

# DIRECT MEASUREMENT OF THE $^{12}\text{C}+^{12}\text{C}$ FUSION REACTION

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On behalf of the Carbon Fusion Experiment (CARFUSE) Collaboration

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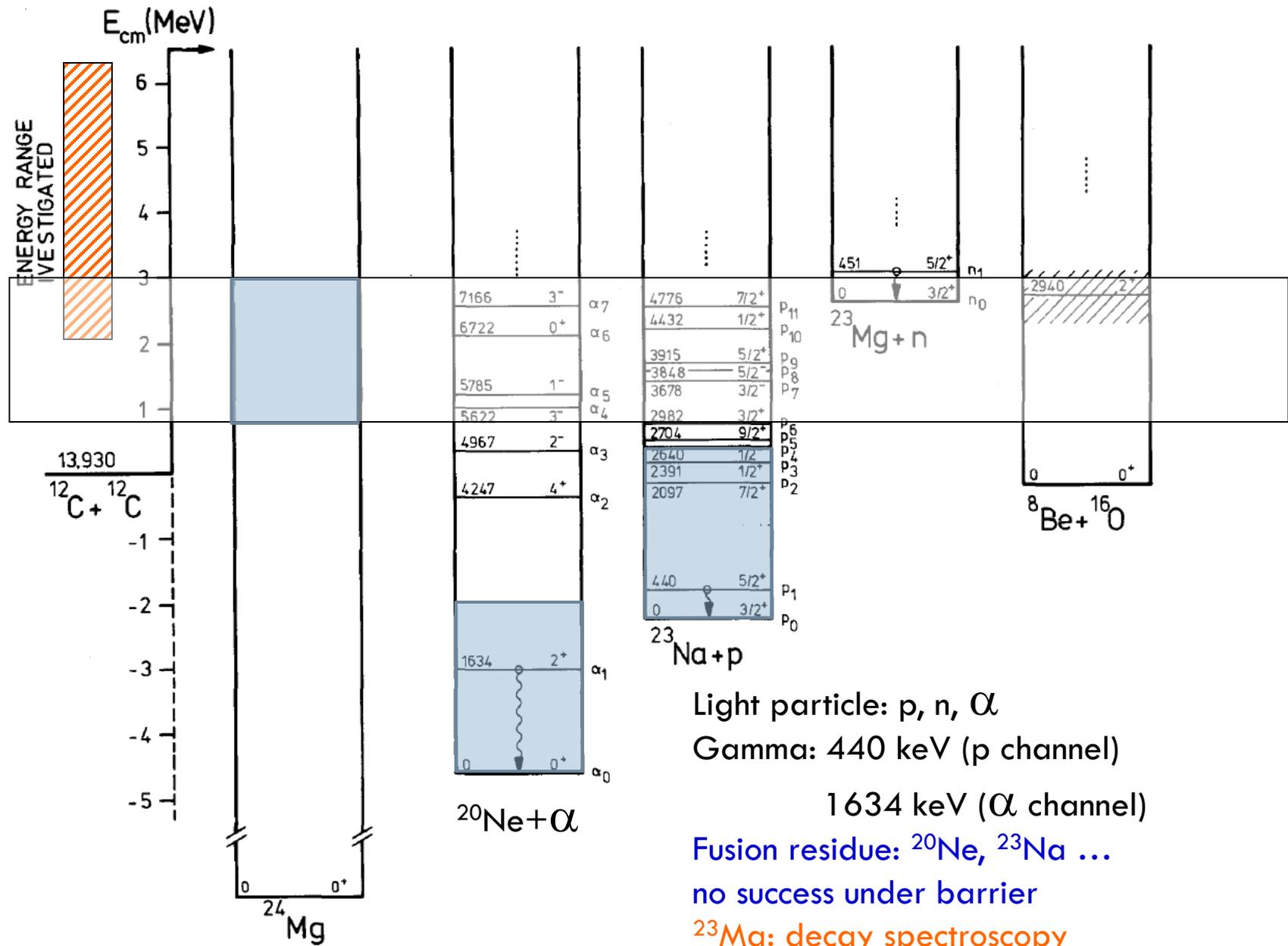
Lanzhou University and Institute of Modern Physics, CAS, China



Key reactions in nuclear astrophysics, Trento, ECT\*, Feb. 16-22, 2025

# CARbon FUSion Experiment (CARFUSE) @LEAF, IMP





Light particle: p, n,  $\alpha$

Gamma: 440 keV (p channel)

1634 keV ( $\alpha$  channel)

Fusion residue:  $^{20}\text{Ne}$ ,  $^{23}\text{Na}$  ...

no success under barrier

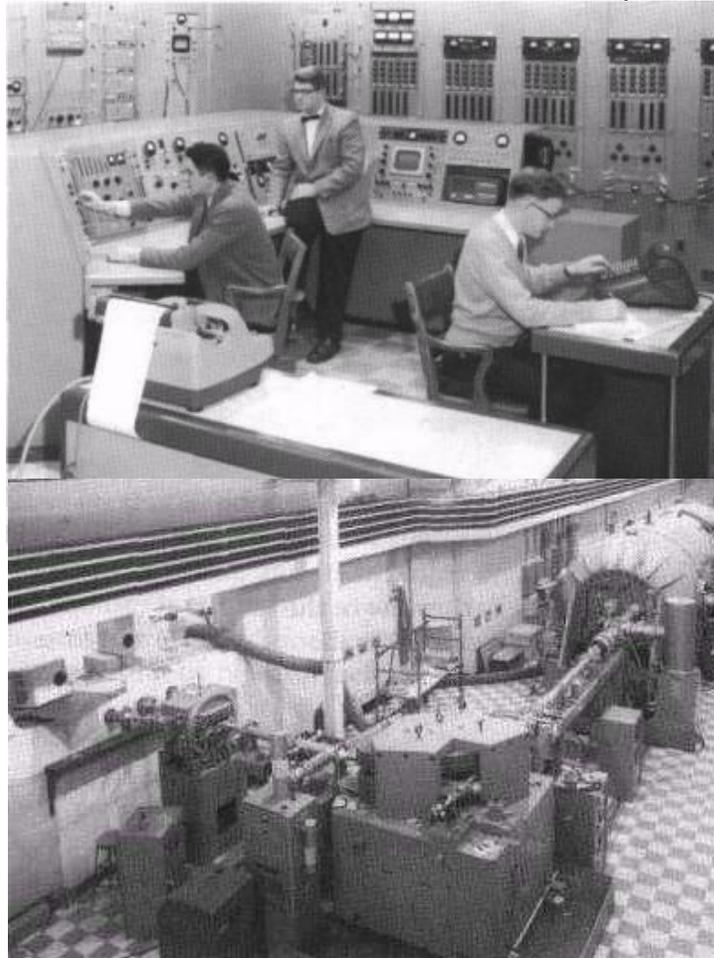
$^{23}\text{Mg}$ : decay spectroscopy

## RESONANCES IN $C^{12}$ ON CARBON REACTIONS

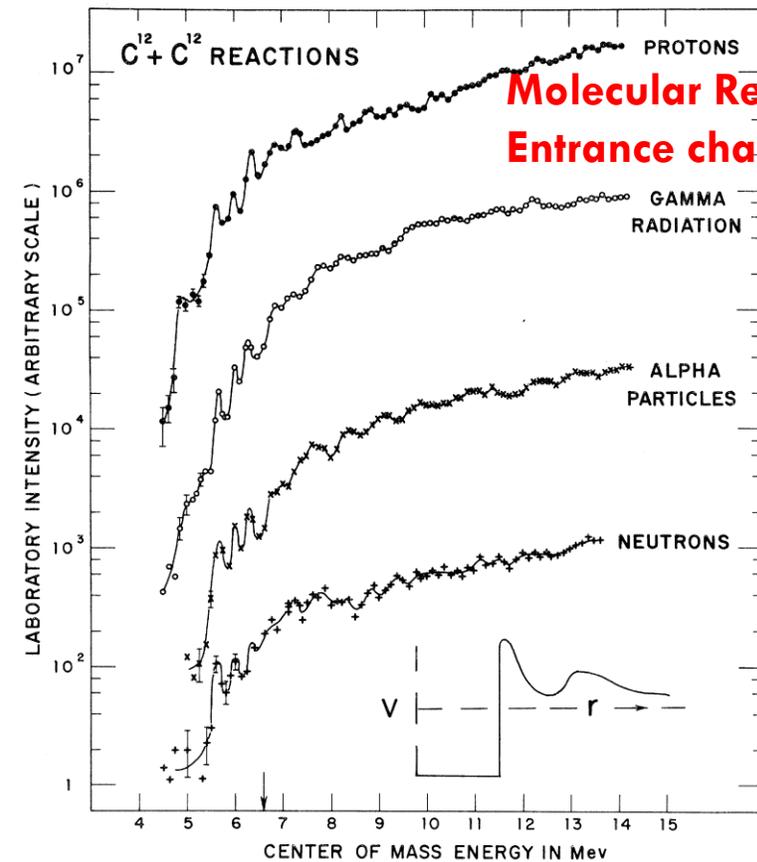
E. Almqvist, D. A. Bromley, and J. A. Kuehner

Atomic Energy of Canada Limited, Chalk River Laboratories, Chalk River, Ontario, Canada

(Received March 28, 1960)



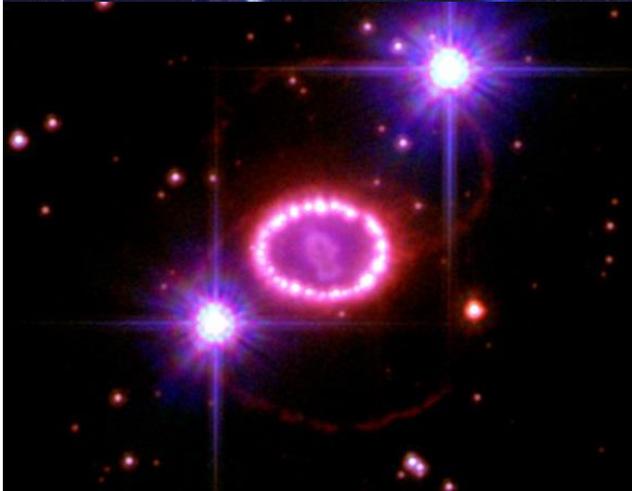
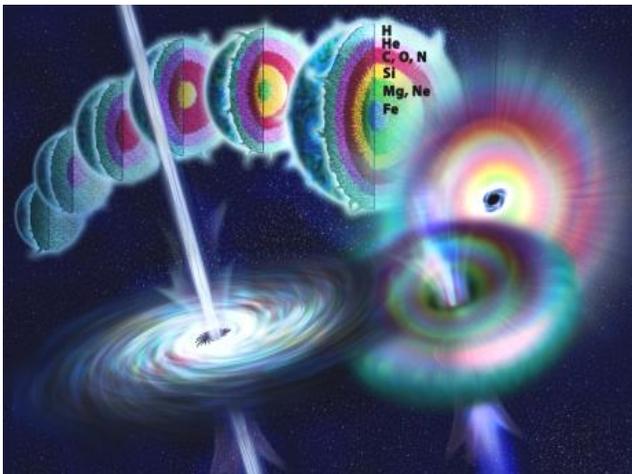
The world's first tandem accelerator installed at Chalk River in 1959.



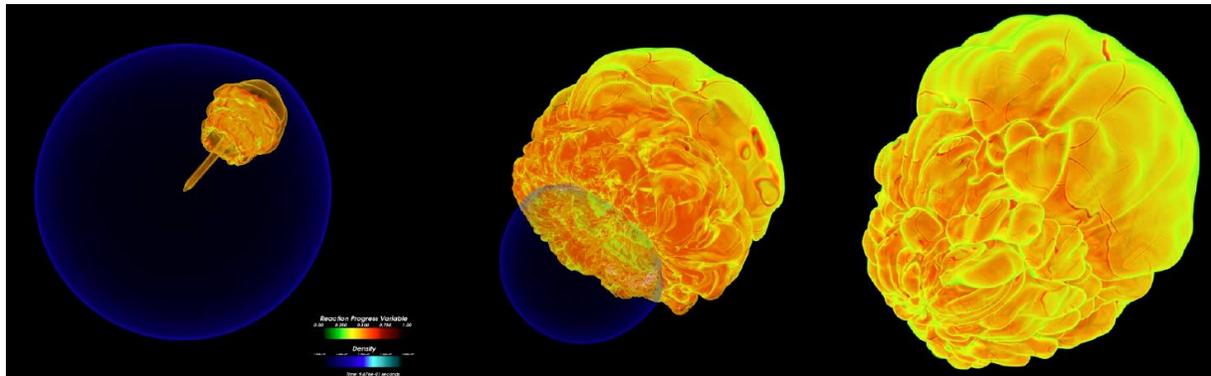
**Molecular resonances** in the  $^{12}C+^{12}C$  fusion reaction measured by Almqvist et al., in 1960

# Carbon burning in the universe

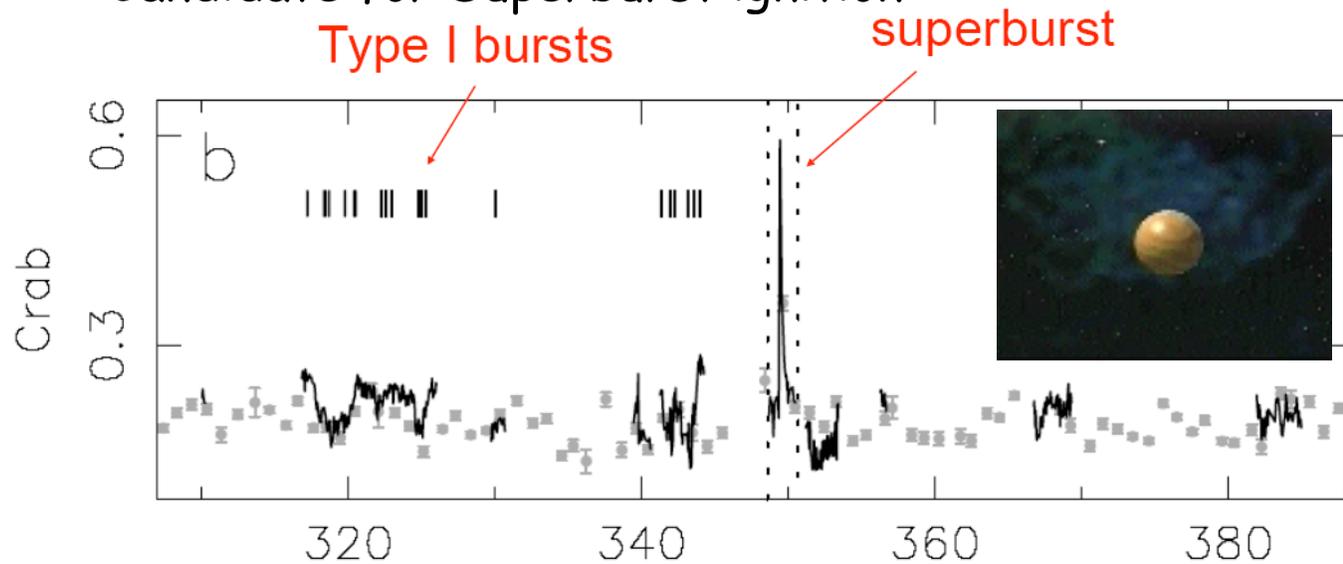
Nucleosynthesis in massive stars



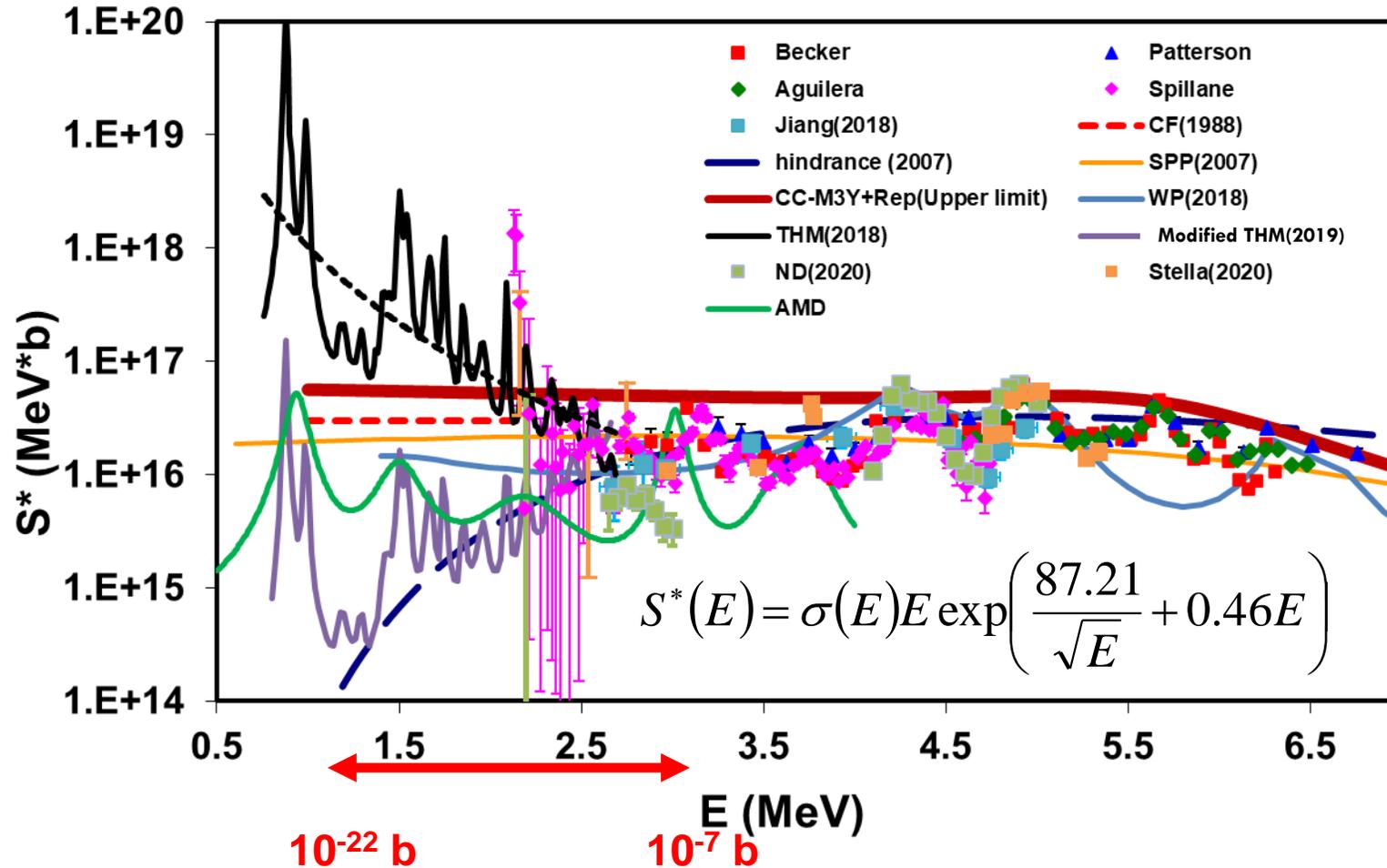
Ignition conditions in type Ia supernovae



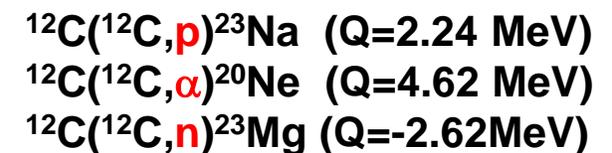
Candidate for Superburst ignition



# Uncertain cross section at stellar energies



- Large difference between THM and Hindrance  $\rightarrow$  Highly uncertain rate
- **INDIRECT:** Corrected THM exhibits a trend similar to Hindrance by replacing PWIA with DWIA
- Unknow resonances: Need better selection  $T=0, J^\pi=0^+, 2^+$

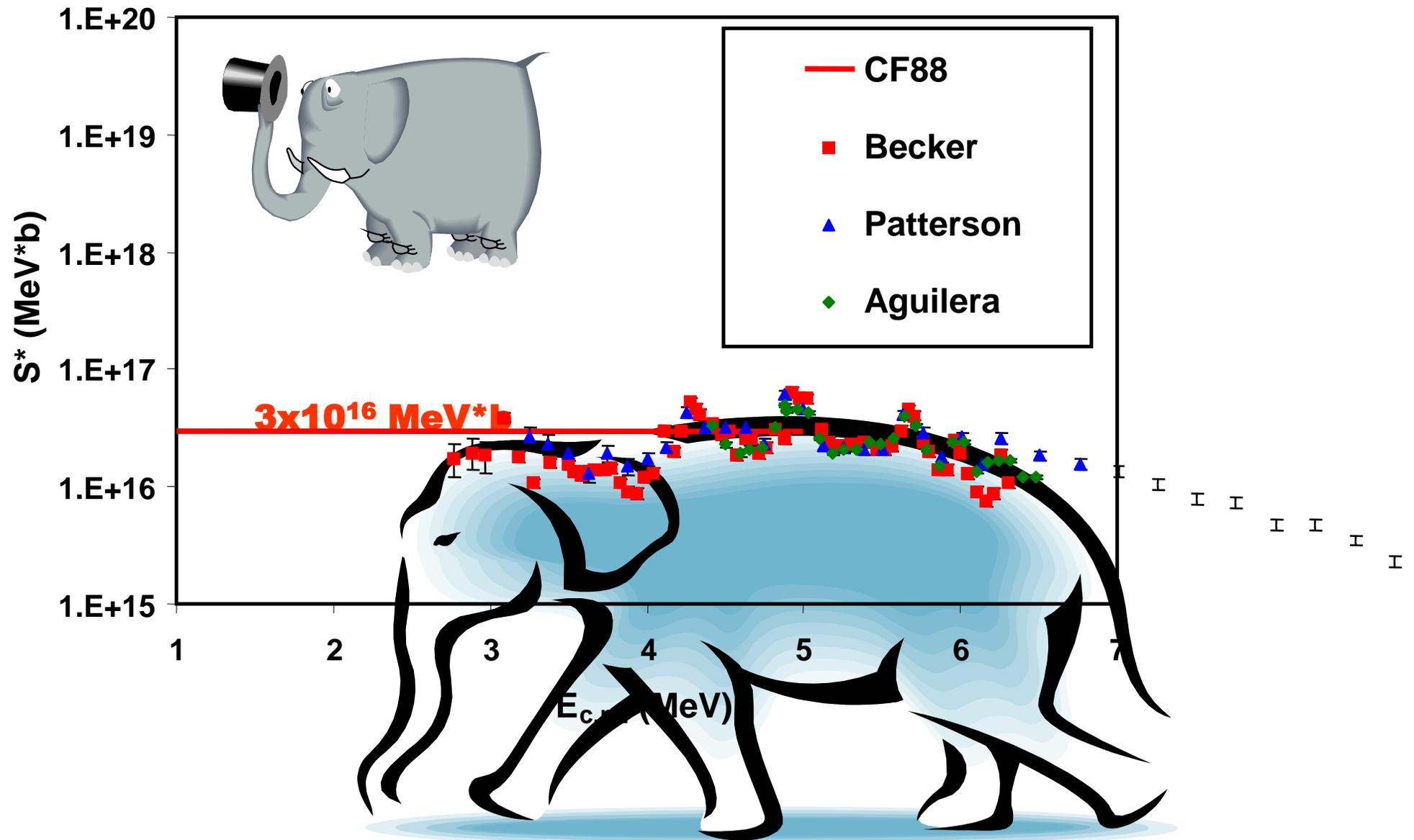


Beck, Mukhamedzhanov and Tang, Eur. Phys. J. A (2020) 56:87

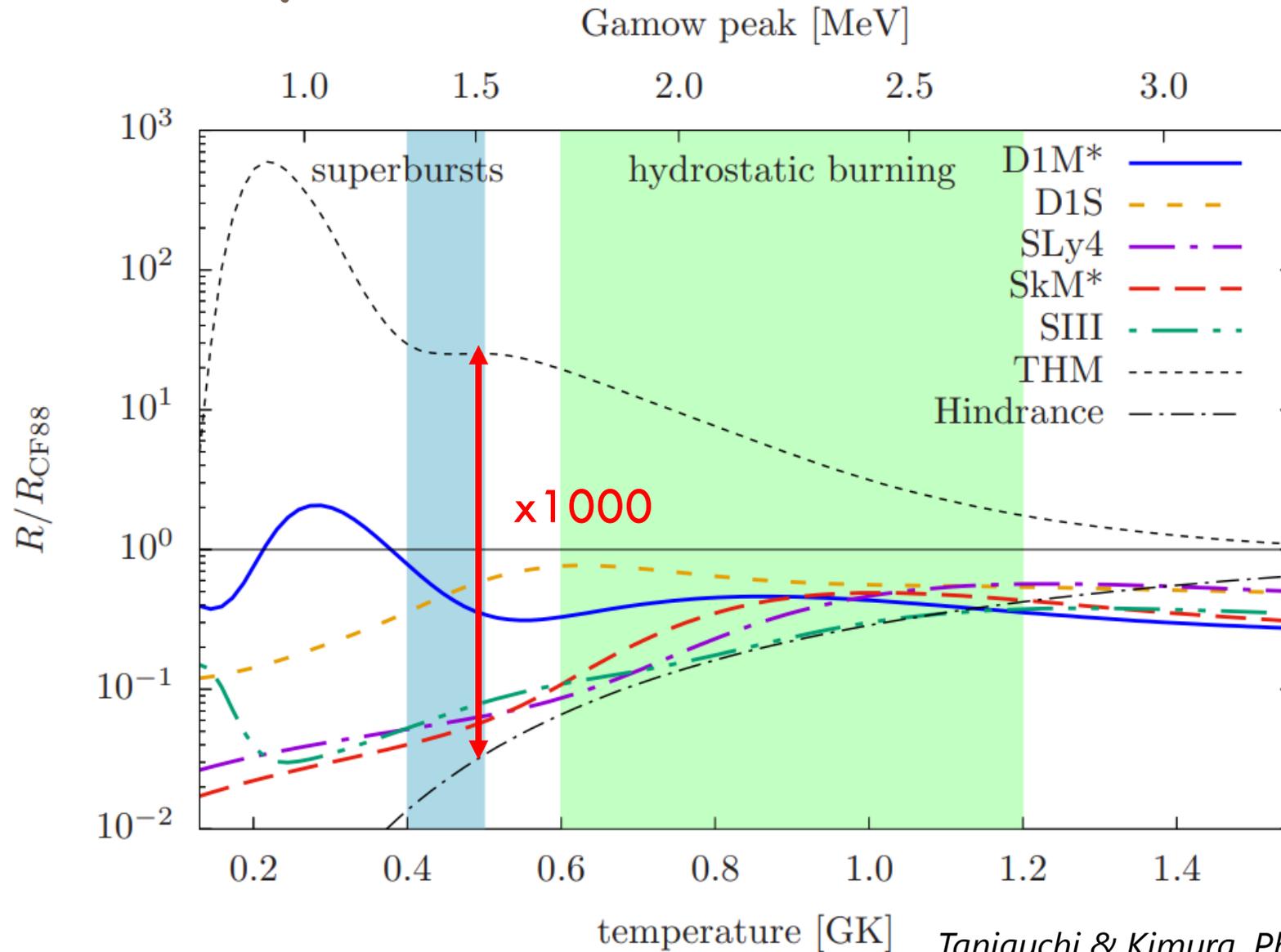
Mukhamedzhanov, Eur. Phys. J. A (2022) 58:71

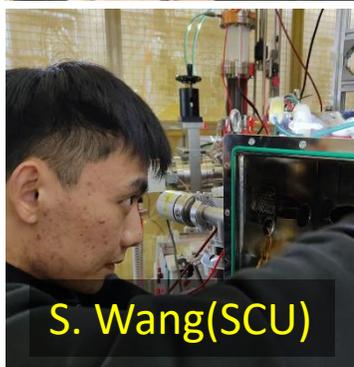
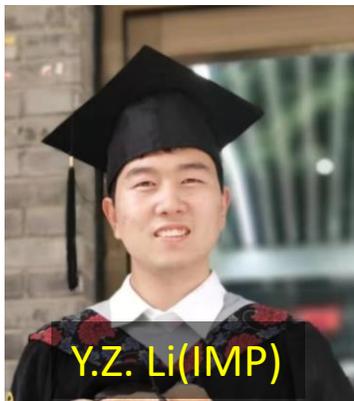
Tang & Ru, EPJ Web of Conferences 260, 01002 (2022)

$$S^*(E) = \sigma E e^{(87.21/\sqrt{E} + 0.46E)}$$



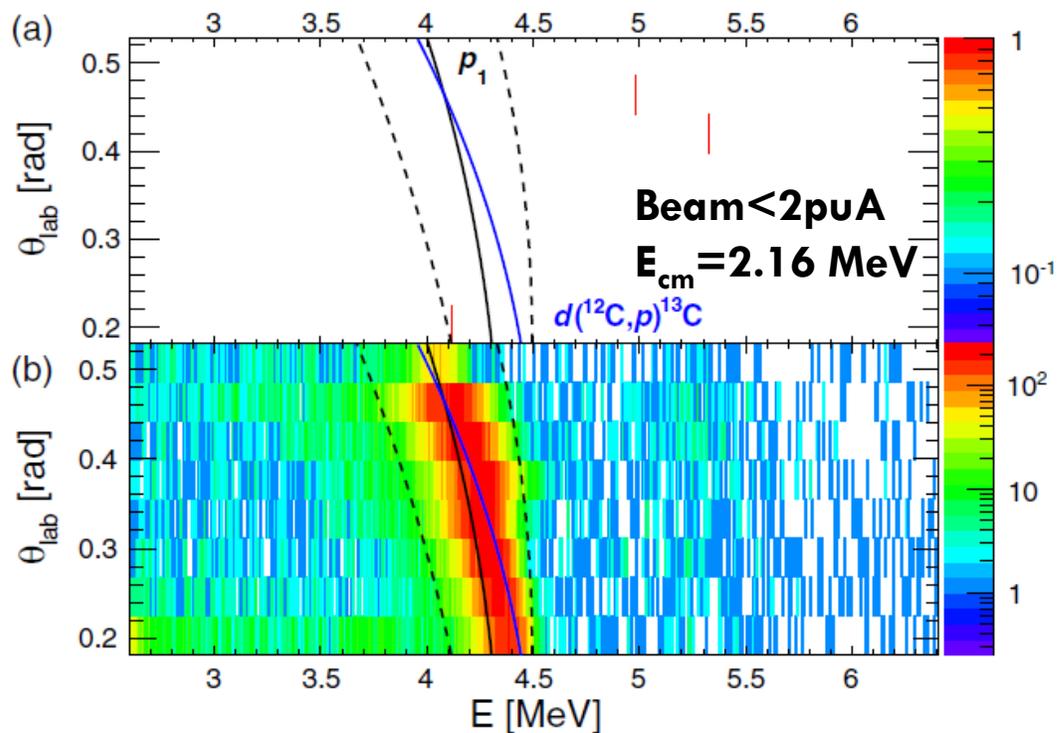
# Uncertainty in the reaction rate



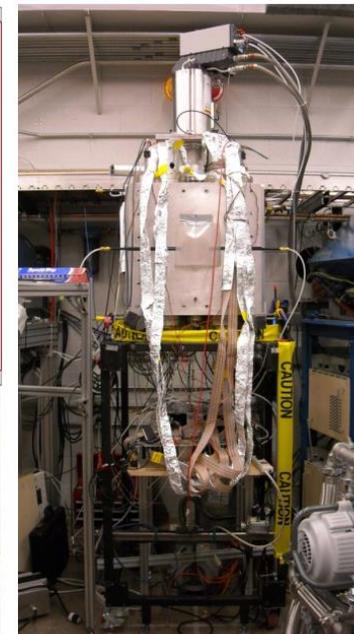
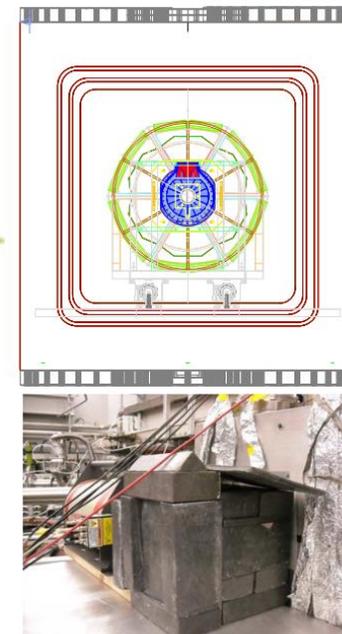
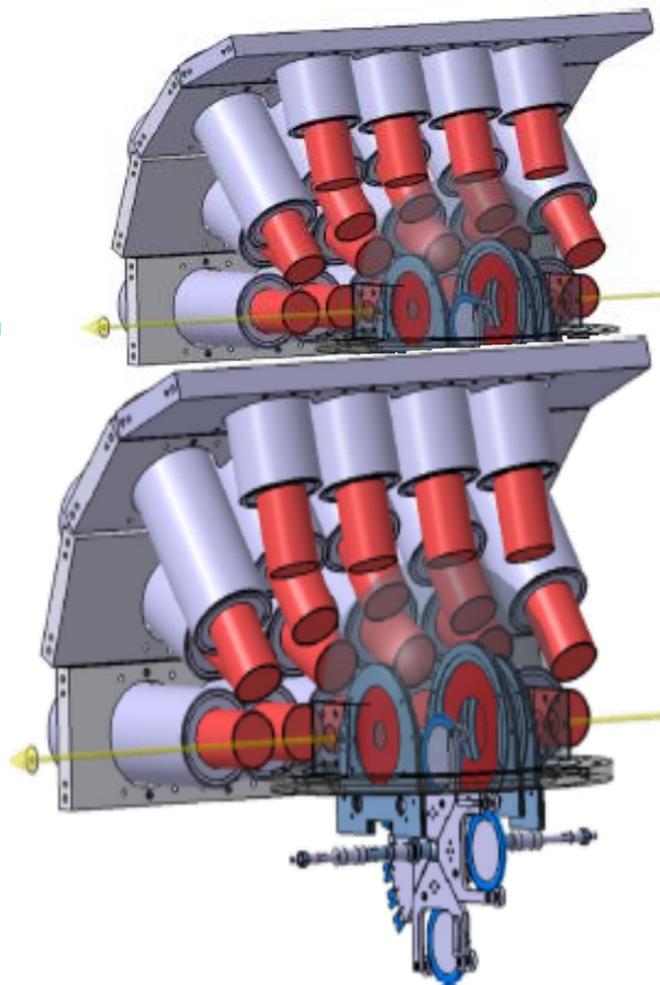


# Direct Measurement of $^{12}\text{C}(^{12}\text{C},\alpha_{0,1})^{20}\text{Ne}$

# Particle- $\gamma$ coincidence at lower stellar energies



Fruet+ PRL(2020)



Beam < 15 puA

Jiang et al. (2012), Jiang et al. (2018)  
Heine et al. (2018), Tan et al. (2021),  
Fruet et al. (2021)

- Particle- $\gamma$  coincidence technique pushed the measurement down to **sub-nb level**
- Only detect  **$p_1$  and  $\alpha_1$  channels**

# Carbon fusion project at LUNA-MV

Massive lead shield and radon flushing → push sensitivity to better than 100 reactions/day



## $^{12}\text{C} + ^{12}\text{C} - \gamma$ measurements

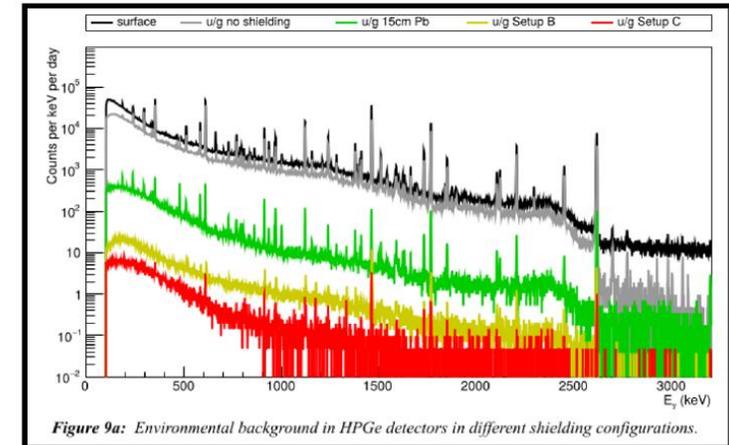


Figure 9a: Environmental background in HPGe detectors in different shielding configurations.

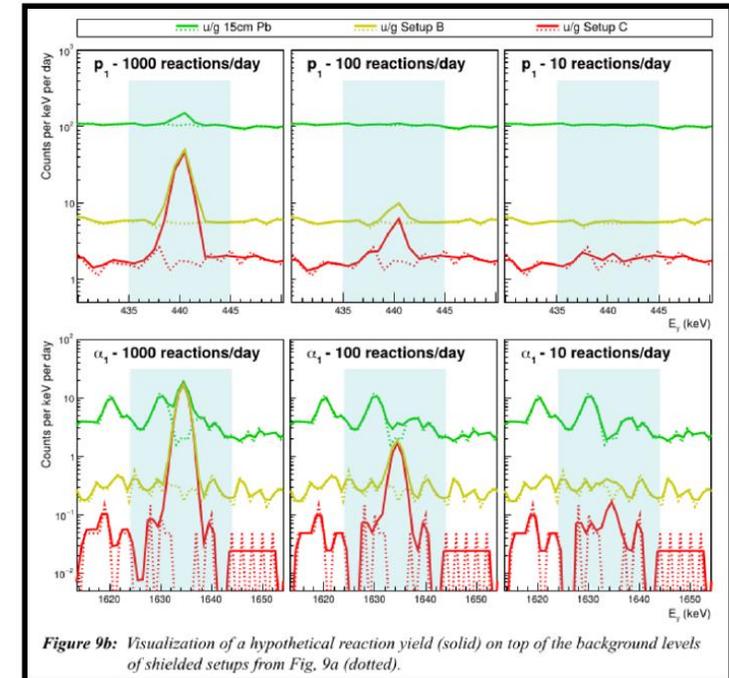
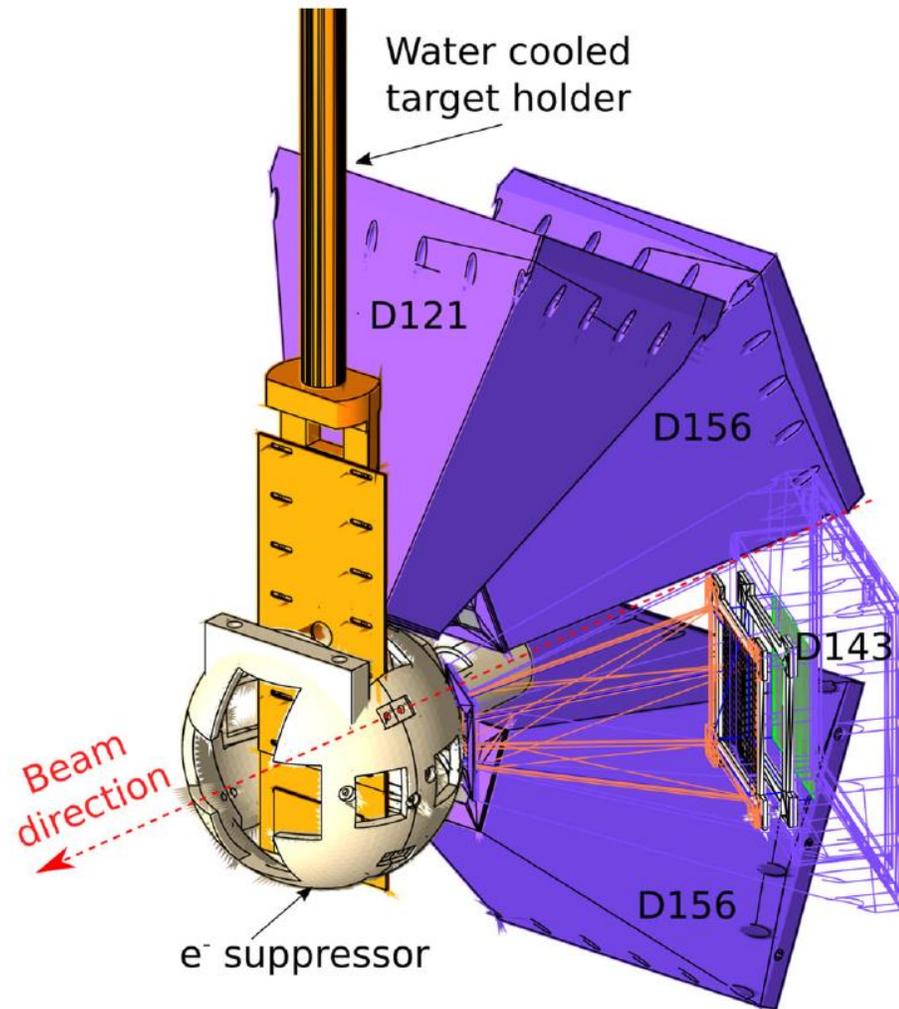
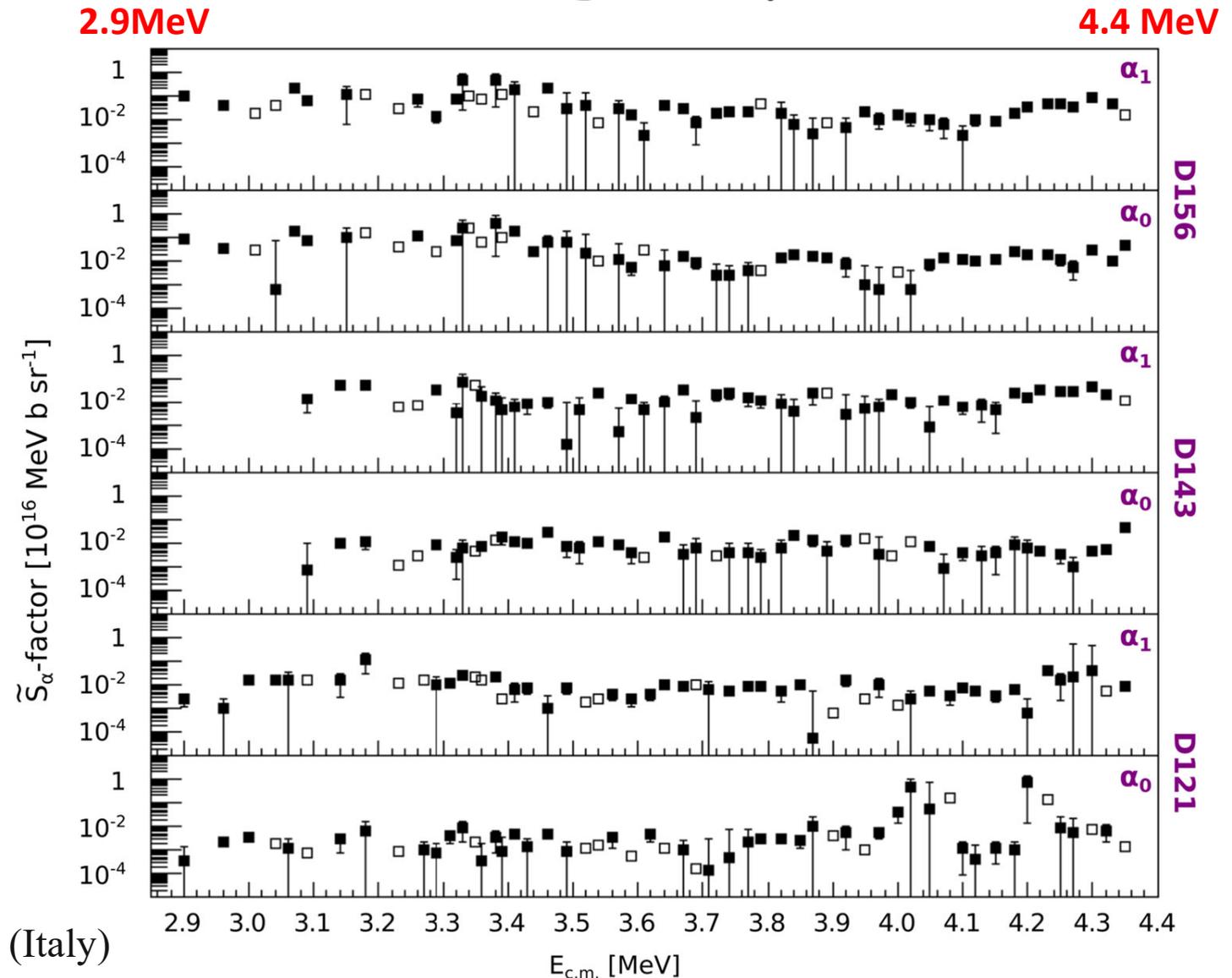


Figure 9b: Visualization of a hypothetical reaction yield (solid) on top of the background levels of shielded setups from Fig. 9a (dotted).

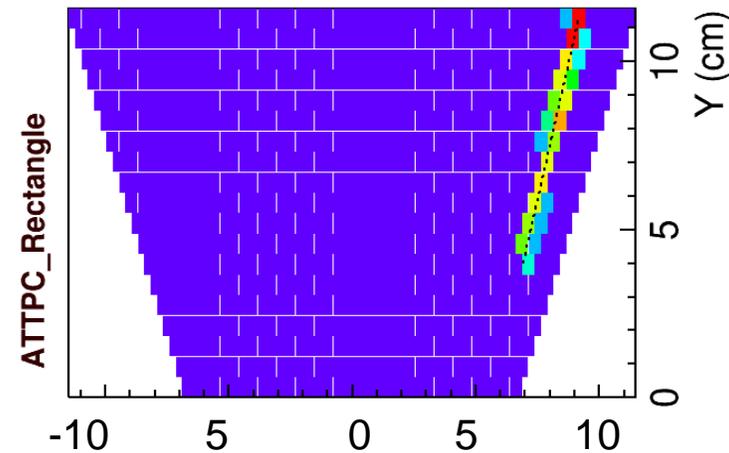
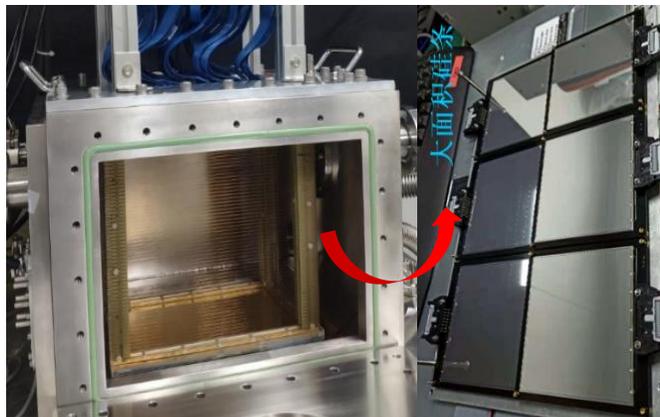
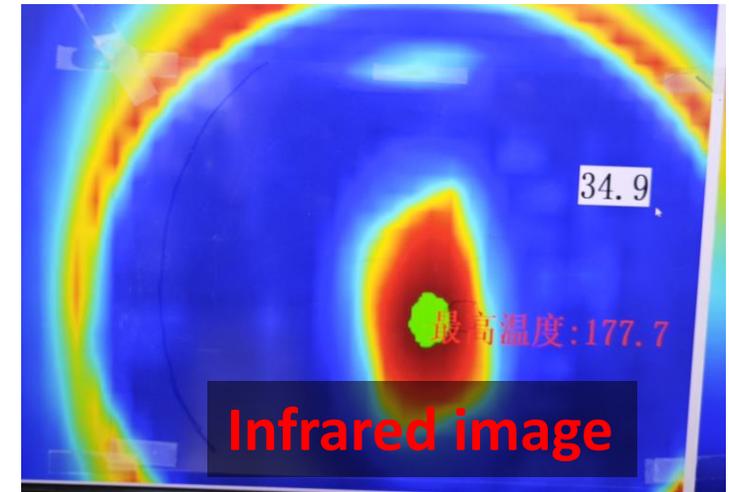
# Direct measurement with charged particles



CIRCE Tandem Accelerator Laboratory in Caserta (Italy)



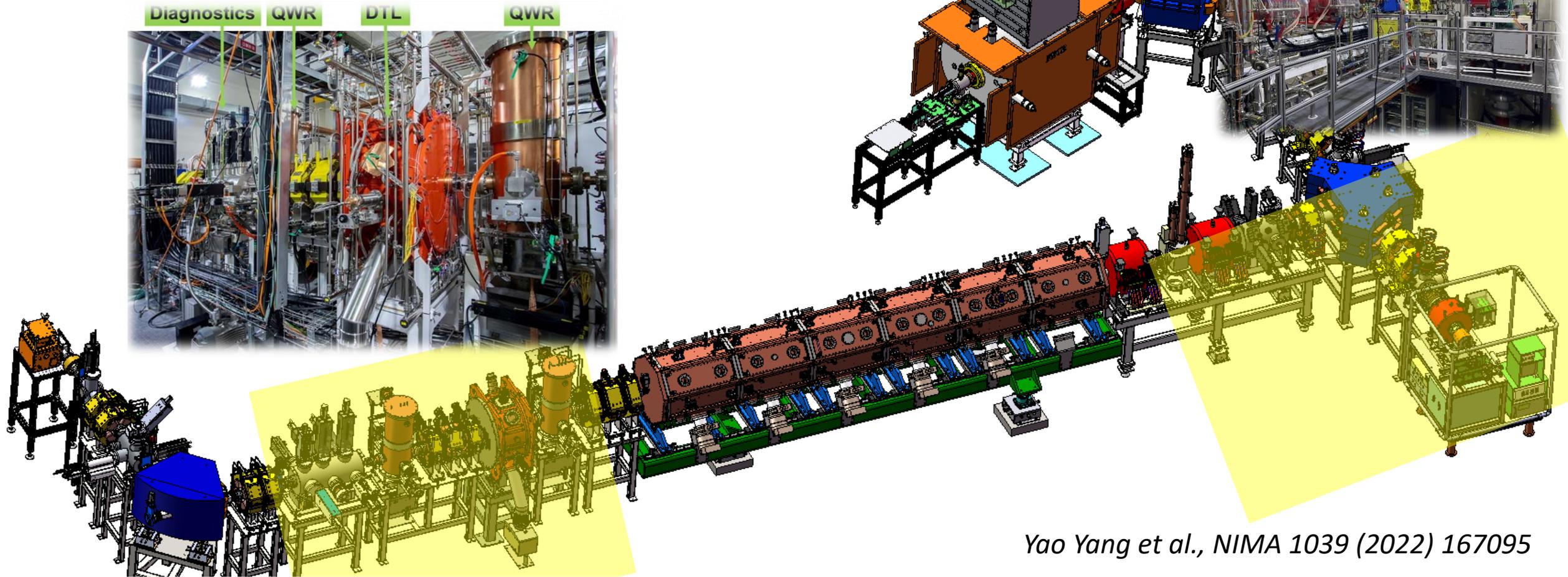
# High Intensity+Time Projection Chamber



- **LINAC**: High Intensity beam up to few hundreds of puA
- **TPC**: Ultra sensitive tracking detector
- **Complementary** to LUNA-MV and other experiments

Z.C.Zhang+ NIMA(2021)  
Doi: 10.1016/j.nima.2021.165740

# Low Energy Heavy Ion Accelerator Facility(LEAF)



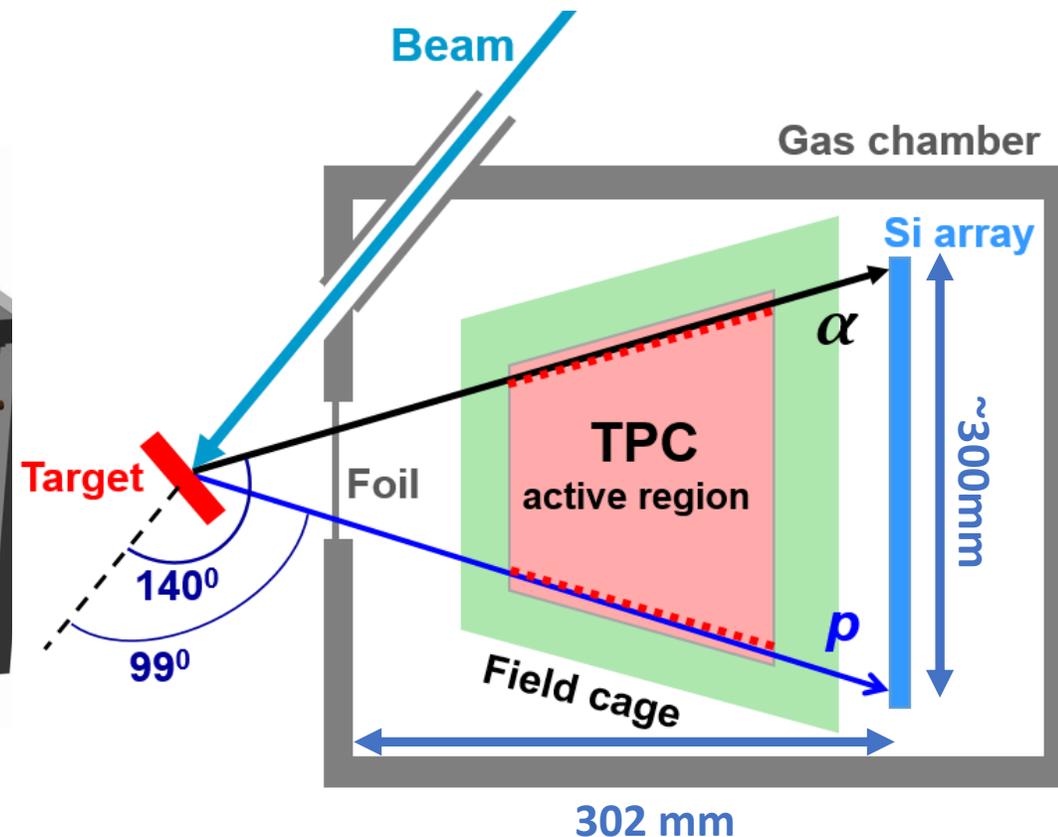
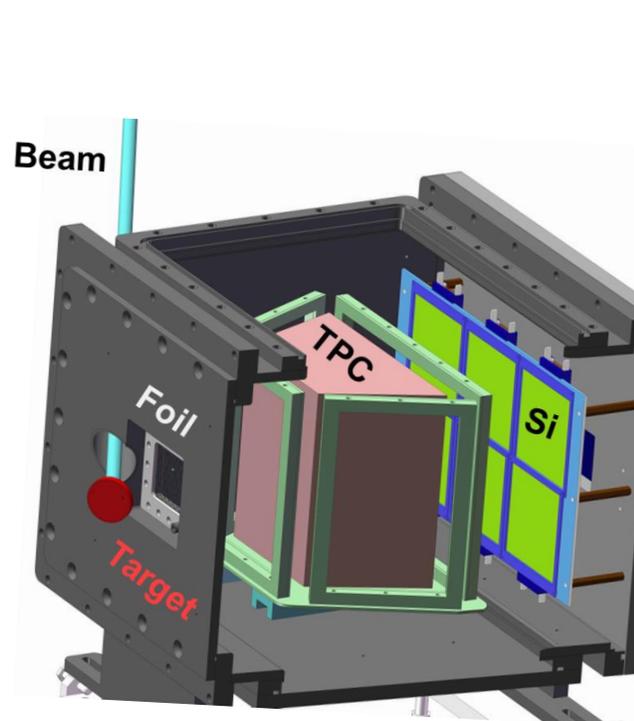
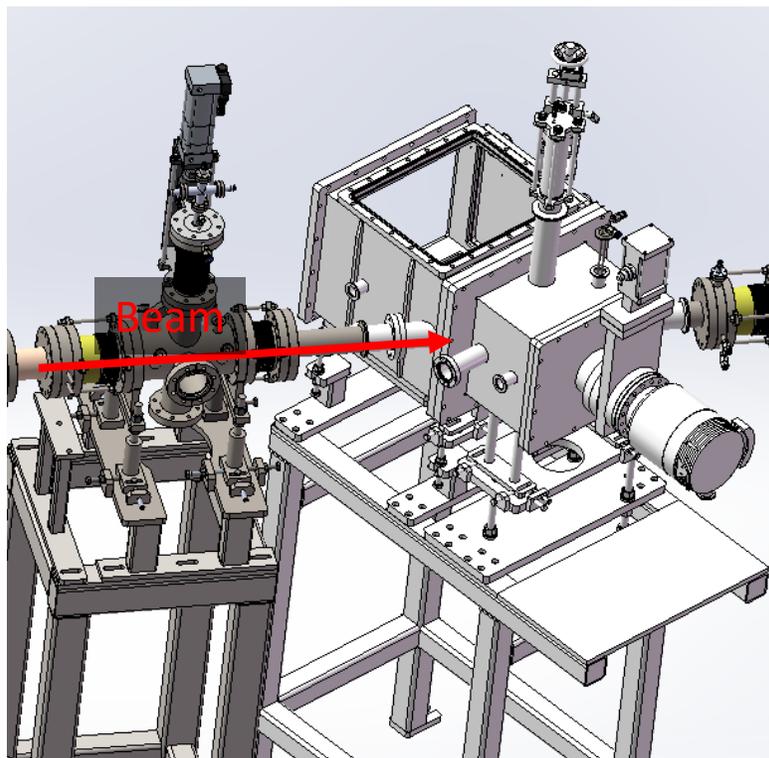
Yao Yang et al., NIMA 1039 (2022) 167095

- LEAF: 45GHz and 14.5GHz ECRs; 0.5MeV/u RFQ; 0.3MeV/u-0.7MeV/u DTL; Energy calibration by  $^{12}\text{C}(p,g)$ ,  $p(15\text{N},\alpha)^{12}\text{C}^*$
- Maximum carbon beam intensity on target:  $\sim 200 \text{ puA}$  (Spillane: 40puA); Energy Spread:  $< 0.2\%(s)$ ; Energy step size:  $\sim 50 \text{ keV}$ ; beam time:  $\sim 1150 \text{ hr}$

Courtesy of Yao Yang (IMP)

# Detector setup

Time Projection Chamber (TPC) + Si array } **Background suppression via tracking**  
**Particle identification**



# X-ray and other beam induced background

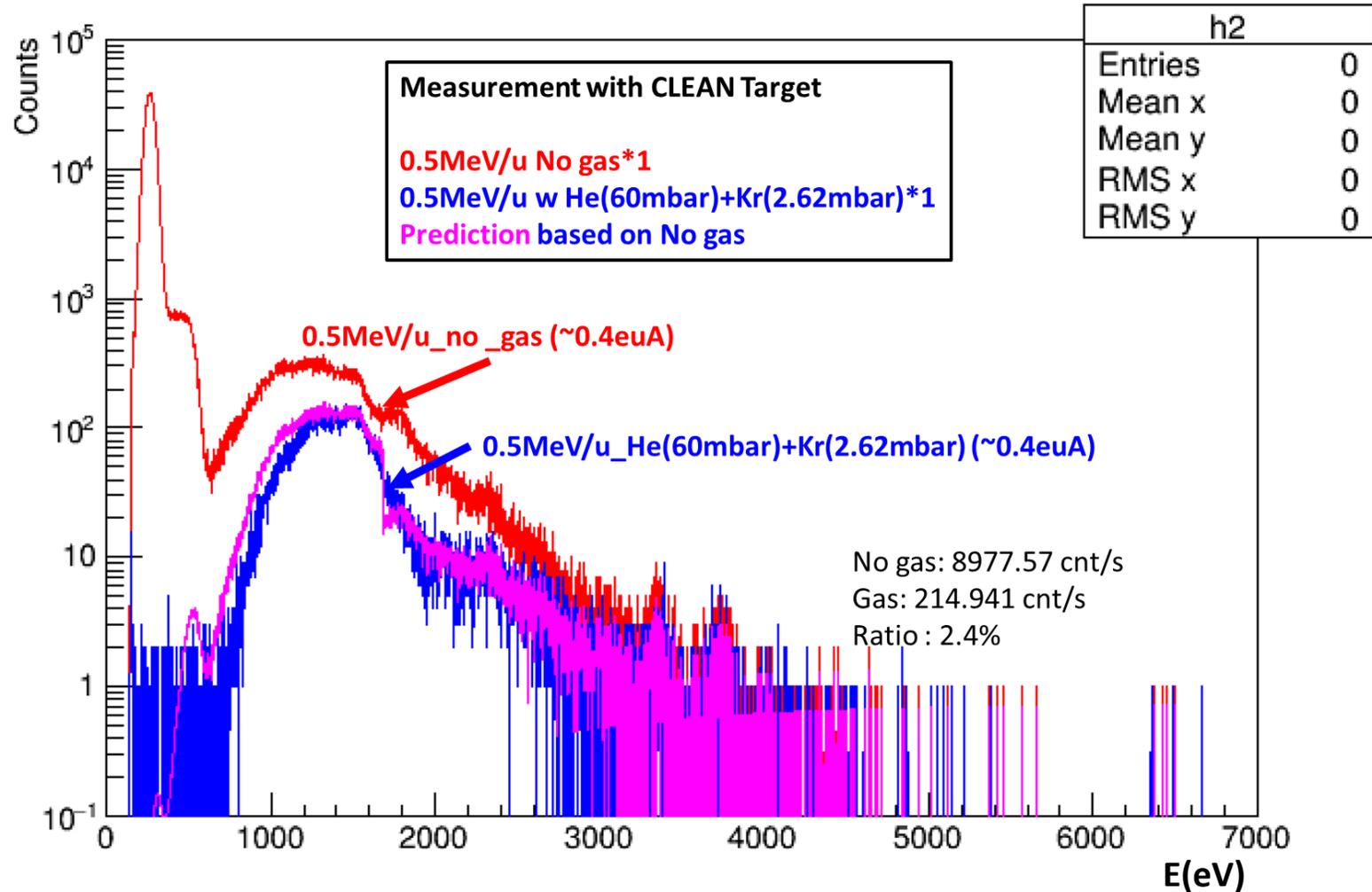


Z.Y. Zhang (USTC)

N.T. Zhang (IMP)

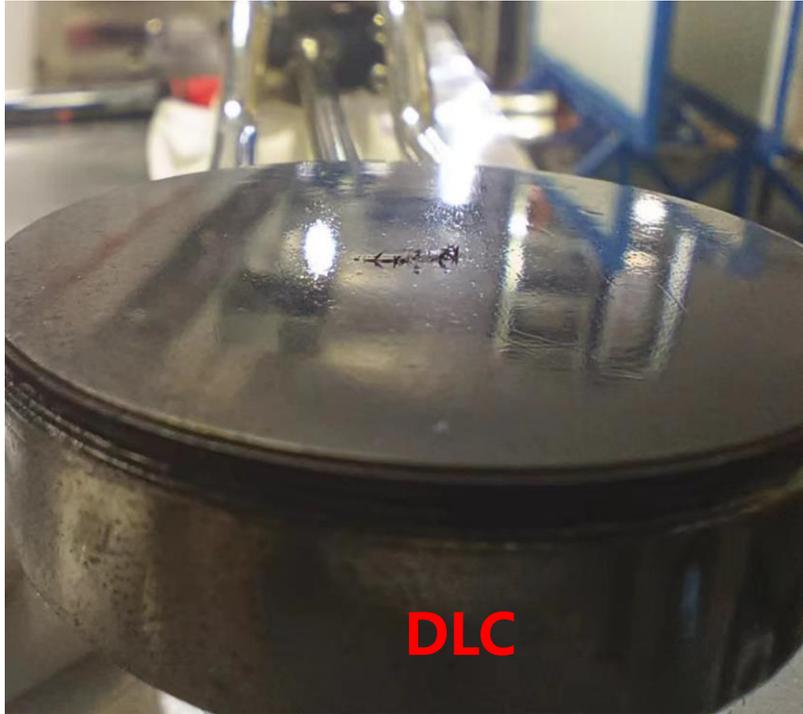


C.J. Shao (IMP)



- Using MicroMegas gas to control the Ion Back Flow(IBF)
- Alpha: Ar(5%)+CO2(5%)+He(90%); Proton: Ar(35%)+CO2(15%)+Kr(50%)

# High Power Carbon with High Purity



**DLC**



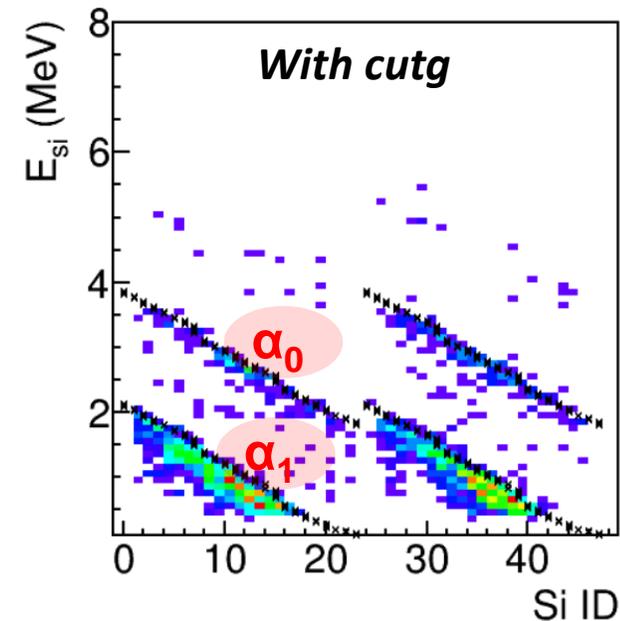
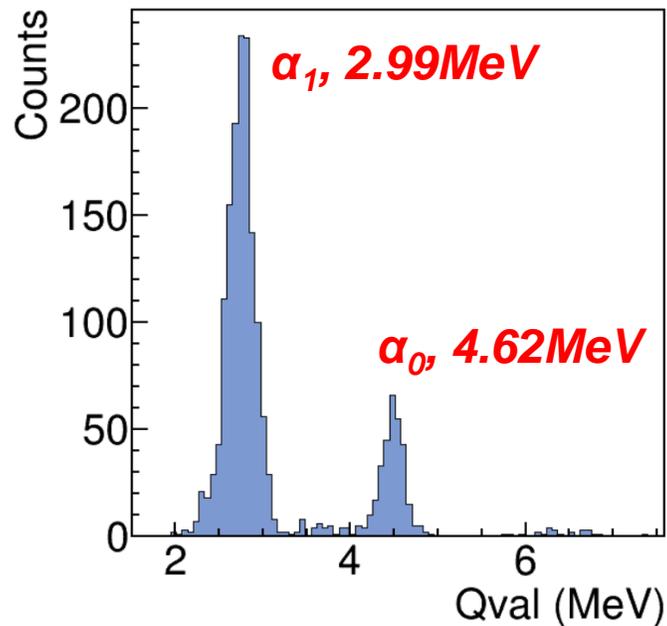
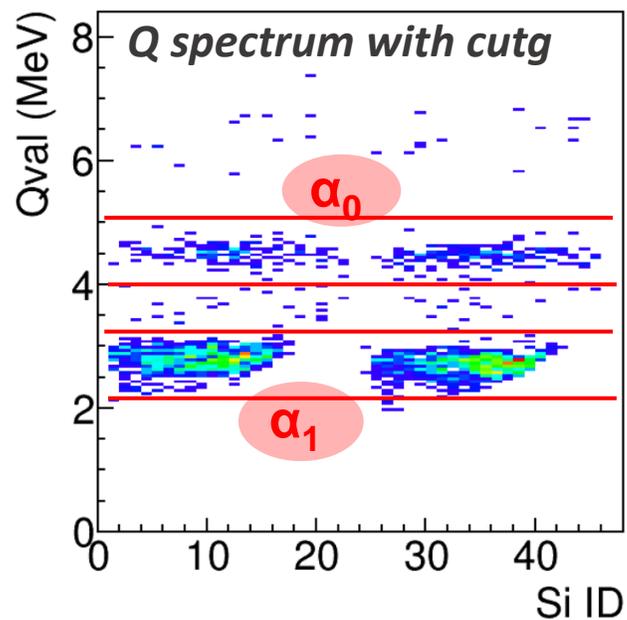
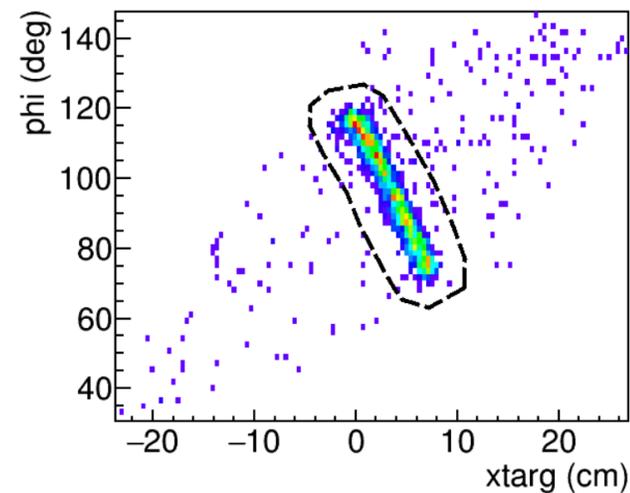
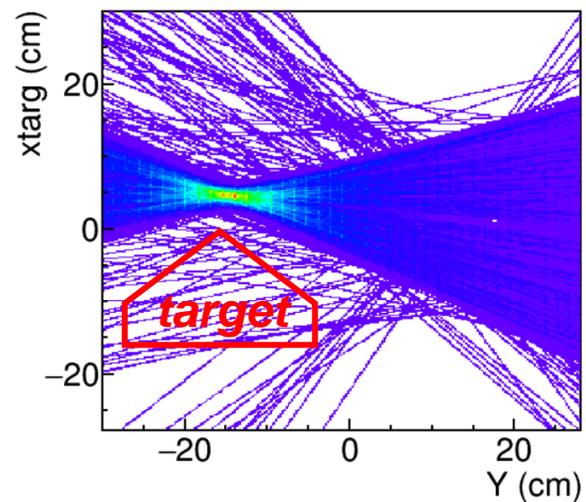
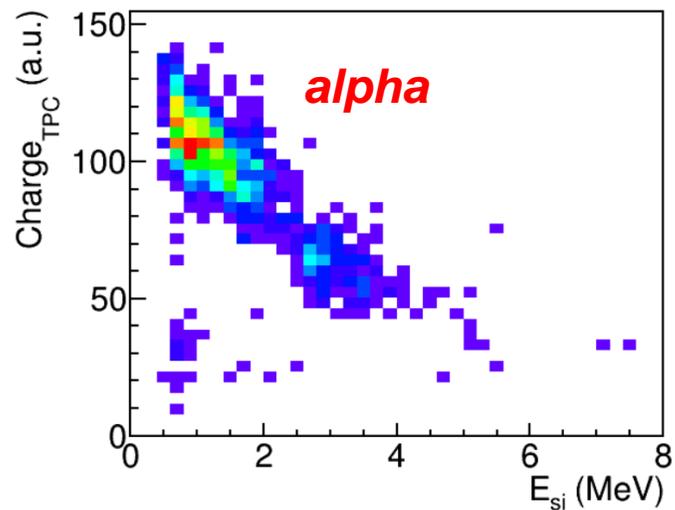
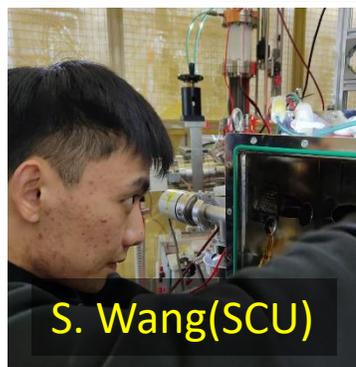
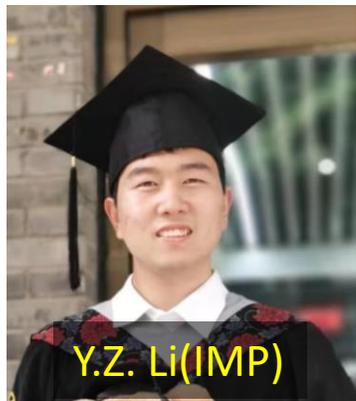
**Graphite (5N)**



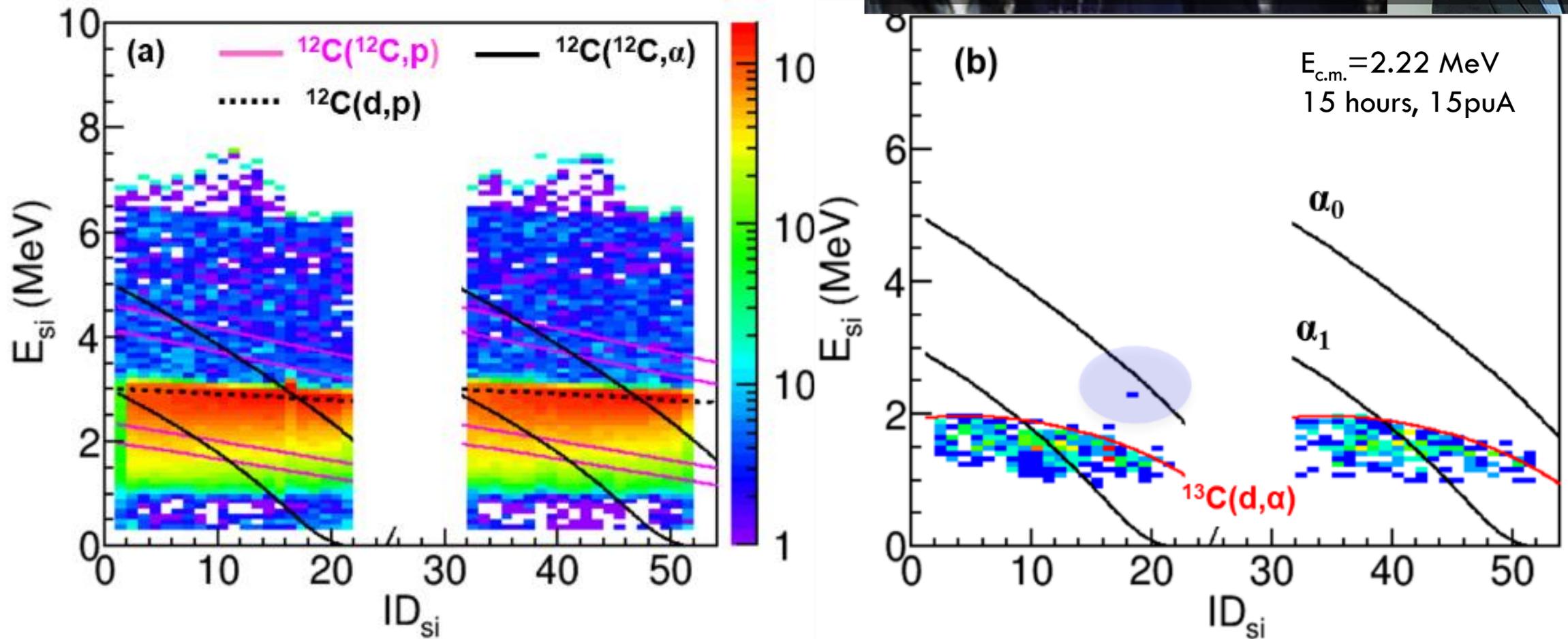
**HOPG**

- Improving thermal conductivity using flexible graphene
- Carbon targets: Diamond like carbon(DLC), Heated graphite (5N), Highly Ordered Pyrolytic Graphite High (HOPG)

# Analysis: $E_{cm}=2.72\text{MeV}$ with Graphite (5N)

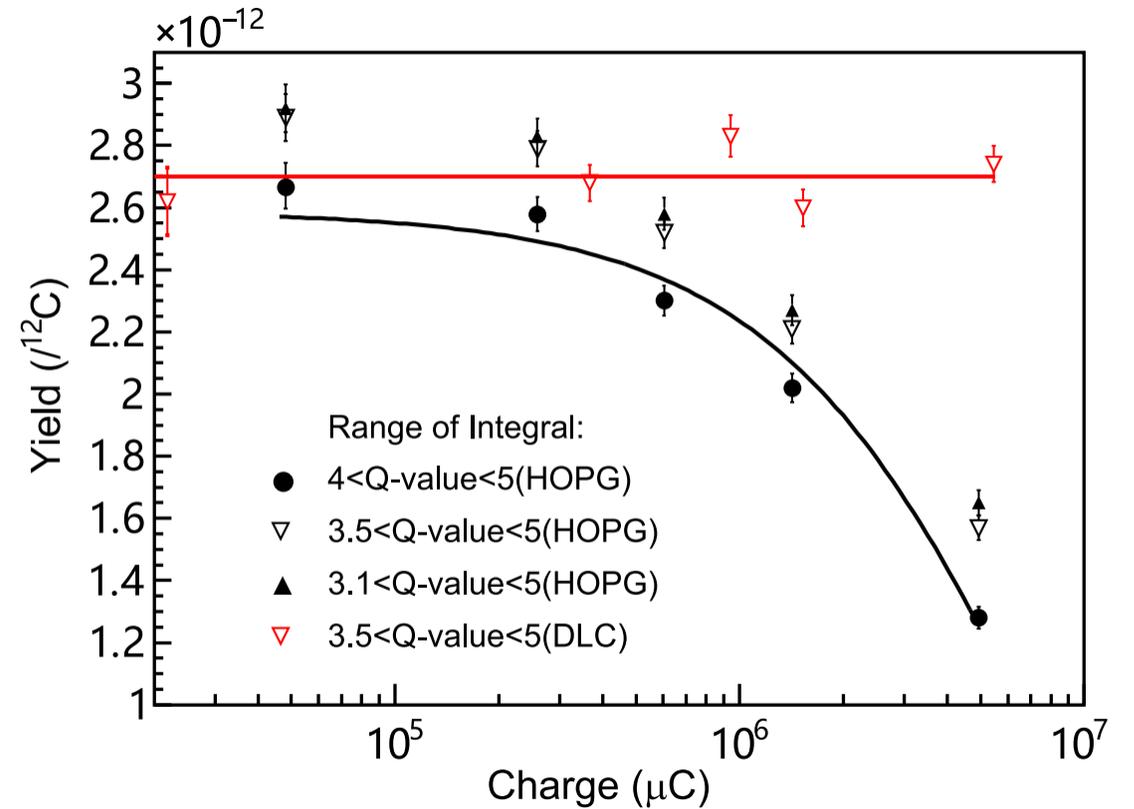
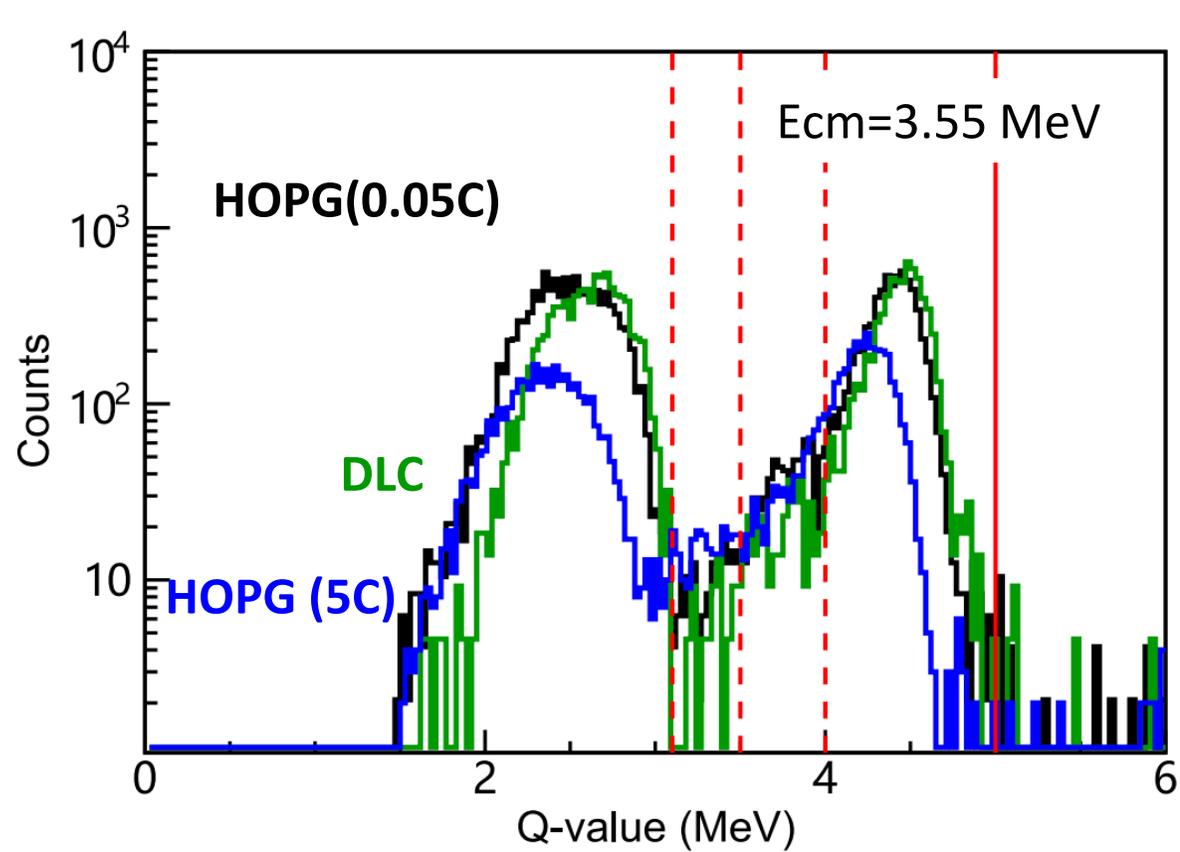


# Another result with HOPG @ $E_{c.m.}=2.2\text{MeV}$

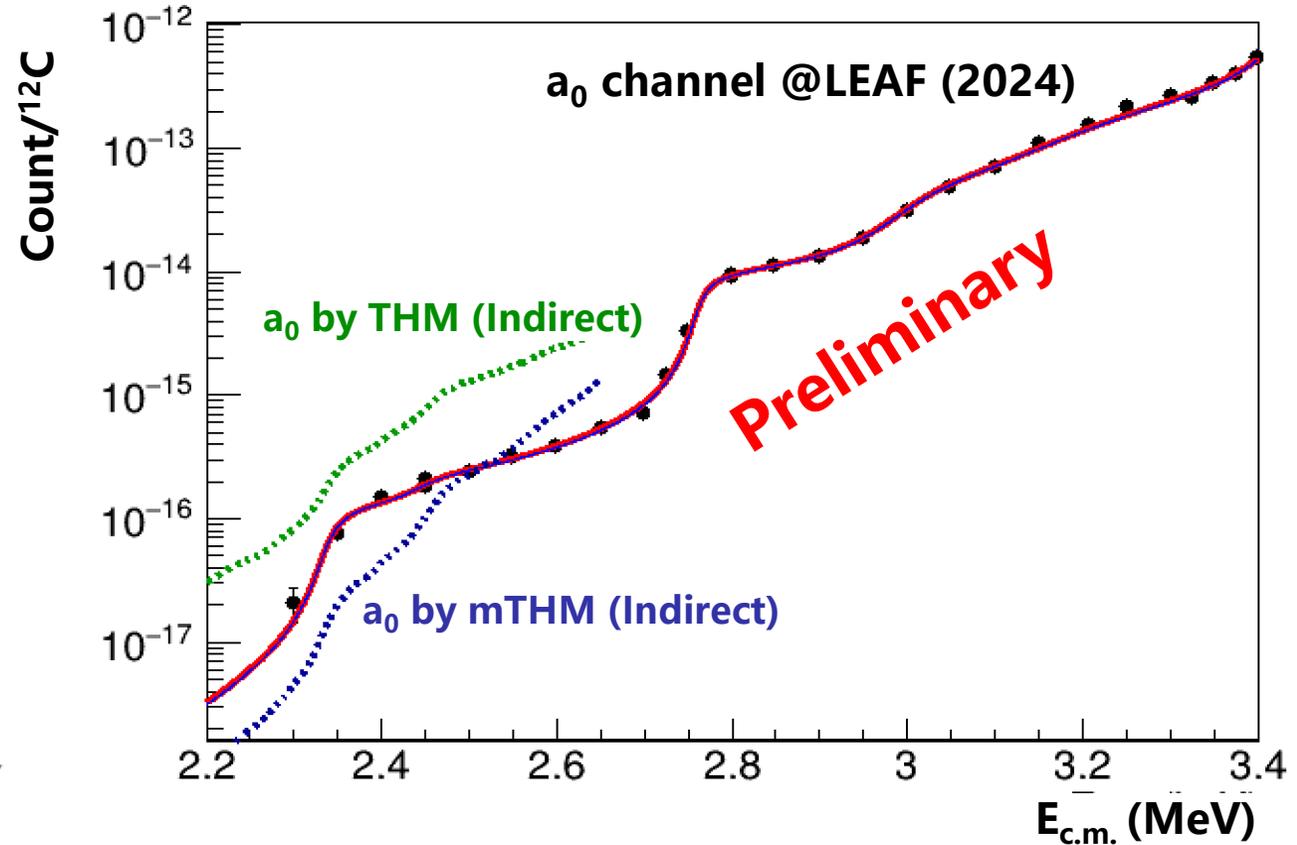
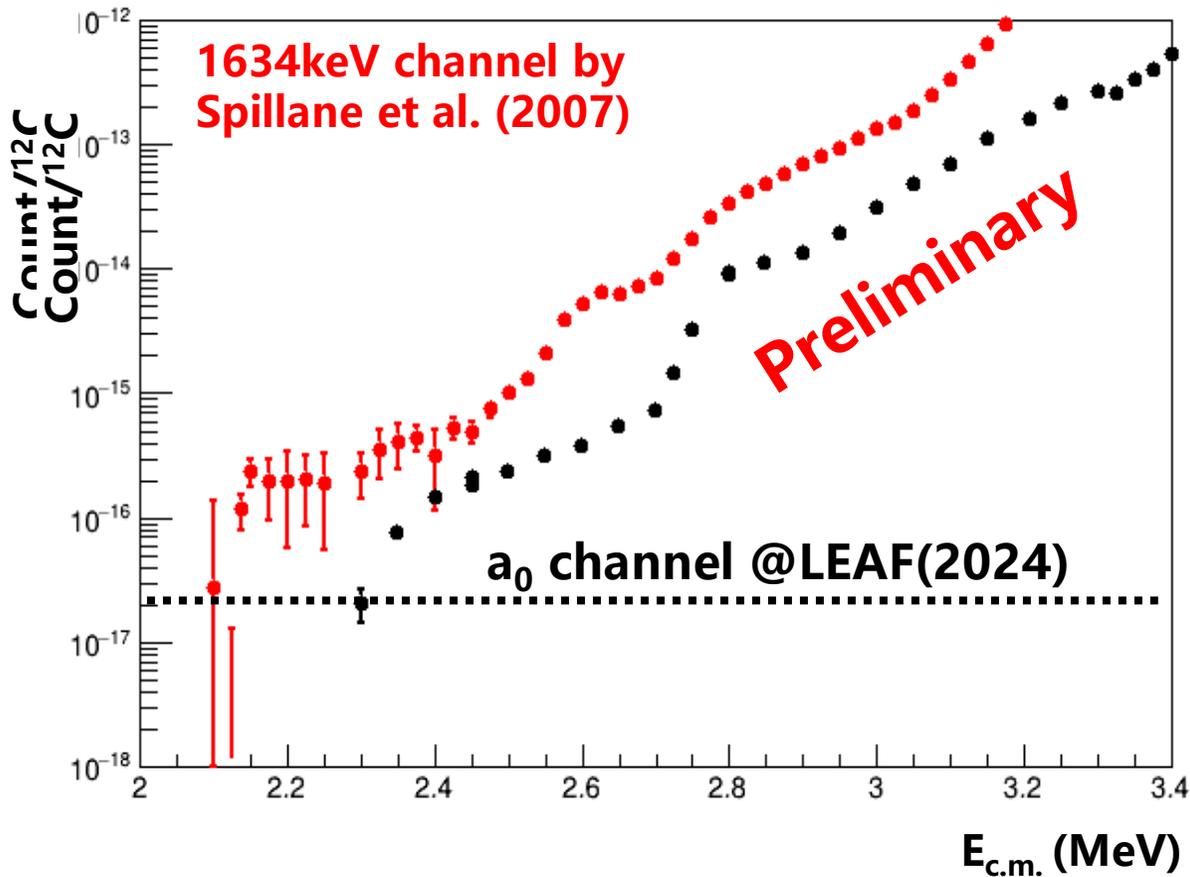


Clear identification with cuts in the energy loss and tracks in TPC

# Degrading of the HOPG target

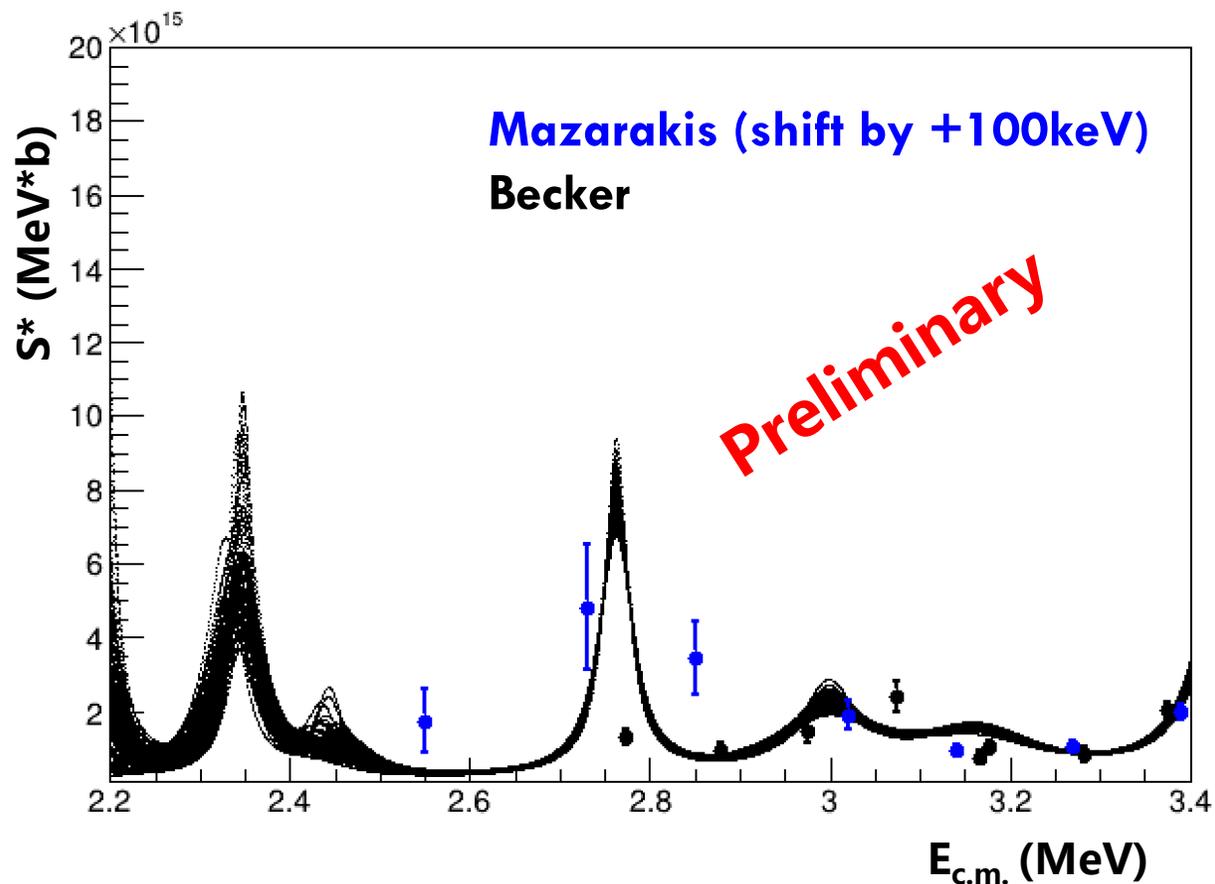
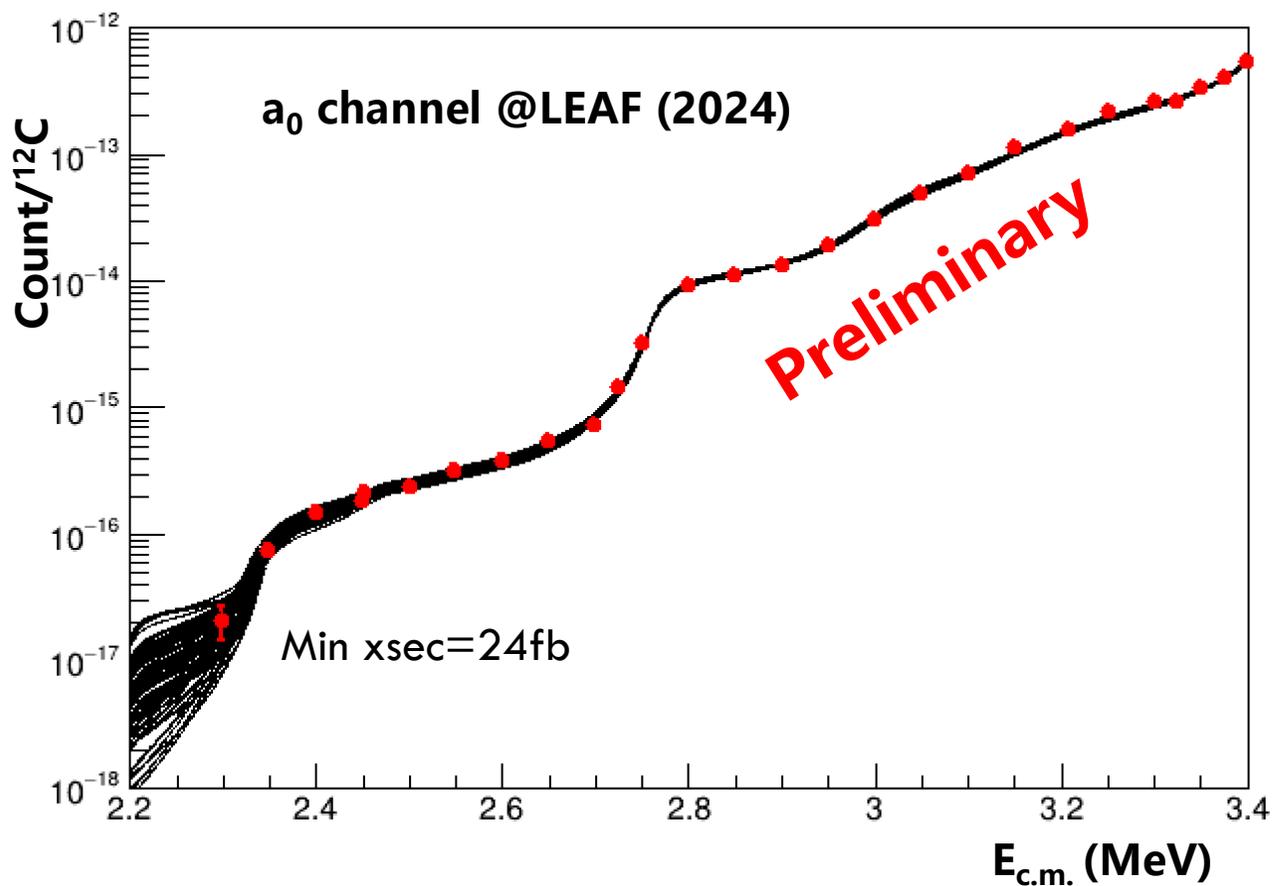


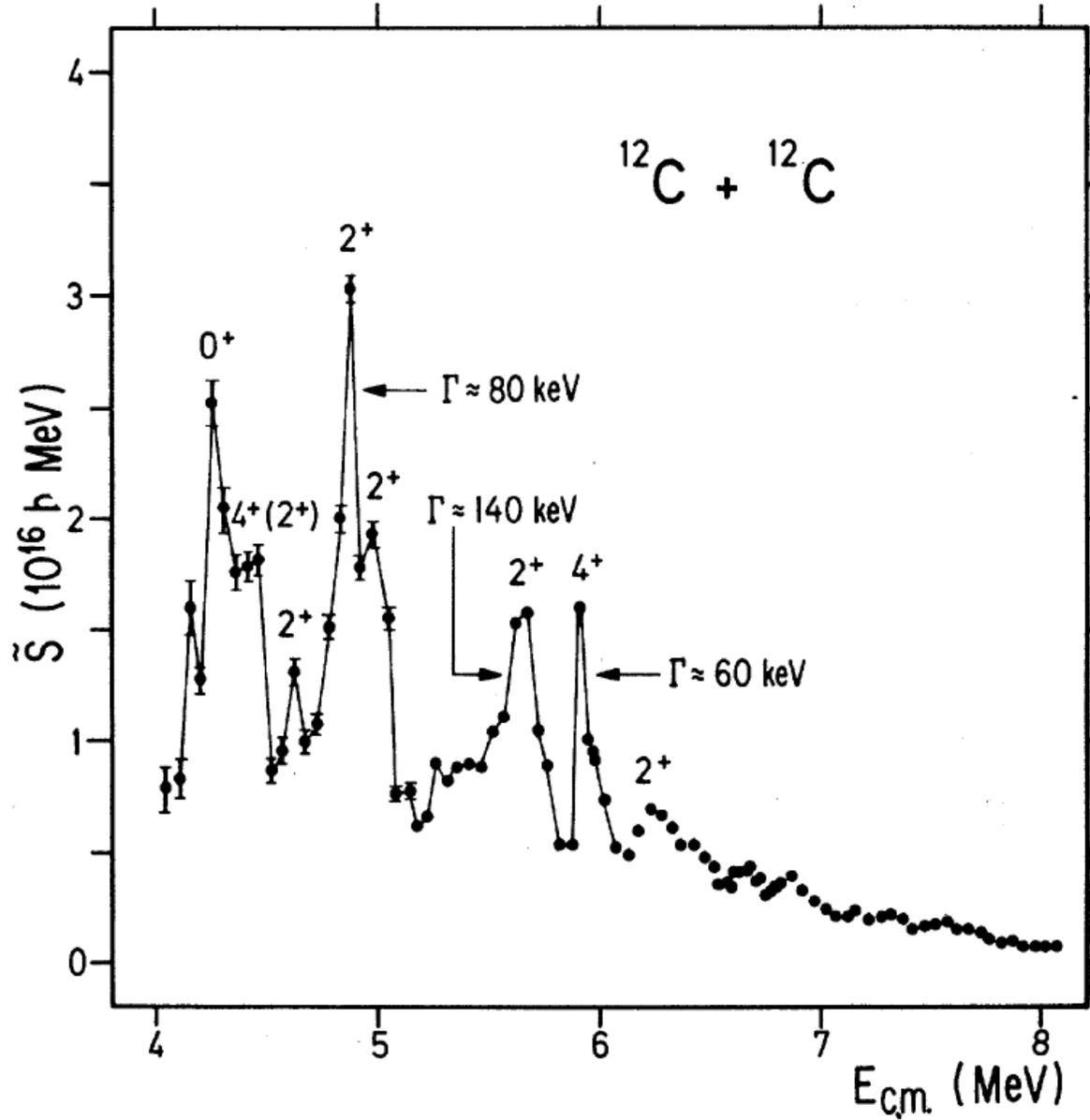
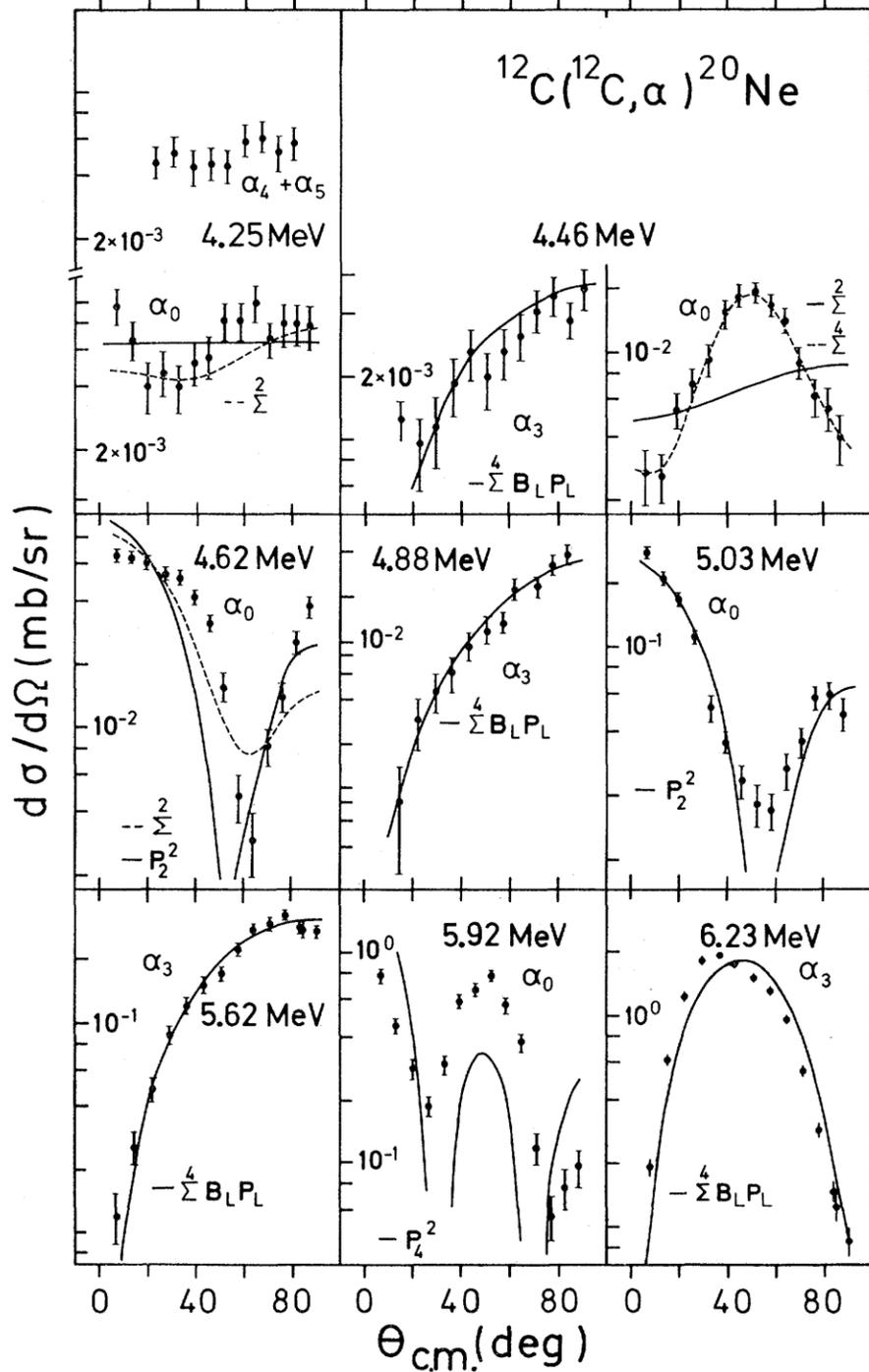
# Preliminary results



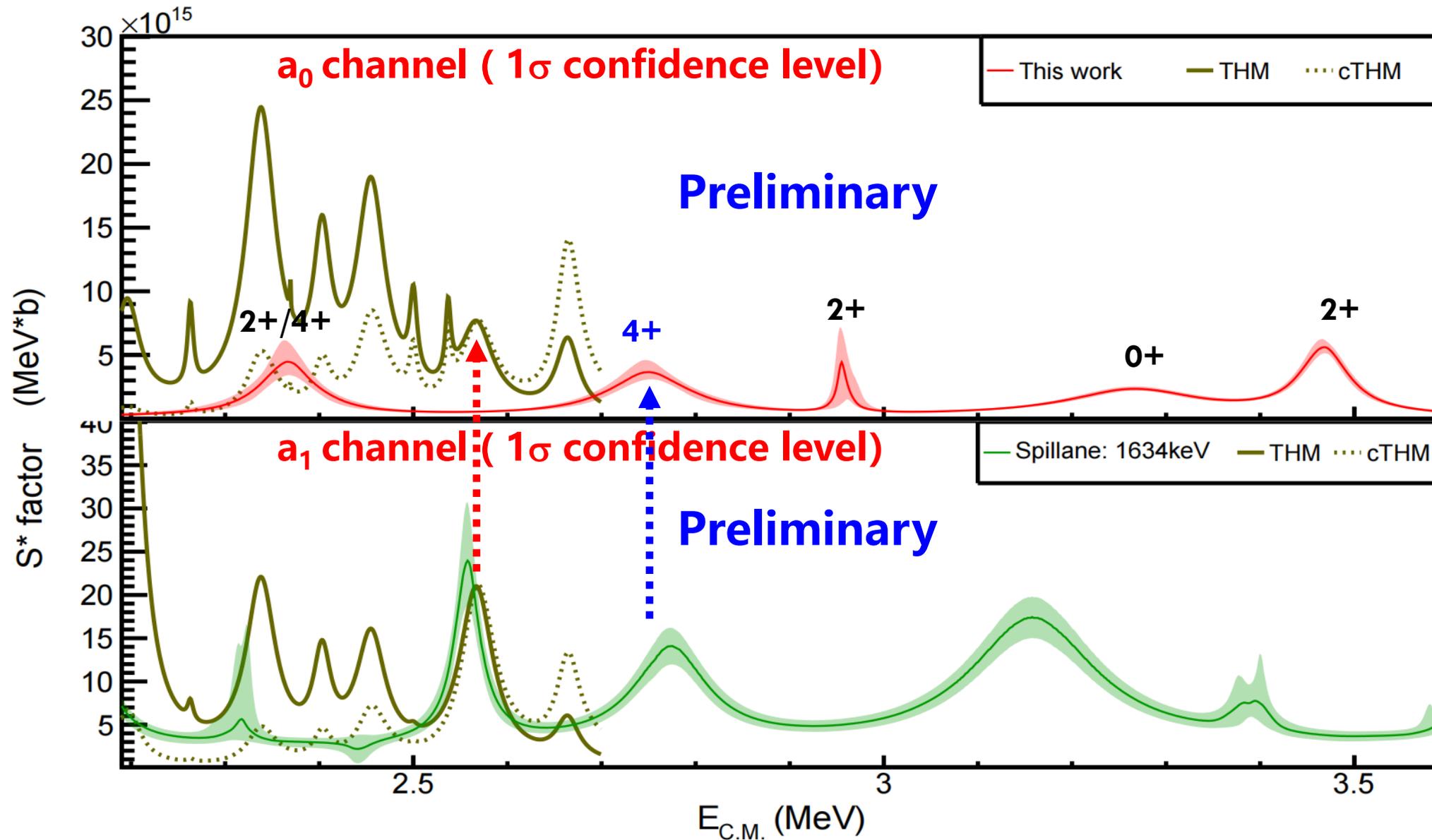
- First direct measurement of  $a_0$  channel at energies below  $E_{cm} = 2.5$  MeV with a sensitivity better than the  $a_1$  channel measured by Spillane et al. (2007)
- The thick target yields of direct measurement disagree with THM and mTHM

# Error analysis using Monte Carlo Method



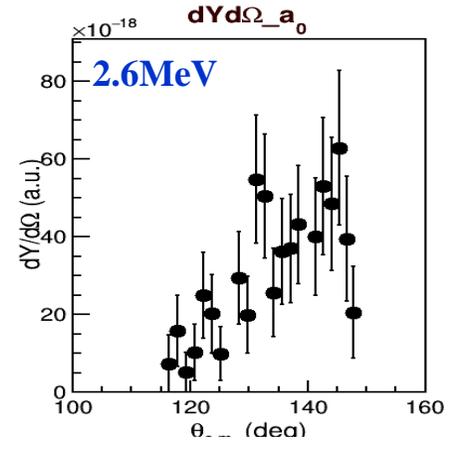
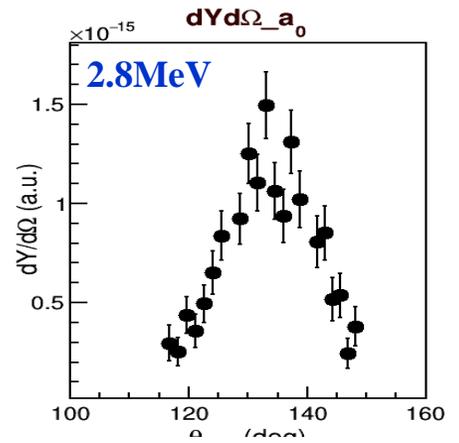
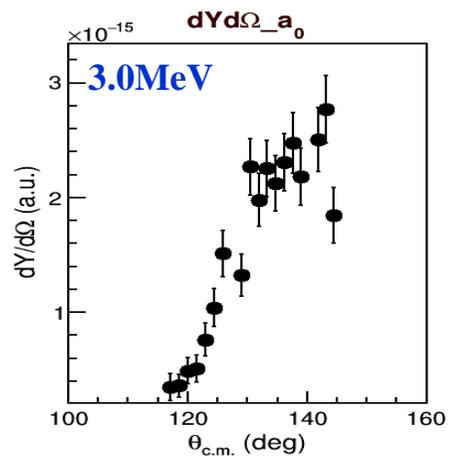


Galster et al., PRC(1977)

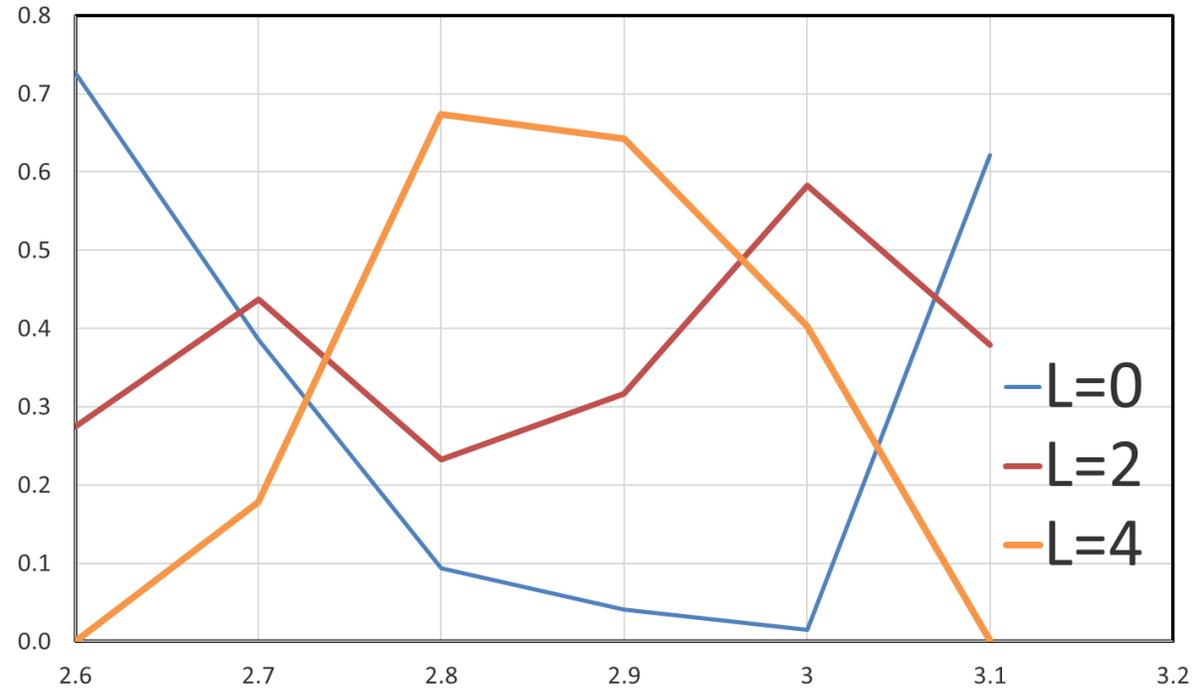
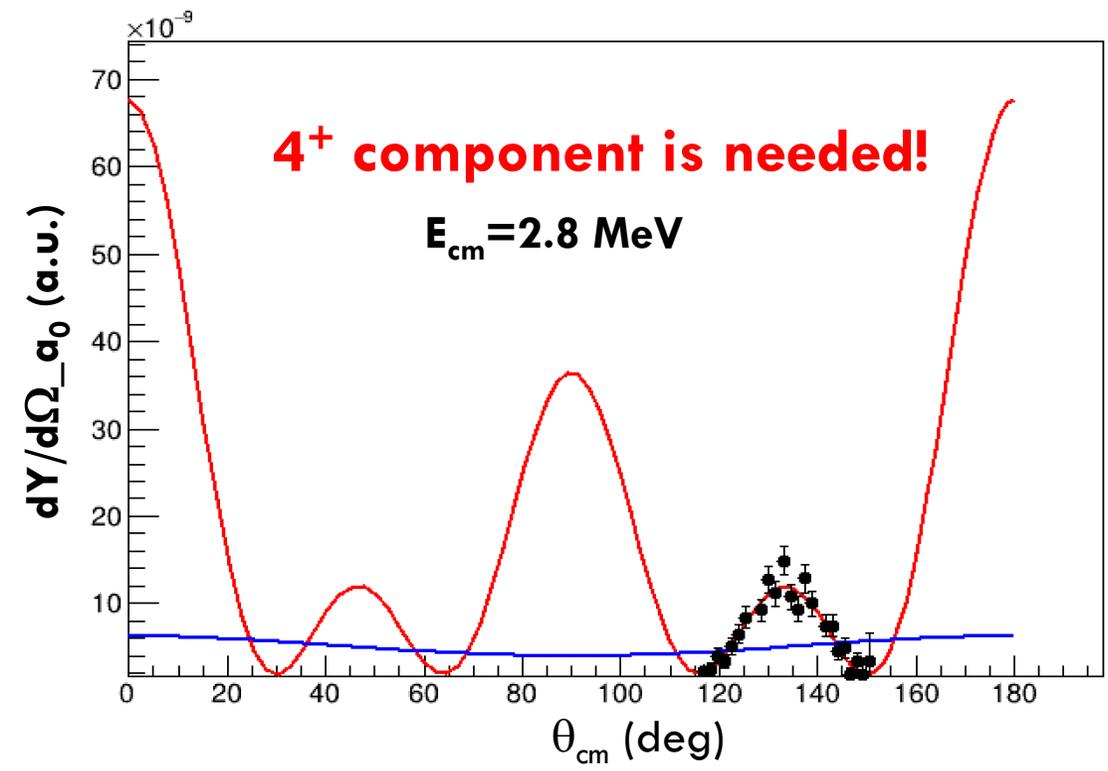


- **2.567MeV ( $0+$ ) observed in THM does not appear in the direct measurement**
- **Spin/Parity assignment seems to agree with the Taniguchi&Kimura prediction of  $0+/2+$**

# Determination of $J^\pi$ of $E_{cm}=2.76$ (MeV)



Contribution of difference spin





# Algebraic approach to nuclear quasimolecular spectra

F. Iachello

*A. W. Wright Nuclear Structure Laboratory, Yale University, New Haven, Connecticut 96511  
and Kernfysisch Versneller Instituut, University of Groningen, Groningen, The Netherlands*  
(Received 17 July 1980)

PHYSICAL REVIEW C

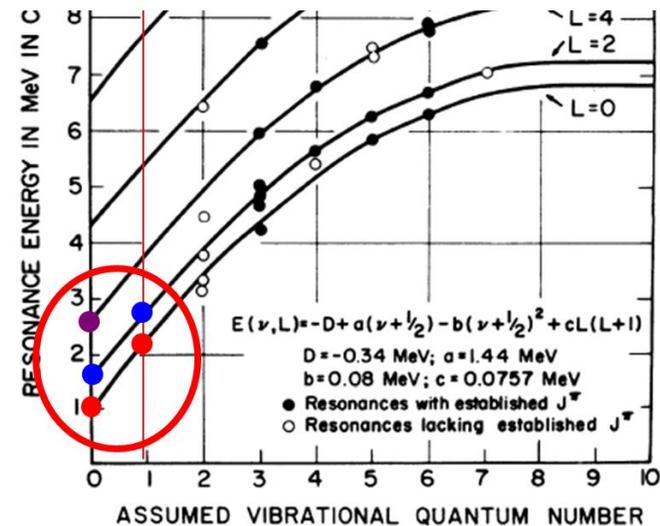
VOLUME 23, NUMBER 6

JUNE 1981

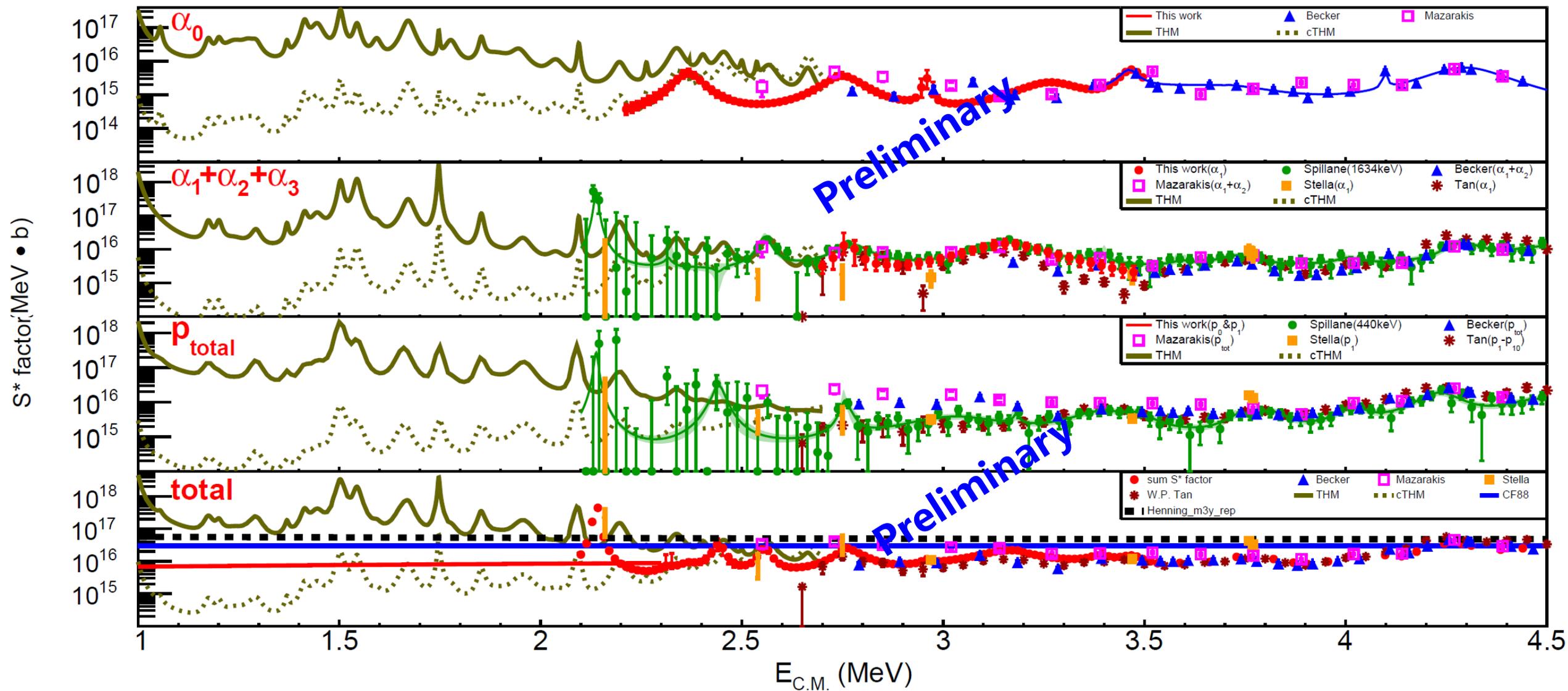
## Rotational and vibrational excitations in nuclear molecular spectra

K. A. Erb and D. A. Bromley

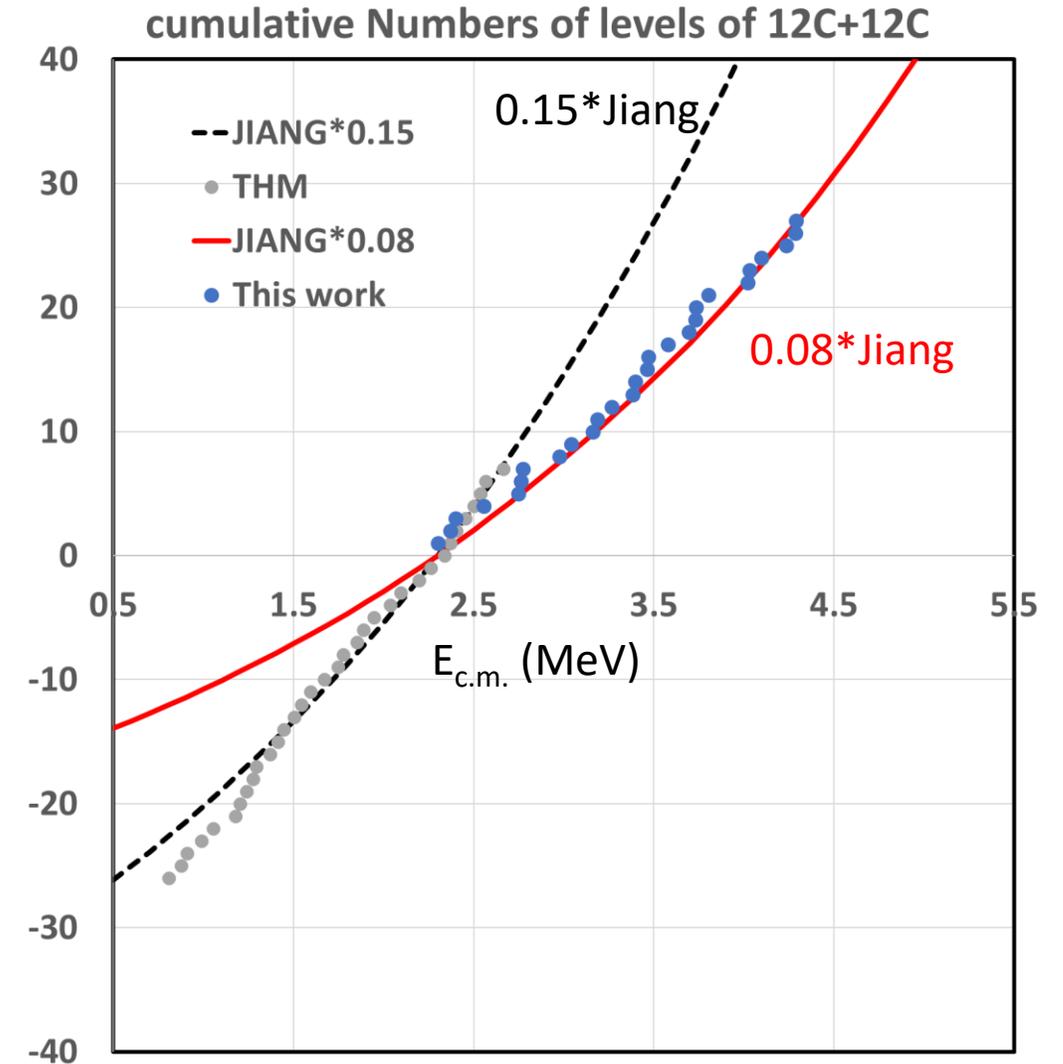
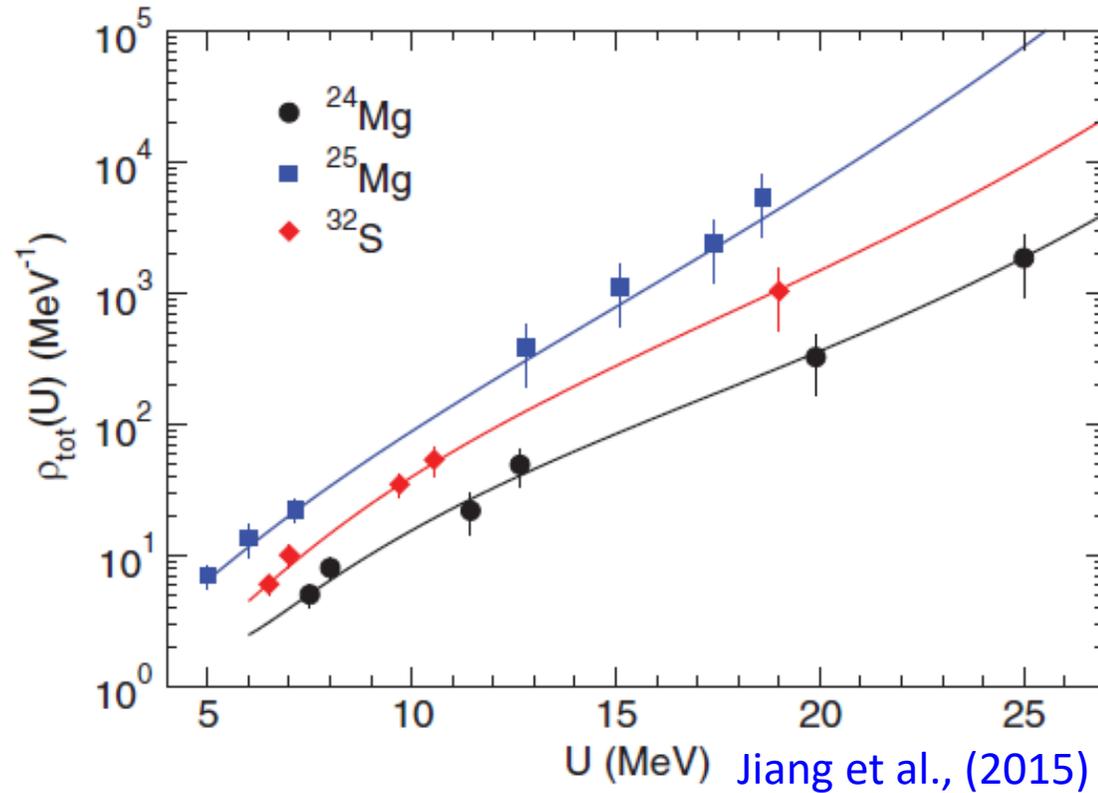
*A. W. Wright Nuclear Structure Laboratory, Yale University, New Haven, Connecticut*  
(Received 17 July 1980)



**Prediction of 4<sup>+</sup> state at 2.55 MeV is confirmed by our experiment!**

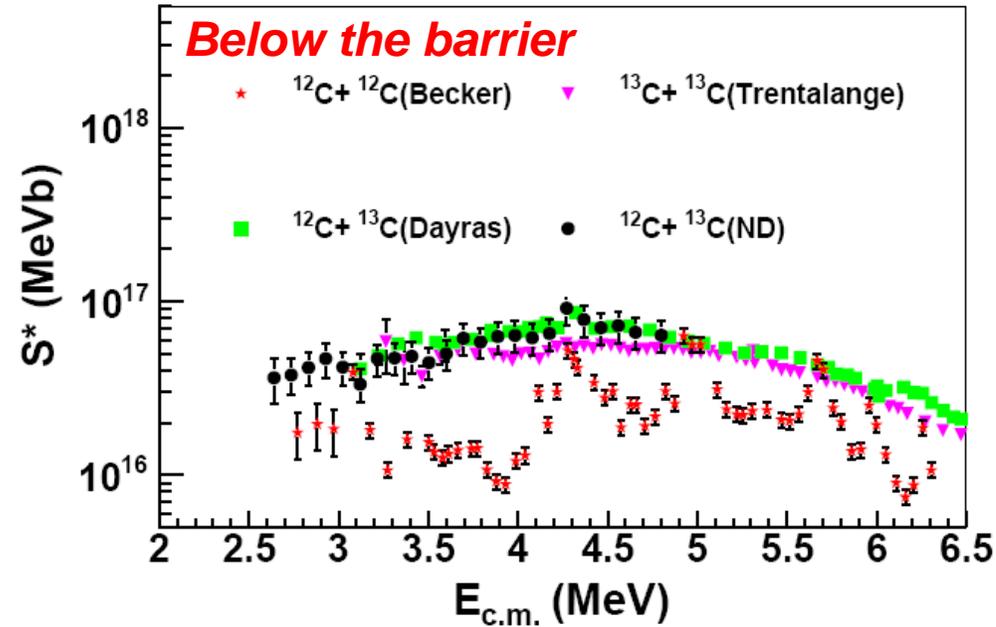


# Level density of the $^{12}\text{C}+^{12}\text{C}$ resonances



- **Direct measurement: 27 resonances observed within [2.3:4.3MeV]**
- **Jiang's level density needs to be scaled by 0.08!**

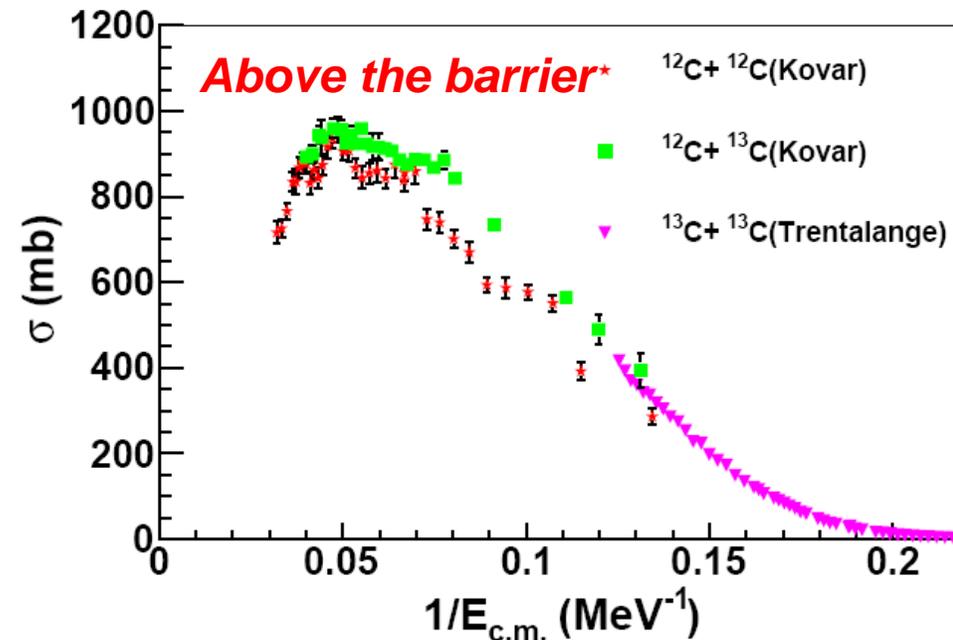
# Correlation among the carbon isotope systems



For most energies, the  $^{12}\text{C}+^{12}\text{C}$  cross sections are suppressed!



Only at resonant energies, the  $^{12}\text{C}+^{12}\text{C}$  cross sections matches with those of  $^{12}\text{C}+^{13}\text{C}$  and  $^{13}\text{C}+^{13}\text{C}$ !



Why?

# Correlation between carbon isotopes

Averaged  $S^*$

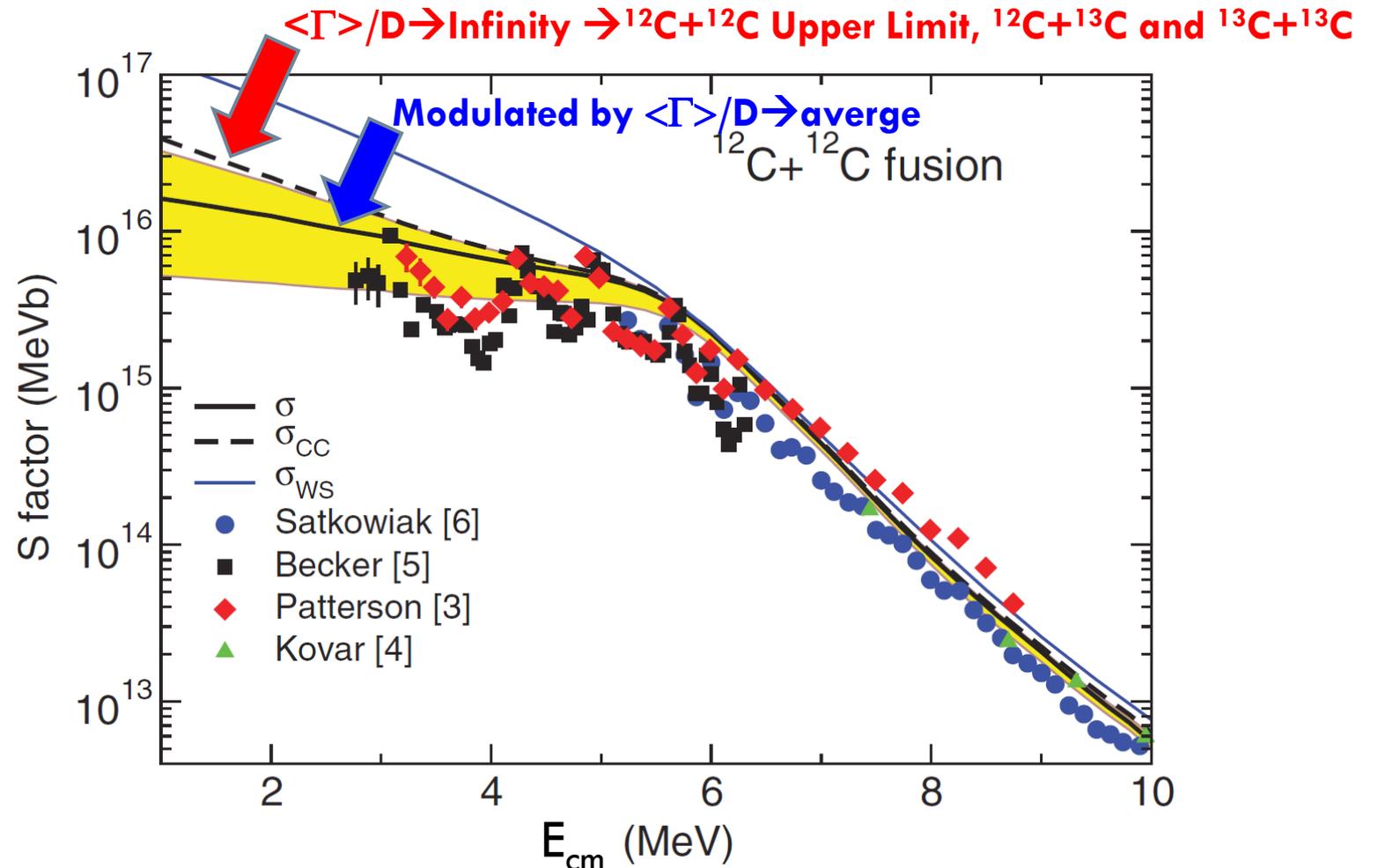
$$\sigma = \sum_J \sigma_{CC}^J P_J$$

States for fusion

$$P_J = 1 - \exp(-2\pi\bar{\Gamma}_J/D_J)$$

$\Gamma$ : resonance width

$D$ : resonance spacing



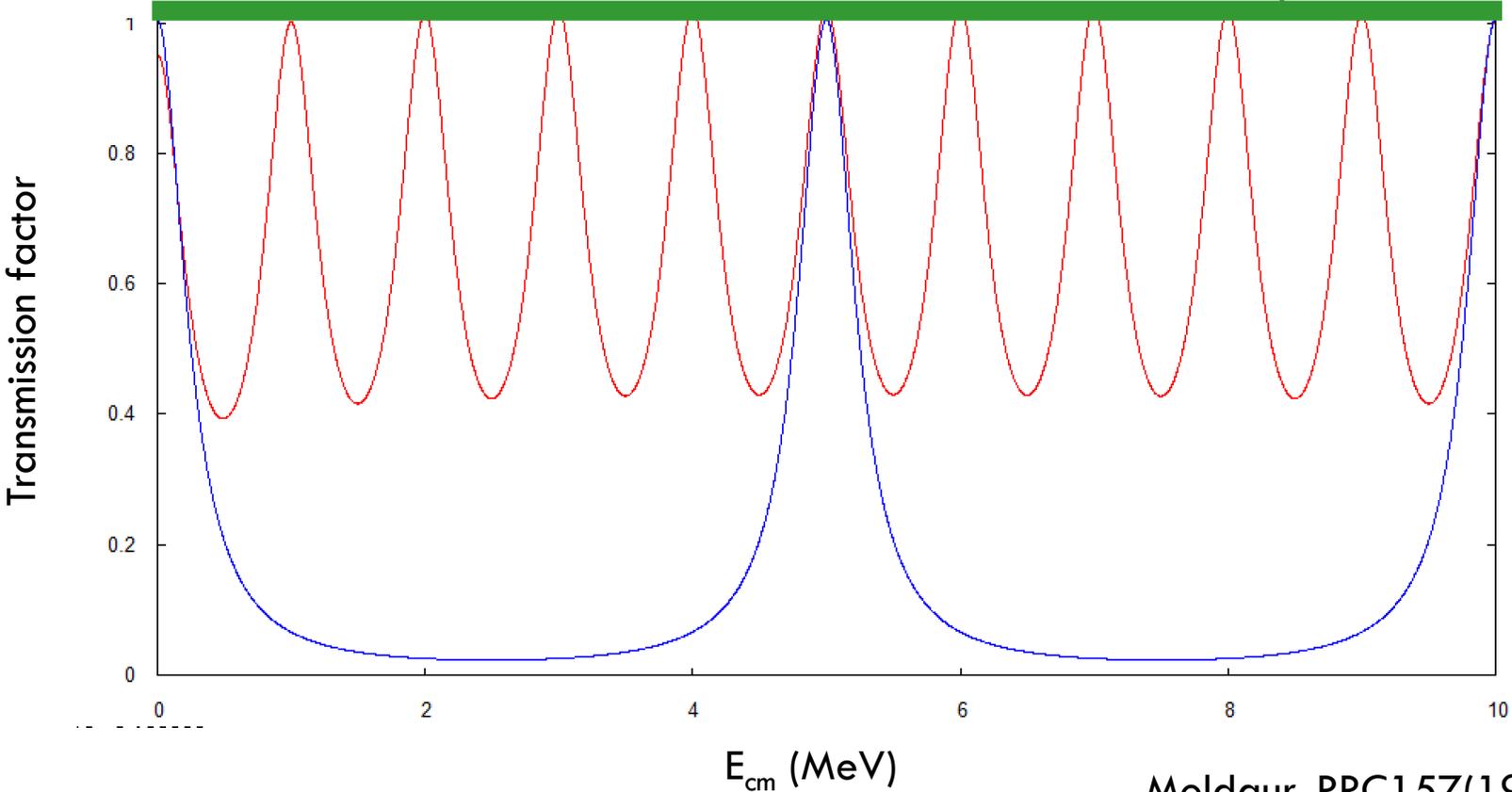
# Correlation between carbon isotopes

$$T = 1 - \exp(-2\pi\bar{\Gamma}/D)$$

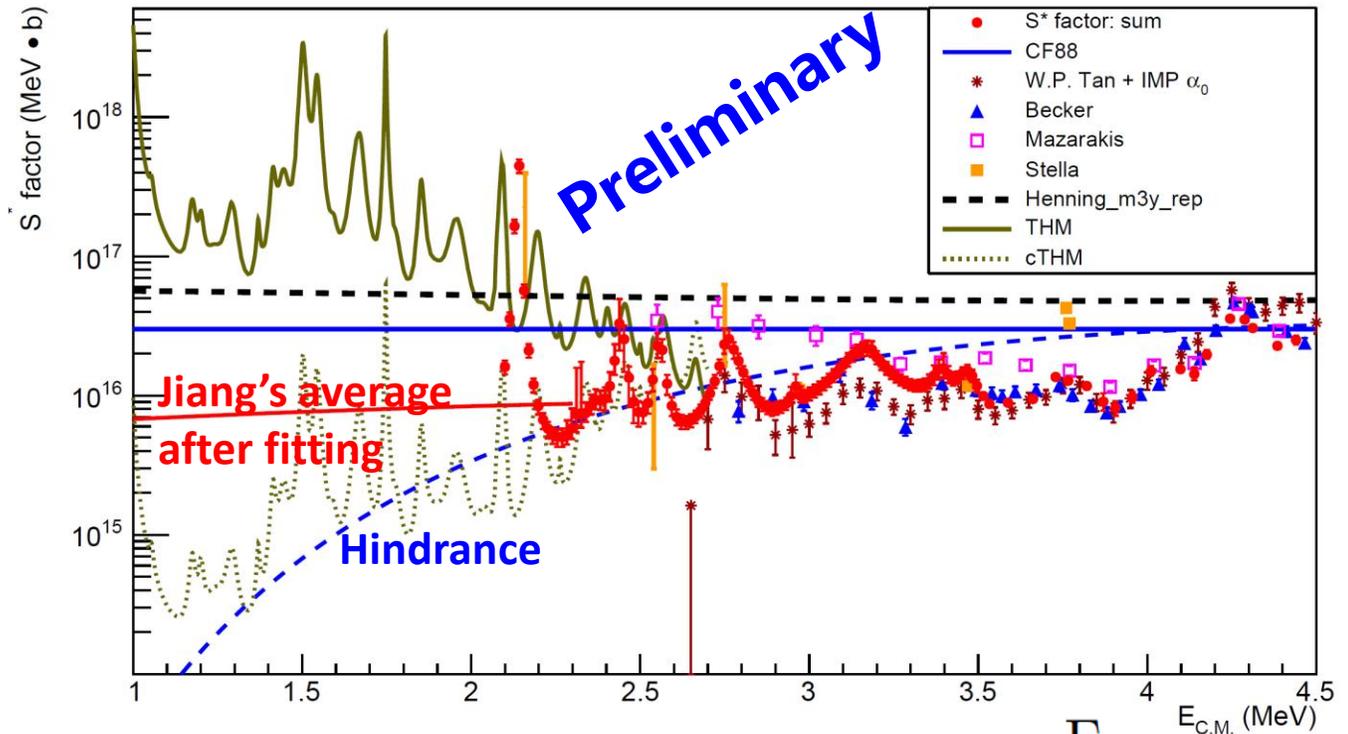
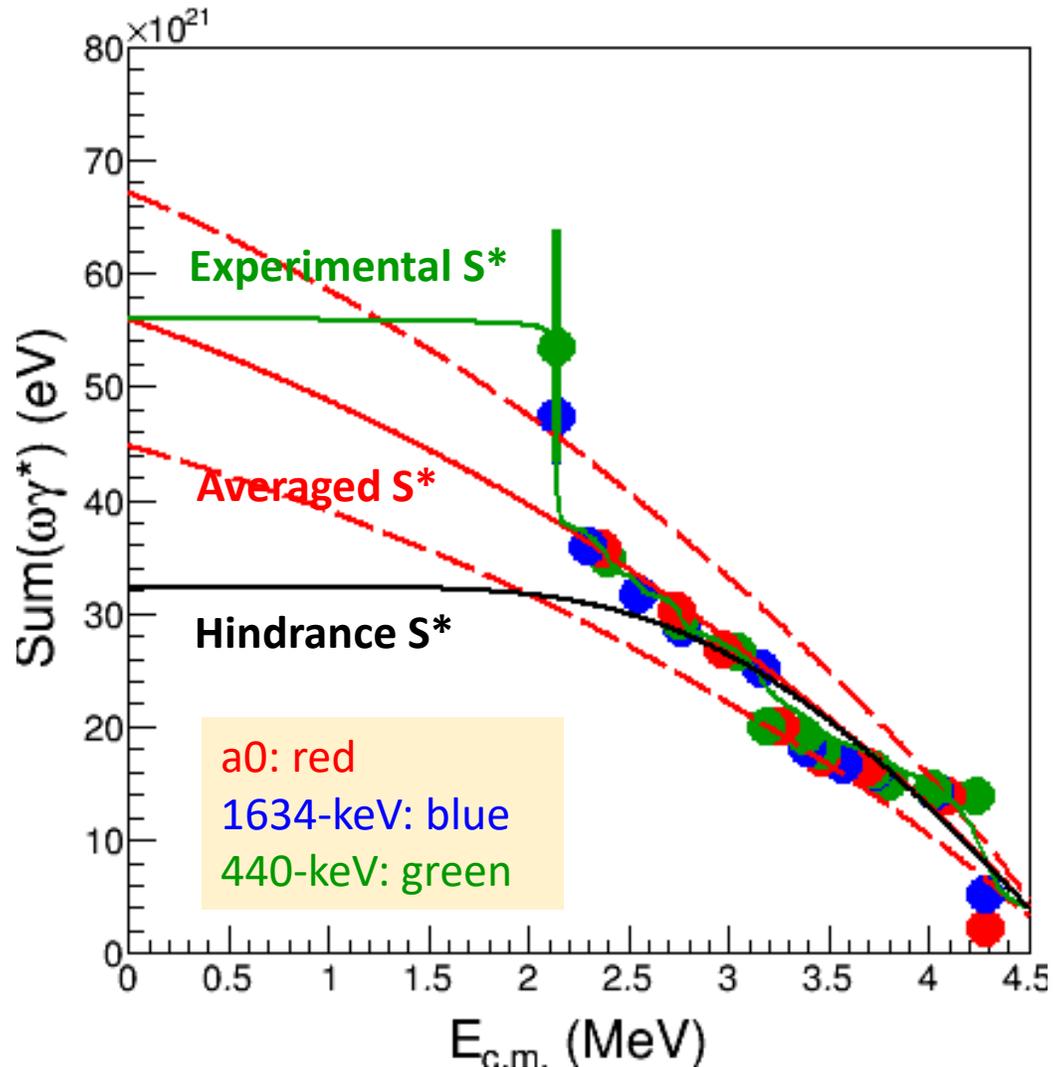
$\Gamma/D=0.1$

$\Gamma/D=0.5$

$\Gamma/D \rightarrow \text{infinity}$



# Sum( $\omega\gamma^*$ ) vs. $E_r$ (MeV)

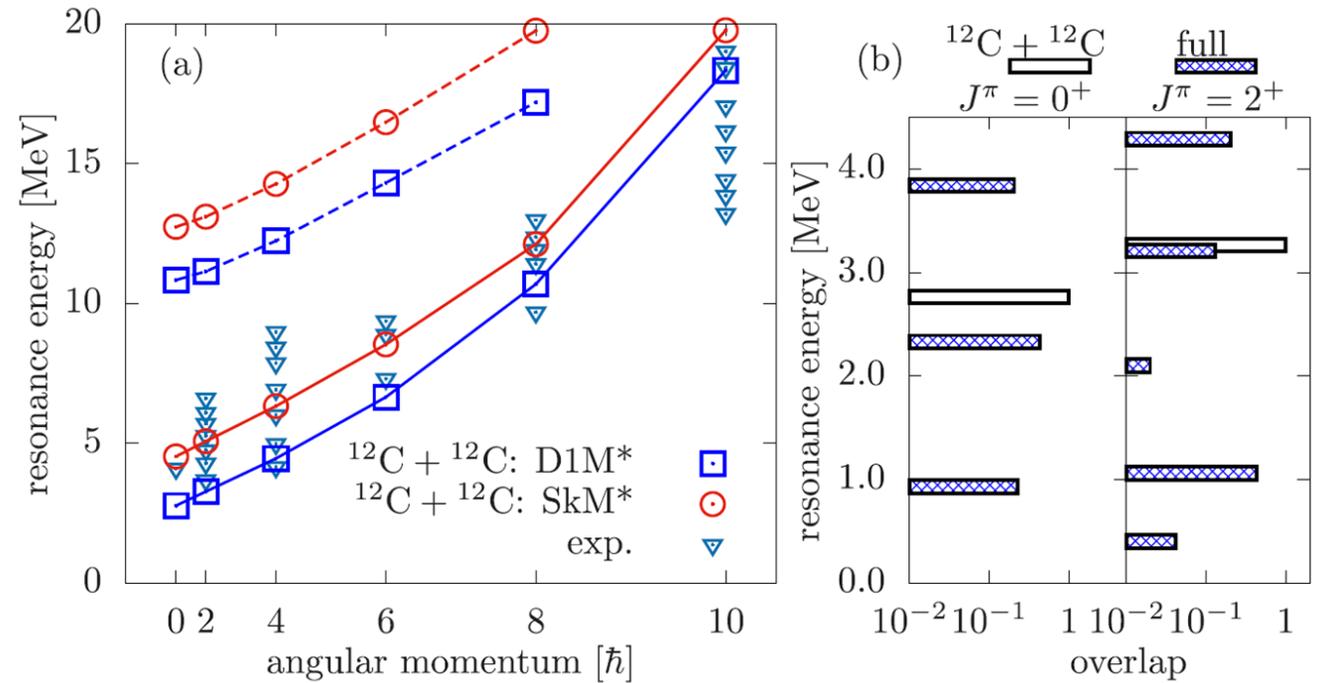
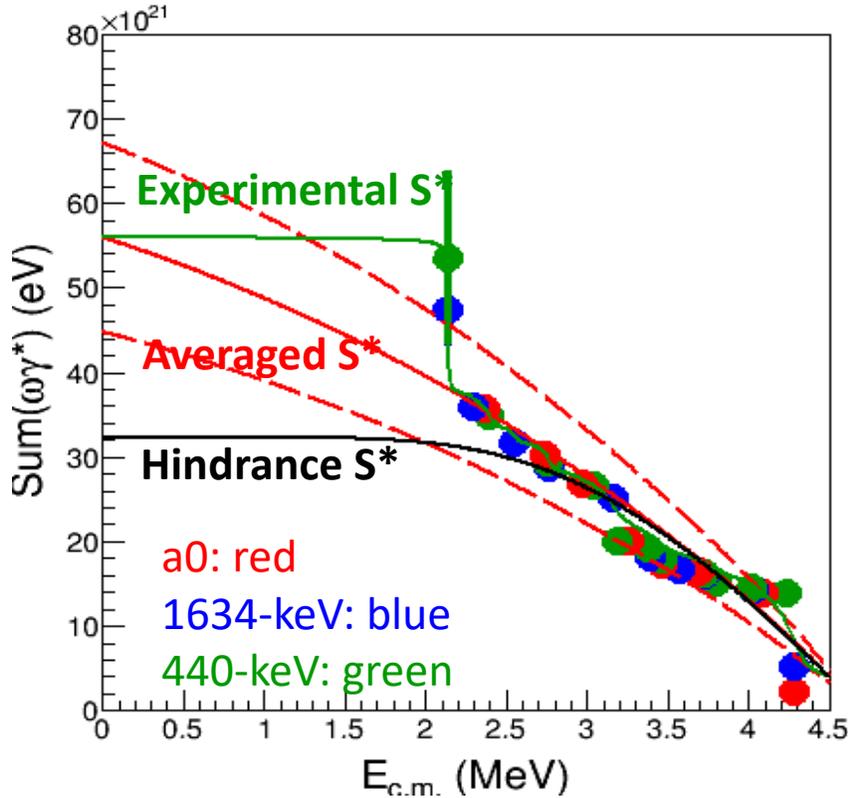


$$\omega\gamma = (2J + 1)(1 + \delta_{12})\Gamma_{12}C_{+12}C(E_R)\frac{\Gamma_b}{\Gamma}$$

$$\omega\gamma^* = \omega\gamma e^{\left(\frac{87.21}{\sqrt{E_R}} + 0.46E_R\right)}$$

$$\int S^*(E)dE = S_{max}^* \frac{\pi\Gamma}{2} = \frac{2\pi\hbar^2}{\mu} \frac{\omega^*\gamma}{\Gamma} \frac{\pi\Gamma}{2} = \frac{\pi^2\hbar^2}{\mu} \omega\gamma^*$$

# Sum rule of the molecular resonance



Taniguchi and Kimura, PLB(2024)

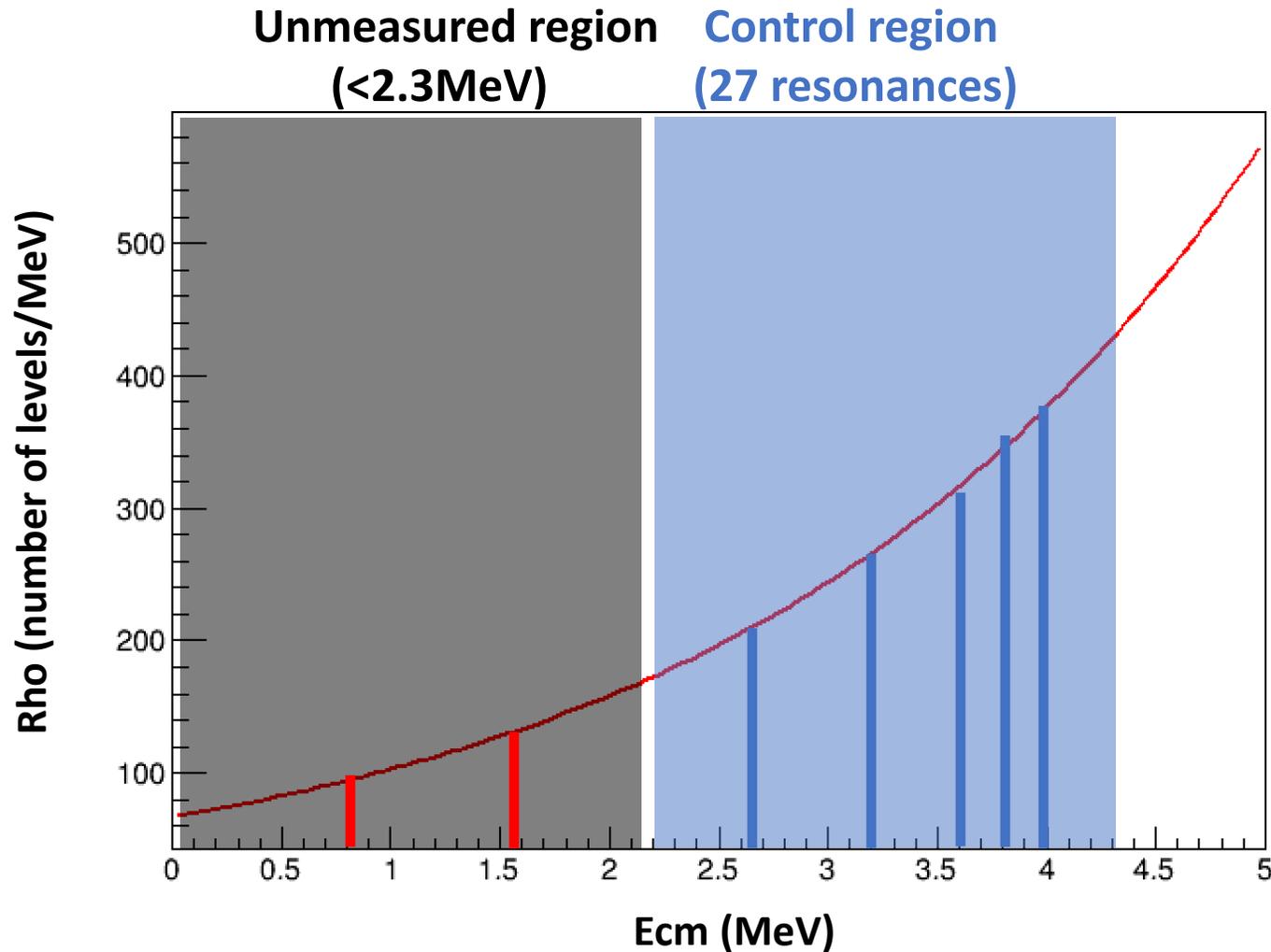
The  $^{12}\text{C}+^{12}\text{C}$  resonance can be **fragmented into small resonances due to the coupling to various decay channels**, but the sum of the strength (after correcting for the penetration effect) should remain same

**Extrapolation**

**Towards lower energies**

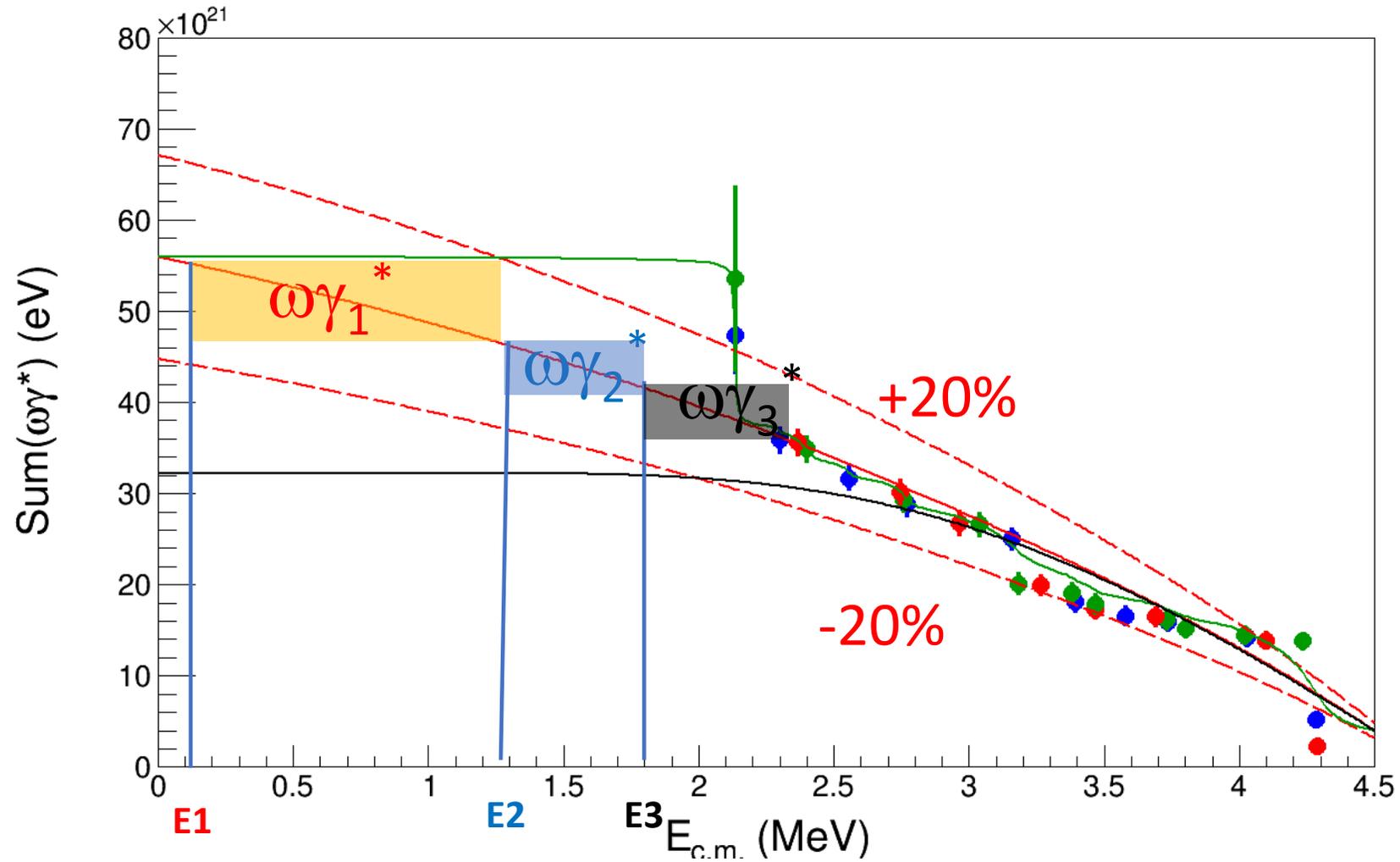
**Using statistical model approach**

# Faked resonances using Monte Carlo method

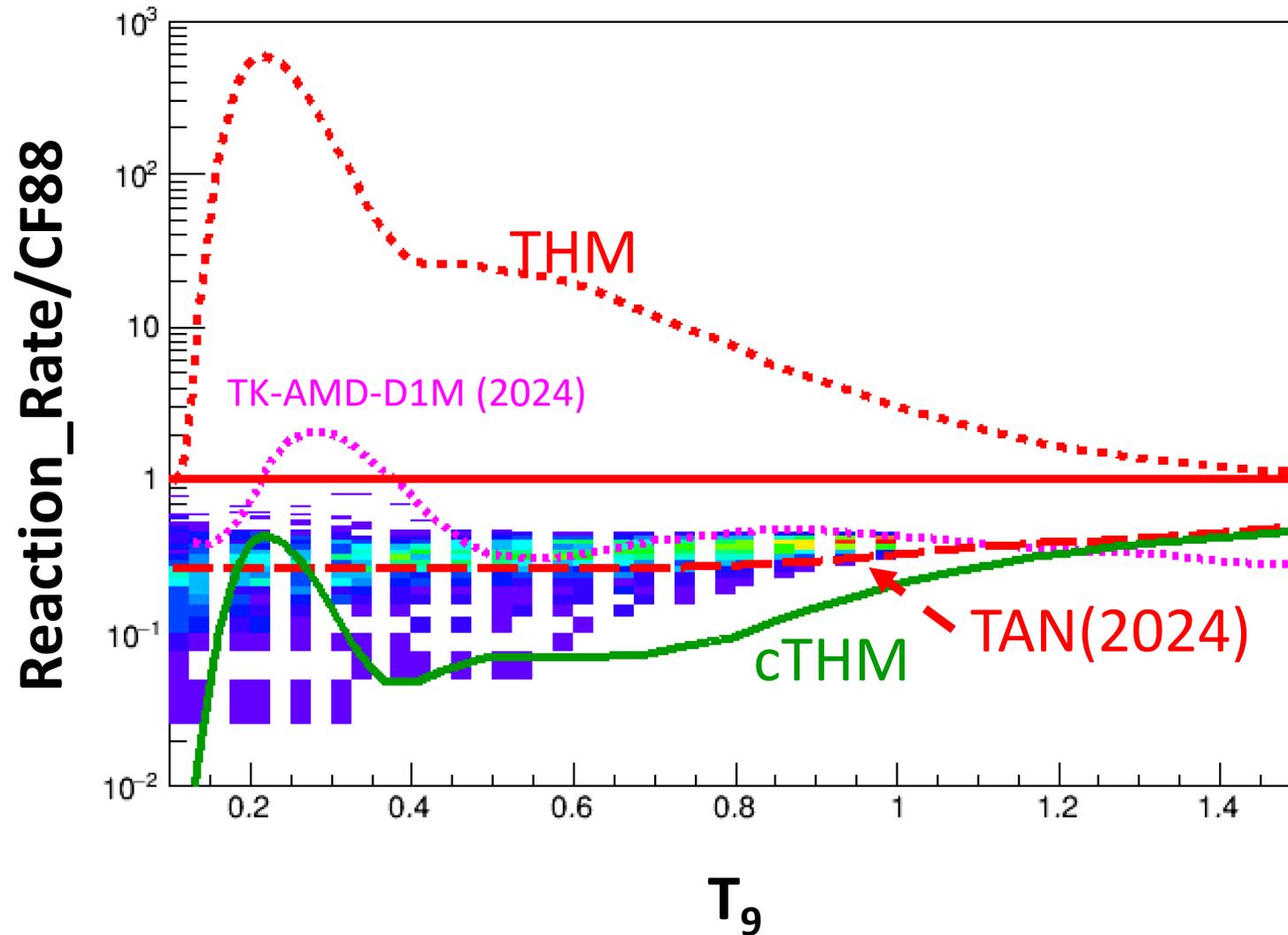


Levels in the unmeasured energy range are generated with a level density constrained by direct measurement

# Sum( $\omega\gamma^*$ ) vs. $E_r$ (MeV)

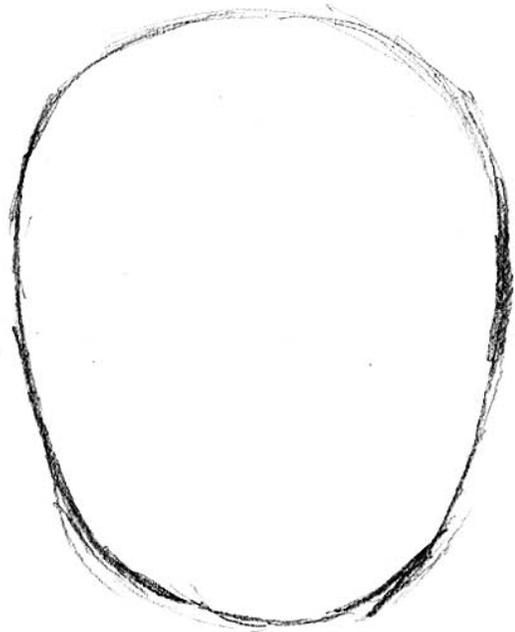


# Reaction rate based on Monte carlo

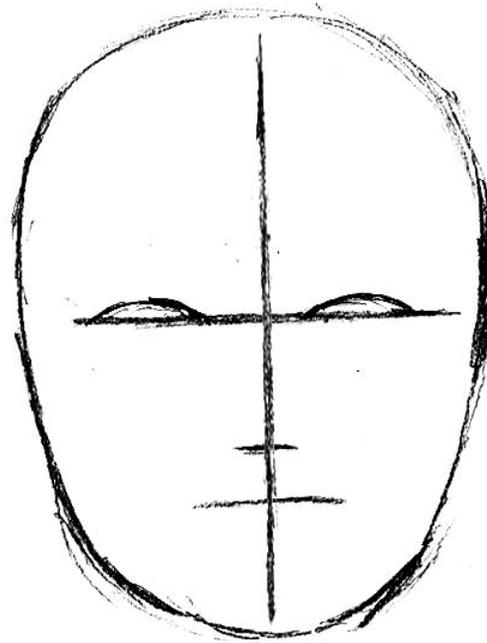


Nature of the  $^{12}\text{C}+^{12}\text{C}$  molecular resonance determines extrapolation

*Resonant Energy, Strength, Penetration Factor*

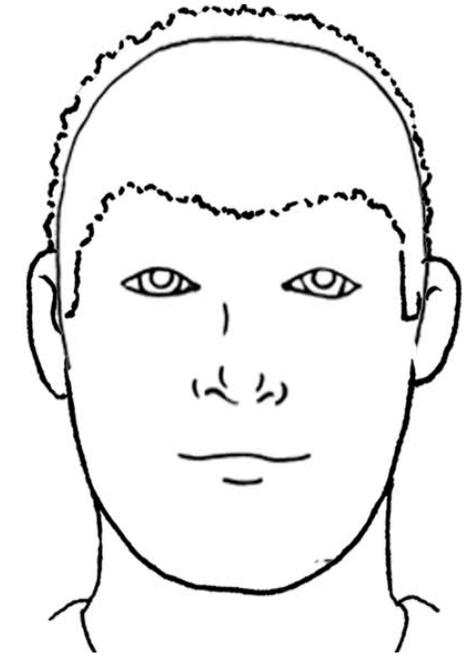


**Gross structure**  
(averaged xsec,  
Upper/lower limits)



**Intermediate Structure**

(structure of total fusion xsec)

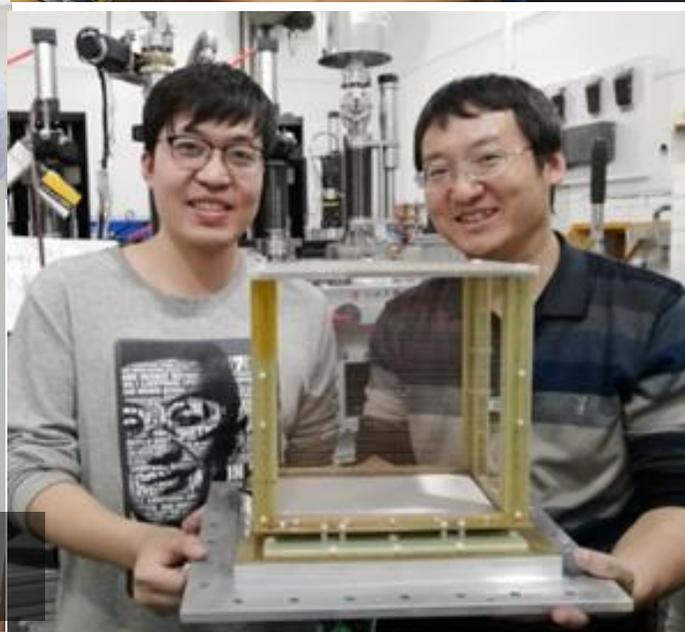
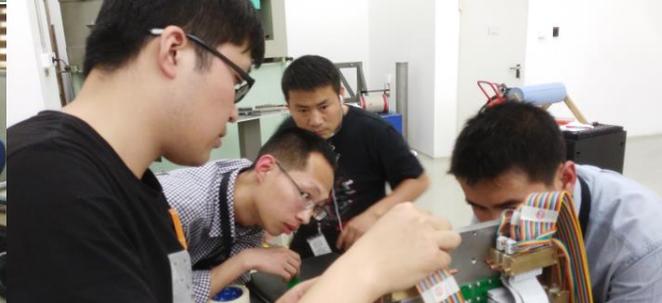
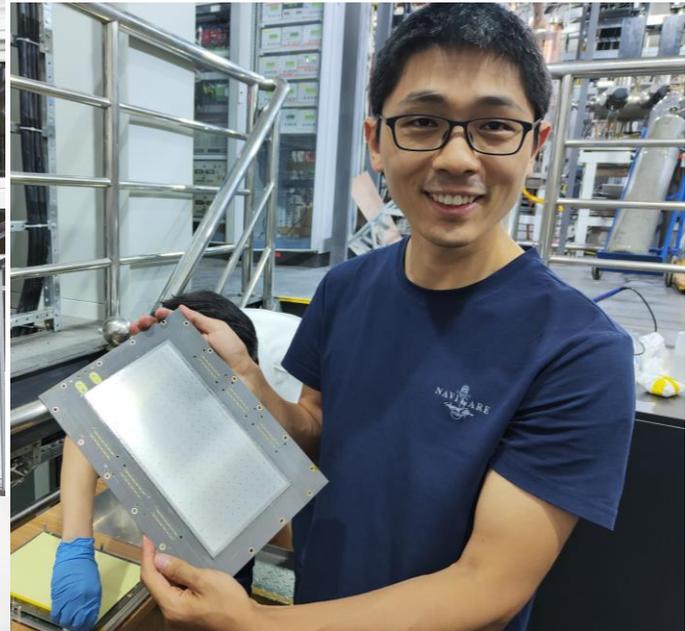
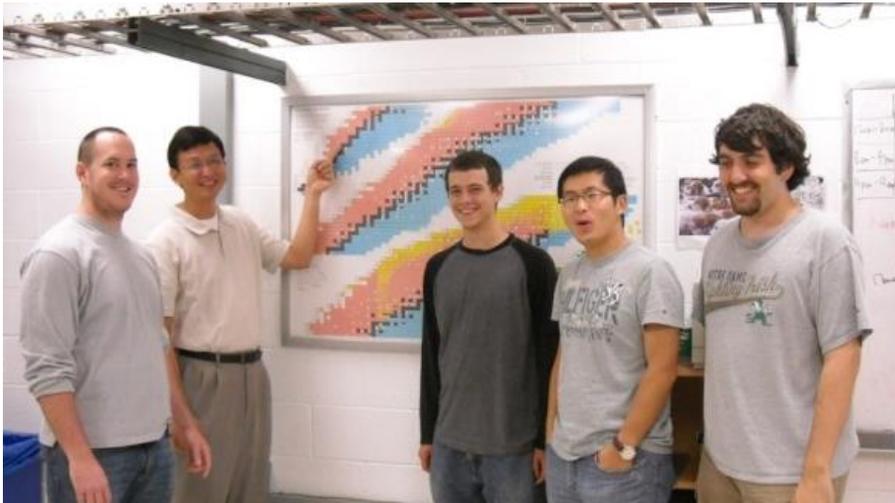


**Fine Structure**  
(Structure in  
decay channels)

# Summary

- Our direct measurement of  $^{12}\text{C}+^{12}\text{C}$ 
  - First direct measurement of  $a_0$  below 2.5 MeV indicates the needs of improving the THM/cTHM
  - Our analysis suggests that statistical model is applicable at low energies
- Indirect (THM,  $^{24}\text{Mg}(\alpha,\alpha')$ )+Direct measurements will provide best extrapolation; Strongly coupled plasma screening needs to be studied
- Collaboration will end up with better science!





Collaborators at ND, RCNP, IFIN-HH, USTC and CIAE