

# Lessons from $\Xi^-$ capture events in emulsion

2023 ECT\* Rockstar Workshop, Trento, Italy, Oct. 2023

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## $V_\Xi$ from $\Xi^-$ capture events

All five KEK & J-PARC  $\Xi^- + {}^A_Z \rightarrow {}^{A'}_\Lambda Z' + {}^{A''}_\Lambda Z''$  capture events in light-nuclei emulsion occur in  $1p_{\Xi^-}$  nuclear states, suggesting attractive  $V_\Xi \geq 20$  MeV.

E. Friedman, A. Gal, PLB 820 (2021) 136555

## Questioning E07 $1s_{\Xi^-}$ assignments in ${}^{14}\text{N}$

Assigned  $1s_{\Xi^-} - {}^{14}\text{N}$  events reinterpreted as  $1p_{\Xi^0} - {}^{14}\text{C}$ .

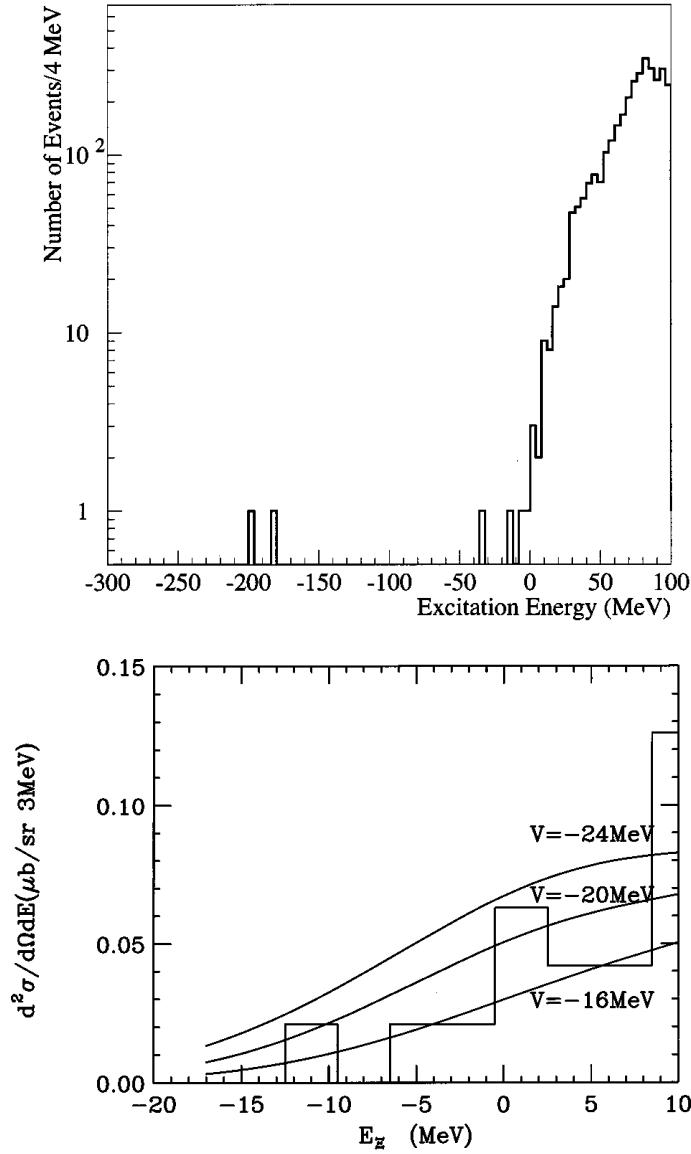
E. Friedman, A. Gal, PLB 837 (2023) 137640

## Remarks on the elusive H dibaryon time permitting...

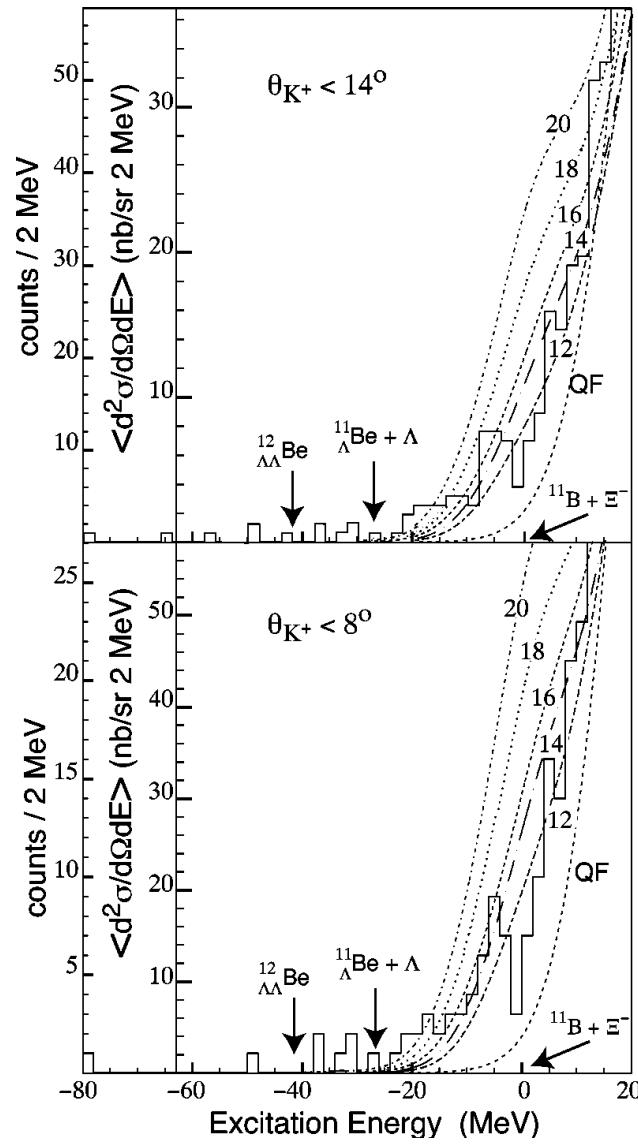
# $E^-$ nuclear physics

from counter experiments,  
from theory and femtoscopy,  
& from capture in emulsion nuclei

E224 (KEK)

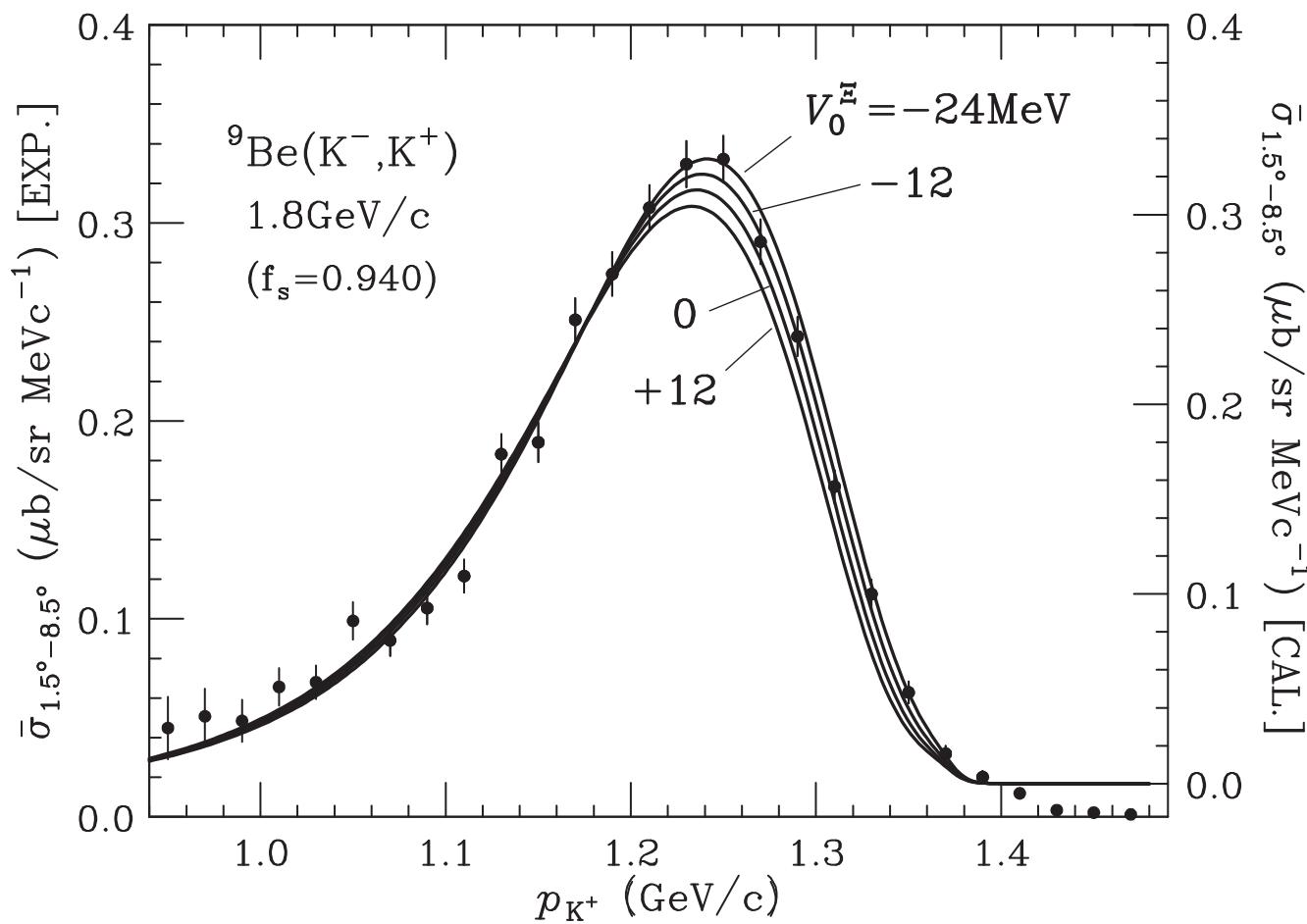


E885 (BNL)



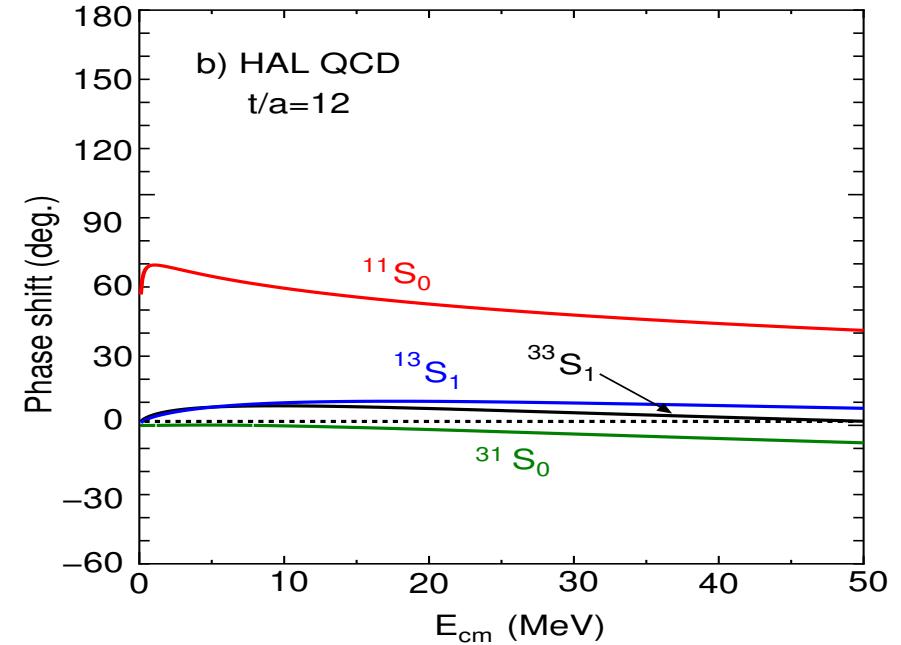
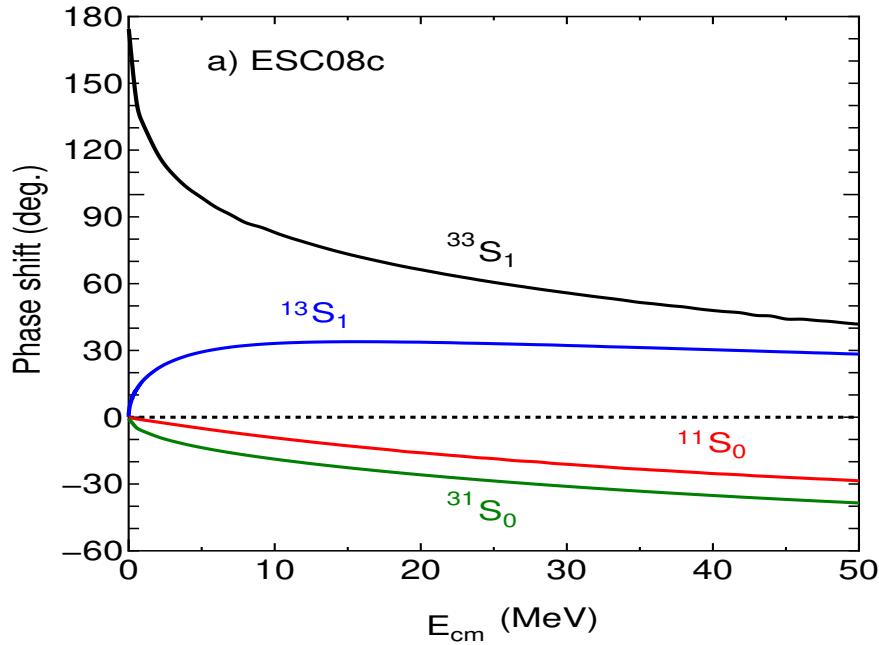
$^{12}\text{C}(K^-, K^+)$  counter experiments, end of 1990s.

Unresolved bound states, if any,  $V_\Xi$  of order 15 MeV



BNL AGS-906 on  ${}^9\text{Be}$ . A Quasi-Free fit by  
 Harada & Hirabayashi, PRC 103 (2021) 024605  
 concludes  $V_{\Xi} = 17 \pm 6$  MeV. Yet, no  $\Xi^-$  bound state  
 smoking gun from  $(\text{K}^-, \text{K}^+)$  experiments.  
 Await J-PARC final E05 & future E70 results.

# $\Xi N$ s-wave model interactions



Nijmegen ESC08c version

HAL-QCD version

Hiyama et al. PRL 124 (2020) 092501:  $A \leq 4$   $\Xi$  hypernuclei  
Substantial model dependence

HAL-QCD: LQCD calculation at  $m_{\pi(K)} = 146(525)$  MeV

Sasaki et al. NPA 998 (2020) 121737

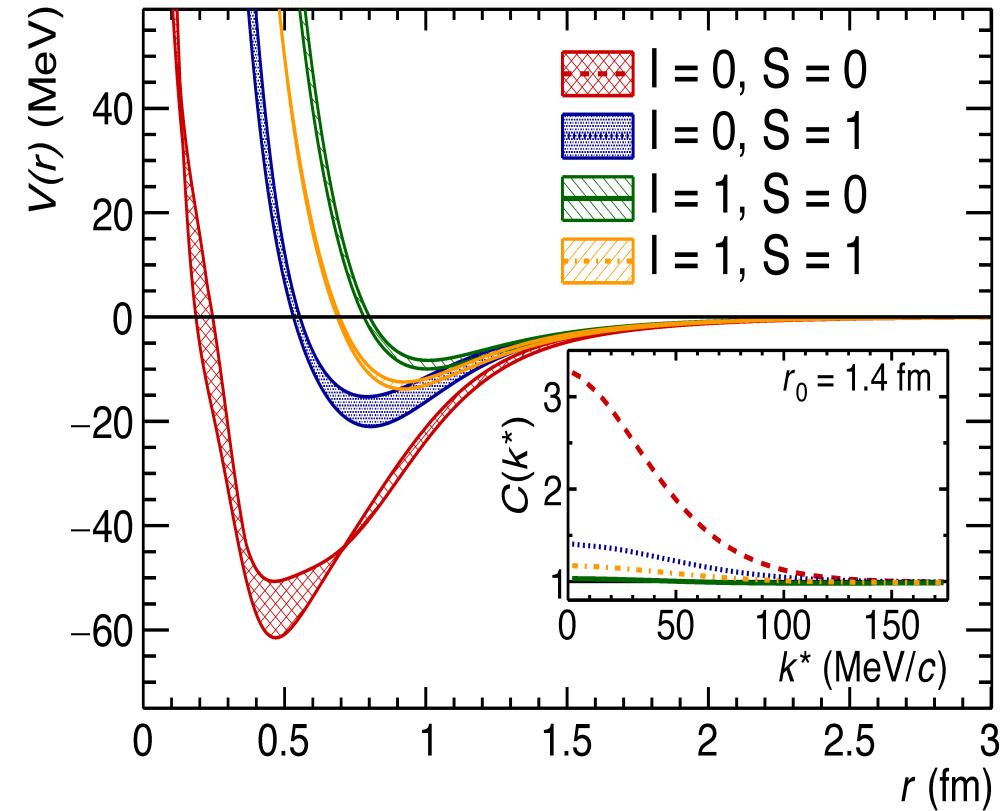
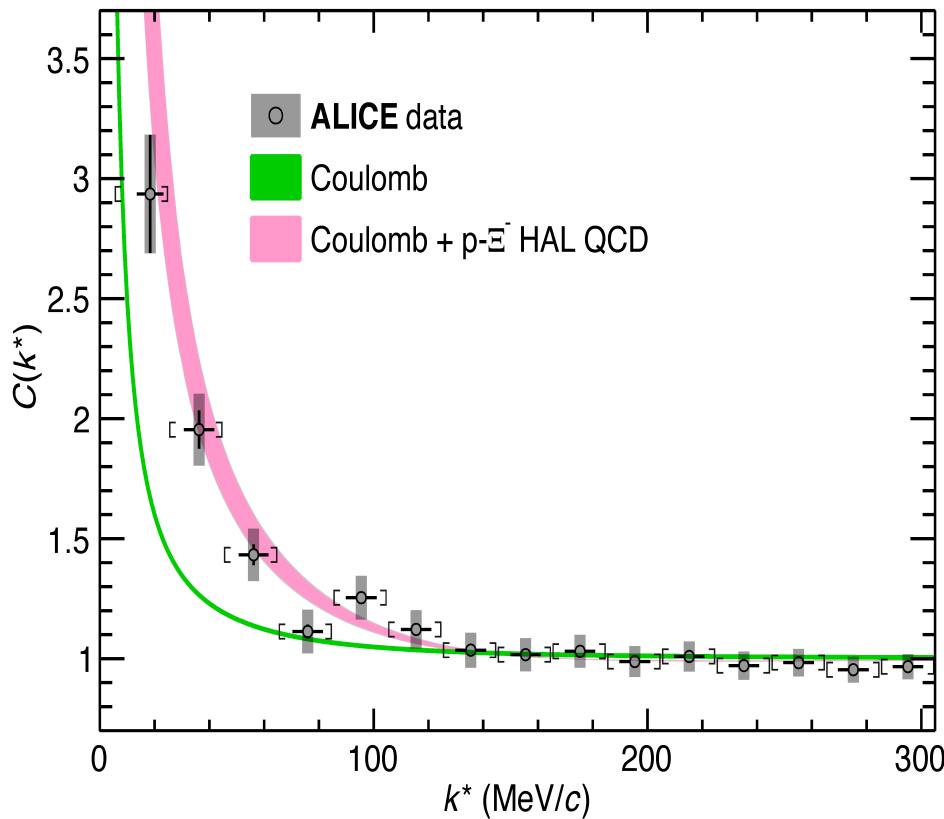
Inoue et al. AIPCP 2130 (2019) 020002:  $V_{\Xi}^{\text{LQCD}} = 4 \pm 2$  MeV

Kohno, PRC 100 (2019) 024313:  $V_{\Xi}^{\text{EFT}} \approx 10$  MeV

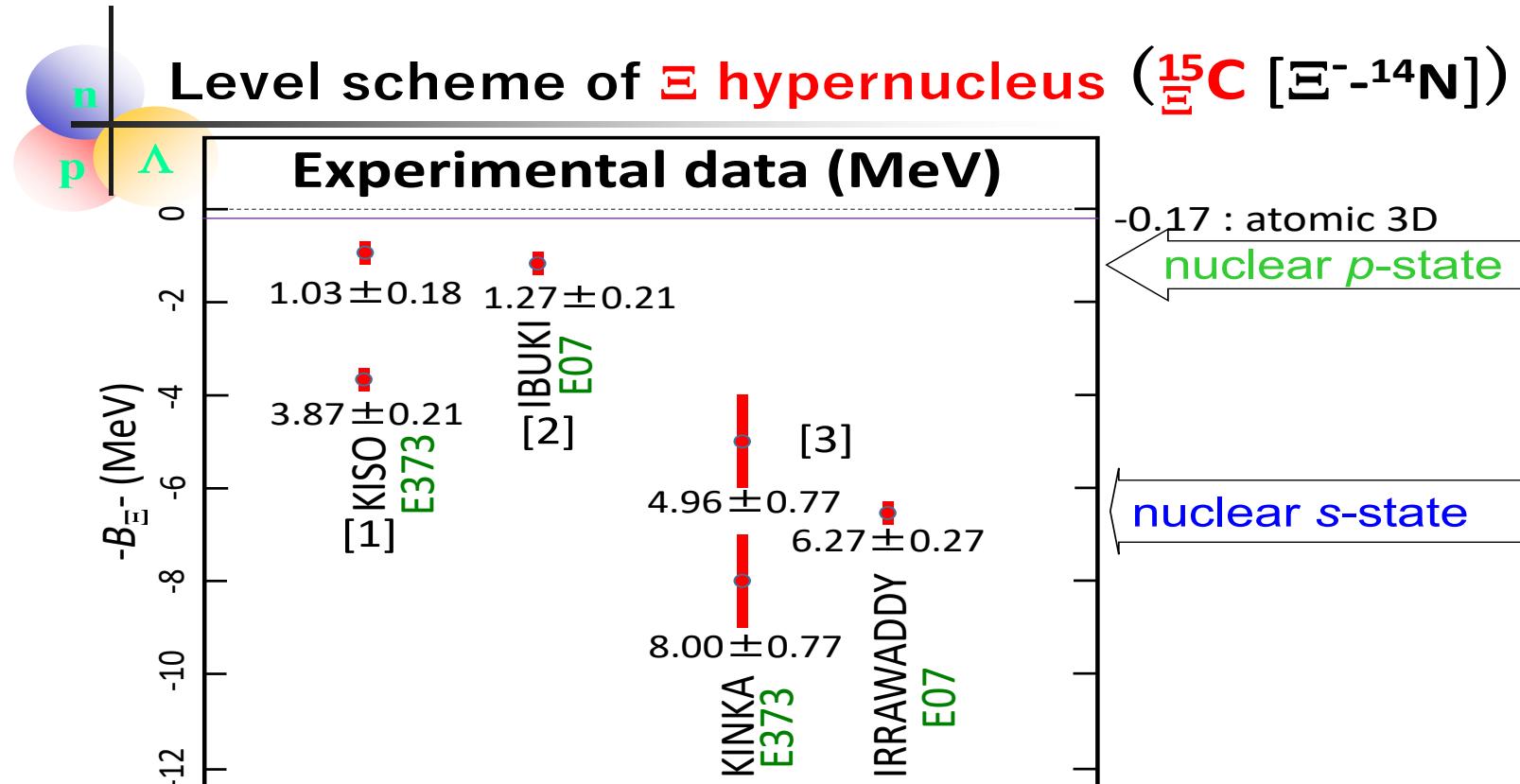
# Femtoscopy study of p- $\Xi^-$ correlations

ALICE, PRL 123 (2019) 112002

attractive HAL-QCD – yes  
repulsive Nijmegen ESC16 – no



# J-PARC E07 $^{14}\text{N}$ events



- [1] K. Nakazawa, et. al., Prog. Theor. Exp. Phys. **2015**, 033D02 (2015),  
E. Hiyama and K. Nakazawa, Ann. Rev. Nucl. Part. Sci. **68**, 131 (2018).
- [2] S. Hayakawa, et. al., Phy. Rev. Lett., **126**, 062501 (2021).
- [3] M. Yoshimoto, et. al., Prog. Theor. Exp. Phys. **2021**, 073D02 (2021).

Yoshimoto et al., PTEP 2021 073D02  
 $1s_{\Xi^-}$  states reported only in  ${}^{14}\text{N}$

IRRAWADDY:  $\Xi_{1s}^- + {}^{14}\text{N} \rightarrow {}^5_{\Lambda}\text{He} + {}^5_{\Lambda}\text{He} + {}^4\text{He} + \text{n}$   
 IBUKI:  $\Xi_{1p}^- + {}^{14}\text{N} \rightarrow {}^5_{\Lambda}\text{He} + {}^{10}_{\Lambda}\text{Be}$

# Twin $\Lambda$ : capture & decay vertices

\*\*\*\* IBUKI (J-PARC E07) PRL 126 (2021) 062501

- A: **capture**  $\Xi_{1p}^- + {}^{14}\text{N} \rightarrow {}^5_\Lambda\text{He} + {}^{10}_\Lambda\text{Be}$
- B: **decay**  ${}^5_\Lambda\text{He} \rightarrow {}^4\text{He} + \text{p} + \pi^-$
- C: **decay**  ${}^{10}_\Lambda\text{Be} \rightarrow 3 \text{ or } 4 \text{ nuclei} + \text{neutrons}$

\*\*\* IRRAWADDY (J-PARC E07) PTEP 2021 073D02

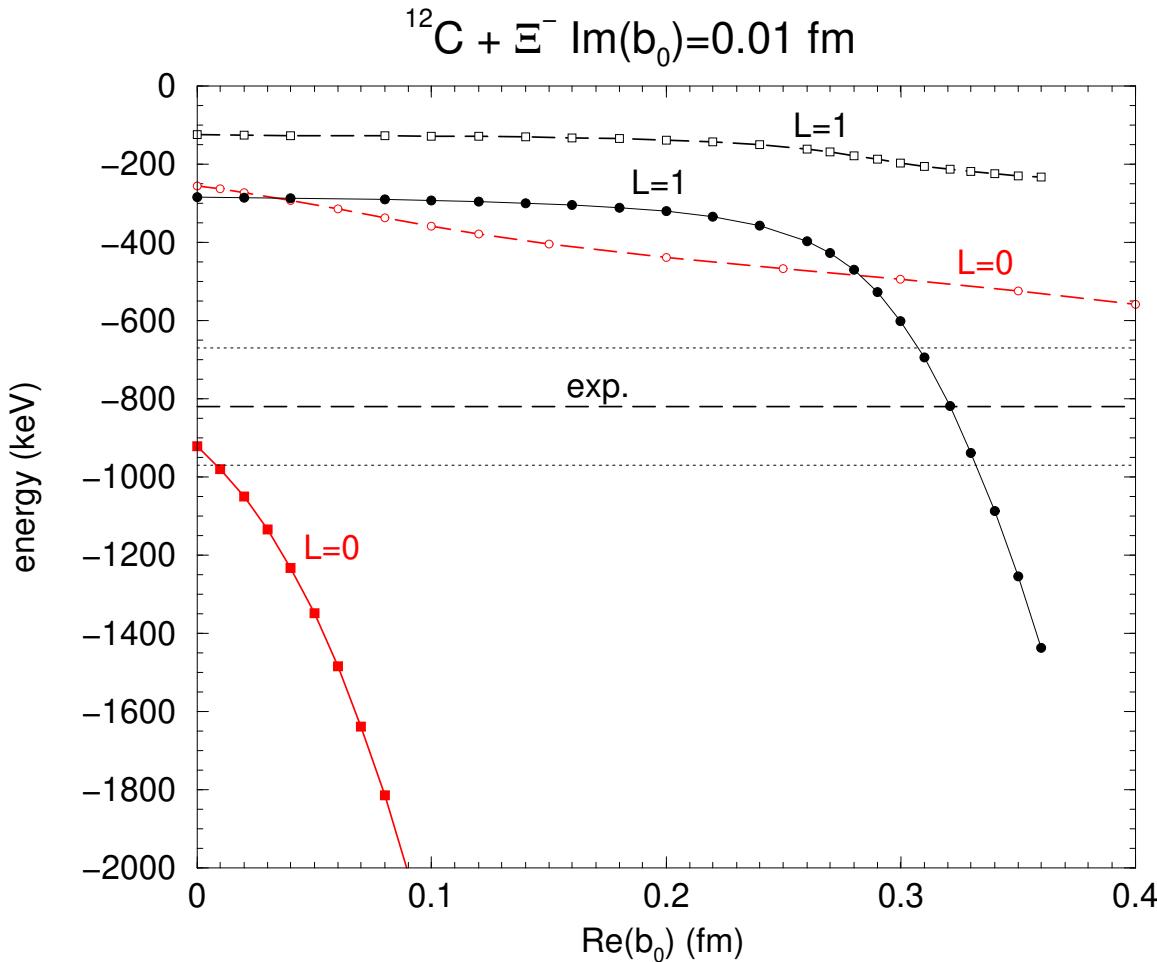
- A: **capture**  $\Xi_{1s}^- + {}^{14}\text{N} \rightarrow 2 {}^5_\Lambda\text{He} + {}^4\text{He} + \text{n}$
- B or C: **decay**  ${}^5_\Lambda\text{He} \rightarrow \text{d} + \text{p} + 2\text{n}$   
(or other ones, always with **fitted** neutrons)

Furthermore,  $1s_{\Xi^-}$  capture rate is only  
a few % of  $1p_{\Xi^-}$  capture rate

# Two-body $\Xi^-$ capture emulsion events

Experiment	Event	$^A_Z$	${}_{\Lambda}^{A'} Z' + {}_{\Lambda}^{A''} Z''$	$B_{\Xi^-}$ (MeV)
KEK E176	10-09-06	$^{12}\text{C}$	${}_{\Lambda}^4 \text{H} + {}_{\Lambda}^9 \text{Be}$	$0.82 \pm 0.17$
KEK E176	13-11-14	$^{12}\text{C}$	${}_{\Lambda}^4 \text{H} + {}_{\Lambda}^9 \text{Be}^*$	$0.82 \pm 0.14$
KEK E176	14-03-35	$^{14}\text{N}$	${}_{\Lambda}^3 \text{H} + {}_{\Lambda}^{12} \text{B}$	$1.18 \pm 0.22$
KEK E373	KISO	$^{14}\text{N}$	${}_{\Lambda}^5 \text{He} + {}_{\Lambda}^{10} \text{Be}^*$	$1.03 \pm 0.18$
J-PARC E07	IBUKI	$^{14}\text{N}$	${}_{\Lambda}^5 \text{He} + {}_{\Lambda}^{10} \text{Be}$	$1.27 \pm 0.21$

- $\Xi^-$  capture occurs mostly from 3D atomic state ( $B_{\Xi^-} = 126, 175$  keV in  $^{12}\text{C}$ ,  $^{14}\text{N}$ , respectively).
- To form  $1s_{\Lambda}^2$  in  $\Xi^- p \rightarrow \Lambda\Lambda$  need  $l_{\Xi^-} = l_p$ , hence expect capture from a Coulomb-assisted  $1p_{\Xi^-}$  nuclear state bound by  $\sim 1$  MeV, evolving by Strong Interaction from a 2P atomic state.



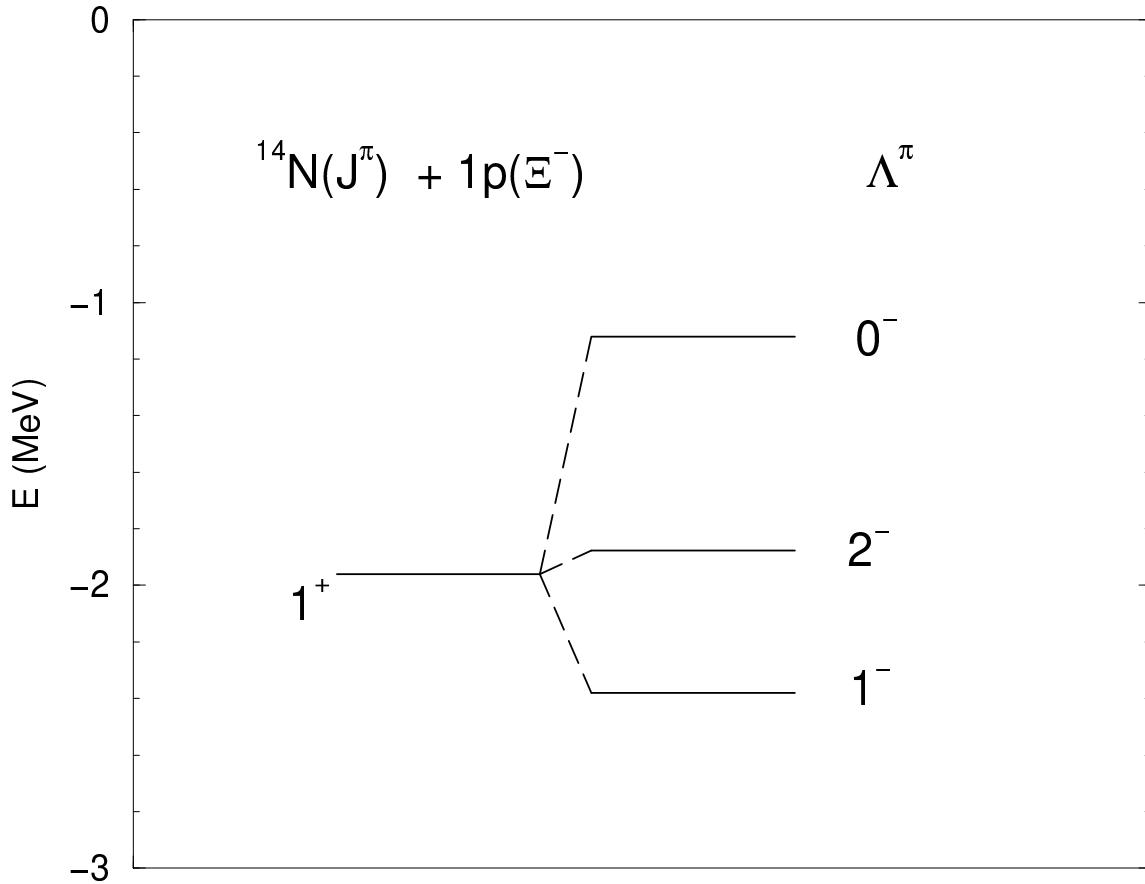
$V_{\text{opt}} = t\rho \sim b_0\rho(r)$ : scan over  $\text{Re } b_0$

Rearrangement:  $3\text{P} \rightarrow 2\text{P}$ ,  $2\text{S} \rightarrow 1\text{S}$ ,  $2\text{P} \rightarrow 1\text{p}$ ,  $1\text{S} \rightarrow 1\text{s}$

Fit exp.:  $\text{Re } b_0 = 0.32 \pm 0.01$  fm  $\Rightarrow V_\Xi = 24.3 \pm 0.8$  MeV

Pauli corrected:  $21.9 \pm 0.7$  MeV, but fails in  $^{14}\text{N}$ :

$B_{1p}^{\Xi^-}$  (calc.) =  $1.96 \pm 0.25$  vs.  $B_{1p}^{\Xi^-}$  (exp.) =  $1.15 \pm 0.20$  MeV



$^{14}\text{N}_{\text{g.s.}}(1^+)$  split by shell-model residual interaction

$$\mathbf{F}_{\Xi N}^{(2)} \mathbf{Q}_N \cdot \mathbf{Q}_\Xi \quad \mathbf{Q} = \sqrt{\frac{4\pi}{5}} \mathbf{Y}_2(\hat{r})$$

$$\mathbf{F}_{\Xi N}^{(2)} = -3 \text{ MeV} \Rightarrow B_{1p}^{\Xi^-}(0^-) = 1.12 \pm 0.25 \text{ MeV}$$

agrees with  $B_{1p}^{\Xi^-}(\text{exp.}) = 1.15 \pm 0.20 \text{ MeV}$

# Density Dependence of $V_\Xi$

$$b_0 \rightarrow b_0(\rho) : \quad \text{Re } b_0(\rho) = \frac{\text{Re } b_0}{1 + \frac{3k_F}{2\pi} \text{Re } b_0^{\text{lab}}}$$

for Pauli correlations, with  $k_F = (3\pi^2\rho/2)^{1/3}$ ,  
reducing  $V_\Xi(\rho_0) = 24.3 \pm 0.8$  to  $21.9 \pm 0.7$  MeV,  
with a systematic uncertainty of  $\approx 1$  MeV.

- A similar procedure fitting both 1s & 1p states in  $^{16}_\Lambda\text{N}$ :  $V_\Lambda(\rho_0) \approx 30$  MeV (FG22).
- $B_{1s}(\Xi^-) \approx 10$  MeV in  $^{12}\text{C}$ ,  $\approx 11.5$  MeV in  $^{14}\text{N}$ ,  
much larger than Kinka's  $8.0 \pm 0.8$  MeV.
- Expect  $B_{1s}(\Xi^-) \approx 8\text{--}9$  MeV in  $^{12}\text{C}(K^-, K^+)$   
(J-PARC E05 → E70).
- Could  $\Xi\text{NN}$  contributions prove useful?

# Remarks on SHF Calculations

Guo-Zhou-Schulze, PRC 104 (2021) L061307

Suppressing SHF nonlocal terms and assuming  $m_{\Xi}^* = m_{\Xi}$ , the SHF  $\Xi$  mean field depth  $V_{\Xi}(\rho_0)$  in n.m. density  $\rho_0=0.17 \text{ fm}^{-1}$  is fixed by fitting

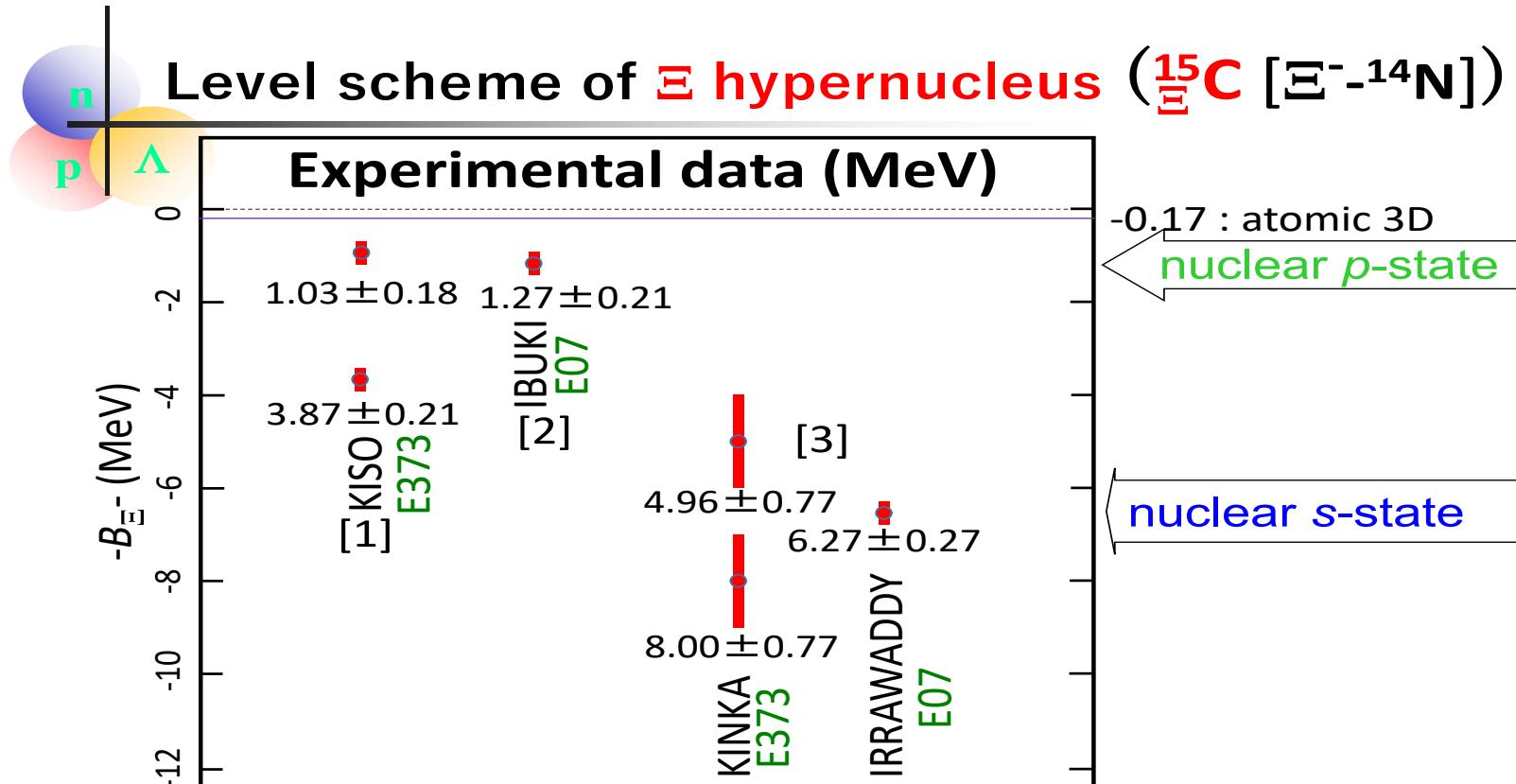
$$V_{\Xi}(\rho_N) = [V_{\Xi}^{(2)}(\rho_N) = a_0\rho_N] + [V_{\Xi}^{(3)}(\rho_N) = a_3\rho_N^2]$$

in  ${}^{14}\text{N}$  to  $B_{\Xi^-}(1s) \approx 8.00 \text{ MeV}$  (KINKA)

and  $B_{\Xi}(1p) \approx 1.15 \text{ MeV}$  (KISO & IBUKI).

Method	Pauli	$V_{\Xi}^{(2)}(\rho_0)$	$V_{\Xi}^{(3)}(\rho_0)$	$V_{\Xi}(\rho_0)$ (MeV)
SHF	No	34.1	-20.4	13.7
$V_{\text{opt}}$	No	27.5	-12.6	14.9
$V_{\text{opt}}$	Yes	24.6	-11.0	13.6

# J-PARC E07 $^{14}\text{N}$ events



[1] K. Nakazawa, et. al., Prog. Theor. Exp. Phys. **2015**, 033D02 (2015),  
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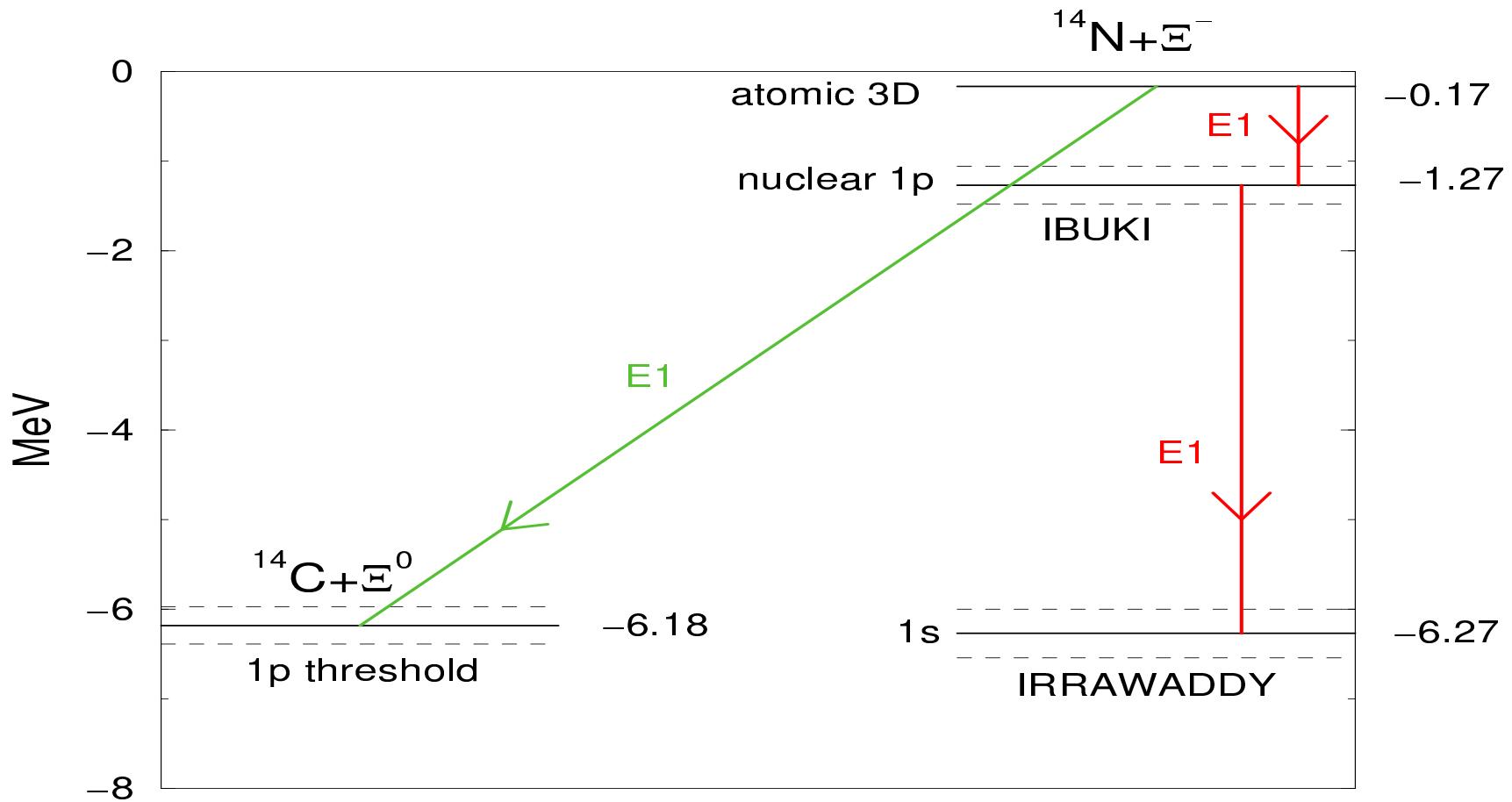
[2] S. Hayakawa, et. al., Phy. Rev. Lett., **126**, 062501 (2021).

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Yoshimoto et al., PTEP 2021 073D02

$1s_{\Xi^-}$  states reported only in  $^{14}\text{N}$

# $1s_{\Xi^-}$ interpreted as $1p_{\Xi^0}$



Friedman-Gal, PLB 837 (2023) 137640

$\Xi^0$  relevance unique to  $^{14}\text{N}$ , not in  $^{12}\text{C}$  or  $^{16}\text{O}$ .

$\Xi^- p \leftrightarrow \Xi^0 n$  ch. exch. induces  $^{14}\text{N} + \Xi^-_{1p} \leftrightarrow ^{14}\text{C} + \Xi^0_{1p}$  mixing.

$^{14}\text{N} + \Xi^-_{3D}$  decays by E1 to both  $^{14}\text{N} + \Xi^-_{1p}$ ,  $^{14}\text{C} + \Xi^0_{1p}$ .

# $\Xi^-$ capture: Summary & Outlook

- $V_{\Xi}(\rho_0) = 24.3 \pm 0.8 \Rightarrow 21.9 \pm 0.7$  MeV with Pauli from twin- $\Lambda$  two-body  $\Xi^-$  capture events.
- KEK-E224 & BNL-E885:  $V_{\Xi}(\rho_0) \approx 16 \pm 2$  MeV.
- BNL-E906:  $V_{\Xi}(\rho_0) = 17 \pm 6$  MeV (QF in  ${}^9\text{Be}$ ).
- EFT & LQCD suggest  $V_{\Xi}(\rho_0) \leq 10$  MeV.
- SHF using E07  ${}^{14}\text{N}$  input:  $V_{\Xi} \approx 14 \pm 1$  MeV, with attractive  $\Xi N$  & repulsive  $\Xi NN$  terms.
- Why all E07  $\Xi_{1s}^-$ -assigned events are in  ${}^{14}\text{N}$ ? A  $\Xi_{1p}^0 - {}^{14}\text{C}$  assignment is more natural.
- Challenge: find one good  $\Xi_{1s}^- - {}^{12}\text{C}$  capture event.

Thanks for your attention!

# The Elusive H Dibaryon

Remarks triggered by G. Farar's 2003 idea

to make H a deeply bound dibaryon,

a long-lived Dark-Matter candidate.

Most recent: arXiv:2306.03123 [hep-ph]

# The elusive H dibaryon

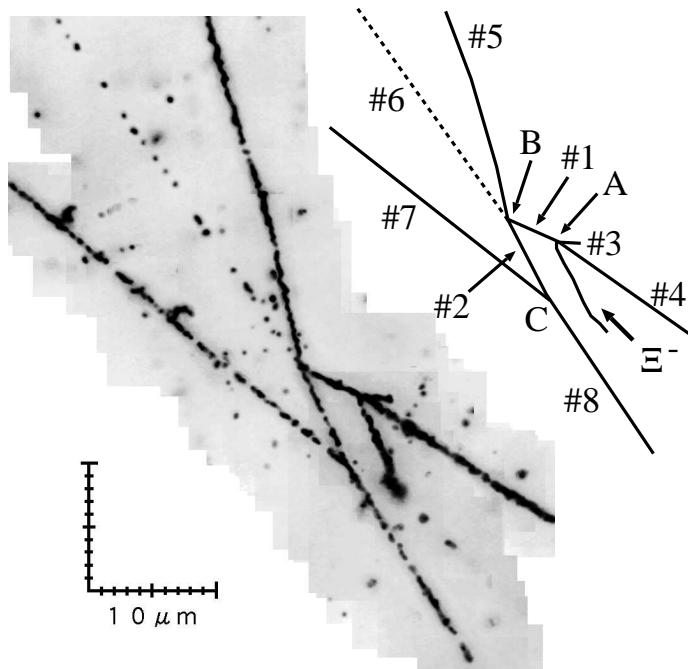
Jaffe's H(uuddss) [PRL 38 (1977) 195] predicted stable

$$H \sim A[\sqrt{1/8} \Lambda\Lambda + \sqrt{1/2} N\Xi - \sqrt{3/8} \Sigma\Sigma,]_{I=S=0}$$

- No H signal in past ( $K^-, K^+$ ) experiments at AGS-BNL & PS-KEK. **Awaiting J-PARC E42.**
- Bound H ruled out by **STAR** study of  $\Lambda\Lambda$  correlation femtoscopy [PRL 114 (2015) 022301].
- Bound H **not** ruled out by **ALICE** study of  $\Lambda\Lambda$  correlation femto [PLB 797 (2019) 134822].
- Bound H **above**  $\Lambda p\pi^-$ ,  $\sim 37$  MeV below  $\Lambda\Lambda$ , ruled out by **ALICE** search for a weakly decaying  $\Lambda\Lambda$  bound state [PLB 752 (2016) 267].

- Bound H **above**  $\Lambda p\pi^-$  ruled out in **Belle** study of  $\Upsilon(1S,2S)$  decays [PRL 110 (2013) 222002].
- Deeply bound H **below**  $\Lambda n$ ,  $m_H \leq 2.05$  GeV, ruled out in **BaBar's**  $\Upsilon(2S,3S) \rightarrow H\bar{\Lambda}\bar{\Lambda}$  search [PRL 122 (2019) 072002].
- H is weakly bound in LQCD calculations, e.g., PRL 127 (2021) 242003, see **Wittig's** talk. SU(3)<sub>f</sub> **breaking** might push it to  $\approx 26$  MeV in the  $\Lambda\Lambda$  continuum, **near NΞ threshold**: HALQCD Collaboration [NPA 881 (2012) 28] & Haidenbauer-Meißner [NPA 881 (2012) 44].

# Constraints from Hypernuclei



Nagara event,  $\Lambda\Lambda^6\text{He}$ , (KEK-E373) PRL 87 (2001) 212502  
 $B_{\Lambda\Lambda}(\Lambda\Lambda^6\text{He}_{\text{g.s.}}) = 6.91 \pm 0.16 \text{ MeV}$ , uniquely identified.

- A:  $\Xi^-$  capture  $\Xi^- + {}^{12}\text{C} \rightarrow \Lambda\Lambda^6\text{He} + t + \alpha$
- B: weak decay  $\Lambda\Lambda^6\text{He} \rightarrow {}^5_\Lambda\text{He} + p + \pi^-$  (no  $\Lambda\Lambda^6\text{He} \rightarrow {}^4\text{He} + \text{H}$ )
- C:  ${}^5_\Lambda\text{He}$  nonmesic weak decay to two  $Z=1$  recoils + n.

Few other weakly decaying  $\Lambda\Lambda^A\text{Z}$  hypernuclei identified.

# Constraints from Hypernuclei

- To forbid  ${}_{\Lambda\Lambda}^6\text{He} \rightarrow \text{H} + {}^4\text{He}$ , set  $B(\text{H}) \leq 7 \text{ MeV}$ . However,  ${}_{\Lambda\Lambda}^6\text{He}$  comes out then **overbound** [Gal, PRL 110 (2013) 179201].
- A correlated  $\Lambda\Lambda$  pair in a given  ${}_{\Lambda\Lambda}^A\text{Z}$  would decay **strongly** to a bound H, contrary to observing  ${}_{\Lambda\Lambda}^A\text{Z}$  in **weak decay**. Furthermore,
- $\text{H} \rightarrow \Lambda n$  weakly,  $\tau \sim 10^{-10} \text{ sec}$ . If below  $\Lambda n$ , it decays weakly,  $\text{H} \rightarrow nn$ , by  $\pi$  exchange, with  $\tau$  not much longer than 1yr,  $\ll \tau(\text{Universe})$ .
- Thus, a deeply bound **uuddss ‘sexaquark’** fails as a long-lived **Dark-Matter** candidate [Gal-Schaefer, in preparation].