Spin Alignment

- Experimental Overview

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Strongly Interacting Matter under Rotation



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The spin state of a vector meson can be described by a 3x3 spin density matrix.

The diagonal element ρ_{00} corresponds to the probability of finding a vector meson in spin state 0 out of 3 possible spin states of -1, 0 and 1.

A deviation of ρ_{00} from 1/3 would indicate a non-zero spin alignment.

$$\rho^{V} = \begin{pmatrix} \rho_{11} & \rho_{10} & \rho_{1-1} \\ \rho_{01} & \rho_{00} & \rho_{0-1} \\ \rho_{-11} & \rho_{-10} & \rho_{-1-1} \end{pmatrix}$$



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- No local cancelation when integrating over phase space as opposed to spin-1/2 particles.
- Access to spin-orbital force $S \cdot (E_{\phi} \times P)$, a term which is canceled in Λ polarization.
- Some mesons, like φ, are expected to originate predominantly from primordial production
 Iess decay contributions if compared to hyperons, more sensitive to early dynamics.



Strong p-wave decay

 ϕ (s \overline{s}) \rightarrow k⁺+ k⁻

 $k^{*0} (d\overline{s}) \rightarrow k^{+} + \pi^{-}$

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Dilepton decay

$$J/\psi(c\bar{c}) \rightarrow \mu^{+} + \mu^{-}$$
$$J/\psi(c\bar{c}) \rightarrow e^{+} + e^{-}$$

 $\frac{dN}{d(\cos\theta^*)} \sim (1-\rho_{00}) + (3\rho_{00}-1)\cos^2\theta^* \quad \frac{dN}{d(\cos\theta^*)} \sim (1+\rho_{00}) + (1-3\rho_{00})\cos^2\theta^*$



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From quark combination :

$$\rho_{00}^{V} = \frac{1 - \langle P_q P_{\overline{q}} \rangle}{3 + \langle P_q P_{\overline{q}} \rangle} \approx \frac{1}{3} - \frac{4}{9} \left\langle P_q P_{\overline{q}} \right\rangle$$



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Global Spin Alignment : STAR Results

- [1]. Liang et., al., Phys. Lett. B 629, (2005);
 Yang et., al., Phys. Rev. C 97, 034917 (2018);
 Xia et., al., Phys. Lett. B 817, 136325 (2021);
 Beccattini et., al., Phys. Rev. C 88, 034905 (2013)
- [2]. Sheng et., al., Phys. Rev. D 101, 096005 (2020);Yang et., al., Phys. Rev. C 97, 034917 (2018)
- [3]. Liang et., al., Phys. Lett. B 629, (2005)
- [4]. Xia et., al., Phys. Lett. B 817, 136325 (2021);
 Gao, Phys. Rev. D 104, 076016 (2021)
- [5]. Muller et., al., Phys. Rev. D 105, L011901 (2022)
- [6]. Sheng et., al., Phys. Rev. D 101, 096005 (2020);
 Phys. Rev. D 102, 056013 (2020); Phys Rev. Lett. 131 042304 (2023); Phys. Rev. D 109, 036004 (2024)
- [7] A. Kumar, B. Muller and D.-L Yang, PRD 108 016020 (2023)
- [8] Sheng, Pu and Wang, Phys. Rev. C 108 054902 (2023)
- [9] Sheng et., al., arXiv:2403.07522
- [10] Lv et. al., Phys. Rev. D 109, 114003 (2024)



STAR, Nature 614 244 (2023)

φ exhibits surprisingly large global spin alignment while K* displays little.

The Large ρ_{00} Surprise

 $\rho_{00} \approx \frac{1}{2} + C_{\Lambda} + C_{\varepsilon} + C_{E} + C_{F} + C_{L} + C_{A} + C_{\varphi} + C_{g}$



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Like electric charges in motion can generate an EM field, *s* and \overline{s} quarks in motion can generate an effective ϕ -meson field.

The ϕ -meson field can polarize *s* and \overline{s} quarks with a large magnitude due to strong interaction, in analogy to how EM field polarize (anti)quarks.



φ-meson Vector Field

PHYSICAL REVIEW C 99, 021901(R) (2019)

Rapid Communications

A and \overline{A} spin interaction with meson fields generated by the baryon current in high energy nuclear collisions

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We propose a dynamical mechanism which provides an interaction between the spins of hyperons and antihyperons and the vorticity of the baryon current in noncentral high energy nuclear collisions. The interaction is mediated by massive vector and scalar bosons, which is well known to describe the nuclear spin-orbit force. It follows from the Foldy-Wouthuysen transformation and leads to a strong-interaction Zeeman effect. The interaction may explain the difference in polarizations of Λ and $\overline{\Lambda}$ hyperons as measured by the STAR Collaboration at the BNL Relativistic Heavy Ion Collider. The signs and magnitudes of the meson-baryon couplings are closely connected to the binding energies of hypernuclei and to the abundance of hyperons in neutron stars.

Similar idea to explain $P_{\Lambda} - P_{\overline{\Lambda}}$



What About K^{*0} meson ?

Particle Species	Quark content	Mass (GeV/c ²)	Spin	Lifetime (fm/c)
φ	sīs	1.092	1	45
K⁺⁰	$d\overline{s}$	0.896	1	4

Sheng et., al., Phys. Rev. D 102, 056013 (2020)



Little field correlation for K^{*0} , causing $\langle P_{\overline{q}}P_{q} \rangle$ to diminish.

Fluctuation Matters



The Rapidity Dependence



$$D^{*+} (c\overline{d}) \rightarrow D^{0} + \pi^{+}$$
$$\downarrow k^{-} + \pi^{+}$$

G. Wilks for STAR, SQM 2024 Theory curve : X.L. Sheng, et al., PRC 108 054902 (2023)

L. Micheletti for ALICE, QM2023

Strong rapidity dependence at both RHIC and LHC. Trend consistent with prediction invoking strong force field.

The Rapidity Dependence



G. Wilks for STAR, SQM 2024 Theory curve : X.L. Sheng, et al., PRC 108 054902 (2023) $\rho^{z}_{00} < 1/3 \implies \rho^{x}_{00} = \rho^{y}_{00} > 1/3$

X.L. Sheng, S. Pu and Q. Wang, PRC 108 054902 (2023)

Strong rapidity dependence at both RHIC and LHC. Trend consistent with prediction invoking strong force field.

What about J/ψ ?

Naïve expectation from fluctuating strong force field : $\rho_{00} > 1/3$ at midrapidity



Forward J/ ψ ρ_{00} at LHC and midrapidity J/ ψ ρ_{00} < 1/3 at RHIC, both < 1/3.

How do we understand $J/\psi \rho_{00}$?

Any Hint on Vortical Structure ?



Centrality Dependence



Spin-Spin Correlation : Vortical Structure



Pang et.al., PRL 117 192301 (2016)

Spin-Spin Correlation : Strong Force



Strong force induced hyperon spin correlation

Lv et. al., Phys. Rev. D 109, 114003 (2024)

New clue to strong interaction.

Spin correlation function :

$$c_{ij} = \frac{f_{\uparrow\uparrow} + f_{\downarrow\downarrow} - f_{\downarrow\uparrow} - f_{\uparrow\downarrow}}{f_{\uparrow\uparrow} + f_{\downarrow\downarrow} + f_{\downarrow\uparrow} + f_{\uparrow\downarrow}}$$

 $f_{m_im_j} = \langle m_im_j|\hat{\rho}|m_im_j\rangle$: fraction of particle pair in the spin state $|m_1m_2\rangle$

In heavy ion collisions with finite global polarization,

$$c_{ij}' = c_{ij} - P_i P_j$$

It can be shown that

$$c_{\Lambda\Lambda}' = \frac{9}{\alpha_{\Lambda}^2} \langle \cos\theta_i^* \cos\theta_j^* \rangle - P_{\Lambda}^2$$

In practice with the consideration of EP resolution

$$c_{\Lambda\Lambda}' = \frac{64}{\pi^2 \alpha_{\Lambda}^2} \frac{\langle \sin(\phi_i^* - \Psi_{\rm EP}) \sin(\phi_j^* - \Psi_{\rm EP}) \rangle}{\langle \cos^2(\Psi_{\rm EP} - \Psi_{\rm RP}) \rangle} - P_{\Lambda}^2$$

Lyuboshitz and Lyuboshitz, Phys. Of Atomic Nuclei, 273 805 (2010) Chen et. al., Phys.Rev. D 95, 034009 (2016) Lv et. al., Phys. Rev. D 109, 114003 (2024)

Chen, Goldstein, Jaffe and JI, NPB 445 380 (1995) Zhang and Wei, arXiv:2301.04096 Shen, Chen and Tang, arXiv:2407.21291

Spin-Spin Correlation in pp



 $\frac{\mathrm{d}N}{\mathrm{d}\cos(\theta^*)} \sim 1 + \alpha_1 \alpha_2 P_{\Lambda_1 \Lambda_2} \cos(\theta^*)$

Correlation induced by parton spin correlation and/or entanglement ? fragmentation and hadronization ?

Within uncertainty no signal is seen when integrated over phase space.

Desirable to study it differentially.

Jan Vanek for STAR, DIS 2024

K^{*0} in Isobar



 $K^{*0} \rho_{00} > 1/3$ at small Npart in isobar. comparable to AuAu at similar Npart

D*+ ρ₀₀



Expectation:

from Recombination : < 1/3from Fragmentation : > 1/3

 $\begin{array}{l} \textbf{Observation}:\\ \textbf{Low } p_t < 1/3\\ \textbf{High } p_t > 1/3 \end{array}$

--- Qualitatively agree with expectation that recombination is relevant at low while fragmentation is relevant at high pt.

However, quantitative agreement could be very challenging.

 $D^{*+}(c\overline{d}) \rightarrow D^{0} + \pi^{+}$ $\downarrow k^{-} + \pi^{+}$

$\rho_{\textbf{00}}$ and CME



 ρ_{00} being larger(smaller) than 1/3 means positive(negative) contribution to CME observables

How to properly account for ρ -meson ρ_{00} in CME analyses ?

ρ_{1-1} and CME



 ρ_{1-1} affects $\Delta \gamma$ in opposite way to ρ_{00}

How to properly account for ρ -meson ρ_{00} in CME analyses ?

Spin is aligned, let's add some magnetism to the mix ...

The Strongest EM Field, But Do We "See" It ?



Despite wide expectation of its existence, its imprint in QGP has been elusive.

EM Field and Phase Diagram



Magnetic field, eB

Mizher, Chernodub and Fraga, PRD 82 105016 (2010) E. Fraga and A. Mizher, PRD 78 025016 (2008)

Rich structure of QCD phase diagram under strong EM field.

EM Field and CME



Probe E Field in Cu + Au Collisions



Asymmetric collisions (Cu+Au) create in-plane E fields.

Charge-dependence of v_1

$$v_1^{\pm} = v_1 \pm Ad'_e$$

$$Ad'_e \sim -\frac{\pi\sigma\tau}{N_{\rm tot}|e|} \int_S \vec{E} \cdot d\vec{S}$$

Hirono, Hongo and Hirano, Phys. Rev. C 90, 021903 (2014)

Study electric conductivity of medium via Cu+Au collisions

Evidence of the Coulomb Field



Qualitatively agrees with expectation from strong E field

10 times smaller than PHSD which uses a lower value of σ . Probably due to that (anti)quarks not all created when EF is strong (< 1 fm).

Study electric conductivity of medium via Cu+Au collisions

Λ and anti- Λ Polarization



 $P_{\Lambda} \approx \frac{1}{2} \frac{\omega}{T} + \frac{\mu_{\Lambda} B}{T}$ $P_{\overline{\Lambda}} \approx \frac{1}{2} \frac{\omega}{T} - \frac{\mu_{\Lambda} B}{T}$

Challenging to see the B effect at later stage

Λ and anti- Λ Polarization



 $P_{\overline{A}} - P_A = -2\frac{\mu_A B}{\tau}$

STAR, PRC 108 014910 (2023)

Challenging to see the B effect at later stage

EM field : Hall, Faraday and Coulomb Effect



Hall effect (Lorentz force) and Faraday + Coulomb effect compete each other.

Hall effect is more relevant for heavy quarks at early stage.

Calculations indicate Faraday + Coulomb effect dominate over Hall effect for light hadrons.

Gursoy, Kharzeev and Rajagopal, PRC 89 054905 (2014) S.K. Das et al., PLB 768 260 (2017) Umut Gursoy, et al., PRC 98 055201 (2018) K. Nakamura et. al., PRC 107 034912 (2023) K. Nakamura et. Al., PRC 107 014901 (2023)

Transported Quarks



$$\begin{array}{l} p: uud \\ \bar{p}: \bar{u}\bar{u}\bar{d} \end{array} \quad v_1^p > v_1^{\bar{p}} \text{ at } \eta > 0 \\ \hline{p}: \bar{u}\bar{u}\bar{d} \end{array}$$

$$\frac{K^{+}: u\bar{s}}{K^{-}: \bar{u}s} \quad v_{1}^{K^{+}} > v_{1}^{K^{-}} \text{ at } \eta > 0$$

 $\pi^{+}: u\bar{d} \qquad v_{1}^{\pi^{-}} > v_{1}^{\pi^{+}} \text{ at } \eta > 0$ $\pi^{-}: \bar{u}d \qquad (\text{#d>#u, Au neutron rich})$

Dunlop, Lisa and Sorensen, PRC 84 044914 (2011) Guo, Liu and Tang, PRC 86 044901 (2012) Nayak, Shi, Xu and Lin, PRC 100 054903 (2019) P. Bozek, PRC 106 L061901 (2022)

Transported quarks carry information from incident nucleons, causing v_1 splitting.

Interplay between Effects



Transported quark effect :

$$p: \underline{uud}$$

$$p: \underline{uud}$$

$$p: \underline{uud}$$

$$v_1^p > v_1^{\overline{p}} \text{ at } \eta > 0$$

$$K^+: \underline{us}$$

$$K^-: \overline{us}$$

$$v_1^{K^+} > v_1^{K^-} \text{ at } \eta > 0$$

$$\pi^+: \underline{ud}$$

$$v_1^{\pi^+} < v_1^{\pi^-} \text{ at } \eta > 0$$

$$\pi^-: \overline{ud}$$

$$(\#d > \#u, \text{ Au neutron rich})$$

 v_1 slope difference between protons and antiprotons: sign change as a function of centrality.

Similar pattern expected for kaons.

No sign change expected for pions.

Sign Change in $\Delta(dv_1/dy)$



Sign change in $\Delta(dv1/dy)$ occurs for both protons and kaons.

The magnitudes follow the expected ordering between protons and kaons.

Pion results are either consistent with zero or negative, as expected.

The electric conductivity of QGP used in iEBY-VISHNU+EM model lies within a plausible interval. (σ =0.023 fm⁻¹)

Strong evidence in favor of EM field at work in QGP

The study of global spin properties in extreme conditions has opened new promising research directions. Recent findings also highlight the significant role of magnetic fields at RHIC, deepening our understanding of spin dynamics.

As is typical in emerging fields, numerous unanswered questions beckon, offering fertile ground for future investigation and inquiry.

Backup Slides

v₁ Splitting of D Mesons



STAR, PRL 123 162301 (2019)

Consistent with Hall effect dominating for heavy quarks.

EM Field and Phase Diagram



M Elia, L. Maio, F. Sanfilippo and A. Stanzione, PRD 105 034511 (2022)

QCD phase diagram under strong EM field.