

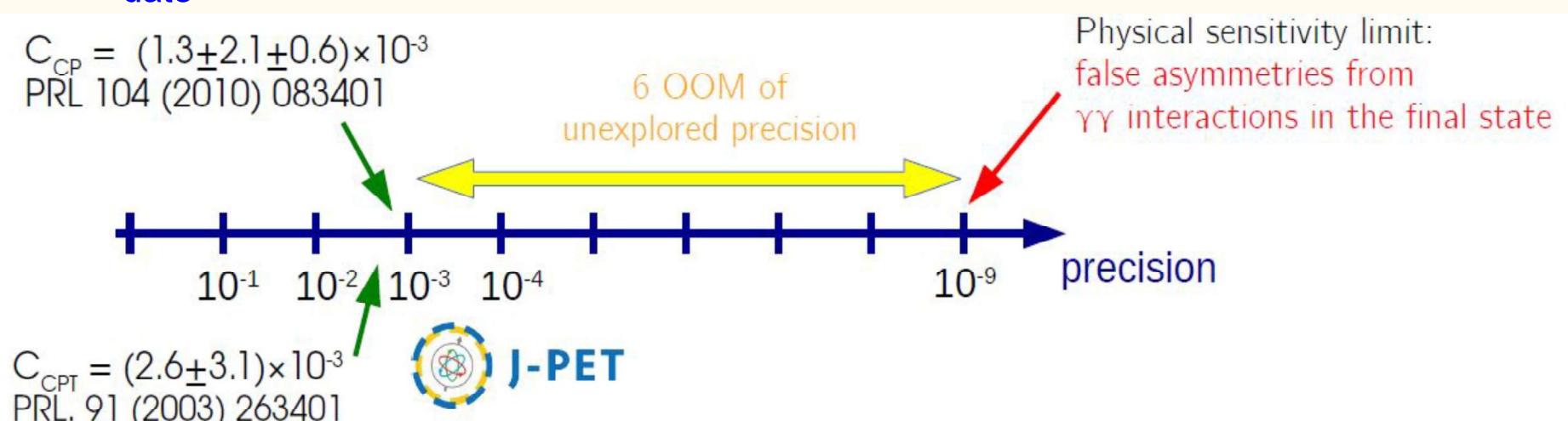
# Discrete Symmetries Investigation in Positronium decays with J-PET facility

Magdalena Skurzok  
on behalf of the **J-PET**  
Collaboration



## Motivation: discrete symmetry tests with o-Ps decays

- ❖ Discrete symmetries are scarcely tested with leptonic systems
  - Neutrino oscillations: Dirac phase,  $\delta\text{CP} \sim 3\sigma$  level [T2K, *Nature* 580 (2020) 339]
  - Electron EDM  $< 4.1 \times 10^{-30}$  [Science 381 (2023) adg4084]
- ❖ Violation of CP and T symmetries have been observed only for systems including quarks, **never discovered in any processes involving purely leptonic matter**
- ❖ So far performed experiments with Ps atoms excluded violation of discrete symmetries as CP, T or CPT only at the level of about 0.3% - many orders of magnitude less precise than the accuracies achieved in the quark sector  
**Ps is the only system consisting of charged leptons used for tests of CP and CPT to date**



- symmetries tests can be made with a very high precision limited, only by the effects due to the weak interaction:  $10^{-14}$  and photon-photon interaction:  $10^{-9}$ . (Standard Model Calculations)  
[Phys. Rev. A 37, 3189 (1988), Z. Phys. C 41, 143 (1988), M. S. Sozzi "Discrete Symmetries and CP violation"]

# Motivation: discrete symmetry tests with o-Ps decays

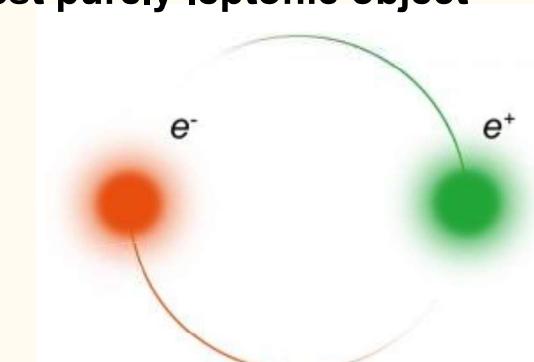
## ➤ POSITRONIUM - the lightest purely leptonic object

bound by a central potential



is eigenstate of the parity operator P

$$P|Ps\rangle = (-1)^L|Ps\rangle$$



eigenstate of the CP operator

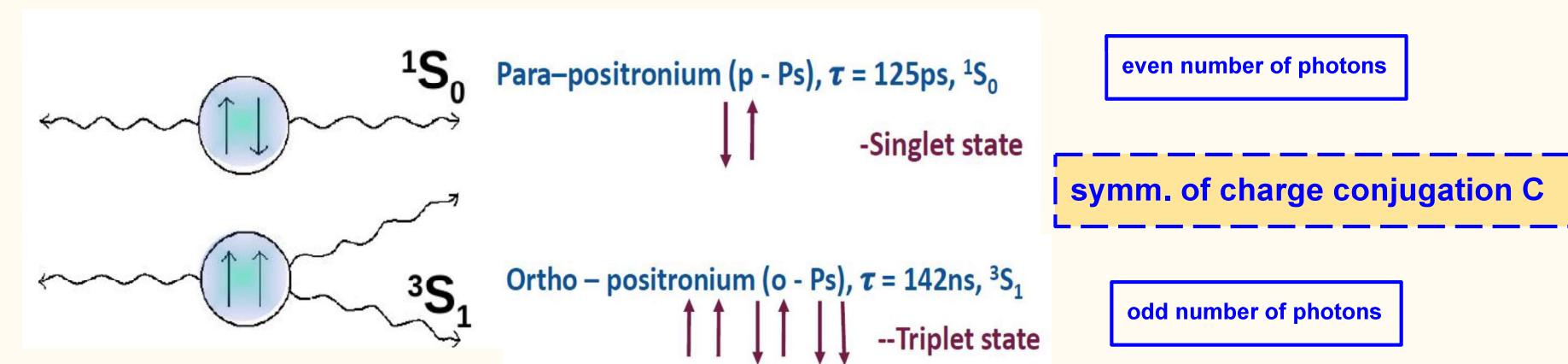
symmetric under the exchange of particles - anti-particles



is eigenstate of the charge conjugation operator C



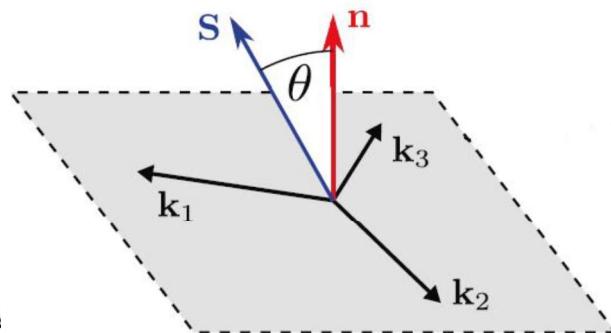
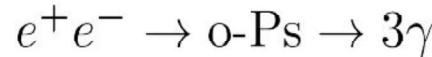
$$C|Ps\rangle = (-1)^{L+S}|Ps\rangle$$



Ps state	$\tau$ [ns]	L	S	J	$J_z$	P	C	CP
$^1S_0$ (para-Ps)	0.125	0	0	0	0	-	+	-
$^3S_1$ (ortho-Ps)	142	0	1	1	-1,0,1	-	-	+

# Testing discrete symmetries with angular correlations in o-Ps $\rightarrow$ 3 $\gamma$ decays

Measurement the expectation value of the symmetry odd-operators



$$\langle \hat{O} \rangle \stackrel{?}{=} 0 \quad \text{for an odd operator}$$

$$\Leftrightarrow \mathcal{CPT}(\hat{O}) = -1$$

$$\Leftrightarrow \mathcal{T}(\hat{O}) = -1$$

$$|\vec{k}_1| > |\vec{k}_2| > |\vec{k}_3|$$

**Required:**

- the o-Ps spin determination
- of o-Ps $\rightarrow$ 3 $\gamma$  decays selection  
(determination of photons momenta)
- determination of annihilation  $\gamma$  polarization



$$O_{CPT} = \vec{S} \cdot (\vec{k}_1 \times \vec{k}_2) / |\vec{k}_1 \times \vec{k}_2| = \cos\theta$$

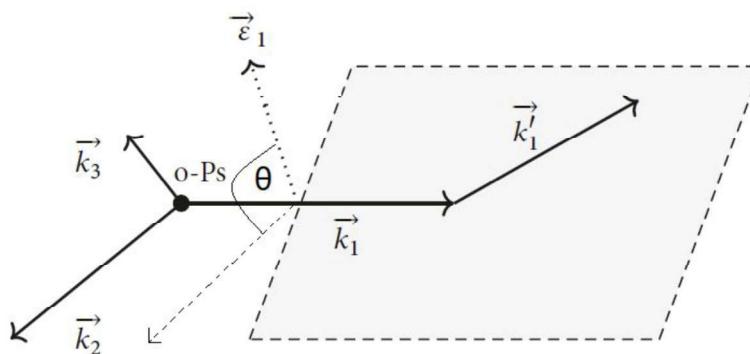
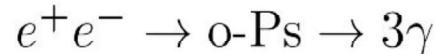
$$O_{CP} = \vec{k}_1 \cdot \vec{\epsilon}_2 / |\vec{k}_1| |\vec{\epsilon}_2| = \cos\theta$$

Operator	C	P	T	CP	CPT
$\vec{S} \cdot \vec{k}_1$	+	-	+	-	-
$\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2)$	+	+	-	+	-
$(\vec{S} \cdot \vec{k}_1)(\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2))$	+	-	-	-	+
$\vec{k}_1 \cdot \vec{\epsilon}_2$	+	-	-	-	+
$\vec{S} \cdot \vec{\epsilon}_1$	+	+	-	+	-
$\vec{S} \cdot (\vec{k}_2 \times \vec{\epsilon}_1)$	+	-	+	-	-

[P. Moskal et al., Acta Phys. Polon. B47 (2016) 509]

# Testing discrete symmetries with angular correlations in o-Ps $\rightarrow$ 3 $\gamma$ decays

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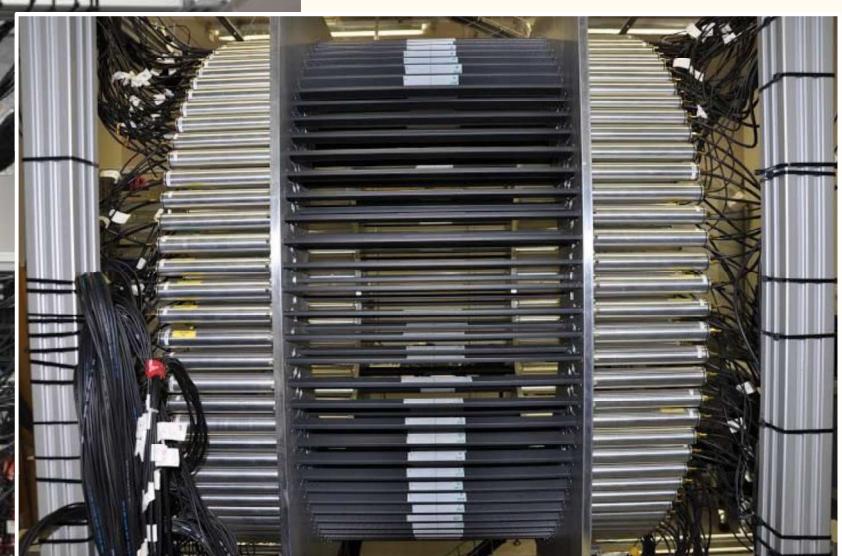
$$O_{CPT} = \vec{S} \cdot (\vec{k}_1 \times \vec{k}_2) / |\vec{k}_1 \times \vec{k}_2| = \cos \theta$$

$$O_{CP} = \vec{k}_1 \cdot \vec{\epsilon}_2 / |\vec{k}_1| |\vec{\epsilon}_2| = \cos \theta$$

Operator	C	P	T	CP	CPT
$\vec{S} \cdot \vec{k}_1$	+	-	+	-	-
$\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2)$	+	+	-	+	-
$(\vec{S} \cdot \vec{k}_1)(\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2))$	+	-	-	-	+
$\vec{k}_1 \cdot \vec{\epsilon}_2$	+	-	-	-	+
$\vec{S} \cdot \vec{\epsilon}_1$	+	+	-	+	-
$\vec{S} \cdot (\vec{k}_2 \times \vec{\epsilon}_1)$	+	-	+	-	-

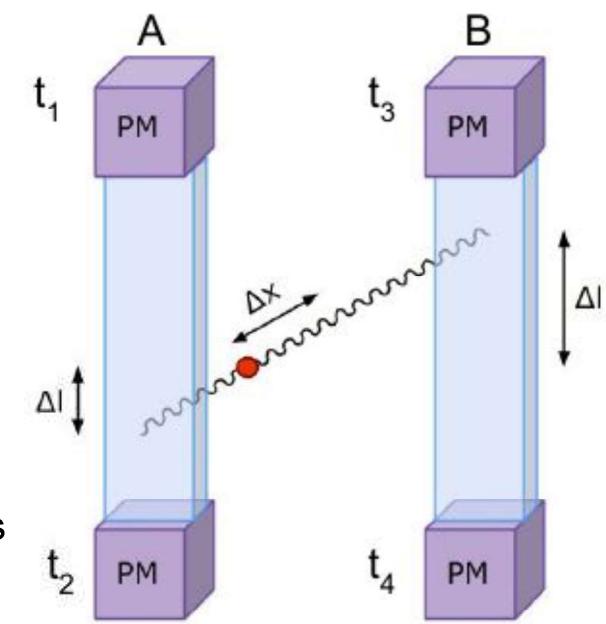
[P. Moskal et al., Acta Phys. Polon. B47 (2016) 509]

# J-PET detector at Jagiellonian University in Kraków, Poland

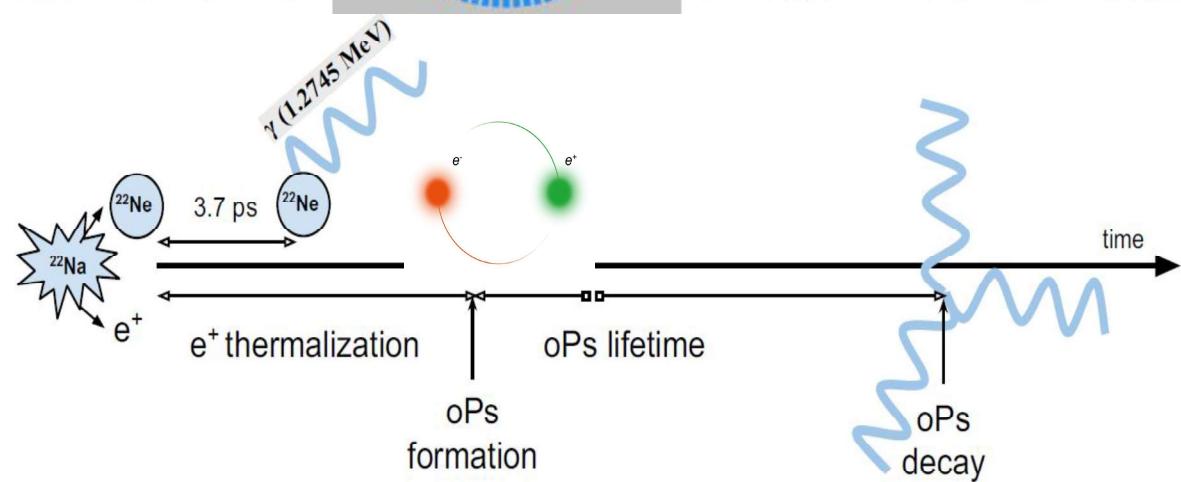
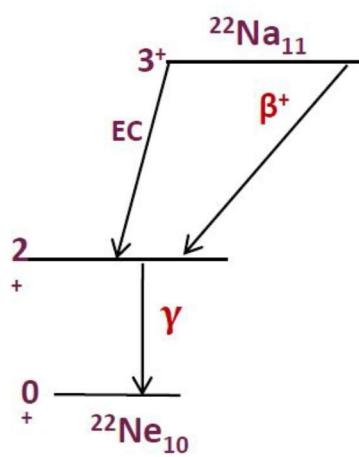
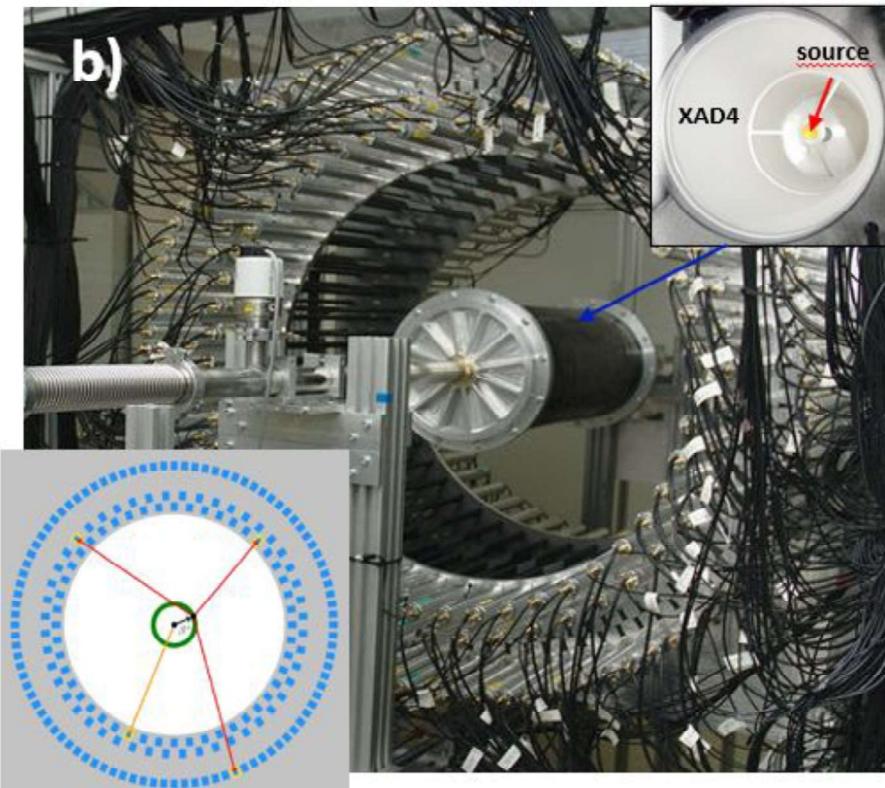
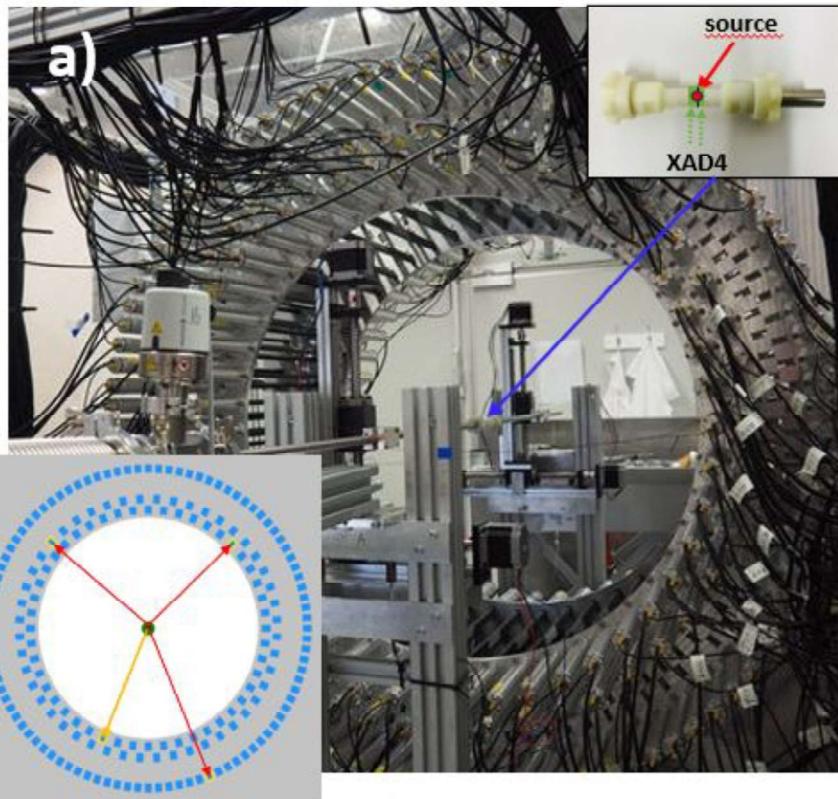


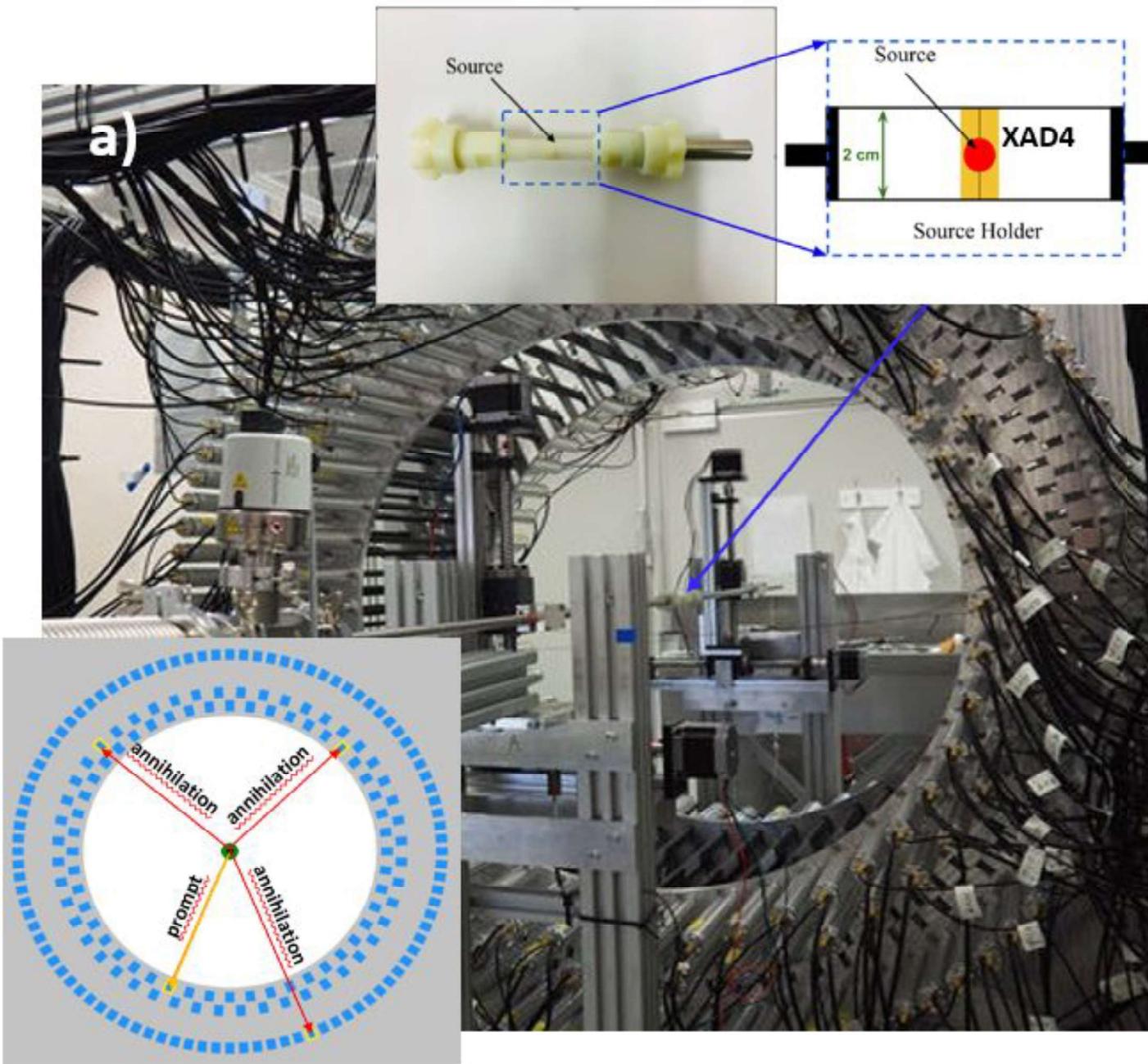
*Exploring quantum entanglement and decay rates  
in Positronium atoms in the framework of J-PET  
detector -> Sushil talk on Tuesday, 1.10*

- 3 layers, 192 EJ-230 scintillators:  $7 \times 19 \times 500 \text{ mm}^3$
- 85 cm radius, 384 R9800 photomultipliers, 1536 channels
- plastic scintillators - small light attenuation
- multithreshold digital electronics and the novel trigger-less DAQ
- interaction time resolution  $\sim 250\text{ps}$ , angular resolution  $\sim 1\text{deg}$

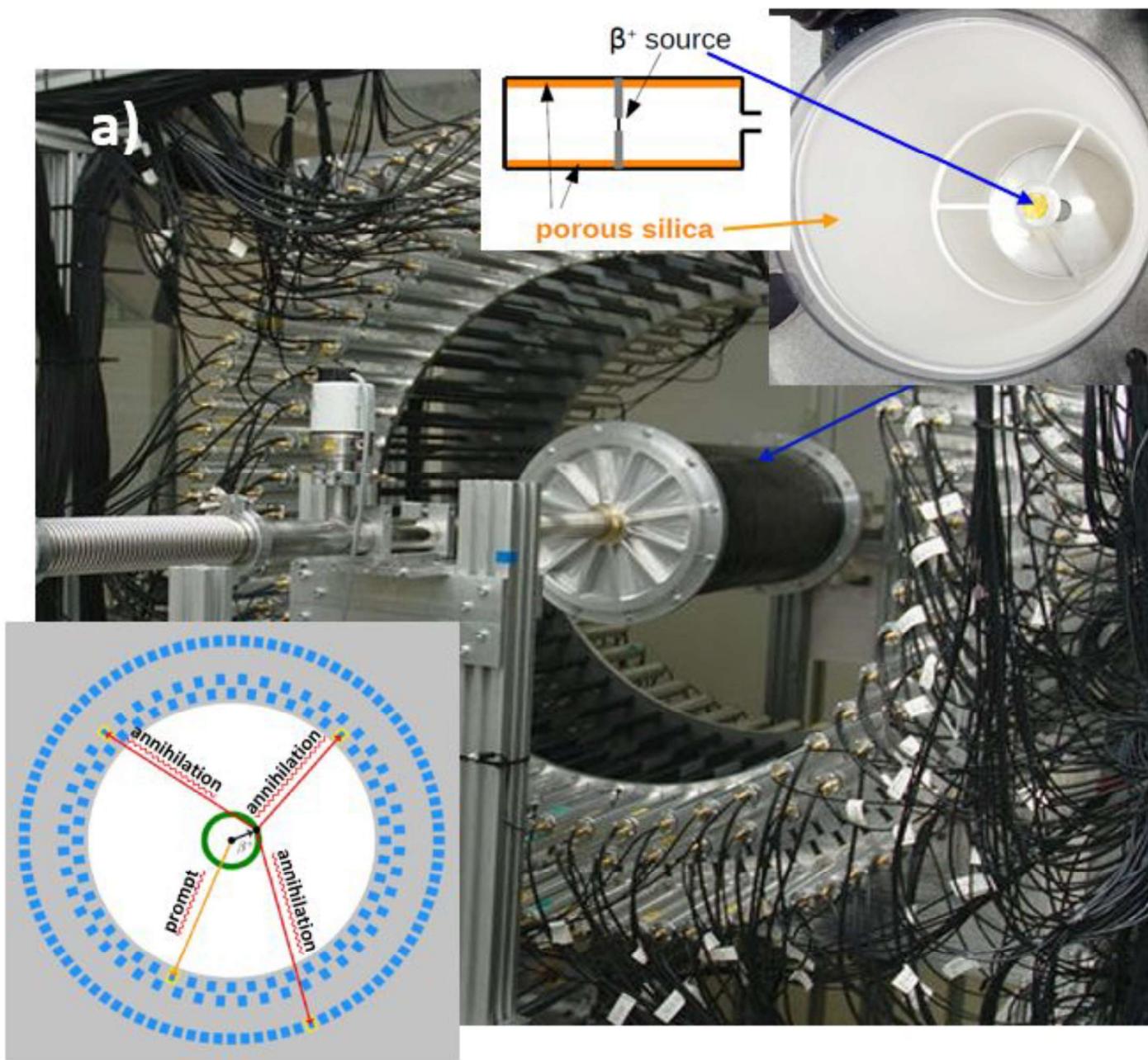


## $\text{o-Ps}$ production in J-PET with an annihilation chamber



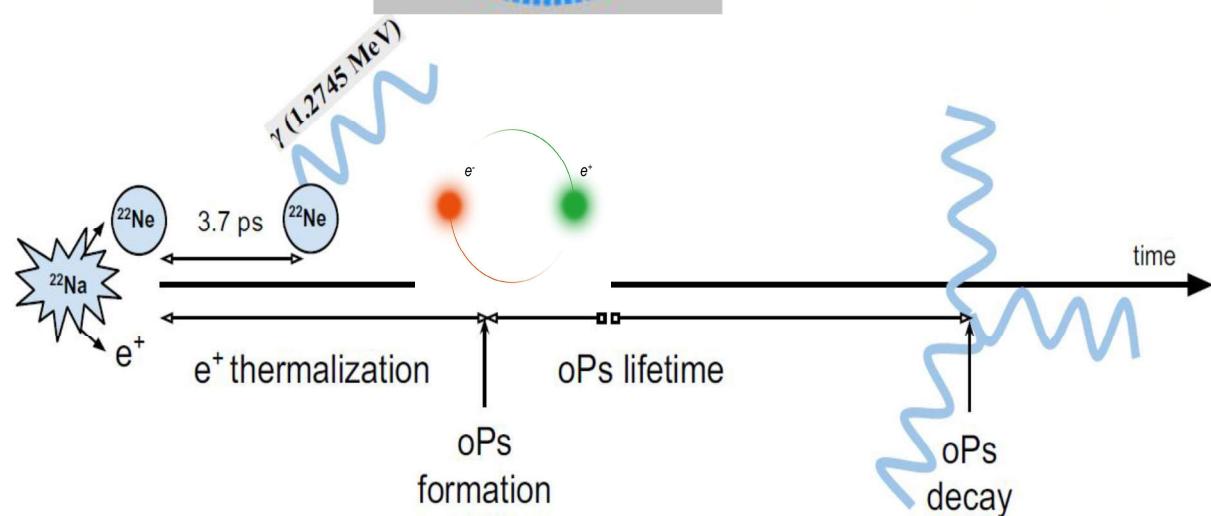
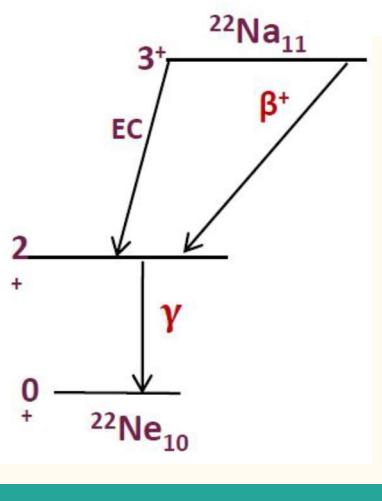
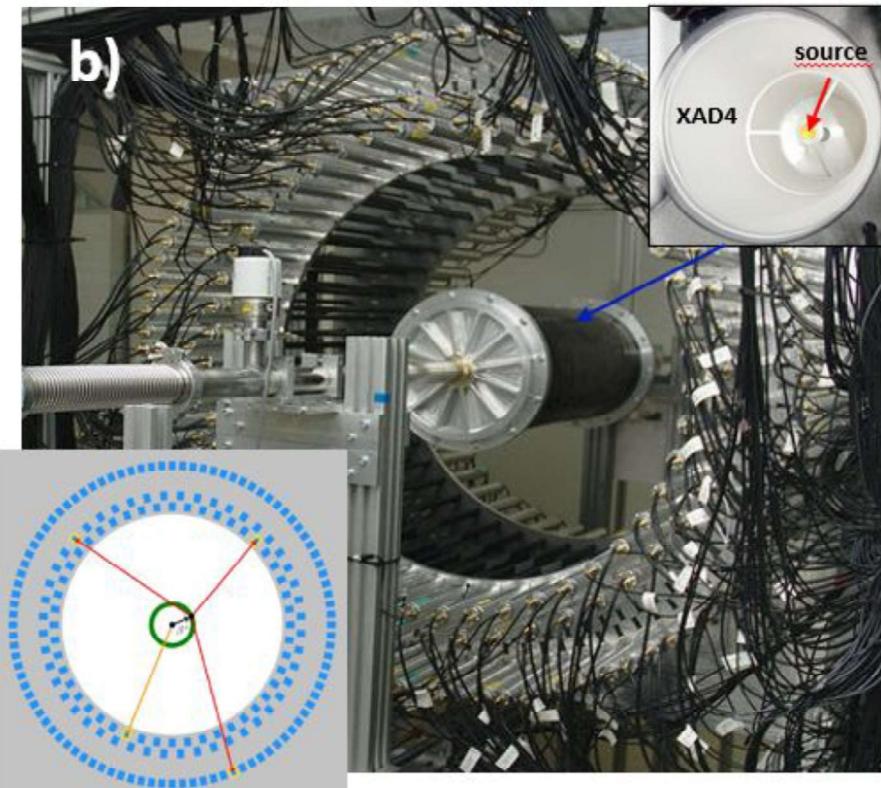
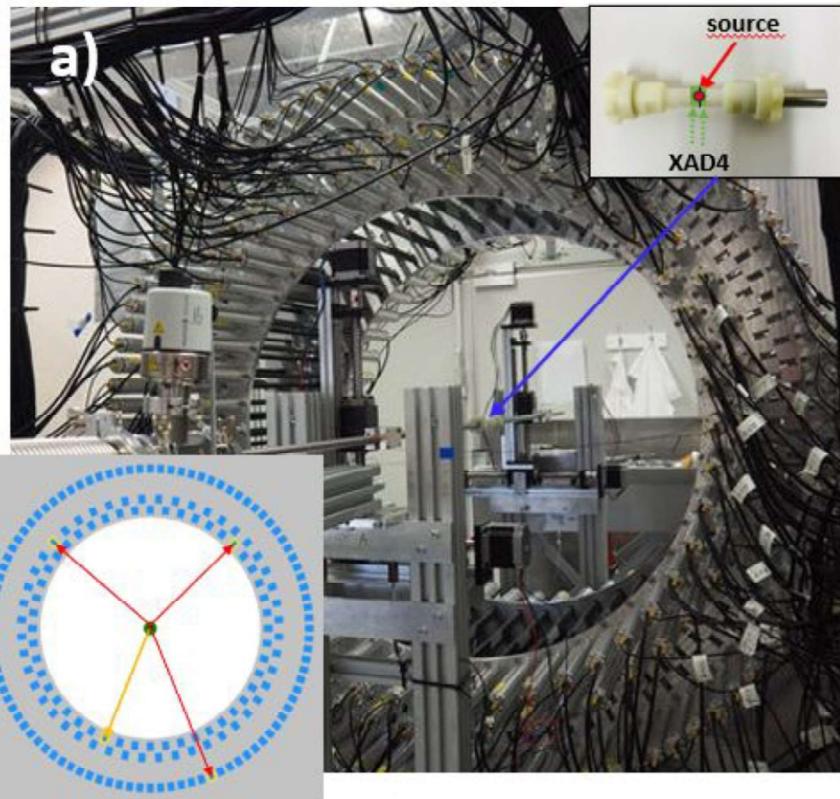


- Small annihilation chamber,  $R = 7\text{cm}$  with internal "bucket" including a positron source surrounded with a layer of porous material XAD4
- 1 or 5 MBq  $\beta^+$   $^{22}\text{Na}$  source placed in the center

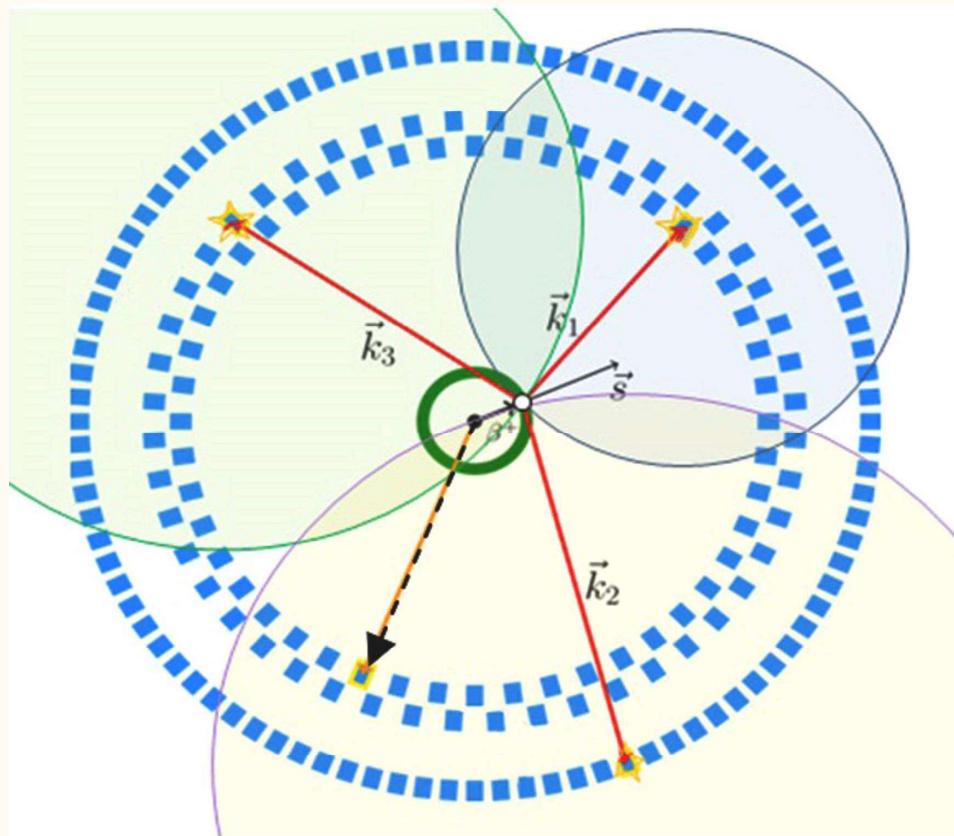


- Extensive-size chamber,  $R=12$  cm
- Walls coated with porous silica material (o-Ps target)
- 10 MBq  $\beta^+$   $^{22}\text{Na}$  source placed in the center

## $\text{o-Ps}$ production in J-PET with an annihilation chamber



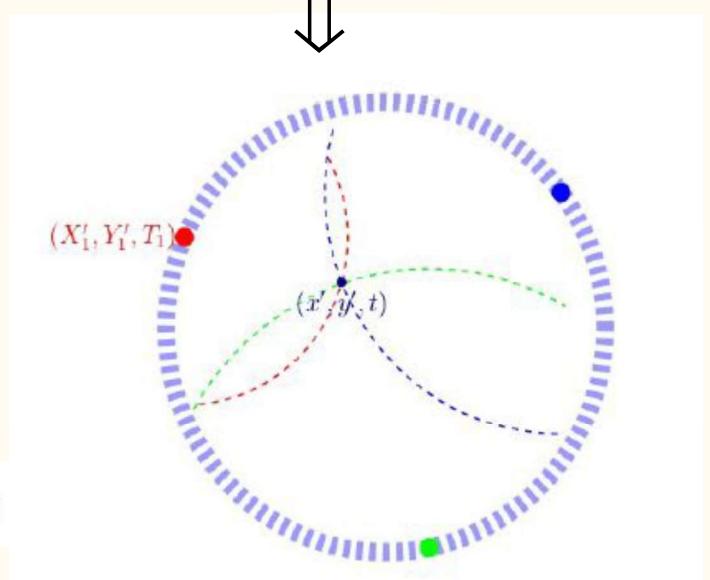
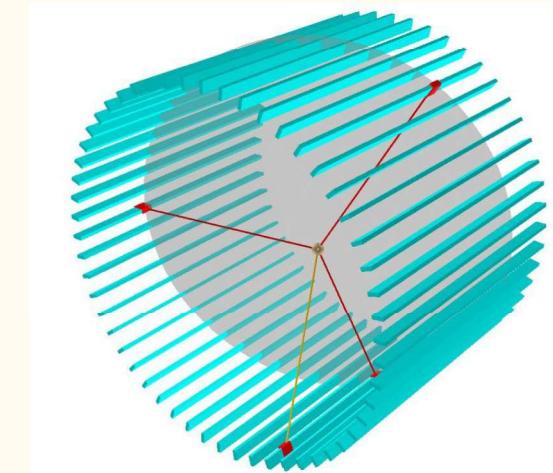
## $\text{o-Ps} \rightarrow 3\gamma$ decays reconstruction in J-PET



The decay point ( $x', y'$ ) in the decay plane and time  $t$  is an intersection of 3 circles, each corresponding to a possible origin points of the incident  $\gamma$

$$(T_i - t)^2 c^2 = (X'_i - x')^2 + (Y'_i - y')^2, \quad i = 1, 2, 3$$

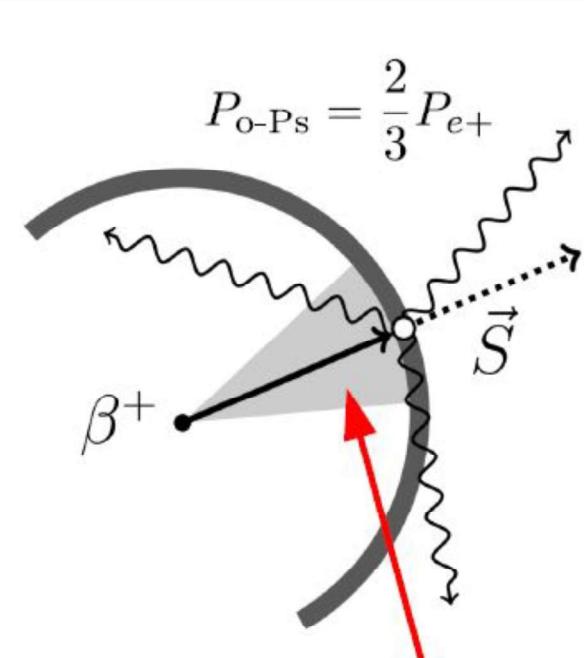
**Trilateration-based** reconstruction to determine the o-Ps annihilation point



[A. Gajos et al., NIM A 819 (2016), 54-59]

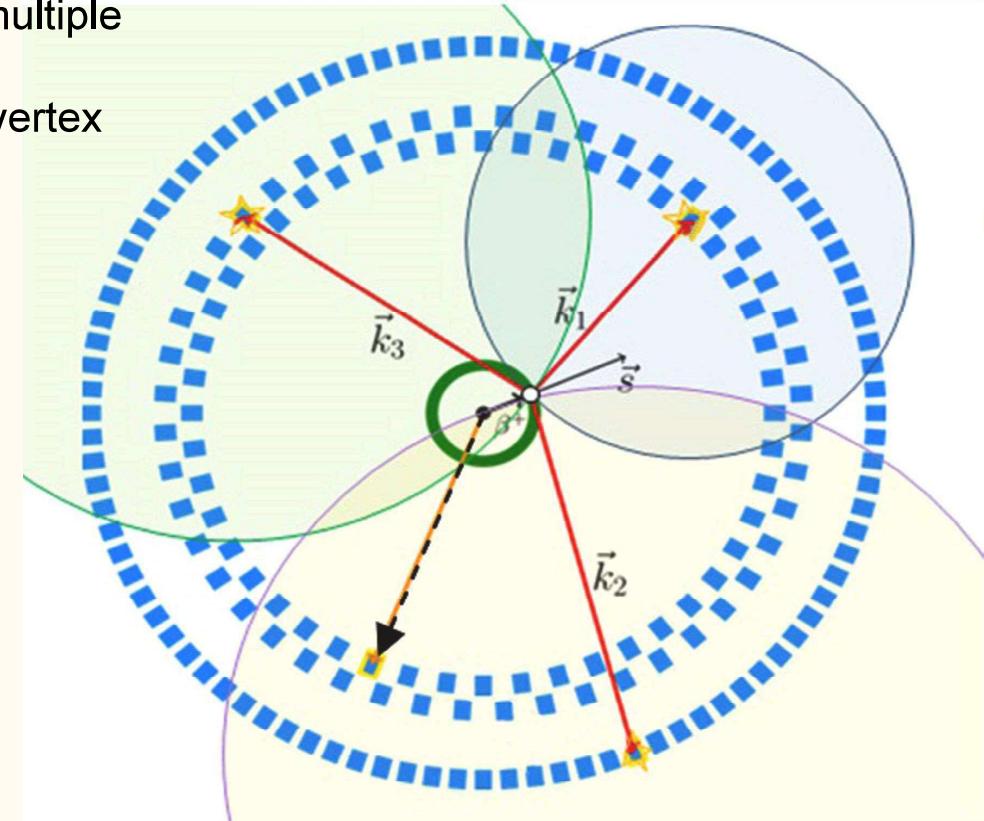
## o-Ps spin determination in J-PET

- \*without magnetic field or polarised positronium source
- \* $e^+$  spin estimated event-by-event recording multiple geometrical configurations
- \* effective polarization depends on o-Ps $\rightarrow 3\gamma$  vertex resolution



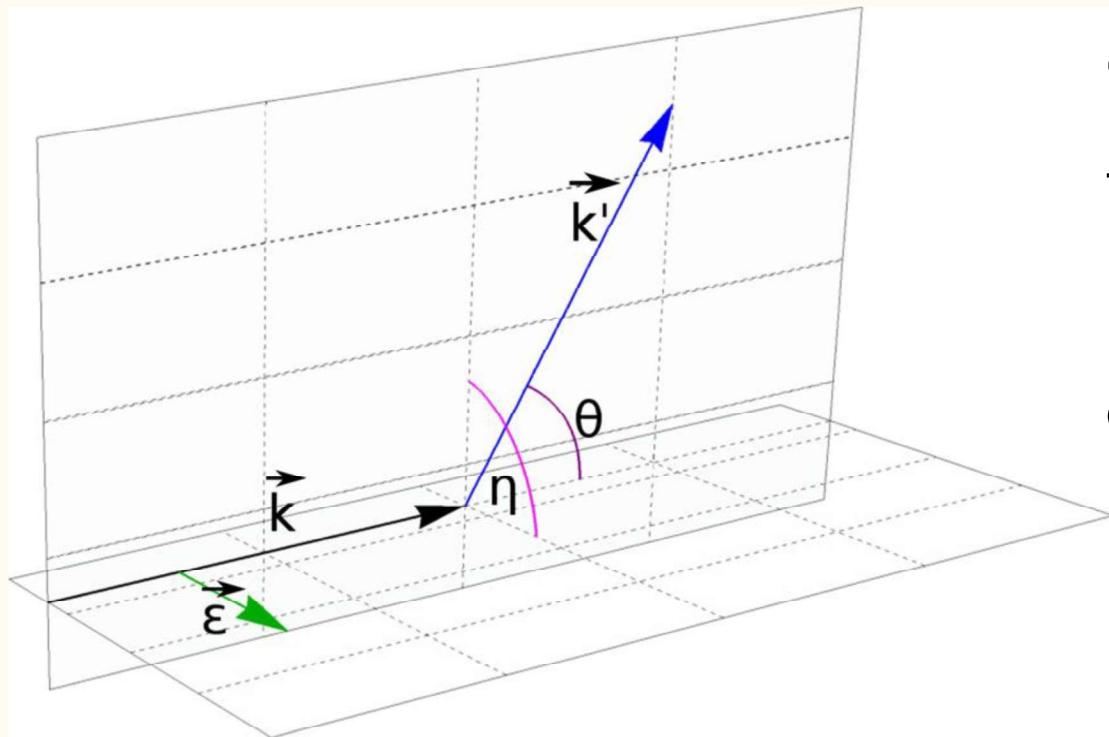
$$P_{e+} \approx \frac{v}{c} \cdot \frac{1}{2} (\cos \alpha + 1)$$

P. Moskal et al., Acta Phys. Polon. B 47 (2016) 509  
 M. Mohammed, et al., Acta Phys. Pol. A 132, 1486 (2017)]



- ★ parity violation in the beta decay (weak interaction)  
 $\Rightarrow e^+$  emitted from  $^{22}\text{Na}$  source are **longitudinally spin-polarized**
- ★ o-Ps polarization is by a factor of 2/3 smaller with respect to the positron polarization since the spin of electrons in the target is not polarized

## determination of annihilation $\gamma$ polarization in J-PET



Compton scattering is at most likely in the plane perpendicular to the electric vector of the photon

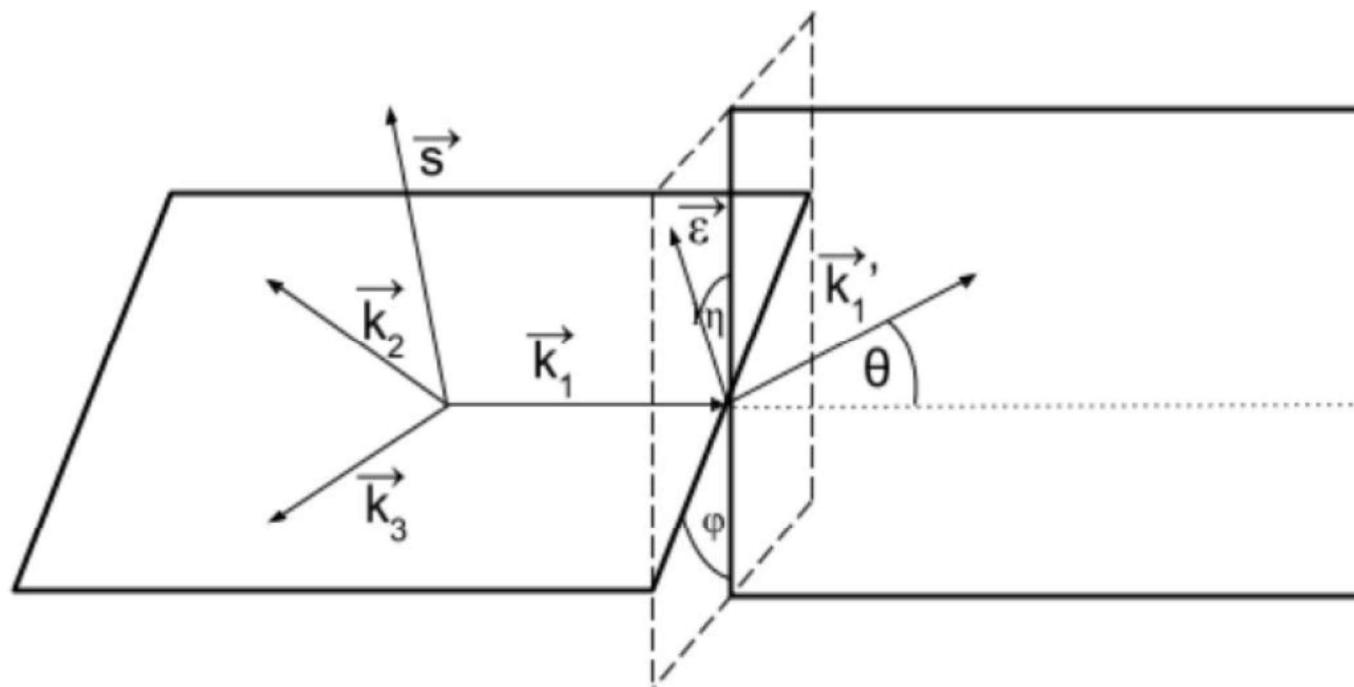


direction of its linear polarization

$$\vec{\epsilon} = \vec{k} \times \vec{k}'$$

independently of the value of theta the **probability of the scattering has its maximum value when the scattering plane is perpendicular to the direction of the electric vector of the primary photon**

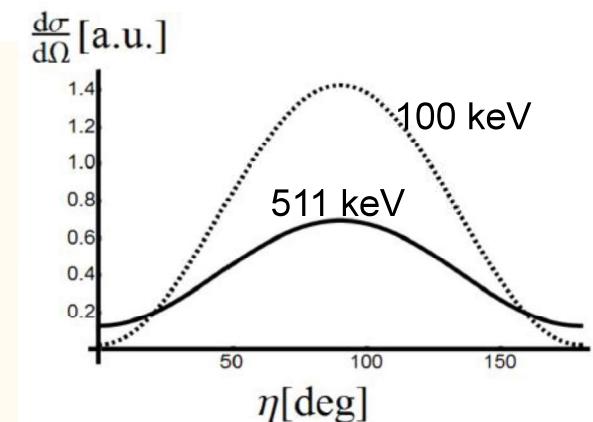
## determination of annihilation $\gamma$ polarization in J-PET



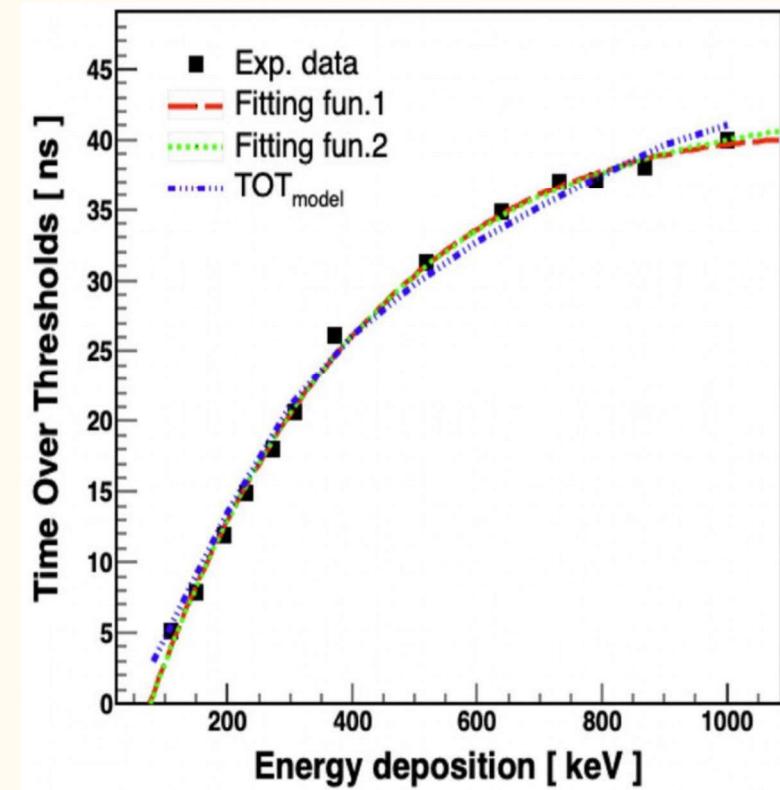
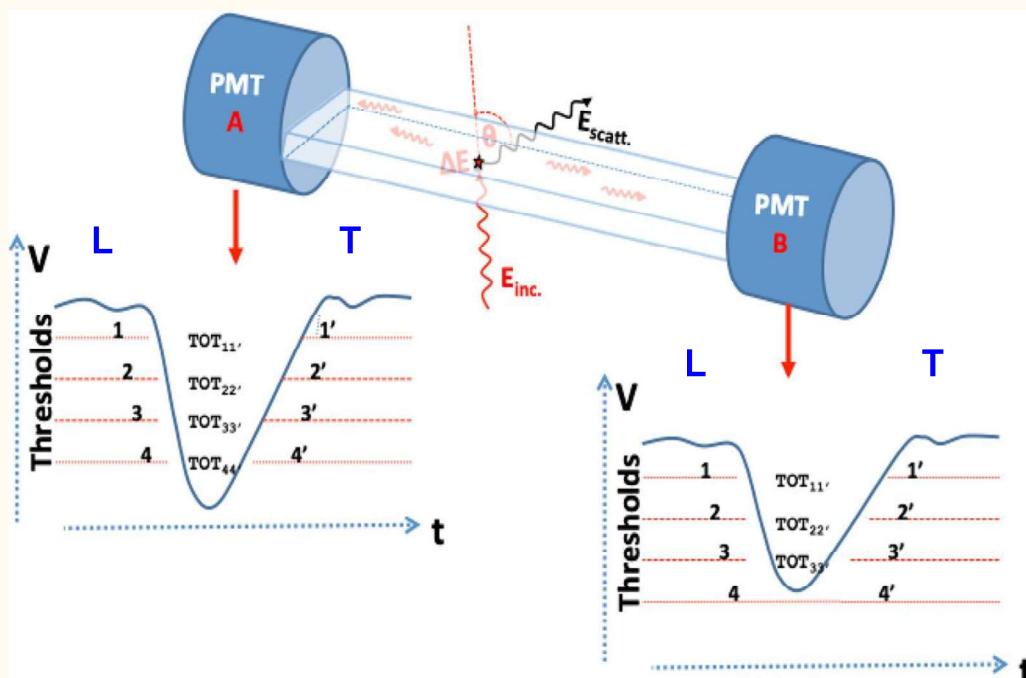
$$\vec{\epsilon} = \vec{k} \times \vec{k}'$$

$$\frac{d\sigma(E, \theta, \eta)}{d\Omega} = \frac{r_0^2}{2} \left( \frac{E'}{E} \right)^2 \left( \frac{E}{E'} + \frac{E'}{E} - 2 \sin^2 \theta \cos^2 \eta \right)$$

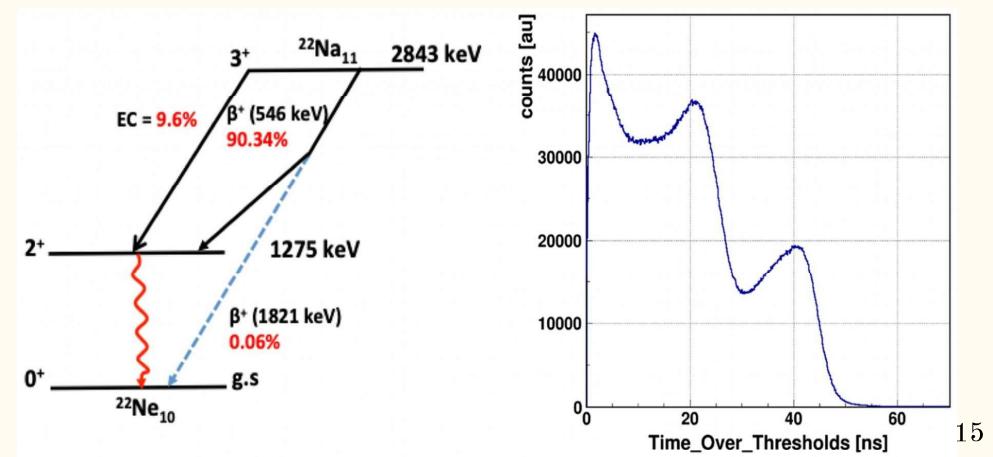
$$E'(E, \theta) = \frac{E}{1 + \frac{E}{m_e c^2} (1 - \cos \theta)}$$



# TOT as a measure of energy

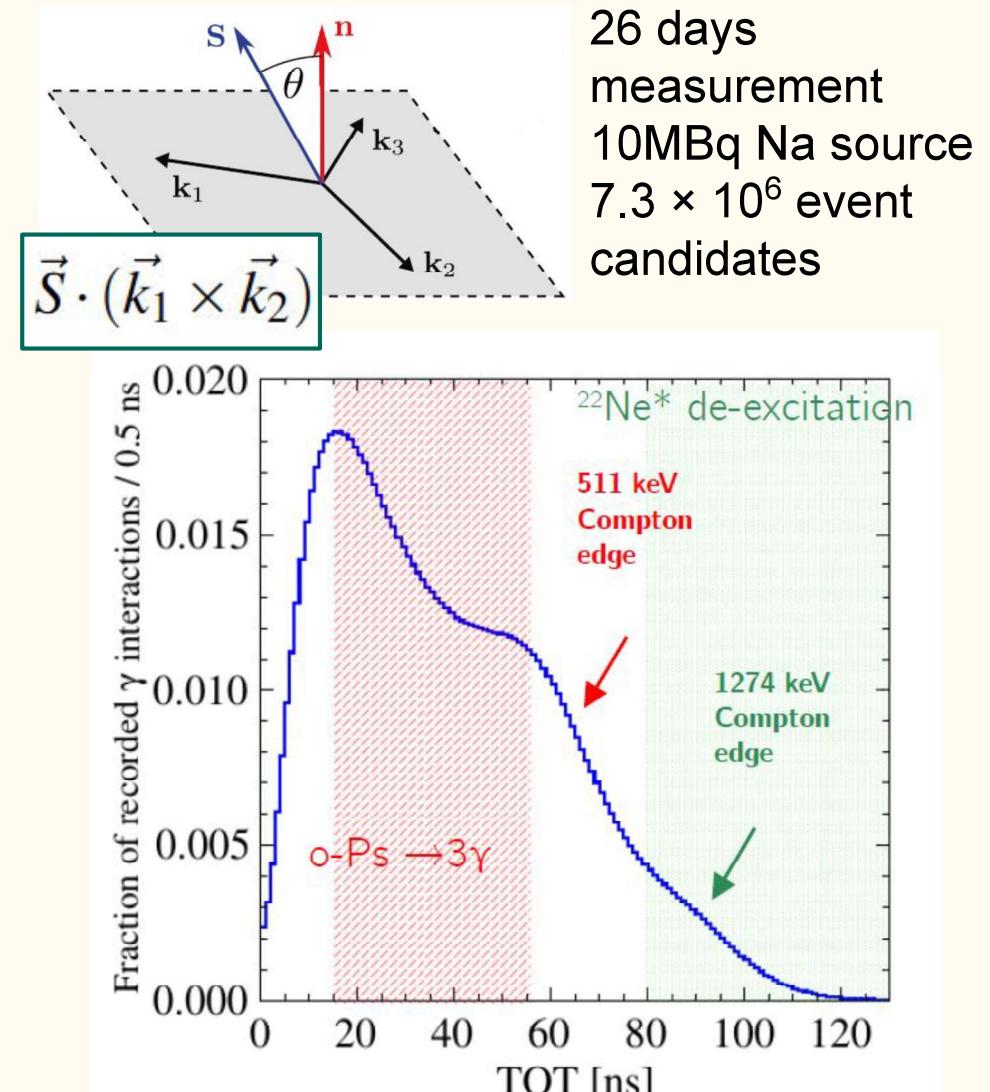
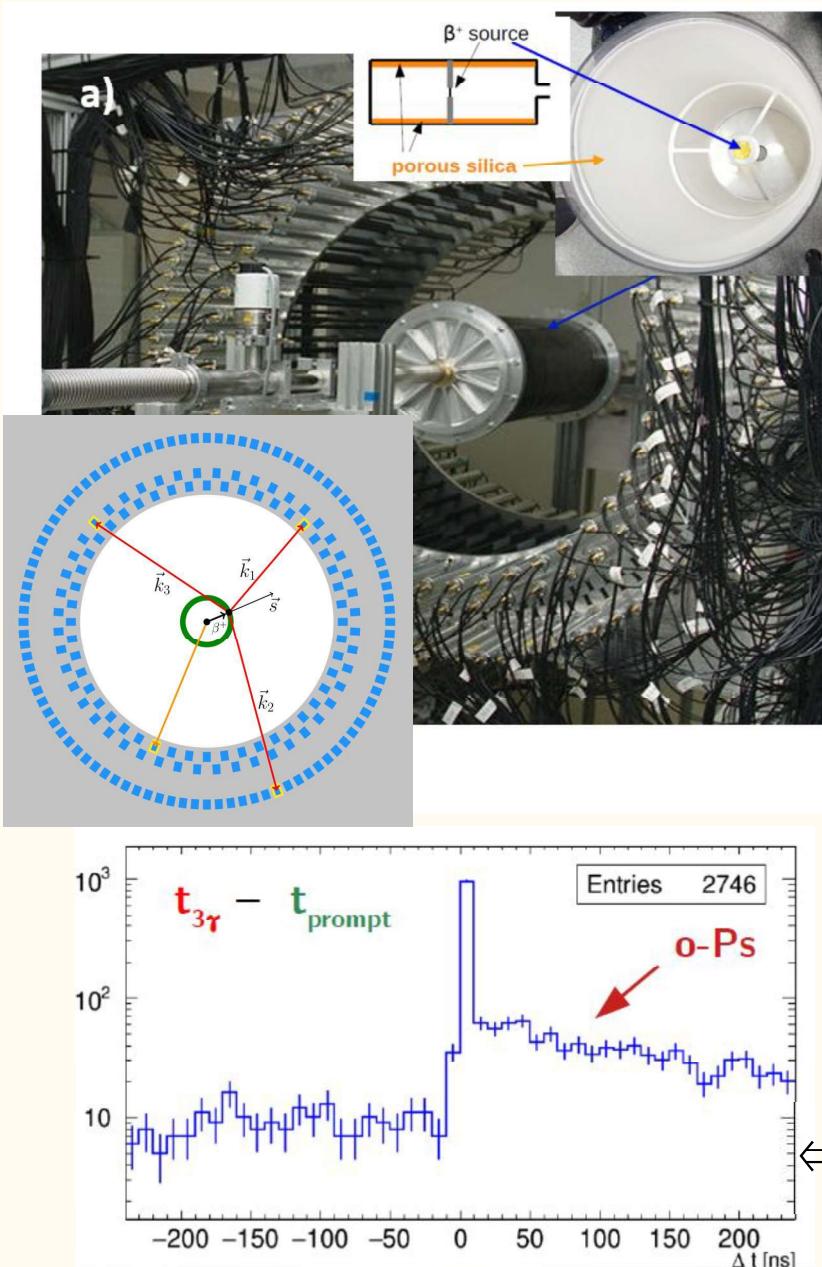


Time Over Threshold (TOT) of PMT signals from a scintillator strip corresponds to  $\gamma$  deposited energy



[S. Sharma, et al., EJNMMI Phys. 7, 39 (2020)  
 S. Sharma, et al., EJNMMI Phys. 10(28) (2023)]

# Towards $\langle O_{CPT} \rangle$ determination: Identification of o-Ps $\rightarrow$ 3 $\gamma$ events

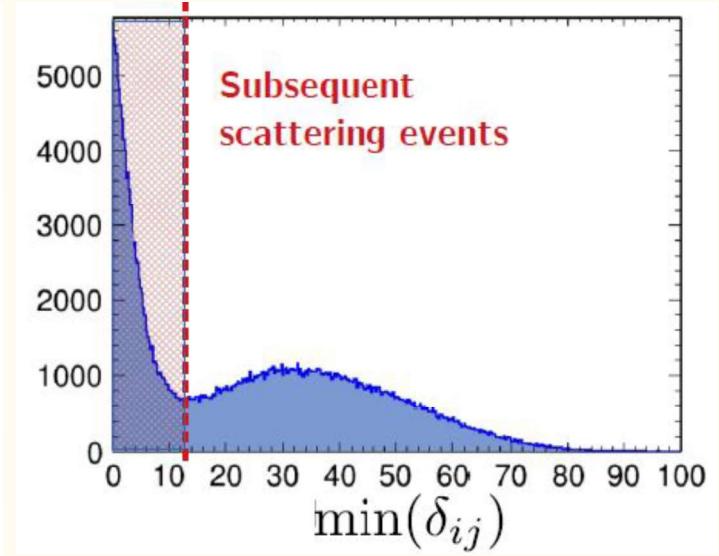
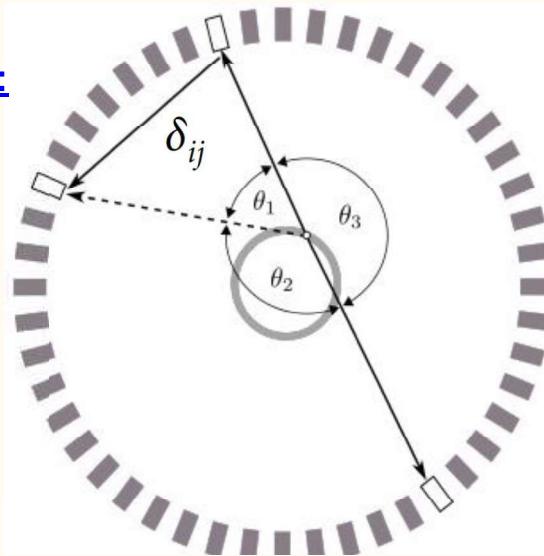


# Towards $\langle O_{CPT} \rangle$ determination: Background subtraction

## Secondary Compton scatterings:

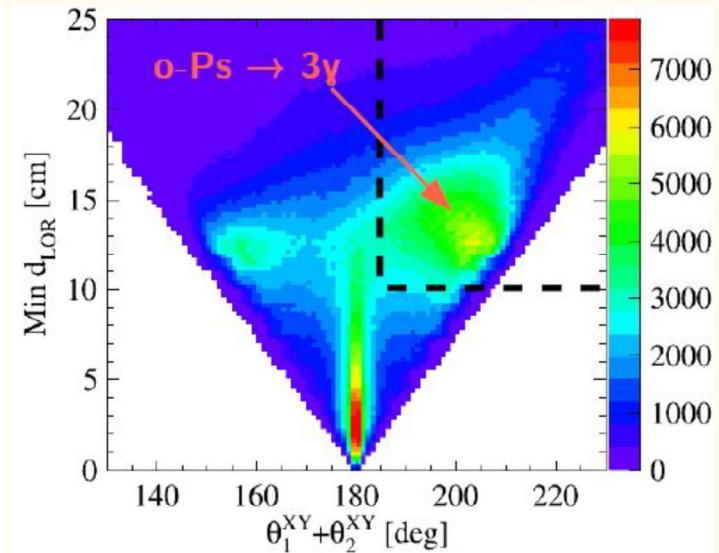
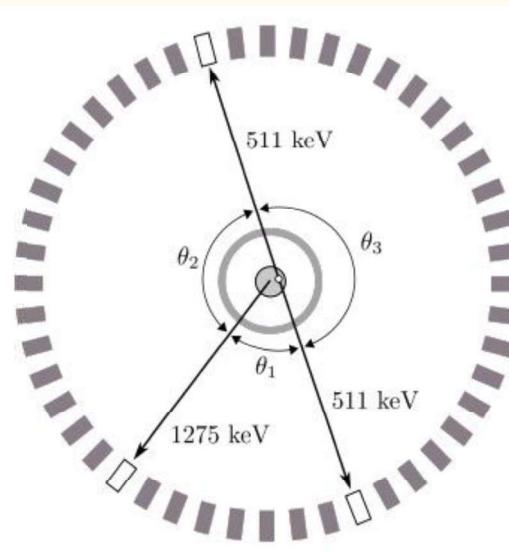
$$* \delta_{ij} = |d_{ij} - c\Delta t_{ij}|$$

computed for each pair of annihilation photon candidates i and j ( $i,j=1,2,3$ )



## 2γ from the β+ source setup coincident with de-excitation photon:

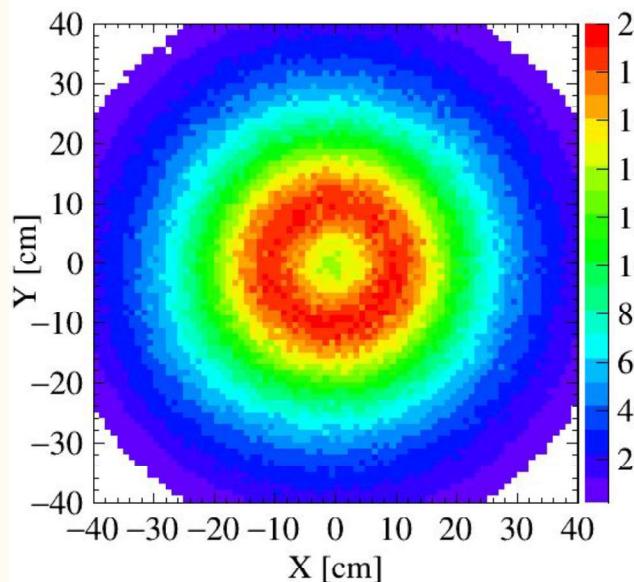
- \* distance between the  $\beta^+$  source location and the closest hypothetical  $2\gamma$  annihilation point on a LOR between two recorded photon interactions
- \* the sum of the two smallest angles between azimuthal coordinates of the recorded  $\gamma$  interaction points



## Towards $\langle O_{CPT} \rangle$ : determination of the CPT - asymmetric observable

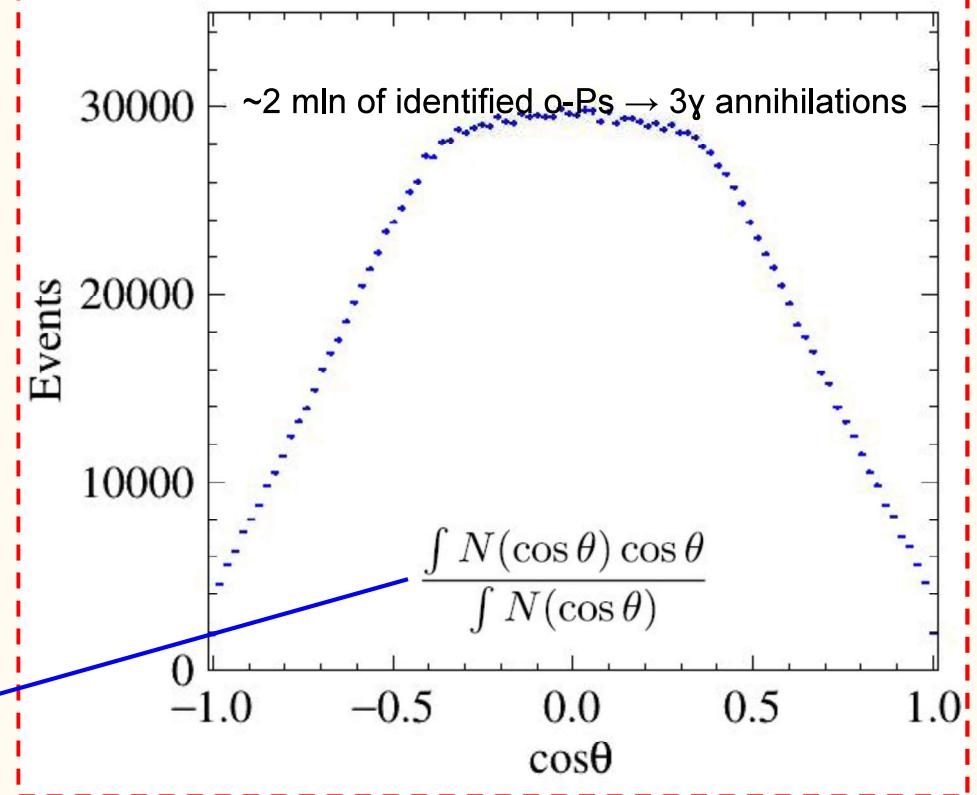
$$O_{CPT} = \vec{S} \cdot (\vec{k}_1 \times \vec{k}_2) / |\vec{k}_1 \times \vec{k}_2| = \cos\theta$$

3γ image of the o-Ps production chamber in the transverse view of the detector (the first!)



$$\langle O_{CPT} \rangle = 0.00025 \pm 0.00036$$

the angle between the direction of initial spin of the o-Ps atom and the normal to the decay plane



P. Moskal, et al., Nature Commun. 12, 5658 (2021)

$$C_{CPT} = \langle O_{CPT} \rangle / P = 0.00067 \pm 0.00095$$

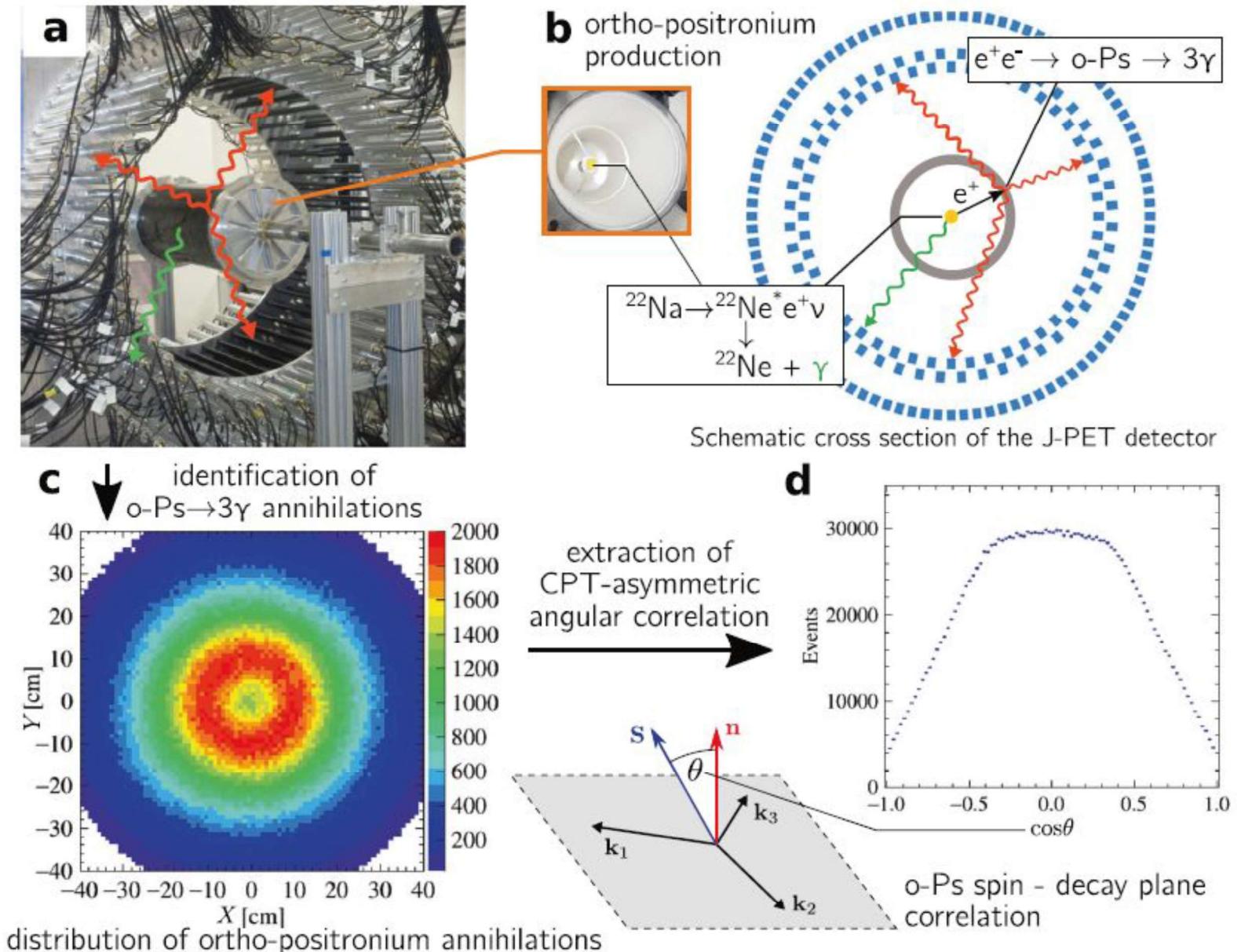
the level of observed CPT violation (after correction of analyzing power - 37.4%)

$$C_{CPT} = 0.0026 \pm 0.0031 \text{ [Phys. Rev. Lett. 91 (2003) 263401 ]}$$

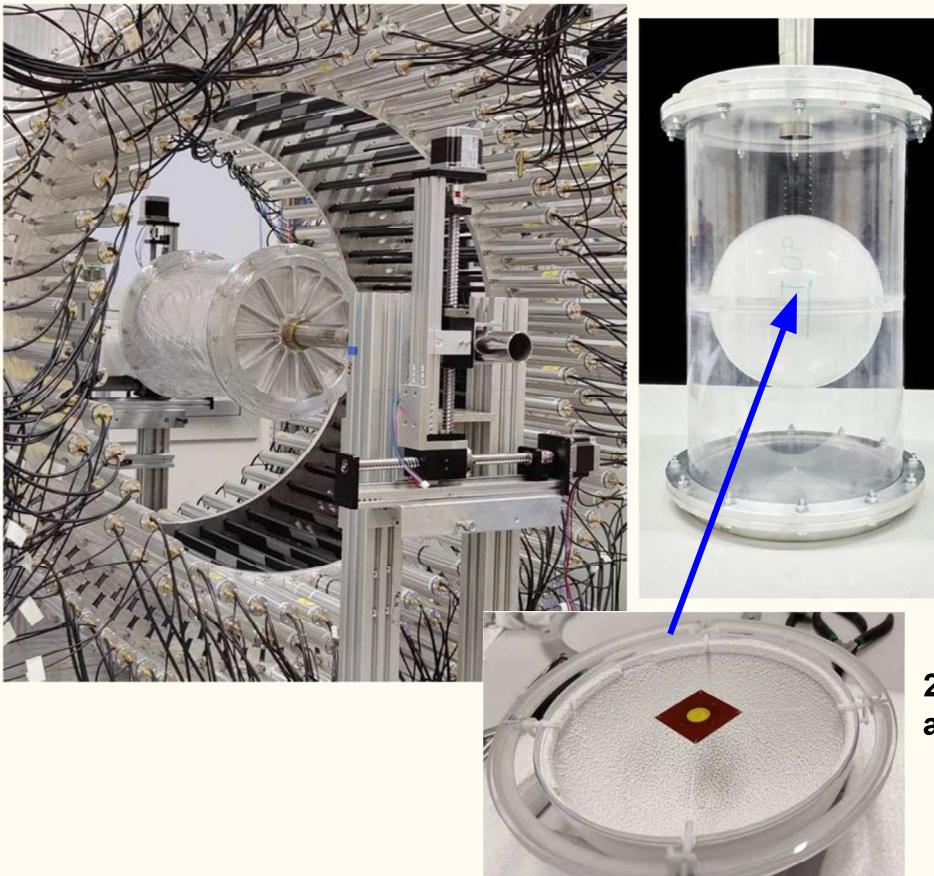
stat error :  $3.3 \times 10^{-4}$   
syst error:  $1.4 \times 10^{-4}$

## Towards $\langle O_{CPT} \rangle$ : summary

26 days of measurement, sodium source activity 10 MBq,  $7.3 \times 10^6$  event candidates

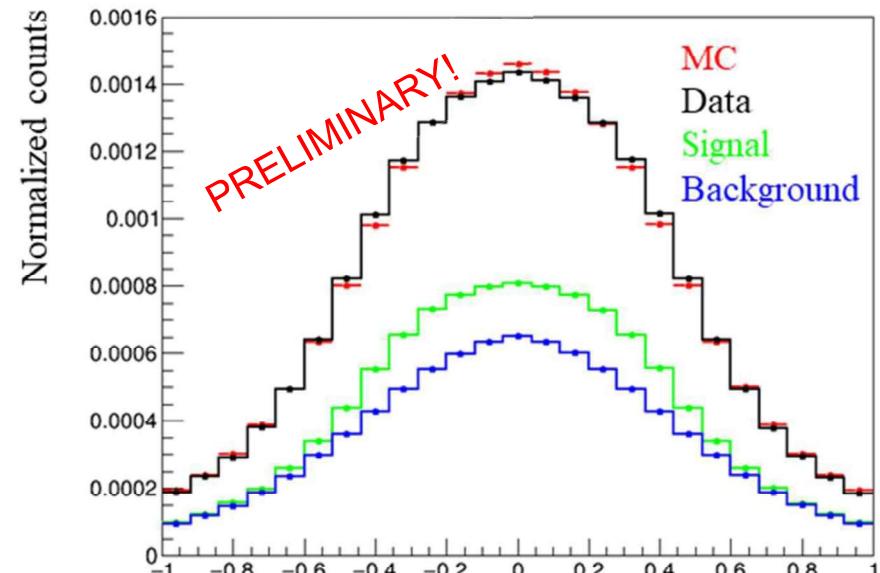


## Towards $\langle O_{CPT} \rangle$ : new preliminary result



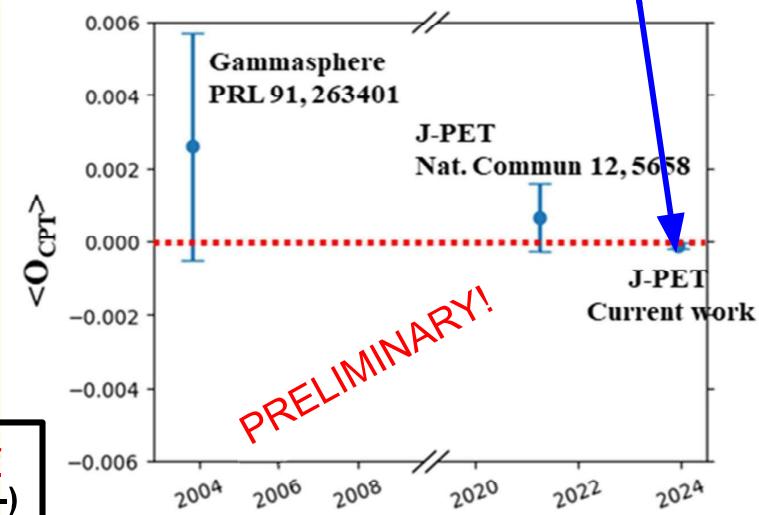
- Spherical annihilation chamber is used to increase positronium formation
- $^{22}\text{Na}$  source with activity of 1 MBq and 4 MBq
- 16 months of continuous data-taking (2021 - 2022)
- about 40mln of event candidates

The achieved precision is a factor of four better than the previous results :-)

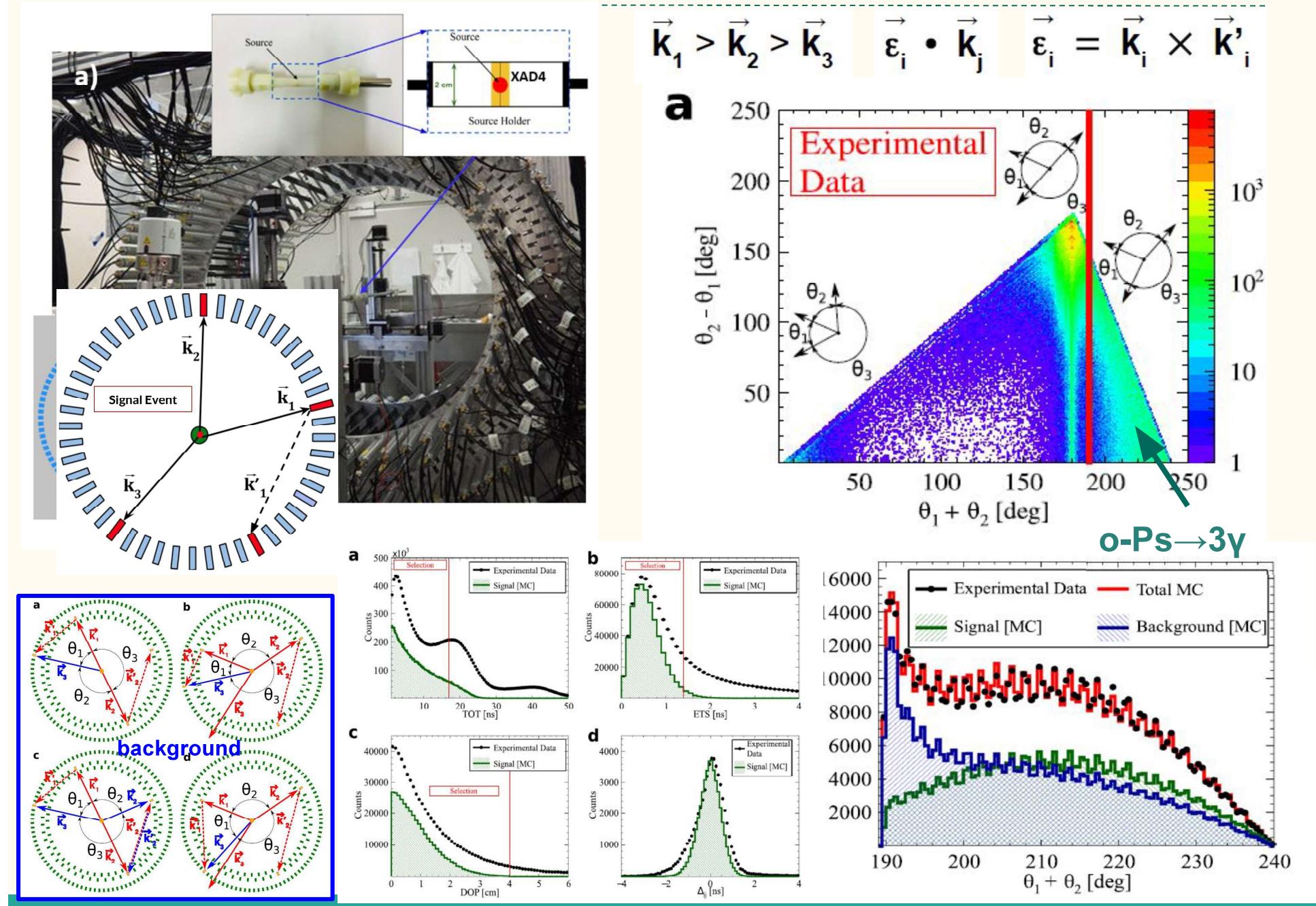


$2.8 * 10^6$  identified o-Ps events from data with 1 MBq source activity (22% of data)

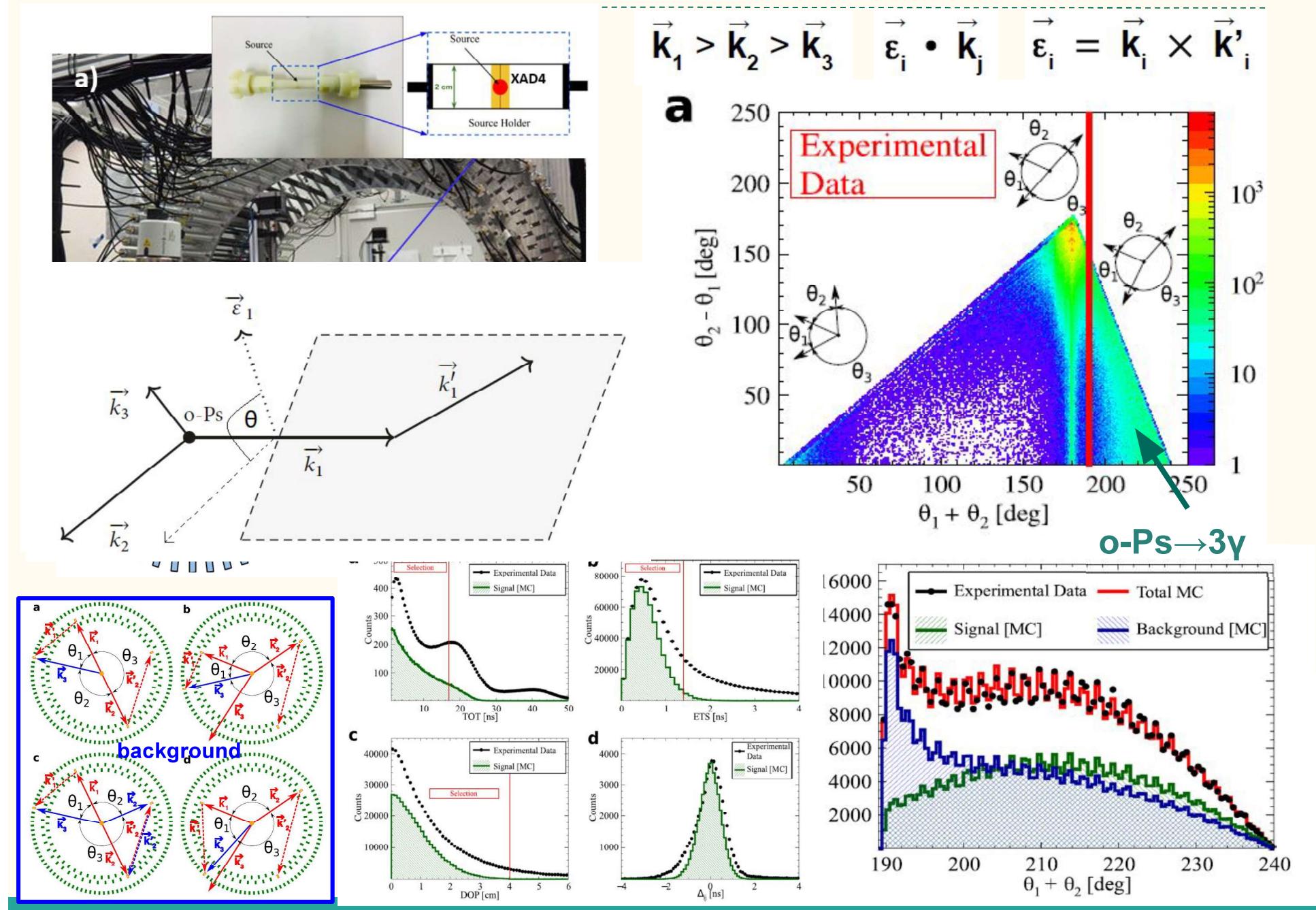
CPT over years



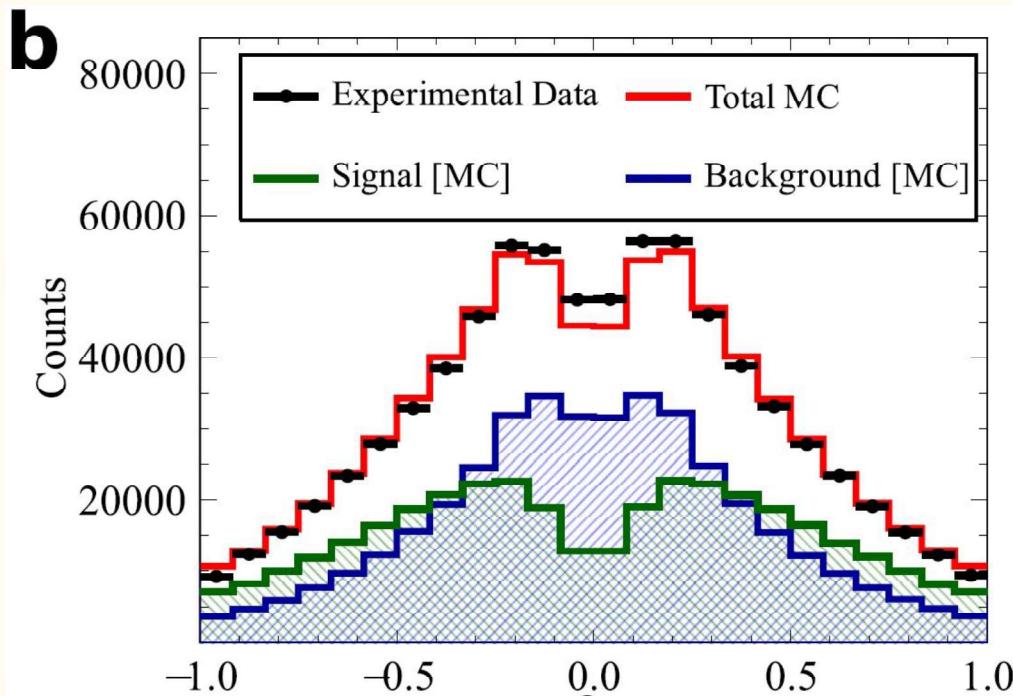
# Towards $\langle O_{CP} \rangle$ determination: Identification of o-Ps $\rightarrow$ 3 $\gamma$ events



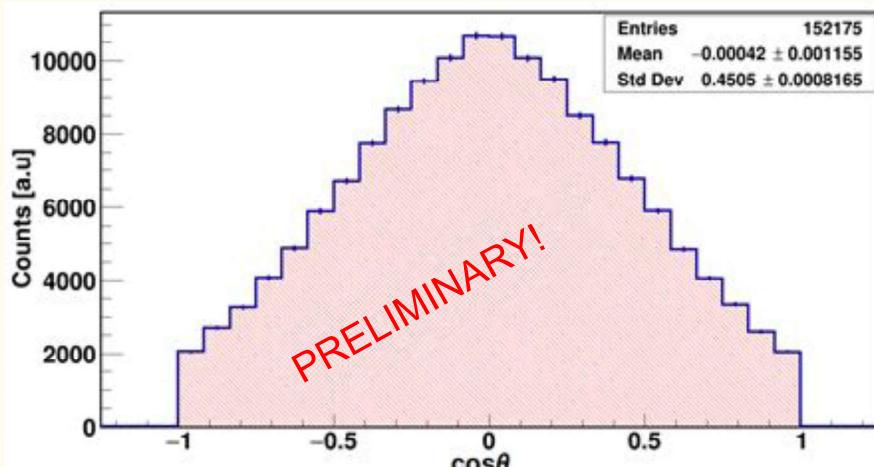
# Towards $\langle O_{CP} \rangle$ determination: Identification of o-Ps $\rightarrow$ 3 $\gamma$ events



## Towards $\langle O_{CP} \rangle$ : determination of the CP observable $O_{CP} = \vec{k}_1 \cdot \vec{\epsilon}_2 / |\vec{k}_1| |\vec{\epsilon}_2| = \cos\theta$

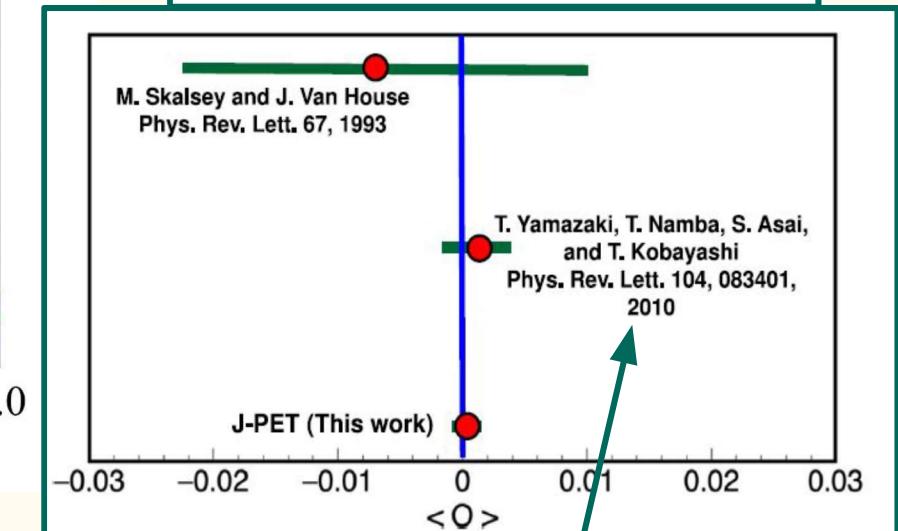


P. Moskal, et al., Nature Commun. 15, 78 (2024)



122 days of measurement, four data runs:  
2 with  $^{22}\text{Na}$  source of 5 MBq activity and  
2 with activity of 1 MBq,  $7.7 \times 10^5$  events

$$\langle O_{CP} \rangle = 0.0005 \pm 0.0007_{\text{stat.}}$$



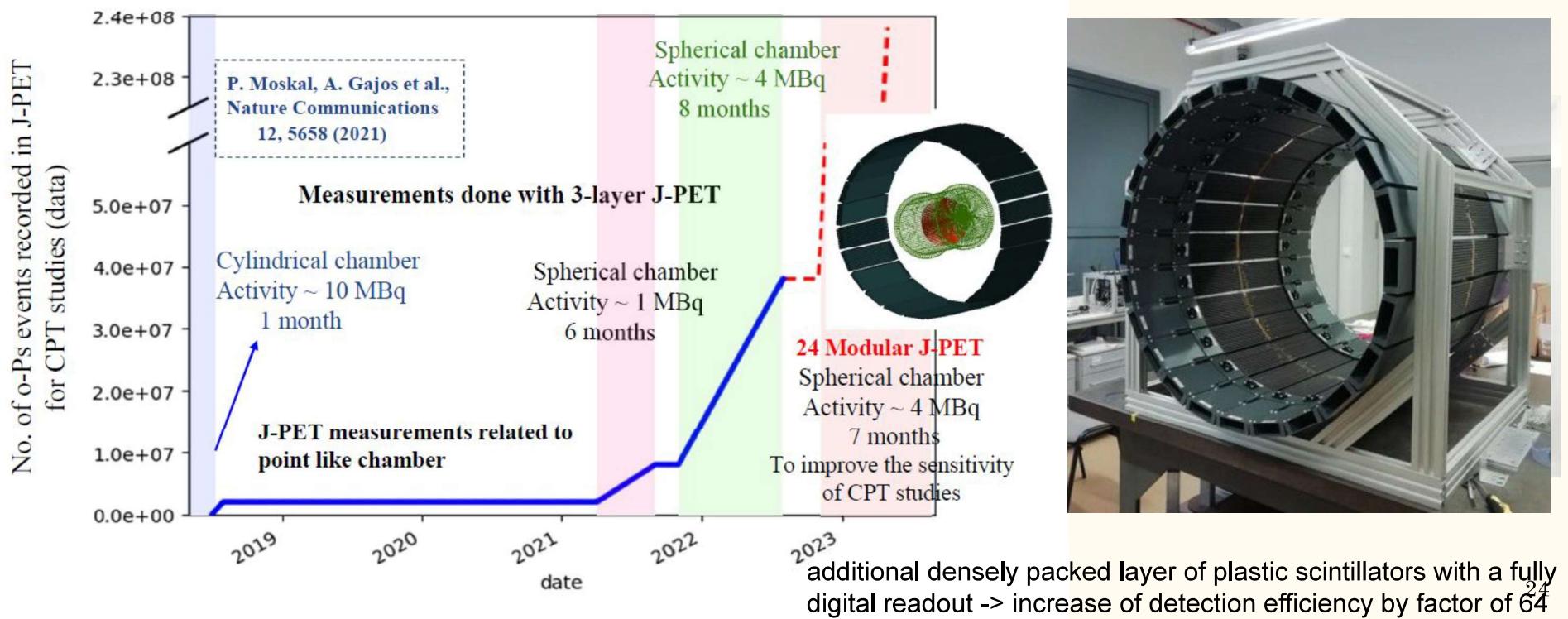
$$\langle C_{CP}[(\vec{S} \cdot \vec{k}_1)(\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2))] \rangle = 0.0013 \pm 0.0022_{\text{stat.}}$$

NEW analysis ongoing for 250 days of measurement,  $^{22}\text{Na}$  source of 0.702 MBq

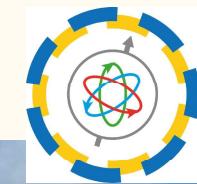
13% of data sample

## Summary and Perspectives

- With J-PET scanner, we are able to perform exclusive measurement of ortho-positronium ( $\text{o-Ps}$ ) annihilation into 3 photons
  - $\text{o-Ps}$  spin event-by-event estimation
  - $\text{o-Ps} \rightarrow 3\gamma$  decays reconstruction including determination of the annihilation point in an extensive-size medium
  - determination of polarization of annihilation  $\gamma$  quanta
- **Sub-permil precision of the CPT and CP tests reached with the first J-PET measurements: over factor of 3 better** than the previous results
- J-PET aims at the sensitivity of the CP and CPT symmetry tests at the level of  $10^{-5}$  with the pending improvements to the setup



# Thank you for your attention



J-PET

