

SPICE, ECT*, Trento, Italy (May 13—May 17, 2024)

High Resolution Missing Mass Spectroscopy of Hypernuclei at JLab and J-PARC

Graduate School of Science, Kyoto University

Toshiyuki Gogami

May 17, 2024

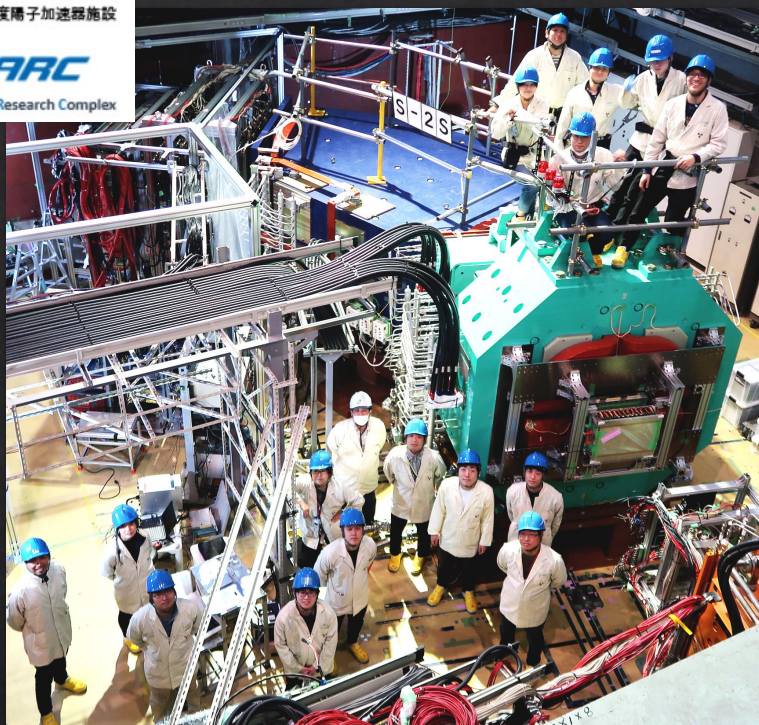


GRADUATE
SCHOOL OF
FACULTY OF
SCIENCE
KYOTO UNIVERSITY

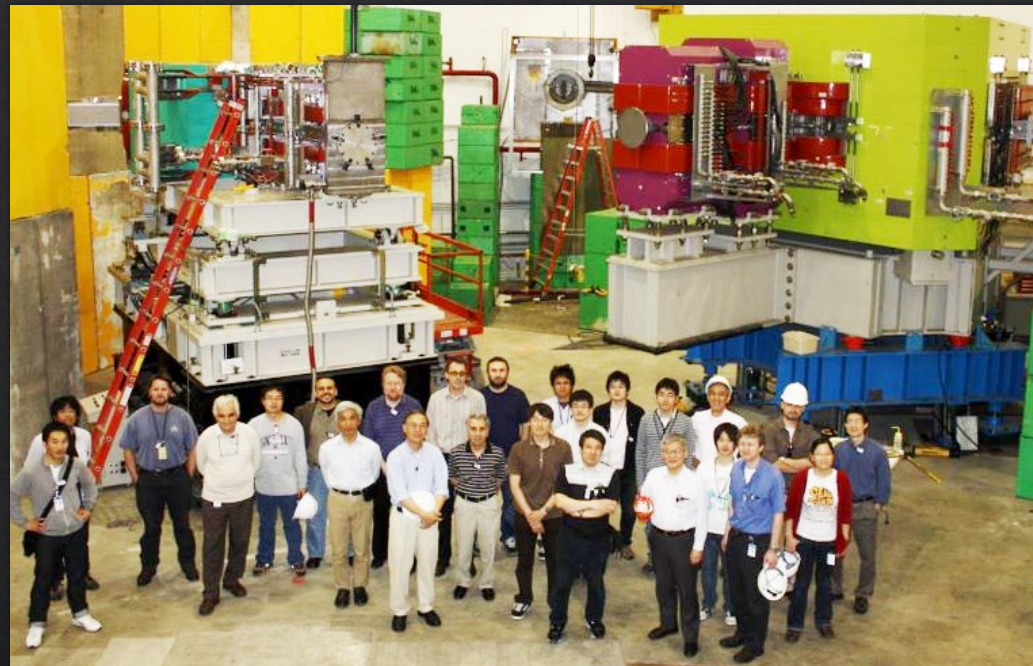


This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093

Λ hypernuclear studies in near future

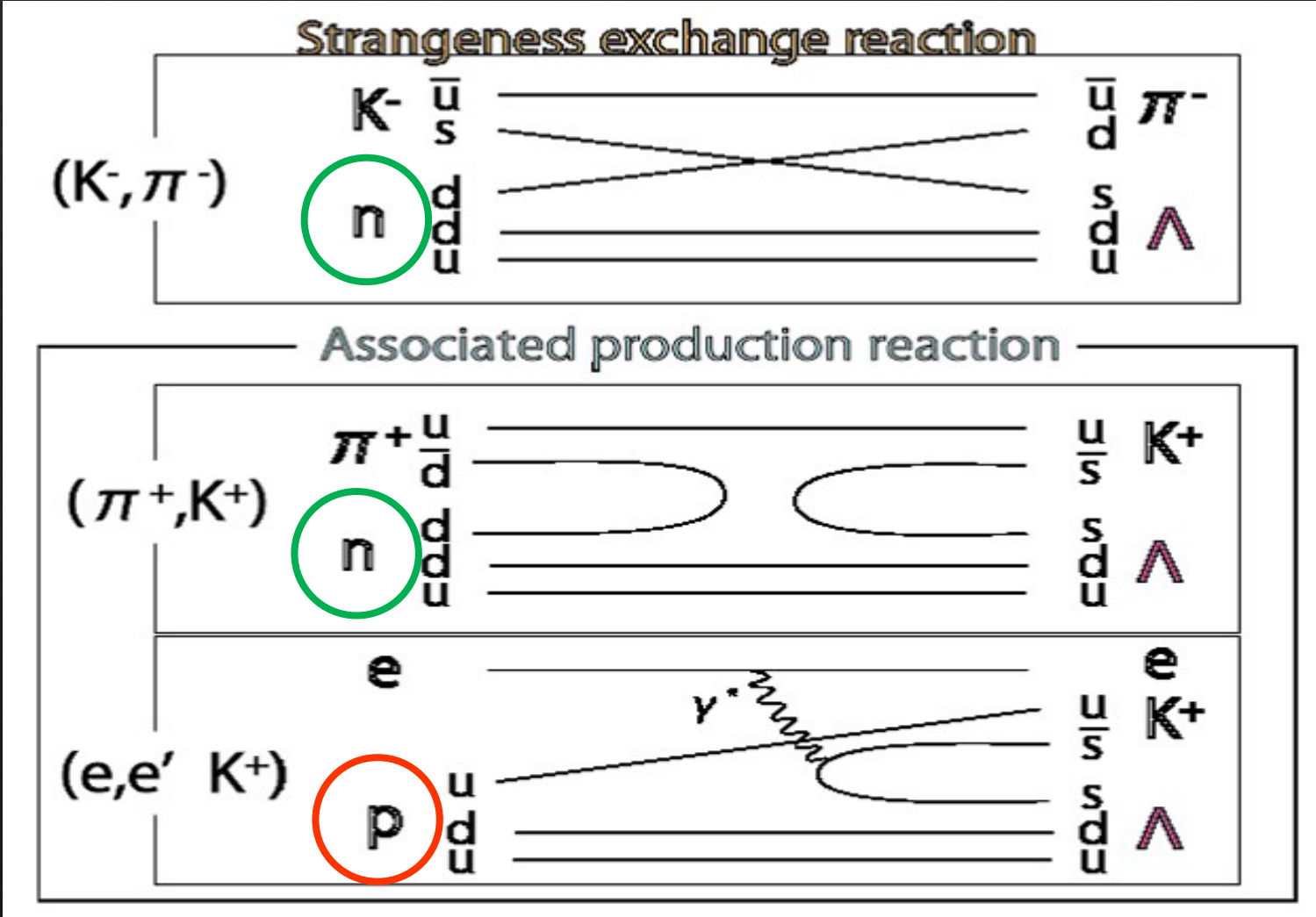


S-2S (2025~)
A = 7, 10, 12



HES-HKS (2027~)
A = 6, 9, 11, 12, 40, 48, 208

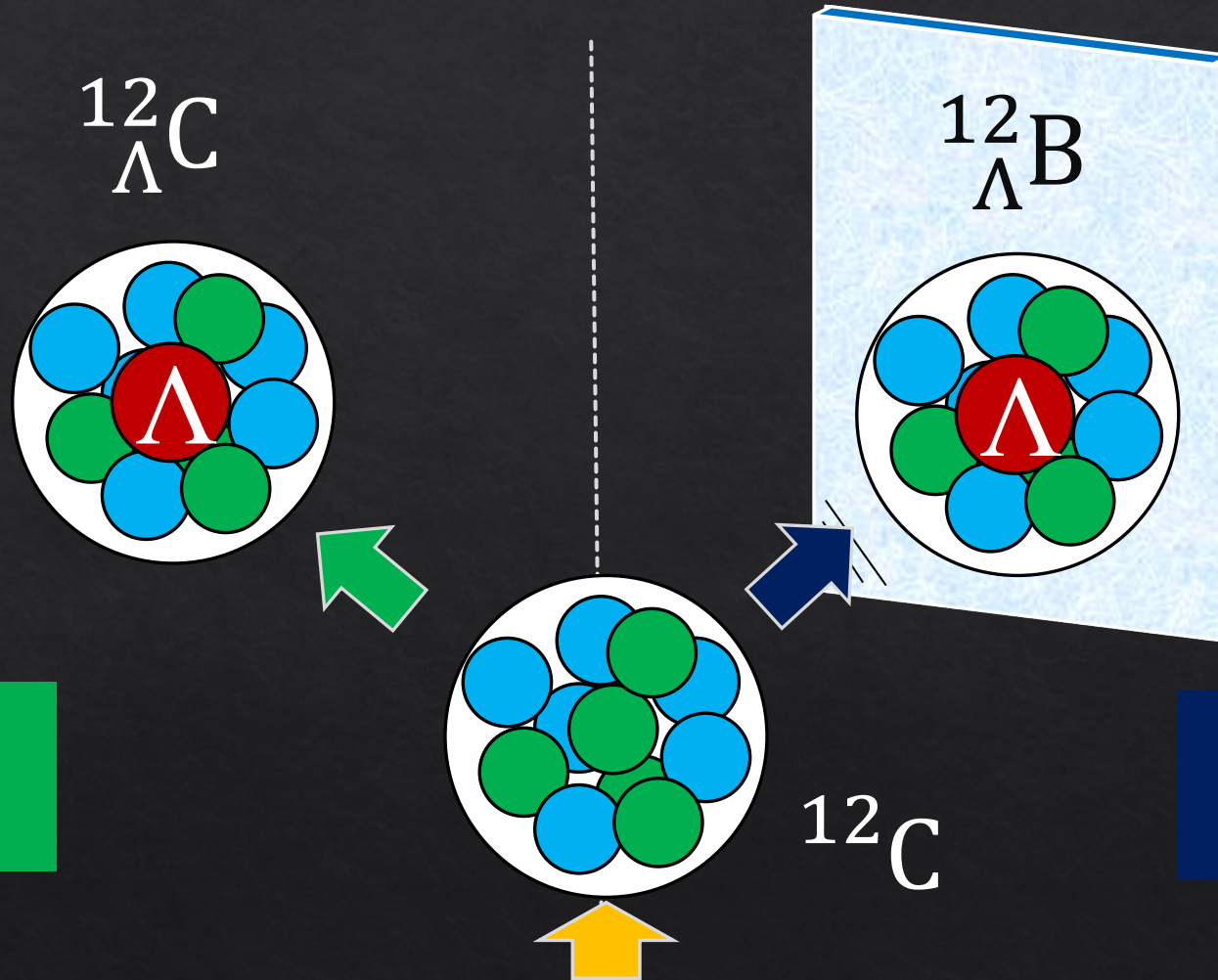
Reactions used at J-PARC and JLab



Hadron Beams
@J-PARC

Electron Beams
@JLab

Mirror Hypernuclear Study



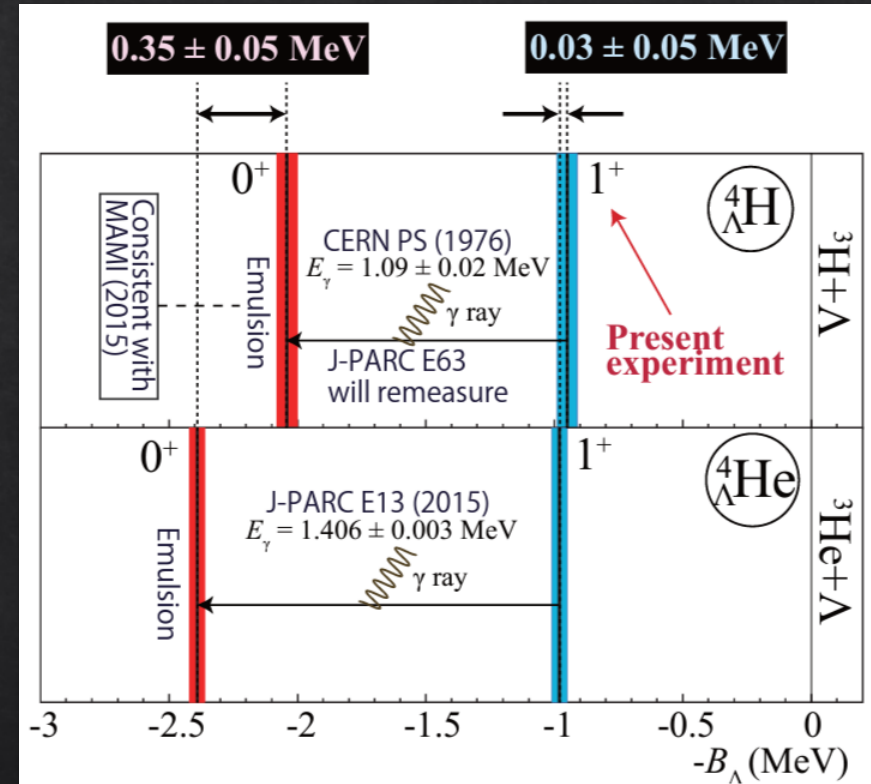
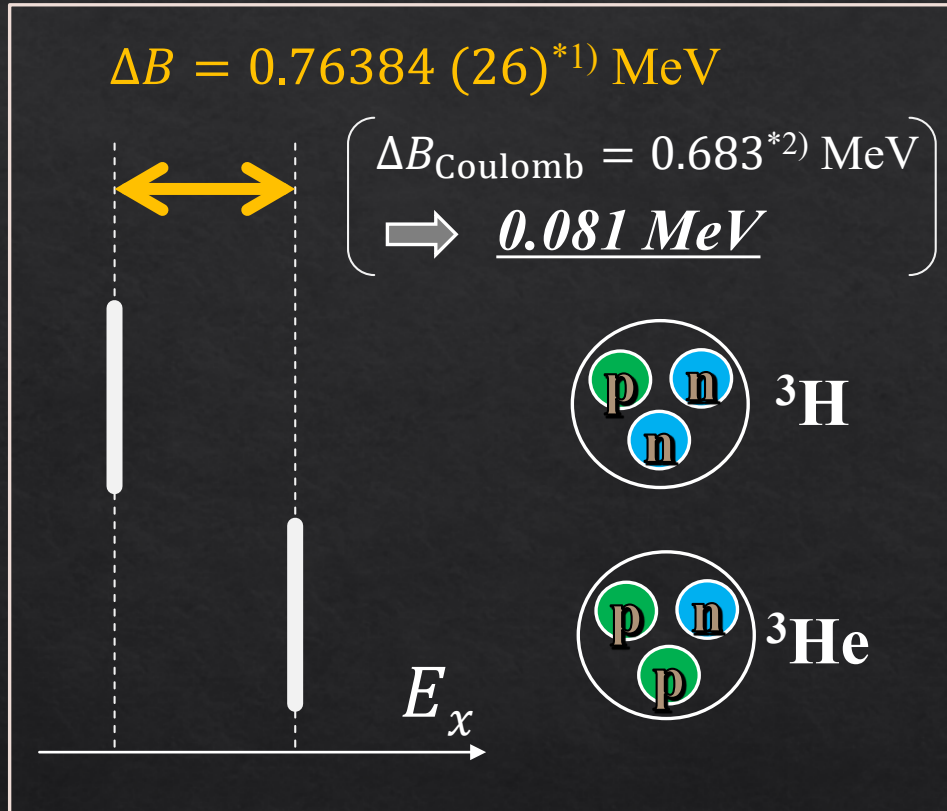
(π^+, K^+)



$(e, e'K^+)$

Charge Symmetry Breaking (CSB), the mystery

Figure from proposal of [JLab E12-19-002](#)



*1) J.H.E.Mattauch *et al.*, *Nucl. Pys.* **67**, 1 (1965).

*2) R.A.Brandenburg, S.A.Coon *et al.*, *NPA294*, 305 (1978).

The CSB origin is not clear yet.

Mirror hypernuclear data for p-shell systems

Isomultiplet	${}^4_{\Lambda}\text{He}-{}^4_{\Lambda}\text{H}$	${}^7_{\Lambda}\text{Be}-{}^7_{\Lambda}\text{Li}^*$	${}^7_{\Lambda}\text{Li}^*-{}^7_{\Lambda}\text{He}$	${}^8_{\Lambda}\text{Be}-{}^8_{\Lambda}\text{Li}$	${}^9_{\Lambda}\text{B}-{}^9_{\Lambda}\text{Li}$	${}^{10}_{\Lambda}\text{B}-{}^{10}_{\Lambda}\text{Be}^*$
Shell model (Gal <i>et al.</i>) [41]	+226	-17	-28	+49	-54	-136
Cluster model (Hiyama <i>et al.</i>) [39, 40]		+150	+130			+20
No-core shell model (Le <i>et al.</i>) [43]	+238	-35	-16	+143		
Experiment	$+233 \pm 92$	-100 ± 90	-20 ± 230	$+40 \pm 60$	-210 ± 220	-220 ± 250

A. Gal, and D. Gazda, Jour. Phys.: Conf. Ser. 966, 012006 (2018)

E. Hiyama et al., Prog. Theor. Phys. 128, 105 (2012).

H. Le et al., Phys. Rev. C 107, 24002 (2023)

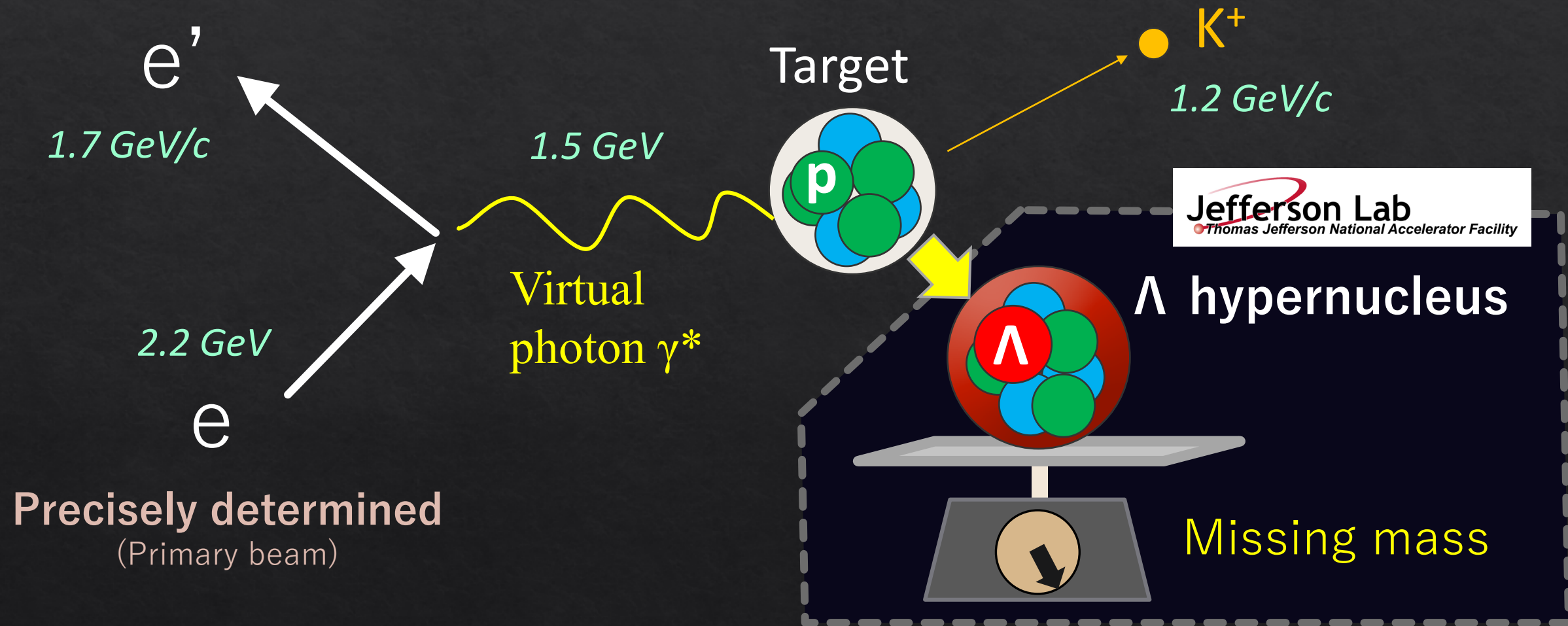
Existing data accuracy is not sufficient for CSB study ($\Delta B_{\text{diff}} > 200$ keV)

$\rightarrow \Delta B_{\text{diff}} \sim 100$ keV for $A = 6, 7, 9, 10, 11, 12$

Missing-mass spectroscopy

(Measure)

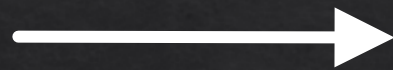
(Measure)



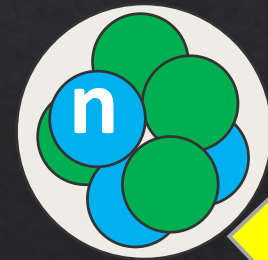
Missing-mass spectroscopy

(Measure)

π^+
 $1.05 \text{ GeV}/c$



Target



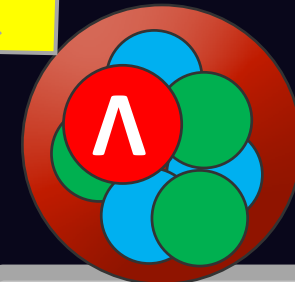
(Measure)

K^+

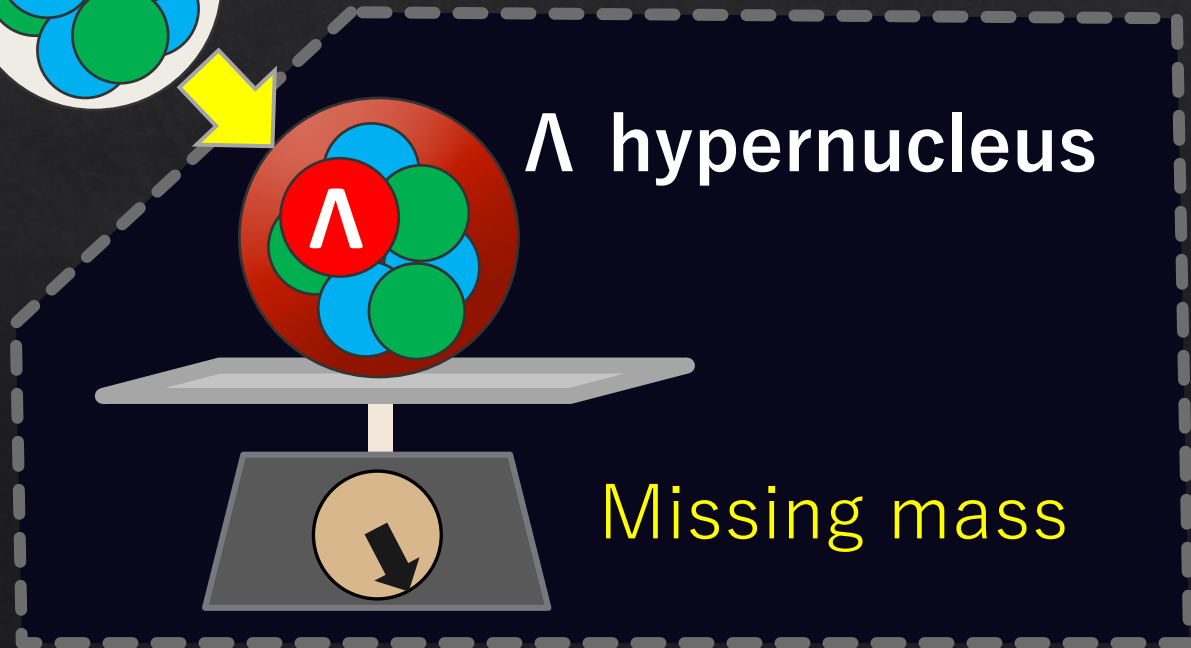
$0.72 \text{ GeV}/c$

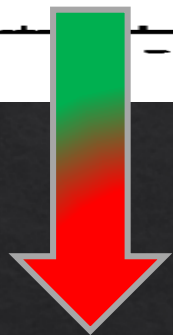
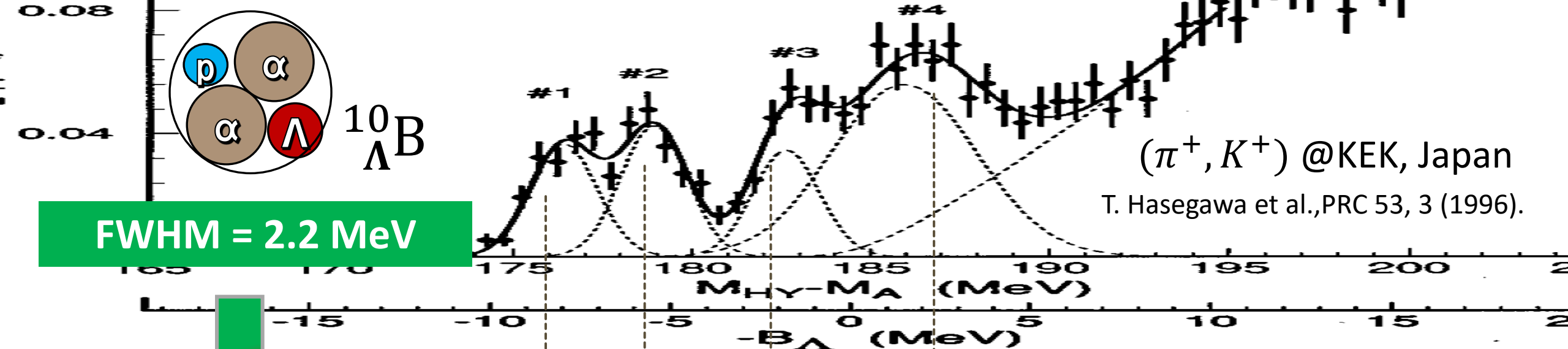


Λ hypernucleus

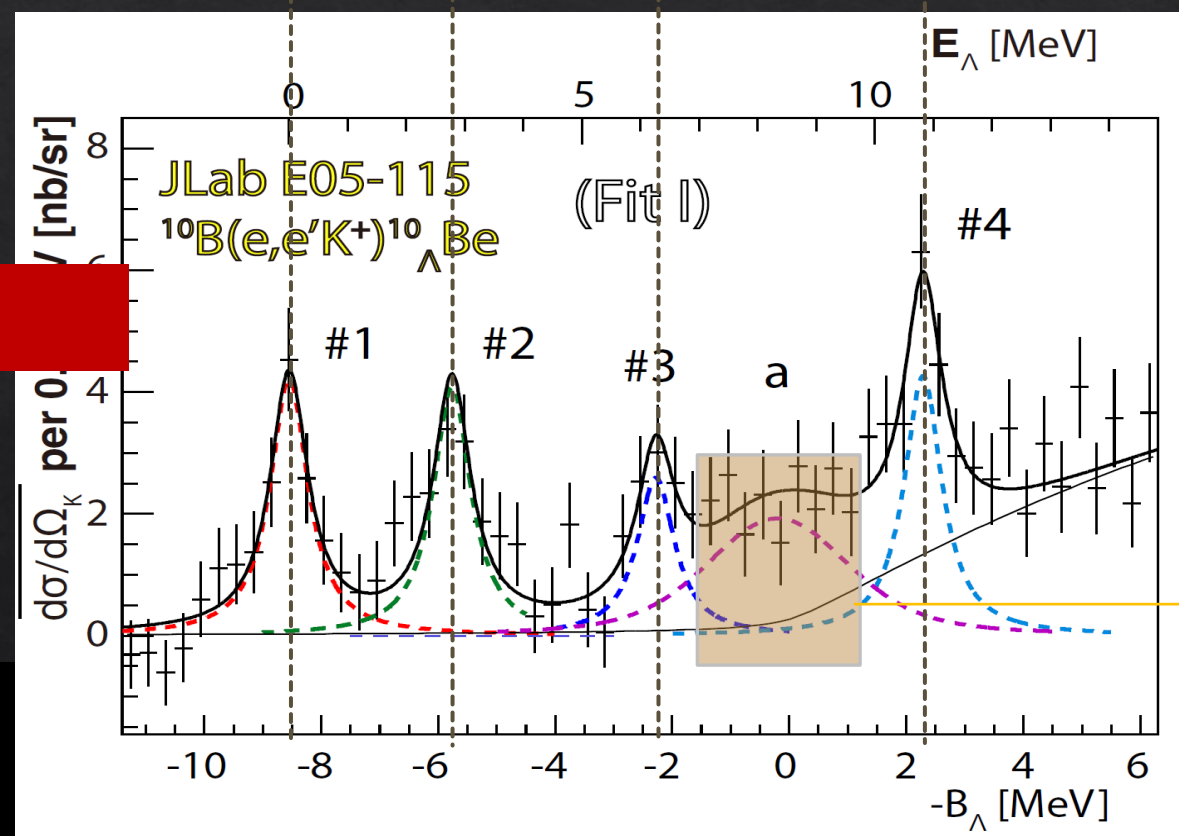


Missing mass

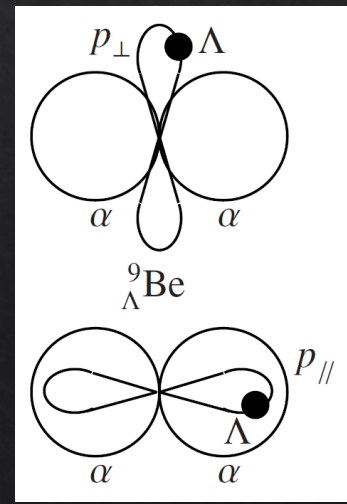




FWHM = 0.8 MeV



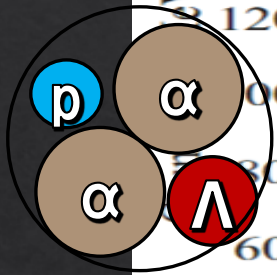
Cluster structure!!



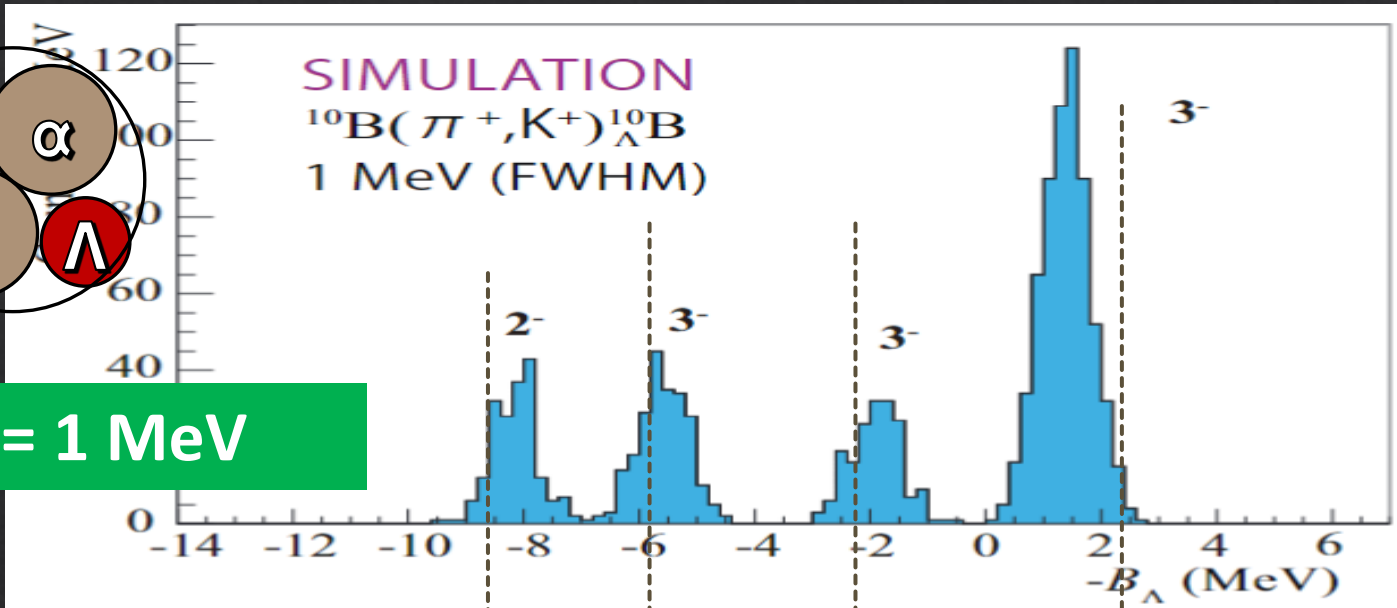
TG et al., PRC 93, 034314 (2016).

A. Umeya et al., J. Phys.: Conf. Ser. 1643 012110 (2020)

$^{10}_{\Lambda}\text{B}$

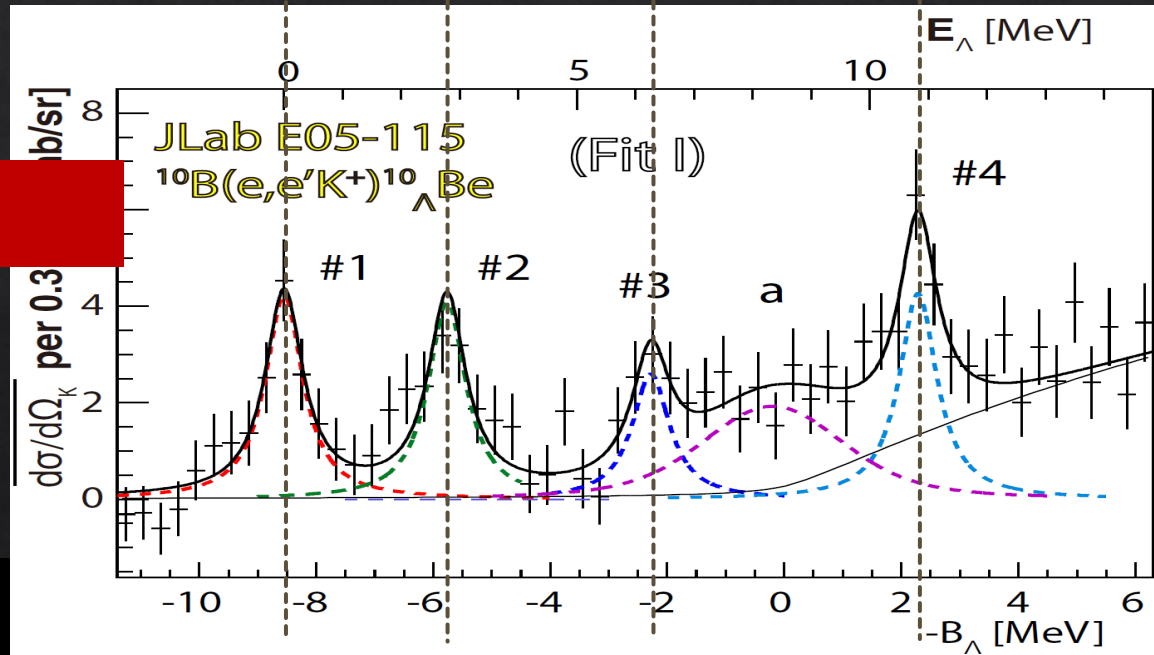
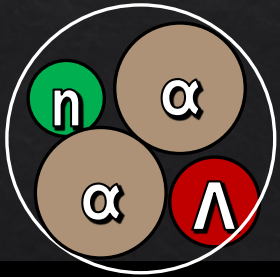


FWHM = 1 MeV



FWHM = 0.8 MeV

$^{10}_{\Lambda}\text{Be}$



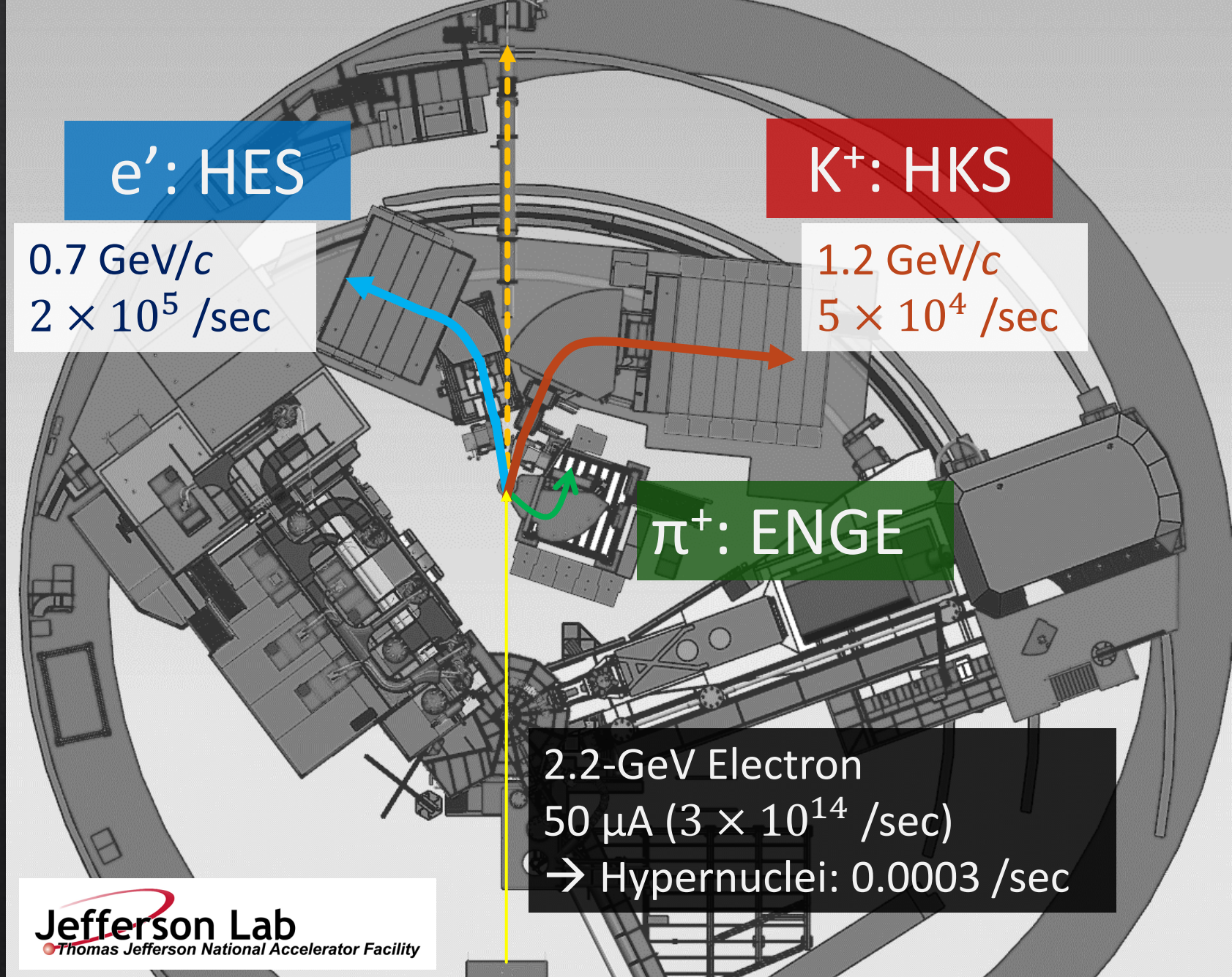
TG et al.,
PRC 93, 034314 (2016).

S-2S

@J-PARC
(J-PARC E94)

HKS
@JLab

New experiment at JLab Hall-C (2027~)





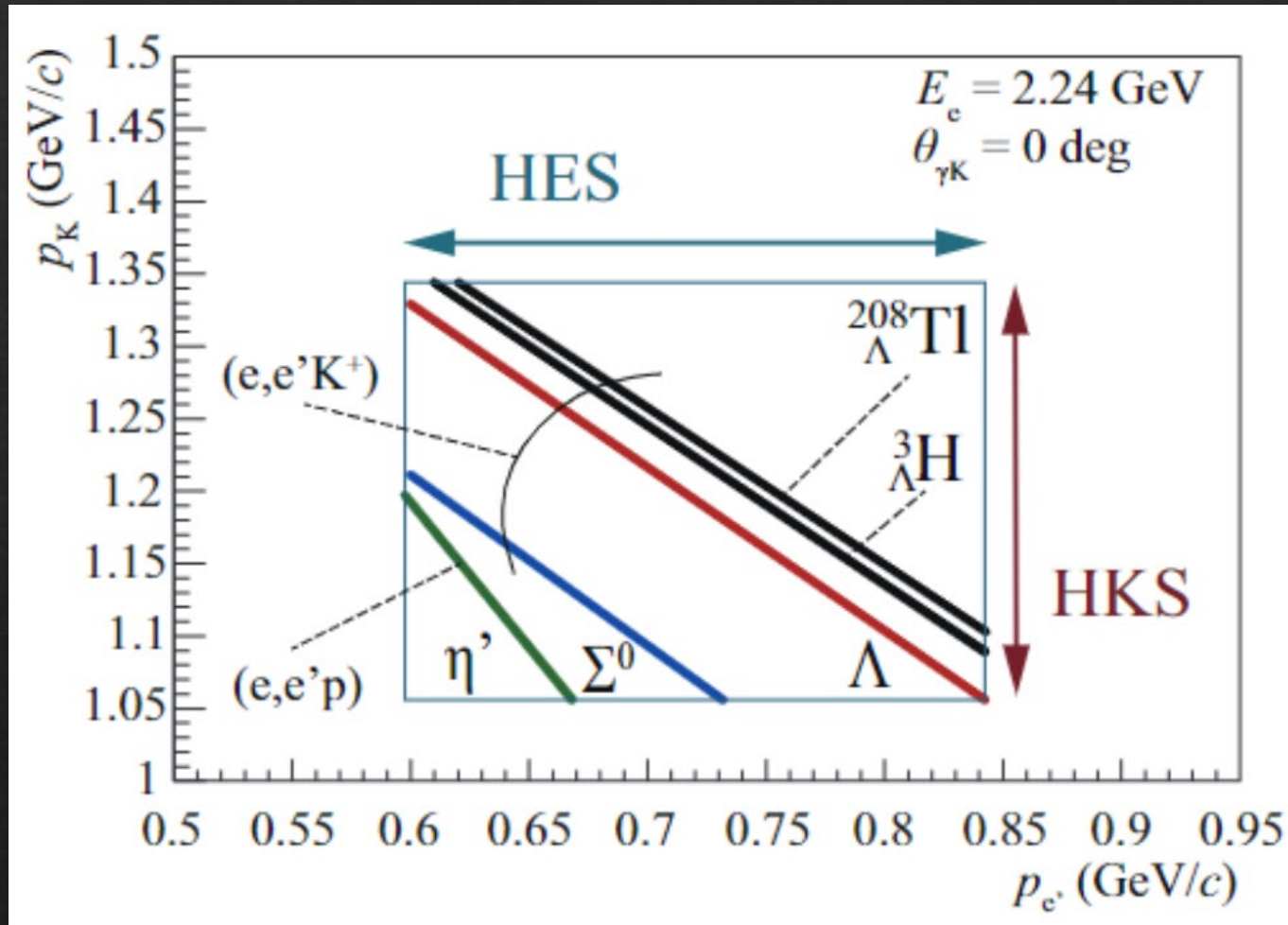
HES

HKS

Hall C (2009)

Jefferson Lab
Thomas Jefferson National Accelerator Facility

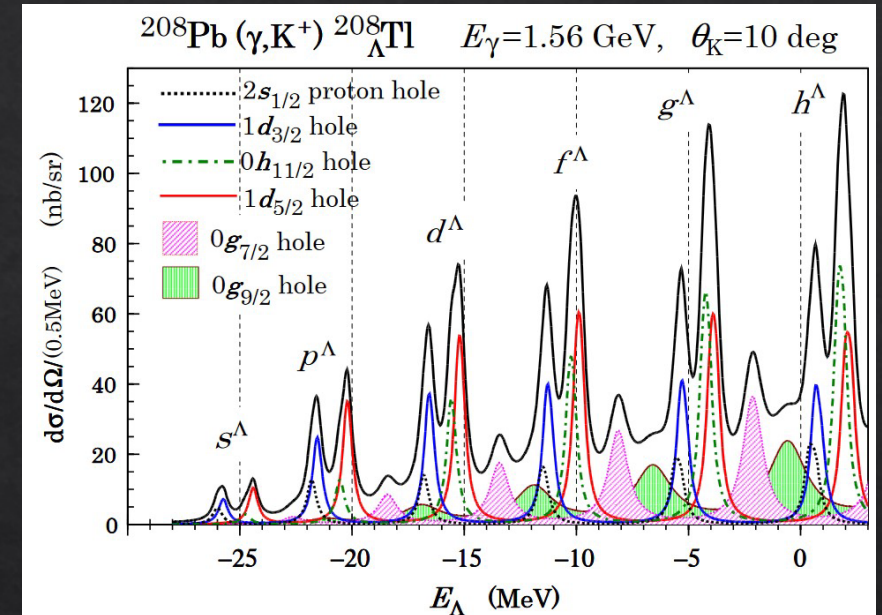
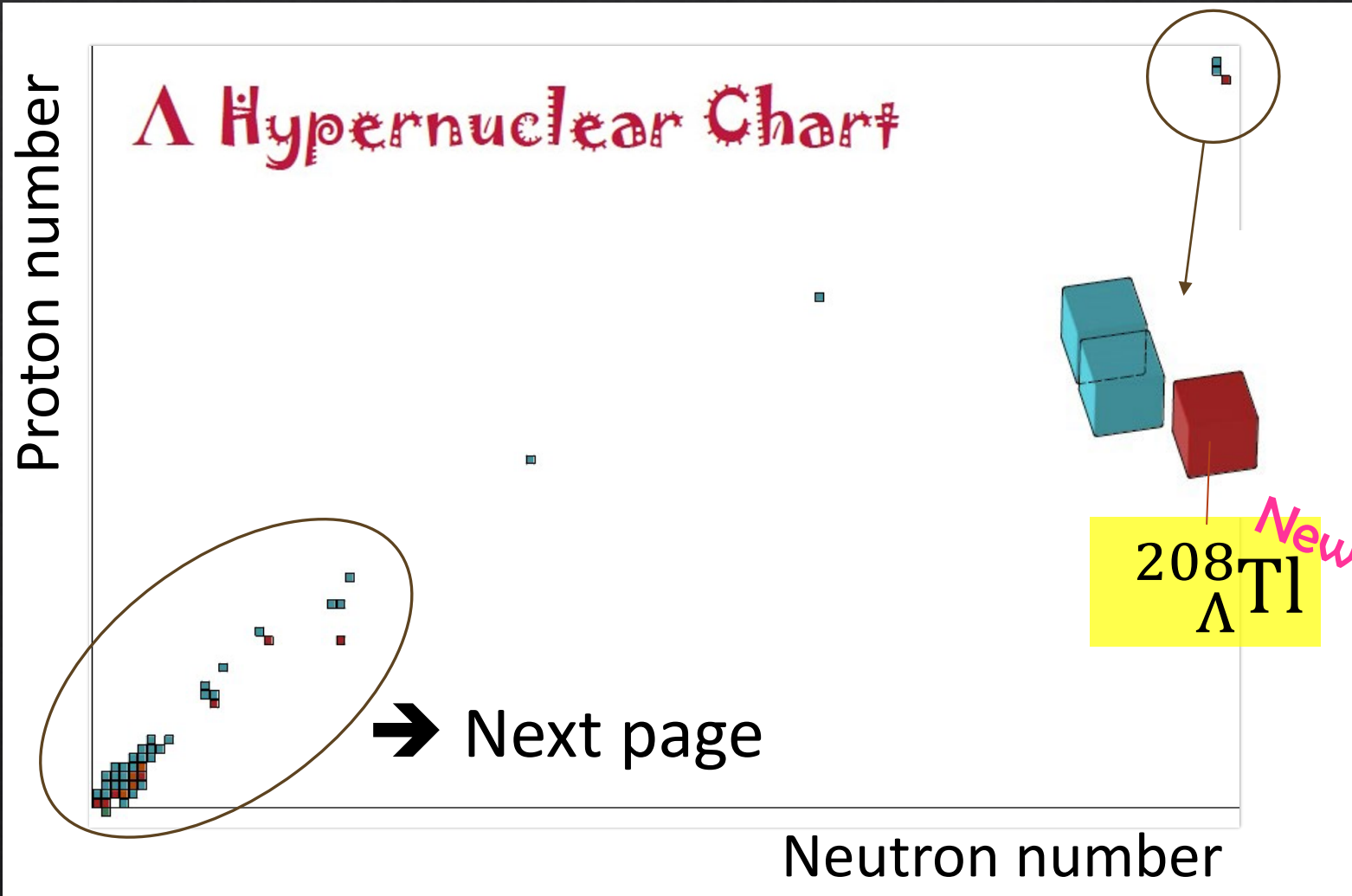
High accuracy calibration by known mass sources



High Accuracy
 $|\Delta B_{\Lambda}^{total}| \leq 70$ keV

Next JLab experiments; light to heavy hypernuclei

T. Motoba, *JPS Conf. Proc.* 17, 011003 (2017)



Approved

JLab E12-20-013

→ Λ NN force

Next JLab experiments; light to heavy hypernuclei

New Proposals
(2024)



Missing mass

LO12-23-013

LO12-23-016

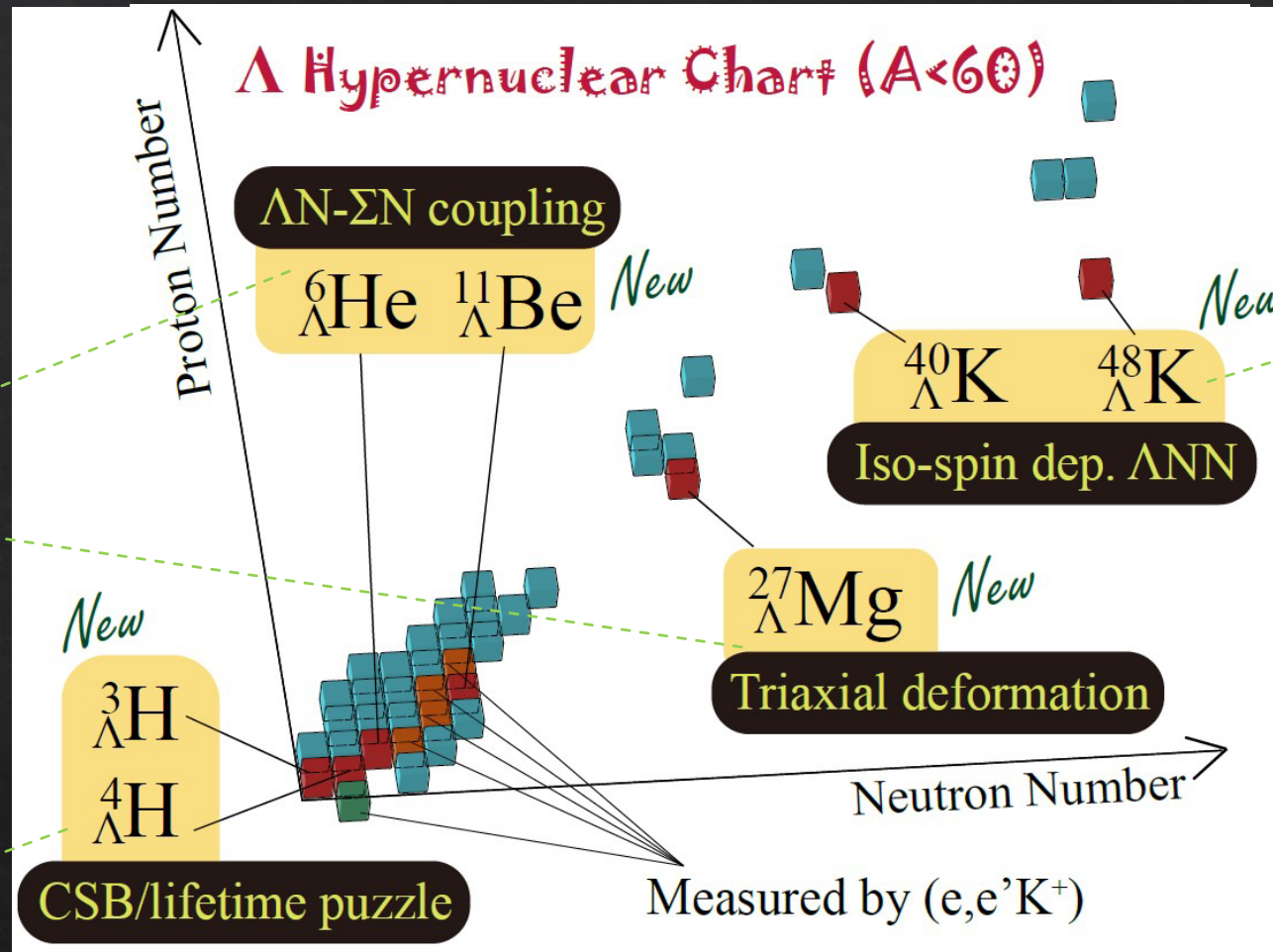
Decay pion

LO12-23-011

Approved

E12-19-002

Excited states!



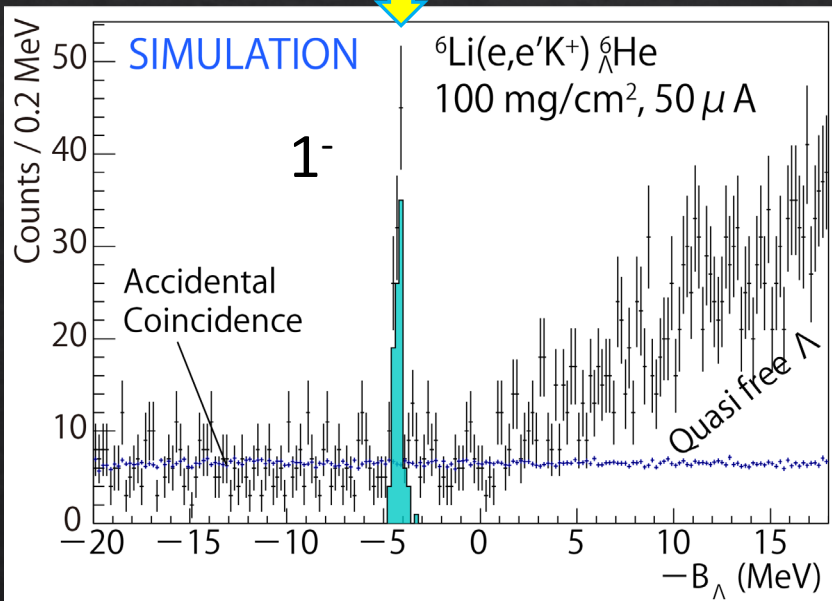
Approved

E12-15-008

JLab LOI12-23-013 → New proposal (2024)

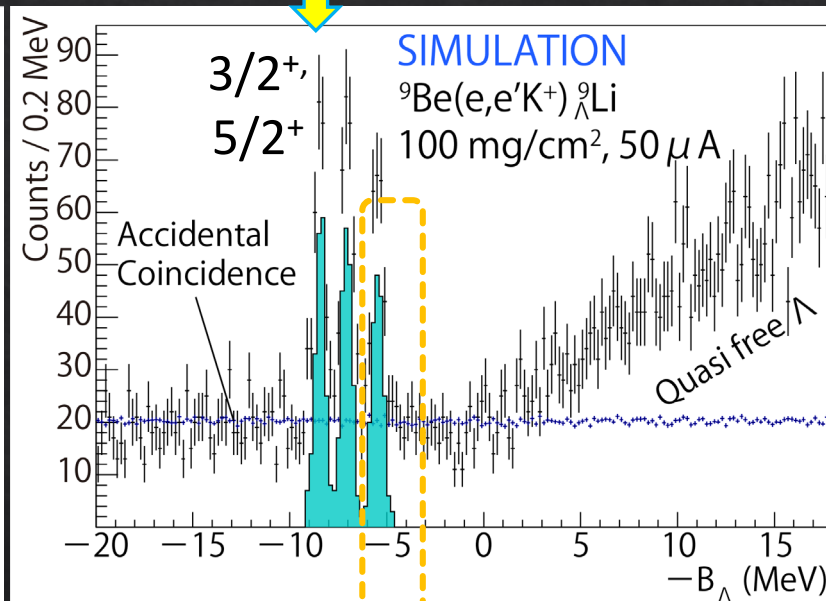
for CSB study

120 hours



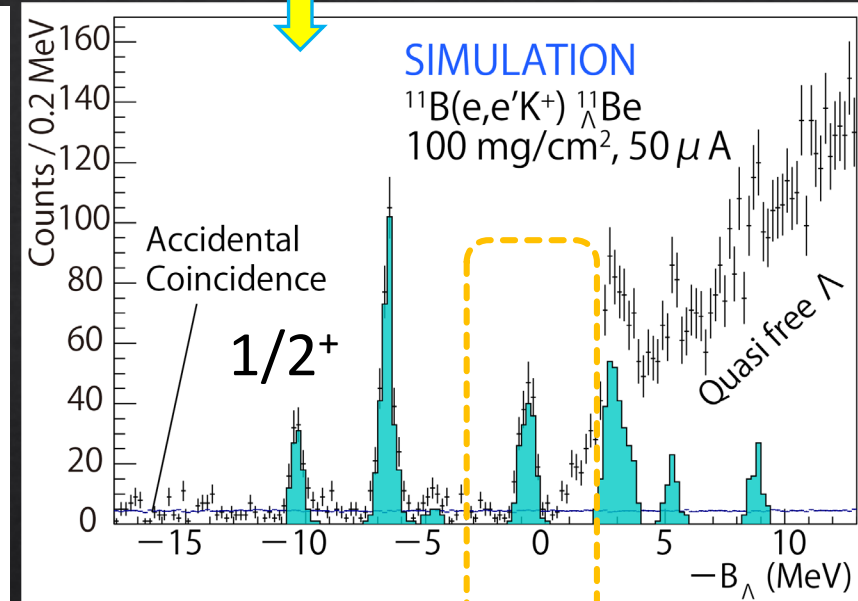
for CSB study

384 hours



for CSB study

72 hours



Accuracy:

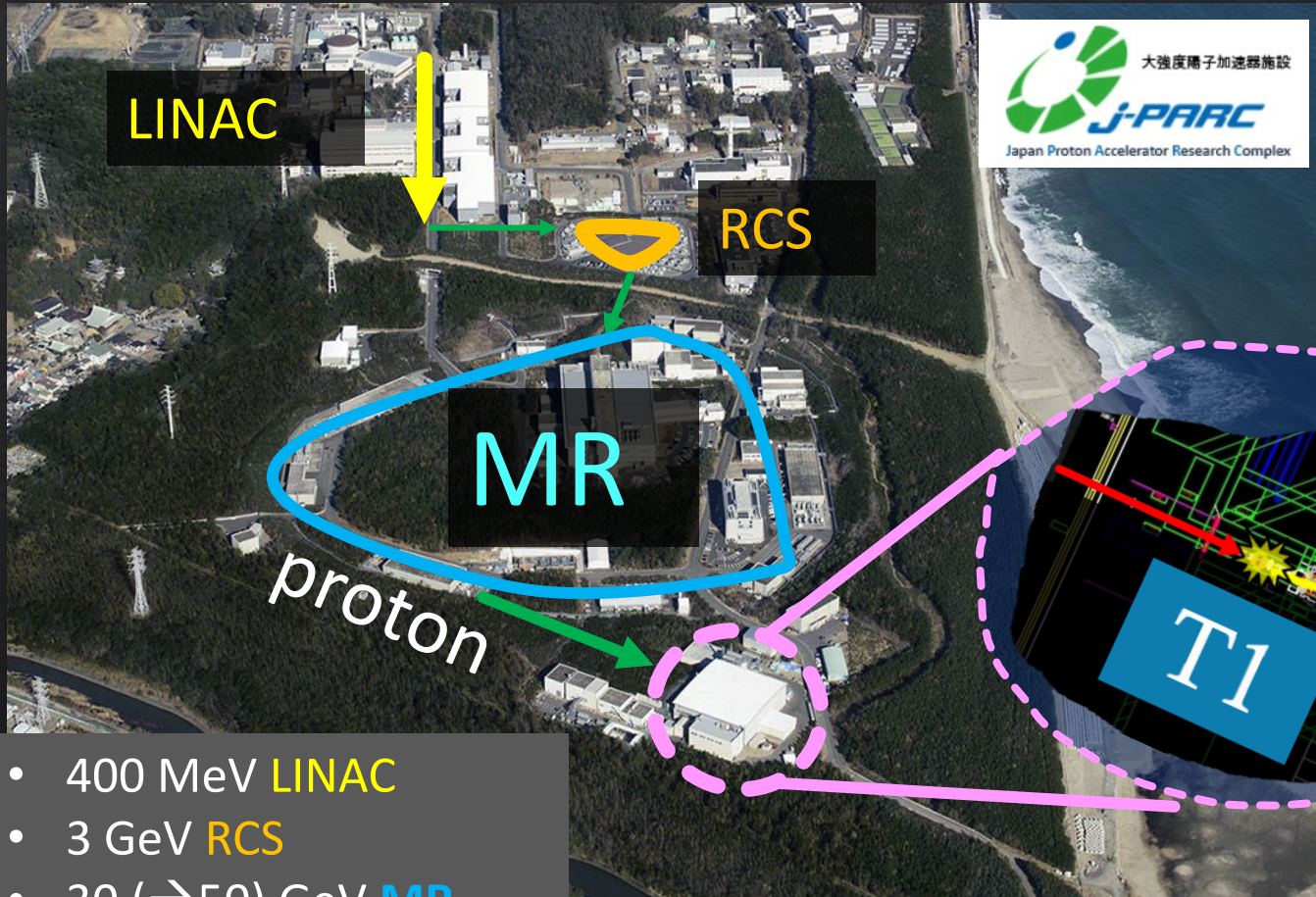
$$|\Delta B_\Lambda^{\text{total}}| \leq 70 \text{ keV}$$

c.f.) [TG et al., PRC 103, L041301 \(2021\)](#)

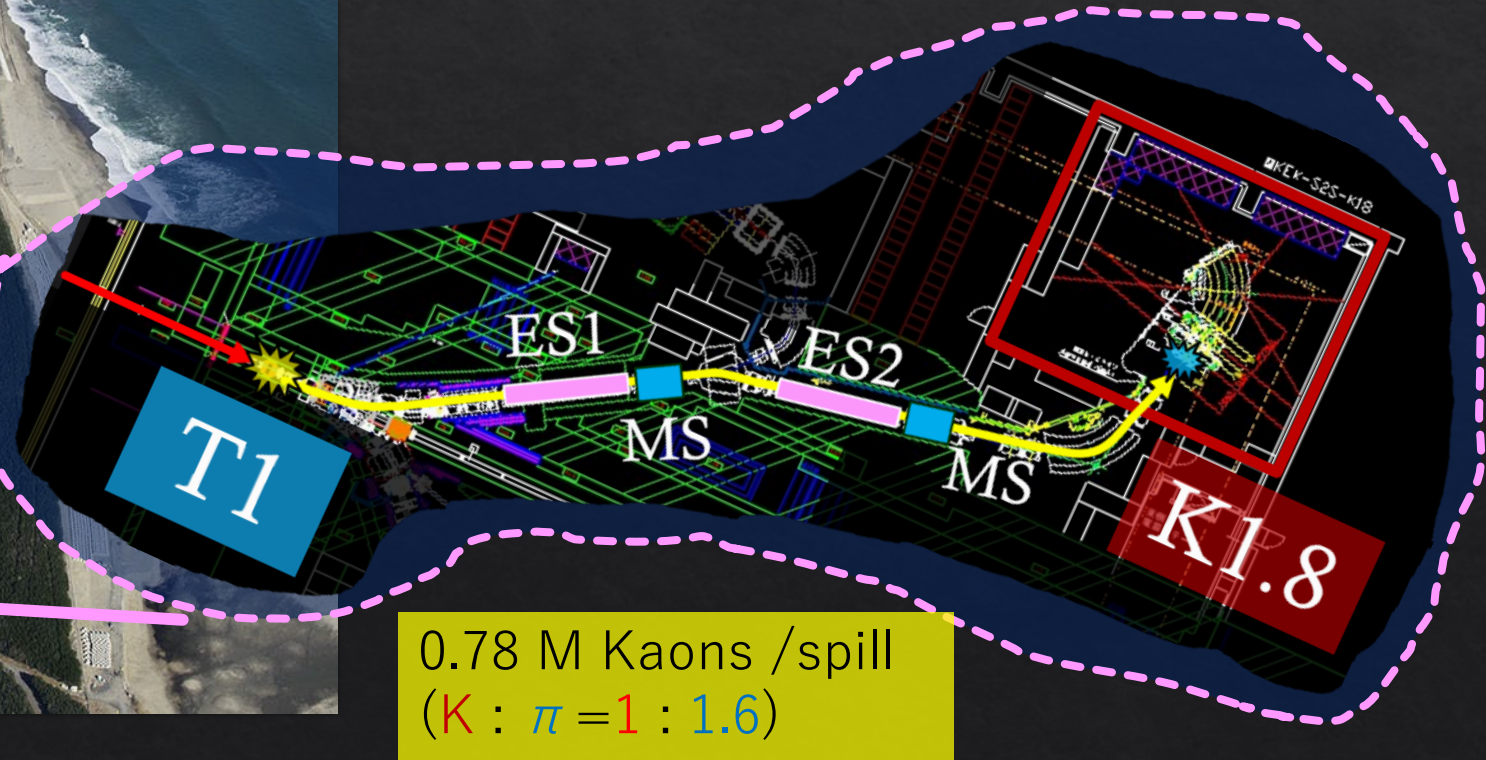
c.f.) [Isaka-san's talk](#)

Cluster / deformation structures

Japan Proton Accelerator Research Complex (J-PARC), Ibaraki, Japan



$A_Z(\pi^+, K^+)_{\Lambda}^AZ$
@K1.8 Beam line



- 400 MeV LINAC
- 3 GeV RCS
- 30 (\rightarrow 50) GeV MR

0.78 M Kaons /spill
(K : π = 1 : 1.6)

Jun 2022



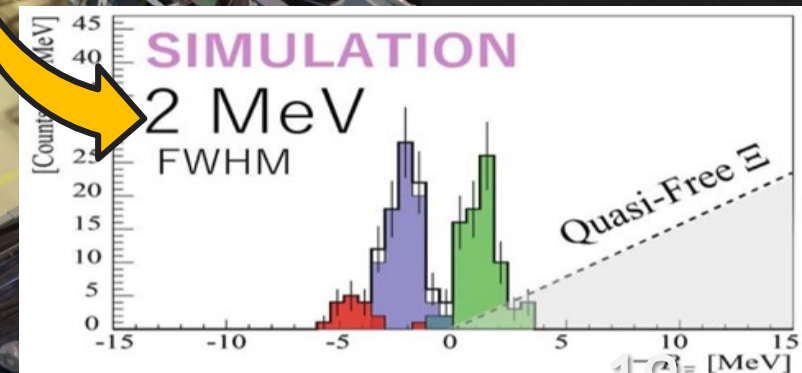
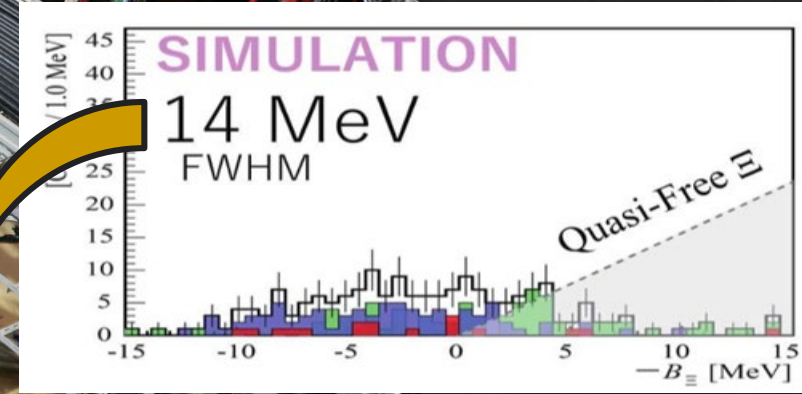
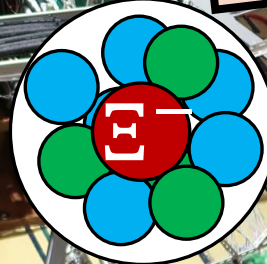
Q2 Q1

1.8 GeV/c

D

K^-

$s\bar{u}$



$s\bar{u}$

K^+

2 m

S-2S

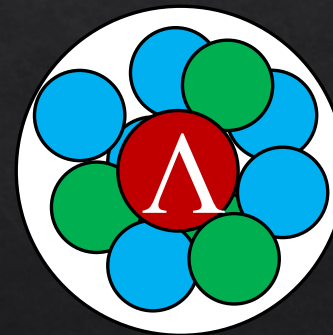
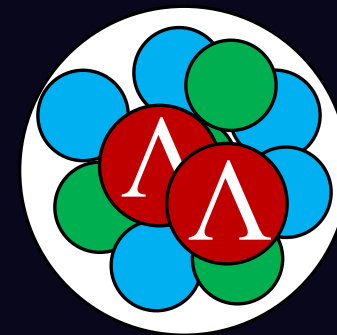
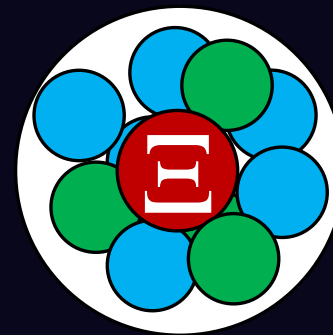
1.37 GeV/c



The first
commissioning/c
alibration data
were taken in
2023 and 2024

Nov 9, 2022 @K1.8 beam line, J-PARC, Japan

"S = -2" study
will start!



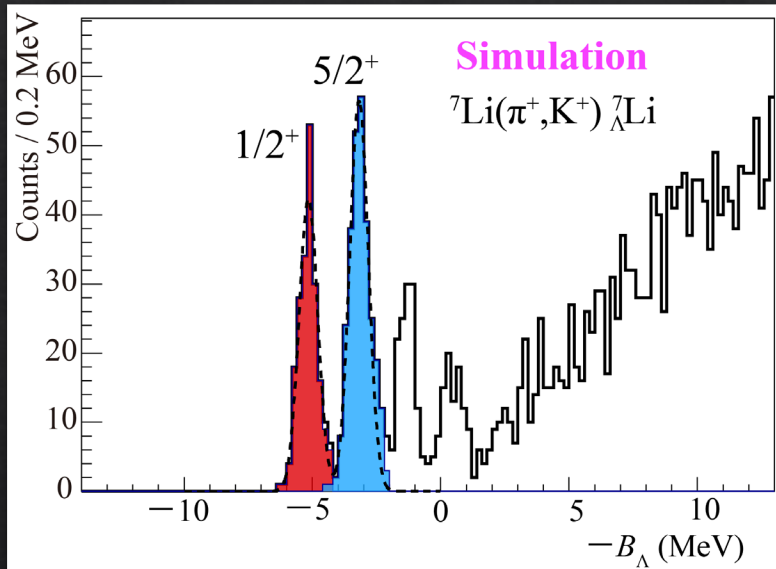
"S = -1"
as well

T. Gogami et al., [EPJ Web Conf. 271, 11002 \(2022\)](#).

Expected spectra (J-PARC E94)

${}^7_{\Lambda}\text{Li}$

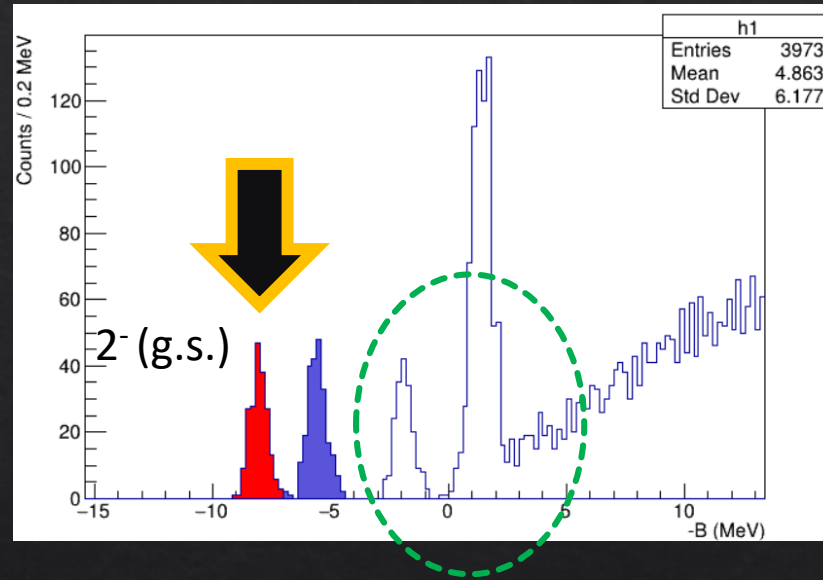
80 hours



Calibration source

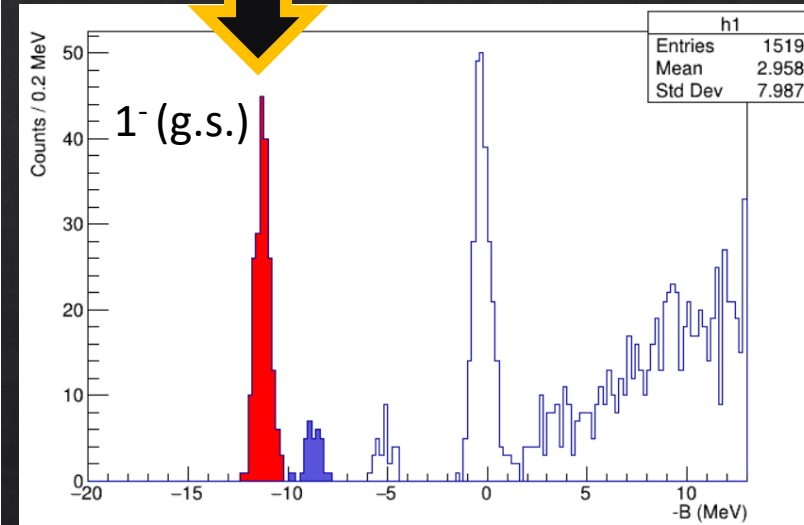
${}^{10}_{\Lambda}\text{B}$

112 hours



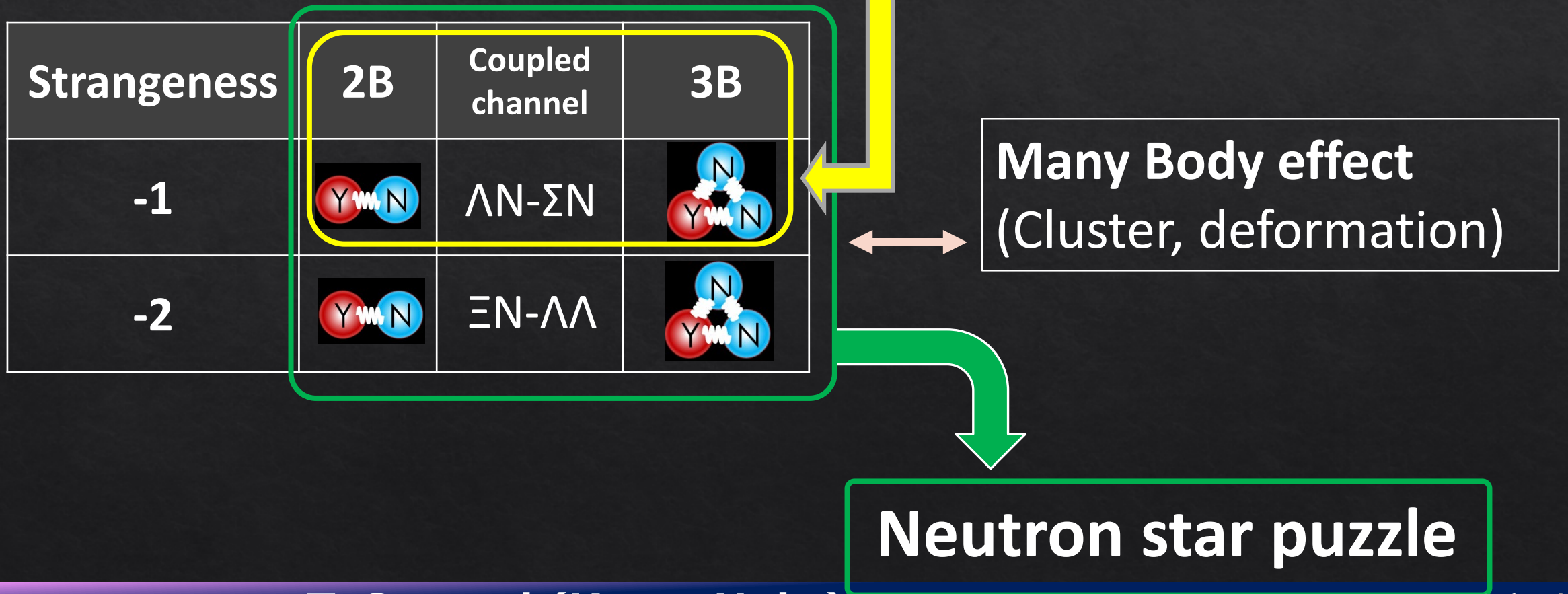
${}^{12}_{\Lambda}\text{C}$

36 hours



$$\left| \Delta B_{\Lambda}^{total} (stat. \oplus sys.) \right| < 0.1 \text{ MeV}$$

CSB ${}^3_{\Lambda}\text{H}$ lifetime puzzle
 $nn\Lambda$ bound puzzle







CSB ${}^3_{\Lambda}\text{H}$ lifetime puzzle

$nn\Lambda$ bound puzzle

Invariant mass spectroscopy by HI beam @LHC, RHIC, GSI

- YN scat. exp.
- Femotoscropy

Strangeness	2B	Coupled channel	3B
-1		$\Lambda N - \Sigma N$	
-2		$\Xi N - \Lambda\Lambda$	

Many Body effect (Cluster, deformation)

- Space observation
- Graviton wave meas.

Neutron star puzzle

J-PARC E63

J-PARC E94

JLab LOI12-23-013

- YN scat. exp.
- Femotoscropy

CSB

${}^3\Lambda\text{H}$ lifetime puzzle

$nn\Lambda$ bound puzzle

JLab E12-19-002

JLab LOI12-23-011

Invariant mass spectroscopy by HI beam @LHC, RHIC, GSI

JLab C12-20-013 (C2)

JLab LOI12-23-016

Many Body effect (Cluster, deformation)

- Space observation
- Graviton wave meas.

Neutron star puzzle

Strangeness	2B	Coupled channel	3B
-1		$\Lambda N - \Sigma N$	
-2		$\Xi N - \Lambda\Lambda$	

J-PARC E70

J-PARC E75

J-PARC E96

JLab E12-15-008

JLab E12-20-013

Summary

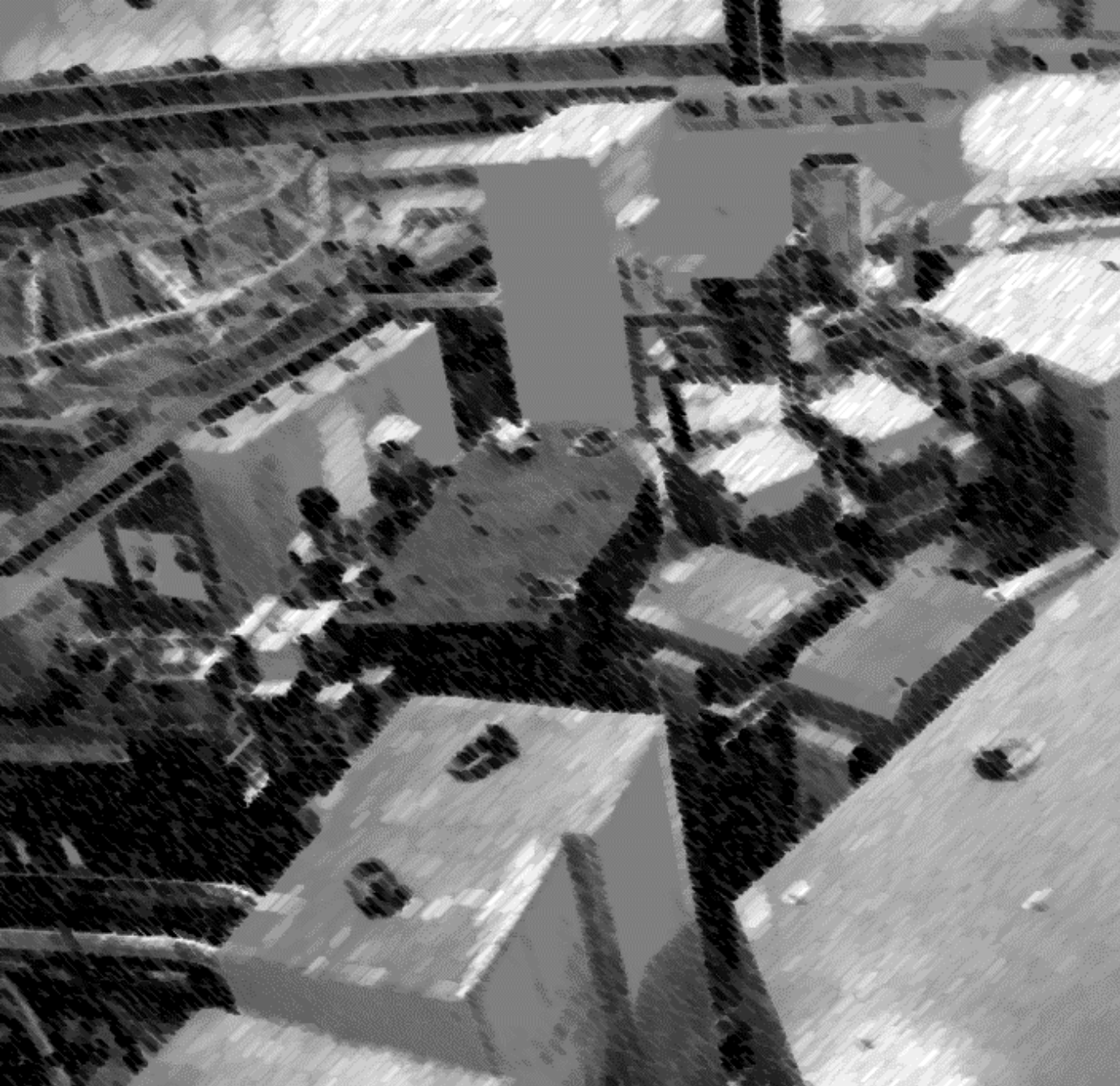
JLab (HES-HKS, 0.6 MeV FWHM, 0.07 MeV accuracy, 2027—)

- ◇ $(e, e'K^+)$ reaction at $\omega = 1.5$ GeV
- ◇ Approved: ${}^3_{\Lambda}\text{H}$, ${}^4_{\Lambda}\text{H}$, ${}^6_{\Lambda}\text{He}$, ${}^9_{\Lambda}\text{Li}$, ${}^{11}_{\Lambda}\text{Be}$, ${}^{27}_{\Lambda}\text{Mg}$, ${}^{40}_{\Lambda}\text{K}$, ${}^{48}_{\Lambda}\text{K}$, ${}^{208}_{\Lambda}\text{Tl}$
→ $\Lambda\text{N CSB}$, ΛNN , tri-axial deformation

J-PARC (S-2S, 1.0 MeV FWHM, 0.1 MeV accuracy, 2024—)

- ◇ (π^+, K^+) and (K^-, K^+) reactions at $p = 1.05$ and 1.8 GeV/ c
- ◇ Approved: ${}^6_{\Lambda}\text{Li}$, ${}^{10}_{\Lambda}\text{B}$, ${}^{12}_{\Lambda}\text{C}$, ${}^7_{\Xi}\text{H}$, ${}^{12}_{\Xi}\text{Be}$
- ◇ New additional plan: ${}^6_{\Lambda}\text{Li}$, ${}^{11}_{\Lambda}\text{B}$ *etc.*
→ $\Lambda\text{N CSB}$, ΞN interaction

Backup



Hall A

- B. Pandey et al., PRC **105**, L051001 (2022)
- K.N. Suzuki et al., PTEP 2022, 1, 013D01 (2022)
- F. Garibaldi et al., PRC 99, 054309 (2019)
- G. M. Urciuoli et al., PRC 91, 034308 (2015)
- F. Cusanno et al., PRL 103, 202501 (2009)
- G. M. Urciuoli et al., NIMA612, 56—68 (2009)
- M. Iodice et al., PRL 99, 052501 (2007)

Hall C

- TG et al., PRC 103, L041301 (2021)
- TG et al., NIMA 900, 69—83 (2018)
- TG et al., PRC 94, 021302(R) (2016)
- TG et al., PRC 93, 034314 (2016)
- Y. Fujii et al., NIMA795, 351—363 (2015)
- L. Tang et al., PRC 90, 034320 (2014)
- S.N. Nakamura et al., PRL 110, 012502 (2013)
- TG et al., NIMA 729, 816—824 (2013)
- L. Yuan et al., PRC 73, 044607 (2006)
- T. Miyoshi et al., PRL 90, 232502 (2003)

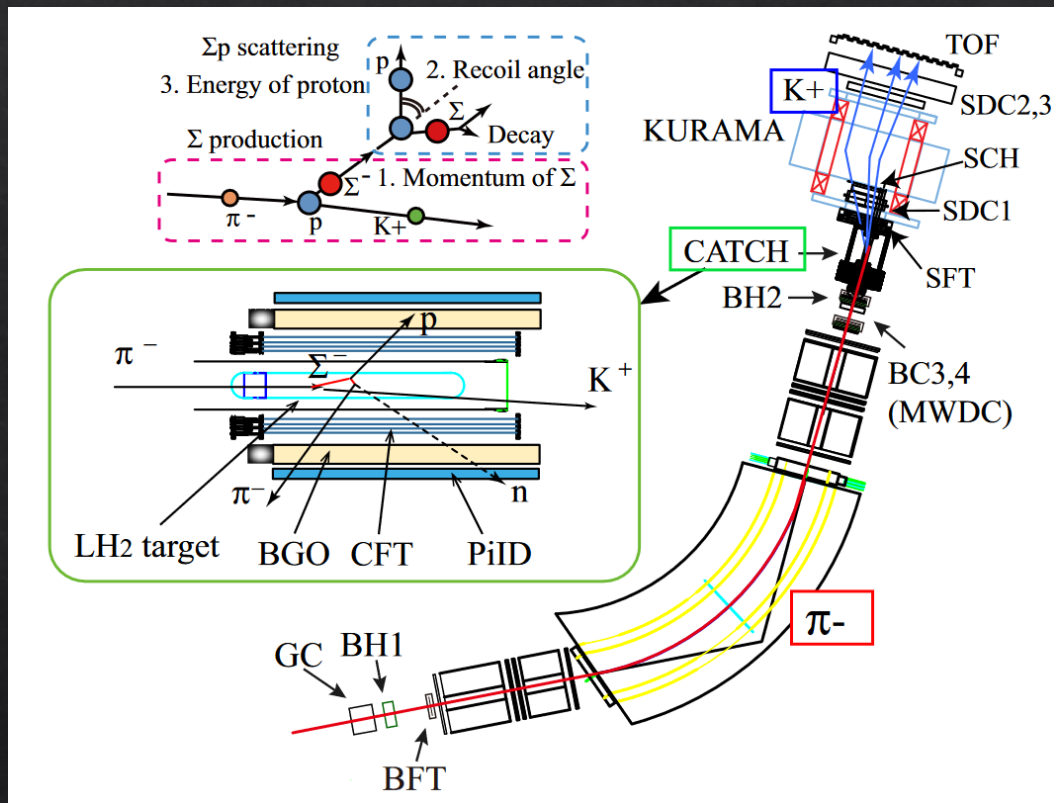
Experimental parameters for the next JLab Experiment

TABLE II. Summary of the kinematics parameters in the proposed experiment.

Item	Value
Beam (e)	Energy (/GeV) (Required) energy spread and drift 1×10^{-4} (FWHM)
PCS + HES (e')	Central momentum $p_{e'}^{\text{cent.}}$ [/(GeV/c)] Central angle $\theta_{ee'}^{\text{cent.}}$ Solid angle acceptance $\Omega_{e'}$ (/msr) (at $p_{e'}^{\text{cent.}}$) Momentum resolution $\Delta p_{e'}/p_{e'}$ 0.74 8.5° 3.4 4.4×10^{-4} (FWHM)
PCS + HKS (K^+)	Central momentum $p_{K^+}^{\text{cent.}}$ [/(GeV/c)] Central angle $\theta_{eK^+}^{\text{cent.}}$ Solid angle acceptance Ω_{K^+} (/msr) (at $p_{K^+}^{\text{cent.}}$) Momentum resolution $\Delta p_{K^+}/p_{K^+}$ 1.20 11.5° 7.0 2.9×10^{-4} (FWHM)
$p(e, e' K^+) \Lambda$	$\sqrt{s} = W$ (/GeV) Q^2 [/(GeV/c) ²] K^+ scattering angle wrt virtual photon, $\theta_{\gamma^* K^+}$ ϵ ϵ_L 1.912 0.036 7.35° 0.59 0.0096

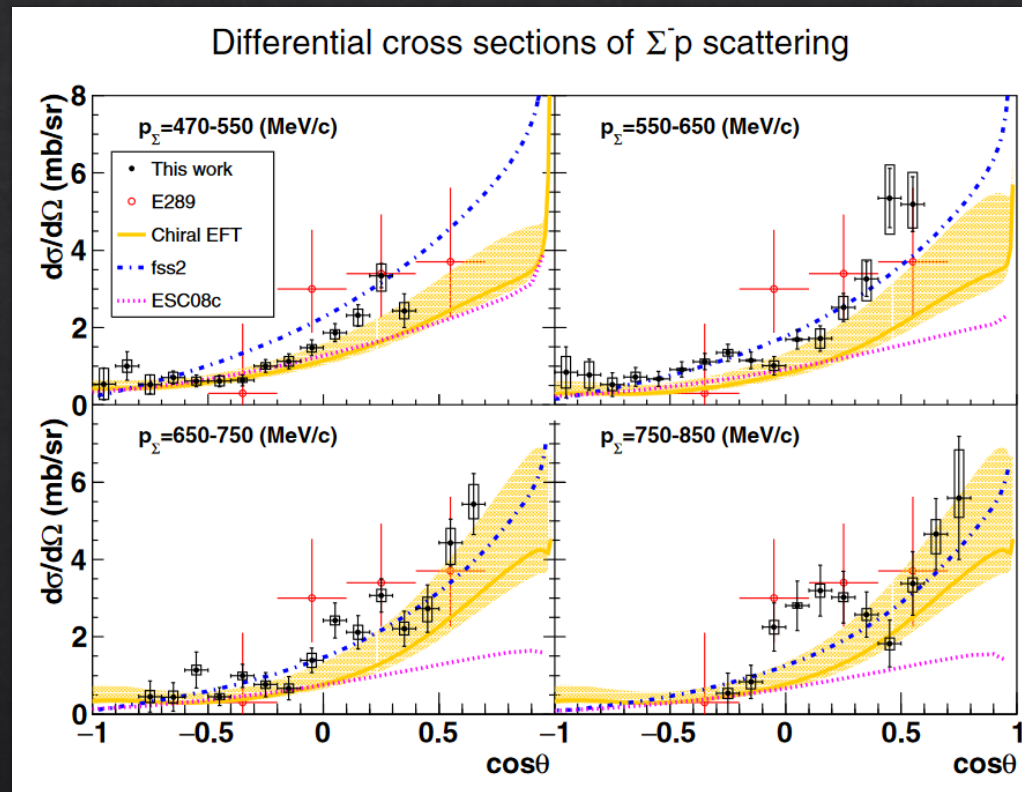
Recent progress in ΥN scattering experiment

K. Miwa et al., PRC 104, 045204 (2021)



J-PARC E40 Experiment

$\Sigma^- p$ elastic



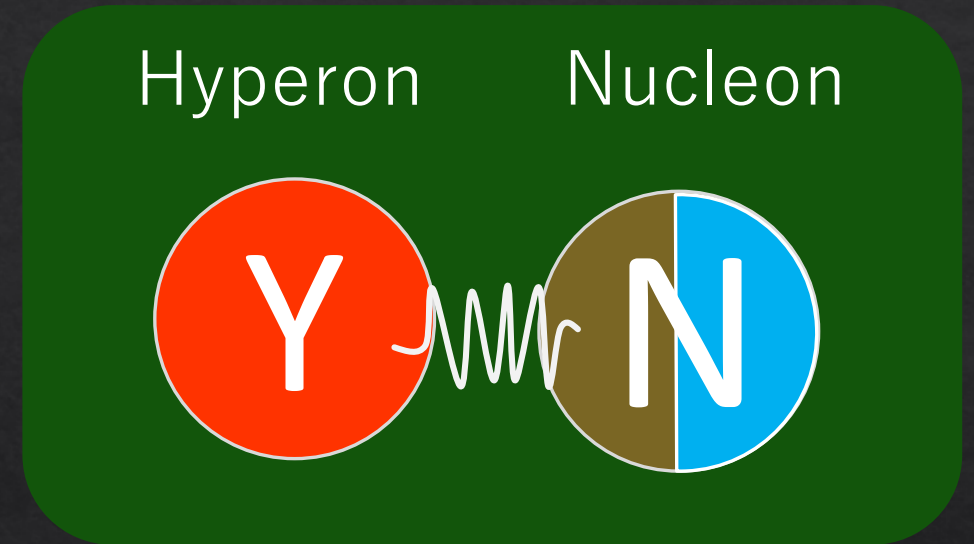
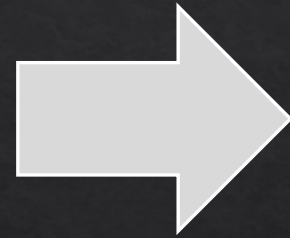
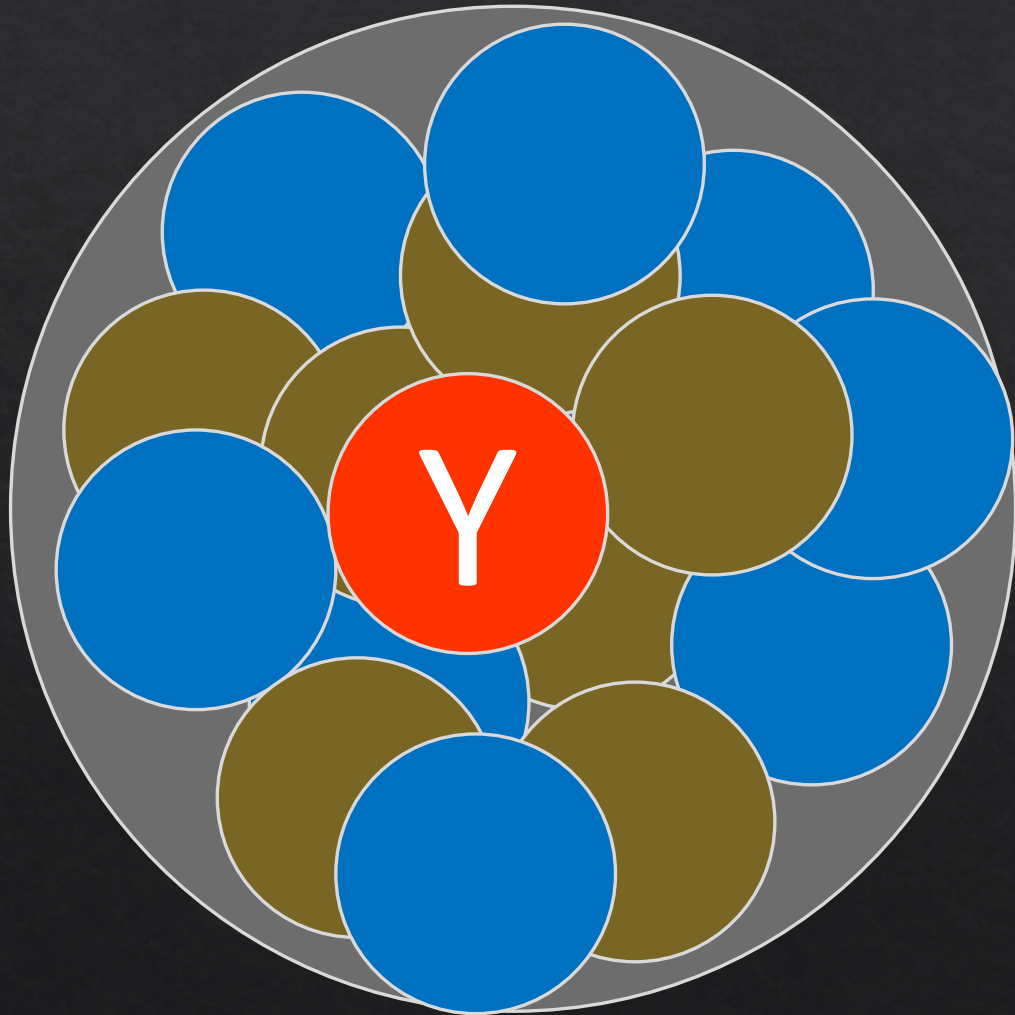
$\Sigma^- p \rightarrow \Lambda n$: K. Miwa et al., Phys. Rev. Lett. 128, 072501 (2022)

$\Sigma^+ p$: T. Nanamura et al., [arXiv:2203.08393](https://arxiv.org/abs/2203.08393) [nucl-ex] (2022)

Λp : J. W. Price et al., AIP Conf. Proc. 2130, 020004 (2019)

Λp : K. Miwa et al., Proposal to J-PARC, P86 (2021)

Hypernuclei \rightarrow YN/YY interactions



Hypernuclear spectroscopy has been playing the most important role for the YN/YY-interaction study

Hyperons in the nature

Hypernuclear
research

- Internal structure

Microscopic



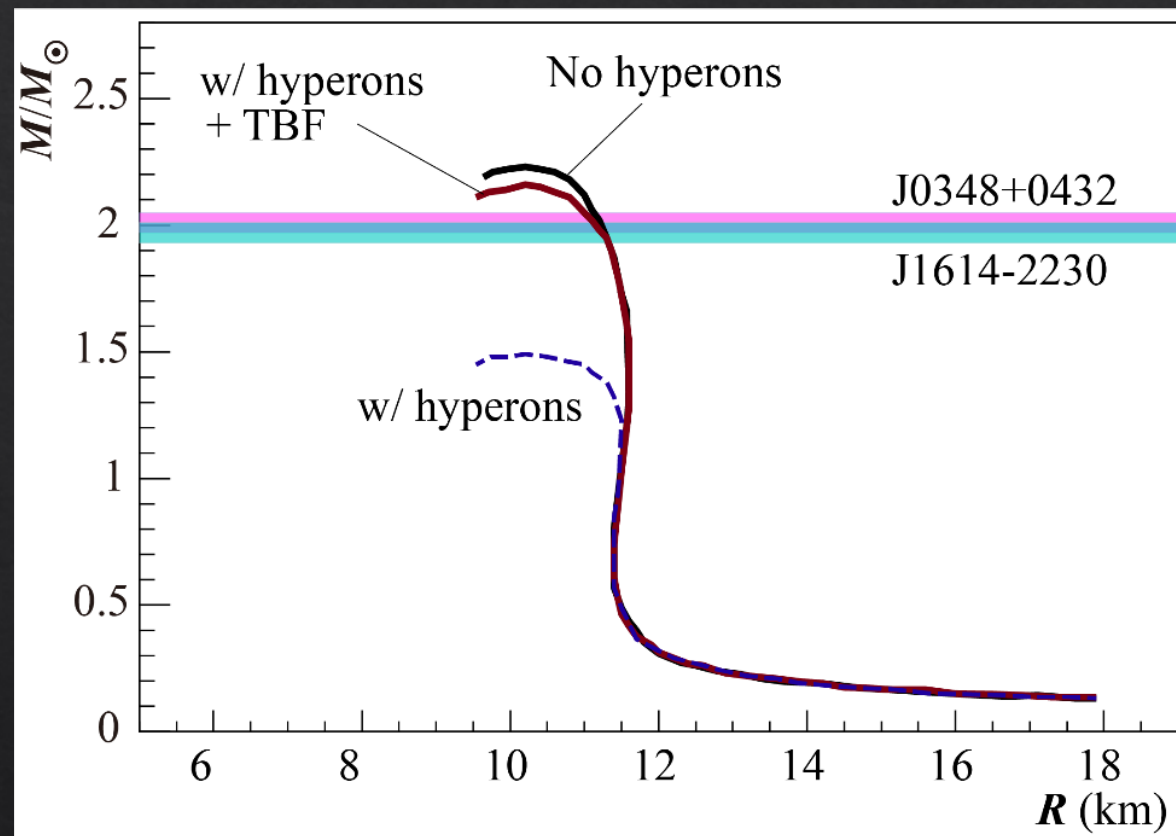
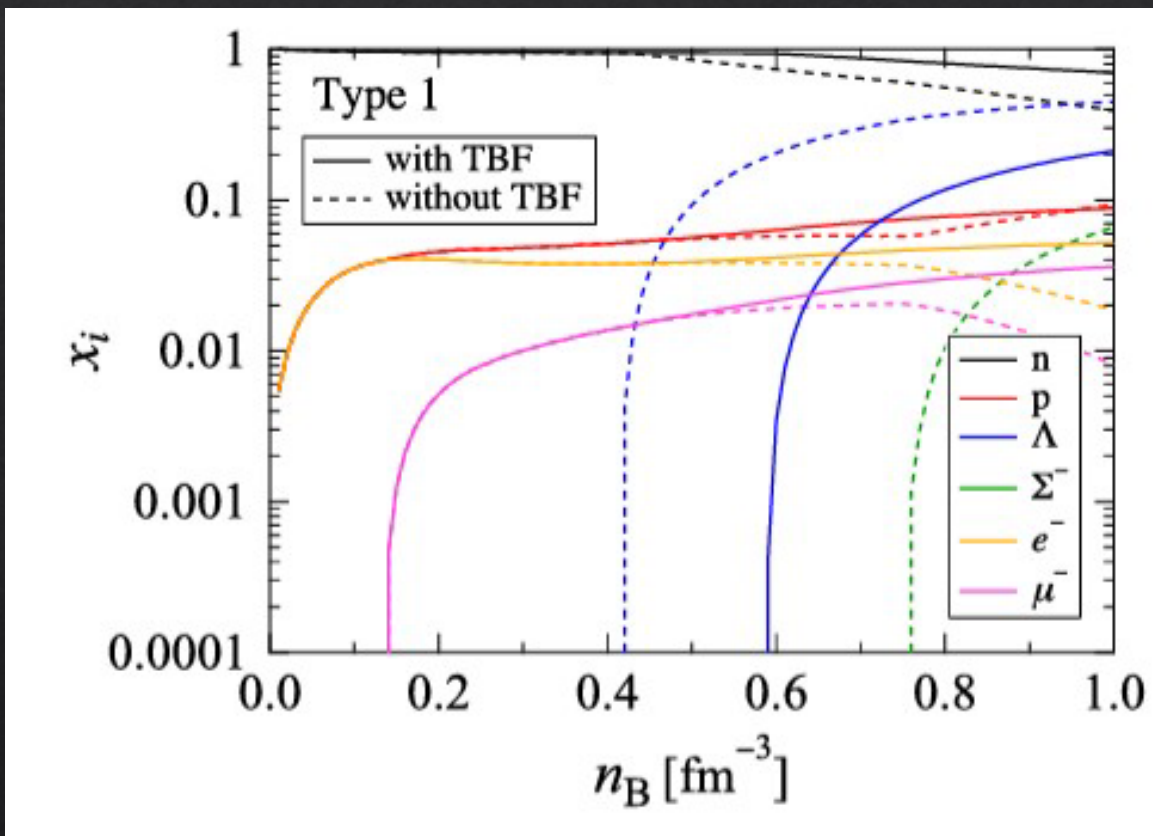
- Cosmological observation
- Gravitational wave measurement

- Mass, radius etc.

Macroscopic

Hyperon puzzle for neutron stars

H. Togashi *et al.*, Phys. Rev. C 93, 035808 (2016)

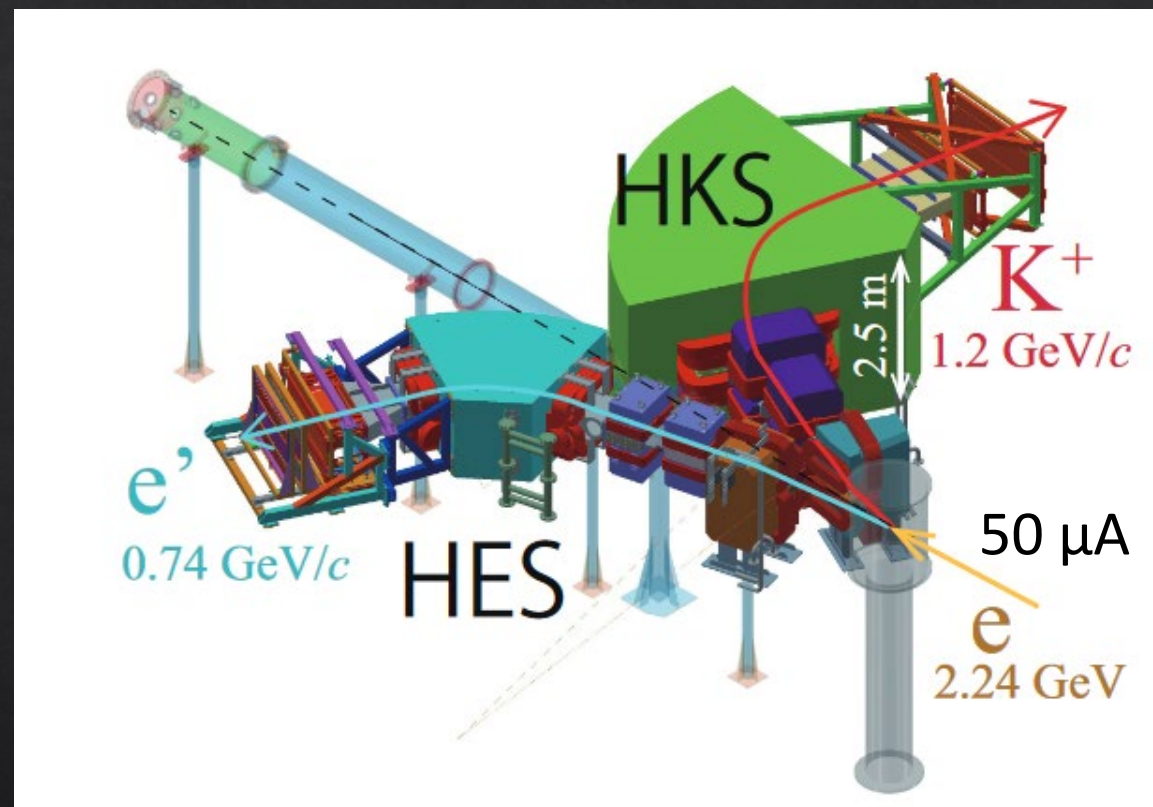


Multi-body force plays an important role
→ JLab E12-15-008, E12-20-013

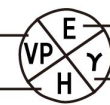
Next experiment at JLab Hall C (FY2026~)



Steven Lassiter & Bert Metzger, JLab Hypernuclear Collaboration Meeting 2022, online, Dec 2022, https://wiki.jlab.org/tegwiki/index.php/Hypernuclear_CollaborationMeeting_2022Dec



Schematic from LOI12-23-013 (TG et al., Lol to PAC51): https://researchmap.jp/gogami/published_papers/42361620/attachment_file.pdf



Hypernucleus		CSB study					
		T<0	T=0	T>0	Now	New JLab	J-PARC
s-shell	$d N \Lambda$ (0^+)	${}^4_\Lambda\text{H}$		${}^4_\Lambda\text{He}$			
	$d N \Lambda$ (1^+)	${}^4_\Lambda\text{H}$ <i>new</i>		${}^4_\Lambda\text{He}$			
p-shell	$\alpha N \Lambda$	${}^6_\Lambda\text{He}$ <i>new</i>		${}^6_\Lambda\text{Li}$ <i>new</i>			
	$\alpha NN \Lambda$	${}^7_\Lambda\text{He}$	${}^7_\Lambda\text{Li}^*$	${}^7_\Lambda\text{Be}$			
	$\alpha d N \Lambda$	${}^8_\Lambda\text{Li}$		${}^8_\Lambda\text{Be}$			
	$\alpha d NN \Lambda$	${}^9_\Lambda\text{Li}$ <i>new</i>	${}^9_\Lambda\text{Be}$	${}^9_\Lambda\text{B}$			
	$\alpha \alpha N \Lambda$	${}^{10}_\Lambda\text{Be}$		${}^{10}_\Lambda\text{B}$ <i>new</i>			
	$\alpha \alpha NN \Lambda$	${}^{11}_\Lambda\text{Be}$ <i>new</i>	${}^{11}_\Lambda\text{B}$ <i>new</i>	${}^{11}_\Lambda\text{C}$			
	$\alpha \alpha d N \Lambda$	${}^{12}_\Lambda\text{B}$		${}^{12}_\Lambda\text{C}$ <i>new</i>			

Isospin multiplet for CSB study

		T < 0		T = 0		CSB study		
		E12-19-002				Now	New JLab	J-PARC
s-shell	(0 ⁺)	${}^4\text{He}$	${}^4_{\Lambda}\text{He}$	${}^4\text{He}$	${}^4_{\Lambda}\text{He}$			
	(1 ⁺)	${}^6\text{He}$	${}^6_{\Lambda}\text{He}$ (new)	${}^6\text{Li}$	${}^6_{\Lambda}\text{Li}$ (new)			
p-shell	α N Λ	${}^7\text{He}$	${}^7_{\Lambda}\text{He}$	${}^7\text{Li}^*$	${}^7_{\Lambda}\text{Li}$			
	α NN Λ	${}^8\text{Li}$	${}^8_{\Lambda}\text{Li}$	${}^8\text{Be}$	${}^8_{\Lambda}\text{Be}$			
	α d N Λ	${}^9\text{Li}$	${}^9_{\Lambda}\text{Li}$ (new)	${}^9\text{Be}$	${}^9_{\Lambda}\text{Be}$			
	α d NN Λ	${}^{10}\text{Be}$	${}^{10}_{\Lambda}\text{Be}$	${}^{10}\text{B}$	${}^{10}_{\Lambda}\text{B}$ (new)			
	α α N Λ	${}^{11}\text{Be}$	${}^{11}_{\Lambda}\text{Be}$ (new)	${}^{11}\text{B}$	${}^{11}_{\Lambda}\text{B}$ (new)			
	α α NN Λ	${}^{12}\text{B}$	${}^{12}_{\Lambda}\text{B}$	${}^{12}\text{C}$	${}^{12}_{\Lambda}\text{C}$ (new)			
	α α d N Λ	${}^{13}\text{C}$	${}^{13}_{\Lambda}\text{C}$	${}^{13}\text{N}$	${}^{13}_{\Lambda}\text{N}$			

LOI12-23-013

E12-19-002

Proposing

Proposing

E94

E94

Isospin multiplet for CSB study

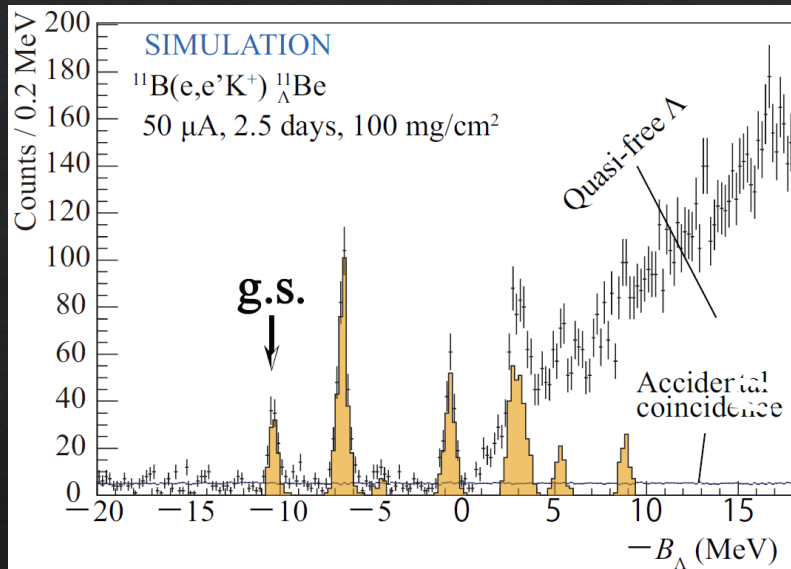
To "complete"

High resolution spectroscopy at J-PARC and JLab

$^{11}_{\Lambda}\text{Be}$



LOI12-23-013



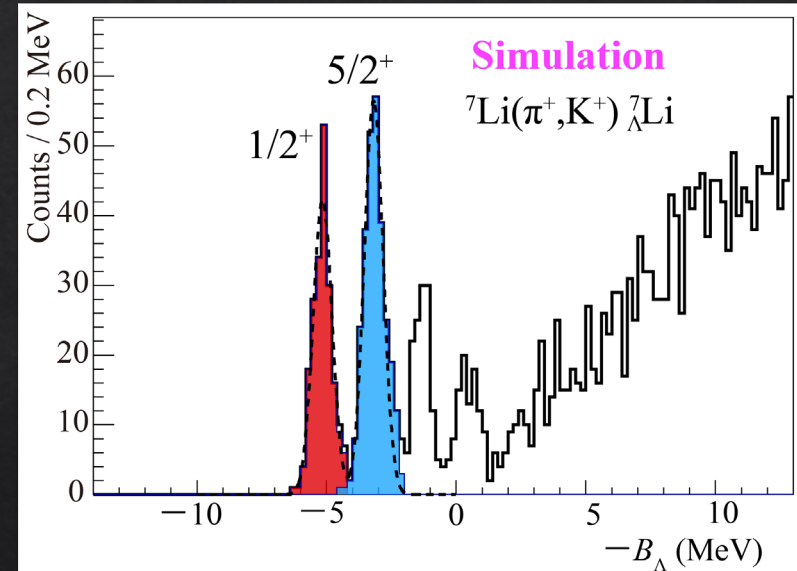
0.6 MeV (FWHM)

09

$^7_{\Lambda}\text{Li}$



E94



1 MeV (FWHM)

08

Hypernuclear Study at JLab

Λ hypernuclear spectroscopy

- ◇ Baryon interaction (YN, YNN)

JLab Hypernuclear Collaboration

- ◇ $(e, e'K^+)$ reaction \rightarrow High resolution/accuracy spectroscopy
- ◇ The method was established at JLab
- ◇ Future experiment (${}^3_{\Lambda}\text{H}$, ${}^4_{\Lambda}\text{H}$, ${}^6_{\Lambda}\text{He}$, ${}^{11}_{\Lambda}\text{Be}$, ${}^{27}_{\Lambda}\text{Mg}$, ${}^{40}_{\Lambda}\text{K}$, ${}^{48}_{\Lambda}\text{K}$, ${}^{208}_{\Lambda}\text{Tl}$)
 - ◇ hypertriton puzzle (binding energy vs. lifetime)
 - ◇ Charge symmetry breaking
 - ◇ Deformation
 - ◇ $\Lambda\text{N}-\Sigma\text{N}$ coupling
 - ◇ iso-spin dependence of ΛNN force

Mar 3, 2023

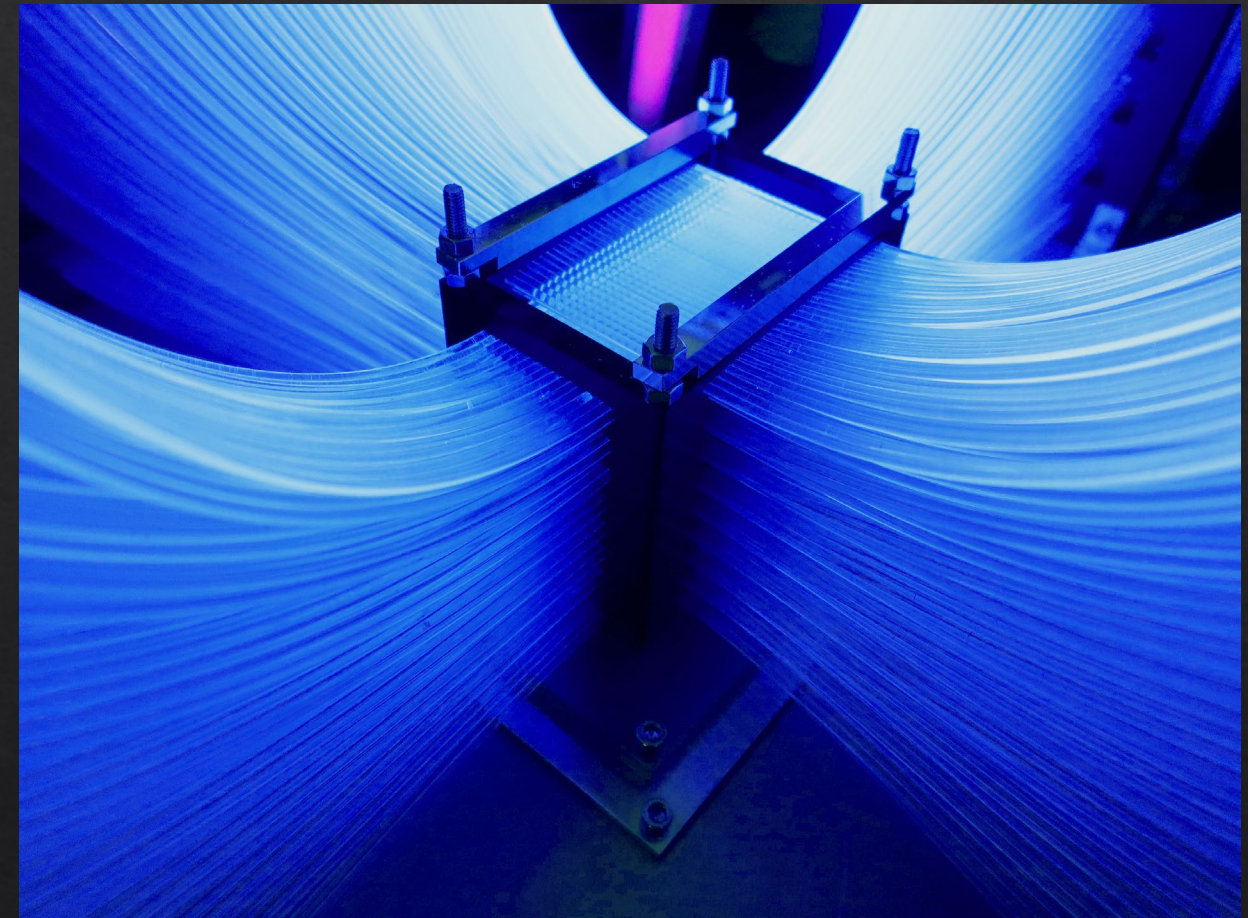
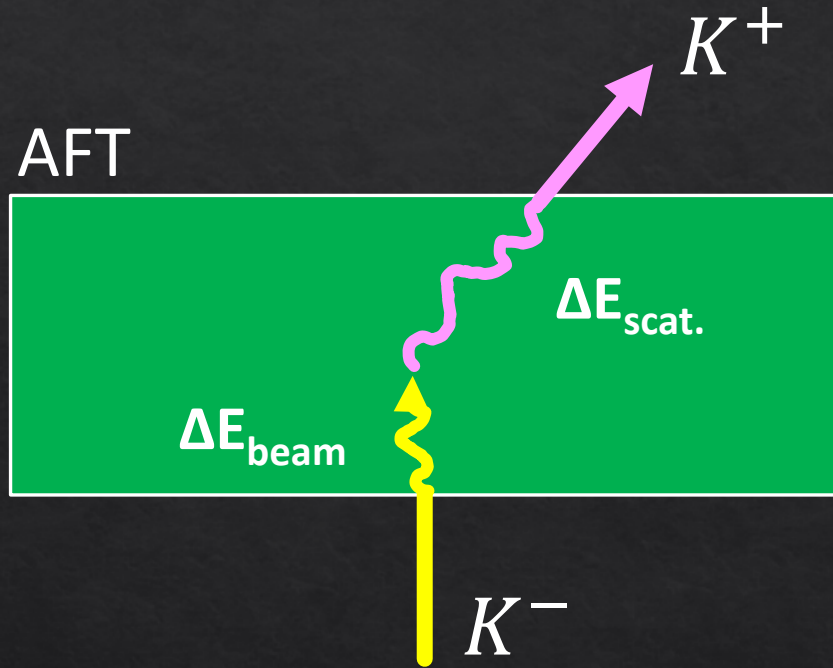
Hypernuclear Physics Workshop:

<https://indico.jlab.org/event/685/>



Direct measurement of energy loss in target

T. K. Harada, *EPJ Web Conf.* 271 (2022) 03006



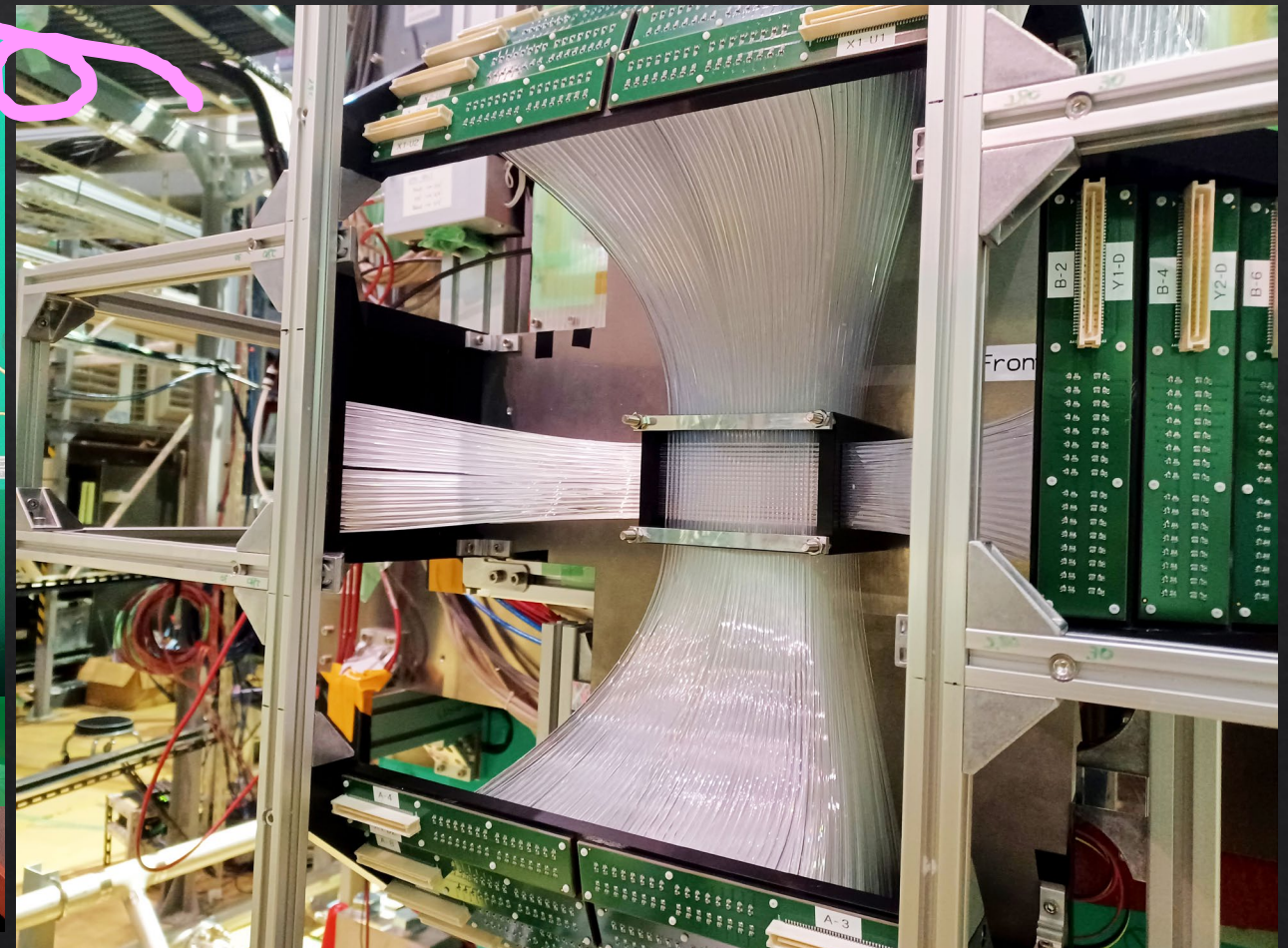
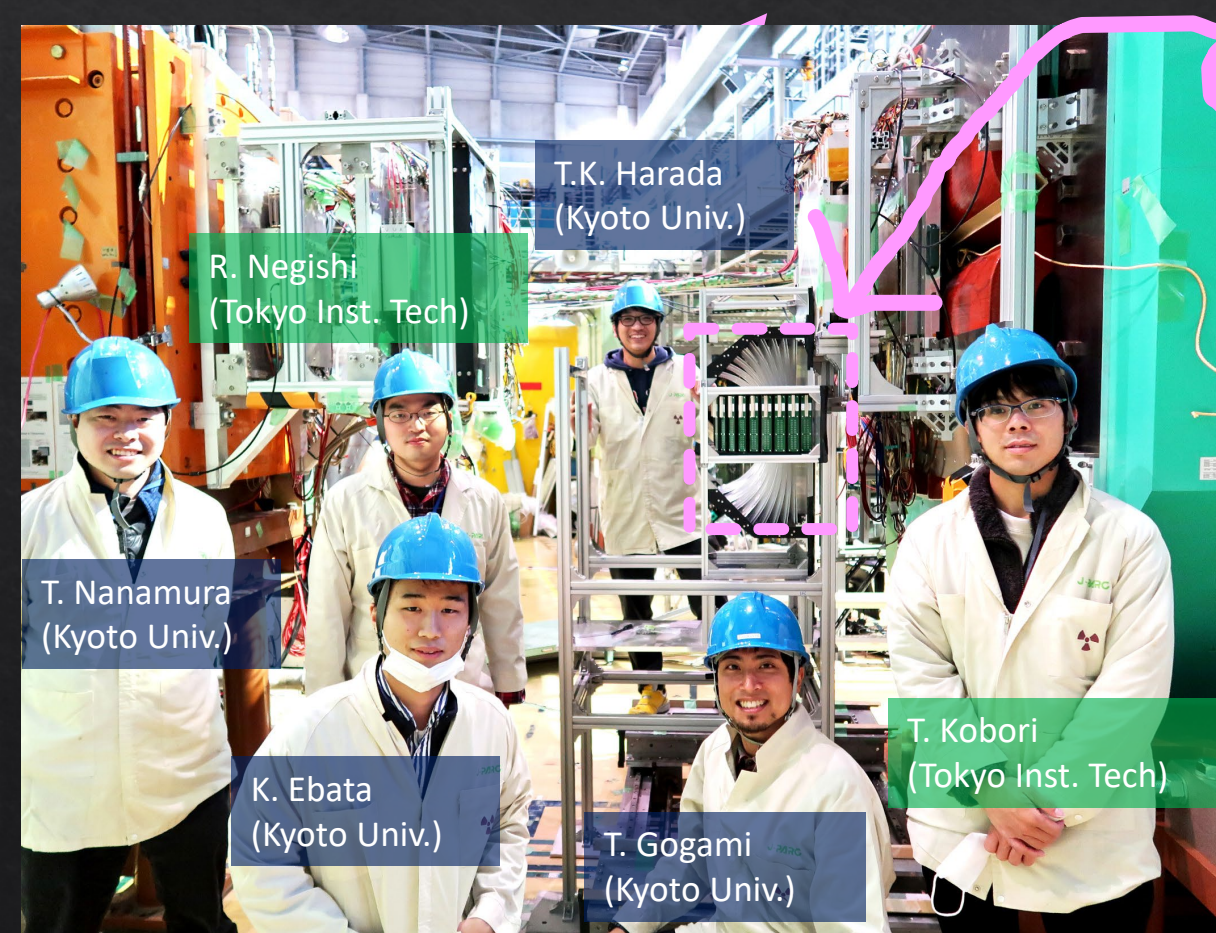
Thick target ...

→ But, high resolution!!

~900-ch of scintillation fibers (CH)

Direct measurement of energy loss in target

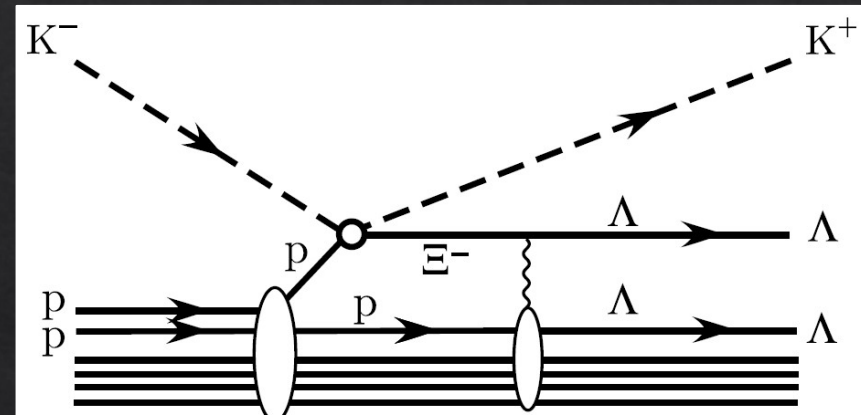
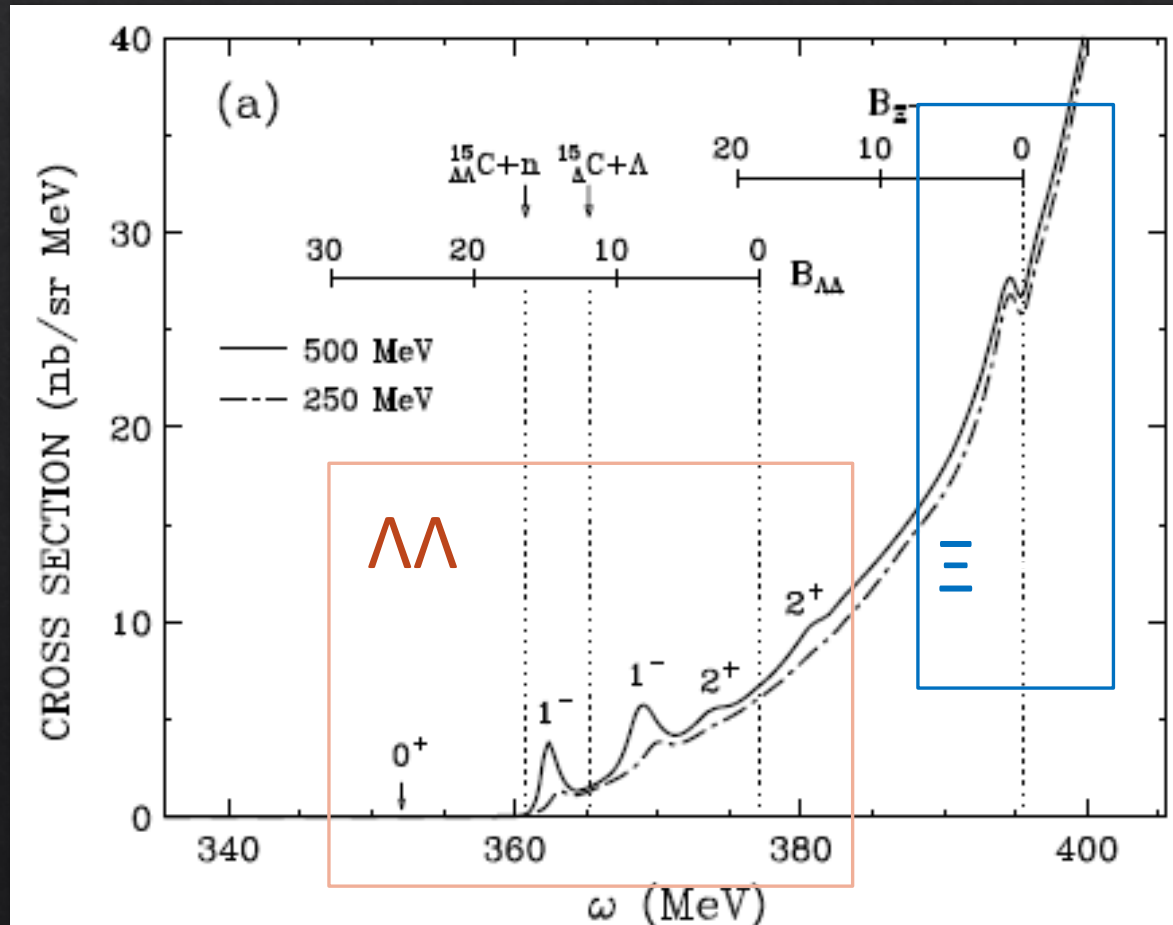
T. K. Harada, EPJ Web Conf. 271 (2022) 03006



(Feb 16, 2023)

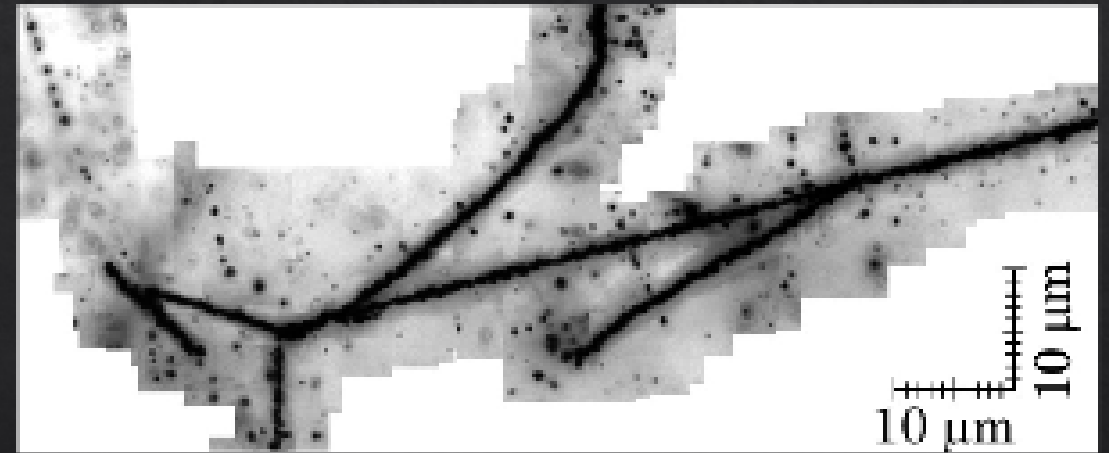
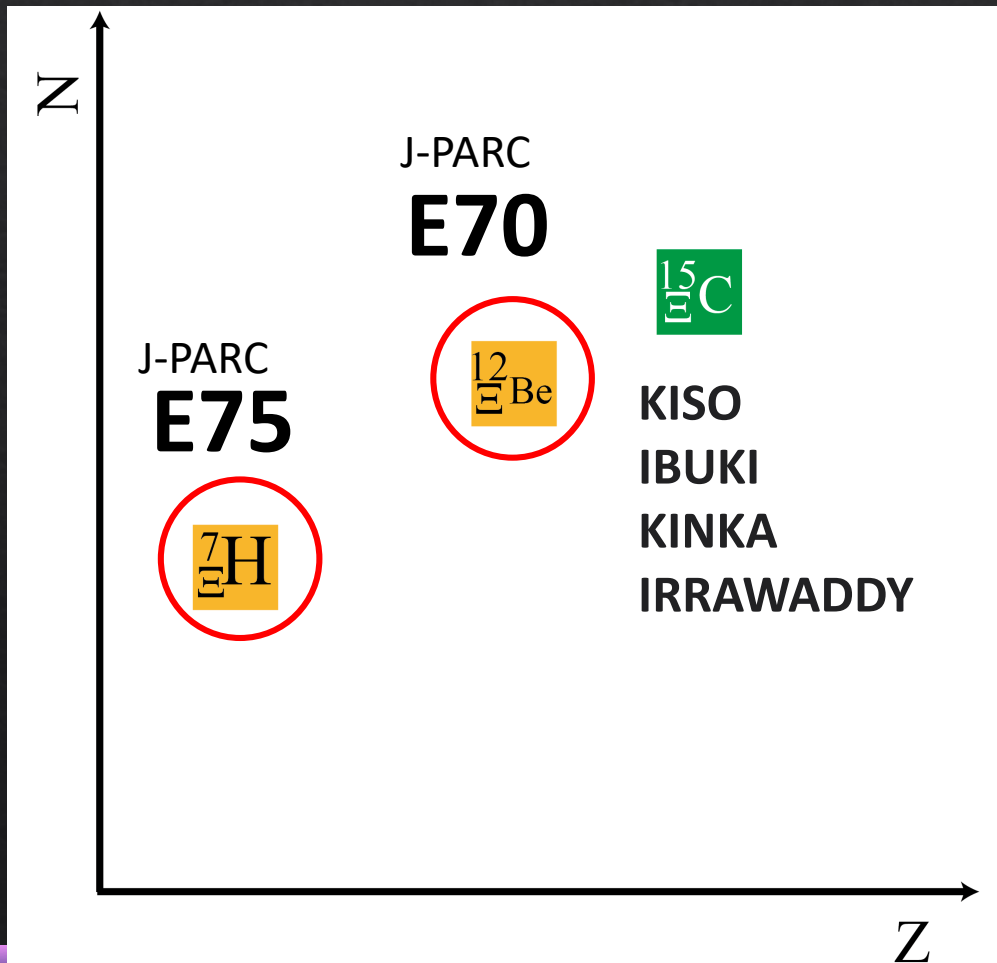
Energy spectrum with the (K^-, K^+) reaction

T. Harada, Y. Hirabayashi, A. Umeya, NPA 914, 85—90 (2013)



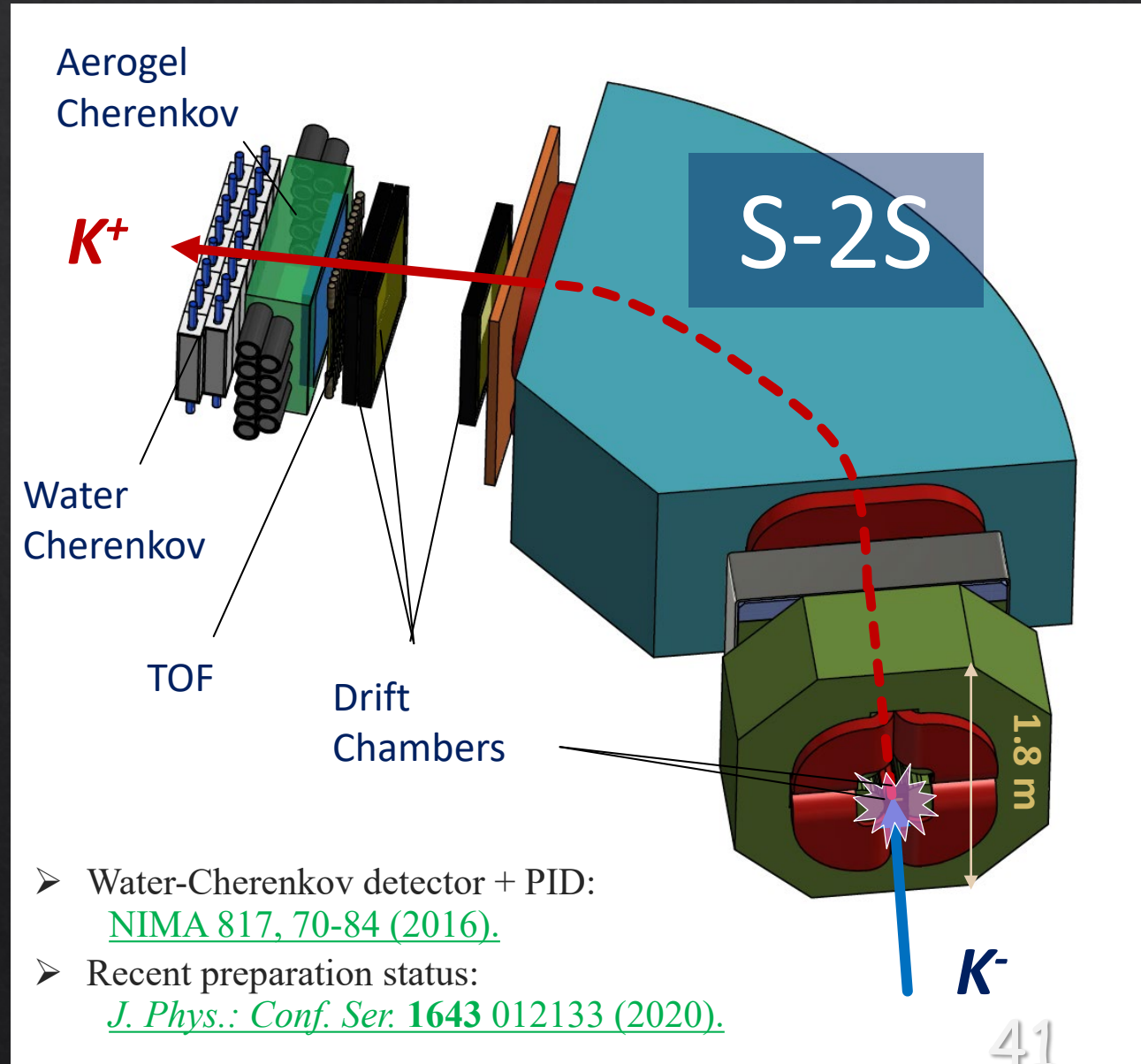
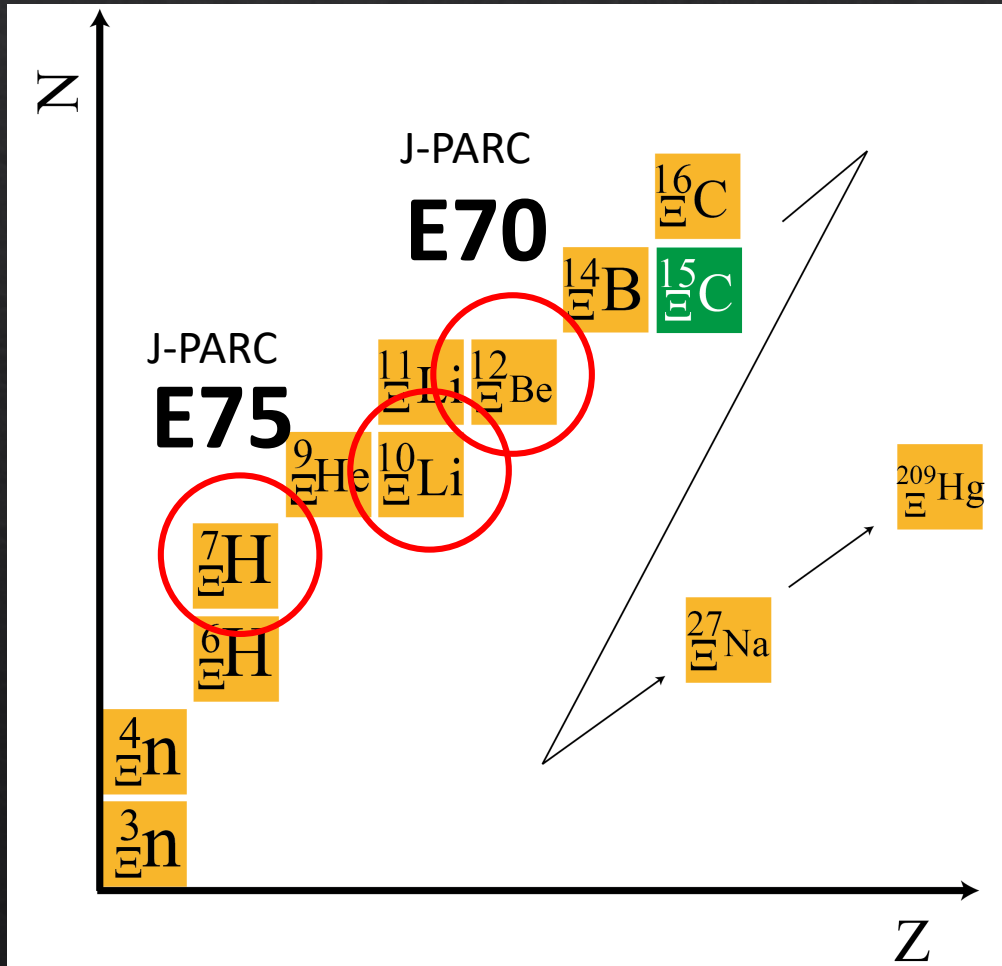
$\Lambda\Lambda$ hypernuclei may be observed

Hypernuclear chart ($S = -2$ floor)



- K. Nakazawa et al., PTEP 2015, 033D02 (2015)
- M. Yoshimoto et al., PTEP 2021, 073D02 (2021)
- S. Hayakawa et al., PRL 126, 062501 (2021)

Hypernuclear chart ($S = -2$ floor)



Some References

J-PARC

- Resent results : <https://j-parc.jp/c/press-release/2022/09/05001005.html>
- Future projects : <https://doi.org/10.1051/epjconf/202227111002>

JLab

- Resent results (nn Λ search experiment) :
 - <https://doi.org/10.1051/epjconf/202227102002>
 - <https://www.kyoto-u.ac.jp/ja/research-news/2022-03-08>
- Future projects : <https://doi.org/10.1051/epjconf/202227101001>

Complication of Ξ hypernuclear structures

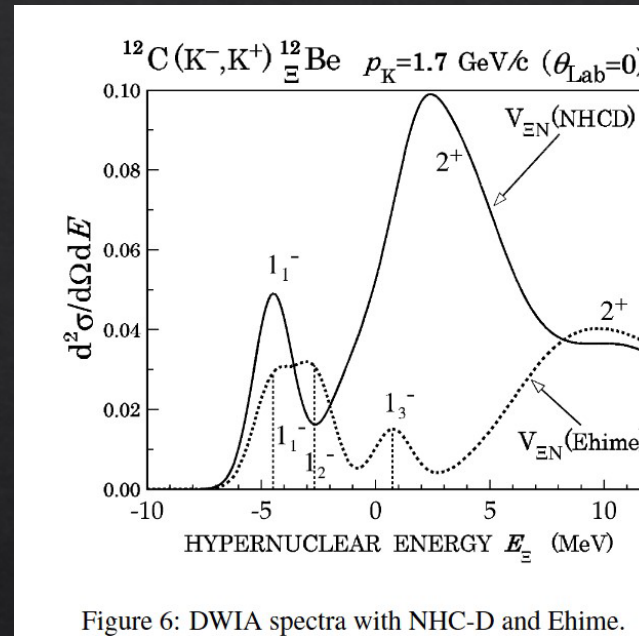
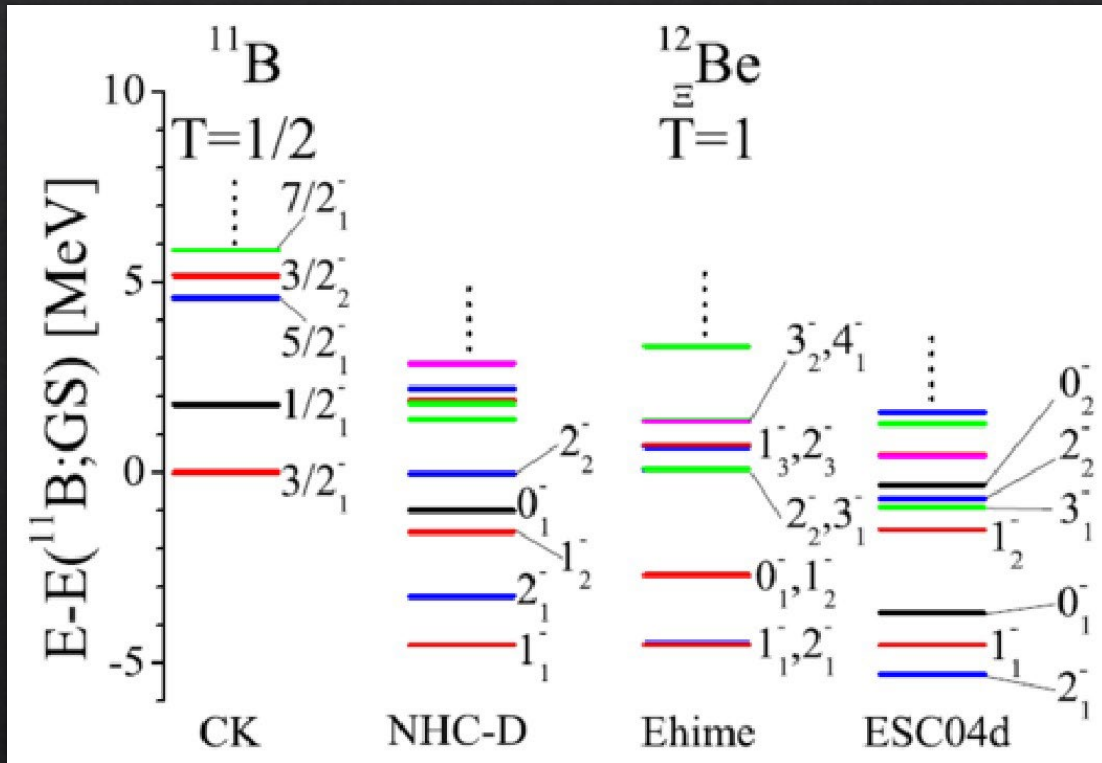


Figure 6: DWIA spectra with NHC-D and Ehime.

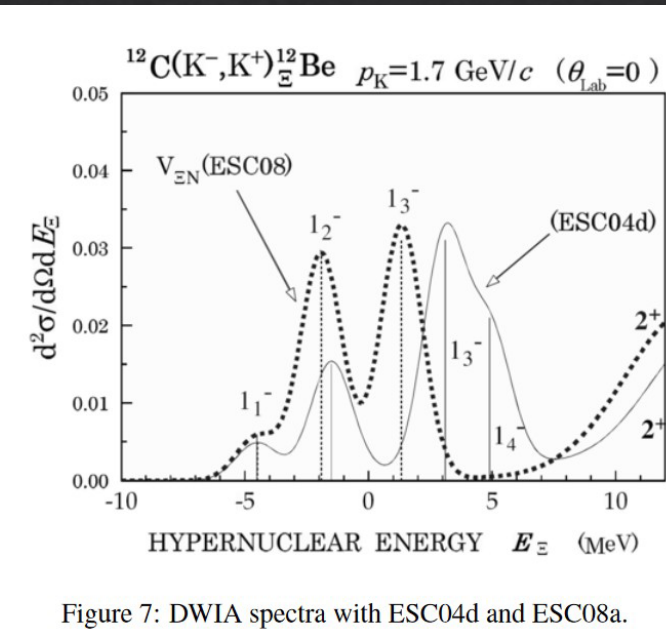
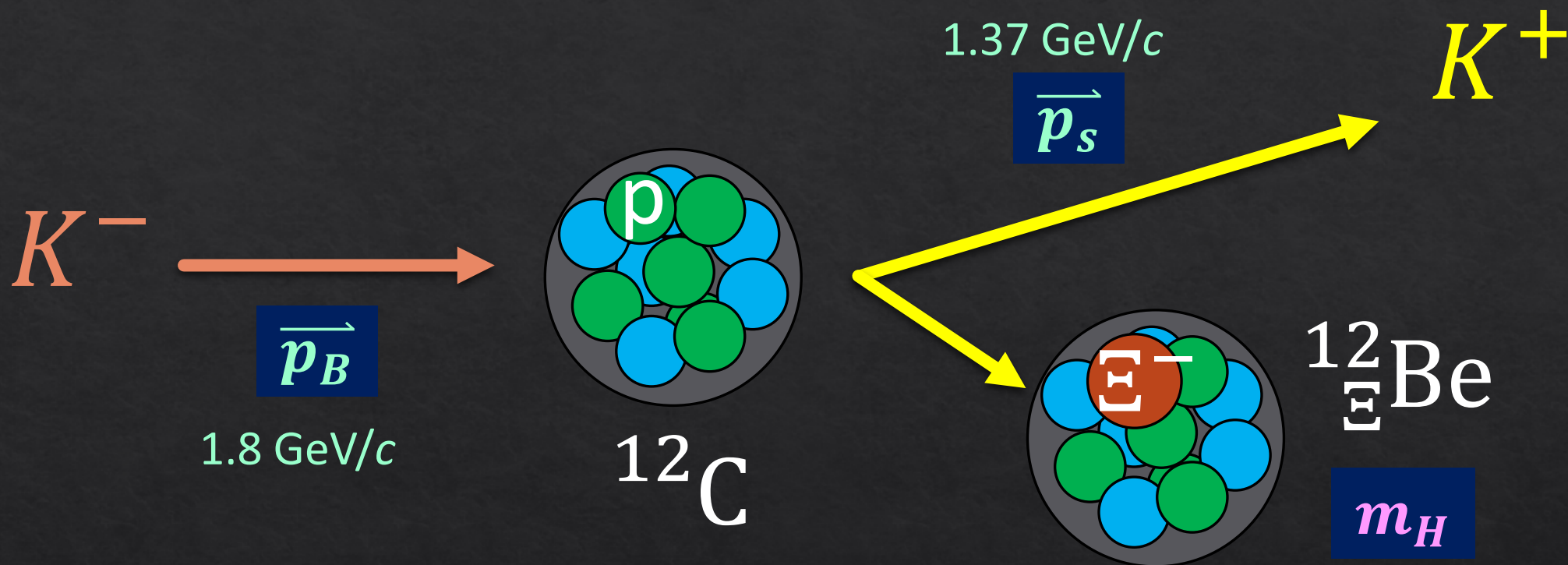


Figure 7: DWIA spectra with ESC04d and ESC08a.

T. Motoba and S. Sugimoto, *NPA* **835** (2010) 223-230

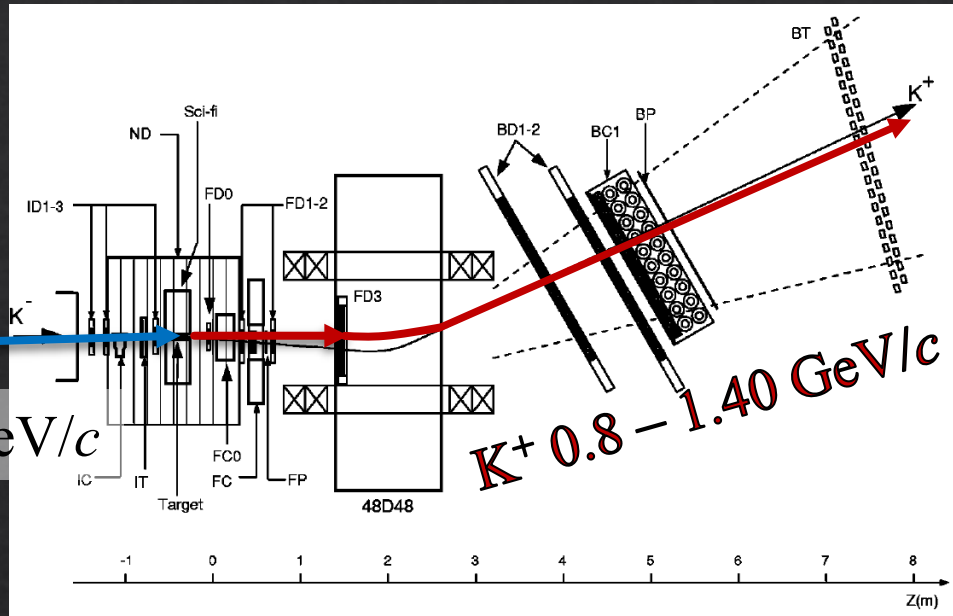
Missing mass spectroscopy with the (K^-, K^+) reaction



$$m_H = \sqrt{E_H^2 - \vec{p}_H^2} = \sqrt{(E_{\text{beam}} + M_t - E_s)^2 - (\vec{p}_B - \vec{p}_s)^2}$$

$$\rightarrow B_{\Xi} = (m_{\text{core}} + m_{\Xi}) - m_H$$

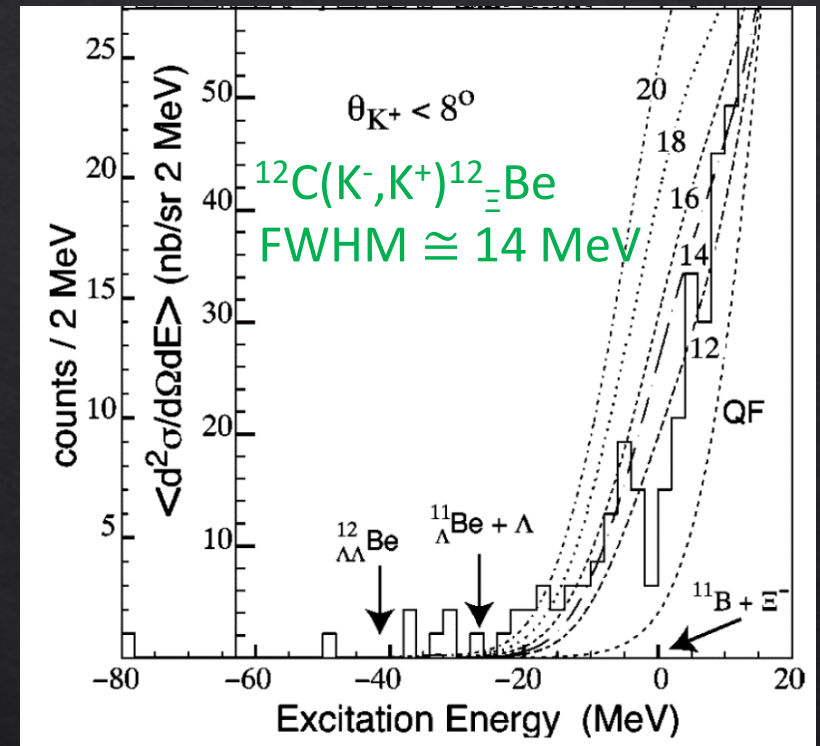
$^{12}\text{C}(K^-, K^+)^{12}_{\Xi}\text{Be} \leftarrow$ Missing-mass measurement



K^- 1.8 GeV/c

K^+ 0.8 - 1.40 GeV/c

P. Khaustov et al., PRC 61 (2000) 054603



Experiment	KEK E224	BNL E885	J-PARC E05
Resolution in FWHM (MeV)	22	14	8

→ 2 MeV in J-PARC E70

→ $V_{0\Xi} \leq 14 \text{ MeV}$

c.f.)

M. Kohno et al., PTP123, 1 (2010)

M. Kohno, PRC 100, 024313 (2019)

Assumption for $^{12}_{\Lambda}\text{C}$ production

$$\underline{^{12}\text{C}(\pi^+, K^+) ^{12}_{\Lambda}\text{C} @ p_{\pi} = 1.64 \text{ GeV}/c}$$

- ◇ Total efficiency = 0.5
- ◇ K survival ratio = 0.46
- ◇ Cross section = 1 $\mu\text{b}/\text{sr}$
- ◇ Solid angle = 55 msr
- ◇ Target thickness = 2 g/cm^2
- ◇ Beam = 3 M pion per spill (spill cycle of 4.2 sec)
- ◇ 5 days
- ◇ S-2S momentum setting is the same as that for the Ξ production

 **391 counts**

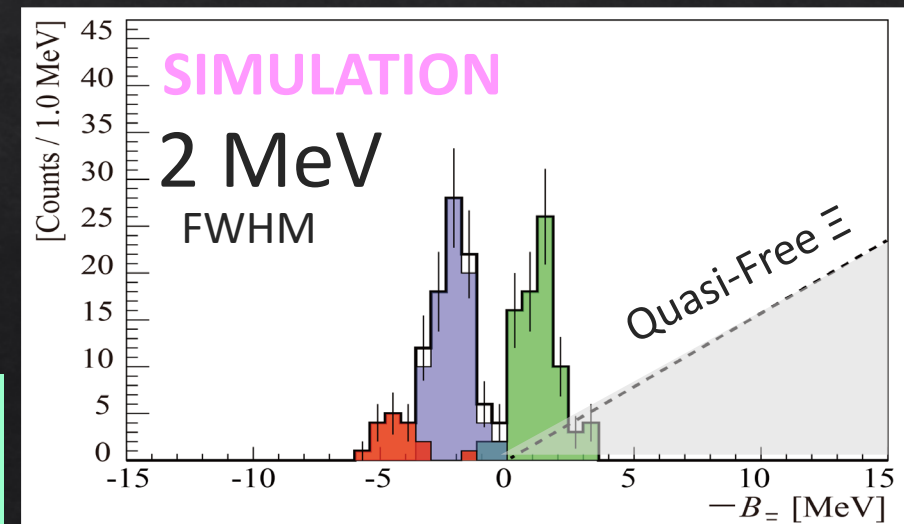
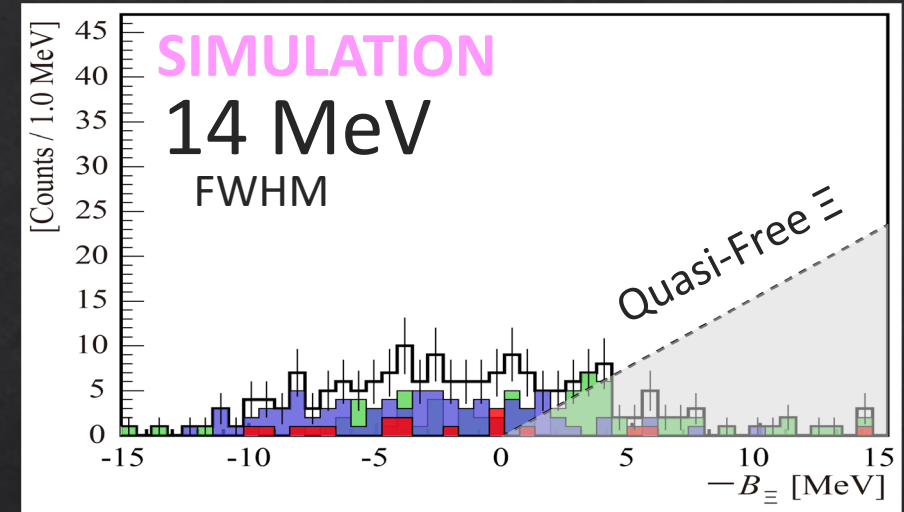
Expected spectrum for the $^{12}_{\Xi}\text{Be}$ production

$$\underline{^{12}\text{C}(K^-, K^+) ^{12}_{\Xi}\text{Be @ } p_{\pi} = 1.8 \text{ GeV}/c}$$

- ◇ Total efficiency = 0.5
- ◇ K survival ratio = 0.46 (8 m optical length)
- ◇ Solid angle = 60 msr
- ◇ Cross section = 60 nb/sr (0—10 deg)
- ◇ Target thickness = 9 g/cm² (AFT made of CH)
- ◇ Beam = 0.8 M kaon per spill (spill cycle of 4.2 sec)
- ◇ 20 days

 **~100 counts**

S-2S



Theory (Interaction) LQCD etc.

M.M. Nagels, Th. A. Rijken, Y. Yamamoto, PRC 102, 054003 (2020)

	ESC16	A1	A2	B1	B2	HAL-QCD
X_2	0.0	2.85	2.55	1.65	1.07	
X_3	0.0	0.0	1.6	0.0	3.0	
X_s	0.0	0.0	0.0	10.	10.	
$^{11}S_0$	2.1	1.4	1.4	-4.0	-4.0	-4.9
$^{13}S_1$	-0.4	-2.2	-2.2	-2.8	-2.8	-2.2
$^{11}P_1$	-0.2	-0.3	-0.3	-0.3	-0.3	
$^{13}P_0$	-5.3	-3.5	-3.5	-2.0	-2.0	
$^{13}P_1$	1.5	1.3	1.3	1.7	1.7	
$^{13}P_2$	-1.2	-1.2	-1.2	-2.3	-2.3	
$^{31}S_0$	9.2	9.9	9.9	6.8	6.8	1.8
$^{33}S_1$	7.6	-13.5	-13.9	-4.7	-4.9	-5.4
$^{31}P_1$	1.0	1.3	1.3	1.0	1.0	
$^{33}P_0$	0.8	1.0	1.0	0.8	0.7	
$^{33}P_1$	-2.0	-2.8	-2.8	-3.0	-3.0	
$^{33}P_2$	0.5	0.1	0.1	-1.0	-1.0	
U_{Ξ}	+13.7	-8.5	-9.0	-10.1	-10.4	-10.6
Γ_{Ξ}^c	5.1	5.7	5.7	0.5	0.5	0.2

Calc.	$^{12}\text{C} + \Xi^-$	$^{14}\text{N} + \Xi^-$	$^{27}\text{Al} + \Xi^-$
	$B_{\Xi} (\Gamma) [/MeV]$		
ESC16 (A1)	4.8 (2.8)	5.1 (3.3)	9.0 (2.9)
ESC16 (B1)	4.9 (0.2)	5.2 (0.24)	9.2 (0.22)
HAL-QCD	4.4 (0.13)	5.5 (0.16)	9.6 (0.12)

→ The **width** is important to be measured as well as the **energy**

K. Sasaki et al., NPA 998, 121737 (2020)

The lightest Ξ hypernuclei

Hypernuclei	chEFT (NLO)	HAL QCD	ESC08c
	$B_{\Xi} (\Gamma)$ [MeV]		
${}^4_{\Xi}\text{H} (1^+)$	0.48 (0.74)	0.36 (0.03—0.06)	10.2 (0.89)
${}^4_{\Xi}\text{n} (1^+)$	0.64 (0.11)	Not bound	