

Pion Production

In GiBUU

With

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Elementary Cross section

Pion production has resonance and background amplitudes

$$\sigma \propto |A_R + A_{BG}|^2 = |A_R|^2 + |A_{BG}|^2 + \textit{interference}$$

We obtain both from MAID2007 analysis for $W < 2$ GeV
of electron- and photon-induced pion production on the nucleon
→ Electron cross section on *nucleon* is correct by construction

$$\sigma \propto |A_R|^2 + \textit{BGterms}$$

We propagate the resonances; the BG terms can be < 0 !

Pion production on the nucleon

Transition currents to resonances:

$$V_{3/2}^{\alpha\mu} = \frac{C_3^V}{M} (g^{\alpha\mu} \not{q} - q^\alpha \gamma^\mu) + \frac{C_4^V}{M^2} (g^{\alpha\mu} q \cdot p - q^\alpha p^\mu) + \frac{C_5^V}{M^2} (g^{\alpha\mu} q \cdot p - q^\alpha p^\mu) + g^{\alpha\mu} C_6^V$$

$$A_{3/2}^{\alpha\mu} = - \left[\frac{C_3^A}{M} (g^{\alpha\mu} \not{q} - q^\alpha \gamma^\mu) + \frac{C_4^A}{M^2} (g^{\alpha\mu} q \cdot p - q^\alpha p^\mu) + C_5^A g^{\alpha\mu} + \frac{C_6^A}{M^2} q^\alpha q^\mu \right] \gamma^5 .$$

C^V from electron data (MAID analysis with CVC)

C^A from fit to neutrino data (experiments on hydrogen/deuterium), so far only C_5^A determined, for other axial FFs only educated guesses

Vertex factor $\Gamma^{\alpha\mu} = (V^{\alpha\mu} - A^{\alpha\mu}) \gamma^5$

Hadron tensor $H^{\mu\nu} = \frac{1}{2} \text{Tr} [\not{p} + M) \Gamma^{\alpha\mu} \Lambda_{\alpha\beta} \Gamma^{\beta\nu}]$

Contract lepton tensor with hadron tensor gives the resonance production cross section:

$$\frac{d\sigma^{\text{med}}}{d\omega d\Omega'} = \frac{|\mathbf{k}'|}{32\pi^2} \frac{\mathcal{P}^{\text{med}}(p')}{[(k \cdot p)^2 - m_\ell^2 M^2]^{1/2}} |\mathcal{M}_R|^2$$

Formalism on Nucleon

$$d\sigma(\nu p \rightarrow \ell^- p \pi^+) = \sum_{\substack{I=3/2 \\ \text{resonances}}} b_i d\sigma_{R_i^{++}},$$

$$d\sigma(\nu n \rightarrow \ell^- n \pi^+) = \frac{1}{3} \sum_{\substack{I=3/2 \\ \text{resonances}}} b_i d\sigma_{R_i^+} + \frac{2}{3} \sum_{\substack{I=1/2 \\ \text{resonances}}} b_i d\sigma_{R_i^+},$$

$$d\sigma(\nu n \rightarrow \ell^- p \pi^0) = \frac{2}{3} \sum_{\substack{I=3/2 \\ \text{resonances}}} b_i d\sigma_{R_i^+} + \frac{1}{3} \sum_{\substack{I=1/2 \\ \text{resonances}}} b_i d\sigma_{R_i^+},$$

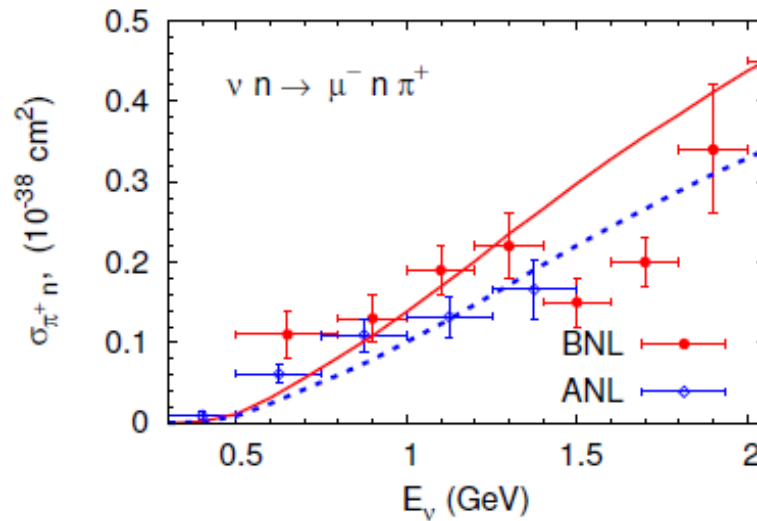
branching ratios $b_i = \Gamma_{\pi N} / \Gamma_{\text{tot}}$

In the vector sector data are described because we use MAID07 analysis
Higher excitations with $W > 2$ are handled by DIS processes through PYTHIA

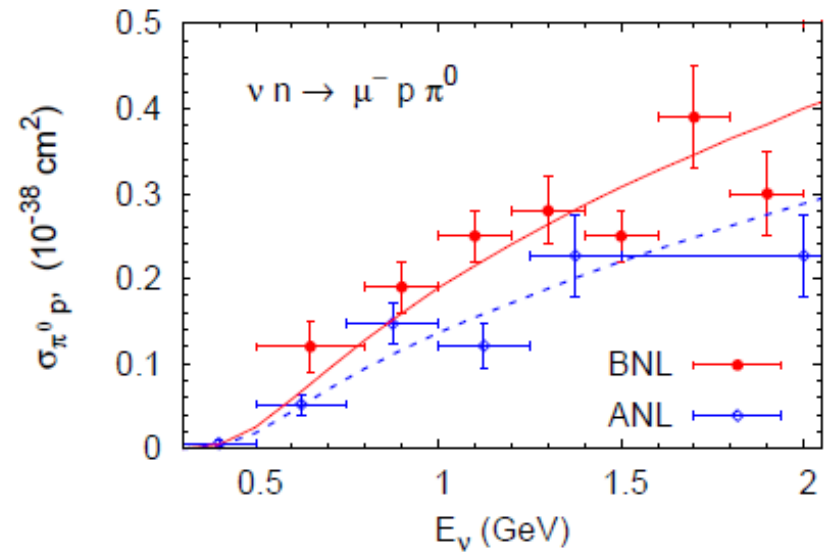
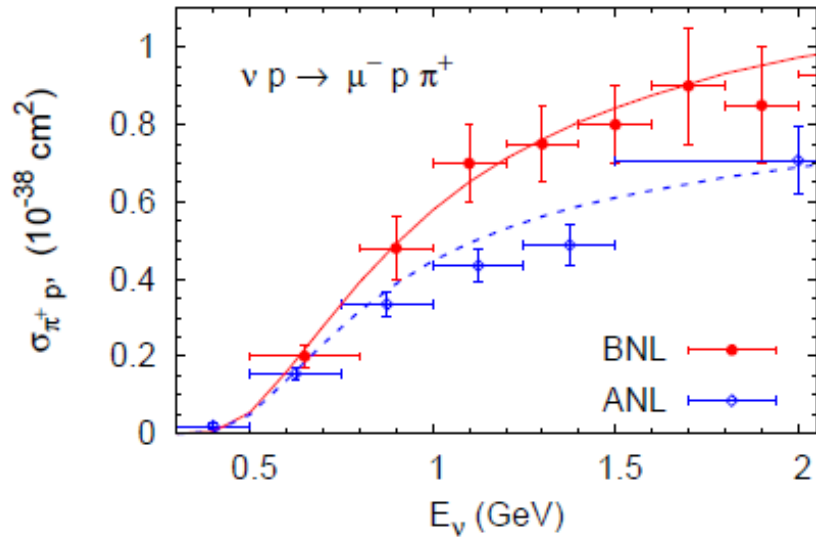
BG parameters:

- for electrons from MAID analysis
- for neutrinos are obtained by fit to nucleon data

Elementary Cross Sections



ANL
is now default



Formalism on Nucleus

Integrate the nucleon cross sections over the Fermi-sea of bound nucleons

$$d\sigma^A = \int \frac{d^3p}{(2\pi)^3} dE P_h(p, E) d\sigma^N P_{PB}$$

Hole spectral function Pauli blocking

Resonances and nucleons sit in potential,
Delta potential is weaker than nucleon potential ($\sim 2/3$)

Final State Interactions of Pions

- Two-body pi absorption through $\pi + N \rightarrow \Delta, \Delta + N \rightarrow NN$
- Three-body pi absorption:

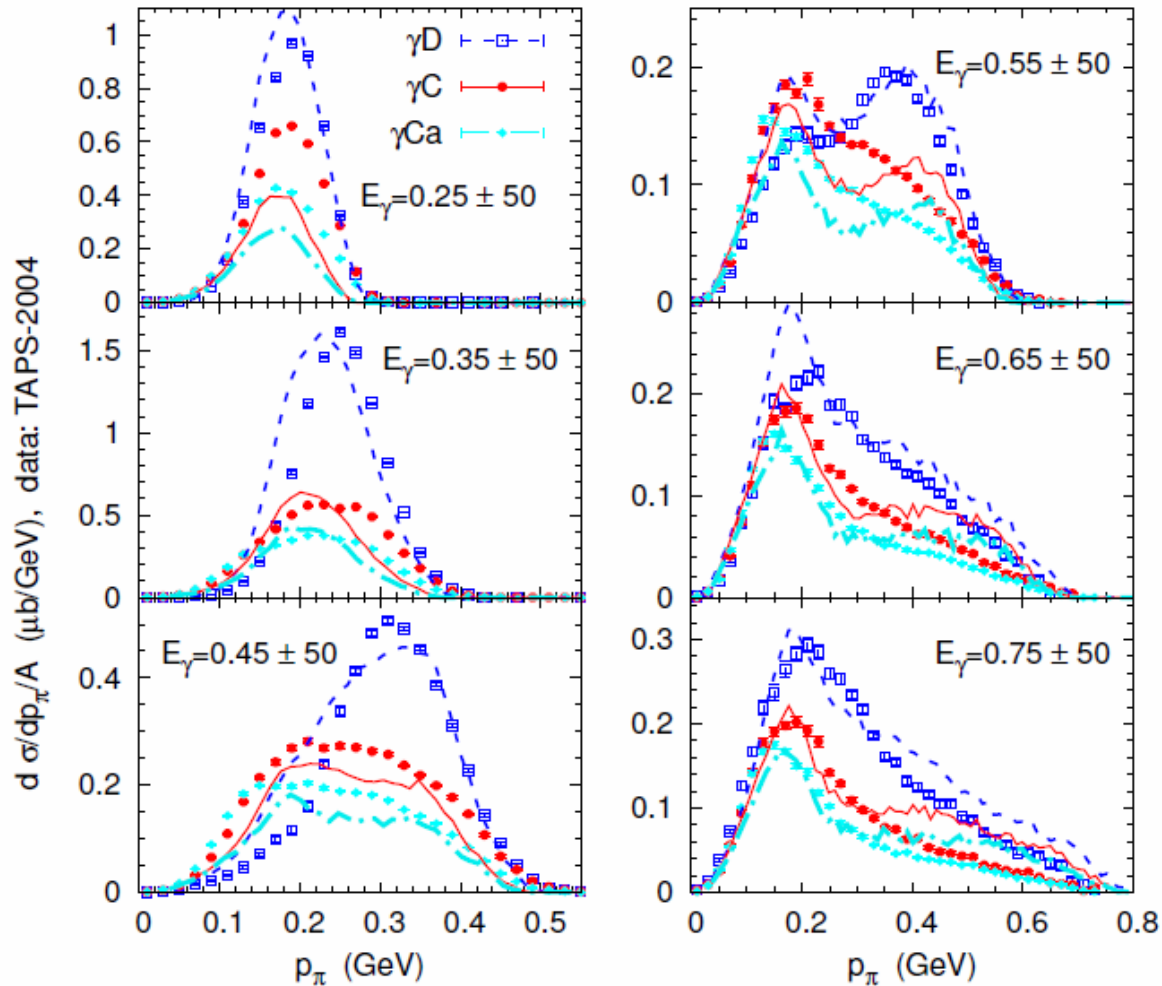
$$\Gamma_{N_A N_B \pi \rightarrow N_a N_b} = \Gamma_{N_A N_B \pi \rightarrow N_a N_b}^{\text{BG}} + \Gamma_{N_A N_B \pi \rightarrow N_a N_b}^{\text{resonance contribution}}$$

$$\Gamma_{N_A N_B \pi \rightarrow N_a N_b}^{\text{BG}} \sim \sigma_{NN \rightarrow NN \pi}^{\text{BG}}$$

$$\Gamma_{N_A N_B \pi \rightarrow N_a N_b}^{\text{resonance contribution}} \sim \sigma_{NN \rightarrow NN \pi}^{\text{resonance contribution}}$$

Test with γA

- $\gamma A \rightarrow \pi^0$ TAPS data



Targets:

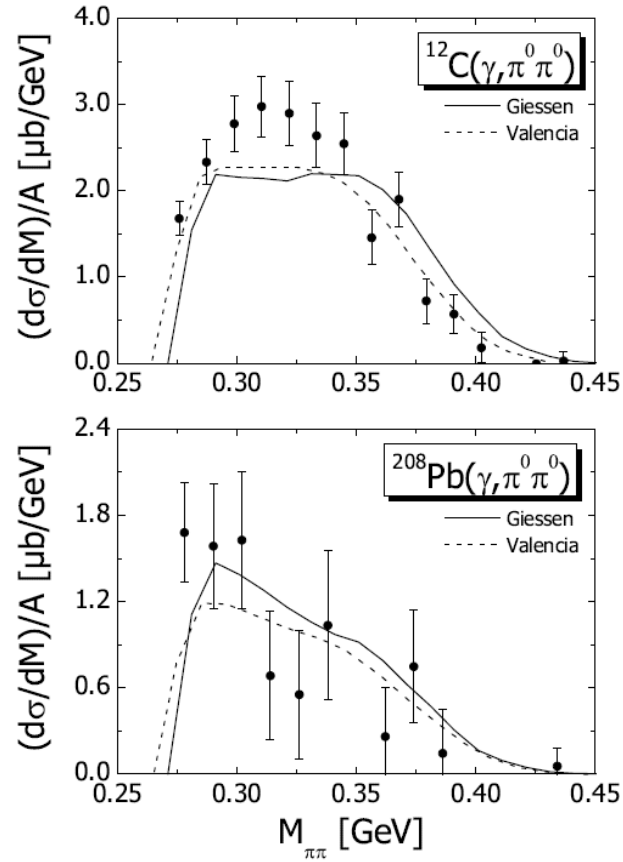
D

C

Ca

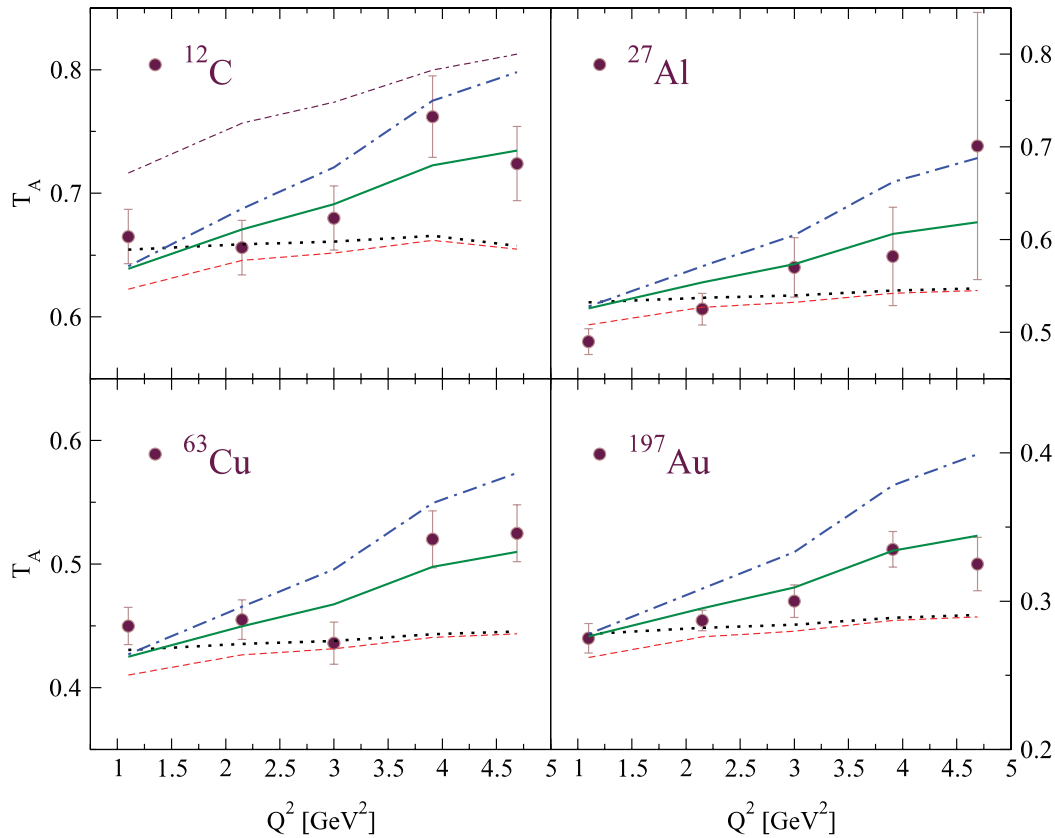
Lalikulich et al,
AIP Conf.Proc.
1663 (2015) 040004

2pi Photoproduction



Test with eA

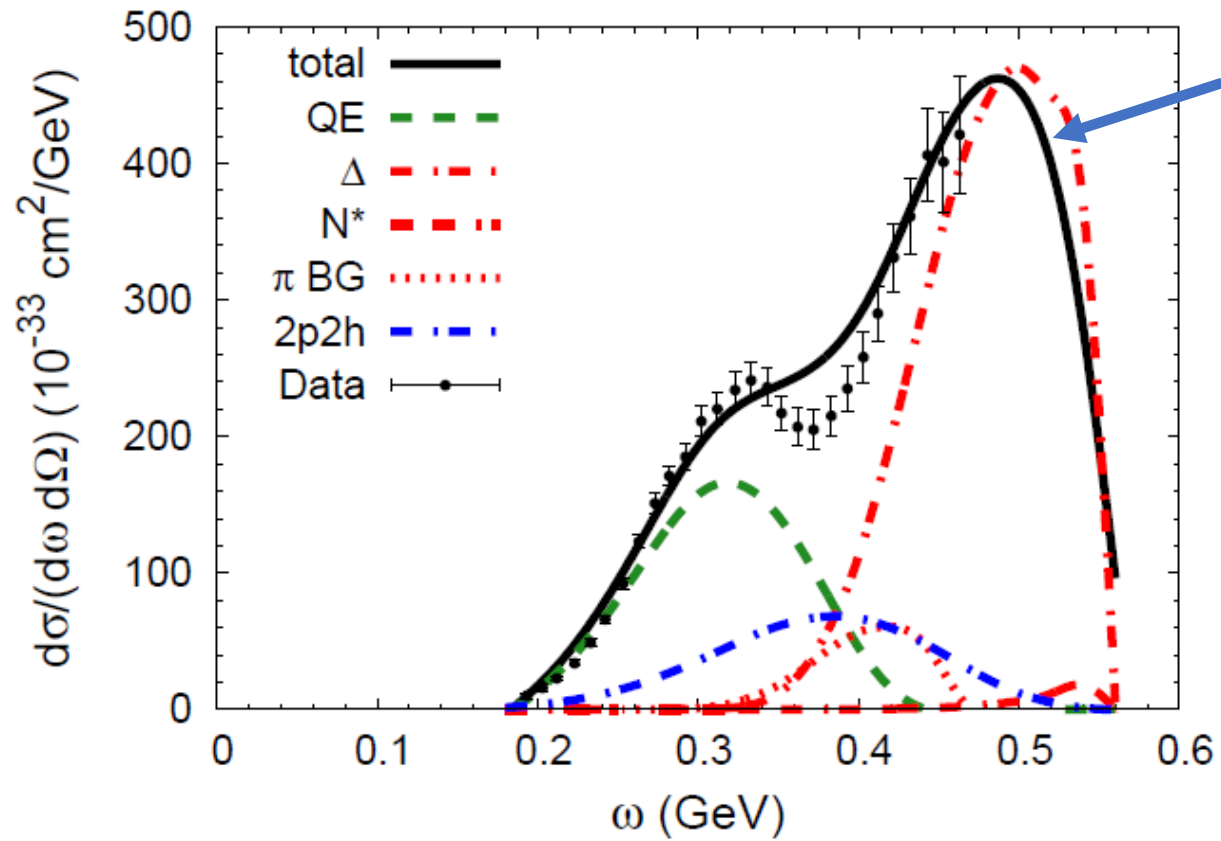
- π^+ JLAB data



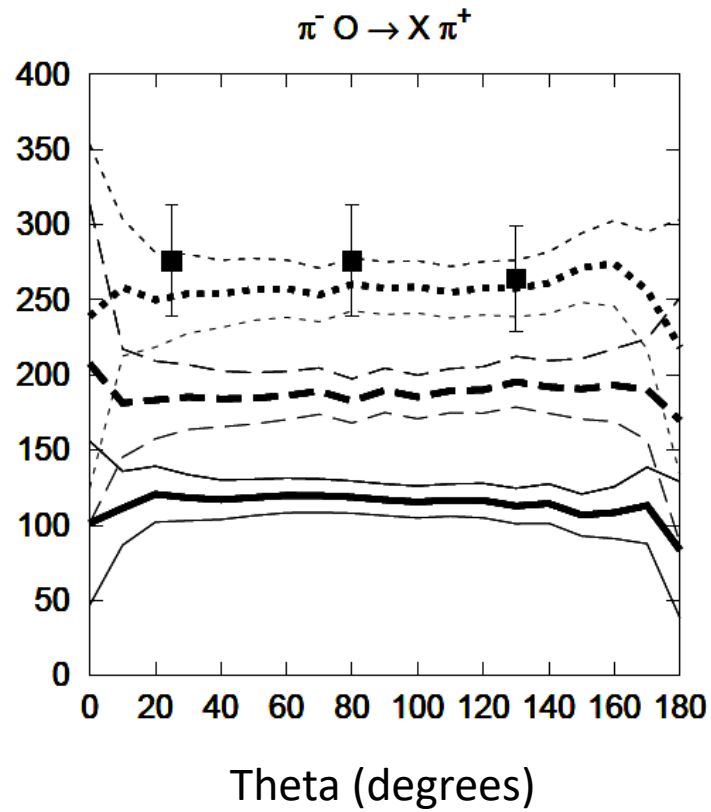
Exp: B. Clasie et al.
Phys. Rev. Lett. 99, 242502 (2007).

GiBUU: Kaskulov et al,
Phys.Rev. C79 (2009) 015207

Resonance-Background Interference



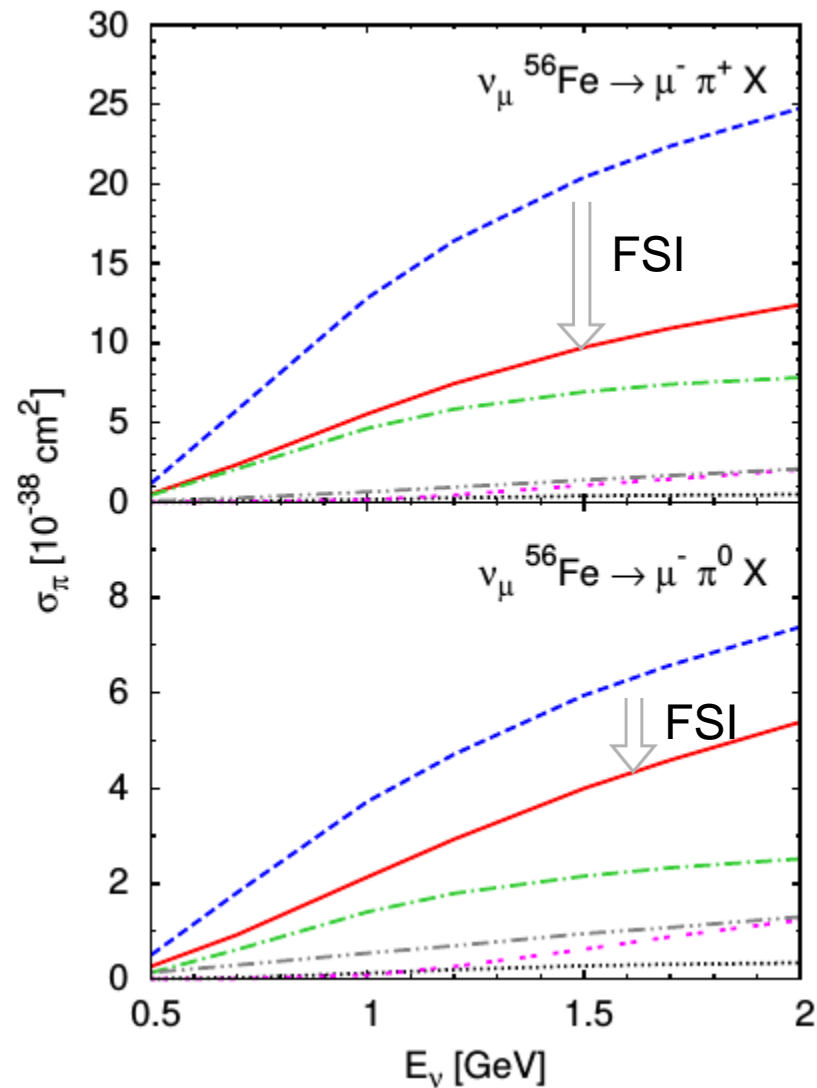
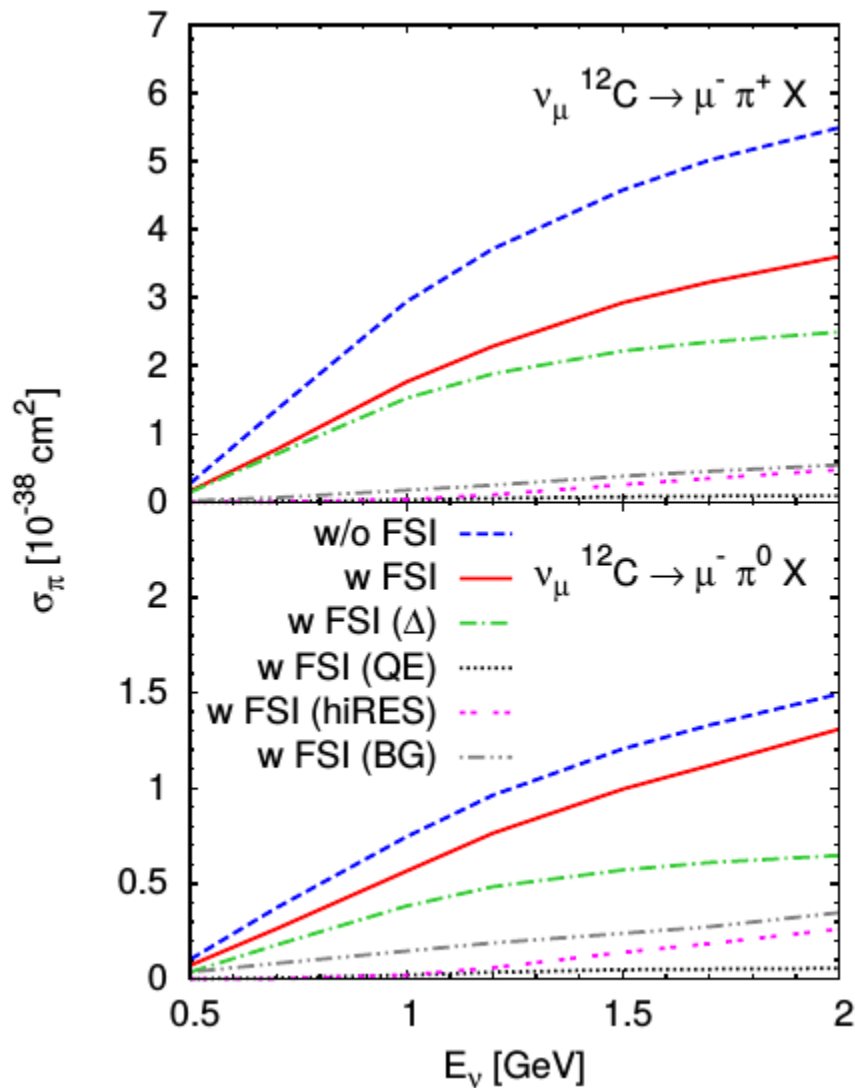
Double Charge Exchange



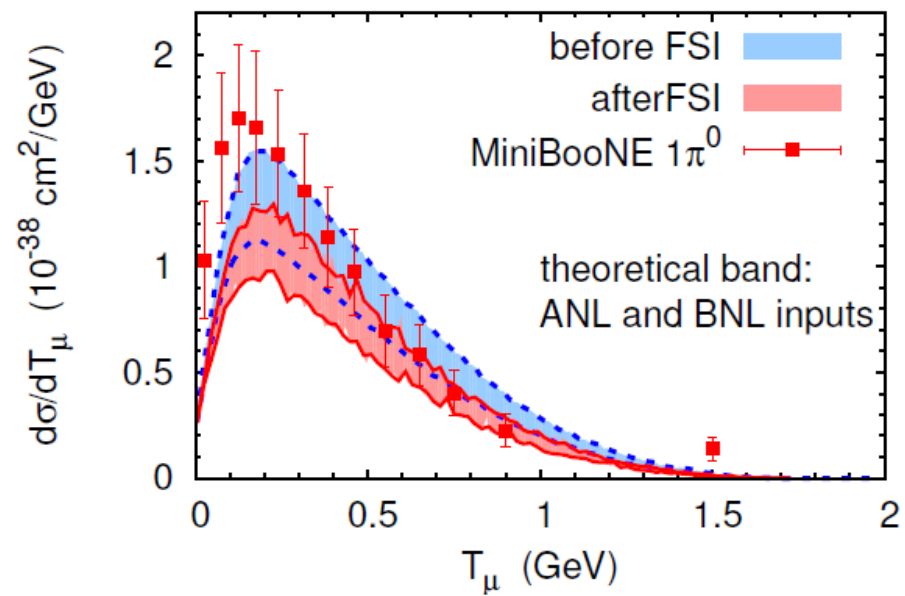
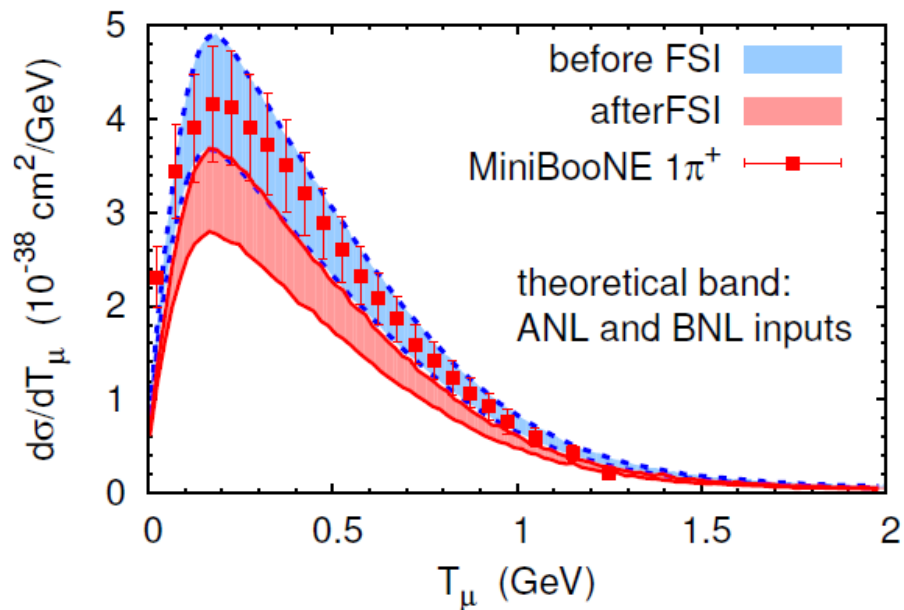
neutrino induced

CC: π^+ and π^0 production

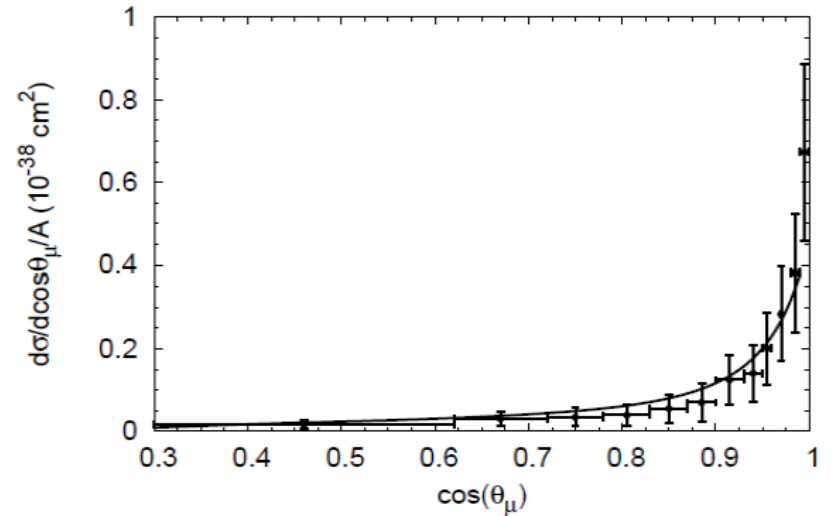
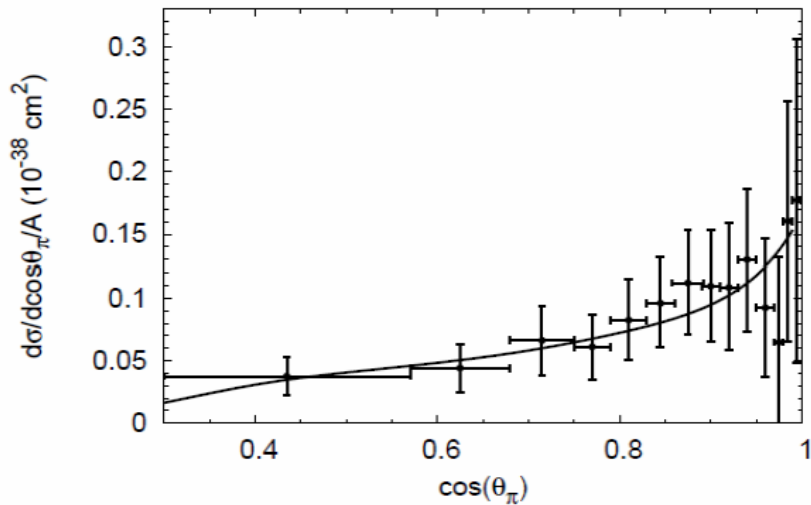
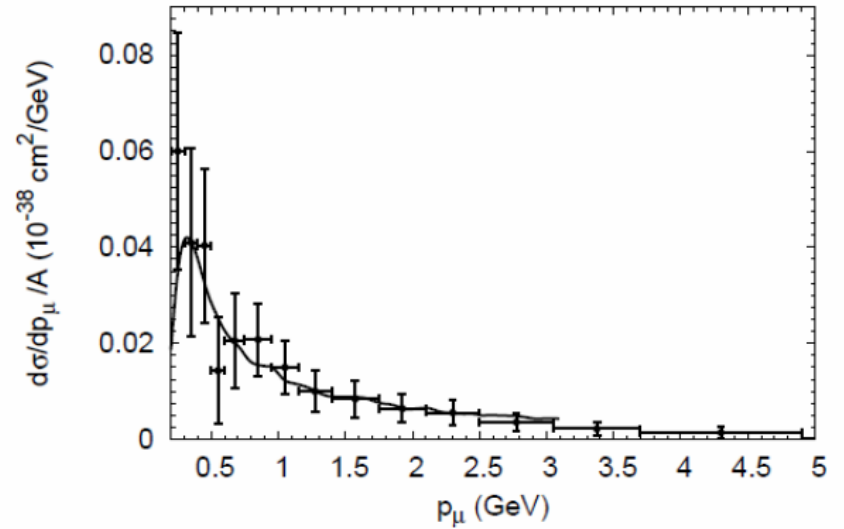
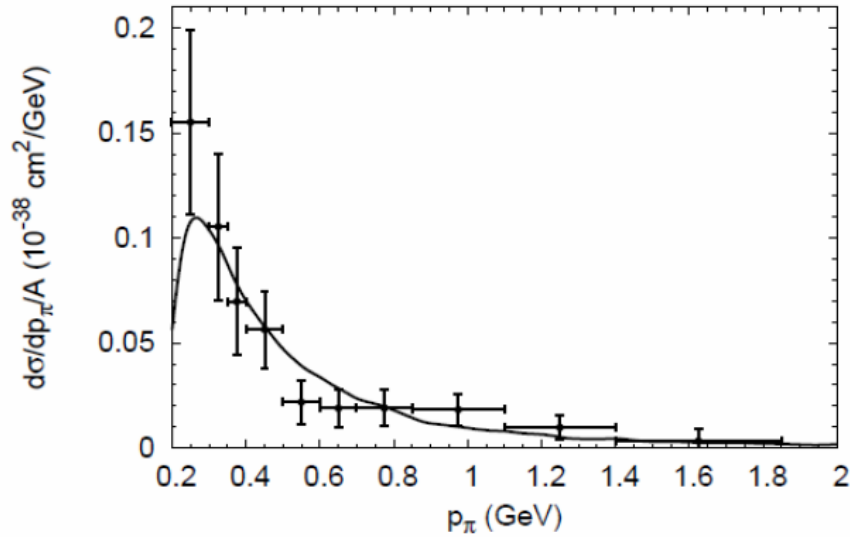
T.Leitner, PhD thesis, 2009



The MiniBooNE Puzzle



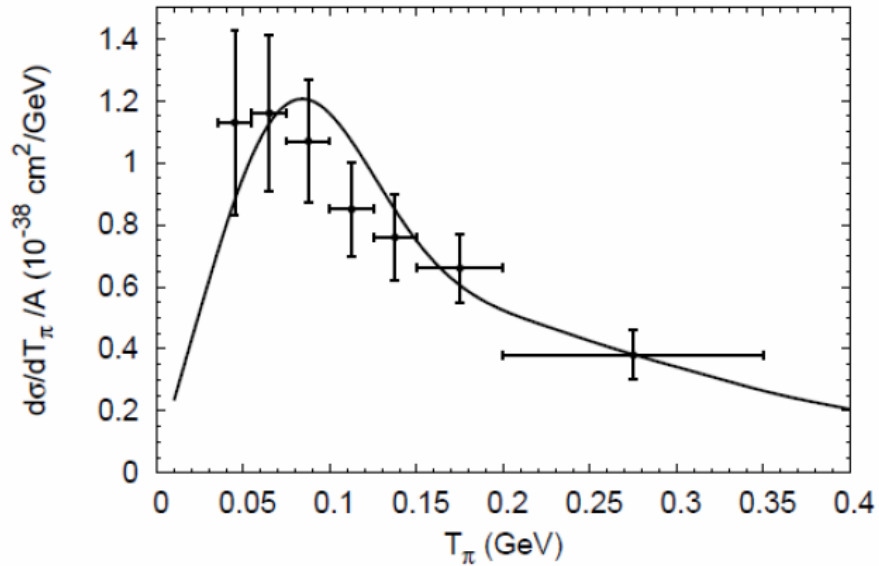
T2K ND280 pions on water



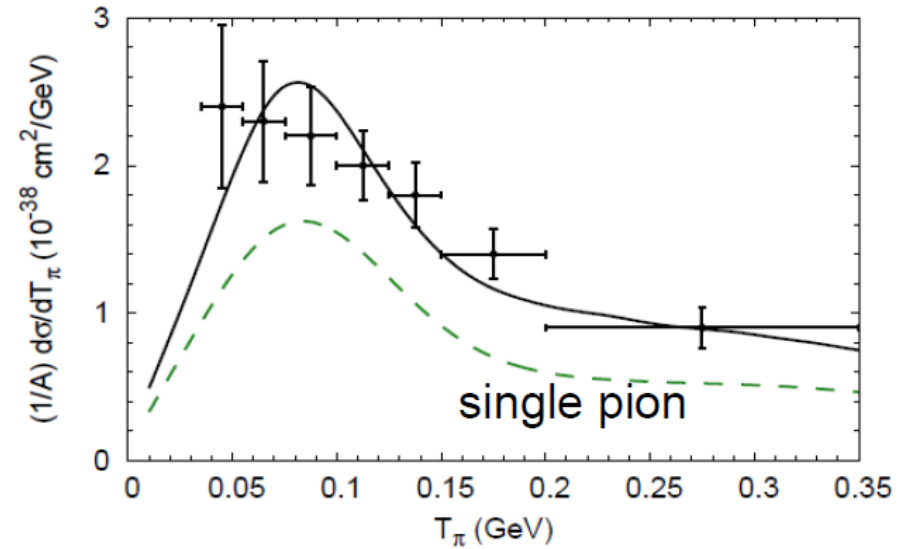
Data: T2K ND280
Phys.Rev. D95 (2017) 012010

MINERvA pions

■ CC charged pions



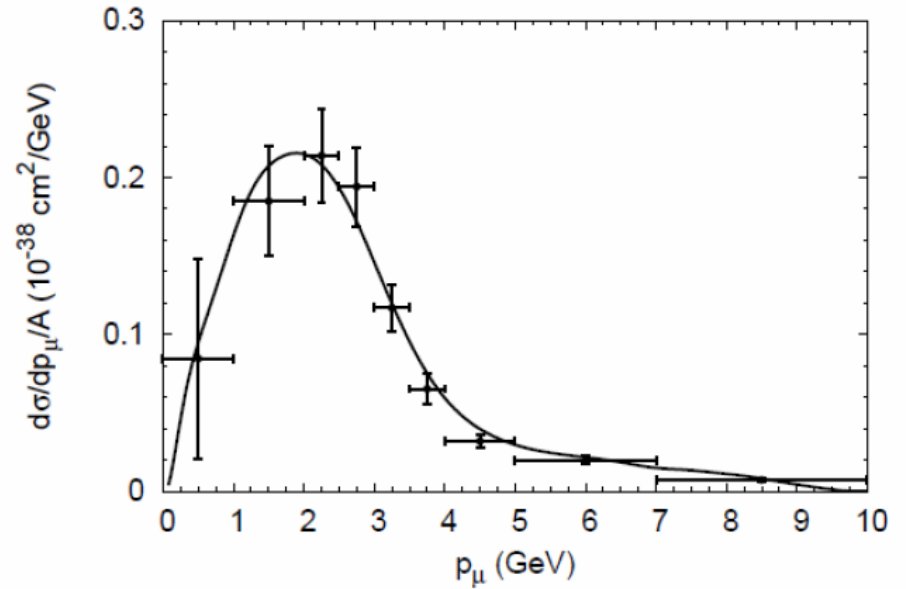
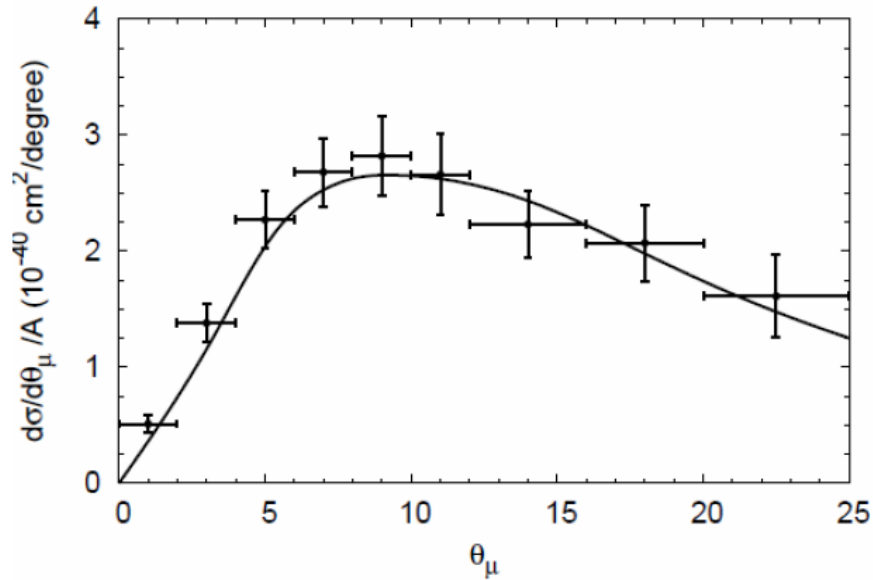
$W < 1.4 \text{ GeV}$



$W < 1.8 \text{ GeV}$, multiple pions

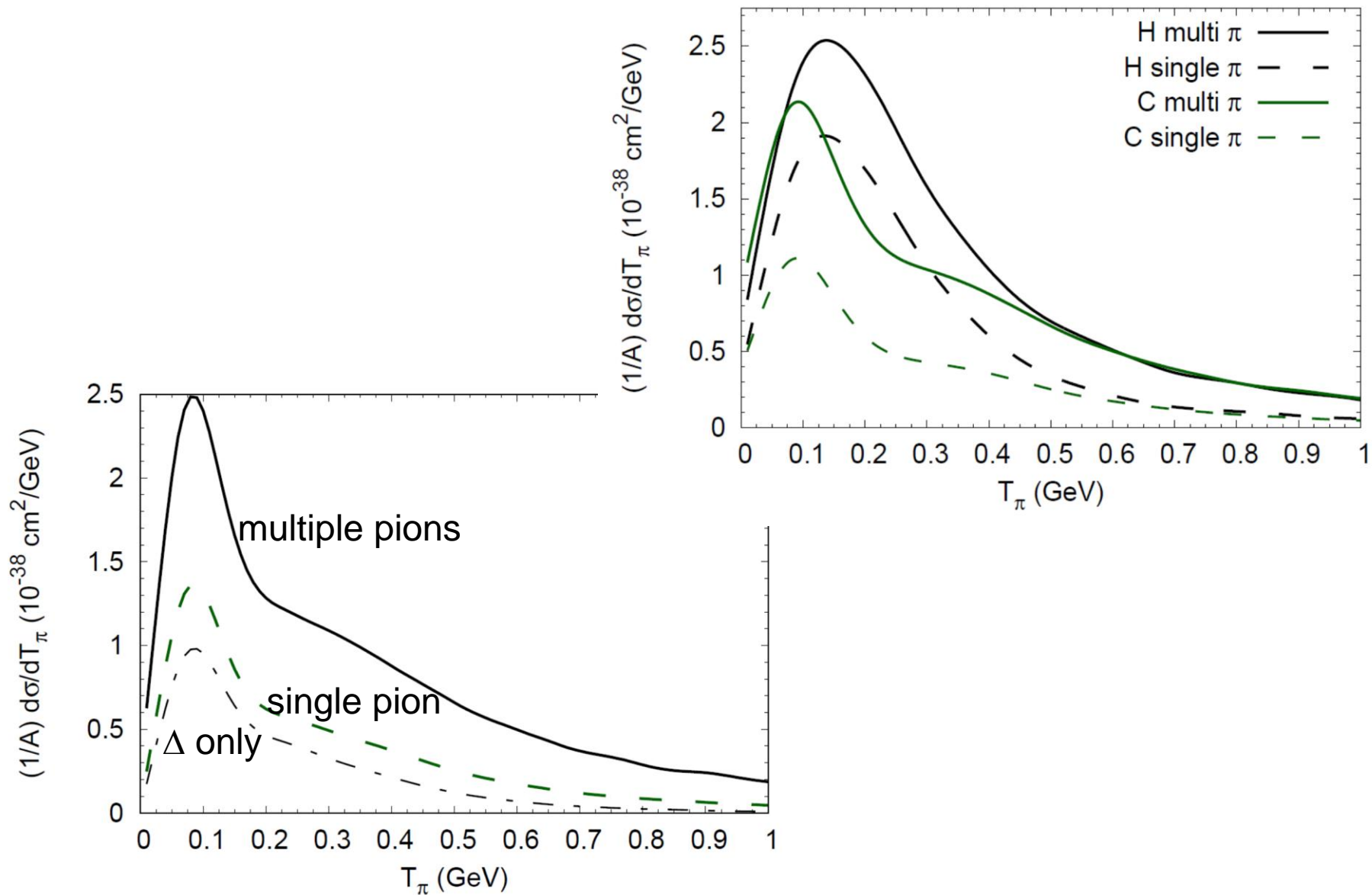
MINERvA pions

■ CC charged pions



$W < 1.8 \text{ GeV}$

Pions at NOvA



Conclusions

- The GiBUU generator has been checked against a large set of pion photo- and electronproduction data.

One and the same consistent model describes all the CC charged pion data from T2K and MINERvA without any special tune.