

Photon-induced interactions in relativistic heavy ion collisions

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TEXAS A&M UNIVERSITY

COMMERCE

SHARE

Gerhard Baur



18 August 2023



(20 January 1944 – 16 June 2023)



The physicist specialized in nuclear reaction theory and nuclear astrophysics.



[Carlos Bertulani](#)

DOI: <https://doi.org/10.1063/PT.6.4o.20230818b>

Gerhard Baur passed away on 16 June 2023 in Stuttgart, Germany, after a long and debilitating disease. He was a distinguished theorist working in nuclear reaction theory at the University of Basel in Switzerland.

Gerhard was born on 20 January 1944 in Stuttgart. In 1970 he earned his PhD from the University of Basel, with work on “Particle vibration coupling and the giant dipole resonance,” mentored by Kurt Alder. From 1971–74 he worked as a postdoc at the Max Planck Institute for Nuclear Physics in Heidelberg, Germany, and in 1974 he was hired as a guest scientist at the Weizmann Institute of Science in Rehovot, Israel. From 1975 to 2009 he had a very productive career as a senior scientist at the Jülich Research Center in Germany.



PHYSICS REPORTS

A Review Section of Physics Letters

ELECTROMAGNETIC PROCESSES IN RELATIVISTIC HEAVY ION COLLISIONS

Carlos A. BERTULANI and Gerhard BAUR

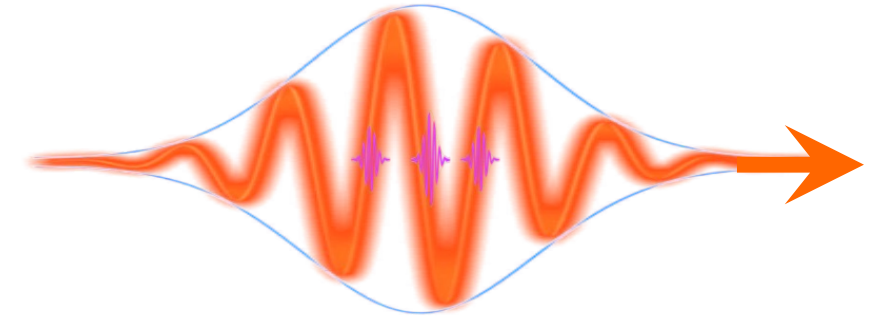
Volume 163 Numbers 5 & 6

June 1988

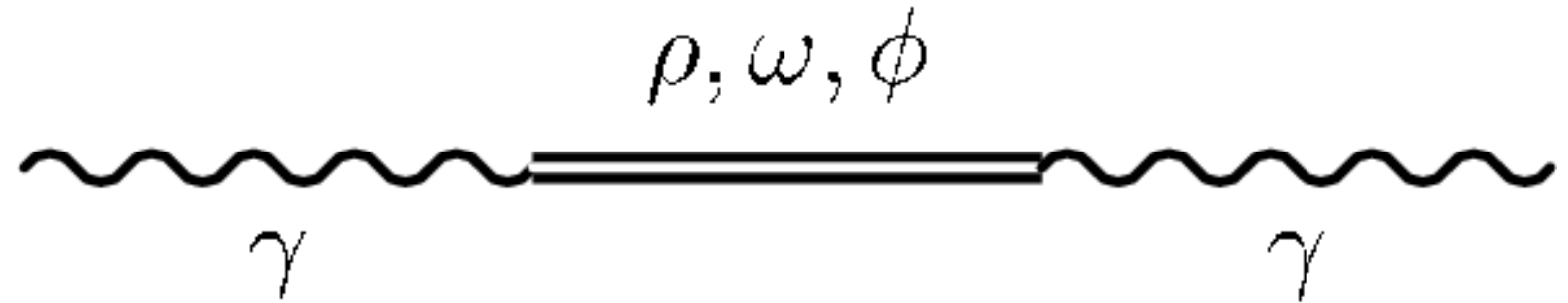
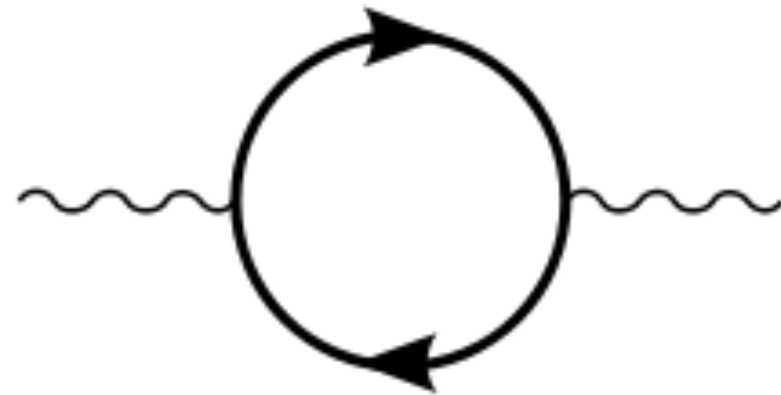
LAST ISSUE OF THIS VOLUME

The clean photon and the dirty photon

* I won't talk about pomeron, dif. dis.



Can fluctuate into particle-antiparticle pairs, e.g., e^+e^- , $q\bar{q}$, etc



$J^P = 1^- \rightarrow$ fluctuates to $\rho, \omega, \phi, J/\Psi$
(Vector meson dominance model)

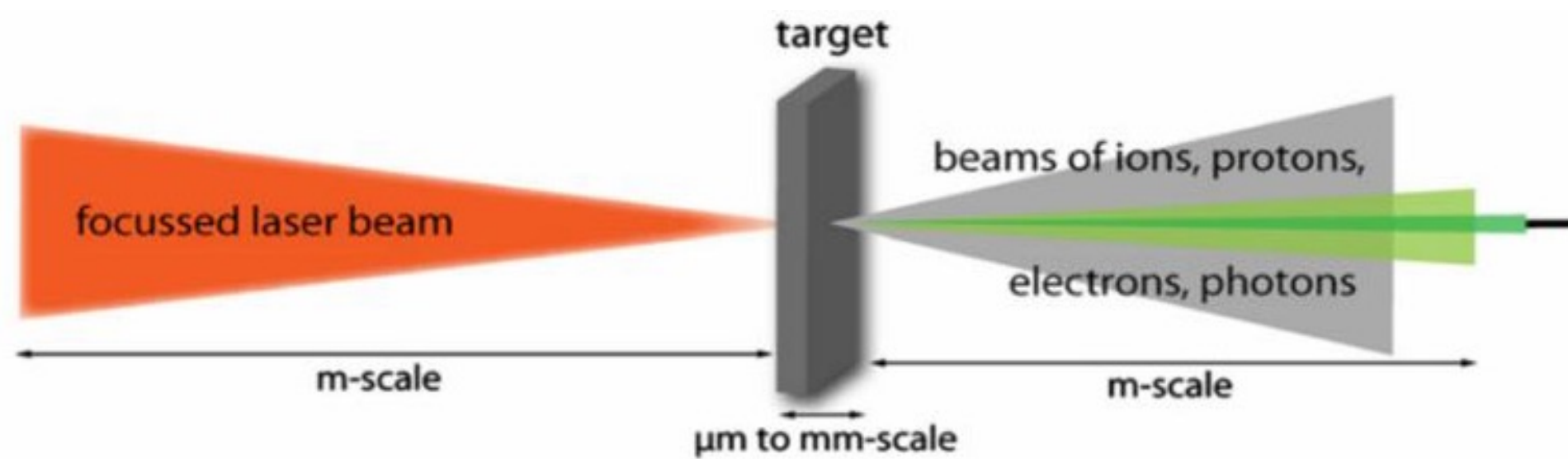
Photon wavefunction:

$$|\gamma\rangle = C_{\text{bare}} |\gamma_{\text{bare}}\rangle + C_{\rho} |\rho\rangle + C_{\omega} |\omega\rangle + C_{\phi} |\phi\rangle + \dots + C_q |q\bar{q}\rangle$$

The photon as a probe

Real photons

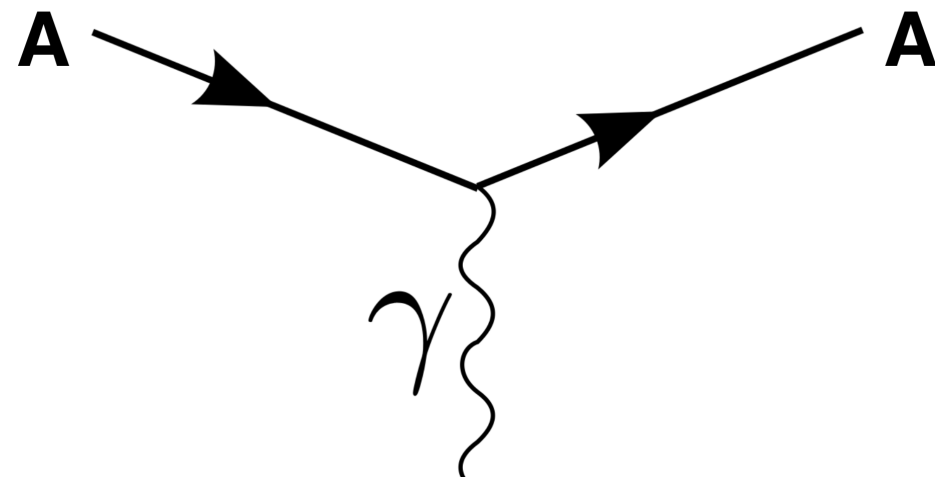
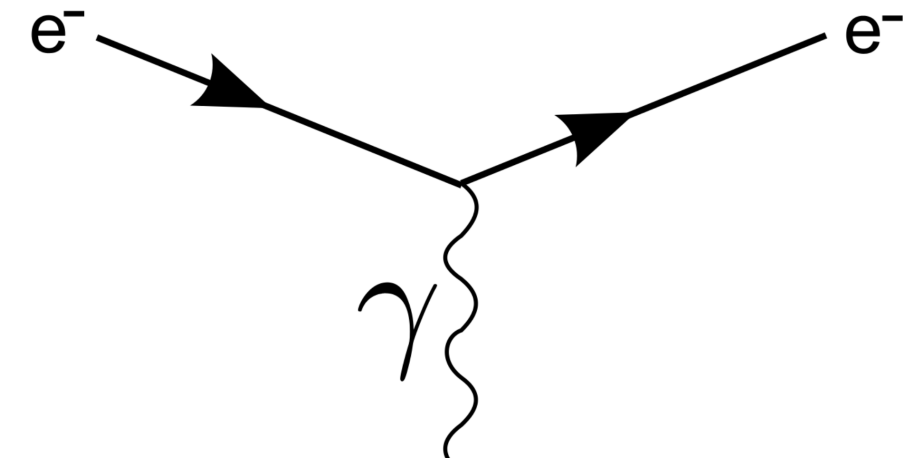
High output lasers



Virtual photons

$$\sigma(\Delta E, |\Delta \mathbf{p}| \neq \Delta E)$$

JLAB, EIC



Quasi real photons

RHIC, CERN (UPC)

$$\sigma(\Delta E, |\Delta \mathbf{p}| \sim \Delta E)$$

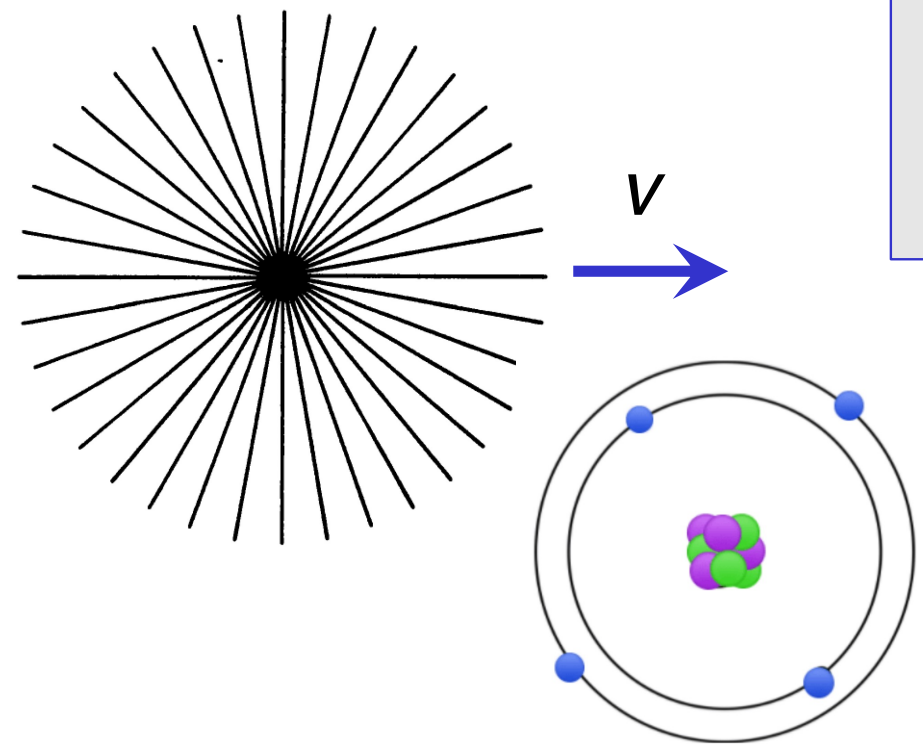
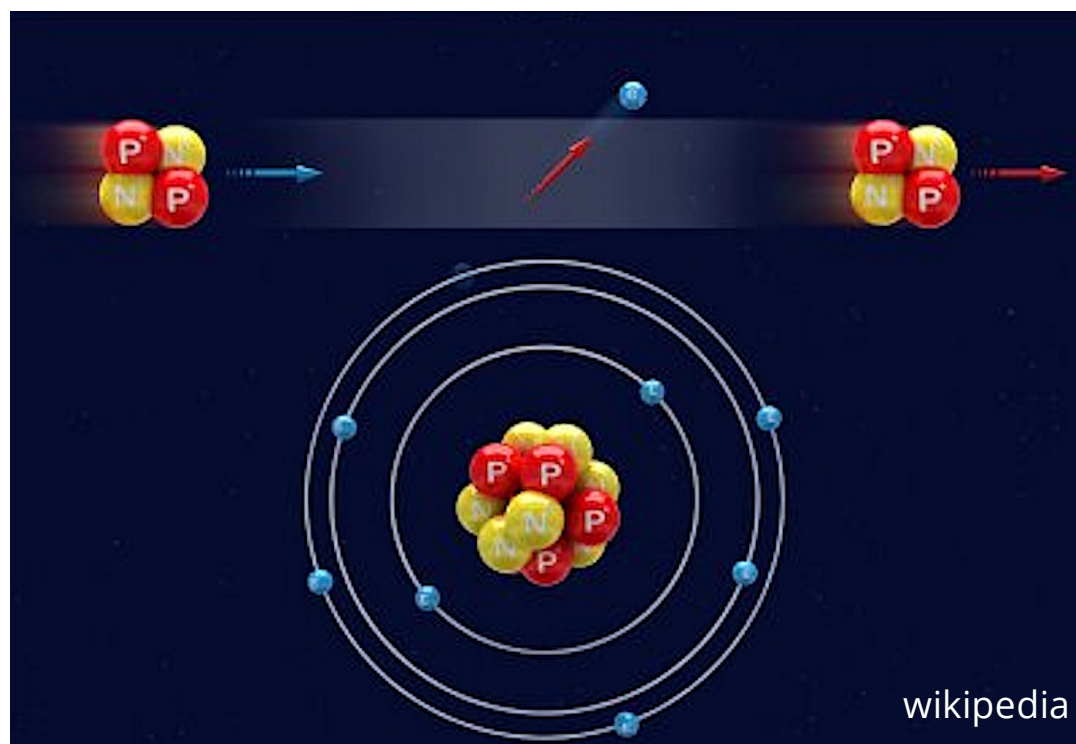
Atomic ionization by α -particles (1924)

Fermi's method:

(a) calculate energy content of time-dependent EM field of α -particle

$$I(\omega) = \frac{c}{4\pi} |\mathbf{E}(\omega) \times \mathbf{B}(\omega)|$$

(b) Multiply $I(\omega)$ by photoionization cross section



$$P(b) = \int I(\omega, b) \sigma_{ph}(\omega) d\omega = \int \frac{N(\omega, b)}{\omega} \sigma_{ph}(\omega) d\omega$$

α -particle in a straight-line motion \rightarrow

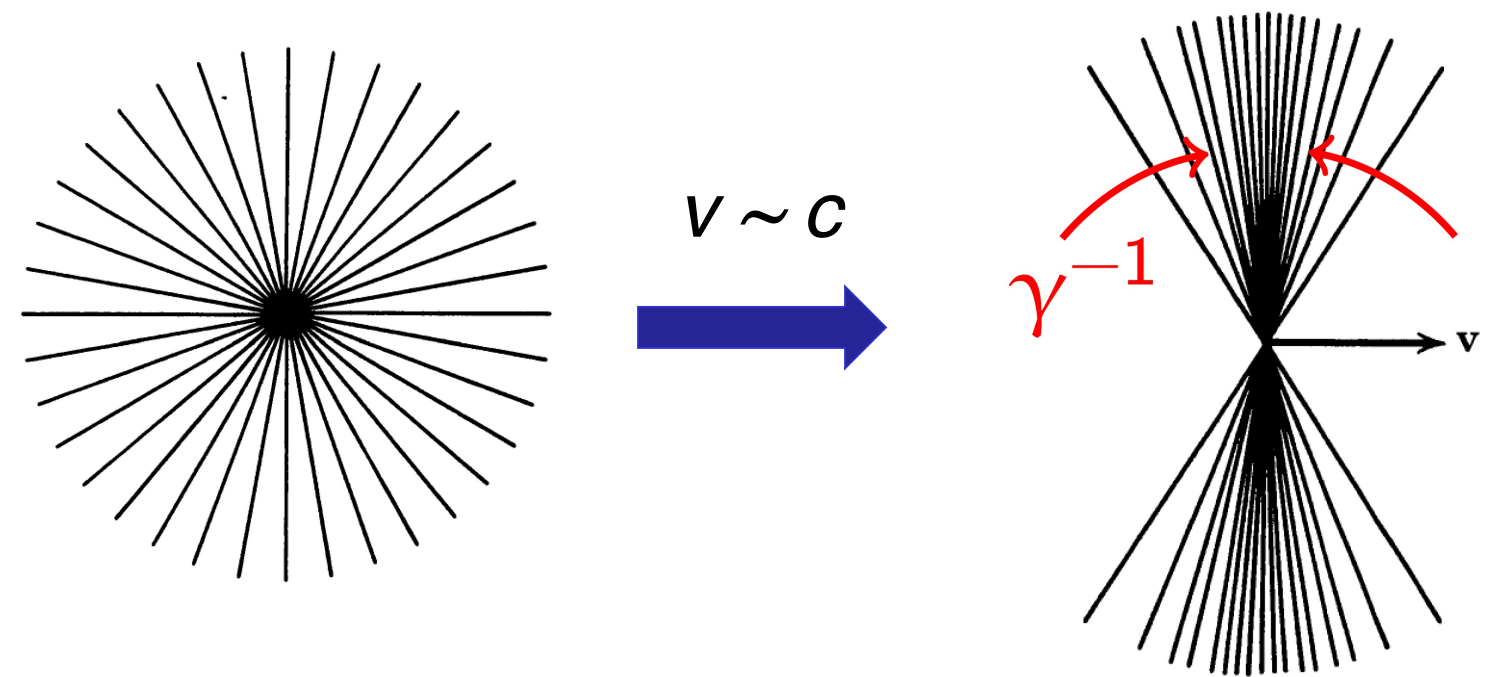
$$N(\omega, b) = \left(\frac{Zec}{\pi v} x \right)^2 [K_1^2(x) + K_0^2(x)], \quad x = \frac{\omega b}{v}$$

E. Fermi, Z. Phys. 29, 315 (1924)

E. Fermi Nuovo Cimento 2, 143 (1925)

Lorentz contraction

Weizsäcker & Williams:
 (a) Use Fermi's method
 (b) Include Lorentz contraction



$$N(\omega, b) = \left(\frac{Zec}{\pi v} x \right)^2 [K_1^2(x) + K_0^2(x)] \quad \text{Fermi} \quad \longrightarrow \quad \text{Weizsäcker \& Williams}$$

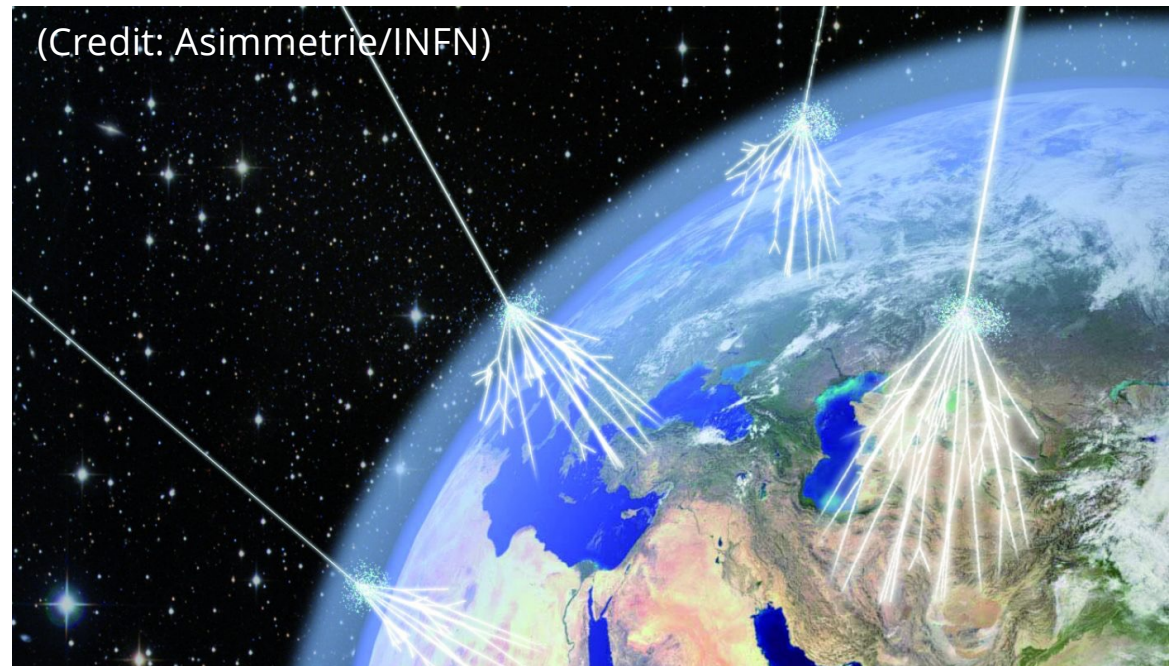
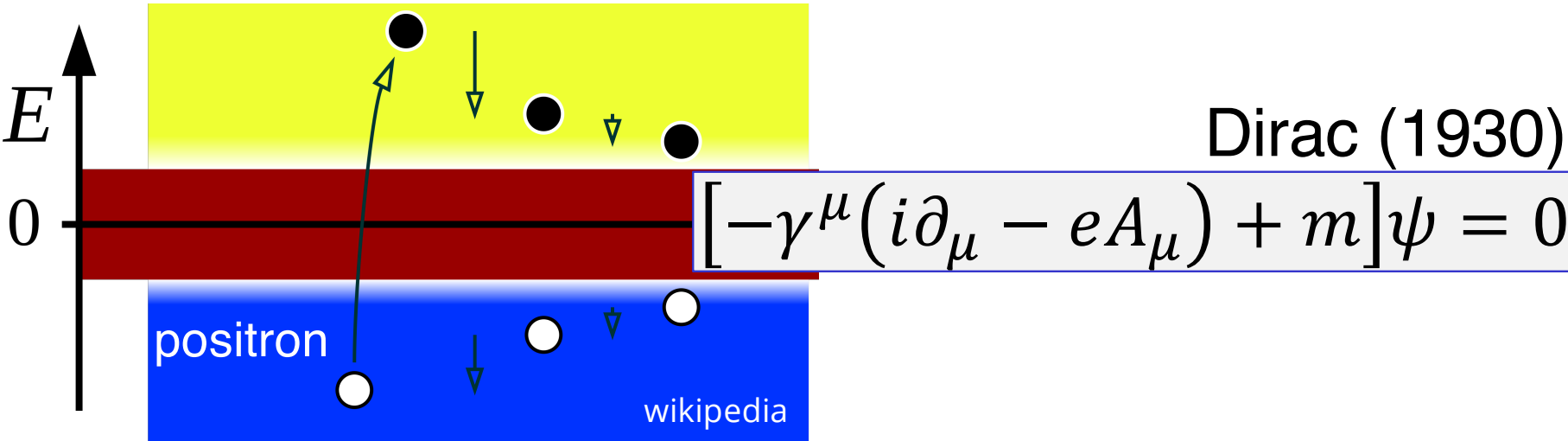
$$N(\omega, b) = \left(\frac{Zec}{\pi v} x \right)^2 \left[K_1^2(x) + \frac{1}{\gamma^2} K_0^2(x) \right], \quad x = \frac{\omega b}{\gamma v}$$

C.F. Weizsäcker, Z. Phys. 88, 612 (1934)

E.J. Williams, Phys. Rev. 45, 729 (1934)

Next 50 years \rightarrow applications in atomic, nuclear, but mainly in particle physics
 Known as the *equivalent photon method* and N the *equivalent photon numbers*

Do antiparticles exist? (1930s)



Search in cosmic rays → no QFT, no QED,
no Feynman diagrams → **brute force QM**

$\psi = \psi_- + \psi_+ = \psi_0 + \psi_1 + \dots$
 Perturbation theory
 $[-i\gamma^\mu\partial_\mu + m]\psi_n = -e \gamma^\mu A_\mu \psi_{n-1}$

W.H. Furry and J.F. Carlson, Phys. Rev. 44, 238 (1933)

L.D. Landau and E.M. Lifshitz, Phys. Zs. Sowjet. 6, 244 (1934)

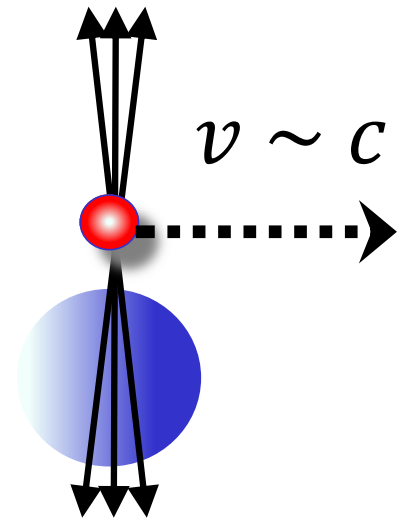
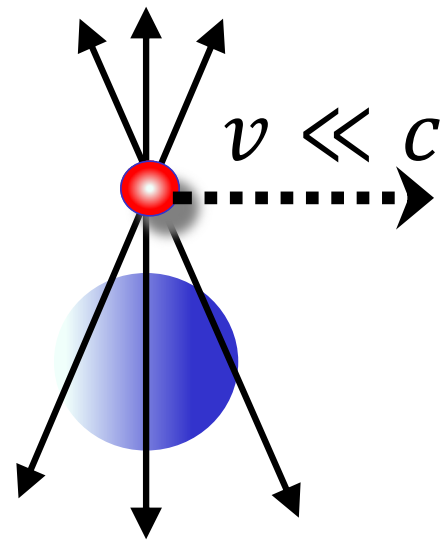
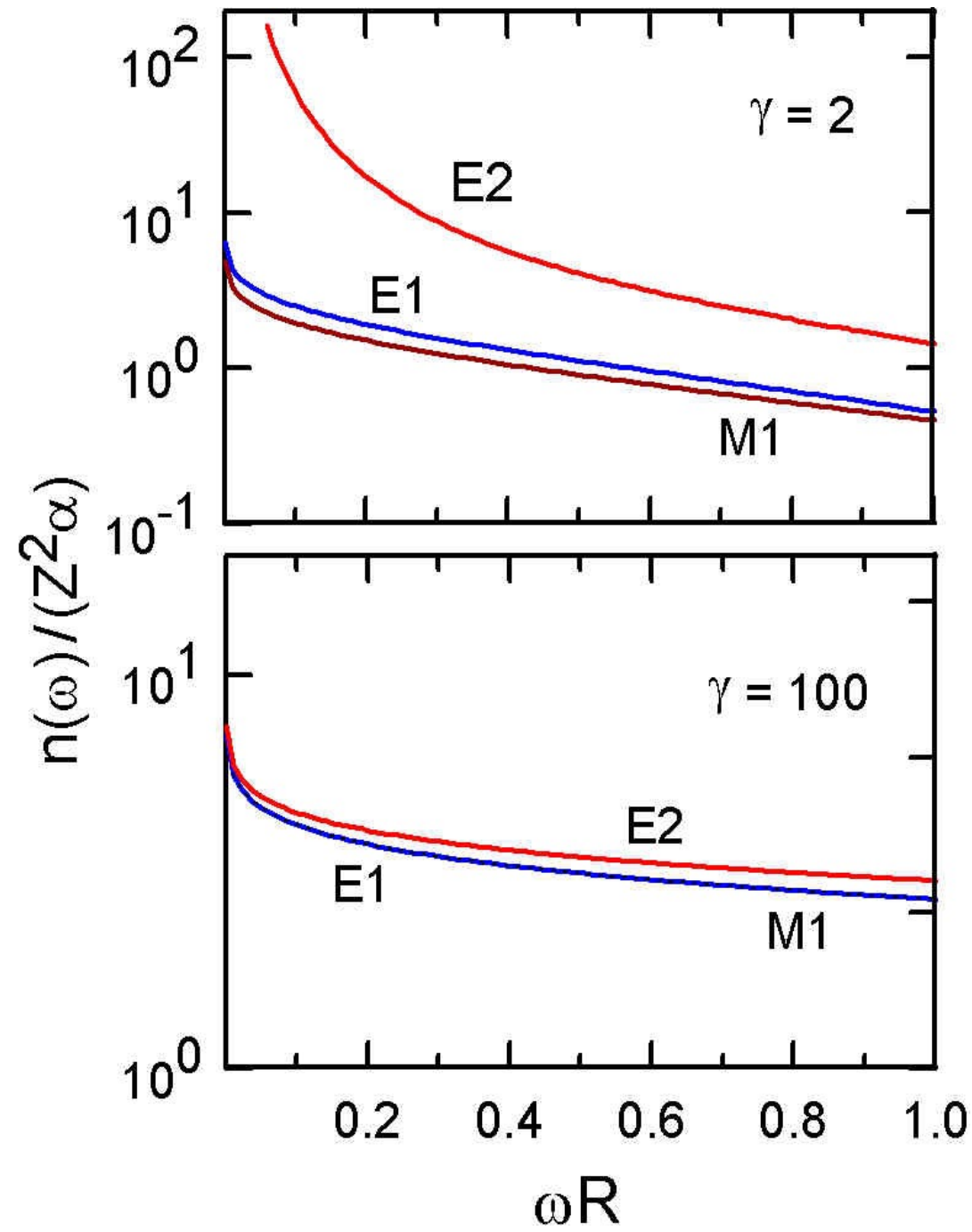
H.J. Bhabha, Proc. R. Soc. London Ser. A 152, 559 (1935)

Y. Nishina, S. Tomonaga and M. Kobayashi, Sci. Pap. Inst. Phys. Chem. Res. 27, 137 (1935)

G. Racah, Nuovo Cimento 14, 93 (1937)

$$\sigma_{e^+e^-} = \frac{28}{27\pi} \left(\frac{Z_1 Z_2 e^4}{m_e} \right)^2 \left[\ln^3 \left(\frac{0.681\gamma}{2} \right) + \mathcal{O}(\ln^2) \right]$$

50 years forward (1985): GSI, RHIC, CERN → UPC



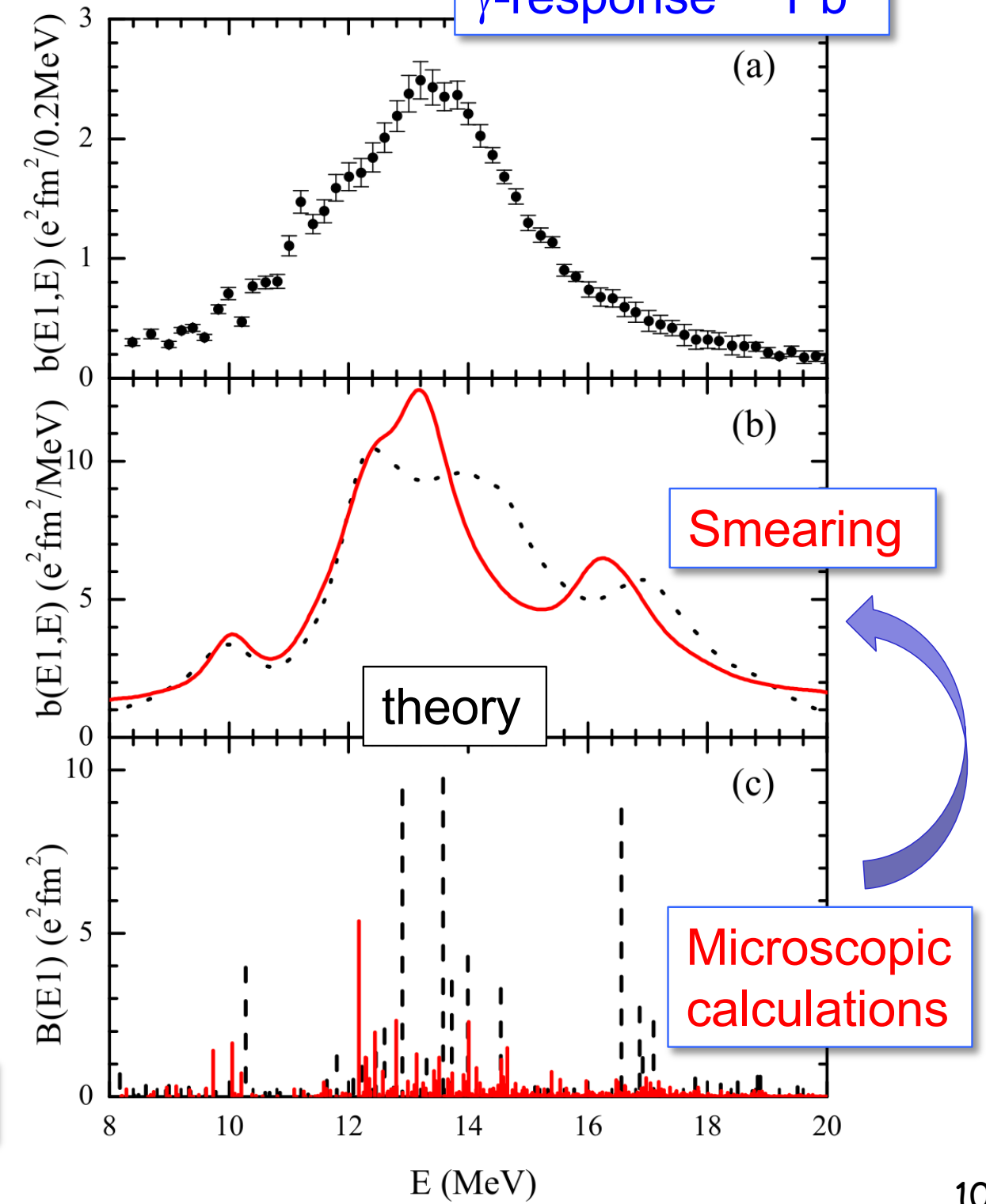
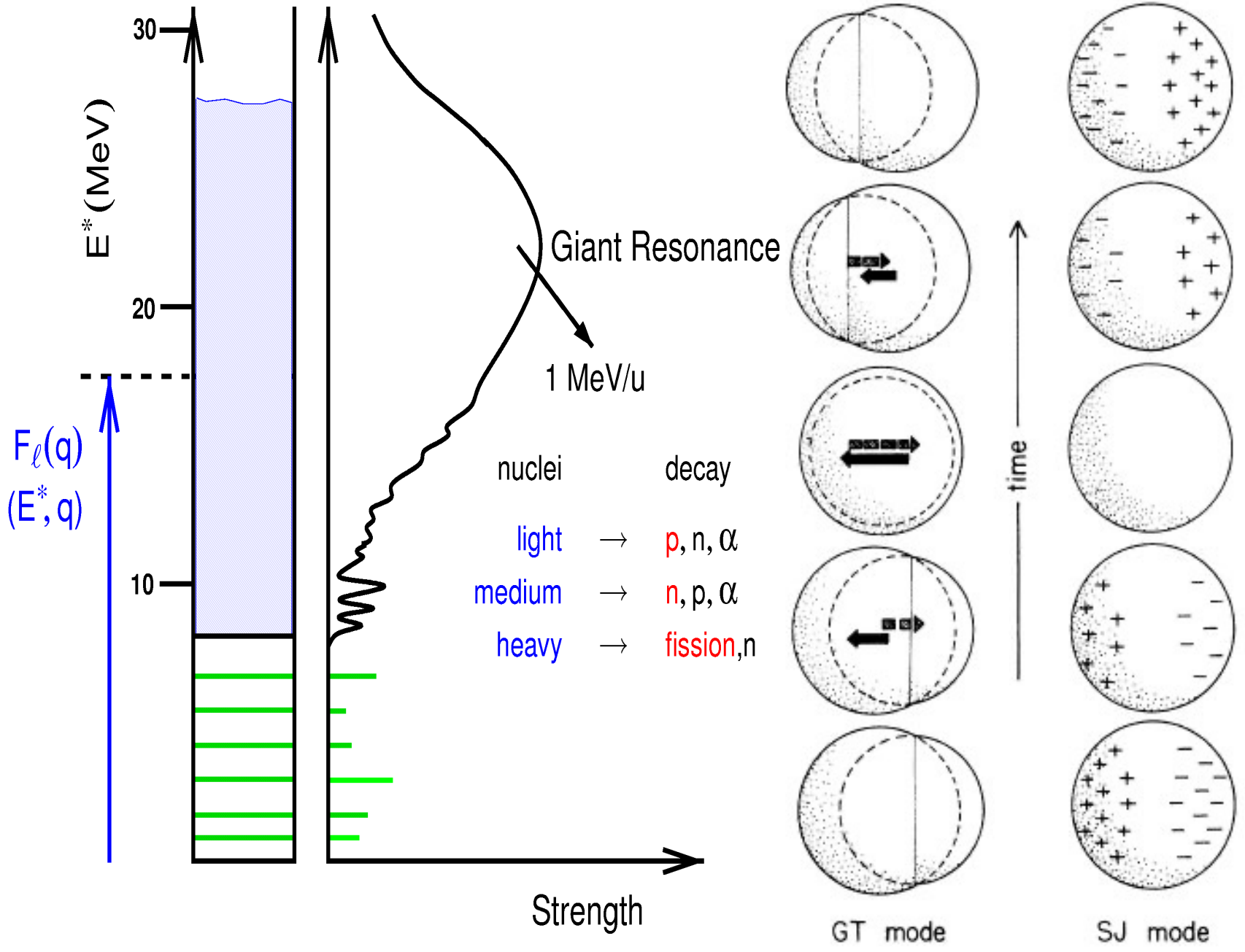
low-energy (tidal)
 $n_{E2} \gg n_{E1} \gg n_{M1} = \frac{v^2}{c^2} n_{E1}$
 high-energy (contraction)
 $n_{E2} \sim n_{E1} \sim n_{M1}$

CB, Baur,
 NPA 442, 739 (1985)
 Phys. Rep. B 163, 299 (1988)

$$n(\omega, b) = \frac{2Z^2\alpha\omega^2}{\pi\gamma^2} \left[K_1^2\left(\frac{\omega b}{\gamma}\right) + \frac{1}{\gamma^2} K_0^2\left(\frac{\omega b}{\gamma}\right) \right] S_{\text{absorption}}(b)$$

Giant resonances in nuclei (1960s-1970s)

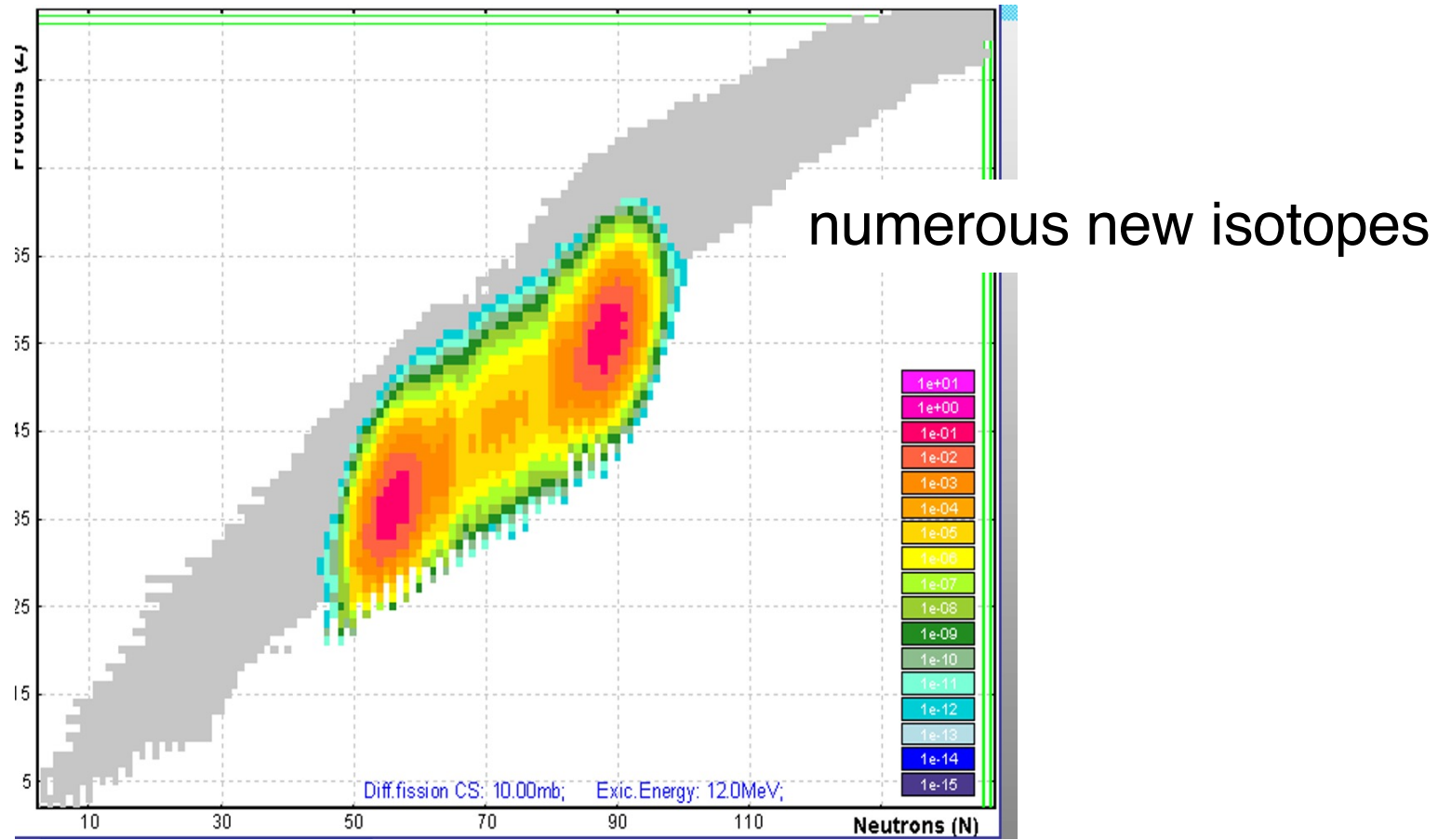
Experiment:
 γ -response ^{208}Pb



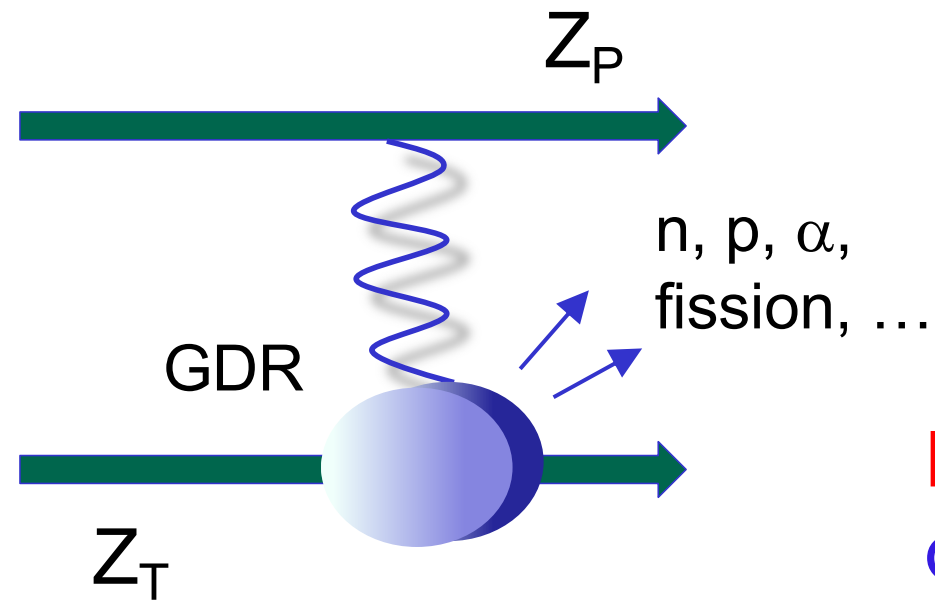
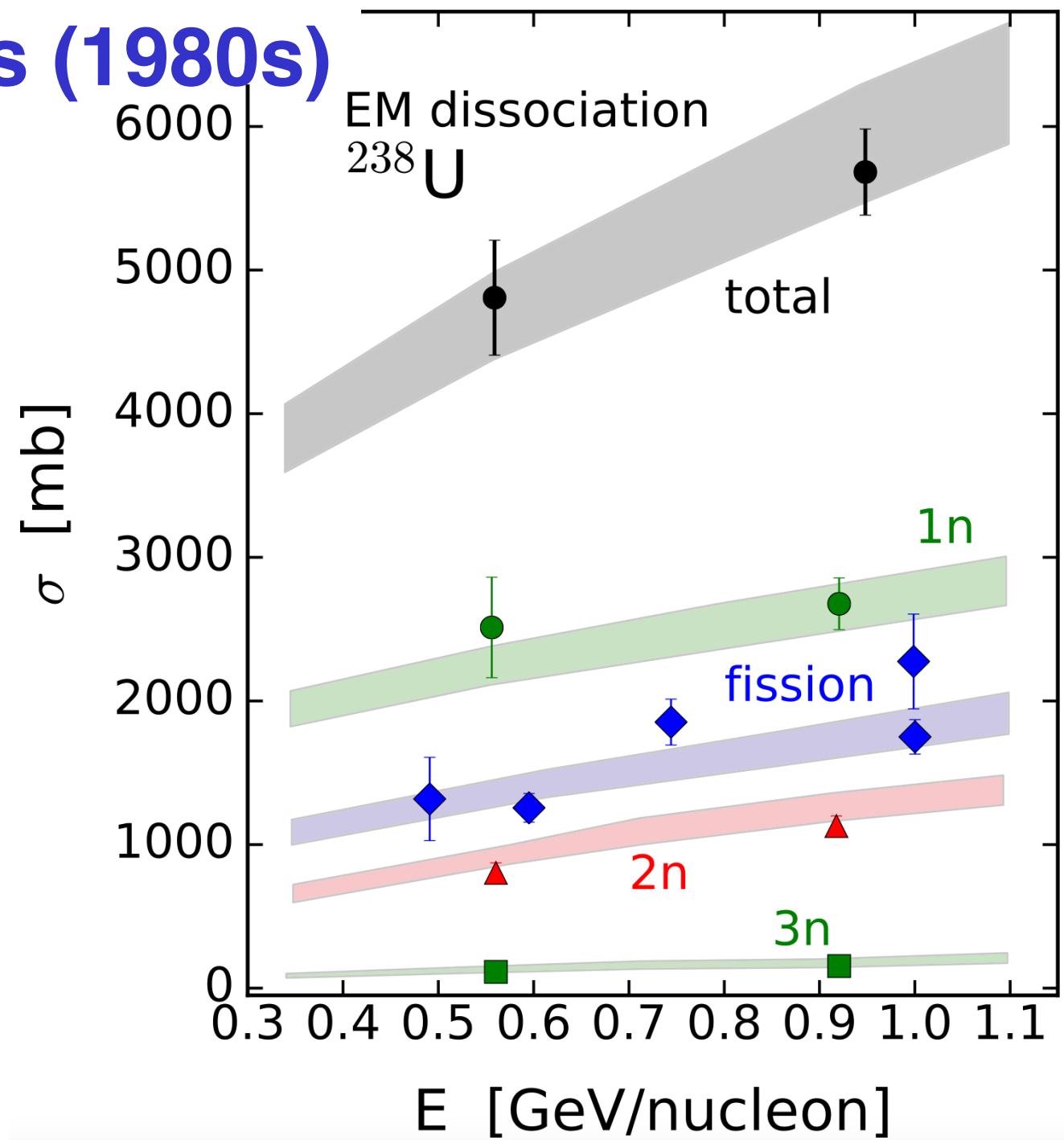
A. Bohr, B. Mottleson, J. Rainwater
 Nobel prize 1975

hydrodynamical models

UPC excitation of giant resonances (1980s)



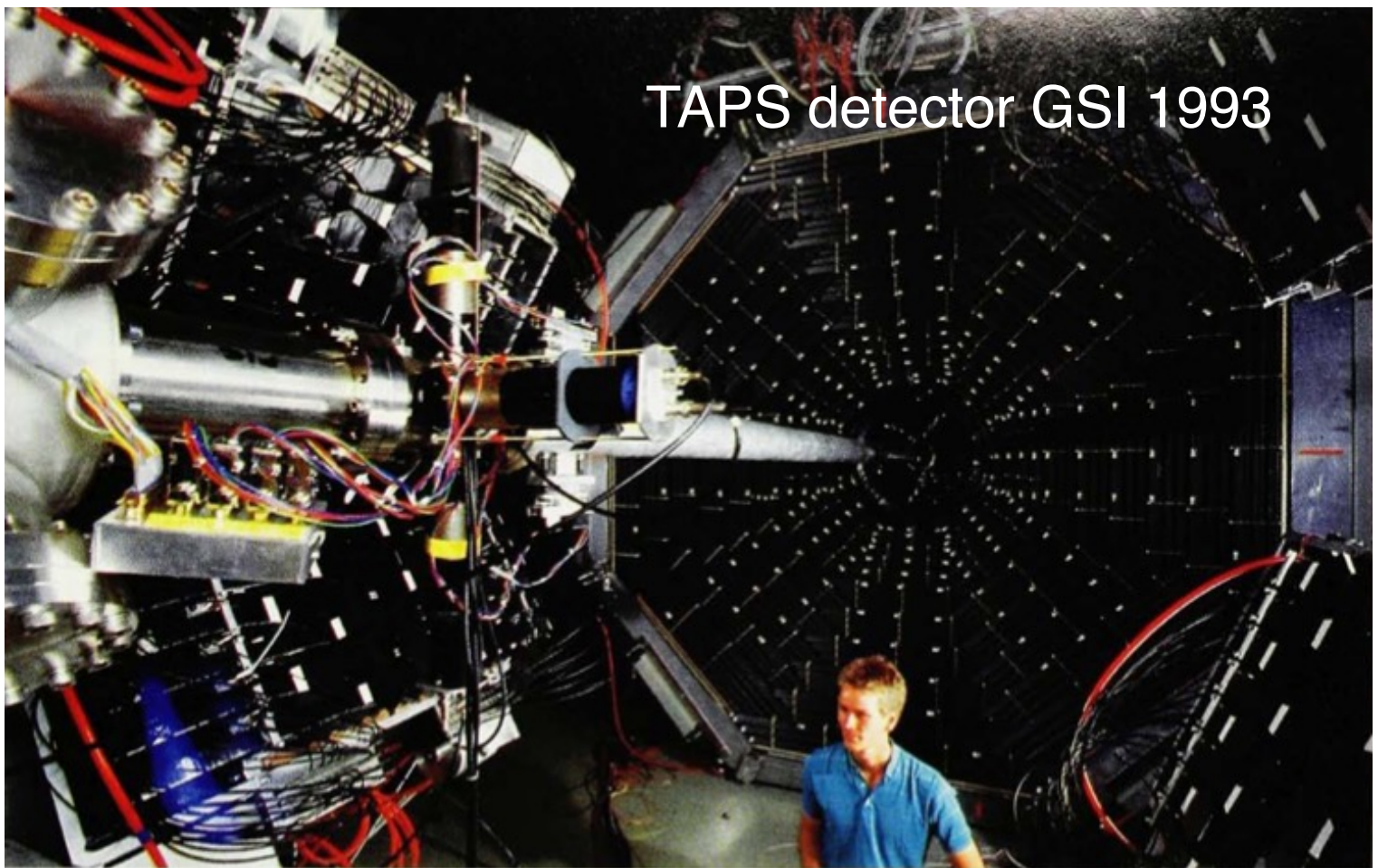
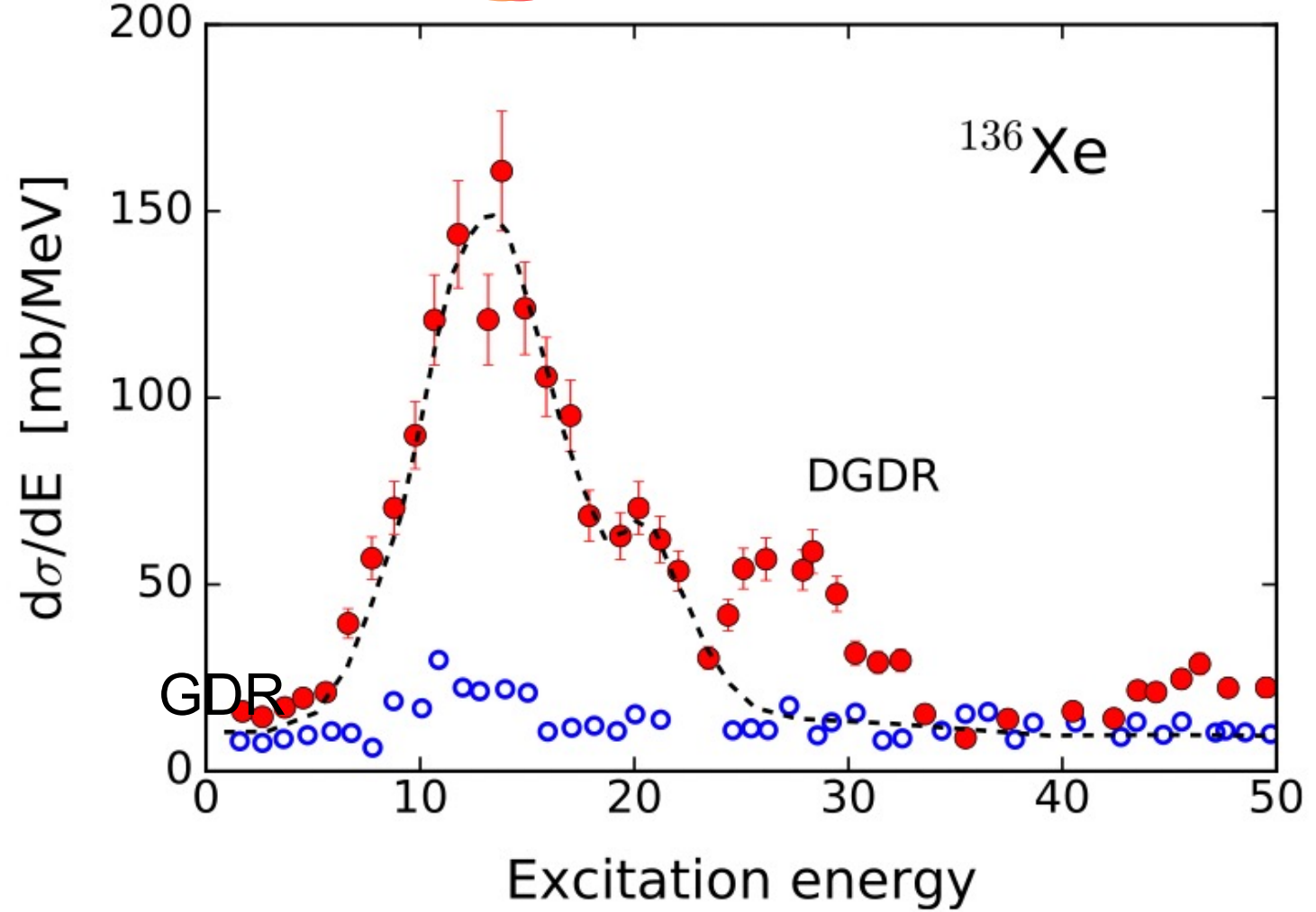
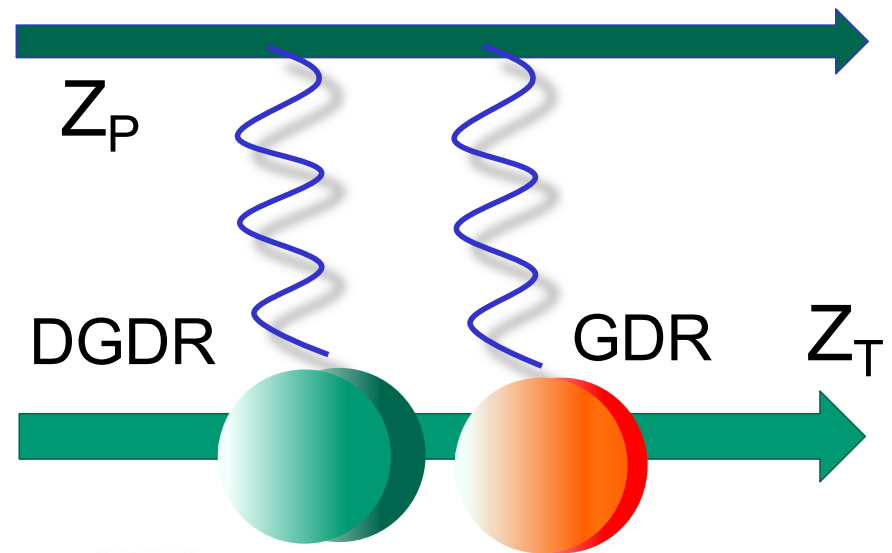
numerous new isotopes



Excitation of multiple giant resonances (prediction)

G. Baur and CB, Nucl. Phys. A482, 313 (1988)

Double giant dipole resonance (1990s)



Experimentally found

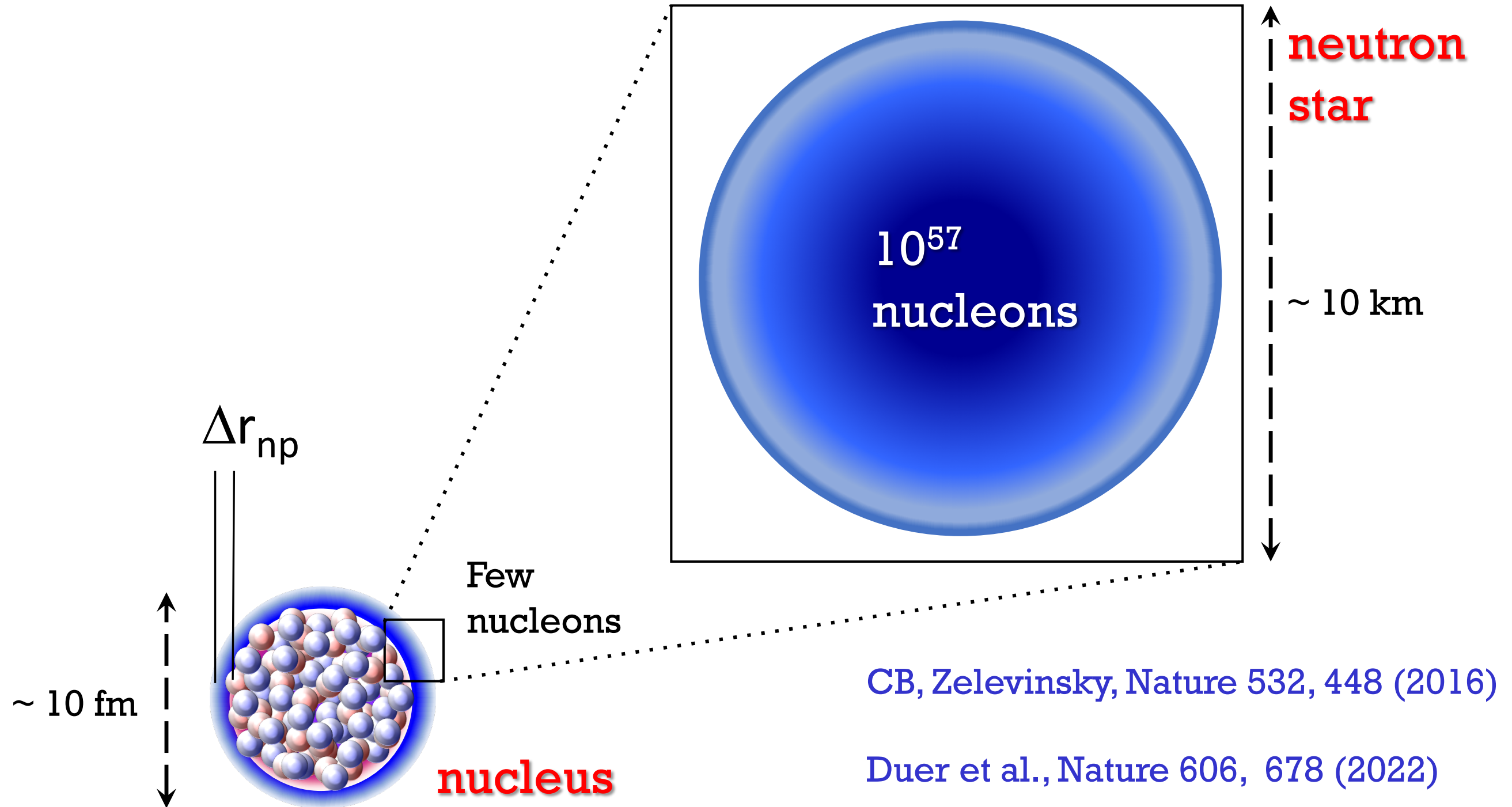
[R. Schmidt *et al.*, PRL 70, 1767 \(1993\)](#)

[J. Ritman *et al.*, PRL 70, 533 \(1993\)](#)

Tests of nuclear microscopic theory

[CB, V. Ponomarev, Phys. Reports 321, 139 \(1999\)](#)

EM nuclear response and neutron stars



Neutron stars

EOS

$$p[\rho] = \rho^2 \frac{d}{d\rho} \left(\frac{E}{A}[\rho] \right)$$

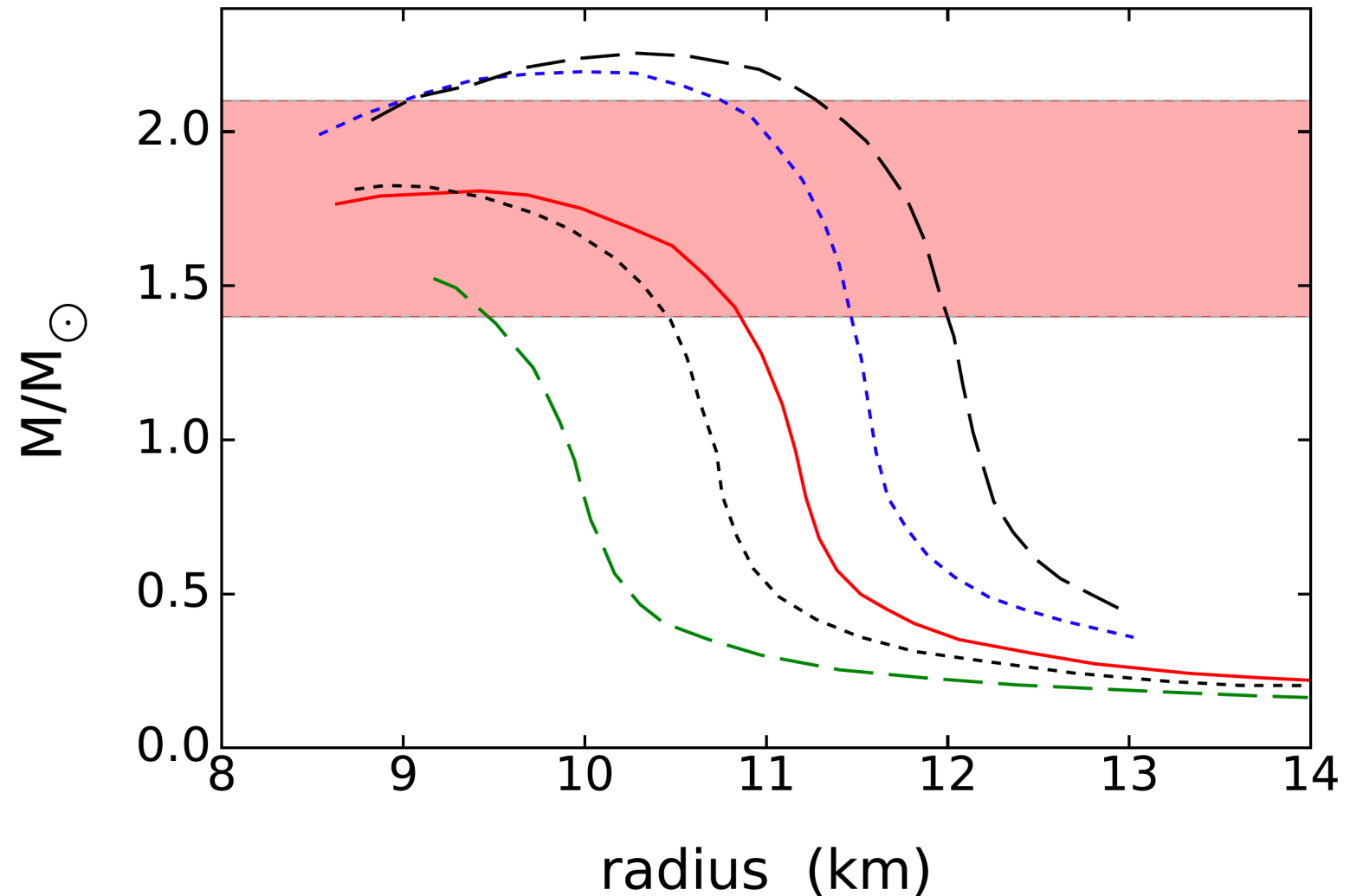
$$\frac{E}{A}[\rho] = \frac{E}{A}[\rho_0] + \frac{1}{18} K_\infty \left(\frac{\rho - \rho_0}{\rho_0} \right)^2 + \dots$$

$$K_\infty = 9\rho_0^2 \left. \frac{d^2 [E/A]}{d\rho^2} \right|_{\rho_0}$$

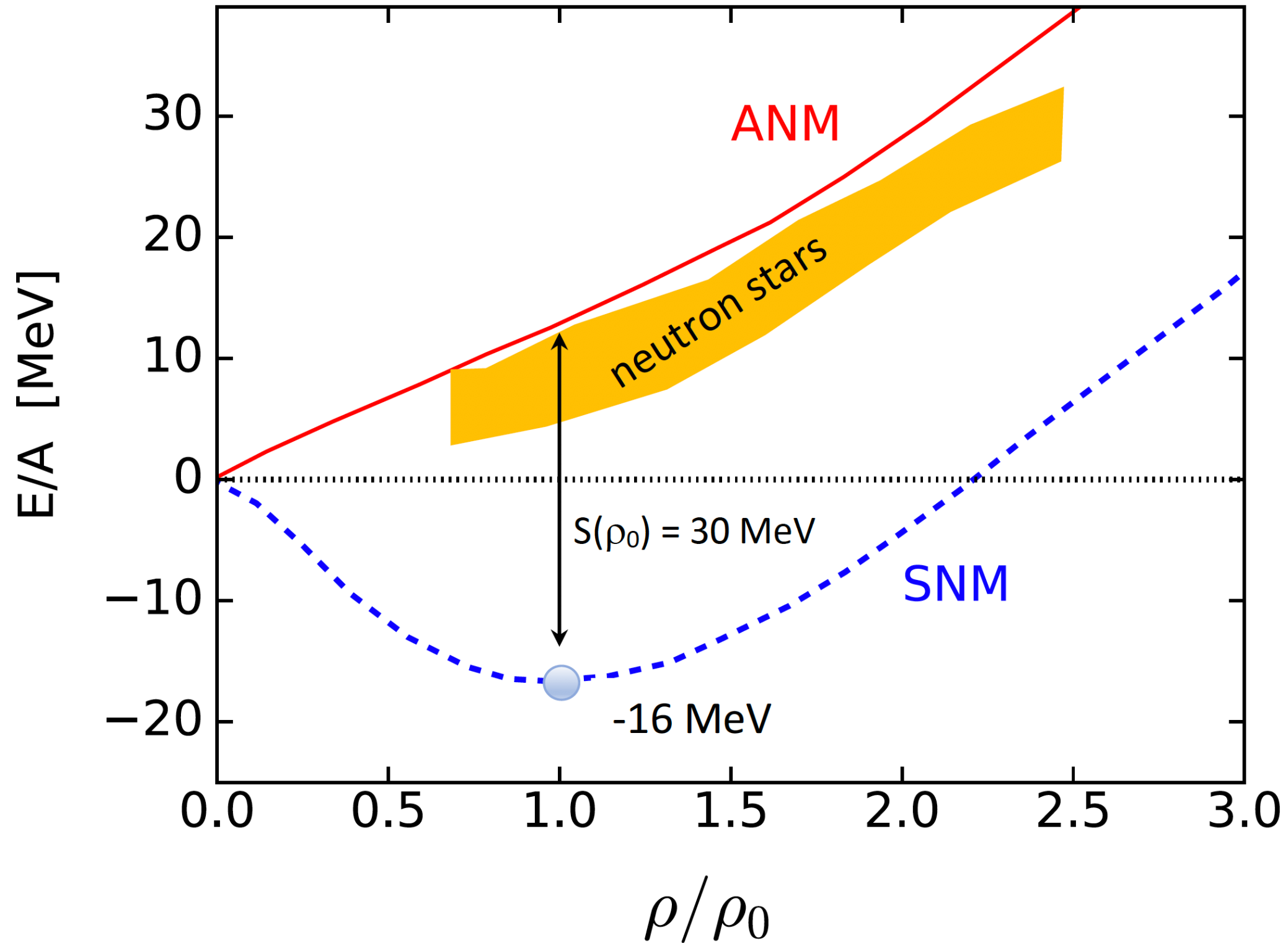
$$\frac{dP}{dr} = - \frac{G\rho(r)M(r)}{r^2} \left[1 + \frac{P(r)}{\rho(r)} \right] \left[1 + \frac{4\pi r^3 P(r)}{M(r)} \right] \left[1 - \frac{2GM(r)}{r} \right]^{-1}$$

$$\frac{dM}{dr} = 4\pi r^2 \rho(r)$$

Tolman-Oppenheimer-Volkoff

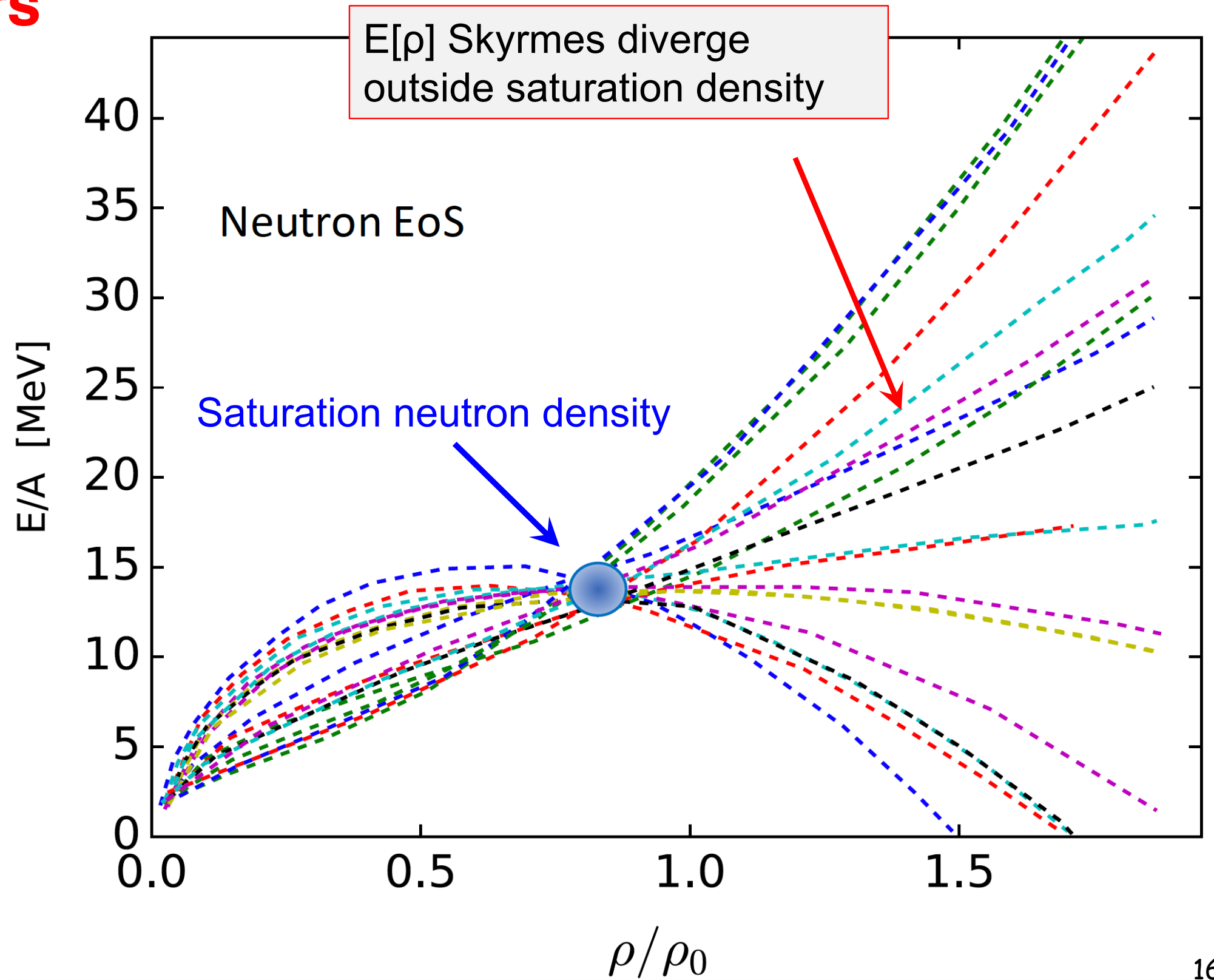


EOS of neutron stars



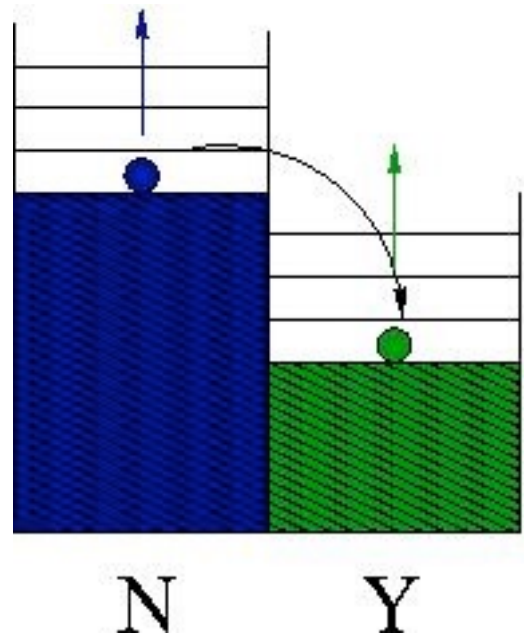
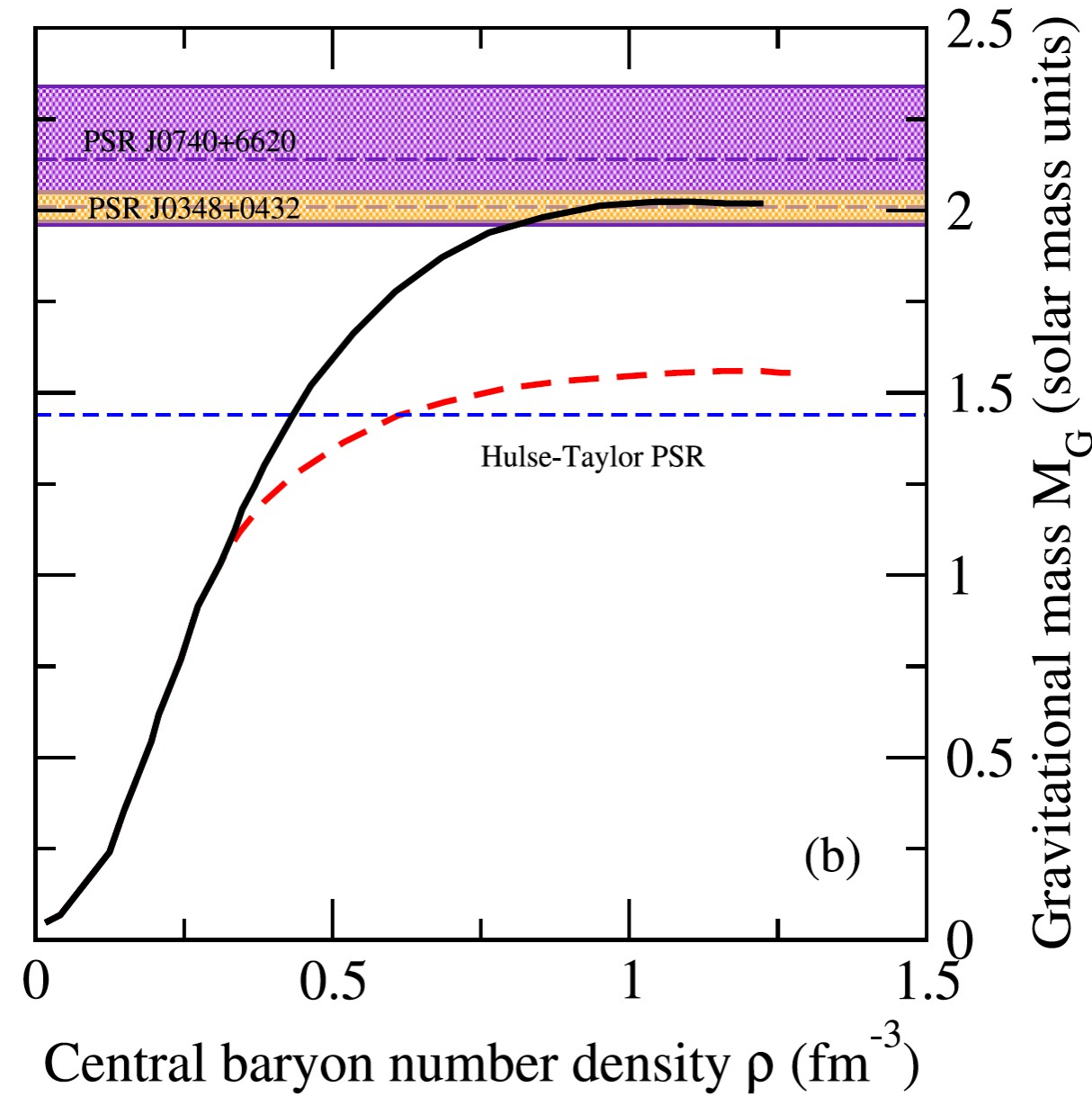
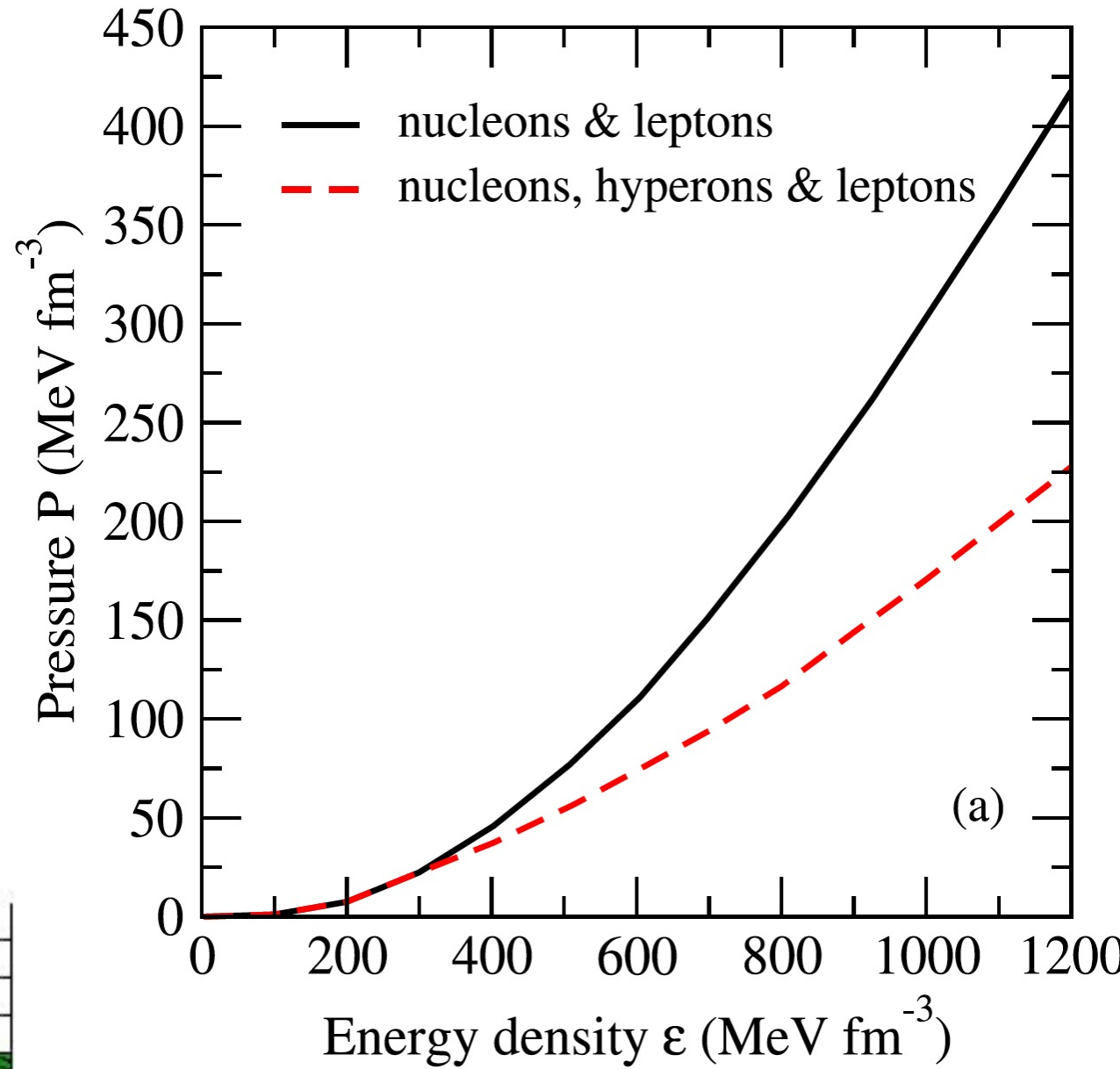
EOS & Neutron stars

Pethick, Ravenhall,
ARNPS 45 (1995) 429



Hyperons and neutron stars

Hyperons make the EoS softer → reduction of the mass



Hyperon "puzzle"

Tolos, Fabbietti, PPNP 112 103770 (2020)

Nuclear astrophysics

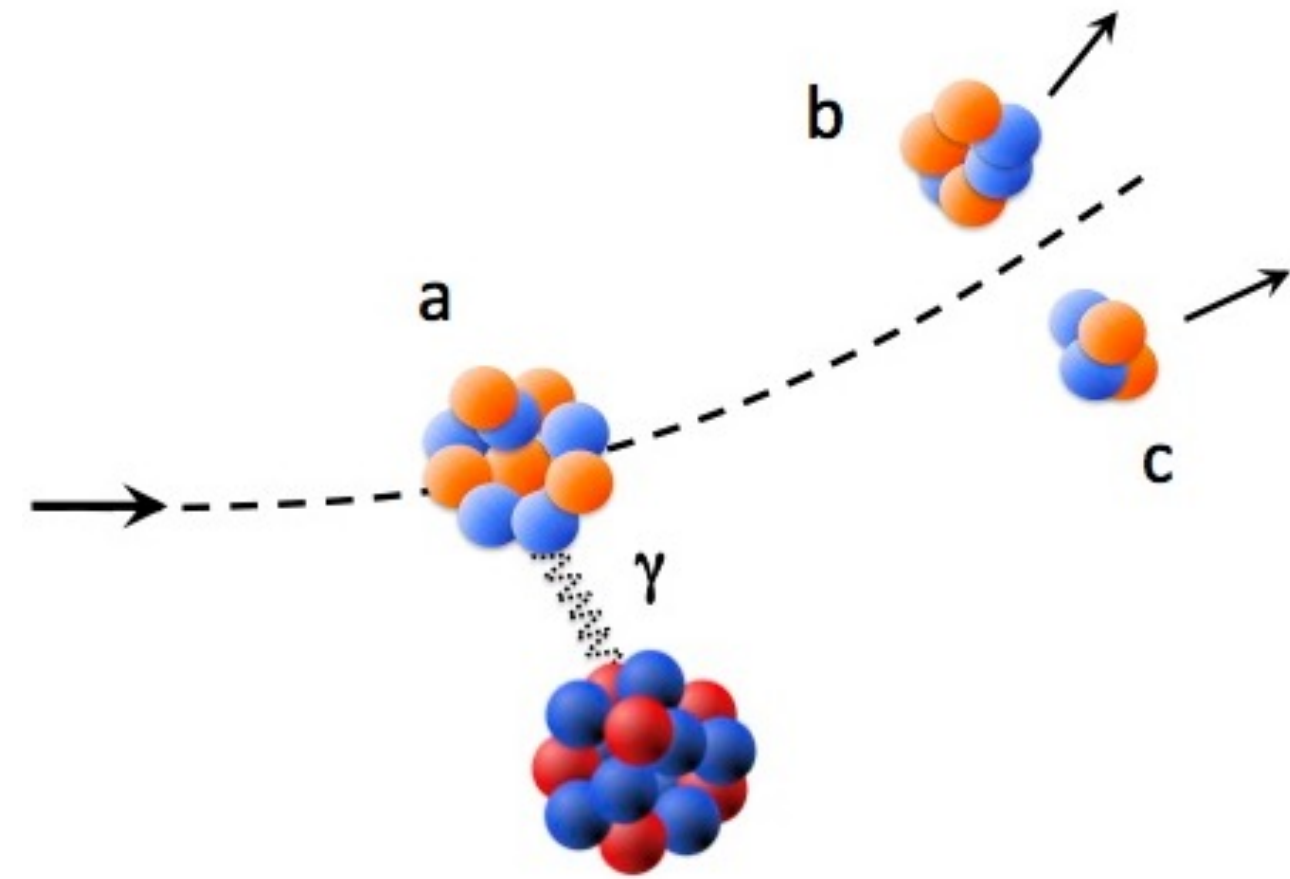
Baur, CB, Rebel, NPA (1986)

$$\frac{d\sigma}{dE_\gamma d\Omega} = \frac{1}{E_\gamma} \sum_1 \frac{dn_1(E_\gamma, \Omega)}{dE_\gamma d\Omega} \sigma_{\gamma + a \rightarrow b + c}(E_\gamma)$$

Theory

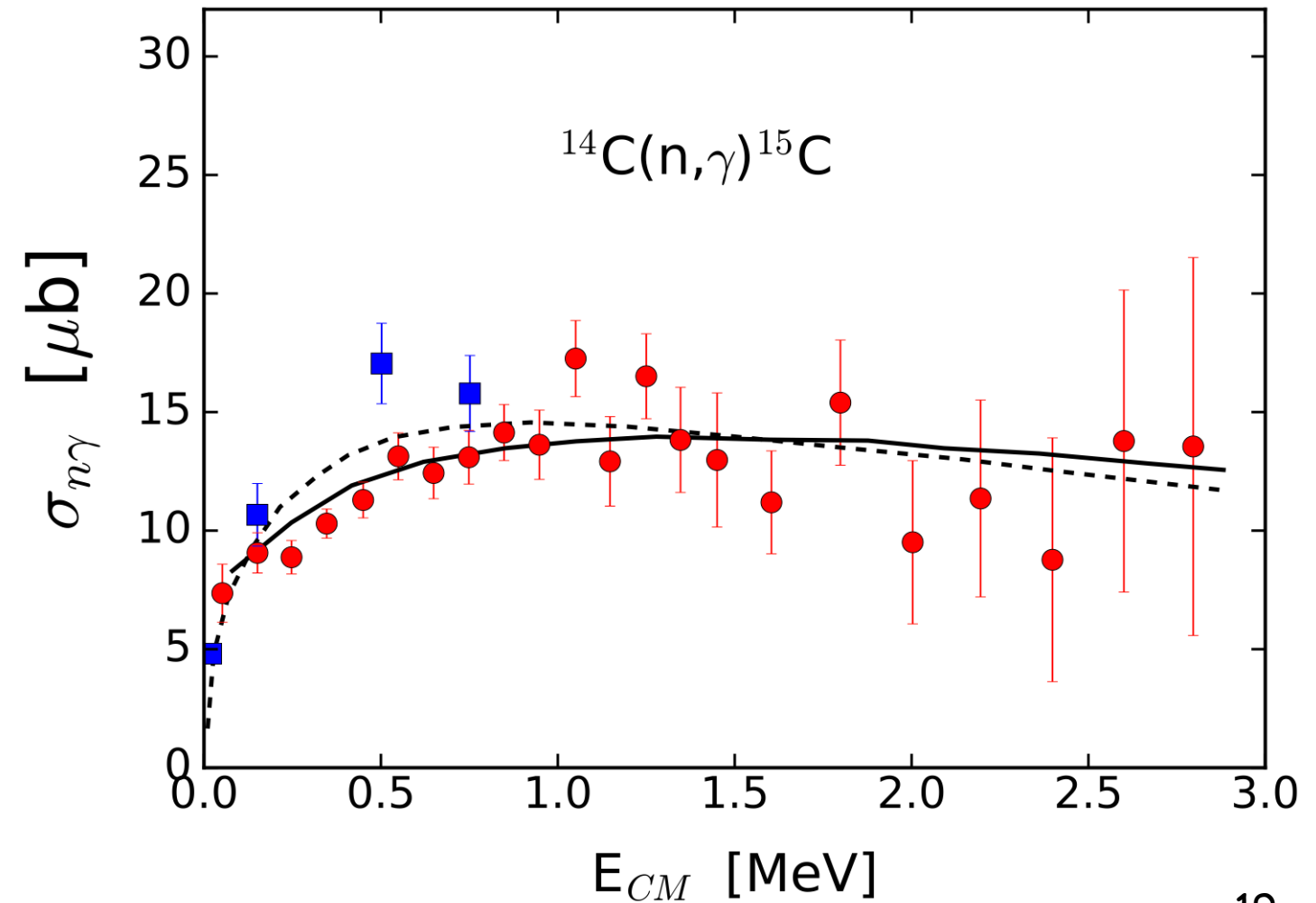
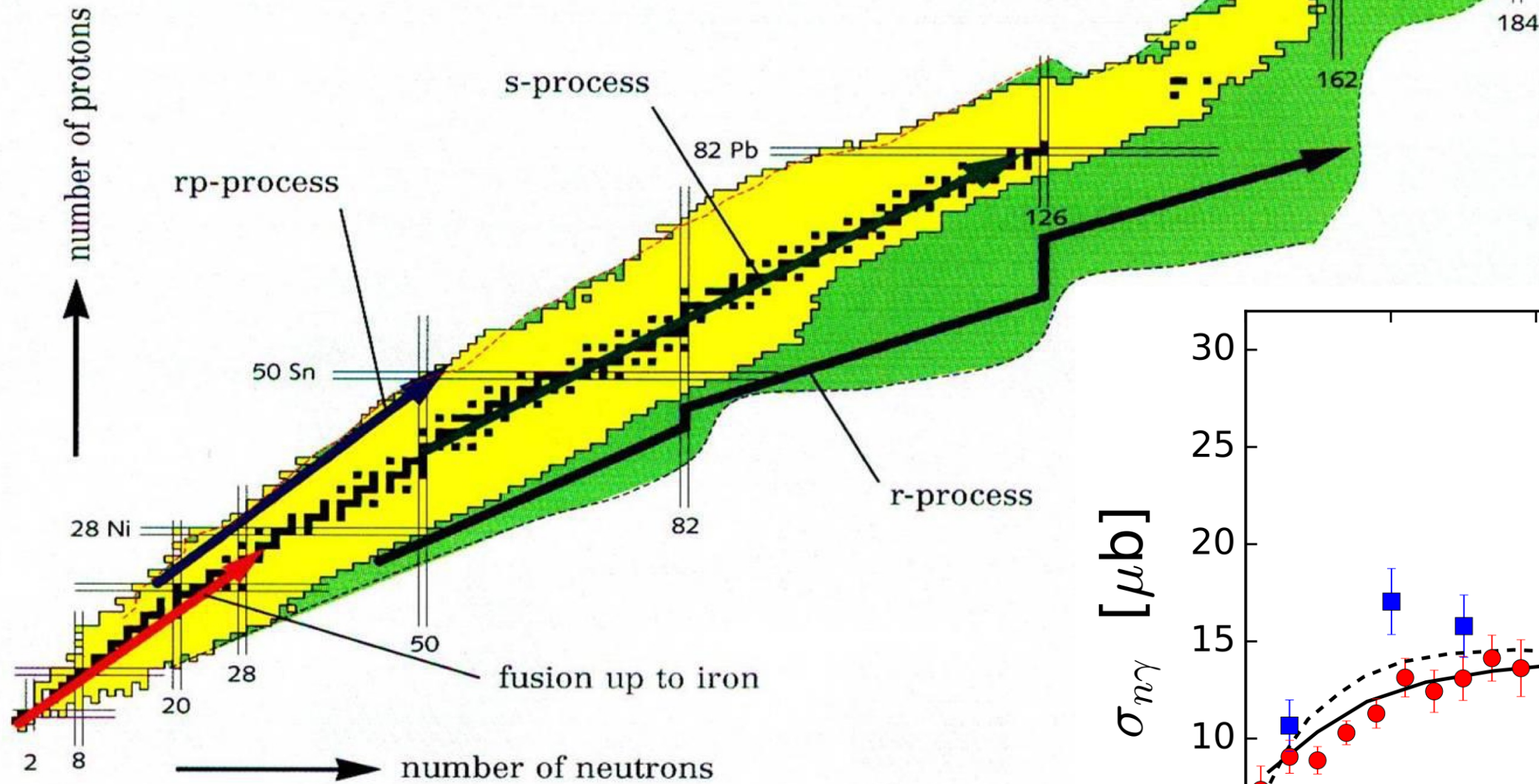
detailed balance

$$\sigma_{b+c \rightarrow a+\gamma} = \frac{2(2j_a + 1)}{(2j_b + 1)(2j_c + 1)} \frac{k_{bc}^2}{k_\gamma^2} \sigma_{\gamma+a \rightarrow b+c}$$



Applications to radiative capture (n,γ) and (p,γ) reactions in nuclear astrophysics

Novae, Supernovae: r-processes



Aumann, Nakamura,
Phys. Scr. T152 (2013) 014012

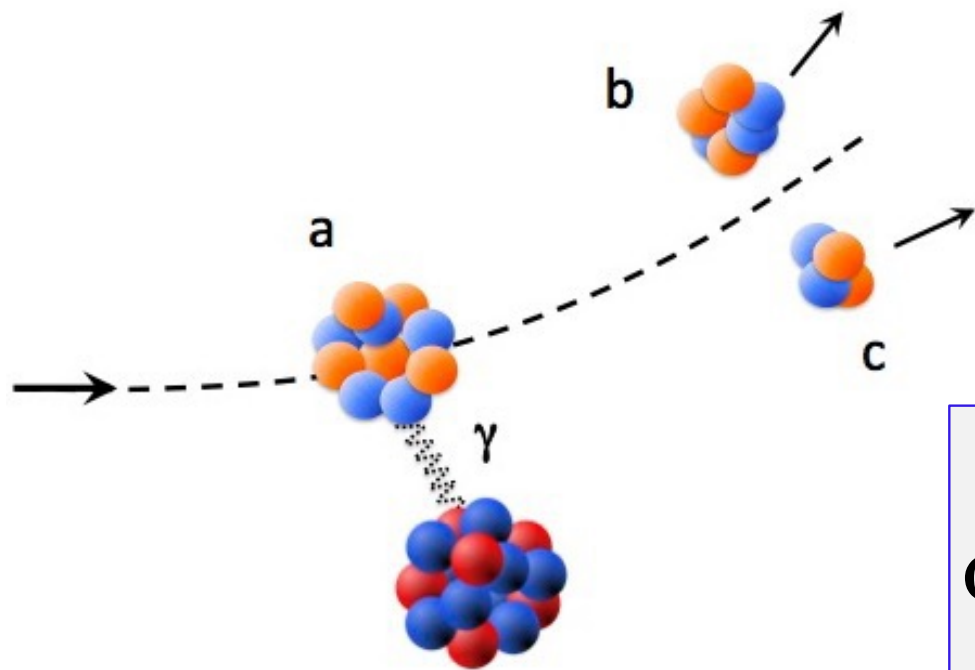
Pigmy resonances & Dipole polarizability

Rossi et al.

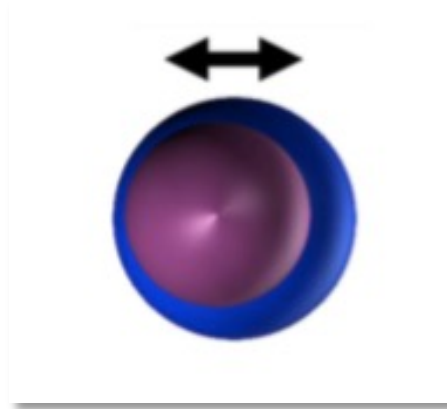
PRL 111 (2013) 242503

Wieland et al.

PRL 102, 092502 (2009)

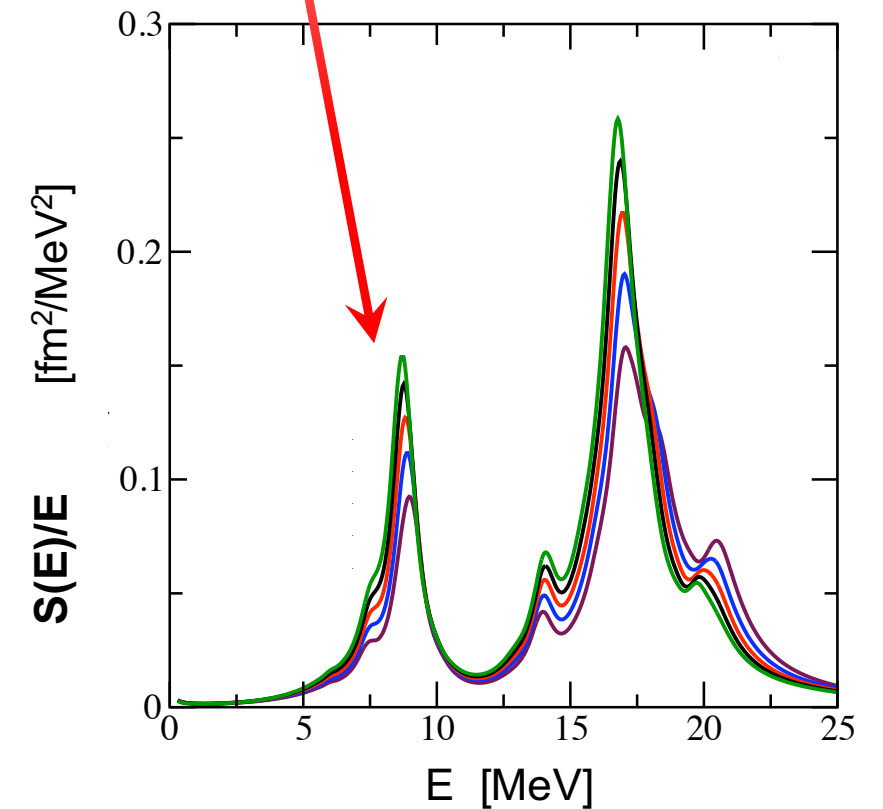
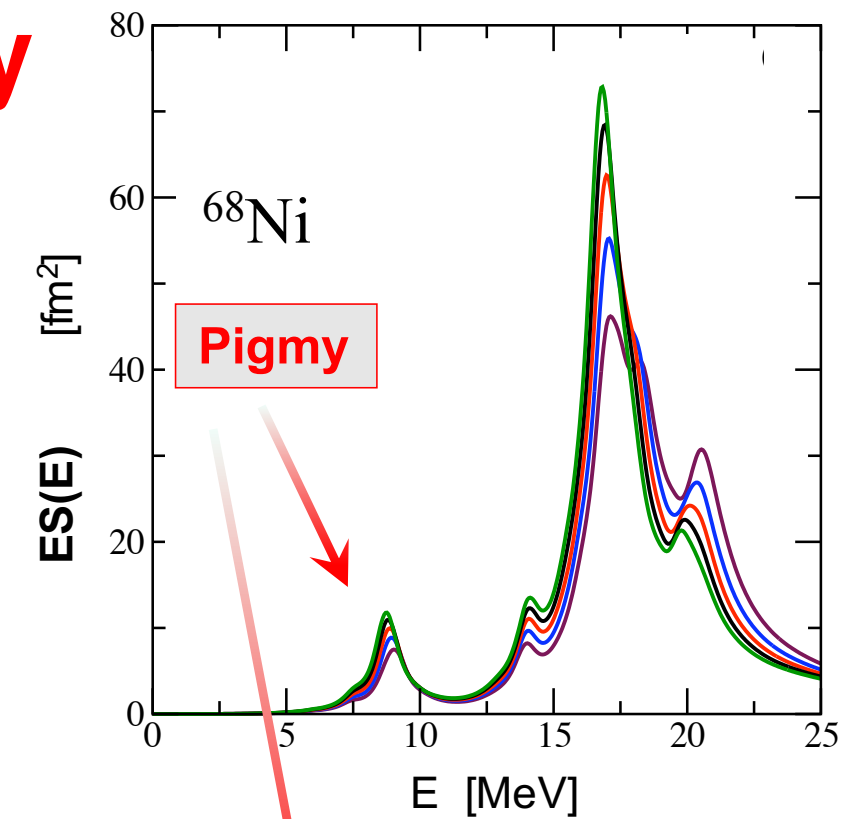


$$\sigma_C \sim (\dots) \int_0^\infty \frac{\sigma_\gamma(E)}{E^2} dE$$

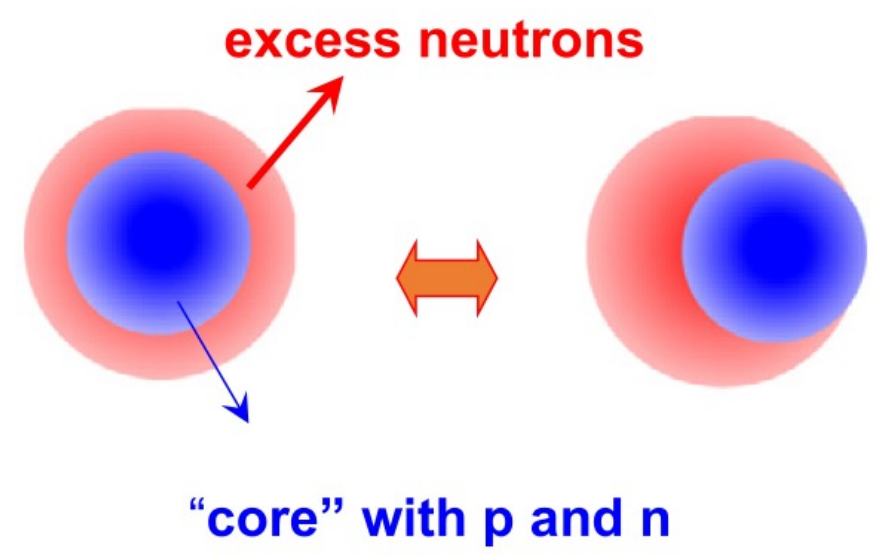
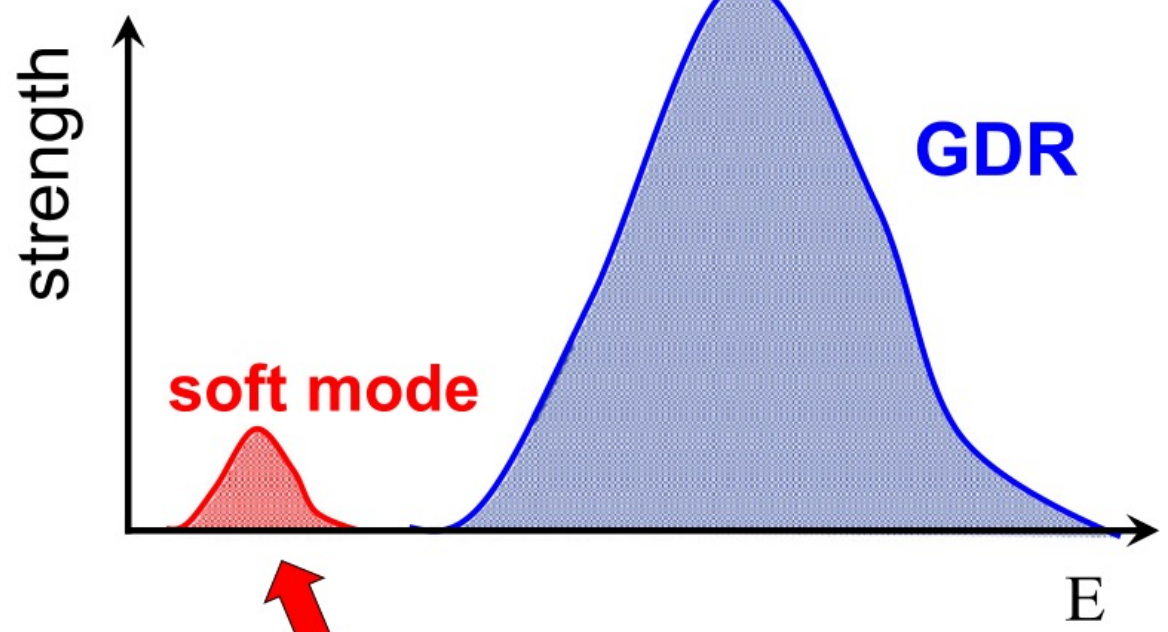
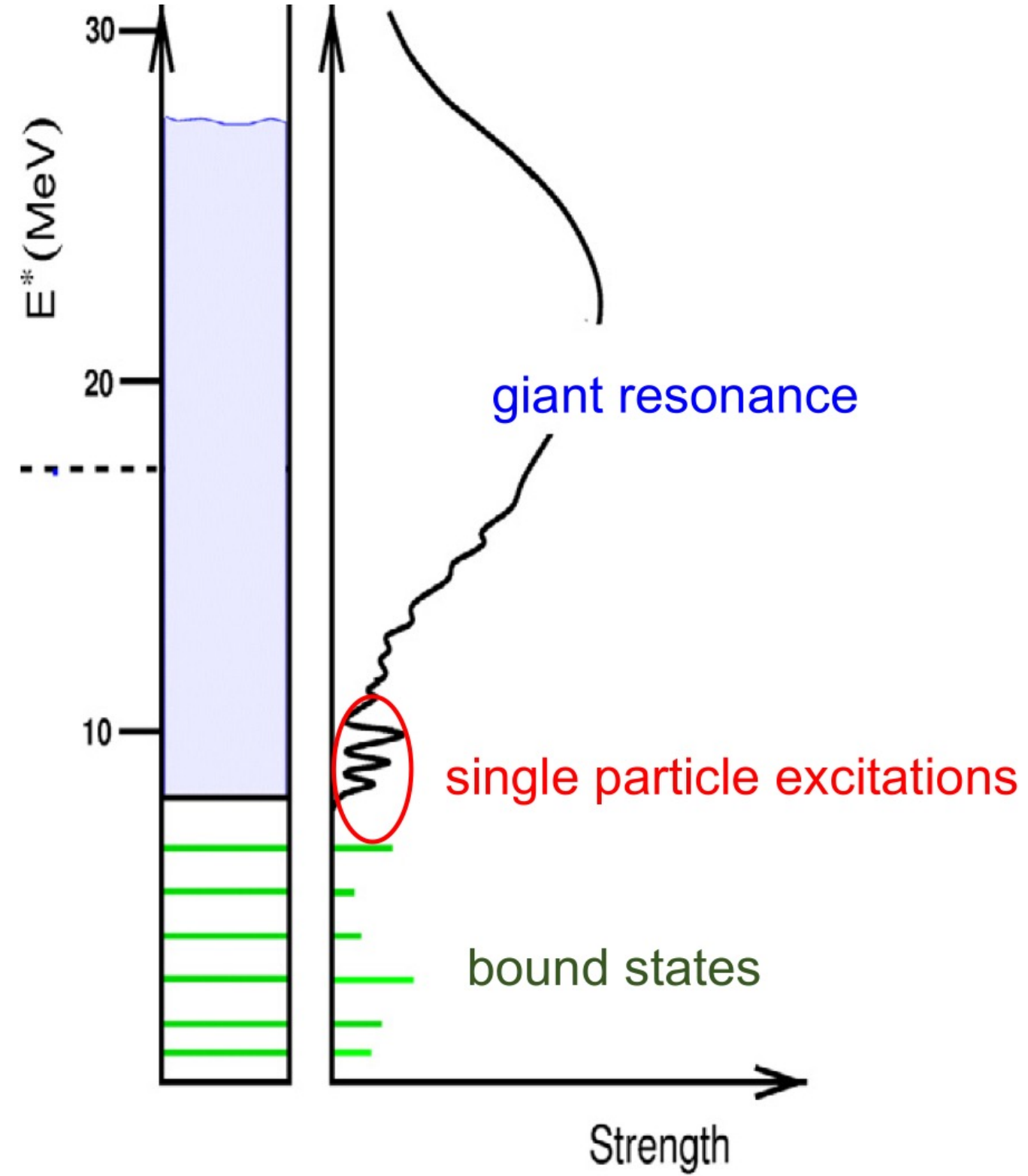


$$\alpha_D = \frac{\hbar c}{2\pi^2} \int_0^\infty \frac{\sigma_\gamma(E)}{E^2} dE$$

$$= \frac{8\pi}{9} \int \frac{B(E1, E_x)}{E_x} dE_x$$



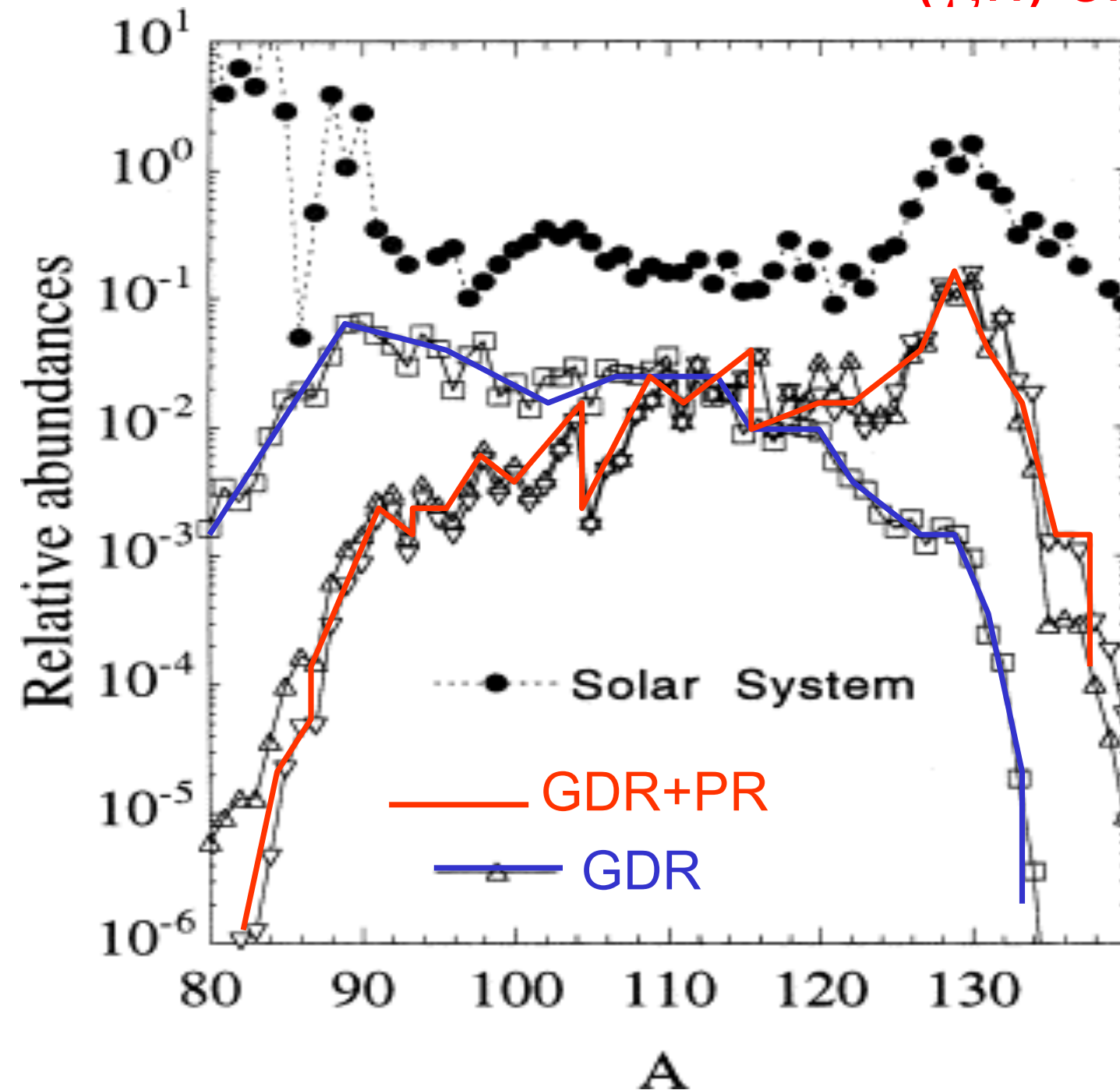
Pigmy resonances



Impact of pygmies on nucleosynthesis (??!)

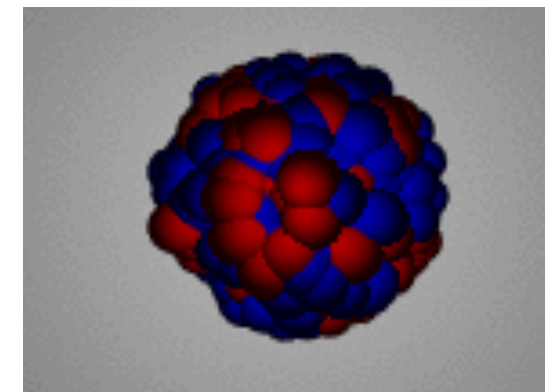
Goriely, PLB 436, 10 (1998)

(γ, n) or (n, γ) cross sections in the r-process

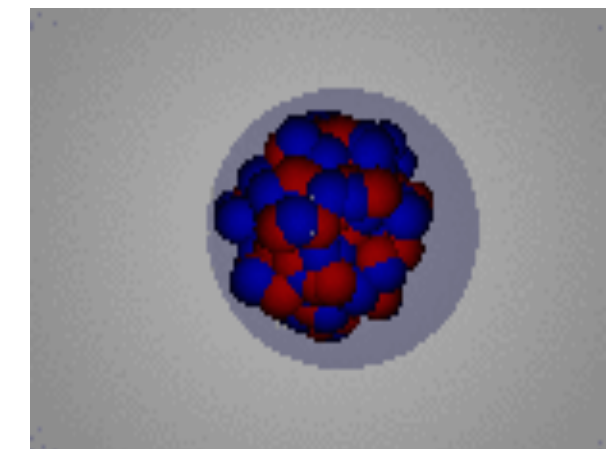


Impact: r-process abundances

- Calculation for $T = 10^9$ K, $N_n = 10^{20}$ cm⁻³, $\tau = 2.3$ s
- Under some conditions, PDR can enhance production in some regions

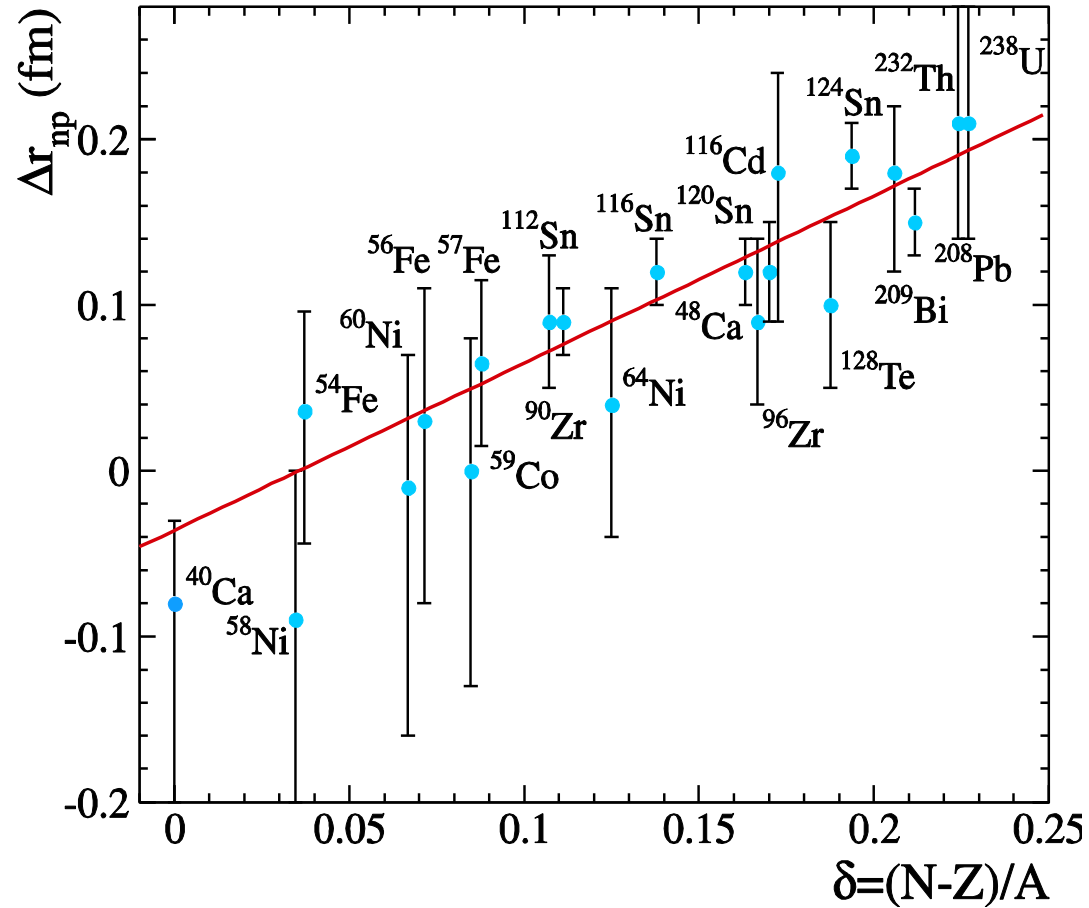


Giant dipole



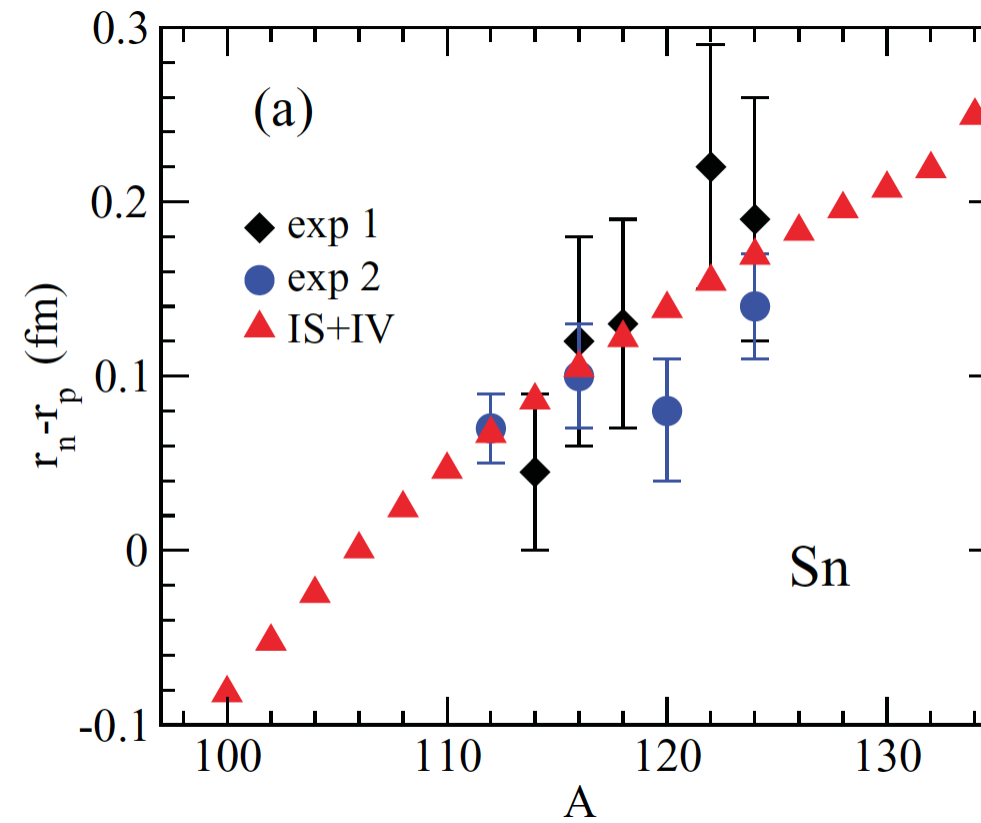
Pygmy dipole

Neutron skins measurements



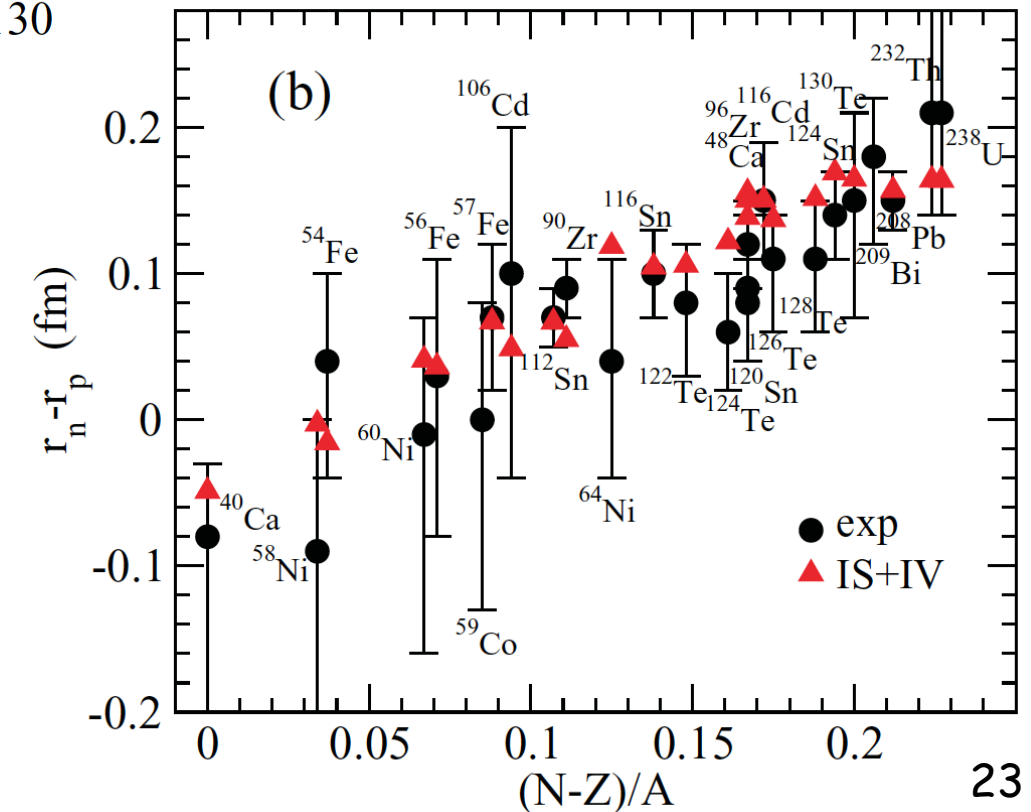
Radii from spin-dipole resonances
 Krasznahorkay et al., PRL 82, 3216 (1999)

Antiprotonic atoms
 Trzcinska et al., PRL 87, 082501 (2001)



Mean field calculations

CB, Liu, Sagawa,
 PRC 85, 014321 (2012)



EOS + symmetry energy

$$\frac{E}{A}[\rho] = \frac{E}{A}[\rho_0] + \frac{1}{18} K_\infty \left(\frac{\rho - \rho_0}{\rho_0} \right)^2 + S \left(\frac{\rho_n - \rho_p}{\rho} \right)^2 + \dots$$

$$S = \frac{1}{2} \frac{\partial^2 (E/A)}{\partial \delta^2} \Big|_{\delta=0} = J + Lx + \frac{1}{2} K_{\text{sym}} x^2 + O(x^3),$$

$$L = 3\rho_0 \frac{dS(\rho)}{d\rho} \Big|_{\rho_0}, \quad \delta = \frac{\rho_n - \rho_p}{\rho}, \quad x = \frac{(\rho - \rho_0)}{3\rho_0}$$

$$\text{For } \rho \sim \rho_0 \text{ and } \delta \sim 1 \Rightarrow p = \frac{L\rho_0}{3}$$

Skyrme	ρ_0	E_0	K_∞	J	L	K_{sym}
SLy5	0.161	-15.99	229.92	32.01	48.15	-112.76
Skxs20	0.162	-15.81	201.95	35.50	67.06	-122.31
SkI5	0.156	-15.82	255.57	36.63	129.27	-155.94

L crucial for neutron matter

Density functional models

For the nucleon-nucleon interaction

$$V(\mathbf{r}_i, \mathbf{r}_j) = V_{ij}^{\text{NN}} + V_{ij}^{\text{Coul}}$$

$$V_{ij}^{\text{Coul}} = -\frac{e^2}{4} \sum_{i,j=1}^A \frac{\tau_{ij}^2 + \tau_{ij}}{|\mathbf{r}_i - \mathbf{r}_j|},$$

$$\tau_{ij} = \tau_i + \tau_j$$

$$V_{ij}^{\text{NN}} = t_0 (1 + x_0 P_{ij}^\sigma) \delta(\mathbf{r}_i - \mathbf{r}_j) + \frac{1}{2} t_1 (1 + x_1 P_{ij}^\sigma) [\hat{\mathbf{k}}_{ij}^2 \delta(\mathbf{r}_i - \mathbf{r}_j) + \delta(\mathbf{r}_i - \mathbf{r}_j) \vec{\mathbf{k}}_{ij}^2] +$$

$$t_2 (1 + x_2 P_{ij}^\sigma) \hat{\mathbf{k}}_{ij} \delta(\mathbf{r}_i - \mathbf{r}_j) \vec{\mathbf{k}}_{ij} + \frac{1}{6} t_3 (1 + x_3 P_{ij}^\sigma) \rho^\alpha \left(\frac{\mathbf{r}_i + \mathbf{r}_j}{2} \right) \delta(\mathbf{r}_i - \mathbf{r}_j) +$$

$$iW_0 \hat{\mathbf{k}}_{ij} \delta(\mathbf{r}_i - \mathbf{r}_j) (\vec{\sigma}_i + \vec{\sigma}_j) \vec{\mathbf{k}}_{ij},$$

$$t_i, x_i, \alpha, W_0$$

are 10 **Skyrme** parameters



$$E[\rho] = \langle \Phi | T + V_{ij}^{\text{Coul}} + V_{ij}^{\text{NN}} | \Phi \rangle$$

+ pairing

HF + BCS

$$\Delta_i = \frac{1}{2} \sum_j \frac{G_{ij} \Delta_j}{\sqrt{(\varepsilon_j - \lambda)^2 + \Delta_j^2}}$$

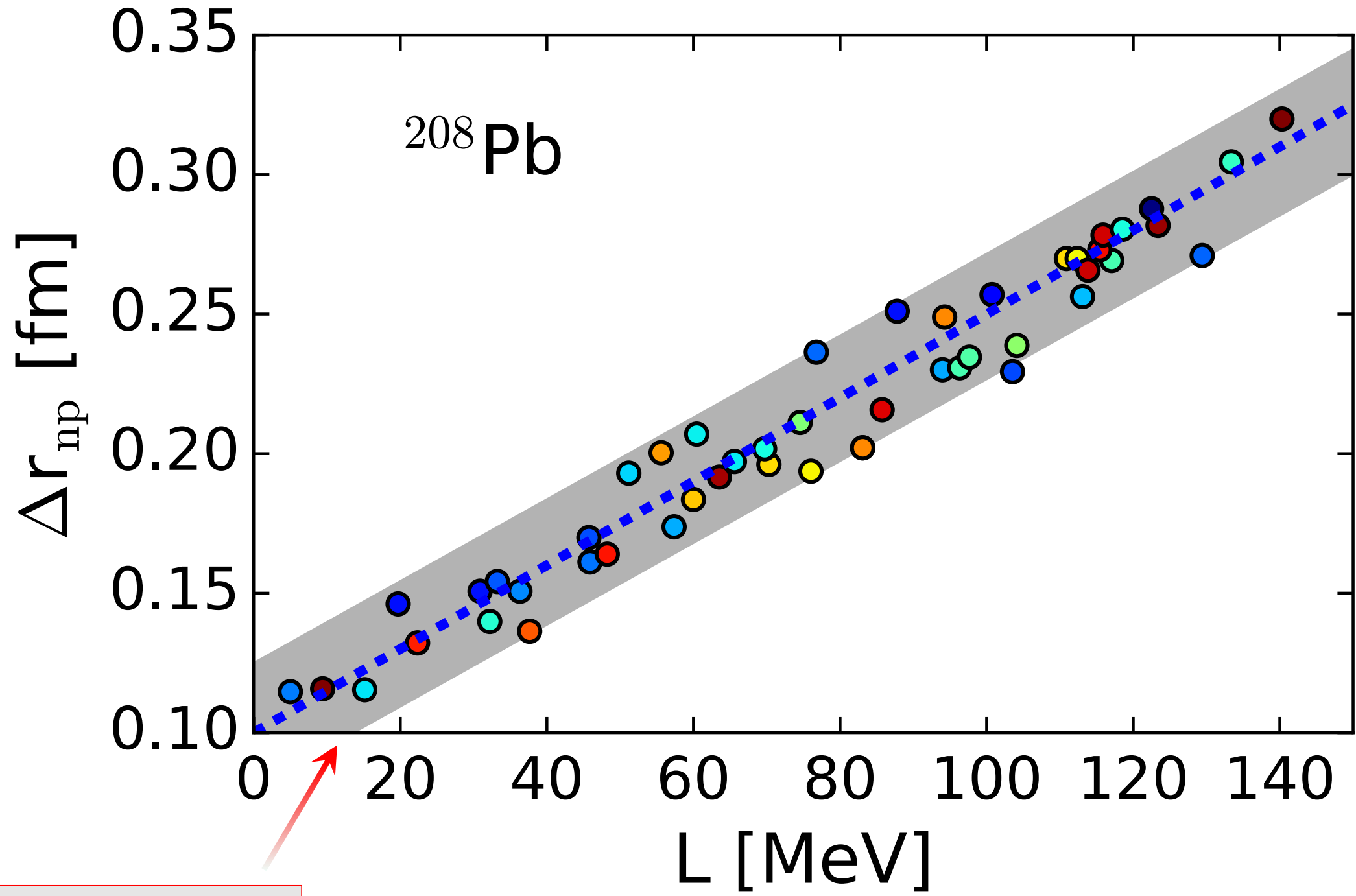
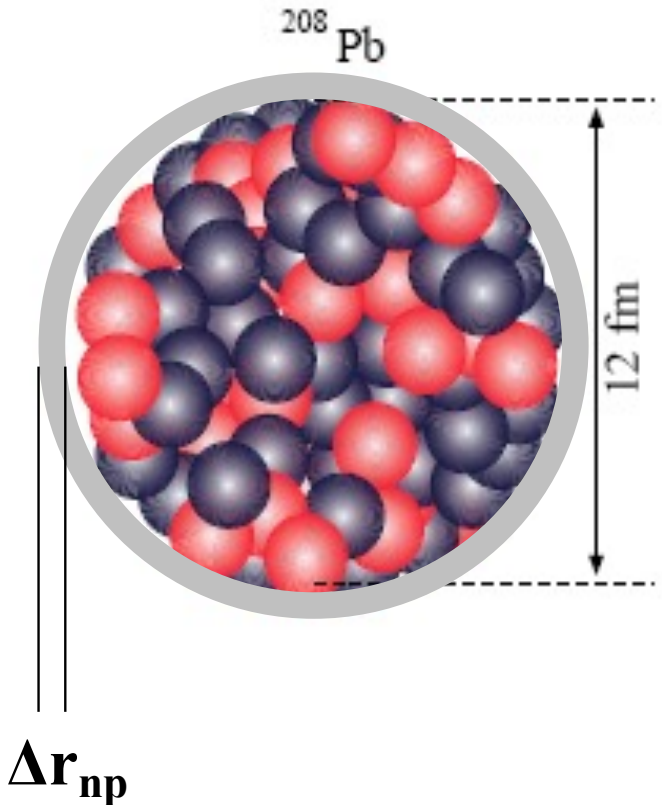
HFB

$$\begin{pmatrix} h_{HF} - \lambda & \Delta \\ -\Delta & -h_{HF} + \lambda \end{pmatrix} \begin{pmatrix} u_k \\ v_k \end{pmatrix} = E_k \begin{pmatrix} u_k \\ v_k \end{pmatrix}$$

$$V = V_0 \left[1 - \eta \left(\frac{\rho(\mathbf{r})}{\rho_0} \right)^\alpha \right] \delta(\mathbf{r}_1 - \mathbf{r}_2), \quad \rho_0 = 0.16 \text{ fm}, \quad \alpha = 1$$

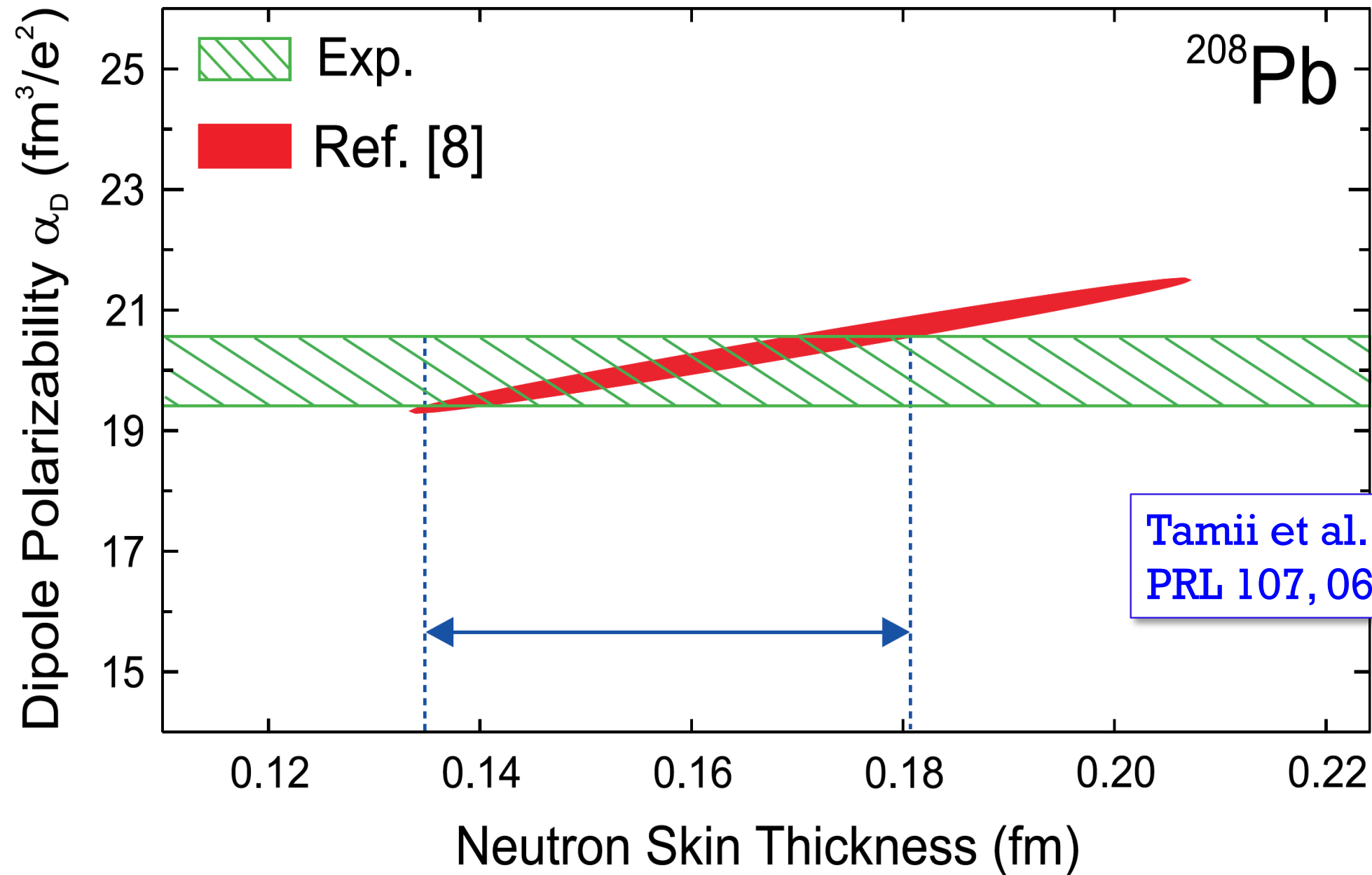
$$\eta = \begin{cases} 0, & \text{"volume" pairing} \\ 1, & \text{"surface" pairing} \\ 1/2, & \text{"mixed" pairing} \end{cases}$$

Correlation between symmetry energy & neutron skin



Numerous EDF

Dipole polarizability & neutron skin



Reinhard, Nazarewicz,
PRC 81, 051303(R) (2010)

Tamii et al.,
PRL 107, 062502 (2011)

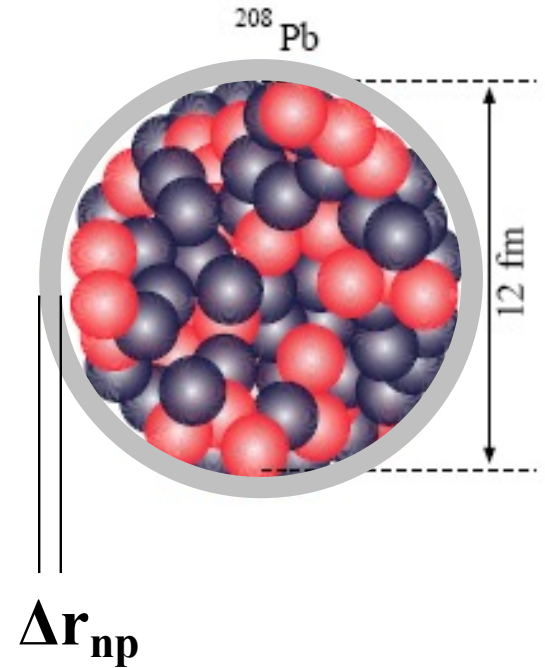
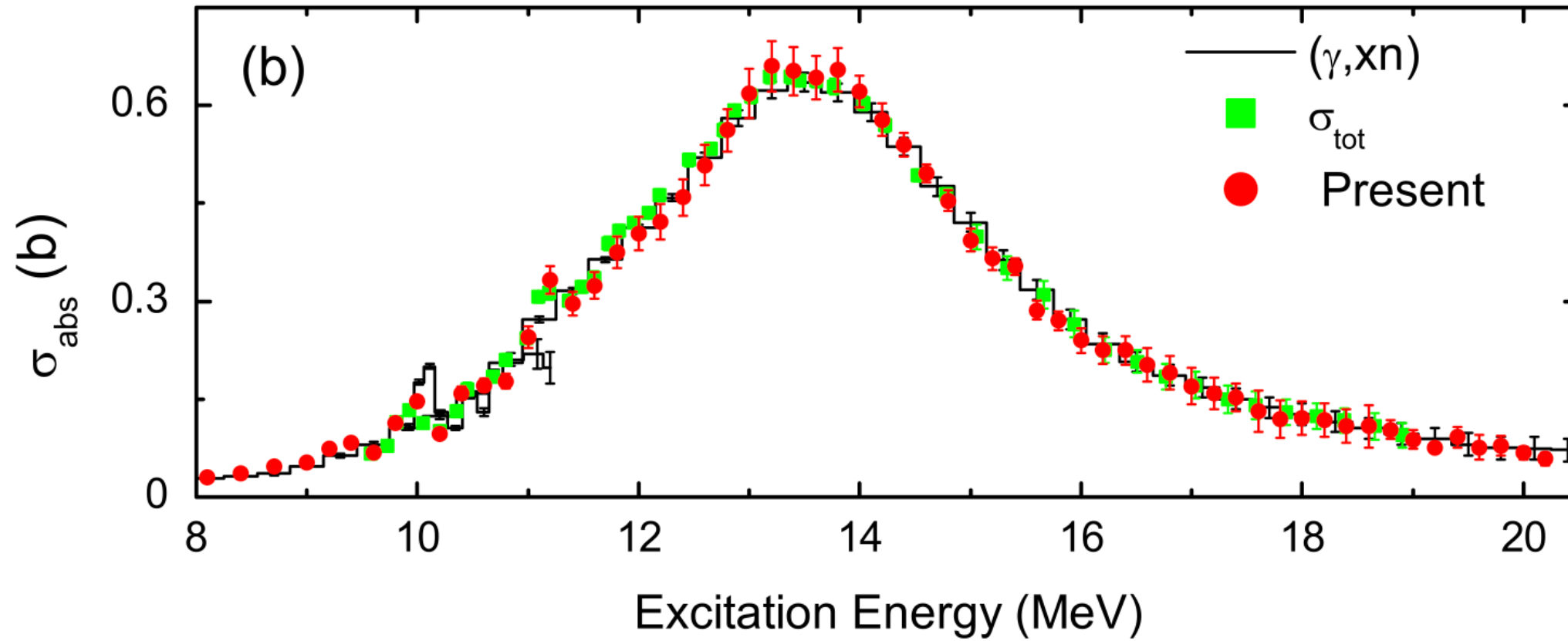
EFT:
Hebeler et al.,
PRL 105, 161102 (2010)

Experiment:

$$\Delta r_{np} \sim 0.156 \text{ fm}$$

$$\Delta r_{np} \sim 0.17 \text{ fm}$$

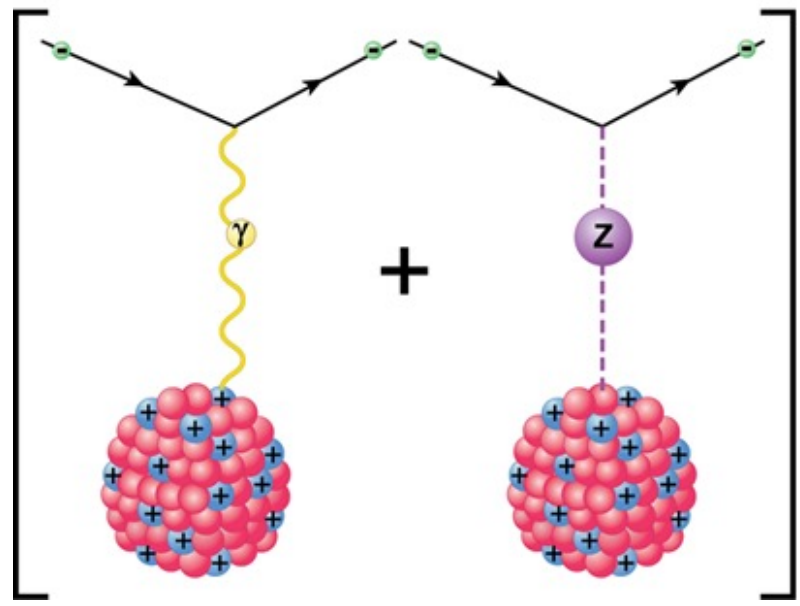
Dipole polarizability & neutron skin



Tamii et al.,
PRL 107, 062502 (2011)

$$\alpha_D = \frac{\hbar c}{2\pi^2} \int_0^\infty \frac{\sigma_\gamma(E)}{E^2} dE$$
$$= \frac{8\pi}{9} \int \frac{B(E1, E_x)}{E_x} dE_x$$

n-skin from PV e⁻ scattering



Abrahamyan et al,
PRL 108, 112502 (2012)

Howowitz et al,
PRC 85, 032501(R) (2012)

$$A_{PV} = \frac{d\sigma_R - d\sigma_L}{d\sigma_R + d\sigma_L}$$

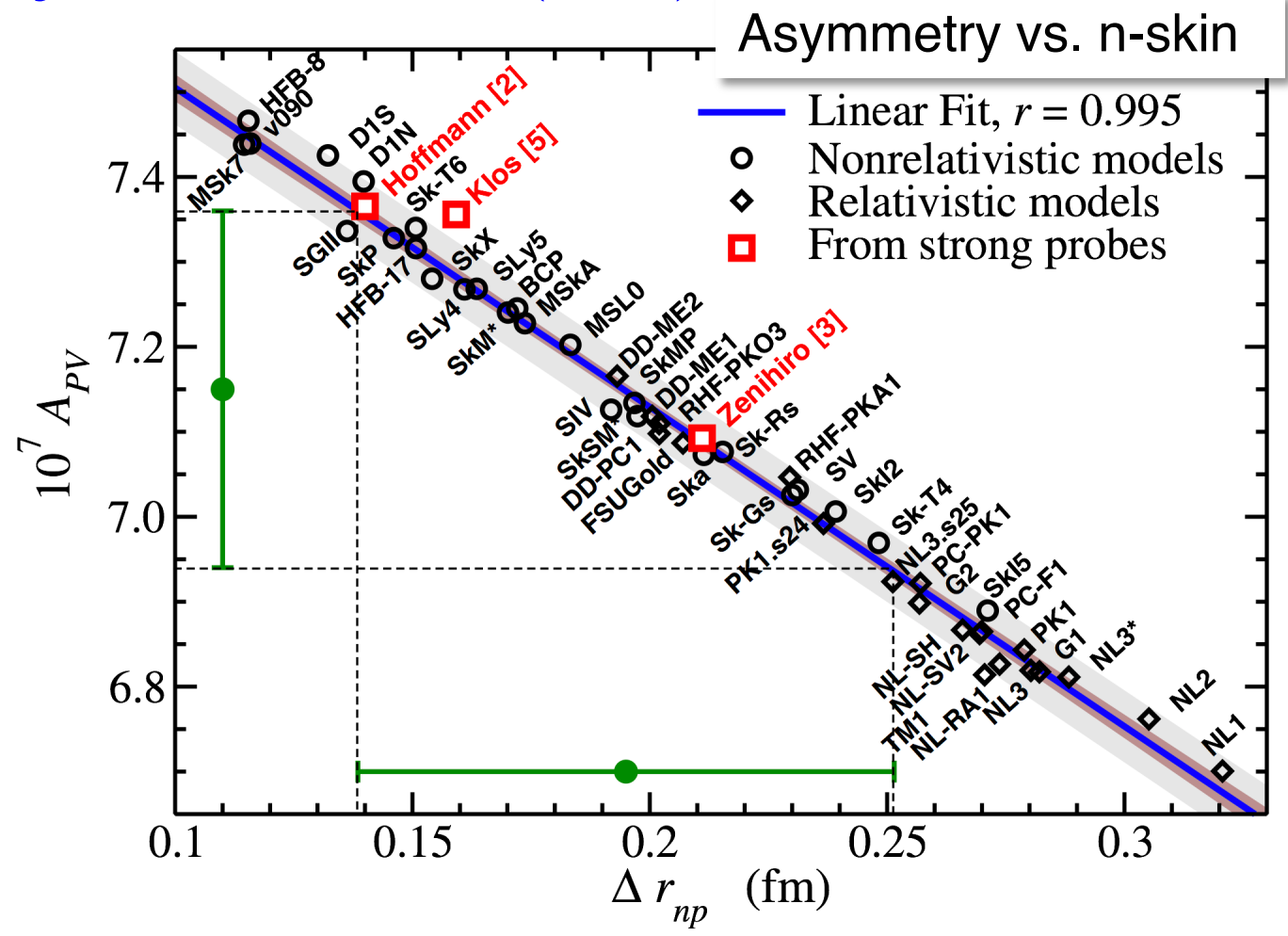
$$A_{PV}(Q^2) \sim \frac{G_F Q^2}{4\pi e^2 \sqrt{2}} \frac{F_W(Q)}{F_{ch}(Q)}$$

$$F_W = \frac{1}{Q_W} \int dr \frac{\sin(Qr)}{Qr} \rho_w(r)$$

$$\rho_w(r) = q_p \rho_{ch}(r) + q_n \int d^3 r' [G_E^p \rho_n + G_E^n \rho_p]$$

$$q_p = 0.0721, \quad q_n = 0.0721,$$

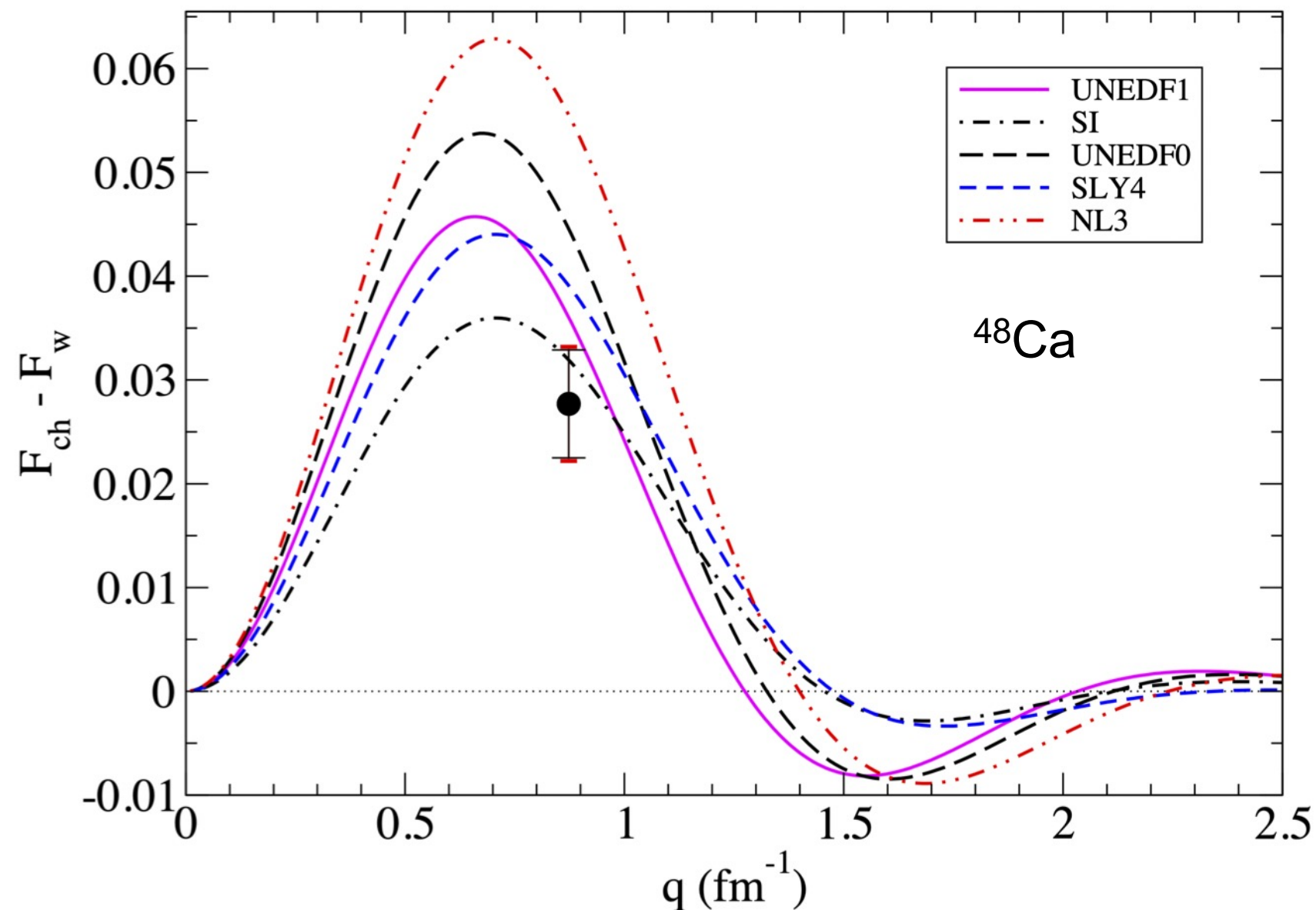
J. Roca-Maza, PRL (2011)



n-skin from e⁻ PV scattering ⁴⁸Ca

$$F(Q^2) \sim 1 - \frac{1}{6}q^2 \langle r^2 \rangle$$

$$\langle r^2 \rangle \cong -6 \frac{dF(Q^2)}{dQ^2}$$



- PREX & CREX: measurement of parity violating asymmetry

- Determine n-skin and/or L by comparison to predictions from DFT

$$(R_n - R_p)_{48\text{Ca}} = 0.121 \pm 0.025 \text{ fm}$$

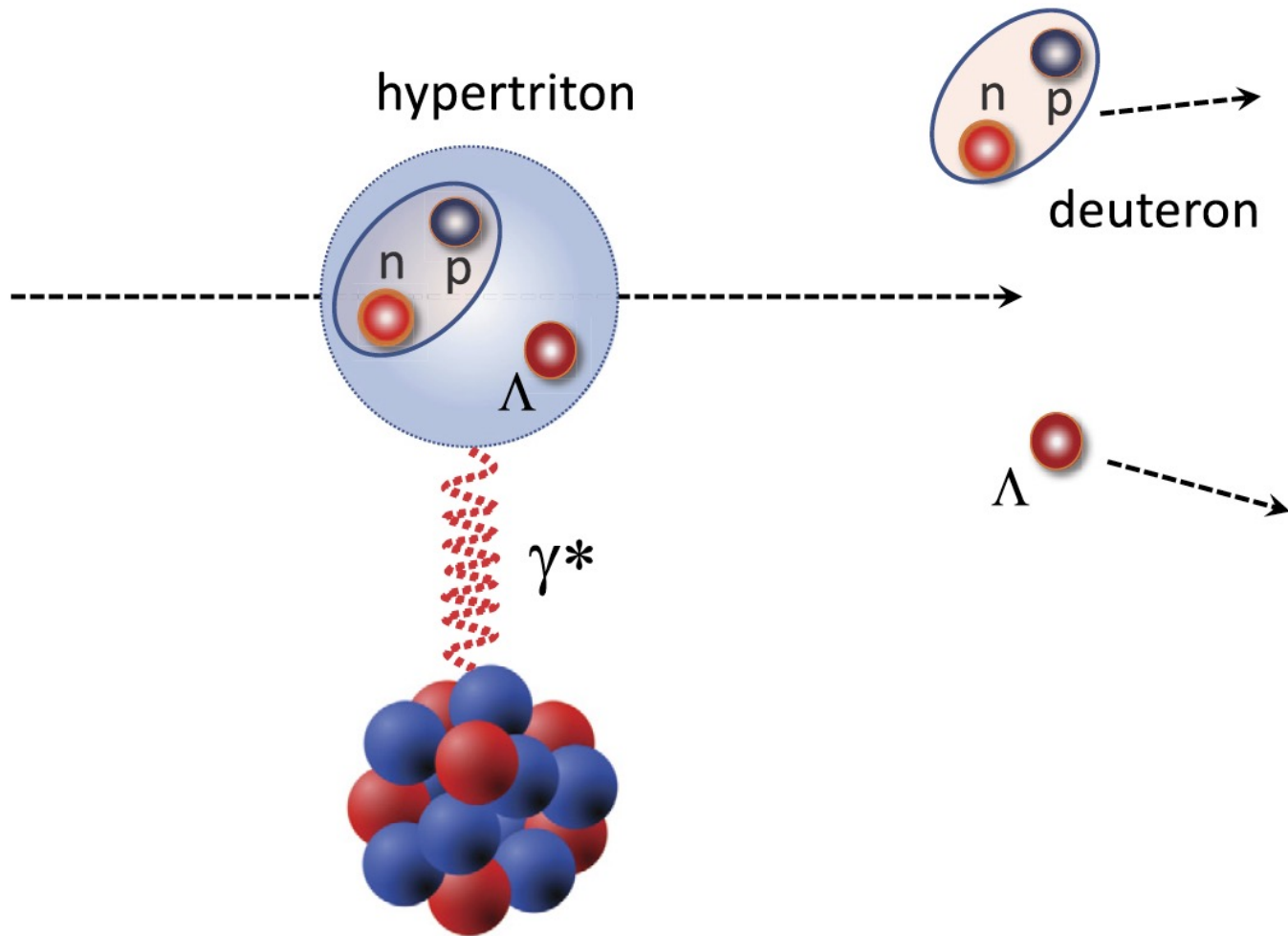
Adhikari et al, PRL 129, 042501 (2022)

too large value for Pb

$$R_n - R_p = 0.33 \pm 0.17 \text{ fm}$$

Adhikari et al, PRL 126, 172502 (2021)

Electromagnetic response of the hypertriton



$$\frac{d\sigma_c}{dE} = \frac{16\pi^3}{9\hbar c} n(E) \frac{dB(E)}{dE}$$

$$n(E) = \frac{2Z_T^2 \alpha}{\pi} \left(\frac{Ec}{\gamma \hbar v^2} \right)^2 \int_0^\infty db b \left[K_1^2 + \frac{1}{\gamma^2} K_0^2 \right] T(b)$$

$$x = Eb/\gamma v$$

First-order perturbation theory

$$\frac{dB(E)}{dE} = \frac{1}{\hbar} \sqrt{\frac{\mu}{2E}} |\langle g.s. || \mathcal{O}_{E1} || E, l \rangle|^2$$

$$\langle g.s. || \mathcal{O}_{E1} || E, l \rangle = (-1)^l \frac{e_{eff}}{\sqrt{4\pi}} \int_0^\infty dr r u_{g.s.}(r) u_{E,l}(r)$$

$$u_{E,l}(r) \rightarrow \sqrt{2\mu_{\Lambda d}/\pi \hbar^2 k} e^{i\delta_l} \sin(kr + \delta_l)$$

Electromagnetic response of the hypertriton

$$\frac{dB(E)}{dE} = \frac{1}{\hbar} \sqrt{\frac{\mu}{2E}} |\langle g.s. || \mathcal{O}_{E1} || E, l \rangle|^2$$

Analytical model:

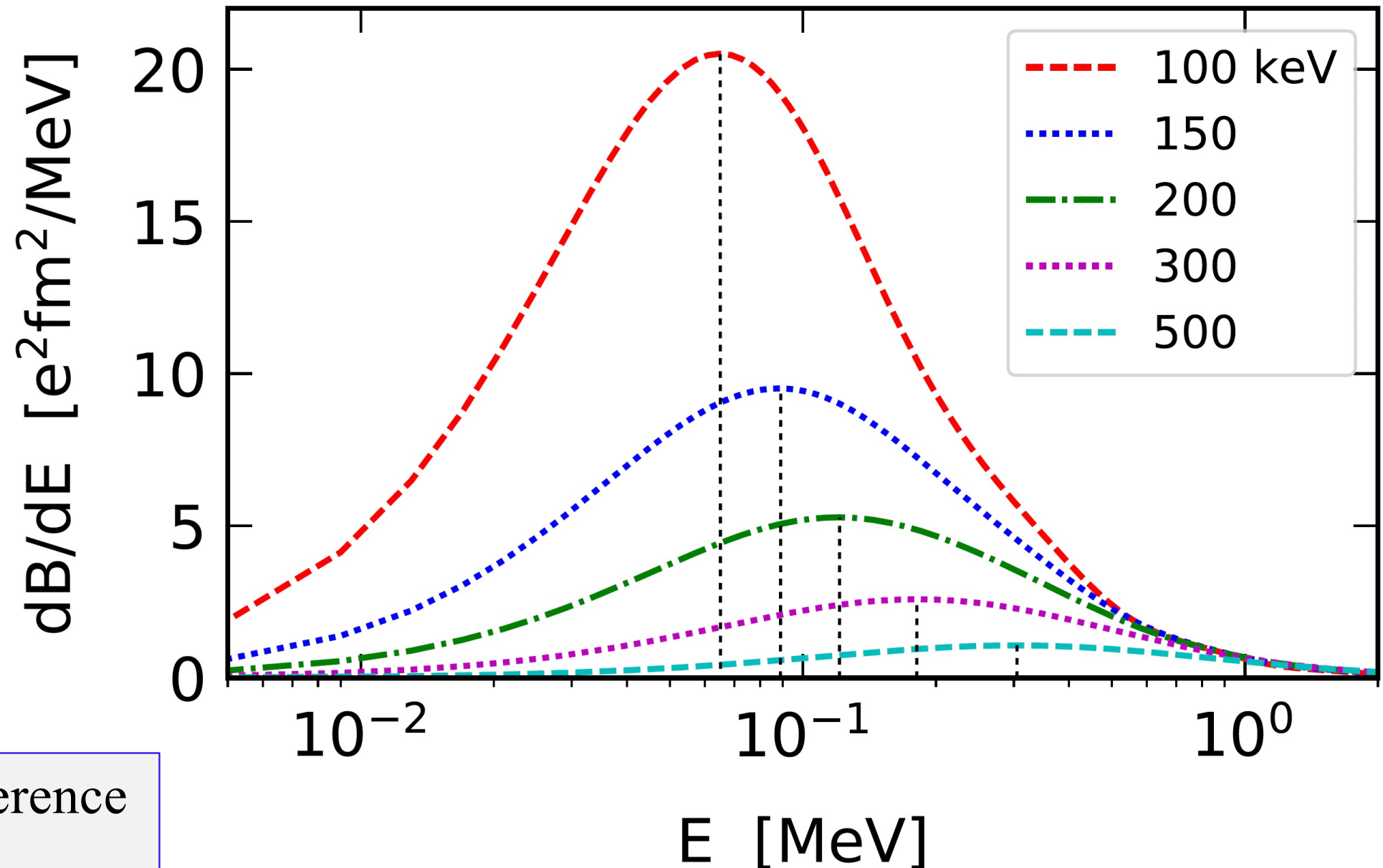
CB, Sustich

Phys. Rev. C 46 (1992) 2340

$$\frac{dB(E)}{dE} = C \sqrt{B_\Lambda} \frac{E^{3/2}}{(E + B_\Lambda)^4}$$

$$E_{max} = \frac{3}{5} B_\Lambda$$

- Excellent agreement < 4% difference
- FSI small

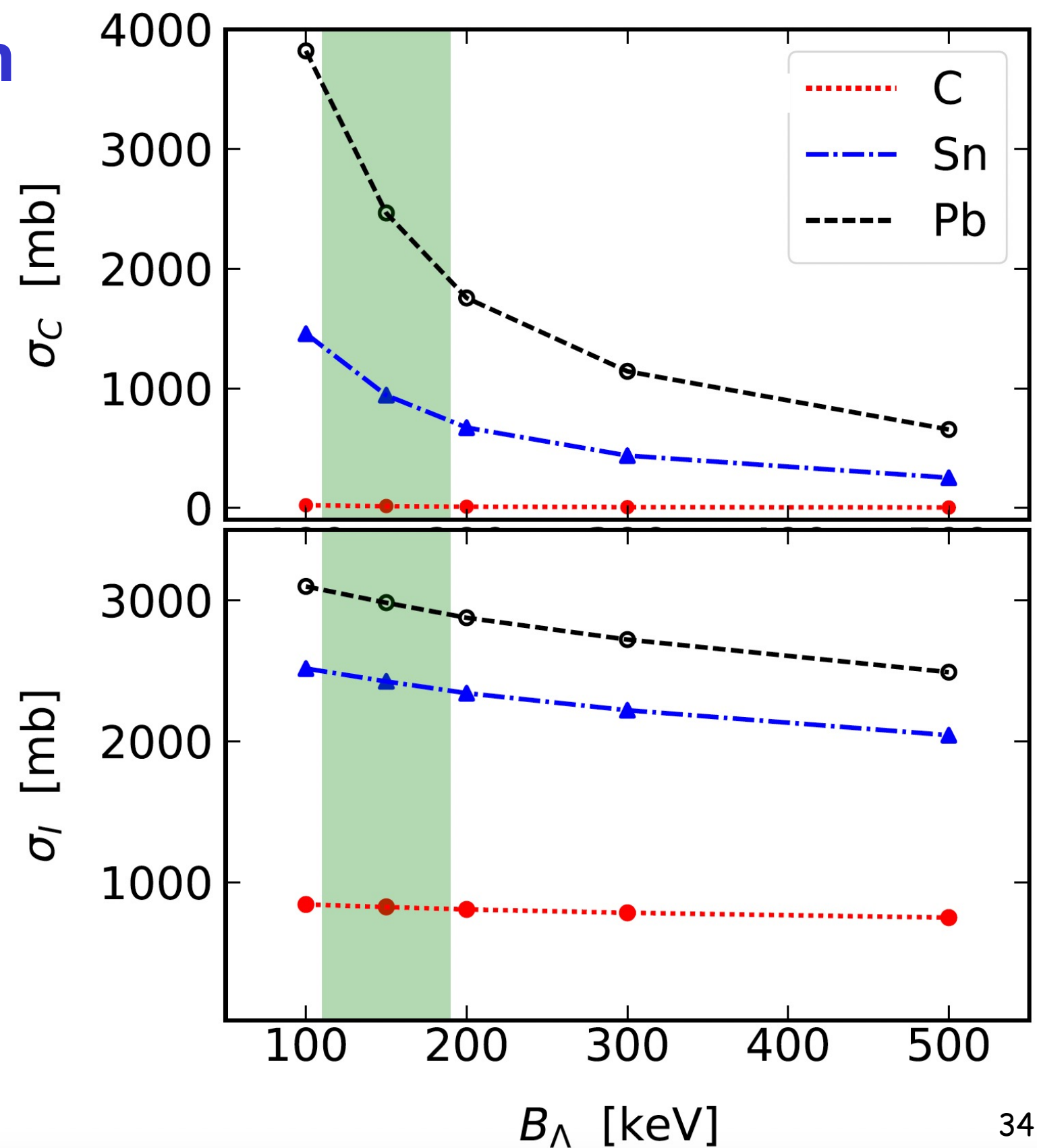


EM response of the hypertriton

1.5 GeV/nuc. ${}^3_{\Lambda}\text{H}$ incident on ${}^{12}\text{C}$, ${}^{120}\text{Sn}$, ${}^{208}\text{Pb}$

B_{Λ} (keV)	$\sigma_C(\text{C})$	$\sigma_C(\text{Sn})$	$\sigma_C(\text{Pb})$
100	22.9	1457.	3820.
150	14.9	942.	2464.
200	10.7	672.	1755.
300	7.1	438.	1142.
500	4.1	253.	656.

B_{Λ} (keV)	$\sigma_I(\text{C})$	$\sigma_I(\text{Sn})$	$\sigma_I(\text{Pb})$
100	842.	2516.	3098.
150	824.	2424.	2982.
200	807.	2341.	2876.
300	783.	2220.	2721.
500	749.	2043.	2490.



PHYSICS TODAY

MARCH 1994



RELATIVISTIC HEAVY-ION PHYSICS WITHOUT NUCLEAR CONTACT

The large electromagnetic field generated by a fast heavy nucleus allows investigation of new electromagnetic processes not accessible with real photons.

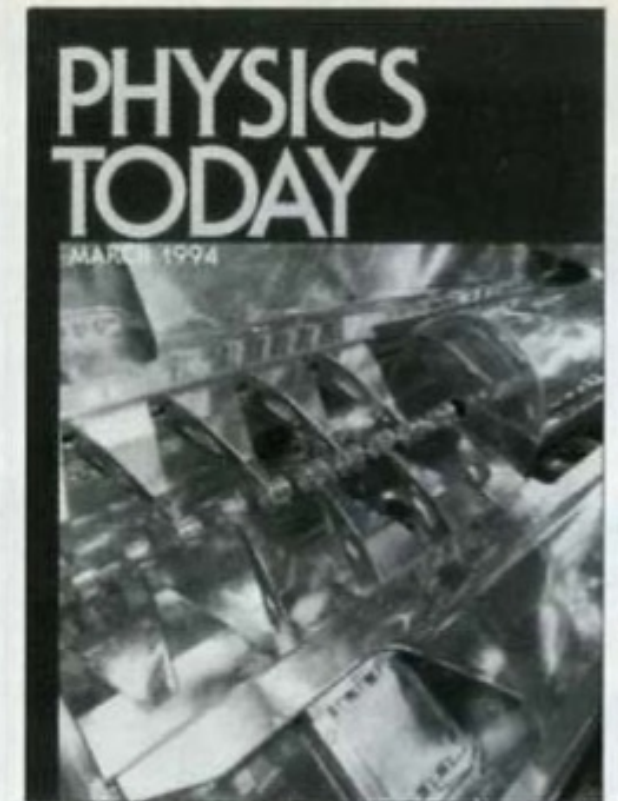
Carlos Bertulani and Gerhard Baur

An increasing number of physicists are investigating nuclear collisions at relativistic energies. (See figure 1.) Accelerators completely devoted to the study of these collisions (such as the Relativistic Heavy Ion Collider at Brookhaven National Laboratory) are under construction. So are hadron colliders (such as the Large Hadron Col-

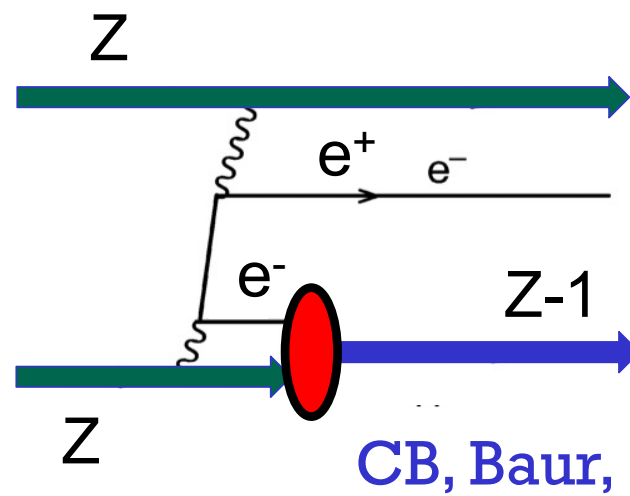
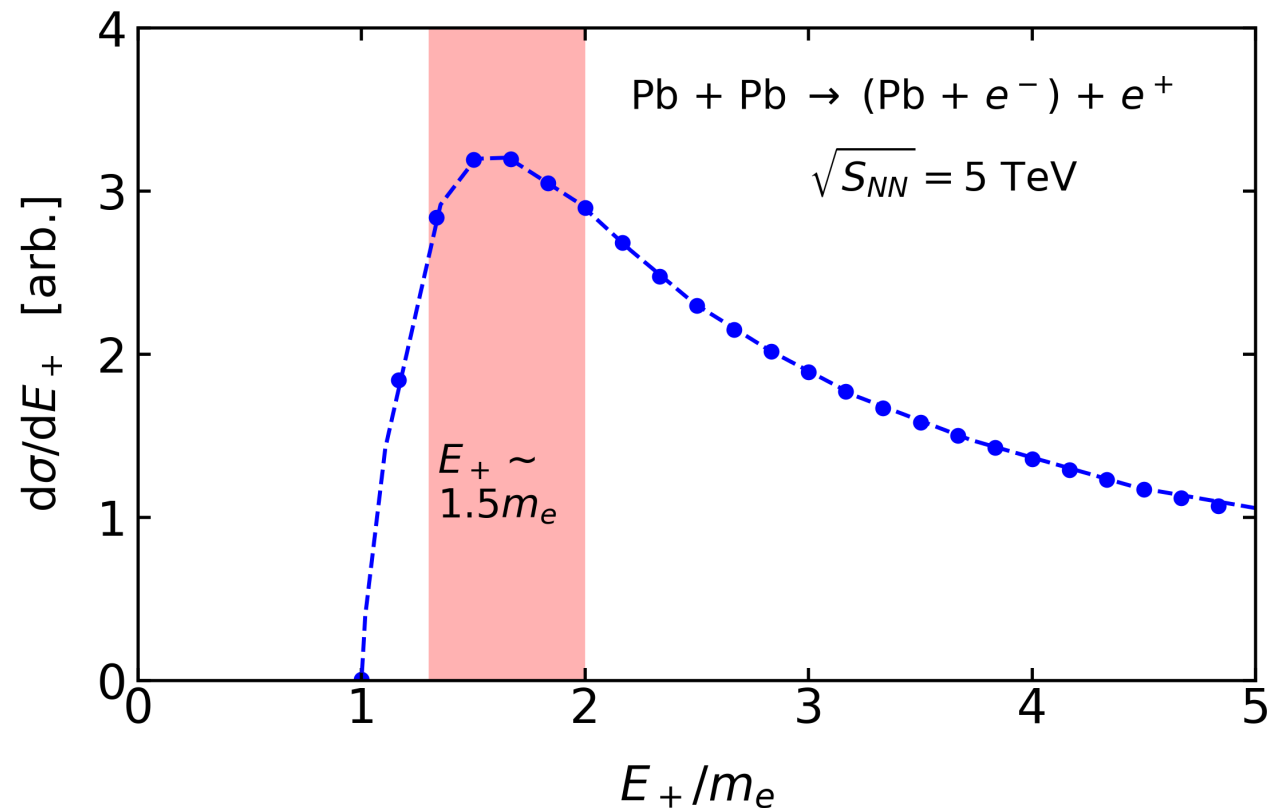
lided by $b/\gamma v$ and that the electric (or magnetic) field during this time interval is very intense: $E \approx \gamma Ze/b^2$. The factor γ , which is $(1 - v^2/c^2)^{-1/2}$, is very large (on the order of 10^4 – 10^7) in relativistic heavy-ion colliders.

Theory

COVER: Inside of a compact high-frequency linear accelerator for heavy ions developed at the Technical University of Munich and at GSI in Darmstadt, Germany. The polished copper structure uses a quadrupole field to focus highly charged ions. Accelerators of this design at GSI and CERN bring ions up to high enough energies that the main accelerators can take them to relativistic energies. In their article on page 22, Carlos Bertulani and Gerhard Baur discuss the physics one can probe by colliding relativistic heavy ions without nuclear contact.



Pair production with capture



K-shell capture. Only 20% capture in higher orbitals.

CB, Baur, Phys. Rep. B 163, 299 (1988)

$$\sigma = \frac{33\pi (Z\alpha)^8}{10} \frac{1}{m_e^2} \frac{1}{e^{2\pi Z\alpha} - 1} [\ln \gamma - 2.051]$$

Electron capture → beam loss at CERN

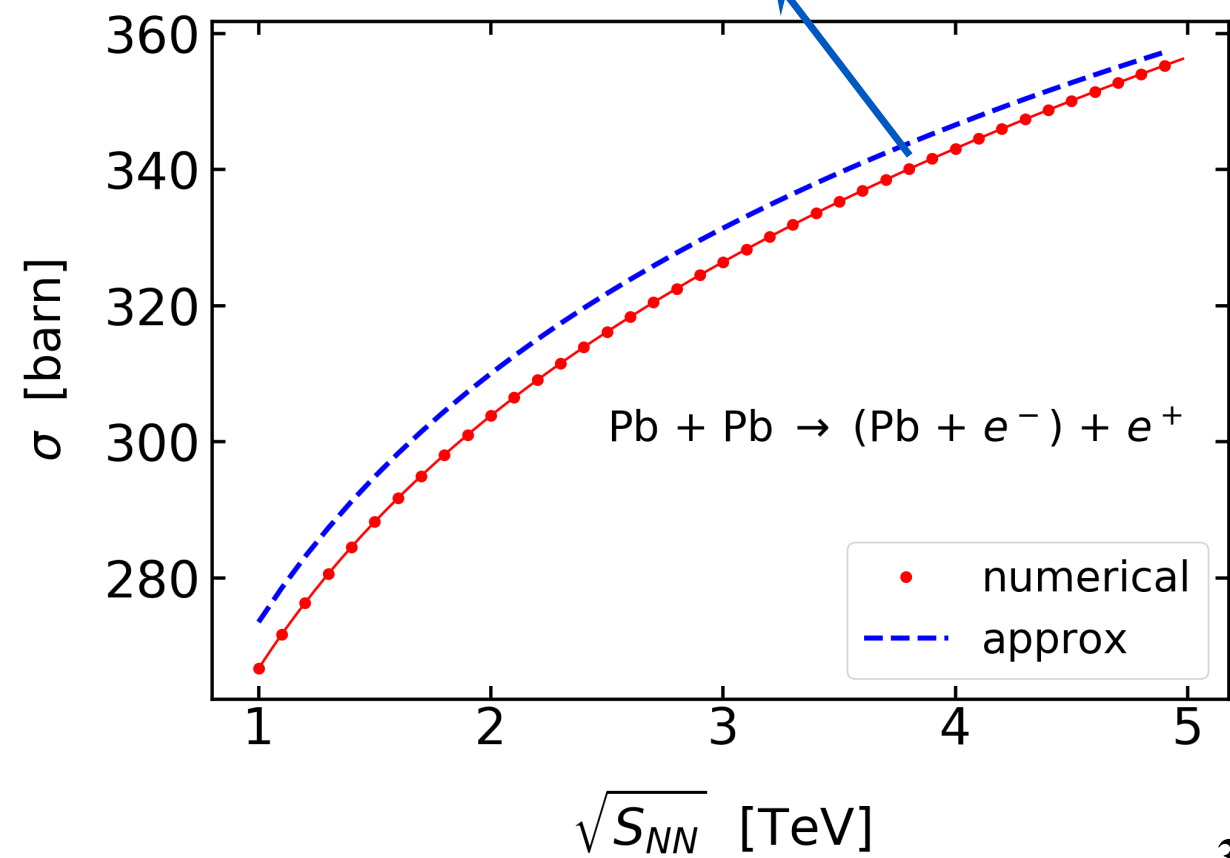
Theory and calculation:

Electromagnetic physics at relativistic heavy ion colliders, for better and for worse

G. Baur and CB, Nucl. Phys. A505, 835 (1989)

Experiment

R. Bruce et al, Phys. Rev. ST Accel. Beams 12, 071002 (2009)



First anti-atom (1996)

Physicists Manage to Create The First Antimatter Atoms

By MALCOLM W. BROWNE
Published: January 5, 1996

But the neutrality of antihydrogen, like that of ordinary hydrogen, renders it impossible to contain or manipulate using magnetic fields. Moreover, an antiatom cannot be contained in an ordinary vessel, since the slightest contact with the container's wall causes it to annihilate. Consequently, other groups are developing enormously sophisticated methods, including interacting lasers, to manipulate and secure antiparticles inside vacuum chambers.

The New York Times

NY Times, January 5, 1996

WORLD U.S. N.Y. / REGION BUSINESS TECHNOLOGY SCIENCE HEALTH SPORTS

Theory:

G. Baur, Phys. Lett. B 311, 343 (1993)

CERN (LEAR): 1996
9 events

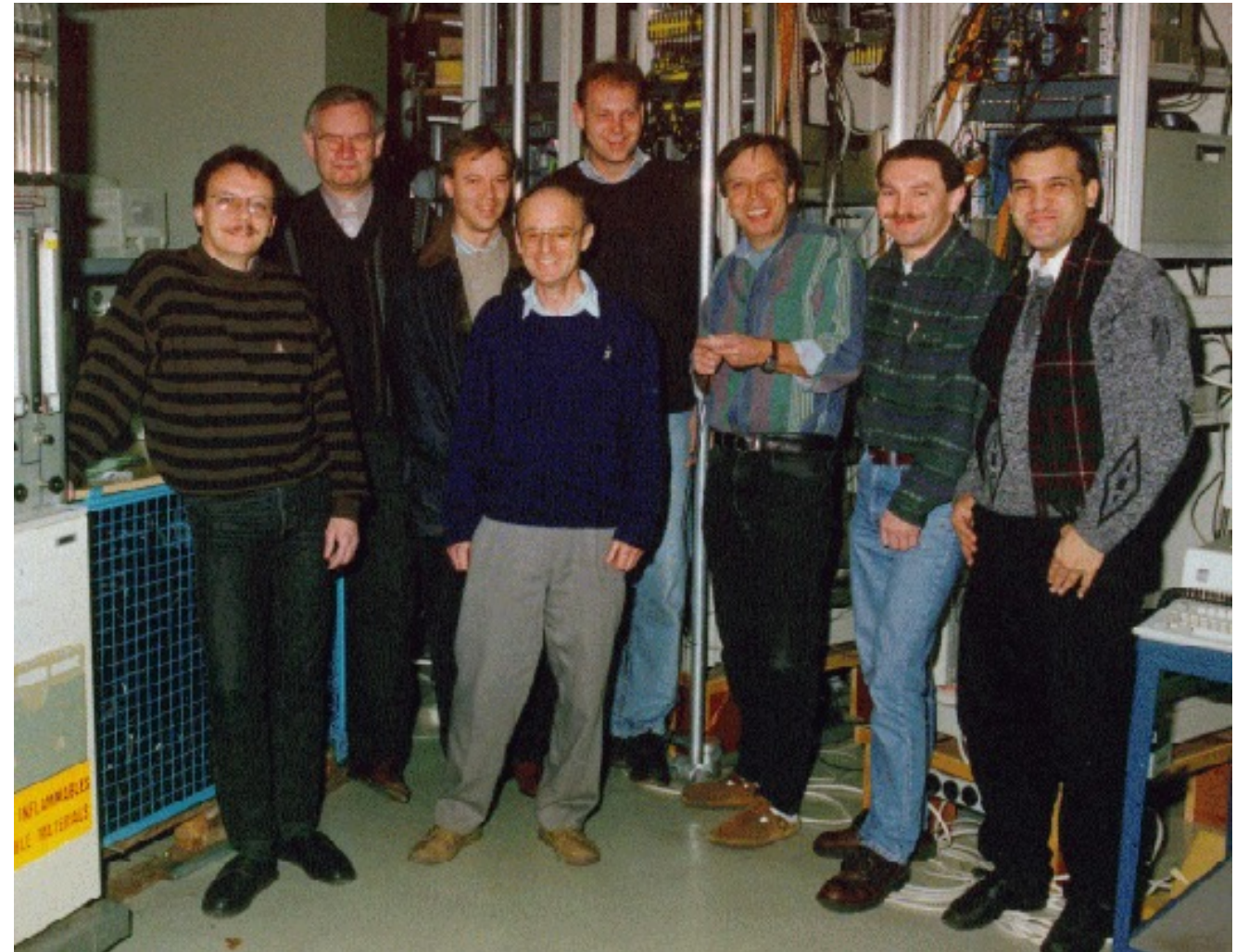
G. Baur *et al.*, Phys. Lett. B 368, 251 1996

Theory:

CB, G. Baur, Phys. Rev. D 58, 034005 (1998)

FERMILAB: 1998
57 events

G. Blanford *et al.*, Phys. Rev. Lett. 80, 3037 (1998)



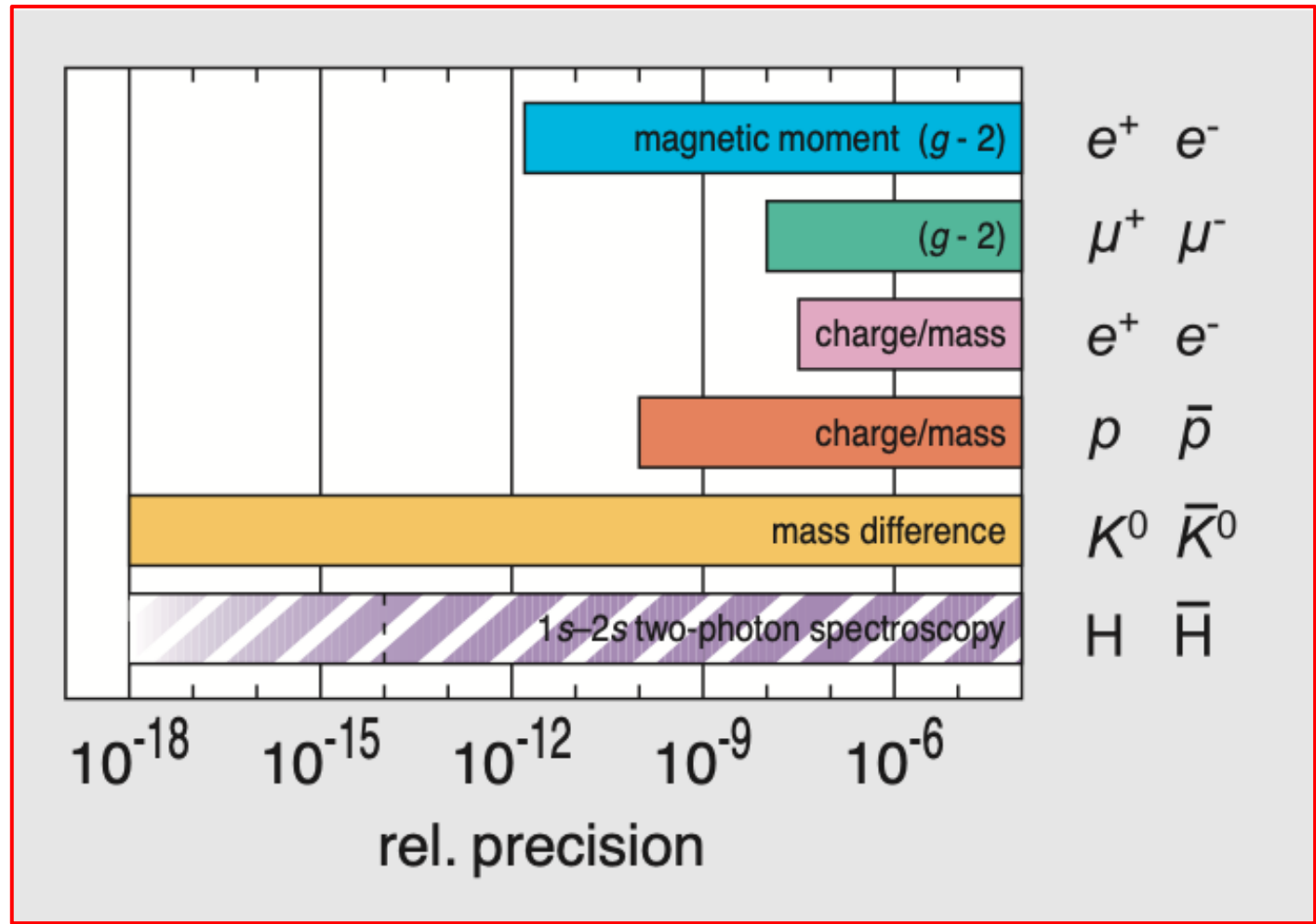
Why antihydrogen?

- **QFT → CPT → Matter and antimatter are symmetric**
This assumes point like elementary particles (quarks and leptons). Experimentally $< 10^{-16}$ cm.
- Finite size superstrings of 10^{-33} cm to achieve **unification at 10^{19} GeV** (Planck mass).
CPT fails at 10^{19} GeV or perhaps at lower energies (as curled-up dimensions decrease the unification energy)

The CPT theorem rests on a foundation which is unsound at the Planck length.

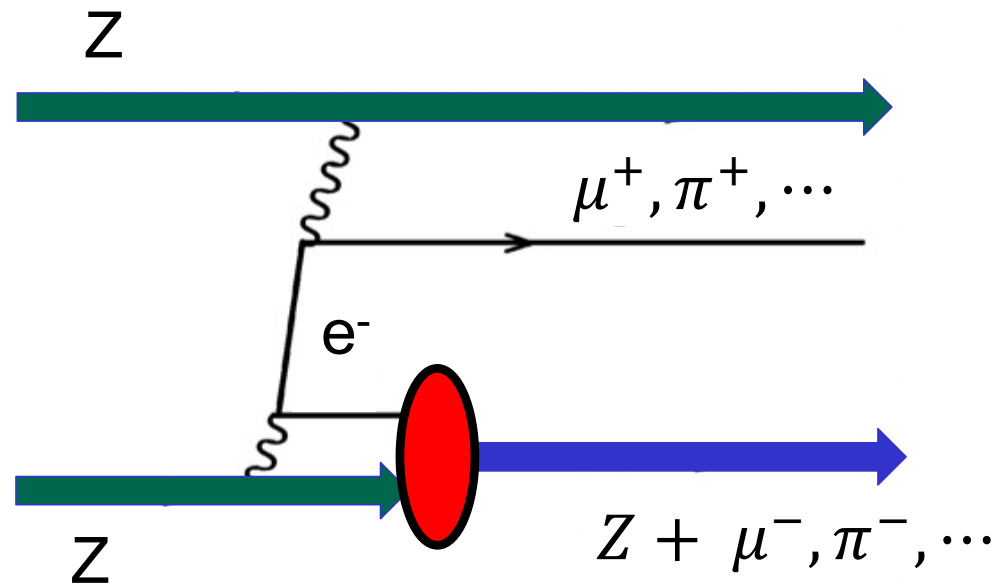
The symmetry of matter and antimatter must rest on experimental evidence.

→ Antihydrogen experiments at CERN: ATHENA, ATRAP, ALPHA, GBAR, PUMA, etc.



Production of exotic Atoms

Bertulani, Ellerman, PRC 81, 044910 (2010)



$$\begin{aligned}
 Z + Z &\rightarrow (Z + \mu^-) + Z + \mu^+ \\
 &\rightarrow (Z + \pi^-) + Z + \pi^+ \\
 &\rightarrow \dots
 \end{aligned}$$

Ingredients:

1. Perturbation theory
2. LO + NLO

$$\Psi_+ = \left[\frac{2\pi a_+}{e^{2\pi a_+} - 1} \right]^{1/2} \left[e^{-ik_+ \cdot r} \boldsymbol{v} + \Psi_{NLO} \right]$$

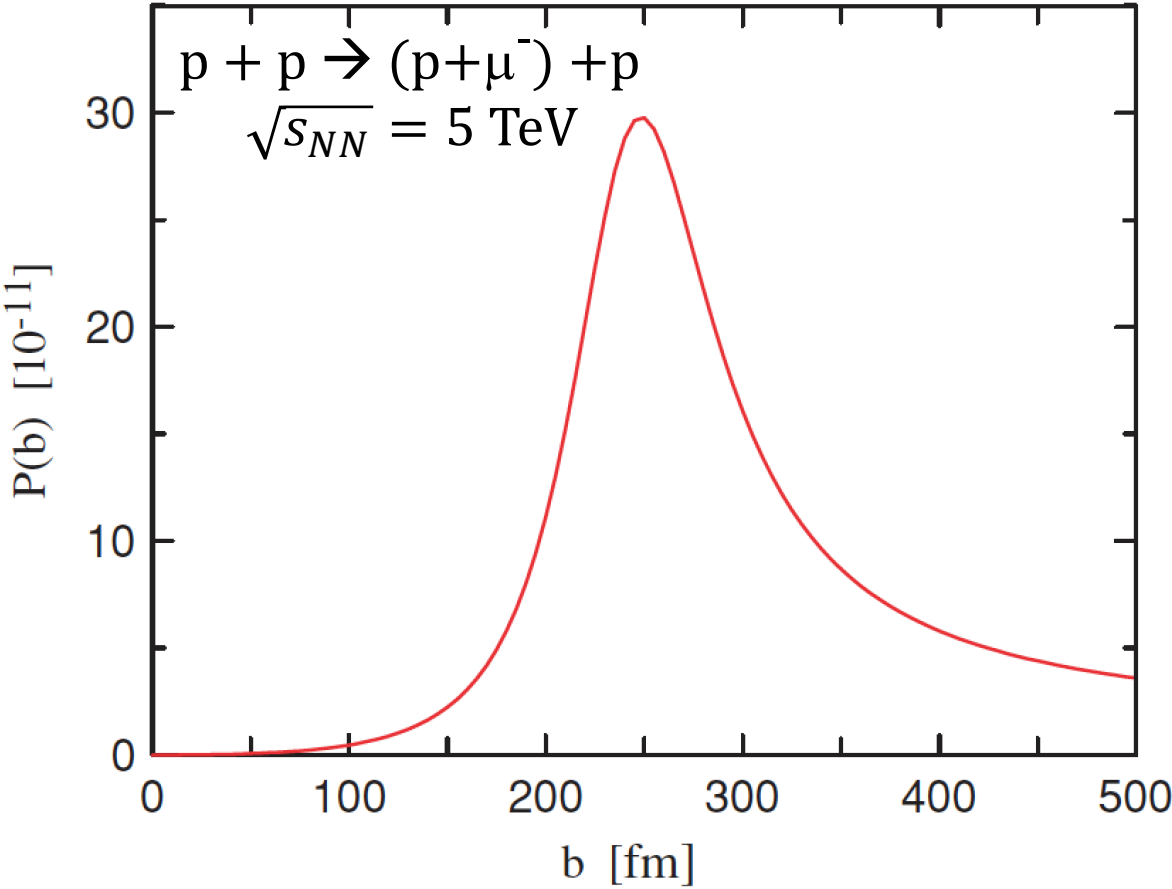
$$\Psi_{NLO} = \frac{Z\alpha}{2\pi^2} \int dq^3 e^{iq \cdot r} \frac{2\gamma^0 E_+ + i\boldsymbol{\gamma} \cdot (\boldsymbol{q} - \boldsymbol{k}_+)}{(q - k_+)^2 (q^2 - k_+^2)}$$

3. Virtual photons expanded in multipoles (E1, E2, ...)

4. Bound state wavefunction for μ⁻, π⁻, ...

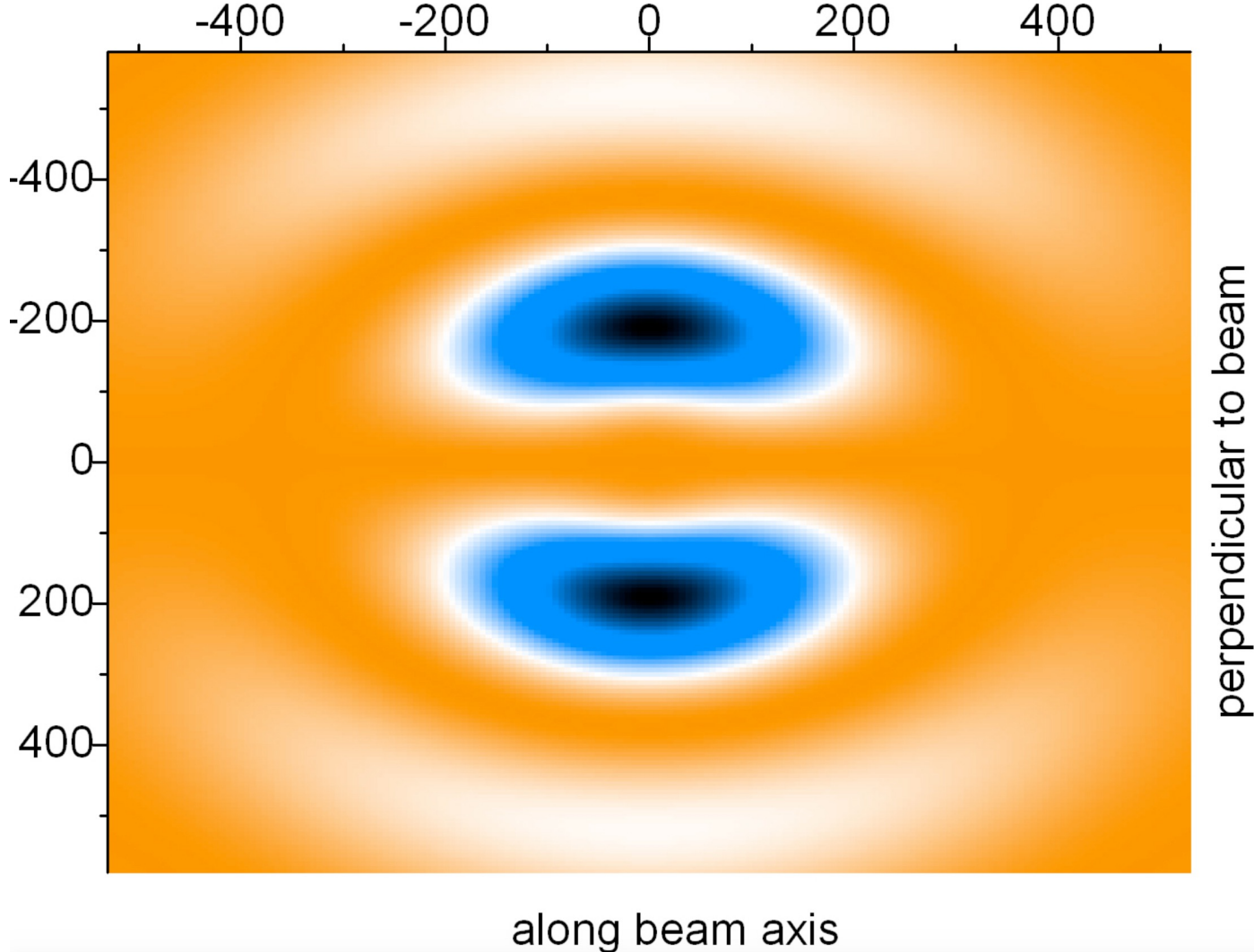
$$\Psi_- = \left[\frac{(Zm\alpha)^3}{\pi} \right]^{1/2} \left[1 + \frac{i}{2} (Z\alpha) \boldsymbol{\alpha} \cdot \frac{\boldsymbol{r}}{r} \right] e^{-(Zm\alpha)r} u$$

Production of exotic Atoms

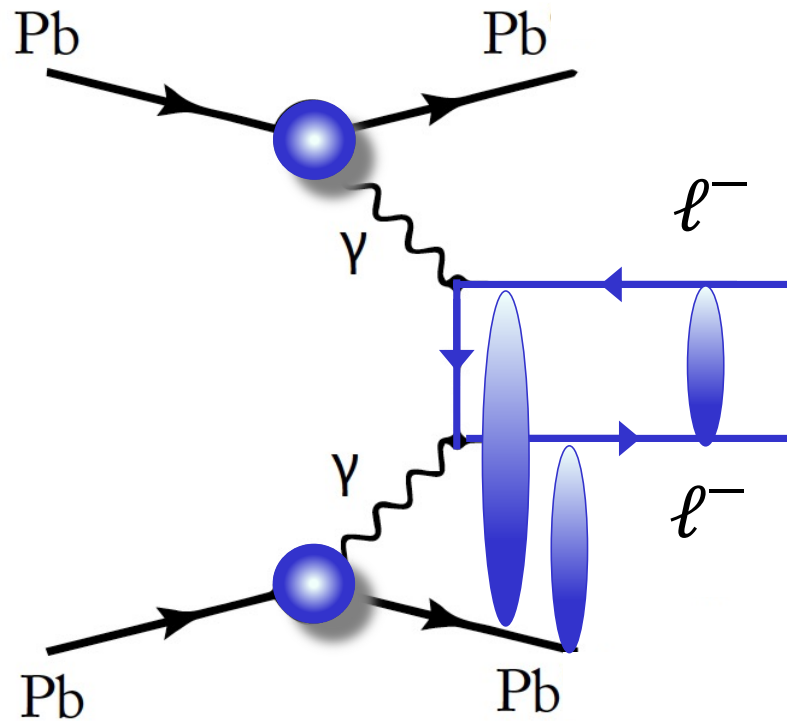


- Production probability maximum at impact parameters
 $b \sim a_{\mu,\pi,\dots}^H$ (Bohr radius)
 e.g., $b \sim 255 \text{ fm}$ for muons

- Production dominated by **electric dipole** (~70%), but electric quadrupole has a substantial contribution (~30%)



Free pair production



Because of Dirac (and cosmic rays):
Lifshitz (1934), Bhabha (1935), Racah (1937), Nishina,
Tomonaga, Kobayashi (1935), Landau (1934)

$$\sigma \sim 200 \text{ kilobarns}$$

at the LHC (10^7 pairs/second)

Coulomb distortions important for large Z
CB, Baur, Phys. Rep. 163, 299 (1988)

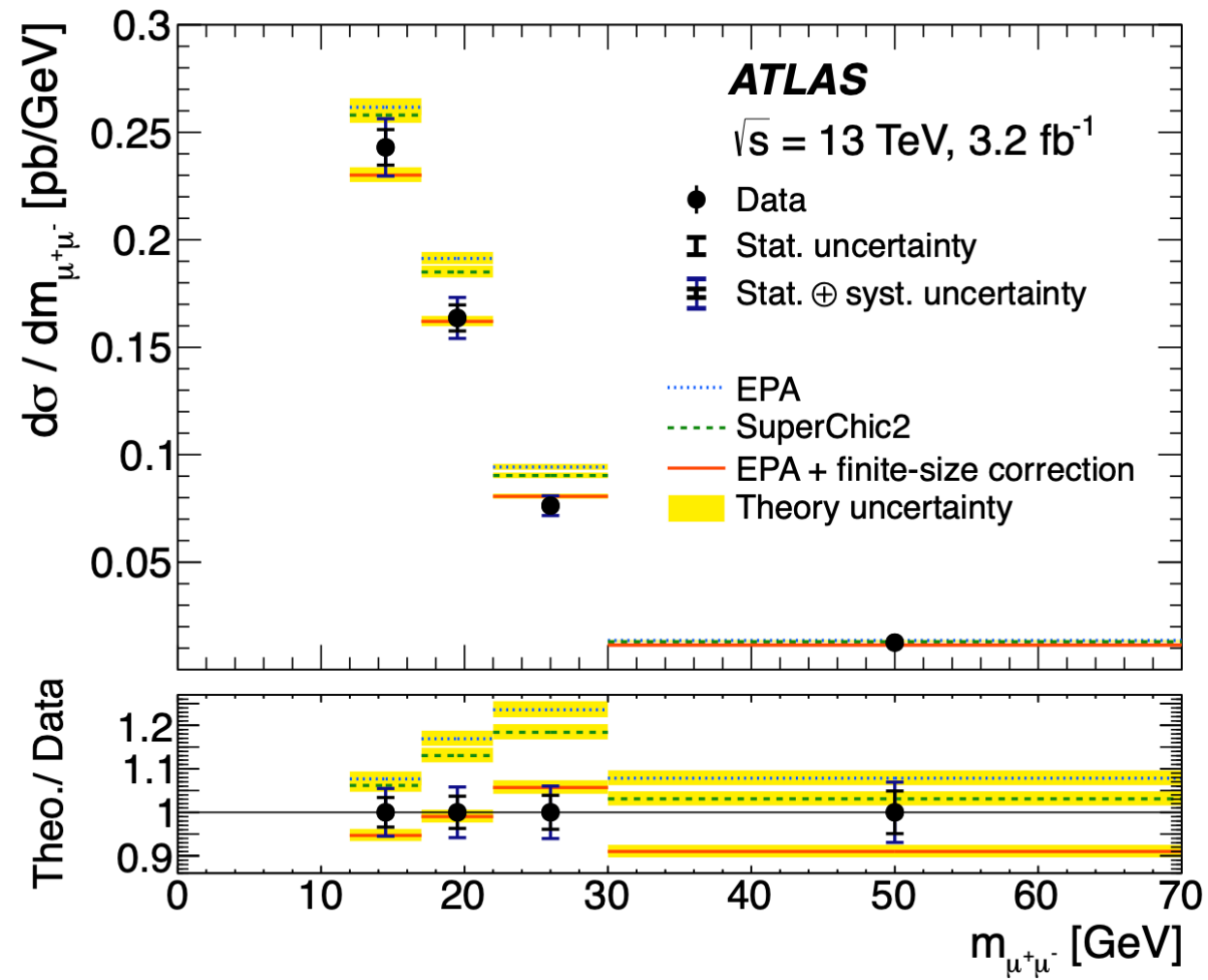
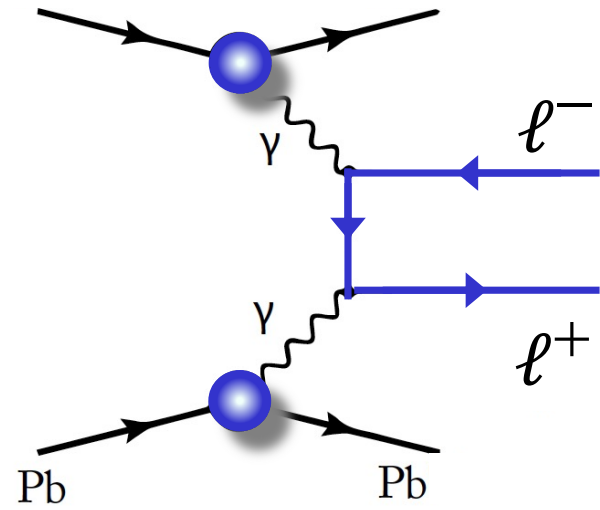
Higher order corrections and multiple pair production
Baur et al., Phys. Rep. 364, 359 (2002)

Cosmic rays experiments difficult

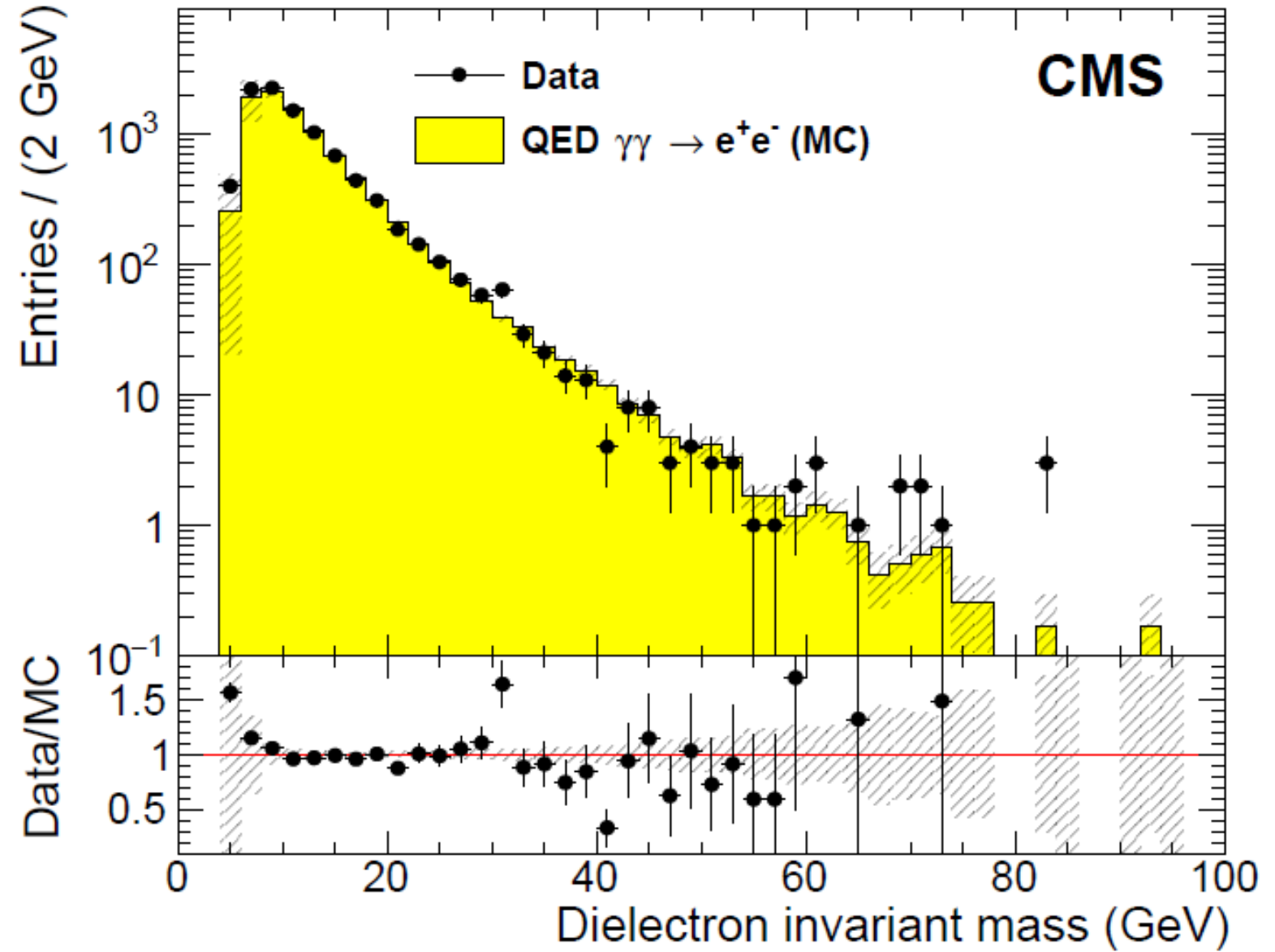
Laboratory experiments difficult and inconclusive
for many decades

(Credit: Asimmetrie/INFN)

Free pair production



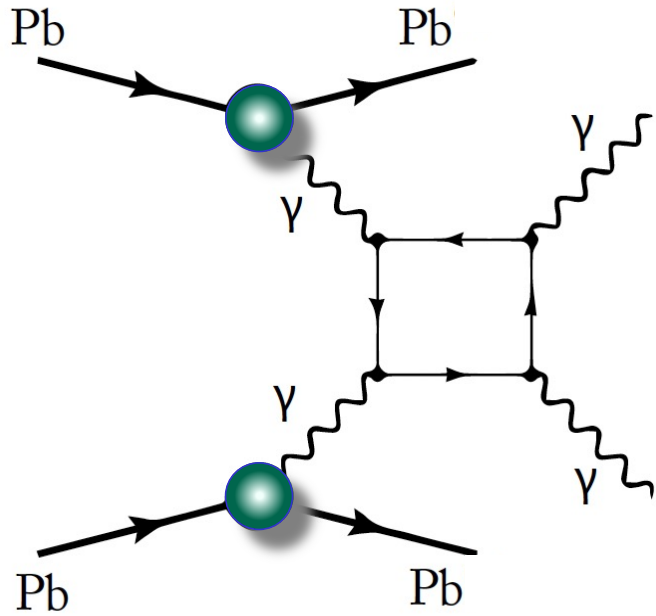
PbPb 390 μb^{-1} (5.02 TeV)



CMS collaboration, JHEP 1201, 052 (2012)

ATLAS collaboration, PLB 777, 303 (2018)

Light-by-light scattering in UPCs



First proposed in

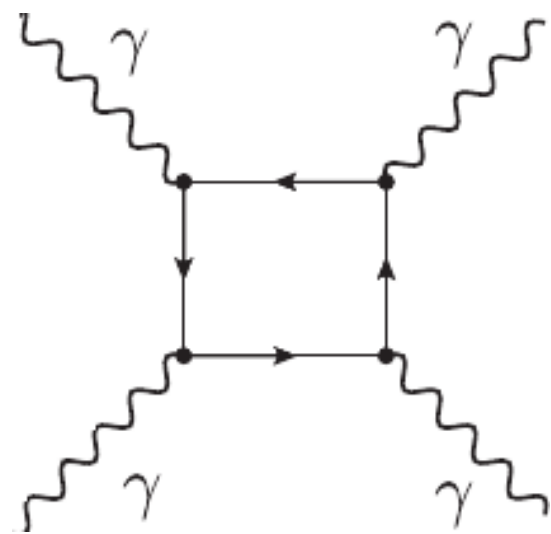
Electromagnetic physics at relativistic heavy ion colliders, for better and for worse
 G. Baur and CB, Nucl. Phys. A505, 835 (1989)

$$\sigma_{\square \rightarrow ZZ\gamma\gamma} = 2.54 \frac{Z^4 \alpha^6}{m_e^2} \left[\ln^3 x - \frac{3}{2} \ln^2 x + \frac{3}{2} \ln x - \frac{3}{4} \right]$$

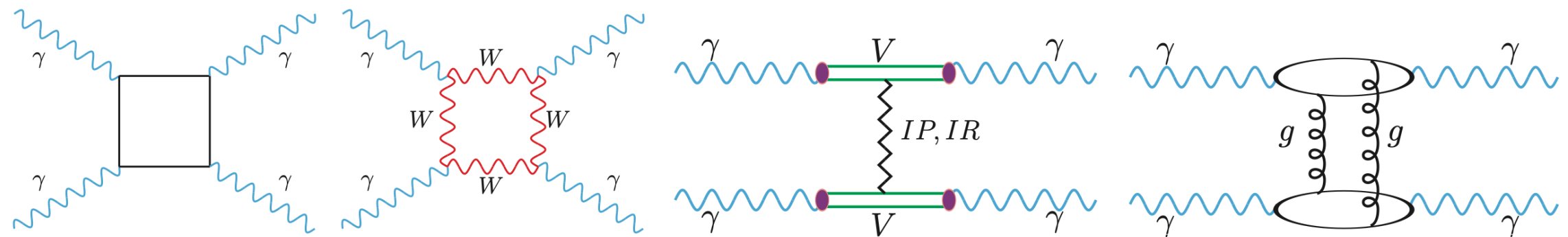
$$x = \frac{\gamma}{R m_e}$$

$\sigma \sim 10^8$ larger than in pp or e^+e^- collisions, although tiny (400 nb)

- Box might contain virtual charged particles (q, ℓ , W) from the SM.
- New charged particles (s-particles, monopoles, unparticles,...)

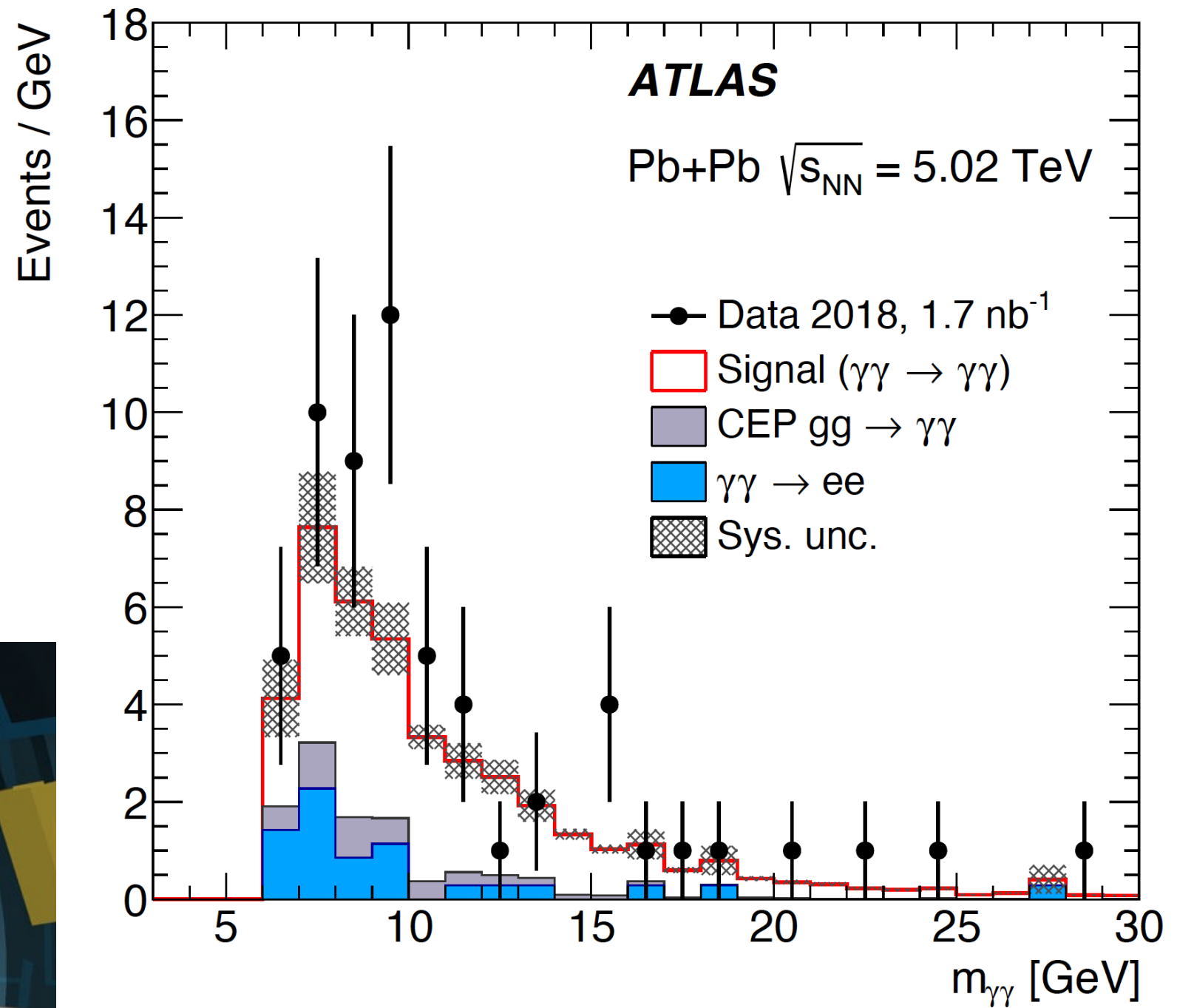
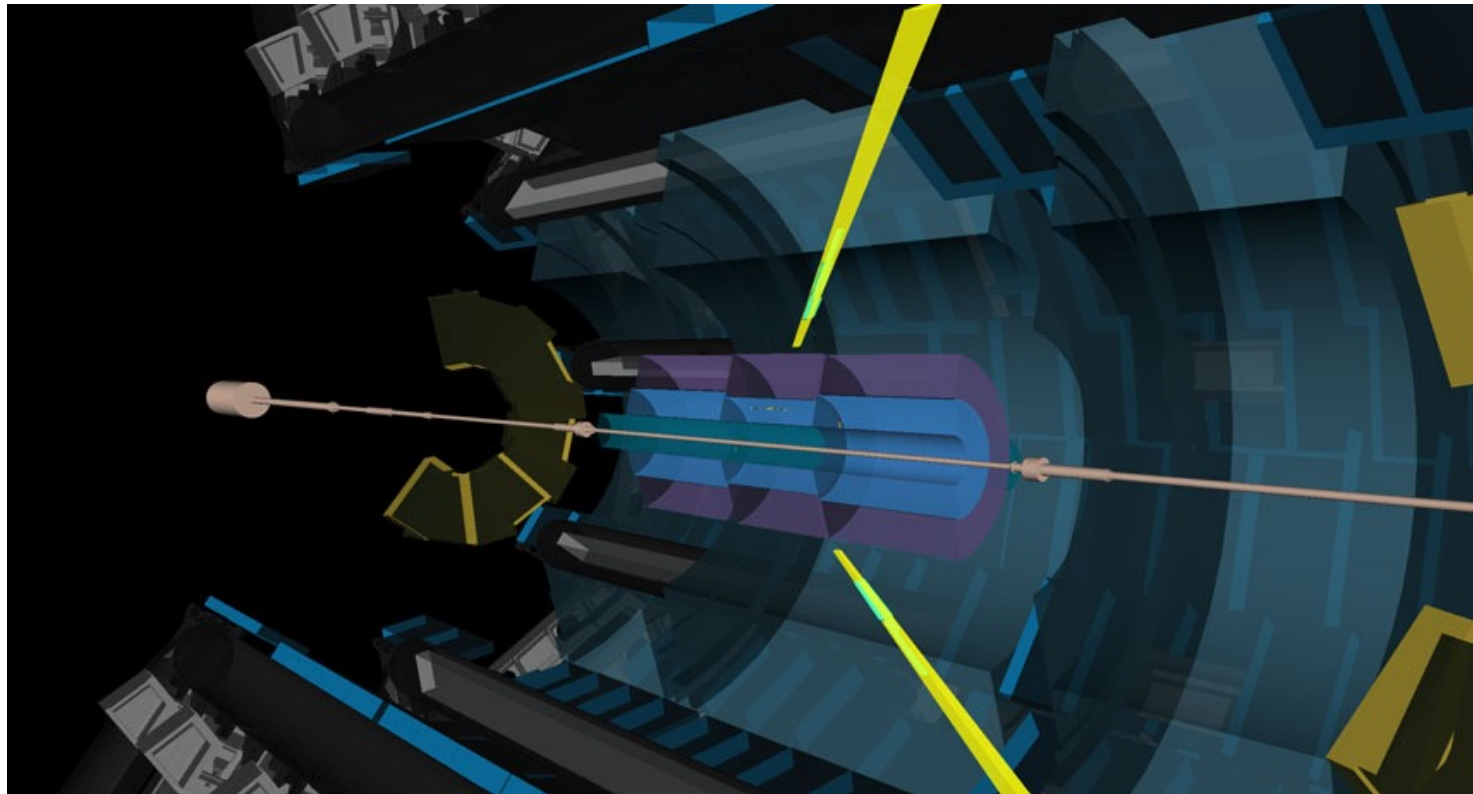
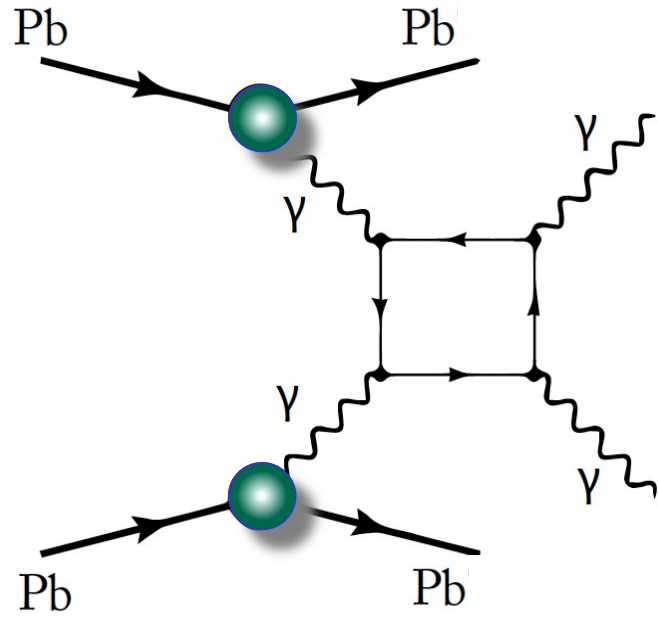


$\sim \mathcal{O}(\alpha^4)$



Kłusek-Gawenda, Lebiedowicz, Szczurek, PRC 93, 044907 (2016)

Light by light scattering



ATLAS collaboration,
Nature Physics 13, 852 (2017)

$\gamma\gamma \rightarrow$ bound states

$$e^+e^- \rightarrow \gamma\gamma \text{ rate} = \alpha^2 \cdot \text{overlap probability} / \text{interaction time}$$

$$= \alpha^2 \cdot (|\psi(0)|^2 / m_e^3) \cdot m_e$$

$$\Delta t = 1/m_e$$



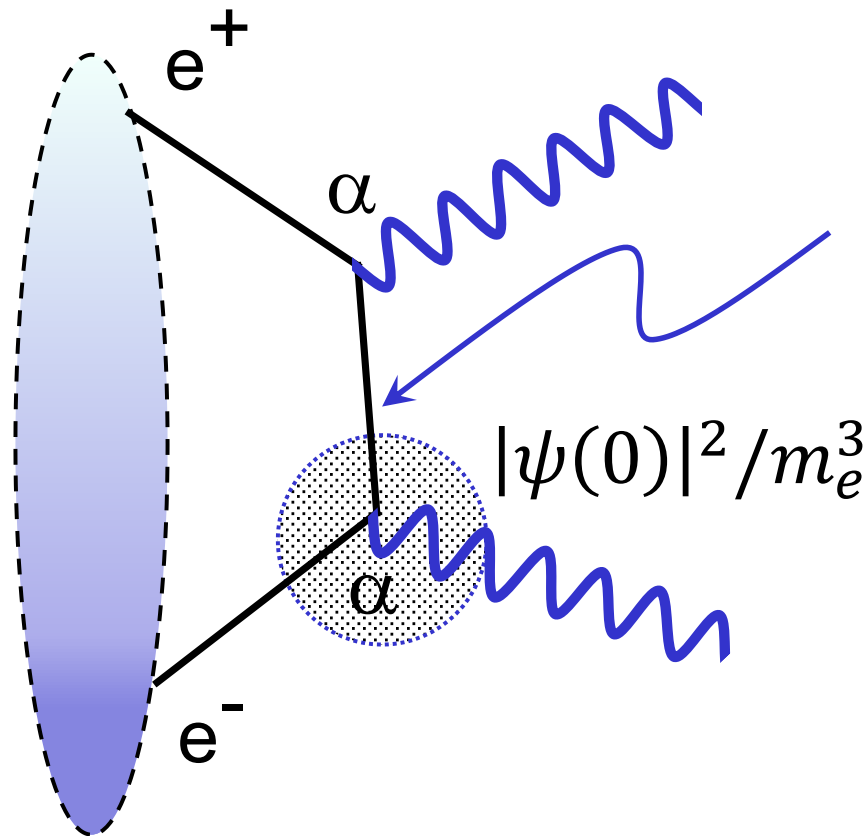
$$\Gamma \sim \alpha^2 |\psi(0)|^2 / m_e^2$$

RECIPE:

- replace electrons by quarks
- get rid of $|\psi(0)|^2$

van Royen, Weisskopf, Nuovo Cimento A 50, 617 (1967)

Appelquist, Politzer, PRL 34, 365 (1975)



$$\Gamma_{\gamma\gamma}^{J=0} = \frac{48\pi\alpha^2}{M^2} |\Psi(0)|^2 \sum_i Q_i^4$$

$$\Gamma_{\gamma\gamma}^{(J=2)} = (2J + 1) \Gamma_{\gamma\gamma}^{(J=0)} = 5 \Gamma_{\gamma\gamma}^{(J=0)}$$

Example: parapositronium ($S = 0$)

$$|\Psi(0)|^2 = (m_e \alpha)^3 / 8\pi n^3$$

Exploring Widths of various Mesons at CERN: CB, PRC 79, 047901 (2009)

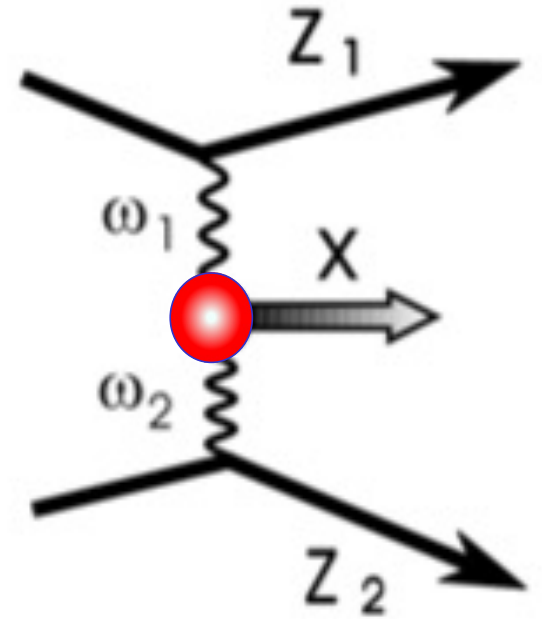
$\gamma\gamma \rightarrow$ bound states

Detailed balance + Fermi's golden rule [F. Low, Phys. Rev. 120, 582 \(1960\)](#)

$$\rightarrow \sigma_{\gamma\gamma}^X(\omega_1, \omega_2) = 8\pi^2 (2J + 1) \frac{\Gamma_{X \rightarrow \gamma\gamma}}{m_X} \delta(\omega_1 \omega_2 \rightarrow m_X^2)$$

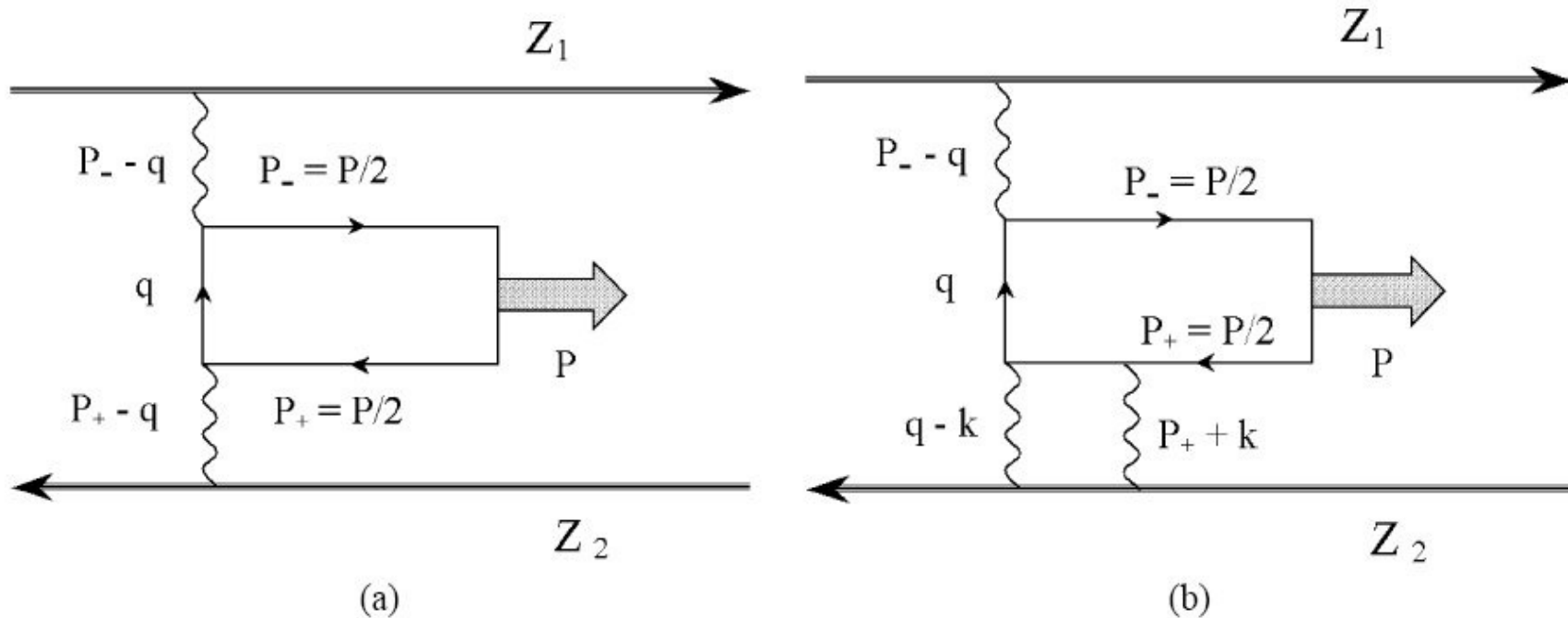
EPA method: [G. Baur and CB, Nucl. Phys. A505, 835 \(1989\)](#)

$$\sigma_{ZZ \rightarrow ZZ+X} = \int \frac{n_1(\omega_1)}{\omega_1} \frac{n_2(\omega_2)}{\omega_2} \sigma_{\gamma\gamma}^X(\omega_1, \omega_2) d\omega_1 d\omega_2$$



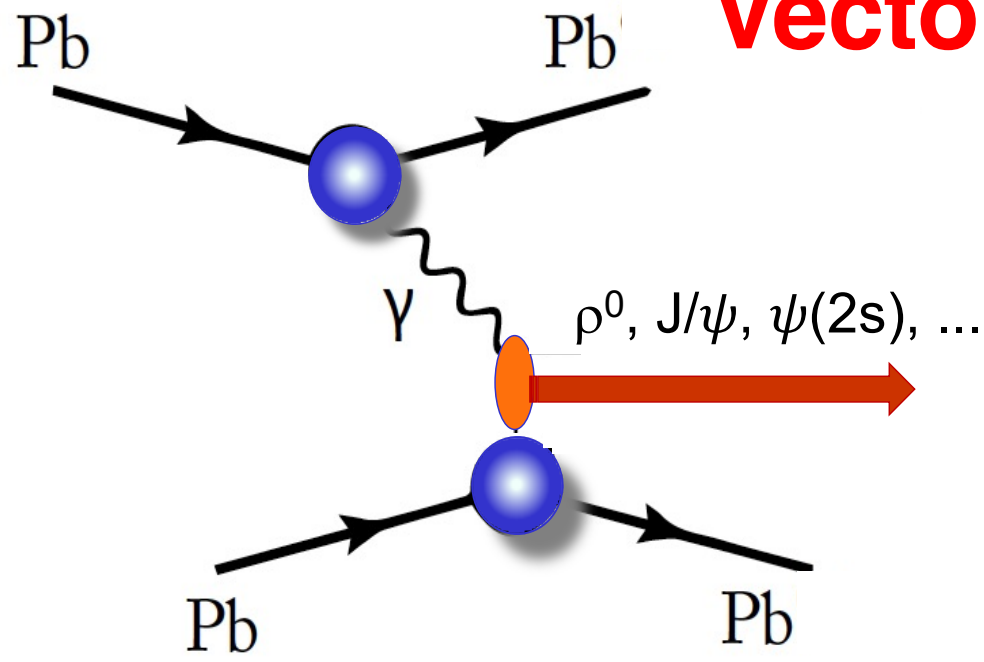
Or calculate corresponding Feynman diagrams and use Weisskopf-Royen projection

[CB, F. Navarra, NPA 703 \(2002\) 861](#)



$$\begin{aligned} \mathbf{J=0} \quad \bar{u}Av &\rightarrow \sqrt{2m_X} \operatorname{tr} \left(\frac{A}{\sqrt{2}} \right) \psi(0) \\ \mathbf{J=1} \quad \bar{u}Av &\rightarrow \sqrt{2m_X} \operatorname{tr} \left(\frac{\hat{\mathbf{e}} \cdot \boldsymbol{\sigma}}{\sqrt{2}} A \right) \psi(0) \end{aligned}$$

Vector meson production (direct, unresolved)



$$\left. \frac{d\sigma^{\gamma A \rightarrow VA}}{dt} \right|_{t=0} = \frac{16\pi^3 \alpha_s \Gamma_{ee}}{3\alpha M_V^5} [xg_A(x, Q^2)]^2_{\text{gluons}}$$

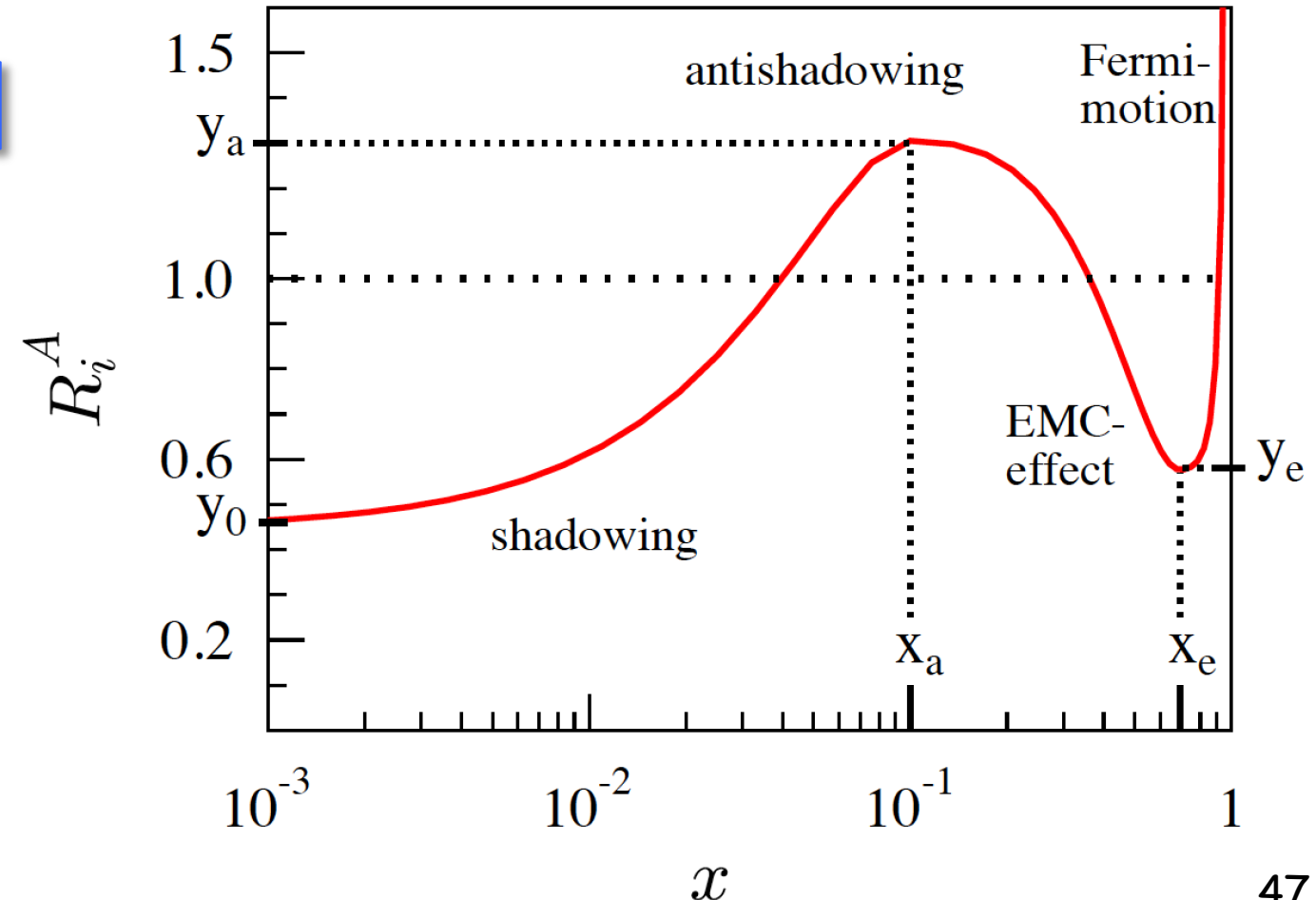
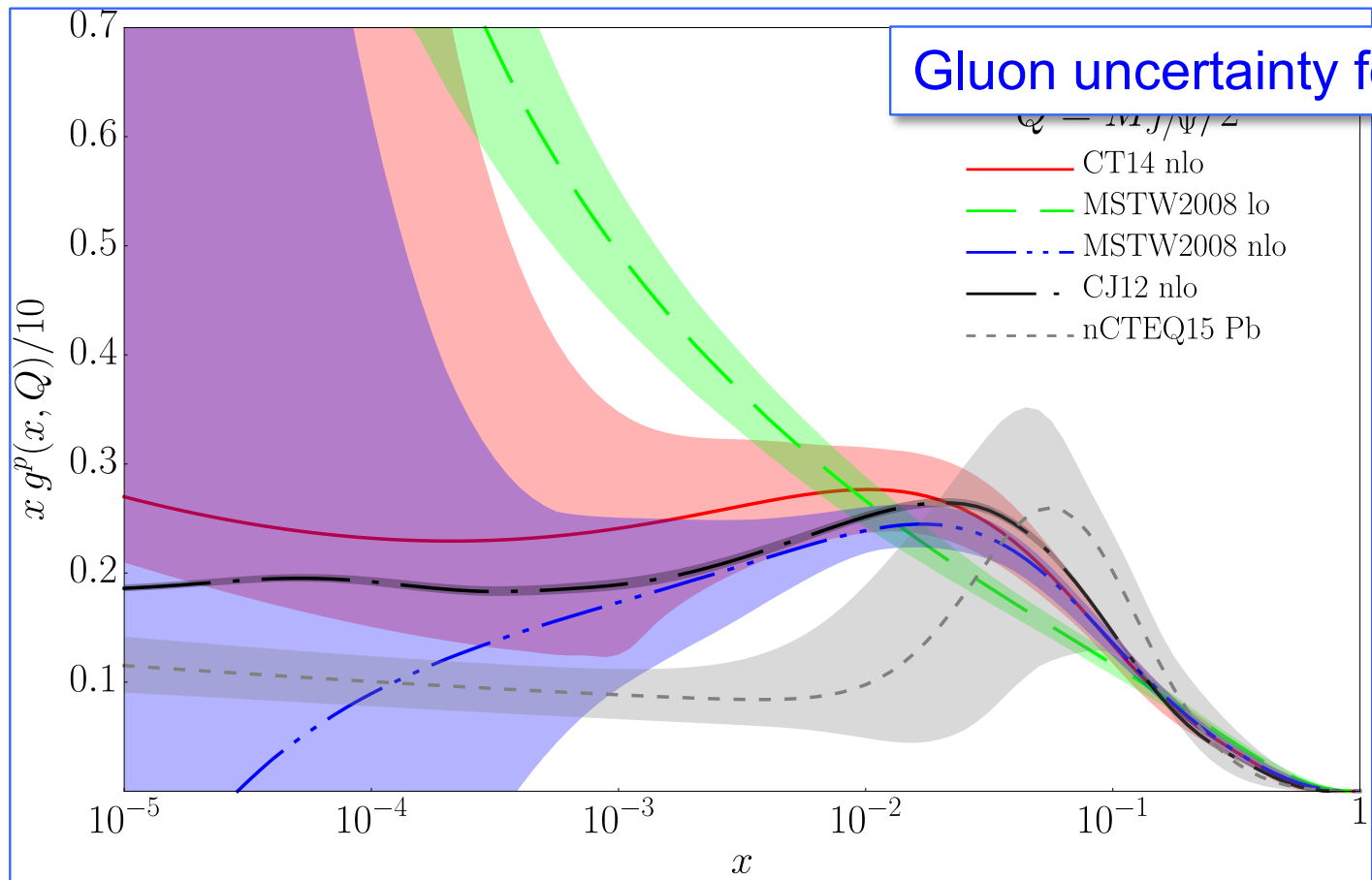
Goncalves, CB, PRC65, 054905 (2002)

Adeluyi, CB, PRC 85, 044904 (2012); C 85, 044904 (2012)

Direct dominant over resolved (photon $q\bar{q}$ content)

Gluon uncertainty for nPDF

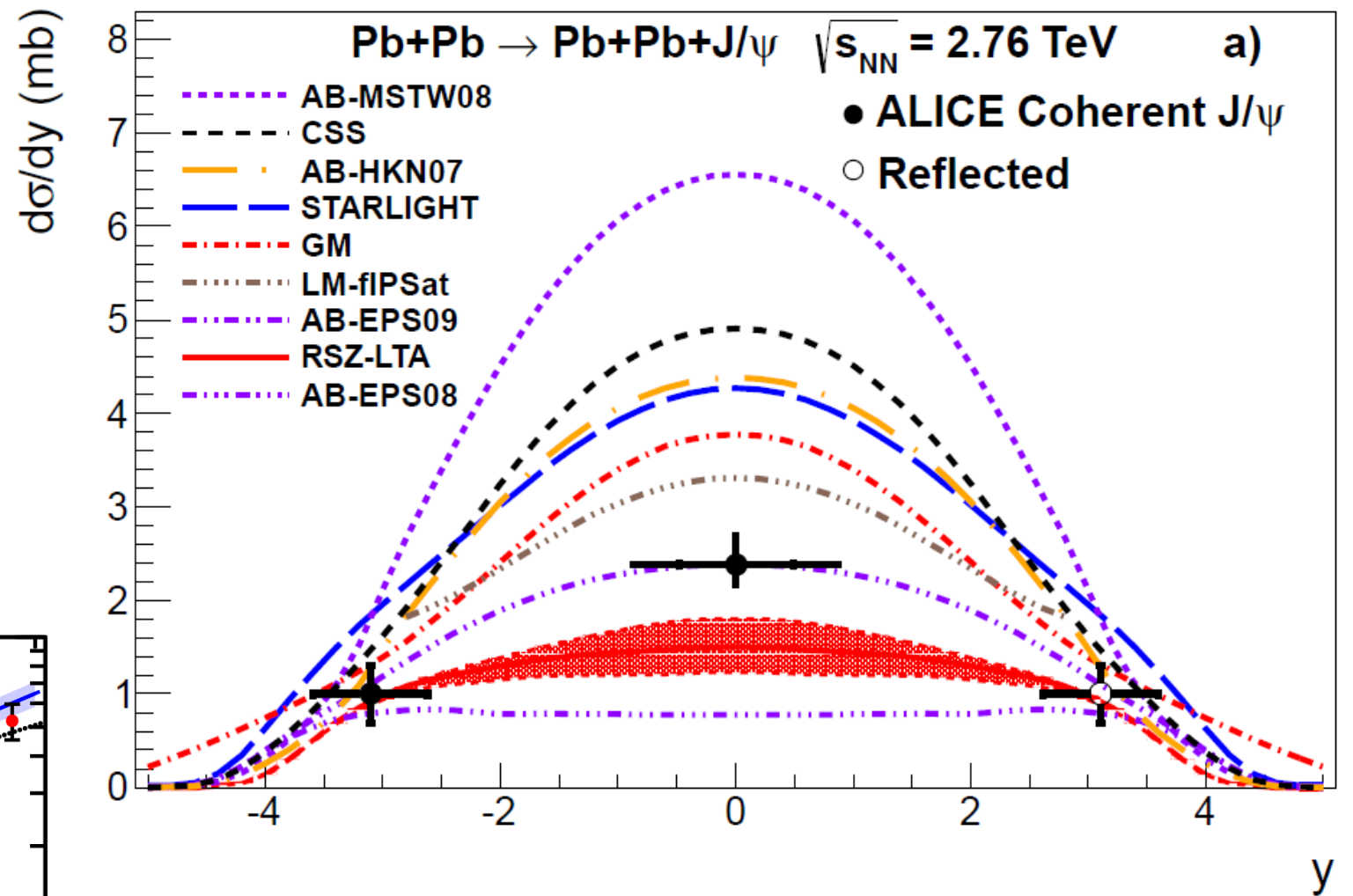
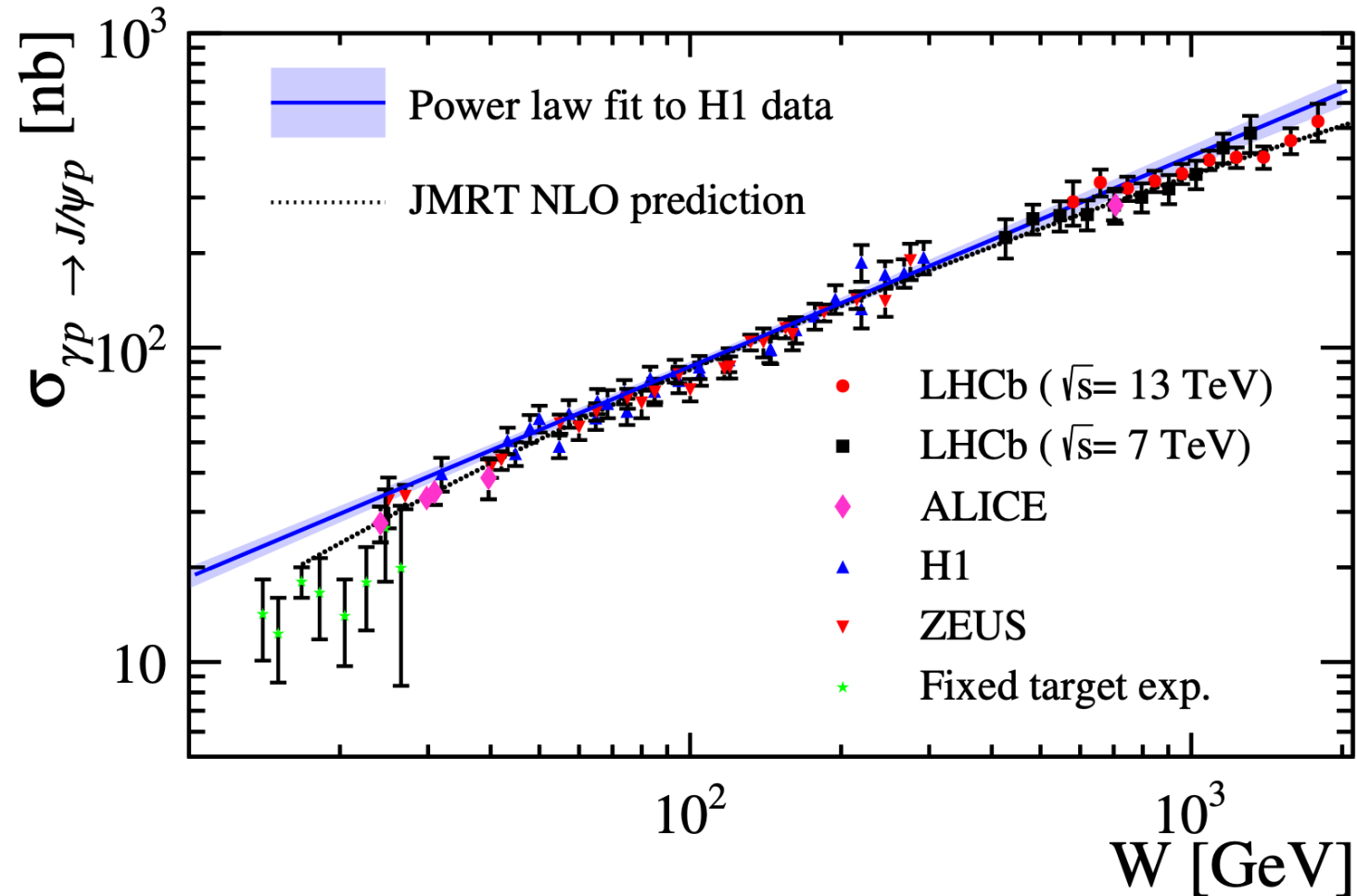
- CT14 nlo
- MSTW2008 lo
- - - MSTW2008 nlo
- CJ12 nlo
- - - nCTEQ15 Pb



J/ψ production & PDFs

ALICE collaboration,
PLB 718, 1273 (2013)
Eur. Phys. J. C73, 2617 (2013)

CMS collaboration,
PLB 772 489 (2017)



LHCb collaboration,
JHEP 10, 167 (2018)

How to continue?

LHC PHYSICS

CMS sees first direct evidence for $\gamma\gamma \rightarrow WW$



In a small fraction of proton collisions at the LHC, the two colliding protons interact only electromagnetically, radiating high-energy photons that subsequently interact or “fuse” to produce a pair of heavy charged particles. Fully exclusive production of such pairs takes place when quasi-real photons are emitted coherently by the protons rather than by their quarks, which survive the interaction. The ability to select such events opens up the exciting possibility of transforming the LHC into a high-energy photon–photon collider and of performing complementary or unique studies of the Standard Model and its possible extensions.

The CMS collaboration has made use of this opportunity by employing a novel method to select “exclusive” events based only on tracking information. The selection is made by requesting that two – and only two – tracks originate from a candidate vertex for the exclusive two-photon production. The power of this method, which was first developed for the pioneering measurement of exclusive production of muon and electron pairs, lies in its effectiveness even in difficult high-luminosity conditions with large event pile-up at the LHC.

The collaboration has recently used this approach to analyse the full data sample collected at $\sqrt{s}=7$ TeV and to obtain the first direct evidence of the $\gamma\gamma \rightarrow WW$ process. Fully leptonic W-boson decays have been measured in final states characterized by opposite-sign and opposite-flavour lepton pairs where one W decays into an electron and a neutrino, the other into a muon and a neutrino (both neutrinos leave undetected). The leptons were required to have: transverse momenta $p_T > 20$ GeV/c and pseudorapidity

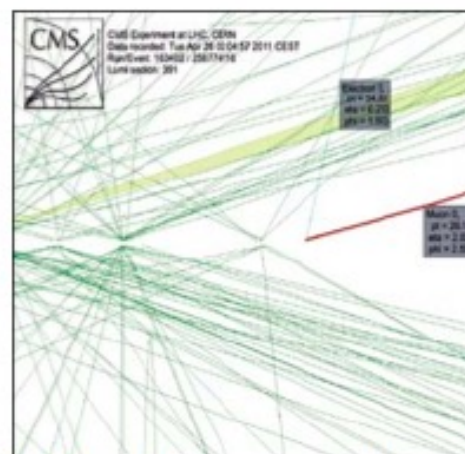


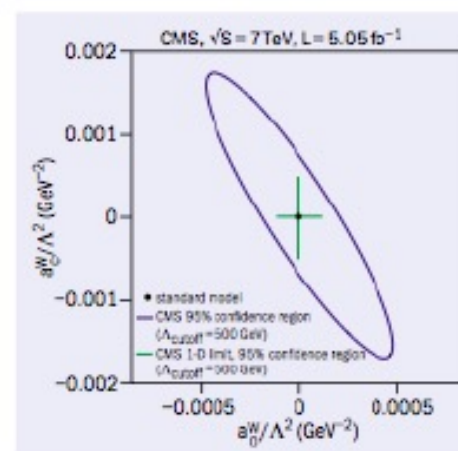
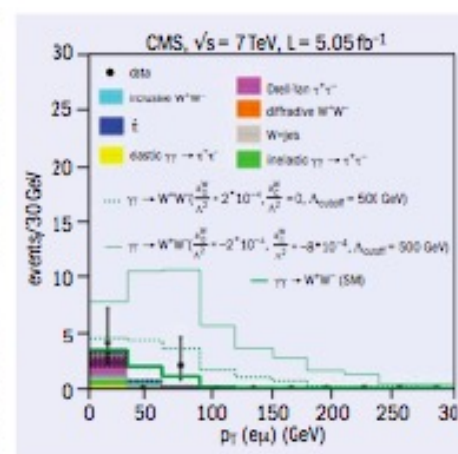
Fig. 1. Above: Proton–proton collisions recorded by CMS at $\sqrt{s}=7$ TeV, featuring candidates for the exclusive two-photon production of a WW pair, where one W boson has decayed into an electron and a neutrino, the other into a muon and a neutrino.

Fig. 2. Top right: The p_T distribution of $e\mu$ pairs in events with no extra tracks compared with the Standard Model expectation (thick green line) and predictions for anomalous quartic gauge couplings (dashed green histograms).

Fig. 3. Right: Limits on anomalous quartic $\gamma\gamma WW$ couplings.

$|\eta| < 2.1$; no extra track associated with their vertex; and for the pair, a total $p_T > 30$ GeV/c. After applying all selection criteria, only two events remained – compared with an expectation of 3.2 events: 2.2 from $\gamma\gamma \rightarrow WW$ and 1 from background (figure 2).

The lack of events observed at large values of transverse momentum for the pair, which would be expected within the Standard



Model, allows stringent limits on anomalous quartic $\gamma\gamma WW$ couplings to be derived. These surpass the previous best limits, set at the Large Electron–Positron collider and at the Tevatron, by up to two orders of magnitude (figure 3).

• **Further reading**

CMS collaboration 2013 arXiv:1305.5596 [hep-ex], submitted to *JHEP*.

Search for New Physics (SUSY particles)

Baur et al., Phys. Rep. 364, 359 (2002)

MSSM The Standard Model and supersymmetric particles.

Standard Model	Supersymmetry
γ, Z^0, h^0, H^0	$\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0$
W^+, H^+	$\tilde{\chi}_1^+, \tilde{\chi}_2^+$
$e^-, \nu_e, \mu^-, \nu_\mu, \nu_\tau$	$\tilde{e}_R^-, \tilde{e}_L^-, \tilde{\nu}_e, \tilde{\mu}_R^-, \tilde{\mu}_L^-, \tilde{\nu}_\mu, \tilde{\nu}_\tau$
τ^-	$\tilde{\tau}_1, \tilde{\tau}_2$
u, d, s, c	$\tilde{u}_R, \tilde{u}_L, \tilde{d}_R, \tilde{d}_L, \tilde{s}_R, \tilde{s}_L, \tilde{c}_R, \tilde{c}_L$
b	\tilde{b}_1, \tilde{b}_2
t	\tilde{t}_1, \tilde{t}_2

$$\gamma\gamma \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \quad (\text{assuming } \tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0)$$

But $M_{\tilde{\chi}_1^\pm} > 67.7 \text{ GeV}$

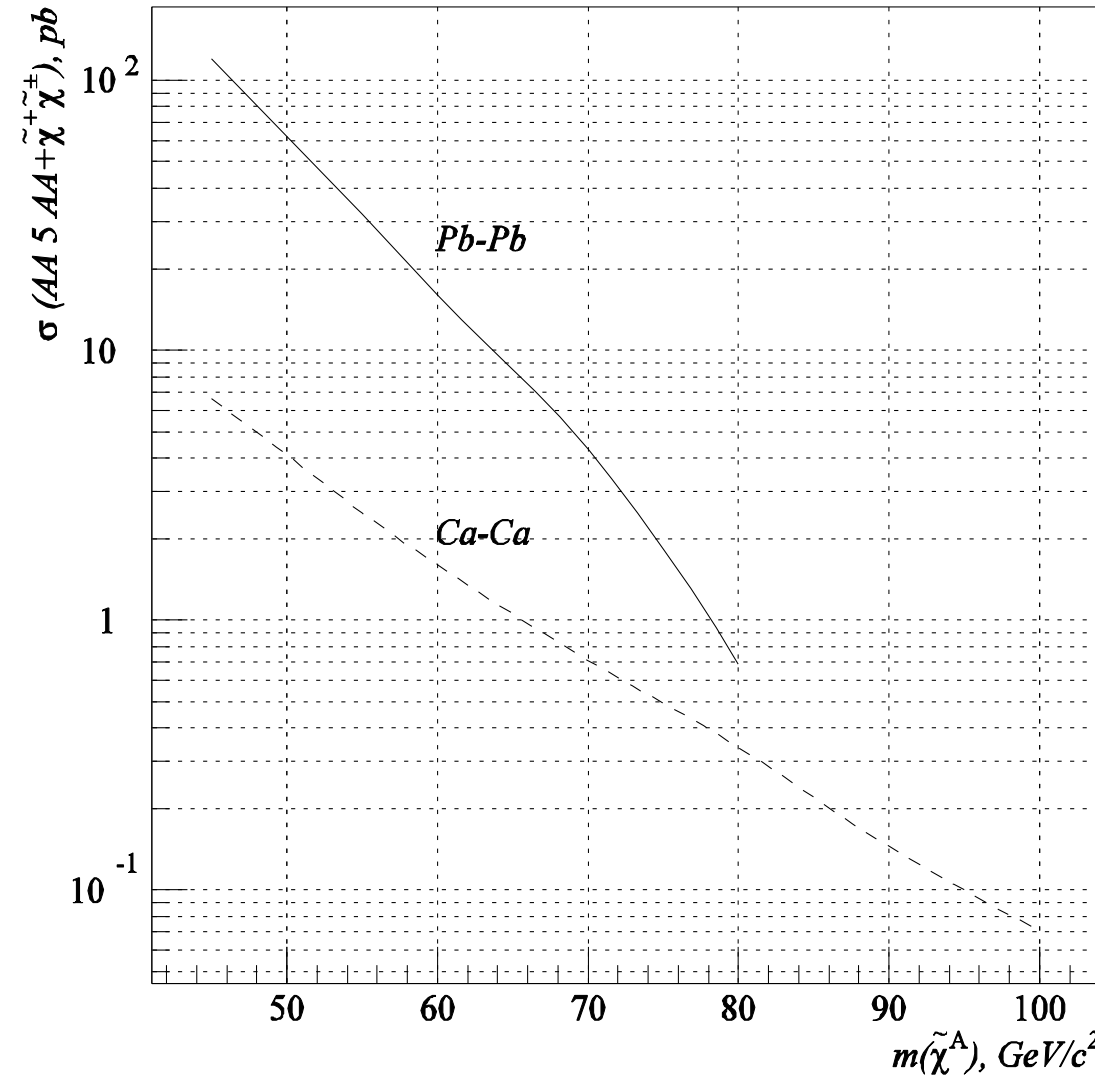


$$\frac{dL}{dW_{\gamma\gamma}} \approx 0$$

for

$$W_{\gamma\gamma} > 200 \text{ GeV}$$

(LHC)



(unlikely?)

Beyond the Standard Model

Higgs: $\gamma\gamma \rightarrow H$ $\sigma \approx 1 \text{ nb}$ at the LHC

Swamped by
 $\gamma\gamma \rightarrow b\bar{b}$ background

Papageorgiu, PRD 40, 92 (1989)

Extra dimensions (Kaluza-Klein):

$$\gamma\gamma \rightarrow \text{graviton}$$

$$\sigma_{\gamma\gamma \rightarrow \text{graviton}} (\text{LHC}) \gg \sigma_{e^+e^- \rightarrow \text{graviton}} (\text{LEP II})$$

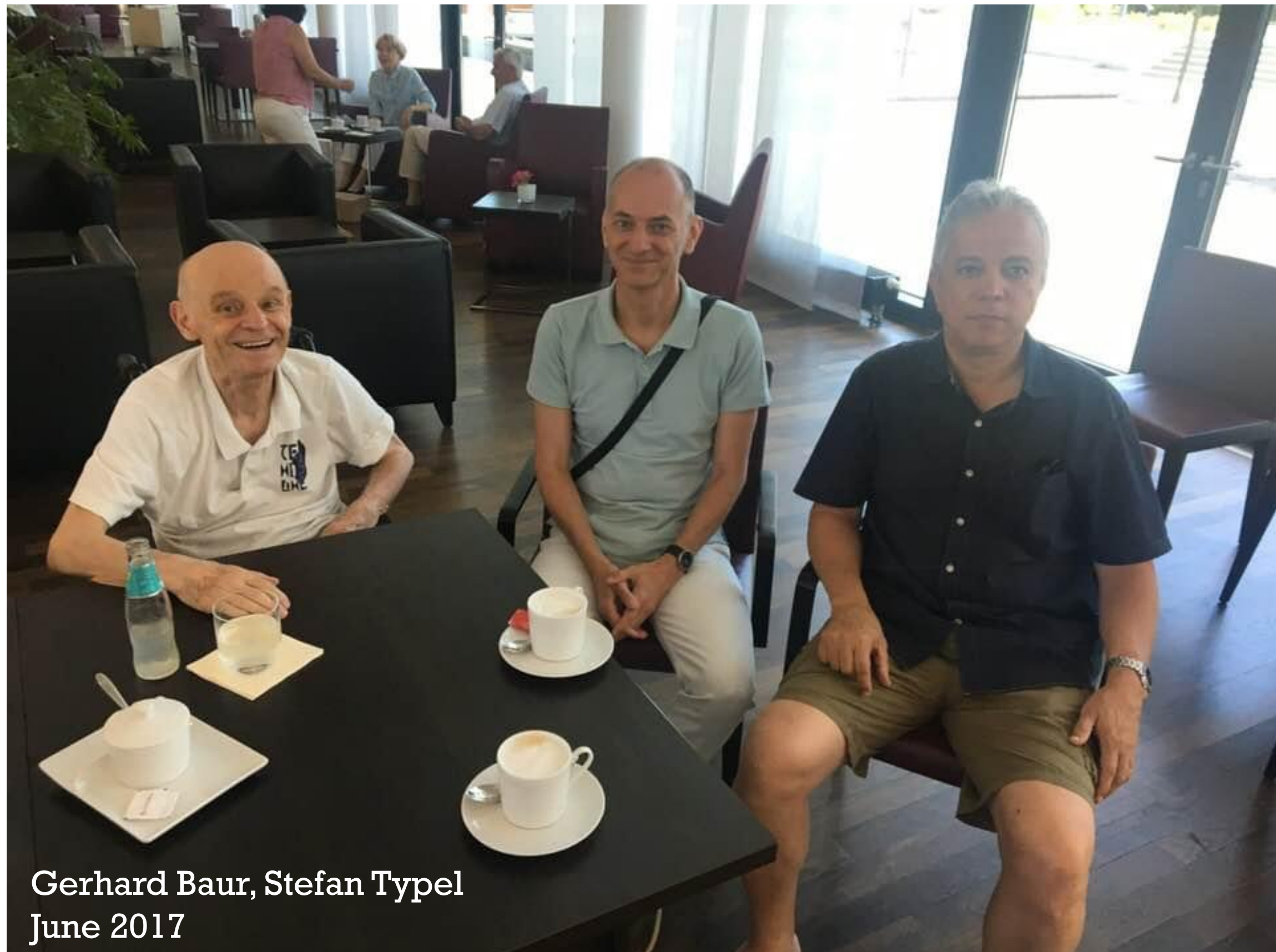
Ahern, Norbury, Poyser, PRD 62, 116001 (2000)

Searching for axionlike particles with low masses

Goncalves, Martins, Rangel, Eur. Phys. J C 81, 522 (2021)

Conclusions

- Ultraperipheral Collisions (UPC) source of the strongest EM fields
- UPCs \rightarrow antihydrogen, atomic and nuclear structure, giant resonances
- UPCs \rightarrow (n,γ) , (p,γ) , (α,γ) for astrophysics
- UPCs \rightarrow exotic meson production
- UPCs \rightarrow parton distribution functions
- UPCs \rightarrow Pygmy resonances, hypernuclei and neutron stars



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