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# Superfluidity of parity-doubled baryons in neutron stars

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arXiv:2409.05670

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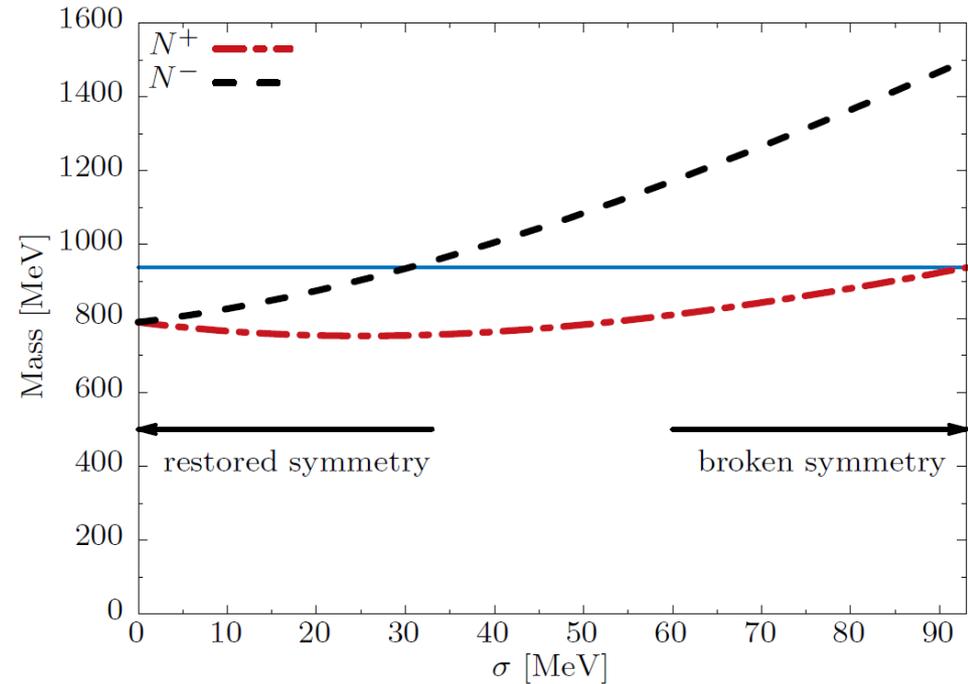
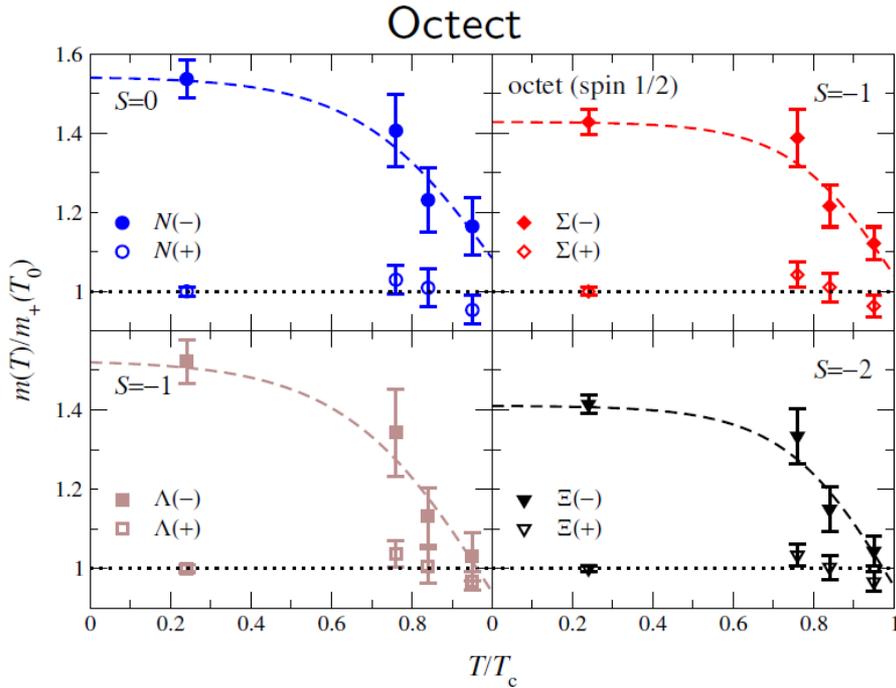
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# Parity doubling of baryons



❑ Lattice QCD at zero  $\mu$

[Aarts et al., 2016-2019]

❑ Survival mass  $m_N \approx m_0 \neq 0$

[DeTar, Kunihiro, 1989]

$$M_{\pm} = \sqrt{m_0^2 + c_1^2 \sigma^2} \mp c_2 \sigma \xrightarrow{\sigma \rightarrow 0} m_0$$

# DeTar-Kunihiro/Parity doublet model

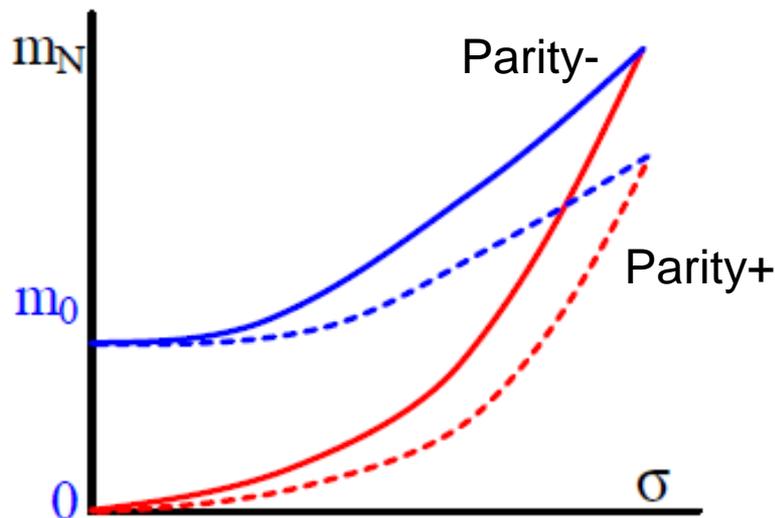
□ SU(2) chiral transformation of 2 nucleons

→ how to assign 2 indep. rotation to them?

$$\psi_{1L} \rightarrow g_l \psi_{1L}, \quad \psi_{1R} \rightarrow g_r \psi_{1R} \sim \psi_{1L} : (1/2, 0) \quad \psi_{1R} : (0, 1/2)$$

$$\psi_{2L} \rightarrow g_r \psi_{2L}, \quad \psi_{2R} \rightarrow g_l \psi_{2R} \sim \psi_{2L} : (0, 1/2) \quad \psi_{2R} : (1/2, 0)$$

$$\mathcal{L}_m = m_0 (\bar{\psi}_2 \gamma_5 \psi_1 - \bar{\psi}_1 \gamma_5 \psi_2) \Rightarrow m_{N_{\pm}} = \frac{1}{2} \left[ \sqrt{c_1 \sigma^2 + 4m_0^2} \mp c_2 \sigma \right]$$



[DeTar and Kunihiro, 1989]

Red: Naive  
Blue: Mirror

# The role of $N^*$

□ Correlations between  $N$  and  $N^*$  at finite  $T$  &  $\mu$

[Koch, Marczenko et al., 2024]

- $\chi_2^B = \chi_2^{++} + \chi_2^{--} + 2\chi_2^{+-}$  : strength & sign of  $\chi_2^{+-}$
- Liquid-gas vs. QCD chiral transitions
- The net-proton fluctuations do not necessarily reflect the net-baryon fluctuations at the chiral phase boundary.

□ The role of  $\Delta(1232)$ : correlations among

$(N, N^*)$  &  $(\Delta, \Delta^*)$

[Marczenko, PRD 2024]

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# **SUPERFLUIDITY IN NEUTRON STARS**

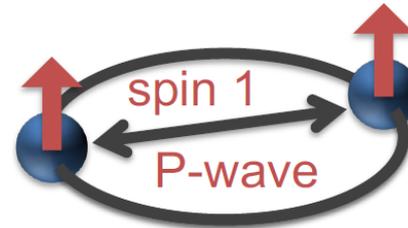
# Superfluidity in neutron stars

□ s-wave superfluid by  $^1S_0$  [Migdal, '60]

□ p-wave superfluid by  $^3P_2$  at  $\rho/\rho_0 > 1/2$  [Tabakin, '68]

✓ Pulsar glitches

✓ Rapid cooling



$$2S+1 L_J$$

S: spin  
L: angular momentum  
J: spin+angular momentum

□ This study: Cooper pairing of parity-doubled neutrons at high density  $\rightarrow$  the role of  $N^*$

▪ Generalized  $\chi$ -sym  $G$  such that  $G \supset \text{naïve \& mirror}$

$$G = U(1)_{1L} \times U(1)_{1R} \times U(1)_{2L} \times U(1)_{2R}$$

▪ Common operators to the naïve & mirror assign.

# Symmetries

## □ $U(1)_L \times U(1)_R$ chiral symmetry

$$(n, n^*) \Leftrightarrow (\psi_1, \psi_2), \quad \psi_i = \psi_{iL} + \psi_{iR}$$

### ▪ Naïve assignment

$$\psi_{1L} \rightarrow U_L \psi_{1L}, \quad \psi_{2L} \rightarrow U_L \psi_{2L}, \quad \psi_{1R} \rightarrow U_R \psi_{1R}, \quad \psi_{2R} \rightarrow U_R \psi_{2R}$$

### ▪ Mirror assignment

$$\psi_{1L} \rightarrow U_L \psi_{1L}, \quad \psi_{2L} \rightarrow U_R \psi_{2L}, \quad \psi_{1R} \rightarrow U_R \psi_{1R}, \quad \psi_{2R} \rightarrow U_L \psi_{2R}$$

## □ Generalized chiral symmetry

$$G = U(1)_{1L} \times U(1)_{2L} \times U(1)_{1R} \times U(1)_{2R}$$

$$\psi_{1L} \rightarrow U_{1L} \psi_{1L}, \quad \psi_{2L} \rightarrow U_{2L} \psi_{2L}, \quad \psi_{1R} \rightarrow U_{1R} \psi_{1R}, \quad \psi_{2R} \rightarrow U_{2R} \psi_{2R}$$

$$\text{Naïve: } U_{1L} = U_{2L}, U_{1R} = U_{2R} \quad \text{Mirror: } U_{1L} = U_{2R}, U_{1R} = U_{2L}$$

# Symmetries

Define 2 symmetries as  $[\psi_L^t = (\psi_{1L}, \psi_{2L})^t]$

$$\psi_L \rightarrow e^{i\theta_L} \psi_L, \quad \psi_R \rightarrow e^{i\theta_R} \psi_R, \quad \text{with } (e^{i\theta_L}, e^{i\theta_R}) \in U(1)_L \times U(1)_R$$

$$\psi_L \rightarrow e^{i\tau_3\theta_L} \psi_L, \quad \psi_R \rightarrow e^{i\tau_3\theta_R} \psi_L, \quad \text{with } (e^{i\tau_3\theta_L}, e^{i\tau_3\theta_R}) \in U(1)_{(1-2)L} \times U(1)_{(1-2)R}$$

$$U(1)_{1L} \times U(1)_{2L} = \frac{U(1)_L \times U(1)_{(1-2)L}}{\mathbb{Z}'_{2L}}, \quad U(1)_{1R} \times U(1)_{2R} = \frac{U(1)_R \times U(1)_{(1-2)R}}{\mathbb{Z}'_{2R}}$$

❖ Global sym  $G$  and its subgroups

$$U(1)_L \times U(1)_R \subset \frac{U(1)_L \times U(1)_{(1-2)L}}{\mathbb{Z}'_{2L}} \times \frac{U(1)_R \times U(1)_{(1-2)R}}{\mathbb{Z}'_{2R}} = U(1)_{1L} \times U(1)_{2L} \times U(1)_{1R} \times U(1)_{2R}$$

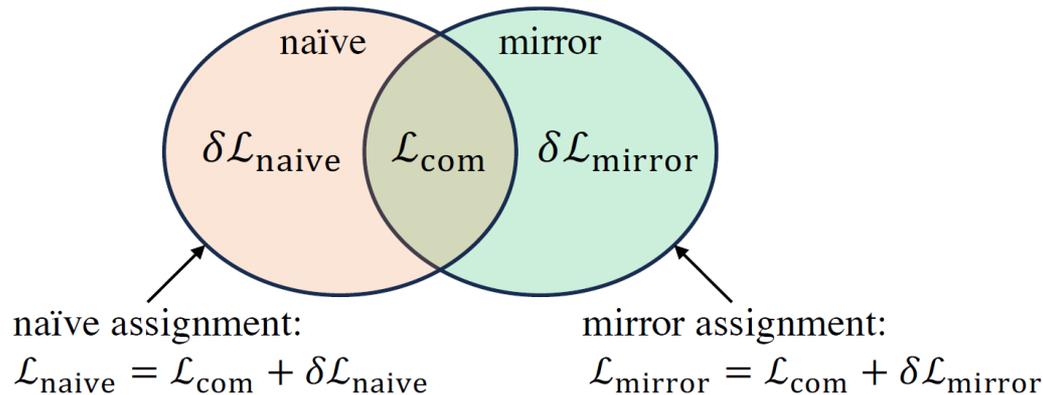
❖ ***Emergent chiral symmetry*** for  $(\psi_1, \psi_2)^t$

$$U(1)_{(1-2)L} \times U(1)_{(1-2)R}$$

❖ Both naïve & mirror as subgroups of ECS

# The Lagrangian w/ ECS

$$\mathcal{L} = \mathcal{L}_{\text{com}} + \delta\mathcal{L}_{\text{naive}} + \delta\mathcal{L}_{\text{mirror}}$$

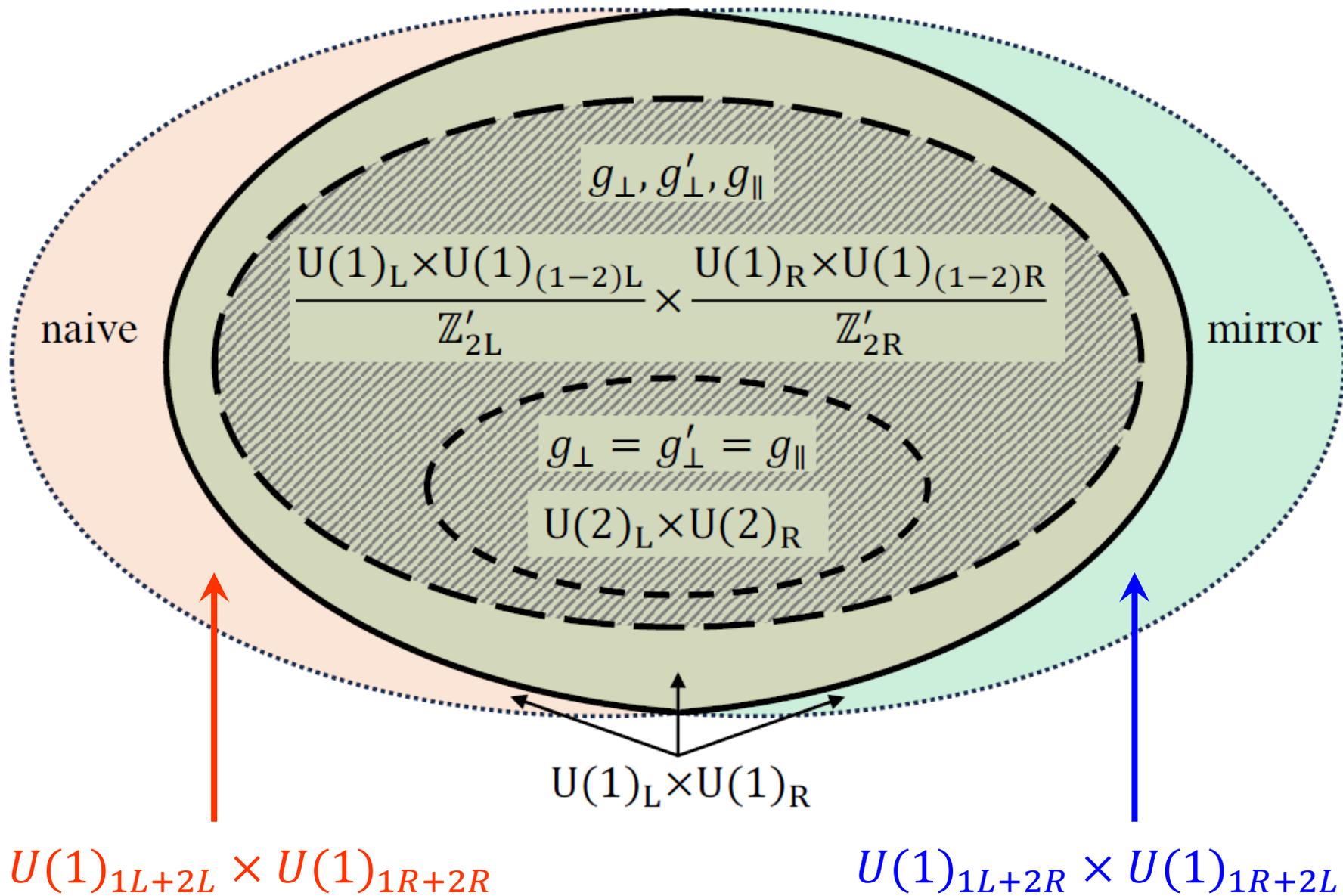


□ Pairing formation  $\rightarrow$  4-point interactions

$$\begin{aligned}\mathcal{L}_{\text{com}} &= \bar{\psi}_1 i\gamma\partial\psi_1 + \bar{\psi}_2 i\gamma\partial\psi_2 \\ &\quad - 4g_{\perp}((\bar{\psi}_1\psi_1)^2 + (\bar{\psi}_1 i\gamma_5\psi_1)^2) - 4g'_{\perp}((\bar{\psi}_2\psi_2)^2 + (\bar{\psi}_2 i\gamma_5\psi_2)^2) \\ &\quad - 8g_{\parallel}((\bar{\psi}_1\psi_2)(\bar{\psi}_2\psi_1) + (\bar{\psi}_1 i\gamma_5\psi_2)(\bar{\psi}_2 i\gamma_5\psi_1)).\end{aligned}$$

□ Special case: 3 equal coupling constants

$\rightarrow SU(2)_L \times SU(2)_R$  emergent chiral sym.



# Mean-field analyses

□ A simplified Lagrangian assuming  $g_{\perp} = g'_{\perp}$

$$\begin{aligned} \mathcal{L}_{\text{com}} = & \bar{\psi} i \gamma \partial \psi - 2g_{\perp} \left( (\bar{\psi} \tau_0 \psi)^2 + (\bar{\psi} \tau_3 \psi)^2 + (\bar{\psi} i \gamma_5 \tau_0 \psi)^2 + (\bar{\psi} i \gamma_5 \tau_3 \psi)^2 \right) \\ & - 2g_{\parallel} \left( (\bar{\psi} \tau_1 \psi)^2 + (\bar{\psi} \tau_2 \psi)^2 + (\bar{\psi} i \gamma_5 \tau_1 \psi)^2 + (\bar{\psi} i \gamma_5 \tau_2 \psi)^2 \right), \end{aligned}$$

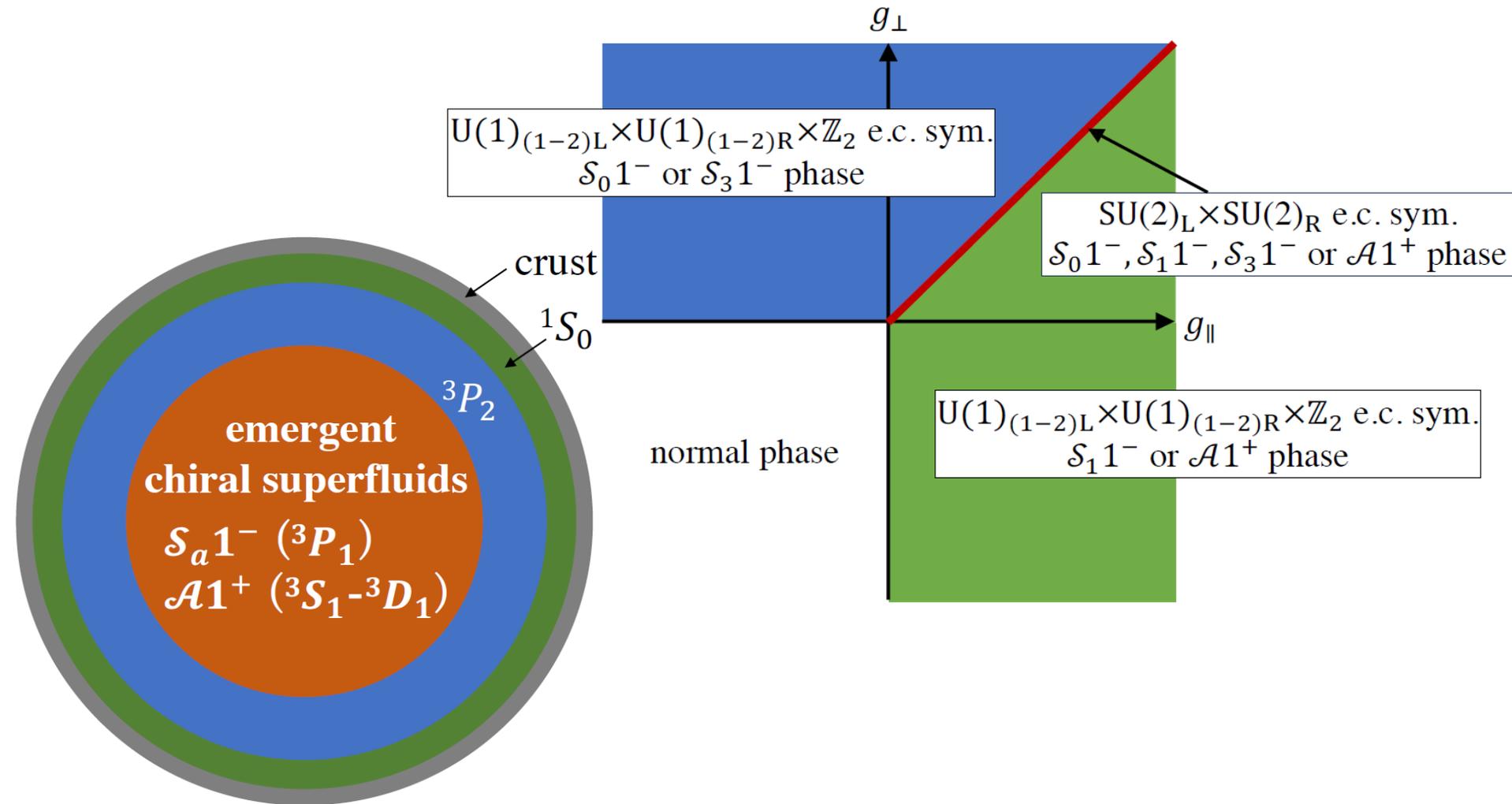
□ Nambu-Gor'kov formalism, mean-field approx. to get the thermodynamic potential

❖ Pairings [note:  $\psi_C = C \gamma^0 \psi^*$ ,  $C = i \gamma^2 \gamma^0$ ]

- $\bar{\psi}_C \vec{\gamma} \gamma_5 \tau_a \psi$  : vector (a=0,1,3), symmetric  $\rightarrow \mathcal{S}_a 1^-$
- $\bar{\psi}_C \vec{\gamma} \tau_2 \psi$  : axial-vector, anti-symmetric  $\rightarrow \mathcal{A} 1^+$

# Phase diagram

□ Cooper pairs: exp. values of  $\mathcal{S}_a 1^-$  and  $\mathcal{A} 1^+$



# Dynamical symmetry breaking

$$\frac{U(1)_L \times U(1)_{(1-2)L}}{\mathbb{Z}'_{2L}} \times \frac{U(1)_R \times U(1)_{(1-2)R}}{\mathbb{Z}'_{2R}} \times SO(3)_S$$

- ❑ Vectorial symmetry  $U(1)_{L+R}$  broken  
→ superfluid phonons
- ❑ Axial symmetry  $U(1)_{L-R}$  unbroken
- ❑ Emergent chiral symmetry broken to  
 $U(1)_{(1-2)(L+R)}$  → emergent pions
- ❑ Spatial rotation symmetry broken to  $SO(2)_S$   
→ magnons
- ❖ NG bosons as sexaquark states w/  $B=2$ : exotic

# Dirac points

□ Single-particle energy with a gap

$$\vec{\delta} = (0, 0, \delta)$$

Dirac points (massless) at  $p_z = \pm\sqrt{\mu^2 + \delta^2}$

$$\varepsilon_q \cong \sqrt{\frac{q_x^2 + q_y^2}{1 + \frac{\mu^2}{\delta^2}} + q_z^2}$$

➤ Propagation along x&y directions in  $v \ll 1$

➤ Propagation along z direction in  $v = c = 1$

→ Anisotropy in transport phenomena, NS cooling

# **SUMMARY**

# Conclusions

- ❑ New types of neutron superfluidity, emergent chiral symmetry breaking & its SSB
- ❑ Toward understanding of multi-quark states in dense QCD
- ❑ Specific in mirror model? Vortices? Cooling? Interface to QM?

**BACKUP**