

Weakly bound states and near-threshold resonances from *ab initio* nuclear theory

Critical stability of few-body quantum systems

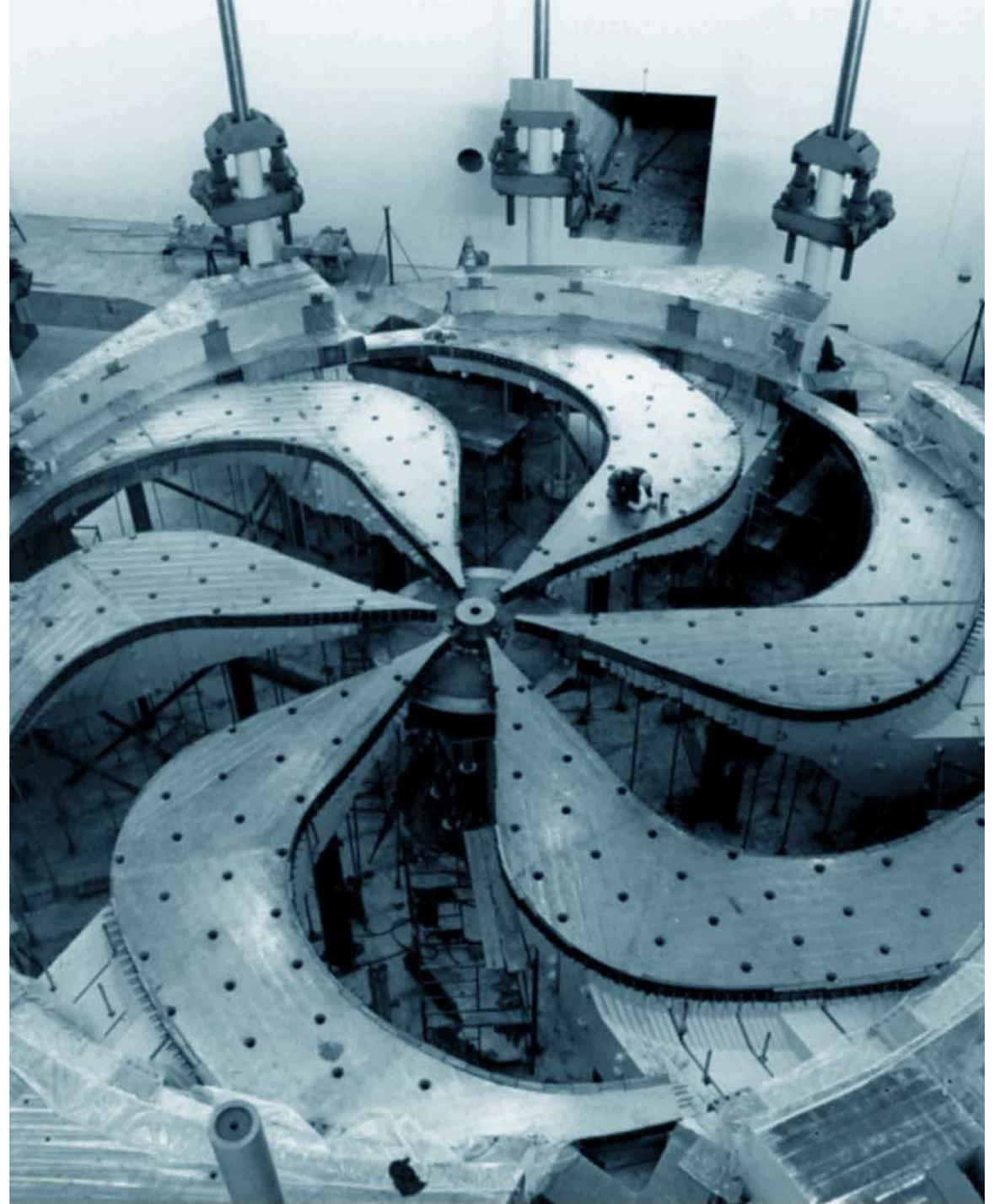
ECT* Trento, October 23 - 27, 2023

Petr Navratil

TRIUMF

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Peter Gysbers (TRIUMF), Michael Gennari (UVic/TRIUMF),
Matteo Vorabbi (Surrey), Jakub Herko (UND)

2023-10-26

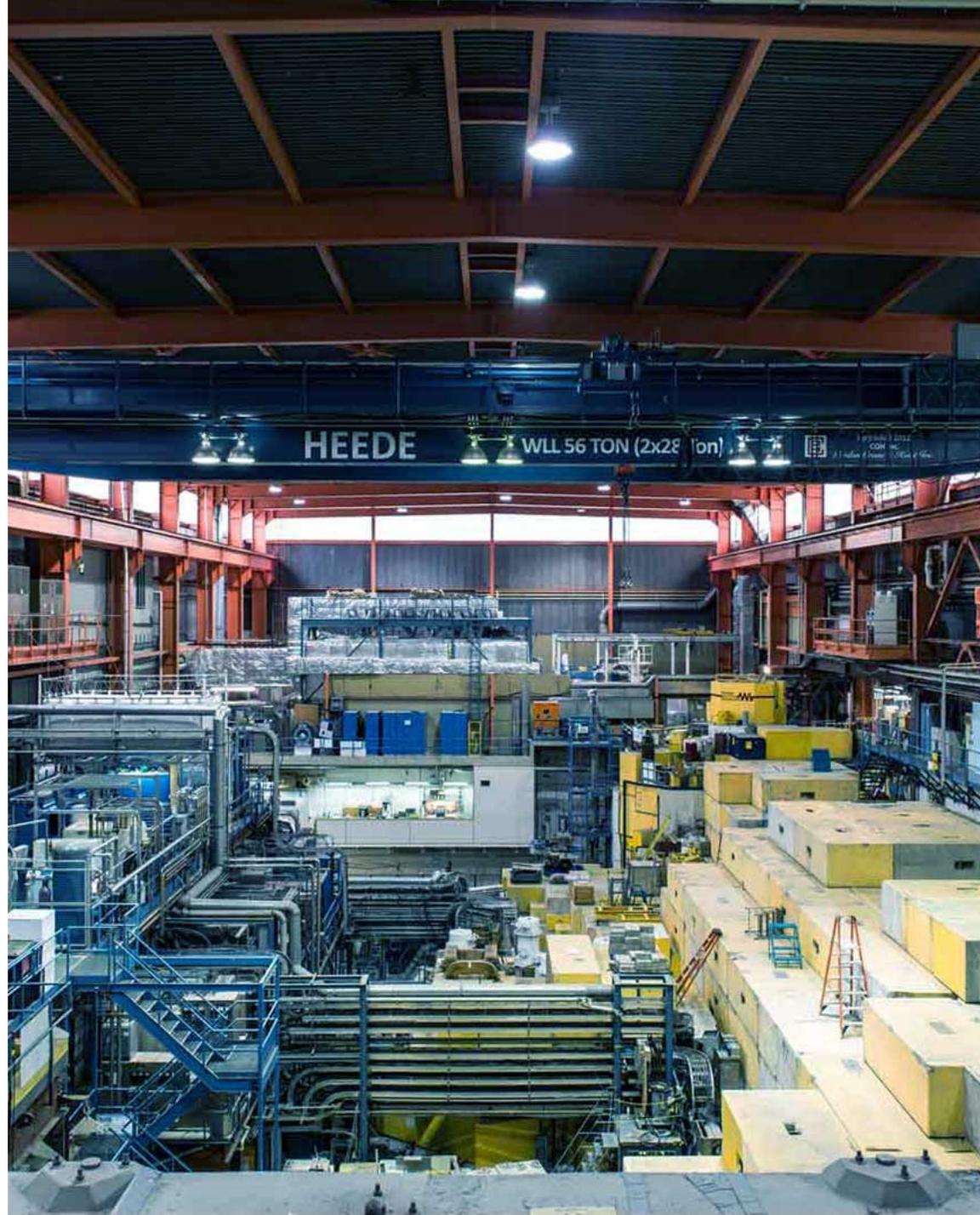


Outline

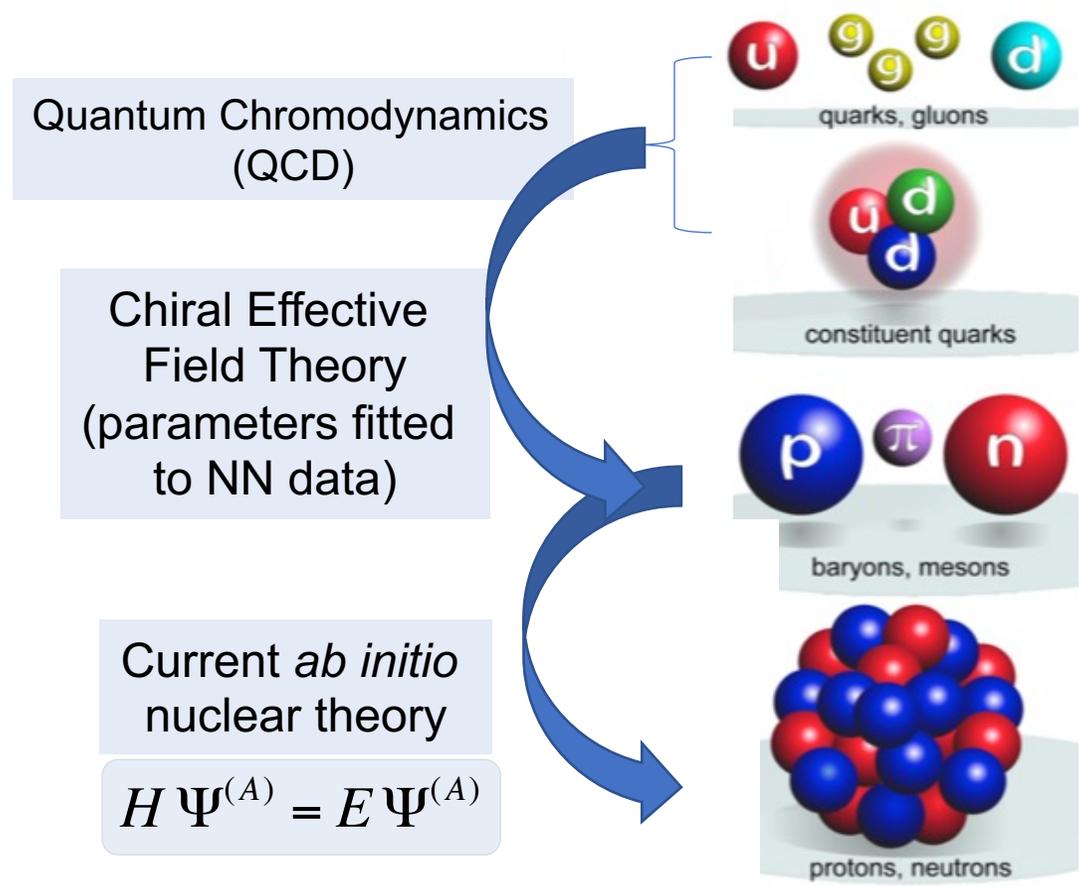
- *Ab initio* nuclear theory
 - No-core shell model (NCSM) and NCSM with continuum (NCSMC)
 - Input chiral NN+3N interactions
- Applications to weakly-bound states and near threshold resonances
 - DT fusion
 - S-wave resonance close to the ${}^6\text{He}+p$ threshold in ${}^7\text{Li}$
 - Parity inversion in ${}^{11}\text{Be}$ ground state
 - β -delayed proton emission in ${}^{11}\text{Be}$
 - Two-neutron Borromean halo nucleus ${}^6\text{He}$

Ab initio nuclear theory

2023-10-26



First principles or *ab initio* nuclear theory – what we do at present



	NN force	NNN force	NNNN force
Q^0 LO			
Q^2 NLO			
Q^3 N ² LO			
Q^4 N ³ LO			



Review

Ab initio no core shell modelBruce R. Barrett^a, Petr Navrátil^b, James P. Vary^{c,*}

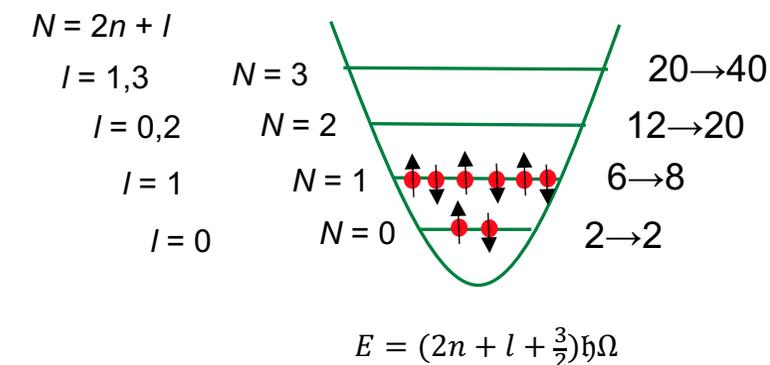
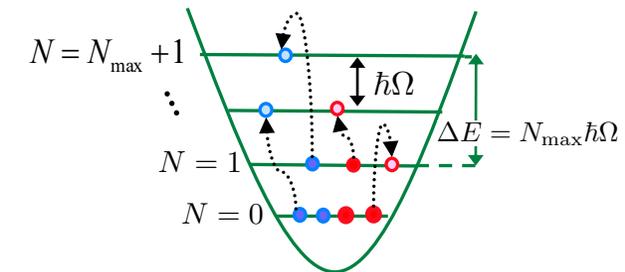
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Ab initio No-Core Shell Model (NCSM)

- Basis expansion method
 - Harmonic oscillator (HO) basis truncated in a particular way (N_{\max})
 - Why HO basis?
 - Lowest filled HO shells match magic numbers of light nuclei (2, 8, 20 – ^4He , ^{16}O , ^{40}Ca)
 - Equivalent description in relative(Jacobi)-coordinate and Slater determinant (SD) basis
- Short- and medium range correlations
- Bound-states, narrow resonances



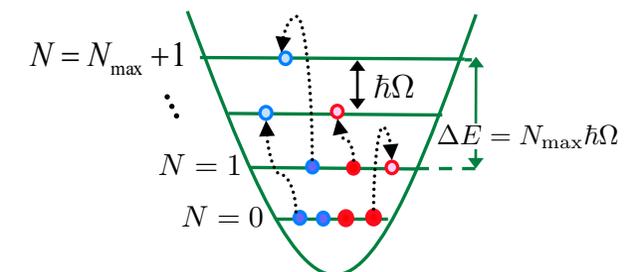
NCSM





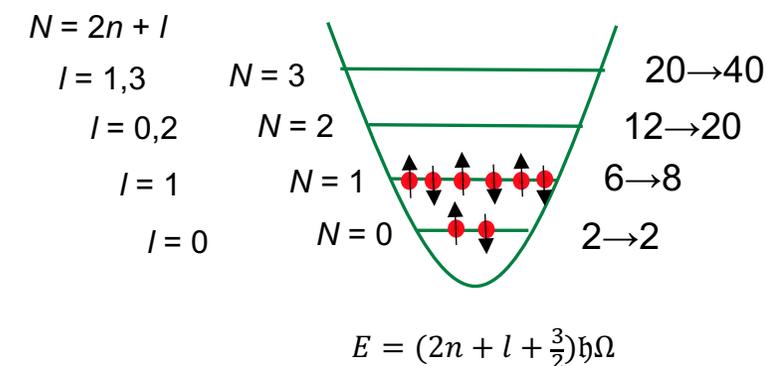
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$$\Psi^A = \sum_{N=0}^{N_{\max}} \sum_i c_{Ni} \Phi_{Ni}^{HO}(\vec{\eta}_1, \vec{\eta}_2, \dots, \vec{\eta}_{A-1})$$

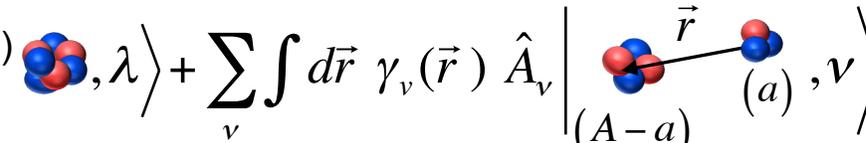
$$\Psi_{SD}^A = \sum_{N=0}^{N_{\max}} \sum_j c_{Nj}^{SD} \Phi_{SDNj}^{HO}(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_A) = \Psi^A \varphi_{000}(\vec{R}_{CM})$$



Ab Initio Calculations of Structure, Scattering, Reactions

Unified approach to bound & continuum states

No-Core Shell Model with Continuum (NCSMC)

$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} \left| \begin{array}{c} (A) \\ \text{Nucleus} \\ \lambda \end{array} \right\rangle + \sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} \left| \begin{array}{c} (A-a) \quad (a) \\ \text{Nucleus} \quad \text{Nucleus} \\ \nu \end{array} \right\rangle$$
The equation shows the wave function $\Psi^{(A)}$ as a sum of two terms. The first term is a discrete sum over λ of c_{λ} times a state $|^{(A)} \text{Nucleus}, \lambda\rangle$, where the nucleus is represented by a cluster of red and blue spheres. The second term is a continuous sum over ν of an integral over $d\vec{r}$ of $\gamma_{\nu}(\vec{r}) \hat{A}_{\nu}$ times a state $|_{(A-a) \text{ Nucleus} \quad (a) \text{ Nucleus}}, \nu\rangle$. This second state is illustrated with a diagram showing a nucleus of $(A-a)$ nucleons and a separate nucleon, with a vector \vec{r} indicating the relative position between the nucleon and the nucleus.

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$$\Psi^{(A)} = \underbrace{\sum_{\lambda} c_{\lambda} \left| \begin{matrix} (A) \\ \text{cluster} \\ \lambda \end{matrix} \right\rangle}_{\text{bound states}} + \sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} \left| \begin{matrix} (A-a) & \vec{r} & (a) \\ \nu & & \nu \end{matrix} \right\rangle$$

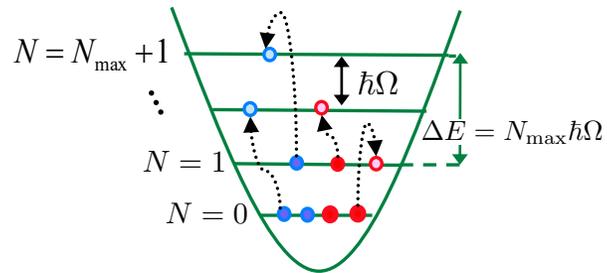
Static solutions for aggregate system,
describe all nucleons close together

Ab Initio Calculations of Structure, Scattering, Reactions

Unified approach to bound & continuum states

No-Core Shell Model with Continuum (NCSMC)

$$\Psi^{(A)} = \underbrace{\sum_{\lambda} c_{\lambda} \left| \begin{matrix} (A) \\ \text{cluster} \\ \lambda \end{matrix} \right\rangle}_{\text{Static solutions for aggregate system}} + \underbrace{\sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} \left| \begin{matrix} (A-a) & \vec{r} & (a) \\ \nu & & \nu \end{matrix} \right\rangle}_{\text{Continuous microscopic cluster states}}$$



Continuous microscopic cluster states, describe long-range projectile-target

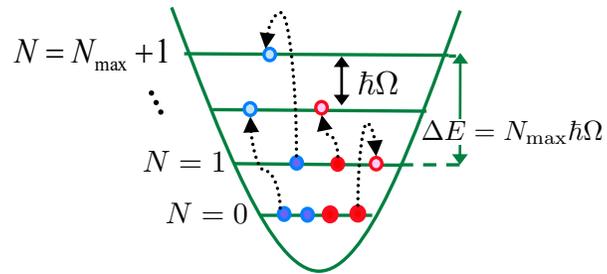
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Ab Initio Calculations of Structure, Scattering, Reactions

Unified approach to bound & continuum states

No-Core Shell Model with Continuum (NCSMC)

$$\Psi^{(A)} = \underbrace{\sum_{\lambda} c_{\lambda} \left| \begin{matrix} (A) \\ \text{cluster} \\ \lambda \end{matrix} \right\rangle}_{\text{Unknowns}} + \underbrace{\sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} \left| \begin{matrix} (A-a) & \vec{r} & (a) \\ \nu & & \nu \end{matrix} \right\rangle}_{\text{Unknowns}}$$



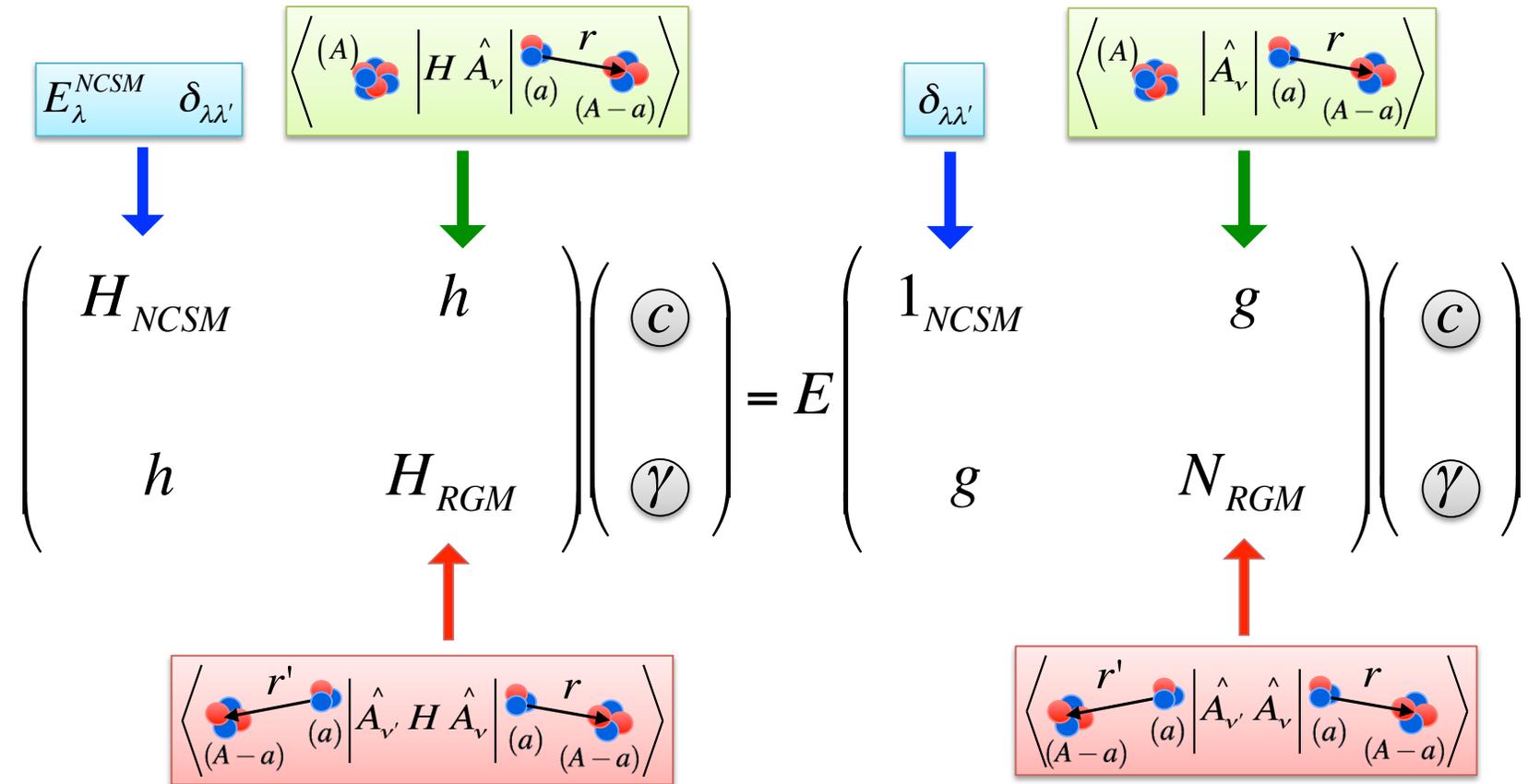
Continuous microscopic cluster states, describe long-range projectile-target

Static solutions for aggregate system, describe all nucleons close together

Coupled NCSMC equations

$$H \Psi^{(A)} = E \Psi^{(A)}$$

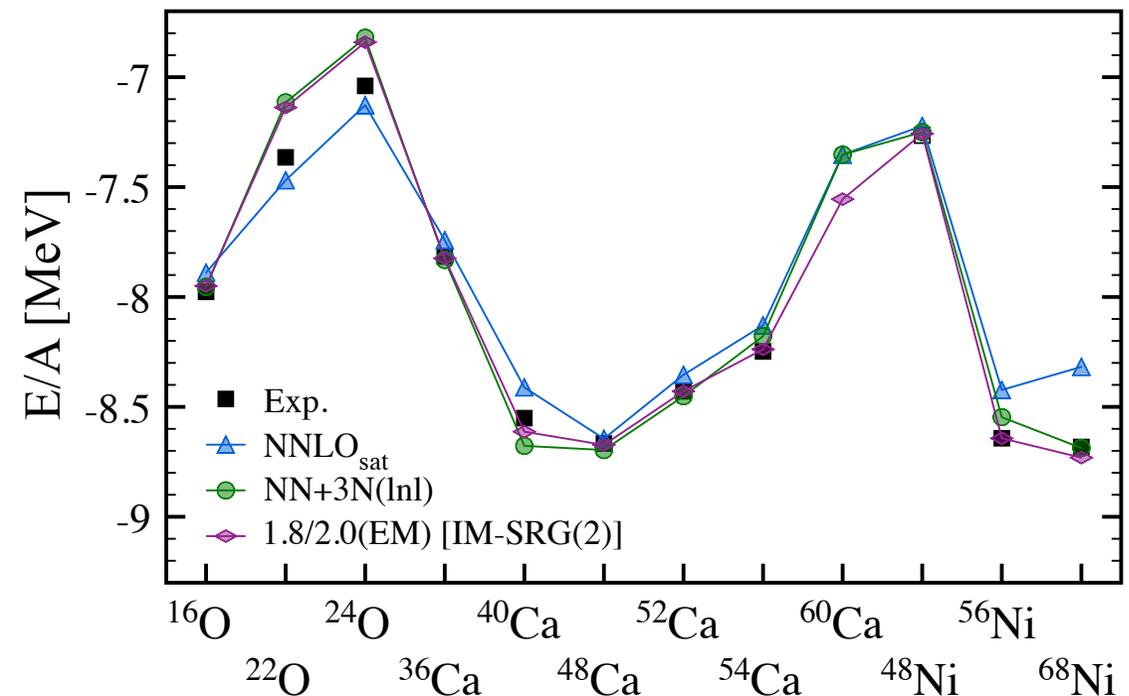
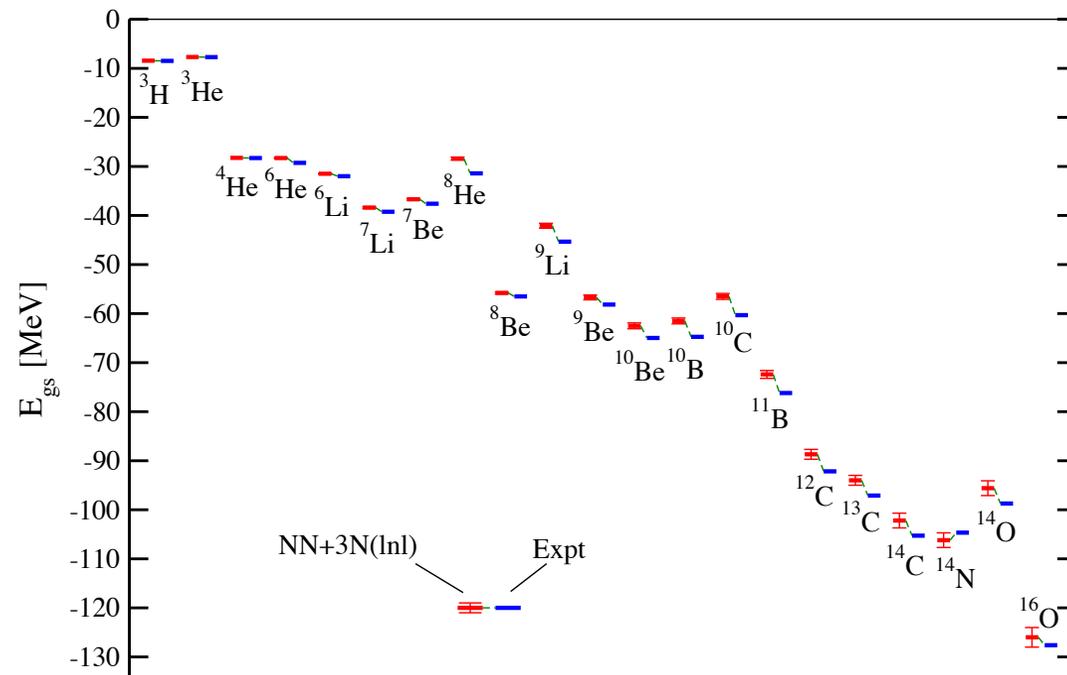
$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} \left| \begin{matrix} (A) \\ \text{cluster} \end{matrix}, \lambda \right\rangle + \sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} \left| \begin{matrix} (A-a) & (a) \\ \text{cluster} & \text{cluster} \end{matrix}, \nu \right\rangle$$



Input for NCSMC calculations: Nuclear forces from chiral Effective Field Theory

- Quite reasonable description of binding energies across the nuclear charts becomes feasible
 - **The Hamiltonian fully determined in $A=2$ and $A=3,4$ systems**
 - Nucleon–nucleon scattering, deuteron properties, ^3H and ^4He binding energy, ^3H half life
 - Light nuclei – NCSM
 - Medium mass nuclei – Self-Consistent Green’s Function method

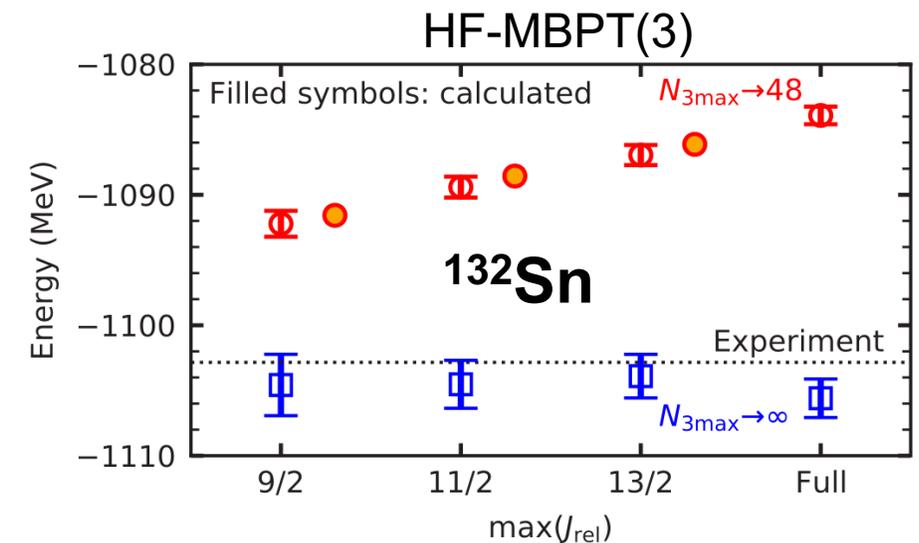
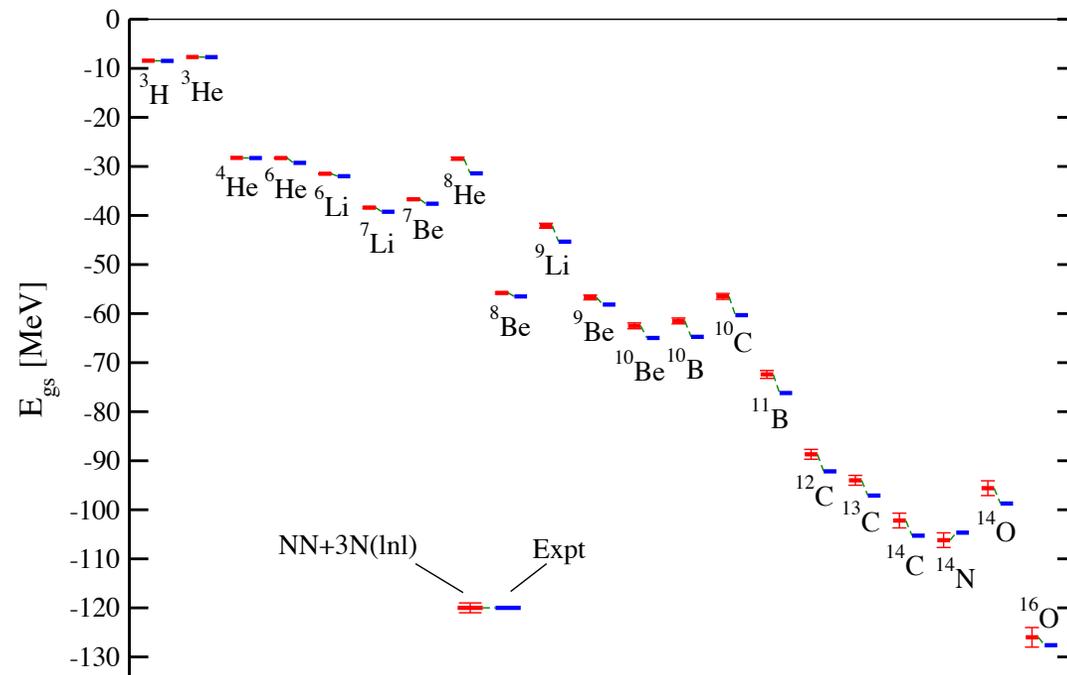
NN N³LO (Entem-Machleidt 2003)
3N N²LO w local/non-local regulator



Input for NCSMC calculations: Nuclear forces from chiral Effective Field Theory

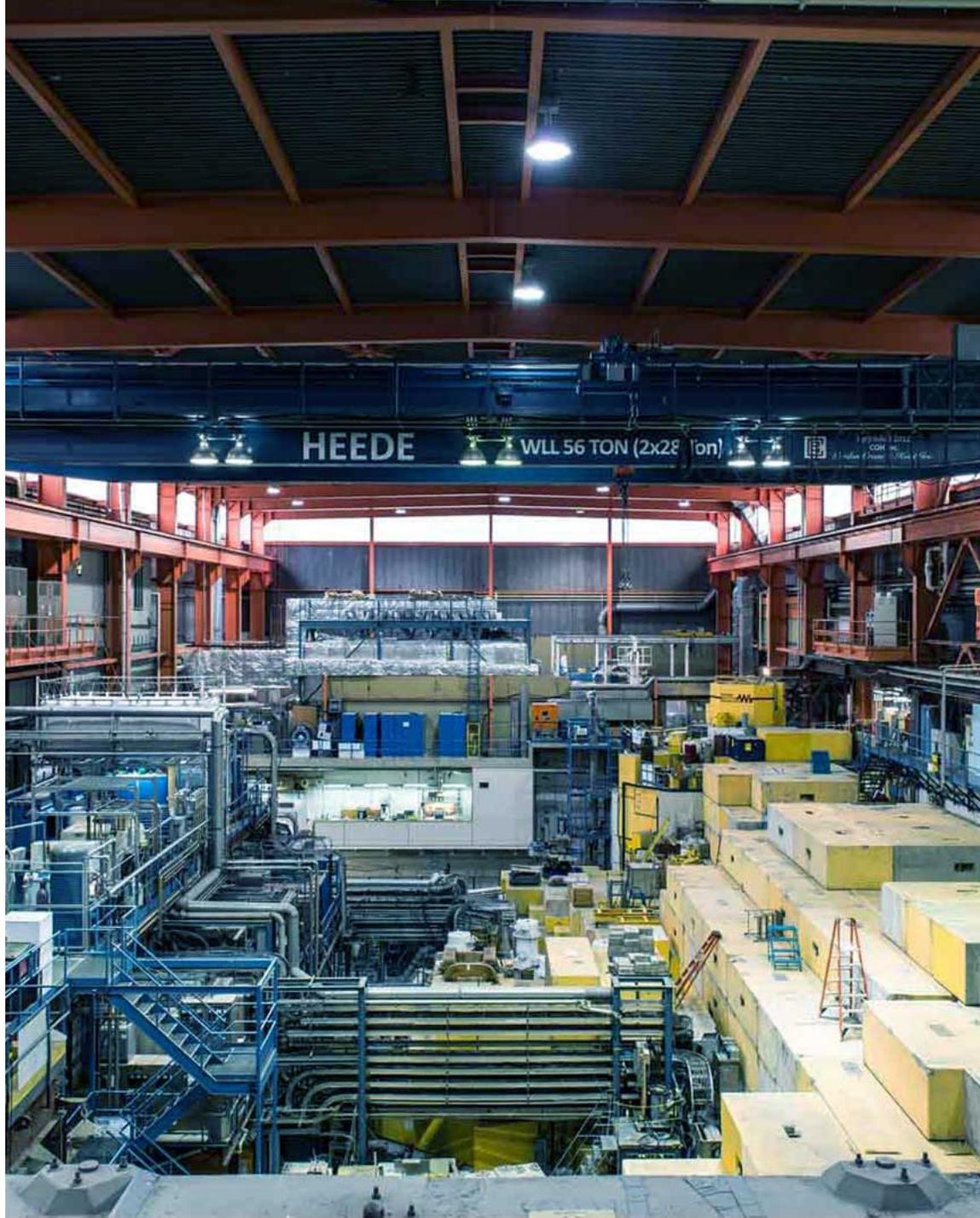
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 - Nucleon–nucleon scattering, deuteron properties, ^3H and ^4He binding energy, ^3H half life
 - Light nuclei – NCSM
 - Heavy nuclei – HF-MBPT(3)

NN N³LO (Entem-Machleidt 2003)
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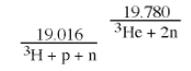
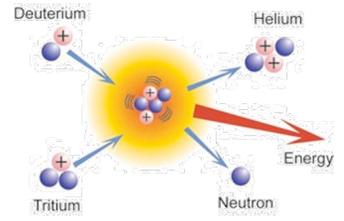
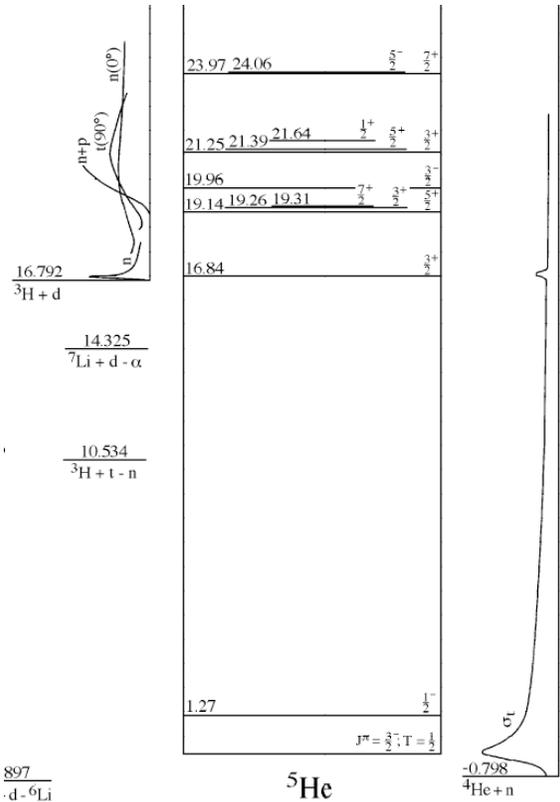
DT fusion

2023-10-26



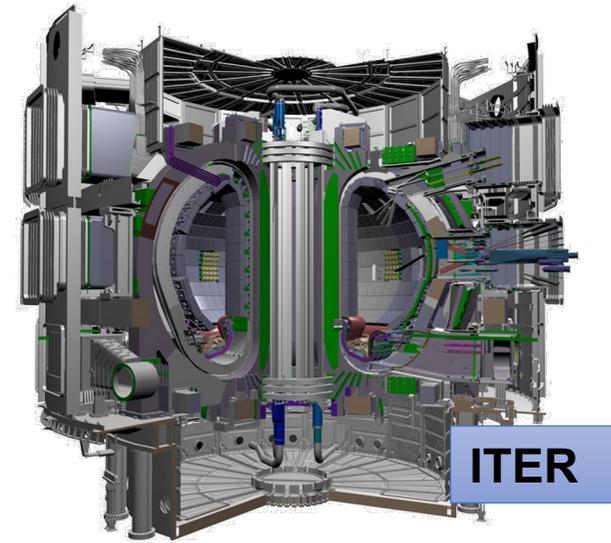
Deuterium-Tritium fusion

- The $d+{}^3\text{H}\rightarrow n+{}^4\text{He}$ reaction
 - The most promising to produce fusion energy in the near future
 - Used to achieve inertial-confinement (laser-induced) fusion at NIF, and magnetic-confinement fusion at ITER
 - With its mirror reaction, ${}^3\text{He}(d,p){}^4\text{He}$, important for Big Bang nucleosynthesis



Resonance at $E_{\text{cm}} = 48 \text{ keV}$ ($E_d = 105 \text{ keV}$)
 in the $J=3/2^+$ channel
 Cross section at the peak: 4.88 b

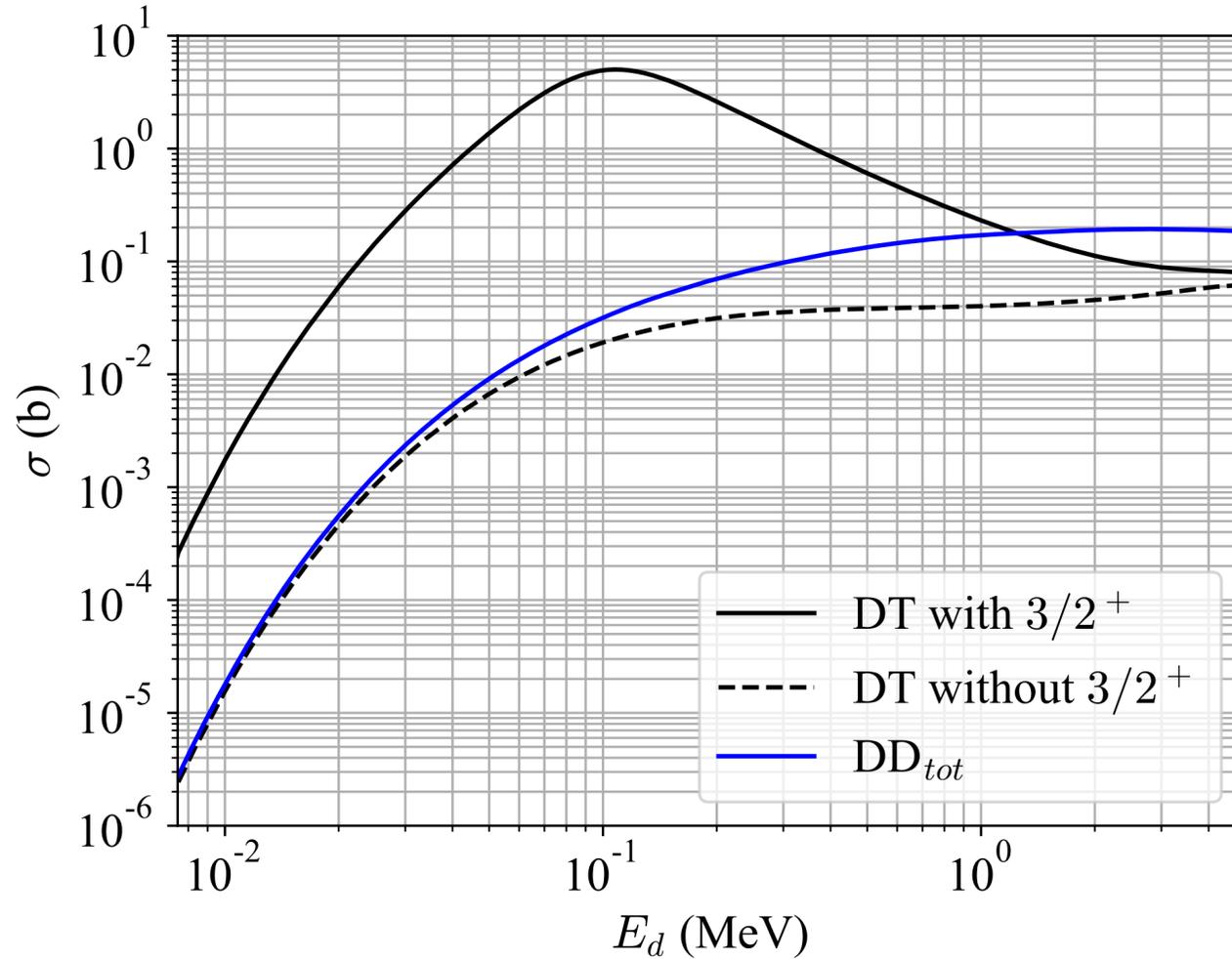
17.64 MeV energy released:
14.1 MeV neutron and 3.5 MeV alpha



897
d - ${}^6\text{Li}$

-1 877

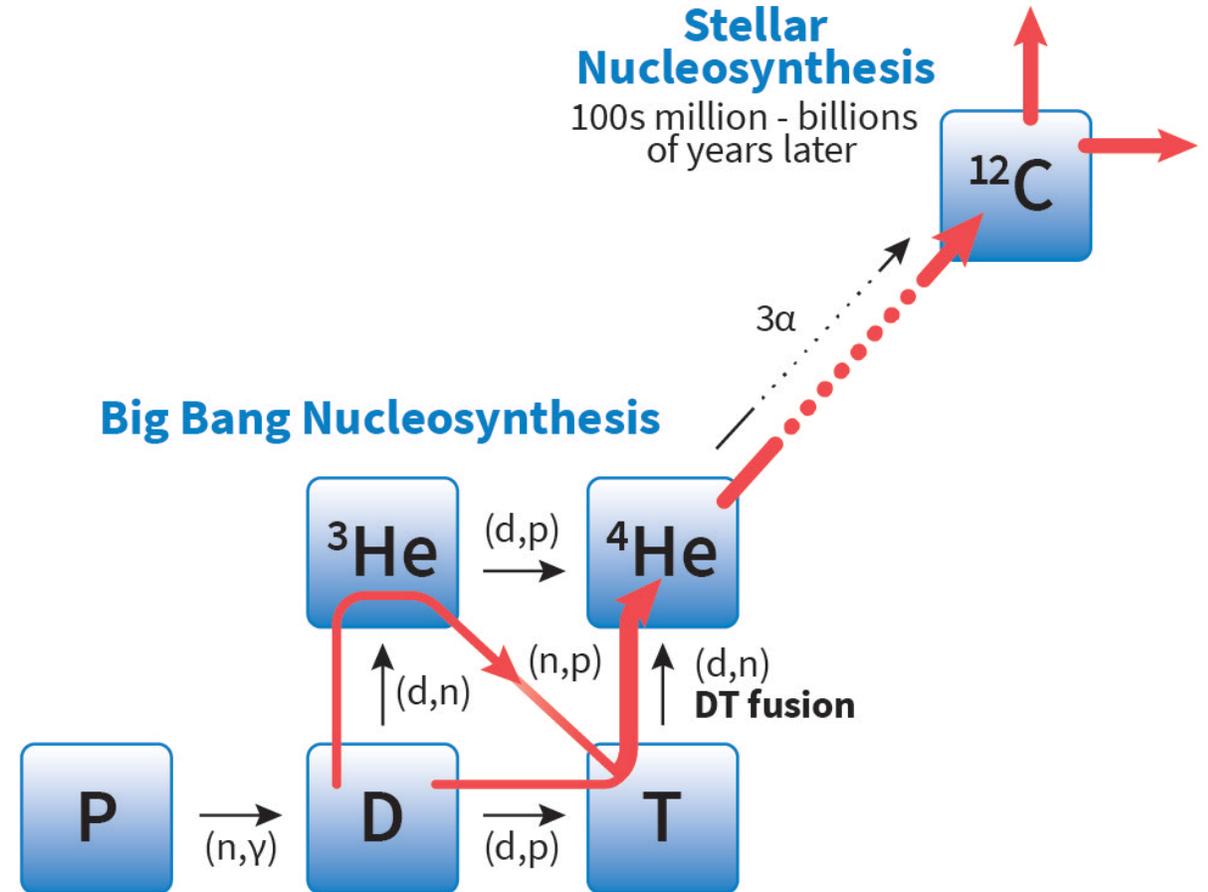
DT cross section would be 100x smaller, like DD, without the $3/2^+$ resonance



Mark Paris
LANL

Big bang Nucleosynthesis and DT fusion

- $D(T,n)\alpha$, enhanced by the $3/2^+$ resonance, is responsible for 99% of primordial ^4He
- The remaining 1% of primordial ^4He came from the $D(^3\text{He},p)^4\text{He}$ reaction, which benefits from the same mirror $3/2^+$ resonance but is suppressed because of the larger Coulomb repulsion between D and ^3He
- This helium became a source for the subsequent creation of $\geq 25\%$ of the carbon and other heavier elements and, thus, a substantial fraction of our human bodies



NCSMC calculation of the DT fusion

$$|\Psi\rangle = \sum_{\lambda} c_{\lambda} \left| \begin{array}{c} \text{He} \\ \text{5} \end{array}, \lambda \right\rangle + \int d\vec{r} u_{\nu_{DT}}(\vec{r}) \hat{A}_{DT} \left| \begin{array}{c} \text{D} \\ \text{T} \end{array}, \nu_{DT} \right\rangle + \int d\vec{r} u_{\nu_{n\alpha}}(\vec{r}) \hat{A}_{n\alpha} \left| \begin{array}{c} \text{n} \\ \alpha \end{array}, \nu_{n\alpha} \right\rangle$$

- 2x7 static ${}^5\text{He}$ eigenstates computed with the NCSM
- Continuous D-T(g.s.) cluster states (entrance channel)
 - Including positive-energy eigenstates of D to account for distortion
- Continuous n- ${}^4\text{He}$ (g.s.) cluster states (exit channel)
- Chiral NN+3N(500) interaction



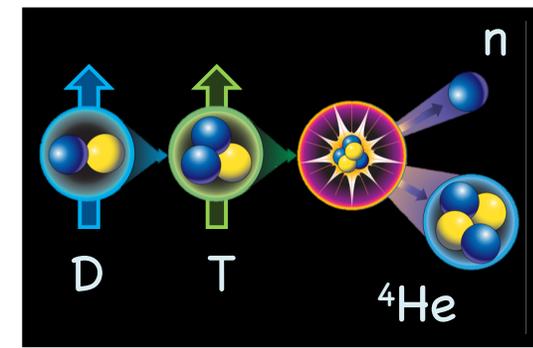
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<https://doi.org/10.1038/s41467-018-08052-8> OPEN

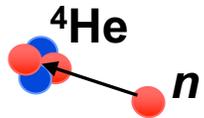
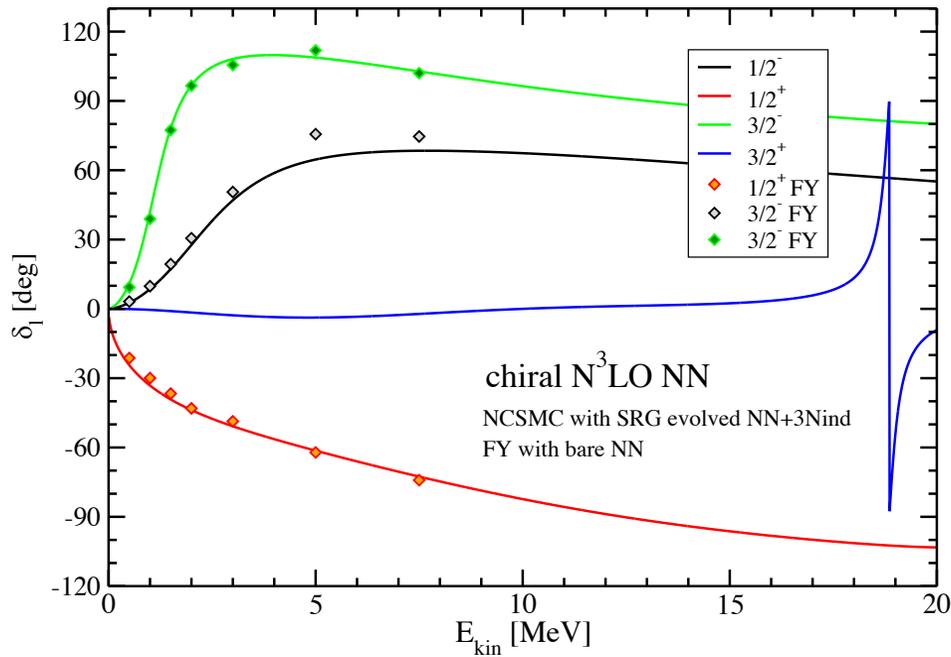
Ab initio predictions for polarized deuterium-tritium thermonuclear fusion

Guillaume Hupin^{1,2,3}, Sofia Quaglioni³ & Petr Navrátil⁴

n - ^4He scattering and $^3\text{H}+d$ fusion within NCSMC

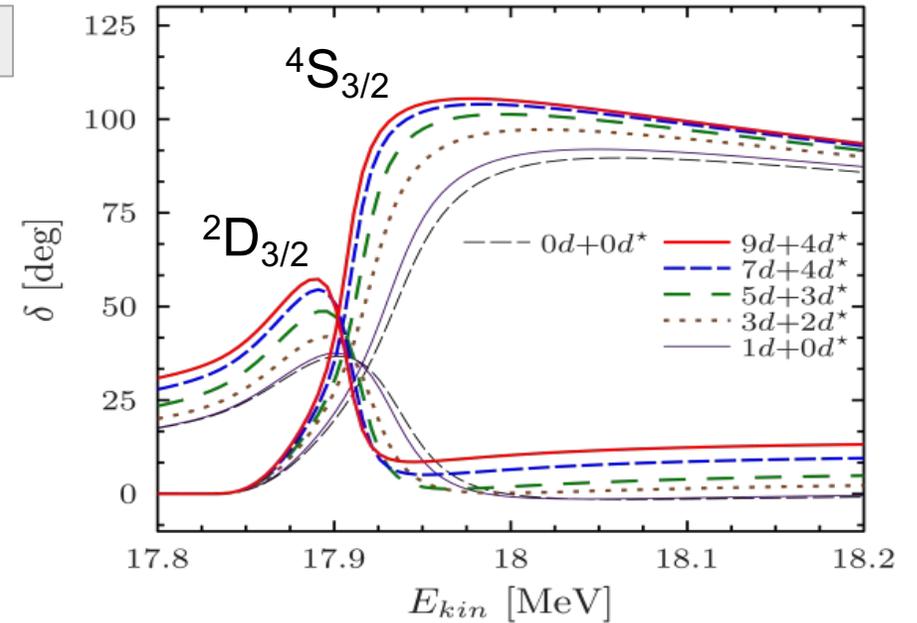


n - ^4He and d + ^3H scattering phase-shifts



$^4\text{He}+n$

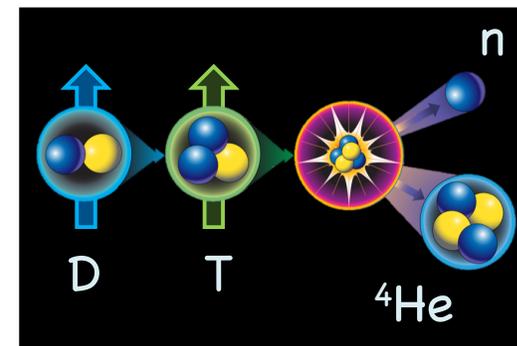
$^4\text{He}+n \rightarrow ^3\text{H}+d$



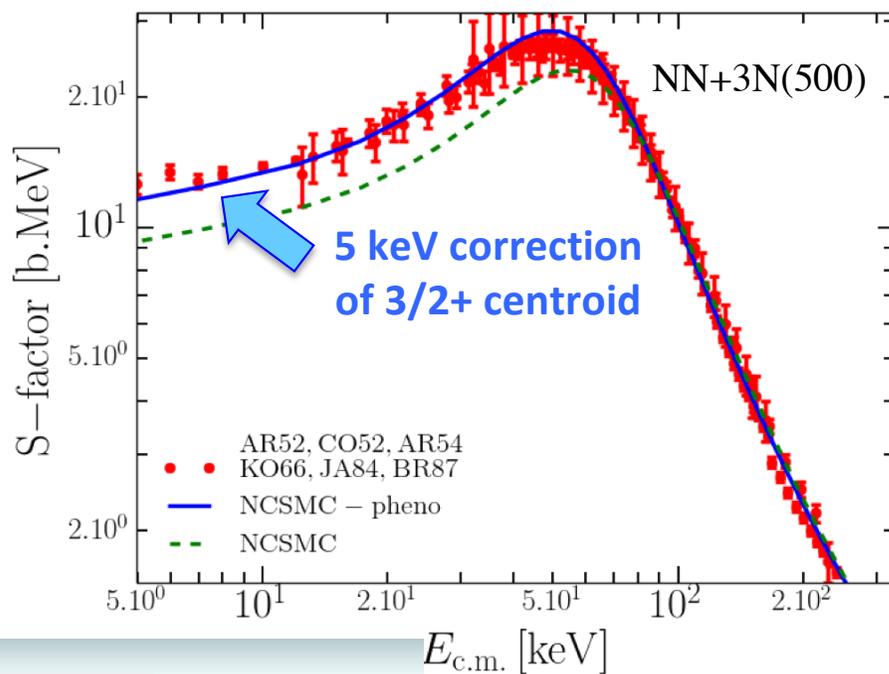
FY: Faddeev-Yakubovsky method - Rimantas Lazauskas

The d - ^3H fusion takes place through a transition of d + ^3H is S -wave to n + ^4He in D -wave: Importance of the **tensor** and **3N** force

$^3\text{H}(d,n)^4\text{He}$ with chiral NN+3N(500) interaction



Astrophysical S-factor



Fusion cross section

$$\sigma(E) = \frac{S(E)}{E} \exp\left(-\frac{2\pi Z_1 Z_2 e^2}{\hbar \sqrt{2E/m}}\right)$$

Astrophysical S-factor: nuclear contribution

'Coulomb' Contribution (tunneling)

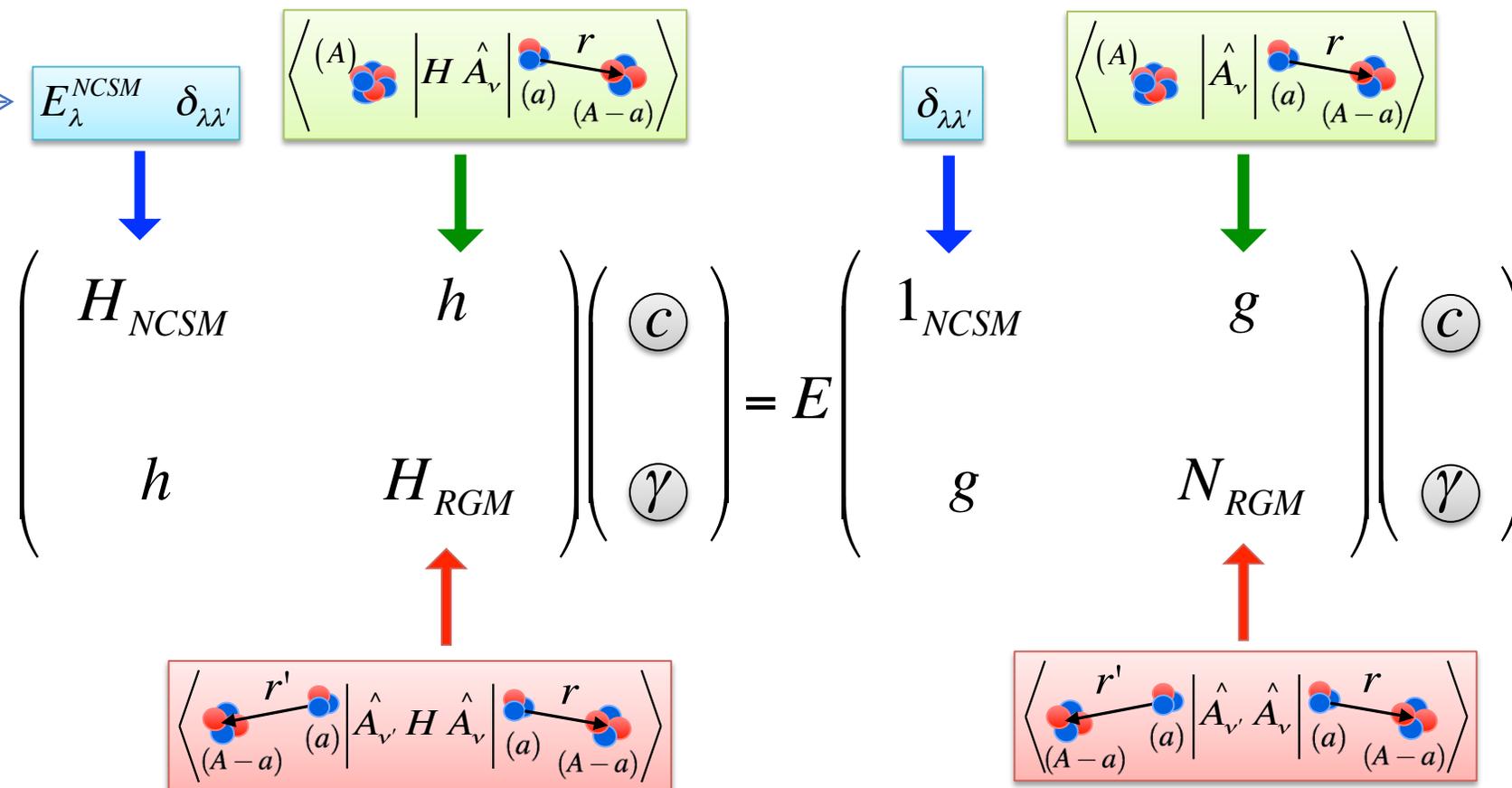


NCSMC phenomenology

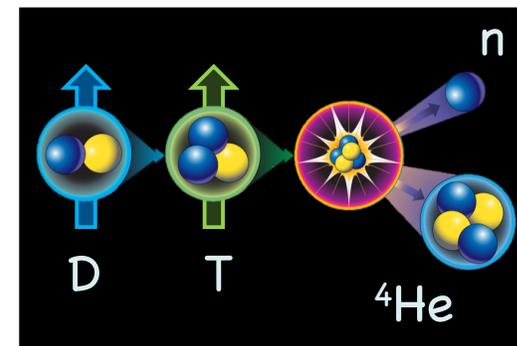
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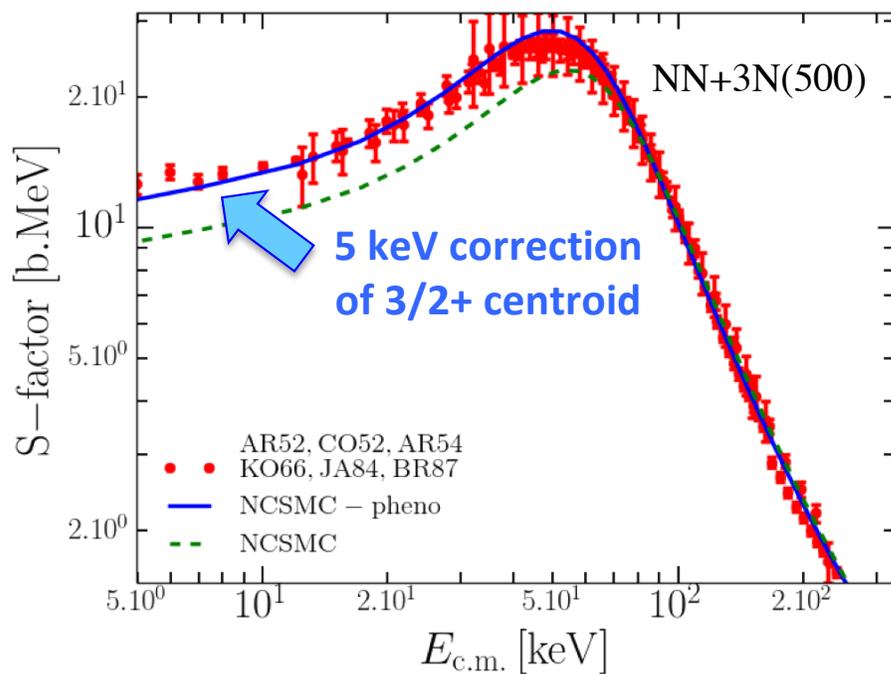
E_{λ}^{NCSM} energies treated as adjustable parameters



$^3\text{H}(d,n)^4\text{He}$ with chiral NN+3N(500) interaction



Astrophysical S-factor



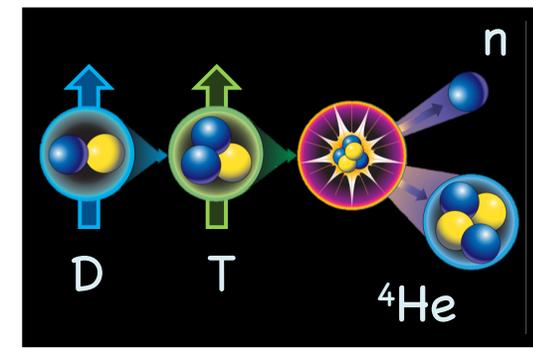
Fusion cross section

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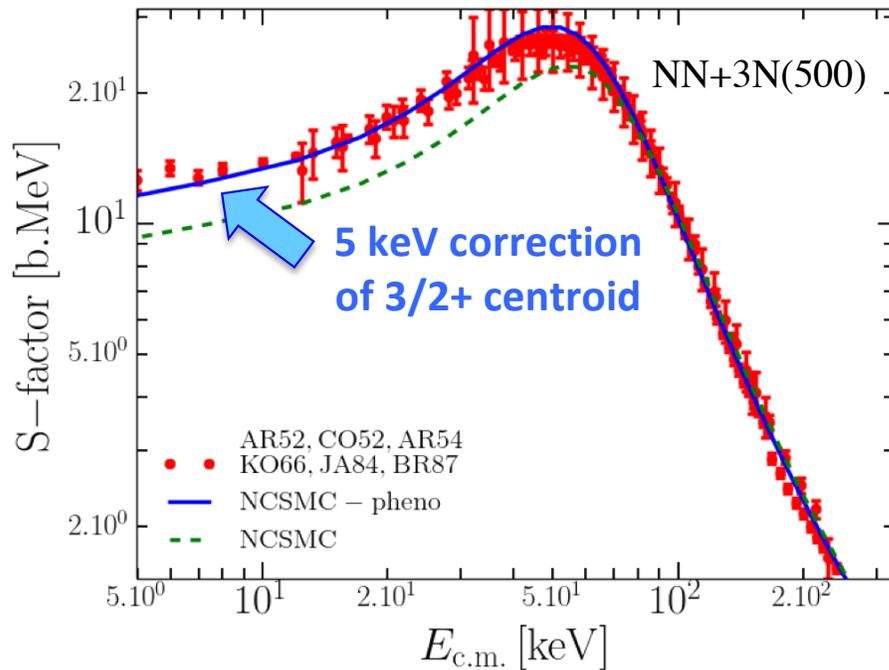
Astrophysical S-factor: nuclear contribution

'Coulomb' Contribution (tunneling)

${}^3\text{H}(d,n){}^4\text{He}$ with chiral NN+3N(500) interaction



Astrophysical S-factor



Assuming the fusion proceeds only in S-wave with spins of D and T completely aligned: Polarized cross section 50% higher than unpolarized

- While the DT fusion rate has been measured extensively, a fundamental understanding of the process is still missing
- Very little is known experimentally of how the polarization of the reactants' spins affects the reaction

$$\sigma_{unpol} = \sum_J \frac{2J+1}{(2I_D+1)(2I_T+1)} \sigma_J$$

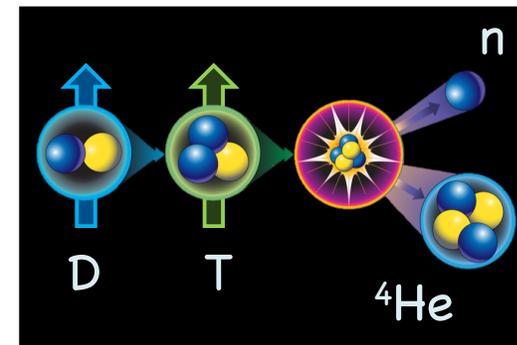
$$\approx \frac{1}{3} \cancel{\sigma_{\frac{1}{2}}} + \frac{2}{3} \sigma_{\frac{3}{2}}$$



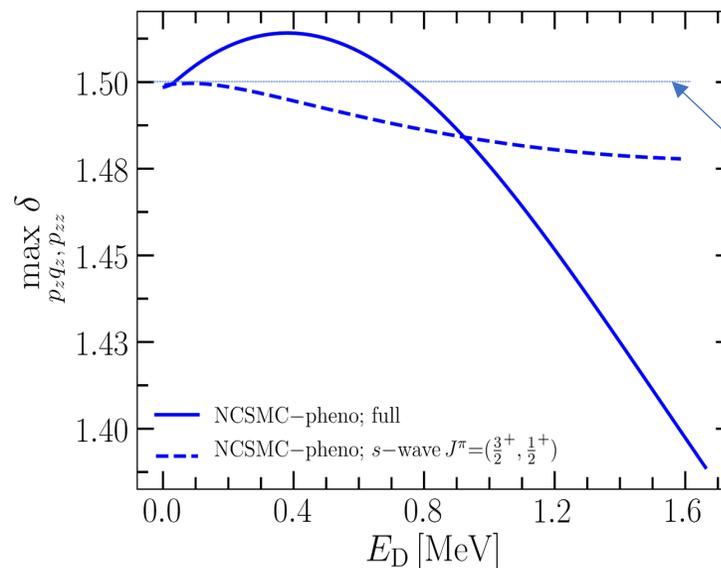
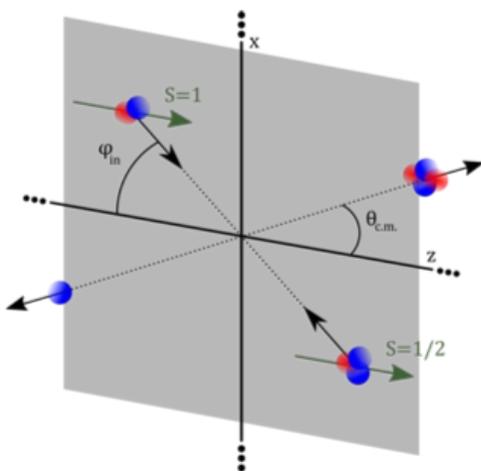
$$\sigma_{pol} \approx 1.5 \sigma_{unpol}$$

$^3\text{H}(d,n)^4\text{He}$ with chiral NN+3N(500) interaction

Polarized fusion



$$\frac{\partial \sigma_{pol}}{\partial \Omega_{c.m.}}(\theta_{c.m.}) = \frac{\partial \sigma_{unpol}}{\partial \Omega_{c.m.}}(\theta_{c.m.}) \left(1 + \frac{1}{2} p_{zz} A_{zz}^{(b)}(\theta_{c.m.}) + \frac{3}{2} p_z q_z C_{z,z}(\theta_{c.m.}) \right)$$



$$\sigma_{unpol} = \sum_J \frac{2J+1}{(2I_D+1)(2I_T+1)} \sigma_J$$

$$\approx \frac{1}{3} \sigma_{\frac{1}{2}} + \frac{2}{3} \sigma_{\frac{3}{2}}$$

↓

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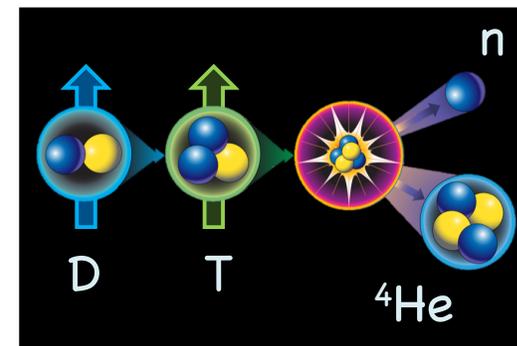
Ab initio predictions for polarized deuterium-tritium thermonuclear fusion

Guillaume Hupin^{1,2,3}, Sofia Quaglioni³ & Petr Navrátil⁴

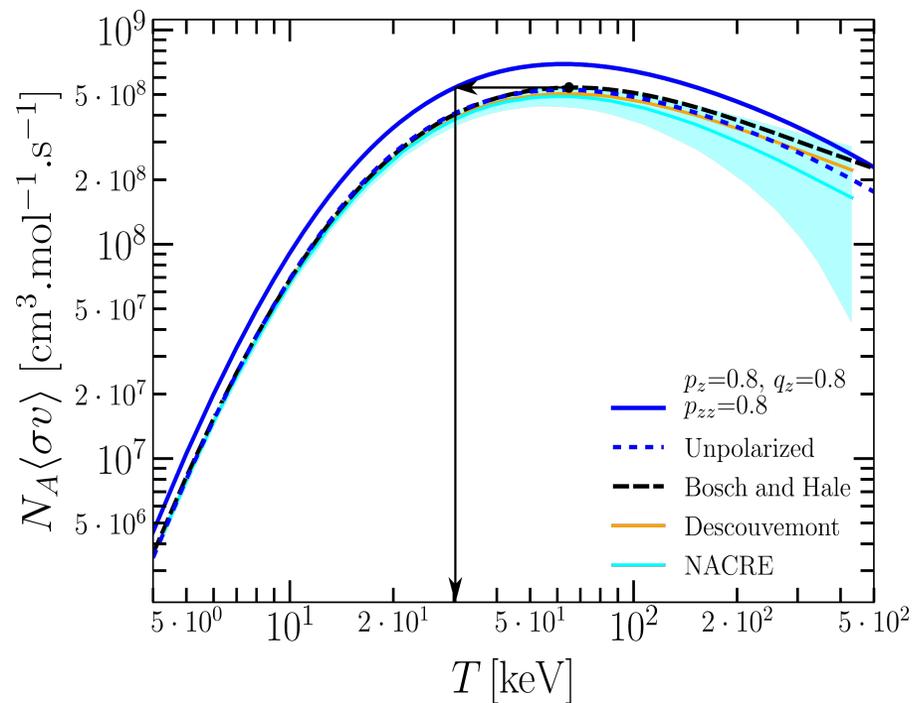
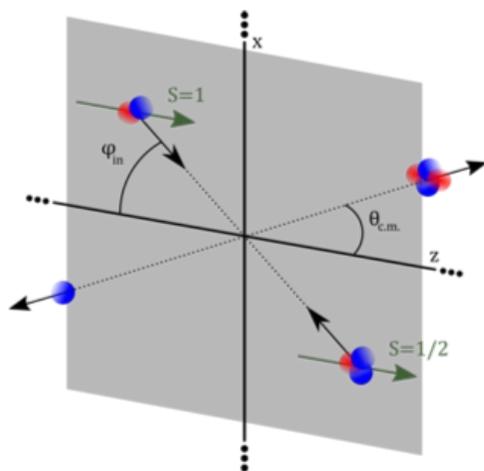
NCSMC calculation demonstrates impact of partial waves with $l > 0$ as well as the contribution of $l = 0$ $J^\pi = \frac{1}{2}^+$ channel

$^3\text{H}(d,n)^4\text{He}$ with chiral NN+3N(500) interaction

Polarized fusion



$$\frac{\partial \sigma_{pol}}{\partial \Omega_{c.m.}}(\theta_{c.m.}) = \frac{\partial \sigma_{unpol}}{\partial \Omega_{c.m.}}(\theta_{c.m.}) \left(1 + \frac{1}{2} p_{zz} A_{zz}^{(b)}(\theta_{c.m.}) + \frac{3}{2} p_z q_z C_{z,z}(\theta_{c.m.}) \right)$$



$$\langle \sigma v \rangle = \sqrt{\frac{8}{\pi \mu (k_b T)^3}} \int_0^\infty S(E) \exp\left(-\frac{E}{k_b T} - \sqrt{\frac{E_g}{E}}\right) dE,$$

For a realistic 80% polarization, reaction rate increases by ~32% or the same rate at ~45% lower temperature



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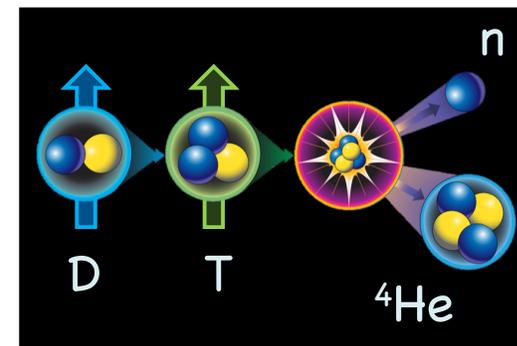
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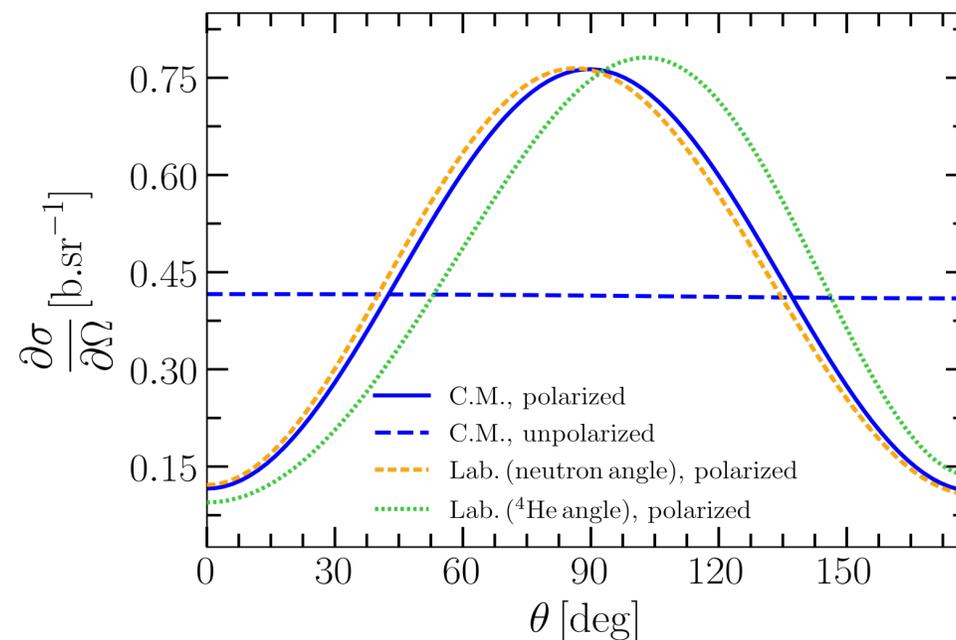
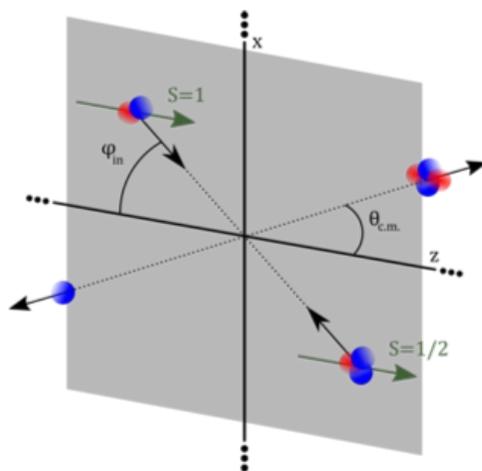
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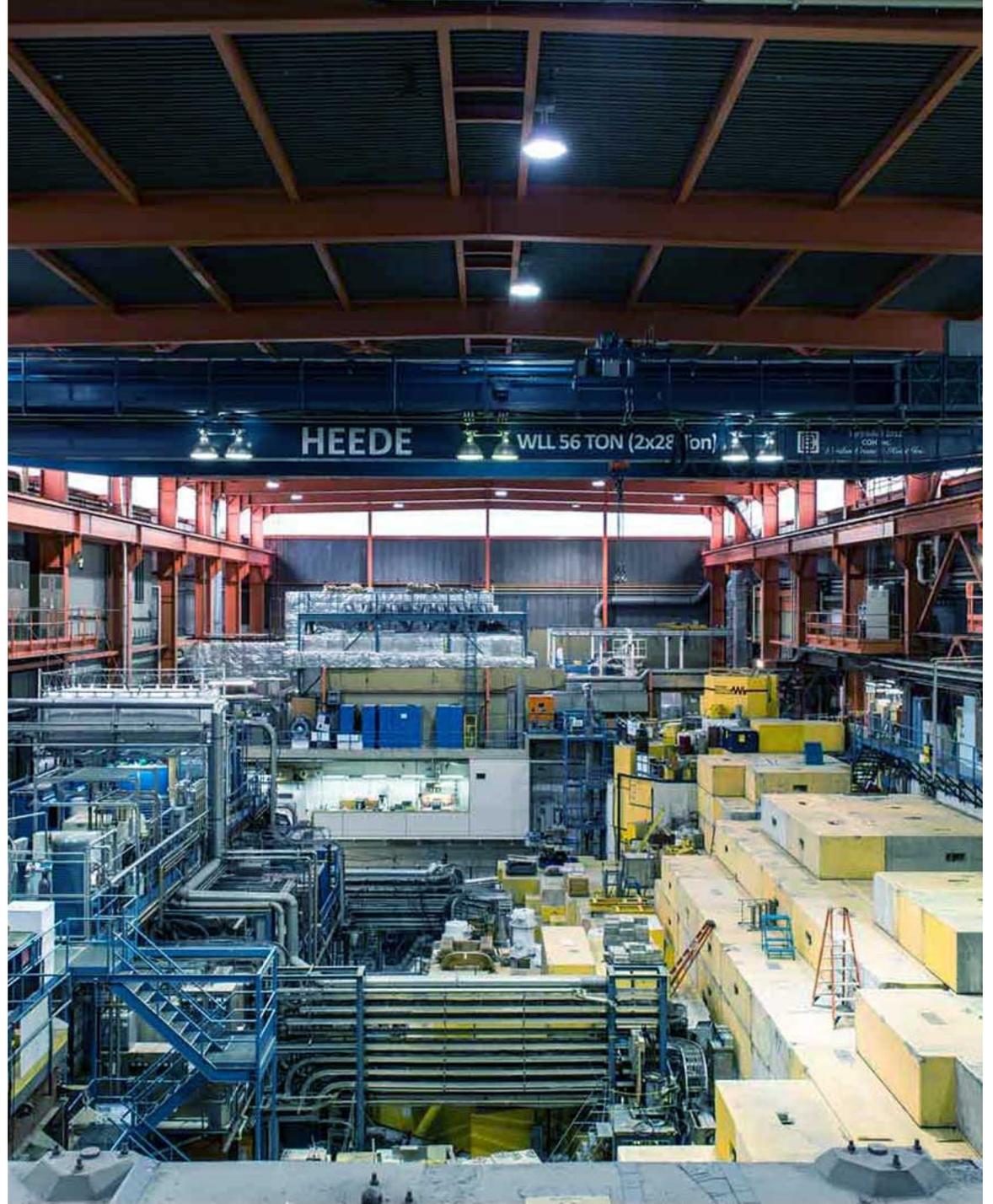


For a realistic 80% polarization, outgoing neutrons and alphas emitted dominantly in the perpendicular direction to the magnetic field



S-wave resonance close to the ${}^6\text{He}+p$
threshold in ${}^7\text{Li}$

2023-10-26



⁷Be and ⁷Li nuclei within the no-core shell model with continuum

 Matteo Vorabbi^{*} and Petr Navrátil[†]

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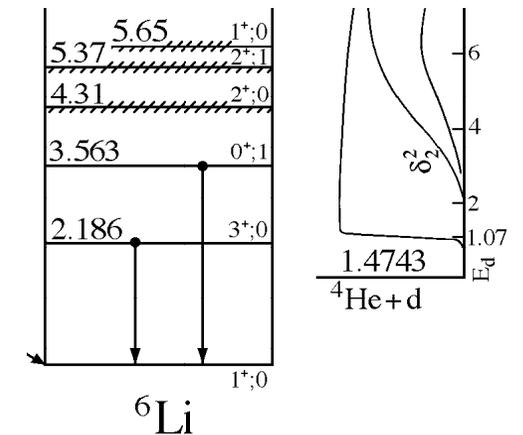
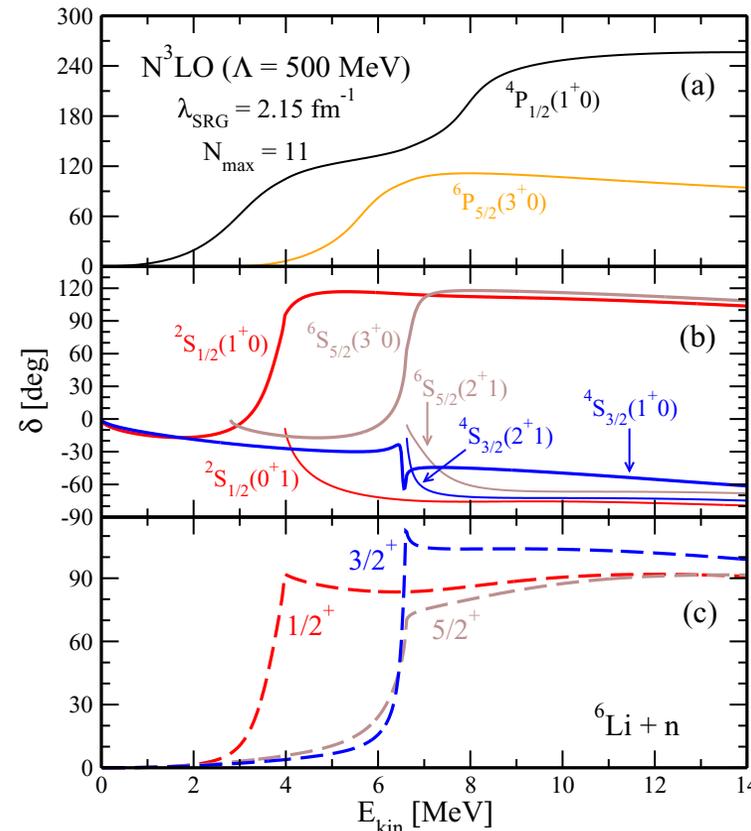
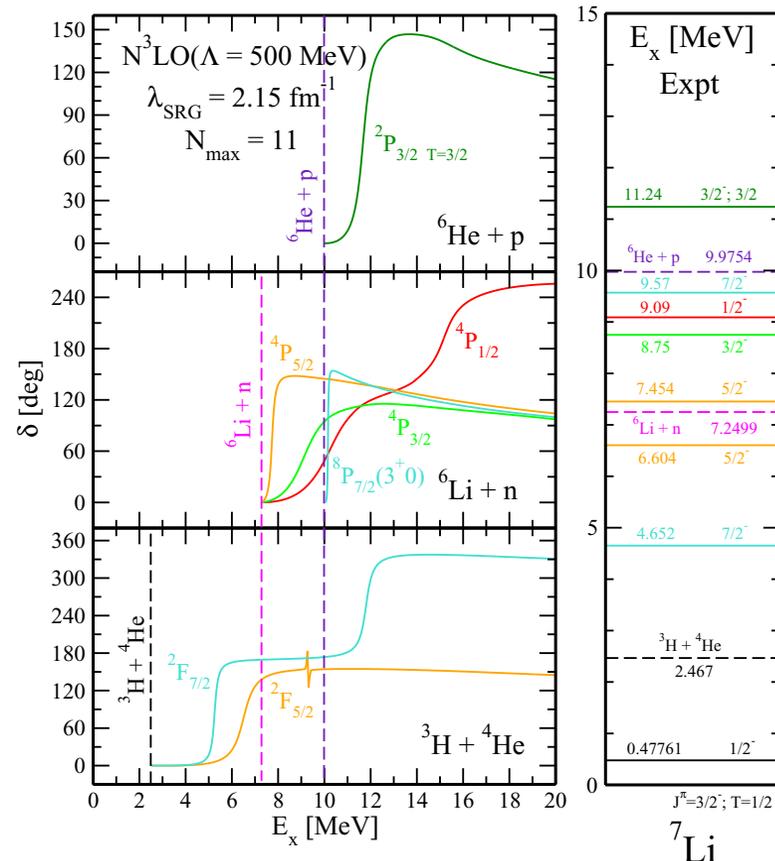
 Guillaume Hupin[‡]

Institut de Physique Nucléaire, CNRS/IN2P3, Université Paris-Sud, Université Paris-Saclay, F-91406, Orsay, France

28

S-wave resonance close to the threshold of ⁶He+p?

- NCSMC study of ⁷Li and ⁷Be nuclei using all binary mass partitions
 - Known resonances reproduced
 - Prediction of several new resonances of both parities



⁷Be and ⁷Li nuclei within the no-core shell model with continuum

Matteo Vorabbi^{*} and Petr Navrátil[†]

TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia V6T 2A3, Canada

Sofia Quaglioni

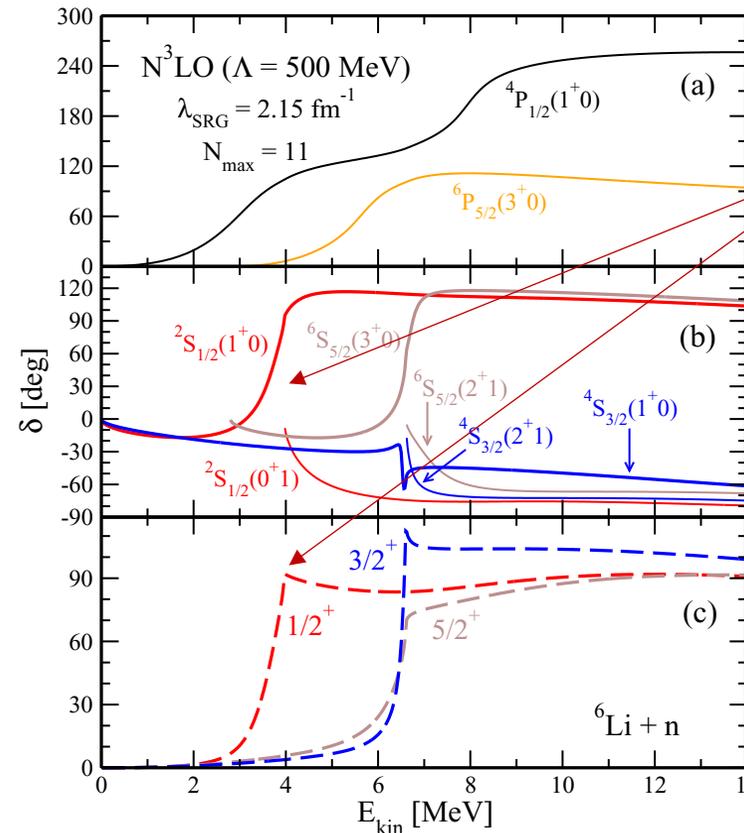
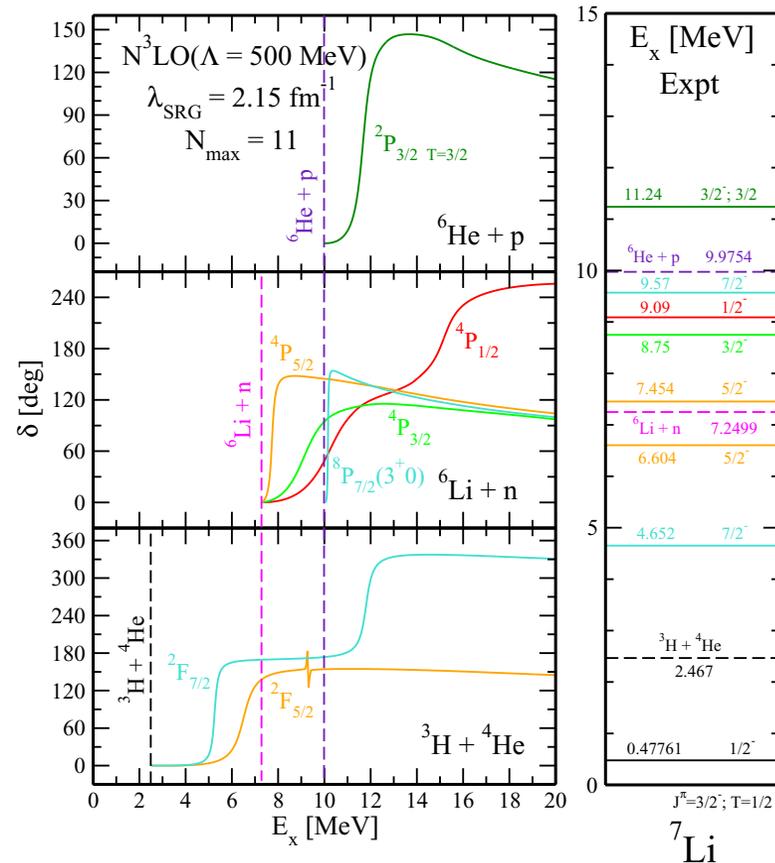
Lawrence Livermore National Laboratory, P. O. Box 808, L-414, Livermore, California 94551, USA

Guillaume Hupin[‡]

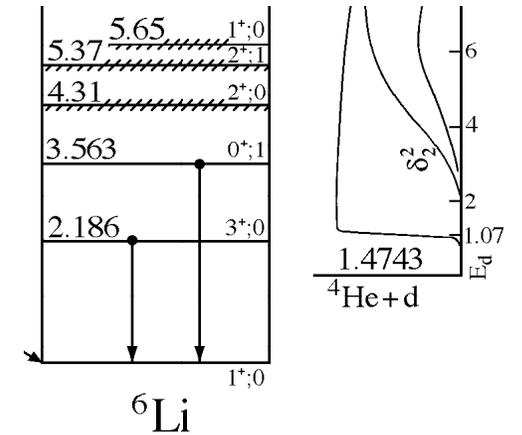
Institut de Physique Nucléaire, CNRS/IN2P3, Université Paris-Sud, Université Paris-Saclay, F-91406, Orsay, France

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S-wave resonance



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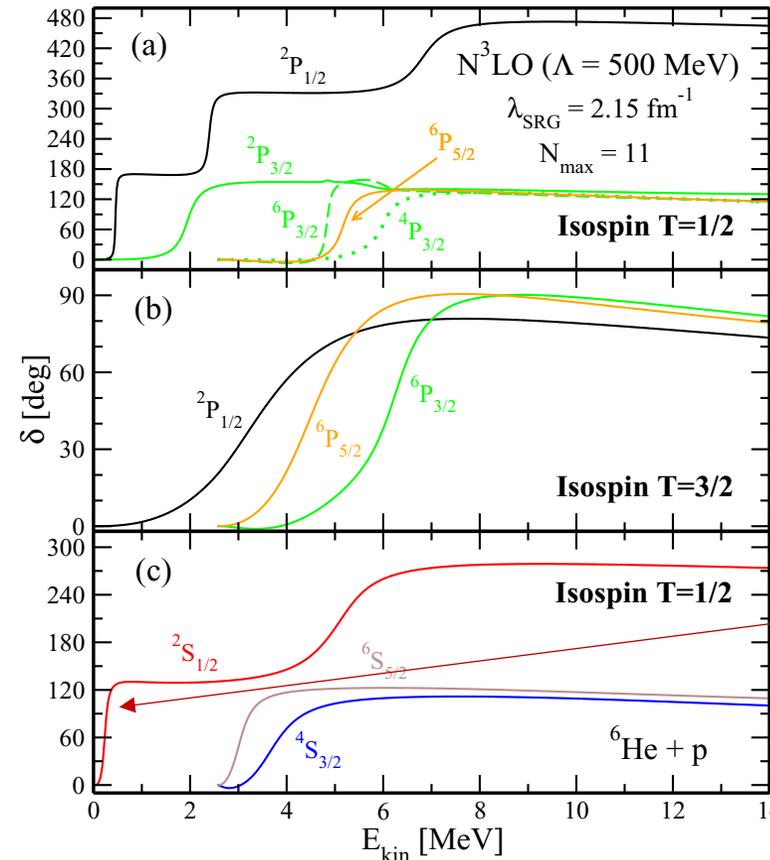
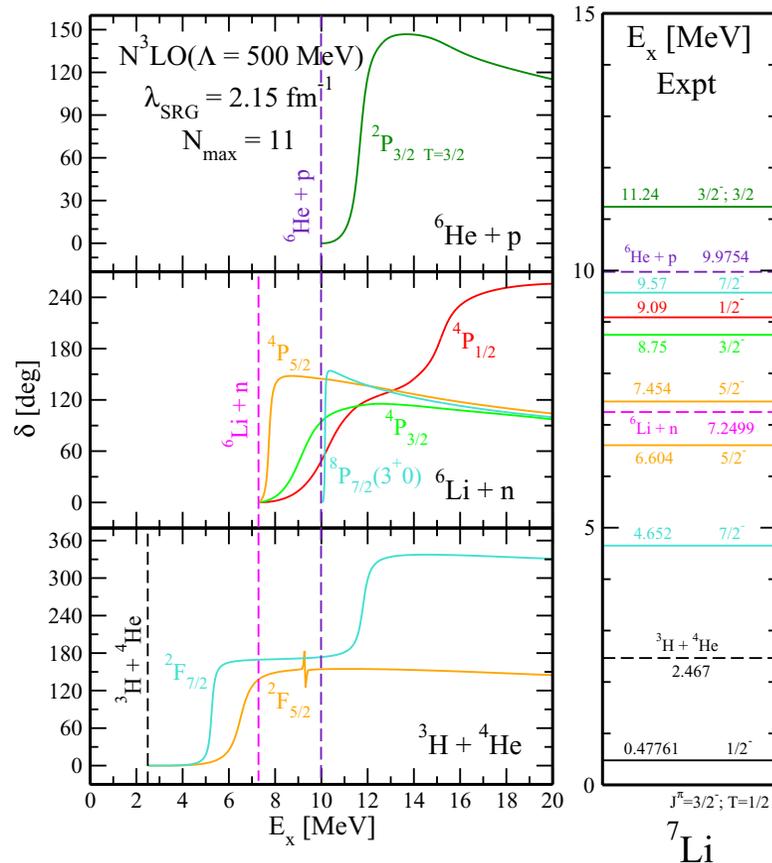
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S-wave resonance close to the threshold of ⁶He+p?

- NCSMC study of ⁷Li and ⁷Be nuclei using all binary mass partitions
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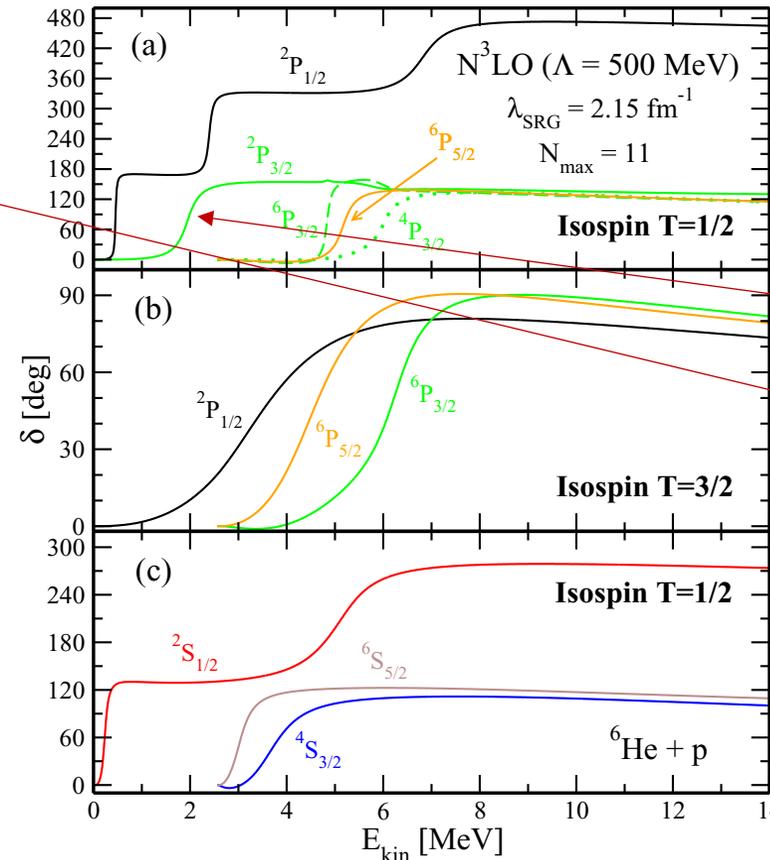
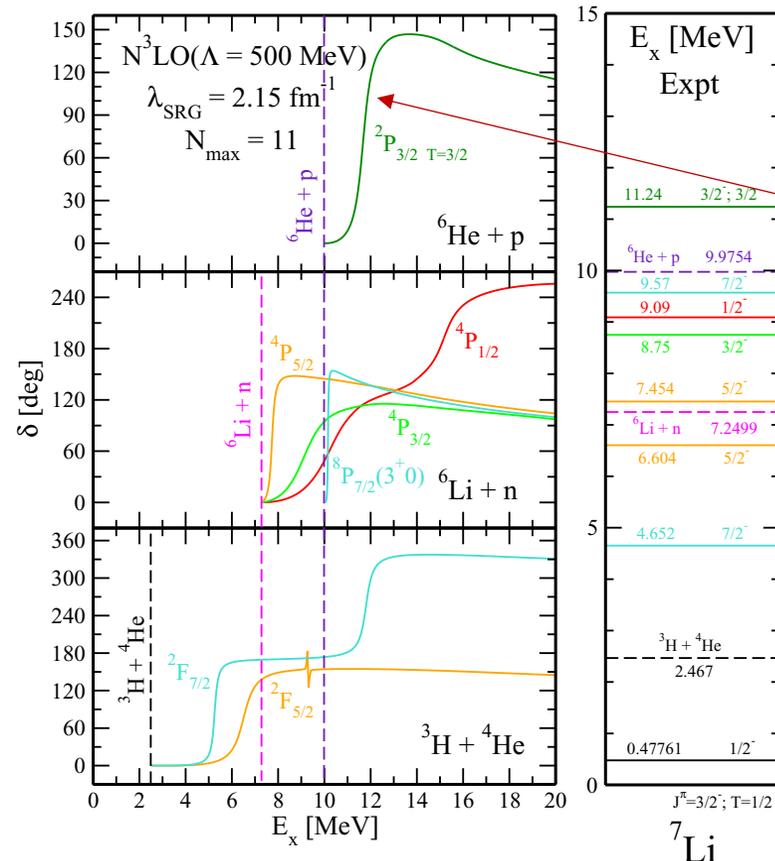


S-wave resonance predicted at low energy in ⁶He+p scattering with possible astrophysics implications.

S-wave resonance

S-wave resonance close to the threshold of ⁶He+p?

- NCSMC study of ⁷Li and ⁷Be nuclei using all binary mass partitions
 - Known resonances reproduced
 - Prediction of several new resonances of both parities



⁶He(d,n)⁷Li* → ⁶He+p
 experiment at Texas A&M
 University Cyclotron Institute

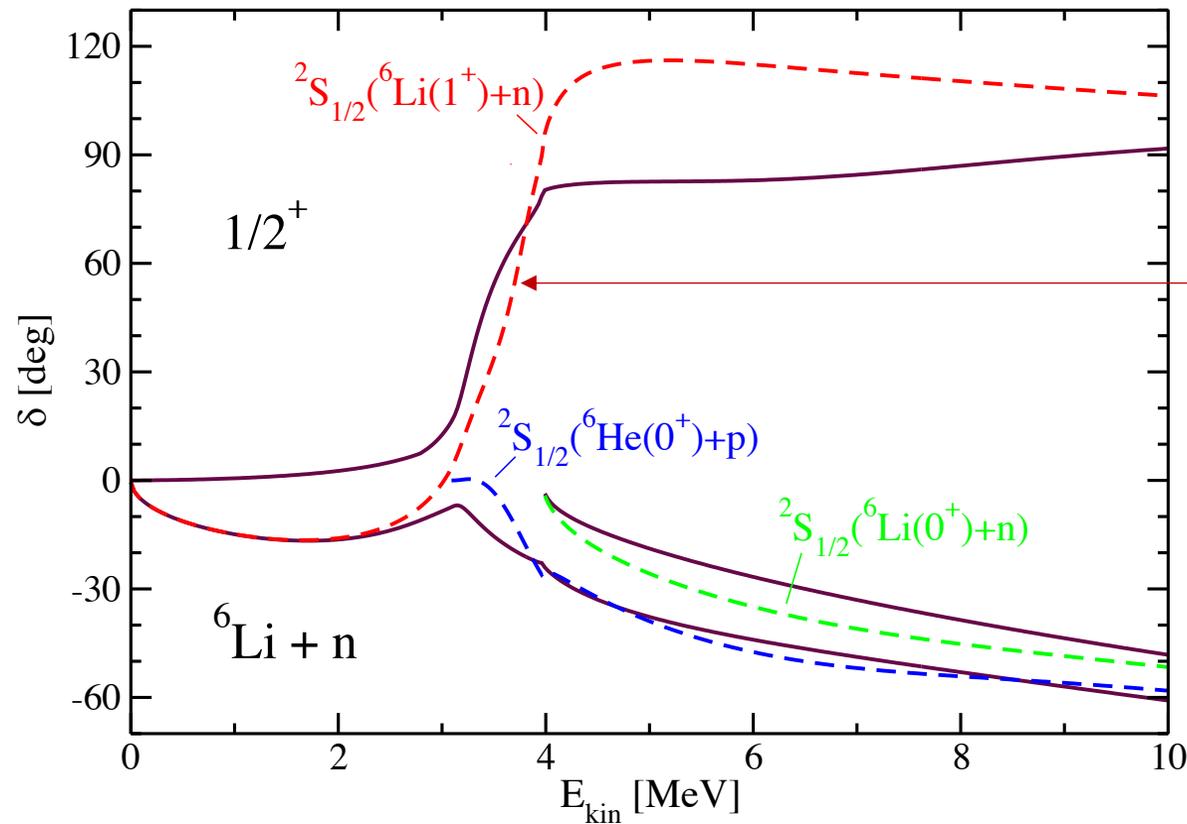
Near threshold resonance not found

3/2- T=1/2 anti-analog
 resonance observed just above
 3/2- T=3/2

Weakness of the calculation - **mass partitions not coupled**:
 The resonance appears in both ⁶Li+n and ⁶He+p. Might be below the ⁶He+p threshold or might decay by charge exchange ⁶He(p,n)⁶Li(gs) ...or might be dissolved in d+n+⁴He continuum (not included)

${}^7\text{Li}$ structure: Coupling of different mass partitions in NCSMC in progress

- ${}^6\text{Li}+n$ and ${}^6\text{He}+p$ coupled calculations



S-wave resonance just above the ${}^6\text{He}+p$ threshold. However, it is in the ${}^6\text{Li}(1^+)+n$ channel; the ${}^6\text{He}(0^+)+p$ S-wave phase shift decreasing similarly as ${}^6\text{Li}(0^+)+n$.

Explains non-observation in the ${}^6\text{He}(d,n){}^7\text{Li}^*$ → ${}^6\text{He}+p$ Texas A&M experiment

PHYSICAL REVIEW C **107**, L061303 (2023)

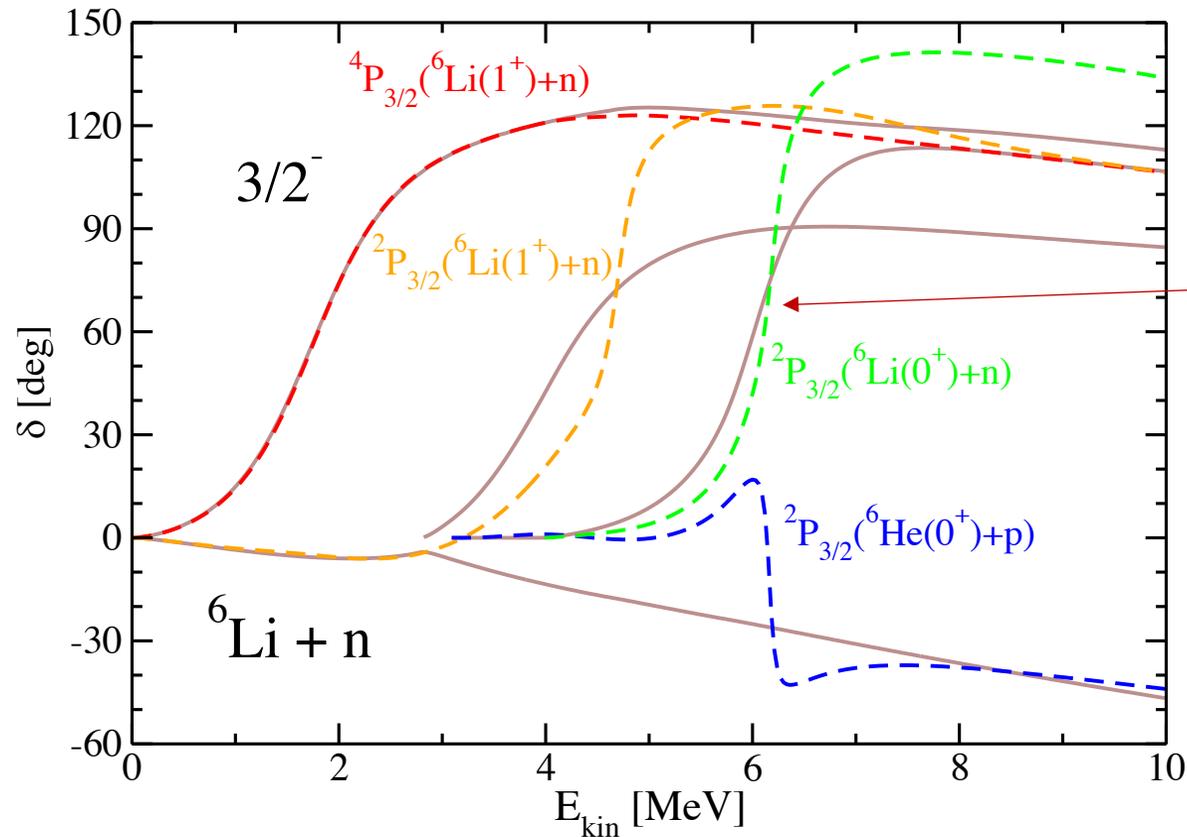
Letter

Search for an s-wave resonance in ${}^7\text{Li}$ just above the proton-decay threshold

N. Dronchi^{1,*}, J. Berkman², R. J. Charity², J. M. Elson², L. G. Sobotka^{1,2}, A. G. Thomas², A. Saastamoinen³, M. Barbui³, J. Bishop³, C. E. Parker³, B. T. Roeder³, G. V. Rogachev^{3,4,5}, D. P. Scriven^{3,4}, S. T. Marley⁶ and R. M. Shaffer⁶

${}^7\text{Li}$ structure: Coupling of different mass partitions in NCSMC in progress

- ${}^6\text{Li}+n$ and ${}^6\text{He}+p$ coupled calculations



$3/2^-$ T=1/2 anti-analog resonance with contributions from both the ${}^6\text{Li}(0^+)+n$ and the ${}^6\text{He}(0^+)+p$ P-waves.

Consistent with the observation in the ${}^6\text{He}(d,n){}^7\text{Li}^* \rightarrow {}^6\text{He}+p$ Texas A&M experiment

PHYSICAL REVIEW C **107**, L061303 (2023)

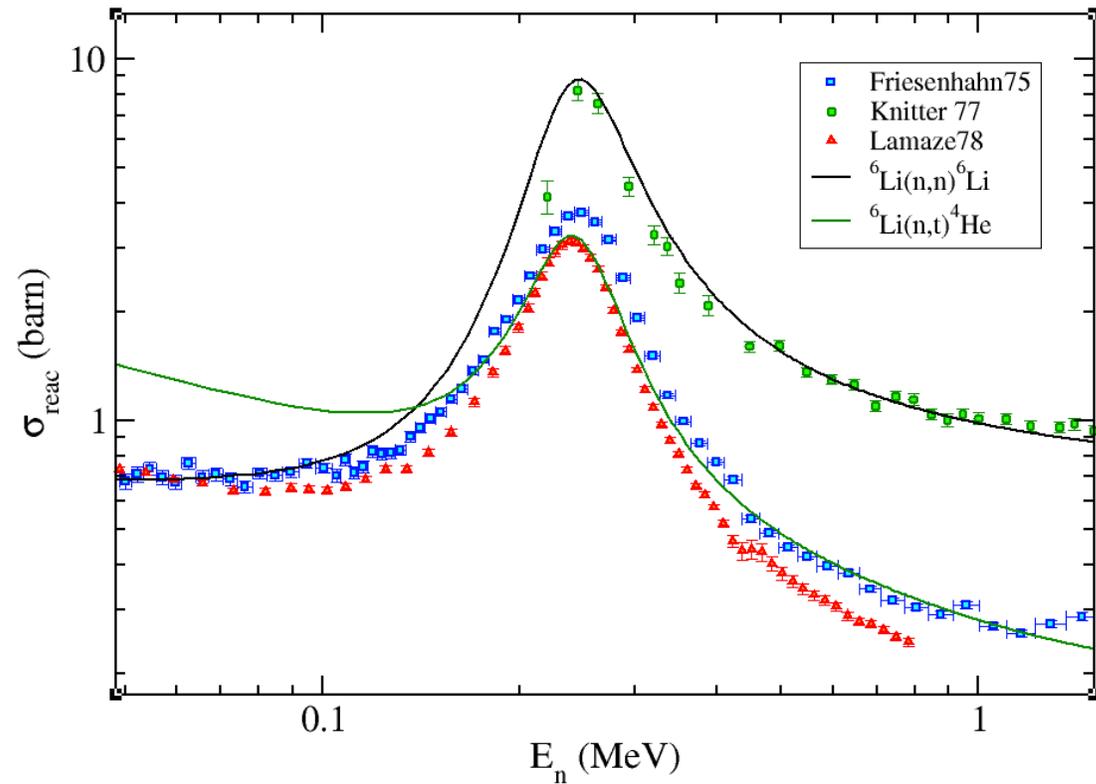
Letter

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${}^7\text{Li}$ structure: Coupling of different mass partitions in NCSMC in progress

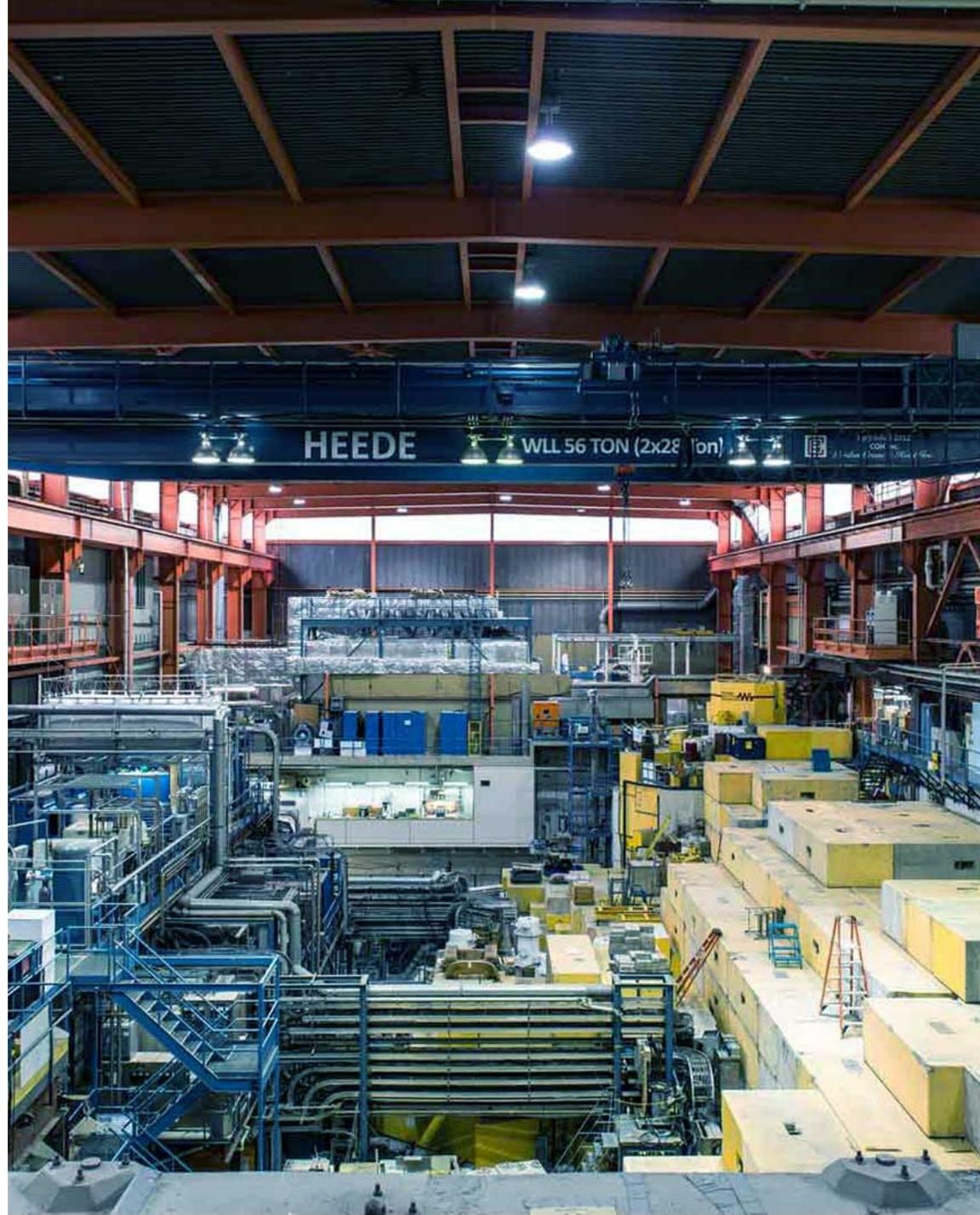
- ${}^4\text{He}+{}^3\text{H}$ and ${}^6\text{Li}+n$ coupled calculations
- First results for ${}^6\text{Li}(n,t){}^4\text{He}$



Next to do: ${}^4\text{He}+{}^3\text{H}$ and ${}^6\text{Li}+n$ and ${}^6\text{He}+p$ coupled calculations

Parity inversion in ^{11}Be ground state

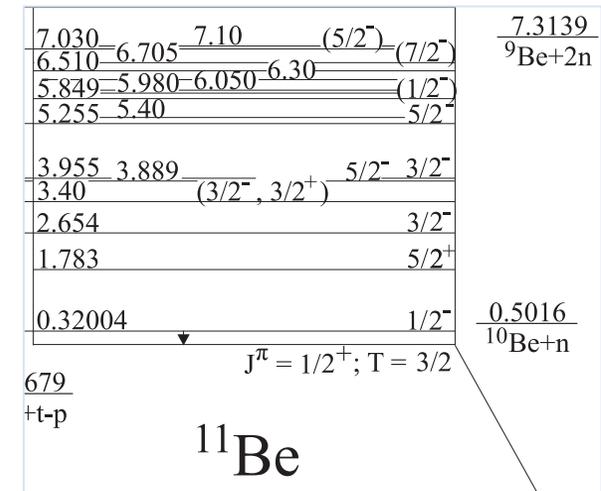
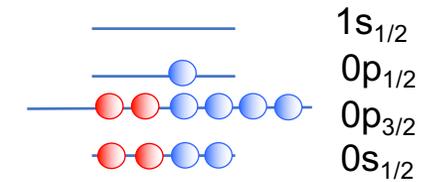
2023-10-26



Neutron-rich halo nucleus ^{11}Be

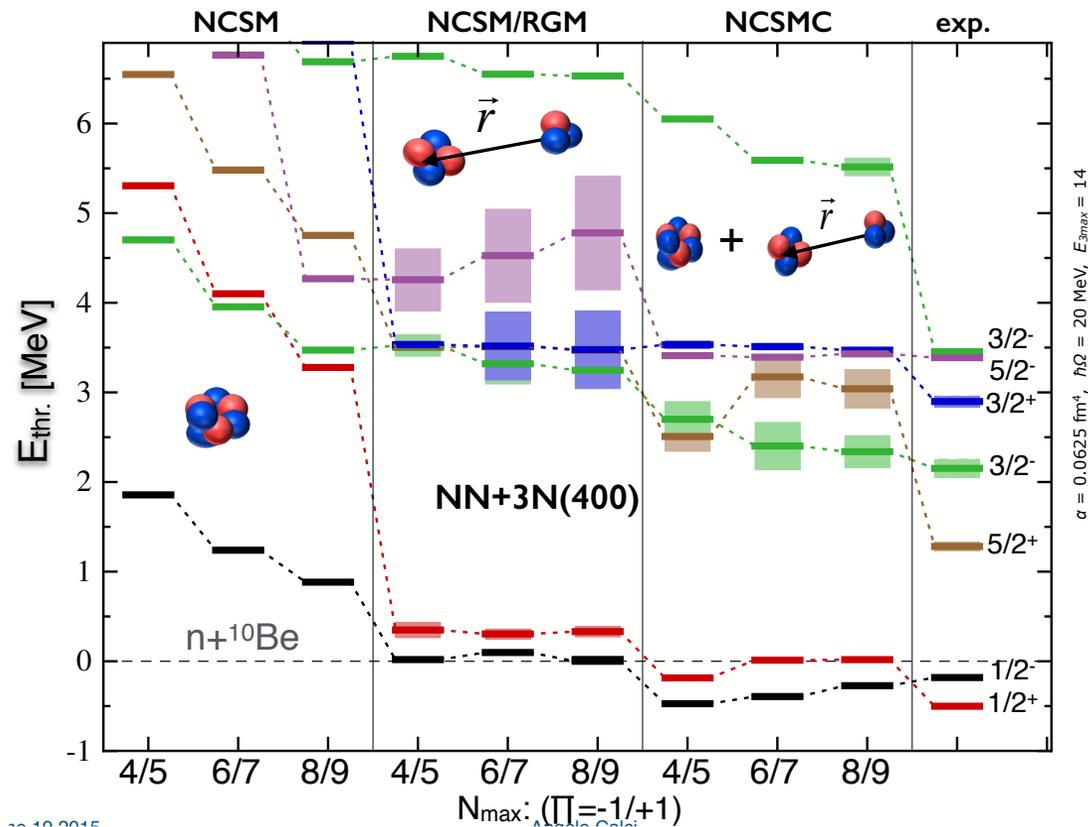
- $Z=4, N=7$
 - In the shell model picture g.s. expected to be $J^\pi=1/2^-$
 - $Z=6, N=7$ ^{13}C and $Z=8, N=7$ ^{15}O have $J^\pi=1/2^-$ g.s.
 - In reality, ^{11}Be g.s. is $J^\pi=1/2^+$ - parity inversion
 - Very weakly bound: $E_{\text{th}}=-0.5$ MeV
 - Halo state – dominated by $^{10}\text{Be-n}$ in the S-wave
 - The $1/2^-$ state also bound – only by 180 keV

- Can we describe ^{11}Be in *ab initio* calculations?
 - Continuum must be included
 - Does the 3N interaction play a role in the parity inversion?



Structure of ^{11}Be from chiral NN+3N forces

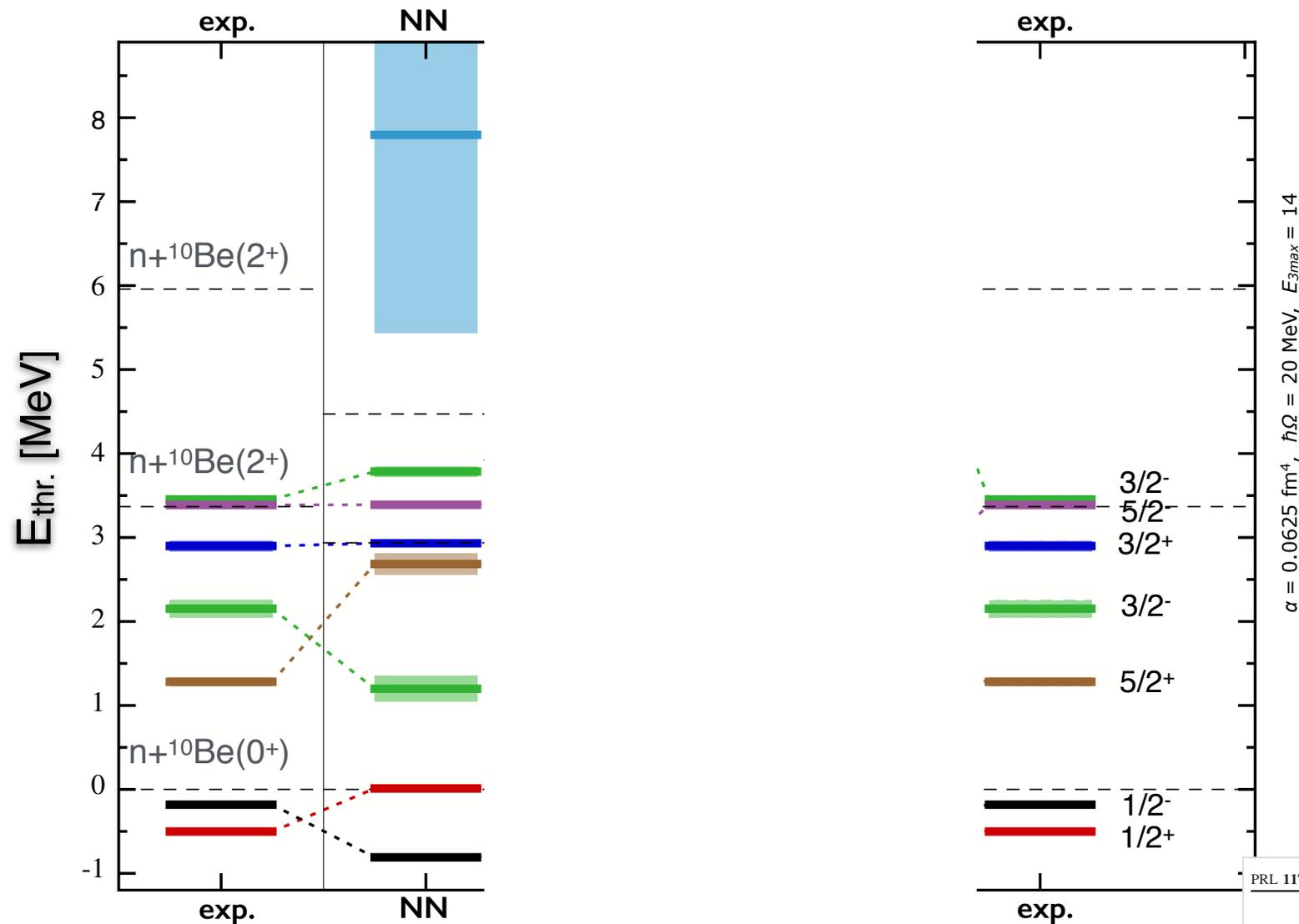
- NCSMC calculations **including chiral 3N** (NN $N^3\text{LO}+N^2\text{LO}$ 3N(400), $N^2\text{LO}_{\text{sat}}$, NN $N^4\text{LO}+3N_{\text{Inl}}$)
 - $n-^{10}\text{Be} + ^{11}\text{Be}$
 - ^{10}Be : 0^+ , 2^+ , 2^+ NCSM eigenstates
 - ^{11}Be : ≥ 6 $\pi = -1$ and ≥ 3 $\pi = +1$ NCSM eigenstates



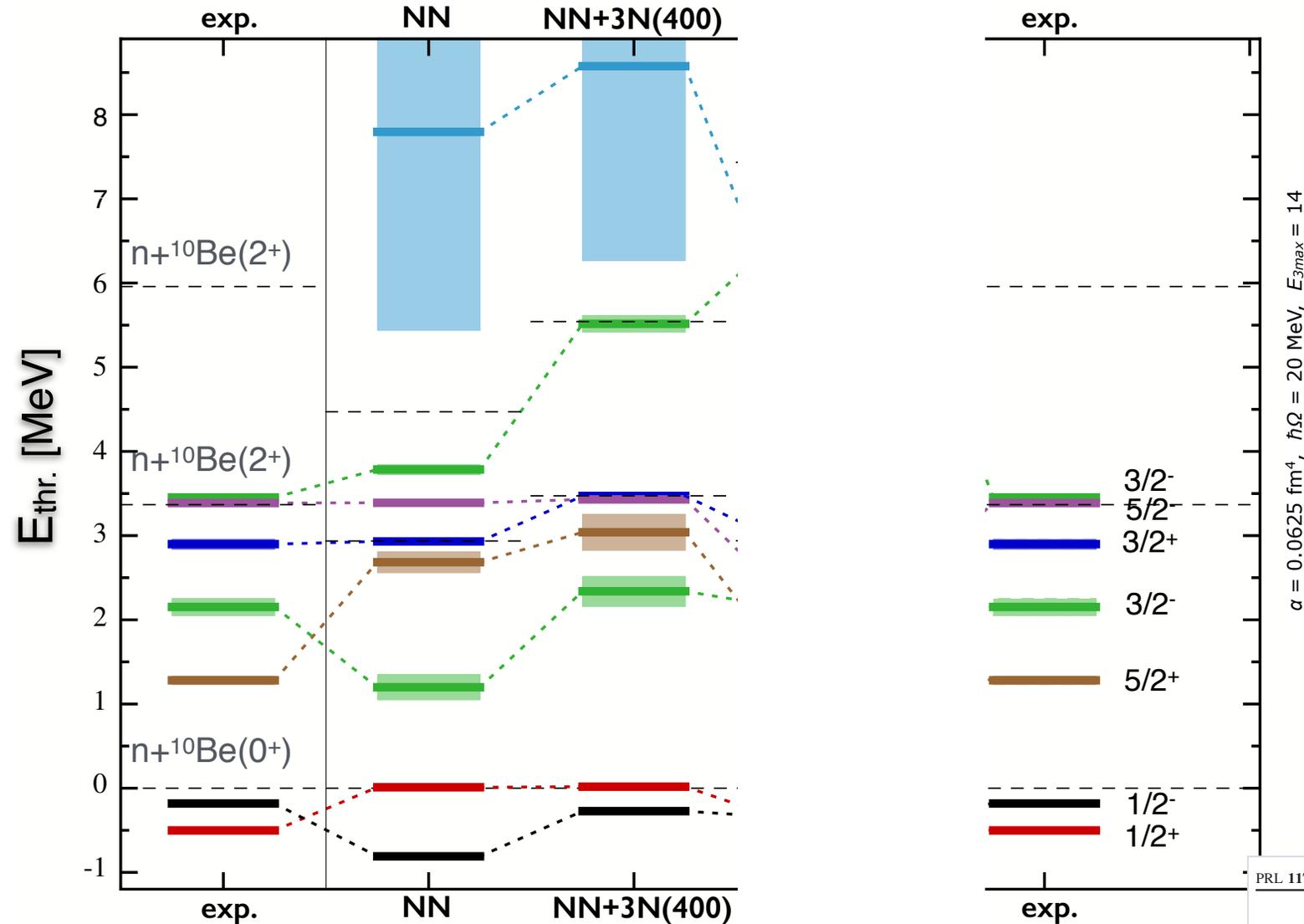
7.030	6.705	7.10	(5/2 ⁻)	7.3139
6.510	6.705	6.30	(7/2 ⁻)	$^{9}\text{Be}+2n$
5.849	5.980	6.050	(1/2 ⁻)	
5.255	5.40		5/2 ⁻	
3.955	3.889		5/2 ⁻ 3/2 ⁻	
3.40			(3/2 ⁻ , 3/2 ⁺)	
2.654			3/2 ⁻	
1.783			5/2 ⁺	
0.32004			1/2 ⁻	0.5016
				$^{10}\text{Be}+n$
679			$J^{\pi} = 1/2^{+}; T = 3/2$	
$^{+}t-p$				

^{11}Be

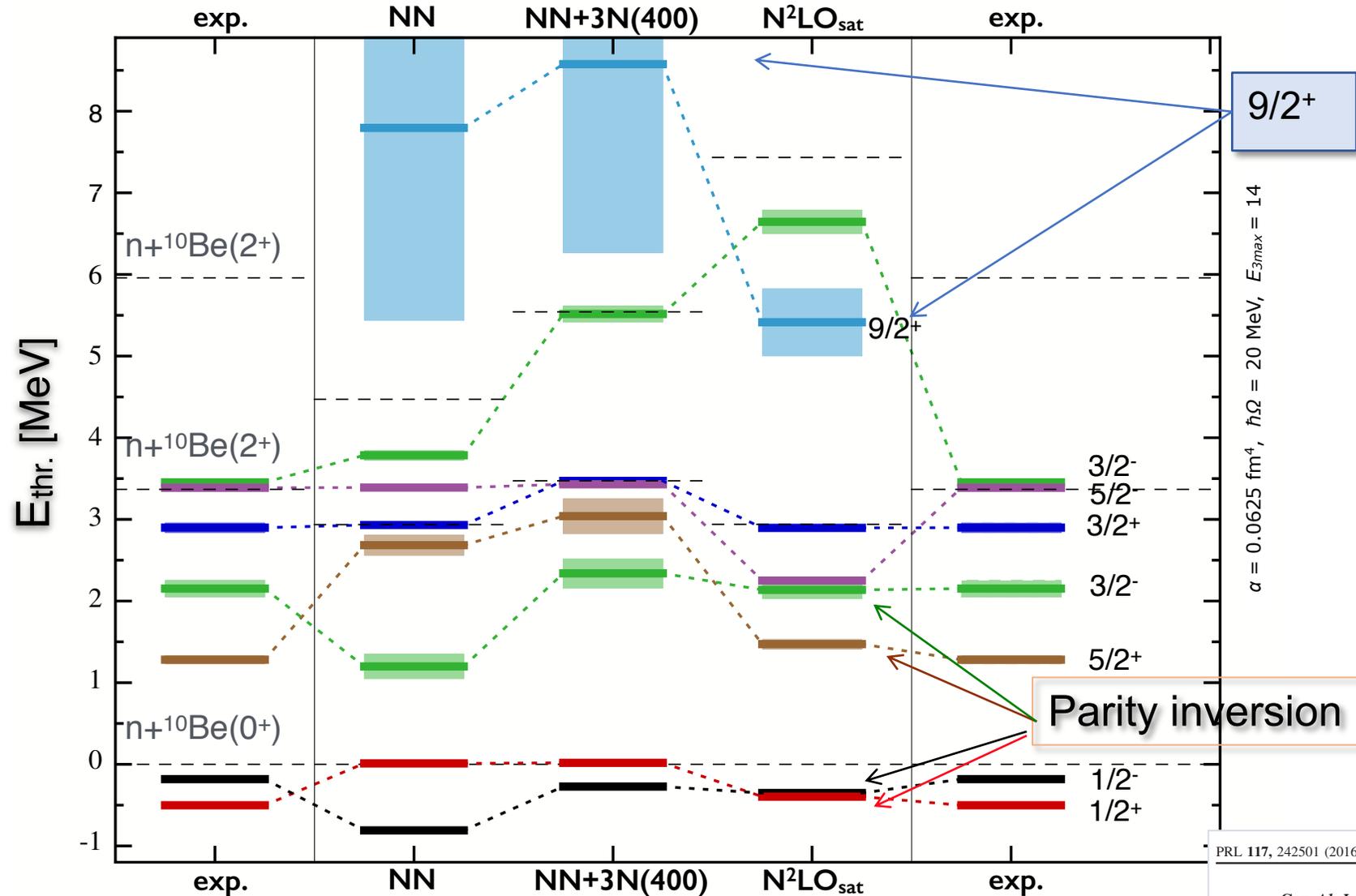
^{11}Be within NCSMC: Discrimination among chiral nuclear forces



^{11}Be within NCSMC: Discrimination among chiral nuclear forces



^{11}Be within NCSMC: Discrimination among chiral nuclear forces



^{11}Be within NCSMC: Discrimination among chiral nuclear forces

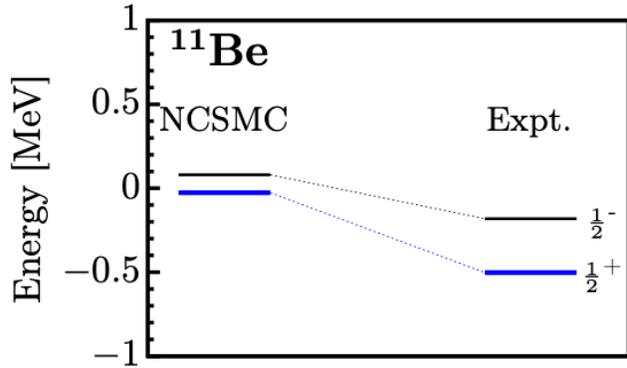
New calculations with NN $N^4\text{LO500}+3\text{N}_{\text{Inl}}$

PHYSICAL REVIEW C **105**, 054316 (2022)

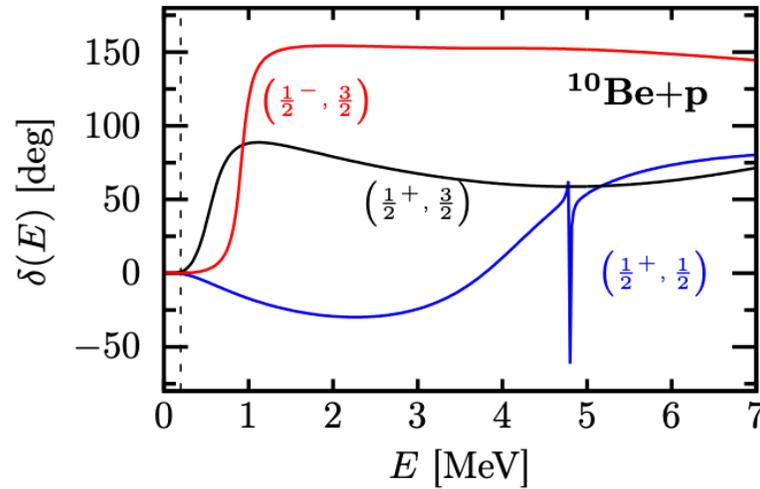
Ab initio calculation of the β decay from ^{11}Be to a $^{10}\text{Be} + p$ resonance

M. C. Atkinson¹, P. Navrátil¹, G. Hupin², K. Kravvaris³ and S. Quaglioni³

$^{11}\text{Be} \rightarrow ^{10}\text{Be} + n$



$^{11}\text{B} \rightarrow ^{10}\text{Be} + p$



Parity inversion reproduced

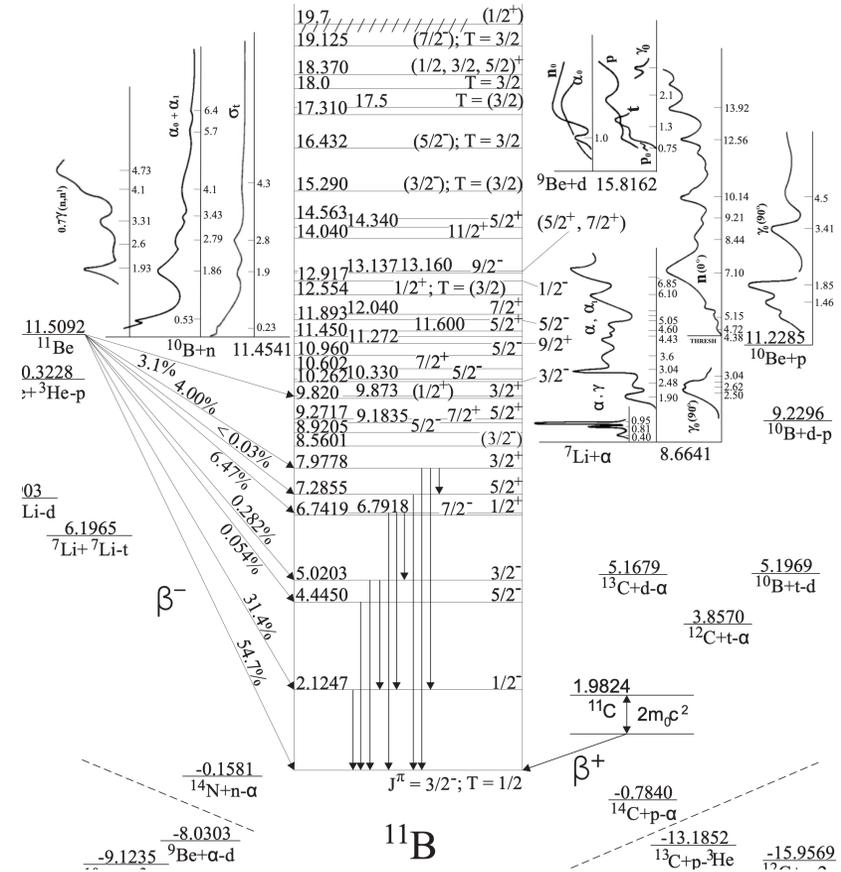
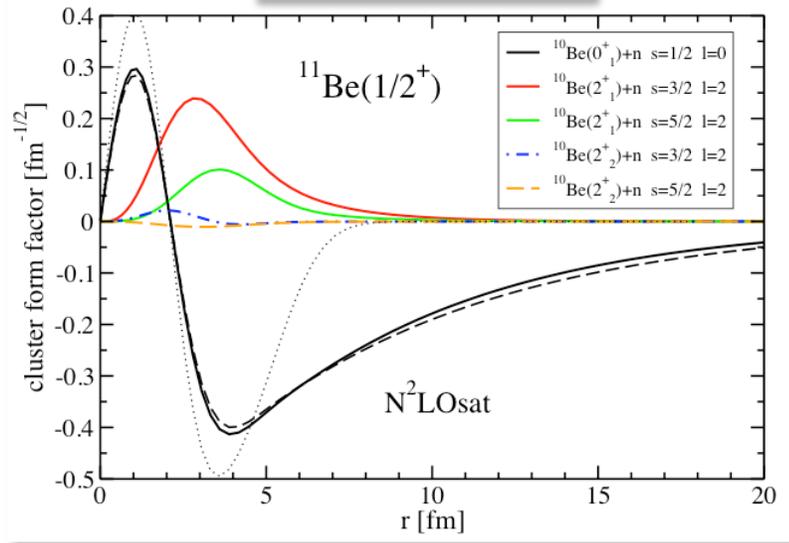


Photo-disassociation of ^{11}Be

Halo structure



cluster form factor

$$= r \langle \Phi_{vr}^{J^{\pi T}} | \hat{A}_v | \psi^{J^{\pi T}} \rangle$$

$$| \Phi_{vr}^{J^{\pi T}} \rangle = \left[\left(| ^{10}\text{Be } \alpha_1 I_1^{\pi_1 T_1} \rangle | n \frac{1}{2}^+ \frac{1}{2} \rangle \right)^{(sT)} Y_\ell(\hat{r}_{10,1}) \right]^{(J^{\pi T})} \frac{\delta(r - r_{10,1})}{r r_{10,1}}$$

Bound to bound	NCSM	NCSMC-phenom	Expt.
B(E1; $1/2^+ \rightarrow 1/2^-$) [e ² fm ²]	0.0005	0.117	0.102(2)

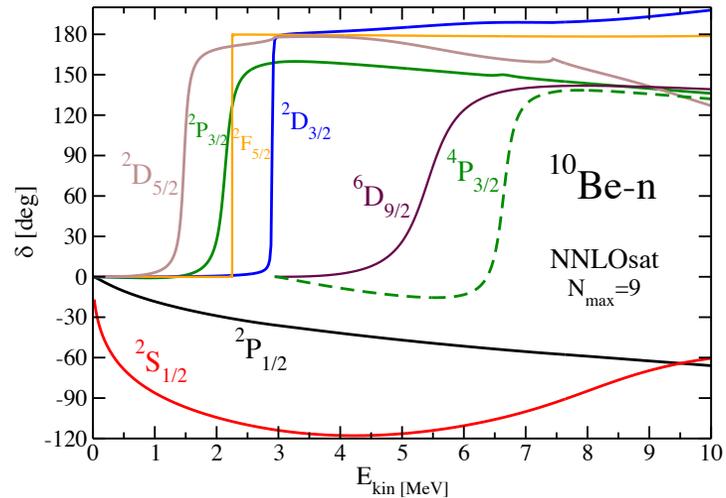
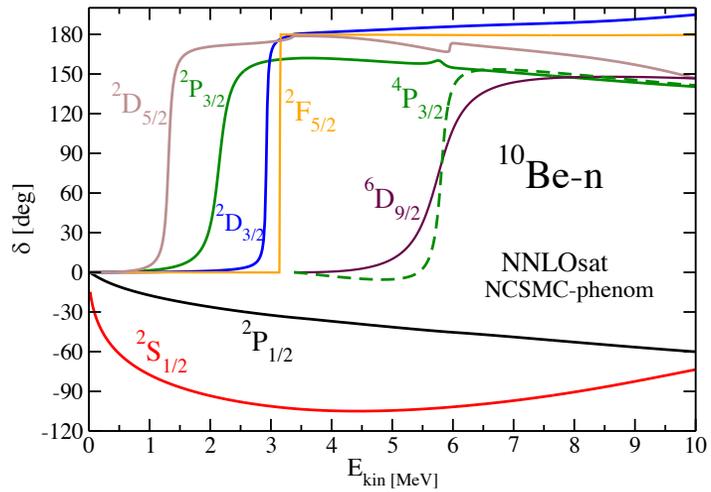
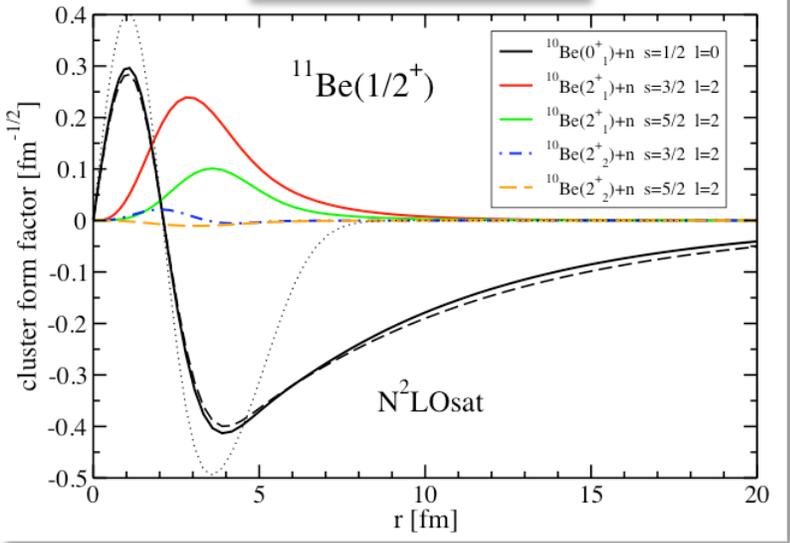


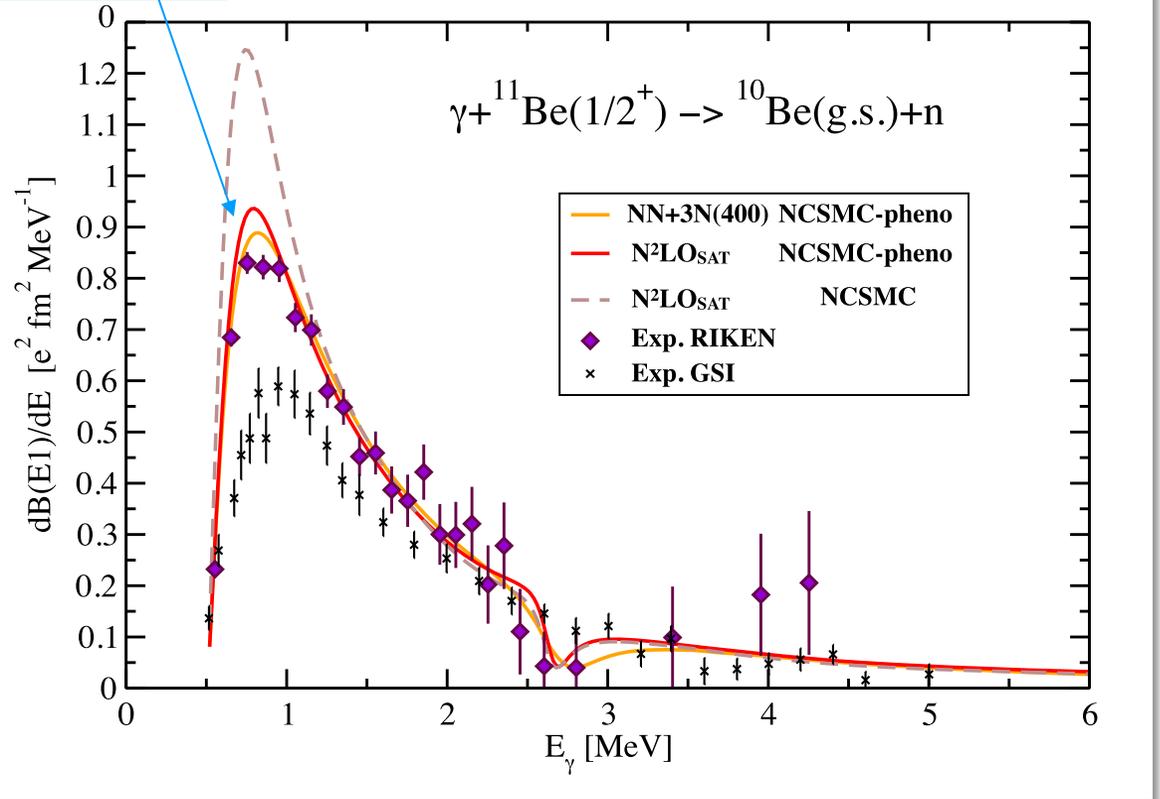
Photo-disassociation of ^{11}Be

Halo structure



Bound to continuum

Not a resonance



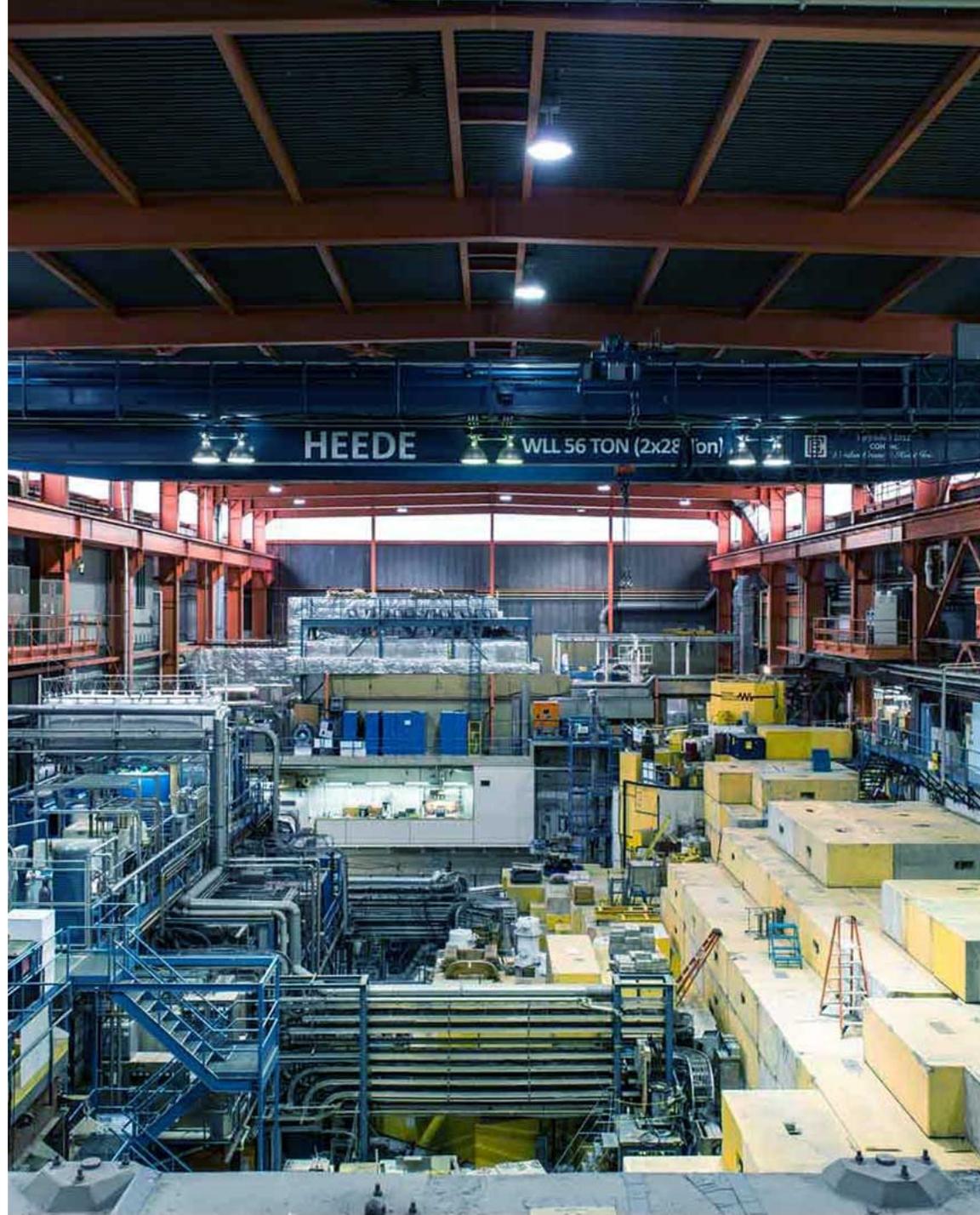
cluster form factor

$$= r \langle \Phi_{vr}^{J^{\pi T}} | \hat{A}_v | \psi^{J^{\pi T}} \rangle$$

$$| \Phi_{vr}^{J^{\pi T}} \rangle = \left[\left(| ^{10}\text{Be } \alpha_1 I_1^{\pi_1 T_1} \rangle \left| n \frac{1}{2}^+ \frac{1}{2} \right. \right) \right]^{(sT)} Y_\ell(\hat{r}_{10,1}) \left]^{(J^{\pi T})} \frac{\delta(r - r_{10,1})}{r r_{10,1}}$$

β -delayed proton emission in ^{11}Be

2023-10-26



β -delayed proton emission in ^{11}Be

45

Physics Letters B 732 (2014) 305–308



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$^{11}\text{Be}(\beta p)$, a quasi-free neutron decay?

K. Riisager^{a,*}, O. Forstner^{b,c}, M.J.G. Borge^{d,e}, J.A. Briz^e, M. Carmona-Gallardo^e,
L.M. Fraile^f, H.O.U. Fynbo^a, T. Giles^g, A. Gottberg^{e,g}, A. Heinz^h, J.G. Johansen^{a,1},
B. Jonson^h, J. Kurcewicz^d, M.V. Lund^a, T. Nilsson^h, G. Nyman^h, E. Rapisarda^d, P. Steier^b,
O. Tengblad^e, R. Thies^h, S.R. Winkler^b

- Indirectly observed $^{11}\text{Be}(\beta p)^{10}\text{Be}$
- Measured an extremely high branching ratio $b_p = 8.3 \pm 0.9 \times 10^{-6}$
 - Orders of magnitude larger than theoretical predictions (e.g. 3.0×10^{-8})
- Two proposed explanations:

D. Baye and E.M. Tursunov, PLB **696**, 4, 464-467 (2011)

- 1 The neutron decays to an unobserved $p+^{10}\text{Be}$ resonance in ^{11}B
- 2 There are unobserved dark decay modes

β -delayed proton emission in ^{11}Be

46

Eur. Phys. J. A (2020) 56:100
<https://doi.org/10.1140/epja/s10050-020-00110-2>

THE EUROPEAN
PHYSICAL JOURNAL A



Regular Article - Experimental Physics

Search for beta-delayed proton emission from ^{11}Be

K. Riisager^{1,a}, M. J. G. Borge^{2,3}, J. A. Briz³, M. Carmona-Gallardo⁴, O. Forstner⁵, L. M. Fraile⁴, H. O. U. Fynbo¹, A. Garzon Camacho³, J. G. Johansen¹, B. Jonson⁶, M. V. Lund¹, J. Lachner⁵, M. Madurga², S. Merchel⁷, E. Nacher³, T. Nilsson⁶, P. Steier⁵, O. Tengblad³, V. Vedia⁴

- New Accelerator Mass Spectrometry experiment that supersedes the 2014 measurement
 - Branching ratio $b_p \sim 2.2 \times 10^{-6}$
 - Upper limit, possible contamination by BeH molecular ions

β -delayed proton emission in ^{11}Be

PHYSICAL REVIEW LETTERS **123**, 082501 (2019)

Editors' Suggestion

Direct Observation of Proton Emission in ^{11}Be

Y. Ayyad,^{1,2,*} B. Olaizola,³ W. Mittig,^{2,4} G. Potel,¹ V. Zelevinsky,^{1,2,4} M. Horoi,⁵ S. Beceiro-Novo,⁴ M. Alcorta,³
C. Andreoiu,⁶ T. Ahn,⁷ M. Anholm,^{3,8} L. Atar,⁹ A. Babu,³ D. Bazin,^{2,4} N. Bernier,^{3,10} S. S. Bhattacharjee,³ M. Bowry,³
R. Caballero-Folch,³ M. Cortesi,² C. Dalitz,¹¹ E. Dunling,^{3,12} A. B. Garnsworthy,³ M. Holl,^{3,13} B. Kootte,^{3,8}
K. G. Leach,¹⁴ J. S. Randhawa,² Y. Saito,^{3,10} C. Santamaria,¹⁵ P. Šiurytė,^{3,16} C. E. Svensson,⁹
R. Umashankar,³ N. Watwood,² and D. Yates^{3,10}

- Directly observed the protons from $^{11}\text{Be}(\beta p)^{10}\text{Be}$
- Measured consistent branching ratio $b_p = 1.3(3) \times 10^{-5}$
 - Still orders of magnitude larger than theoretical predictions
- Predict the proton resonance at 11.425(20) MeV from the proton energy distribution
 - Predicted to be either $\frac{1}{2}^+$ or $\frac{3}{2}^+$
 - Corresponds to excitation energy of 197 keV

NCSMC extended to describe exotic ^{11}Be βp emission

$$|^{11}\text{Be or } ^{11}\text{B}\rangle = \sum_{\lambda} c_{\lambda}^{J^{\pi} T} |A\lambda J^{\pi} T\rangle + \sum_{\nu} \int dr r^2 \frac{\gamma_{\nu}^{J^{\pi} T}(r)}{r} \hat{A}_{\nu} |\Phi_{\nu r}^{J^{\pi} T}\rangle$$

$$|\Phi_{\nu r}^{J^{\pi} T}\rangle = \left[\left(|^{10}\text{Be } \alpha_1 I_1^{\pi_1} T_1\rangle |N \frac{1}{2}^+ \frac{1}{2}\rangle \right)^{(sT)} Y_{\ell}(\hat{r}_{10,1}) \right]^{(J^{\pi} T)} \times \frac{\delta(r-r_{10,1})}{rr_{10,1}}, \quad \text{n for } ^{11}\text{Be or p for } ^{11}\text{B}$$

Input chiral interaction

NN N⁴LO(500) + 3N(Ini)

↑

Entem-Machleidt-Nosyk 2017

3N N²LO w local/non-local regulator

Including 0^+_{gs} and 2^+_1 states of ^{10}Be

$$B(\text{GT}) = \frac{1}{2} \left| \langle \Psi_{^{11}\text{B}}^{\frac{1}{2}^+ \frac{1}{2}} \parallel \hat{G}\text{T} \parallel \Psi_{^{11}\text{Be}}^{\frac{1}{2}^+ \frac{3}{2}} \rangle \right|^2$$

PHYSICAL REVIEW C **105**, 054316 (2022)

Ab initio calculation of the β decay from ^{11}Be to a $^{10}\text{Be} + p$ resonance

M. C. Atkinson¹, P. Navrátil¹, G. Hupin², K. Kravvaris³, and S. Quaglioni³

Gamow-Teller and Fermi β -decay in NCSMC

- Compute GT and Fermi matrix element in NCSMC

$$M_F = \left\langle \Psi^{J^\pi T_f M_{T_f}} \left| T_+ \right| \Psi^{J^\pi T_i M_{T_i}} \right\rangle$$

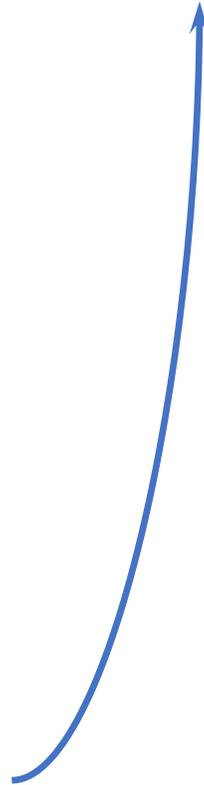
- Total isospin (or GT) operator $T_+ = T_+^{(1)} + T_+^{(2)}$ for partitioned system

$$M_F \sim \underbrace{\langle A\lambda_f J_f T_f M_{T_f} | T_+ | A\lambda_i J_i T_i M_{T_i} \rangle}_{\text{NCSM matrix element}} + \underbrace{\langle A\lambda J_f T_f M_{T_f} | T_+ \mathcal{A}_{\nu i} | \Phi_{\nu r}^{J_i T_i M_{T_i}} \rangle}_{\text{NCSM-Cluster matrix elements}} + \underbrace{\langle \Phi_{\nu r}^{J_f T_f M_{T_f}} | \mathcal{A}_{\nu f} T_+ | A\lambda_i J_i T_i M_{T_i} \rangle}_{\text{NCSM-Cluster matrix elements}} + \underbrace{\langle \Phi_{\nu r}^{J_f T_f M_{T_f}} | \mathcal{A}_{\nu f} T_+ \mathcal{A}_{\nu i} | \Phi_{\nu r}^{J_i T_i M_{T_i}} \rangle}_{\text{Continuum (cluster) matrix element}}$$

NCSM matrix element

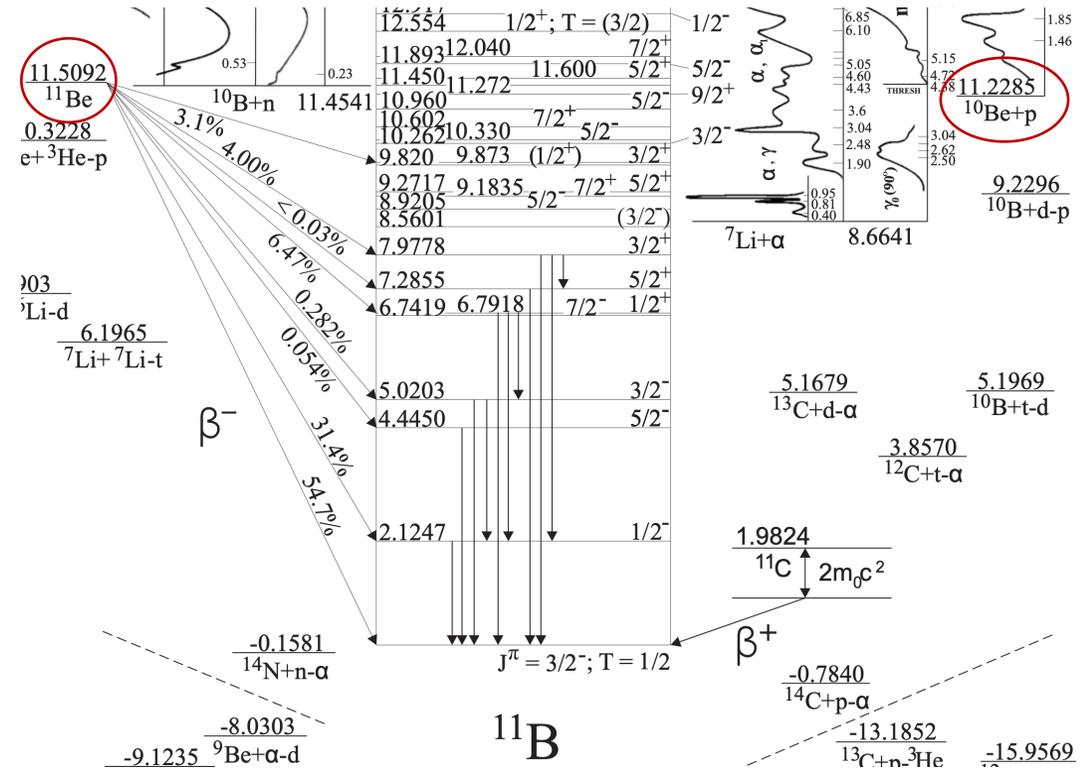
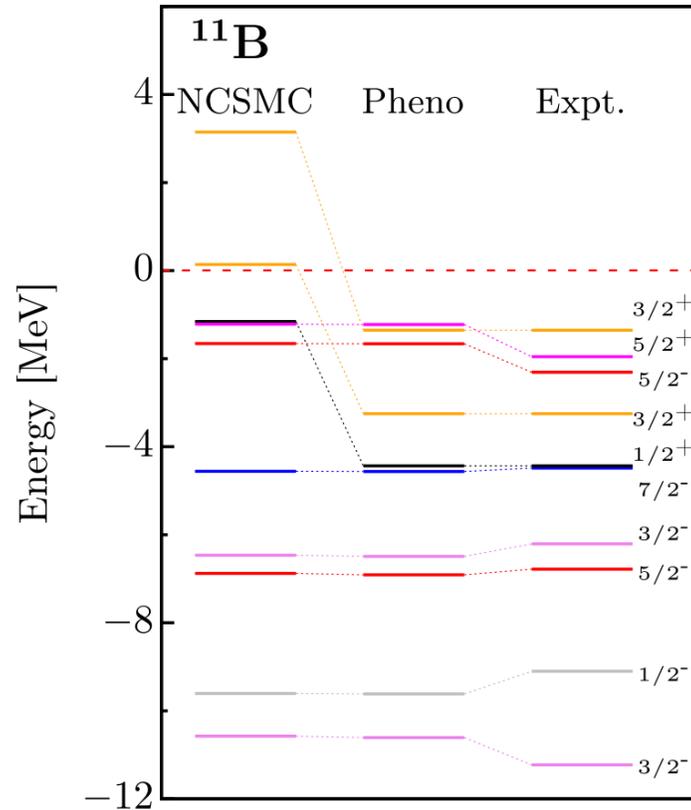
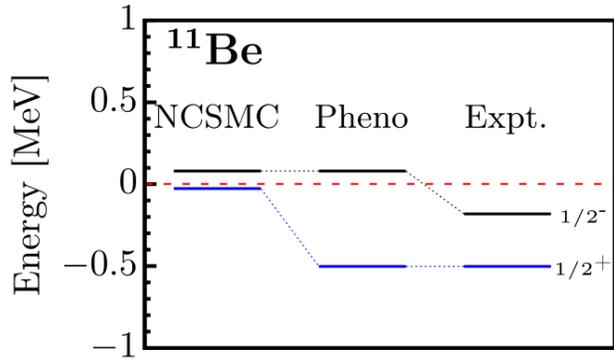
NCSM-Cluster matrix elements

Continuum (cluster) matrix element



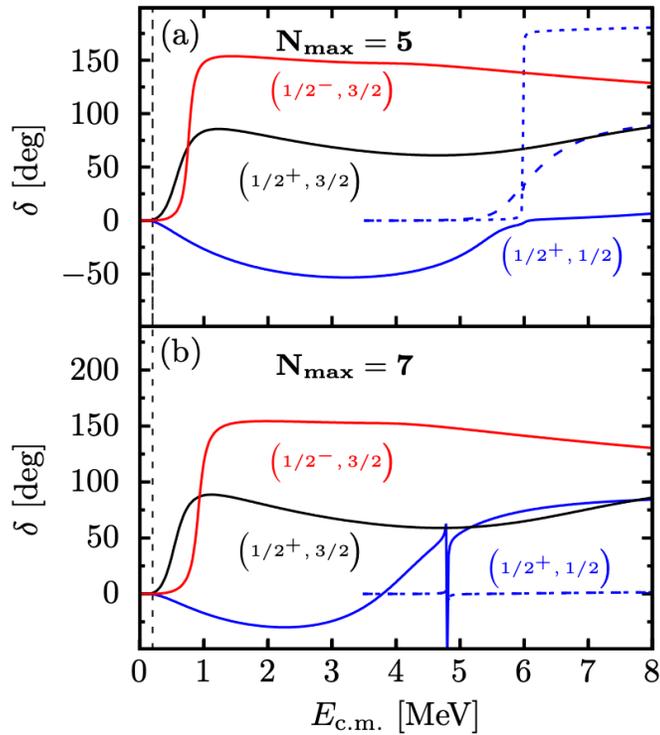
^{11}Be and ^{11}B nuclear structure results

- Bound states wrt $^{10}\text{Be}+N$ thresholds

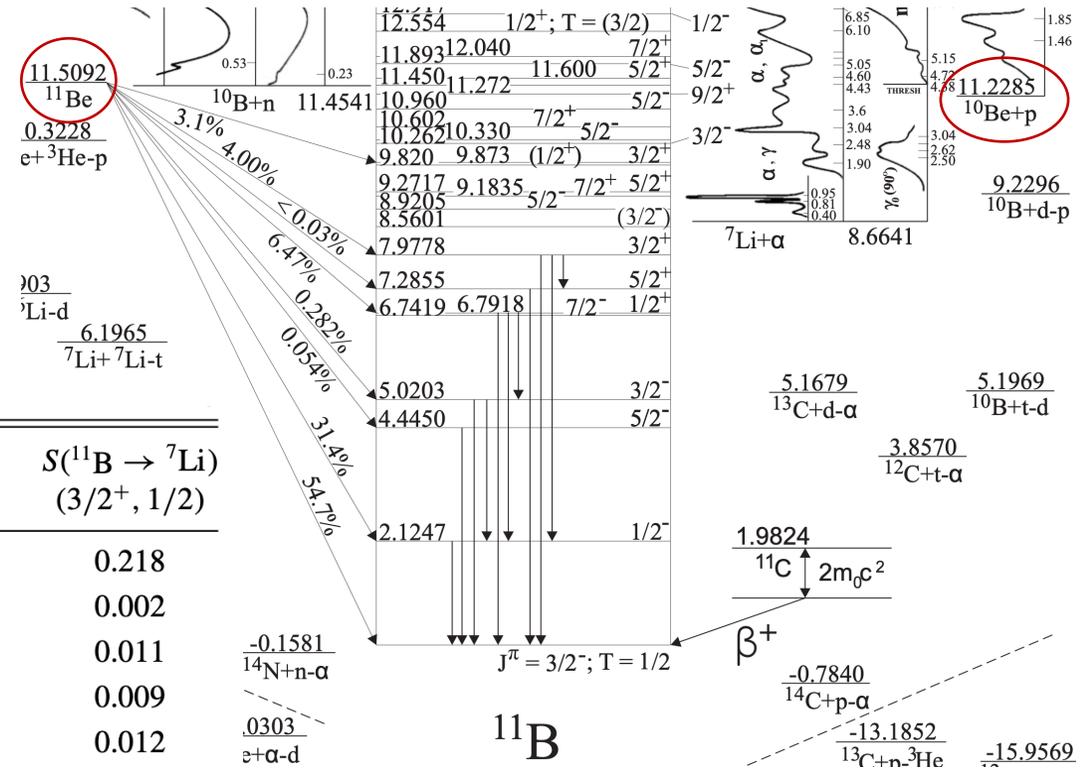


^{11}Be and ^{11}B nuclear structure results

- ^{11}B resonances above $^{10}\text{Be}+p$ threshold

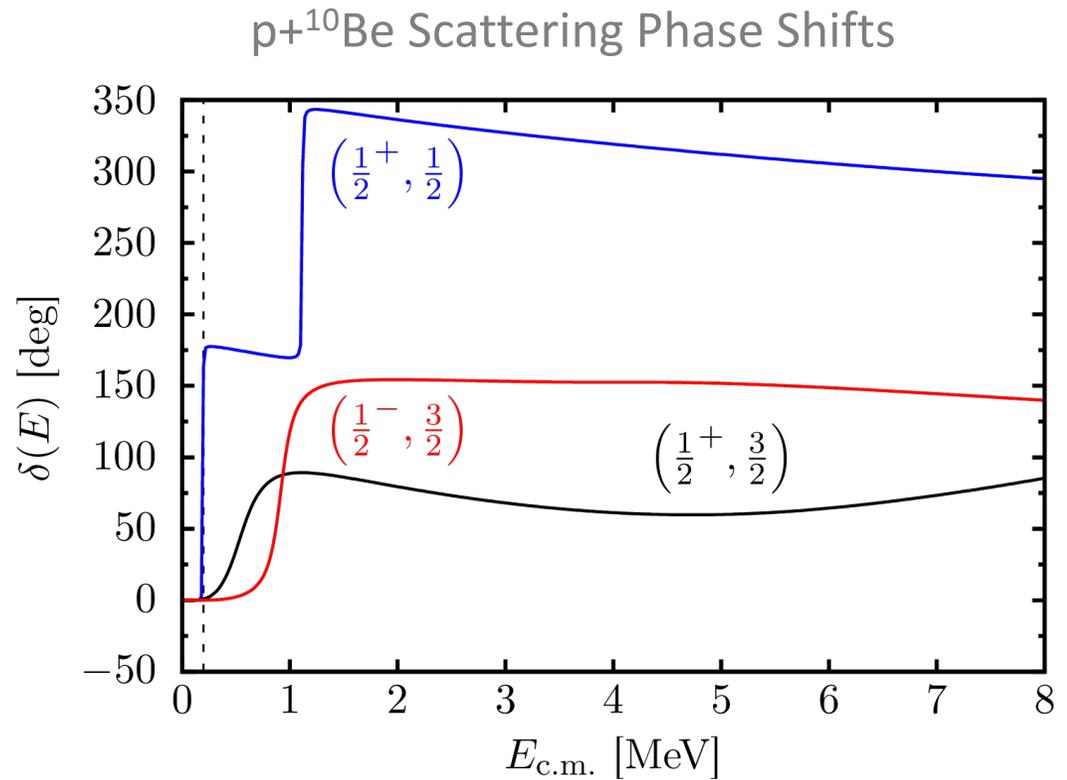


J^π	$S(^{11}\text{B} \rightarrow ^{10}\text{Be})$ ($0^+, 1$)	$S(^{11}\text{B} \rightarrow ^{10}\text{B})$ ($1_1^+, 0$) ($1_2^+, 0$)	$S(^{11}\text{B} \rightarrow ^7\text{Li})$ ($3/2^+, 1/2$)
$1/2_1^+$	0.276	0.250 2×10^{-4}	0.218
$1/2_2^+$	0.0525	0.171 0.562	0.002
$1/2_3^+$	0.067	0.231 0.188	0.011
$3/2_1^+$	0.079	6×10^{-4} 0.215	0.009
$3/2_2^+$	4×10^{-4}	0.581 0.002	0.012
$3/2_3^+$	6×10^{-4}	0.011 0.006	0.021
$3/2_4^+$	0.067	0.034 0.35	0.006



NCSMC extended to describe exotic ^{11}Be βp emission, supports large branching ratio due to narrow $\frac{1}{2}^+$ resonance

$^{11}\text{Be} \rightarrow (^{10}\text{Be}+p) + \beta^- + \bar{\nu}_e$ GT transition

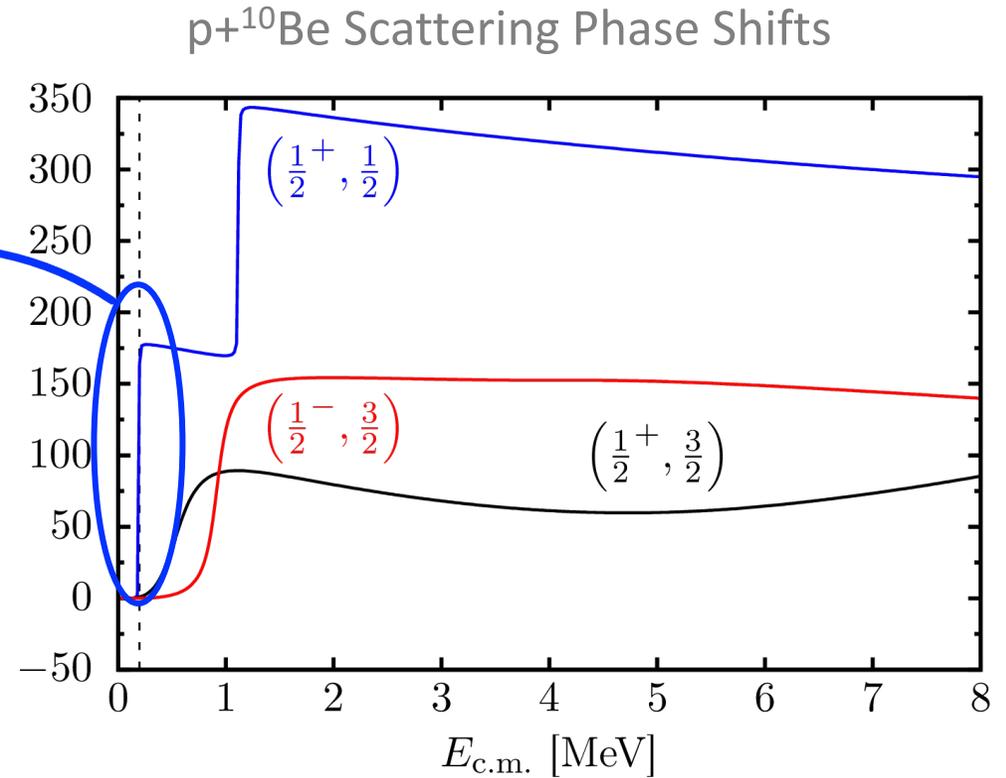
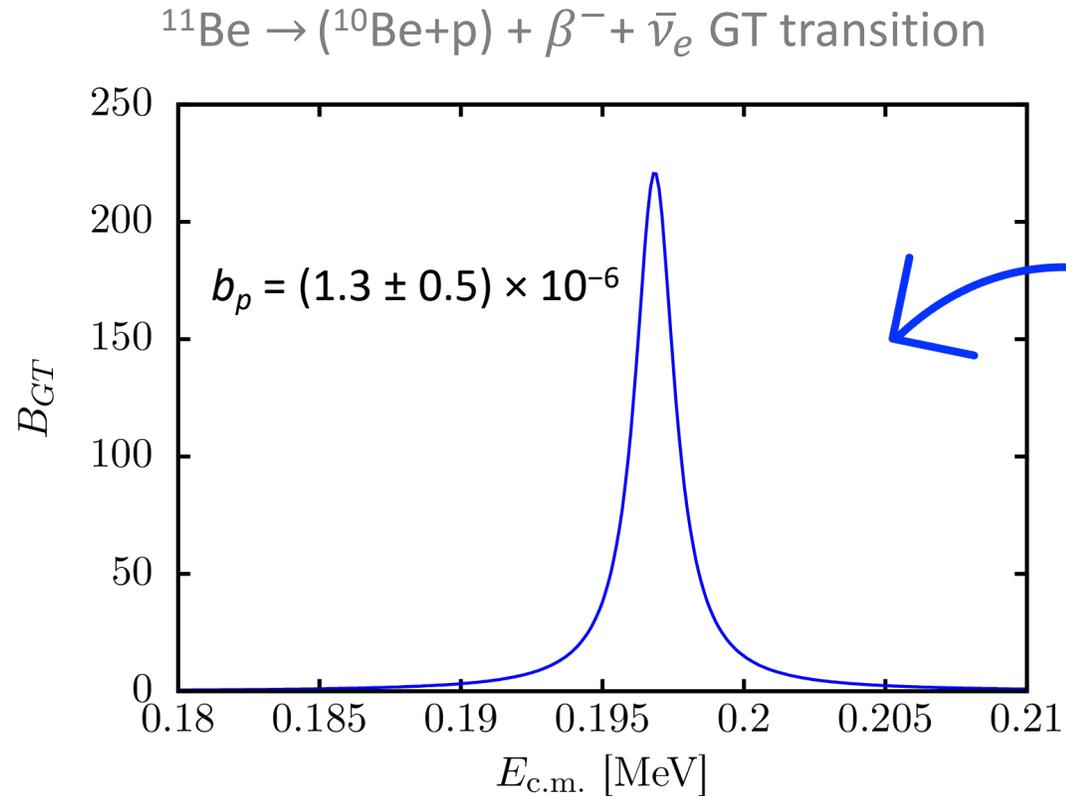


PHYSICAL REVIEW C **105**, 054316 (2022)

Ab initio calculation of the β decay from ^{11}Be to a $^{10}\text{Be} + p$ resonance

M. C. Atkinson¹, P. Navrátil¹, G. Hupin², K. Kravvaris³, and S. Quaglioni³

NCSMC extended to describe exotic ^{11}Be βp emission, supports large branching ratio due to narrow $\frac{1}{2}^+$ resonance

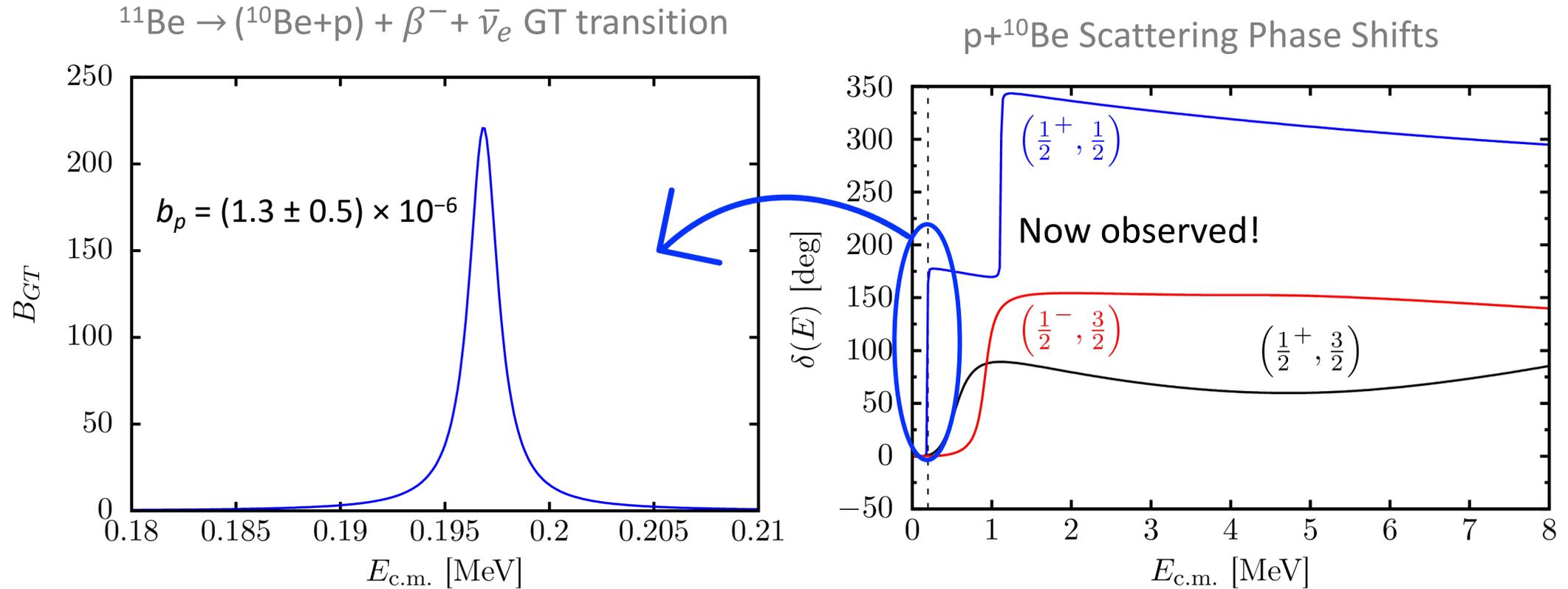


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PHYSICAL REVIEW LETTERS **129**, 012502 (2022)

Observation of a Near-Threshold Proton Resonance in ^{11}B

E. Lopez-Saavedra^{1,*}, S. Almaraz-Calderon^{1,†}, B. W. Asher¹, L. T. Baby¹, N. Gerken¹, K. Hanselman¹, K. W. Kemper¹, A. N. Kuchera², A. B. Morelock¹, J. F. Perello¹, E. S. Temanson¹, A. Volya¹ and I. Wiedenhöver¹

PHYSICAL REVIEW LETTERS **129**, 012501 (2022)

Evidence of a Near-Threshold Resonance in ^{11}B Relevant to the β -Delayed Proton Emission of ^{11}Be

Y. Ayyad^{1,2,*}, W. Mittag^{2,3}, T. Tang², B. Olaizola⁴, G. Potel⁵, N. Rijal², N. Watwood², H. Alvarez-Pol¹, D. Bazin^{2,3}, M. Caamaño¹, J. Chen⁶, M. Cortesi², B. Fernández-Domínguez¹, S. Giraud², P. Gueye^{2,3}, S. Heinitz⁷, R. Jain^{2,3}, B. P. Kay⁶, E. A. Mauger⁷, B. Monteaudo², F. Ndayisabye^{2,3}, S. N. Paneru², J. Pereira², E. Rubino², C. Santamaria², D. Schumann⁷, J. Surbrook^{2,3}, L. Wagner², J. C. Zamora² and V. Zelevinsky^{2,3}

PHYSICAL REVIEW C **105**, 054316 (2022)

Ab initio calculation of the β decay from ^{11}Be to a $^{10}\text{Be} + p$ resonance

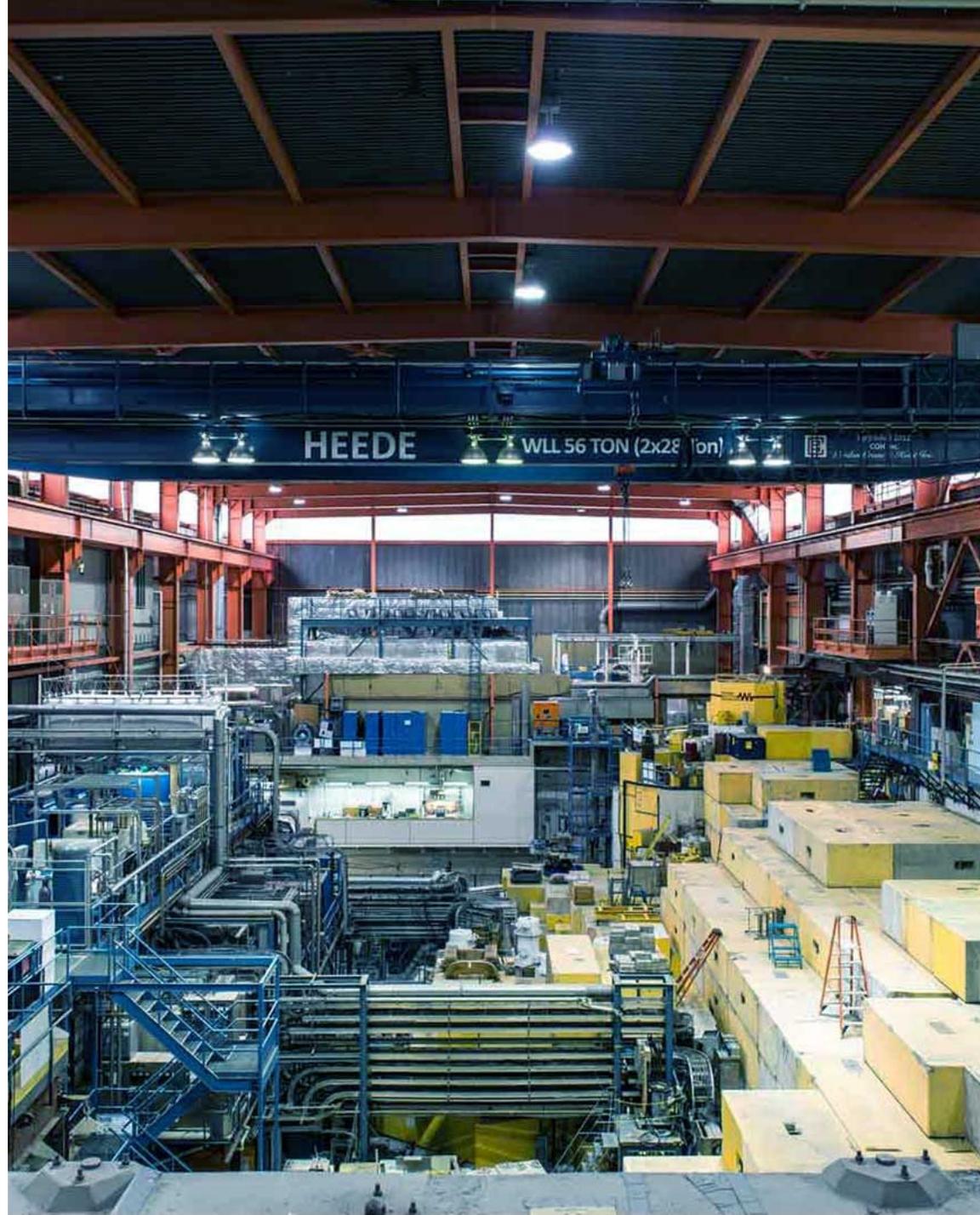
M. C. Atkinson¹, P. Navrátil¹, G. Hupin², K. Kravvaris³ and S. Quaglioni³

β -delayed proton emission in ^{11}Be

- New FRIB experiment measuring proton emission led by Jason Surbrook reports branching ratio $b_p \sim 8(4) \times 10^{-6}$
 - Lower but still consistent with Ayyad TRIUMF experiment
- More experiments planned!
- NCSMC calculations will be extended by **including the $^7\text{Li}+\alpha$** mass partition

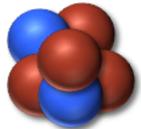
Two-neutron Borromean halo nucleus ${}^6\text{He}$

2023-10-26



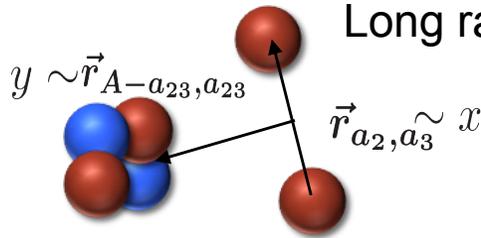
NCSM for three-body clusters

NCSM
Short range description

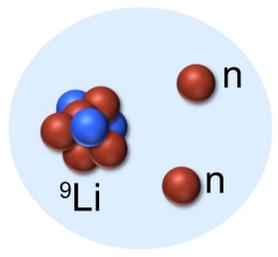
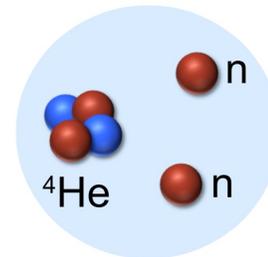


+

NCSM/RGM-3B
Long range description



Two-neutron Borromean halo nuclei



$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} \left| \begin{array}{c} \text{cluster} \\ \lambda \end{array} \right\rangle + \sum_{\nu} \int d\vec{x} d\vec{y} \gamma_{\nu}(\vec{x}, \vec{y}) \hat{A}_{\nu} \left| \begin{array}{c} \text{cluster} \\ \nu \end{array} \right\rangle$$

Unknowns

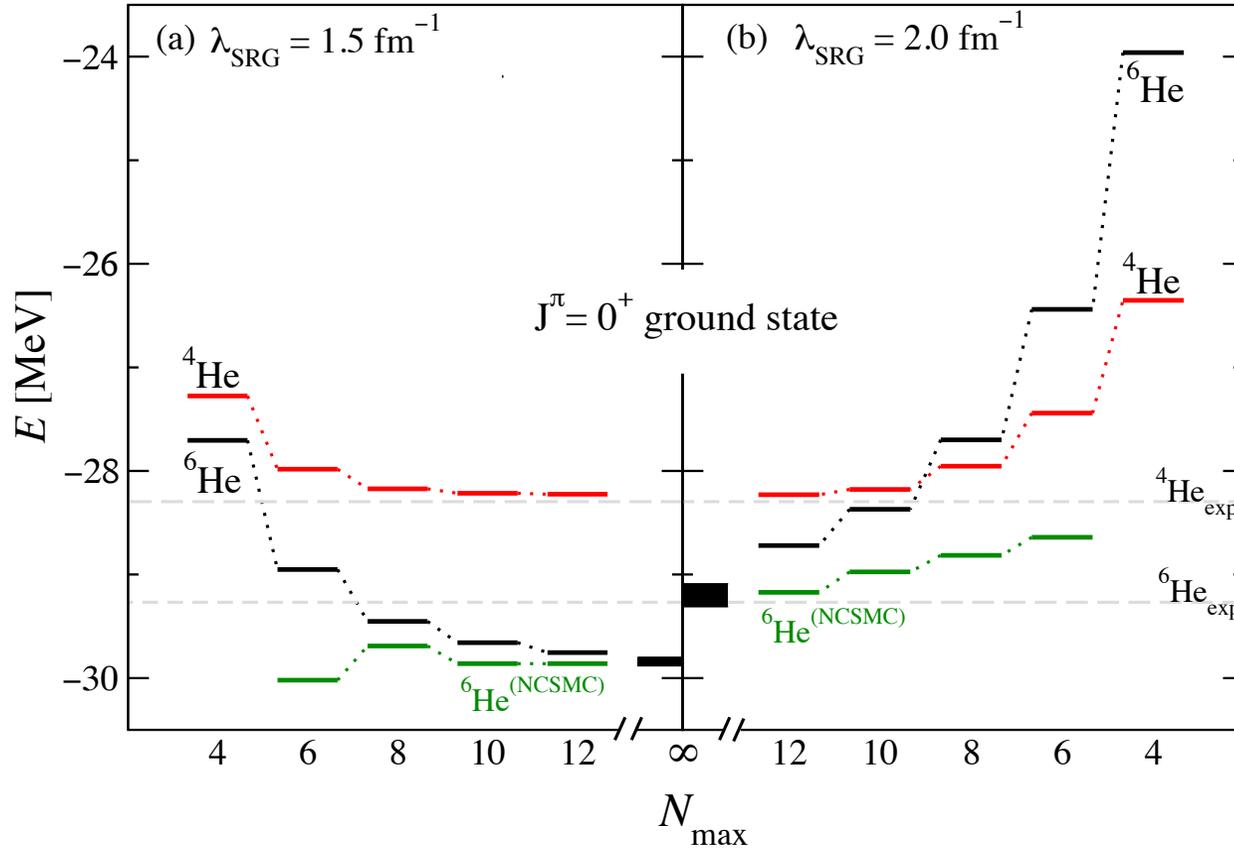
Three-cluster dynamics within the *ab initio* no-core shell model with continuum:
How many-body correlations and α clustering shape ${}^6\text{He}$

Sofia Quaglioni,^{1,*} Carolina Romero-Redondo,^{1,†} Petr Navrátil,^{2,‡} and Guillaume Hupin^{3,§}

How Many-Body Correlations and α Clustering Shape ${}^6\text{He}$

Carolina Romero-Redondo,^{1,*} Sofia Quaglioni,^{1,†} Petr Navrátil,^{2,‡} and Guillaume Hupin^{3,§}

NCSMC for three-body clusters: ${}^6\text{He} \sim {}^4\text{He}+n+n$

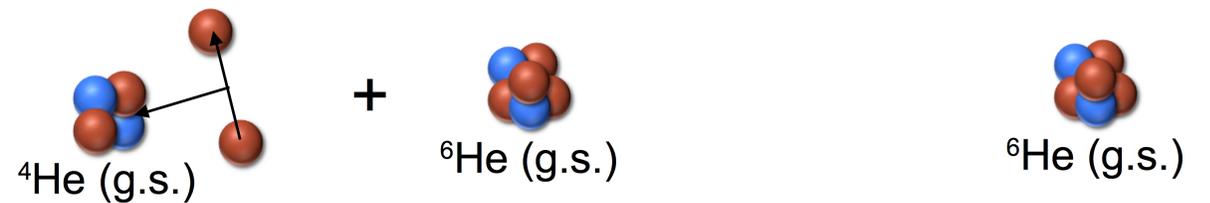


SRG $N^3\text{LO}$ NN potential

NCSMC

vs.

NCSM



Three-cluster dynamics within the *ab initio* no-core shell model with continuum:
How many-body correlations and α clustering shape ${}^6\text{He}$

Sofia Quaglioni,^{1,*} Carolina Romero-Redondo,^{1,†} Petr Navrátil,^{2,‡} and Guillaume Hupin^{3,§}

PRL 117, 222501 (2016)

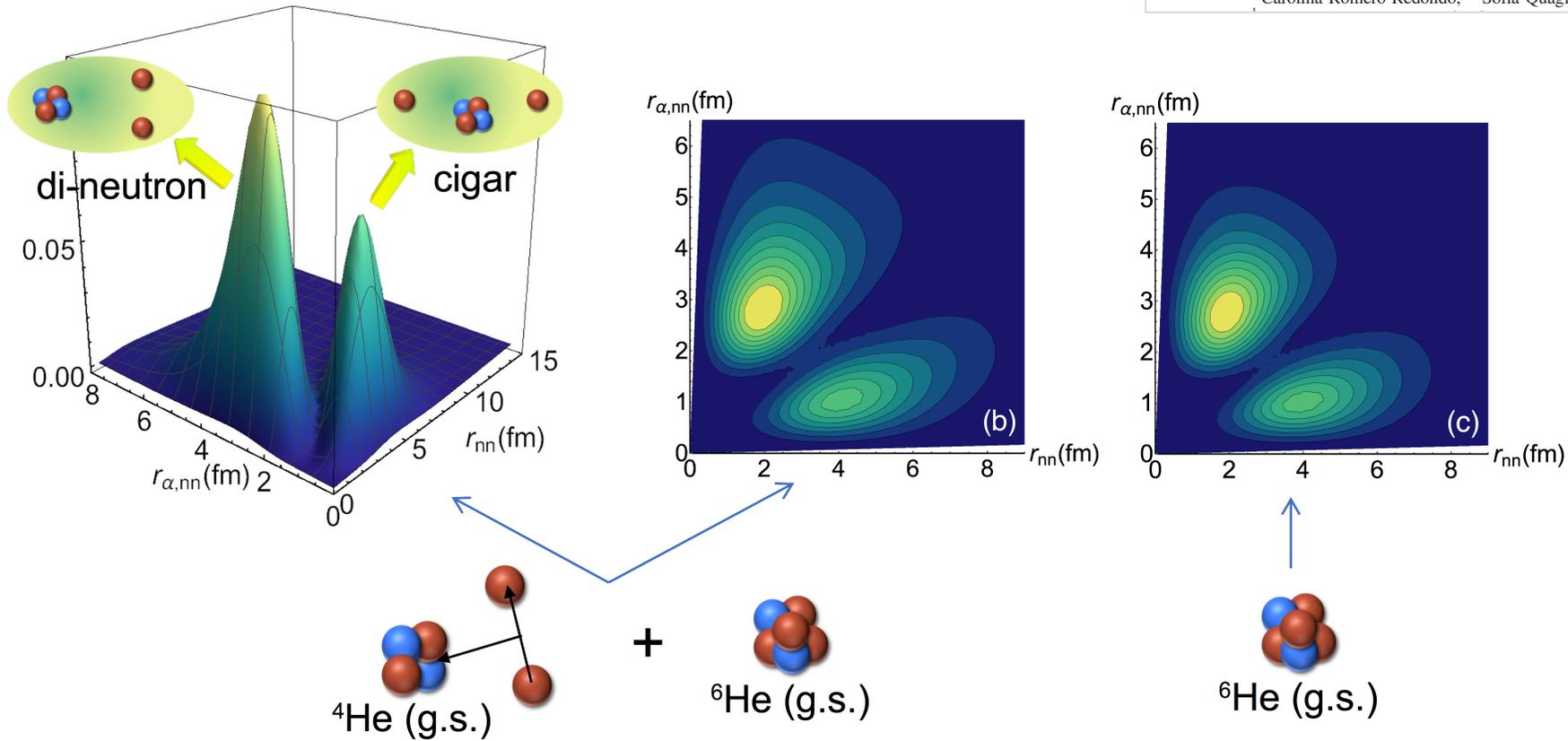
PHYSICAL REVIEW LETTERS

week ending
25 NOVEMBER 2016

How Many-Body Correlations and α Clustering Shape ${}^6\text{He}$

Carolina Romero-Redondo,^{1,*} Sofia Quaglioni,^{1,†} Petr Navrátil,^{2,‡} and Guillaume Hupin^{3,§}

NCSMC for three-body clusters: ${}^6\text{He} \sim {}^4\text{He}+n+n$



The probability distribution of the ${}^6\text{He}$ ground state presents two peaks corresponding to the di-neutron and cigar configurations

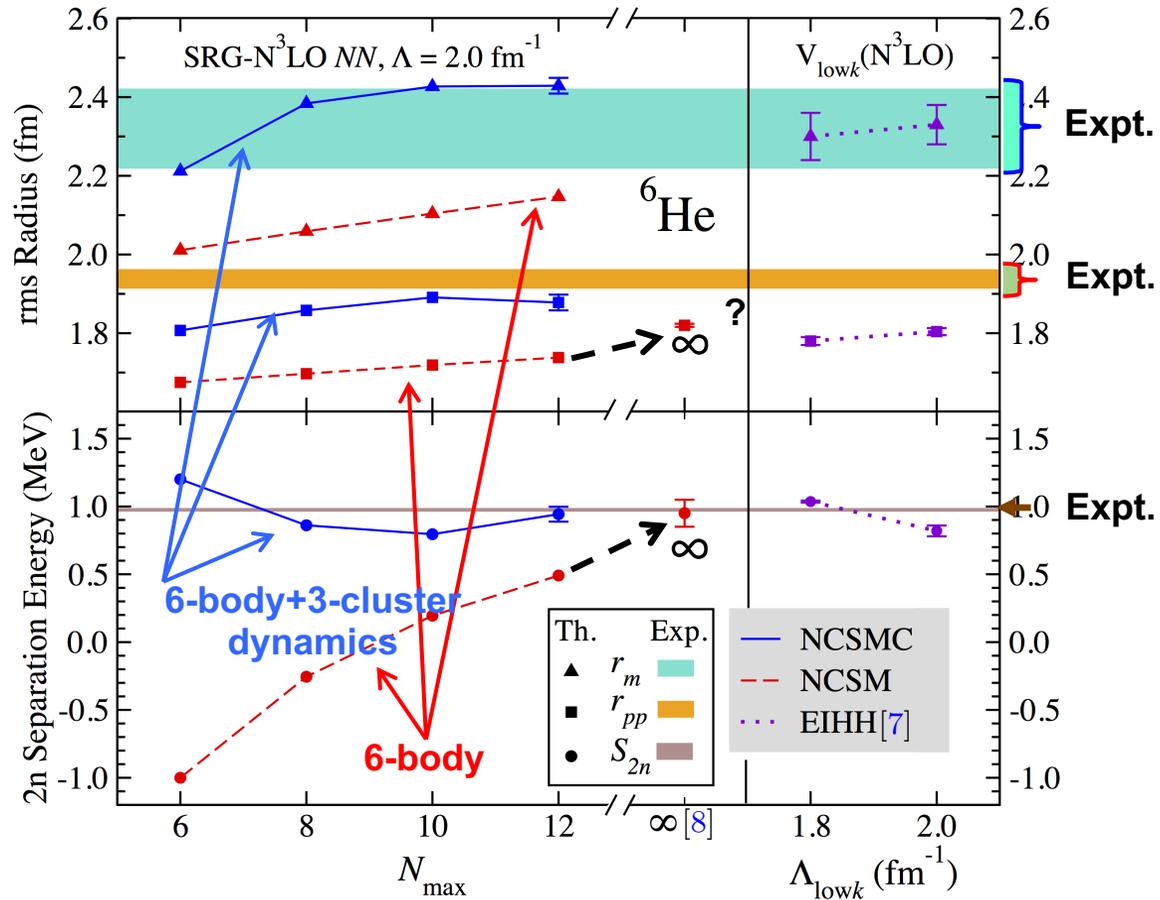
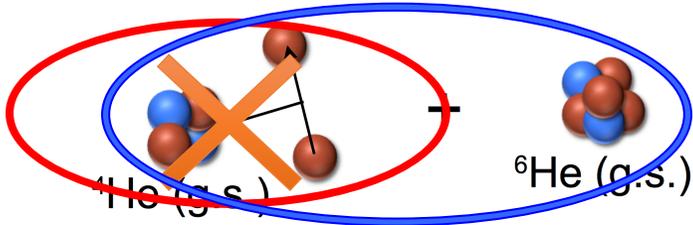
Three-cluster dynamics within the *ab initio* no-core shell model with continuum:
How many-body correlations and α clustering shape ${}^6\text{He}$

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How Many-Body Correlations and α Clustering Shape ${}^6\text{He}$

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NCSMC for three-body clusters: ${}^6\text{He} \sim {}^4\text{He}+n+n$



Separation energy, point proton and matter radius simultaneously consistent with experiment

Conclusions

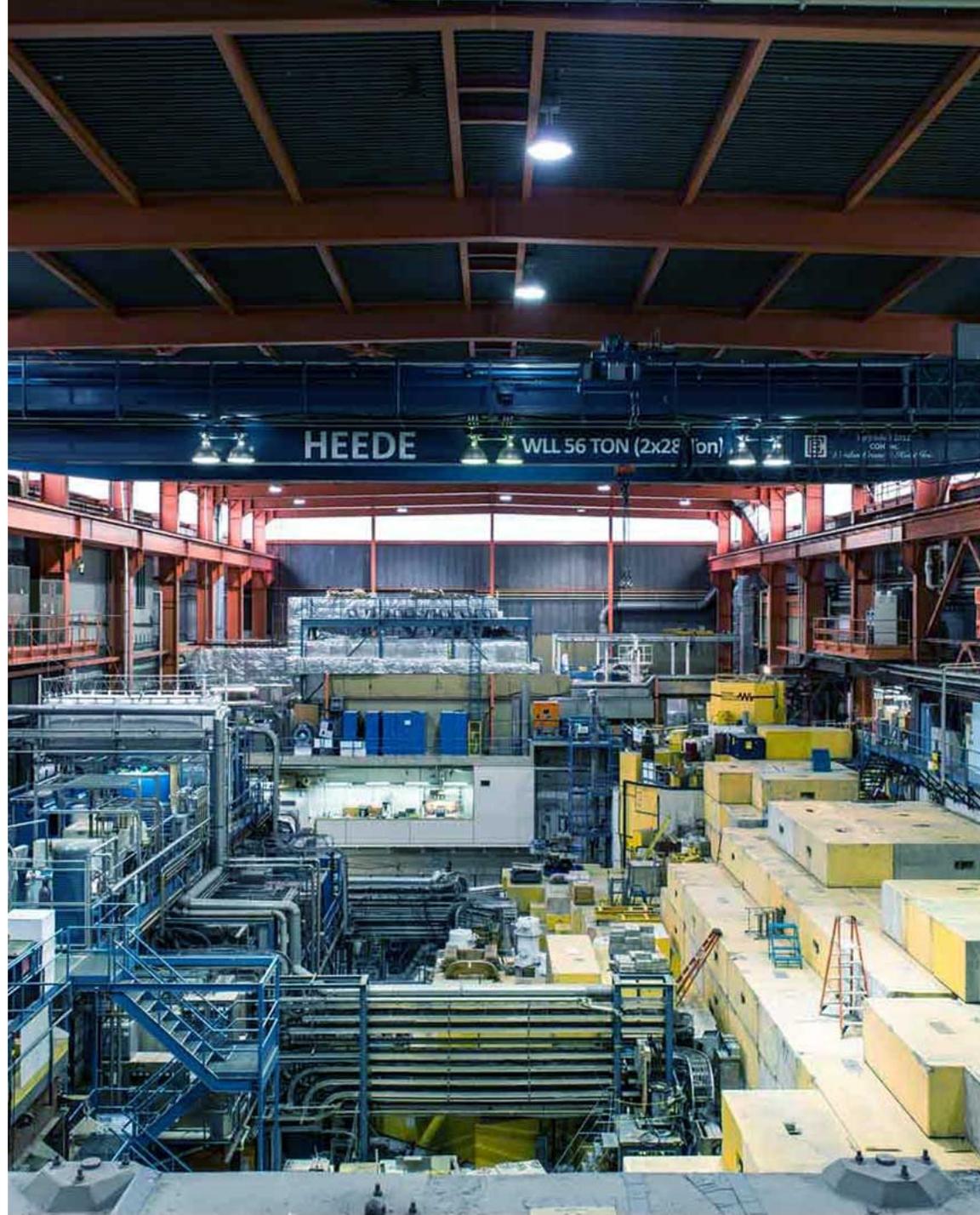
- *Ab initio* nuclear theory
 - Makes connections between the low-energy QCD and many-nucleon systems
 - Applicable to nuclear structure, reactions including those relevant for astrophysics, electroweak processes, tests of fundamental symmetries
 - Very recently reach extended to heavy nuclei
- Applications of *ab initio* no-core shell model with continuum to nuclear structure and reactions
 - DT fusion - near threshold $3/2^+$ S-wave resonance
 - $1/2^+$ S-wave resonance close to the ${}^6\text{He}+p$ threshold in ${}^7\text{Li}$
 - Parity inversion in ${}^{11}\text{Be}$ ground state – weakly bound halo state
 - β -delayed proton emission in ${}^{11}\text{Be}$ - near threshold $1/2^+$ S-wave resonance
 - Two-neutron Borromean halo nucleus ${}^6\text{He}$ - di-neutron and cigar configurations in the ground state

In synergy with experiments, *ab initio* nuclear theory is the right approach to understand low-energy properties of atomic nuclei

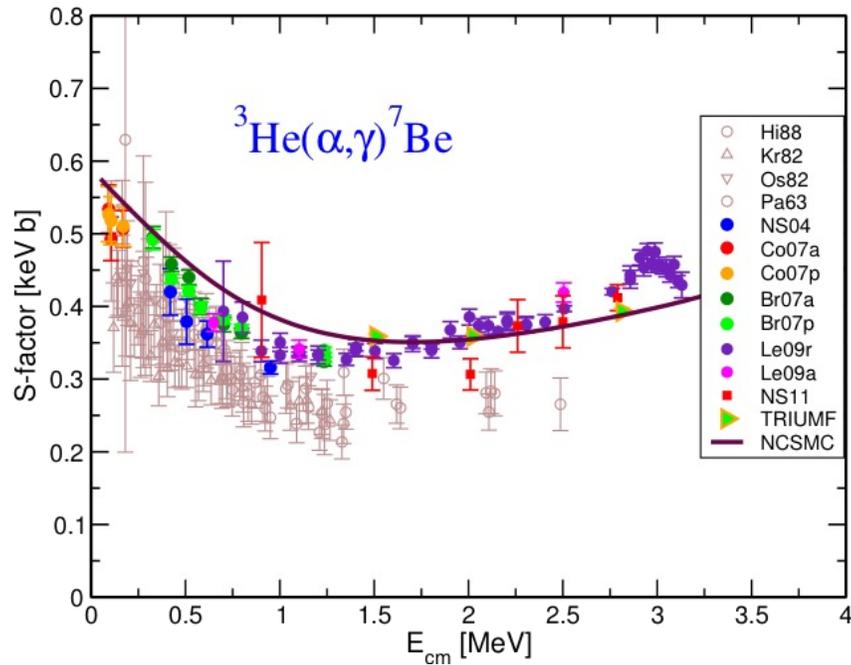
Thank you!
Merci!
Grazie!



Backup slides



^7Be structure and capture reactions important for astrophysics



Physics Letters B 757 (2016) 430–436

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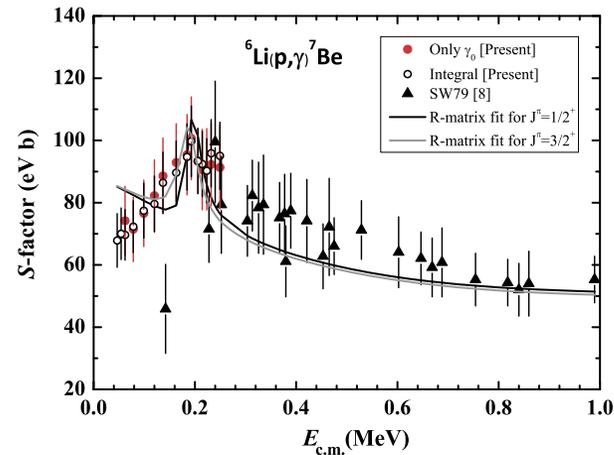
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$^3\text{He}(\alpha, \gamma)^7\text{Be}$ and $^3\text{H}(\alpha, \gamma)^7\text{Li}$ astrophysical S factors from the no-core shell model with continuum



Jérémy Dohet-Eraly^{a,*}, Petr Navrátil^a, Sofia Quaglioni^b, Wataru Horiuchi^c, Guillaume Hupin^{b,d,1}, Francesco Raimondi^{a,2}



What resonances do we find in ^7Be within NCSMC?

PHYSICAL REVIEW C **100**, 024304 (2019)

^7Be and ^7Li nuclei within the no-core shell model with continuum

Matteo Vorabbi[✉] and Petr Navrátil[†]

TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia V6T 2A3, Canada

Sofia Quaglioni

Lawrence Livermore National Laboratory, P. O. Box 808, L-414, Livermore, California 94551, USA

Guillaume Hupin[✉]

Institut de Physique Nucléaire, CNRS/IN2P3, Université Paris-Sud, Université Paris-Saclay, F-91406, Orsay, France

Physics Letters B 725 (2013) 287–291

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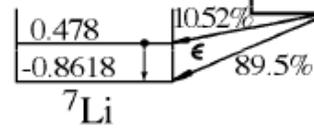
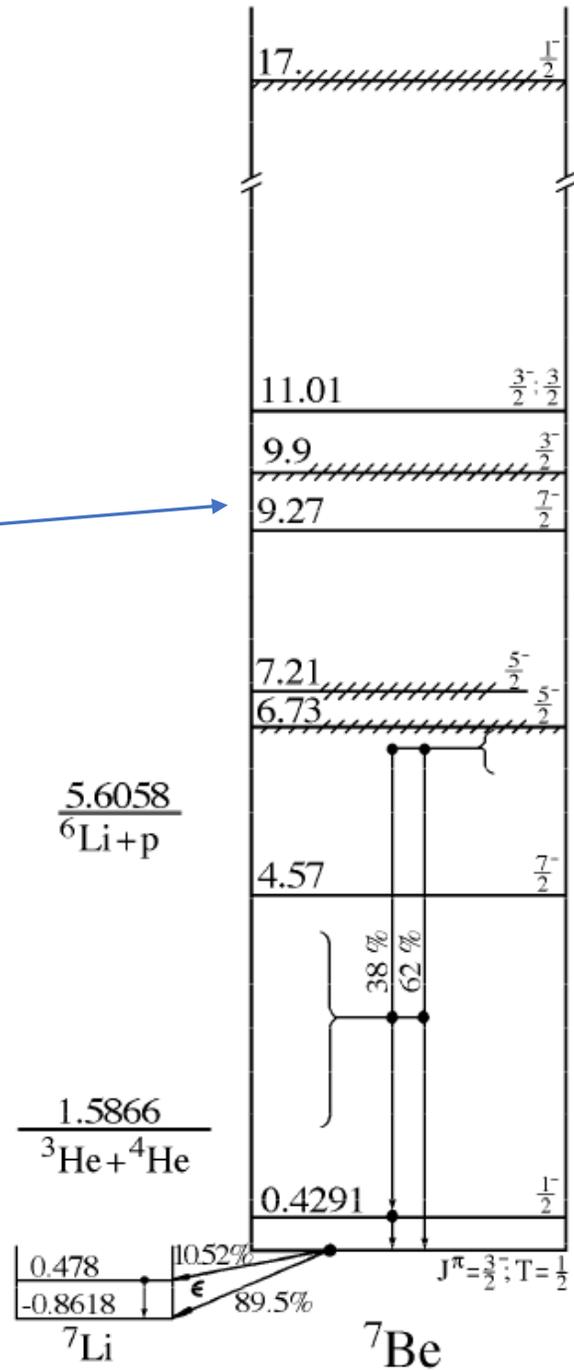
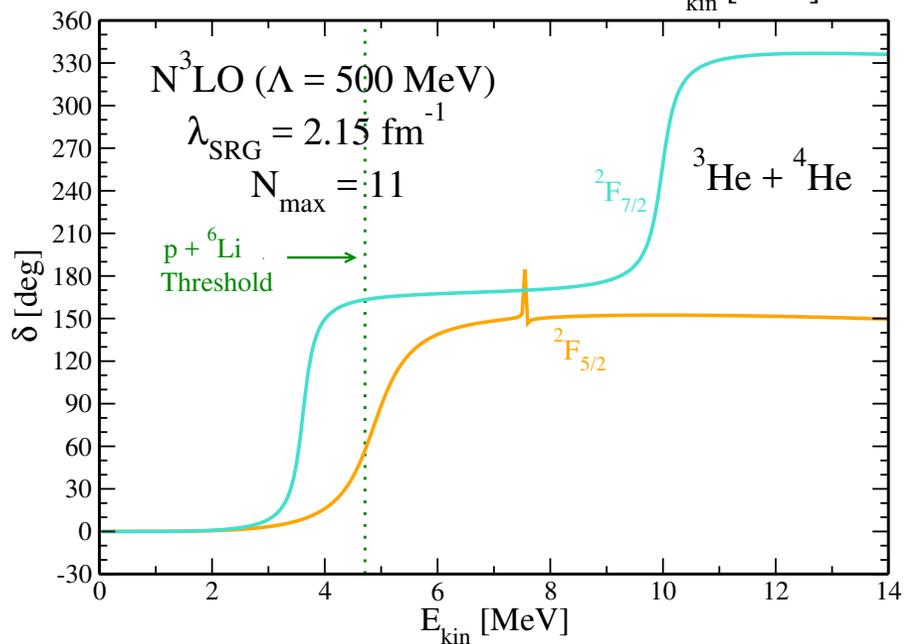
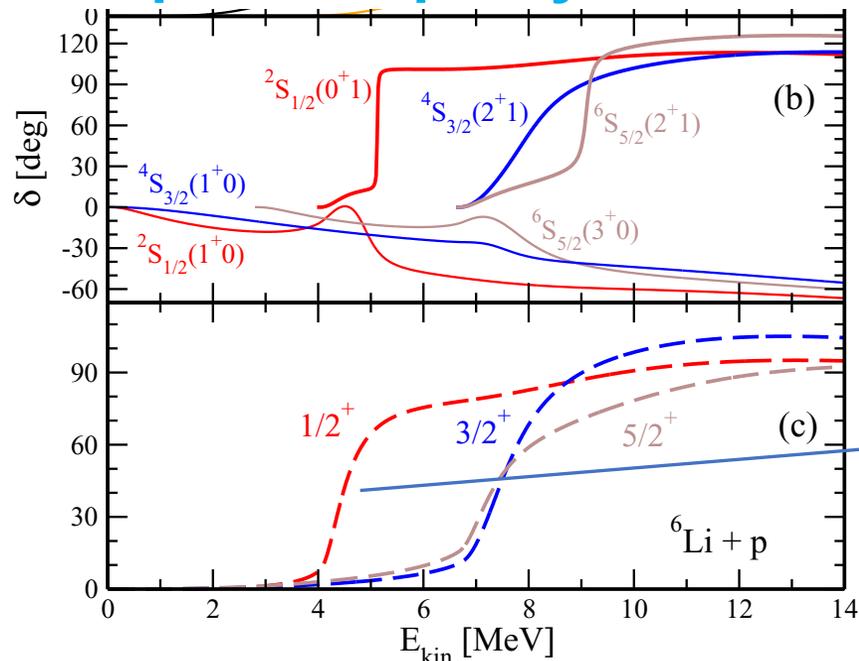
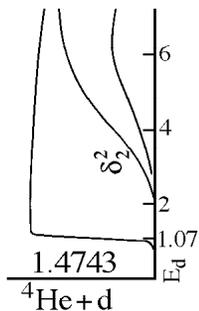
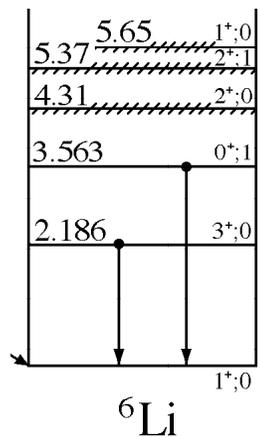


A drop in the $^6\text{Li}(p, \gamma)^7\text{Be}$ reaction at low energies



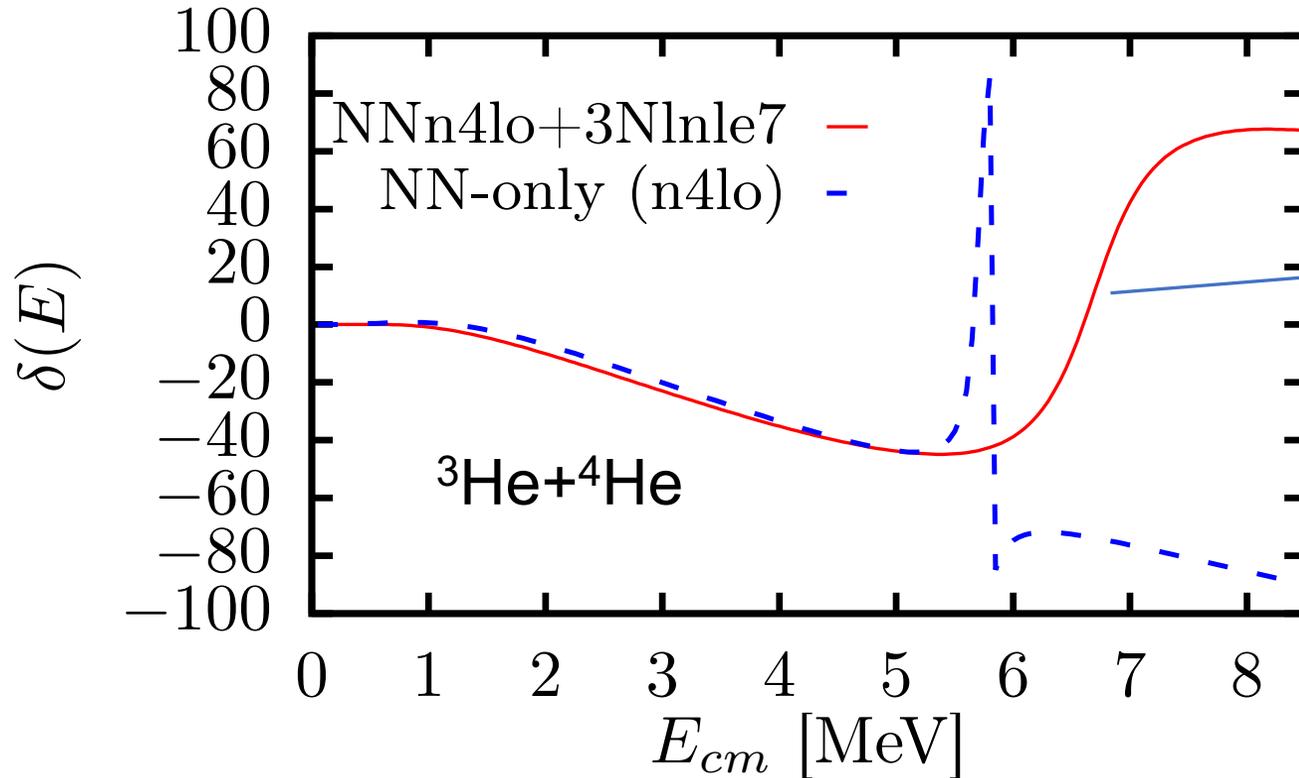
J.J. He^{a,*}, S.Z. Chen^{a,b}, C.E. Rolfs^{c,a}, S.W. Xu^a, J. Hu^a, X.W. Ma^a, M. Wiescher^d, R.J. deBoer^d, T. Kajino^{e,f}, M. Kusakabe^g, L.Y. Zhang^{a,b}, S.Q. Hou^{a,b}, X.Q. Yu^a, N.T. Zhang^a, G. Lian^h, Y.H. Zhang^a, X.H. Zhou^a, H.S. Xu^a, G.Q. Xiao^a, W.L. Zhan^a

${}^7\text{Be}$ – New positive-parity states

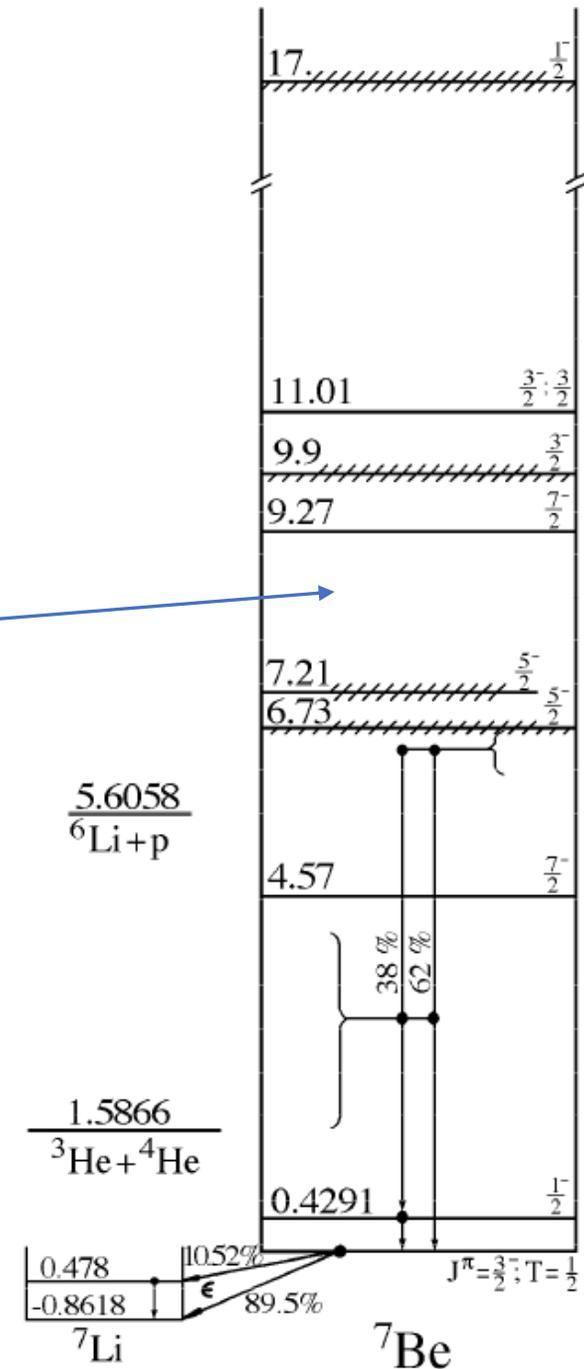


${}^7\text{Be}$ – New positive-parity states

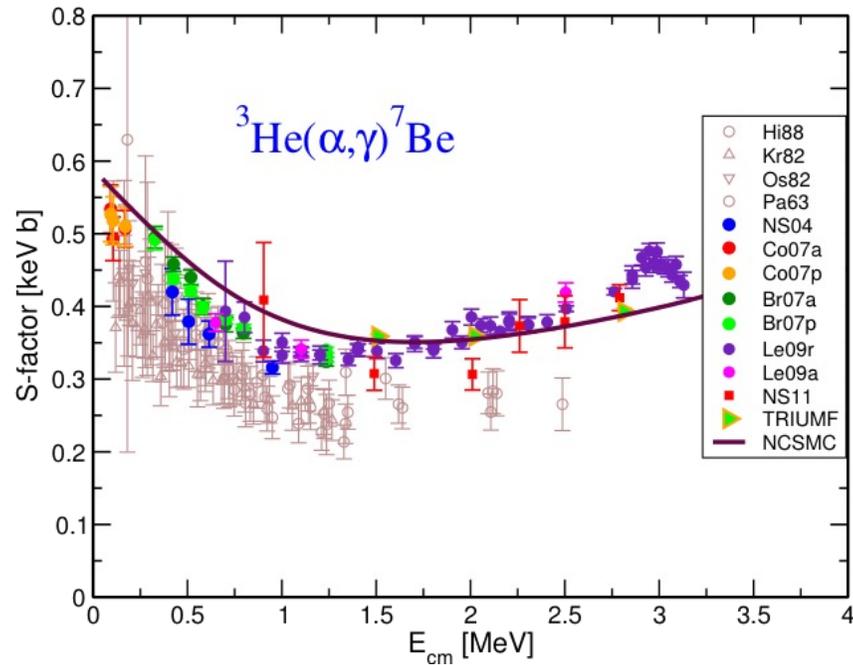
$$N_{max} = 10, \hbar\omega = 20 \text{ MeV}, \lambda = 2.0 \text{ fm}^{-1}$$



Preliminary – in progress



S-factor for ${}^3\text{He}(\alpha,\gamma){}^7\text{Be}$ and ${}^6\text{Li}(p,\gamma){}^7\text{Be}$ reaction



Physics Letters B 757 (2016) 430–436

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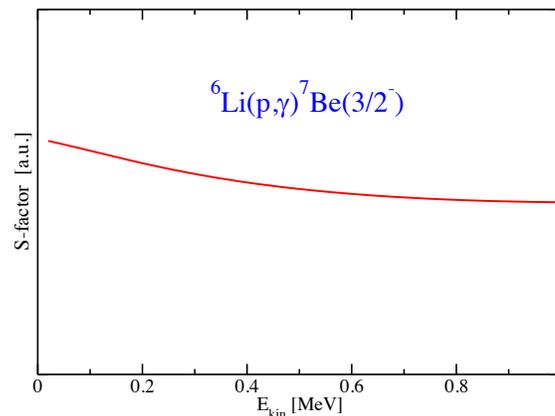
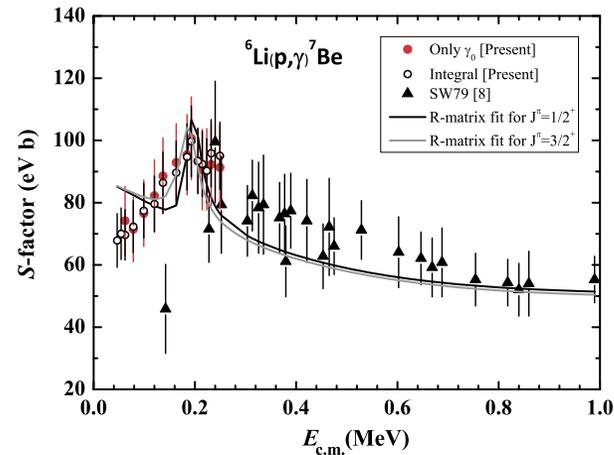
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PHYSICAL REVIEW C 100, 024304 (2019)

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A drop in the ${}^6\text{Li}(p,\gamma){}^7\text{Be}$ reaction at low energies



J.J. He^{a,*}, S.Z. Chen^{a,b}, C.E. Rolfs^{c,a}, S.W. Xu^a, J. Hu^a, X.W. Ma^a, M. Wiescher^d, R.J. deBoer^d, T. Kajino^{e,f}, M. Kusakabe^g, L.Y. Zhang^{a,b}, S.Q. Hou^{a,b}, X.Q. Yu^a, N.T. Zhang^a, G. Lian^h, Y.H. Zhang^a, X.H. Zhou^a, H.S. Xu^a, G.Q. Xiao^a, W.L. Zhan^a

No resonance in ${}^7\text{Be}$ close to ${}^6\text{Li}+p$ threshold contrary to claim in Lanzhou experiment

Still, we predict a $1/2^+$ resonance at ~ 3 MeV above ${}^6\text{Li}+p$ threshold

Need to couple all mass partitions to get a reliable prediction of its properties