

ECT* Workshop

“Critical stability of few-body quantum systems”

October 23-27, 2023, Trento (Italy)

Large scattering lengths & Four-neutron correlations



F. Miguel Marqués





- ▶ Scattering lengths:
 - neutron off exotic ‘containers’
 - $^{17}\text{B}+\text{n}$: a shocking case!
- ▶ Experimental program @ RIKEN:
 - stat. & acceptance: effective range
 - multi-channel: determine (a_s, r_e) !
 - Universality ($|a_s|/r_e \sim 100$)



- ▶ Tetraneutron “signal”!
 - resonance / spatial correlations?
 - link to momentum correlations?
- ▶ Experimental program @ RIKEN:
 - first 4n invariant masses
 - some low-energy structures
 - explore full kinematics...



📄 Emeline Oliveira, PhD



📄 Audrey Anne, PhD

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► Low-energy scattering :

$$\varphi_k(r) \approx \frac{\sin(kr + \delta_0)}{kr}, \quad k = \sqrt{2\mu E} \quad (1)$$

$$\sigma(k) = 4\pi \frac{\sin^2(\delta_0)}{k^2} \quad (2)$$

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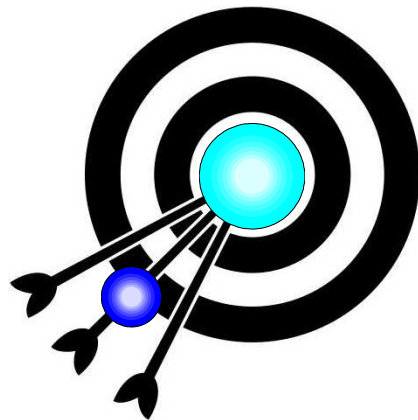
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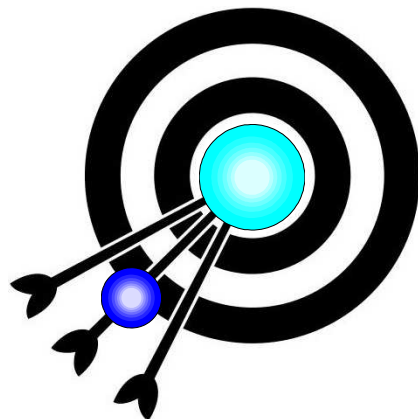
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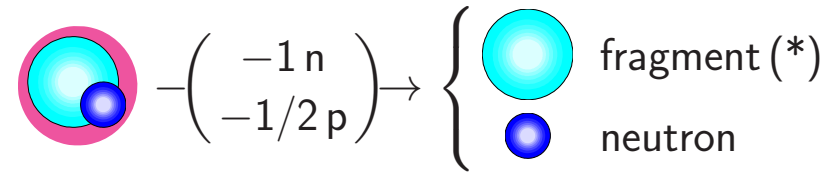
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- ✓ neutrons are neutral
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- ✗ exotic nuclei (& neutrons) are unstable

• knockout reactions :



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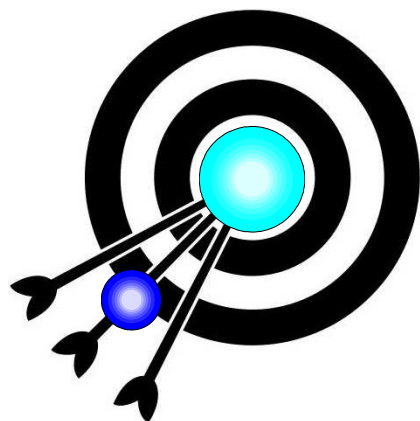
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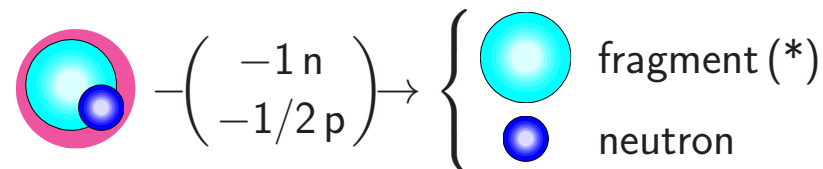
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• halo nuclei : Bertsch, PRC 57 (1998) 1366

$$\psi_i(r) \approx e^{-\alpha r} / r, \quad \alpha = \sqrt{2\mu_i S_n} \quad (5)$$

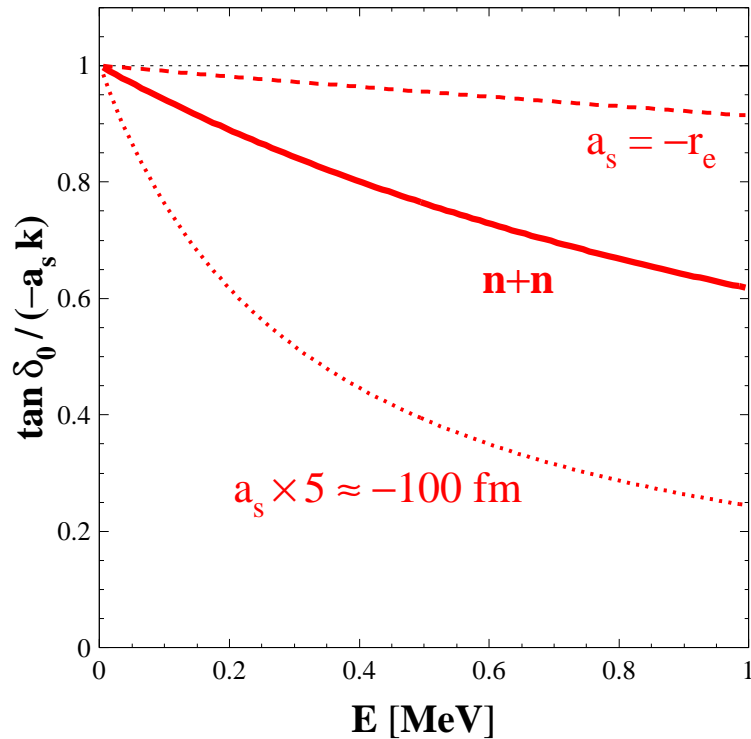
$$\sigma(k) \approx \left(\cos \delta_0 + \frac{\alpha}{k} \sin \delta_0 \right)^2 \frac{k}{(\alpha^2 + k^2)^2} \quad (6)$$

⇒ $\sigma(k) = (2/4/6)$ & $\delta_0 = (3)$

► Effective-range (k^2) term ?

$$\frac{-a_s k}{\tan \delta_0} = 1 - \frac{a_s r_e}{2} k^2 + \mathcal{O}(k^4)$$

n+n $\begin{cases} a_s = -18.5 \text{ fm} \\ r_e = 2.8 \text{ fm} \end{cases}$

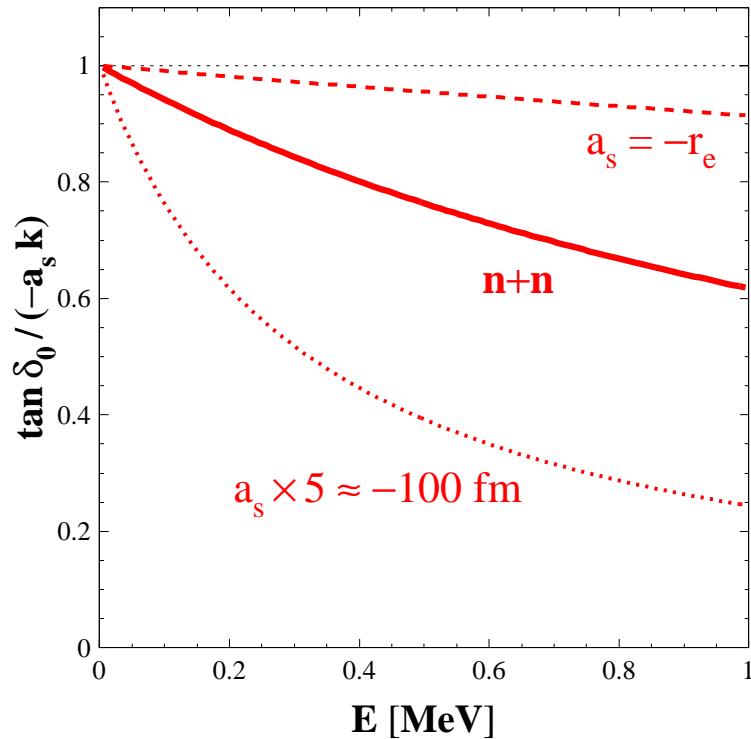


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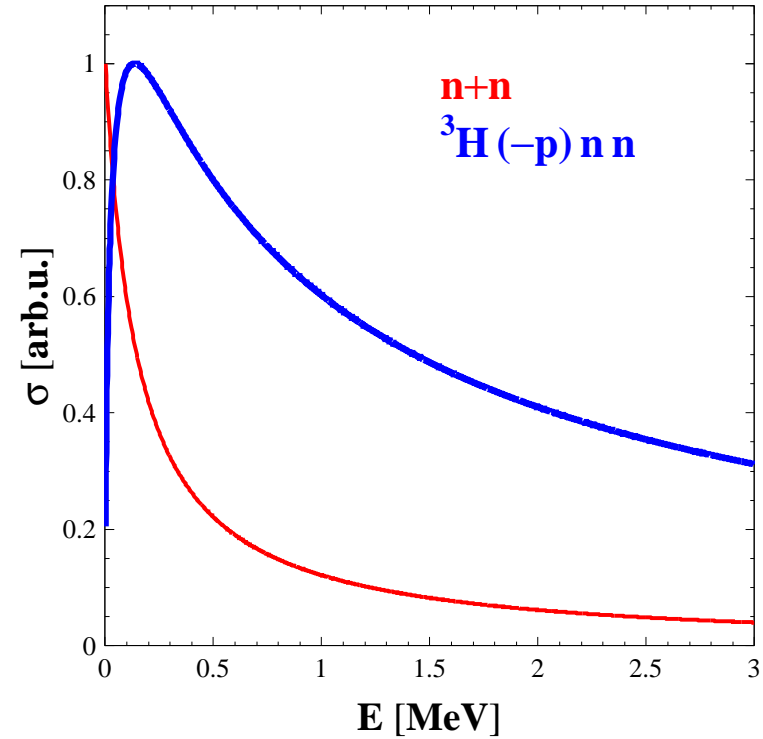
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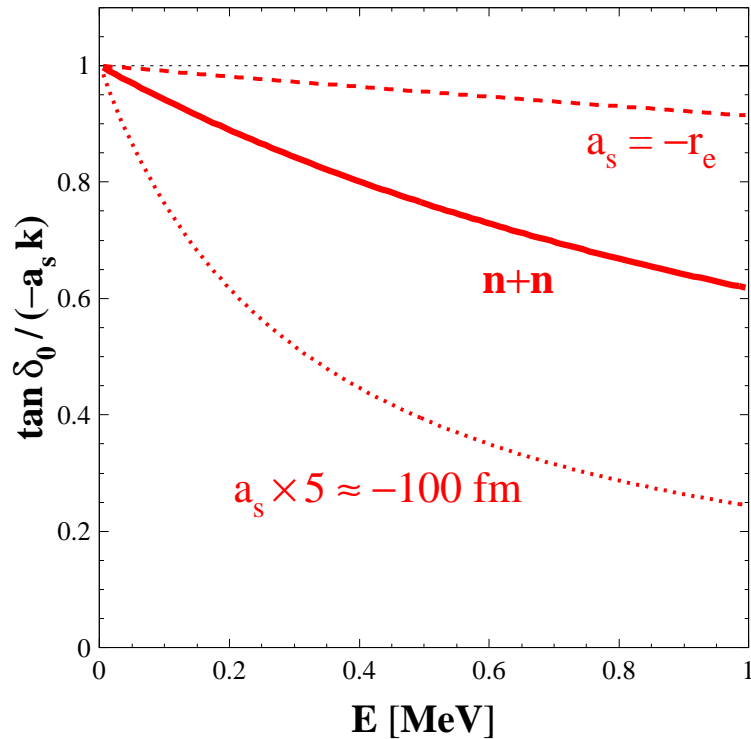
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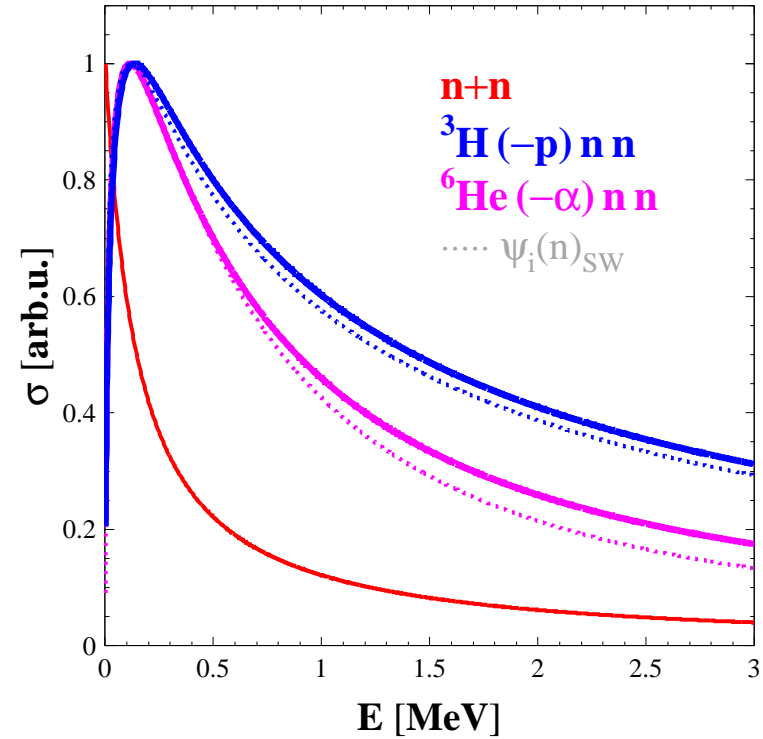
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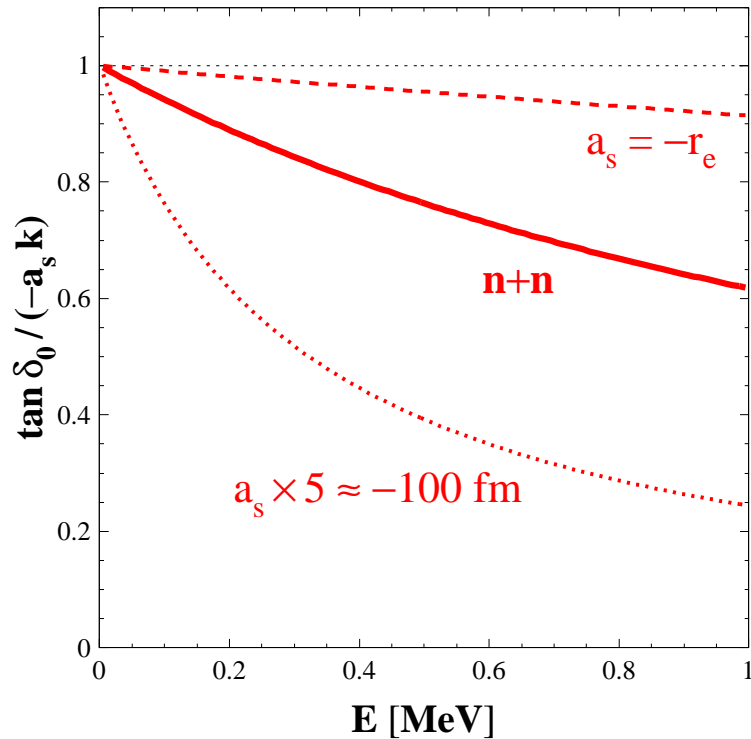
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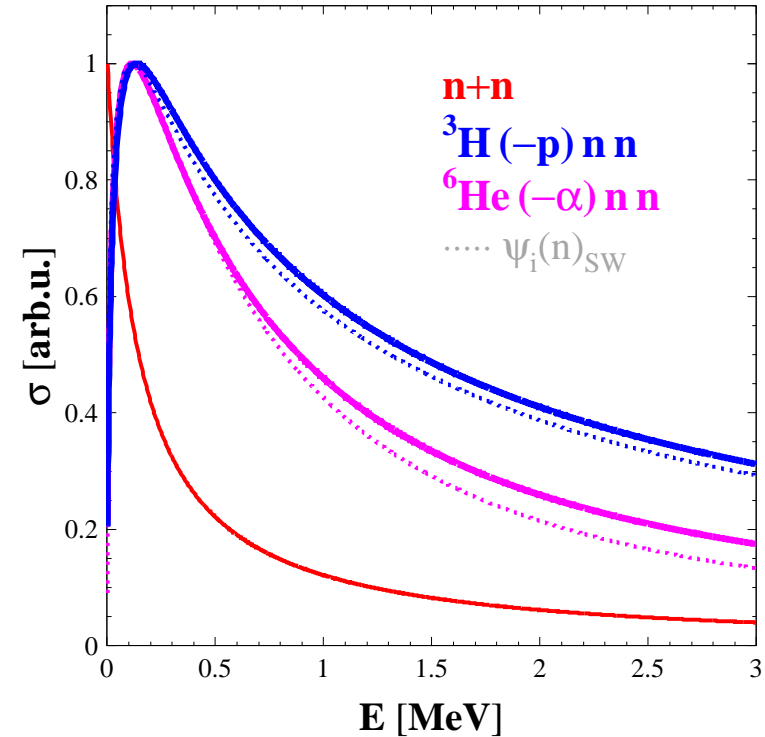
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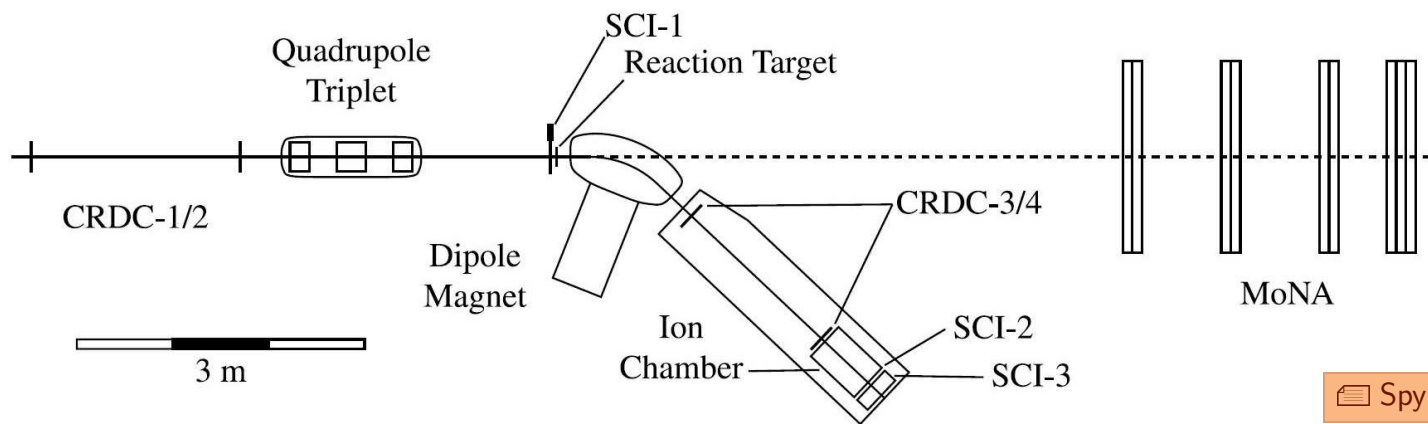


► $n+(A>1)$: Carbonell, SciPost Phys Proc 3 (2020) 008

- attractive n-N / n-A Pauli repulsion
- $|a_s| \sim r_e$ progressively from + to - ...

⇒ until Z=5: ${}^{18}_5\text{B}$!!!

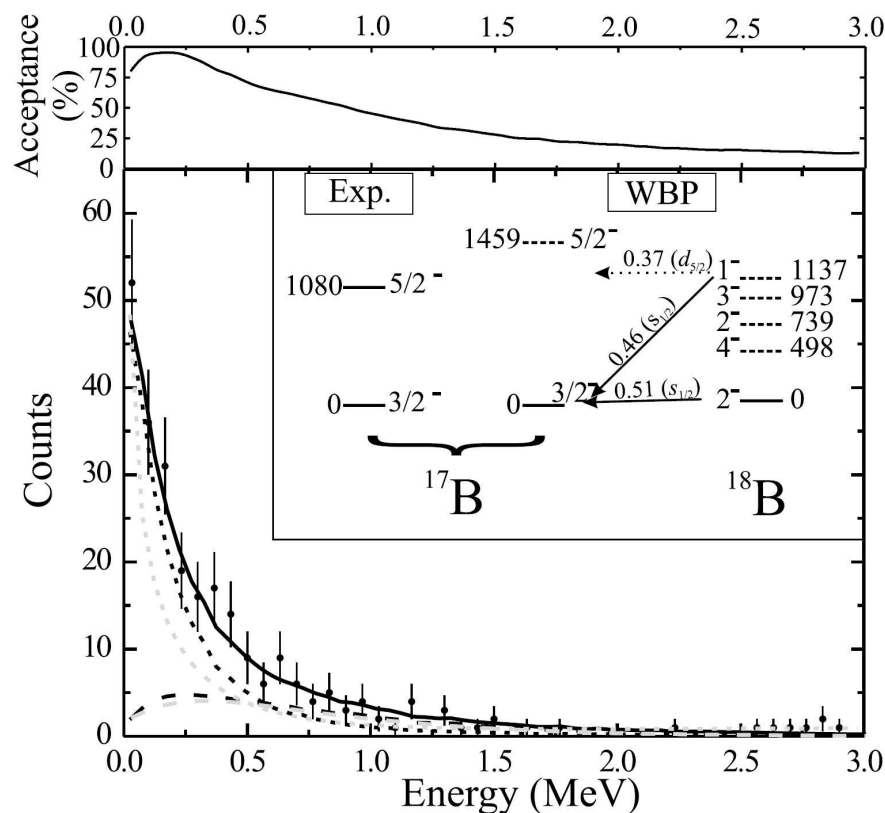
Boron 18: only a limit is known



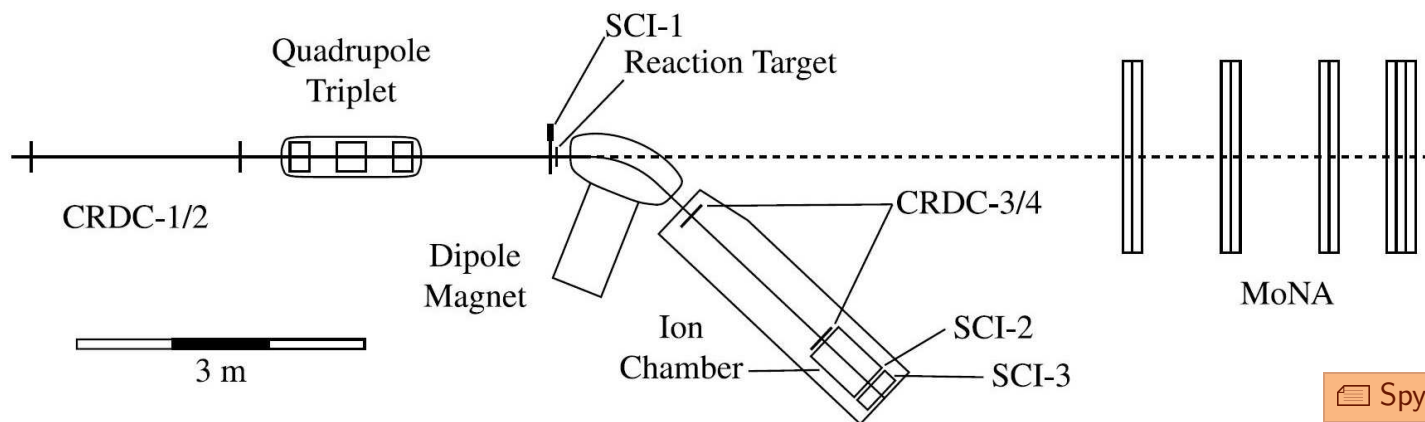
☞ Spyrou, PLB 683 (2010) 129

▶ $^{19}\text{C} (\text{Be}, -1p) ^{18}_5\text{B}$ @ 62 MeV/N:

✓ first evidence of $^{17}\text{B} + n$ virtual state



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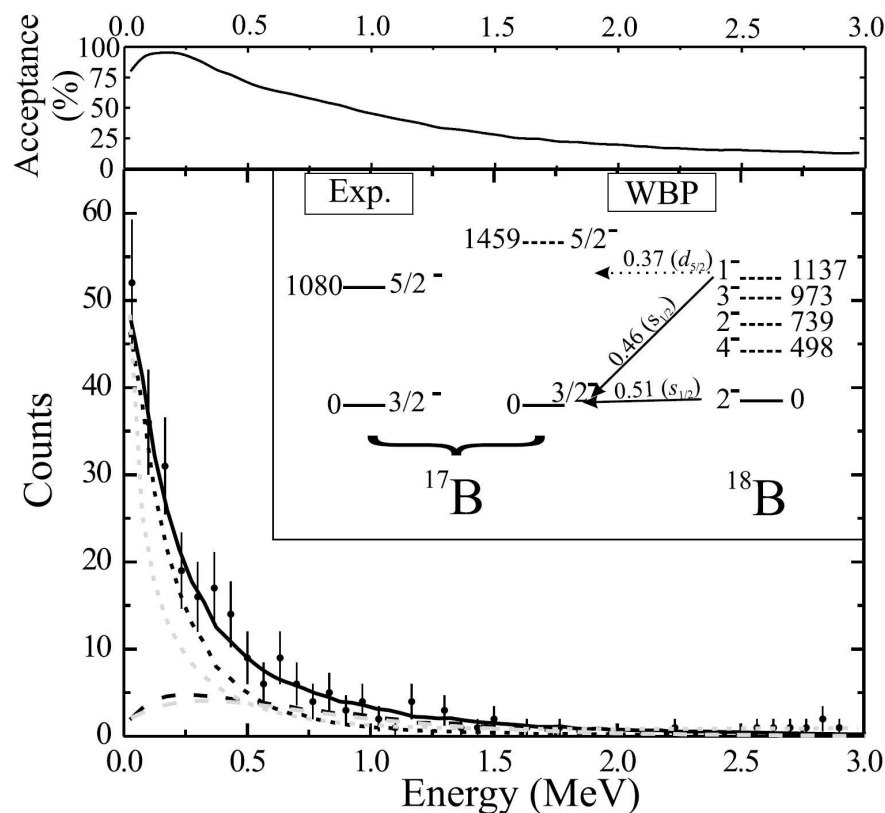


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- ✓ first evidence of $^{17}\text{B}+n$ **virtual state**
- ✗ $E(^{17}\text{B}+n)$ only below ~ 1 MeV
- ✗ insensitive to r_e
- ✗ insensitive to lower bound on a_s
- ✗ ad-hoc “non-resonant” Maxwellian ...


⇒ $a_s(^{17}\text{B}+n) < -50$ fm



► Efimov effect:

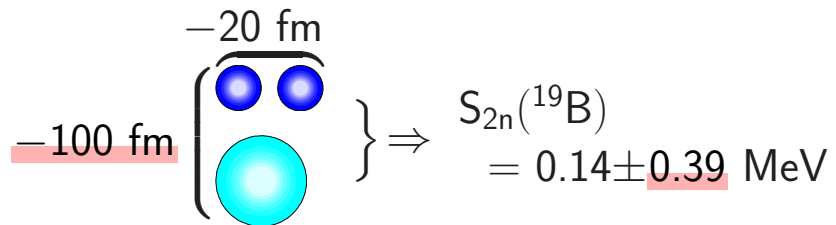
“a scale-invariant 3-body attraction”

📖 Naidon, Rep Prog Phys 80 (2017) 056001

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- Borromean binding ()

● Efimov physics:

- Universality if $|a_s| \gg r_e \dots$



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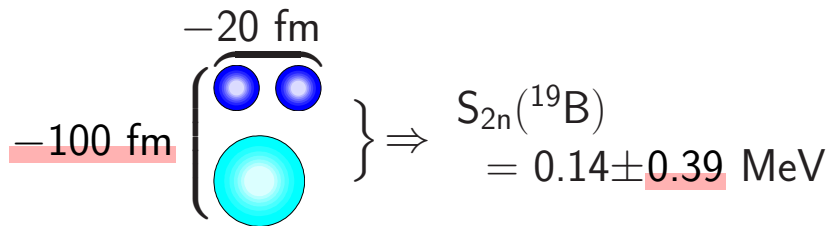
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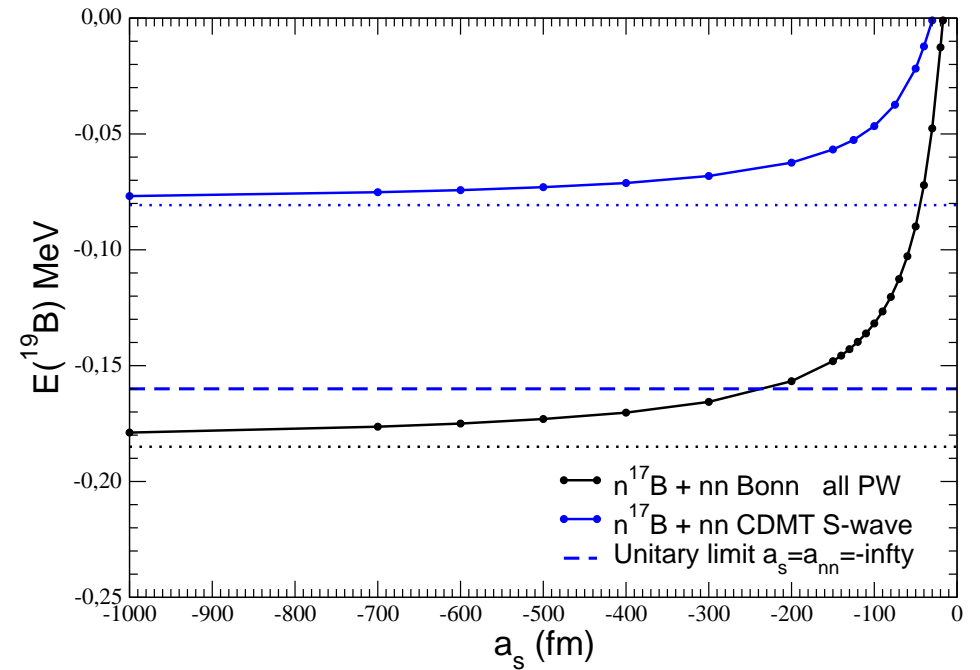
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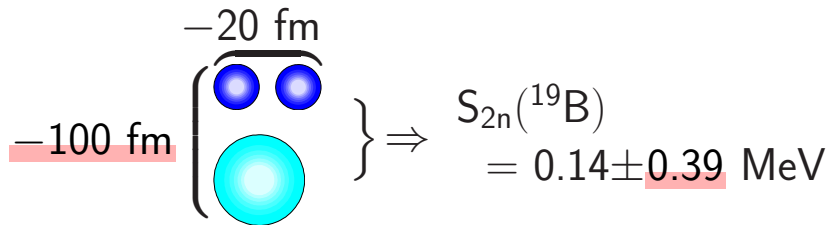
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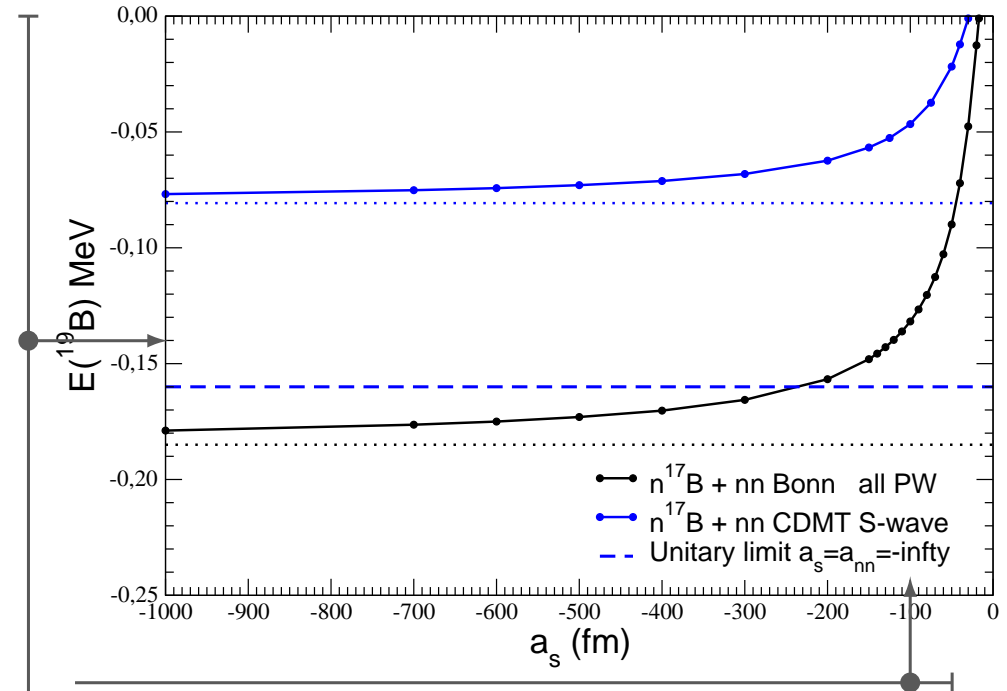
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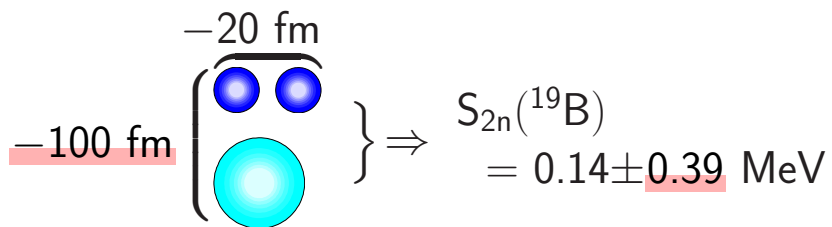
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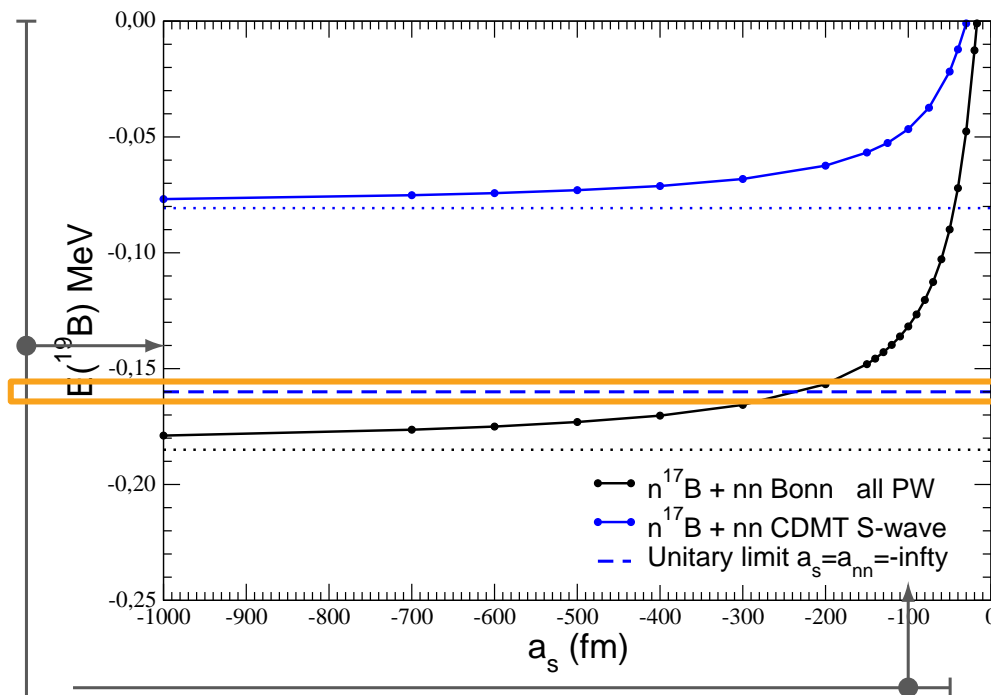
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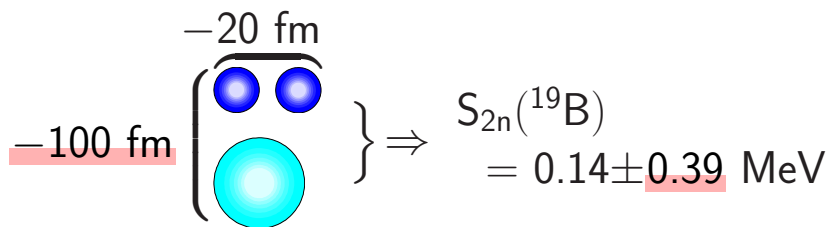
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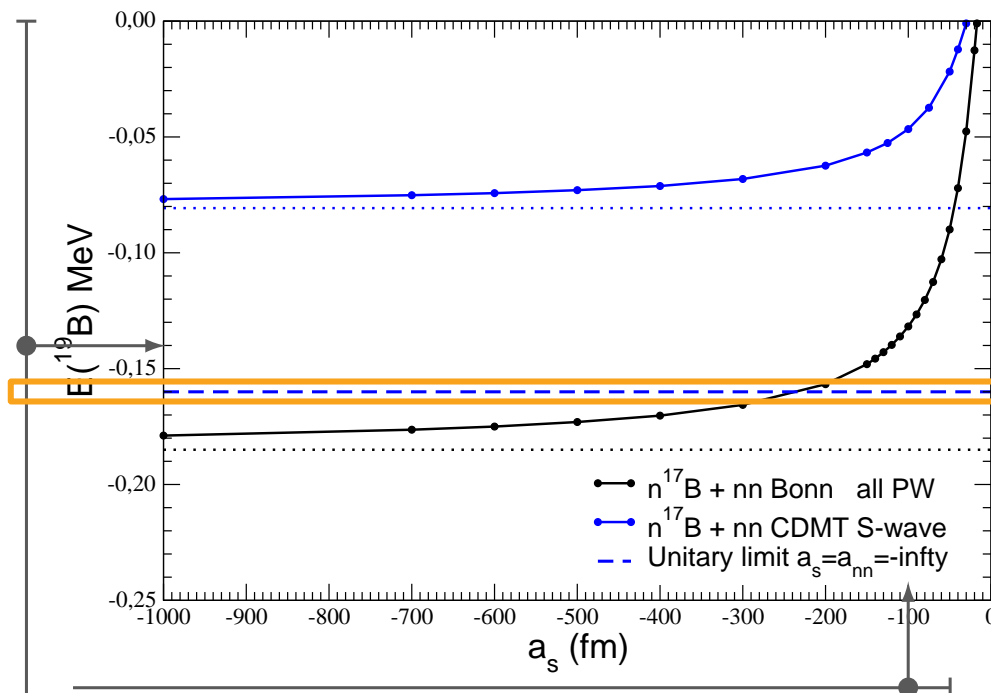
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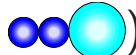
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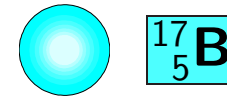


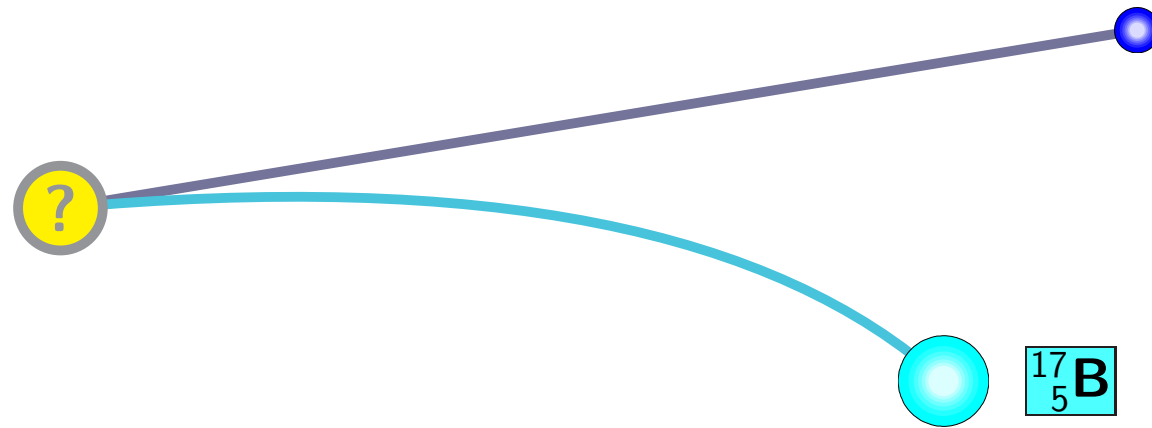
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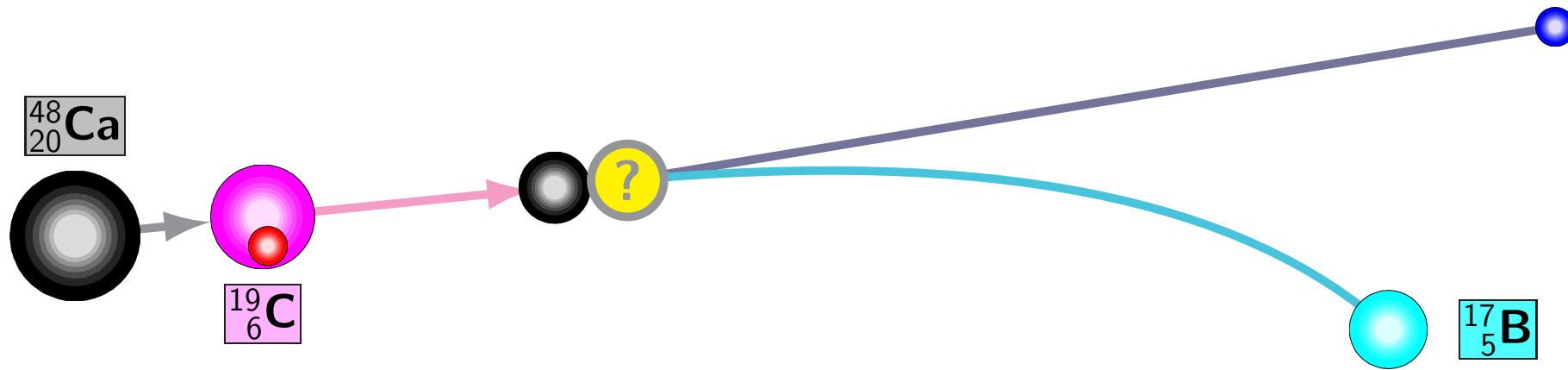
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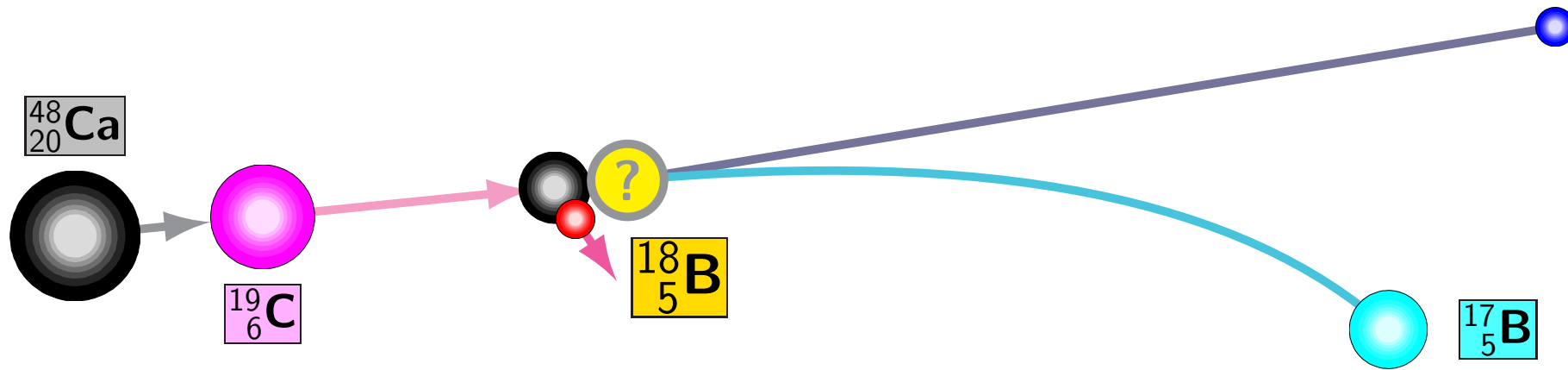


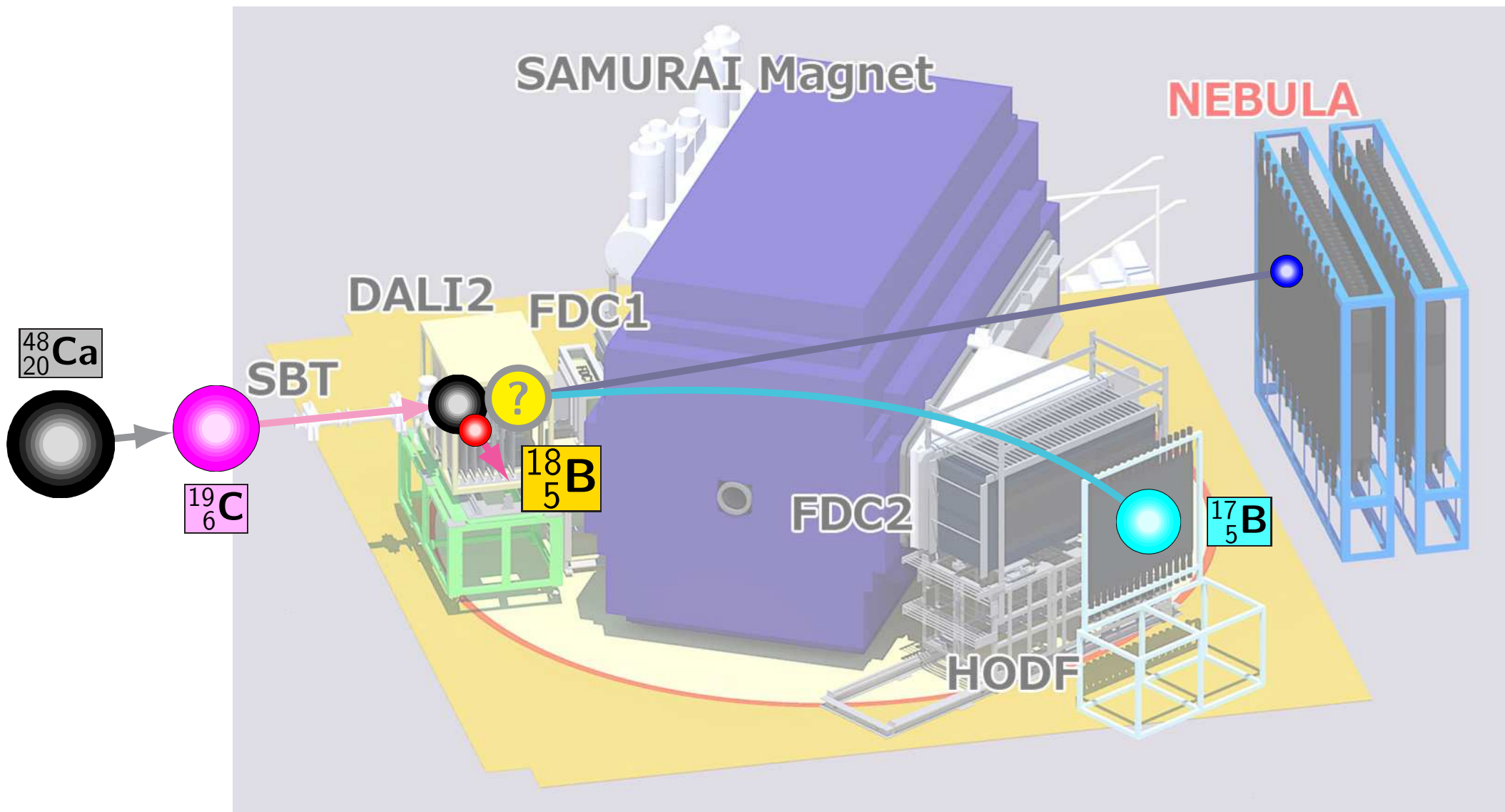
- ✓ ^{19}B bound state & unbound states!
- ✓ good description @ Unitary Limit!
- ✗ other trimers unlikely ($a_s \sim \text{kfm}$ )
- ✓ $|\Psi(r, R)|^2$: molecule-like!
- ✓ only binary inputs (no 3NF)!!!

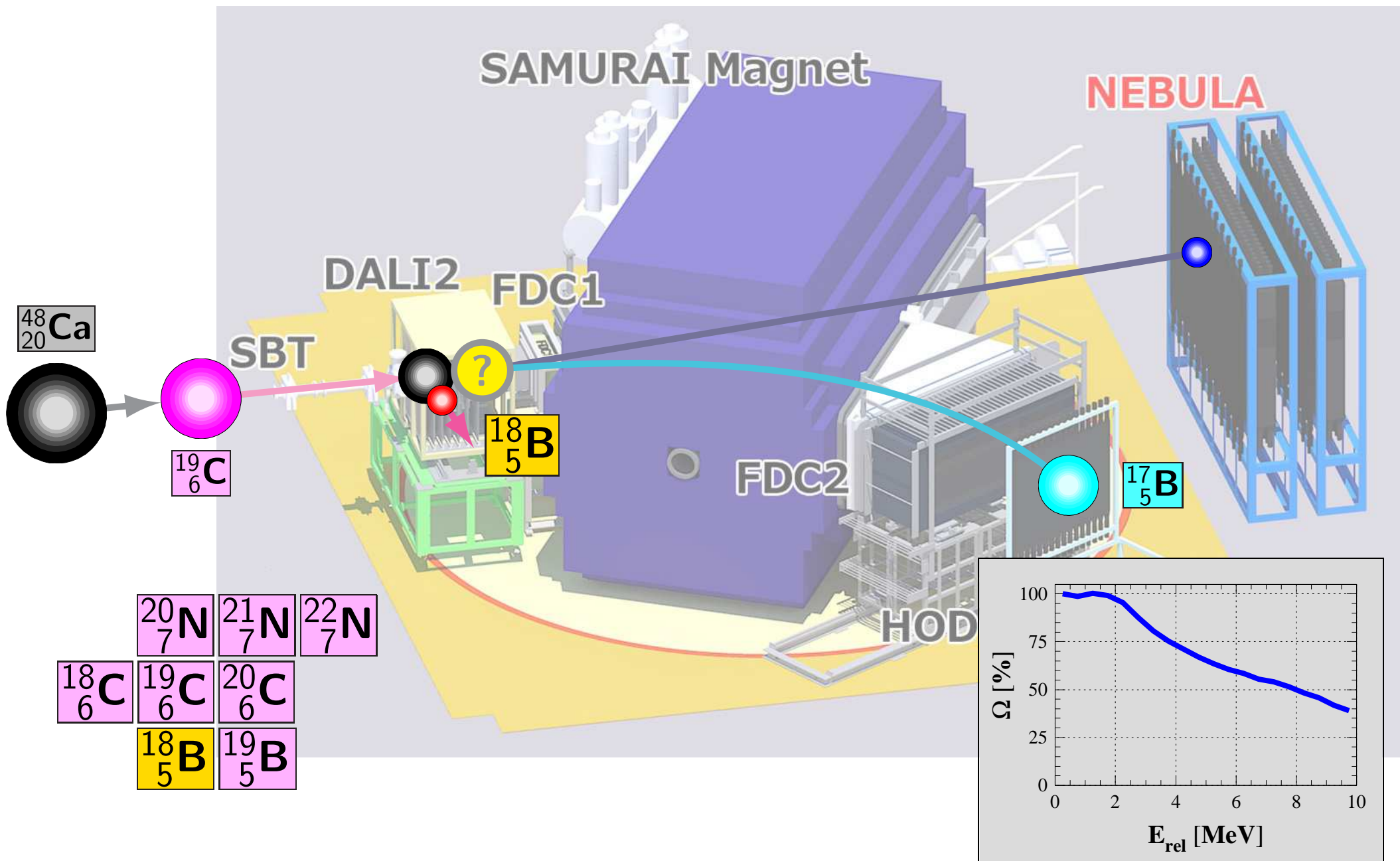




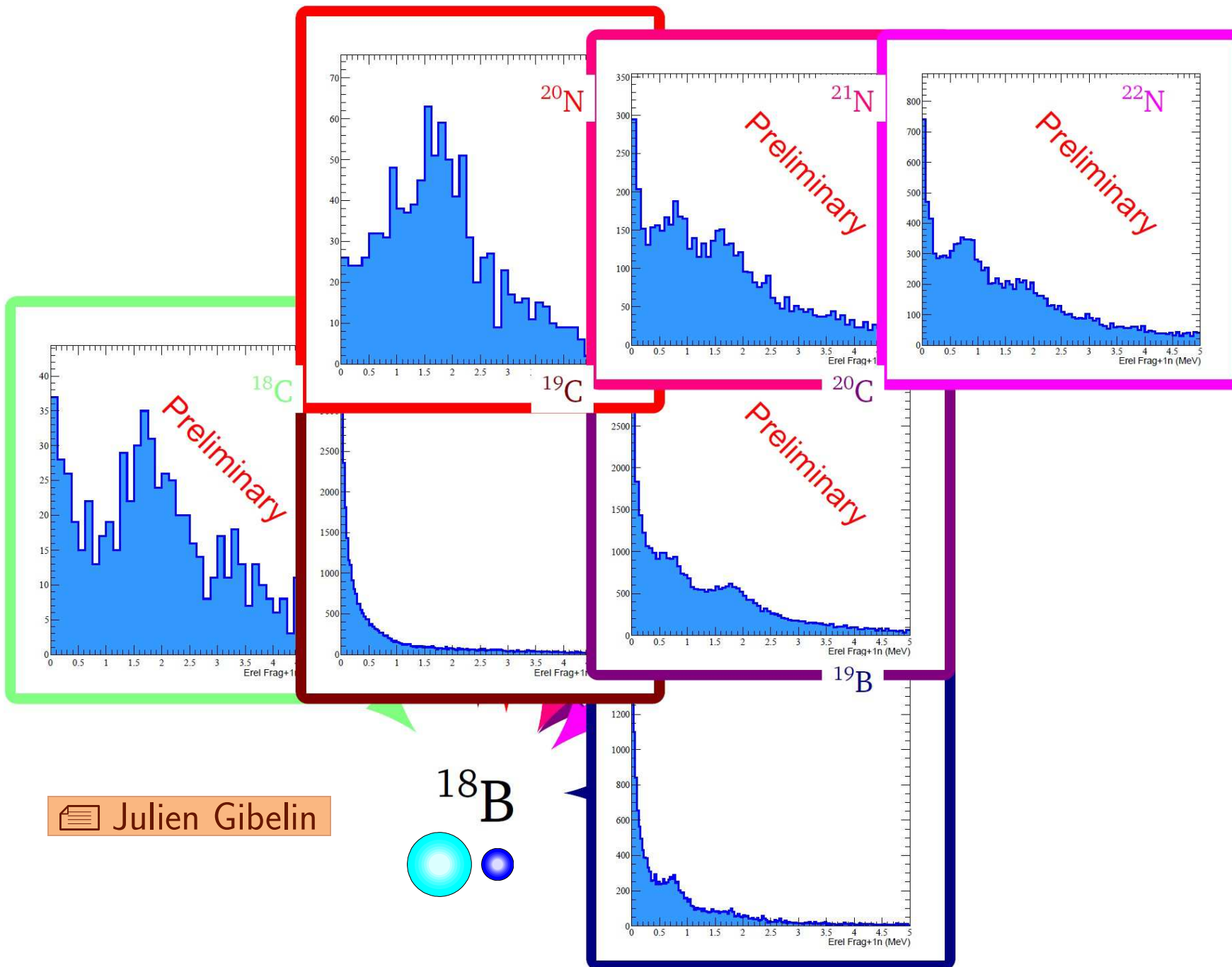




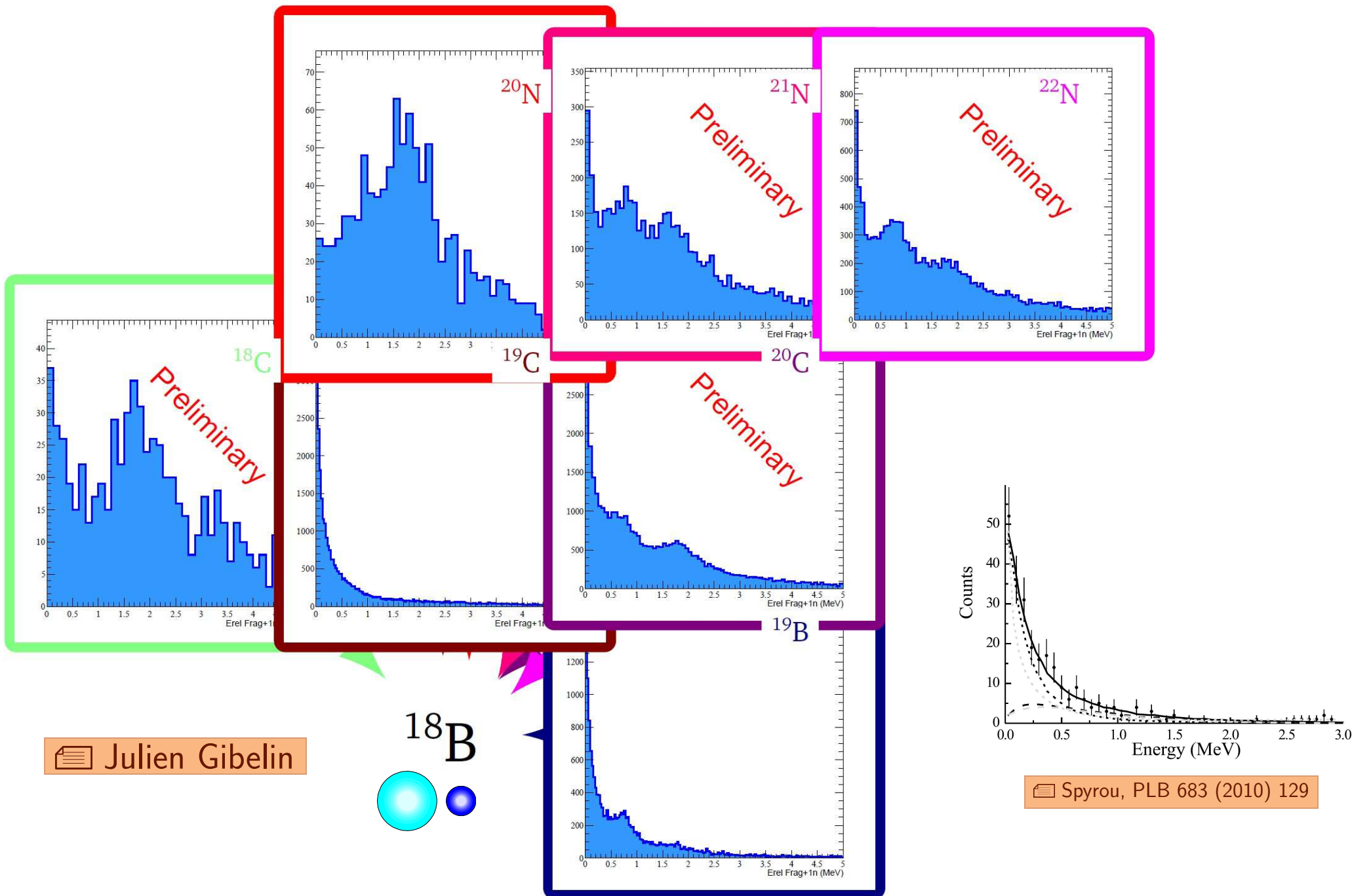


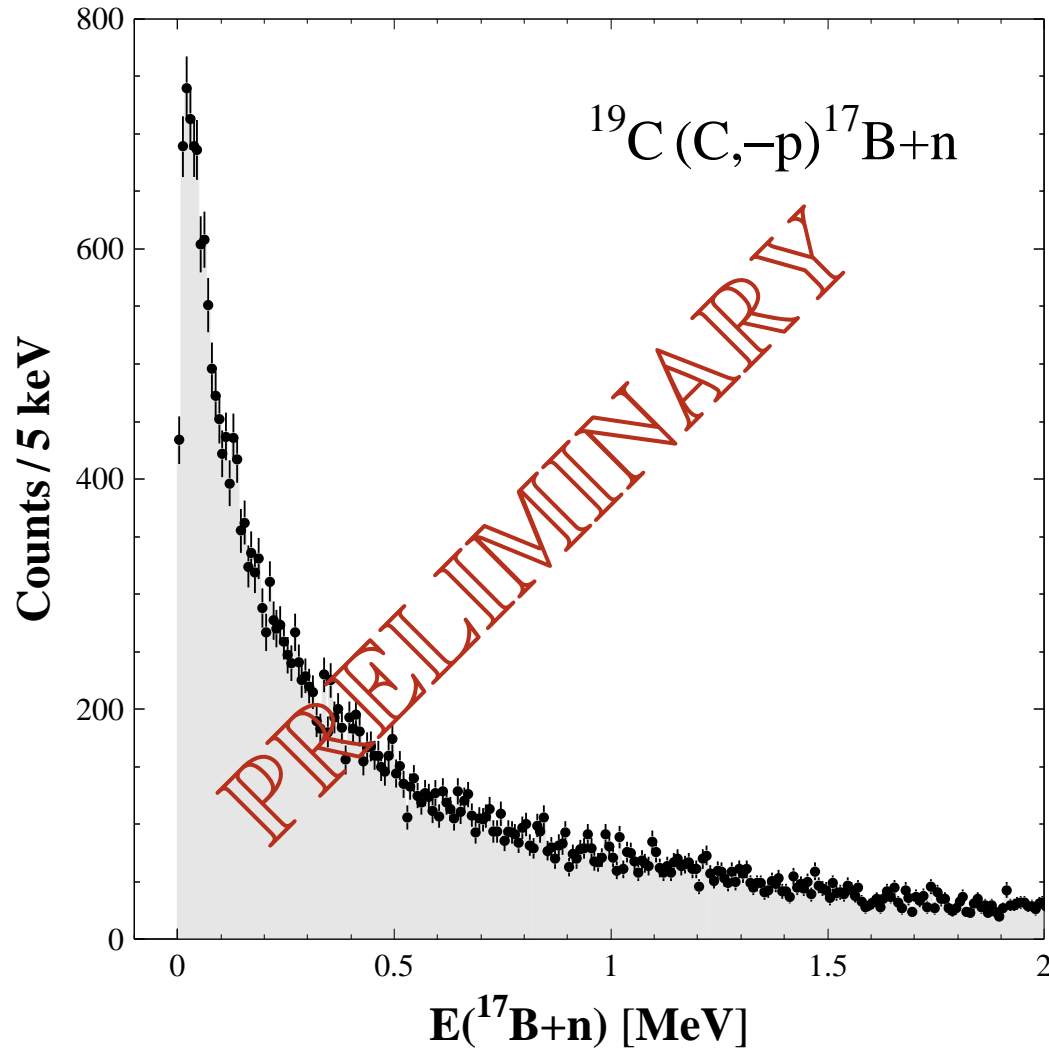


Boron 18: virtual state from 6 channels !



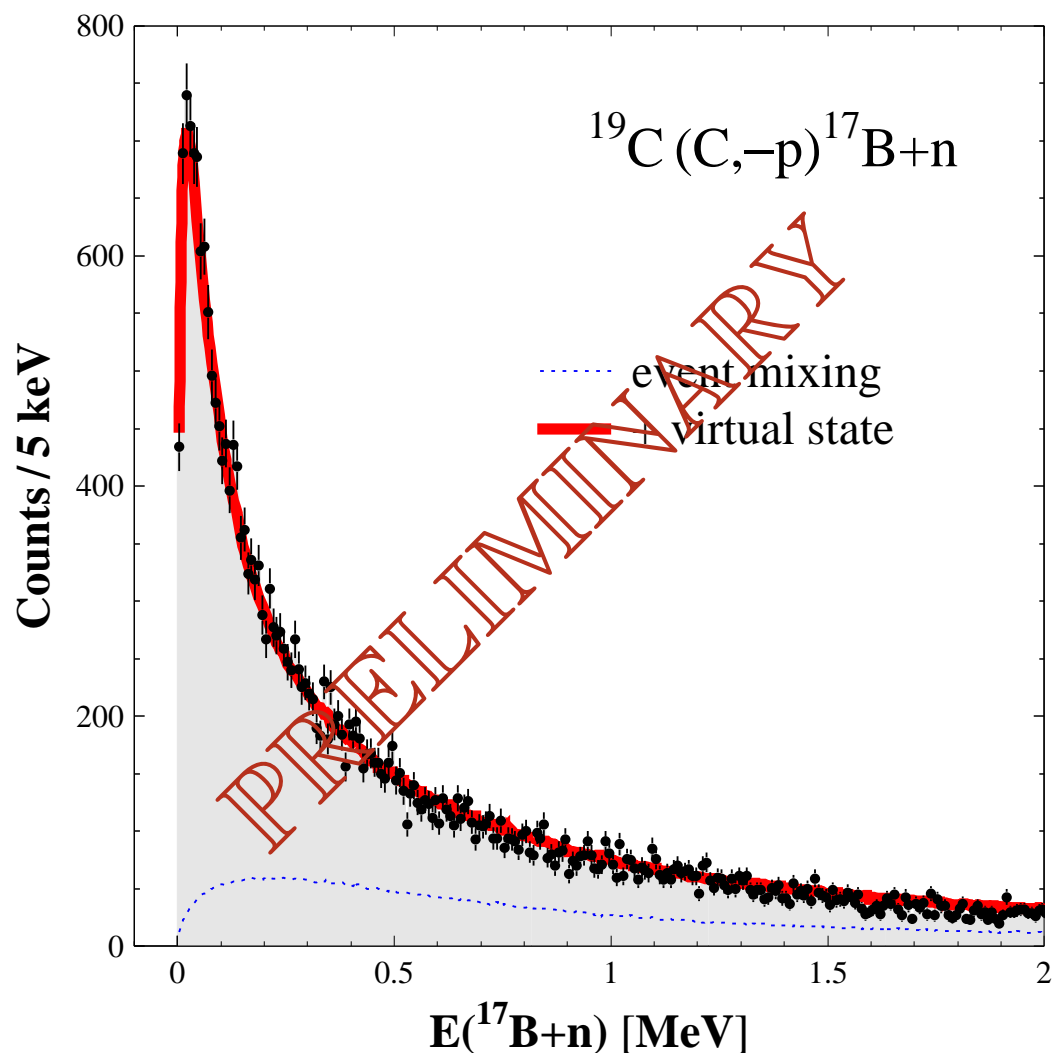
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- ✓ uncorrelated component: event mixing
- ✓ 'pure' population from s-wave halo
- ✓ $S_n(^{19}\text{C}) \sim 0.5$ MeV: asymptotic $\psi_i(\text{n})$

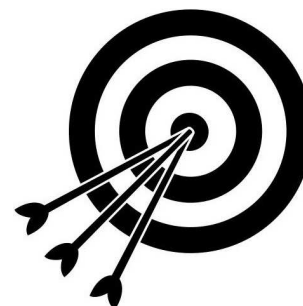


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⇒ very accurate fit for:

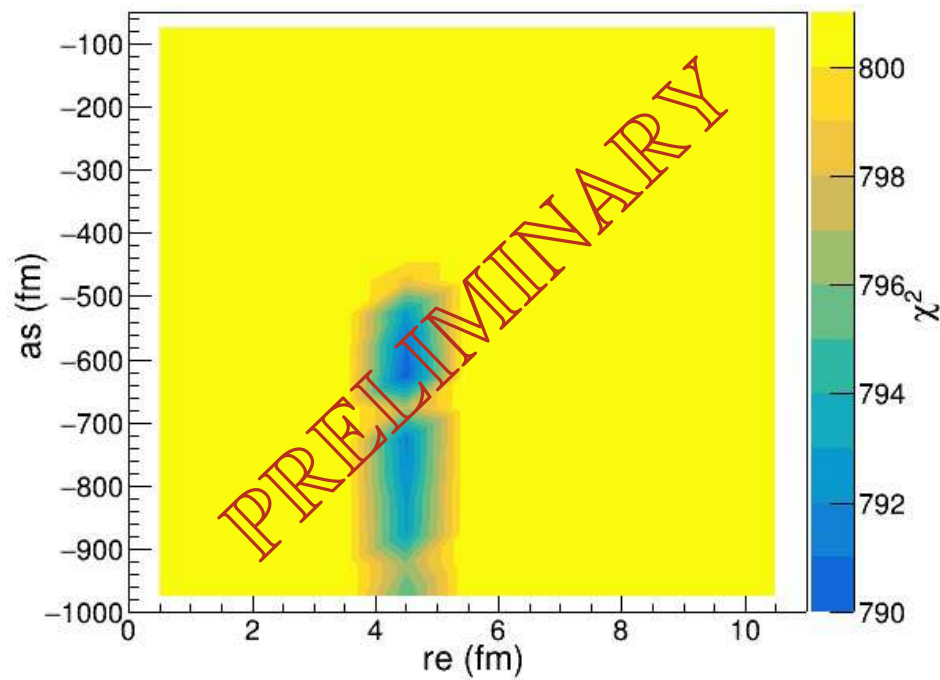
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$\frac{|a_s|}{r_e} = 150$!!!

► $\chi^2(a_s, r_e)$ surface:

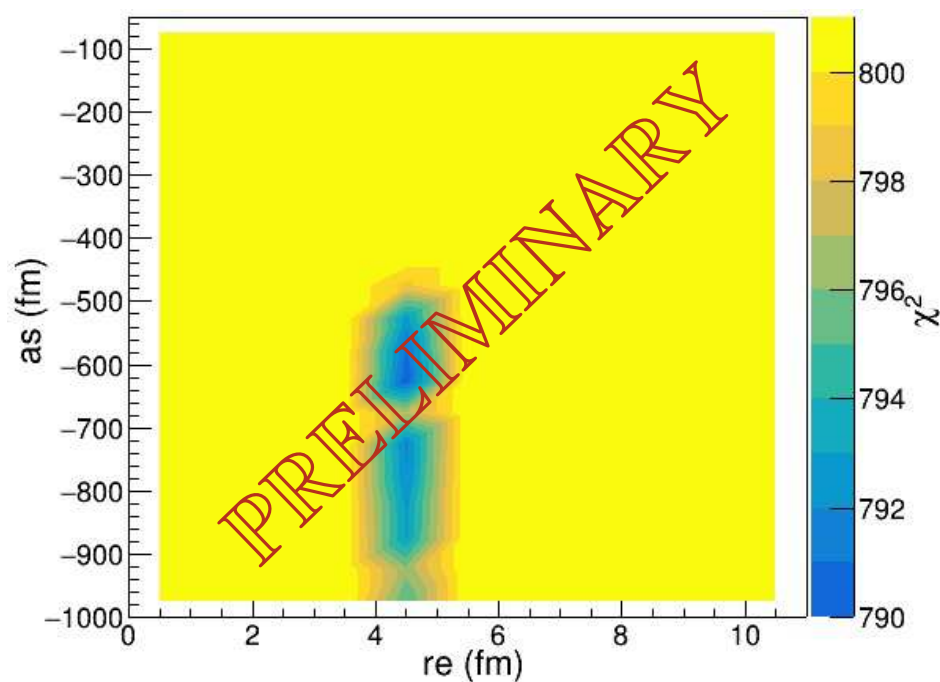
- $^{19}\text{C}(\text{C}, -\text{p})^{17}\text{B} + \text{n}$
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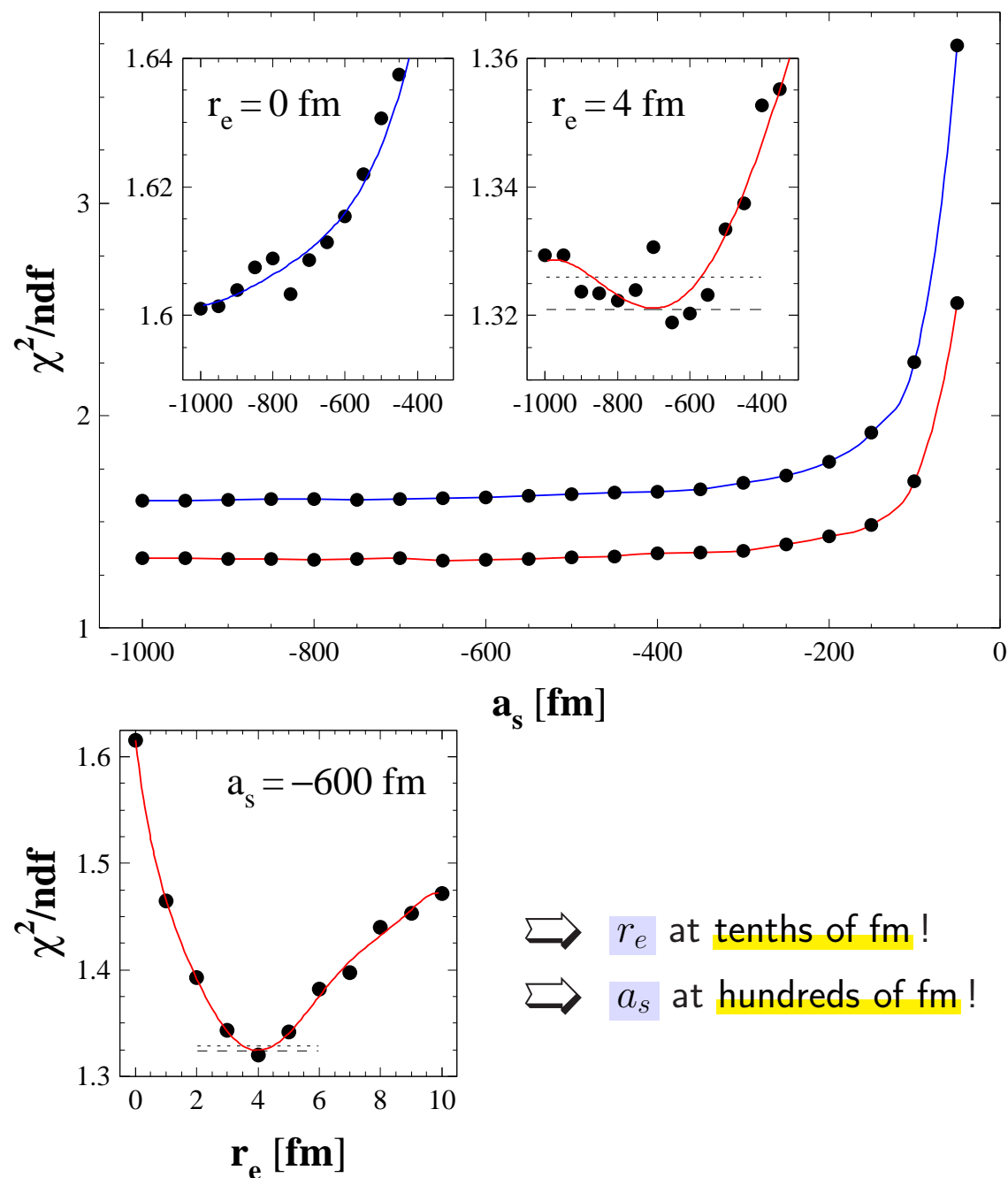
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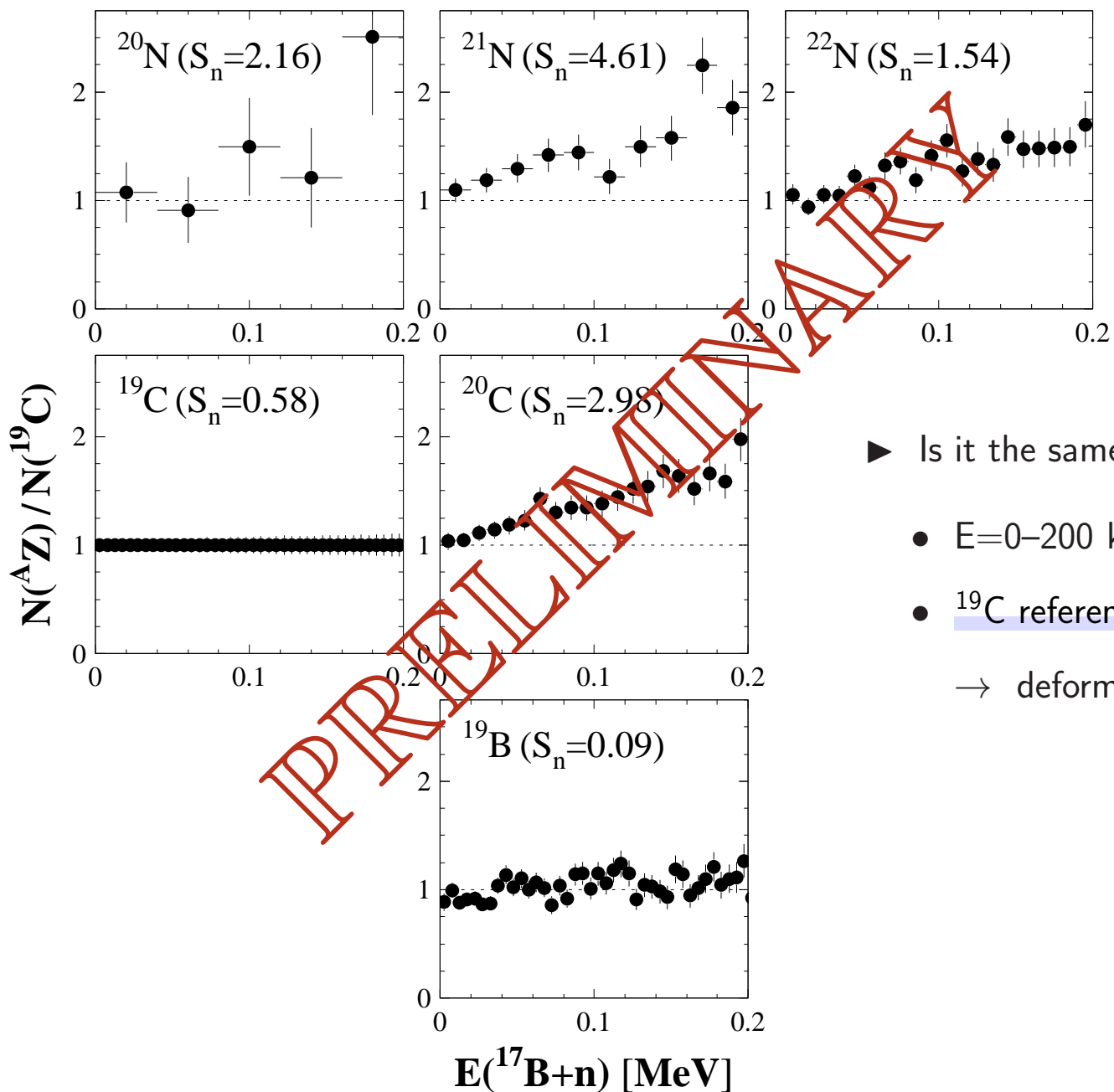
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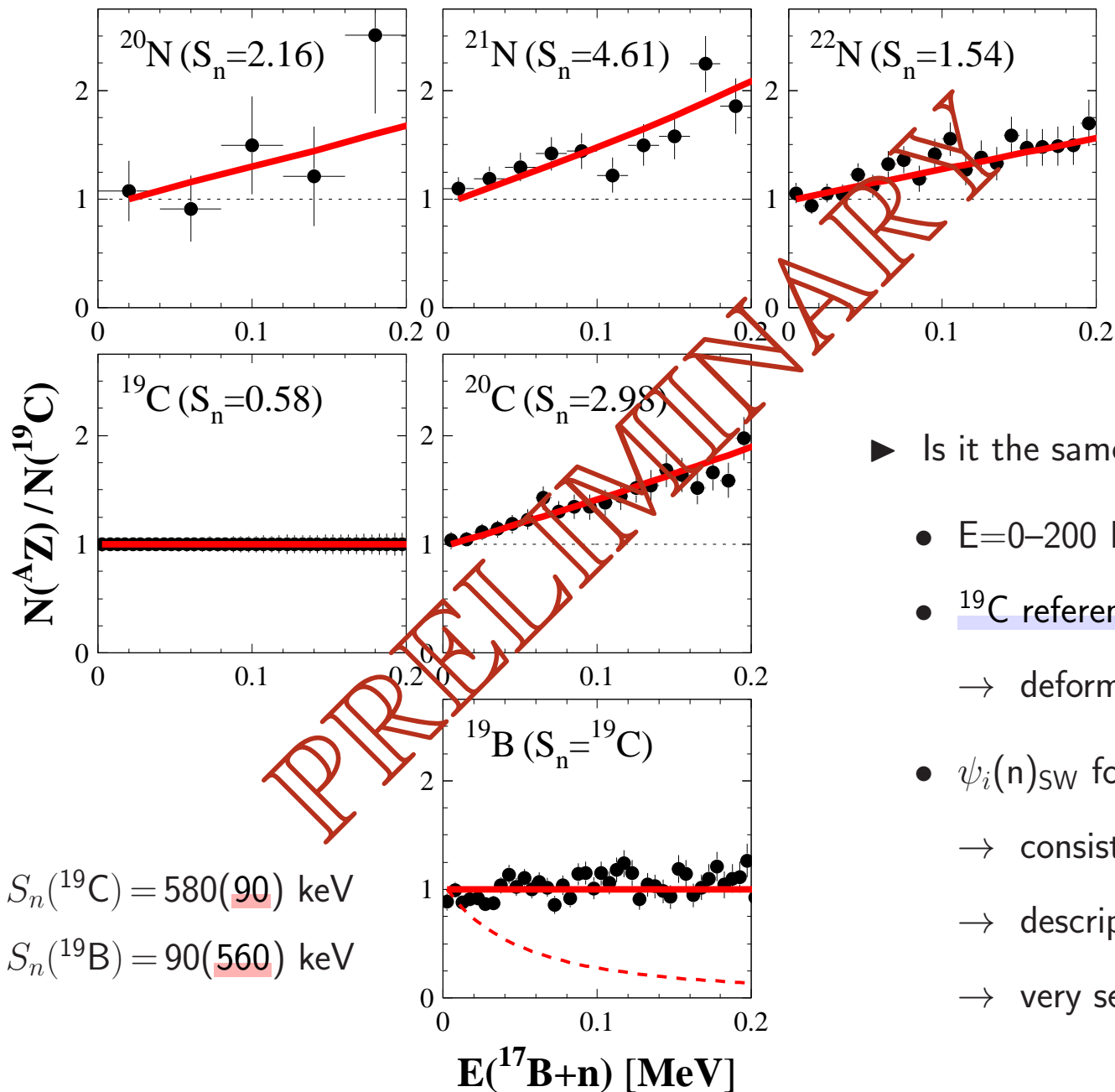




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- ^{19}C reference ('pure' state)
 - deformation increases with S_n
- $\psi_i(n)_{\text{SW}}$ for $(a_s, r_e) = (-600, 4)$ fm
 - consistent with same state !
 - description of container effects
 - very sensitive to $S_n(^{19}\text{B})$!!!

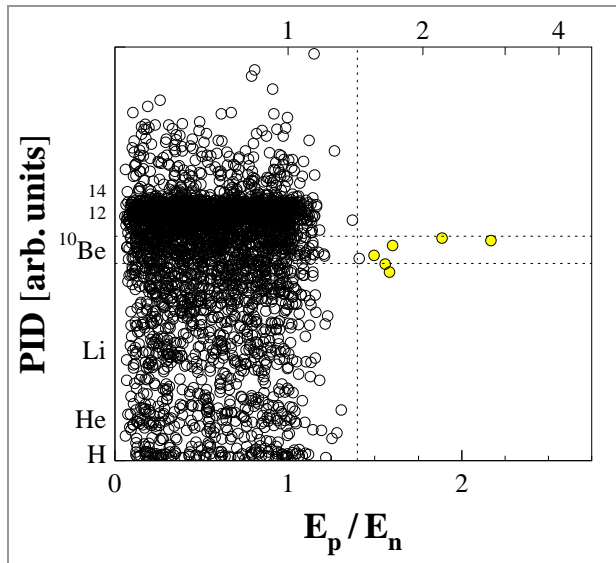


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Confirmation of a 4n “signal”



FMM, PRC 65 (2002) 044006

FMM, arXiv:nucl-ex/0504009

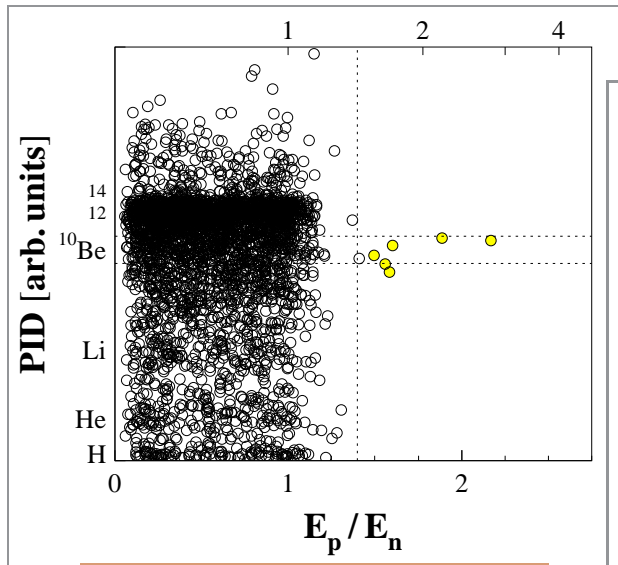
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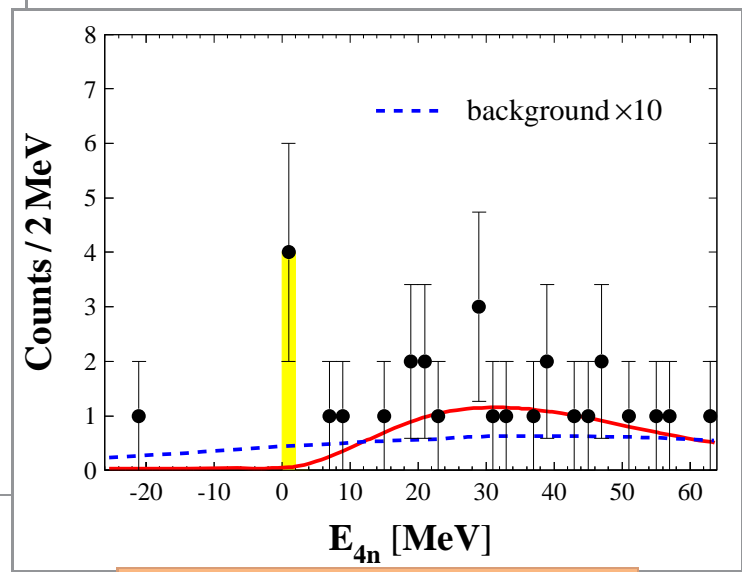
FMM & Carbonell, EPJA 57 (2021) 105



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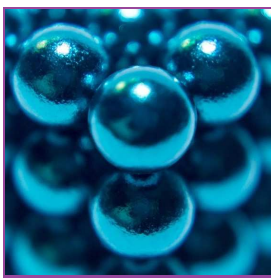
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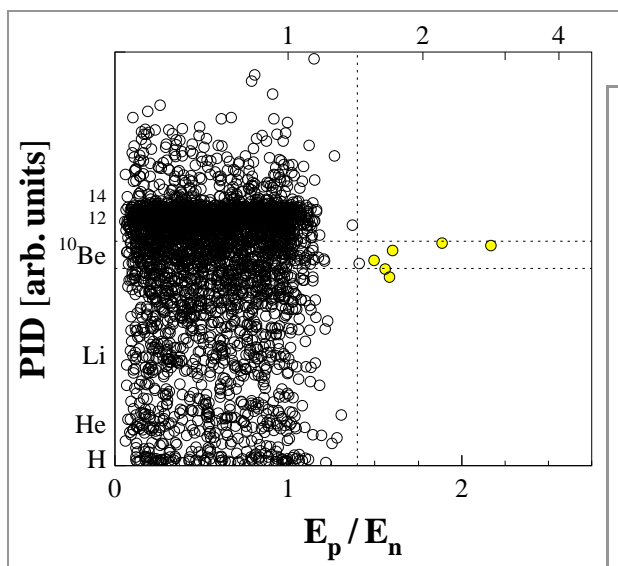
Kisamori, PRL 116 (2016) 052501

$$E(4n) = 0.8 \pm 1.3 \text{ MeV } (4.9\sigma)$$

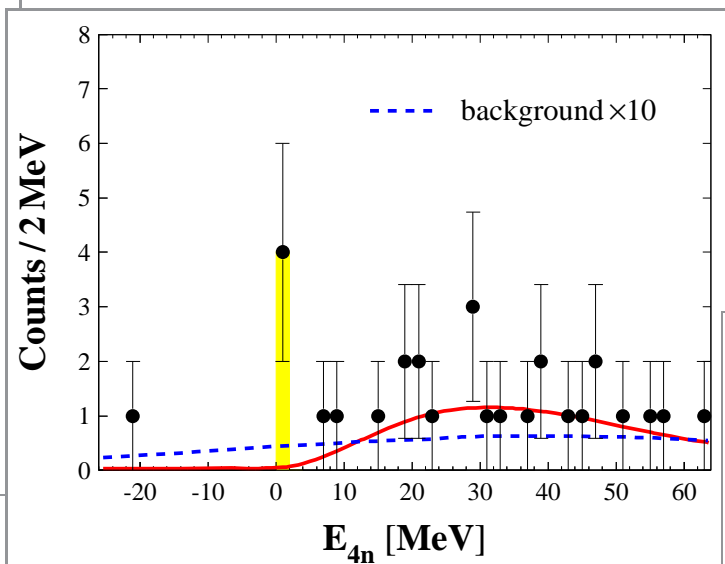


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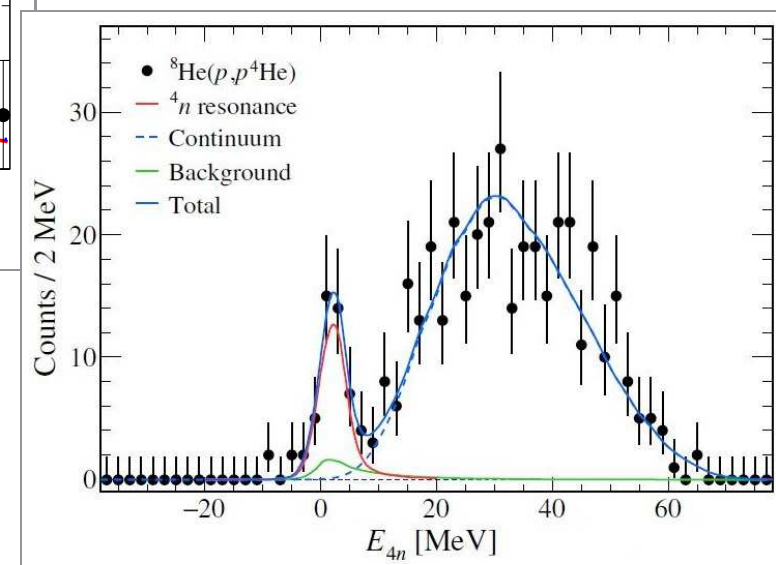
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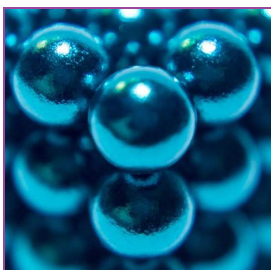
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$E(4n) = 0.8 \pm 1.3 \text{ MeV } (4.9\sigma)$

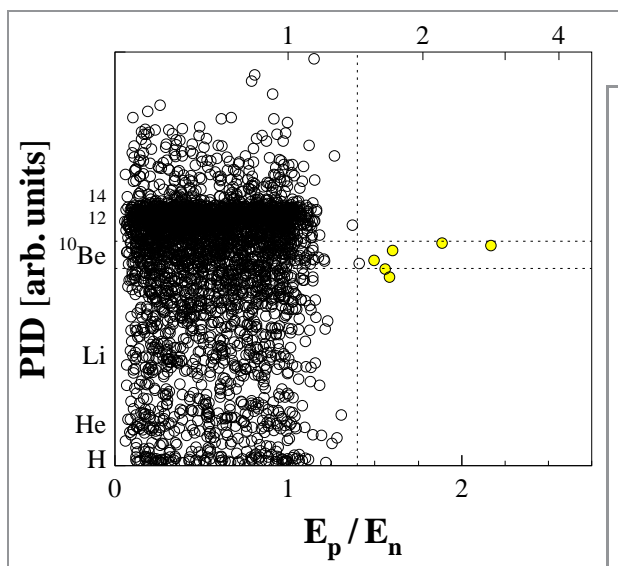


Duer, Nature 606 (2022) 678

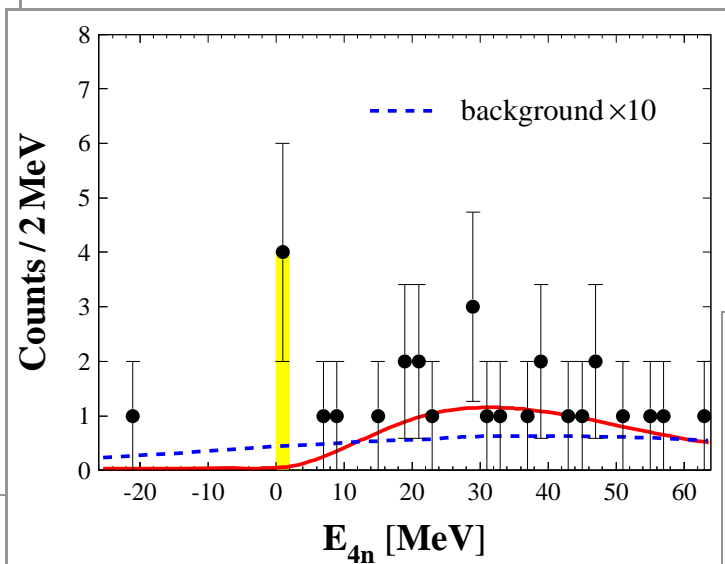
$E(4n) = 2.4 \pm 0.6 \text{ MeV } (\gg 5\sigma)$



Confirmation of a 4n “signal”



FMM & Carbonell, EPJA 57 (2021) 105



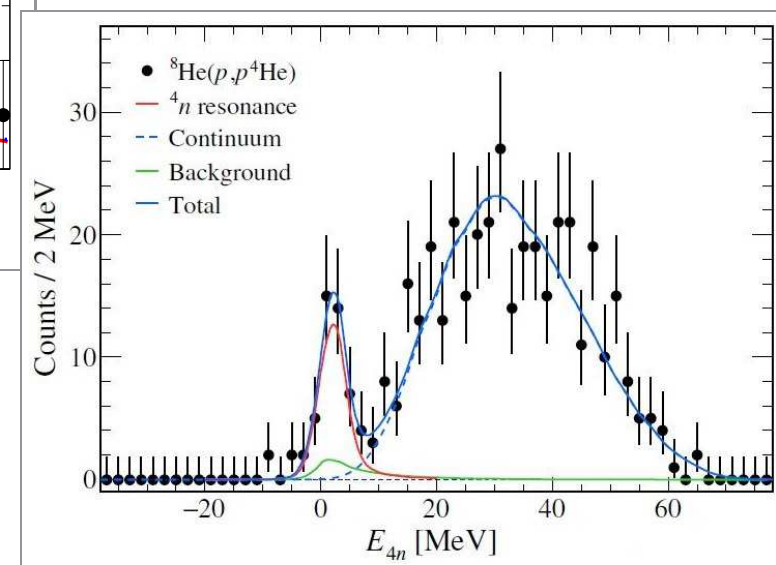
FMM, PRC 65 (2002) 044006

FMM, arXiv:nucl-ex/0504009

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Kisamori, PRL 116 (2016) 052501

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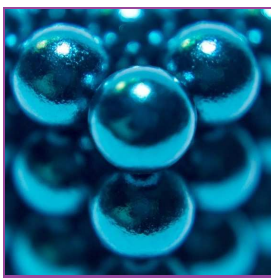


Duer, Nature 606 (2022) 678

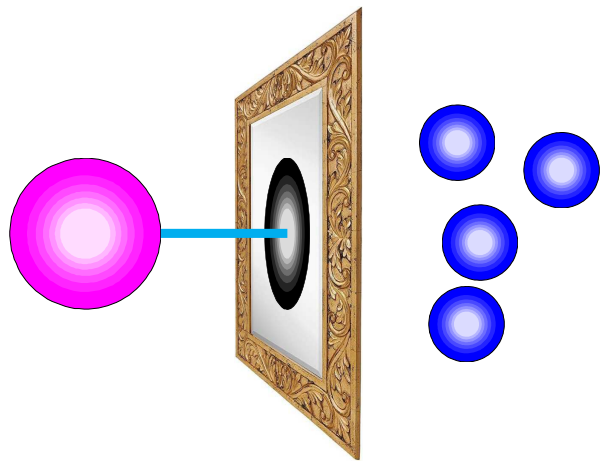
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Lazauskas, PRL 130 (2023) 102501

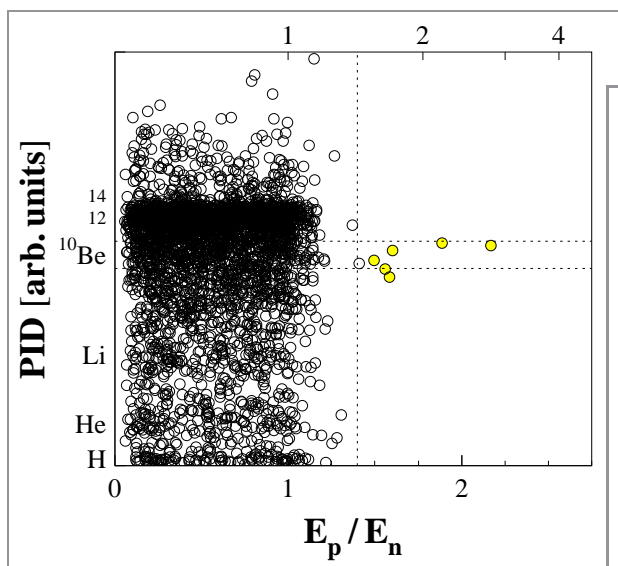
(nn)-(nn) correlations in ^8He ?



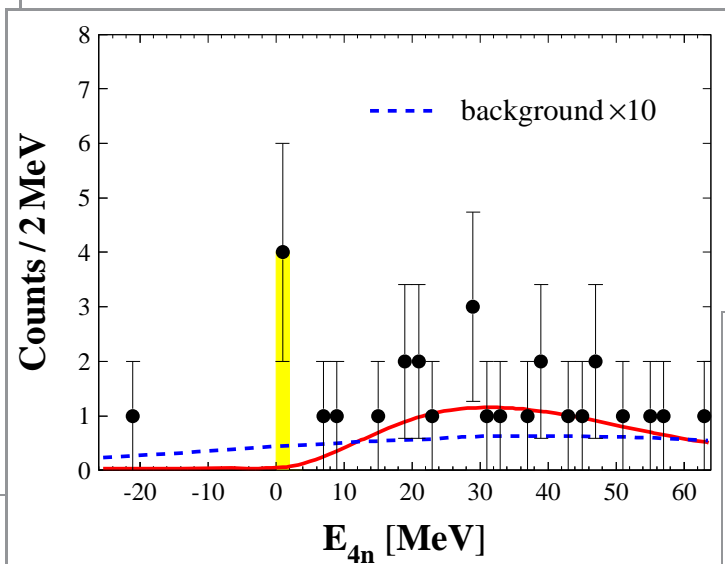
?



Confirmation of a 4n "signal"



FMM & Carbonell, EPJA 57 (2021) 105



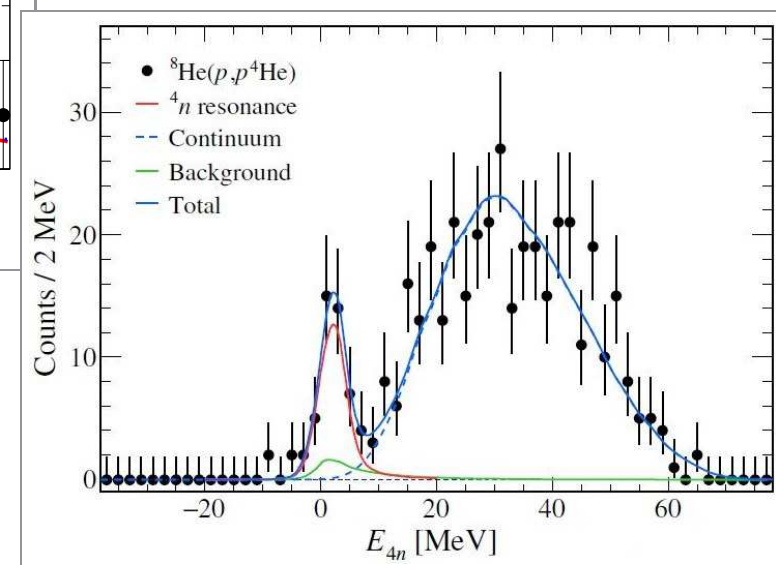
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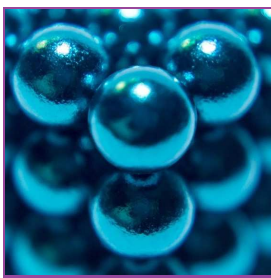


Duer, Nature 606 (2022) 678

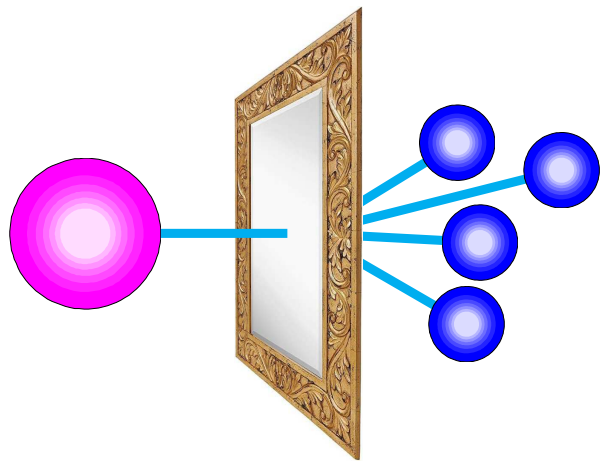
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Lazauskas, PRL 130 (2023) 102501

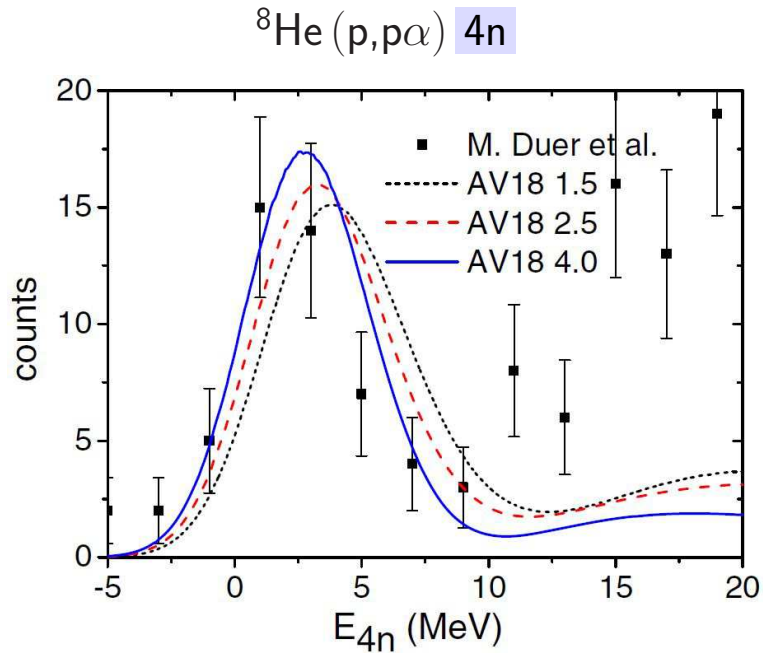
(nn)-(nn) correlations in ^8He ?



?



Low-energy structures in nuclear reactions with 4n in the final state



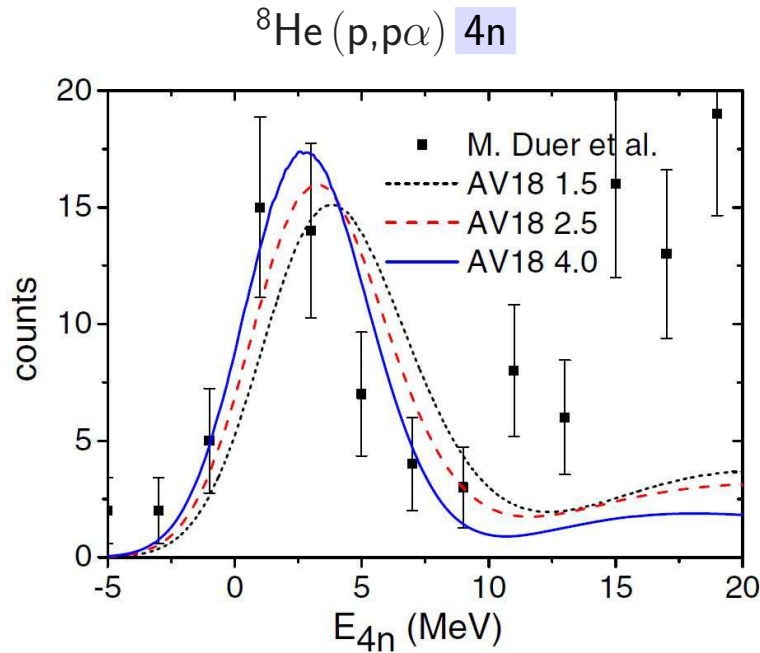
- ${}^8\text{He}$ (nn)-(nn) correlations
- core+4n : fast core removal
- general phenomenon in 4n haloes?
- ⇒ no need of 4n resonance

Low-energy structures in nuclear reactions with 4n in the final state

► How to disentangle both hypothesis?

$$\text{core} \left(\begin{matrix} (nn) \\ (nn) \end{matrix} \right) \} \Rightarrow E(4n) \sim 0 \Leftarrow \{ \text{}^4\text{n-core} \}$$

⇒ new observables (invariant mass)

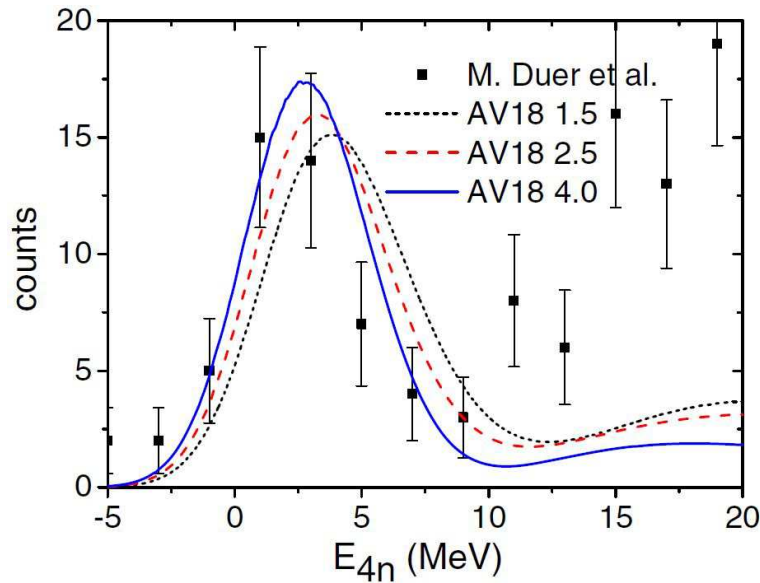


- ${}^8\text{He}$ (nn)-(nn) correlations
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Low-energy structures in nuclear reactions with 4n in the final state

${}^8\text{He} (p, p\alpha) {}^4\text{n}$



- ${}^8\text{He}$ (nn)-(nn) correlations
- core+4n: fast core removal
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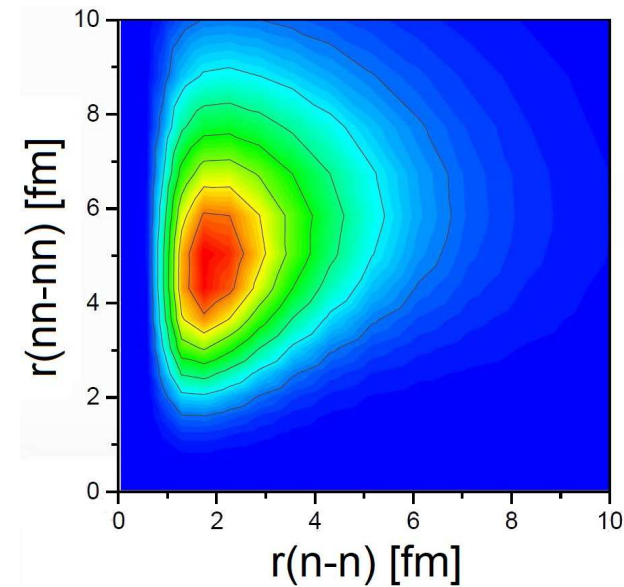
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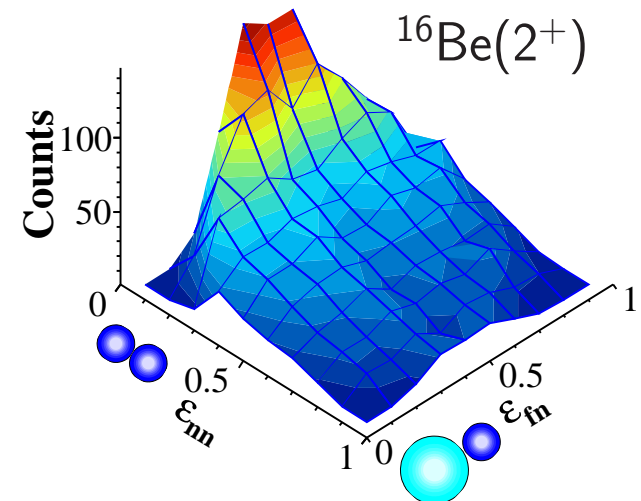
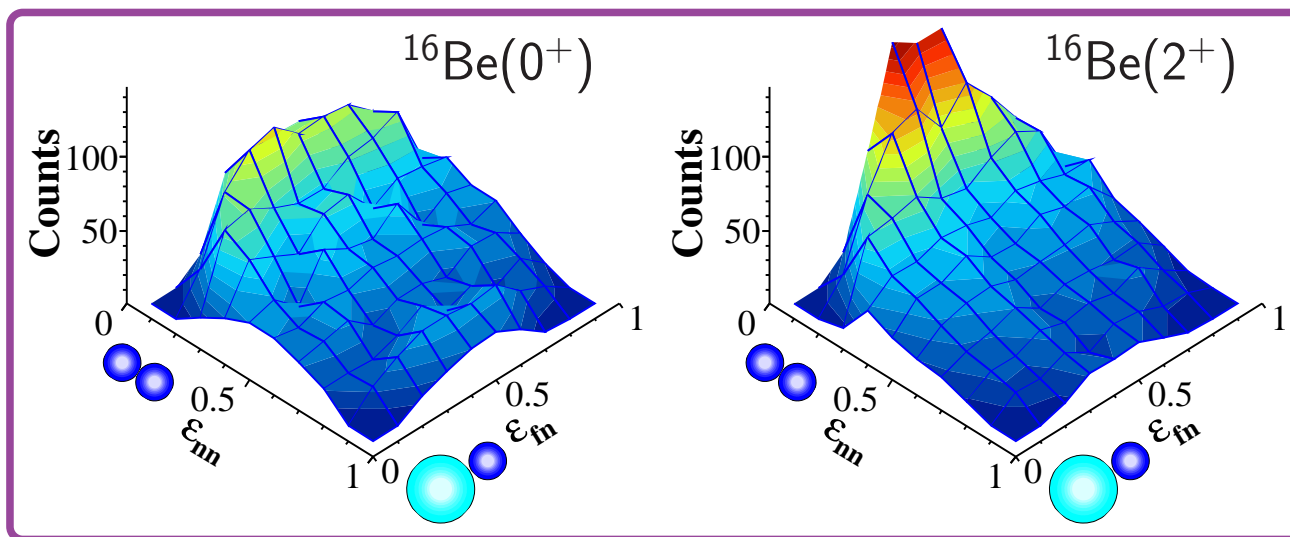
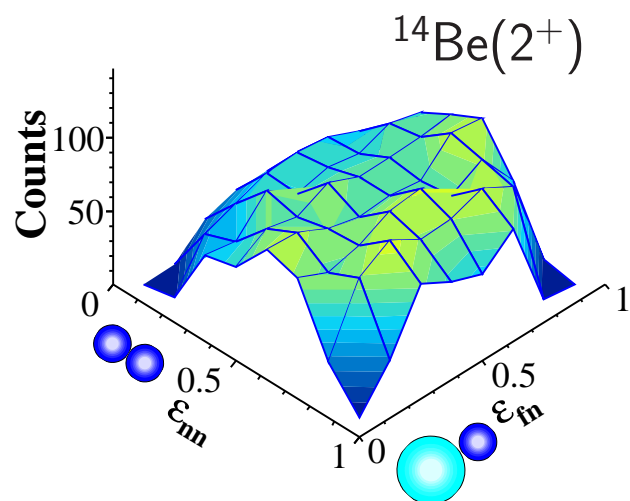
⇒ **new** observables (invariant mass)

► Spatial (nn)-(nn) correlations:

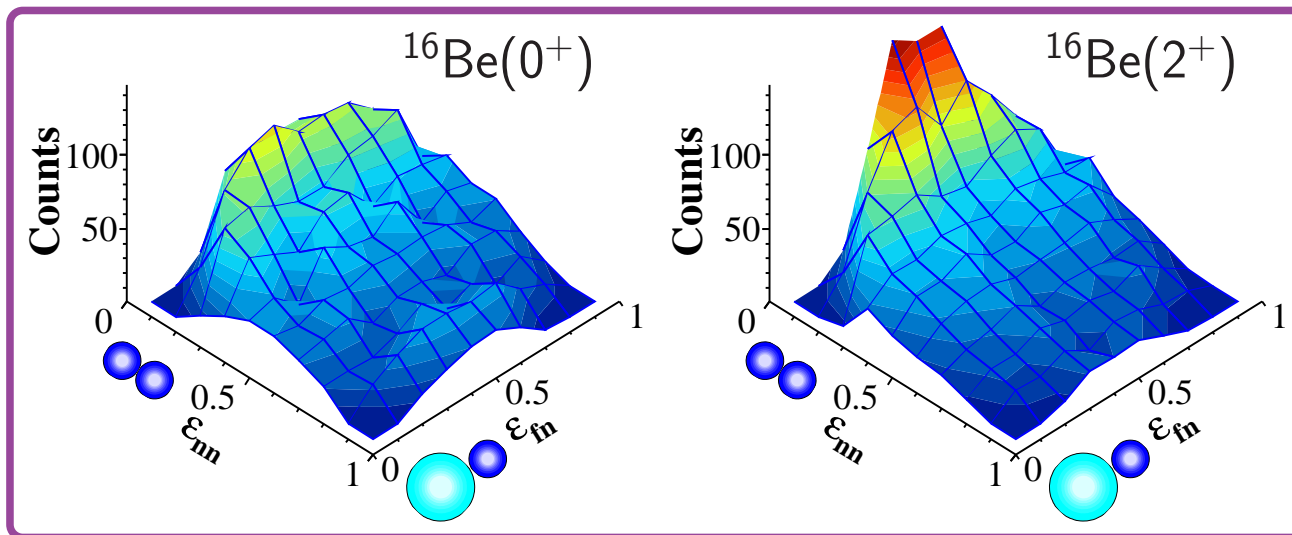
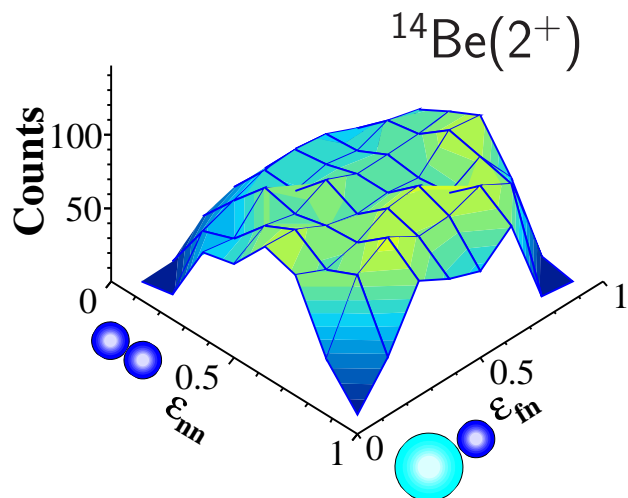


⇒ link to (exp) **momentum space**?

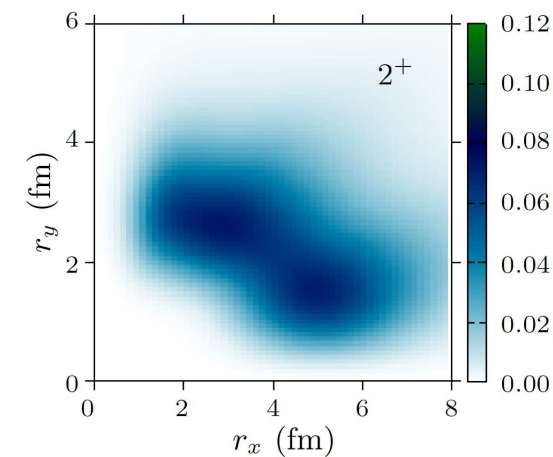
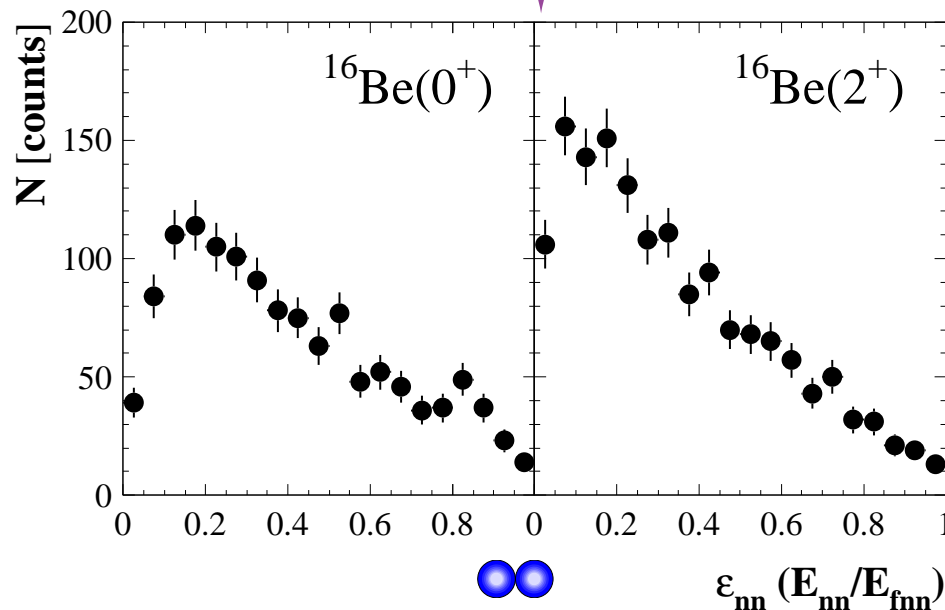
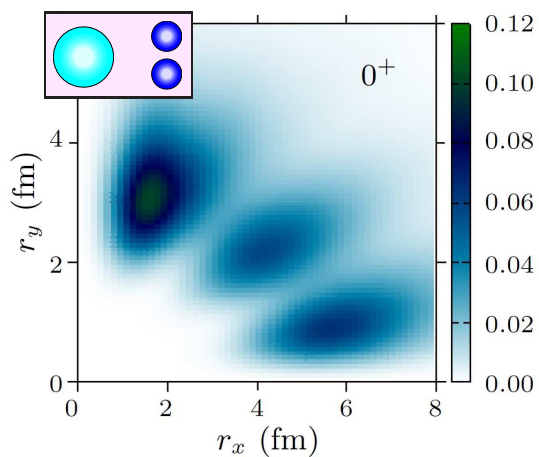
► Dalitz plot of 2n decay :



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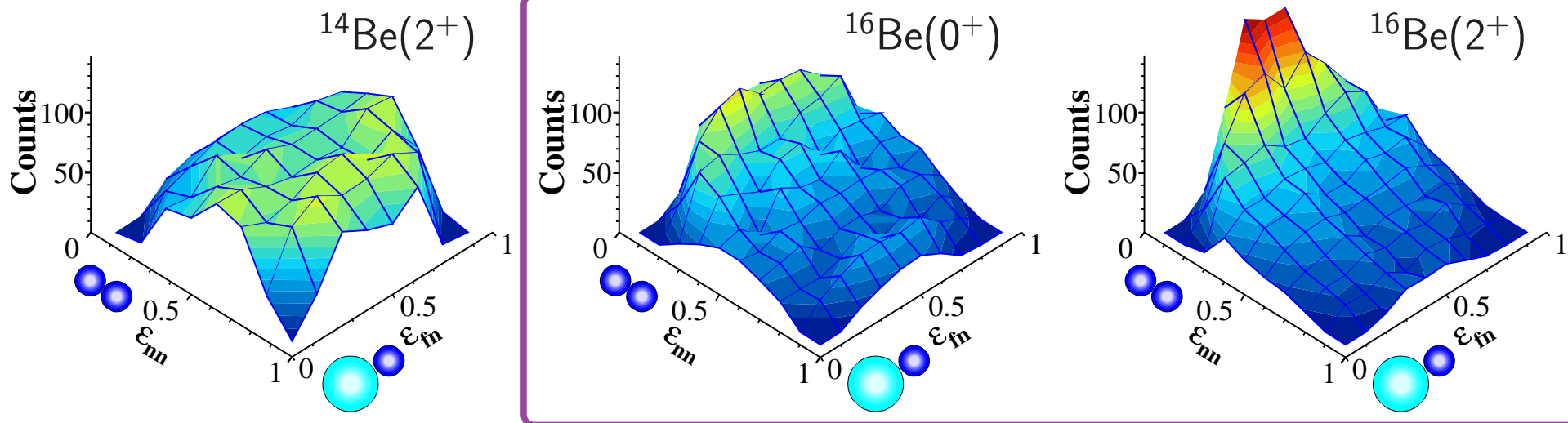


Casal, PRC 99 (2019) 014604

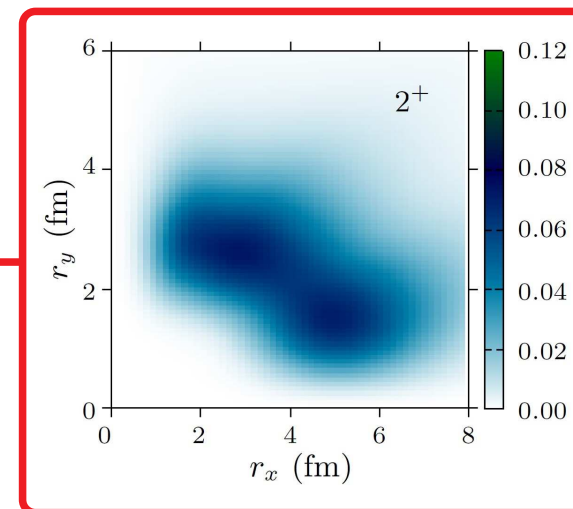
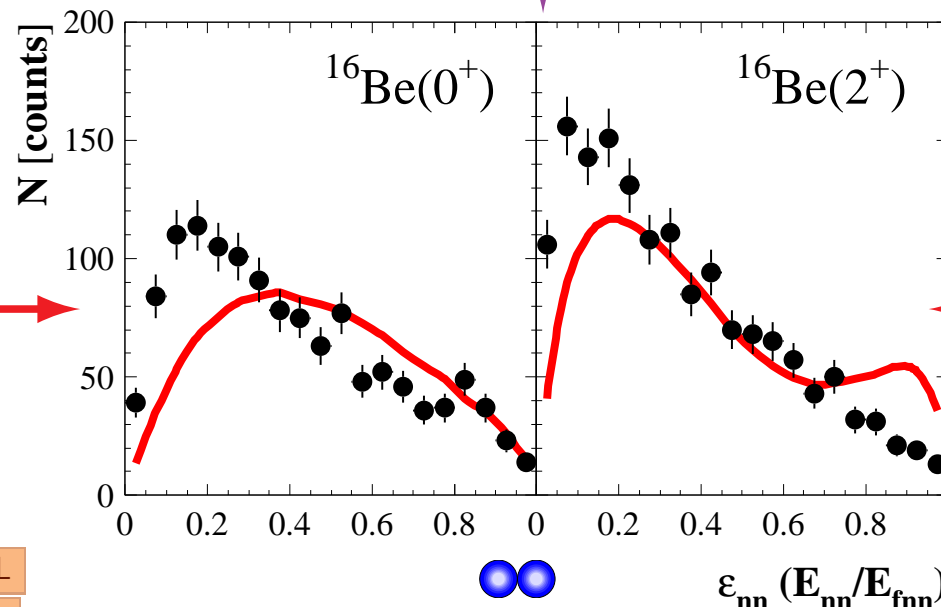
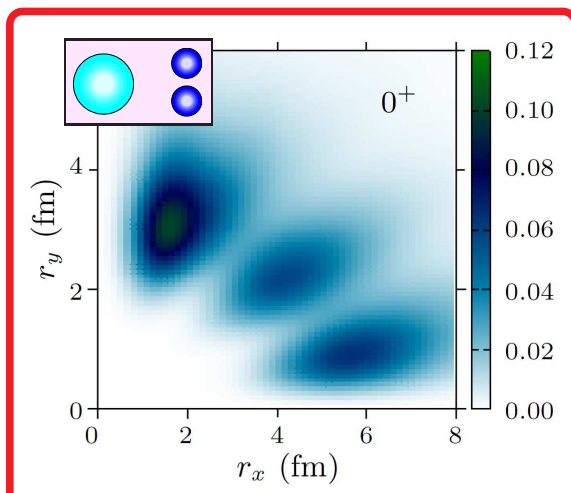


Beryllium 16 : $\psi(2n)$ in momentum space

► Dalitz plot of 2n decay :



Casal, PRC 99 (2019) 014604



Monteagudo, submitted to PRL

Wang, PRL 126 (2021) 142501

Pauli-principle driven correlations in four-neutron nuclear decays

“The valence neutrons are pushed to the symmetry-allowed configurations in the 4n-precursor structure ... It should be noted that much more correlation information characterizing core+4n decay in principle exist. However ... at the moment we find too premature to discuss such complicated things”

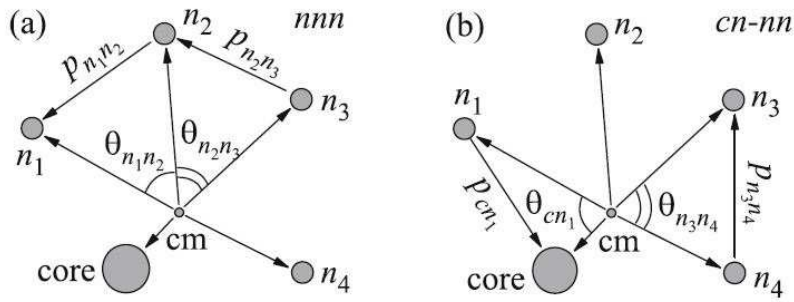


Fig. 3. Schemes of kinematical variables describing 5-body decays, which are used in constructing correlated two-dimensional energy $\{\varepsilon_{ik}, \varepsilon_{nm}\}$ and angular $\{\theta_{ik}, \theta_{nm}\}$ distributions of fragments. Examples (a) of “connected” nnn and (b) of “disconnected” $cn-nn$ topologies. The related energy distribution parameters are defined as $\varepsilon_{ik} = p_{ik}^2 / (2\mu_{ik} E_T)$

$${}^7\text{H} : [p_{3/2}^4]_0 \rightarrow C_{2323}[p_{3/2}^4]_0 + C_{0123}[s_{1/2}^2 p_{3/2}^2]_0, \quad (12)$$

$${}^{28}\text{O} : [d_{3/2}^4]_0 \rightarrow C_{4343}[d_{3/2}^4]_0 + C_{0143}[s_{1/2}^2 d_{3/2}^2]_0 + C_{0123}[s_{1/2}^2 p_{3/2}^2]_0. \quad (13)$$

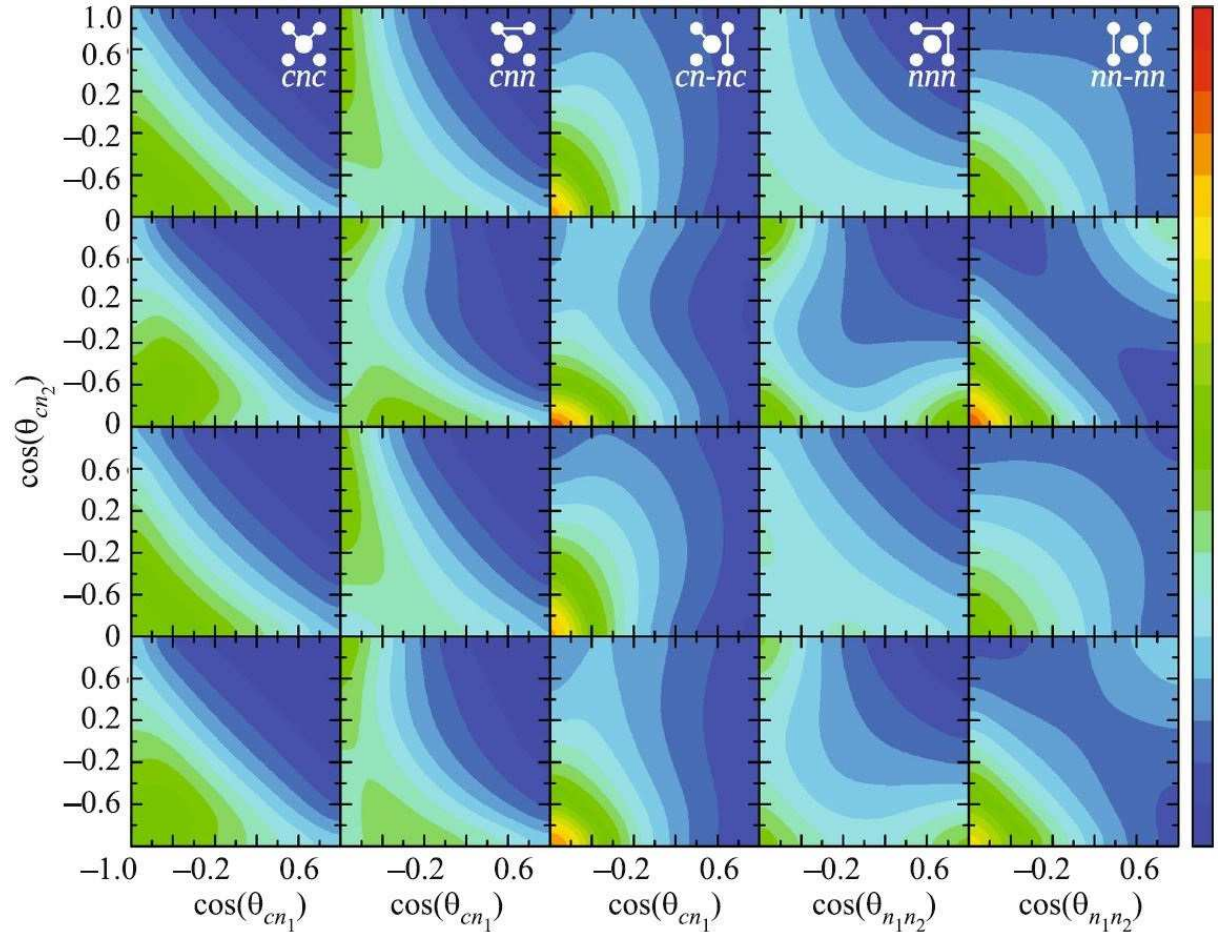
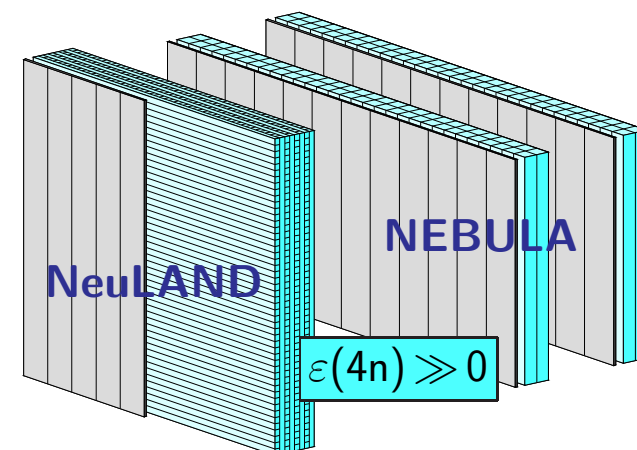
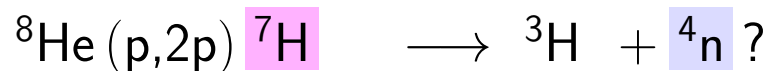


Fig. 9. Correlated distributions for core+4n decays in $C_{0123}[s_{1/2}^2 p_{3/2}^2]_0 + C_{0121}[s_{1/2}^2 p_{1/2}^2]_0$ configuration mixing. The following cases are illustrated: $C_{0121} = 1, 0.48, -0.48,$ and 0 .

► 2016/17 “trineutron campaign” @ RIKEN:

→ first **invariant-mass** measurement of **4n decay**!

reaction	initial state	final state	σ	results
(’16) $^4\text{He} (^8\text{He}, \alpha\alpha) ^4\text{n}$ Shimoura, NP1512-SHARAQ10			nb	$N_{\text{evt}} \sim 10\text{ s}$ $^4\text{n}: E, \Gamma$
(’17) $^8\text{He} (\text{p}, \text{p}\alpha) ^4\text{n}$ Paschalis, NP1406-SAMURAI19			μb	$N_{\text{evt}} \sim 1000\text{ s}$ $^4\text{n}: E, \Gamma$
(’17) $^8\text{He} (\text{p}, 2\text{p}) \{^3\text{H} + ^4\text{n}\}$ FMM/Yang, NP1512-SAMURAI34 			mb	$N_{\text{evt}} \sim 10,000\text{ s}$ $^4\text{n} \& ^7\text{H}: E, \Gamma, \Omega$

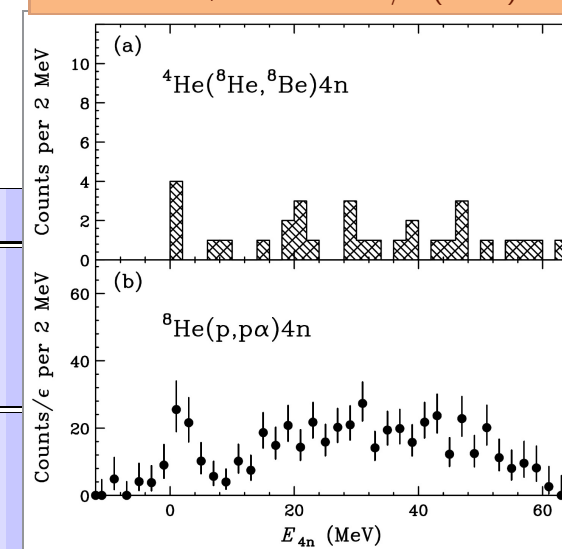


► 2016/17 “traneutron campaign” @ RIKEN :

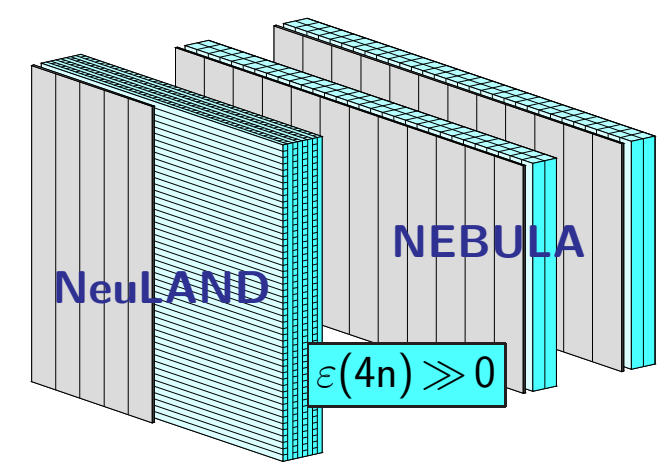
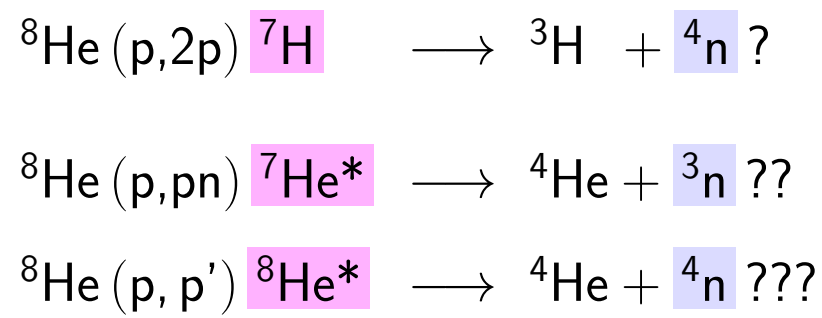
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Shimoura, NP News 33/3 (2023) 15

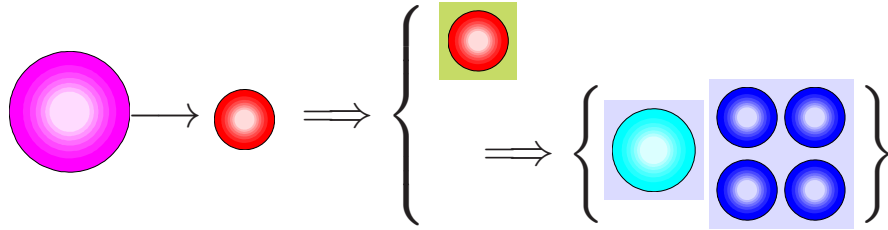
reaction	initial state	final state
(¹⁶) ${}^4\text{He}({}^8\text{He}, \alpha\alpha) {}^4\text{n}$ Shimoura, NP1512-SHARAQ10		
(¹⁷) ${}^8\text{He}(p, p\alpha) {}^4\text{n}$ Paschalis, NP1406-SAMURAI19		
(¹⁷) ${}^8\text{He}(p, 2p) \{ {}^3\text{H} + {}^4\text{n} \}$ FMM/Yang, NP1512-SAMURAI34 		



mb $N_{\text{evt}} \sim 10,000$ s
 ${}^4\text{n} \& {}^7\text{H}: E, \Gamma, \Omega$

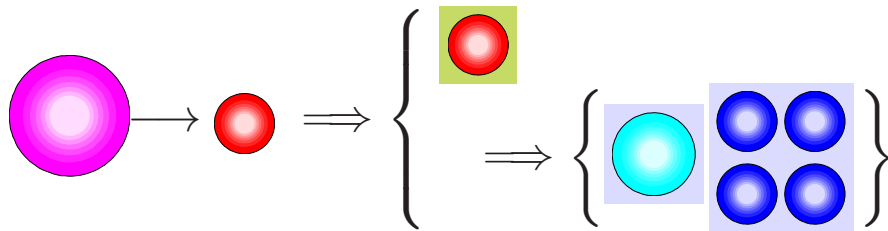


${}^8\text{He} (p, p') {}^4\text{He} + 4n$ @ 150 MeV/N :

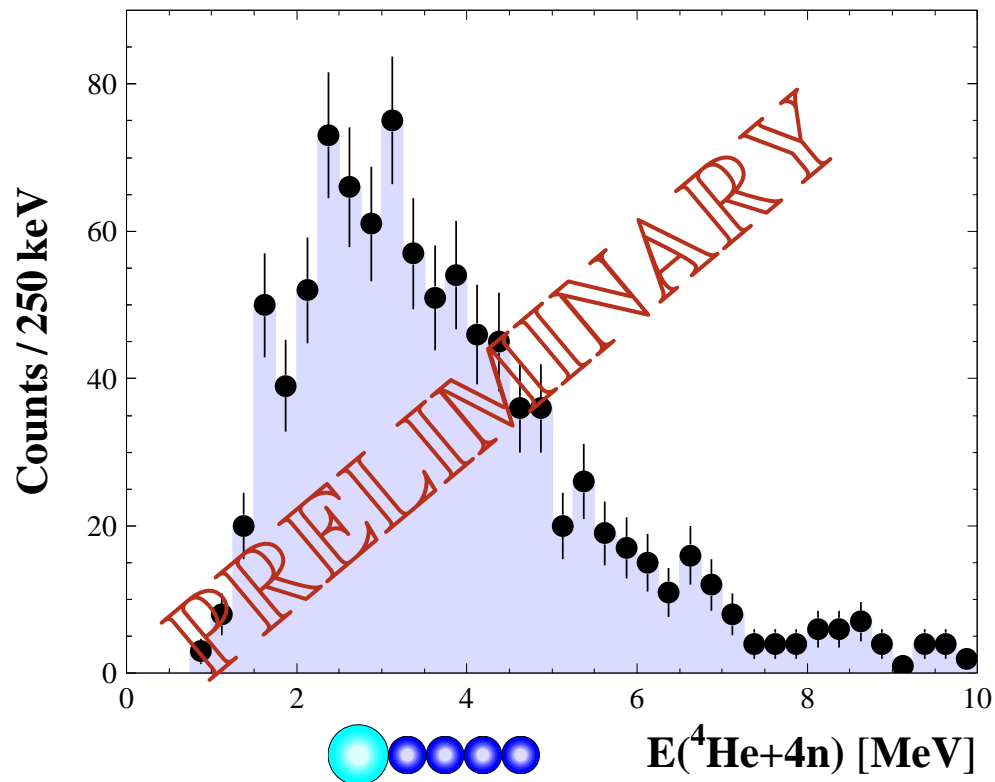


 Audrey Anne, PhD

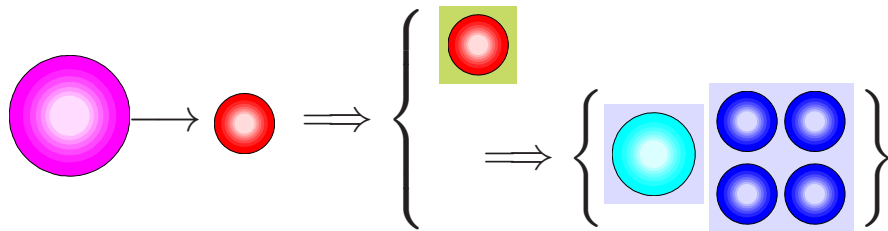
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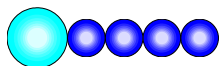
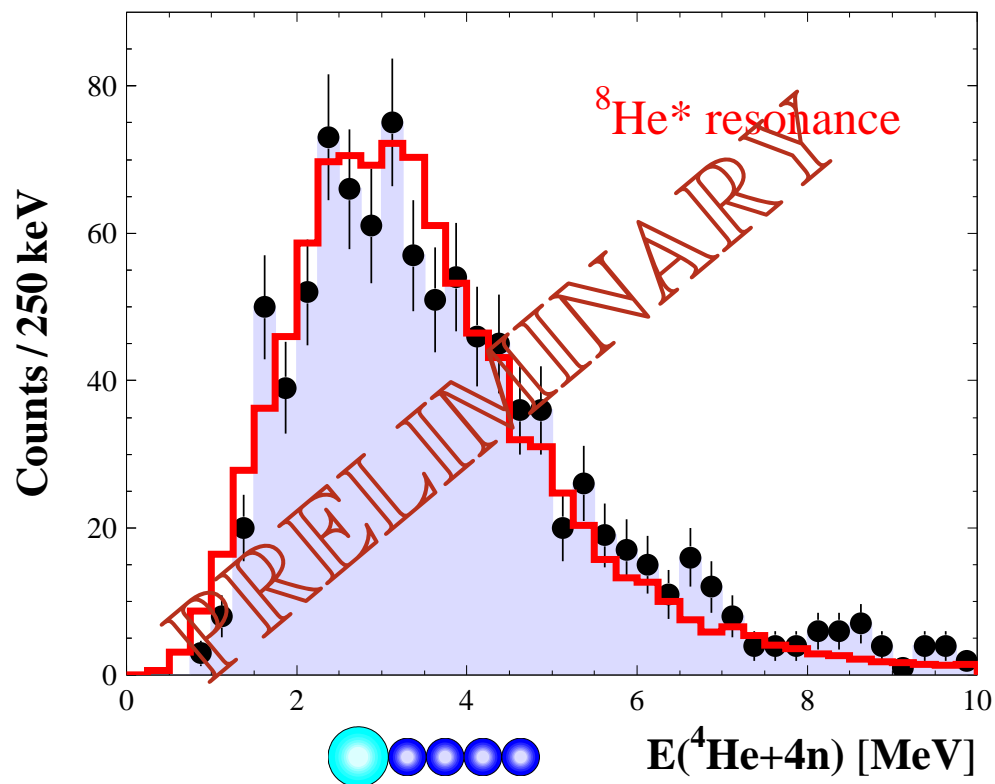
 Audrey Anne, PhD



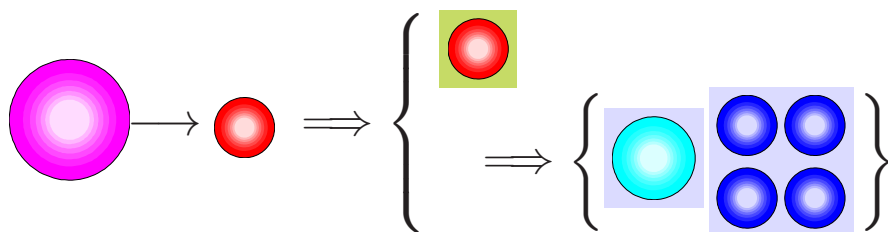
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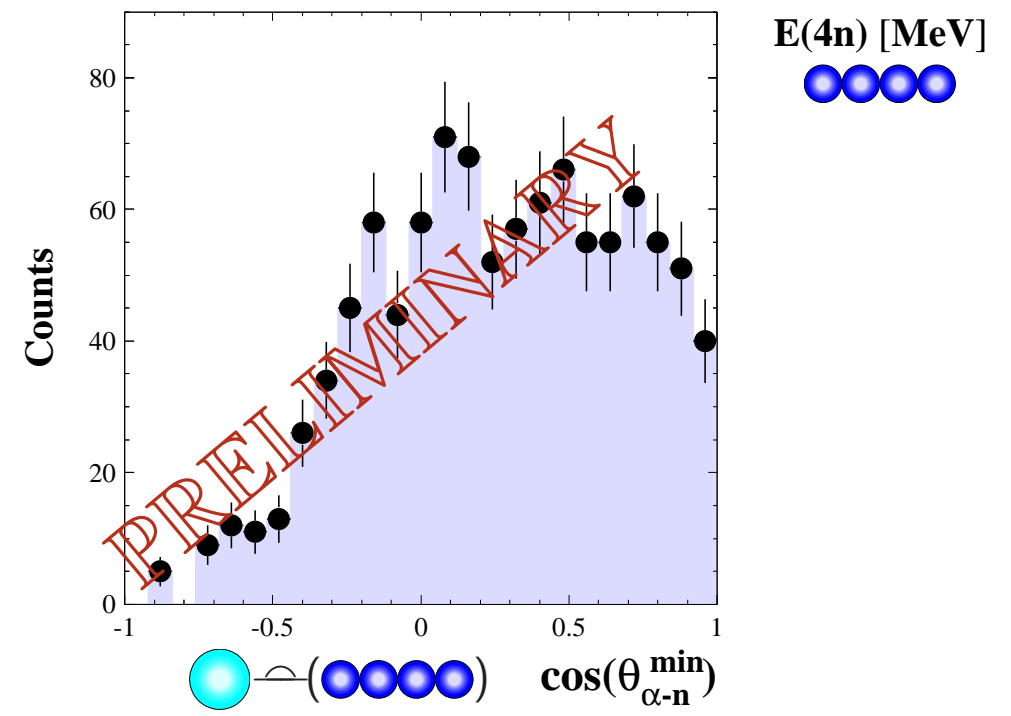
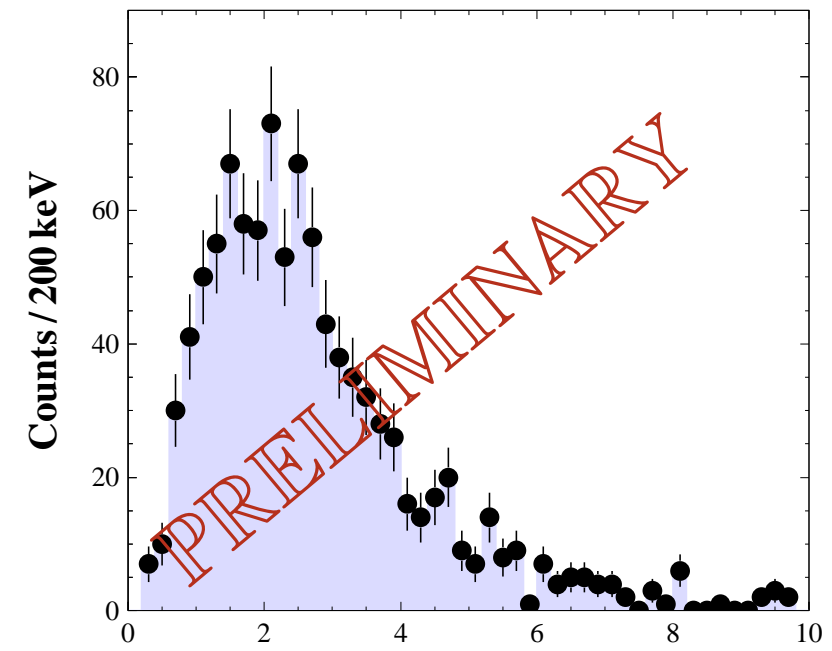
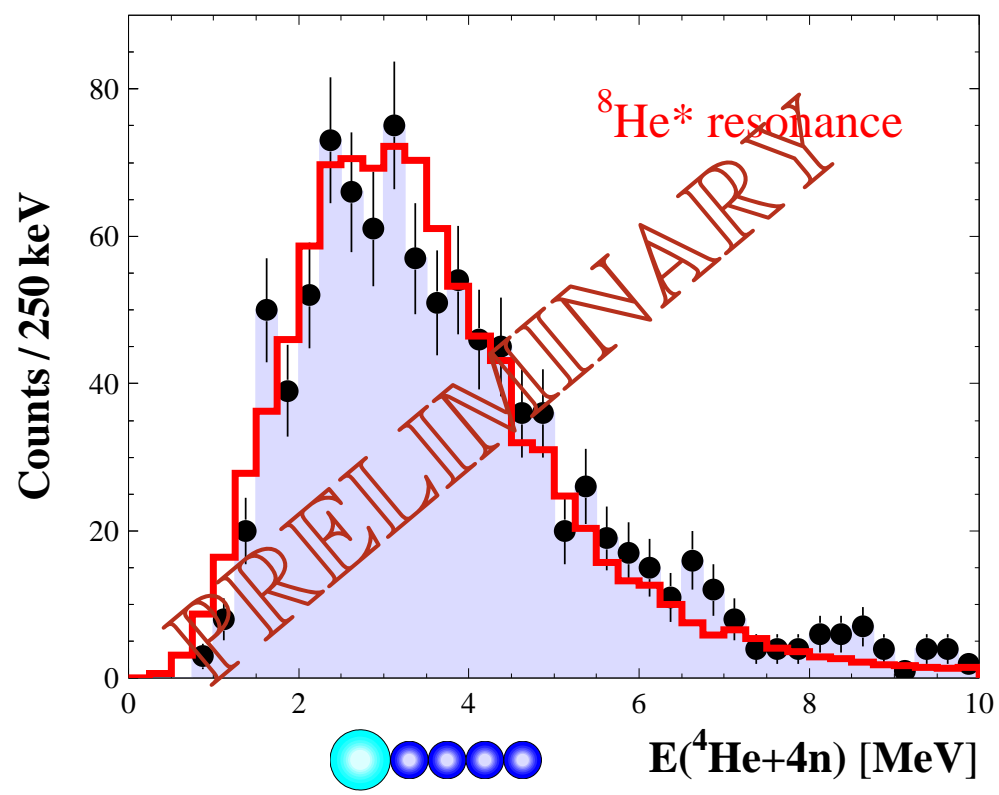
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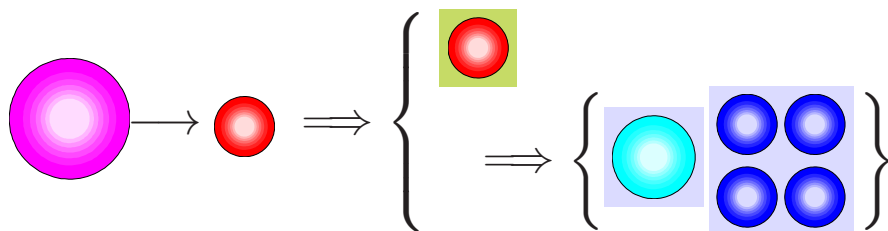
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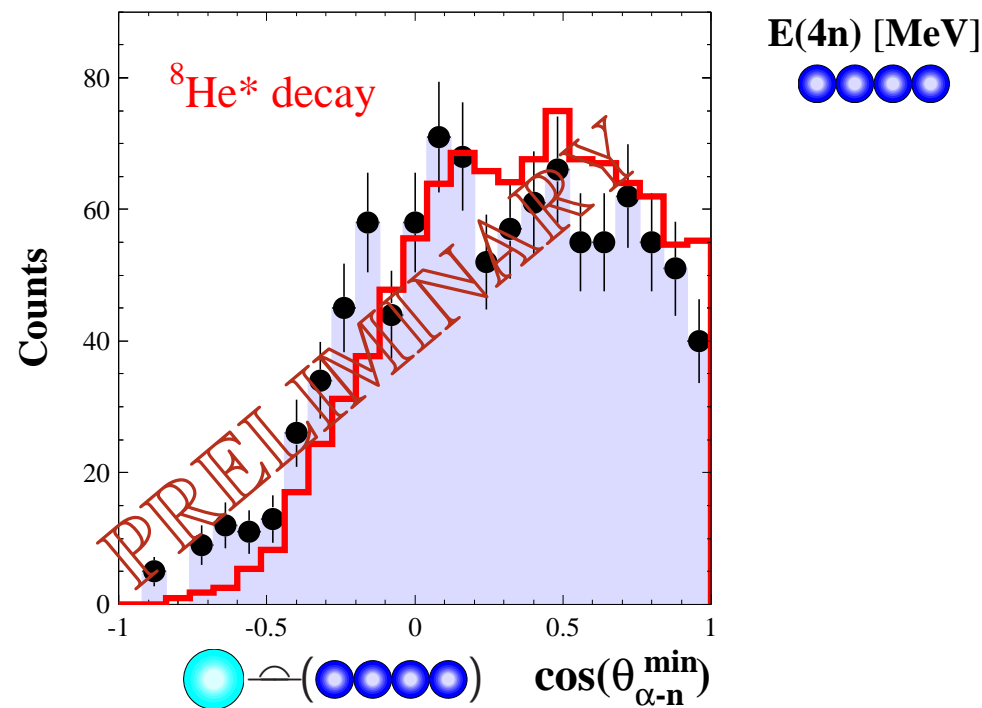
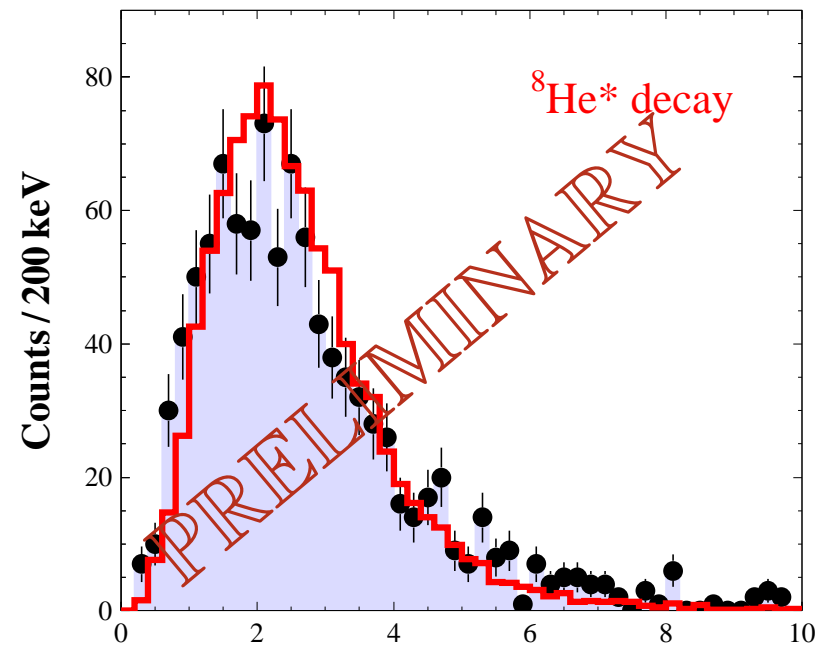
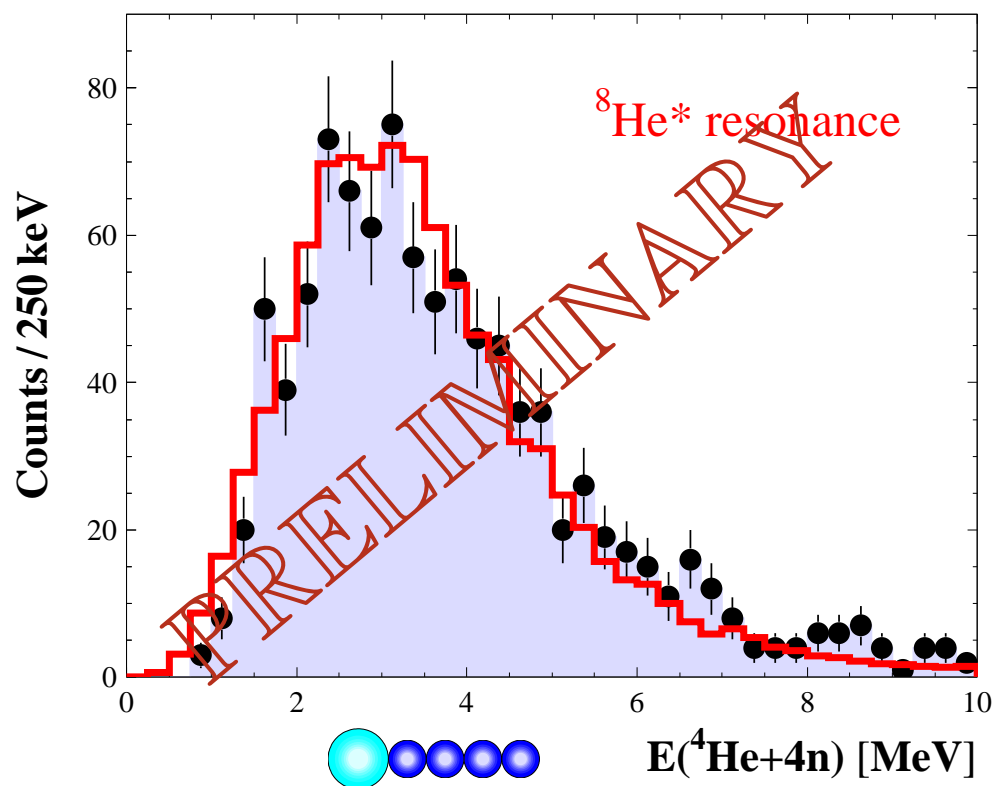
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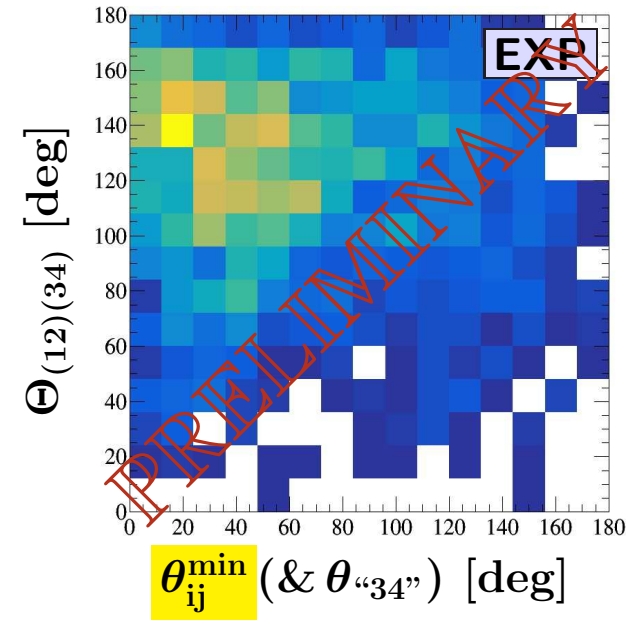
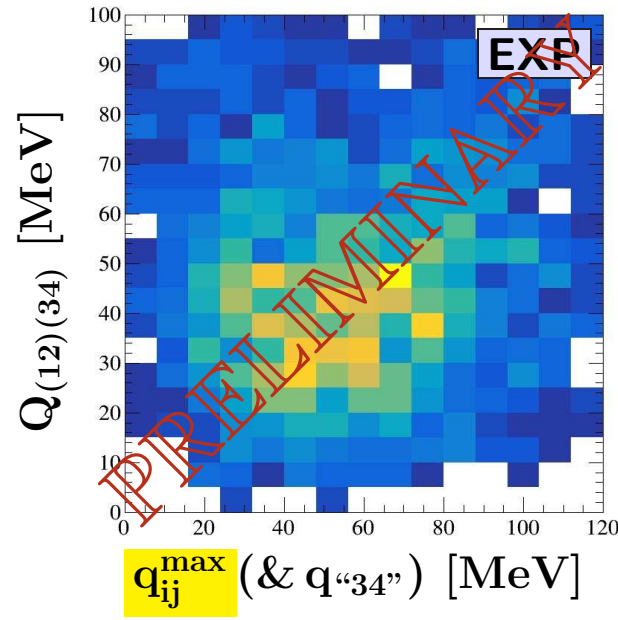
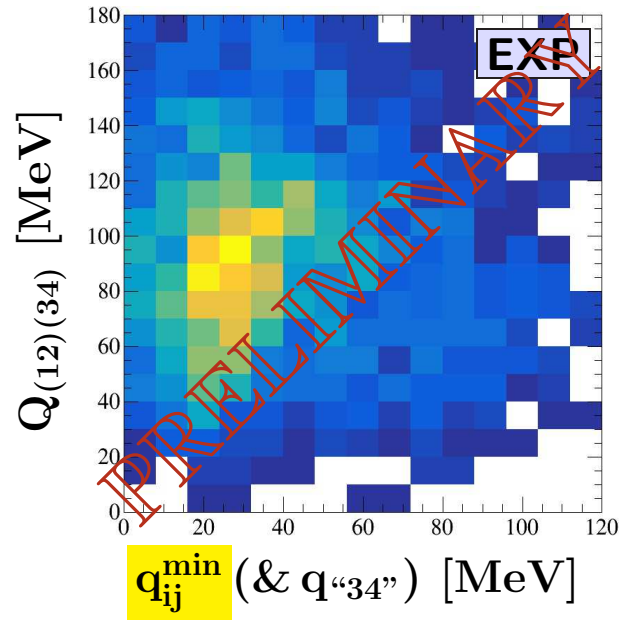
$^8\text{He} (p,p') ^4\text{He} + 4n$ @ 150 MeV/N :



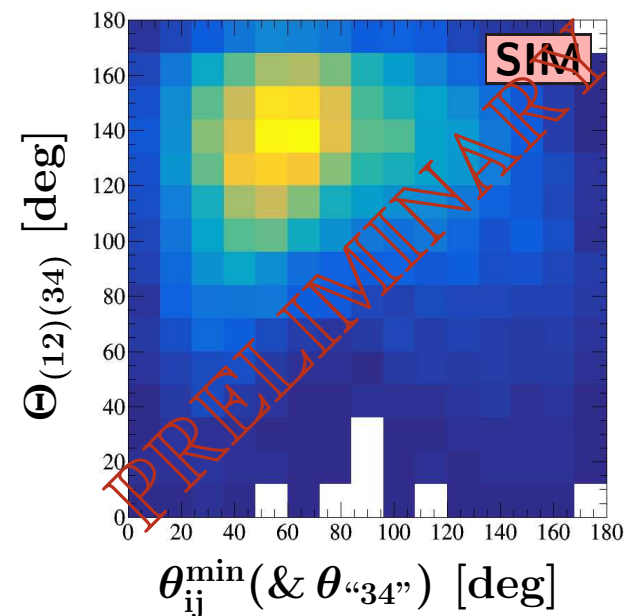
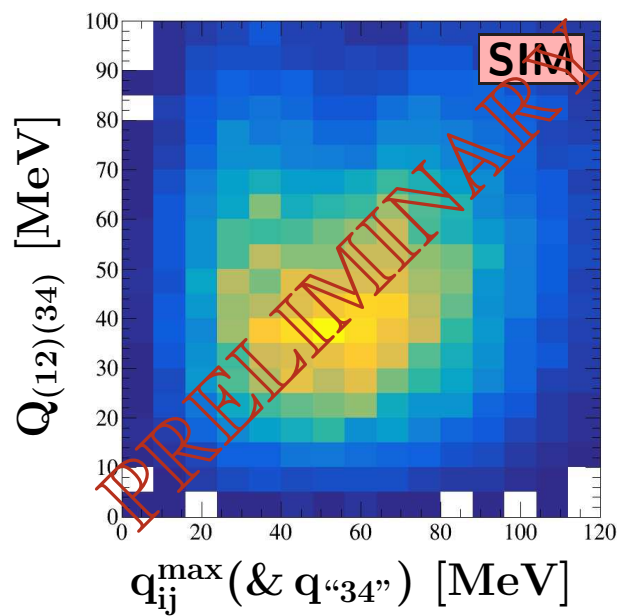
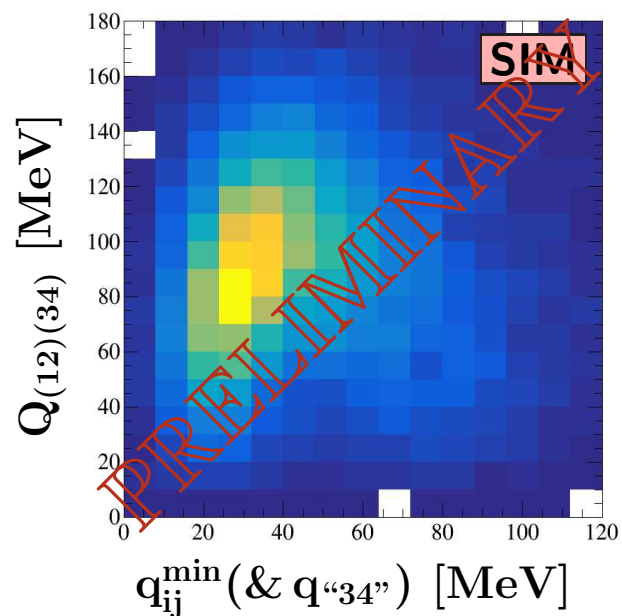
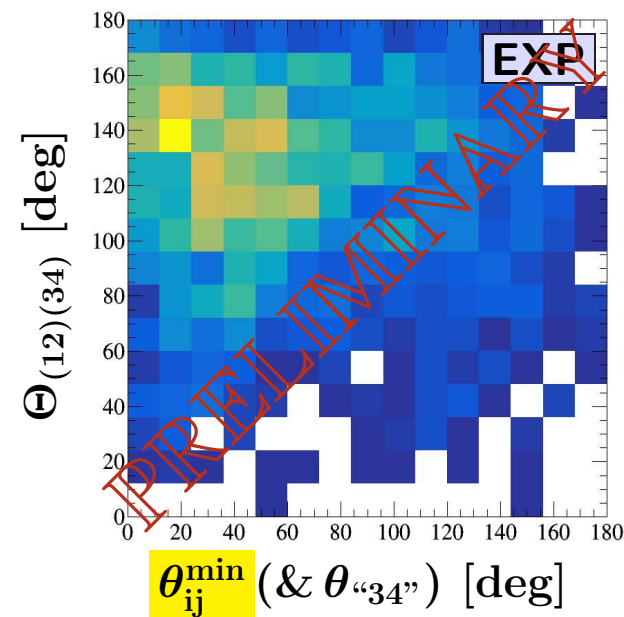
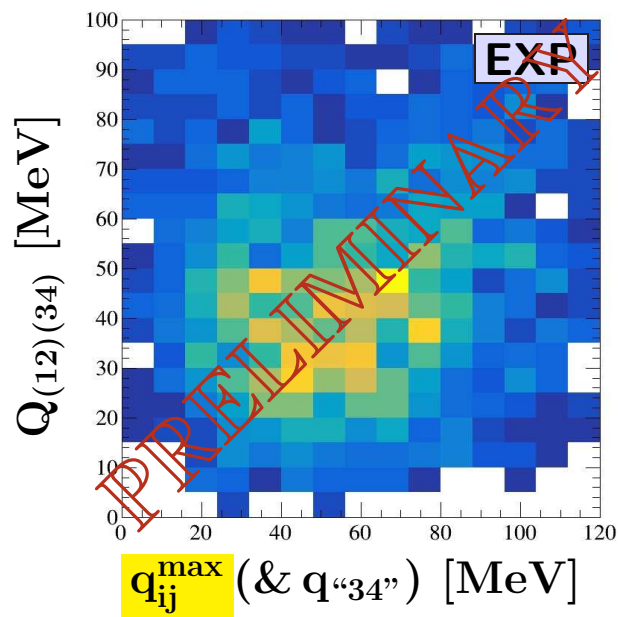
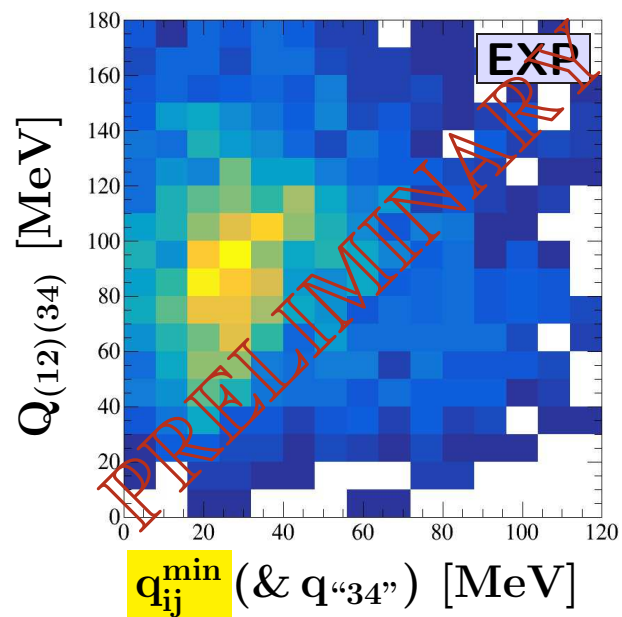
Audrey Anne, PhD



Preliminary 4n correlation observables



Preliminary 4n correlation observables





📄 Emeline Oliveira, PhD



📄 Audrey Anne, PhD

- ▶ Scattering lengths:
 - neutron off exotic ‘containers’
 - $^{17}\text{B}+n$: a shocking case!
- ▶ Experimental program @ RIKEN:
 - stat. & acceptance: effective range
 - multi-channel: determine (a_s, r_e) !
 - Universality ($|a_s|/r_e \sim 100$)

- ▶ Tetraneutron “signal”!
 - resonance / spatial correlations?
 - link to momentum correlations?
- ▶ Experimental program @ RIKEN:
 - first $4n$ invariant masses
 - some low-energy structures
 - explore full kinematics...