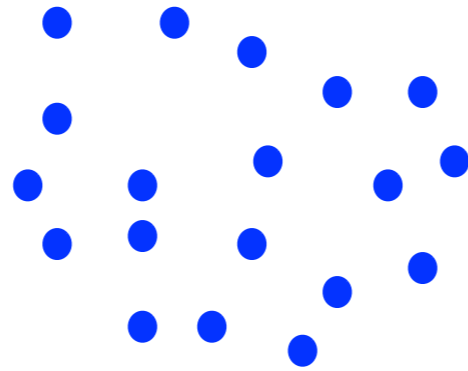


# Towards a holographic description of hydro with spin

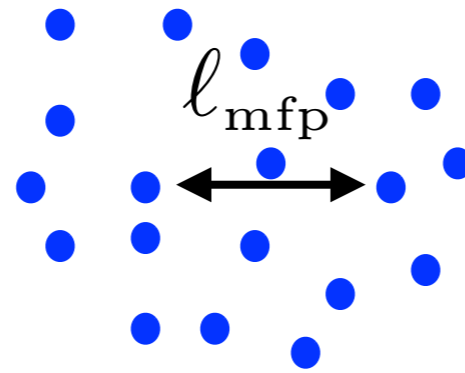
A. Yarom

Together with C. Cartwright, A. D. Gallegos, U. Gursoy and R. Klein

# Simple hydrodynamics

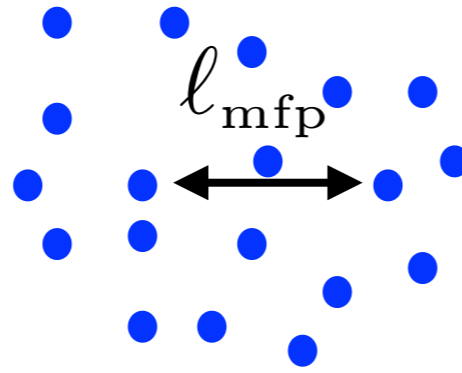


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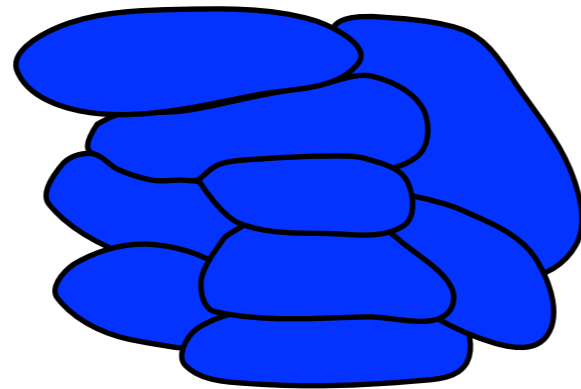


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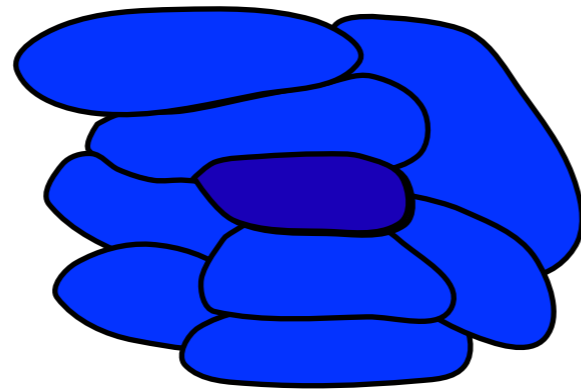
$$L \gg \ell_{\text{mfp}}$$



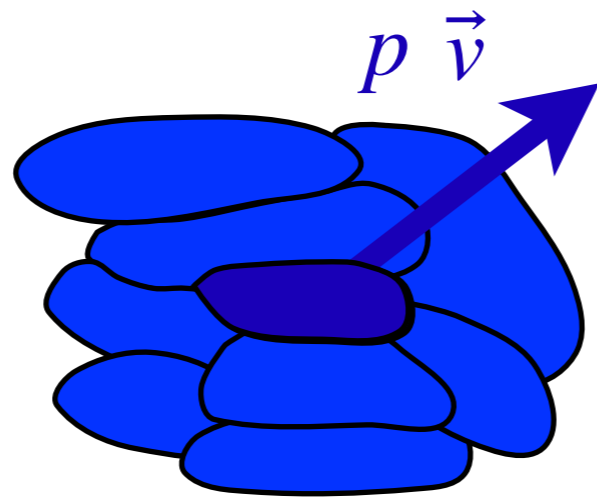
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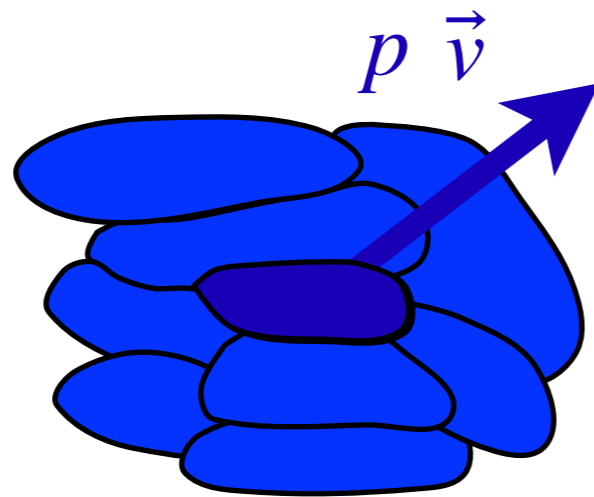
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# Simple hydrodynamics

$$\dot{\vec{v}} + \vec{v} \cdot \vec{\nabla} \vec{v} = - \vec{\nabla} p + \eta \nabla^2 \vec{v}$$

$$\vec{\nabla} \cdot \vec{v} = 0$$

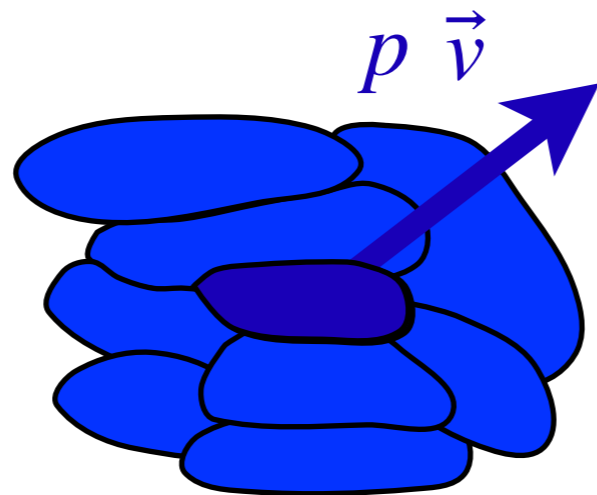




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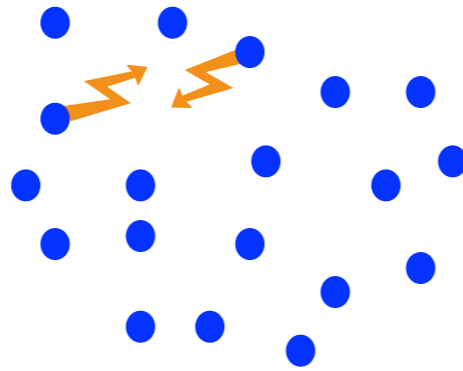
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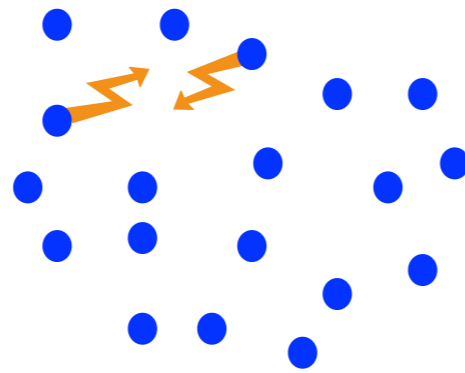
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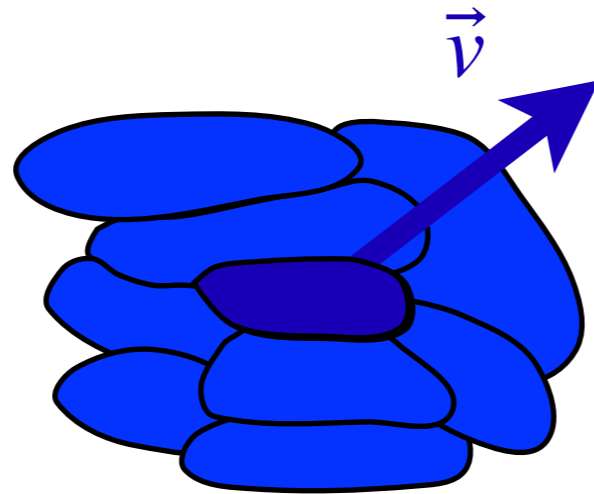


	Viscosity (mPa s)
Water	1
Whole milk	2
Olive oil	56
Pitch	$10^{11}$

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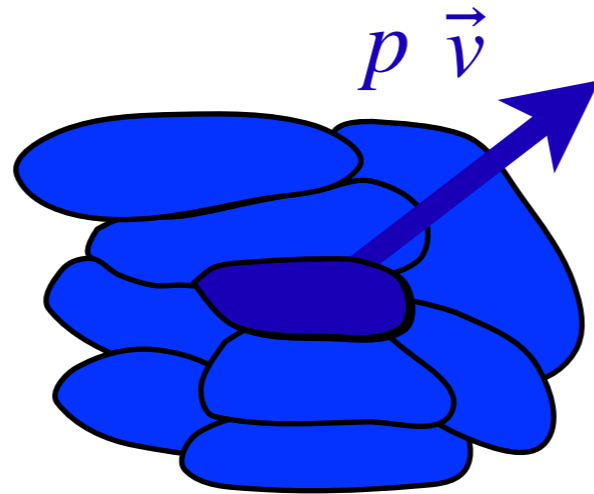
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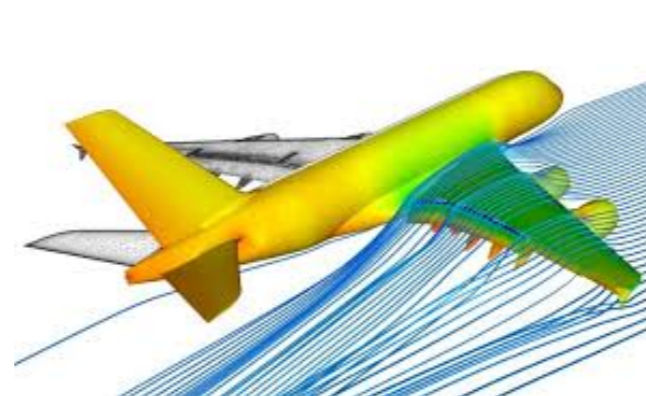
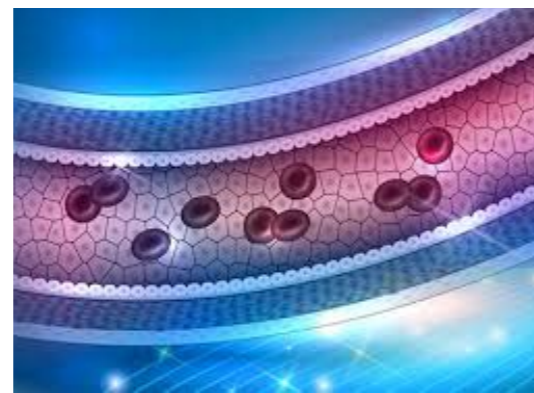


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It works!

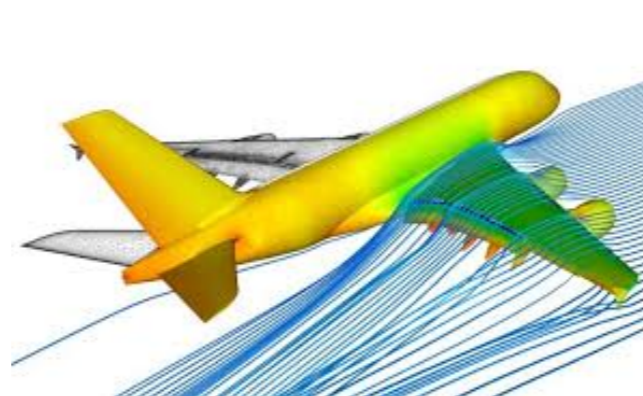
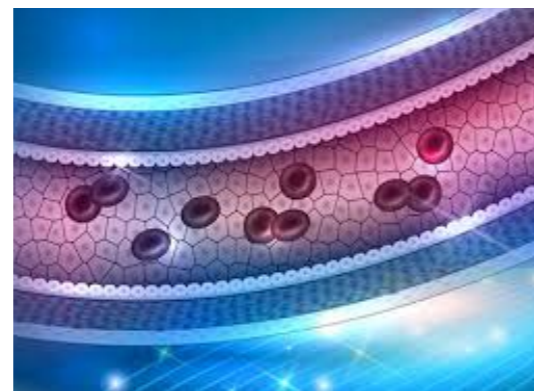


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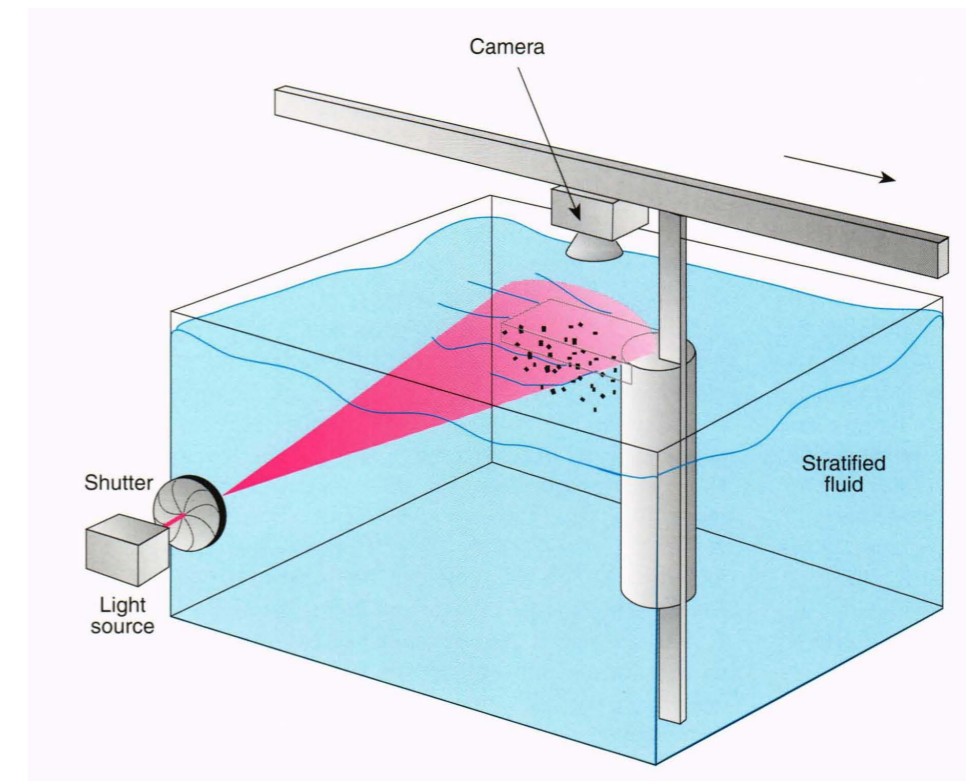
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It works!



Can be verified!



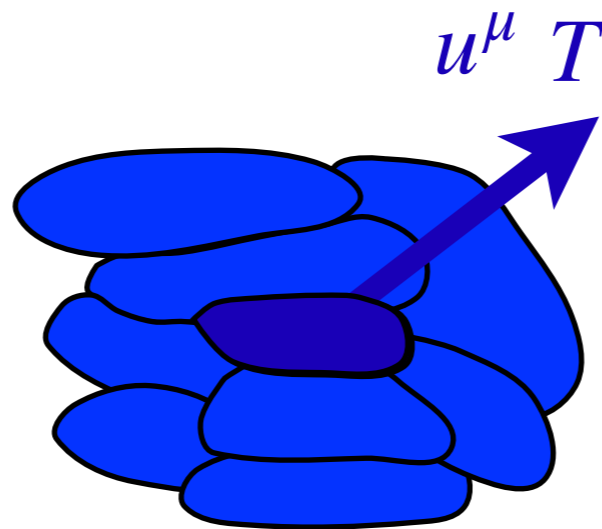
(S. Diamond, 1994)

# Relativistic hydrodynamics

$$\nabla_{\mu} T^{\mu\nu} = 0$$

where

$$T^{\mu\nu} = \epsilon(T)u^{\mu}u^{\nu} + P(T)(\eta^{\mu\nu} + u^{\mu}u^{\nu}) - 2\eta(T)\sigma_{\mu\nu} + \dots$$



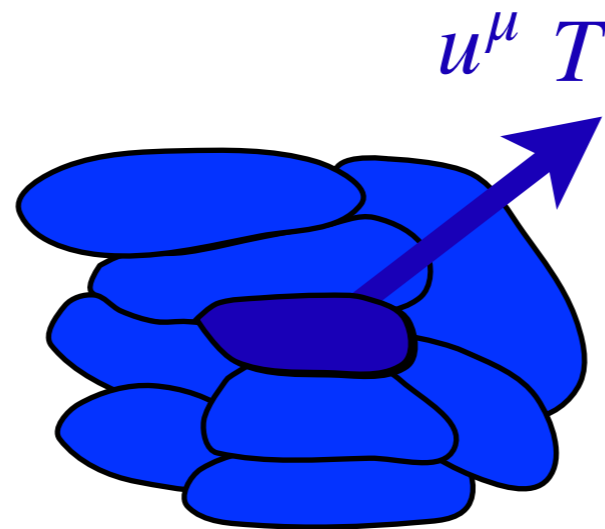


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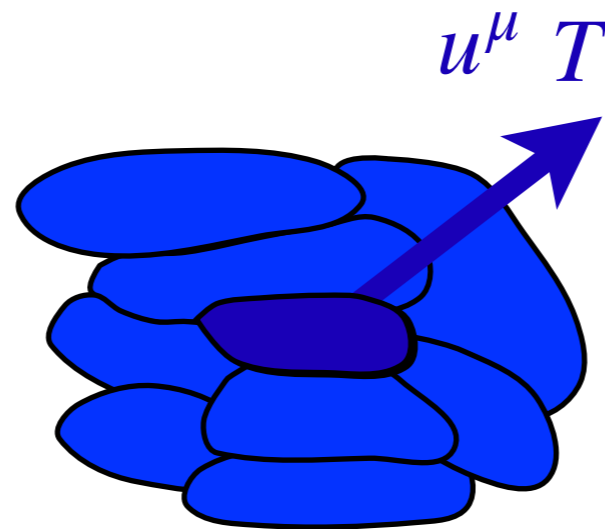


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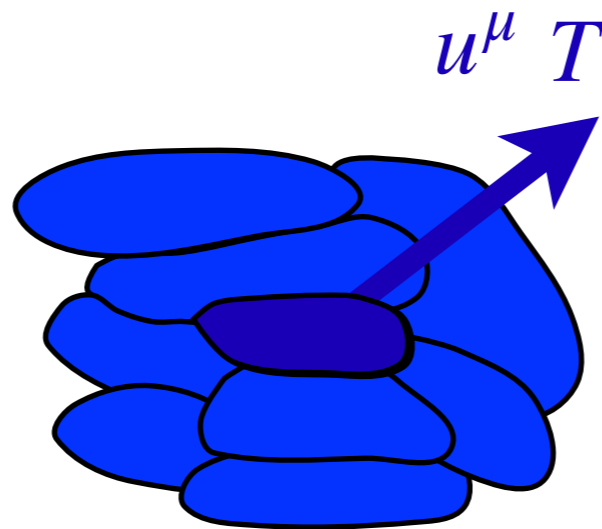


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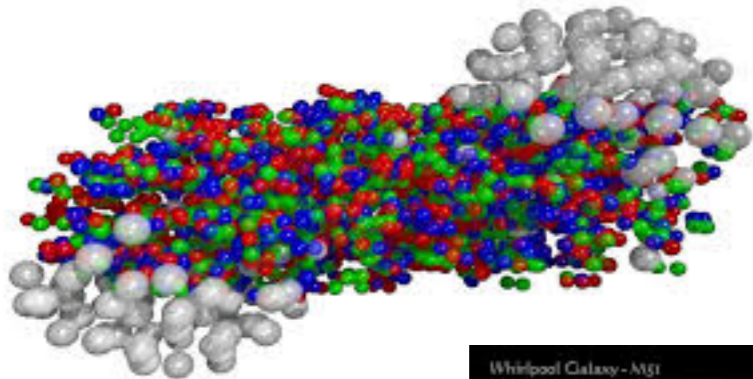
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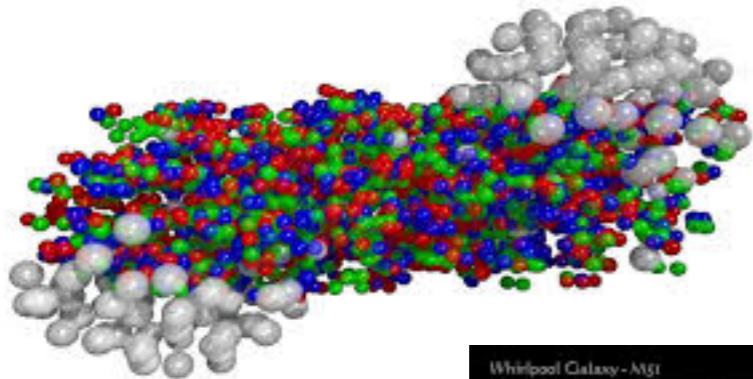
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It works.



Can be verified.



?

# Holographic hydrodynamics

$$\mathcal{L} = \text{tr} \left( \frac{1}{2g} F_{\mu\nu} F^{\mu\nu} + \sum_{I=1}^6 D_{\mu} X^I D^{\mu} X^I + i \sum_{A=1}^4 \bar{\psi}^A \bar{\sigma} D_{\mu} \psi_A + \frac{g^2}{2} \sum_{I,J} [X^I, X^J][X^I, X^J] + \text{Yukawa interactions} \right)$$

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$$X^1 = \begin{pmatrix} \phi_{11}^1 & \phi_{12}^1 & \cdots \\ \vdots & \vdots & \vdots \end{pmatrix}$$



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⋮  
⋮  
⋮

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⋮  
⋮  
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# Holographic hydrodynamics

$\sim \phi^4$

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$\sim \phi \bar{\psi} \psi$

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$\vdots$   
 $\vdots$   
 $\vdots$

$\vdots$   
 $\vdots$   
 $\vdots$

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$$\epsilon = \frac{3\pi^2 N^2}{8} T^4$$

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# AdS/CFT

$$ds^2 = g_{mn} dx^m dx^n$$



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$$ds^2 = g_{mn} dx^m dx^n$$

Solve

$$R_{mn} - \frac{1}{2} g_{mn} R + \Lambda g_{mn} = \dots$$

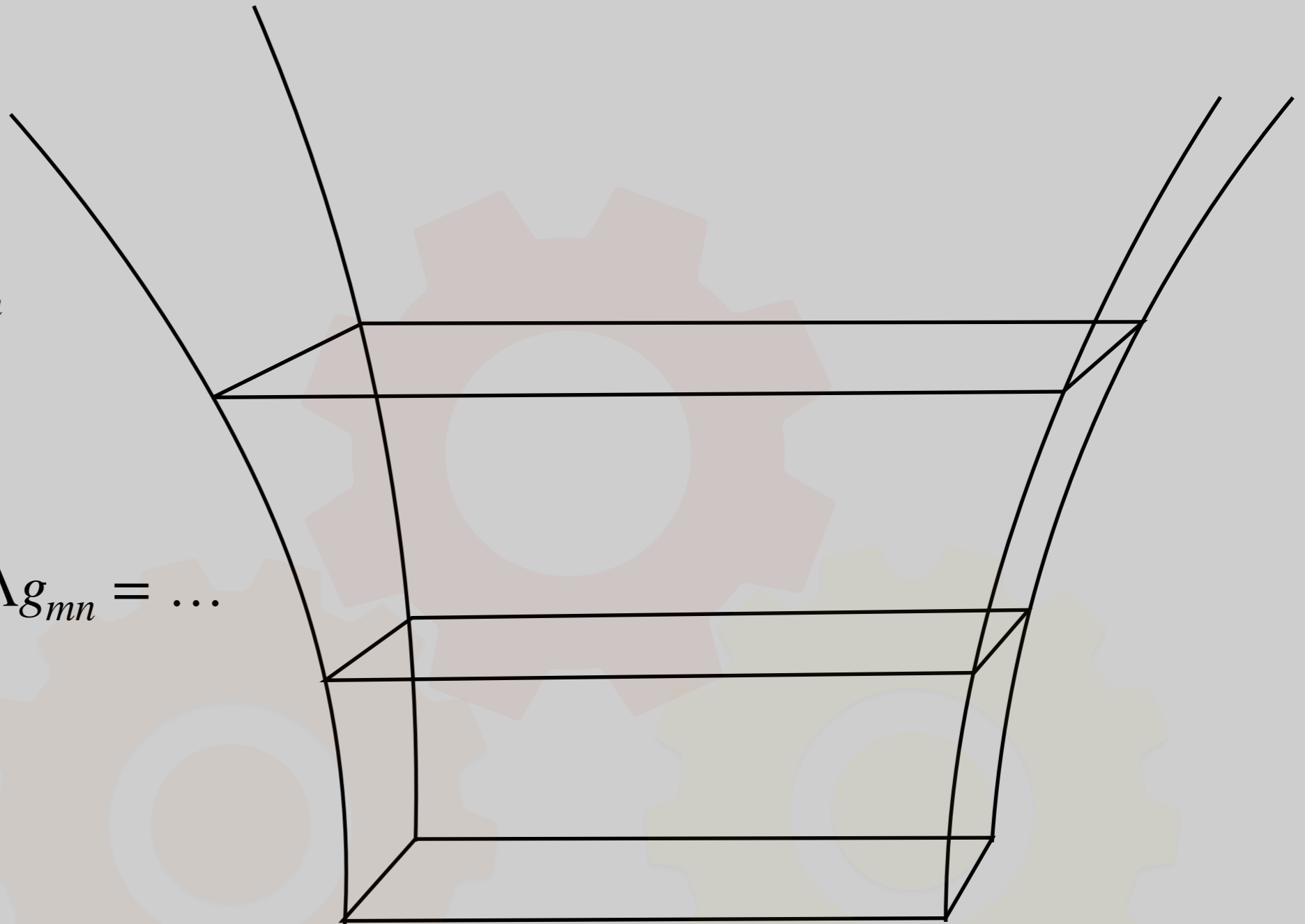


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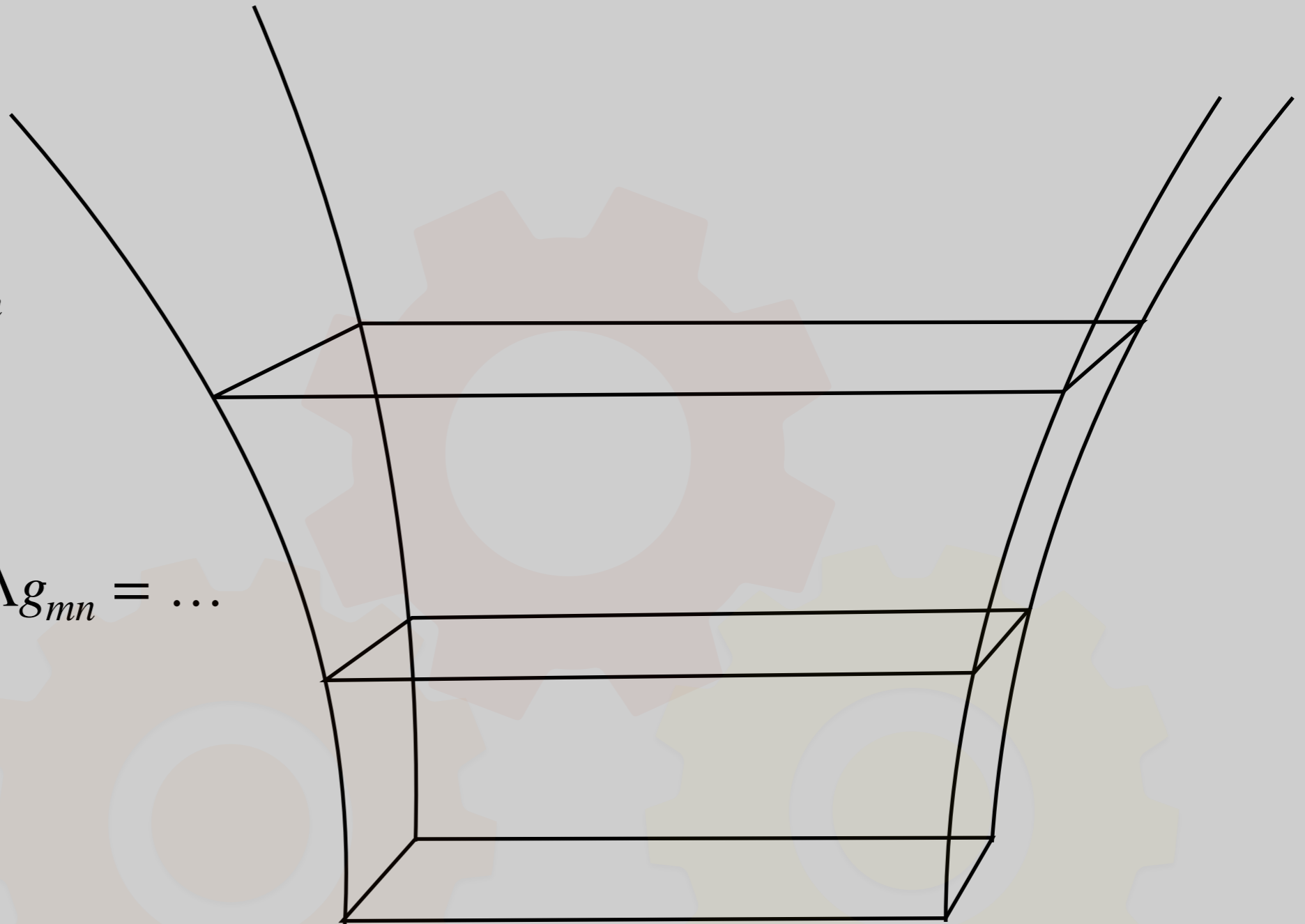
$$ds^2 = g_{mn} dx^m dx^n$$

Solve

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Evaluate

$$\lim g^{mn} \sim \langle T^{\mu\nu} \rangle$$





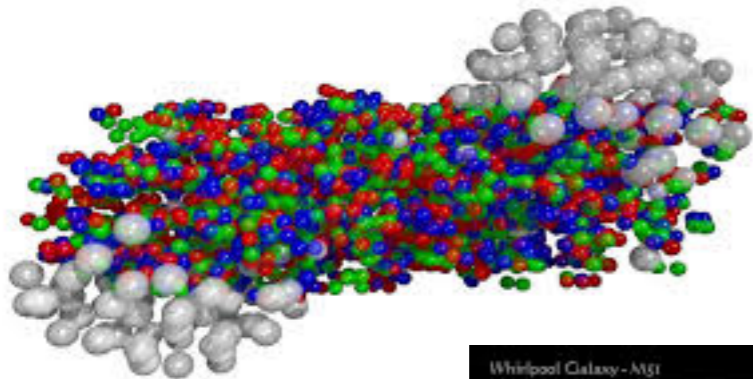
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It works.



Can be verified.



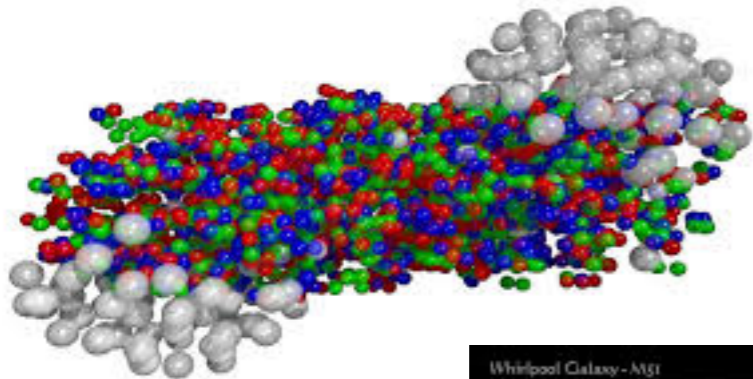
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Can be verified(?)

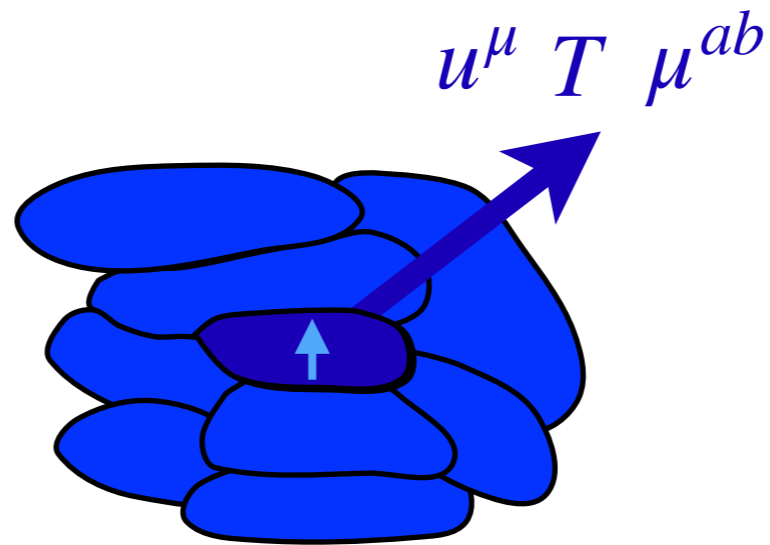


# Spin hydrodynamics

$$\nabla_{\mu} T^{\mu\nu} = 0 \quad \nabla_{\mu} J^{\mu\nu\rho} = 0$$

$$J^{\mu\nu\rho} = x^{\nu} T^{\mu\rho} - x^{\rho} T^{\mu\nu} + S^{\mu\nu\rho}$$

$$S^{\mu\nu\rho} = S^{\mu\nu\rho}[u, T, \mu^{\alpha\beta}] \quad T^{\mu\nu} = T^{\mu\nu}[u, T, \mu^{\alpha\beta}]$$



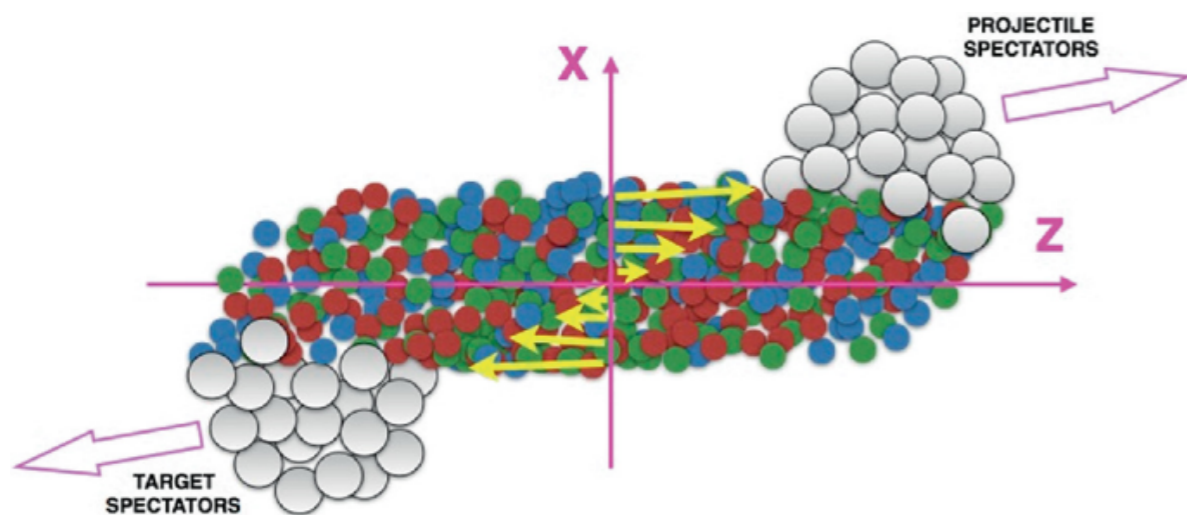
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# Spin hydrodynamics

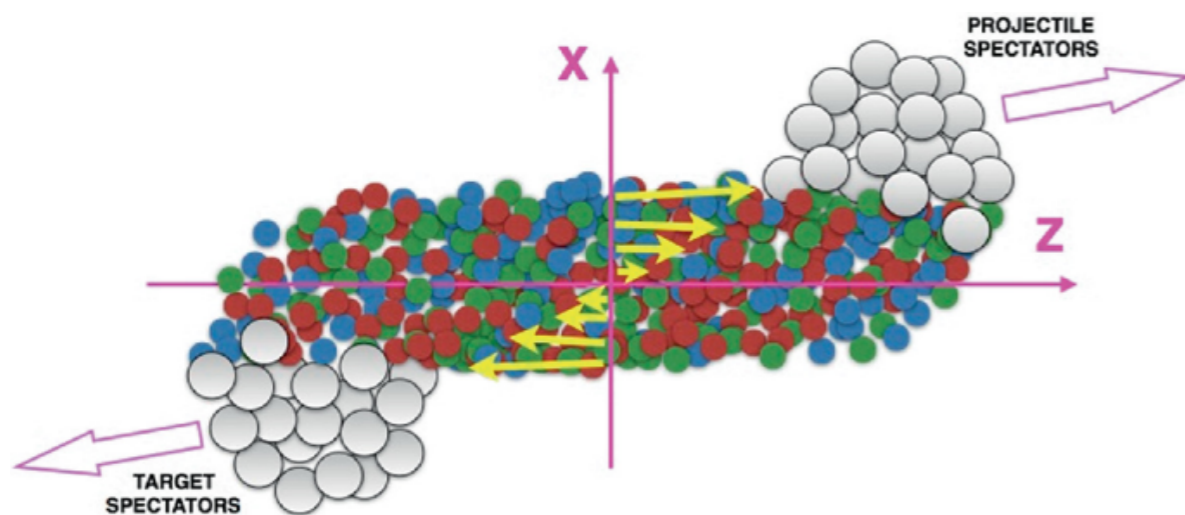
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It works?

Can be verified?



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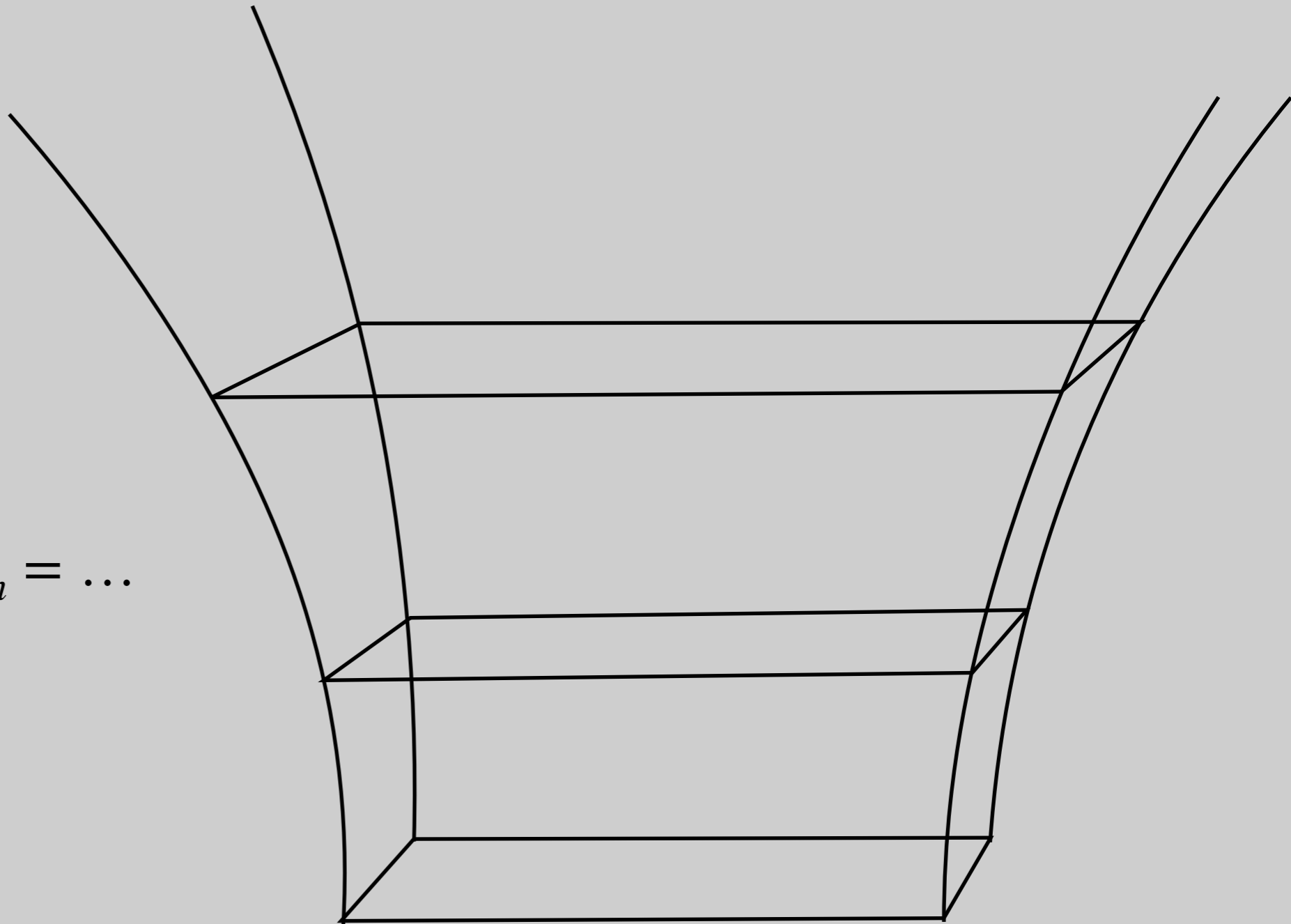
$$ds^2 = g_{mn} dx^m dx^n$$

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$$R_{mn} - \frac{1}{2} g_{mn} R + \Lambda g_{mn} = \dots$$

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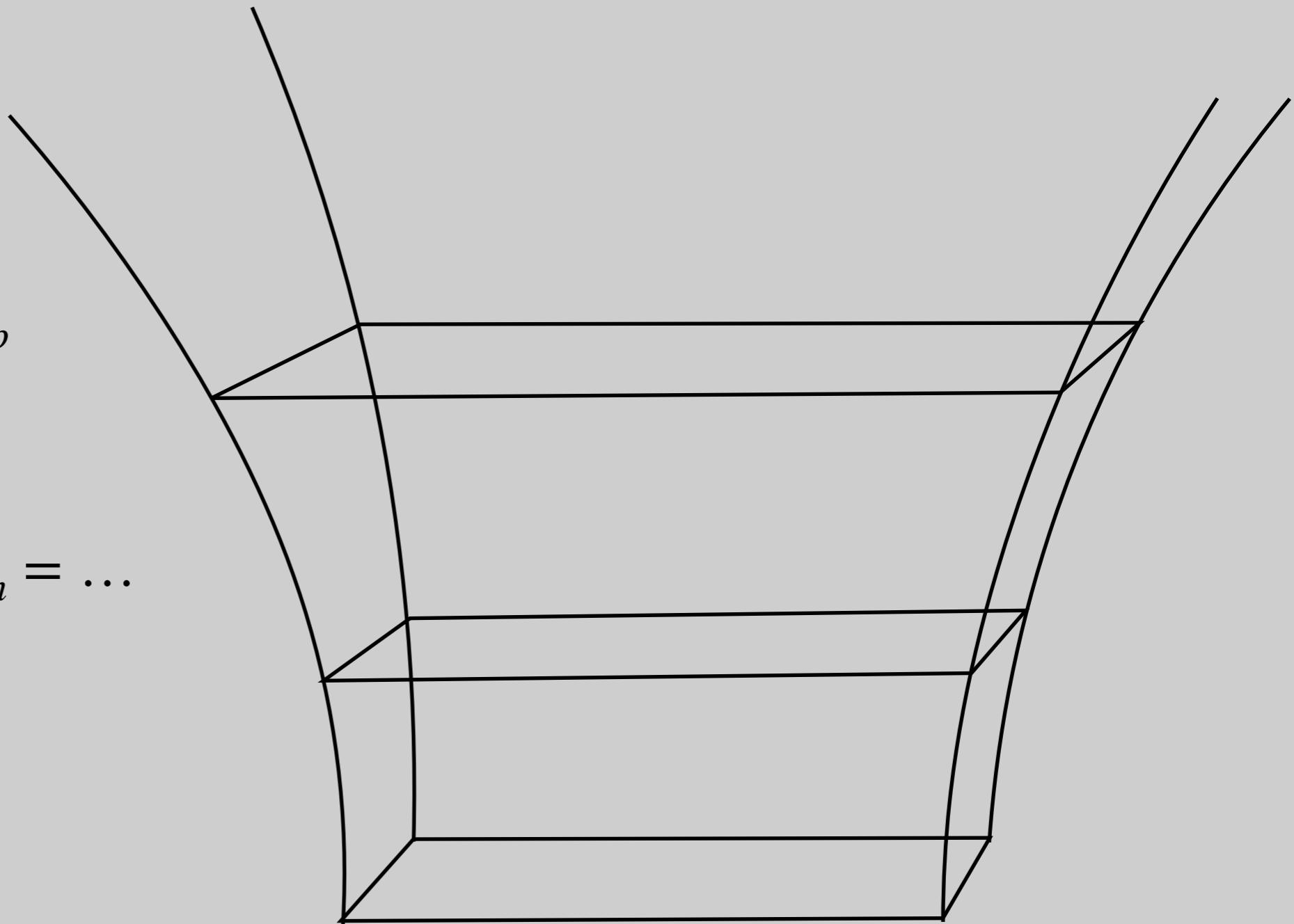
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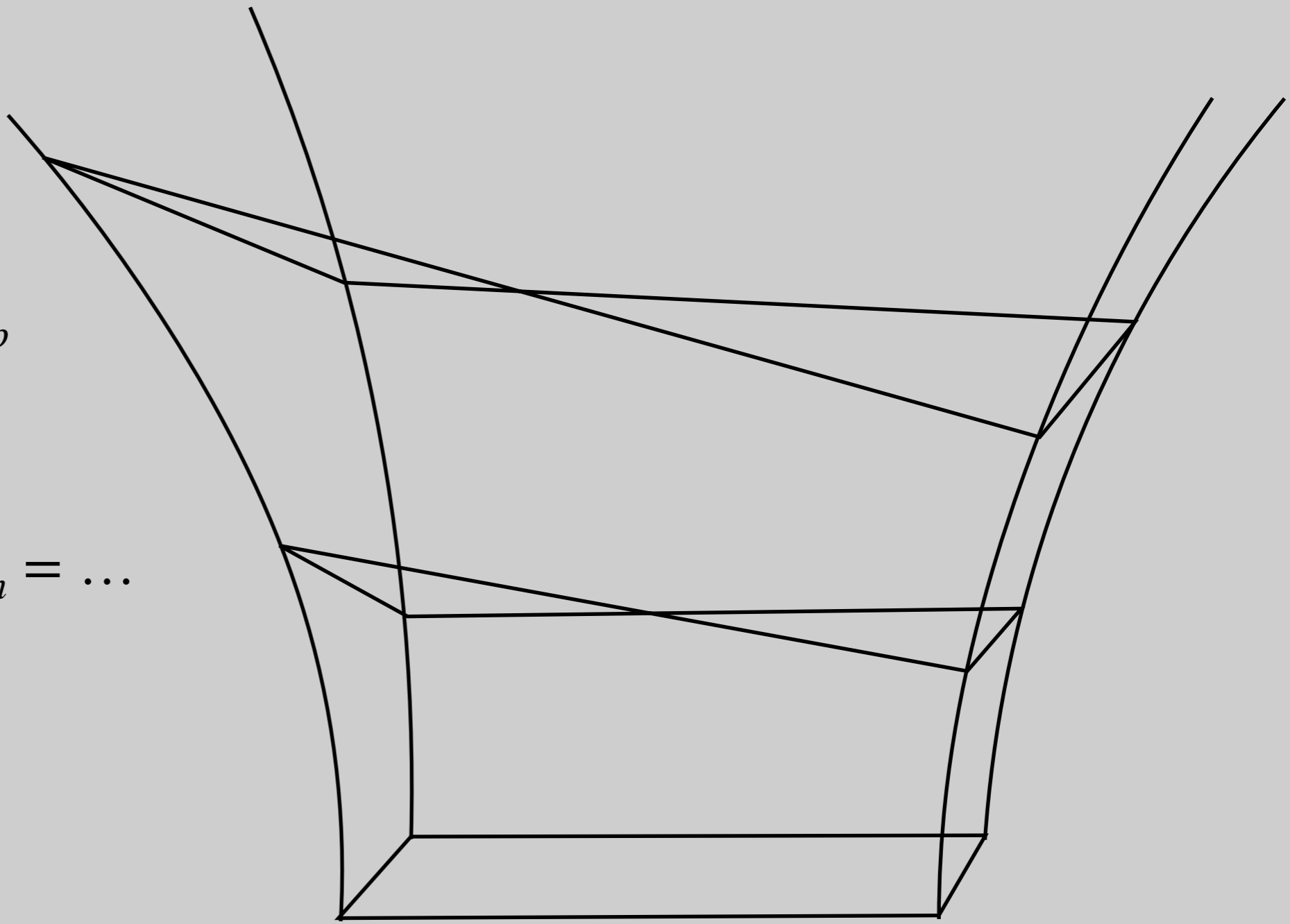
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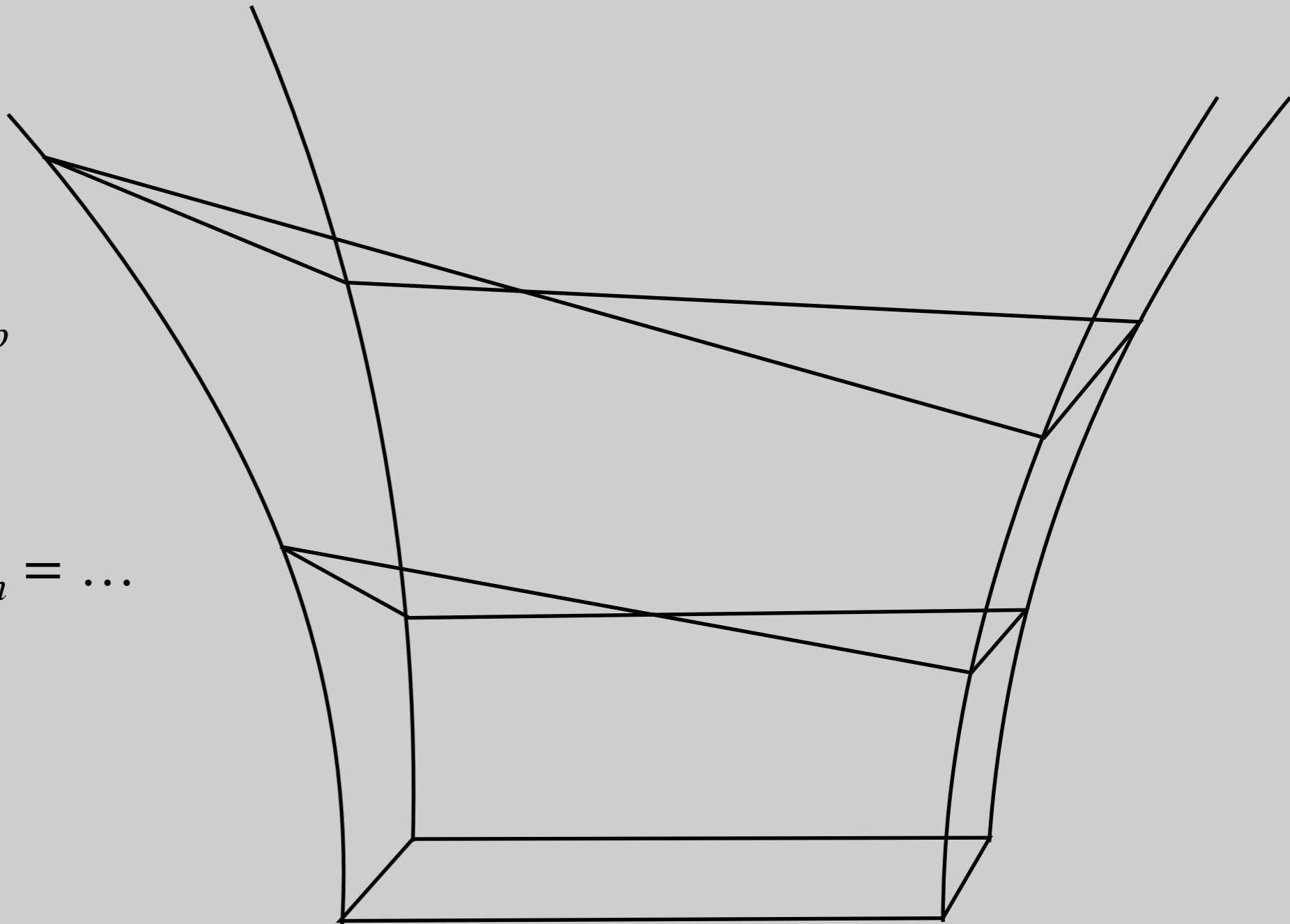
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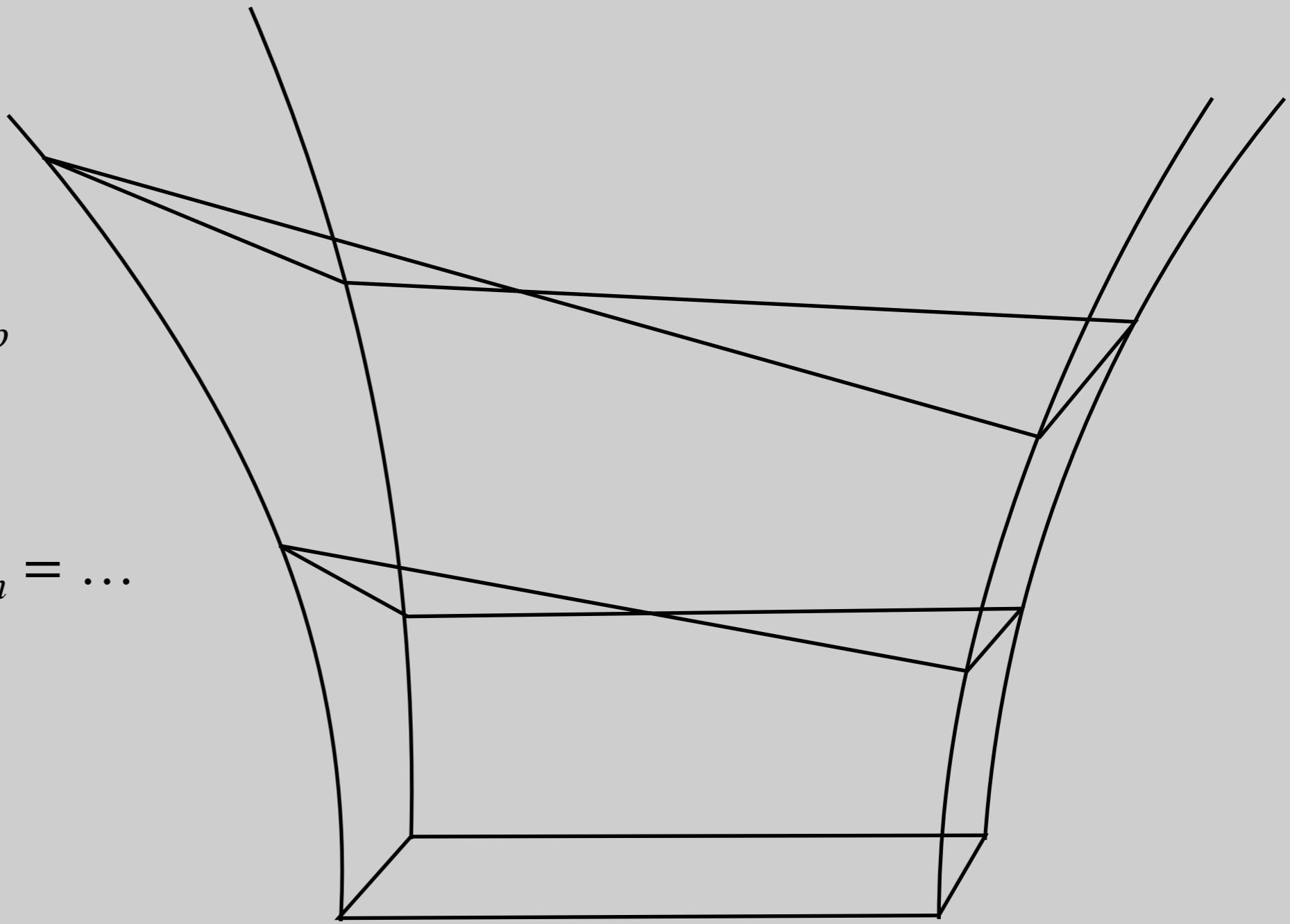
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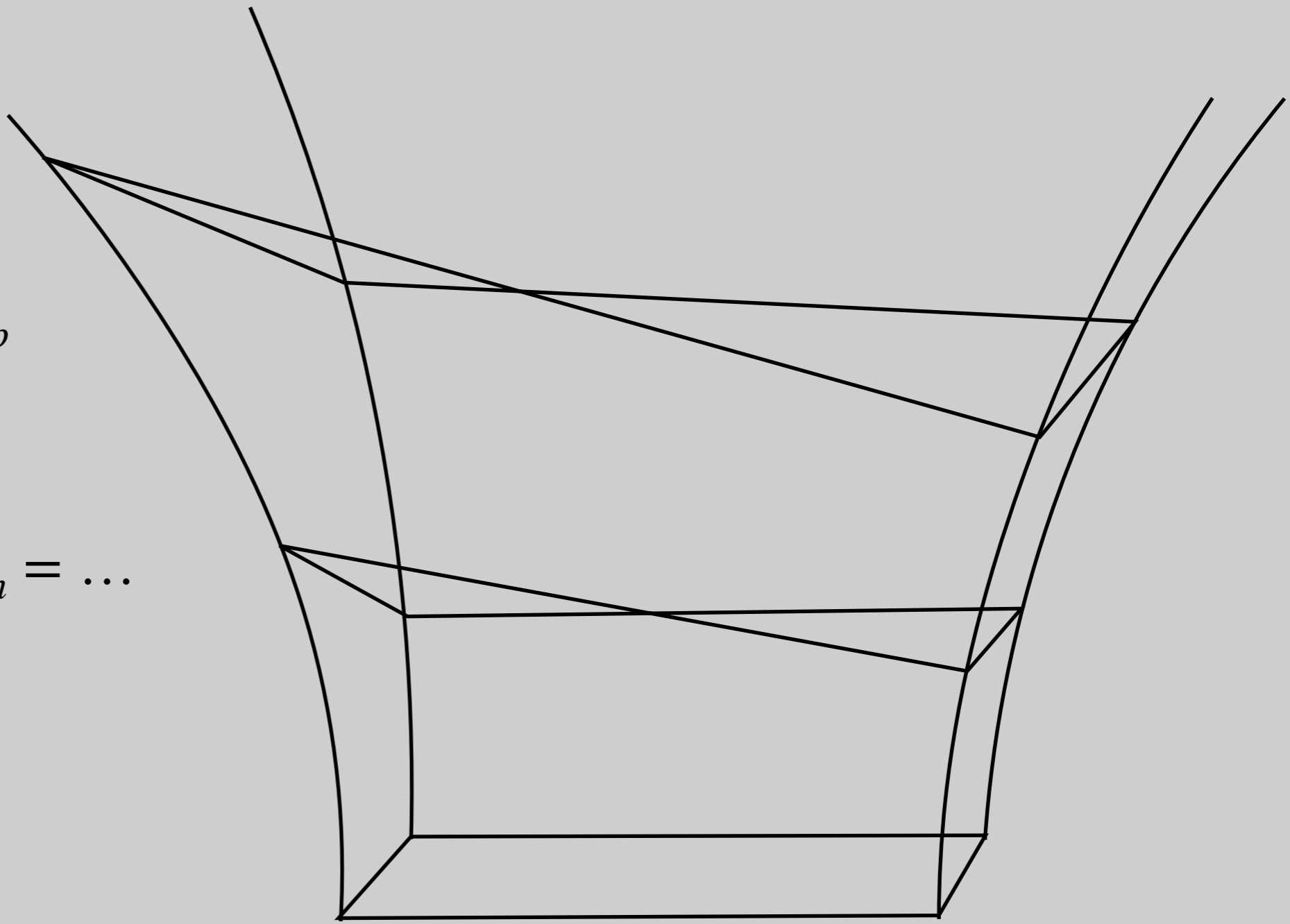
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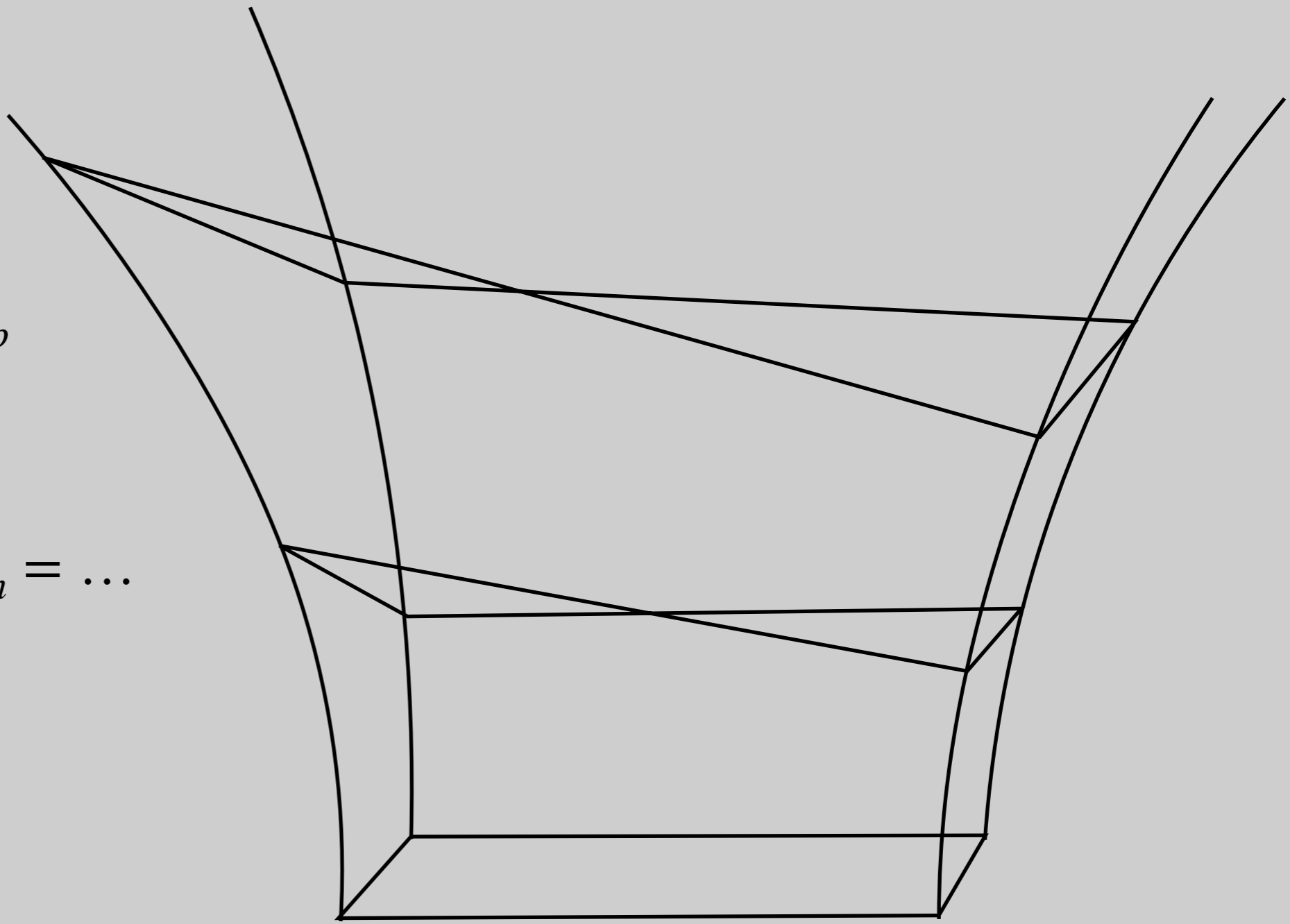
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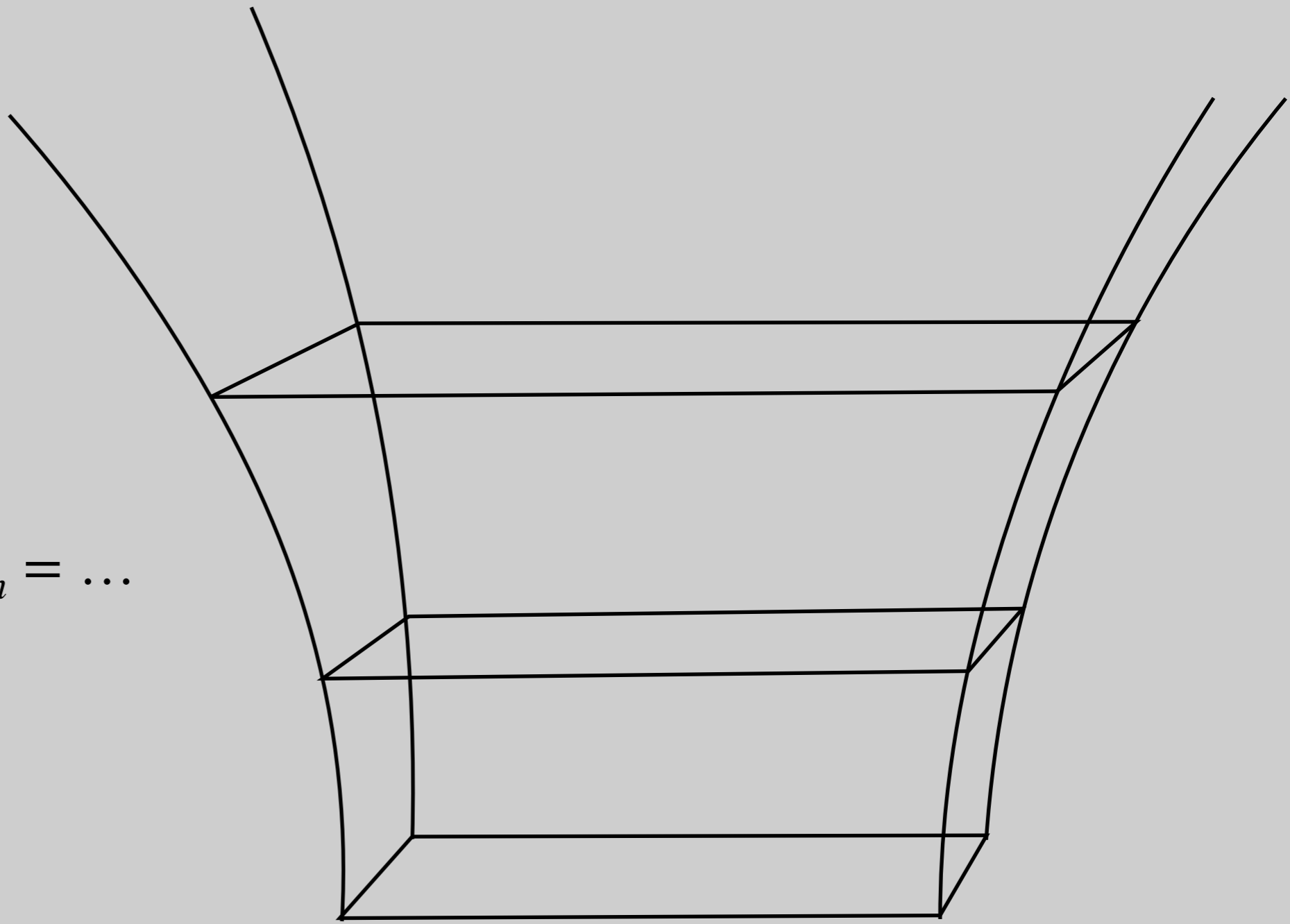
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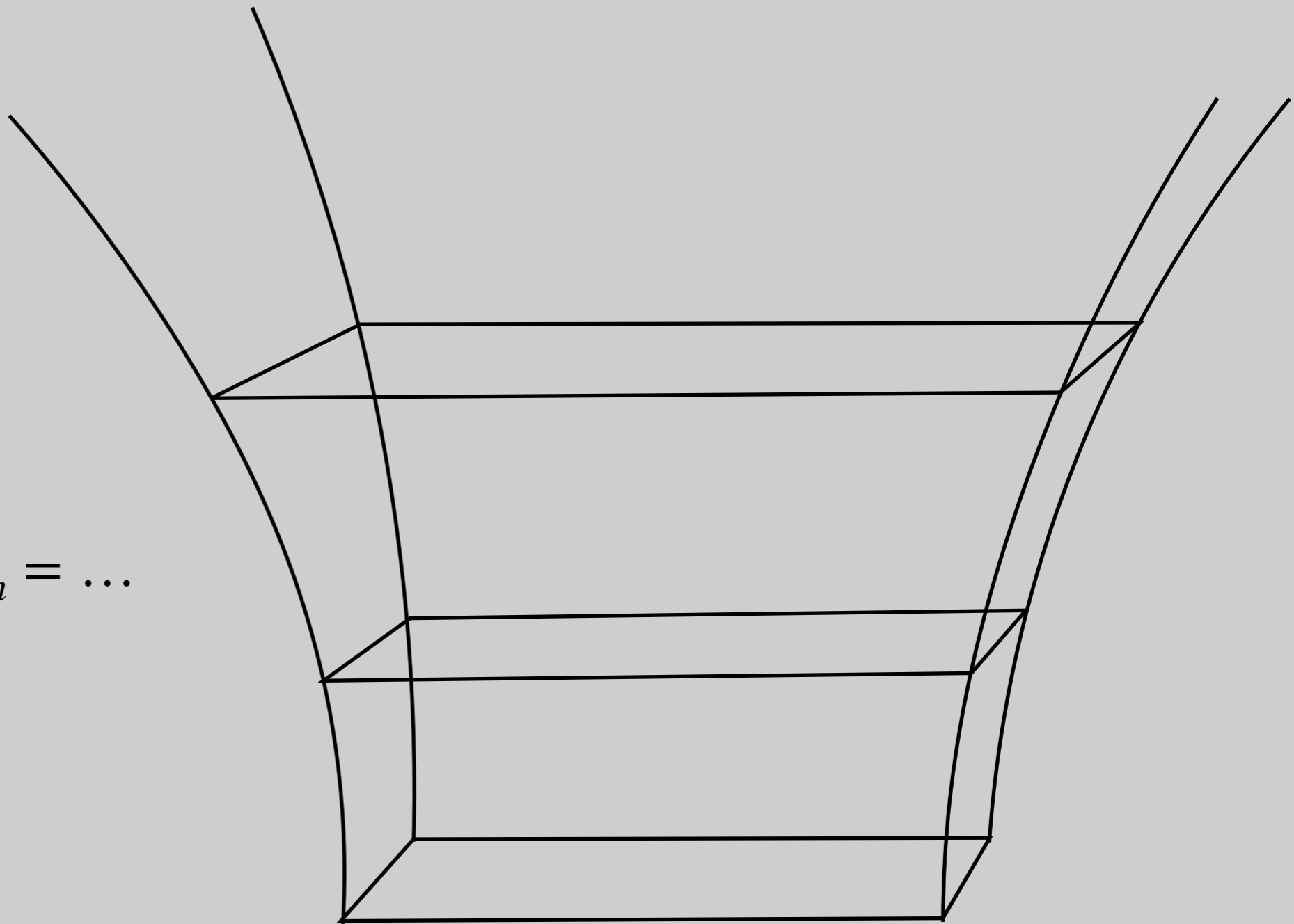
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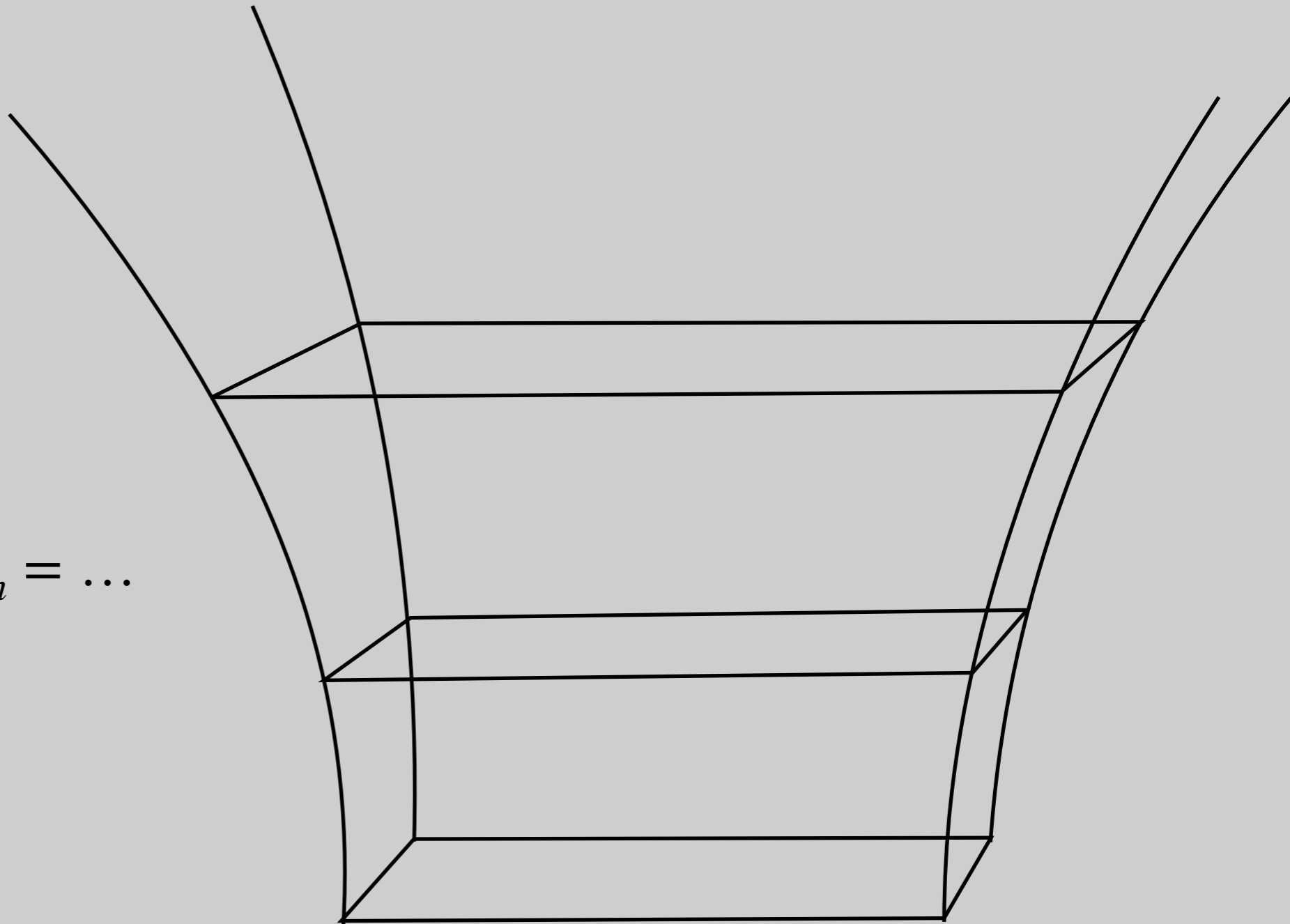
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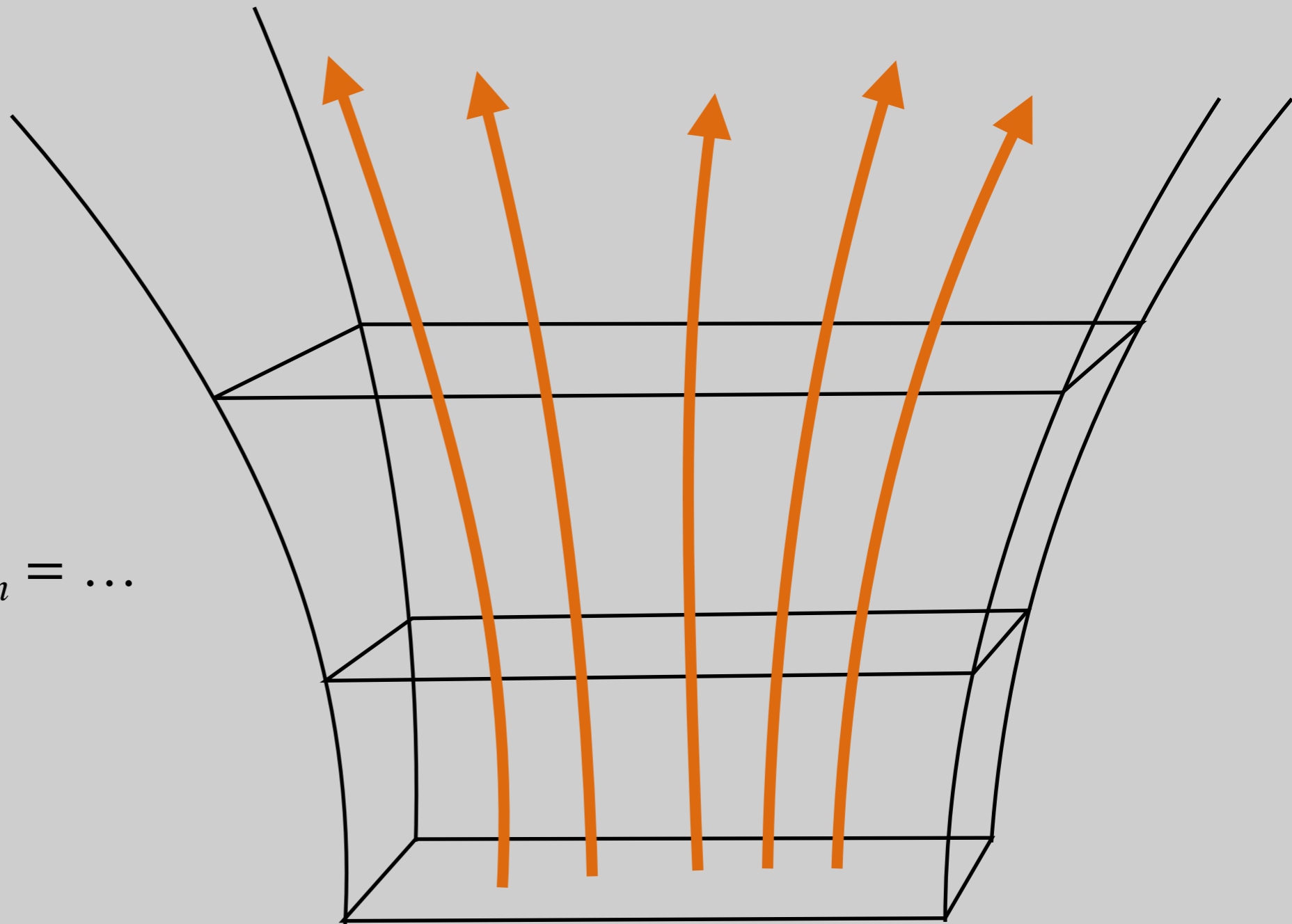
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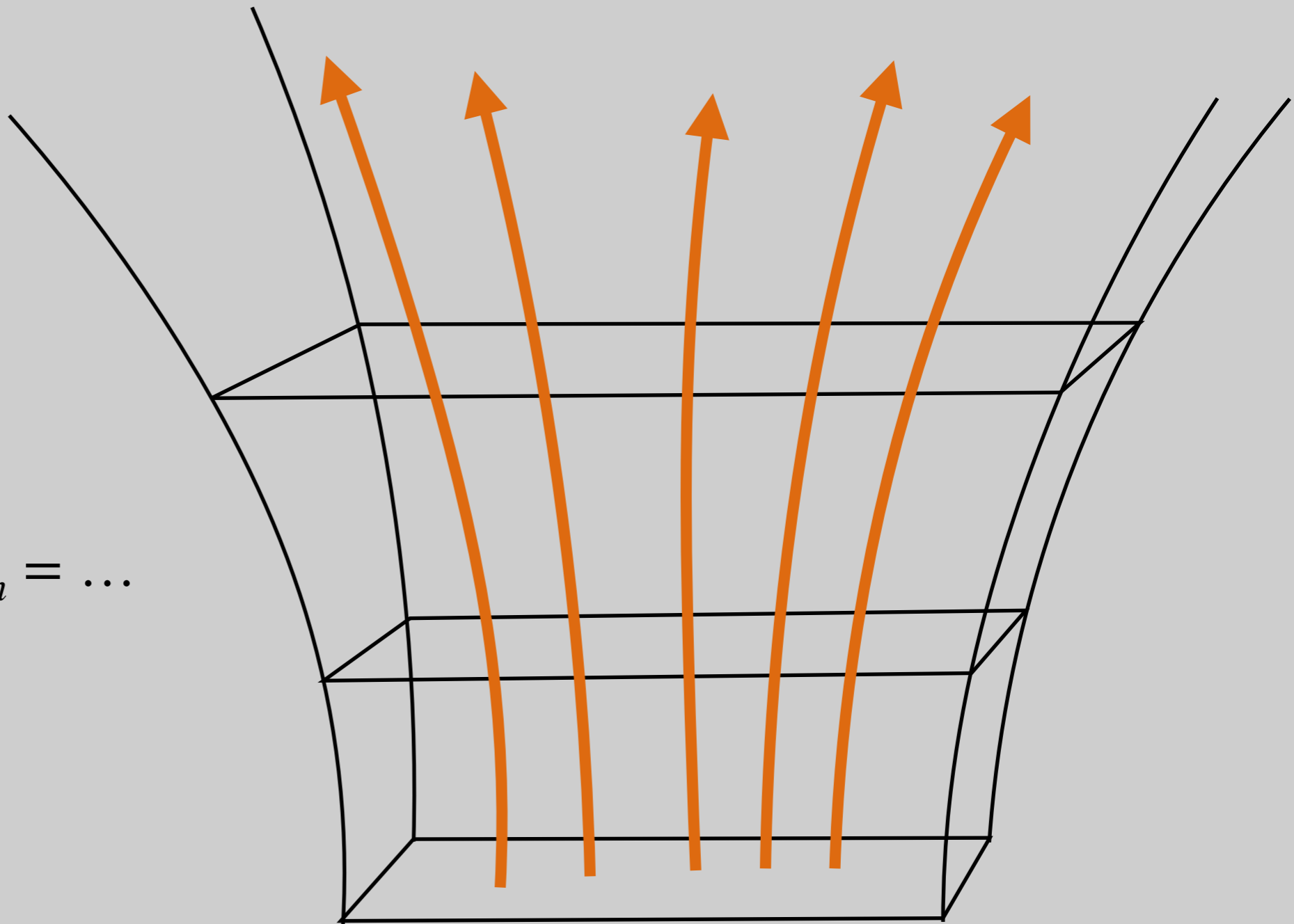
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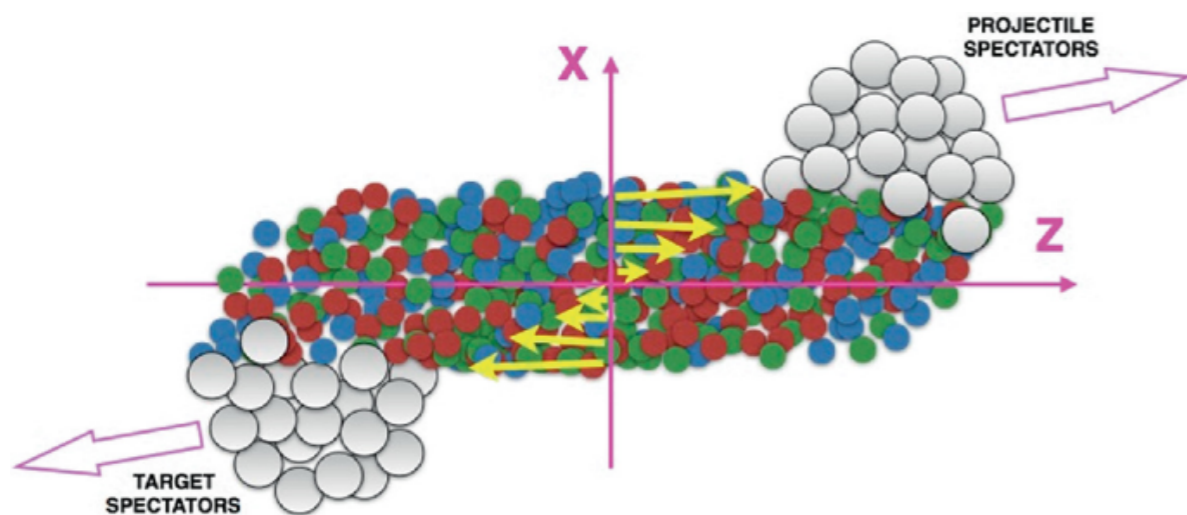
# Spin hydrodynamics

$$\nabla_{\mu} T^{\mu\nu} = 0 \quad \nabla_{\mu} J^{\mu\nu\rho} = 0$$

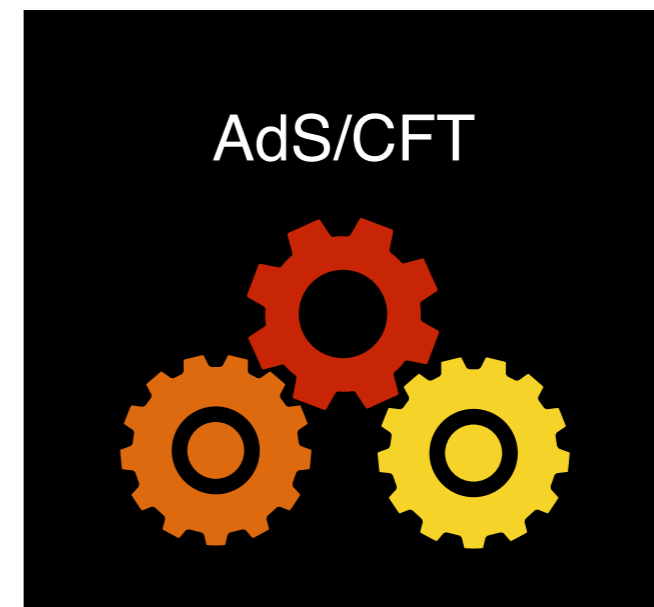
$$J^{\mu\nu\rho} = x^{\nu} T^{\mu\rho} - x^{\rho} T^{\mu\nu} + S^{\mu\nu\rho}$$

$$S^{\mu\nu\rho} = S^{\mu\nu\rho}[u, T, \mu^{\alpha\beta}] \quad T^{\mu\nu} = T^{\mu\nu}[u, T, \mu^{\alpha\beta}]$$

It works?



It can be verified





**Thank you**