

Parton cascades at DLA: the role of the evolution variable

André Cordeiro

In collaboration with:

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Fabio Dominguez, Guilherme Milhano

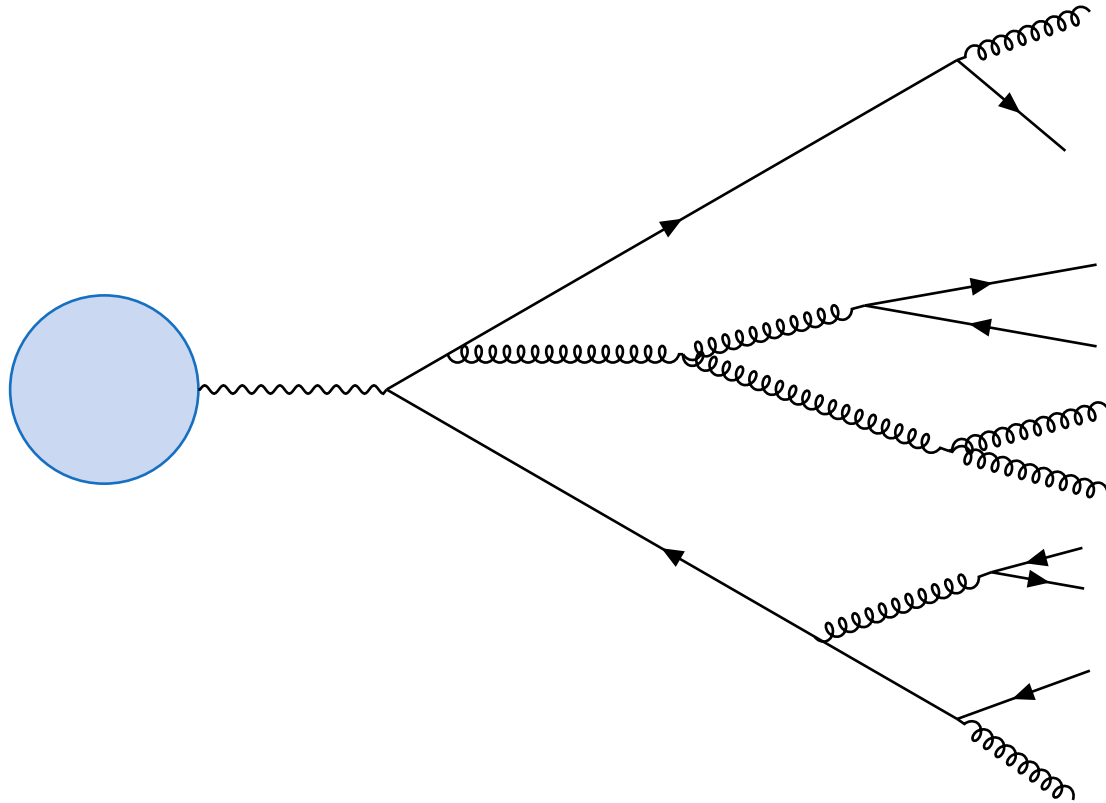


TÉCNICO
LISBOA

New jet quenching tools to explore equilibrium and non-equilibrium dynamics in heavy-ion collisions

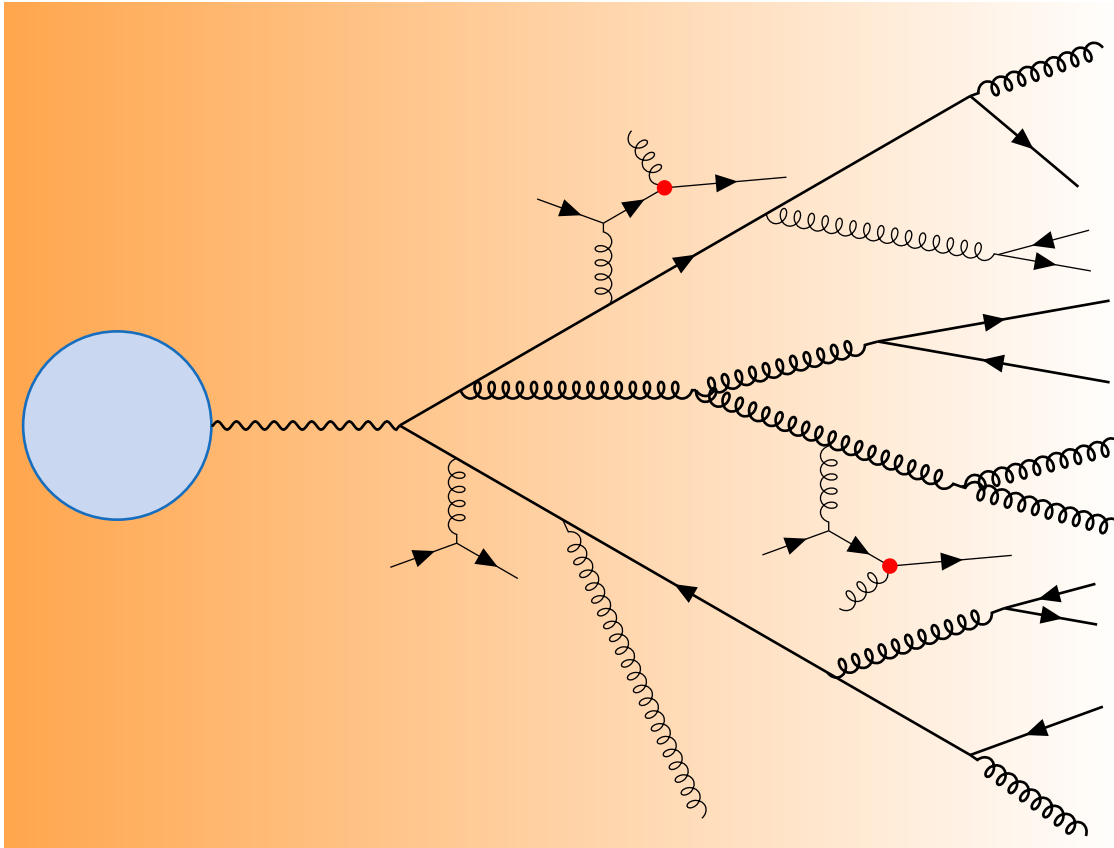
12–16 February 2024

Parton Showers in a Coloured Medium



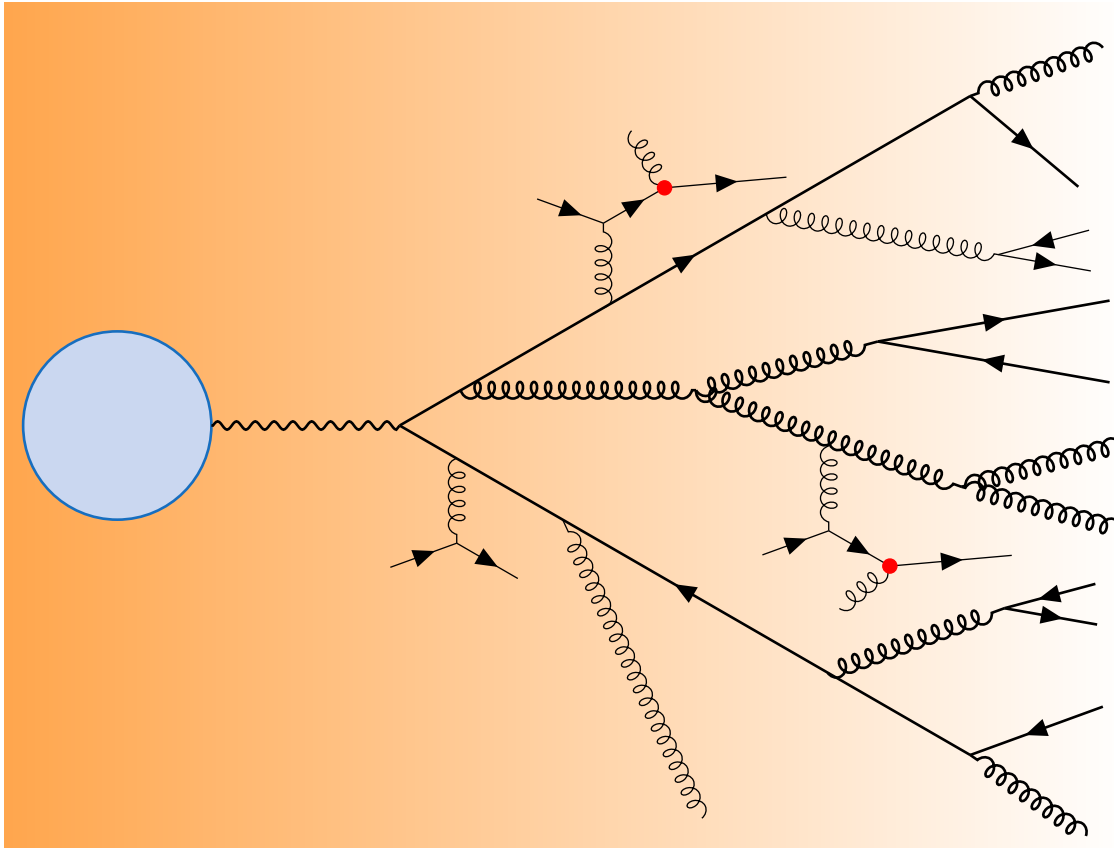
- Hard partons radiate until the hadronisation scale → Multi-scale object

Parton Showers in a Coloured Medium



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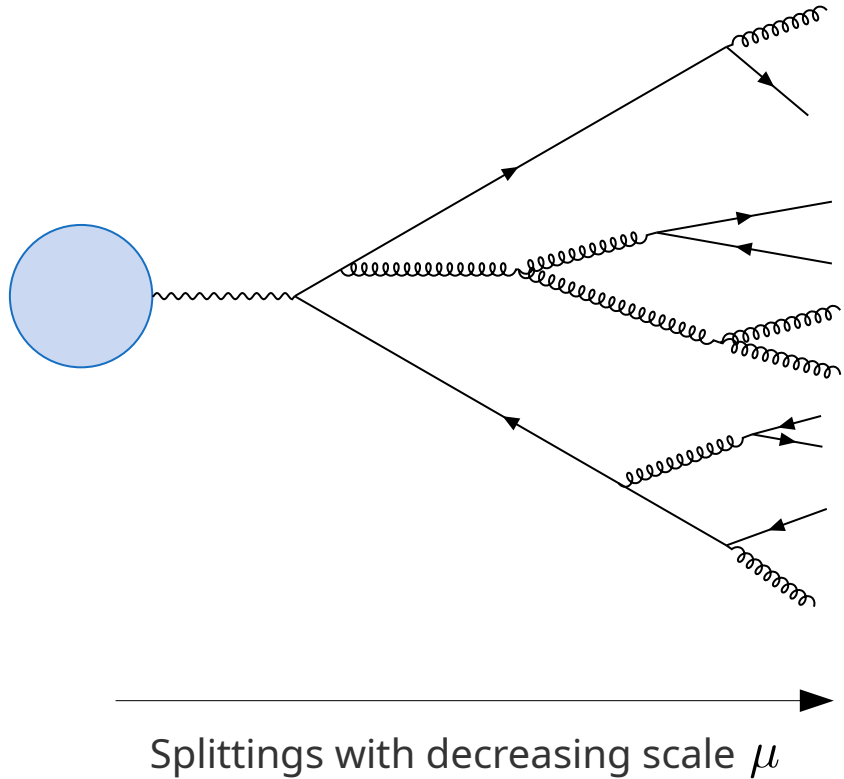


- Hard partons radiate until the hadronisation scale → Multi-scale object
- Time-ordered picture needed for medium interface with the cascade

Is jet quenching sensitive to the ordering of vacuum-like splittings?

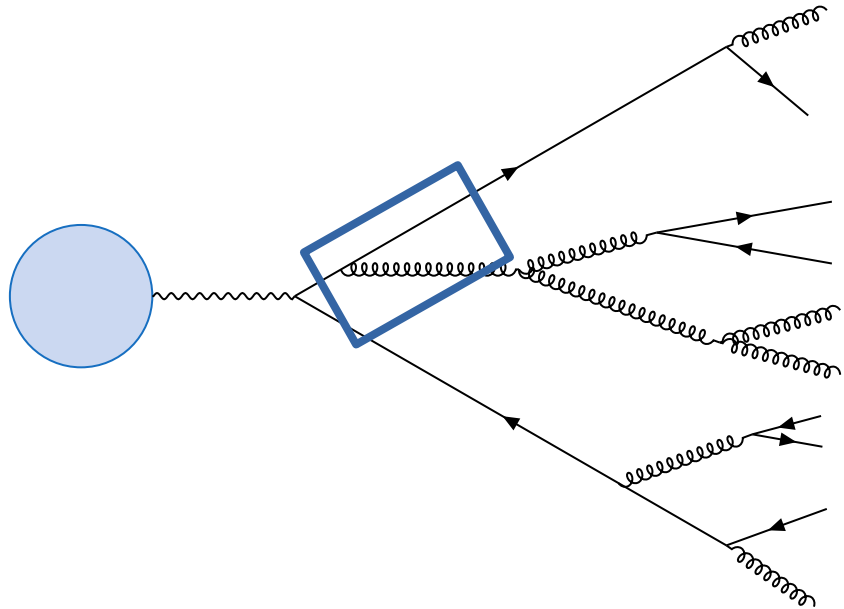
**First, a look at vacuum
(proton-proton) showers**

How to build a parton shower



How to build a parton shower

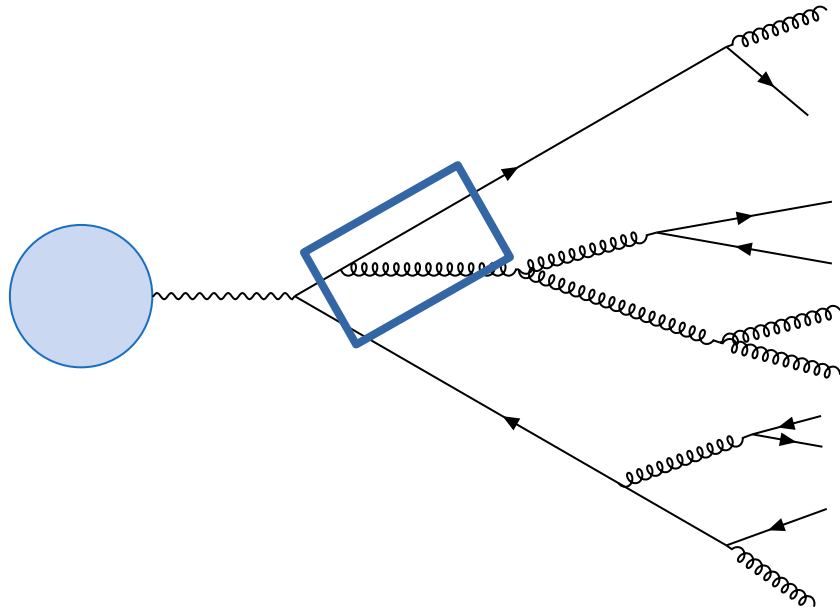
Building blocks: QCD splittings



Splittings with decreasing scale μ

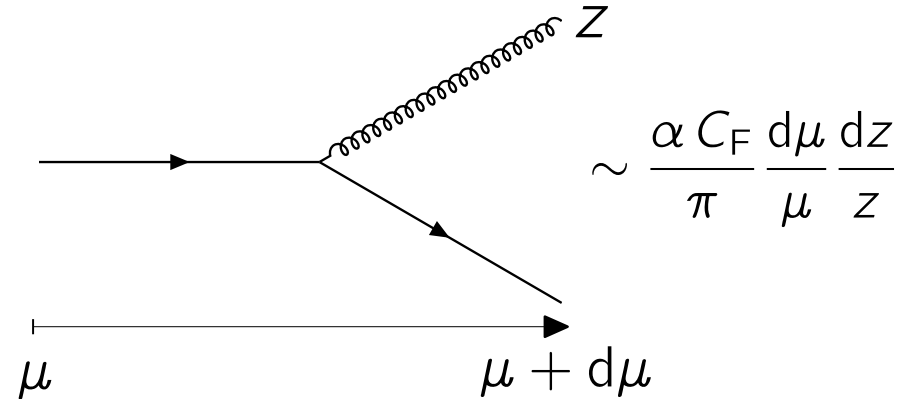
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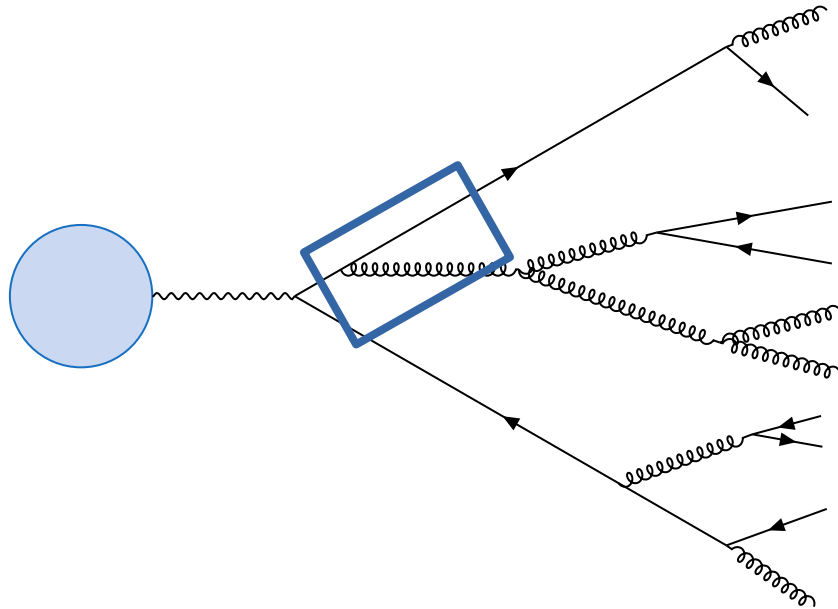
→ Splittings with decreasing scale μ

Splitting probability given by pQCD:



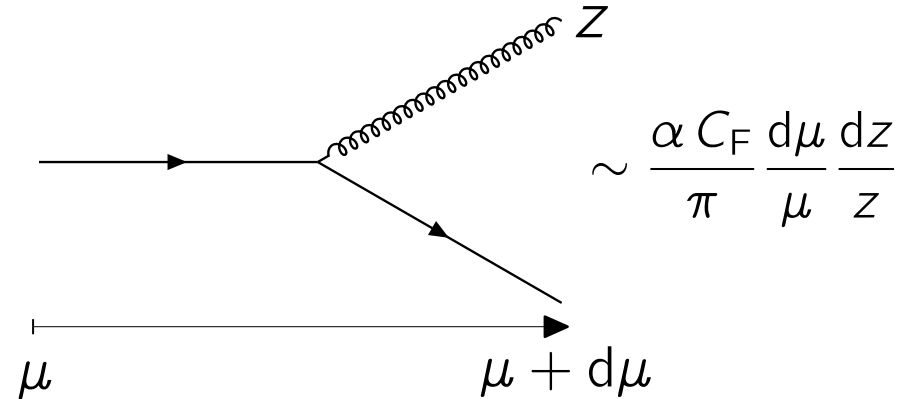
How to build a parton shower

Building blocks: QCD splittings



→ Splittings with decreasing scale μ

Splitting probability given by pQCD:



Probability of not emitting until some scale s :

$$\Delta(s_{\text{prev}}, s) = \exp \left\{ -\frac{\alpha C_R}{\pi} \int_s^{s_{\text{prev}}} \frac{d\mu}{\mu} \int_{z_{\text{cut}}(\mu)}^1 \frac{dz}{z} \right\}$$

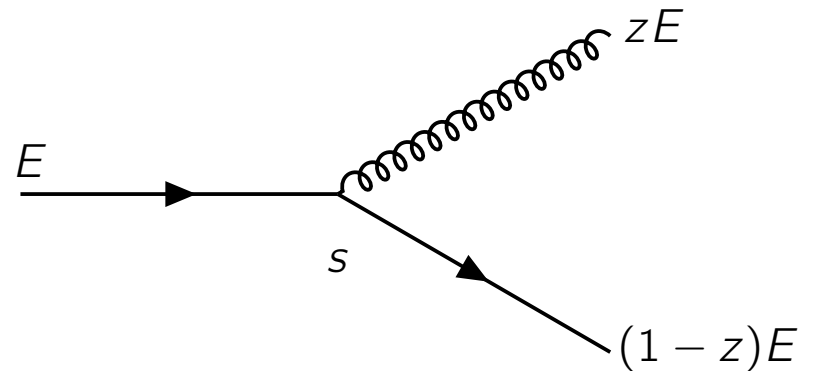
Yields the next emission scale s , given the previous scale s_{prev}

Building differently ordered cascades

No-emission probability:

$$\Delta(s_{\text{prev}}, s) = \exp \left\{ -\frac{\alpha C_R}{\pi} \int_s^{s_{\text{prev}}} \frac{d\mu}{\mu} \int_{z_{\text{cut}}(\mu)}^1 \frac{dz}{z} \right\}$$

Splitting variables:



Building differently ordered cascades

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Interpretations for the scale:

$$s \rightarrow p^2 = \frac{|\mathbf{p}_{\text{rel}}|^2}{z(1-z)}$$

(Virtuality)

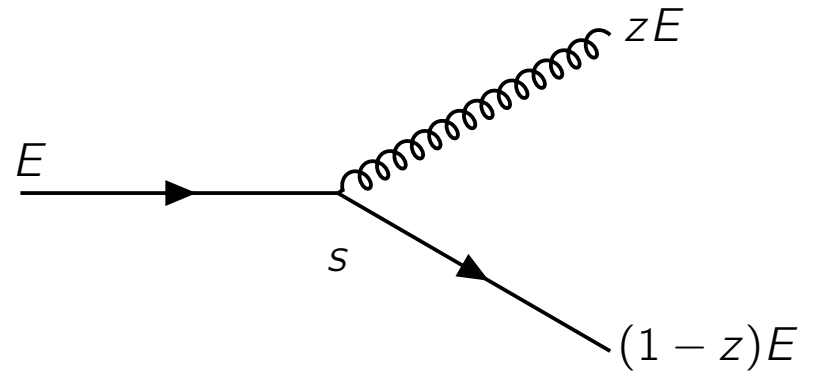
$$s \rightarrow t_{\text{form}}^{-1} = \frac{p^2}{E} = \frac{|\mathbf{p}_{\text{rel}}|^2}{Ez(1-z)}$$

(Formation time)

$$s \rightarrow \zeta = \frac{p^2}{E^2 z(1-z)} = \left(\frac{|\mathbf{p}_{\text{rel}}|}{Ez(1-z)} \right)^2$$

(Angle)

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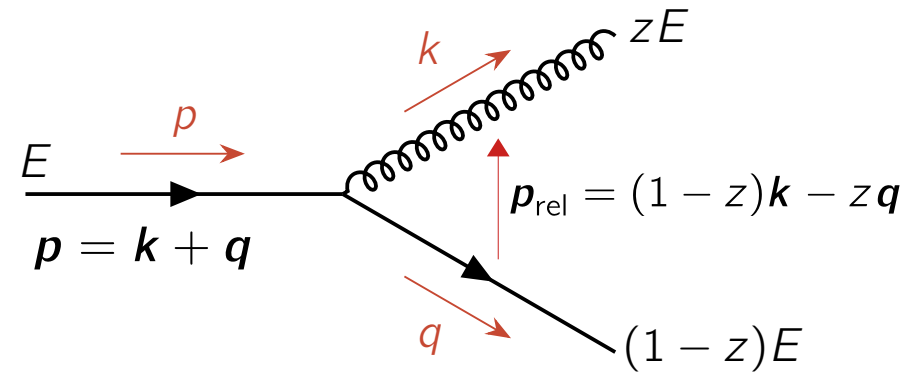
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To generate a splitting:



1. Sample a scale from $\Delta(s_{\text{prev}}, s)$
 2. Sample a fraction from $\hat{P}(z) \propto 1/z$
- Ensure that** $|\mathbf{p}_{\text{rel}}|^2 > \Lambda^2$

Building differently ordered cascades

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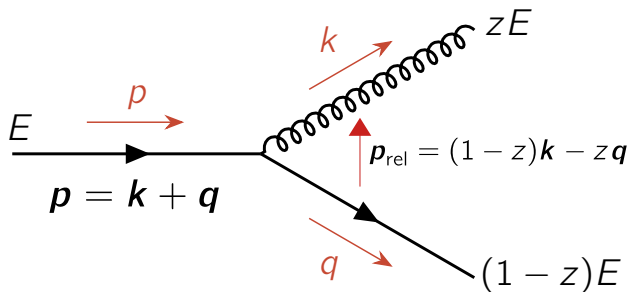
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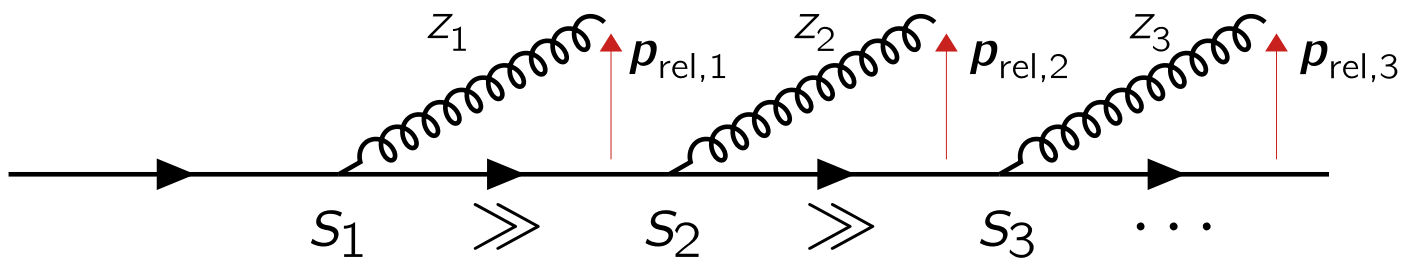
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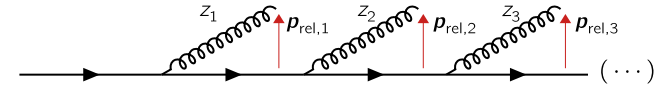


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This results in the strong ordering of scales

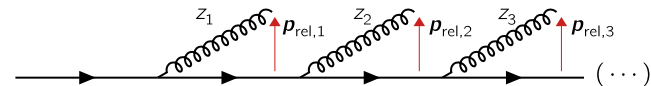
Parton Shower Details



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Parton Shower Details



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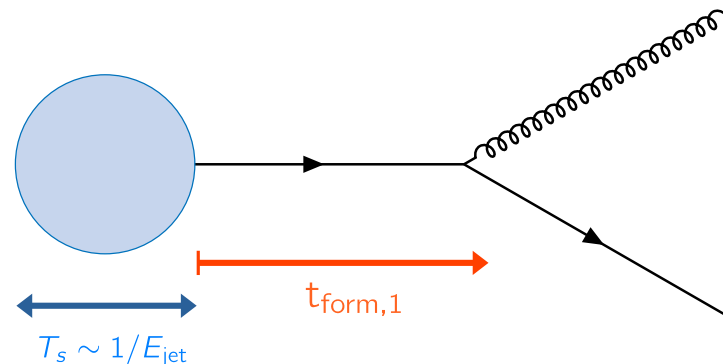
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- Splittings must happen above an hadronisation scale: $|\mathbf{p}_{\text{rel}}|^2 > \Lambda^2$

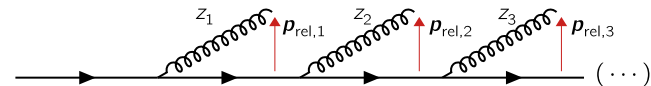
- This provides a **soft cutoff**: $z > z_{\text{cut}}(s)$

e.g.: Formation time ordering $|\mathbf{p}_{\text{rel}}|^2 > \Lambda^2 \iff z(1-z) > \frac{\Lambda^2}{t_{\text{form}}^{-1} E}$

- Initialisation condition for the shower: $t_{\text{form}}^{-1} < E$



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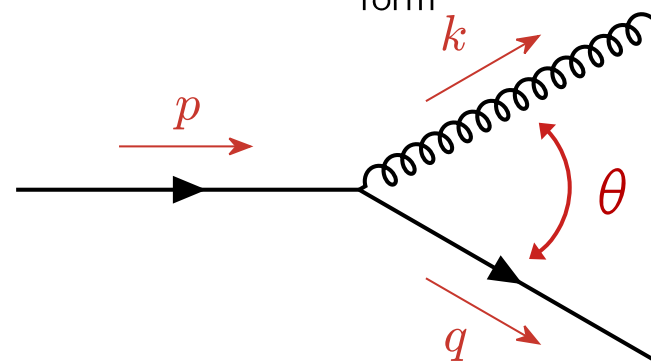
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- For consistency between orderings: $\zeta < 4 \implies |\mathbf{p}_{\text{rel}}| < \frac{E}{2}$
(Enforced via retries)

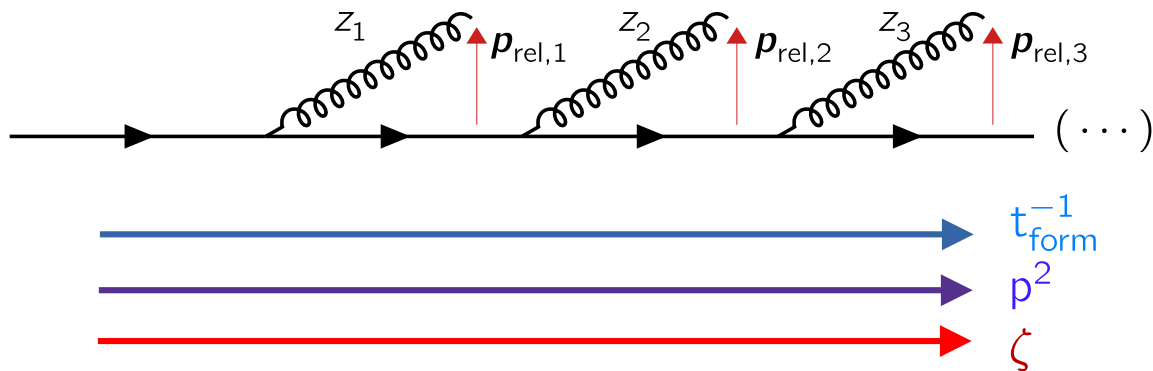
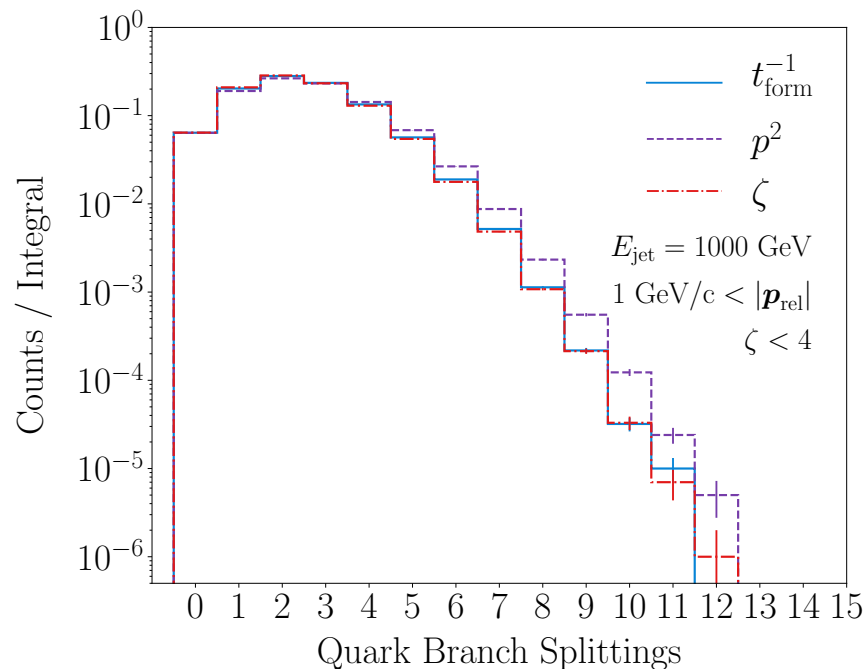


Massless Limit : $\zeta \simeq 2(1 - \cos \theta)$ 8

Results (Work in Progress)

Differences in Ordering Choices

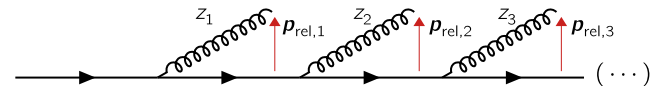
Splittings along the quark branch



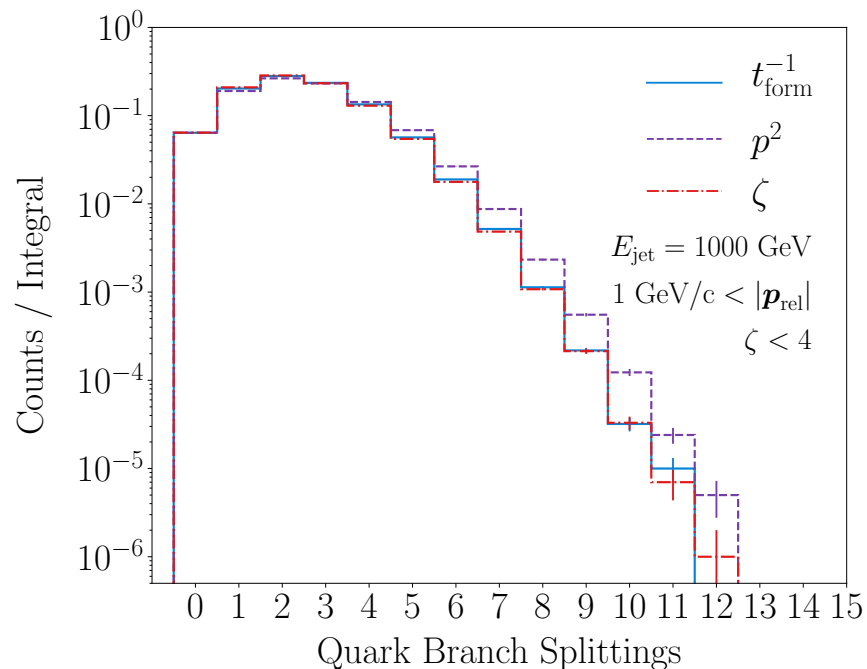
The strictly decreasing scale is different for the three algorithms

Different orderings \rightarrow Different phase-space for allowed splittings

Differences in Ordering Choices

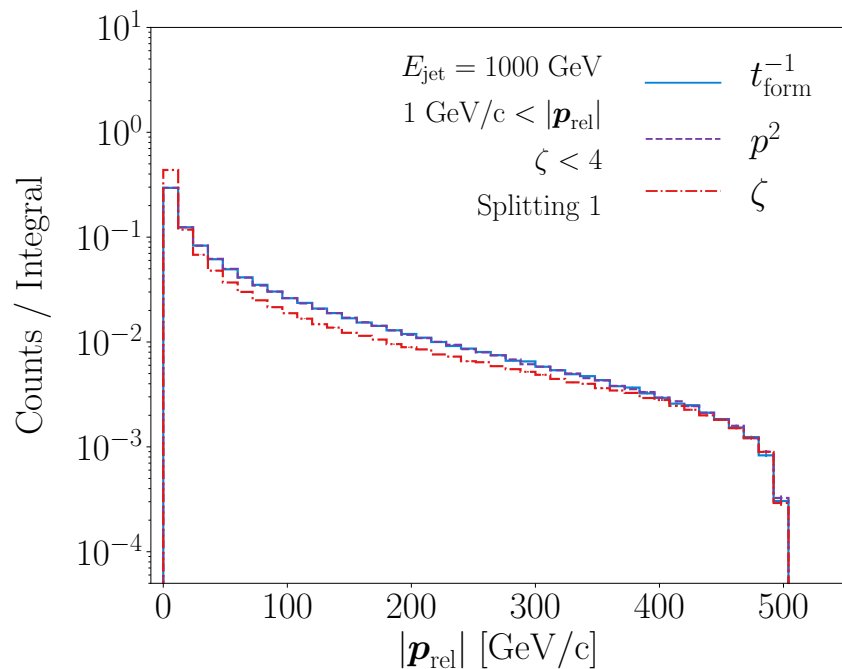


Splittings along the quark branch



Different orderings \rightarrow Different phase-space for allowed splittings

Relative transverse momentum (1st splitting)



Transverse momentum distributions

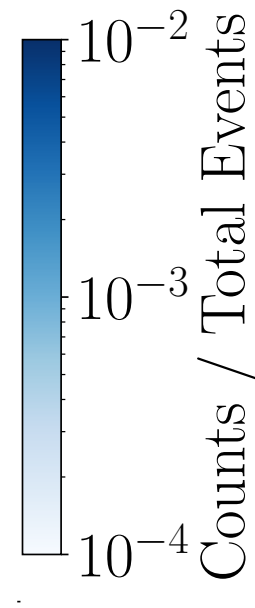
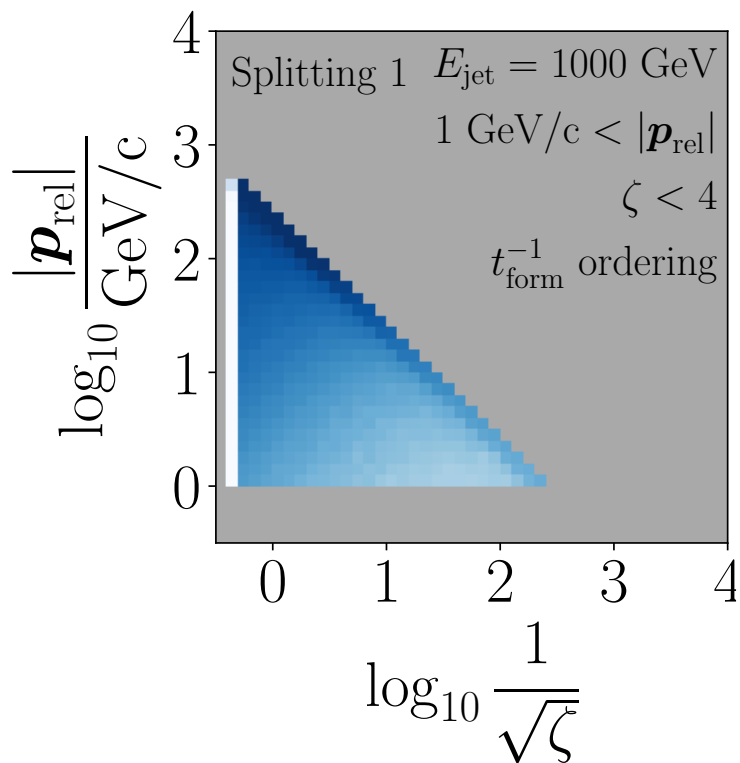
follow $\frac{d\mathbf{p}_{\text{rel}}^2}{p_{\text{rel}}^2}$

Lund Plane Densities

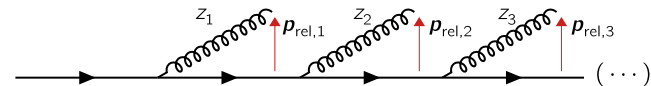


Consider the shower evolution along the quark branch:

*Exaggerated scale

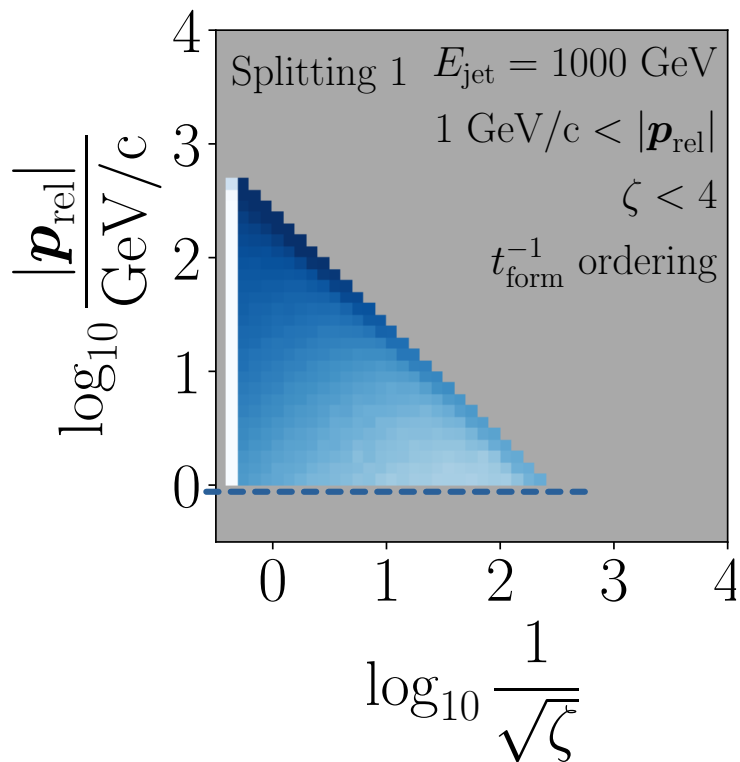


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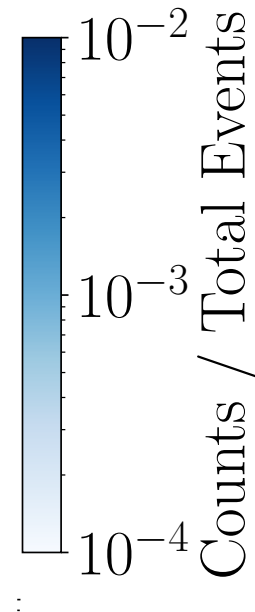
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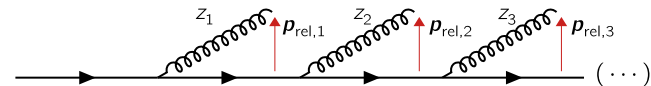


Lund Plane Boundaries:

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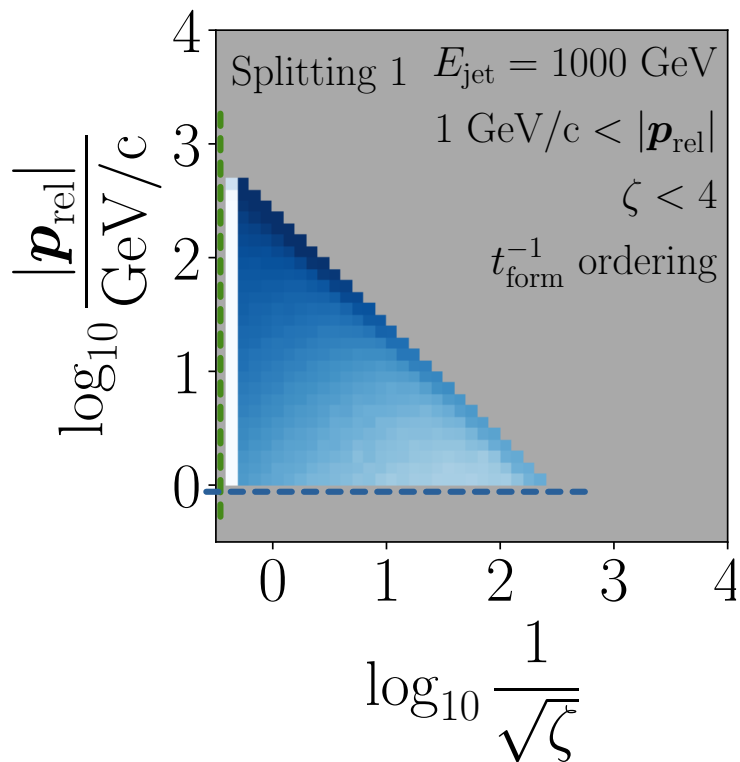


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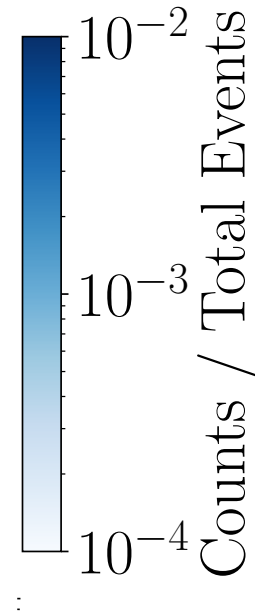
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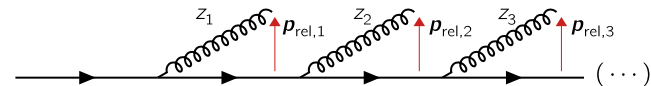


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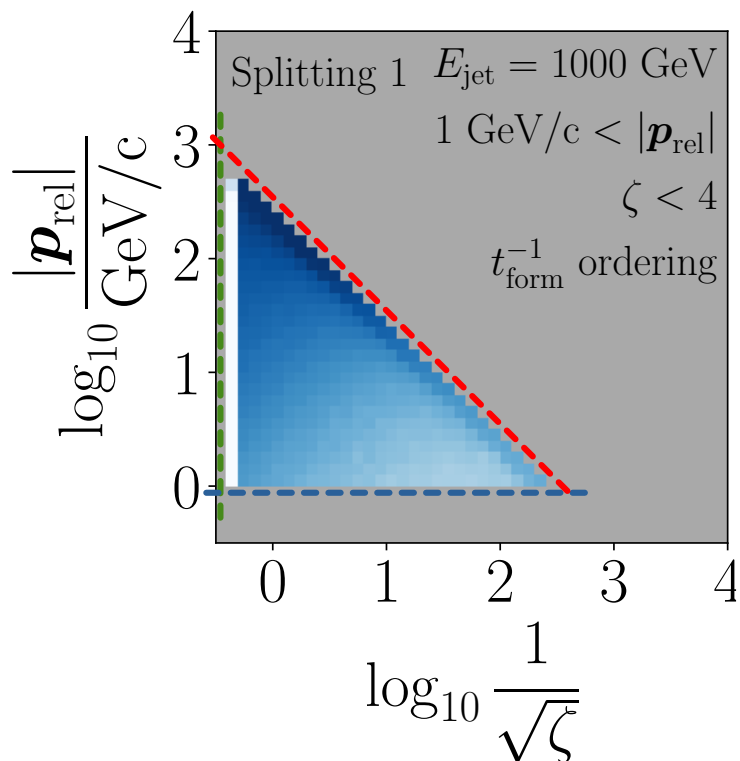


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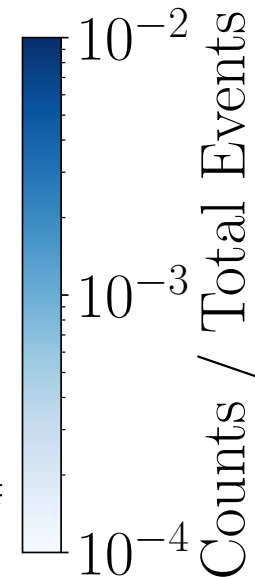


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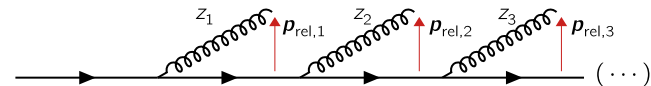
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- Energy constraint: $\frac{E}{4} > E z(1-z) = |\mathbf{p}_{\text{rel}}| \frac{1}{\sqrt{\zeta}}$



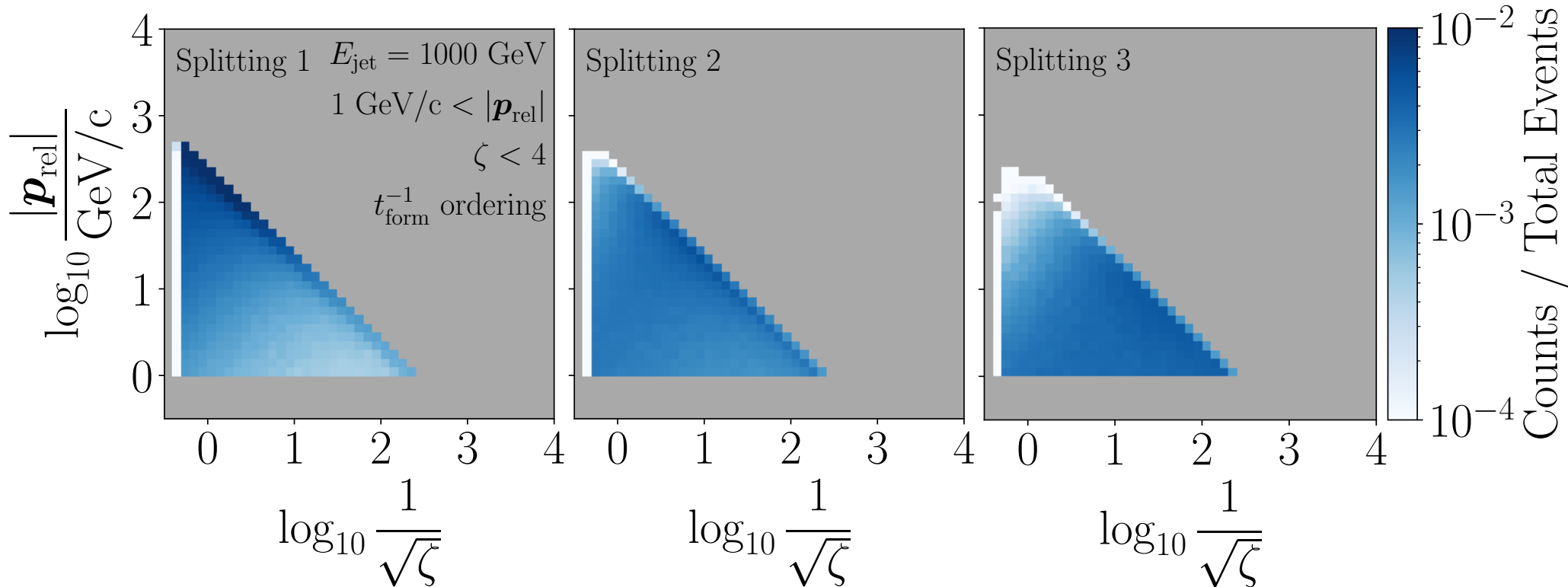
Shower evolution: Both transverse momentum and angle decrease.

Lund Plane Densities



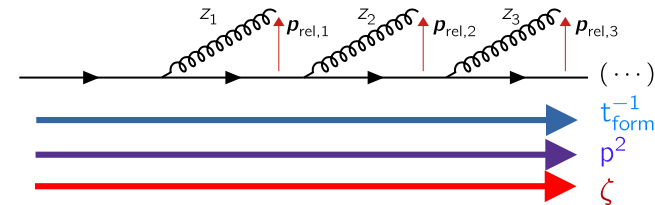
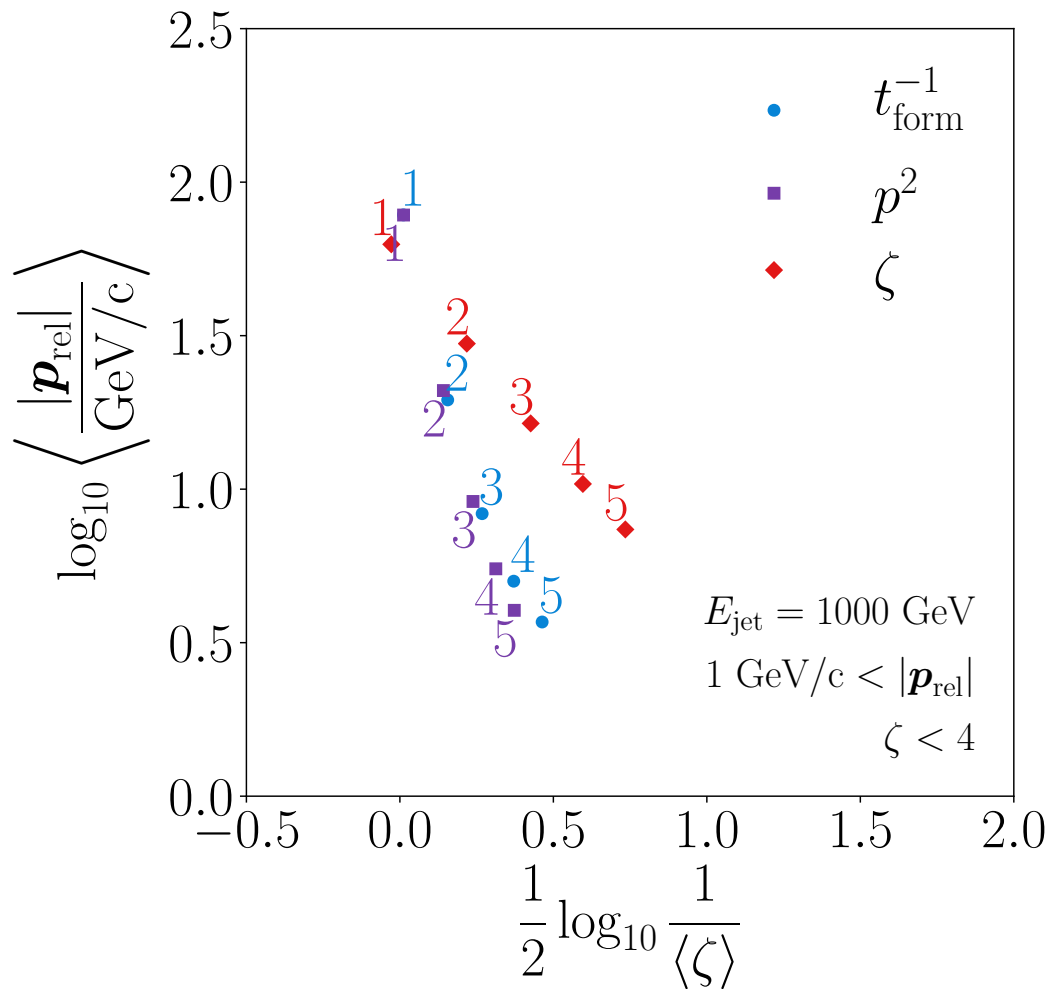
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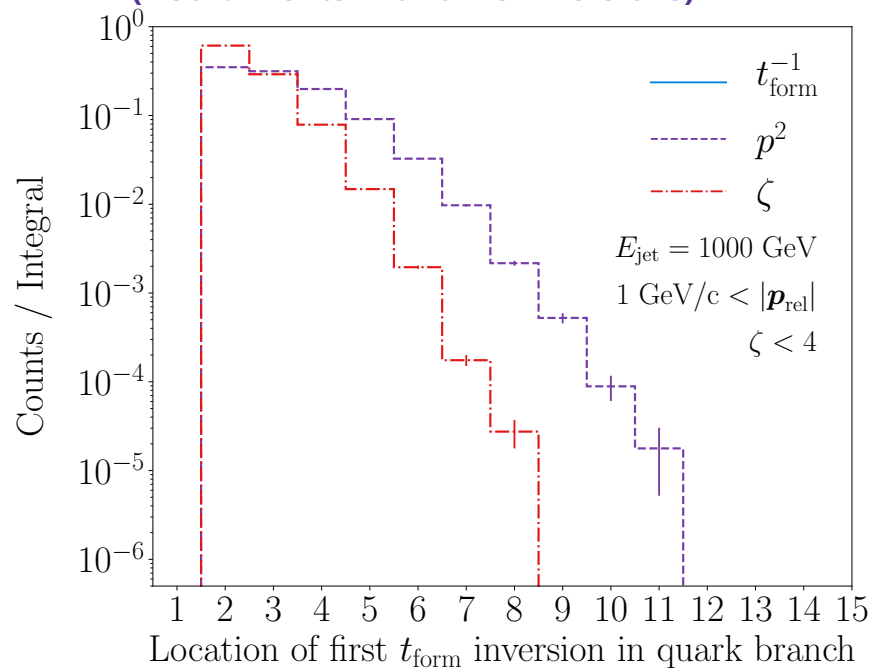
Lund Plane Trajectories



**Differences between
 phase-space trajectories**
**→ Uncertainty at DLA
 Accuracy**

Inversions in Kinematic Variables

(~ 30% Events with time inversions)

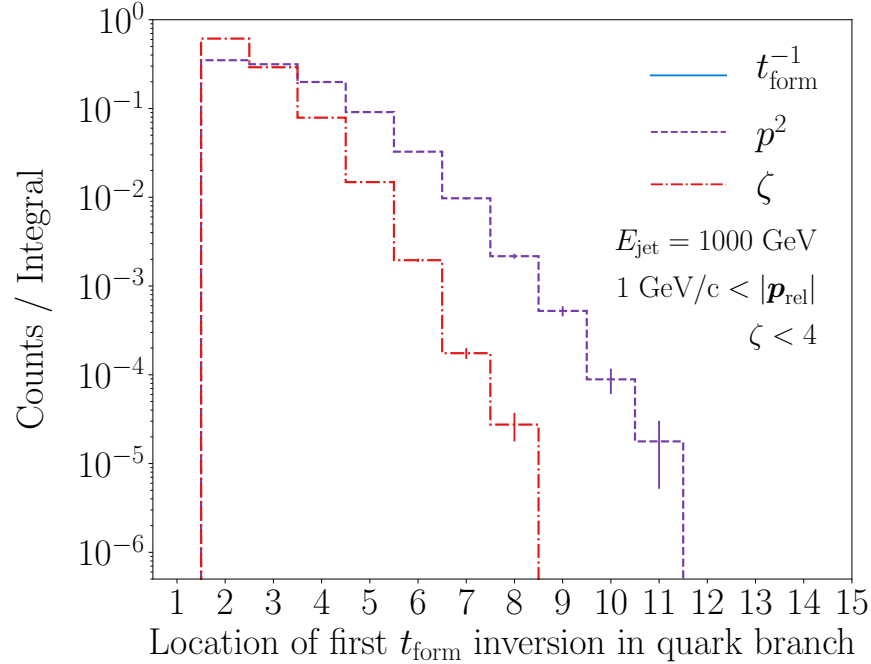


Formation Time Inversions:

Splittings with a formation time shorter
that their immediate predecessor.

Inversions in Kinematic Variables

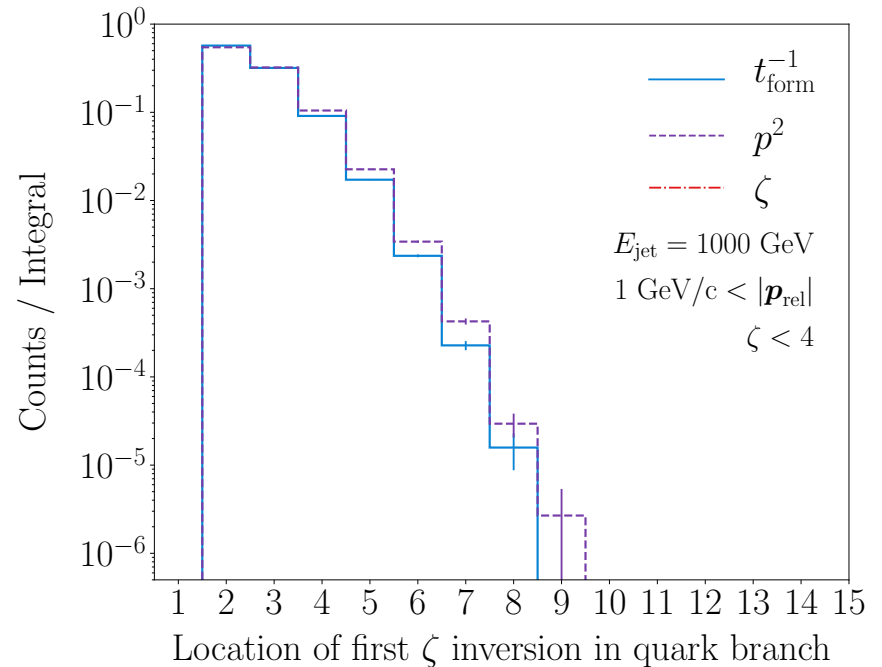
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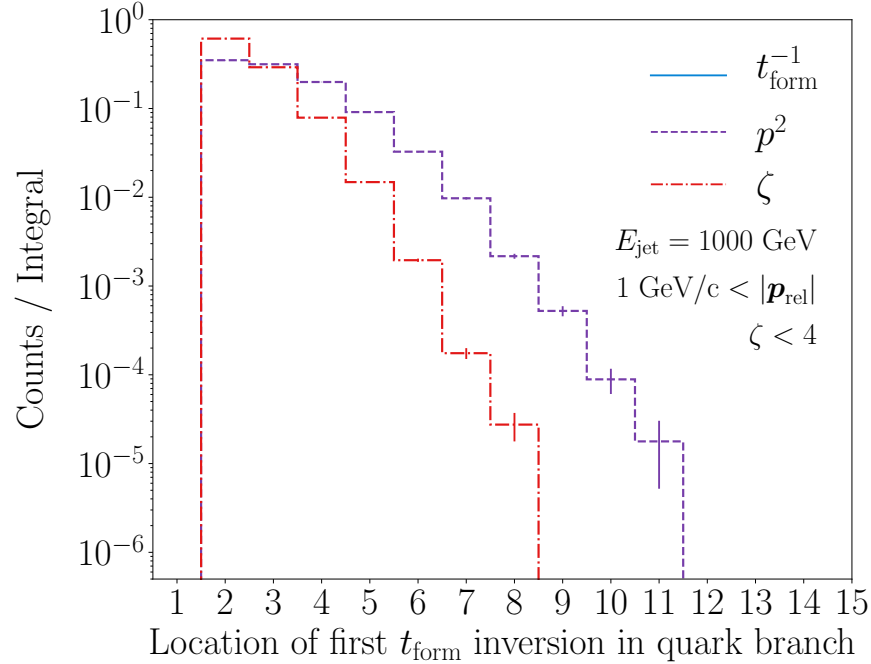
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Angular inversions

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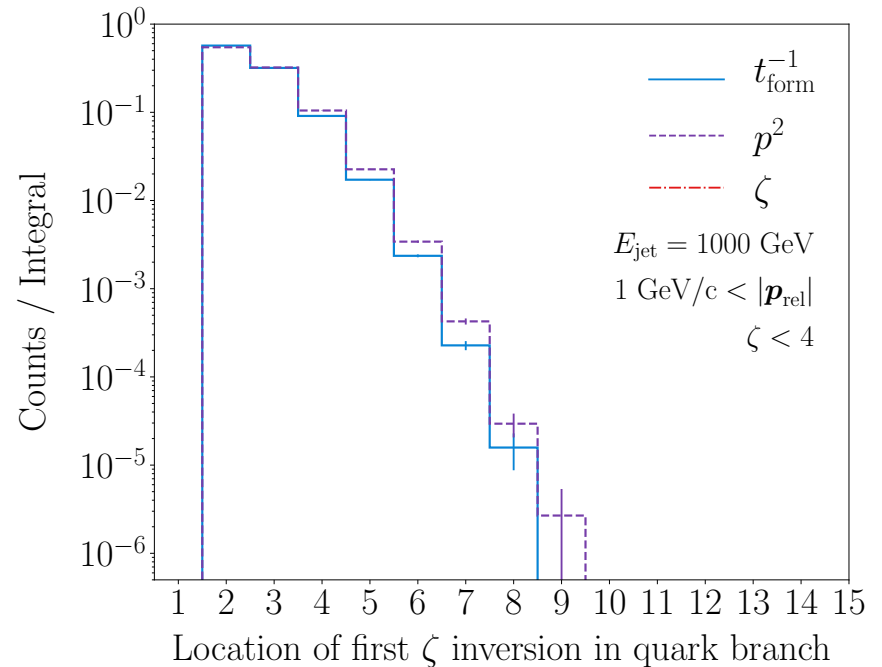
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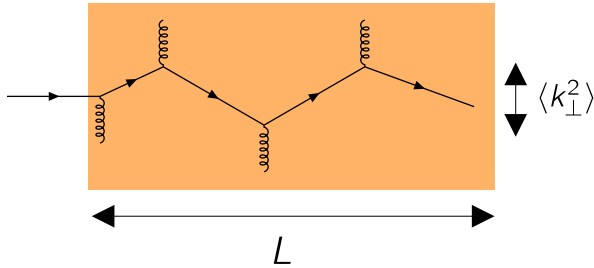
Angular inversions

Can this discrepancy translate into differences in quenching magnitude?

Now, a simple jet quenching model!

Choosing a quenching condition

(Tywoniuk, Wed 14:00)

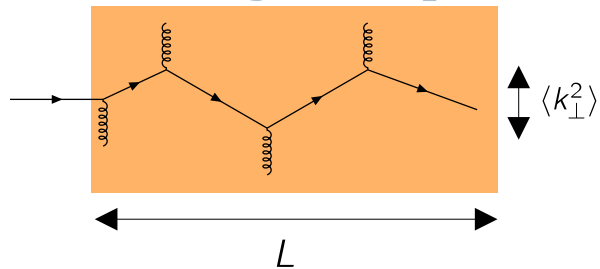


Medium parameters (for a simple model):

- Medium length: L
- Transport coefficient: $\hat{q} \sim \frac{\langle k_{\perp}^2 \rangle}{\lambda}$

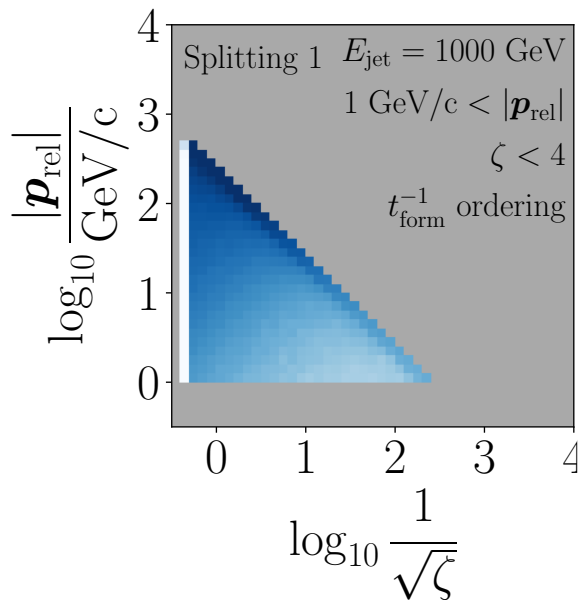
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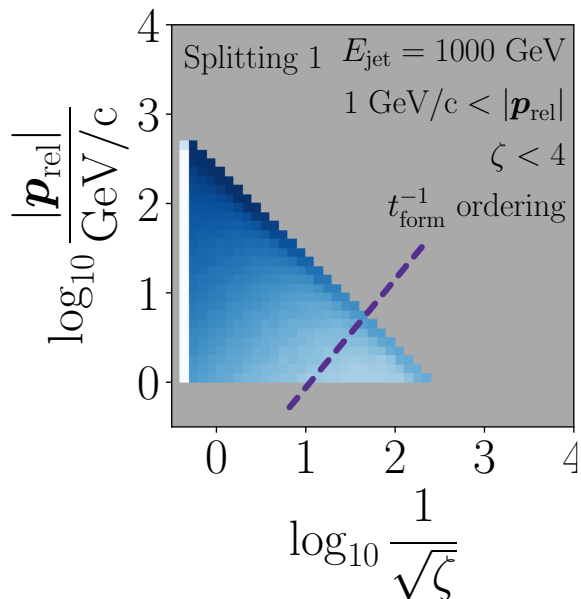
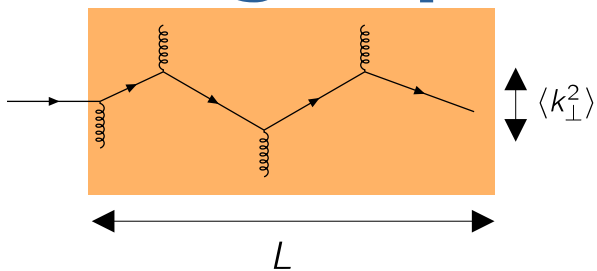
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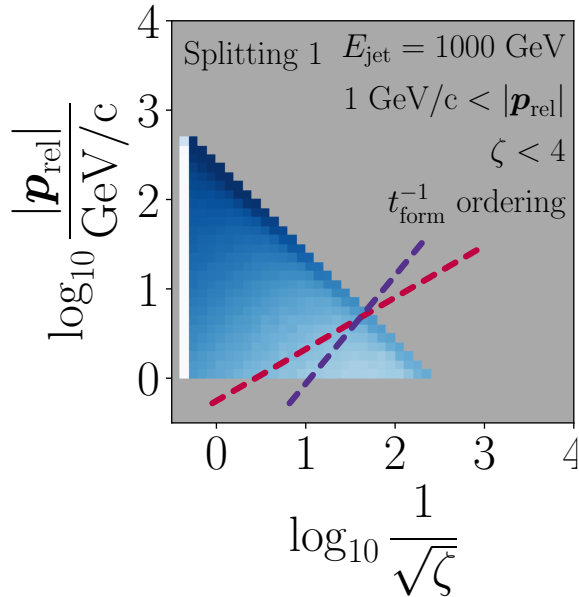
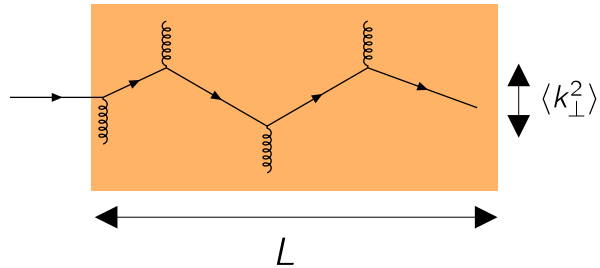
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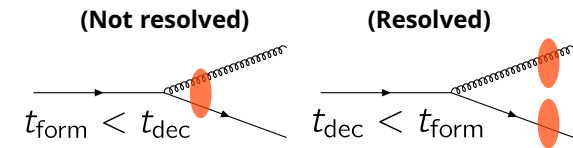
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$$|\mathbf{p}_{rel}|^2 < \hat{q} t_{form} \iff \underbrace{(\hat{q}\zeta)^{-1/3}}_{t_{dec}} < t_{form}$$

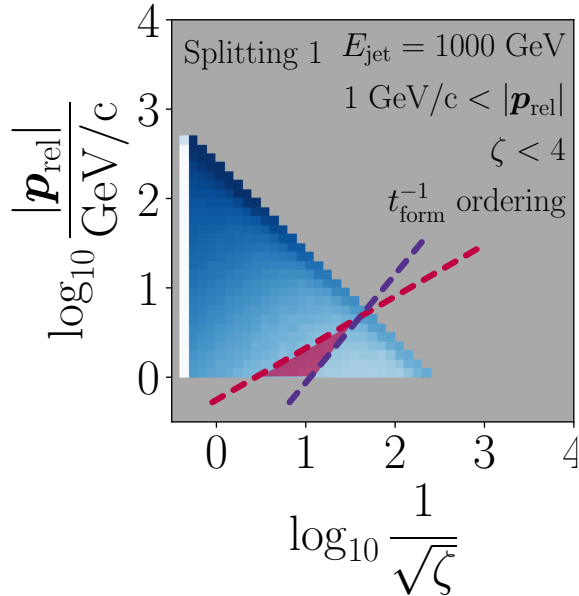
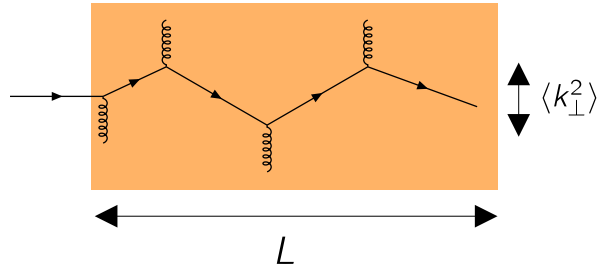
Medium resolves splittings on the (de)coherence time scale

→ Daughters lose energy individually



Choosing a quenching condition

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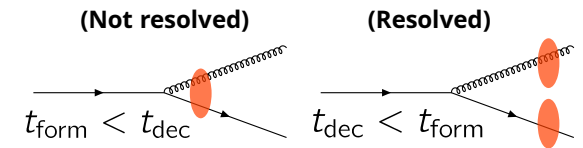
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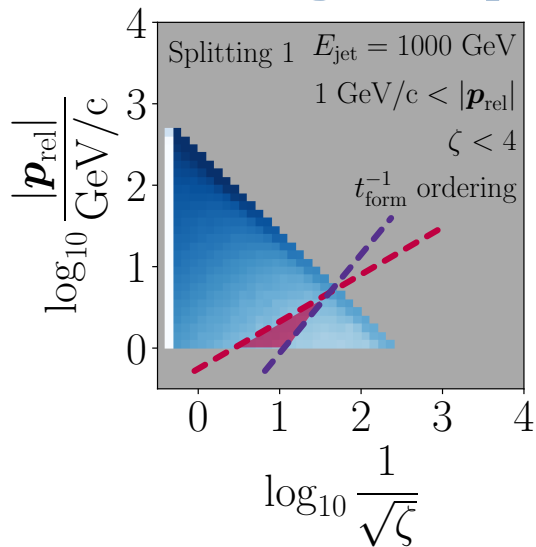
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Eliminate events within this area:

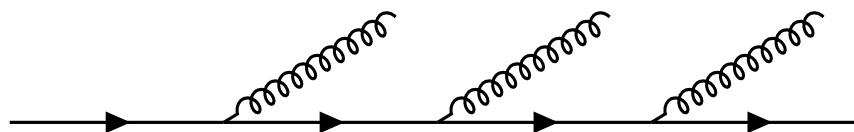
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Choosing a quenching condition

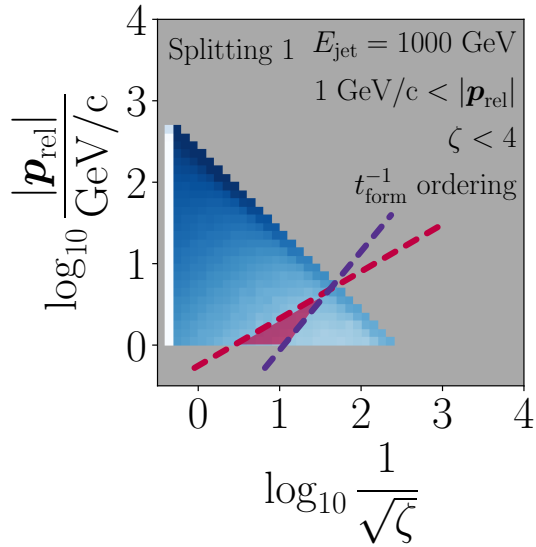


Eliminate events within this area:

$$\mathcal{P}_{\text{quench}} = \Theta(L > t_{\text{form}} > t_{\text{dec}}) \quad t_{\text{dec}} = (\hat{q}\zeta)^{-1/3}$$



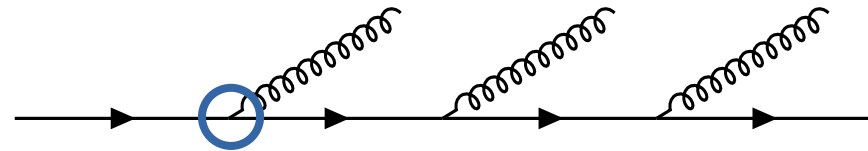
Choosing a quenching condition



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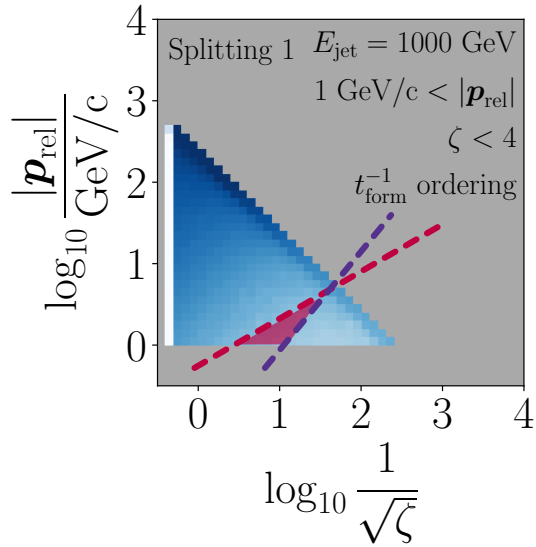
$$\mathcal{P}_{\text{quench}} = \Theta(L > t_{\text{form}} > t_{\text{dec}}) \quad t_{\text{dec}} = (\hat{q}\zeta)^{-1/3}$$

Two implementations:



- Option 1: Apply only to first splitting

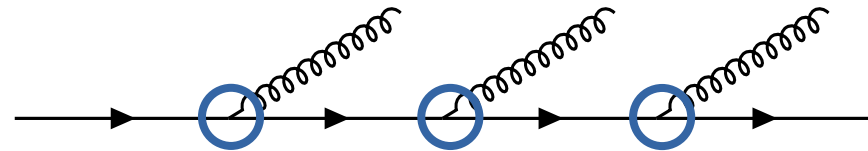
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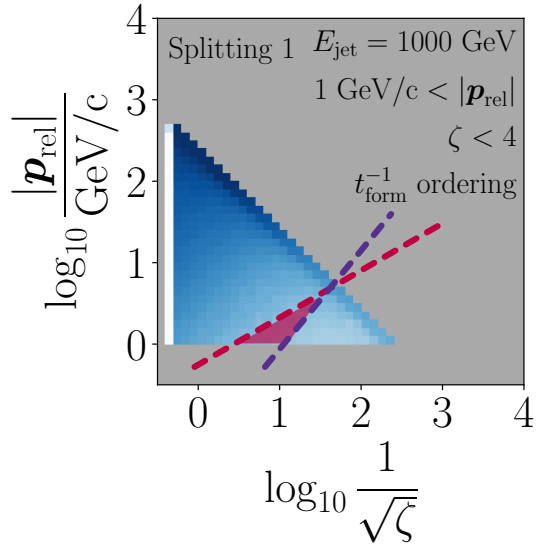
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Two implementations:



- Option 1: Apply only to first splitting
- Option 2: Apply to whole quark branch

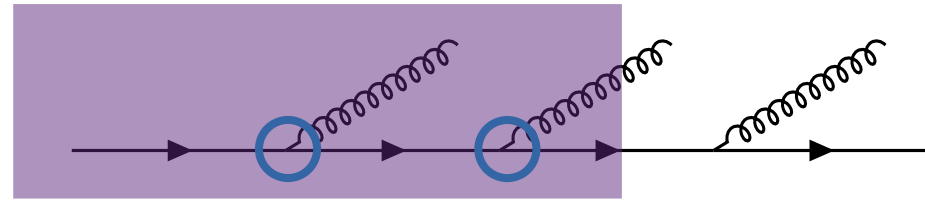
Choosing a quenching condition



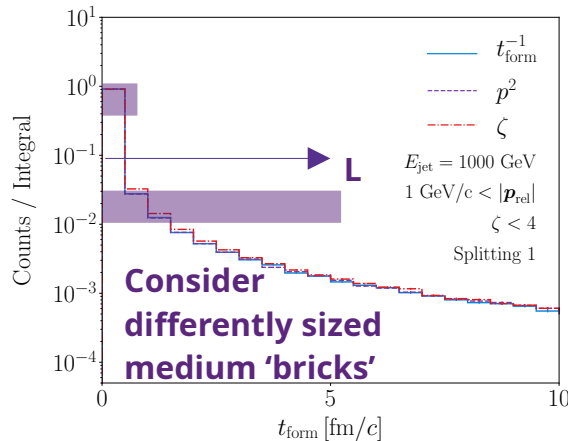
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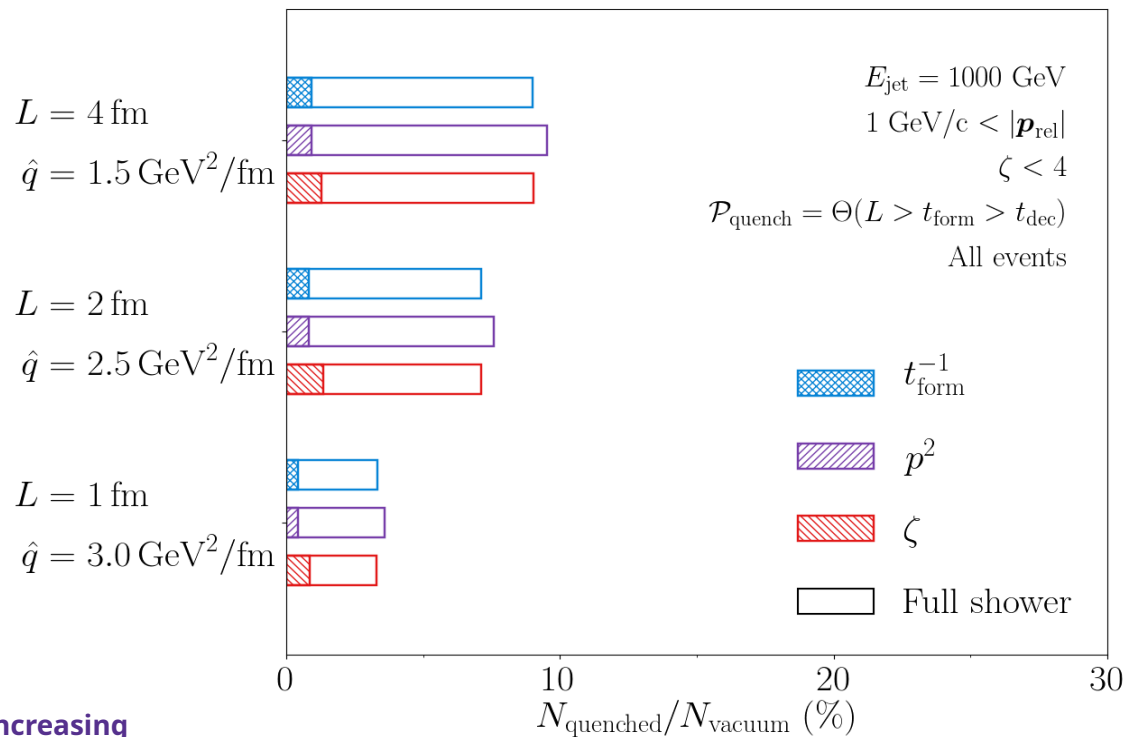
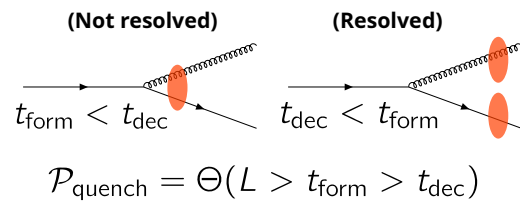


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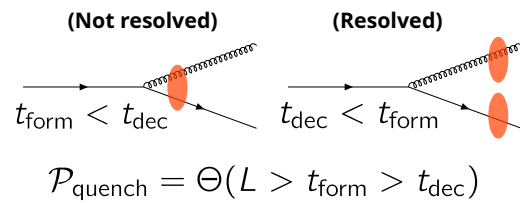
Fraction of Quenched Events

Percentage of events eliminated by the quenching condition

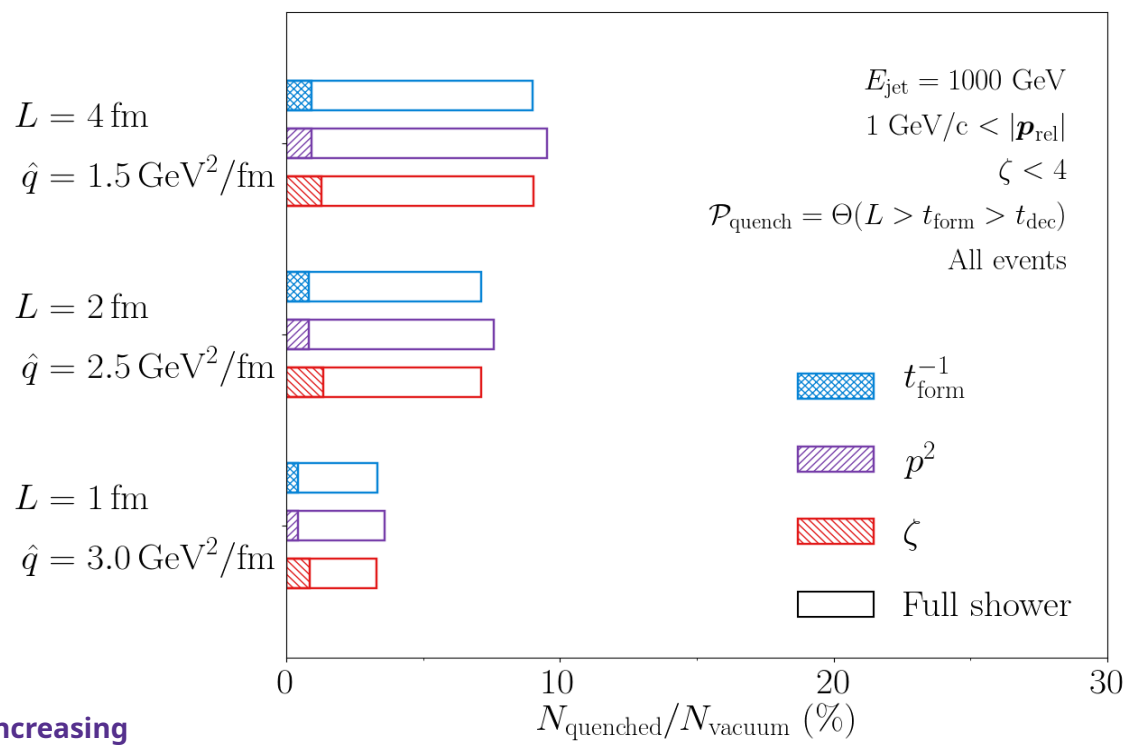


Increasing
quenching effects

Fraction of Quenched Events



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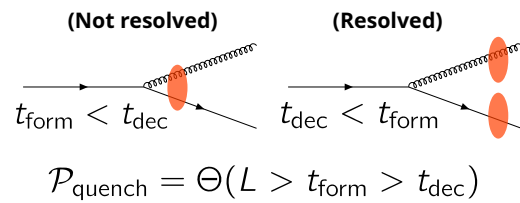


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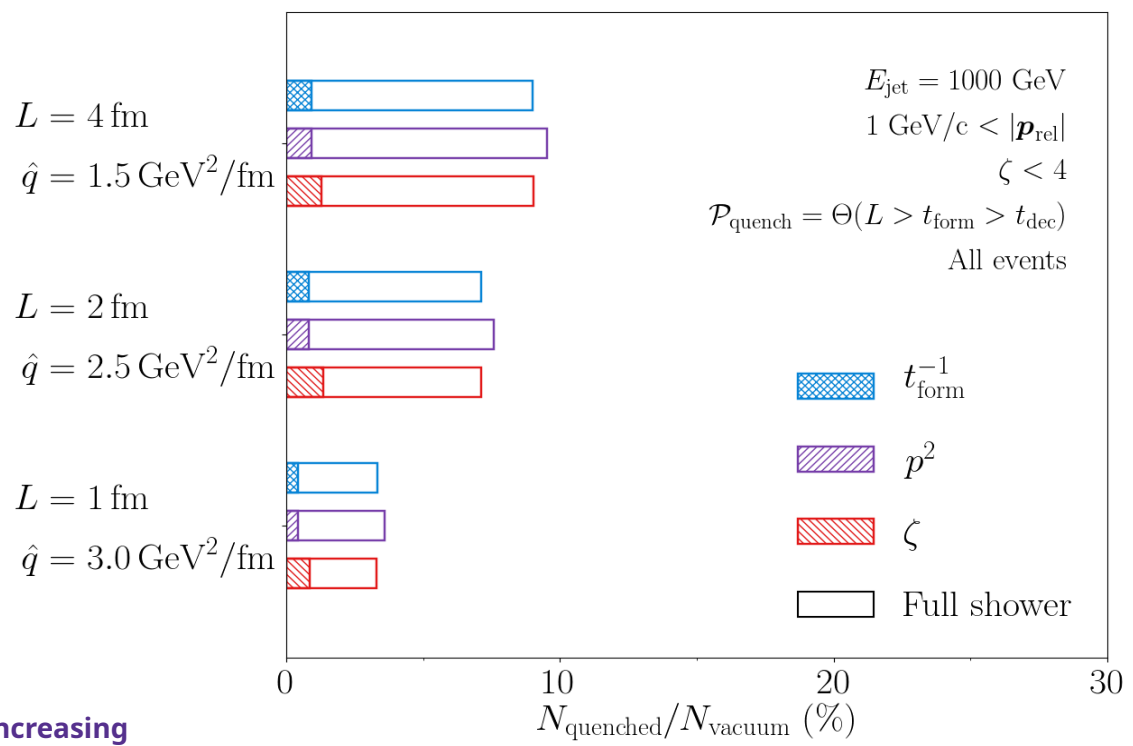
Applying condition to the first splitting → Significant differences in quenching between algorithms

Differences are **seen to remain (for larger L)** when applying the condition to the full quark branch.

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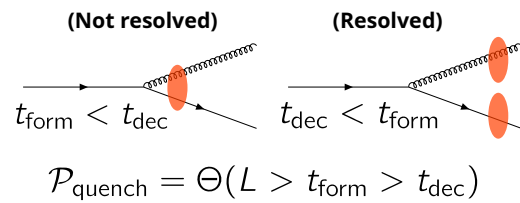


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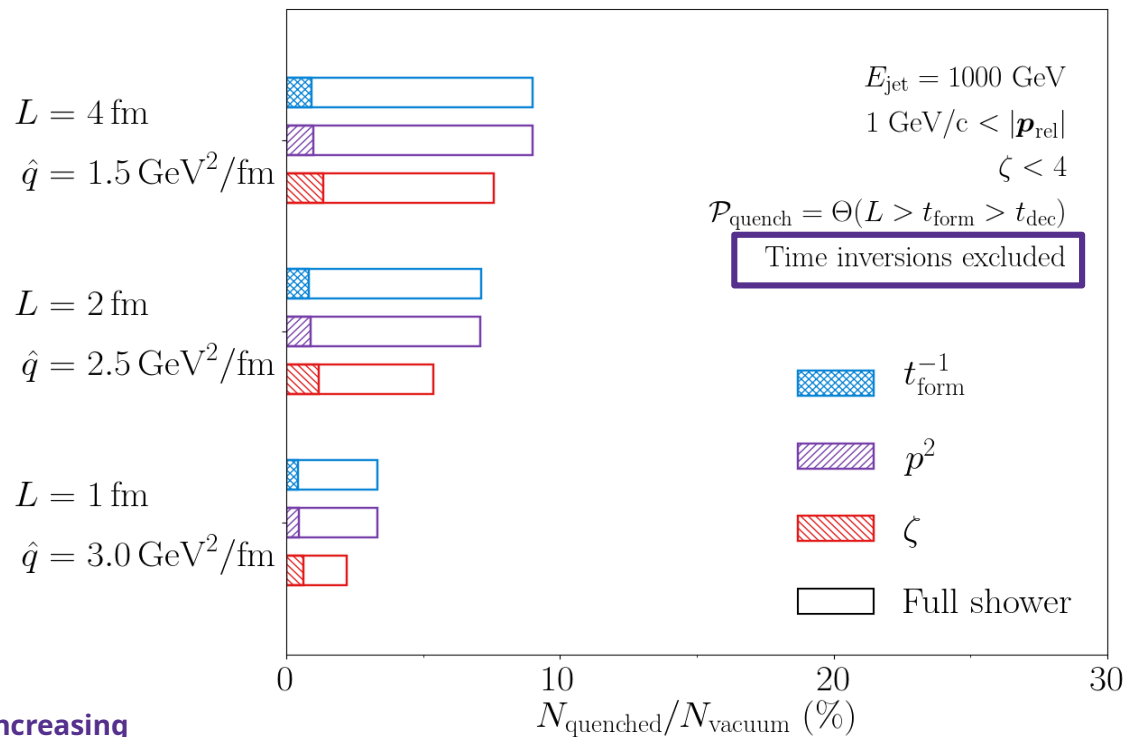
What role do time-inversions play in these quenching differences?

Fraction of Quenched Events



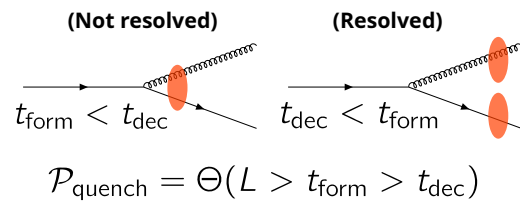
Discarding time-inverted events from the samples:

(Ad-hoc 'cut')



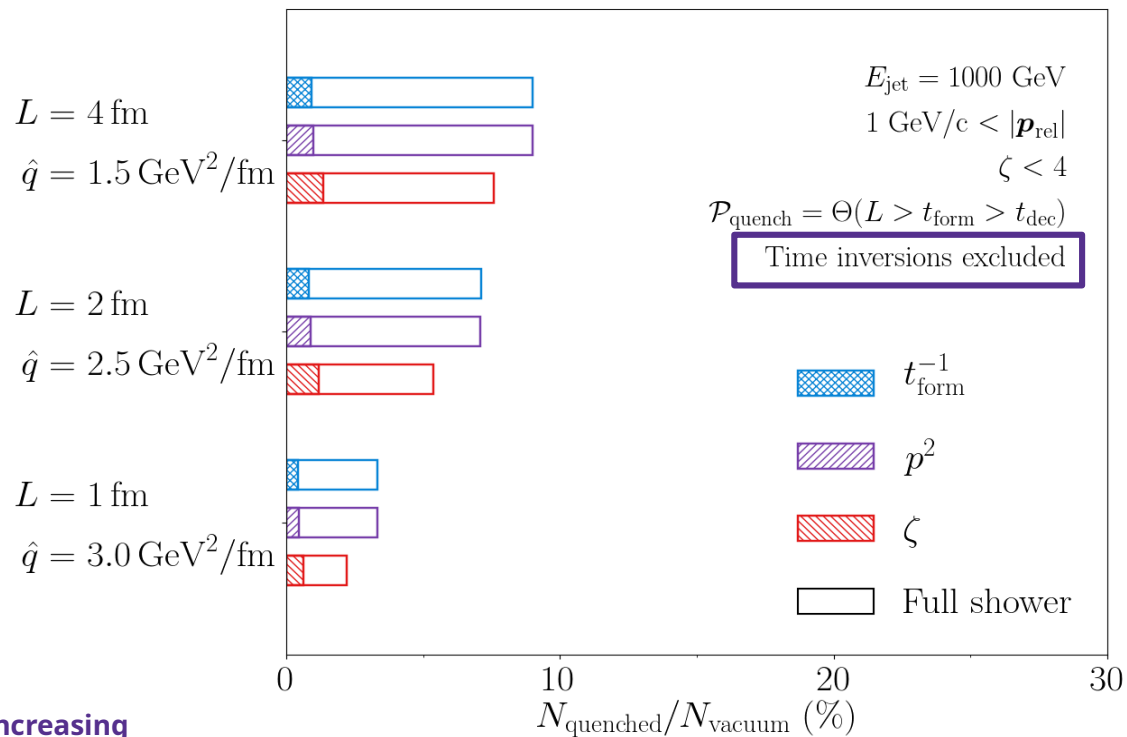
*** All events with at least one time-inverted splitting are removed before applying the quenching model

Fraction of Quenched Events



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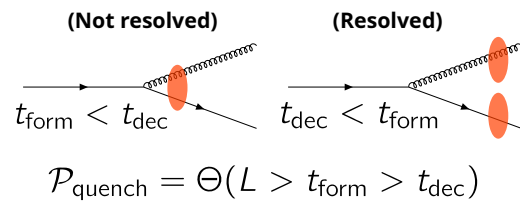
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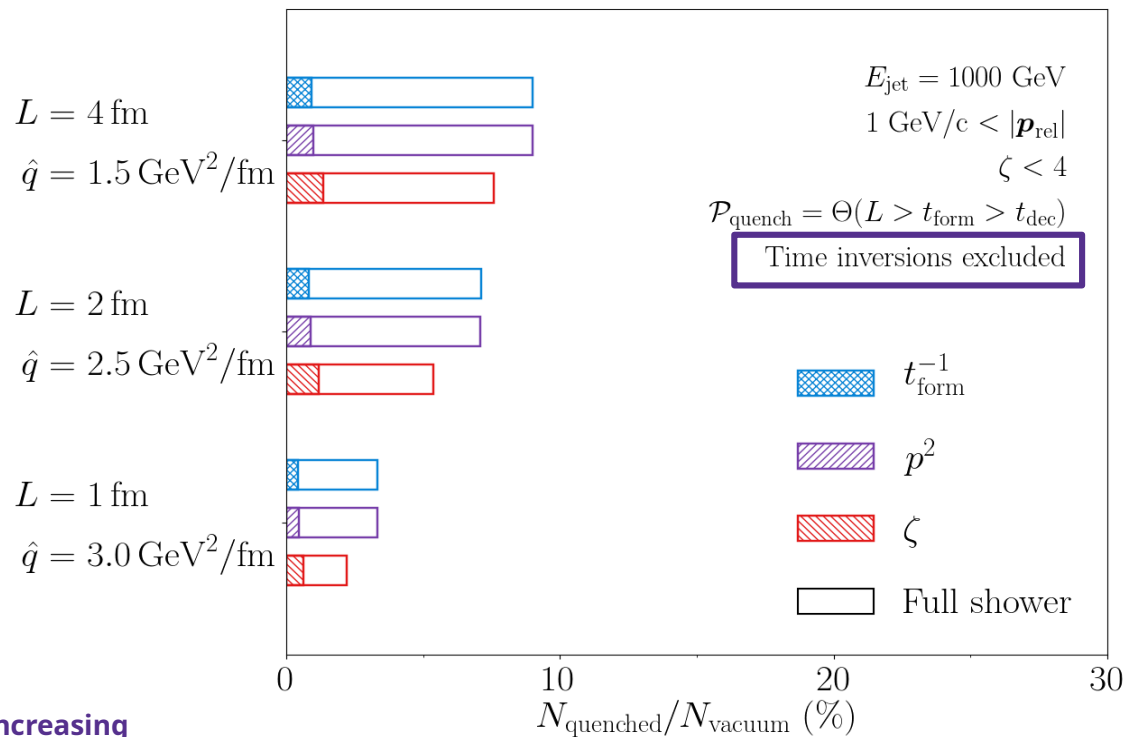
For angular ordered showers:
 $\Rightarrow \zeta$ strictly decreasing
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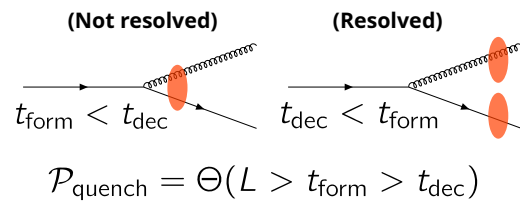


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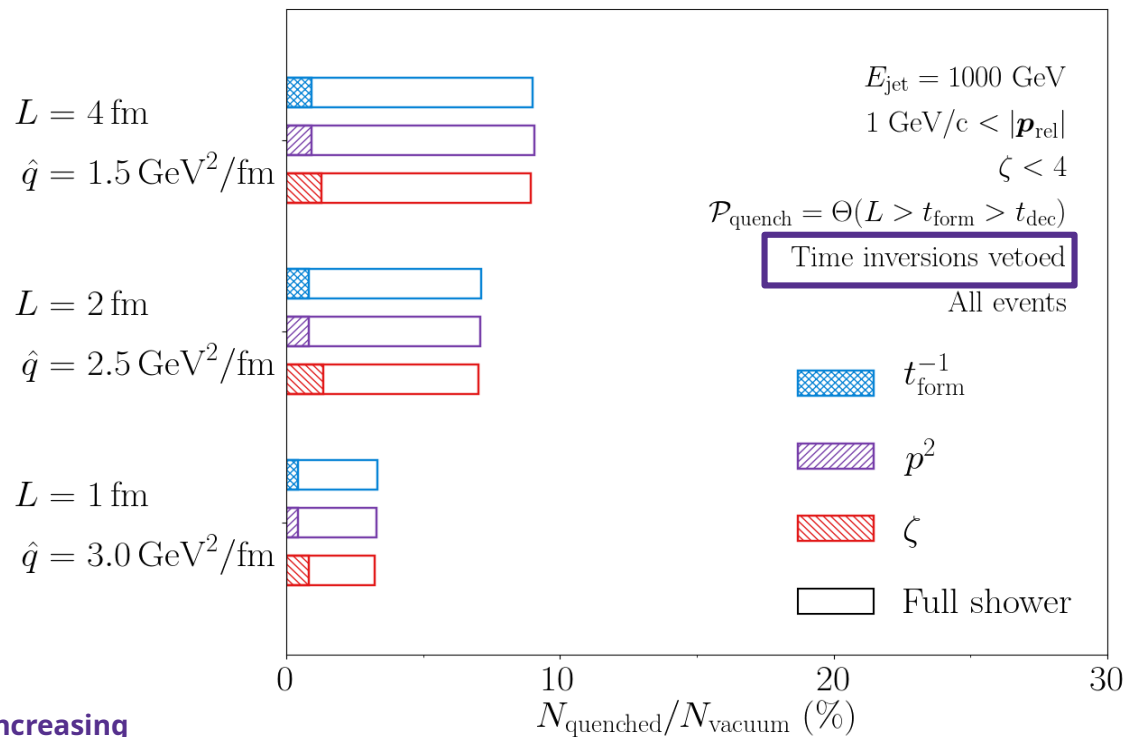
This is only one way of preventing inversions!

Fraction of Quenched Events



Vetoing the time-inversions by retrial:

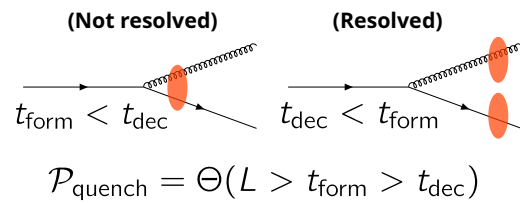
(Phase-space is adjusted splitting by splitting)



*** Time-inverted splittings are re-tried while generating the shower

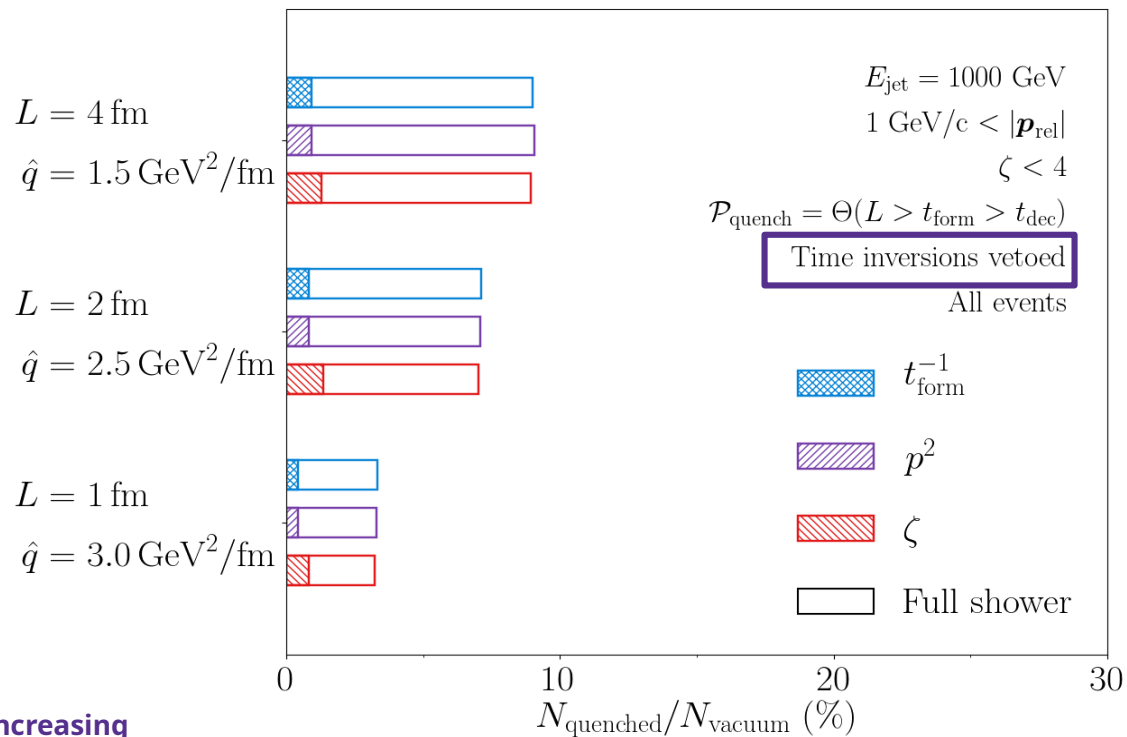
Increasing quenching effects

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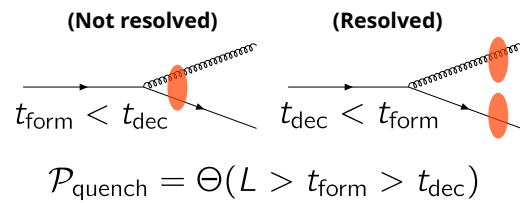
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Fraction of quenched events remains levelled across algorithms for the 'Full Branch' condition

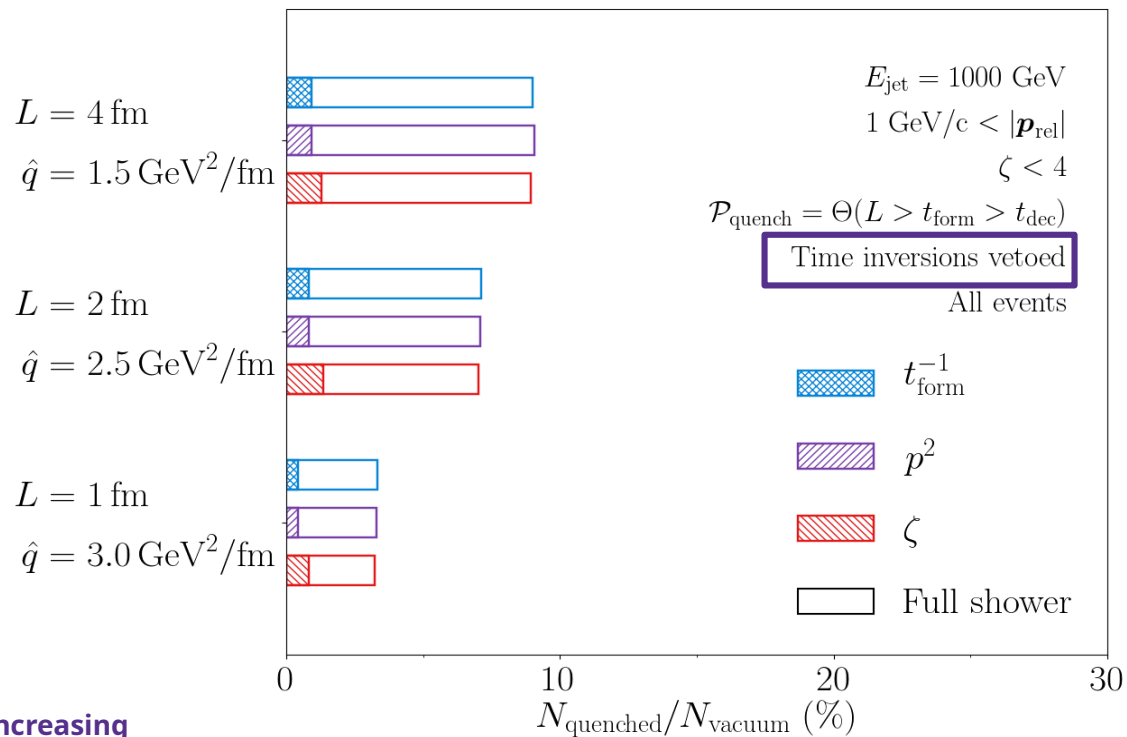
Warning: Phase-space altered splitting-by-splitting

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The implementation details of the jet interface with a time-evolving medium are crucial!

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- **A toy Monte Carlo parton shower was developed:**
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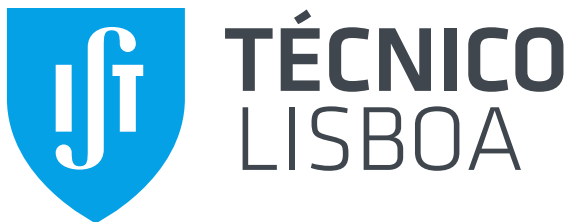
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Thanks!

Acknowledgements



European Research Council
Established by the European Commission



This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093



IGFAE
Instituto Galego de Física de Altas Enerxías



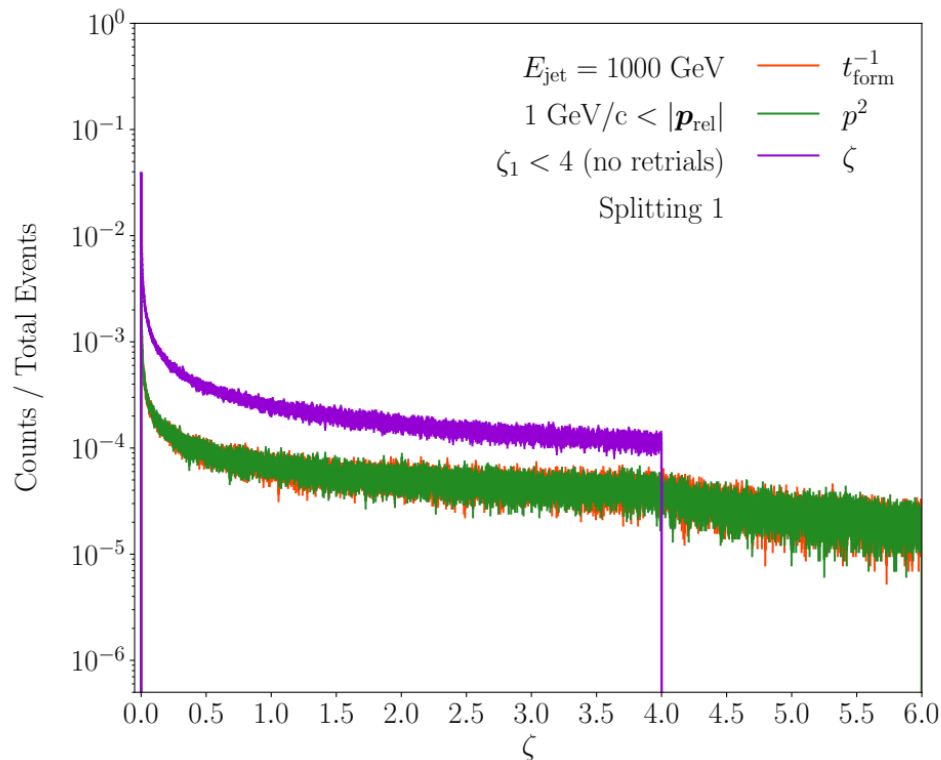
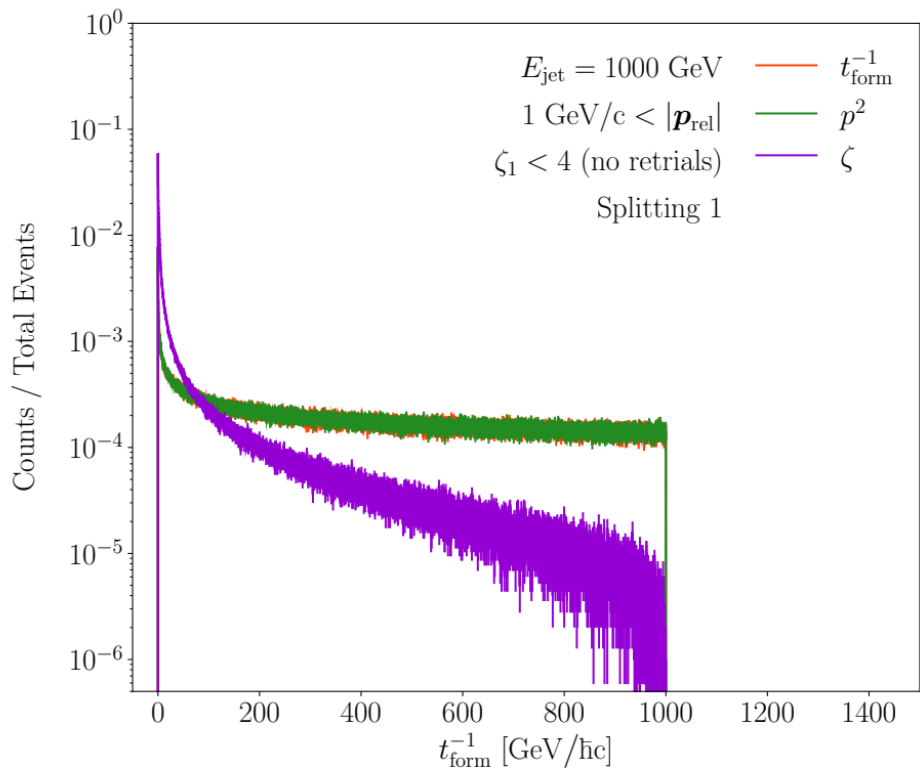
Fundação
para a Ciência
e a Tecnologia



REPÚBLICA
PORTUGUESA

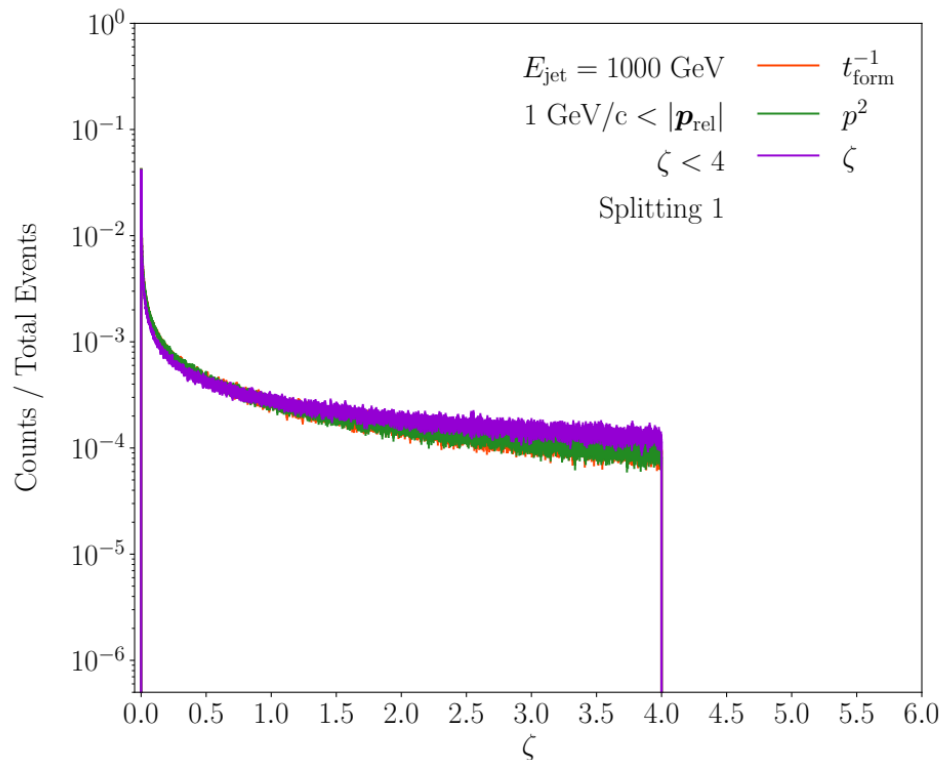
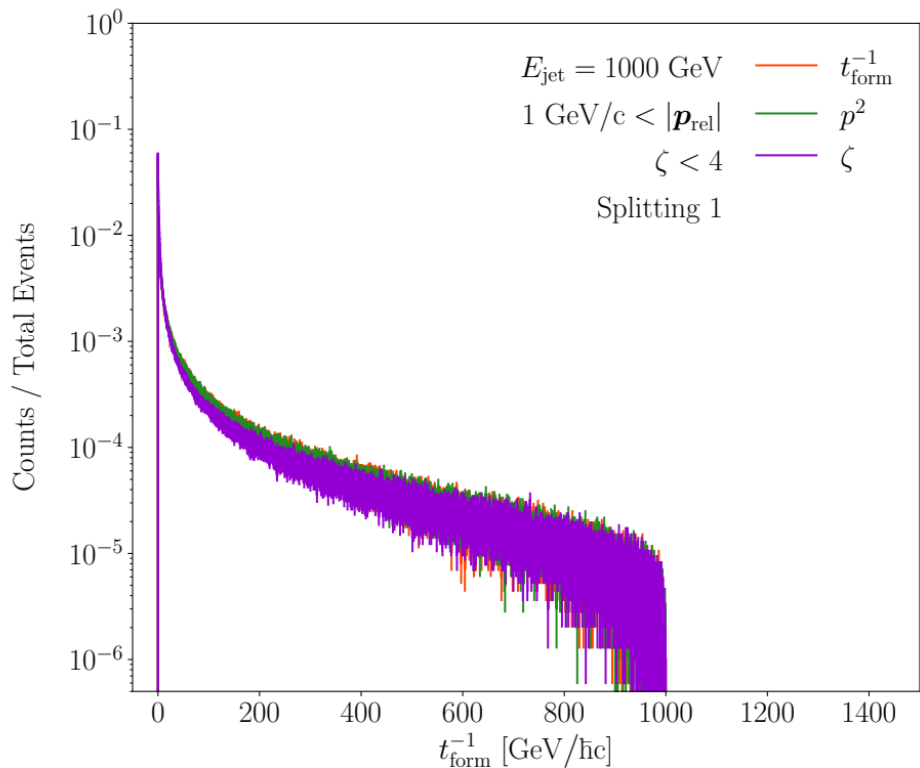
Backup Slides

Without the consistency condition



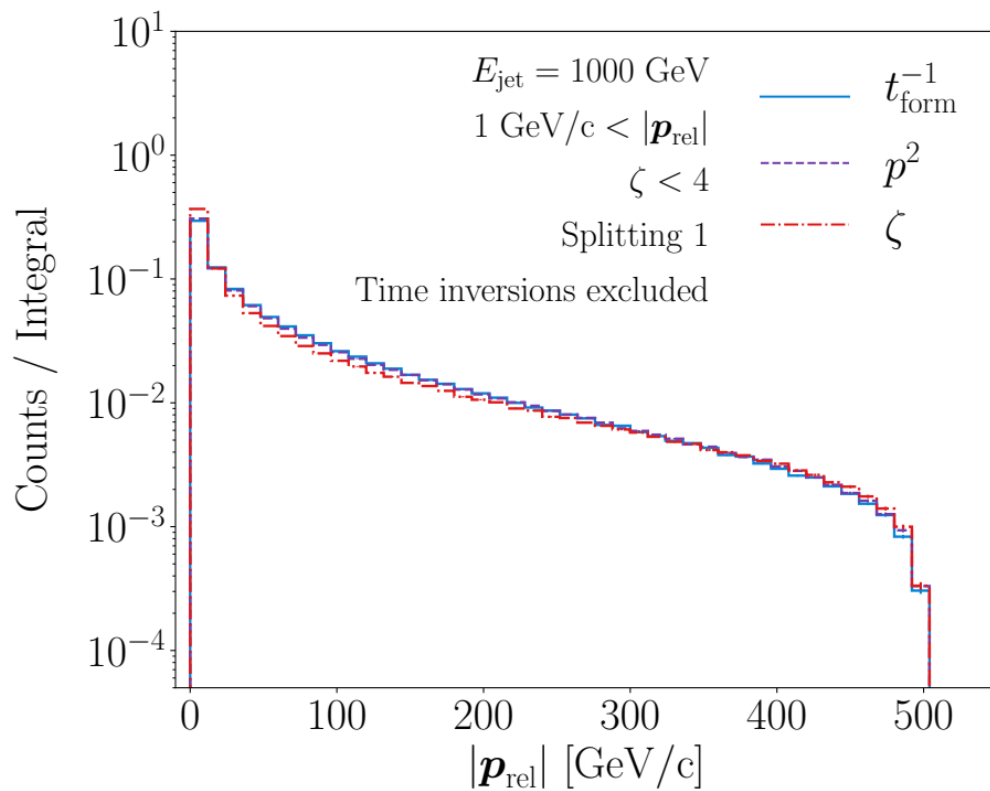
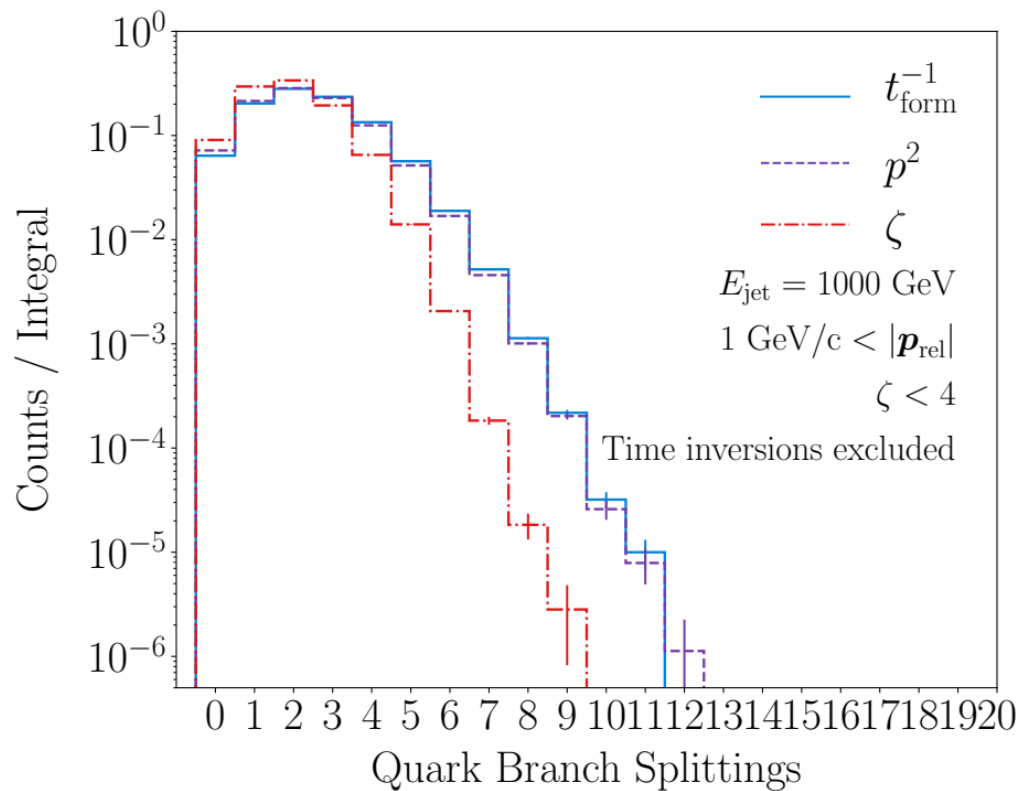
If the condition $\zeta < 4$ is used simply to initialise the angular shower, the time and angle distributions do not behave consistently across algorithms

With the consistency condition

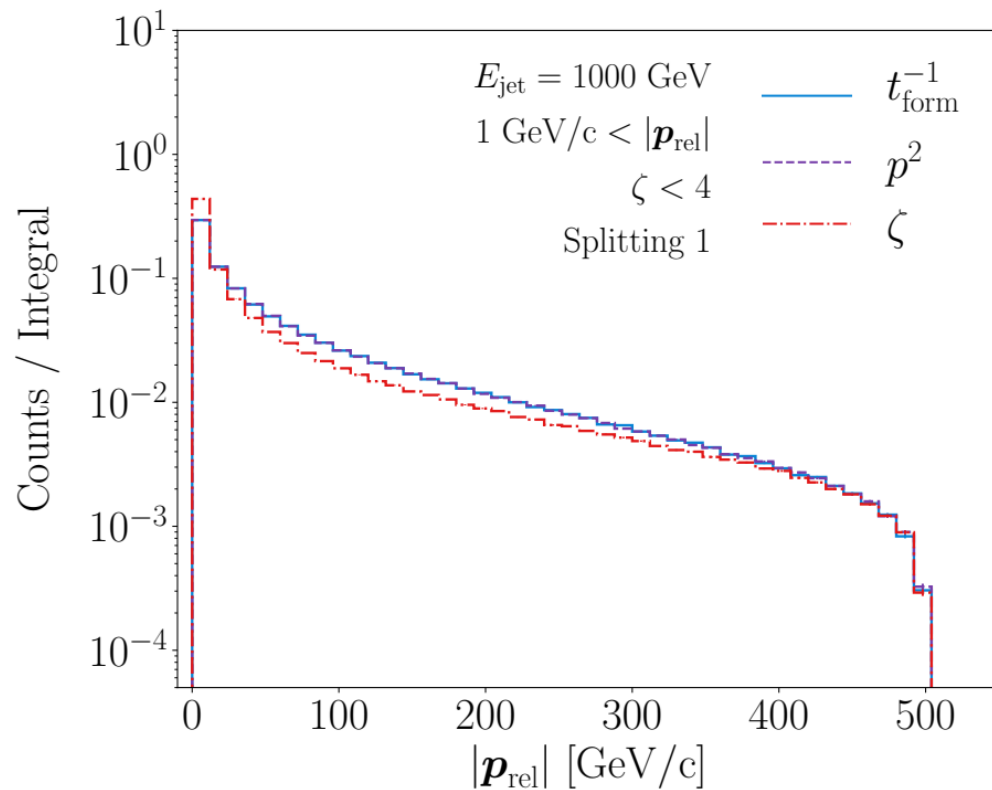
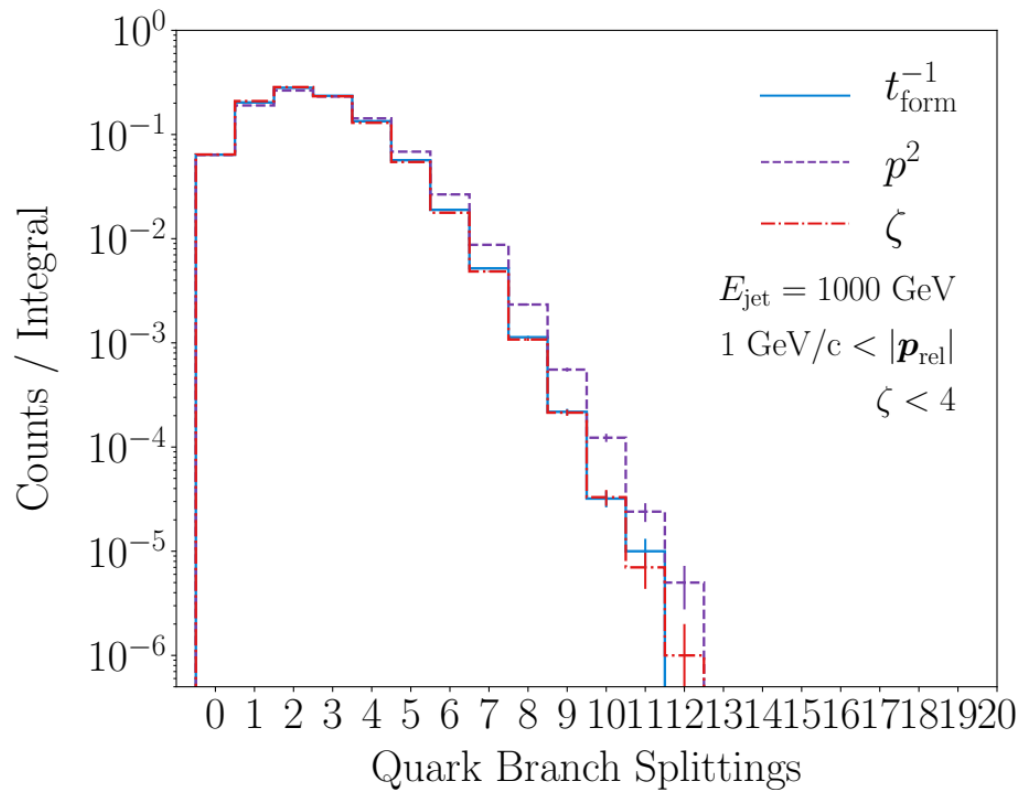


When the condition $\zeta < 4$ is used as a veto for all emissions, the distributions become consistent.

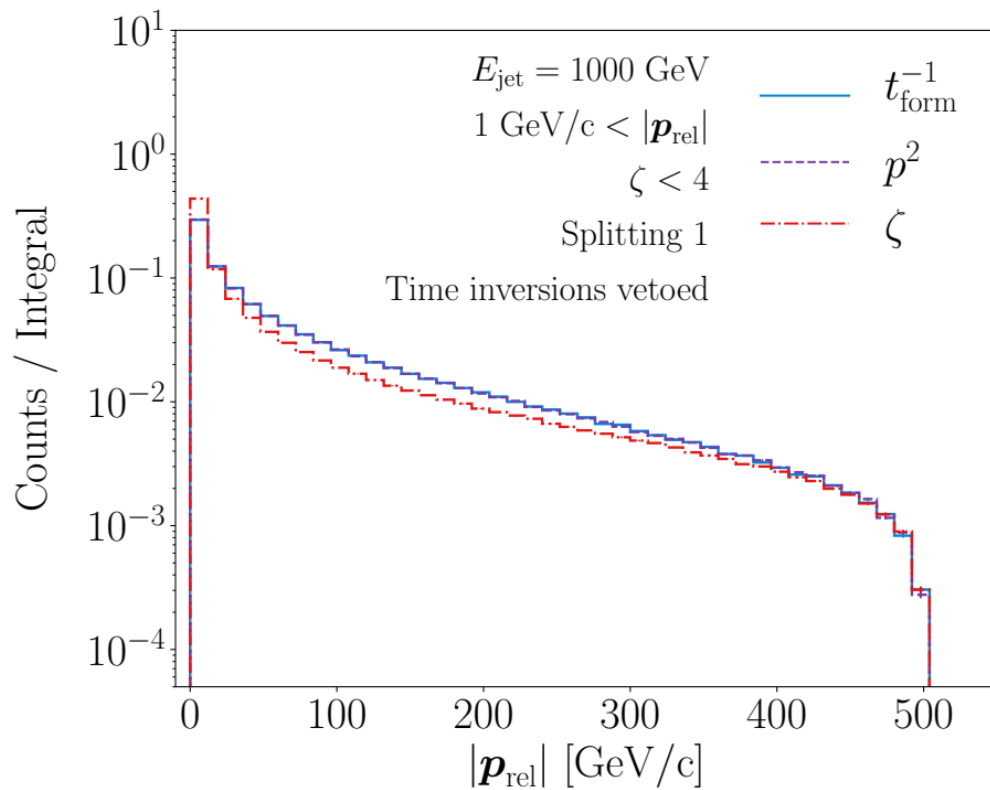
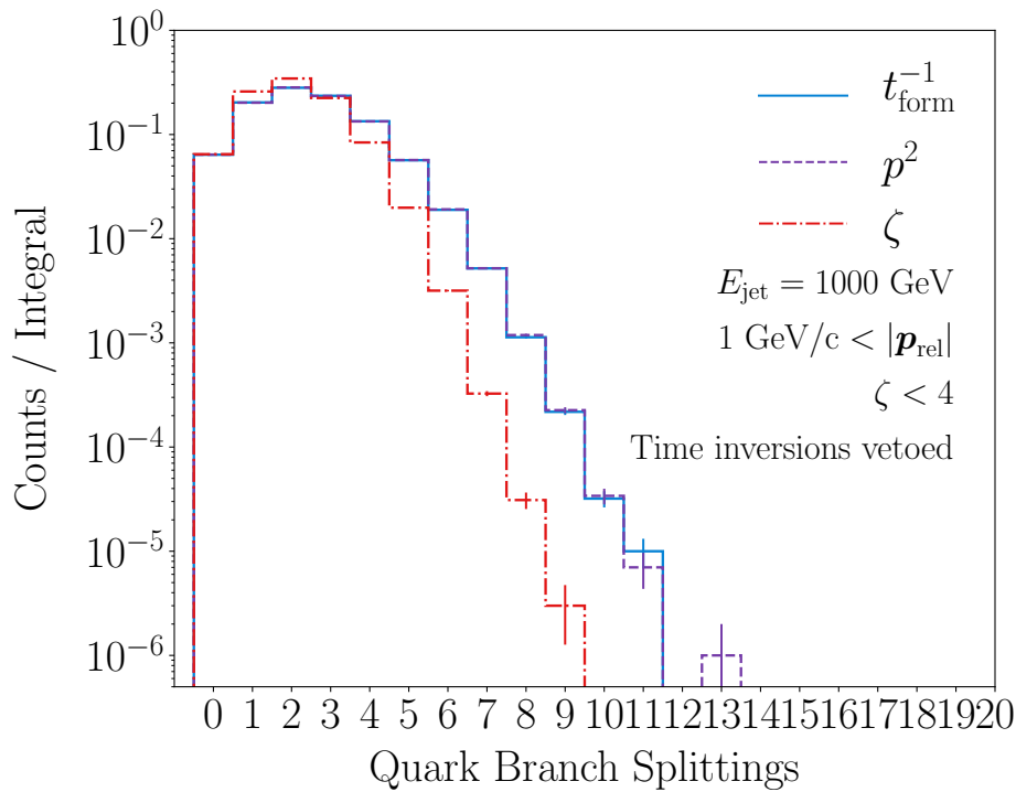
Excluding time inversions – 1D Distributions



Inclusive Sample - 1D Distributions

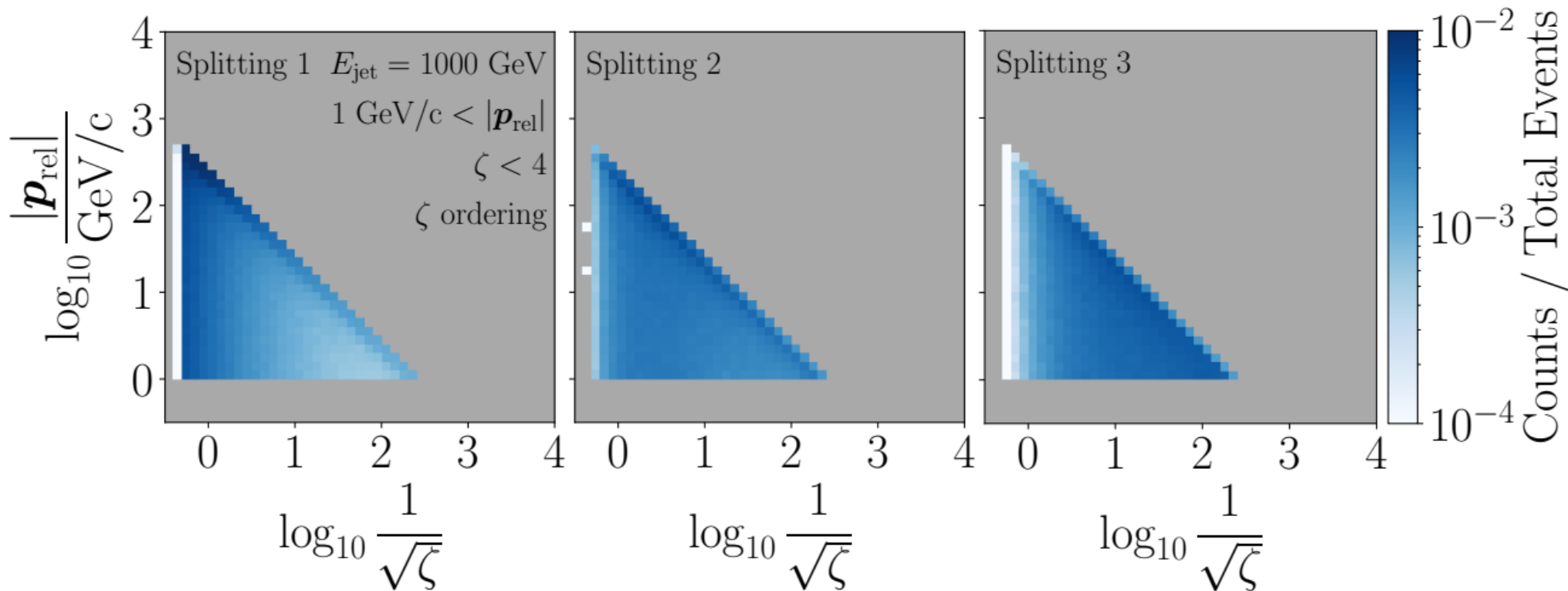


Vetoing time inversions - 1D Distributions



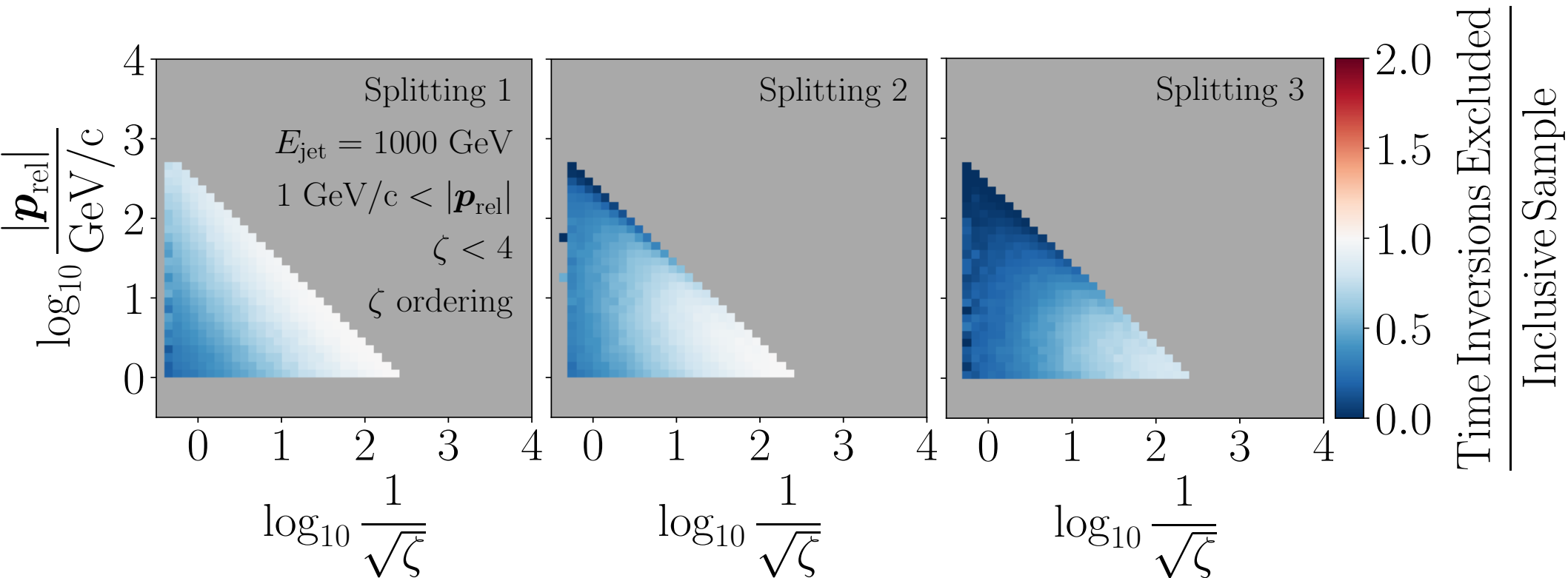
Inclusive Sample - Lund Planes

*Ordered in angle



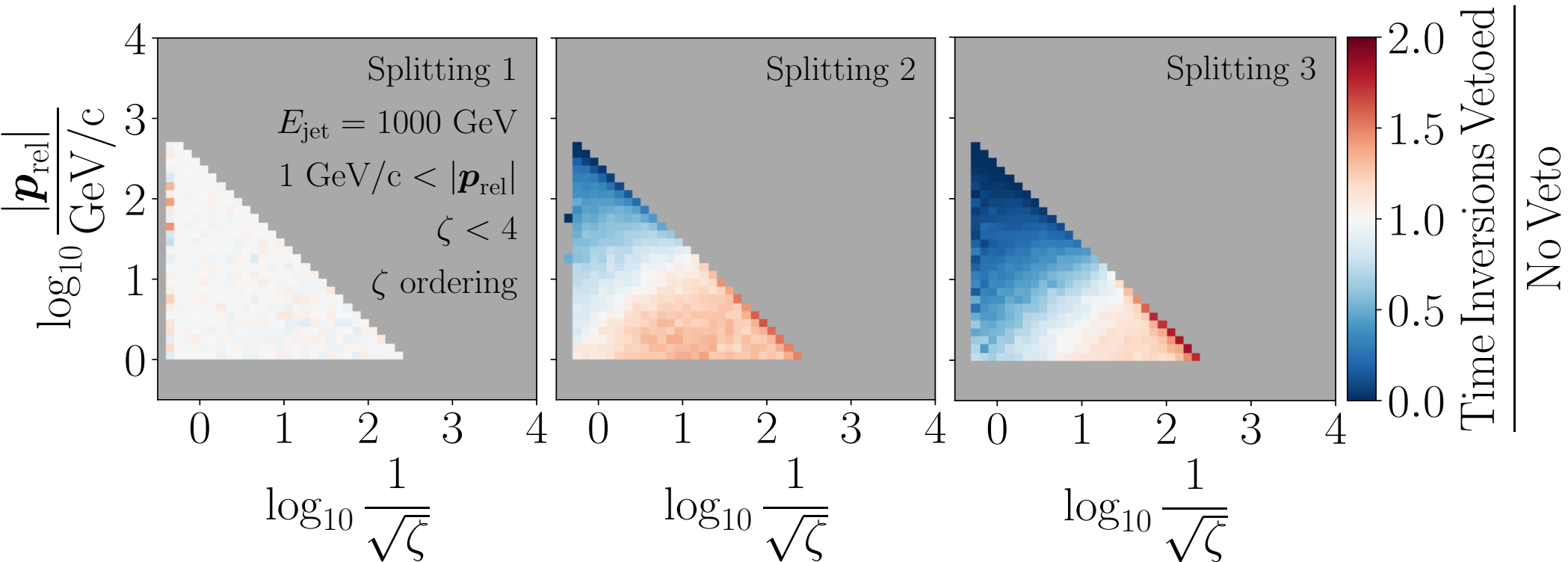
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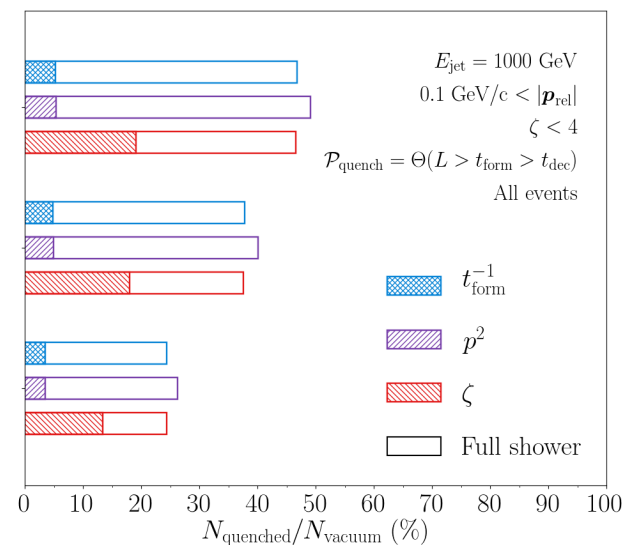
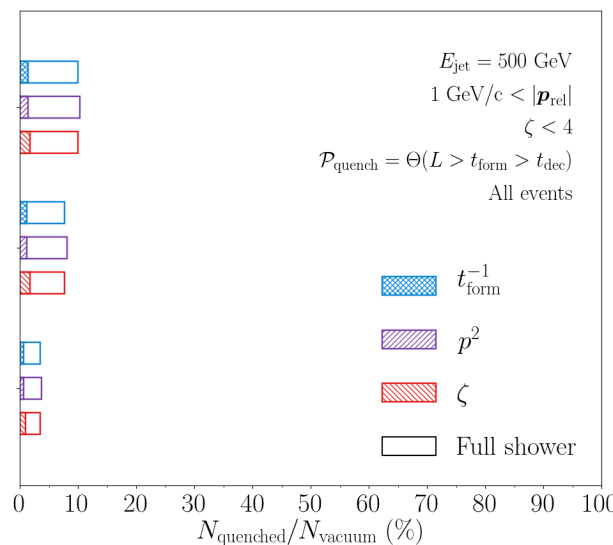
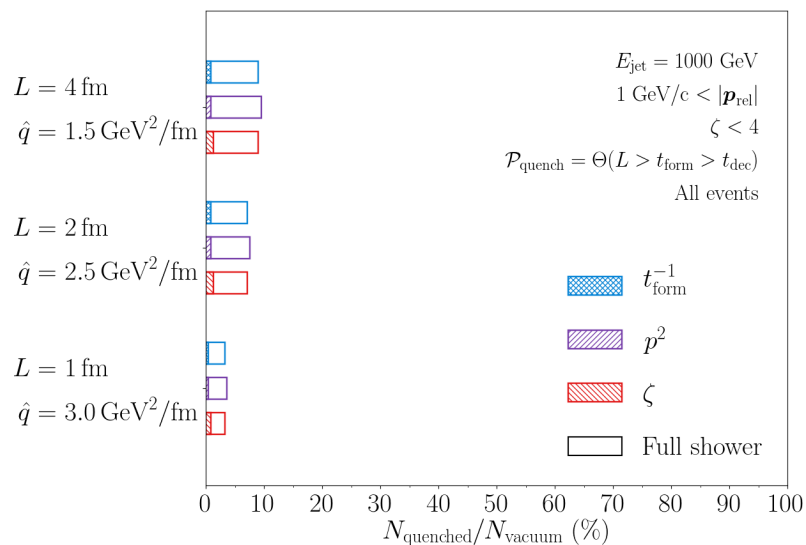


Quenching Weights

$E_{\text{jet}} = 1000 \text{ GeV}, \Lambda = 1 \text{ GeV}$

$E_{\text{jet}} = 500 \text{ GeV}$

$\Lambda = 0.1 \text{ GeV}$



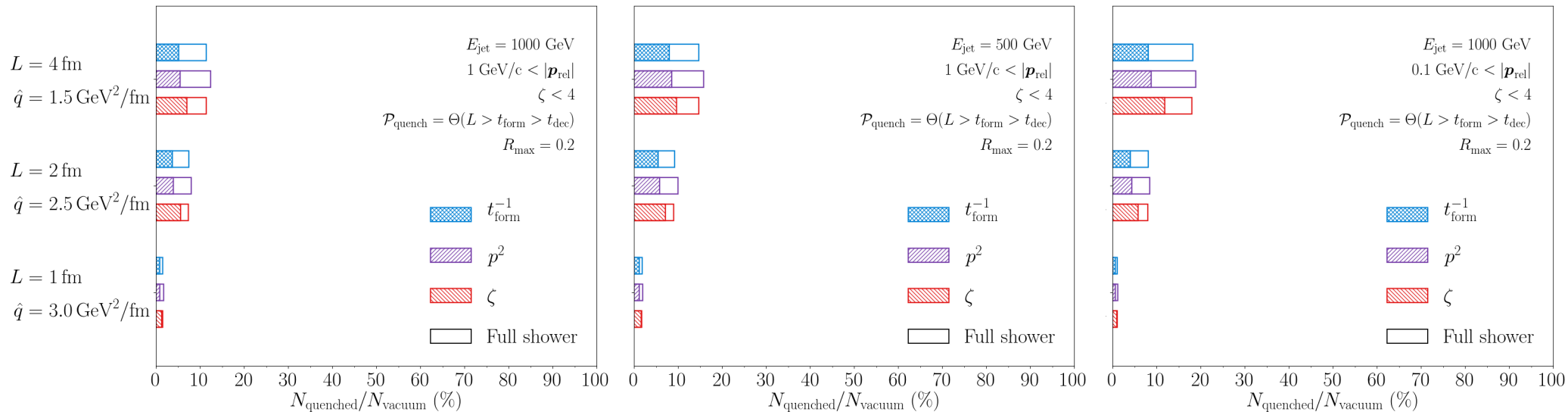
An apparent dependence on the hadronisation cutoff and initial jet energy

Quenching Weights – Radius Cut

$E_{\text{jet}} = 1000 \text{ GeV}, \Lambda = 1 \text{ GeV}$

$E_{\text{jet}} = 500 \text{ GeV}$

$\Lambda = 0.1 \text{ GeV}$



Cut all events whose quark branch has a splitting wider than $R_{\text{max}} = 0.2$
- This defines the new vacuum sample, and the quenching model is applied on top of this cut

An aggressive cut, but it returns independence of E_{jet} and Λ .