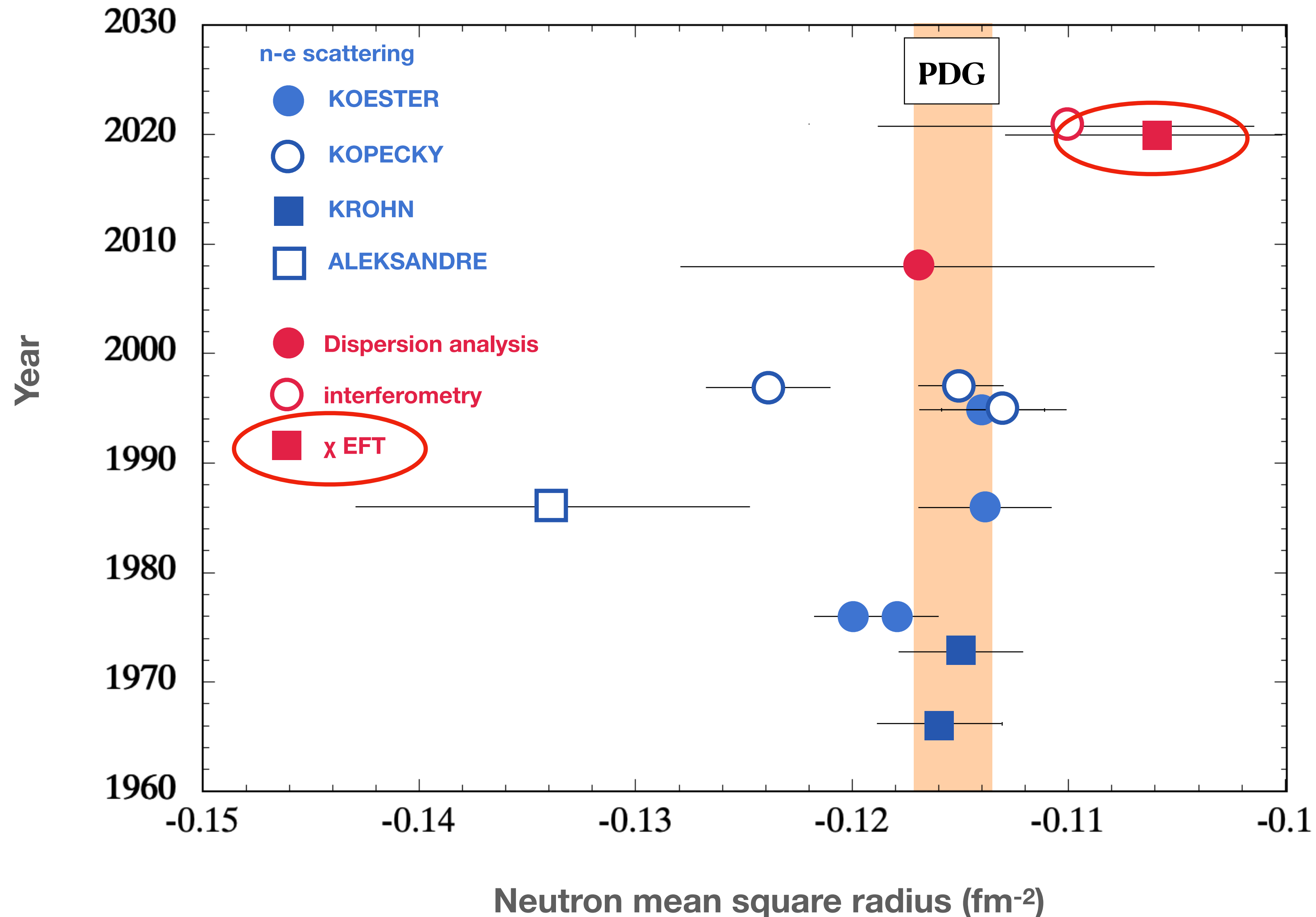
Neutron Charge Radius

中性子半径グラフ2023_KG_枠のみ



Neutron Charge Radius

中性子半径グラフ2023_KG_枠のみ



A.A. Filin et al. (Bochum G.)
Phys. Rev. Lett. 124(2020) 082501

$$\langle r_d^2 \rangle = \langle r_{str}^2 \rangle + \langle r_p^2 \rangle + \langle r_n^2 \rangle + RC$$

μD exp. theory

● Low-energy e-scattering activities in Japan

- SCRIT : started operation for online-produced radioactive isotopes
the world's first and currently only-one facility
ISOL upgrade to 2kW is underway for $^{132}\text{Sn}(e,e')$
feasibility studies for ^{46}Ar suggested to be a proton-bubble nucleus
- ULQ2 : 1) e+p, e+D scattering
data collection completed. data analysis underway

● ongoing activities and future prospects

- charge form factors of exotic nuclei
- neutron-distribution radius by electron scattering
- ^{208}Pb n-skin thickness by low-energy electron scattering

SCRIT

ULQ2