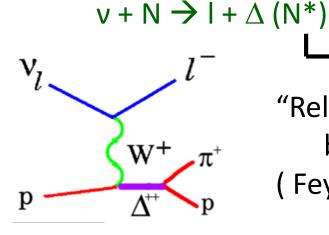
Yoshinari Hayato

(Kamioka, ICRR, The Univ. of Tokyo)

Based on D.Rein, and L.M.Sehgal, Ann. of Phys. 133(1981), and D.Rein, Z.Phys. C35 (1987) 43-64





"Relativistic harmonic oscillator model" by Feynman, Kislinger and Ravndal (Feynman et al. Phys. Rev. D3 (1971) 2706)

Initial helicity amplitude code was provided by one of the authors.

The interferences between the resonances are taken into account as appeared in the original paper.

Total cross-section: Integrated over the allowed kinematic region of W and q^2 . (=Consider mass of the lepton)

Further corrections (improvements)

Lepton mass and spin correction

Kuzmin et al. Mod.Phys.Lett. A19 (2004) 2815-2829

Phys.Part.Nucl. 35 (2004) S133-S138

Lepton mass correction

Berger & Sehgal Phys.Rev.D76:113004,2007

Form factors

1) Original

Axial vector mass is set to 1.21 GeV/c² by default.

 $(1.01, 1.11 \text{ and } 1.31 \text{ GeV/c}^2 \text{ are supported.})$

2) Graczyk-Sobczyk

Phys.Rev. D77 (2008) 053001

(Nowak Arxiv:0909.3659)

Parameters are fixed by re-fitting the ANL and BNL data.

Determination of kinematics in nucleus

- 1) Select nucleon momentum
- 2) Determine lepton kinematics in nucleon rest frame
- 3) Determine pion and nucleon kinematics in Adler frame Pion distribution from $\Delta(1232)$

Follow prescription by Rein (1981)

Pion from the other resonance

Isotropic in resonance rest frame.

Determination of original resonance

 $\sigma(D(1232))/\sigma(All\ resonances)$

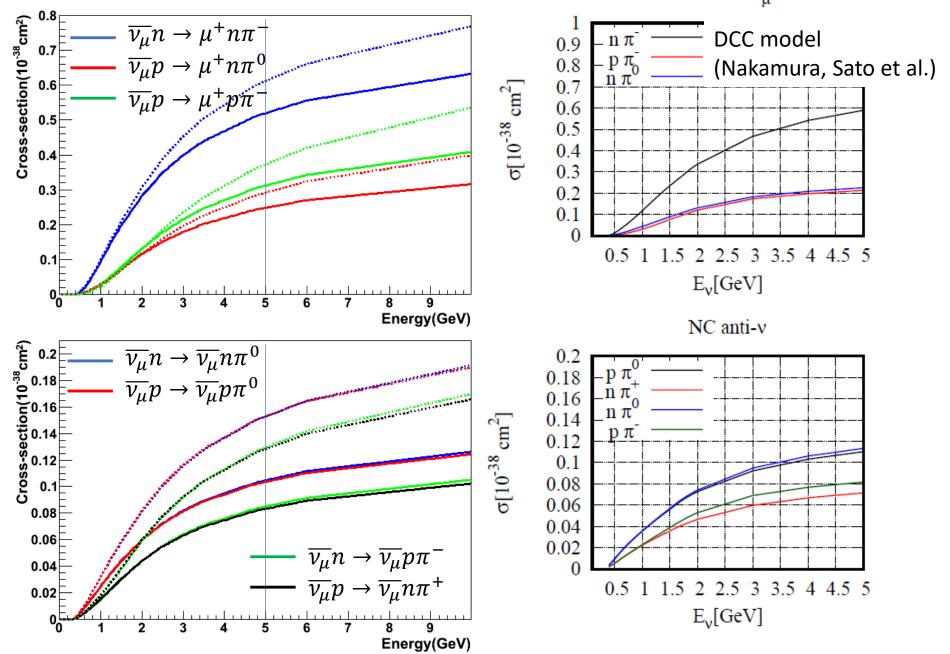
4) If the momentum of nucleon is below

the Fermi-surface momentum,

this event is suppressed.

- (~ a few % of events are discarded ~ suppressed)
- 5) X % of pions are not emitted at all. (Delta-absorption) X was 20% before introducing 2p2h. Now X is set to 0%.

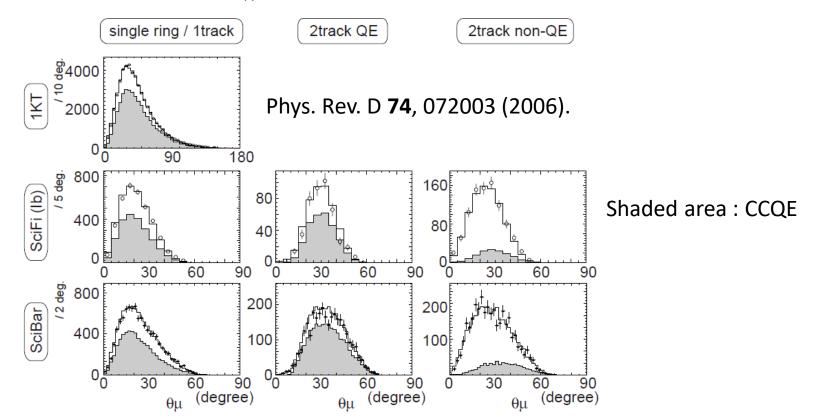
Single π production cross-section (W<2GeV)_{CC anti-v_µ}



Axial vector mass 1.21 GeV/c²

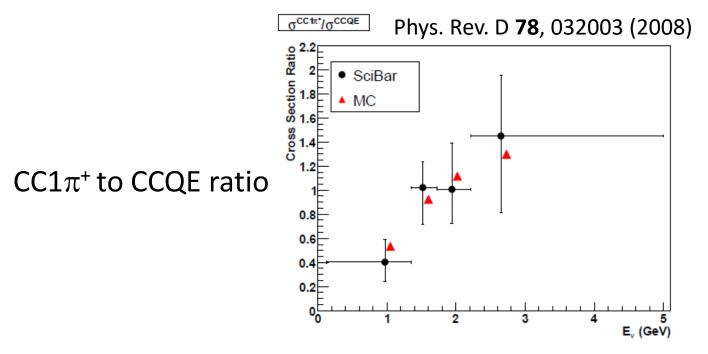
1) Suppression of forward going μ in inclusive sample (K2K) Larger M_A for CCQE + Bodek-Yang correction were not sufficient.

(K2K oscillation analysis : $M_A=1.1$ GeV/c² for CCQE & 1π production)



Axial vector mass 1.21 GeV/c²

2) CC1 π ⁺ to CCQE ratio and NC π ⁰ to CCQE @ K2K is almost unity



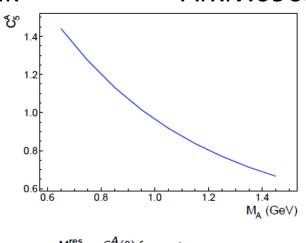
- 3) CCQE M_A seemed to be 1.21 GeV/c² @K2K (from shape)
- 4) # of π^0 (mainly from NC 1 π^0 production) in atmospheric ν sample agrees quite well.

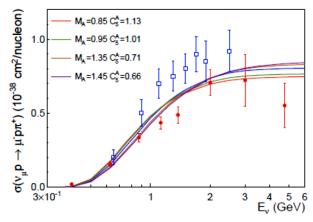
Alternative form factor

Graczyk-Sobczyk Phys.Rev. D77 (2008) 053001

Nowak

Arxiv:0909.3659



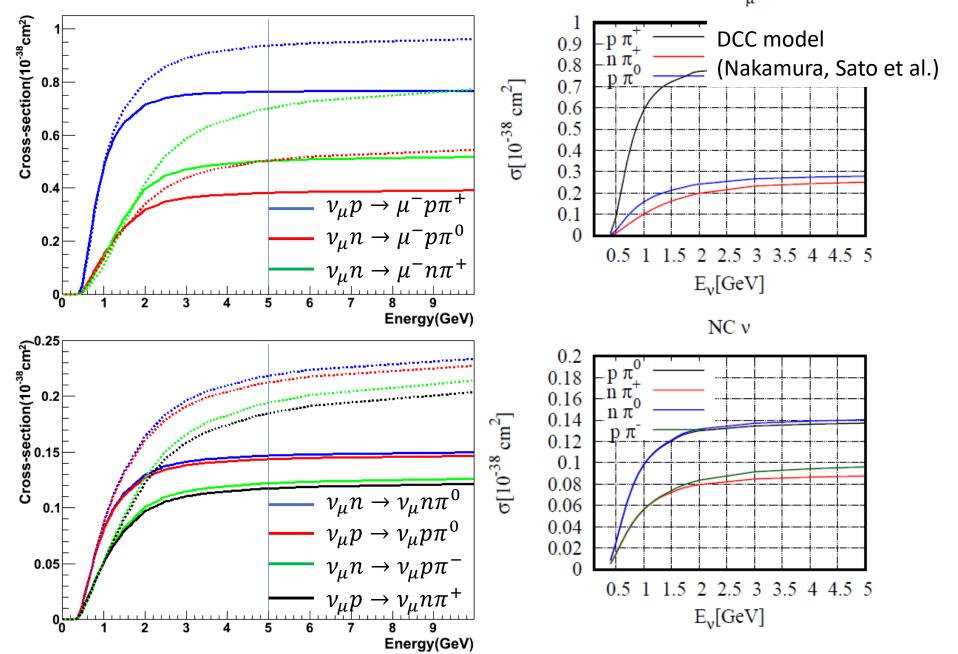


 M_A^{res} vs $C_5^A(0)$ for const xsec

Samples from the curve: nearly const A. Bercellie, P. Rodrigues et al.

- Parameters in nucleon model:
 - $C_5^A(0)$ Value of axial FF at $Q^2=0$. Main effect is normalization of total xsec
 - M_A^{res} Mass parameter in axial FF. Affects both shape of $d\sigma/dQ^2$ and overall normalization.
 - BG Scale of J = 1/2 nonresonant background terms
- ▶ Try to reparametrize $(M_A^{res}, C_5^A(0))$ into (shape, norm) for convenience
- Best fit: $M_A^{\text{res}} = 0.95$, $C_5^A(0) = 1.01$ Choose BG scale 1.3 ± 0.2

Single π production cross-section (W<2GeV) $_{_{CC\,\nu_{\mu}}}$

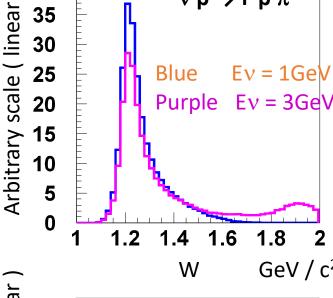


Single π production distributions

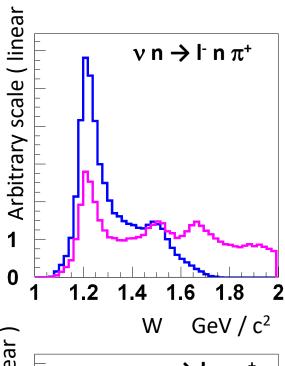
40

Invariant mass of resonance (W)

 $\nu p \rightarrow l^- p \pi^+$ Δ^{++} (1232) dominant

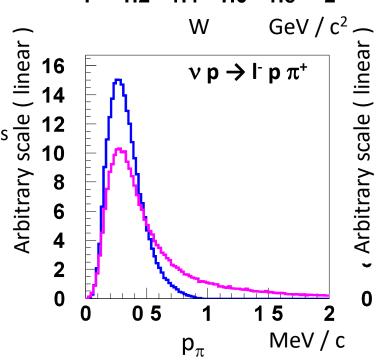


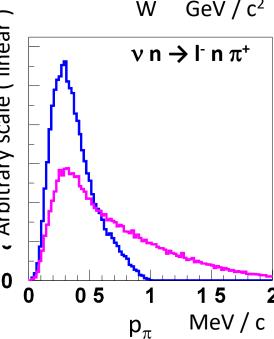
 $v p \rightarrow l^- p \pi^+$



momentum of π

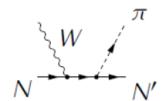
first order : determined by resonance masses

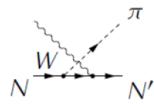


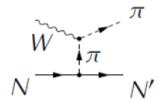


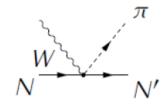
Model is implemented by M. Kabirnezhad Adapt for Neut by C. Wret

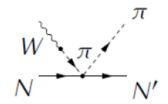
 The new model includes resonant (Rein-Sehgal model) and non-resonant interactions (5 diagrams from Hernandez et.al) coherently!





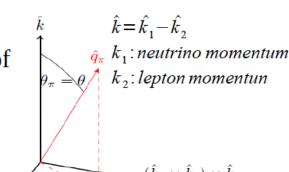






E. Hernandez, J. Nieves and M. Valverde, Phys. Rev. D **76** (2007) 033005

- We need to define a common framework to calculate the helicity amplitudes, Isobaric system.
- The main challenge is to calculate helicity amplitudes of the above diagrams in this frame.
- It is suitable for neutrino generators.
- The new model output is $d \sigma / dW dQ^2 d \Omega_{\pi}$ pion angles are part of cross-section!



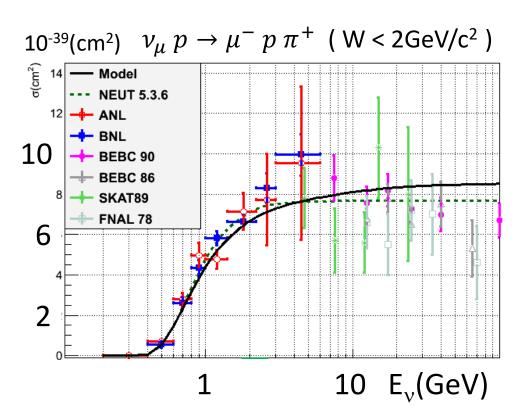
 $\phi_{\pi} = \phi$ $\hat{k}_{1} \times \hat{k}_{2}$

The main effects of nonresonant bkg is for pion angles due to the interference terms with resonances!

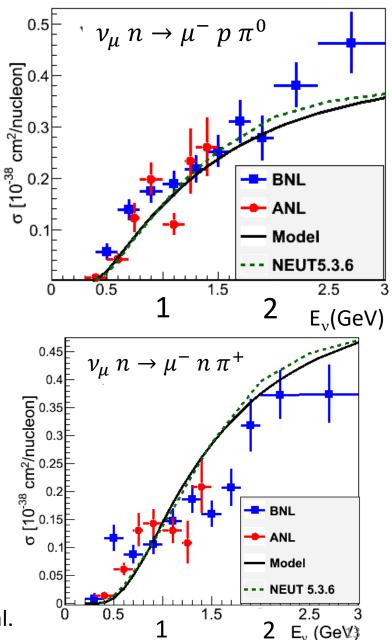
(Slide by M. Kabirnezhad)

New π model is implemented by M. Kabirnezhad Adapt for Neut by C. Wret

Interaction cross-sections

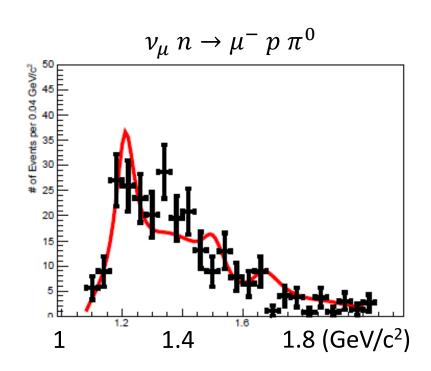


Figures by M. Kabirnezhad, ANL & BNL data is reanalyzed by C. Wilkinson et al.

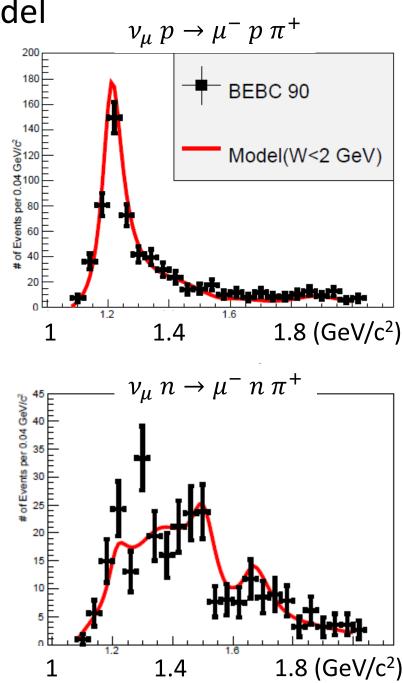


New π model is implemented by M. Kabirnezhad Adapt for Neut by C. Wret

Intermediate resonance
Invariant mass distributions



(Figures by M. Kabirnezhad)



New π model is implemented by M. Kabirnezhad Adapt for Neut by C. Wret

Angular distribution of π in the Adler frame

T2K ND280 neutrino flux

