ELECTRON AND PROTON SCATTERING ON STABLE AND EXOTIC NUCLEI

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ECT* Workshop: Probing exotic structure of short-lived nuclei by electron scattering - ECT* Trento 16-20 July 2018

WHY ELECTRON SCATTERING ?

powerful tool to investigate nuclear structure and dynamics
 predominantly EM interaction, QED, weak compared with nuclear int.
 BA one-photon exchange approx

OPEA

 \sim

photon can explore the whole target volume

independently vary (w, q): it is possible to map the nuclear response as a function of its excitation energy with a spatial resolution that can be adjusted to the scale of the processes that need to be studied









beyond particle emission threshold: GR collective excitations electric and magnetic giant multipole resonances





 Δ , N^* , nucleon resonances, mesons, deep inelastic scattering......



ELECTRON AND PROTON SCATTERING ON STABLE AND EXOTIC NUCLEI

- E and QE eA scattering:
- detailed information obtained for stable nuclei
- electron scattering can be extended to unstable nuclei
- \cdot understanding the evolution of nuclear properties as a function of N/Z asymmetry
- models tested in comparison with available data applied to isotopic chains
- evolution of nuclear properties with models of proven reliability in stable isotopes will test the ability of the established nuclear theory in the domain of exotic nuclei
- elastic eA (p distrib.) pA scattering (p and n distribution)
- optical potential for elastic pA and QE eA scattering

ELASTIC ELECTRON-NUCLEUS SCATTERING





 $V_{\rm coul}$ DW for electrons: solve partial wave Dirac eq. c.s. still reflects the behavior of the charge proton density distribution

- RMF using a DDME where the couplings between meson and baryon fields are functions of the density
- RMF: nucleus system of Dirac nucleons coupled to the exchange mesons (σ , ω , ρ) and elm field through an effective Lagrangian, whose parameters adjusted to reproduce NM EOS and global properties of spherical closed-shell nuclei
- Open-shell nuclei require unified and self-consistent treatment of MF and pairing correlations: RHB

neutron and proton density distributions



neutron and proton density distributions



neutron and proton density distributions



ELASTIC ELECTRON SCATTERING: DWBA



ELASTIC ELECTRON SCATTERING: DWBA

Ca isotopes





shift toward smaller angles

















$$e + A \Longrightarrow e' + N + (A - 1)$$

1NKO

both e' and N detected (e,e'p) (A-1) discrete eigenstate exclusive (e,e'p) proton-hole states properties of bound protons s.p. aspects of nuclear structure validity and limitation of IPSM nuclear correlations

EXCLUSIVE







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EXCLUSIVE

 $e + A \Longrightarrow e' + N + (A - 1)$

only e' detected

all final states included

discrete and continuum spectrum

less specific information more closely related to the dynamics of initial nuclear g.s.

width of QE peak direct measurement of average mom. of nucleons in nuclei, shape depends on the energy and momentum distribution of the bound nucleons

INCLUSIVE





$$\begin{split} E_{\rm m} &= \omega - \frac{{p'_1}^2}{2m} - \frac{{p_B}^2}{2m(A-1)} = W_B^* - W_A \qquad {\rm rr} \\ \vec{p}_{\rm m} &= \vec{q} - \vec{p'}_1 = -\vec{p}_1 = \vec{p}_B \qquad {\rm mis} \end{split}$$

missing energy

missing momentum

Experimental data: E_m and p_m distributions



Experimental data: E_m and p_m distributions

eigenstate

 $^{16}\mathrm{O}(e,e'p)$ For E_m corresponding 6.32 to a peak we assume that the residual nucleus is in a discrete 15 N g.s. 127 10-30 50-100 INEVICI 100 - 150 150-200 200-250 60 20 40 80 E_m [MeV] Saclay data for ¹⁶O(e,e'p) [Mougey et al., Nucl. Phys. A335, 35 (1980)]



ONE-HOLE SPECTRAL FUNCTION

$S(\vec{p_{1}}, \vec{p_{1}}; E_{m}) = \langle \Psi_{i} | a_{\vec{p_{1}}}^{+} \delta(E_{m} - H) a_{\vec{p_{1}}} | \Psi_{i} \rangle$



joint probability of removing from the target a nucleon p_1 leaving the residual nucleus in a state with energy $E_{\rm m}$



 $\vec{p}_1 = \vec{\bar{p}}_1$

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$$\begin{split} \int S(\vec{p_1}, \vec{p_1}; E_m) dE_m &= \rho(\vec{p_1}, \vec{p_1}) & \text{inclusive reaction : one-body density} \\ \vec{p_1} &= \vec{p_1} & \longrightarrow & \rho(\vec{p_1}, \vec{p_1}) = F(\vec{p_1}) \\ \hline \text{MOMENTUM DISTRIBUTION} \\ F(\vec{p_1}) &= \int |\Psi_i(\vec{p_1}, \vec{p_2}, ..., \vec{p_A}|^2 d\vec{p_2}...d\vec{p_A}) & \text{probability of finding in the target} \\ a \text{ nucleon with momentum } p_1 \end{split}$$



 $\sigma = K L^{\mu\nu} W_{\mu\nu}$



(/(-1)
$$|\Psi_{
m i}
angle$$

 $|\Psi_{
m f}
angle$

$$\sigma = KL^{\mu\nu} W_{\mu\nu}$$





hadron tensor



 $\sigma = K L^{\mu\nu} W_{\mu\nu}$ hadron tensor $W^{\mu\nu} = \overline{\sum_{i,f}} J^{\mu}(\vec{q}) J^{\nu*}(\vec{q}) \delta(E_{i} - E_{f})$ $J^{\mu}(\vec{q}) = \int e^{i\vec{q}\cdot\vec{r}} \langle \Psi_{f} \mid \hat{J}^{\mu}(\vec{r}) \mid \Psi_{i} \rangle d\vec{r}$



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(e,e'p)

- exclusive reaction n
- DKO mechanism: the probe interacts through a one-body current with one nucleon which is then emitted the remaining nucleons are spectators
- impulse approximation IA



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For each E_m the mom. dependence of the SF is given by the mom. distr. of the quasi-hole states n produced in the target nucleus at that energy and described by the normalized OF

The norm of the OF, the spectroscopic factor gives the probability that n is a pure hole state in the target.

IPSM



There are correlations and the strength of the quasi-hole state is fragmented over a set of s.p. states $0 \le \lambda_n \le 1$



Direct knockout DWIA (e,e'p)

$$\lambda_n^{1/2} \langle \chi^{(-)} \mid j^{\mu} \mid \phi_n \rangle$$

- j^µ one-body nuclear current
- $\chi^{(-)}$ s.p. scattering w.f. $H^+(\omega + E_m)$
- ϕ_n s.p. bound state overlap function H(-E_m)
- \bullet λ_n spectroscopic factor
- $\ensuremath{\bullet}$ $\chi^{(\text{-})}$ and ϕ consistently derived as eigenfunctions of a Feshbach optical model Hamiltonian

DWIA-RDWIA calculations

- phenomenological ingredients usually adopted
- $\stackrel{\label{eq:constraint}}{=} \chi^{(-)}$ phenomenological optical potential
- $\stackrel{\text{\tiny $\#$}}{=} \phi_n$ phenomenological s.p. wave functions WS, HF MF (some calculations including correlations are available)
- nonrelativistic (DWIA) relativistic (RDWIA) ingredients
- $\stackrel{\text{\tiny $\rlap{$\stackrel{\atop}{$}$}}{} \lambda_n$ extracted in comparison with data: reduction factor applied to the calculated c.s. to reproduce the magnitude of the experimental c.s.

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DWIA and RDWIA: excellent description of (e,e'p) data

Experimental data: p_m distributions



NIKHEF data & CDWIA calculations

Experimental data: p_m distributions











¹⁶O(e,e'p)









DWIA WS wave function





(ω ,q) const: E₀=483.2 MeV θ =61.52 deg. q=450 MeV/c T_p=100 MeV parallel kin: E₀=483.2 MeV T_p=100 MeV

NIKHEF data G.J. Kramer Ph. D. Thesis (1990)



DWIA WS wave function



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C.Giusti et al. PRC 024615 (2011)







 $\lambda_n = 0.49 \text{ DWIA-WS}$ 0.51 DWIA-HF 0.49 RDWIA

(ω ,q) const kin

parallel kin

 $\lambda_n = 0.65 \text{ DWIA-WS}$ 0.64 DWIA-HF 0.69 RDWIA

 $\lambda_n = 0.56 \text{ DWIA-WS}$ 0.55 DWIA-HF 0.52 RDWIA ^{40,48,52,60}Ca(e,e'p)

DWIA-WS DWIA-HF and RDWIA for Ca isotopes

even-even isotopes, spherical nuclei where the s.p. levels are fully occupied and pairing effects should be minimized





(e,e'p) measurements offer a unique opportunity for studying the dependence of the properties of bound protons on N/Z

DWIA-WS DWIA-HF RDWIA: good and similar description of the available (e,e'p) data on ⁴⁰Ca and ⁴⁸Ca

DWIA-WS DWIA-HF RDWIA: analogous behavior increasing N/Z asymmetry:

the different s.p. bound-state w.f. responsible for only a part of the differences, an important contribution is given also by FSI described in the calculations by phenomenological optical potentials

OP affects the size and the shape of the cross section in a way that strongly depends on kinematics: its dependence on N/Z deserves careful investigation (e,e'p) measurements offer a unique opportunity for studying the dependence of the properties of bound protons on N/Z

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OPTICAL POTENTIAL

- (e,e'p): in DWIA bound and scattering states are eigenfunctions of a non-Hermitian energy-dependent OP and should be obtained from a consistent microscopic manybody calculation
- (e,e'p): in DWIA calculations phenomenological OPs are usually adopted
- * OP describes elastic nucleon-nucleus scattering
- * phenomenological and theoretical OP

OPTICAL POTENTIAL

PHENOMENOLOGICAL: assume a form and a dependence on a number of adjustable parameters for the real and imaginary parts that characterize the shape of the nuclear density distribution and that vary with the nuclear energy and the nucleus mass number.

Parameters obtained through a fit to pA elastic scattering data

THEORETICAL: microscopic calculations require the solution of the full many-body nuclear problem. Some approximations are needed.

We do not expect better description of experimental data but greater predictive power when applied to situations where exp. data not available M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2016) Theoretical optical potential derived from nucleonnucleon chiral potentials

M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2017) Theoretical optical potential derived from nucleonnucleon chiral potentials at N⁴LO

Purpose: study the domain of applicability of microscopic two-body chiral potentials to the construction of an OP Theoretical framework for pA elastic scattering

We start from the full (A+1) body LS equation

 $T = T + VG_0(E)VT$

Separation into two coupled integral equations

 $T = U + G_0(E)PT$ T transition op. for elastic scattering, $U = V + VG_0(E)QU$ U OP

Free propagator

Projection operators

Free Hamiltonian

External interaction

 $G_0(E) = (E - H_0 + i\epsilon)^{-1}$

P+Q=1

 $H_0 = h_0 + H_A$

 $V = \sum_{i=1}^{A} v_{0i}$

The spectator expansion

Consistent framework to calculate U and T



 au_{ijk}

The spectator expansion

Consistent framework to calculate U and T



Impulse Approximation

$$au_i \approx t_{0i}$$

The free NN t matrix

The free two-body propagator

$$t_{0i} = v_{0i} + v_{0i}g_i t_{0i}$$

$$g_i = \frac{1}{E - h_0 - h_i + i\epsilon}$$

$$U = \sum_{i=1}^{A} t_{0i}$$

Impulse Approximation

$$au_i \approx t_{0i}$$

The free NN t matrix

The free two-body propagator

$$t_{0i} = v_{0i} + v_{0i}g_i t_{0i}$$

$$g_i = \frac{1}{E - h_0 - h_i + i\epsilon}$$

$$U = \sum_{i=1}^{A} t_{0i}$$

We have to solve only 2-body equations

Optimum Factorization Approximation

$$\begin{split} U(q,K;\omega) &= \frac{A-1}{A} \, \eta(q,K) \sum_{N=n,p} t_{pN} \begin{bmatrix} q, \frac{A+1}{A}K; \omega \end{bmatrix} \begin{array}{c} \rho_N(q) \\ & \ddots \end{array} \\ \end{split}$$

$$\begin{split} & & \\ & & \\ \hline & & \\ NN \ t-matrix \\ & & \\ NN \ interaction \end{split} \quad \begin{array}{c} n, p \ densities \end{array}$$

$$q=k'-k$$
 $K=\frac{1}{2}(k'+k)$

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n,p densities calculated within the RMF description of spherical nuclei using a DDME model

NN interaction chiral potentials...

CHIRAL POTENTIAL

When the concept of EFT was applied to low-energy QCD, ChPT was developed

Within ChPT it became possible to implement chiral symmetry consistently in a theory of pionic and nuclear interactions

The theory is based on a perturbative expansion in powers of $(Q/\Lambda_{\chi})^n$ where Q is the magnitude of the three-momentum of the external particles or the pion mass and Λ_{χ} is the chiral symmetry breaking scale of the chiral EFT

From the perturbative expansion only a finite number of terms contribute at a given order





E. Epelbaum et al. . PRL 115 122391 (2015), EPJA 51 53 (2015) EKM
D.R. Entem et al. PRC 91 014002 (2015), PRC 96 024004 (2017) EMN

M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2016) Theoretical optical potential derived from nucleonnucleon chiral potentials

order by order convergence: it is mandatory to use chiral potentials at N³LO to describe elastic pA and NN scattering data
M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2017) Theoretical optical potential derived from nucleonnucleon chiral potentials at N⁴LO

Purpose: check the convergence and assess the theoretical errors associated with the truncation of the chiral expansion in the construction of an OP M. Vorabbi, P. Finelli, C. Giusti, PRC 93 034619 (2017) Theoretical optical potential derived from nucleonnucleon chiral potentials at N⁴LO

Purpose: check the convergence and assess the theoretical errors associated with the truncation of the chiral expansion in the construction of an OP

Results: robust convergence has been reached at N⁴LO, agreement with data neither better nor worse than with chiral NN potentials at N³LO

¹⁶O 200 MeV ⁴⁰Ca



M. Vorabbi, P. Finelli, C. Giusti PRC 96 044001 (2017)

investigate and compare predictive power of our microscopic OP and of phenomenological OP in comparison with exp. data in a wider range of nuclei, including isotopic chains

M. Vorabbi, P. Finelli, C. Giusti, arXiv:1806.01037v1 (2018) Proton-Nucleus Elastic Scattering: Comparison between Phenomenological and Microscopic Optical Potentials

Comparison phenomenological and microscopic OP

PHENONOMENOLOGICAL OP

GLOBAL given in a wide range of nuclei and energies

NROP up to ~200 MeV, for higher energies it is generally believed that the Schroedinger picture should be taken over by a Dirac approach. Global ROP available up to ~1 GeV

NROP Koning at al. NPA 713 231 (2003) (KD) for nuclei $24 \le A \le 209$ and energies from 1 keV to 200 MeV, more recently extended to 1 GeV, to test at which energy the predictions of a phen. NROP fail

Calculations with TALYS (ECIS-06)

MICROSCOPIC OP

chiral potentials at N⁴LO describe NN scattering data up to 300 MeV and our OP can be used up to ~ 300 MeV Comparison phenomenological and microscopic NROP

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(2003) (KD) for r and energies fro more recently ex test at which energy range of a phen. NROP fail	comparison in the 150-330 MeV

Calculations with TALYS (ECIS-06)









PROSPECTS...

- the model can be improved
- folding integral
- 3N forces, medium effects
- application to nuclear reactions.... (e,e'p)