



SAPIENZA  
UNIVERSITÀ DI ROMA

# The Lund plane, what (I think) we've learned so far

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European Research Council

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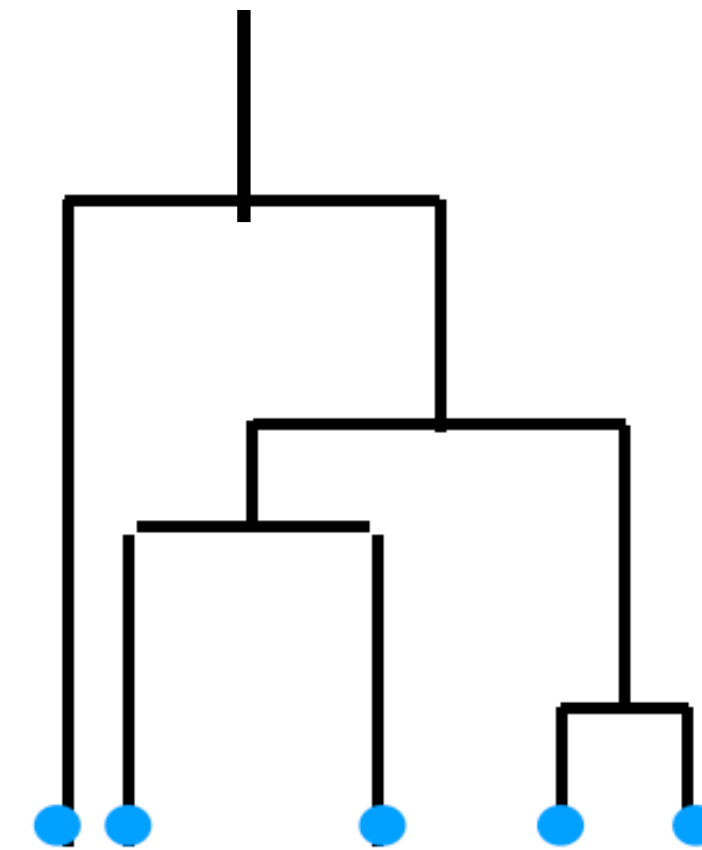
*New jet quenching tools to explore equilibrium  
and non-equilibrium dynamics in heavy-ion collisions  
12-16 February, ECT\* Trento*

# Jet substructure to probe the internal dynamics of jets

Essentially, two ways of looking inside jets:

## Use the jet tree:

hierarchical structure of jet constituents using the clustering history of a “physical” clustering algorithm

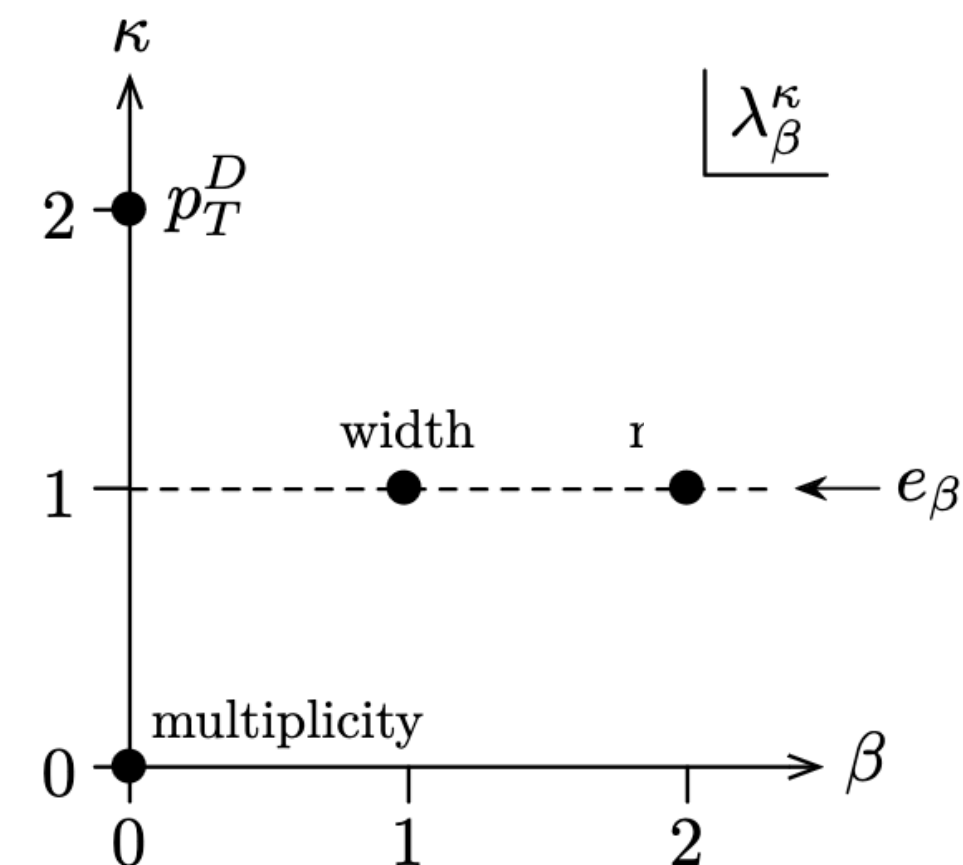


## Use energy flows:

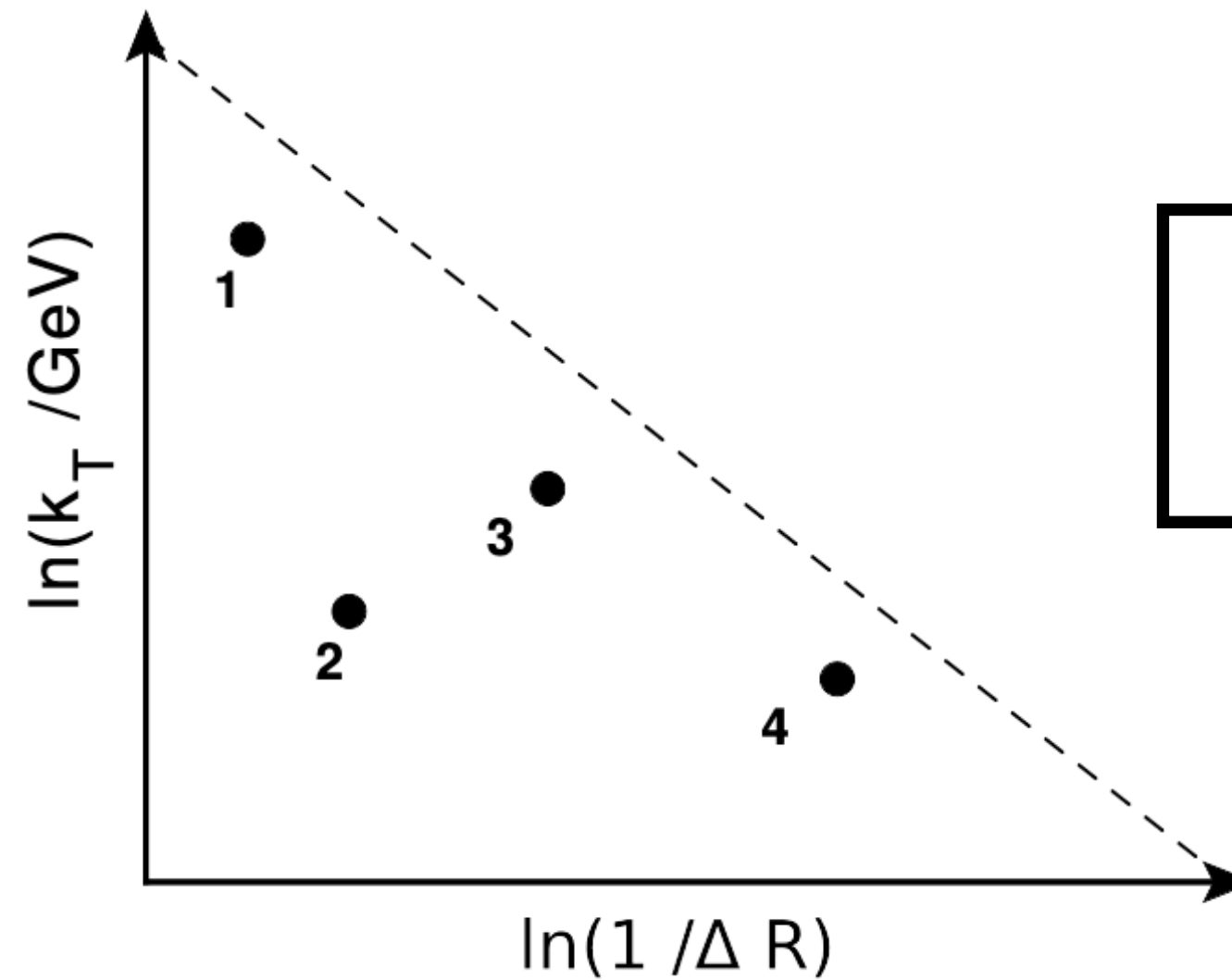
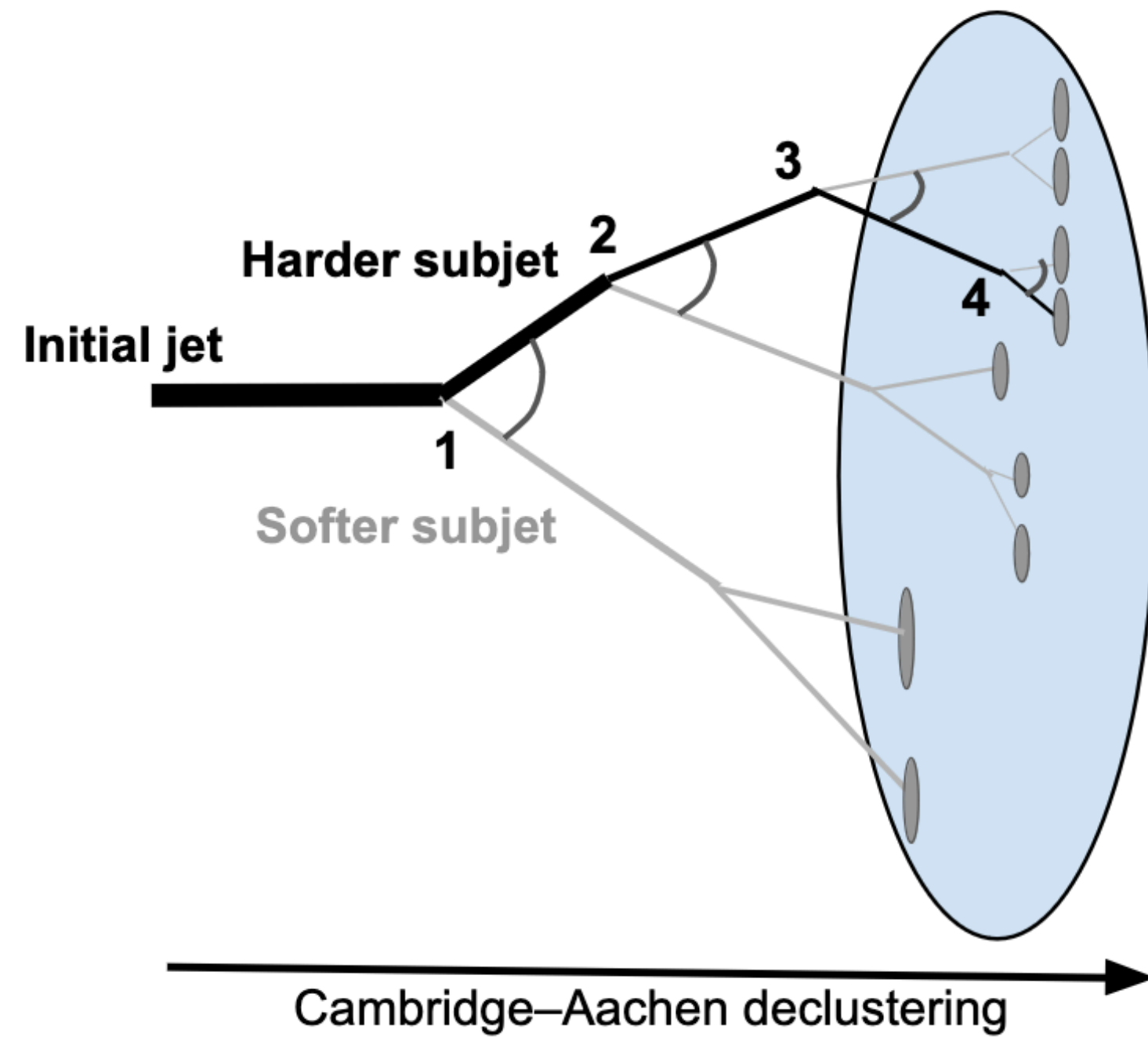
build jet-shape observables using energies and angles of jet constituents

example, generalised angularities  $\rightarrow$

$$\lambda_{\beta}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \left( \frac{R_i}{R_0} \right)^{\beta}$$



## The primary Lund jet plane density



$$\rho(k_T, \Delta R) \equiv \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T / \text{GeV}) d \ln(R / \Delta R)}$$

*Dreyer et al, JHEP 12 (2018) 064*

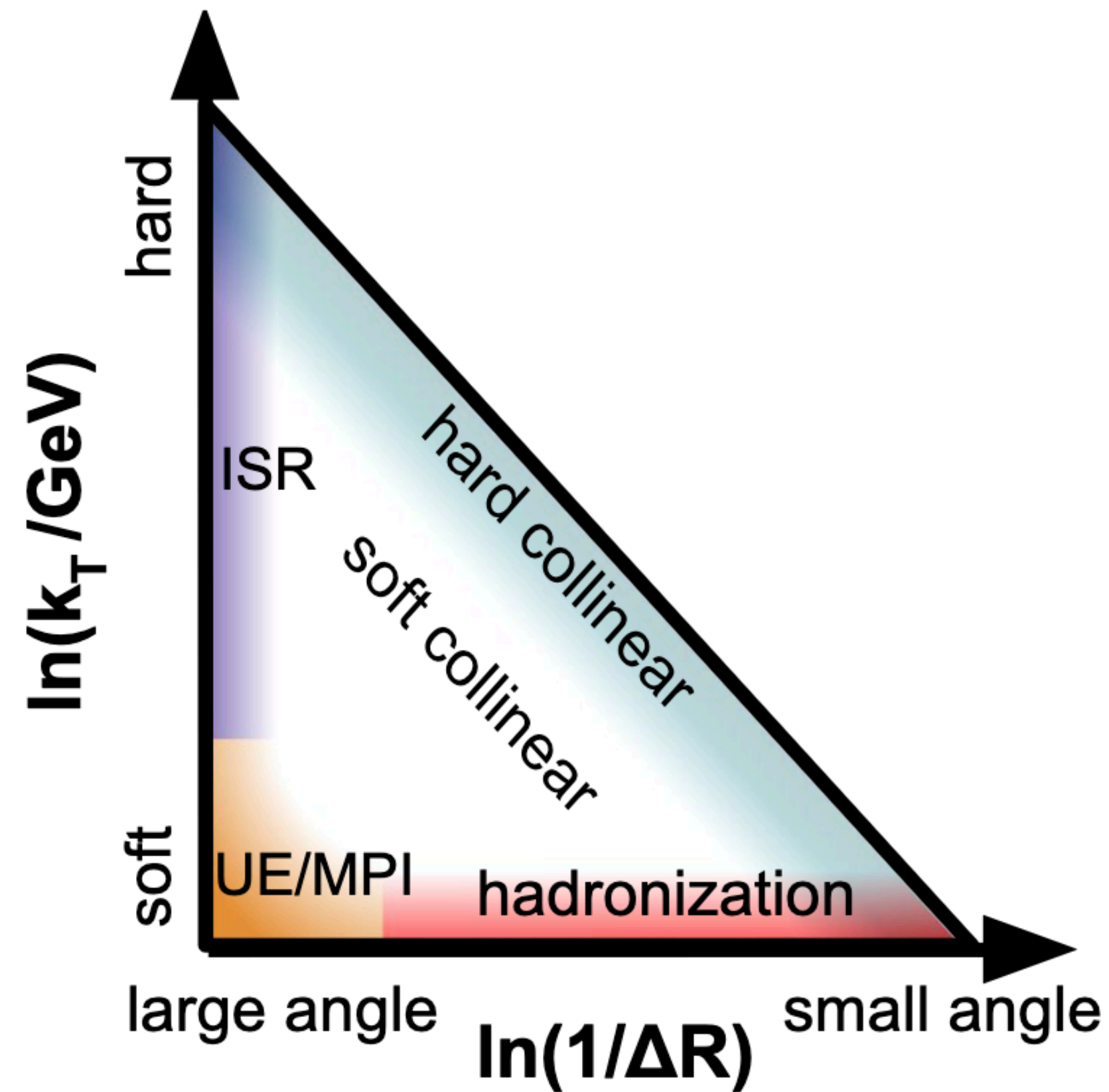
The jet tree is built using CA algorithm

The subleading prong kinematics are registered onto the lund plane for every node following the leading branch at each step

The density is expressed double-differentially in  $\ln(k_T)\ln(R/\Delta R)$ , approx the momentum and angular scaling of QCD radiation

In the soft and collinear limit:  $\rho(k_T, \Delta R) \approx \frac{2}{\pi} C_R \alpha_S(k_T)$

# The primary Lund jet plane density in pp



Detailed information about the jet radiation pattern

Constrain to different aspects of the parton shower in a modular fashion:

separation of hard/soft and large/small angle physics

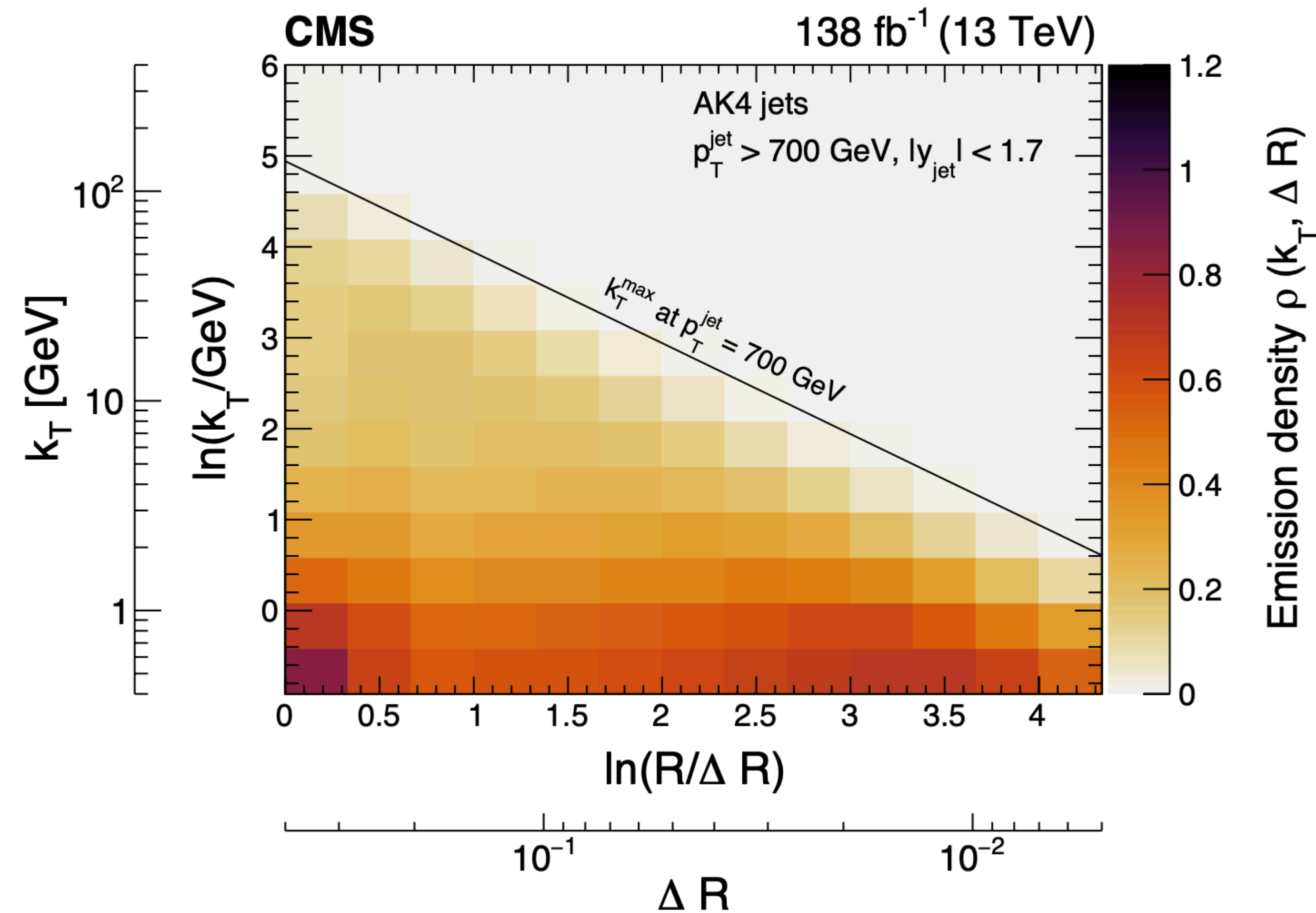
Analytically calculable *Lifson et al, JHEP 10 (2020) 170*

All groomed observables are subsamples of the Lund plane

$$\rho(k_T, \Delta R) \equiv \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T / \text{GeV}) d \ln(R / \Delta R)}$$

## The Lund jet plane density in pp

Fully corrected Lund jet plane for R=0.4 jets using charged particles



The analysis requires a 3D unfolding of the emissions (plus the 1D unfolding of the normalization,  $N_{\text{jets}}$ )

To build a response matrix:

- match det-level and part-level jets
- match det-level and part-level splittings
- unique geometrical matching:**  
 det-level splitting is the closest to part-level splitting and viceversa

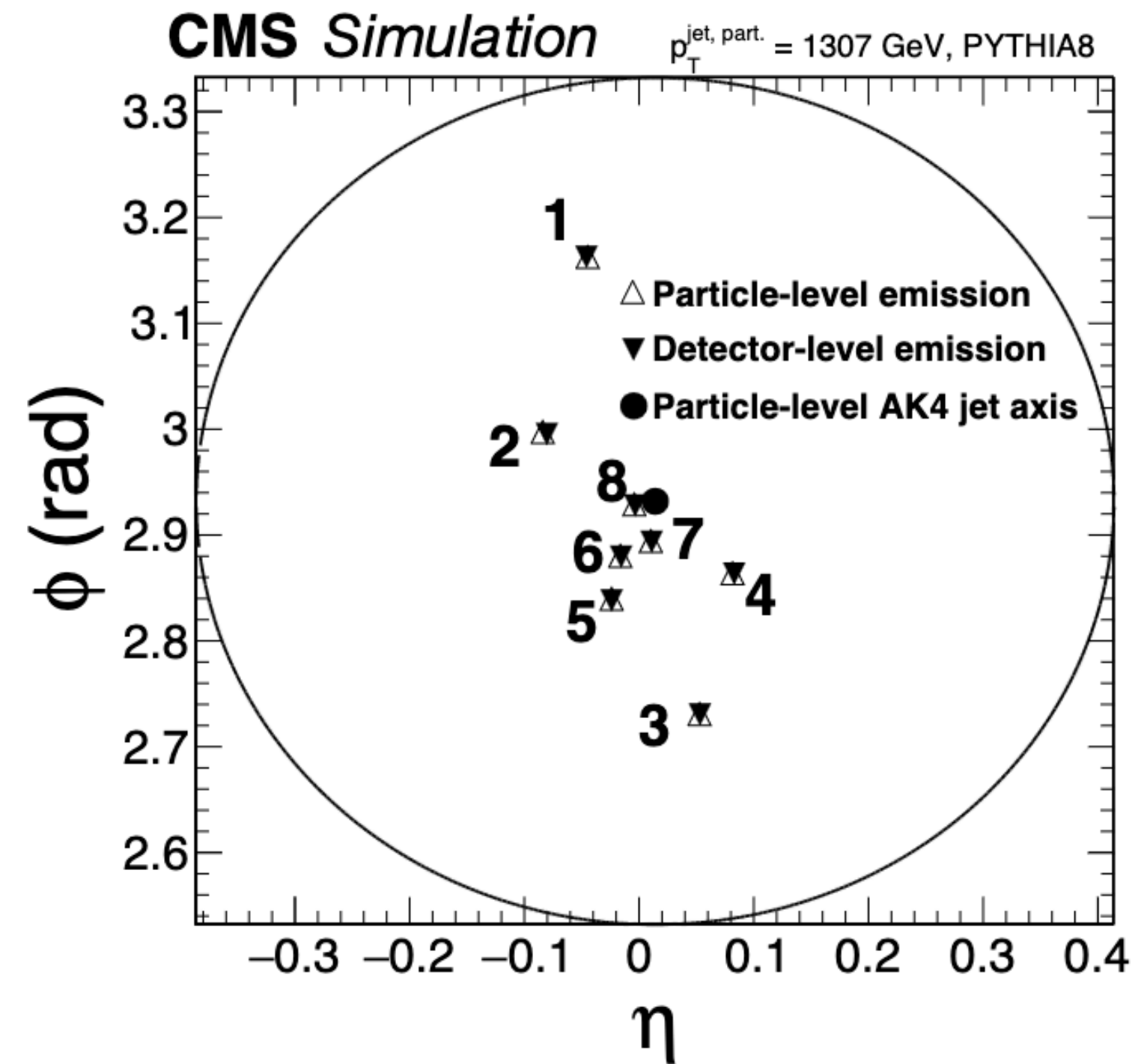
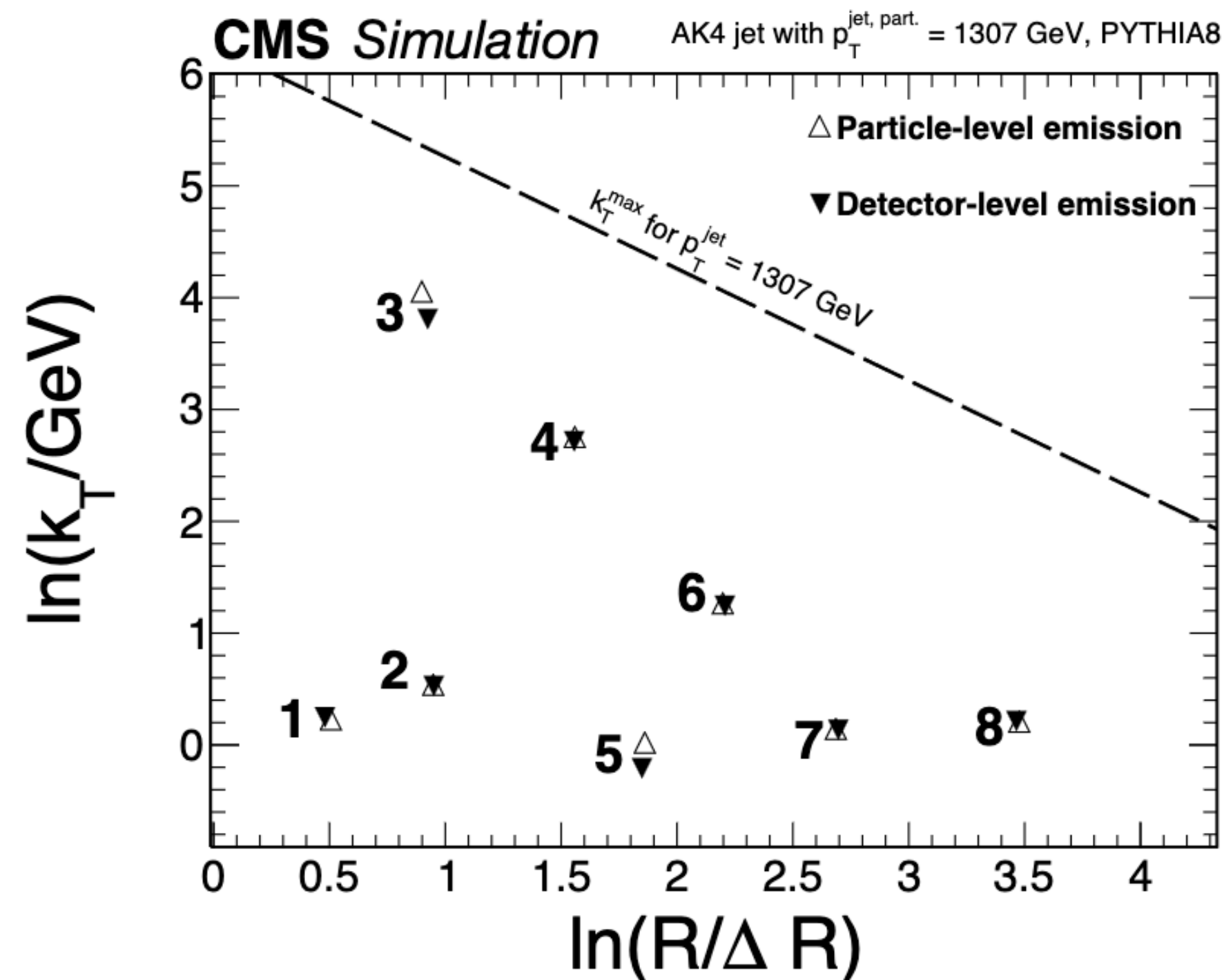
Correct for the matching purity and efficiency



# The Lund jet plane density in pp: geometrical matching of splittings

CMS-PAS-SMP-22-007

Flat geometrical matching



In general there is good correspondence between detector and particle level splittings, matching eff and purities  $\sim 90\%$

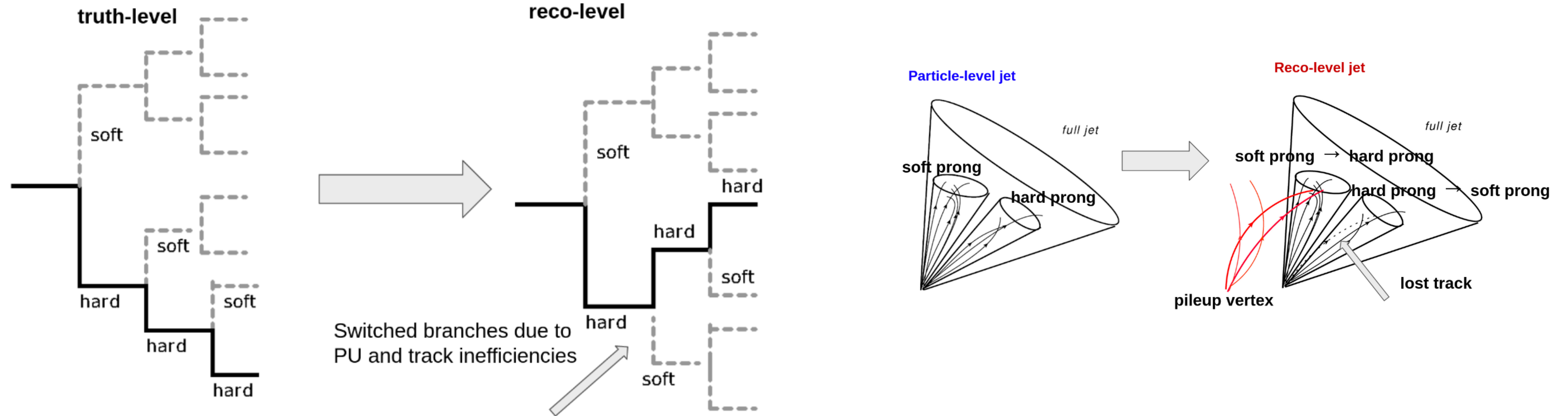
Detector effects such as tracking efficiency and momentum smearing can worsen the correspondence

Large purity correction in the limit of soft and large-angle emissions due to UE and pileup

Large efficiency corrections in the region of small angles and low  $k_T$  due to det-level low  $p_T$  cutoffs

# The Lund jet plane density in pp: mismatches

CMS-PAS-SMP-22-007



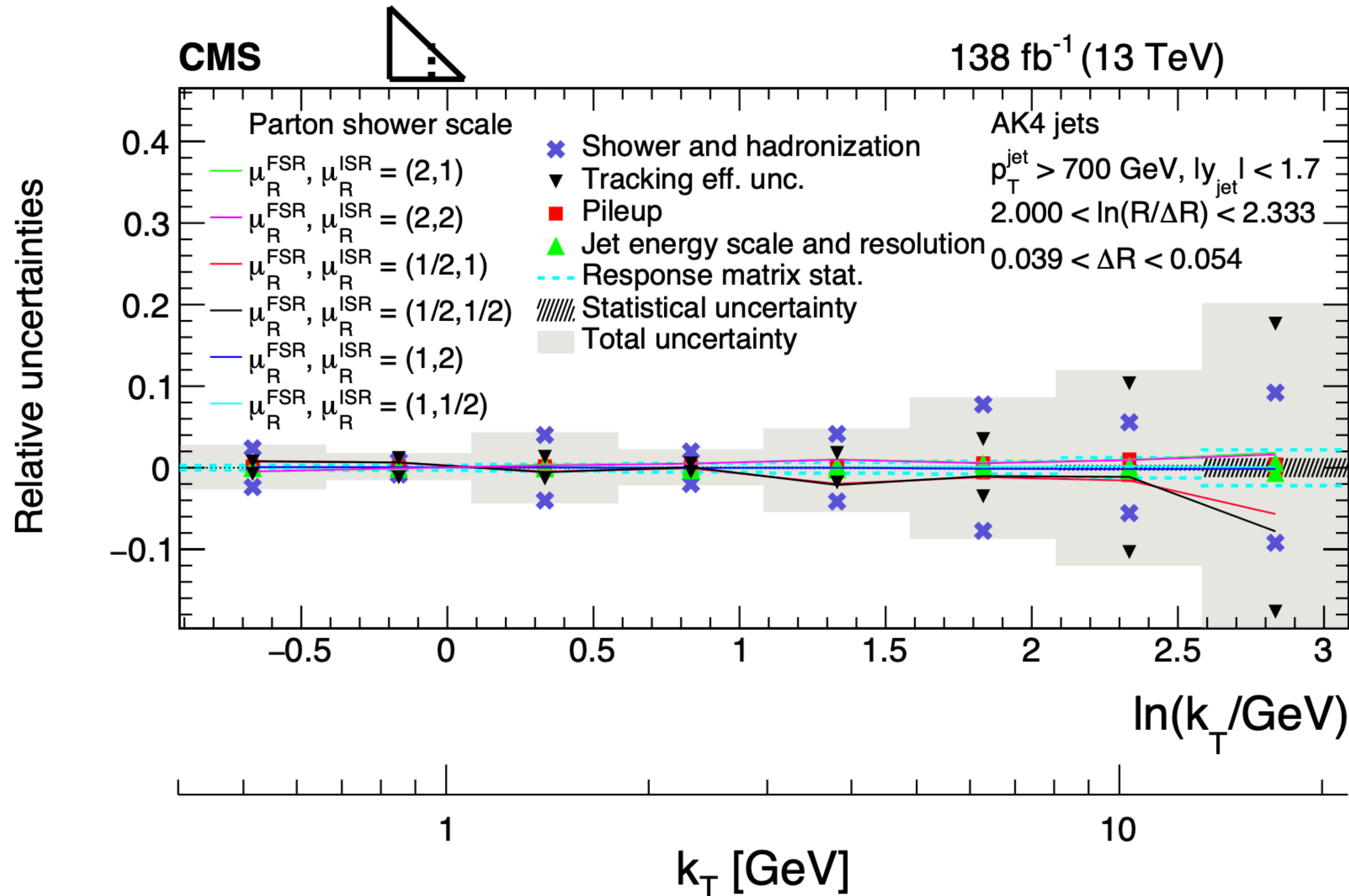
Residual mismatches

Correspondence between particle and det-level splittings is lost

Typically due to swaps between the leading and subleading prongs due to pileup and track losses

Few percent of the matched emissions in simulation that contribute as off-diagonalities in the response matrix

# The Lund jet plane density in pp



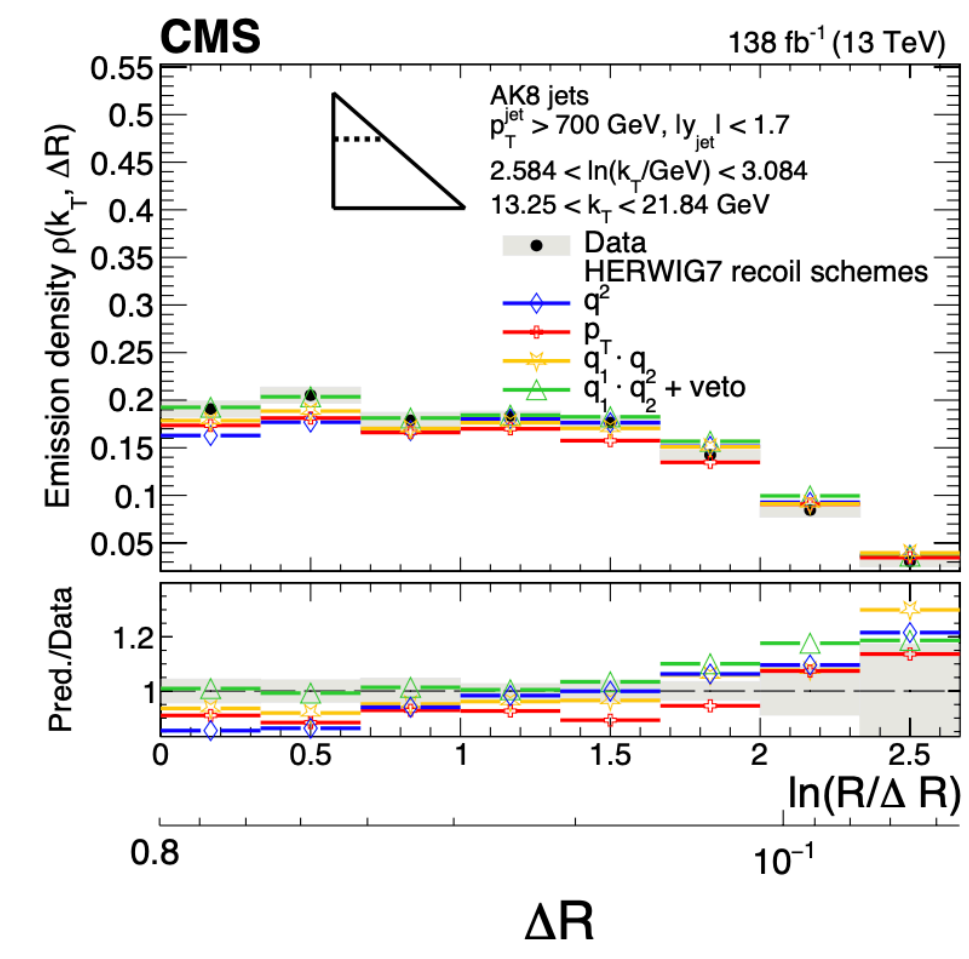
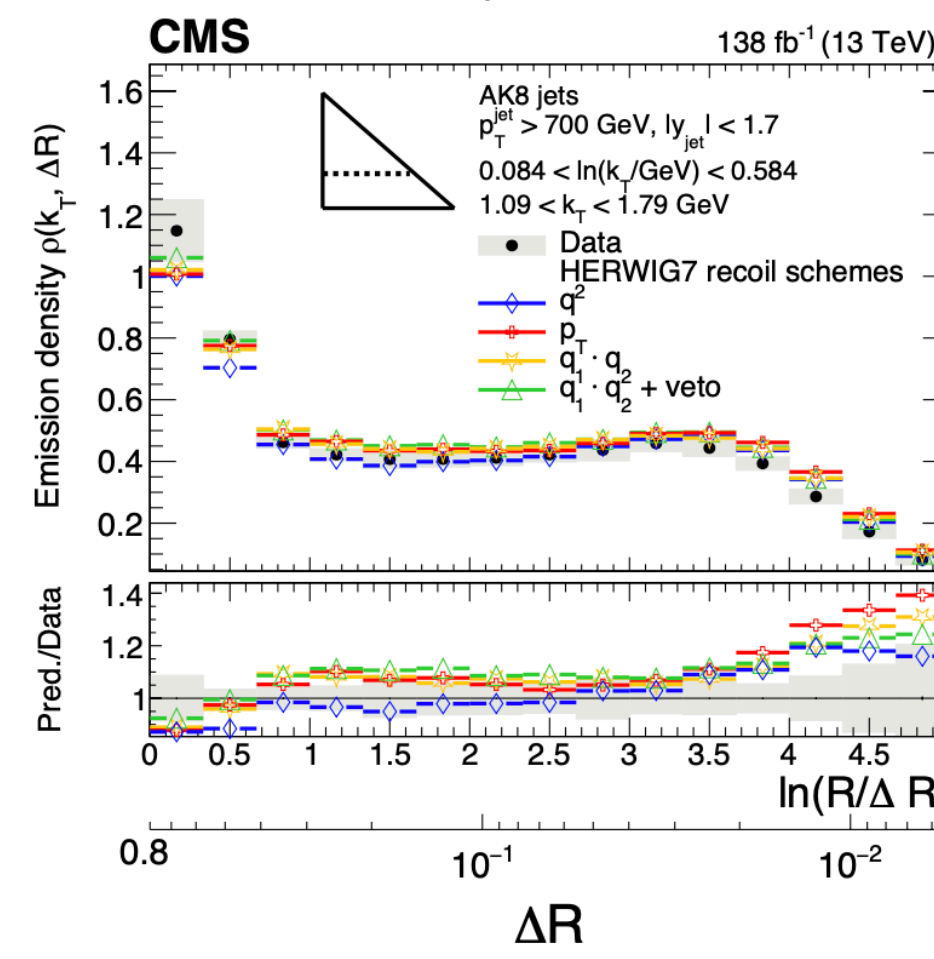
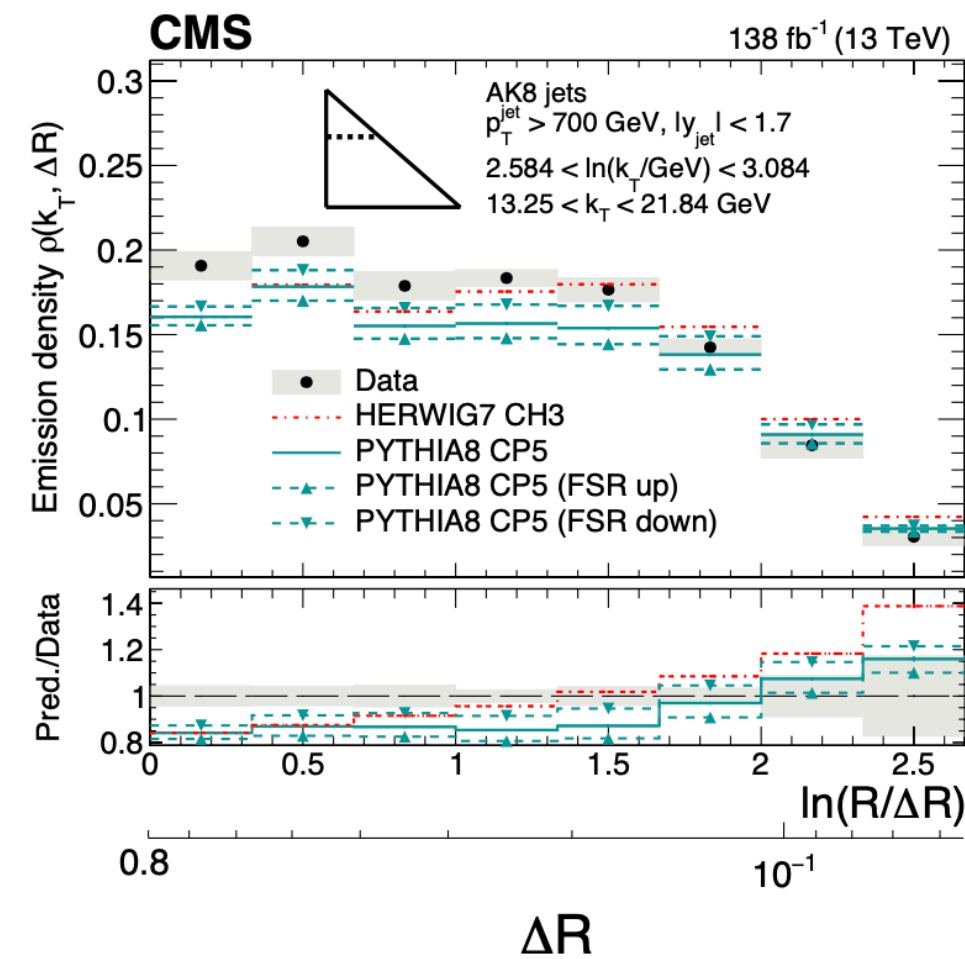
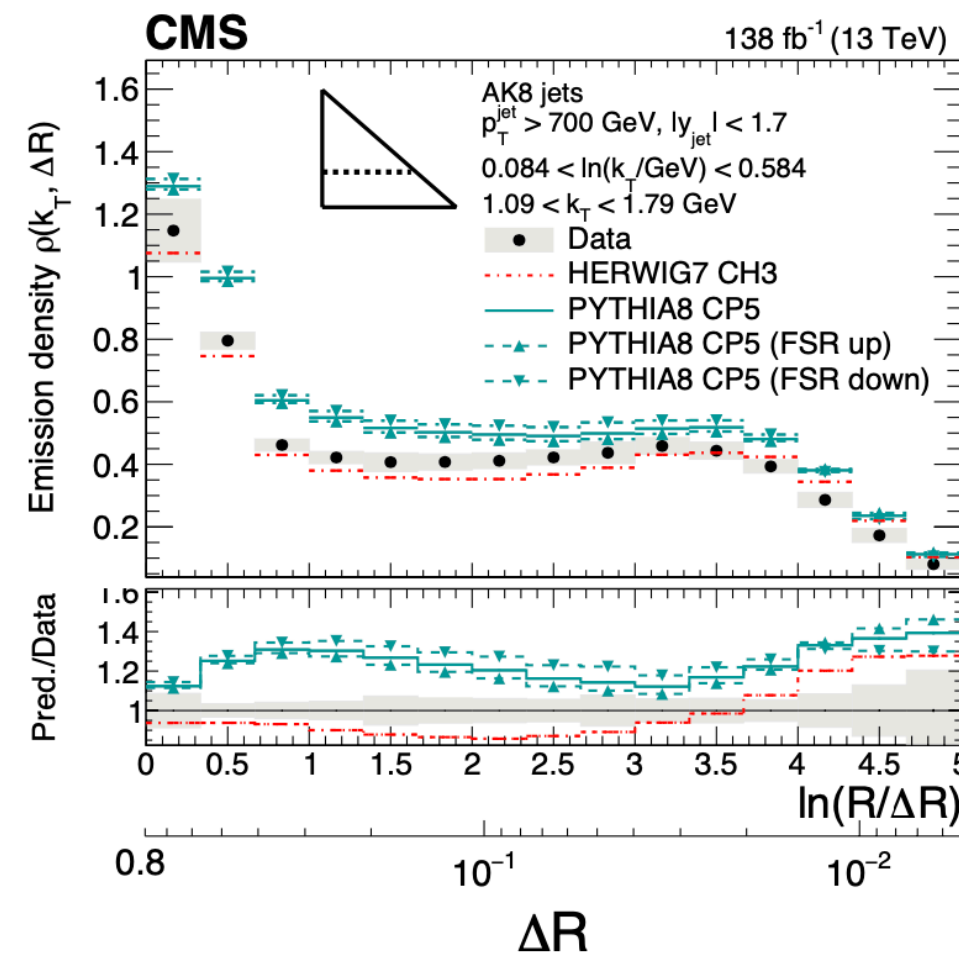
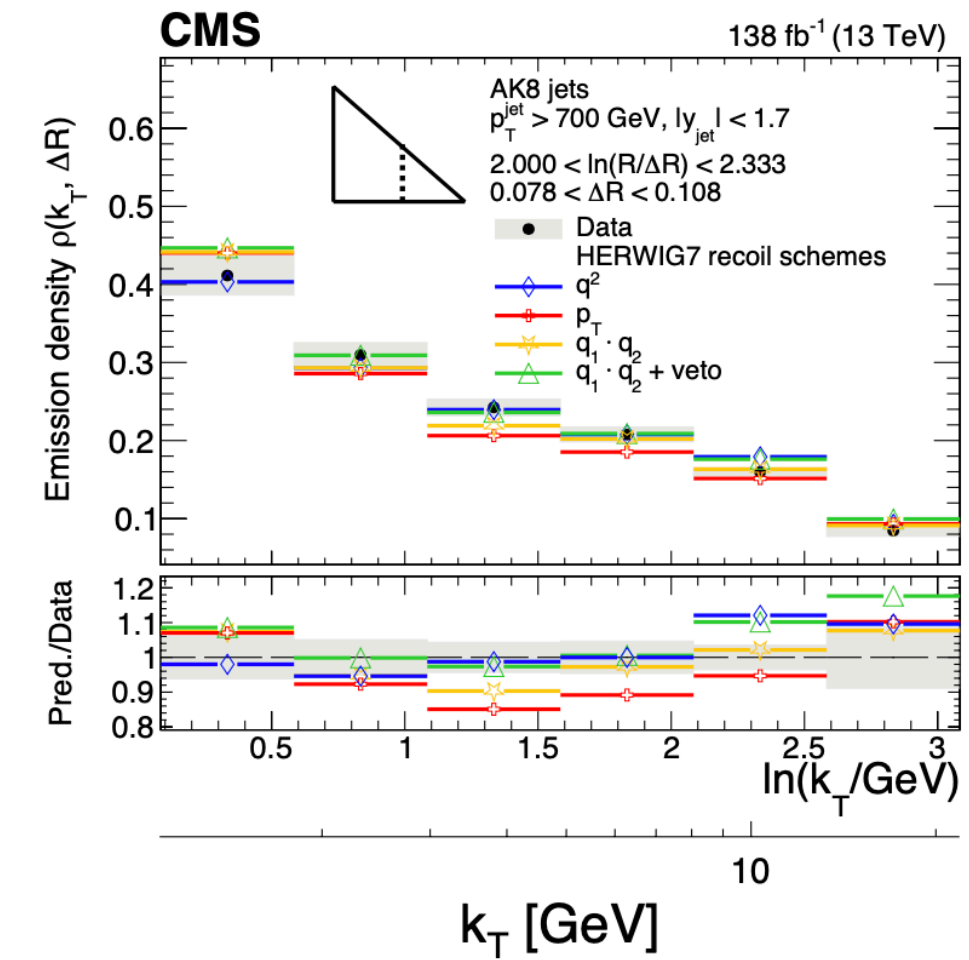
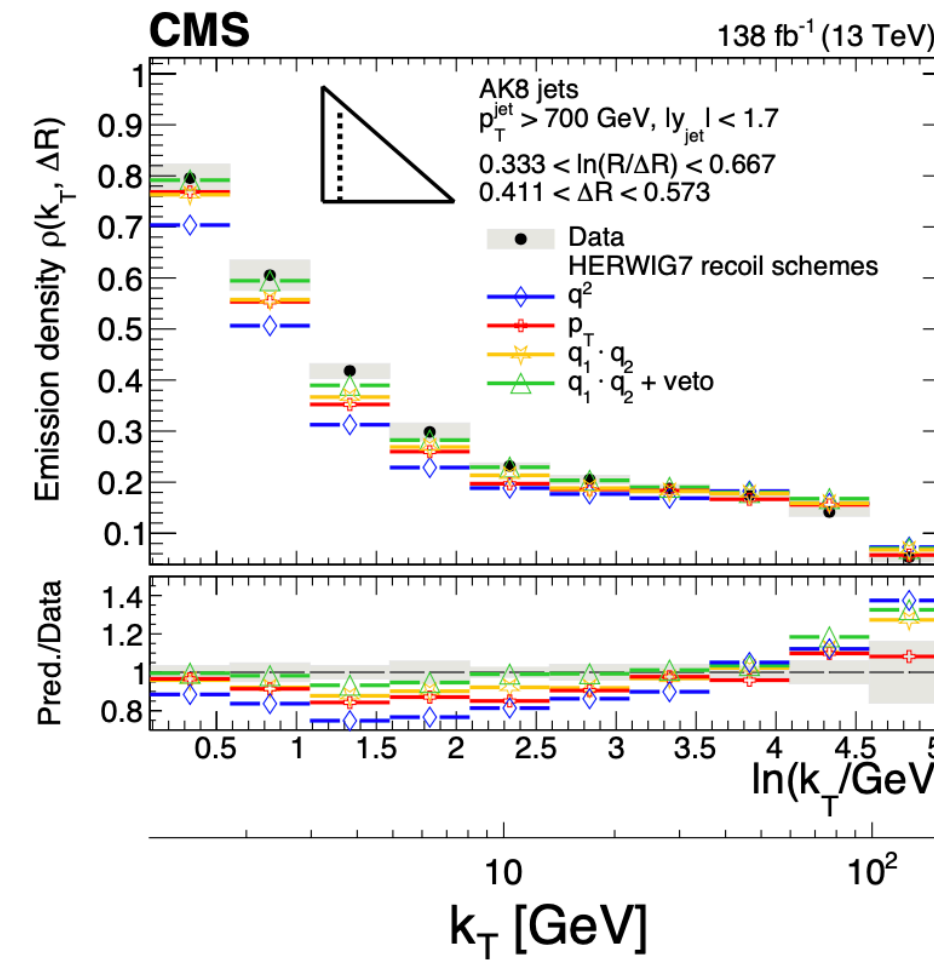
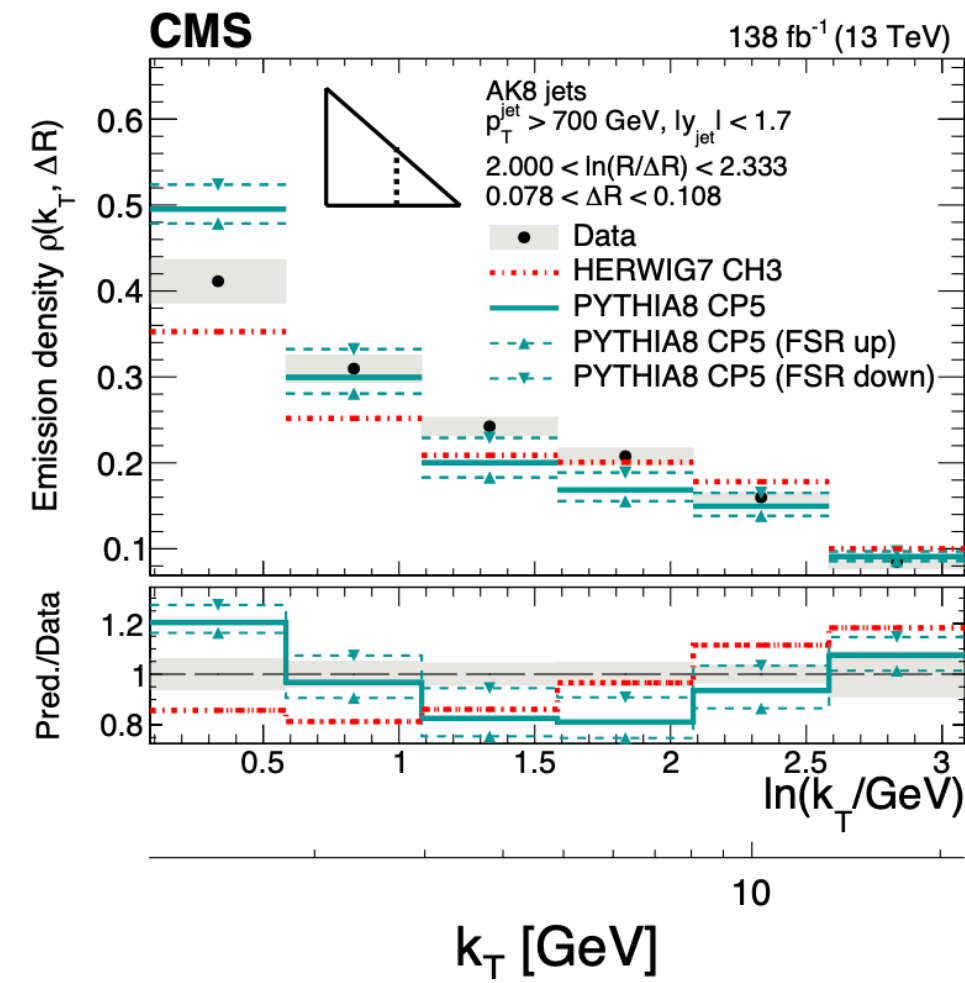
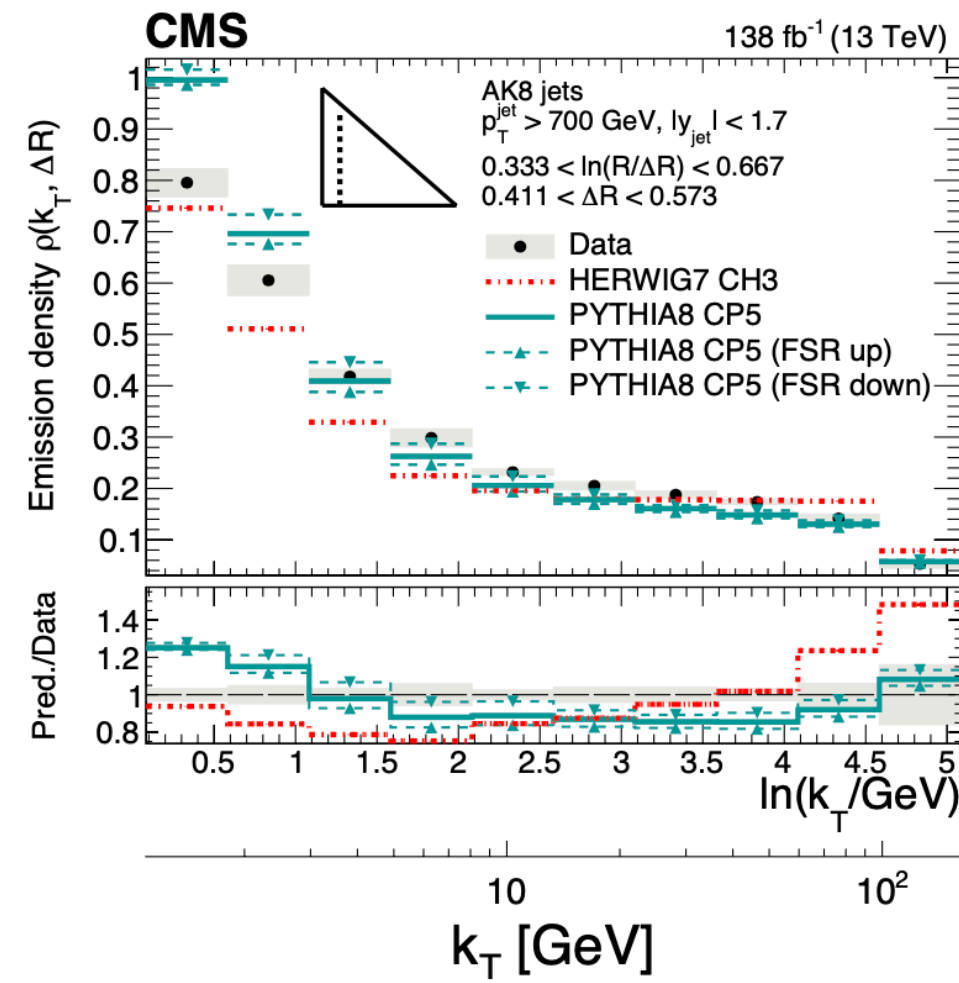
Dominant uncertainties:

track. eff uncertainty, up to ~20%  
 model dependency, up to ~10%

The track inefficiency uncertainty hits badly the high- $k_T$  perturbative domain  
 Swaps can be mitigated by measuring the full Lund plane, not the primary!

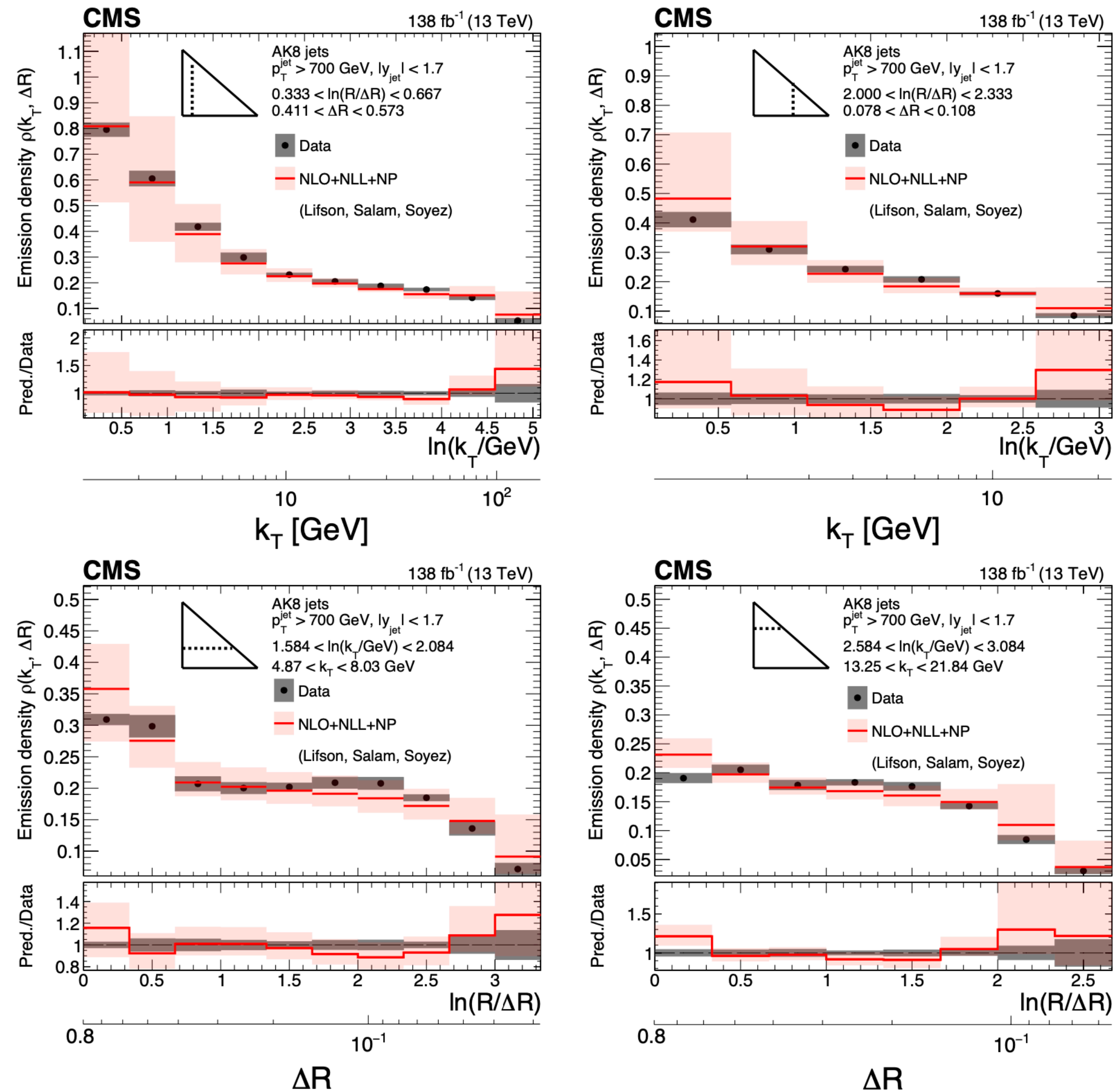


# The Lund jet plane density in pp



Examples of comparisons to Pythia tunes and Herwig recoil schemes

# The Lund jet plane density in pp



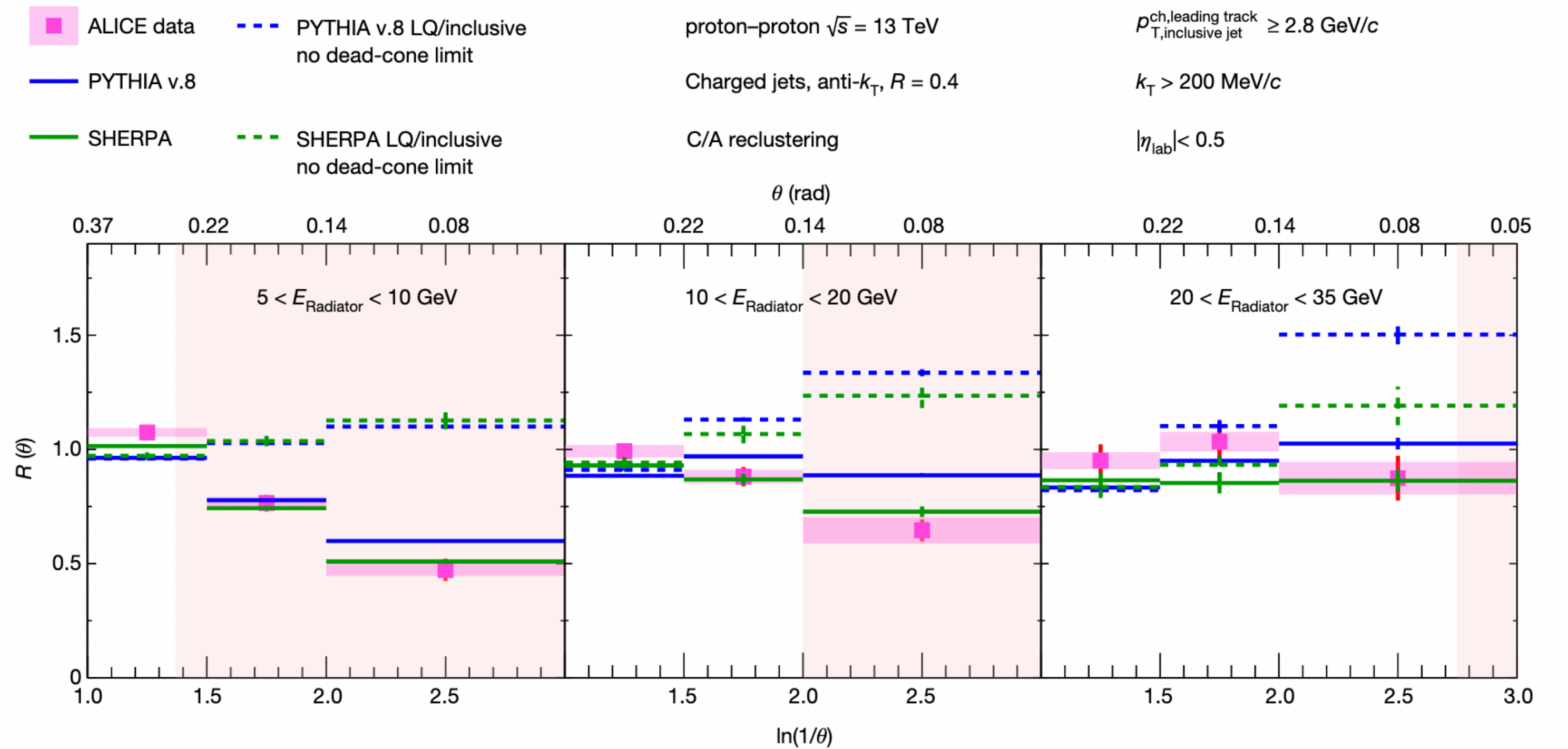
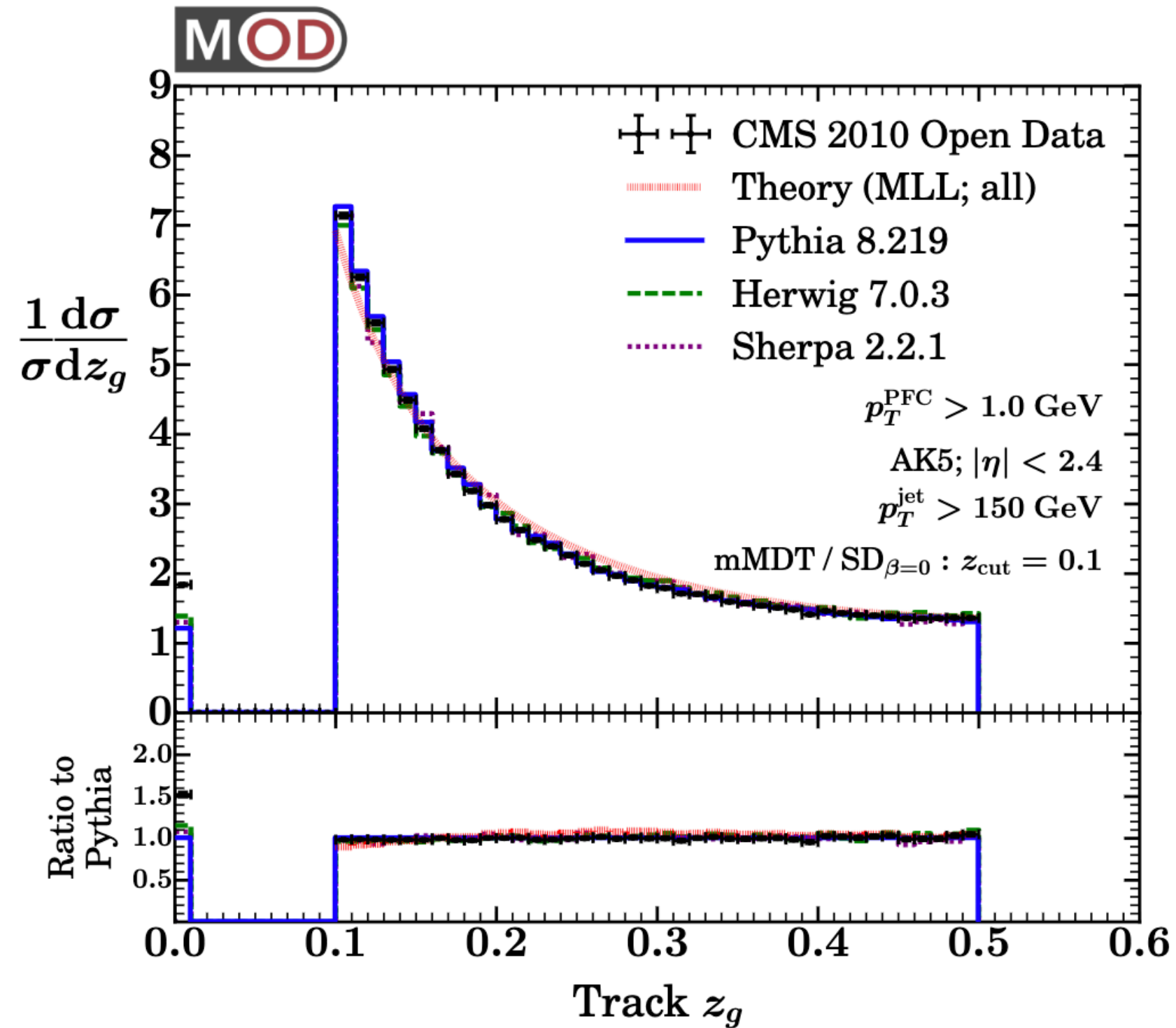
NLO+NLL+NP analytical calculation  
 based on [Lifson et al, JHEP 10 \(2020\) 170](#)



# Exposing building blocks of QCD with the Lund plane, 2 examples

Larkoski et al, *Phys. Rev. Lett.* 119, 132003 (2017)

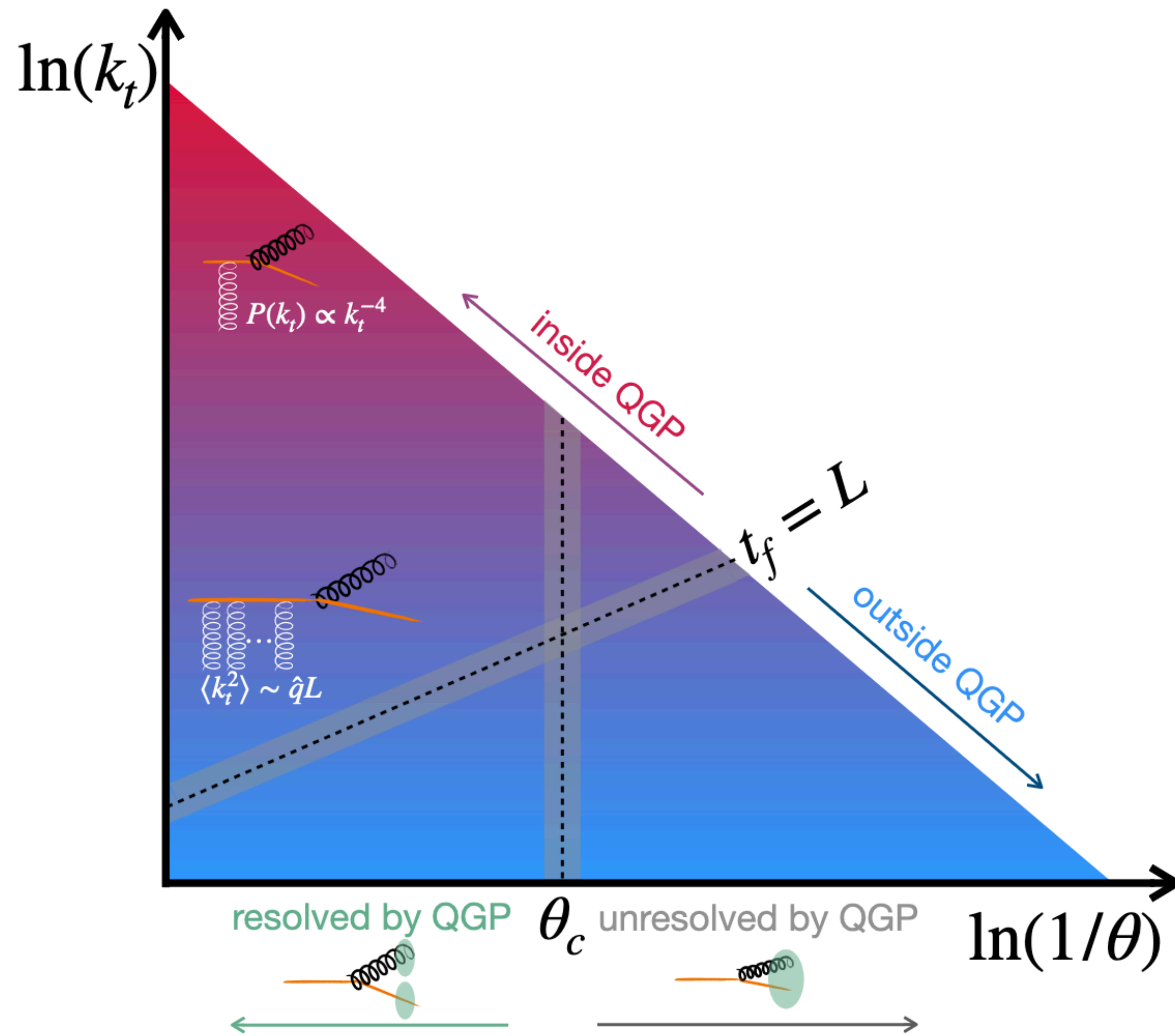
*ALICE, Nature* 605, 440-446 (2022)



SoftDrop momentum balance that asymptotes to the QCD splitting energy at sufficiently high jet energy

Direct visualization of the dead cone effect in bins of the energy of the radiating prong

# The Lund plane in heavy-ion collisions



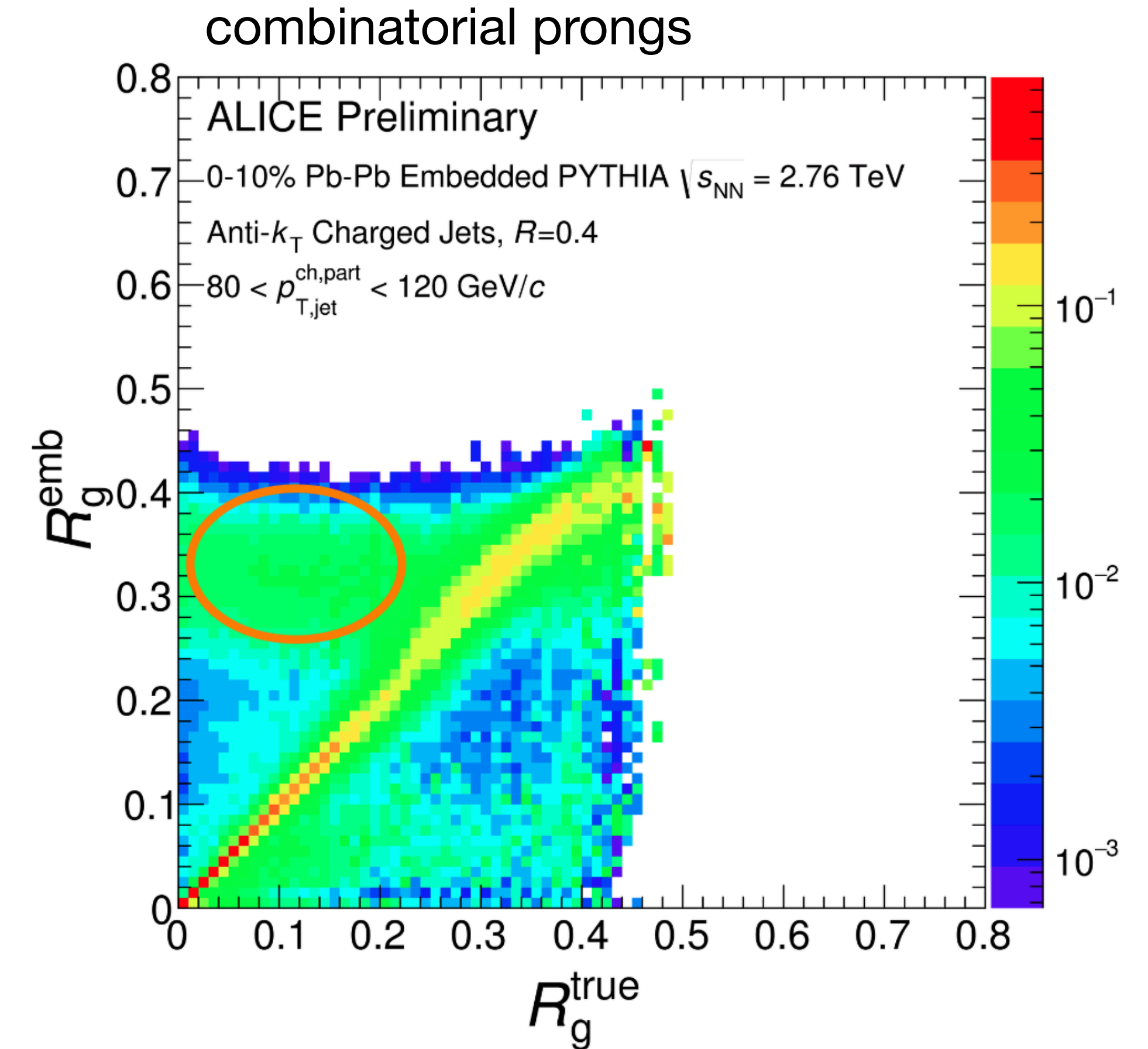
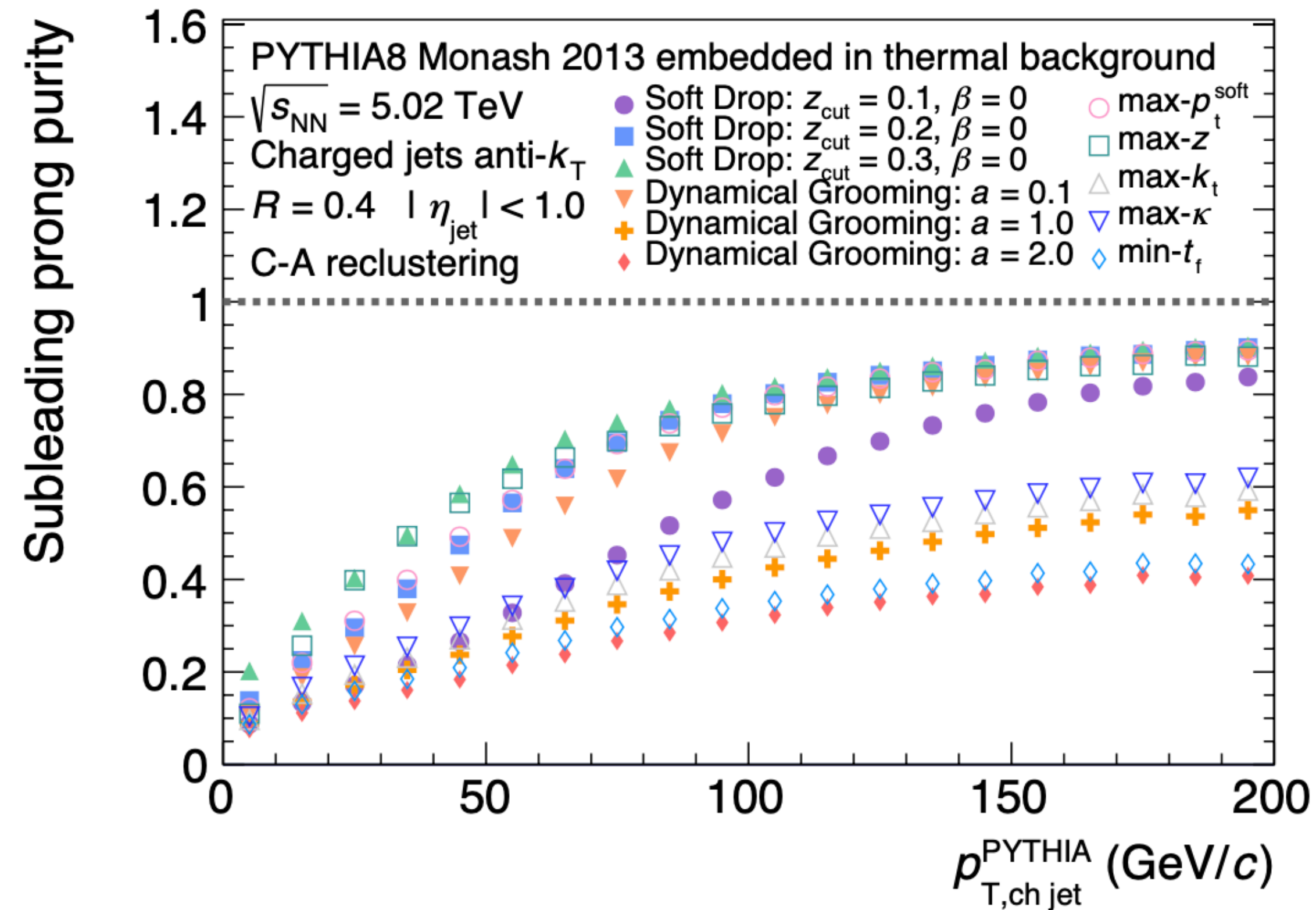
Strategies to isolate and characterize QGP-induced signal and map it to the microscopic properties of the QGP

sketch from Cunqueiro et al arXiv:2311.07643



# Scans of the Lund plane in PbPb: mismatches

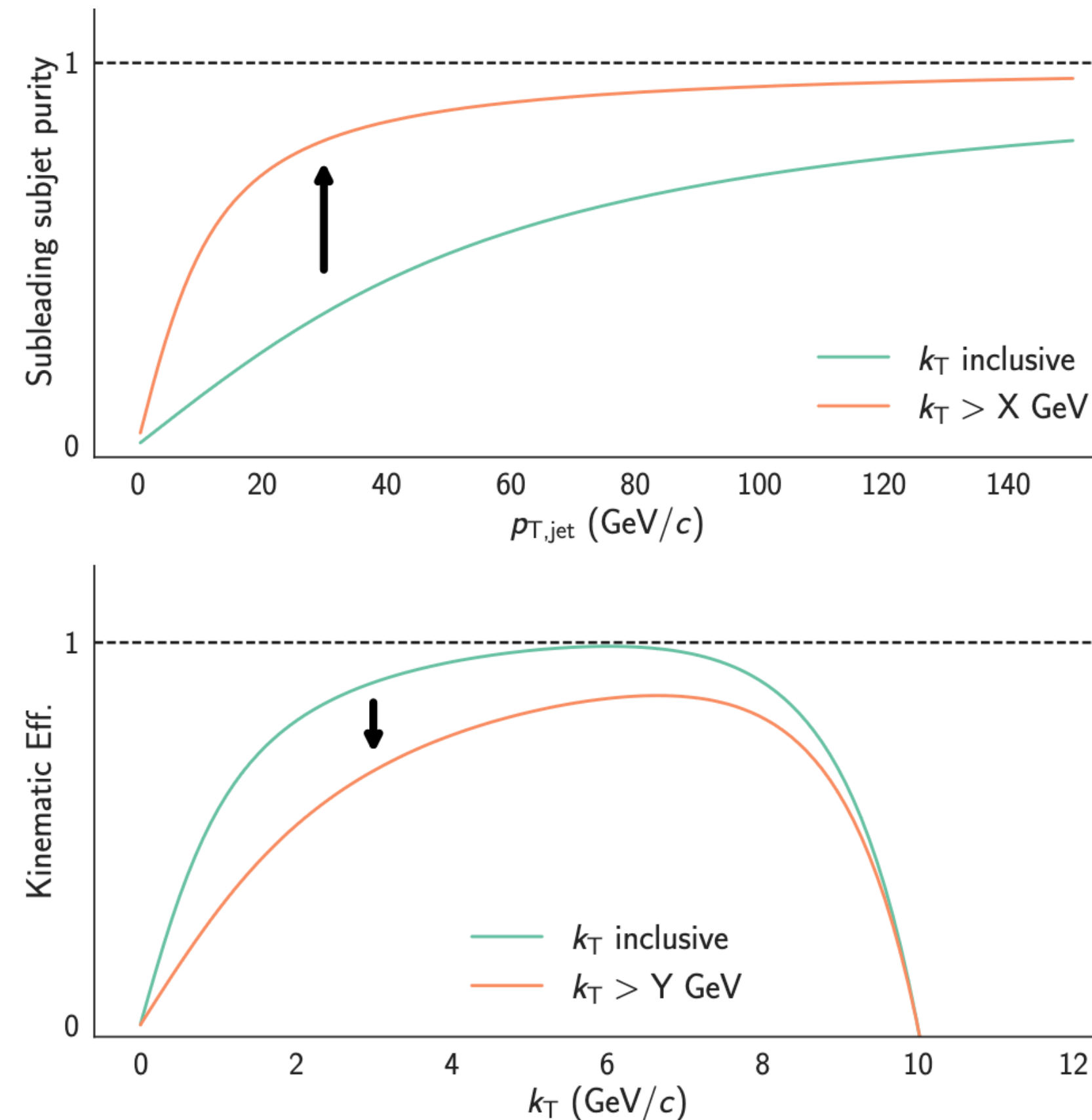
*Mulligan, Ploskon, Phs.Rev.C102 (2020)*



What in pp is just a few percent can become overwhelming in PbPb due to the large UE

## Scans of the Lund plane in PbPb: mismatches

- Dynamical Grooming exhibits **reduced subleading subjet purity** in Pb–Pb
- **Off-diagonal mismatched splittings** are major component at low  $k_T$
- **Problematic for unfolding**
- Caused by **requirement to always select a splitting**
- **Address by minimum measured  $k_T$  requirement**
- Trade **improved purity** for **reduced dynamic range** and kinematic efficiency
- **Minimum  $z$**  has similar impact



Raymond Ehlers, Lund Plane Workshop 23

Slide from Raymond showing a typical trade-off:

you cut on a variable ( $k_T$  of the splitting in this case) in order to suppress combinatorial prongs but then you have to deal with a big purely MC-based correction due to the background smearing of that variable

# Scans of the Lund plane in PbPb: uncertainties

## Model (prior) uncertainty

in pp is dominant

in PbPb, several strategies:

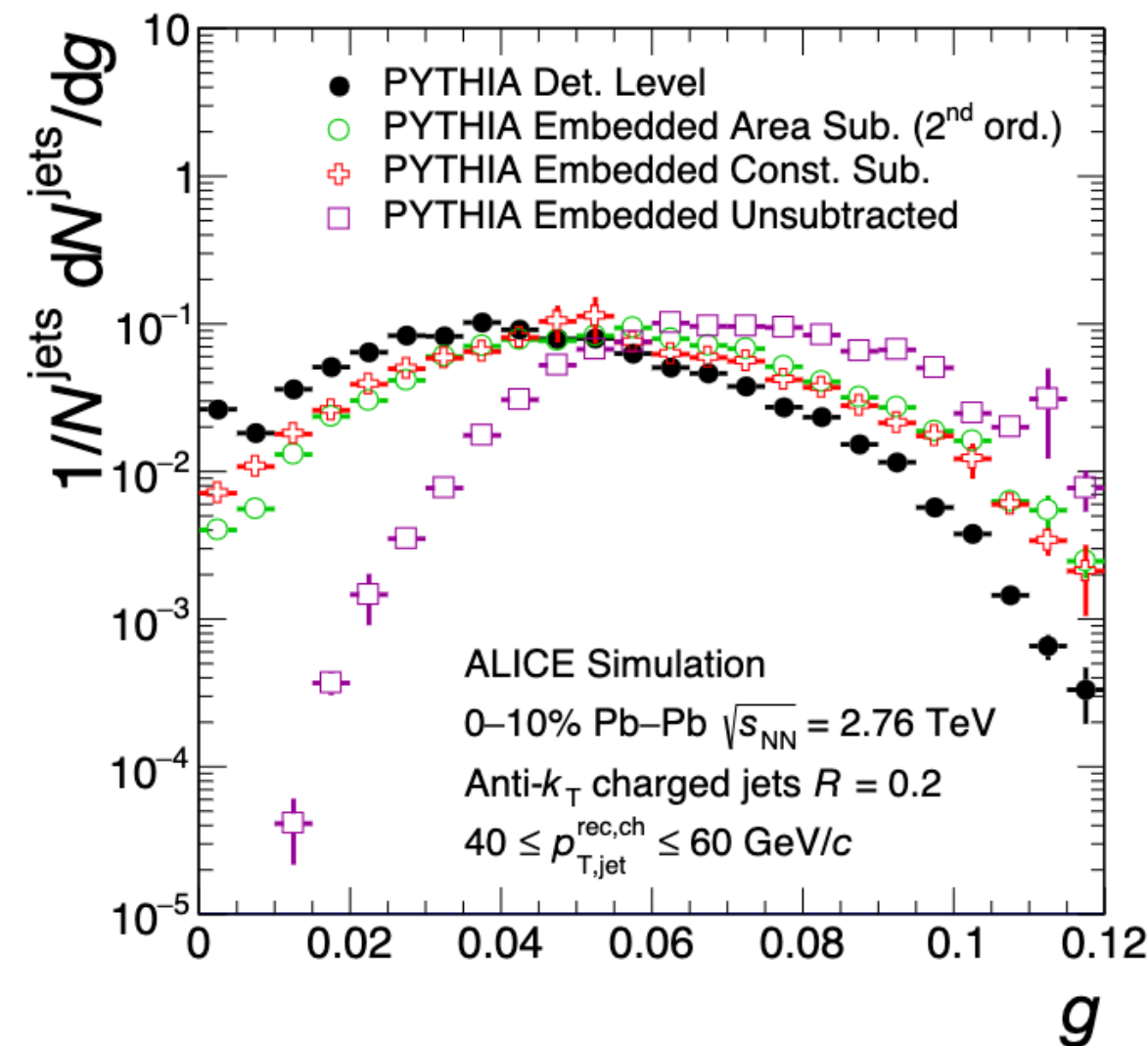
- nominal is typically pythia/herwig embedded into PbPb
- variation is a change of the q/g fraction in the vacuum baseline
- other educated guesses inspired by theory, see for instance [Phys.Lett.B 849 \(2024\) 138412](#)

## Background subtraction uncertainty

in pp we do not subtract the UE contribution

in PbPb, different strategies:

Constituent subtraction  
vs unbiased area  
subtraction



Pb–Pb	Relative uncertainty (%)					
	Trk. eff.	Unfolding	Generator	Tagging	Bkgd. sub.	Total
$z_g$						
0–10% $R = 0.2$	1–4%	1–4%	1–7%	1–2%	1–6%	4–10%
0–10% $R = 0.4$	1–13%	1–4%	1–7%	2–26%	4–28%	9–41%
30–50% $R = 0.4$	0–2%	0–5%	1–7%	1–6%	2–5%	5–9%
$\theta_g$						
0–10% $R = 0.2$	1–8%	1–4%	1–5%	1–19%	1–14%	3–24%
30–50% $R = 0.4$	3–6%	1–7%	1–5%	0–4%	2–15%	6–15%
30–50% $R = 0.4$ $z_{cut} = 0.4$	4–11%	2–11%	1–5%	1–5%	1–13%	4–20%

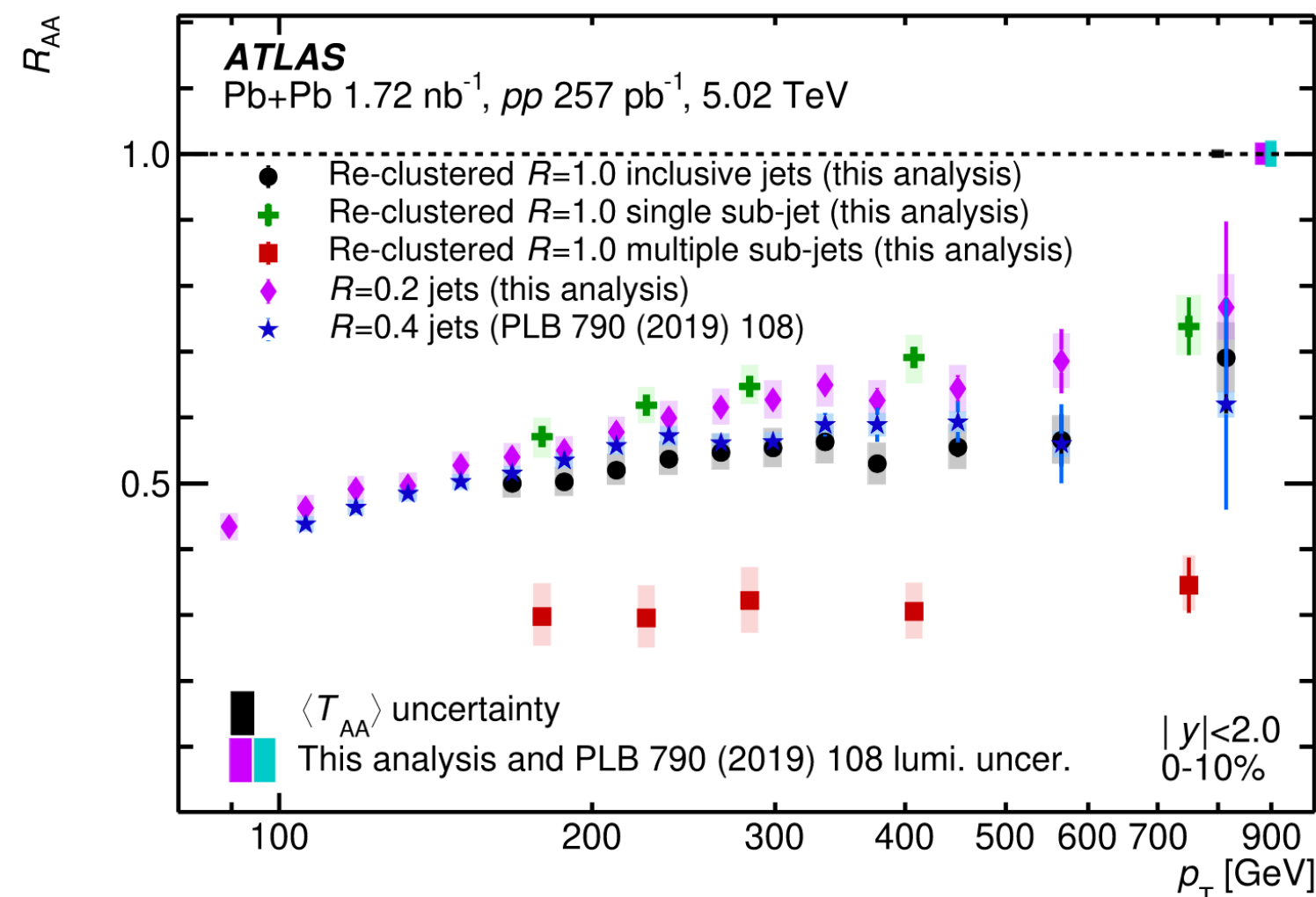
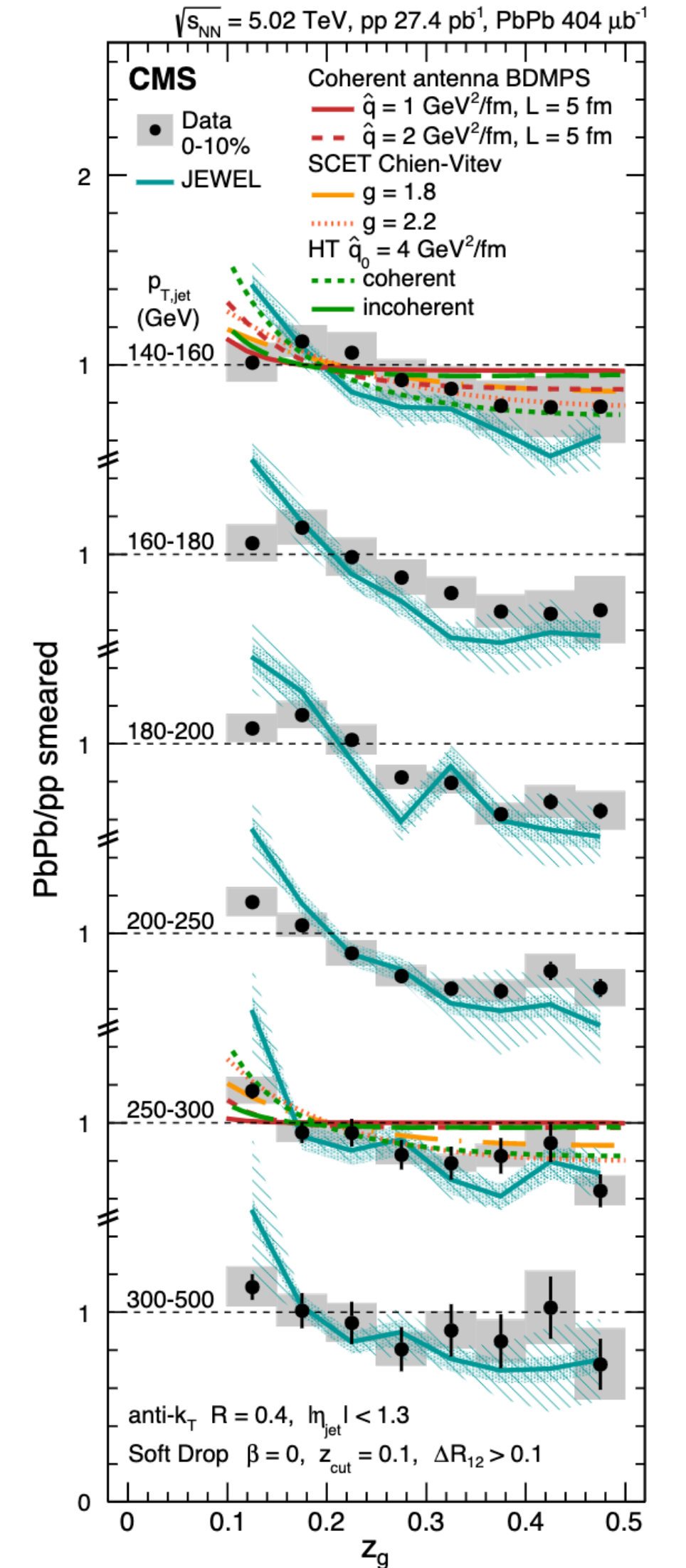
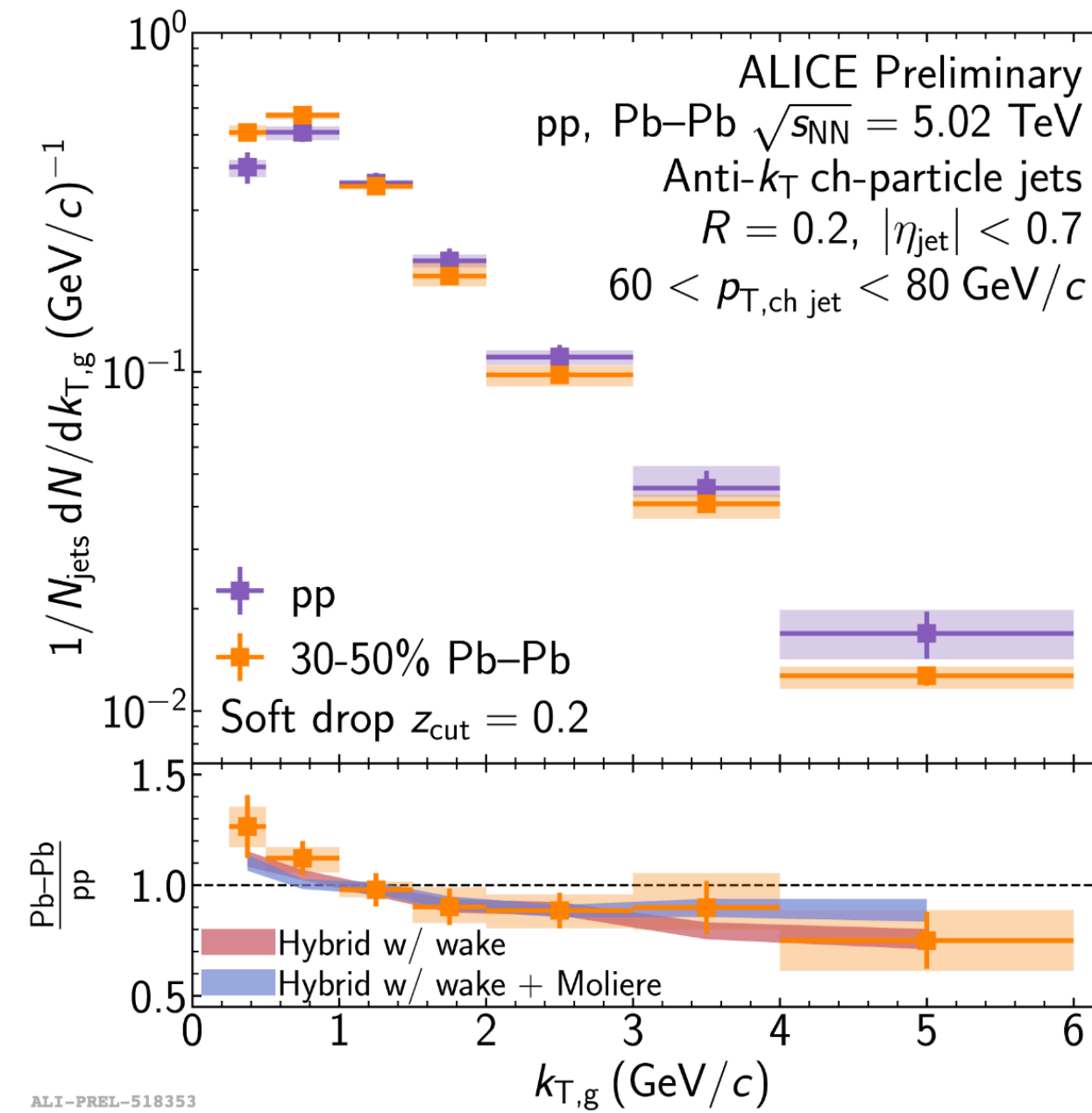
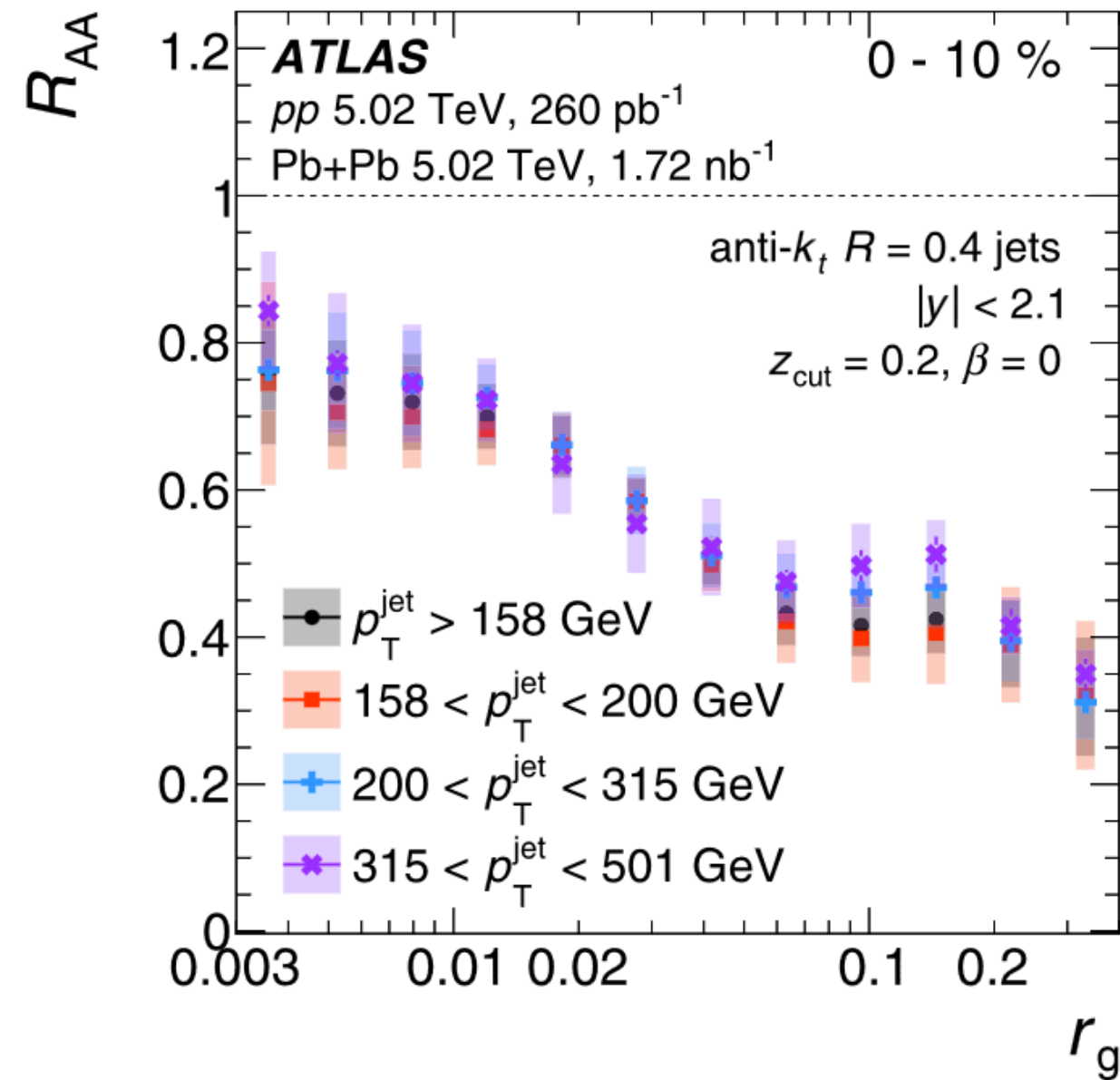
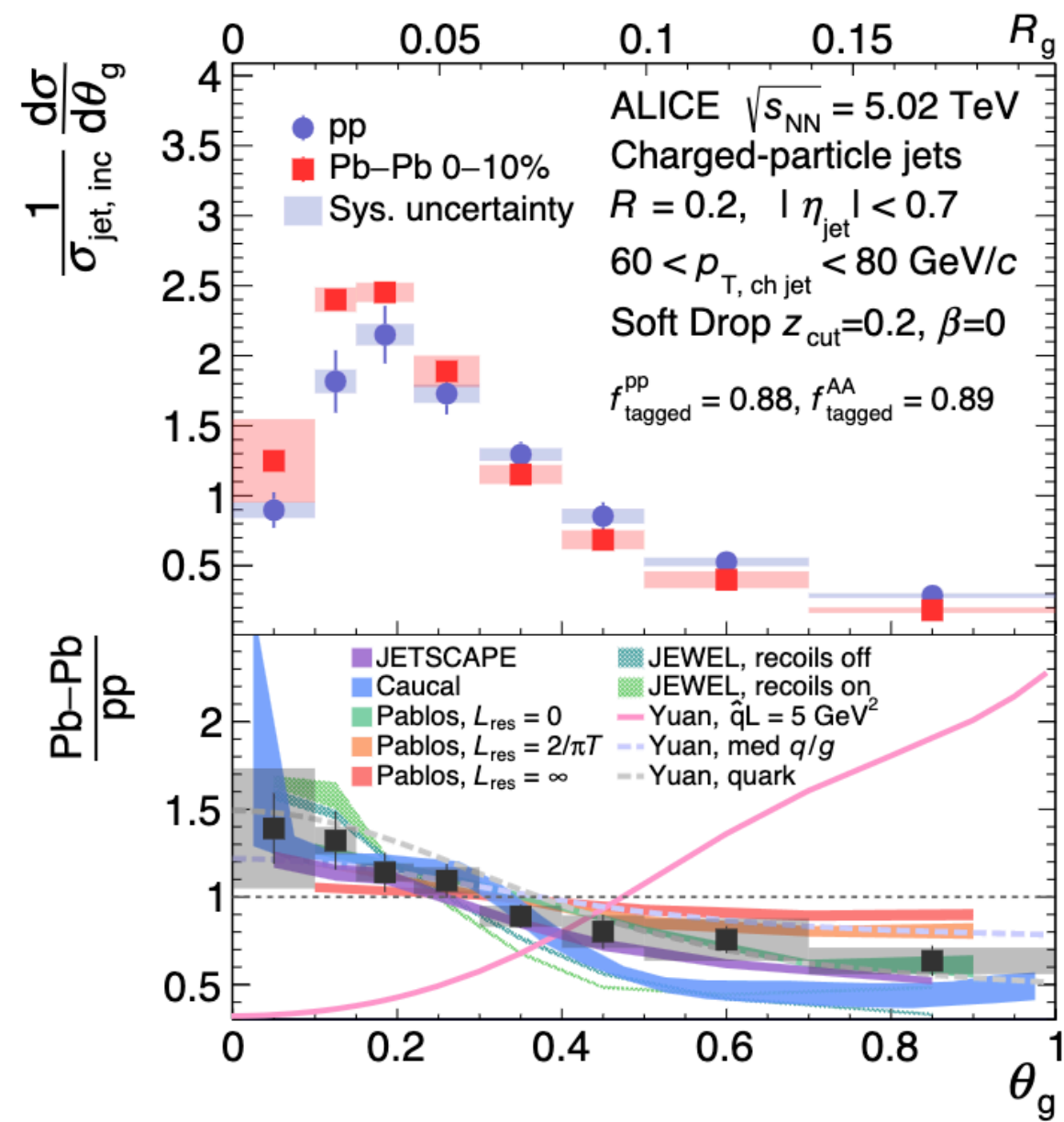
**Table 1:** Summary of systematic uncertainties on the Pb–Pb measurements. The ranges correspond to the minimum and maximum systematic uncertainties obtained. All values correspond to  $z_{cut} = 0.2$  unless otherwise noted.

Different  $R_{max}$  parameter in the event-wise constituent subtraction method were explored

[JHEP10\(2018\)139](#)  
[JHEP 1406 \(2014\) 092](#)  
[Phys.Rev.Lett. 110 \(2013\) 16](#)



# Scans of the Lund plane in PbPb: collage of results



In general all we see is a suppression of broad substructures, also at the level of jet shapes



## **A standard? factorized picture**

Due to formation time arguments, the shower is expected to factorize into an early, high-energy vacuum shower and a subsequent medium-modified shower

—>there is no experimental confirmation yet of factorization [see Alba's talk](#)

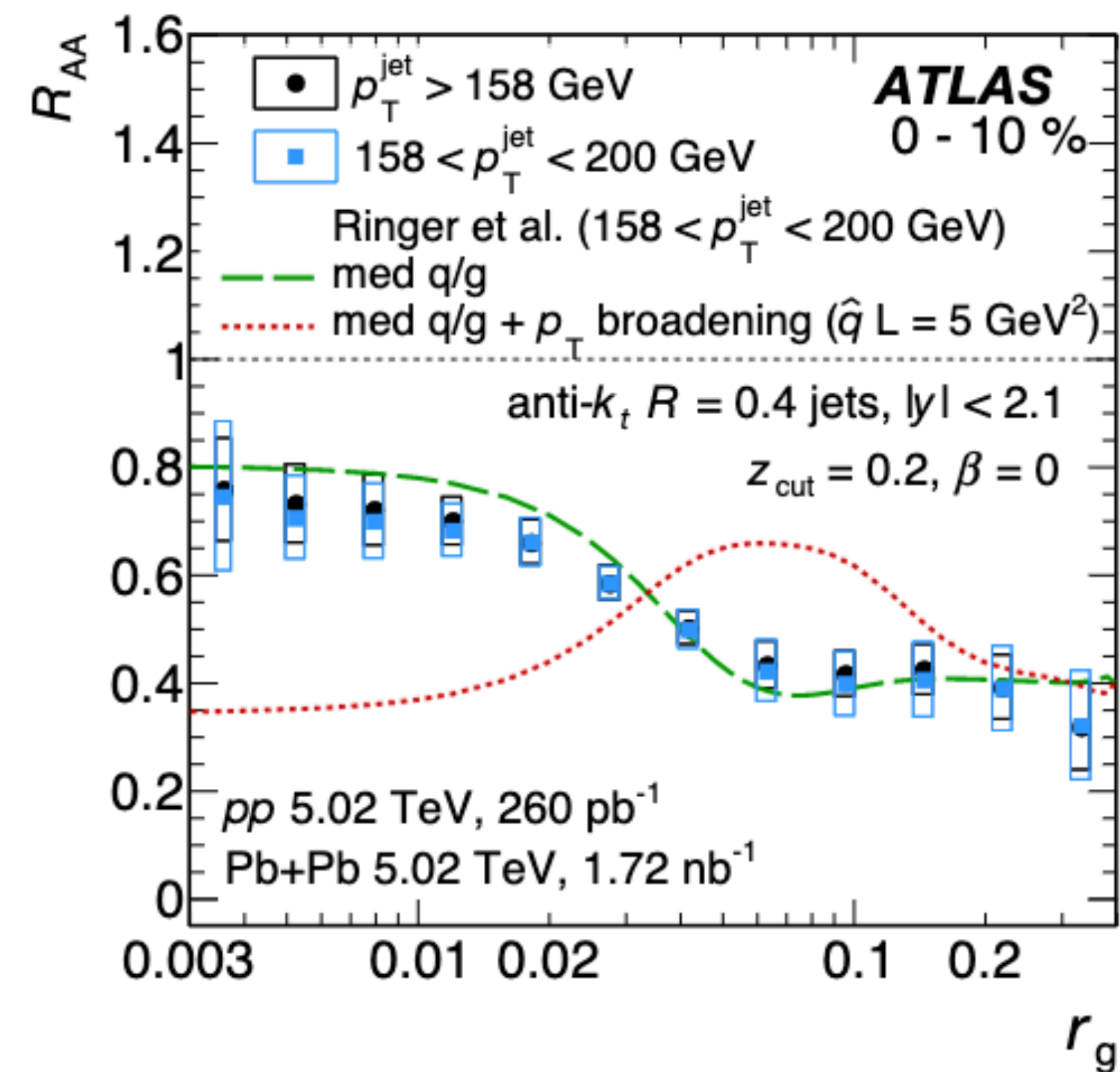
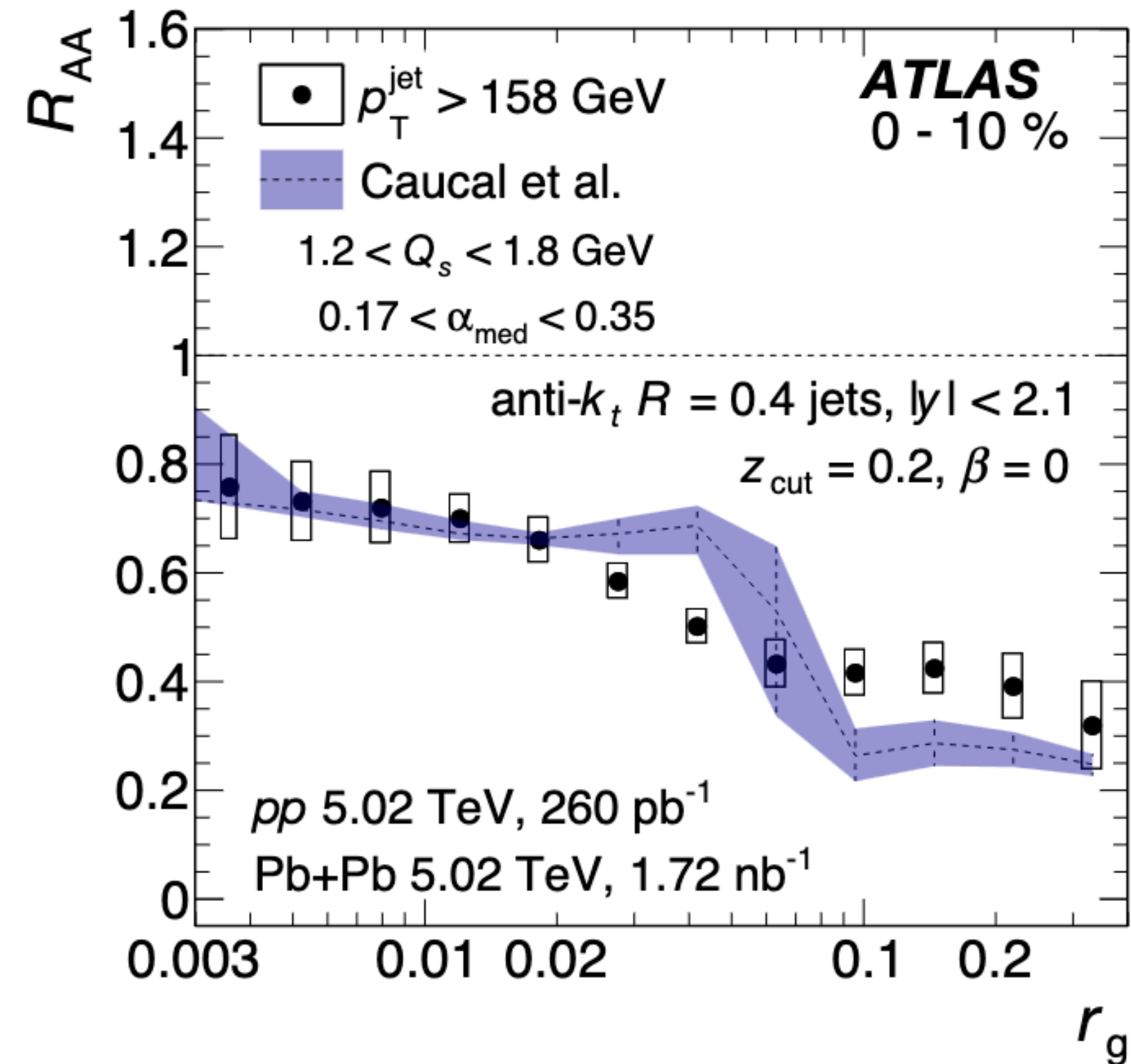
In this picture, early broad vacuum showers result into more quenched jets because they contain more in-medium emitters

Broad structures are more quenched and thus filtered out to other jet momentum bins, resulting in an **effective narrowing of the jet substructure**

In this picture color coherence regulates the amount of survivor bias by further reducing the amount of in-medium emitters

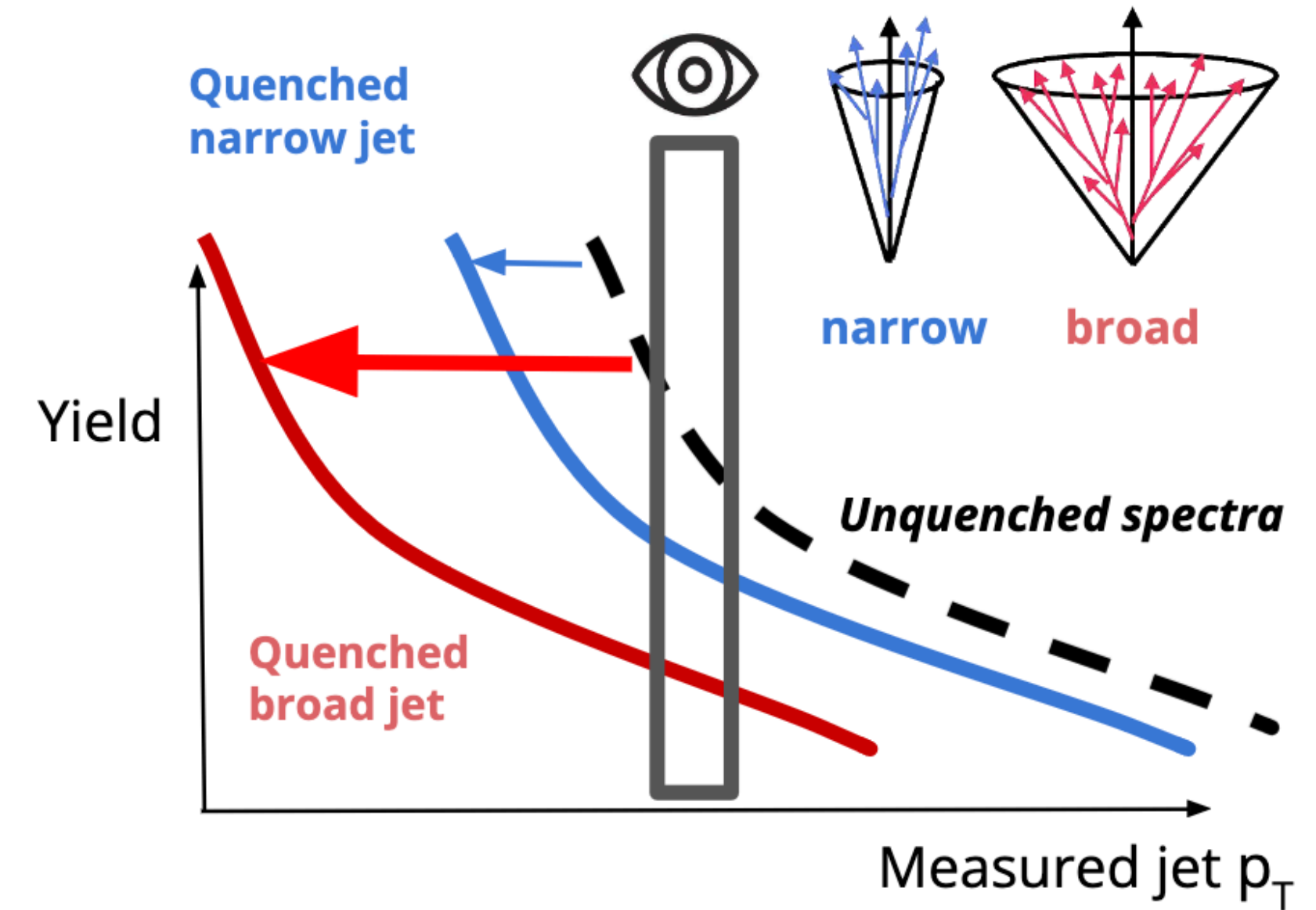
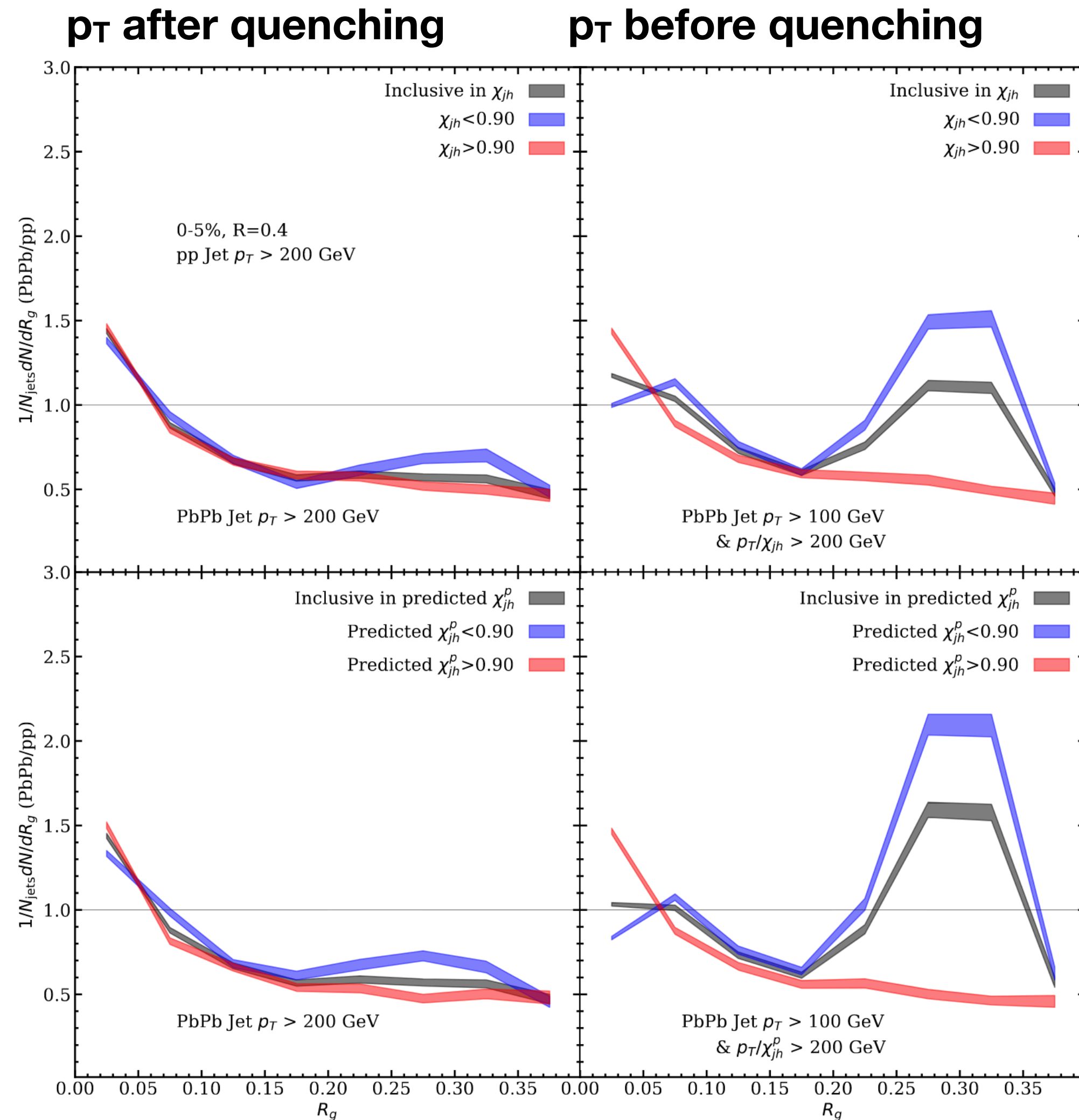
## Scans of the Lund plane in PbPb: collage of results

*ATLAS, Phys. Rev. C 107 (2023) 054909*



An intriguing step behaviour around the coherence angle in the implementation of Caucal et al  
 But step function also present in a model with no explicit implementation of coherence angle!

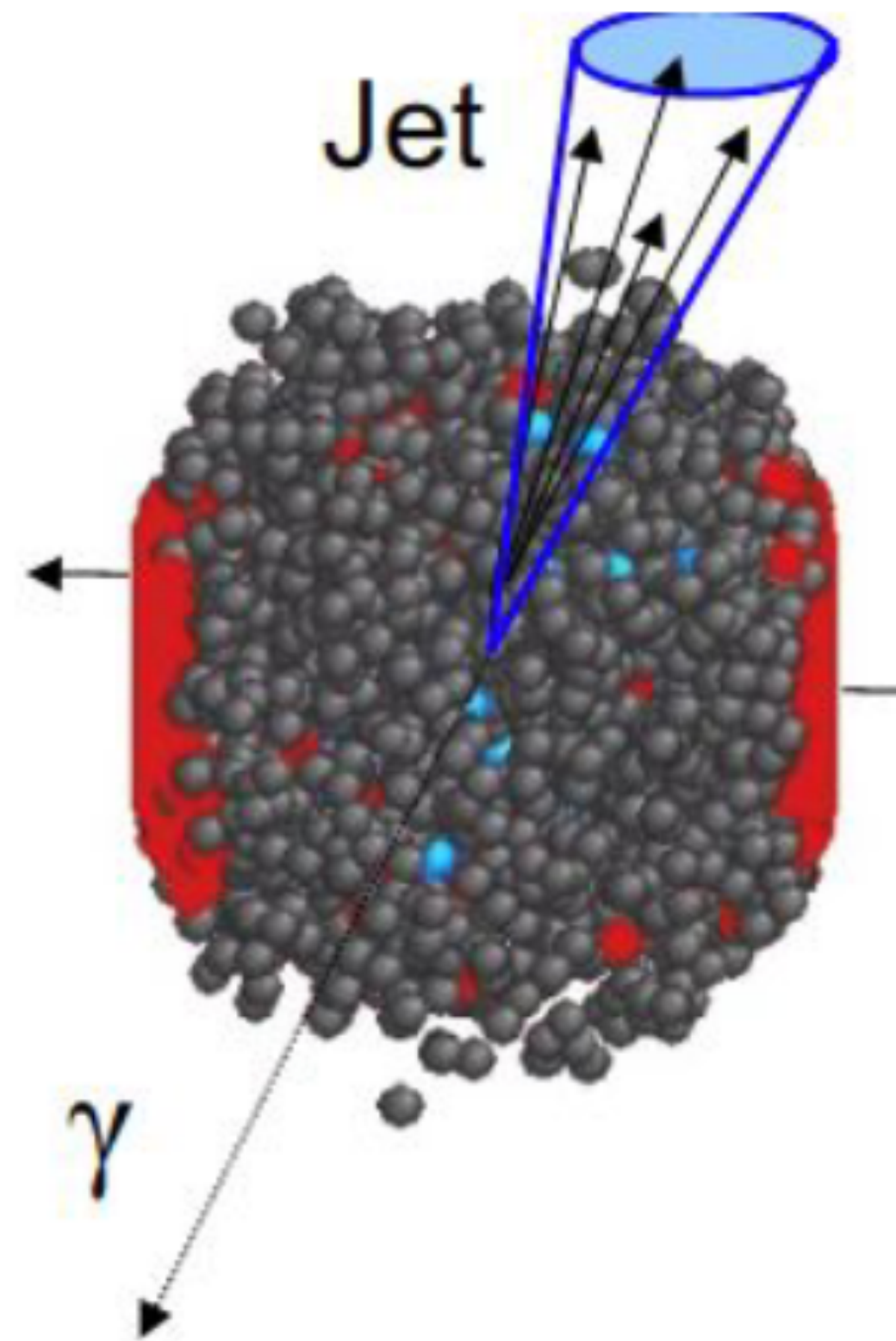
# $\gamma$ -jet substructure: suppression of the survivor bias



Inclusive measurements are limited by selection bias  
 Effective narrowing: broader jets are more quenched and migrate to lower p<sub>T</sub> bins



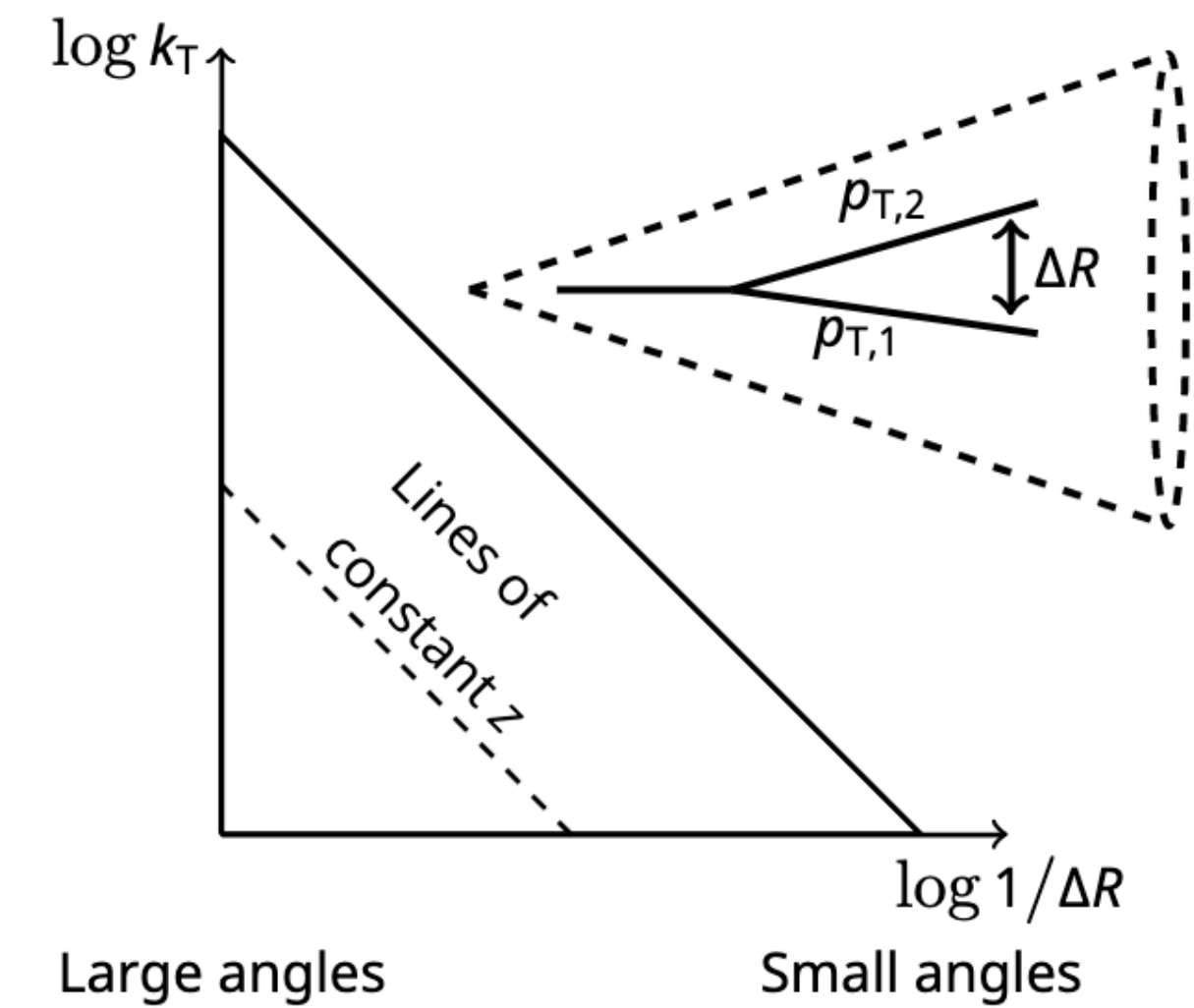
## $\gamma$ -jet substructure: suppression of the survivor bias



The EW boson does not interact strongly with the QGP

The ratio  $x_J = p_T^{jet} / p_T^\gamma$  can be used as a proxy of the degree of quenching of the recoiling jet

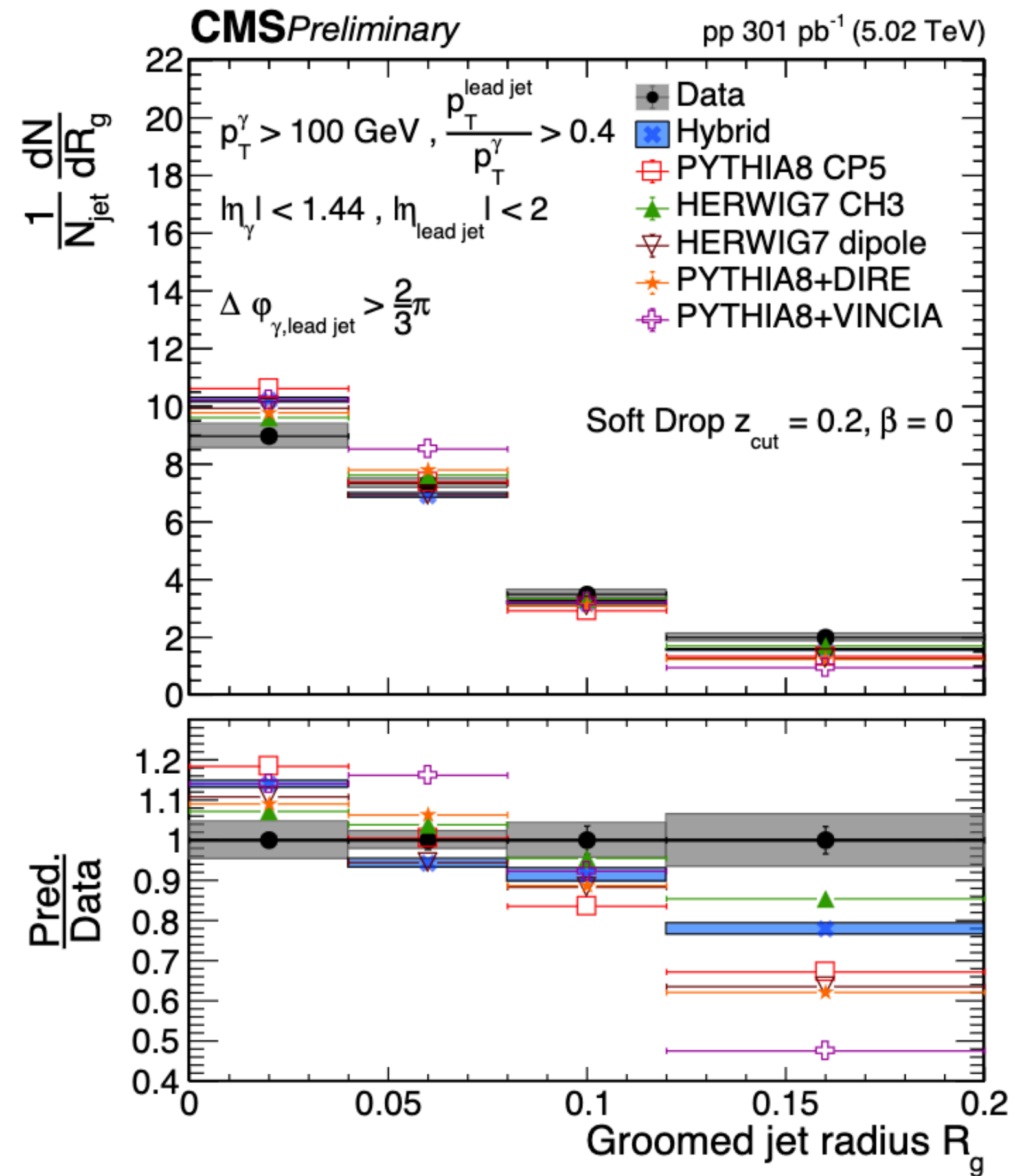
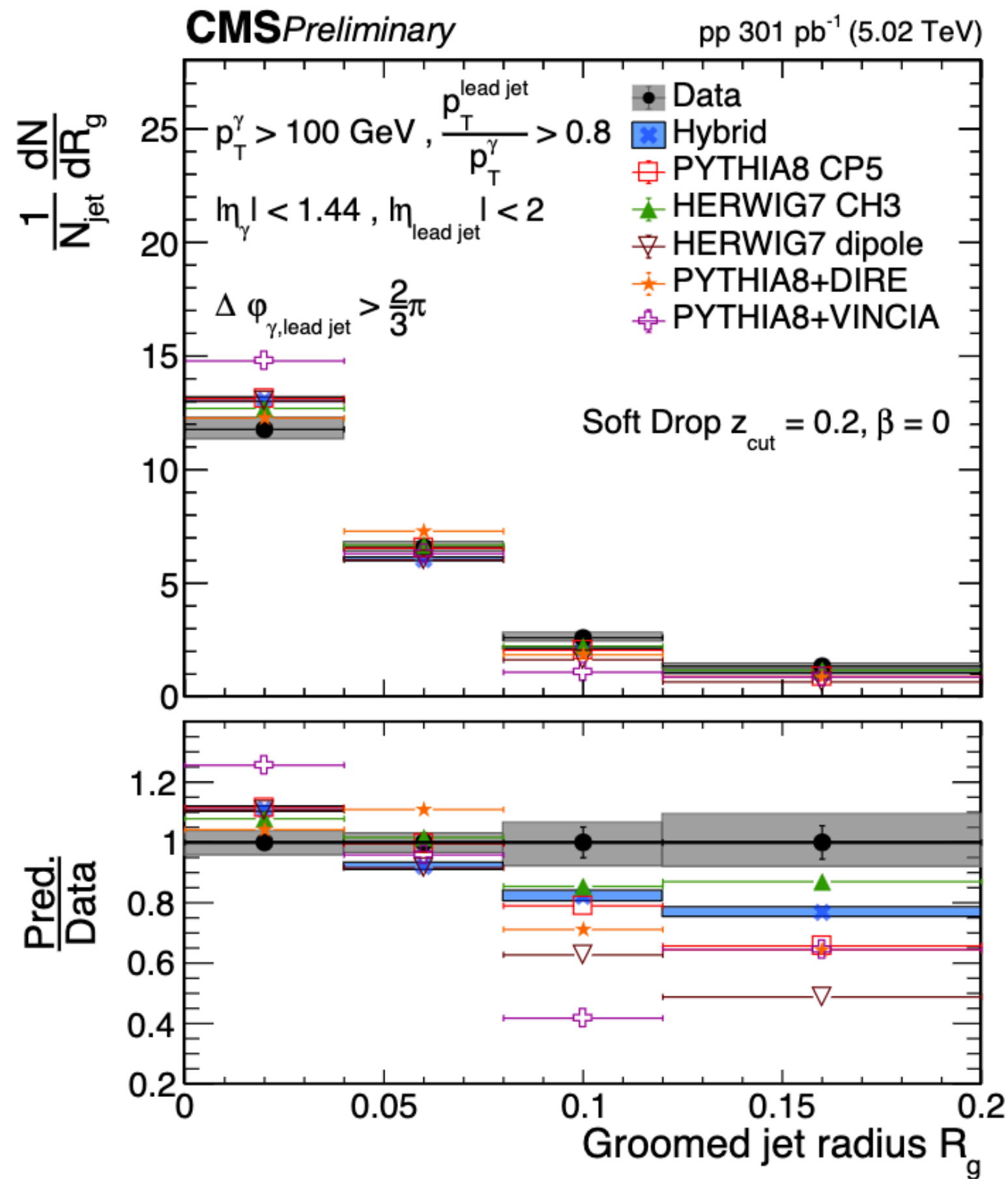
We look at the Lund plane section defined by SoftDrop grooming





# $\gamma$ -jet substructure: suppression of the survivor bias

pp



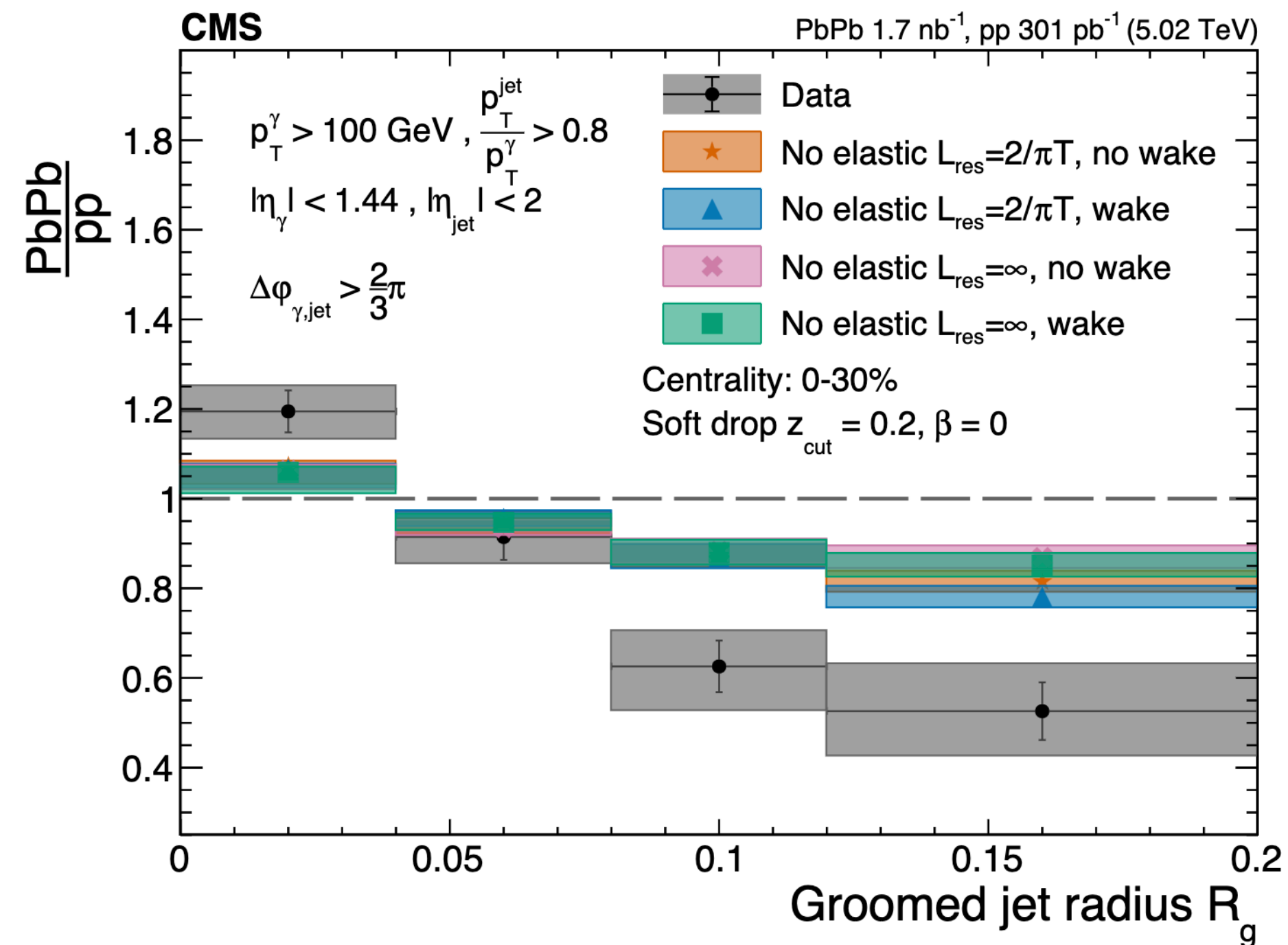
More ( $x_J > 0.8$ ) or less ( $x_J > 0.4$ ) balanced jets due to vacuum out of cone radiation

Worse description by models than in the inclusive case, in particular in the tails of the distribution

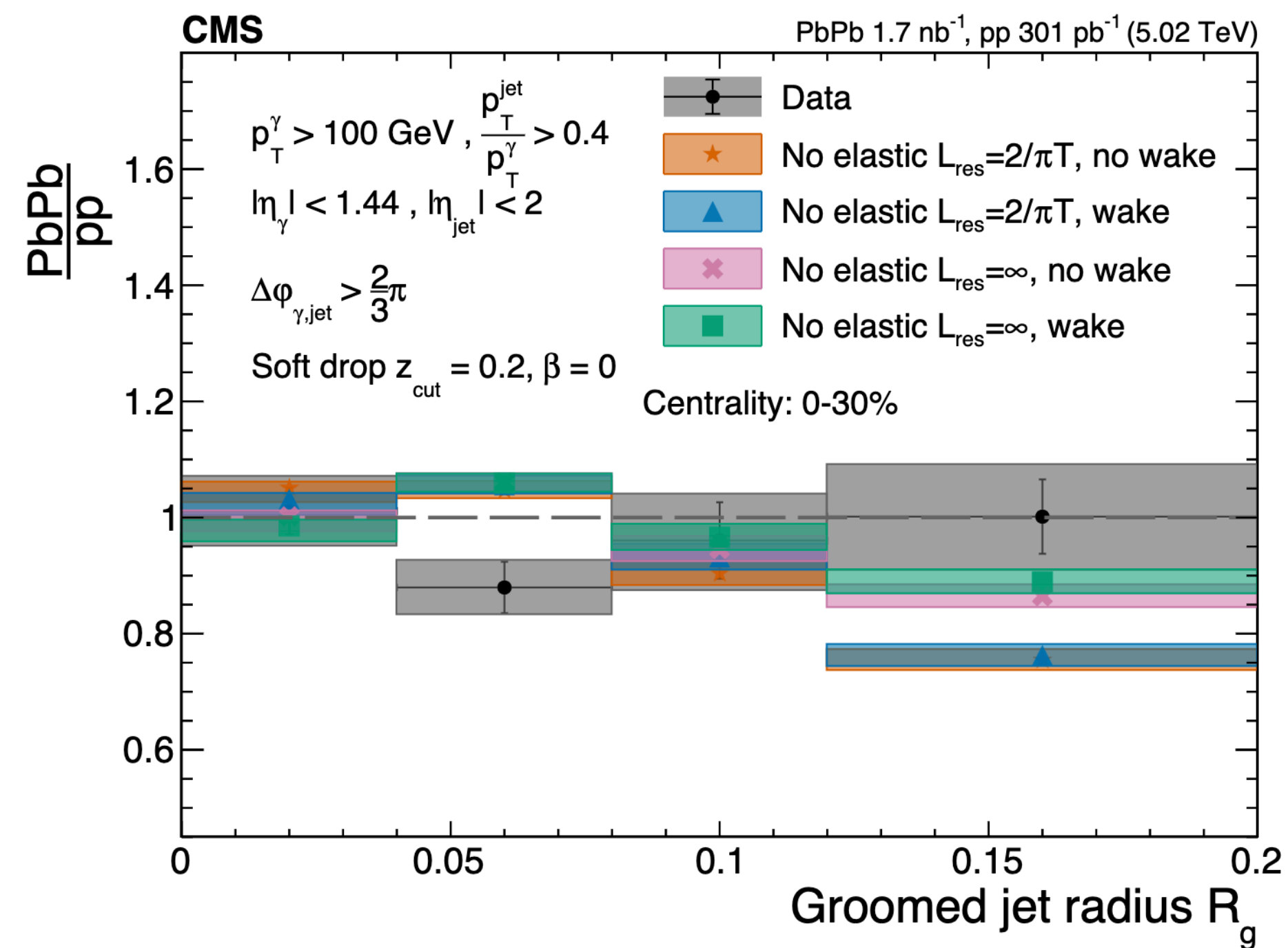
# $\gamma$ -jet substructure: suppression of the survivor bias

PbPb

less quenched  $x_J > 0.8$



more quenched  $x_J > 0.4$



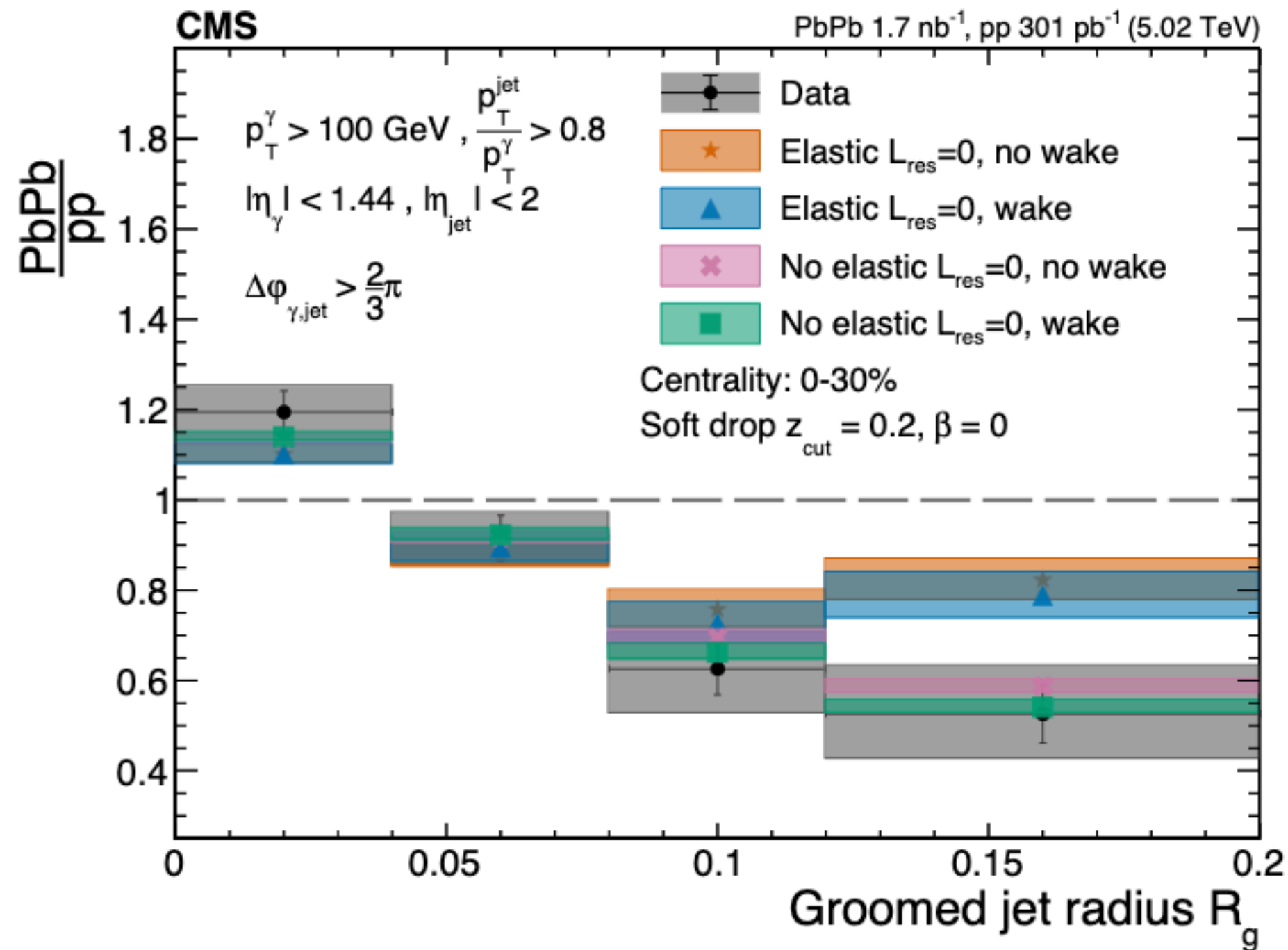
Strong narrowing for jets that are less quenched

No narrowing when including more quenched jets in the recoil sample → survivor bias!

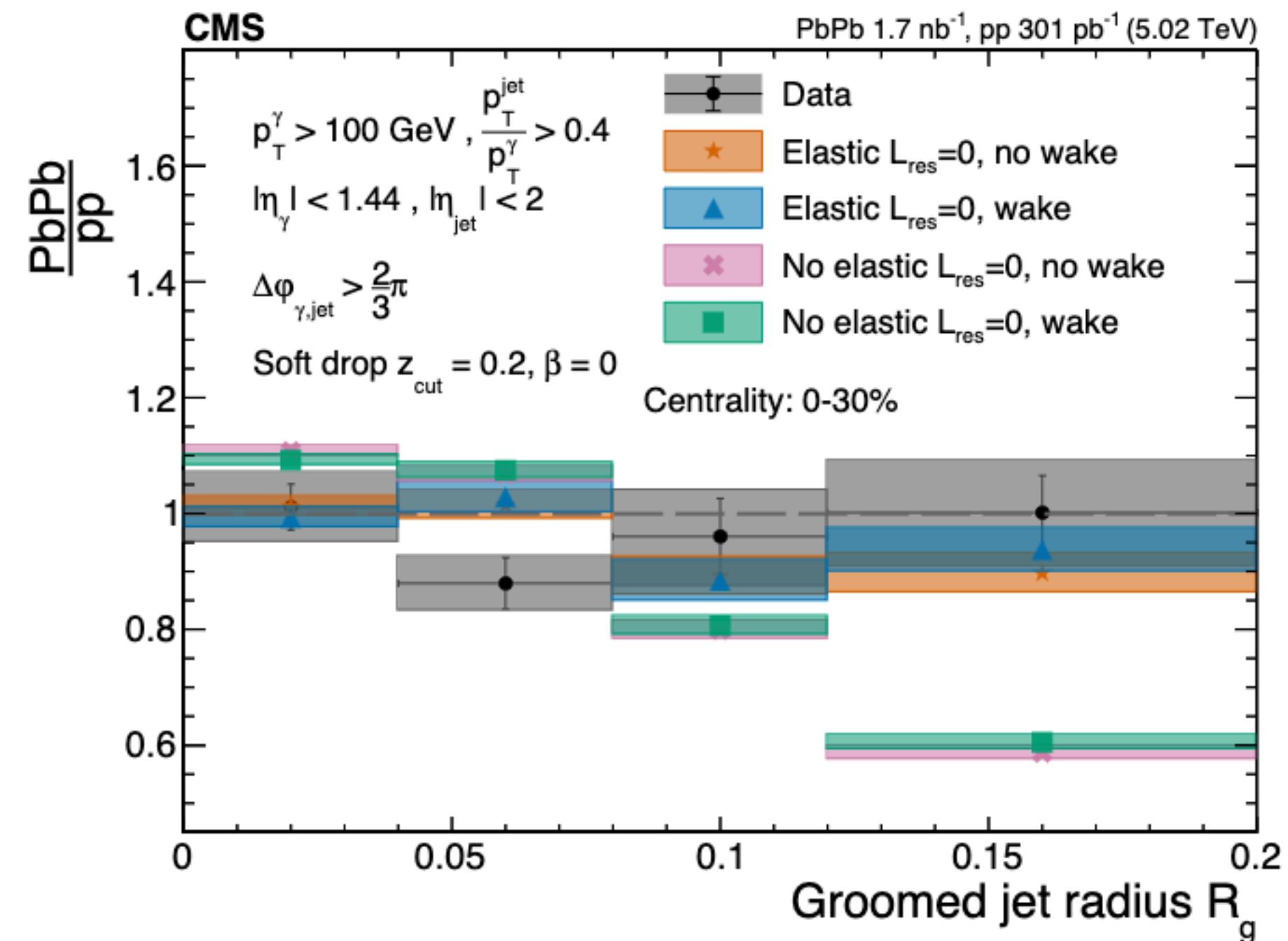
# $\gamma$ -jet substructure: suppression of the survivor bias

PbPb

less quenched  $x_J > 0.8$



more quenched  $x_J > 0.4$



## Comparison to the Hybrid model ([Rajagopal et al, JHEP 10 \(2014\) 019](#))

Factorized by construction

Interplay of several mechanisms:

Energy loss

Elastic hard interactions (interaction with free q/g within QGP)

Resolution length

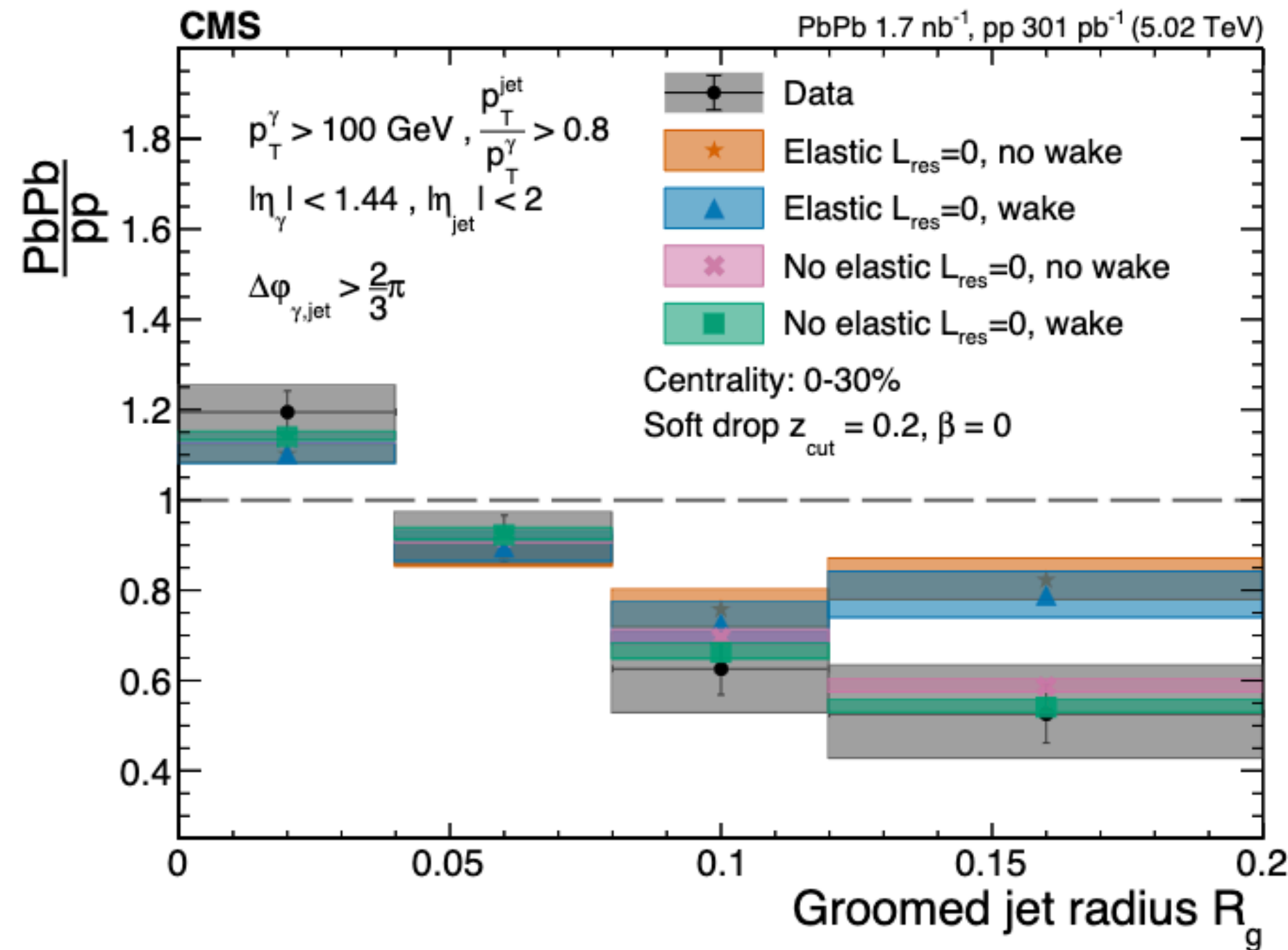
small-R suppresses nonperturbative effects like the wake!



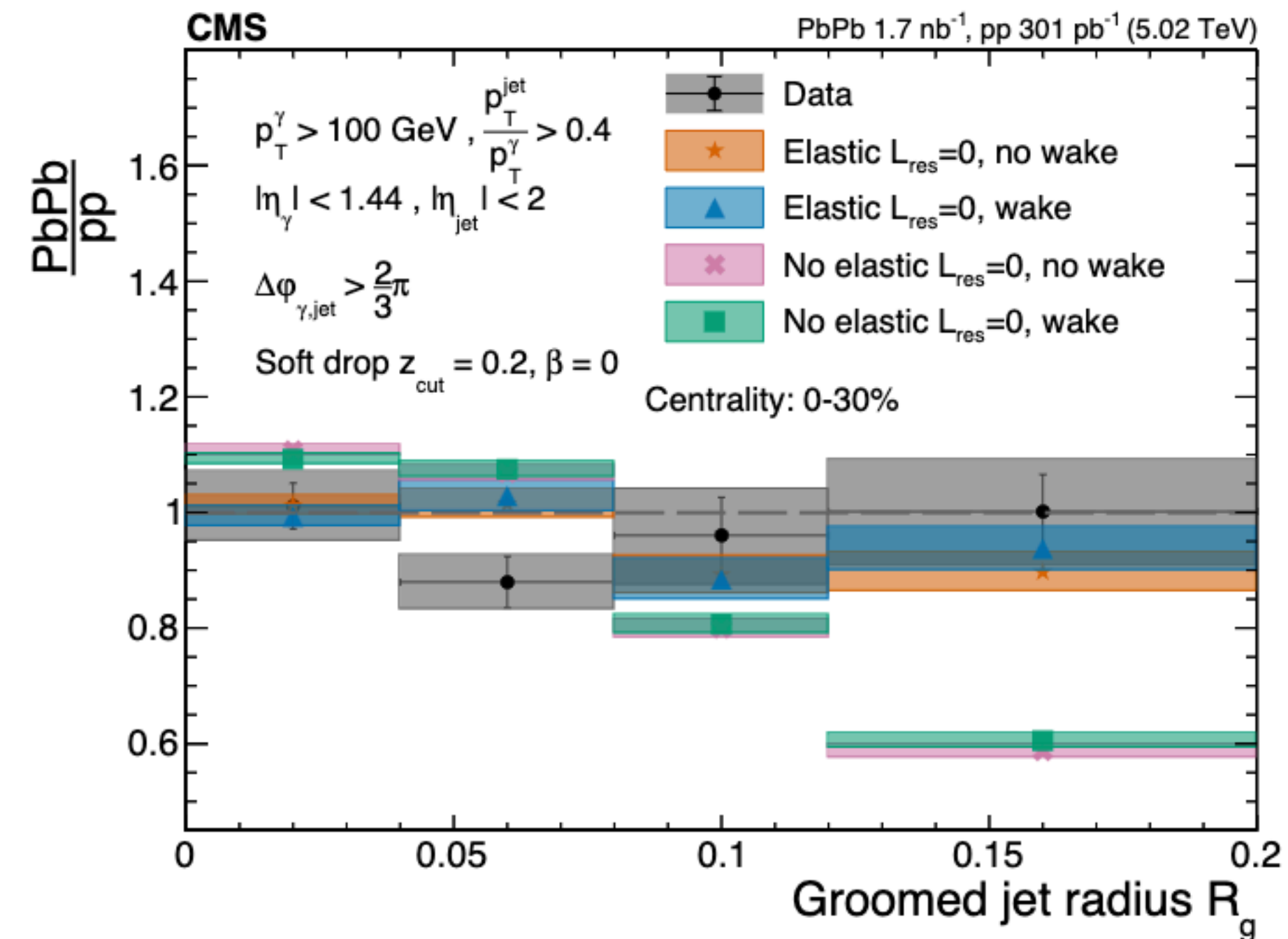
# $\gamma$ -jet substructure: suppression of the survivor bias

PbPb

less quenched  $x_J > 0.8$



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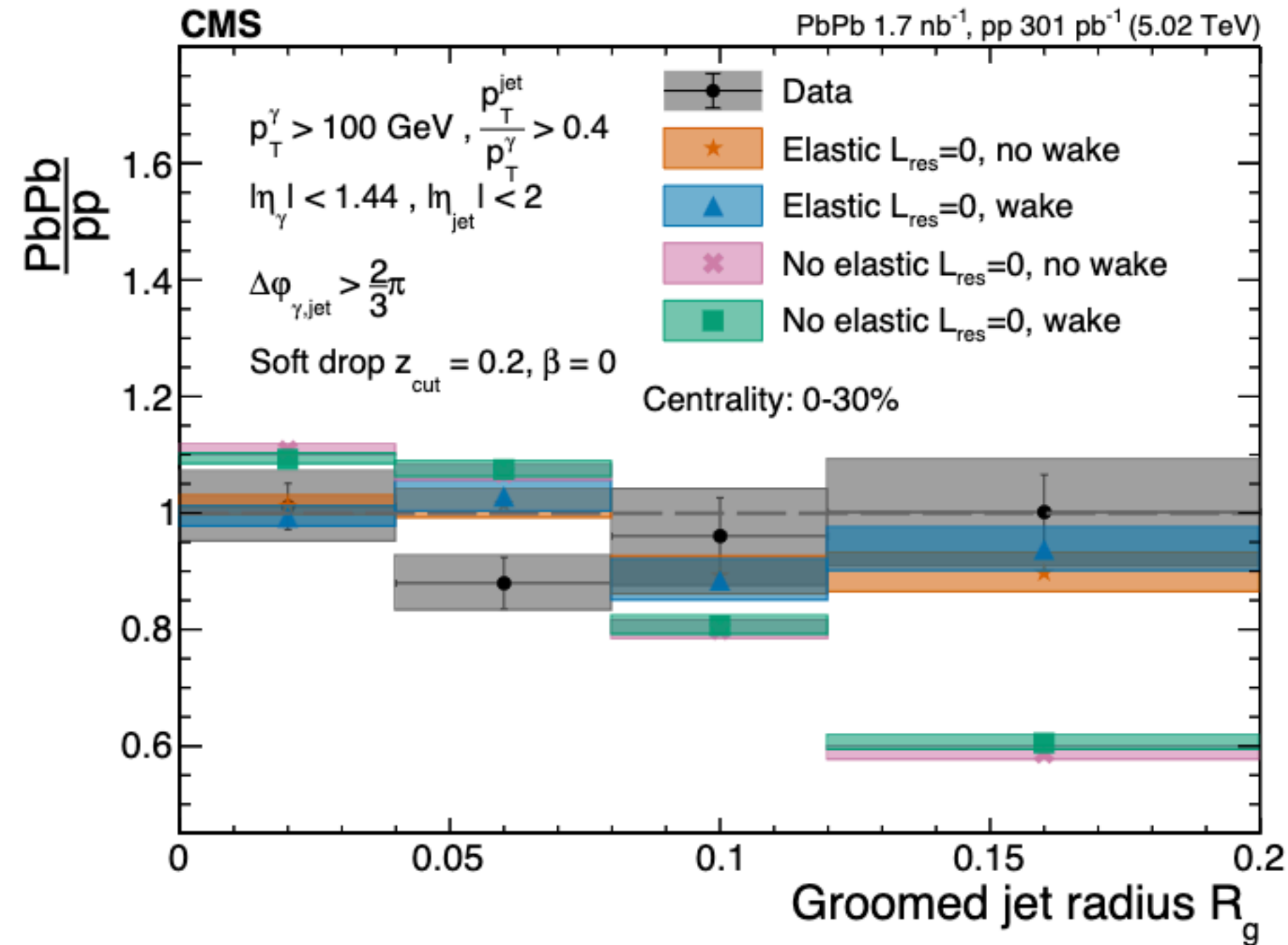
## Comparison to the Hybrid model ([Rajagopal et al, JHEP 10 \(2014\) 019](#))

Not a single set of parameters describes the differential data consistently  
Great constraining power of the data

small- $R$  suppresses nonperturbative effects like the wake!

# $\gamma$ -jet substructure, prospects

$x_J > 0.4$



The survivor bias can be fully suppressed when  $x_J \rightarrow 0$   
 (the model has a strong survivor bias down to  $x_J=0.1$ )

Since low jet  $p_T$  is limited by detector effects, such zero bias limit can be achieved by increasing the energy of the photons

Ideally, **simultaneous measurement of  $x_J$  and substructure**, current results are statistically limited

# Summary

The Lund plane density in pp: strong constrain to the parton shower in a “modular” fashion

Building blocks of the parton shower exposed: splitting functions, dead cone.

Inspection of the Lund plane in heavy-ion collisions is an active area of research, fundamental microscopic properties of the QGP at reach

In order to measure the amount of intrajet broadening to link it to fundamental properties, survivor bias needs to be suppressed: new possibilities using EW-boson tagged jet substructure

Interplay between anti angular ordered emissions and CA algorithm for jet quenching needs further study

New interesting possibilities in the domain of heavy flavour jet substructure, but not the scope of this talk