Fluctuations of conserved charges from lattice and HRG and the freezout in HIC



- Introduction: Fluctuations of conserved charges and hadron resonance gas
- Hardon resonance gas with repulsive interactions and fluctuations of baryon
 number
- Chiral condensate in HRG and chiral crossover line at large baryon density
- Baryon number fluctuations and baryon-strangeness correlation along the crossover line and freeze-out condition in RHIC
- Summary

New developments in studies of the QCD phase diagram, ECT*, Trento, September 9-13, 2024

QCD thermodynamics at non-zero chemical potential

Taylor expansion :

$$\frac{p(T,\mu_B,\mu_Q,\mu_S)}{T^4} = \sum_{i,j,k} \frac{1}{i!j!k!\dots} \chi^{BQS}_{ijk} \cdot \left(\frac{\mu_B}{T}\right)^i \cdot \left(\frac{\mu_Q}{T}\right)^j \cdot \left(\frac{\mu_s}{T}\right)^k \quad \text{hadronic}$$

$$\frac{p(T,\mu_u,\mu_d,\mu_s)}{T^4} = \sum_{i,j,k} \frac{1}{i!j!k!} \chi^{uds}_{ijk} \cdot \left(\frac{\mu_u}{T}\right)^i \cdot \left(\frac{\mu_d}{T}\right)^j \cdot \left(\frac{\mu_s}{T}\right)^k \quad \text{quark}$$

$$\chi^{abc}_{ijk} = T^{i+j+k} \frac{\partial^i}{\partial \mu^i_a} \frac{\partial^j}{\partial \mu^j_b} \frac{\partial^k}{\partial \mu^k_c} \frac{1}{VT^3} \ln Z(T,V,\mu_a,\mu_b,\mu_c)|_{\mu_a=\mu_b=\mu_c=0}$$

Taylor expansion coefficients give the fluctuations and correlations of conserved charges, e.g.

$$\chi_2^X = \chi_X = \frac{1}{VT^3} (\langle X^2 \rangle - \langle X \rangle^2) \qquad \qquad \chi_{11}^{XY} = \frac{1}{VT^3} (\langle XY \rangle - \langle X \rangle \langle Y \rangle)$$

information about carriers of the conserved charges (hadrons or quarks)

probes of deconfinement

Second order Taylor expansion coefficients and HRG

HISQ, m_{π}^{phys} , $a = 1/(TN_{\tau})$

Bollweg et al (HotQCD), PRD 104 (2021) 074512



HRG works up to temperatures $\simeq 145-150 \text{ MeV}$

Higher order Taylor expansion coefficients and HRG

HISQ, m_{π}^{phys} , $a = 1/(TN_{\tau})$



Bollweg et at (HotQCD), PRD 105 (2022) 074511



For 4th order expansion coefficient HRG may work only for T < 140 MeV

For 6th and 8th order expansion coefficients turn negative around T_c HRG, only works for T < 135 MeV HRG with repulsive mean field

Repulsive B-B interactions are not present in usual HRG

Ellis, Kapusta, Huovinen et al, ...



Biswas, PP, Sharma, PRC 109 (2024) 055206

Improved agreement between lattice and HRG

Baryon number fluctuations in HRG with repulsive mean field





WB continuum correspond to small box LT=2

HRG with repulsive mean field can explain the lattice result on 6^{th} and 8^{th} order baryon number fluctuation up to T=155 MeV

Chiral condensate in HRG



Chiral crossover line at large baryon density

 $\Delta_R^l(T,\mu_B) \simeq \frac{1}{2} \Delta_R^l(T=0) \Rightarrow T_{pc}(\mu_B) \quad \text{Biswas, PP, Sharma, PRC 109 (2024) 055206}$



 $T_c(\mu_B = 0) \simeq 160 \text{ MeV}$ $T_{pc}(\mu_B)/T_{pc}(0) = 1 - \kappa_2 (\mu_B/T_{pc}(0))^2 - \kappa_4 (\mu_B/T_{pc}(0))^4$

 $\kappa_2 = 0.0150(2)$ and $\kappa_4 = 3.1(6) \times 10^{-5}$

in agreement with lattice QCD

For $\mu_B > 400$ MeV the chiral crossover line is above the freeze-out line

Chiral crossover line for strangeness neutral case

Biswas, PP, Sharma, PRC 109 (2024) 055206



The effects of repulsive interactions lead to larger chiral crossover temperature

Imposing strangeness neutrality results only in small shift of the chiral transition line, smaller than the effects of the repulsive interactions.

Chiral crossover line for strangeness neutral case

 $R_{nm}^{XY}(T,\mu_B) = \frac{\chi_n^X(T,\mu_B)}{\chi_m^Y(T,\mu_B)} \quad \text{can probe freeze-out conditions in RHIC}$

Bazavov et al, PRD 101 (2020) 074502; Bollweg et at, arXiv:2407.03516



Conditions in RHIC: $n_S = 0$, $n_Q/n_B = 0.4 \Rightarrow$





Baryon number fluctuations along the freeze-out line



Bollweg et at, arXiv:2407.03516

$$R_{12}^B(T_{pc}(\mu_B), \mu_B) = R_{12}^p(\sqrt{s_{NN}})$$

 $\Rightarrow \mu^f_B = \mu^f_B(\sqrt{s_{NN}})$

2°. 2°. 2°. 2°. 2°. 2°. 2°.

1.2

agreement with $(T^f(\sqrt{s_{NN}}), \mu_B^f(\sqrt{s_{NN}}))$ obtained from statistical model fits of particle yields

Bazavov et al, PRD 101 (2020) 074502

 $\begin{aligned} R^B_{nm} &< 1 \\ R^B_{42} &< R^B_{31} \text{ for large } \mu_B \end{aligned}$

in agreement with LQCD

Correlations of strangeness with baryon number and strangeness along the freeze-out line



Bollweg et at, arXiv:2407.03516

Tension between LQCD and STAR BES-II for $\sqrt{<}39$ GeV

Underestimated feed-down from excited states ?



• Fluctuations and correlations of conserved charges can be understood in terms of HRG if missing baryons are included

• For higher order baryon number fluctuations repulsive interactions play an important role

• For baryon chemical potential >400 MeV the estimated chiral crossover temperature is larger than the chemical freeze-out temperature

 Lattice results and the experimental results on fluctuations and correlations of conserved charges indicate that interactions in hadron gas just below the transition temperature are significant

• Fluctuations and correlations of conserved charges can be used to determine the freeze-out conditions in RHIC