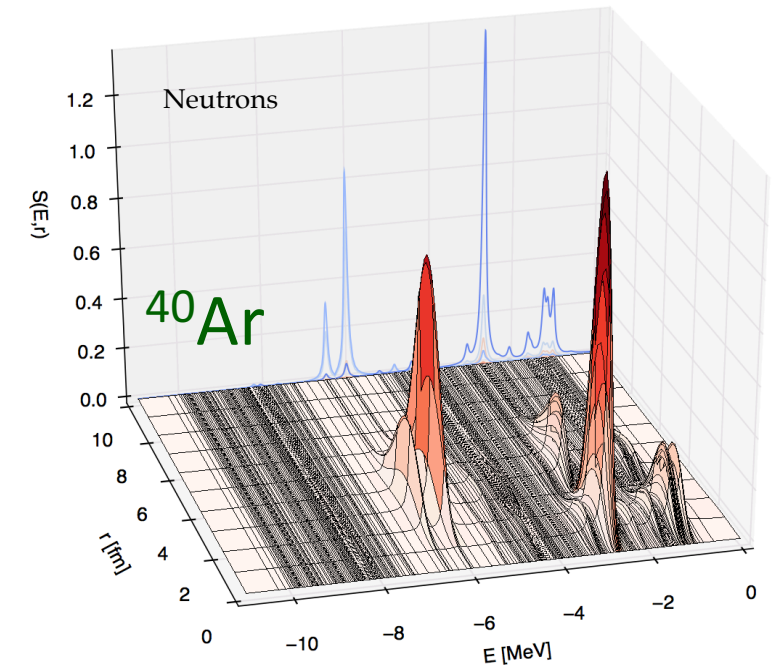
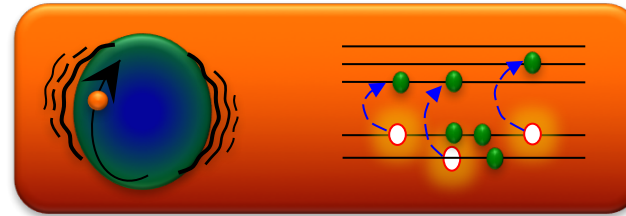
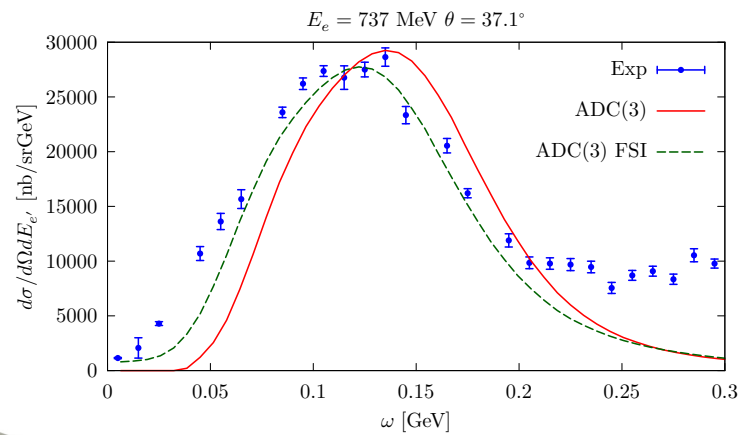


Use of *ab initio* approaches for accurate lepton-nucleus scattering

Carlo Barbieri — University of Surrey

10 July 2018



Current Status of low-energy nuclear physics

Composite system of interacting fermions

Binding and limits of stability

Coexistence of individual and collective behaviors

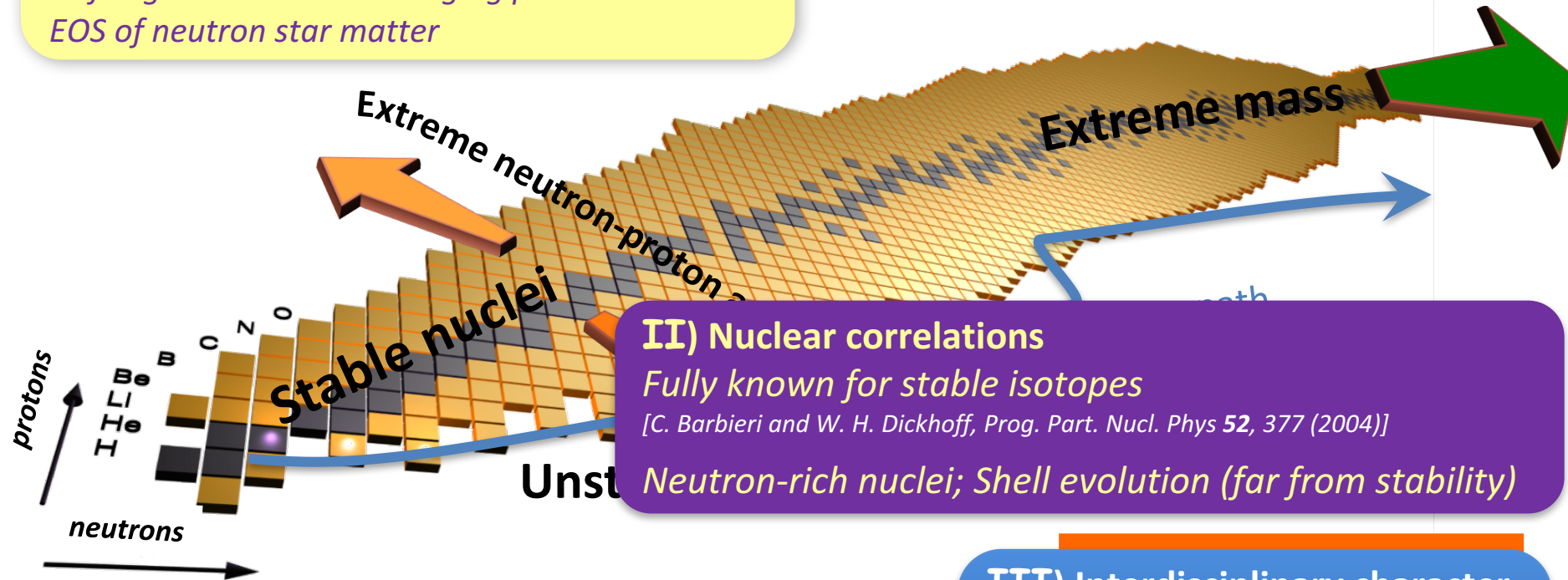
Self-organization and emerging phenomena

EOS of neutron star matter

Experimental

programs

RIKEN, FAIR, FRIB...



II) Nuclear correlations

Fully known for stable isotopes

*[C. Barbieri and W. H. Dickhoff, Prog. Part. Nucl. Phys **52**, 377 (2004)]*

Neutron-rich nuclei; Shell evolution (far from stability)

I) Understanding the nuclear force

QCD-derived; 3-nucleon forces (3NFs)

First principle (ab-initio) predictions

III) Interdisciplinary character

Astrophysics

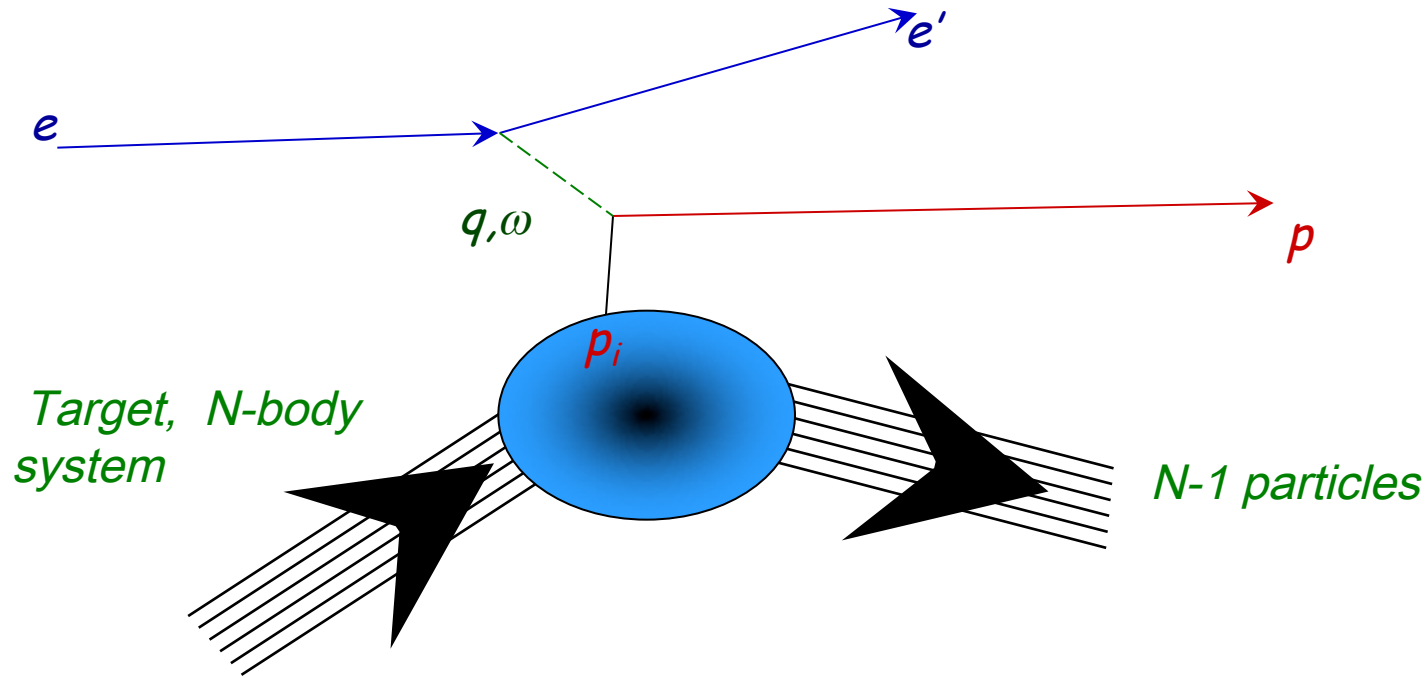
Tests of the standard model

Other fermionic systems:

ultracold gasses; molecules;

Spectroscopy via knock out reactions-*basic idea*

Use a probe (ANY probe) to eject the particle we are interested to:



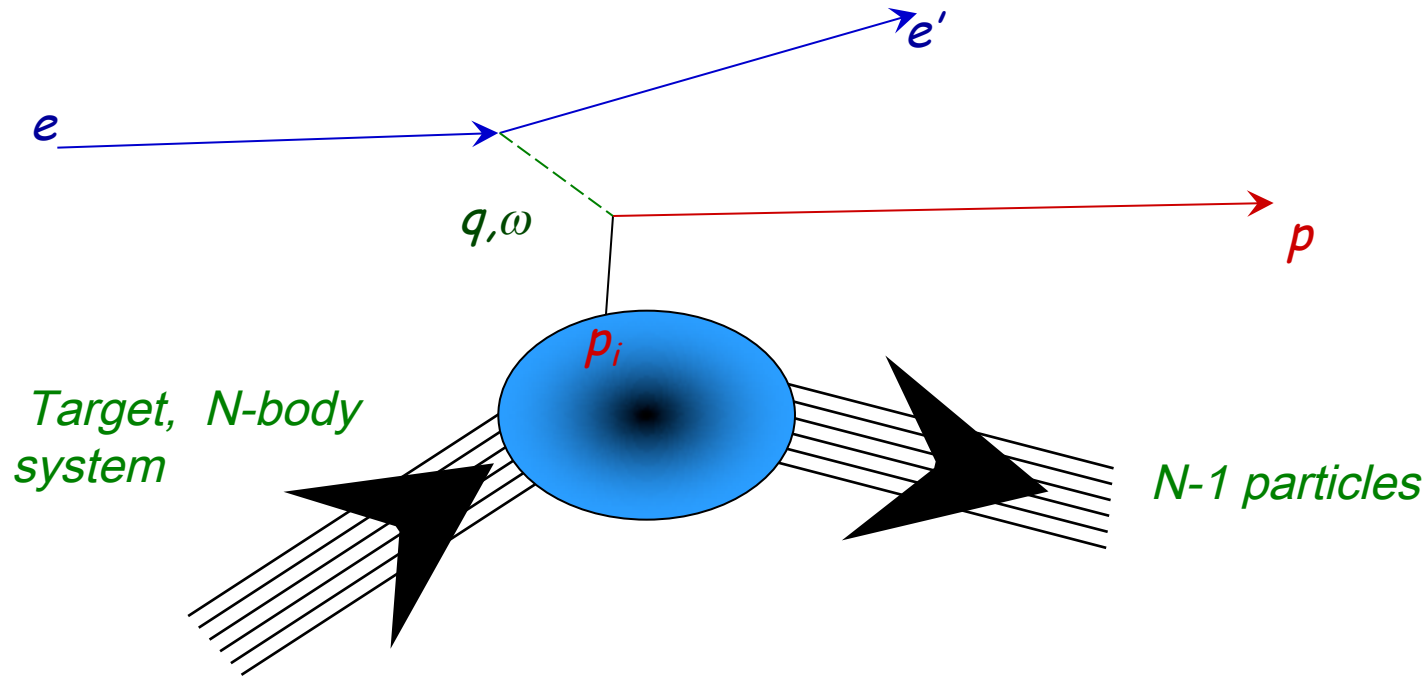
Basic idea:

- we know, e , e' and p
- "get" *energy and momentum of p_i* :
$$p_i = k_{e'} + k_p - k_e$$
$$E_i = E_{e'} + E_p - E_e$$

Better to choose
large transferred
momentum and weak
probes!!!

Spectroscopy via knock out reactions—*basic idea*

Use a probe (ANY probe) to eject the particle we are interested to:

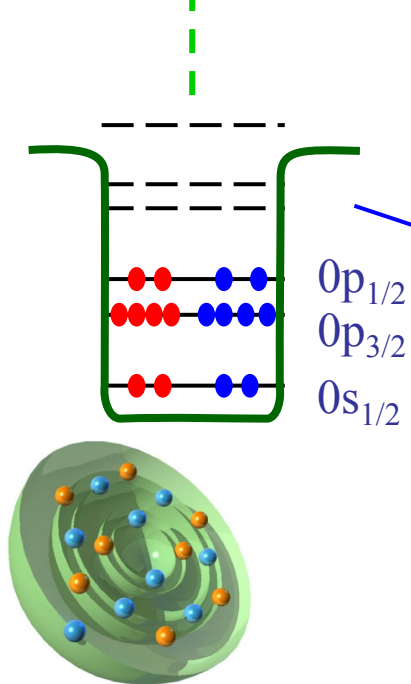


In plane wave impulse approximation (PWIA):

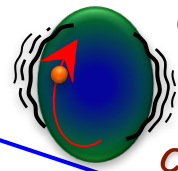
$$\frac{d\sigma_{(e,e'p)}}{dE_{e'} d\Omega_{e'} d\Omega_p} = \sigma_{ep} \times S^h(p_m, E_m)$$

Concept of correlations

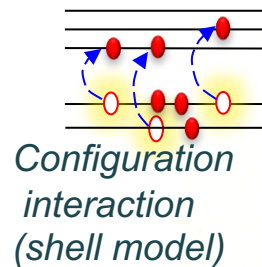
independent
particle picture



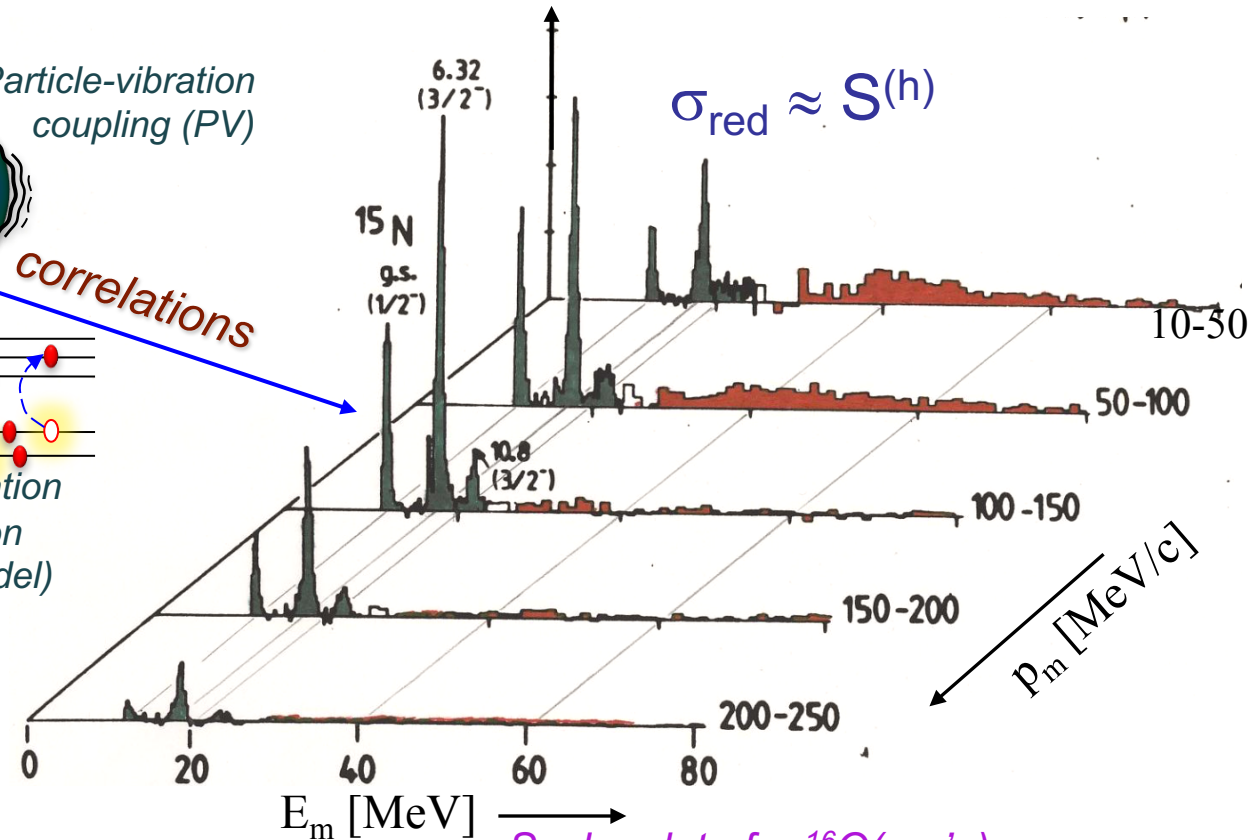
Particle-vibration
coupling (PV)



correlations



Spectral function: distribution of
momentum (p_m) and energies (E_m)



Saclay data for $^{16}\text{O}(e, e'p)$

[Mougey et al., Nucl. Phys. A335, 35 (1980)]

Understood for a few stable closed shells:

[CB and W. H. Dickhoff, Prog. Part. Nucl. Phys 52, 377 (2004)]

Concept of correlations

independent
particle picture

Spectral function: distribution of
momentum (p_m) and

Particle-vibration
coupling

Want to understand structure and nuclear forces
directly from first principles (ab initio).

So far, fully characterised only for closed-shell and
stable isotopes... (!)

[W. Dickhoff, CB, Prog. Part. Nucl. Phys. **52**, 377 (2004)]

Saclay data for $^{16}\text{O}(e,e'p)$

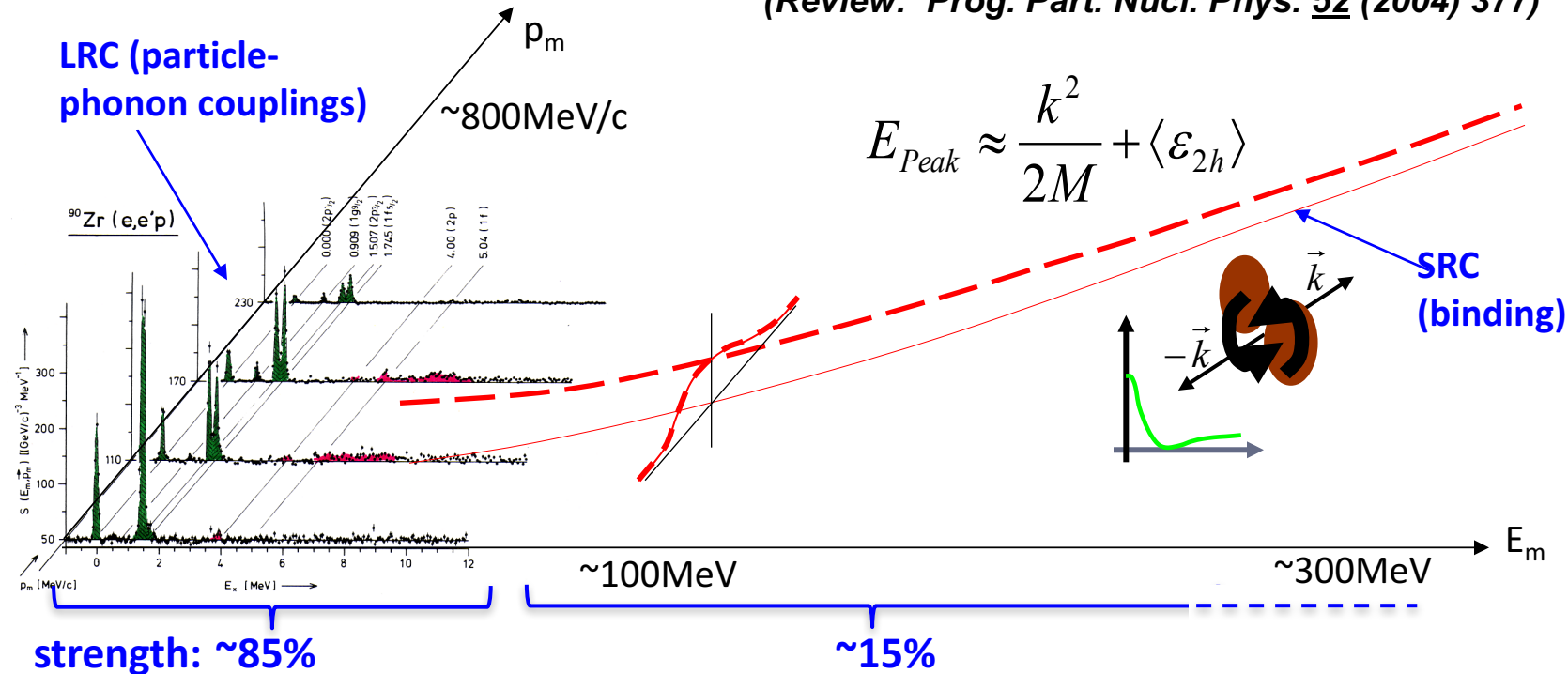
[Mougey et al., Nucl. Phys. A335, 35 (1980)]

Understand for a few stable closed shells:

[CB and W. H. Dickhoff, Prog. Part. Nucl. Phys **52**, 377 (2004)]

Distribution of (All) the Nuclear Strength

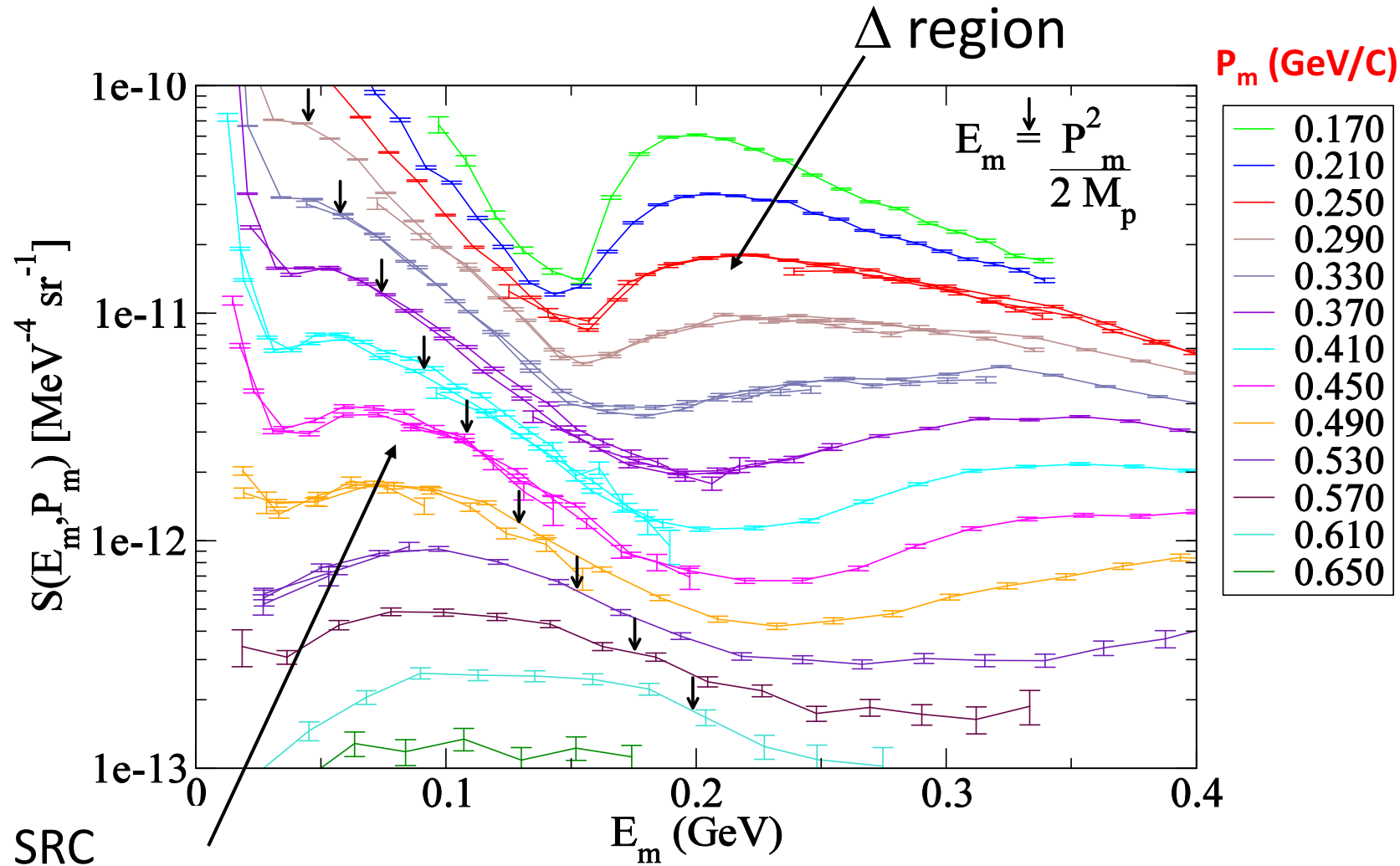
(Review: Prog. Part. Nucl. Phys. 52 (2004) 377)



Interest in short range correlations:

- a fraction of the total number of nucleons:
 - ~10% in light nuclei (VMC, FHNC, Green's function)
 - 15-20% in heavy systems (CBF, Green's function)
- can explain up to **2/3 of the binding energy** [see ex. PRC51, 3040 ('95) for ^{16}O]
- influence NM saturation properties [see ex. PRL90, 152501 ('03)]

Spectral strength of ^{12}C from exp. E97-006



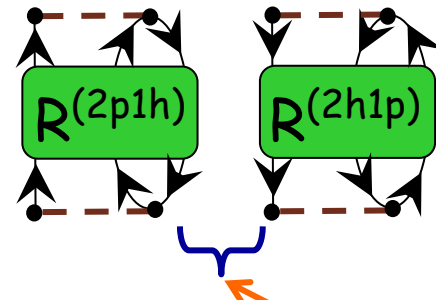
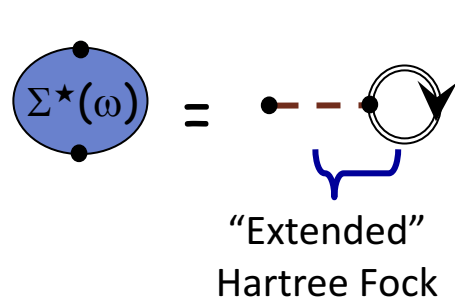
SRC
correlations

D.Rohe, et. al, Eur. Phys. J. **A17**, 349 (2003),
Phys. Rev. Lett. **93** 182501 (2004).

The FRPA Method in Two Words

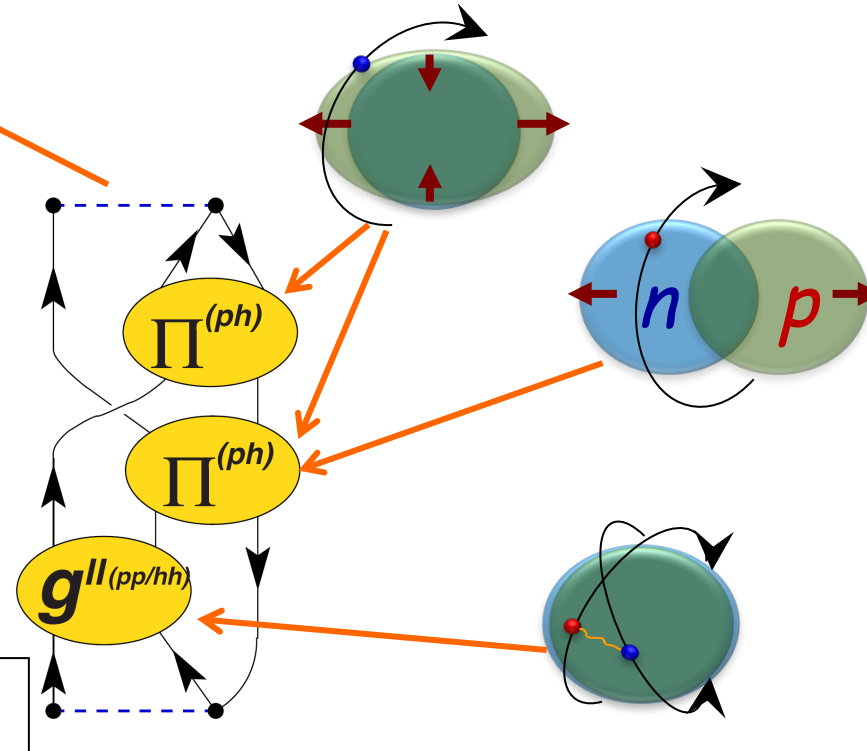
Particle vibration coupling is the main mechanism driving the redistribution and fragmentation of particle strength—especially in the quasielastic regions around the Fermi surface...

CB et al.,
Phys. Rev. C **63**, 034313 (2001)
Phys. Rev. A **76**, 052503 (2007)
Phys. Rev. C **79**, 064313 (2009)

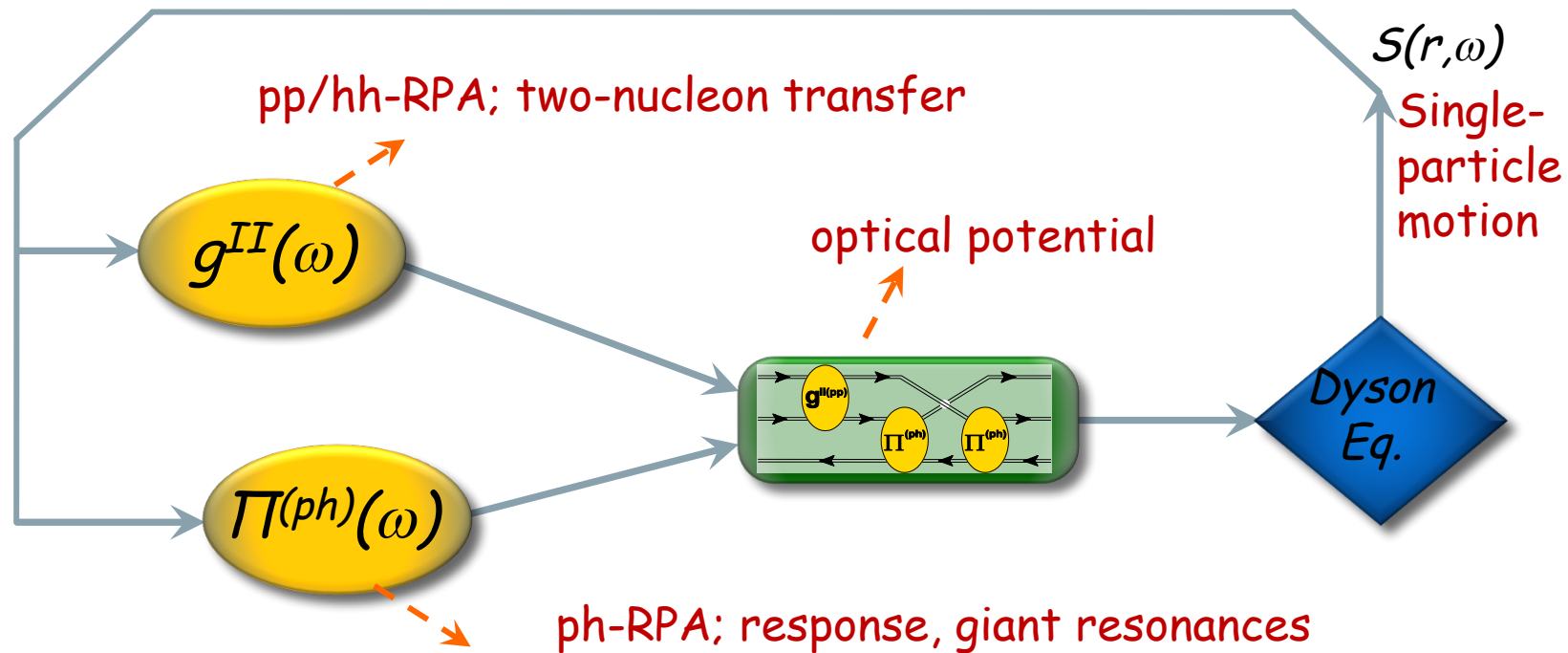


- A complete expansion requires all types of particle-vibration coupling
...these modes are all resummed exactly and to all orders in a *ab initio* many-body expansion.

- The Self-energy $\Sigma^*(\omega)$ yields *both* single-particle states and scattering



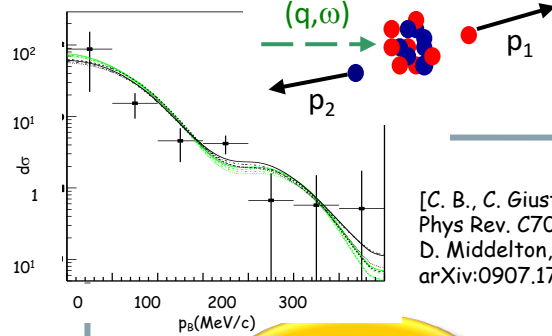
Self-Consistent Green's Function Approach



- Global picture of nuclear dynamics
- Reciprocal correlations among effective modes
- Guaranties *macroscopic conservation laws*

Self-Consistent Green's Function Approach

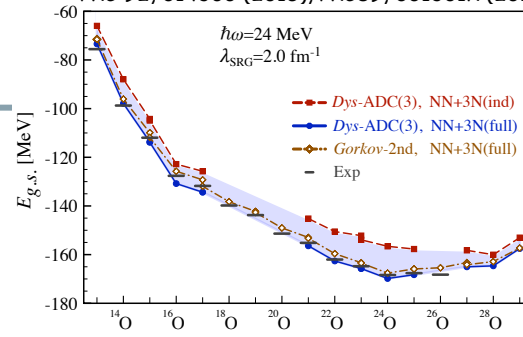
$^{16}\text{O}(e,e'pn)^{14}\text{N}$ @ MAINZ



[C. B., C. Giusti, et al.
Phys Rev. C70, 014606 (2004)
D. Middleton, et al.
arXiv:0907.1758; EPJA in print]

Binding energies

[PRL. 111, 062501 (2013),
PRC 92, 014306 (2015), PRC89, 061301R (2014)]



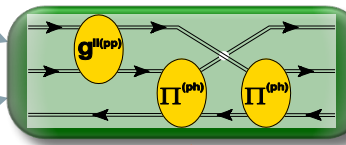
Ionization energies/
affinities, in atoms

[CB, D. Van Neck,
AIP Conf.Proc.1120,104 ('09) & in prep]

		Hartree-Fock	FRPAc	Experiment [16, 17]
He:	1s	0.918 (+14)	0.9008 (-2.9)	0.9037
Be ²⁺ :	1s	5.6672 (+116)	5.6551 (-0.5)	5.6556
Be:	2s	0.3093 (-34)	0.3224 (-20.2)	0.3426
	1s	4.733 (+200)	4.5405 (+8)	4.533
Ne:	2p	0.852 (+57)	0.8037 (+11)	0.793
	1s	1.931 (+149)	1.7967 (+15)	1.782
Mg ²⁺ :	2p	3.0068 (+56.9)	2.9537 (+3.8)	2.9499
	1s	4.4827	4.3589	
Mg:	3s	0.253 (-28)	0.280 (-1)	0.281
	2p	2.282 (+162)	2.137 (+17)	2.12
Ar:	3p	0.591 (+12)	0.579 (±0)	0.579
	3s	1.277 (+202)	1.065 (-10)	1.075
	3s		1.544	
	2p	9.571 (+411)	9.219 (+59)	9.160

$g^{II}(\omega)$

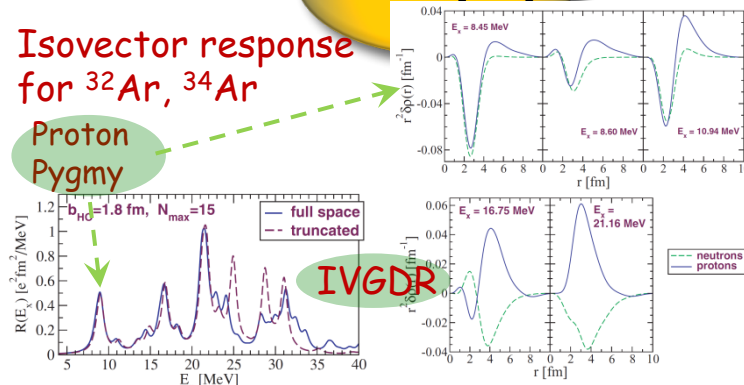
$\Pi^{(ph)}(\omega)$



Dyson
Eq.

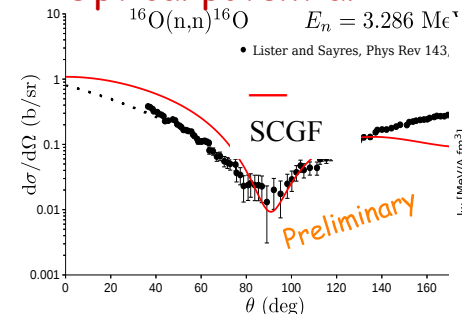
Isovector response
for ^{32}Ar , ^{34}Ar

Proton
Pygmy

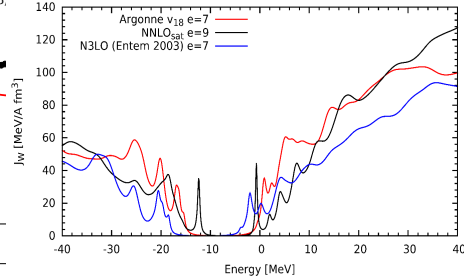


[C. B., K. Langanke, et al., Phys Rev. C77, 024304 (2008)]

Optical potential



arXiv:1612.01478 [nucl-th]



Reach of *ab initio* methods across the nuclear chart

Approximate approaches for closed-shell nuclei

- Since 2000's
- SCGF, CC, IMSRG
- Polynomial scaling

Approximate approaches for open-shells

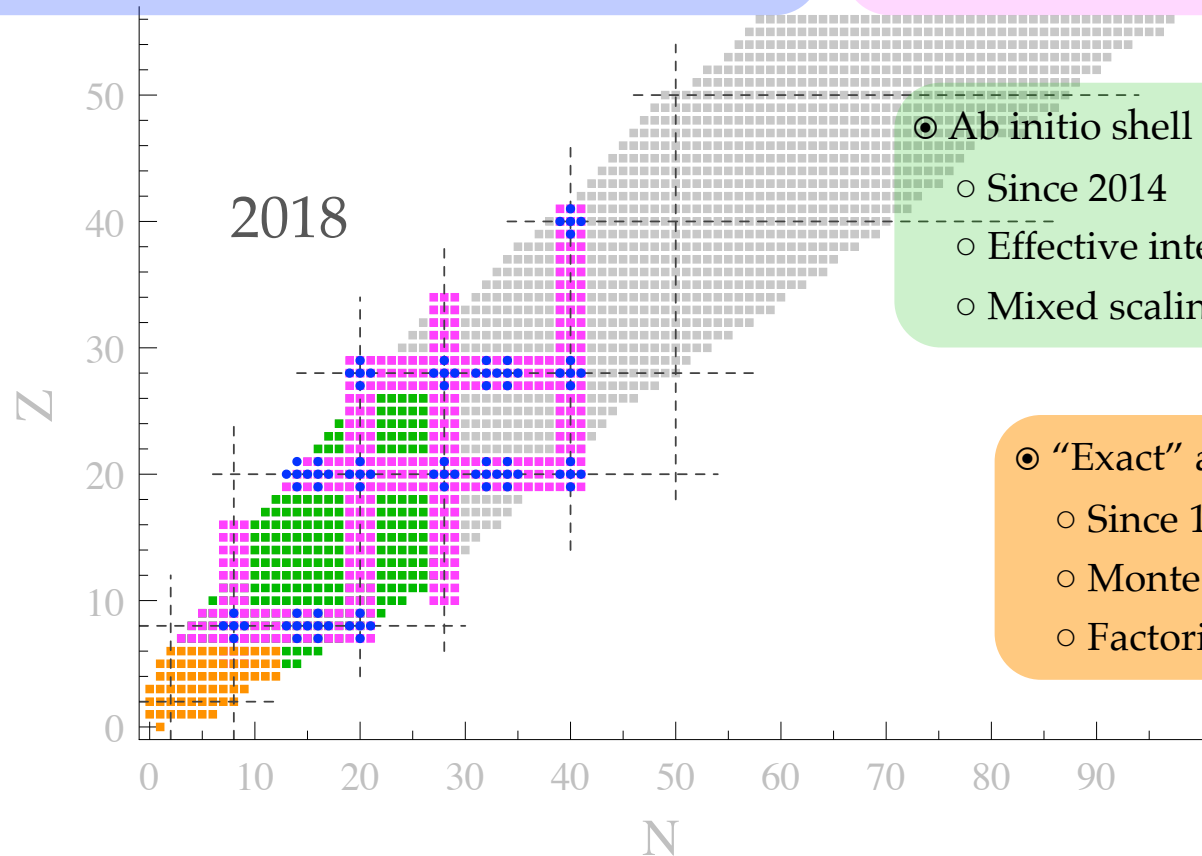
- Since 2010's
- GGF, BCC, MR-IMSRG
- Polynomial scaling

Ab initio shell model

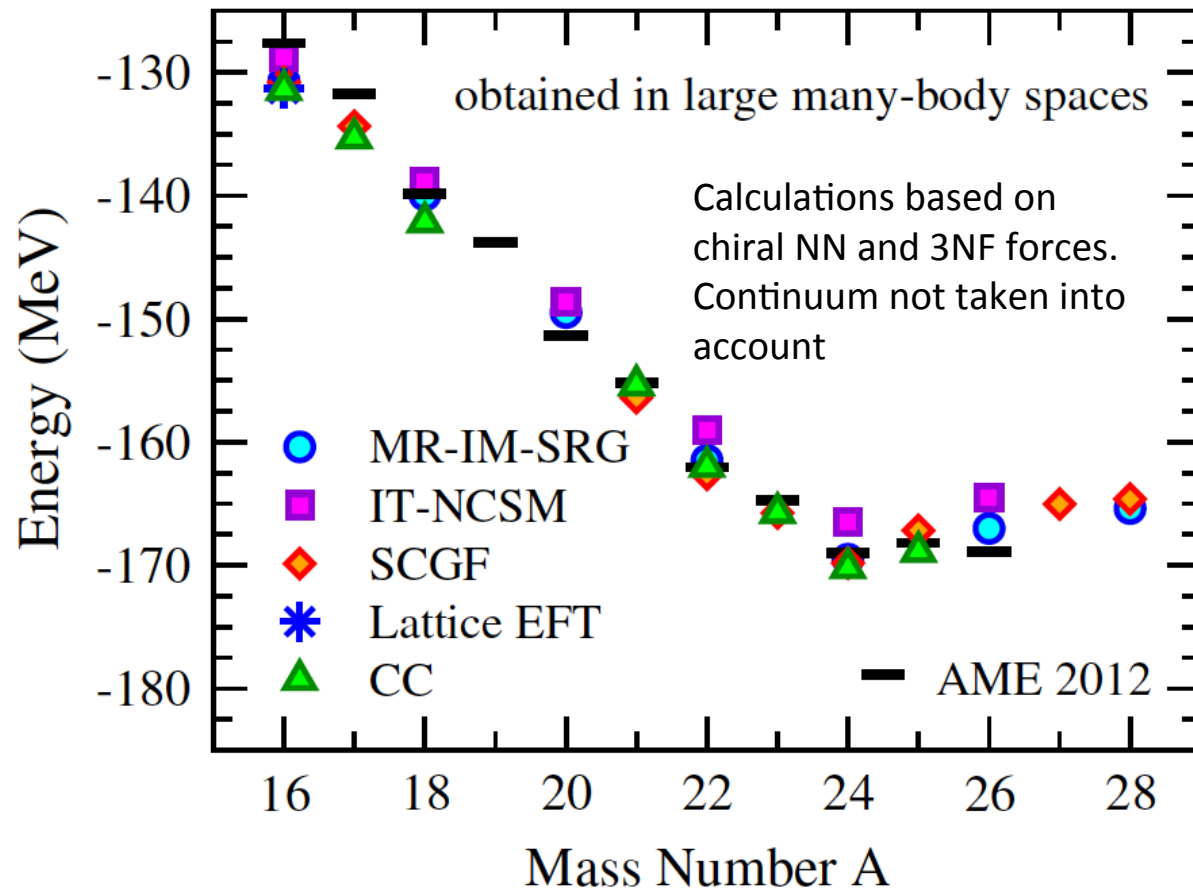
- Since 2014
- Effective interaction via CC/IMSRG
- Mixed scaling

"Exact" approaches

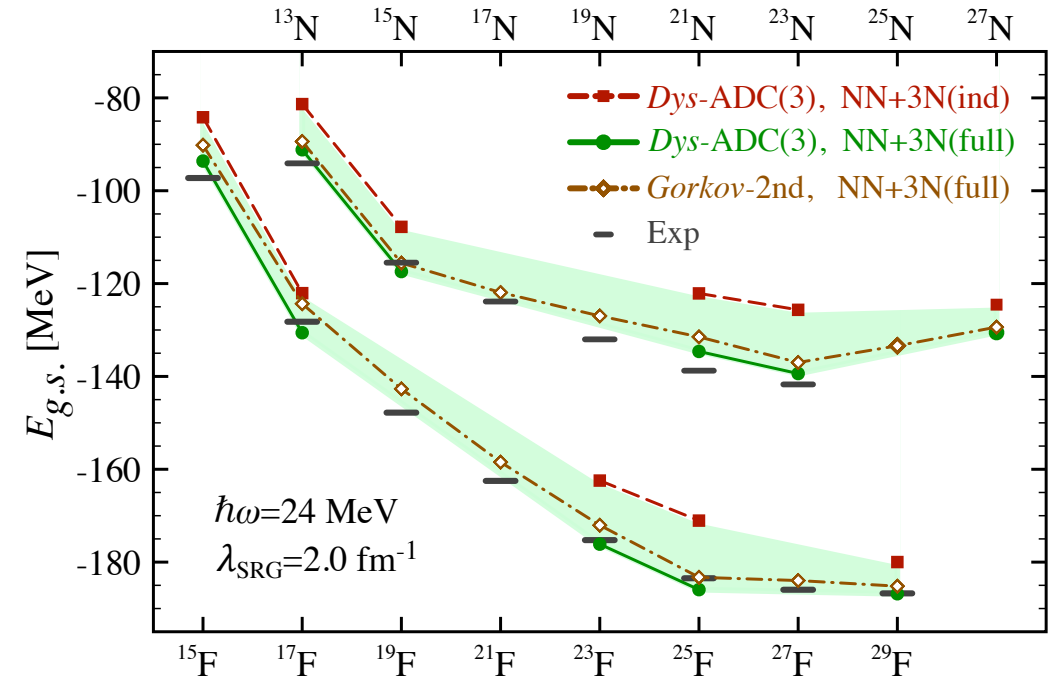
- Since 1980's
- Monte Carlo, CI, ...
- Factorial scaling



Benchmark of *ab-initio* methods in the oxygen isotopic chain



A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. **111**, 062501 (2013)
and Phys. Rev. C **92**, 014306 (2015)



→ 3NF tensor and 3NF near fluorine's dripline

Hebeler, Holt, Menendez, Schwenk, Ann. Rev. Nucl. Part. Sci. in press (2015)

N3LO ($\Lambda = 500$ MeV/c) chiral NN interaction evolved to 2N + 3N forces (2.0 fm $^{-1}$)

N2LO ($\Lambda = 400$ MeV/c) chiral 3N interaction evolved (2.0 fm $^{-1}$)

Comparison of nuclear forces – ^AO and $^A\text{Si}/^A\text{S}$

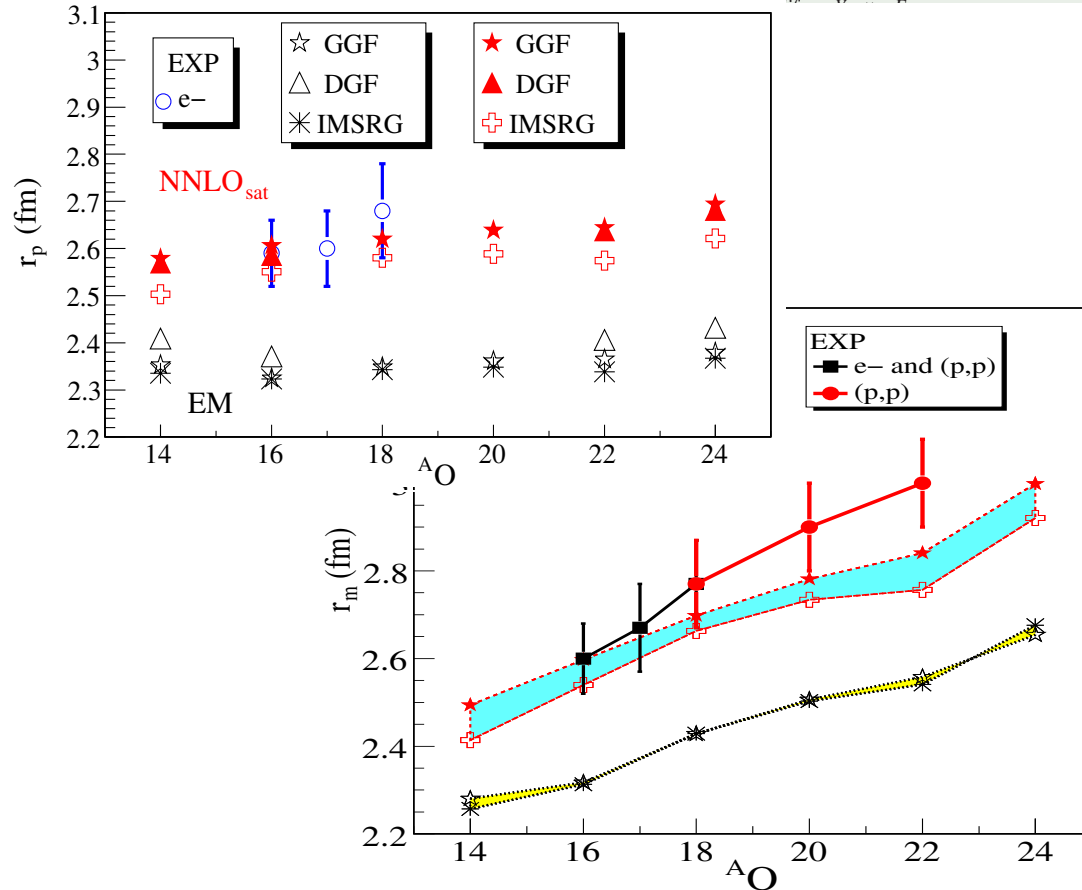
PRL 117, 052501 (2016)

PHYSICAL REVIEW LETTERS

week ending
29 JULY 2016

Radii and Binding Energies in Oxygen Isotopes: A Challenge for Nuclear Forces

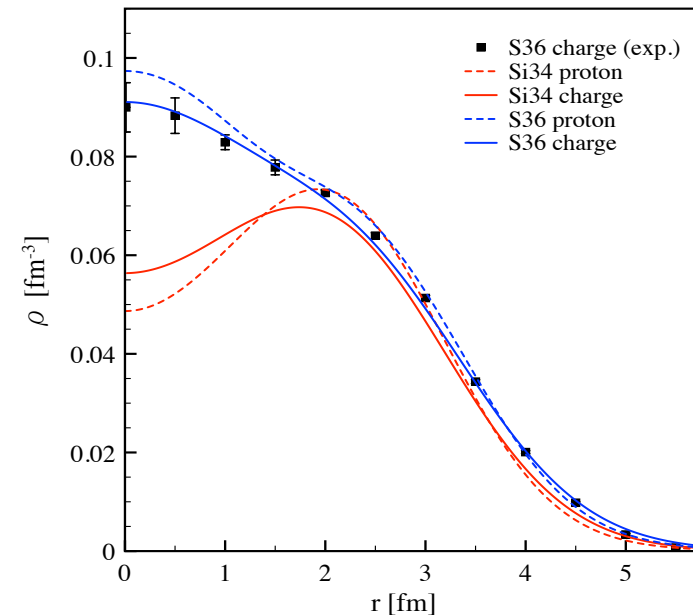
V. Lapoux,^{1,*} V. Somà,¹ C. Barbieri,² H. Hergert,³ J. D. Holt,⁴ and S. R. Stroberg⁴



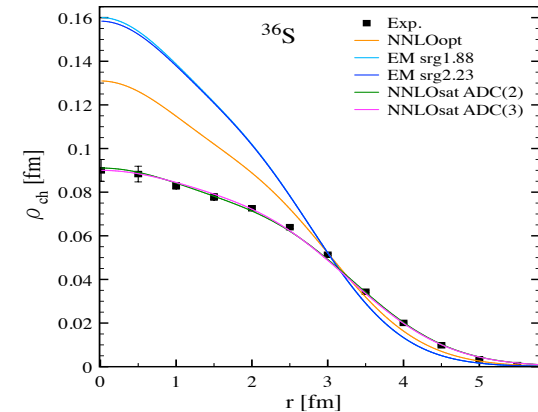
Saturation and radii now predicted accurately!

Duguet, Somà, Lecuse, CB, Navrátil, Phys.Rev. C95, 034319 (2017)

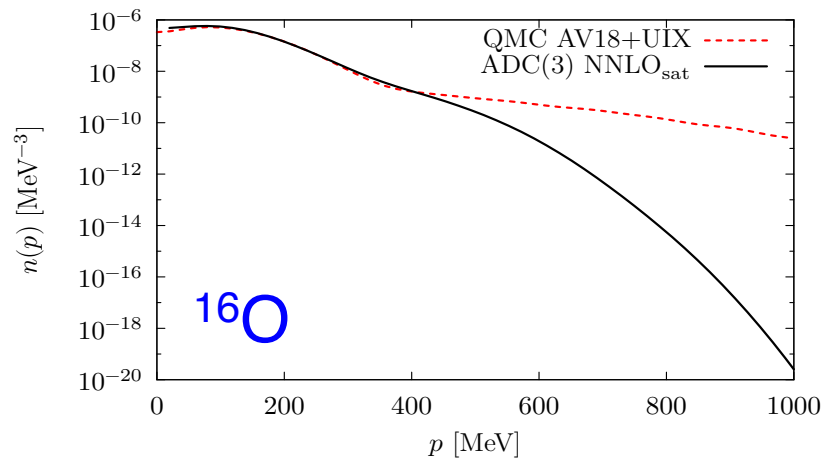
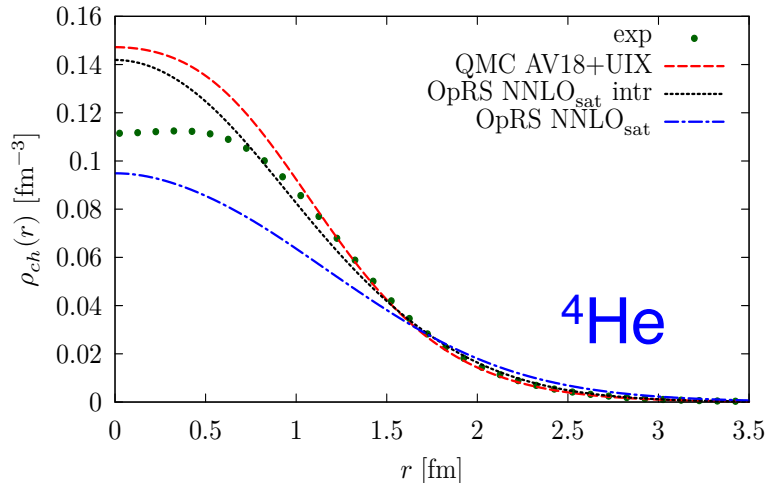
- ^{34}Si is unstable, charge distribution is still unknown
- Suggested central depletion from mean-field simulations
- *Ab-initio* theory confirms predictions
- Other theoretical and experimental evidence:
Phys. Rev. C **79**, 034318 (2009),
Nature Physics **13**, 152–156 (2017).



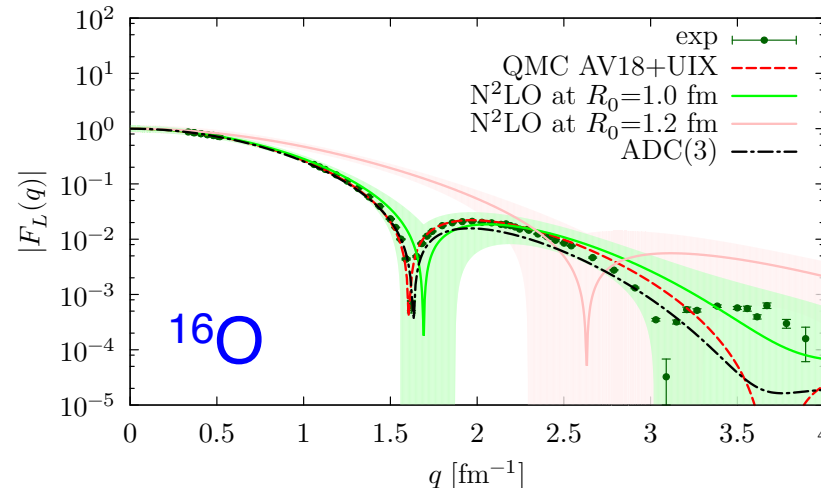
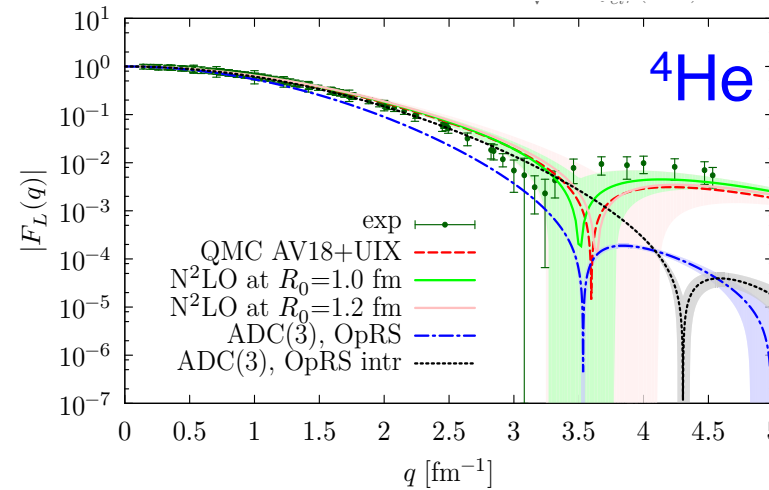
Validated by charge distributions and neutron quasiparticle spectra:



Prediction for chrg./mom. distributions and form factors



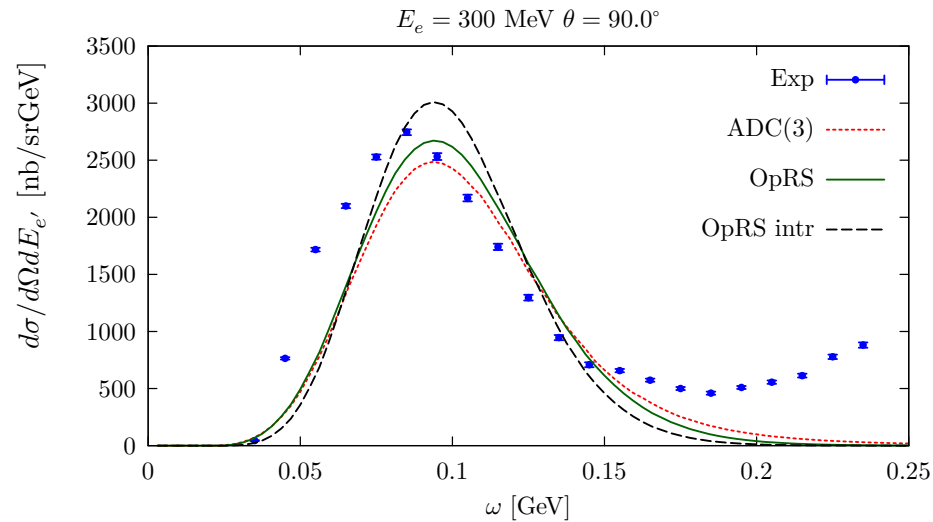
$$F_L(\mathbf{q}) = \frac{1}{Z} \frac{G_E^p(Q_{el}^2) \tilde{\rho}_p(q) + G_E^n(Q_{el}^2) \tilde{\rho}_n(q)}{\sqrt{1 + Q_{el}^2/(4m^2)}}$$



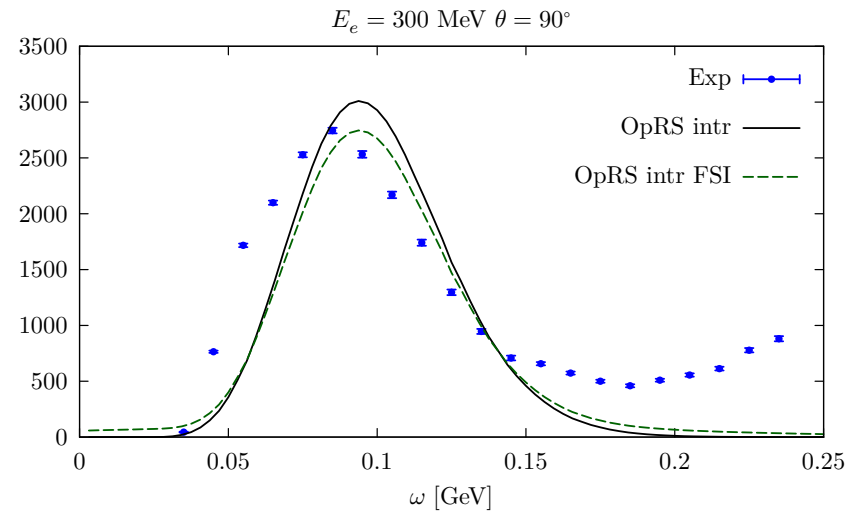
- Calculations from the spectral functions obtained using SCGF
- Based on the saturating chiral N2LO-sat nuclear force
- Comparison to QMC calculations based on **local chiral forces** and/or **AV18+UIX** [PRC96, 024326 ('17) PRC96, 054007 ('17) PRC97, 044318 ('18)]

$^4\text{He}-e^-$ cross sections from the SCGF Spect. Fnct.

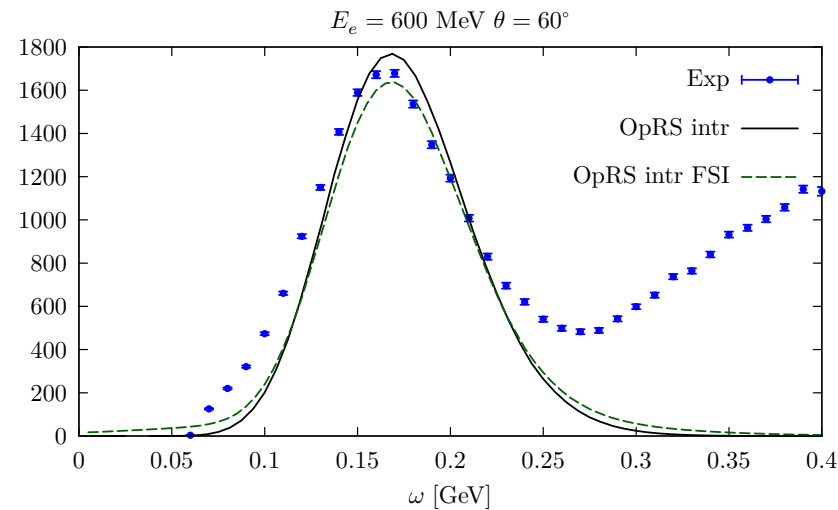
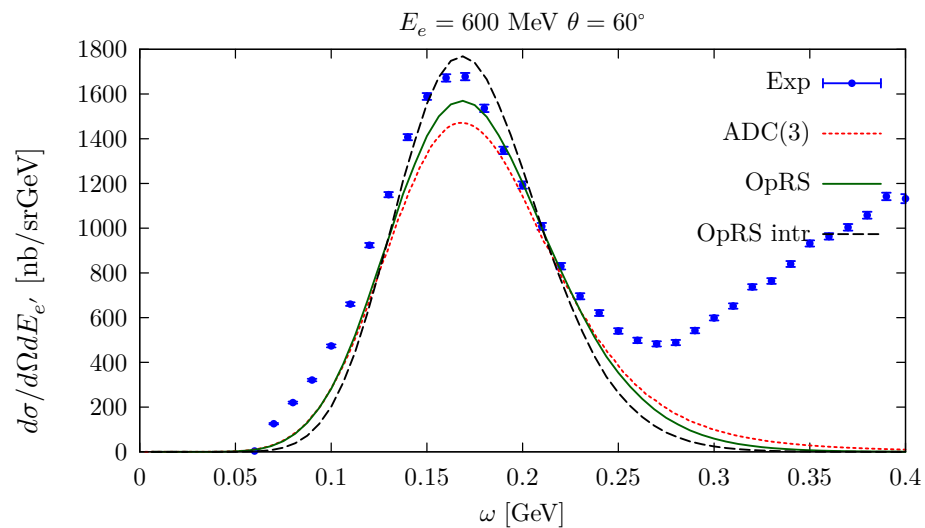
PW Impulse approximation:



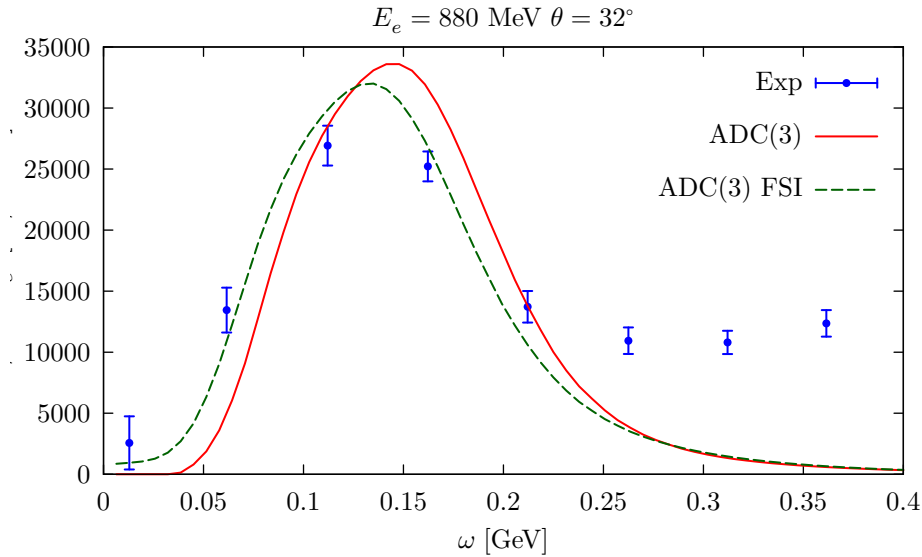
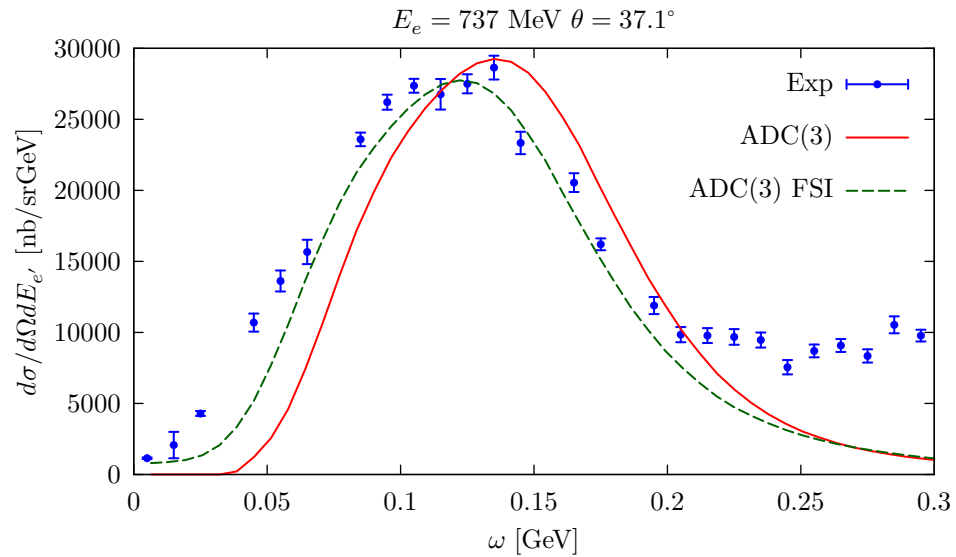
Adding FSI:



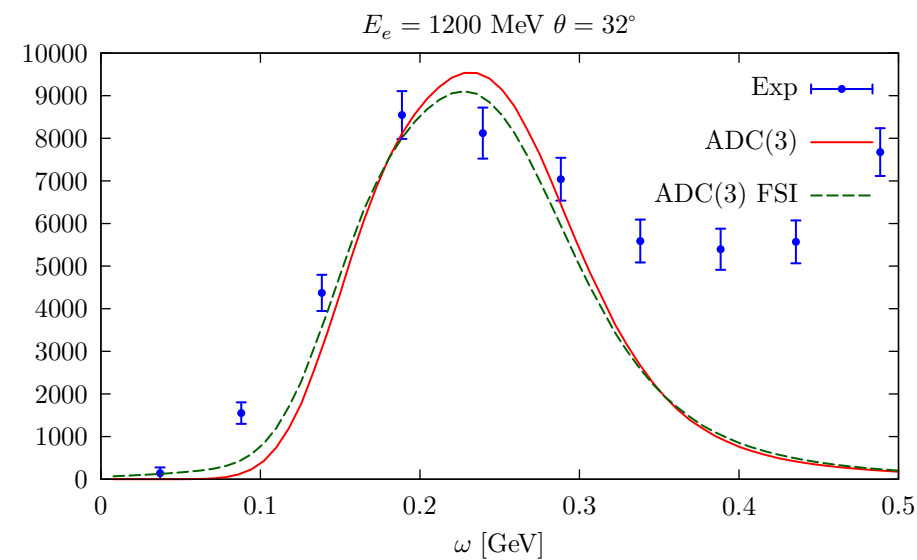
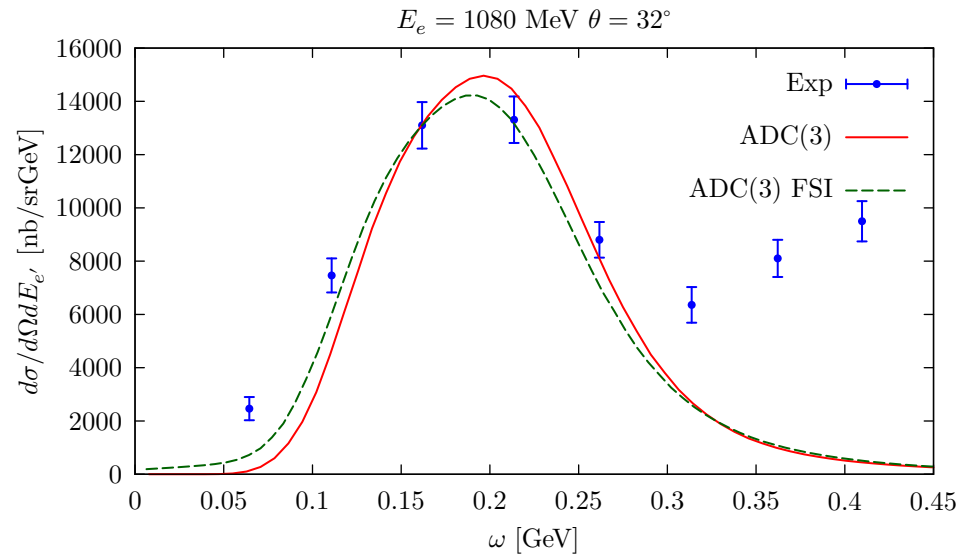
Based on the
saturating chiral
N2LO-sat
nuclear force



$^{16}\text{O}-e^-$ cross sections from the SCGF Spect. Fnct.

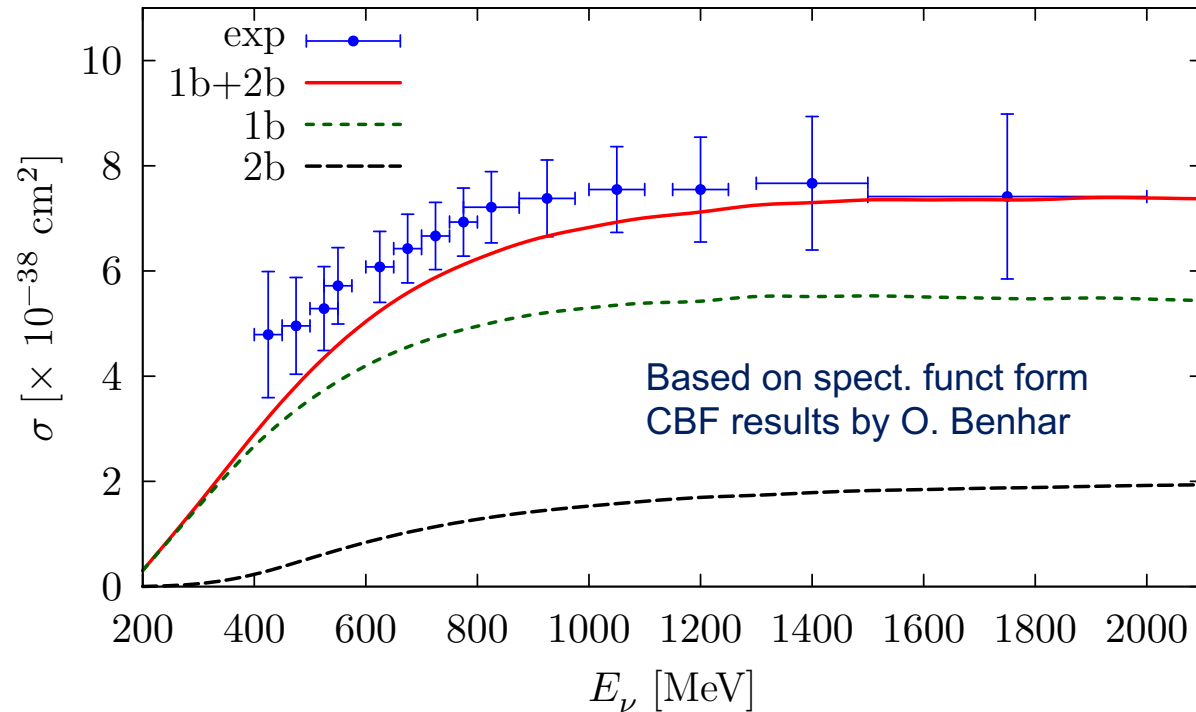


Based on the
saturating chiral
N2LO-sat
nuclear force



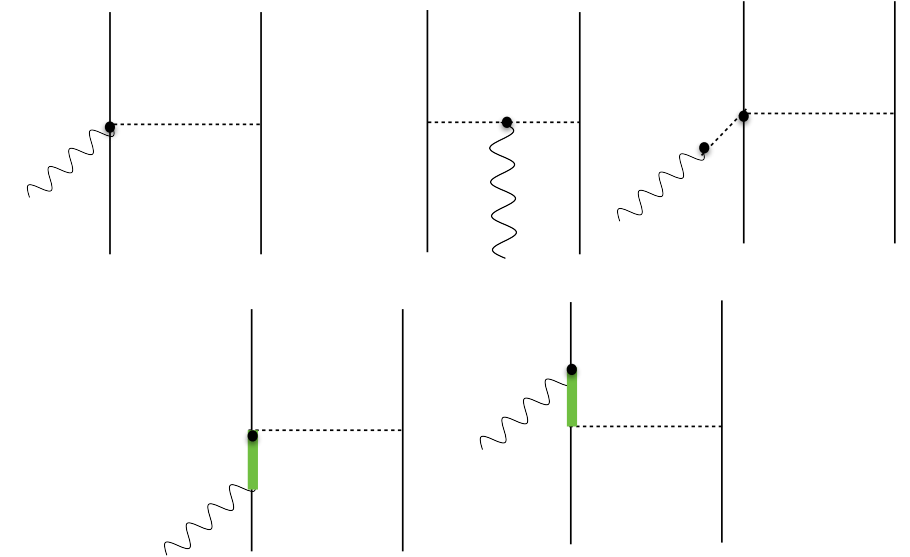
Role of two-body (meson exchange) currents in ν -A

CC0 π total cross section: MiniBooNE data



The 2p2h contribution is needed to explain the magnitude of the total cross section

- Two-body diagrams contributing to the axial and vector responses

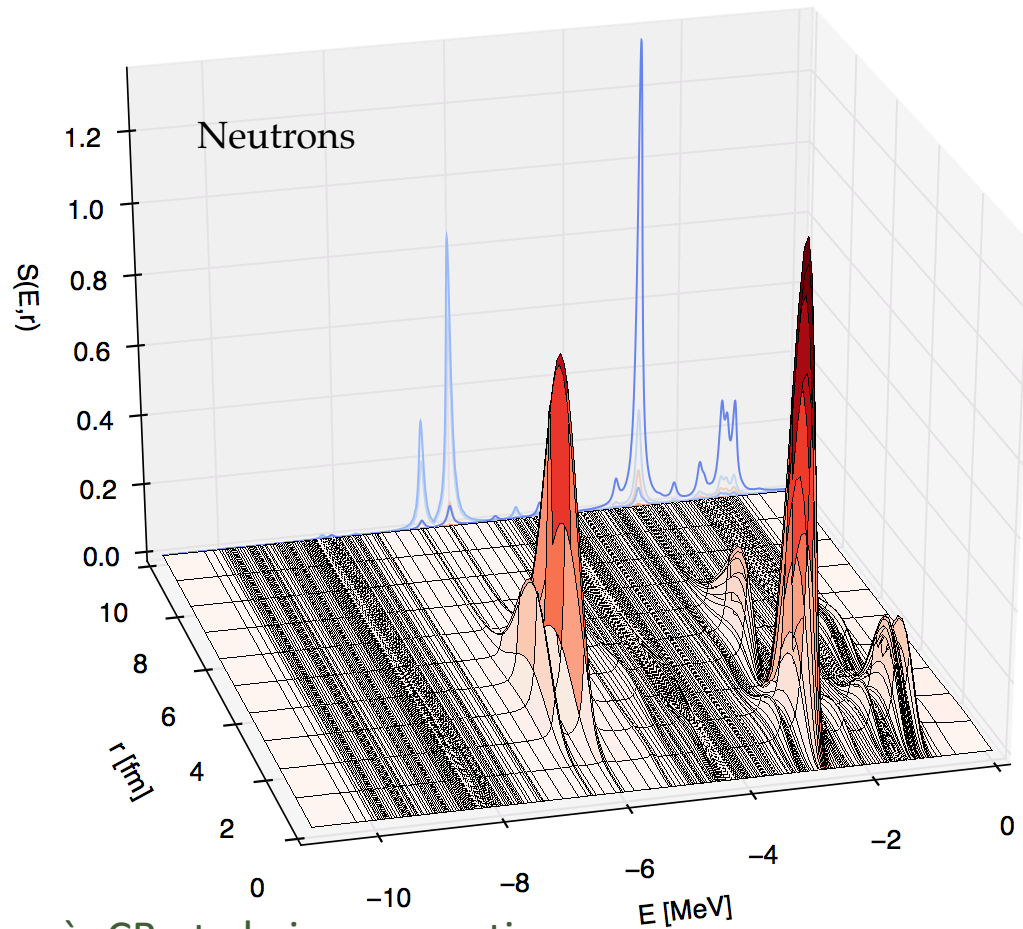


- Preliminary implementation discards 1b-2b interference:

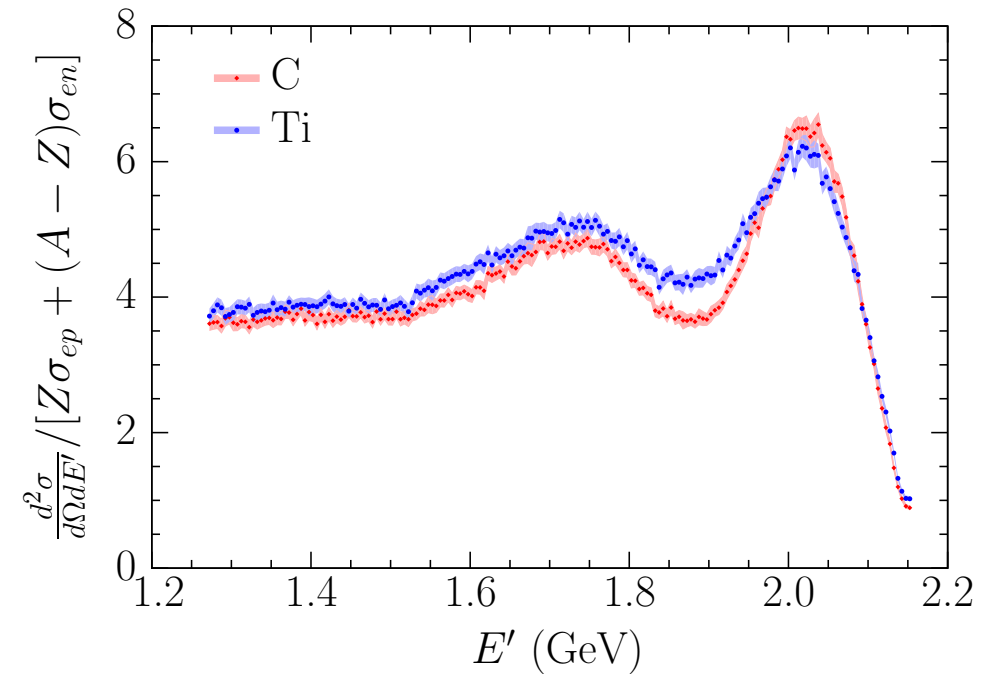
$$W_{2p2h}^{\mu\nu} = W_{ISC}^{\mu\nu} + W_{MEC}^{\mu\nu} + \cancel{W_{int}^{\mu\nu}}$$

Calculations by N. Rocco, see also talk by O. Benhar afterward

Spectral function for ^{40}Ar



V. Somà, CB et al., in preparation



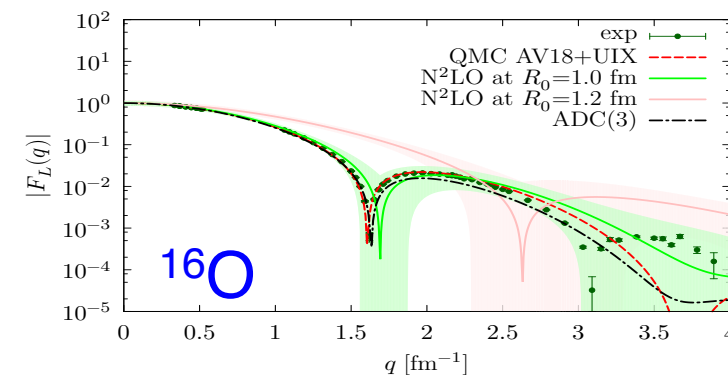
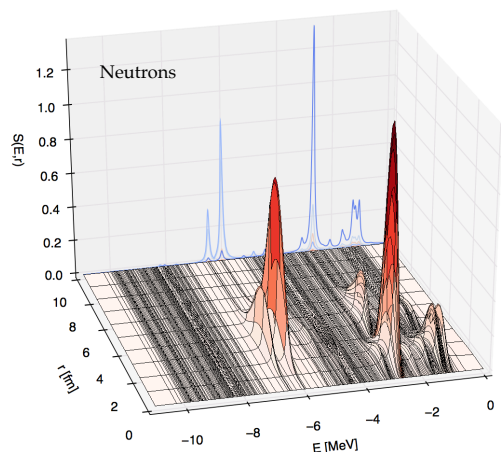
- Experimental data now available for Jlab:
H. Dai et al., arXiv:1803.01910
 - Ab initio simulations based on the ADC(2) truncation of the N2LO-sat Hamiltonian
- Validation of initial state correlation before they are implemented in neutrino- ^{40}Ar simulations

Summary

Thank you for your attention!!

Saturating chiral interactions and 3N forces:

- Description of nuclear g.s. in the pf shell is improved-especially in the trends w.r.t. iso-sopin asymmetry.
- Radii: newer generations of chiral interaction can give satisfactory radii.



Applications to electron and neutrino scattering:

- Spectral functions (not only for 1-body!) are extracted naturally from the SCGF formalism.
- good reproduction of charge/momentum distribution and electron scattering.
- Inclusion of electroweak currents (1b and 2b) underway (by N. Rocco).



A. Cipollone, N. Rocco
A. Idini, F. Raimondi



V. Somà, T. Duguet

ECT*

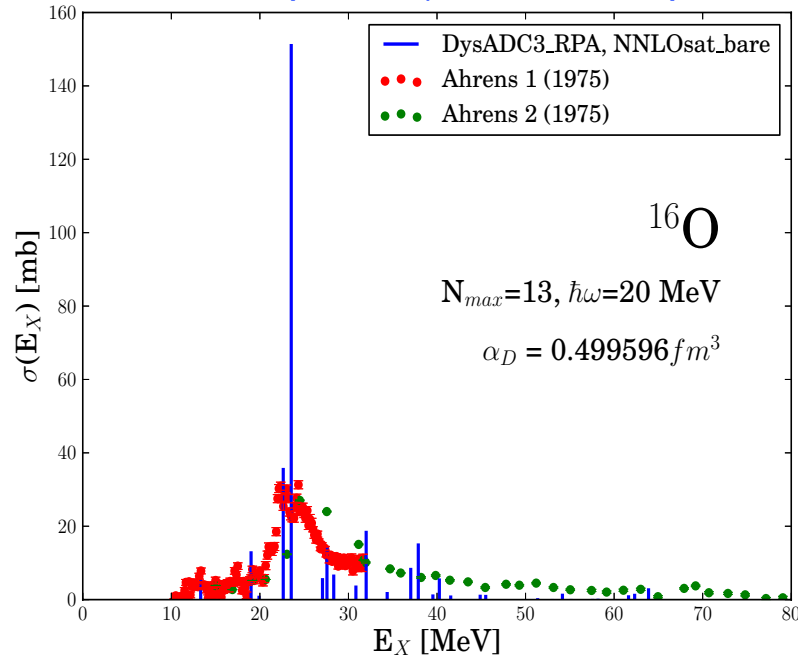
A. Carbone



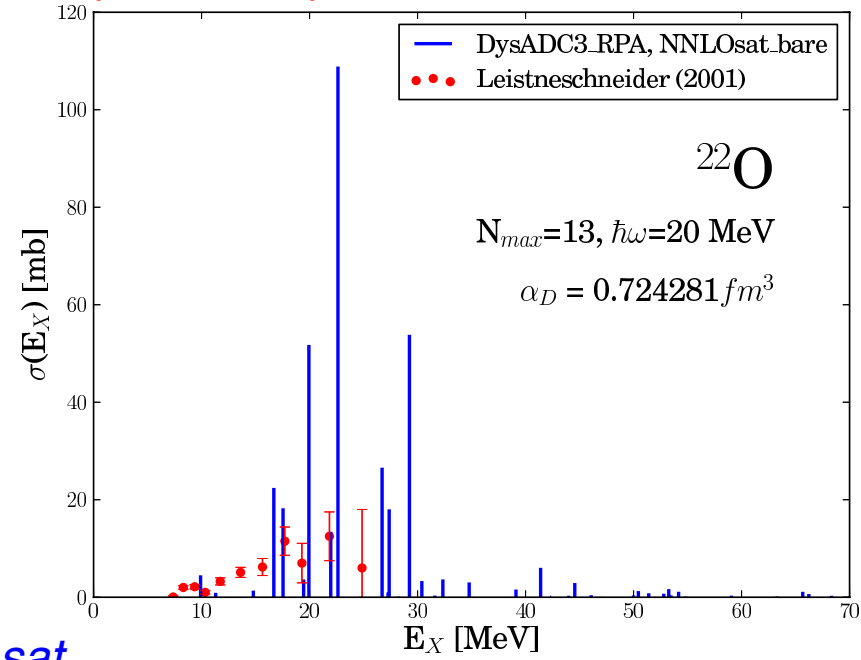
P. Navratil

Results for Oxygen isotopes

σ from RPA response (discretized spectrum) vs σ from photoabsorption and Coulomb excitation



NNLOsat

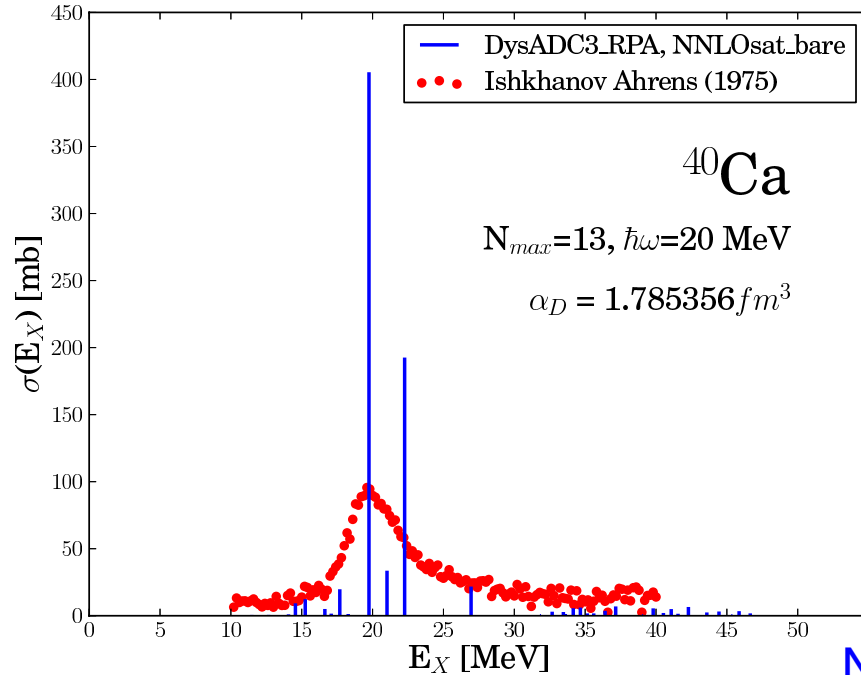


- GDR position of ^{16}O reproduced
- Hint of a soft dipole mode on the neutron-rich isotope

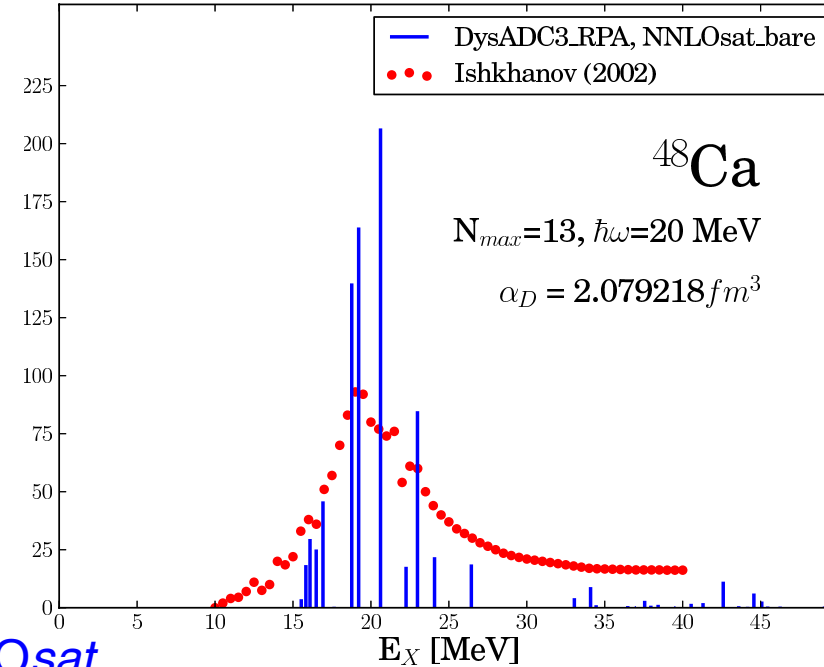
Nucleus	Dipole polarizability α_D (fm ³)		
	SCGF	CC/LIT	Exp
^{16}O	0.50	0.57(1)	0.585(9)
^{22}O	0.72	0.86(4)	0.43(4)

Results for Calcium isotopes

σ from RPA response (discretized spectrum) vs σ from photoabsorption and Coulomb excitation



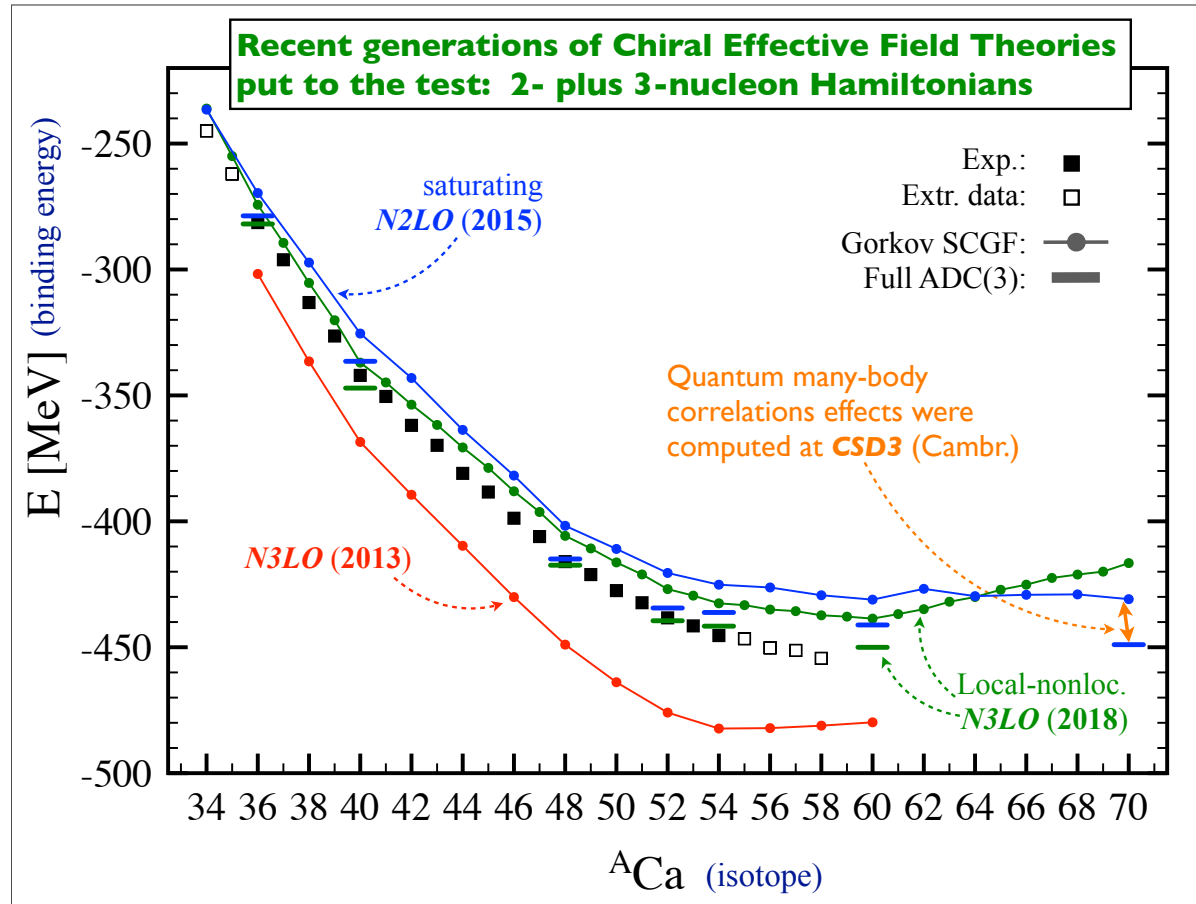
NNLOsat



- Positions of GDRs reproduced

Nucleus	Dipole polarizability α_D (fm ³)		
	SCGF	CC/LIT	Exp
^{40}Ca	1.79	1.47 (1.87) _{thresh}	1.87(3)
^{48}Ca	2.08	2.45	2.07(22)

Comparison of nuclear forces – ${}^A\text{Ca}$ and ${}^A\text{O}$



V. Somà, F. Raimondi, CB, P. Navrátil, T. Duguet, in preparation

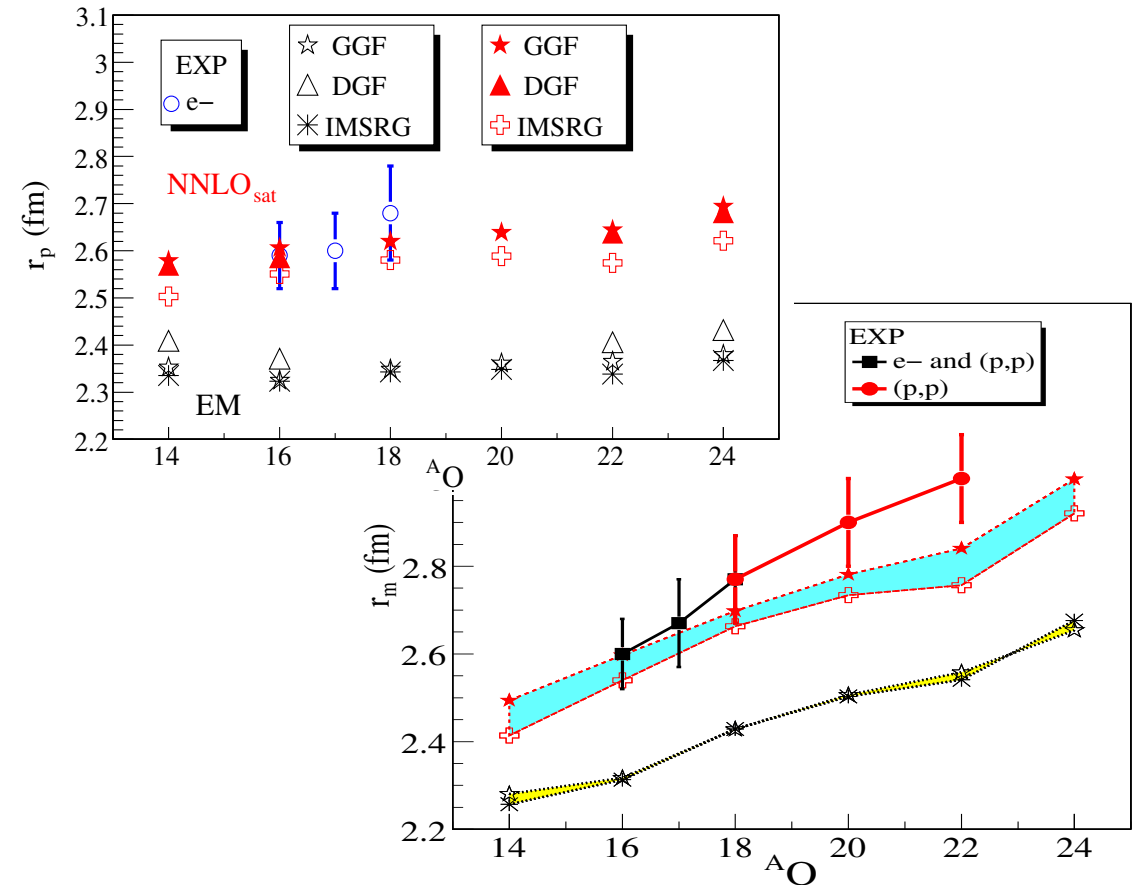
PRL 117, 052501 (2016)

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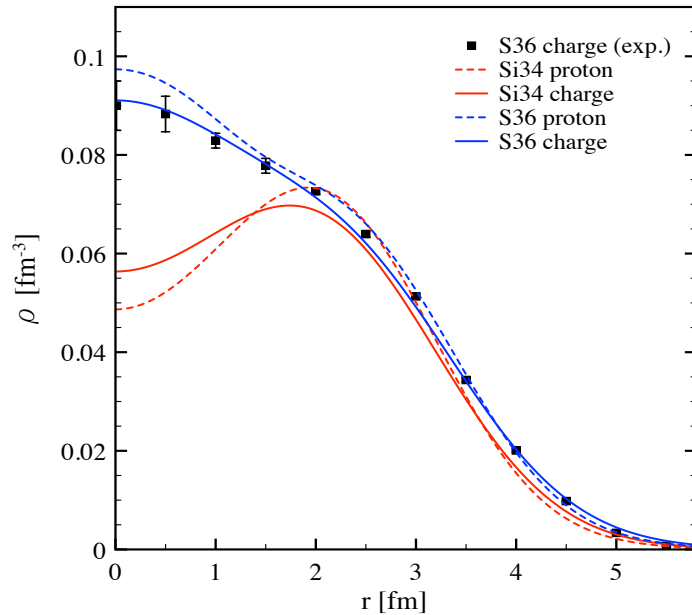
Radii and Binding Energies in Oxygen Isotopes: A Challenge for Nuclear Forces

V. Lapoux,^{1,*} V. Somà,¹ C. Barbieri,² H. Hergert,³ J. D. Holt,⁴ and S. R. Stroberg⁴



Saturation and radii now predicted accurately!

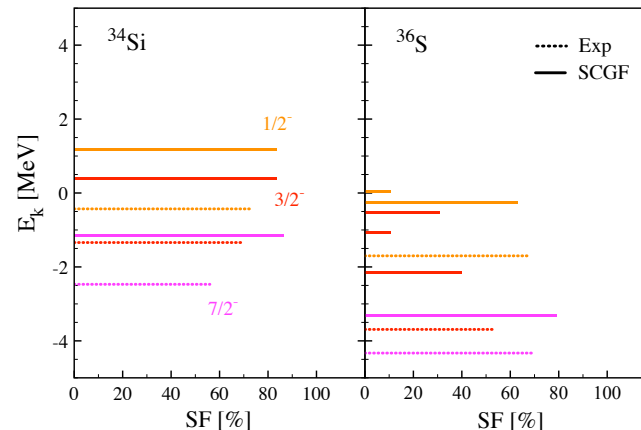
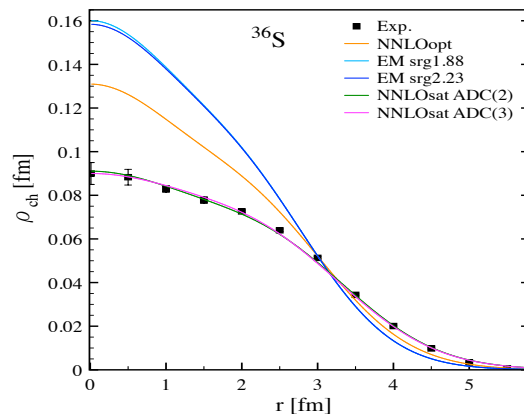
Bubble nuclei... ^{34}Si prediction



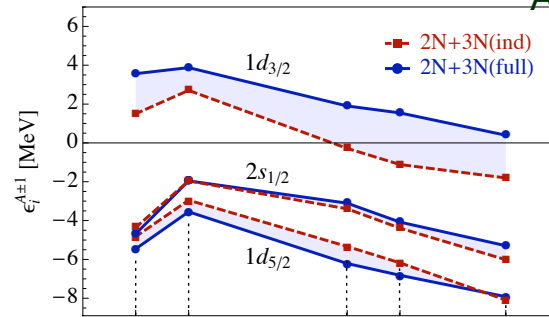
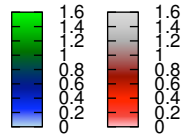
Duguet, Somà, Lecuse, CB, Navrátil,
Phys.Rev. **C95**, 034319 (2017)

- ^{34}Si is unstable, charge distribution is still unknown
- Suggested central depletion from mean-field simulations
- *Ab-initio* theory confirms predictions
- Other theoretical and experimental evidence:
Phys. Rev. **C 79**, 034318 (2009),
Nature Physics **13**, 152–156 (2017).

Validated by charge distributions and neutron quasiparticle spectra:



Neutron spectral function of Oxygens



A. Cipollone, CB, P. Navrátil, *Phys. Rev. C* **92**, 014306 (2015)

