

ULTRAPERIPHERAL HEAVY-ION COLLISIONS - THEORY CONSIDERATIONS

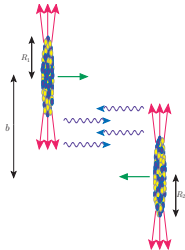
Mariola Kłusek-Gawenda

*The Henryk Niewodniczański Institute of Nuclear Physics
Polish Academy of Sciences*

- Equivalent Photon Approximation
- $\gamma\gamma \rightarrow \gamma\gamma$
- $\ell^+\ell^-\ell^+\ell^-$ production
- $\pi^+\pi^-\pi^+\pi^-$ production
- Electromagnetic excitation of nuclei and neutron evaporation

2023 CMS heavy ion workshop: bringing together the LHC heavy ion community

ULTRAPERIPHERAL COLLISION OF HEAVY IONS



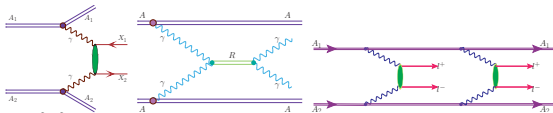
The strong electromagnetic field is a source of photons that can induce electromagnetic reactions in ion-ion collisions. Electromagnetism is a long-range force, so electromagnetic interactions occur even at relatively large ion-ion separations.

$$\text{UPC: } b_{\min} = R_1 + R_2 \approx 14 \text{ fm}$$

$$\text{Photon energy: } \omega = \frac{\gamma}{b_{\min}} \approx \gamma \times 15 \text{ MeV}$$

$$\text{Virtuality: } Q^2 = \frac{1}{R^2} \approx 0.0008 \text{ GeV}^2$$

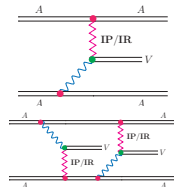
$\gamma\gamma$ fusion



- ✓ $\rho^0 \rho^0, J/\psi J/\psi$
- ✓ $\pi^+ \pi^-, \pi^0 \pi^0$
- ✓ $c\bar{c}, b\bar{b}$
- ✓ $e^+ e^-, \mu^+ \mu^-, \tau^+ \tau^-$
- ✓ $\gamma\gamma$

- ✓ $p\bar{p}$
- ✓ $\pi^+ \pi^- \pi^+ \pi^-$
- ✓ $e^+ e^- e^+ e^-$
- ✓ $\mu^+ \mu^- \mu^+ \mu^-$

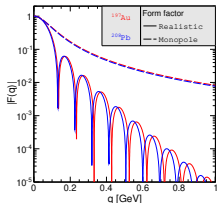
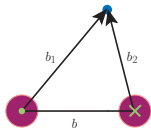
Photoproduction



- ✓ $\rho^0, J/\psi$
- ✓ $\rho^0 \rho^0, J/\psi J/\psi$

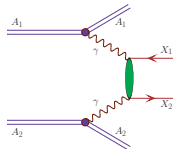
EQUIVALENT PHOTON APPROXIMATION

$$\begin{aligned}
 \sigma_{A_1 A_2 \rightarrow A_1 A_2 X_1 X_2} &= \int \sigma_{\gamma\gamma \rightarrow X_1 X_2}(\omega_1, \omega_2) d\omega_1 d\omega_2 n(\omega_1) n(\omega_2) \rightarrow \dots n(\omega) = \int_{R_{min}}^{\infty} 2\pi b db N(\omega, b) \dots \\
 &= \int \sigma_{\gamma\gamma \rightarrow X_1 X_2}(W_{\gamma\gamma}) N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2} d\bar{b}_x d\bar{b}_y d^2 b \\
 &= \int \frac{d\sigma_{\gamma\gamma \rightarrow X_1 X_2}(W_{\gamma\gamma})}{d \cos \theta} N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2} d\bar{b}_x d\bar{b}_y d^2 b \\
 &\times \frac{d \cos \theta}{dy_{X_1} dy_{X_2} dp_t} \times dy_{X_1} dy_{X_2} dp_t.
 \end{aligned}$$

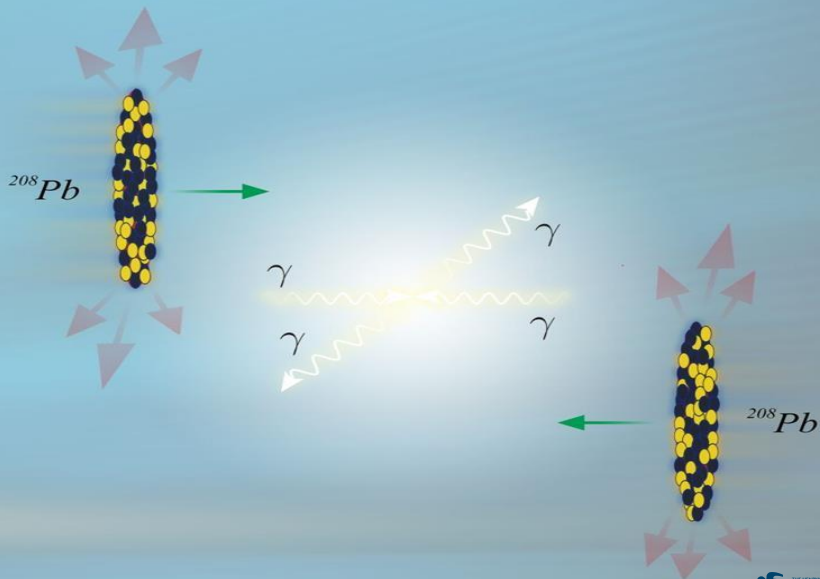


$$N(\omega, b) = \frac{Z^2 \alpha_{em}}{\pi^2 \beta^2} \frac{1}{\omega} \frac{1}{b^2} \times \left| \int d\chi \chi^2 \frac{F\left(\frac{\chi^2 + u^2}{b^2}\right)}{\chi^2 + u^2} J_1(\chi) \right|^2$$

$$F(\mathbf{q}^2) = \frac{4\pi}{|\mathbf{q}|} \int \rho(r) \sin(|\mathbf{q}| r) r dr$$



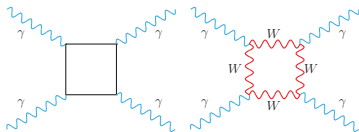
LIGHT-BY-LIGHT SCATTERING



LIGHT-BY-LIGHT SCATTERING

Boxes

WELL-KNOWN



Fermionic boxes (LO QED)

FormCalc.

W Box

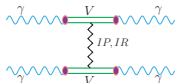
LoopTools.

$$|\mathcal{M}_{\gamma\gamma \rightarrow \gamma\gamma}|^2 = \alpha_{em}^4 f(\hat{t}, \hat{u}, \hat{s})$$

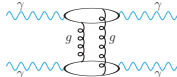
VDM-Regge

WE ADD

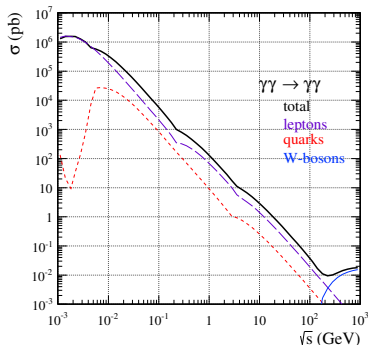
2-gluon exch.



fluctuation of γ
into virtual ρ, ω, ϕ



formally 3-loops



We have compared our results with:

- Jikia et al. (1993),
- Bern et al. (2001),
- Bardin et al. (2009).

Bern et al. consider QCD and QED corrections ([two-loop Feynman diagrams](#)) to the one-loop fermionic contributions in the ultrarelativistic limit ($\hat{s}, |\hat{t}|, |\hat{u}| \gg m_f^2$).
The corrections are [quite small numerically](#).

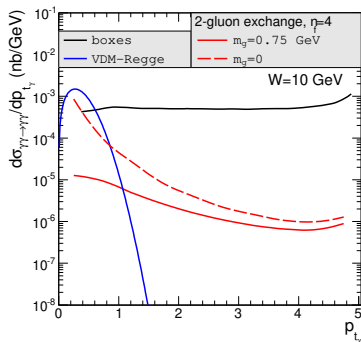
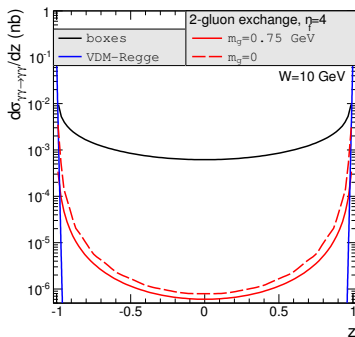
ELEMENTARY CROSS SECTION

$$z = \cos \theta$$

- ✓ boxes
- ✓ VDM-Regge
- ✓ 2-gluon exchange

$$W = 10 \text{ GeV}$$

$$p_{t\gamma} = p \sin \theta$$



$\theta = \frac{\pi}{2}$ - boxes , large z (low $p_{t\gamma}$) - VDM-Regge.

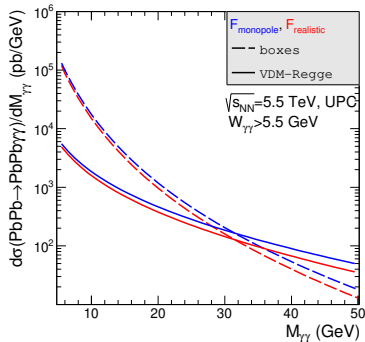
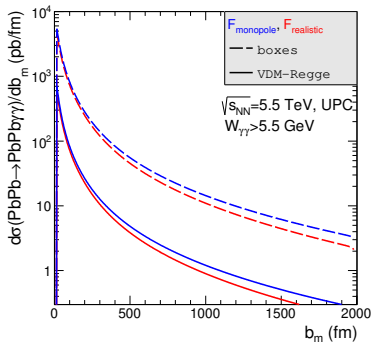
AA \rightarrow AA $\gamma\gamma$ - FORM FACTOR

\Rightarrow realistic

\Rightarrow monopole

impact parameter

$W_{\gamma\gamma} = M_{\gamma\gamma}$



\uparrow theoretical distribution

VDM-Regge: $W_{\gamma\gamma} > 30$ GeV

$\frac{\sigma_{monopole}}{\sigma_{realistic}}$ \nearrow for larger value of kinematical variables

AA \rightarrow AA $\gamma\gamma$ - CMS & ATLAS RESULTS - $M_{\gamma\gamma} > 5$ GeV

\Rightarrow CMS Coll., Phys. Lett. **B797** (2019) 134826

x $E_{t\gamma} > 2$ GeV

x $|\eta_{\gamma}| < 2.4$

x $M_{\gamma\gamma} > 5$ GeV

x $p_{t\gamma\gamma} < 1$ GeV

x $A_{co} < 0.01$

\Rightarrow ATLAS Collaboration, JHEP **03** (2021) 243

x $E_{t\gamma} > 2.5$ GeV

x $|\eta_{\gamma}| < 2.4$

x $M_{\gamma\gamma} > 5$ GeV

x $p_{t\gamma\gamma} < 1$ GeV

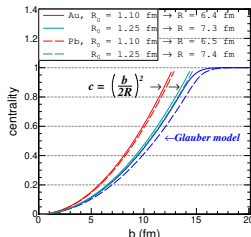
x $A_{co} < 0.01$

| Experiment | | Theory | | |
|-------------------|---|-----------------------------------|-----------------------------|---------------------------|
| Collaboration | σ nb | Nuclear radius: $R = R_0 A^{1/3}$ | | Glauber model |
| | | $\sigma(b = 13\text{fm})$ | $\sigma(b = 14.8\text{fm})$ | $\sigma(b = 20\text{fm})$ |
| ATLAS (2018 data) | $78 \pm 13(\text{stat.}) \pm 7(\text{syst.})$ | 52 | 50 | 45 |
| ATLAS (2015+2018) | $120 \pm 17(\text{stat.}) \pm 13(\text{syst.})$ | 82 | 80 | 71 |
| CMS (2015) | $120 \pm 46(\text{stat.}) \pm 28(\text{syst.})$ | 105 | 103 | 92 |

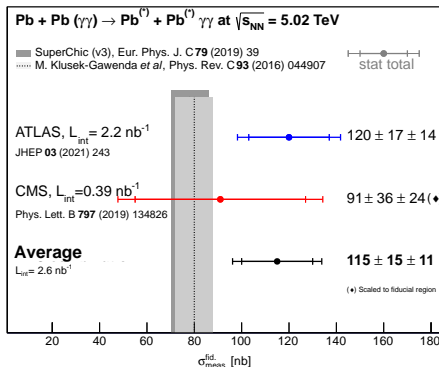
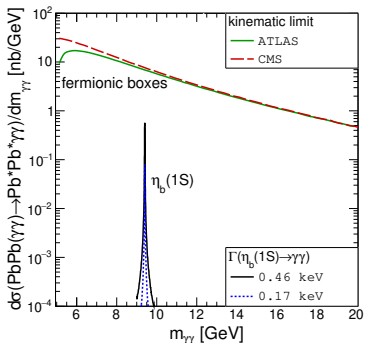
UPC $\rightarrow b_{min} > 2 \times R$

SO FAR IT WAS 14 FM

| | |
|--------------------|--------|
| centrality [%] | 100 |
| nucleus and radius | b (fm) |
| Pb, $R = 6.5$ fm | 13.0 |
| Pb, $R = 7.4$ fm | 14.8 |
| Pb Pb, Glauber | 20.0 |

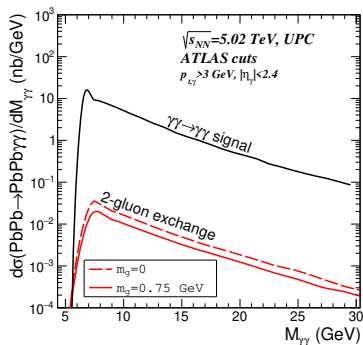


2022 RESULTS

 $\eta_b(1S)$ The averaged $\sigma(Pb + Pb \rightarrow Pb + Pb\gamma\gamma)$ 

- The European Union's Horizon 2020 research and innovation program under STRONG-2020, G. K. Krintiras, I. Grabowska-Bold, M. Klusek-Gawenda and É. Chapon and R. Chudasama, *Acta Phys. Polon. Supp.* **16** (2023) 1, 123;
Light-by-light scattering cross-section measurements at LHC

HIGHER ORDER PROCESSES..?

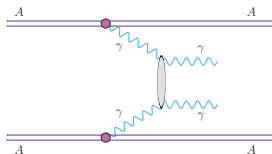
 $\gamma\gamma$ invariant mass

Coherent sum of both processes...?

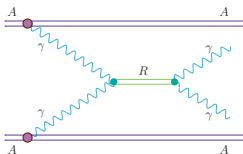
Pionic boxes...?

AA → AAγγ FOR $M_{\gamma\gamma} < 5$ GeV ?

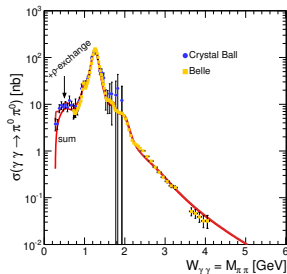
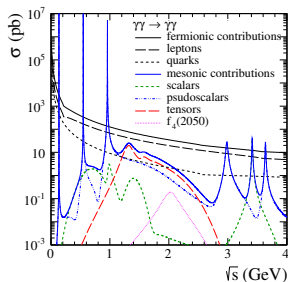
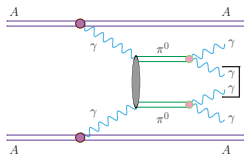
CONTINUUM



RESONANCES



BACKGROUND



⇒ P. Lebedowicz, A. Szczurek, *Phys. Lett.* **B772** (2017) 330,
The role of meson exchanges in light-by-light scattering

⇒ M. K-G, A. Szczurek, *Phys. Rev.* **C87** (2013) 054908;
 $\pi^+\pi^-$ and $\pi^0\pi^0$ pair production in photon-photon
and in ultraperipheral ultrarelativistic heavy-ion collisions

UPC OF AA...

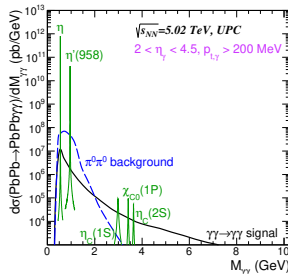
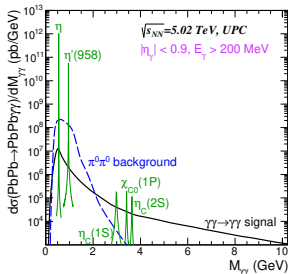
ALICE cuts

✓ boxes

✓ bkg

✓ mesons

LHCb cuts



Total nuclear cross section [nb]

| Energy | $W_{\gamma\gamma} = (0 - 2) \text{ GeV}$ | | $W_{\gamma\gamma} > 2 \text{ GeV}$ | |
|-------------------|--|---------|------------------------------------|------|
| | ALICE | LHCb | ALICE | LHCb |
| Fiducial region | | | | |
| Boxes | 4 890 | 3 818 | 146 | 79 |
| $\pi^0 \pi^0$ bkg | 135 300 | 40 866 | 46 | 24 |
| η | 722 573 | 568 499 | | |
| $\eta'(958)$ | 54 241 | 40 482 | | |
| $\eta_c(1S)$ | | | 9 | 5 |
| $\chi_{c0}(1P)$ | | | 4 | 2 |
| $\eta_c(2S)$ | | | 2 | 1 |

AA \rightarrow AA $\gamma\gamma$ @ FORWARD REGION ?

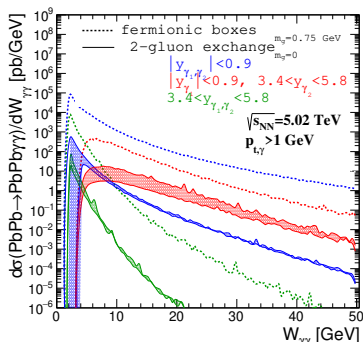
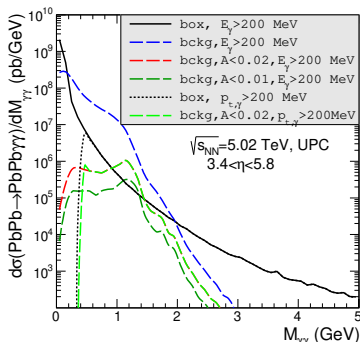
- ✓ ALICE Collaboration,
Letter of Intent: A Forward Calorimeter (FoCal) in the ALICE experiment,
CERN-LHCC-2020-009

FoCAL $\rightarrow 3.4 < \eta < 5.8$

The forward electromagnetic and hadronic calorimeter is an upgrade to the ALICE experiment, to be installed during LS3 for data-taking in 2027–2029 at the LHC.

$E_\gamma > 0.2$ GeV

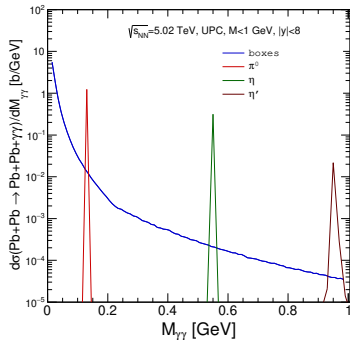
$p_{t,\gamma} > 1$ GeV



Boxes & Pionic bkg & 2-gluon exchange (with effective gluon mass)

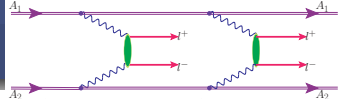
AA \rightarrow AA $\gamma\gamma$ @ LOW p_t REGION ?

$$M_{\gamma\gamma} < 1 \text{ GeV}$$



$$\gamma\gamma \rightarrow \pi^0 \rightarrow \gamma\gamma$$

FOUR-LEPTON PRODUCTION



$$\frac{d\sigma_{A_1 A_2 \rightarrow A_1 A_2 (\ell^+ \ell^-) (\ell'^+ \ell'^-)}}{dy_{\ell^+}^I dy_{\ell^-}^I dy_{\ell'^+}^{II} dy_{\ell'^-}^{II}} = \frac{1}{2} \int \left(\frac{dP^I}{\gamma\gamma \rightarrow \ell^+ \ell^- (b, y_{\ell^+}^I, y_{\ell^-}^I; p_{t, \ell})} \times \frac{dP^{II}}{\gamma\gamma \rightarrow \ell'^+ \ell'^- (b, y_{\ell'^+}^{II}, y_{\ell'^-}^{II}; p_{t, \ell})} \right)$$

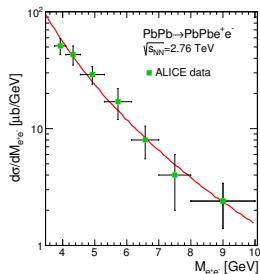
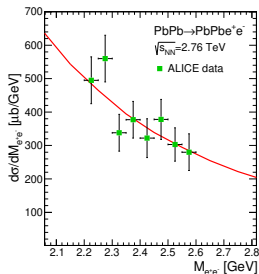
$$\times 2\pi b db$$

$$P_{\gamma\gamma \rightarrow \ell^+ \ell^-} (b; y_{\ell^+}, y_{\ell^-}, p_{t, \ell}) = \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \times \frac{d\sigma_{\gamma\gamma \rightarrow \ell_1 \ell_2} (W_{\gamma\gamma})}{d \cos \theta} d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{\ell_1 \ell_2}$$

$$2.2 \text{ GeV} < M_{ee} < 2.6 \text{ GeV}$$

$$|y_e| < 0.9$$

$$3.7 \text{ GeV} < M_{ee} < 10 \text{ GeV}$$

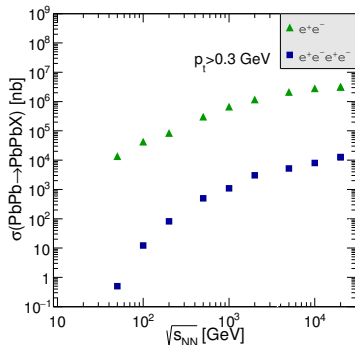


Good description of single pair production \Rightarrow two $e^+ e^-$ pair production...?

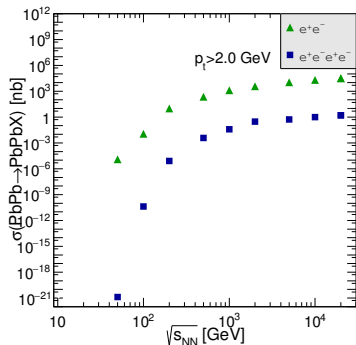
$$AA \rightarrow AAe^+e^- \text{ \& \ } AA \rightarrow AAe^+e^-e^+e^-$$

Single e^+e^- pair production vs. double scattering production of two e^+e^- pairs

$p_t > 0.3 \text{ GeV}$



$p_t > 2.0 \text{ GeV}$



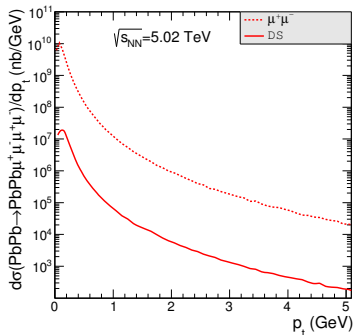
$$AA \rightarrow AA\mu^+\mu^- \text{ \& \ } AA \rightarrow AA\mu^+\mu^-\mu^+\mu^-$$

Single $\mu^+\mu^-$ pair production

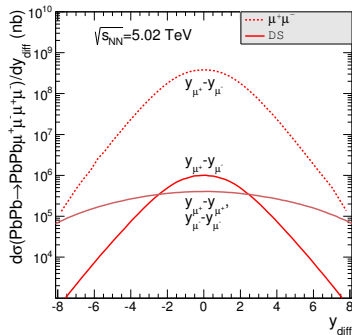
v.

double scattering production of two $\mu^+\mu^-$ pairs

$p_{t,\mu}$



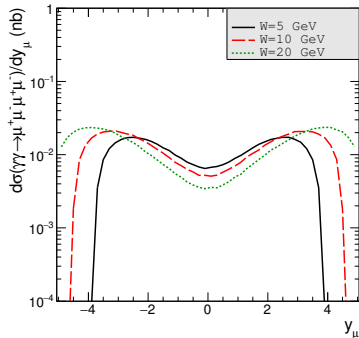
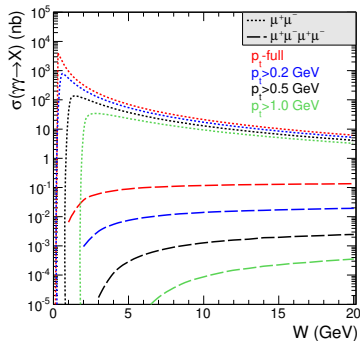
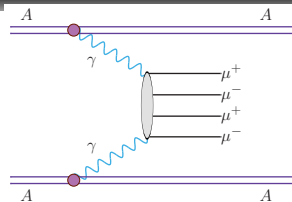
y_{diff}



$$\sigma_{\ell^+\ell^-} \simeq 1000 \times \sigma_{\ell^+\ell^-\ell^+\ell^-}$$

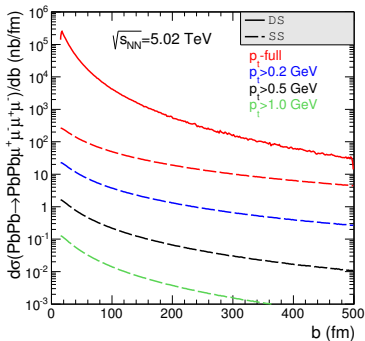
$\gamma\gamma \rightarrow \mu^+\mu^-\mu^+\mu^-$ - SINGLE SCATTERING


KATIE- an event generator that is specially designed to deal with initial states that have an explicit transverse momentum dependence but can also deal with on-shell initial states. KATIE is a parton-level generator for hadron scattering but requires only a few adjustments to deal with photon scattering.

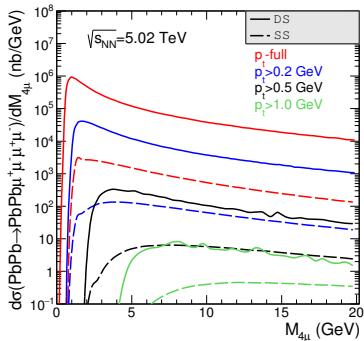


$$AA \rightarrow AA \mu^+ \mu^- \mu^+ \mu^-$$

impact parameter



$W_{\gamma\gamma} = M_{4\mu}$

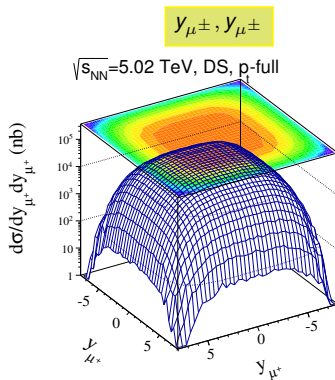
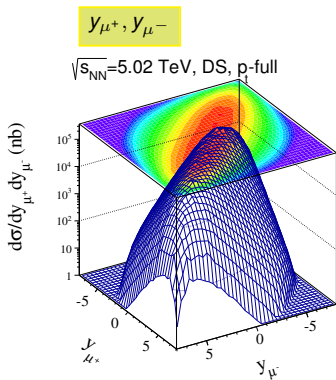


It is difficult to isolate range of SS domination

*DS - double-scattering mechanism

*SS - a NEW single-scattering mechanism

$$AA \rightarrow AA \mu^+ \mu^- \mu^+ \mu^-$$



creation of similar distributions by ALICE or CMS?

$$AA \rightarrow AA \pi^+ \pi^- \pi^+ \pi^-$$

H1 DATA

H1prelim-18-011

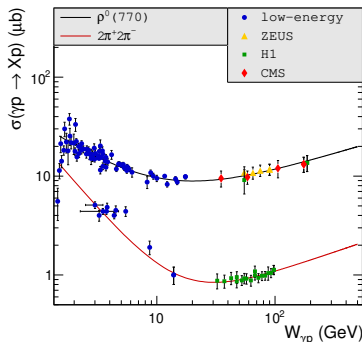
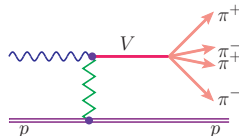
April 10, 2018

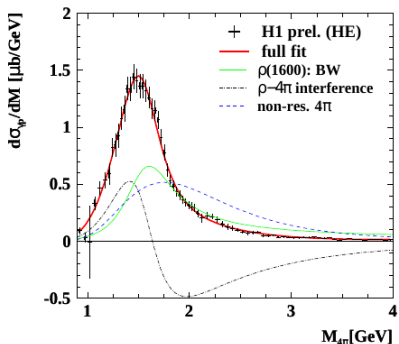
Submitted to **DIS-2018**, Kobe, 16–20 April, 2018

Exclusive Photoproduction of $2\pi^+2\pi^-$ Final State at H

Abstract

Exclusive production of four charged pions at the ep collider HERA is studied at small photon virtualities $Q^2 < 2 \text{ GeV}^2$. The data were taken with the H1 detector in the years 2006 and 2007 at a centre-of-mass energies of $\sqrt{s} = 319 \text{ GeV}$ and $\sqrt{s} = 225 \text{ GeV}$; correspond to an integrated luminosity of 7.6 pb^{-1} and 1.7 pb^{-1} respectively. The cross section of the reaction $\gamma p \rightarrow (2\pi^+2\pi^-)Y$ is determined in the phase space of $35 < W_{\gamma p} < 100 \text{ GeV}$, $|t| < 1 \text{ GeV}^2$ and $M_Y < 1.6 \text{ GeV}$. The 4π mass spectra indicate that the reaction proceeds predominantly via production and decay of ρ' resonances. The fit however does not allow yet to distinguish unambiguously between the hypotheses of one or two broad and overlapping ρ' resonances.

vector meson ?



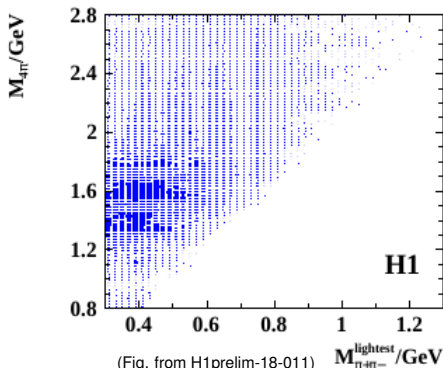
(Fig. from H1prelim-18-011)

77. The $\rho(1450)$ and the $\rho(1700)$

Updated November 2015 by S. Eidelman (Novosibirsk), C. Hanhart (Juelich) and G. Venanzoni (Frascati).

In our 1988 edition, we replaced the $\rho(1600)$ entry with two new ones, the $\rho(1450)$ and the $\rho(1700)$, because there was emerging evidence that the 1600-MeV region actually contains two ρ -like resonances. Erkel [1] had pointed out this possibility with a theoretical analysis on the consistency of 2π and 4π electromagnetic form factors and the $\pi\pi$ scattering length. Donnachie [2], with a full analysis of data on the 2π and 4π final states in e^+e^- annihilation and photoproduction reactions, had also argued that in order to obtain a consistent picture, two resonances were necessary. The existence of $\rho(1450)$ was supported by the analysis of $\eta\rho^0$ mass spectra obtained in photoproduction and e^+e^- annihilation [3], as well as that of $e^+e^- \rightarrow \omega\pi$ [4].

The analysis of [2] was further extended by [5,6] to include new data on 4π -systems produced in e^+e^- annihilation, and in τ -decays (τ decays to 4π , and e^+e^- annihilation to 4π can be related by the Conserved Vector Current assumption). These systems were successfully analyzed using interfering contributions from two ρ -like states, and from the tail of the $\rho(770)$ decaying into two-body states. While specific conclusions on $\rho(1450) \rightarrow 4\pi$ were obtained, little could be said about the $\rho(1700)$.



(Fig. from H1prelim-18-011)

DECAY MODE

$$M_{4\pi} = 1.6 \text{ GeV}$$

or

$$M_{4\pi} = 1.45 \text{ GeV} \ \& \ M_{4\pi} = 1.7 \text{ GeV}$$

RESONANCES SKETCH PDG

$\rho(1570)$

$$I^G(J^{PC}) = 1^+(1^{--})$$

$\rho(1570)$ MASS

| VALUE (MeV) | EVT5 | DOCUMENT ID | TECN | COMMENT |
|-----------------------|------|---------------------|----------|--|
| 1570 ± 36 ± 62 | 54 | ¹ AUBERT | 08S BABR | 10.6 e ⁺ e ⁻ → φπ ⁰ γ |

$\rho(1570)$ WIDTH

| VALUE (MeV) | EVT5 | DOCUMENT ID | TECN | COMMENT |
|----------------------|------|---------------------|----------|--|
| 144 ± 75 ± 43 | 54 | ³ AUBERT | 08S BABR | 10.6 e ⁺ e ⁻ → φπ ⁰ γ |

$\rho(1570)$ DECAY MODES

| Mode | Fraction (Γ _i /Γ) |
|--|------------------------------|
| Γ ₁ e ⁺ e ⁻ | |
| Γ ₂ φπ | not seen |
| Γ ₃ ωπ | |

$\rho(1450)$ [1]

$$I^G(J^{PC}) = 1^+(1^{--})$$

Mass $m = 1465 \pm 25$ MeV [1]
Full width $\Gamma = 400 \pm 60$ MeV [1]

| $\rho(1450)$ DECAY MODES | Fraction (Γ _i /Γ) | ρ (MeV/c) |
|-------------------------------|------------------------------|-----------|
| π π | seen | 720 |
| π ⁺ π ⁻ | seen | 719 |
| 4π | seen | 669 |

$\rho(1700)$ [1]

$$I^G(J^{PC}) = 1^+(1^{--})$$

Mass $m = 1720 \pm 20$ MeV [1] (ηρ⁰ and π⁺π⁻ modes)
Full width $\Gamma = 250 \pm 100$ MeV [1] (ηρ⁰ and π⁺π⁻ modes)

| $\rho(1700)$ DECAY MODES | Fraction (Γ _i /Γ) | ρ (MeV/c) |
|-----------------------------------|------------------------------|-----------|
| 2(π ⁺ π ⁻) | seen | 803 |

$\rho(770)$ [14]

$$I^G(J^{PC}) = 1^+(1^{--})$$

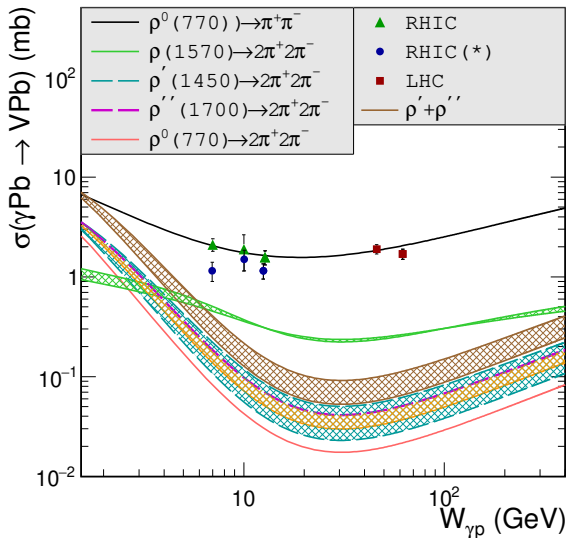
Mass $m = 775.26 \pm 0.25$ MeV
Full width $\Gamma = 149.1 \pm 0.8$ MeV
Γ_{ee} = 7.04 ± 0.06 keV

| $\rho(770)$ DECAY MODES | Fraction (Γ _i /Γ) | Scale factor/ Confidence level | ρ (MeV/c) |
|---|----------------------------------|-----------------------------------|--------------|
| π π | ~ 100 | % | 363 |
| π ⁺ π ⁻ π ⁺ π ⁻ | (1.8 ± 0.9) × 10 ⁻⁵ | | 251 |

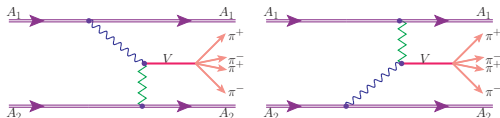
MY CALCULATION

| m [GeV] | Γ [GeV] | Γ(e ⁺ e ⁻) [keV] |
|----------------------------|--------------|---|
| $\rho(1570)$ | | |
| 1.57 ± 0.07 | 0.144 ± 0.09 | 0.35 – 0.5* |
| $\rho(1450) \equiv \rho'$ | | |
| 1.465 ± 0.025 | 0.40 ± 0.05 | 4.3 – 6* |
| $\rho(1700) \equiv \rho''$ | | |
| 1.72 ± 0.02 | 0.25 ± 0.01 | 7.6 ± 1.3 |

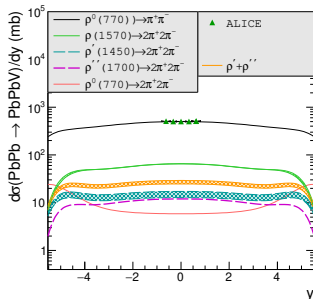
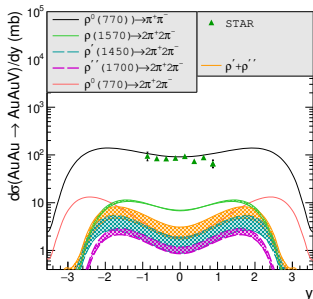
COHERENT VECTOR MESON PHOTOPRODUCTION

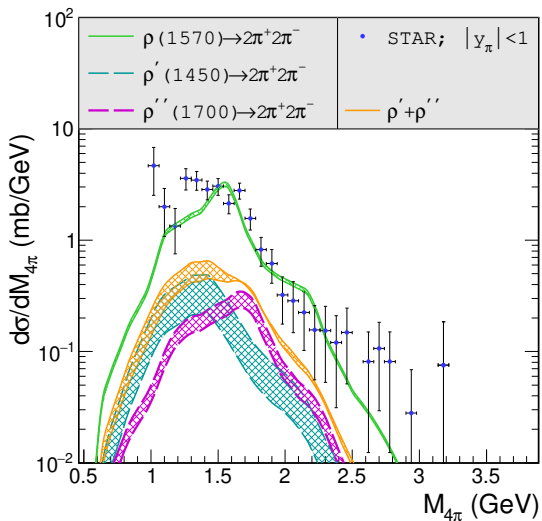


DIFFERENTIAL CROSS SECTION



$$\frac{\sigma(A_1 A_2 \rightarrow A_1 A_2 2\pi^+ 2\pi^-)}{dy_V} = d^2 b \times \left[\int \omega_1 \frac{dN(\omega_1, b)}{d^2 b d\omega_1} \sigma_{\gamma A_2 \rightarrow VA_2}(W_{\gamma A_2}) + \int \omega_2 \frac{dN(\omega_2, b)}{d^2 b d\omega_2} \sigma_{\gamma A_1 \rightarrow VA_1}(W_{\gamma A_2}) \right]$$

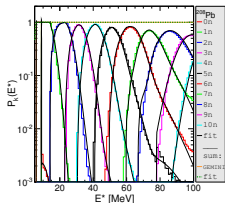
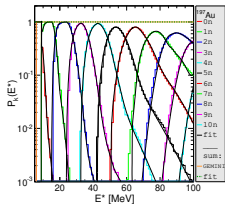




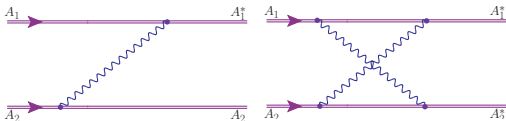
Success of $\rho(1570)$ - Results for the LHC are necessary

ELECTROMAGNETIC EXCITATION

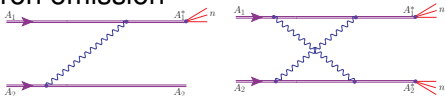
$$P_k(E^*)$$



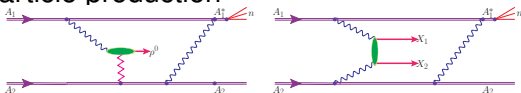
➤ Photon \rightarrow nucleus excitation

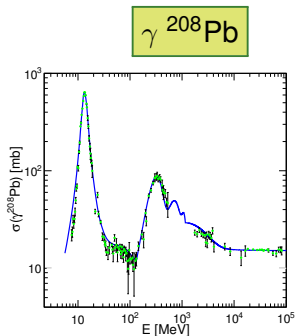
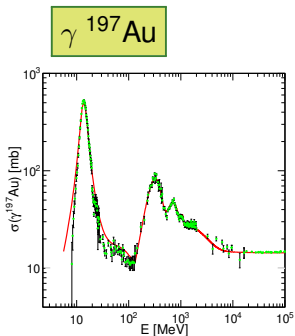


✚ neutron emission



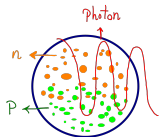
✚ particle production



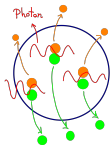


$$\sigma_{\gamma A} = \sigma_{\text{GDR}} + \sigma_{\text{QD}} + \sigma_{\text{nucleon res.}} + \sigma_{\text{nucleon cont.}}$$

- ❶ Giant Dipole Resonance
 $E_{\gamma} < 40$ MeV



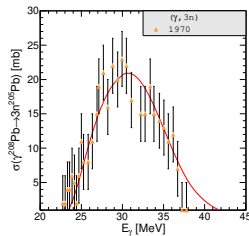
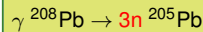
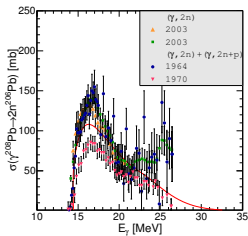
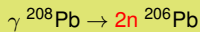
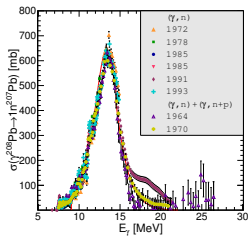
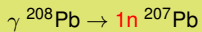
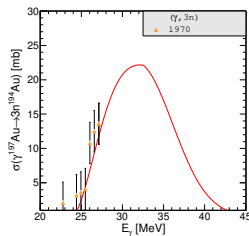
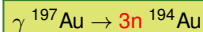
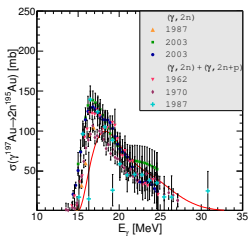
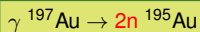
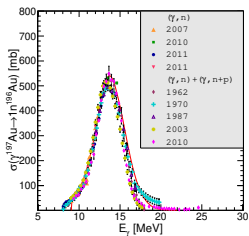
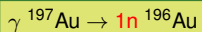
- ❷ quasi-deuteron contribution
 $E_{\gamma} = (40 - 100)$ MeV



- ❸ nucleon resonances
 $E_{\gamma} = (0.1 - 1)$ GeV

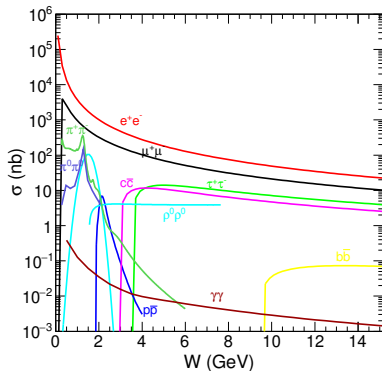
- ❹ break-up of nucleons
 $E_{\gamma} > 1 - 8$ GeV





CONCLUSION

- EPA in the impact parameter space
- Fourier transform of the charge distribution
- Multidimensional integrals \rightarrow differential cross section
- Description of experimental data for UPC
- Predictions include the experimental acceptance
- Electromagnetic excitation - ZDC
- Collaboration - theoreticians and experimenters
- Future:
 - more forward/backward region
 - lower p_t



Thank you