

# Developing optical potentials from $\chi_{\text{EFT}}$ NN interactions to describe nuclear reactions involving exotic nuclei

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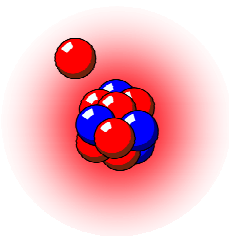
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# Halo Nuclei

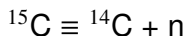
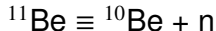
Exotic nuclear structures are found far from stability  
 In particular halo nuclei with peculiar quantal structure :

- Light, **n-rich** nuclei
- Low  $S_n$  or  $S_{2n}$

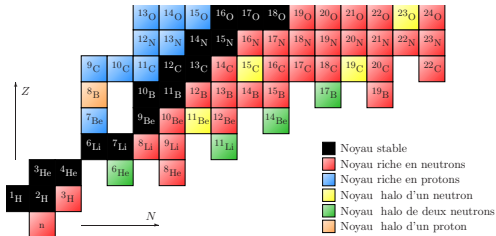
Exhibit **large matter radius**  
 due to strongly clustered structure :  
 neutrons tunnel far from the **core** and form a **halo**



## One-neutron halo



## Two-neutron halo



**Proton** halos are possible but less probable :  ${}^8\text{B}$ ,  ${}^{17}\text{F}$

## Reactions with Halo Nuclei

Halo nuclei are **fascinating** objects  
but difficult to study [ $\tau_{1/2}(^{11}\text{Be})= 13 \text{ s}$ ]

⇒ require **indirect** techniques, new **probes**, like reactions :

**Elastic scattering**

**Transfer**

**Knockout**

**Breakup** ≡ dissociation of **halo** from **core**  
by interaction with target

Need good understanding of the reaction mechanism

(i.e. a good **reaction model**)

have reliable inputs for the model

(i.e. **optical potentials** to describe the interactions with target)

## Few-Body Model of Reaction

**Projectile** ( $P$ ) modelled as a two-body quantum system :  
**core** ( $c$ ) + loosely bound **nucleon** ( $n$ ) described by

$$H_0 = T_r + V_{cn}(\mathbf{r})$$

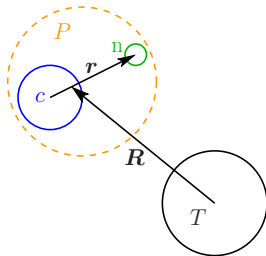
$V_{cn}$  effective interaction  
 describes the **quantum system**  
 with ground state  $\Phi_0$

Target  $T$  assumed structureless

Interaction with target simulated by **optical potentials**  
 $\Rightarrow$  breakup reduces to **three-body** scattering problem :

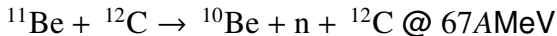
$$[T_R + H_0 + V_{cT} + V_{nT}] \Psi(\mathbf{r}, \mathbf{R}) = E_T \Psi(\mathbf{r}, \mathbf{R})$$

with initial condition  $\Psi(\mathbf{r}, \mathbf{R}) \xrightarrow{Z \rightarrow -\infty} e^{iKZ} \Phi_0(\mathbf{r})$

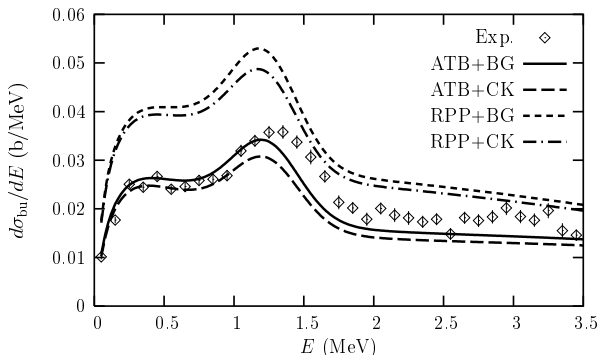


## Significance of Optical Potentials

Breakup of  $^{11}\text{Be}$  on C depends on  $V_{cT}$  (and slightly on  $V_{nT}$ )



[P.C., Goldstein, Baye, PRC 70, 064605 (2004)]



Exp. : [Fukuda *et al.* PRC 70, 054606 (2004)]

Since the core  $c$  is itself exotic,  $V_{cT}$  is usually poorly known  
 $\Rightarrow$  We build optical potentials by double-folding of  $\chi_{\text{EFT}} V_{\text{NN}}$

# Nucleus-Nucleus Interaction

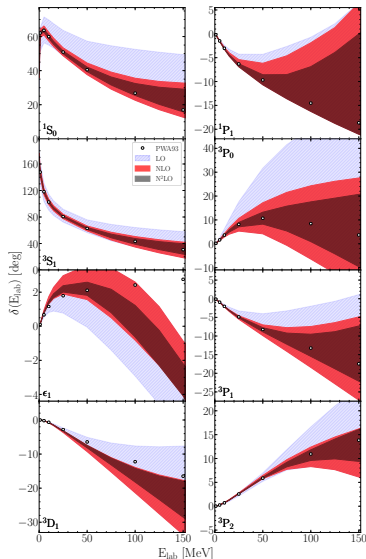
**Idea** : using a double-folding procedure with accurate NN interactions from  $\chi_{\text{EFT}}$

Gezerlis *et al.* have developed **local** NN interactions up to N<sup>2</sup>LO

[PRL 111, 032501 (2013),  
PRC 90, 054323 (2014)]

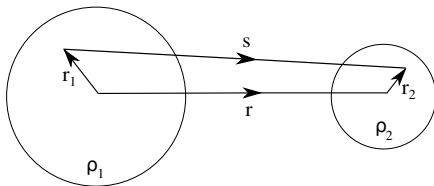
Based on this formalism, we build a **double-folding** potential

[Durant *et al.* PLB 782, 668 (2018)]



## Double-folding potential : Real Part

We build a double-folding potential at the Hartree-Fock level



$$V_F = V_D + V_{EX}$$

$$V_D(r) = \int \rho_1(\mathbf{r}_1) \rho_2(\mathbf{r}_2) v_D(s) d\mathbf{r}_1 d\mathbf{r}_2$$

$$V_{EX}(r, E) = \int \rho_1(\mathbf{r}_1, \mathbf{r}_2 + \mathbf{s}) \rho_2(\mathbf{r}_2, \mathbf{r}_1 - \mathbf{s}) v_{EX}(s) \exp\left[\frac{i\mathbf{k}(r) \cdot \mathbf{s}}{\mu/m_N}\right] d\mathbf{r}_1 d\mathbf{r}_2$$

$$k^2(r) = \frac{2\mu}{\hbar^2} [E_{c.m.} - V_F(r, E_{c.m.}) - V_{Coul}(r)]$$

$\Rightarrow$  potential built **iteratively**

[Durant *et al.* PLB 782, 668 (2018)]



## Double-folding potential : Imaginary Part

Imaginary part can be taken proportional to real part

$$W(r) = N_W V_F(r)$$

with  $N_W \simeq 0.5-1$

[Pereira *et al.* PLB 670, 330 (2009)]

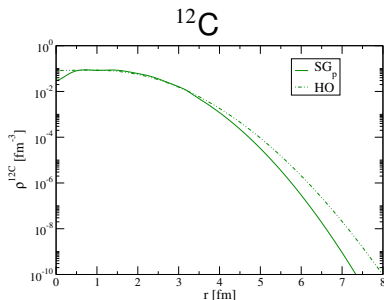
or using **dispersive relations**

[Durant, PC, Schwenk PRC 102, 014622 (2020)]

$$W(r, E_{c.m.}) = -\frac{1}{\pi} \mathcal{P} \int_{-\infty}^{+\infty} \frac{V_{Ex}(r, E)}{E - E_{c.m.}} dE$$

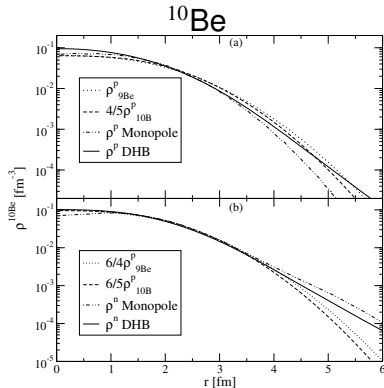
# Nuclear Densities

Use densities from the literature



Densities from  $e$  scattering

- Sum of Gaussians
- Harmonic Oscillator functions



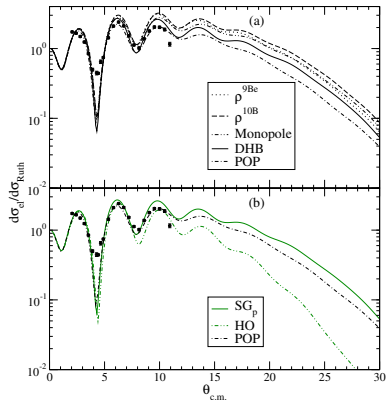
Densities from  $e$  scattering on  $^9\text{Be}$  and  $^{10}\text{B}$

from microscopic calculations

- cluster : [Descouvemont, Itagaki  
PPTP 2020, 023D02 (2020)]
- DHF : [Chamon *et al.*  
CPC 267, 108061 (2021)]

$^{10}\text{Be}$  Elastic Scattering on  $^{12}\text{C}$  @  $E_{\text{Lab}} = 59.4\text{A MeV}$ 

Th : [Durant, PC PRC 106, 044608 (2022)]



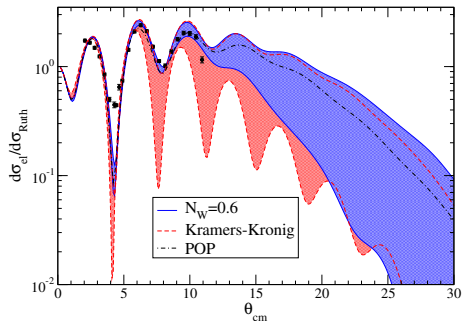
Exp : M. Cortina-Gil PhD

Good agreement with data  
 Phenomenological Optical Potential  
 works better [Al-Khalili, Tostevin, Brooke  
 PRC 55, R1018 (1997)]

- Little sensitivity to  $^{10}\text{Be}$  density  
 DHB works best
- Larger sensitivity to C density  
 Sum of Gaussian works best

$^{10}\text{Be}$  Elastic Scattering on  $^{12}\text{C}$  @  $E = 59.4\text{A MeV}$ 

Th : [Durant, PC PRC 106, 044608 (2022)]



Good agreement with data  
(no fitting parameter)

- @ forward angles where Coulomb significant
- @ large angles nuclear dominated

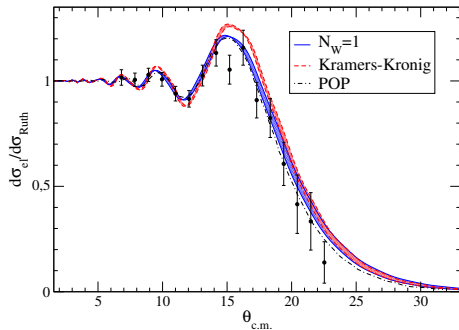
Exp : M. Cortina-Gil PhD

Sensitivity to cutoff  $R_0$  of  $V_{\text{NN}}$

- $R_0 = 1.6$  fm is softer  $\Rightarrow$  less absorption
- $R_0 = 1.2$  fm is harder  $\Rightarrow$  more absorptive and more oscillations
- $N_W = 0.6$  is less sensitive to  $R_0$

$^{10}\text{Be}$  Elastic Scattering on  $^{208}\text{Pb}$  @  $E_{\text{Lab}} = 127 \text{ MeV}$ 

Th : [Durant, PC PRC 106, 044608 (2022)]



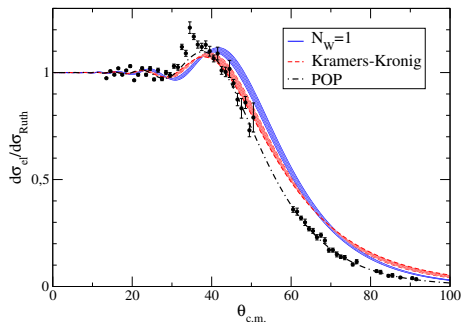
Good agreement with data  
(no fitting parameter)

- Coulomb dominated  
⇒ less sensitive to nuclear
- $R_0 = 1.6$  and  $1.2$  fm  
perform equally well
- $N_W = 1$  slightly better  
but fitting parameter

Exp : [Duan *et al.* Chin. Phys. C 44, 024001 (2020)]

$^{10}\text{Be}$  Elastic Scattering on  $^{64}\text{Zn}$  @  $E = 28.3$  MeV

Th : [Durant, PC PRC 106, 044608 (2022)]



Fair agreement with data  
(no fitting parameter)

- Coulomb dominated  
⇒ less sensitive to nuclear
- $R_0 = 1.6$  and  $1.2$  fm  
perform equally well
- $N_W = 1$  slightly less good  
although 1 fitting parameter

Exp : [Di Pietro *et al.* PRC 85, 054607 (2012)]

## Collisions with $^{11}\text{Be}$

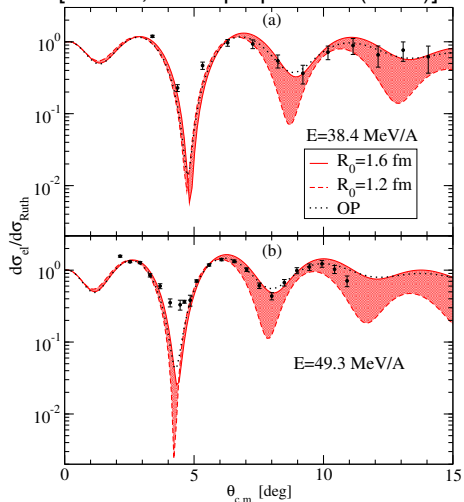
Collision of  $^{11}\text{Be}$  on various targets at different energies  
 analysed in few-body model of reactions  
 Dynamical Eikonal Approximation (DEA)

[Baye, P. C., Goldstein, PRL 95, 082502 (2005)]

- $^{11}\text{Be}$  described as  $^{10}\text{Be}+n$   
 $V_{cn}$  : Halo-EFT @ NLO  
 [PC, Phillips, Hammer PRC 98, 034610 (2018)]  
 Parameters fitted on *ab initio* predictions (ANC,  $\delta_s$ ,  $\delta_p \dots$ )  
 [Calci *et al.* PRL 117, 242501 (2016)]
- $V_{^{10}\text{Be}T}$  built by **double folding**
- $V_{nT}$  : Koning Delaroche

$^{11}\text{Be}$  elastic scattering on C

Th : [Durant, PC in preparation (2024)]

Exp : [Lapoux *et al.* PLB 658, 198 (2008)]

[M. Cortina-Gil PhD]

Good agreement with exp.

(no fitting parameter)

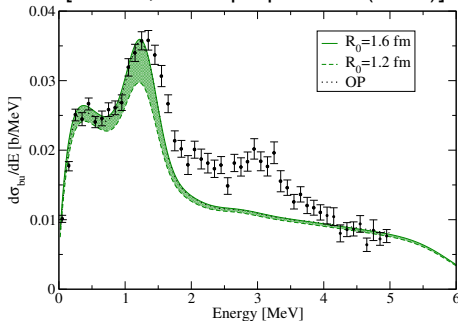
- @ forward angles where Coulomb significant
- @ large angles nuclear dominated
- $R_0 = 1.6 \text{ fm}$  is softer  $\Rightarrow$  less absorption as good as POP [Al-Khalili, Tostevin, Brooke PRC 55, R1018 (1997)]
- $R_0 = 1.2 \text{ fm}$  is harder  $\Rightarrow$  more absorptive and stronger oscillations



$^{11}\text{Be}$  breakup on C @ 67A MeVEnergy distribution  $d\sigma_{\text{bu}}/dE$ 

Excellent agreement with exp. (no fitting parameter in OP)

Th : [Durant, PC in preparation (2024)]

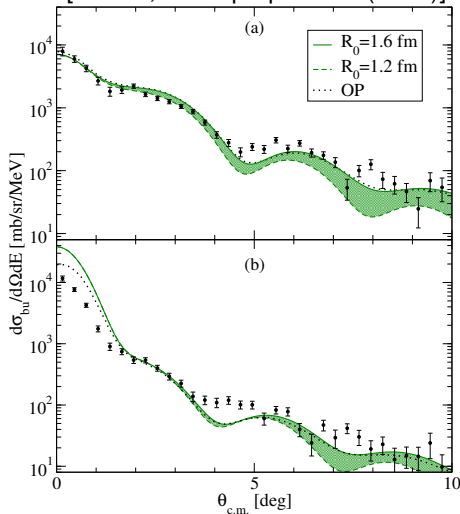


- reproduces peak @  $E_{5/2^+} = 1.3 \text{ MeV}$   
 $V_{3b}$  simulates  $^{10}\text{Be}$  excitation  
 [PC, Phillips, Hammer  
 PLB 825, 136847 (2022)]
- missing peak @  $E_{3/2^+} = 3 \text{ MeV}$   
 $3/2^+$  dominated by  $^{10}\text{Be}(2^+)$   
 [Moro, Lay PRL 109, 23250 (2012)]
- $R_0 = 1.6 \text{ fm}$  performs well  
 (less absorption)
- $R_0 = 1.2 \text{ fm}$  too absorptive

Exp : [Fukuda *et al.* PRC 70, 054606 (2004)]

$^{11}\text{Be}$  breakup on C @ 67A MeV

Th : [Durant, PC in preparation (2024)]



## Angular distributions

- (a)  $E_{5/2^+} = 1.3$  MeV
- (b)  $E \leq 0.2$  MeV

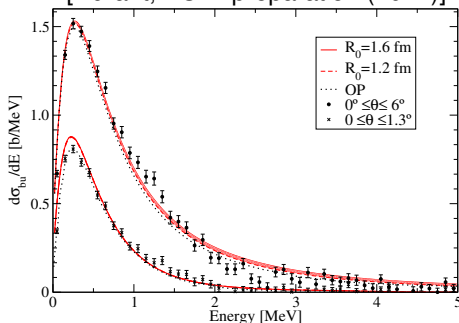
Excellent agreement with exp.  
(no fitting parameter in OP)

- similar sensitivity as for elastic scattering
- $R_0 = 1.6$  fm performs well (less absorption)
- $R_0 = 1.2$  fm too absorptive

Exp : [Fukuda *et al.* PRC 70, 054606 (2004)]

$^{11}\text{Be}$  breakup on Pb @ 69A MeV

Th : [Durant, PC in preparation (2024)]



Energy distributions

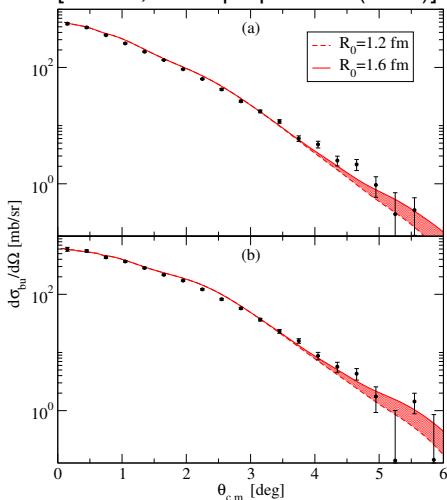
Excellent agreement with exp.  
for both angular cuts  
(no fitting parameter in OP)

- Coulomb dominated  
⇒ less sensitive to nuclear
- $R_0 = 1.6$  and  $1.2$  fm  
perform equally well

Exp : [Fukuda *et al.* PRC 70, 054606 (2004)]

$^{11}\text{Be}$  breakup on Pb @ 69A MeV

Th : [Durant, PC in preparation (2024)]



## Angular distributions

- (a)  $E \leq 1$  MeV
- (b)  $E \leq 5$  MeV

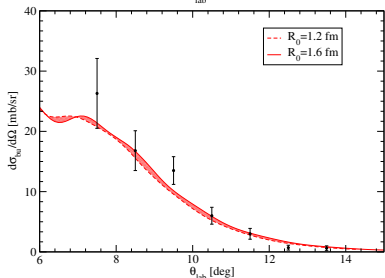
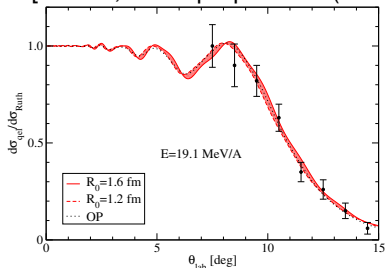
Excellent agreement with exp.  
(no fitting parameter in OP)

- Coulomb dominated  
⇒ less sensitive to nuclear
- $R_0 = 1.6$  and  $1.2$  fm  
perform equally well

Exp : [Fukuda *et al.* PRC 70, 054606 (2004)]

$^{11}\text{Be}$  on Pb @ 19A MeV

Th : [Durant, PC in preparation (2024)]



Angular distributions for

- Scattering (el. & inel.)
- (inclusive) breakup  
(n not measured)

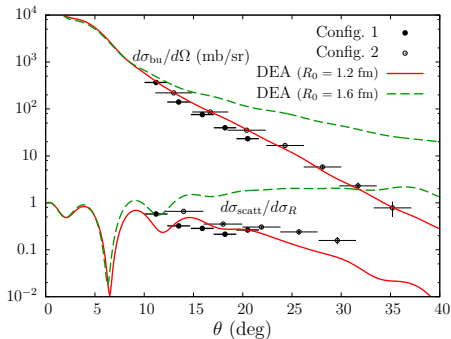
Excellent agreement with exp.  
(no fitting parameter in OP)

- Coulomb dominated  
 $\Rightarrow$  less sensitive to nuclear
- $R_0 = 1.6$  and  $1.2$  fm  
perform equally well

Exp : [Duan *et al.* PRC 105, 034602 (2022)]

$^{11}\text{Be}$  on C @ 22A MeV

Preliminary data. . .

Exp : [Ota *et al.* in preparation (2024)]

Angular distributions for

- (inclusive) breakup  
(n not measured)
- scattering (el. & inel.)

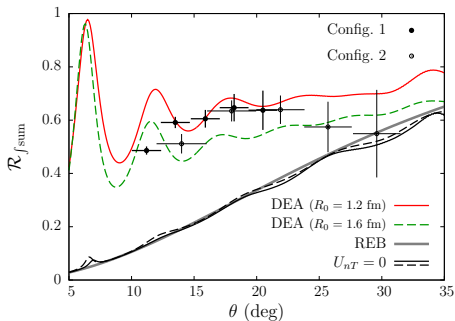
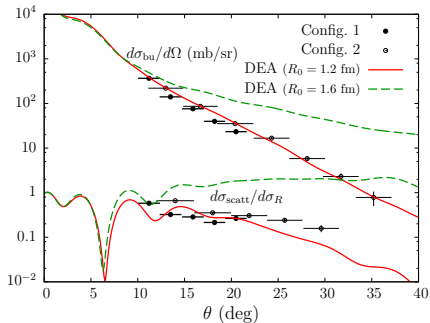
**Nuclear** dominated

⇒ very sensitive to nuclear int.

- $R_0 = 1.6$  fm **too soft**  
⇒ not absorptive enough
- $R_0 = 1.2$  fm  
performs very **well**

$^{11}\text{Be}$  on C @ 22A MeVThe **Ratio Method**...

[PC, Johnson, Nunes PLB 705, 112 (2011), PRC 88, 044602 (2013)]



$$\mathcal{R}_{j\text{sum}} = \frac{\int d\sigma_{\text{bu}}/dEd\Omega dE}{d\sigma_{\text{el}}/d\Omega + \int d\sigma_{\text{bu}}/dEd\Omega dE}$$

- smooth
- independent of  $V_{cT}$

## Summary and prospect

- Exotic nuclei studied mostly through **reactions**
- **Optical potentials** are necessary inputs
- **Optical potentials** can be built by double-folding
  - ▶ Using  $\chi_{\text{EFT}}$  NN interactions
  - ▶ Densities from literature
  - ▶ **Good agreement** with experiment (no fitting parameter)
    - ★ Scattering of nuclei
    - ★ Reactions of clusterised nuclei (**halos**)
- Future :
  - ▶ include 3N forces ?
  - ▶ account for **non-locality** ?

**Dream** : with the same NN interaction

- Compute densities of **core**
- Structure of **halo** nucleus
- **Optical potential**



# Thanks...

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Victoria Durant

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Ron Johnson



Filomena Nunes



Shuya Ota

