

Anisotropic Jet Broadening and the $R_{AA} \times v_2$ Puzzle

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ECT*
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J. Bahder



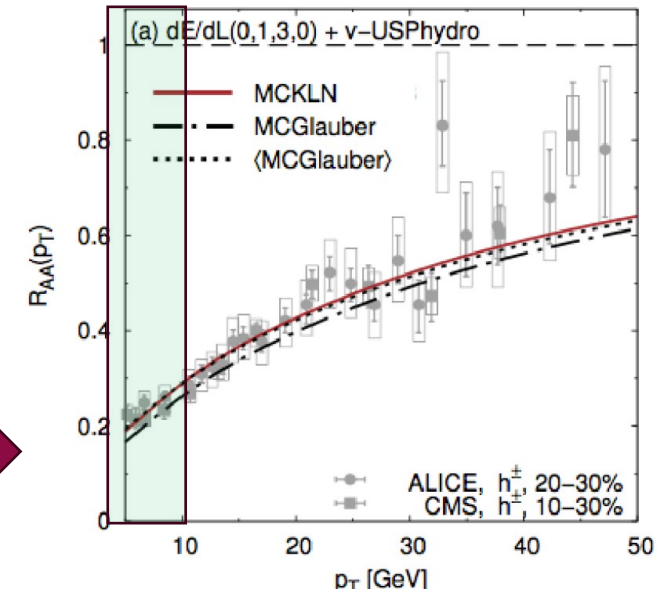
In collaboration with Hasan
Rahman, Dr. Matthew Sievert, and Dr.
Ivan Vitev



Coupled Observables & the $R_{AA} \times v_2$ Puzzle

- Coupled descriptions are more discriminating
 - a simultaneous description of the observables with a single model
- pQCD models of $R_{AA} \times v_2$
 - Enduring challenge...
 - Success: $p_T > 10$ GeV
 - Failure: $1 \text{ GeV} < p_T < 10 \text{ GeV}$
 - Underpredicted anisotropic flow for well-behaved R_{AA}
 - Something is missing!

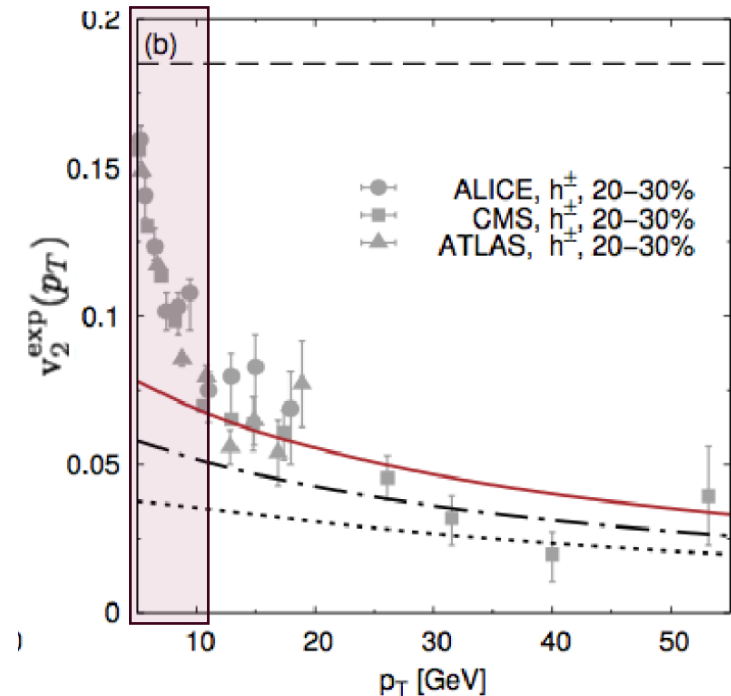
R_{AA} Good!
Down to $p_T > 5$ GeV



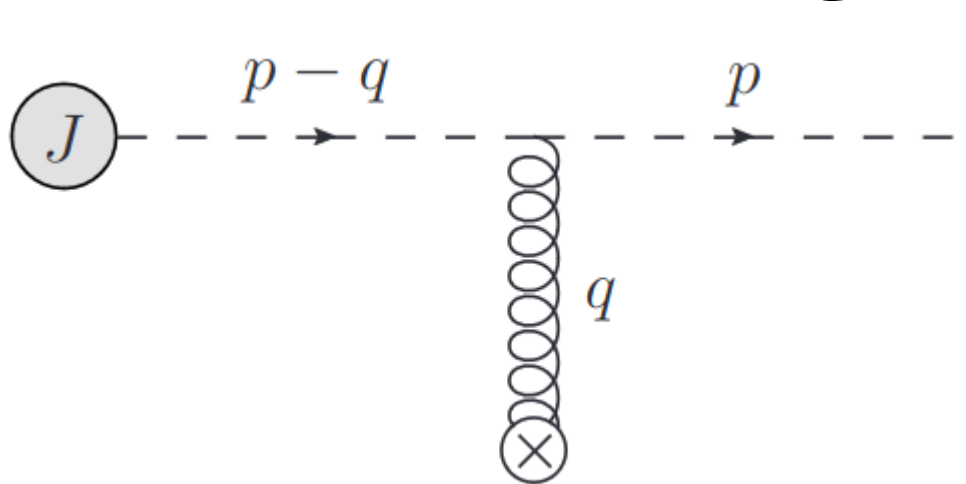
Noronha-Hostler et al:
([arXiv: 1602.03788](https://arxiv.org/abs/1602.03788))

Missing v_2 !!!

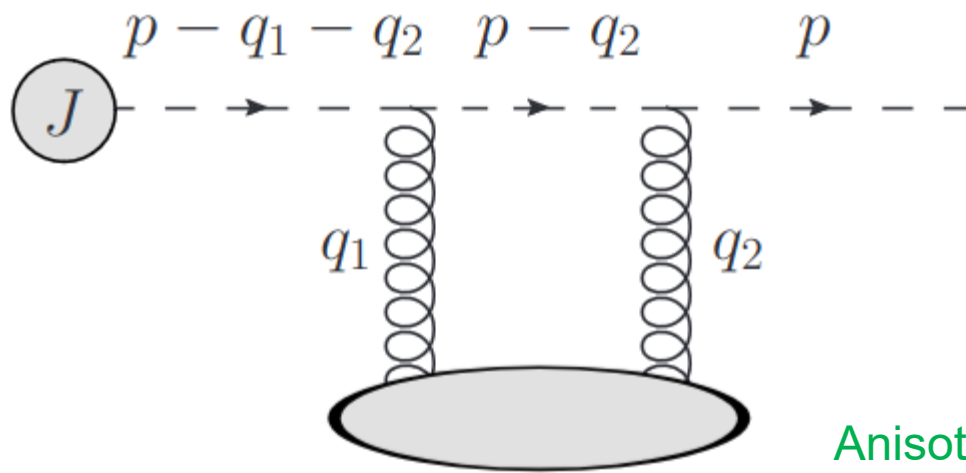
Suspiciously only around
 $p_T < 10$ GeV



Jet Broadening – Isotropic vs Anisotropic



A. V. Sadofyev, I. Vitev,
& M. D. Sievert
Phys.Rev.D 104 (2021)
([arXiv:2104.09513](https://arxiv.org/abs/2104.09513))



Anisotropic

$$g a_i^{\mu a}(q) = t_i^a u_i^\mu v_i(q) (2\pi) \delta(q^0 - \mathbf{u}_i \cdot \mathbf{q})$$

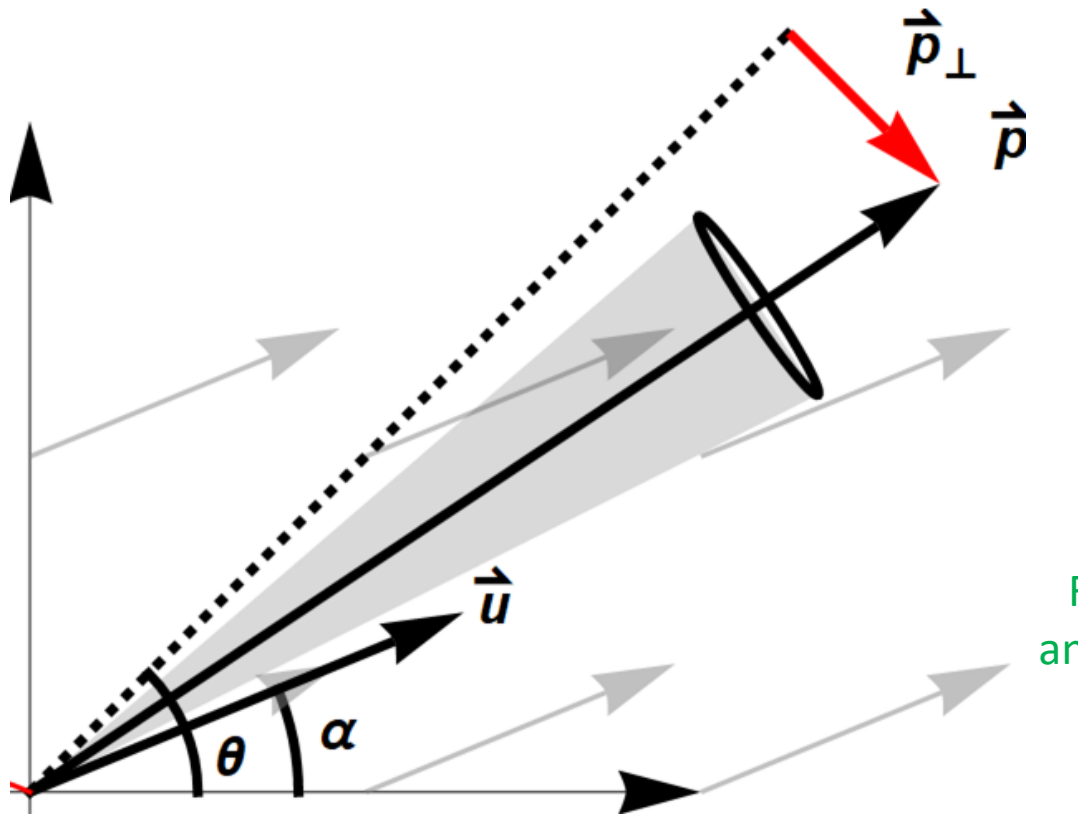
Preferred direction!

$$a_i^{\mu a}(q) = g^{\mu+} (t^a)_i \left[2\pi \delta(q^+) \right] \left[\frac{-g_{eff}}{q_T^2} \right]$$

No vector info

- Difference in setup – constraints on external gluon field
- Isotropic
 - Jet quark moves lightcone (+), medium quark moves lightcone (-)
- Anisotropic
 - Jet quark moves lightcone (+), medium quark moves with medium flow
- Two vector directions associated with the medium
 - Flow
 - Gradients

Anisotropic Jet Broadening: "Jet Drift"



Flow enhanced
and flow direction
controlled

$$\langle \vec{q}_{drift} \rangle = \hat{e}_\perp \int d\tau \begin{array}{|c|c|c|c|} \hline 3 & \mu^2(\tau) & \ln \frac{E(\tau)}{\mu(\tau)} & \frac{u_\perp(\tau)}{1 - u_\parallel(\tau)} \\ \hline E(\tau) & \lambda(\tau) & & \\ \hline \end{array}$$

$$\begin{aligned} \frac{1}{\lambda} &= \sigma \rho \\ \rho &\propto T^3 \\ \mu &\propto T \end{aligned}$$

- "New" class of pQCD effects: asymmetric / anisotropic
- Flow-Mediated Drift
 - Preferential broadening in direction of medium flow
- Can use analytic approximation to discuss "trajectory of the average"
- L. Antiporda, J. Bahder, H. Rahman & M. D. Sievert
 - Jet Drift Analytic Phenomenology
 - Phys.Rev.D 105 (2022) ([arXiv: 2110.03590](https://arxiv.org/abs/2110.03590))

Energy suppressed

Temperature Enhanced

Anisotropic Jet Broadening: Flow-Gradient Mediated

Quadratic in Pathlength

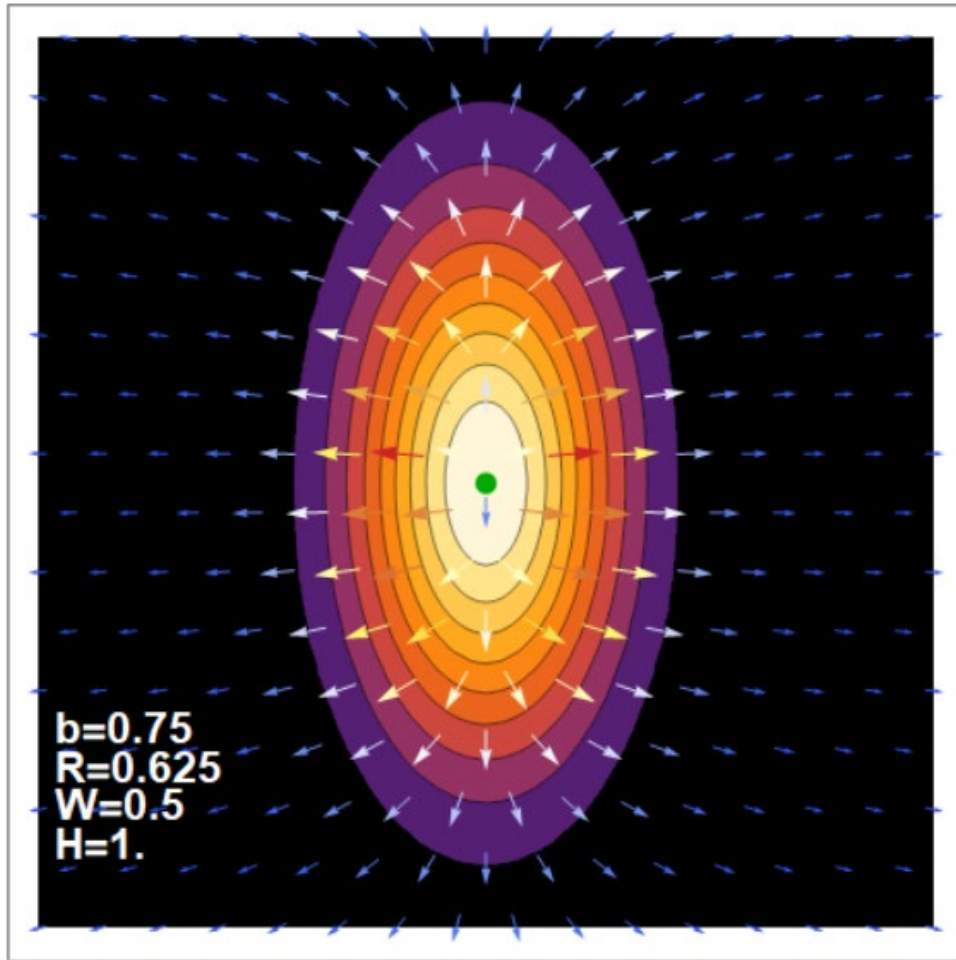
Energy suppressed

Flow enhanced
and flow direction
modulated

- Mixed Flow-Gradient-Mediated Drift
 - Phenomenology follows flow-mediated drift
 - Small effect in isolation, couples to enhance flow-mediated drift
- A backseat player for now

$$\begin{aligned}
 \langle \vec{q}_{fgdrift} \rangle = & -\frac{3(2\pi)^2 g^2}{2} \int_0^L dz z \frac{1}{\lambda} \\
 & \times \left[((\nabla_{\perp} T) u_{\perp}) \frac{u_{\perp}}{(1-u_z)^2} \left(3T \ln \left(\frac{E}{gT} \right) - T \right) \right. \\
 & + \nabla_{\perp} u_z \left(\frac{2}{(1-u_z)^3} \right) u_{\perp} T^2 \ln \left(\frac{E}{gT} \right) \\
 & \left. + \nabla_{\perp} u_{\perp} \frac{2u_{\perp}}{(1-u_z)^2} T^2 \ln \left(\frac{E}{gT} \right) \right]
 \end{aligned}$$

Elliptical Media =?= Elliptic Modulation



$$T(x, y) = T_0 \exp \left[-\frac{x^2}{2\sigma_x^2} \right] \exp \left[-\frac{y^2}{2\sigma_y^2} \right]$$

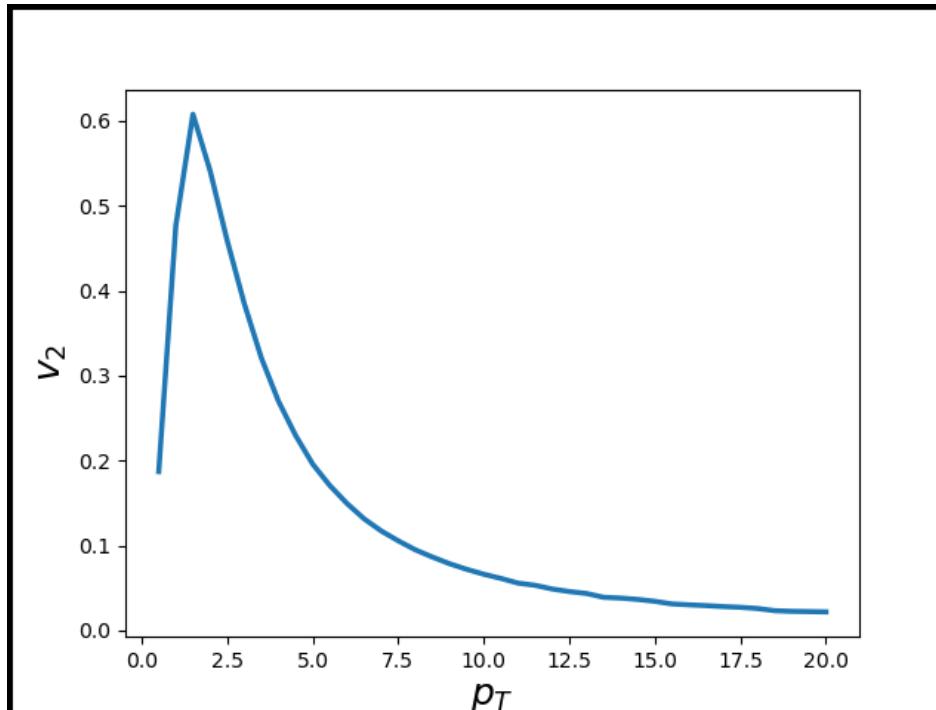
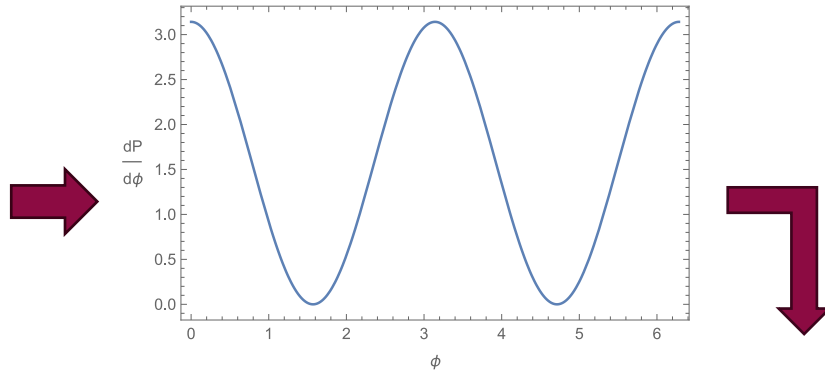
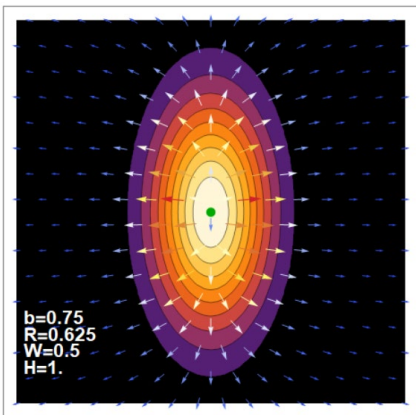
$$\vec{u}(x, y) = u_0 \sqrt{\sigma_y \sigma_x} \left(\frac{x}{\sigma_x^2} \hat{i} + \frac{y}{\sigma_y^2} \hat{j} \right) \exp \left[-\frac{x^2}{2\sigma_x^2} \right] \exp \left[-\frac{y^2}{2\sigma_y^2} \right]$$

$$W(b) = 2\sigma_x = 2R - b,$$

$$H(b) = 2\sigma_y = \sqrt{4R^2 - b^2}$$

- 2D Gaussian Temperature & Flow
- Take an angular sweep of hard partons,
- Compute R_{AA} and v_2 for various p_T
 - Drop all scale factors
(no physical scale for medium)

Drift Couples to Event Geometry

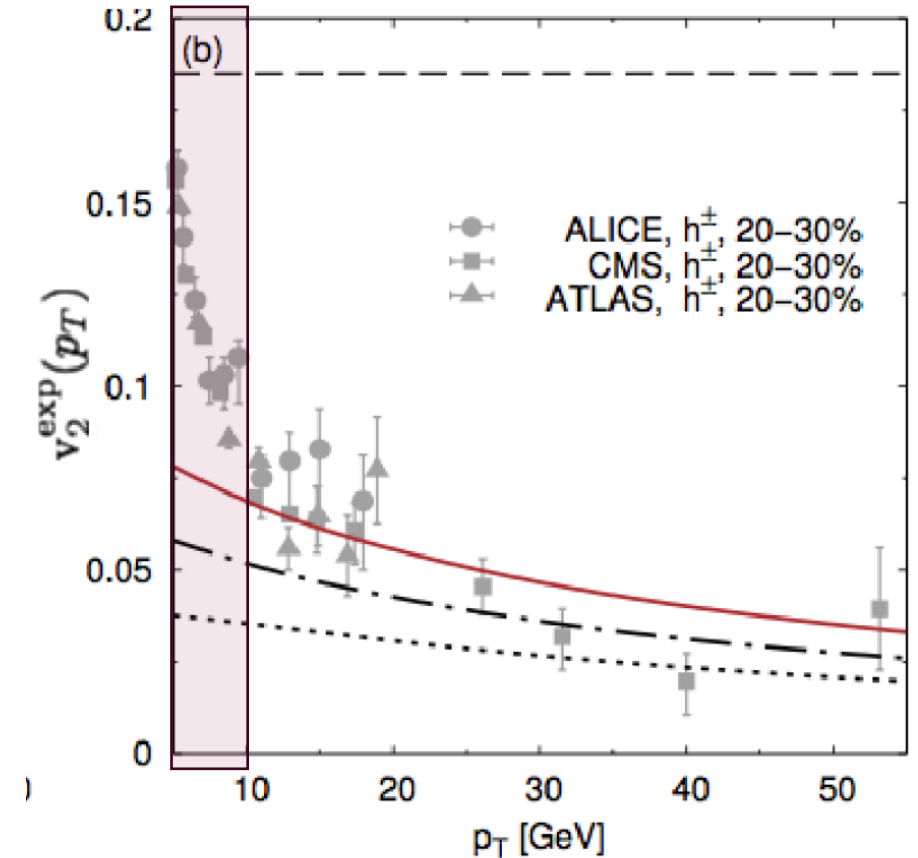


- Drift strength arbitrarily scaled for visual effect
 - Jet p_T dependence accurate
- Elliptic modulation: additional v_2 !
 - Drift is strongest at low p_T , matching missing v_2
 - $(1/E) \log(E)$ behavior in p_T
- Review:
 - Missing v_2 , $p_T < 10$ GeV
 - Jet Drift enhances v_2 , $p_T < 10$ GeV
 - ... Suspicious, no?

The Well-Trodden: Elliptic Flow from Energy Loss

Noronha-Hostler et al:
([arXiv: 1602.03788](https://arxiv.org/abs/1602.03788))

- Need an energy loss model to address $R_{AA}(x) v_2$ puzzle
 - Jet quenching responsible for elliptic flow - $p_T > 10$ GeV
 - Implement analytic approximation to first-order GLV energy loss
- Jet quenching goes roughly quadratically in pathlength
 - Enhances energy suppressed drift at late times
- Largest flow values likely seen by jets at late times near plasma "wavefront"



$$\langle q_{GLV}(\tau) \rangle = -\frac{C_R \alpha_s}{\pi} \int_{\tau_0}^{\infty} d\tau \frac{\mu^2(\tau)}{\lambda(\tau)} (\tau - \tau_0) \ln \left(\frac{E(\tau)}{\mu(\tau)} \right)$$

Vitev: ([arXiv:0012092](https://arxiv.org/abs/0012092))

Vision to Study Realistic Drift

Test effect of addition of jet drift to realistic event-by-event jet-medium simulations on $R_{AA}(x) v_2$ puzzle

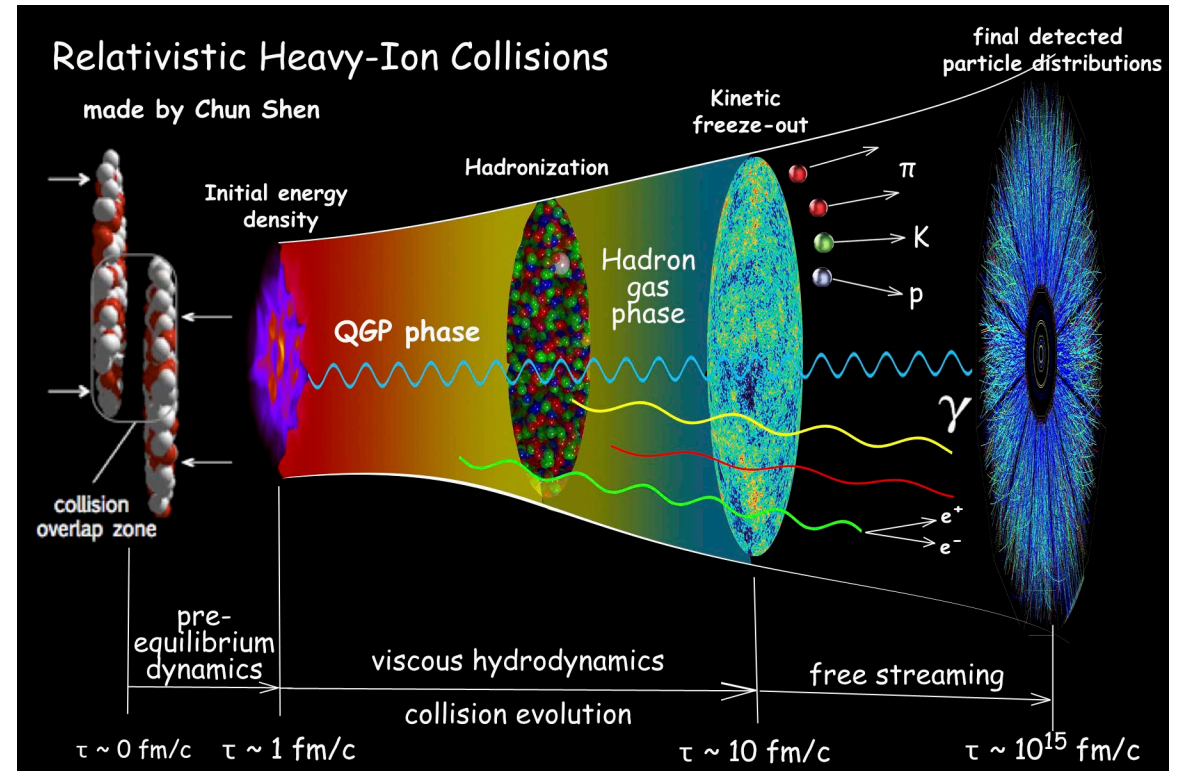
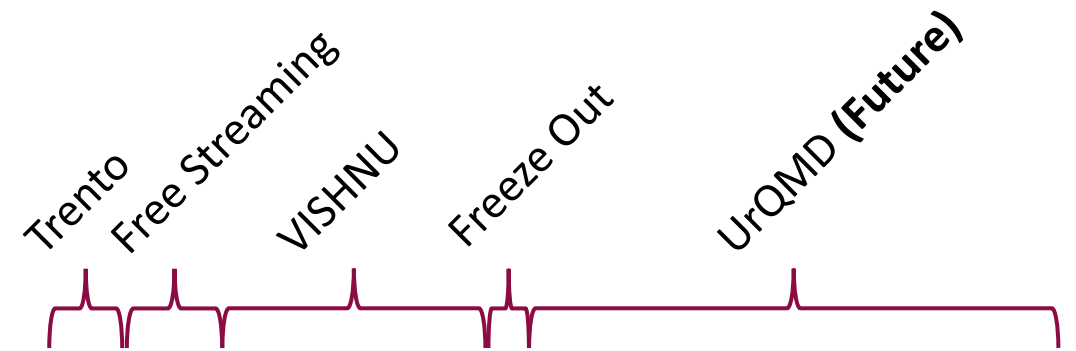
- Realistic 2+1D model of QGP temperature and flow
- Perturbative energy loss model
- Perturbative drift model
- Differential treatment of jet trajectories
- Fragmentation to observable particles
- Experimental-Type R_{AA} and v_2 measurements

Medium Model

Duke QCD – “hic-eventgen”

- Initial HIC Conditions (Trento)
 - Initial energy densities
- Free streaming
 - Generating initial flow in the pre-equilibrium phase from gradients
- Hydrodynamics (VISHNU)
 - Relativistic Fluid Eqs. -> EMT Conservation
- Freezeout
 - Cooper-Frye particlization sampler

“hic-eventgen”
[arXiv:1804.06469](https://arxiv.org/abs/1804.06469)
[GitHub](#)

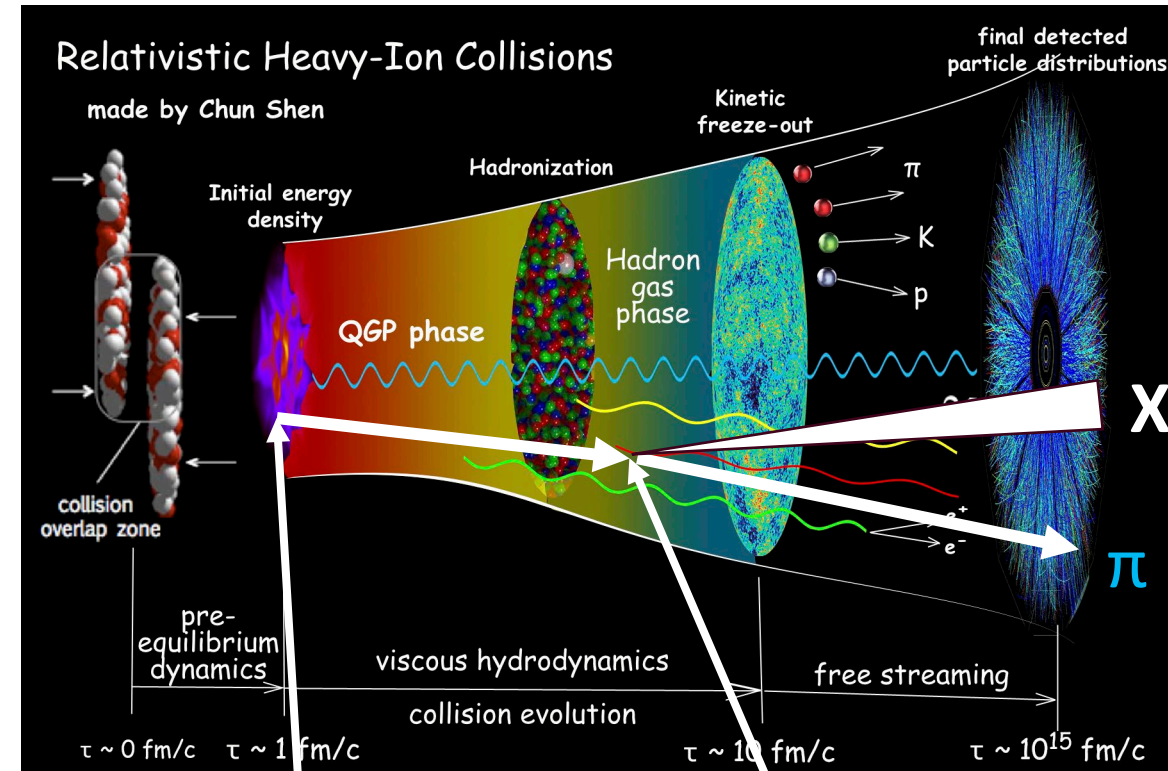
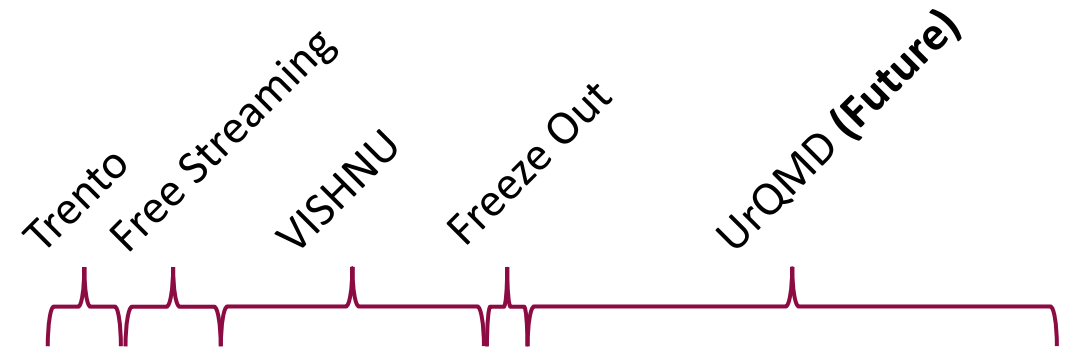


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JMA Jet Model

([GitHub](#))

- Jet Physics Wrapper overtop "hic-eventgen"
- Partonic Scattering Inputs (Pythia & CNM Theory)
 - Jet production from pp hard partonic scatterings
 - Theoretical cold nuclear matter effects from saturation theory
- Parton Propagation in QGP (EL & Drift Theory)
 - Jet energy loss & drift applied to pA products
- Fragmentation
 - Event-by-event Sampling of Fragmentation Functions for hadron momentum fraction

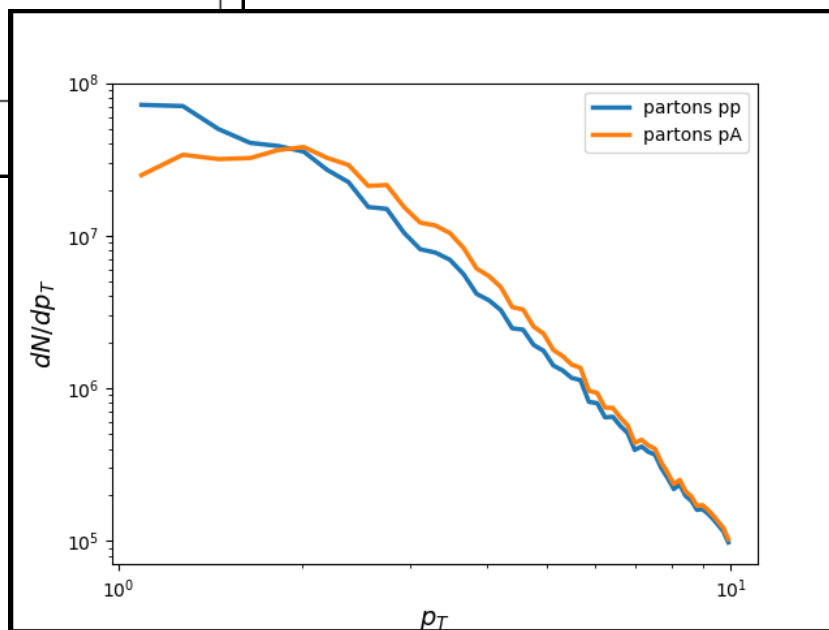
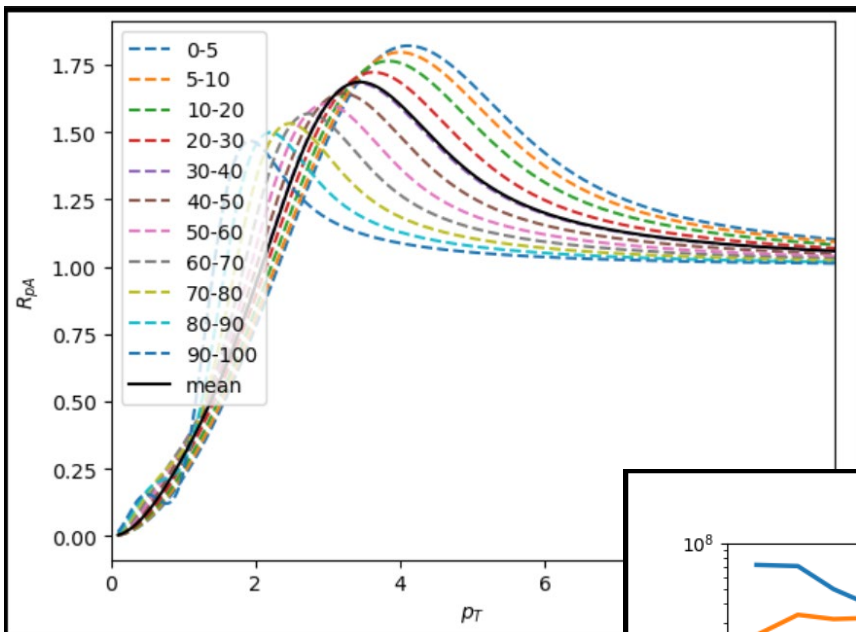


Chun Shen / O.S.U / VISHNU Collaboration

[Pythia](#) Hard Scattering
& Theoretical CNM Effects

Fragmentation

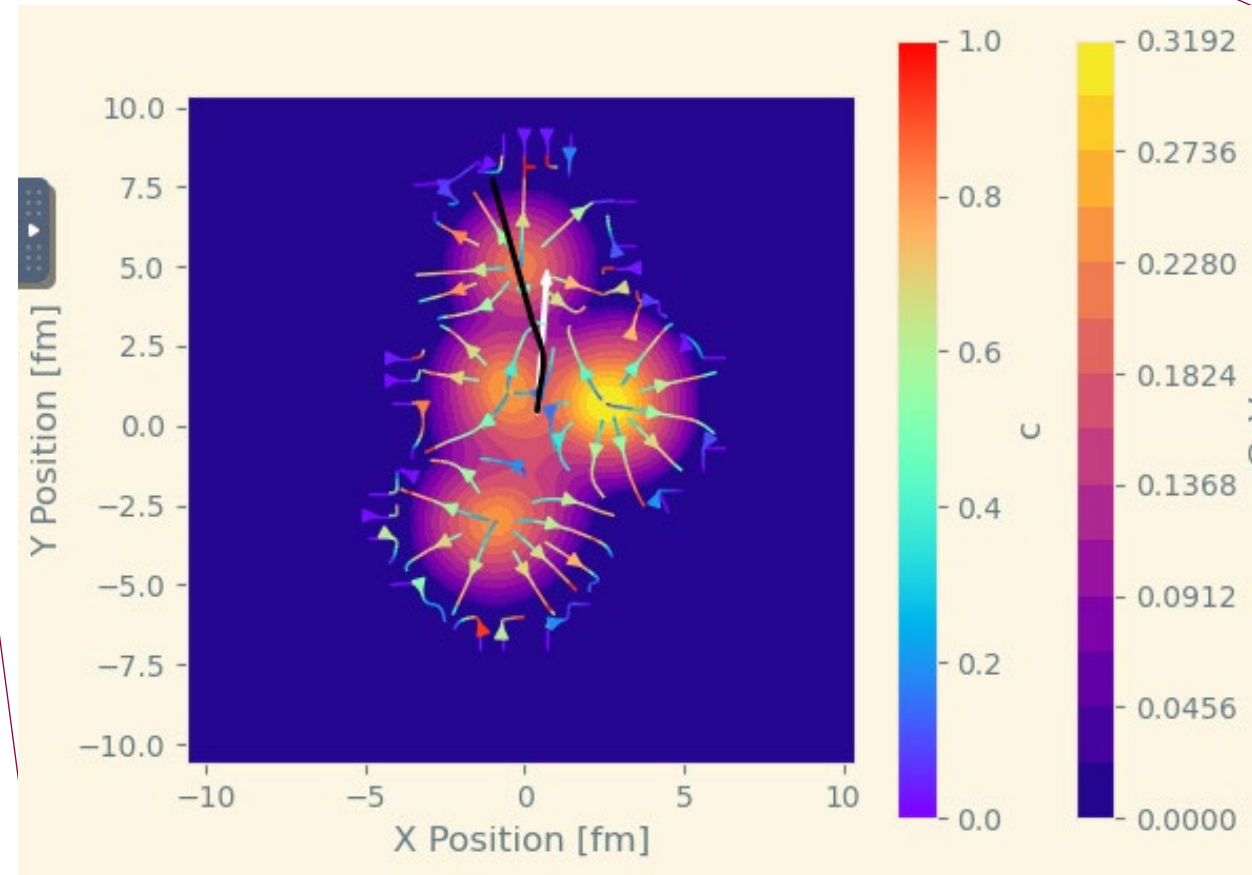
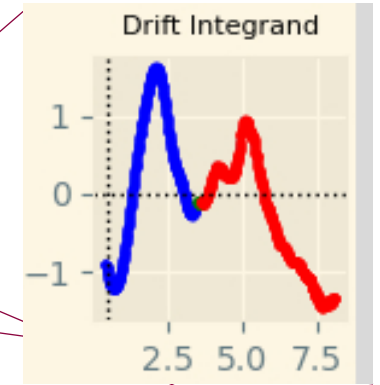
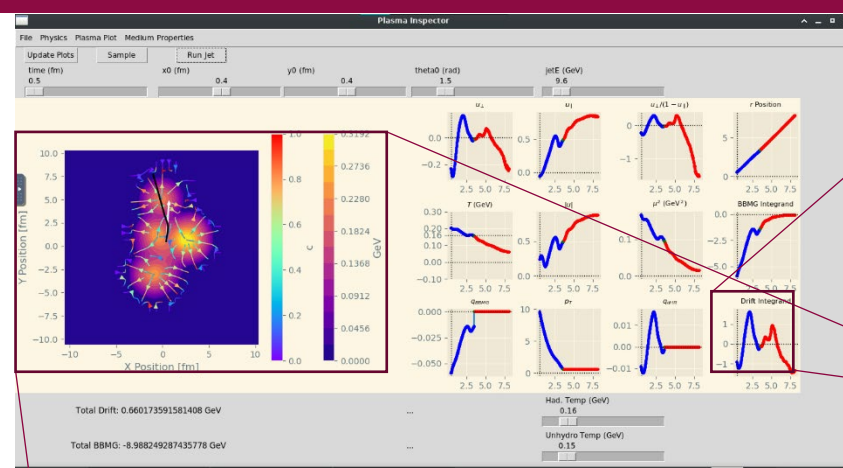
Jet Distribution & Cronin Effect



- pp jet distribution from [Pythia](#) pp collisions @ 5.02 TeV
- All events 2->2 partonic hard products
 - Dijets (before QGP effects)
 - Light quarks & gluons
 - Access to dijet observables
- R_{pA} computed from saturation theory
 - ([arXiv: 0307037](#))
 - Two parameter, flexible form
 - Needs modification for gluon jets...
 - **Especially important for drift!**

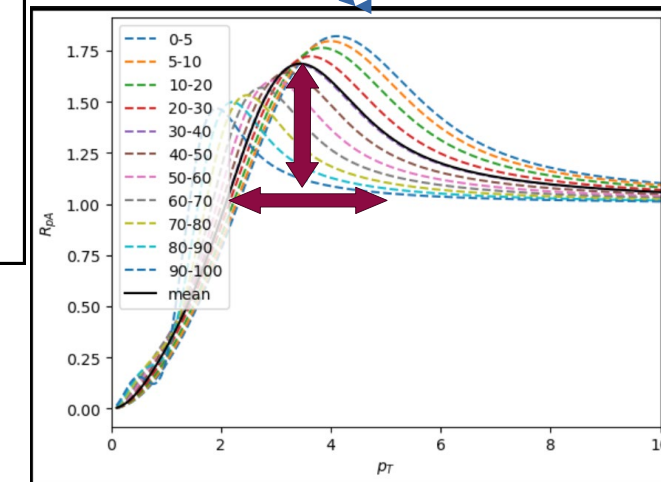
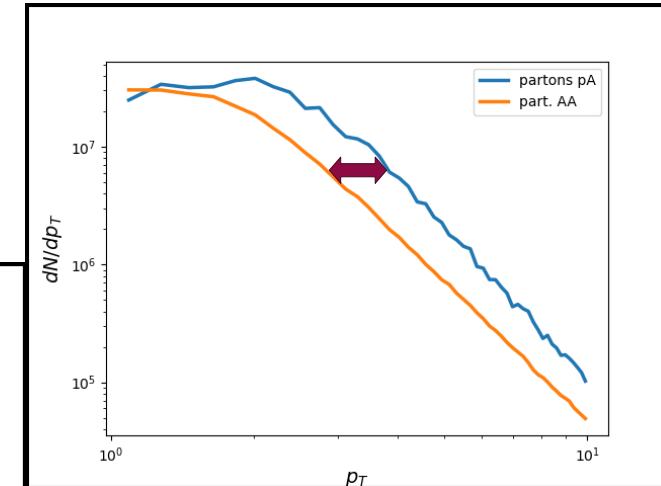
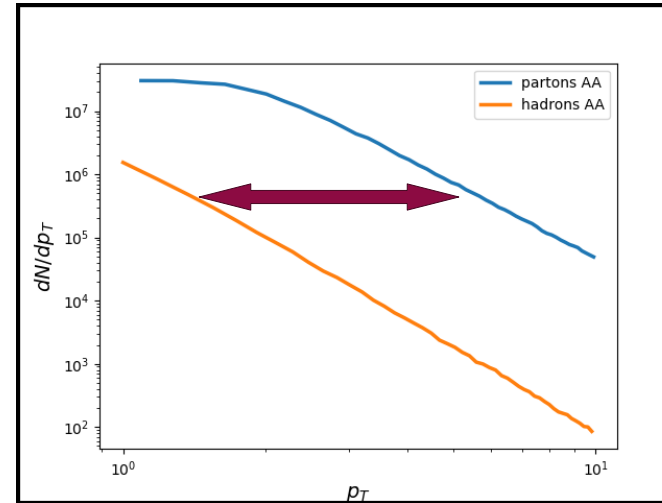
JMA Jet Trajectories

- Hard partons - not “jets”
 - Uncontrolled factorization of hadronization from jet-medium int.
- Jet trajectories
 - Binary collision density weighting of production points
 - Computed within QGP phase of hydro backgrounds
 - EL & Drift cut off at $T < 155$ MeV



On Free Parameters

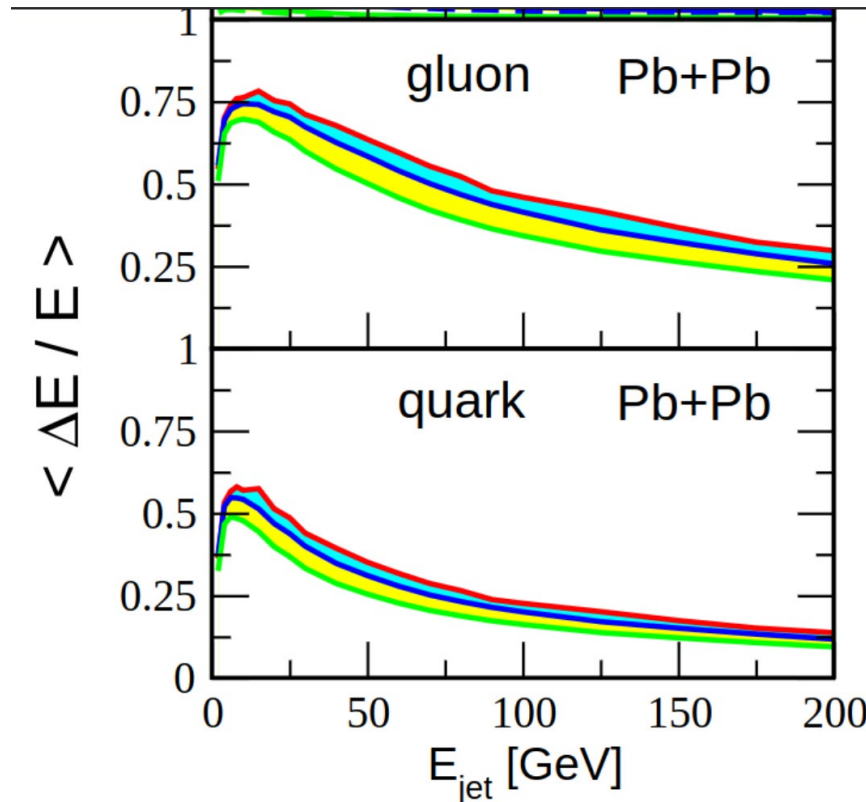
- DukeQCD “hic-eventgen” medium model parameters set by Bayesian parameter estimation
 - ([arXiv:1804.06469](https://arxiv.org/abs/1804.06469))
- Jet spectra set by choice of scattering & CNM theory
 - Pythia tuned to pp data
 - 2 parameter CNM analytic model
- Jet-medium interaction theory fully defined by coupling
- Fragmentation
 - Choice of fragmentation functions
 - Very non-trivial



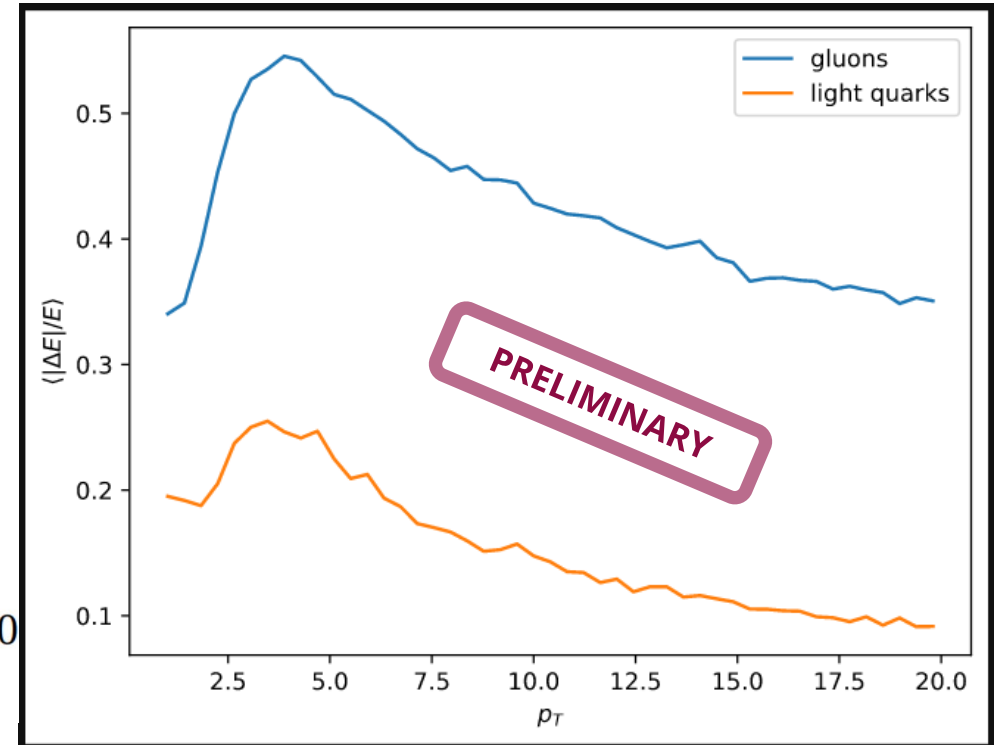
Effect Strengths - EL

- Compare JMA (right) to perturbative simulation results in Woods-Saxon Glauber models (left)

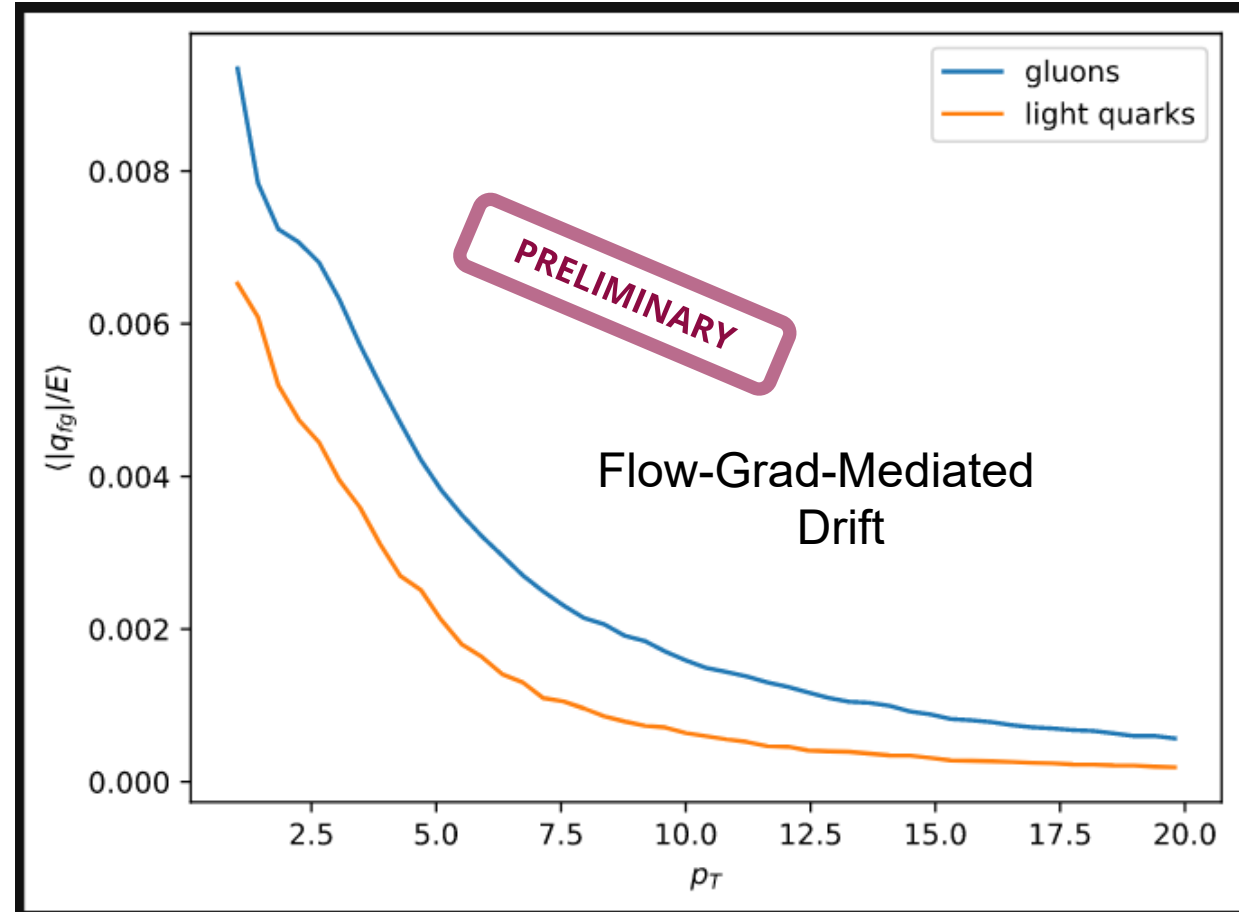
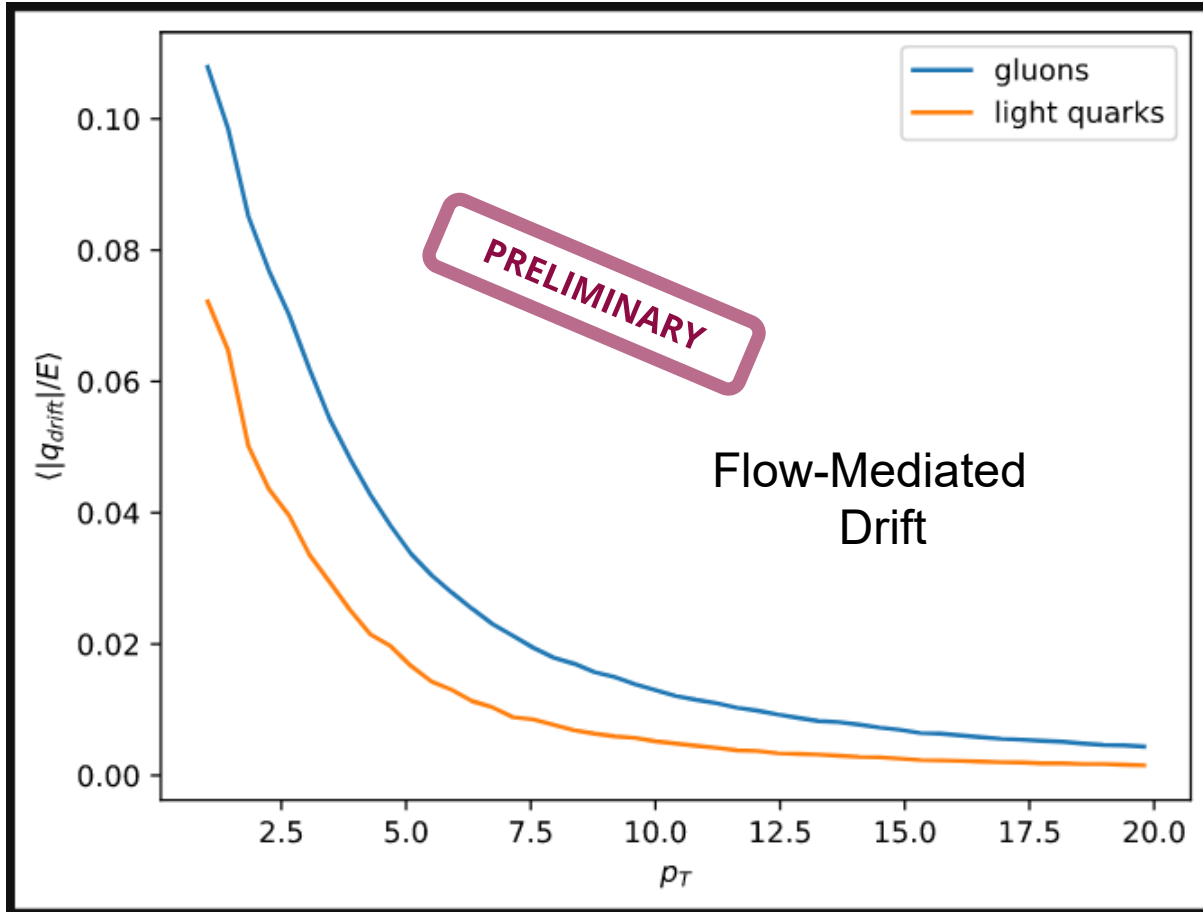
- Mismatch to simple analyses
 - Red Flag!
- Wait to see R_{AA}
- More details shortly



[arXiv:0603010](https://arxiv.org/abs/0603010)



Effect Strengths – Flow & Flow-Grad Drift

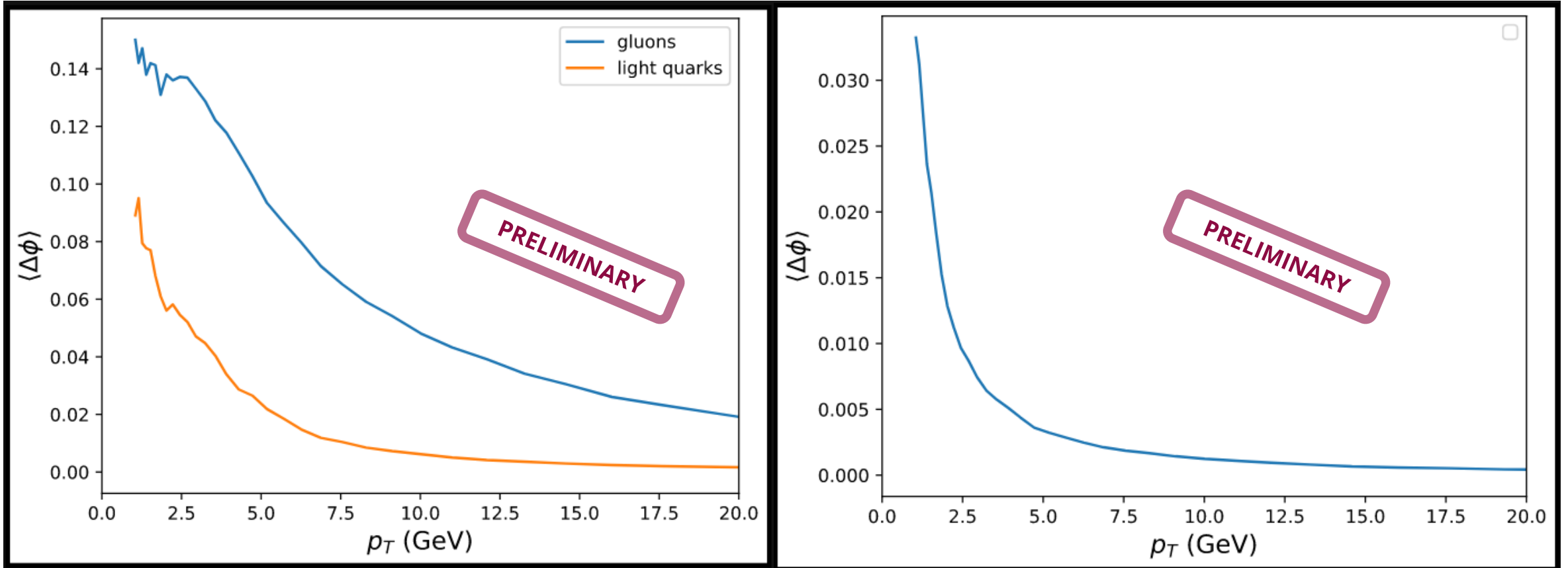


- No other perturbative simulation for comparison
- We will evaluate when we talk v_2 !

Note y-axes scale difference left to right panel



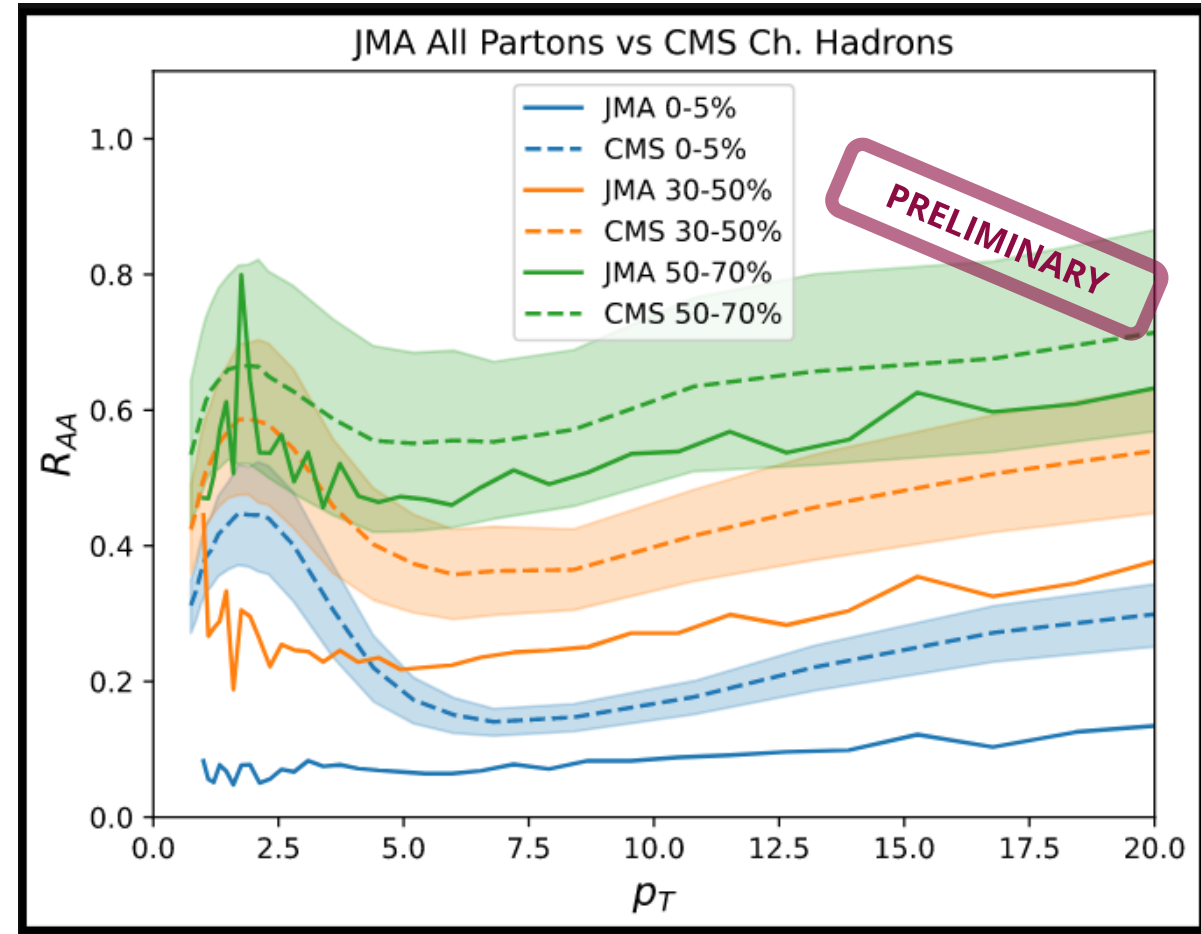
Typical Deflections



- Some deflections are experimentally measurable! (0.1 rad \approx 5.7 deg)
 - Anecdotally: experimentalists have said 5 deg is measurable
 - Note: Deflections binned in *partonic* p_T
- **Large numbers of hard partons experience measurable drift deflection!**
- Fragmentation seems to wash out much of the effect

R_{AA} Insights - Partonic

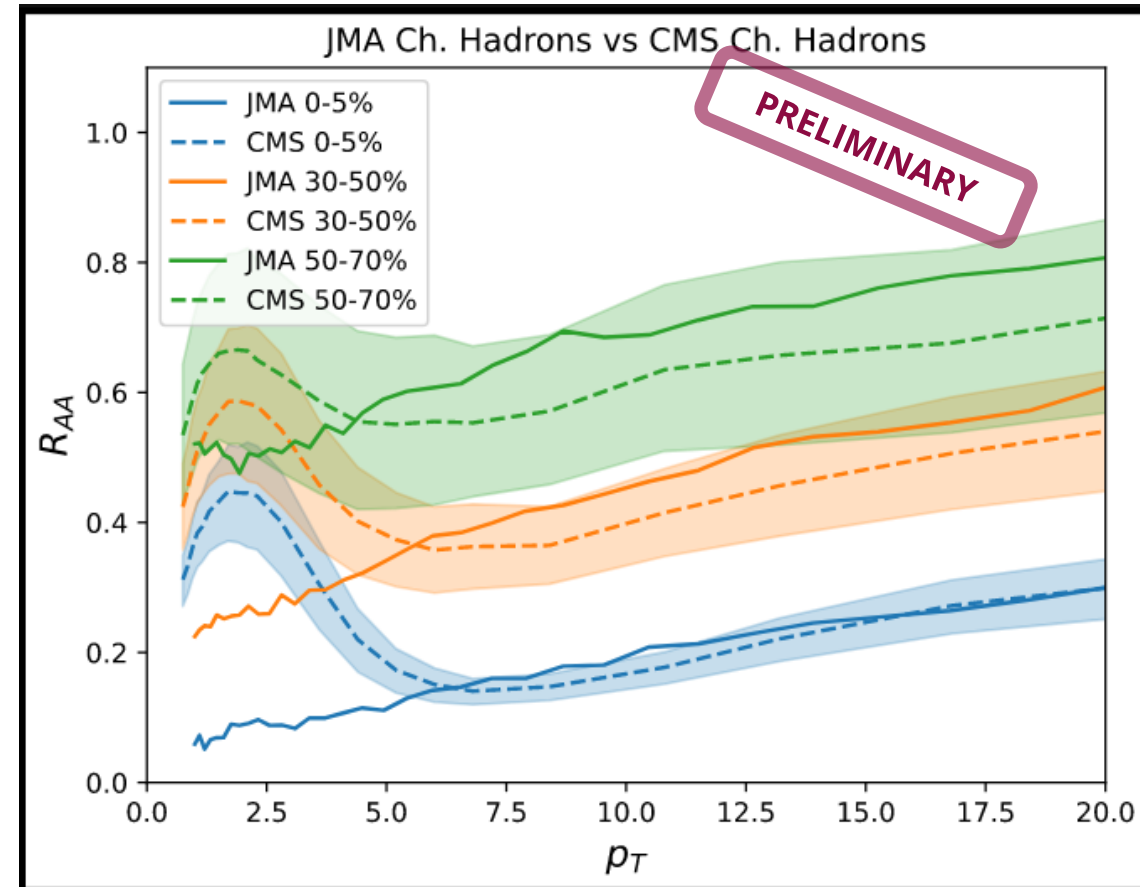
- General behavior in the right ballpark
 - Scale of suppression reduced after fragmentation
- “Low end” of hard p_T R_{AA} structure
 - Probably some sort of nonperturbative / other physics driving R_{AA}
 - Small upturn due to CNM effects



CMS: <https://doi.org/10.17182/hepdata.77101.v2>

R_{AA} Insights - Hadronic

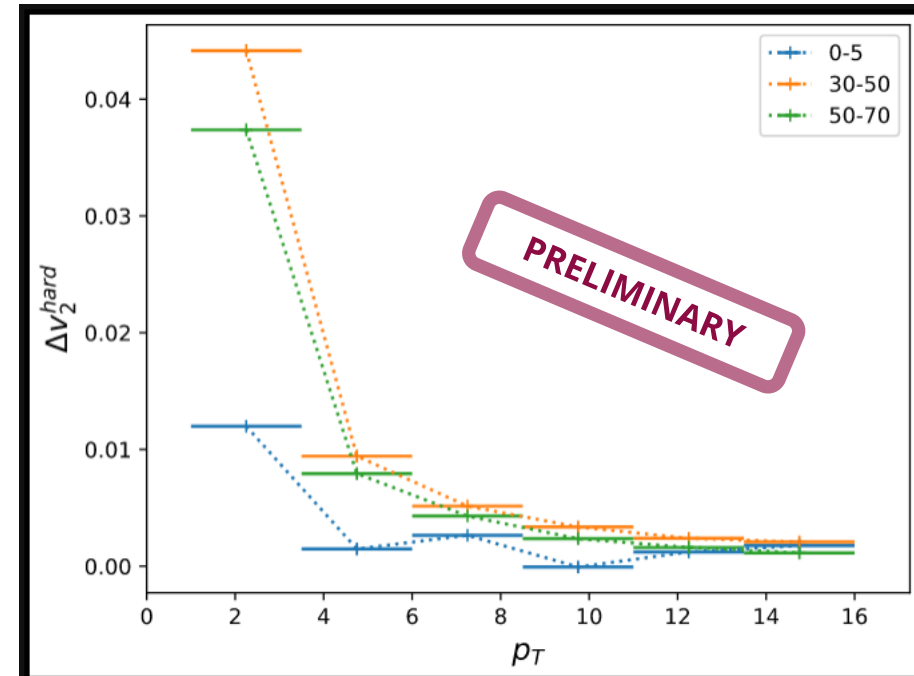
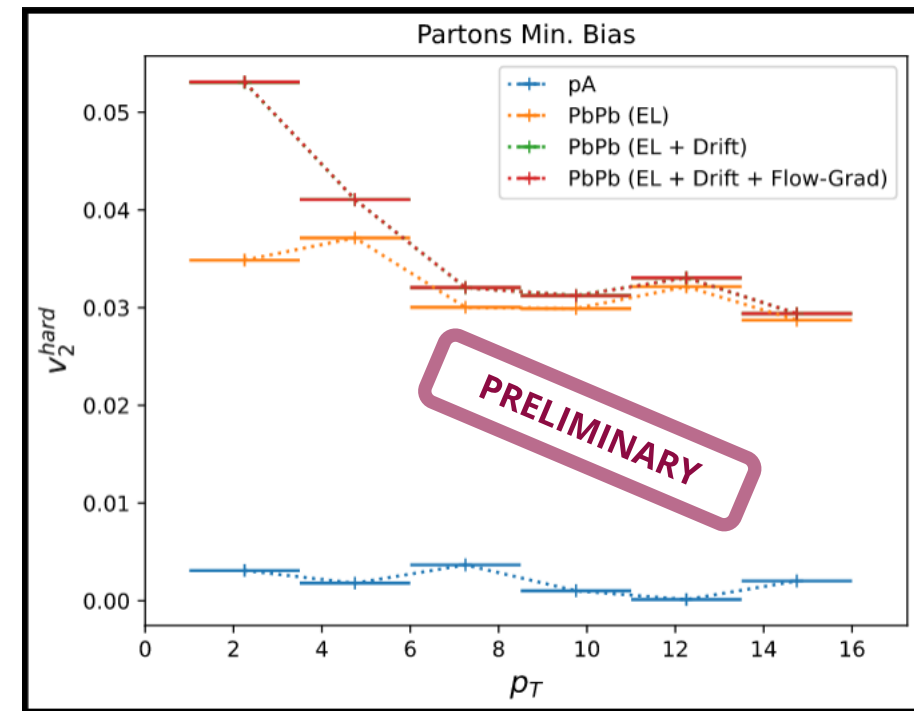
- Coupling $g=2$ under-predicts suppression
 - Coupling scans in progress, $g=2.2$ eyeballed
- Centrality scaling accurate-ish, but seems to get worse in peripheral bins



CMS: <https://doi.org/10.17182/hepdata.77101.v2>

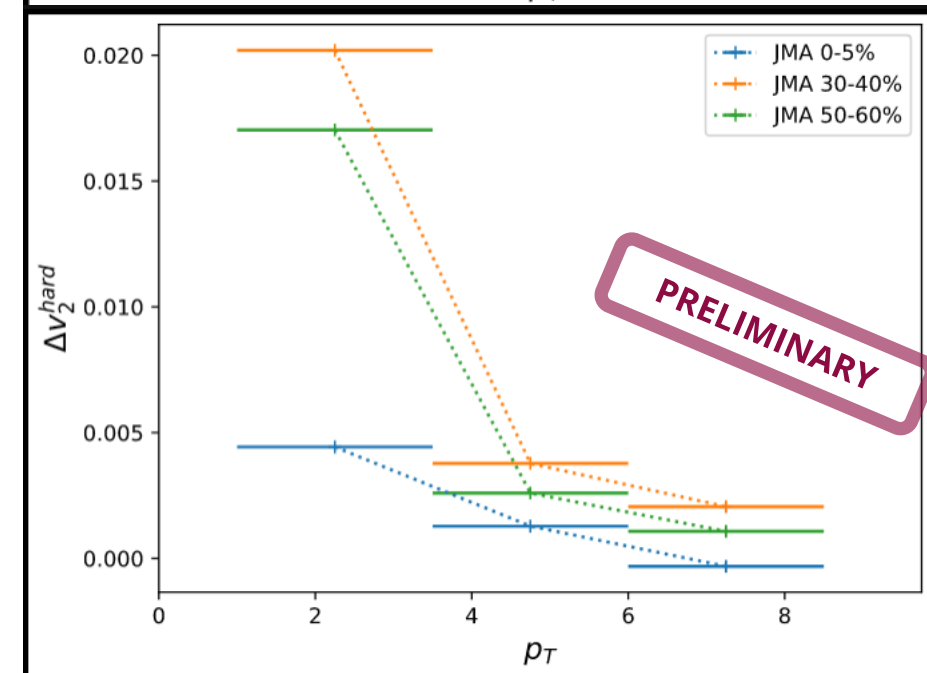
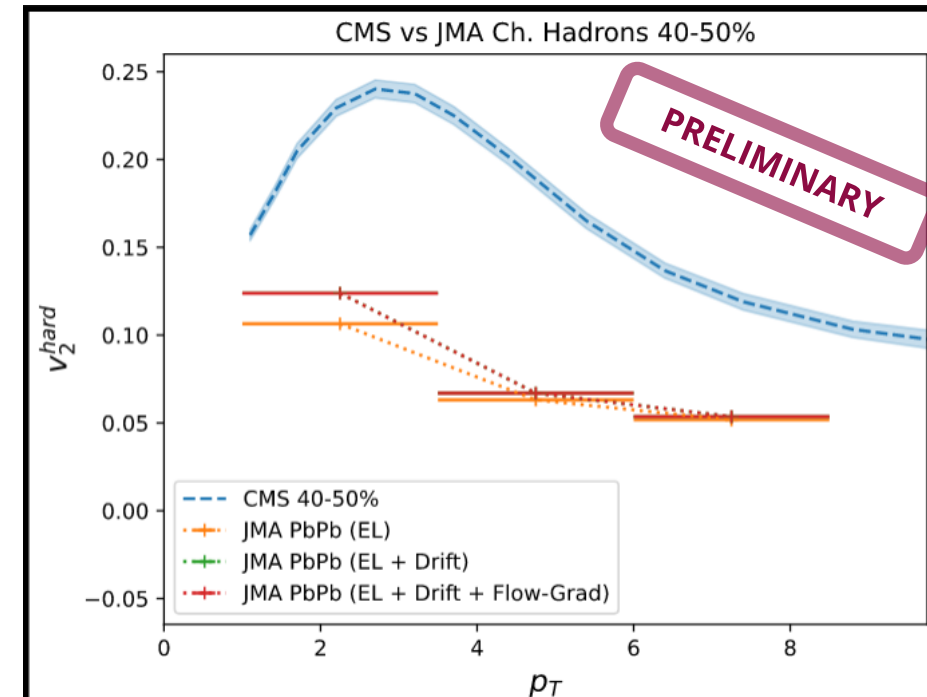
v_2 Insights - Partonic

- Elliptic modulation of hard partons is clear and systematic at low p_T
- Drift effects show nontrivial enhancement over energy loss alone in partonic distribution
- Absolute scale uncertain...
 - Needs convergence testing
 - Affected by fragmentation, CNM, etc.



v_2 Insights - Hadronic

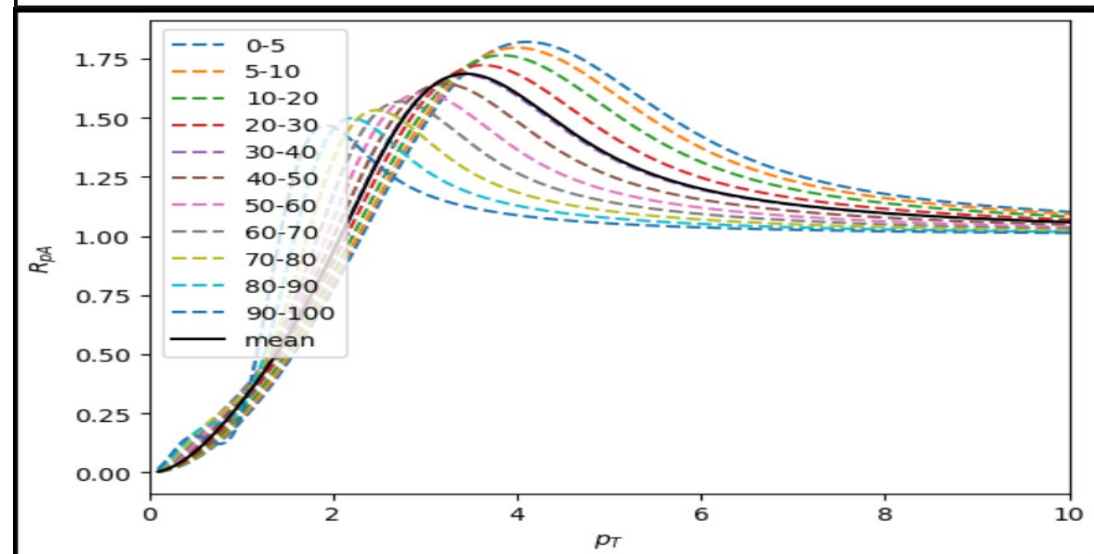
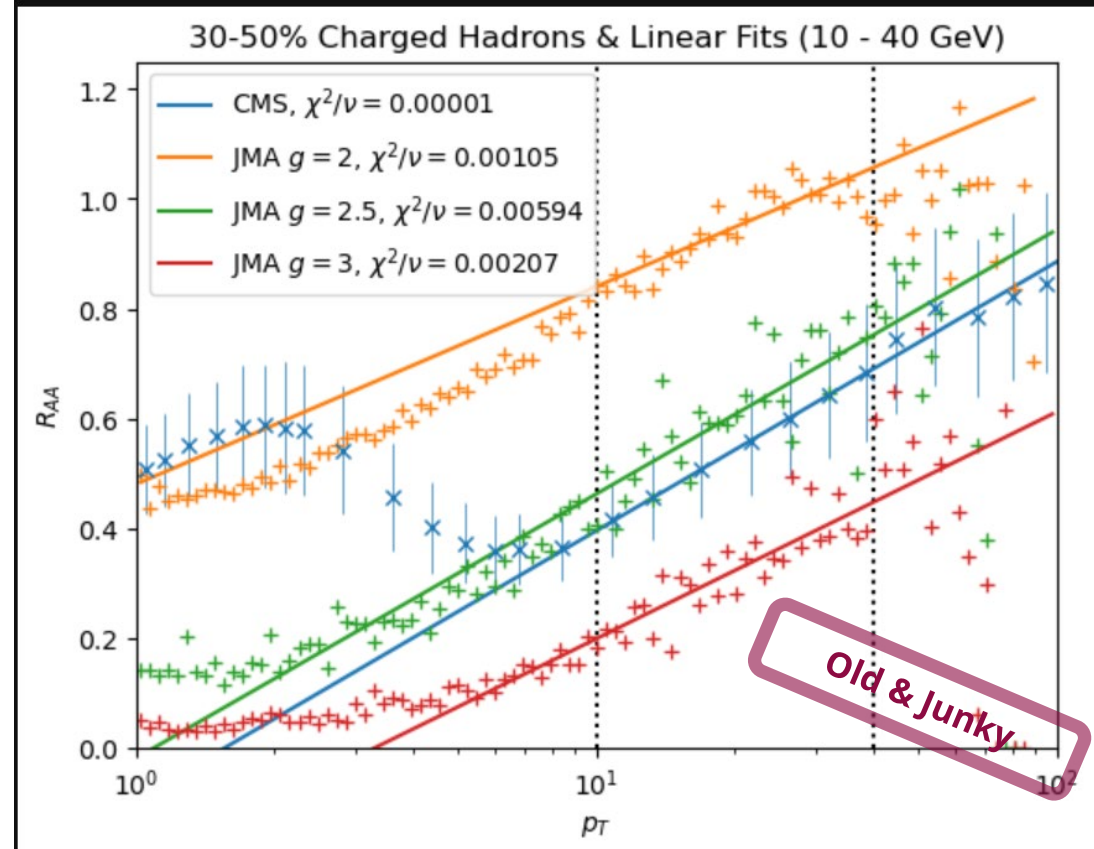
- Drift enhancement of elliptic flow of charged hadrons is still clear and systematic at low p_T
 - Scale dependent on FF choice, coupling, & sensitive to variation with MC sampling changes
 - Systematics robust & similar to expected effects
- Secretly, this is not the correct quantity to compare to data...



CMS: <https://doi.org/10.17182/hepdata.77603>

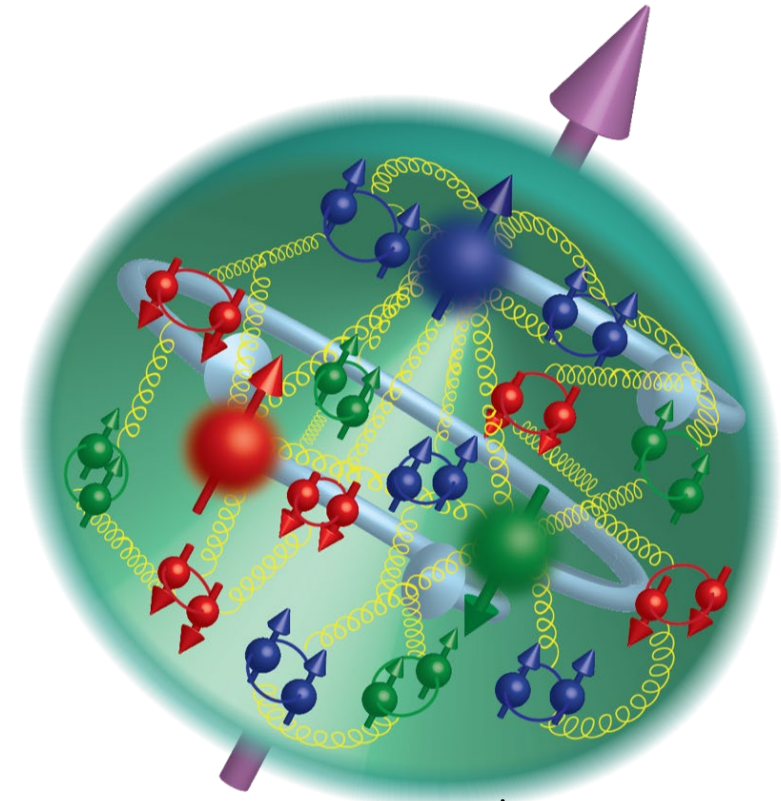
Future: Parameter Fits

- g from high pt
 - Min-bias & max-drift centralities
 - log fit of high pt region
- CNM params from low pt
 - Fixed coupling...
 - Bayesian inference against R_{AA} and v_2 data



Future: Competing Timescales & Hadron Gas

- Jets see substantial pathlengths in hadron gas phase
- Plan to form theory of parton-hadron interaction via Parton Distribution Functions (PDFs) for hadrons
 - Potential parton-hadron drift-like interactions
- Possible to have post-fragmentation deflection
 - Potential hadron-hadron drift-like interactions



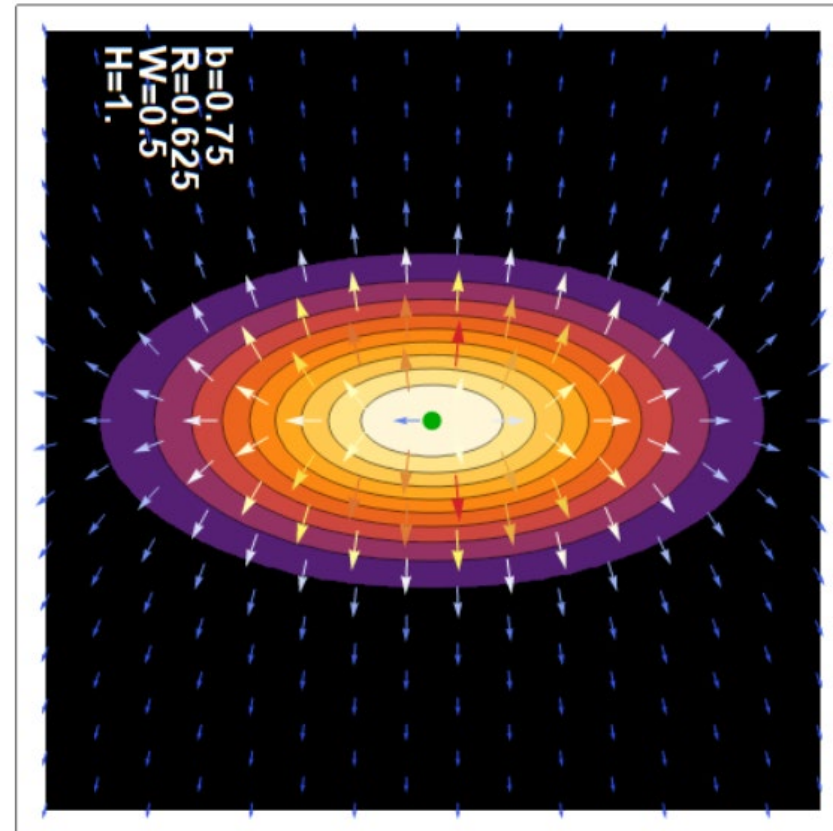
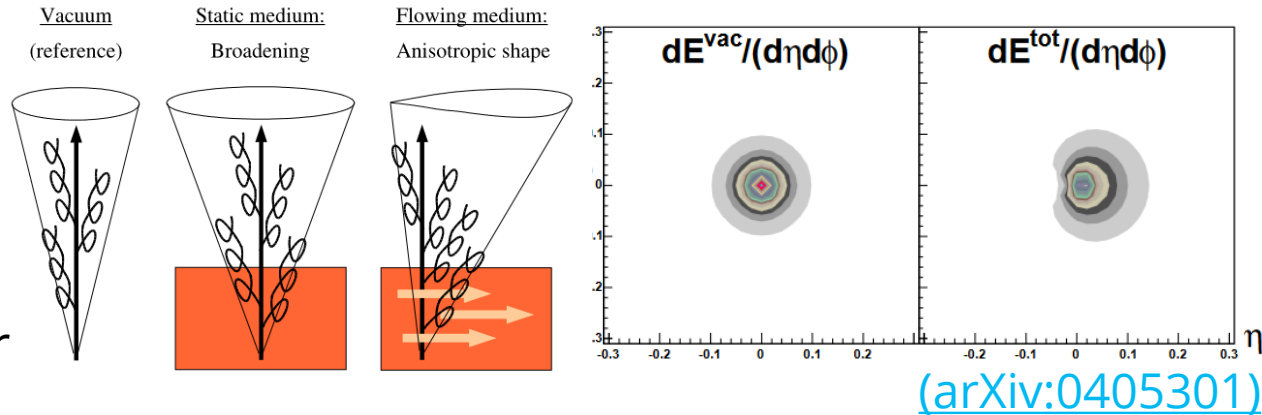
Argonne
National Lab

Future: New Observables

- “JMA” machinery is robust
- Drift likely has implications for many other observables
 - Jet shapes
 - See “Jet Drift-Like” effect from Lorentz Boost with medium ([arXiv:0405301](https://arxiv.org/abs/0405301))
 - **Jet wake asymmetries!**
 - E3C wake imaging could see asymmetric wake!
 - Wake may couple to parton level – larger drift

- **Elliptic modulation correlators?**

Other ideas?



The Bottom Line:

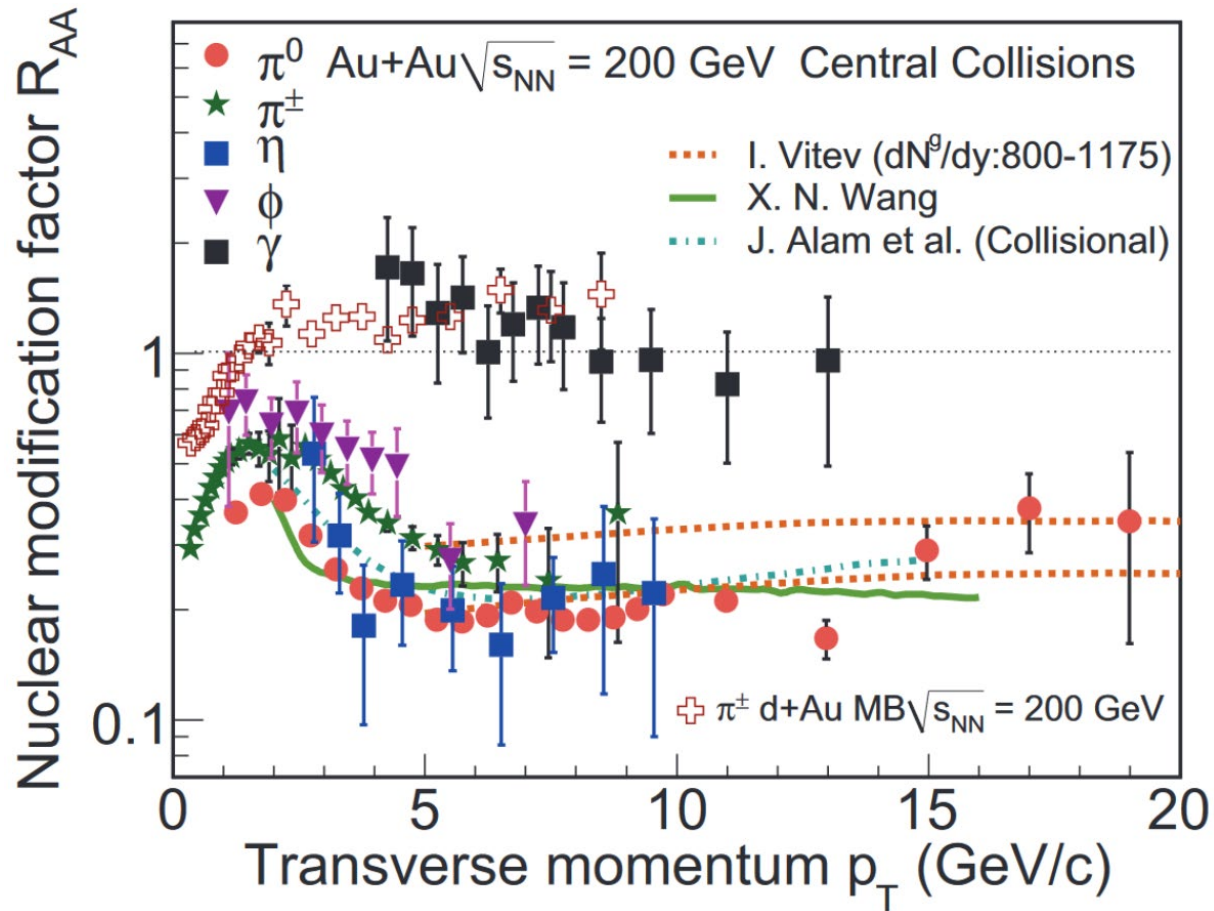
“Jet Drift” (Asymmetric Broadening)
enhances hard particle v_2 for $p_T < 10$ GeV!

Hot Takes!

Ideas!

Questions!

Discriminating Power is Very Limited



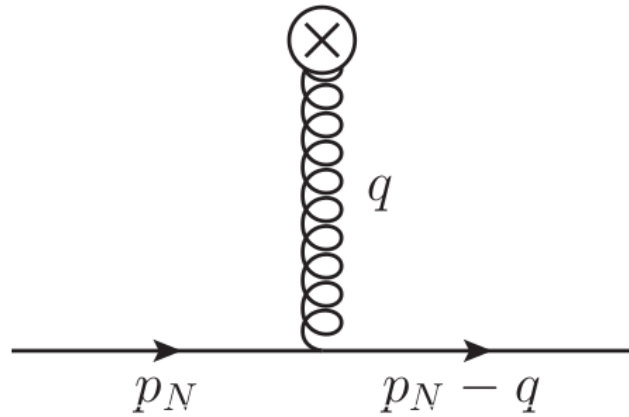
[arXiv:1207.7028](https://arxiv.org/abs/1207.7028)

What's wrong?

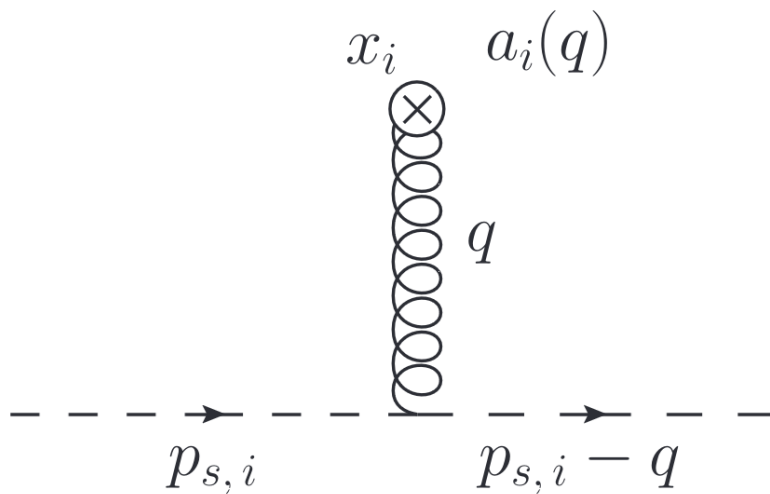
Observables are essentially model agnostic!

- R_{AA} – Nuclear modification factor
 - Can be fit with many competing models
- v_n^{hard} – Flow harmonics
 - Easy to fudge by scaling quenching
- Acoplanarities
 - Excessive background noise
 - Often impossible to even distinguish broadening from narrowing!

Medium Gluon Field Potentials



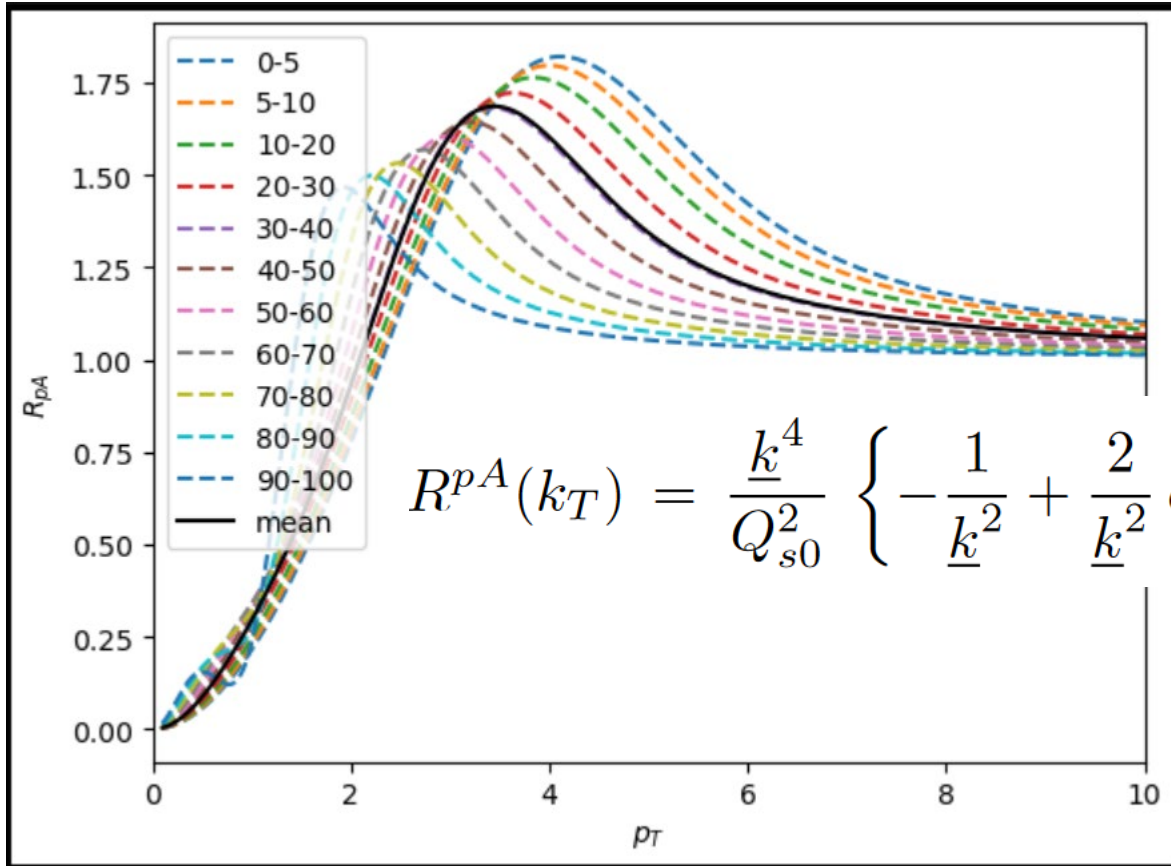
$$a_i^{\mu a}(q) = g^{\mu+} (t^a)_i \underbrace{[2\pi\delta(q^+)]}_{\text{Eikonal delta function (antiparallel)}} \underbrace{\left[\frac{-g_{eff}}{q_T^2} \right]}_{\text{v(q) Static scattering centers}}$$



$$g a_i^{\mu a}(q) = t_i^a u_i^\mu v_i(q) (2\pi) \delta(q^0 - \mathbf{u}_i \cdot \mathbf{q}) \left. \vphantom{g a_i^{\mu a}(q)} \right\} \text{Quark moves with medium}$$

$$v_i(q) \equiv v_i(q^2 - (\mathbf{u}_i \cdot \mathbf{q})^2) \equiv \underbrace{\frac{-g^2}{q^2 + \mu_i^2 - (\mathbf{u}_i \cdot \mathbf{q})^2 - i\epsilon}}_{\text{v(q) Dynamic directional scattering centers}}$$

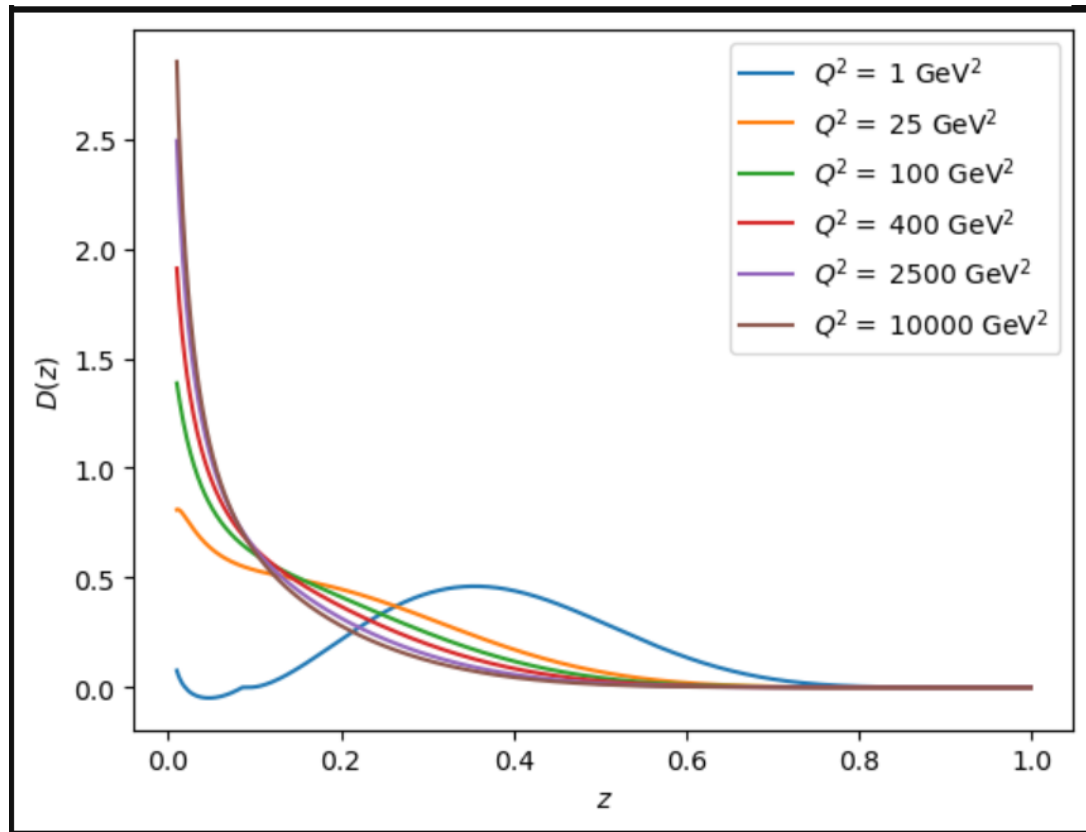
Jet Spectrum & Cronin Effect



- RpA computed from saturation theory
 - [arXiv: 0307037](https://arxiv.org/abs/0307037)
 - Two parameter, flexible form

- Q_{s0} saturation scale
- Λ - infrared cutoff

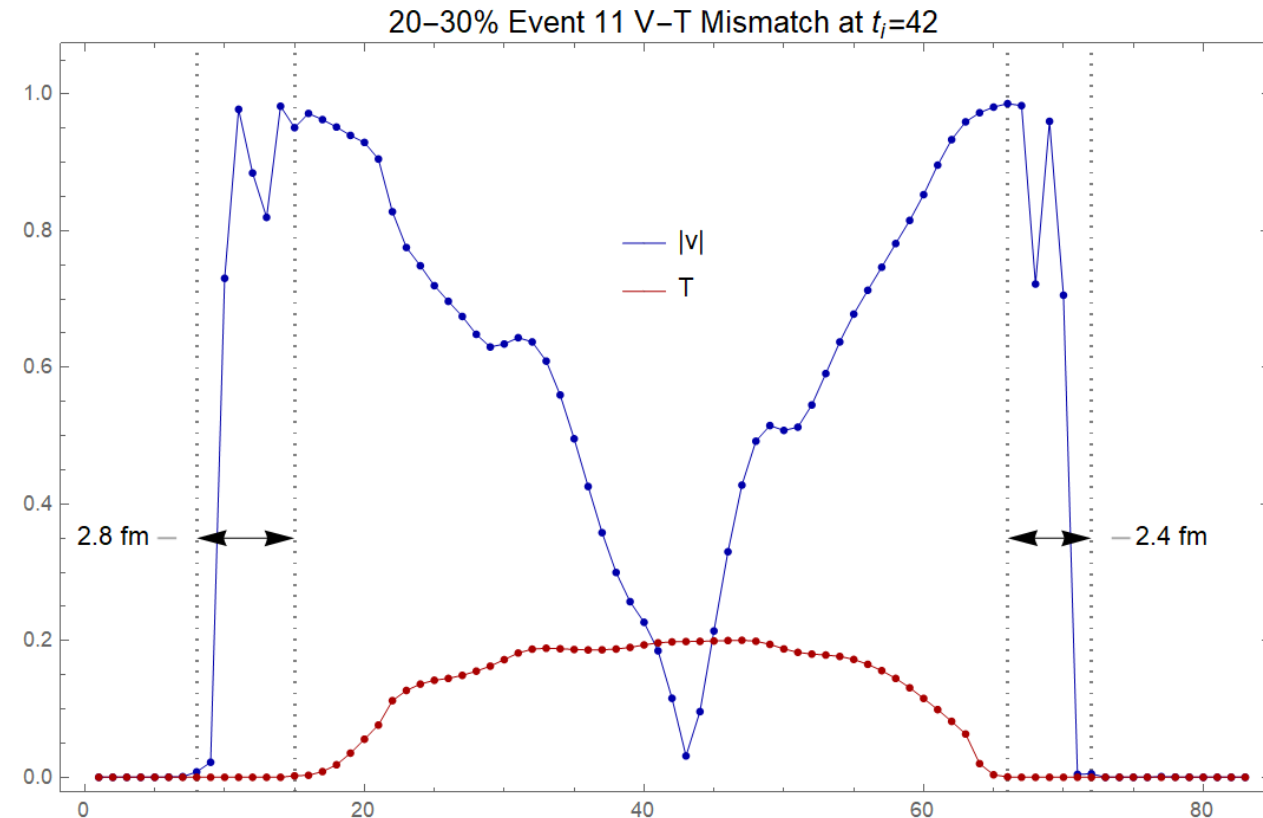
Fragmentation



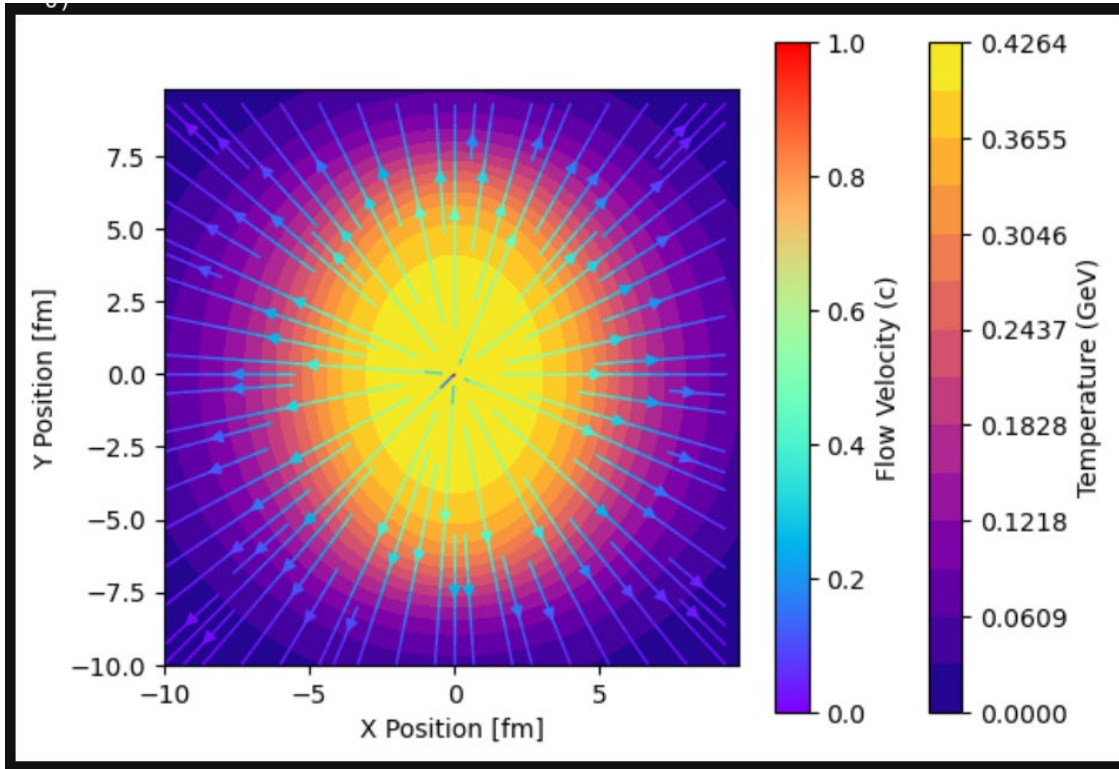
- Fragmentation functions describe probability distribution for hadron momentum, given parton momentum
- “JAM20-SIDIS_FF_pion_nlo”
 - ([arXiv: 2101.04664](https://arxiv.org/abs/2101.04664))
- Simple sampling... Complicated implications for Drift
 - Fragmentation downshifts p_T of hard particles
 - Shifts domain of strong drift even farther down

Questions Raised by Hyro

- "Velocity spill" may be reflective of problems with event-edge velocity accuracy
 - Most important region for drift!



Future: Simple Models



E.G. Woods-Saxon Density
Glauber model

$$T_A(\vec{x}_\perp) = \int dz \rho(\vec{r}) = \int dz \frac{\rho_0}{1 + \exp\left(\frac{\vec{r}-R}{a}\right)}$$

$$n_{bc}(\vec{x}_\perp) \propto T_A(\vec{x}_\perp) T_A(\vec{x}_\perp) \propto [S(\vec{x}_\perp)]^2 \propto [T(\vec{x}_\perp)]^6$$

$$T(\vec{x}_\perp) \propto \left(\int dz \rho(\vec{r} + \vec{b}/2) \int dz \rho(\vec{r} - \vec{b}/2) \right)^{1/6}$$

- Step-wise build-up of realistic optical Glauber models
- Gives insights into parts of medium model that affect drift & EL
- Time consuming...

Bread & Butter Jet Observables in QGP

- R_{AA} – Nuclear modification factor

- Measurement of jet energy loss (quenching)

Ratio of yield in AA collisions to scaled yield of pp collisions:
“Jet Suppression via QGP Effects”

$$R_{AA} = \frac{\frac{d\sigma^{AA}}{dp_T}}{\left(\frac{d\sigma^{pp}}{dp_T}\right) N_{coll}}$$

- V_n^{hard} – Flow harmonics

- Measurement of event geometry coupling

$$v_n e^{in\Psi_n}(p_T, \eta) \equiv \frac{\int_0^{2\pi} d\phi \frac{dN}{d\phi dp_T d\eta} e^{in\phi}}{\int_0^{2\pi} d\phi \frac{dN}{d\phi dp_T d\eta}}$$

- Acoplanarities

- Measurement of broadening effects

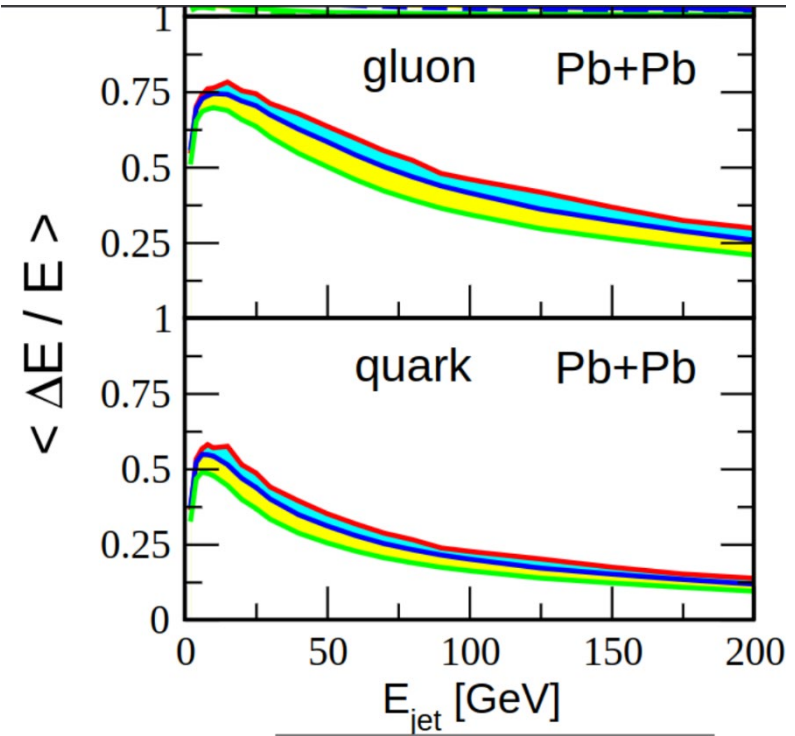
“Relative jet cone broadening measures”

Not relevant here...

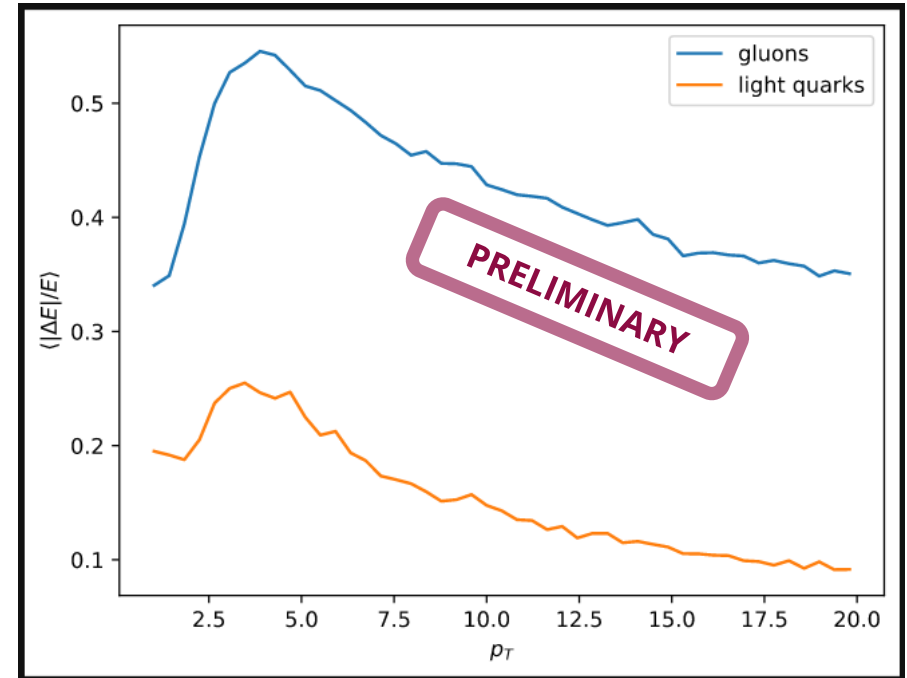
Essentially just Fourier harmonics of the azimuthal distribution of jets:
“Shape of jet azimuthal distribution”

Future: Numerical Energy Loss & Drift

- Currently using analytic approximations for average
- Numerical calculations may change the proportionality of drift to EL strength
 - Distinct from coupling shift
- Analytic approximations do not predict identical mean strength of EL



[arXiv:0603010](https://arxiv.org/abs/0603010)



Elliptic modulation vs v_2

- Particles are correlated
 - Dijet events
- Nontrivial modification to v_2 as measured in experiment
- Mixing of hard and soft v_2
- Possible enhancement to v_2

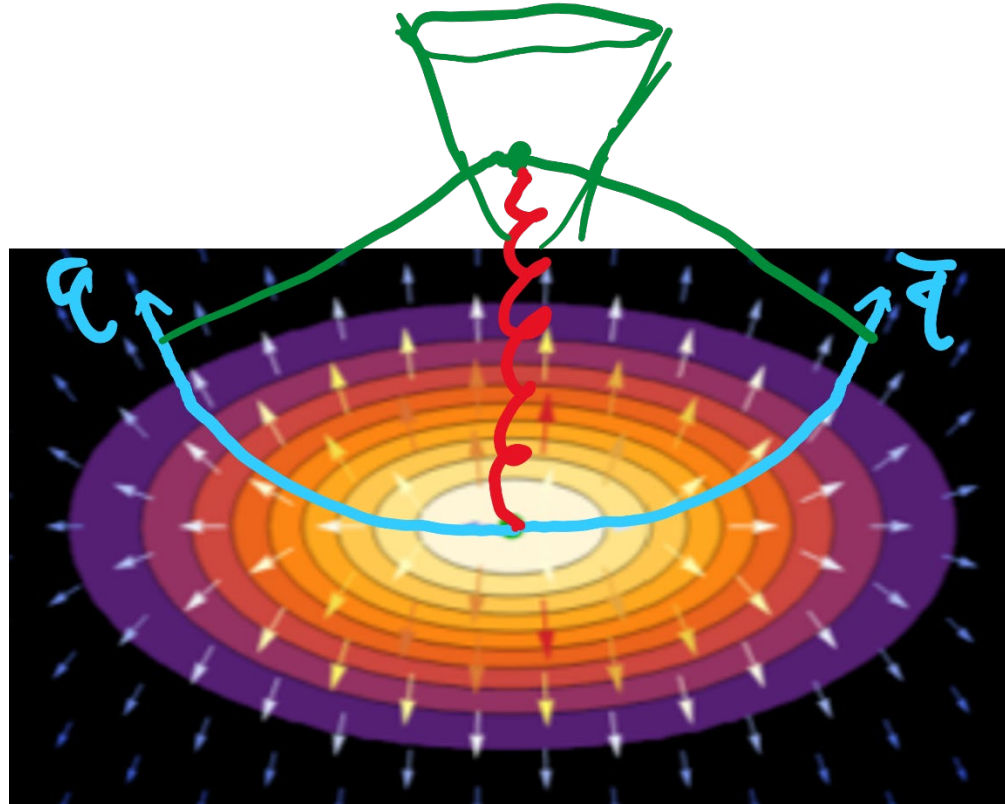
$$v_n e^{in\Psi_n}(p_T, \eta) \equiv \frac{\int_0^{2\pi} d\phi \frac{dN}{d\phi dp_T d\eta} e^{in\phi}}{\int_0^{2\pi} d\phi \frac{dN}{d\phi dp_T d\eta}}$$

$$\frac{dN_{\text{pairs}}}{d^3p^a d^3p^b} = \frac{dN}{d^3p^a} \frac{dN}{d^3p^b} + \delta_2(p^a, p^b)$$

$$\begin{aligned} v_n\{2\}(p_T, \eta) &\equiv \frac{\langle V_{n\Delta}(p_T, \eta, p_T^b, \eta^b) \rangle_{p_T^b, \eta^b}}{\sqrt{\langle V_{n\Delta}(p_T^a, \eta^a, p_T^b, \eta^b) \rangle_{p_T^a, \eta^a, p_T^b, \eta^b}}} \\ &= \frac{\langle v_n(p_T, \eta) \bar{v}_n \cos n(\Psi_n(p_T, \eta) - \bar{\Psi}_n) \rangle}{\sqrt{\langle \bar{v}_n^2 \rangle}} + \langle \delta_{2,n} \rangle \\ &\simeq \sqrt{\langle v_n(p_T, \eta)^2 \rangle}. \end{aligned}$$

Note on “Coalescence” in Fragmentation

- Many in the field believe quark “coalescence” is a source of enhanced v_2 of hard particles
- If coalescence is a significant effect, jet drift may enhance it
- No perturbative QCD model for fragmentation involving coalescence
 - Hard to treat on the same footing as our other jet effects



- Market model is “Lund String” fragmentation
- Curiosity-level tests with Pythia Lund-String fragmentation give evidence of coalescence
 - Enhanced high “z” hadrons with drift
- Plans in the works to do measurements of coalescence significance as function of $\Delta\phi_{jets}$, still not understood

Dataset Info



Quick Note on Error Assessment

- $g=2.2$: ~13k Events
- Event geometries oversampled by 100x hard processes
- 11 uniformly sampled angles per production point
- $\sim 16\text{M}$ parton trajectories / case

- Error estimates have been done with jack-knife resampling
- Time consuming to compute, but shown to correlate with number of trajectories.
- Suspect with this dataset we have precision on v_2 measurements of $\pm < 0.25\%$, as compared to similarly sized result sets

