



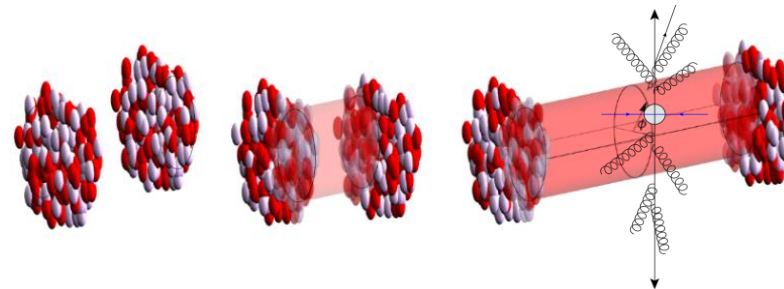
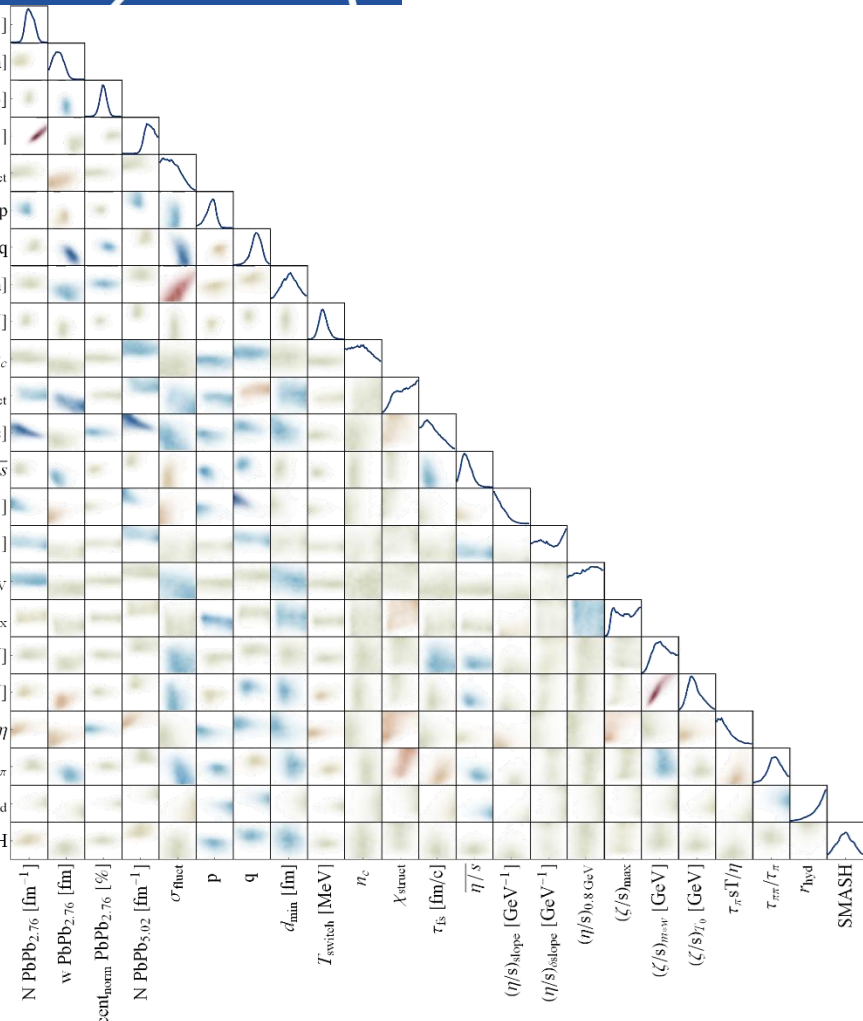
Universiteit
Utrecht



Macroscopic QGP Properties

Towards precision physics with global analyses

[2112.13771](#), [2206.13522](#) (PRL) and [2305.00015](#) with Govert Nijs and Giuliano Giacalone



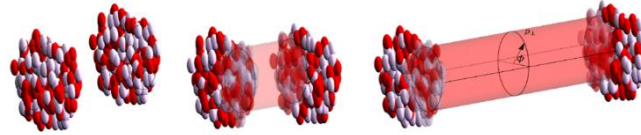
Wilke van der Schee
CMS Week, ECT* Trento
29 May 2023

Outline

Three parts:

1. Neutron skin, also as an illustration of Bayesian analyses
2. Ultracentral collisions: specific and interesting physics
3. The shape of nuclei and preparing for oxygen collisions

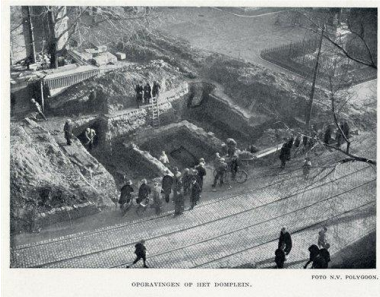
Standard model of heavy ion collisions



(# parameters)

Trajectum

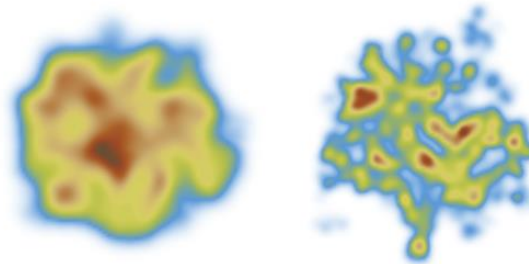
- New public heavy ion code
- Originally Utrecht (now MIT/CERN)
- Fast
- Precise (all cuts equal to experiment)
- Scalable



Roman excavations in **Utrecht** in 1929

Initial stage (13)

Subnucleonic structure? (8)



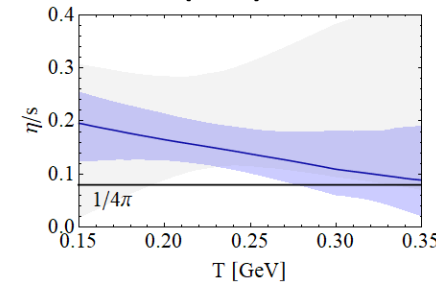
Non-thermal flow? (2)
with hydrodynamised initial stage

Fluctuations? (1)

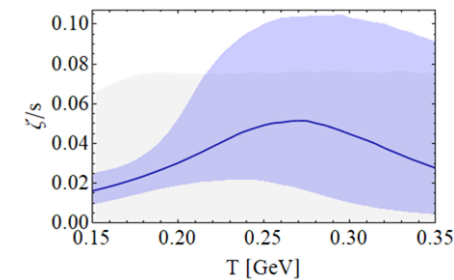
Shape (2)

Viscous hydrodynamics (10)

Shear viscosity (4)



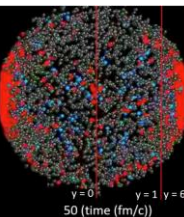
Bulk viscosity (3)



Second order transports: 2

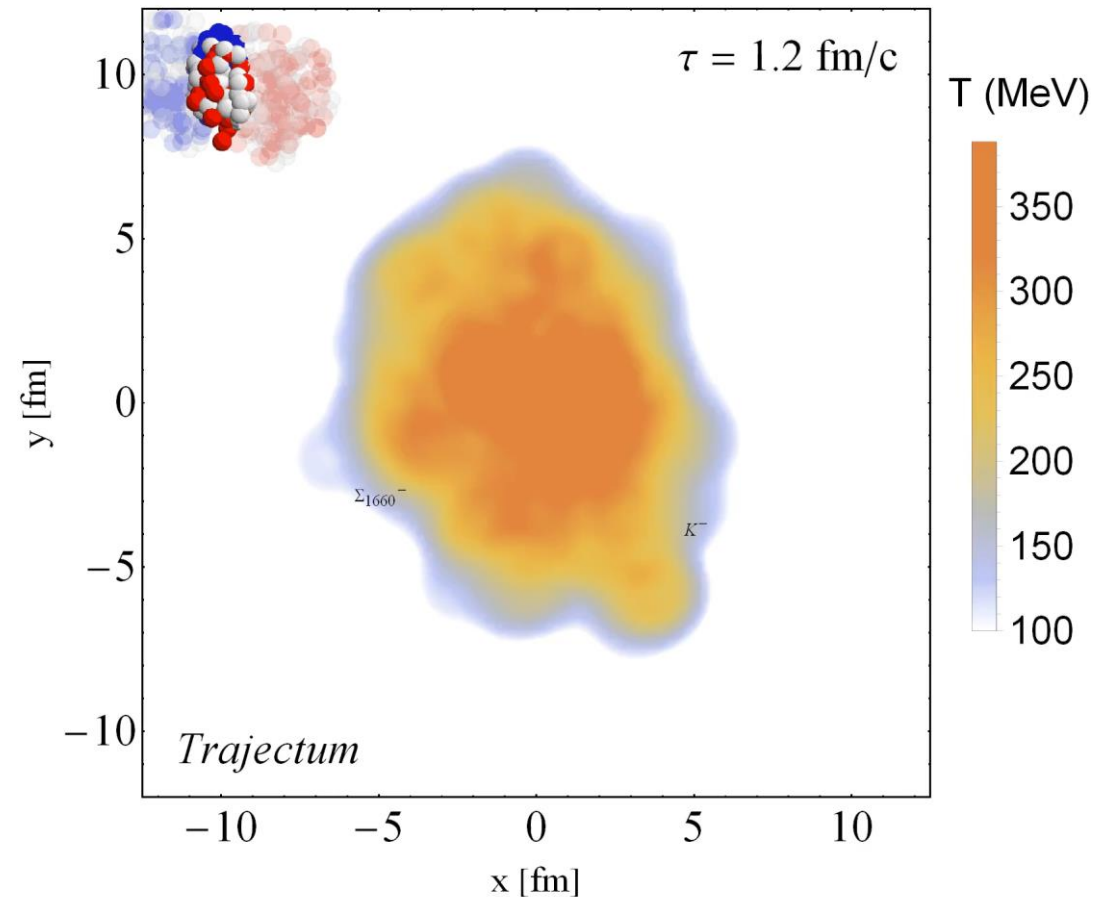
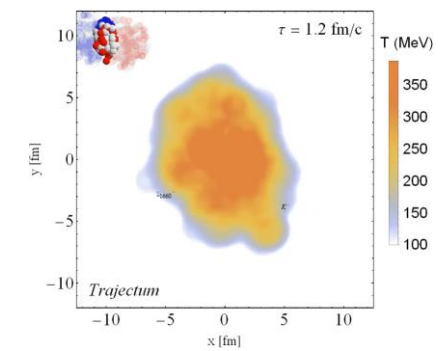
EOS: 1

Cascade of hadrons (1)



Trajectum

1. Quite straightforward to use (see param file, right)
2. Includes analyse routine
 - Parallelised: can analyse unlimited number of events



```
general{
  output=out
  format=smash
  f0500=false
  numevents=1
  seed=7398984.747399307
  debugoutput=true
  numthreads=2
}
entropyacceptanceprobability{
  0:0.0
  24:0.0
  24.5:0.05
  25.5:0.05
  26:0.0
  100:0.0
}
trentosubstructurePbPb{
  dmin=0.63933
  w=0.701919
  sigmann=70.0
  sigmafluct=0.73579
  p=0.14388
  q=1.0
  Eref=0.2
  norm=23.507
  freestreamingreferencetime=1.1708
  freestreamingvelocity=0.62672
  weaktostrong=0.0
  nref=20
  alpha=0
  nc=3.2747
  voverw=0.4892041602706295
}
secondorderhydro{
  numlatticesites=166.0
  latticesize=33.2
}
musclsolverktnmodfastmidpoint{
  cflconstant=0.08
}
LatticeE0StempdepDuke{
  shearhg=0.0895066
  shearmin=0.0895066
  shearslope=0.43252
  shearcrv=0.231195
  shearrelaxationtime=6.318855
  bulkmax=0.0030138
  bulkT0=0.21471
  bulkwidth=0.10906
  bulkrelaxationtime=0.0687
  deltapiiovertaupi=1.3333333333333333
  phi7overpressure=0.128571
  taupiovertaupi=1.61033
  lambdapiiovertaupi=1.2
  deltaPiiovertaupi=0.6666666666666666
  lambdaPiiovertaupi=1.6
  phi1overpressure=0
  phi3overpressure=0
  phi6overpressure=0
}
cooperfryehadronizer{
  freezeouttemp=153.456
  rapidityrange=0.1
}
```


Neutron skin

The background features a dark blue space with a faint, glowing neutron star on the left, emitting light rays. On the right, there is a detailed 3D model of a nucleus, represented as a cluster of red and blue spheres.

WITH A SHORT INTRO ON BAYESIAN ANALYSIS

Performing a global analysis

Model depends on parameters non-linearly

- Run model on 1200 'design' points
- Use an emulator for any point in parameter space (**GP**)

Markov Chain Monte Carlo

- 653 data points
- Obtain posterior probability density of parameters

Compare posterior with data

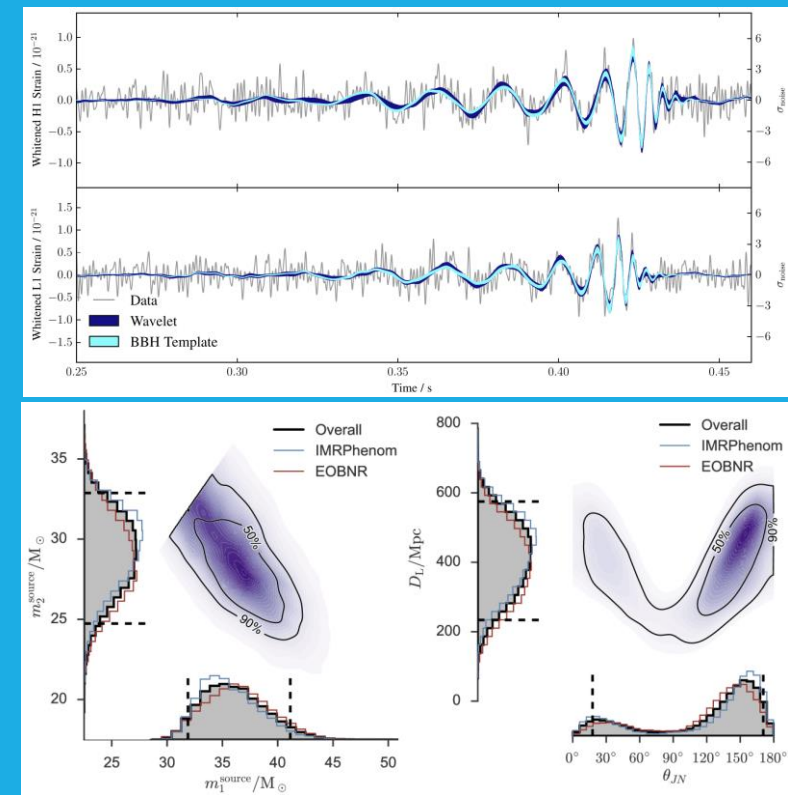
- Can include high statistics run

Bayes theorem:

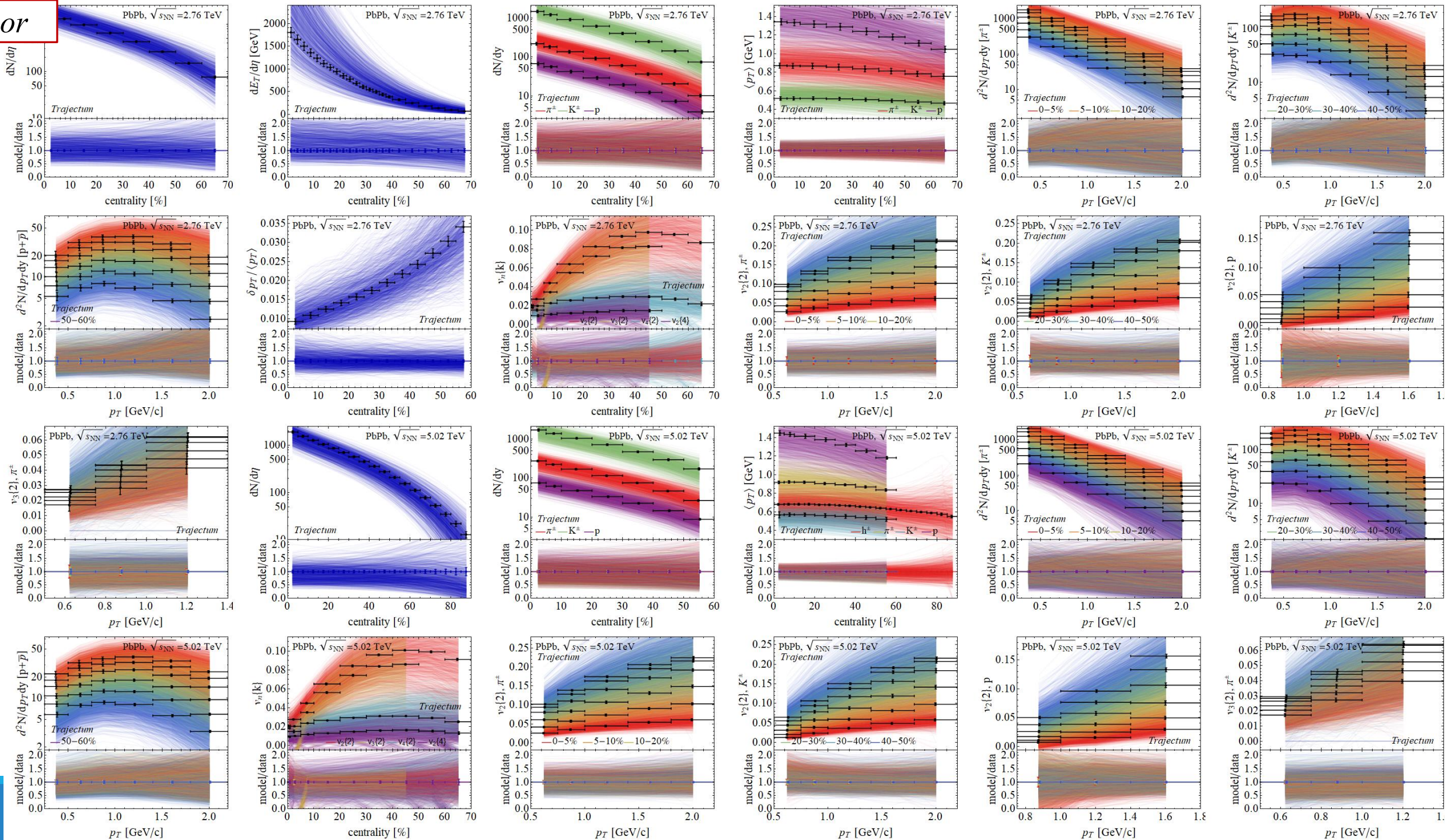
$$\mathcal{P}(\mathbf{x}|\mathbf{y}_{\text{exp}}) = \frac{e^{-\Delta^2/2}}{\sqrt{(2\pi)^n \det(\Sigma(\mathbf{x}))}} \mathcal{P}(\mathbf{x})$$

$$\text{with } \Delta^2 = (\mathbf{y}(\mathbf{x}) - \mathbf{y}_{\text{exp}}) \cdot \Sigma(\mathbf{x})^{-1} \cdot (\mathbf{y}(\mathbf{x}) - \mathbf{y}_{\text{exp}})$$

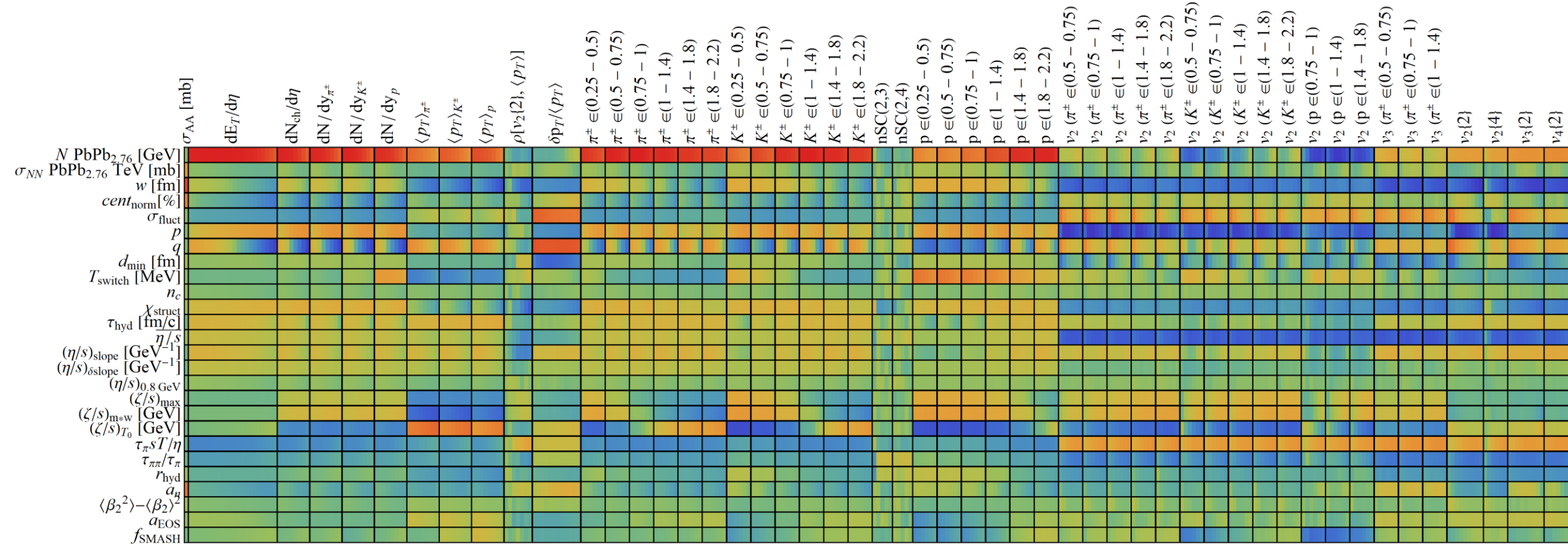
Same technique: gravitational waves

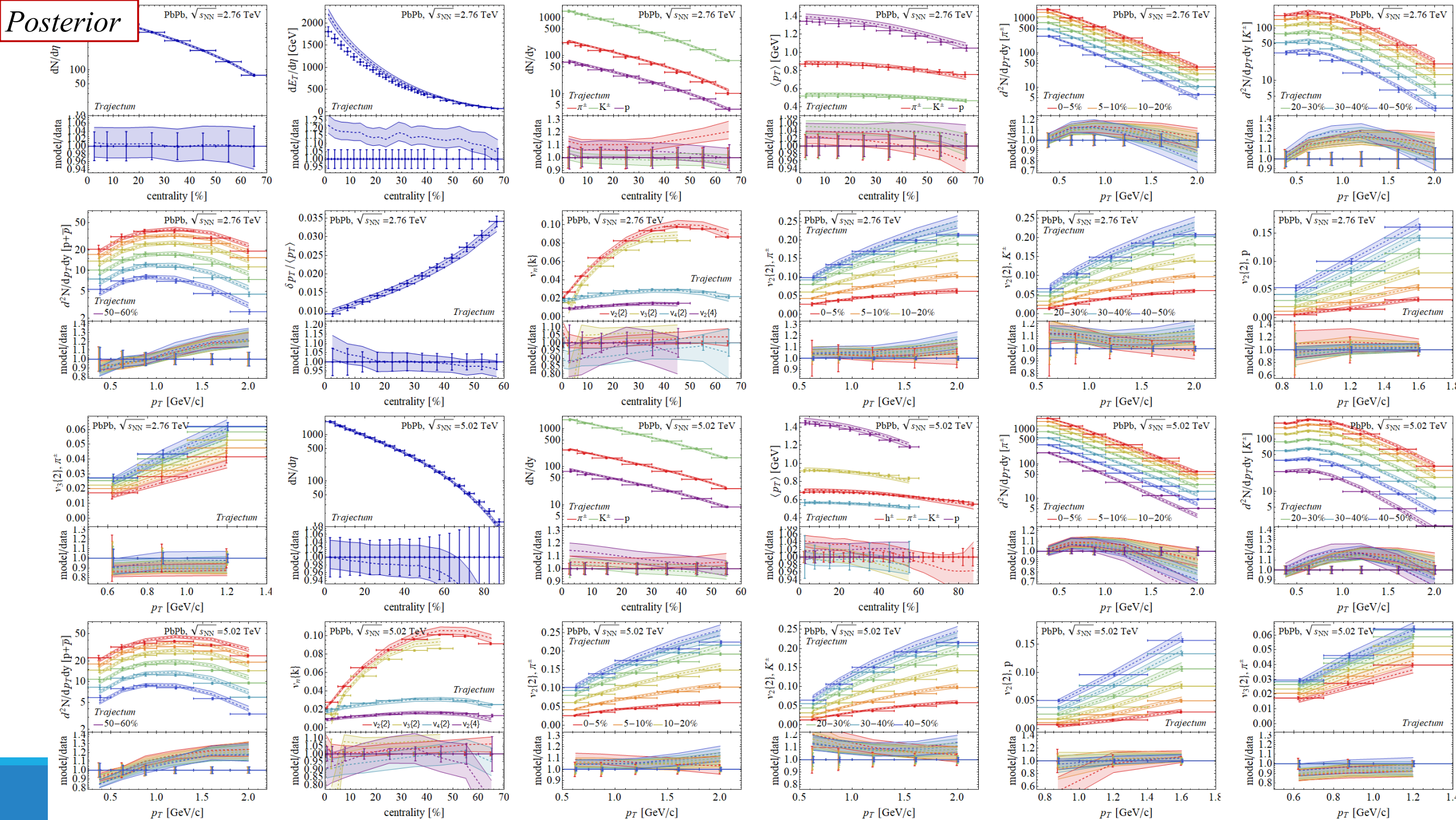


Prior



Design parameter-observable correlations:

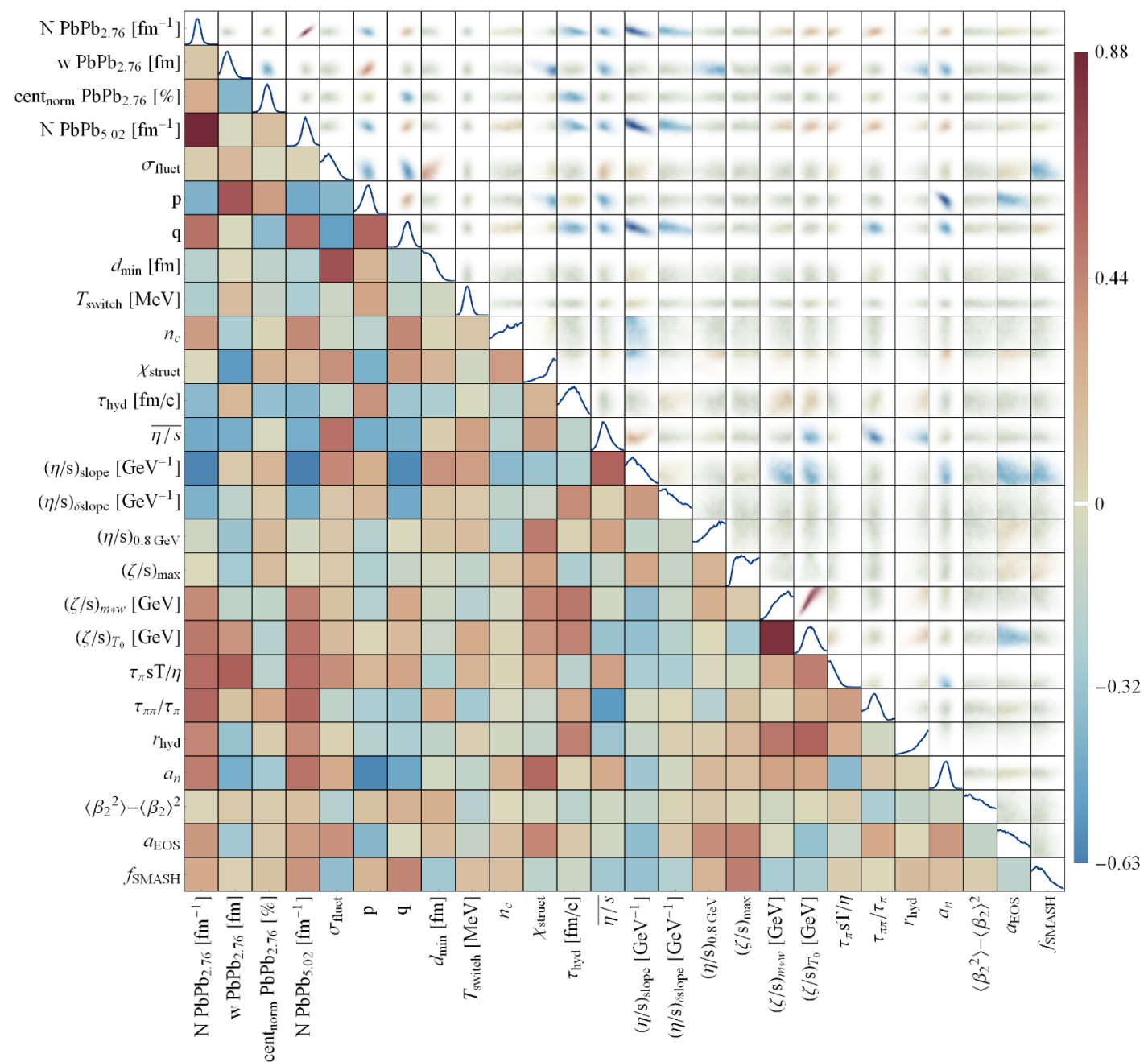




Full posterior distributions

1. Some parameters better constrained than others

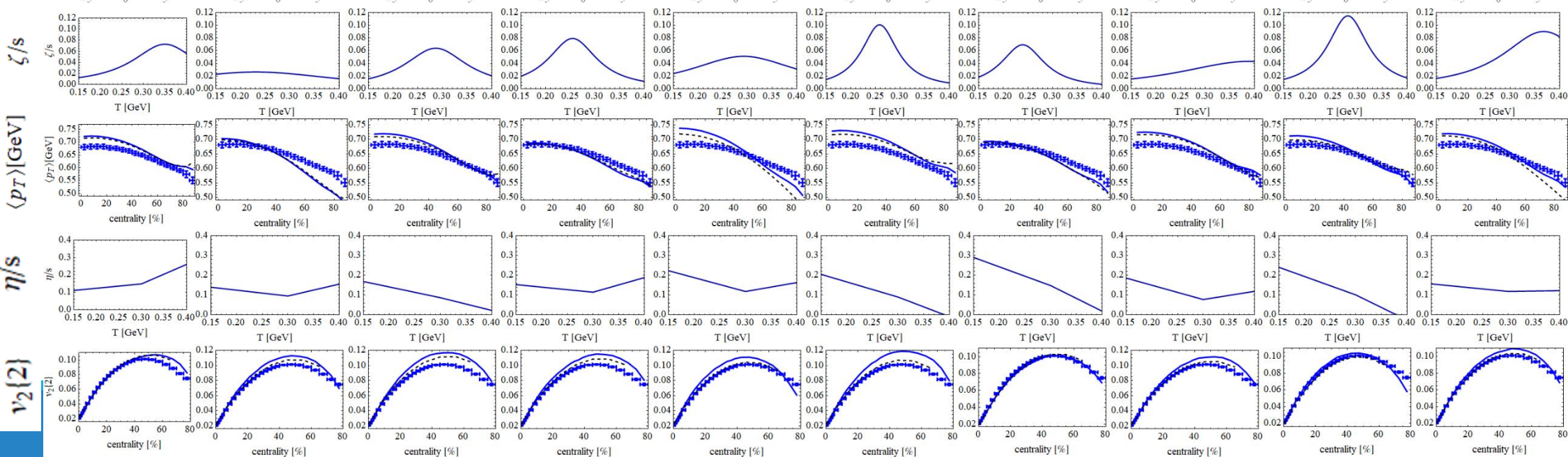
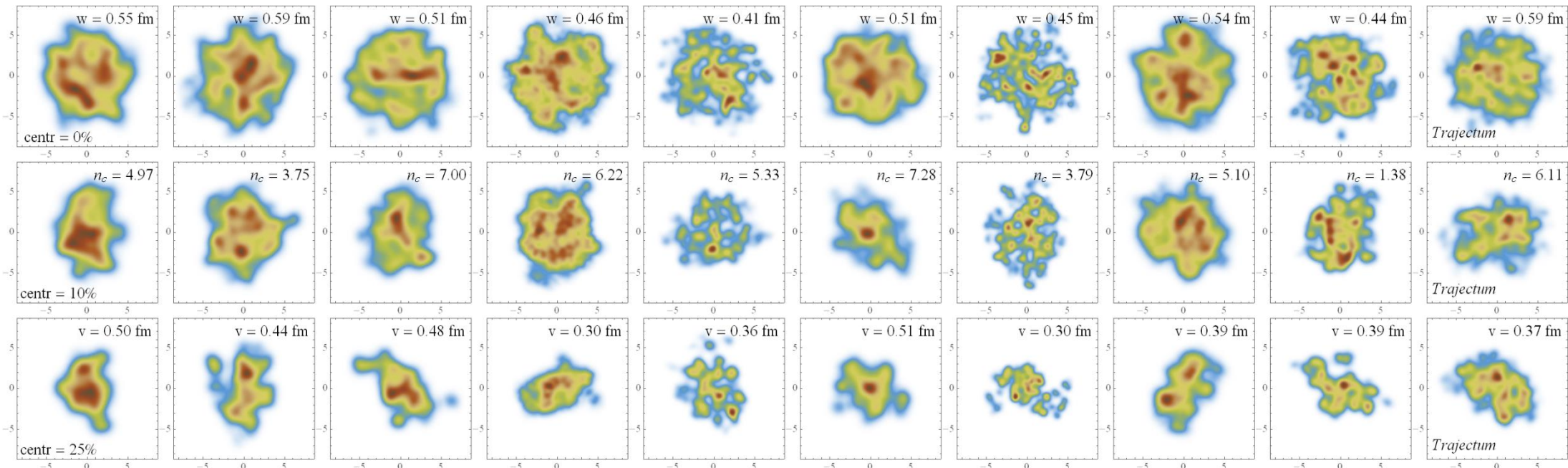
- Correlations add important information, e.g. width constrained much more accurately if q parameter is known



Ten different probable parameter settings \rightarrow

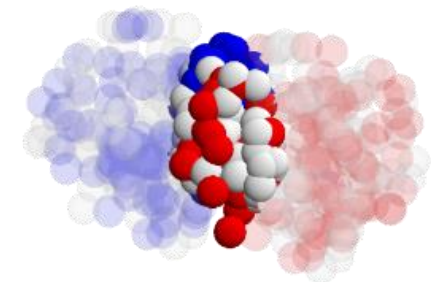
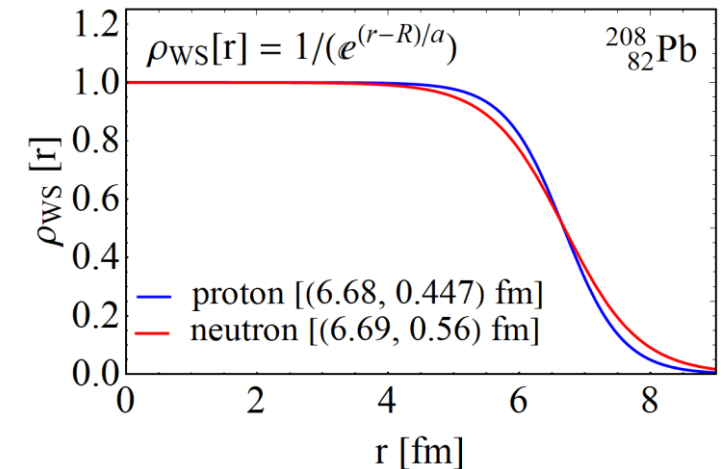
Energy + viscosities + experiment

Centrality \rightarrow



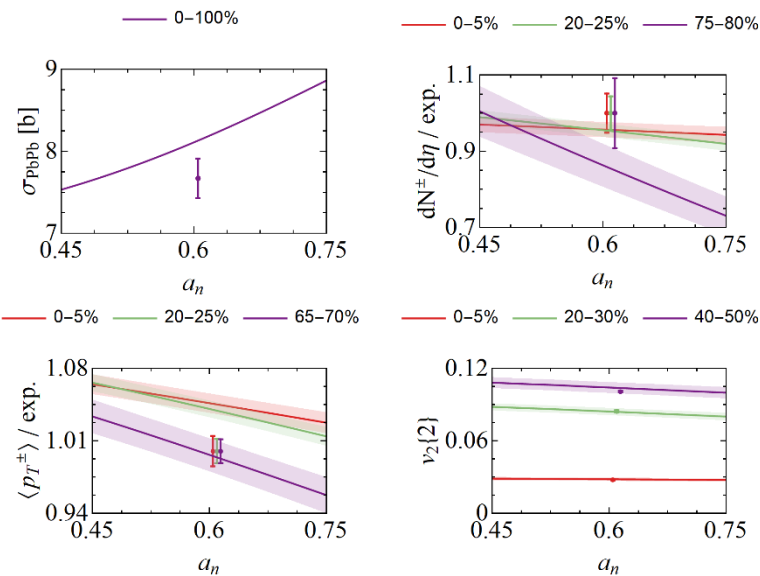
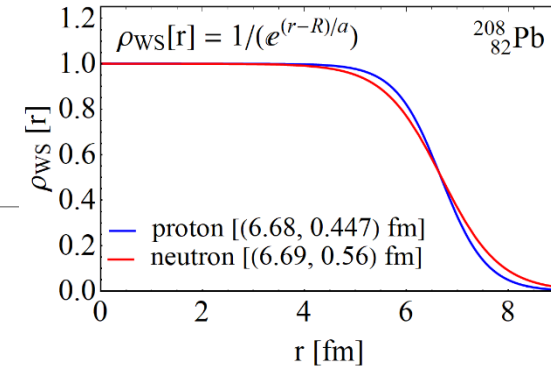
The neutron skin

1. Nucleus charge profile can be measured very accurately
 - Much more uncertainty in the profile of the neutrons
 - Relevant to understand cold QCD: EOS for neutron stars
2. Can we make progress using heavy ion collisions?
 - Isospin symmetry makes distinction neutron/proton difficult
 - Leverage accurate proton knowledge and obtain profile of nucleus?
3. How to obtain the profile of a nucleus?
 - Wood-Saxon + MC-Glauber + (model like Trento) → dynamics
 - Currently state-of-the-art ...
4. Profile influences many observables
 - Interplay with bulk viscosity, Trento model etc
 - Likely need a full global analysis

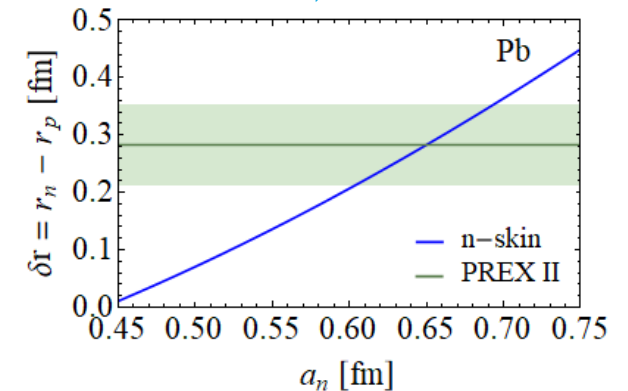


The neutron skin - emulator

- Plan is to vary a for neutrons and see if HIC can constrain it
 - a determines the neutron radius (approx. linear for RMS radius)
- First step: what does the emulator say?
 - Using a precise global analysis (26 parameters, 3000 design points)



- Main change: cross section
 - Measures 'size' of nucleus
- Both multiplicity and mean p_T change
 - Mainly for peripheral ('skin effect')
- Small changes for other observables

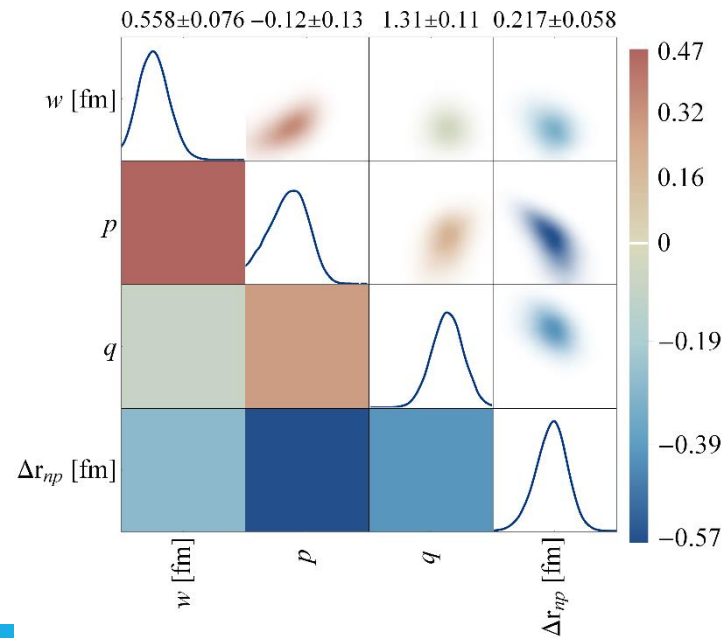
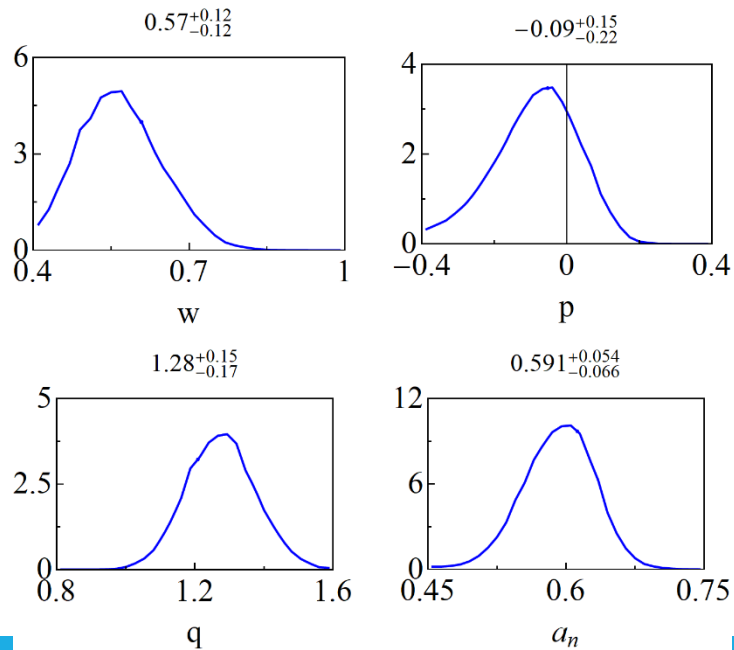
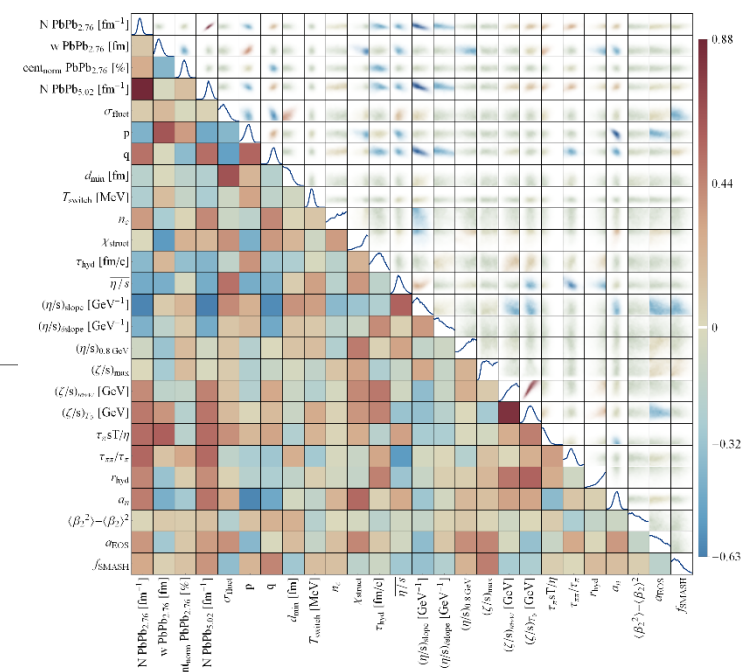


$$\mathcal{E} \propto \left(\frac{1}{2} T_A^p + \frac{1}{2} T_B^p \right)^{q/p} = (T_A T_B)^{q/2} \Big|_{p=0}$$

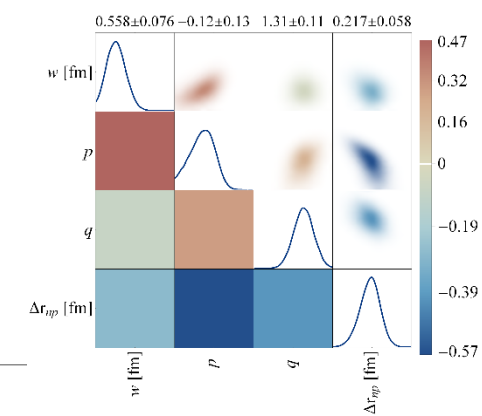
The neutron skin - posterior

1. Three parameters are most sensitive to the neutron skin:

- The nucleon width and the Trento parameters p and q
- Small correlation with width (cross section is highly sensitive to w)
- Very strong anticorrelation with p ; centrality dependence is crucial

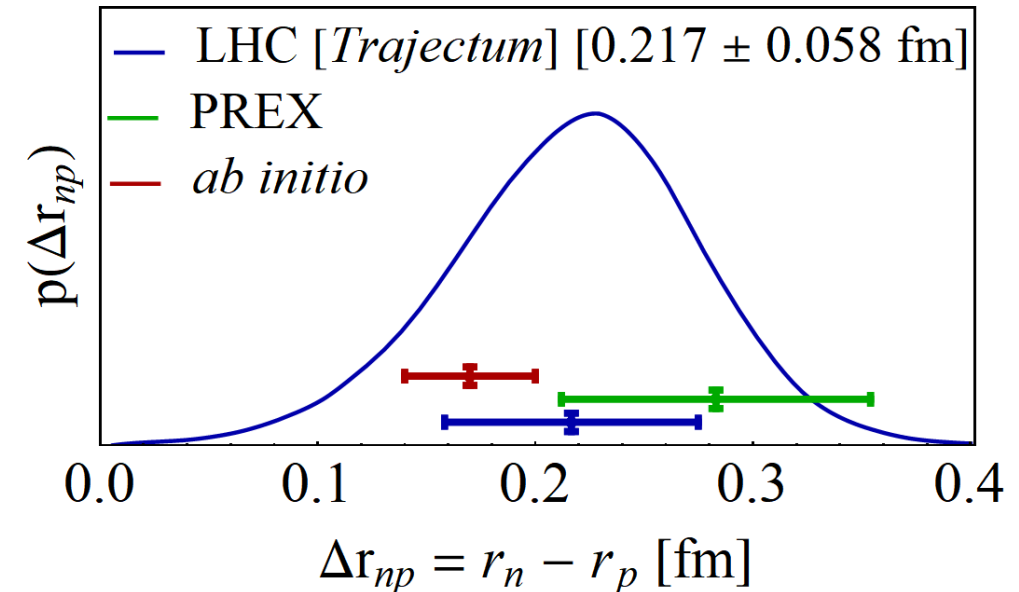


The neutron skin – final result

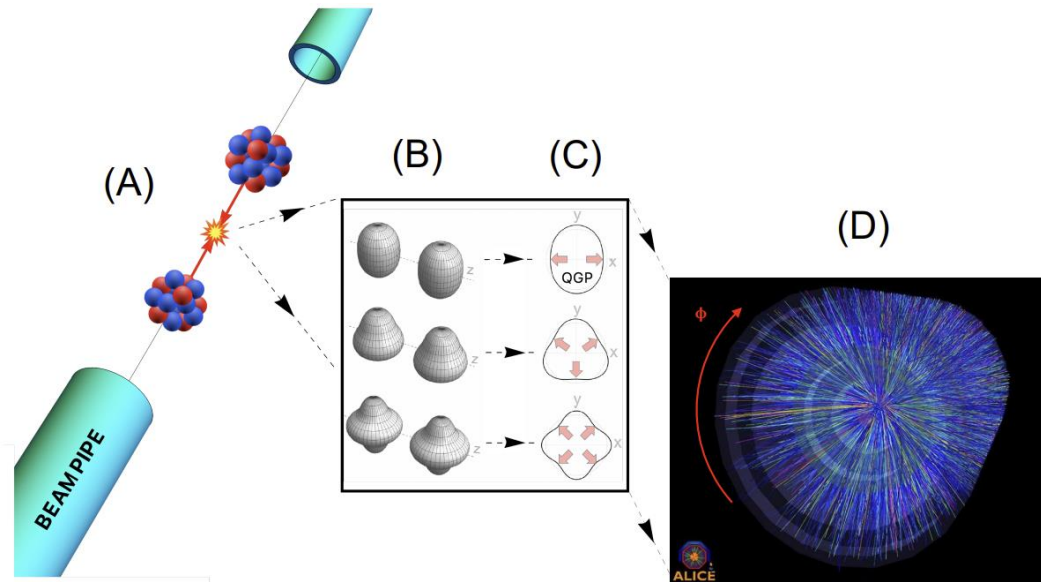


1. Transform to neutron radius minus proton radius
2. Final result consistent but smaller than PREX II
3. Uncertainty is about 20% smaller than PREX II
4. Cross section is crucially important, but also centrality dependence
 - Important to vary Trento parameters in particular

Not competitive with weighted averages (from 14 different methods), but adds unique experimental determination of neutron skin



The shape of nuclei



Isobar collisions at STAR – Flow and mean p_T

$v_2\{2\}$

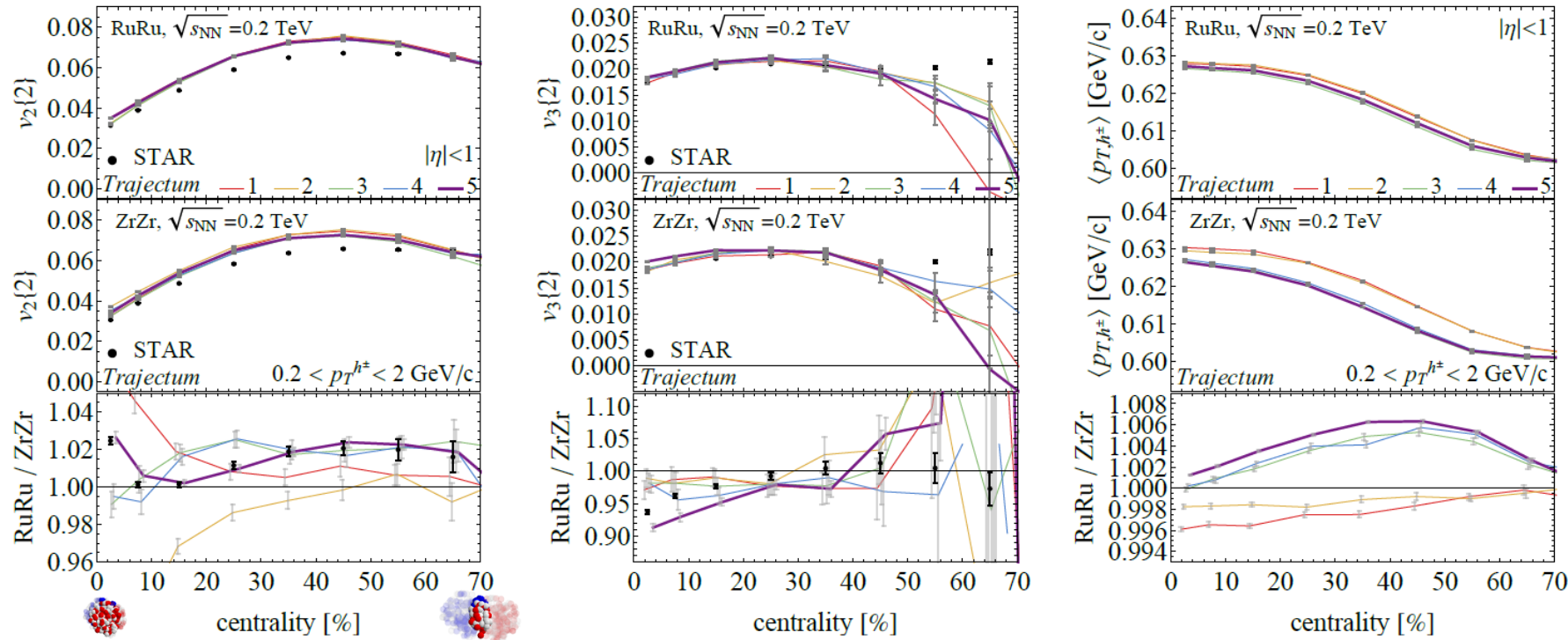
$v_3\{2\}$

$\langle p_{T,h^\pm} \rangle$

RuRu

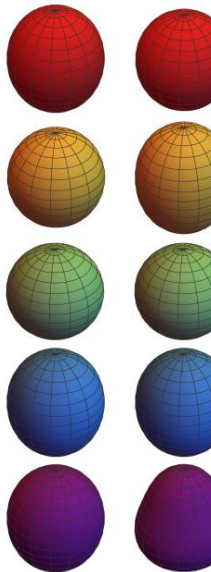
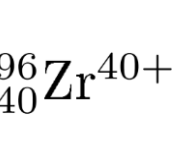
ZrZr

Ratio



Original motivation was to study Chiral Magnetic Effect (CME, not found...)

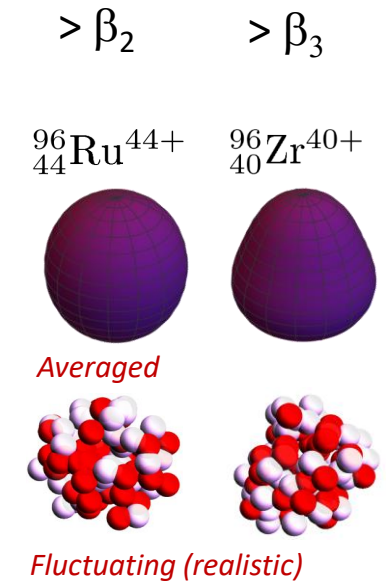
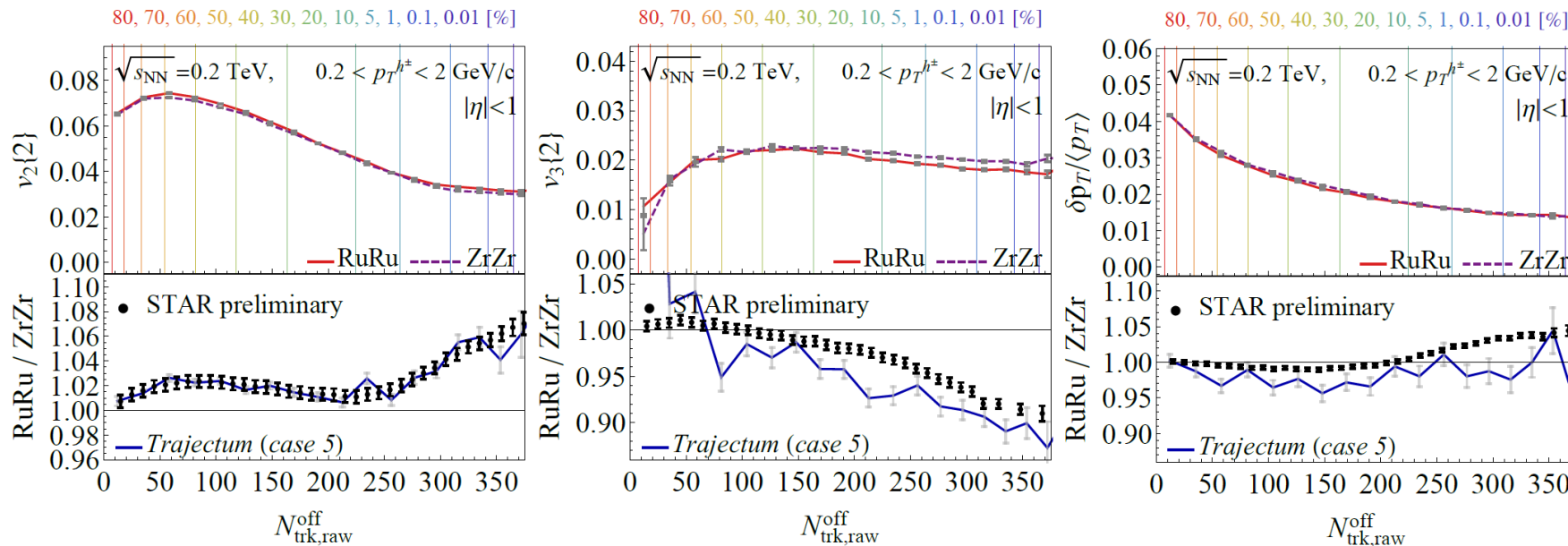
- Turns out that the background is significant, can be studied with **hydro** only
- Note that *Trajectum* is not fitted to RHIC energies, no absolute agreement
- Requires many events, percent level accuracy

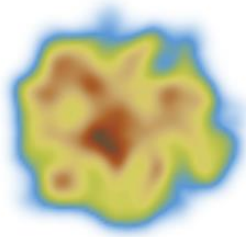


Extremely ultracentral collisions

Going to 0.01% centrality (we sample from 250M Trento events)

- Excellent match v2, v3 and pt fluct somewhat overpredicted
- Extremely ultracentral is ideal regime to probe nuclear structure (also: better hydro!)



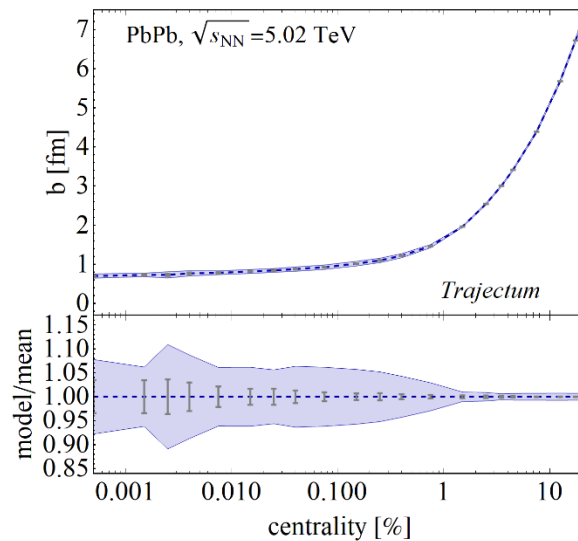


Extremely ultracentral collisions at the LHC

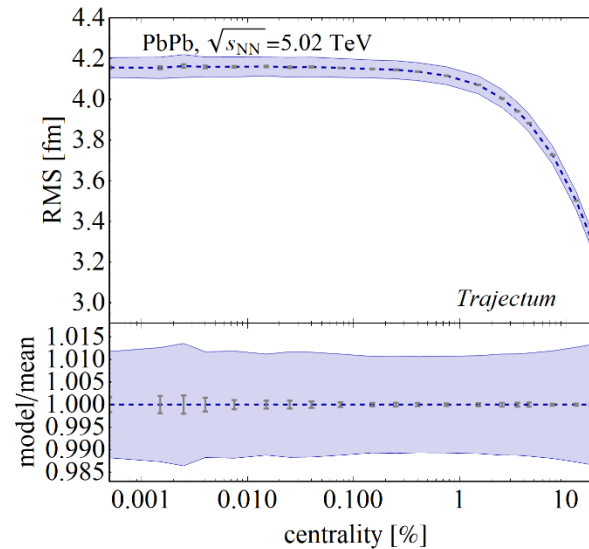
Unique physics

- Collisions at almost zero/constant impact parameter
- Constant volume, no impact parameter fluctuations, but temperature fluctuations

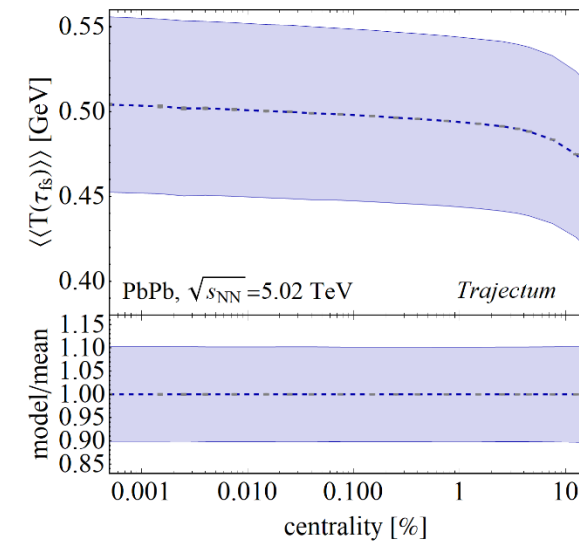
Impact parameter

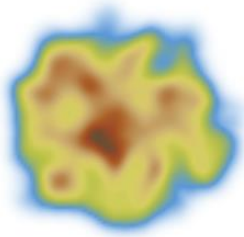


Size



Temperature at hydro start



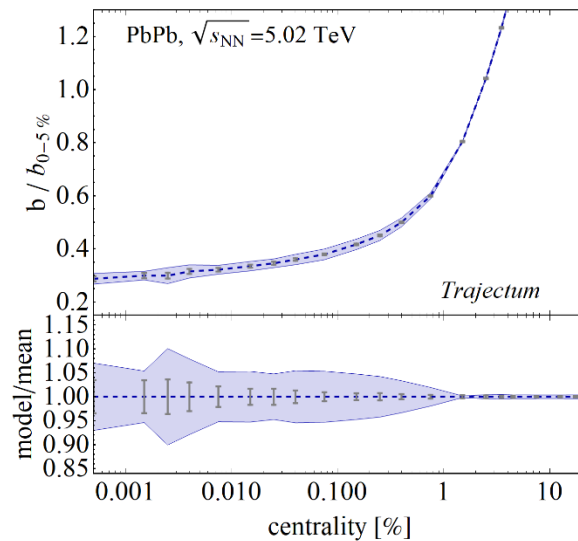


Extremely ultracentral collisions at the LHC

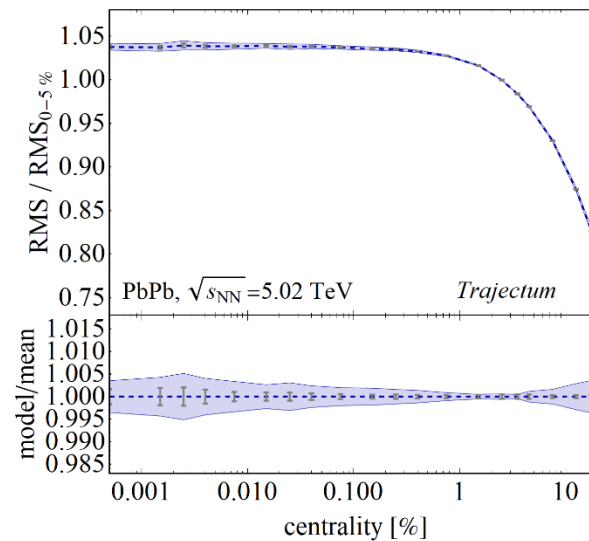
Significant reduction in uncertainty when taking ratio with 0-5% centrality class

- Stronger for temperature (depends on uncertain hydro starting time)
- Somewhat curious impact parameter uncertainty that is not reduced

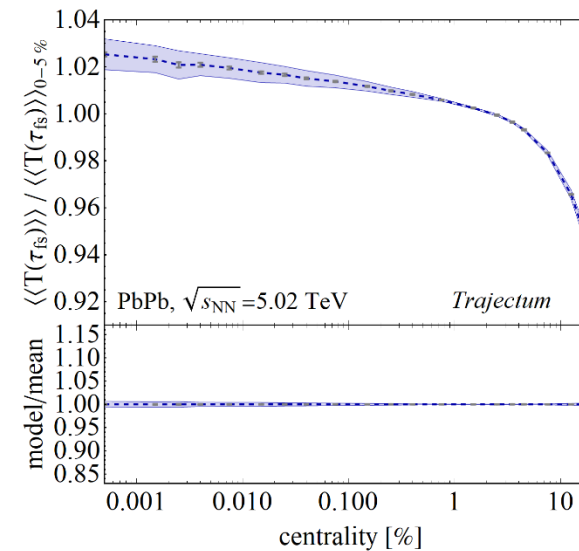
Impact parameter



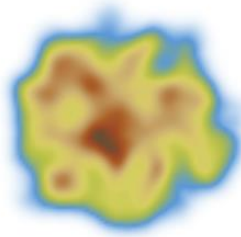
Size



Temperature at hydro start

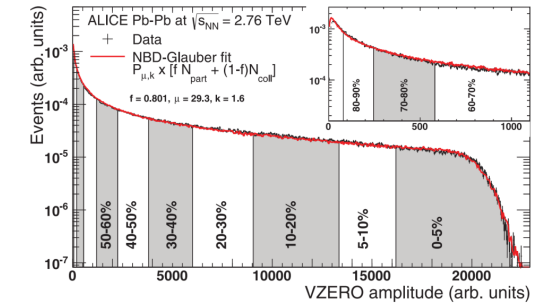


Extremely ultracentral collisions at the LHC

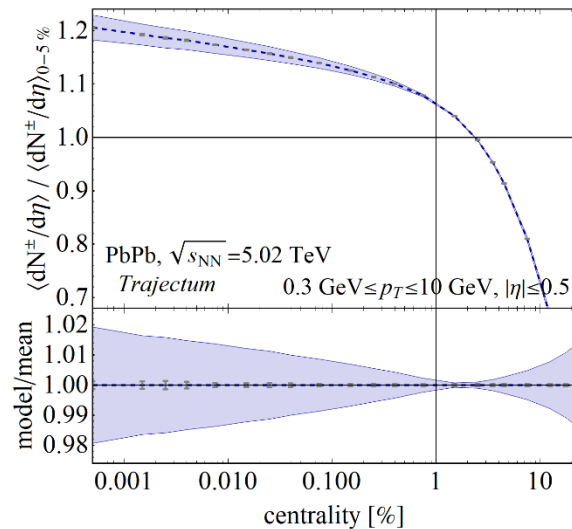


Characteristic rise in mean transverse momentum

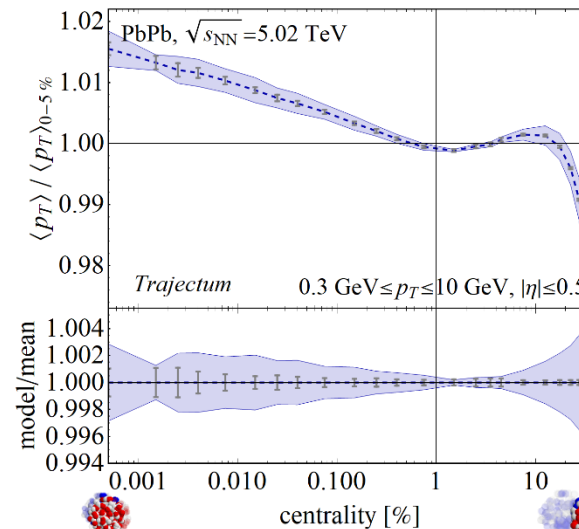
- Collective effect: thermalization, relation with temperature and entropy
- Somewhat curious dip around 2%, not understood



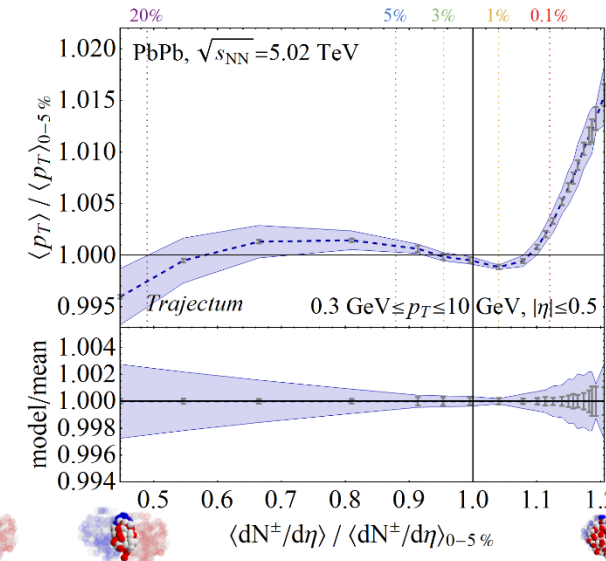
Multiplicity (knee)

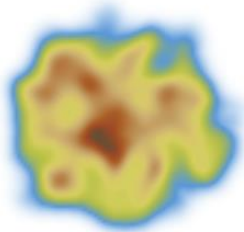


Transverse momentum



Transverse momentum vs N_{ch}



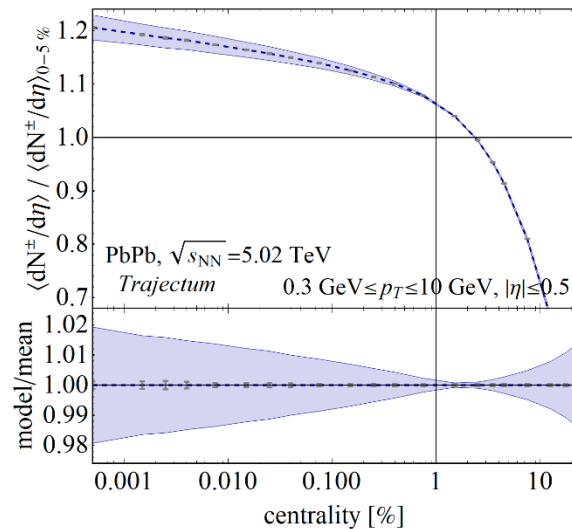


Extremely ultracentral collisions at the LHC

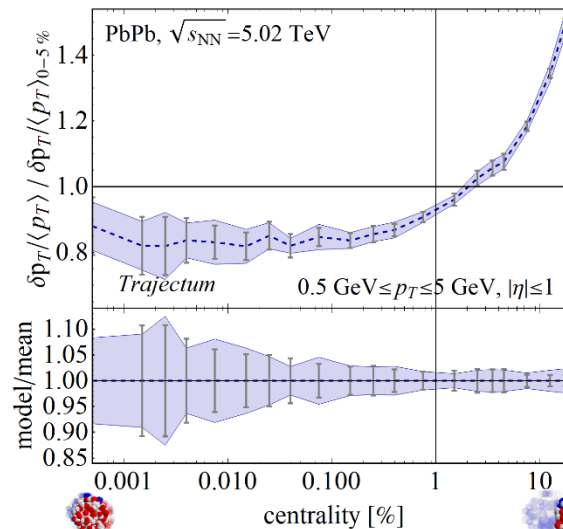
Characteristic decrease in pT fluctuations

- Below ~1% centrality the impact parameter doesn't vary anymore
- Subtle but physically important 'bend'

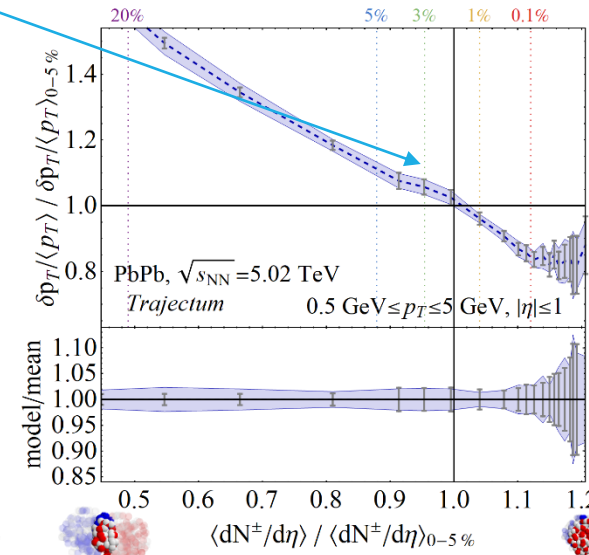
Multiplicity (knee)



pT fluctuations



pT fluctuations vs N_{ch}



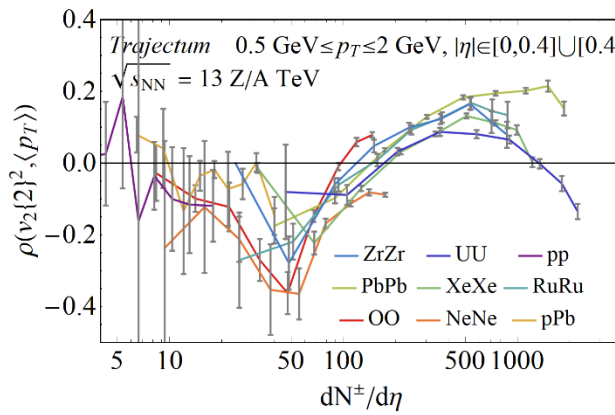
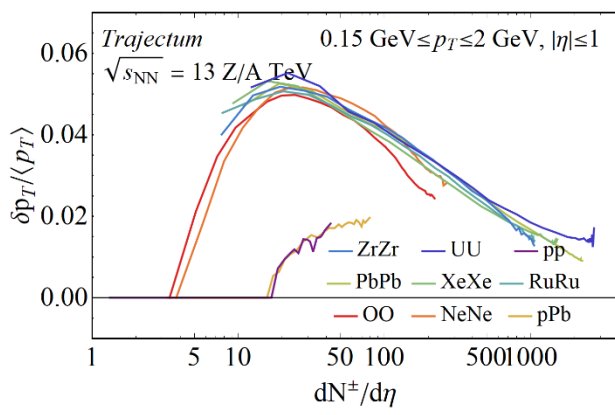
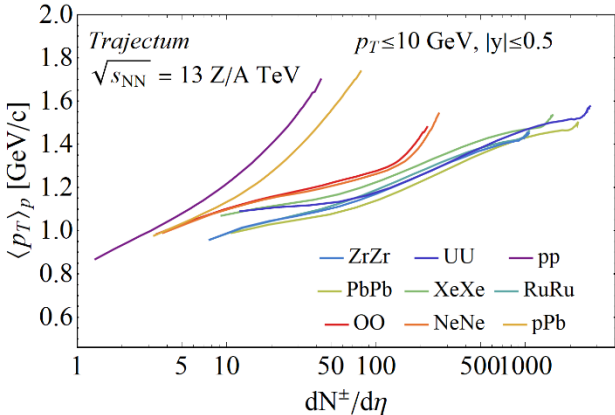
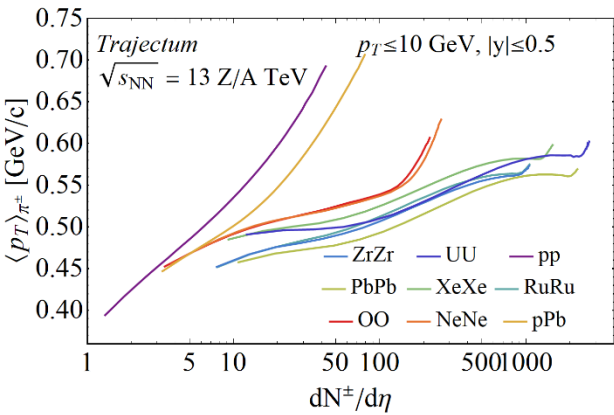
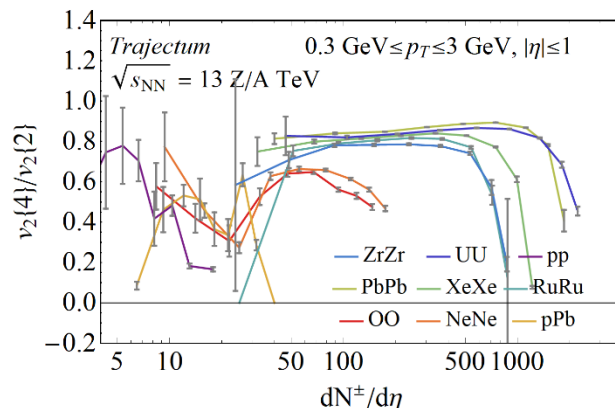
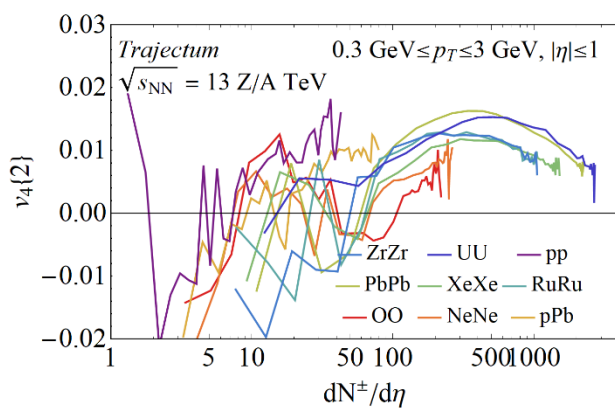
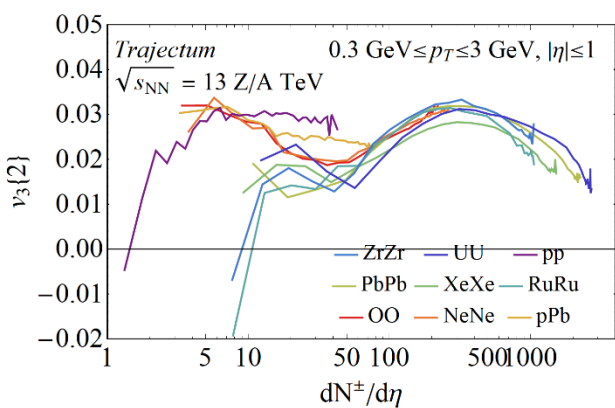
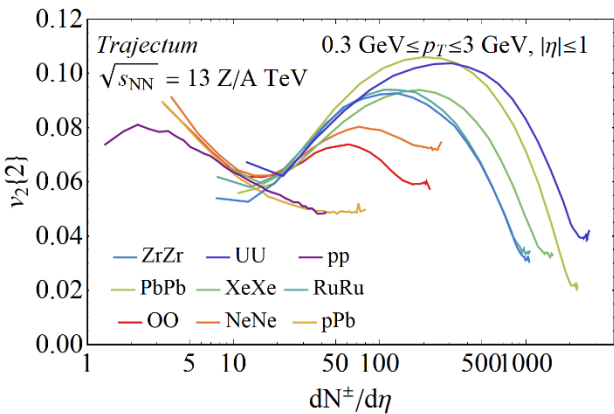
Bonus slide

Special O-O and p-O run

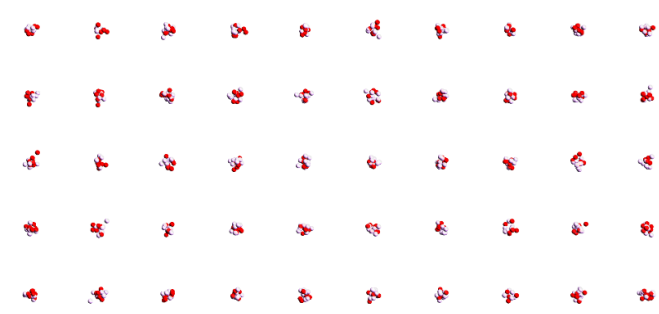
- ❑ Physics motivations: study of emergence of collective effects in small systems; measurements relevant for cosmic rays (extensive air shower modelling), etc.
- ❑ Experiments requested $\sim \text{nb}^{-1}$ for each of OO and pO. ~ 1 week (including commissioning), most likely in 2024
- ❑ No impediment from accelerators but radiological impact of high-intensity oxygen beam requires mitigation measures and additional beams stoppers to be able to access Booster when LEIR operates.
- ❑ Needed resources allocated in this MTP



Several systems with MAP settings (systematic analysis with ratios for some to appear)

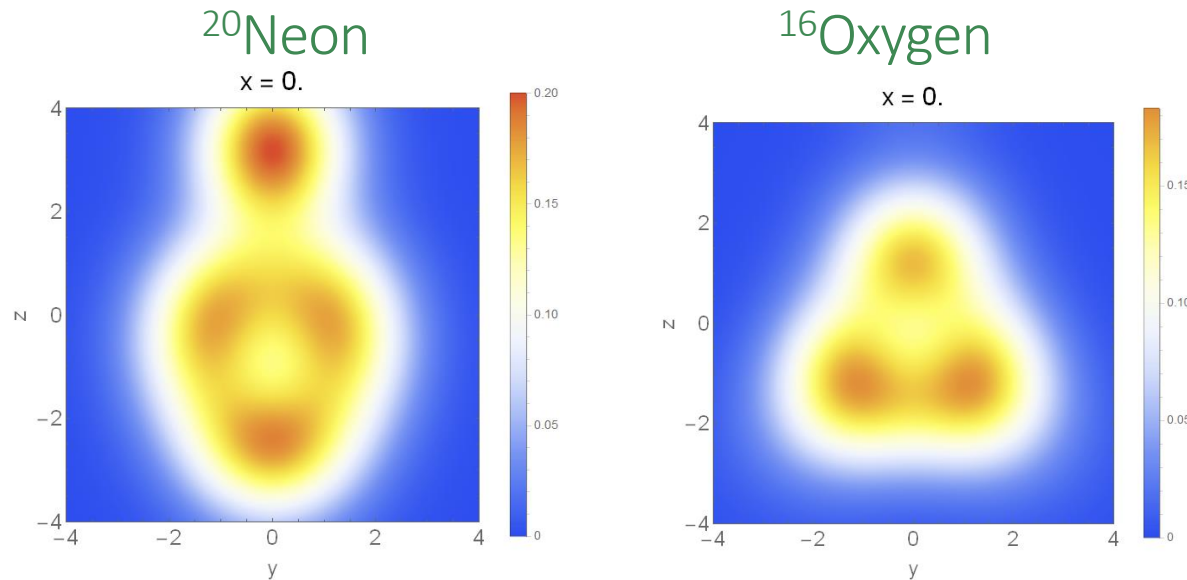


^{16}O and ^{20}Ne nuclear structure

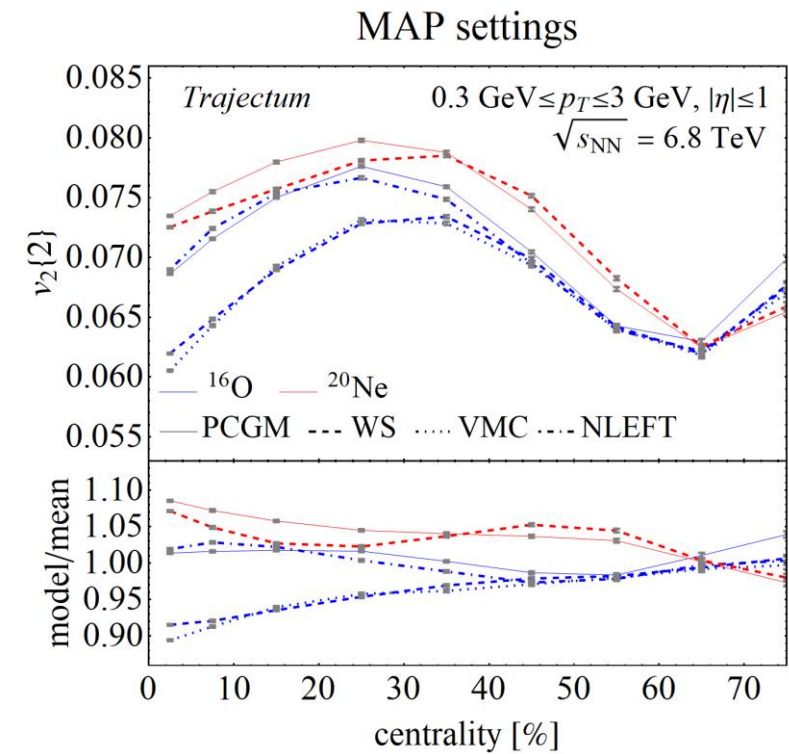


Do we understand and/or need to understand the shape of O and Ne?

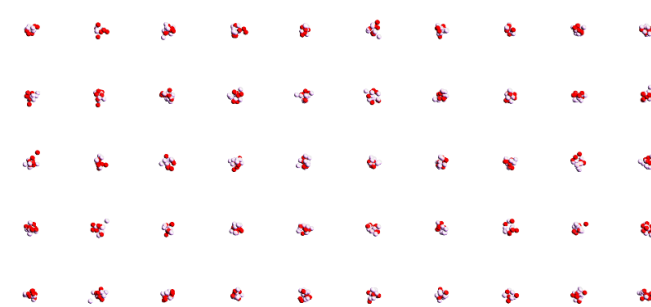
- Naively it seems so: large uncertainty
- Interesting by itself: combination of 4 or 5 alpha particles
- Work in progress: state-of-the-art Projected Generator Coordinate Method (PGCM) results:



Work in process with B. Bally et al

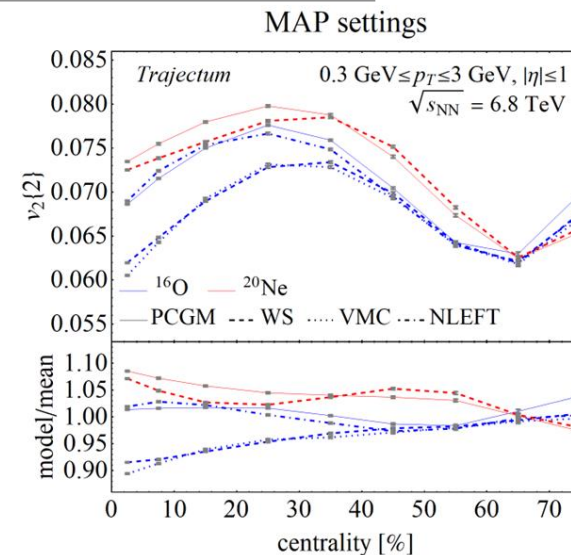
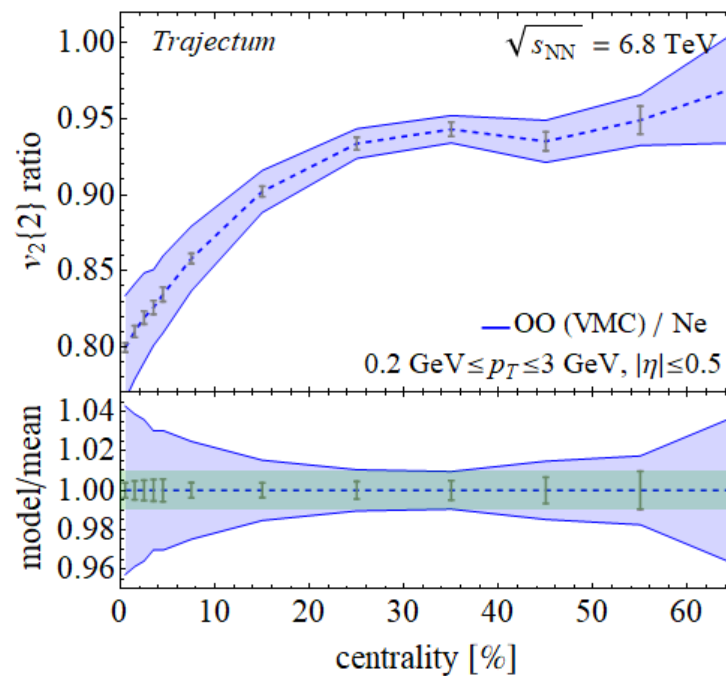
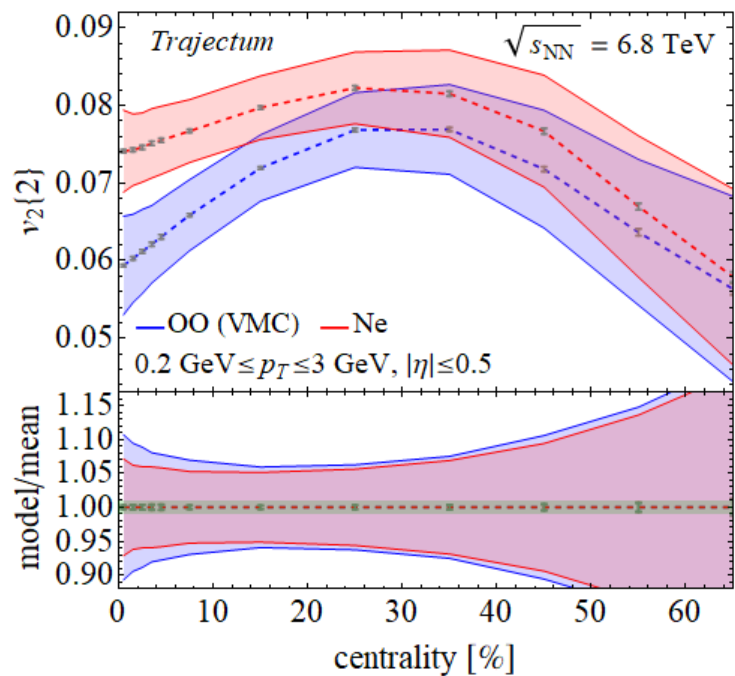


Systematic uncertainty could be a problem



What about the systematics?

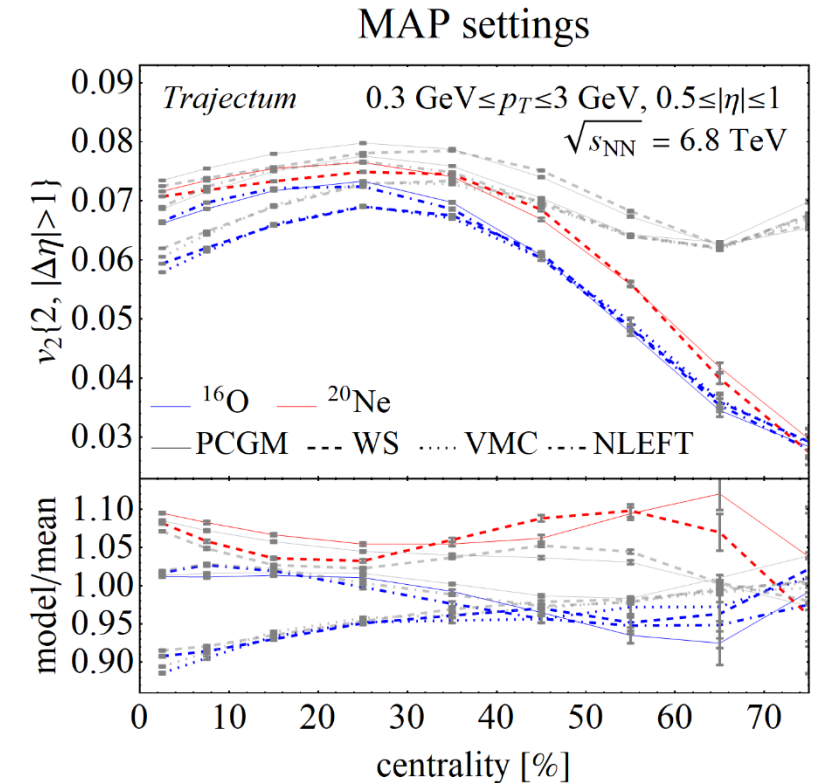
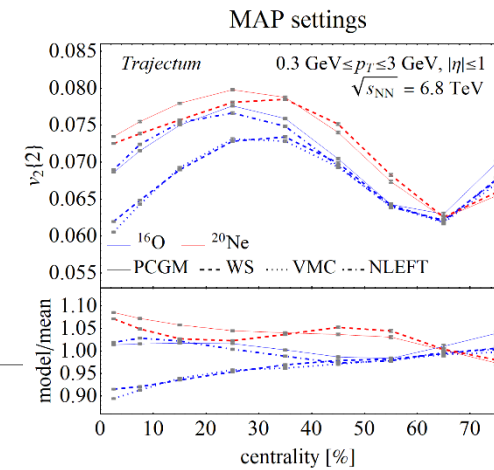
- Barely significant difference between Oxygen and Neon elliptic flow within systematics
- **The ratio**, however, is accurate at percent level (!). Sweet spot at $\sim 25\%$ centrality
- But does it help us? Is the ratio what we need for nuclear structure?



Systematic uncertainty potentially a problem

$v_2\{2\}$ (much) smaller when applying a $\Delta\eta$ cut

- More of a theoretical worry than an experimental one (at least for CMS and ATLAS)
- Also straightforward (but expensive...) to solve theoretically
- Ratios quite robust, at least for central collisions

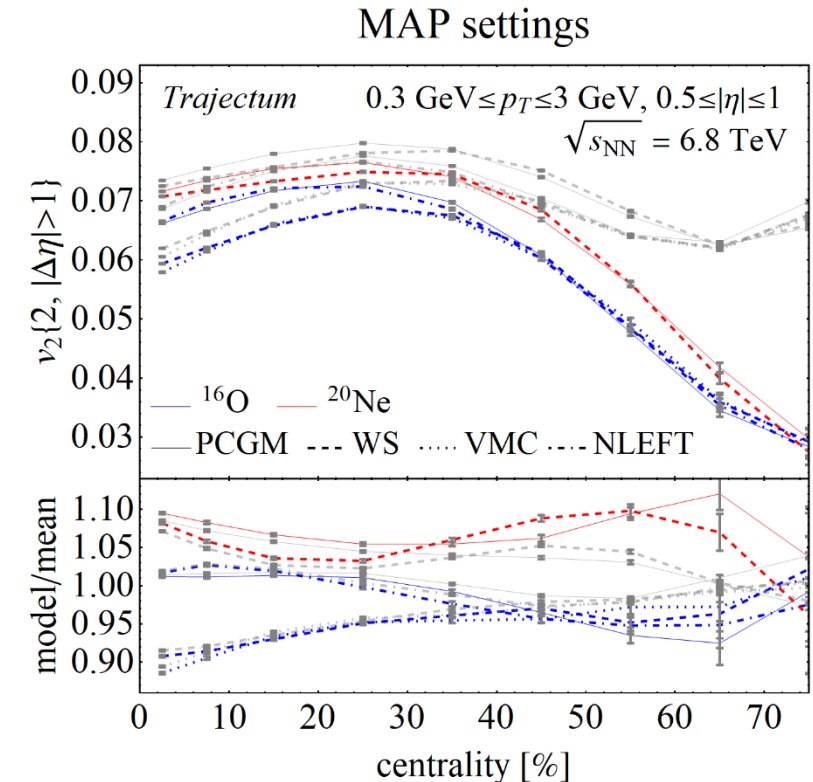
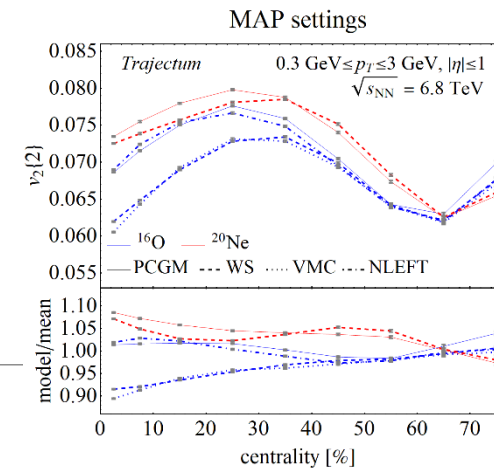


Resonance decays are potentially a problem

$v_2\{2\}$ (much) smaller when applying a $\Delta\eta$ cut

- More of a theoretical worry than an experimental one (at least for CMS and ATLAS)
- Also straightforward (but expensive...) to solve theoretically
- Ratios quite robust, at least for central collisions

Also subtleties how to impose d_{\min} ...

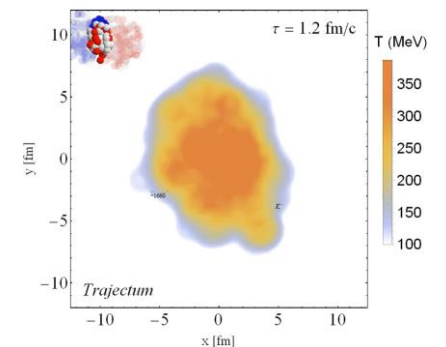
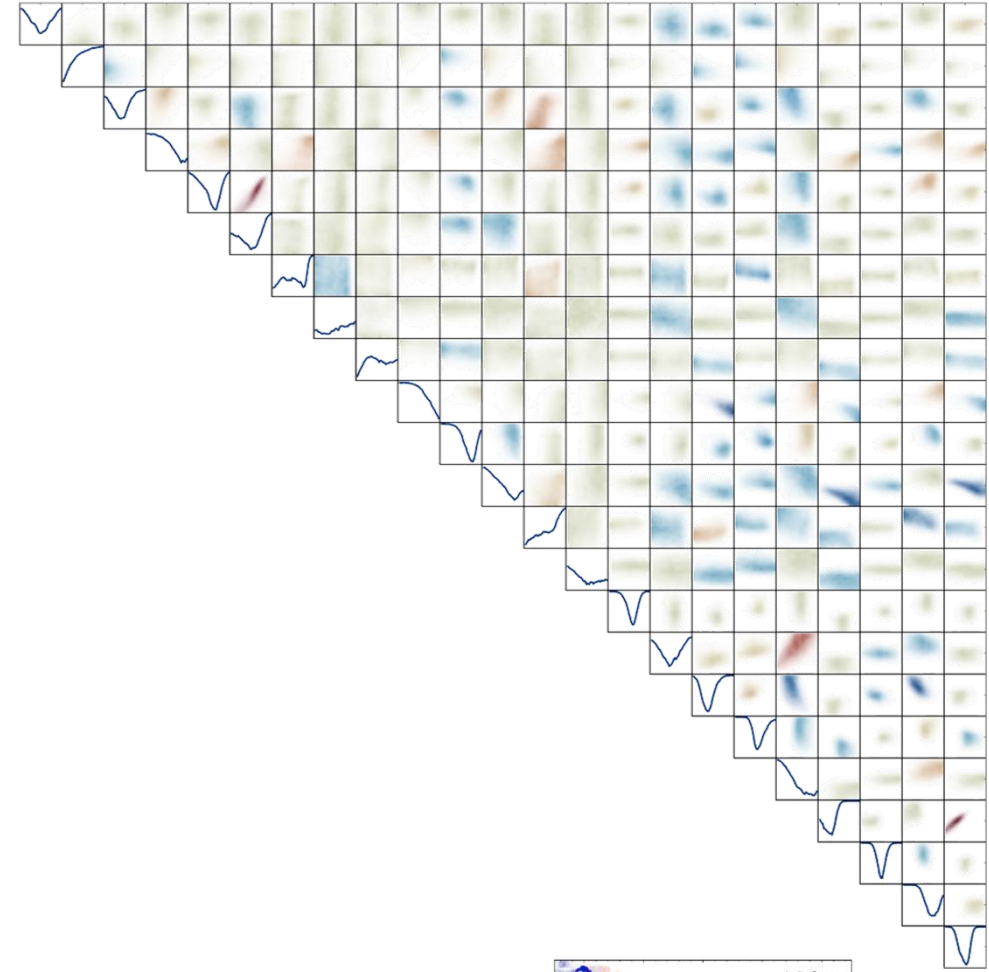


Discussion

Exciting progress using global analyses

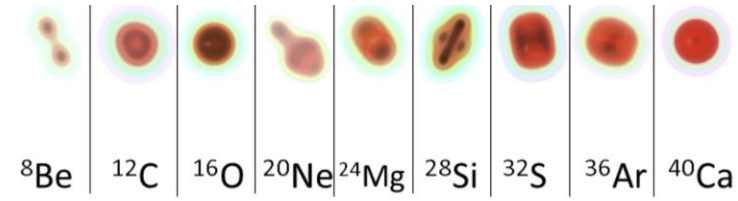
- Heavy ion collisions towards percent level precision
- Still interesting measurement potential: extremely ultracentral
- Nuclear structure becoming relevant and interesting

Oxygen collisions to be performed at the LHC summer 2024!



Back-up

Nuclear structure and heavy ion collisions



Isobar collisions raise several questions:

- Are HIC sensitive to nuclear structure? Yes, but at percent level accuracy
- Are HIC understood at percent level? Historically likely not...

A more systematic approach

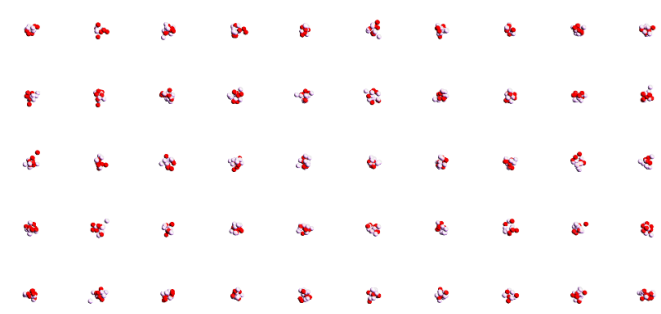
- Vary several approaches to nuclear structure
- Vary parameter settings within current posterior distribution
- **Do we need an (isobar) ratio to make progress?**

Oxygen (and Neon?) at CERN

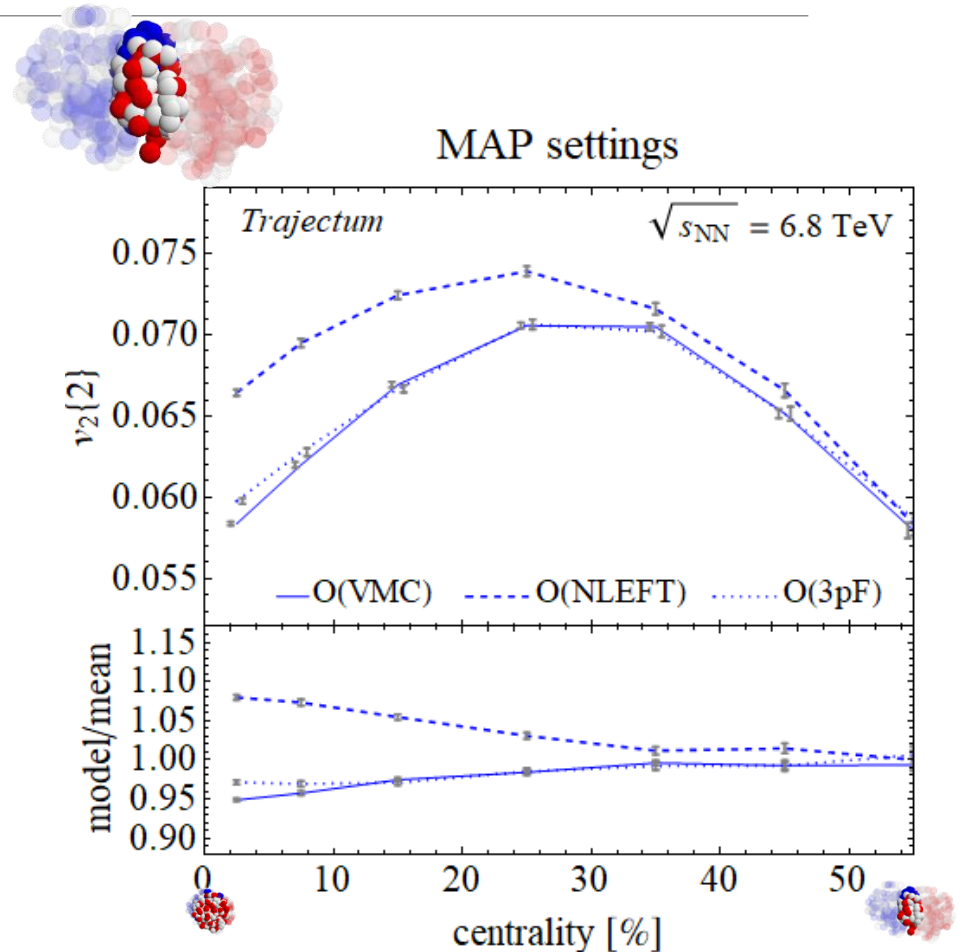
- Independently interesting: the smallest droplet of QGP, cosmic rays (p-O collisions)
- Oxygen (Neon) specifically interesting: can we see 4 (5) clusters of alpha-particles?
- Neon – Lead beam gas collisions foreseen at LHCb fixed target mode

pp opportunities
at the LHC

Oxygen nuclear structure



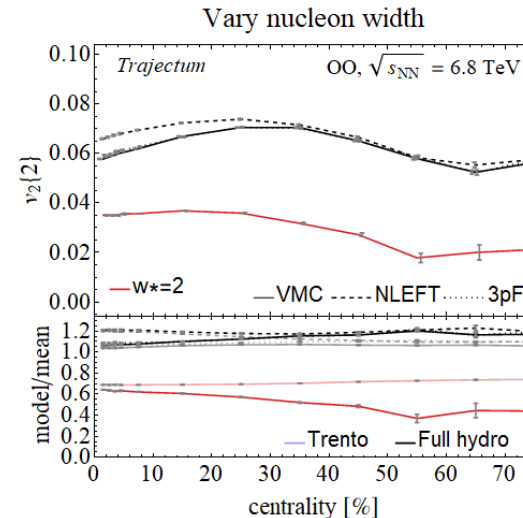
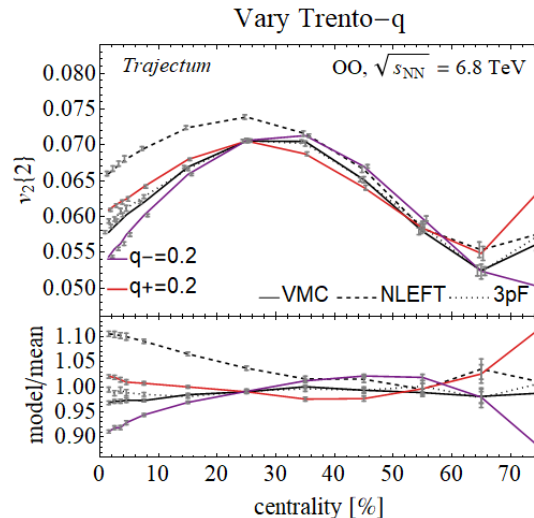
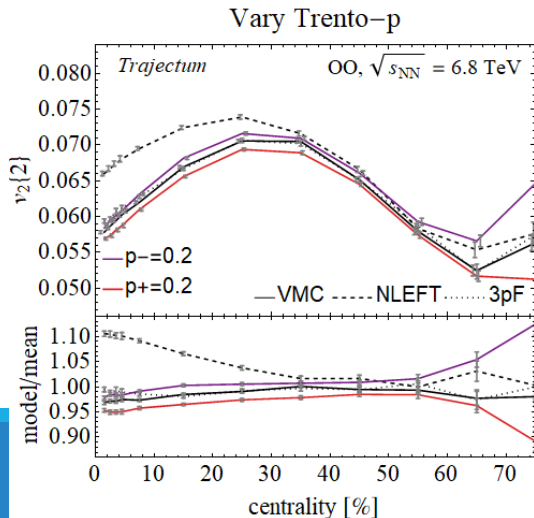
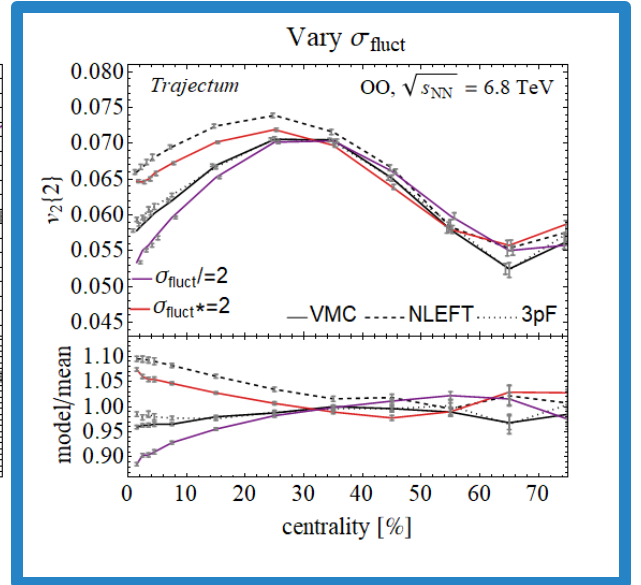
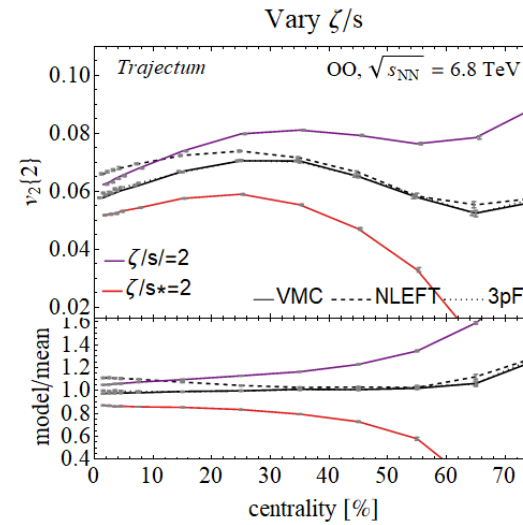
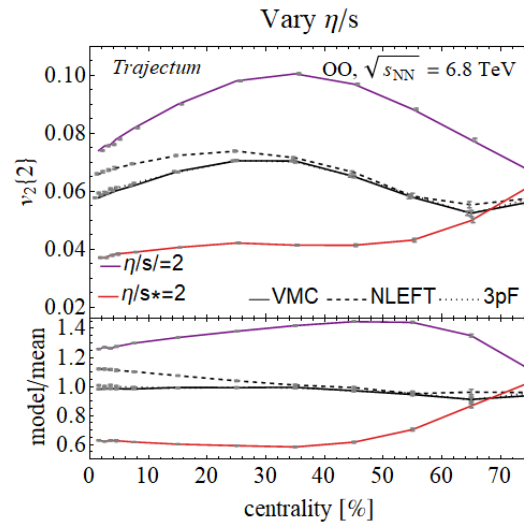
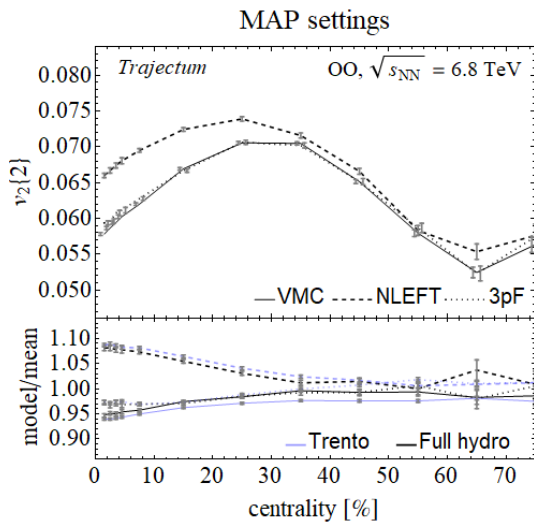
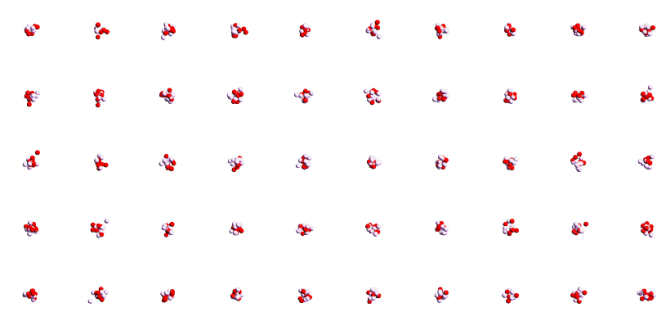
1. Comparing two state-of-the-art microscopics with old profile (MAP run with 100M events per run)
 - 3pF: 3 parameter Wood-Saxon Fermi fit from 1976 with d_{\min}
 - VMC: Variational Monte Carlo to sample wave function with advanced nucleon interaction
 - NLEFT: Nuclear Lattice Effective Field Theory, ground state with 'pin holes' (no repulsive interaction implemented)
2. Elliptic flow does not distinguish VMC/3pF
 - Other observables can (e.g. mean transverse momentum)
3. Significant differences for central collisions



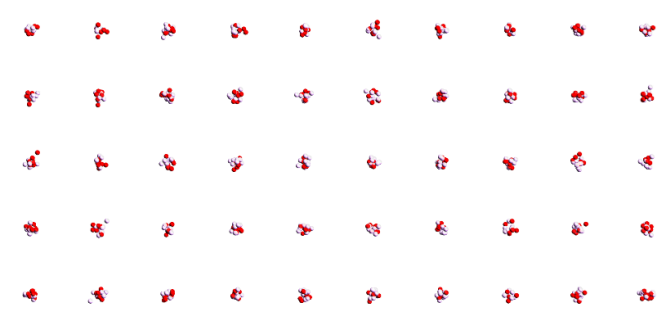
Oxygen nuclear structure

Are results robust when varying parameter?

- Not really... nuclear structure similar to fluctuations



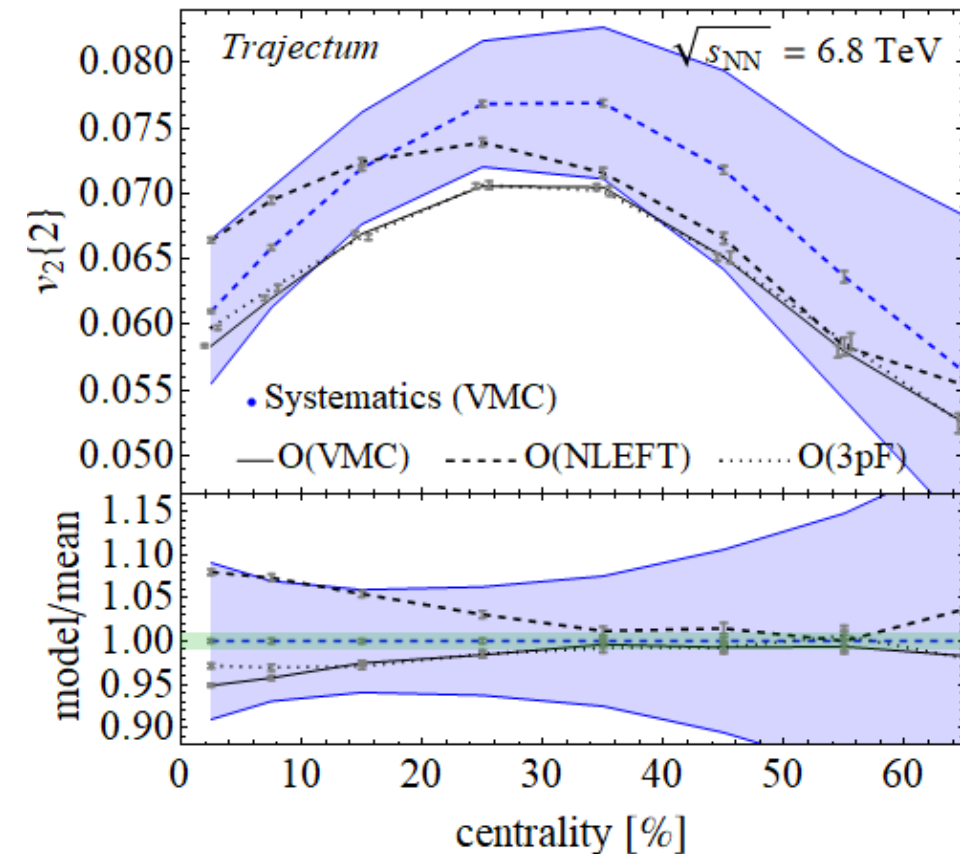
Oxygen nuclear structure



Can we do this more systematically?

- Parameters such as viscosities are highly correlated
- Take random sample of 'probable' parameter settings
- Compute one standard deviation systematic uncertainty

Systematic uncertainty comparable to differences due to nuclear structure



The PbPb cross section and the centrality normalisation

Cross section follows from

- Luminosity (van der Meer scan, dominates uncertainty)
- The number of collisions
- First measured **in April 2022 (!)**

ALICE can accurately measure collisions in 0-90% region

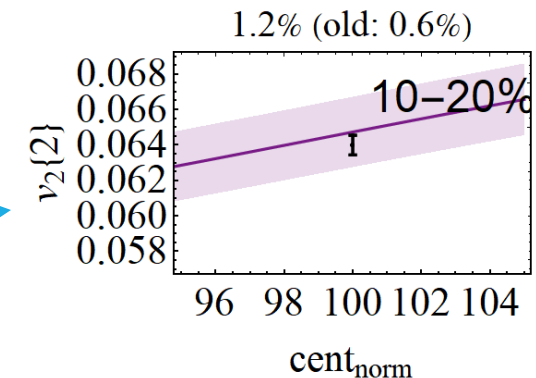
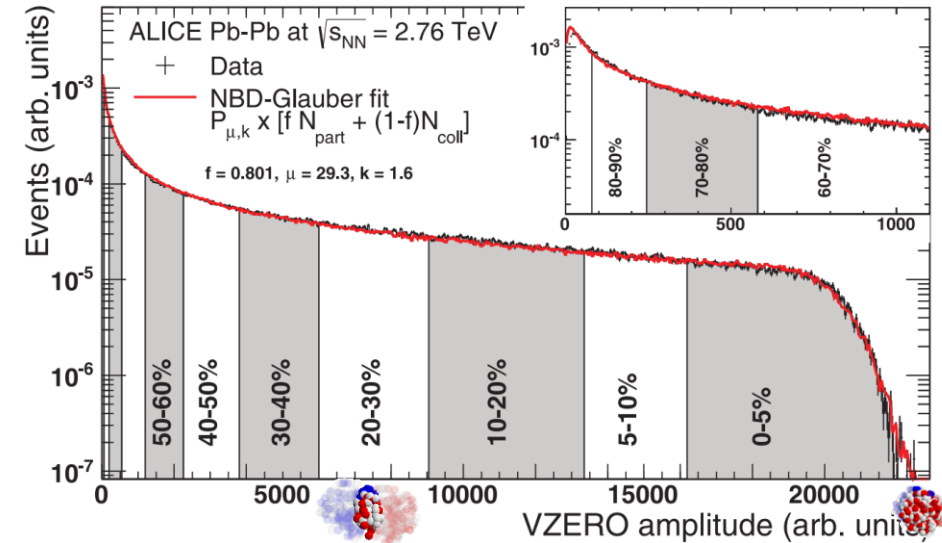
- 90-100% is estimated from NBD Glauber fit

Trajectum defines 100% by having at least one nucleon-nucleon interaction

- Now also a parameter, perhaps as a check, or to address experimental uncertainty
- We take a Gaussian prior of width 1%

Centrality normalisation trivially correlates **all** observables by shifting classes

- Probably best to marginalise over in MCMC Bayesian analysis
- Means ALICE should quote this uncertainty separately
- Important even for some central observables ($v_2\{2\}$)

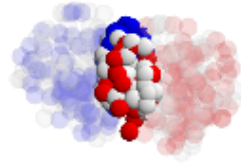


The nucleon width and the total PbPb hadronic cross section

What is easier to measure the width than by simply measuring the size?

Fix nucleon-nucleon cross section:

$$P_{\text{coll}} = 1 - \exp\left[-\sigma_{gg} \int dx dy \int dz \rho_A \int dz \rho_B\right]$$



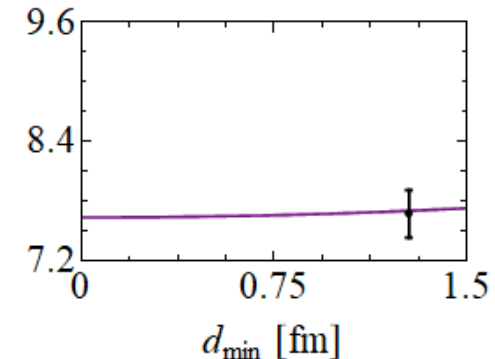
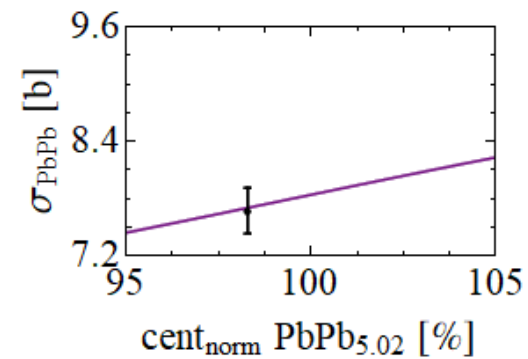
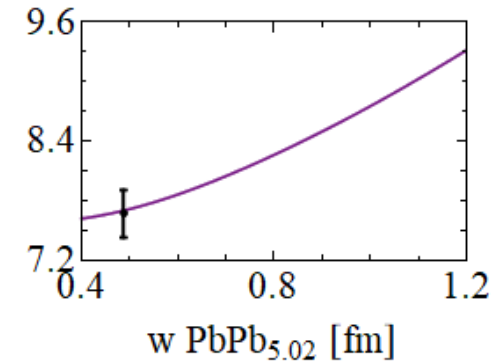
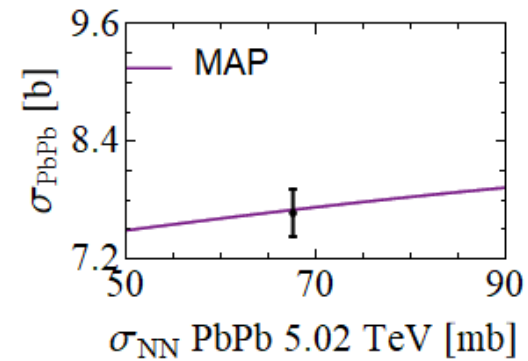
e.g. collision probability tuned to σ_{NN} for Gaussian profile ρ

Theoretically, cross section only depends on

- Nucleon-nucleon cross section
- Nucleon Gaussian width (dominant)
- Centrality normalisation
- Minimum inter-nucleon spacing

Makes the cross section a robust observable

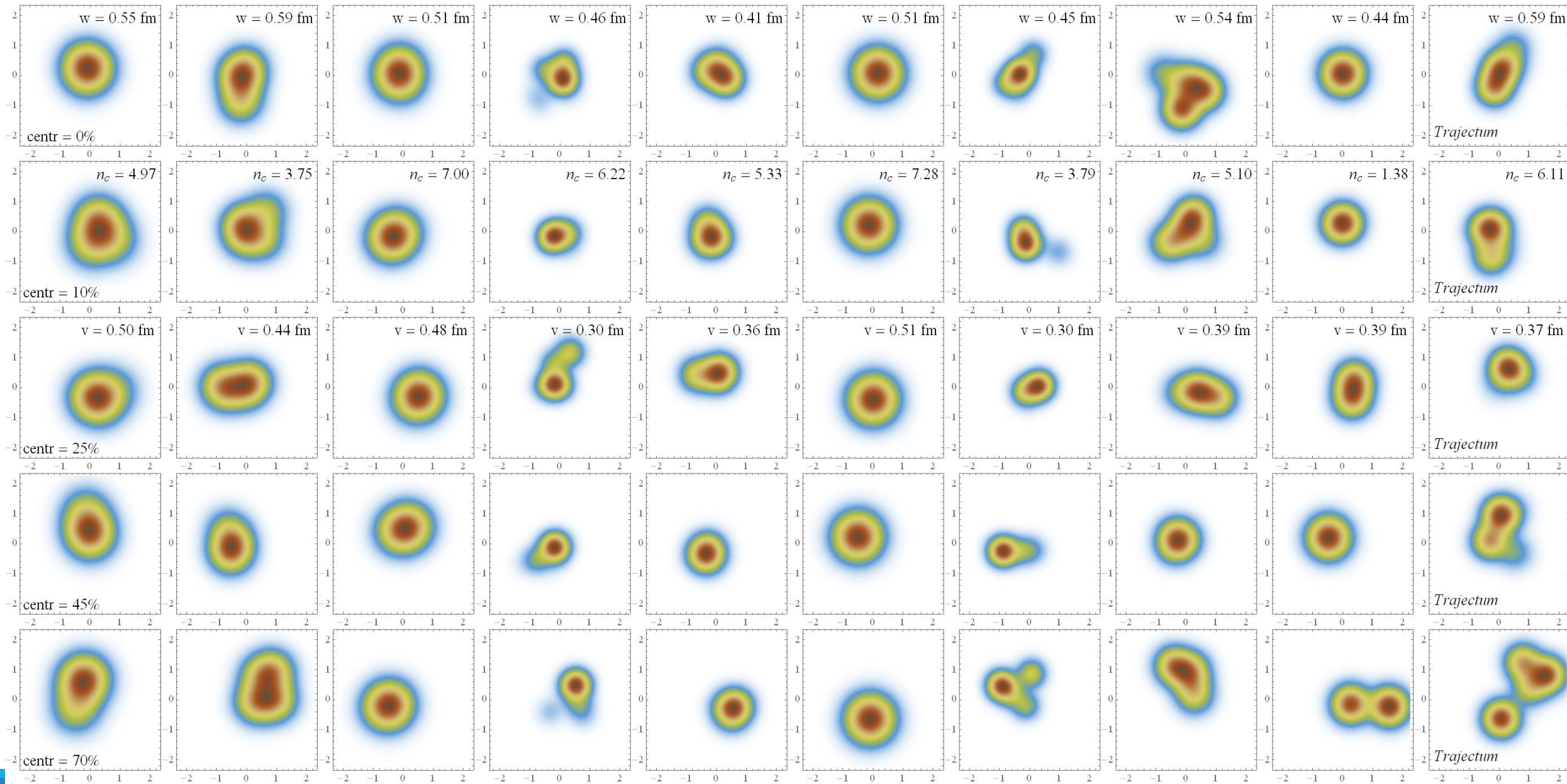
- Basically implying every model needs to get this right
- Basically implying the nucleon width should be small



Ten different probable parameter settings \rightarrow

Thickness function nucleon

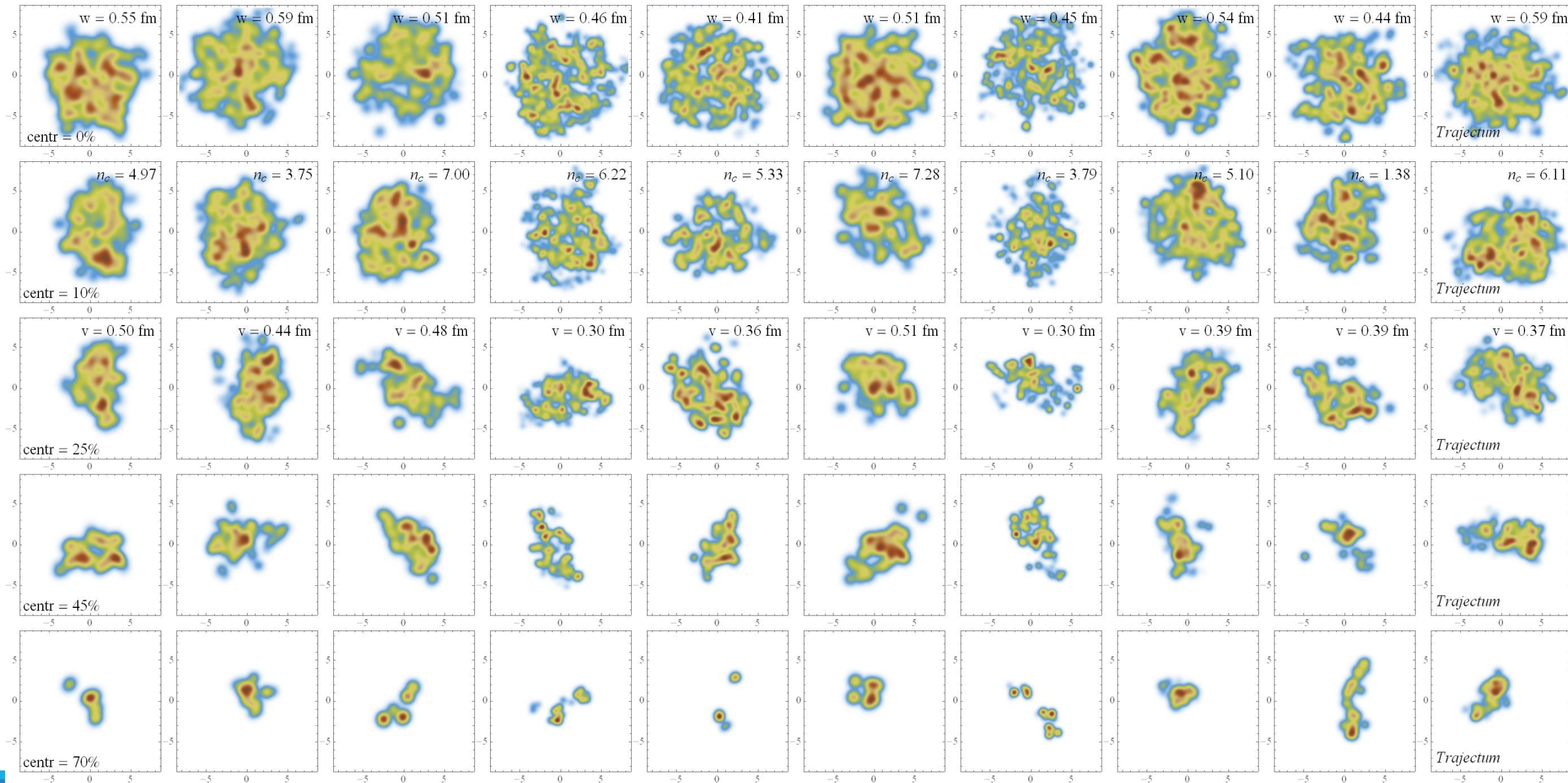
Configurations \rightarrow



Ten different probable parameter settings \rightarrow

Thickness function Pb

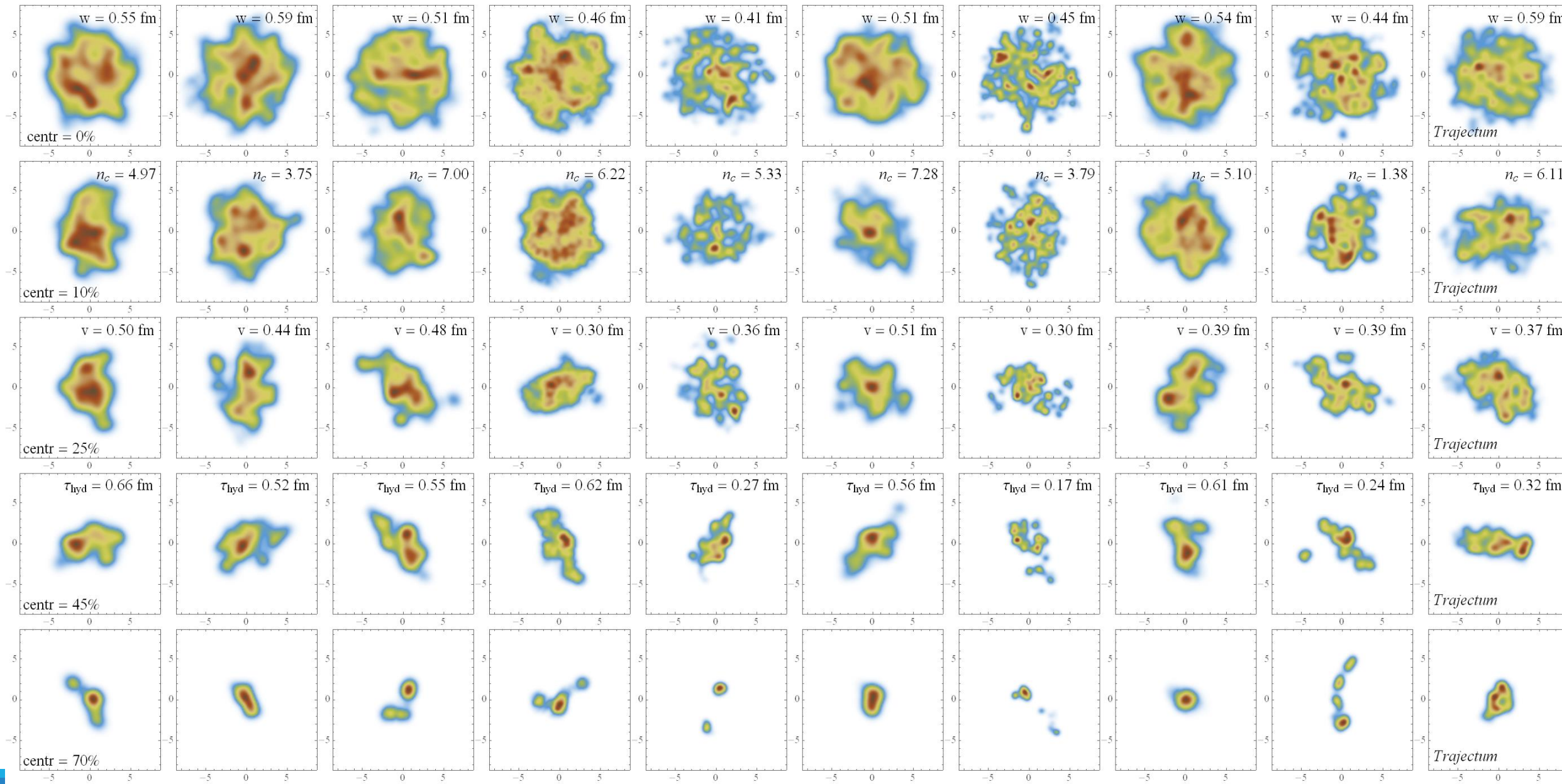
Centrality \rightarrow



Ten different probable parameter settings \rightarrow

Energy density function Pb

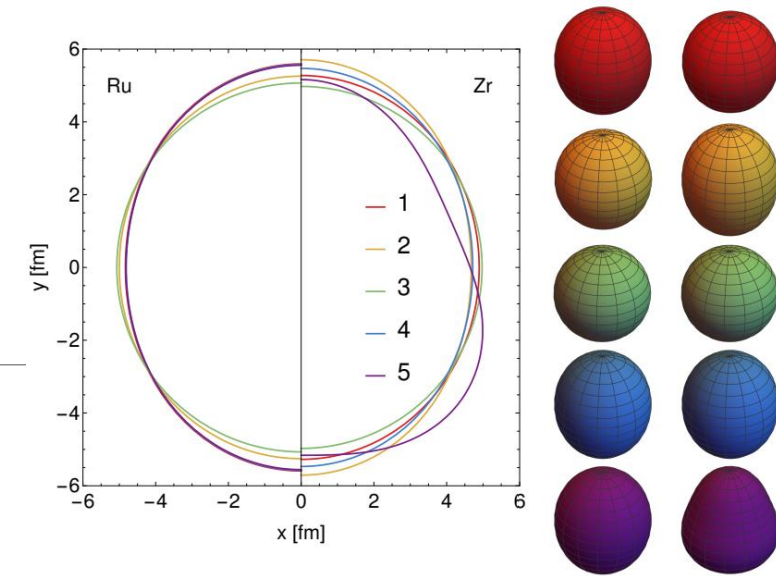
Centrality \rightarrow



Isobar collisions at STAR

Five different cases simulated:

nucleus	R_p [fm]	σ_p [fm]	R_n [fm]	σ_n [fm]	β_2	β_3	σ_{AA} [b]
$^{96}_{44}\text{Ru}(1)$	5.085	0.46	5.085	0.46	0.158	0	4.628
$^{96}_{40}\text{Zr}(1)$	5.02	0.46	5.02	0.46	0.08	0	4.540
$^{96}_{44}\text{Ru}(2)$	5.085	0.46	5.085	0.46	0.053	0	4.605
$^{96}_{40}\text{Zr}(2)$	5.02	0.46	5.02	0.46	0.217	0	4.579
$^{96}_{44}\text{Ru}(3)$	5.06	0.493	5.075	0.505	0	0	4.734
$^{96}_{40}\text{Zr}(3)$	4.915	0.521	5.015	0.574	0	0	4.860
$^{96}_{44}\text{Ru}(4)$	5.053	0.48	5.073	0.49	0.16	0	4.701
$^{96}_{40}\text{Zr}(4)$	4.912	0.508	5.007	0.564	0.16	0	4.829
$^{96}_{44}\text{Ru}(5)$	5.053	0.48	5.073	0.49	0.154	0	4.699
$^{96}_{40}\text{Zr}(5)$	4.912	0.508	5.007	0.564	0.062	0.202	4.871



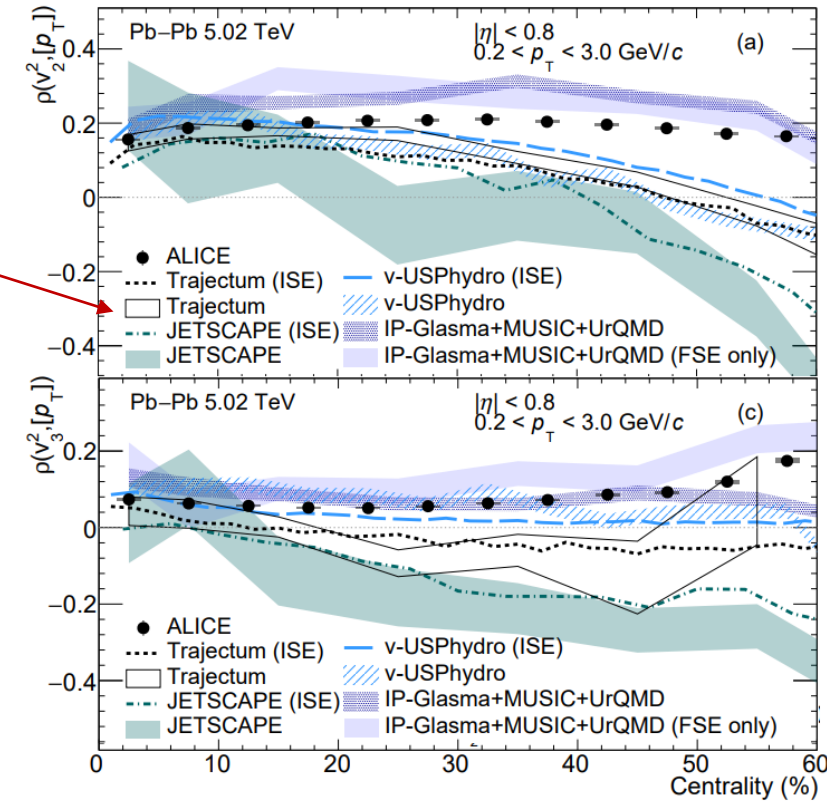
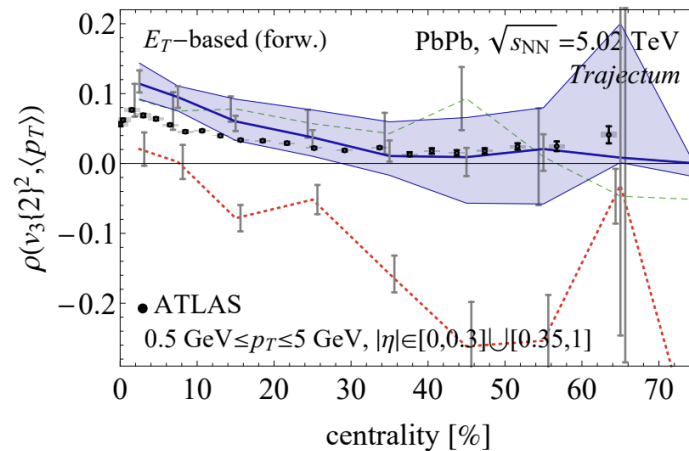
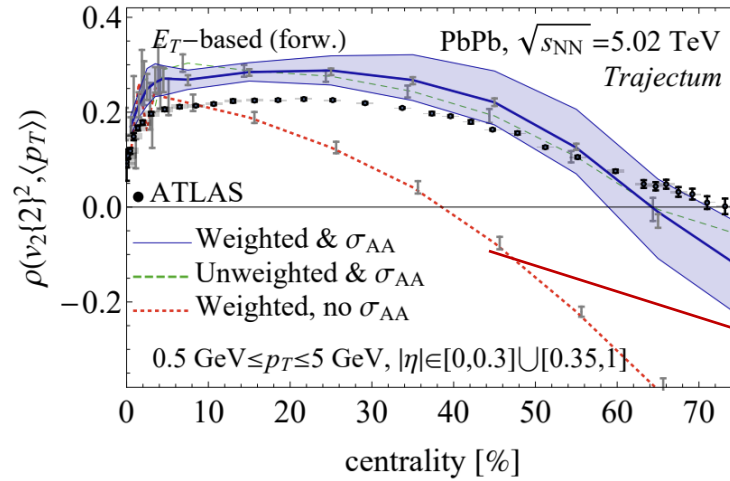
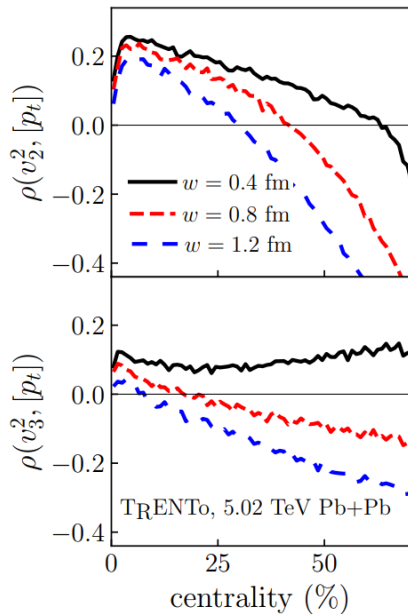
1. e-A scattering experiments(STAR case 1)
2. Theory (finite-range liquid drop model, STAR 2)
3. DFT with neutron skin (spherical) [1]
4. DFT with neutron skin (deformed, $\beta_2 = 0.16$) [1]
5. As 4, but with β_2 from electric transition probability and β_3 from comparing AMPT with STAR [2]

Bonus: mean p_T and v_2 or v_3 correlations

A Bayesian MAP check: unfitted data:

- Triple differential observables:
- Correlation p_T and v_n

Anticipated by (simpler) Trento analysis:

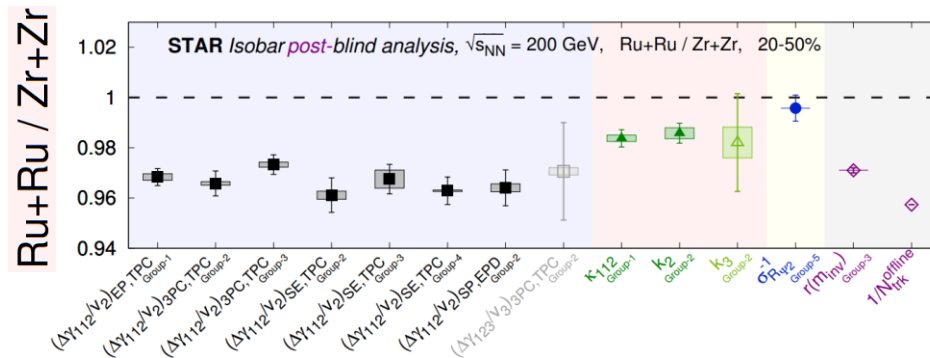


Isobar collisions at STAR

Varying the magnetic field

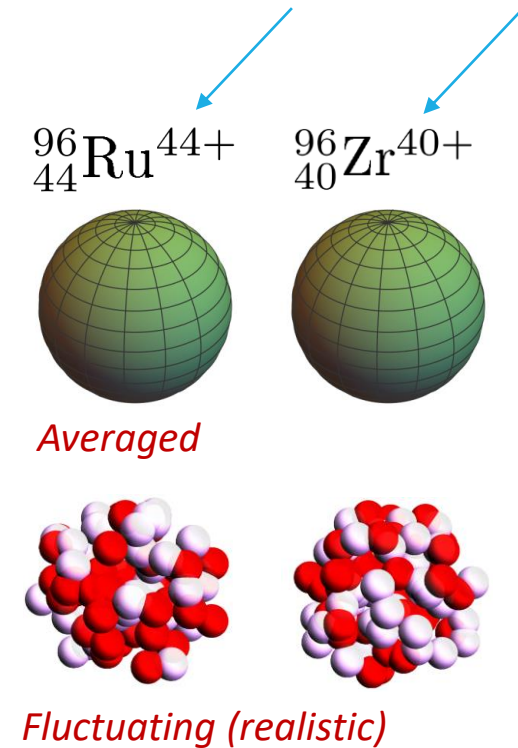
Idea: similar nuclei (same # of baryons), different charge

- Ruthenium generates a 10% larger magnetic field
- Ideal set-up to suppress background and detect Chiral Magnetic Effect (CME)
- Very precise blinded analysis by STAR:



CME-like

No CME



Unfortunately (?), no CME detected

For each case we run 0.5M collisions except for case 5 (5M), 14M in total.

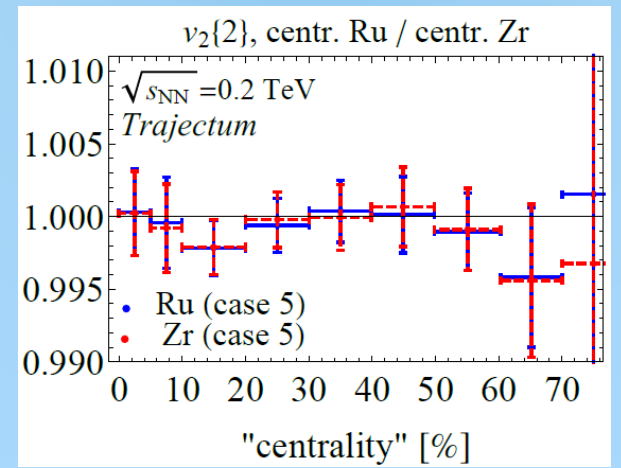
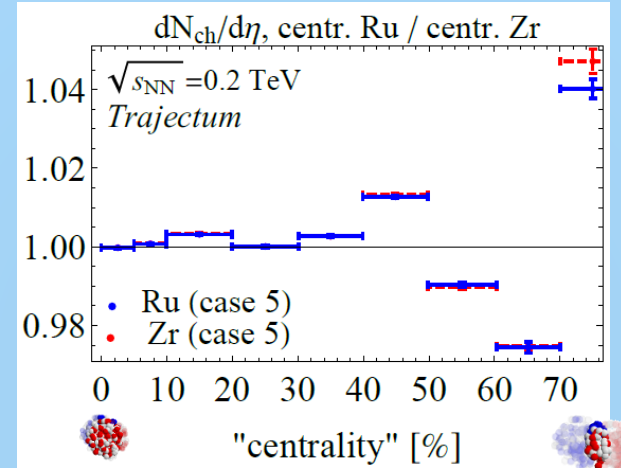
Isobar collisions at STAR - Multiplicity

Precision and non-conventional definition of centrality

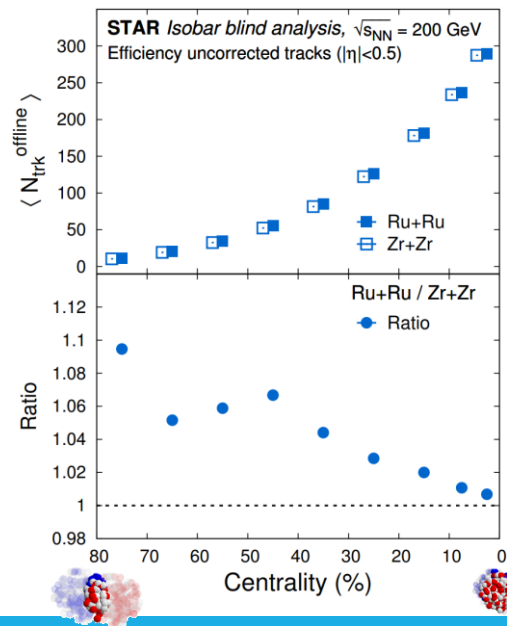
Subtlety in STAR data: "centrality label" is different for Ru and Zr

- Especially important for multiplicity (~7% effect)
- Hardly significant for other observables (<0.5% for v_2)

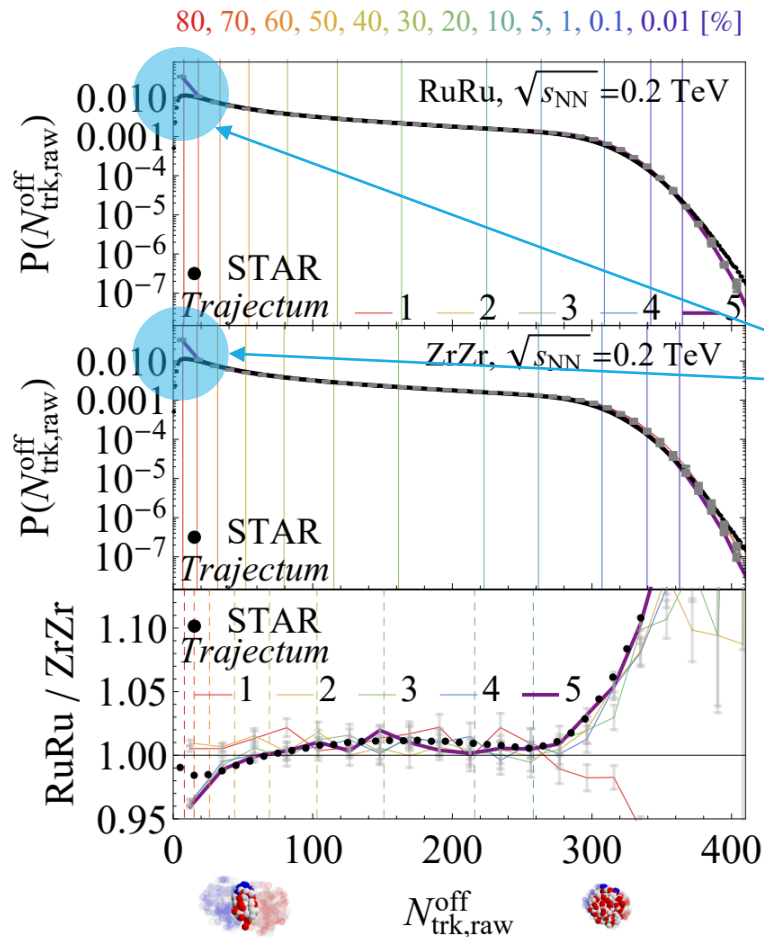
Theory: only change centrality bounds



Centrality label (%)	Centrality(%)	Ru+Ru $N_{trk}^{offline}$	$\langle N_{trk}^{offline} \rangle$	Zr+Zr Centrality(%)	Zr+Zr $N_{trk}^{offline}$	$\langle N_{trk}^{offline} \rangle$
0-5	0-5.01	258.-500.	289.32	0-5.00	256.-500.	287.36
5-10	5.01-9.94	216.-258.	236.30	5.00-9.99	213.-256.	233.79
10-20	9.94-19.96	151.-216.	181.76	9.99-20.08	147.-213.	178.19
20-30	19.96-30.08	103.-151.	125.84	20.08-29.95	100.-147.	122.35
30-40	30.08-39.89	69.-103.	85.22	29.95-40.16	65.-100.	81.62
40-50	39.89-49.86	44.-69.	55.91	40.16-50.07	41.-65.	52.41
50-60	49.86-60.29	26.-44.	34.58	50.07-59.72	25.-41.	32.66
60-70	60.29-70.04	15.-26.	20.34	59.72-70.00	14.-25.	19.34
70-80	70.04-79.93	8.-15.	11.47	70.00-80.88	7.-14.	10.48
20-50	19.96-49.86	44.-151.	89.50	20.08-50.07	41.-147.	85.68

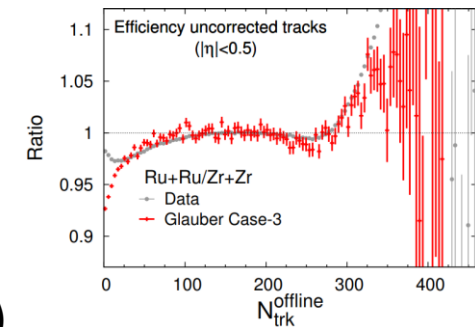
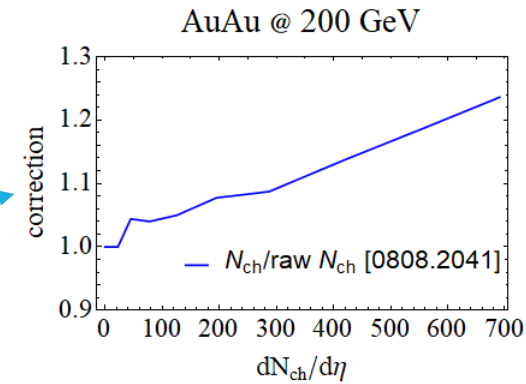


Isobar collisions at STAR - Multiplicity



Better to directly look at (raw) data

- Experimental subtlety: crucial to correct for detector efficiency
- *Trajectum* subtlety: norm not fitted to RHIC energy: multiply mult by 1.21
- Experiment misses (many) very peripheral collisions: multiply $P(N)$ by 1.31 to correct for this (not for ratio)
- Ratio experiment: normalise both and divide
Subtle: experiment unreliable for $N_{trk} < 50$
 Ratio theory: integrate **Ru+Zr experiment and Ru+Zr theory** for $N_{trk} > 50$ and require ratio to match
 Exp-theory comparison only depends on $N_{trk} > 50$



Only case 3, 4 and 5 match well over entire range (neutron-skin)

Initial state predictors

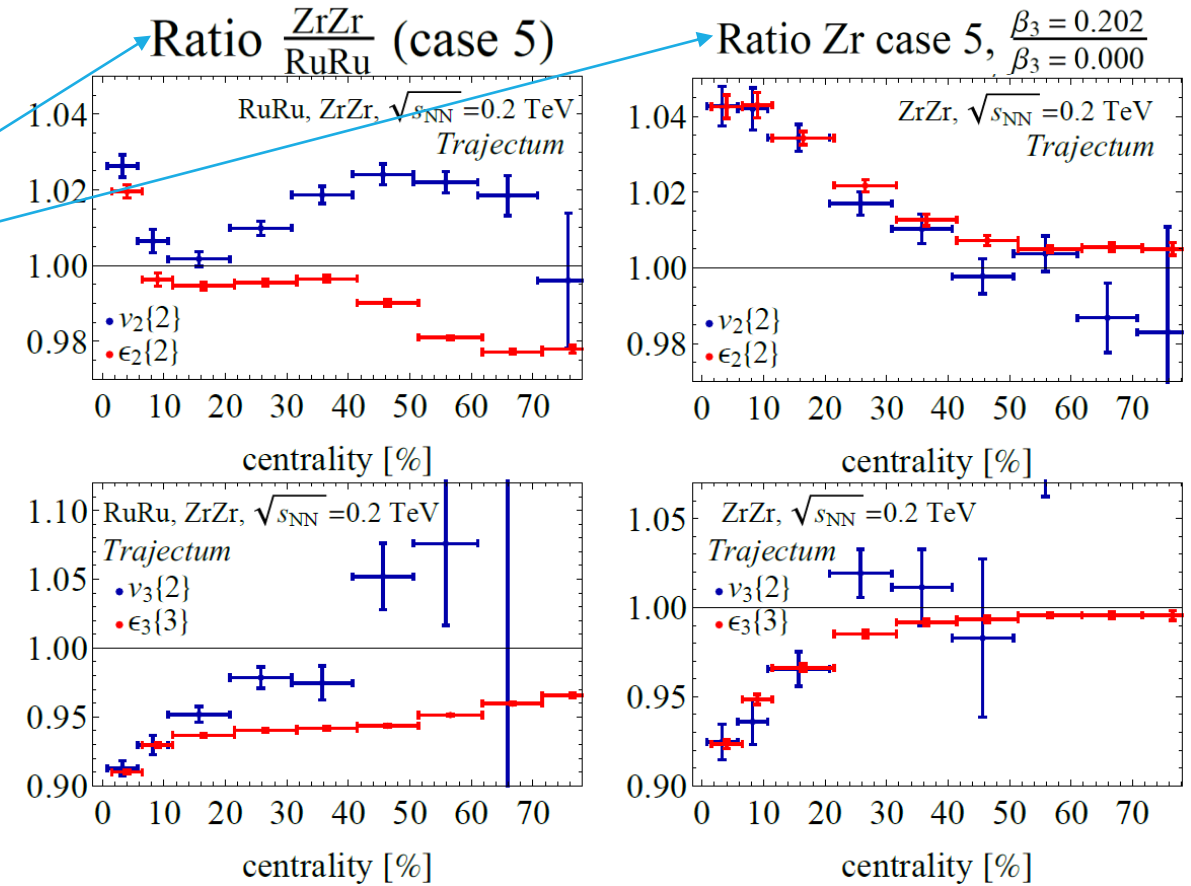
With large sample we can verify the relation

$$v_n\{2\} = \kappa \epsilon_n\{2\}$$

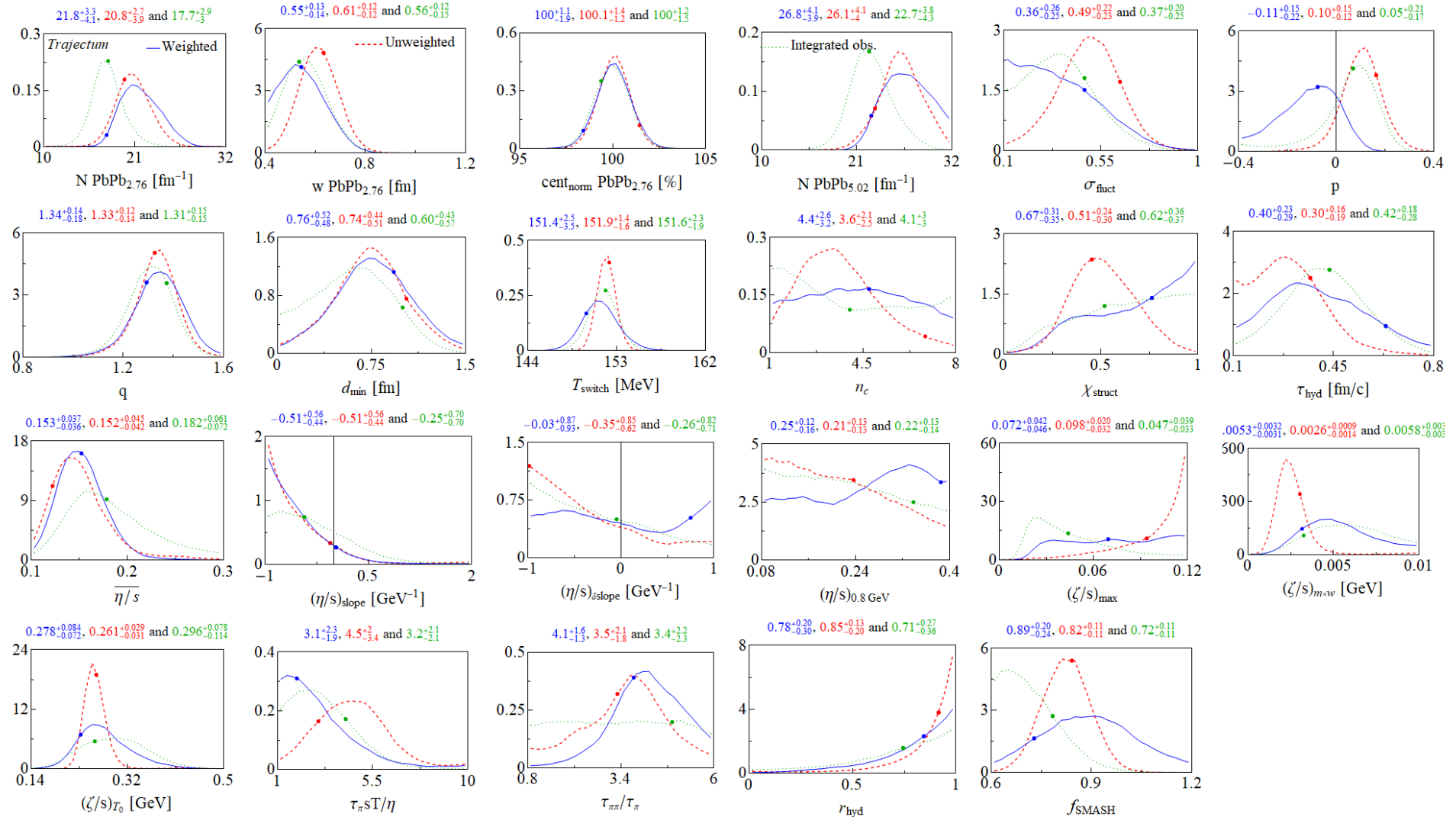
All else being equal this works, e.g. within Zr as in right plots

If also size changes etc (Zr vs Ru), it can affect κ and the initial geometry cannot be used

Unfortunate: hydro is expensive...

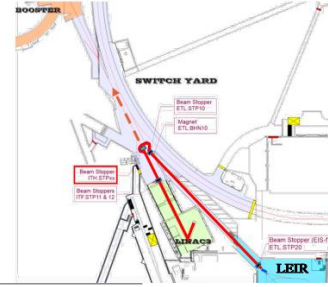


Full posterior distributions

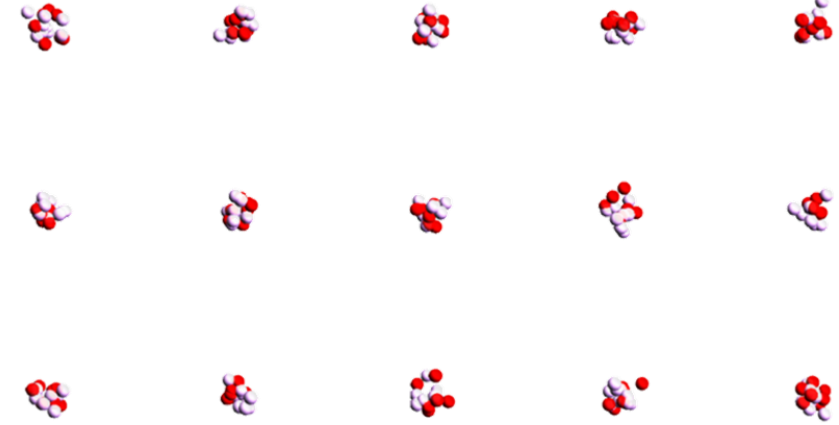
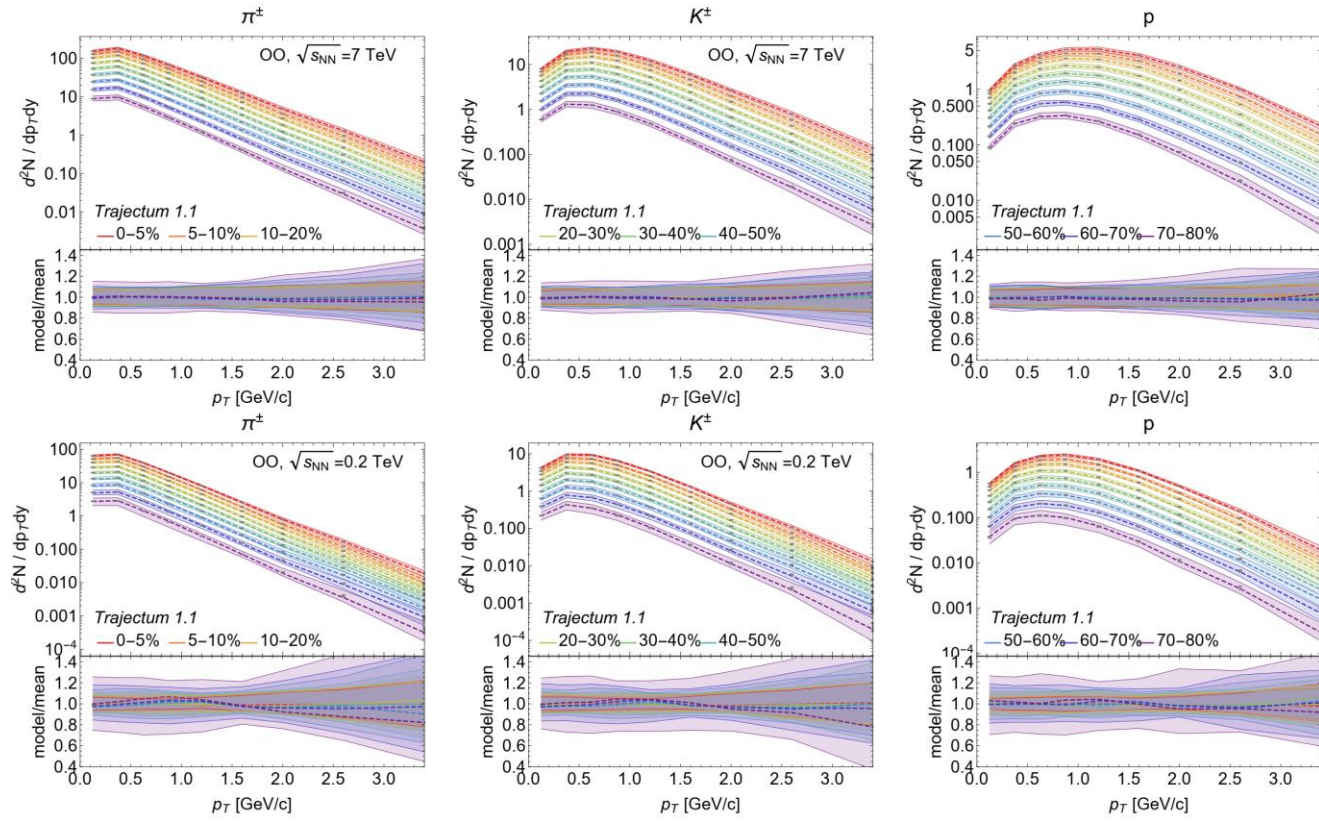


Exciting: oxygen-oxygen special run in 2024!

- Special **O-O** and **p-O** run
- ❑ Physics motivations: study of emergence of collective effects in small systems; measurements relevant for cosmic rays (extensive air shower modelling), etc.
 - ❑ Experiments requested $\sim \text{nb}^{-1}$ for each of OO and pO. ~ 1 week (including commissioning), most likely in 2024
 - ❑ No impediment from accelerators but radiological impact of high-intensity oxygen beam requires mitigation measures and additional beams stoppers to be able to access Booster when LEIR operates.
 - ❑ Needed resources allocated in this MTP

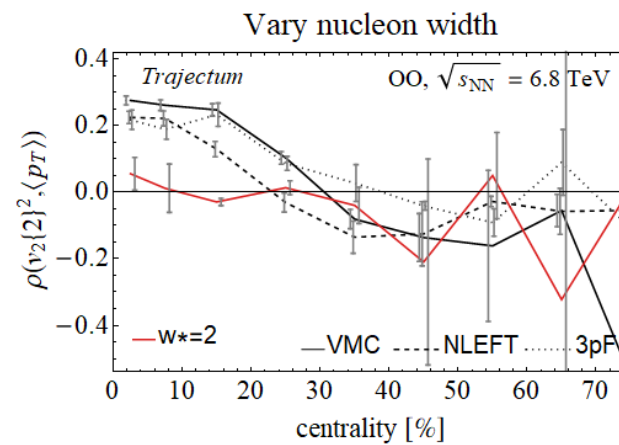
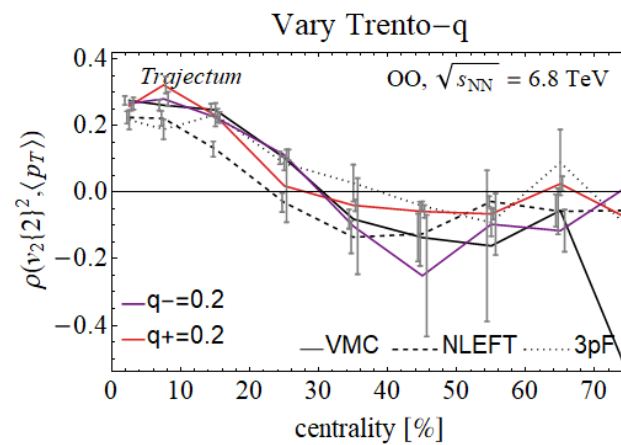
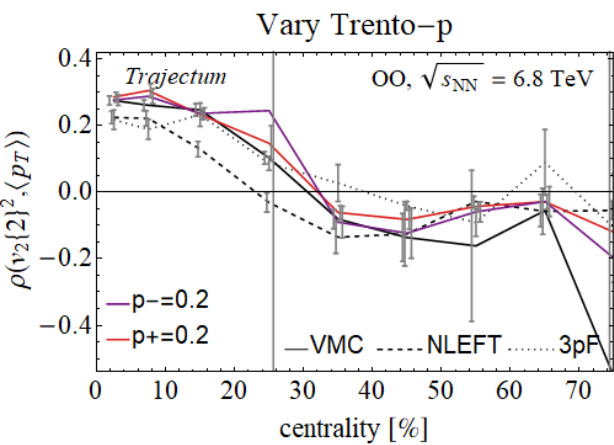
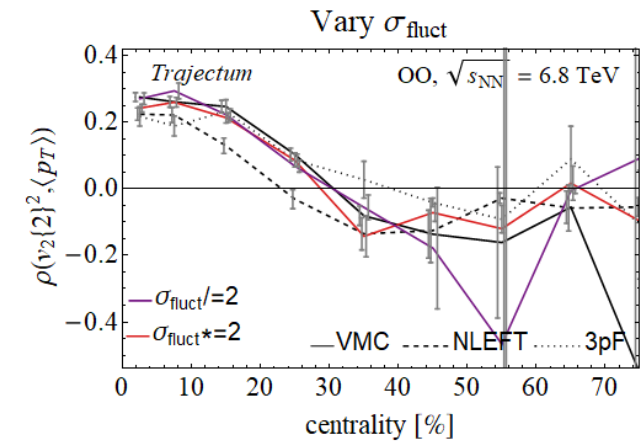
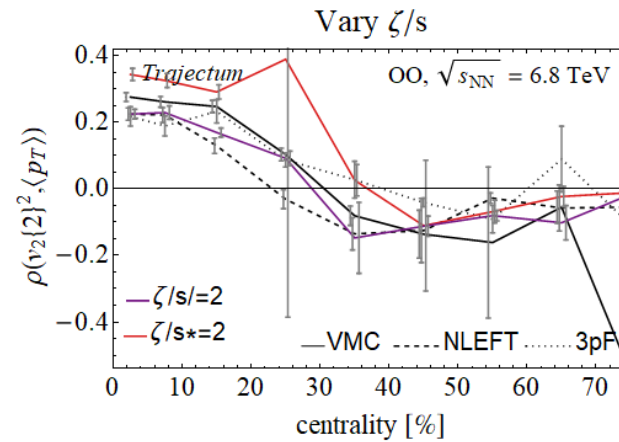
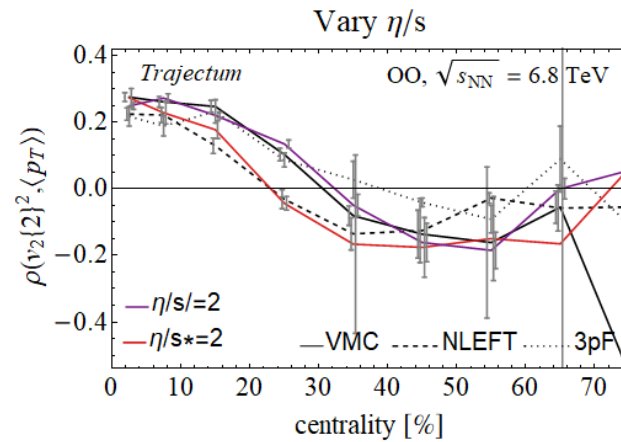
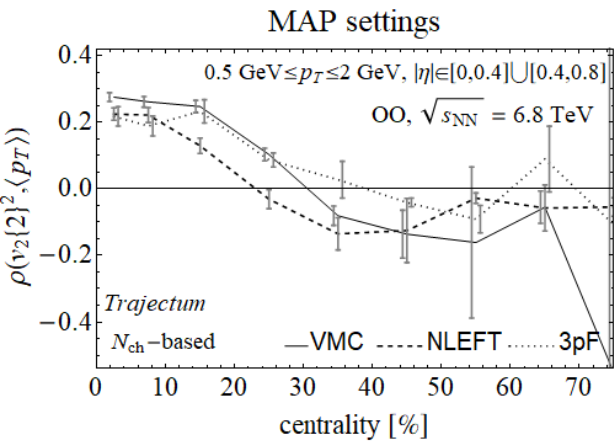
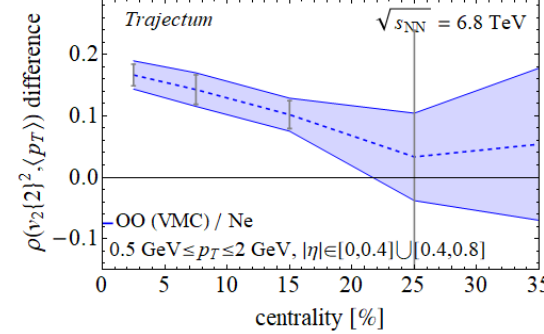
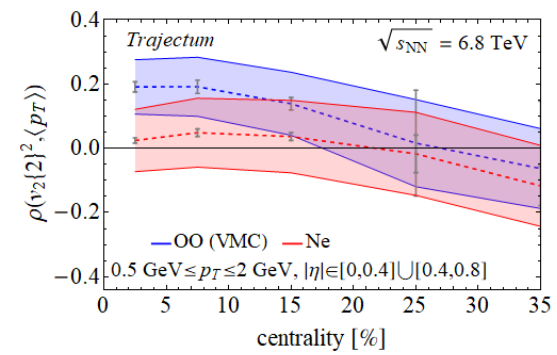


1. Predictions for oxygen at RHIC (run already performed) and LHC
 - Perhaps surprisingly narrow predictions, only fitted on PbPb data



Correlation between v_2 and mean p_T

Vary some model parameters (for VMC only)



Conjectured to be a good observable. But must be careful with width and viscosities.