

Overview of next-generation oscillation experiments

Callum Wilkinson

*Thanks to Stephen Dolan, Luke Pickering,
Patrick Stowell and Clarence Wret for material*



accelerator long-baseline

Overview of next-generation oscillation experiments

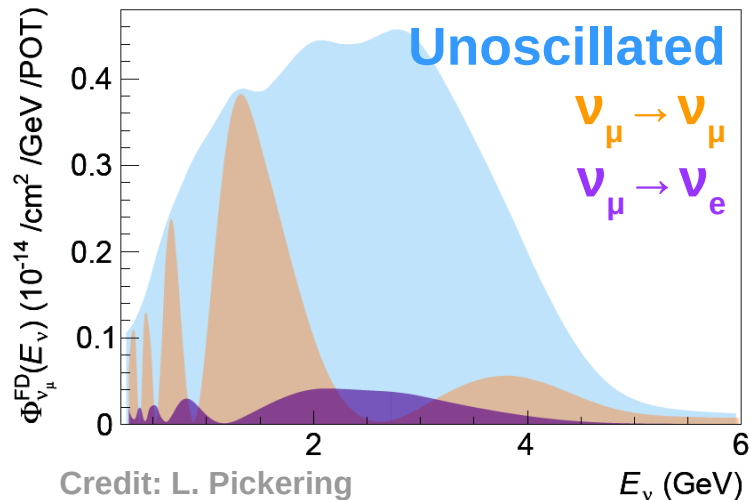
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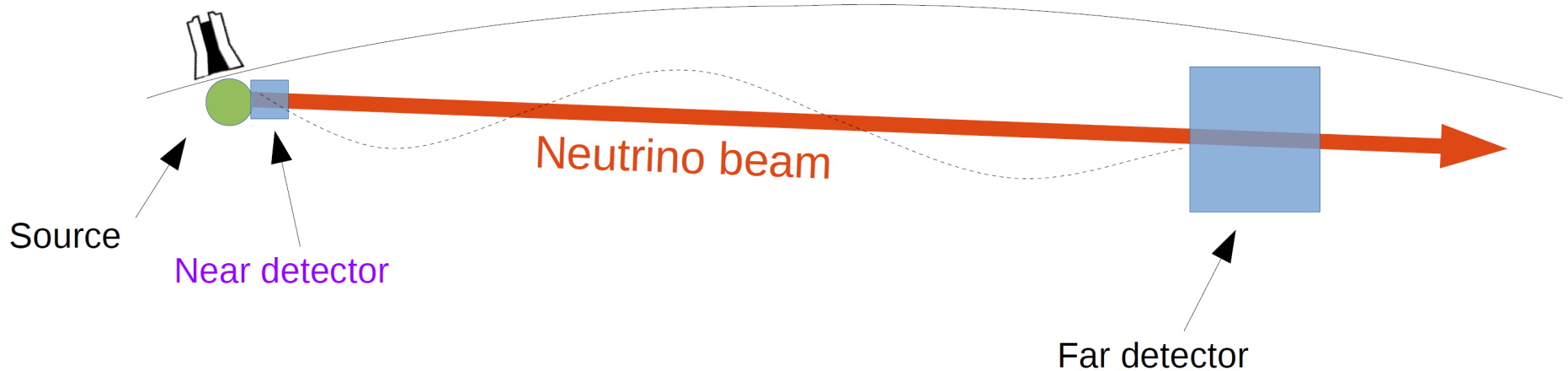
Accelerator neutrino experiments

$$R(\vec{\mathbf{x}}) = \int dE \underbrace{\Phi(E_\nu) \times \sigma(E_\nu, \vec{\mathbf{x}})}_{\text{Near}} \times \underbrace{\epsilon(\vec{\mathbf{x}}) \times P(E_\nu; \nu_A \rightarrow \nu_B)}_{\text{Far}}$$



- Complex inference of **oscillation probability** from measured **event rate**
- Near detector to constrain **neutrino flux** and **cross-section** models/systematics
- Different near and far detector fluxes mean uncertainties do not neatly cancel
- **Detector smearing** introduces further ambiguities at both near and far detectors

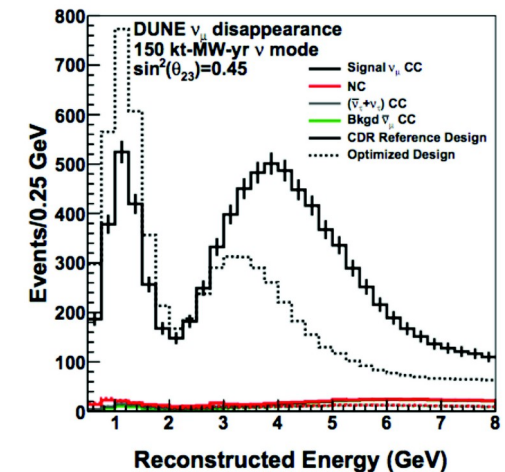
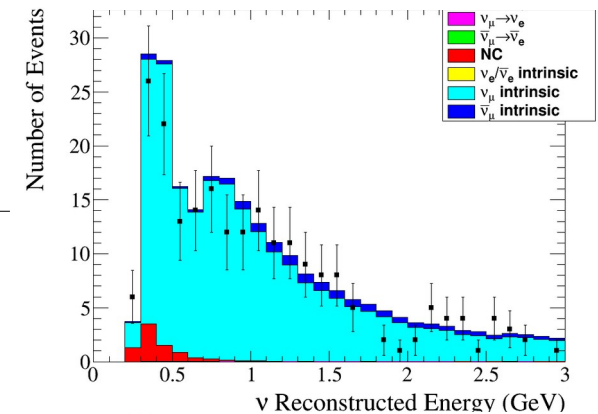
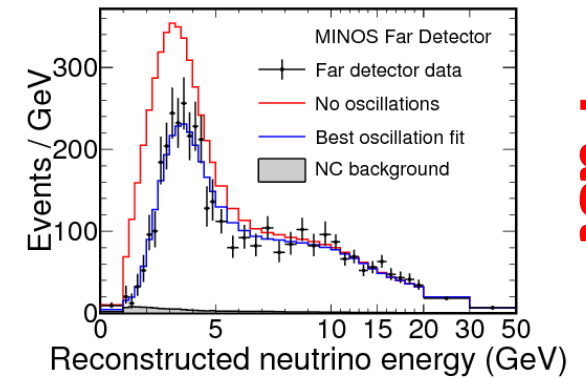
Accelerator neutrino experiments



- Δm_{32}^2 sets $P_{\max} \sim 500 L/E_\nu$ (km/GeV)
- Trade-off between L and E:
 - $R \sim 1/L^2$
 - $R \sim E_\nu$
 - Matter effect increases with E
- Choice of detector technology important for E_ν reconstruction and resolution

Accelerator neutrino experiment history

Name	L (km)	Peak E_ν (GeV)	Year (projected)	FD mass
K2K	250	1	1999-2004	22.5 kt
MINOS	735	3	2005-2012	5.4 kt
OPERA	732	17	2008-2012	1.35 kt
T2K	295	0.6	2010-(202?)	27.2 kt
NOvA	810	2	2013-(202?)	14 kt
DUNE	1285	2.5	(2031-204?)	40 kt
Hyper-K	295	0.6	(2028-204?)	187 kt



Past

Past

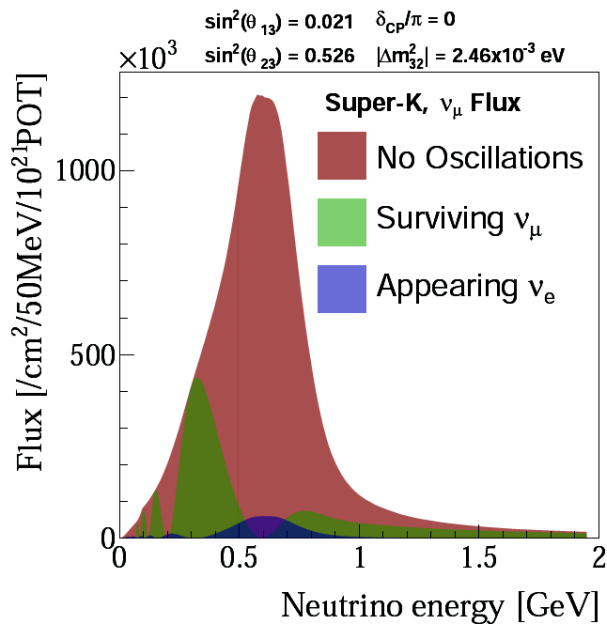
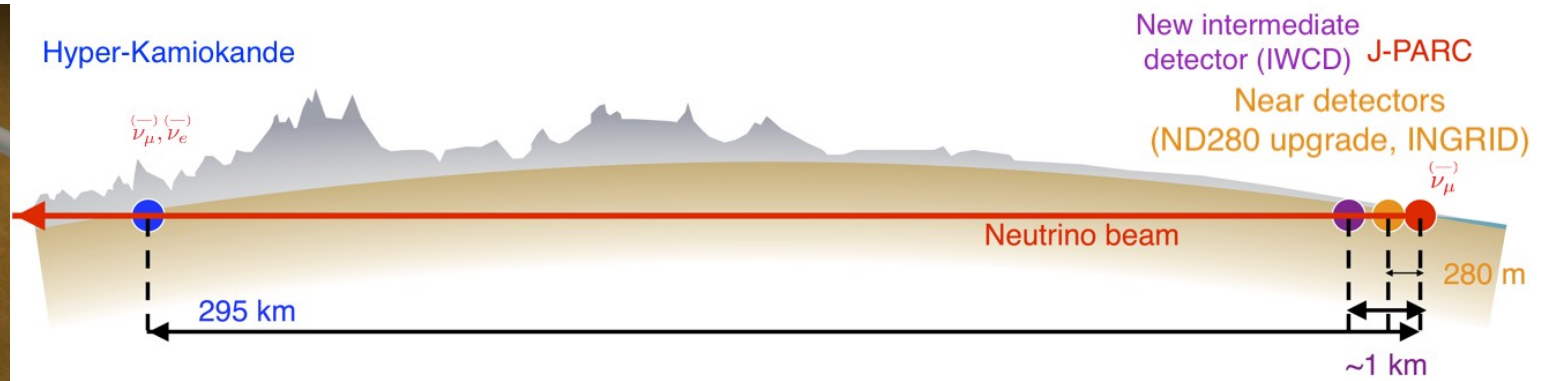
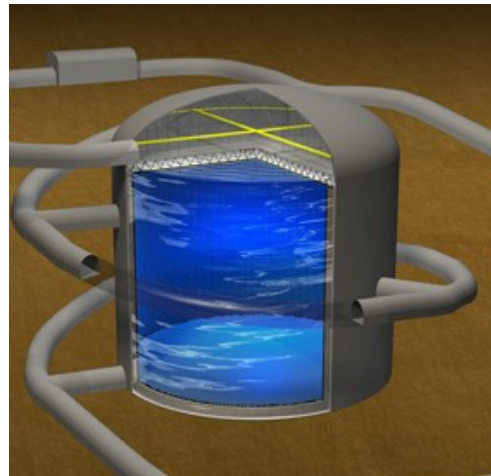
Present

Present

Future

Future

Hyper-K overview

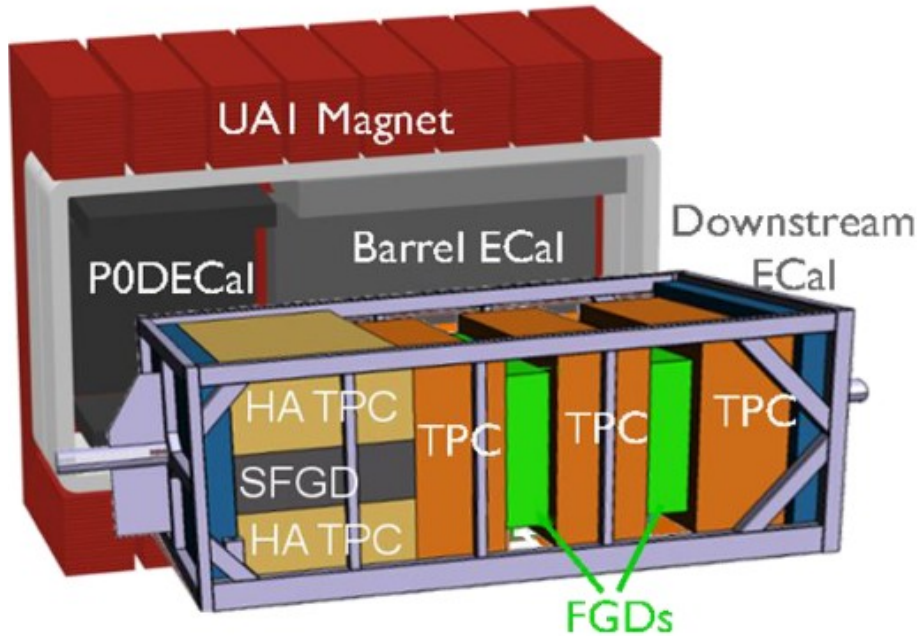


Credit: L. Pickering

- $L \approx 295 \text{ km}$; $E_\nu \approx 0.6 \text{ GeV}$ (*narrow band*); water Cherenkov detector
- Significant upgrade to T2K design:
 - 1.3 MW beam
 - Upgraded near detector complex
 - 187 kt FV tank ($\sim 7x$ Super-K FV)
- Civil construction underway, physics ~ 2028

Hyper-K near detector

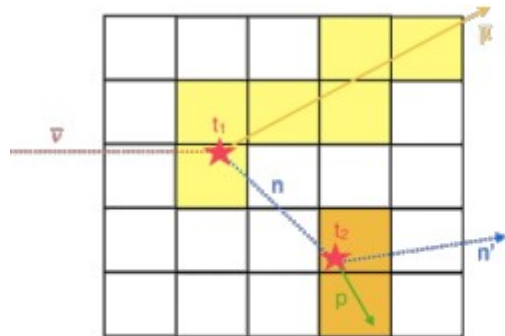
2.5° off axis



Upgraded (T2K) ND280:

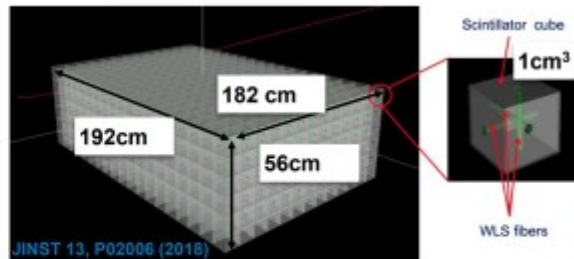
- High resolution SFGD
- Improved angular acceptance
- Neutron tagging capabilities

+Intermediate Water Cherenkov Detector (IWCD)



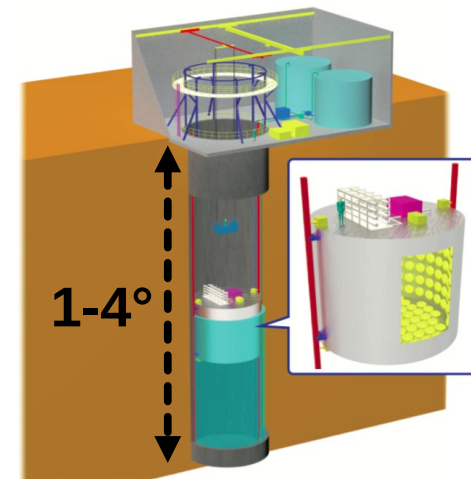
Neutron measurements

Phys. Rev. D **101**, 092003
Phys. Rev. D **110**, 032019

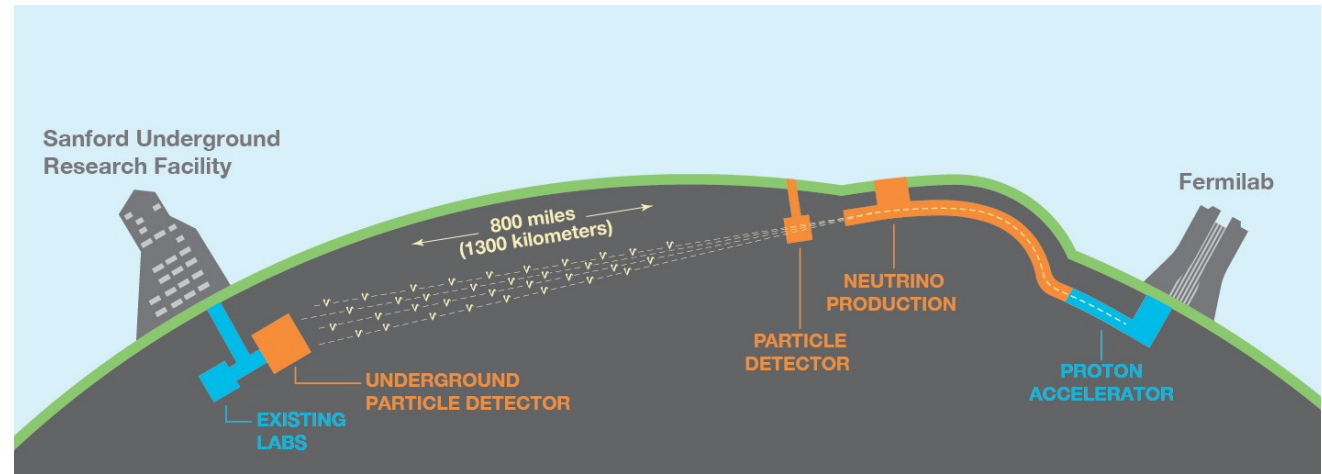
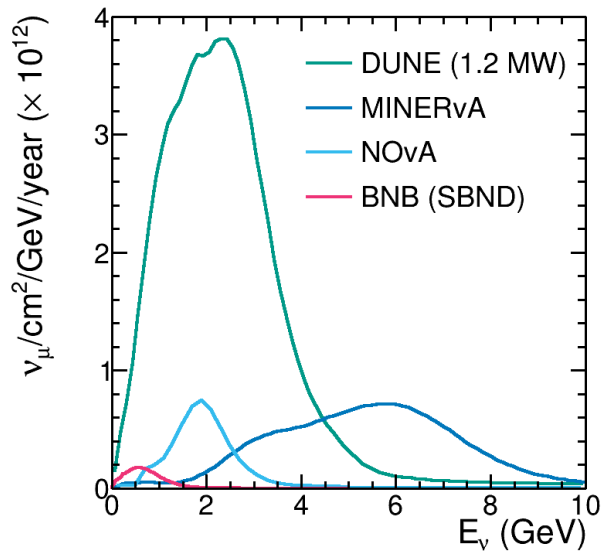


Super-fine granularity

JINST **13**, P02006



DUNE overview



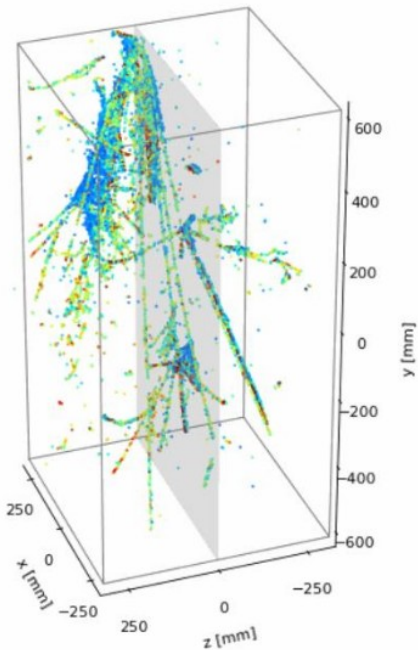
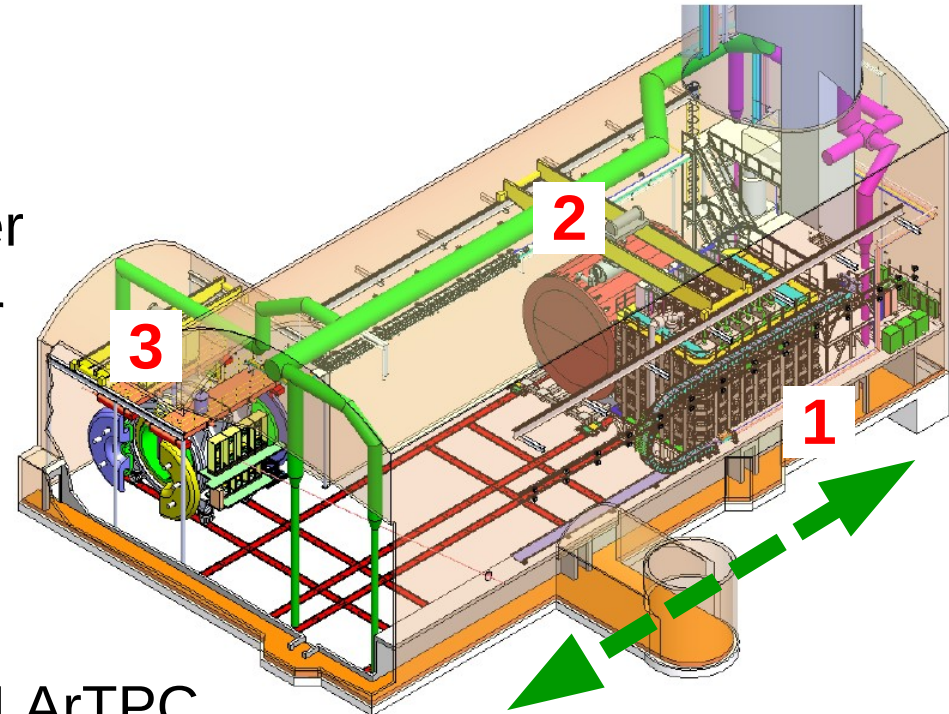
- $L \approx 1285$ km; $E_{\nu} \approx 2.5$ GeV (*broad band*); liquid argon time projection chamber (LArTPC)
- High-intensity neutrino beam (1.2 \rightarrow 2.4 MW)
- Near detector system at Fermilab
- 4 x 17 kt LAr far detector modules at SURF

DUNE near detector

Moveable

Three major components:

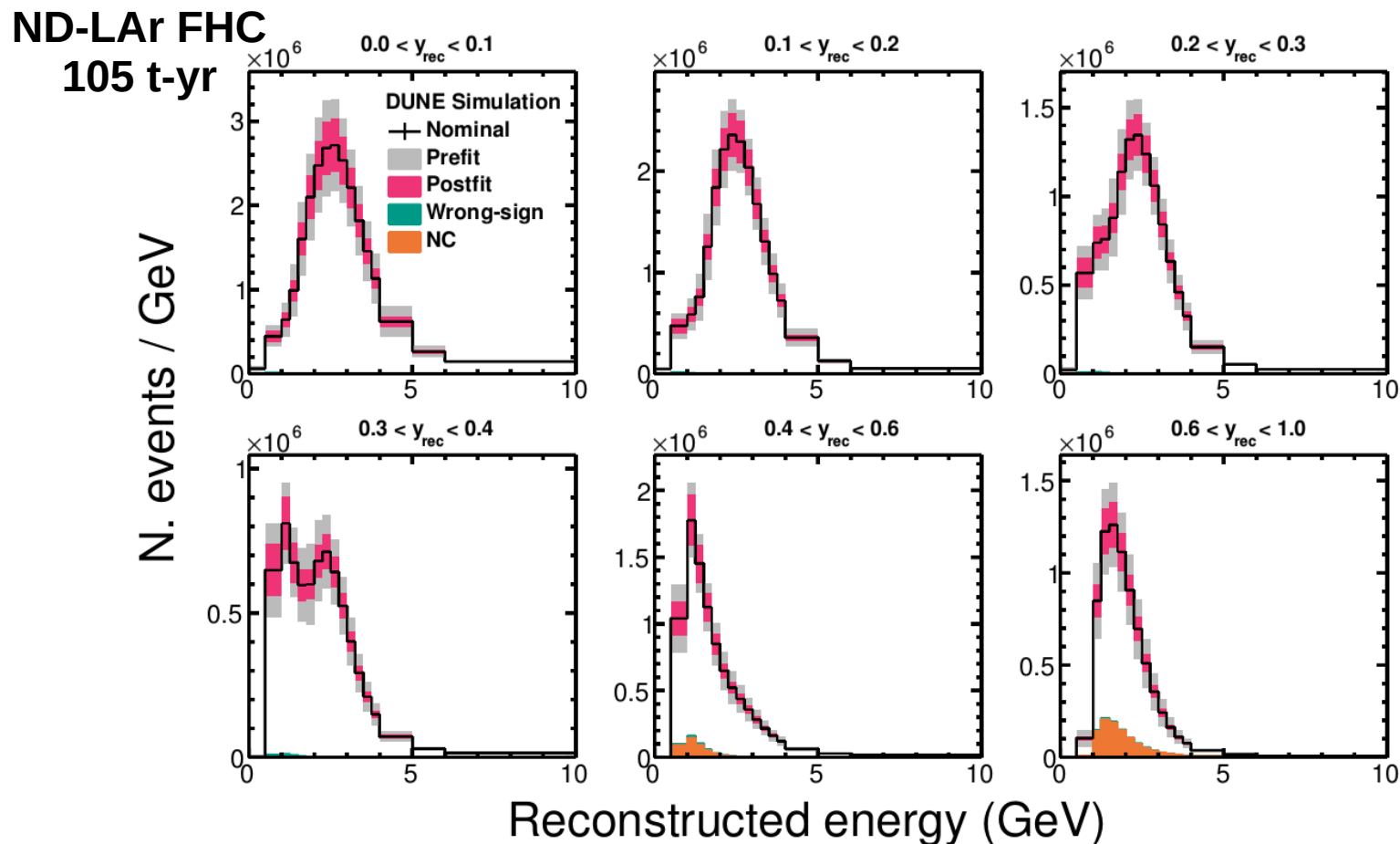
- 1 – Pixelated 150 t LArTPC
- 2 – Downstream magnetized tracker
- 3 – SAND: dedicated beam monitor



- High resolution core LArTPC
- Off-axis movement accesses different fluxes
- Some neutron detection abilities with SAND
- Magnet allows separation/constraint of $\nu/\bar{\nu}$
- Able to tolerate high rate environment

A high-rate environment?

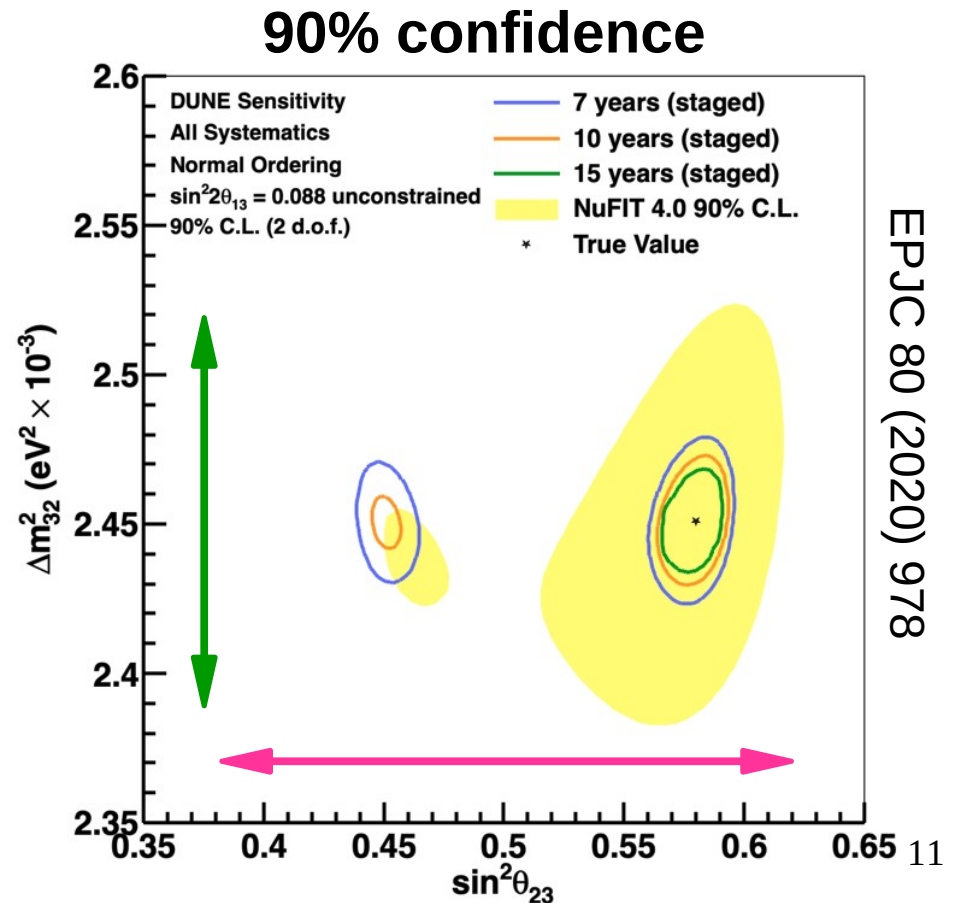
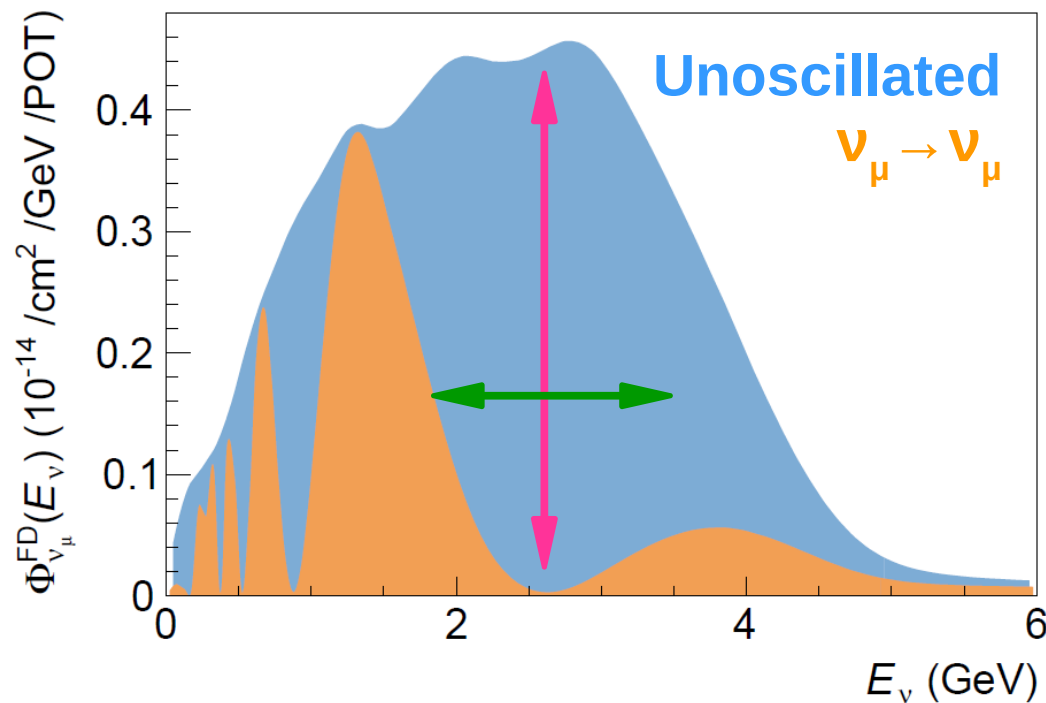
≈ 100 million events/year in the DUNE ND LArTPC



Measurement aims: disappearance

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu) = 1 - (\underbrace{\cos^4 \theta_{13} \sin^2 2\theta_{23}}_{\text{pink bar}} + \underbrace{\sin^2 2\theta_{13} \sin^2 \theta_{23}}_{\text{green bar}}) \sin^2 \Phi_{32} + \dots$$

$$\Phi_{ji} = \frac{1.27 \Delta m_{ji}^2 L}{E_\nu}$$



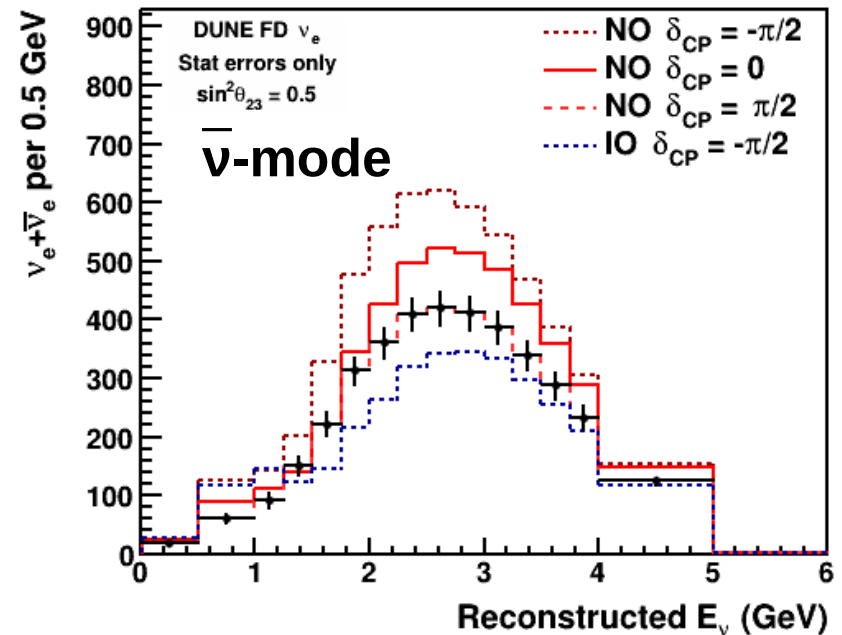
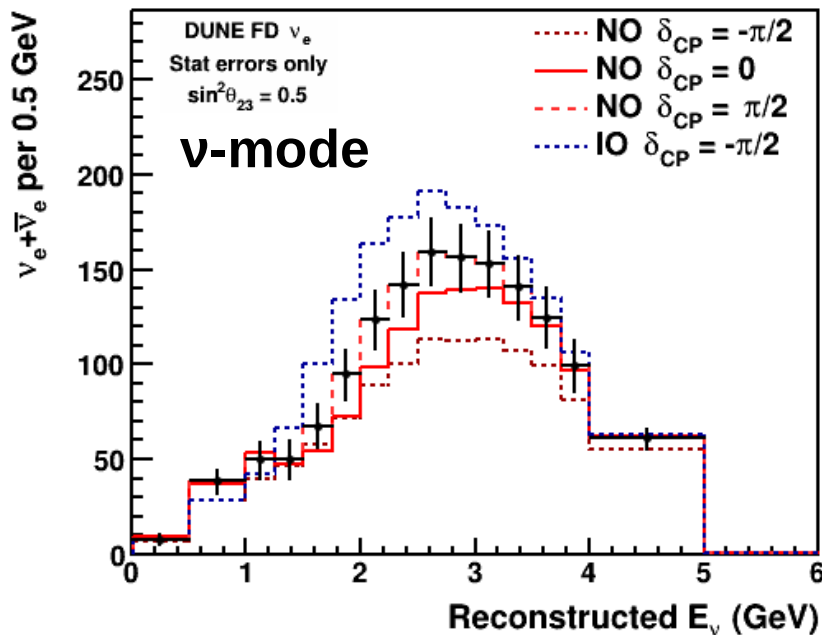
Measurement aims: MO and CPV

$$\begin{aligned}
 P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) &= \sin^2 \theta_{23} \sin^2 2\theta_{13} \frac{\sin^2(\Phi_{31} - aL)}{(\Phi_{31} - aL)^2} \Phi_{31}^2 \\
 &+ \sin 2\theta_{23} \sin 2\theta_{13} \sin 2\theta_{12} \frac{\sin(\Phi_{31} - aL)}{(\Phi_{31} - aL)} \Phi_{31} \frac{\sin(aL)}{(aL)} \Phi_{21} \cos(\Phi_{31} \pm \delta_{CP}) \\
 &+ \dots \\
 \Phi_{ji} &= \frac{1.27 \Delta m_{ji}^2 L}{E_\nu} \quad a = \pm \frac{G_F N_e}{\sqrt{2}}
 \end{aligned}$$

Sign change
for ν_e and $\bar{\nu}_e$

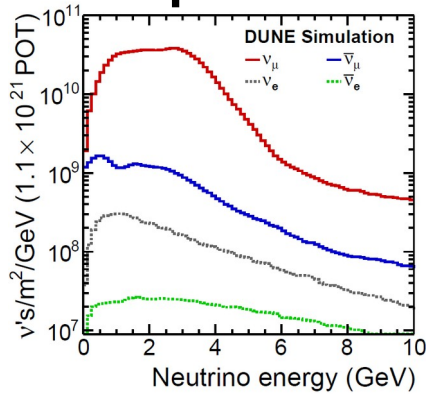
Interplay
between MO
and δ_{CP}

Matter effect
increases with E_ν ,
Enhances MO
sensitivity

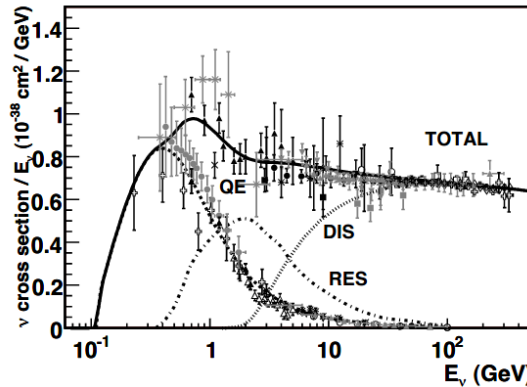


Sketch of an oscillation analysis

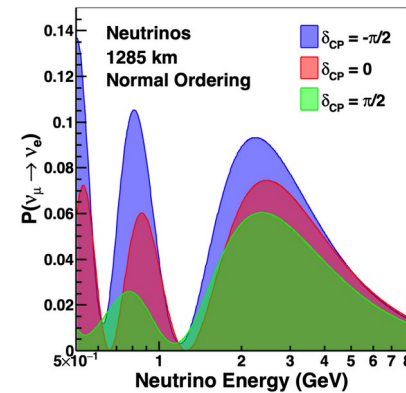
Flux prediction



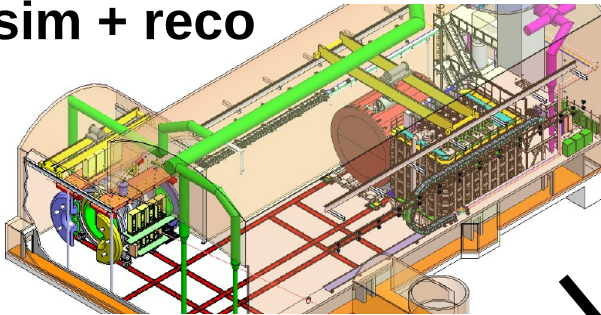
Interaction model



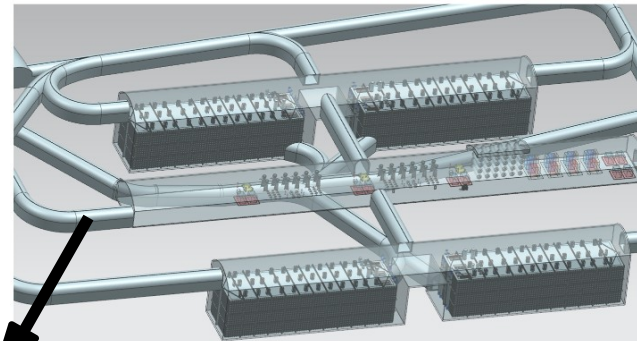
Oscillations



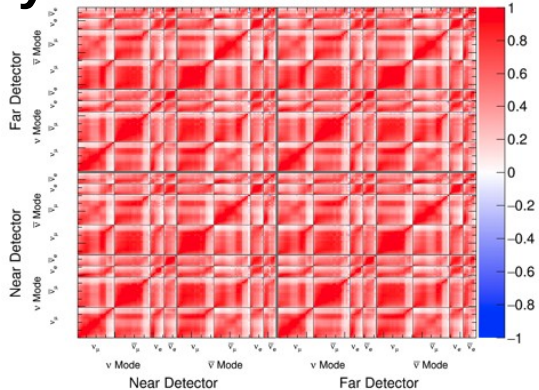
ND sim + reco



FD sim + reco



Systematic uncertainties



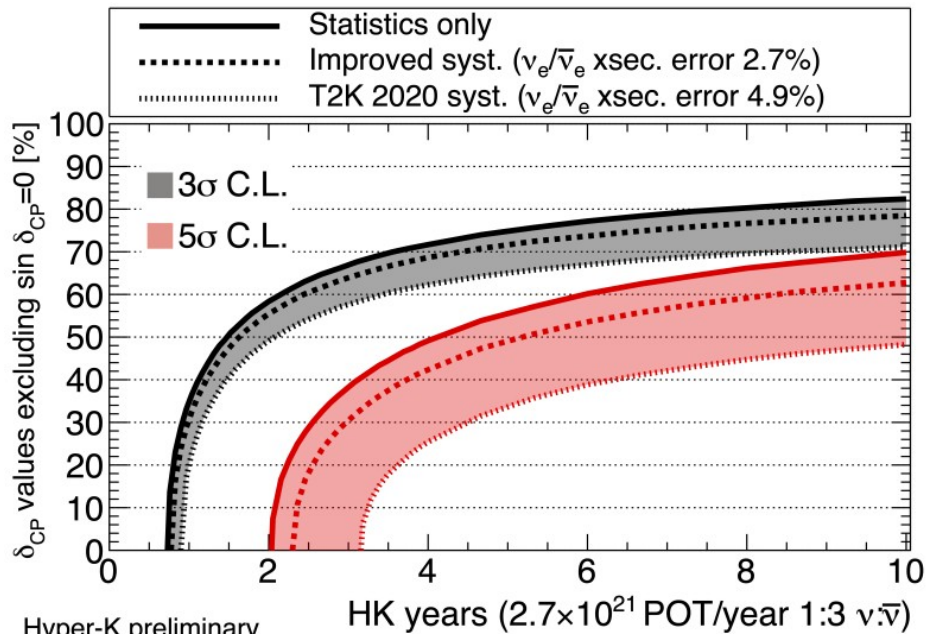
$$\chi^2(\vec{\vartheta}, \vec{x}) = 2 \sum_i^{N_{\text{bins}}} \left[M_i(\vec{\vartheta}, \vec{x}) - D_i + D_i \ln \left(\frac{D_i}{M_i(\vec{\vartheta}, \vec{x})} \right) \right] + \sum_j^{N_{\text{sys}}} \left[\frac{\Delta x_j}{\sigma_j} \right]^2$$

Fitting framework

EPJC 80 (2020) 978

PRD 105 (2022) 7, 072006

Hyper-K sensitivity projections

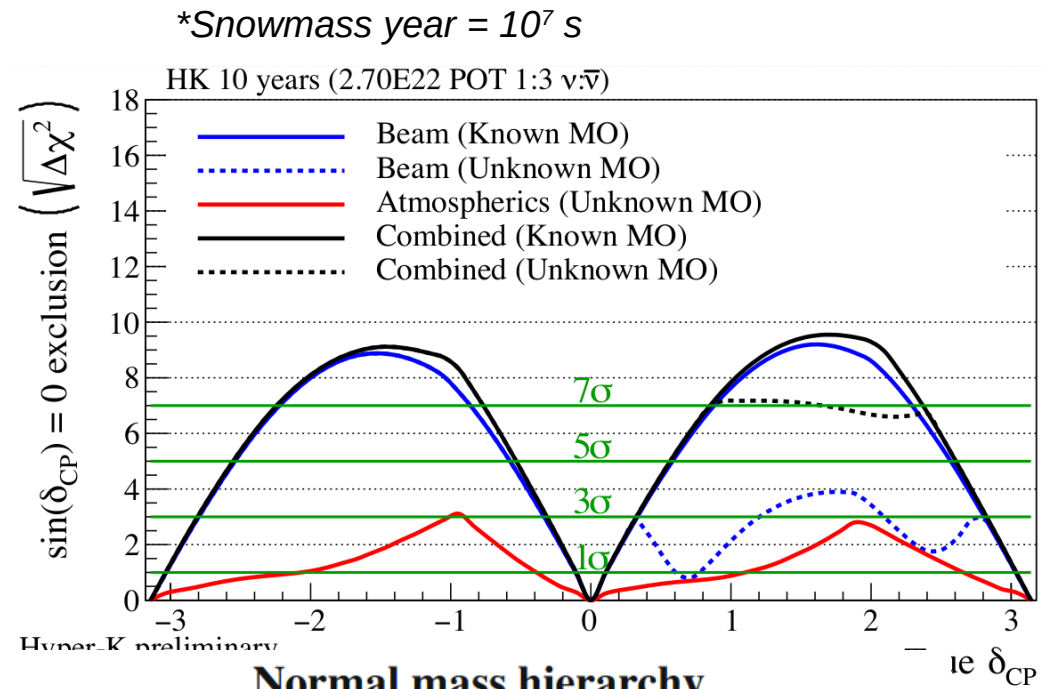


Hyper-K preliminary

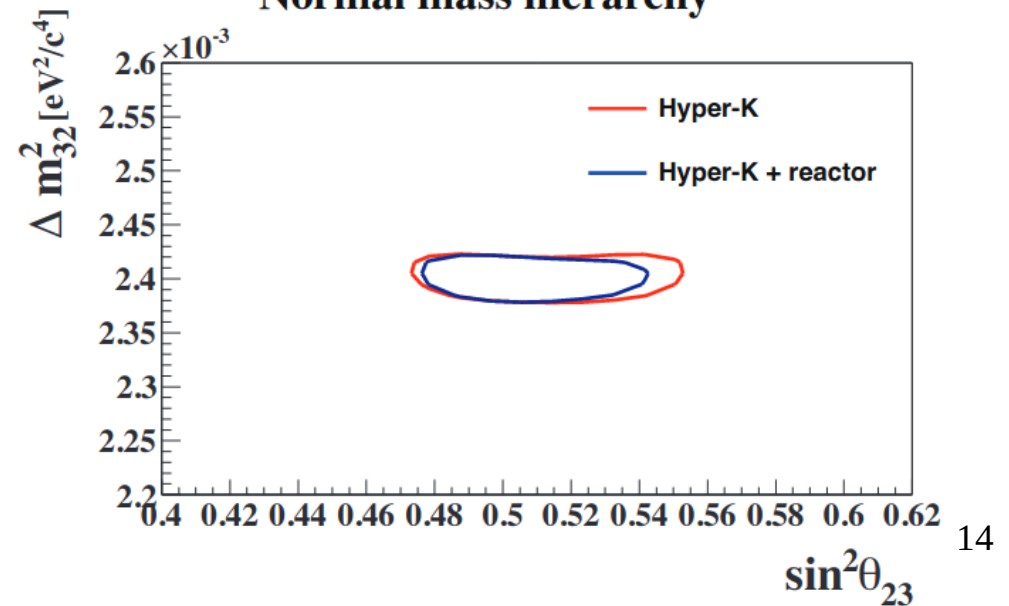
True normal ordering (known)

$$\sin^2 \theta_{13} = 0.0218 \pm 0.0007, \sin^2 \theta_{23} = 0.528, \Delta m_{32}^2 = 2.509 \times 10^{-3} \text{ eV}^2/c^4$$

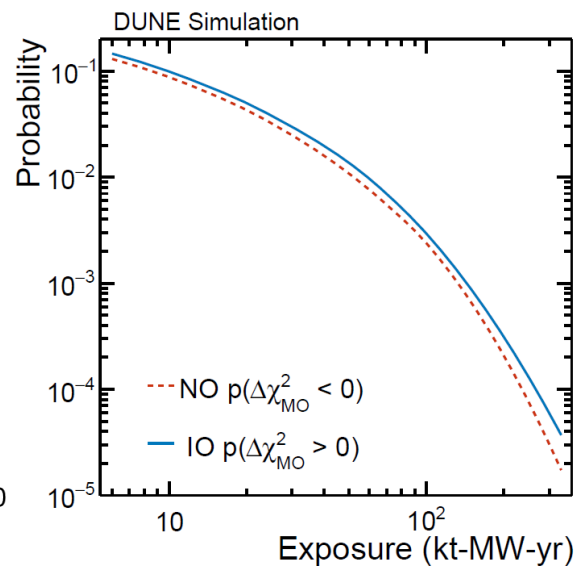
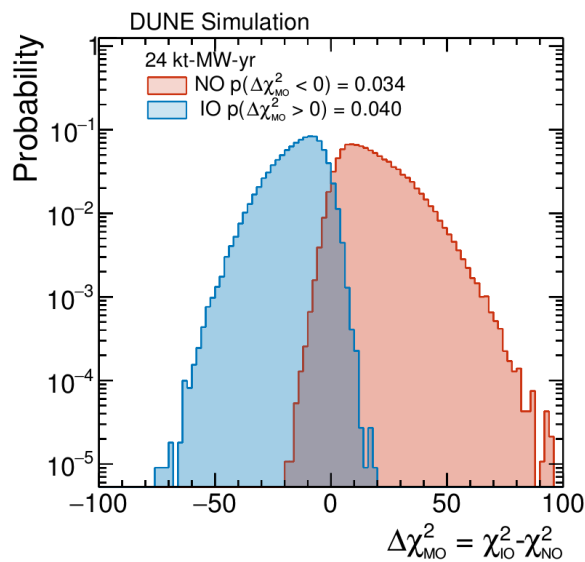
- Strong CPV constraint – MO from atmospheric or other experiments
- >3 σ CPV, 50% δ_{CP} values in 2 years
- >5 σ CPV, 50% δ_{CP} values in 5 years
- Precision δ_{CP} , Δm_{32}^2 , θ_{23} , θ_{13}



Normal mass hierarchy



DUNE sensitivity projections

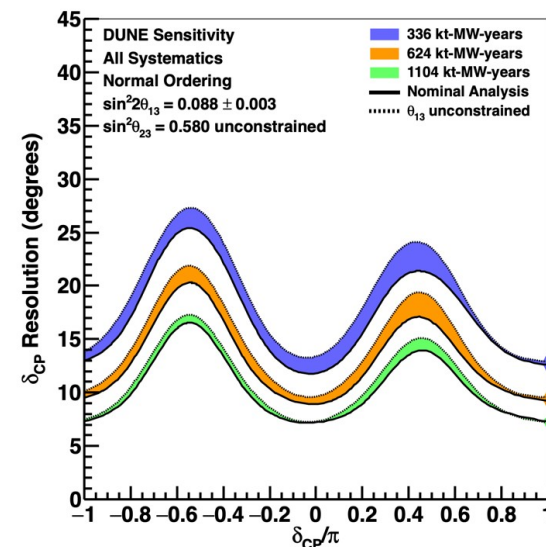
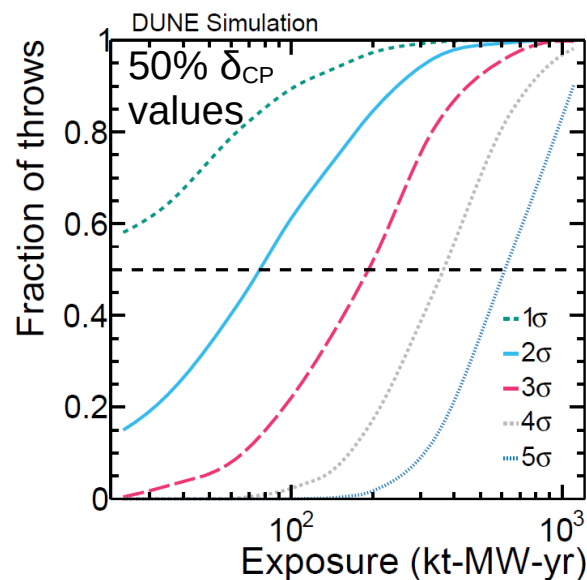
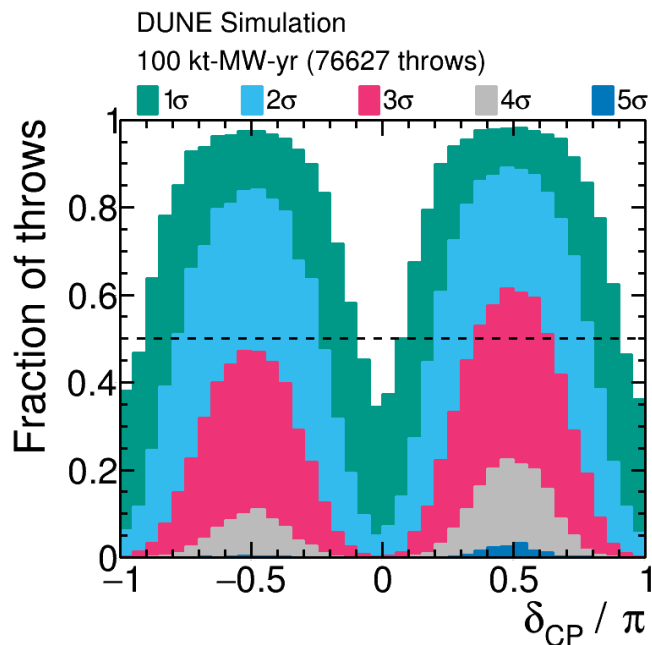


Phase I:

- MO to $>5\sigma$
- 3σ CPV if $\delta_{\text{CP}} \pm \pi/2$

Phase II:

- $>5\sigma$ CPV, $>50\%$ δ_{CP} values
- $>3\sigma$ CPV, $>75\%$ δ_{CP} values
- Precision δ_{CP} , Δm_{32}^2 , θ_{23} , θ_{13}



Fantastic, I'm sold!





What are the limiting systematics?



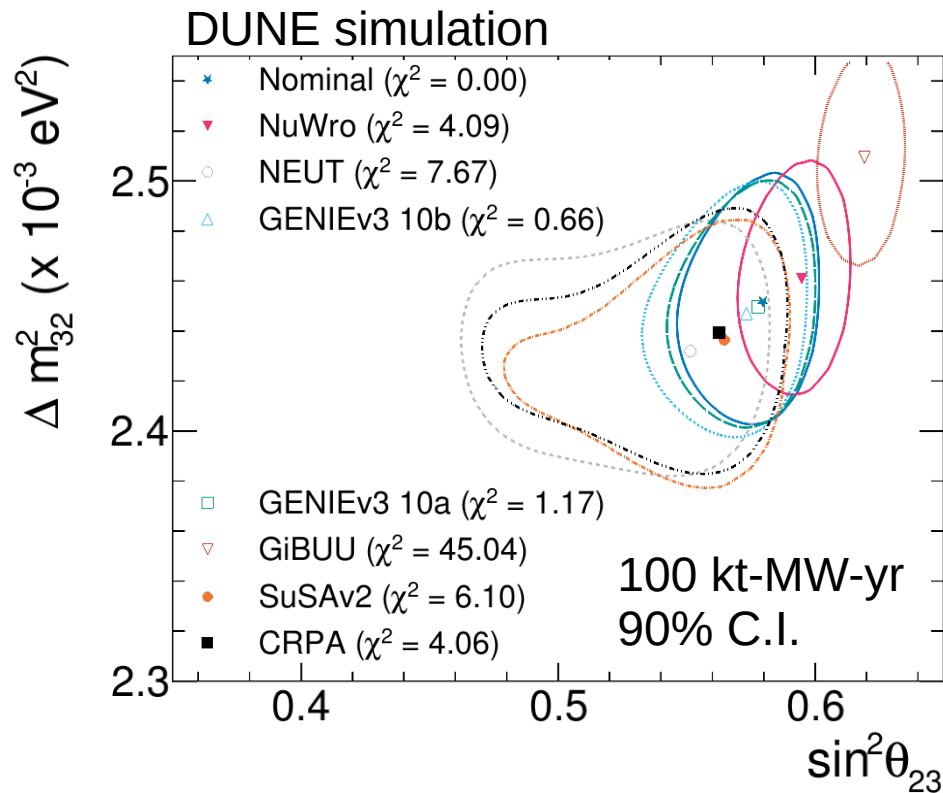
- Current experiments are statistics limited ~ 100 FD ν_e events
- DUNE+HK will be systematics limited ~ 1000 FD ν_e events
- **Cross-section systematics are dominant systematic now**
- DUNE/HK: need residual ND \rightarrow FD uncertainties \approx percent level

Current systematic uncertainties

(Table from S. Dolan's NuFact talk)

Uncertainty on N_e^{rec}		
Cross Sections	$\sim 4\%$	$\sim 3.5\%$
All Syst.	$\sim 5\%$	$\sim 3.5\%$

How limiting?



- DUNE example: ND+FD fit with full* systematic uncertainty model
- Alternative model choice leads to out of model biases
- If we were operating DUNE now, this **would be** limiting

*EPJC 80 (2020) 978

PRD 105 (2022) 7, 072006

What about the near detectors???

Event rate

Neutrino flux

Cross section

Detector smearing

Oscillation probability

$$R(\vec{x}) = \int dE \underbrace{\Phi(E_\nu) \times \sigma(E_\nu, \vec{x})}_{\text{Near}} \times \underbrace{\epsilon(\vec{x}) \times P(E_\nu; \nu_A \rightarrow \nu_B)}_{\text{Far}}$$

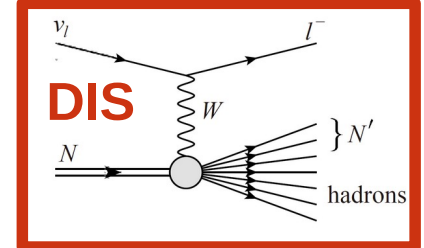
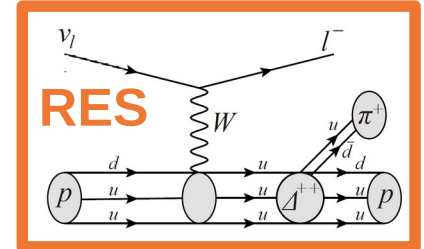
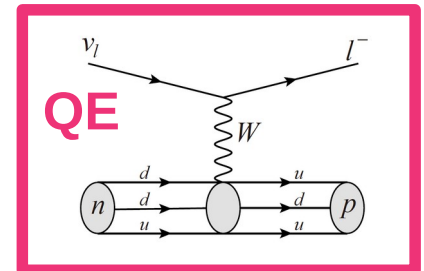
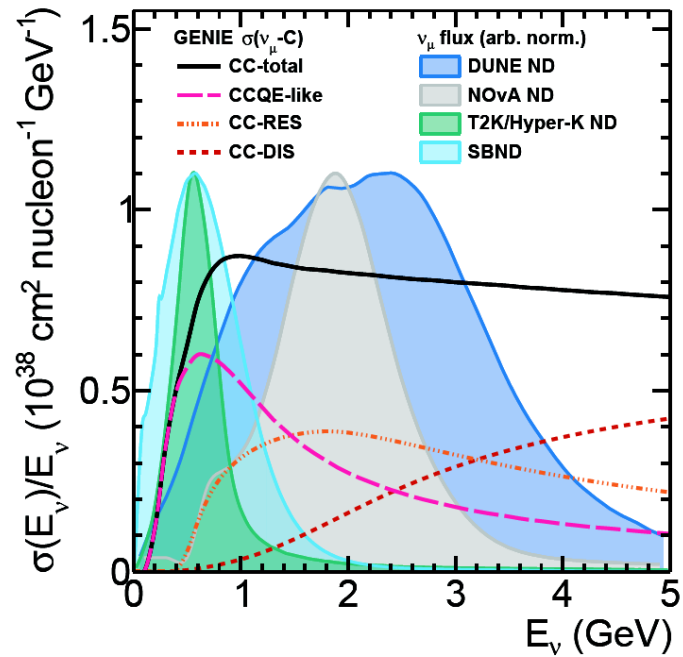
- Ambiguities between cross-section and flux uncertainties
- Different fluxes between near and far
- Imperfect and non-identical ND and FD
- Missing degrees of freedom! Model differences cannot be covered by systematics in the base model



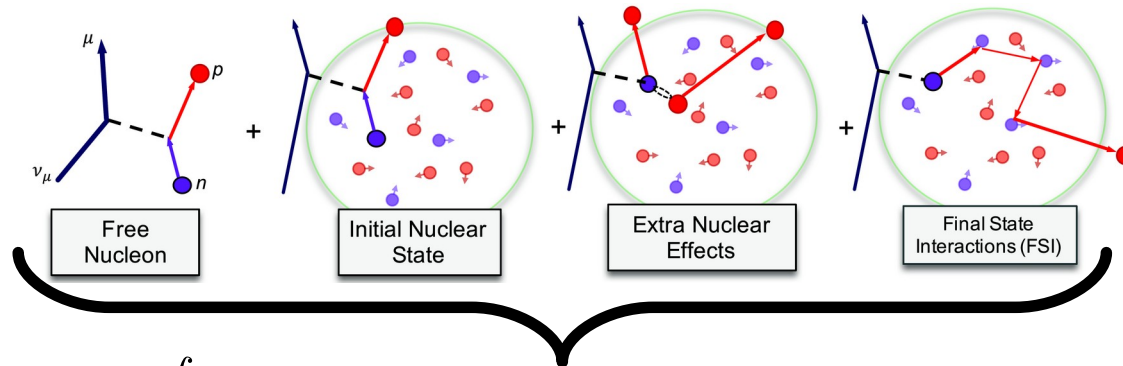
So what do we need to model?

Key issues:

- E_ν dependence
- E_ν reconstruction
- ν_e/ν_μ and $\bar{\nu}_e/\bar{\nu}_\mu$
- Extrapolation out of detector acceptance

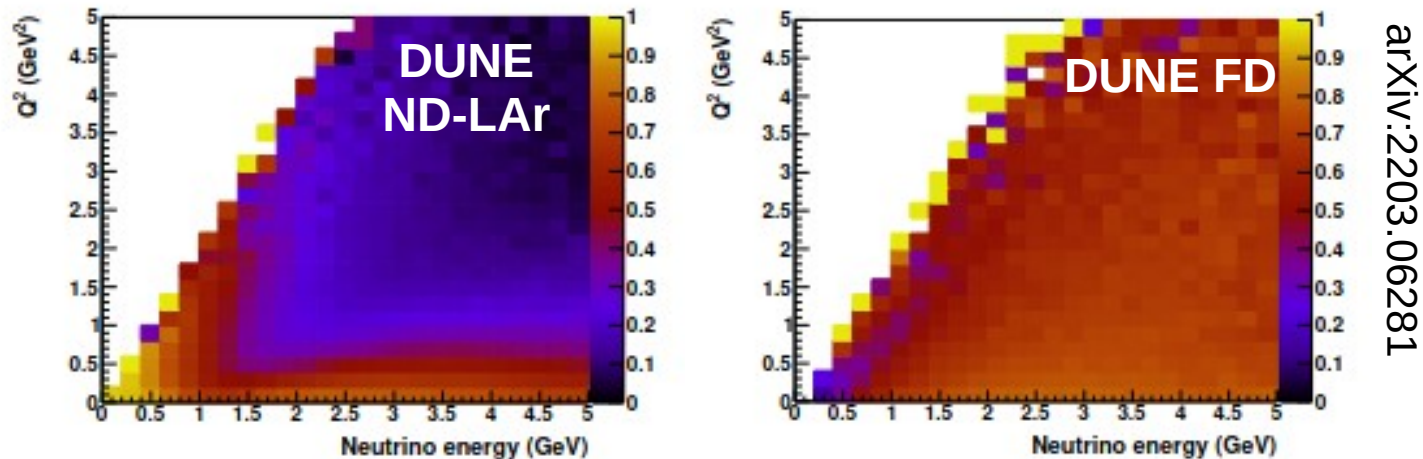


Energy transfer



$$R(\vec{x}) = \int dE \Phi(E_\nu) \times \sigma(E_\nu, \vec{x}) \times \epsilon(\vec{x}) \times P(E_\nu; \nu_A \rightarrow \nu_B)$$

Extrapolation out of detector acceptance

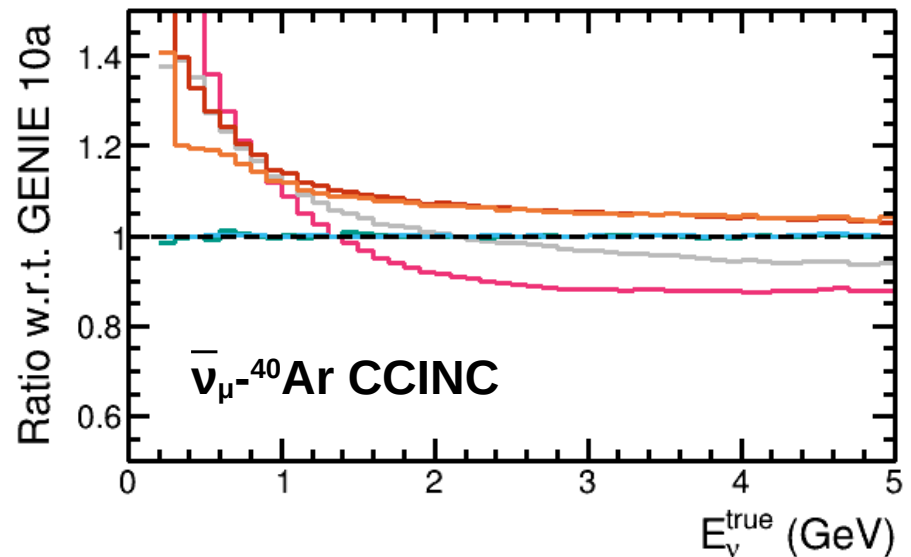
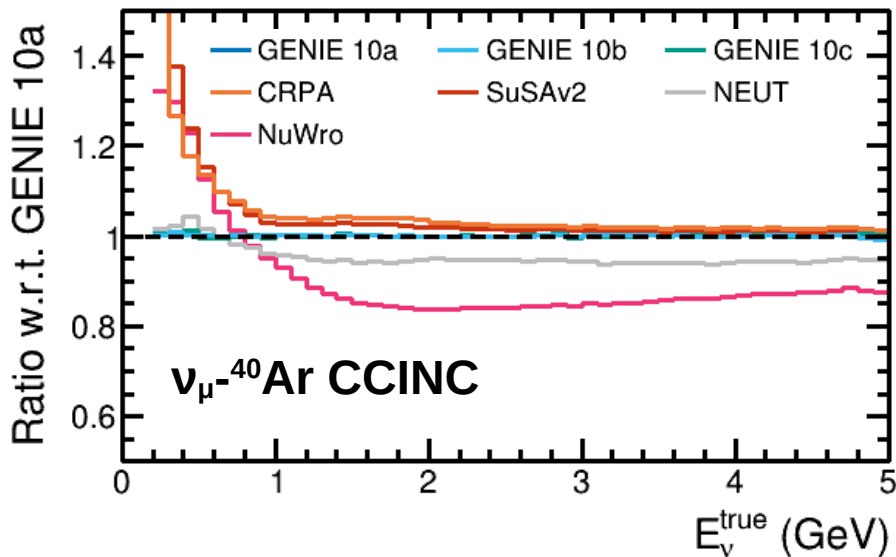
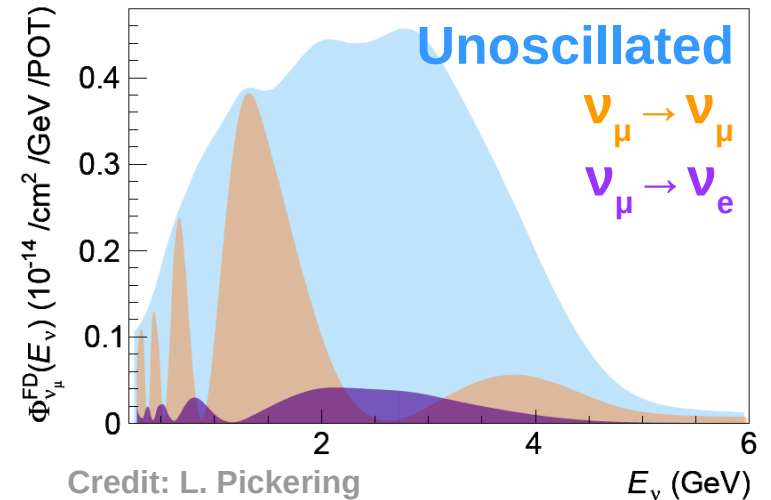


arXiv:2203.06281

- ND and FD acceptances are different even if designs are similar → detector size, pile-up
- Implicit trust in model and uncertainties to extrapolate to the additional phase-space

E_ν dependence

- Different ND and FD fluxes: ND \rightarrow FD extrapolation relies on E_ν dependence
- Differences between current models +inconsistent between ν_μ and $\bar{\nu}_\mu$
- True for both HK and DUNE



E_ν reconstruction methods

(1) **Leptonic** variables only:

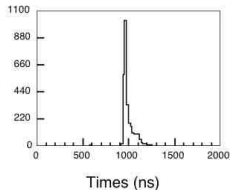
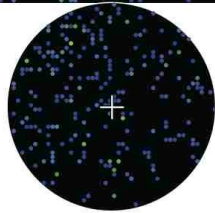
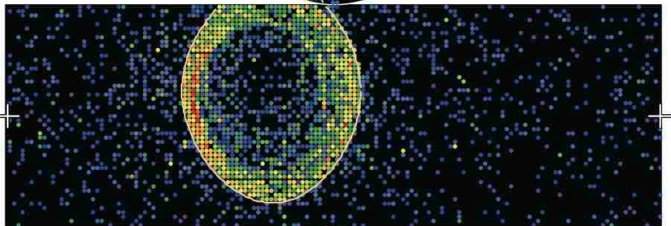
$$E_\nu^{QE} = \frac{m_p^2 - m_n'^2 - m_\mu^2 + 2m_n' E_\mu}{2(m_n' - E_\mu + p_\mu \cos \theta_\mu)}$$

Super-Kamiokande

Run 3962 Sub 125 Ev 965982
97-05-01:15:32:29
Inner: 2887 hits, 9607 pE

Charge (pe)

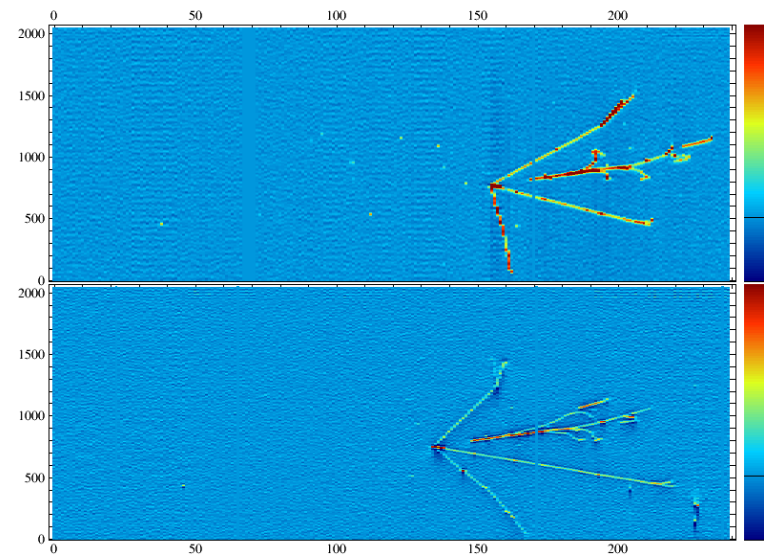
- * >26.7
- * 23.3-26.7
- * 20.2-23.3
- * 17.3-20.2
- * 14.7-17.3
- * 12.2-14.7
- * 10.0-12.2
- * 8.0-10.0
- * 6.2- 8.0
- * 4.7- 6.2
- * 3.3- 4.7
- * 2.2- 3.3
- * 1.3- 2.2
- * 0.7- 1.3
- * 0.2- 0.7
- * < 0.2



Water Cherenkov: T2K, Hyper-K

(2) **Leptonic** and **hadronic** information:

$$E_\nu = E_\mu + E_{\text{had}}$$



**Tracking calorimeter: NOvA;
Liquid Argon TPCs: DUNE**

E_ν reconstruction methods

(1) **Leptonic** variables only:

$$E_\nu^{QE} = \frac{m_p^2 - m_n'^2 - m_\mu^2 + 2m_n' E_\mu}{2(m_n' - E_\mu + p_\mu \cos \theta_\mu)}$$

- CC0 π
- Non-CCQE contributions
- Pion production < threshold
- Pion prod. + absorption rate
- Smearing from nuclear model

(2) **Leptonic** and **hadronic** information:

$$E_\nu = E_\mu + E_{\text{had}}$$

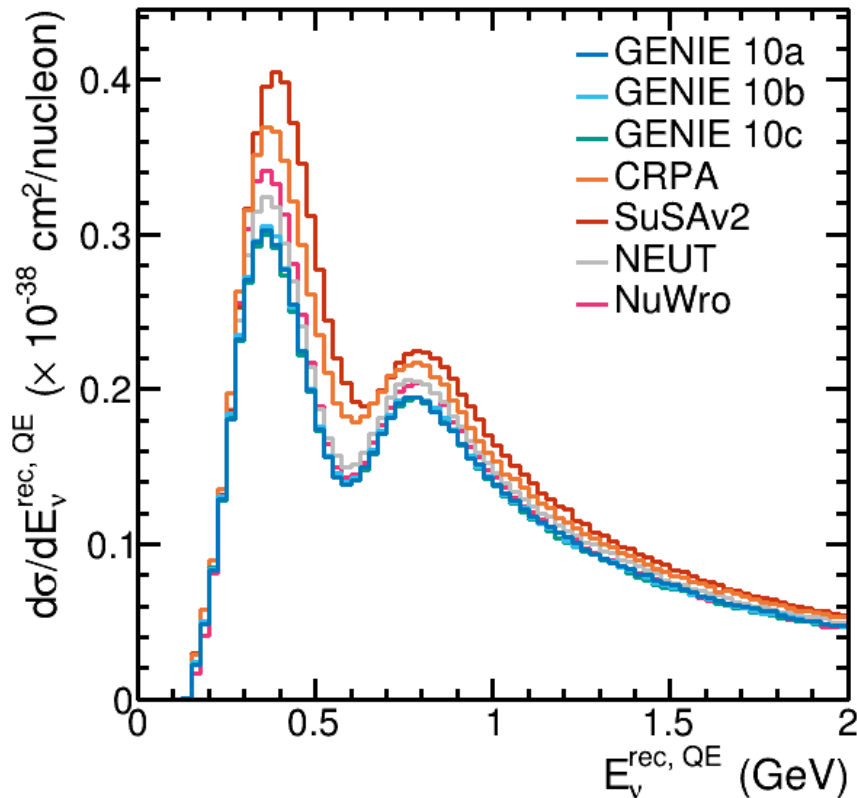
- CC-inclusive
- Pion production rate below experimental threshold
- Neutral energy fraction
- Nuclear model initial and final state effects

+ E_ν dependence for all of the above!

E_ν reconstruction status

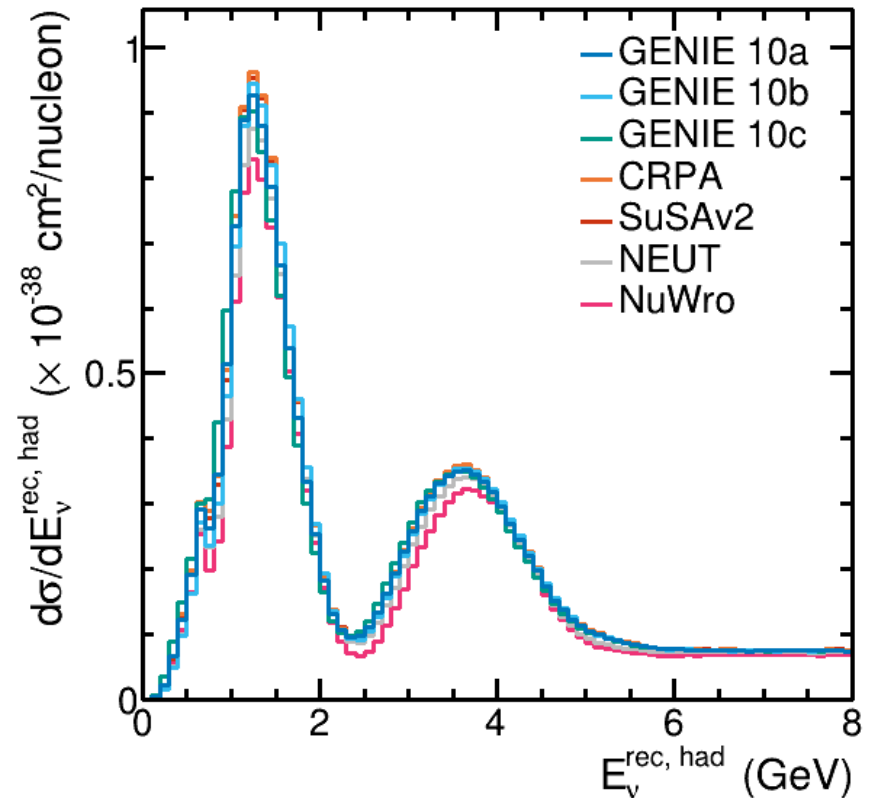
Hyper-K FHC ν_μ CC0 π

Perfect lepton reconstruction

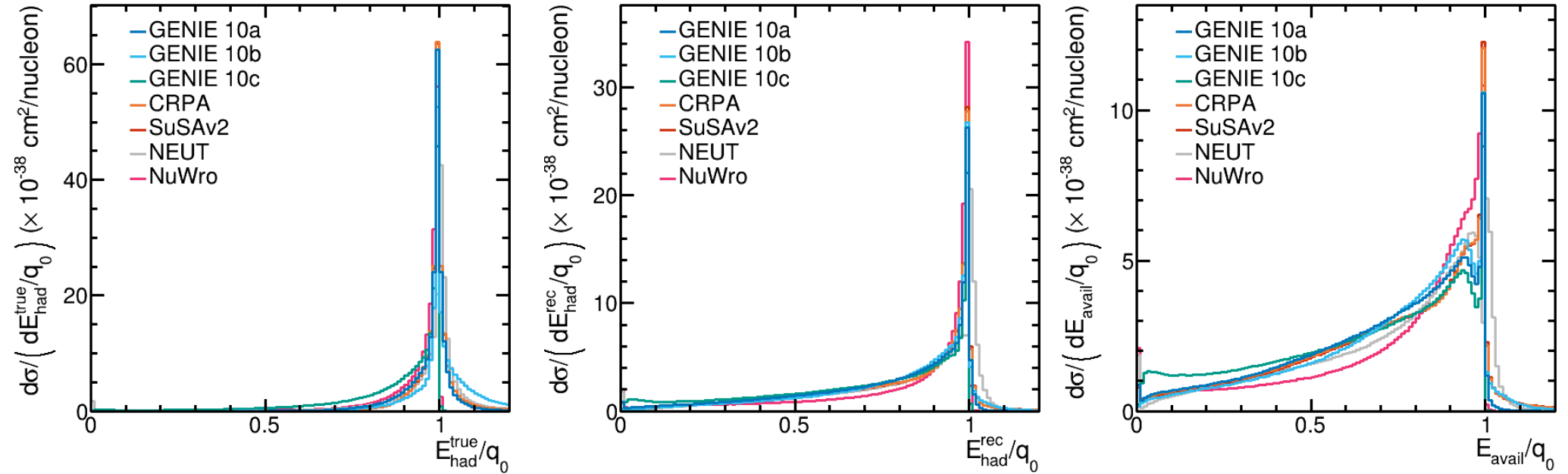


DUNE FHC ν_μ CCINC

Perfect reconstruction of all particles except neutrons



How well do we model E_{had} ?



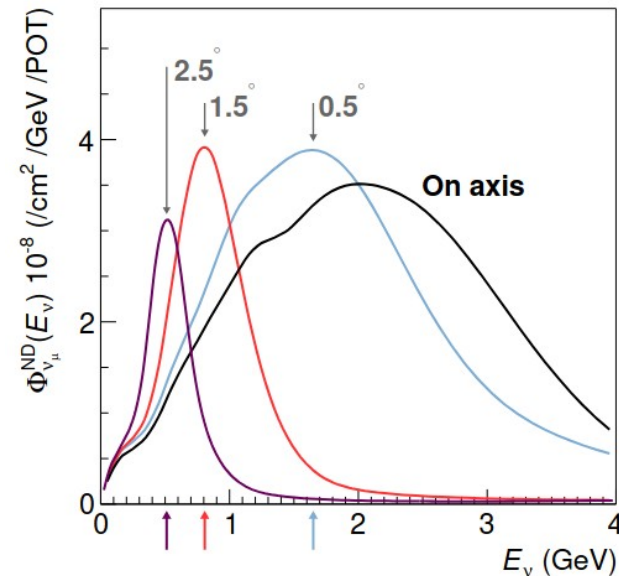
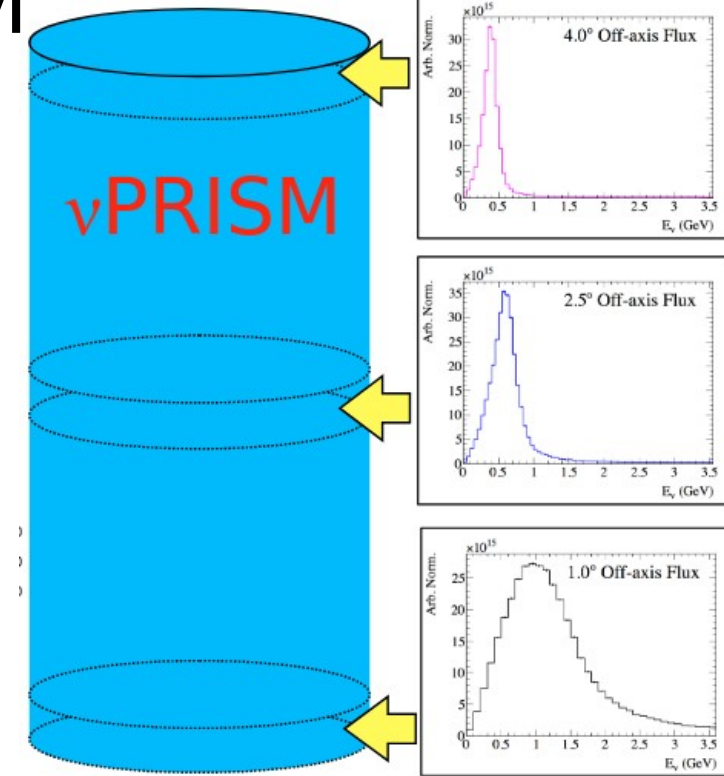
$$E_{\text{had}}^{\text{true}} = \left(\sum_{i=n,p} E_{\text{kin}}^i \right) + \left(\sum_{i=\pi^\pm, \pi^0, \gamma, K^0, K^\pm} E_{\text{total}}^i \right)$$

$$E_{\text{had}}^{\text{reco}} = \left(\sum_{i=p} E_{\text{kin}}^i \right) + \left(\sum_{i=\pi^\pm, \pi^0, \gamma, K^0, K^\pm} E_{\text{total}}^i \right)$$

$$E_{\text{avail}} = \left(\sum_{i=p, \pi^\pm} E_{\text{kin}}^i \right) + \left(\sum_{i=, \pi^0, \gamma, K^0, K^\pm} E_{\text{total}}^i \right)$$

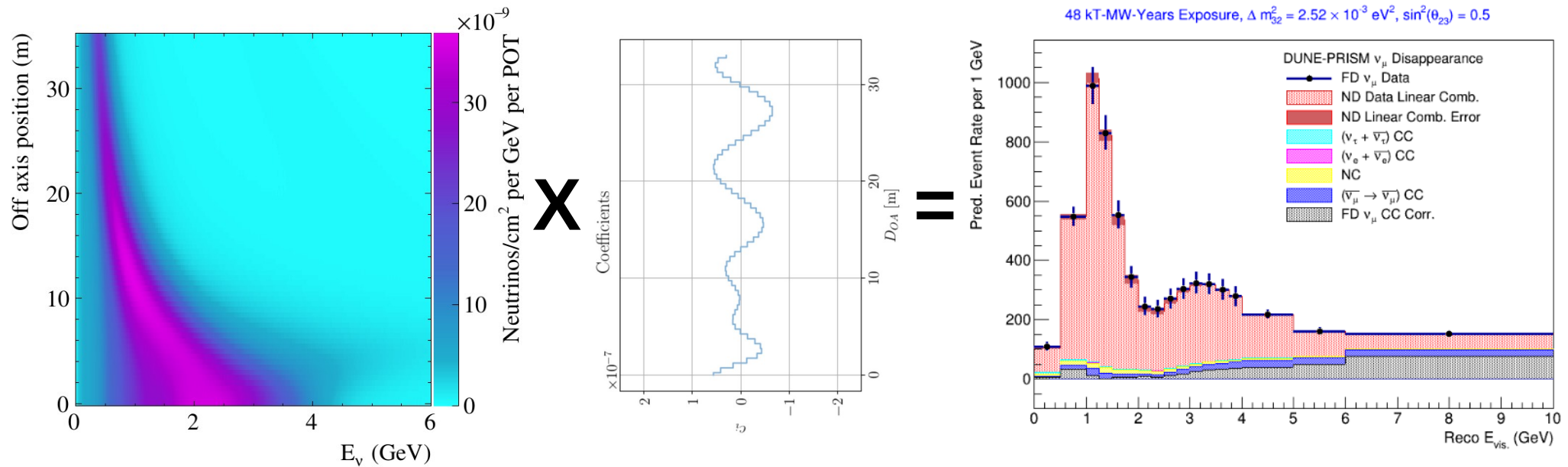
Tackling E_ν dependence: PRISM

- Moving away from the beam axis reduces the flux width and peak E_ν
- Possible with IWCD for HK and the off-axis movement of the DUNE ND
- Adds important information to break flux*XSEC degeneracy!
- But each flux is still extended and complex, still not a trivial problem



Instruments 5, no. 4, p31, 2021

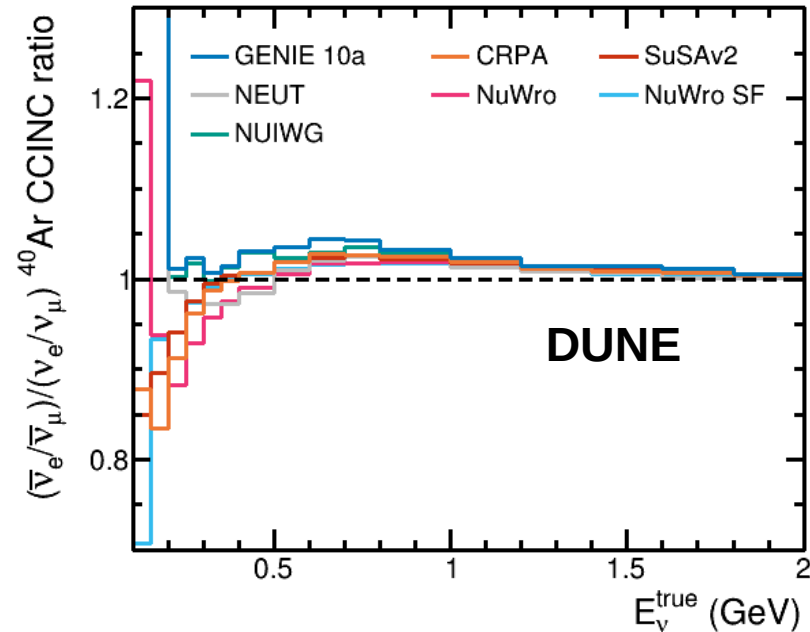
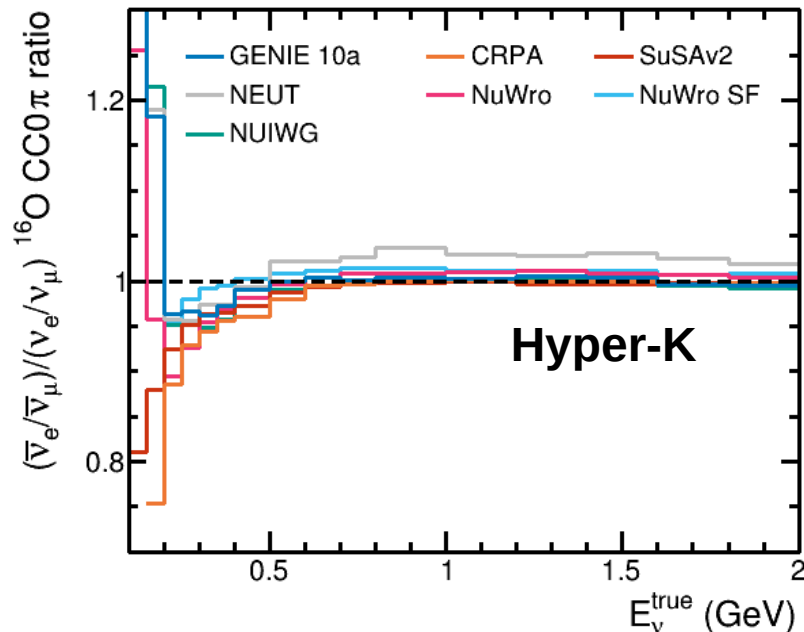
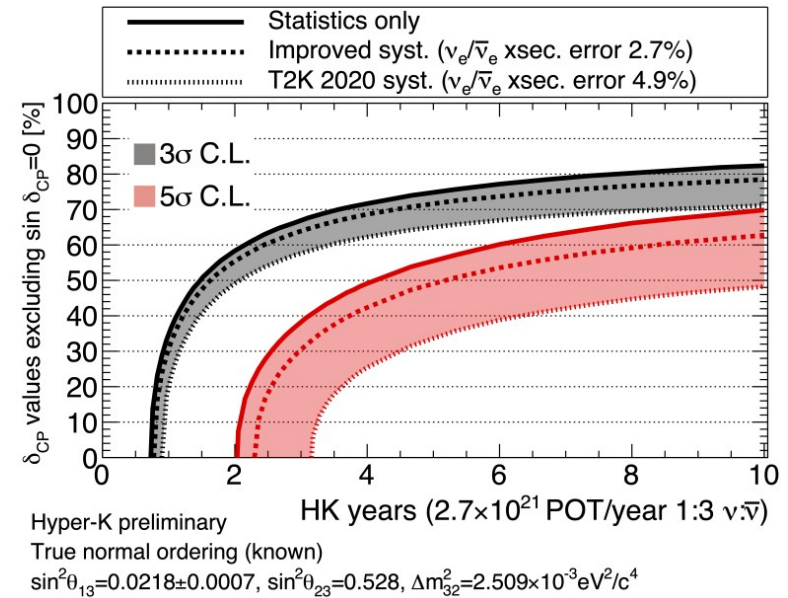
PRISM linear combination analyses



- Linear combinations of off-axis data approximate the oscillated FD flux
- *Reduces* cross-section model dependence
- **But** the overall sensitivity likely to be lower (subdividing ND statistics, complex flux uncertainty)
- Unclear what the remaining XSEC uncertainties are → stress on different parts of the model/phase space

ν_e/ν_μ and $\bar{\nu}_e/\bar{\nu}_\mu$

- ND ν_e and $\bar{\nu}_e$ rates are low, ND vs FD fluxes very different
- PRISM less useful for ν_e due to different production kinematics
- HK and DUNE likely to rely on theory, HK explicitly show impact
- Current generator implementations differ by more than assumed uncertainties



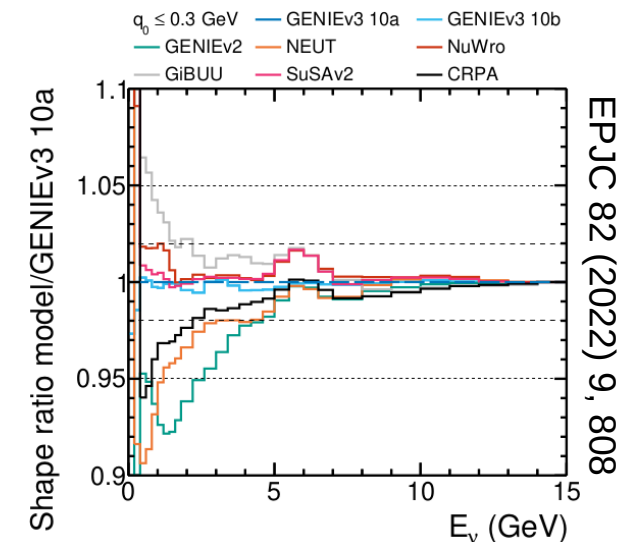
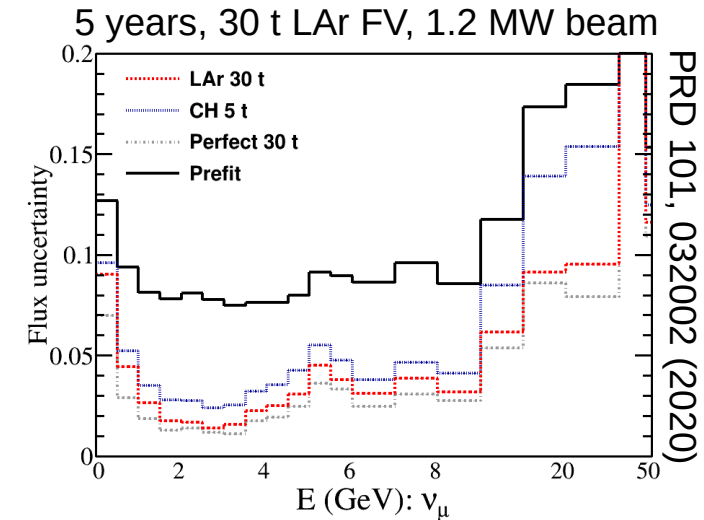
ND standard candles?

With large ND event rates, possible to utilize (faint) standard candles:

- $\nu+e \rightarrow \nu+e$ elastic scattering
- Inverse muon decay: $\nu_\mu + e \rightarrow \mu + \nu_e$
- The low- ν technique
- Isolating hydrogen events
- Coherent pion scattering

Rely on: a known cross section and/or isolating a region of phase space

New/extra challenges for systematic modeling



Do we have a path to precision?

Maybe? But not a purely experimental one...



Needs:

- A theoretically consistent XSEC model, implemented in a generator
- A robust uncertainty model
- Dedicated measurement programs
- Improved near detectors

Hinchliffe's rule [\[edit \]](#)

In the field of [particle physics](#), the concept is known as **Hinchliffe's rule**, after physicist [Ian Hinchliffe](#), who stated that if a research paper's title is in the form of a yes-no question, the answer to that question will be "no".^{[39][40]} The adage led into a humorous attempt at a [liar paradox](#) by a 1988 paper, written by physicist [Boris Kayser](#) under the pseudonym "Boris Peon", which bore the title: "Is Hinchliffe's Rule True?".^{[41][42][40]}

https://en.wikipedia.org/wiki/Betteridge's_law_of_headlines



Ultimate precision: joint fits



- Unless HK+DUNE expose significant new physics*, their joint fit will be the legacy precision oscillation measurement
- No longer adequate to consider parameters “effective” with the freedom we currently allow
- A-scaling will be a significant challenge/need
- Consistent model which is precise over a broader E_ν range
- Others?

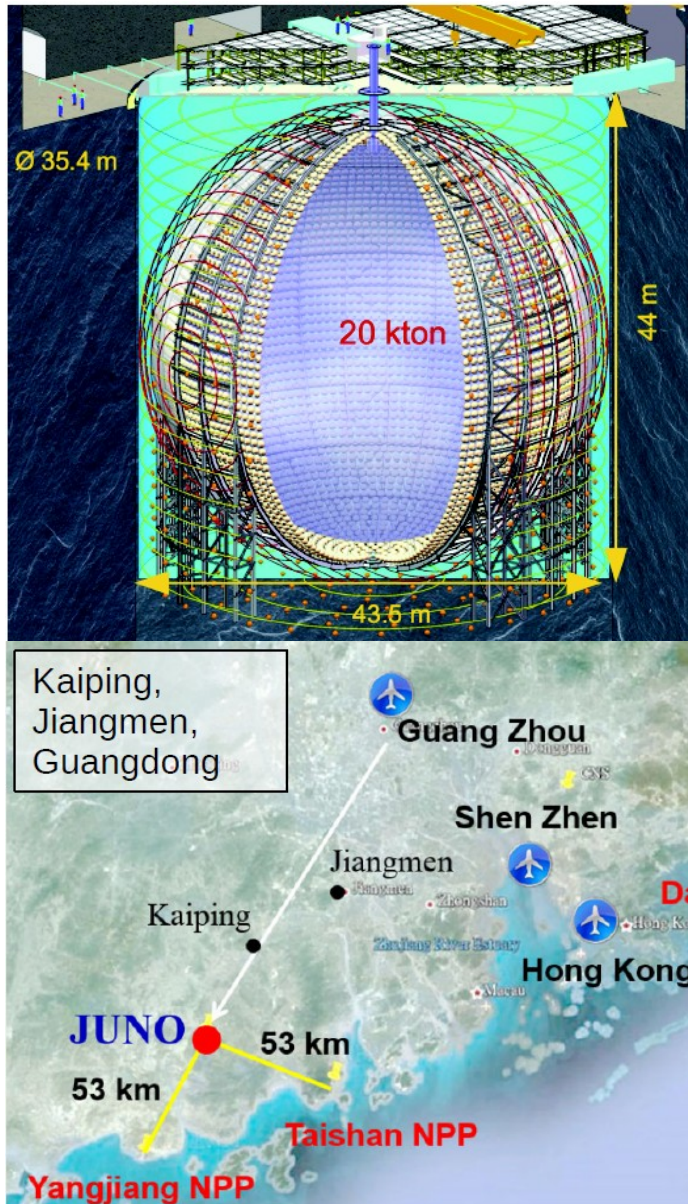
**Of course, if they do uncover new physics, the same issues will just be more urgent*

Concluding thoughts

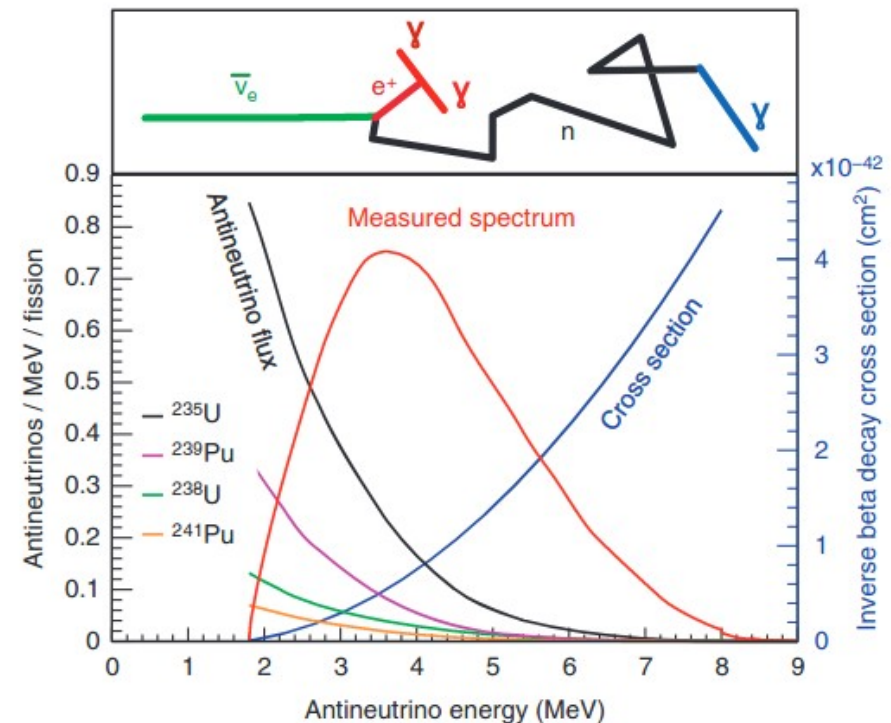
- DUNE and HK promise precision oscillation measurements
- Cross-section systematics will be limiting without significant improvements to the current situation
- A high-performance ND helps constrain the problem, and offers new opportunities!
- But, more sophisticated theory and complete uncertainty models are also essential
- A strong relationship between measurement and theory is the only way to achieve precision

Backup

JUNO: Jiangmen Underground Neutrino Observatory

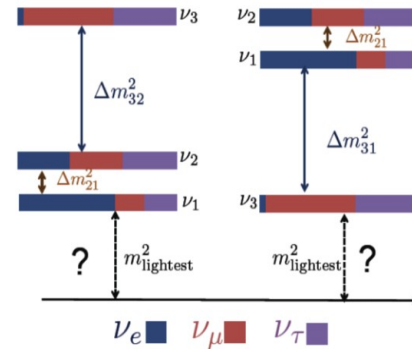
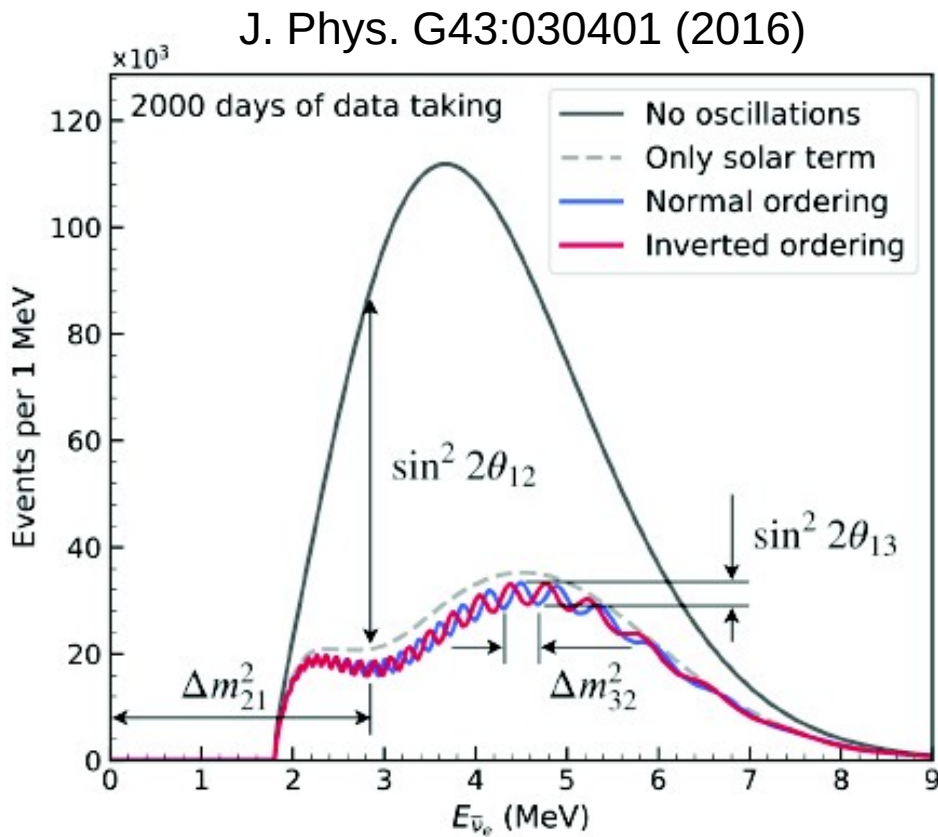


- Reactor antineutrino experiment
- 20 kt liquid scintillator detector ~50 km from 2x ~20 GW reactor complexes
- 75% photocathode coverage → 3%/√E energy resolution
- Construction ongoing, data taking 2023



Reactor neutrino future - JUNO

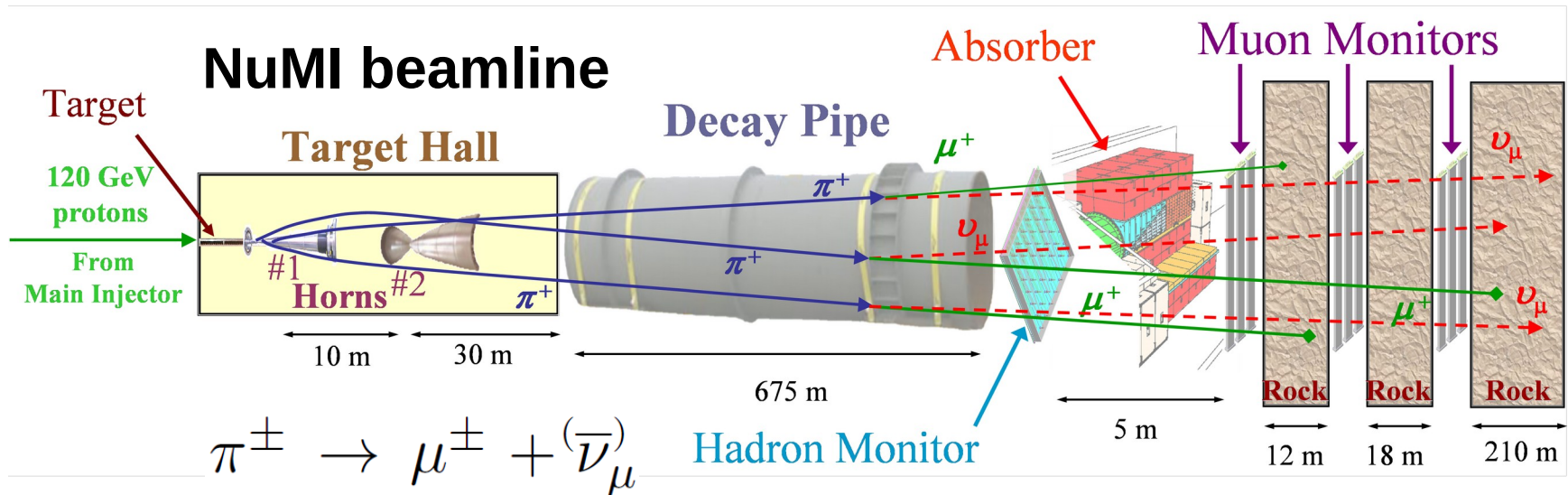
$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Phi_{31} + \sin^2 \theta_{12} \sin^2 \Phi_{32}) - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Phi_{21}$$



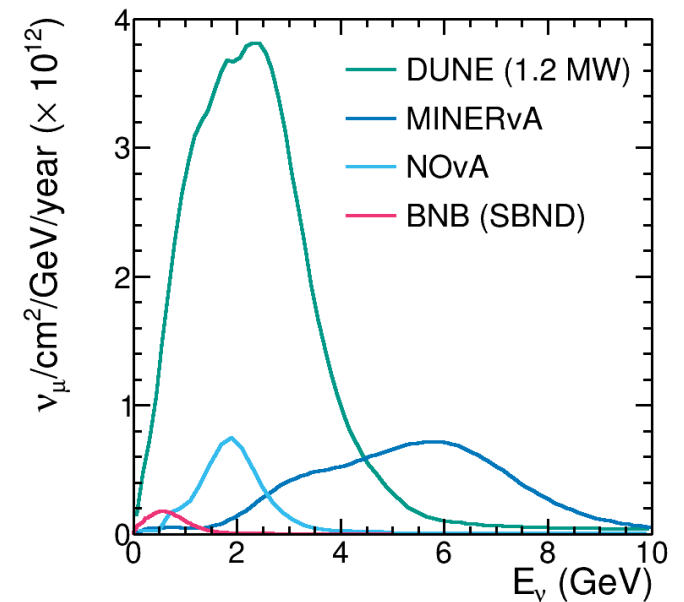
$$\Phi_{ji} = \frac{1.27 \Delta m_{ji}^2 L}{E_\nu}$$

- High-precision measurements on “solar terms” $\sin^2 \theta_{12}$ and Δm_{21}^2
- At long baselines, NO/IO spectra differ due to competing Φ_{31} and Φ_{32} terms
- **But**, clearly very sensitive to energy scale and resolution

Accelerator neutrino beams

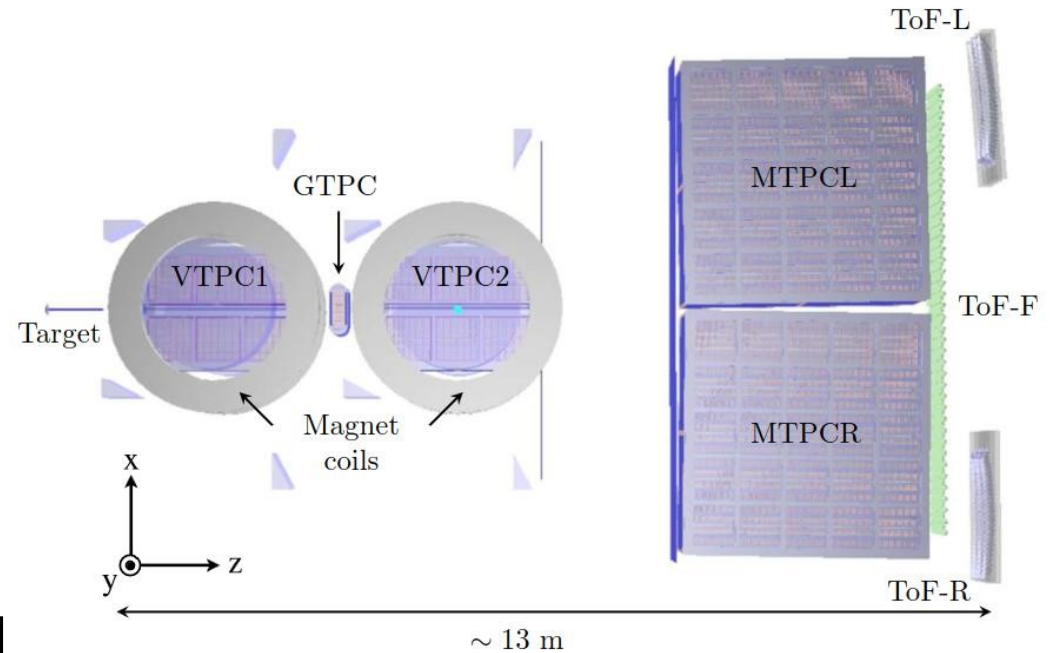


- O(10-100) GeV primary proton beams
- O(10 GeV) secondary pions and kaons
- Focused with electromagnetic horns
- *But still cover a broad E_ν range*



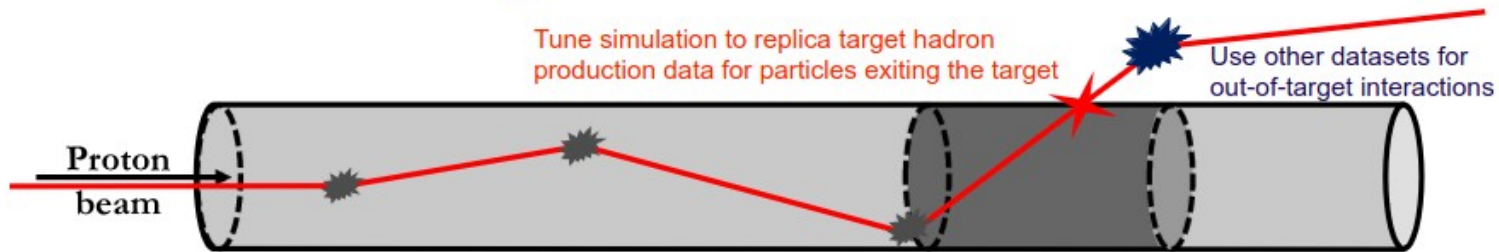
Accelerator neutrino flux uncertainty

- Dedicated hadron production measurements at fixed target beam facilities:
 - Thin target
 - Replica target
- Example: NA61/SHINE*, used for T2K → **5-10% uncertainties**



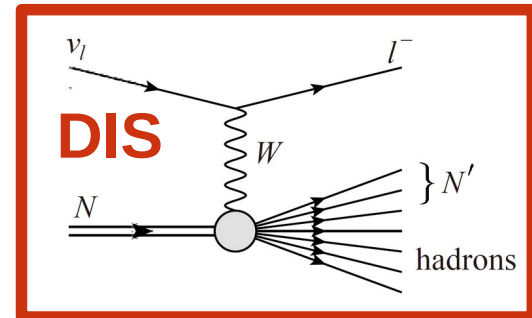
Eur. Phys. J. C76, 617 (2016)

Eur. Phys. J. C79, 100 (2019)



The low- ν method [1,2]

$$\frac{d\sigma}{dq_0} = \frac{G_F^2 M}{\pi} \int_0^1 \left(F_2 - \frac{q_0}{E_\nu} [F_2 \mp xF_3] + \frac{q_0}{2E_\nu^2} \left[\frac{Mx(1 - R_L)}{1 + R_L} F_2 \right] + \frac{q_0^2}{2E_\nu^2} \left[\frac{F_2}{1 + R_L} \mp xF_3 \right] \right) dx$$

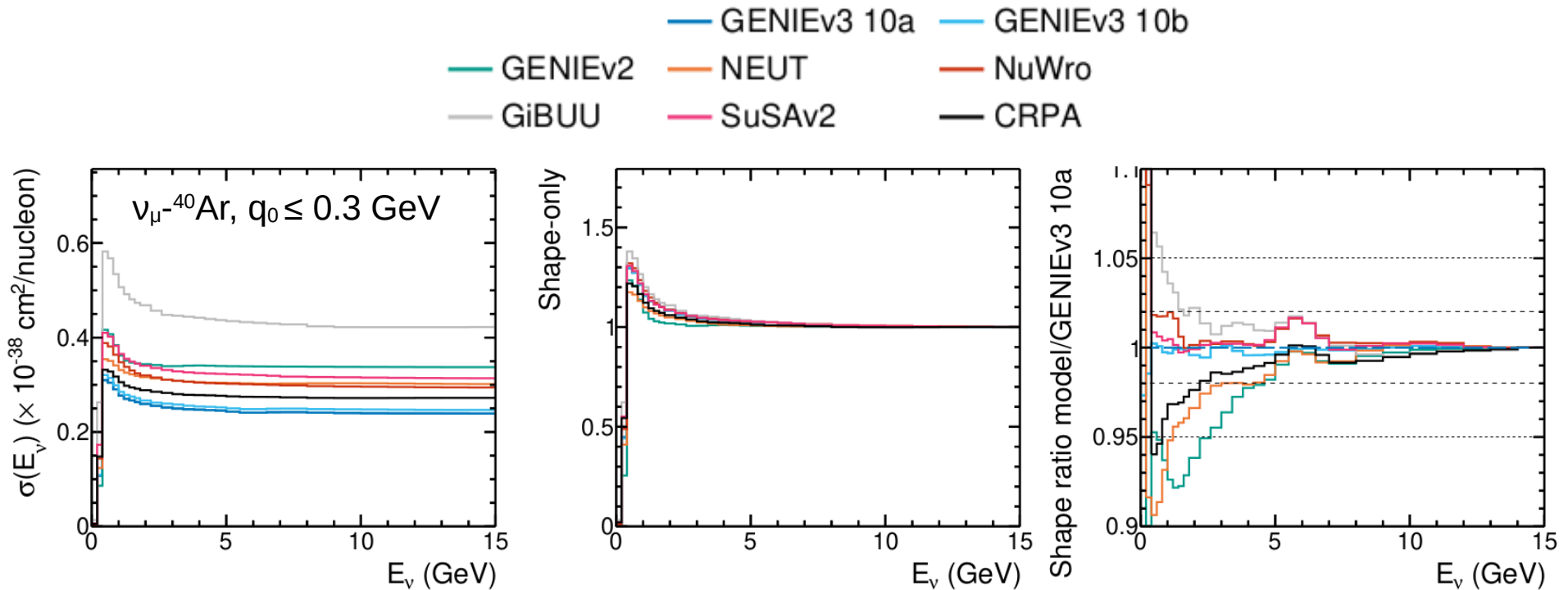


- Comes from the observation that if $q_0/E_\nu \ll 1$, the cross section is approximately constant with E_ν
- The rate as a function of E_ν gives access to the flux *shape*
- Very closely linked to the “low- y ” ($y = q_0/E_\nu$) method [2]

[1] S. R. Mishra in Workshop on Hadron Structure Functions and Parton Distributions, 84 , p84. World Scientific, 1990

[2] R. Belusevic and D. Rein Phys. Rev. D 38 (1988) 2753–2757

Is the low- q_0 cross section well described?



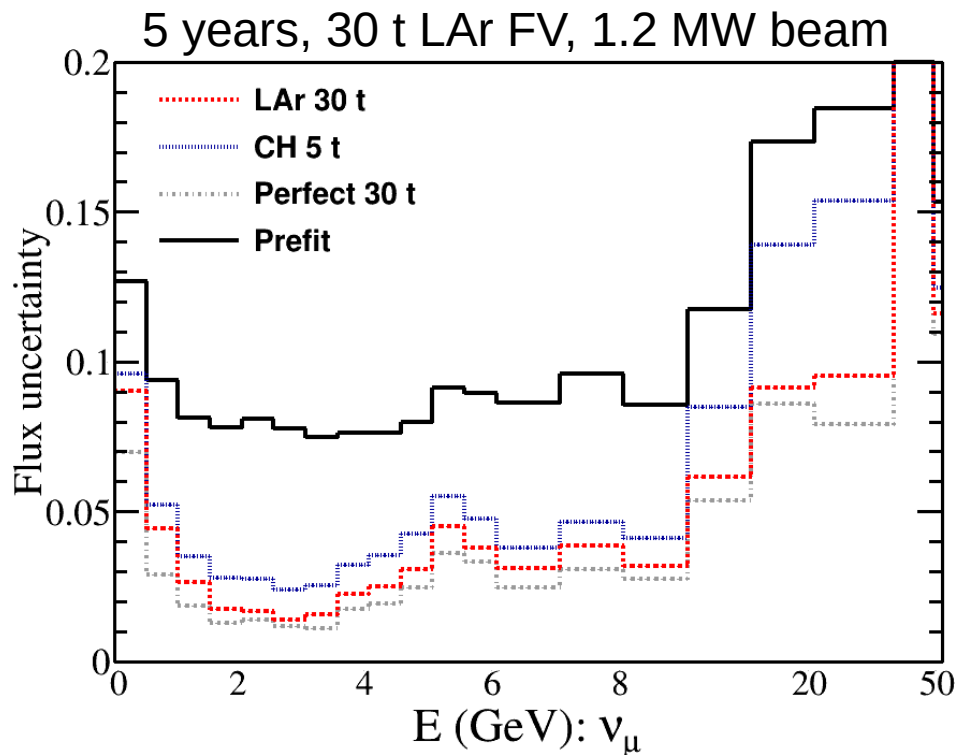
Compare a variety of new/commonly used generator models

Normalize to a fixed point at high energy – where q_0/E_{ν} corrections are smallest

Take a ratio w.r.t a reference model

Neutrino-electron elastic scattering

- The known, but small, cross section can be used to constrain the flux. ~5000 LAr ND events/year
- A powerful additional tool for achieving DUNE's sensitivities, and resolving flux \leftrightarrow cross section ambiguities



$$E_\nu = \frac{E_e}{1 - \frac{E_e(1 - \cos \theta)}{m}}$$

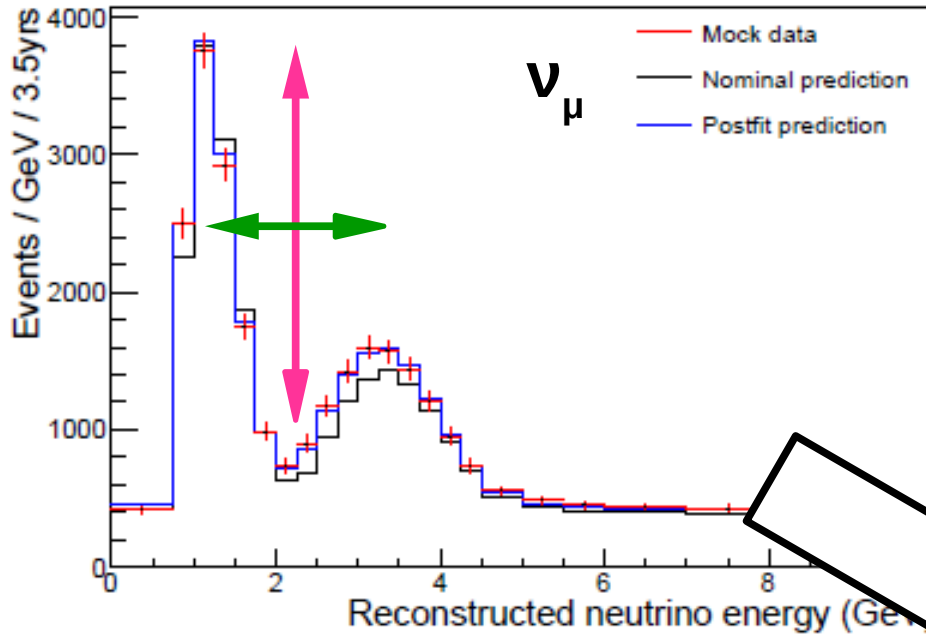
- Strong normalization constraint due to known XSEC
- Weak shape constraint due to detector smearing and beam divergence

Few-GeV cross-section models

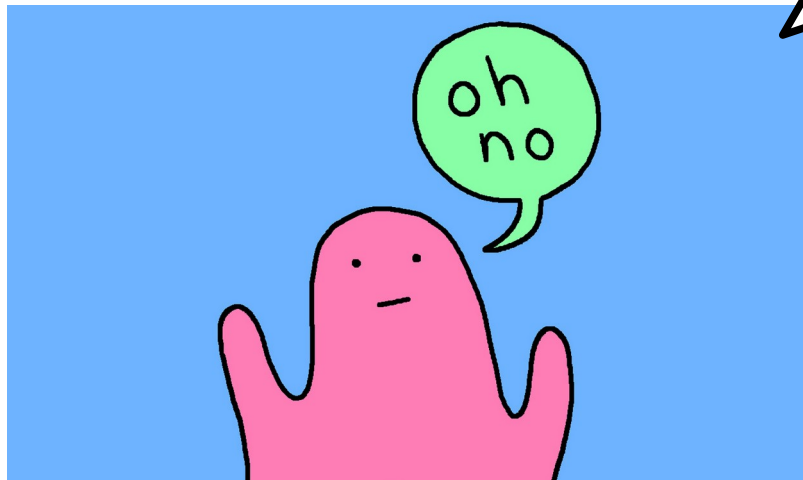
A variety of model predictions are on the market – use a variety to investigate potential for bias:

- **GENIEv2** – used in many published results
- **GENIEv3 10a** and **GENIEv3 10b** – currently used by many active experiments (10a vs 10b have different FSI models)
- **SUSAv2** and **CRPA**: state-of-the-art nuclear response modeling for pionless events (implemented in GENIE ~v3.2.0)
- **NEUT**: used by T2K
- **NuWro**: performs well w.r.t. world cross-section data
- **GiBUU**: sophisticated hadron-transport, different neutrino–nucleon model, also performs well in world data comparisons

Bias studies: cross-section mismodeling



- Shift 20% of proton energy to neutrons (for all E_ν)
- Subtle impact on spectra, but large bias in oscillation parameters



90% confidence

