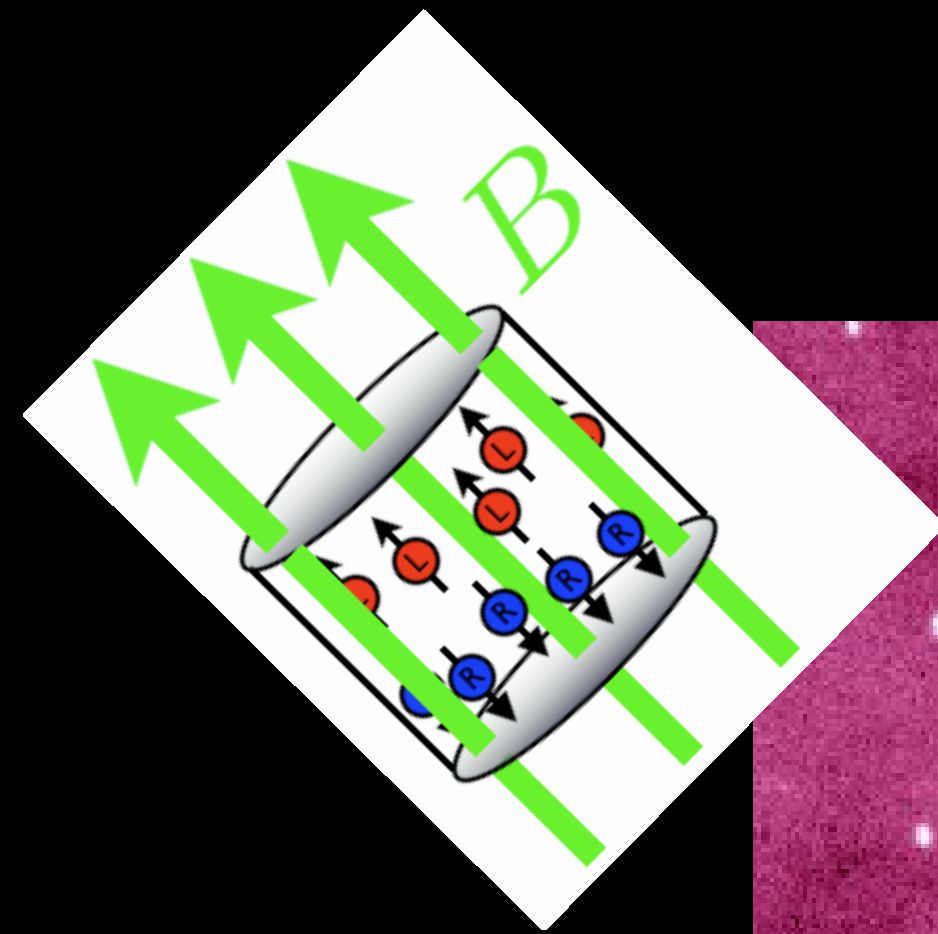


# Discussion contribution: Chiral Hydrodynamics Kicks Neutron Stars

ECT\* Workshop: Strongly interacting matter in extreme magnetic fields

ECT\*, Trento, Italy

September 26-7th, 2023



[Kaminski, Uhlemann, Schaffner-Bielich, Bleicher; *Phys.Lett.B* (2016)]

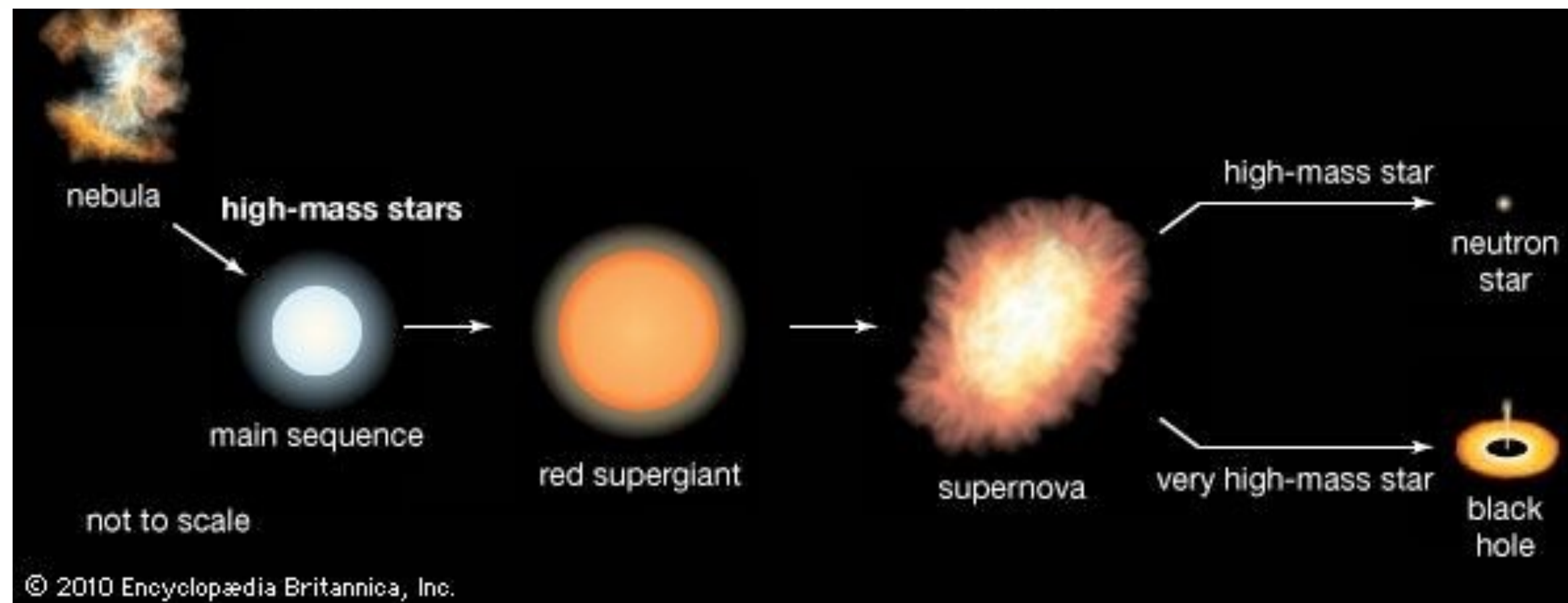


Matthias Kaminski  
University of Alabama

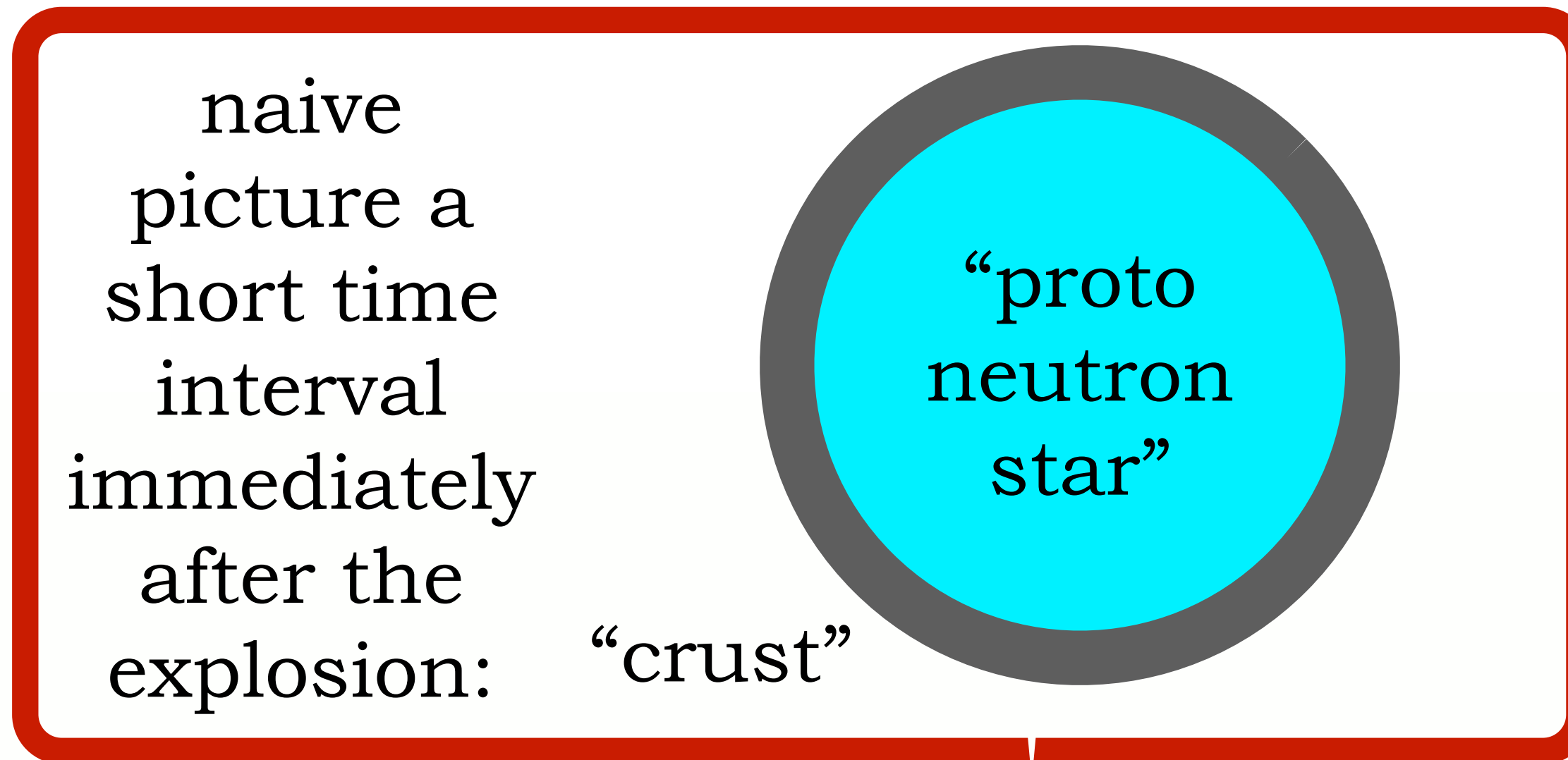


# Neutron star picture

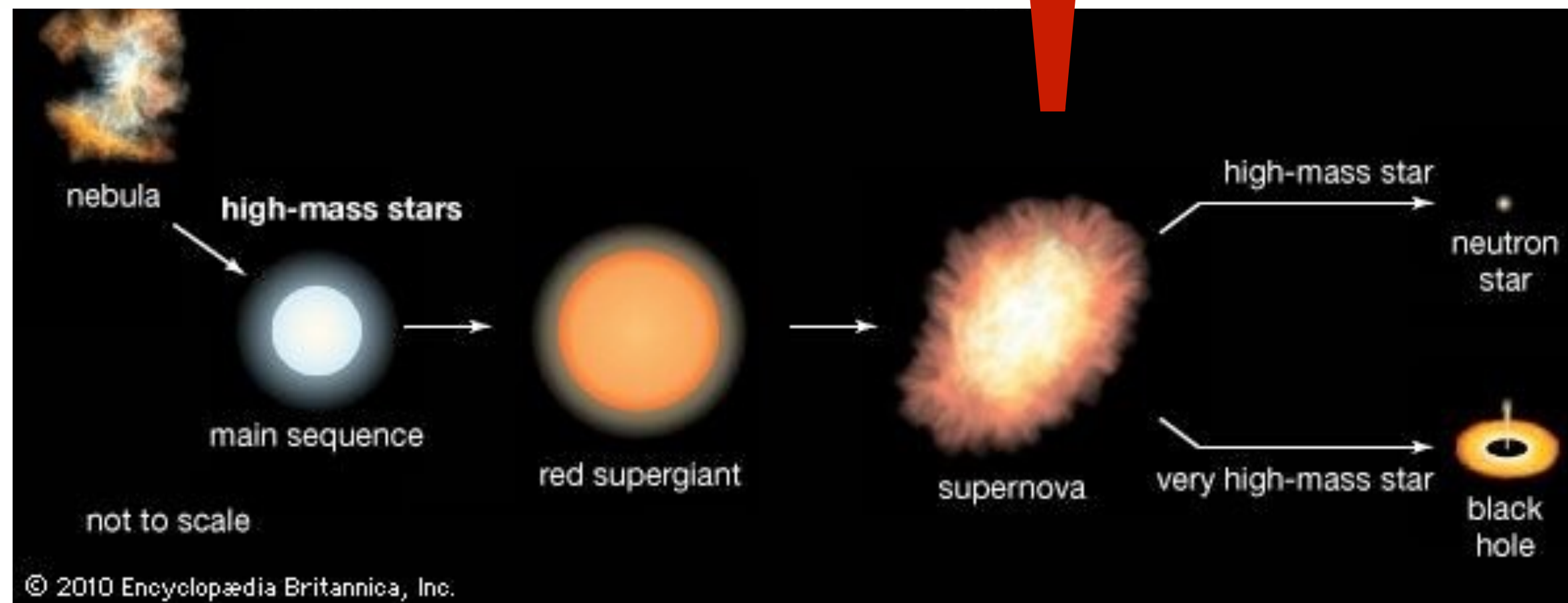
- ▶ compact star
  - \* small radius
  - \* large mass
  - \* high density
- ▶ quick rotation
- ▶ large  $B$  field



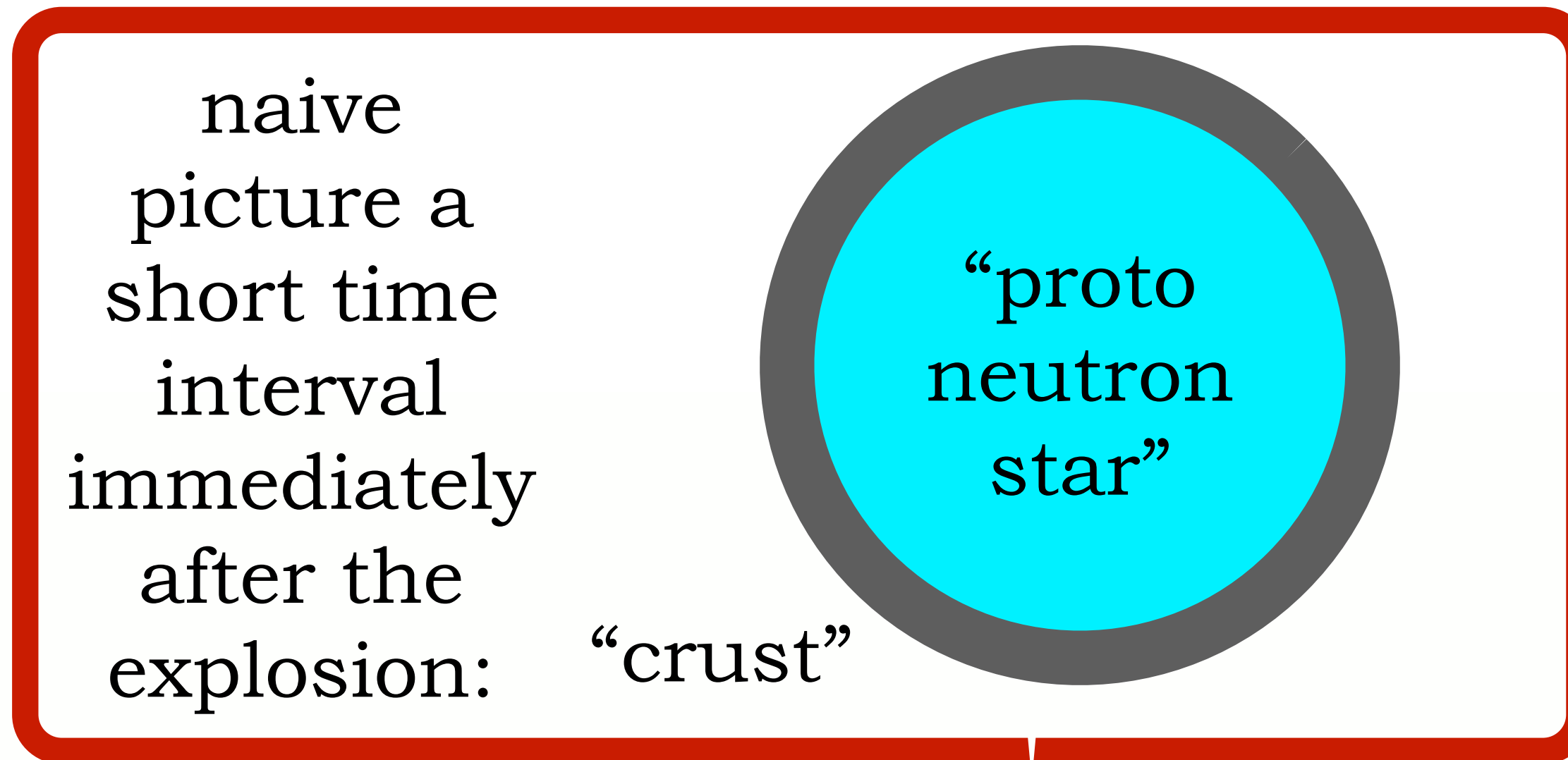
# Neutron star picture



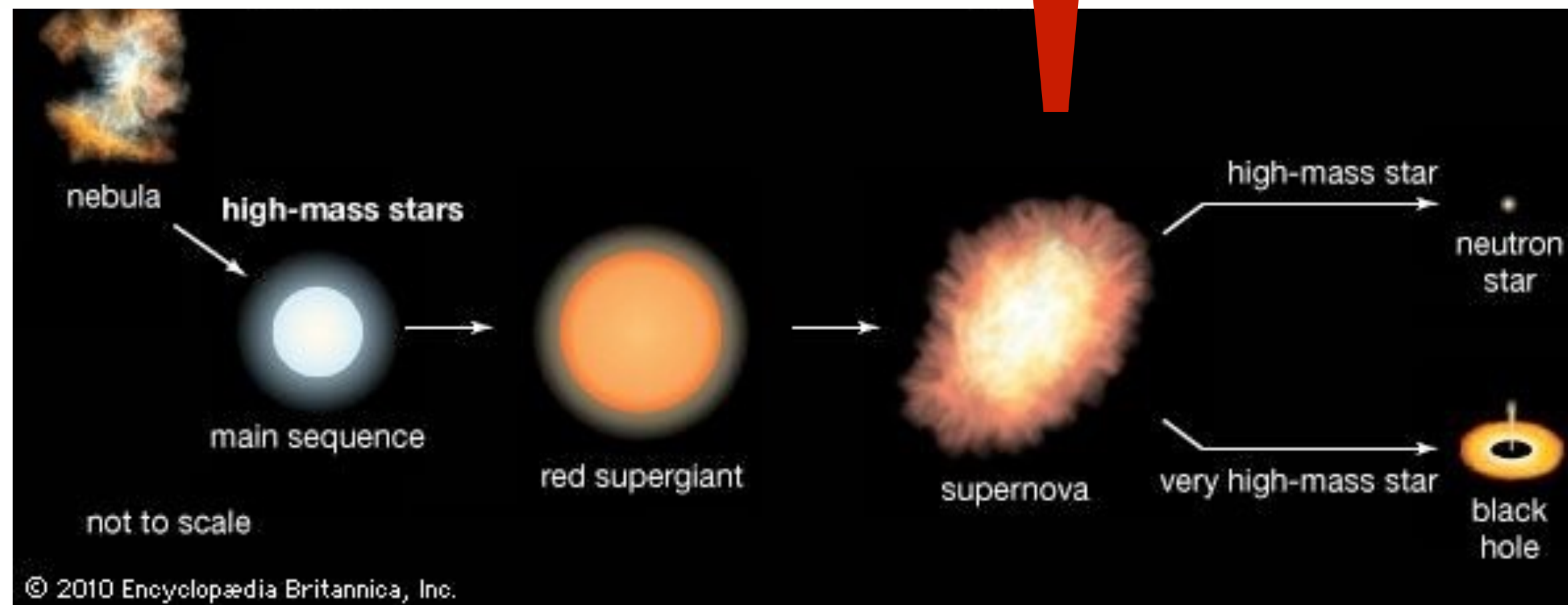
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# Neutron star picture



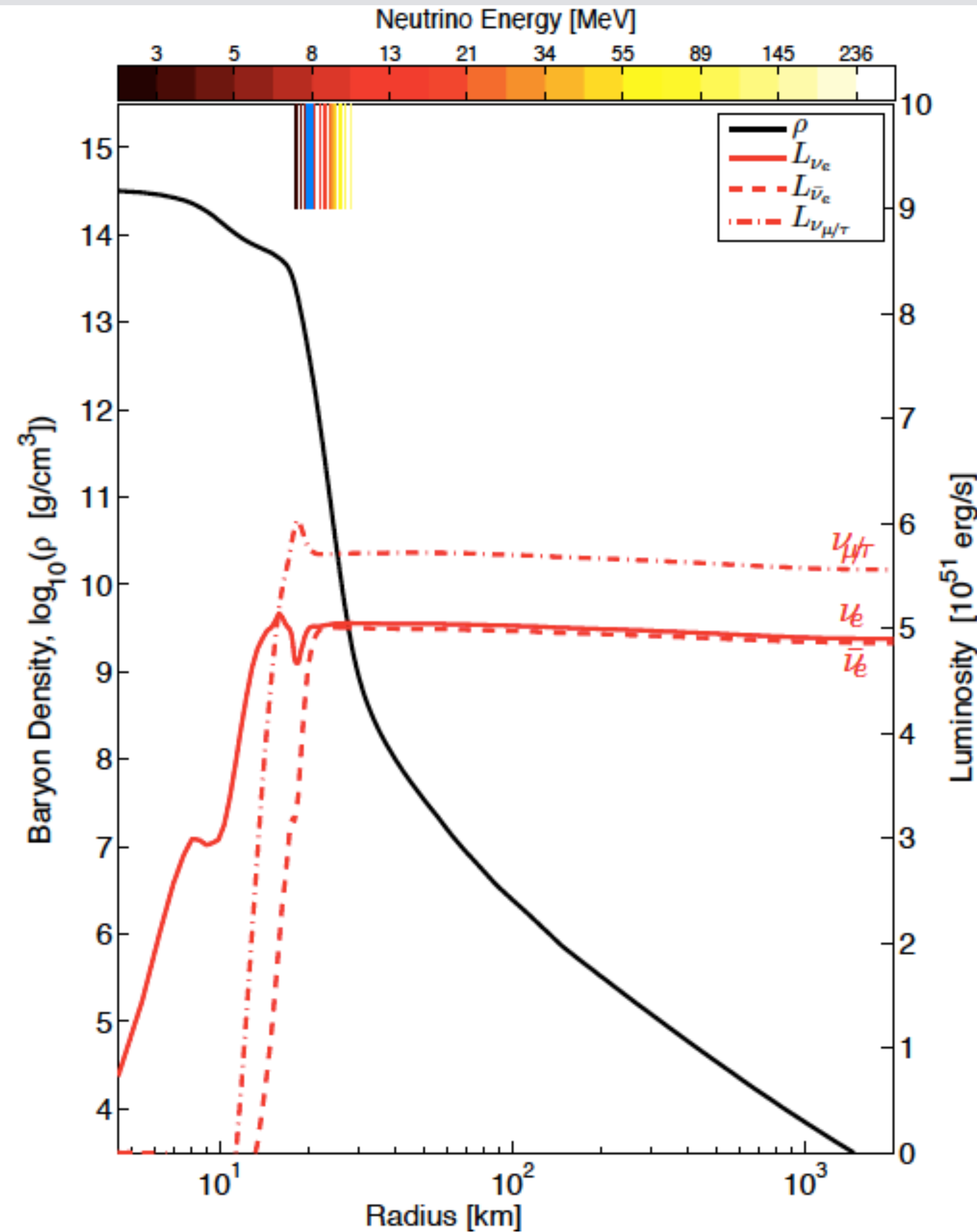
- ▶ compact star
  - \* small radius
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  - \* high density
- ▶ quick rotation
- ▶ large  $B$  field



proto-neutron stars are dense objects with “crust” and preferred directions



# First 10 seconds inside proto-neutron stars

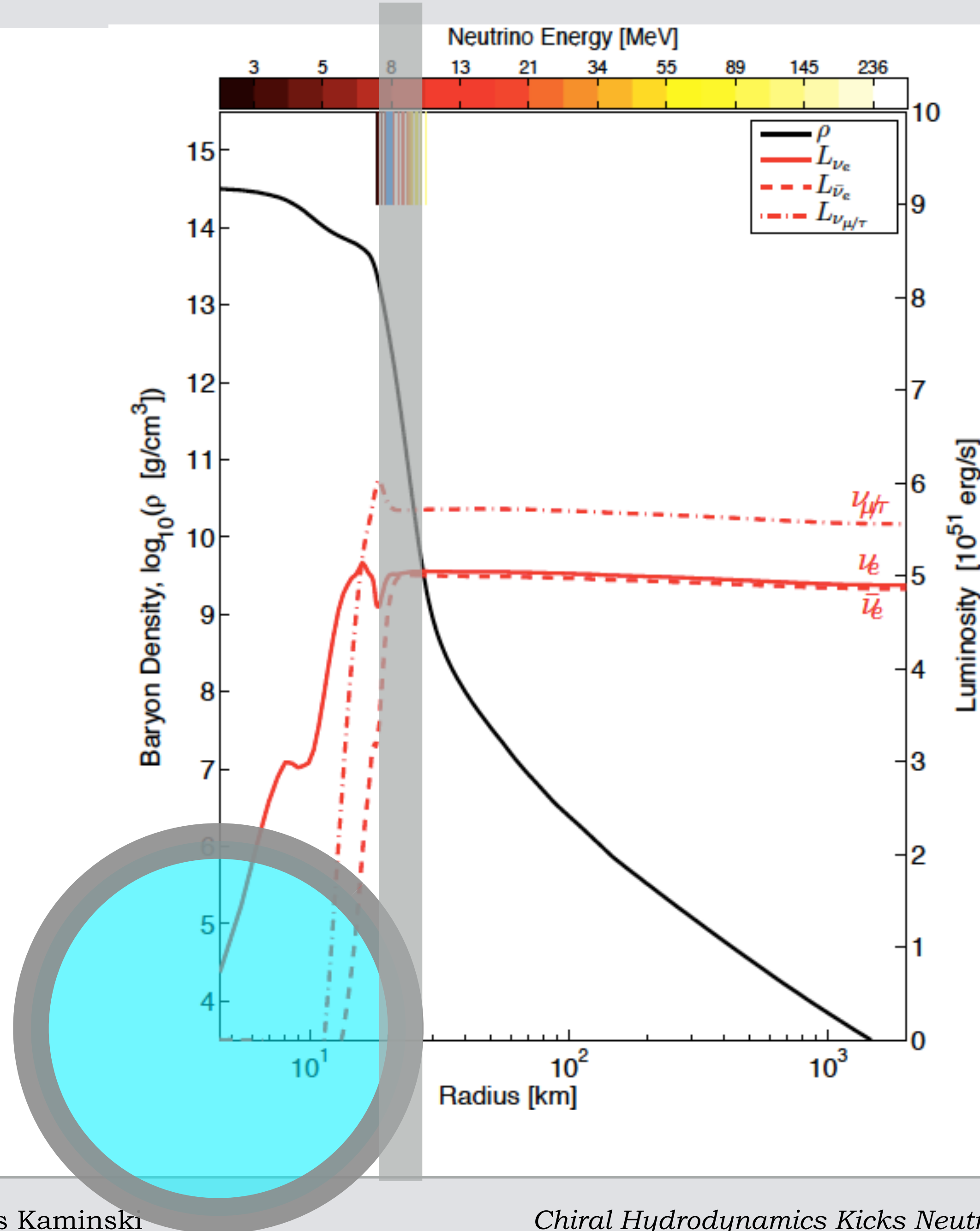


[Fischer et al.; PRD (2011)]

cf. [Wongwathanarat, Janka, Muller; (2012)]

- ▶ baryonic matter:
  - 10 km radius
- ▶ neutrinos: last scattering surfaces around 10 km
- ▶ no anti-neutrinos
- ▶ only electron flavor inside 10 km
- ▶ high densities
- ▶ neutrinos trapped! (everything trapped)

# First 10 seconds inside proto-neutron stars



[Fischer et al.; PRD (2011)]

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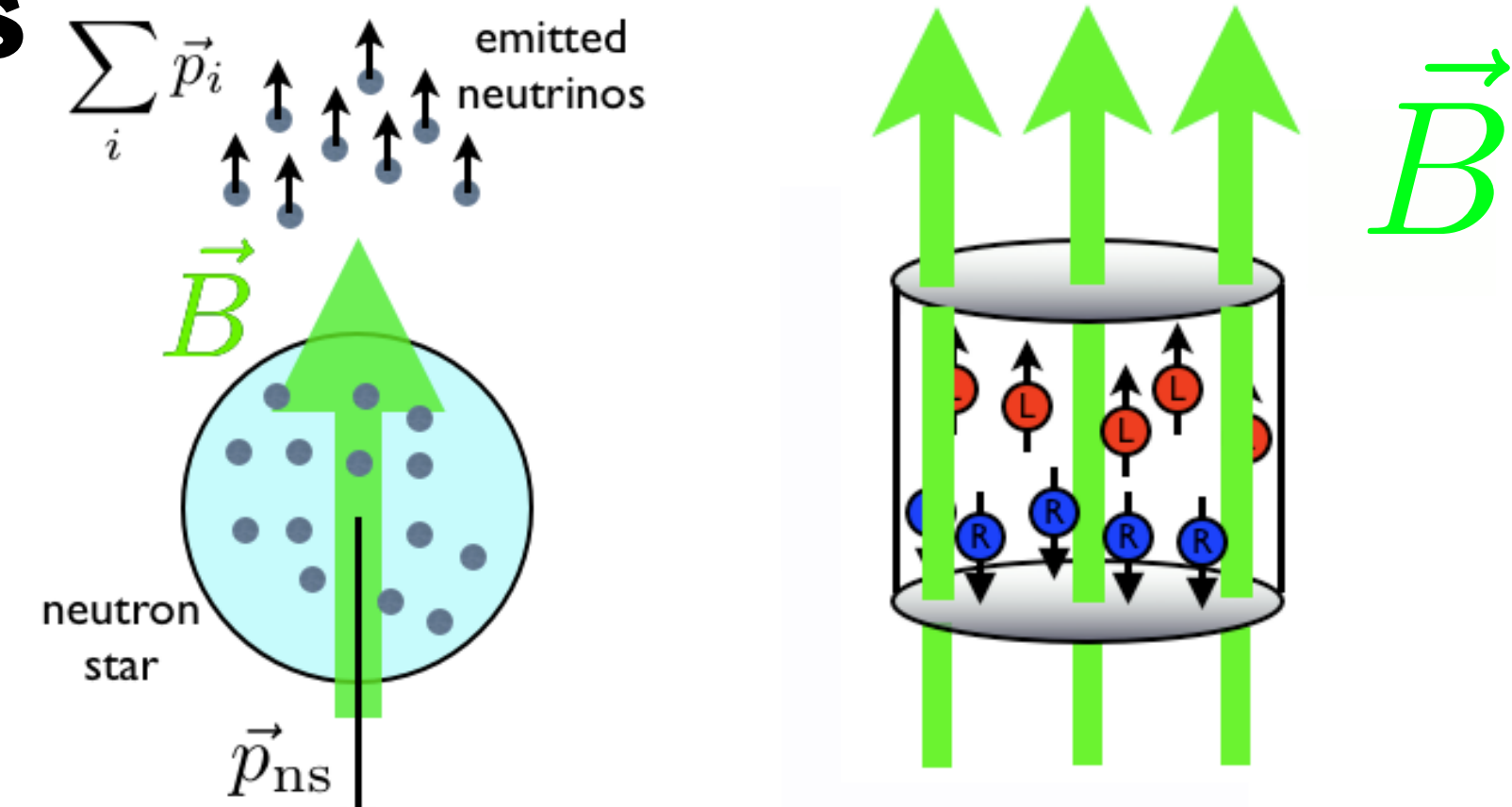
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- ▶ only electron flavor inside 10 km
- ▶ high densities
- ▶ neutrinos trapped! (everything trapped)

This simulation data confirms our naive picture; apply hydrodynamics!

# Our assumptions

- simulation data from previous slide valid [Fischer et al.; PRD (2011)]  
[Wongwathanarat, Janka, Muller; (2012)]
- hydrodynamic approximation applicable
- strong magnetic field exists inside proto-neutron star for about 10 seconds

## Result in kicks from chiral hydrodynamics



# Dirty details: chiral effects in vector/axial currents

see e.g. [Jensen, Kovtun, Ritz; JHEP (2013)]

[Neiman, Oz; JHEP (2010)]

Vector current (e.g. QCD  $U(1)$ )

$$J_V^\mu = \dots + \xi_V \omega^\mu + \xi_{VV} B^\mu + \xi_{VA} B_A^\mu$$

chiral  
magnetic  
effect

Axial current (e.g. QCD axial  $U(1)$ )

$$J_A^\mu = \dots + \xi \omega^\mu + \xi_B B^\mu + \xi_{AA} B_A^\mu$$

chiral  
vortical  
effect

chiral  
separation  
effect

Note:

\* hydrodynamic frame choice

[Ammon, Kaminski et al.; JHEP (2017)]

\* consistent vs covariant

[Landsteiner; APhysPolC (2016) ]

[Landsteiner et al; JHEP (2011) ]



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[Ammon, Kaminski et al.; JHEP (2017)]

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[Landsteiner; APhysPolC (2016) ]

[Landsteiner et al; JHEP (2011) ]

# More details: Chiral effects in various currents

[Neiman, Oz; JHEP (2010)]

correcting and generalizing [Son, Surowka; PRL (2009)]

More than one current

$$\langle \partial_\mu J_a^\mu \rangle = \frac{1}{8} C_{abc} \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu}^b F_{\rho\sigma}^c$$

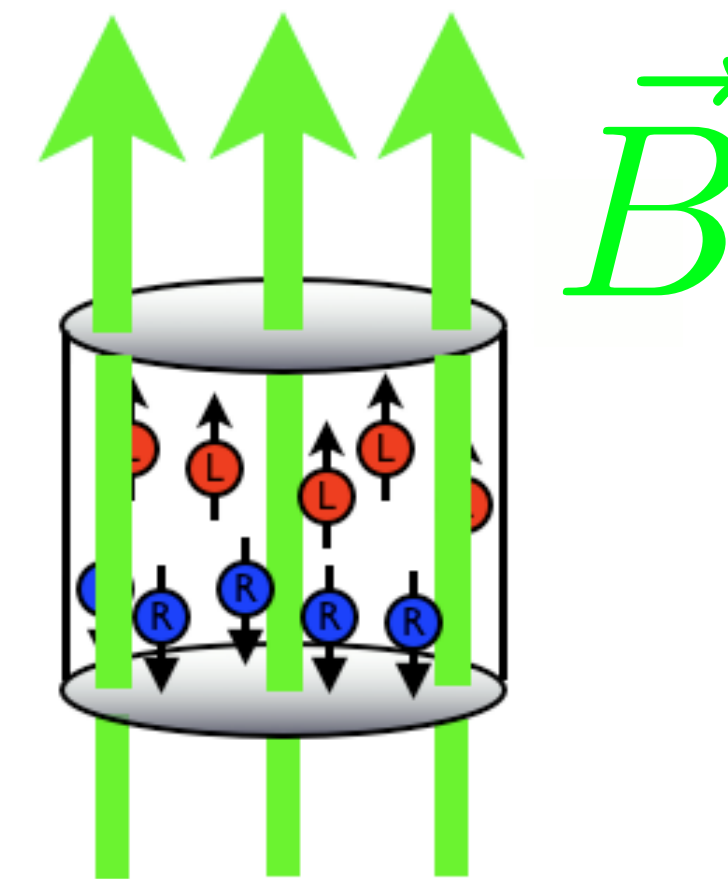
Constitutive relation:

$$J_a^\mu = n_a u^\mu + \sigma_a^b V_b^\mu + \sigma_a^V \omega^\mu + \sigma_{ab}^B B^{b\mu} + \mathcal{O}(\partial^2)$$

Chiral magnetic conductivity:

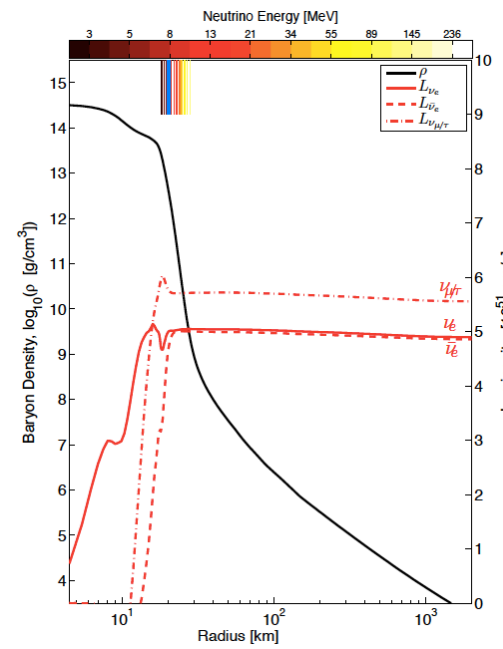
$$\sigma_{ab}^B = C_{abc} \mu^c$$

various charges  
(e.g. lepton number,  
electromagnetic charge, ...)

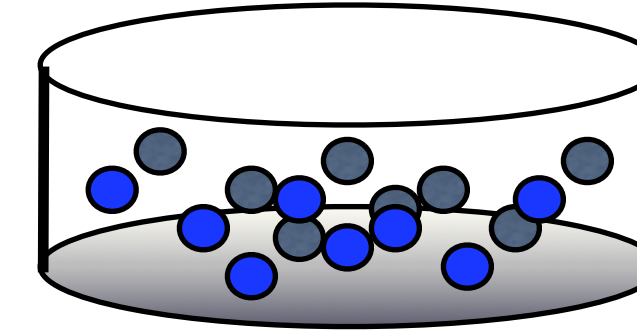


# Relevant currents in neutron stars

[Kaminski, Uhlemann, Schaffner-Bielich, Bleicher; PLB (2016)]



A bucket full of electrons and electron neutrinos with short mean free path



$$B = 0.1 \text{ MeV}^2$$

$$\mu^\ell \approx 300 \text{ MeV}$$

Microscopic (standard model) currents: lepton/axial/EM:

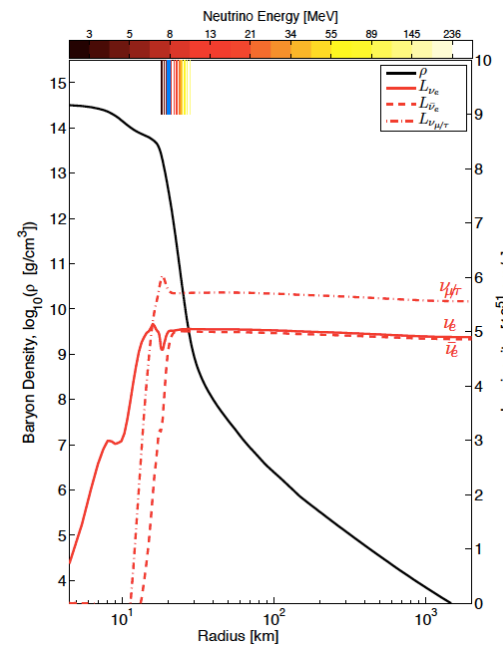
$$J_\ell^\mu = \bar{e}_L \gamma^\mu e_L + \bar{e}_R \gamma^\mu e_R + \bar{\nu} \gamma^\mu \nu \quad \text{neutrinos and electrons}$$

$$J_{\ell 5}^\mu = \bar{e}_L \gamma^\mu e_L - \bar{e}_R \gamma^\mu e_R + \bar{\nu} \gamma^\mu \nu \quad \text{“inseparable”}$$

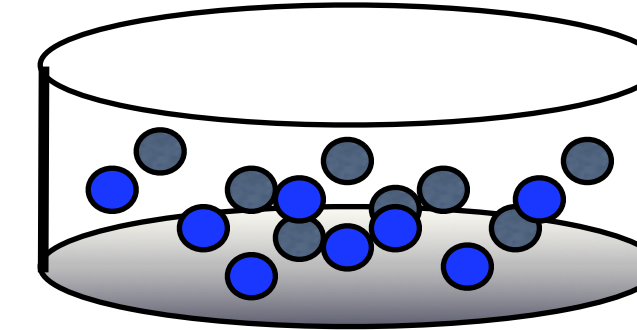
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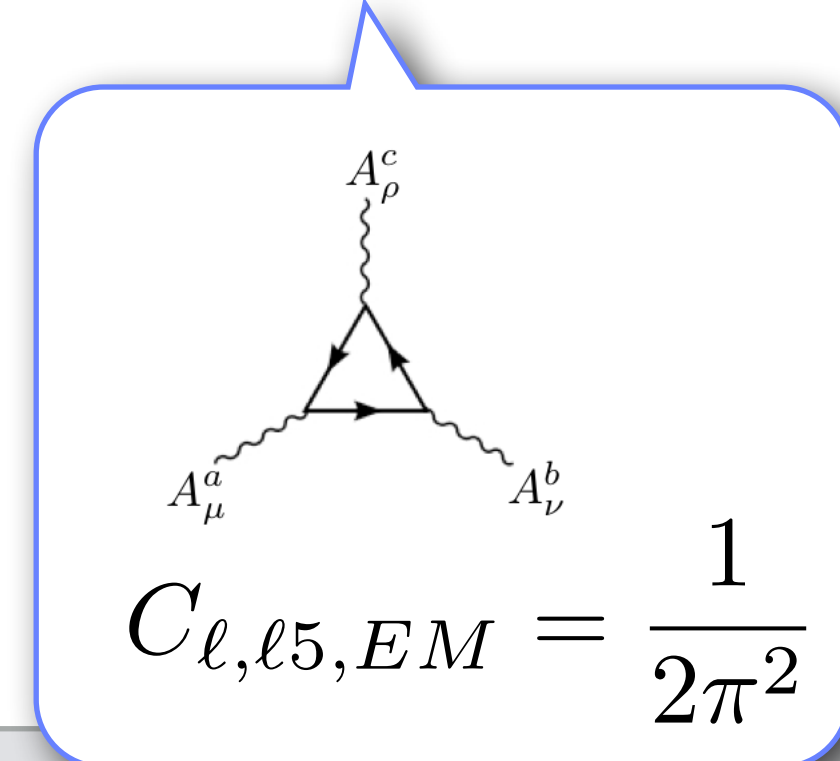
$$J_{EM}^\mu = \bar{e}_L \gamma^\mu e_L + \bar{e}_R \gamma^\mu e_R$$

“proto  
neutron  
star”  
“crust”

Macroscopic (hydrodynamic) description:  $\sigma_{ab}^B = C_{abc} \mu^c$

$$J_\ell \sim \sigma_{\ell,EM}^B B \approx C \mu^{\ell 5} B$$

$$J_{\ell 5} \sim \sigma_{\ell 5,EM}^B B \approx C \mu^\ell B$$

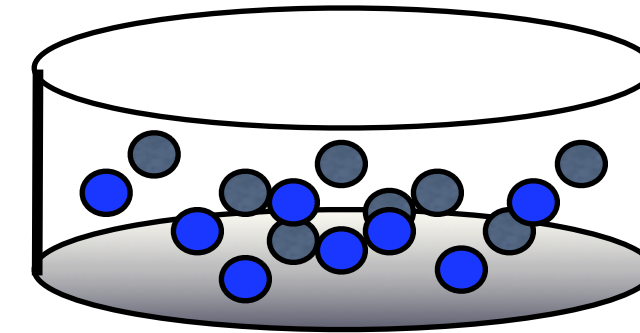




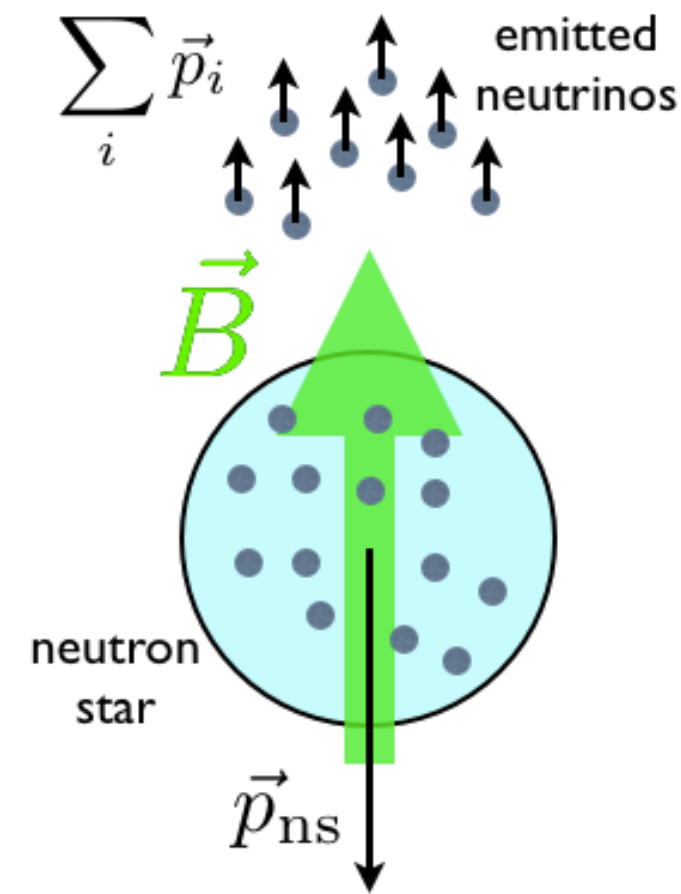
# Estimate of the neutron star kick

[Kaminski, Uhlemann, Schaffner-Bielich, Bleicher; PLB (2016)]

A bucket full of electrons and  
electron neutrinos with short  
mean free path



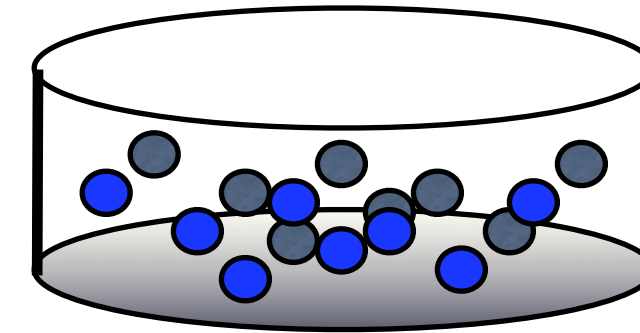
$$B = 0.1 \text{ MeV}^2$$
$$\mu^{\ell} \approx 300 \text{ MeV}$$
$$\langle p_{\nu} \rangle \approx \mu^{\ell}.$$



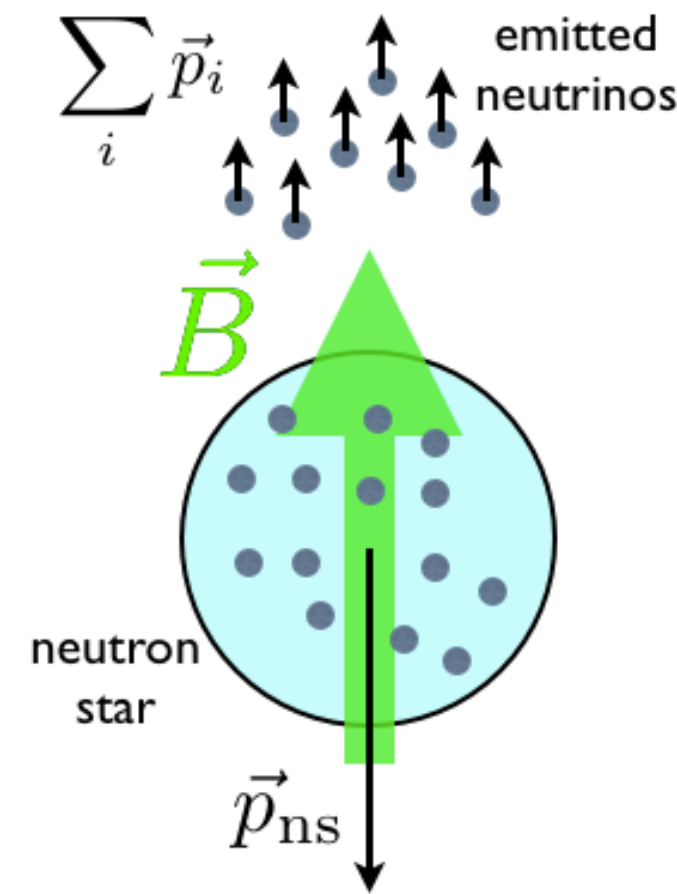
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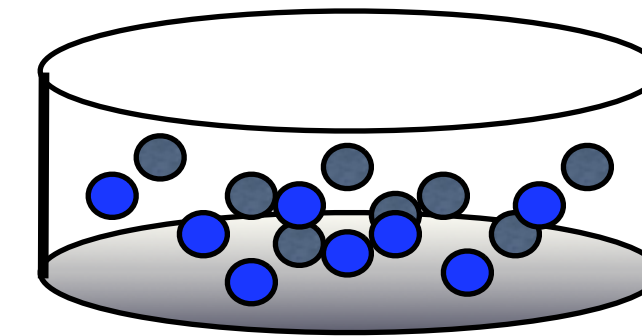
Chiral conductivity:

$$\sigma_{\ell 5, EM}^B = C_{\ell, \ell 5, EM} \mu^\ell = \frac{1}{2\pi^2} \mu^\ell$$

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[Kaminski, Uhlemann, Schaffner-Bielich, Bleicher; PLB (2016)]

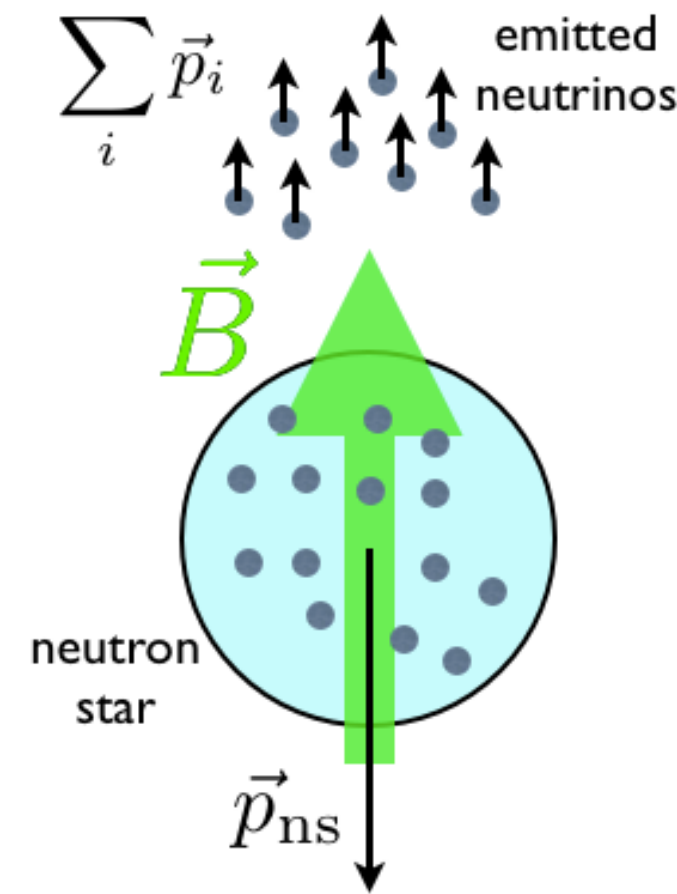
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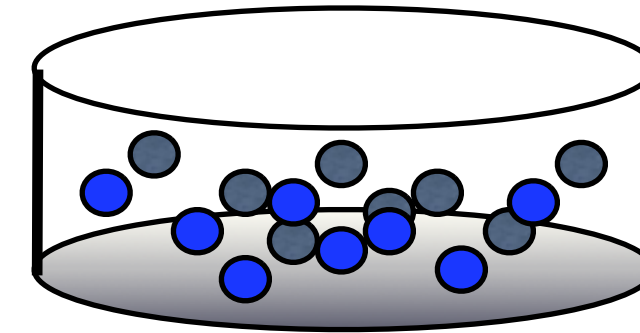
Axial lepton current:

$$\vec{J}_{\ell 5} = C \mu^\ell \vec{B} \approx \vec{e}_B \cdot 1 \text{ MeV}^3$$

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[Kaminski, Uhlemann, Schaffner-Bielich, Bleicher; PLB (2016)]

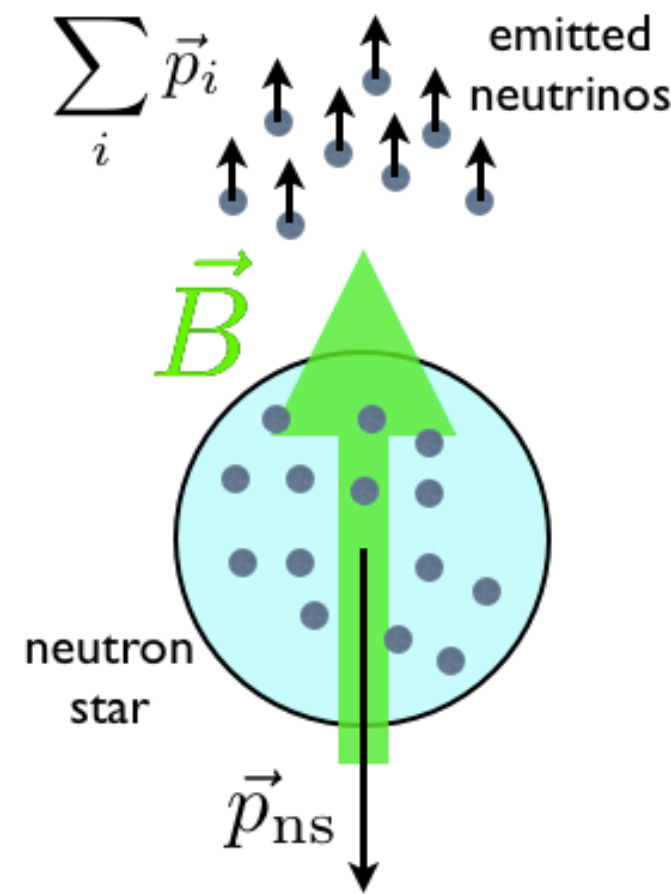
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Particle flux and momentum transfer:

$$\dot{N}_\nu = |\vec{J}| A_{\text{surface}}$$

$$\approx 10^{54} / \text{s}$$

$$\Delta P_{\text{NS}} = \Delta t \dot{N}_\nu \langle p_\nu \rangle$$

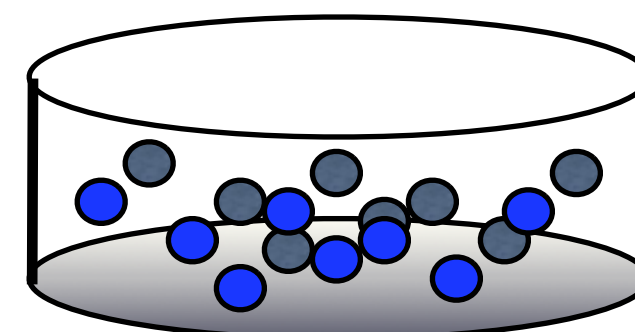
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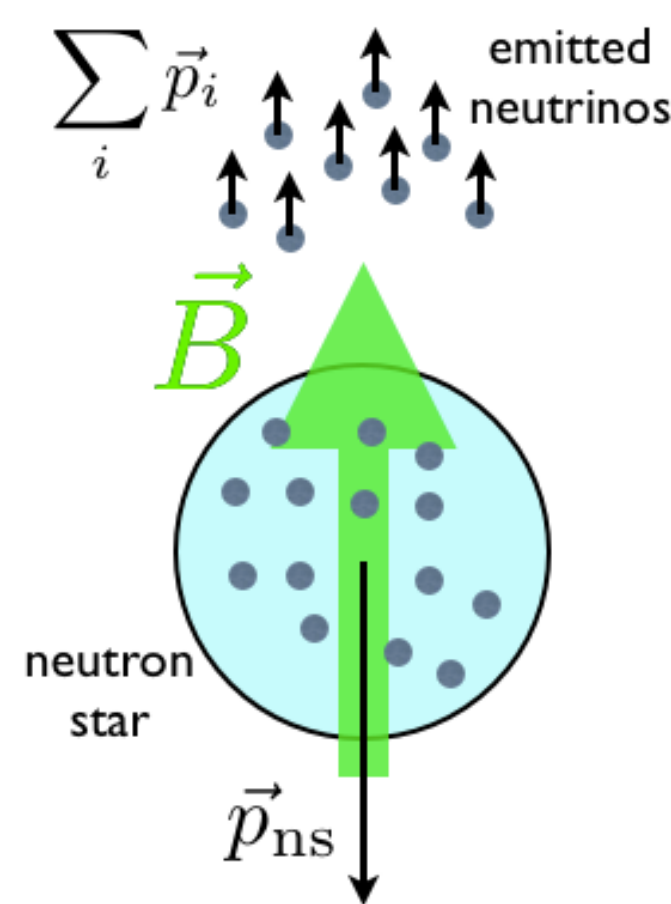
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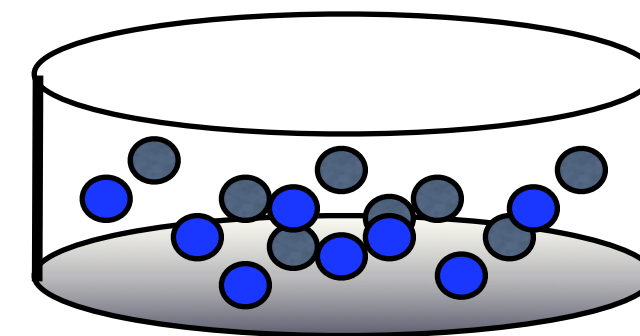
$$\approx 10^{54} / \text{s} \quad \Delta t \approx 10 \text{ s}$$

Neutron star mass:  $m_{\text{NS}} = 3 \cdot 10^{30} \text{ kg}$

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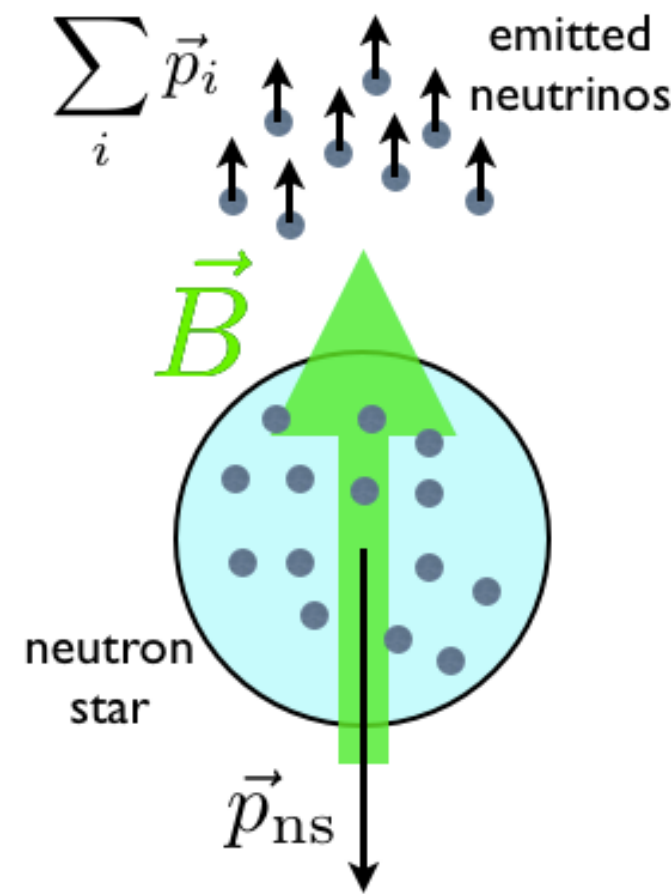
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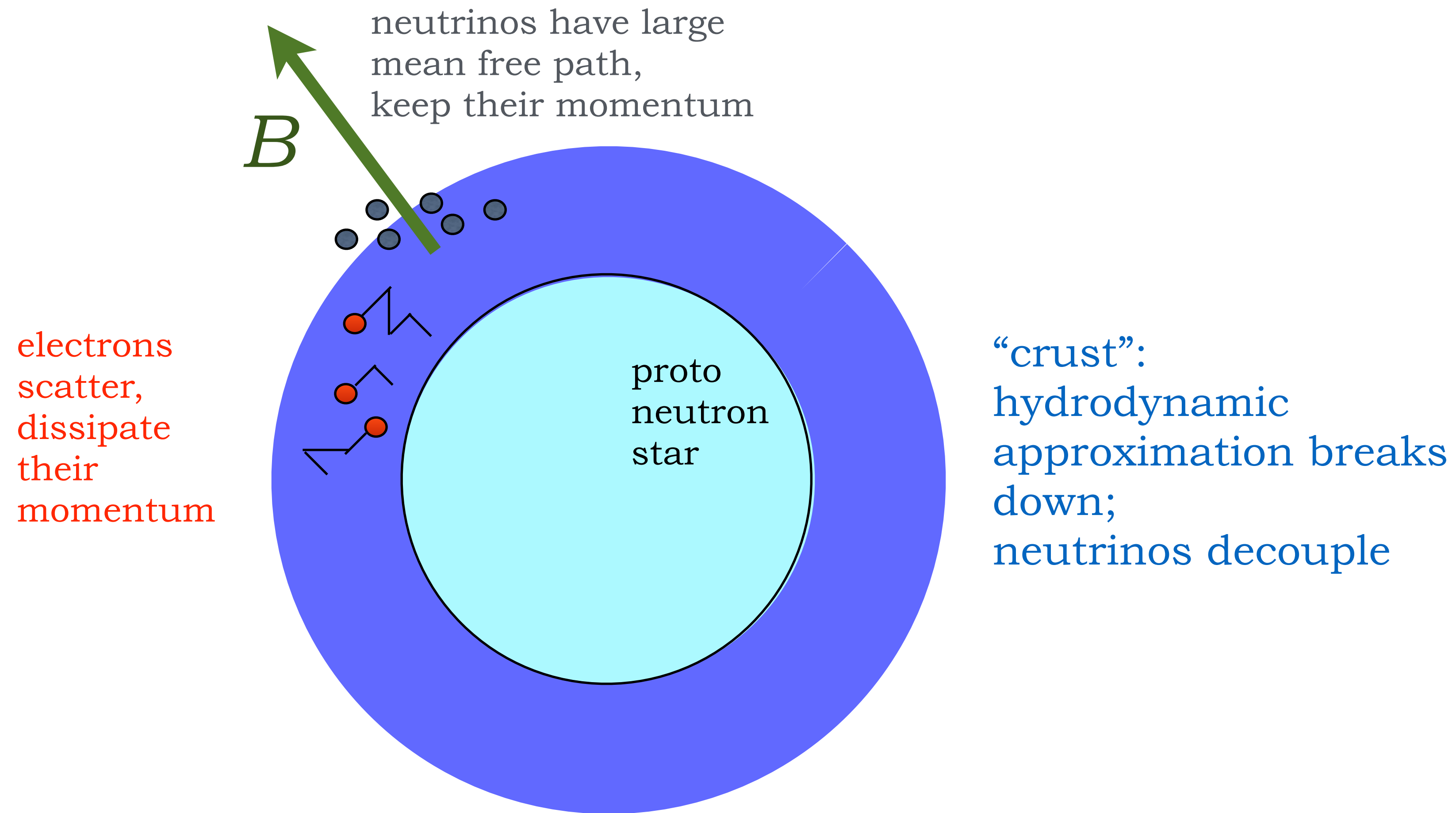
$$\approx 10^{54} / \text{s} \quad \Delta t \approx 10 \text{ s}$$

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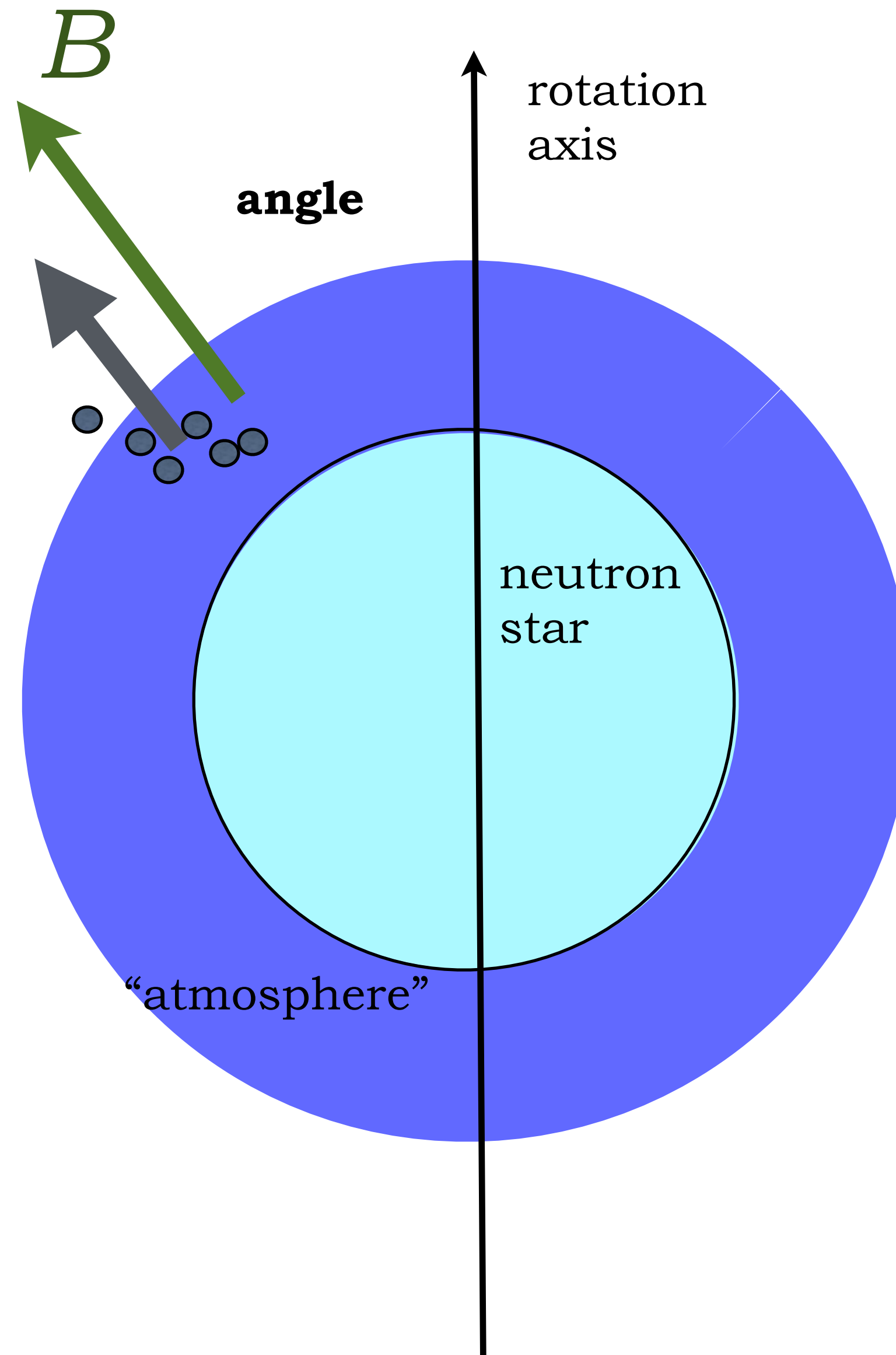
Kick velocity agrees with observations:

$$\Rightarrow v_{\text{kick}} \approx 1000 \frac{\text{km}}{\text{s}}$$

# Filtering at the “crust”



# Observable signal?



Prediction: Kick magnitude depends on angle between rotation axis and internal magnetic field axis.

For fast spinning neutron stars, kick directed along rotation axis.

Data on rotation/ $B$ /kick axes:

<http://adsabs.harvard.edu/abs/2012ApJ...755..141B>

<http://adsabs.harvard.edu/abs/2007ApJ...670..635W>

<http://adsabs.harvard.edu/abs/1988srin.conf...65W>

<http://adsabs.harvard.edu/abs/2007ApJ...656..399W>



# CVE neutron star kicks

$$\sigma_a^V = \frac{1}{2} C_{abc} \mu^b \mu^c - \beta_a T^2, \quad \sigma_{ab}^B = C_{abc} \mu^c$$

$$j^\mu = n u^\mu + \sigma E^\mu + \sigma^B B^\mu + \sigma^V \omega^\mu + \dots$$

“chiral vortical  
conductivity”

[Erdmenger, Haack, Kaminski,  
Yarom; JHEP (2008)]

[Banerjee et al.; JHEP (2011)]

CVE kick possible but suppressed by orders of magnitude

$$\omega \approx 10^{-17} \text{ MeV}$$

$$B \sim 10^{12} \text{ G} \approx 0.1 \text{ MeV}^2$$

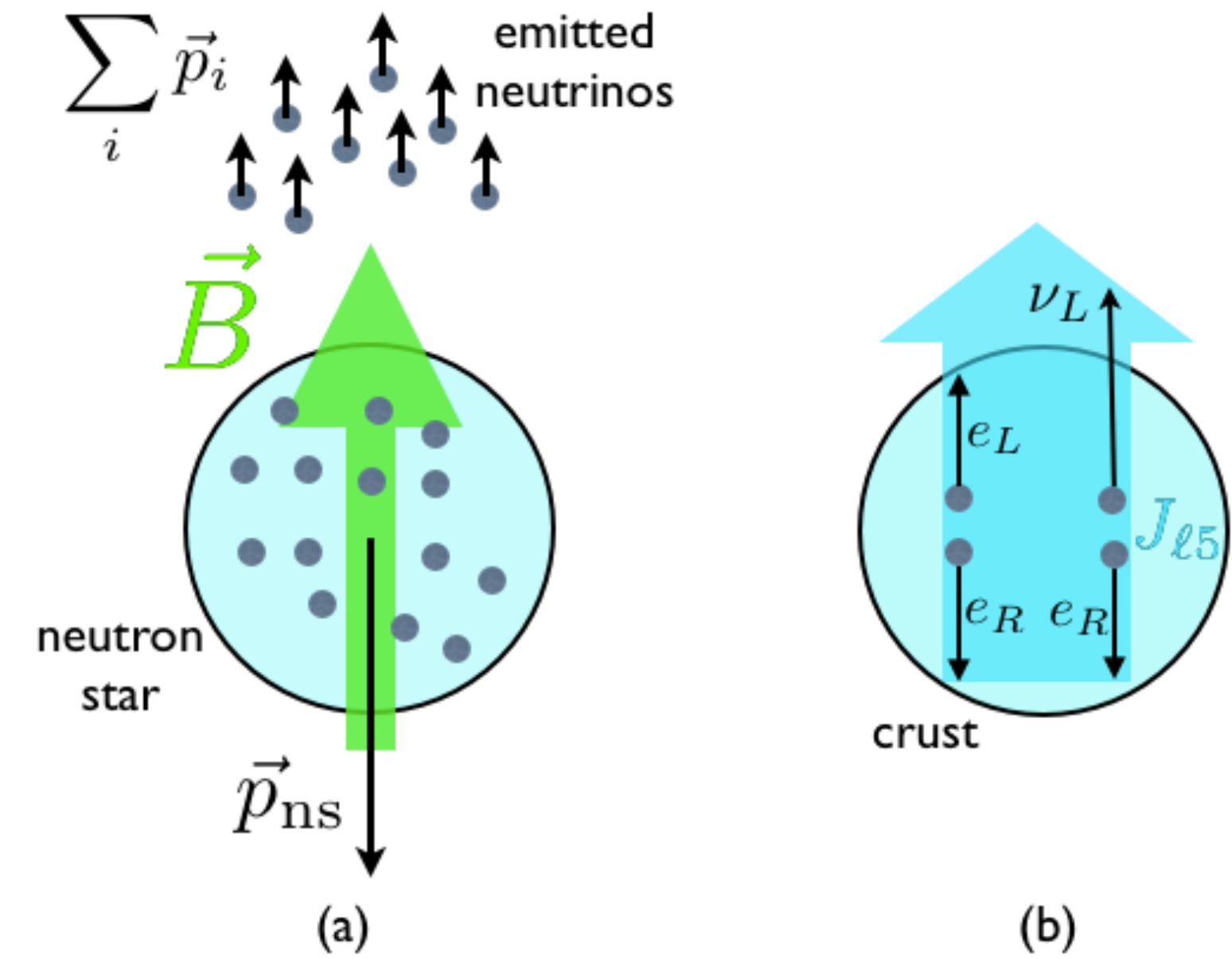
[Kaminski, Uhlemann, Schaffner-Bielich, Bleicher; PLB (2016)]

stronger CVE kick possible due to formation of ergo sphere

[Shaverin, Yarom; arXiv (2014)]

see also [Shaverin; arXiv (2018)]

# Summary



- Yes, standard (first order) **CME (maybe CVE) can lead to neutron star kicks**

# Two categories of kick mechanisms

Something has to cause an asymmetry in the momentum distribution.

## 1.) asymmetric supernova explosion

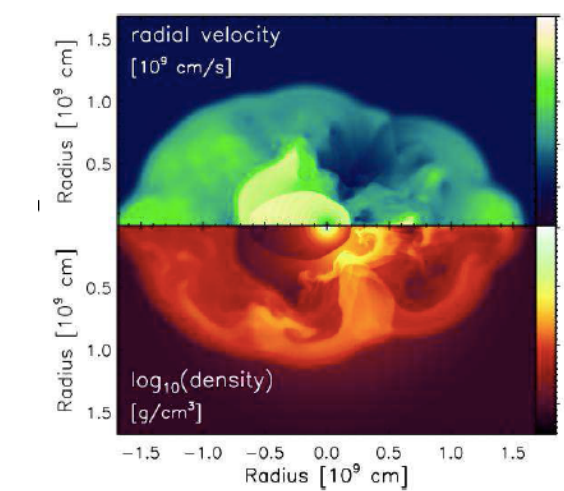
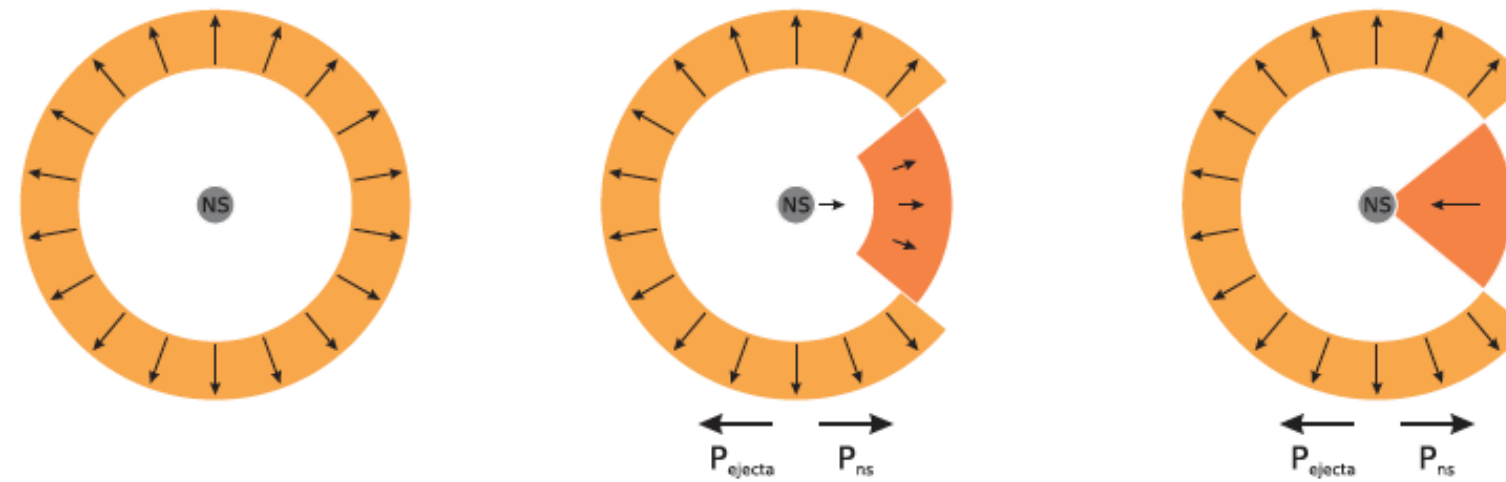
- ▶ kicks of about 1000 km/s
- ▶ random seed perturbations plus hydro instabilities (SASI)
- ▶ hydro model, neutrino transport, boundary cond's
- ▶ timescale: ~5 seconds

[Scheck, Kifonidis, Janka, Muller; (2003)]

[Wongwathanarat, Janka, Muller; (2010)]

[Wongwathanarat, Janka, Muller; (2012)]

[Blondin et al;  
'02)]



## 2.) asymmetric emission of matter

- ▶ neutrino emission [Vilenkin (1978)]
- ▶ beyond the standard model [Fuller, Kusenko, Mocioiu, Pascoli (2003)]
- ▶ neutrino kicks, nucl-th [Sagert, Schaffner-Bielich (2007)]

# Problems with previous kick mechanisms

ad 1.) asymmetric supernova explosion

- ▶ numerical analysis, no analytic understanding
- ▶ no magnetic dipole fields, no chiral hydro
- ▶ instabilities disturbed by other hydro effects?

ad 2.) asymmetric emission of matter

- ▶ neutrino kick too small, neutrinos “too cold”
- ▶ microscopic asymmetry washed out *[Kusenko, Segre, Vilenkin (1998)]*
- ▶ need physics beyond the standard model

*[Fuller, Kusenko, Mocioiu, Pascoli (2003)]*

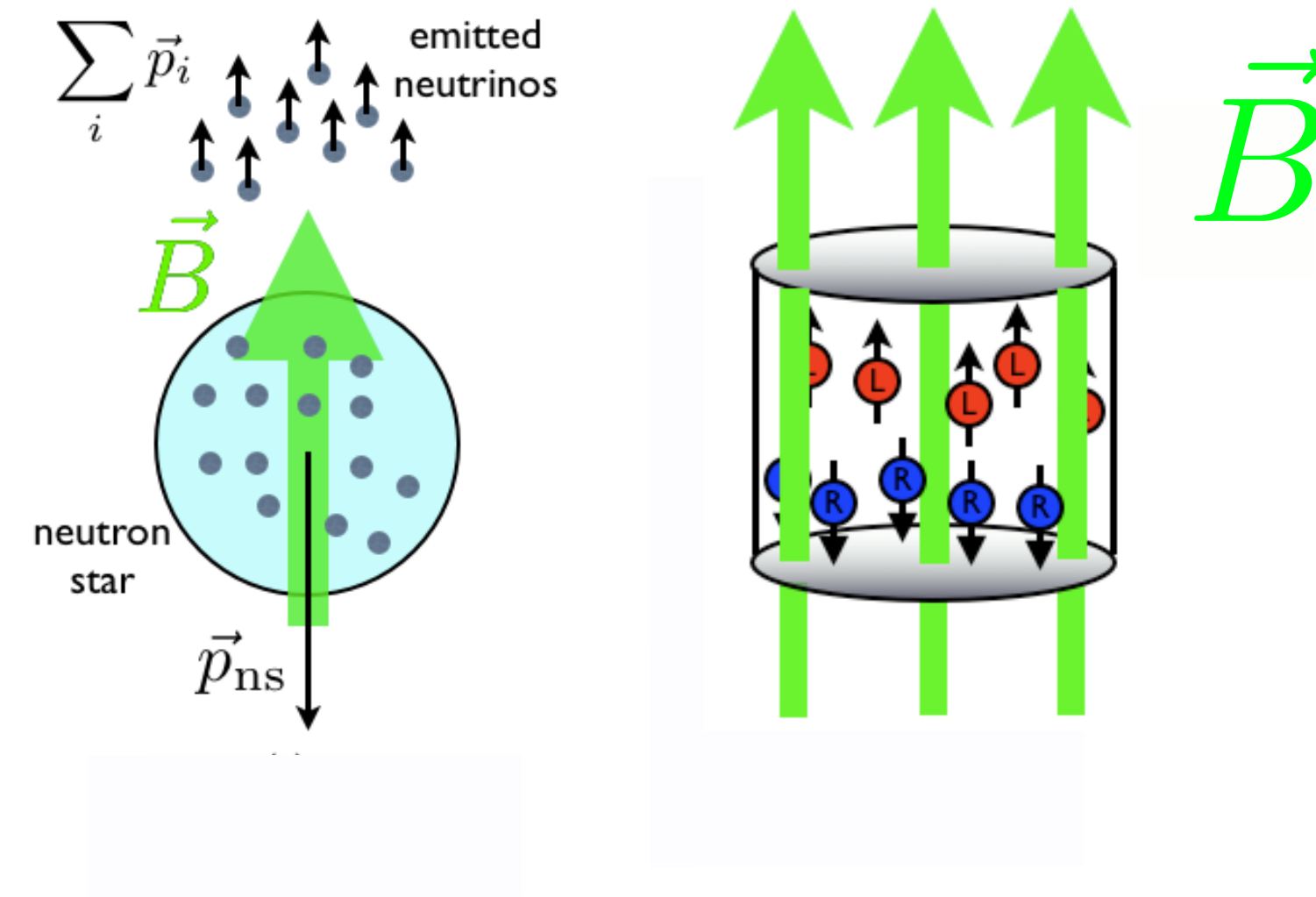
Our anomalous hydrodynamic formalism  
addresses and overcomes these problems.



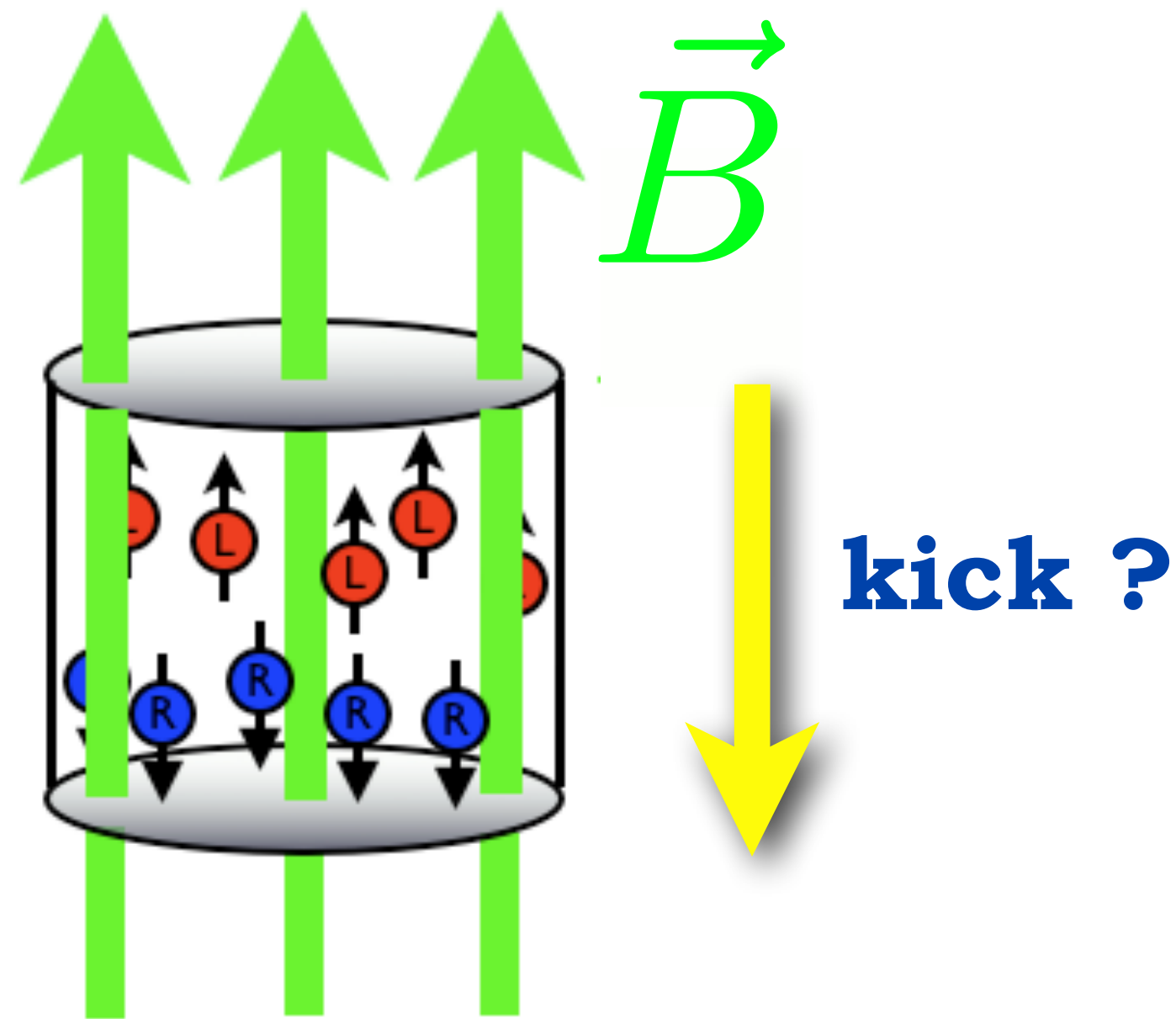
# APPENDIX

# Physics behind the kick

thermal energy of neutrinos is transformed to kinetic energy of the neutron star by chiral hydrodynamic process



# Chiral hydrodynamics & neutron star kicks



*hydrodynamics:* fluids with left-handed and right-handed particles produce a **current** along magnetic field

*e.g. right/left-handed electrons, neutrinos, ...*

*theory: [Son, Surowka; PRL (2009)]  
[Landsteiner]*

*experiment: [Huang et al; PRX (2015)]*



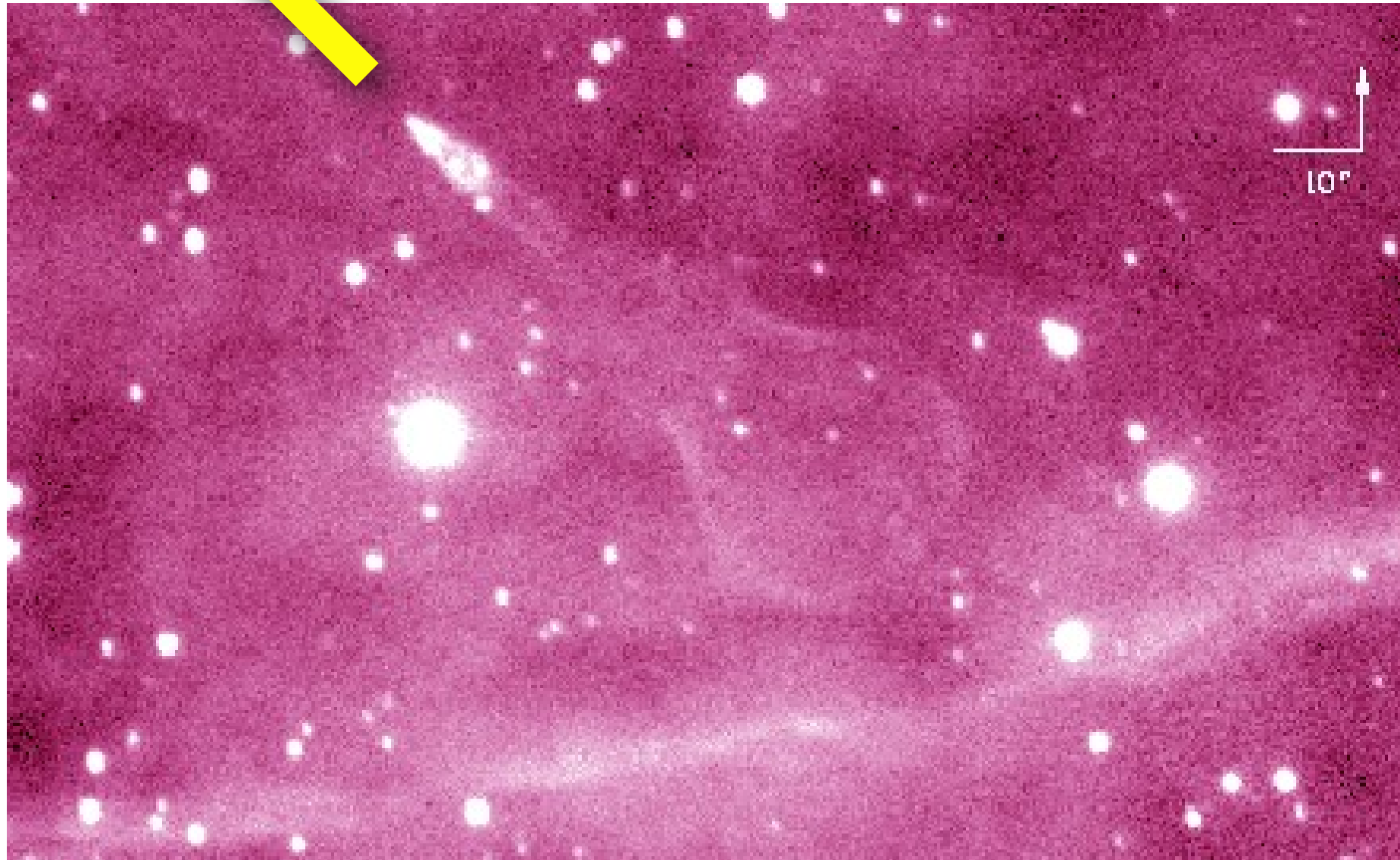
*observation:* neutron stars undergo a large momentum change (a kick)

*[Chatterjee et al.; Astrophys. J (2005)]*

Can chiral hydrodynamics be relevant for neutron star kicks?

# Kick observations

**kick**



*[Chatterjee et al.; Astrophys. J (2005)]*

*Nebula discovered: [Cordes et al; Nature (1993)]*



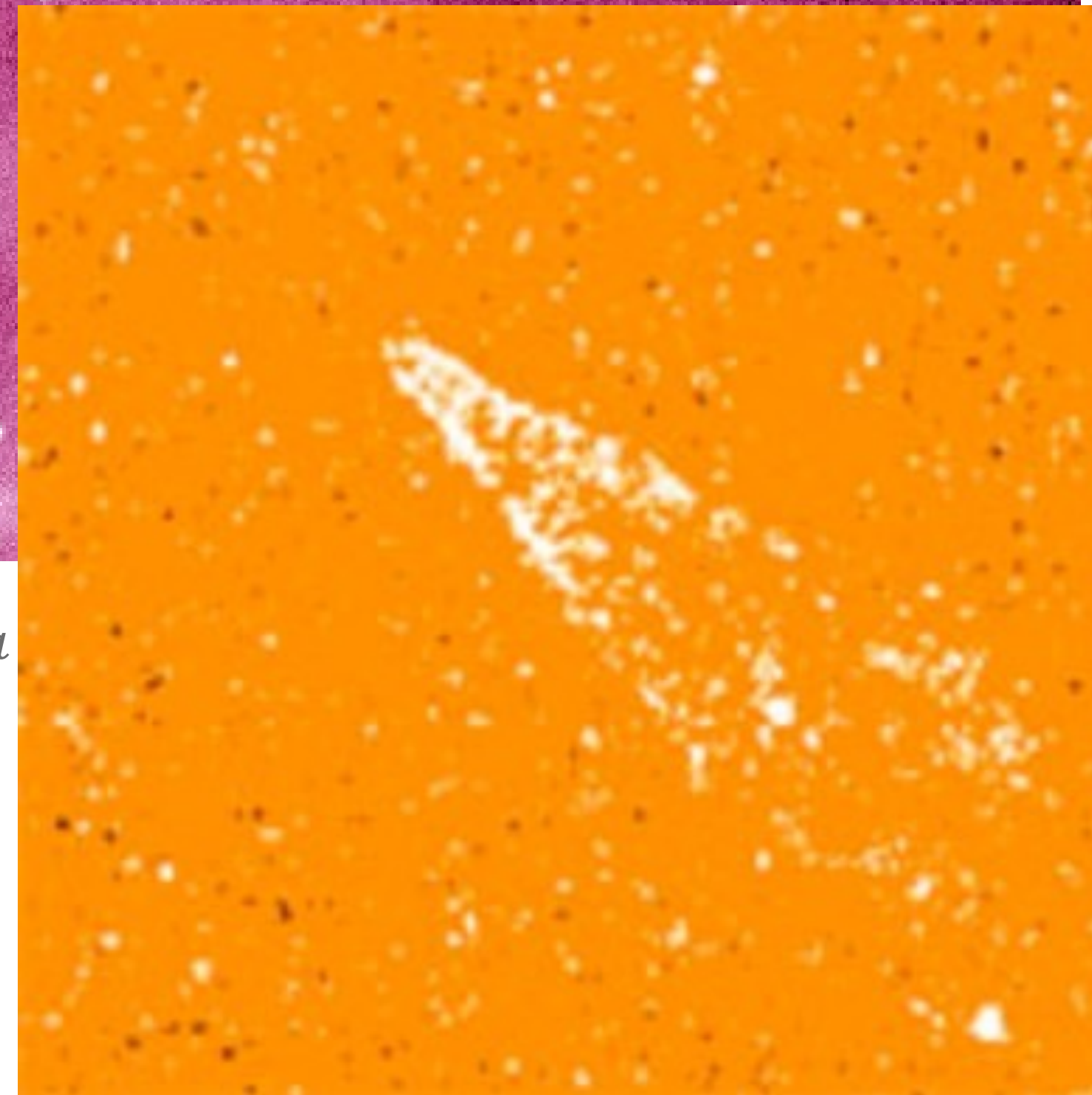
# Kick observations



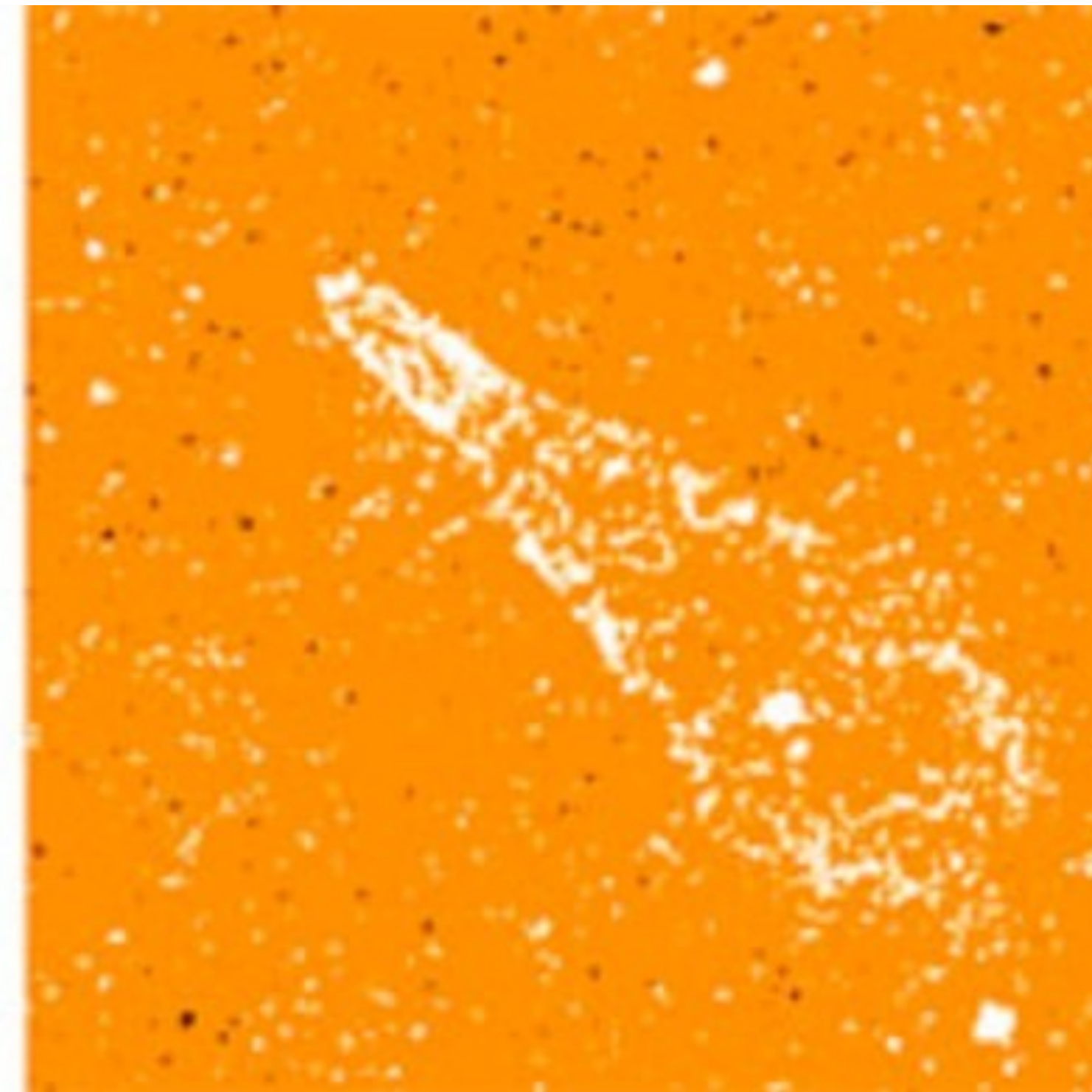
[Chatterjee et al.; *Astrophys. J* (2005)]

[Hubble Space Telescope (NASA/ESA),  
Shami Chatterjee, Cornell University]

*Nebula*



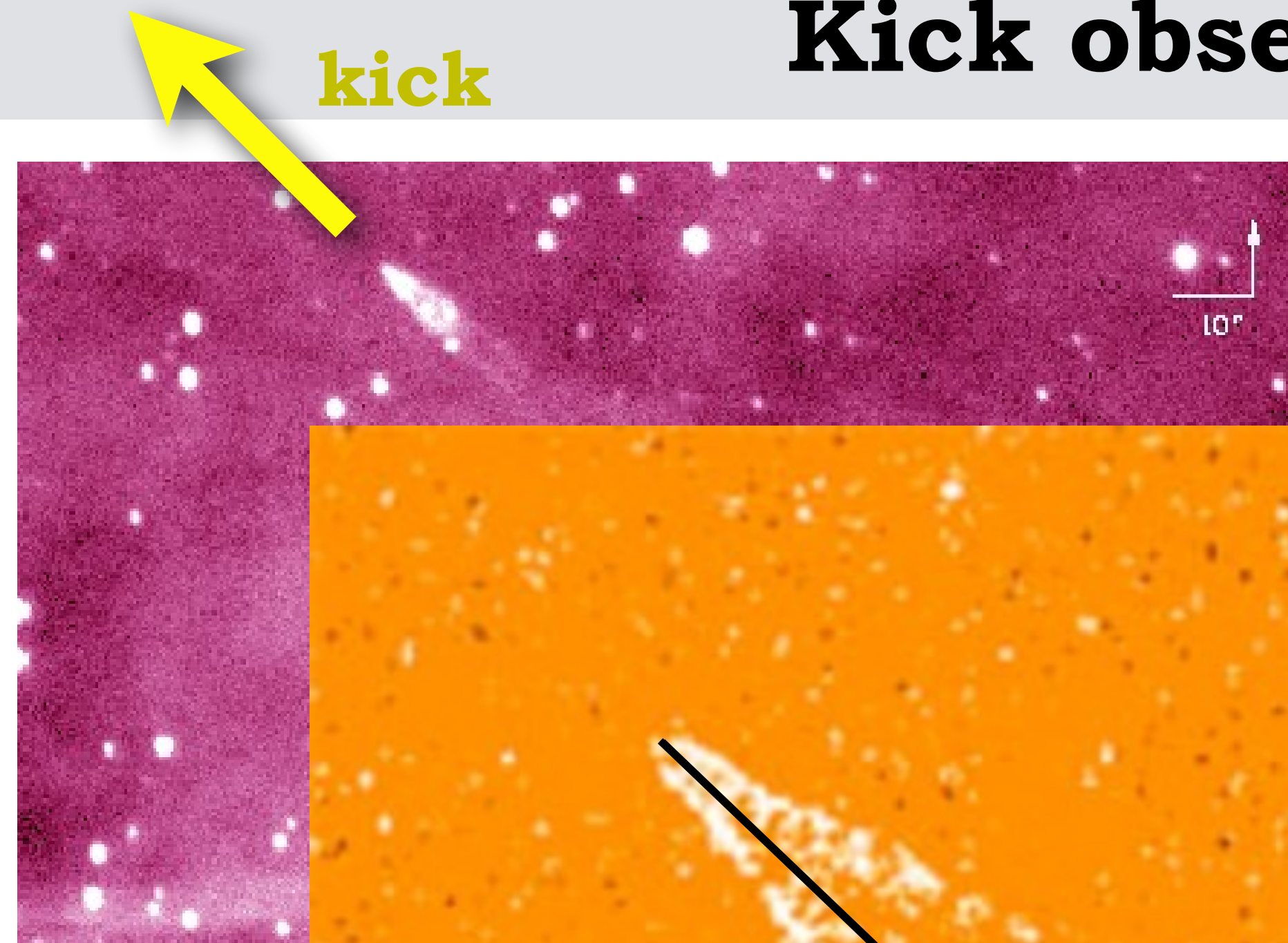
December 1994



December 2001



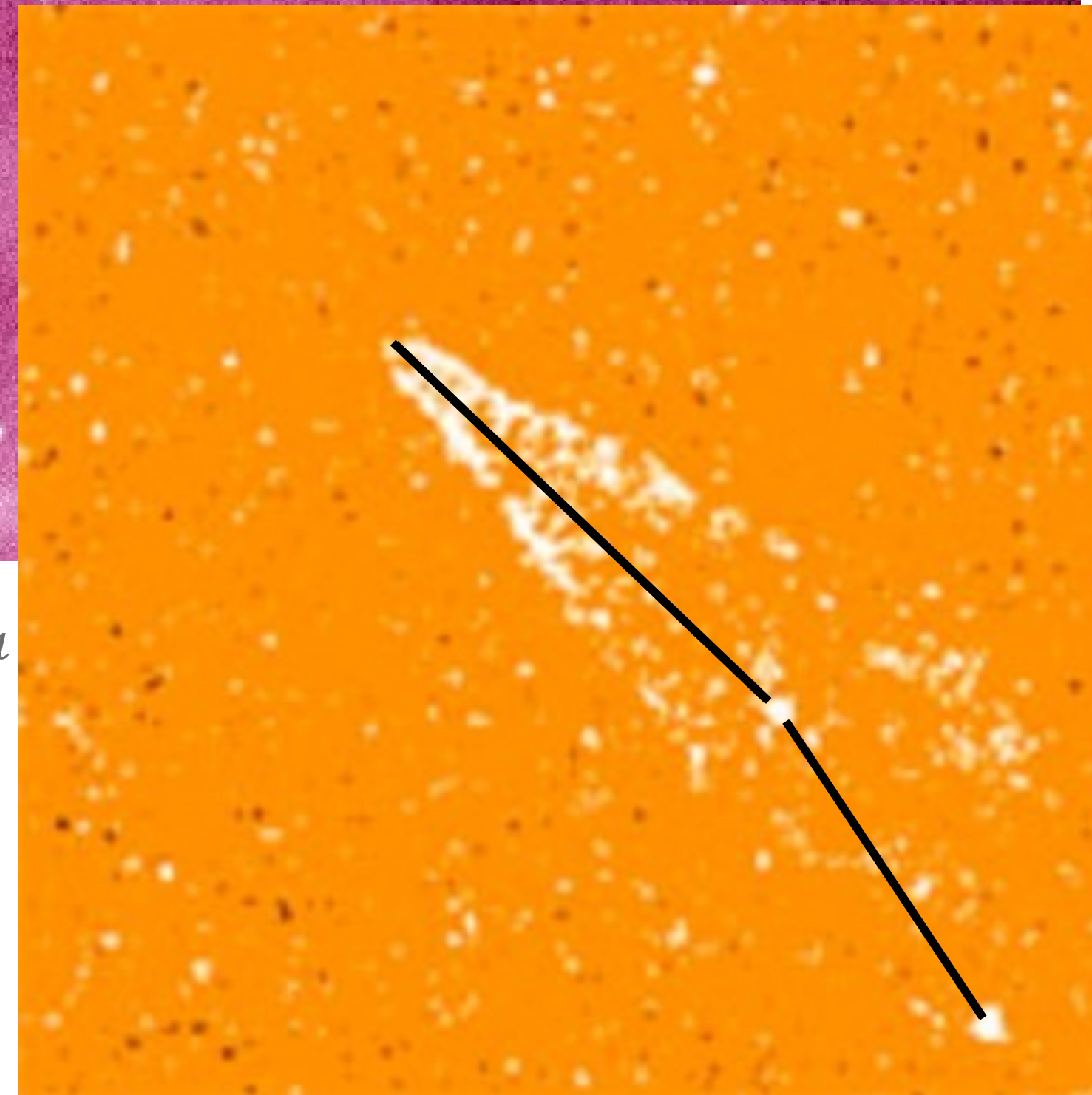
# Kick observations



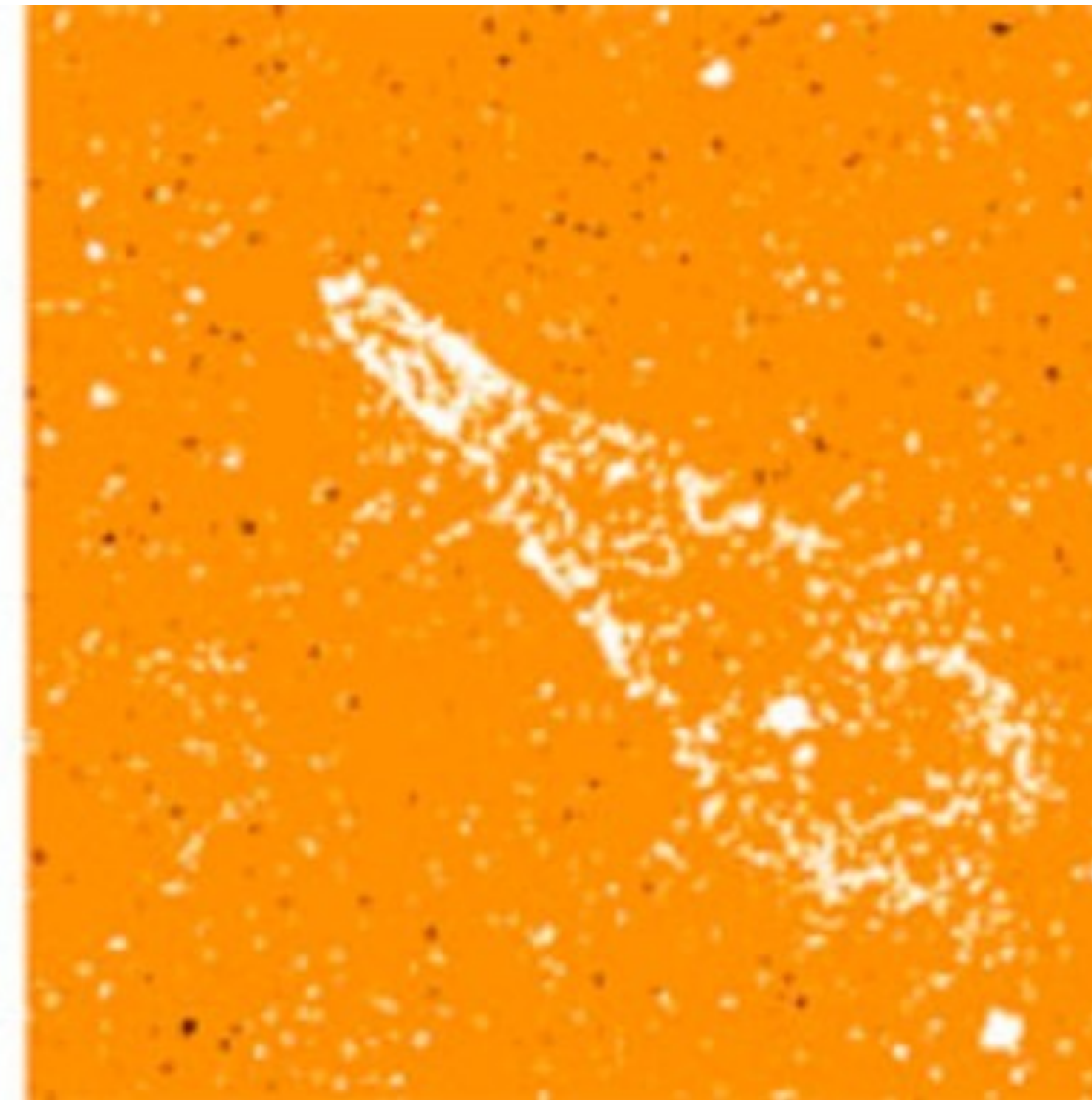
[Chatterjee et al.; *Astrophys. J* (2005)]

[Hubble Space Telescope (NASA/ESA),  
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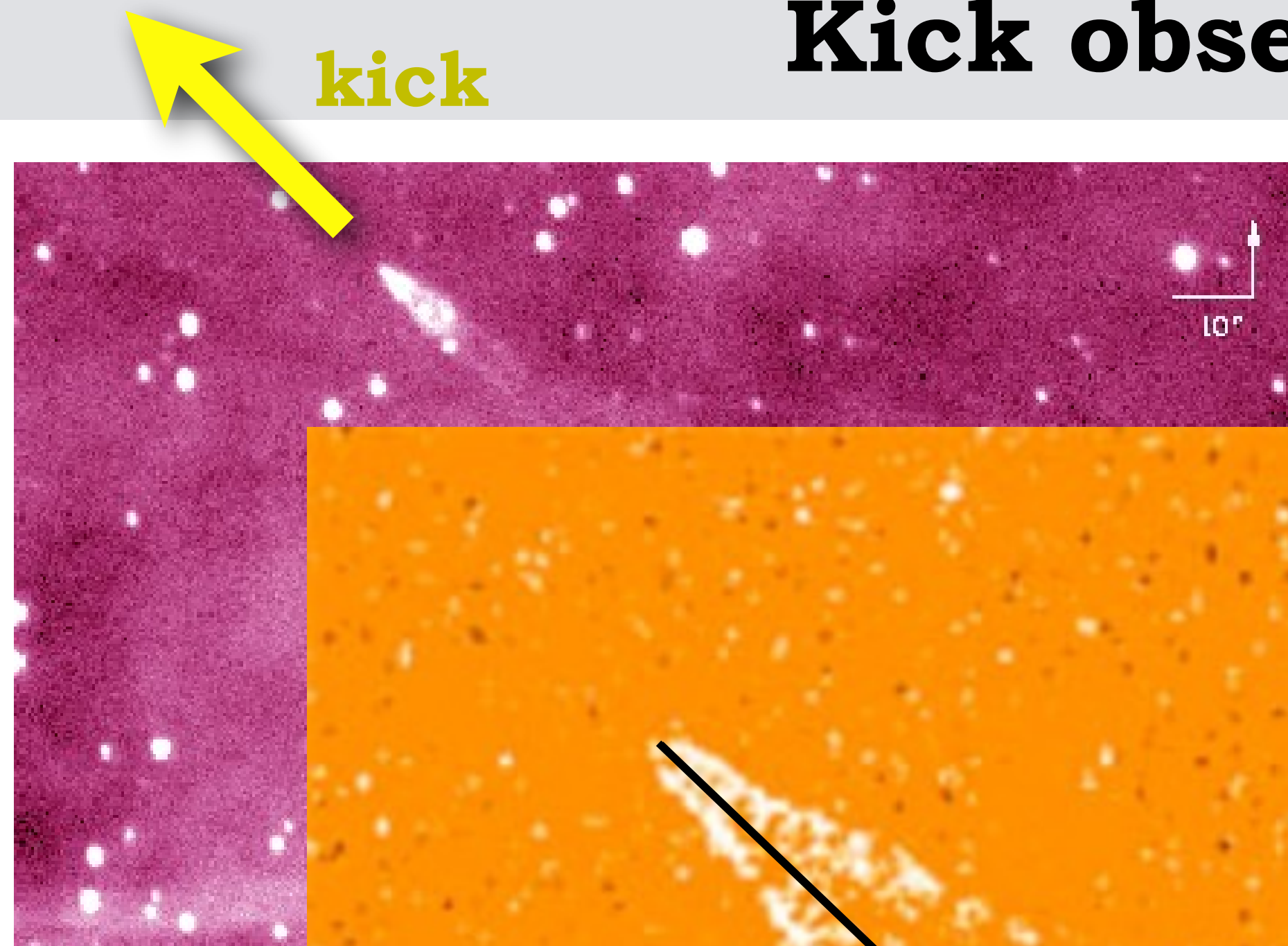
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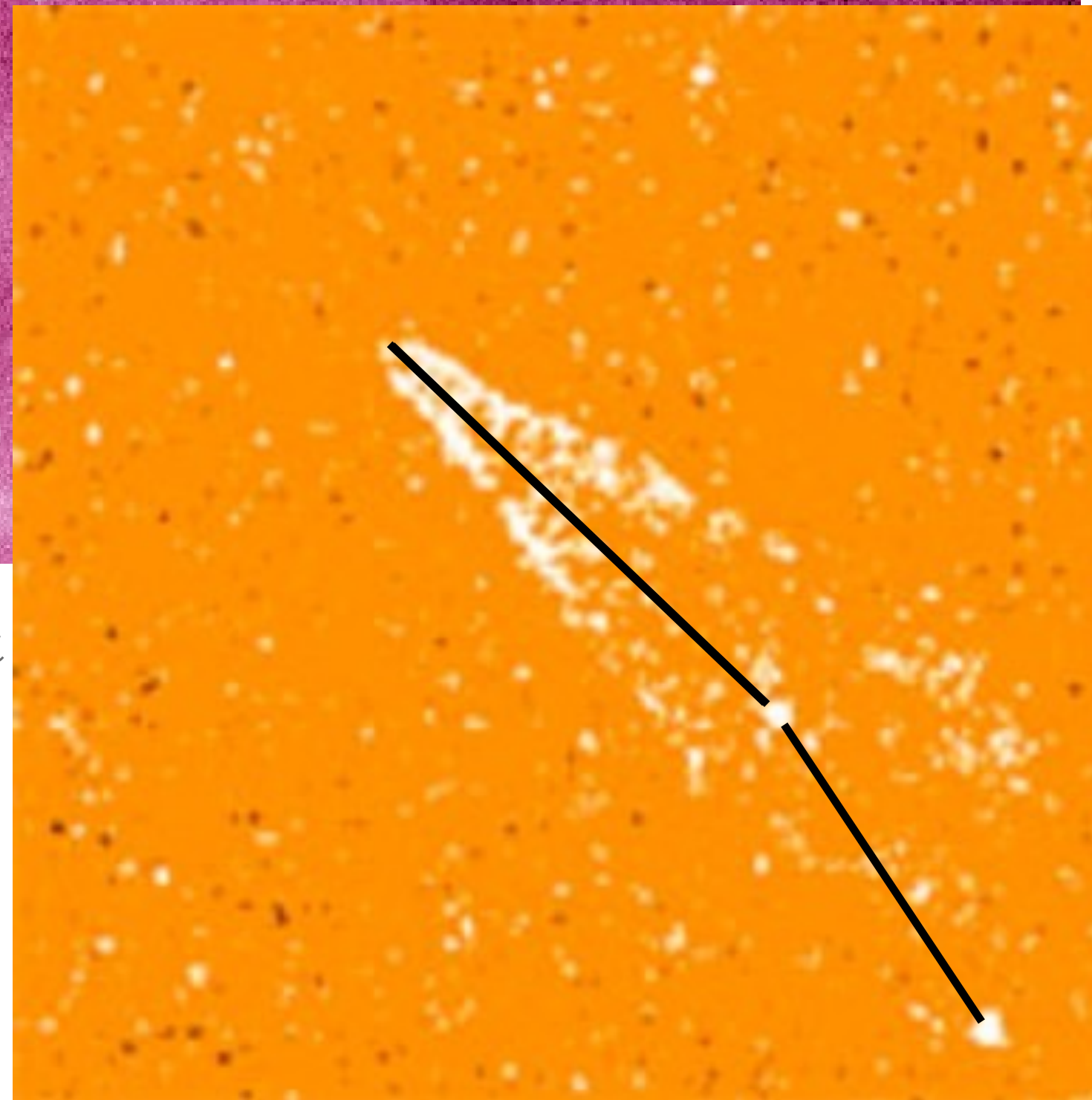
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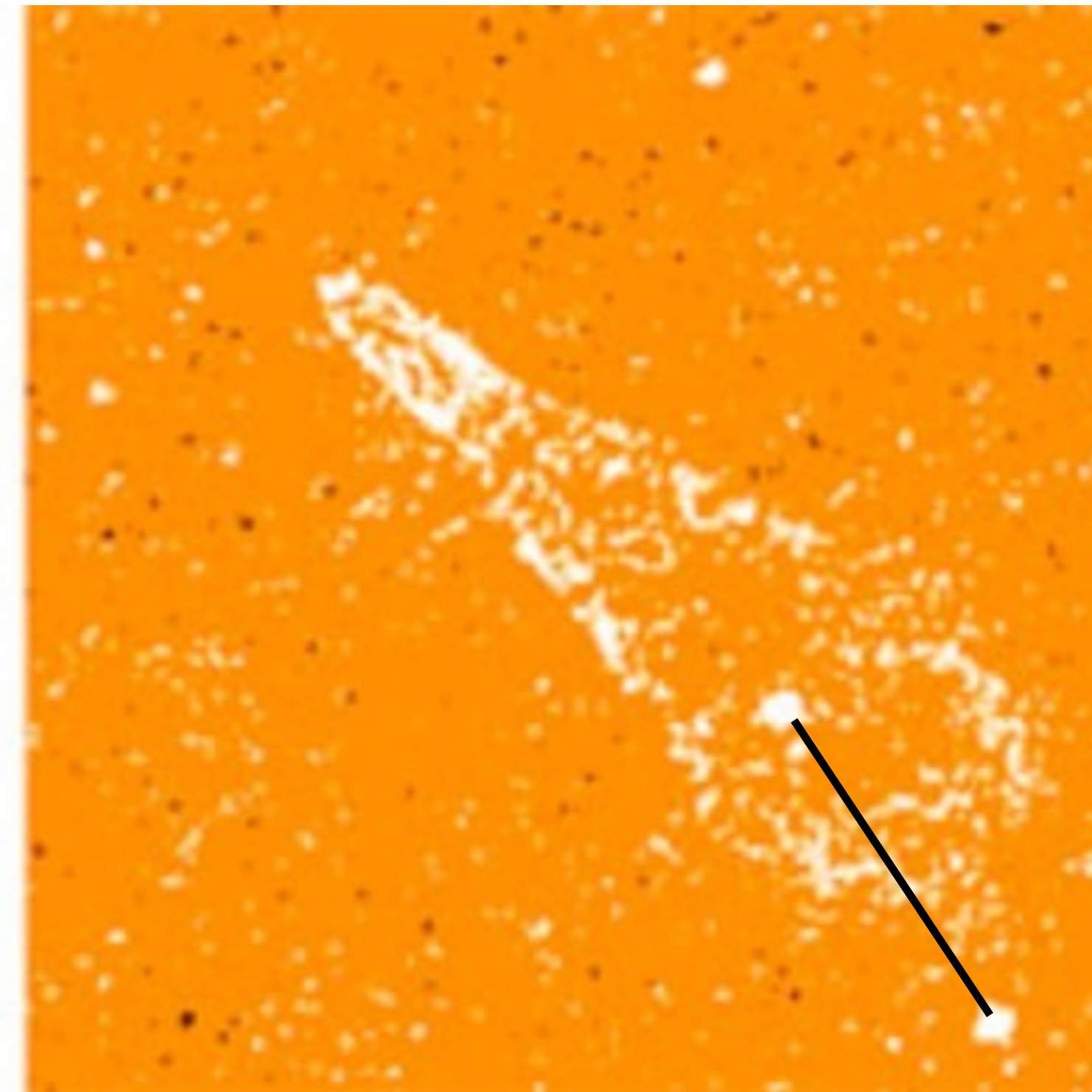
*Nebula*

[Chatterjee et al.; *Astrophys. J* (2005)]

[Hubble Space Telescope (NASA/ESA),  
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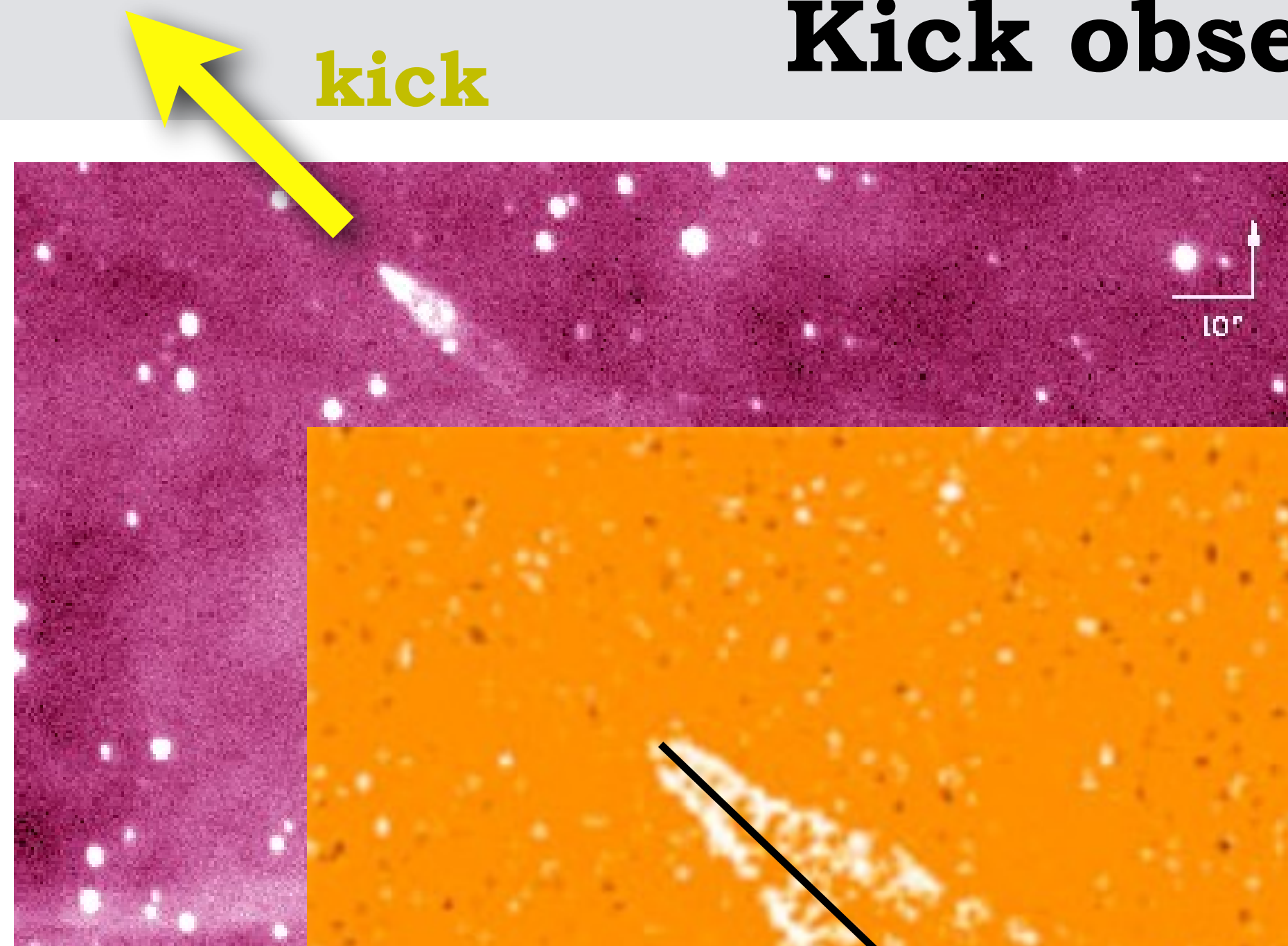
December 1994



December 2001



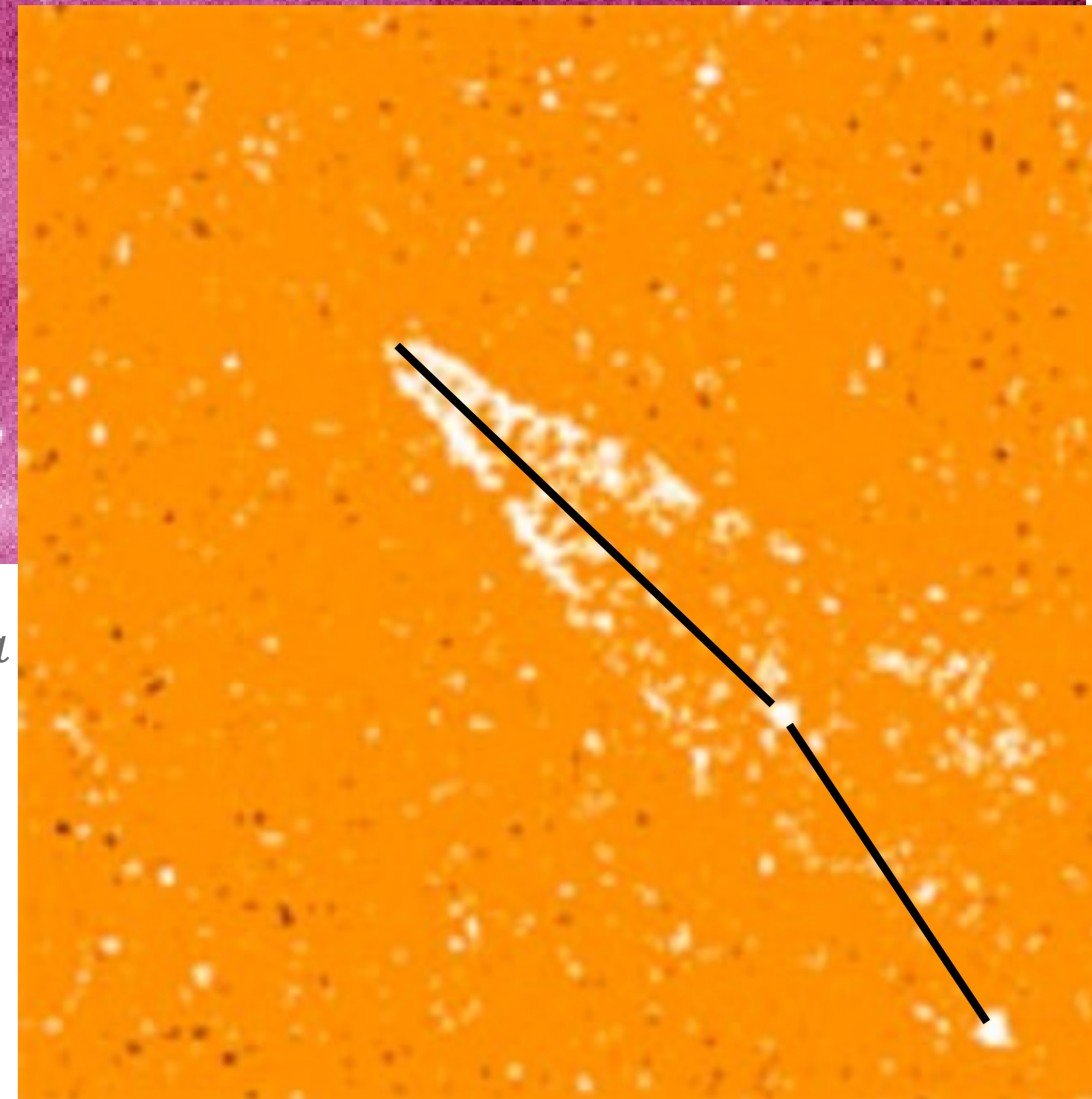
# Kick observations



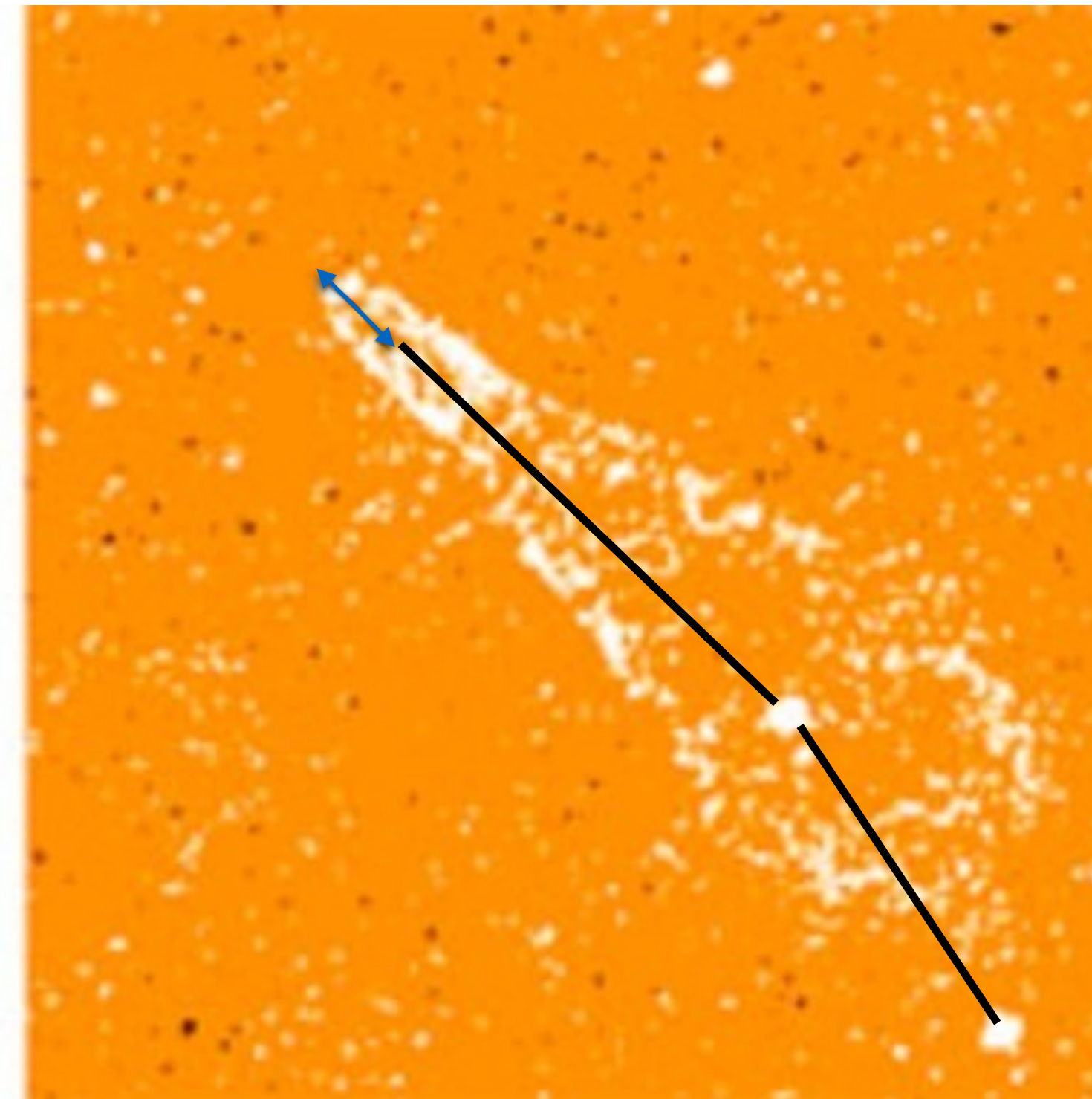
*Nebula*

[Chatterjee et al.; *Astrophys. J* (2005)]

[Hubble Space Telescope (NASA/ESA),  
Shami Chatterjee, Cornell University]



December 1994



December 2001

Neutron stars kicked out of their initial position  
with velocities  $\sim 1000$  km/s

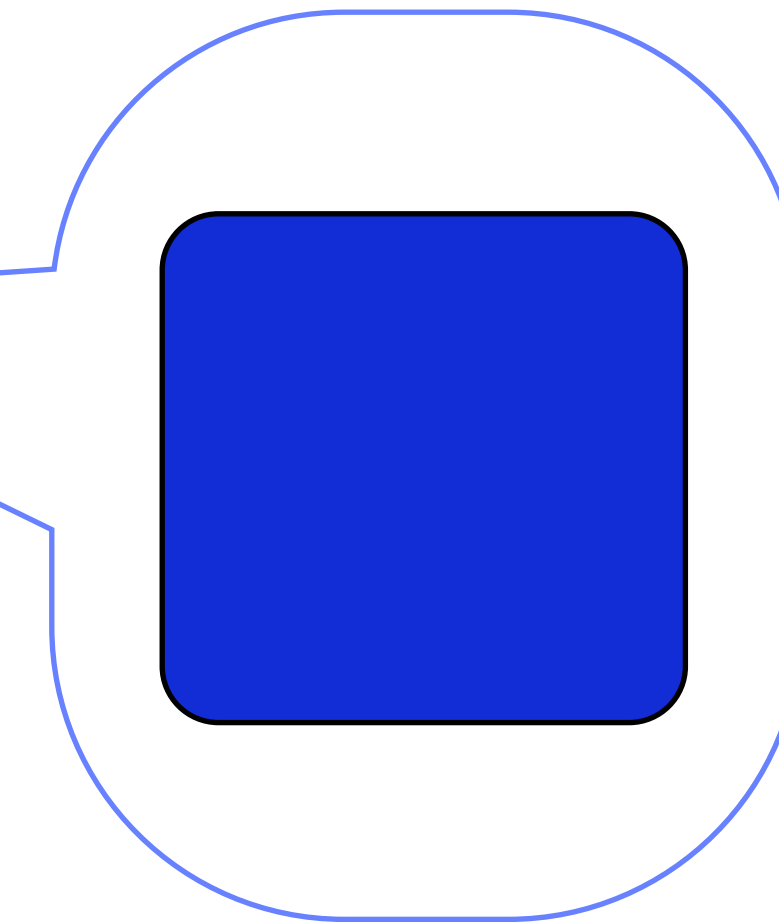
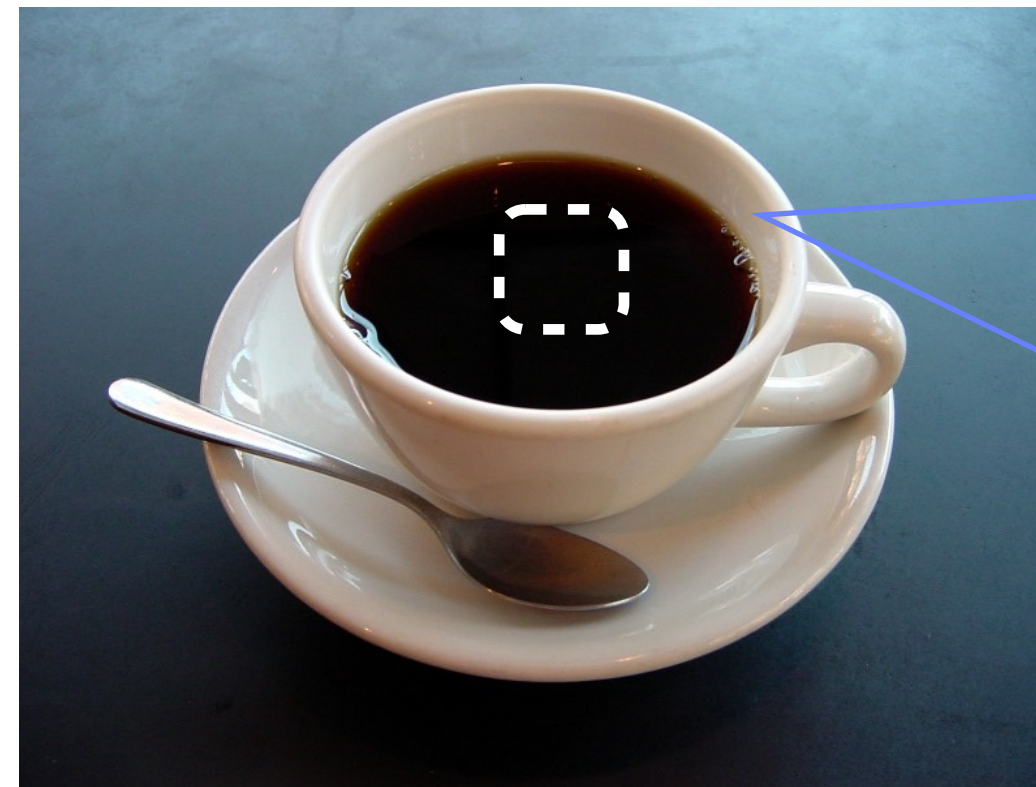


# Hydrodynamic variables

## Thermodynamics

$$T, \mu, u^\nu$$

*thermodynamic variables:  
temperature, chemical potential,  
fluid velocity*



## Hydrodynamics

$$T(t, \vec{x}), \mu(t, \vec{x}), u^\nu(t, \vec{x})$$

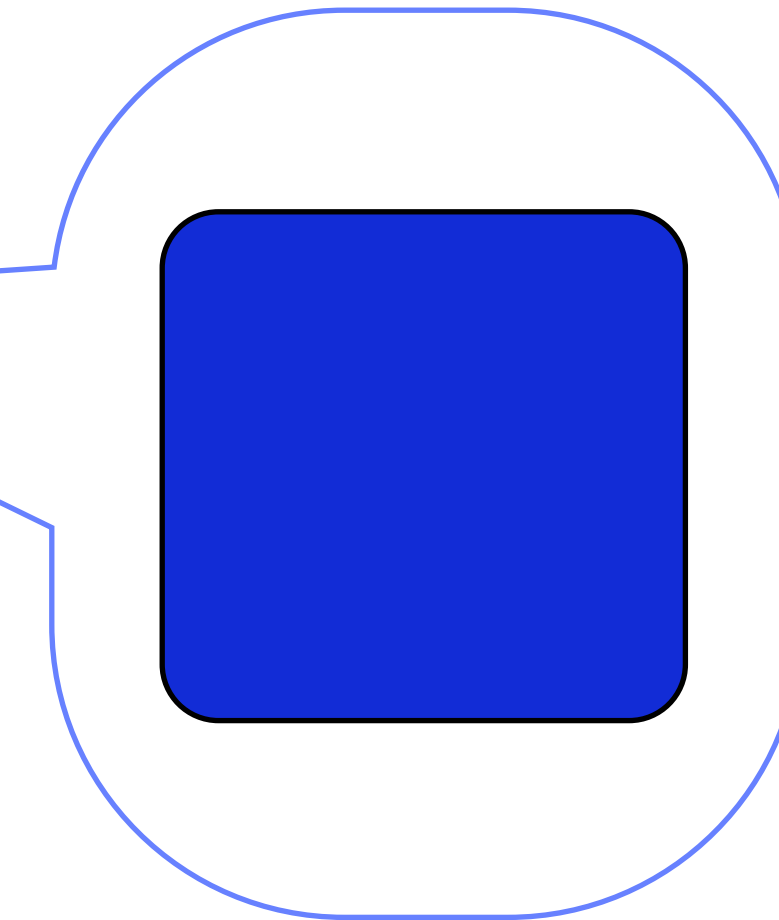
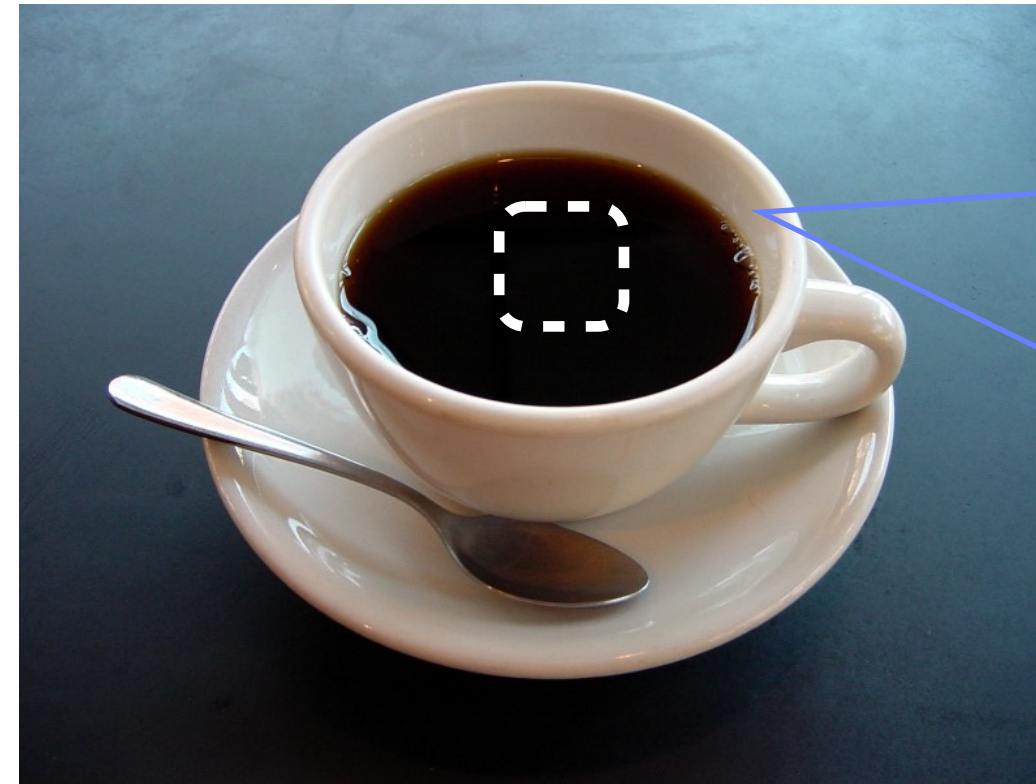


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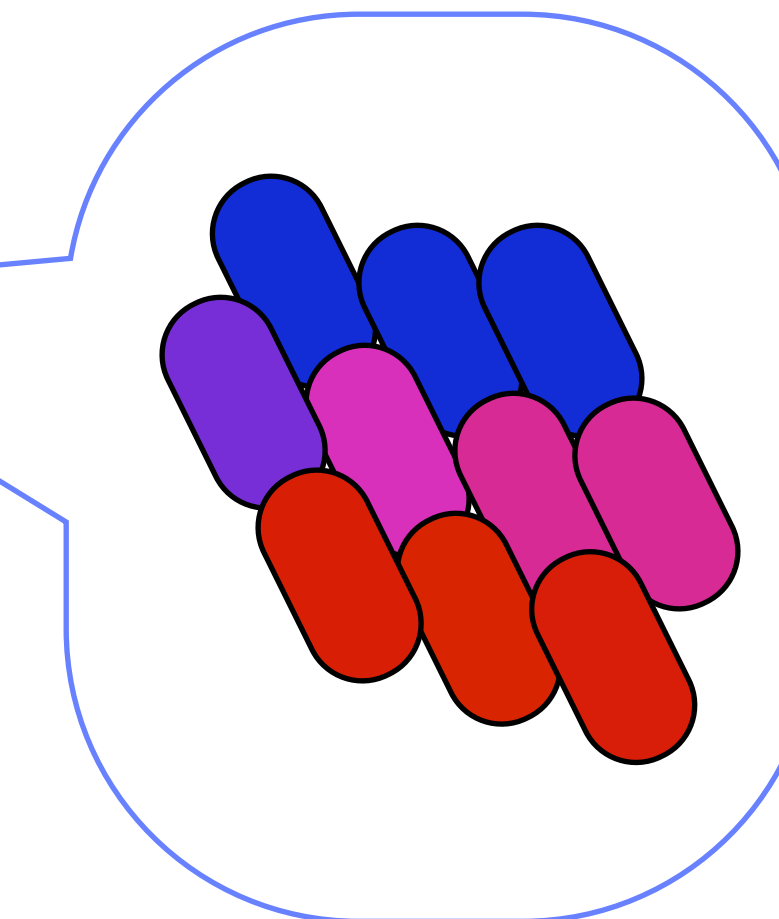
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*hydrodynamic fields  
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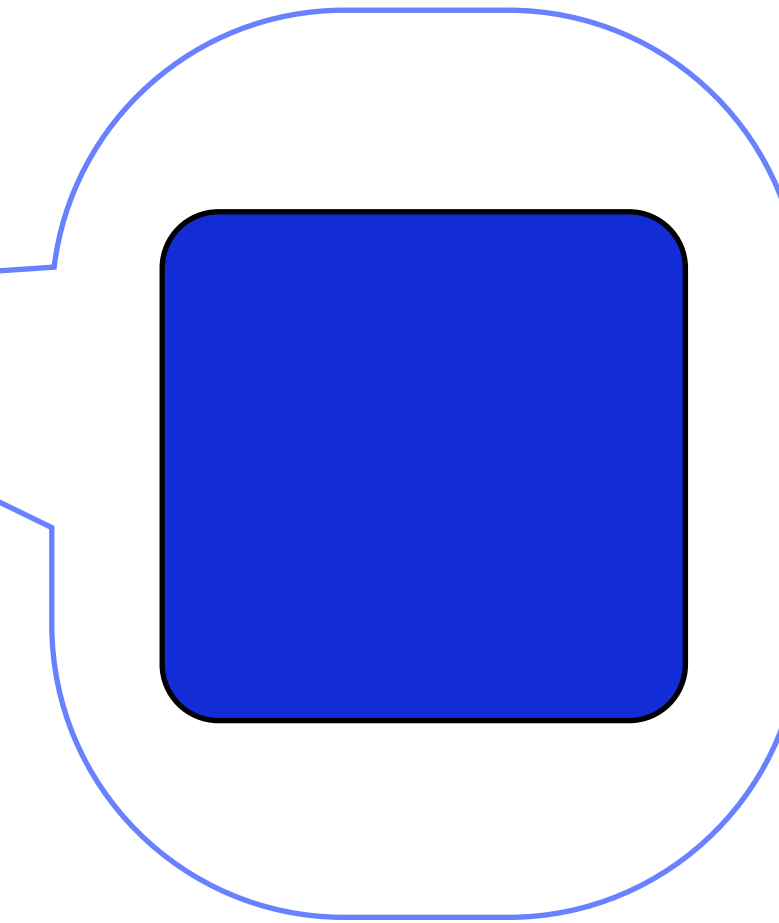
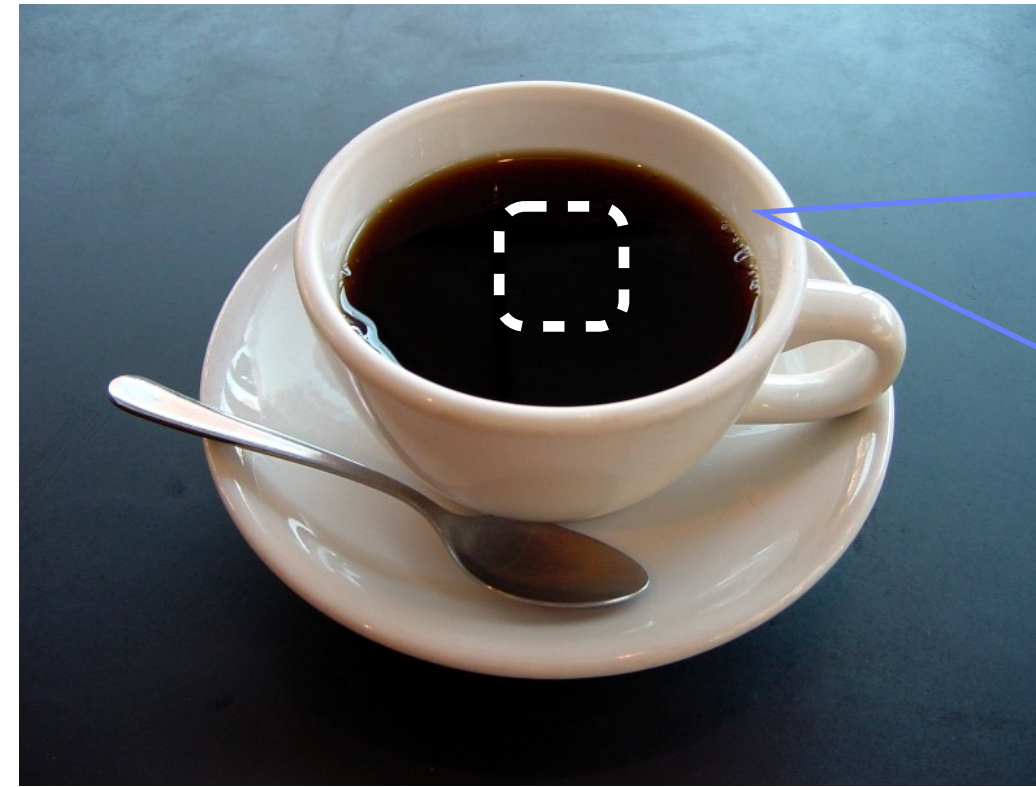


# Hydrodynamic variables

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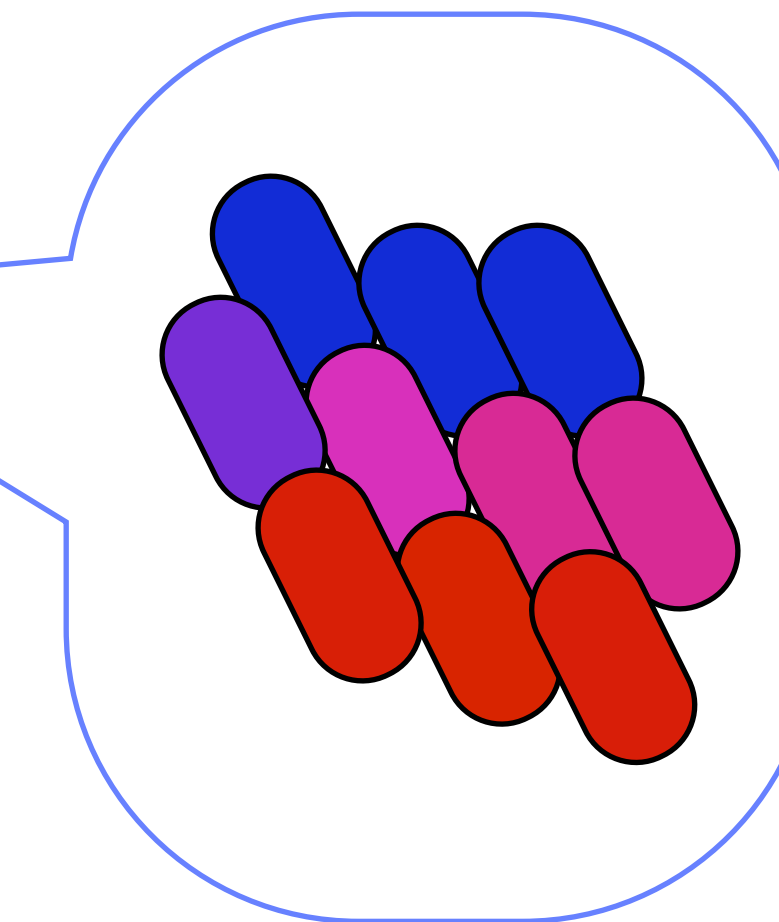
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# Hydrodynamics

effective field theory, expansion in gradients of fields

- fields  $T(x)$ ,  $\mu(x)$ ,  $u^\nu(x)$   
*temperature*      *chemical potential*      *fluid velocity*
- sources  $A_\mu(x), \dots$   
*gauge field*
- conservation equation  $\nabla_\nu j^\nu = 0$
- constitutive equation (Landau frame)





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*Conserved current*  $j^\mu = nu^\mu + \nu^\mu$   
*gradient terms*

Form can be derived and restricted from first principles.

[Landau, Lifshitz]

[Jensen, Kaminski, Kovtun, Meyer, Ritz, Yarom; PRL (2012)]

$$\nabla_{\nu} j^{\nu} = 0 \quad \text{classical theory}$$

# Chiral hydrodynamics

[Son, Surowka; PRL (2009)]

Derived for any theory with *chiral anomaly*

(e.g. the standard model  
of particle physics)

$$\nabla_{\mu} j^{\mu} = C \epsilon^{\nu\rho\sigma\lambda} F_{\nu\rho} F_{\sigma\lambda}$$

quantum theory



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quantum theory

Generalized constitutive equation with external fields:

$$j^{\mu} = n u^{\mu} + \sigma E^{\mu} + \sigma^B B^{\mu} + \sigma^V \omega^{\mu} + \dots$$

(non) conserved current   
 (ideal) charge flow   
 conductivity term   
chiral magnetic conductivity   
 . . .   
 Agrees with gauge/gravity prediction  
 [Erdmenger, Haack, Kaminski, Yarom; JHEP (2008)]  
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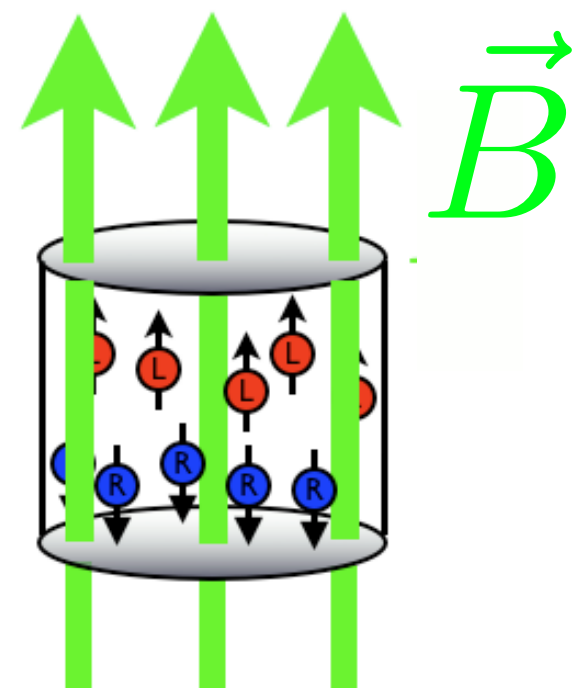
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$$\sigma^B = C \mu$$

anomaly-coefficient  $C$



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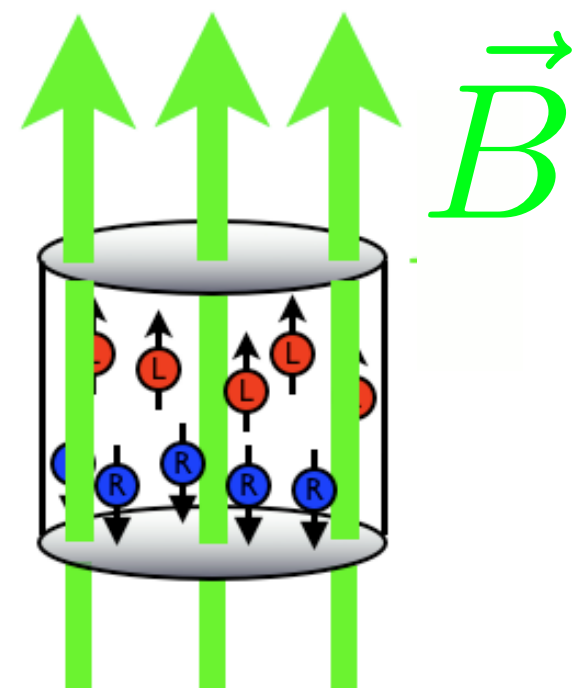
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(non) conserved current (ideal) charge flow conductivity term *chiral magnetic conductivity* *chiral vortical conductivity* . . . gravity prediction  
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Chiral magnetic conductivity:

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Measured in Weyl semi metals !

e.g. [Huang et al; PRX (2015)]  
[Landsteiner] various others ...

energy extraction ?  
neutron stars ?