

# Inclusive diffraction at the EIC

## Extracting Reggeon contribution

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# Outline

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- Inclusive diffraction at HERA
- Description of diffraction: Pomeron and Reggeon components
- EIC pseudodata for diffractive cross section
- Extraction of Pomeron and Reggeon, estimate of uncertainties

*Extracting the partonic structure of colorless exchanges at the Electron Ion Collider* e-Print: [2406.02227](#)

Continuation of series of works on diffraction at ep/eA machines:

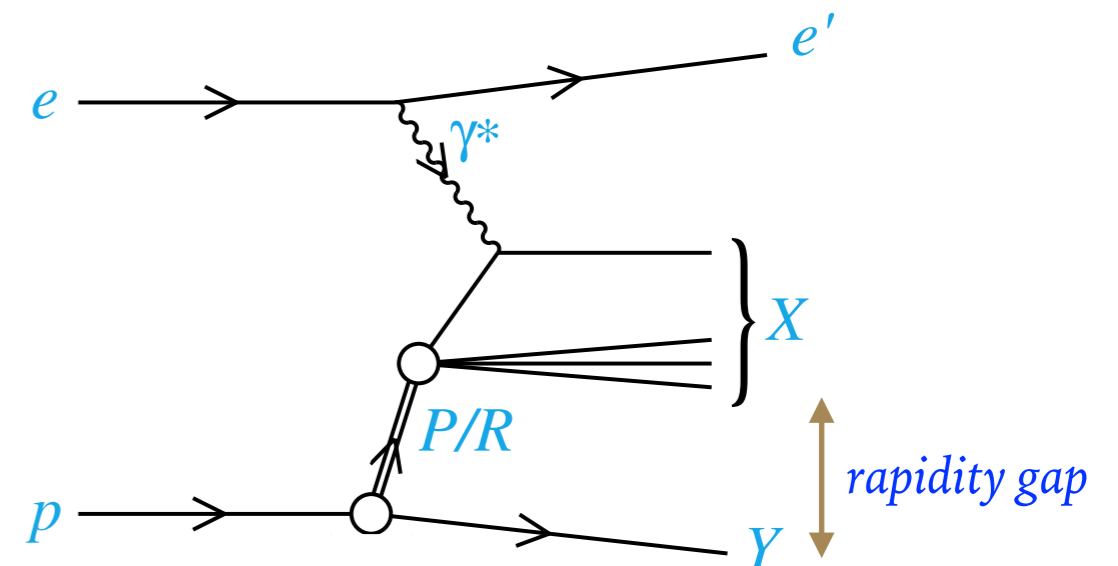
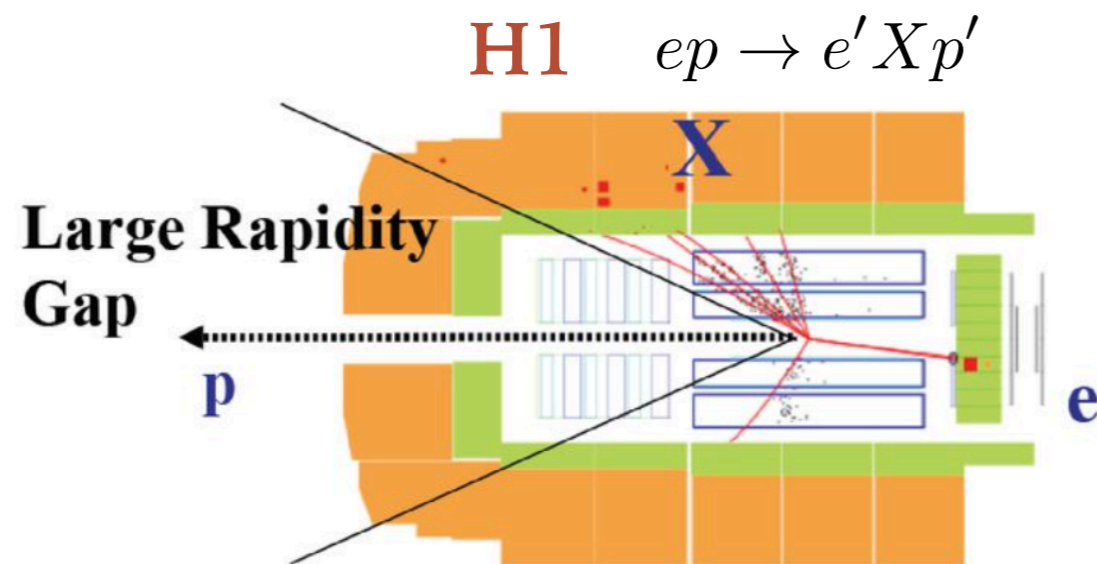
*Inclusive diffraction in future electron-proton and electron-ion colliders* e-Print: [1901.09076](#)

*Diffractive longitudinal structure function at Electron Ion Collider* e-Print: [2112.06839](#)

also EIC Yellow Report, Sec. 7.1.6, 8.5.7

# Diffraction in DIS

- Diffractive characterized by the **rapidity gap**: no activity in part of the detector
- At HERA in electron-proton collisions: about 10% events diffractive
- Interpretation of diffraction : need **colorless exchange**

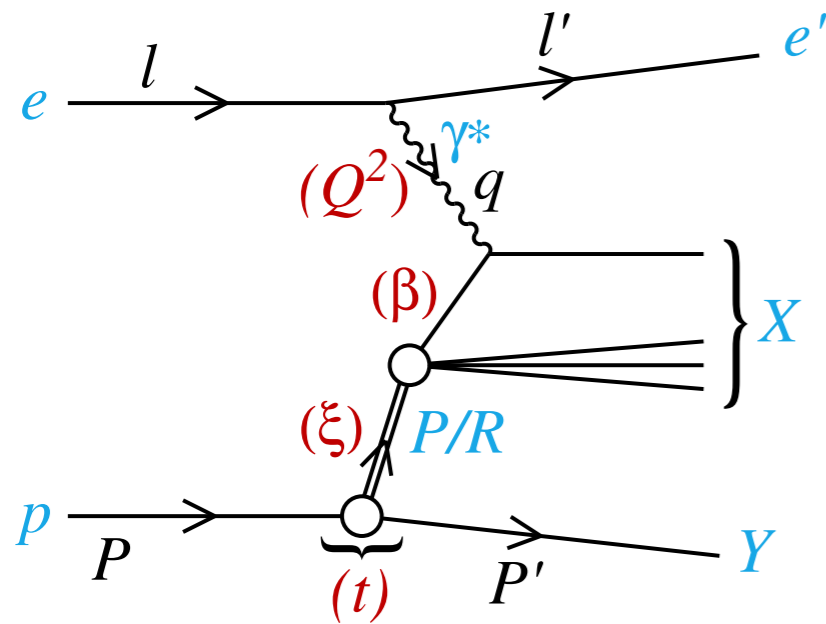


## Questions:

- What is the nature of this exchange ? Partonic composition ?
- One, two, or more exchanges ? Pomeron  $IP$ , Reggeon  $IR$  ?
- Energy, momentum transfer dependence ?

# Diffractive kinematics in DIS

## Standard DIS variables:



electron-proton  
cms energy squared:

$$s = (l + P)^2$$

photon-proton  
cms energy squared:

$$W^2 = (q + P)^2$$

inelasticity

$$y = \frac{P \cdot q}{P \cdot l}$$

Bjorken x

$$x = \frac{Q^2}{2P \cdot q} = \frac{Q^2}{ys} = \frac{Q^2}{Q^2 + W^2}$$

(minus) photon virtuality

$$Q^2 = -q^2$$

$$x = \xi \beta$$

## Diffractive DIS variables:

$$\xi = x_{IP} = \frac{x}{\beta} = \frac{Q^2 + M_X^2 - t}{Q^2 + W^2}$$

momentum fraction of the  
Pomeron w.r.t hadron

$$\beta = \frac{Q^2}{2(P - P') \cdot q} = \frac{Q^2}{Q^2 + M_X^2 - t}$$

momentum fraction of parton  
w.r.t Pomeron

$$t = (P' - P)^2$$

4-momentum transfer squared

# Diffractive cross section, structure functions

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**Diffractive cross section** depends on 4 variables  $(\xi, \beta, Q^2, t)$  :

$$\frac{d^4\sigma^D}{d\xi d\beta dQ^2 dt} = \frac{2\pi\alpha_{\text{em}}^2}{\beta Q^4} Y_+ \sigma_r^{\text{D}(4)}(\xi, \beta, Q^2, t)$$

$$Y_+ = 1 + (1 - y)^2$$

**Reduced** cross section depends on two **structure functions**:

$$\text{4-D: } \sigma_r^{\text{D}(4)}(\xi, \beta, Q^2, t) = F_2^{\text{D}(4)}(\xi, \beta, Q^2, t) - \frac{y^2}{Y_+} F_L^{\text{D}(4)}(\xi, \beta, Q^2, t)$$

Upon integration over  $t$ :

$$\text{3-D: } F_{2,L}^{\text{D}(3)}(\xi, \beta, Q^2) = \int_{-\infty}^0 dt F_{2,L}^{\text{D}(4)}(\xi, \beta, Q^2, t)$$

Dimensions:

$$[\sigma_r^{\text{D}(4)}] = \text{GeV}^{-2}$$

$$\sigma_r^{\text{D}(3)} \quad \text{Dimensionless}$$

# Diffraction at HERA: importance of 'Reggeon'

$\xi \sigma_r^{D(4)} \simeq \xi F_2^{D(4)}$  vs  $\xi$  for fixed  $|t| = 0.25 \text{ GeV}^2$  in bins of  $\beta, Q^2$

Described by two contributions:

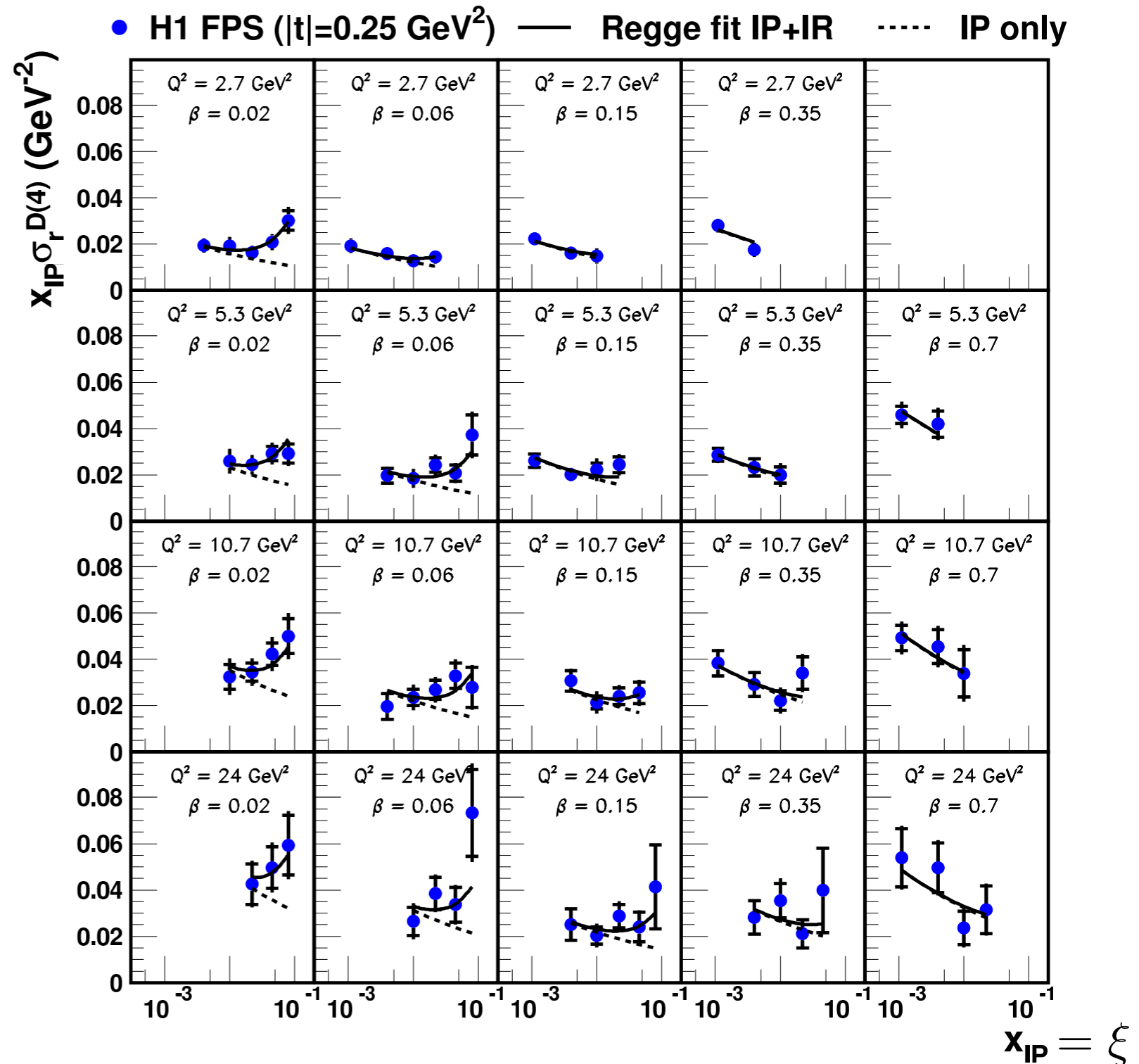
Leading 'Pomeron' at low  $\xi$

$$\xi f_{IP} \sim \xi^{-0.22}$$

Subleading 'Reggeon' at high  $\xi$

$$\xi f_{IR} \sim \xi^{1.0}$$

Subleading terms poorly constrained



# Reggeon in photoproduction data

Similar observation in

photoproduction  $Q^2 \sim 0$

$$\gamma + p \rightarrow X + p$$

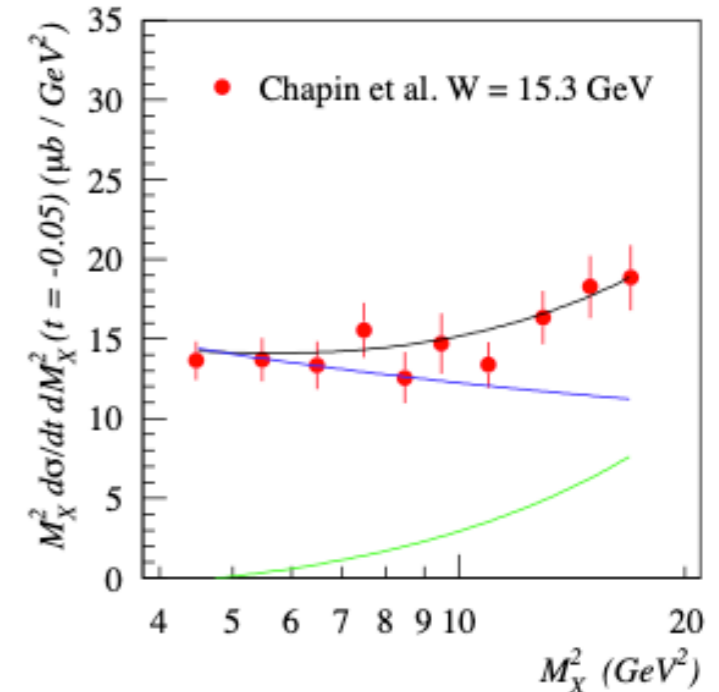
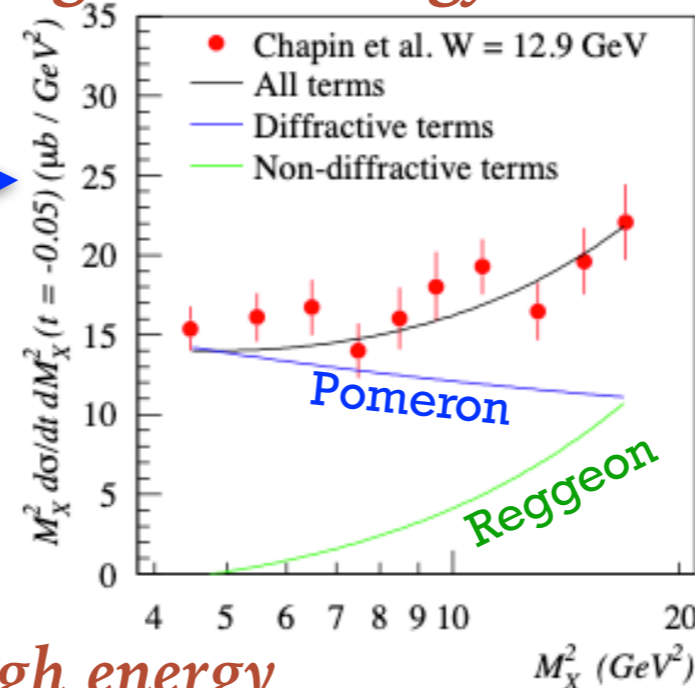
Fit using **Regge** model

**Subleading** exchanges present at HERA

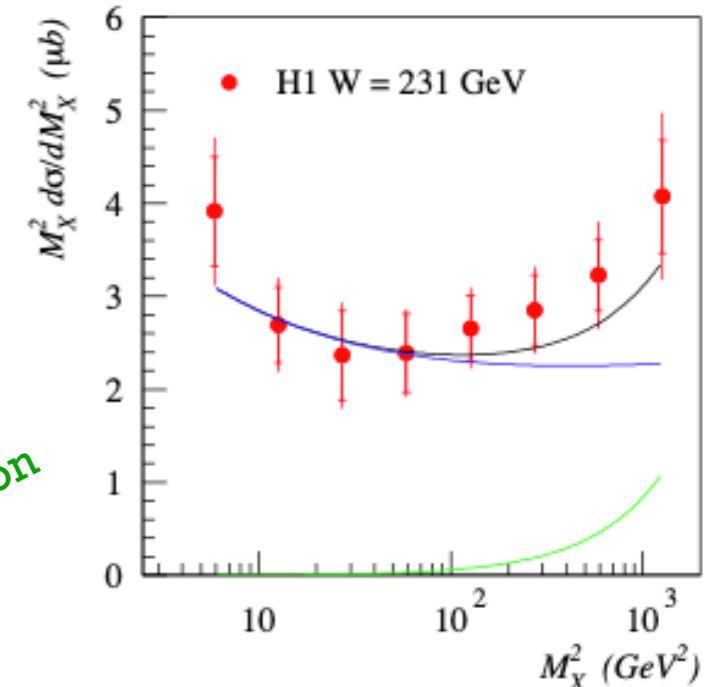
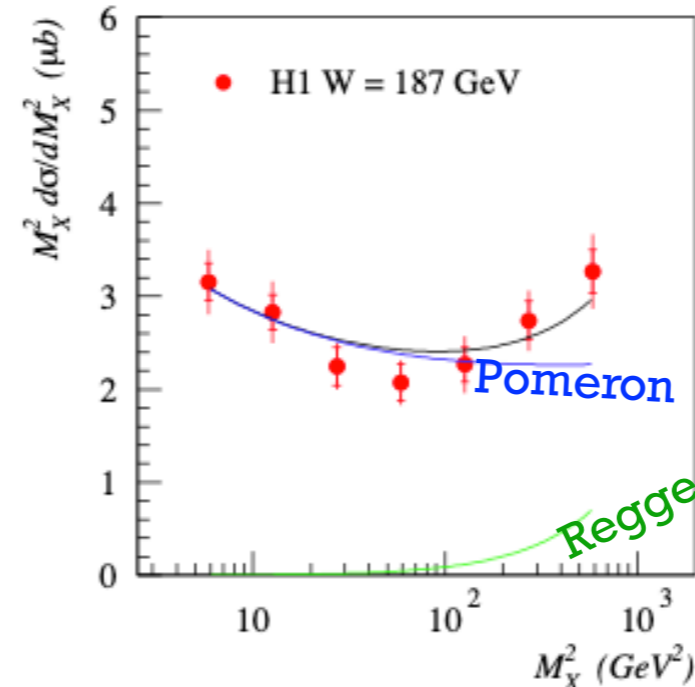
More dominant at **lower energies**

EIC (esp. with varying beam energies) has great potential to explore the nature of these exchanges and transition between them

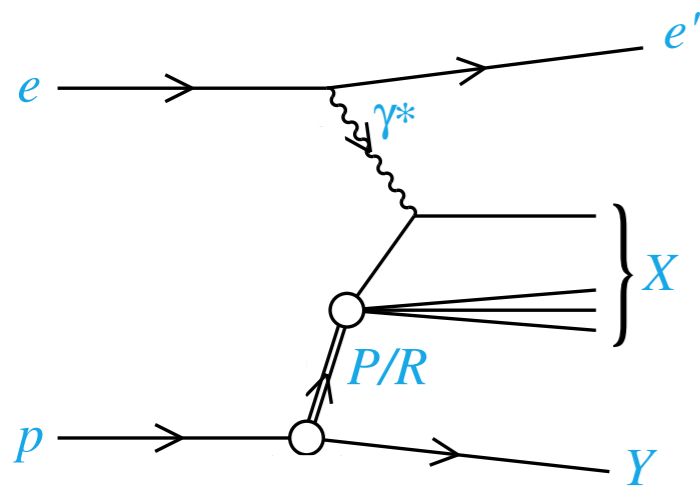
*Fixed target: low energy*



*H1: high energy*



# Extraction of DPDF from HERA data

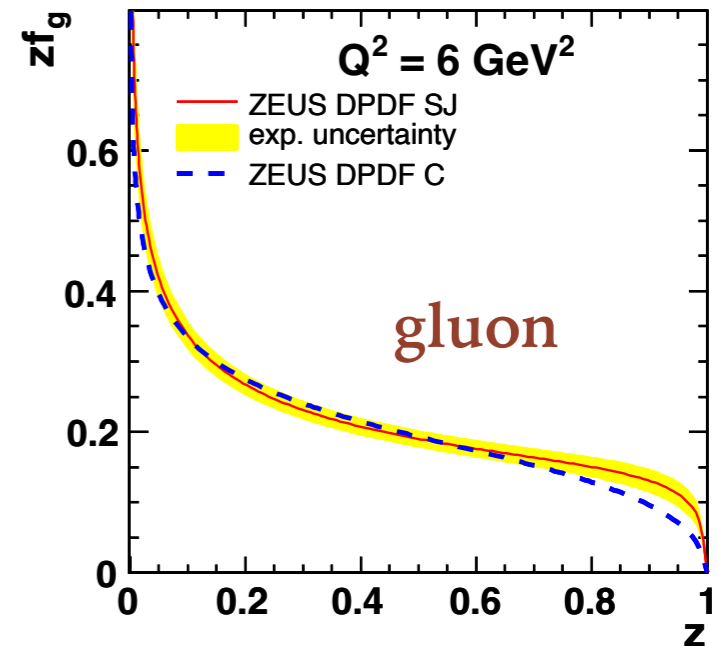
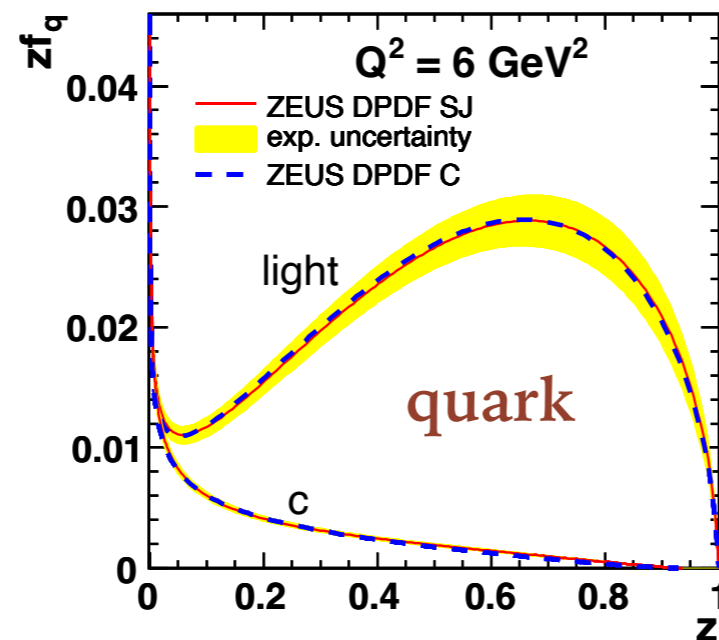


Example of DPDFs extracted from the ZEUS data

**QCD** analysis at **NLO**

Partonic content of the Pomeron contribution extracted

Dominated by the **gluon density**



Successfully used to describe the diffractive data from HERA

but

Large  $z$  gluon not very well constrained (need dijet data)

Only Pomeron extracted, Reggeon parametrized using GRV pion



# Diffraction at EIC

## EIC complementarity to HERA

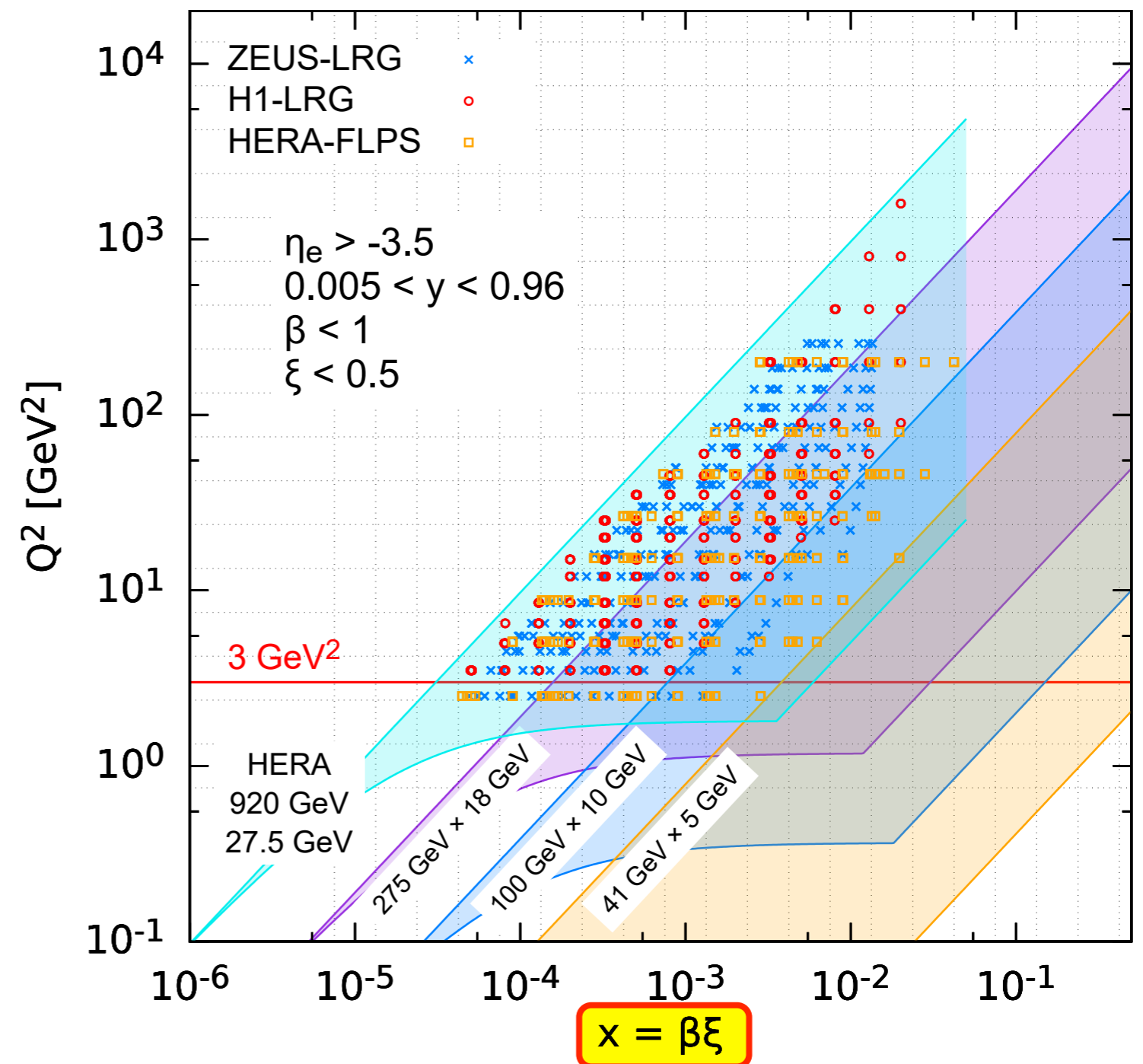
Large  $x \rightarrow$  Large  $\xi$  : constraints on subleading (Reggeon) exchange

Large  $x \rightarrow$  Large  $\beta$  : constraints on large  $z$  region of DPDFs

At EIC use **forward tagging** instrumentation to detect forward protons and study diffraction

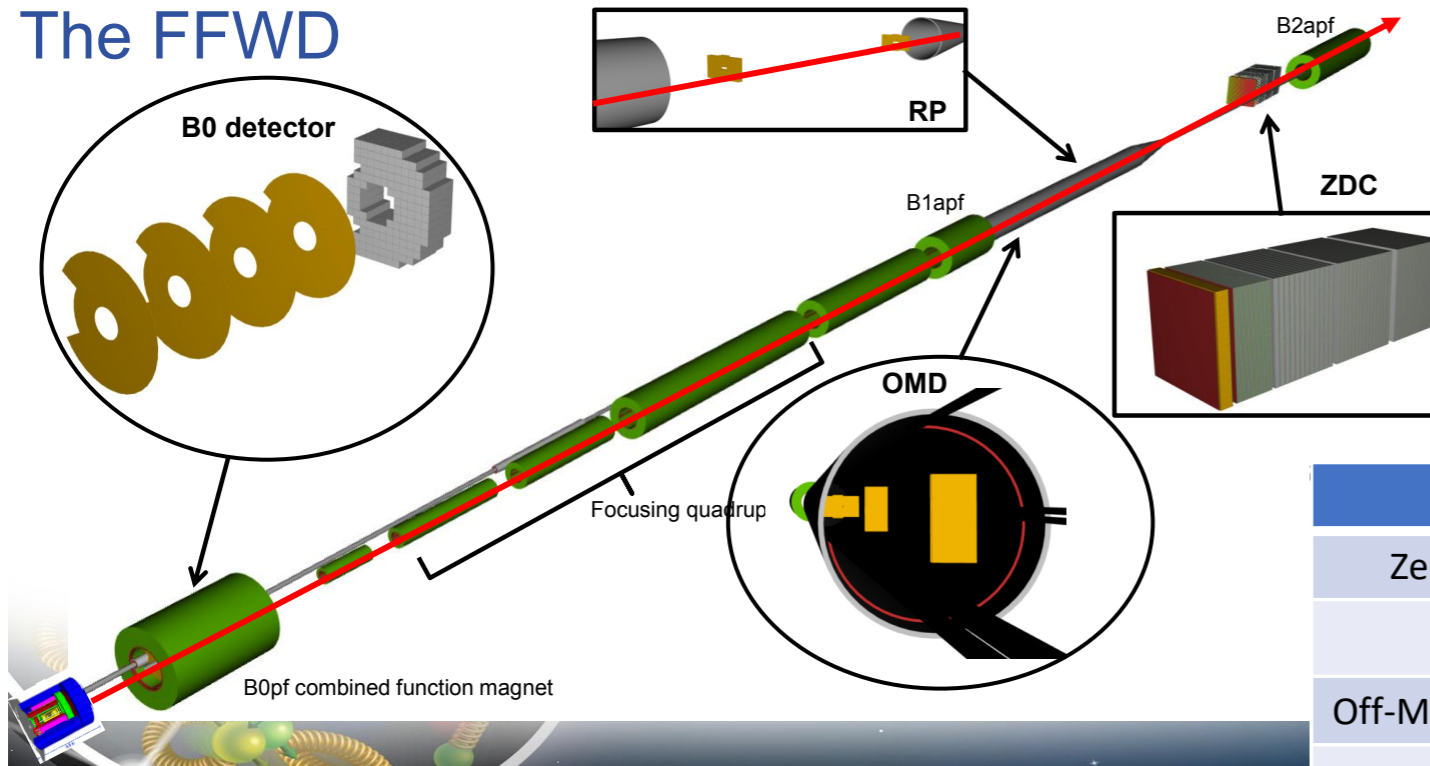
*Only selected energy scenarios at EIC shown*

## EIC 3 scenarios - HERA



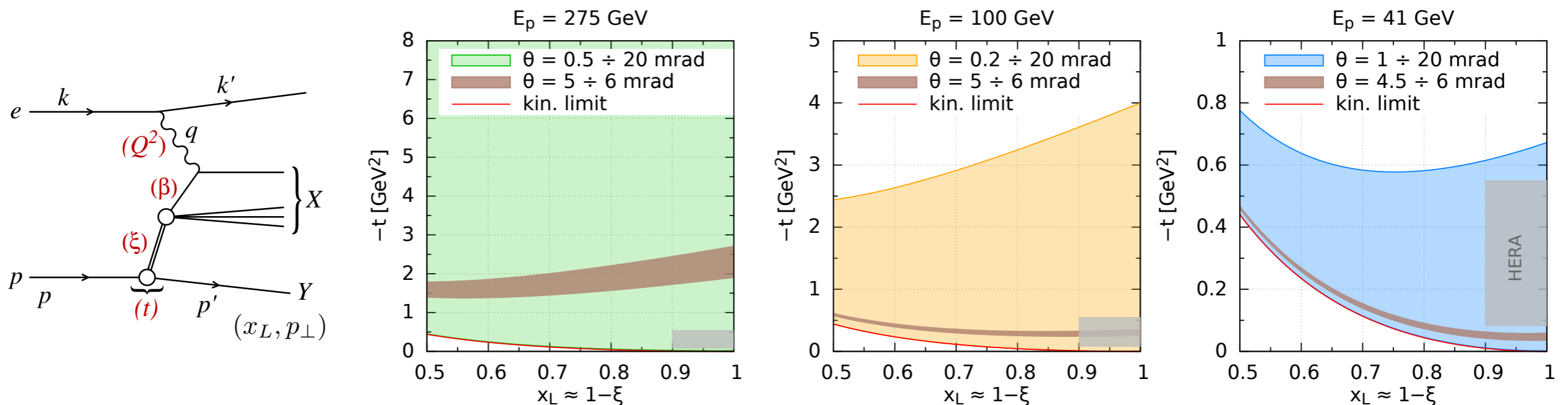
# Forward instrumentation at EIC and acceptance

## The FFWD



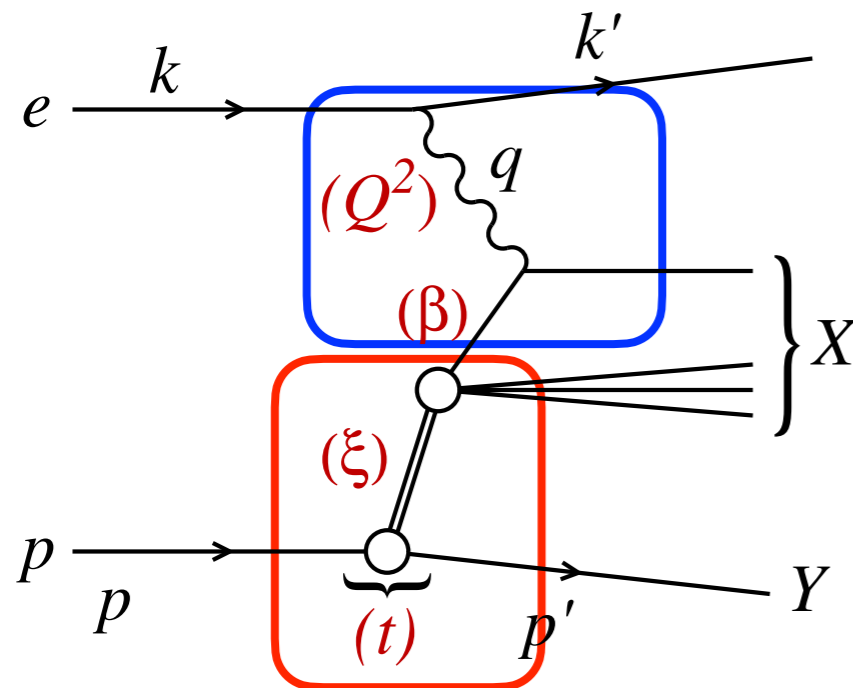
Forward detectors have wide acceptance in  $\xi$  and  $t$  for detecting protons

Detector	Acceptance
Zero-Degree Calorimeter (ZDC)	$\theta < 5.5$ mrad ( $\eta > 6$ )
Roman Pots (2 stations)	$0.0^* < \theta < 5.0$ mrad ( $\eta > 6$ )
Off-Momentum Detectors (2 stations)	$0.0 < \theta < 5.0$ mrad ( $\eta > 6$ )
B0 Detector	$5.5 < \theta < 20$ mrad ( $4.6 < \eta < 5.9$ )



# Pseudodata generation: collinear factorization for diffraction

Use the collinear factorization for the description of HERA and pseudodata simulation



Collins

Collinear factorization in diffractive DIS

$$F_{2/L}^{D(4)}(\beta, \xi, Q^2, t) = \sum_i \int_{\beta}^1 \frac{dz}{z} C_{2/L,i} \left( \frac{\beta}{z}, Q^2 \right) f_i^D(z, \xi, Q^2, t)$$

- Diffractive cross section can be factorized into the convolution of the perturbatively calculable **partonic cross sections** and **diffractive parton distributions (DPDFs)**
- Partonic cross sections are the **same as in the inclusive DIS**
- The DPDFs are non-perturbative objects, but evolved perturbatively with **DGLAP**

# EIC pseudodata generation: model

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Use ZEUS  $IP + IR$  fit with the GRV pion structure function for the  $IR$   
Pseudodata generated in all 4-variables :  $(\beta = z, \xi, Q^2, t)$

## Diffraction PDF:

$$f_k^{D(4)}(z, Q^2, \xi, t) = \phi_{IP}(\xi, t) f_k^{IP}(z, Q^2) + \phi_{IR}(\xi, t) f_k^{IR}(z, Q^2)$$

## Fluxes:

$$\phi_M(\xi, t) = \frac{e^{B_M t}}{\xi^{2\alpha_M(t)-1}}$$

## Trajectories:

$$\alpha_M(t) = \alpha_M(0) + \alpha'_M t \quad M = IP, IR$$

## Reduced cross section:

$$\sigma_{\text{red}}^{D(4)} = \phi_{IP}(\xi, t) \mathcal{F}_2^{IP}(\beta, Q^2) + \phi_{IR}(\xi, t) \mathcal{F}_2^{IR}(\beta, Q^2) \\ - \frac{y^2}{Y_+} [\phi_{IP}(\xi, t) \mathcal{F}_L^{IP}(\beta, Q^2) + \phi_{IR}(\xi, t) \mathcal{F}_L^{IR}(\beta, Q^2)]$$

## Flux parameters:

$$\xi \phi_{IP}(\xi, t) \propto \xi^{-0.22} e^{-7|t|}$$

ZEUS fit  
parameters

$$\xi \phi_{IR}(\xi, t) \propto \xi^{0.6+1.8|t|} e^{-2|t|} = \xi^{0.6} e^{(-2+1.8 \ln \xi) |t|}$$

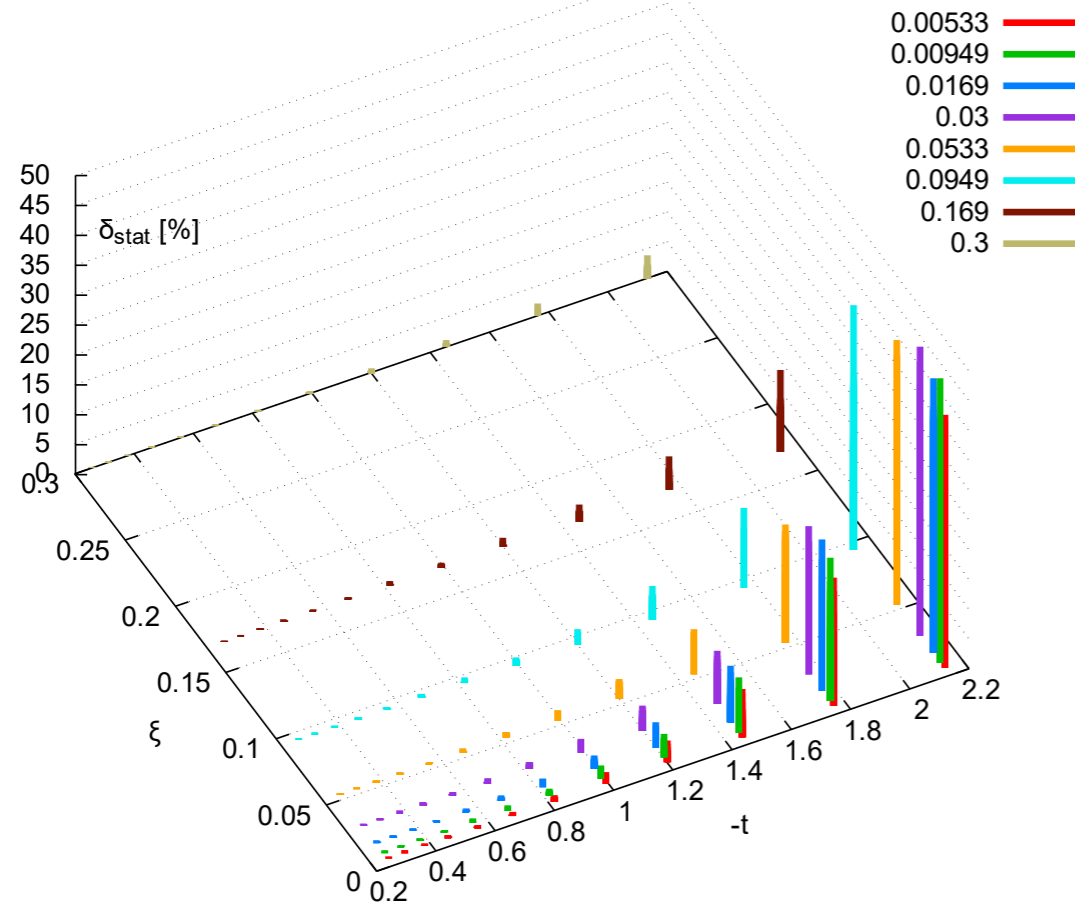
# EIC pseudodata generation: lumi, energy, errors

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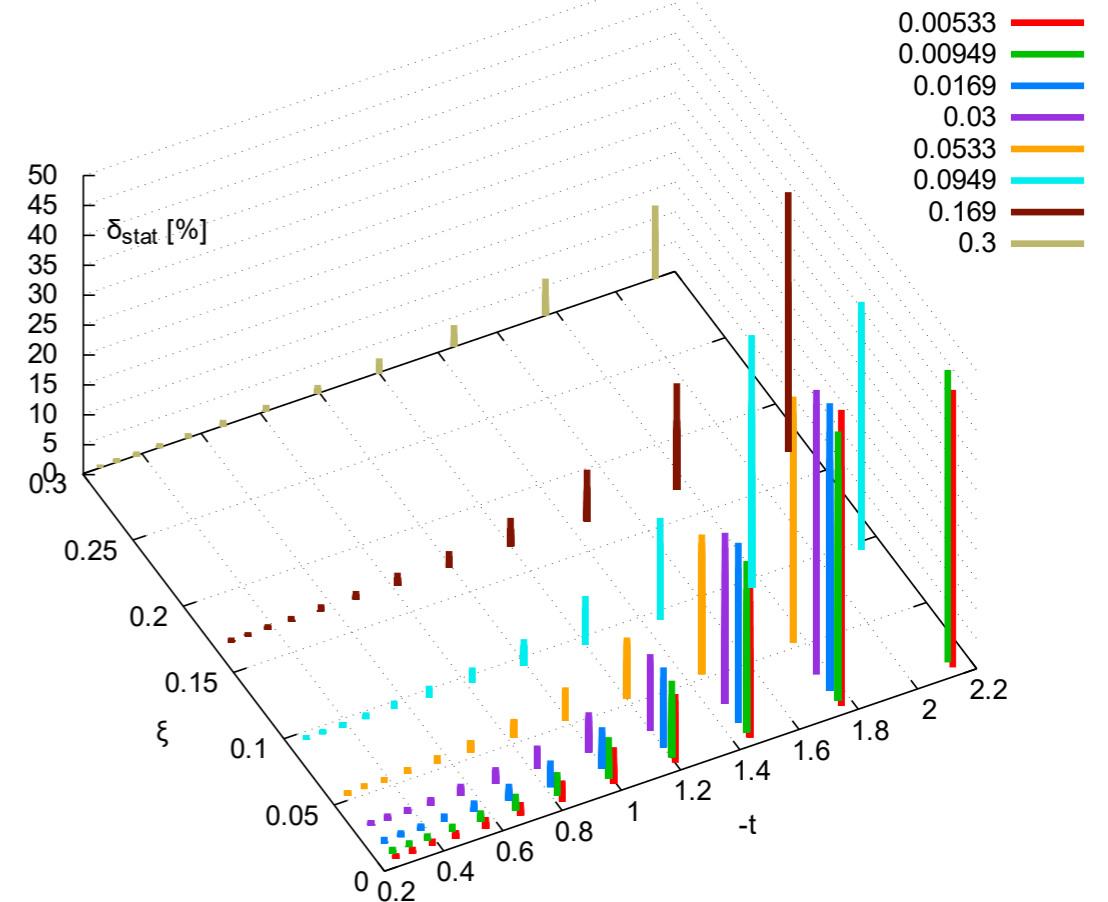
- Use NC simulations for EIC (no HERA nor CC yet)
- Three scenarios for integrated luminosity and energy :
  - $\mathcal{L} = 100 \text{ fb}^{-1}$  at high energy  $E_e = 18 \text{ GeV} \times E_p = 275 \text{ GeV}$
  - $\mathcal{L} = 10 \text{ fb}^{-1}$  at high energy  $E_e = 18 \text{ GeV} \times E_p = 275 \text{ GeV}$
  - $\mathcal{L} = 10 \text{ fb}^{-1}$  at low energy  $E_e = 5 \text{ GeV} \times E_p = 41 \text{ GeV}$
- Require  $0.005 < y < 0.96$
- Sparse and dense binning scenarios
- 5% uncorrelated systematics, 2% normalization error on top
- Randomly fluctuate each data point according to the uncertainties

# Pseudodata: statistical errors

ep beams 18 GeV × 275 GeV,  $L = 100 \text{ fb}^{-1}$



ep beams 18 GeV × 275 GeV,  $L = 10 \text{ fb}^{-1}$

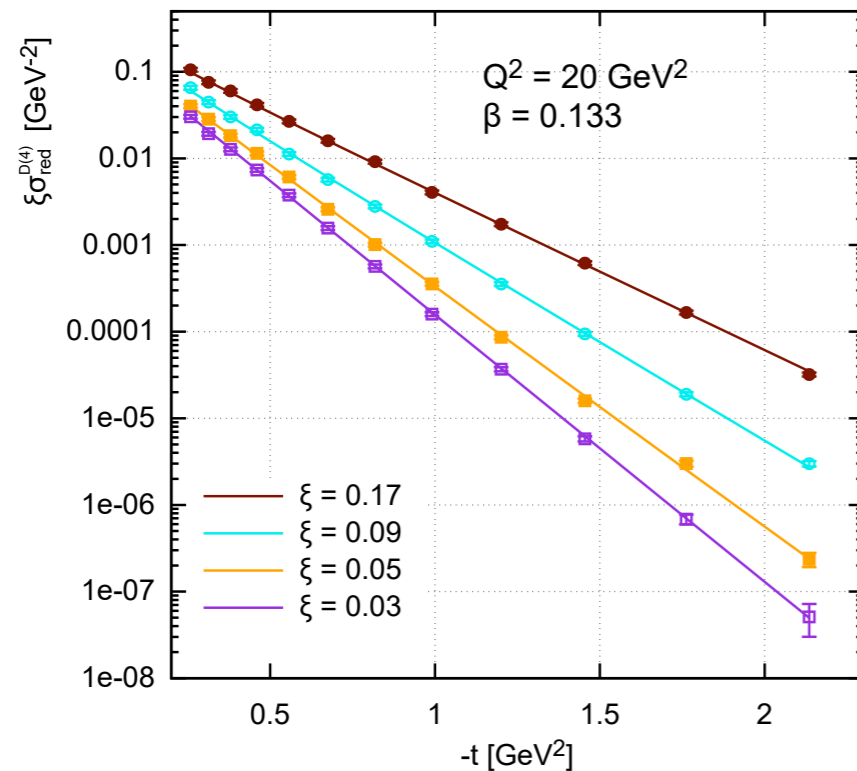


For  $Q^2 < 50 \text{ GeV}^2$  and  $|t| < 1.2 \text{ GeV}^2$

$\mathcal{L} = 10 \text{ fb}^{-1}$ : less than 4% data points have  $\delta_{\text{stat}} > 5 \%$

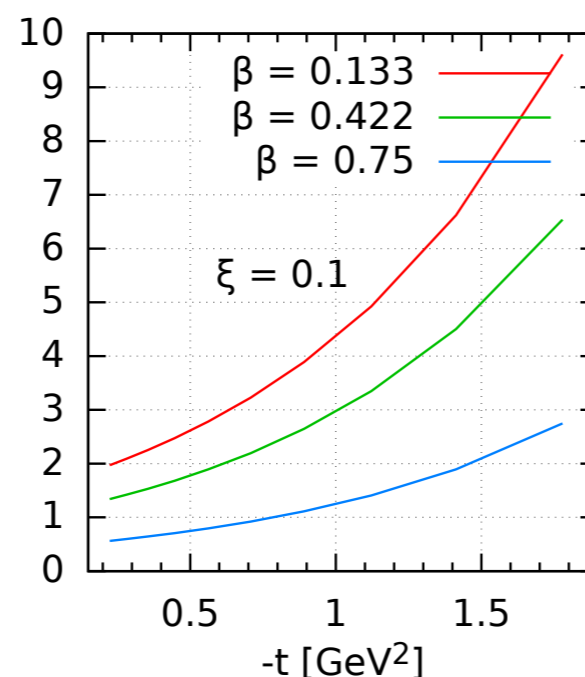
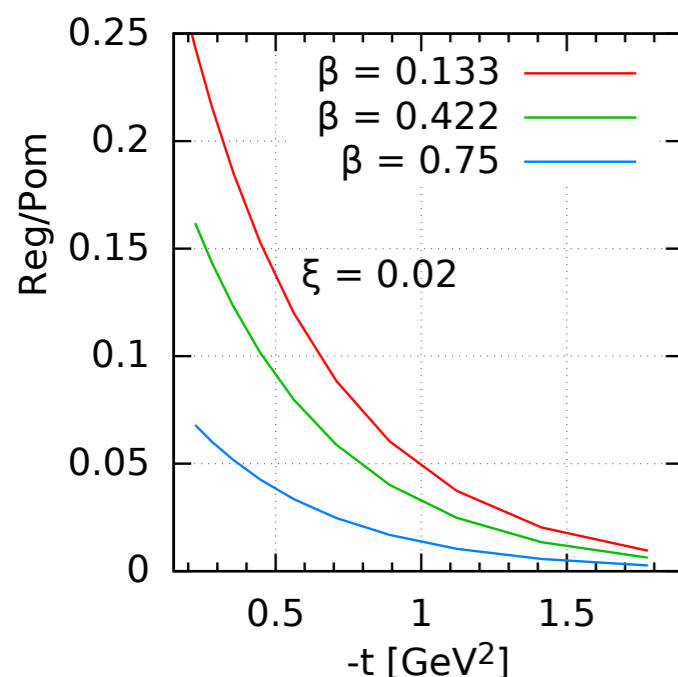
$\mathcal{L} = 100 \text{ fb}^{-1}$ : all data points have  $\delta_{\text{stat}} < 4.3 \%$

# Reggeon and Pomeron component in cross section at EIC



## 4D cross section pseudodata

- Changing  $t$  slope as transitioning from Pomeron to Reggeon dominated region
- $\sigma_r^D$  slowly varying with  $Q^2$

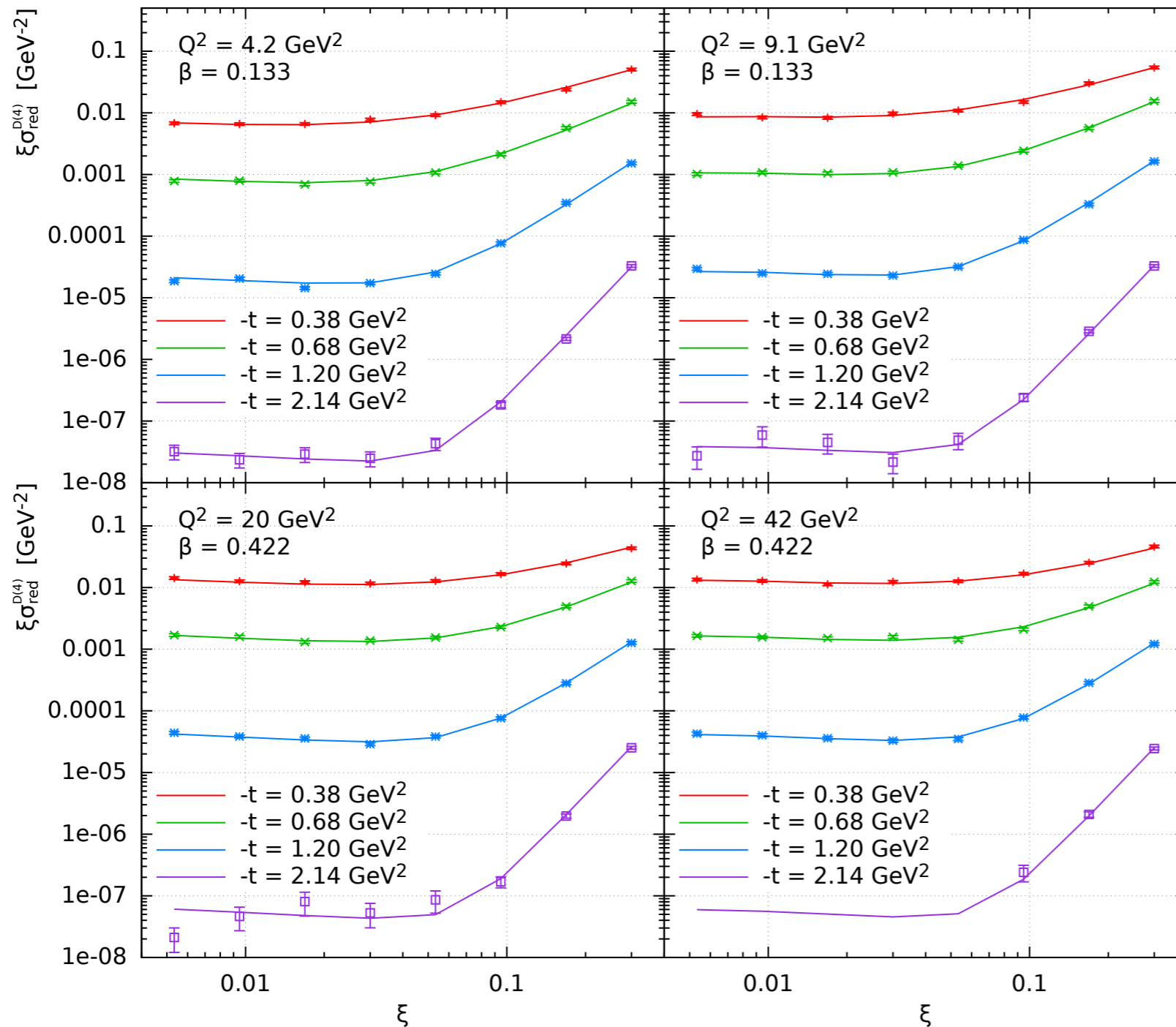


## $IR/IP$ ratio vs $-t$ for $\xi = 0.01, 0.1$

- Change of ratio for small vs large  $\xi$  as a function of  $-t$ : different slope
- $IR/IP < 1$  for small  $\xi \sim 0.02$
- $IR/IP > 1$  for larger  $\xi \geq 0.1$  : not accessible at HERA

# Example of the pseudodata: $\xi$ dependence

$\sigma_{\text{red}}^{D(4)}$  for ep beams 18 GeV  $\times$  275 GeV,  $L = 100 \text{ fb}^{-1}$



$\sigma_r^D$  slowly varying with  $Q^2$

Transition between  $IP/IR$  clearly visible

Need to measure  $\xi \geq 0.1$



# Parametrisation for fitting the pseudodata

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- Treat the Pomeron and Reggeon contributions as symmetrically as possible
- Light quark separation not possible with only inclusive NC fits
- For both  $\mathbb{P}$  and  $\mathbb{R}$  fit the gluon and the sum of quarks
- Generic parametrization at  $Q_0^2 = 1.8 \text{ GeV}^2$  :

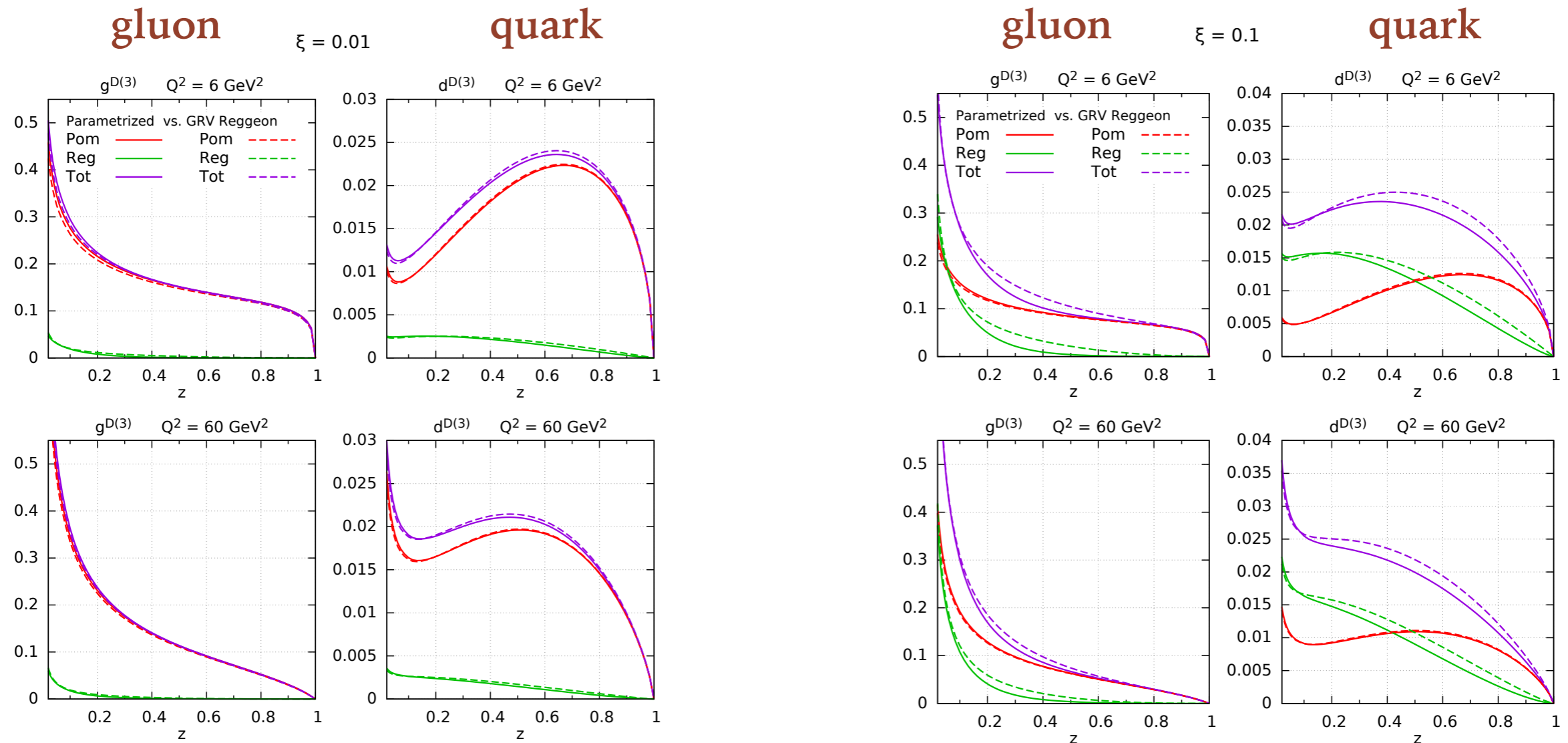
$$f_k^{(m)}(x, Q_0^2) = A_k^{(m)} x^{B_k^{(m)}} (1-x)^{C_k^{(m)}} (1 + D_k^{(m)} x^{E_k^{(m)}})$$

where  $k = q, g$  and  $m = \mathbb{P}, \mathbb{R}$

- Following sensitivity studies a suitable choice is:
  - $f_q^{\mathbb{P}}$  has A,B,C parameters
  - $f_g^{\mathbb{P}}$  has A,B,C parameters
  - $f_q^{\mathbb{R}}$  has A,B,C,D parameters
  - $f_g^{\mathbb{R}}$  has A,B,C parameters
- In addition fit for the parameters of the fluxes for  $\mathbb{P}$  and  $\mathbb{R}$ :  $\alpha(0), \alpha', B$

$$\frac{e^{B^{(m)}t}}{\xi^{2\alpha^{(m)}(t)-1}} \quad \alpha^{(m)}(t) = \alpha^{(m)}(0) + \alpha'^{(m)}t$$

# Recovering the Pomeron and Reggeon inputs



Fit results with free Reggeon parametrization (solid) made to the pseudodata based on the GRV pion structure function (dashed)

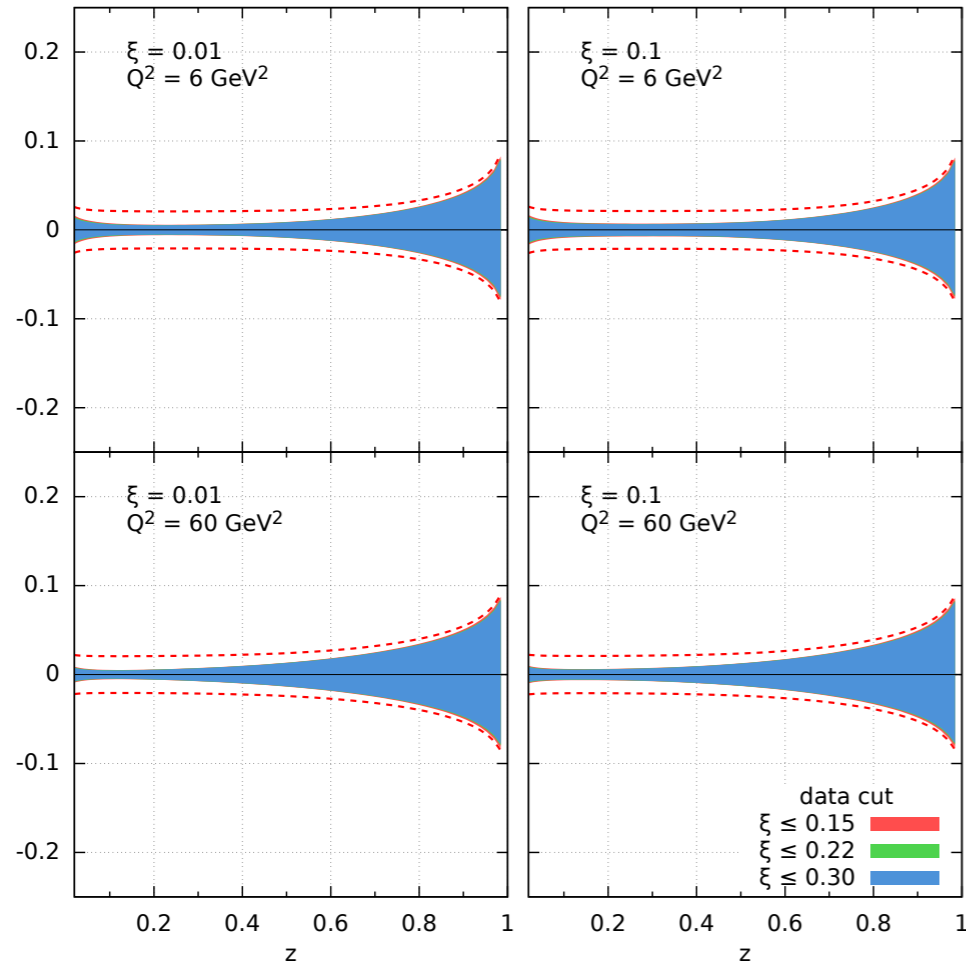
**Reggeon** reproduced reasonably well

**Pomeron** reproduced almost perfectly

# Uncertainties of diffractive PDFs: Pomeron

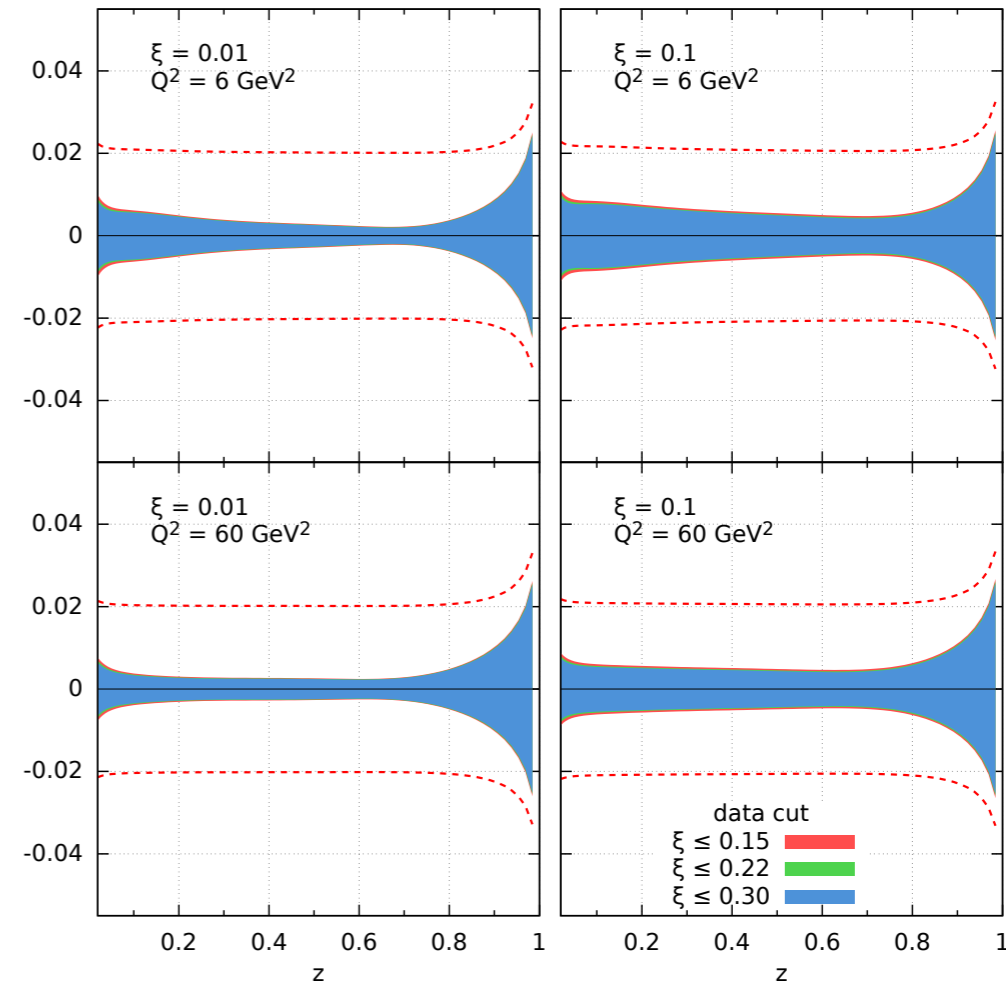
## Pomeron gluon

Pomeron gluon data cut:  $t \geq -1.5 \text{ GeV}^2$



## Pomeron quark

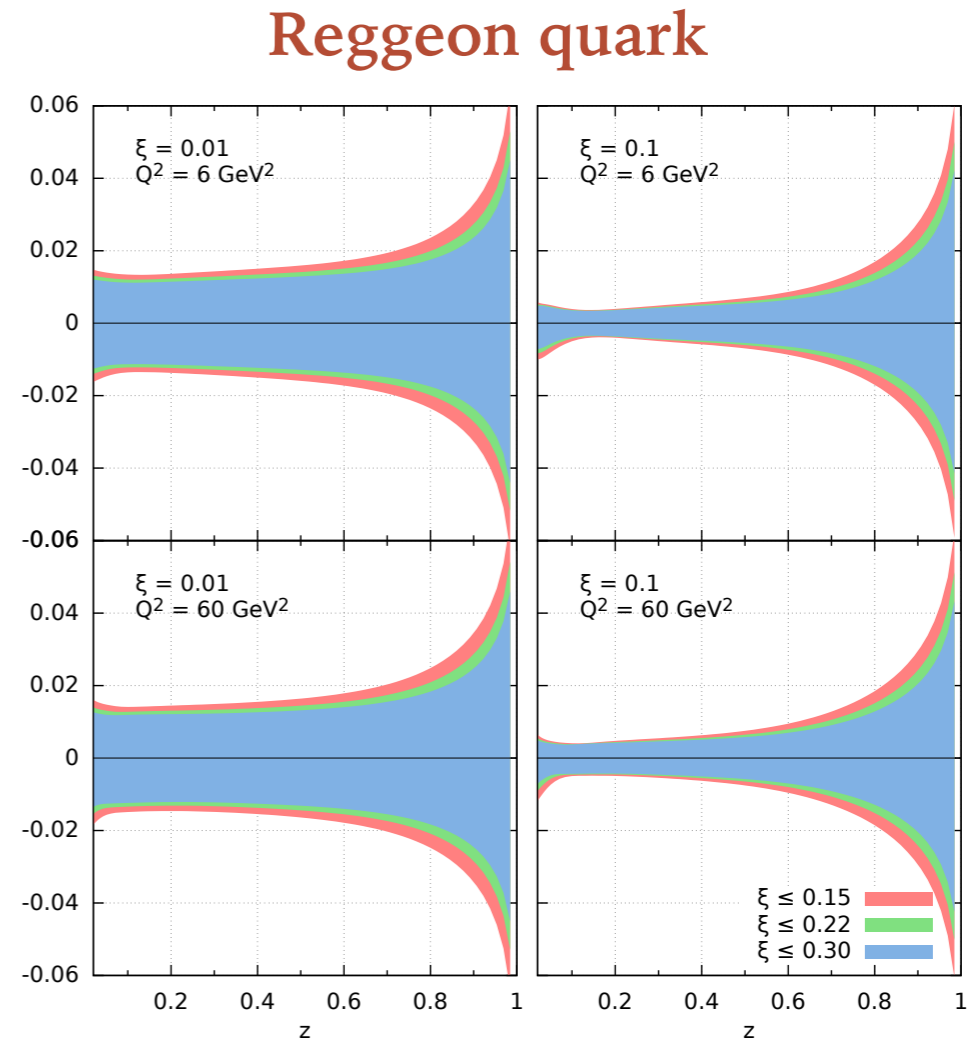
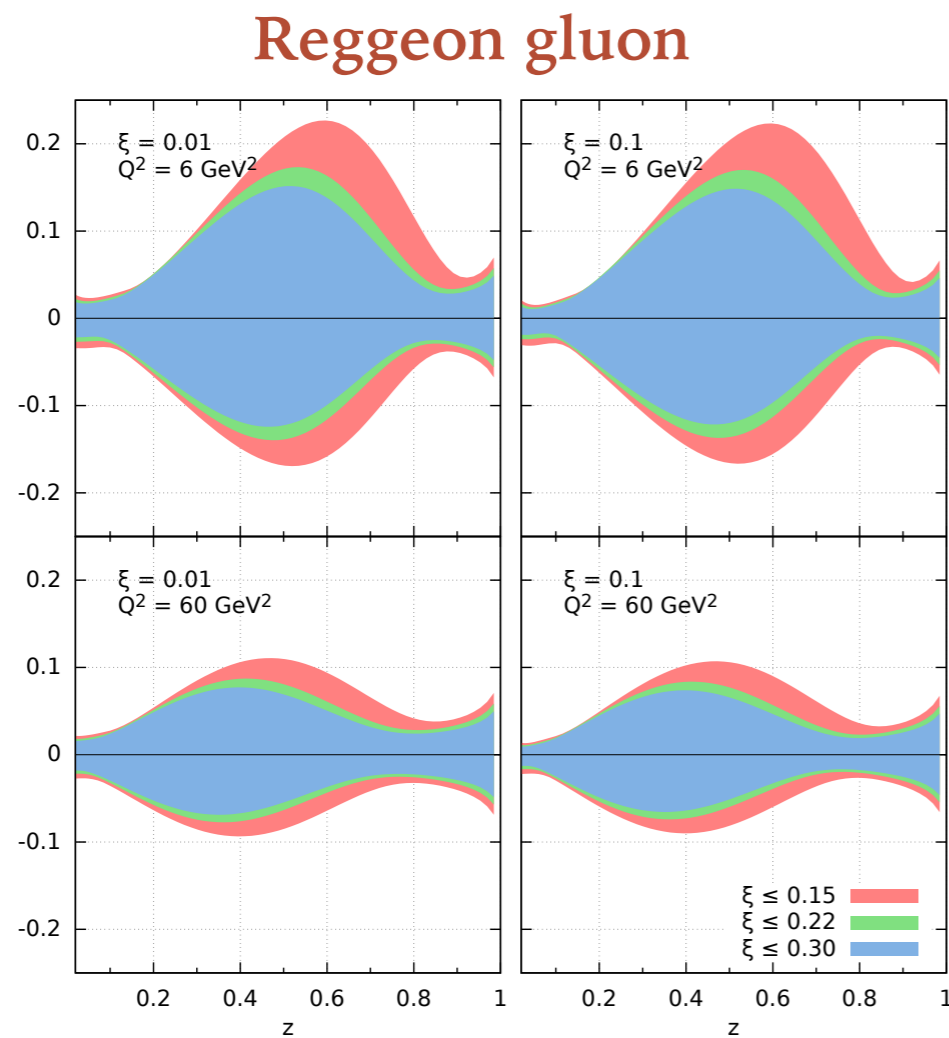
Pomeron quark data cut:  $t \geq -1.5 \text{ GeV}^2$



- relative uncertainty
- <few % or better in most regions
- larger uncertainty for gluon at large  $z$  (and also small  $z$ )
- normalization error at 2% is dominant at most regions (dashed red)

*linear horizontal scale  
note different vertical scale for  
gluons and quarks*

# Uncertainties of diffractive PDFs: Reggeon



- $< 2\%$  or better in most regions for quark except at large  $z$
- Larger uncertainty for Reggeon gluon which is much smaller than Pomeron gluon
- Mild sensitivity to the cut on  $\xi$  for gluon, quark less sensitive
- Minimal sensitivity to the cut on  $t$ , dense vs sparse binning, lower luminosity  $\mathcal{L} = 10 \text{ fb}^{-1}$

**EIC can constrain Reggeon at similar level of precision as the Pomeron even when restricting data to  $|t| \leq 0.5 \text{ GeV}^2$  and  $\xi_{\text{max}} \simeq 0.15 \div 0.2$**

# Precision on flux parameters

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Regge type flux for Pomeron/Reggeon :

$$f_{\mathbb{P},\mathbb{R}}^p(\xi, t) = A_{\mathbb{P},\mathbb{R}} \frac{e^{B_{\mathbb{P},\mathbb{R}}t}}{\xi^{2\alpha_{\mathbb{P},\mathbb{R}}(t)-1}}$$

Trajectory :

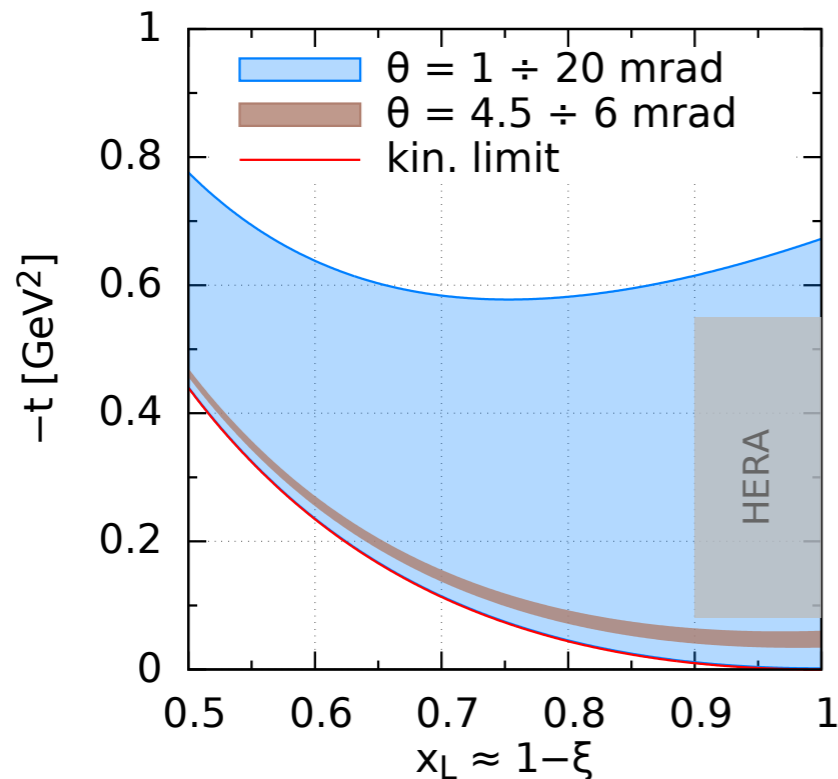
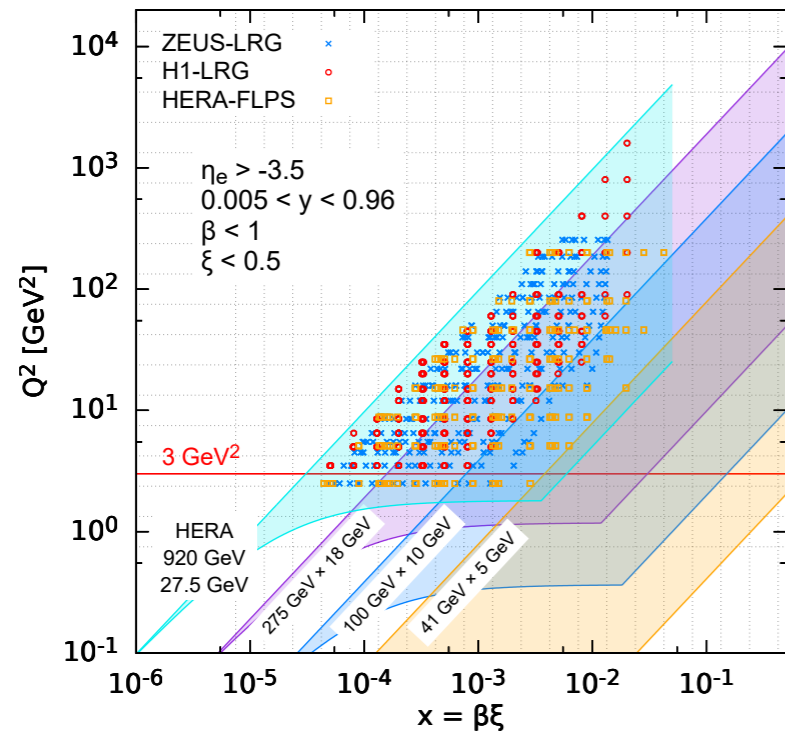
$$\alpha_{\mathbb{P},\mathbb{R}}(t) = \alpha_{\mathbb{P},\mathbb{R}}(0) + \alpha'_{\mathbb{P},\mathbb{R}} t$$

Parameter	Input	Fit
$\alpha_{\mathbb{P}}(0)$	1.11	$1.1119 \pm 0.0007$
$\alpha'_{\mathbb{P}}$	0	$-0.0024 \pm 0.0010$
$B_{\mathbb{P}} [\text{GeV}^{-2}]$	7	$7.033 \pm 0.010$
$\alpha_{\mathbb{R}}(0)$	0.70	$0.7014 \pm 0.0018$
$\alpha'_{\mathbb{R}}$	0.90	$0.8957 \pm 0.0021$
$B_{\mathbb{R}} [\text{GeV}^{-2}]$	2	$2.020 \pm 0.073$

Input values recovered with very precisely

Some flux parameters get correlated with the PDF parameters

# Low energy scenario



- Low energy scenario:

$$E_e = 5 \text{ GeV} \times E_p = 41 \text{ GeV}$$

- Kinematics restricted:

- $\xi \geq 0.01$ , by cms energy

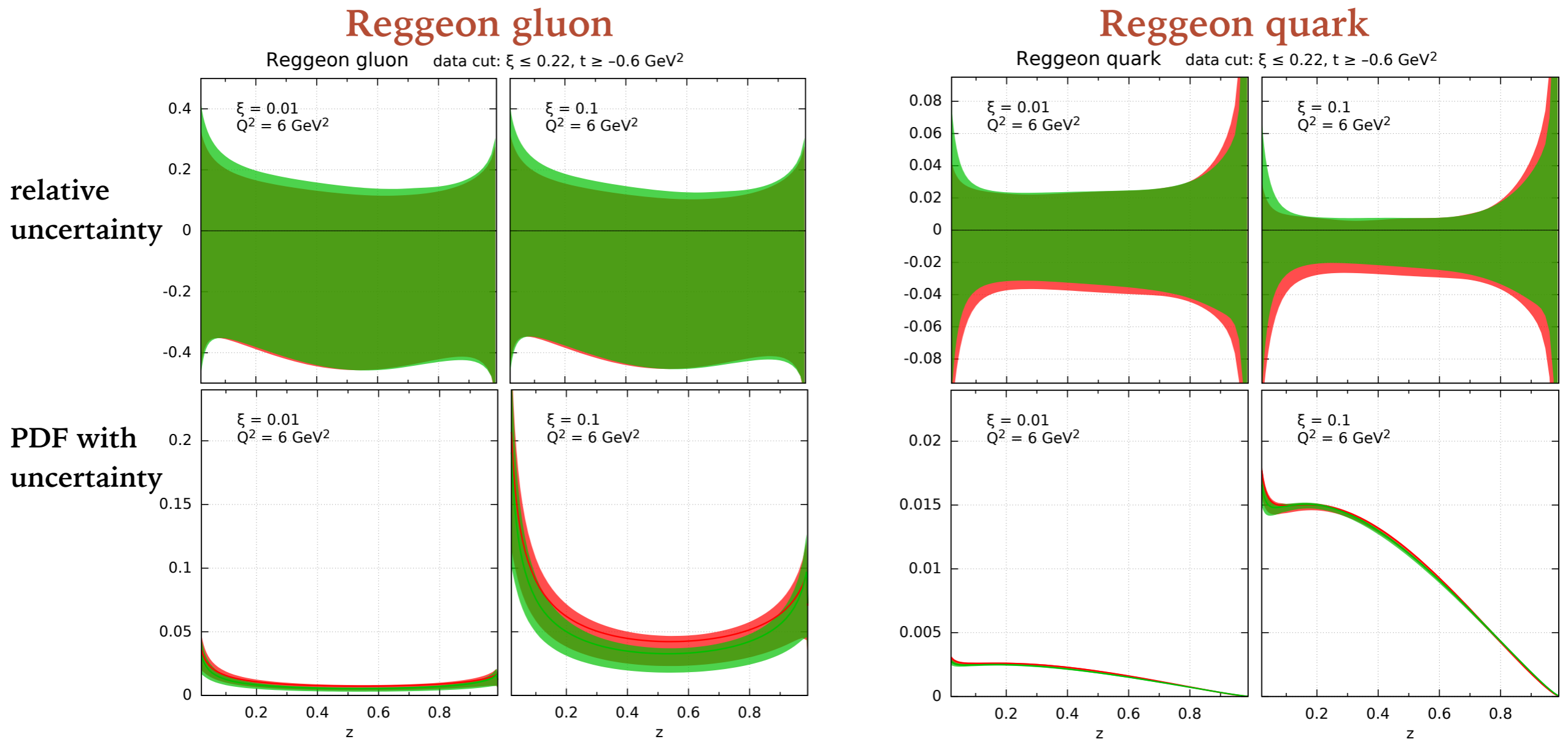
- $t \geq -0.6 \text{ GeV}^2$ , forward detector acceptance

- Reggeon dominated

- Fix Pomeron from HERA and fit only Reggeon

- Luminosity  $\mathcal{L} = 10 \text{ fb}^{-1}$

# Low energy: Reggeon DPDFs and uncertainties



- Quark Reggeon constrained very well
- Larger uncertainty for Reggeon gluon which is much smaller than Pomeron gluon
- Two bands indicate sensitivity to two Monte Carlo samples: small variation

**Low energy data at EIC can already determine Reggeon**

# Summary

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- 4-D fit with Pomeron and Reggeon to the diffractive pseudodata
- EIC can extract flux parameters and partonic structure of the subleading ‘Reggeon’ exchange with similar precision to the leading ‘Pomeron’ exchange
- Constraints on Reggeon already from low energy run

More work needed on uncertainties:

- Experimental (correlated systematics)
- Theoretical (model dependence, parton parametrization)

Ideas for further studies:

- Combined HERA and EIC fits
- Charged current contribution