#### KAMPAI (ECT\* workshop) @ Trento, Italy

- Kaonic, Antiprotonic, Muonic, Pionic and "onia" exotic Atoms: Interchanging knowledge and recent results -

Sept 30, 2024

/acuum Polarization

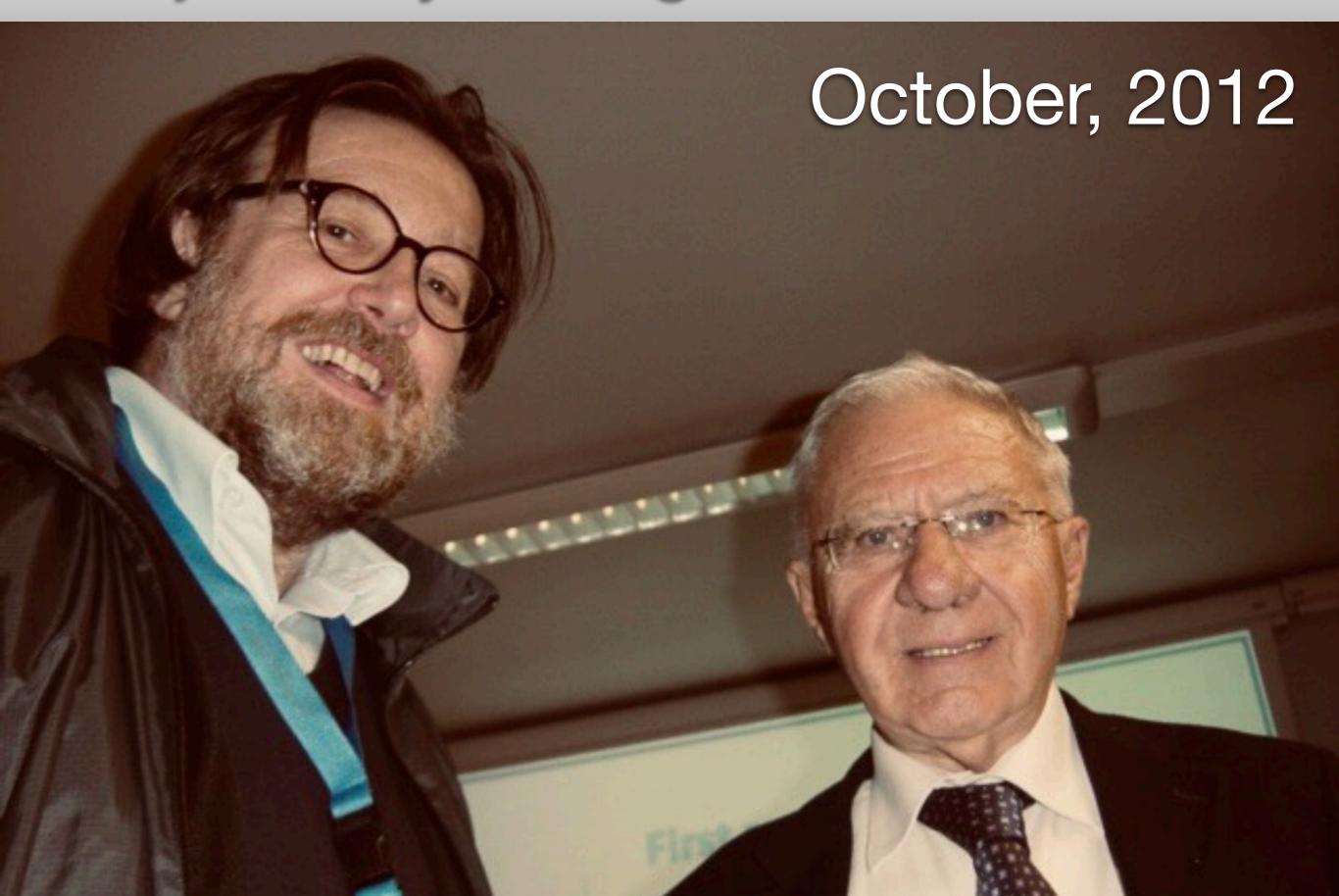
# Precision X-ray Spectroscopy in Muonic Atoms and Molecules

Self Energy

Shinji OKADA (Chubu Univ.) for HEATES collaboration

Negative muon

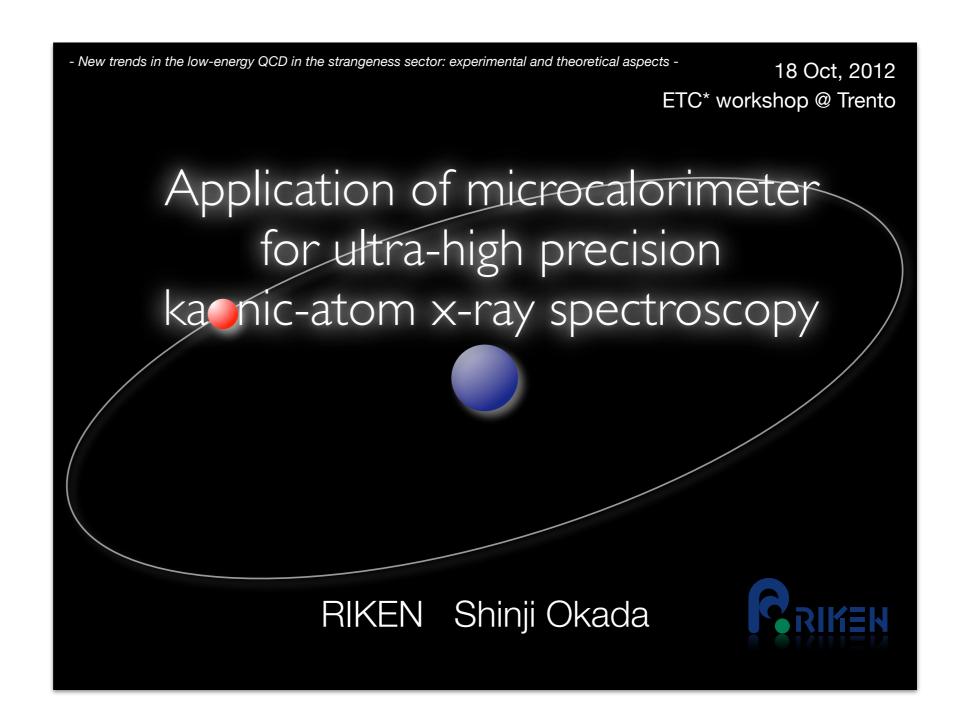
# just 12 years ago here in ECT\*



# ECT\* - Oct 2012



# My presentation 12 years ago

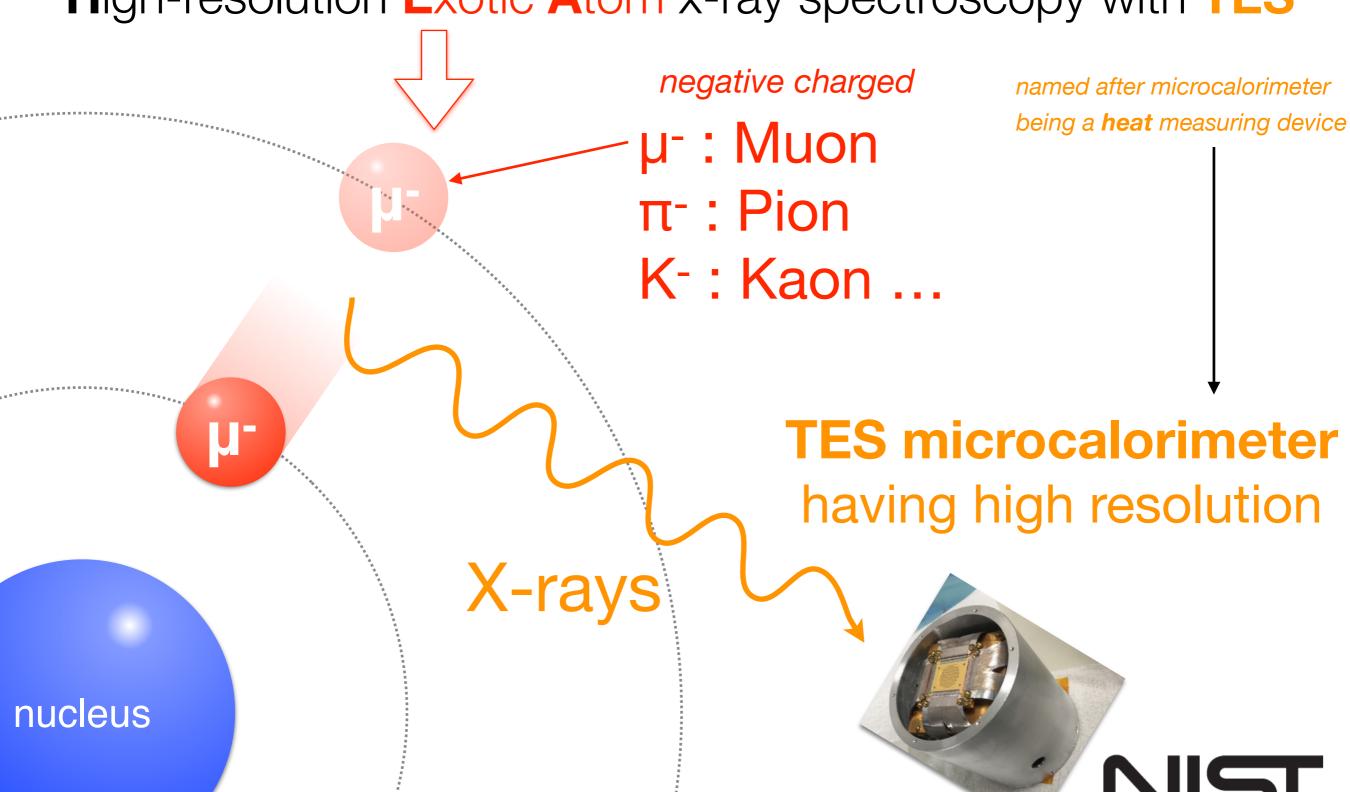




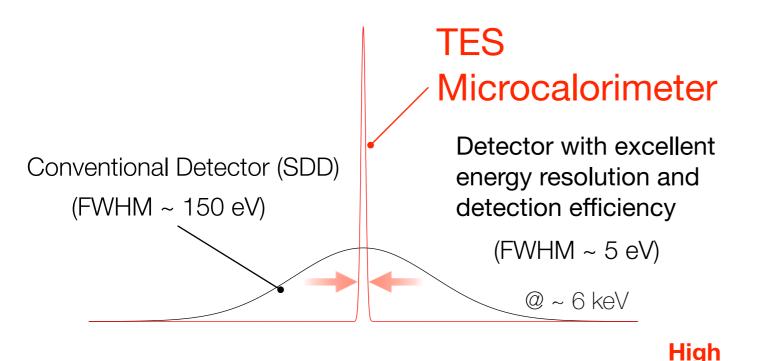
This was "the idea stage" of this project before the "HEATES collaboration" with NIST began.

# **HEATES** project

High-resolution Exotic Atom x-ray spectroscopy with TES



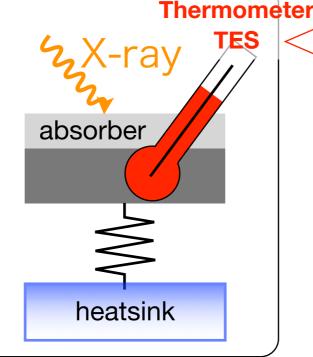
# Innovative Spectroscopic Techniques

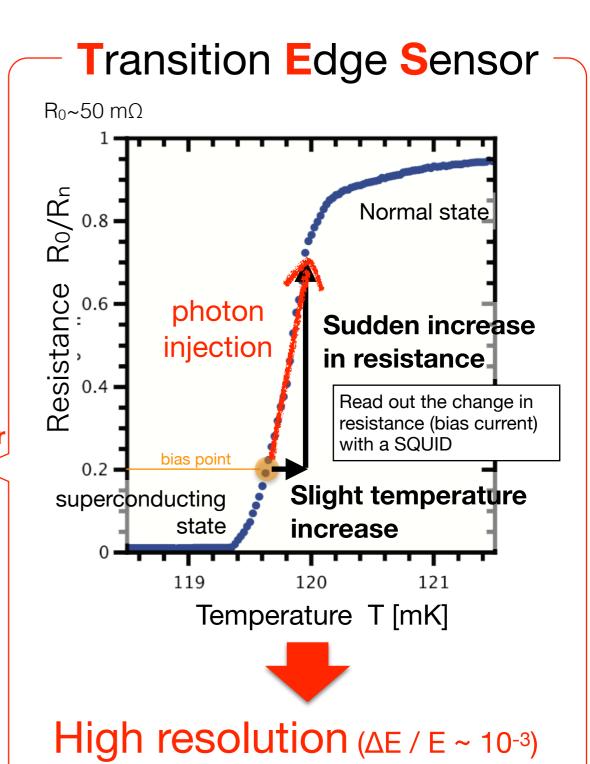


TES microcalorimeters

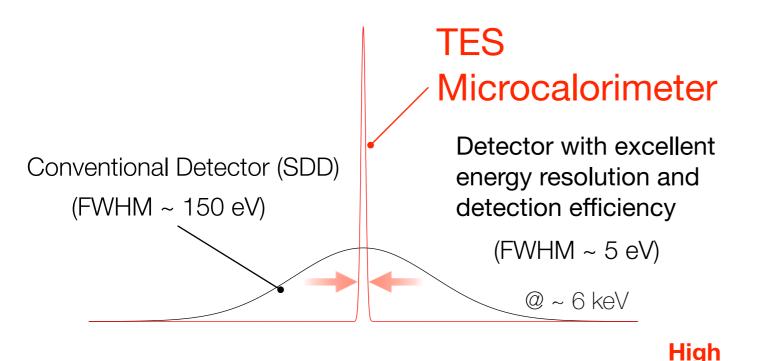
1. incident particles are absorbed by the absorber

- 2. energy  $\Delta E$  is converted to phonons
- 3. **slight temperature rise** is measured with high sensitivity thermometer TES





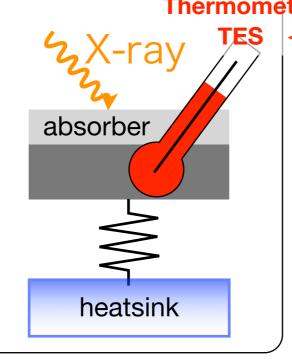
# Innovative Spectroscopic Techniques

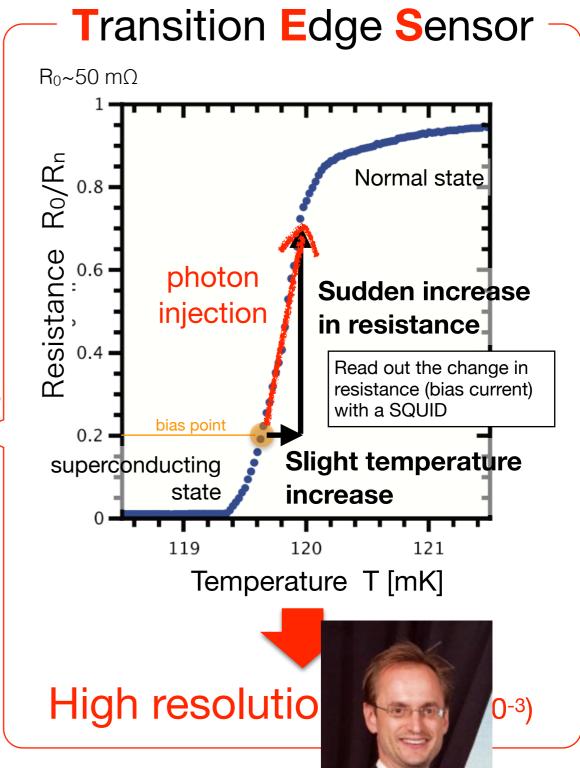


TES microcalorimeters

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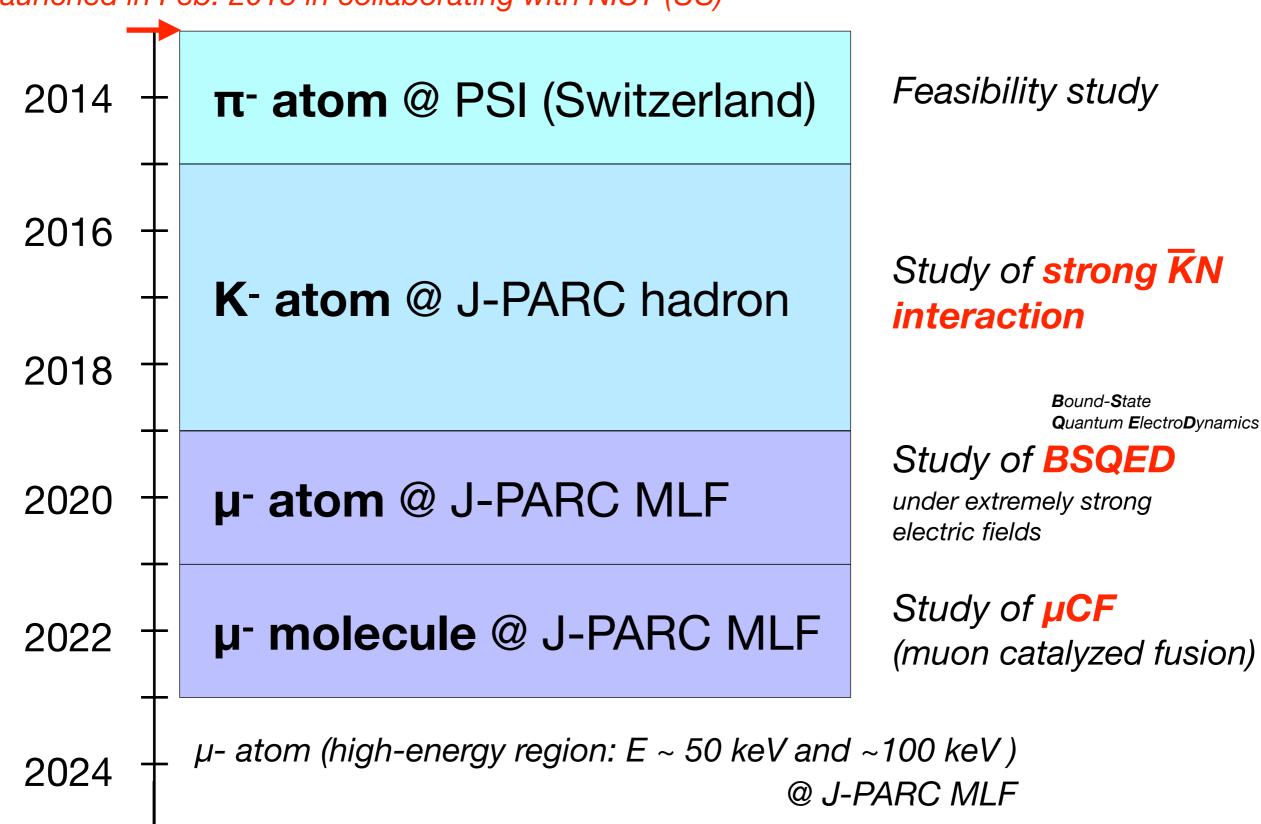




Please refer to presentation of Joel Ullom (NIST) tomorrow for further details!

# History (Study of exotic atoms using TES)

Launched in Feb. 2013 in collaborating with NIST (US)



## Results

#### 3 publications & a new measurement

(a)	Kaonic atom	Phys. Rev. Lett. 128, 112503 (2022).	a single sharp X-ray peak
(b)	Muonic atom	Phys. Rev. Lett. 130, 173001 (2023).	(absolute energy)
(c)	Muonic atom ~Serendipity~	Phys. Rev. Lett. 127, 053001 (2021).	a broad structure
(d)	Muonic molecule	New experiment (to be published)	(complex of many X-ray lines)

## Results

#### 3 publications & a new measurement

(a)	Kaonic atom	Phys. Rev. Lett. 128, 112503 ( <mark>2022</mark> ).	a single sharp X-ray peak
(b)	of Tadashi Hash	to presentation 130, nimoto (RIKEN)	(absolute energy)
(C)	the day after Muonic atom ~Serendipity~		a broad structure
(d)	Muonic molecule	New experiment (to be published)	(complex of many X-ray lines)

#### Results

#### 3 publications & a new measurement

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→ focusing on these two latest results

#### Contents

- 1. Muonic atom (BSQED)
- 2. Muonic molecule (µCF)
- 3. Summary & Outlook

a single sharp X-ray peak (absolute energy)

# 1. Muonic atom (QED)

# Collaboration (µNe)

#### J-PARC MLF 2019MS01 collaboration (for μNe)

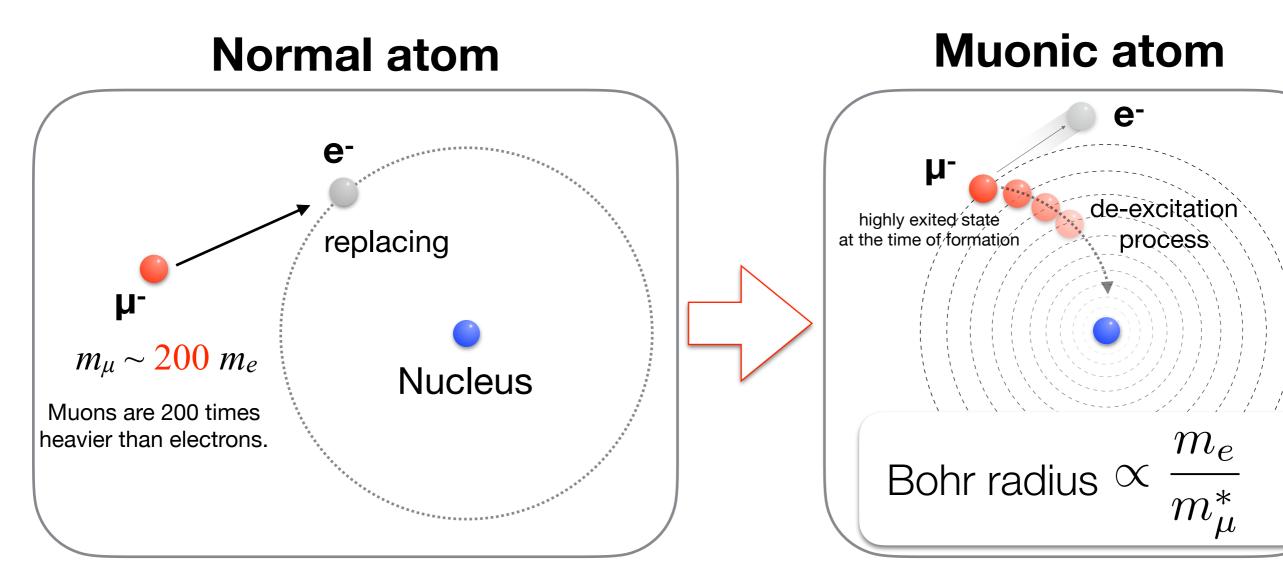
Shinji	Okada	Chubu Univ.			
Miho	Katsuragawa				
Kairi	Mine	IPMU			
Tadayuki	Takahashi	IPMU			
Shinichiro	Takeda				
Tadashi	Hashimoto	JAEA			
Shin	Watanabe JAXA				
Naritoshi	Kawamura				
Sohtaro	Kanda	Japan			
Yasuhiro	Miyake				
Kouichiro	Shimomura				
Patrick	Strasser	rasser			
Soshi	Takeshita				
Motonobu	Tampo				
I Huan	Chiu				
Kazuhiko	Ninomiya	Osaka Univ.			
Hirofumi	Noda				
Toshiyuki	Azuma				
TadaAki	Isobe	RIKEN			
Yasuhiro	Ueno				

Ryota		Hayakawa			
Yuto		Ichinohe	Rikkyo Univ.	Japan	
Shinya		Yamada			
Yasushi		Kino	Tohoku Univ.		
Kenichi		Okutsu	TOTIONU OTIIV.		
Takuma		Okumura	Tokyo		
Hirotaka		Suda	Metropolitan		
Hideyuki		Tatsuno	Univ.		
Paul		Indelicato	CNRS	France	
Nancy		Paul	CINDO		
Douglas	A.	Bennett			
William	B.	Doriese			
Malcolm	S.	Durkin			
Joseph	Joseph W.				
Johnathon	D.	Gard			
Gene	C.	Hilton	NICT	110	
Kelsey	Kelsey M. Galen C. Carl D.		NIST	US	
Galen					
Carl					
Dan	R.	Schmidt			
Daniel	Daniel S.				
Joel	N.	Ullom			

(Nuclear & Hadron + Atomic & Muon + Astro) physicists + TES experts

#### Muonic atom

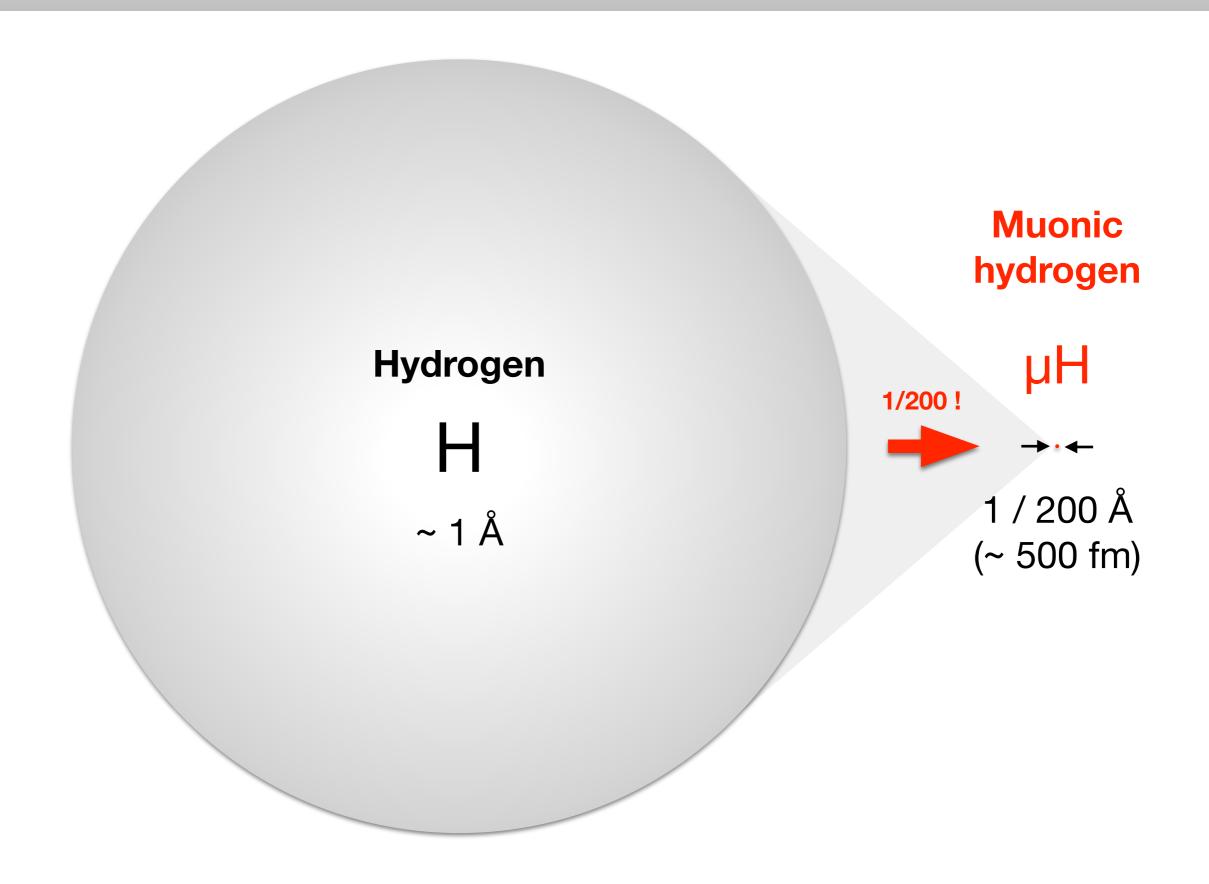
Muon atoms are formed when negative muons are replaced by electrons.



(inversely proportional to their reduced mass)

These radii are as small as 1/200 (µ- atom) compared to the normal atoms.

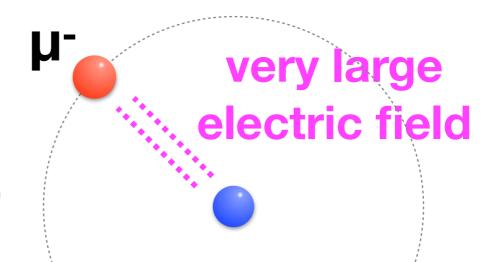
# Image of the scale



# Extremely close to the nucleus!

Bohr radius

 $R_{\mu} \sim 1/200 \ R_e \ (\mu^- \ \text{atom})$ 

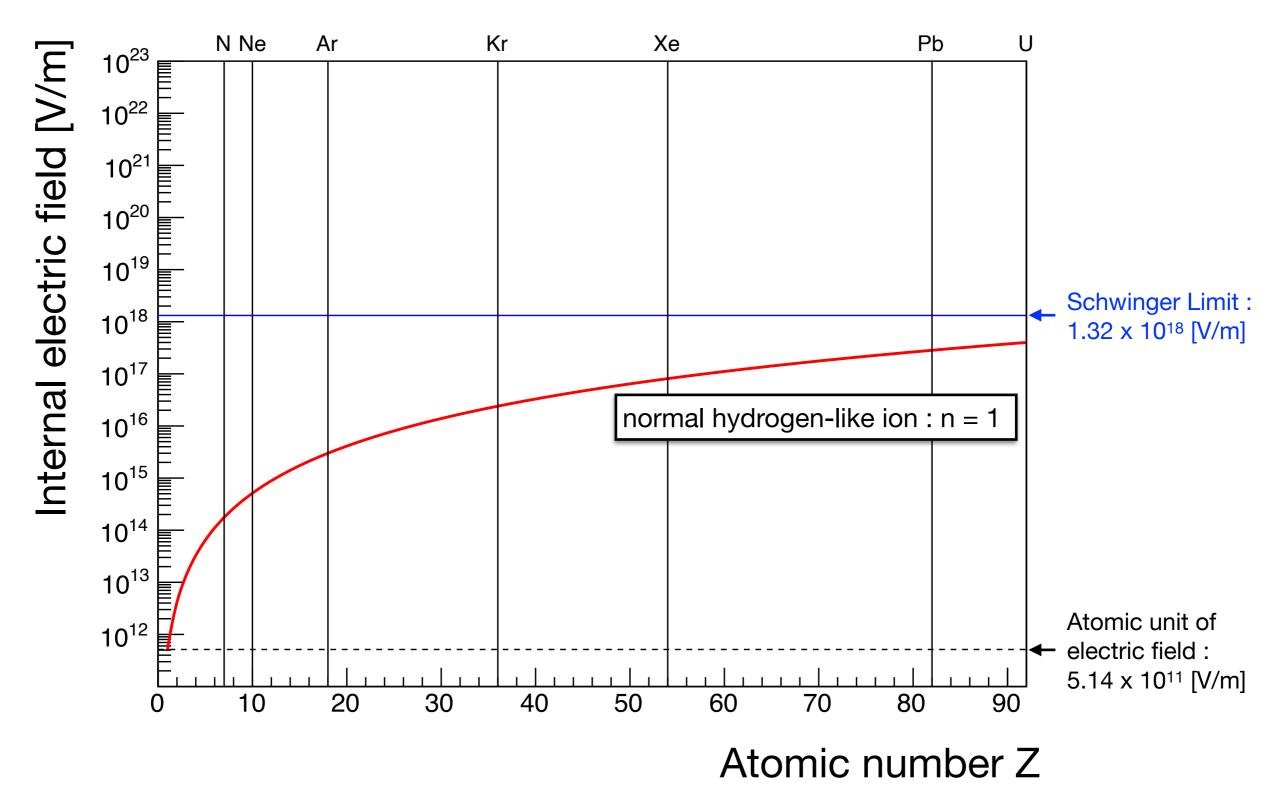


- √ µ- feels an extremely large electric field
  - ⇒internal electric field strength is proportional to the squire of the mass ratio to atoms
    - (→ being 200² (=40,000) times higher than that of normal H-like ions.)

Study of "QED under strong field"

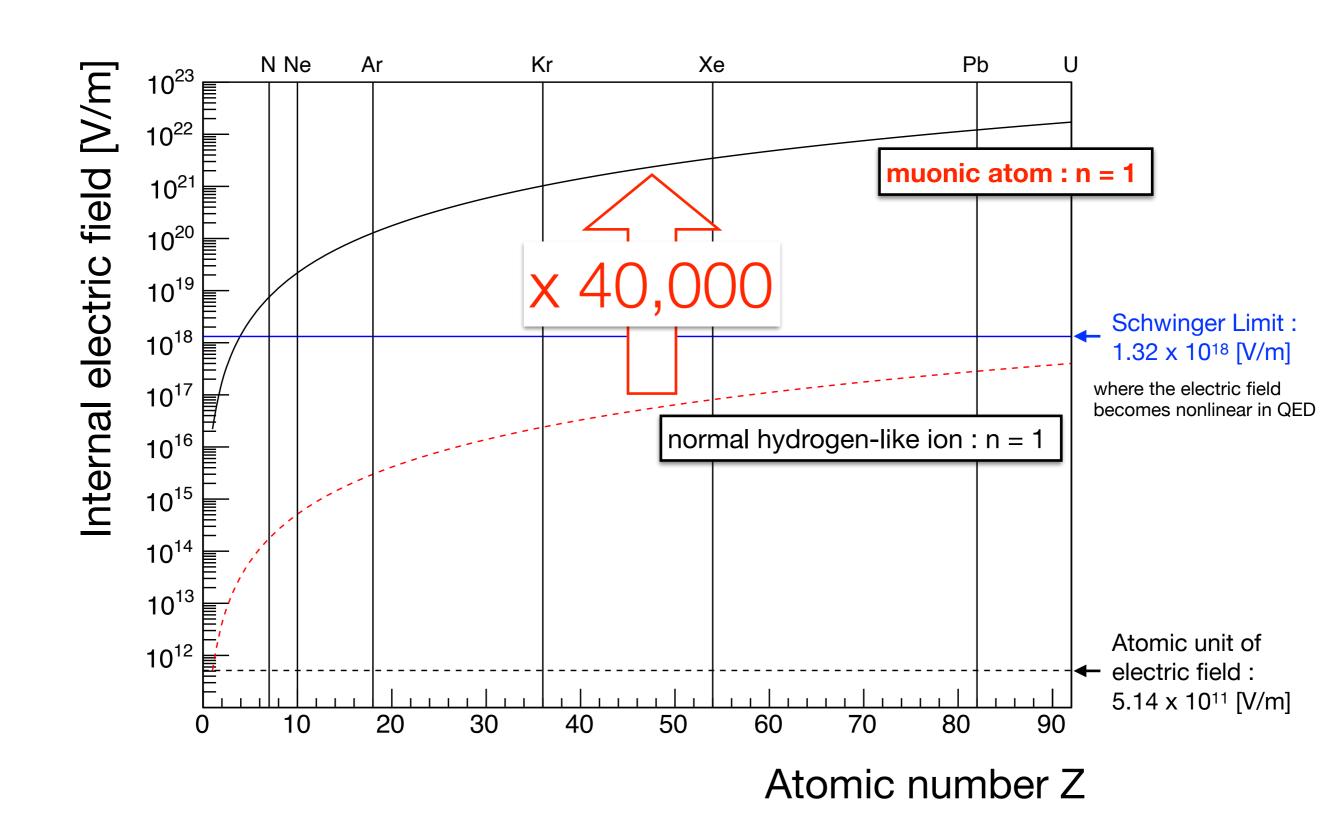
QED: Quantum ElectroDynamics

## Internal electric field $\propto Z^3$

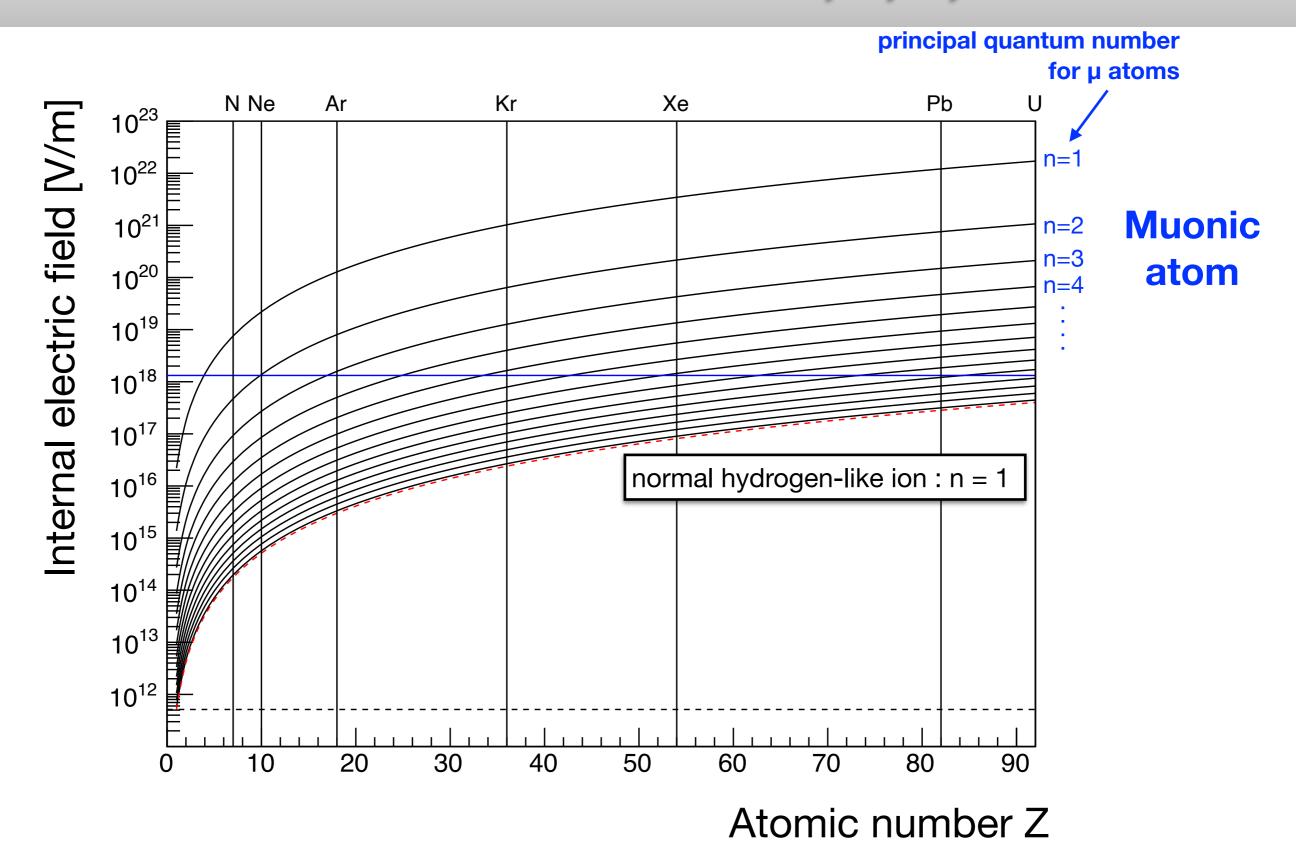


strong electric field @ heavier atoms

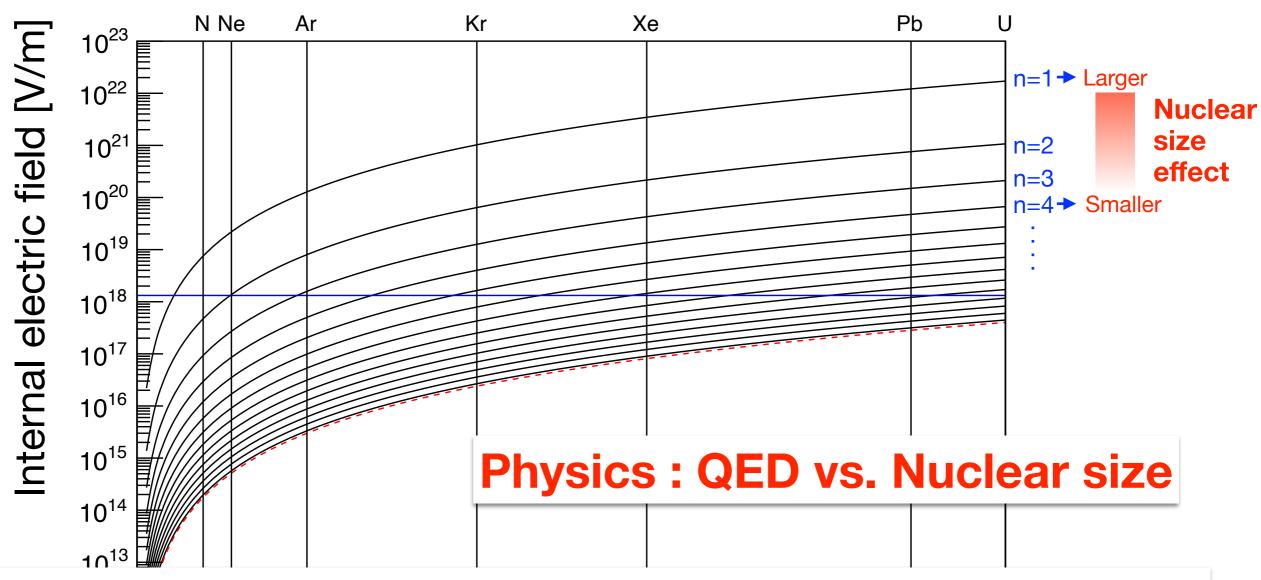
### Internal electric field: x 2002



# Muonic atom : n = 1,2,3,4...



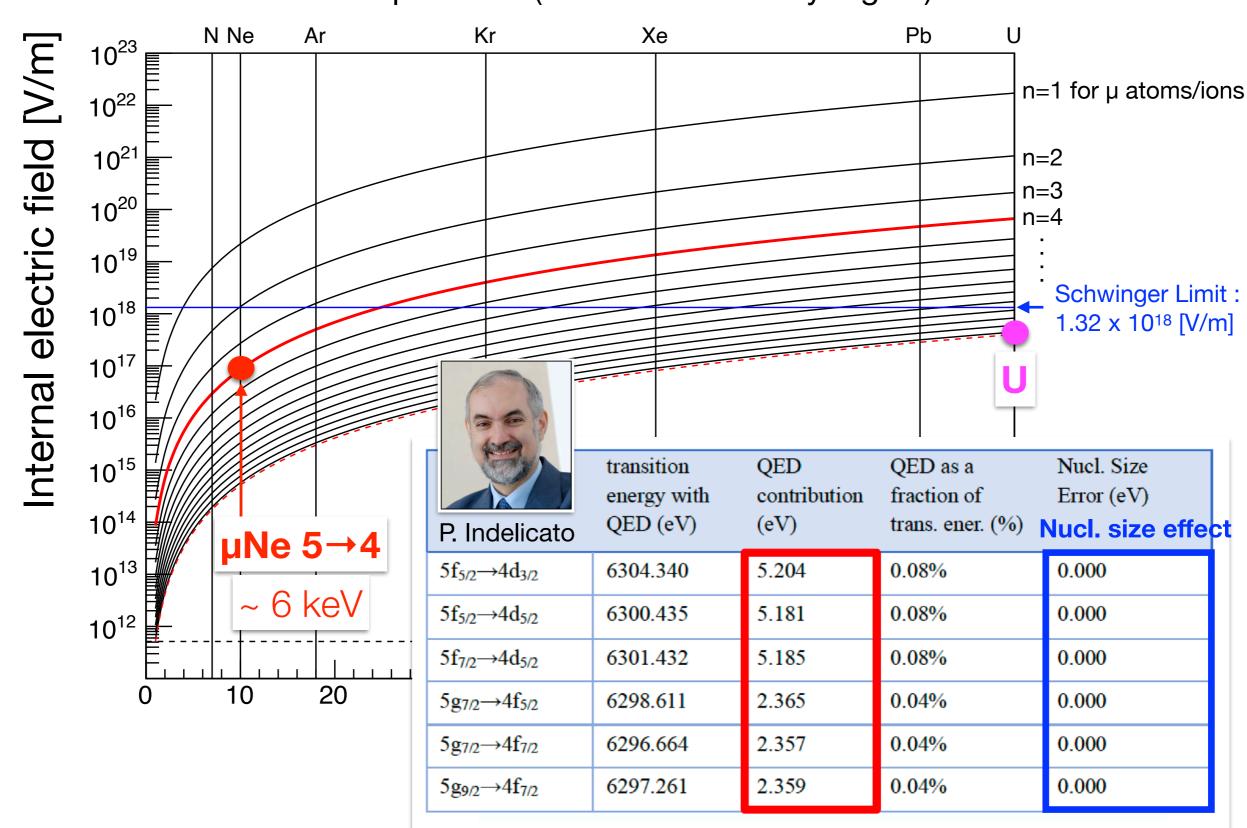
# Avoiding nuclear-size effect



- ✓ But, in the Lower "n" (principal quantum number) state, nuclear size effect (overlapping with nucleus) become dominant.
- → Carefully choose X-ray transition into the energy level where the nuclear size effect is negligible but having significant QED effect

#### Proof-of-Principle Experiment with µNe 5→4

The first experiment (with ~10 keV X-ray region)



# PRL (2021)

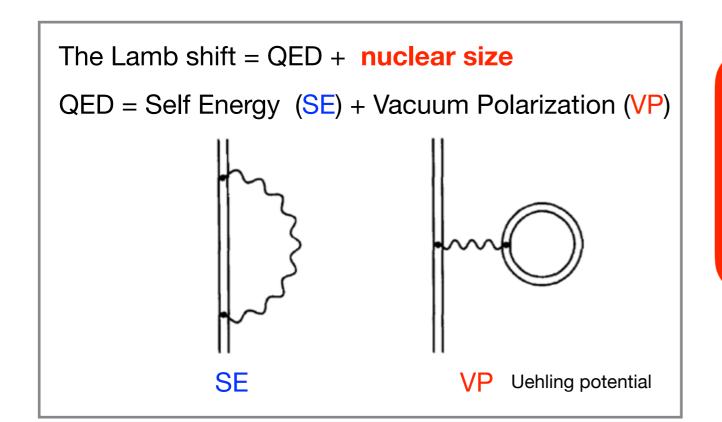


#### PHYSICAL REVIEW LETTERS 126, 173001 (2021)

TABLE I. Transition energies, QED, and finite size corrections for transitions amenable to BSQED tests in muonic atoms and antiprotonic atoms, compared to transitions of similar energies in highly charged ions. All energies are given in eV.

		Initial	Final	Theoretical	1st order	2nd order					
Particle	Element	state	state	transition energy	QED	QED	$g-2 \bar{p}$	FNS	FNS/QED	Exp.	Ref.
$e^{-}$	<sup>40</sup> Ar	$2p_{3/2}$	$1s_{1/2}$	3322.9931	-1.1238	0.0007		-0.0090	0.804%	3322.993(14)	[6]
$\mu^-$	$^{20}$ Ne	$6h_{11/2}$	$5g_{9/2}$	3419.6828	0.3845	0.0042		0.0001	0.013%		
$\bar{p}$	<sup>40</sup> Ar			3522.9850	1.2209	0.0124	0.0618	0.0002	0.014%		
$e^{-}$	<sup>56</sup> Fe	$2p_{3/2}$	$1s_{1/2}$	6973.1815	-3.8873	0.0042		-0.0527	1.357%	6972.73(24)	[50]
$\mu^-$	<sup>20</sup> Ne	$5g_{9/2}$	$4f_{7/2}$	6297.2616	2.3365	0.0229		0.0003	0.013%		
$e^{-}$	<sup>84</sup> Kr	$2p_{3/2}$	$1s_{1/2}$	13 508.9648	-11.4244	0.0181		-0.2963	2.594%	13 508.95(50)	[66]
$\mu^-$	<sup>20</sup> Ne	$4f_{7/2}$	$3d_{5/2}$	13 616.0000	14.4762	0.1334		0.0034	0.023%		
$ar{p}$	<sup>40</sup> Ar	$11n_{21/2}$	$10m_{19/2}$	13 729.2333	24.6024	0.2198	0.9635	0.0080	0.032%		
$e^{-}$	<sup>132</sup> Xe	$2p_{3/2}$	$1s_{1/2}$	31 283.9469	-43.0973	0.1068		-3.1806	7.380%	31 284.9(18)	[67]
$\bar{p}$	<sup>20</sup> Ne	$6h_{11/2}$	$5g_{9/2}$	29 183.5476	106.3705	0.9818	4.7013	0.0719	0.068%		
$\bar{p}$	$^{84}$ Kr	$13q_{25/2}$	$12o_{23/2}$	32 965.1496	85.8828	0.7744	5.4909	0.0606	0.071%		
$e^{-}$	$^{238}U$	$2p_{3/2}$	$1s_{1/2}$	102 175.0991	-257.2281	1.2278		-198.5110	77.173%	102 178.1(43)	[15]
$\mu^-$	<sup>132</sup> Xe	$6h_{11/2}$	$5g_{9/2}$	100 690.8984	246.5741	2.4873		0.2473	0.100%		
$\bar{p}$	$^{40}Ar$	$6h_{11/2}$	$5g_{9/2}$	97 106.9665	524.4471	5.1928	52.0324	1.0708	0.204%		
$ar{p}$	$^{84}$ Kr	$9l_{17/2}$	$8k_{15/2}$	105 534.2194	505.7241	4.8782	57.9787	1.0624	0.210%		
$ar{p}$	<sup>132</sup> Xe	$12o_{23/2}$		95 937.8866	398.9032	3.7678	46.7550	0.7860	0.197%		
$\mu^-$	$^{84}$ Kr	$4f_{7/2}$	$3d_{5/2}$	178 245.9903	712.8101	7.1647		0.4179	0.059%		
$\mu^-$	<sup>132</sup> Xe	$5g_{9/2}$	$4f_{7/2}$	185 826.8188	664.5075	7.4047		1.1906	0.179%		
$\bar{p}$	$^{84}$ Kr	$8k_{15/2}$	$7i_{13/2}$	154 113.2949	856.7465	8.5547	125.2672	2.6925	0.314%		
$\bar{p}$	<sup>132</sup> Xe	$10m_{19/2}$		170 796.0859	905.9163	8.9726	150.2826	3.2019	0.353%		
$\bar{p}$	$^{184}W$		$11n_{21/2}$	180 885.6145	912.1929	8.9936	166.1718	3.5826	0.393%		
$\bar{p}$	<sup>238</sup> U	,	$13q_{25/2}$	172 808.8745	806.8144	7.9071	150.2331	3.2202	0.399%		

# highly charged ion vs. muonic atom

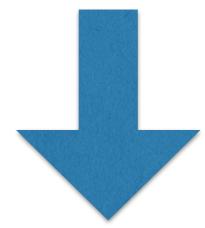


muonic atom: VP > SE

highly charged ion : SE > VP



- → µ- feel "bare" nuclear charge freeing from "polarization" charge.
- → resulting in enhanced VP



#### observing different effects

⇒ complementary relationship

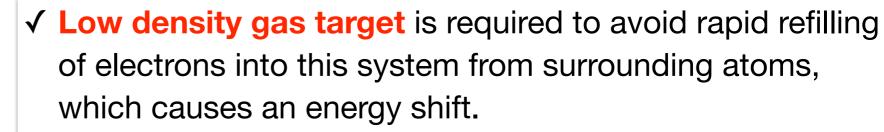
# Low pressure gas target



muon peels off most (or all) of electrons bound to the nucleus

Auger electrons

deexcitation process



✓ But it is difficult to efficiently stop muons experimentally on low-density targets. → resulting low intensity

High-intensity low-energy µ-@J-PARC MLF



TES detector having both "high resolution" and "large effective area"

Z+
nucleus

refilling

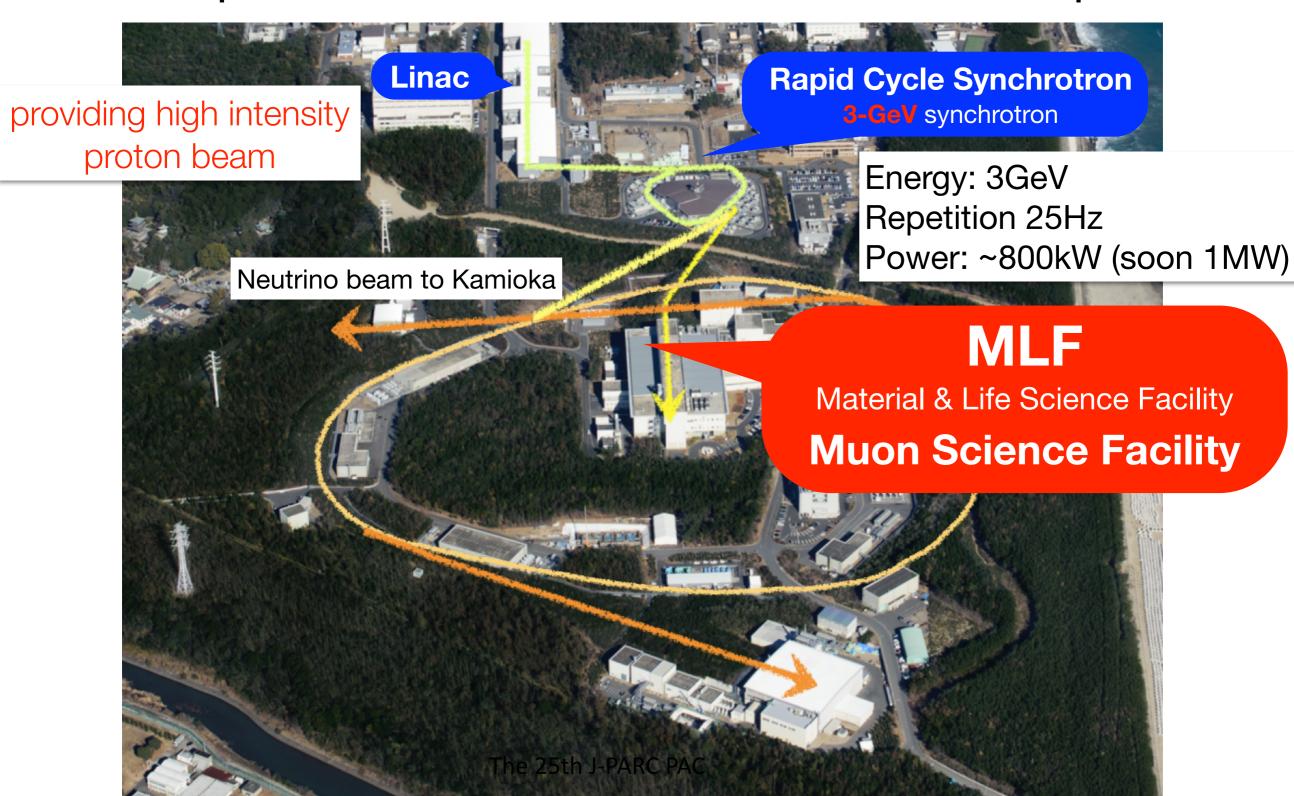
→ energy shift

e-

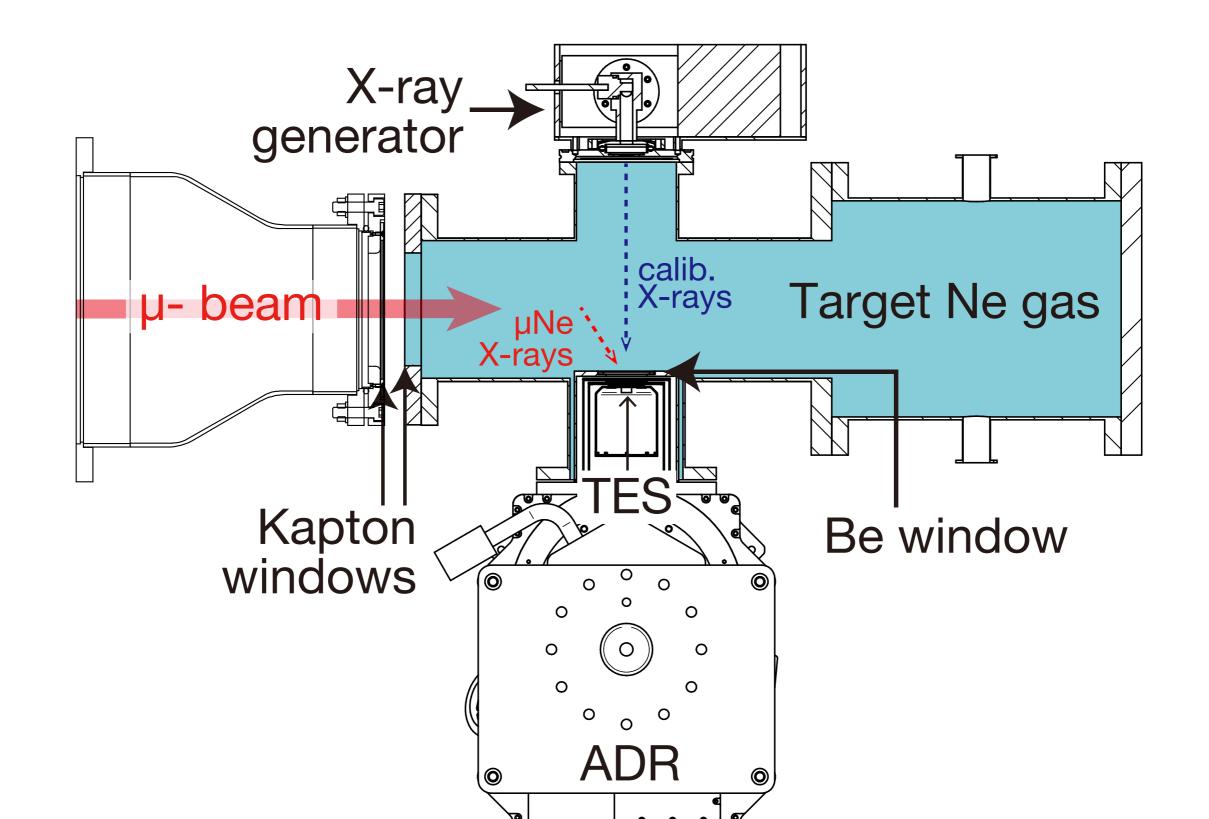
from surrounding atoms

#### J-PARC

#### Japan Proton Accelerator Research Complex

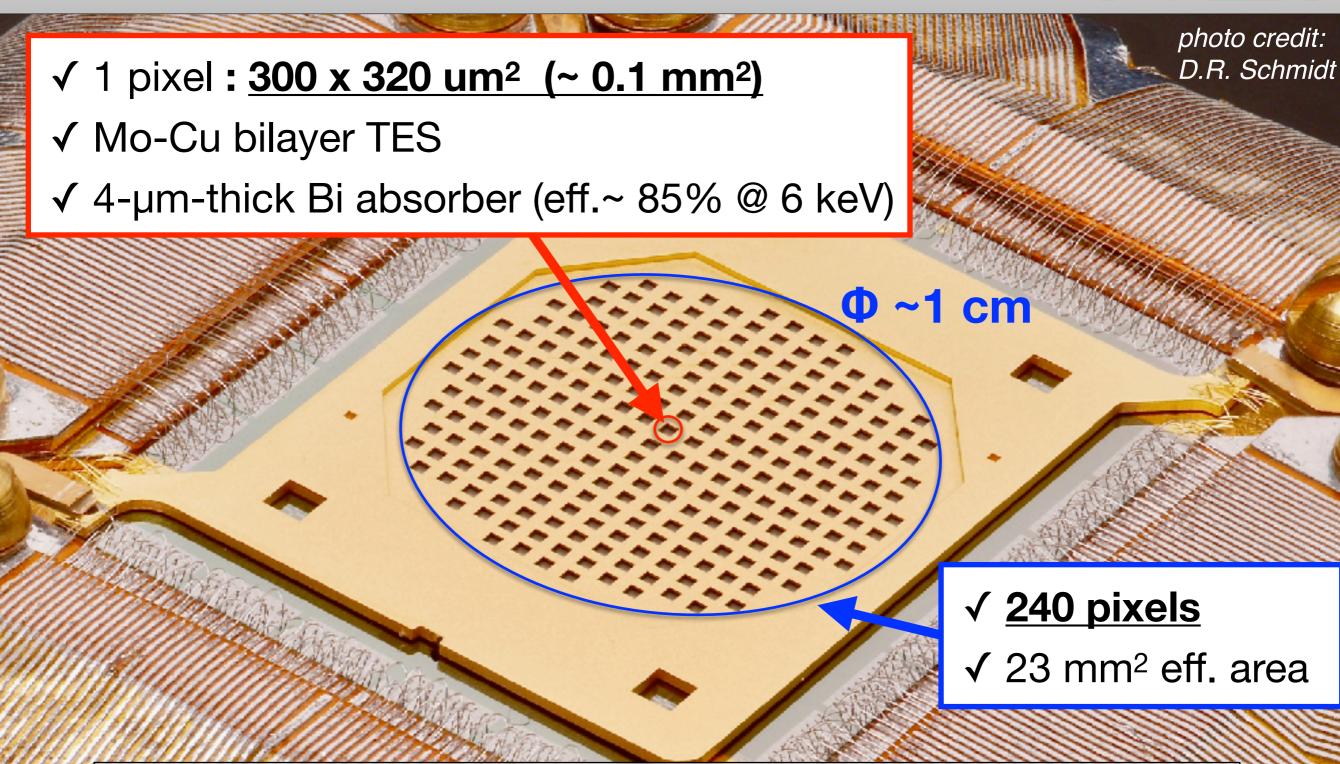


# Experimental setup



## TES array





small pixel size -> multi-pixel array

### Adiabatic Demagnetization Refrigerator (ADR)

✓ Cooled down to 70 mK with ADR & pulse

#### **102 DENALI**

**Pulse Tube ADR Cryostat** 

Vacuum Jacket Size

33 cm X 22 cm X

66 cm Tall

Experimental Volume 24 cm X 15 cm X 14 cm Tall

1st Stage Cooling Power 25 W @ 55 K

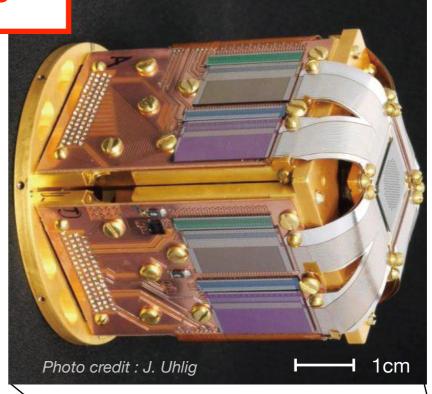
2nd Stage Cooling Power 0.7 W @ 4.2 K

GGG Cooling Capacity
1.2 J @ 1 K
(< 500 mK @ GGG)

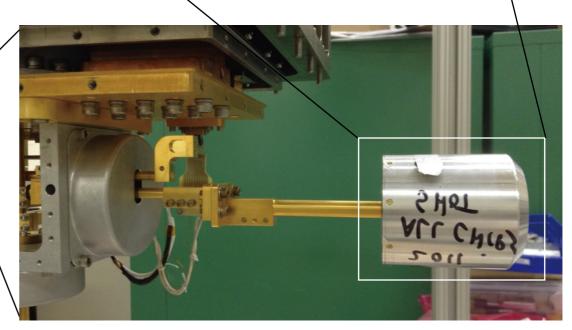
ADR Base Temperature < 50 mK

FAA Cooling Capacity
118 mJ @ 100 mK

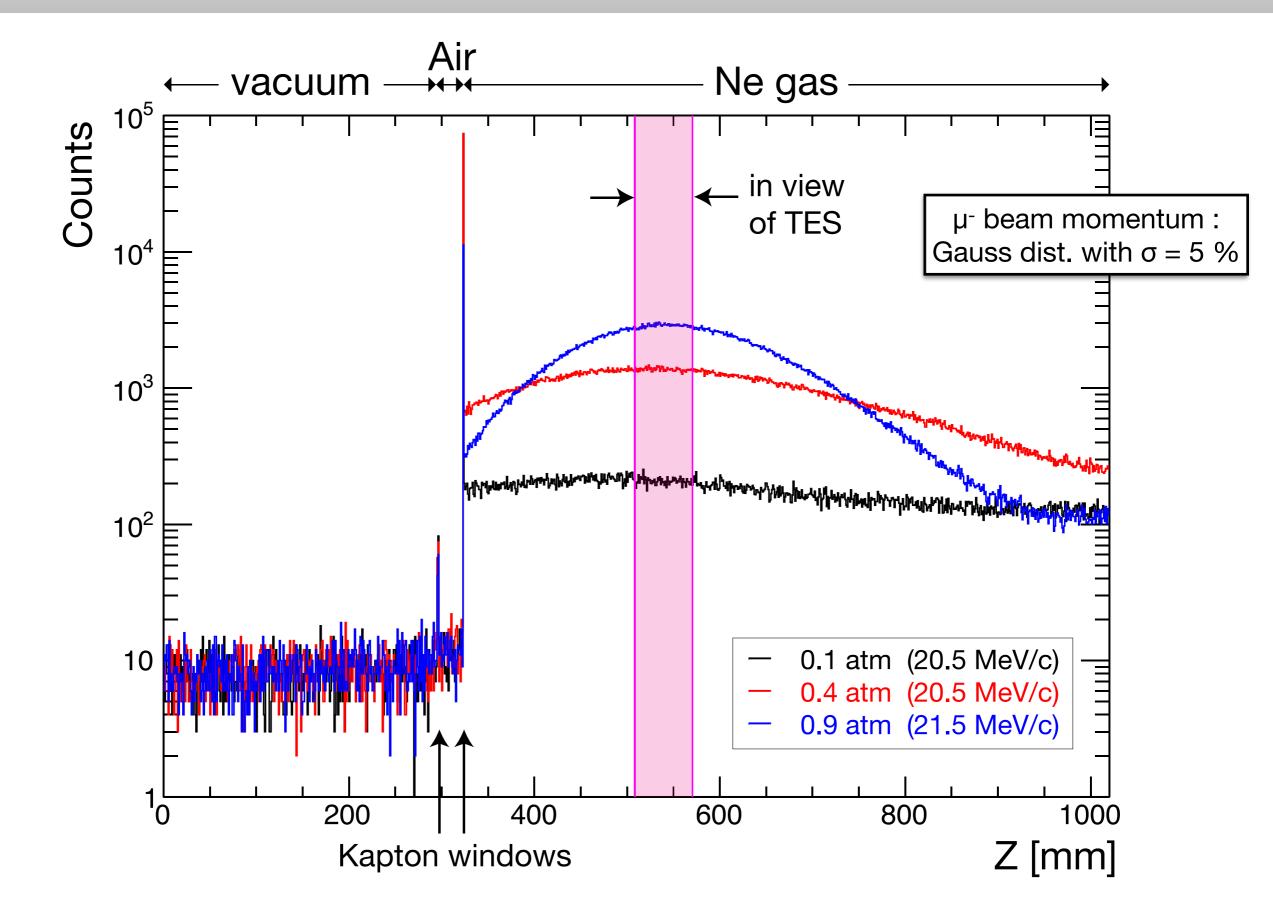




TES chip

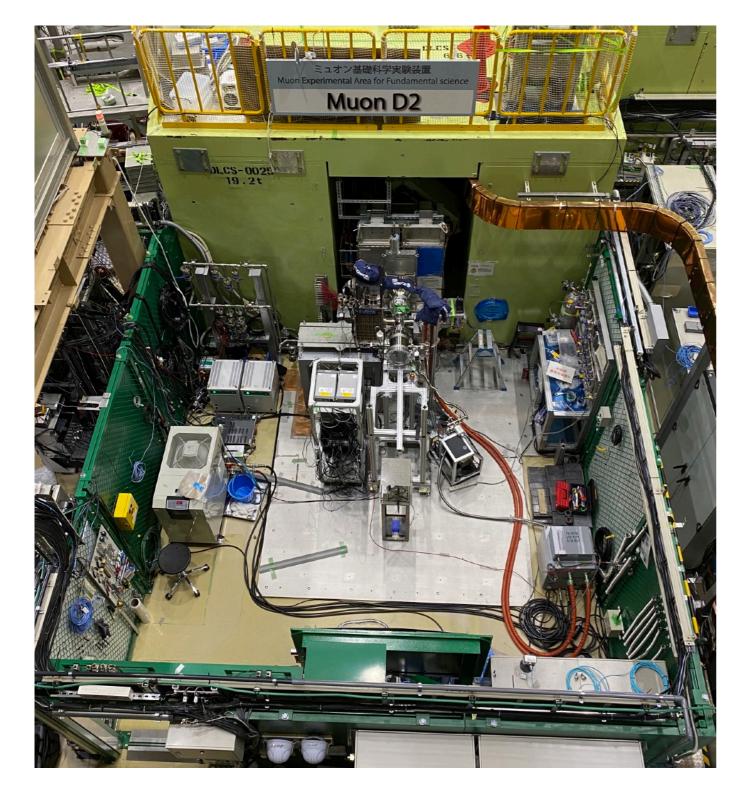


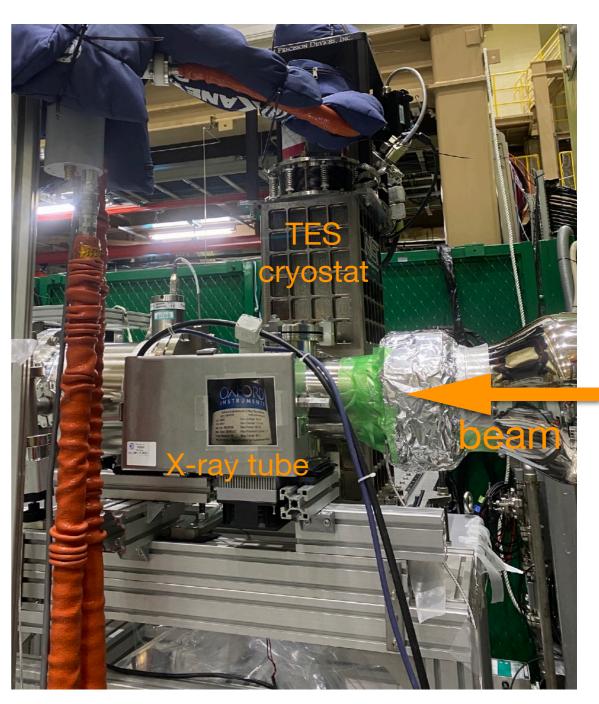
# μ- stopping distribution (sim)



## **Photos**

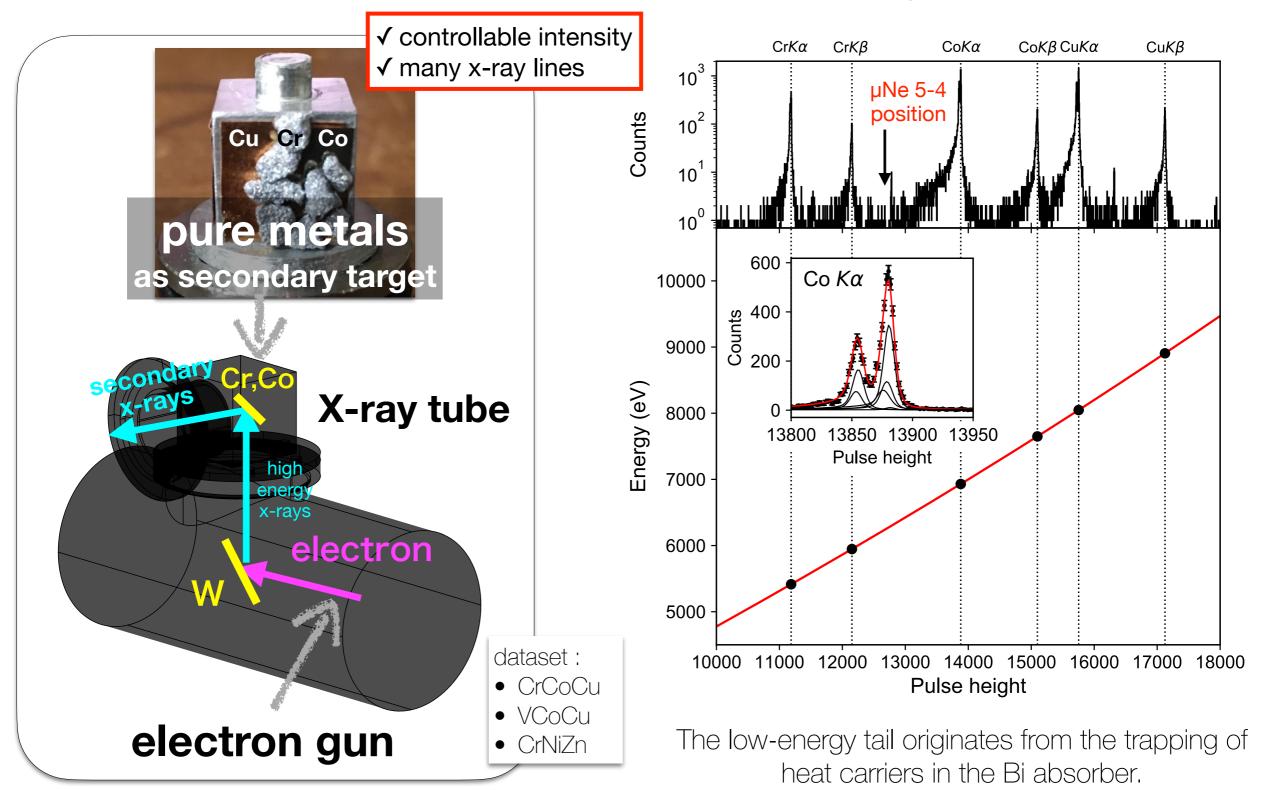
#### Muon beamline @ J-PARC



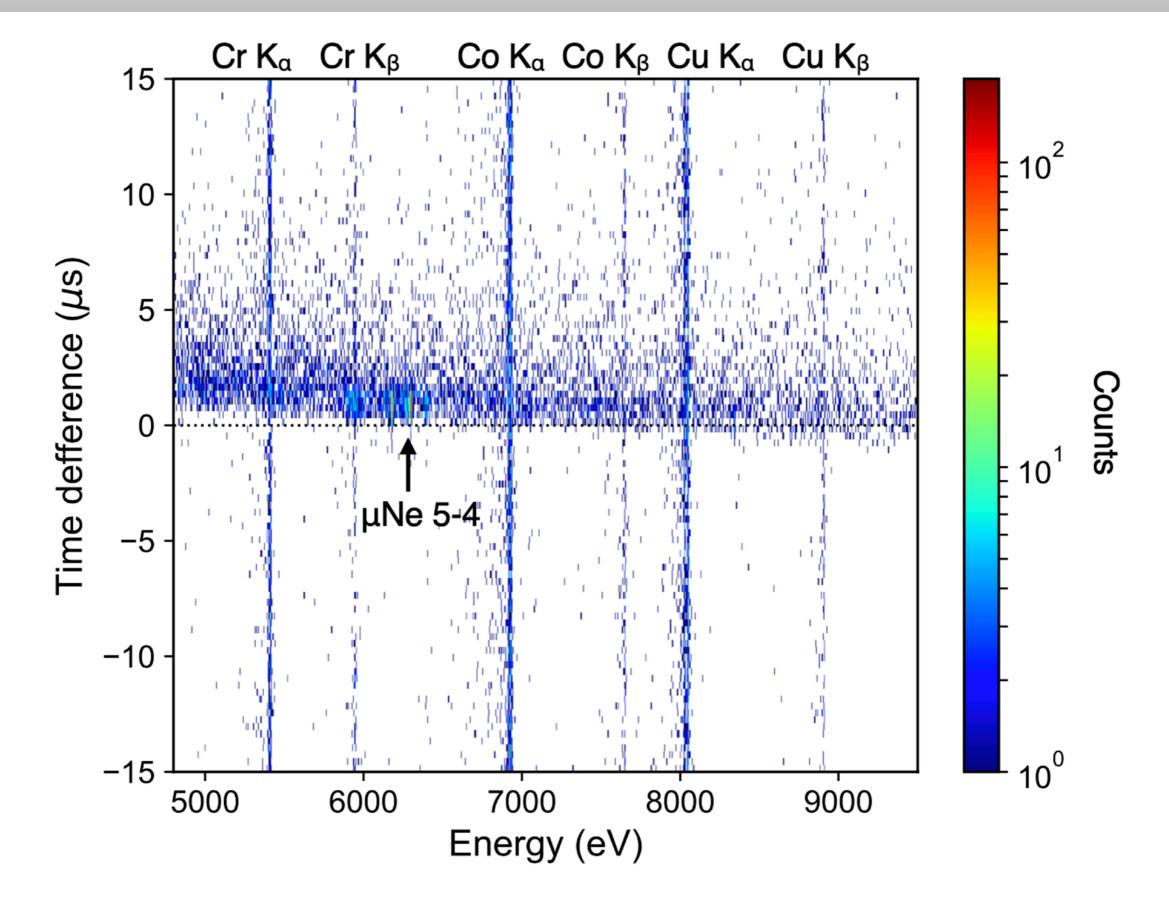


# Energy calibration

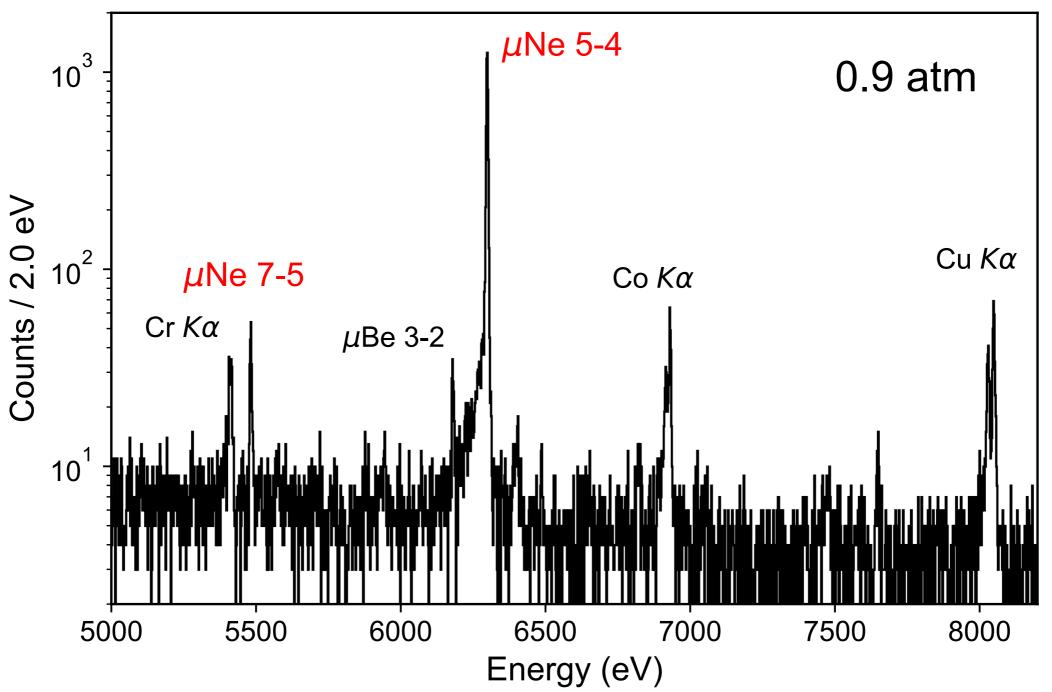
#### Continuous X-ray irradiation during experiment



# Energy vs. Timing (muon arrival time)

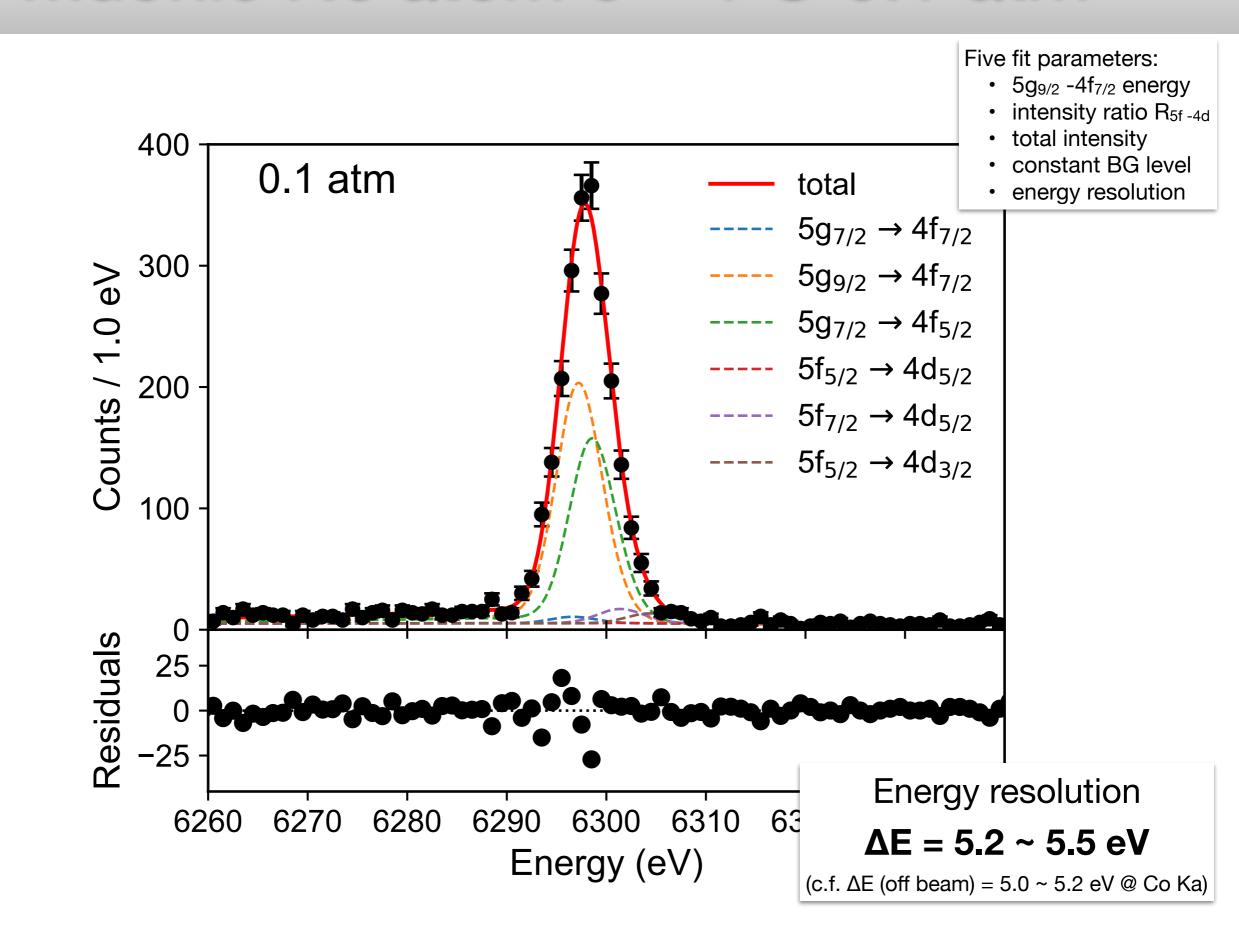


# Muonic-atom X-ray spectrum



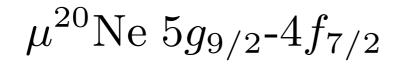
Typical count rates of muonic X-rays: 1-3 cps / TES array (Calibration X-rays: ~ 400 cps / TES array)

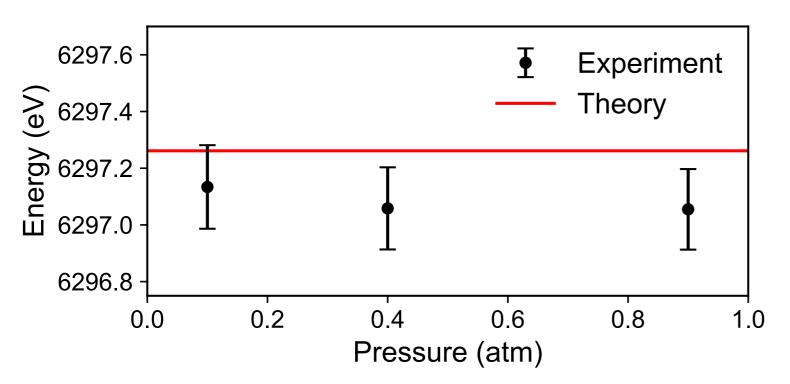
### Muonic Ne atom 5→4 @ 0.1 atm



# Results (pressure dependence)

Stat. error ~ 0.04 eV Syst. error ~ 0.13 eV





#### Breakdown of syst error

- 1. Thermal crosstalk: 0.11 eV
  - → due to crosstalk correction
- 2. Calibration: 0.07 eV
  - → evaluated by Fe Ka (as ref. line)
- 3. Low energy tail: 0.01 eV
  - → response w/ & w/o beam

#### BSQED calculation (MCD-FGME code) includes :

- first- and second-order QED corrections
- the full Breit interaction
- all-order retardation effects
- the FNS contributions

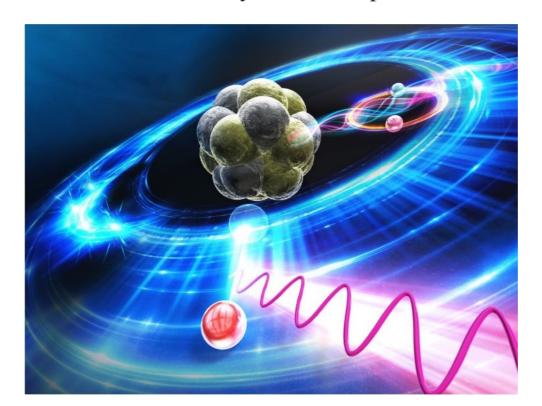
# Published: PRL (2023)

#### PHYSICAL REVIEW LETTERS 130, 173001 (2023)

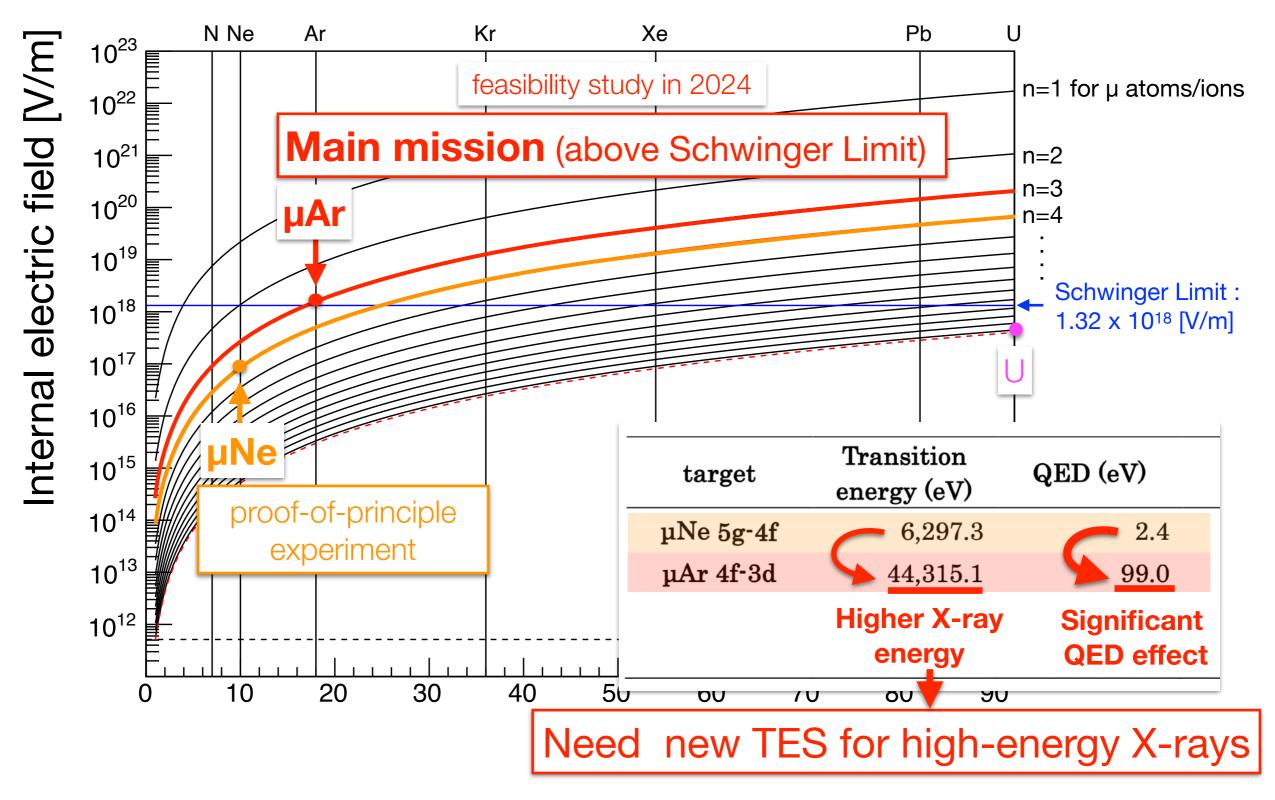
## Proof-of-Principle Experiment for Testing Strong-Field Quantum Electrodynamics with Exotic Atoms: High Precision X-Ray Spectroscopy of Muonic Neon

```
T. Okumura, T. Azuma, T. Hashimoto, R. Hayakawa, G. C. Hilton, Y. Ichinohe, P. Indelicato, T. Isobe, S. Kanda, M. Katsuragawa, N. Kawamura, Y. Kino, K. Kino, K. Mine, Y. Miyake, K. M. Morgan, T. Isobe, S. Kanda, M. Katsuragawa, N. Kawamura, K. Okutsu, N. Paul, T. C. D. Reintsema, D. R. Schmidt, K. Shimomura, P. Strasser, H. Suda, D. S. Swetz, T. Takahashi, S. Takeda, S. Takeshita, M. Tampo, H. Tatsuno, Y. Ueno, J. N. Ullom, S. Watanabe, and S. Yamada, Yamada
```

(Received 8 December 2021; revised 10 February 2023; accepted 10 March 2023; published 27 April 2023)



## What's Next?



→ The feasibility study has been completed in this February.

observing a broad structure (being complex of many X-ray lines)

# 2. Muonic molecule (µCF)

# Collaboration (µdd\*)

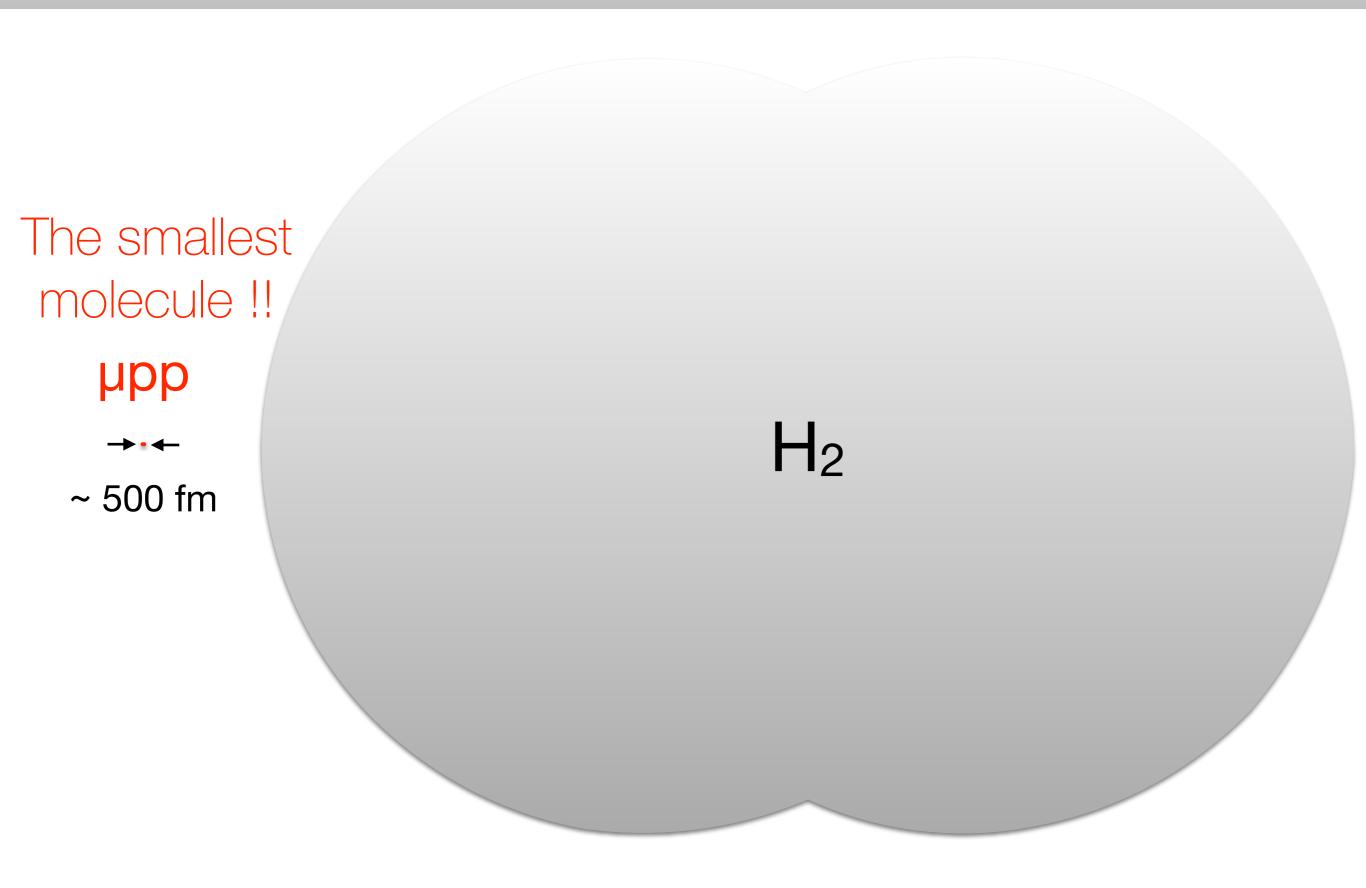
#### J-PARC MLF 2019MS01 collaboration (for µdd\*)

Shinji Okada	Chubu Univ.	
Yuichi Toyama	Chubu Univ.	
Tadayuki Takahashi	IPMU	
Tadashi Hashimoto	JAEA	
Shin Watanabe	JAXA	
Sohtaro Kanda		Japan
Naritoshi Kawamura	KEK	
Yasuhiro Miyake		
Hiroaki Natori		
Kouichiro Shimomura		
Patrick Strasser		
Motonobu Tampo		
Izumi Umegaki		
Hirofumi Noda	Osaka Univ.	
Toshiyuki Azuma	RIKEN	
Katsuhiko Ishida	RINEN	
Ryota Hayakawa		
Yuto Ichinohe	Diklara Univ	
Toshiki Sato	Rikkyo Univ.	
Shinya Yamada		

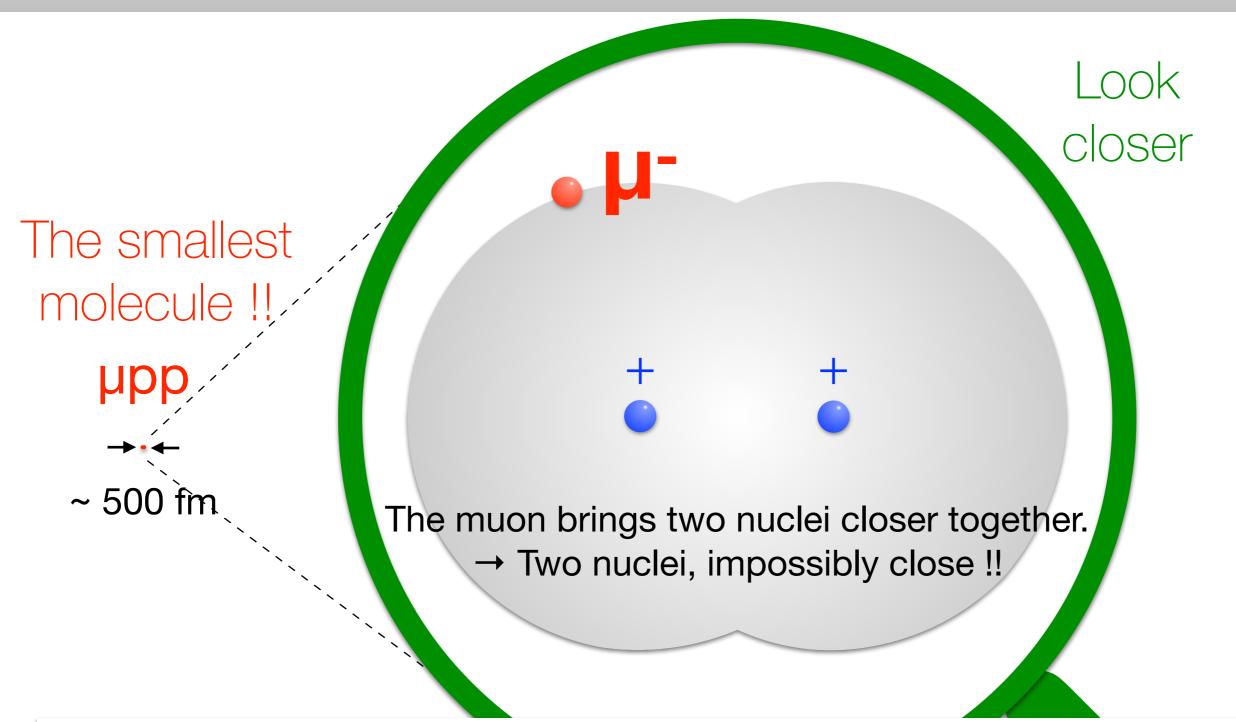
Yasushi		Kino			
Ren		Konishi		Japan	
Ryota		Nakashima	Tohoku Univ.		
Kenichi		Okutsu	ionoku Univ.		
Kyosuke		Sasaki			
Takuma		Yamashita			
Takuma		Okumura	Tokyo Metropolitan		
Hideyuki		Tatsuno	Univ.		
Douglas	A.	Bennett		US	
William	B.	Doriese			
Malcolm	S.	Durkin			
Joseph	W.	Fowler			
Johnathon	D.	Gard			
Gene	C.	Hilton	NUCT		
Kelsey	M.	Morgan	NIST		
Galen	C.	O'Neil			
Carl	D.	Reintsema			
Dan	R.	Schmidt			
Daniel	S.	Swetz			
Joel	N.	Ullom			

(Nuclear & Hadron + Atomic & Muon + Astro) physicists + TES experts

# Scaled image, again



## Muonic molecule



Compared to the reach of nuclear force (a few fm), it becomes small enough to allow nuclear reactions to occur within the molecule.

## **Fusion**

Thermonuclear fusion

Vigorous collisions in plasma at several hundred million degrees Celsius



Large repulsion due to electromagnetic force

Fusion with muons

Nuclei easily approach each other

+ + +

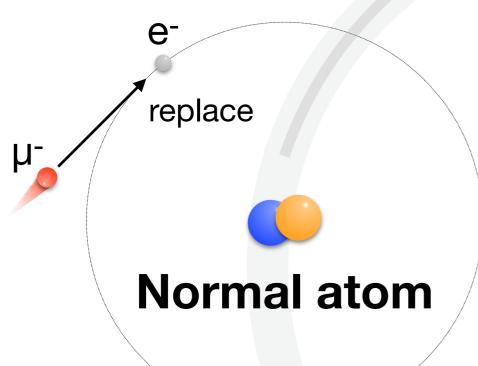
No repulsion by electromagnetic forces up to the size of a muonic molecule

# Muon-Catalyzed Fusion (µCF)

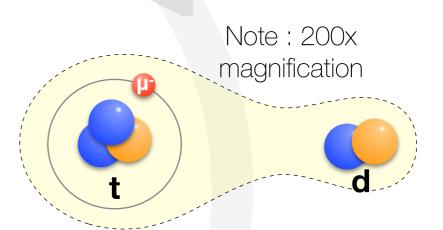
Interestingly, it causes a chain reaction!

Note: 200x magnification

Fusion cycle with muons as "catalysts"



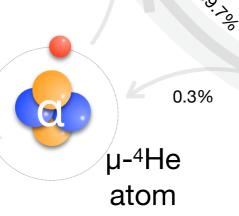
#### **Muonic atom**

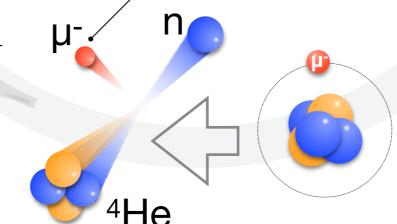


#### Muonic molecule

free muon (re-emitted after nuclear fusion) can re-create muonic atom & molecules.

The phenomenon of some muons going out of cycle is known as "a sticking problem".





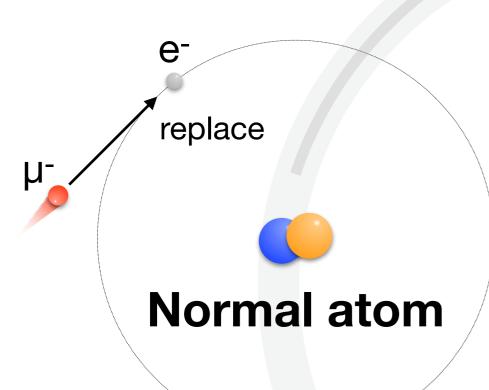
This cycle continues until the muon lifetime (~2 µs) is over.

# Muon-Catalyzed Fusion (µCF)

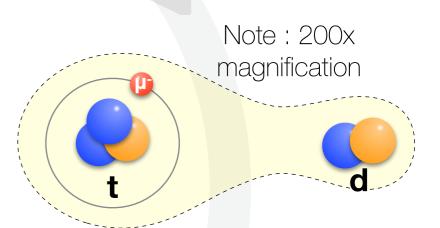
Interestingly, it causes a chain reaction!

Note: 200x magnification

Fusion cycle with muons as "catalysts"



**Muonic atom** 



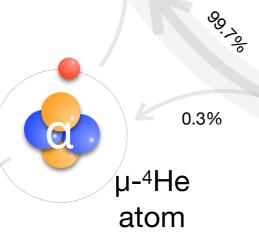
Muonic molecule

free muon (re-emitted after nuclear fusion)

4

No experiment has ever captured "evidence" of muon molecules.

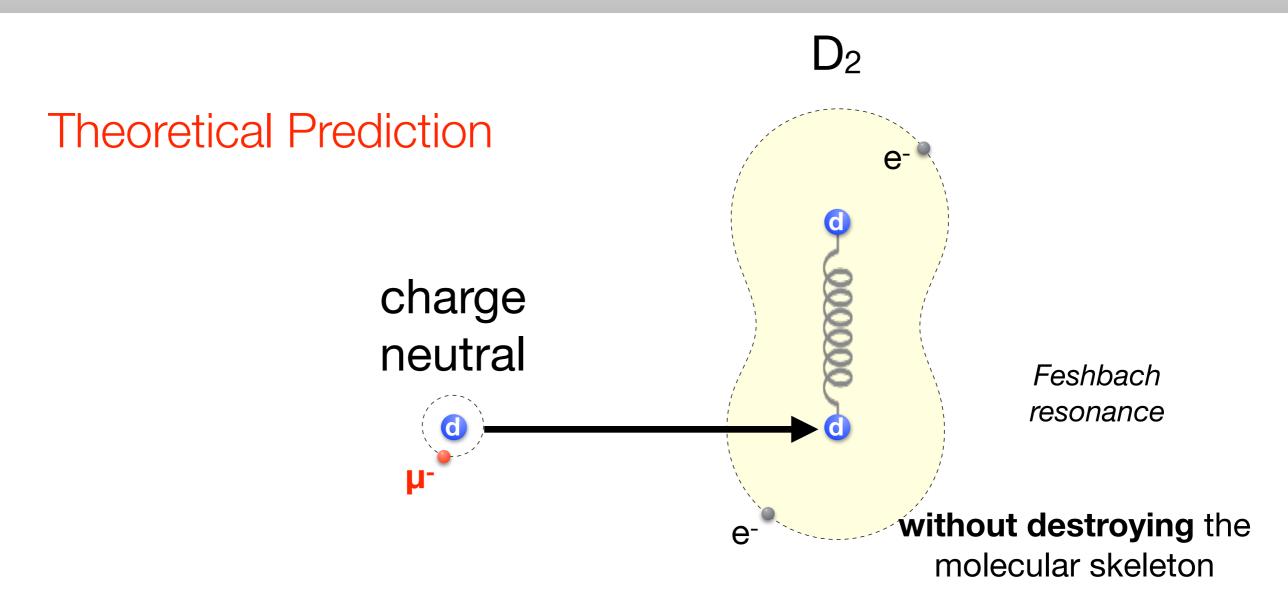
The phenomenon of some muons going out of cycle is known as "a sticking problem".



4He

until the muon lifetime (~2 µs) is over.

# How µ molecules are created?



If the muonic atom collide "gently" to the normal molecule, the excess energy of ddµ molecule formation is passed to the rovibrational excitation energy of D<sub>2</sub> molecule.

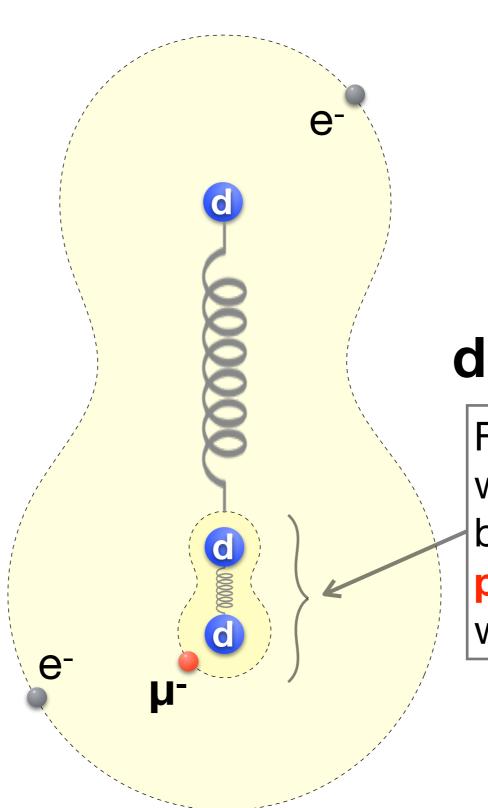
⇒ Resonant generation (Vesman mechanism)

## Molecule in molecule!

Theoretical prediction

Matryoshka-like



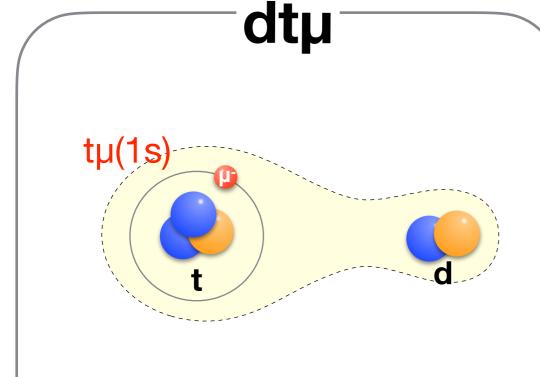


ddµ molecule

Forms a molecule within a molecule by acting as a pseudo-nucleus with charge +1

## Exited state of muonic molecule

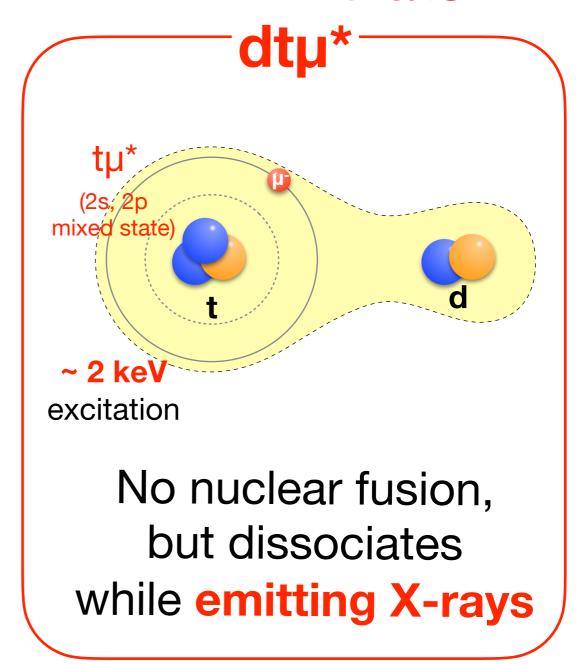
#### Ground state



Immediately leading to nuclear fusion

No chance to measure 1

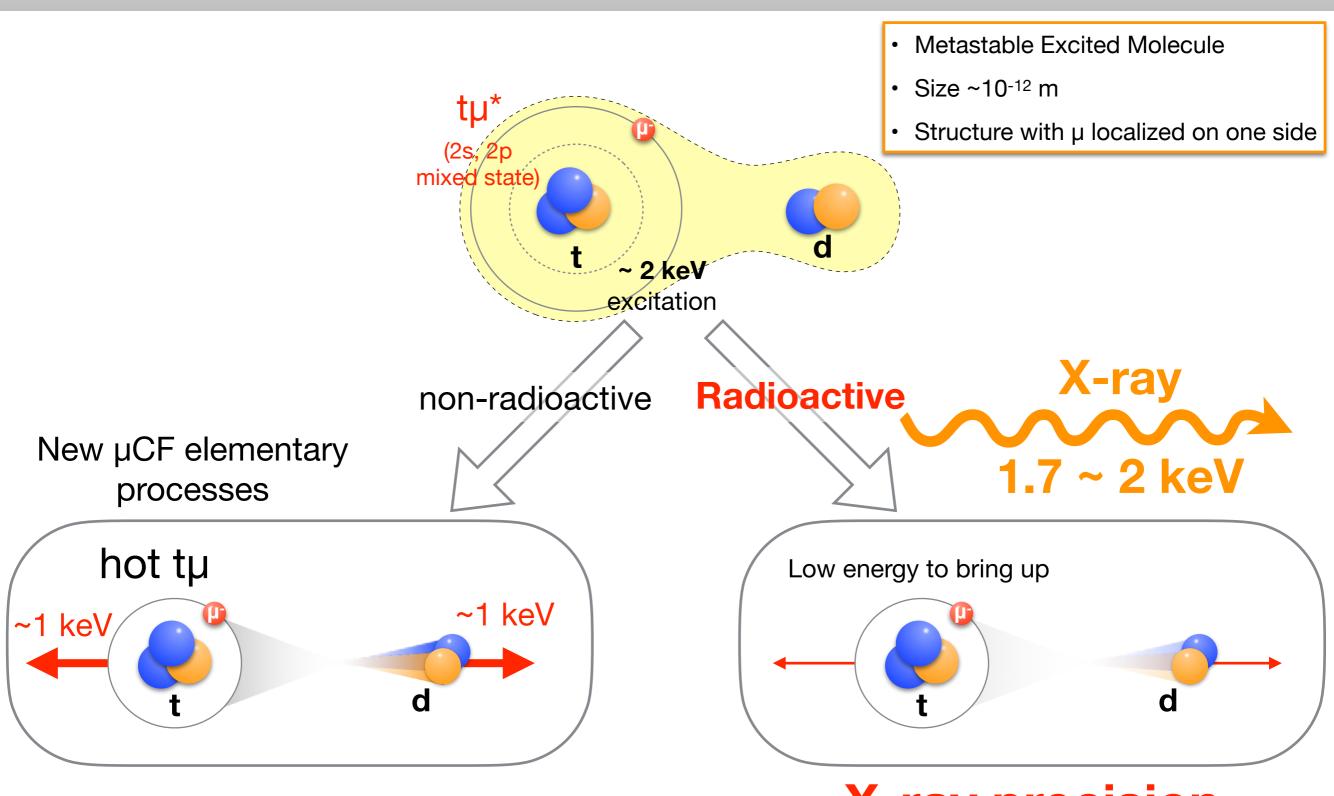
#### **Excited state**



#### Measure this 1

to determine what quantum states are being produced and how.

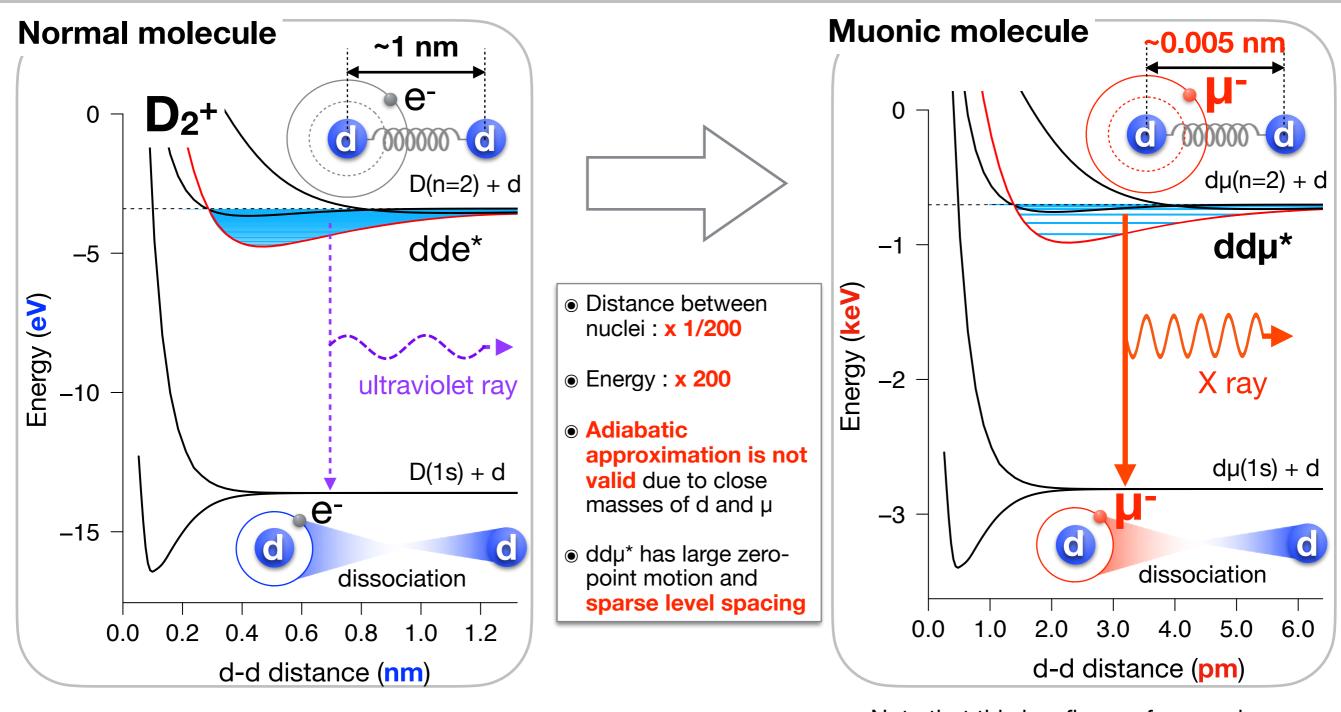
## Dissociation of excited molecules



Inflight µCF study

X-ray precision spectroscopy

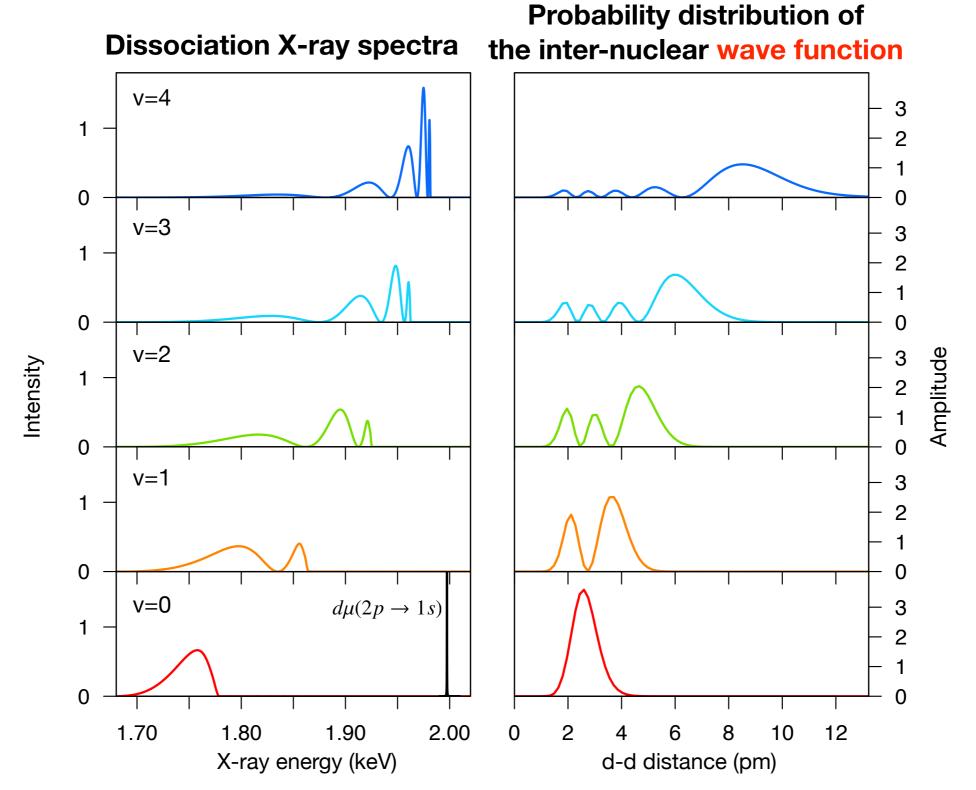
### High Precision Spectroscopy of Muonic Molecules



Note that this is a figure of convenience. (In fact, such adiabatic approximate potentials cannot be fully understood.)

Requires a **few-body calculation** that simultaneously solves for the motion of nuclei and heavy negatively charged particles. → Y. Kino & T. Yamashita

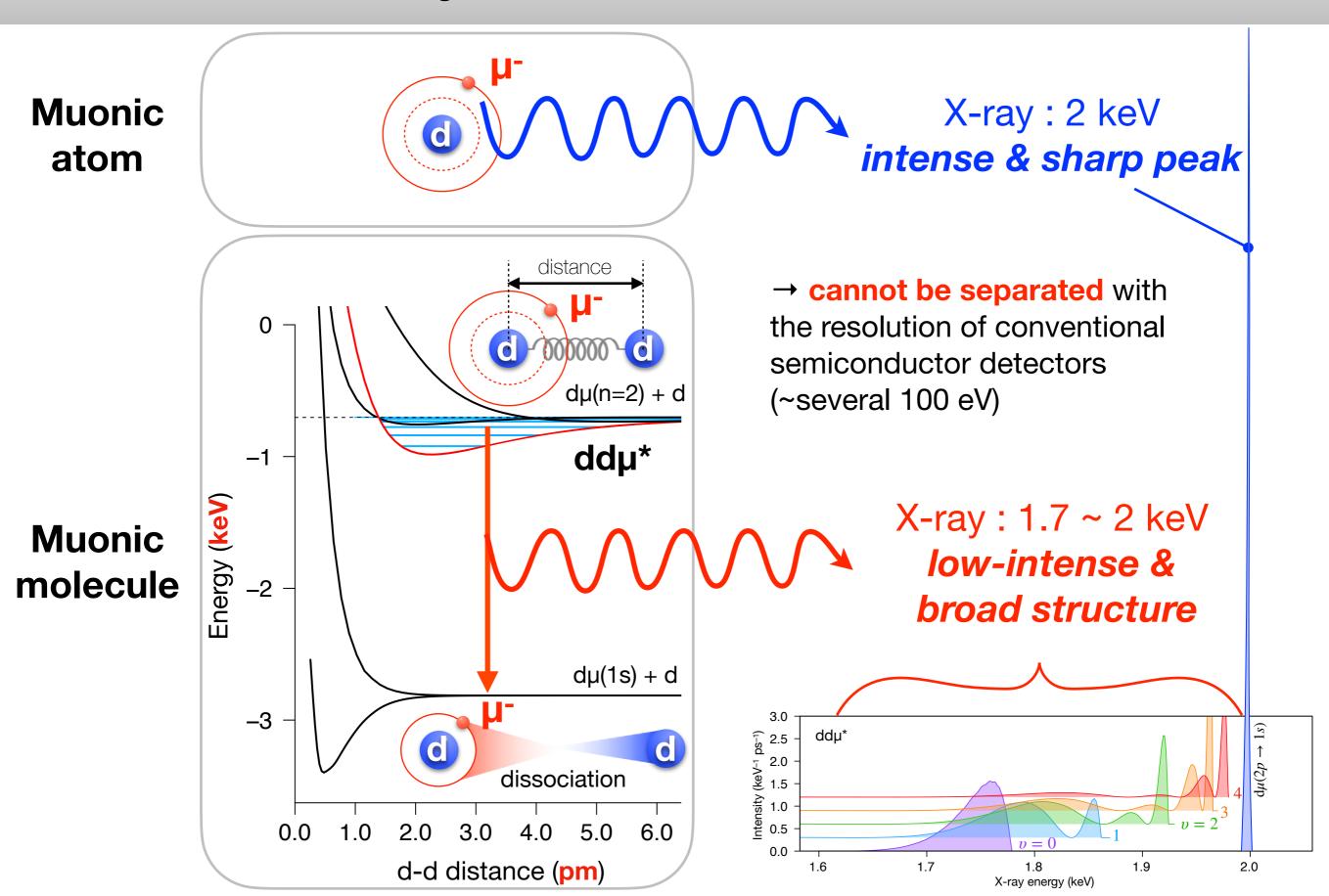
### Radiation dissociation spectra of excited µ molecules



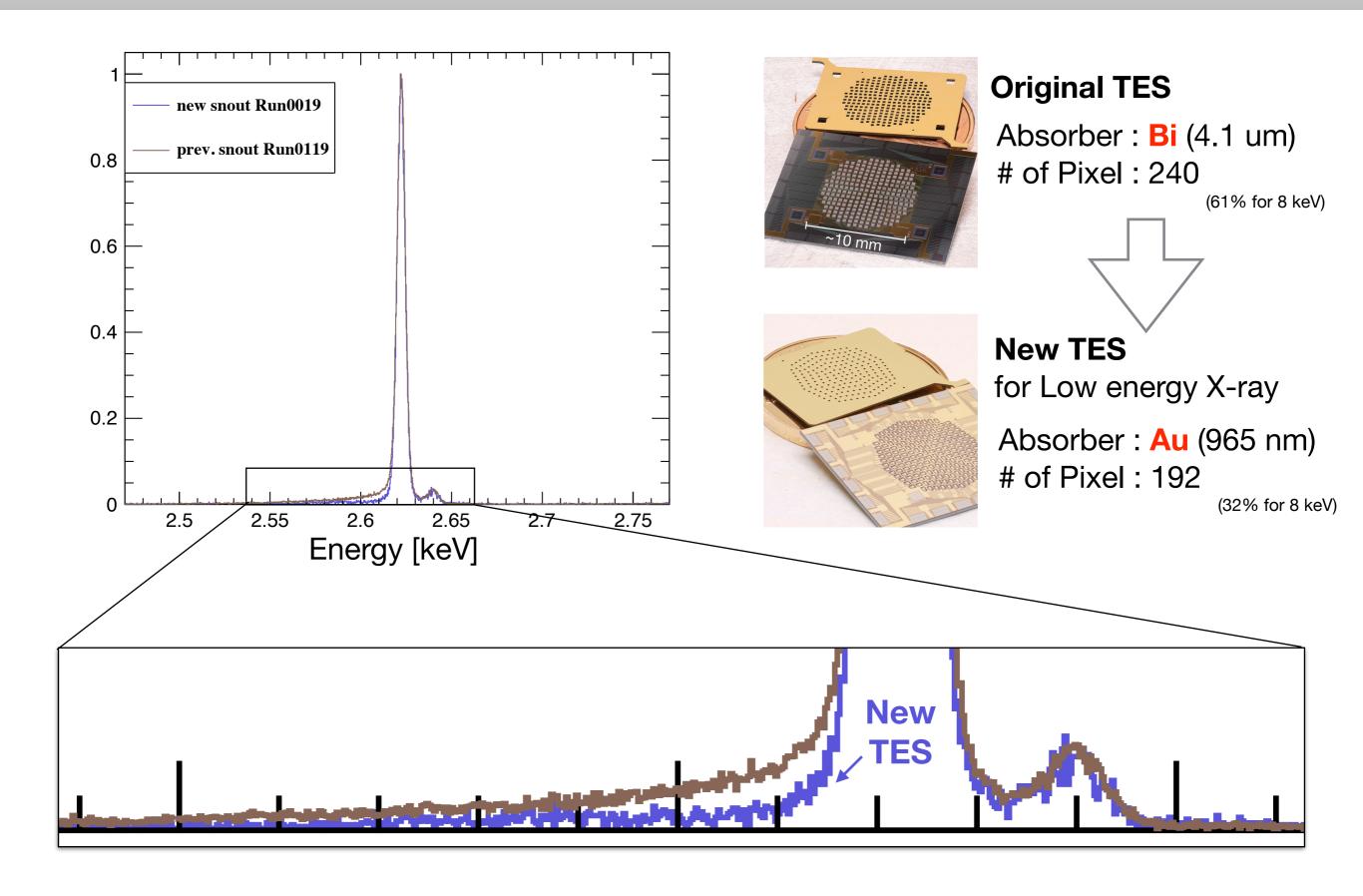
The X-ray energy spectrum is expected to have a very characteristic structure reflecting the shape of the wavefunction!!

山下琢磨: 2020/7/27 領域研究会

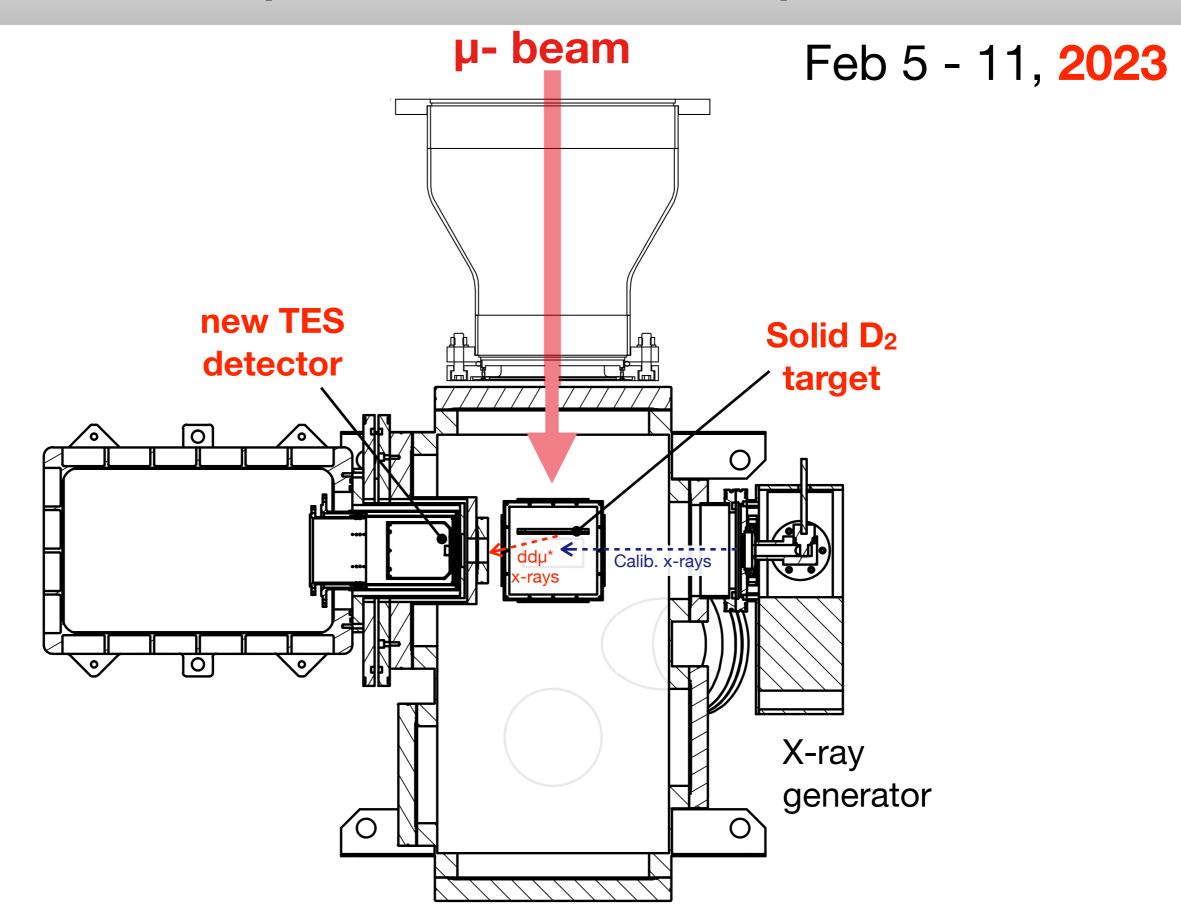
# Difficulty of the measurement



## New TES: Less tail component

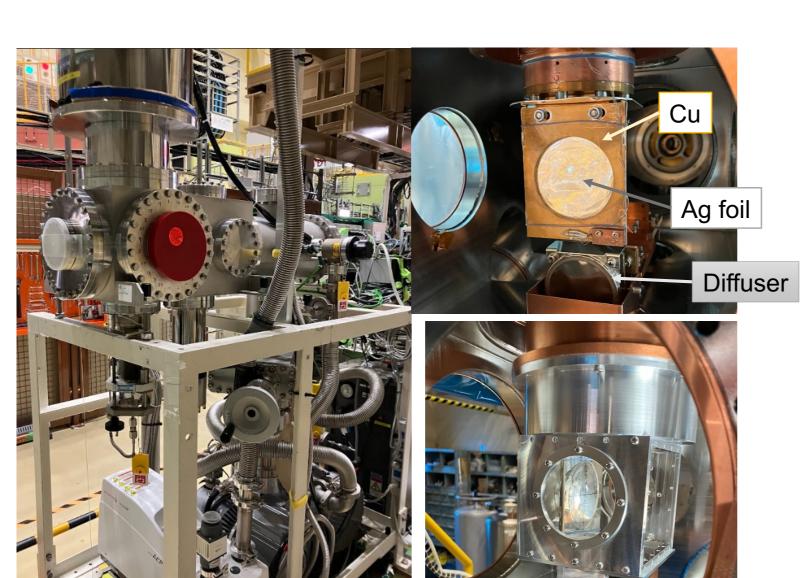


# Experimental setup



# Solid deuterium system

#### P. Strasser et al. NIMA 460, 451 (2001)



Al thermal shield

(before attaching window)

Solid deuterium target system

Base: Ag foil (100 µm)

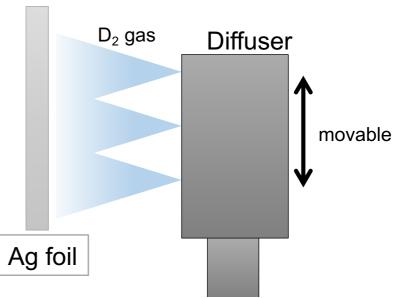
Target size: Ф60

Thickness: 1 mm

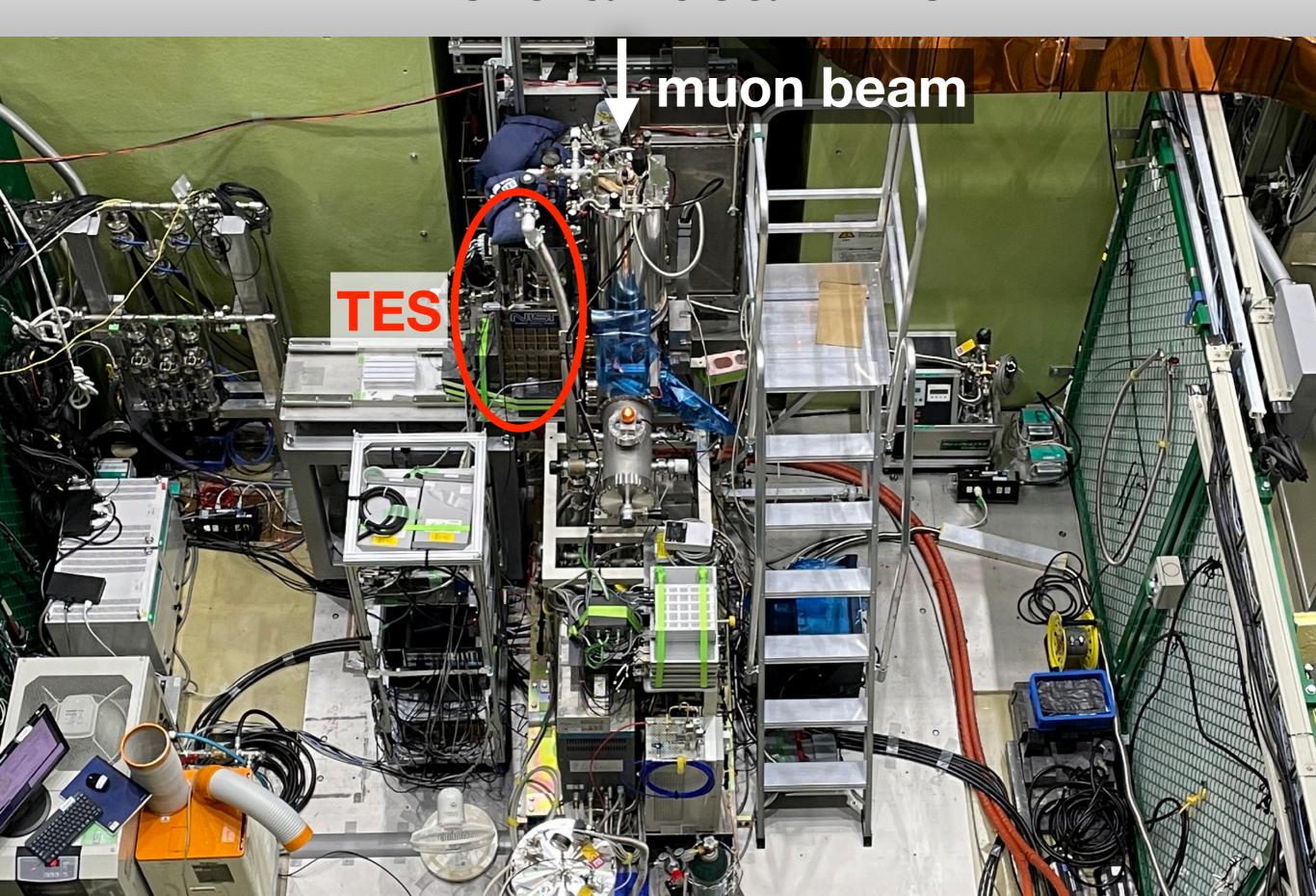
Temperature: ~3 K (Liq. He coolant)

Chamber pressure: 1x10-6 Pa

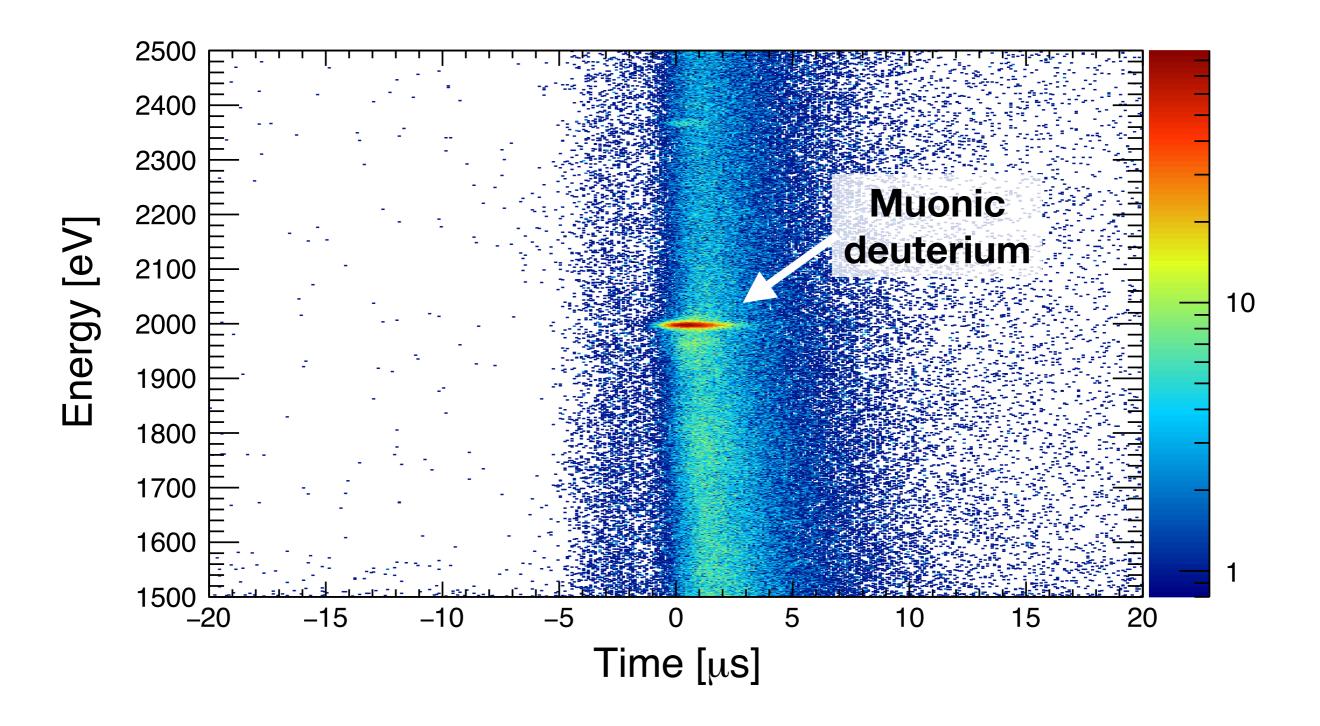
✓ Stable operation during the measurement.



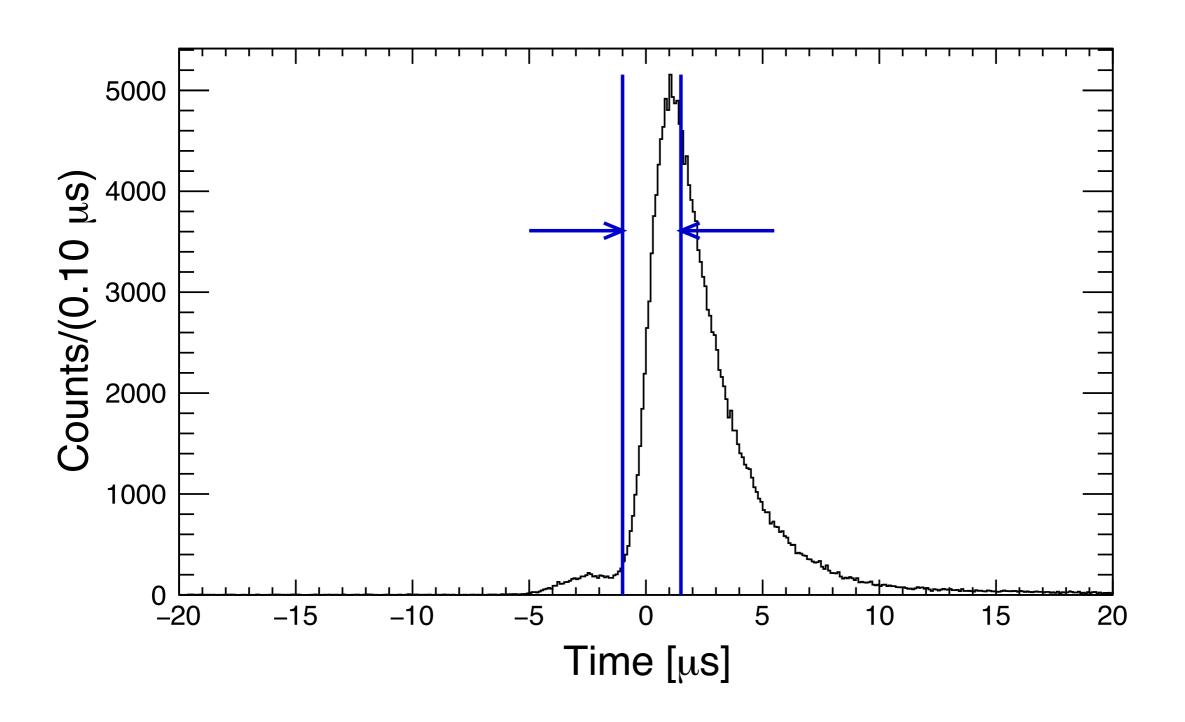
## Photo at beamline



# Energy vs. Time



# Timing cut



# 3. Summary & Outlook

# Summary

- The following advantages of TES have made it possible to conduct accelerator experiments that were not possible before
  - 1. Combination of energy resolution and detection efficiency (multi-pixel)

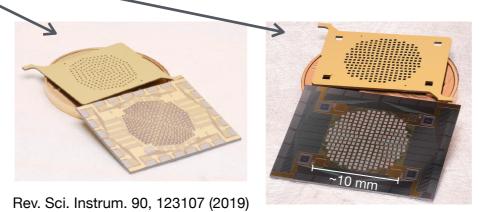
    Muonic atoms
    - → High-precision absolute energy measurement for rare events
  - 2. Covering a wide energy range with high resolution Muonic molecule
    - → Interesting broad structures are now visible in detail. This was not possible with the crystal spectrometer.

# Developed TES for high-energy X-rays

Name	5 keV TES	10 keV TES	50 keV TES	100 keV TES
Saturation energy	10 keV	20 keV	70 keV	150 keV
Readout system	TDM	TDM	microwave	microwave
Absorber thickness (material)	0.965 µm (Au)	4.1 μm (Bi)	1.85 μm (Au) & 20 μm (Bi)	0.5 mm (Sn)
Absorber area	0.34 x 0.34 mm <sup>2</sup>	0.320 x 0.305 mm <sup>2</sup>	0.73 x 0.73 mm <sup>2</sup>	1.3 x 1.3 mm <sup>2</sup>
Absorber collimated area	0.28 x 0.28 mm <sup>2</sup>	0.305 x 0.290 mm <sup>2</sup>	0.67 x 0.67 mm <sup>2</sup>	(no collimator)
Number of pixel	192	240	96	96
Total collection area	15.1 mm <sup>2</sup>	21.2 mm <sup>2</sup>	43.1 mm <sup>2</sup>	162 mm²
ΔE (FWHM)	5 eV @ 6 keV	5 eV @ 6 keV	20 eV @ 40 keV ( 8 eV @ 17 keV )	60~70 eV @ 130 keV

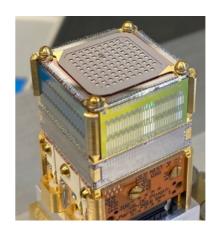
#### **Existing TES**

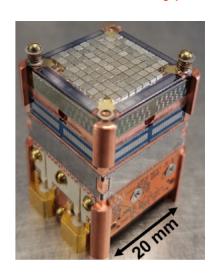
(have been using since 2016)



#### **Brand-new TES detector**

(brought from NIST this January)





## Outlook

A new proposal application (muon S1 type) are being submitted for various experiments using this new TES system, very recently.

Next generation X-ray detector

covering a wide energy range

10 keV

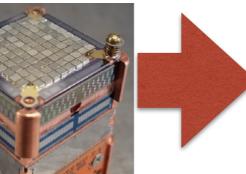
50 keV

100 keV









J-PARC High-intensity μ- source



From basic physics study to applications in non-destructive elemental analysis

- ✓ QED verification under strong electric field
- ✓ Metastable muonic molecules (related to µCF study)
- √ Nuclear radius
- ✓ Non-destructive analysis

Thank you for your attention.